

# Dark Hypercharge Symmetry

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**FLASY - 2025**

- 1 Introduction
- 2 Anomalies in SM: Uniqueness of Hypercharge
- 3  $U(1)_X$  anomaly cancellation: Known Solutions
- 4  $U(1)_X$  anomaly cancellation: Dark Hypercharge Symmetry
- 5 The Dark  $Z'$  Gauge Boson
- 6 The Dark Sector
- 7 Constraining Light  $Z'$
- 8 Conclusion

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- 2 Anomalies in SM: Uniqueness of Hypercharge
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- 6 The Dark Sector
- 7 Constraining Light  $Z'$
- 8 Conclusion

- Despite its many successes, Standard Model (SM) is an incomplete theory
- New physics Beyond Standard Model (BSM) is needed to explain Neutrino mass and mixing, Dark Matter, Matter - Antimatter Asymmetry, Vacuum Stability, Hierarchy Problem etc
- $U(1)_X$  gauge theories are one of the simplest extensions of SM
- They naturally occur in many popular BSM extensions e.g. GUTs, Left-Right Symmetry etc
- In recent times there is a growing interest in using  $U(1)_X$  symmetries to explain various phenomenon
- In addition to its simplicity  $U(1)_X$  theories are highly predictive: Gauge charges of SM and BSM fermions can be fixed by anomaly cancellation conditions

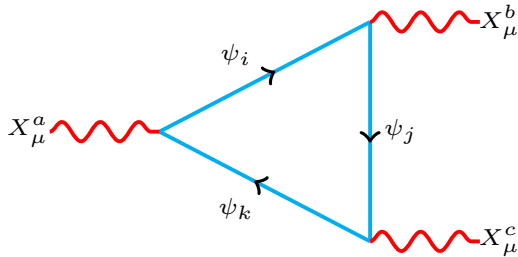
- Anomalies: Whenever a symmetry of the classical theory which does not survive to the quantum theory
- Anomalies can potentially occur whenever a classically invariant field theory with a continuous symmetry is quantized
- Historically they were first discovered in context of  $\pi^0 \rightarrow \gamma\gamma$  decay<sup>1</sup>
- Especially for gauge symmetries presence of anomalies can have serious consequences and can make the theory nonunitary and nonrenormalizable.
- Thus any gauge theory should always be anomaly free.
- A pure gauge theories with no "matter fields" or a gauge theory with only scalar matter fields is always anomaly free
- However one has to be careful when the gauge theory also has fermionic matter fields like SM

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<sup>1</sup>S. L. Adler, Phys. Rev. 177 (5), 2426–2438 (1969); J. S. Bell, R. Jackiw, Nuovo Cimento A. 60 (1): 47–61 (1969)

# Triangle Diagrams

- The "gauge anomalies" in field theory are induced by the triangle diagrams



- For a gauge theory to be anomaly free, the total contribution of all such diagrams must vanish
- For theories with multiple gauge symmetries such as SM: All triangle diagrams with odd number of non-abelian gauge bosons attached to the vertices vanish
- Thus, one has to worry about anomaly only when the theory also has abelian  $U(1)$  gauge symmetries like the case of SM

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- 4  $U(1)_X$  anomaly cancellation: Dark Hypercharge Symmetry
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- 6 The Dark Sector
- 7 Constraining Light  $Z'$
- 8 Conclusion

# Anomalies in Standard Model

- SM is a theory with:
  - An abelian gauge symmetry  $U(1)_Y$
  - Its fermions are also "chiral" i.e. the left and right counterpart fields do not have same charge under both  $SU(2)_L$  and  $U(1)_Y$
  - SM can be potentially anomalous
- All anomalies must be cancelled for SM to be a unitary and renormalizable field theory
- The complete set of anomaly cancellation conditions for SM are:

$$[SU(3)_C]^2 U(1)_Y = \sum_i Y_{Q^i} - \sum_j Y_{q^j}, \quad (1a)$$

$$[SU(2)_L]^2 U(1)_Y = \sum_i Y_{L^i} + 3 \sum_j Y_{Q^j}, \quad (1b)$$

$$[U(1)_Y]^3 = \sum_{i,j} (Y_{L^i}^3 + 3Y_{Q^j}^3) - \sum_{i,j} (Y_{l^i}^3 + 3Y_{q^j}^3), \quad (1c)$$

$$[G]^2 U(1)_Y = \sum_{i,j} (Y_{L^i} + 3Y_{Q^j}) - \sum_{i,j} (Y_{l^i} + 3Y_{q^j}). \quad (1d)$$



# Anomaly Cancellation in SM: Uniqueness of Hypercharge

## One Generation Case

- Let's first consider only one generation of SM fermions
- For SM to be anomaly free the  $U(1)_Y$  charges of SM fermions should be such that all anomalies cancel
- Canonical SM hypercharge assignment for fermions is

$Q$	$u_R$	$d_R$	$L$	$e_R$	$\Phi$
$\frac{Y}{3}$	$\frac{4Y}{3}$	$\frac{-2Y}{3}$	$-Y$	$-2Y$	$Y$

- One can check explicitly that it cancels all the anomalies.
- The usual choice for  $Y$  is either  $Y = 1$  or  $Y = 1/2$  depending on how you defined relation between hypercharge ( $Y$ ) and electric charge ( $Q$ )
  - If you define  $Q = T_3 + Y/2$ ;  $T_3$  being the third component of  $SU(2)_L$ , then  $Y = 1$
  - If you define  $Q = T_3 + Y$ , then  $Y = 1/2$
- Is this hypercharge assignment unique?
- NO!

