

Selection rules for cLFV processes from residual flavour groups

Claudia Hagedorn IFIC - UV/CSIC

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Overview

- Introduction
- Idea of residual symmetries
- Systematic search
- Allowed cLFV processes
- Experimental constraints and prospects
- Summary and outlook

Based on

Lorenzo Calibbi, CH, Michael A. Schmidt, James Vandeleur (2505.24350 [hep-ph])



Introduction

- Standard Model (SM) is very successful. Nevertheless, several phenomena are not explained within SM.
 - Replication of fermion generations
 - Fermion masses
 - Quark and lepton mixing
 - Baryon asymmetry of the Universe (BAU)
 - Dark Matter (DM)
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 - Replication of fermion generations
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 - Dark Matter (DM)
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- Additionally, beyond SM (BSM) theories can have a rich phenomenology.
 - Processes forbidden/highly suppressed in SM can be in reach
 - Flavour and CP violation needs to be kept under control
 - Possible correlations among different signals



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Idea: Keep some residual symmetry among **charged leptons** and neutrinos, G_e and G_v , with $G_e \neq G_v$ Mismatch of symmetries corresponds to lepton mixing



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see e.g. Feruglio/CH/Ziegler ('12)

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Indeed, the minimal choice Z₃ is often encountered (and G_ν = Z₂ × Z₂)
 Typical A₄ and S₄ models leading to tri-bimaximal mixing see e.g. Altarelli/Feruglio ('05), He/Keum/Volkas ('06), Lam ('08)



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Also four interesting mixing patterns (Case 1) through Case 3 b.1)) arising from $G_f = \Delta(3 n^2)$ and $G_f = \Delta(6 n^2)$ and CP require Z_3 as residual group among charged leptons (and $G_{\nu} = Z_2 \times CP$) see e.g. CH/Meroni/Molinaro ('14), Ding/King/Neder ('14)



- Indeed, the minimal choice Z_3 is often encountered (and $G_{\nu} = Z_2 \times Z_2$)
- This Z_3 symmetry has been coined **lepton triality** $e \sim 1, \mu \sim \omega$ and $\tau \sim \omega^2$ with ω being the 3rd root of unity, $\omega = e^{\frac{2\pi i}{3}}$ correspond to Z_3 charge 0 for e, 1 for μ and 2 for τ (modulo 3) see e.g. Ma ('10)



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- It is known that it **forbids** cLFV processes such as $\mu \rightarrow e \gamma$, $\mu \rightarrow e e \overline{e}$ and $\mu - e$ conversion in nuclei N but **allows** for the tri-lepton tau lepton decays

$$\tau \rightarrow e e \bar{\mu}$$
 and $\tau \rightarrow \mu \mu \bar{e}$

see e.g. Feruglio/CH/Lin/Merlo ('08), Csaki/Delaunay/Grojean/Grossman ('08), Ma ('10), Holthausen/Lindner/Schmidt ('12), Pascoli/Zhou ('16), Bigaran et al. ('22), Lichtenstein/Schmidt/Valencia/Volkas ('23)

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- Indeed, the minimal choice Z_3 is often encountered (and $G_{\nu} = Z_2 \times Z_2$)
- However, it is definitely not the only possibility Other known examples are:
 - $G_e = Z_4$ (and $G_\nu = Z_2 \times Z_2$) from S_4 leads to bimaximal mixing see e.g. de Adelhart Toorop/Feruglio/CH ('11)
 - G_e = Z₅ (and G_v = Z₂ × Z₂ or G_v = Z₂ × CP) from A₅ (and CP) leads to golden ratio(-like) mixing see e.g. Feruglio/Paris ('11), Di Iura/CH/Meloni ('15), Ballett/Pascoli/Turner ('15),

Li/Ding ('15)

- $G_e = Z_7$ can arise in scenarios with the flavour symmetry PSL(2,7) see e.g. de Adelhart Toorop/Feruglio/CH ('11)
- further examples for G_e from $\Sigma(n \varphi)$ see e.g. CH/Meroni/Vitale ('13)



• Consider **small** $G_e = Z_N$ with $N \le 8$ (also discussed direct products)



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- Consider **small** $G_e = Z_N$ with $N \le 8$ (also discussed direct products)
- Are residuals of some discrete group that fits in U(3), maybe also SU(3)
- Take into account all possible flavour charge assignments (α, β, γ); also those where two flavours have the same charge,
 e.g. Q(e) = 0, Q(μ) = 0 and Q(τ) = 1
 - \rightarrow consequences
 - Flavour charge assignments that require embedding in U(3) are encountered, e.g. Q(e) = 0, $Q(\mu) = 0$ and $Q(\tau) = 2$ in $G_e = Z_3$
 - Also $G_e = Z_2$ is included in the search



What is not included?

