

# Progress towards high-repetition-rate GeV-scale plasma-modulated plasma accelerators



UNIVERSITY OF  
**OXFORD**



Science and  
Technology  
Facilities Council

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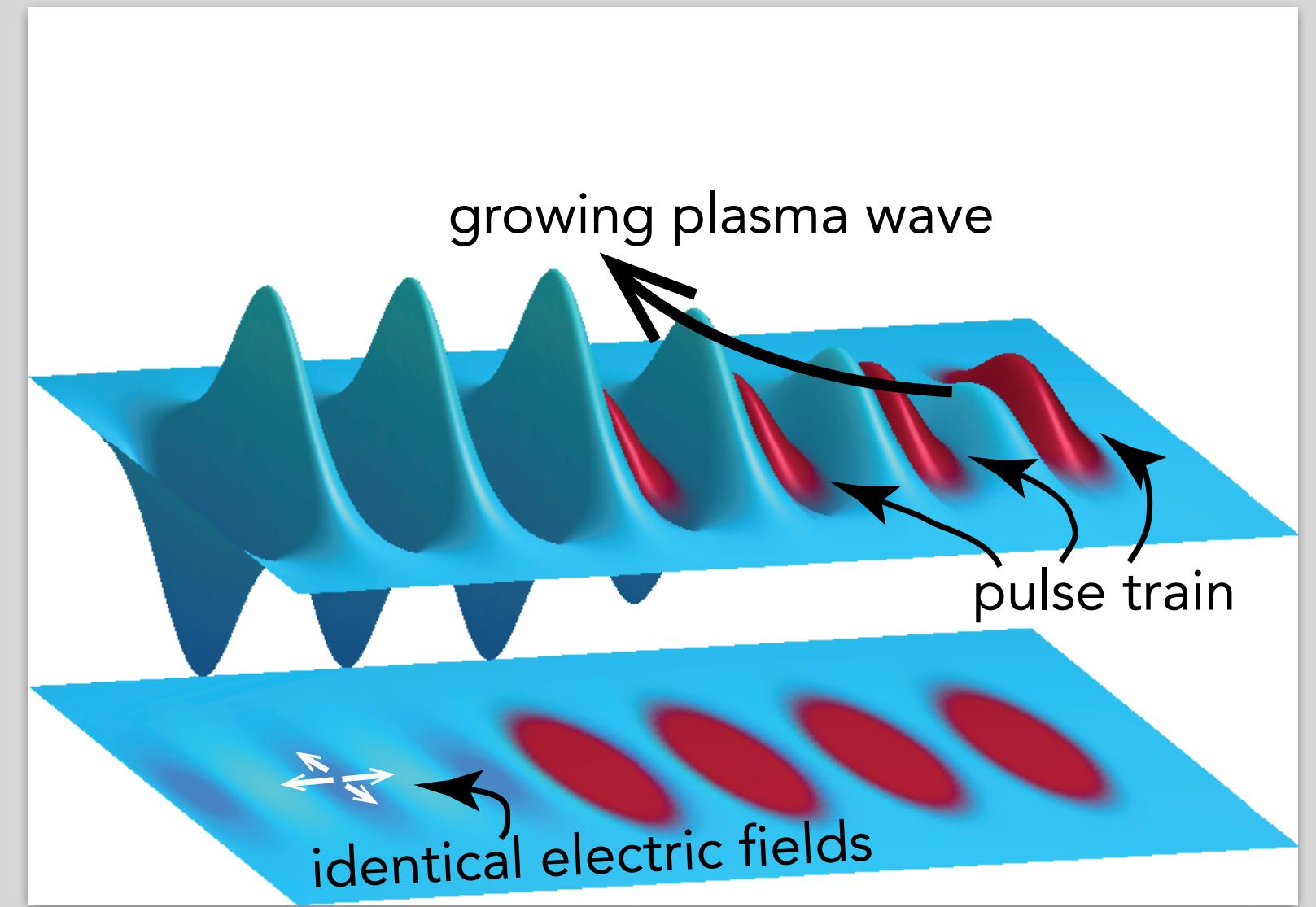
# Could we drive GeV-scale, kHz accelerators with existing lasers?

- ▶ Difficult to drive multi-GeV, multi-kHz LWFAs with Ti:sapphire owing to their low wall-plug efficiency
- ▶ Commercially-available Yb:YAG thin-disk lasers can generate  $\sim 1 \text{ J}$ ,  $\sim 1 \text{ ps}$ , 1 kHz pulses:
  - Herkommer *et al.* *Opt. Exp.* **28** 30164 (2020): 0.72 J, 0.9 ps, 1 kHz
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- ▶ Could we drive LWFAs with these lasers?



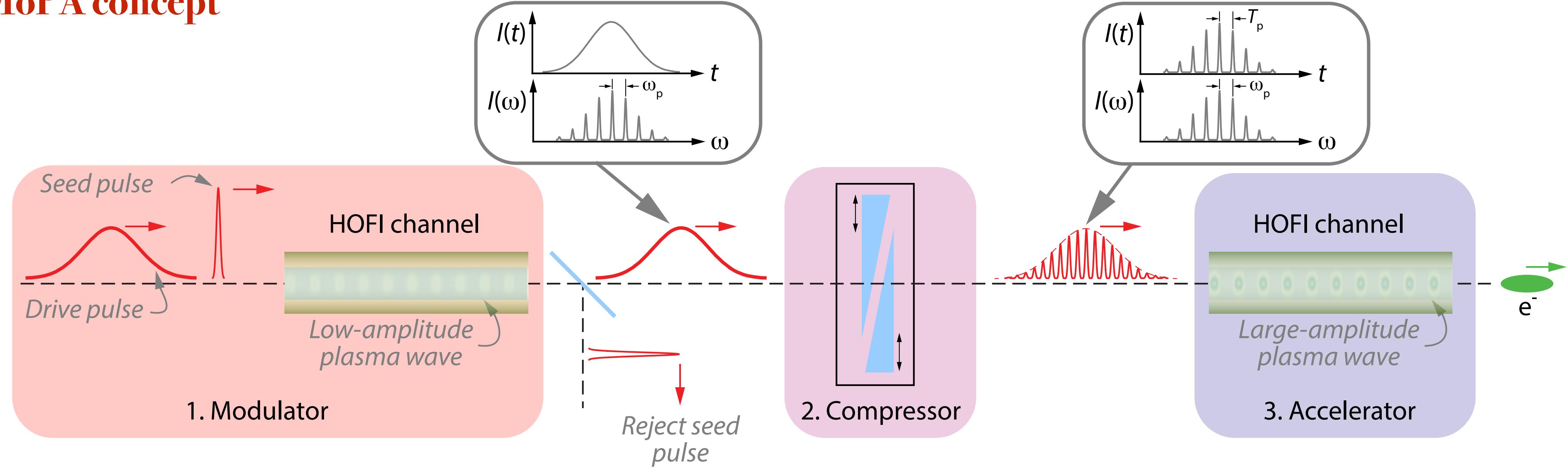
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- ▶ Could we drive LWFAs with these lasers?
  - ▶ Pulses too long to drive wake directly, but could resonantly excite wakefield if modulate pulse at plasma period
    - Many theory papers on multi-pulse published in 1990s
    - Strongly-related to plasma beat-wave accelerator (PBWA): beat two frequencies together s.t.  $\omega_1 - \omega_2 = \omega_p$



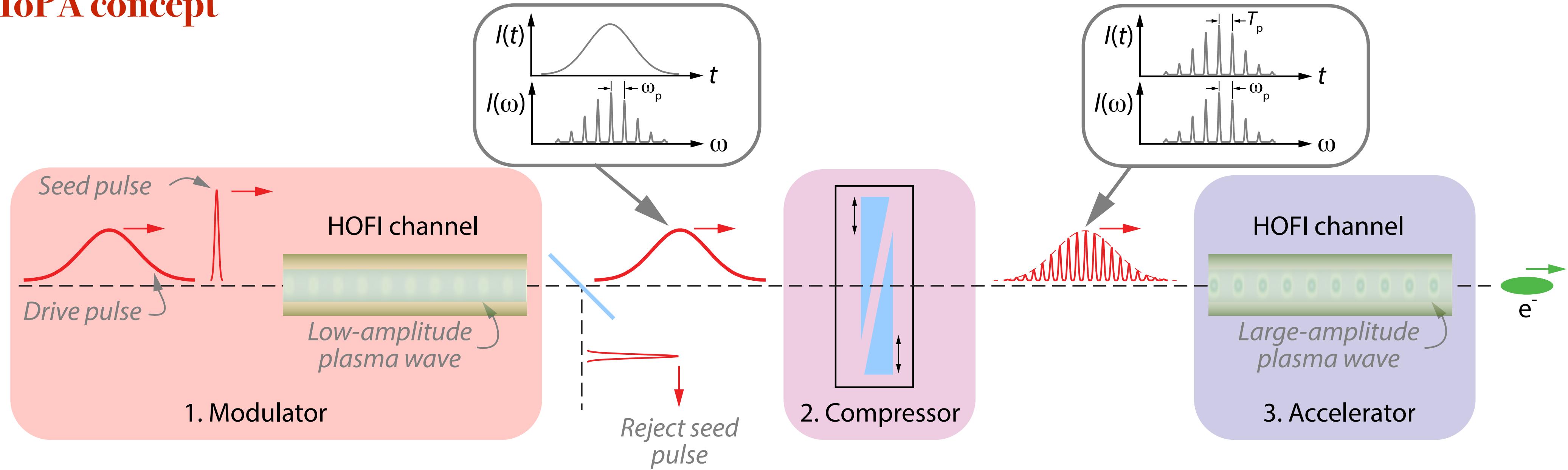
# P-MoPA: Plasma-Modulated Plasma Accelerator

## The P-MoPA concept



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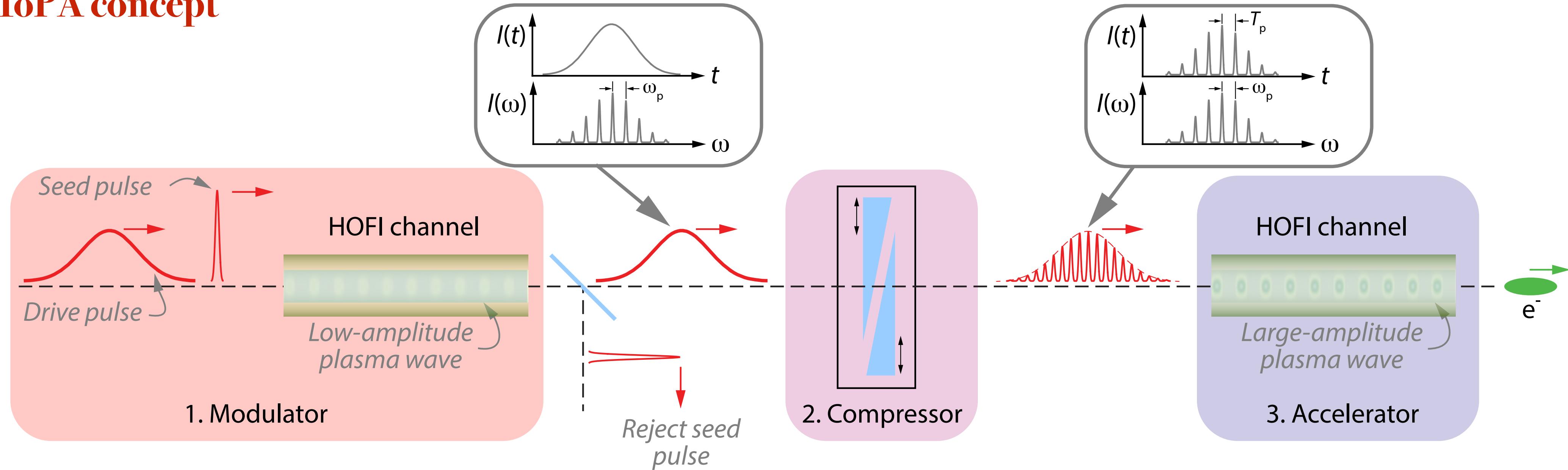


