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Flavored Peccei-Quinn symmetries in the minimal vDFSZ model

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 $\underbrace{ \mathcal{L}_{\mathrm{I}} = \mathcal{L}_{\mathrm{SM}} + i\overline{\nu_{R}}\gamma^{\mu}\partial_{\mu}\nu_{R} - \left(\overline{\ell_{L}}\mathbf{Y}_{\nu}^{*}\widetilde{\Phi}\nu_{R} + \frac{1}{2}\overline{\nu_{R}}\mathbf{M}_{R}\nu_{R}^{c} + \mathrm{H.c.} \right) }$

$\mathcal{L}_{\mathrm{I}} = \mathcal{L}_{\mathrm{SM}} + i\overline{\nu_{R}}\gamma^{\mu}\partial_{\mu}\nu_{R} - \left(\overline{\ell_{L}}\mathbf{Y}_{\nu}^{*}\widetilde{\Phi}\nu_{R} + \frac{1}{2}\overline{\nu_{R}}\mathbf{M}_{R}\nu_{R}^{c} + \mathrm{H.c.}\right)$











Majorana Mass Eigenstates

$$\mathbf{M}_{\nu}^{\mathrm{I}} = -\frac{v^{2}}{2} \mathbf{Y}_{\nu} \mathbf{M}_{R}^{-1} \mathbf{Y}_{\nu}^{T}$$
$$\mathbf{U}_{L}^{\nu T} \mathbf{M}_{\nu}^{\mathrm{I}} \mathbf{U}_{L}^{\nu} = \operatorname{diag}\left(m_{1}, m_{2}, m_{3}\right)$$



2



The lightest neutrino is predicted to be massless!

Global U(1)_{PQ}

 $\Phi_k \to \exp\left(i\zeta\chi_k\right)\Phi_k , \quad q_{L_{\alpha}} \to \exp\left(i\zeta\chi_{q_{\alpha}}^L\right)q_{L_{\alpha}} , \quad d_{R_{\alpha}} \to \exp\left(i\zeta\chi_{d_{\alpha}}^R\right)d_{R_{\alpha}} , \quad u_{R_{\alpha}} \to \exp\left(i\zeta\chi_{u_{\alpha}}^R\right)u_{R_{\alpha}} \\ \sigma \to \exp\left(i\zeta\chi_{\sigma}\right)\sigma , \qquad \ell_{L_{\alpha}} \to \exp\left(i\zeta\chi_{\ell_{\alpha}}^L\right)\ell_{L_{\alpha}} , \quad e_{R_{\alpha}} \to \exp\left(i\zeta\chi_{e_{\alpha}}^R\right)e_{R_{\alpha}} , \quad \nu_{R_{j}} \to \exp\left(i\zeta\chi_{\nu_{j}}^R\right)\nu_{R_{j}}$

2HDM

$$\Phi_{1,2} = \frac{1}{\sqrt{2}} \begin{pmatrix} \phi_{1,2}^+ \\ (v_{1,2} + \rho_{1,2}) e^{ia_{1,2}/v_{1,2}} \end{pmatrix}$$

Complex Singlet

$$\sigma = \frac{1}{\sqrt{2}} \left(v_{\sigma} + \rho_{\sigma} \right) e^{i a_{\sigma} / v_{\sigma}}$$

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Complex Singlet

$$\sigma = \frac{1}{\sqrt{2}} \left(v_{\sigma} + \rho_{\sigma} \right) e^{ia_{\sigma}/v_{\sigma}}$$

