

# Shape coexistence in Sn isotopes around $A=110$

Young GAMMA Meeting - Asiago 2024

Giacomo Corbari

Università degli Studi di Milano - INFN Milano

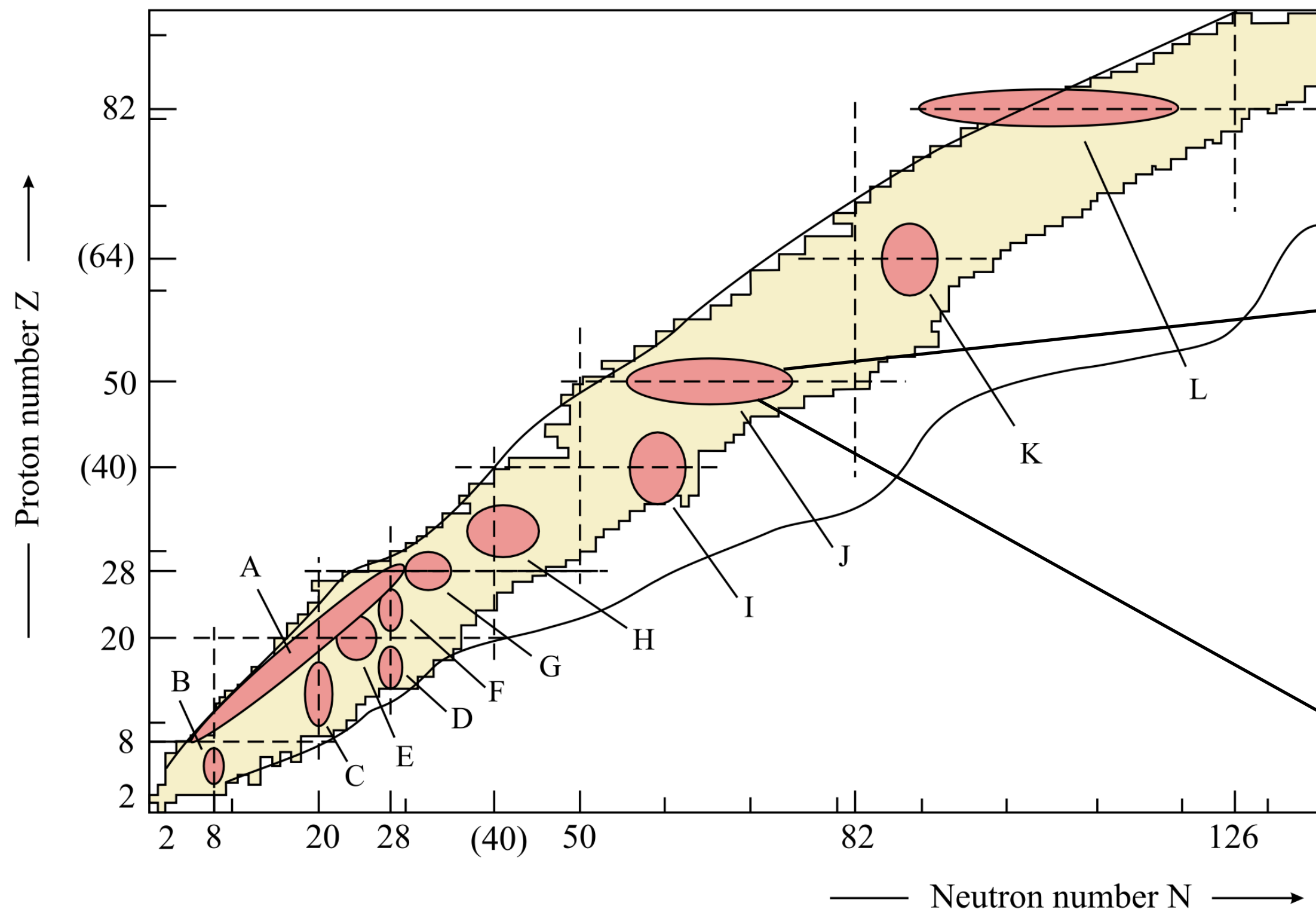


UNIVERSITÀ  
DEGLI STUDI  
DI MILANO

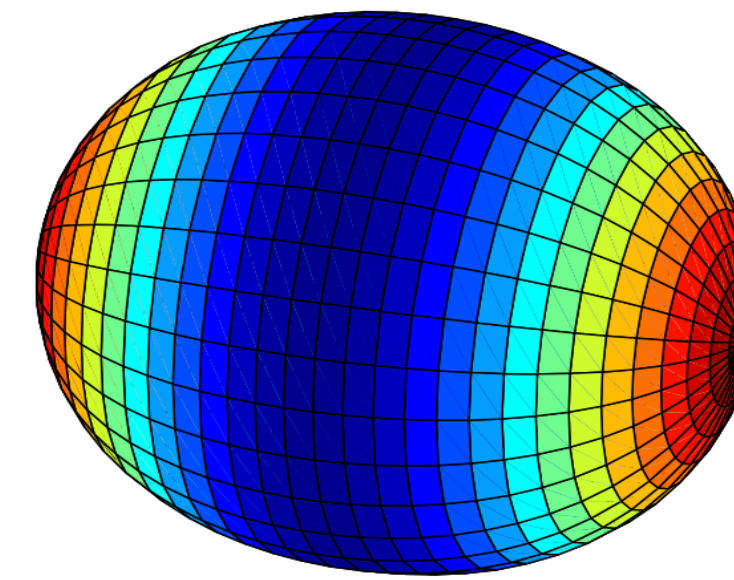


# Shape coexistence

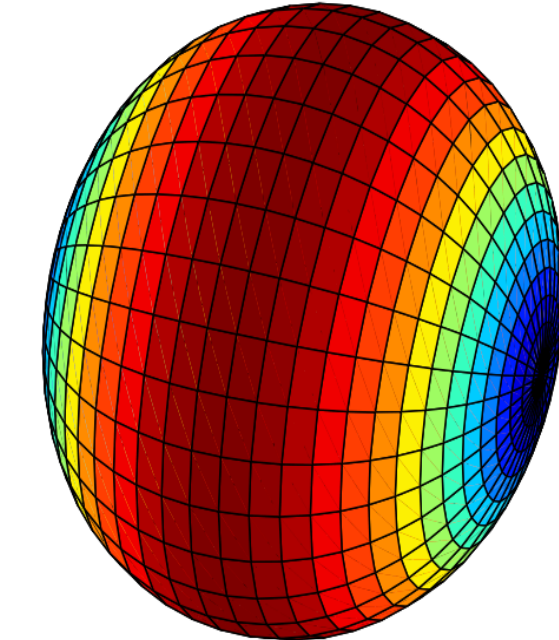
Quadrupole deformations predicted and observed in excited states of nuclei around the  $A \sim 110$  region



Prolate



Oblate



Z=50

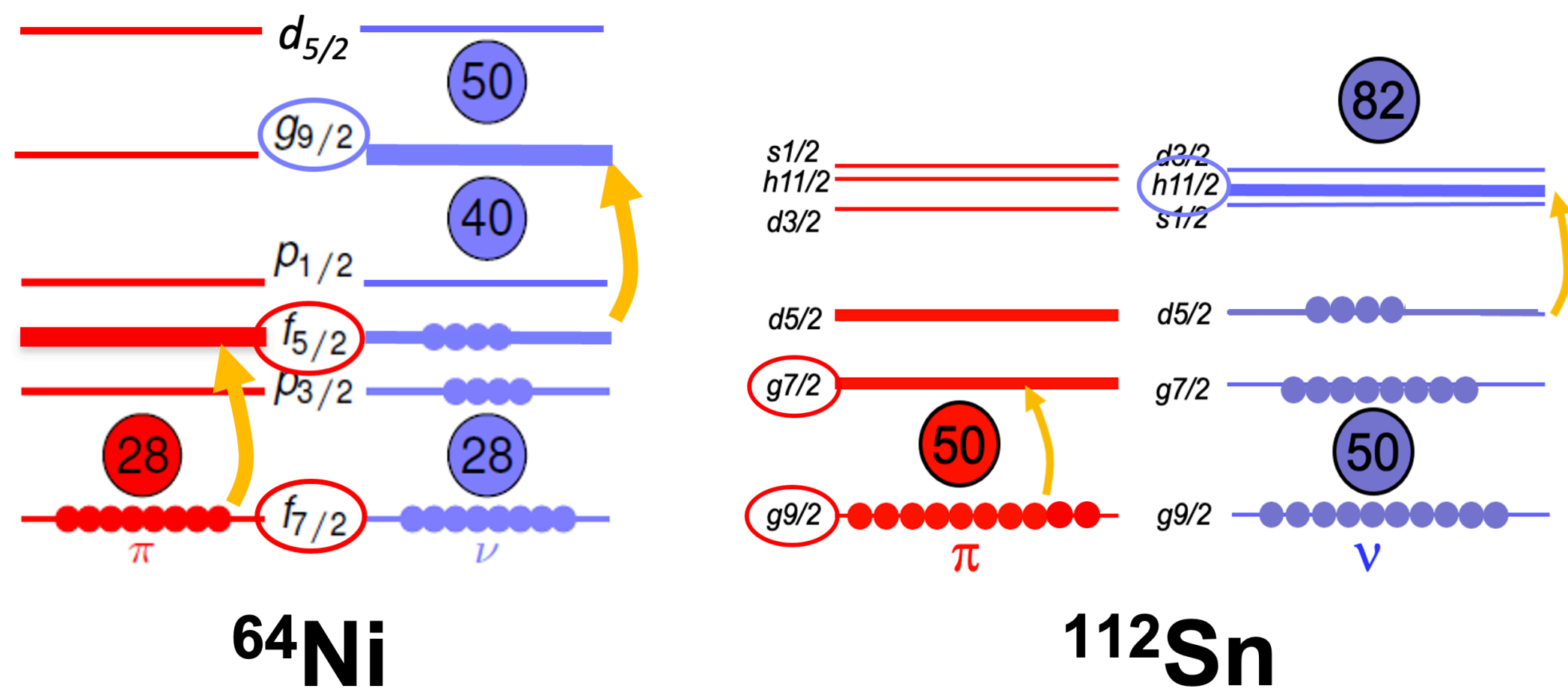
$^{109}\text{Sb}$ $\beta^+$	$^{110}\text{Sb}$ $\beta^+$	$^{111}\text{Sb}$ $\beta^+$	$^{112}\text{Sb}$ $\beta^+$	$^{113}\text{Sb}$ $\beta^+$	$^{114}\text{Sb}$ $\beta^+$	$^{115}\text{Sb}$ $\beta^+$	$^{116}\text{Sb}$ $\beta^+$	$^{117}\text{Sb}$ $\beta^+$	$^{118}\text{Sb}$ $\beta^+$	$^{119}\text{Sb}$ e- capture
$^{108}\text{Sn}$ $\beta^+$	$^{109}\text{Sn}$ $\beta^+$	$^{110}\text{Sn}$ e- capture	$^{111}\text{Sn}$ $\beta^+$	$^{112}\text{Sn}$ $2\beta^+$	$^{113}\text{Sn}$ $\beta^+$	$^{114}\text{Sn}$ Stable	$^{115}\text{Sn}$ Stable	$^{116}\text{Sn}$ Stable	$^{117}\text{Sn}$ Stable	$^{118}\text{Sn}$ Stable
$^{107}\text{In}$ $\beta^+$	$^{108}\text{In}$ $\beta^+$	$^{109}\text{In}$ $\beta^+$	$^{110}\text{In}$ $\beta^+$	$^{111}\text{In}$ e- capture	$^{112}\text{In}$ $\beta^+$	$^{113}\text{In}$ Stable	$^{114}\text{In}$ $\beta^-$	$^{115}\text{In}$ $\beta^-$	$^{116}\text{In}$ $\beta^-$	$^{117}\text{In}$ $\beta^-$
$^{106}\text{Cd}$ $2\beta^+$	$^{107}\text{Cd}$ $\beta^+$	$^{108}\text{Cd}$ $2\beta^+$	$^{109}\text{Cd}$ e- capture	$^{110}\text{Cd}$ Stable	$^{111}\text{Cd}$ Stable	$^{112}\text{Cd}$ Stable	$^{113}\text{Cd}$ $\beta^-$	$^{114}\text{Cd}$ $2\beta^-$	$^{115}\text{Cd}$ $\beta^-$	$^{116}\text{Cd}$ $2\beta^-$
$^{105}\text{Ag}$ $\beta^+$	$^{106}\text{Ag}$ $\beta^+$	$^{107}\text{Ag}$ Stable	$^{108}\text{Ag}$ $\beta^-$	$^{109}\text{Ag}$ Stable	$^{110}\text{Ag}$ $\beta^-$	$^{111}\text{Ag}$ $\beta^-$	$^{112}\text{Ag}$ $\beta^-$	$^{113}\text{Ag}$ $\beta^-$	$^{114}\text{Ag}$ $\beta^-$	$^{115}\text{Ag}$ $\beta^-$

K. Heyde and J. Wood, Rev. Mod. Phys. 83, 1467 (2011)

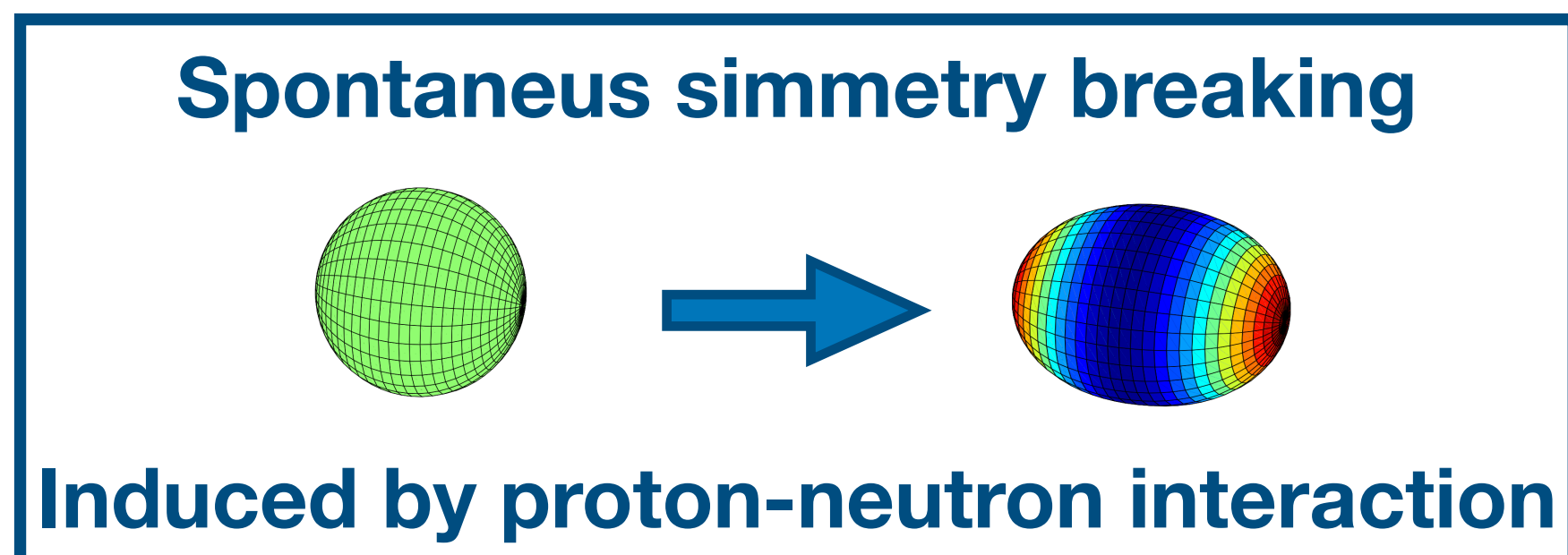
B. Lu, J. Zhao, E. Zhao, S. Zhou, EPJ Web of Conferences 38 05003 (2012)

# Origin of the $0^+$ excitations

## Shape coexistence at $Z=50$



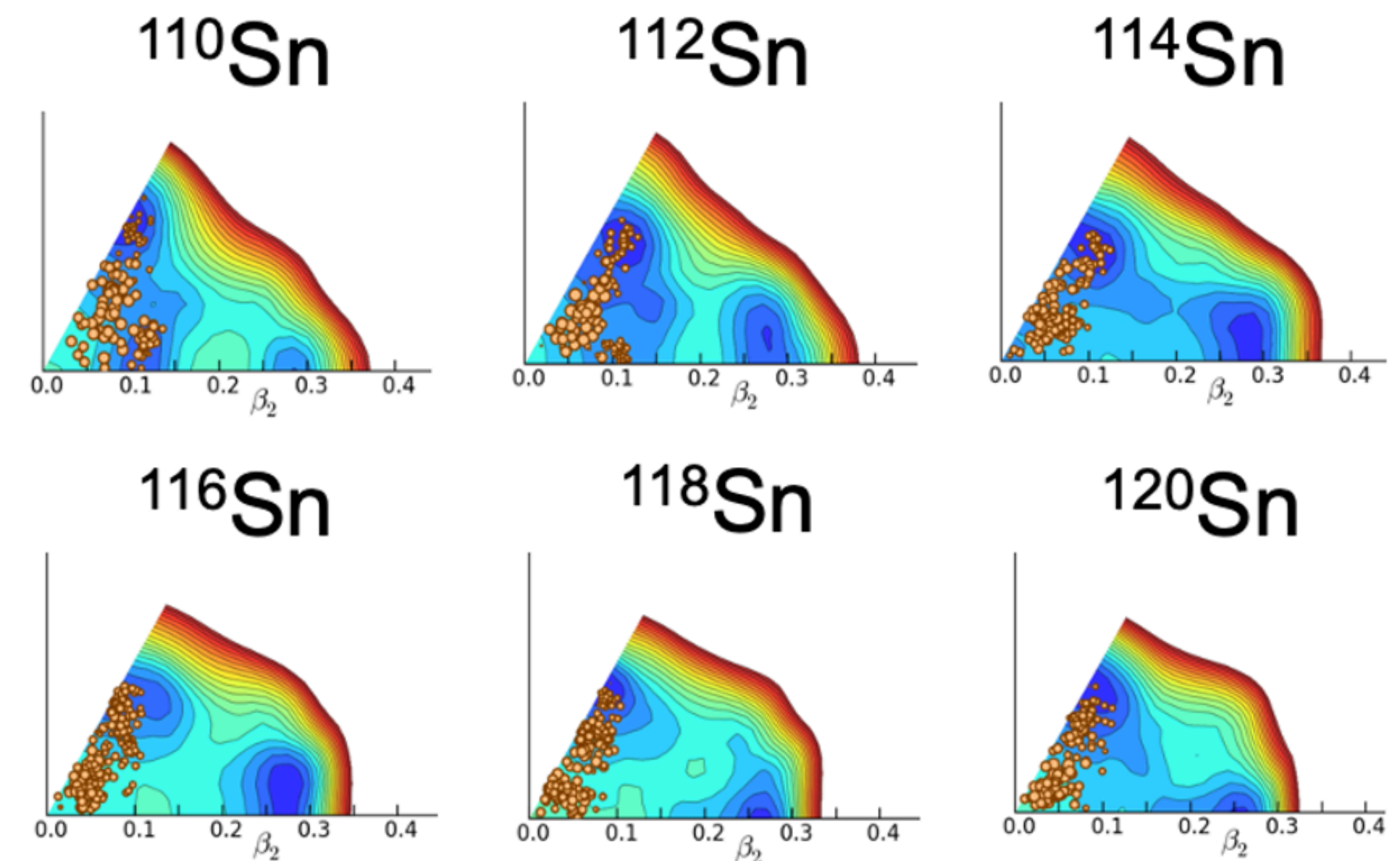
## Expected similar scenario to Ni



## Hartree-Fock-Bogoliubov PES

T. Togashi et al., Phys. Rev. Lett. 121, 062501 (2018).

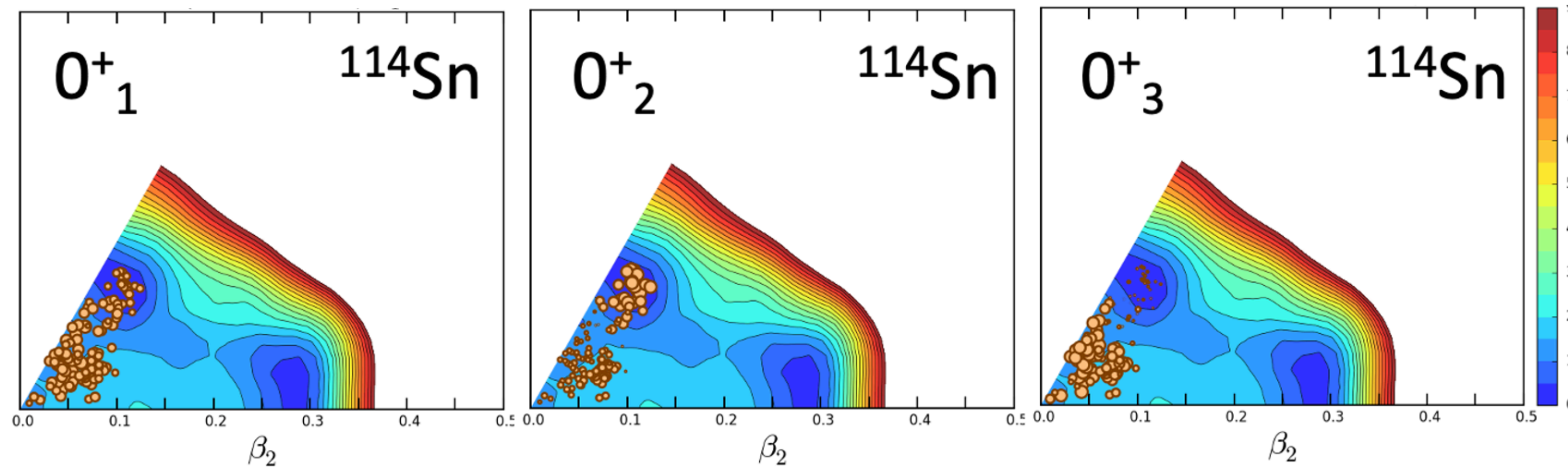
T. Otzuka, Y. Tsunoda, to be published.



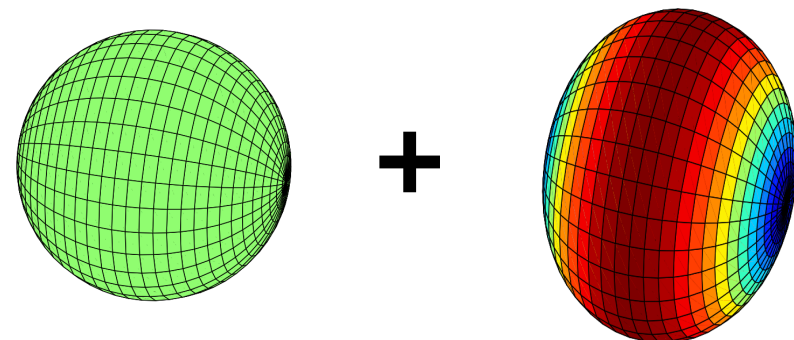
**Well-separated prolate minimum appearing from  $^{112}\text{Sn}$  up to  $^{118}\text{Sn}$**



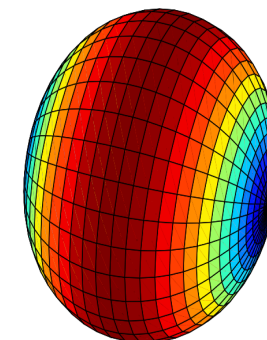
# A study case: $^{114}\text{Sn}$



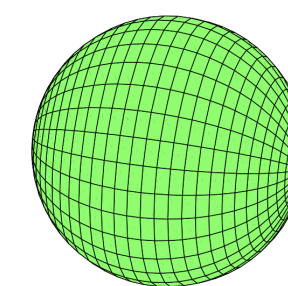
Spherical + oblate g.s.