# Anomaly Cancellation in SM: Uniqueness of Hypercharge

## One Generation Case

- One can find other solutions for SM fermion hypercharge assignments which also cancel anomalies
- One more solution can be found simply by interchanging the hypercharges of  $u_R$  and  $d_R$  i.e.  $Y_{u_R} = \frac{-2Y}{3}$  and  $Y_{d_R} = \frac{4Y}{3}$
- Another solution is  $Y_{u_R} + Y_{d_R} = 0$  and  $Y_L = Y_Q = Y_{e_R} = 0$ .
- However, all these other solutions have problems
  - Most serious problem is that none of these solutions give correct electric charges of the SM fermions
  - It is also not possible to define a new relation between  $Y$  and  $Q$  that gives correct electric charges for all SM fermions
  - Mass generation of all fermions cannot be achieved with only the SM Higgs. One will need more scalars.
- In summary for one generation of SM fermions, the anomaly cancellation conditions alone don't give an unique solution
- The additional requirement that the hypercharge assignment must lead to correct electric charges of SM fermions, makes the assignment unique.

# Anomaly Cancellation in SM: Uniqueness of Hypercharge

## Three Generations of SM fermions

- What happens with full three generations of SM fermions?
- The canonical choice is to give all generations of a given type of fermion the same hypercharge

$Q^i$	$u_{\text{R}}^i$	$d_{\text{R}}^i$	$L^i$	$e_{\text{R}}^i$	$\Phi$
$\frac{Y}{3}$	$\frac{4Y}{3}$	$\frac{-2Y}{3}$	$-Y$	$-2Y$	$Y$

- Thus with the canonical choice the SM hypercharges, the anomalies cancel generation by generation
- Are there other options?
- Yes! All other solutions discussed before can also work in a similar way. They all again will have the same problems so we have to again reject them
- In addition one can have new solutions

# Anomaly Cancellation in SM: Uniqueness of Hypercharge

## Three Generations of SM fermions

- One new solution is obtained when:

$$\begin{aligned} Y_{Q^i} = -Y_{Q^j} = Y, \quad Y_{Q^k} = 0 & \quad Y_{u_R^l} = -Y_{u_R^m} = Y', \quad Y_{u_R^n} = 0 \\ Y_{d_R^r} = -Y_{d_R^s} = Y'', \quad Y_{d_R^t} = 0 & \quad Y_{L^i} = Y_{e_R^j} = 0 \end{aligned}$$

- Another solution is obtained when

$$\begin{aligned} Y_{L^i} = -Y_{L^j} = Y, \quad Y_{L^k} = 0 & \quad Y_{e_R^l} = -Y_{e_R^m} = Y', \quad Y_{e_R^n} = 0 \\ Y_{Q^i} = Y_{u_R^j} = Y_{d_R^k} = 0 & \end{aligned}$$

- Again both these solutions have same problem as other solutions and hence should be rejected
- In summary, even with full three generations of SM fermions, the canonical hypercharge assignment is unique modulo an overall normalization factor.

- 1 Introduction
- 2 Anomalies in SM: Uniqueness of Hypercharge
- 3  $U(1)_X$  anomaly cancellation: Known Solutions
- 4  $U(1)_X$  anomaly cancellation: Dark Hypercharge Symmetry
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# $U(1)_X$ Anomaly Cancellation Conditions

- If we want to add a new  $U(1)_X$  gauge symmetry to the SM then one has to ensure that it is also not anomalous
- The extra anomaly cancellations needed are:

$$[SU(3)_C]^2[U(1)_X] = \sum_i X_{Q^i} - \sum_j X_{q'^j}. \quad (2a)$$

$$[SU(2)_L]^2[U(1)_X] = \sum_i X_{L^i} + 3 \sum_j X_{Q'^j}. \quad (2b)$$

$$[U(1)_Y]^2[U(1)_X] = \sum_{i,j} (Y_{L^i}^2 X_{L^i} + 3Y_{Q'^j}^2 X_{Q'^j}) - \sum_{i,j} (Y_{l^i}^2 X_{l^i} + 3Y_{q'^j}^2 X_{q'^j}). \quad (2c)$$

$$[U(1)_Y][U(1)_X]^2 = \sum_{i,j} (Y_{L^i} X_{L^i}^2 + 3Y_{Q'^j} X_{Q'^j}^2) - \sum_{i,j} (Y_{l^i} X_{l^i}^2 + 3Y_{q'^j} X_{q'^j}^2). \quad (2d)$$

$$[U(1)_X]^3 = \sum_{i,j} (X_{L^i}^3 + 3X_{Q'^j}^3) - \sum_{i,j} (X_{l^i}^3 + 3X_{q'^j}^3). \quad (2e)$$

$$[G]^2[U(1)_X] = \sum_{i,j} (X_{L^i} + 3X_{Q'^j}) - \sum_{i,j} (X_{l^i} + 3X_{q'^j}). \quad (2f)$$