- Breaking effects of residual symmetry *G_e* (shifts in flavon VEVs, cross-talk between different symmetry breaking sectors, etc.)
 - \rightarrow consequences
 - e.g. in case of lepton triality $\tau \rightarrow \mu\mu\bar{\mu}$ becomes allowed, but its BR should be more suppressed than $\tau \rightarrow \mu\mu\bar{e}$



What is not included?

- Breaking effects of residual symmetry *G_e* (shifts in flavon VEVs, cross-talk between different symmetry breaking sectors, etc.)
- Effects arising from concrete model realisation
 - \rightarrow consequences

e.g. in case of lepton triality BR ($\tau \rightarrow \mu \mu \bar{e}$) \gg BR ($\tau \rightarrow e e \bar{\mu}$) in SUSY version of well-known A_4 model

see e.g. Muramatsu/Nomura/Shimizu ('16)

but conclusion depends on whether certain flavon components mix or not

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see e.g. Pascoli/Zhou ('16)
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• Interested in studying cLFV processes, lepton number is conserved



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- Use SMEFT operators and focus on their flavour structure

e.g.
$$\frac{1}{\Lambda^2} (\overline{\ell}_{\mu} \gamma_{\nu} \ell_{e}) (\overline{\ell}_{\mu} \gamma^{\nu} \ell_{e}) \to e e \mu^{\dagger} \mu^{\dagger}$$



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- All operators conserve *number of charged leptons*,
 i.e.

$$(n_e^- - n_e^+) + (n_\mu^- - n_\mu^+) + (n_\tau^- - n_\tau^+) \equiv \Delta n_e + \Delta n_\mu + \Delta n_\tau = 0$$

Example: $ee\mu^{\dagger}\tau^{\dagger}$ is characterised by $\{\Delta n_e, \Delta n_{\mu}, \Delta n_{\tau}\} = \{2, -1, -1\}$ and fulfils the equation



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• All operators are *invariant under residual symmetry* $G_e = Z_N$ i.e. $\alpha \Delta n_e + \beta \Delta n_\mu + \gamma \Delta n_\tau = 0 \mod N$

with α flavour charge of e, β of μ and γ of τ



- Denote particular flavour charge assignment as $Z_N(\alpha, \beta, \gamma)$
- Labelling can be reduced with the two constraints to two parameters $\delta_1 = \beta \alpha$ and $\delta_2 = \gamma \beta$ and the constraint

0 mod
$$N = \delta_1 \Delta n_\mu + (\delta_1 + \delta_2) \Delta n_\tau$$

so we have $N(\delta_1, \delta_2)$



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• $N(\delta_1, \delta_2)$ does not uniquely specify flavour charge assignment, e.g. $\mathbb{Z}_3(0, 0, 1)$ $\mathbb{Z}_3(1, 1, 2)$ $\mathbb{Z}_3(2, 2, 0)$ $\} \rightarrow 3(0, 1)$



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- $N(\delta_1, \delta_2)$ does not uniquely specify flavour charge assignment
- At this stage e, μ and τ can be permuted
- We put flavour charge assignments compatible with *SU*(3) in **boldface**, but *N*(δ₁, δ₂) does not mean all corresponding flavour charge assignments have this property,

 $3\alpha + 2\delta_1 + \delta_2 = 0 \mod N$

e.g. **4**(**0**, **1**) corresponds to **Z**₄(**1**, **1**, **2**), but also $Z_4(0,0,1)$

Additional condition: C. Hagedorn

• Several equivalences among the flavour charge assignments: common factors, permutations, complex conjugation



- Several equivalences among the flavour charge assignments: common factors, permutations, complex conjugation
- For flavour structures:

Hermitian conjugation, trivial flavour structures (e.g. ee^{\dagger}), combinations of invariant flavour structures are not included



• Systematic scan over all possible flavour charge assignments $Z_N(\alpha, \beta, \gamma)$

$$0 \le \alpha \le \beta$$
, $0 \le \beta \le \gamma$, $0 \le \gamma \le N - 1$

• Scan over flavour structures $\{\Delta n_e, \Delta n_\mu, \Delta n_\tau\}$

$$0 \le \Delta n_e \le N$$
, $-N \le \Delta n_\mu \le N$, $\Delta n_\tau = -\Delta n_e - \Delta n_\mu$



