

The rise of Particle Physics

Rome, 23–24 Sept 2024

Riccardo Barbieri
SNS, Pisa

1. A brief appendix to Alvaro's talk (also in memory of Raul Gatto)
2. Flavour in the "mid term" of BSM

After Appelquist, Politzer

DeRujula, Glashow

(1975)

DeRujula, Georgi, Glashow

MESON HYPERFINE SPLITTINGS AND LEPTONIC DECAYS

R. BARBIERI*, **R. GATTO****, R. KÖGERLER* and Z. KUNSZT*

**CERN-Geneva-Switzerland*

***Istituto di Fisica and Istituto Nazionale di Fisica Nucleare, Roma, Italy*

Received 3 May 1975

**MESON MASSES AND WIDTHS IN A GAUGE THEORY WITH
LINEAR BINDING POTENTIAL**

R. BARBIERI, R. KÖGERLER and Z. KUNSZT *

CERN, Geneva

and

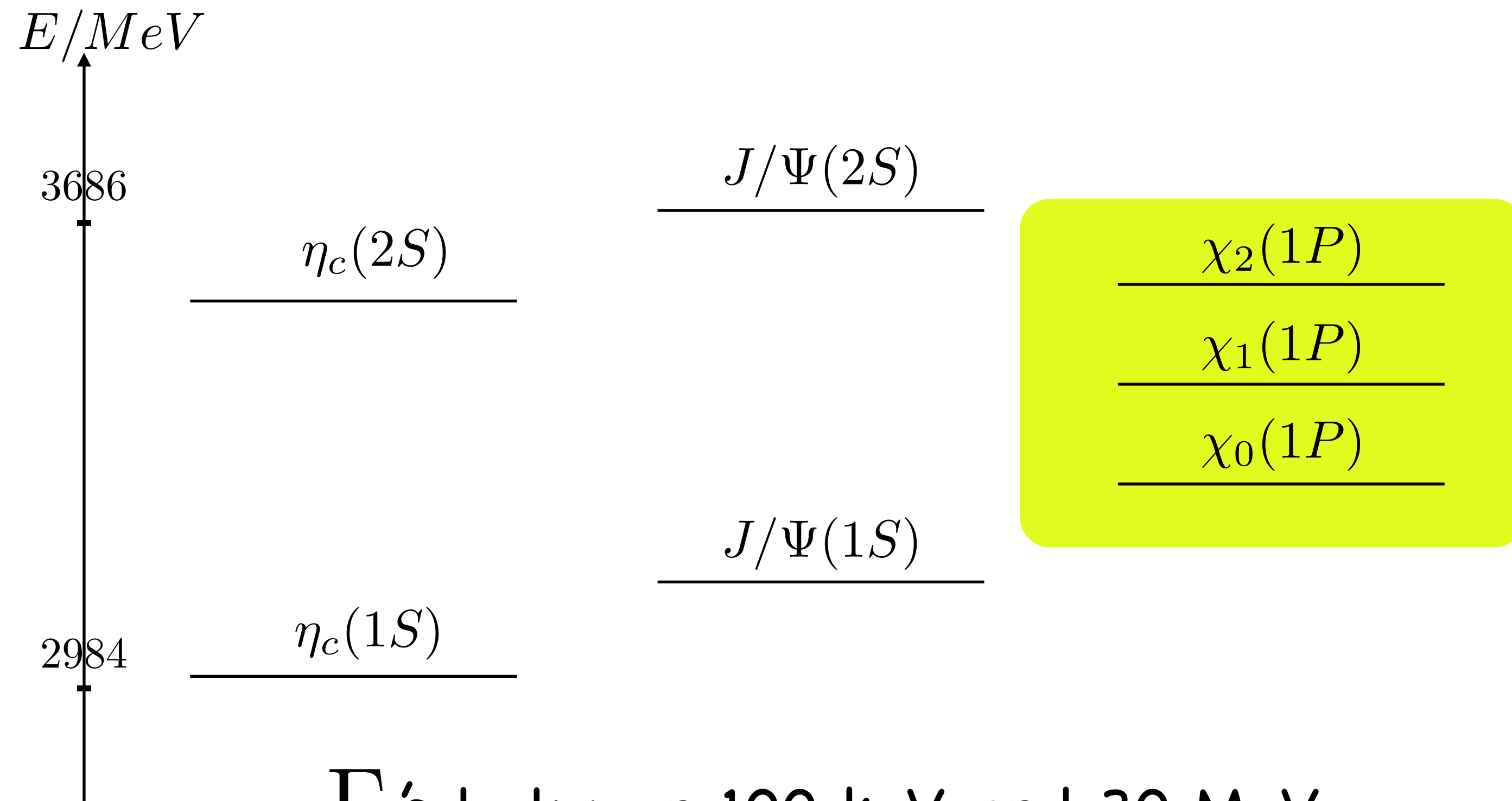
R. GATTO

Istituto di Fisica dell'Università, Roma

Received 1 July 1975

The November Revolution

$$e^+e^- \rightarrow J/\Psi \rightarrow e^+e^- \quad \text{Discovery: Nov 1974}$$



Γ 's between 100 keV and 30 MeV

What about the P waves?

CALCULATION OF THE ANNIHILATION RATE OF P WAVE QUARK-ANTIQUARK BOUND STATES

R. BARBIERI, **R. GATTO*** and R. KÖGERLER
CERN, Geneva, Switzerland

Received 27 October 1975

SINGULAR BINDING DEPENDENCE IN THE HADRONIC WIDTHS OF 1^{++} AND 1^{+-} HEAVY QUARK ANTIQUARK BOUND STATES

R. BARBIERI and **R. GATTO***
CERN, Geneva, Switzerland

and

E. REMIDDI