$$a = \frac{1}{v_a} \sum_{i=1,2,\sigma} \chi_i a_i v_i$$

Global U(1)_{PQ} $\Phi_k \to \exp\left(i\zeta\chi_k\right)\Phi_k \ , \ \ q_{L_{\alpha}} \to \exp\left(i\zeta\chi_{q_{\alpha}}^L\right)q_{L_{\alpha}} \ , \ \ d_{R_{\alpha}} \to \exp\left(i\zeta\chi_{d_{\alpha}}^R\right)d_{R_{\alpha}} \ , \ \ u_{R_{\alpha}} \to \exp\left(i\zeta\chi_{u_{\alpha}}^R\right)u_{R_{\alpha}} \\ \sigma \to \exp\left(i\zeta\chi_{\sigma}\right)\sigma \ , \qquad \ell_{L_{\alpha}} \to \exp\left(i\zeta\chi_{\ell_{\alpha}}^L\right)\ell_{L_{\alpha}} \ , \ \ e_{R_{\alpha}} \to \exp\left(i\zeta\chi_{e_{\alpha}}^R\right)e_{R_{\alpha}} \ , \ \ \nu_{R_{j}} \to \exp\left(i\zeta\chi_{\nu_{j}}^R\right)\nu_{R_{j}}$ 2HDM **Complex Singlet** $\sigma = \frac{1}{\sqrt{2}} \left(v_{\sigma} + \rho_{\sigma} \right) e^{i a_{\sigma} / v_{\sigma}}$ $\Phi_{1,2} = \frac{1}{\sqrt{2}} \begin{pmatrix} \phi_{1,2}^+ \\ (v_{1,2} + \rho_{1,2}) e^{ia_{1,2}/v_{1,2}} \end{pmatrix}$ $a = \frac{1}{v_a} \sum_{i=1,2,\sigma} \chi_i a_i v_i \quad \xrightarrow{\text{Mass Basis}} \quad \mathcal{L}_{\theta} = \left(\bar{\theta} + \frac{Na}{v_a}\right) \frac{g_s^2}{32\pi^2} G^a_{\mu\nu} \tilde{G}^{\mu\nu}_a$



Global U(1)_{PQ} $\Phi_k \to \exp\left(i\zeta\chi_k\right)\Phi_k \,, \quad q_{L_{\alpha}} \to \exp\left(i\zeta\chi_{q_{\alpha}}^L\right)q_{L_{\alpha}} \,, \quad d_{R_{\alpha}} \to \exp\left(i\zeta\chi_{d_{\alpha}}^R\right)d_{R_{\alpha}} \,, \quad u_{R_{\alpha}} \to \exp\left(i\zeta\chi_{u_{\alpha}}^R\right)u_{R_{\alpha}}$ $\sigma \to \exp\left(i\zeta\chi_{\sigma}\right)\sigma \,, \qquad \ell_{L_{\alpha}} \to \exp\left(i\zeta\chi_{\ell_{\alpha}}^L\right)\ell_{L_{\alpha}} \,, \quad e_{R_{\alpha}} \to \exp\left(i\zeta\chi_{e_{\alpha}}^R\right)e_{R_{\alpha}} \,, \quad \nu_{R_{j}} \to \exp\left(i\zeta\chi_{\nu_{j}}^R\right)\nu_{R_{j}}$ 2HDM **Complex Singlet** $\sigma = \frac{1}{\sqrt{2}} \left(v_{\sigma} + \rho_{\sigma} \right) e^{i a_{\sigma} / v_{\sigma}}$ $\Phi_{1,2} = \frac{1}{\sqrt{2}} \left(\frac{\phi_{1,2}^+}{(v_{1,2} + \rho_{1,2})} e^{ia_{1,2}/v_{1,2}} \right)$ $a = \frac{1}{v_a} \sum_{i=1,2,\sigma} \chi_i a_i v_i \quad \xrightarrow{\text{Mass Basis}} \quad \mathcal{L}_{\theta} = \left(\swarrow + \frac{Na}{v_a} \right) \frac{g_s^2}{32\pi^2} G^a_{\mu\nu} \tilde{G}^{\mu\nu}_a$ In the Low energy effective theory $\langle a \rangle_{k=0,1,...,N_{\rm DW}-1} = (-1 + 2\pi k) v_a / N_{\rm DW}$ $m_a = 5.70(7) \left(\frac{10^{12} \text{GeV}}{f}\right) \mu \text{eV}$