• Output

Flavour		Flavour	Flav	our		Flavour
charges	d_ℓ	structures	char	ges	d_ℓ	structures
2 (0 , 1)	3	$e\mu^\dagger$	4(1,	1)	6	$e\mu^\dagger\mu^\dagger au$
	6	$\mu\mu au^{\dagger} au^{\dagger}$	3 * 24	-		$ee au^\dagger au^\dagger$
		$e\mu au^{\dagger} au^{\dagger}$			9	$e\mu\mu au^\dagger au^\dagger au^\dagger$
		$ee au^\dagger au^\dagger$				$eee\mu^\dagger\mu^\dagger au^\dagger$
3(0,1)	3	$e\mu^\dagger$			12	$\mu\mu\mu\mu au^{\dagger} au^{\dagger} au^{\dagger} au^{\dagger} au^{\dagger}$
	9	$\mu\mu\mu\mu au^{\dagger} au^{\dagger} au^{\dagger}$				$eeee\mu^\dagger\mu^\dagger\mu^\dagger\mu^\dagger$
		$e\mu\mu au^{\dagger} au^{\dagger} au^{\dagger}$	5 (0 ,	1)	3	$e\mu^\dagger$
		$ee\mu au^{\dagger} au^{\dagger} au^{\dagger}$			15	$\mu\mu\mu\mu\mu\mu au^{\dagger} au^{\dagger} au^{\dagger} au^{\dagger} au^{\dagger}$
		$eee au^\dagger au^\dagger au^\dagger$				$e\mu\mu\mu\mu\tau^{\dagger} au^{\dagger} au^{\dagger} au^{\dagger} au^{\dagger} au^{\dagger}$
3(1,1)	6	$e\mu au^\dagger au^\dagger$				$ee\mu\mu\mu\tau^{\dagger} au^{\dagger} au^{\dagger} au^{\dagger} au^{\dagger} au^{\dagger}$
		$e\mu^{\dagger}\mu^{\dagger} au$				$eee\mu\mu au^{\dagger} au^{\dagger} au^{\dagger} au^{\dagger} au^{\dagger}$
		$ee\mu^{\dagger}\tau^{\dagger}$				$eeee\mu au^{\dagger} au^{\dagger} au^{\dagger} au^{\dagger} au^{\dagger}$
	9	$\mu\mu\mu\mu au^{\dagger} au^{\dagger} au^{\dagger}$				$eeee au^\dagger au^\dagger au^\dagger au^\dagger au^\dagger$
		$eee au^\dagger au^\dagger au^\dagger$	5(1,	1)	6	$e\mu^{\dagger}\mu^{\dagger} au$
		$eee\mu^{\dagger}\mu^{\dagger}\mu^{\dagger}$,	9	$eeu\tau^{\dagger}\tau^{\dagger}\tau^{\dagger}$

• Translate flavour structures of SMEFT operators into cLFV processes e.g. $e\mu^{\dagger}$



• Consider SMEFT operators up to dimension 6, i.e. $d_{\ell} \leq 6$

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• Confront the results with current and future experimental limits



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- Distinguish between low-energy cLFV experiments and possible cLFV searches at high-energy colliders



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- Distinguish between low-energy cLFV experiments and possible cLFV searches at high-energy colliders
- Consider up to three scenarios inspired by typical UV completions
 - Scenario 1: Tree-level new physics contributions all allowed Wilson coefficients (WCs) are set to $C_x = 1$ apart from the ones of the dipole operator $C_d = \frac{e}{16 \pi^2} \approx 0.002$
 - Scenario 2: One-loop new physics contributions all WCs are set to $C_x = \frac{1}{16 \pi^2} \approx 0.006$ and $C_d = \frac{e}{16 \pi^2} \approx 0.002$
 - Scenario 3: Dipole operators suppressed by Yukawa coupling meaning $C_d = \frac{\sqrt{2} m_\ell e}{16 \pi^2 v}$

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(formulae, see e.g. Calibbi/Marcano/Roy ('21))



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No RG running. No matching of SMEFT to LEFT.

