

QUANTUM Stefano Giagu Sapienza Università di Roma and INFN Roma

Workshop Computing@CSN5 - Bari - October 14-16th, 2024



INTRODUCTION & OUTLOOK

- quantum computers offer an intriguing path for a paradigmatic change of computing in the natural sciences, with the potential for achieving a significant speed-up of numerical simulations and big data analysis
- INFN research activities can help realising and test this potential (and leverage it in the future) through a source of formidable challenging computational problems
- equipping classical ML algorithms with QC may offer the possibility of exploit QC acceleration with current NISQ devices, and find ways to prove quantum utility
- Outlook:
 - Quantum Computing & QML
 - Example applications
 - The road ahead & summary

Recent reviews on QML:

- Y.Wang, J.Liu, A comprehensive review of Quantum Machine Learning: from NISQ to Fault Tolerance, arXiv:2401.11351 [quant-ph]
- D.Peral Garcia et al, Systematic literature review: Quantum machine learning and its applications, Comp. Sci. Rev. 51 (2004) 100619
- A. Di Meglio et al, Quantum Computing for High-Energy Physics, Summary of the QC4HEP Working Group, arXiv:2307.03236 [quant-ph]



- Y. Gujju et al, Quantum machine learning on near-term quantum devices: Current state of supervised and unsupervised techniques for real-world applications, Phys. Rev. Applied 21, 067001





QC (R)EVOLUTION AND EFFORT WORLDWIDE

quantum initiatives ongoing today in >40 countries global Q-tecnology market projected to reach \$106b by 2040



despite the fact that:

for practical applications, quantum computing today is at a similar stage of development as classical computers in the '50 ...







AND QUANTUM HYPE ... BREAKING: Quantum computing enters online dating! "Our quantum matching system helps you find a partner for a lifetime, not just a night."



https://hitomatch.com/



Testimonials

Here's what they have to say.





HitoMatch helped me find my soulmate. The quantum matches and profile videos made a huge difference.

I couldn't be happier with the connection I've made!

John K.

if you believe Everett's multi worlds interpretation of QM, there's a version of you that will find your perfect match

in any case it is w/o doubts a spectacular random number generator ...









HOW PARTICLE PHYSICS CAN HELP QUANTUM COMPUTING?

"Nature isn't classical, dammit, and if you want to make a simulation of nature, you better make it quantum mechanical."

(1982) - Richard Feynman

WATERLOO IQC Institute for WATERLOO

#worldchangingquantum

Simulating Physics with Computers

Richard P. Feynman

Department of Physics, California Institute of Technology, Pasadena, California 91107

Received May 7, 1981

Particle Physics is inherently quantum mechanical, thus simulating theory and analysing experimental data with quantum computers seems a very good idea







PARTICLE PHYSICS AND QC

major application areas in HEP that may benefit from QC/QML





Sampling Adaptive vendor/ customer interactions **Decision support** Training

Simulation

Chemistry Pharmaceuticals **Materials Electric batteries**

Optimization

Travel and transportation Logistics/supply chain Network infrastructure Air traffic control Work scheduling Financial serivces

QC use-cases in 2023 for IBM



 $|1\rangle$



QUANTUM COMPUTING

- Computing paradigm that explicitly leverage quantum mechanical properties of matters to perform calculations
 - in contraposition to CC where QM enters only indirectly (eg. semiconductors in CPUs follow QM rules)
 - QC are not "faster" computers wrt CC, but systems that do computation in different ways
 - QC are not general purpose machines that speed up any problem wrt CC
- Takes advantage of:
 - Superposition and Entanglement → exponential representation power
 - Constructive/destructive interference → guide the computation toward the correct solution amplifying the probabilities of correct answers and reducing the probabilities of incorrect ones
- and other useful/problematic features:
 - Quantum operations (gates) as **unitary transformations** \rightarrow reversible computing
 - Output is the result of a quantum state measurement according to Born rule \rightarrow stochastic computation
 - **No-cloning** theorem → information security / complex/resource hungry error-correction
 - Quantum state coherence and isolation \rightarrow computation stability and errors





