

jet quenching

theoretical and experimental aspects

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jets in vacuum

Ellis, Stirling, Webber, *QCD and Collider Physics*, CUP (1996)
Dokshitzer, Khoze, Mueller, Troyan, *Basics of Perturbative QCD*, Ed. Frontieres (1991)
Salam, *Towards Jetography*, arXiv:0906.1833 [hep-ph]

hard scattering processes in hadronic collisions

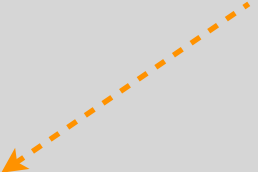
the cross section for the production of a back-to-back pair of hard partons in a hadronic collision can be written

$$\sigma^{AB \rightarrow kl} \sim f_i^A(x_1, \mu_F^2) \otimes f_j^B(x_2, \mu_F^2) \otimes \hat{\sigma}^{ij \rightarrow kl}(p_1 = x_1 P_1, p_2 = x_2 P_2, \alpha_s(\mu_R^2), Q^2/\mu_F^2, Q^2/\mu_R^2)$$

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- 
- high- p_T processes result from interaction between parton constituents [quarks and gluons] of the incoming hadrons
 - parton content of hadrons described by parton distribution functions [PDFs]
 - non-perturbative objects
 - scale [Q^2] dependence driven [perturbatively] by DGLAP evolution
 - universal, determined from global data fits

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- partonic cross section
 - does not depend on the details of the hadronic wave functions [factorization]
 - only involves high momentum transfers [short distance and time scales]; all low momentum scales in the PDFs
 - can be calculated to any order in perturbation theory

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$$\sigma^{AB \rightarrow kl} \sim f_i^A(x_1, Q^2) \otimes f_j^B(x_2, Q^2) \otimes \hat{\sigma}^{ij \rightarrow kl}(p_1, p_2, \alpha_s(Q^2)) + \mathcal{O}(1/Q^2)$$

hard scattering processes in hadronic collisions

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- what is factorized into the PDFs depends on the perturbative order to which partonic cross-section is calculated [must be done consistently :: always be suspicious of calculations that mix perturbative orders – most likely they do not make sense]
- in principle three momentum scales [of the same order] are involved
 - ↪ factorization scale μ_F [separation between long- and short-distance physics] at which PDFs are evaluated
 - ↪ renormalization scale μ_R at which the coupling is calculated
 - ↪ hard scale Q^2 that characterizes parton-parton scattering
- the relation between these scales is fixed by higher order calculations :: to all orders the cross section does not depend on μ_F and μ_R
- a standard approximation is to take [at LO] $\mu_F = \mu_R = Q^2$:: their relative variation [by a factor 2, say] estimates theoretical uncertainty

$$\sigma^{AB \rightarrow kl} \sim f_i^A(x_1, Q^2) \otimes f_j^B(x_2, Q^2) \otimes \hat{\sigma}^{ij \rightarrow kl}(p_1, p_2, \alpha_s(Q^2)) + \mathcal{O}(1/Q^2)$$

branching of hard parton

outgoing [virtual] high- p_t parton relaxes virtuality down to hadronization scale by branching

branching independent of parton's previous history [i.e. it also factorizes]

$$\sigma^{AB \rightarrow X} \sim f_i^A(x_1, Q^2) \otimes f_j^B(x_2, Q^2) \otimes \hat{\sigma}_{ij \rightarrow k} \otimes D_{k \rightarrow X}(z, Q^2)$$

- X =parton

- fragmentation function only includes parton branching
- [perturbative] DGLAP-like evolution towards lower Q^2

- fragmentation function [generic]

- probability distribution for parton k to result in 'state' X carrying fraction z of parton's momentum
- encodes [perturbative] branching and [non-perturbative] hadronization
- in principle depends on separate scale μ_{frag} [set here to Q^2]

- X =hadrons [or jets]

- fragmentation function includes hadronization
- constrained from global fits to data [since factorizable and universal] with evolution still driven by DGLAP [analogous to PDFs]
- different in MC event generators
 - ➔ evolution [branching] down to hadronization scale followed by hadronization prescription [Lund strings, cluster, local parton-hadron duality]

[perturbative] partonic branching

$$t \frac{\partial}{\partial t} D_i(x, t) = \sum_j \int_x^1 \frac{dz}{z} \frac{\alpha_s}{2\pi} P_{ji}(z) D_j(x/z, t)$$

evolution of the momentum fraction distribution of partons produced from original parton i
resums multiple branchings to leading logarithmic order $O[(\alpha_s \log Q^2)^n]$

parton splitting function :: probability of parton i to come from splitting of parton j



probabilistic interpretation clearer from integral formulation [also useful for numerical MC implementation]

$$D(x, t) = \Delta(t) D(x, t_0) + \Delta(t) \int_{t_0}^t \frac{dt_1}{t_1} \frac{1}{\Delta(t_1)} \int \frac{dz}{z} P(z) D\left(\frac{x}{z}, t_1\right)$$

$$\Delta(t) = \exp \left[- \int_{t_0}^t \frac{dt'}{t'} \int dz \frac{\alpha_s(t', z)}{2\pi} P(z, t') \right]$$

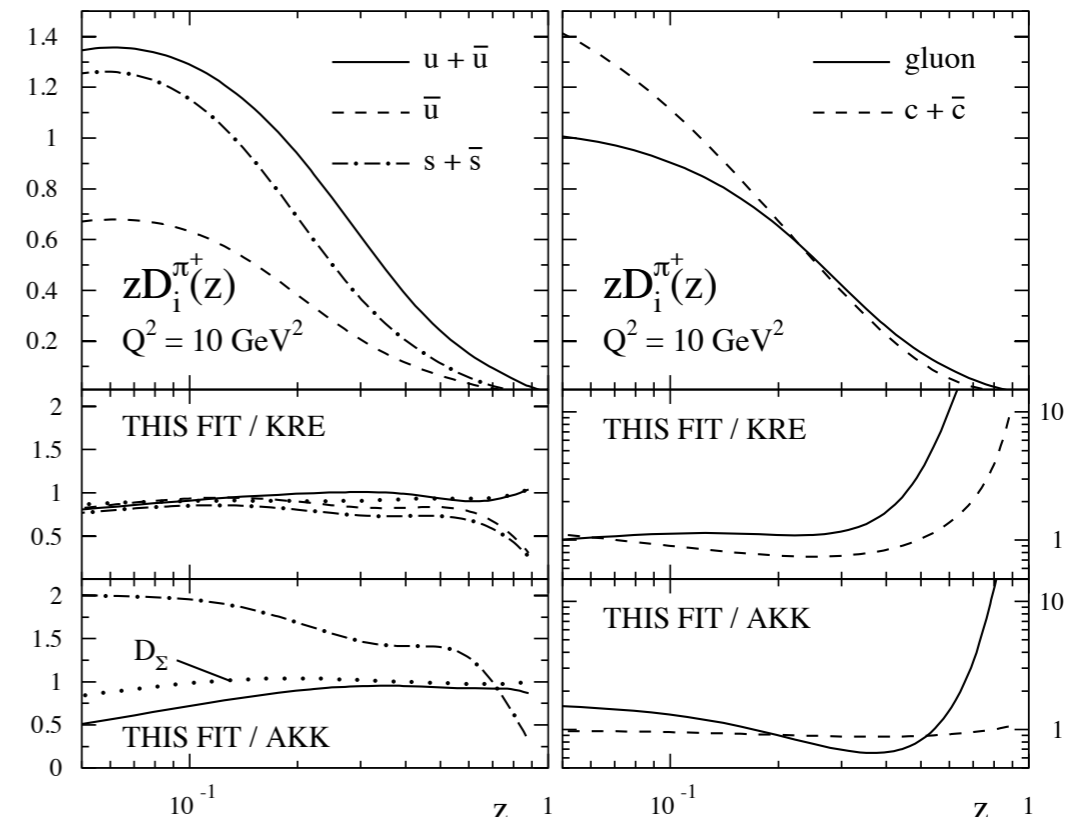
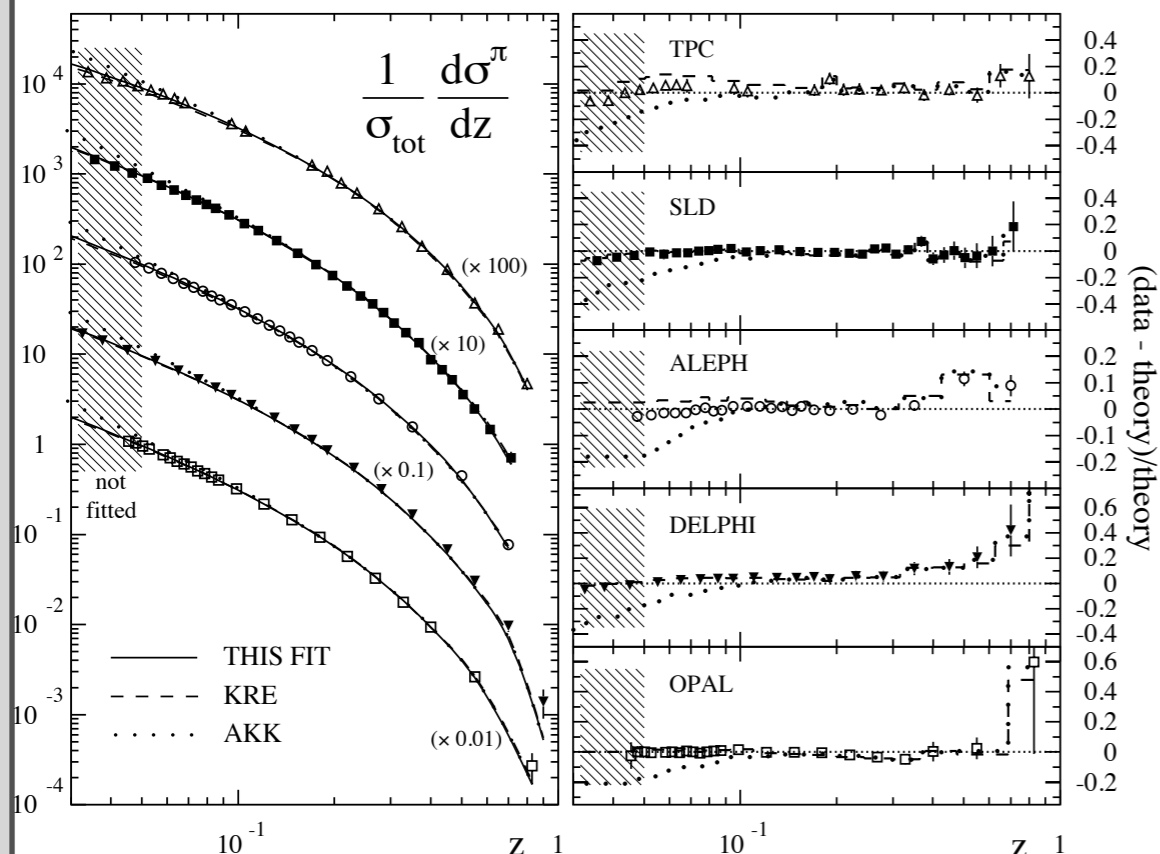
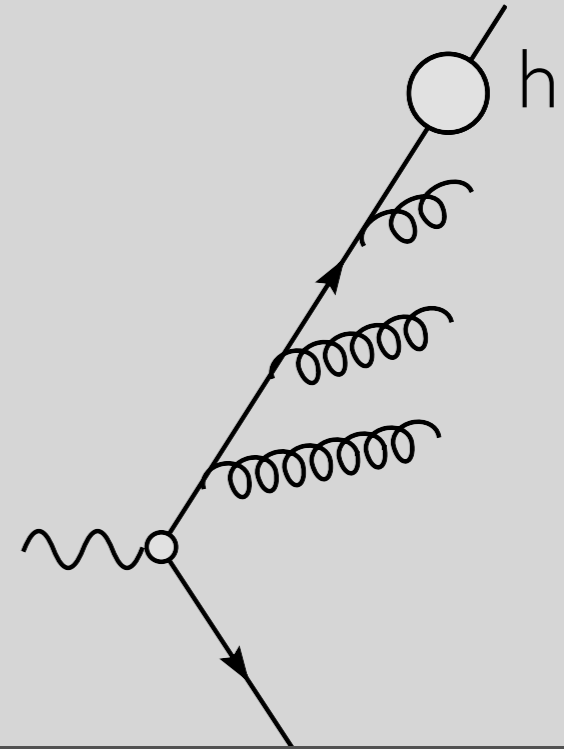
Sudakov form factor

- probability of no resolvable splitting between scales t_0 and t

branching + hadronization [pathway #1]

include hadronization in the definition of fragmentation functions

- scale evolution still DGLAP-like driven [as before]
- hadronization not understood from first principles
 - ◉ non-perturbative information in evolution initial conditions
 - ◉ constrained from data global fit



branching + hadronization [pathway #2]

Monte Carlo event generators [PYTHIA, HERWIG] proceed differently

- probabilistic implementation of evolution [parton shower] with the Sudakov form factors

- ◉ down to hadronization scale [~ 1 GeV]

$$\Delta(t) = \exp \left[- \int_{t_0}^t \frac{dt'}{t'} \int dz \frac{\alpha_s(t', z)}{2\pi} P(z, t') \right]$$

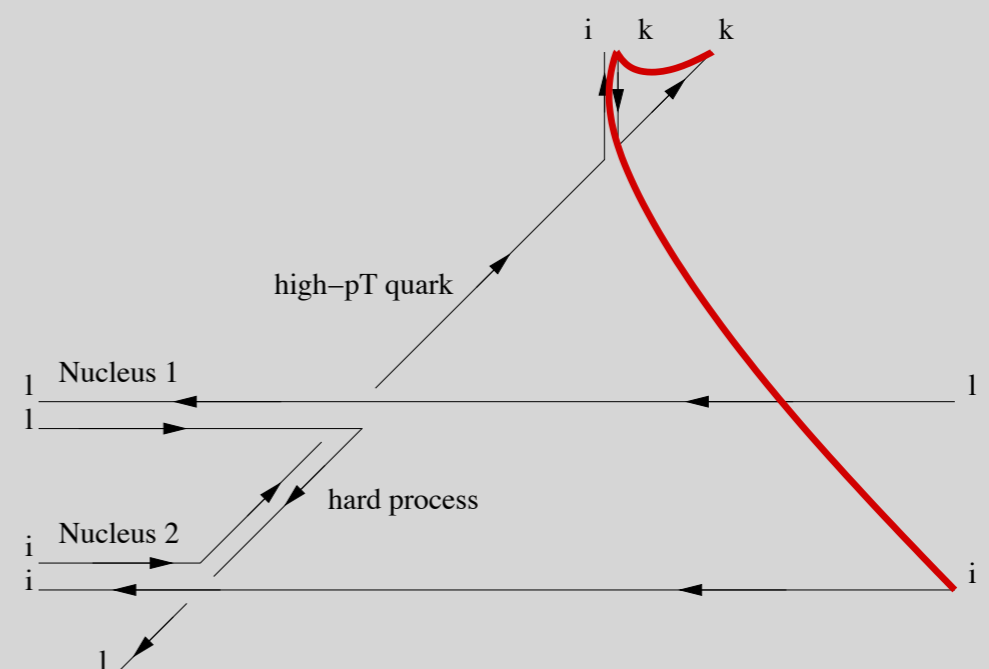
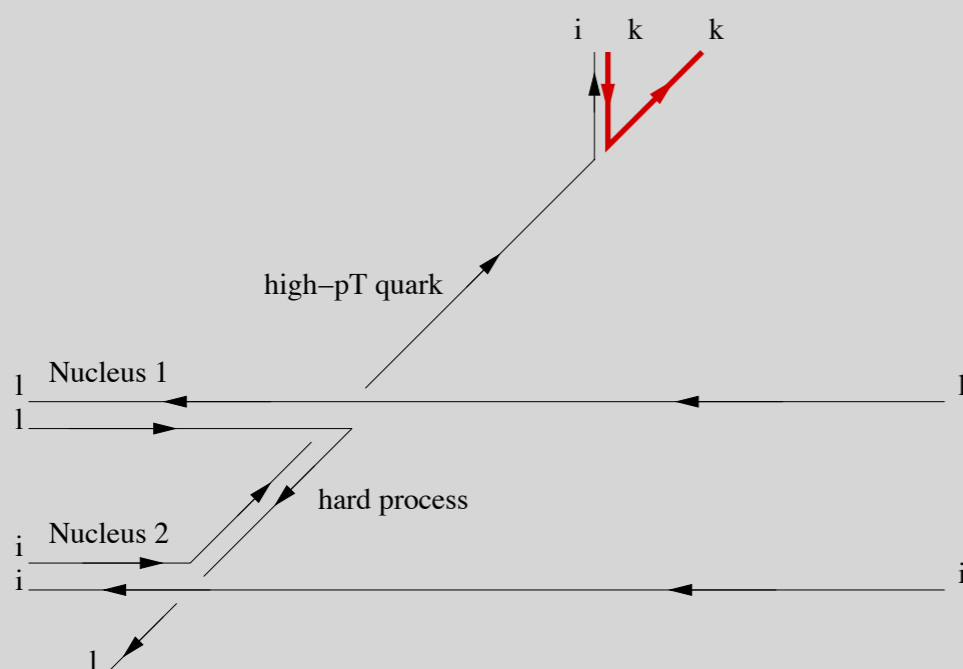
- identification of colour singlet objects [strings, clusters]

- ◉ colour information tracked to $1/N_c$ accuracy [gluon = quark-antiquark pair]

- ◉ hadronization by string-breaking/cluster decay

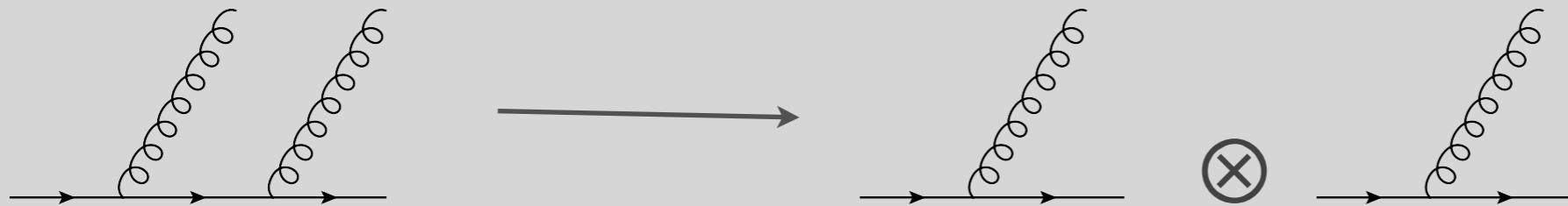
- ▶ long strings/large mass clusters lead to increased and softer multiplicity

- ▶ tuned to data :: 'reproduces' data extracted fragmentation functions

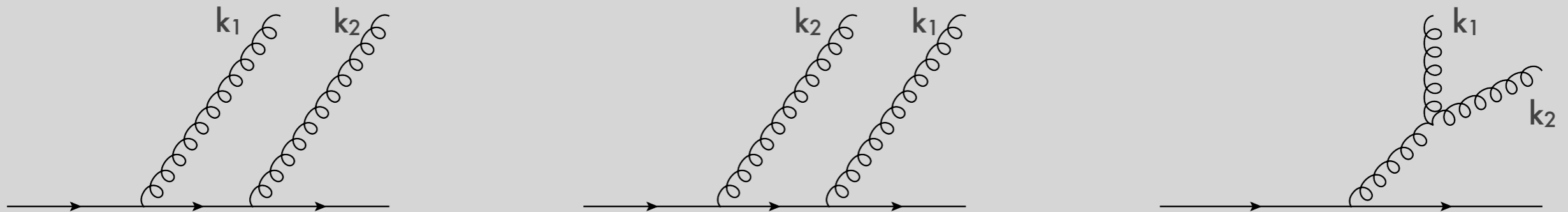


coherent branching

so far we have assumed that successive branchings are independent



however, interferences play an important role



- coherence between successive splittings results in suppression of radiation of 2nd gluon at angles larger than 1st emission angle :: angular ordering

- large angle 2nd gluon emissions cannot resolve quark and gluon separately :: emitted as if from initial quark
- gluon emission is collinearly singular :: dominated by strong hierarchy in emission angles
- not the full story [also need energy-momentum conservation for full description] but qualitatively right

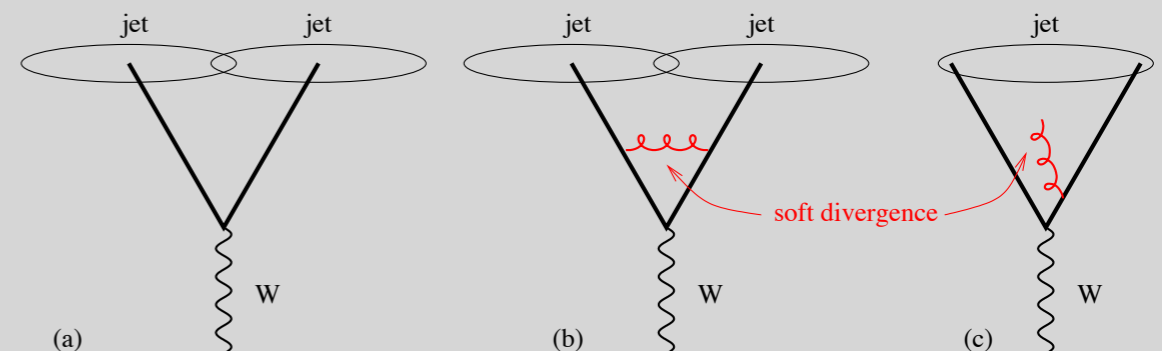
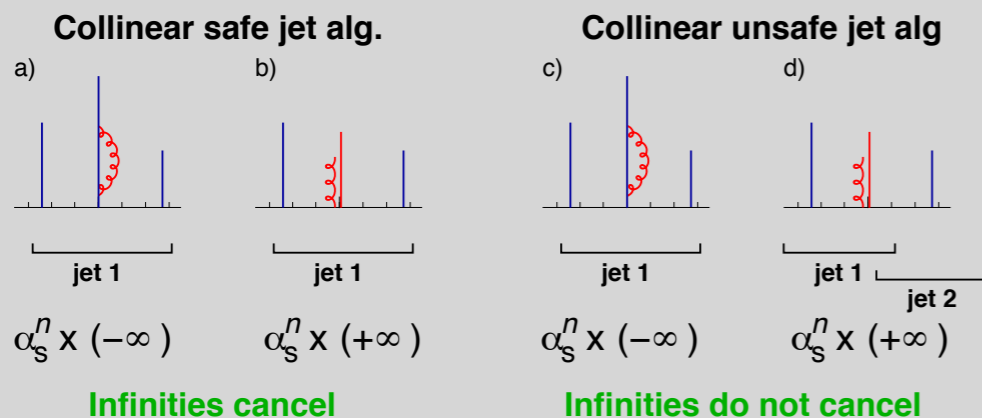
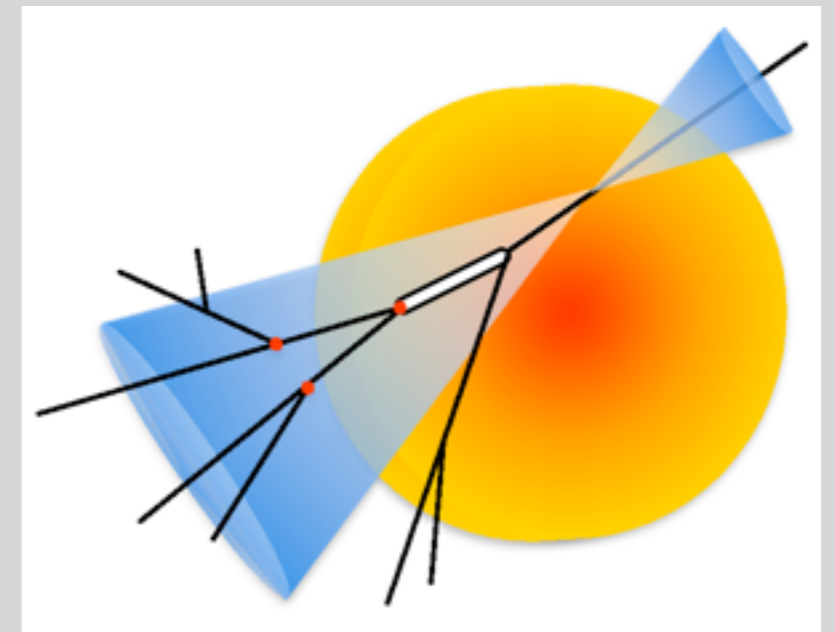
jet definition

the collimated spray of particles that results from the branching of the original hard parton and subsequent hadronization of the fragments

in order to **define** a jet, a set of rules on how to group particles into a jet and how to assign a momentum to the jet must be specified

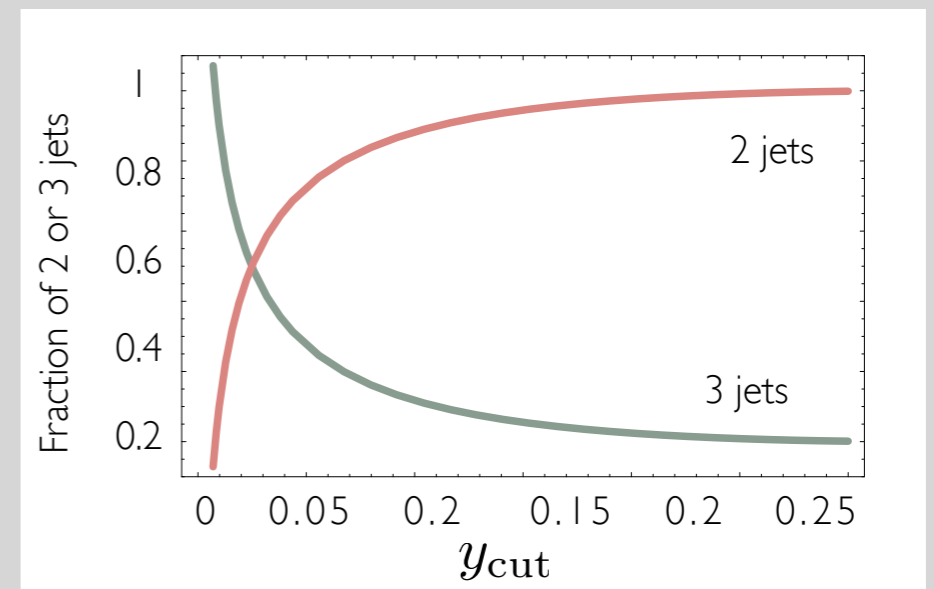
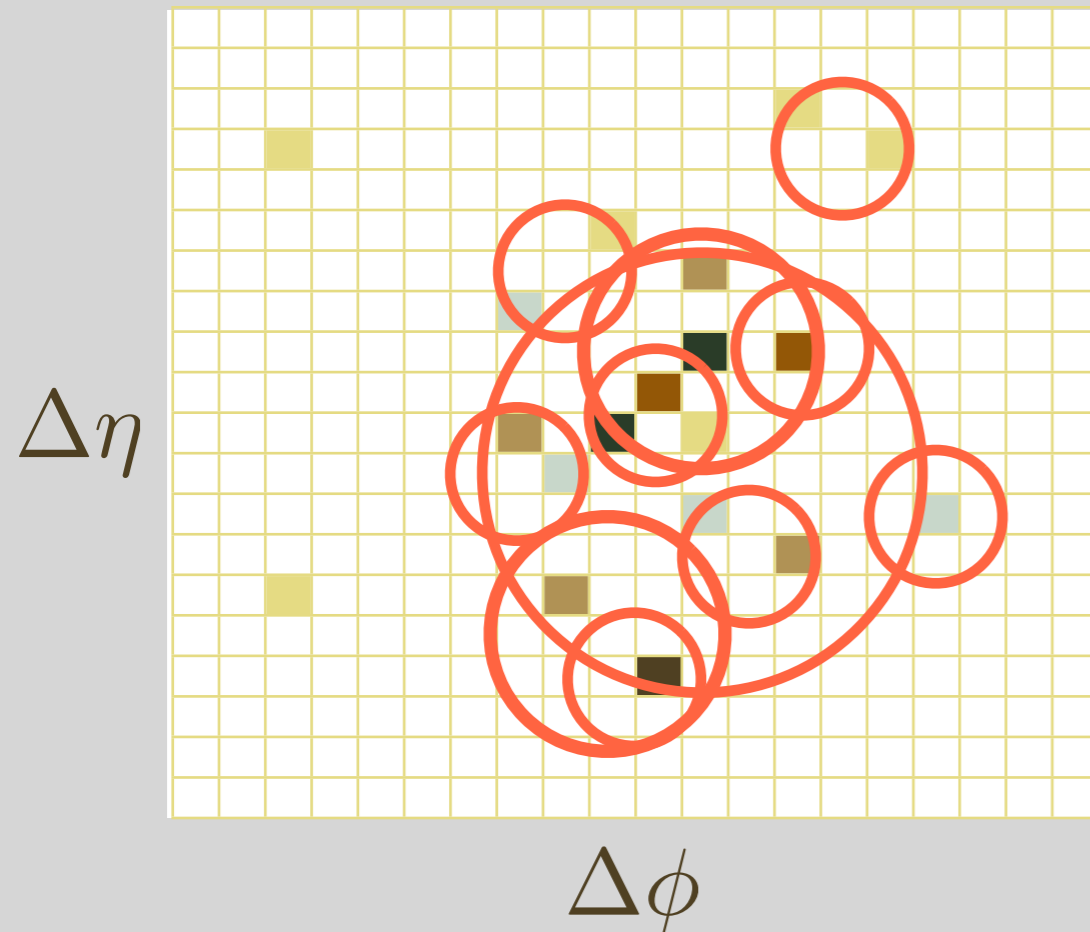
:: properties of a good jet definition ::

- the same for experimental analysis, analytical partonic calculations and Monte Carlo simulations
- collinear safe [the emission of a collinear gluon does not change what is identified as a jet]
- IR safe [the emission of a soft gluon does not change the jet]
- is not sensitive to hadronization details



jet resolution scale

the jet definition is completed by specifying a resolution scale [jet size]



different jet sizes result in a different number of jets

most commonly used [at present] jet algorithm [also in HIC]

—○ define distance measures [R= 'jet cone radius]

$$d_{ij} = \min(1/p_{ti}^2, 1/p_{tj}^2) \frac{\Delta R_{ij}^2}{R^2}$$

$$\Delta R_{ij}^2 = (y_i - y_j)^2 + (\phi_i - \phi_j)^2$$

$$d_{iB} = 1/p_{ti}^2$$

—○ sequentially recombine particles:

1. compute all d_{ij} and d_{iB}
2. find the minimum of the d_{ij} and d_{iB}
3. if it is a d_{ij} , recombine i and j into a single new particle and return to step 1.
4. otherwise, if it is a d_{iB} , declare i to a [final state] jet, and remove it from the list
5. stop when no particles remain

↪ *jet grows around hard seeds*

↪ *collinear branchings clustered at the beginning*

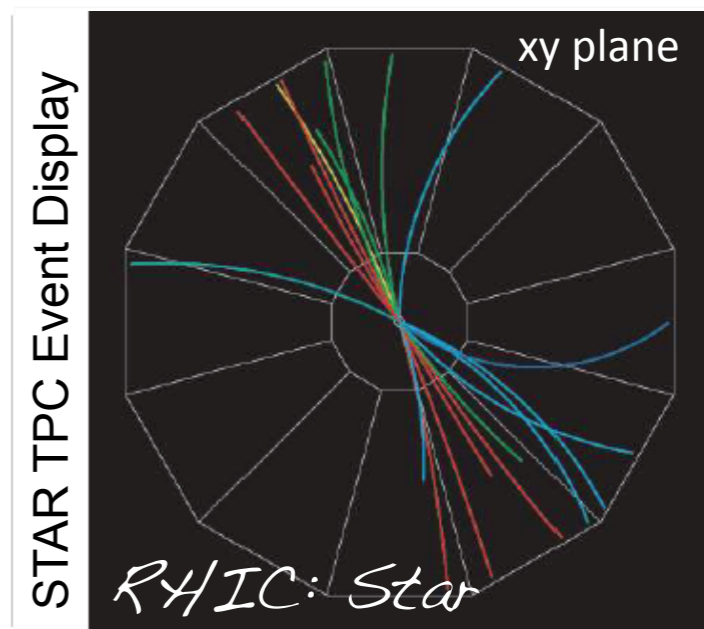
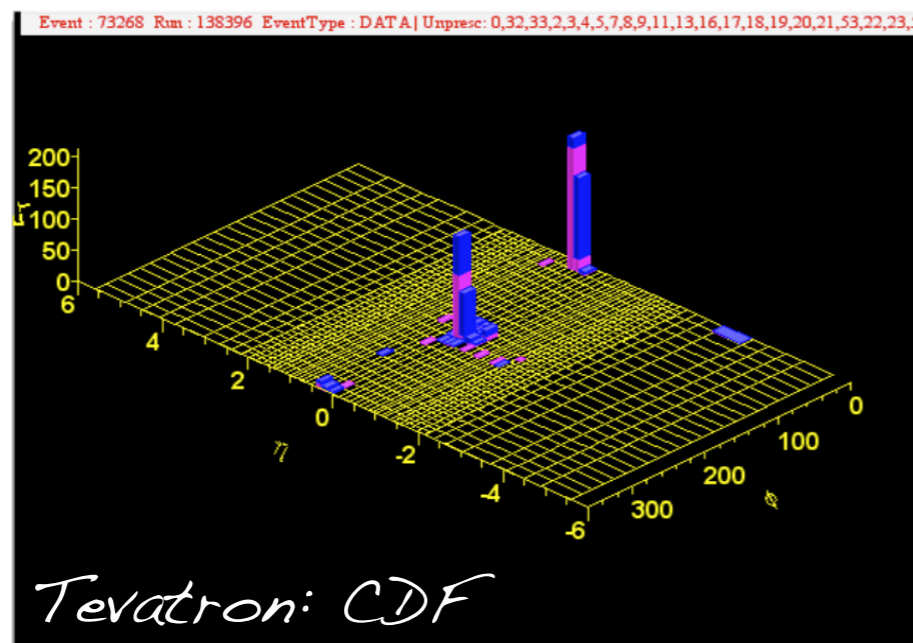
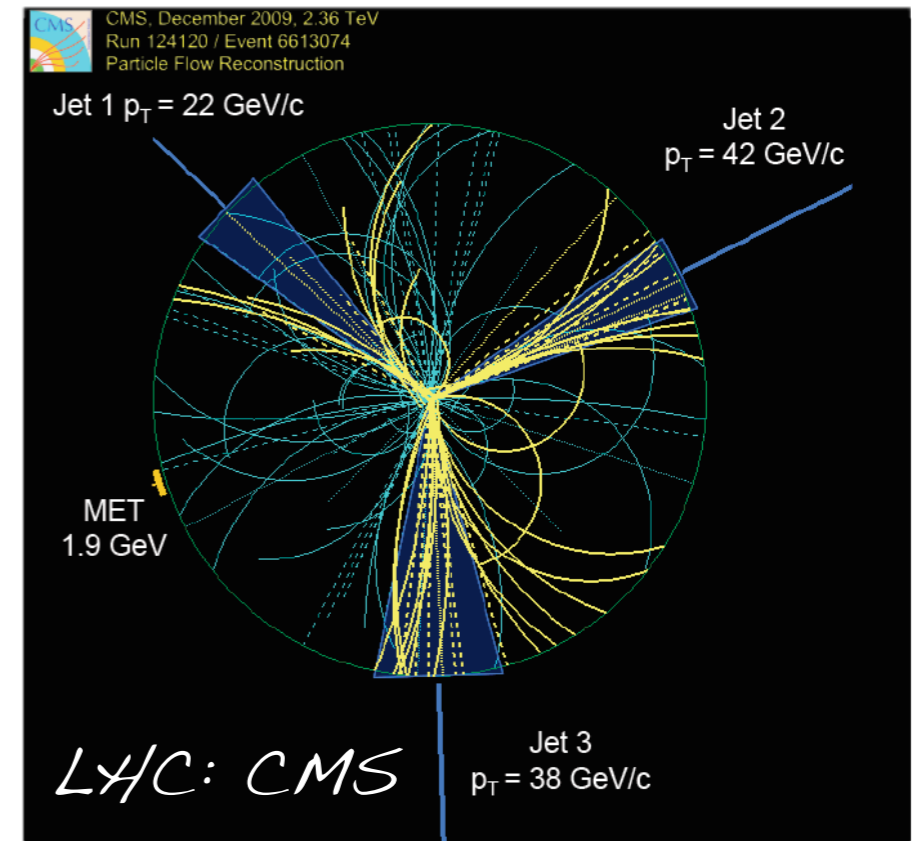
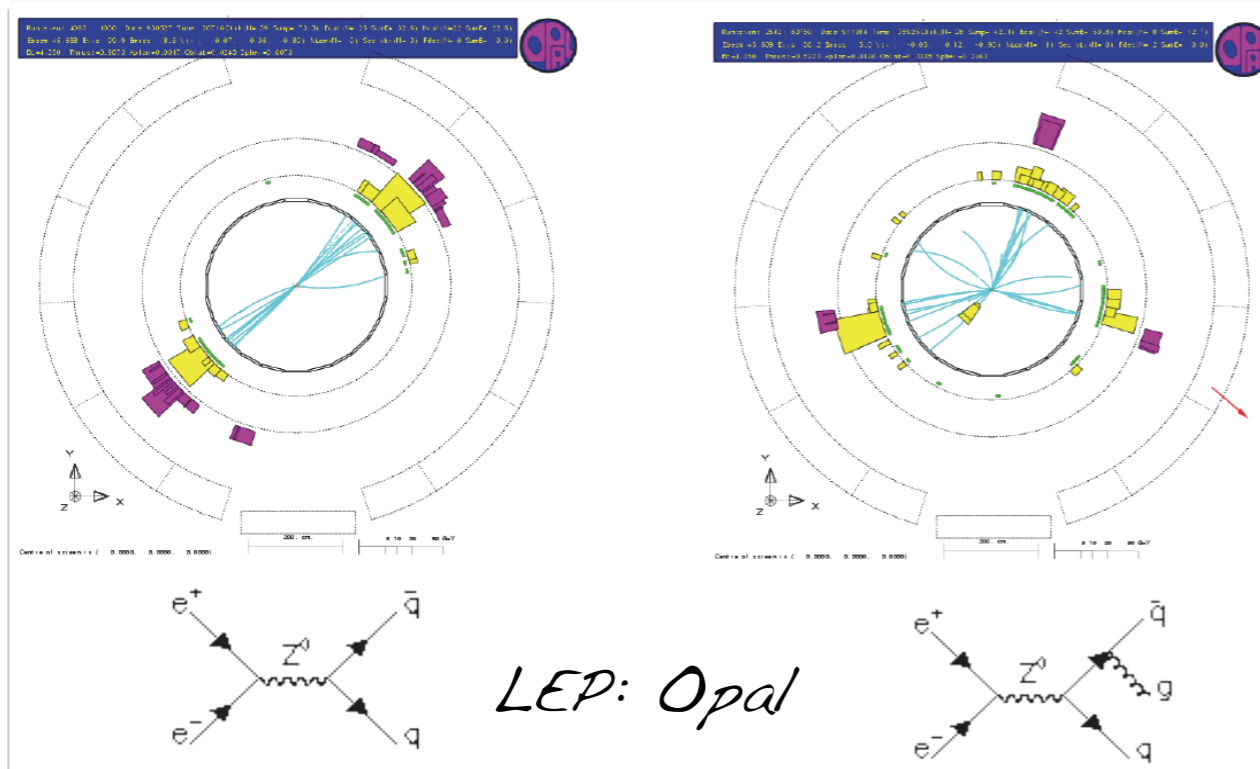
↪ *gives circular hard jets*