## Step 1: Modulator:

- Co-propagate long (1 ps), high-energy “drive” pulse with low-amplitude wake driven by short (< 100 fs), low-energy “seed” pulse
- Drive develops sidebands at  $\omega = \omega_0 \pm m\omega_p$

# P-MoPA: Plasma-Modulated Plasma Accelerator

## The P-MoPA concept

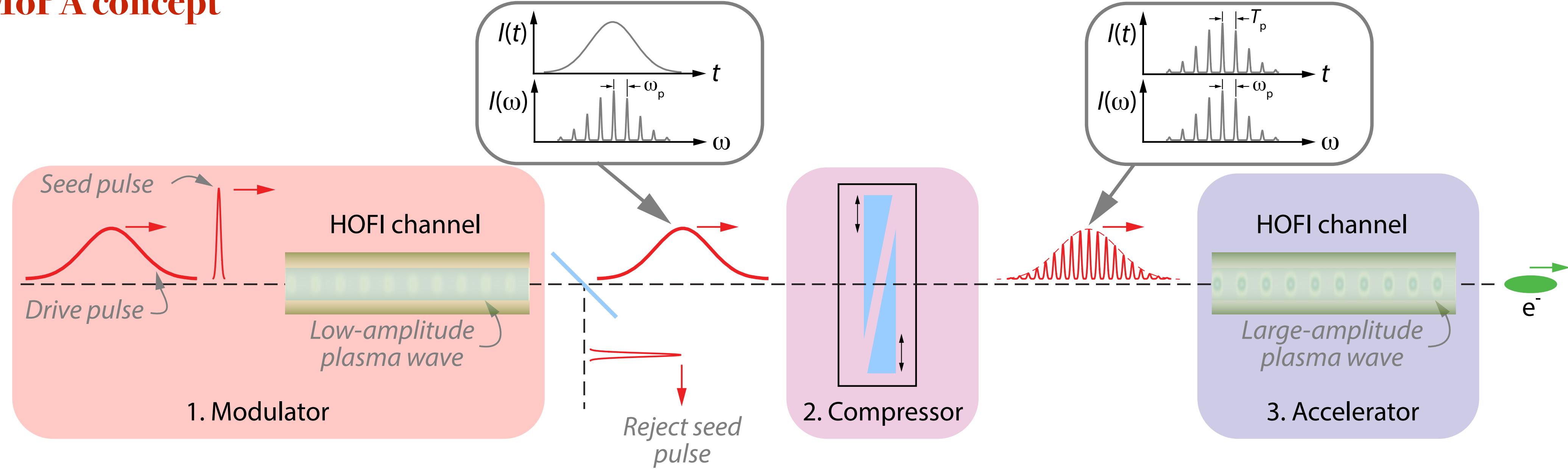


### Step 2: Compressor:

- Remove spectral phase of spectrally-modulated drive
- Forms a train of short pulses spaced by  $\Delta t = 2\pi/\omega_p$