ELEMENTS OF A QUANTUM CIRCUIT MODEL OF COMPUTATION

• in a general way any computation (classical or quantum) is based on three fundamental elements:

input data \rightarrow operations on data \rightarrow output results

- in a quantum circuit these elements are described by:
- **qubits** (quantum bits): basic unit of quantum information
 - store information as classical bits in a CC
- quantum logic gates: operators that transform quantum data
 - the building blocks of QC, like classical logic gates in CC
- quantum measurement: the operation that allows to access classically the resulting quantum state
 - reading out information from a quantum system lacksquaregenerally change the state and destroy the computation that we are performing
 - can't predict the exact outcome of a quantum \bullet measurement, due to the probabilistic nature of QM all we can predict are only likelihood







QUBIT: QUANTUM BIT

- basic unit of quantum computation representation
 - **classical bit**: binary ("0 or 1")

computational basis typically used as canonical basis:

$$0\rangle = \begin{bmatrix} 1\\0 \end{bmatrix} \quad |1\rangle = \begin{bmatrix} 0\\1 \end{bmatrix}$$

$$|\psi\rangle = \begin{bmatrix} a_0 \\ a_1 \end{bmatrix} = a_0 \begin{bmatrix} 1 \\ 0 \end{bmatrix} + a_1 \begin{bmatrix} 0 \\ 1 \end{bmatrix} = a_0 |0\rangle + a_1 |1\rangle = \cos$$

Extending this to a system of n qubits forms a 2ⁿ-dimensional Hilbert Space eg. 2^n complex numbers \rightarrow a quantum system can contain much more information)







TECHNOLOGIES FOR QUANTUM COMPUTERS

- not yet a standard way to implement qubits, unlike for classical bits encoded in transistors

 - current leading technology in the quantum computing commercial space: superconducting qubits

Superconducting Loops



resistance-free current oscillates back and forth around a circuit loop. An injected microwave signal excites the current into superposition states

fast operations, built on existing SC industry

quick decoherence, must be kept cold

Trapped ions or neutral atoms arrays



use the energy levels of electrons in neutral atoms or ions as qubits. Excite them with lasers to a higher energy level. Assign the qubit values based on their energy status

very stable, high gate fidelity, 2D and 3D

slower operation, complex laser technology required

Linear / non-linear optical QC



use particles of light to carry and process information. Qubits realised by processing states of different modes of light through both linear and nonlinear element (quantum microprocessor based on laser photonics)

operate at room temperature, photons less sensitive to env. emerging technology, hard to build large number of gates, cannot stop photons ...

O.Ezratty, Eur. Phys. J. <u>A 59, 94 (2023)</u>

• physically, qubits can be any two-level systems: the spin of an electron, the polarization of a proton, two superconducting current directions ...





EXAMPLES OF QUANTUM COMPUTERS

SYCAMORE CHIP

IBM Q

Google 53/67 qubits



1121/133 (low error/ faster) qubits today 1000+ near-term

actual quantum processor is just O(2x2 cm²) needs cooling&protection from environment to preserve the quantum capabilities

source: IBM



EXAMPLES OF QUANTUM COMPUTERS ...

• Quantum Computing on Arduino ...



Disclaimer from the author: "This quantum emulator may not actually solve any real-world problems faster than a classical computer. But neither do most other quantum computers right now...

\$10 - 7 qubits emulator implements Hadamard, CNOT, X, Y, S, T and Z gates

Davide Gessa, github project

 Elego Uno (a much cheaper version of Arduino Uno) processor



OPERATIONS OVER QUBITS: QUANTUM GATES&CIRCUITS

- change in the state, in a similar way as we operate on classical bits through logical operations
- length-preserving, linear transformation, which represent a rotation on the Bloch sphere:

 $|\psi'\rangle = U|\psi\rangle$ with U unitary matrix: $U: U^{\dagger}U = I$

- **quantum circuit** = a collection of quantum gates that operates on qubits
- quantum software is programmed by building these circuits



NOTE: when ported to the real quantum hw can look very different from the initial design (circuit adaptation, transpiling)

• quantum computation proceeds by applying physical operations on a quantum state of qubits inducing a

• a state-changing operator is called a quantum gate, and it is represented by a complex unitary matrix, eg