Oblate  $0^+_2$



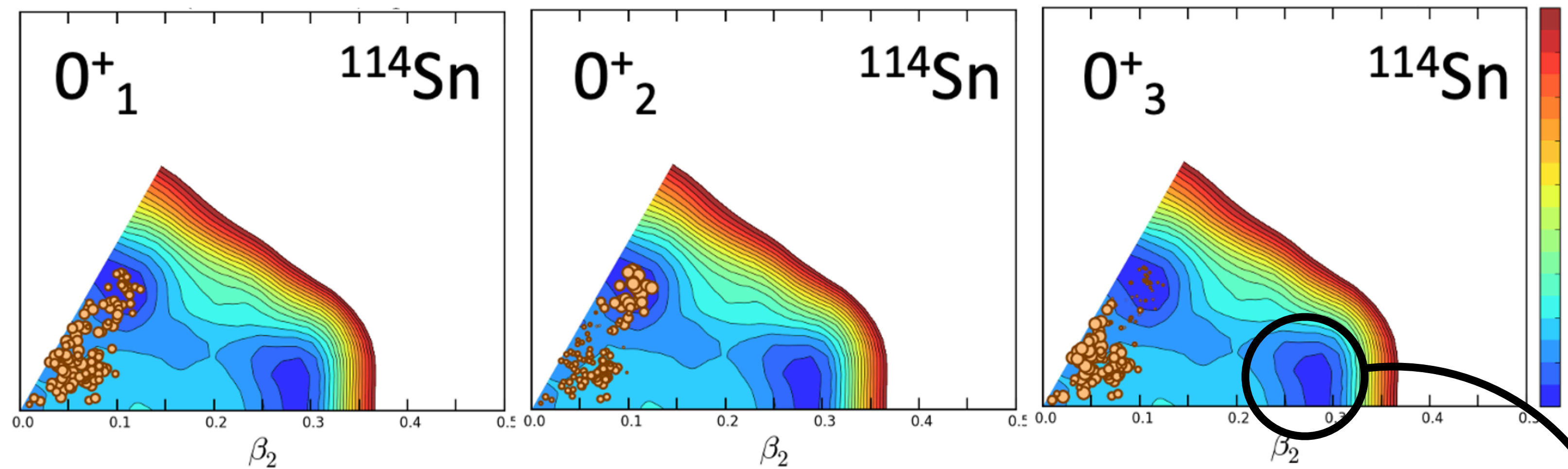
Spherical  $0^+_3$



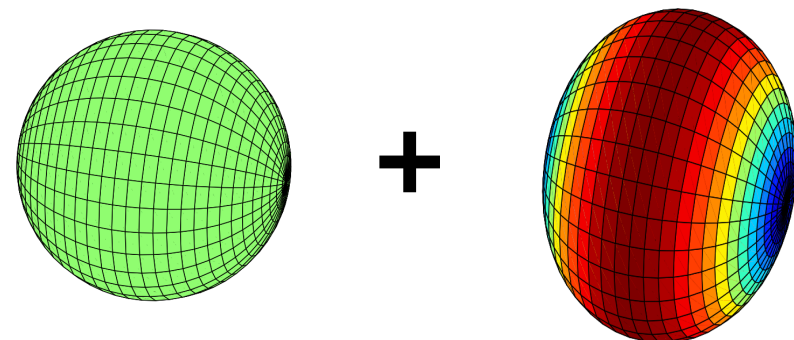
T. Otzuka, Y. Tsunoda, to be published.  
T. Togashi et al., Phys. Rev. Lett. 121, 062501 (2018).



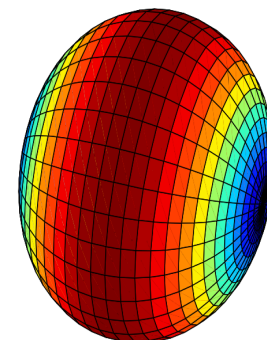
# A study case: $^{114}\text{Sn}$



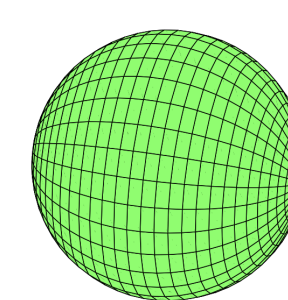
Spherical + oblate g.s.



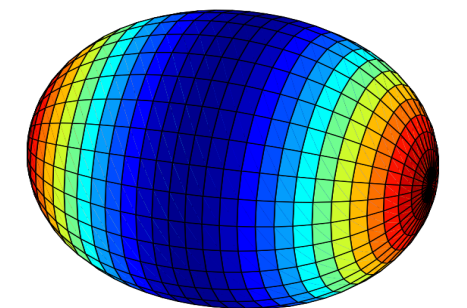
Oblate  $0^+_2$



Spherical  $0^+_3$



**Prolate  $0^+_4$  ??**



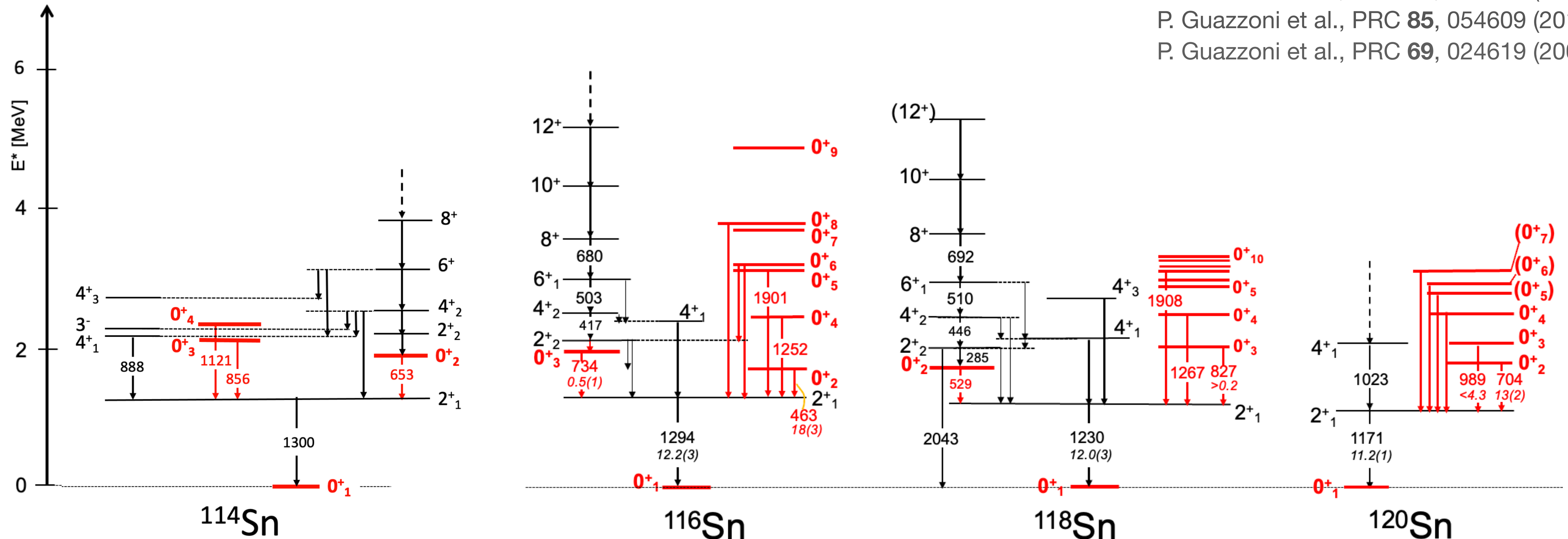
T. Otzuka, Y. Tsunoda, to be published.  
T. Togashi et al., Phys. Rev. Lett. 121, 062501 (2018).



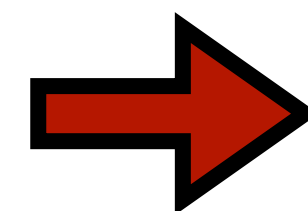
# How to probe shape coexistence?

Several  $0^+$  states observed in this region!

- R. L. Auble et al., PRC **6**, 2223 (1972)
- P. Guazzoni et al., PRC **74**, 054605 (2006)
- P. Guazzoni et al., PRC **85**, 054609 (2012)
- P. Guazzoni et al., PRC **69**, 024619 (2004)



Few lifetimes known!



Experimental investigation needed



# A series of complementary experiments

Experiment at LNL with AGATA-PRISMA on Sn isotopes near  $A=110$

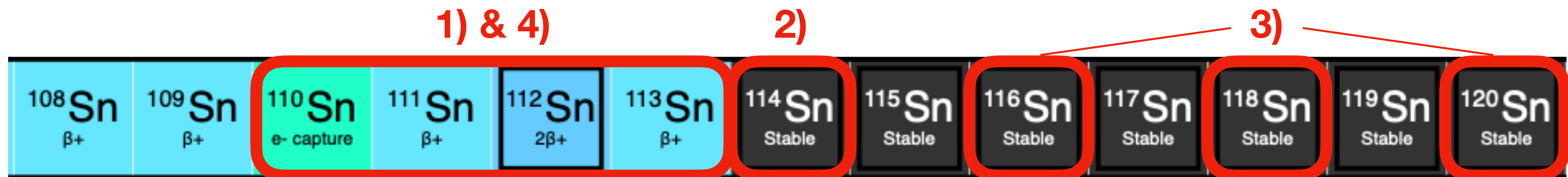
1) Lifetime measurements of  $0^+$  states in  $^{112}\text{Sn}$  - July 2022

Experiments at IFIN-HH on  $^{112-120}\text{Sn}$  at sub-barrier energies

2) Lifetime measurements of  $0^+$  states in  $^{114}\text{Sn}$  - October 2022

3) Low-spin spectroscopy of  $^{116-118-120}\text{Sn}$  with different probes - October 2023

4) Lifetime measurements of  $^{111,112,113}\text{Sn}$  - November 2023





# A series of complementary experiments

Experiment at LNL with AGATA-PRISMA on Sn isotopes near  $A=110$

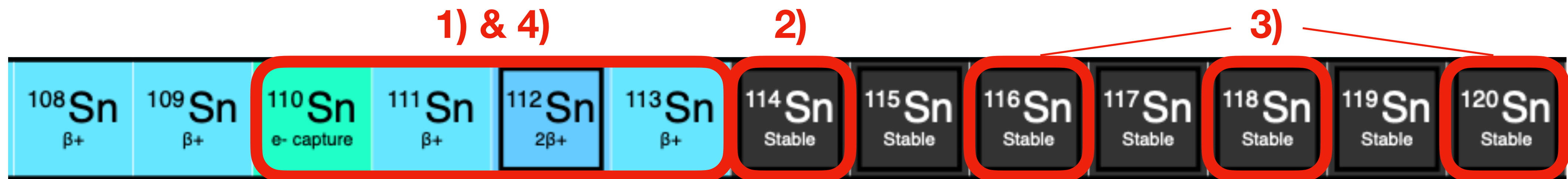
1) Lifetime measurements of  $0^+$  states in  $^{112}\text{Sn}$  - July 2022

Experiments at IFIN-HH on  $^{112-120}\text{Sn}$  at sub-barrier energies

2) Lifetime measurements of  $0^+$  states in  $^{114}\text{Sn}$  - October 2022

3) Low-spin spectroscopy of  $^{116-118-120}\text{Sn}$  with different probes - October 2023

4) Lifetime measurements of  $^{111,112,113}\text{Sn}$  - November 2023





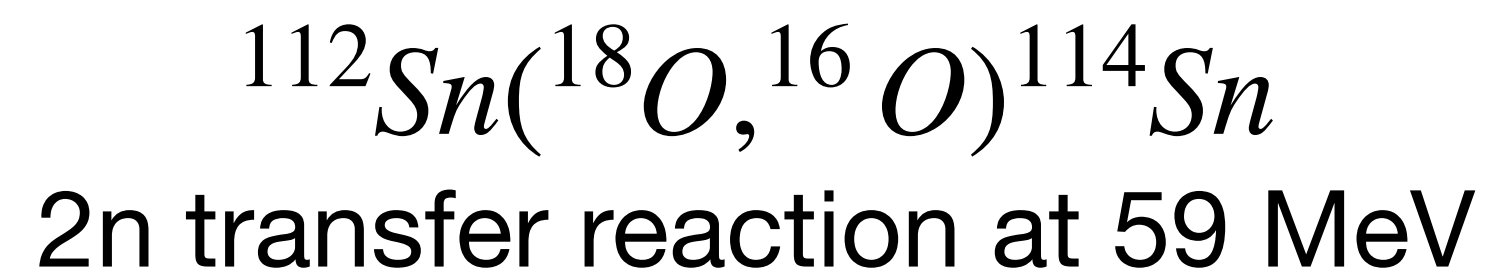
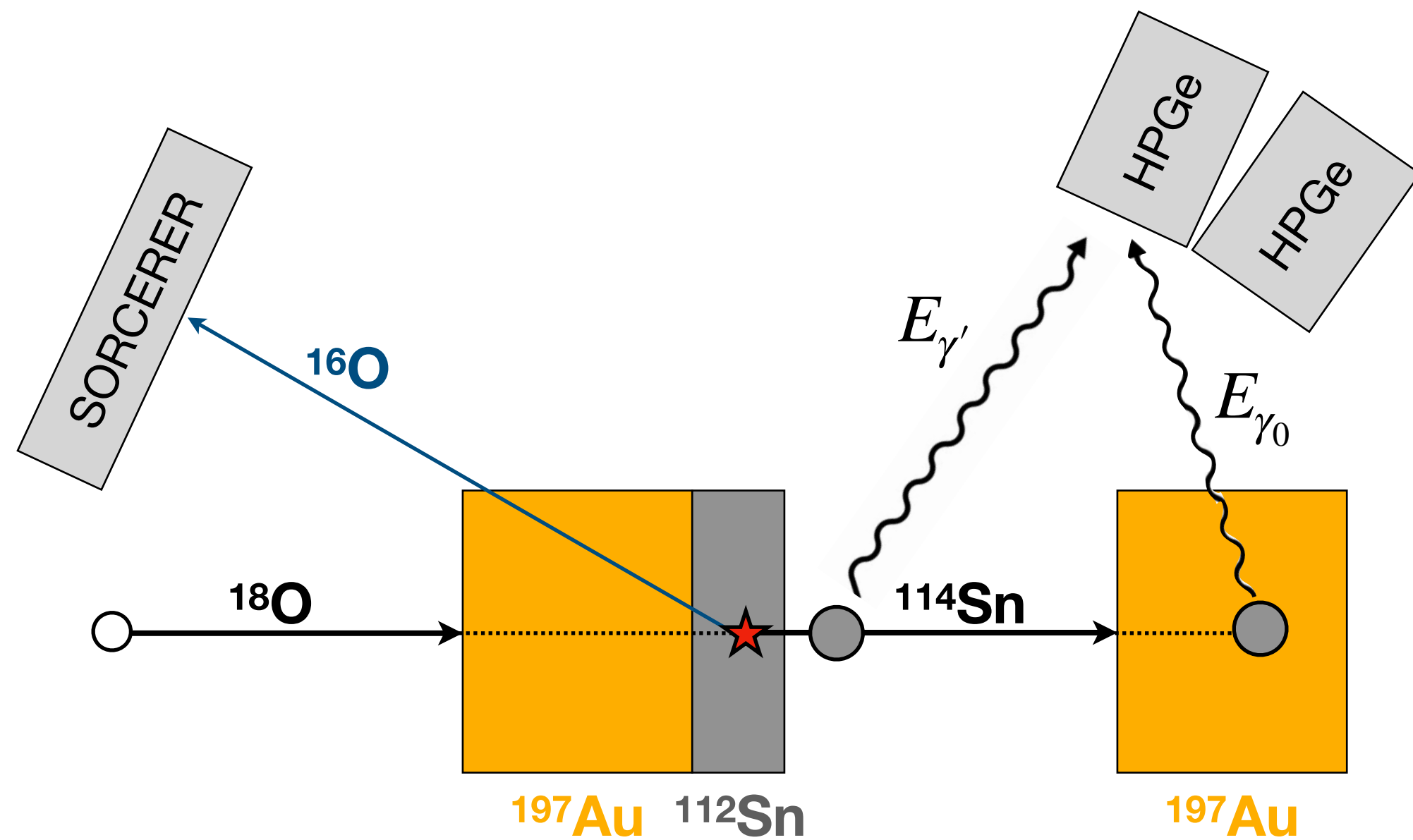
# ROSPHERE + Plunger @ IFIN

## $^{114}\text{Sn}$ - 2n transfer

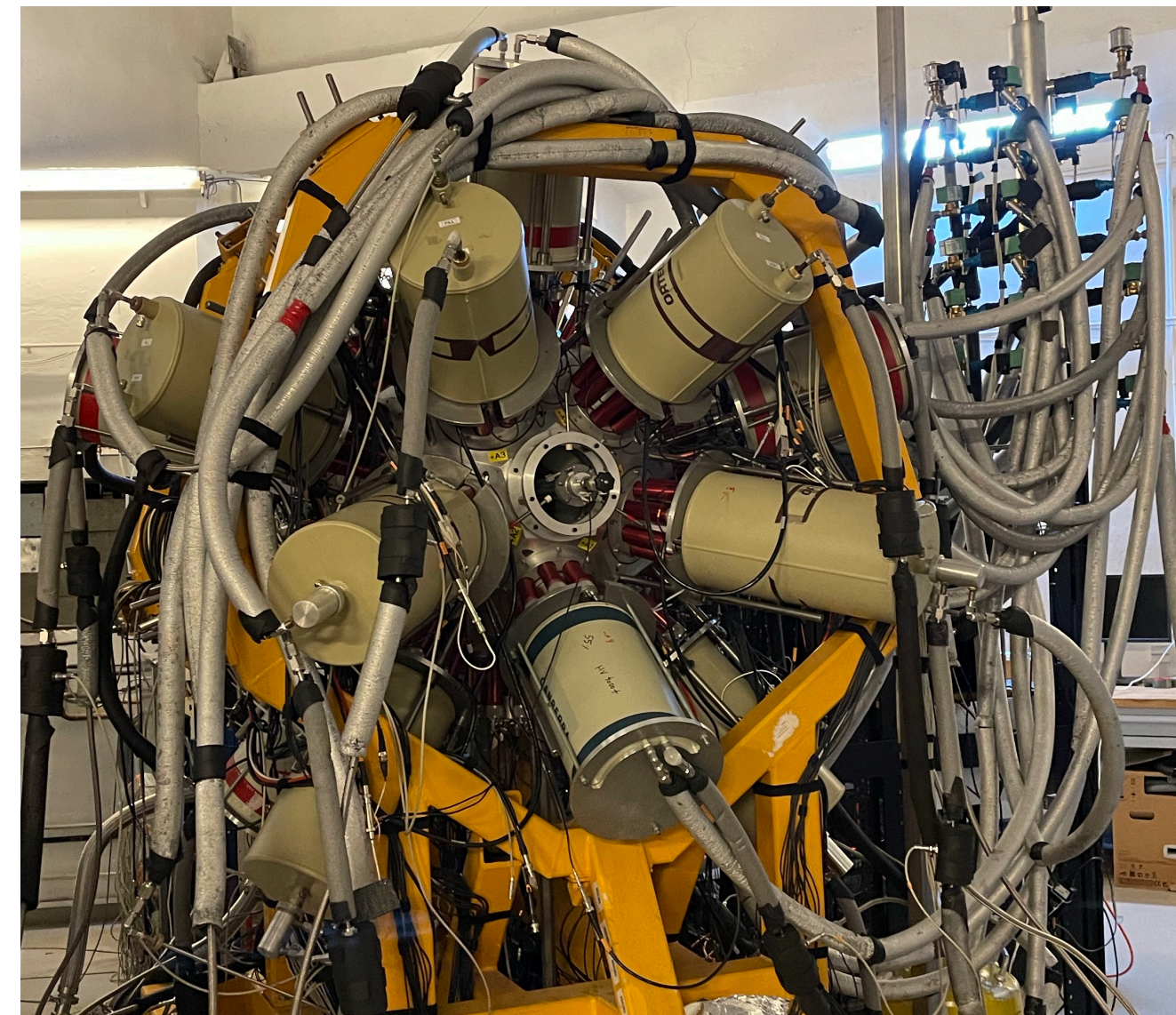


# ROSPHERE-SORCERER @ IFIN

Experiment in November 2022

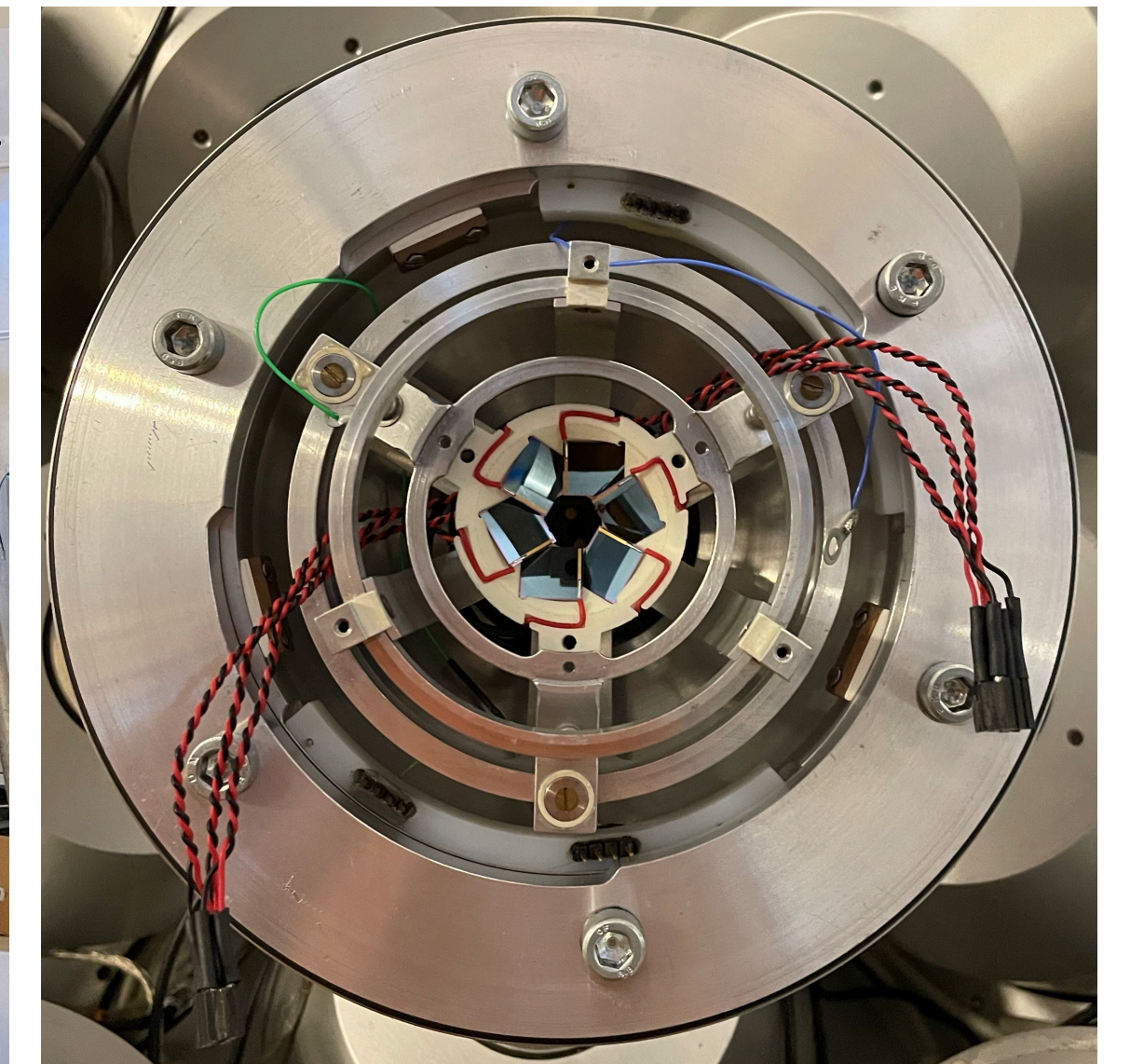


## ROSPHERE



- 20 HPGe + BGO
- 5 CeBr scintillators

## SORCERER



- 6 Si solar cells

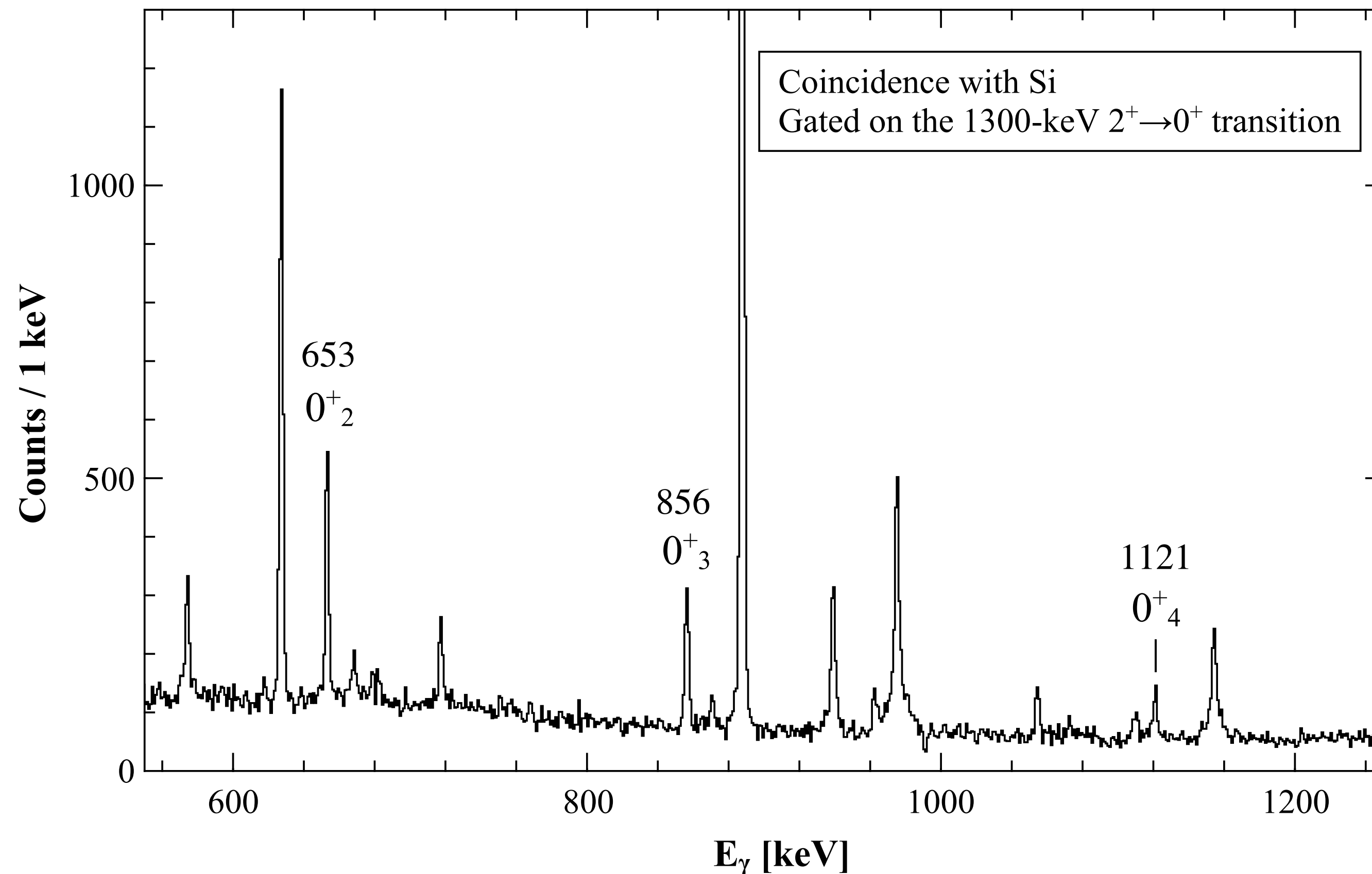
D. Bucurescu et al., NIM A 837 (2016) 1–10