Jets

- experimental aspects

Mateusz Płoskon

Jets in collider experiments

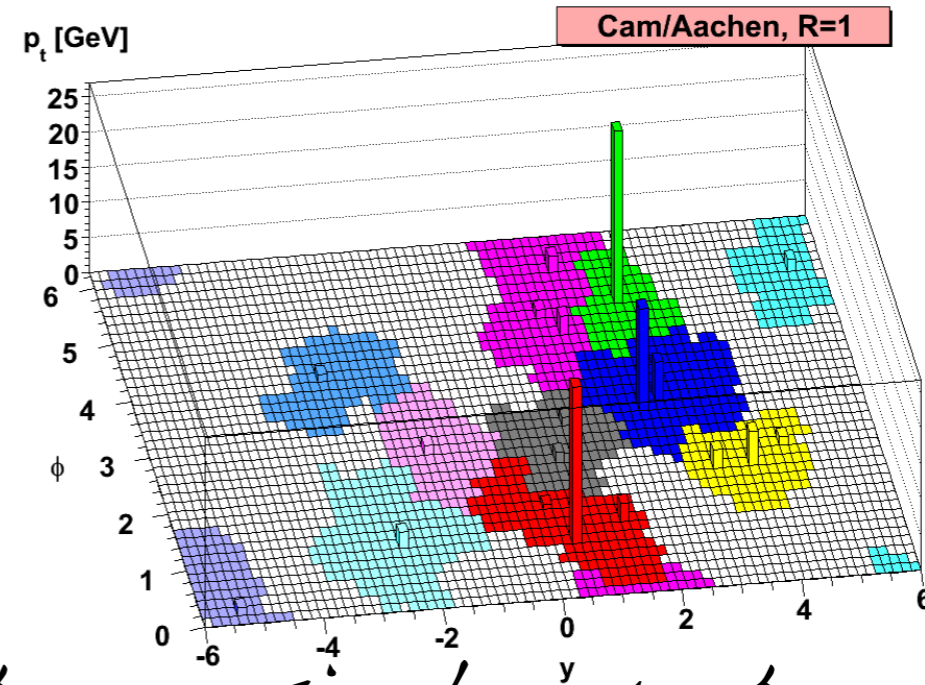
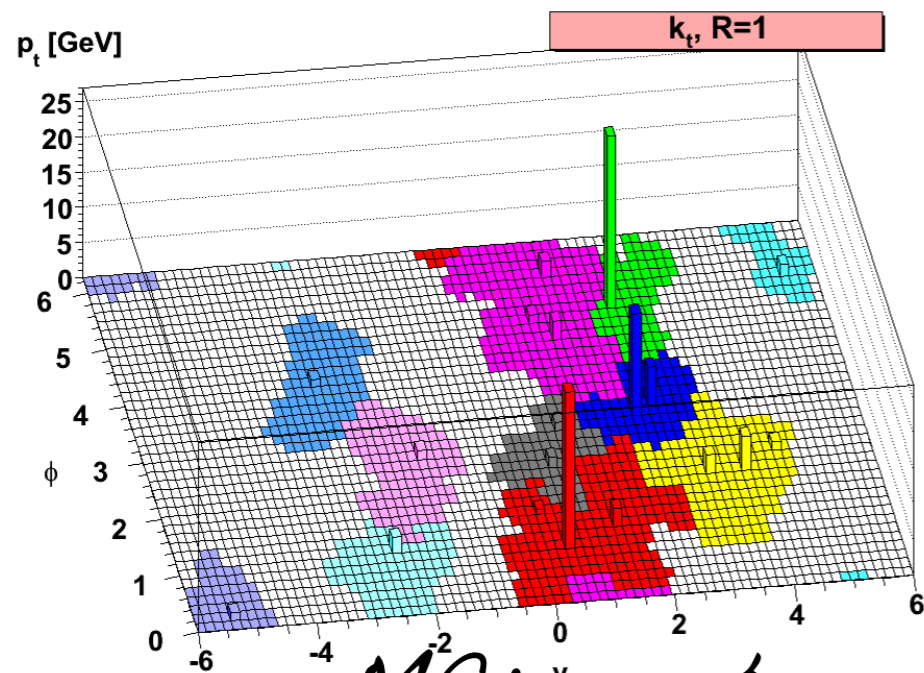


Optimum jet finder algorithm

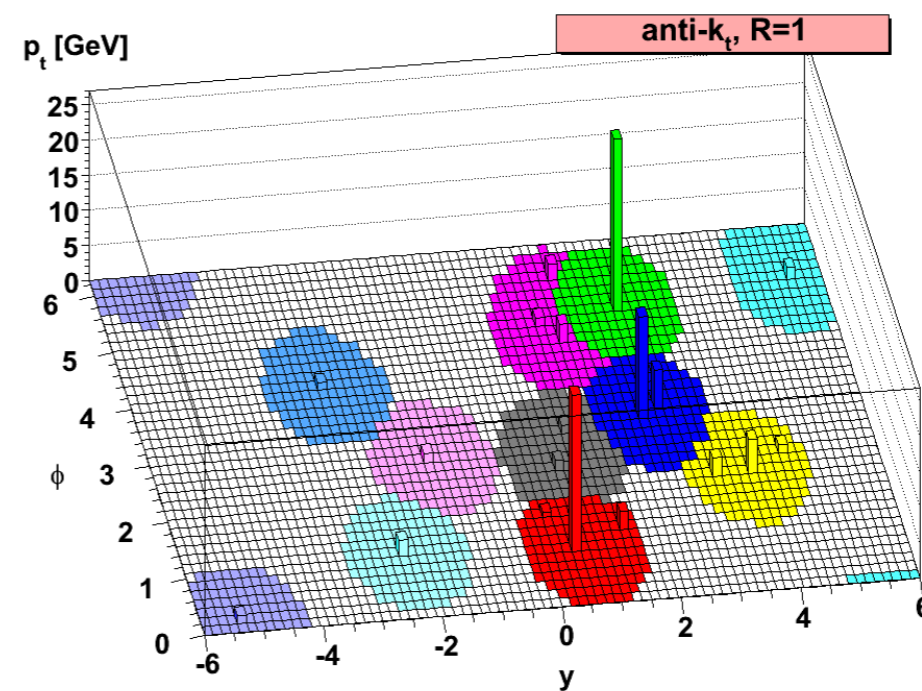
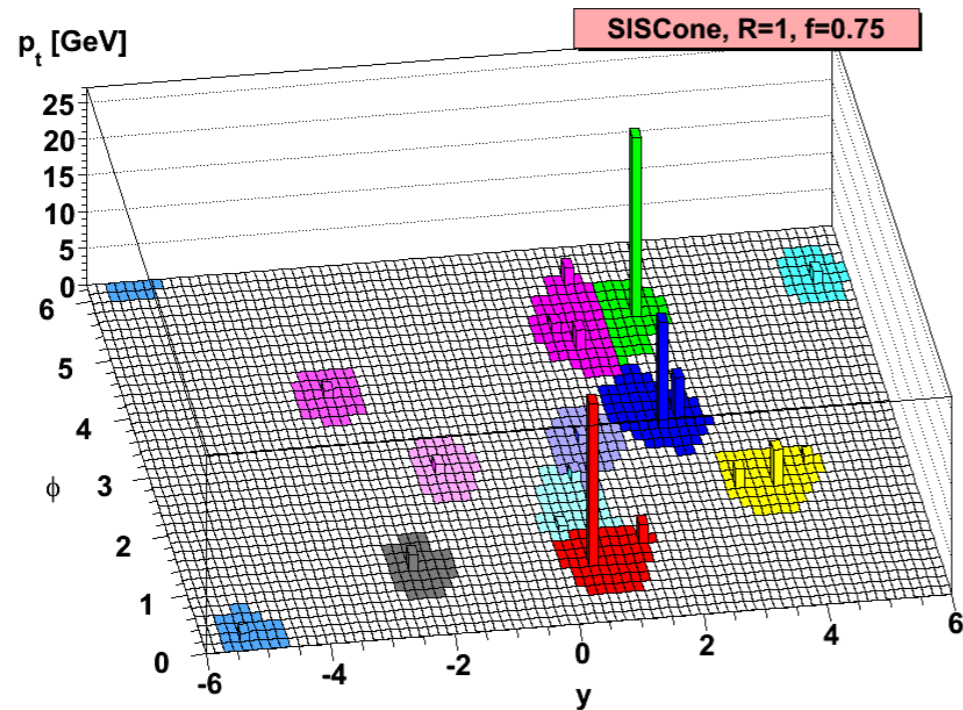
Several important properties that should be met by a jet definition are [3]:

1. Simple to implement in an experimental analysis;
2. Simple to implement in the theoretical calculation;
3. Defined at any order of perturbation theory;
4. Yields finite cross section at any order of perturbation theory;
5. Yields a cross section that is relatively insensitive to hadronization.

Jet finding - jet finders

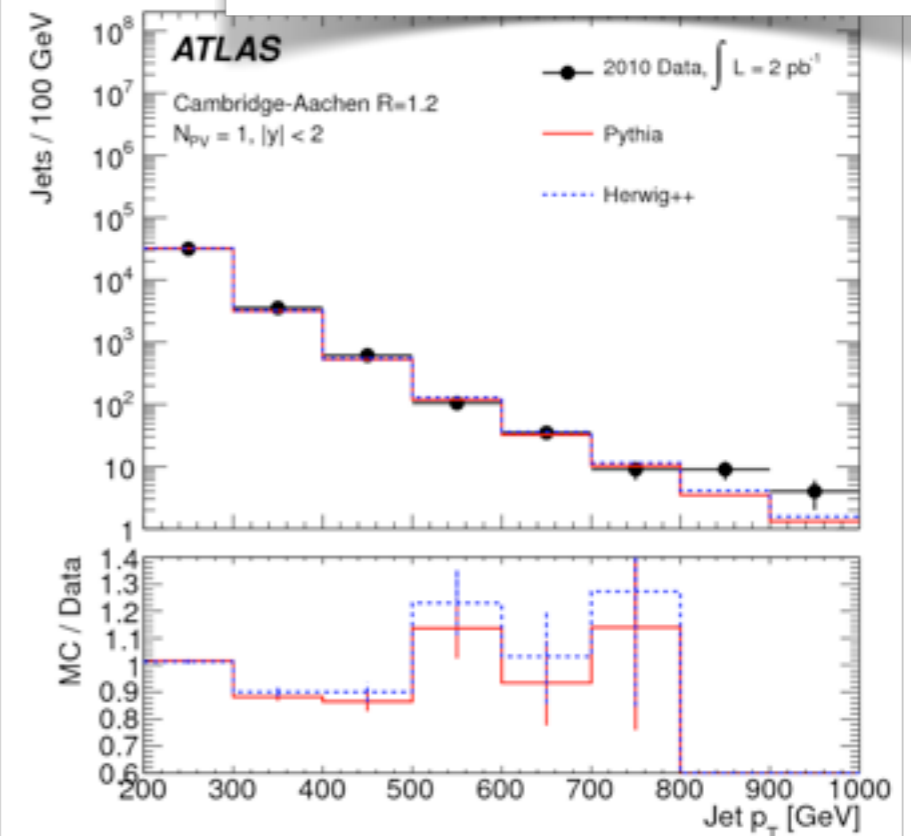
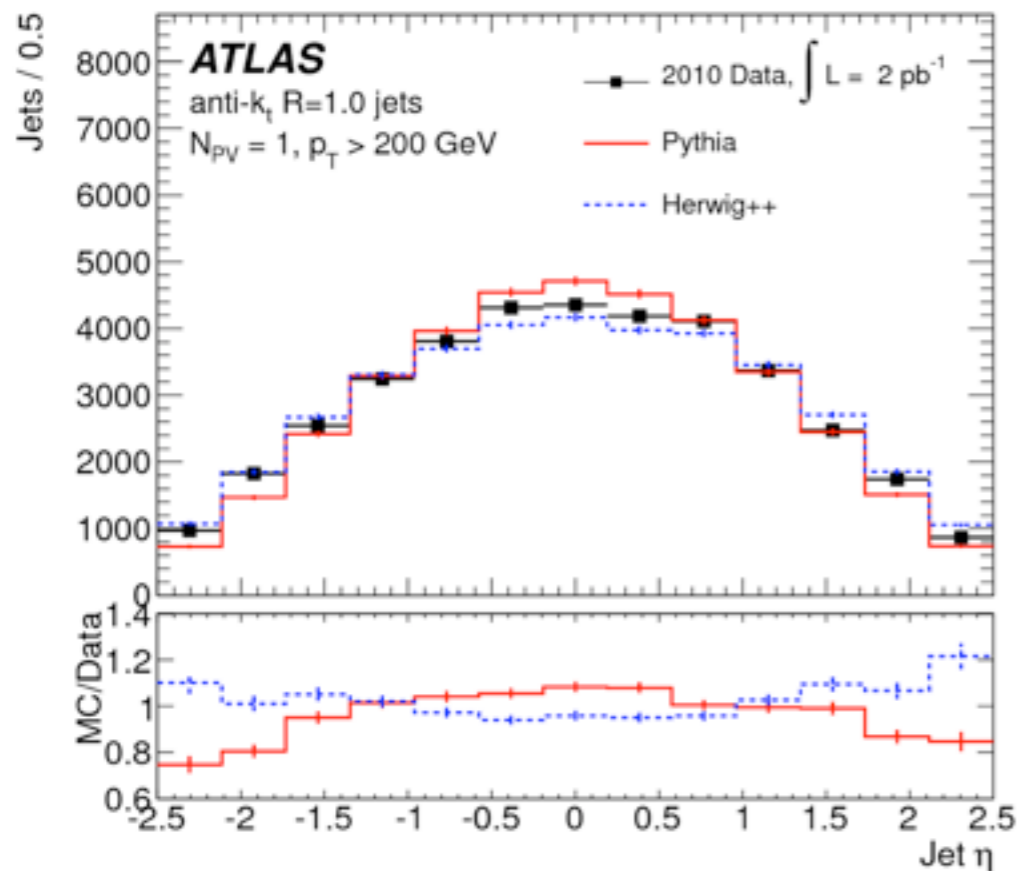
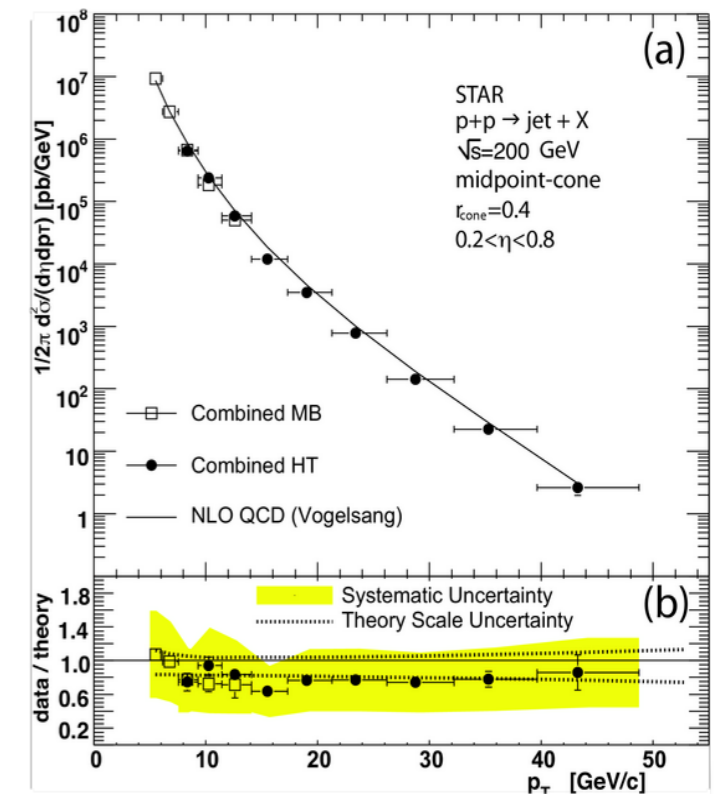
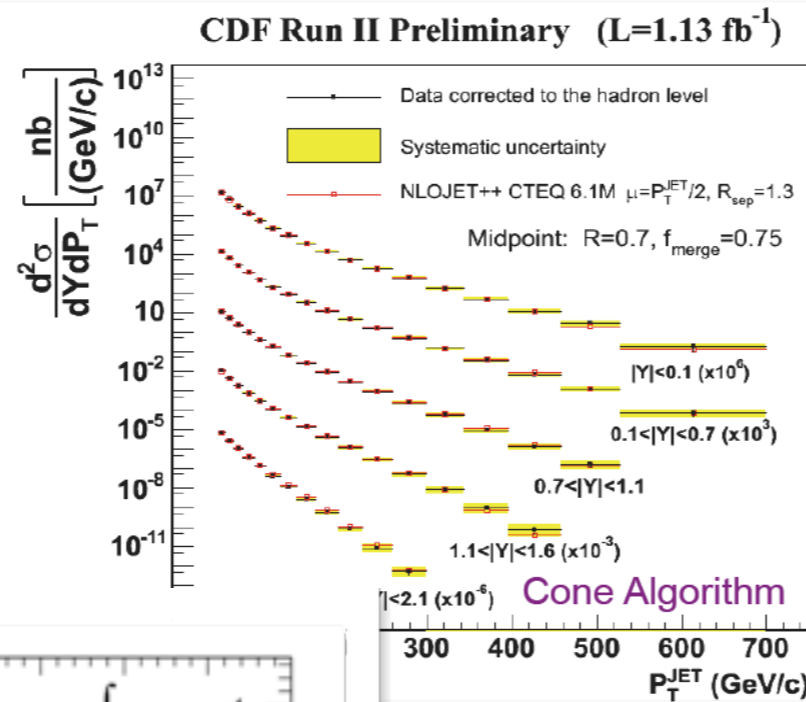


MC: proton-proton - single event

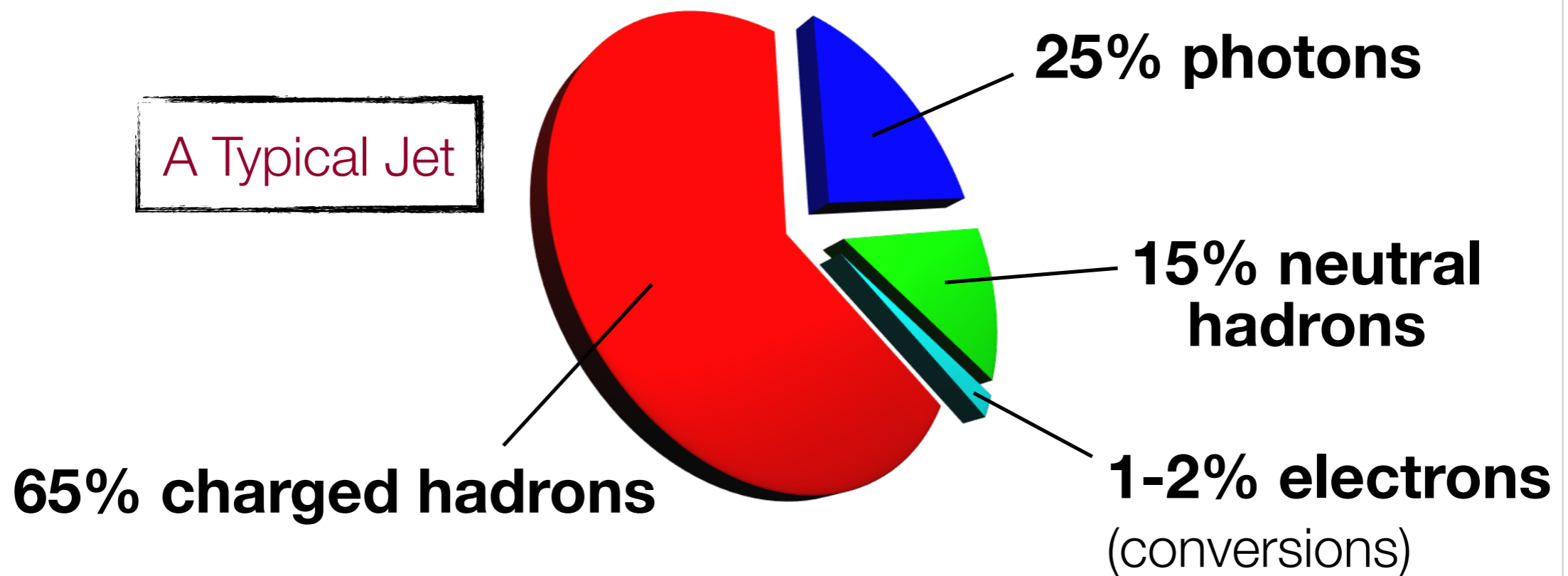


Jets in collider experiments

Jets are fairly well known by now... and well described by theory and MC



JET composition



Measure a jet?

Need to have control over all components...

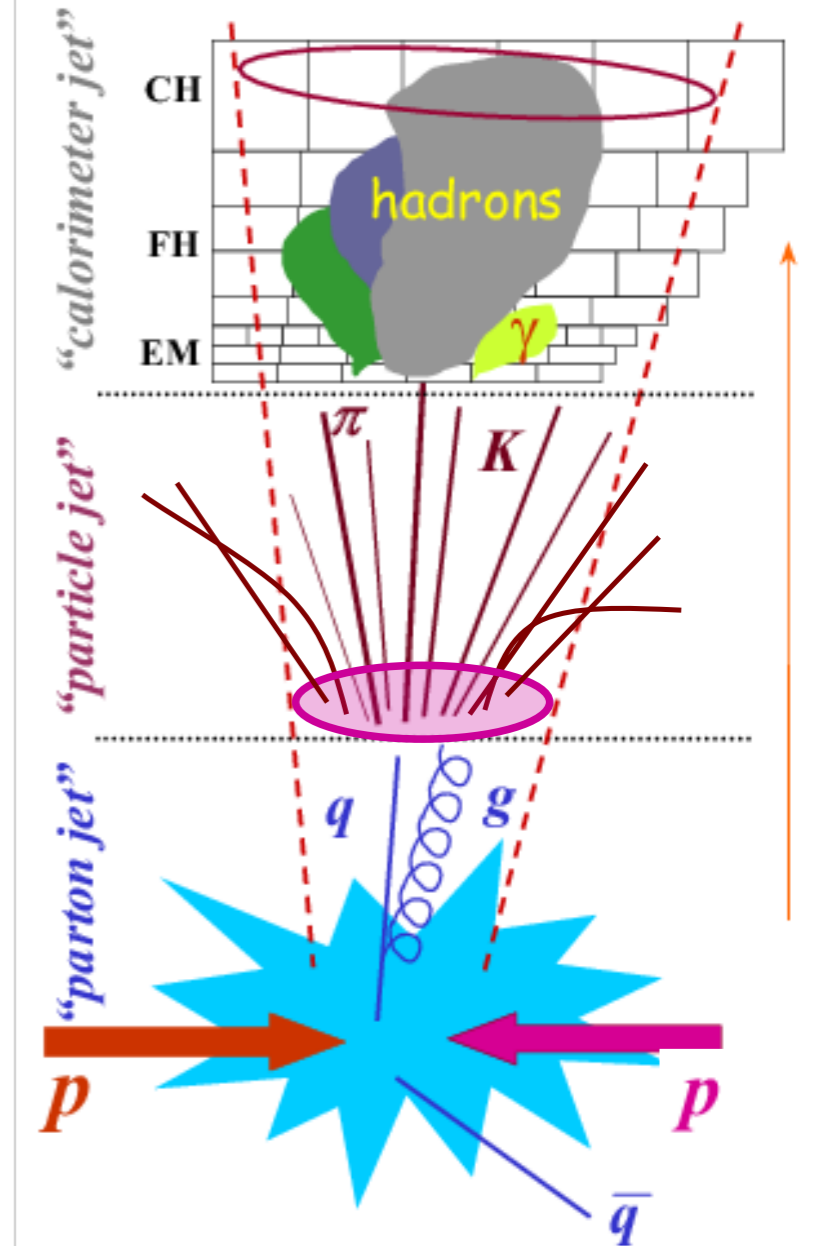
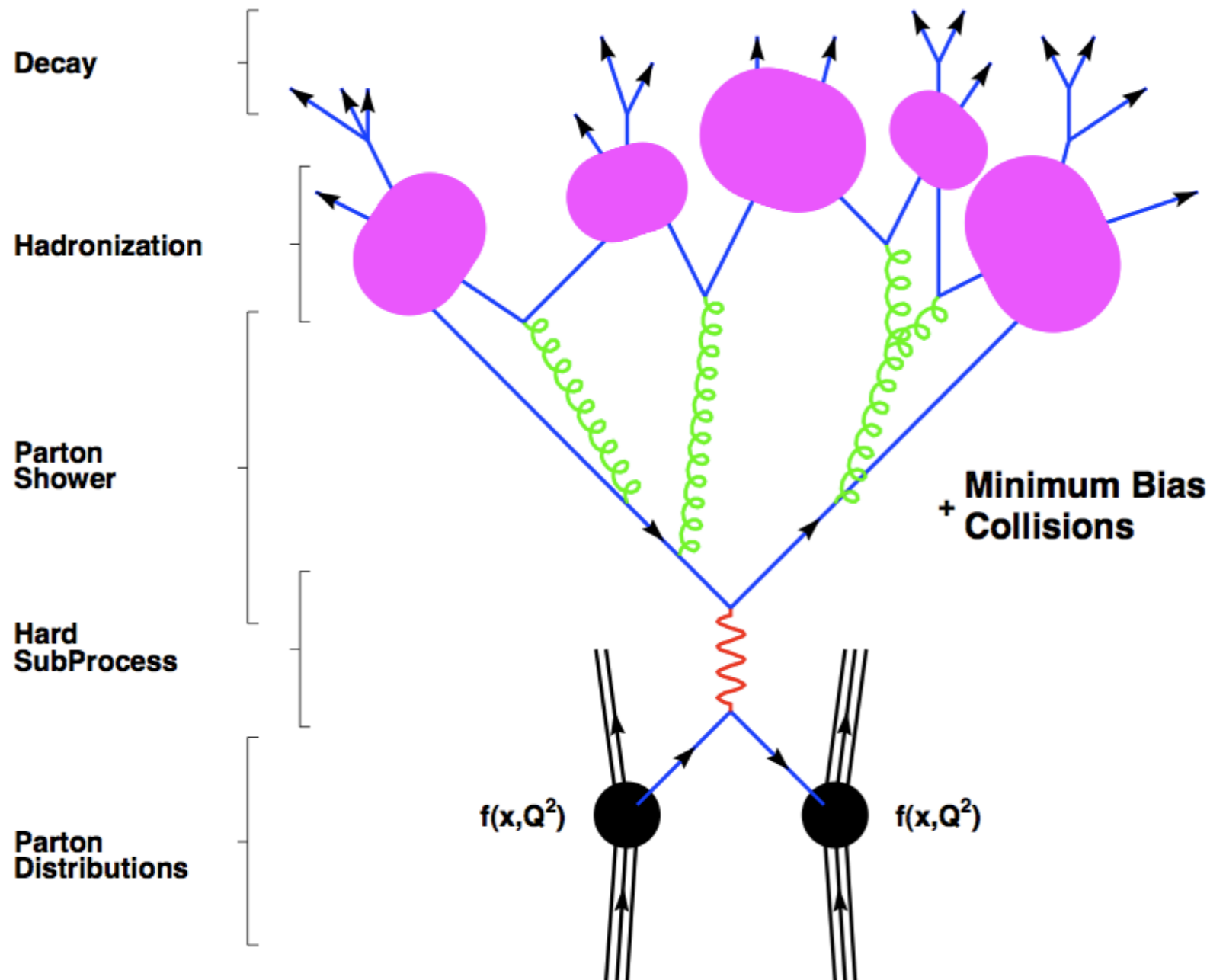
Measure or "know"

the [unknown] rest from DATA + MC

$$J(\vec{p}_{partons}) \approx J(\vec{p}_{shower}) \approx J(\vec{p}_{hadrons}) \approx J(\vec{p}_{cells/tracks})$$