The Strong CP Problem is solved

Axions are naturally light, weakly coupled with ordinary matter, cosmologically stable, and can be nonthermally produced in the early Universe being an excellent DM candidate

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Cosmological Scenarios for Axion Production

Axion dark matter via the misalignment mechanism in the pre-inflationary scenario

$$\Omega_a h^2 \simeq \Omega_{\rm CDM} h^2 \frac{\theta_0^2}{2.15^2} \left(\frac{f_a}{2 \times 10^{11} {\rm GeV}} \right)^{\frac{1}{2}}$$

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And in the post-inflationary scenario

 $\left< \theta_0^2 \right> \simeq 2.15^2$

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Cosmological Scenarios for Axion Production



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Cosmological Scenarios for Axion Production



$$-\mathcal{L}_{\text{mass}} = \overline{d_L} \mathbf{M}_d d_R + \overline{u_L} \mathbf{M}_u u_R + \overline{e_L} \mathbf{M}_e e_R + \overline{\nu_L} \mathbf{M}_D^* \nu_R + \frac{1}{2} \overline{\nu_R} \mathbf{M}_R \nu_R^c + \text{H.c.}$$



$$-\mathcal{L}_{\text{mass}} = \overline{d_L} \mathbf{M}_d d_R + \overline{u_L} \mathbf{M}_u u_R + \overline{e_L} \mathbf{M}_e e_R + \overline{\nu_L} \mathbf{M}_D^* \nu_R + \frac{1}{2} \overline{\nu_R} \mathbf{M}_R \nu_R^c + \text{H.c.}$$



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$$-\mathcal{L}_{\text{mass}} = \overline{d_L} \mathbf{M}_d d_R + \overline{u_L} \mathbf{M}_u u_R + \overline{e_L} \mathbf{M}_e e_R + \overline{\nu_L} \mathbf{M}_D^* \nu_R + \frac{1}{2} \overline{\nu_R} \mathbf{M}_R \nu_R^c + \text{H.c.}$$



Procedure

Equivalence classes with the maximum number of zeros

Procedure



Procedure	Experim	ental Data	
TIOCEUUIE	Parameter	Best fit $\pm 1\sigma$	
	$m_d(imes \mathrm{MeV})$	$4.67^{+0.48}_{-0.17}$	
ence classes with	$m_s(imes \mathrm{MeV})$	$93.4_{-3.4}^{+8.6}$	
vinum number of	$m_b(\times \text{ GeV})$	$4.18\substack{+0.03\\-0.02}$	C
	$m_u(\times \text{MeV})$	$2.16^{+0.49}_{-0.26}$	ž
zeros	$m_c(imes { m GeV})$	1.27 ± 0.02	0
	$m_t(imes ext{GeV})$	172.69 ± 0.30	2
↓	$ heta_{12}^q(^\circ)$	13.04 ± 0.05	(
•	$ heta_{23}^q(\circ)$	2.38 ± 0.06	
e system of equations	$ heta_{13}^q(\circ)$	0.201 ± 0.011	
e PO charges	$\qquad \qquad $	68.75 ± 4.5	
	Parameter	Best Fit $\pm 1\sigma$;
L	$m_e(\times \text{keV})$	$510.99895000 \pm 0.00000015$	
•	$m_\mu(imes { m MeV})$	$105.6583755 \pm 0.0000023$	
mpatibility at the 1σ	$m_{ au}(imes { m GeV})$	1.77686 ± 0.00012	
all observables	$\Delta m_{21}^2 \left(\times 10^{-5} \ {\rm eV}^2 \right)$	$7.50^{+0.22}_{-0.20}$	Γ
	$ \Delta m_{31}^2 \left(\times 10^{-3} \text{ eV}^2 \right) [\text{NO}]$	$2.55^{+0.02}_{-0.03}$	ת ד
	$ \Delta m_{31}^2 \left(\times 10^{-3} \text{ eV}^2 \right) [\text{IO}]$	$2.45_{-0.03}^{+0.02}$	
	$ heta_{12}^\ell(\circ)$	34.3 ± 1.0	
	$ heta_{23}^{\ell}(^{\circ})[\mathrm{NO}]$	49.26 ± 0.79	Ū
	$\theta_{23}^{\ell}(^{\circ})[\mathrm{IO}]$	$49.46^{+0.00}_{-0.97}$	
	$\theta_{13}^{(\circ)}[\text{NO}]$	$8.53^{+0.12}_{-0.12}$	
	$\theta_{13}^{\circ}(^{\circ})[\mathrm{IO}]$	$8.58_{-0.14}$	