T. Beck, C. Costache, R. Lică et al., NIM A 951 (2020) 163090



# ROSPHERE @ IFIN: $^{114}\text{Sn}$ thick target

3-days test experiment in 2021 with a thick  $10 \text{ mg/cm}^2$   $^{112}\text{Sn}$  target



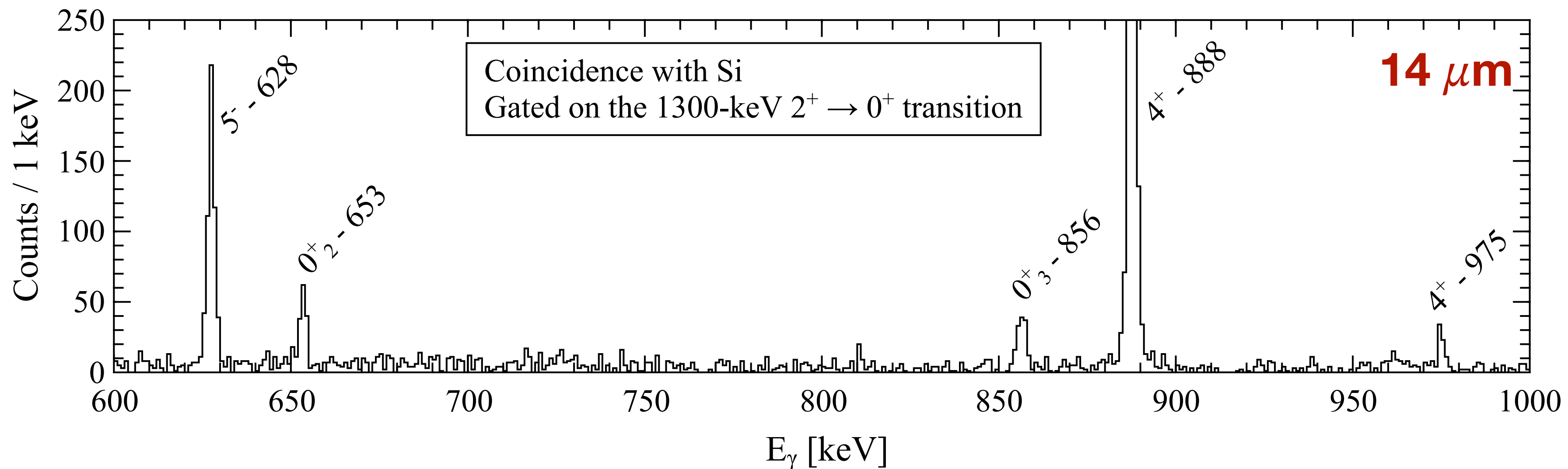
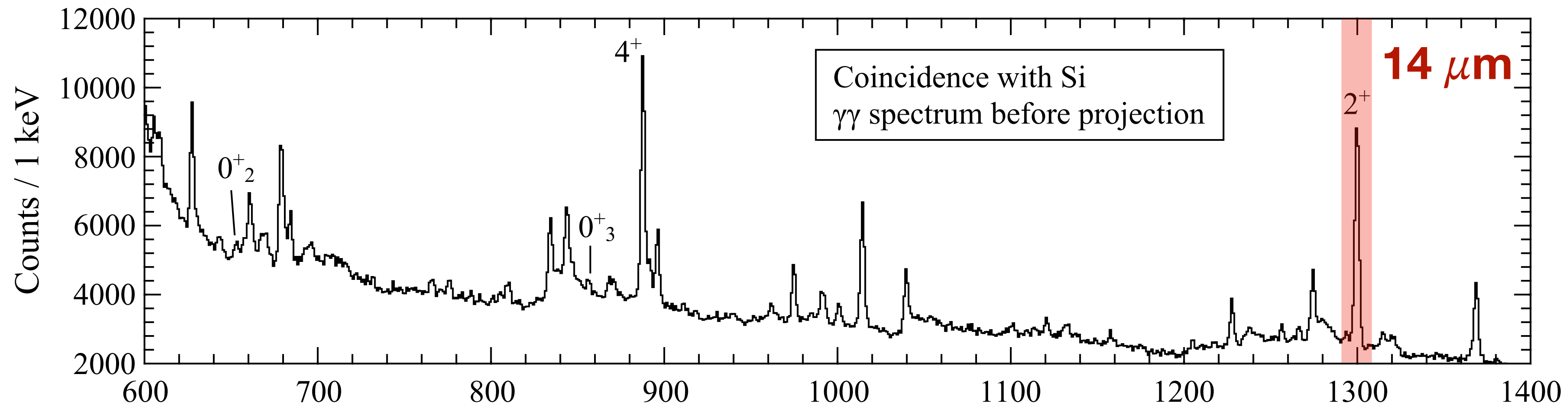
	Counts	Intensity
$0^+_2$	953	100%
$0^+_3$	705	74%
$0^+_4$	190	20%

In the  $0^+_4 \rightarrow 2^+_1$  transition, we observe 20% of the counts respect to the  $0^+_2 \rightarrow 2^+_1$

**No lineshape of  $0^+$  transitions observed with thick target!**



# $^{114}\text{Sn}$ - $\gamma\gamma$ coincidences



Plunger distances:  
14, 22, 42, 74  $\mu\text{m}$

ToF range: 2 - 15 ps

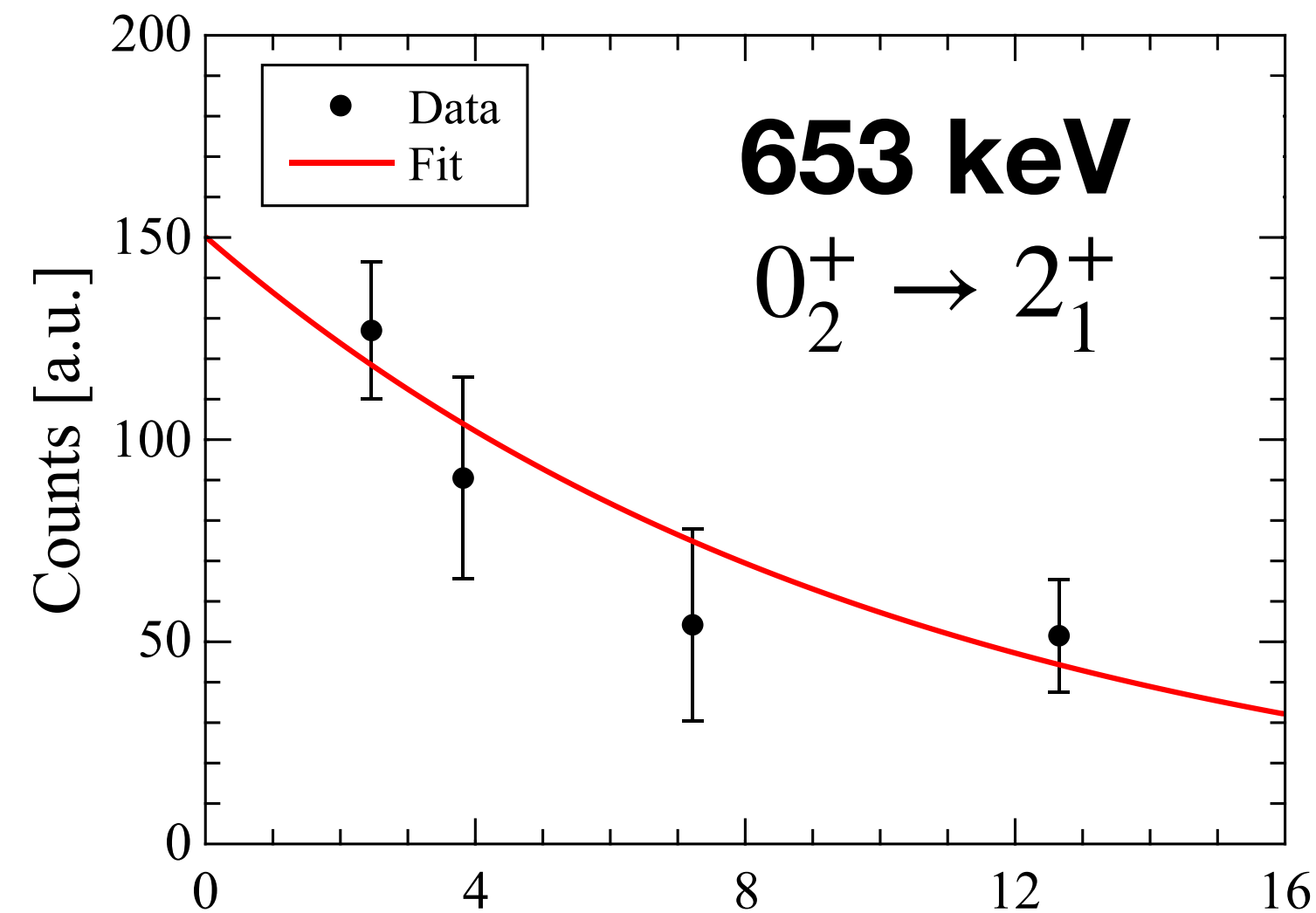
**$\gamma\gamma$  coincidences with  
observation of the  
stopped intensities**



# $^{114}\text{Sn}$ - Lifetimes of $0^+$ states

Preliminary results!

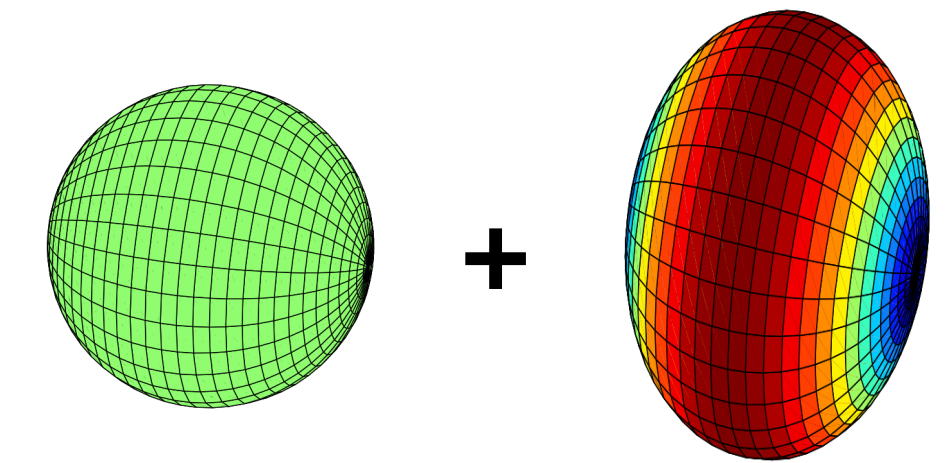
Possible interpretation



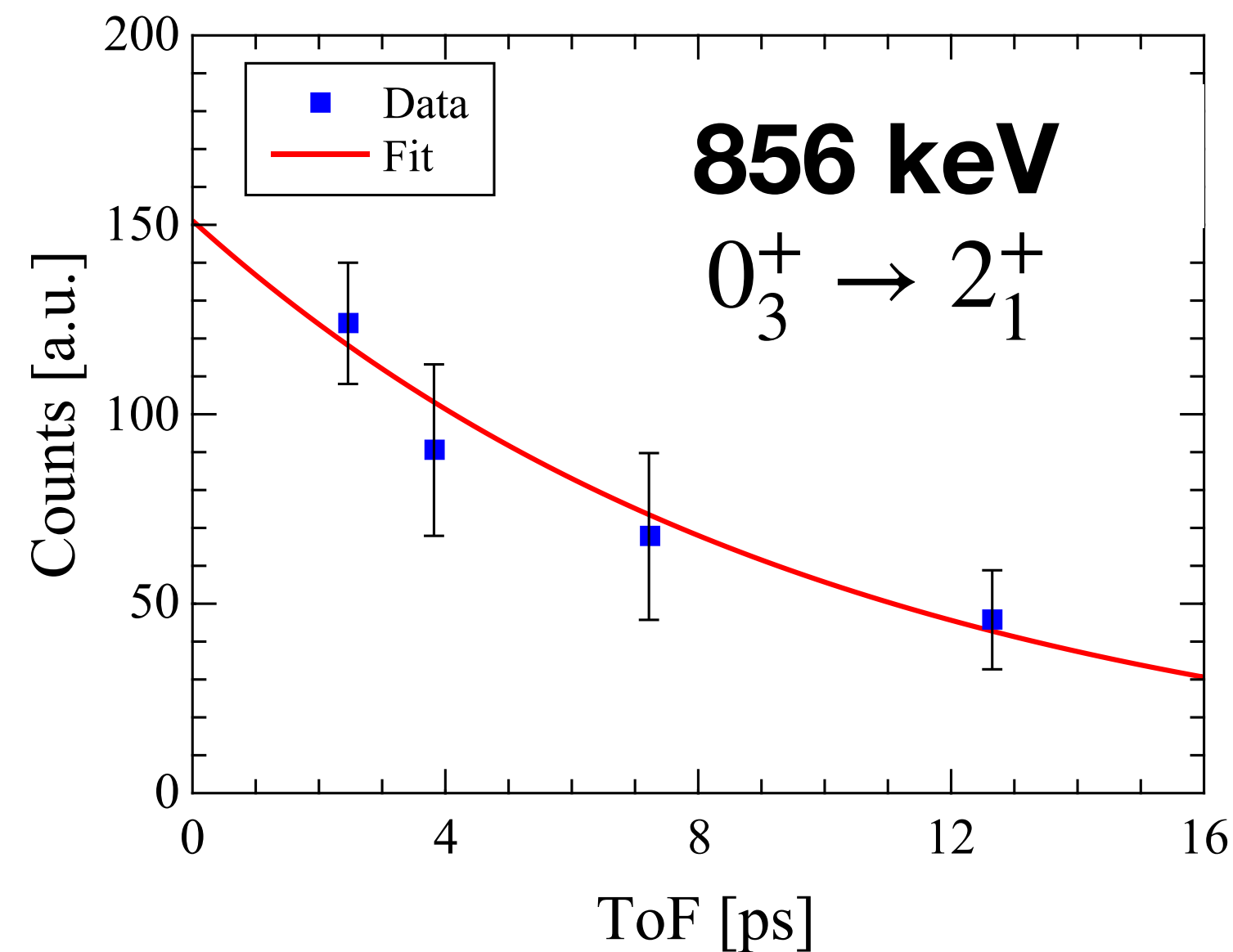
$$T_{1/2} = 7.2 \pm 2.5 \text{ ps}$$

$$B(E2) = 20.2 \pm 7.0 \text{ W.u.}$$

Lit:  $T_{1/2} = 6.5 \pm 2.3 \text{ ps}$



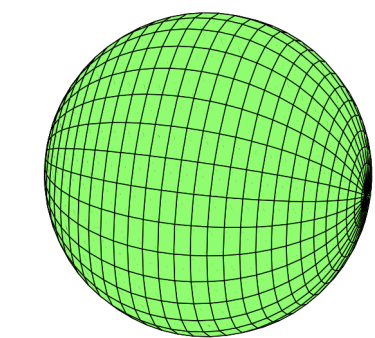
Spherical + Oblate



$$T_{1/2} = 6.9 \pm 2.2 \text{ ps}$$

$$B(E2) = 5.4 \pm 1.7 \text{ W.u.}$$

Lit:  $T_{1/2} > 7.6 \text{ ps}$



Spherical



# ROSPHERE @ IFIN

## $^{116,118,120}\text{Sn}$ with different probes



# 116-118-120Sn @ IFIN

Experiment in Fall 2023

$^{13}\text{C} + ^{117}\text{Sn}$  @ 43 MeV  
 $^{13}\text{C} + ^{119}\text{Sn}$  @ 43 MeV  
 $^{16}\text{O} + ^{116}\text{Cd}$  @ 56 MeV

1n, 2p, 1 $\alpha$  transfer reactions

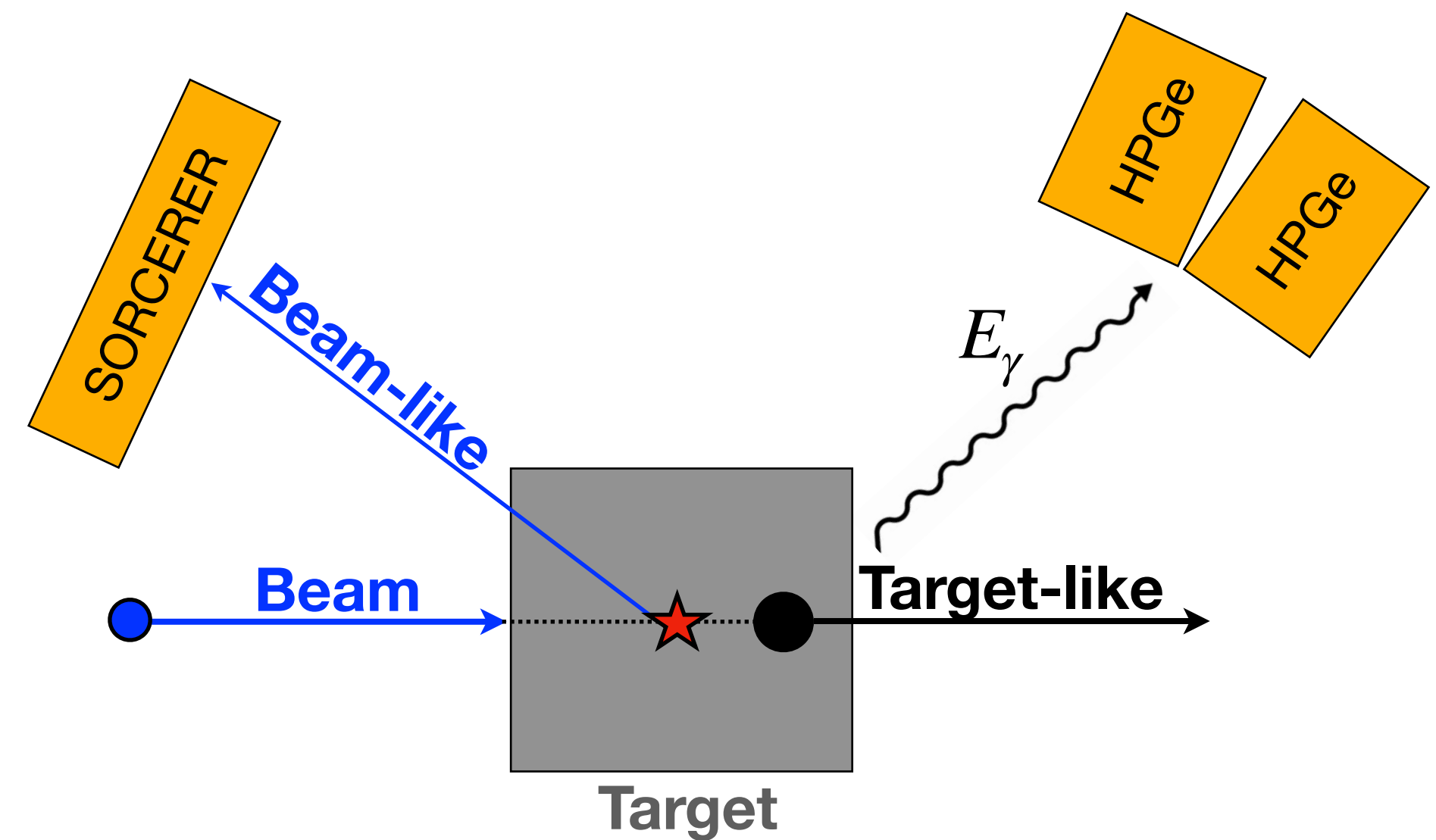
$^{116}\text{Sn} \Rightarrow +1n$

$^{118}\text{Sn} \Rightarrow +1n, -1n, -2p$

$^{120}\text{Sn} \Rightarrow -1n, -1\alpha$

D. Bucurescu et al., NIM A 837 (2016) 1–10

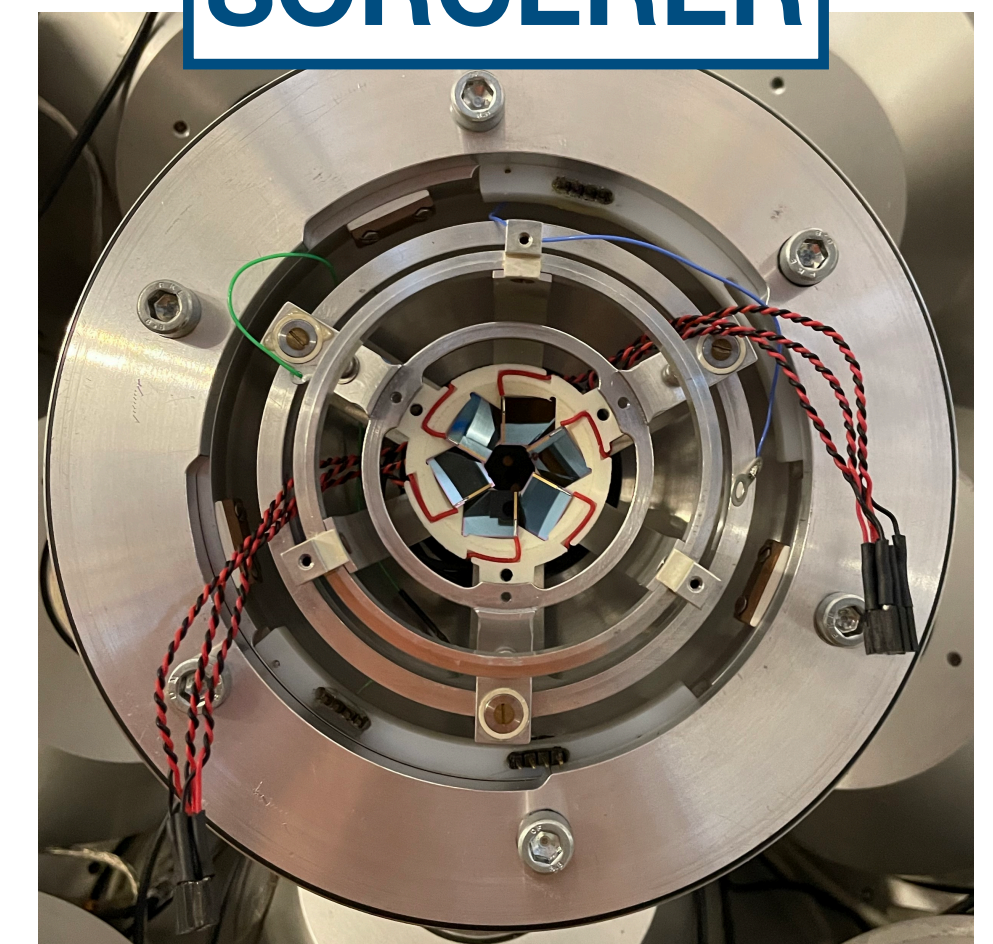
T. Beck, C. Costache, R. Lică et al., NIM A 951 (2020) 163090



