

# Theory introduction

**Paride Paradisi**

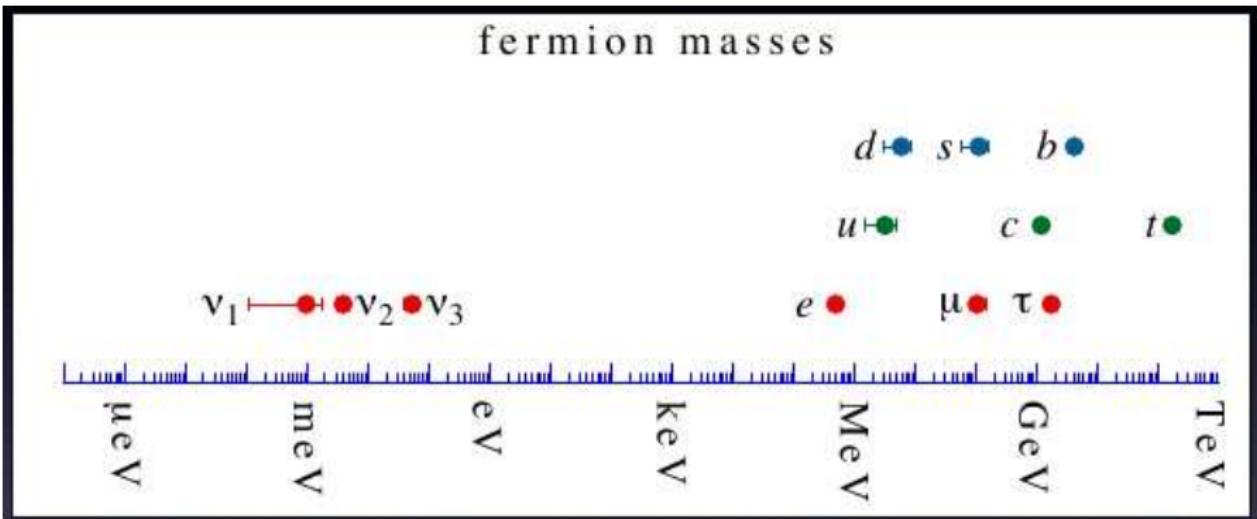
CERN

The eighth meeting on B physics  
February 6-7th, 2012, GENOVA

- ① Open questions
- ② The SM flavour puzzle
- ③ Messages from the B-factories and Tevatron
- ④ The New Physics flavour & CP problems
- ⑤ “Flavour-test” of NP models: the case of SUSY
  - ▶ SUSY MFV scenarios
  - ▶ SUSY GUT scenarios
  - ▶ SUSY flavour models
- ⑥ LHC vs. Flavour
- ⑦ Conclusions

- ① Which is the underlying mechanism regulating the EWSB?
- ② Which is the connection between EWSB and flavor physics?
- ③ Are there new flavor symmetries beyond the puzzling fermion mass spectrum?
- ④ Are there new flavor violating interactions not governed by the SM Yukawas? That is, to which extent the MFV hypothesis is valid?
- ⑤ Do the new sources of CPV accounting for the BAU have an impact on flavor physics and/or EDMs?
- ⑥ Which is the role of flavor physics in the LHC era?
- ⑦ Do we expect to understand the (SM and NP) flavor puzzles through the interplay of flavor physics and the LHC?
- ⑧ .....

# The fermion mass puzzle



$$|V_{CKM}| \sim \begin{pmatrix} 1 & \lambda_c & \lambda_c^3 \\ \lambda_c & 1 & \lambda_c^2 \\ \lambda_c^3 & \lambda_c^2 & 1 \end{pmatrix}, \quad |V_{PMNS}| \simeq \begin{pmatrix} 0.79 - 0.86 & 0.50 - 0.61 & 0.0 - 0.2 \\ 0.25 - 0.53 & 0.47 - 0.73 & 0.56 - 0.79 \\ 0.21 - 0.51 & 0.42 - 0.69 & 0.61 - 0.83 \end{pmatrix}_{3\sigma}$$

Hierarchical

Anarchic / Tribimaximal

# Flavor Physics within the SM

- $\mathcal{L}_{Kinetic+Gauge}^{\text{SM}} + \mathcal{L}_{Higgs}^{\text{SM}}$  has a large  $U(3)^5$  global **flavour symmetry**

$$\mathbf{G} = \mathbf{U}(3)^5 = \mathbf{U}(3)_{\mathbf{u}} \otimes \mathbf{U}(3)_{\mathbf{d}} \otimes \mathbf{U}(3)_{\mathbf{Q}} \otimes \mathbf{U}(3)_{\mathbf{e}} \otimes \mathbf{U}(3)_{\mathbf{L}}$$

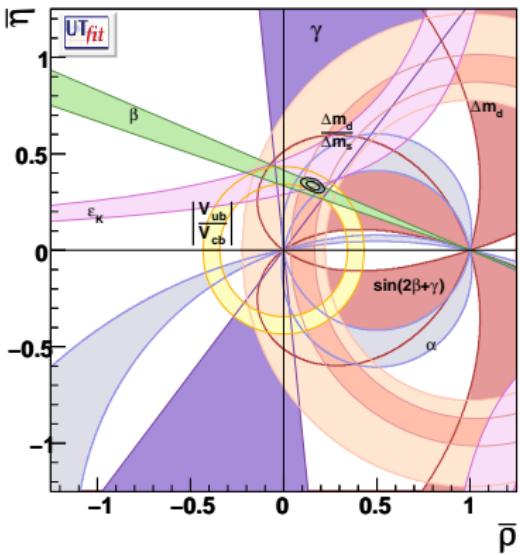
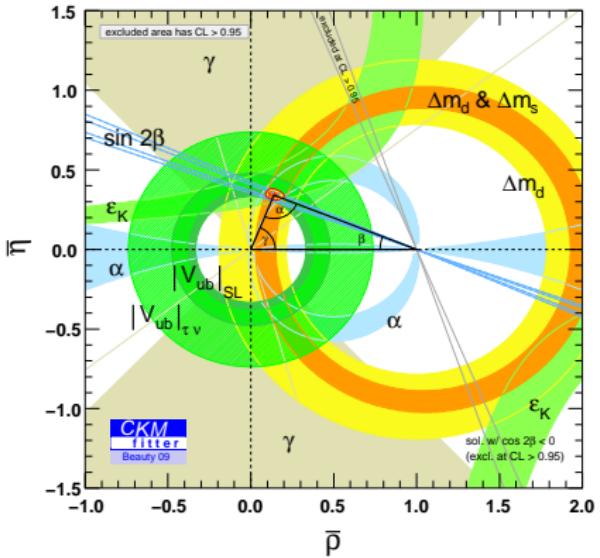
- $\mathcal{L}_{\text{Yukawa}} = \bar{Q}_L \mathbf{Y}_{\mathbf{D}} D_R \phi + \bar{Q}_L \mathbf{Y}_{\mathbf{U}} U_R \tilde{\phi} + \bar{L}_L \mathbf{Y}_{\mathbf{L}} E_R \phi + h.c$  break  $G$  down to

$$\mathbf{G} \rightarrow \mathbf{U}(1)_{\mathbf{B}} \times \mathbf{U}(1)_{\mathbf{e}} \times \mathbf{U}(1)_{\mu} \times \mathbf{U}(1)_{\tau}$$

- **CKM matrix:**  $\mathbf{Y}_{\mathbf{U}} = V_{CKM} \times \text{diag}(y_u, y_c, y_t)$  for  $\mathbf{Y}_{\mathbf{D}} = \text{diag}(y_d, y_s, y_b)$

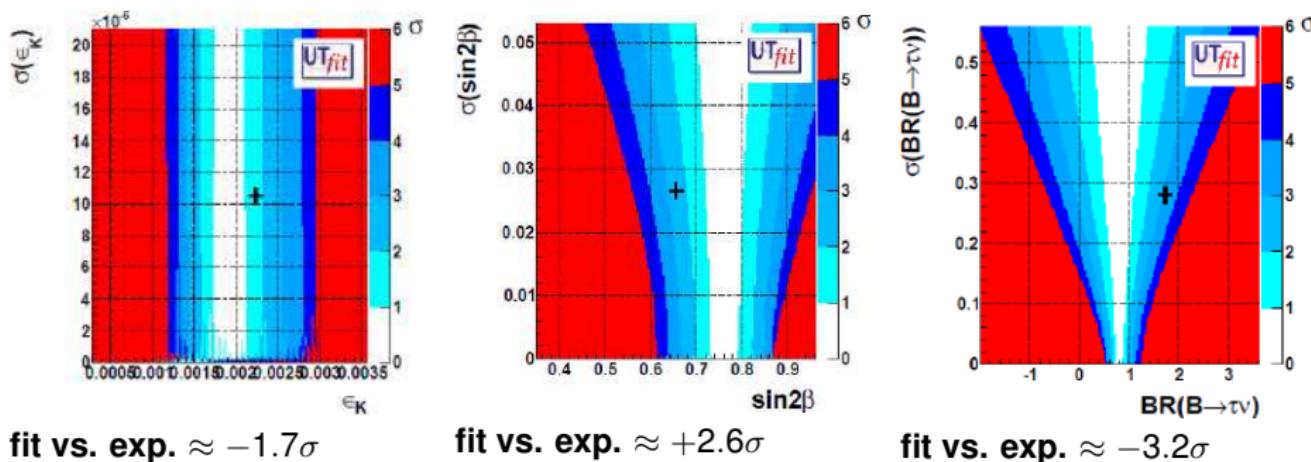
$$V_{CKM} = \begin{pmatrix} V_{ub} & V_{us} & V_{ut} \\ V_{cd} & V_{cs} & V_{cb} \\ V_{ud} & V_{us} & V_{tb} \end{pmatrix} = \begin{pmatrix} n \leftarrow \frac{e^-}{\bar{\nu}} p & K \leftarrow \frac{\ell^-}{\bar{\nu}} \pi & B \leftarrow \frac{\ell^-}{\bar{\nu}} \pi \\ D \leftarrow \frac{\ell^-}{\bar{\nu}} \pi & D \leftarrow \frac{\ell^-}{\bar{\nu}} K & B \leftarrow \frac{\ell^-}{\bar{\nu}} D \\ B^0 \leftarrow \bar{B}^0 & B_s \leftarrow \bar{B}_s & t \leftarrow W b \end{pmatrix}$$

# Messages from the B-factories



**"Very likely, flavour and CP violation in FC processes are dominated by the CKM mechanism" (Nir)**

# UT tensions



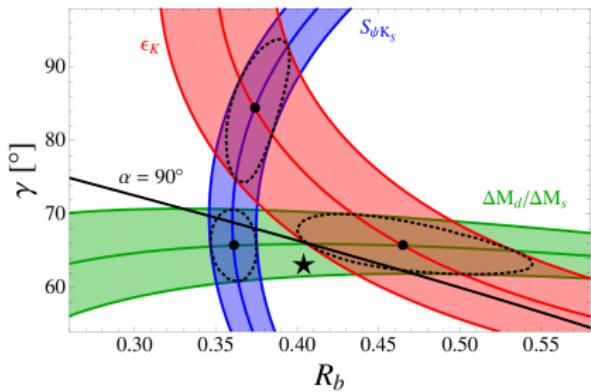
Similar conclusions from the CKMfitter collaboration ('10)

- ① These “UT tension” are interesting but not significant yet.
- ② To monitor the impact of BSM scenarios on the UT analyses.
- ③ To monitor the implications of possible solutions of the “UT tension” in BSM scenarios.

# UT tensions and NP

- “Tensions” in the the UT analysis
- Look at  $\epsilon_K$ ,  $S_{\psi K_S}$ , and  $\Delta M_d/\Delta M_s$  in the  $R_b$ - $\gamma$  plane from tree-level processes

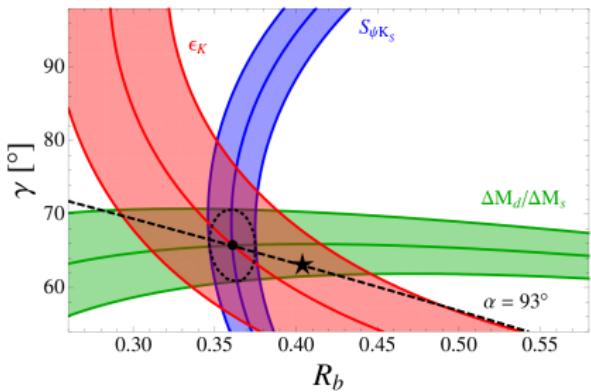
$$R_t = \frac{|V_{td} V_{tb}^*|}{|V_{cd} V_{cb}^*|}$$
$$R_b = \frac{|V_{ud} V_{ub}^*|}{|V_{cd} V_{cb}^*|}$$



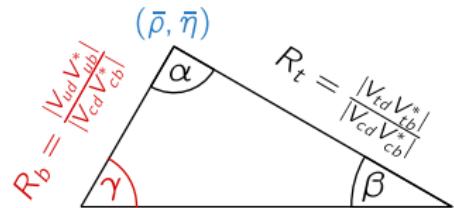
[Altmannshofer, Buras, Gori, P.P, Straub, '09; Buras, Nagai, P.P, '10]

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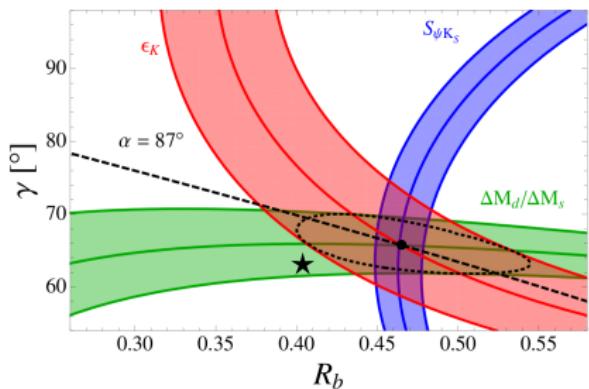
Possible solutions:

- +24% NP effect in  $\epsilon_K$

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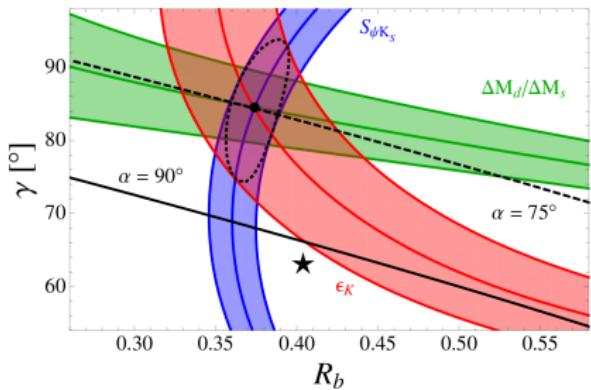
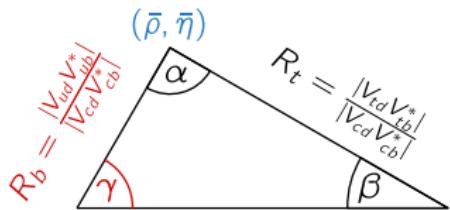
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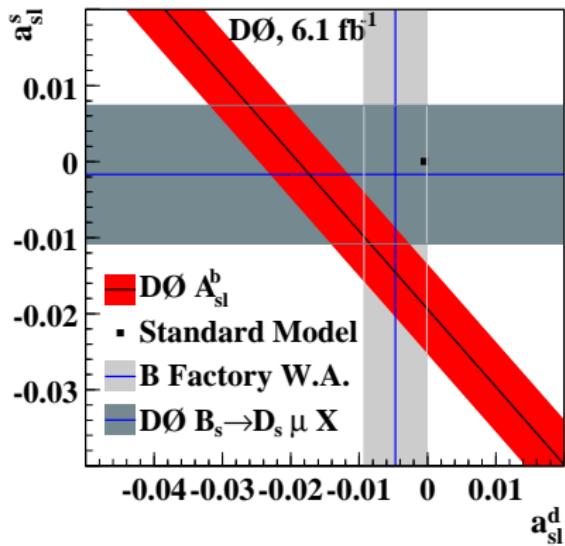


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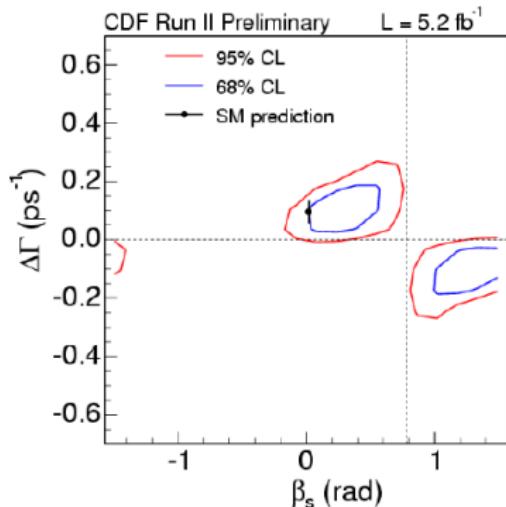
- ① +24% NP effect in  $\epsilon_K$
- ②  $-6.5^\circ$  NP phase in  $B_d$  mixing
- ③ -22% NP effect in  $\Delta M_d/\Delta M_s$

[Altmannshofer, Buras, Gori, P.P, Straub, '09; Buras, Nagai, P.P, '10]

# CPV in $B_s$ mixing



$$A_{\text{SL}}^q \equiv \frac{\Gamma(\bar{B}_q \rightarrow l^+ X) - \Gamma(B_q \rightarrow l^- X)}{\Gamma(\bar{B}_q \rightarrow l^+ X) + \Gamma(B_q \rightarrow l^- X)},$$



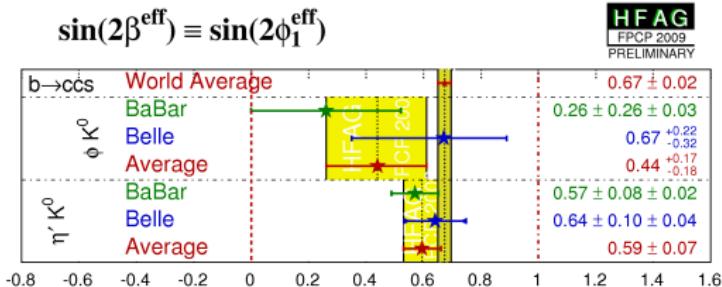
$$S_{\psi\phi} = \sin(2|\beta_s| - 2\phi_{B_s})$$

New Physics in the  $B_s$  mixing phase?

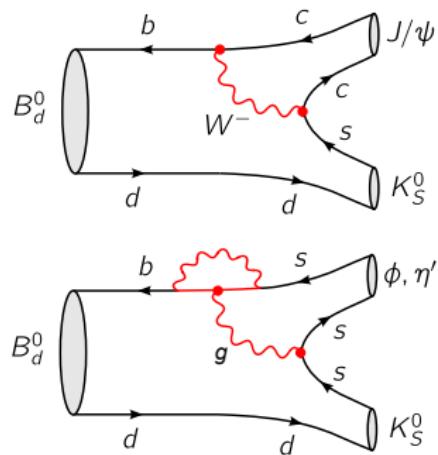
# $\sin 2\beta_{\text{eff}}$ tensions

- In the SM,  $(\sin 2\beta)_{\psi K_S} \approx (\sin 2\beta)_{\phi K_S} \approx (\sin 2\beta)_{\eta' K_S}$
- $B_d \rightarrow \psi K_S$  dominated by tree level,  $\phi K_S$  and  $\eta' K_S$  are loop-induced

Data indicate  $S_{\phi K_S} < S_{\eta' K_S} < S_{\psi K_S}$



[adapted from HFAG]



New physics in the decay amplitudes?

The SuperB will tell us...

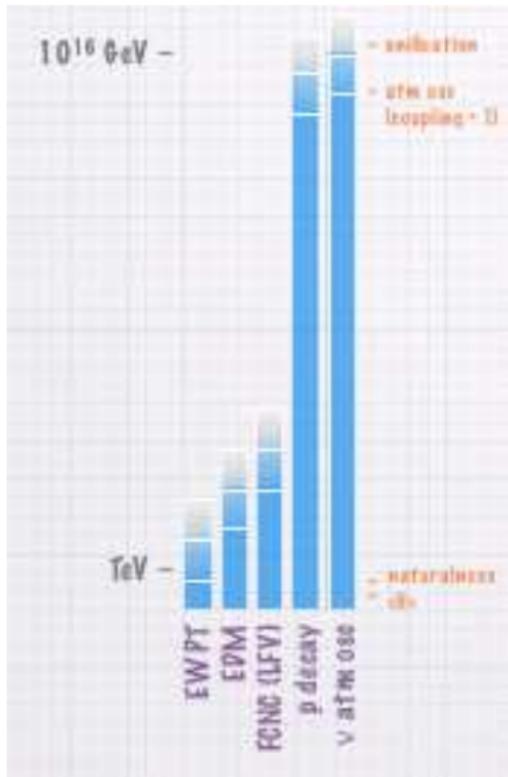
# The NP “scale”

- **Gravity**  $\Rightarrow \Lambda_{\text{Planck}} \sim 10^{18-19} \text{ GeV}$
- **Neutrino masses**  $\Rightarrow \Lambda_{\text{see-saw}} \lesssim 10^{15} \text{ GeV}$
- **BAU**: evidence of CPV beyond SM
  - ▶ Electroweak Baryogenesis  $\Rightarrow \Lambda_{\text{NP}} \lesssim \text{TeV}$
  - ▶ Leptogenesis  $\Rightarrow \Lambda_{\text{see-saw}} \lesssim 10^{15} \text{ GeV}$
- **Hierarchy problem**:  $\Rightarrow \Lambda_{\text{NP}} \lesssim \text{TeV}$
- **Dark Matter**  $\Rightarrow \Lambda_{\text{NP}} \lesssim \text{TeV}$

## SM = effective theory at the EW scale

$$\mathcal{L}_{\text{eff}} = \mathcal{L}_{\text{SM}} + \sum_{d \geq 5} \frac{c_{ij}^{(d)}}{\Lambda_{NP}^{d-4}} O_{ij}^{(d)}$$

- $\mathcal{L}_{\text{eff}}^{d=5} = \frac{y_\nu^{ij}}{\Lambda_{\text{see-saw}}} L_i L_j \phi \phi,$
- $\mathcal{L}_{\text{eff}}^{d=6}$  generates FCNC operators



$$\text{BR}(\ell_i \rightarrow \ell_j \gamma) \sim \frac{1}{\Lambda_{NP}^4}$$

# The NP flavor problem

$$\mathcal{L}_{\text{eff}} = \mathcal{L}_{\text{SM}} + \sum_{d=6} \frac{c_{ij}^{(6)}}{\Lambda_{NP}^2} O_{ij}^{(6)}$$

[Isidori, Nir, Perez '10]

Operator	Bounds on $\Lambda$ (TeV)		Bounds on $c_{ij}$ ( $\Lambda = 1$ TeV)		Observables
	Re	Im	Re	Im	
$(\bar{s}_L \gamma^\mu d_L)^2$	$9.8 \times 10^2$	$1.6 \times 10^4$	$9.0 \times 10^{-7}$	$3.4 \times 10^{-9}$	$\Delta m_K; \varepsilon_K$
$(\bar{s}_R d_L)(\bar{s}_L d_R)$	$1.8 \times 10^4$	$3.2 \times 10^5$	$6.9 \times 10^{-9}$	$2.6 \times 10^{-11}$	$\Delta m_K; \varepsilon_K$
$(\bar{c}_L \gamma^\mu u_L)^2$	$1.2 \times 10^3$	$2.9 \times 10^3$	$5.6 \times 10^{-7}$	$1.0 \times 10^{-7}$	$\Delta m_D;  q/p , \phi_D$
$(\bar{c}_R u_L)(\bar{c}_L u_R)$	$6.2 \times 10^3$	$1.5 \times 10^4$	$5.7 \times 10^{-8}$	$1.1 \times 10^{-8}$	$\Delta m_D;  q/p , \phi_D$
$(\bar{b}_L \gamma^\mu d_L)^2$	$5.1 \times 10^2$	$9.3 \times 10^2$	$3.3 \times 10^{-6}$	$1.0 \times 10^{-6}$	$\Delta m_{B_d}; S_{B_d \rightarrow \psi K}$
$(\bar{b}_R d_L)(\bar{b}_L d_R)$	$1.9 \times 10^3$	$3.6 \times 10^3$	$5.6 \times 10^{-7}$	$1.7 \times 10^{-7}$	$\Delta m_{B_d}; S_{B_d \rightarrow \psi K}$
$(\bar{b}_L \gamma^\mu s_L)^2$	$1.1 \times 10^2$	$1.1 \times 10^2$	$7.6 \times 10^{-5}$	$7.6 \times 10^{-5}$	$\Delta m_{B_s}$
$(\bar{b}_R s_L)(\bar{b}_L s_R)$	$3.7 \times 10^2$	$3.7 \times 10^2$	$1.3 \times 10^{-5}$	$1.3 \times 10^{-5}$	$\Delta m_{B_s}$



**“Generic” flavor violating sources at the TeV scale are excluded**

- SM without Yukawa interactions:  $U(3)^5$  global **flavour symmetry**

$$U(3)_u \otimes U(3)_d \otimes U(3)_q \otimes U(3)_e \otimes U(3)_L$$

- Yukawa interactions break this symmetry
- Proposal for any New Physics model:

**Yukawa structures as the **only** sources of flavour violation**



**Minimal Flavour Violation** [D'Ambrosio et al. '02]

**Notice that MFV allows new “flavour blind”CPV phases!**

[Kagan et al. '09] (model-independent)

[Ellis et al. '07] (SUSY)

[Colangelo et al., '08], [Smith et al. '09] (SUSY)

[Altmannshofer et al., '08,'09], [P.P & Straub, '09] (SUSY)

[Buras et al., '10,'10] (2HDM)

# MFV & the NP flavor problem

$$(c_{\text{MFV}}^{\Delta F=1})_{ij} \sim \textcolor{red}{V_{ti}^* V_{tj}}, \quad (c_{\text{MFV}}^{\Delta F=2})_{ij} \sim (\textcolor{red}{V_{ti}^* V_{tj}})^2$$

$\Delta F = 1, 2$ MFV operators	$\Lambda(\text{TeV})$	Observables
$H^\dagger \left( \overline{D}_R Y^{d\dagger} Y^u Y^{u\dagger} \sigma_{\mu\nu} Q_L \right) (e F_{\mu\nu})$	6.1 TeV	$B \rightarrow X_s \gamma, B \rightarrow X_s \ell^+ \ell^-$
$\frac{1}{2} (\overline{Q}_L Y^u Y^{u\dagger} \gamma_\mu Q_L)^2$	5.9 TeV	$\epsilon_K, \Delta m_{B_d}, \Delta m_{B_s}$
$H_D^\dagger \left( \overline{D}_R Y^{d\dagger} Y^u Y^{u\dagger} \sigma_{\mu\nu} T^a Q_L \right) (g_s G_{\mu\nu}^a)$	3.4 TeV	$B \rightarrow X_s \gamma, B \rightarrow X_s \ell^+ \ell^-$
$(\overline{Q}_L Y^u Y^{u\dagger} \gamma_\mu Q_L) (\overline{E}_R \gamma_\mu E_R)$	2.7 TeV	$B \rightarrow X_s \ell^+ \ell^-, B_s \rightarrow \mu^+ \mu^-$
$(\overline{Q}_L Y^u Y^{u\dagger} \gamma_\mu Q_L) (e D_\mu F_{\mu\nu})$	1.5 TeV	$B \rightarrow X_s \ell^+ \ell^-$