 $\delta^{\ell}(^{\circ})[NO]$

 $\delta^{\ell}(^{\circ})[IO]$

 $194^{+24}_{-22} \\ 284^{+26}_{-28}$





Maximally-Restrictive Quark Textures

U(1) charges	Maximally restrictive mass matrices
Model $(\mathbf{M}_d, \mathbf{M}_u)$ $\chi_{q_\alpha}^L + \frac{s_\beta^2}{3} \chi_{d_\alpha}^R - \frac{2s_\beta^2}{3} \chi_{u_\alpha}^R + \frac{4s_\beta^2}{3}$	$4_3^d \sim \begin{pmatrix} 0 & 0 & \times \\ 0 & \times & \times \end{pmatrix}$
$\begin{array}{c cccc} & Q_{1}^{\mathrm{I}} & & (0,1,2) & (2,1,0) & (3,2,0) \\ & Q_{1}^{\mathrm{II}} & & (0,-1,-2) & (-3,-2,-1) & (-2,-1,1) \end{array}$	$ \begin{array}{cccc} \left(\times & \times & 0\right) \\ & & \left(\begin{array}{cccc} & \times & \times & 0\\ & & \left(\begin{array}{cccc} & 0 & 0 & \times\\ & & 0 & \times & 0\end{array}\right) \end{array} $
$\begin{array}{c c} Q_2^{\rm I} & (0,1,2) & (2,1,0) & (3,0,1) \\ Q_2^{\rm II} & (0,-1,-2) & (-3,-2,-1) & (-2,1,0) \end{array}$	$ = \frac{\left(\times 0 \times \right)}{\left(\begin{array}{c} 0 0 \times \end{array} \right)} $
$\begin{array}{c ccccccccccccccccccccccccccccccccccc$	$ \begin{bmatrix} \mathbf{P}_{12} \mathbf{b}_{1}^{a} \mathbf{P}_{23} \sim \begin{pmatrix} 0 & \bullet & 0 \\ \times & \times & 0 \end{pmatrix} \\ \begin{pmatrix} 0 & \times & \bullet \end{pmatrix} $
$\begin{array}{c c} & & & & & & & & & & & & & & & & & & &$	$\mathbf{P}_{123}5_1^u \mathbf{P}_{12} \sim \begin{pmatrix} 0 & 0 & \times \\ \times & 0 & 0 \end{pmatrix}$ $\begin{pmatrix} 0 & \bullet & \times \\ & & & & \end{pmatrix}$
	$\mathbf{P}_{12}4_3^u \sim \begin{pmatrix} 0 & 0 & \times \\ \times & \times & 0 \end{pmatrix}$ $\begin{pmatrix} 0 & \bullet & \times \end{pmatrix}$
	$\mathbf{P}_{321}4_3^u\mathbf{P}_{23} \sim \begin{pmatrix} \times & 0 & \times \\ 0 & \times & 0 \end{pmatrix}$