ROSPHERE



SORCERER



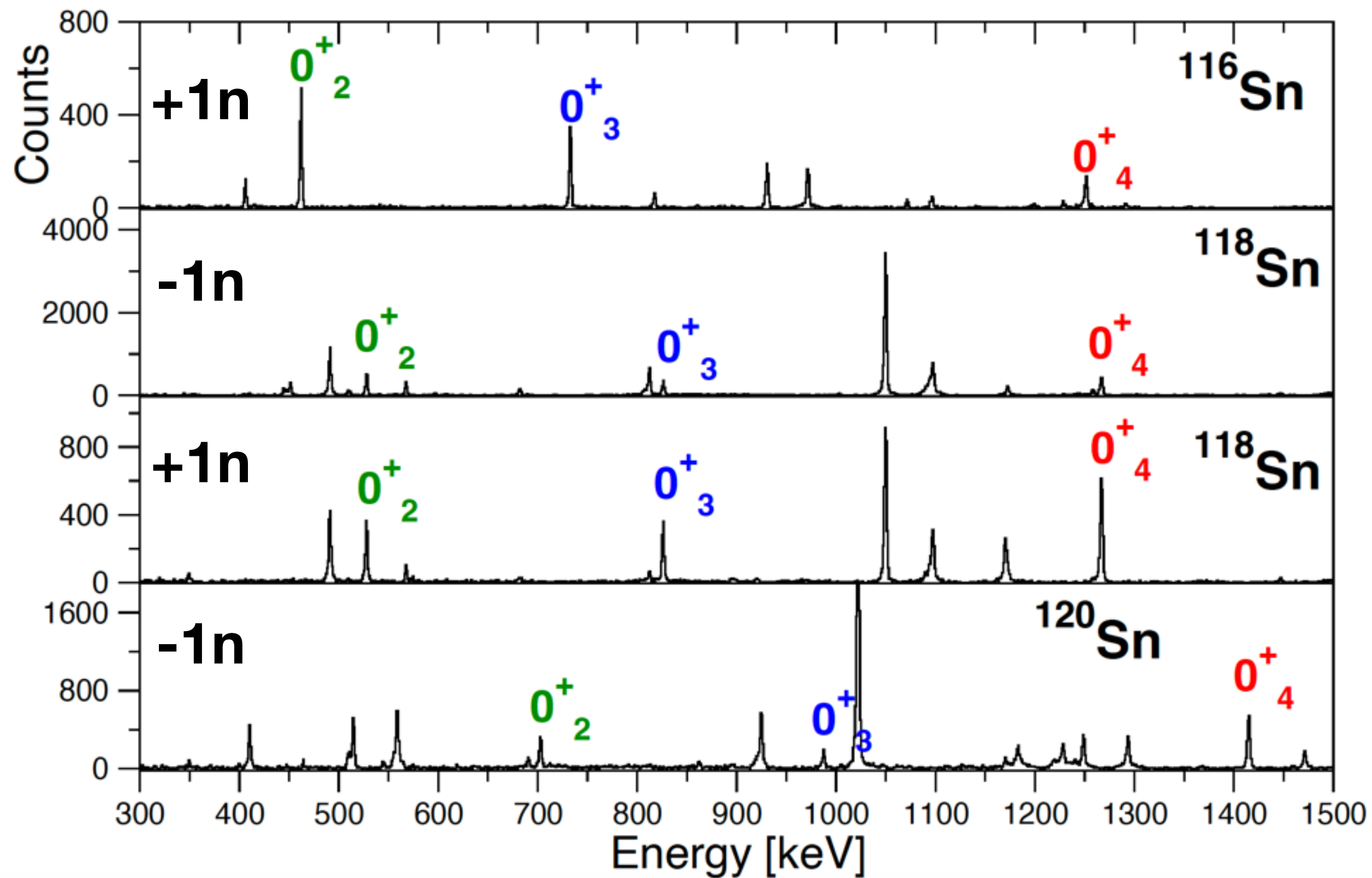
- 18 HPGe + BGO
- 5 CeBr scintillators

- 6 Si solar cells

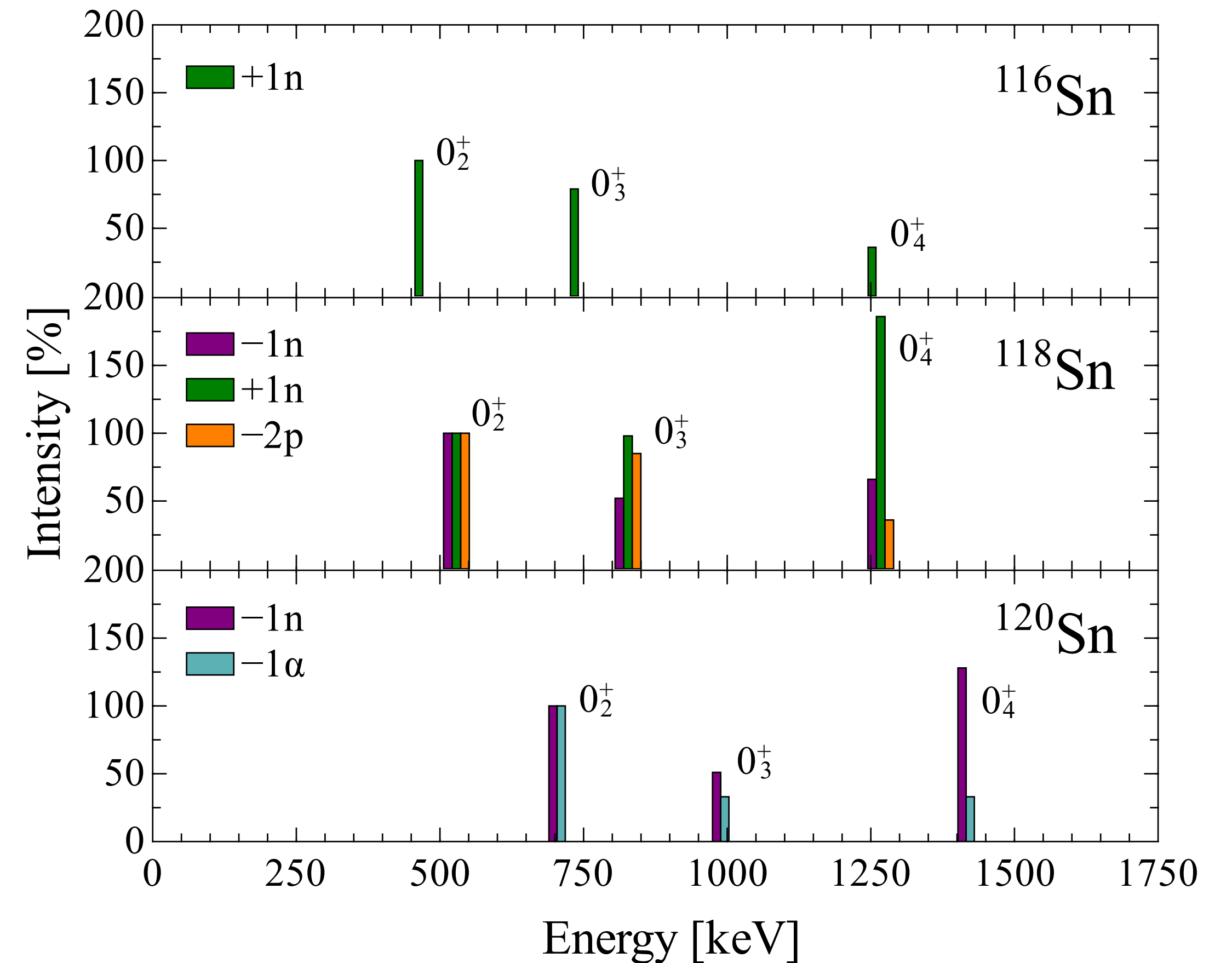


# 116-118-120Sn: Spectroscopy and DSAM

$\gamma\gamma$  projections, gated on the  $2_1^+ \rightarrow 0_1^+$  transition  
for the  $\pm 1n$  reactions



Relative intensities of  $0^+ \rightarrow 2_1^+$  transitions





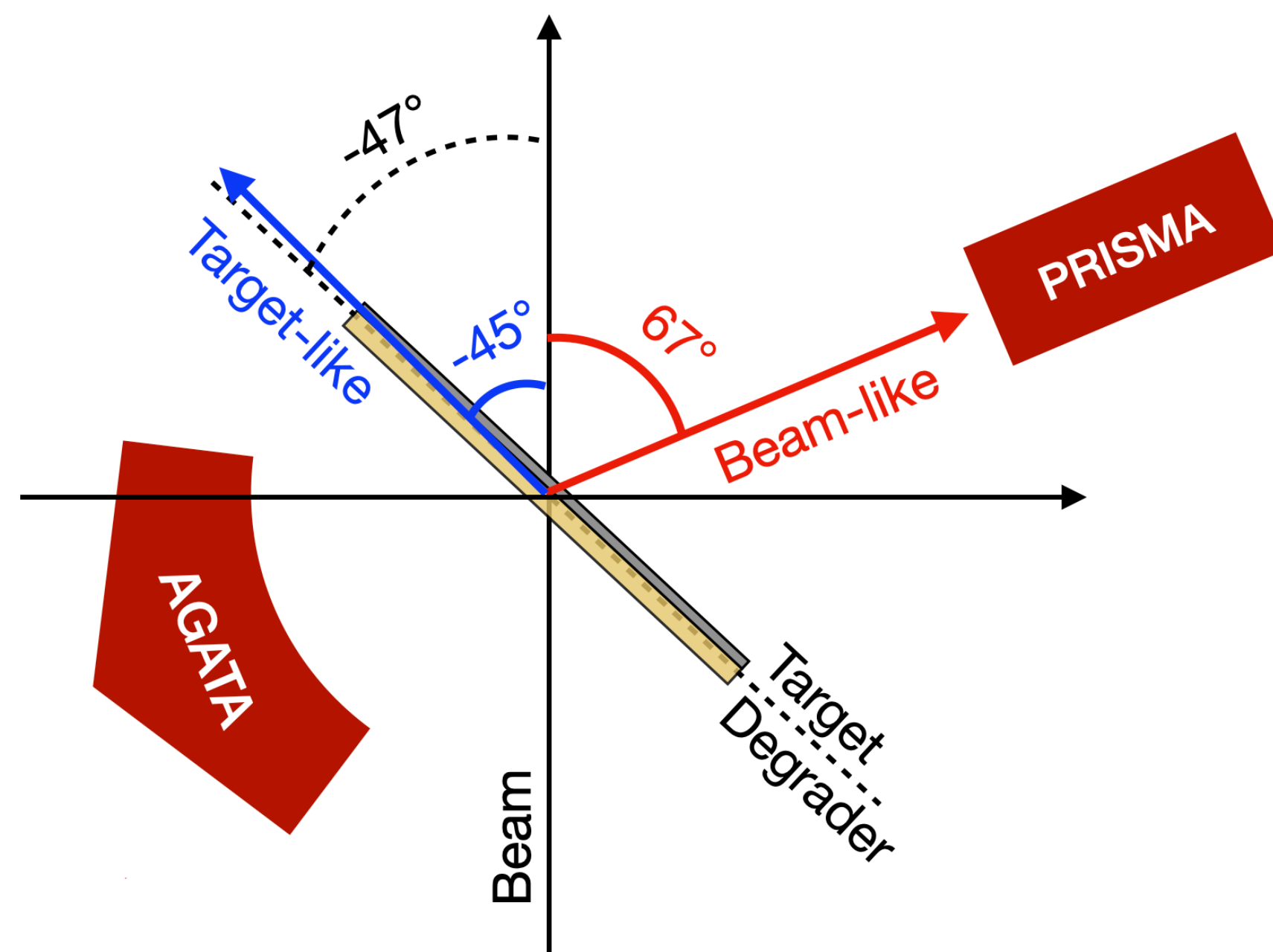
# **AGATA-PRISMA @ LNL**

## **$^{110-114}\text{Sn}$ - multi-nucleon transfer**

# Spectroscopy with PRISMA

$^{32}\text{S} + ^{110}\text{Cd} @ 164 \text{ MeV}$   
Multi-nucleon transfer reaction

Effective thick target - DSAM



Master Thesis of **Paolo Pellegrini**

UNIVERSITÀ DEGLI STUDI DI MILANO  
FACOLTÀ DI SCIENZE E TECNOLOGIE

Laurea in Fisica

**Study of the coexistence of nuclear shapes  
in the isotopes of Sn and Cd of mass  $A \sim 110$   
with the AGATA-PRISMA apparatus**

Relatrice: Prof.ssa Silvia Leoni  
Correlatore: Dott. Simone Bottoni

Candidato: Paolo Pellegrini  
matricola: 465934

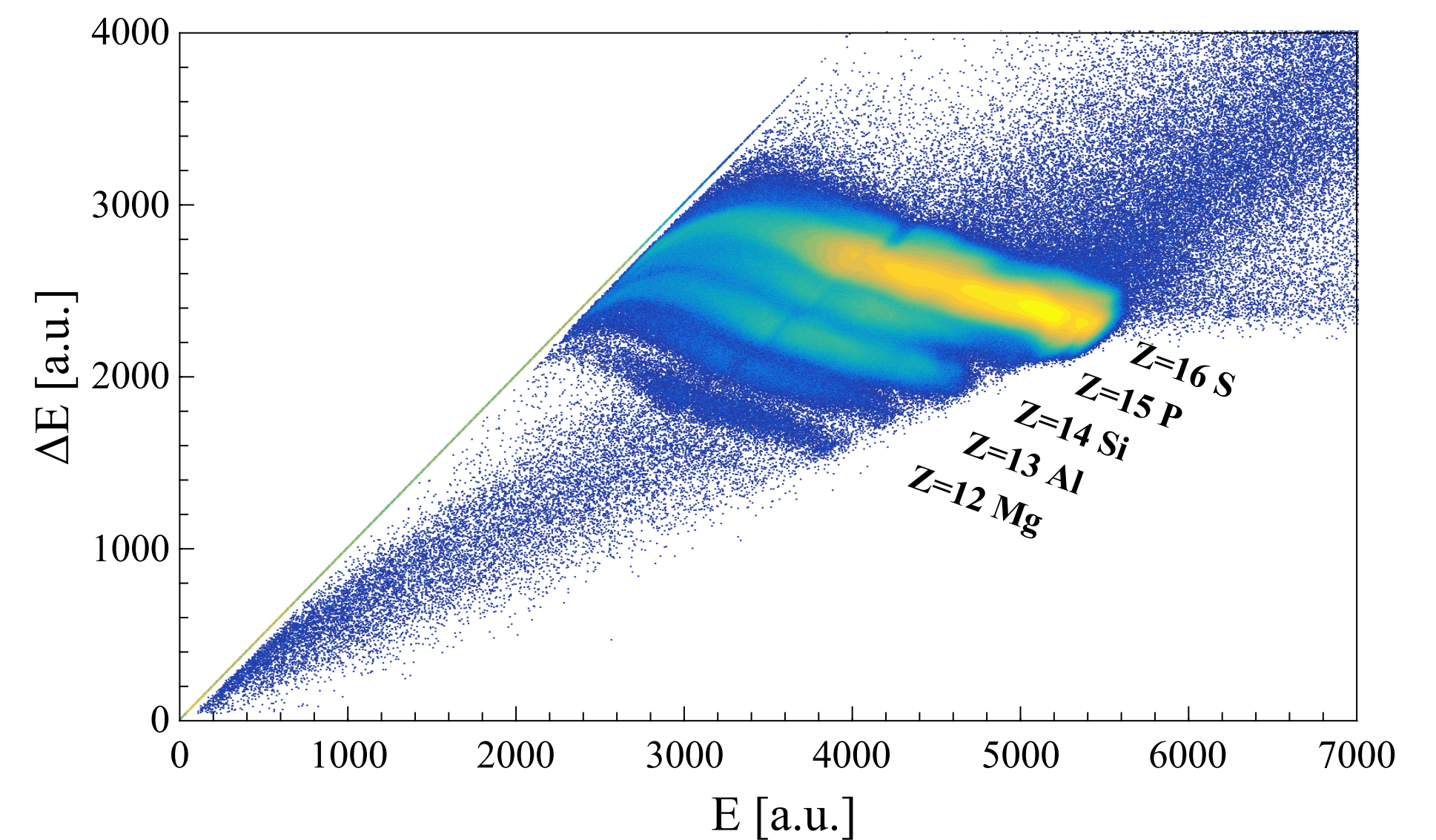
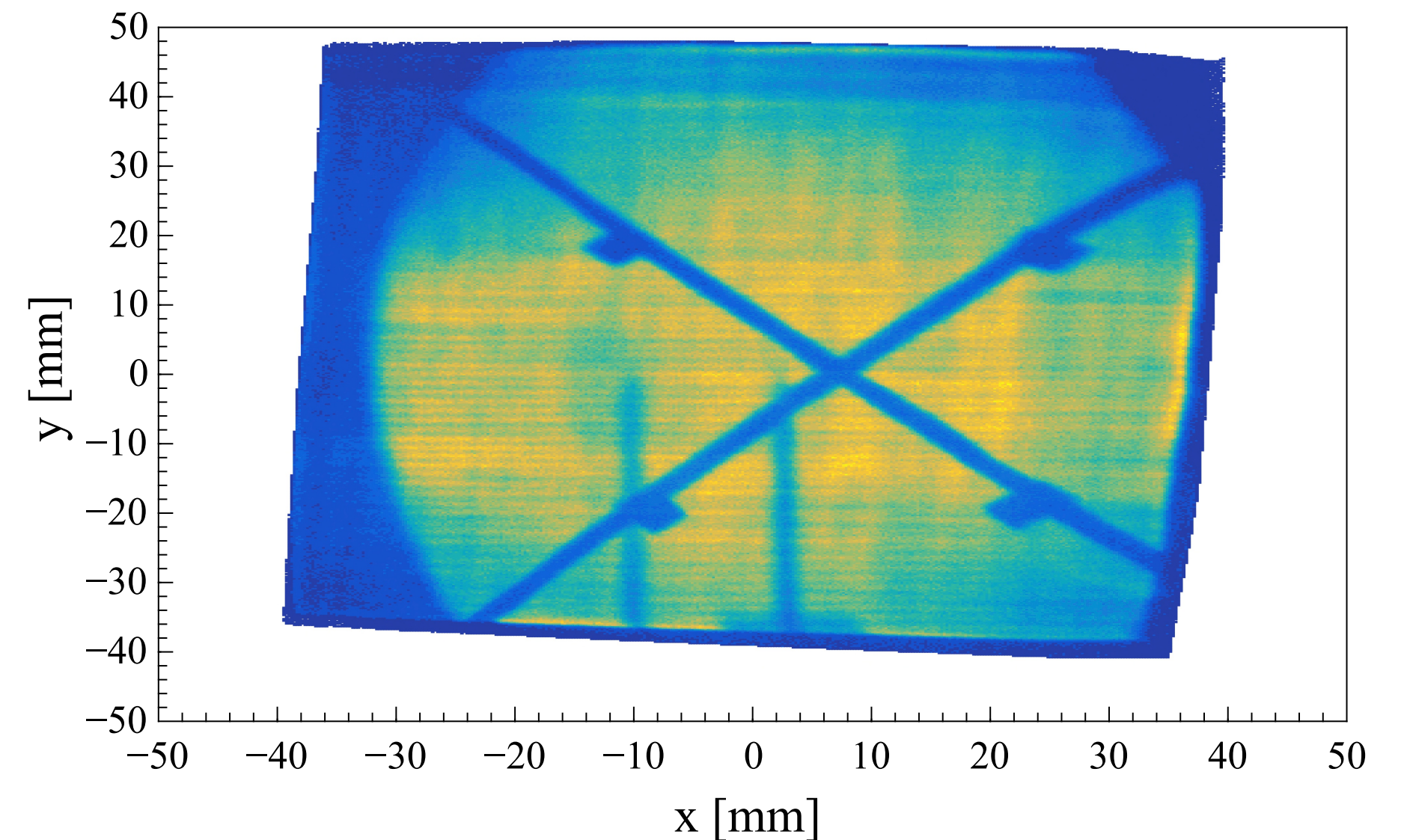
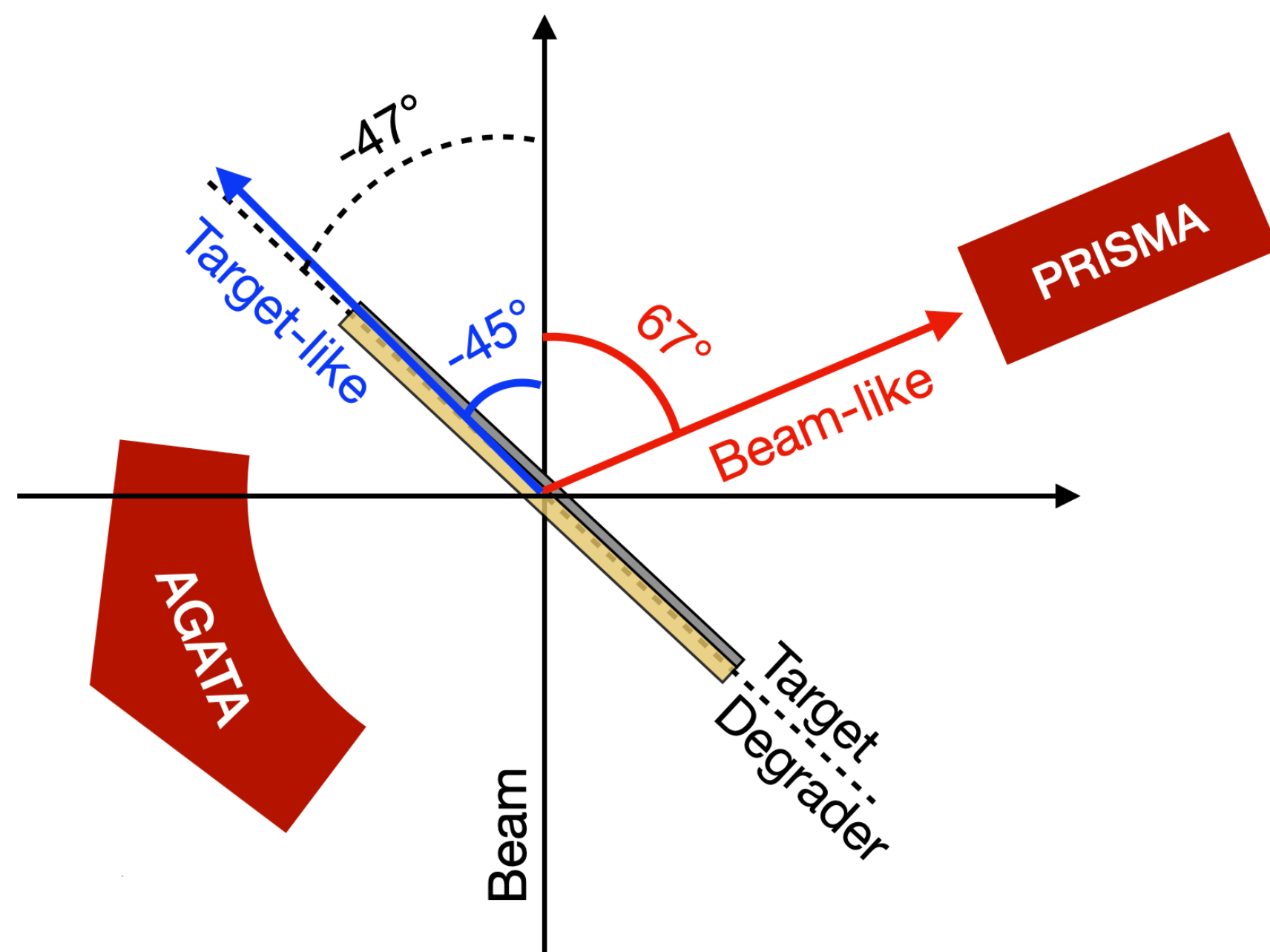
Anno Accademico 2022/2023