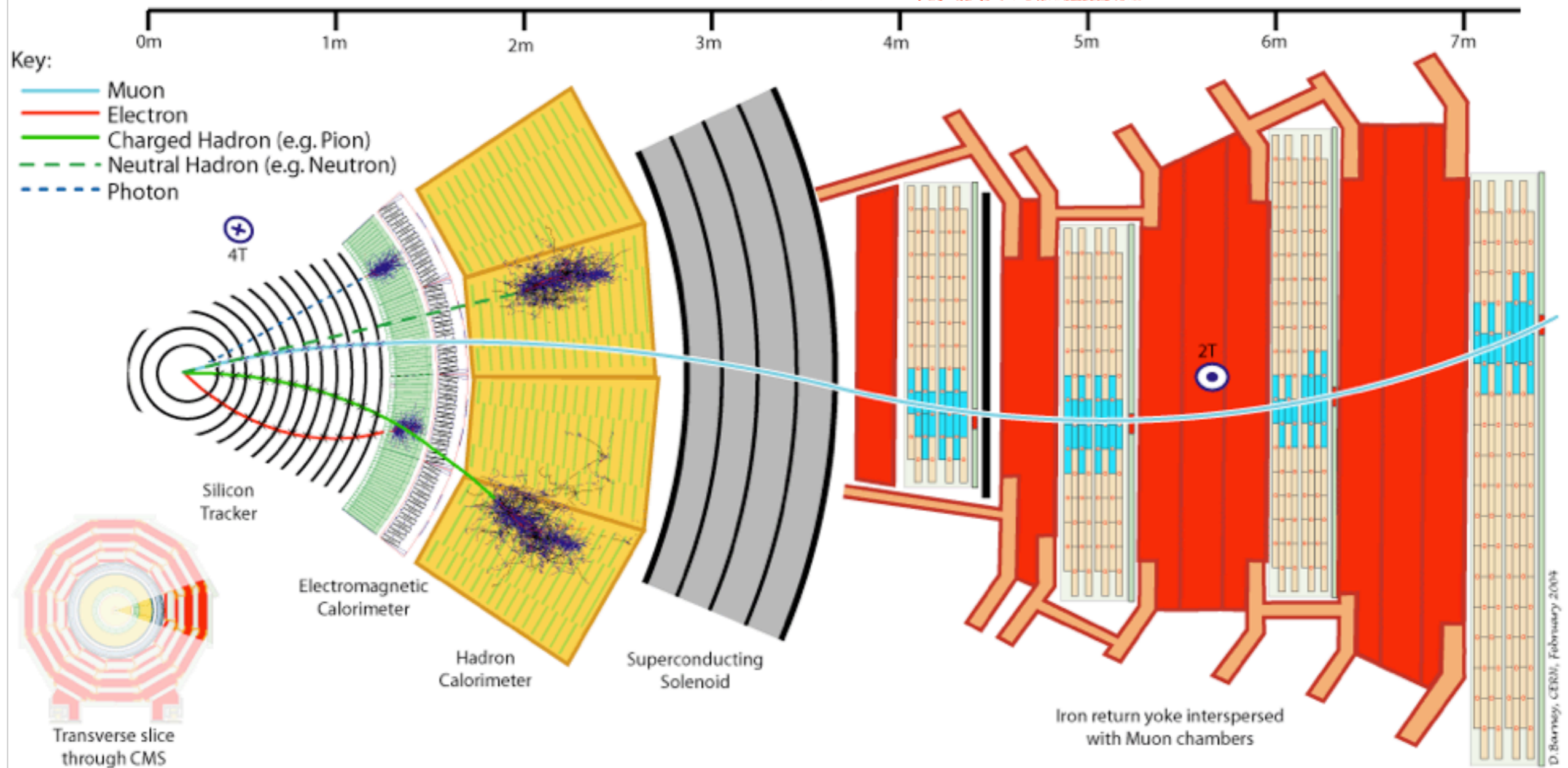
Jet: from parton to

detector

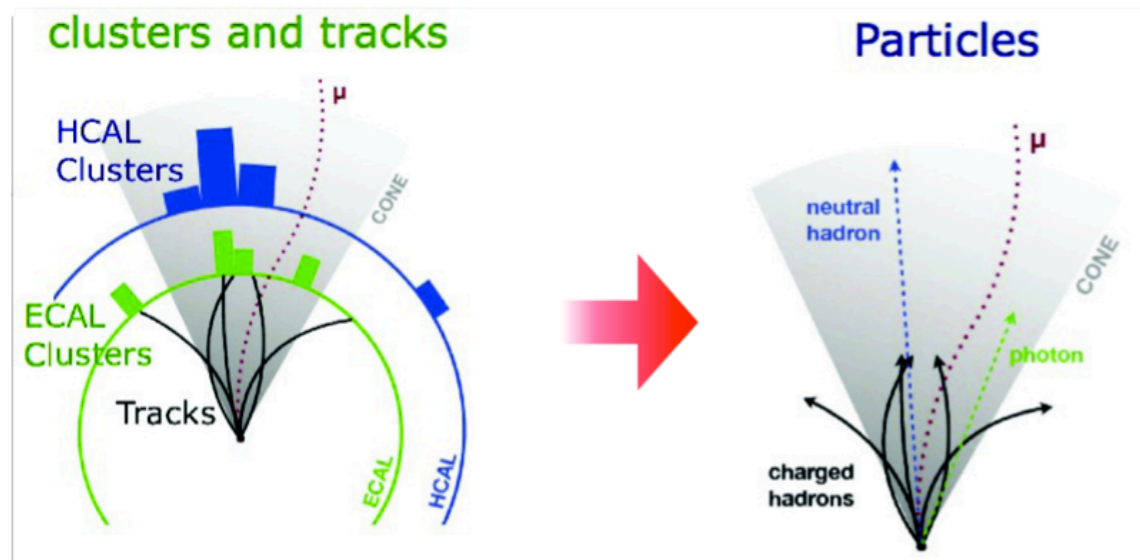


A Jet Detector

Primary sub-detectors: Silicon tracker, ECAL, HCAL muon chambers

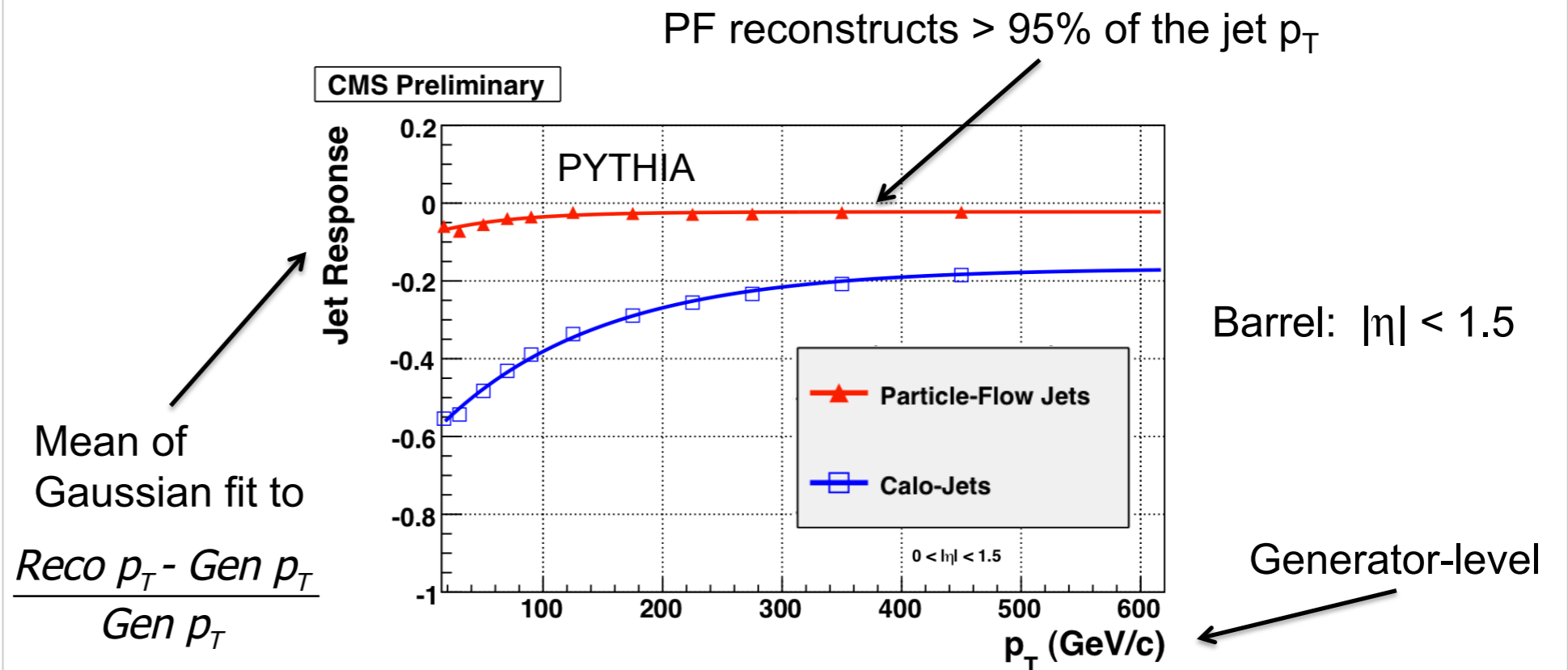


Improvements in jet reconstruction on detector level => Particle flow

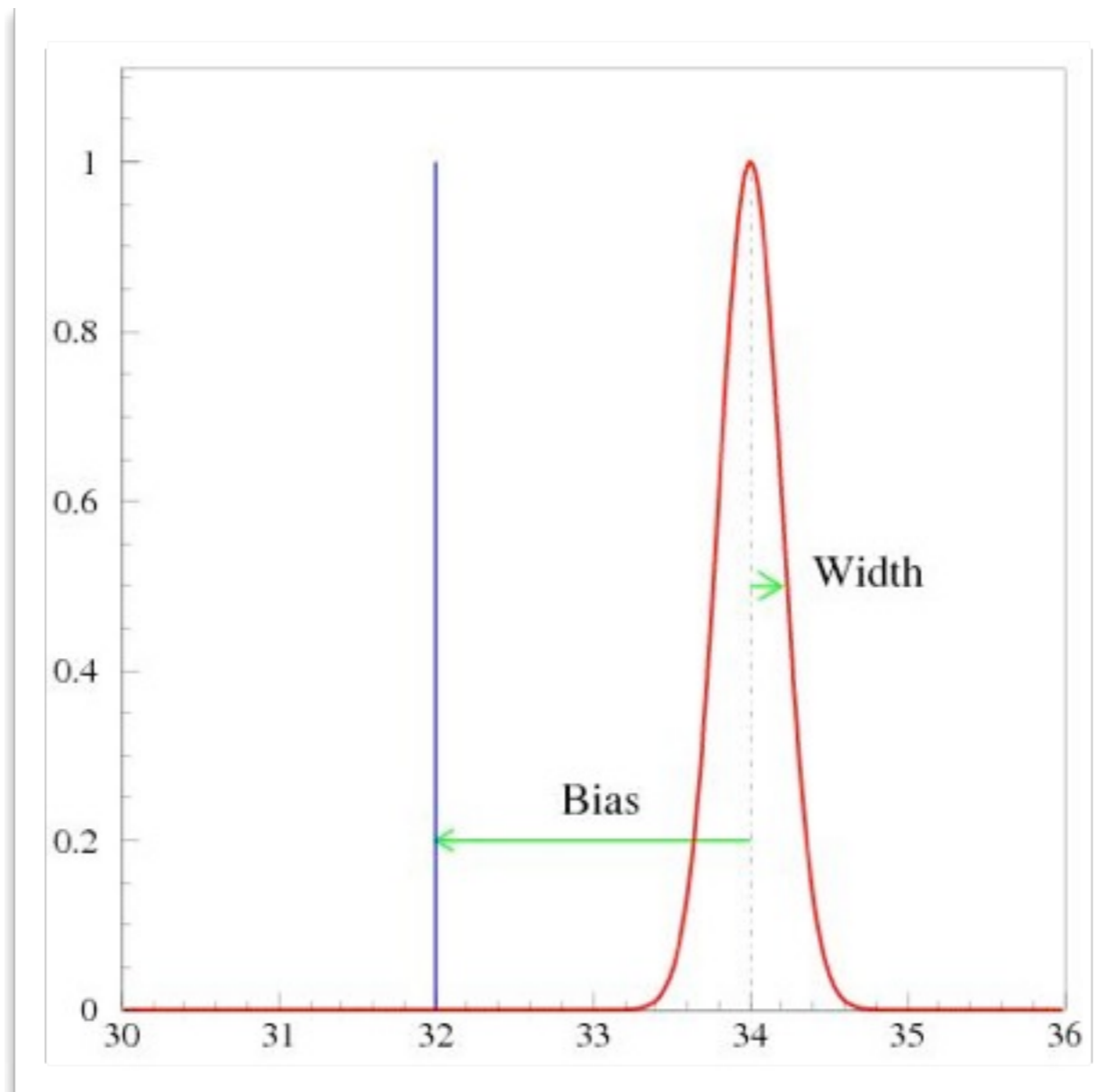


Purely calorimeter jet
vs. Particle Flow jet

Better response w.r.t.
calorimeter measurement
=> smaller jet-energy
corrections



Jet: energy scale & resolution

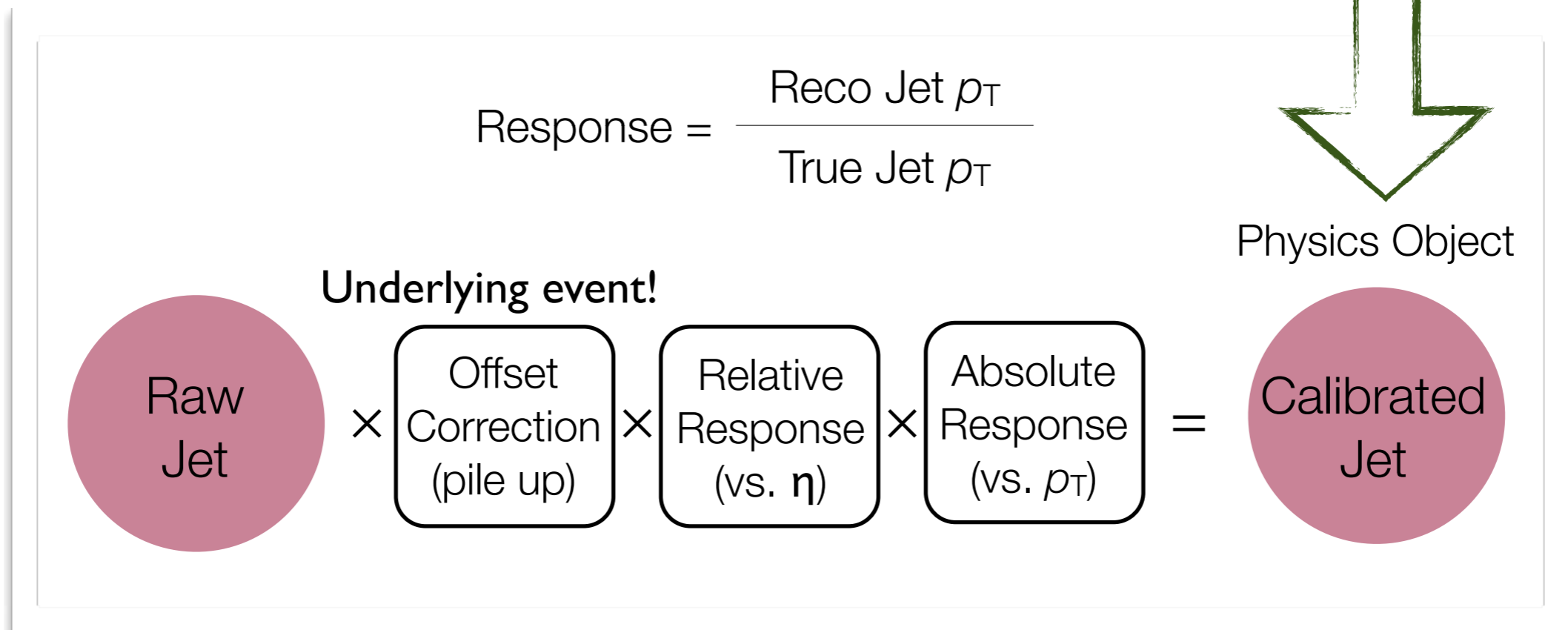


*Control over
the two
crucial
in p-p and AA
collisions*

Bias == Scale

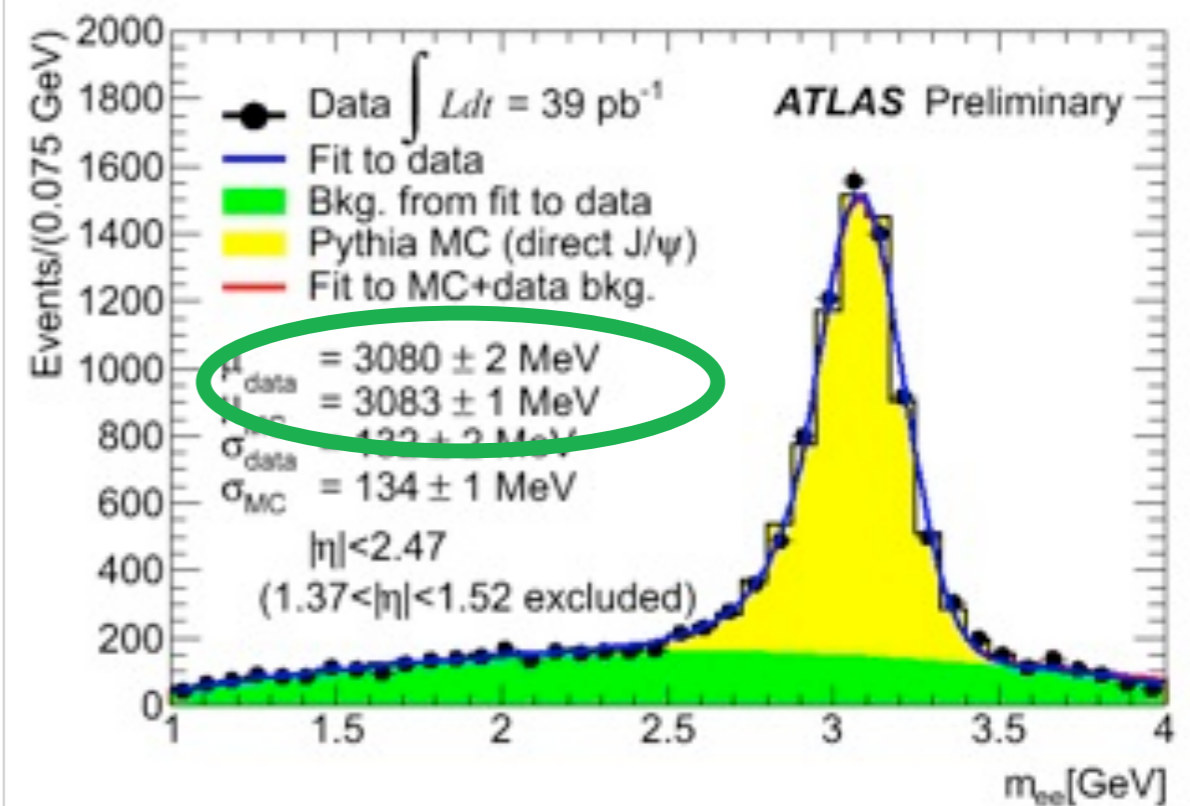
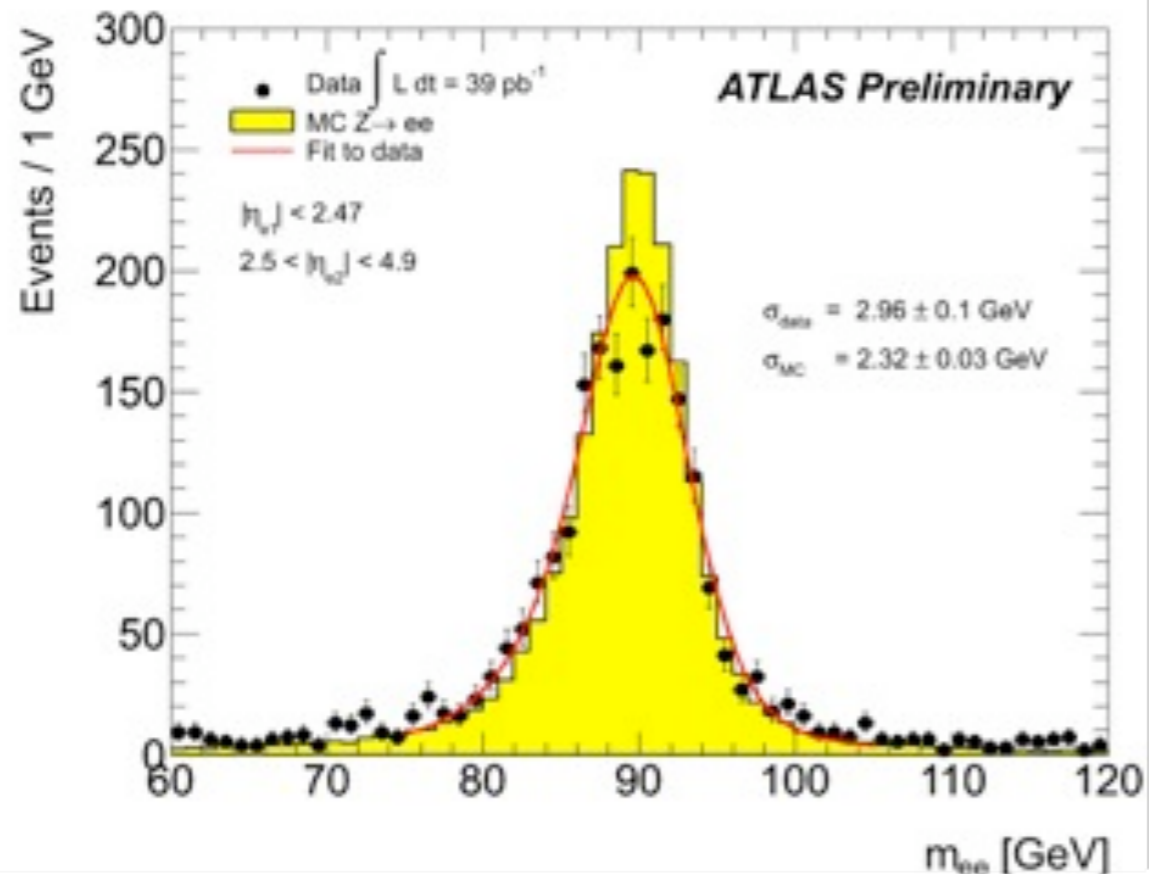
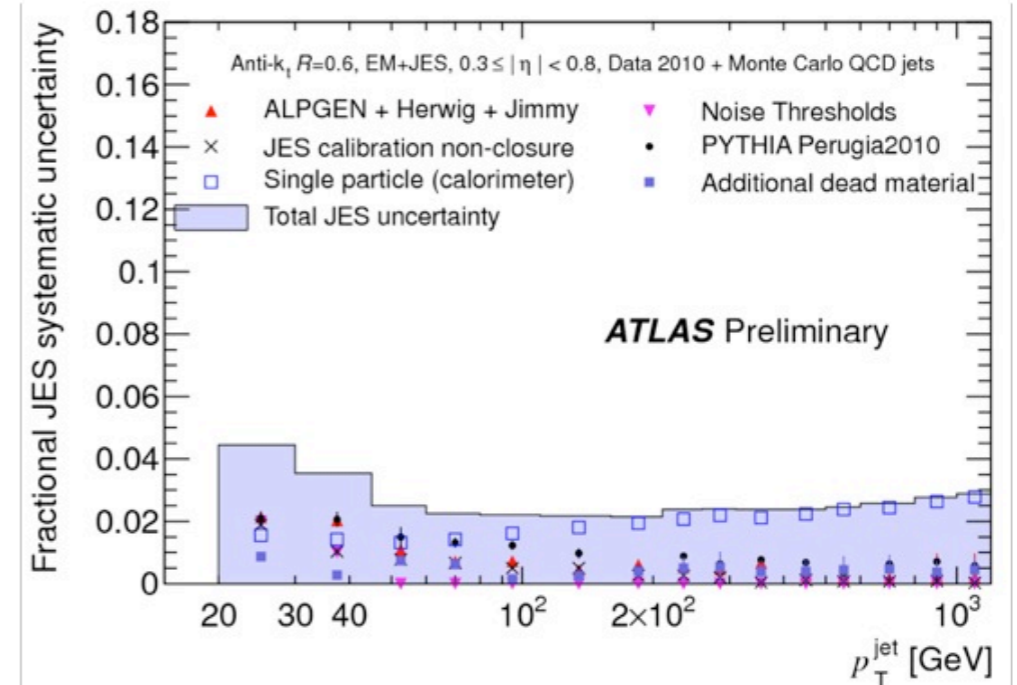
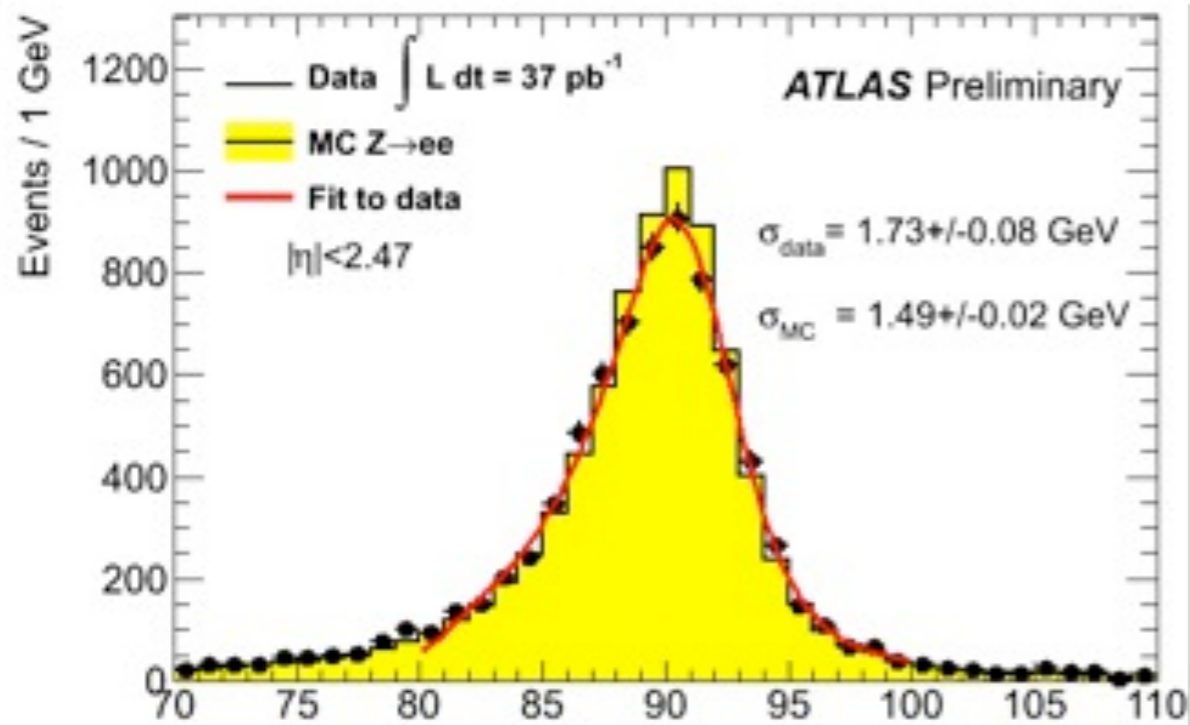
Width == Resolution

JET: From Measured to meaningful...



This is an experimental enterprise!
It is a substantial effort...

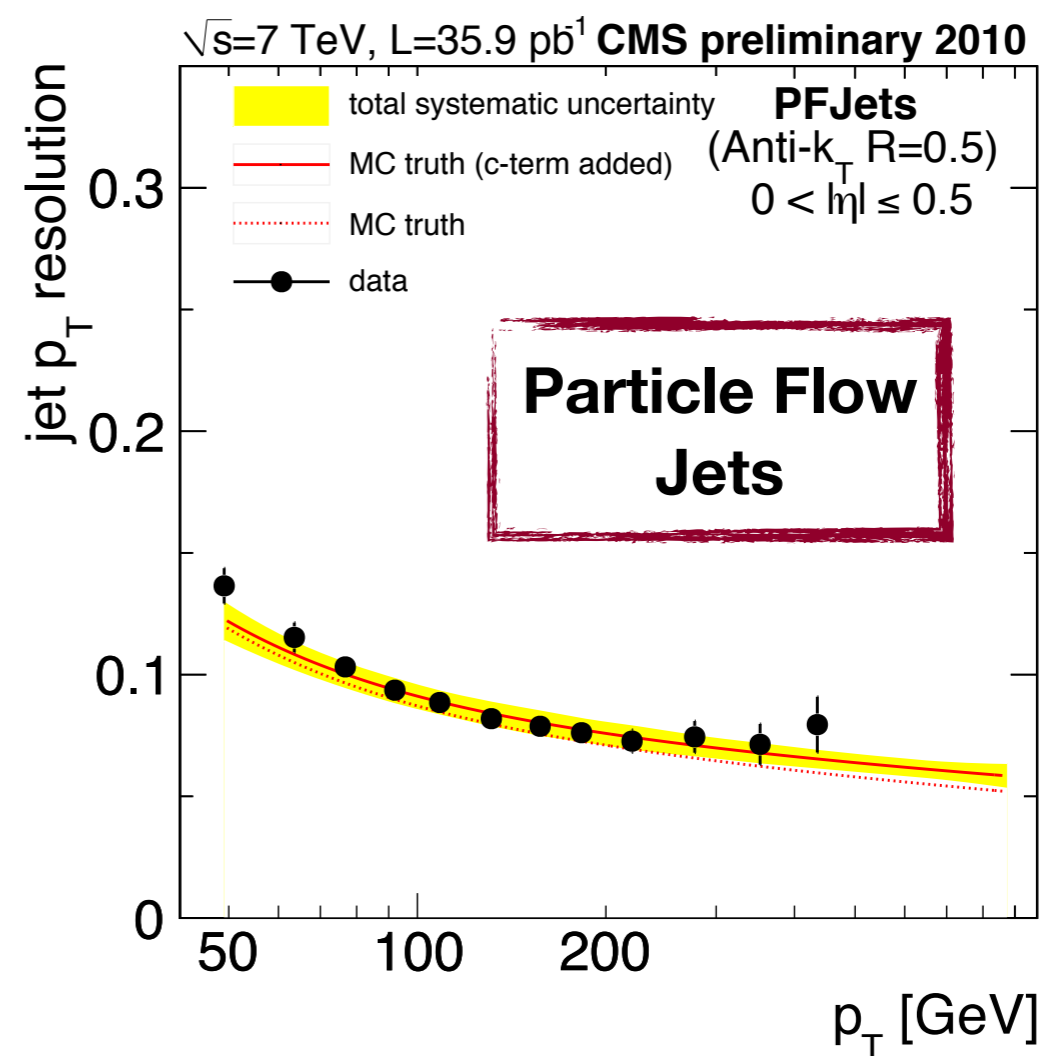
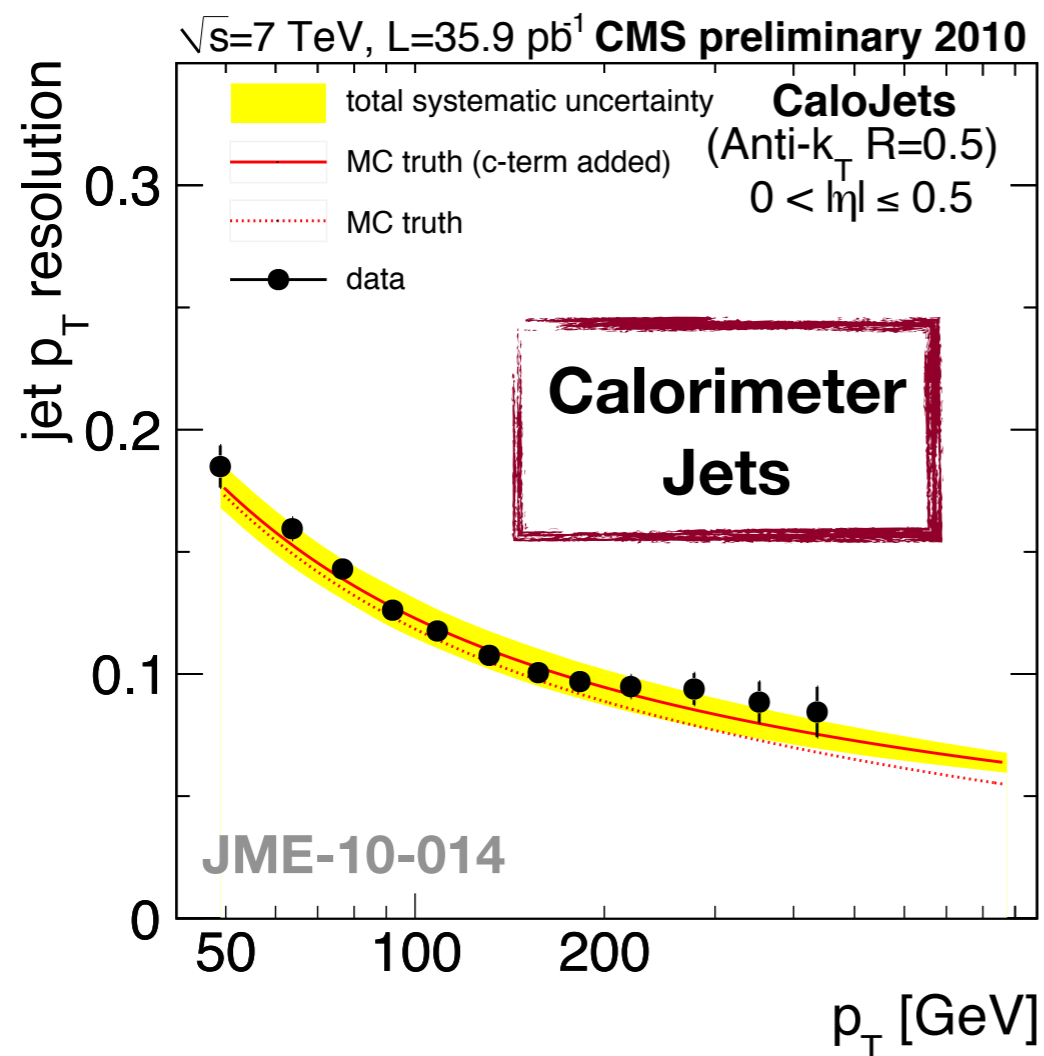
Control of the energy scale - ATLAS - linearity



Jet energy resolution

An example: proton-proton collisions

$$\mathcal{A} = \frac{p_T^{\text{Jet1}} - p_T^{\text{Jet2}}}{p_T^{\text{Jet1}} + p_T^{\text{Jet2}}} \longrightarrow \frac{\sigma(p_T)}{p_T} = \sqrt{2} \sigma_{\mathcal{A}}$$



jet-medium interactions

Casalderrey-Solana, Salgado, Introductory lectures on jet quenching, arXiv:0712.3443 [hep-ph]
JGM, *High- p_t in heavy ion collisions: an abridged overview*, arXiv:1202.0646 [hep-ph]

high- p_t processes in heavy ion collisions

- factorized description of hadron production at high- p_t in heavy ion collisions is a, phenomenological consistent, working assumption

$$\sigma^{AB \rightarrow h} \sim f_i^A(x_1, Q^2) \otimes f_j^B(x_2, Q^2) \otimes \sigma^{ij \rightarrow k} \otimes D_{k \rightarrow h}(z, Q^2)$$

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PDFs [initial state]

- universal, non-perturbative
- scale dependence from DGLAP evolution
- determined from global fits [eA, pA]
- control of nuclear modifications essential
[cold nuclear matter effects]

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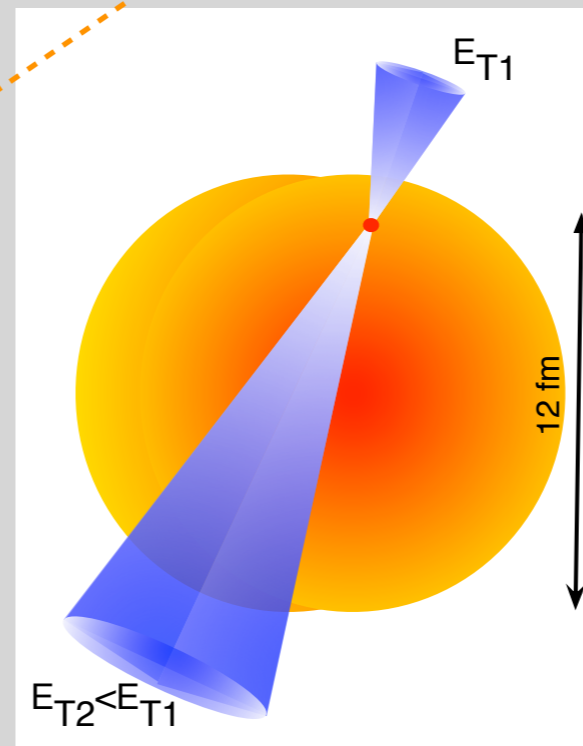
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- localized on point-like scale [$\sim 1/E_T$] and thus oblivious to the surrounding QCD medium



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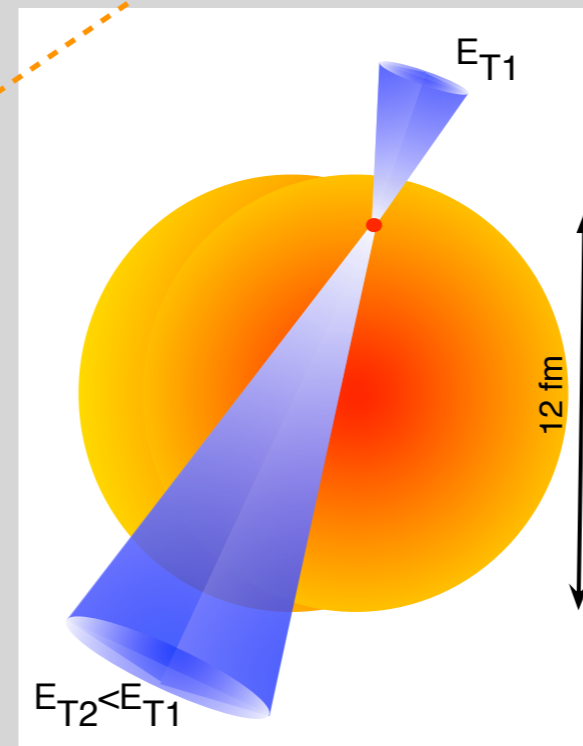
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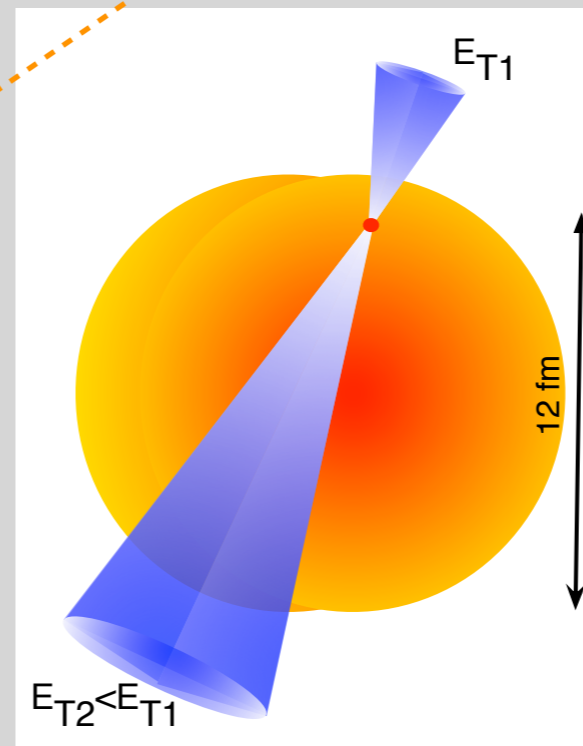
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jet quenching :: the modifications effected on the propagating parton, and on its shower, by the QCD medium it traverses

dual role of jet quenching studies

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- ultimately jet quenching studies [medium induced modifications of observed properties of high- p_t properties] allow for detailed characterization of produced medium
 - ↪ high- p_t probes are created early
 - ↪ their production mechanism is under good theoretical control
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 - ↪ the observable consequences of probe-medium interactions encode detailed information on medium properties

HOWEVER

- full potential as medium probes limited by theoretical understanding of the microscopic dynamics responsible for the observed modifications
 - ↪ jet quenching studies provide the necessary constraints on the dynamics

dual role of jet quenching studies

- ultimately jet quenching studies [medium induced modifications of observed properties of high- p_t properties] allow for detailed characterization of produced medium
 - ↪ high- p_t probes are created early
 - ↪ their production mechanism is under good theoretical control
 - ↪ they can traverse a significant in-medium path length
 - ↪ the observable consequences of probe-medium interactions encode detailed information on medium properties

HOWEVER

- full potential as medium probes limited by theoretical understanding of the microscopic dynamics responsible for the observed modifications
 - ↪ jet quenching studies provide the necessary constraints on the dynamics

what can conceivably happen to a jet that develops in the presence of a hot, dense and coloured medium?

jet-medium interactions [jet quenching]

induced radiation

- medium transfers momentum to jet components
 - :: increases splitting probability and broadens radiation
 - :: finite quark mass vetos small angle radiation [dead cone]
- medium disturbs coherence between successive splittings
 - :: modified angular pattern

→ K.Tywoniuk [Tue 12.15]

dynamics of emitted quanta

- transverse transport of all jet components

color exchanges with medium

- modified colour flow in the jet
 - :: affects hadronization irrespectively of where it occurs

→ A.Beraudo [Tue 11.45]

medium response to jet propagation

- recoil, ...

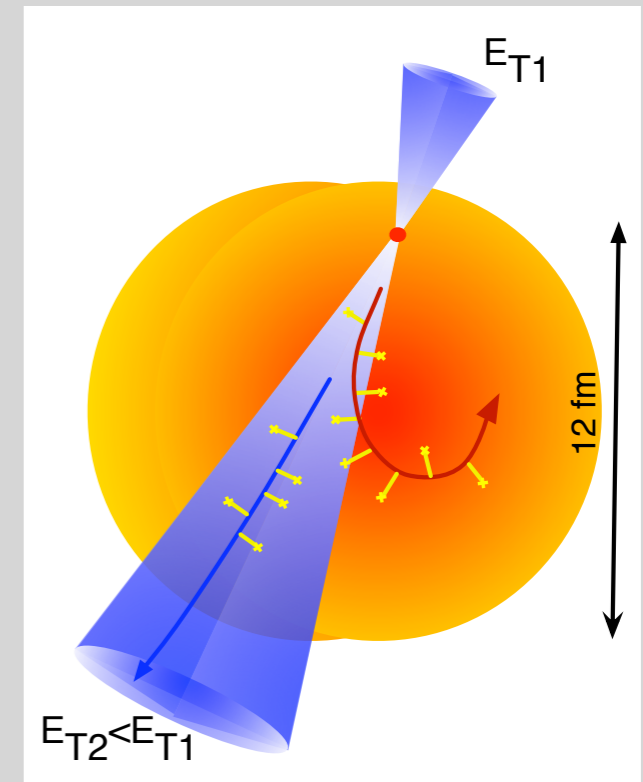
→ T.Renk [Tue 9.00]

modelling

- piecewise description
- first principle probabilistic or effective formulation for Monte Carlo implementation
- embedding in medium

observables

- jet quenching without jets
 - ↪ hadronic spectra [R_{AA} , correlations, etc...]
 - ↪ in principle very sensitive to hadronization effects
- jet quenching with reconstructed jets
 - ↪ in principle less sensitive to hadronization details
 - ↪ mechanisms irrelevant for parton energy loss may play significant role
 - a gluon radiated from the hard parton is energy lost for that parton, but not necessarily so for that parton's jet



parton energy loss [schematic]

- Brownian motion

$$\langle k_{\perp}^2 \rangle \sim \hat{q} L$$

- accumulated phase

$$\left\langle \frac{k_{\perp}^2 L}{\omega} \right\rangle \sim \frac{\hat{q} L^2}{\omega} \sim \frac{\omega_c}{\omega}$$

characteristic gluon energy

- number of coherent scatterings

$$N_{coh} \sim \frac{t_{coh}}{\lambda}$$

$$t_{coh} \sim \frac{\omega}{k_{\perp}^2} \sim \sqrt{\frac{\omega}{\hat{q}}}$$

$$k_{\perp}^2 \sim \hat{q} t_{coh}$$

1 parameter medium definition

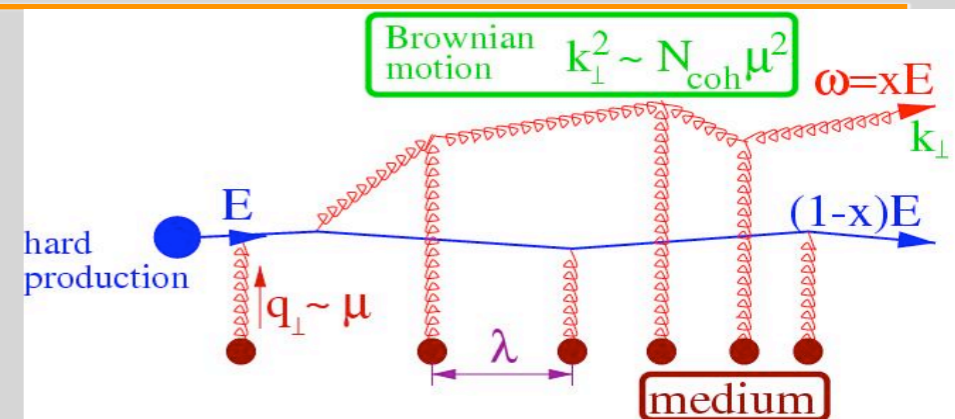
- gluon energy distribution

$$\omega \frac{dI_{med}}{d\omega dz} \sim \frac{1}{N_{coh}} \omega \frac{dI_1}{d\omega dz} \sim \alpha_s \sqrt{\frac{\hat{q}}{\omega}}$$

non-abelian LPM

- average energy loss

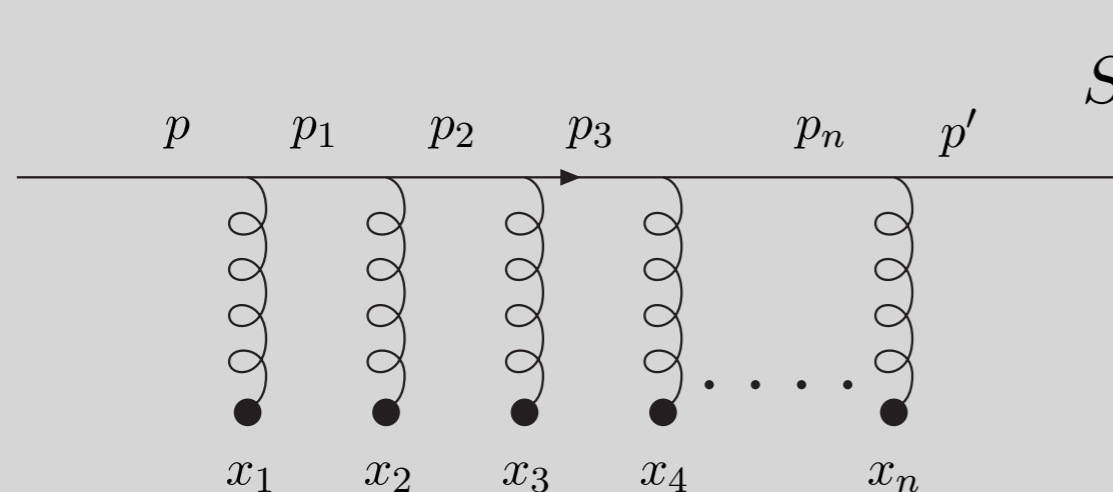
$$\Delta E = \int_0^L dz \int_0^{\omega_c} \omega d\omega \frac{dI_{med}}{d\omega dz} \sim \alpha_s \omega_c \sim \alpha_s \hat{q} L^2$$



$$\hat{q} \simeq \frac{\mu^2}{\lambda}$$

in-medium parton propagation

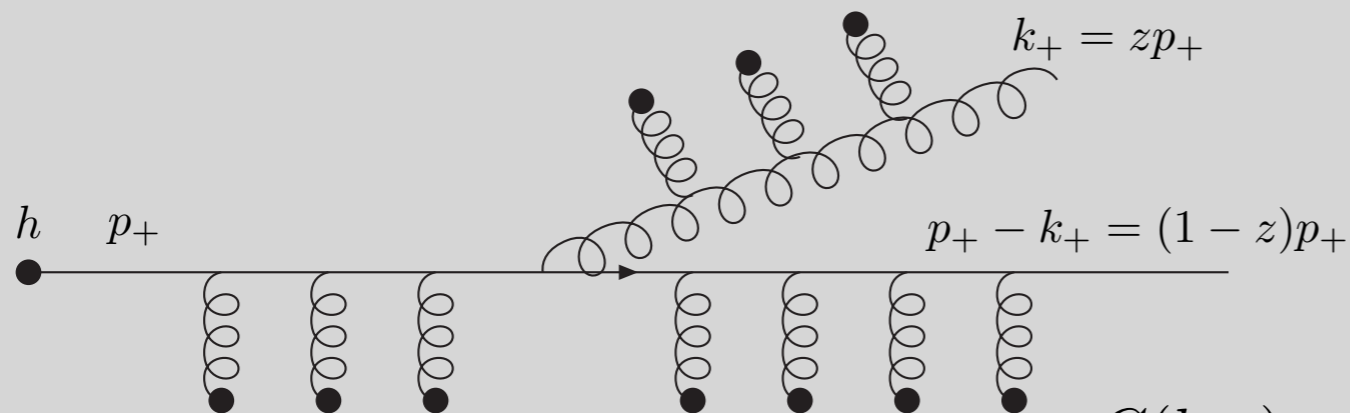
medium as set of static localized scattering centres



$$S_1(p', p) = \int d^4x \, e^{i(p'-p) \cdot x} \, \bar{u}(p') \, ig A_\mu^a(x) T^a \gamma^\mu \, u(p)$$

$$W(\mathbf{x}) = \mathcal{P} \exp \left[ig \int dx_+ A_-(x_+, \mathbf{x}) \right]$$

eikonal propagation [parton energy much larger than medium kicks]

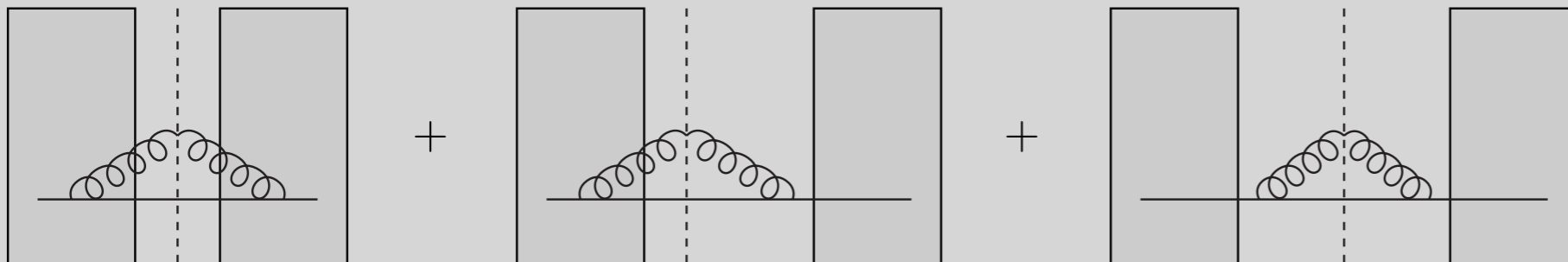


$$G(b, a) = \int \mathcal{D}\mathbf{r}(x_+) \exp \left\{ i \frac{p_+}{2} \int dx_+ \left[\frac{d\mathbf{r}}{dx^+} \right]^2 \right\} W(\mathbf{r})$$

beyond, but close to, eikonal propagation [allow for transverse brownian motion] of radiated gluon

single gluon emission [BDMPS]

building block for parton energy loss calculation [modified splitting kernel]



$$\begin{aligned}
 \langle |\mathcal{M}_{a \rightarrow bc}|^2 \rangle = & \frac{g^2}{N^2 - 1} 2\text{Re} \left[\frac{1}{k_+^2} \int_{x_{0+}}^{L_+} dx_+ \int_{x_+}^{L_+} d\bar{x}_+ \int d\mathbf{x} d\bar{\mathbf{x}} e^{i\mathbf{k}_\perp (\mathbf{x} - \bar{\mathbf{x}})} \times \right. \\
 & \left\langle W_{aa_1}(\mathbf{0}, x_{0+}, x_+) T_{a_1 b_1}^{c_1} \frac{\partial}{\partial \mathbf{y}} G_{c_1 c}(\mathbf{y} = 0, x_+; \mathbf{x}, L_+) W_{b_1 b}(\mathbf{0}, x_+, L_+) \times \right. \\
 & W_{b\bar{b}_1}^\dagger(\mathbf{0}, \bar{x}_+, L_+) \frac{\partial}{\partial \bar{\mathbf{y}}} G_{c\bar{c}_1}(\bar{\mathbf{x}}, L_+; \bar{\mathbf{y}} = 0, \bar{x}_+) T_{\bar{b}_1 \bar{a}_1}^{\bar{c}_1} W_{\bar{a}_1 a}^\dagger(\mathbf{0}, x_{0+}, \bar{x}_+) \left. \right\rangle - \\
 & - \frac{2}{k_+} \frac{\mathbf{k}_\perp}{k_\perp^2} \int_{x_{0+}}^{L_+} dx_+ \int d\mathbf{x} e^{i\mathbf{k}_\perp \cdot \mathbf{x}} \left\langle W_{aa_1}(\mathbf{0}, x_{0+}, x_+) T_{a_1 b_1}^{c_1} \times \right. \\
 & \left. \frac{\partial}{\partial \mathbf{y}} G_{c_1 c}(\mathbf{y} = 0, x_+; \mathbf{x}, L_+) \times W_{b_1 b}(\mathbf{0}, x_+, L_+) T_{b\bar{a}_1}^{c_1} W_{\bar{a}_1 a}^\dagger(\mathbf{0}, x_{0+}, L_+) \right\rangle \left. \right] + \\
 & + \frac{4g^2 C_R}{k_\perp^2}
 \end{aligned}$$

medium averages

local in longitudinal space [scattering centres are independent, no colour in between them], only 2-point field correlator is relevant

$$\frac{1}{N} \text{Tr} \langle W^\dagger(\mathbf{x}_\perp) W(\mathbf{y}_\perp) \rangle = \frac{1}{N} \text{Tr} \left\langle \exp \left\{ -ig \int dx_+ A_-^\dagger(x_+, \mathbf{x}_\perp) \right\} \times \right. \\ \left. \times \exp \left\{ ig \int dx_+ A_-(x_+, \mathbf{y}_\perp) \right\} \right\rangle$$

expand Wilson lines, perform colour algebra, etc.