- There are many solutions to these anomaly cancellation conditions
- **$L_i - L_j$  Solutions:** One of the popular solution which is very well studied
- The charges of SM fermions under  $U(1)_X$  symmetry are given by<sup>2</sup>

$$\begin{aligned} X_{L^i} &= -X_{L^j} = X, X_{L^k} = 0; & i, j, k &= 1, 2, 3 \text{ \& } i \neq j \neq k \\ X_{e_R^l} &= -X_{e_R^m} = X, X_{e_R^n} = 0; & l, m, n &= 1, 2, 3 \text{ \& } l \neq m \neq n \\ X_{Q^i} &= X_{q^j} = 0; & i, j &= 1, 2, 3 \quad \forall i, j. \end{aligned}$$

- This is a vector solution with  $U(1)_X$  charges of left and right handed fermions being same.
- One unique feature of this solution is that no new BSM fermion is needed to cancel the anomalies

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<sup>2</sup>X. G. He, G. C. Joshi, H. Lew, and R. R. Volkas; Phys. Rev. D. 43 (1991) 22-24

# $U(1)_X$ Anomaly Cancellation Conditions: **B – L Solution**

- There are several known solutions which require presence of new BSM fermions (typically right handed neutrinos) to cancel anomalies
- **B – L Solution:** The  $B - L$  solution is one of the oldest and most popular solution
- The charges of SM and right handed BSM fermion ( $f_i$ ;  $i = 1, 2, 3$ ) are given by

$$\begin{aligned} X_{Q^i} &= X_{q^j} = 1/3; \quad i, j, k = 1, 2, 3, \\ X_{L^i} &= X_{\ell^j} = X_{f^i} = -1; \quad \forall i, j. \end{aligned}$$

- Notice that again its a vector solution with  $U(1)_X$  charges of the BSM fermion  $f_i$  being same as that of SM neutrinos.
- Its also a "flavor blind" symmetry with  $B - L$  charges of each generation being same.
- During phenomenology part of the talk, I will use the equivalent results of the  $B - L$  case as the reference to compare with our results



# $U(1)_X$ Anomaly Cancellation Conditions: Other Solutions

- There are several other solutions: I will just list some of the other popular ones

- $B - 3L_i$ : Charges are<sup>3</sup>

$$X_{Qi} = X_{qj} = 1/3; \quad i, j = 1, 2, 3,$$

$$X_{Li} = X_{l_i} = X_f = -3, \quad X_{Lk} = X_{l_k} = 0; \quad i, k = 1, 2, 3 \text{ \& } i \neq k.$$

- $B_i - 3L_j$ : Charges are<sup>4</sup>

$$X_{Qi} = X_{q_i} = 1, \quad X_{Qj} = X_{q_j} = 0; \quad i, j = 1, 2, 3 \text{ \& } i \neq j,$$

$$X_{Lj} = X_{l_j} = X_f = -3, \quad X_{Lk} = X_{l_k} = 0; \quad j, k = 1, 2, 3 \text{ \& } j \neq k.$$

- Variants such as  $B - 2L_i - L_j$ ,  $B - \frac{3}{2}(L_i + L_j)$ ,  
 $B_1 - yB_2 + (y - 3)B_3 + L_i + L_j$  etc. are also possible
- One common feature of all these solutions is that they are all vector solutions i.e. the  $U(1)_X$  charges of left and right handed fermions of a given type are same
- Are chiral solutions analogous to hypercharge solution in SM case possible?

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<sup>3</sup>E. Ma, Phys. Lett. B 433 (1998) 74–81,

<sup>4</sup>C. Bonilla, T. Modak, R. Srivastava, and J. W. F. Valle, Phys. Rev. D 98 no. 9, (2018) 095002

- 1 Introduction
- 2 Anomalies in SM: Uniqueness of Hypercharge
- 3  $U(1)_X$  anomaly cancellation: Known Solutions
- 4  $U(1)_X$  anomaly cancellation: Dark Hypercharge Symmetry**
- 5 The Dark  $Z'$  Gauge Boson
- 6 The Dark Sector
- 7 Constraining Light  $Z'$
- 8 Conclusion

# $U(1)_X$ Anomaly Cancellation Conditions: Chiral Solutions

- The chiral solutions have not been explored much in literature
- One of the known chiral solutions is for the  $B - L$  symmetry<sup>5</sup> where the BSM fermions  $f_i$ ;  $i = 1, 2, 3$  have  $U(1)_X$  charges of  $+4, +4, -5$
- We also found that one can also have chiral solutions for gauged Baryon ( $U(1)_B$ ) and Lepton ( $U(1)_L$ ) symmetries
- All these solutions although chiral, are very limited in their chirality
- In all of them the SM fermions are still vector under  $U(1)_X$  symmetry and only BSM fermions have exotic  $U(1)_X$  charges
- This is in contrast of the SM hypercharge case where the left and right counterpart of all types are fermions have different hypercharges
- Are similar solutions for  $U(1)_X$  symmetries possible?