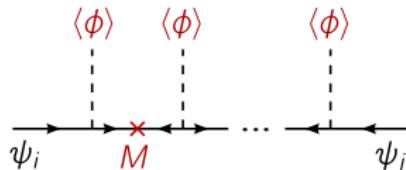
Observable	Experiment	MFV prediction	SM prediction
$A_{CP}(B_s \rightarrow \psi \phi)$	[0.10, 1.44] @ 95% CL	0.04(5)	0.04(2)
$A_{CP}(B \rightarrow X_s \gamma)$	< 6% @ 95% CL	< 0.02	< 0.01
$\mathcal{B}(B_d \rightarrow \mu^+ \mu^-)$	$< 1.8 \times 10^{-8}$	$< 1.2 \times 10^{-9}$	$1.3(3) \times 10^{-10}$
$\mathcal{B}(B \rightarrow X_s \tau^+ \tau^-)$	—	$< 5 \times 10^{-7}$	$1.6(5) \times 10^{-7}$
$\mathcal{B}(K_L \rightarrow \pi^0 \nu \bar{\nu})$	$< 2.6 \times 10^{-8}$ @ 90% CL	$< 2.9 \times 10^{-10}$	$2.9(5) \times 10^{-11}$

[D'Ambrosio et al. '02; Hurth et al. '08, Isidori, Nir & Perez '10]

## SM vs. NP flavor problems

- ① MFV is not a theory of flavour and it has not been probed yet.
- ② Can the SM and NP flavour problems have a common explanation?
- **Froggat-Nielsen '79: Hierarchies from SSB of a Flavour Symmetry**

$$\epsilon = \frac{\langle \phi \rangle}{M} \ll 1 \Rightarrow Y_{ij} \propto e^{(a_i + b_j)}$$



- **Flavor protection from flavor models:** [Lalak, Pokorski & Ross '10]

Operator	$U(1)$	$U(1)^2$	$SU(3)$	MFV
$(\bar{Q}_L X_{LL}^Q Q_L)_{12}$	$\lambda$	$\lambda^5$	$\lambda^3$	$\lambda^5$
$(\bar{D}_R X_{RR}^D D_R)_{12}$	$\lambda$	$\lambda^{11}$	$\lambda^3$	$(y_d y_s) \times \lambda^5$
$(\bar{Q}_L X_{LR}^D D_R)_{12}$	$\lambda^4$	$\lambda^9$	$\lambda^3$	$y_s \times \lambda^5$

- Is this flavor protection enough?
- Is it possible to disentangle among different flavour models by means of their predicted pattern of deviation w.r.t. the SM predictions in flavour physics?

- Why CP violation? Motivation:

- ▶ Baryogenesis requires extra sources of CPV
- ▶ The QCD  $\bar{\theta}$ -term  $\mathcal{L}_{CP} = \bar{\theta} \frac{\alpha_s}{8\pi} G\tilde{G}$  is a CPV source beyond the CKM
- ▶ Most UV completion of the SM, e.g. the MSSM, have many CPV sources
- ▶ However, TeV scale NP with  $\mathcal{O}(1)$  CPV phases generally leads to EDMs many orders of magnitude above the current limits  $\Rightarrow$  the New Physics CP problem.

- How to solve the New Physics CP problem?

- ▶ Decoupling some NP particles in the loop generating the EDMs (e.g. hierarchical sfermions, split SUSY, 2HDM limit...)
- ▶ Generating CPV phases radiatively  $\phi_{CP}^f \sim \alpha_w/4\pi \sim 10^{-3}$
- ▶ Generating CPV phases via small flavour mixing angles  $\phi_{CP}^f \sim \delta_{fj}\delta_{fj}$  with  $f = e, u, d$ : maybe the absence of NP signals in FCNC processes and EDMs have a common origin?

- **High-energy frontier:** A unique effort to determine the NP scale
- **High-intensity frontier (flavor physics):** A collective effort to determine the flavor structure of NP

## Where to look for New Physics at the low energy?

- Processes very suppressed or even forbidden in the SM

- ▶ FCNC processes ( $\mu \rightarrow e\gamma$ ,  $\tau \rightarrow \mu\gamma$ ,  $B_{s,d}^0 \rightarrow \mu^+\mu^-$ ,  $K \rightarrow \pi\nu\bar{\nu}$ )
- ▶ CPV effects in the electron/neutron EDMs,  $d_{e,n}$ ...
- ▶ FCNC & CPV in  $B_{s,d}$  decay/mixing &  $D$  mixing amplitudes

- Processes predicted with high precision in the SM

- ▶ EWPO as  $(g-2)_\mu$ :  $a_\mu^{exp} - a_\mu^{SM} \approx (3 \pm 1) \times 10^{-9}$ , a discrepancy at  $3\sigma$ !
- ▶ LU in  $R_M^{\theta/\mu} = \Gamma(M \rightarrow e\nu)/\Gamma(M \rightarrow \mu\nu)$  with  $M = \pi, K$

# Experimental status

Observable	SM prediction	Theory error	Present result	Future error	Future Facility
$S_{B_s \rightarrow \psi\phi}$	<b>0.036</b>	$\leq 0.01$	$\lesssim  0.2 $	<b>0.01</b>	<b>LHCb</b>
$S_{B_d \rightarrow \phi K}$	$\sin(2\beta)$	$\leq 0.05$	$0.44 \pm 0.18$	0.1	LHCb
$A_{SL}^d$	$-5 \times 10^{-4}$	$10^{-4}$	$-(5.8 \pm 3.4)10^{-3}$	$10^{-3}$	LHCb
$A_{SL}^s$	$2 \times 10^{-5}$	$< 10^{-5}$	$(1.6 \pm 8.5)10^{-3}$	$10^{-3}$	LHCb
$A_{CP}(b \rightarrow s\gamma)$	$< 0.01$	$< 0.01$	$-0.012 \pm 0.028$	0.005	Super- <i>B</i>
$\mathcal{B}(B \rightarrow \tau\nu)$	$1 \times 10^{-4}$	$20\% \rightarrow 5\%$	$(1.73 \pm 0.35)10^{-4}$	5%	Super- <i>B</i>
$\mathcal{B}(B \rightarrow \mu\nu)$	$4 \times 10^{-7}$	$20\% \rightarrow 5\%$	$< 1.3 \times 10^{-6}$	6%	Super- <i>B</i>
$\mathcal{B}(B_s \rightarrow \mu^+ \mu^-)$	$3 \times 10^{-9}$	$20\% \rightarrow 5\%$	$< 1.1 \times 10^{-8}$	10%	<b>LHCb</b>
$\mathcal{B}(B_d \rightarrow \mu^+ \mu^-)$	$1 \times 10^{-10}$	$20\% \rightarrow 5\%$	$< 1.5 \times 10^{-8}$	[?]	<b>LHCb</b>
$B \rightarrow K\nu\bar{\nu}$	$4 \times 10^{-6}$	$20\% \rightarrow 10\%$	$< 1.4 \times 10^{-5}$	20%	Super- <i>B</i>
$ q/p _{D\text{-mixing}}$	1	$< 10^{-3}$	$(0.86^{+0.18}_{-0.15})$	0.03	Super- <i>B</i>
$\phi_D$	0	$< 10^{-3}$	$-(9.6^{+8.3}_{-9.5})^\circ$	$2^\circ$	Super- <i>B</i>
$\mathcal{B}(K^+ \rightarrow \pi^+ \nu\bar{\nu})$	$8.5 \times 10^{-11}$	8%	$(1.73^{+1.15}_{-1.05})10^{-10}$	10%	<i>K</i> factory
$\mathcal{B}(K_L \rightarrow \pi^0 \nu\bar{\nu})$	$2.6 \times 10^{-11}$	10%	$< 2.6 \times 10^{-8}$	[?]	<i>K</i> factory

[Altmannshofer, Buras, Gori, Paradisi, and Straub, '09; Isidori, Nir, and Perez, '10]

**Superstars of 2011-2013 in flavour physics:**  $\mu \rightarrow e\gamma$ ,  $B_s \rightarrow \psi\phi$ ,  $B_{s,d} \rightarrow \mu^+ \mu^-$

Observable	Experiment	SM prediction		
$10^4 \times \text{BR}(B \rightarrow X_s \gamma)$	$3.55 \pm 0.26$	26	$3.15 \pm 0.23$	27
$S_{K^* \gamma}$	$-0.16 \pm 0.22$	26	$(-2.3 \pm 1.6)\%$	31
$10^6 \times \text{BR}(B \rightarrow X_s \ell^+ \ell^-)_{[1,6]}$	$1.63 \pm 0.50$	37, 38	$1.59 \pm 0.11$	42
$10^7 \times \text{BR}(B \rightarrow X_s \ell^+ \ell^-)_{> 14.3}$	$4.3 \pm 1.2$	37, 38	$2.3 \pm 0.7$	10
$10^7 \times \text{BR}(B \rightarrow K^* \ell^+ \ell^-)_{[1,6]}$	$1.71 \pm 0.22$	7, 49, 68	$2.28 \pm 0.63$	
$10^7 \times \text{BR}(B \rightarrow K^* \ell^+ \ell^-)_{[14,18,16]}$	$1.11 \pm 0.13$	7, 49, 68	$1.13 \pm 0.33$	
$10^7 \times \text{BR}(B \rightarrow K^* \ell^+ \ell^-)_{[16,19]}$	$1.35 \pm 0.15$	7, 49, 68	$1.34 \pm 0.51$	
$\langle F_L \rangle (B \rightarrow K^* \ell^+ \ell^-)_{[1,6]}$	$0.61 \pm 0.09$	7, 49, 51	$0.77 \pm 0.04$	
$\langle F_L \rangle (B \rightarrow K^* \ell^+ \ell^-)_{[14,18,16]}$	$0.28 \pm 0.09$	7, 49, 51	$0.37 \pm 0.17$	
$\langle F_L \rangle (B \rightarrow K^* \ell^+ \ell^-)_{[16,19]}$	$0.23 \pm 0.08$	7, 49, 51	$0.34 \pm 0.22$	
$\langle A_{FB} \rangle (B \rightarrow K^* \ell^+ \ell^-)_{[1,6]}$	$-0.04 \pm 0.12$	7, 49, 51	$0.03 \pm 0.02$	
$\langle A_{FB} \rangle (B \rightarrow K^* \ell^+ \ell^-)_{[14,18,16]}$	$-0.50 \pm 0.07$	7, 49, 51	$-0.41 \pm 0.11$	
$\langle A_{FB} \rangle (B \rightarrow K^* \ell^+ \ell^-)_{[16,19]}$	$-0.38 \pm 0.10$	7, 49, 51	$-0.35 \pm 0.11$	
$\langle S_3 \rangle (B \rightarrow K^* \ell^+ \ell^-)_{[1,6]}$	$0.27 \pm 0.56$	51	$(-0.3 \pm 1.1) 10^{-2}$	
$\langle A_9 \rangle (B \rightarrow K^* \ell^+ \ell^-)_{[1,6]}$	$0.09 \pm 0.39$	51	$(1.5 \pm 2.4) 10^{-4}$	

# Experimental status

Process	Present	Future	Experiment
$\text{BR}(\mu \rightarrow e\gamma)$	$1.2 \times 10^{-11}$	$\mathcal{O}(10^{-13})$	MEG, PSI
$\text{BR}(\mu \rightarrow eee)$	$1.1 \times 10^{-12}$	$\mathcal{O}(10^{-14})$	?
$\text{BR}(\mu + \text{Ti} \rightarrow e + \text{Ti})$	$1.1 \times 10^{-12}$	$\mathcal{O}(10^{-18})$	J-PARC
$\text{BR}(\tau \rightarrow e\gamma)$	$1.1 \times 10^{-7}$	$\mathcal{O}(10^{-8})$	SuperB
$\text{BR}(\tau \rightarrow eee)$	$2.7 \times 10^{-7}$	$\mathcal{O}(10^{-9})$	SuperB
$\text{BR}(\tau \rightarrow e\mu\mu)$	$2. \times 10^{-7}$	$\mathcal{O}(10^{-9})$	SuperB
$\text{BR}(\tau \rightarrow \mu\gamma)$	$6.8 \times 10^{-8}$	$\mathcal{O}(10^{-8})$	SuperB
$\text{BR}(\tau \rightarrow \mu\mu\mu)$	$2 \times 10^{-7}$	$\mathcal{O}(10^{-9})$	SuperB, LHCb
$\text{BR}(\tau \rightarrow \mu ee)$	$2.4 \times 10^{-7}$	$\mathcal{O}(10^{-9})$	SuperB
$ d_{Tl}  \text{ [e cm]}$	$< 9.0 \times 10^{-25}$	$\approx 10^{-29}$	Pospelov & Ritz, 2005
$ d_{Hg}  \text{ [e cm]}$	$< 3.1 \times 10^{-29}$	?	?
$ d_h  \text{ [e cm]}$	$< 2.9 \times 10^{-26}$	$\approx 10^{-28}$	PSI, Institute Laue-Langevin

- **Theory:**

$$M_{12}^q = (M_{12}^q)_{\text{SM}} C_{B_q} e^{2i\varphi_{B_q}}, \quad (q = d, s).$$

$$\Delta M_q = 2 |M_{12}^q| = (\Delta M_q)_{\text{SM}} C_{B_q},$$

$$S_{\psi K_S} = \sin(2\beta + 2\varphi_{B_d}),$$

$$S_{\psi \phi} = \sin(2|\beta_s| - 2\varphi_{B_s}),$$

where  $V_{td} = |V_{td}|e^{-i\beta}$  and  $V_{ts} = -|V_{ts}|e^{-i\beta_s}$ . From global CKM fits based only on tree-level observables

$$\sin(2\beta)_{\text{tree}} = 0.775 \pm 0.035,$$

$$\sin(2\beta_s)_{\text{tree}} = 0.038 \pm 0.003.$$

- **Experiments:**

$$S_{\psi K_S}^{\text{exp}} = 0.676 \pm 0.020,$$

$$S_{\psi \phi(t_0)}^{\text{exp}} = -0.03 \pm 0.18.$$

- Theory

$$A_f(t) = S_f \sin(\Delta M t) - C_f \cos(\Delta M t) . \quad (1)$$

In the SM,  $|S_f|$  and  $C_f$  are universal for  $\bar{b} \rightarrow \bar{q}' q' \bar{s}$  ( $q' = c, s, d, u$ ):  
 $-\eta_f S_f \simeq \sin 2\beta$  and  $C_f \simeq 0$  where  $\eta_f = \pm 1$ . NP effects can contribute to