# P-MoPA: Plasma-Modulated Plasma Accelerator

## The P-MoPA concept

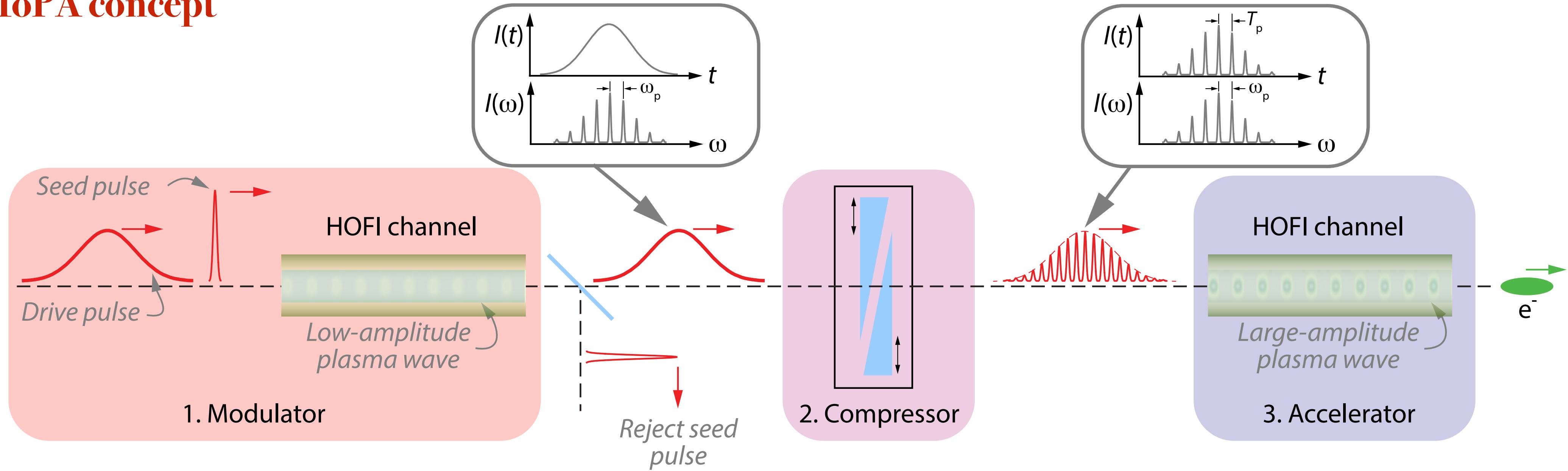


### Step 3: Accelerator:

- Train resonantly excites a large-amplitude wakefield

# P-MoPA: Plasma-Modulated Plasma Accelerator

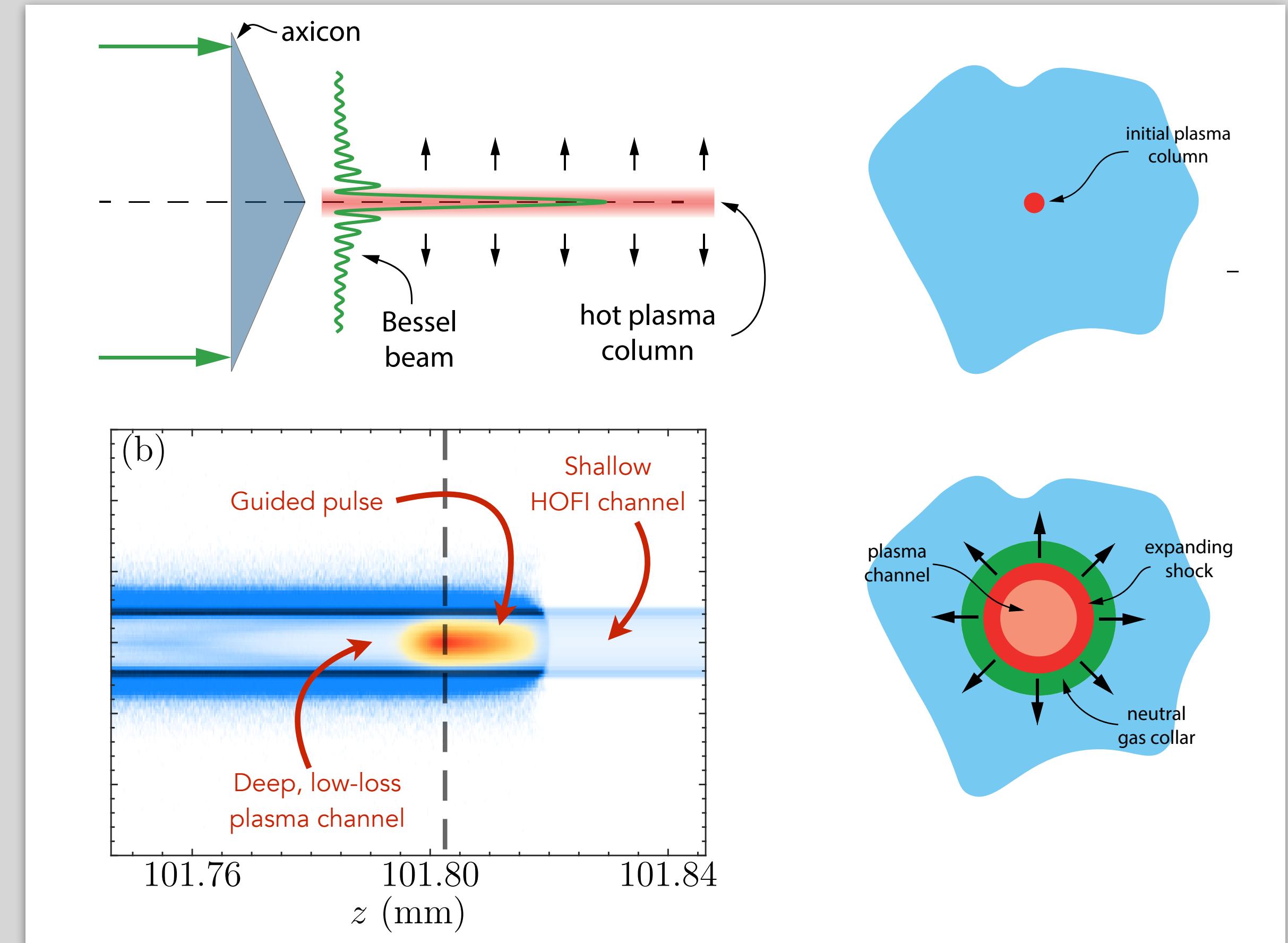
## The P-MoPA concept



# HOFI plasma channels

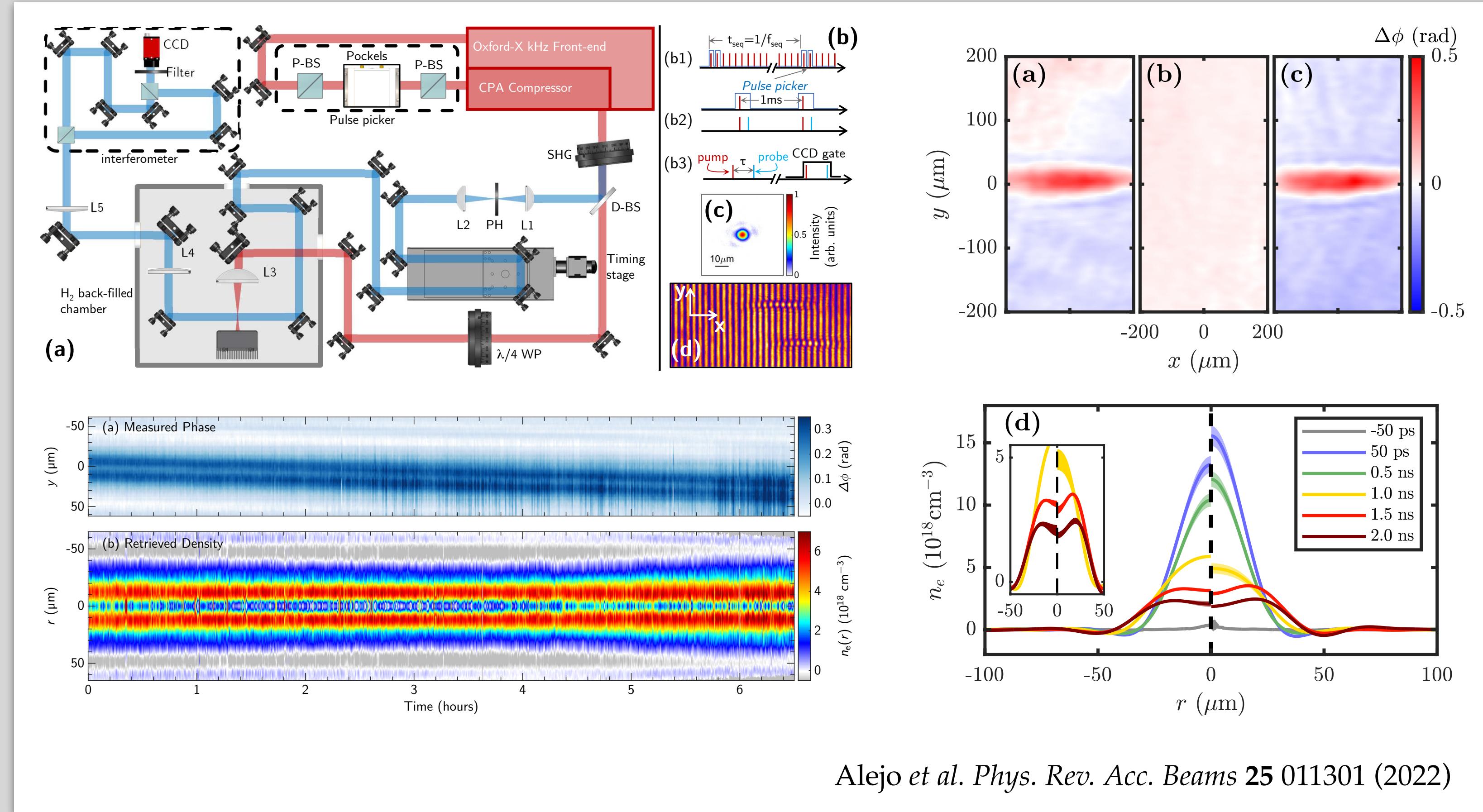
# Hydrodynamic optical-field-ionized (HOFI) plasma channels

- ▶ Channels formed by hydrodynamic expansion of collisionally-heated plasma column pioneered by Milchberg et al.
  - Free-standing & “indestructible”
  - Requires high density ( $\gtrsim 10^{18} \text{ cm}^{-3}$ ) for efficient heating
- ▶ Optical field ionization can create lower density channels ( $\lesssim 10^{17} \text{ cm}^{-3}$ )
  - Expansion  $\rightarrow$  weak channel
  - Ionization of gas collar  $\rightarrow$  deep, low loss ( $L_{\text{attn}} \gg 1 \text{ m}$ ) channels



- Durfee & Milchberg, *Phys. Rev. Lett.* **71** 2409 (1993)  
Volbeyn et al. *Phys. of Plas.* **6** 2269 (1999)  
Lemos et al., *Phys. of Plas.* **20** 063102 (2013)  
Lemos et al., *Phys. of Plas.* **20** 103109 (2013)  
Hooker et al., AAC (2016)  
Shalloo et al. *Phys. Rev. E* **97** 053203 (2018)  
Shalloo et al. *Phys. Rev. Accel. Beam* **22** 41302 (2019)
- Picksley et al. *Phys. Rev. E* **102** 053201 (2020)  
Feder et al. *Phys. Rev. Res.* **2** 043173 (2020)  
Maio et al. *Phys. Rev. Lett.* **125** 074801 (2020)  
Alejo et al. *Phys. Rev. Acc. Beams* **25** 011301 (2022)  
Shrock et al. *Phys. Rev. Lett.* **133** 045002 (2024)  
Miao et al. *Phys. Rev. Accel. Beams* **27** 081302 (2024)  
Picksley et al. *Phys. Rev. Lett.* **133** 255001 (2024)

# HOFI channels are capable of kHz repetition rates



- ▶ 2 HOFI channels generated 1 ms apart have same properties
- ▶ (short) HOFI channels generated at 0.4 kHz for 6.5 hours

# Simulations of P-MoPAs

# P-MoPA: Modulator

- ▶ Seed-driven wake modulates amplitude of drive to:

sidebands 

$$b(\zeta, \tau) \approx |b(\zeta, 0)| \sum_{m=-\infty}^{\infty} i^m J_m(-\beta) \exp[im(\omega_{p0}\tau + \Delta\phi')]$$

$$\beta = 2 \frac{\omega_{p0}^2}{8\omega_L} \frac{\delta n_e}{n_{e0}} \frac{L_{\text{mod}}}{v_{g,\text{mod}}} \quad \text{modulator parameter}$$



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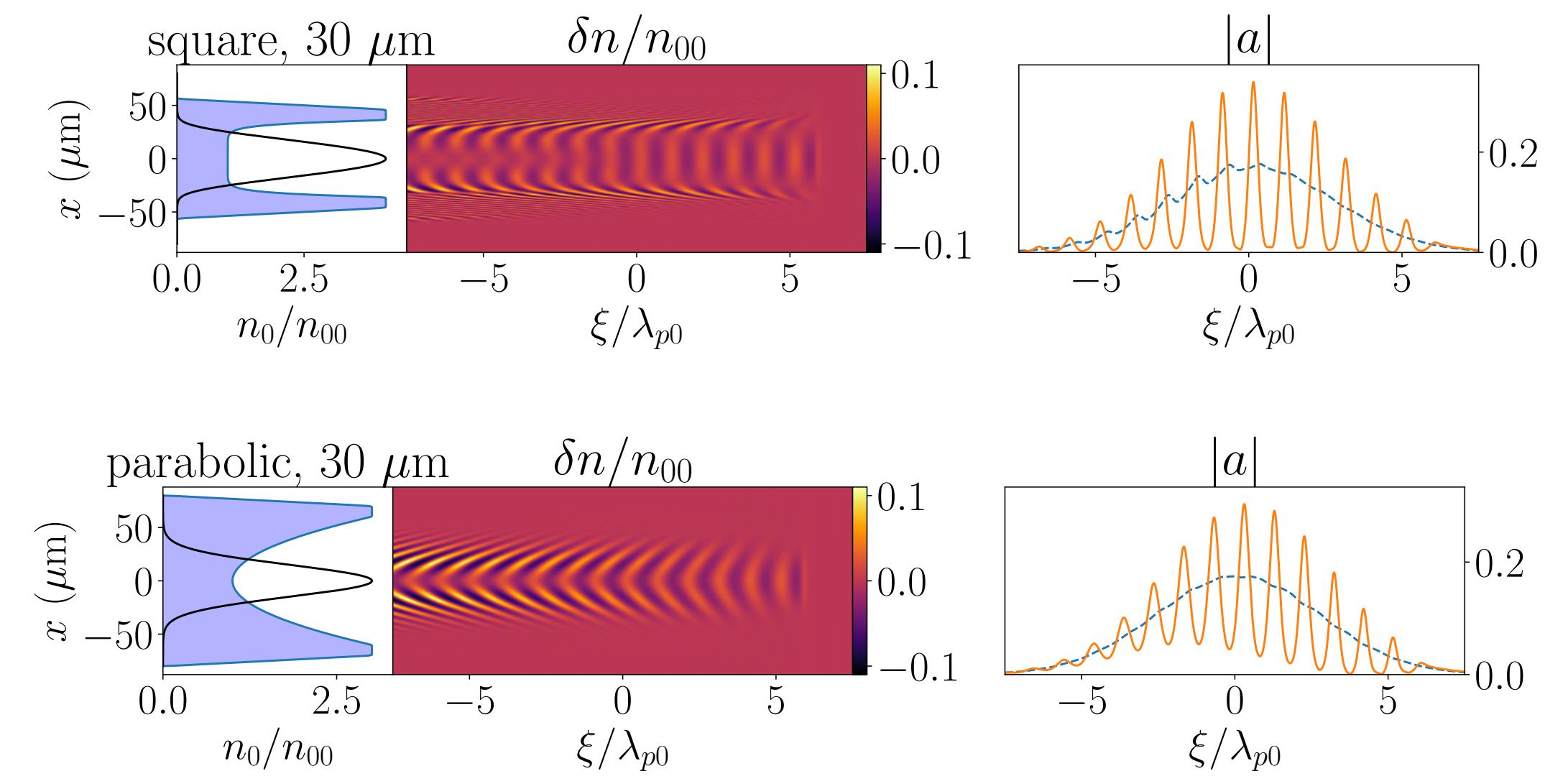
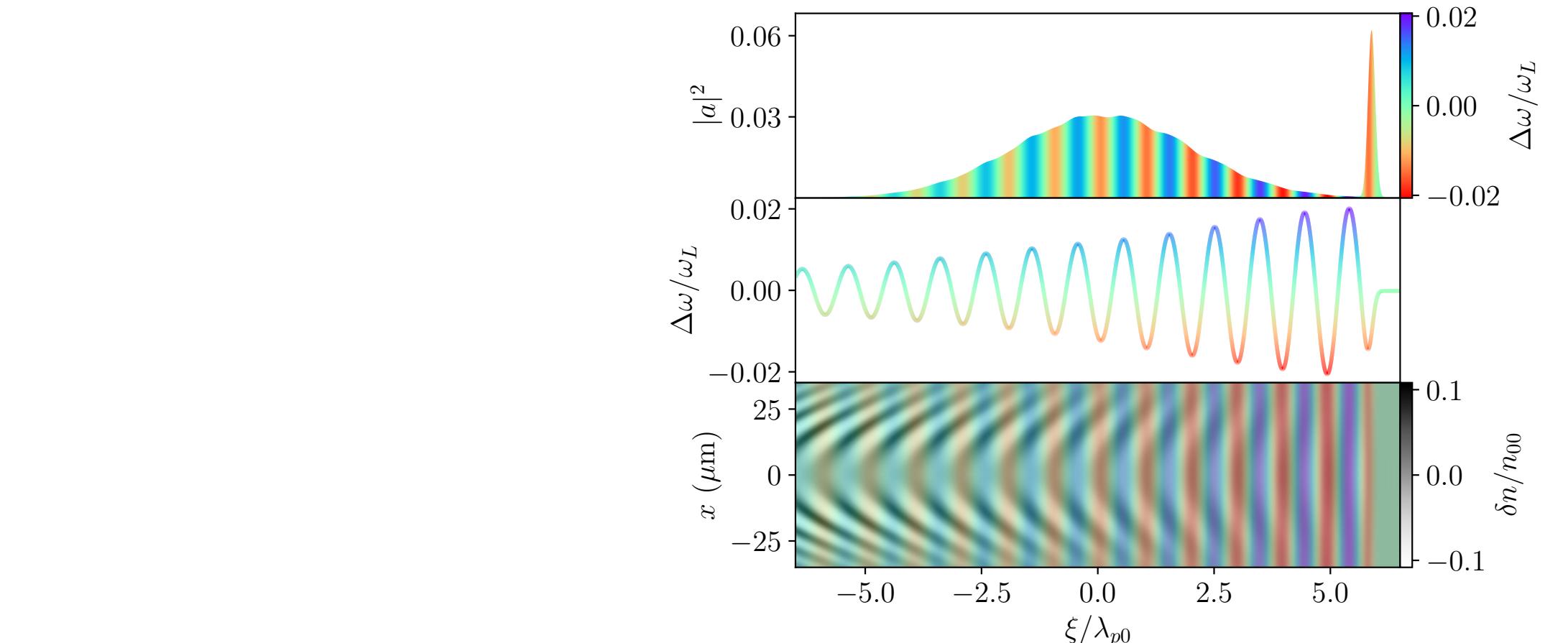
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- ▶ 3D fluid theory shows:
  - Spectral modulation is a radial average  $\Rightarrow$  independent of radial position
  - Curvature of wake reduces modulation
  - Stable operation possible over wide range of parameters