QC PARADIGMS

Туре	Discrete Gate (DG)	Continuous Variable (CV)	Quantum Annealer (QA)
Computing	Digital	Digital/Analog	Analog
Property	Universal (any quantum algorithm can be expressed)	Universal - GBS non-Universal	Not universal — certain quantum systems
Advantage	most algorithms and tech support	uncountable Hilbert (configuration) space	continuous time quantum process
How?	IBM – Qiskit ~500 Qubits	Xanadu Quantum Lab 	DWave – LEAP ~7000 Qubits
What?			
	$input \begin{bmatrix} 0 \\ H \\ 0 \\ H \\ 0 \\ H \\ 0 \\ 0 \\ 0 \\ 0 \\$	Interferometer U_1 S U_2 D Φ	E QA finds wide minima failed tunnelling state

credit: Michael Spannowsky

- Universal gate-based quantum computers designed to tackle a wide range of problems, evolution decomposed in elementary gates
- Quantum Annealers designed specifically for optimization problems:
 - uses a network of qubits and couplers arranged to efficiently map optimization problems onto the quantum hardware
 - allows for the effective translation of optimization problems into Hamiltonian equations and the subsequent minimization of these equations by applying an annealing process



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QUANTUM ALGORITHMS IN THE NISQ REGIME

- assuming the availability of fault-tolerant quantum processors supporting a large number of qubits and quantum gates
 - Shor's (proved exponential speedup in factoring prime numbers), Grover's (polynomial (quadratic) speedup for searching in an unsorted db), Quantum MC, Quantum Fourier Transform ...
- these are the so called noisy intermediate-scale quantum devices (NISQ):
 - no error correction: produce only approximate results of computations
 - lacksquare
- some kind of advantage or utility wrt classical algorithms:
 - ex. find the ground-state energy of a many-body system (ex. a molecule) with quantum annealers

ex. Quantum Machine Learning

• an entire zoo of sophisticated quantum algorithms that can offer speedups over classical algorithms has been proposed in literature

60+ quantum algorithms with quantum speedup https://quantumalgorithmzoo.org/

• however current quantum computers support only O(10¹÷10³) qubits, and not all necessarily able to interact with each others:

algorithms limited to use only a few qubits and gates with deep impact on quantum algorithmic design and achievable performance

• interesting to narrow down the objective: finding computational problems that can be solved by NISQ device while possibly exhibiting



credit: M.Troyer - Quantum Colloquium 2021 - Simons Institute







APPROACHES TO COMBINE QC AND ML

data processing device

data generating system



different possibilities:

- CC: classical data being processed classically but with methods inspired by QC algorithms (like tensor networks)
- QC: quantum data processed with classical algorithms, eg use classical ML to help preparing and use QC (describe quantum state in a compact manner, state preparation, qubit error correction, ...)
- CQ: classical data processed with quantum devices
- QQ: quantum data being processed by a quantum computer. Connected to CQ (just change the input data), becomes interesting with the development of quantum sensing

E.A. Gilles Brassard, S. Gambs: Machine learning in a quantum world. In: Advances in Artificial Intelligence, pp. 431–442. Springer (2006)







encode the task into a parametrised cost function (ansatz)

- evaluated in a QC
- parameters optimised (trained) in a CC



a set of algorithms inspired by classical ML that all share the same common idea:

Variational Q-Algorithms ex. Quantum-NN



Energ Based

Finds the ground-state of a quantum system using a quantum-classical hybrid approach (ex. Quantum Boltzman Machines)



WHY QML?

- QML works well with NISQ:
 - resources are available
 - been show that QML algorithms give the correct result)
- and can in principle improve classical ML:
 - speed-up and complexity
 - sample efficiency
 - representational power
 - energy efficiency

 \bullet

. . .

• flexible, can be implemented with a small number of qbits and then scaled up when more

• more robust to noise (noise in differentiable optimisation works as regulariser, up to some level has



QUANTUM NEURAL NETWORKS

typical example of a QNN:



ENCODING CLASSICAL DATA

- encoding of classical data is a crucial step in implementing CQ-QML algorithms
- example: amplitude encoding

$$x = \begin{bmatrix} x_0 \\ x_1 \end{bmatrix} \to |x\rangle = \frac{1}{\|x\|} (x_0 |0\rangle + x_1 |1\rangle) =$$

- fewer qubits needed: exponential compression $n_q \propto O(\log N)$
- more complex preparation and readout: # of gates $n_g \propto O(\text{poly}(N))$