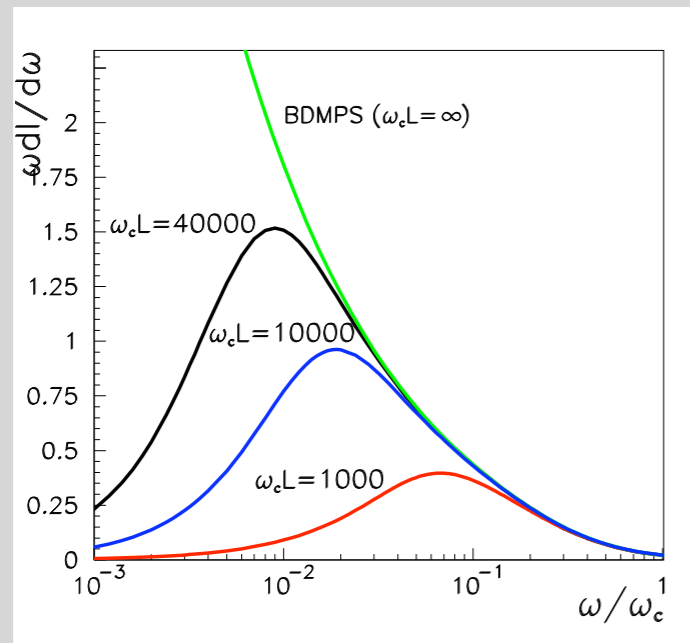
$$\frac{1}{N} \text{Tr} \langle W^\dagger(\mathbf{x}_\perp) W(\mathbf{y}_\perp) \rangle \simeq \exp \left\{ -\frac{C_F}{2} \int dx_+ n(x_+) \sigma(\mathbf{y}_\perp - \mathbf{x}_\perp) \right\}$$

$$k_+ \frac{dI}{dk_+ d^2\mathbf{k}_\perp} = \frac{\alpha_S C_R}{(2\pi)^2 k_+} 2\text{Re} \int_{x_{0+}}^{L_+} dx_+ \int d^2\mathbf{x} e^{-i\mathbf{k}_\perp \cdot \mathbf{x}} \times \\ \times \left[\frac{1}{k_+} \int_{x_+}^{L_+} d\bar{x}_+ e^{-\frac{1}{2} \int_{x_+}^{L_+} d\xi n(\xi) \sigma(\mathbf{x})} \frac{\partial}{\partial \mathbf{y}} \cdot \frac{\partial}{\partial \mathbf{x}} \mathcal{K}(\mathbf{y} = 0, x_+; \mathbf{x}, \bar{x}_+) - \right. \\ \left. - 2 \frac{\mathbf{k}_\perp}{\mathbf{k}_\perp^2} \cdot \frac{\partial}{\partial \mathbf{y}} \mathcal{K}(\mathbf{y} = 0, x_+; \mathbf{x}, L_+) \right] + \frac{\alpha_S C_R}{\pi^2} \frac{1}{\mathbf{k}_\perp^2}$$

$$\mathcal{K}(\mathbf{r}(x_+), x_+; \mathbf{r}(\bar{x}_+), \bar{x}_+) = \int \mathcal{D}\mathbf{r} \exp \left[\int_{x_+}^{\bar{x}_+} d\xi \left(i \frac{p_+}{2} \dot{\mathbf{r}}^2 - \frac{1}{2} n(\xi) \sigma(\mathbf{r}) \right) \right]$$

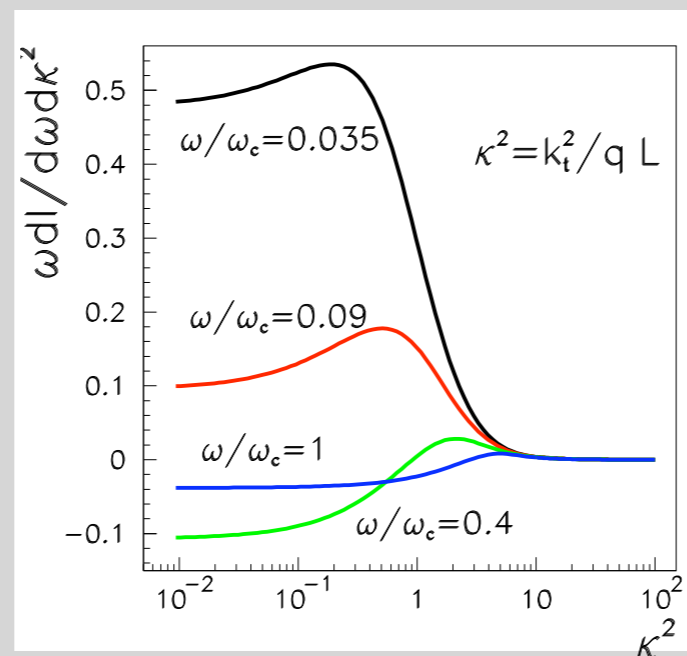
numerics

↪ energy loss of leading parton → longitudinal softening



↗ $\hat{q}L^2$

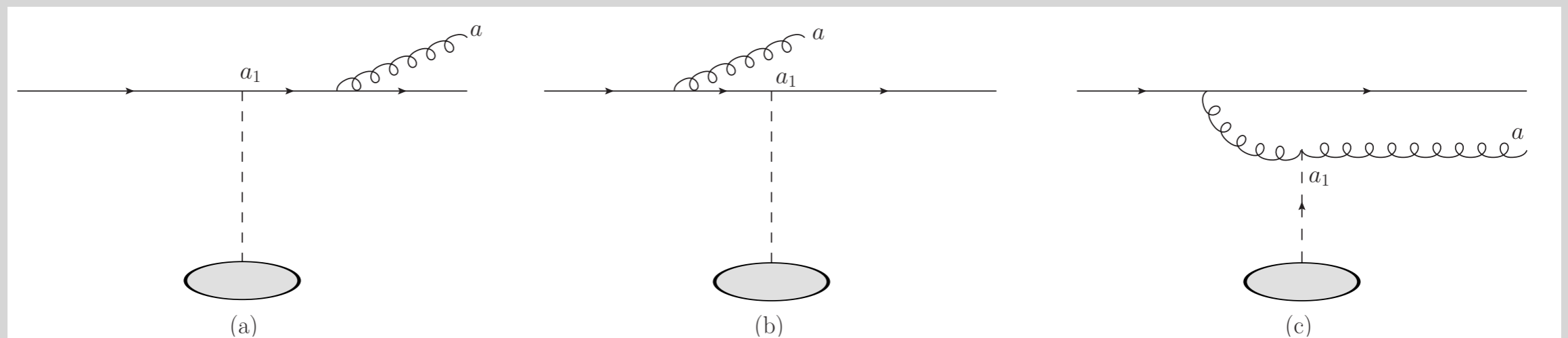
↪ k_t broadening



↗ $\hat{q}L$

opacity expansions

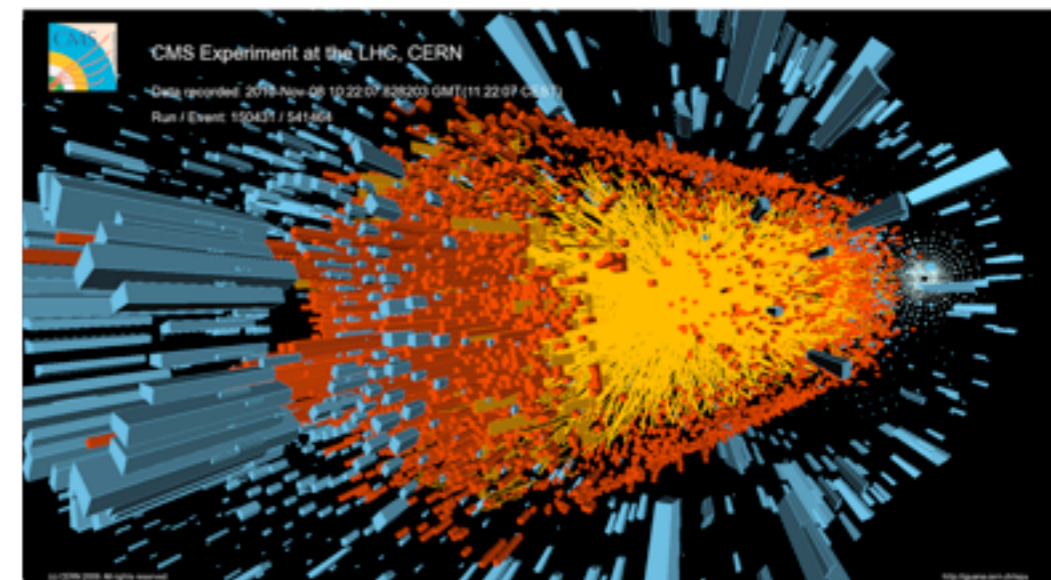
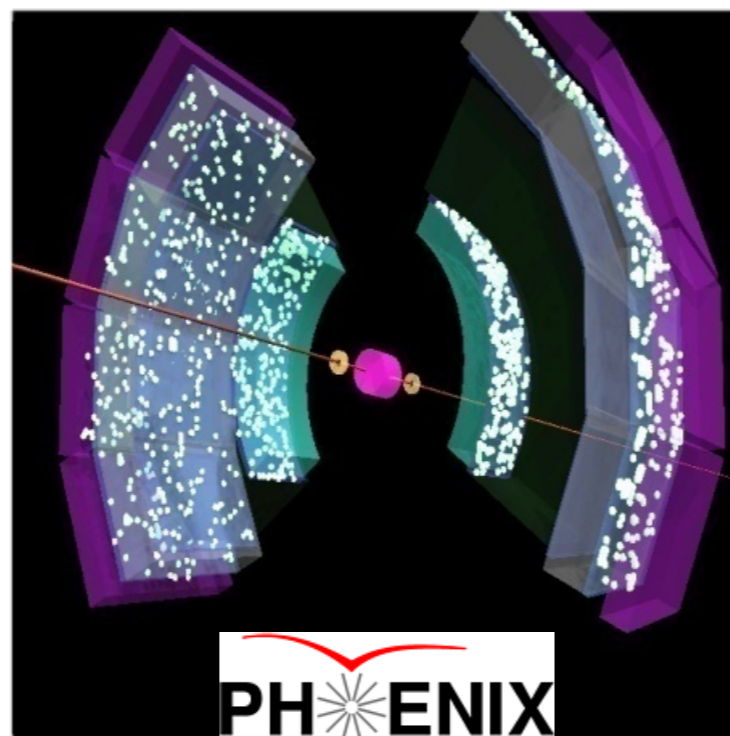
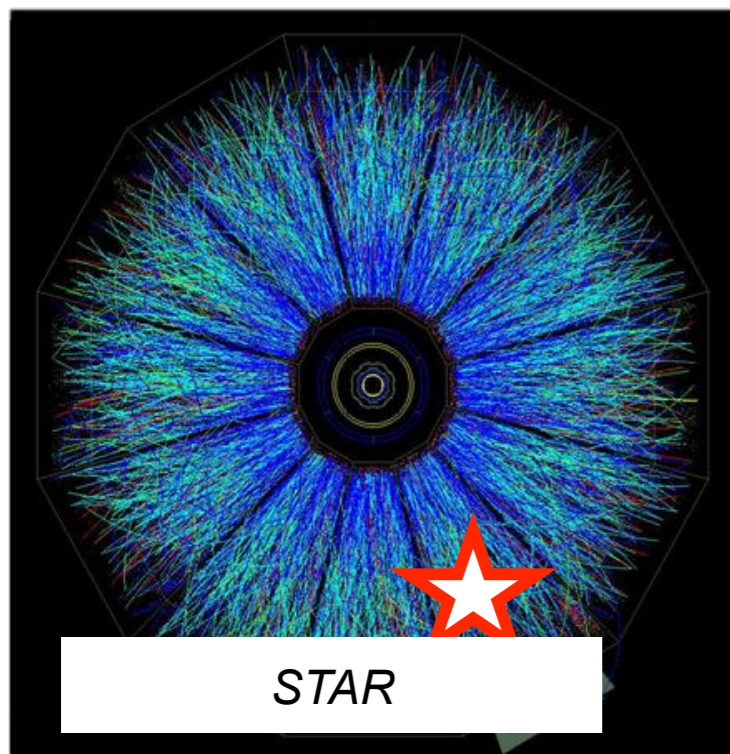
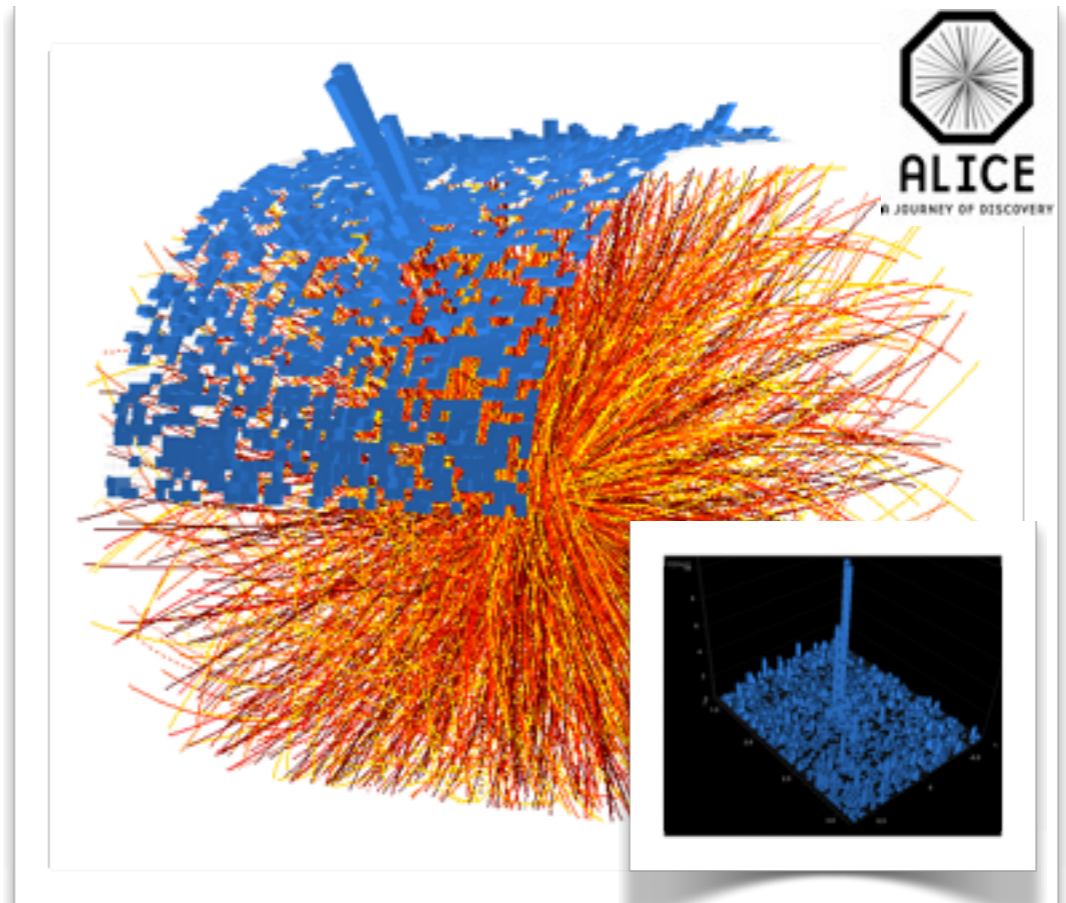
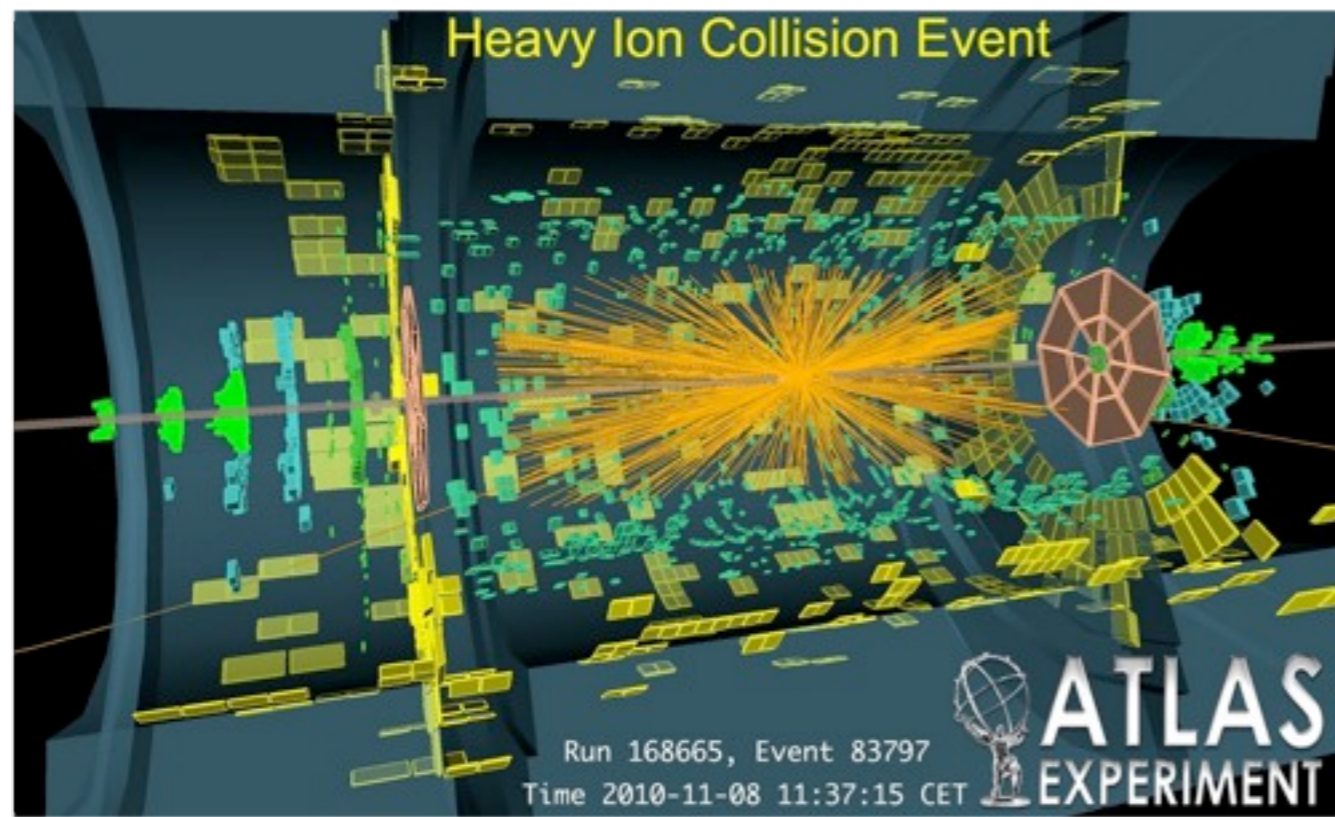
- it is often useful to perform calculation in the opacity expansion [GLV]
 - ↪ this is an expansion on [medium extent/elastic mean free path]
 - ↪ in practical terms it corresponds to allowing for a finite total number of medium interactions
 - ↪ $N=1$ opacity is then



- ↪ much simpler framework
- ↪ captures essential features

a whole lot left to say...

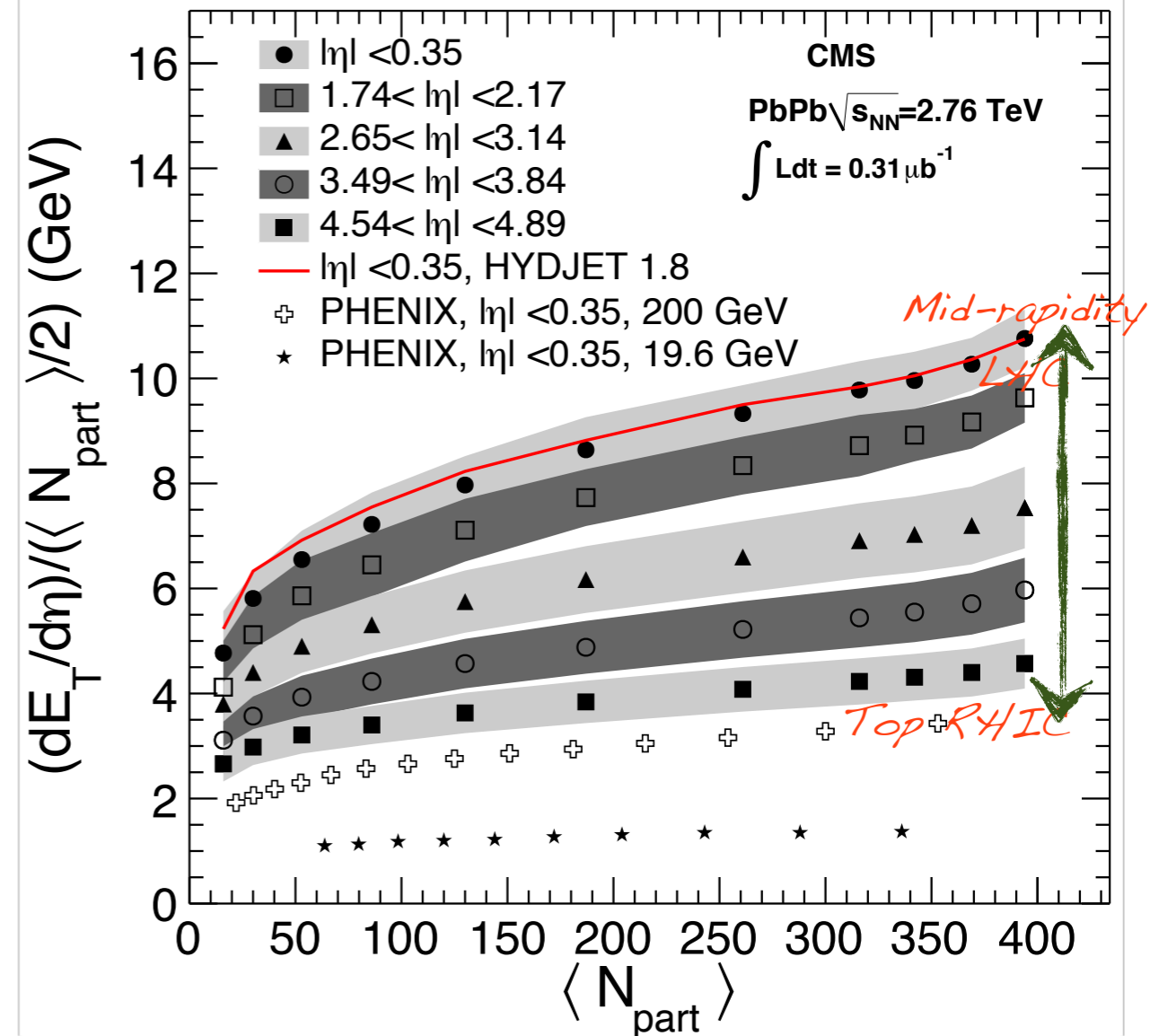
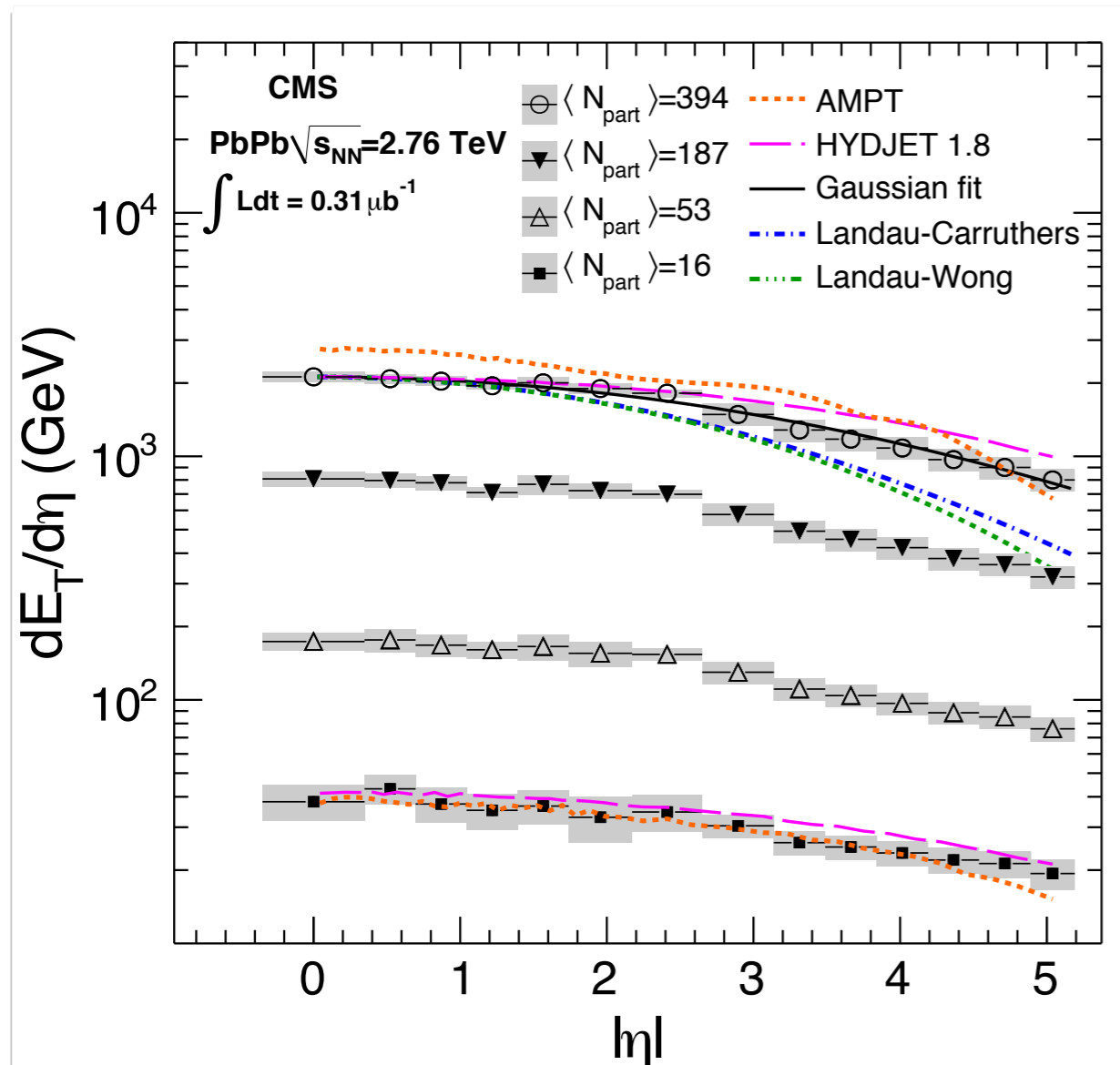
Heavy-ion collisions



Energy density: RHIC to LHC

LHC > 2.5 x RHIC

... within a volume (per nucleon)

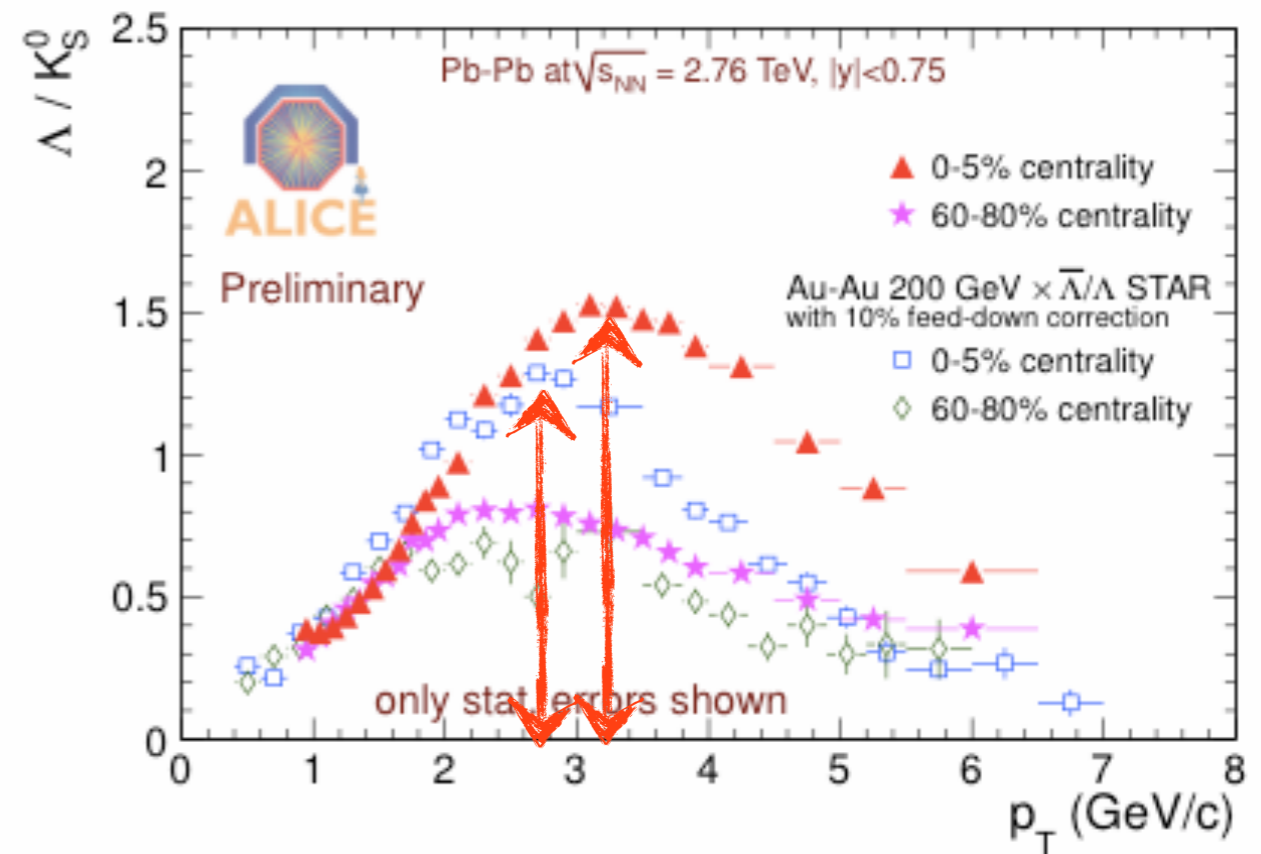
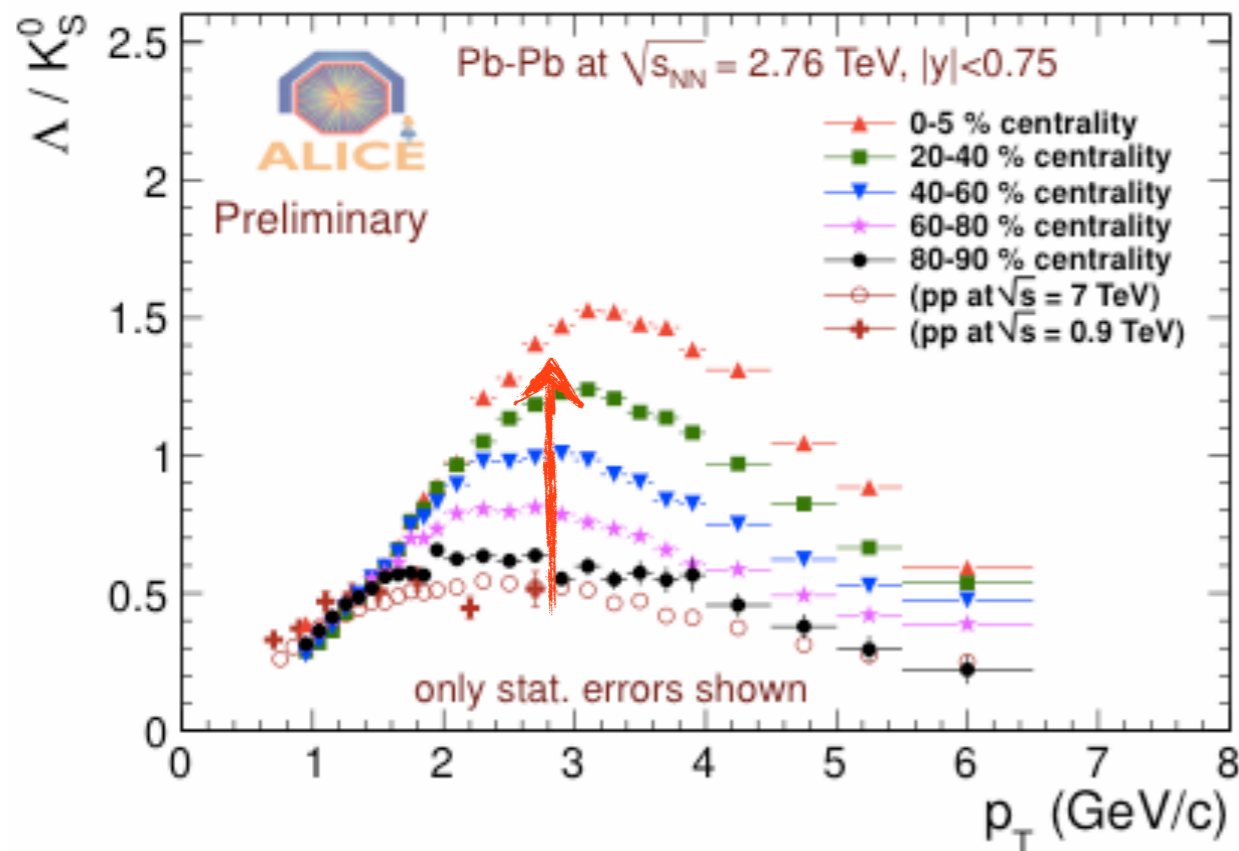


Hadron production in heavy-ion collisions

A slight digression...

RHIC vs LHC

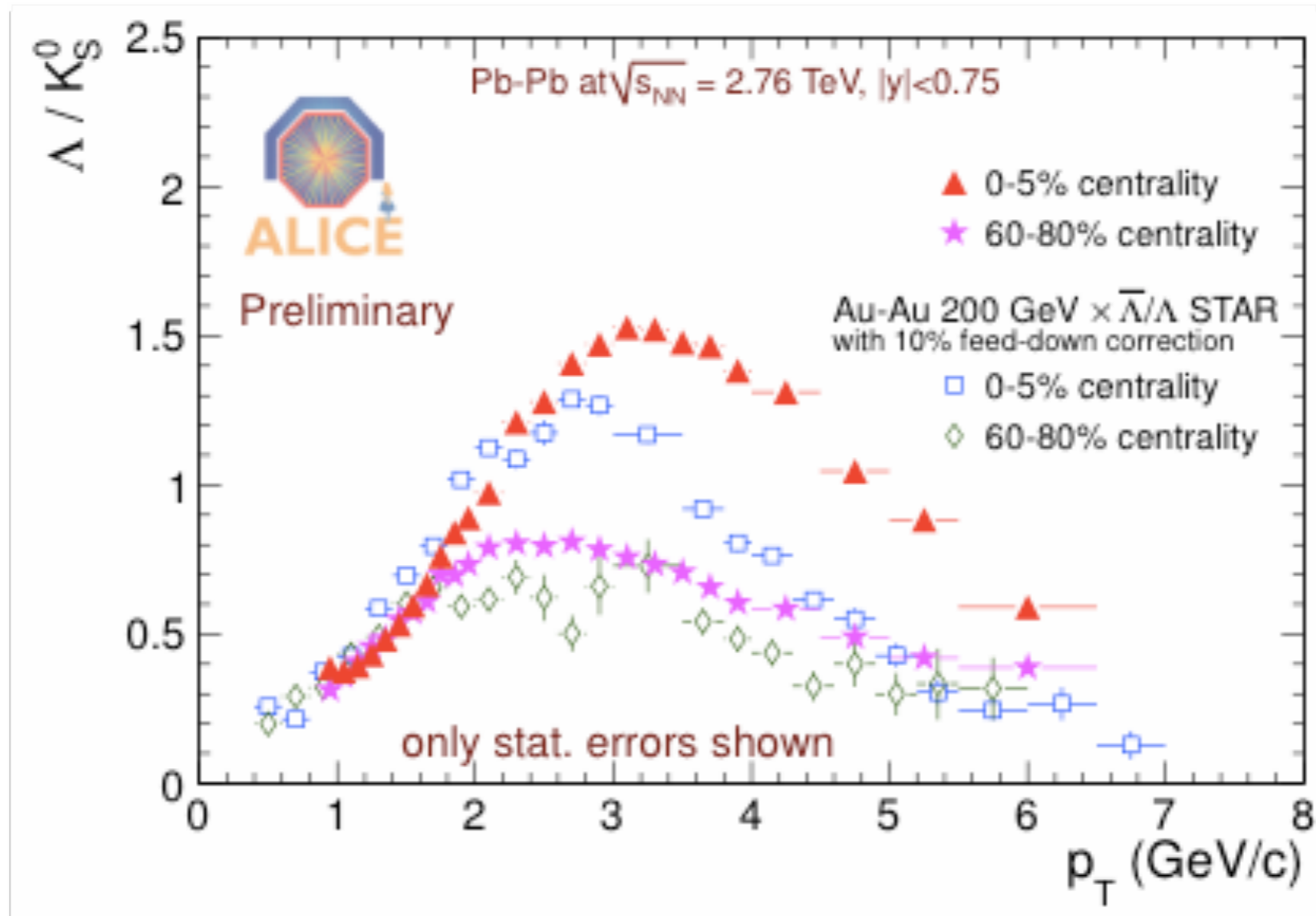
(LHC: higher mean p_T - more flow)



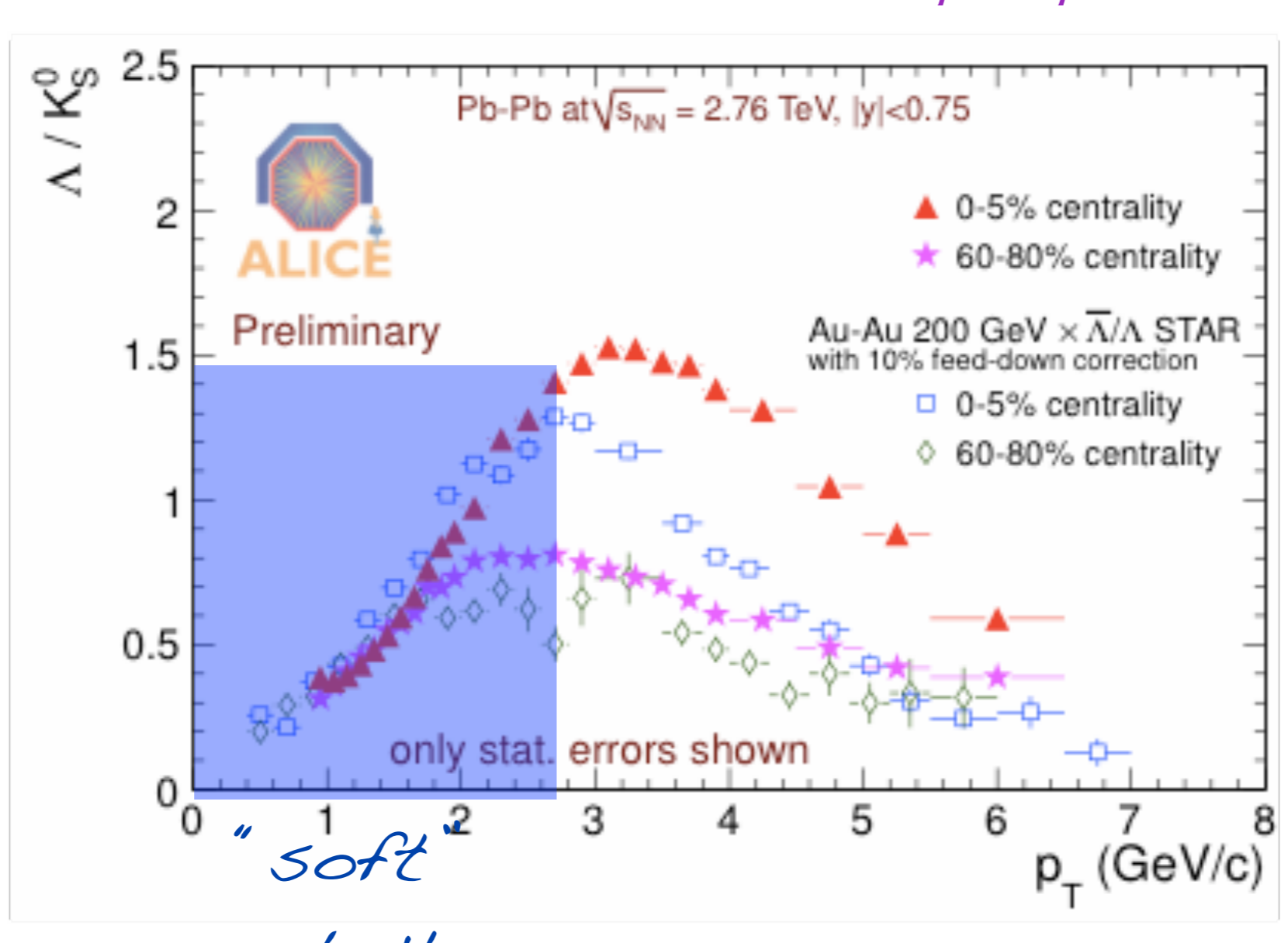
Much more baryons than mesons in central collisions as compared to proton-proton (coalescence/recombination? bulk+jet?)