Jakobsson *et al.* *Phys. Rev. Lett.* **127** 184801 (2021)  
 van de Wetering *et al.* *Phys. Rev. E* **108** 015204 (2023)



# P-MoPA: Compressor

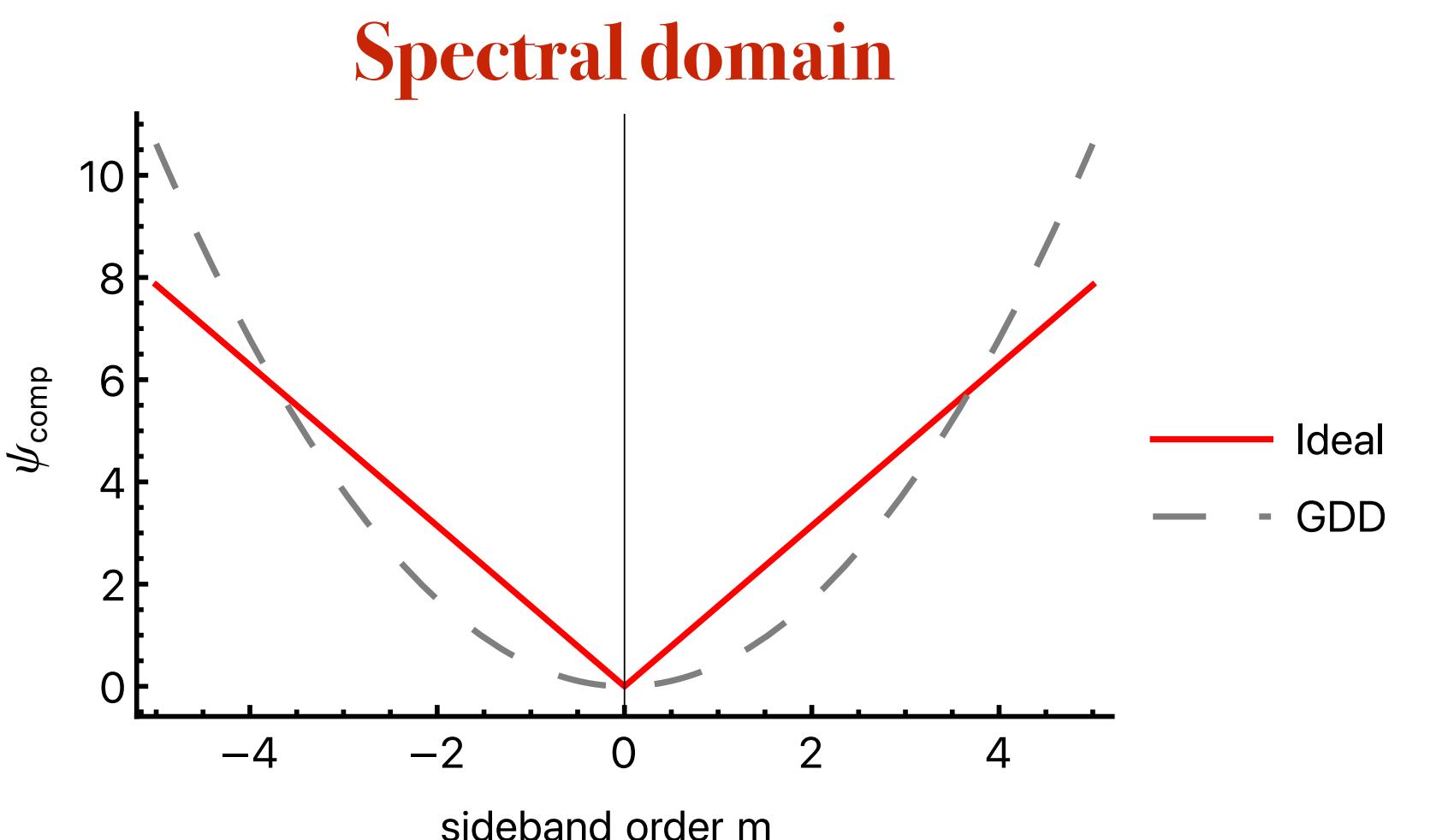
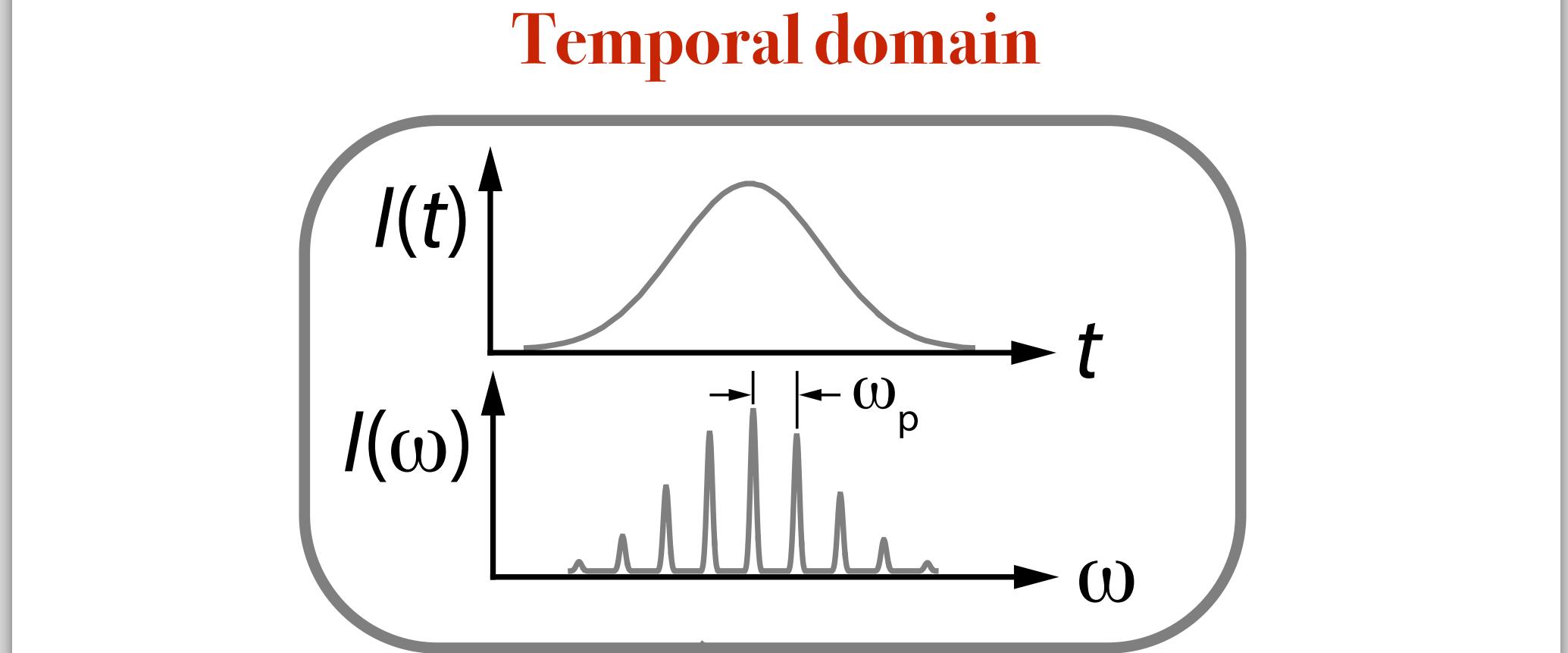
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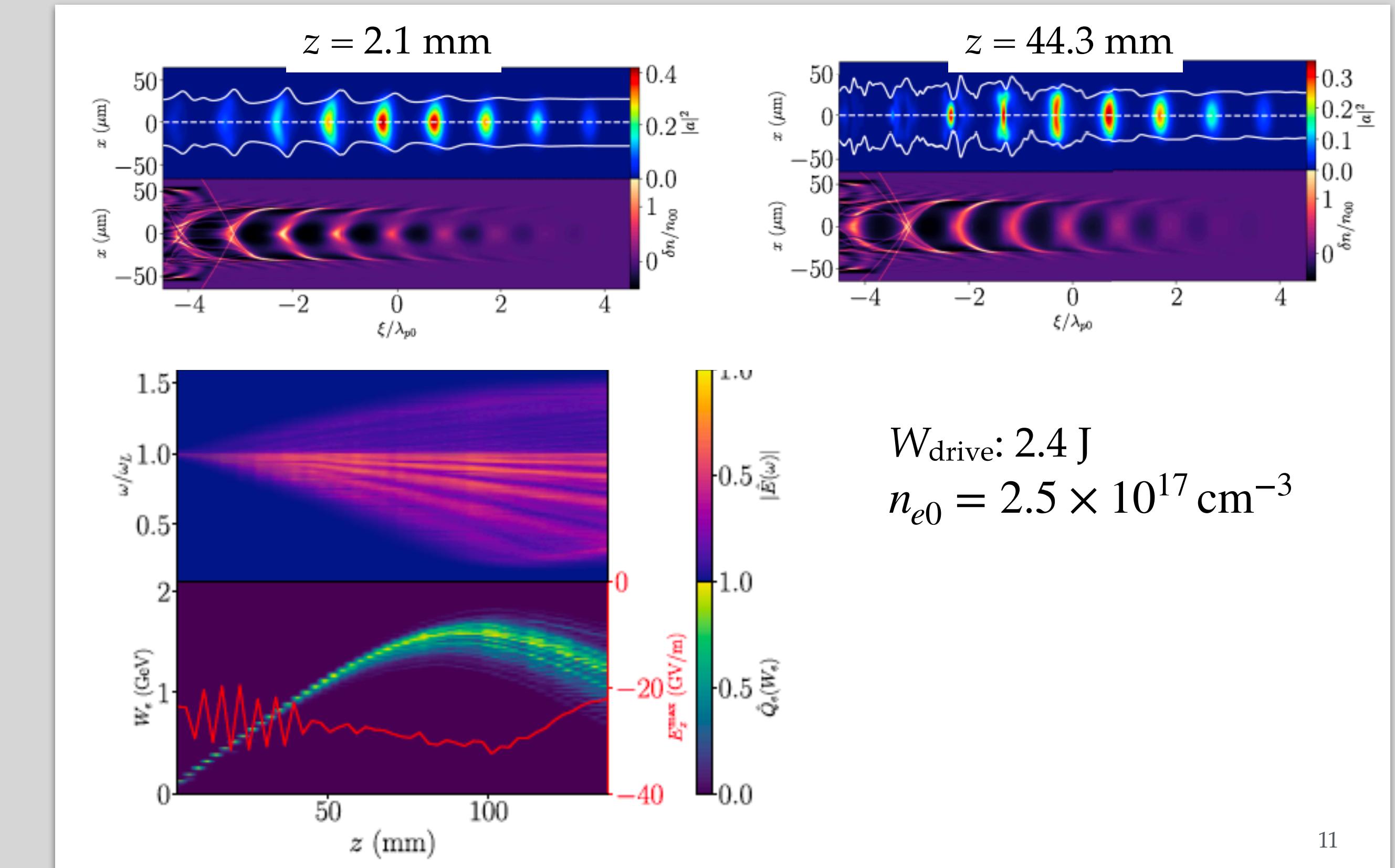
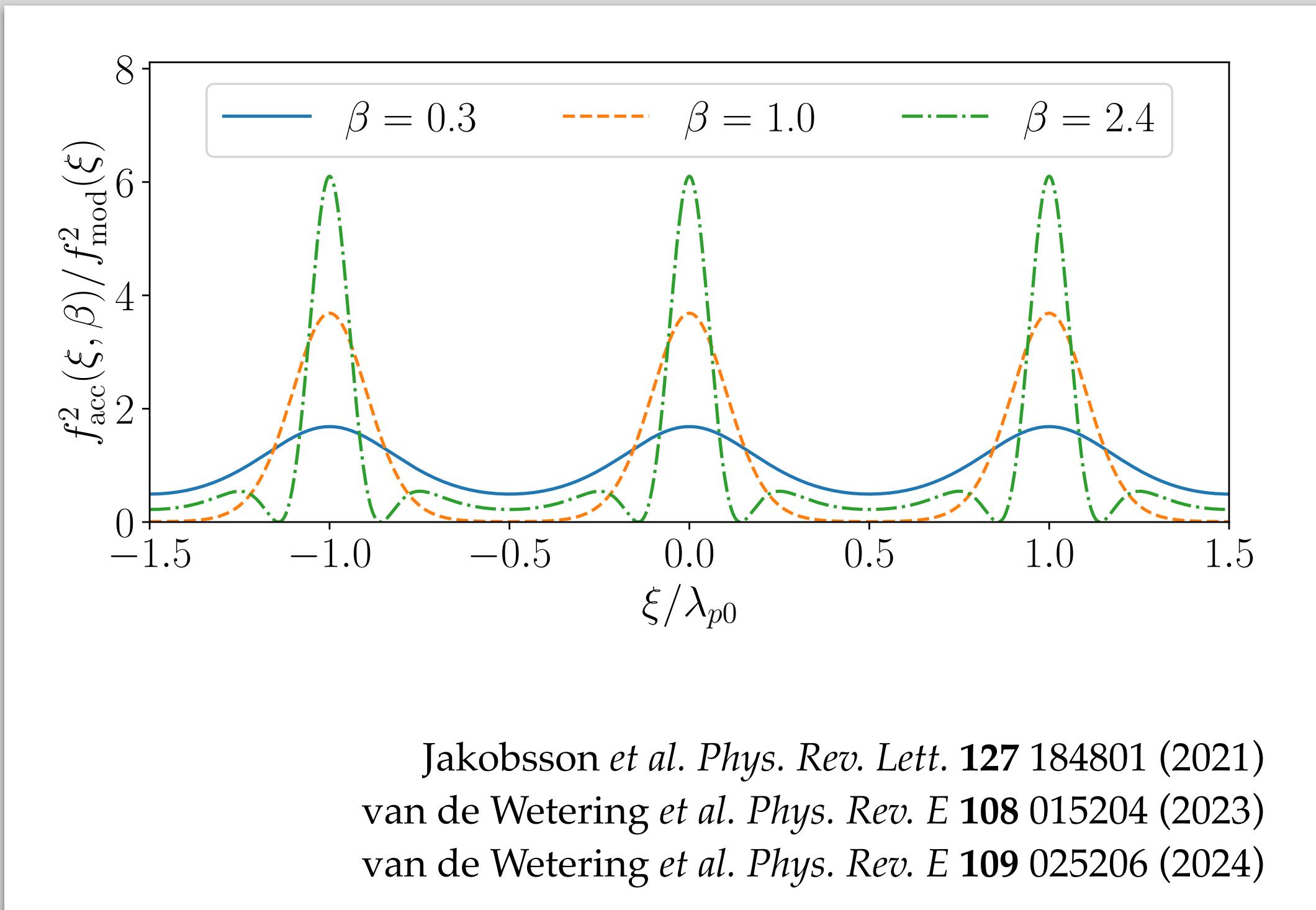
Spectralphase :  $\psi_m \approx -|m|\frac{\pi}{2}$