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<sup>5</sup>J. C. Montero and V. Pleitez; Phys. Lett. B 675 (2009) 64–68; E. Ma and R. Srivastava, Phys. Lett. B 741 (2015) 217–222; E. Ma and R. Srivastava, Mod. Phys. Lett. A 30 no. 26, (2015) 1530020, E. Ma, N. Pollard, R. Srivastava, and M. Zakeri, Phys. Lett. B 750 (2015) 135–138

- Such solutions are indeed possible.
- In fact we have found a whole class of hitherto unknown solutions, all completely chiral in their  $U(1)_X$  charge assignments <sup>6</sup>
- We call them Dark Hypercharge Solutions:
- Like Hypercharge, left and right handed counterparts of all fermions have different  $U(1)_X$  charges
- They require addition of SM gauge singlet BSM fermions  $f_i$
- These BSM fermions can belong to the dark sector with the lightest of them being a good dark matter symmetry
- The associated gauge boson  $Z'$  connects the dark sector to visible sector: Hence Dark Hypercharge

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<sup>6</sup>H. Prajapati, R.S., arXiv: 2411.02512 [hep-ph]

- We have obtained class of solutions of under three different scenarios :
  - **S(I)** : Only one generation of SM fermions is charged under  $U(1)_X$  ( $X_{\psi^i} = X_{\psi^j} = 0, X_{\psi^k} = X, \quad i, j, k = 1, 2, 3 \text{ \& } i, j \neq k$ ).
  - **S(II)** : Two generations share the same charge under  $U(1)_X$ , while one generation remains uncharged ( $X_{\psi^i} = X_{\psi^j}, X_{\psi^k} = 0, \quad i, j, k = 1, 2, 3 \text{ \& } i, j \neq k$ ).
  - **S(III)** : All three generations of SM fermions are charged under the new symmetry, and their charges are identical across generations ( $X_{\psi^i} = X_{\psi^j} = X_{\psi^k}, \quad i, j, k = 1, 2, 3$ ).
- In addition we demand that the masses of SM fermions are generated through the SM Higgs boson itself. No BSM scalar needed for SM fermion mass generation

- For one generation (S(I)) case we get only one solution:

$Q$	$u_R$	$d_R$	$L$	$e_R$	$f_1$	$f_2$	$f_3$	$\Phi$
$\frac{-X_L}{3}$	$\frac{2X_L}{3} - X_{e_R}$	$\frac{-4X_L}{3} + X_{e_R}$	$X_L$	$X_{e_R}$	$k$	$-k$	$2X_L - X_{e_R}$	$X_L - X_{e_R}$

- For two generation (S(II)) case we get following solutions:

$Q$	$u_R$	$d_R$	$L$	$e_R$	$f_1$	$f_2$	$f_3$	$\Phi$
$\frac{-X_L}{3}$	$\frac{-4X_L}{3}$	$\frac{2X_L}{3}$	$X_L$	$2X_L$	0	$k$	$-k$	$-X_L$
$\frac{-X_L}{3}$	$\frac{2X_L}{3} - X_{e_R}$	$\frac{-4X_L}{3} + X_{e_R}$	$X_L$	$X_{e_R}$	0	$2X_L - X_{e_R}$	$2X_L - X_{e_R}$	$X_L - X_{e_R}$

- For three generation (S(III)) case we get following solutions:

$Q$	$u_R$	$d_R$	$L$	$e_R$	$f_1$	$f_2$	$f_3$	$\Phi$
$\frac{-X_L}{3}$	$\frac{-4X_L}{3}$	$\frac{2X_L}{3}$	$X_L$	$2X_L$	0	$\kappa$	$-\kappa$	$-X_L$
$-\frac{X_L}{3}$	$-\frac{4X_L}{3} + \kappa$	$\frac{2X_L}{3} - \kappa$	$X_L$	$2X_L - \kappa$	$\kappa$	$\kappa$	$\kappa$	$\kappa - X_L$
$\frac{1}{s}$	$-(\kappa - \frac{4}{s})$	$\kappa - \frac{2}{s}$	$-\frac{3}{s}$	$\kappa - \frac{6}{s}$	$5\kappa$	$-4\kappa$	$-4\kappa$	$-(\kappa - \frac{3}{s})$
$-\frac{X_L}{3}$	$\frac{-4X_L}{3} - \frac{s^2 - \kappa^2}{8}$	$\frac{2X_L}{3} + \frac{s^2 - \kappa^2}{8}$	$X_L$	$2X_L + \frac{s^2 - \kappa^2}{8}$	$\frac{1}{8}(-4s^2 + 3s\kappa + \frac{\kappa^3}{s})$	$\frac{1}{8}(5s^2 + 3\kappa^2)$	$-\frac{1}{8}(4s^2 + 3s\kappa + \frac{\kappa^3}{s})$	$-X_L + \frac{\kappa^2 - s^2}{8}$

- As you can see,  $U(1)_X$  charges of all fermions are chiral
- We need three dark sector BSM fermions  $f_i$ ;  $i = 1, 2, 3$  to cancel anomalies
- Mass of all SM fermions can be generated just with the SM Higgs boson

- In all cases all fermions have completely chiral  $U(1)_X$  charges
- We always need three dark sector fermions to cancel anomalies
- Only SM Higgs is enough to generate mass of all SM fermions
- To make the dark sector gauge boson massive, we need to add another SM singlet scalar
- Masses of dark sector fermions can also be generated by addition of SM gauge singlet scalars
- Let's now look at the phenomenological aspects of the Dark Hypercharge Symmetry