*LHC similar to RHIC
Maximum at slightly higher- p_T*

bulk, jets, medium and p_T :
arbitrary regions
and INFORMAL Language

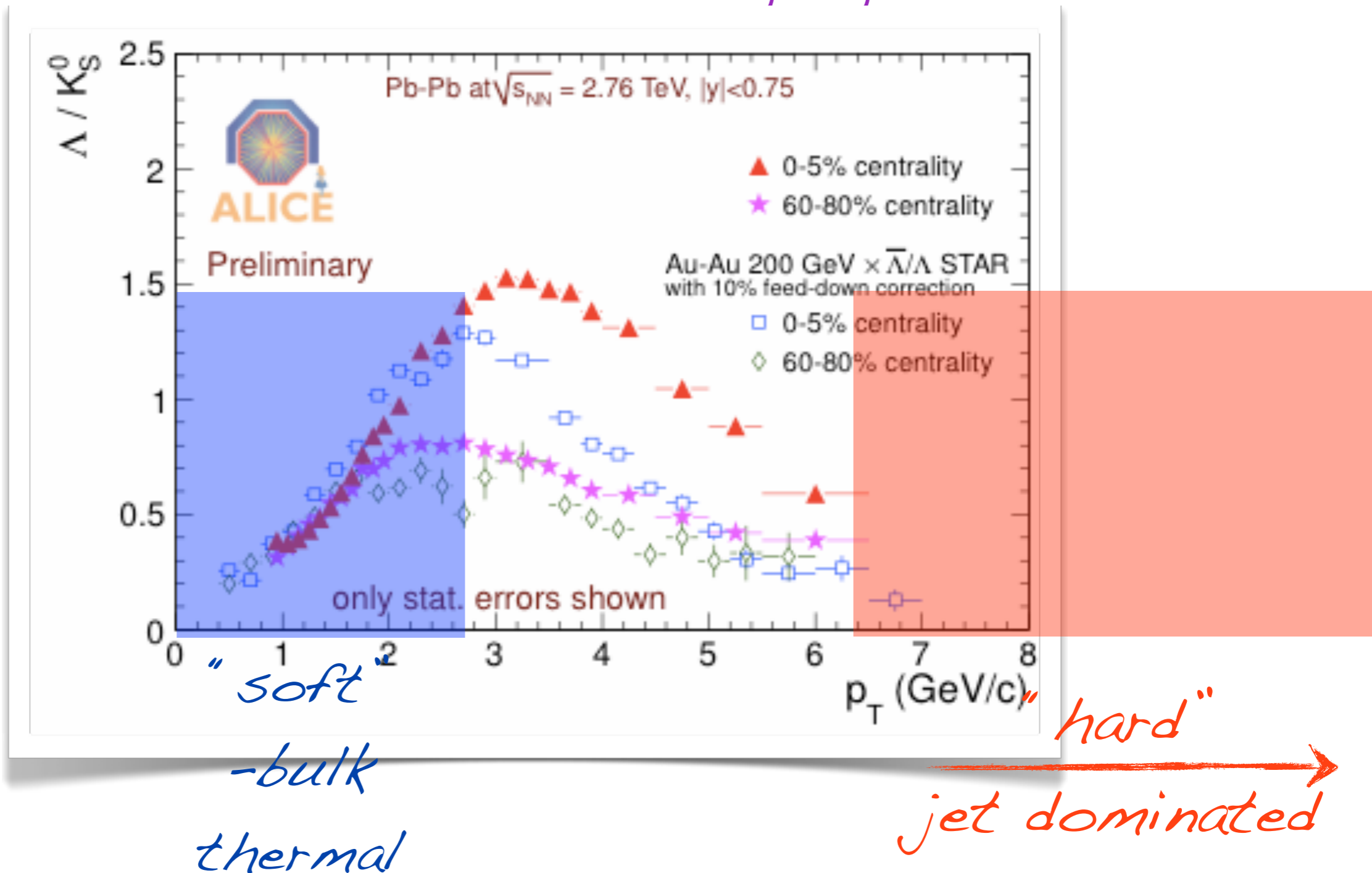


bulk, jets, medium and p_T :
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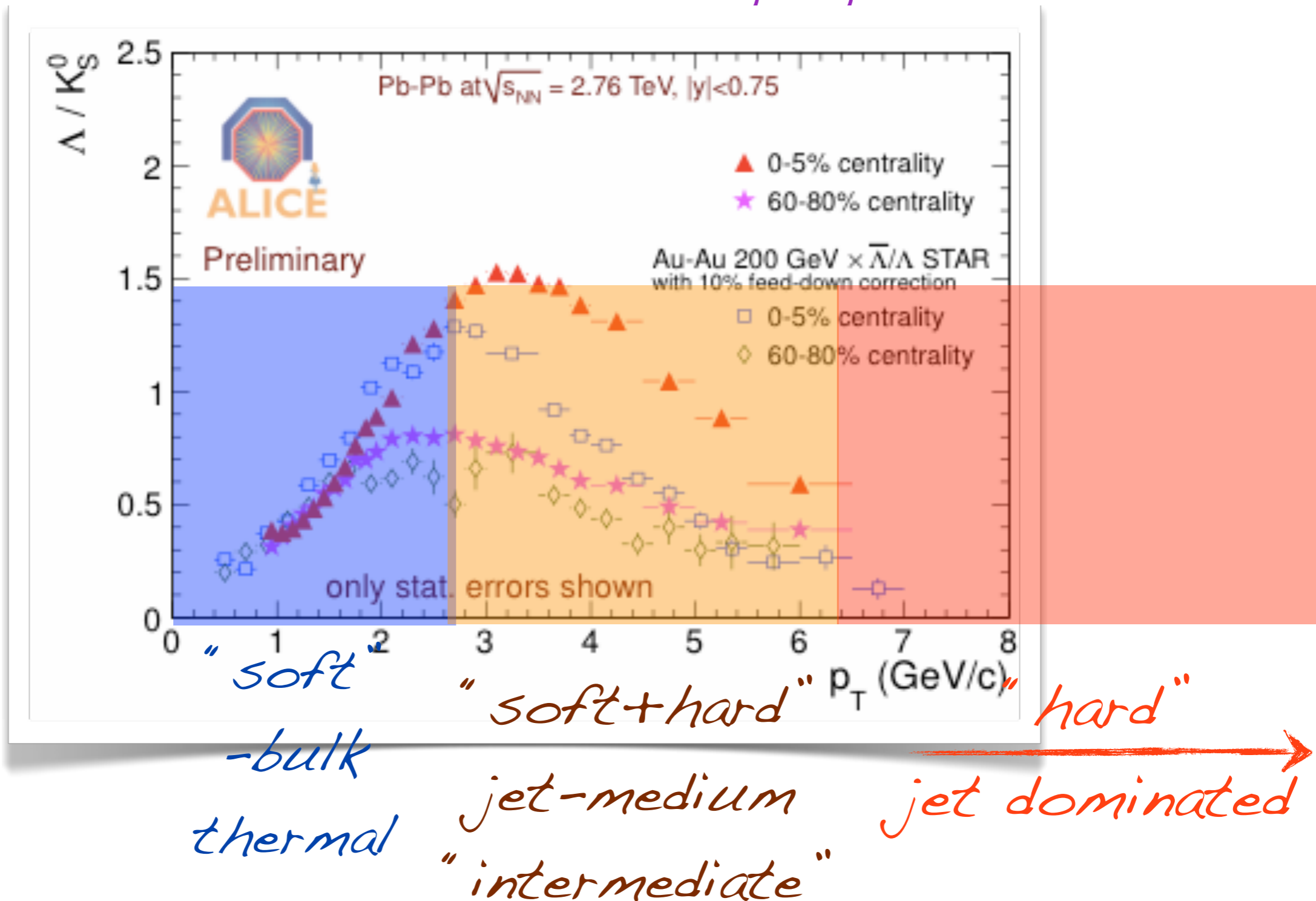


"soft"
-bulk
thermal

bulk, jets, medium and p_T :
arbitrary regions
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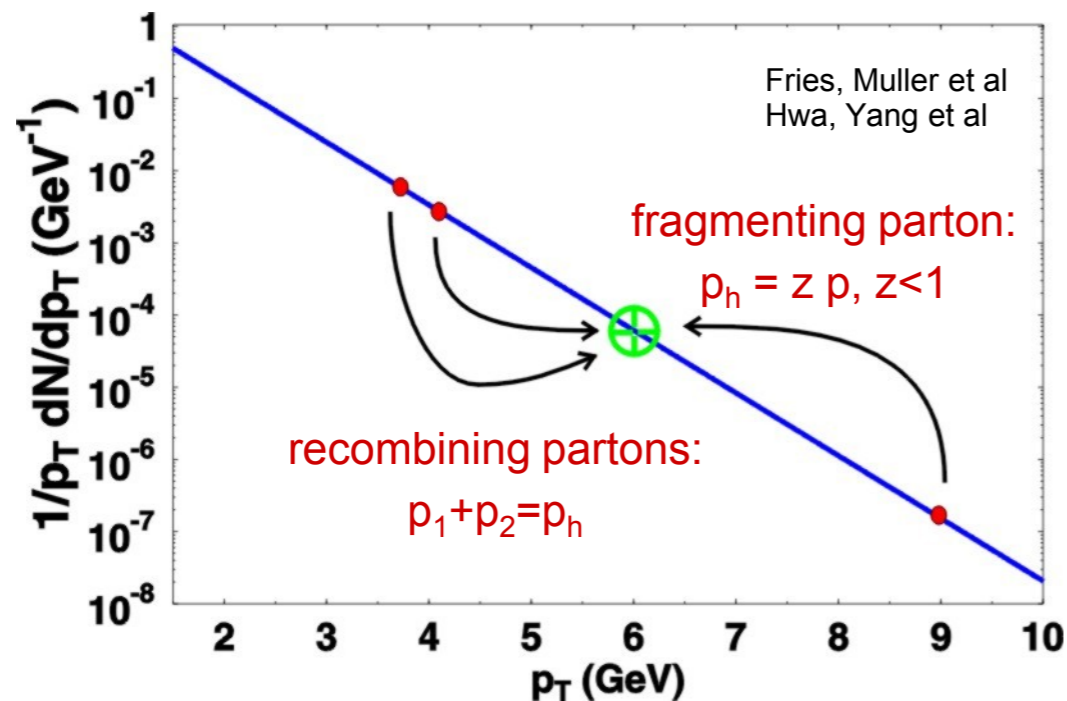


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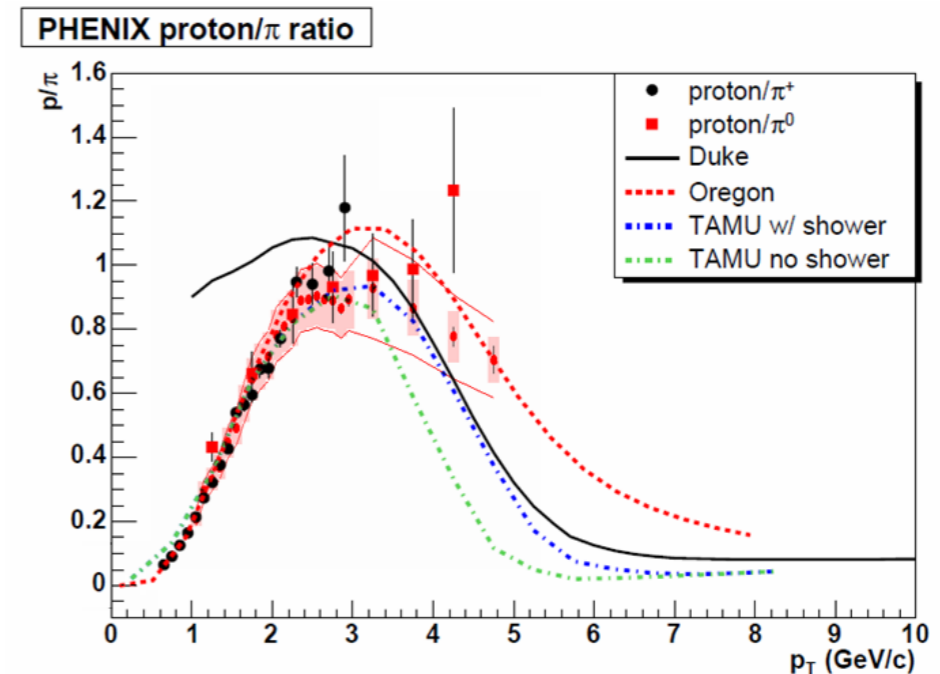


Hadronization of bulk+hard

- parton coalescence

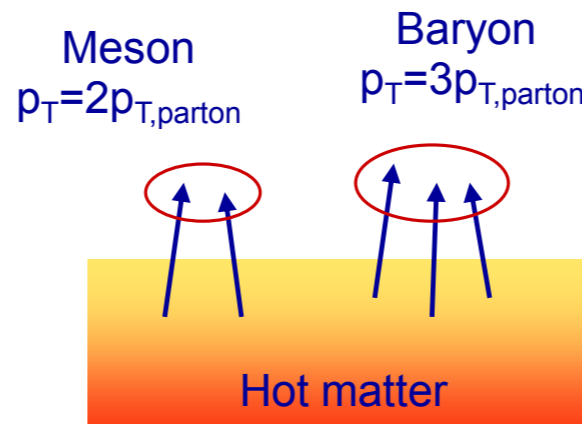


Recombination of thermal ('bulk') partons produces baryons at larger p_T

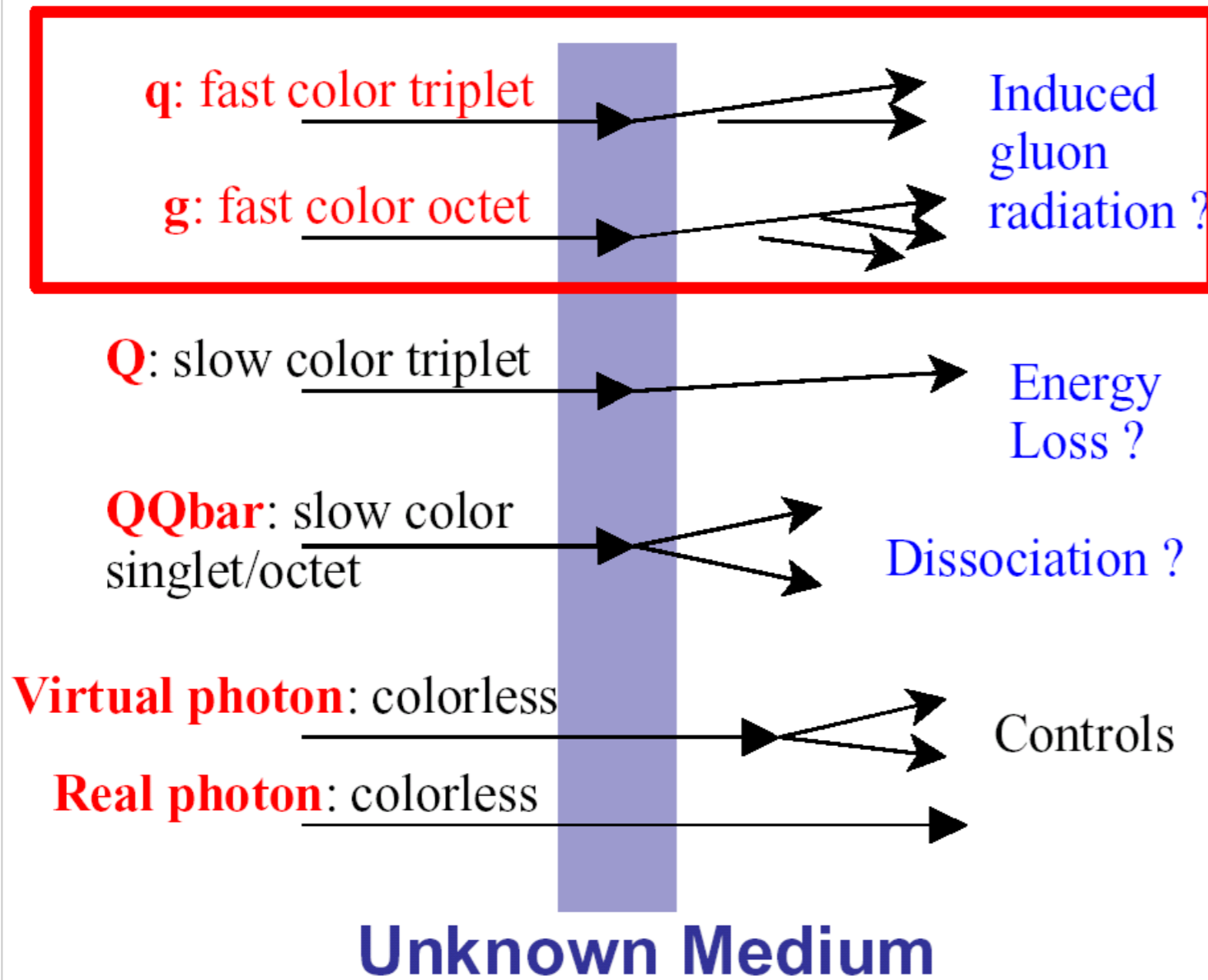


Recombination enhances baryon/meson ratio

Note also: v_2 scaling



The probes



*jet suppression
(quenching)*

charm/bottom dynamics

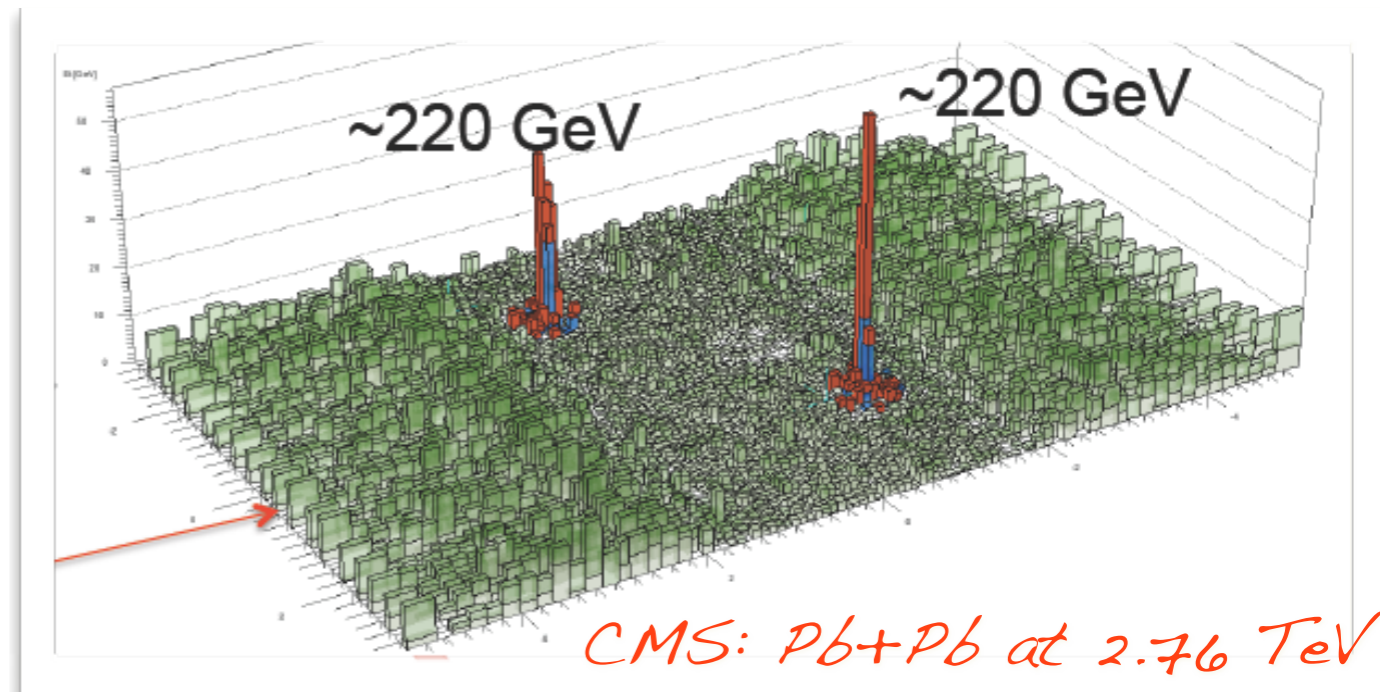
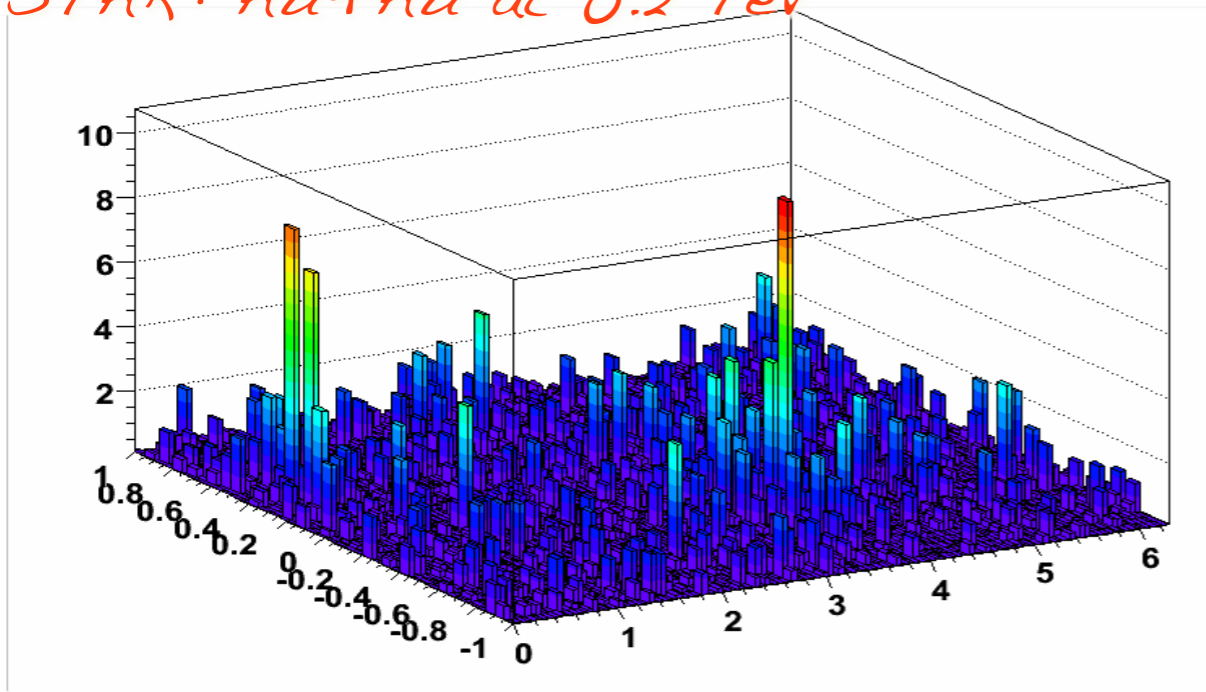
J/ψ & Υ

color-less particles

Jets in heavy-ion collisions

RHIC & LHC

STAR: Au+Au at 0.2 TeV



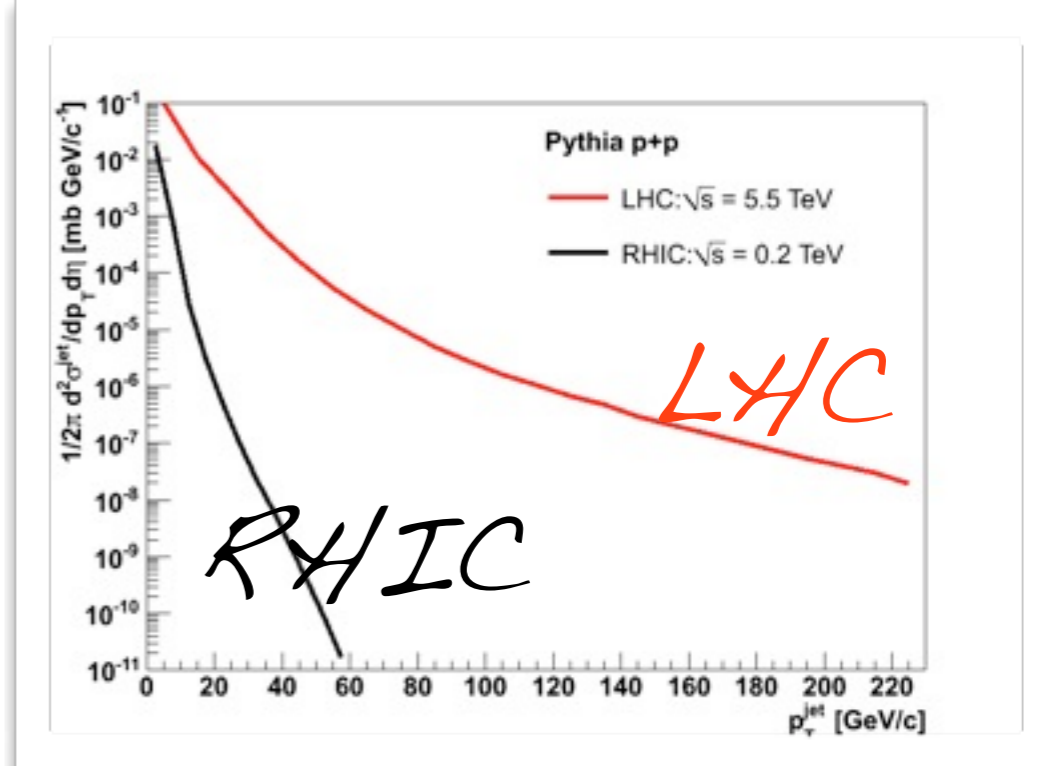
LHC + RHIC: QCD evolution of jet quenching?

Vary energy of the jet:

LHC: Vary the scale with which QGP is probed (a la DIS)

Compare and contrast RHIC and LHC

Jets in heavy-ion collisions RHIC & LHC



Jets in heavy-ion environment - few experimental notes:

- large combinatorial backgrounds (especially at RHIC)
- energy within an event varies from point to point ("fluctuations")
- a plus for LHC is larger kinematic reach - abundance of high-energy jets (higher- p_T measurements less affected by backgrounds)
 - => various approaches among experiments for background suppression AND/OR jet energy-resolution corrections
- is there an optimal jet definition for heavy-ion collisions (?)
 - => use multiple jet algorithms (?); sub-jets (?); filtering (?)
- jets are reported on the particle (generator) level - hadronization corrections (to the "parton" jet) in HI collisions impossible

Jets in heavy-ion collisions RHIC & LHC

LHC

RHIC

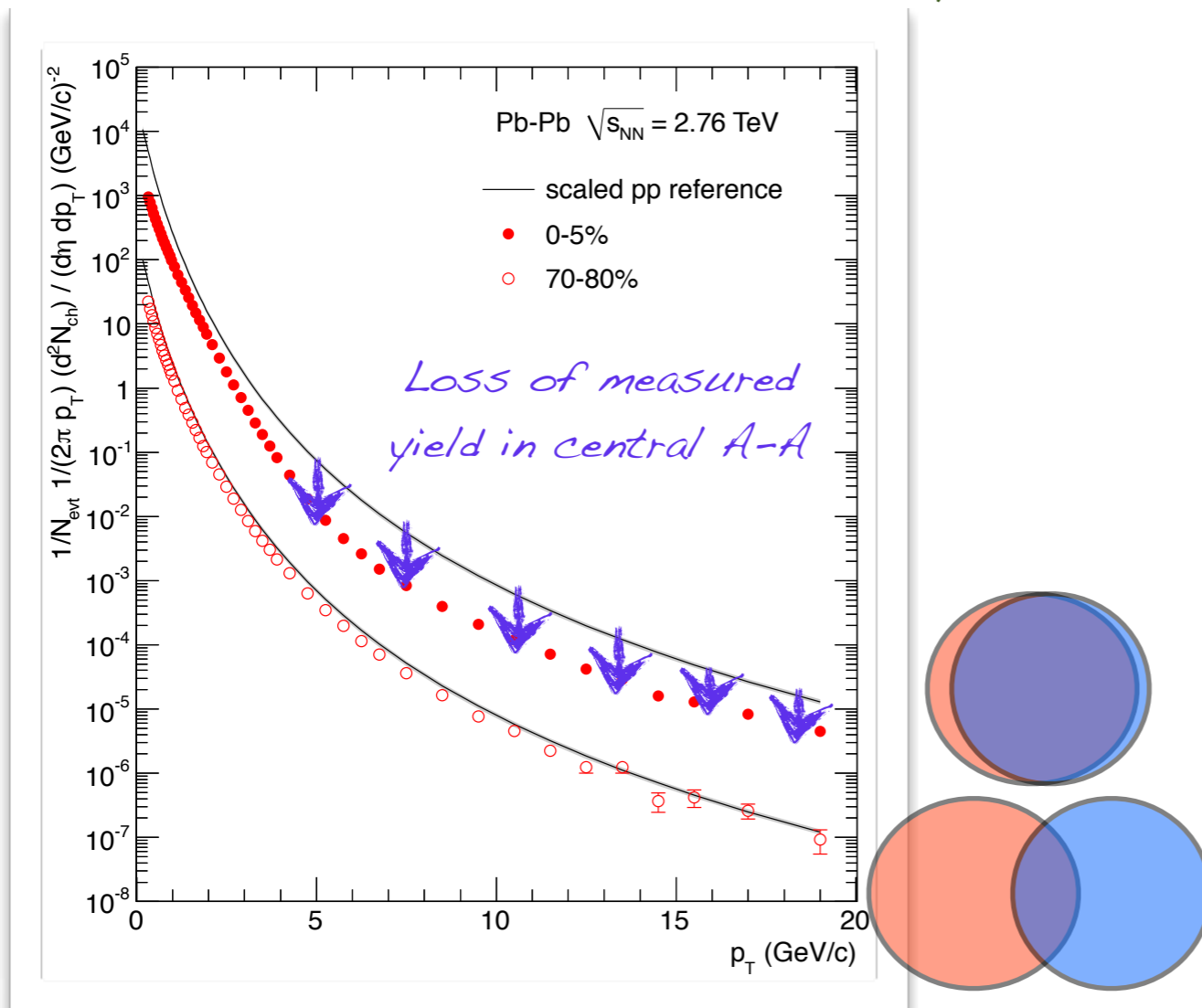
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"Easier" (than full jet reconstruction) exercise: Jet-quenching via leading hadrons

Inclusive hadron production

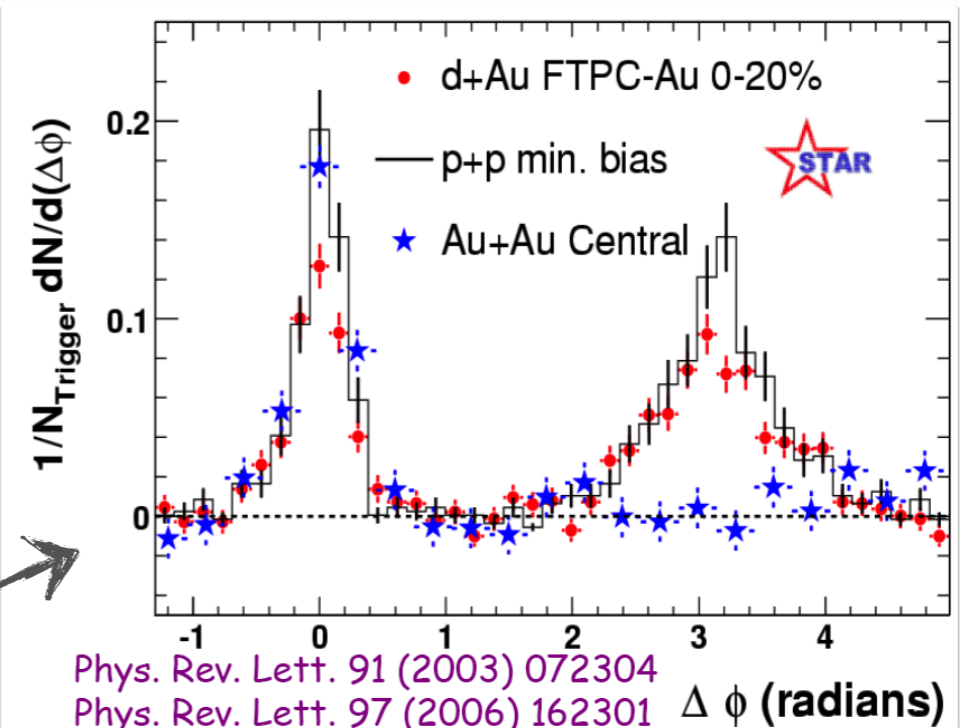
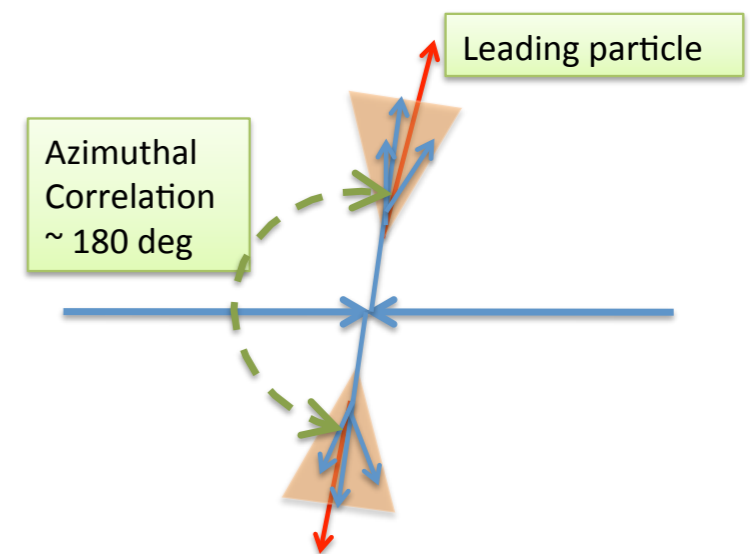
Measured as a function of collision centrality



Note on correlations: interesting tool to study the "intermediate"- p_T region - jets vs flow and recombination

Di-hadron correlations

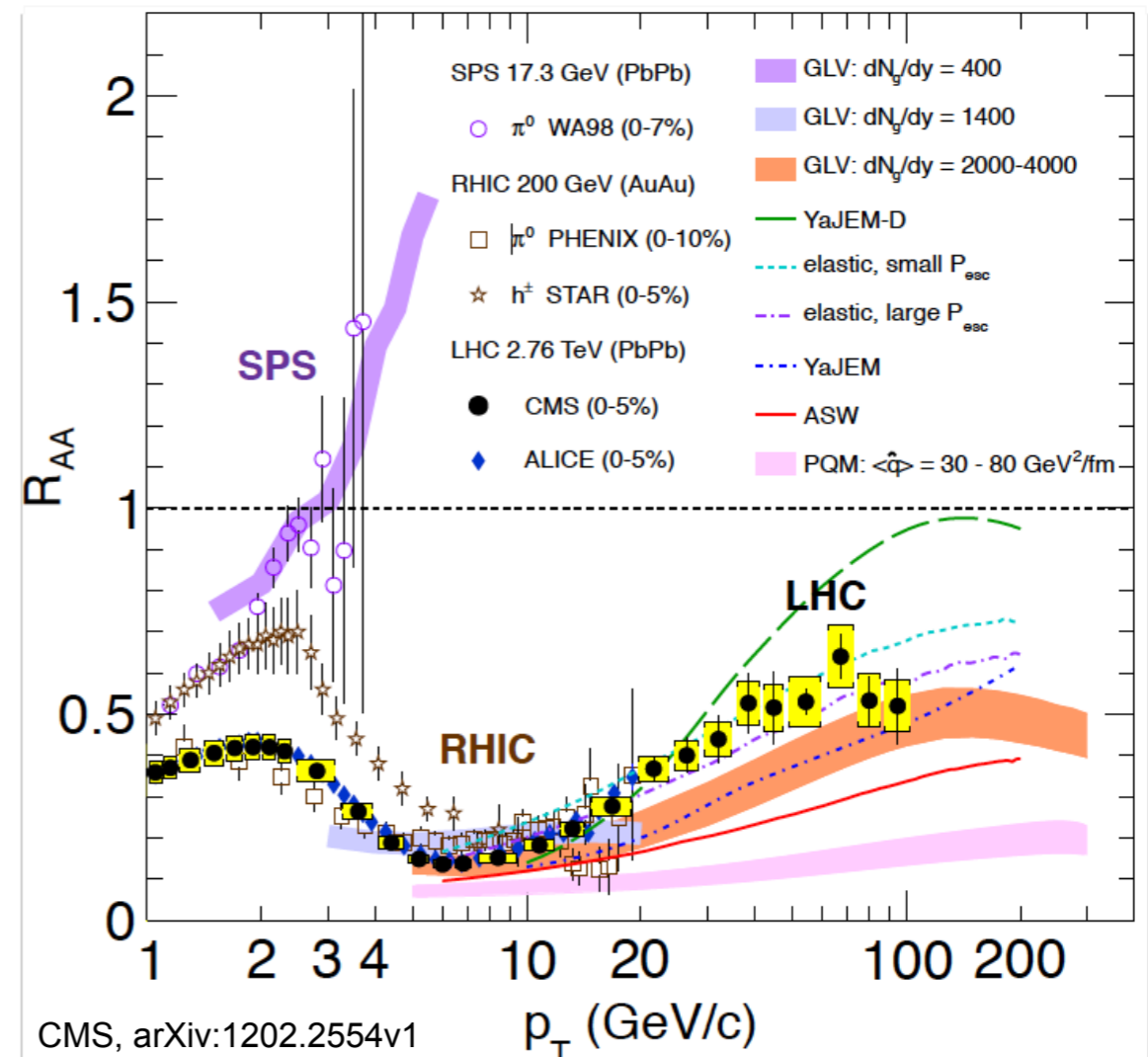
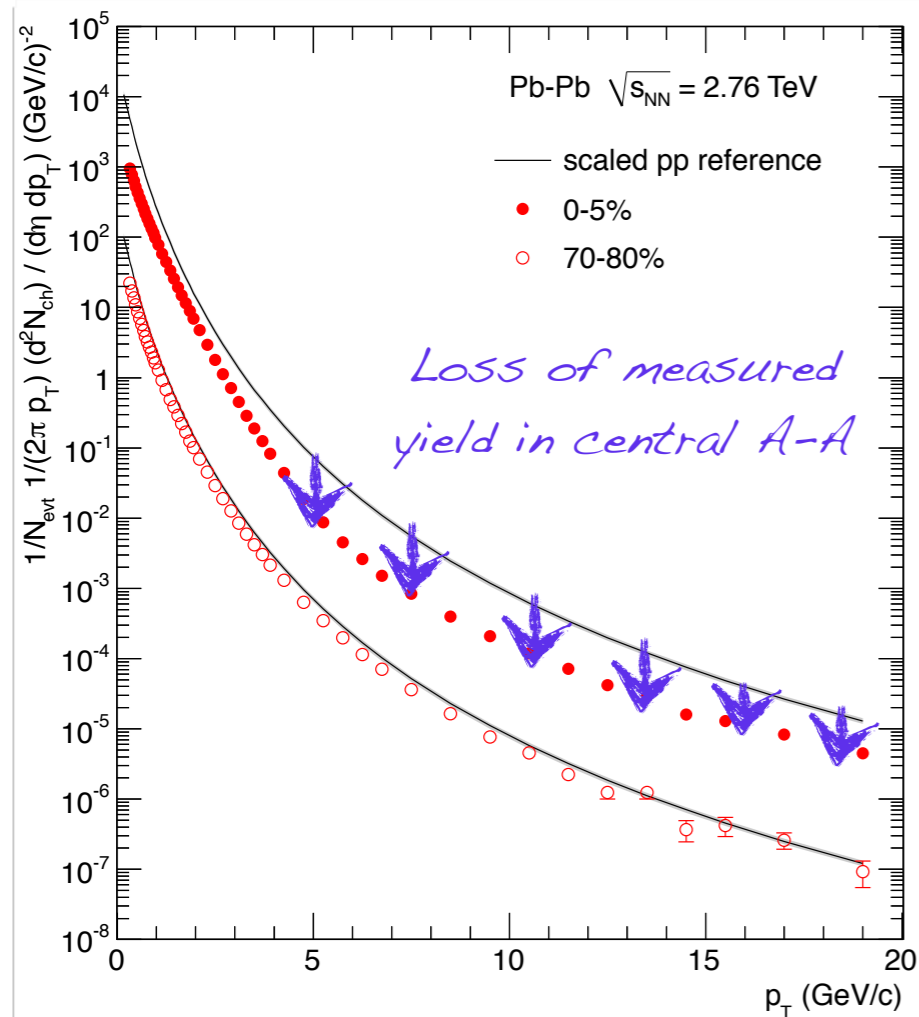
Rates of recoil ("away-side") hadrons suppressed



Hadron suppression

Nuclear modification factor:

$$R_{AA} = \frac{\#(\text{particles observed in AA collision per } N\text{-}N \text{ (binary) collision})}{\#(\text{particles observed per } p\text{-}p \text{ collision})}$$



"No effect" case is for $R_{AA} = 1$ at high p_T where hard processes dominate

R_{AA} for different particle type

Is parton energy loss different
for gluons, light-quarks and heavy-quarks?