# Spectroscopy with PRISMA

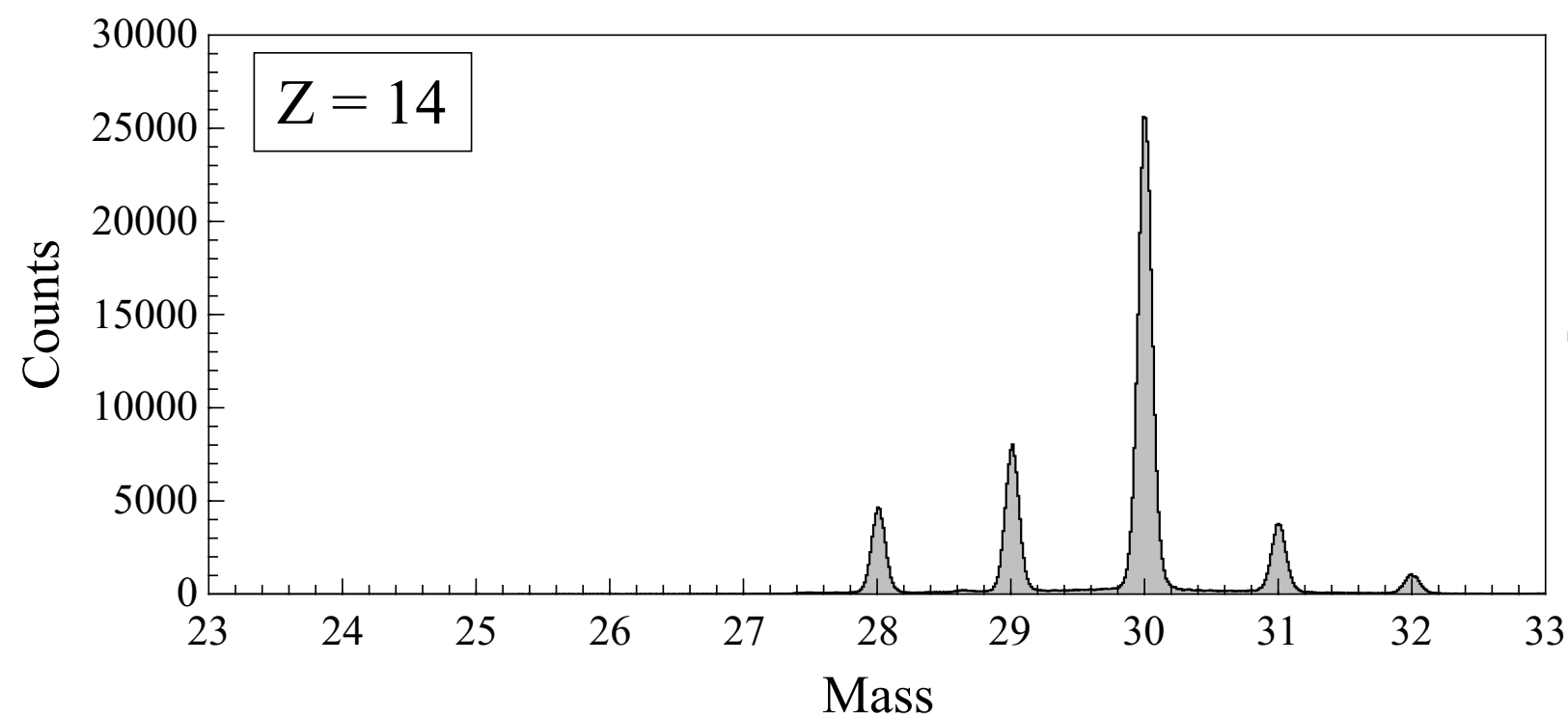
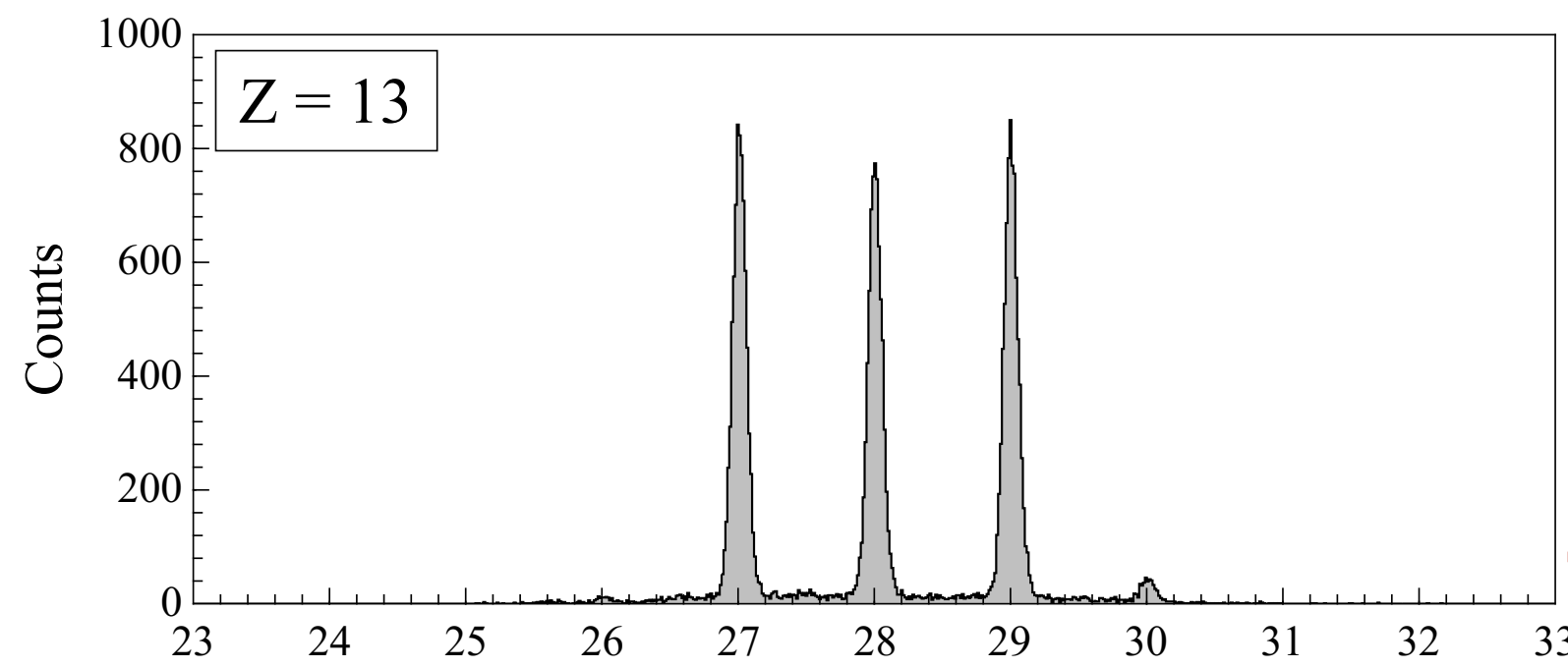
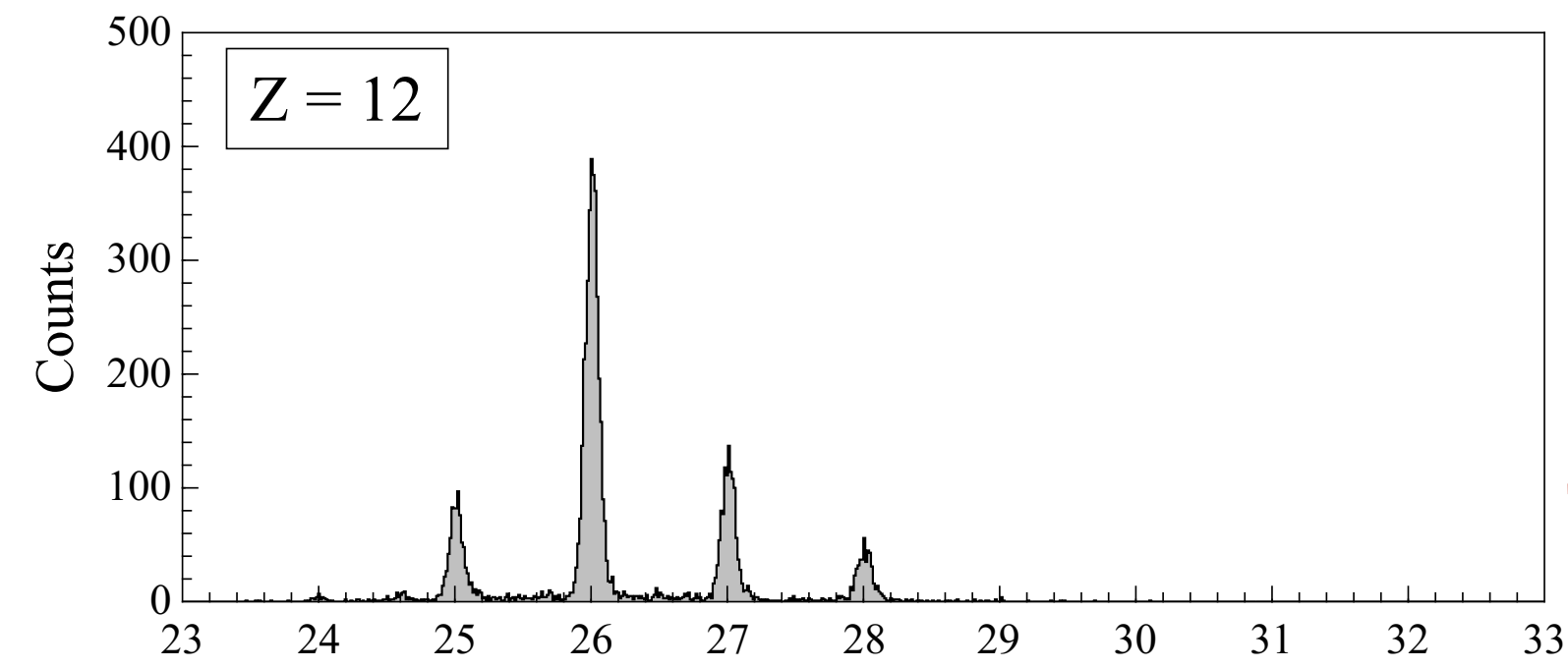
$^{32}\text{S} + ^{110}\text{Cd} @ 164 \text{ MeV}$   
Multi-nucleon transfer reaction

Effective thick target - DSAM





# Mass distributions

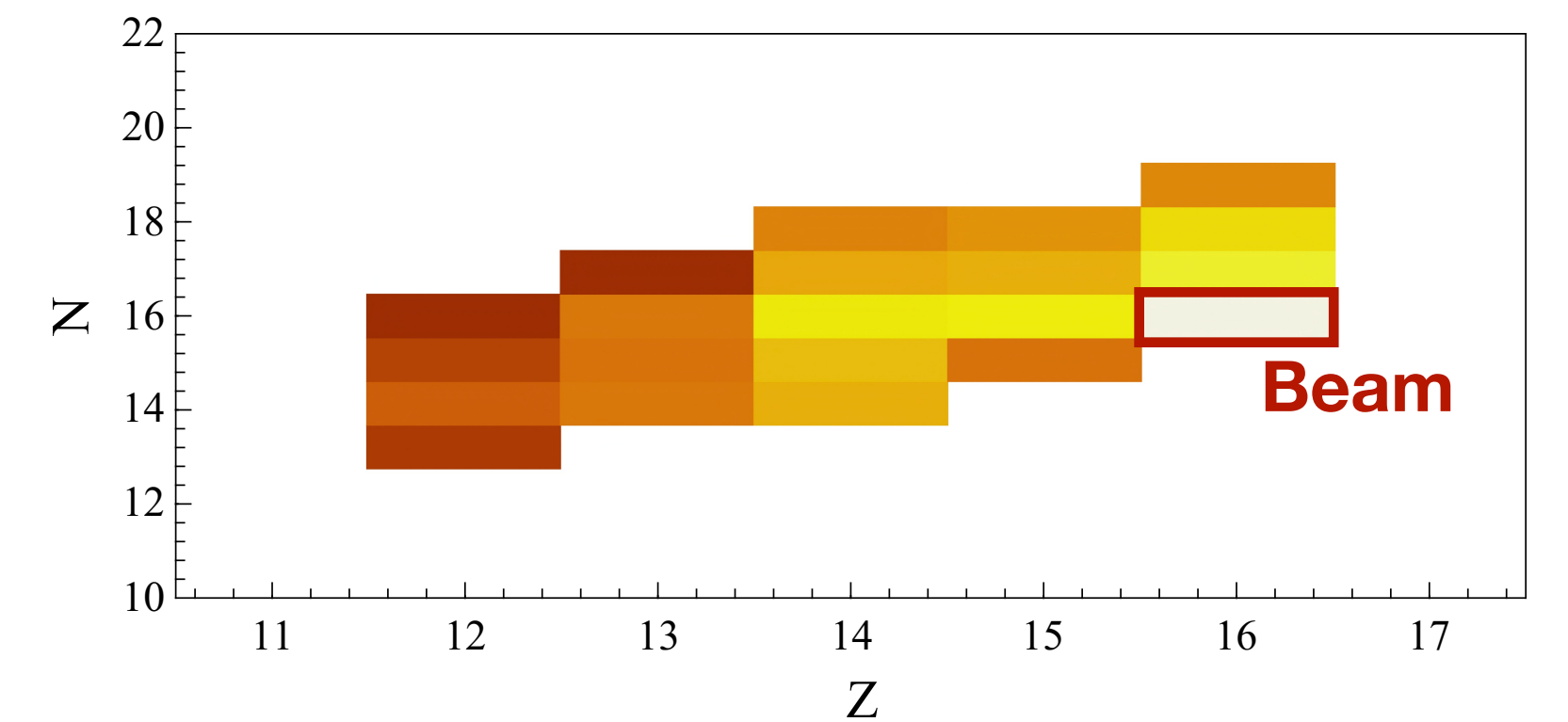
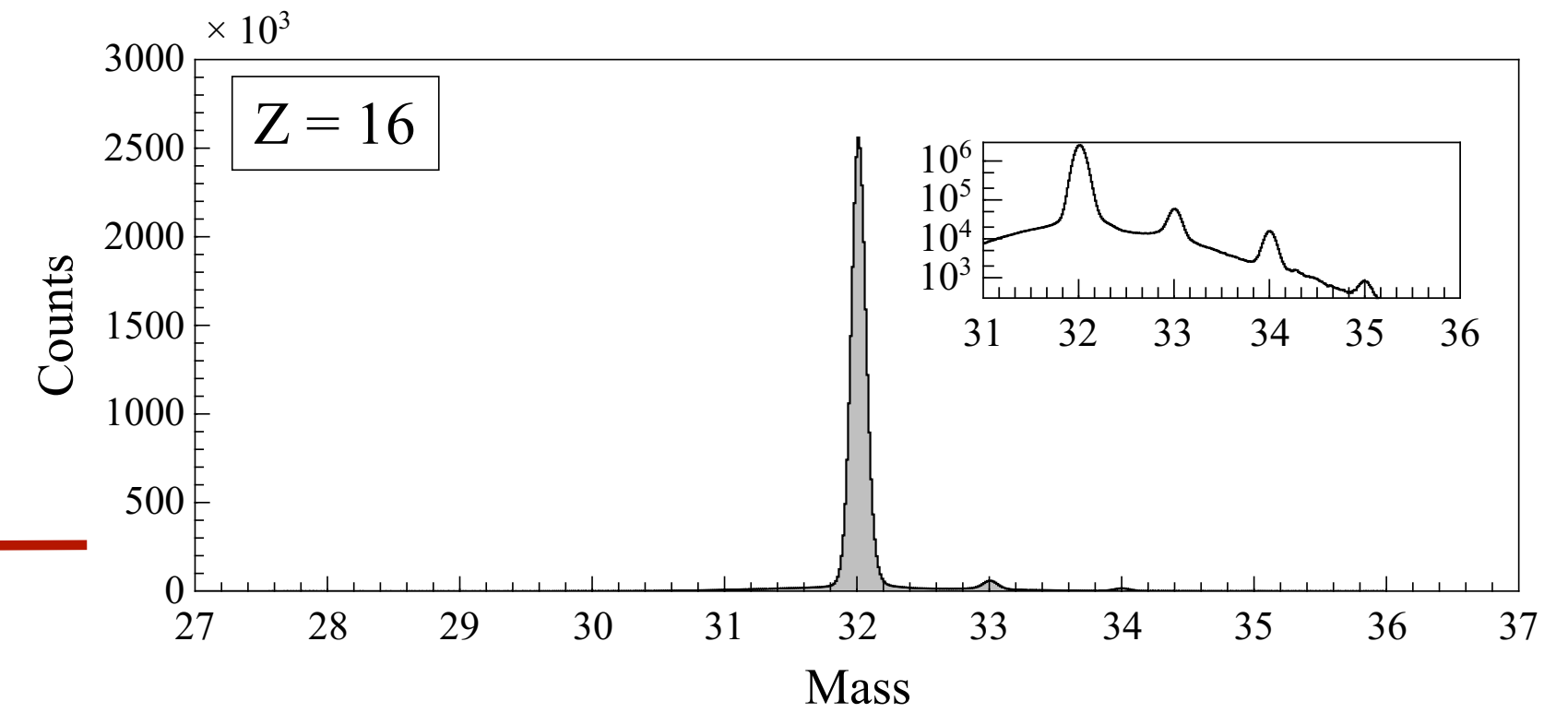
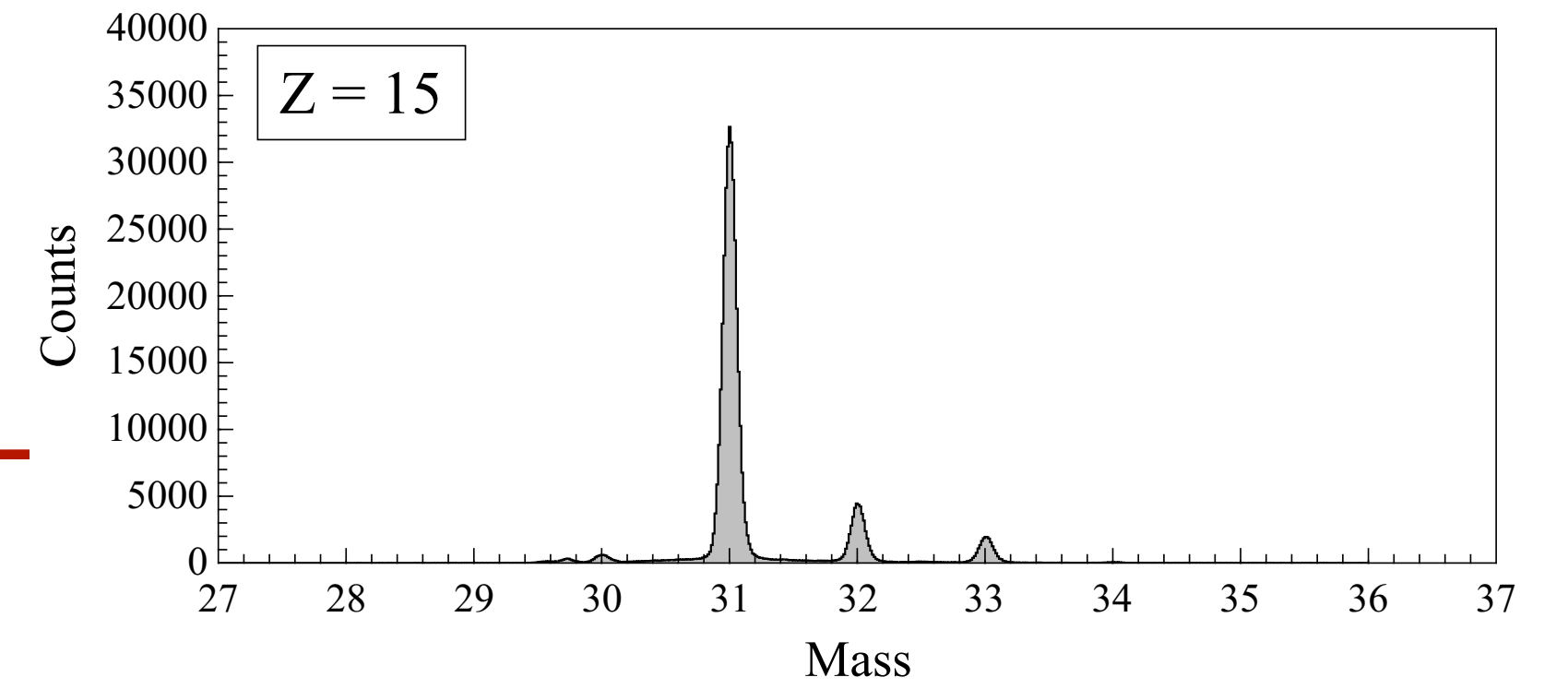