- i) the  $B_d$  mixing amplitude;
- ii) the decay amplitudes  $\bar{b} \rightarrow \bar{q} q \bar{s}$  ( $q = s, d, u$ ).

$$\lambda_f = e^{-2i(\beta + \phi_{B_d})} (\bar{A}_f / A_f) , \quad (2)$$

$\phi_{B_d} \equiv$  NP phase of  $B_d$  mixing,  $A_f$  ( $\bar{A}_f$ ) is the decay amplitude for  $B_d(\bar{B}_d) \rightarrow f$ .

$$A_f = \langle f | \mathcal{H}_{\text{eff}} | B_d \rangle , \quad \bar{A}_f = \langle f | \mathcal{H}_{\text{eff}} | \bar{B}_d \rangle , \quad (3)$$

$$S_f = \frac{2\text{Im}(\lambda_f)}{1 + |\lambda_f|^2} , \quad C_f = \frac{1 - |\lambda_f|^2}{1 + |\lambda_f|^2} . \quad (4)$$

$$A_f = A_f^c \left[ 1 + a_f^u e^{i\gamma} + \sum_i \left( b_{fi}^c + b_{fi}^u e^{i\gamma} \right) \left( C_i^{\text{NP}*}(M_W) + \eta_f \tilde{C}_i^{\text{NP}*}(M_W) \right) \right] , \quad (5)$$

$$B_s \rightarrow \mu^+ \mu^-$$

- Theory

$$\mathcal{H}_{\text{eff}} = -C_S Q_S - C_P Q_P - \tilde{C}_S \tilde{Q}_S - \tilde{C}_P \tilde{Q}_P$$

$$\begin{aligned} Q_S &= m_b (\bar{s} P_R b) (\bar{\ell} \ell) , \quad Q_P = m_b (\bar{s} P_R b) (\bar{\ell} \gamma_5 \ell) \\ \tilde{Q}_S &= m_b (\bar{s} P_L b) (\bar{\ell} \ell) , \quad \tilde{Q}_P = m_b (\bar{s} P_L b) (\bar{\ell} \gamma_5 \ell) \end{aligned}$$

$$\text{BR}(B_s \rightarrow \mu^+ \mu^-) = \frac{\tau_{B_s} F_{B_s}^2 m_{B_s}^3}{32\pi} \sqrt{1 - 4 \frac{m_\mu^2}{m_{B_s}^2}} \left( |B|^2 \left( 1 - 4 \frac{m_\mu^2}{m_{B_s}^2} \right) + |A|^2 \right)$$

$$A = 2 \frac{m_\mu}{m_{B_s}} C_{10}^{\text{SM}} + m_{B_s} (C_P - \tilde{C}_P) , \quad B = m_{B_s} (C_S - \tilde{C}_S)$$

$$C_{10}^{\text{SM}} \approx \frac{g_2^2}{16\pi^2} \frac{4G_F}{\sqrt{2}} V_{tb} V_{ts}^*$$

$$\text{BR}(B_s \rightarrow \mu^+ \mu^-)_{\text{SM}} = (3.60 \pm 0.37) \times 10^{-9}$$

- Experiment

$$\text{BR}(B_s \rightarrow \mu^+ \mu^-)_{\text{exp}} \lesssim 1.1 \times 10^{-8} \quad [\text{LHCb '11}]$$

## $B \rightarrow K^* \ell^+ \ell^-$ observables

Obs.	[46]	[47]	[16]	[48] [50]	[51]	most sensitive to
$F_L$	$-S_2^c$	$F_L$		$F_L$	$F_L$	$C_{7,9,10}^{(t)}$
$A_{FB}$	$\frac{3}{4} S_6^s$	$A_{FB}$	$A_{FB}$	$-A_{FB}$	$-A_{FB}$	$C_7, C_9$
$S_5$	$S_5$					$C_7, C'_7, C_9, C'_{10}$
$S_3$	$S_3$	$\frac{1}{2}(1 - F_L) A_T^{(2)}$			$\frac{1}{2}(1 - F_L) A_T^{(2)}$	$C'_{7,9,10}$
$A_9$	$A_9$		$\frac{2}{3} A_9$		$A_{im}$	$C'_{7,9,10}$
$A_7$	$A_7$		$-\frac{2}{3} A_7^D$			$C_{7,10}^{(t)}$

Table 1: Dictionary between different notations for the  $B \rightarrow K^* \mu^+ \mu^-$  observables and Wilson coefficients they are most sensitive to (the sensitivity to  $C_7^{(t)}$  is only present at low  $q^2$ ).

$$S_i = (I_i + \bar{I}_i) \left/ \frac{d(\Gamma + \bar{\Gamma})}{dq^2} \right., \quad A_i = (I_i - \bar{I}_i) \left/ \frac{d(\Gamma + \bar{\Gamma})}{dq^2} \right..$$

**see references in Altmannshofer, P.P., Straub, '11**

The soft-sector contains a huge number of FV and/or CPV parameters: natural  $O(1)$  values for these parameters are excluded by the exp. data

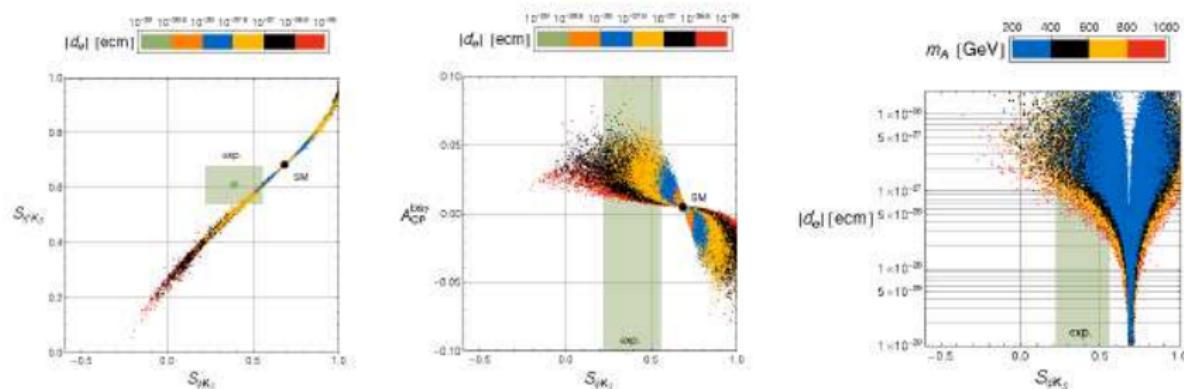
## Flavor problem: solutions

- ① **Decoupling:**  $m_{SUSY} \gg \text{TeV}$ , the hierarchy problem is (partly) reintroduced
- ② **Degeneracy:** sfermion masses nearly degenerate, e.g. gauge mediation, flavour models, MFV...
- ③ **Alignment:** quark and squark mass matrices aligned [Nir & Seiberg '93]

## CP problem: solutions

- ① Degeneracy & Alignment do not solve the CP problem as flavor blind phases are allowed
- ② **CPV from flavor effects**  $\Rightarrow$  EDMs suppressed by small mixing angles
- ③ Hp in flavor models: CP spontaneously broken in the flavor sector by flavon VEVs [Nir & Rattazzi '96]
- ④ Applying the same idea to MFV: CPV only from MFV-compatible terms breaking the flavour blindness [P.P & Straub, '09]

# MSSM with MFV and “flavour blind” phases



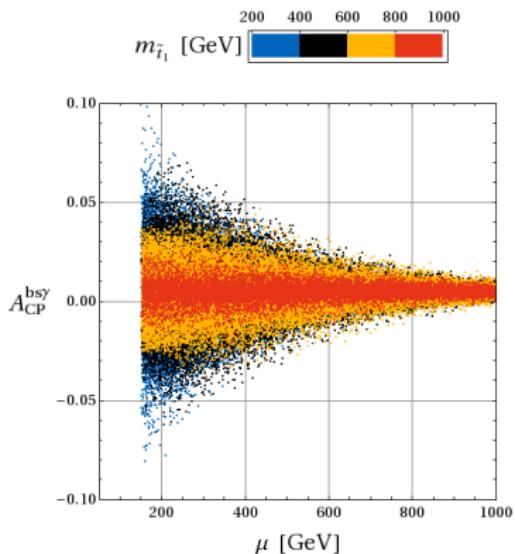
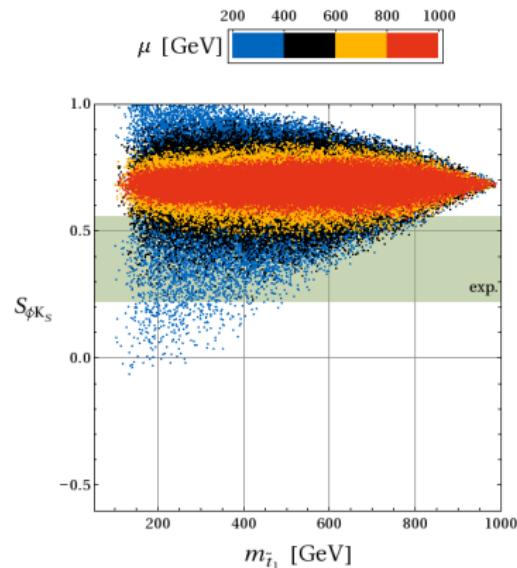
- CP violating  $\Delta F = 0$  and  $\Delta F = 1$  dipole amplitudes can be strongly modified
- $S_{\phi K_S}$  and  $S_{\eta' K_S}$  can simultaneously be brought in agreement with the data
- sizeable and correlated effects in  $A_{CP}^{K^0 \bar{K}^0} \simeq 1\% - 6\%$
- lower bounds on the electron and neutron EDMs at the level of  $d_{e,n} \gtrsim 10^{-26} \text{ e cm}$
- large and correlated effects in the CP asymmetries in  $B \rightarrow K^+ \mu^+ \mu^-$   
(WA, Ball, Bharucha, Buras, Straub, Wick)

- the leading NP contributions to  $\Delta F = 2$  amplitudes are not sensitive to the new phases of the FBMSSM
- CP violation in meson mixing is SM like
- i.e. small effects in  $S_{\psi \phi}$ ,  $S_{\psi K_S}$  and  $\epsilon_K$
- in particular:  $0.03 < S_{\psi \phi} < 0.05$

A combined study of all these observables and their correlations constitutes a very powerful test of the FBMSSM

[Altmannshofer,Buras & P.P., '08]

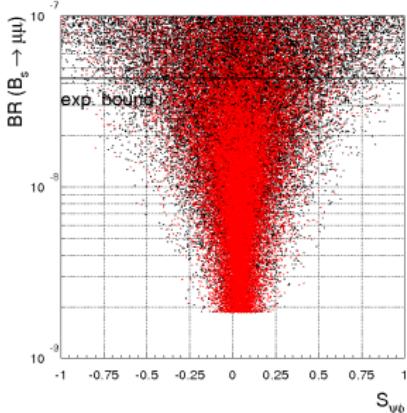
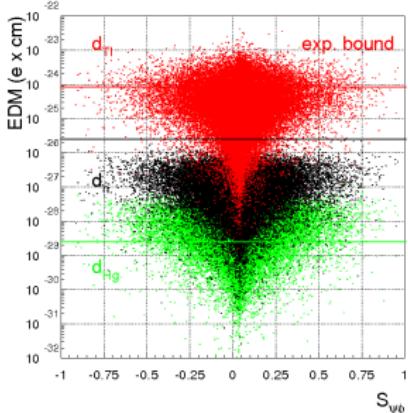
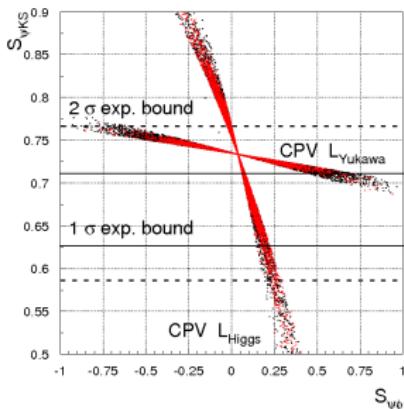
# Implications for direct searches of SUSY particles



- $S_{\phi K_S} \simeq 0.4$  implies  $\mu \lesssim 600$  GeV and  $m_{\tilde{t}_1} \lesssim 700$  GeV
- $A_{CP}^{bs\gamma} \gtrsim 2\%$  implies  $\mu \lesssim 600$  GeV and  $m_{\tilde{t}_1} \lesssim 800$  GeV

[Altmannshofer,Buras& P.P., '08]

## 2HDM with MFV and “flavour blind” phases



- Main messages:

- The “UT tension” is “solved” by a **NP phase in  $B_d$ -mixing** ( $S_{\psi K_S}$ ) implying a **large NP phase in  $B_s$ -mixing** ( $S_{\psi \phi}$ ), in agreement with present data ( $\epsilon_K$  remains SM-like).
- Non-standard** CPV effects in  $B_s$  mixing  $S_{\psi \phi}$  imply **lower bounds for the EDMs** in the experimental reach as well as **non-standard** values for  $\text{BR}(B_{s,d} \rightarrow \mu^+ \mu^-)$ .
- An extended Higgs sector below the TeV** scale is required for such a pattern of deviation from the SM  $\Rightarrow$  the **interplay of LHC** ( $M_H$ ), **LHCb** ( $S_{\psi \phi}, B_{s,d} \rightarrow \mu^+ \mu^-$ ), and **EDMs experiments** ( $d_n, d_{Tl}, d_{Hg}$ ) will probe or falsify the scenario.