Maximally-Restrictive Lepton Textures

	U(1) charges				Maximally re mass ma	estrictive trices	
Model	$(\mathbf{M}_{e},\mathbf{M}_{D},\mathbf{M}_{R})$)	$\chi_{\sigma} \qquad \chi^L_{\ell_{\alpha}} - s^2_{\beta}$	$\chi^R_{e_\alpha} - 2s_\beta^2$	$\chi^R_{ u_j}$			
L_1	$(4_3^e, 2_1^D, 2_1^R)$ 1	/2 (-3/2, -1/2, 1/2)	(1/2, -1/2, -3/2)	(-1/2, 1/2)	4_{3}^{e}	$\sim \begin{pmatrix} 0 & 0 & \times \\ 0 & \times & \times \end{pmatrix}$	$2_1^D \sim \begin{pmatrix} \bullet & 0 \\ \bullet & \bullet \\ 0 \end{pmatrix}$
L_2	$(4_3^e, 3_1^D, 1_{1,1}^R)$	1 (0, 1, 2)	(2, 1, 0)	(1, 0)		$\left(\times \times 0 \right)$	
L_3	$(4_3^e, 3_1^D, 1_{1,2}^R)$ 1	/2 $(-1/4, 3/4, 7/4)$	(7/4, 3/4, -1/4)	(3/4, -1/4)	Ee.	$\begin{pmatrix} 0 & 0 & \times \\ 0 & \times & 0 \end{pmatrix}$	$2^D_2 \sim \left(\begin{array}{c} \bullet & \bullet \\ \bullet & 0 \end{array} \right)$
L_4	$(4_3^e, 3_2^D, 1_2^R)$	1 (-3/2, -1/2, 1/2)	(1/2, -1/2, -3/2)	(-1/2, 3/2)		$\sim \begin{pmatrix} 0 & \times & 0 \\ \times & 0 & \times \end{pmatrix}$	$\begin{array}{c} 2 \\ 0 \\ \bullet \end{array}$
L_5	$(4_3^e, 3_2^D, 1_{1,3}^R)$	1 $(-5/2, -3/2, -1/2)$	(-1/2, -3/2, -5/2)	(-3/2, 1/2)		$1_1^R \sim \begin{pmatrix} 0 & \times \\ \cdot & \times \end{pmatrix}$	$3_1^D \sim \begin{pmatrix} \bullet & 0\\ 0 & 0 \end{pmatrix}$
L_6	$(4_3^e, 3_3^D, 1_{1,3}^R)$	1 (-3/2, -1/2, 1/2)	(1/2, -1/2, -3/2)	(-3/2, 1/2)		$1_2^R \sim \begin{pmatrix} \times & \times \\ \cdot & 0 \end{pmatrix}$	$3_2^D \sim \begin{pmatrix} \bullet & 0 \\ \bullet & 0 \\ 0 & \bullet \end{pmatrix}$
L_7	$(4_3^e, 3_3^D, 1_2^R)$	1 (-1/2, 1/2, 3/2)	(3/2, 1/2, -1/2)	(-1/2, 3/2)		$2_1^R \sim \begin{pmatrix} 0 & \times \\ \cdot & 0 \end{pmatrix}$	$3_3^D \sim \begin{pmatrix} \bullet & 0\\ 0 & \bullet\\ 0 & \bullet \end{pmatrix}$
L_8	$(4^e_3, 3^D_4, 1^R_{1,4})$	1 (-3, -2, -1)	(-1, -2, -3)	(-1,0)			i 0 0
L_9	$(4_3^e, 3_4^D, 1_{1,3}^R)$ 1	$/2 \ (-11/4, -7/4, -3/4)$	(-3/4, -7/4, -11/4)	(-3/4, 1/4)			$3_4^D \sim \left[\bullet 0 \right]$
L_{10}	$(5_1^e, 2_2^D, 1_{1,4}^R)$	1 (-1, -2, 0)	(0, -3, -1)	(-1, 0)			\• •
L_{11}	$(5_1^e, 2_2^D, 1_{1,3}^R)$ 1	/2 $(-3/4, -7/4, 1/4)$	(1/4, -11/4, -3/4)	(-3/4, 1/4)			

Axion-to-Photon Coupling



Axion-to-Photon Coupling



Axion-to-photon coupling allows to probe the different models at helioscope and haloscope experiments

Requiring $v_{\sigma} \gg v_{1,2}$ for an "invisible" axion, the singlet effectively decouples from the scalar particles of the **2HDM**

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How are these processes controlled in our models?