Mass spectra for each Z

$$\frac{\Delta A}{A} \sim \frac{1}{240}$$

Target-like reaction products

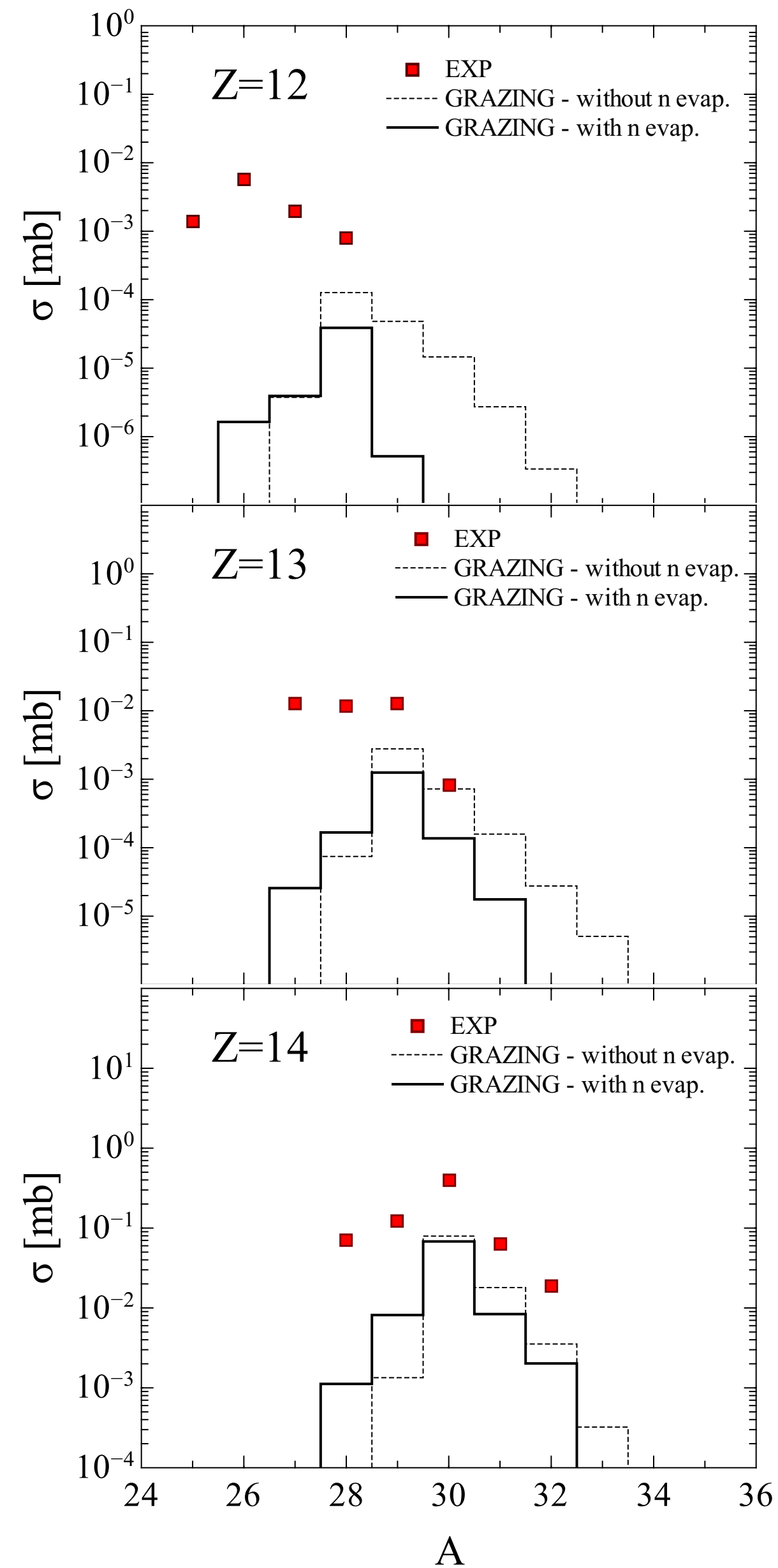
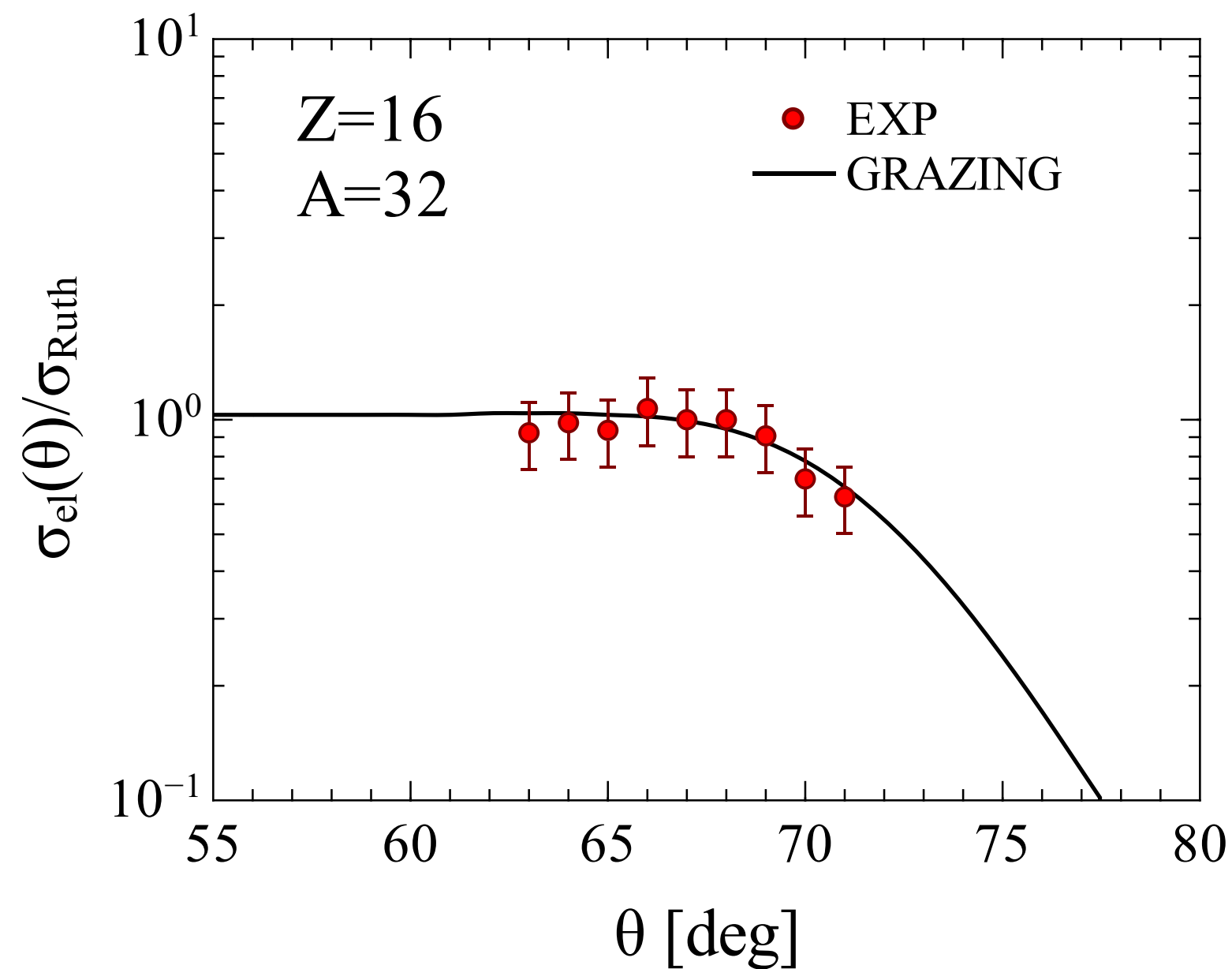
$^{109}\text{Te}$	$^{110}\text{Te}$	$^{111}\text{Te}$	$^{112}\text{Te}$	$^{113}\text{Te}$	$^{114}\text{Te}$	$^{115}\text{Te}$	$^{116}\text{Te}$	$^{117}\text{Te}$
$^{108}\text{Sb}$	$^{109}\text{Sb}$	$^{110}\text{Sb}$	$^{111}\text{Sb}$	$^{112}\text{Sb}$	$^{113}\text{Sb}$	$^{114}\text{Sb}$	$^{115}\text{Sb}$	$^{116}\text{Sb}$
$^{107}\text{Sn}$	$^{108}\text{Sn}$	$^{109}\text{Sn}$	$^{110}\text{Sn}$	$^{111}\text{Sn}$	$^{112}\text{Sn}$	$^{113}\text{Sn}$	$^{114}\text{Sn}$	$^{115}\text{Sn}$
$^{106}\text{In}$	$^{107}\text{In}$	$^{108}\text{In}$	$^{109}\text{In}$	$^{110}\text{In}$	$^{111}\text{In}$	$^{112}\text{In}$	$^{113}\text{In}$	$^{114}\text{In}$
$^{105}\text{Cd}$	$^{106}\text{Cd}$	$^{107}\text{Cd}$	$^{108}\text{Cd}$	$^{109}\text{Cd}$	$^{110}\text{Cd}$	$^{111}\text{Cd}$	$^{112}\text{Cd}$	$^{113}\text{Cd}$



# Cross section

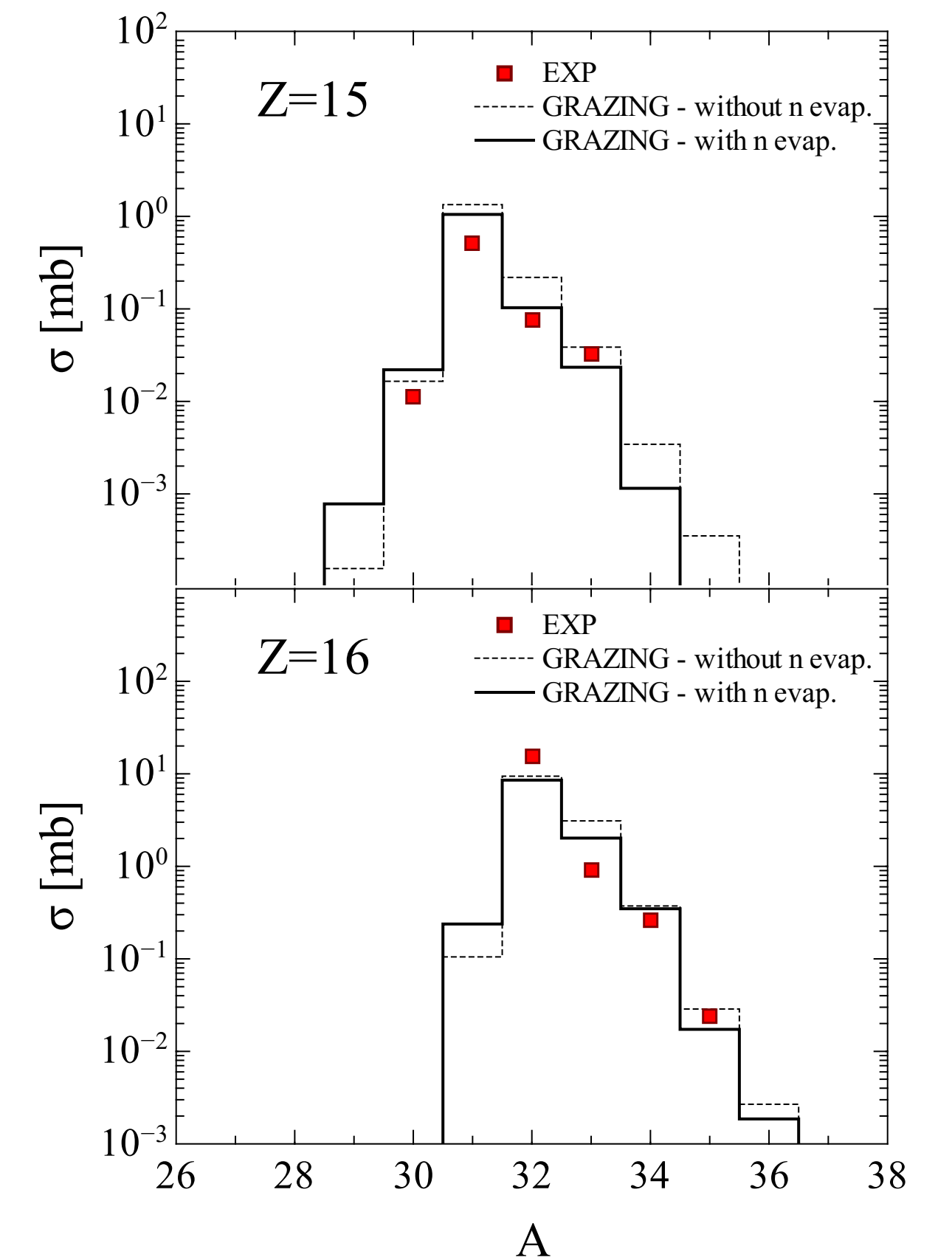
**Angular distribution**  
for the quasi-elastic channel

Comparison with GRAZING  
calculation, normalised on  
the Rutherford cross section



**Inclusive cross sections**  
for all the reaction channels

Comparison with GRAZING  
calculations





# Summary

- The shape coexistence was investigated in the region of **Sn isotopes around  $A \sim 110$** , by performing multi-nucleon transfer reactions near the Coulomb barrier
- The ongoing analysis will give additional information on the **microscopic structure** of  $^{110-120}\text{Sn}$ , especially on **reaction mechanism, p/n character of excitations and deformed structures.**

# Perspectives

- New lifetime measurements @ IFIN of  $^{114-120}\text{Sn}$  isotopes scheduled in 2024!
- Final results will be combined and compared with MCSM calculation to pin down the nature of the shape coexistence phenomena in this region



# Thank you for your attention!

## Collaboration:

G. Corbari<sup>1,2</sup>, P. Pellegrini<sup>1</sup>, S. Bottoni<sup>1,2</sup>, F.C.L. Crespi<sup>1,2</sup>, S. Leoni<sup>1,2</sup>, N. Mărginean<sup>4</sup>, M. Ciemała<sup>3</sup>, B. Fornal<sup>3</sup>, P. Aguilera<sup>7</sup>, M. Balogh<sup>6</sup>, J. Benito<sup>7</sup>, G. Benzoni<sup>2</sup>, M. Boromiza<sup>4</sup>, D. Brugnara<sup>6</sup>, F. Camera<sup>1,2</sup>, S. Carollo<sup>7</sup>, G. Ciconali<sup>1,2</sup>, N. Cieplicka-Orynczak<sup>3</sup>, C. Clisu-Stan<sup>4</sup>, G. Colombi<sup>8,1</sup>, C. Costache<sup>4</sup>, C. Cuciuc<sup>5</sup>, A. Ertoprak<sup>6</sup>, R. Escudeiro<sup>7</sup>, F. Galtarossa<sup>6</sup>, D. Filipescu<sup>4</sup>, N. Florea<sup>4</sup>, I. Gheorge<sup>4</sup>, A. Goasduff<sup>6</sup>, A. Gottardo<sup>6</sup>, A. Ionescu<sup>4</sup>, Ł. Iskra<sup>3</sup>, S.M. Lenzi<sup>7</sup>, R. Lică<sup>4</sup>, R. Mărginean<sup>4</sup>, M. Matejska-Minda<sup>3</sup>, D. Mengoni<sup>7</sup>, C. Michelagnoli<sup>8</sup>, C. Mihai<sup>4</sup>, B. Million<sup>2</sup>, D.R. Napoli<sup>6</sup>, C. Neacșu<sup>4</sup>, A. Negreț<sup>4</sup>, C.R. Niță<sup>4</sup>, A. Olăcel-Coman<sup>4</sup>, T. Otsuka<sup>10</sup>, J. Pellumaj<sup>6</sup>, R.M. Pèrez-Vidal<sup>6</sup>, S. Pigliapoco<sup>7</sup>, E. Pilotto<sup>7</sup>, M. Poletti<sup>7</sup>, F. Recchia<sup>7</sup>, K. Rezyunkina<sup>7</sup>, M. Sedlak<sup>6</sup>, M. Sferrazza<sup>9</sup>, L. Stan<sup>4</sup>, Y. Tsunoda<sup>10</sup>, A. Turturică<sup>4</sup>, S. Ujeniuc<sup>4</sup>, J.J. Valiente-Dobòn<sup>6</sup>, O. Wieland<sup>2</sup>, I. Zanon<sup>6</sup>, L. Zago<sup>7</sup>, G. Zhang<sup>7</sup>, H. Zhen<sup>7</sup>

<sup>1</sup> Dipartimento di Fisica, Università degli Studi di Milano, Italy

<sup>2</sup> INFN, Sezione di Milano, Italy

<sup>3</sup> Institute of Nuclear Physics, IFJ-PAN, Krakow, Poland

<sup>4</sup> Horia Hulubei National Institute for Physics and Nuclear Engineering, Măgurele, Romania

<sup>5</sup> Extreme Light Infrastructure, Nuclear Physics, Măgurele, Romania

<sup>6</sup> INFN, Laboratori Nazionali di Legnaro, Italy

<sup>7</sup> Dipartimento di Fisica and INFN, Sezione di Padova, Padova, Italy

<sup>8</sup> Institut Laue-Langevin, Grenoble, France

<sup>9</sup> Université libre de Bruxelles (ULB), Belgium

<sup>10</sup> University of Tokyo, Tokyo, Japan



UNIVERSITÀ  
DEGLI STUDI  
DI MILANO



UNIVERSITÀ  
DEGLI STUDI  
DI PADOVA

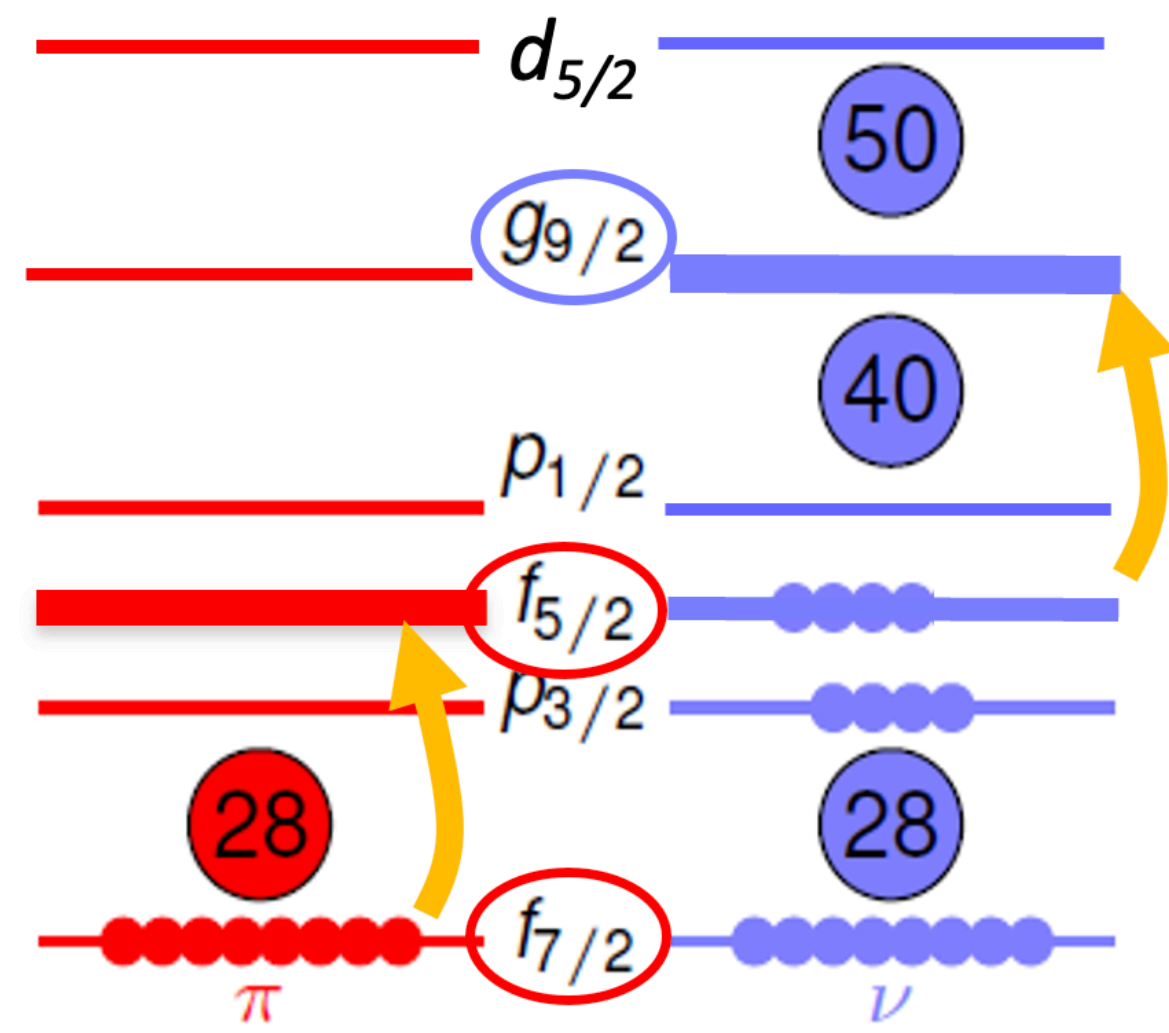


ULB

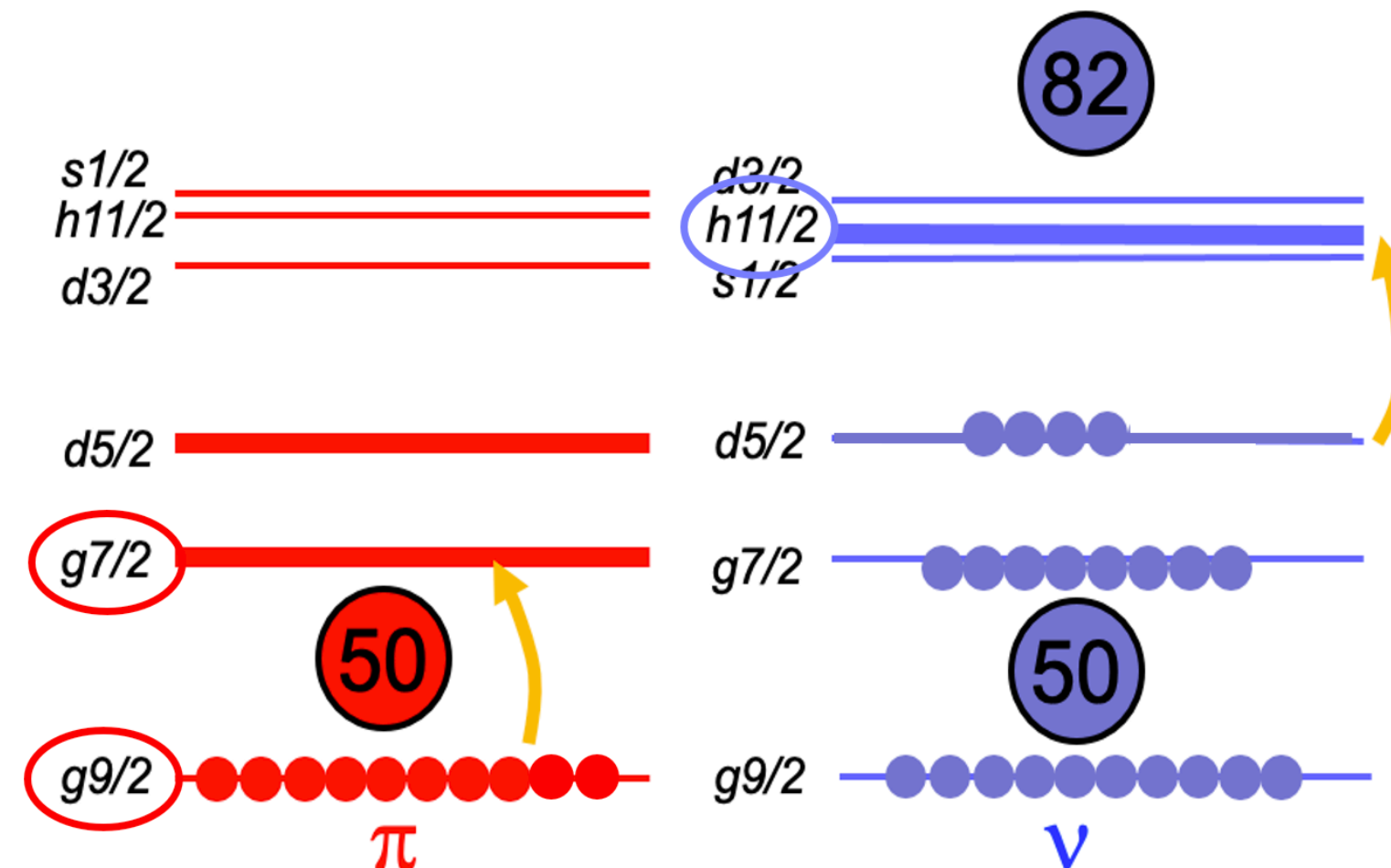


# Backup slides

# Backup - Monopole-driven excitations



**$^{64}\text{Ni}$**



**$^{112}\text{Sn}$**

- Spontaneous symmetry breaking due to p-n interaction
- Driven by the **monopole part of the tensor force**
- Neutron excitation in  $g_{9/2}$  induces a **reduction of the  $f_{5/2}$ - $f_{7/2}$  splitting** ( $Z=28$  shell gap)