*Istituto di Fisica dell'Università, Bologna,
Istituto Nazionale di Fisica Nucleare, Sezione di Bologna, Italy*

Received 10 February 1976

$$\Gamma_{\text{ann}}(0^{++}) = \frac{96\alpha_s^2}{M^4} |\phi_p'(0)|^2, \quad \Gamma_{\text{ann}}(2^{++}) = \frac{128}{5} \frac{\alpha_s^2}{M^4} |\phi_p'(0)|^2$$

$$\Gamma_{\text{ann}}(1^{++}) \approx \frac{n}{3} \frac{128}{3\pi} \frac{\alpha_s^3}{M^4} |\phi_1'(0)|^2 \lg \frac{4m^2}{4m^2 - M^2}$$

The annihilation rates into hadrons of P-wave heavy quark-antiquark bound states are calculated within SU(3) colour gauge theory (in particular for the charm scheme). An interesting feature we find is a logarithmic divergence for small binding for the states 1^{++} and 1^{+-} . Implications for the asymptotic freedom approach to the decay rates of the new particles are discussed. An attempt to use quantitatively the obtained results for all the C-even P-waves gives

$$\Gamma_{\text{ann}}(0^{++}) : \Gamma_{\text{ann}}(2^{++}) : \Gamma_{\text{ann}}(1^{++}) \approx 15 : 4 : 1.$$

$^3P_{0,1,2}$ parameter measurements



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Physics Letters B 533 (2002) 237–242

PHYSICS LETTERS B

www.elsevier.com/locate/npe

E760

New measurements of the resonance parameters of the $\chi_{c0}(1^3P_0)$ state of charmonium