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No RG running. No matching of SMEFT to LEFT. C. Hagedorn



C. Hagedorn No RG running. No matching of SMEFT to LEFT.



- Comment on possible cLFV searches at high-energy colliders
- Test SMEFT operators with same sign tau leptons via scattering

$$e^{\pm}e^{\pm} \to \tau^{\pm}\tau^{\pm}, \quad e^{\pm}\mu^{\pm} \to \tau^{\pm}\tau^{\pm}, \quad \mu^{\pm}\mu^{\pm} \to \tau^{\pm}\tau^{\pm}$$

• With proposed experiment μ TRISTAN testable Hamada et al. ('22)

$$\sigma(\mu^+\mu^+ \to \tau^+\tau^+) = \frac{s}{2\pi} \frac{|C_x|^2}{\Lambda^4} \simeq 25 \,\text{fb} \,\left(\frac{\sqrt{s}}{2 \,\text{TeV}}\right)^2 \left(\frac{10 \,\text{TeV}}{\Lambda/\sqrt{|C_x|}}\right)^4$$

For $\sqrt{s} = 2$ TeV and $C_x = 1$ limit on new physics scale is $\Lambda \approx 30$ TeV

see e.g. Fridell/Kitano/Takai ('23)



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• Other possible probe four-body *Z* boson decays, e.g. $Z \rightarrow \tau \tau \bar{e} \bar{e}$, but constraints on Λ are (very) weak

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see e.g. Heeck/Sokhashvili ('24) FLASY 2025

Summary

- Derived selection rules for cLFV processes arising from residual symmetry $G_e = Z_N$ with $N \le 8$
- Focussing on SMEFT operators with dimension six or less all possible flavour charge assignments turn out to be equivalent to one for $G_e = Z_N$ with $N \le 4$
- If the flavour charges of *e* and *μ* are different, *μ* → *e* transitions are forbidden
- If so, experimental constraints on cLFV tau lepton decays and muonium to antimuonium conversion, $M \rightarrow \overline{M}$, are crucial, see $G_e = Z_3$ and $G_e = Z_4$



Outlook

- Consider **concrete models** with studied residual group G_e
- Analyse SMEFT operators with **lepton number violation**
- Apply **same logic to quark sector** and discuss quark flavour violation
 - Use G_e also for quarks, potentially with same flavour charge assignment
 - Or assume different residual symmetries for up and down quarks that in general also differ from G_e

Many thanks for your attention!

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... one last point

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> Proposal submission/Application for program participation: www.munich-iapbp.de

If you are interested, please register!

Back-up slides



• Output

			Fla	avour arges	d.o	Flavour structures
Flavour charges	d_ℓ	Flavour structures	7(1	1 , 2)	9	$e\mu^2(\tau^{\dagger})^3$
6(0,1)	3	$e\mu^{\dagger}$				$e^{-}(\mu^{+})^{-} au^{+}$ $e^{3}\mu^{\dagger}(au^{\dagger})^{2}$
	18	$\mu^{\circ}(au^{+})^{\circ} = e\mu^{5}(au^{\dagger})^{6}$			15	$e(\mu^{\dagger})^5 au^4 \ e^4\mu(au^{\dagger})^5$
		$e^2 \mu^4 (au^\dagger)^6 \ e^3 \mu^3 (au^\dagger)^6$			21	$e^5(\mu^\dagger)^4 au^\dagger \ \mu^7(au^\dagger)^7$
		$e^4\mu^2(au^\dagger)^6 \ e^5\mu(au^\dagger)^6$	8(0, 1)			$e^7(\tau^{\dagger})^7$
		$e^6(au^\dagger)^6$		D , 1)	3	$\frac{e^{\mu}(\mu^{\dagger})^{\mu}}{e\mu^{\dagger}}$
${f 6}({f 1},{f 1})$	6	$e(\mu^\dagger)^2 au$	Ň		24	$\mu^8(au^\dagger)^8$
	9	$e^3(au^\dagger)^3$				$e\mu^{\hat{7}}(\tau^{\dagger})^{8}$
	12	$e^2 \mu^2 (au^\dagger)^4$				$e^2\mu^{\hat{6}}(au^{\dagger})^8$
		$e^4(\mu^\dagger)^2(au^\dagger)^2$				$e^3 \mu^5 (au^\dagger)^8$
	15	$e\mu^{4}(au^{\dagger})^{5}$				$e^4 \mu^4 (au^\dagger)^8$
		$e^5(\mu^\dagger)^{4} au^\dagger$				$e^5 \mu^3 (au^\dagger)^8$
	18	$\mu^{6}(\tau^{\dagger})^{6}$				$e^6\mu^2(au^\dagger)^8$