There is a "Decoupled" entry in the matrices of type "5"

$$\mathbf{M}_{f} = \mathbf{P}_{\mathbf{b}} \begin{pmatrix} 0 & 0 & a_{1} = \frac{m_{f_{2}}m_{f_{1}}}{a_{2}} \\ 0 & a_{3} = m_{f_{1}} & 0 \\ a_{2} & 0 & a_{4} = \frac{\sqrt{\left(a_{2}^{2} - m_{f_{2}}^{2}\right)\left(m_{f_{3}}^{2} - a_{5}\right)}}{a_{2}} \end{pmatrix} \mathbf{P}_{\mathbf{c}}$$

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Leads to zeros in the N_k matrices

$$5^{d,u,e}: \mathbf{N}_{d,u,e} \sim \begin{pmatrix} \times & 0 & 0 \\ 0 & \times & \times \\ 0 & \times & \times \end{pmatrix}, 5^{s,c,\mu}: \mathbf{N}_{d,u,e} \sim \begin{pmatrix} \times & 0 & \times \\ 0 & \times & 0 \\ \times & 0 & \times \end{pmatrix}, 5^{b,t,\tau}: \mathbf{N}_{d,u,e} \sim \begin{pmatrix} \times & \times & 0 \\ \times & \times & 0 \\ 0 & 0 & \times \end{pmatrix}$$

$$d_i, u_i, e_i$$

$$(\mathbf{N}_{d,u,e})_{ij}$$

$$H, I$$

$$d_j, u_j, e_j$$

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 d_i, u_i, e_i $(\mathbf{N}_{d,u,e})_{ij}$ H, I

FCNCs are controlled

J.R. R, H.B. Câmara, R.G. Felipe, F.R. Joaquim; *PRD* 110 (2024) 3, 035027

Flavor-Violating Axion Couplings to Fermions

Effective Axion-Fermion Interactions

$$\mathcal{L}_{aff} = \frac{\partial_{\mu}a}{2f_a} \overline{f_{\alpha}} \gamma^{\mu} \left(\mathbf{C}_{\alpha\beta}^{V,f} + \mathbf{C}_{\alpha\beta}^{A,f} \gamma_5 \right) f_{\beta}$$

 $\mathbf{C}^{V,f} = \frac{1}{N} \left(\mathbf{U}_{R}^{f\dagger} \boldsymbol{\chi}_{f}^{R} \mathbf{U}_{R}^{f} + \mathbf{U}_{L}^{f\dagger} \boldsymbol{\chi}_{f}^{L} \mathbf{U}_{L}^{f} \right) , \ \mathbf{C}^{A,f} = \frac{1}{N} \left(\mathbf{U}_{R}^{f\dagger} \boldsymbol{\chi}_{f}^{R} \mathbf{U}_{R}^{f} - \mathbf{U}_{L}^{f\dagger} \boldsymbol{\chi}_{f}^{L} \mathbf{U}_{L}^{f} \right)$

Flavor-Violating Axion Couplings to Fermions

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The matrices of **type "5"** also lead to **zeros** in the **C**^{*f*} **matrices**

$$5^{d,u,e}: \mathbf{C}^{d,u,e} \sim \begin{pmatrix} \times & 0 & 0 \\ 0 & \times & \times \\ 0 & \times & \times \end{pmatrix}, 5^{s,c,\mu}: \mathbf{C}^{d,u,e} \sim \begin{pmatrix} \times & 0 & \times \\ 0 & \times & 0 \\ \times & 0 & \times \end{pmatrix}, 5^{b,t,\tau}: \mathbf{C}^{d,u,e} \sim \begin{pmatrix} \times & \times & 0 \\ \times & \times & 0 \\ 0 & 0 & \times \end{pmatrix}$$