- 1 Introduction
- 2 Anomalies in SM: Uniqueness of Hypercharge
- 3  $U(1)_X$  anomaly cancellation: Known Solutions
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- 6 The Dark Sector
- 7 Constraining Light  $Z'$
- 8 Conclusion

- The covariant derivative is defined as

$$D_\mu = \partial_\mu + ig_s T_g^a G_\mu^a + ig T_w^a W_\mu^a + ig' \frac{Y}{2} B_\mu + ig_x X C_\mu. \quad (3)$$

where

$$\langle \phi \rangle = \frac{1}{\sqrt{2}} \begin{bmatrix} 0 \\ v \end{bmatrix}, \quad \langle \chi_i \rangle = \frac{v_i}{\sqrt{2}}. \quad (4)$$

- The mass spectrum of the gauge bosons are generated by the expansion of the kinetic terms of the scalars, as given below

$$(D_\mu)^\dagger D^\mu + (D_\mu \chi_i)^\dagger D^\mu \chi_i, \quad (5)$$

- We can write the mass matrix of the gauge bosons in the basis  $(B^\mu, W_3^\mu, C^\mu)$  as

$$\mathcal{M}_v^2 = \frac{v^2}{4} \begin{pmatrix} g'^2 & -gg' & 2g'X_\phi g_x \\ -gg' & g^2 & -2gX_\phi g_x \\ 2g'X_\phi g_x & -2gX_\phi g_x & 4u^2 g_x^2 \end{pmatrix}, \quad (6)$$

where  $u^2 = X_\phi^2 + u_\chi^2/v^2$ , and  $u_\chi$  is defined as  $u_\chi = \sqrt{\sum_i (X_{\chi_i}^2 v_i^2)}$ .

- The mass eigen states are given by

$$m^2 = \frac{v^2}{8}(A_0 - \sqrt{B_0^2 + C_0^2}), \quad M^2 = \frac{v^2}{8}(A_0 + \sqrt{B_0^2 + C_0^2}), \quad (7)$$

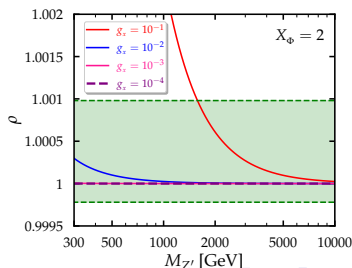
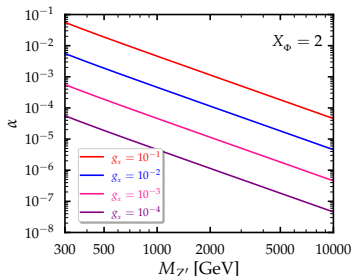
where  $A_0 = g^2 + g'^2 + 4u^2 g_x^2$ ,  $B_0 = 4X_\phi g_x \sqrt{g^2 + g'^2}$ ,  $C_0 = 4u^2 g_x^2 - (g^2 + g'^2)$ .

And the  $W$  boson mass is given as  $M_W^2 = (gv)^2/4$ .

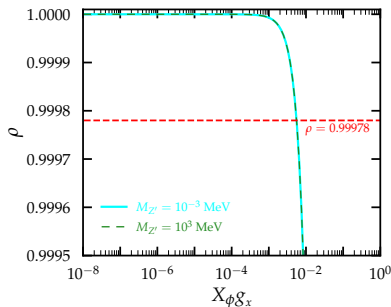
- The ratio of gauge boson masses is measured through the parameter

$$\rho' = \frac{\rho}{\cos^2 \alpha + \left(\frac{M_{Z'}}{M_Z}\right)^2 \sin^2 \alpha} = 1. \quad \rho - 1 = \left[ \left(\frac{M_{Z'}}{M_Z}\right)^2 - 1 \right] \sin^2 \alpha.$$

- For the case of  $M_{Z'}[g_x, u_\chi] > M_Z[g_x, u_\chi]$



- For the case of  $M_{Z'}[g_x, u_\chi] < M_Z[g_x, u_\chi]$ 
  - The  $\rho$  parameter could be approximated as,  $\rho \approx \left(1 + \frac{4X_\phi^2 g_x^2}{g^2 + g'^2}\right)^{-1}$
  - This implies that the  $\rho$  parameter is independent of  $M_{Z'}$



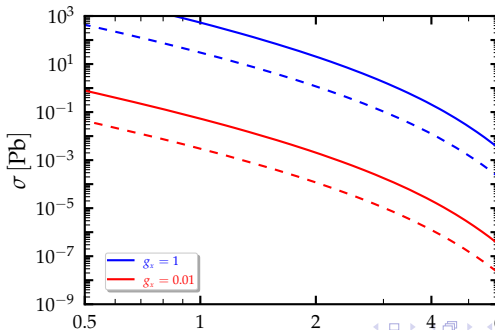
- In the low mass limit of  $M_{Z'}$ ,  $X_\phi g_x \lesssim 5.5 \times 10^{-3}$  is adequate to satisfy the  $\rho$  parameter,  $M_{Z'} \approx u_\chi g_x$ .