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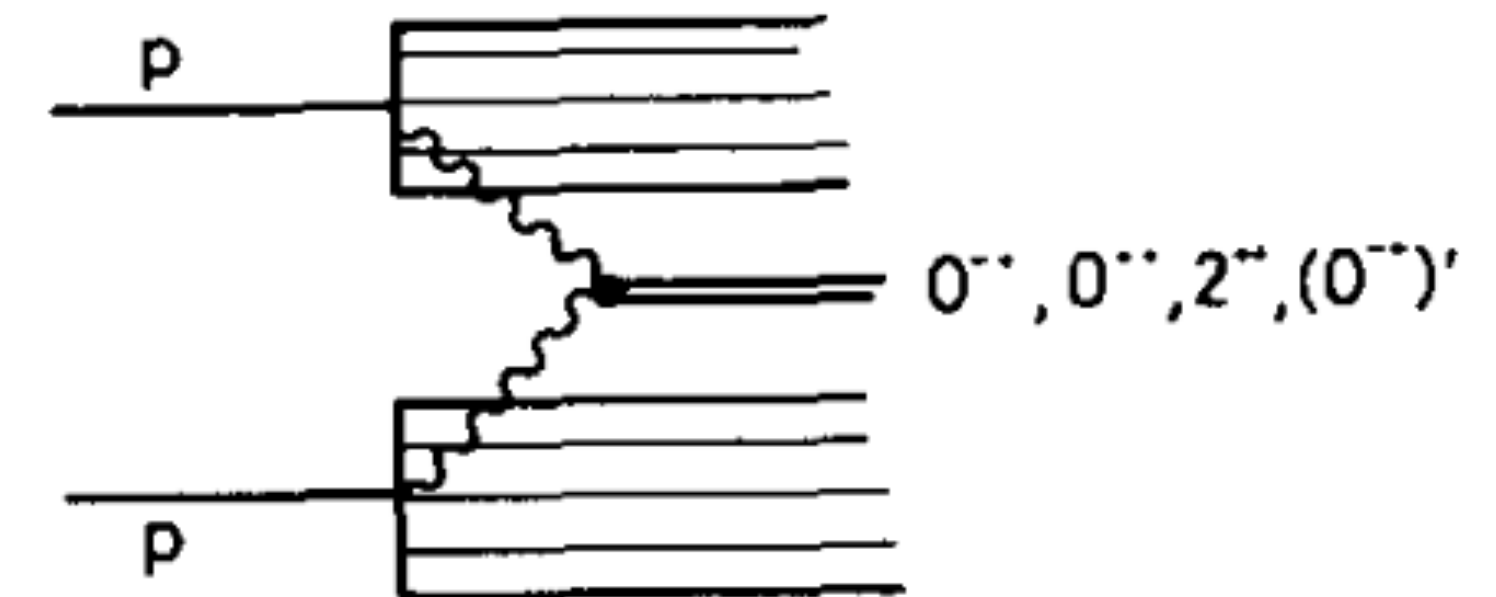
Nuclear Physics B 717 (2005) 34–47

NUCLEAR
PHYSICS B

E385

Measurement of the resonance parameters of the $\chi_1(1^3P_1)$ and $\chi_2(1^3P_2)$ states of charmonium formed in antiproton–proton annihilations

Fermilab



About 30 years after
the November revolution

SINGULAR BINDING DEPENDENCE IN THE HADRONIC WIDTHS OF
 1^{++} AND 1^{+-} HEAVY QUARK ANTIQUARK BOUND STATES

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First measured in 1986 at Crystal Ball (SLAC)

Now:

$$\Gamma(\chi_{c0}) = 10.5 \pm 0.6 \quad \Gamma(\chi_{c2}) = 1.93 \pm 0.11 \quad \Gamma(\chi_{c1}) = 0.84 \pm 0.04 \quad \text{MeV}$$

$$\Gamma(0^{++}) : \Gamma(2^{++}) : \Gamma(1^{++}) = 12 : 2.4 : 1$$

Needed refinements

⇒ “Colour-singlet” model (+ NLO) $2m$

Relativistic, colour-octet, binding corrections
NRQCD $mv, \Lambda_{QCD}, mv^2, \dots$

Strong Radiative Corrections to Annihilations of Quarkonia in QCD

#8

Riccardo Barbieri (Pisa, Scuola Normale Superiore and INFN, Pisa), E. d'Emilio (Pisa, Scuola Normale Superiore and INFN, Pisa), G. Curci (CERN), E. Remiddi (Bologna U.) (Jan, 1979)