Jakobsson *et al.* *Phys. Rev. Lett.* **127** 184801 (2021)  
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# P-MoPA: Accelerator

- Modulator parameter  $\beta$  controls temporal profile of pulse train
  - For  $\beta_{\text{opt}} \approx 1.43$ , wake 72% larger than PBWA with same pulse energy
  - Can drive wakes with  $\sim 50\%$   $E_{\text{wb}}$



# Demonstration of Step 3 : Resonant wakefield excitation in a plasma channel

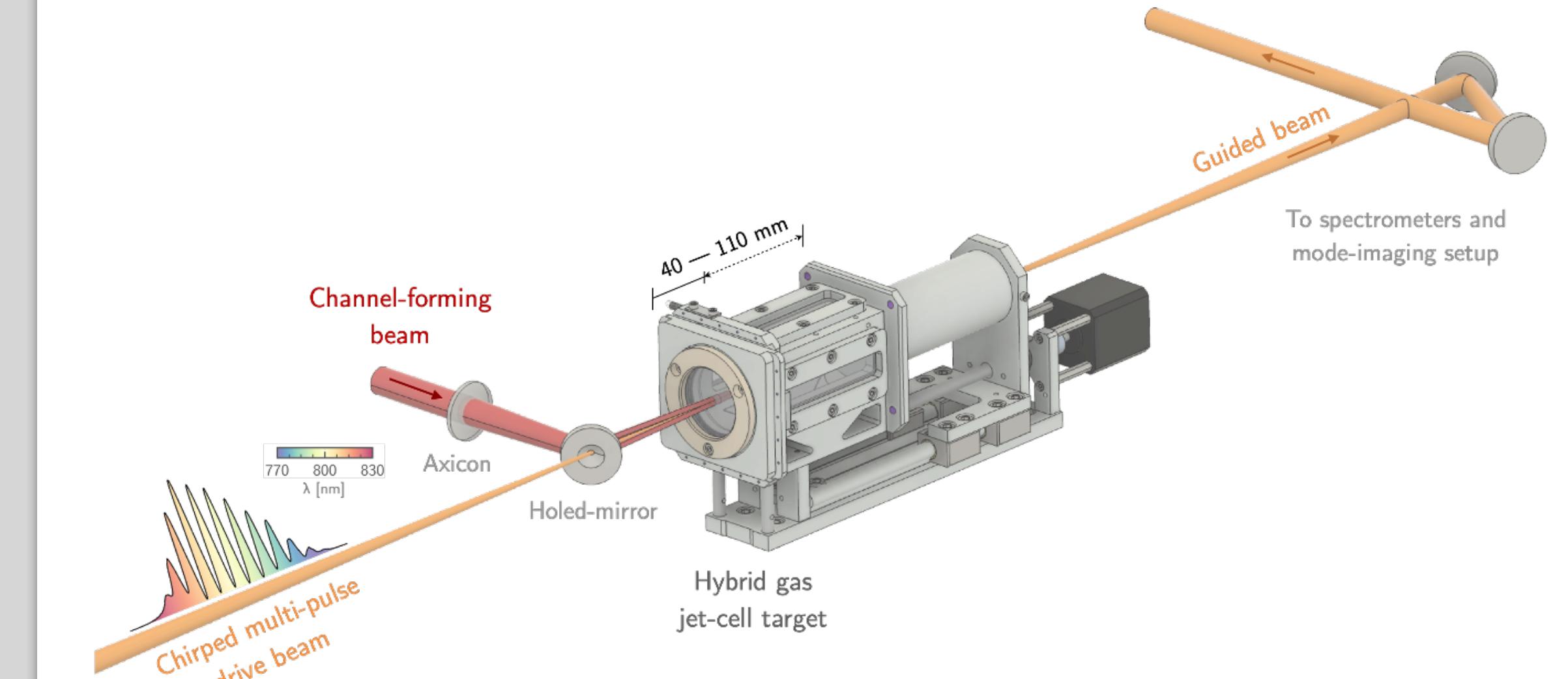
# Experimental set-up

## ► Objectives

- Demonstrate guiding of joule-scale pulse trains in  $\sim 100$  mm long HOFI channels
- Demonstrate resonant excitation of wakefield

Astra-Gemini Laser, RAL

Ross *et al.* *Phys. Rev. Res.* **6** L022001 (2024)



### Pulse train

$$\begin{aligned}E &= (2.5 \pm 0.5) \text{ J} \\w_0 &= (45.5 \pm 3.4) \mu\text{m} \\z_R &= (7.9 \pm 0.7) \text{ mm}\end{aligned}$$

### Channel-forming beam

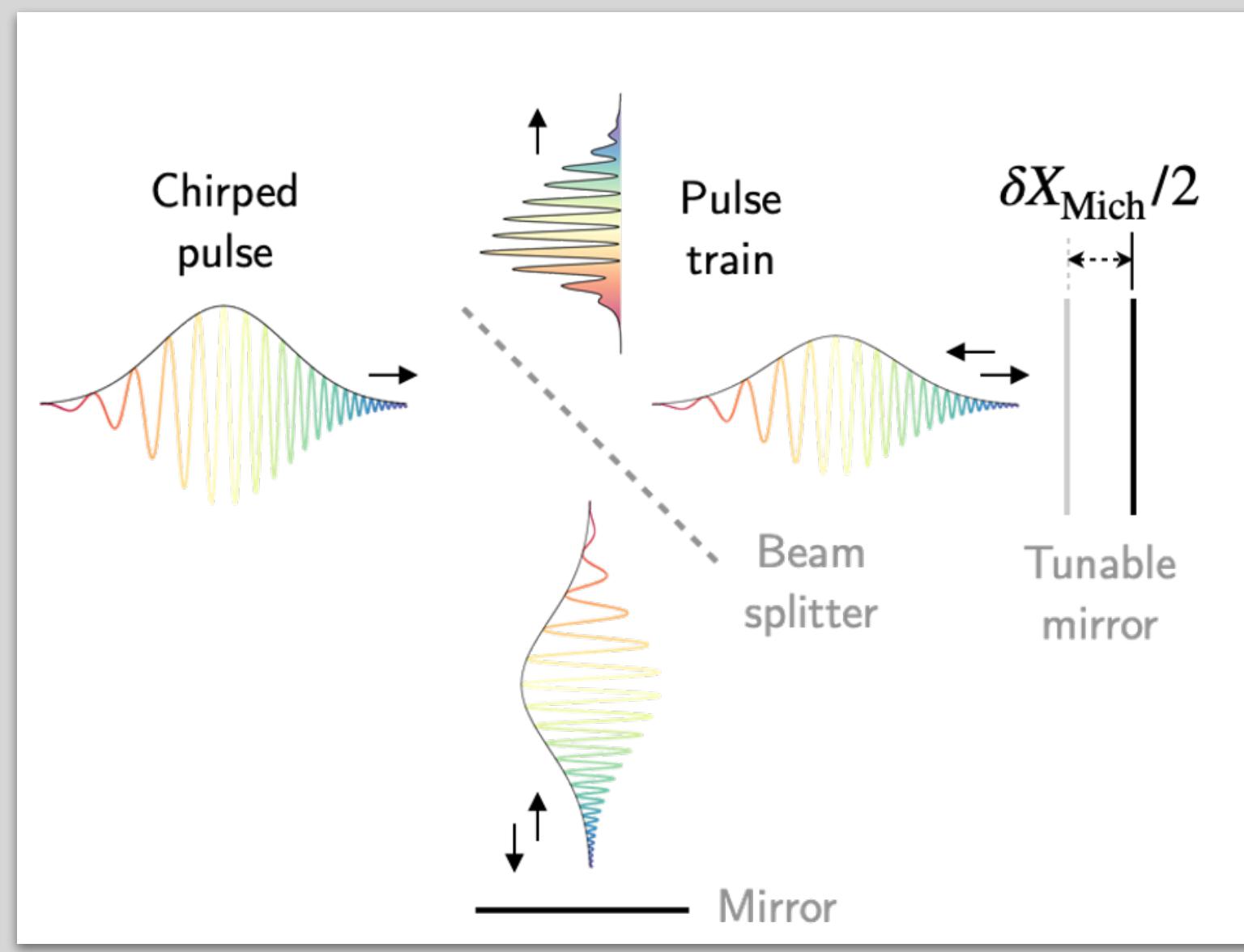
$$\begin{aligned}\tau &= 80 \text{ fs} \\E &\sim 100 \text{ mJ} \\\theta_{\text{base}}^{\text{axicon}} &= 3.6^\circ\end{aligned}$$