Expectation: $\Delta E_g > \Delta E_{\text{light-}q} > \Delta E_{\text{heavy-}q}$

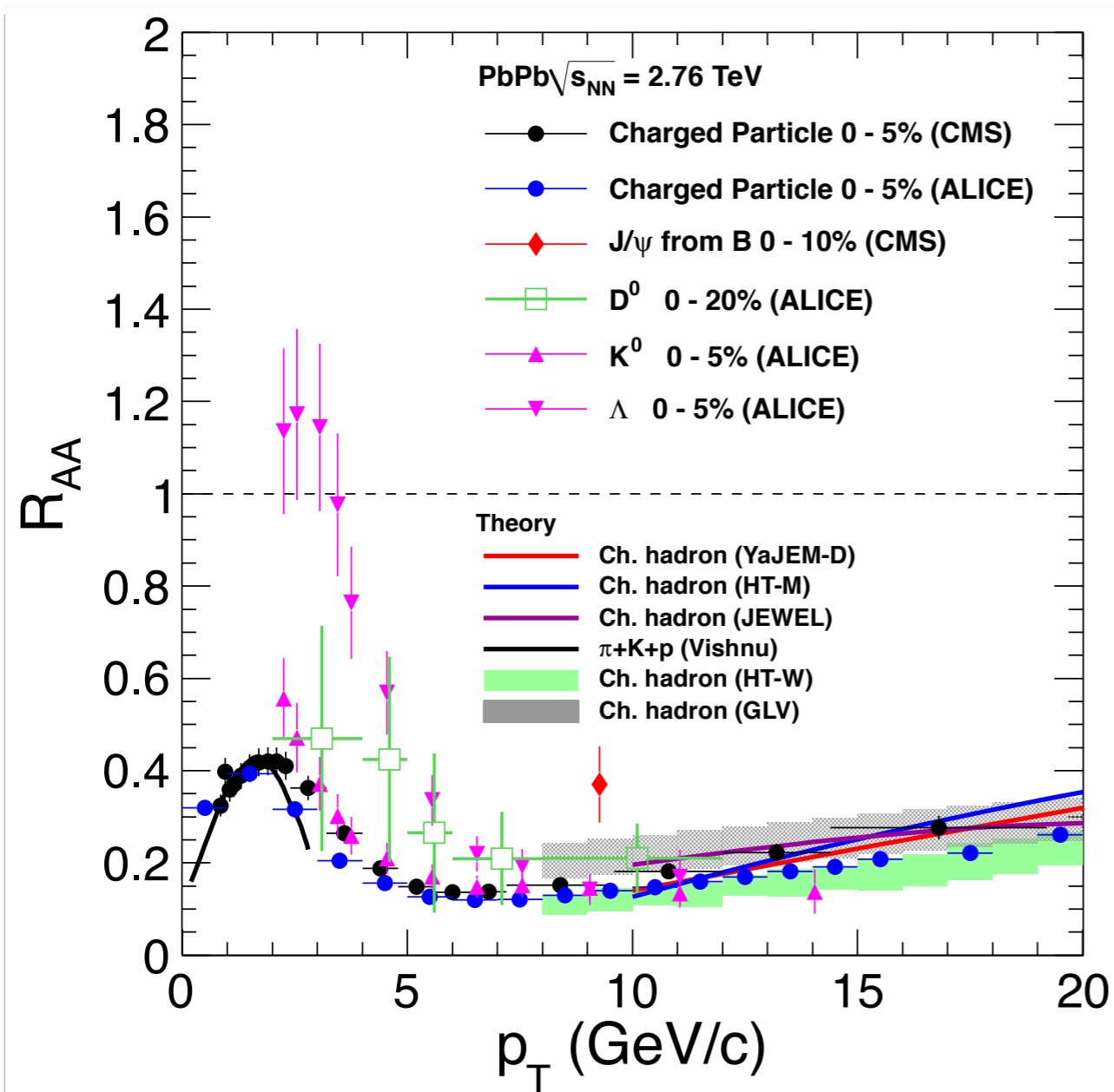
Casimir (color factor)
- gluons "glue" better to
the medium than quarks

"Dead-cone" effect:
mass of the parent quark
 \Rightarrow radiation for angles $\theta < m/E$
is suppressed

$\Rightarrow R_{AA}^{\text{pions}} < R_{AA}^{\text{D-mesons}} < R_{AA}^{\text{B-mesons}}$

RAA for different particle type

Discussion based on LHC results



Similar suppression for heavier- q (strange, charm) and gluons (large elastic e-loss; less dep. on mass?; color factor? - small effect?)

J/ ψ from B-decays - dead cone effect?

Lambda vs K⁰ R_{AA} below 7 GeV - manifestation of flow (?)

Rise towards higher p_T 's:

1) Harder partonic spectrum (as compared to RHIC)

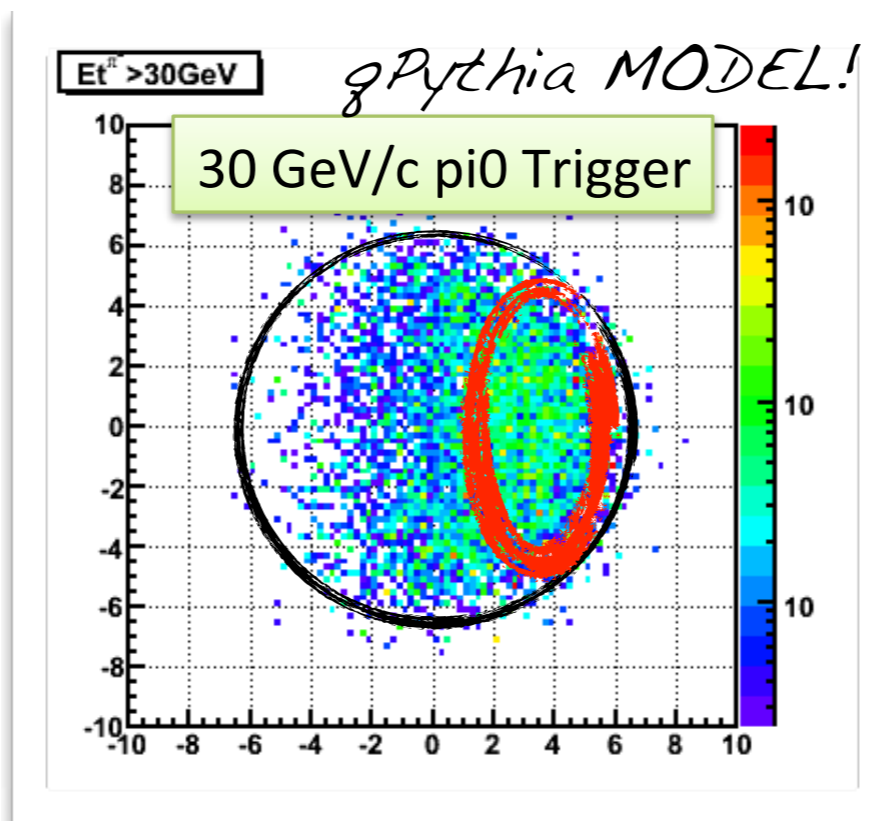
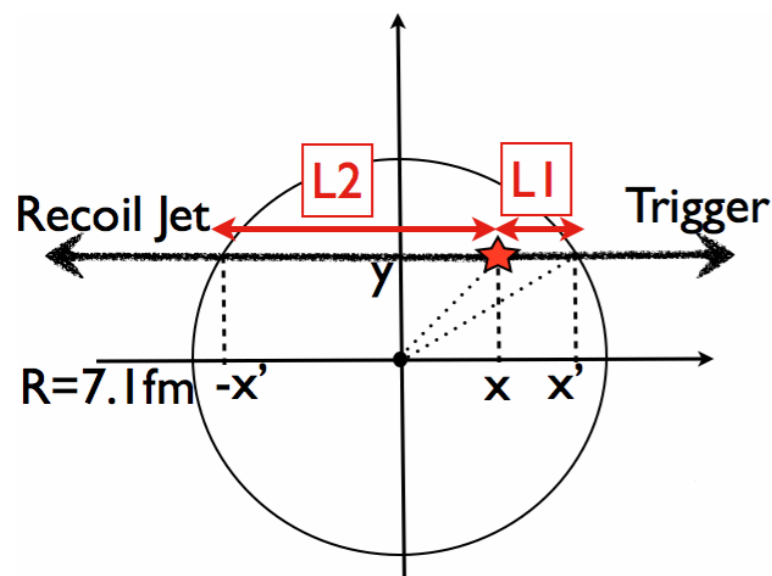
2) Weak dependence of [pQCD] e-loss on parton energy

Not shown but measured:

Photons and Z's not suppressed \rightarrow quenching is a final state effect

So, why bother with full jet reconstruction in heavy-ion collisions?

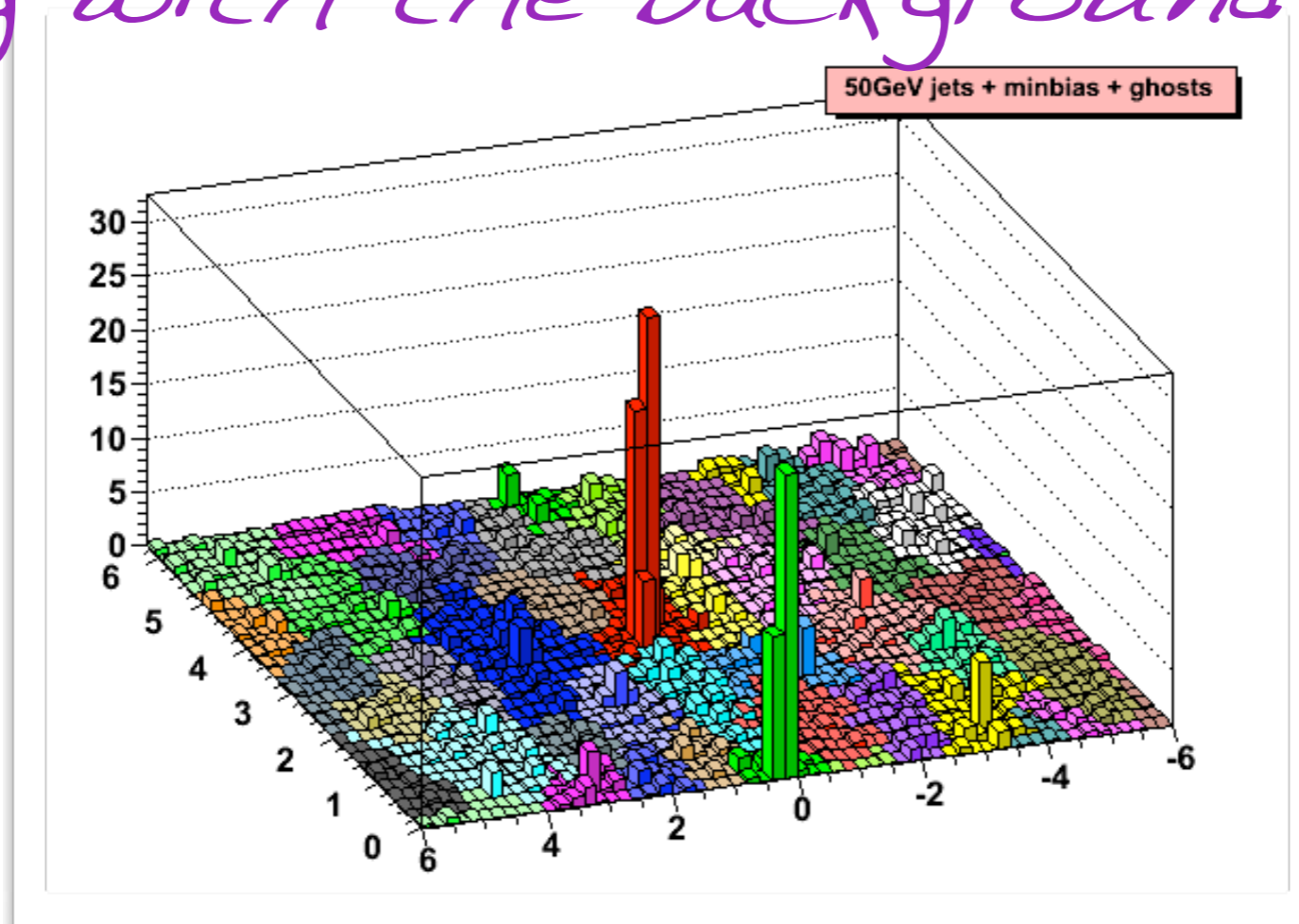
R_{AA} and correlations of leading hadrons provide constraints on density of the medium (\hat{q}), however do not tell us about the *parton* energy loss and its dynamics; leading hadrons are biased towards jets that interact little or not at all with the medium



So called **surface bias**:
requesting a high- p_T
particle selects a
population of jets close to
surface of the medium -
these jets interact only
little (or not at all) with
the medium

=> full jet reconstruction premise: integrate over the hadronic degrees of freedom; better access to the parton energy scale; dynamics of the jet quenching (?); other promising observables: gamma-jet correlations

H/I jet finding: dealing with the background energy



A single event: all particles clustered ("assigned") to a jet

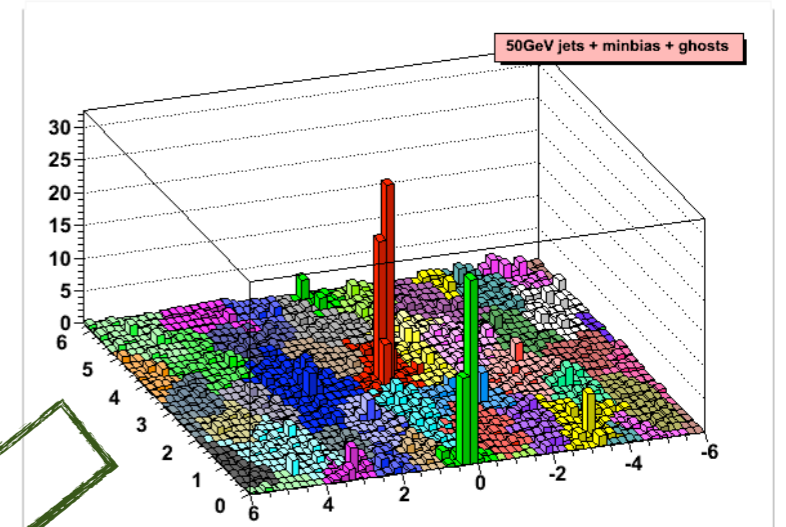
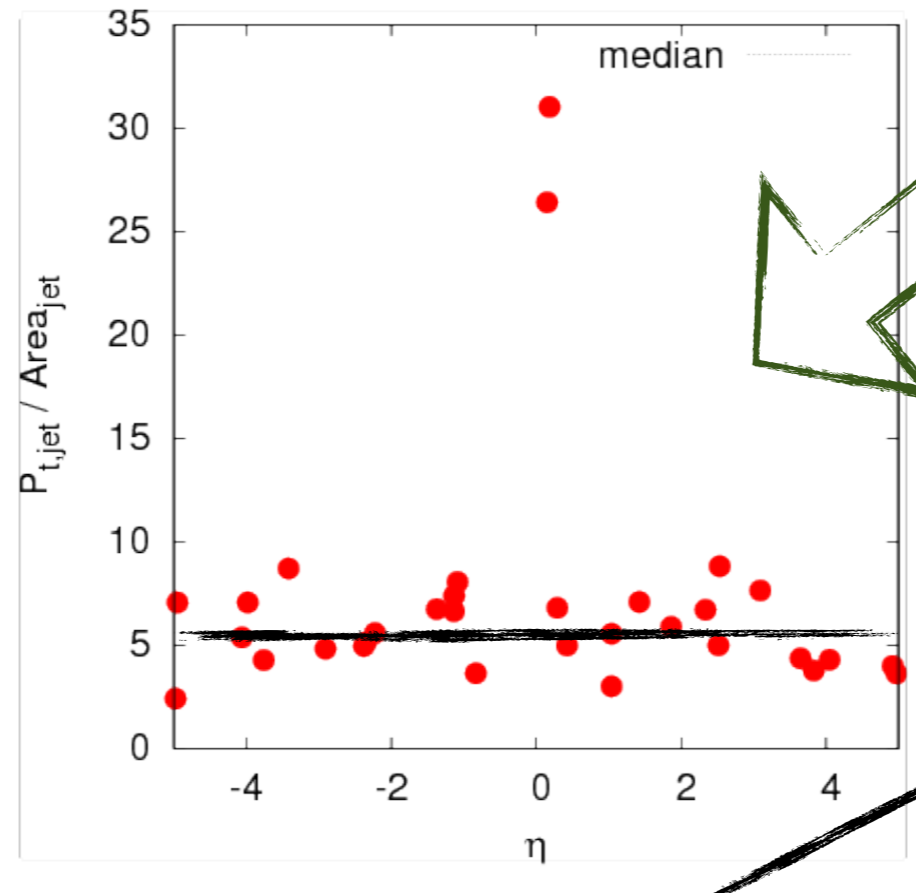
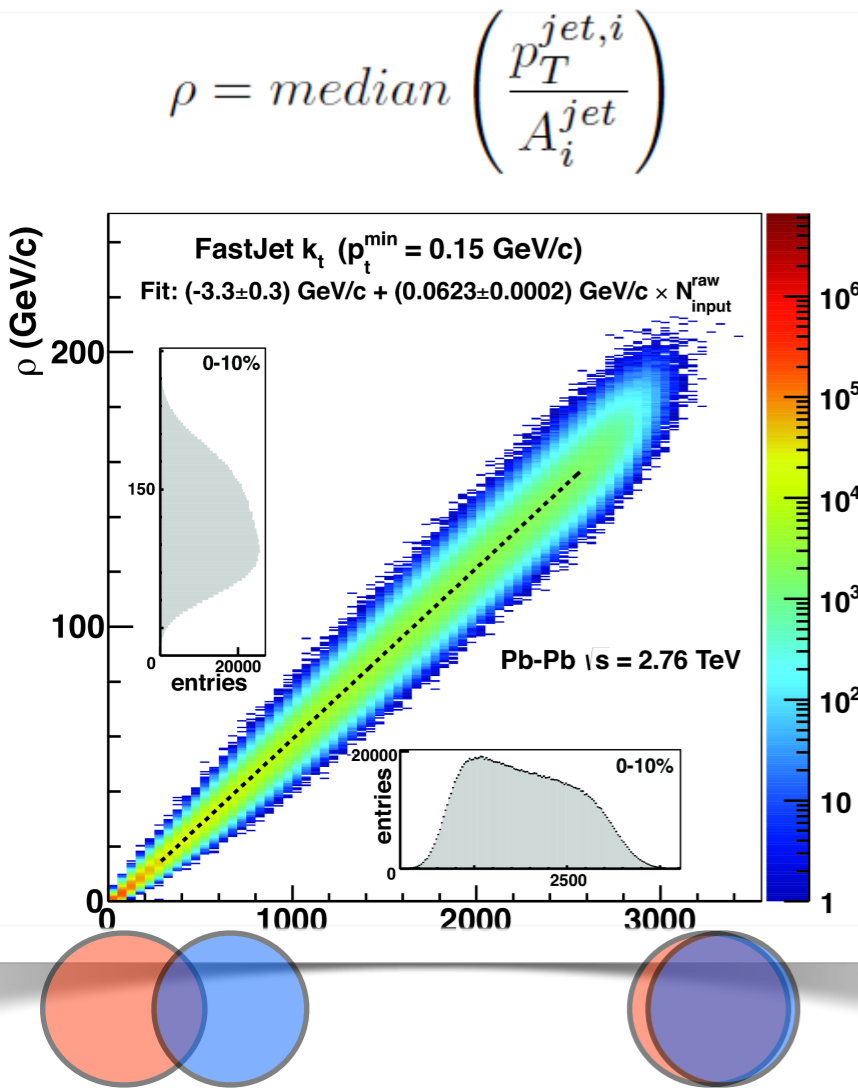
Many of these objects are simply background

Energy of the signal jets overestimated due to background energy

*=> several possibilities to subtract the average background and/or
suppress the background particles [and background jets]*

HI jet finding: treatment of the background

Method 1



average background energy density

$$p_T = p_T^{\text{raw}} - \rho \times \text{Area}_{\text{jet}}$$

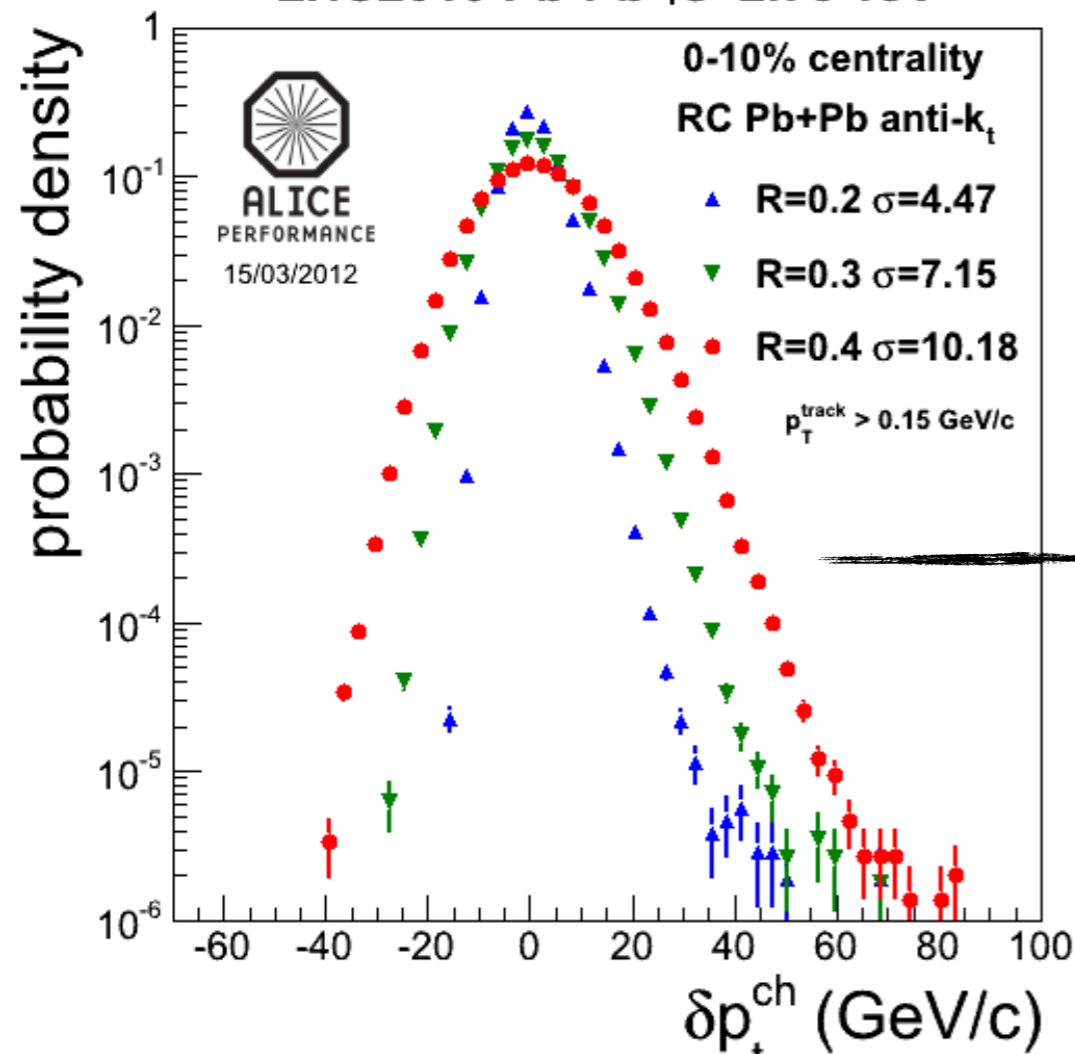
Must correct for remaining residual energy resolution

- magnitude of the correction is related to the background fluctuations*
- jet Area : small R (area) - smaller correction*

Jet reconstruction in HI collisions:

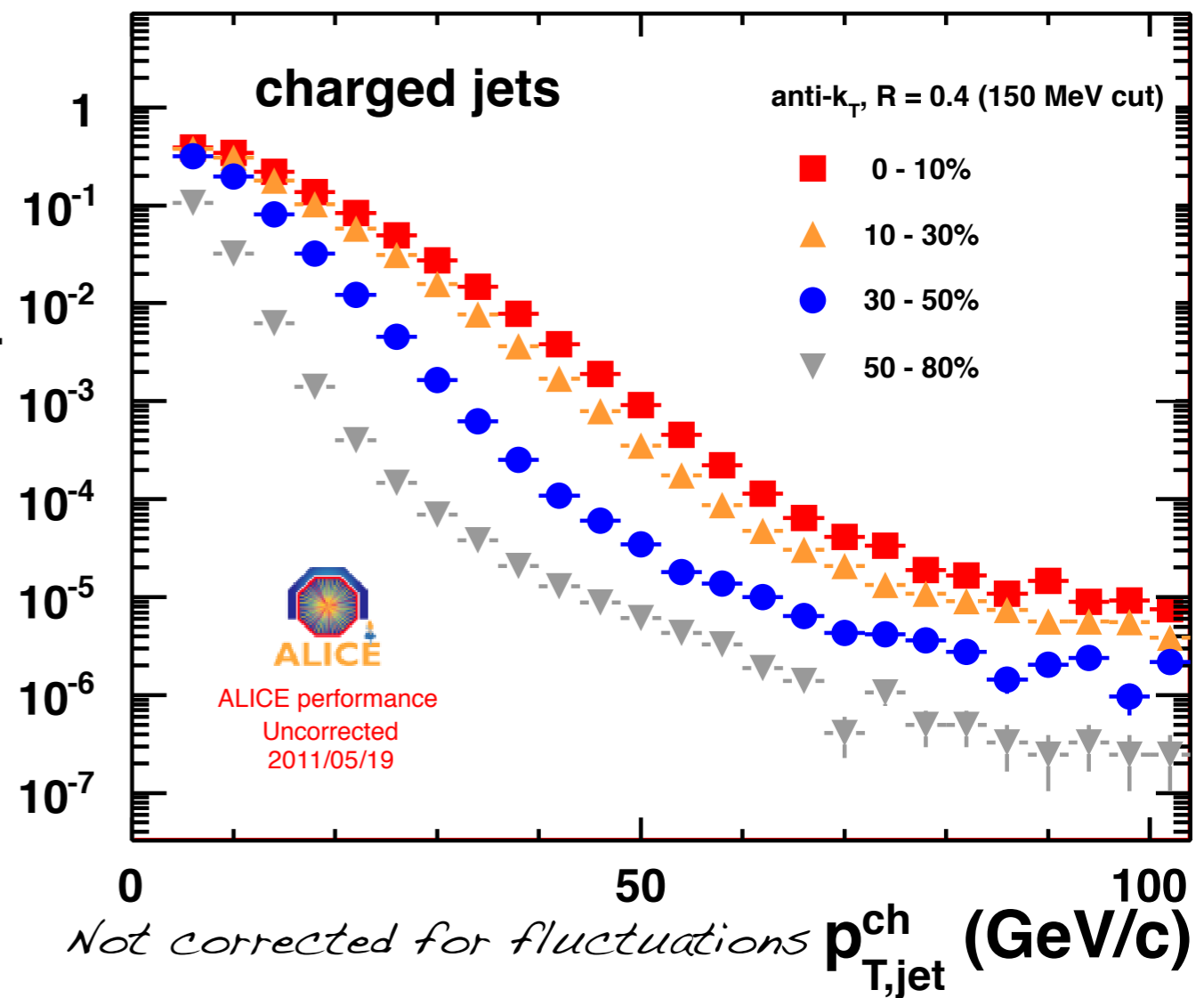
Background fluctuations: characterized by δp_T ; spectrum before corrections

LHC2010 Pb-Pb $\sqrt{s}=2.76$ TeV



$1/N_{\text{evt}} dN/dp_T d\eta$ (c/GeV)

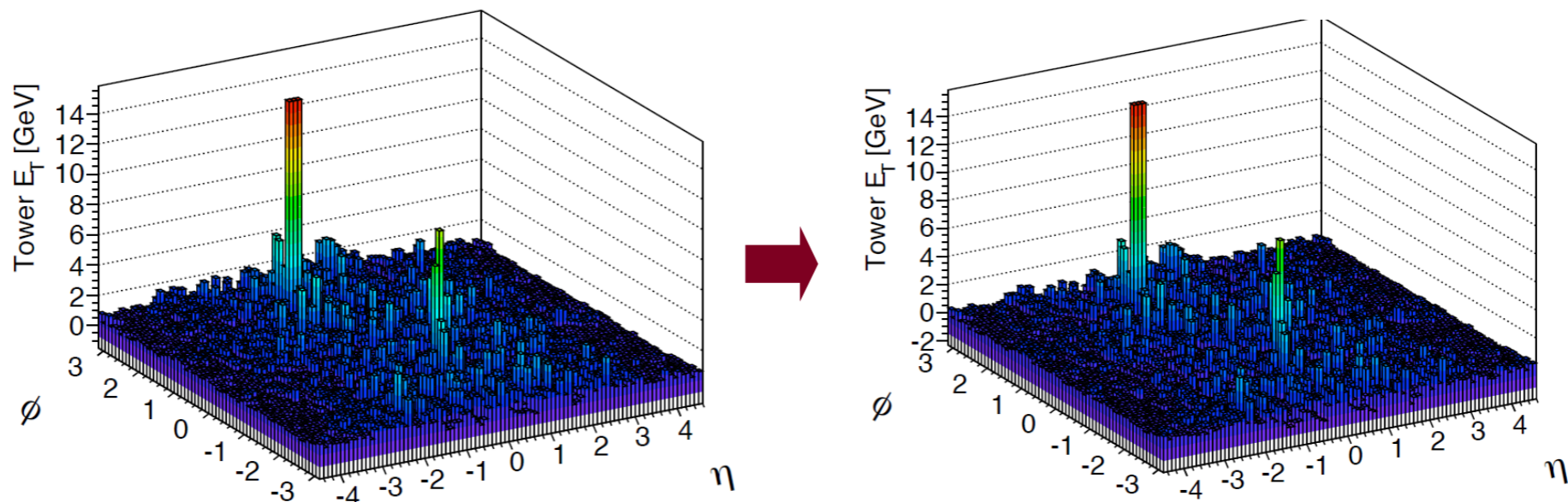
LHC2010 Pb-Pb $\sqrt{s_{NN}} = 2.76$ TeV



Energy resolution function: δp_T

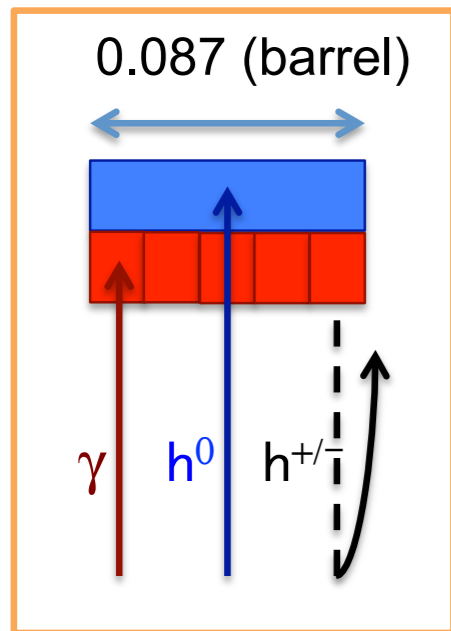
Background corrections in Atlas

- Reconstruction algorithm anti- k_t (0.2, 0.4).
- Input: calorimeter towers 0.1×0.1 ($\Delta\eta \times \Delta\phi$).
- Event-by-event background subtraction: $E_{Tsub}^{cell} = E_T^{cell} - \rho^{layer}(\eta) \times A^{cell}$
- ➡ Anti- k_t reconstruction prior to a background subtraction.
- ➡ Underlying event estimated for each longitudinal layer and η slice separately.
- We exclude jets with $D = E_{Ttower}^{max} / \langle E_{Ttower} \rangle > 4$ to avoid biasing subtraction from jets **but no jet rejection based on D** .
- Iteration step to exclude jets with $E_T > 50$ GeV from background estimation.
Jets corrected for flow contribution.

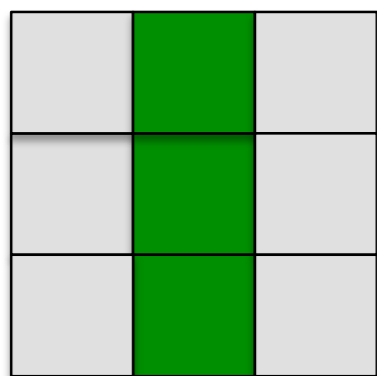


Background subtraction / jet energy corrections (CMS)

PF pseudo-tower



η strip



0.087 (barrel)

a) Event-by-event subtraction of the heavy-ion background

- Reconstructed particles towered into an (η, ϕ) grid according to HCAL cell dimensions
- Mean tower energy and dispersion are calculated for each η strip
- Same iterative background subtraction applied in [0], described in [1]
- Random cone studies: good agreement between background fluctuations in data and HYDJET simulations
- The effect of quenching on the energy scale is constrained using the jet associated charged particle spectra

b) Jet energy corrections (JEC) based on GEANT simulation of PYTHIA jets

c) Validation of the BG subtraction + JEC for PYTHIA jets embedded in HYDJET

[0] CMS, arXiv:1102.1957

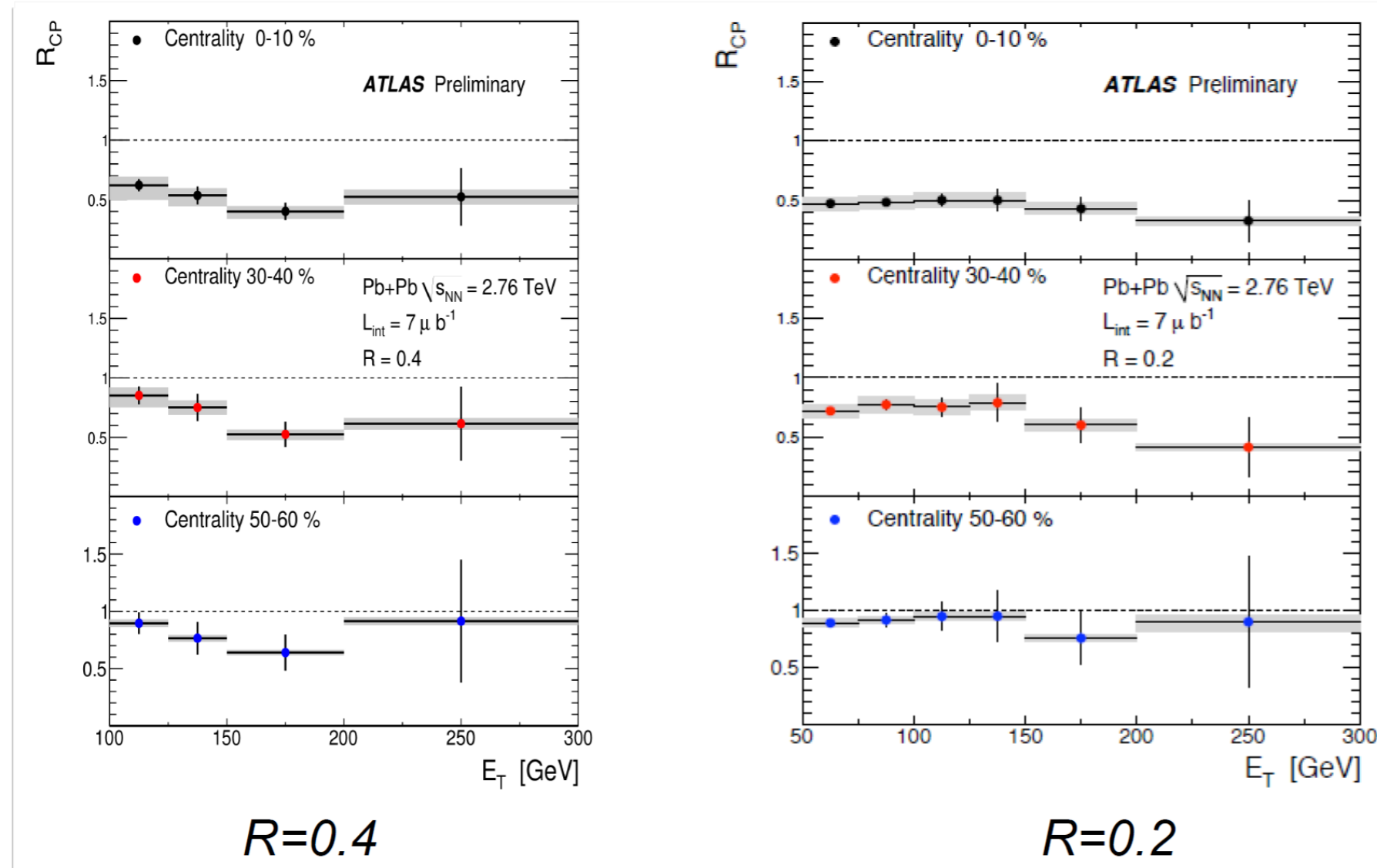
[1] Kodolova et al., EPJC 50 (2007) 117

discussion of measurements

Text

Jet $R_{\text{Central-Peripheral}}$

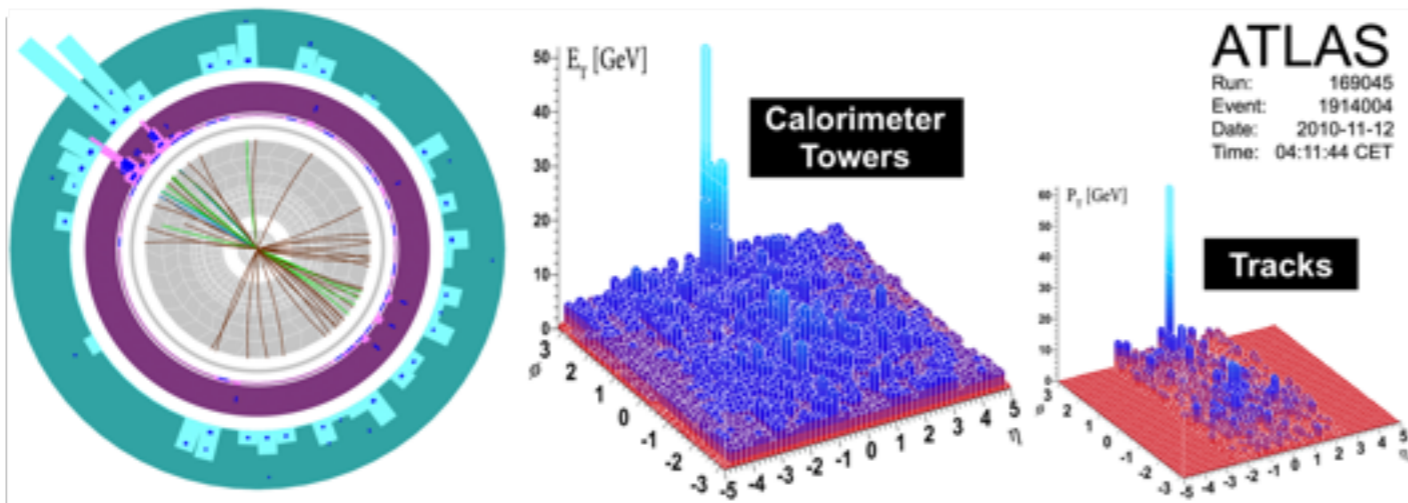
R_{CP} : similar as R_{AA} , but denominator are not yields from proton-proton but from peripheral heavy-ion collisions