$$d_i, u_i, e_i$$

$$(\mathbf{C}^{d,u,e})_{ij} a$$

$$d_j, u_j, e_j$$

Flavor-Violating Axion Couplings to Fermions

Effective Axion-Fermion Interactions

$$\mathcal{L}_{aff} = \frac{\partial_{\mu}a}{2f_a} \overline{f_{\alpha}} \gamma^{\mu} \left(\mathbf{C}_{\alpha\beta}^{V,f} + \mathbf{C}_{\alpha\beta}^{A,f} \gamma_5 \right) f_{\beta}$$

$$\mathbf{C}^{V,f} = \frac{1}{N} \left(\mathbf{U}_{R}^{f\dagger} \boldsymbol{\chi}_{f}^{R} \mathbf{U}_{R}^{f} + \mathbf{U}_{L}^{f\dagger} \boldsymbol{\chi}_{f}^{L} \mathbf{U}_{L}^{f} \right) , \ \mathbf{C}^{A,f} = \frac{1}{N} \left(\mathbf{U}_{R}^{f\dagger} \boldsymbol{\chi}_{f}^{R} \mathbf{U}_{R}^{f} - \mathbf{U}_{L}^{f\dagger} \boldsymbol{\chi}_{f}^{L} \mathbf{U}_{L}^{f} \right)$$

The matrices of **type "5"** also lead to **zeros** in the **C**^{*f*} **matrices**

$$5^{d,u,e}: \mathbf{C}^{d,u,e} \sim \begin{pmatrix} \times & 0 & 0 \\ 0 & \times & \times \\ 0 & \times & \times \end{pmatrix}, 5^{s,c,\mu}: \mathbf{C}^{d,u,e} \sim \begin{pmatrix} \times & 0 & \times \\ 0 & \times & 0 \\ \times & 0 & \times \end{pmatrix}, 5^{b,t,\tau}: \mathbf{C}^{d,u,e} \sim \begin{pmatrix} \times & \times & 0 \\ \times & \times & 0 \\ 0 & 0 & \times \end{pmatrix}$$

 d_i, u_i, e_i $(\mathbf{C}^{d,u,e})_{ij} a$ d_j, u_j, e_j

FCNCs are again controlled

Flavor-Violating Axion Couplings to Quarks ($N_{DW} = 1$)



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This highlights the effectiveness of minimal flavoured PQ symmetries in aligning frameworks with highly constrained observations

Axion Couplings to Leptons ($N_{\rm DW} = 1$)



Flavor-conserving couplings are not automatically suppressed and depend on $\tan \beta = v_2/v_1$

Axion mass upper bound (meV)

Model	$\mathrm{Q}_4^{d,s}$	Model	$\mathrm{Q}_{2}^{u} \; ; \; \mathrm{Q}_{2}^{c} \; ; \; \mathrm{Q}_{2}^{t} \; ; \; \mathrm{Q}_{4}^{b}$
L_2	[1.8, 5.6]		
L_4	[0.9, 1.3]	lepton models	
L_5	[1.0, 1.6]		2.7×10^{-2}
L_6	[1.8, 5.4]		3.7×10^{-2}
L_7	[1.2, 2.2]		2.1×10^{-2}
Lo			1.5×10^{-1}
L/8		ЛI	$7.8 imes 10^{-2}$
L_{10}^e	[2.5, 32.7]	ł	
${ m L}^{\mu}_{10}$	[2.3, 15.8]		
\mathbf{L}_{10}^{τ}	[1.9, 6.8]		

- Lepton constraints set the axion mass bound in the d or s decoupled models
- Therefore, the axion mass can be up to two orders of magnitude larger than in the other scenarios
 - As a result, the whole post-inflationary region remains viable while still accommodating flavourviolating axion couplings

Summary and Outlook

Work done:

- \checkmark Study of the theoretical framework of the **minimal** vDFSZ for flavour;
- Identification of the maximally-restrictive pairs of quark and lepton mass matrices compatible with current masses, mixing and CP violation data;
- Axion-photon couplings computed for different models;
- Phenomenology of axion couplings to quarks and charged leptons, with emphasis on flavor-violating terms.

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Thank you !