[Buras, Isidori & P.P., '10]

## Abelian vs. Non-abelian flavor models

- Non-abelian models predict  $\approx$  degenerate 1st & 2nd sfermion masses
  - ▶ Suppressed contributions to  $1 \leftrightarrow 2$  transitions
  - ▶ Potentially large contributions to  $2 \leftrightarrow 3$  transitions
- In abelian models, sfermions of different generations need not be degenerate
  - ▶ A single  $U(1)$  &  $O(1)$  1-2 mass splitting lead to  $(\delta_{d,u}^{LL})_{12} \sim \mathcal{O}(\lambda)$
  - ▶  $U(1) \times U(1)$  allows *alignement* in the down sector  $(\delta_d^{LL})_{12} \approx 0 \Rightarrow (\delta_u^{LL})_{12} \sim \mathcal{O}(\lambda)$
  - ▶ Large effects in  $D^0$ - $\bar{D}^0$  mixing and neutron EDM

## Chirality structure of flavour violating terms

- Different flavour symmetries lead to different patterns of flavour violation
- Mass insertions:  $M_{\tilde{d}}^2 = \text{diag}(\tilde{m}^2) + \tilde{m}^2 \begin{pmatrix} \delta_d^{LL} & \delta_d^{LR} \\ \delta_d^{RL} & \delta_d^{RR} \end{pmatrix}$
- $\delta^{LL}, \delta^{RR}, \delta^{LR}$  fixed by the flavour symmetry up to  $O(1)$  factors

# Representative flavour models

Representative (non-) abelian flavour models (not just 4 examples...!)

AC model  $U(1)$   
[Agashe, Carone]

Large,  $O(1)$  RR  
mass insertions

AKM model  $SU(3)$   
[Antusch, King, Malinsky]

Only CKM-like RR  
mass insertions

RVV model  $SU(3)$   
[Ross, Velasco-S., Vives]

CKM-like LL & RR  
mass insertions

$\delta$ LL model  $(S_3)^3$   
[e.g. Hall, Murayama]

Only CKM-like LL  
mass insertions

$$\delta_d^{LL} \sim \begin{pmatrix} \cdot & 0 & 0 \\ 0 & \cdot & \lambda^2 \\ 0 & \lambda^2 & \cdot \end{pmatrix} \quad \delta_d^{RR} \sim \begin{pmatrix} \cdot & 0 & 0 \\ 0 & \cdot & 0 \\ 0 & 0 & \cdot \end{pmatrix}$$

$$\delta_d^{LL} \sim \begin{pmatrix} \cdot & \lambda^3 & \lambda^2 \\ \lambda^3 & \cdot & \lambda \\ \lambda^2 & \lambda & \cdot \end{pmatrix} \quad \delta_d^{RR} \sim \begin{pmatrix} \cdot & \lambda^5 & \lambda^3 \\ \lambda^5 & \cdot & \lambda^2 \\ \lambda^3 & \lambda^2 & \cdot \end{pmatrix}$$

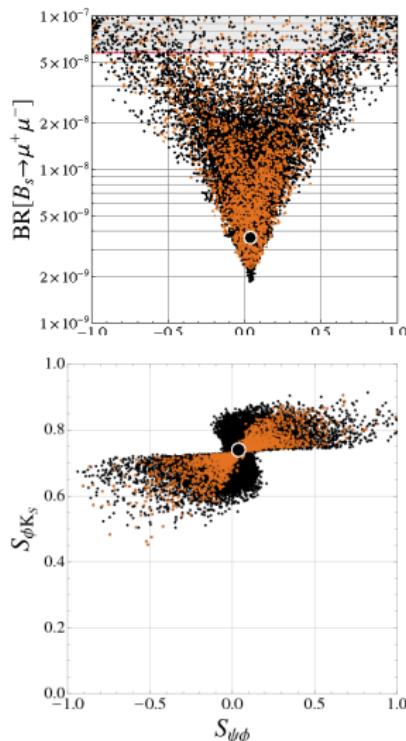
$$\delta_d^{RR} \sim \begin{pmatrix} \cdot & 0 & 0 \\ 0 & \cdot & 1 \\ 0 & 1 & \cdot \end{pmatrix} \quad \delta_d^{RR} \sim \begin{pmatrix} \cdot & \lambda^3 & \lambda^3 \\ \lambda^3 & \cdot & \lambda^2 \\ \lambda^3 & \lambda^2 & \cdot \end{pmatrix} \quad \delta_d^{RR} \sim \begin{pmatrix} \cdot & \lambda^3 & \lambda^2 \\ \lambda^3 & \cdot & \lambda \\ \lambda^2 & \lambda & \cdot \end{pmatrix} \quad \delta_d^{RR} \sim \begin{pmatrix} \cdot & 0 & 0 \\ 0 & \cdot & 0 \\ 0 & 0 & \cdot \end{pmatrix}$$

Hp: CP is spontaneously broken in the flavor sector [Nir & Rattazzi '96]

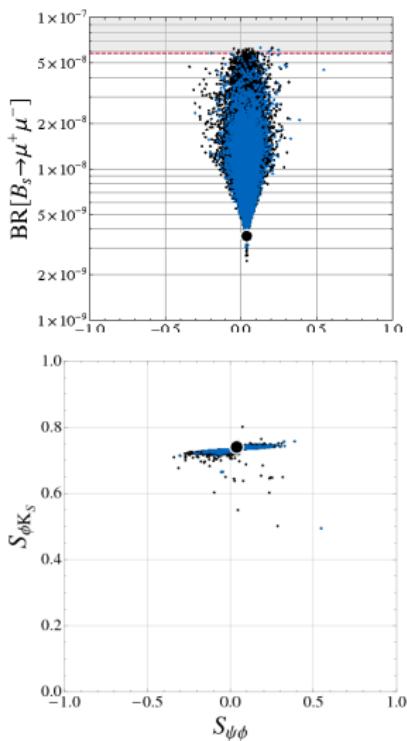
# $b \rightarrow s$ transitions & SUSY flavor models

[Altmannshofer et al., '09]

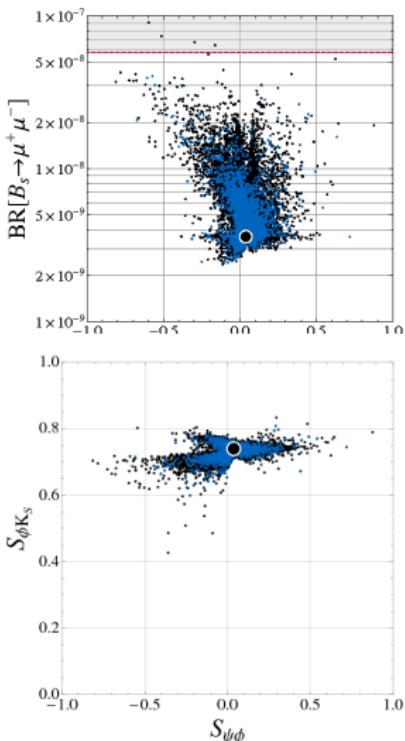
AC



AKM



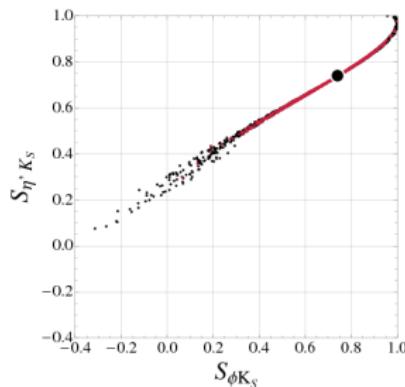
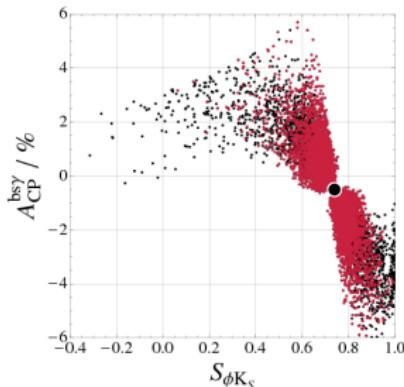
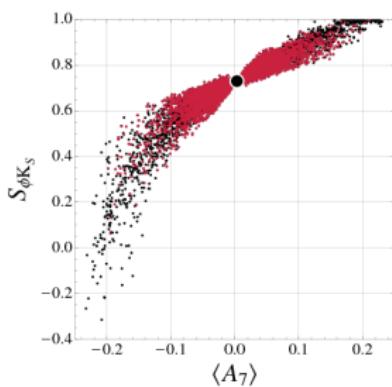
RVV



- Orange (Blue) points: UT tension solved through contribution to  $\Delta M_d / \Delta M_s$  ( $\epsilon_K$ )
- Scan ranges:  $m_0 < 2 \text{ TeV}$ ,  $M_{1/2} < 1 \text{ TeV}$ ,  $|A_0| < 3m_0$ ,  $5 < \tan \beta < 55$

Pattern of NP effects in the  $\delta\text{LL}$  model:

- No large effects in  $S_{\psi\phi}$
- Large, correlated effects in  $S_{\phi K_S}$ ,  $S_{\eta' K_S}$ ,  $A_{\text{CP}}(b \rightarrow s\gamma)$ ,  $\langle A_{7,8} \rangle$  and EDMs
- $\langle A_{7,8} \rangle$ : T-odd CP asymmetries in  $B \rightarrow K^* \ell^+ \ell^-$

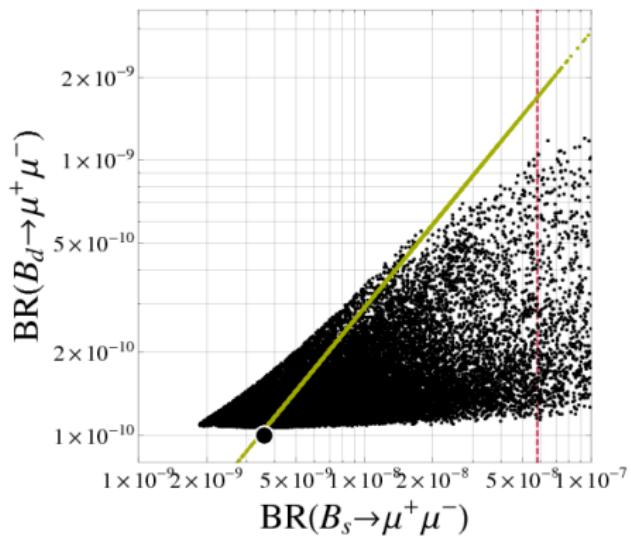


- Scan ranges:  $m_0 < 2 \text{ TeV}$ ,  $M_{1/2} < 1 \text{ TeV}$ ,  $|A_0| < 3m_0$ ,  $5 < \tan \beta < 55$ ,

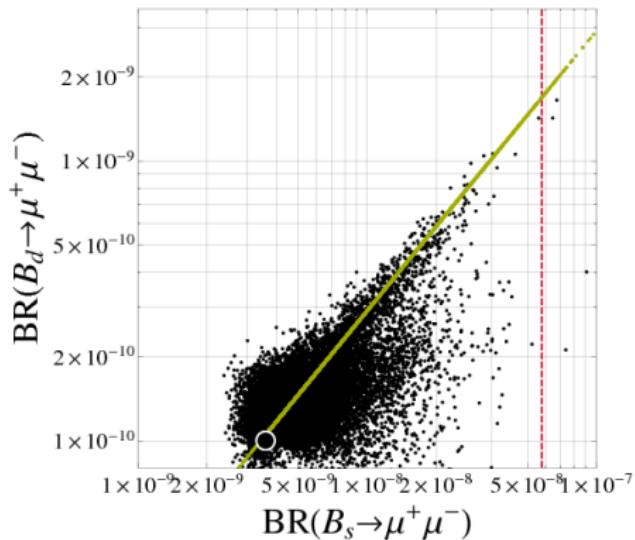
[Altmannshofer et al., '09]

# $Br(B_s \rightarrow \mu^+ \mu^-)$ vs. $Br(B_d \rightarrow \mu^+ \mu^-)$

**Abelian (AC)**



**Non abelian (RVV)**

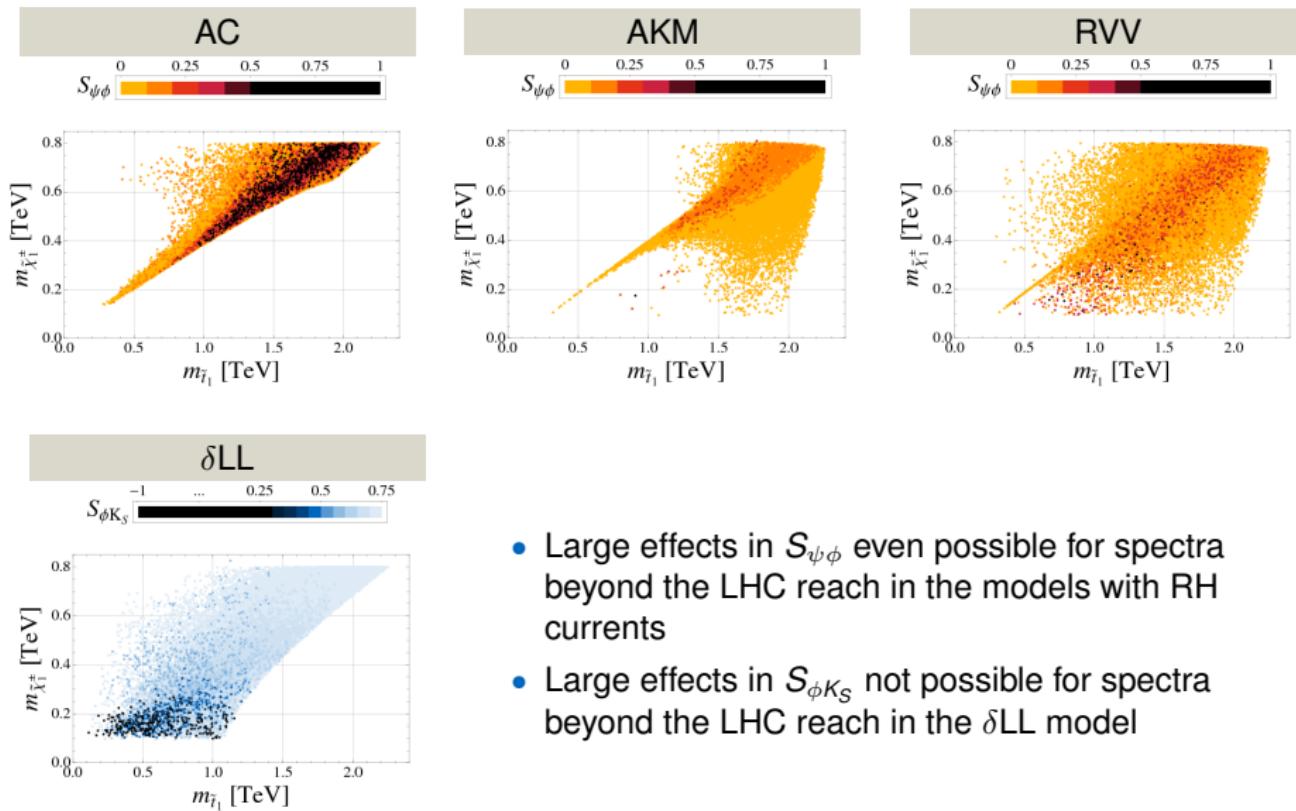


[Altmannshofer et al., '09]

$$Br(B_s \rightarrow \mu^+ \mu^-)/Br(B_d \rightarrow \mu^+ \mu^-) = |V_{ts}/V_{td}|^2 \text{ in MFV models}$$