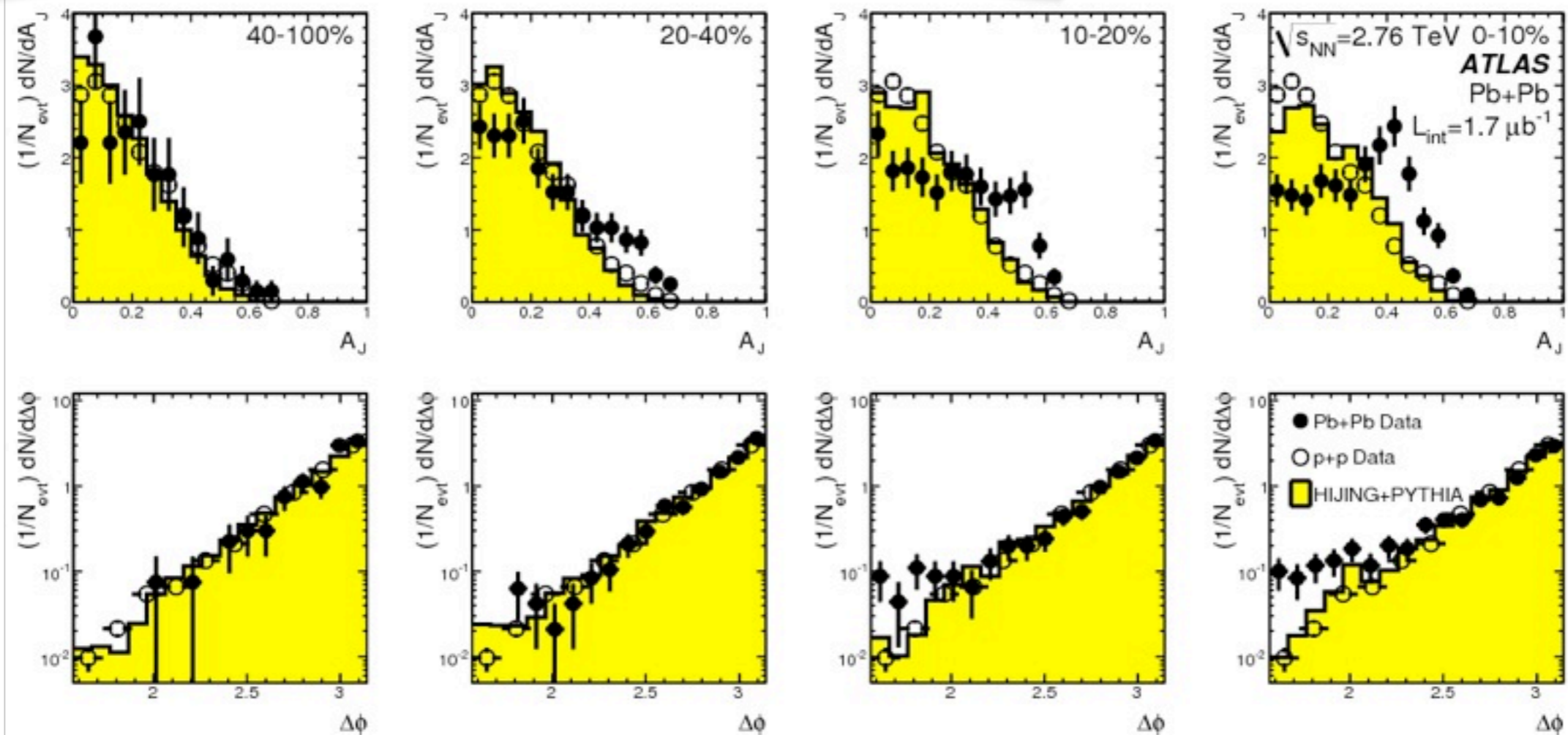
Flat! - in contrast to R_{AA} of hadrons

$R_{\text{CP}} \sim 0.5 \Rightarrow$ suppression - jets loose energy in most central events
- the radiation is not captured within the jet cone (R)

LHC: Di-jet asymmetry

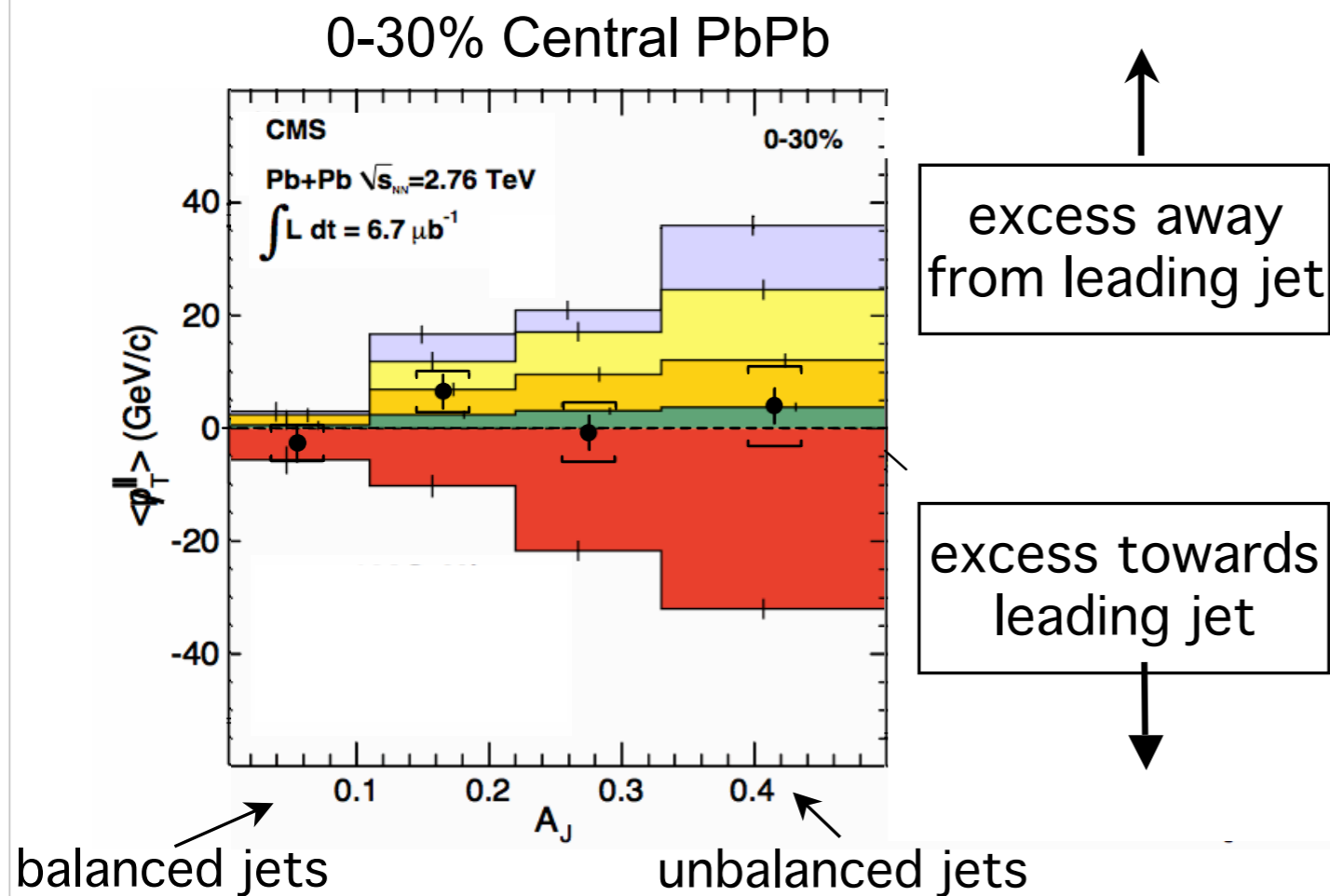


$$A_J \equiv \frac{E_{T1} - E_{T2}}{E_{T1} + E_{T2}}$$

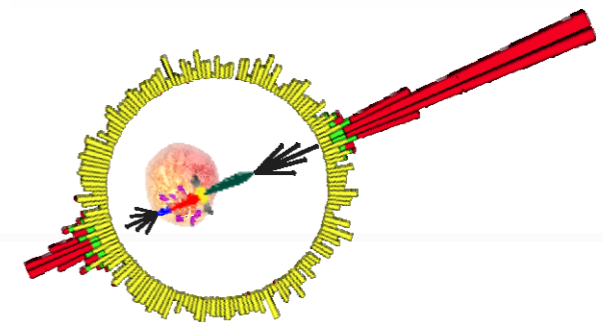
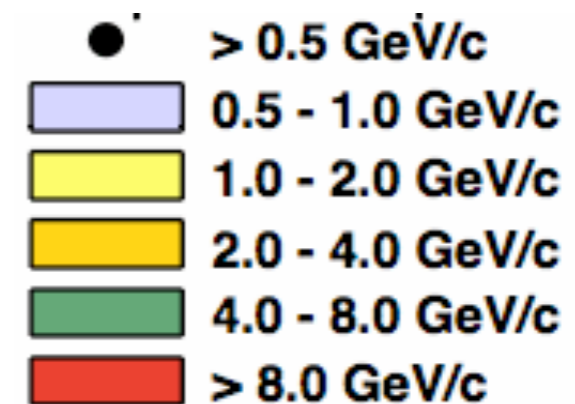


di-jet asymmetry: where does the energy go?

Missing p_T^{\parallel} : $p_T^{\parallel} = \sum_{\text{Tracks}} -p_T^{\text{Track}} \cos(\phi_{\text{Track}} - \phi_{\text{Leading Jet}})$

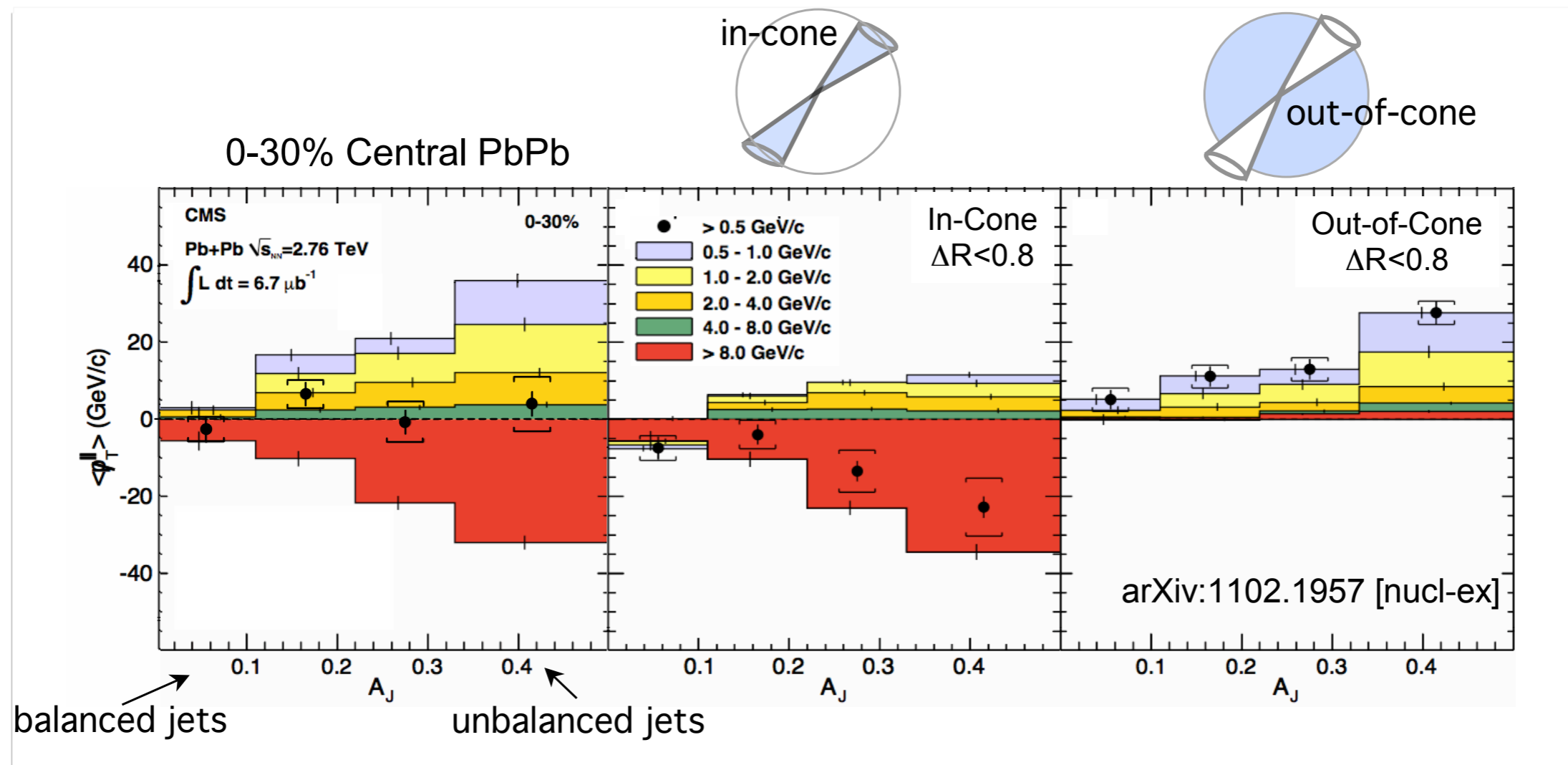


Calculate missing p_T in ranges of track p_T :

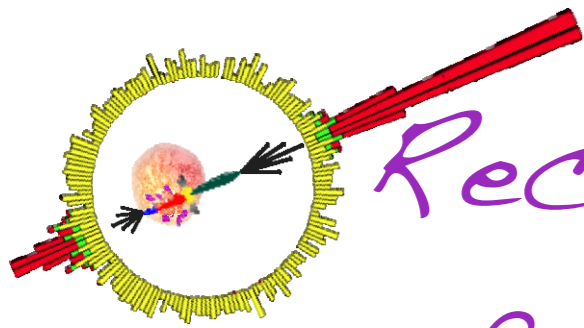


*The momentum difference
balanced by low- p_T particles*

di-jet asymmetry: where does the energy go?

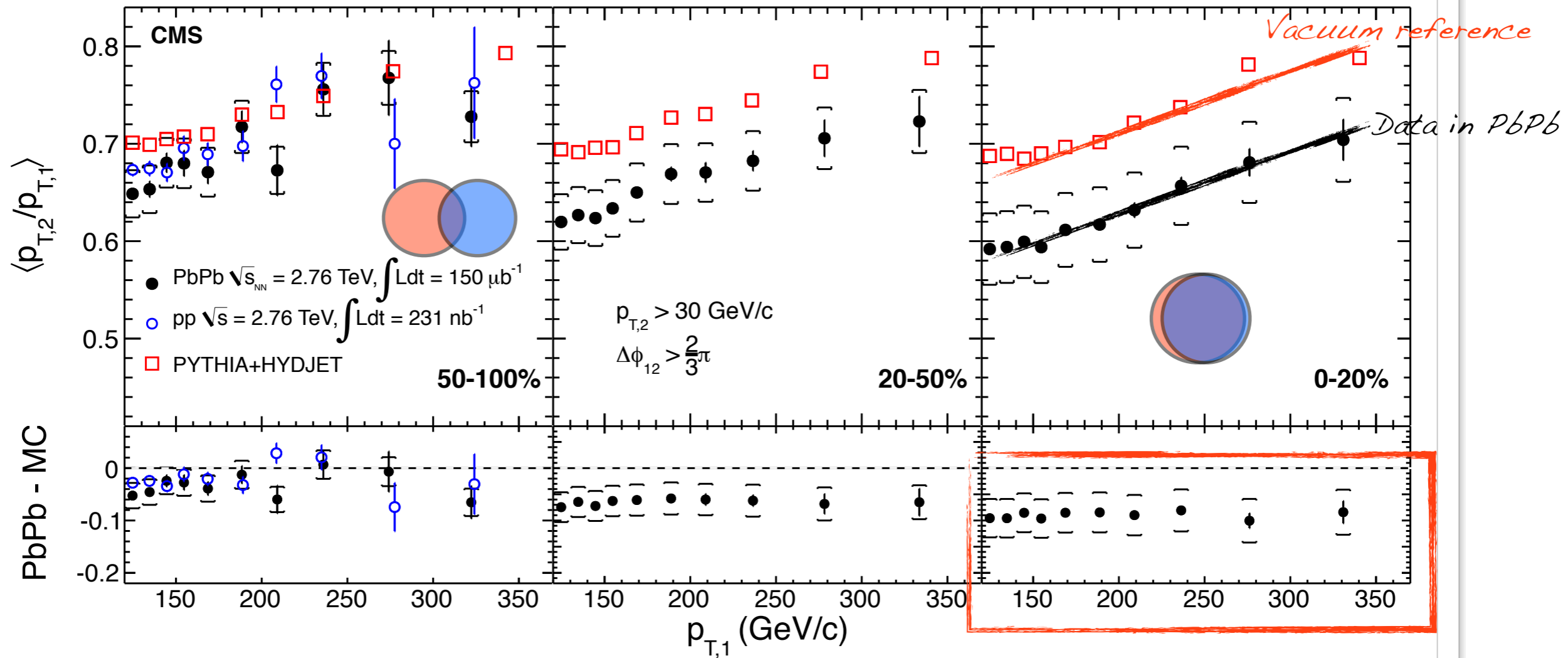


The low- p_T particles "balancing" the lost energy appear at large angles wrt recoil jet



Recoil jet (2) energy-loss as a function of trigger jet (1) p_T

$p_{T,2} > 30 \text{ GeV}/c$



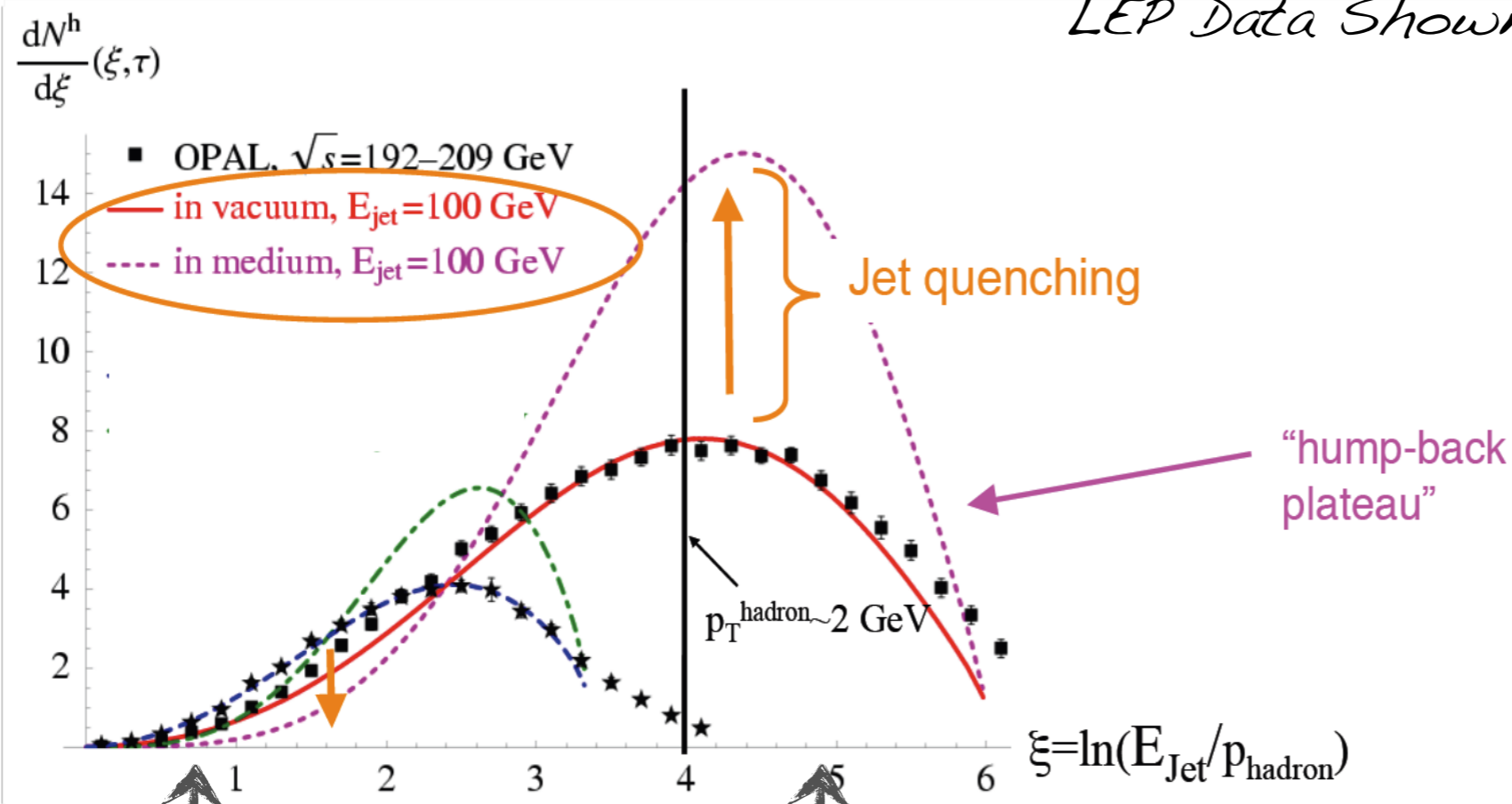
Ratio follows the PYTHIA+HYDJET reference with the same rate - constant offset over 200 GeV in p_T

Modified jet fragmentation

- an expectation from jet quenching

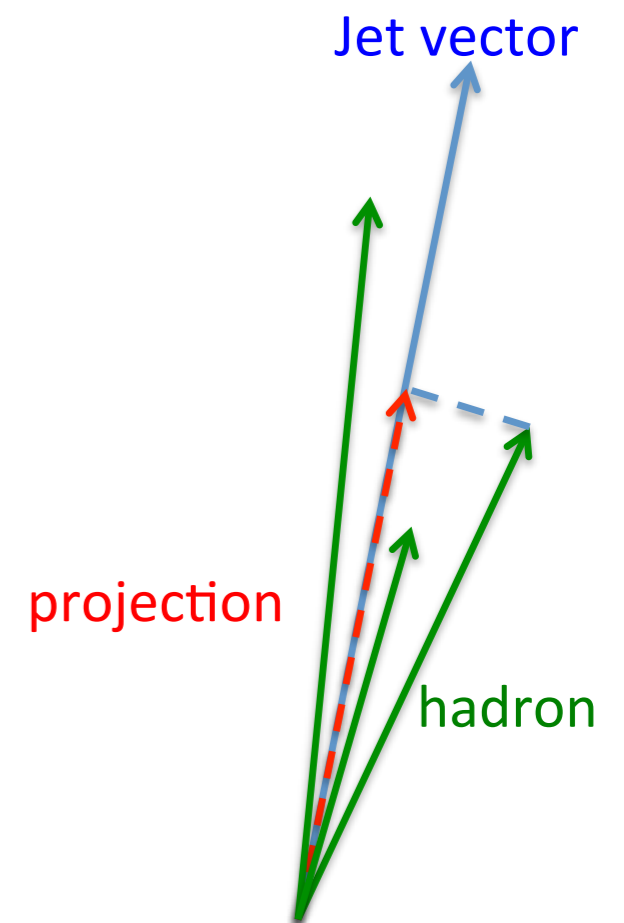
$$\xi = \ln(E_{\text{jet}}/p_{\text{hadron}})$$

LEP Data Shown

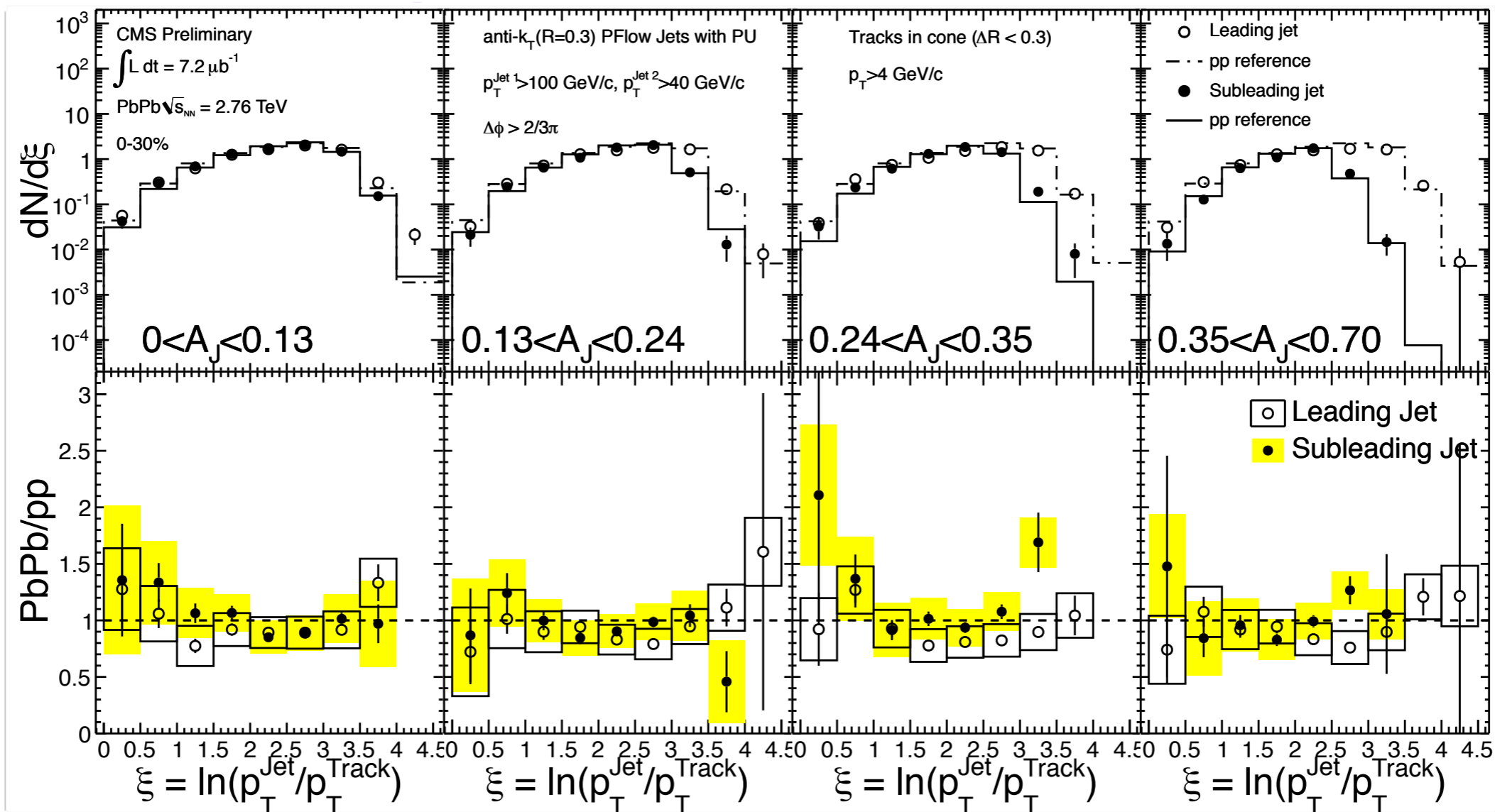


High momentum
hadrons

Low momentum
hadrons

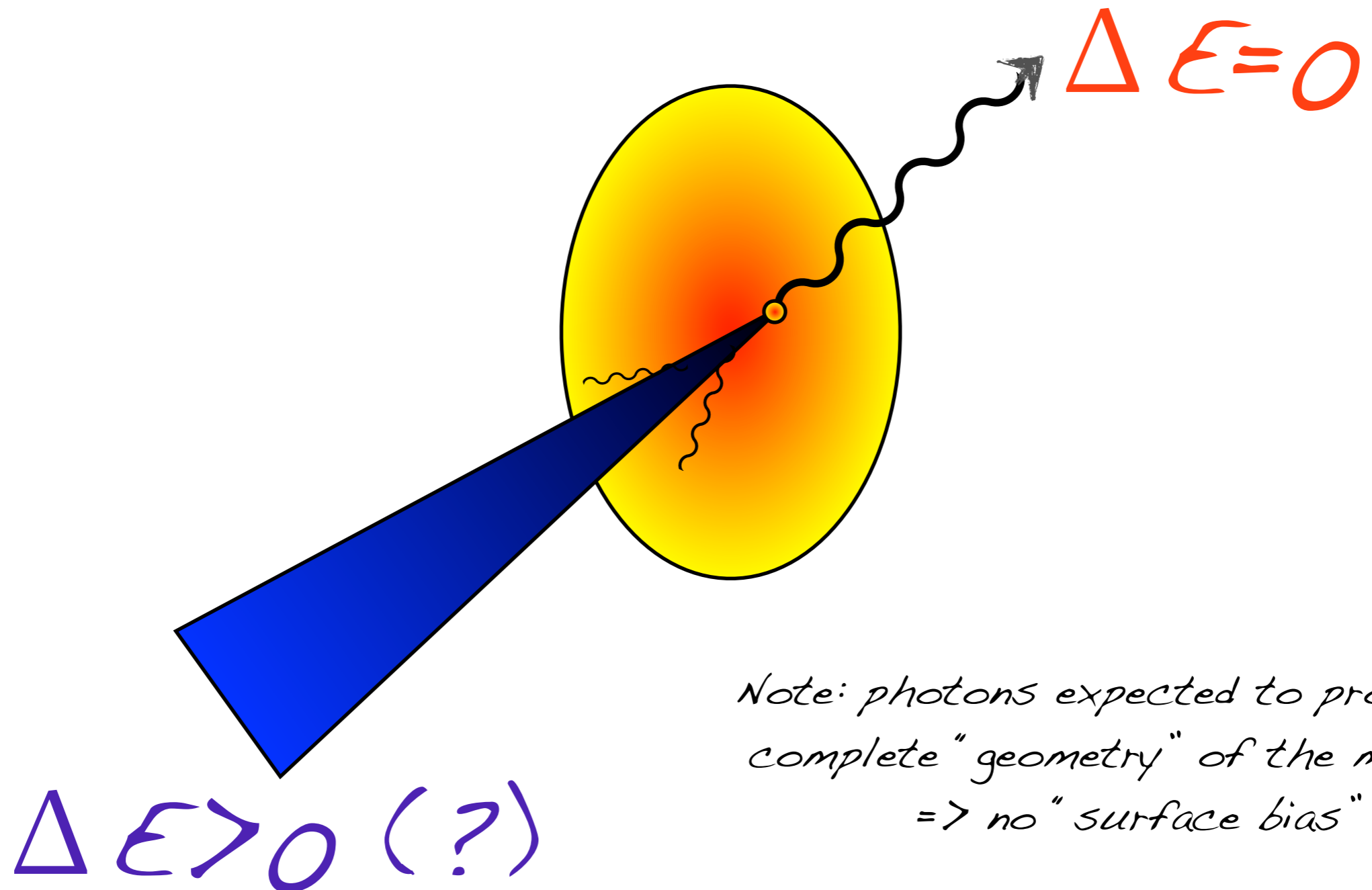


Jet fragmentation in Heavy-ion collisions



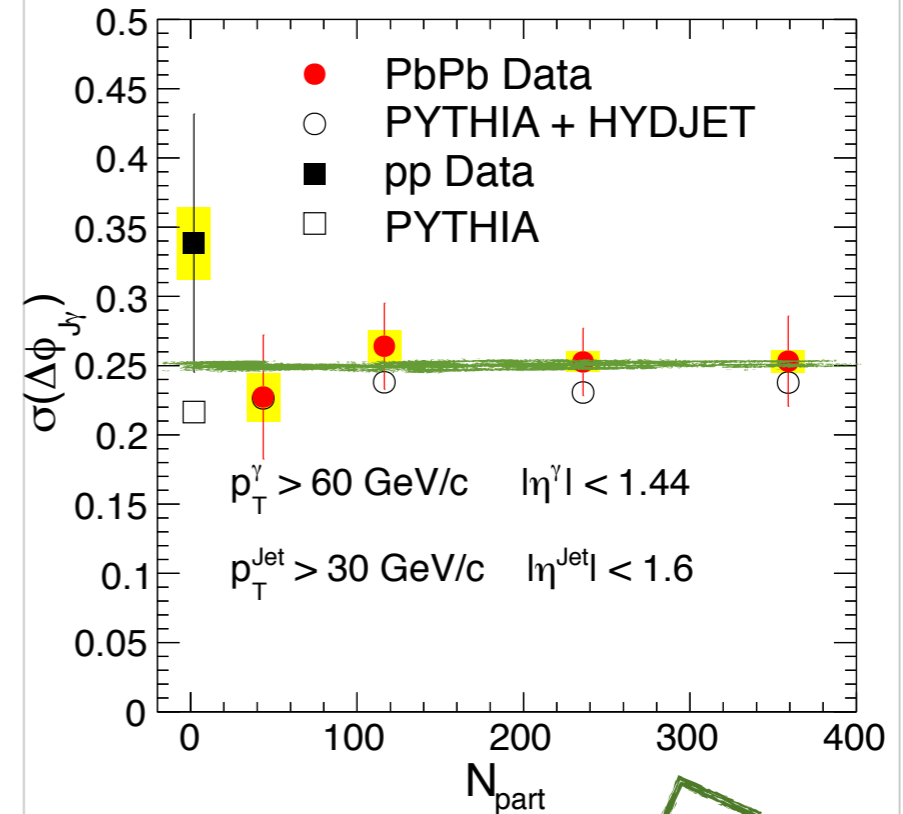
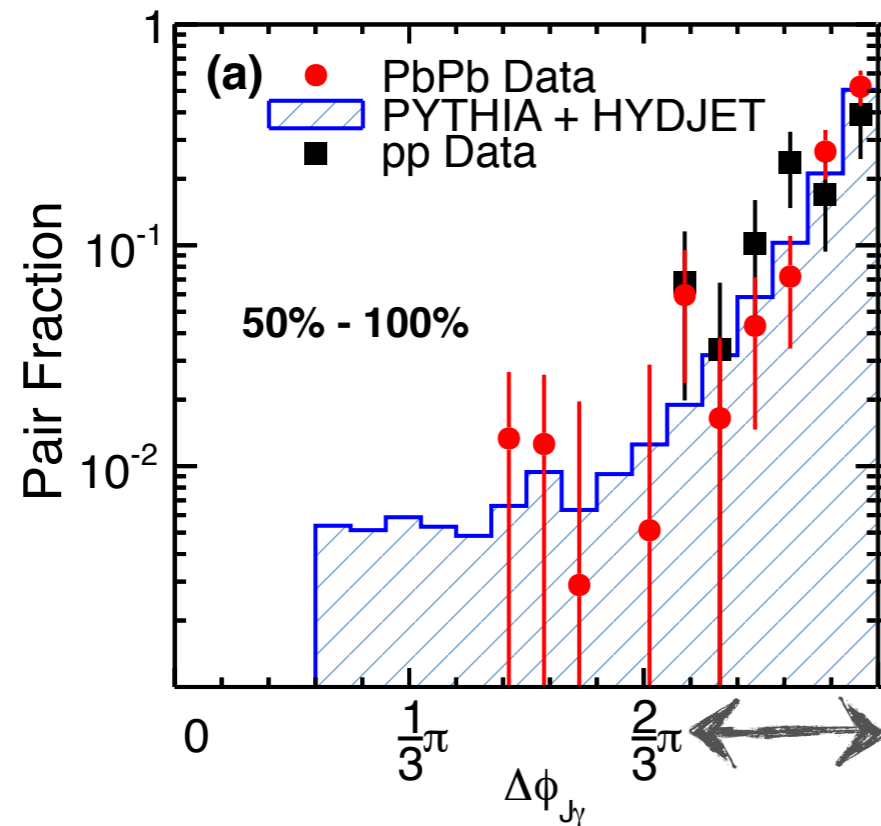
CMS observation: Fragmentation of jets that lost energy consistent with jet fragmentation in proton-proton (vacuum) - similar observations by ATLAS
- a question: is the particle composition of the jet modified?