Restrictions from single flavour structure

$$\begin{array}{lll} e\mu^{\dagger} - N(0,a) & ee\mu^{\dagger}\mu^{\dagger} - 2N(N,a) & ee\mu^{\dagger}\tau^{\dagger} - N(N-a,2a) \\ \mu\tau^{\dagger} - N(a,0) & \mu\mu\tau^{\dagger}\tau^{\dagger} - 2N(a,N) & e\mu^{\dagger}\mu^{\dagger}\tau - N(a,a) \\ e\tau^{\dagger} - N(a,N-a) & ee\tau^{\dagger}\tau^{\dagger} - 2N(a,N-a) & e\mu\tau^{\dagger}\tau^{\dagger} - N(2a,N-a) \end{array}$$

a is an integer



Restrictions from single flavour structure



a is an integer



NT(S S)		Observable	Curren	t (Λ in TeV)	Future (Λ in TeV)			
$IV(o_1, o_2)$		Observable	Constraint	$\Lambda_{ m T}\left(\Lambda_{ m T\chi} ight)$	$\Lambda_{ m L}\left(\Lambda_{ m L\chi} ight)$	Constraint	Λ_{T}	$\Lambda_{ m L}$
2(0, 1)	$e\mu^\dagger$	${ m BR}(\mu o e \gamma)$	1.5×10^{-13} [53]	3000(73)	3000 (73)	$6 imes 10^{-14}$ [54]	3900	3900
		${ m BR}(\mu o ee \bar{e})$	1.0×10^{-12} [55]	500(290)	520(23)	10^{-16} [56]	5000	5200
		$\operatorname{CR}(\mu\operatorname{Au}\to e\operatorname{Au})$	$7 imes 10^{-13}$ [57]	1800 (1800)	430(140)	—	—	—
		$\operatorname{CR}(\mu\operatorname{Al}\to e\operatorname{Al})$	—		_	6×10^{-17} [58, 59]	15000	4000
9	$ee\mu^{\dagger}\mu^{\dagger}$	$\mathrm{P}(\mathrm{M}\to\overline{\mathrm{M}})$	$8.2 imes 10^{-11}$ [61]	9.5	0.76	10^{-13} [62]	51	4.1
2(1,0)	μau^{\dagger}	$BR(\tau \to \mu \gamma)$	$4.2 imes 10^{-8}$ [65]	20(2.1)	20(2.1)	$6.9 imes 10^{-9}$ [72]	32	32
		$BR(\tau \to \mu \rho)$	$1.7 imes 10^{-8}$ [66]	21(20)	5.9(1.6)	$5.5 imes 10^{-10}$ [72]	49	14
		${ m BR}(au o \mu \phi)$	$2.3 imes 10^{-8}$ [66]	14(14)	3.2(1.1)	$8.4 imes 10^{-10}$ [72]	33	7.3
		$BR(\tau \to \mu \pi)$	1.1×10^{-7} [63]	7.8	0.62	$7.1 imes 10^{-10}$ [72]	28	2.2
		$BR(\tau \to \mu K)$	$2.3 imes 10^{-8}$ [68]	14	1.1	$4.0 imes 10^{-10}$ [72]	39	3.1
		${ m BR}(au o \mu \mu ar \mu)$	$1.9 imes 10^{-8}$ [70]	16(16)	5.3(1.3)	$3.6 imes 10^{-10}$ [72]	42	14
		$BR(au o \mu e \overline{e})$	$1.8 imes 10^{-8}$ [69]	15(15)	5.3(1.2)	$2.9 imes 10^{-10}$ [72]	42	15
	$ee\mu^\dagger\mu^\dagger$	$P(M \rightarrow \overline{M})$	$8.2 imes 10^{-11}$ [61]	9.5	0.76	10^{-13} [62]	51	4.1
	$ee\mu^\dagger au^\dagger$	${ m BR}(au o eear\mu)$	$1.5 imes 10^{-8}$ [69]	16	1.3	$2.3 imes 10^{-10}$ [72]	45	3.6