[Hurth, Isidori, Kamenik & Mescia, '08]

# LHC vs. flavour



- Large effects in  $S_{\psi\phi}$  even possible for spectra beyond the LHC reach in the models with RH currents
- Large effects in  $S_{\phi K_S}$  not possible for spectra beyond the LHC reach in the  $\delta LL$  model

[Altmannshofer, Buras, Gori, P.P. and Straub, '09]

- **Neutrino Oscillation**  $\Rightarrow m_{\nu_i} \neq m_{\nu_j} \Rightarrow \text{LFV}$
- **see-saw**:  $m_\nu = \frac{(m_\nu^D)^2}{M_R} \sim eV$ ,  $M_R \sim 10^{14-16} \Rightarrow m_\nu^D \sim m_{top}$
- **LFV** transitions like  $\mu \rightarrow e\gamma$  @ 1 loop with exchange of
  - ▶  $W$  and  $\nu$  in the **SM** framework (**GIM**) with  $\Lambda_{NP} \equiv M_R$

$$Br(\mu \rightarrow e\gamma) \sim \frac{m_\nu^D{}^4}{M_R^4} \leq 10^{-50}$$

- ▶  $\tilde{W}$  and  $\tilde{\nu}$  in the **MSSM** framework (**SUPER-GIM**) with  $\Lambda_{NP} \equiv \tilde{m}$

$$Br(\mu \rightarrow e\gamma) \sim \frac{m_\nu^D{}^4}{\tilde{m}^4} \leq 10^{-11}$$



- **LFV** signals are undetectable (**detectable**) in the **SM** (**MSSM**)

## RG induced Quark & Lepton FV interactions in SUSY GUTs

- **SUSY SU(5)** [Barbieri & Hall, '95]

$$(\delta_{LL}^{\tilde{q}})_{ij} \sim h^u h^{u\dagger}_{\phantom{u}ij} \sim h_t^2 V_{CKM}^{ik} V_{CKM}^{kj*} \rightarrow (\delta_{RR}^{\tilde{e}})_{ij} \simeq (\delta_{LL}^{\tilde{q}})_{ij}$$

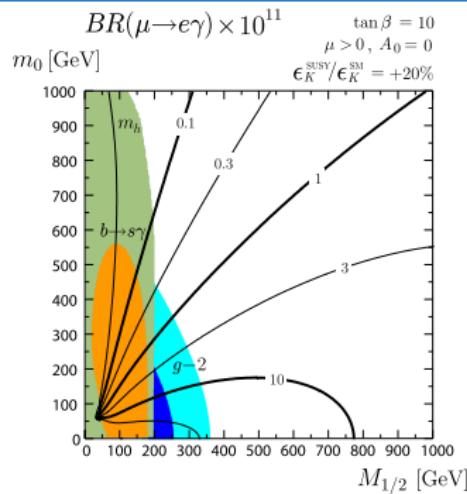
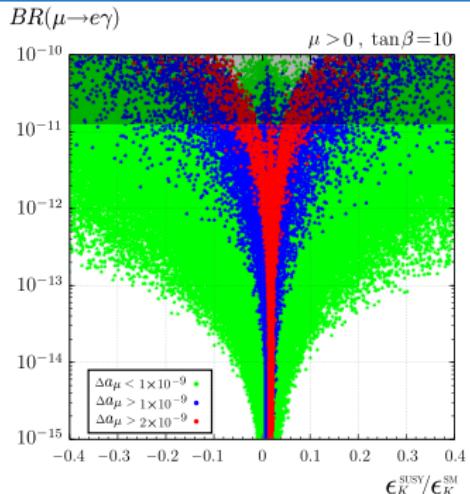
- **SUSY SU(5)+RN** [Yanagida et al., '95]

$$(\delta_{LL}^{\tilde{e}})_{ij} \sim (h^\nu h^{\nu\dagger})_{ij} \quad \& \quad (\delta_{RR}^{\tilde{e}})_{ij} \sim (h^u h^{u\dagger})_{ij}$$

- **SUSY SU(5)+RN** [Moroi, '00] & **SO(10)** [Chang, Masiero & Murayama, '02]

$$\sin \theta_{\mu\tau} \sim \frac{\sqrt{2}}{2} \Rightarrow (\delta_{LL}^{\tilde{e}})_{23} \sim 1 \Rightarrow (\delta_{RR}^{\tilde{q}})_{23} \sim 1$$

# Quark-Lepton correlations in SUSY SU(5)+RN

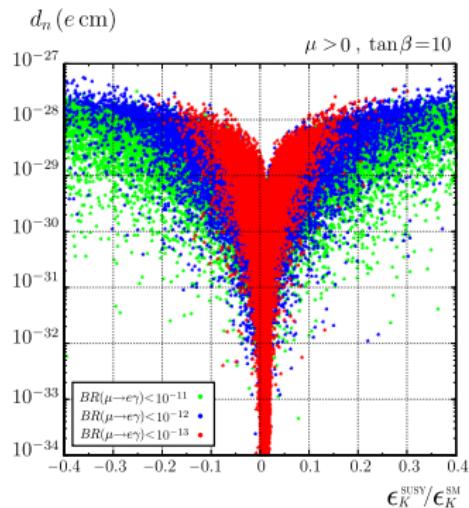
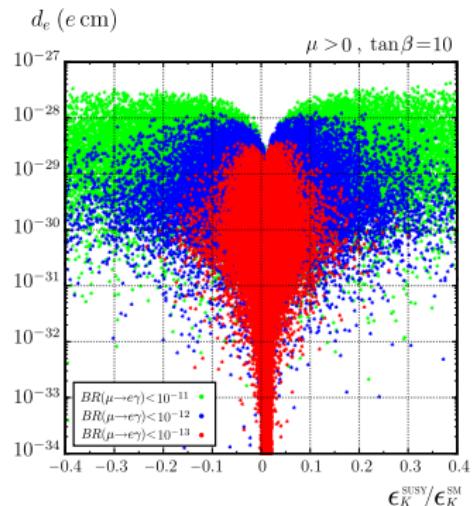


- Main messages:

- Parameter scan:  $(m_0, M_{1/2}) < 1 \text{ TeV}, |A_0| < 3m_0, \tan\beta = 10$  and  $\mu > 0$ .  
Hierarchical  $\nu_L$  &  $N_R$ ,  $10^{11} \leq M_{\nu_3}(\text{GeV}) \leq 10^{15}$  and  $10^{-5} \leq U_{e3} \leq 0.1$ .
- The “**UT tension**” is “solved” through SUSY effects in  $\epsilon_K$  implying a **lower bound** for  $BR(\mu \rightarrow e\gamma)$  in the reach of MEG.
- A simultaneous explanation for both the  $(g-2)_\mu$  and the **UT anomalies** implies  $BR(\mu \rightarrow e\gamma) \geq 10^{-12}$  and SUSY particles in the LHC reach.

[Buras, Nagai & P.P., '10]

# Quark-Lepton correlations in SUSY SU(5)+RN

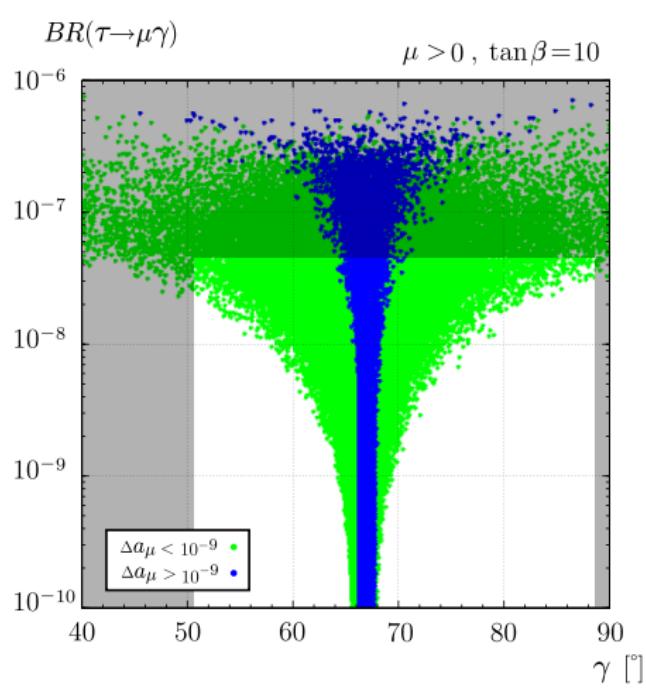
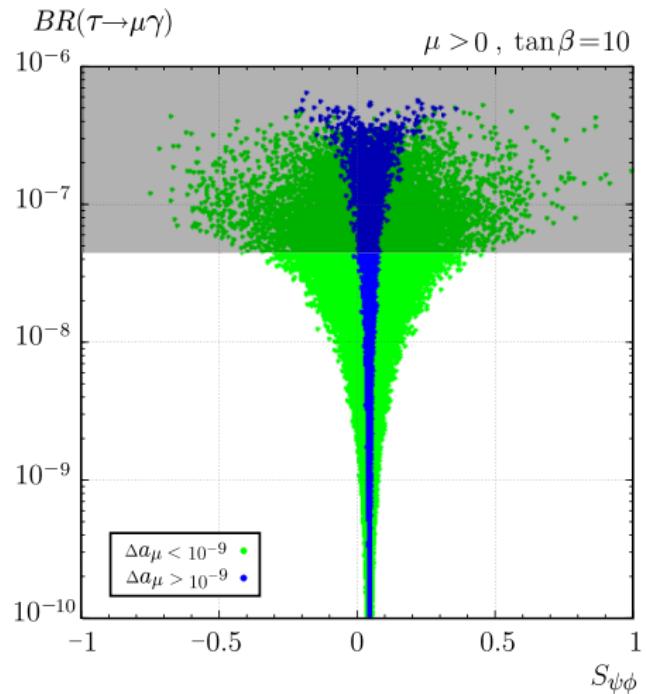


- Main messages:

- Parameter scan:  $(m_0, M_{1/2}) < 1 \text{ TeV}$ ,  $|A_0| < 3m_0$ ,  $\tan\beta = 10$  and  $\mu > 0$ .  
Hierarchical  $\nu_L$  &  $N_R$ ,  $10^{11} \leq M_{\nu_3}(\text{GeV}) \leq 10^{15}$  and  $10^{-5} \leq U_{e3} \leq 0.1$ .
- Sizable **non-standard** effects in  $\epsilon_K$  always implies large values for the **electron and neutron EDMs**, in the reach of the planned experimental resolutions.

[Buras, Nagai & P.P., '10]

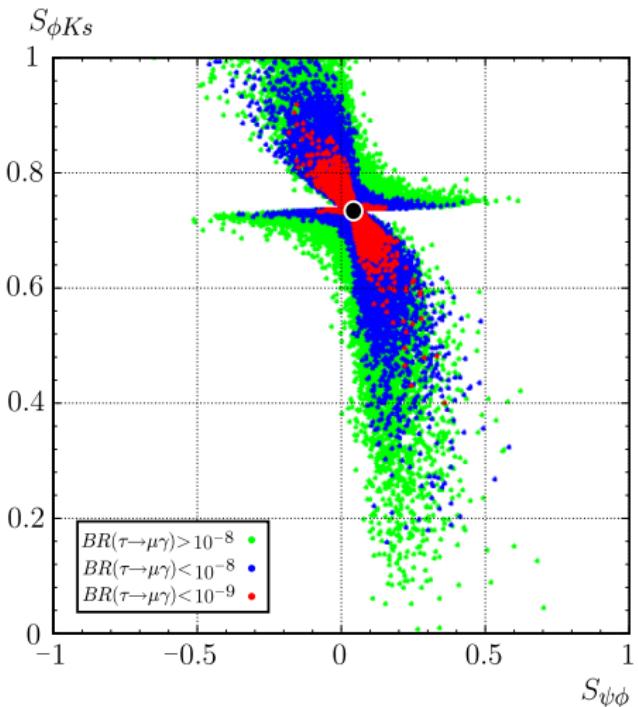
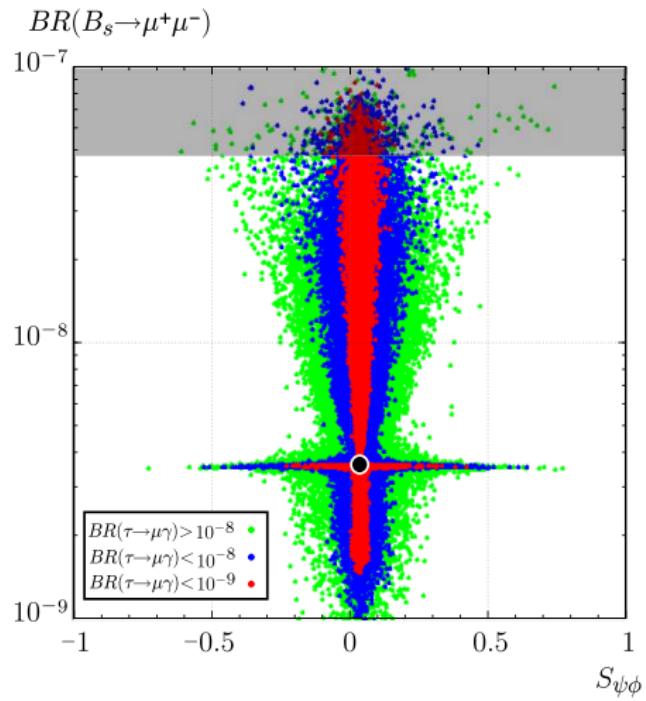
# Quark-Lepton correlations in SUSY SU(5)+RN