# Production and decays of $Z'$

- To be concrete henceforth we take one of the models of the S(III) type to do the phenomenological studies. The charges of particles are

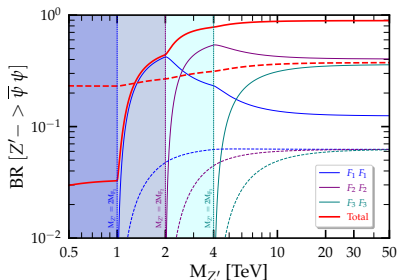
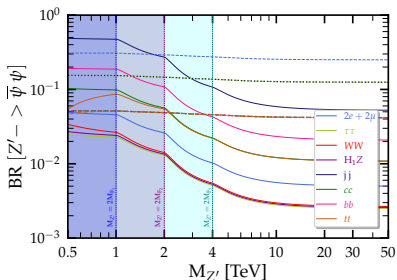
$U(1)$	$Q$	$u_R$	$d_R$	$L$	$e_R$	$f_1$	$f_2$	$f_3$	$\Phi$	$\chi_0$
$U(1)_Y$	$\frac{1}{3}$	$\frac{4}{3}$	$-\frac{2}{3}$	$-1$	$-2$	$0$	$0$	$0$	$1$	$0$
$U(1)_X$	$-\frac{1}{3}$	$\frac{5}{3}$	$-\frac{7}{3}$	$1$	$-1$	$10$	$-18$	$17$	$2$	$-6$

- In hadronic colliders the most efficient process involving  $Z'$  production is Drell-Yan  $q\bar{q} \rightarrow Z'$ ,

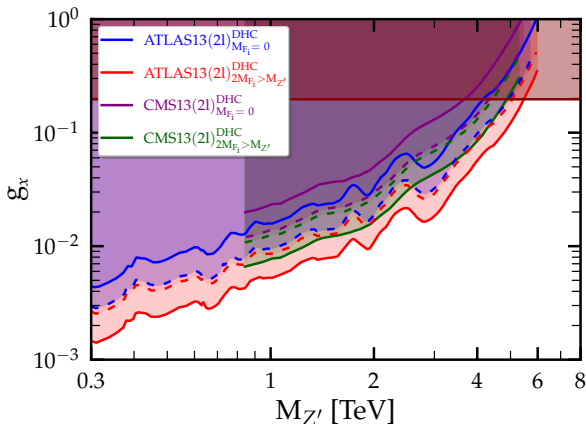


# Production and decays of $Z'$

- In the DHC symmetry, the total branching fraction of invisible decay is approximately 90% when the branching fraction saturates. In contrast, in the  $B - L$  symmetry, it is about 38%.
- In the fermionic decay modes, the dileptonic branching fraction, is much smaller in DHC (0.5%) compared to say  $B - L$  (25%).



- We used the ATLAS<sup>7</sup> and CMS<sup>8</sup> search for  $Z'$  in Dilepton resonance at  $pp$  collisions with ( $\sqrt{s} = 13$ ) TeV and an integrated luminosity of  $139 \text{ fb}^{-1}$ .



<sup>7</sup>ATLAS Collaboration, Phys. Lett. B 796 (2019) 68–87,

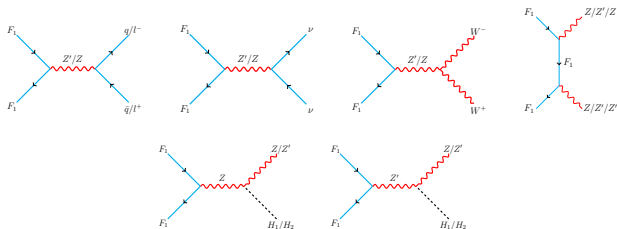
<sup>8</sup>CMS Collaboration, JHEP 07 (2021) 208

- 1 Introduction
- 2 Anomalies in SM: Uniqueness of Hypercharge
- 3  $U(1)_X$  anomaly cancellation: Known Solutions
- 4  $U(1)_X$  anomaly cancellation: Dark Hypercharge Symmetry
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- 6 The Dark Sector**
- 7 Constraining Light  $Z'$
- 8 Conclusion

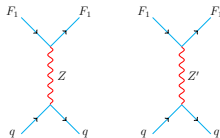


# Dark Matter Constraints

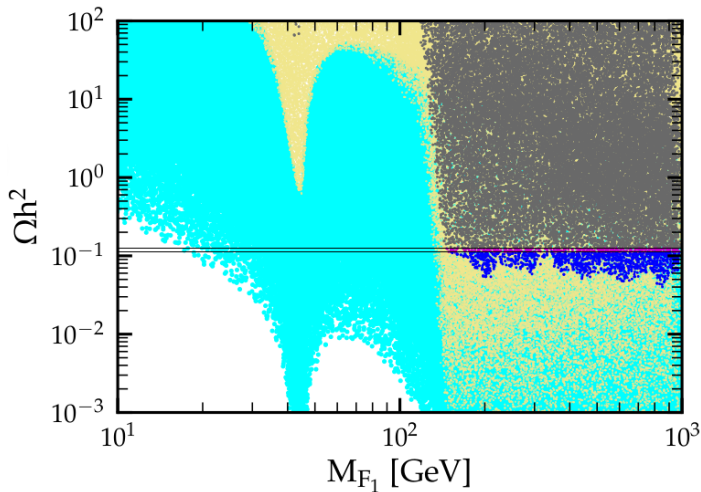
- As mentioned before, the BSM fermions  $f_i$ ;  $i = 1, 2, 3$  belong to the dark sector and the lightest of them can be dark matter
- The charges and interaction strength of the dark matter to all SM particles is completely fixed by the anomaly cancellation conditions. This makes the model highly predictive
- Feynman diagram contributing to DM annihilation