**Analogy with  $^{112}$ - $^{114}\text{Sn}$  isotopes**

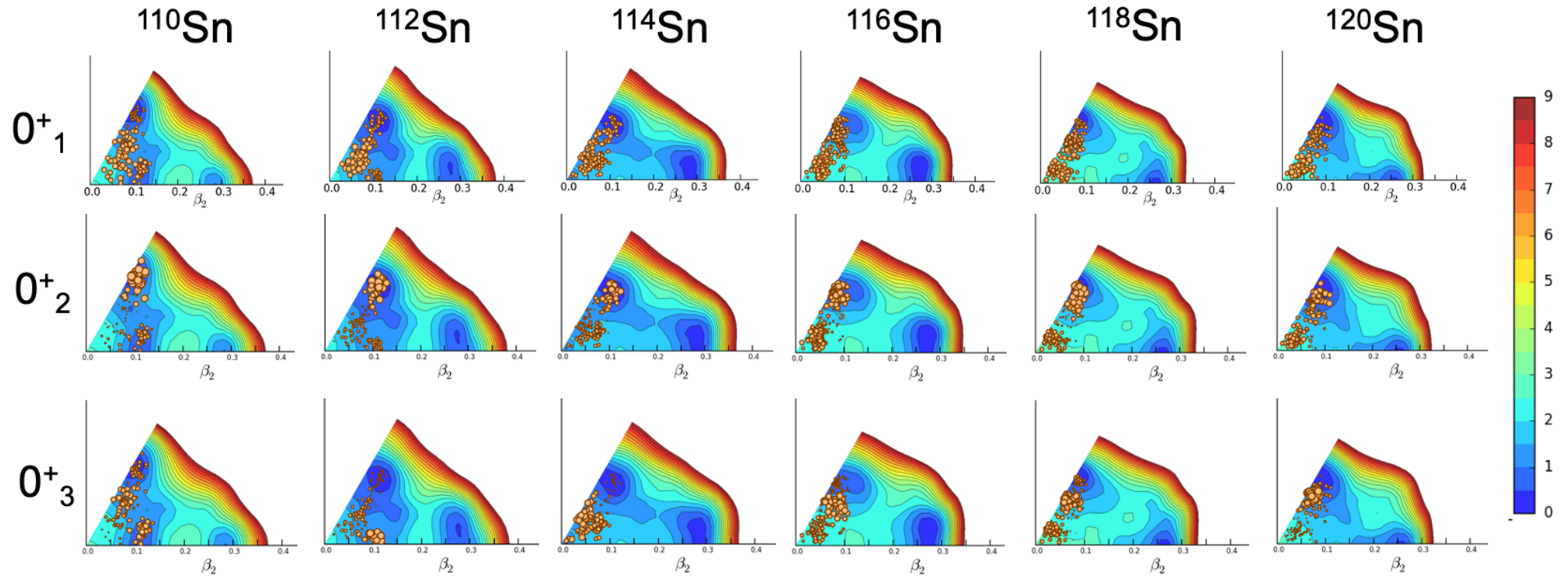
Neutron excitation in  $h_{11/2}$  induces a **reduction of the  $g_{7/2}$ - $g_{9/2}$  splitting** ( $Z=50$  shell gap)

S. Leoni et al., Phys. Rev. Lett. 118, 162502 (2017)

N. Mărginean et al., Phys. Rev. Lett. 125, 102502 (2020)



# Backup - MCSM calculations



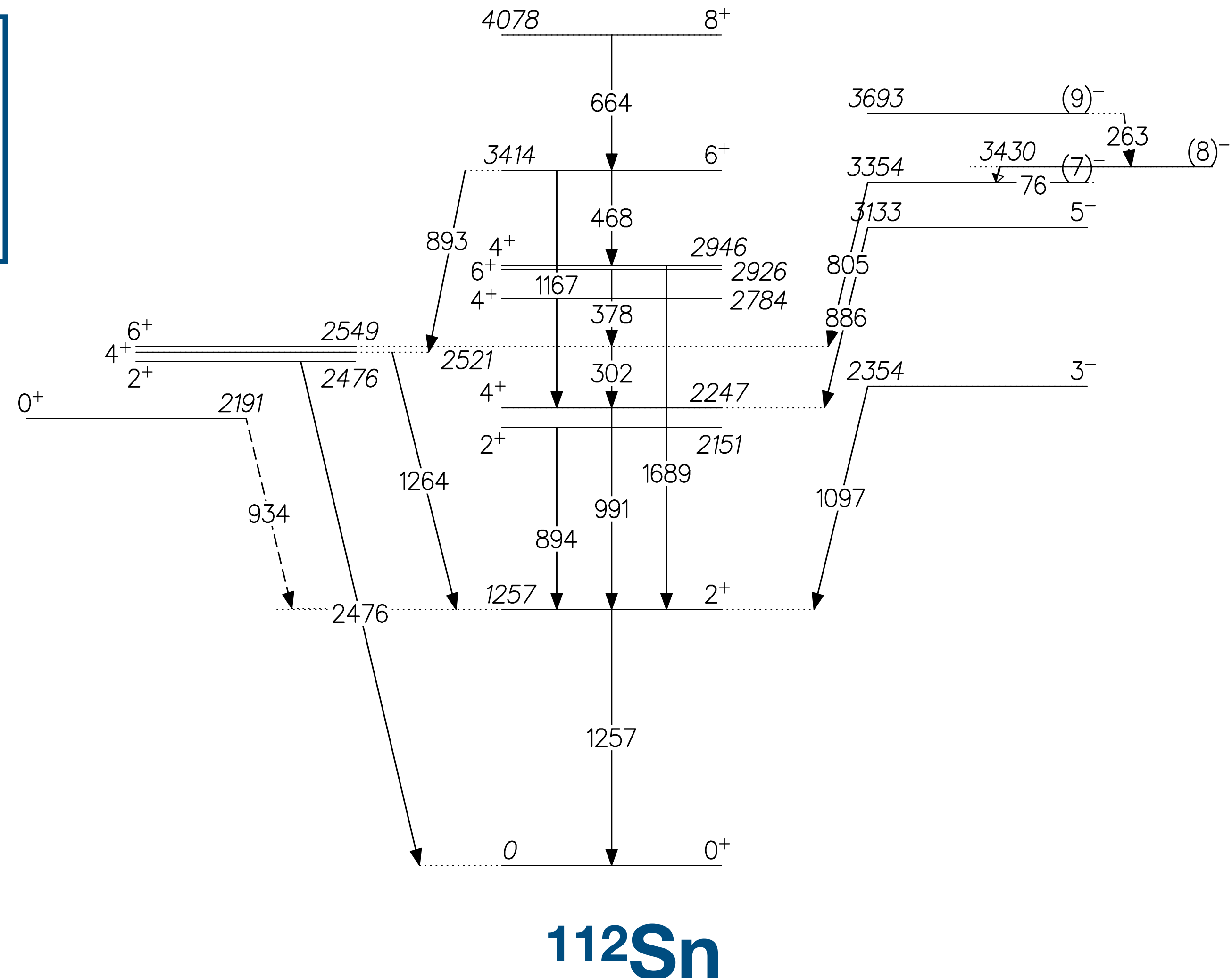
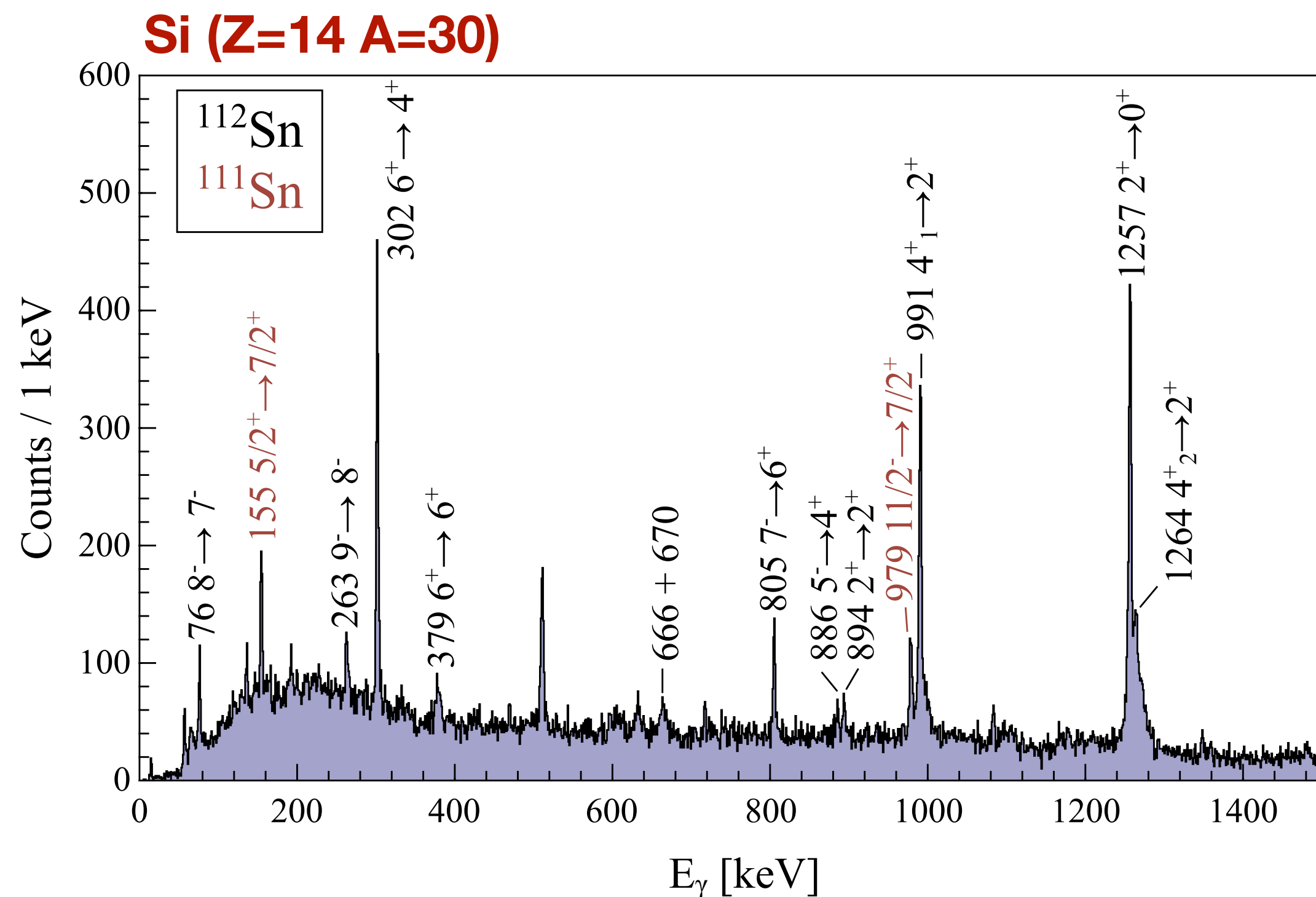
**Preliminary calculations!**

T. Otzuka, Y. Tsunoda, to be published.

T. Togashi et al., Phys. Rev. Lett. 121, 062501 (2018).

# Backup - Ion-gated $\gamma$ spectra

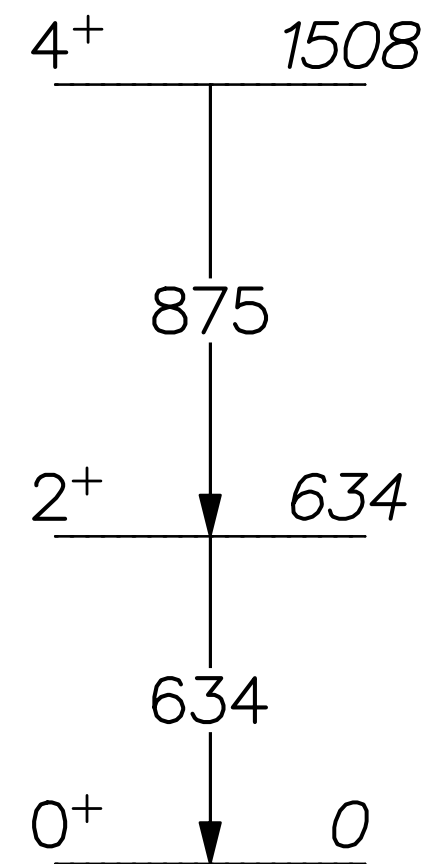
- Study of population of states with MNT
- Observation of low-spin states up to  $J_{max} = 9$
- Transitions of states with  $T_{1/2} \gtrsim ps$