**hierarchical  $\nu_L$  and  $N_R$**

[Buras, Nagai & P.P., '10]

# Quark-Lepton correlations in SUSY SU(5)+RN



**hierarchical  $\nu_L$  and  $N_R$**

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## New Physics scenarios

- ① **Real left-handed currents**,  $C_i \in \mathbf{R}$ ,  $C'_i = 0$ . This is realised e.g. in models with MFV in the definition of D'Ambrosio et al., i.e. no CP violation beyond the CKM phase.
- ② **Complex left-handed currents**,  $C_i \in \mathbf{C}$ ,  $C'_i = 0$ . This is realised e.g. in models with MFV and flavour-blind phases.
- ③ **Complex right-handed currents**,  $C'_i \in \mathbf{C}$ ,  $C_i = 0$ .
- ④ **Generic NP**,  $C_i \in \mathbf{C}$ ,  $C'_i \in \mathbf{C}$ .
- ⑤ Models with non-standard Z couplings: only  $C_{9,10}^{(')}$  with  $C_9^{(')} = -(1 - 4s_w^2)C_{10}^{(')}$

$$\chi^2(\vec{C}) = \sum_i \frac{\left(O_i^{\text{exp}} - O_i^{\text{th}}(\vec{C})\right)^2}{(\sigma_i^{\text{exp}})^2 + (\sigma_i^{\text{th}}(\vec{C}))^2}.$$

Altmannshofer, P.P., Straub, '11

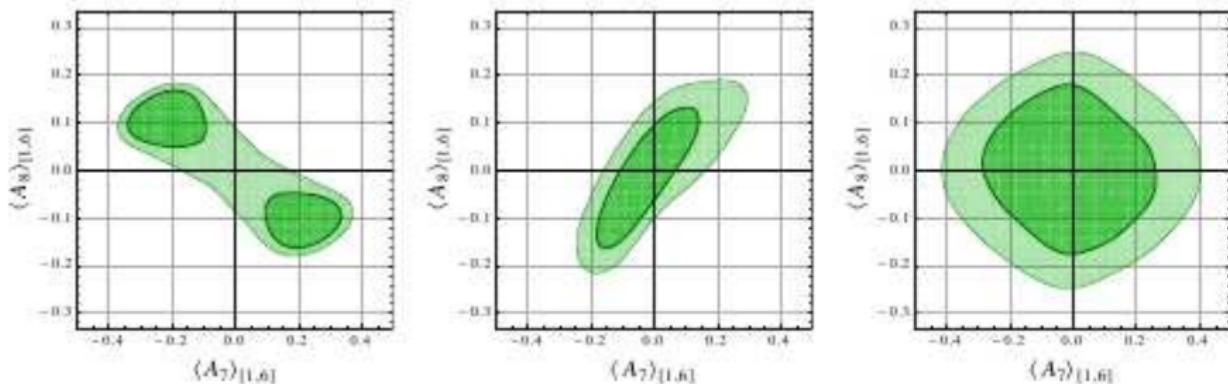


Figure 7: Fit predictions for the low- $q^2$  CP asymmetries  $\langle A_{7,8} \rangle$  in  $B \rightarrow K^* \mu^+ \mu^-$  in the case of complex left-handed currents (left), complex right-handed currents (centre) and generic NP (right). Shown are 68% and 95% C.L. regions.

**Altmannshofer, P.P., Straub, '11**

# $B \rightarrow K^* \ell^+ \ell^-$ observables

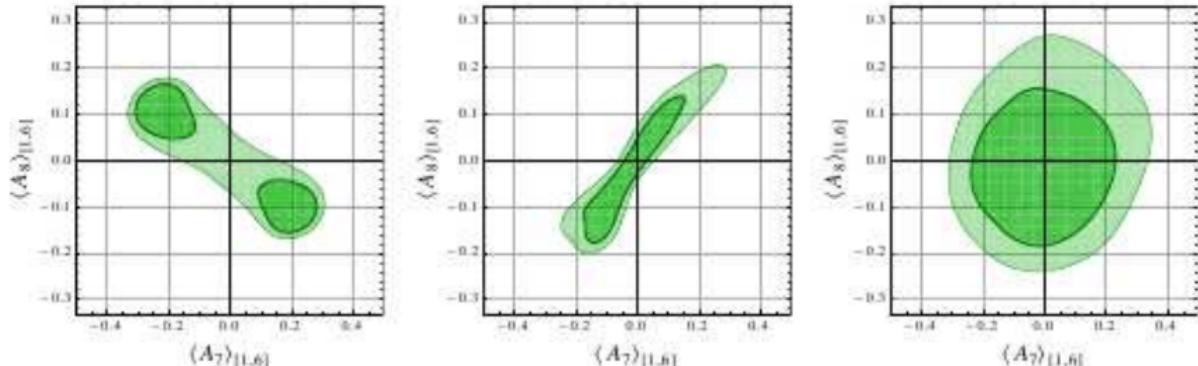


Figure 11: Fit predictions for the low- $q^2$  CP asymmetries  $\langle A_{7,8} \rangle$  in  $B \rightarrow K^* \mu^+ \mu^-$  for the scenario with left-handed (left), right-handed (centre) or generic (right) modified  $Z$  couplings. Shown are 68% and 95% C.L. regions.

**Altmannshofer, P.P., Straub, '11**

# $B \rightarrow K^* \ell^+ \ell^-$ observables

Scenario	$\text{BR}(B_s \rightarrow \mu^+ \mu^-)$	$\text{BR}(B_s \rightarrow \tau^+ \tau^-)$	$ \langle A_7 \rangle_{[1,6]} $	$ \langle A_8 \rangle_{[1,6]} $	$ \langle A_9 \rangle_{[1,6]} $	$\langle S_3 \rangle_{[1,6]}$
Real LH	$[1.0, 5.6] \times 10^{-9}$	$[2, 12] \times 10^{-7}$	0	0	0	0
Complex LH	$[1.0, 5.4] \times 10^{-9}$	$[2, 12] \times 10^{-7}$	$< 0.31$	$< 0.15$	0	0
Complex RH	$< 5.6 \times 10^{-9}$	$< 12 \times 10^{-7}$	$< 0.22$	$< 0.17$	$< 0.12$	$[-0.06, 0.15]$
Generic NP	$< 5.5 \times 10^{-9}$	$< 12 \times 10^{-7}$	$< 0.34$	$< 0.20$	$< 0.15$	$[-0.11, 0.18]$
LH Z peng.	$[1.4, 5.5] \times 10^{-9}$	$[3, 12] \times 10^{-7}$	$< 0.27$	$< 0.14$	0	0
RH Z peng.	$< 3.8 \times 10^{-9}$	$< 8 \times 10^{-7}$	$< 0.22$	$< 0.18$	$< 0.12$	$[-0.03, 0.18]$
Generic Z p.	$< 4.1 \times 10^{-9}$	$< 9 \times 10^{-7}$	$< 0.28$	$< 0.21$	$< 0.13$	$[-0.07, 0.19]$
scalar current	$< 1.1 \times 10^{-8}$	$< 1.3(2.3) \times 10^{-6}$	0	0	0	0

Table 3: Predictions at 95% C.L. for the branching ratios of  $B_s \rightarrow \mu^+ \mu^-$  and  $B_s \rightarrow \tau^+ \tau^-$  and predictions for low- $q^2$  angular observables in  $B \rightarrow K^* \mu^+ \mu^-$  (neglecting tiny SM effects below the percent level) in all the scenarios. The scenarios “Real LH”, “Complex LH”, “Complex RH”, “Generic NP”, “LH Z peng.”, “RH Z peng.”, and “Generic Z p.” correspond to the scenarios discussed in sec. [3.2.1] sec. [3.2.2] sec. [3.2.3] sec. [3.2.4] sec. [4.1.1] sec. [4.1.2] and sec. [4.1.3] respectively, assuming negligible (pseudo)scalar currents. In the scenario “scalar current” only scalar currents are considered. The number quoted for  $B_s \rightarrow \tau^+ \tau^-$  in the “scalar current” scenario refers to the maximum value for its branching ratio in the case of dominant scalar (pseudoscalar) currents.

- **Theory**

$$a_f \equiv \frac{\Gamma(D^0 \rightarrow f) - \Gamma(\bar{D}^0 \rightarrow f)}{\Gamma(D^0 \rightarrow f) + \Gamma(\bar{D}^0 \rightarrow f)}, \quad f = K^+K^-, \pi^+\pi^-$$

SCS decay amplitude  $A_f(\bar{A}_f)$  of  $D^0$  ( $\bar{D}^0$ ) to a CP eigenstate  $f$

$$\begin{aligned} A_f &= A_f^T e^{i\phi_f^T} \left[ 1 + r_f e^{i(\delta_f + \phi_f)} \right], \\ \bar{A}_f &= \eta_{CP} A_f^T e^{-i\phi_f^T} \left[ 1 + r_f e^{i(\delta_f - \phi_f)} \right] \end{aligned}$$

Direct CPV  $\iff r_f \neq 0, \delta \neq 0$  and  $\phi_f \neq 0$

$$a_f^{\text{dir}} \equiv \frac{|A_f|^2 - |\bar{A}_f|^2}{|A_f|^2 + |\bar{A}_f|^2} = -2r_f \sin \delta_f \sin \phi_f$$

- **Experiment**

$$a_{K^+K^-} - a_{\pi^+\pi^-} = -(0.82 \pm 0.21 \pm 0.11) \quad [\text{LHCb '11}]$$

$$\Delta a_{CP} = a_K^{\text{dir}} - a_\pi^{\text{dir}} = -(0.65 \pm 0.18) \quad [\text{LHCb '11, CDF '11, Belle '08 and BaBar '07}]$$

- **Effective Hamiltonian**

$$\mathcal{H}_{|\Delta c|=1}^{\text{eff-NP}} = \frac{G_F}{\sqrt{2}} \sum_i C_i Q_i + \text{h.c.},$$

$$\begin{aligned} Q_8 &= \frac{m_c}{4\pi^2} \bar{u}_L \sigma_{\mu\nu} T^a g_s G_a^{\mu\nu} c_R, \\ \tilde{Q}_8 &= \frac{m_c}{4\pi^2} \bar{u}_R \sigma_{\mu\nu} T^a g_s G_a^{\mu\nu} c_L. \end{aligned}$$

- **Master formula for  $\Delta a_{CP}$ : SM + NP**

$$\begin{aligned} \Delta a_{CP} &\approx \frac{-2}{\sin \theta_c} \left[ \text{Im}(V_{cb}^* V_{ub}) \text{Im}(\Delta R^{\text{SM}}) + \sum_i \text{Im}(C_i^{\text{NP}}) \text{Im}(\Delta R^{\text{NP}_i}) \right] \\ &= -(0.13\%) \text{Im}(\Delta R^{\text{SM}}) - 9 \sum_i \text{Im}(C_i^{\text{NP}}) \text{Im}(\Delta R^{\text{NP}_i}) \end{aligned}$$

$\Delta R^{\text{SM}} \approx \alpha_s(m_c)/\pi \approx 0.1$  in perturbation theory and  $a_K^{\text{dir}} = -a_\pi^{\text{dir}}$  in the  $SU(3)$  limit. In naive factorization

$$|\text{Im}(\Delta R^{\text{NP}_{8,\tilde{8}}})| \approx 0.2$$

- $\Delta a_{CP}$  in SUSY

$$|\Delta a_{CP}^{\text{SUSY}}| \approx 0.6\% \left( \frac{|\text{Im}(\delta_{12}^u)_{LR}^{\text{eff}}|}{10^{-3}} \right) \left( \frac{\text{TeV}}{\tilde{m}} \right) ,$$

- Disoriented  $A$  terms

$$\text{Im}(\delta_{12}^u)_{LR} \approx \frac{\text{Im}(A) \theta_{12} m_c}{\tilde{m}} \approx \left( \frac{\text{Im}(A)}{3} \right) \left( \frac{\theta_{12}}{0.5} \right) \left( \frac{\text{TeV}}{\tilde{m}} \right) \times 10^{-3} ,$$

- Split families:  $m_{\tilde{q}_1,2} \gg m_{\tilde{q}_3}$ ,  $(\delta_{33}^u)_{RL} = A m_t / m_{\tilde{q}_3}$