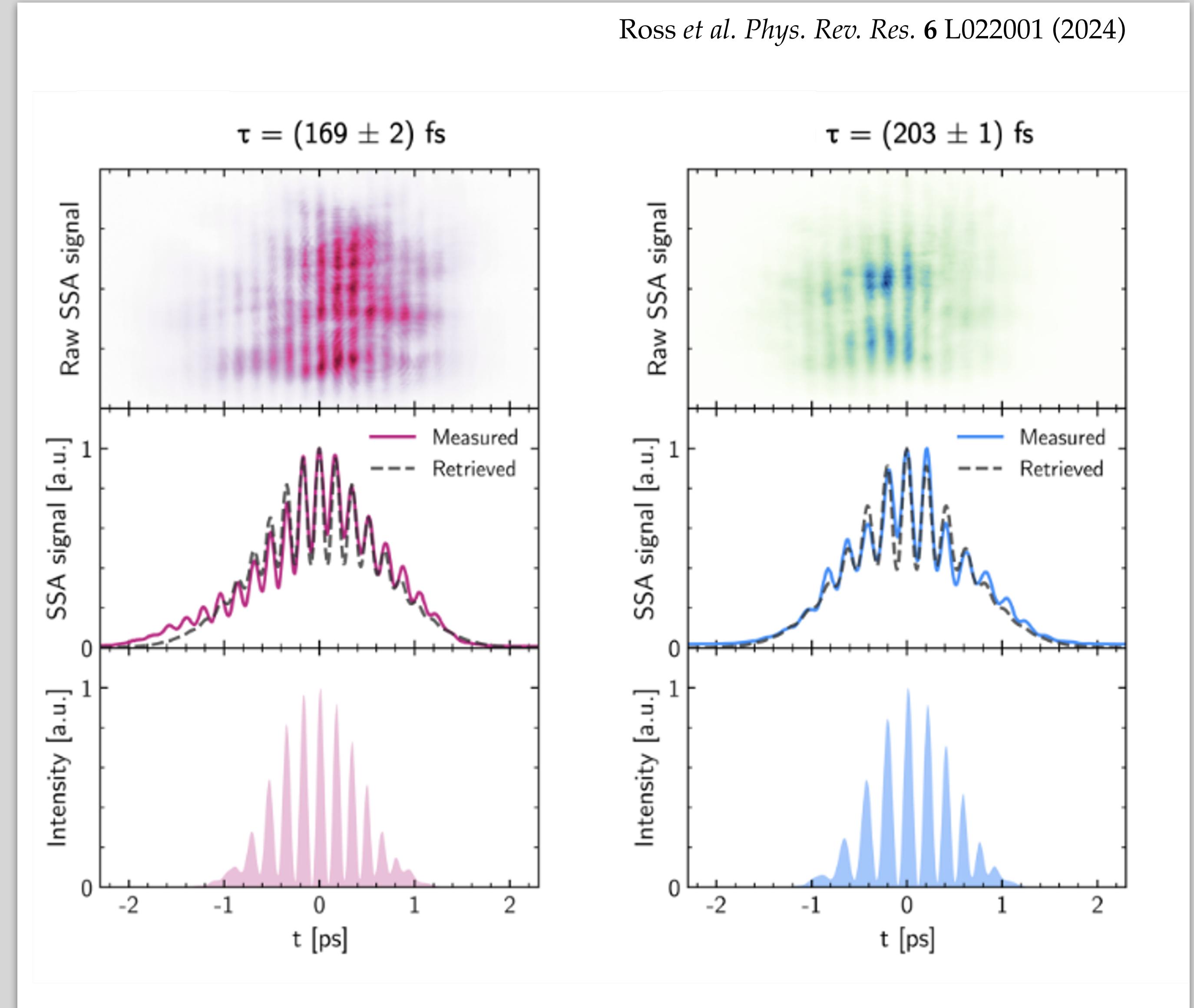
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13 - 19 April 2025

# Generation of “dummy” pulse trains

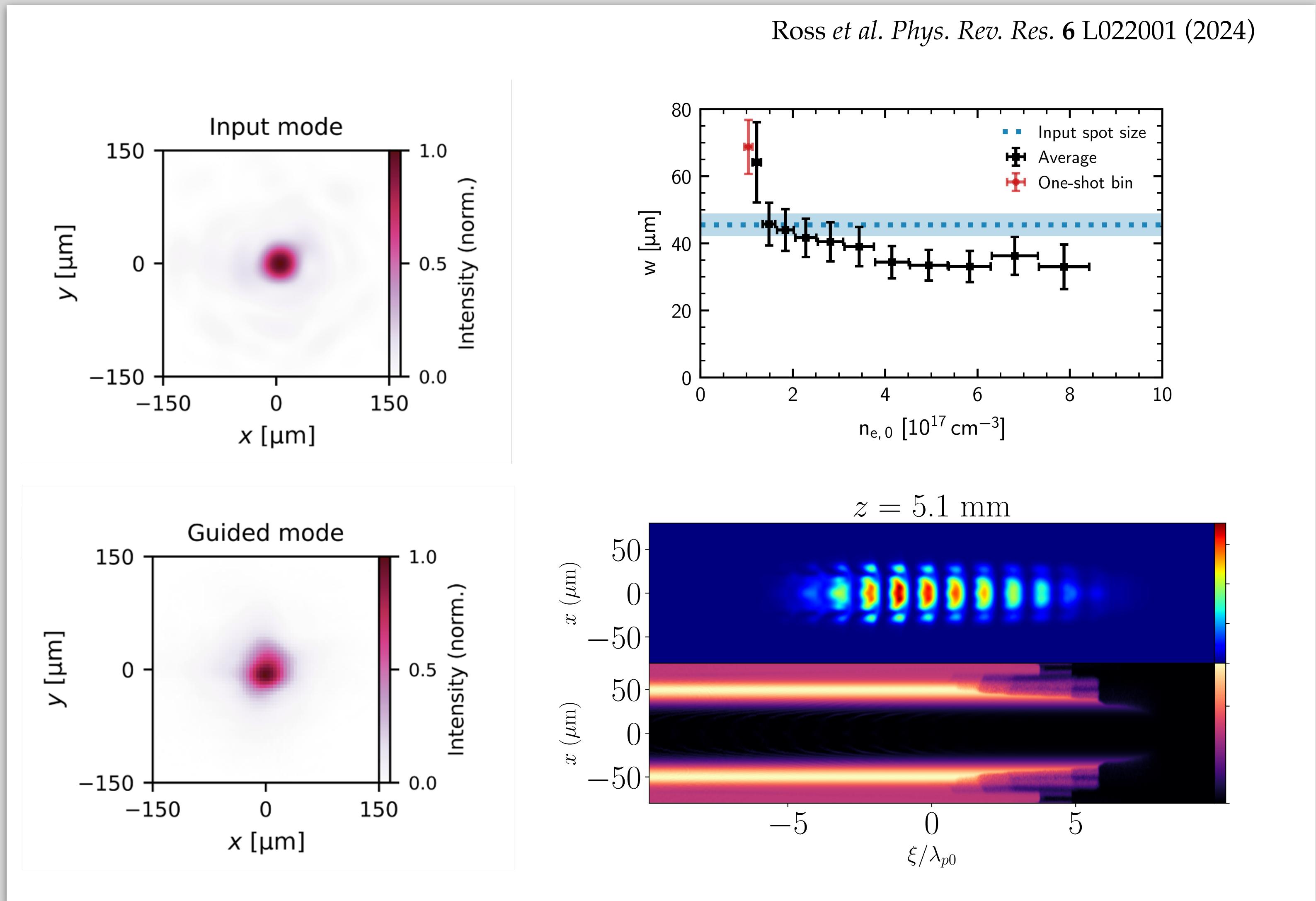


- ▶ Pulse train generated by:
  - Chirping Gemini pulse to  $\sim 1$  ps
  - Filtering chirped pulse with Michelson interferometer
- ▶ Trains characterized by;
  - Measuring spectrum
  - SSA
  - Use Dazzler to compensate for TOD



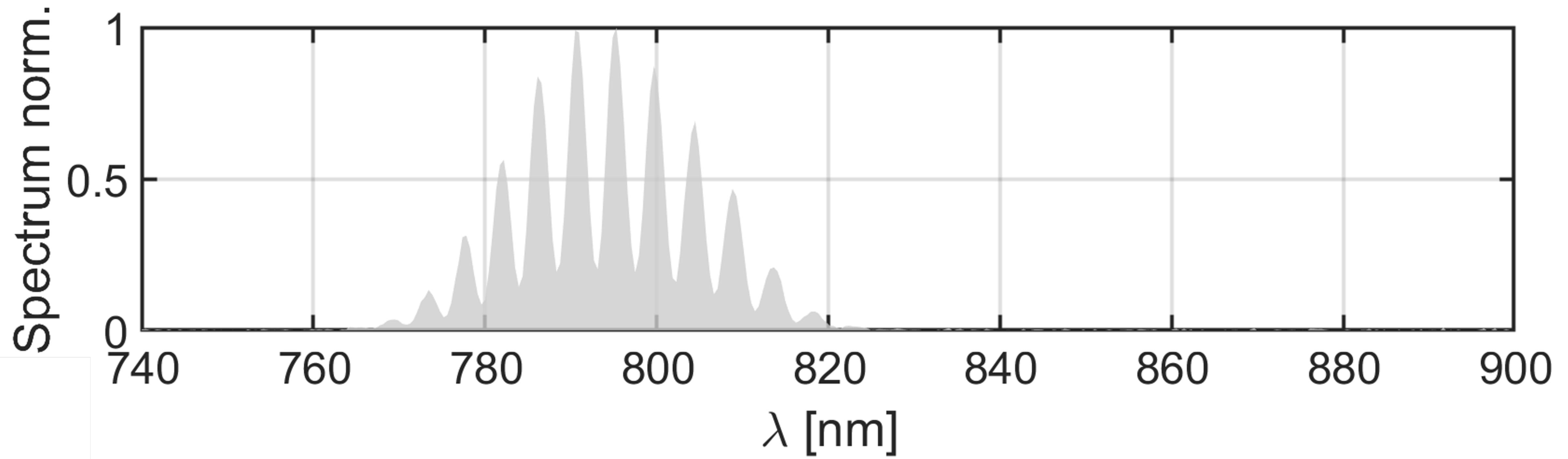
# Joule-scale pulse trains can be guided in a HOFI channel

- ▶ Joule-scale pulse trains guided over 110 mm ( $\sim 17 z_R$ )
- ▶ Input spot  $\sim 70\%$  overlap with lowest-order mode
- ▶ PIC simulations confirm that first few pulses condition the HOFI channel



# Pulse train spectra show resonant excitation ...

Ross *et al.* *Phys. Rev. Res.* **6** L022001 (2024)