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2(1,1)	$e\tau^{\dagger} \ { m BR}(au o e\gamma)$	$3.3 imes 10^{-8}$ [67]	22(2.2)	22(2.2)	$9.0 imes 10^{-9}$ [72]	30	30
	${ m BR}(au o e ho)$	$2.2 imes 10^{-8}$ [66]	20(19)	5.6(1.5)	$3.8 imes 10^{-10}$ [72]	54	15
	${ m BR}(au o e \phi)$	$2.0 imes 10^{-8}$ [66]	15(15)	3.4(1.2)	$7.4 imes 10^{-10}$ [72]	35	7.7
	${ m BR}(au o e\pi)$	$8.0 imes 10^{-8}$ [64]	8.5	0.67	$7.3 imes 10^{-10}$ [72]	27	2.2
	${ m BR}(au o eK)$	$2.6 imes 10^{-8}$ [68]	14	1.1	$4.0 imes 10^{-10}$ [72]	40	3.2
	${ m BR}(au ightarrow eear{e})$	$2.7 imes 10^{-8}$ [69]	15(15)	7.3(1.2)	$4.7 imes 10^{-10}$ [72]	40	20
	${ m BR}(au o e \mu ar\mu)$	$2.7 imes 10^{-8}$ [69]	14(14)	7.3(1.1)	$4.5 imes 10^{-10}$ [72]	38	20
	$ee\mu^{\dagger}\mu^{\dagger} \mathrm{P}(\mathrm{M} ightarrow \overline{\mathrm{M}})$	$8.2 imes 10^{-11}$ [61]	9.5	0.76	10^{-13} [62]	51	4.1
	$e\mu^{\dagger}\mu^{\dagger}\tau \ \mathrm{BR}(\tau ightarrow \mu\mu\bar{e})$	$1.7 imes 10^{-8}$ [69]	16	1.2	$2.6 imes 10^{-10}$ [72]	44	3.5
${f 3}({f 1},{f 1})$	$e\mu^{\dagger}\mu^{\dagger}\tau \ \mathrm{BR}(au o \mu\mu ar{e})$	$1.7 imes 10^{-8}$ [69]	16	1.2	$2.6 imes 10^{-10}$ [72]	44	3.5
	$ee\mu^{\dagger}\tau^{\dagger} \mathrm{BR}(au o eear{\mu})$	$1.5 imes 10^{-8}$ [69]	16	1.3	$2.3 imes 10^{-10}$ [72]	45	3.6
${f 4}({f 1},{f 1})$	$e\mu^{\dagger}\mu^{\dagger}\tau \ \mathrm{BR}(\tau ightarrow \mu\mu\bar{e})$	$1.7 imes 10^{-8}$ [69]	16	1.2	$2.6 imes 10^{-10}$ [72]	44	3.5
${f 4}({f 2},{f 3})$	$ee\mu^{\dagger}\mu^{\dagger} \ P(M \to \overline{M})$	$8.2 imes 10^{-11}$ [61]	9.5	0.76	10^{-13} [62]	51	4.1
${f 4}({f 3},{f 2})$	$ee\mu^{\dagger}\tau^{\dagger} \ \mathrm{BR}(\tau \to ee\bar{\mu})$	$1.5 imes 10^{-8}$ [69]	16	1.3	2.3×10^{-10} [72]	45	3.6

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$N(\delta_1,\delta_2)$		Obcommoble	Current (Λ in	TeV)	Future (Λ in TeV)		
		Observable	Constraint	Λ_{T}	Constraint	Λ_{T}	
${f 2}({f a},{f b})^{\ddagger},{f 4}({f 3},{f 2})$	$\mu(\mathbf{a},\mathbf{b})^{\ddagger},4(3,2)$ $\mu\mu au^{\dagger} au^{\dagger}$		_		0.3 fb [83]	30	
		$BR(Z \to \tau \tau \bar{\mu} \bar{\mu})$	$2 imes 10^{-3}$ [31]	0.001	10^{-12} [31]	0.25	
${f 2}({f a},{f b})^{\ddagger},{f 4}({f 1},{f 1})$	$ee au^\dagger au^\dagger$	$BR(Z \to \tau \tau \bar{e}\bar{e})$	2×10^{-3} [31]	0.001	10^{-12} [31]	0.25	
2(0,1), 3(1,1), 4(2,3)	$e\mu au^{\dagger} au^{\dagger}$	$BR(Z \to \tau \tau \bar{e}\bar{\mu})$	2×10^{-3} [31]	0.001	10^{-12} [31]	0.21	

^{\ddagger} **2**(**a**, **b**) stands for **2**(**0**, **1**), **2**(**1**, **0**) and **2**(**1**, **1**).