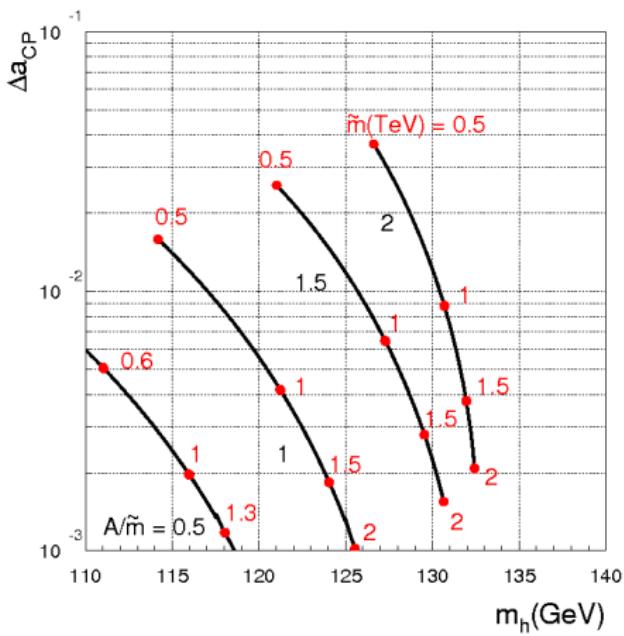
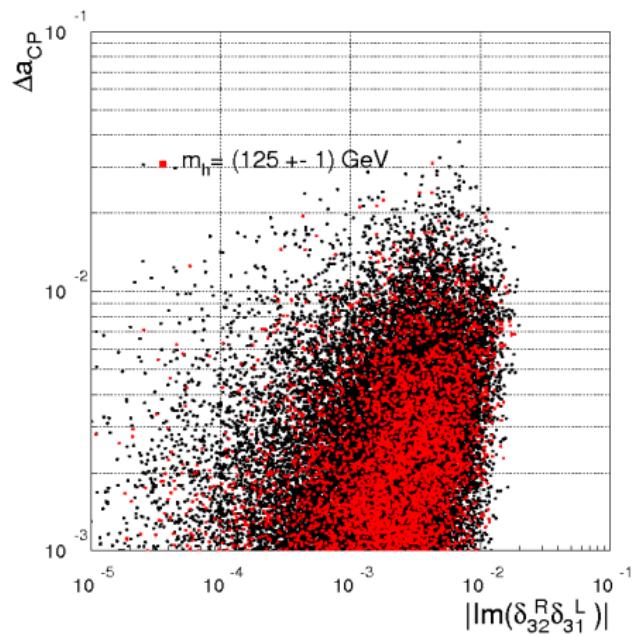
$$(\delta_{12}^u)_{RL}^{\text{eff}} = (\delta_{13}^u)_{RR} (\delta_{33}^u)_{RL} (\delta_{32}^u)_{LL} , \quad (\delta_{12}^u)_{LR}^{\text{eff}} = (\delta_{13}^u)_{LL} (\delta_{33}^u)_{RL} (\delta_{32}^u)_{RR} .$$

$$\begin{aligned} (\delta_{32}^u)_{LL} &= O(\lambda^2), & (\delta_{13}^u)_{RR} &= O(\lambda^2) & \rightarrow & & (\delta_{12}^u)_{RL}^{\text{eff}} &= O(\lambda^4) = O(10^{-3}) , \\ (\delta_{13}^u)_{LL} &= O(\lambda^3), & (\delta_{32}^u)_{RR} &= O(\lambda) & \rightarrow & & (\delta_{12}^u)_{LR}^{\text{eff}} &= O(\lambda^4) = O(10^{-3}) . \end{aligned}$$

[G.F.Giudice, G.Isidori, & P.P, '12]

# $\Delta a_{CP}$ and SUSY

[G.F.Giudice, G.Isidori, & P.P, '12]

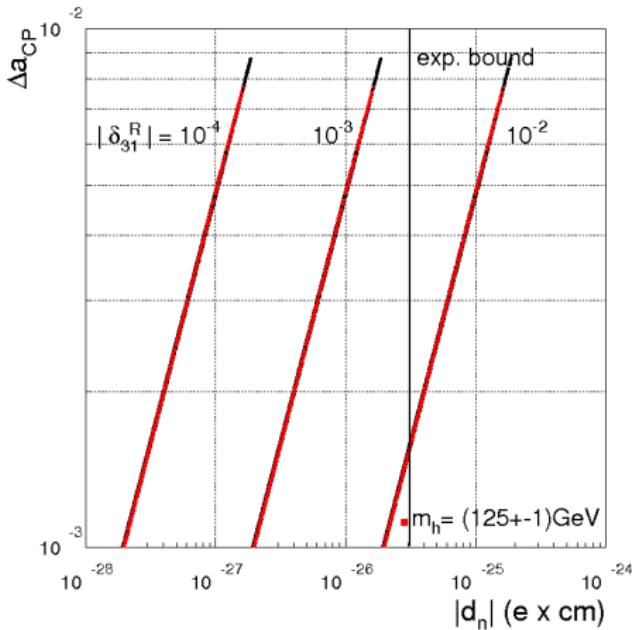
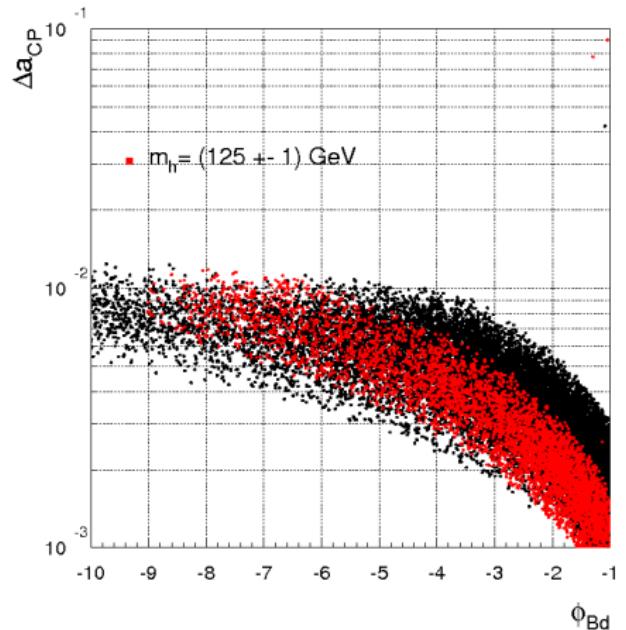


Left:  $0.5 \text{ TeV} \leq \tilde{m}, \tilde{m}_g \leq 2 \text{ TeV}, \tan \beta = 10, |A| \leq 3$ .

Right:  $|Im[(\delta_{32}^u)_{RR}(\delta_{31}^u)_{LL}]| = 10^{-2}, \tilde{m} \leq 2 \text{ TeV}$ , and  $A = 0.5, 1, 1.5, 2$ .

# $\Delta a_{CP}$ and SUSY

[G.F.Giudice, G.Isidori, & P.P, '12]



Left:  $(\delta_{32}^u)_{RR} = 0.2$  and  $\phi_{\delta_{31}^L} \in \pm(30^\circ, 60^\circ)$ ,  $|(\delta_{31}^d)_{LL}| < 0.1$ .  
 Right:  $(\delta_{13}^u)_{LL} = 10^{-2}$ ,  $(\delta_{32}^u)_{RR} = 0.2i$ .

# CPV in D-physics

CPV in  $D^0 - \bar{D}^0$   $\sim \text{Im}((V_{cb} V_{ub}) / (V_{cs} V_{us})) \sim 10^{-3}$  in the SM

- $\langle D^0 | \mathcal{H}_{\text{eff}} | \bar{D}^0 \rangle = M_{12} - \frac{i}{2} \Gamma_{12}, \quad |D_{1,2}\rangle = p|D^0\rangle \pm q|\bar{D}^0\rangle$
- $\frac{q}{p} = \sqrt{\frac{M_{12}^* - \frac{i}{2} \Gamma_{12}^*}{M_{12} + \frac{i}{2} \Gamma_{12}}}, \quad \phi = \text{Arg}(q/p)$
- $x = \frac{\Delta M_D}{\Gamma} = 2\tau \text{Re} \left[ \frac{q}{p} (M_{12} - \frac{i}{2} \Gamma_{12}) \right]$
- $y = \frac{\Delta \Gamma}{2\Gamma} = -2\tau \text{Im} \left[ \frac{q}{p} (M_{12} - \frac{i}{2} \Gamma_{12}) \right]$   
 $\mathbf{S}_f = 2\Delta Y_f = \frac{1}{\Gamma_D} (\hat{\Gamma}_{\bar{D}^0 \rightarrow f} - \hat{\Gamma}_{D^0 \rightarrow f})$
- $\eta_f^{\text{CP}} S_f = x \left( \left| \frac{q}{p} \right| + \left| \frac{p}{q} \right| \right) \sin \phi - y \left( \left| \frac{q}{p} \right| - \left| \frac{p}{q} \right| \right) \cos \phi$
- $\mathbf{a}_{\text{SL}} = \frac{\Gamma(D^0 \rightarrow K^+ \ell^- \nu) - \Gamma(\bar{D}^0 \rightarrow K^- \ell^+ \nu)}{\Gamma(D^0 \rightarrow K^+ \ell^- \nu) + \Gamma(\bar{D}^0 \rightarrow K^- \ell^+ \nu)} = \frac{|q|^4 - |p|^4}{|q|^4 + |p|^4}$

[Nir et al., Kagan et al., Petrov et al., Bigi et al., Buras et al., ...]

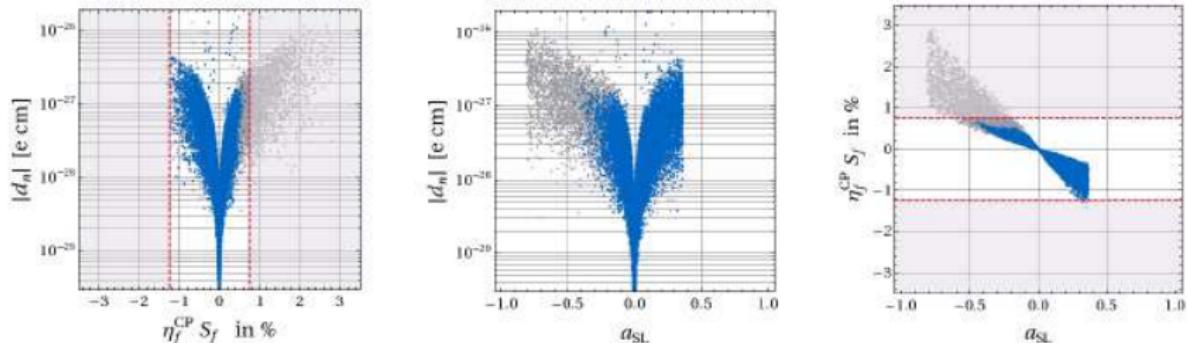


FIG. 3: Correlations between  $d_n$  and  $S_f$  (left),  $d_n$  and  $a_{SL}$  (middle) and  $a_{SL}$  and  $S_f$  (right) in SUSY alignment models. Gray points satisfy the constraints (8)-(10) while blue points further satisfy the constraint (11) from  $\phi$ . Dashed lines stand for the allowed range (18) for  $S_f$ .

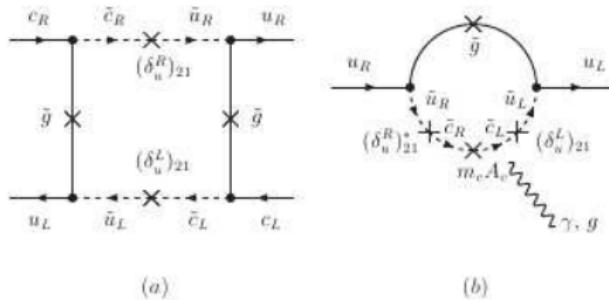


FIG. 2: Examples of relevant Feynman diagrams contributing (a) to  $D^0 - \bar{D}^0$  mixing and (b) to the up quark (C)EDM in SUSY alignment models.

# "DNA-Flavour Test"

	SSU(5)	AC	RVV2	AKM	$\delta LL$	FBMSSM	
$S_{\phi K_S}$	★★★	★★★	●●	■	★★★	★★★	
$A_{CP}(B \rightarrow X_s \gamma)$	■	■	■	■	★★★	★★★	
$B \rightarrow K^{(*)} \nu \bar{\nu}$	■	■	■	■	■	■	
$\tau \rightarrow \mu \gamma$	★★★	★★★	★★★	■	★★★	★★★	
$D^0 - \bar{D}^0$	■	★★★	■	■	■	■	
$A_{7,8}(B \rightarrow K^* \mu^+ \mu^-)$	■	■	■	■	★★★	★★★	vs. 
$A_9(B \rightarrow K^* \mu^+ \mu^-)$	■	■	■	■	■	■	
$S_{\psi \phi}$	★★★	★★★	★★★	★★★	■	■	
$B_s \rightarrow \mu^+ \mu^-$	★★★	★★★	★★★	★★★	★★★	★★★	
$\epsilon_K$	★★★	■	★★★	★★★	■	■	
$K^+ \rightarrow \pi^+ \nu \bar{\nu}$	■	■	■	■	■	■	
$K_L \rightarrow \pi^0 \nu \bar{\nu}$	■	■	■	■	■	■	
$\mu \rightarrow e \gamma$	★★★	★★★	★★★	★★★	★★★	★★★	
$\mu + N \rightarrow e + N$	★★★	★★★	★★★	★★★	★★★	★★★	
$d_n$	★★★	★★★	★★★	★★★	●●	★★★	
$d_e$	★★★	★★★	★★★	●●	■	★★★	
$(g-2)_\mu$	★★★	★★★	★★★	●●	★★★	★★★	

★★★, ●●, ■ = Large, Moderate, Invisible NP effects [Altmannshofer, Buras, Gori, P.P., and Straub, '09]

- **The important questions in view of future experiments are:**
  - ▶ What are the expected deviations from the SM predictions induced by TeV NP?
  - ▶ Which observables are not limited by theoretical uncertainties?
  - ▶ In which case we can expect a substantial improvement on the experimental side?
  - ▶ What will the measurements teach us if deviations from the SM are [not] seen?
- **Our (personal) answers are:**
  - ▶ The expected deviations from the SM predictions induced by NP at the TeV scale with generic flavor structure are already ruled out by many orders of magnitudes.
  - ▶ On general grounds, we can expect any size of deviation below the current bounds.
  - ▶ The theoretical limitations are highly process dependent. Several channels involving leptons in the final state, and selected time-dependent asymmetries, have a theoretical errors well below the current experimental sensitivity.
  - ▶ On the experimental side there are excellent prospects of improvements. One order of magnitude improvements in several clean  $B_{s,d}$ ,  $D$ ,  $K$ , and  $\pi$  (LFU tests in  $\pi_{\ell 2}$ ) observables are possible within a few years. Improvements of several orders of magnitudes are expected in LFV processes ( $\mu \rightarrow e\gamma$ ,  $\mu Ti \rightarrow eTi$ ) and EDM experiments ( $d_n$ ,  $d_{Tl}$ ).

- There is no doubt that new low-energy flavor data will be complementary with the high- $p_T$  part of the LHC program.
- The synergy of both data sets can teach us a lot about the new physics at the TeV scale.