EXAMPLE: EXPRESSIBILITY FOR A SINGLE QUBIT

Low expressibility



• expressibility: circuit's ability to generate (pure) states that are well representative of the Hilbert space • in the case of a single qubit, the expressibility corresponds to the circuit's ability to explore the Bloch sphere

High expressibility

S. Sim et al: <u>arXiv:1905.10876</u>









EXPRESSIBILITY VS TRAINABILITY: THE BARREN PLATEAUS PROBLEM

- variational circuits are affected by the presence of large regions in the loss landscape where the variance of the gradient is almost 0 (flat loss landscape)
- a circuit initialised in one of these areas will be untrainable using any gradient-based algorithm
- it can be shown that the gradient's variance exponentially decrease with the # of qubits

$$ig \langle \partial_{ heta} L ig
angle \simeq 0$$

Var[$\partial_{ heta} L$] $\sim 2^{-n}$ J.R. Mc Clean et al., Nat

with not too-deep circuits and not too much entanglement:





global loss



. Comm.

• a possible mitigation strategy: use local cost functions that only have information from part of the circuit coupled

$\operatorname{Var}[\partial_{\theta} L] \gtrsim \operatorname{poly}(n)^{-}$

Cerezo et al: <u>arXiv:2001.00550</u>









QML AND QUANTUM ADVANTAGE

Quantum Convolutional Neural Networks are (Effectively) Classically Simulable

Pablo Bermejo, Paolo Braccia, Manuel S. Rudolph, Zoë Holmes, Lukasz Cincio, M. Cerezo <u>P. Bermejo et al, arXiv:2408.12739</u>

<u>M.Cerzo et al, QTML 2024</u>

Does provable absence of barren plateaus imply classical simulability? Or, why we need to rethink variational quantum computing

M. Cerezo, Martin Larocca, Diego García-Martín, N. L. Diaz, Paolo Braccia, Enrico Fontana, Manuel S. Rudolph, Pablo Bermejo, Aroosa Ijaz, Supanut Thanasilp, Eric R. Anschuetz, and Zoë Holmes

> This provokes the question: Could the very same structure that allows one to provably avoid barren plateaus be leveraged to efficiently simulate the loss function classically? Here we argue that the answer to this question is 'yes'. Specifically, we claim that loss landscapes which provably do not exhibit barren plateaus can be simulated using a classical algorithm that runs in polynomial time. Importantly, this simulation might still necessitate

is the quantum advantage the right goal for QML? M. Schuld, N.Kiloran PRX Quantum 2 030101

Until error correction will be available (2030?) better to focus on an intermediate milestone: quantum utility ...

our work can not, and does not intend to, prove that there is no scenario whatsoever where it may be necessary to train a QCNN on a quantum computer. However, the burden of proof now rests firmly in the hands of any proponent of QCNNs to identify such cases and until then it is good practice to maintain a healthy skepticism that such cases can be found. Hence we boldly claim: There is currently no evidence that QCNNs will work on classically non-trivial tasks, and their place in the upper echelon of promising QML architectures should be seriously revised.







QUANTUM UTILITY

High-fidelity quantum computation outside the reach of exact classical simulation methods

It is the first major milestone on the path to Quantum Advantage.

Useful quantum computation requires utility-scale hardware and co-designed scalable software capabilities.

This means systems larger than 100 qubits, where simulations are not a viable alternative.

IBM quantum 2024



140

120 100

circuit width

Evidence for the utility of QC before fault tolerance 127 qubits / 2880 CX gates



Nature, 618, 500 (2023)













EXEMPLES OF QML APPLICATIONS IN HEP Experiment Theory





A. Di Meglio et al: <u>arXiv:2307.03236 [quant-ph]</u>





QML IN HEP: HIGGS CLASSIFICATION

Classical Support Vector Machine with Quantum Kernels acceleration employed in probing of the Higgs boson coupling to the top quark with the $t\bar{t}H(\rightarrow\gamma\gamma)$ channel