- Feynman Diagrams Contributing to DM-nucleon Scattering



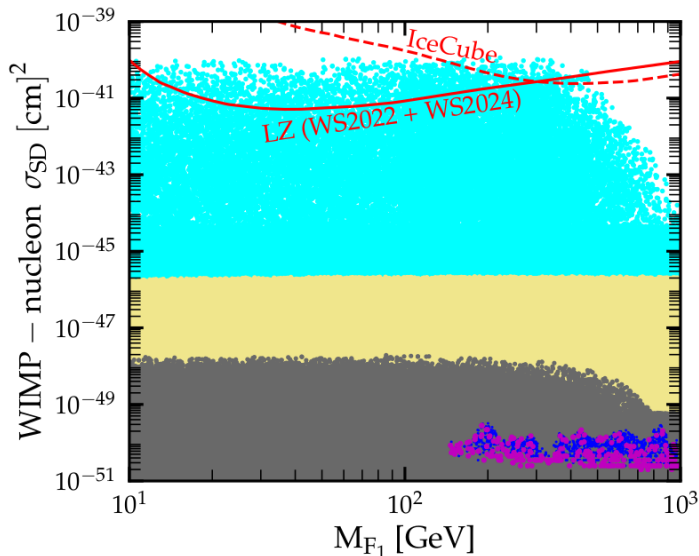
- Measured Relic Abundance<sup>9</sup>  $0.1126 \leq \Omega h^2 \leq 0.1246$ .



<sup>9</sup>Planck Collaboration, 641 (2020) A6

# Direct Detection Constraints

- Direct Detection Constraints<sup>10</sup>

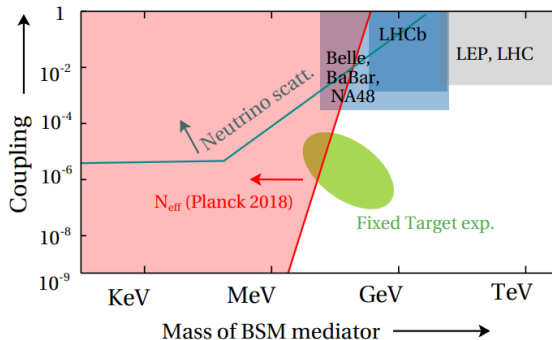


<sup>10</sup>IceCube Collaboration, Eur. Phys. J. C 77 no. 3, (2017) 146

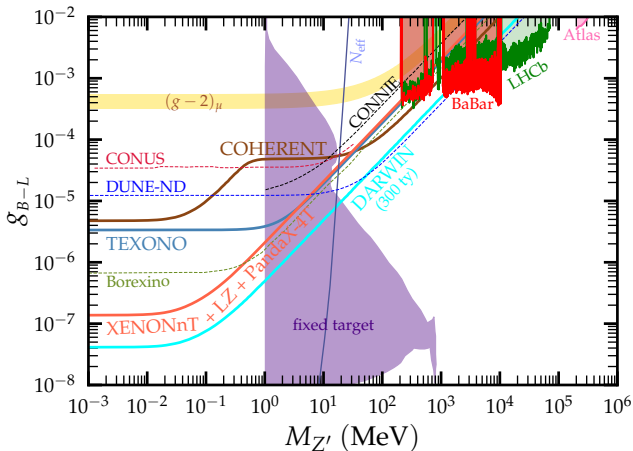
LUX-ZEPLIN Collaboration, Phys. Rev. Lett. 131 no. 4, (2023) 041002

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- 2 Anomalies in SM: Uniqueness of Hypercharge
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- Light  $Z'$  can be constrained from different experiments like Direct Detection Experiments, Fixed target experiments, Supernovae Cooling,  $N_{\text{eff}}$  etc.

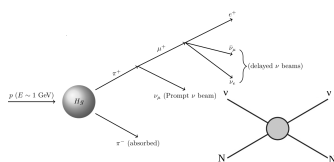


- As an example the parameter space for coupling and mass of the  $Z'$  from gauged  $B - L$  has been constrained through various experiments<sup>11</sup>

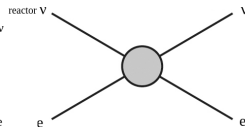
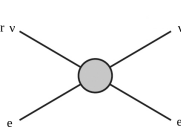


<sup>11</sup>Anirban Majumdar, Dimitrios K. Papoulias, Hemant Prajapati, Rahul Srivastava;  
Phys.Rev.D 111 (2025) 7, 073006 • e-Print: 2411.04197 [hep-ph]