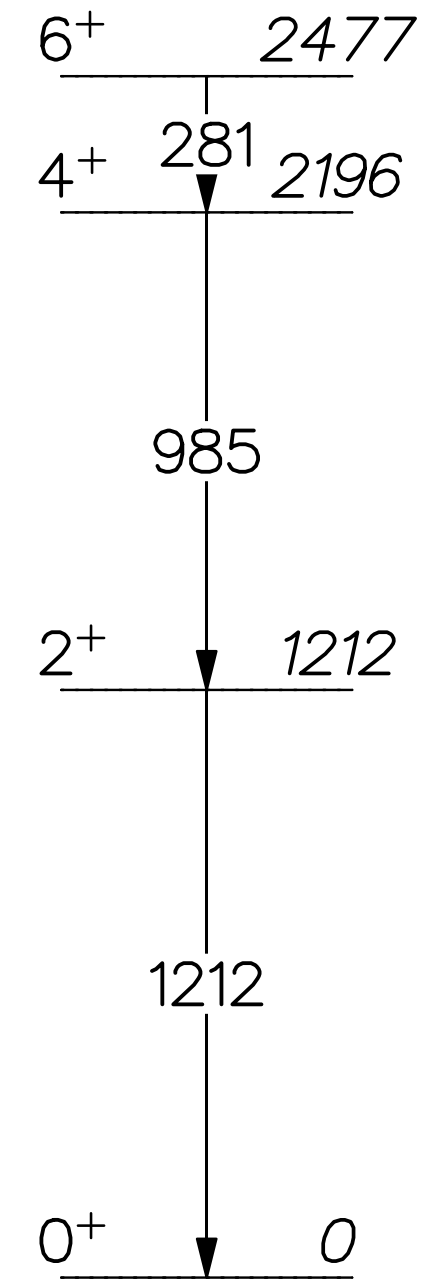


# Backup

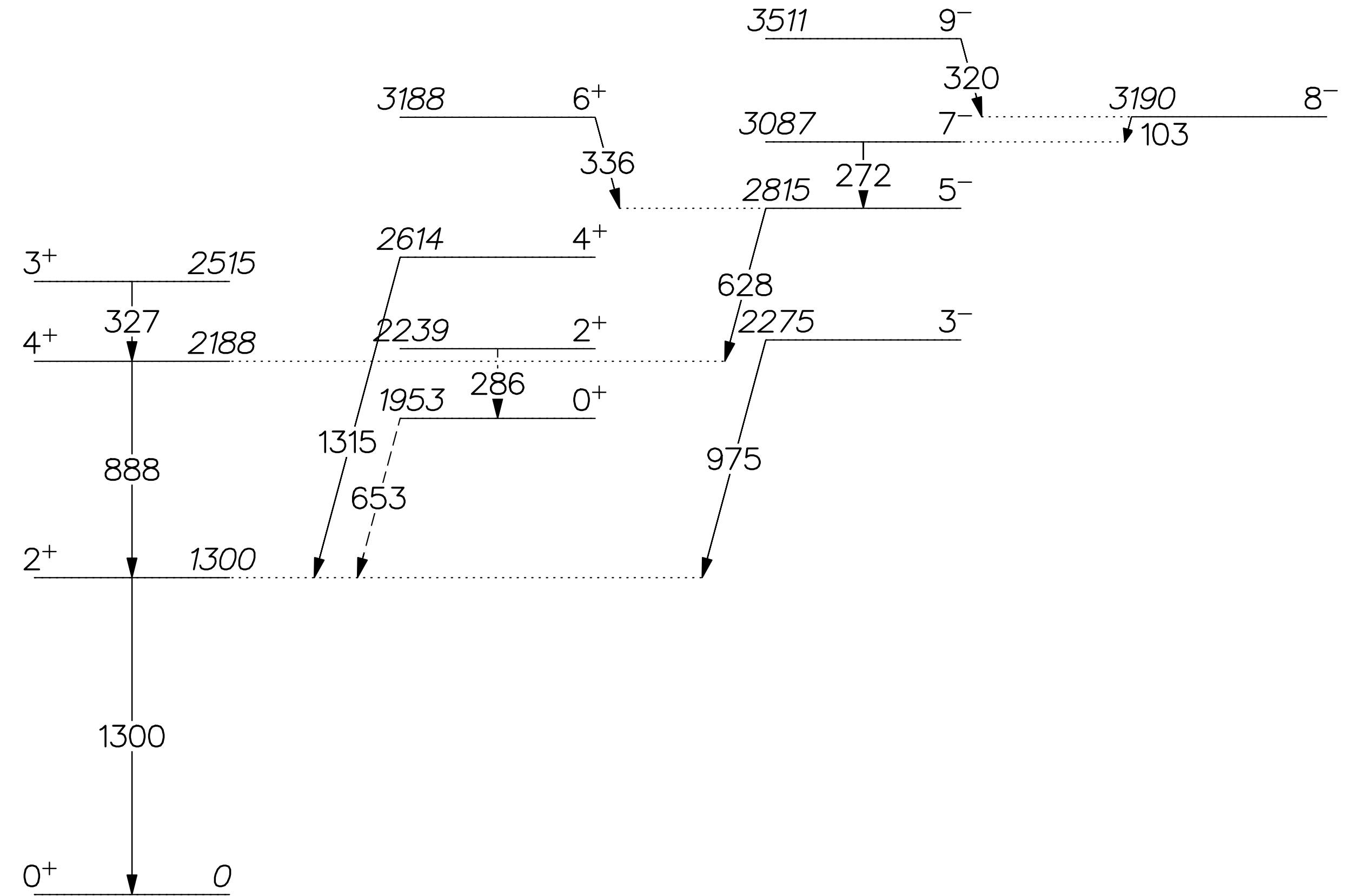
## AGATA-PRISMA level schemes



$^{108}\text{Cd}$



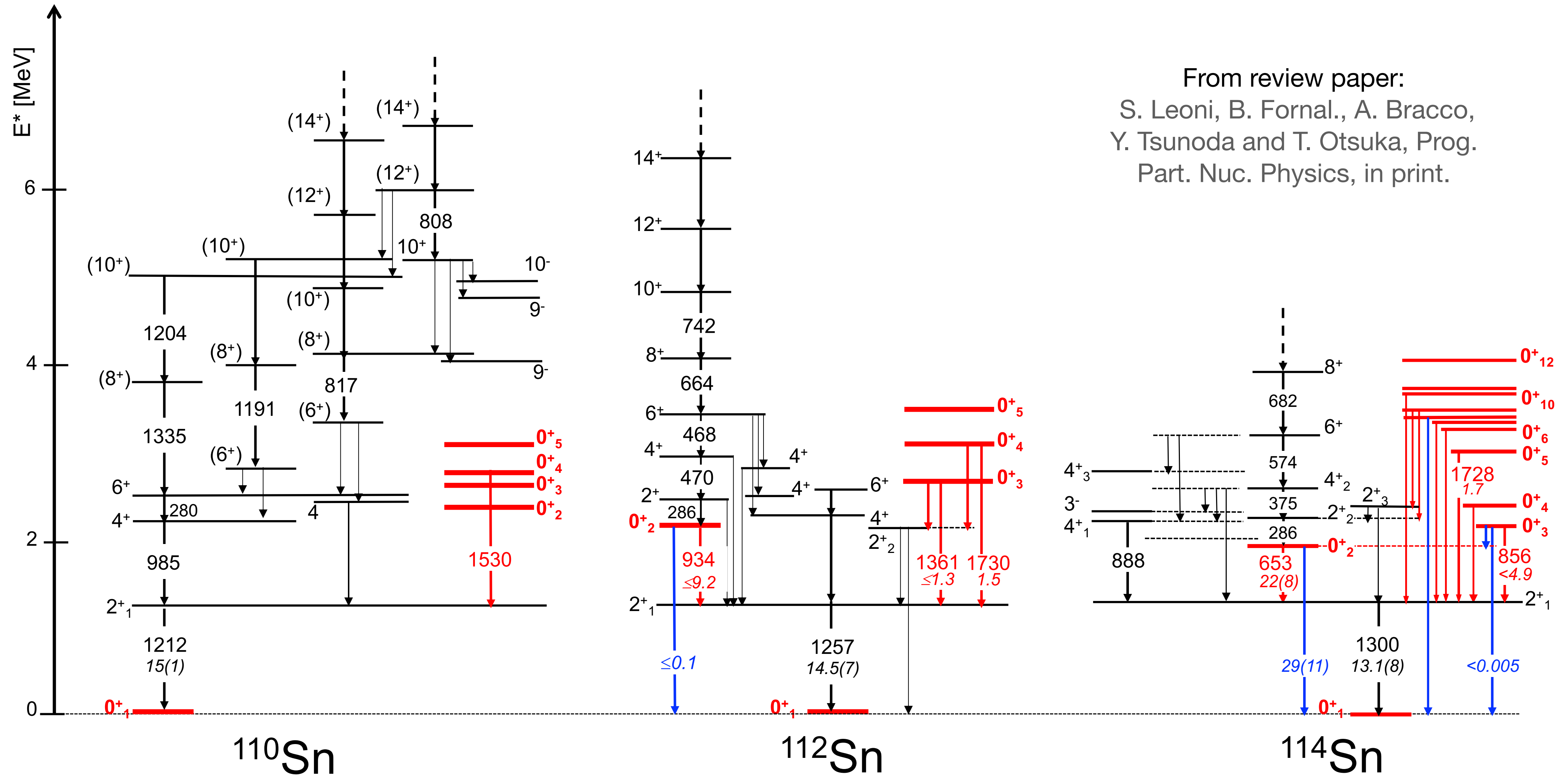
$^{110}\text{Sn}$



$^{114}\text{Sn}$

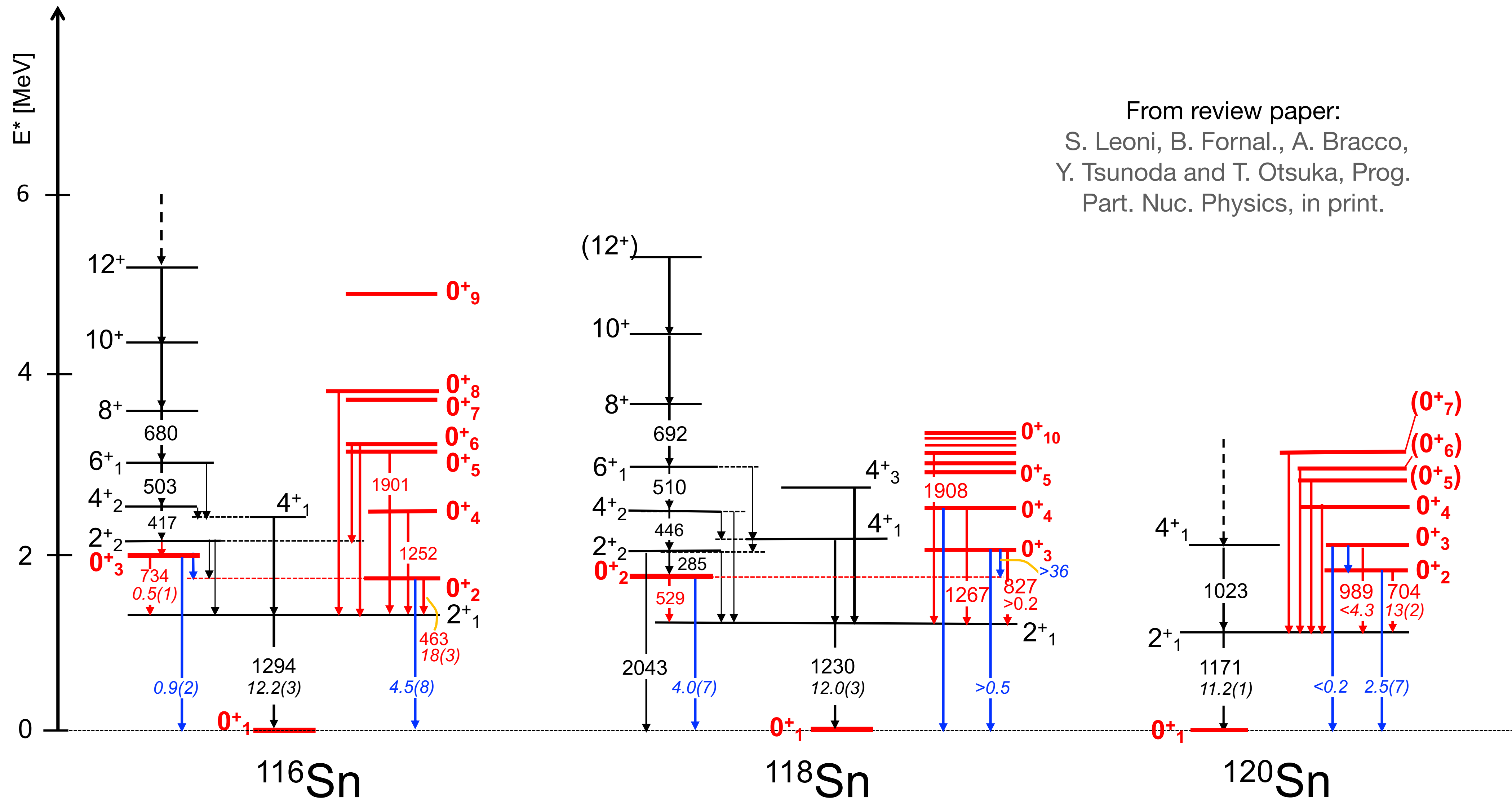


# Backup - Level schemes 110-114Sn





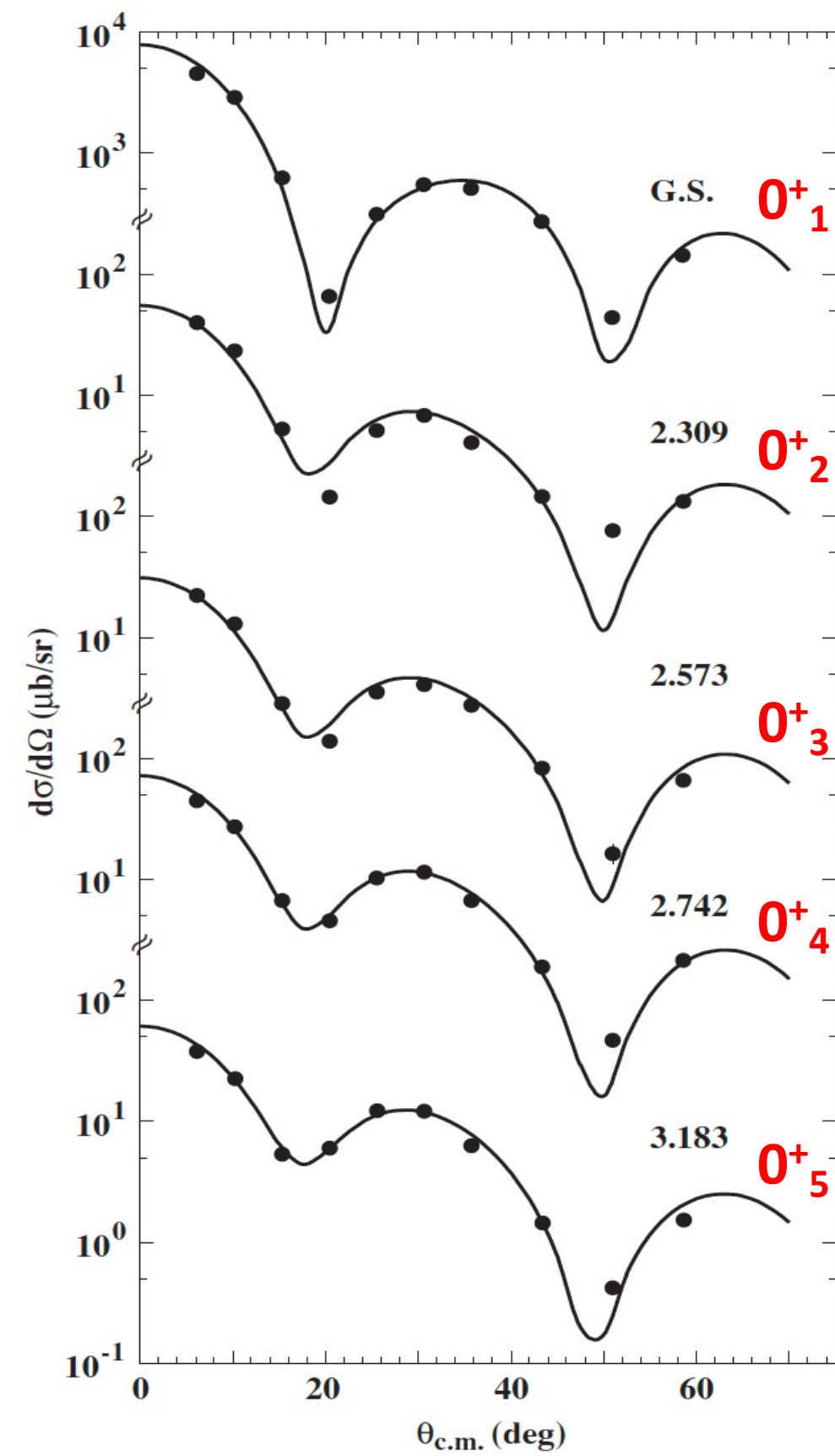
# Backup - Level schemes $^{116-120}\text{Sn}$



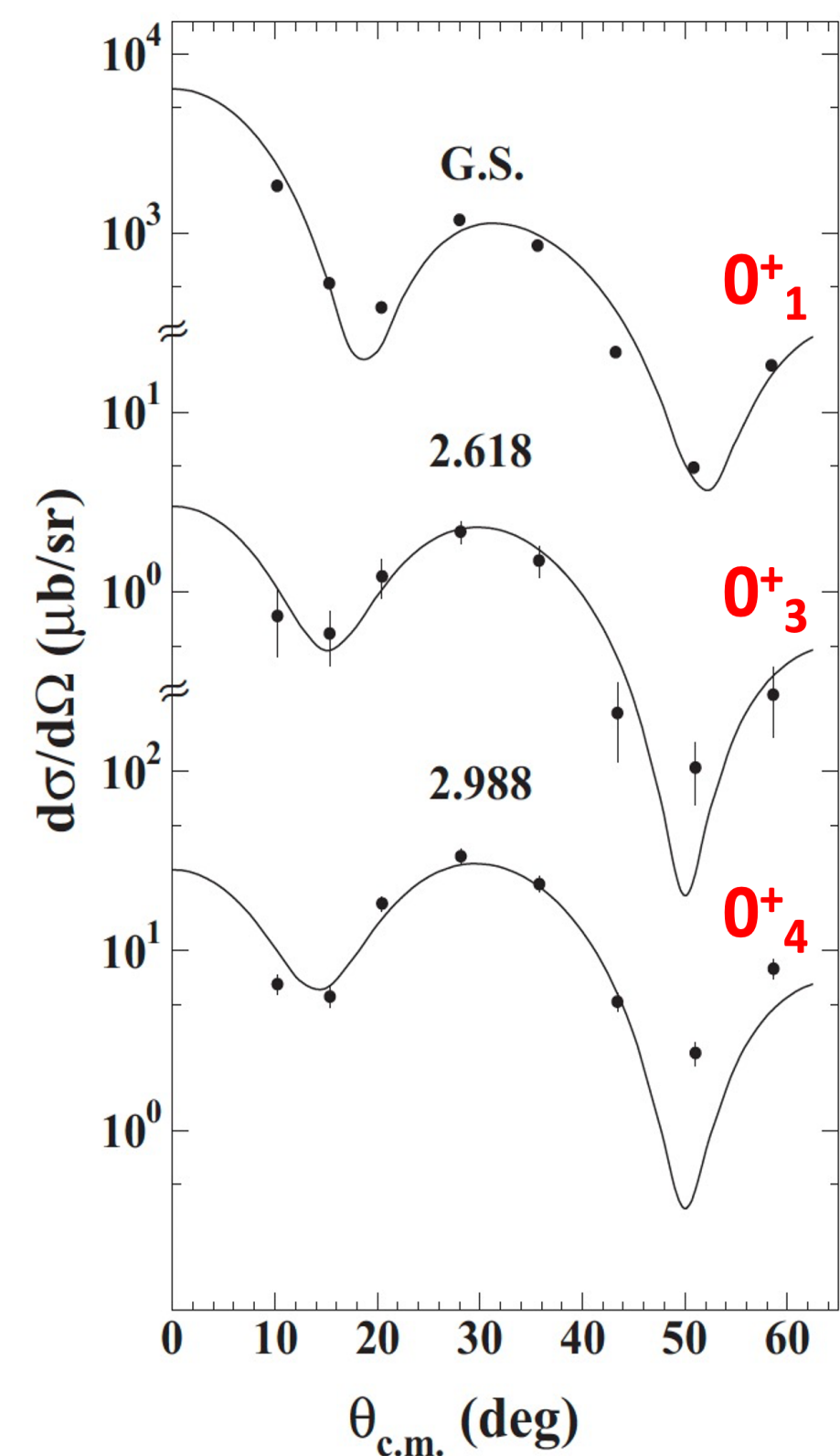
From review paper:  
S. Leoni, B. Fornal., A. Bracco,  
Y. Tsunoda and T. Otsuka, Prog.  
Part. Nuc. Physics, in print.

# Backup - (p,t) reactions

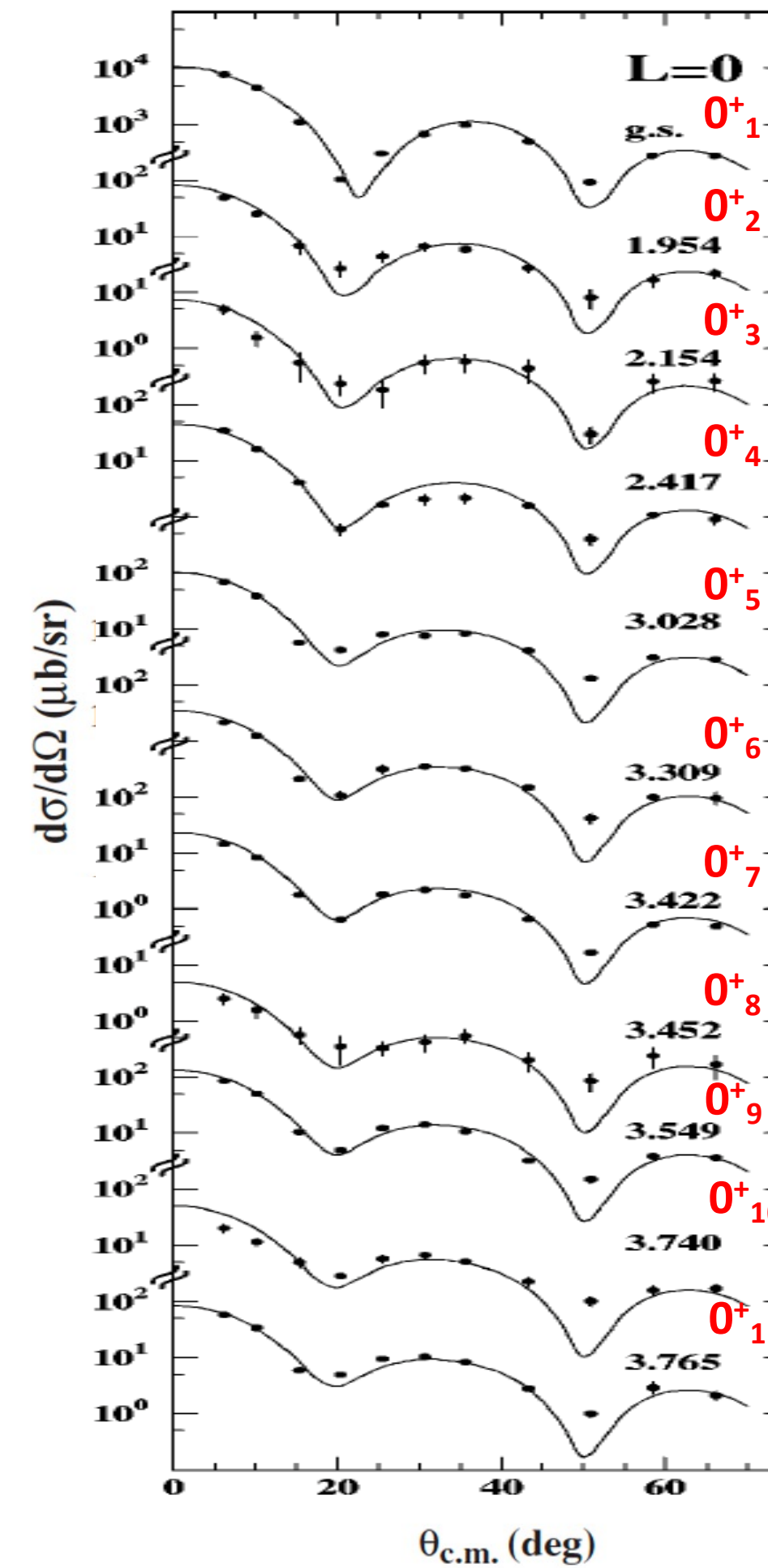
$^{110}\text{Sn}$



$^{112}\text{Sn}$



$^{114}\text{Sn}$

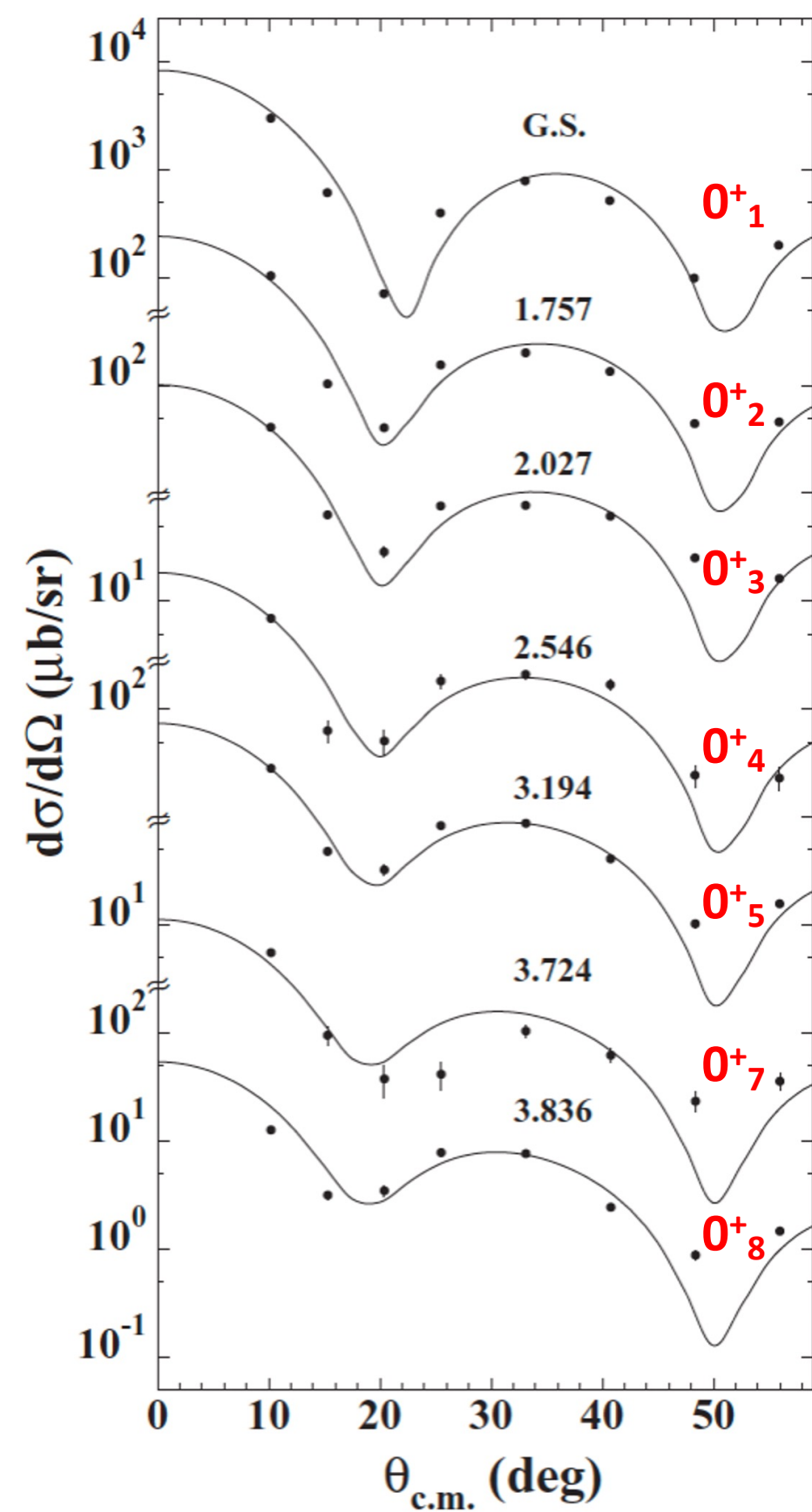


From review paper:  
S. Leoni, B. Fornal., A. Bracco,  
Y. Tsunoda and T. Otsuka, Prog.  
Part. Nuc. Physics, in print.

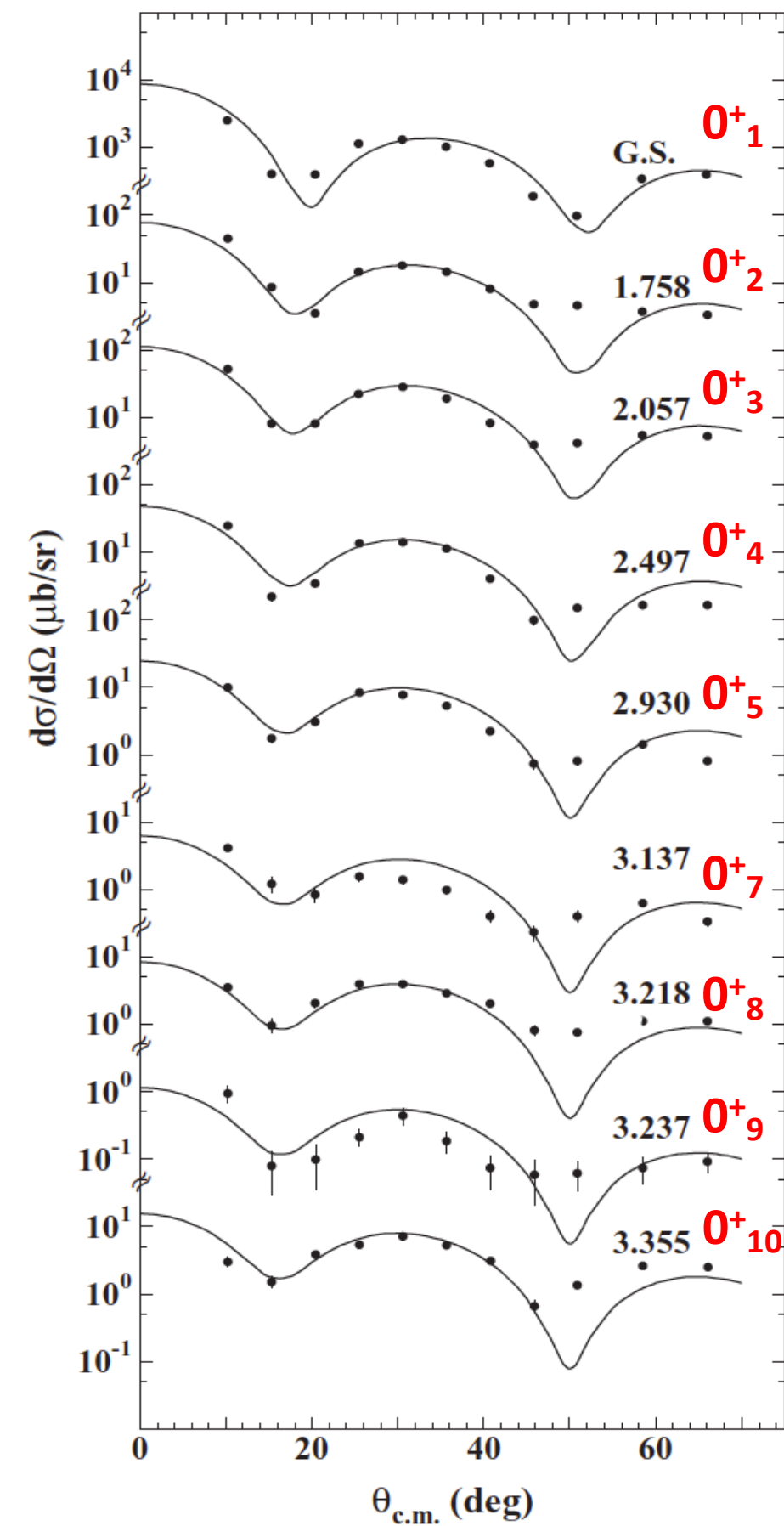


# Backup - (p,t) reactions

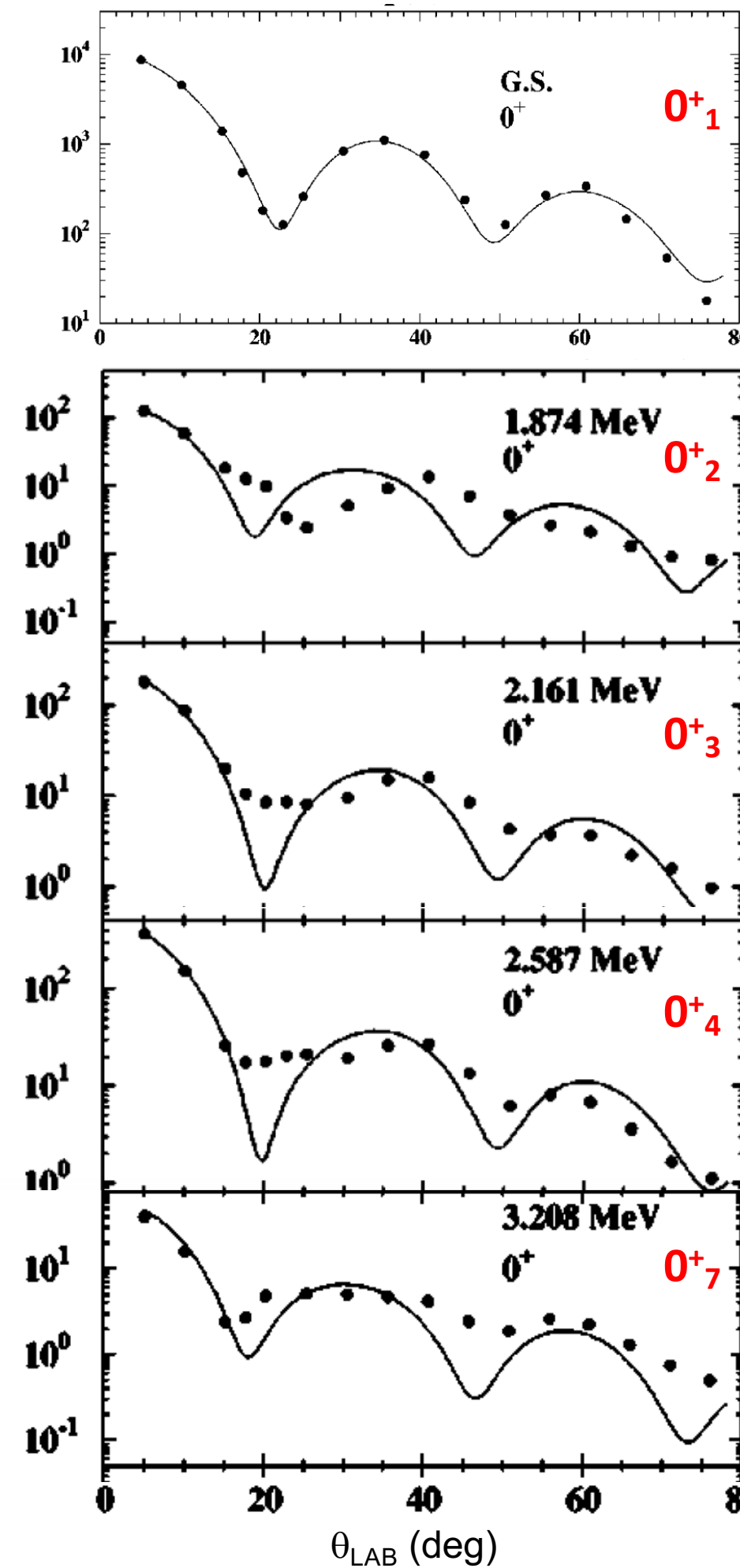
$^{116}\text{Sn}$



$^{118}\text{Sn}$



$^{120}\text{Sn}$



From review paper:  
S. Leoni, B. Fornal., A. Bracco,  
Y. Tsunoda and T. Otsuka, Prog.  
Part. Nuc. Physics, in print.