QSVM

$$\begin{array}{c} y' = sgn(\sum_{i=1}^{t} \alpha_{i}y_{i}k(\vec{x}_{i},\vec{x}') + b) \quad \text{SVM output} \\ |0\rangle \\ \vdots \\ |0\rangle \\ \end{array}$$

$$\begin{array}{c} \psi' = sgn(\sum_{i=1}^{t} \alpha_{i}y_{i}k(\vec{x}_{i},\vec{x}') + b) \quad \text{SVM output} \\ |0\rangle \\ \Rightarrow \quad k(\vec{x}_{i},\vec{x}_{j}) = |\langle \Phi(\vec{x}_{i})|\Phi(\vec{x}_{j})\rangle|^{2} = |\langle 0^{\otimes N}|\mathcal{U}_{\Phi(\vec{x}_{j})}^{\dagger}|0^{\otimes N}\rangle|^{2} \\ \Rightarrow \quad k(\vec{x}_{i},\vec{x}_{j}) = |\langle \Phi(\vec{x}_{i})|\Phi(\vec{x}_{j})\rangle|^{2} = |\langle 0^{\otimes N}|\mathcal{U}_{\Phi(\vec{x}_{j})}^{\dagger}|0^{\otimes N}\rangle|^{2} \\ \Rightarrow \quad 0.930 \\ \end{array}$$

Dataset:

- signal and dominant backgrounds considered, simulated with Delphes
- input features: 23 object-based kinematic variables from the ATLAS analysis







A QUANTUM ANNEALER EXAMPLE: HIGGS CLASSIFICATION

- an alternative approach: using a programmable quantum annealer ...
- task: classification of $H \rightarrow \gamma \gamma$ versus di-photon background

Quantum Annealing:

- define an ensamble of week classifiers $C_i(x) = \pm 1/N_c$
- maps the solution of the problem to the ground state of an Ising Hamiltonian

$$H = \sum_{i,j} J_{ij} s_i s_j + \sum_i h_i s_i \qquad C_i = \sum_i I_j$$

$$C_{ij} = \frac{1}{4} \sum_t C_i(x_t) C_j(x_t) \qquad h_i = \lambda - C_i + \frac{1}{2} \sum_j I_j$$

- minimize H and return the ground state, building a strong classifier as:

$$R(x) = \sum_{i} s_i^* c_i(x) \in$$

<u>A. Mott et al, Nature volume 550, pages 375–379 (2017)</u>





QML: HYBRID QUANTUM GNN FOR TRACK RECONSTRUCTION

- challenge to track reconstruction algorithms
- idea: explore the possibility to speedup the task by implementing an hybrid classical-quantum Graph Neural Network trained to determine charged particle trajectories from hits in a LHC inner tracker detector
- -charged particle tracks are represented as a graph over the detector hits
 - -nodes: hits in a detector layer
 - -edges: track segments
 - -nodes and edges information is updated trough message passing leveraging an attention mechanism to identify most relevant nodes

INFN-Ferrara: V.Amitrano, M.Argenton, C.Bozzi, E.Calore, L.Cappelli, F.Schifano

• one of the hard challenges at the future HL-LHC upgrade, when the increase in the instantaneous rate of particle collisions will yield many more detector hits, and thus measurements will pose a combinatorial



















QML: HYBRID QUANTUM GNN FOR TRACK RECONSTRUCTION



INFN-Ferrara: V.Amitrano, M.Argenton, C.Bozzi, E.Calore, L.Cappelli, F.Schifano

first implemented by Cenk Tüysüz et al, arXiv:2012.01379





QML: HYBRID QUANTUM GNN FOR TRACK RECONSTRUCTION

Accuracy is, as expected, higher with lower pileup



Training Accuracy





INFN-Ferrara: V.Amitrano, M.Argenton, C.Bozzi, E.Calore, L.Cappelli, F.Schifano







QUANTUM ANOMALY DETECTION FOR QCD JETS

- notion of normal behavior
- model-independent searches for NP effects



• Anomaly Detection describes a class of algorithms that aims at the identification of rare items, events or observations, which deviate significantly from the majority of the data and do not conform to a well-defined

• Gained increasing interest recently in experiments at the LHC, as a viable ML approach to implement signal

ANOMALY DETECTION

 $R^{300} \rightarrow R^{l}, l = 4, 8, 16$

K.A.Wozniak et al, arXiv:2301.10780











QUANTUM ANOMALY DETECTION FOR QCD JETS



K.A.Wozniak et al, arXiv:2301.10780



entanglement and expressivity increase



QUANTUM ANOMALY DETECTION FOR LONG LIVED PARTICLES

ATLAS muon spectrometer information

NORMAL event

"image" representation of a prompt decay in multi-muons



ANOMALOUS event

"image" representation of a highly displaced decay in multi-muons







QML IN HEP: ANOMALY DETECTION FOR LONG LIVED PARTICLES





description of the quantum noise and quantum error correction a crucial issues still to be solved