# $CE\nu NS$ and $E\nu ES$ constraints on Light $Z'$ from Dark HyperCharge Symmetry



Solar  $\nu$



- **Experiment:**  
**COHERENT**

- $\nu$  Source:  $\pi$ -DAR,  $\mu$ -DAR
- Target: LAr (2020 data), Csl (2021 data)
- Relevant Interaction:  **$CE\nu NS$ ,  $E\nu ES$**

- **Experiment:**  
**XENONnT, LZ, PandaX-4T, and DARWIN** ( future sensitivity)

- $\nu$  Source: Solar  $\nu_e$
- Target: LXe TPC
- Relevant Interaction:  **$E\nu ES$**

- **Experiment:**  
**TEXONO**

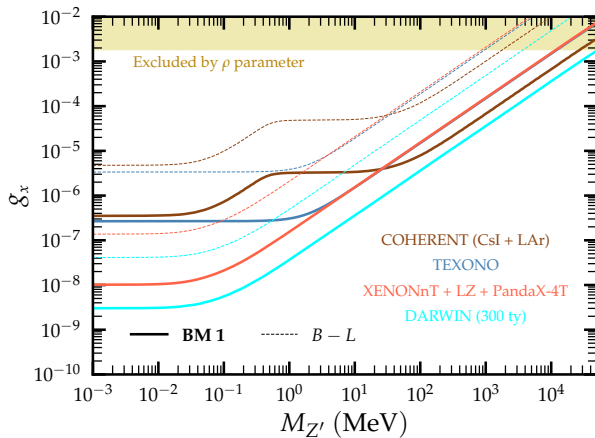
- $\nu$  Source: Reactor  $\bar{\nu}_e$
- Target: Csl
- Relevant Interaction:  **$E\nu ES$**

# Benchmark Dark Hypercharge Models

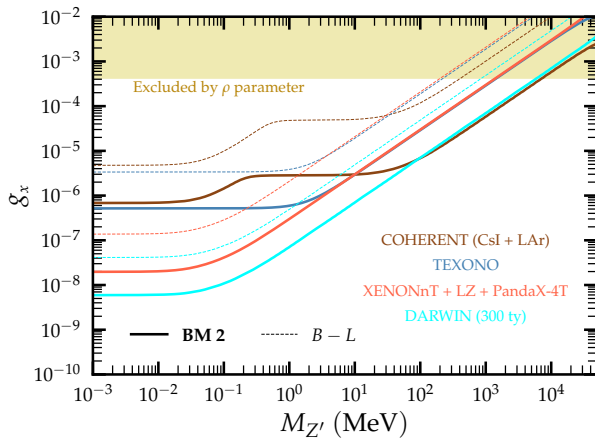
Fields	Hypercharge (Y)	Weak Isospin (T <sup>3</sup> )	U(1) <sub>X</sub> Charge			
			BM 1	BM 2	BM 3	B - L
$u_L$	1/3	1/2	-13/3	-3	-1/3	1/3
$u_R$	4/3	0	-4/3	10	5/3	1/3
$d_L$	1/3	-1/2	-13/3	-3	-1/3	1/3
$d_R$	-2/3	0	-22/3	-16	-7/3	1/3
$e_L$	-1	-1/2	13	9	1	-1
$e_R$	-2	0	10	-4	-1	-1
$\nu_L$	-1	1/2	13	9	1	-1
$f^1$	0	0	16	-110	10	-1
$f^2$	0	0	16	88	-18	-1
$f^3$	0	0	16	88	17	-1
$\phi$	1	-	3	13	2	0



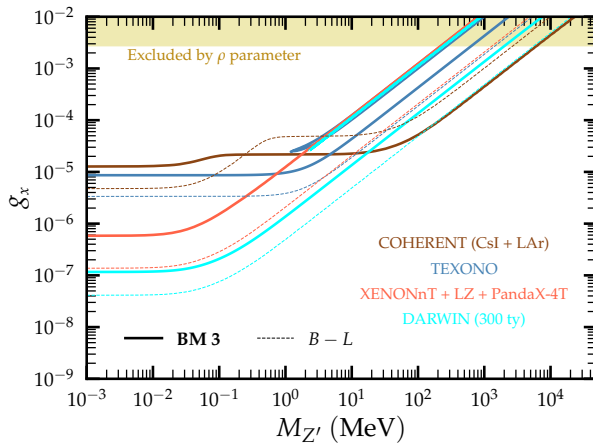
# $CE\nu NS$ and $E\nu ES$ constraints on $Z'$ from BM 1



# CE $\nu$ NS and E $\nu$ ES constraints on $Z'$ from BM 2



# $CE\nu NS$ and $E\nu ES$ constraints on $Z'$ from BM 3



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- Extensions of the Standard Model with  $U(1)_X$  gauge symmetries are strongly motivated.
- The charges of SM fermions are constrained by anomaly cancellation conditions, making  $U(1)_X$  models highly predictive.
- I discussed a new class of models where all SM fermions have chiral charges under the  $U(1)_X$  symmetry.
- The anomaly cancellation necessitates need to add three BSM fermions which can be identified as dark fermions with the lightest of them being a good dark matter candidate.
- I also discussed the phenomenological signatures of certain Benchmark Models for both heavy and light  $Z'$  cases.
- These dark hypercharge models can be tested in various experiments.

Thank You