Photon-jet



*Note: photons expected to probe the complete "geometry" of the medium
=> no "surface bias"*

Photon($\Delta E=0$)-jet($\Delta E>0$)



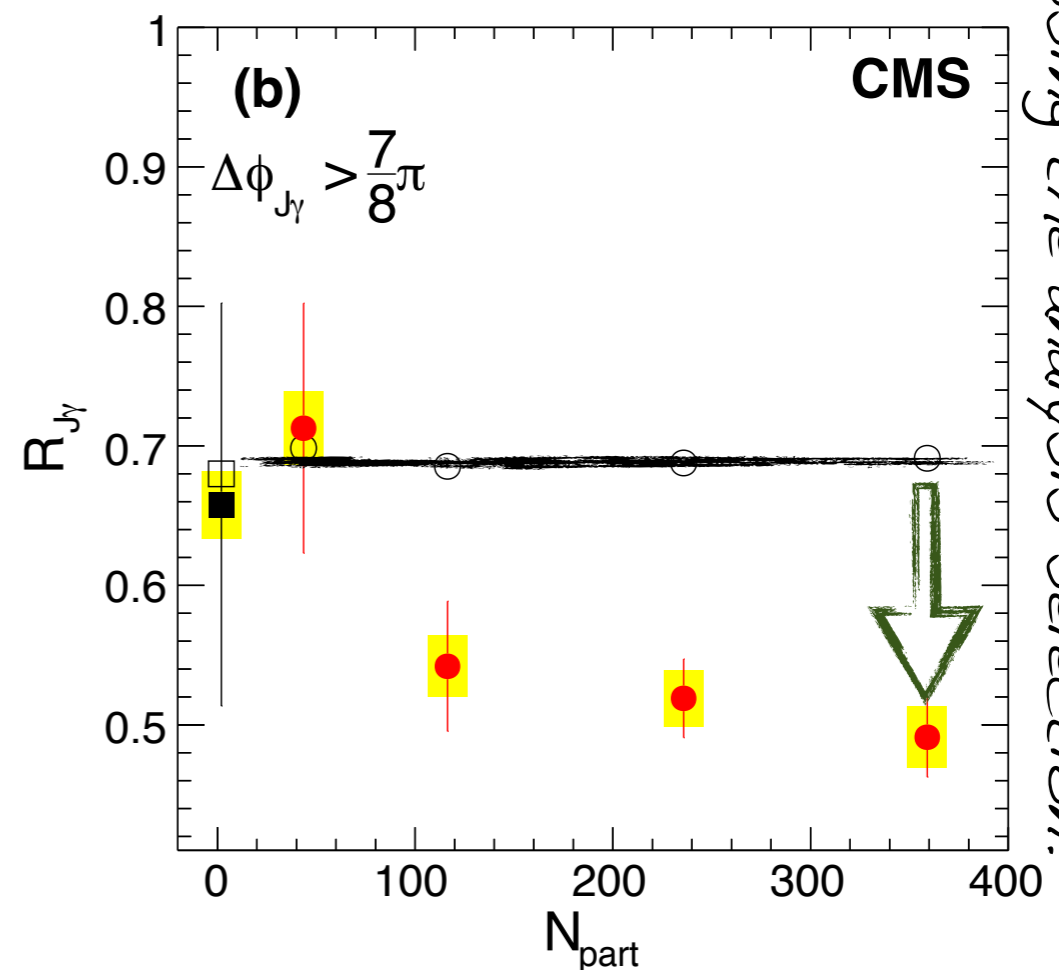
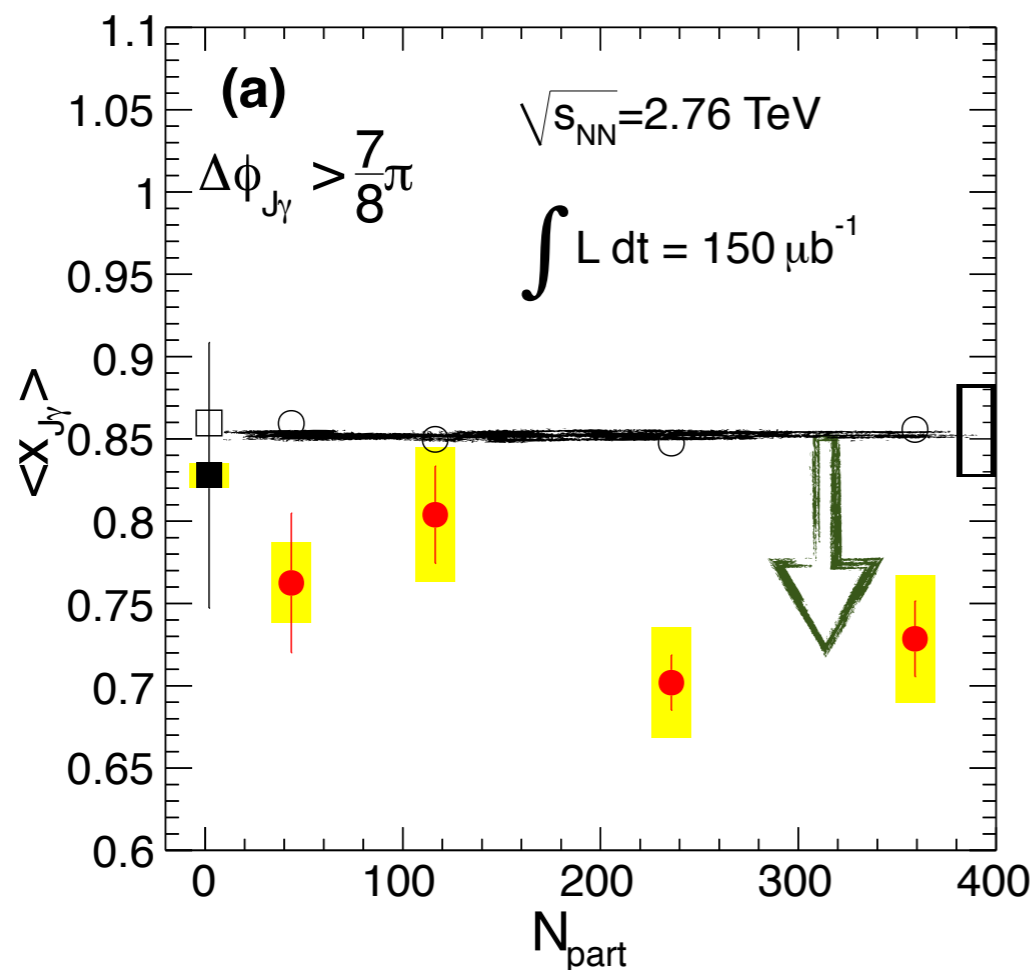
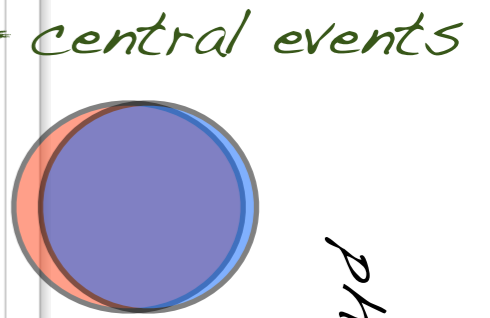
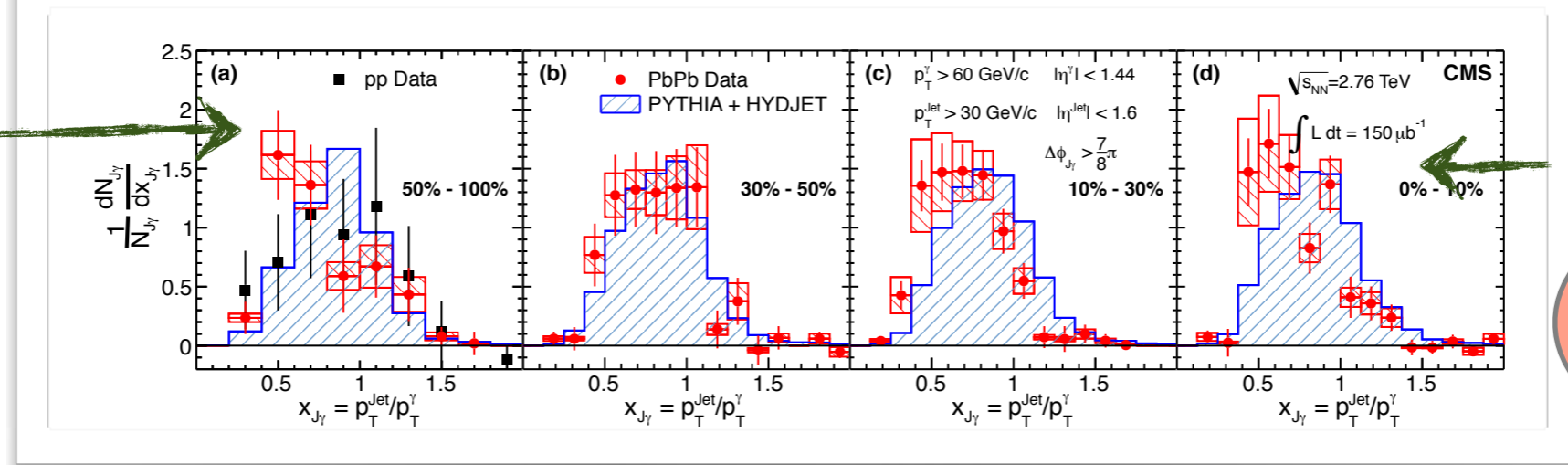
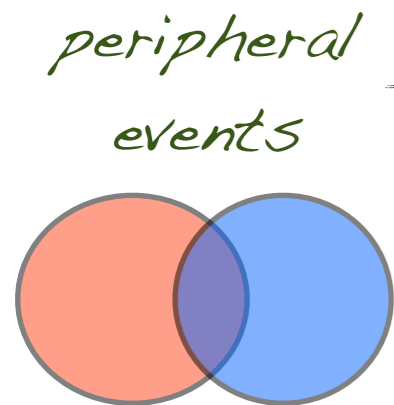
Fit $\frac{1}{N_{J\gamma}} \frac{dN_{J\gamma}}{d\Delta\phi_{J\gamma}} = \frac{e^{(\Delta\phi - \pi)/\sigma}}{(1 - e^{-\pi/\sigma}) \sigma}$

Range: $\Delta\phi > 2\pi/3$

"Width" consistent with vacuum

Photon($\Delta E=0$)-jet($\Delta E>0$)

The asymmetry ratio $x_{J\gamma} = p_T^{\text{Jet}} / p_T^{\gamma}$ is used to quantify the photon+jet momentum imbalance.

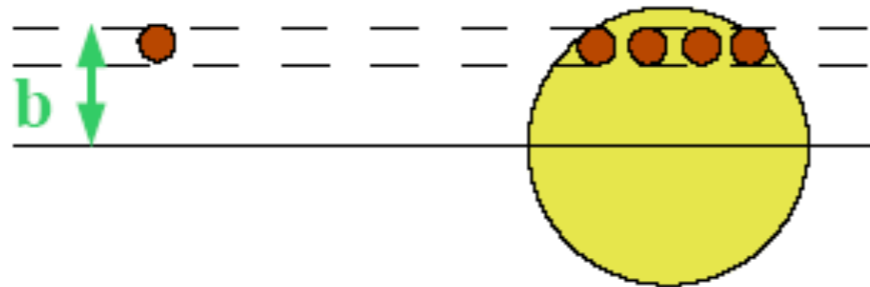


$R_{J\gamma}$ - the fraction of isolated jet photons that have an associated jet passing the analysis selection.

Thanks!

- For graphics/slides from: P. Govoni, M. Nguyen, T. Hemmick, P. Jacobs, M. van Leeuwen, J. Putschke, C. Roland, M. Rybář, I. Wingerter
- For the material by collaborations: ALICE, ATLAS, CMS, PHENIX, STAR

Nuclear geometry - Glauber model and hard processes



Nuclear thickness function

Normalized nuclear density $\rho(b, z)$:

$$\int dz db \rho(b, z) = 1$$

$$T_A(b) = \int_{-\infty}^{\infty} dz \rho(b, z)$$

Inelastic cross section for p+A:

$$\sigma_{pA}^{inel} = \int d\vec{b} \left(1 - \left[1 - T_A(b) \sigma_{NN}^{inel} \right]^A \right)$$

Glauber scaling: hard processes with large momentum transfer

- short coherence length \Rightarrow successive NN collisions independent
- p+A is incoherent superposition of N+N collisions

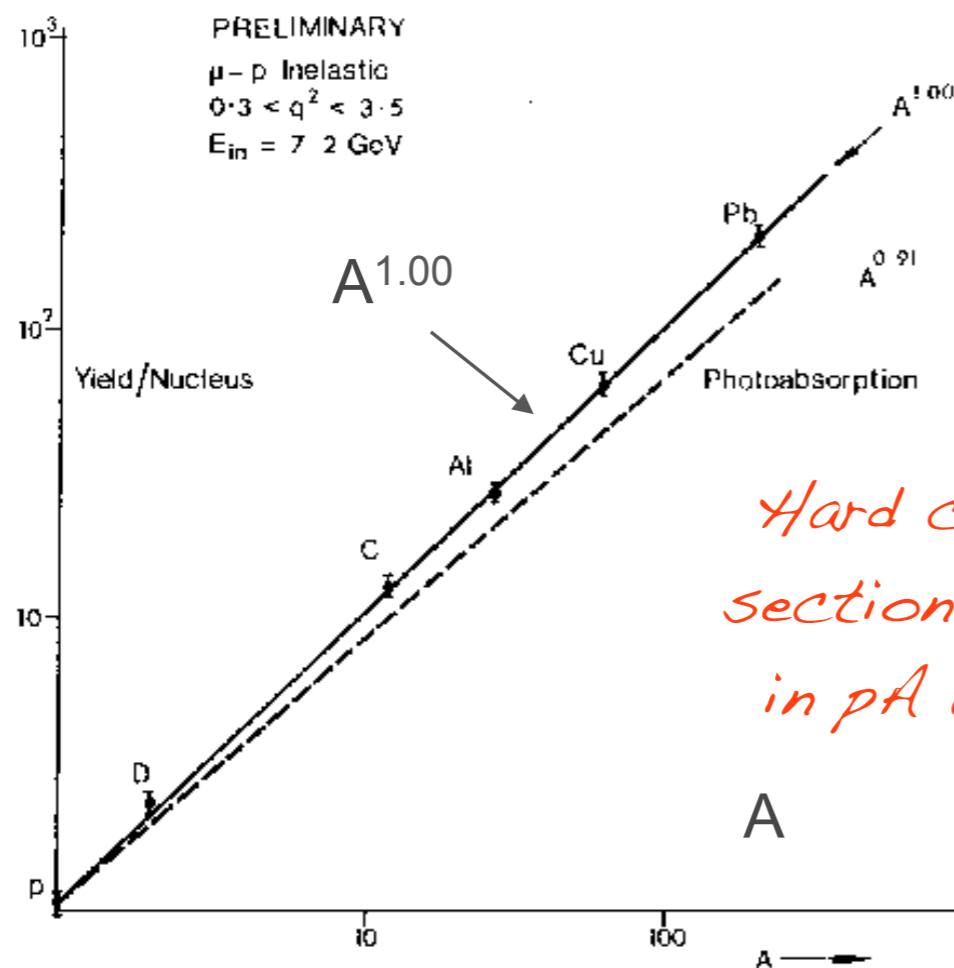
$$\sigma_{pA}^{hard} \approx A \sigma_{NN}^{hard} \int d\vec{b} T_A(\vec{b}) = A \sigma_{NN}^{hard}$$

Glauber scaling of hard processes

Glauber scaling: $\sigma_{pA}^{hard} = A \sigma_{NN}^{hard}$

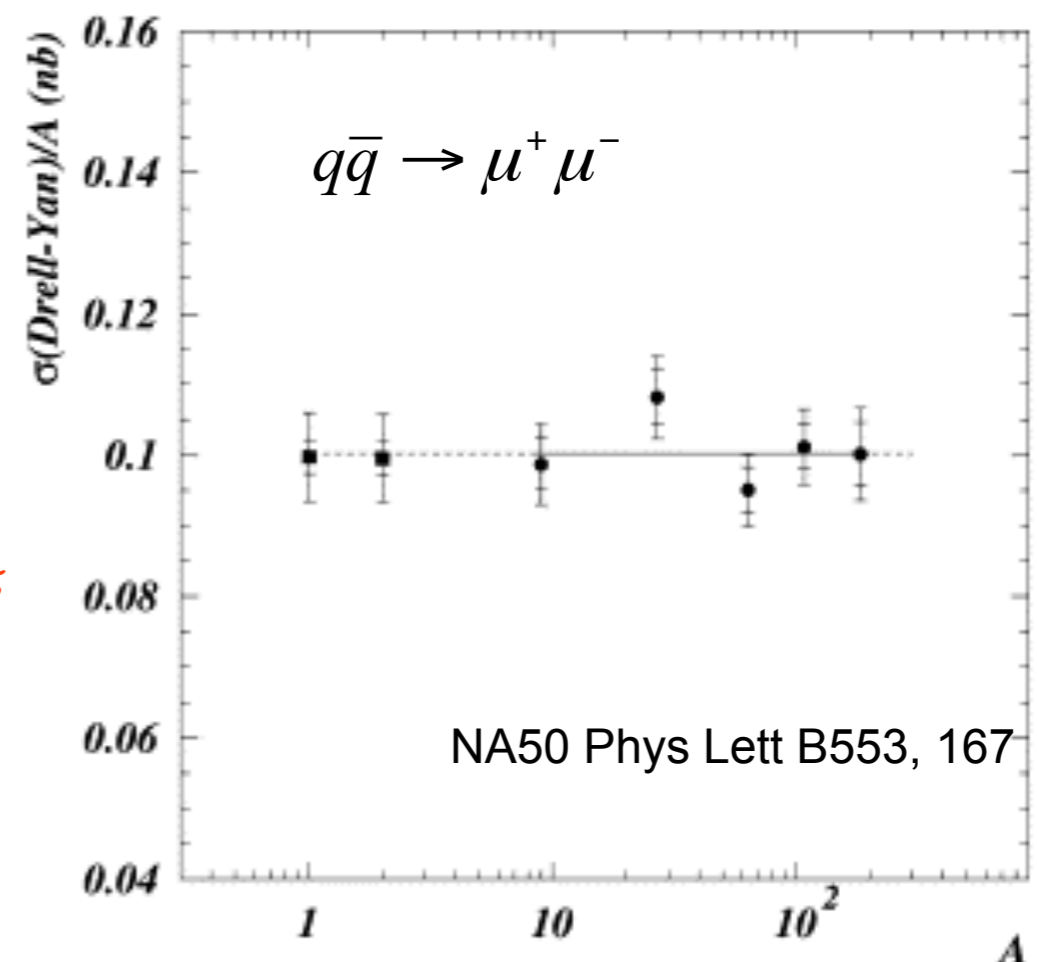
σ_{inel} for 7 GeV muons on nuclei

M. May et al, Phys Rev Lett 35, 407 (1975)

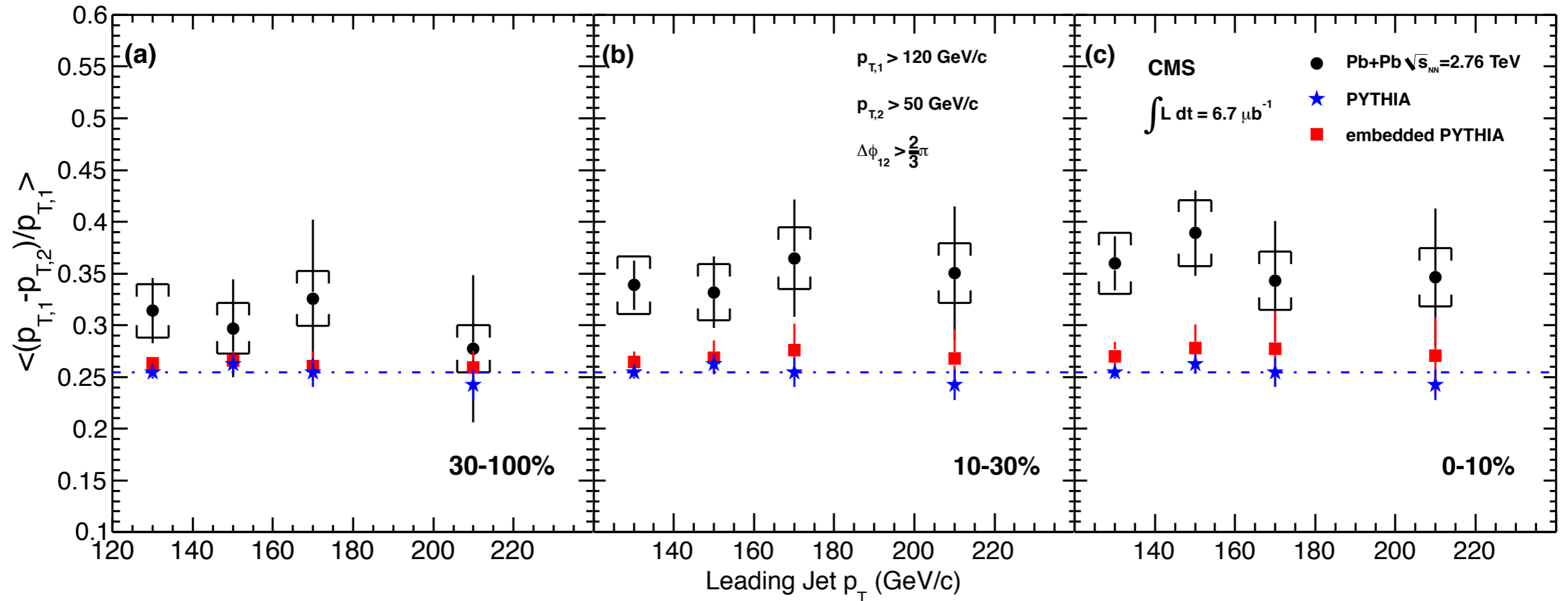


Hard cross-section scales in pA as $A^{1.0}$

$\sigma_{Drell-Yan}/A$ in p+A at SPS



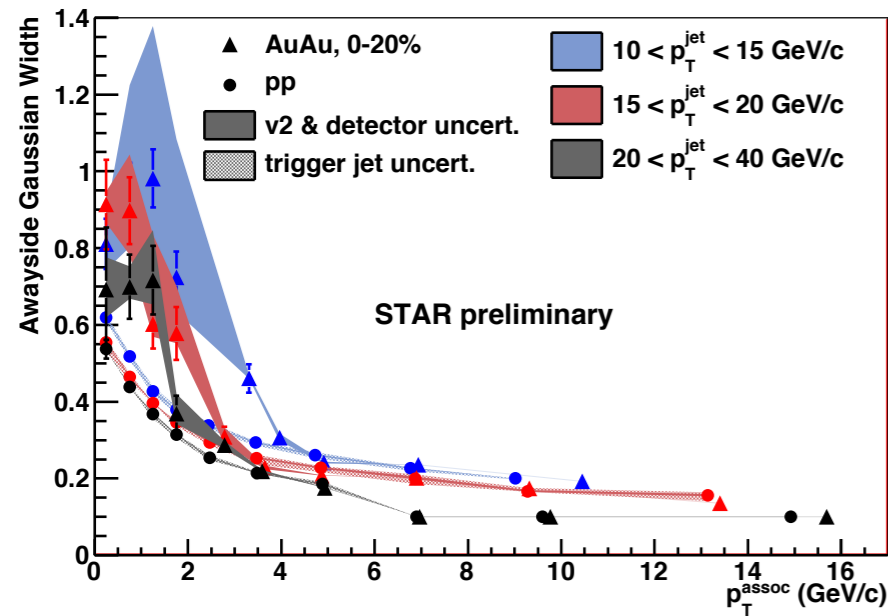
Di-jet asymmetry



The fractional imbalance:

- grows with collision centrality and reaches a much larger value than in PYTHIA or PYTHIA+DATA
- clearly visible even for the highest- p_T jets observed in the data set
- the $p_{T,1}$ dependence of the excess imbalance is compatible with either a constant difference or a constant fraction of $p_{T,1}$.

Jet-hadron coincidences



Broadening & softening of the recoil jet at RHIC

Figure 1. The Gaussian widths of the away-side jet peaks in Au-Au (triangles) and p-p (circles) indicate broadening of the away-side jet in Au-Au.

STAR @ RHIC

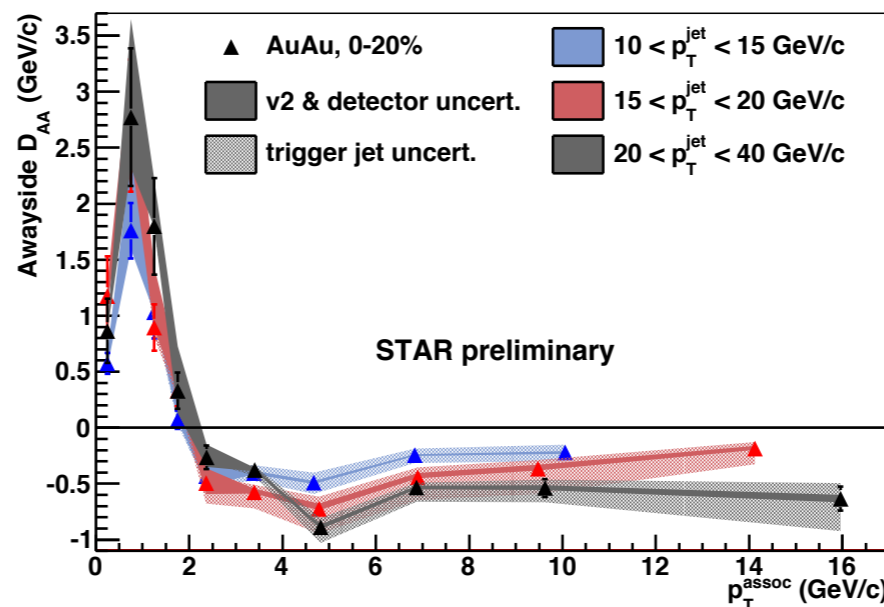
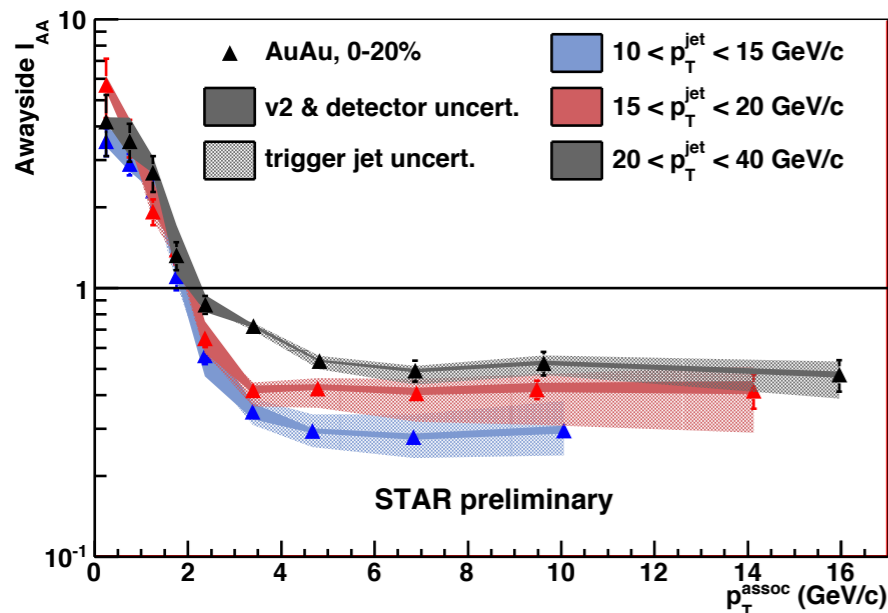
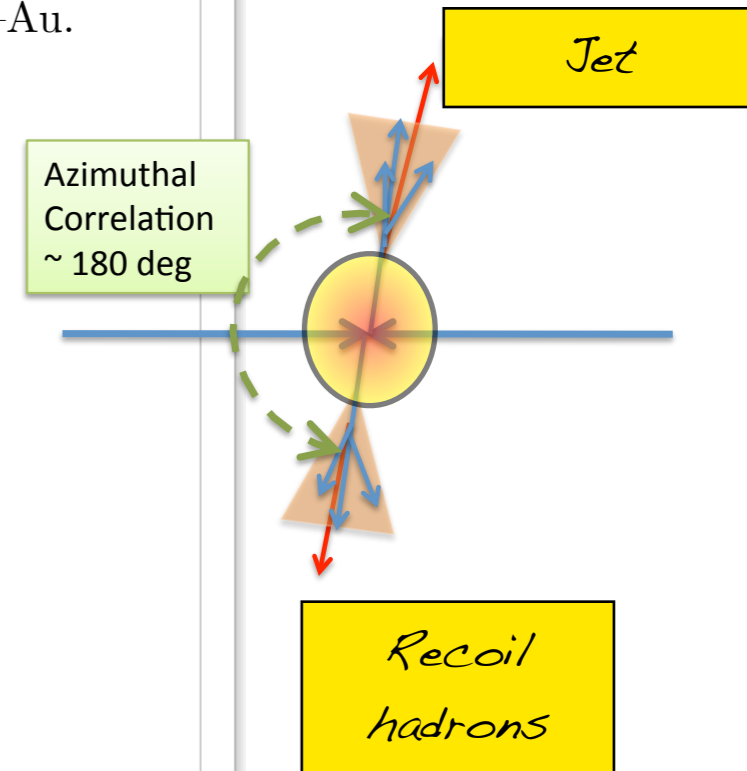


Figure 2. The away-side I_{AA} (left) and D_{AA} (right) indicate a softening of the away-side jet for three reconstructed jet energy ranges. The away-side D_{AA} shows that high- p_T^{assoc} suppression is compensated for by low- p_T^{assoc} enhancement.

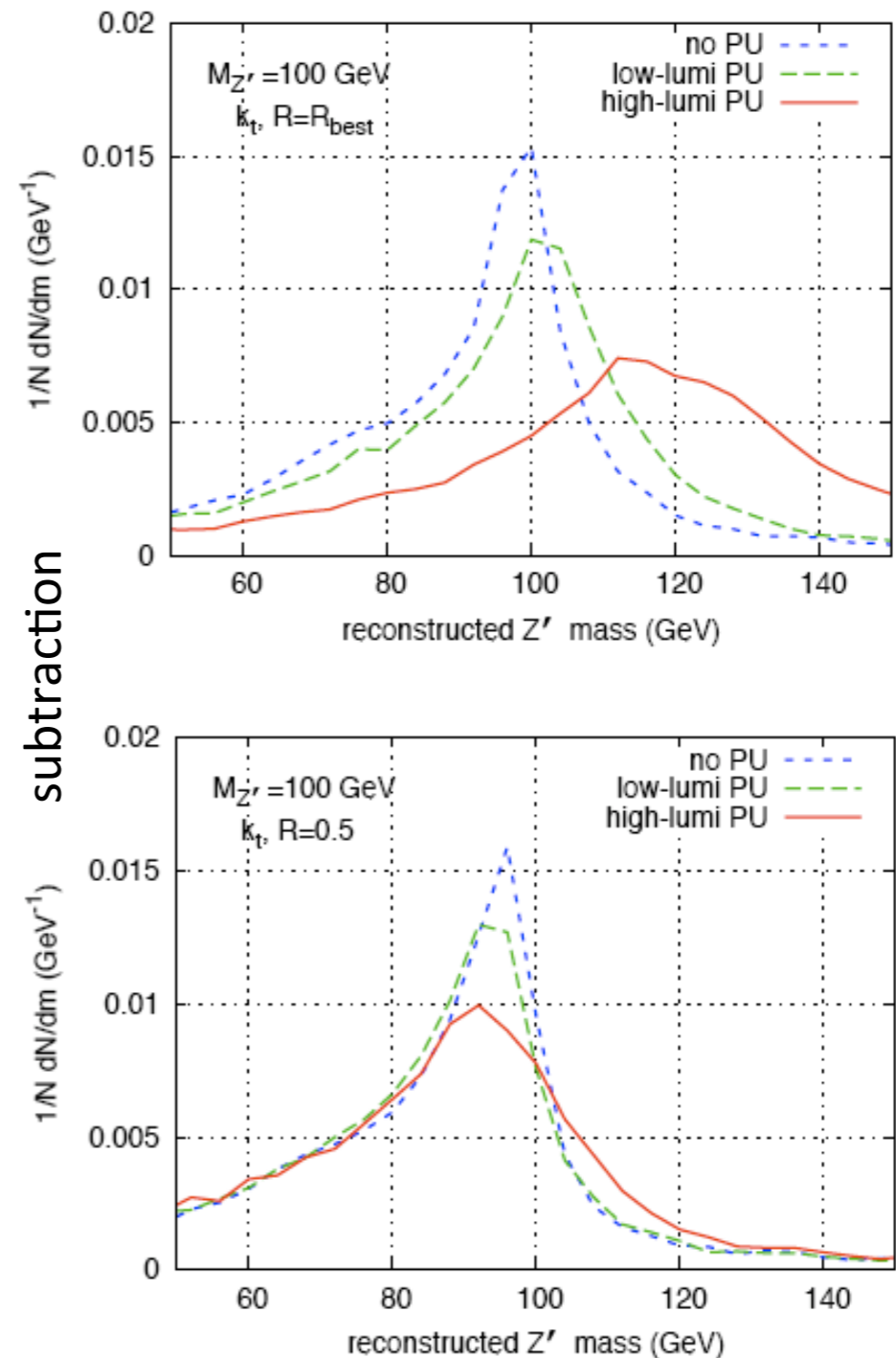


Background subtraction

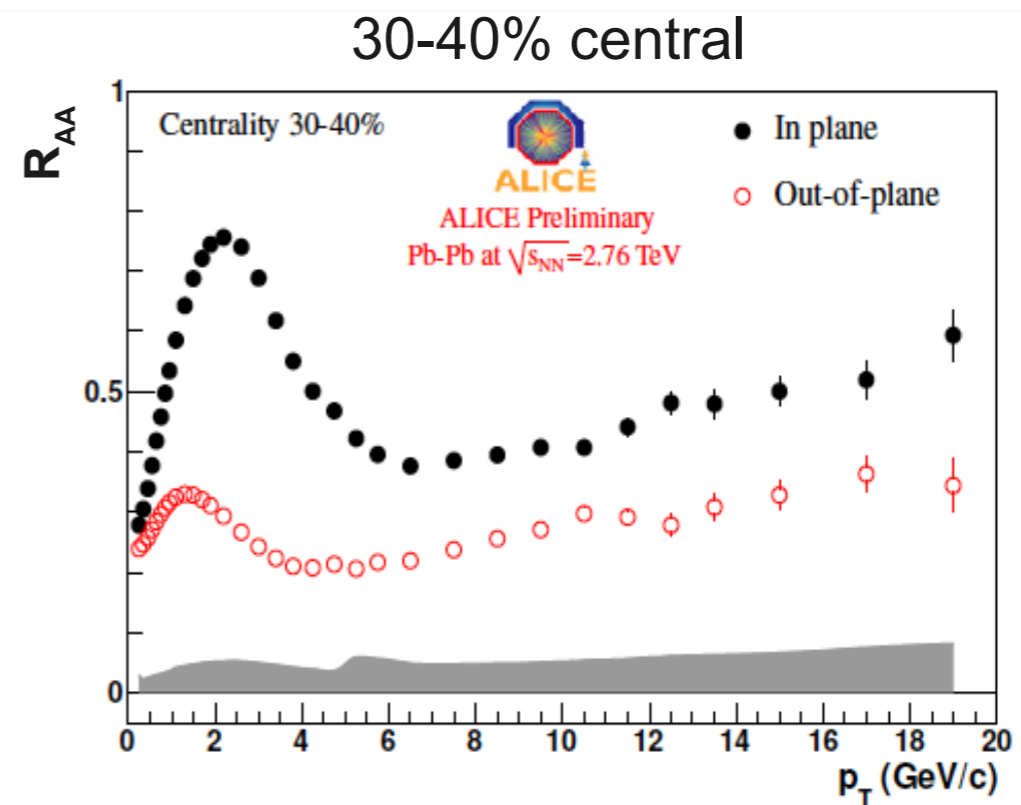
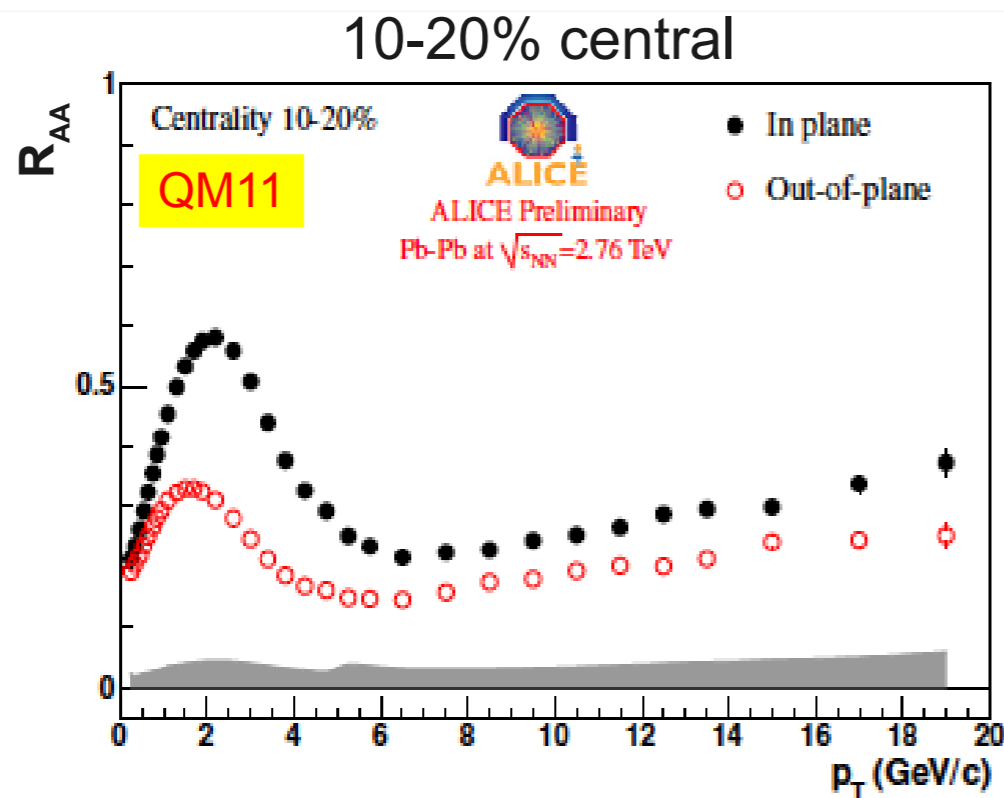
$$p_T^{jet} = p_T^{cluster} - \rho \times Area$$

$$p_T^{jet} = p_T^{true} \otimes \delta\rho$$

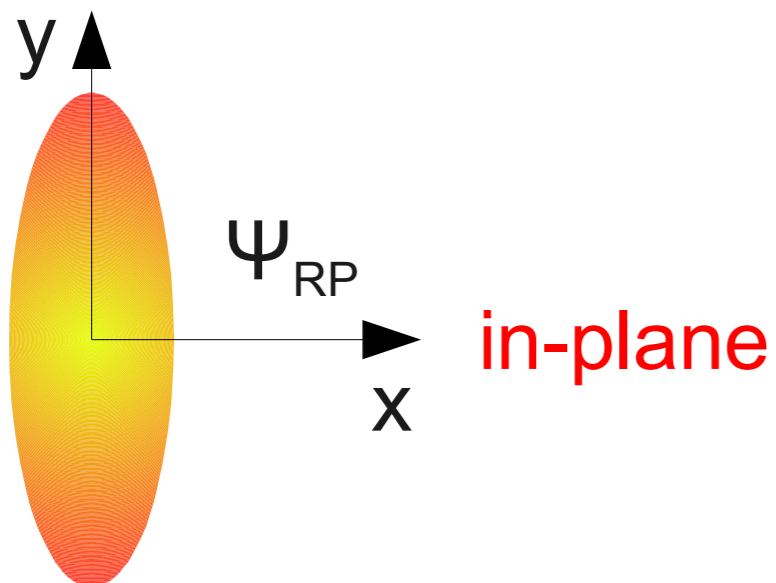
- ρ : median pT per unit area of the diffuse background in an event – measured using background “jets” as found by kT algorithm
- A: area of the jet – measured using number of artificially injected infinitely soft particles of finite “size” into an event that are clustered into the jet
- $\delta\rho$: uncertainty due to noise fluctuations – non-uniformity of the event background



R_{AA} wrt reaction plane



out-of-plane



Suppression out-of-plane stronger \leq longer in-medium path length - significant effect even at 20 GeV/c
 \Rightarrow Path length dependence of energy loss ?

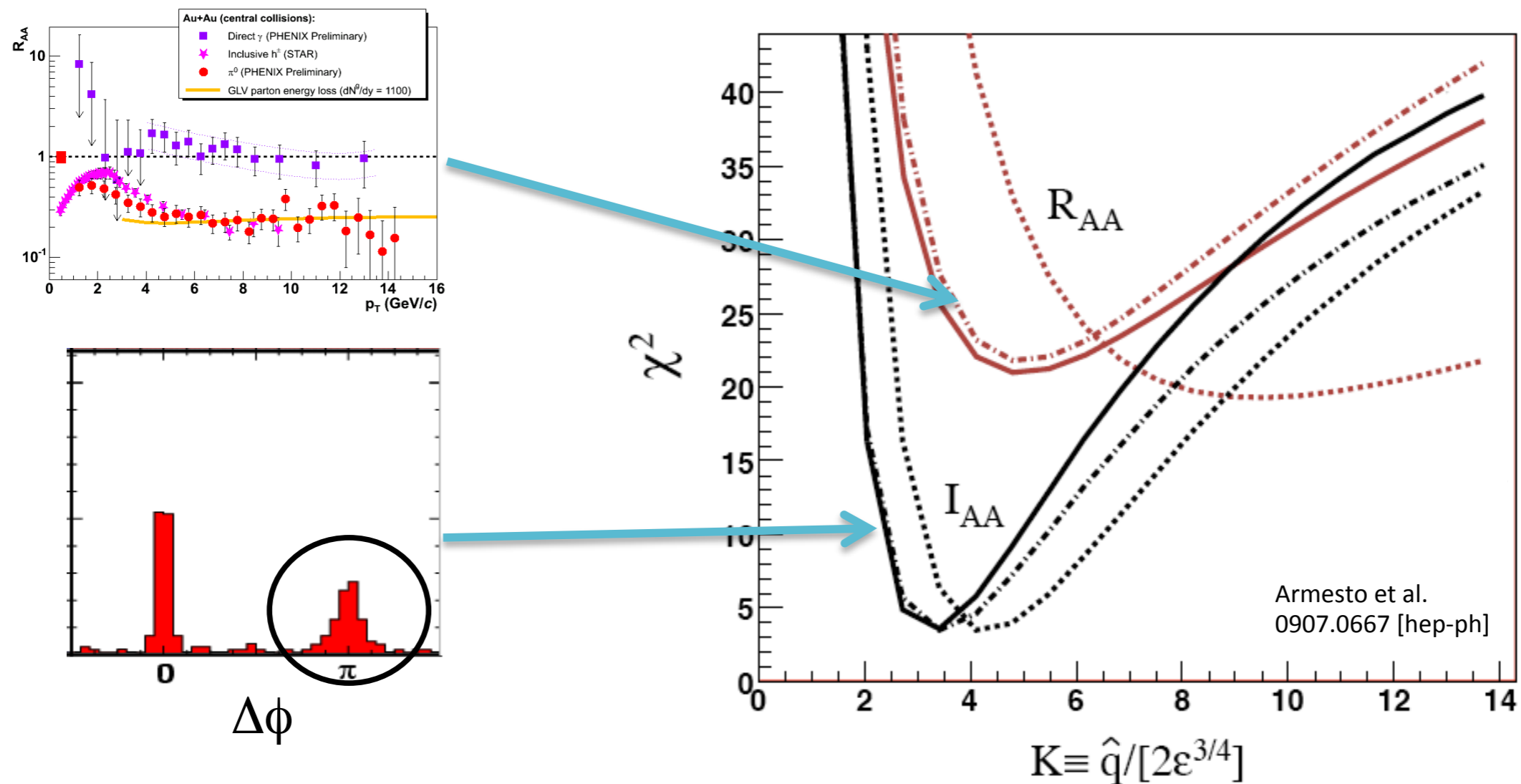
Additional constraints to energy loss models (?)

- similar information from v_2 at high p_T

$$R_{AA}(\varphi) = R_{AA}(1 + 2v_2 \cos 2(\varphi - \psi))$$

High- p_T hadrons: quantitative analysis

Model calculation: ASW quenching weights, detailed geometry
Simultaneous fit to data.



Reasonably self-consistent fit of independent observables
Main limitation is the accuracy of the theory...