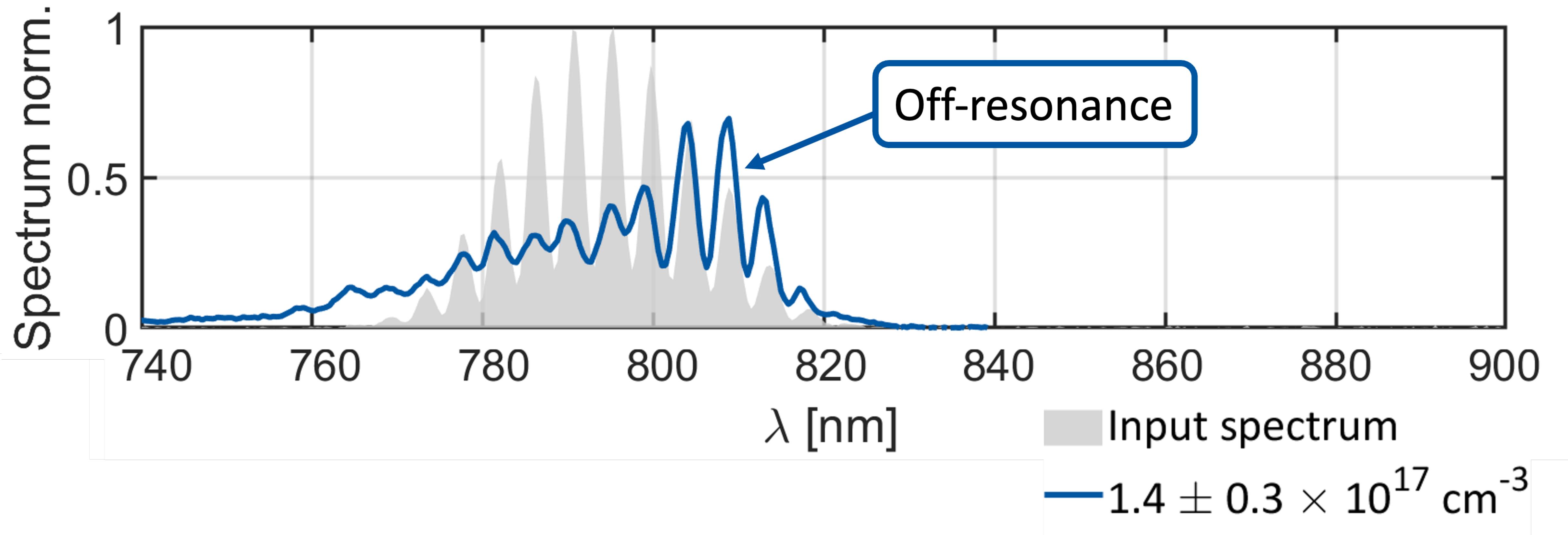


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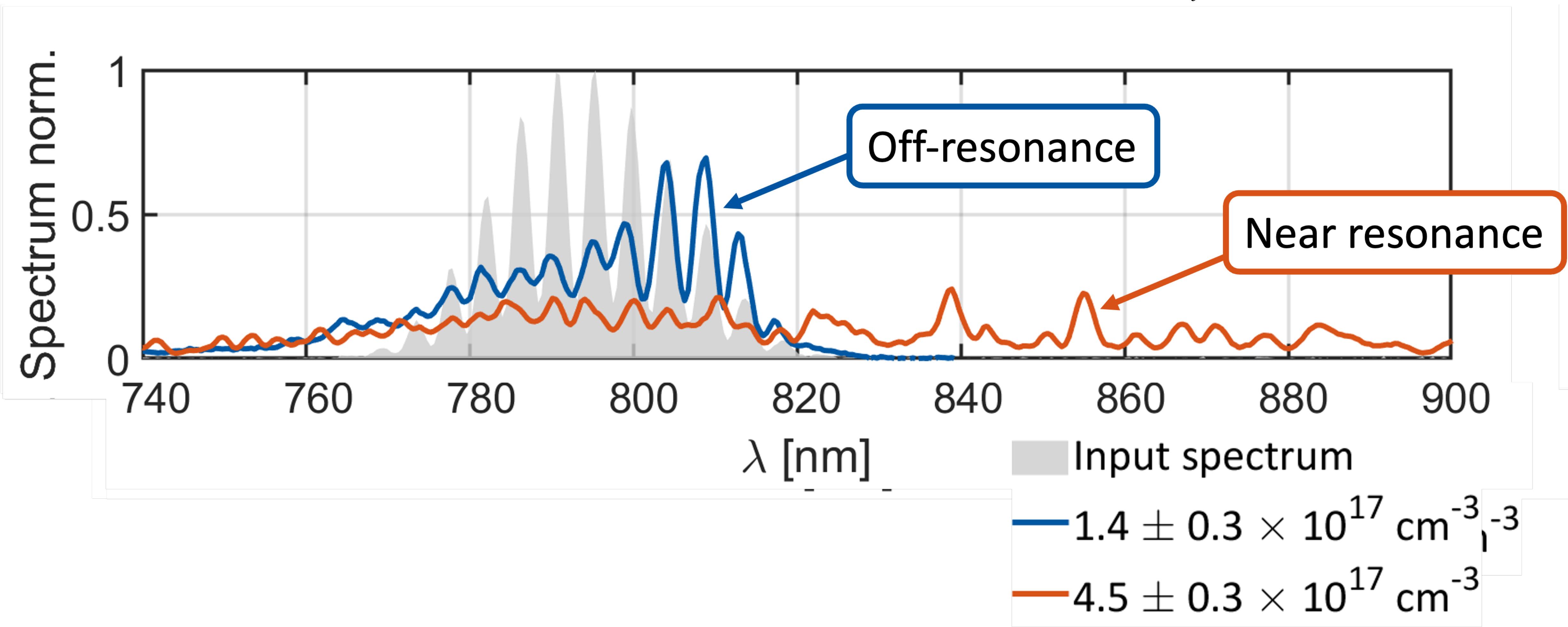
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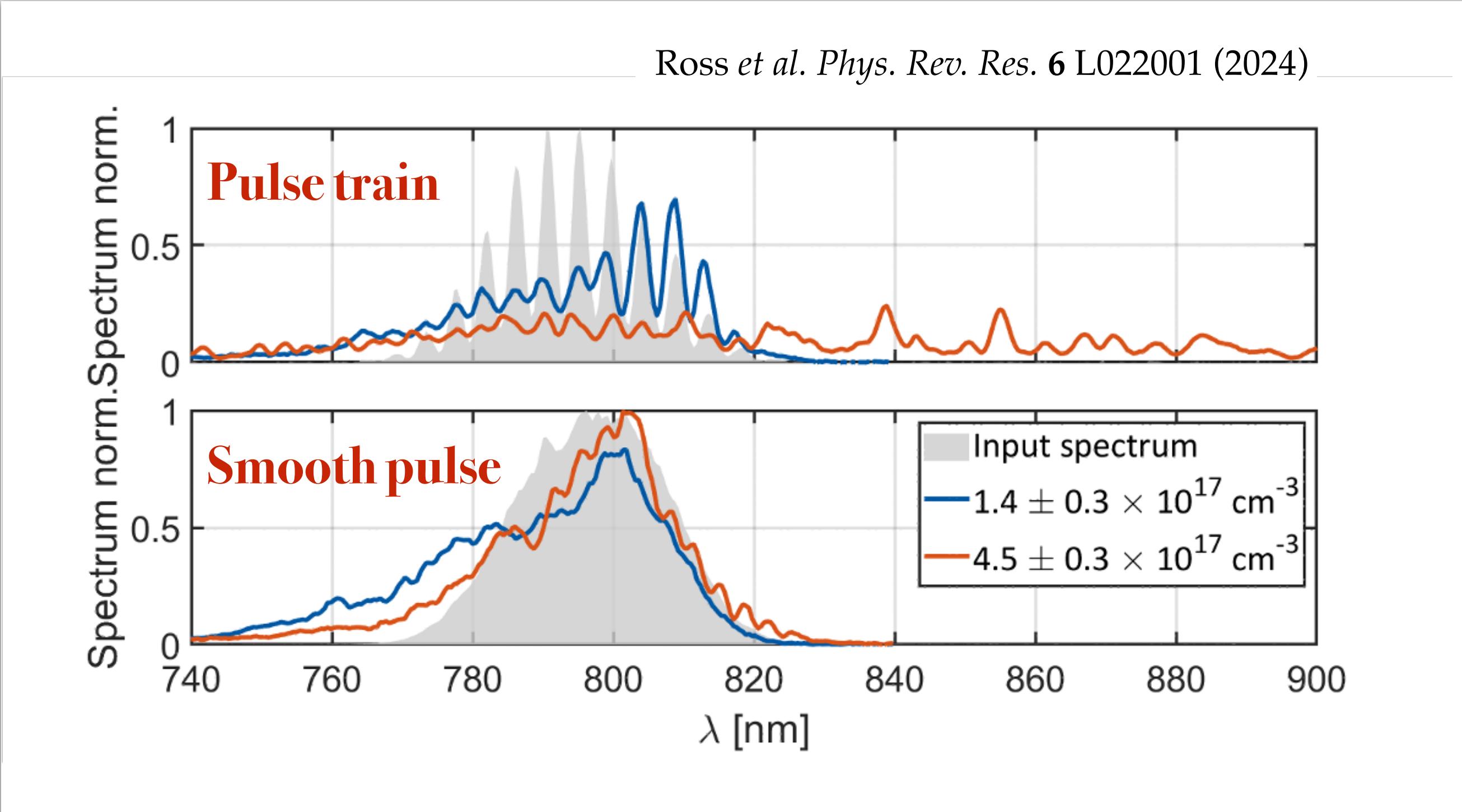


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Ross *et al.* *Phys. Rev. Res.* **6** L022001 (2024)