S.Bordoni et al, Particles 2023, 1, 1–15



GENERATIVE QML: QUANTUM DIFFUSION MODELS

Data



generators like DALL-E, Stable Diffusion, ...), image denoising, inpainting, super-resolution,



GENERATIVE QML: QUANTUM DIFFUSION MODEL

- can be used in a full quantum or in an hybrid mode, where the quantum circuit is trained in the latent space of a classical AE
- conditioning achieved by adding ancillary qubits to encode labels

Quantum Denoiser



• Quantum Diffusion Models: data points encoded into quantum states. Markov chain implemented by a quantum circuit acting as a denoiser



GENERATIVE QML: FIRST APPLICATIONS IN HEP

- Simulation of the LHCb calorimeter module: Quantum-GAN •
- Simulation of a b-jet dataset with a Quantum Circuit Born Machine ٠



Total energy measured by the module [arbitrary units]

work in progress: dealing with instabilities in the qGAN training and needs for large number of qubits ...



Measured b-hadron decay distance from PV [mm]

INFN-Padova: A. Gianelle, J.Hagen, D.Lucchesi, L.Sestini, D.Zuliani











GENERATIVE QML: FIRST APPLICATIONS IN DRUGDISCOVERY

candidates (KRAS inhibitors).



solutions

• generative model running on quantum hardware that surpasses the best classical models in generating potential drug candidates for cancer. A hybrid classical AI-QuantumML model was used to simulate millions of drug

• an indication of how quantum computing and AI can already integrate to provide innovative state-of-the-art

M.G. Vakili et al, arXiv:2402.08210 [quant-ph]







THE ROAD AHEAD (CONCLUSION)

- Quantum computing may offer great opportunities for researcher in INFN:
 - exciting field supported in the public and private sectors
 - a lot of space for original ideas and new algorithms yet to be discovered
- Many questions need to be answered:
 - what are the really promising applications (in our field, and outside)?
 - how we benchmark performances?
 - how to cope with classical data encoding/reduction?
 - QML trainability?
 - •
- quantum advantage in real-word applications will require a new generation of quantum computers and algorithms in terms of size, fault tolerance, connectivity and quantum gates implementation, but already today we are entering the quantum utility regime ...



SOME RECENT PROMISING RESULTS ...

[Submitted on 19 Sep 2024]

Hardware-efficient quantum error correction using concatenated bosonic qubits

Harald Putterman, Kyungjoo Noh, Connor T. Hann, Gregory S. MacCabe, Shahriar Aghaeimeibodi, Rishi N. Patel, Menyoung Lee, William M. Jones, Hesam Moradinejad, Roberto

Rodriguez, Neha Mahuli, Jefferson Rose, J Arriola, James Barnett, Przemyslaw Bienia Cosmic, Ana Valdes Curiel, Erik Davis, Lai Michael T. Fang, Yawen Fang, Matthew J. Justin Hand, Yuan He, Mike Hernandez, D Karabalin, Peter J. Karalekas, Andrew J. Ke Guillaume Marcaud, Gavin McCabe, Cody Pagdilao, Nicola Pancotti, Ashley Panduro Resnick, Alex Retzker, Omar A. Reyna, Ma

Landmark IBM error correction paper published on the cover of Nature

IBM has created a quantum error-correcting code about 10 times more efficient than prior methods a milestone in quantum computing research.

https://www.nature.com/articles/s41586-024-07107-7

An in-principle super-polynomial quantum advantage for approximating combinatorial optimization problems via computational learning theory



<u>N.Pirnay et al, Sci.Adv. 2024 (arXiv:2212.08678)</u>

AWS Center for QC @ Caltech: arXiv:2409.13025



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NEWS 09 October 2024

Google uncovers how quantum computers can beat today's best supercomputers

Quantum machines have a noise threshold past which classical machines cannot best them. researchers have learnt.

By Dan Garisto



A. Morvan et al, Phase transitions in random circuit sampling. Nature 634, 328-333 (2024)











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