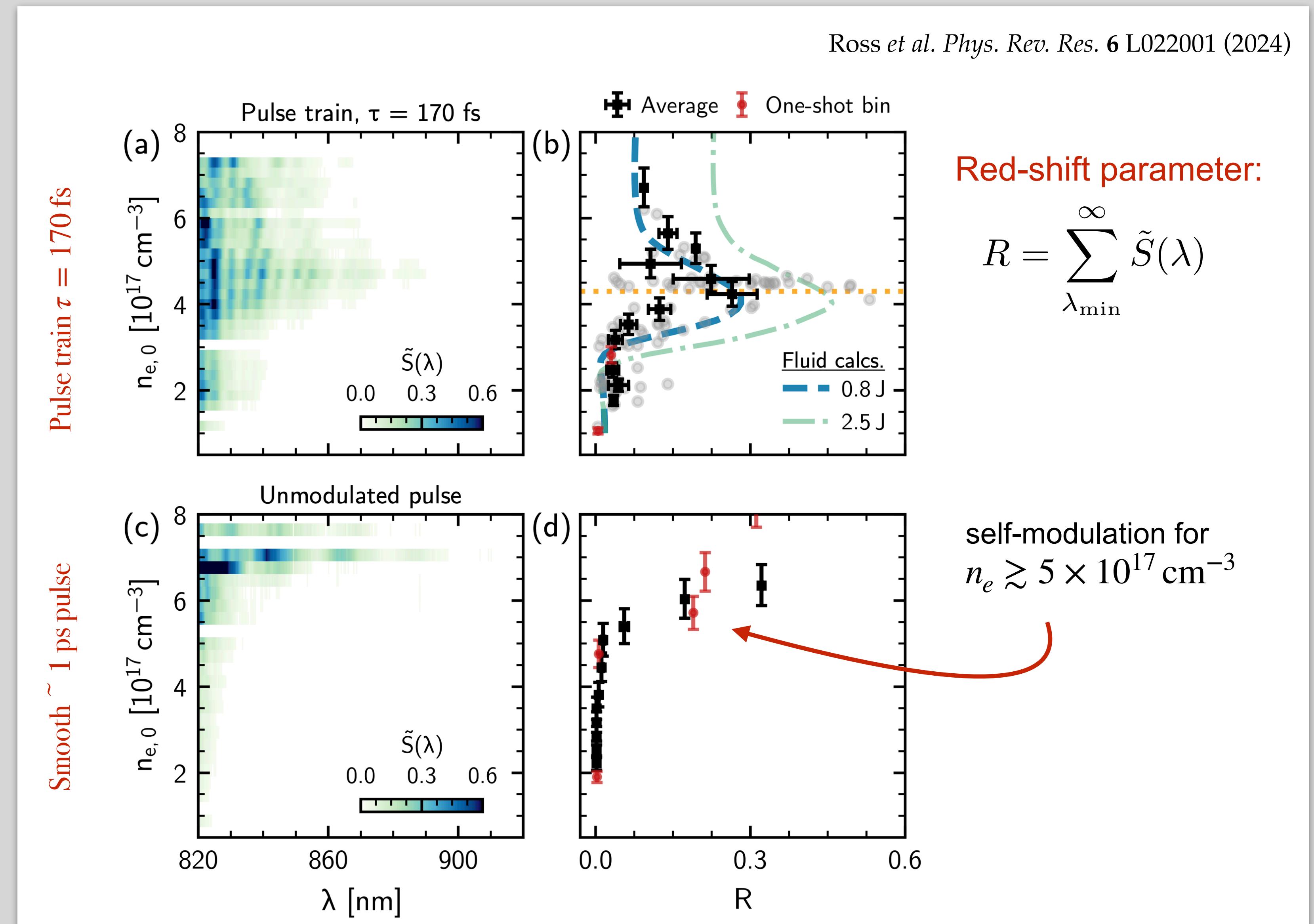
# ... but smooth pulse does not



- ▶ Block one-arm of Michelson
  - Smooth  $\sim 1$  ps pulse
  - 2.7 J on target
- ▶ No red-shifting observed!

# Clear resonance observed for pulse trains, but not for smooth pulses

Ross et al. *Phys. Rev. Res.* **6** L022001 (2024)



# Comparison with simulations

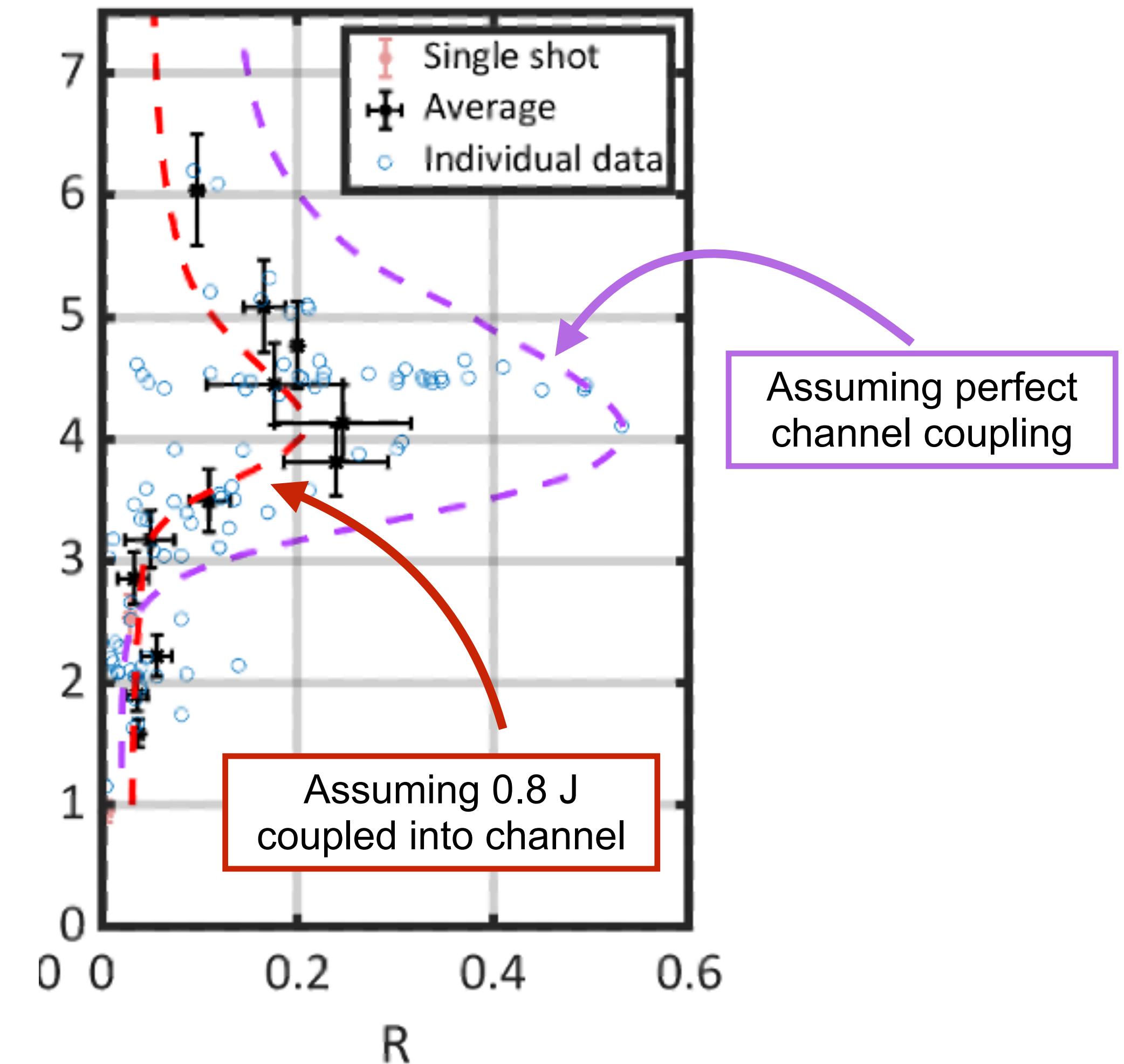
## ► Experimental realities

- Lowest-order mode overlap  $\sim 80\%$
- Pointing jitter of pulse train at channel entrance  $\sim 31 \mu\text{m}$

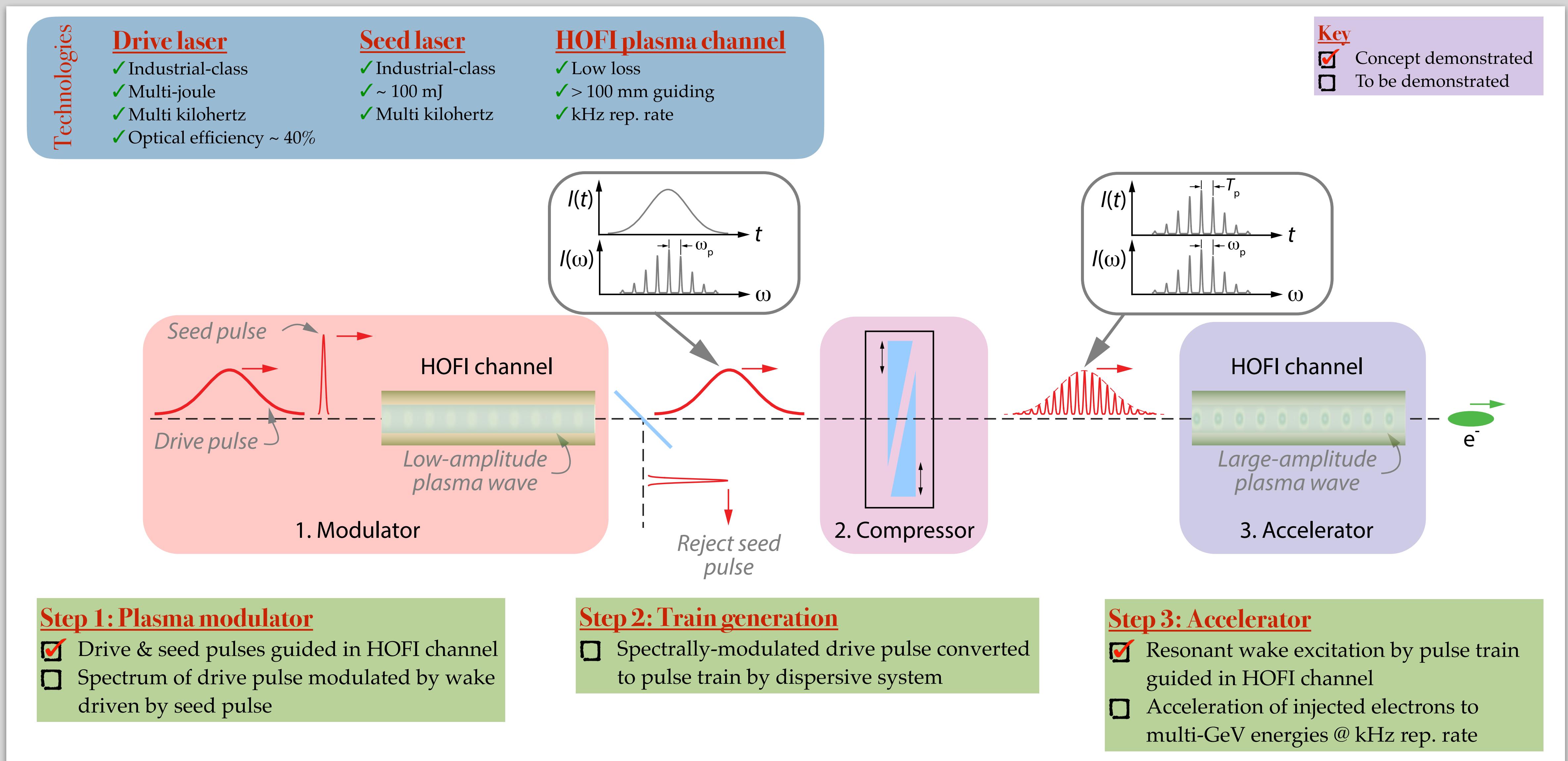
## ► Simulations

- 2D cylindrical fluid benchmarked against PIC
- Largest shifts agree well with calcn for perfect coupling
- Average shifts consistent with  $\sim 0.8 \text{ J}$  coupled into channel
- Accel. gradient 3 - 10 GeV / m
- [i.e. (0.3 - 1) GeV over the stage]

Ross *et al.* *Phys. Rev. Res.* **6** L022001 (2024)



# Summary of progress



## Step 1: Plasma modulator

- Drive & seed pulses guided in HOFI channel
- Spectrally-modulated drive pulse converted to pulse train by dispersive system

## Step 2: Train generation

- Spectrally-modulated drive pulse converted to pulse train by dispersive system

## Step 3: Accelerator

- Resonant wake excitation by pulse train guided in HOFI channel
- Acceleration of injected electrons to multi-GeV energies @ kHz rep. rate

## Post-doc opportunities!

We have funding for post-doc positions to work on the P-MoPA scheme

Please contact me if you'd like to discuss these further

[simon.hooker@physics.ox.ac.uk](mailto:simon.hooker@physics.ox.ac.uk)



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## Summary

- ▶ The P-MoPA scheme offers a possible route to kHz, GeV-scale plasma accelerators driven by industrial-class lasers
- ▶ HOFI channels can meet requirements of modulator & accelerator stages
  - Operate at kHz rep. rate for extended period
  - Guide joule-scale pulse trains over  $\sim 100$  mm
- ▶ Successful proof-of-principle demonstration of accelerator stage
  - Joule-scale pulse trains guided in  $\sim 100$  mm HOFI channel
  - Resonant wakefield excitation in plasma channel observed
  - Acceleration gradient 3 - 10 GeV / m ( $\sim 1$  GeV stage energy gain)