η_c

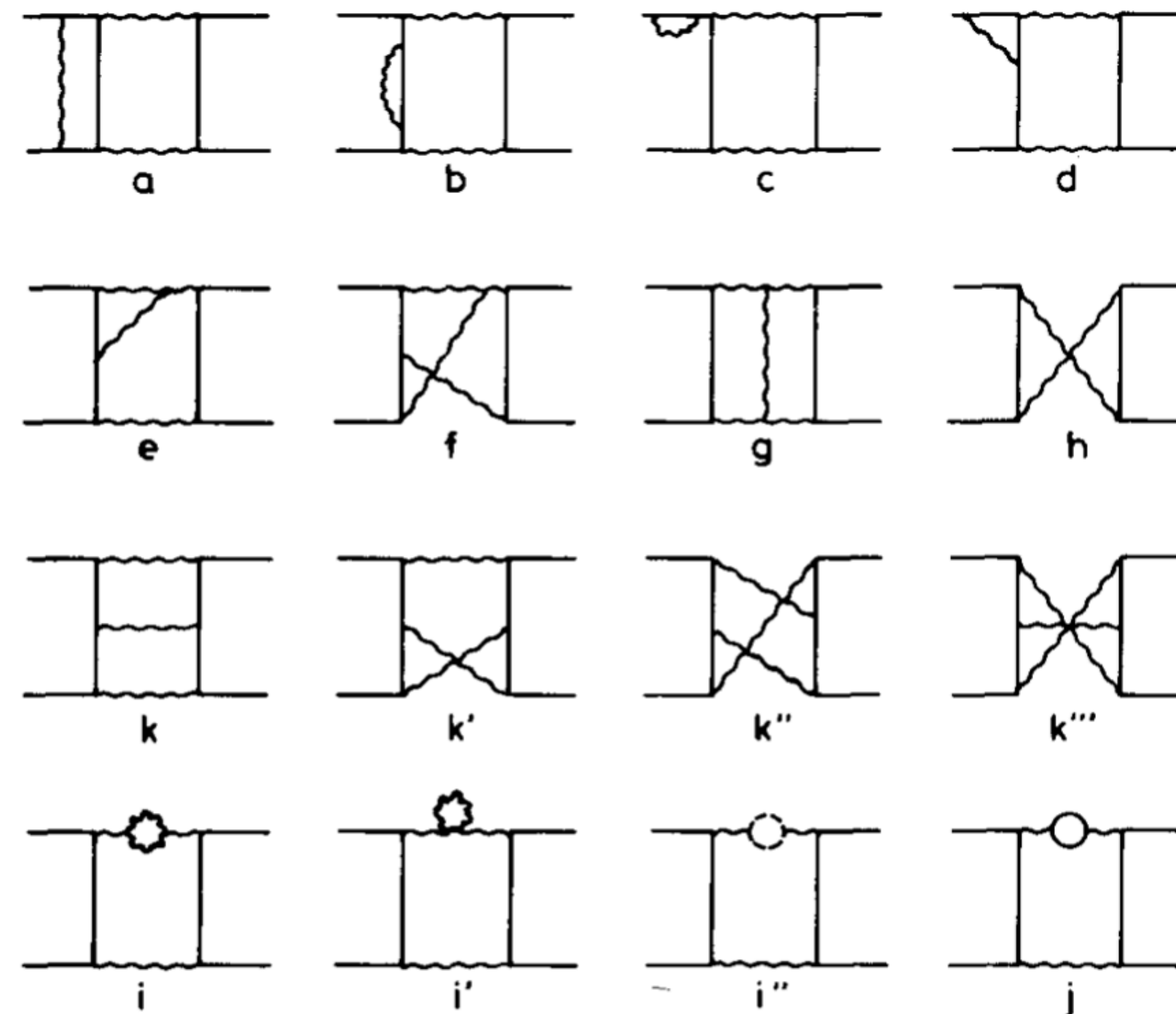
Published in: *Nucl.Phys.B* 154 (1979) 535-546

Strong QCD Corrections to p Wave Quarkonium Decays

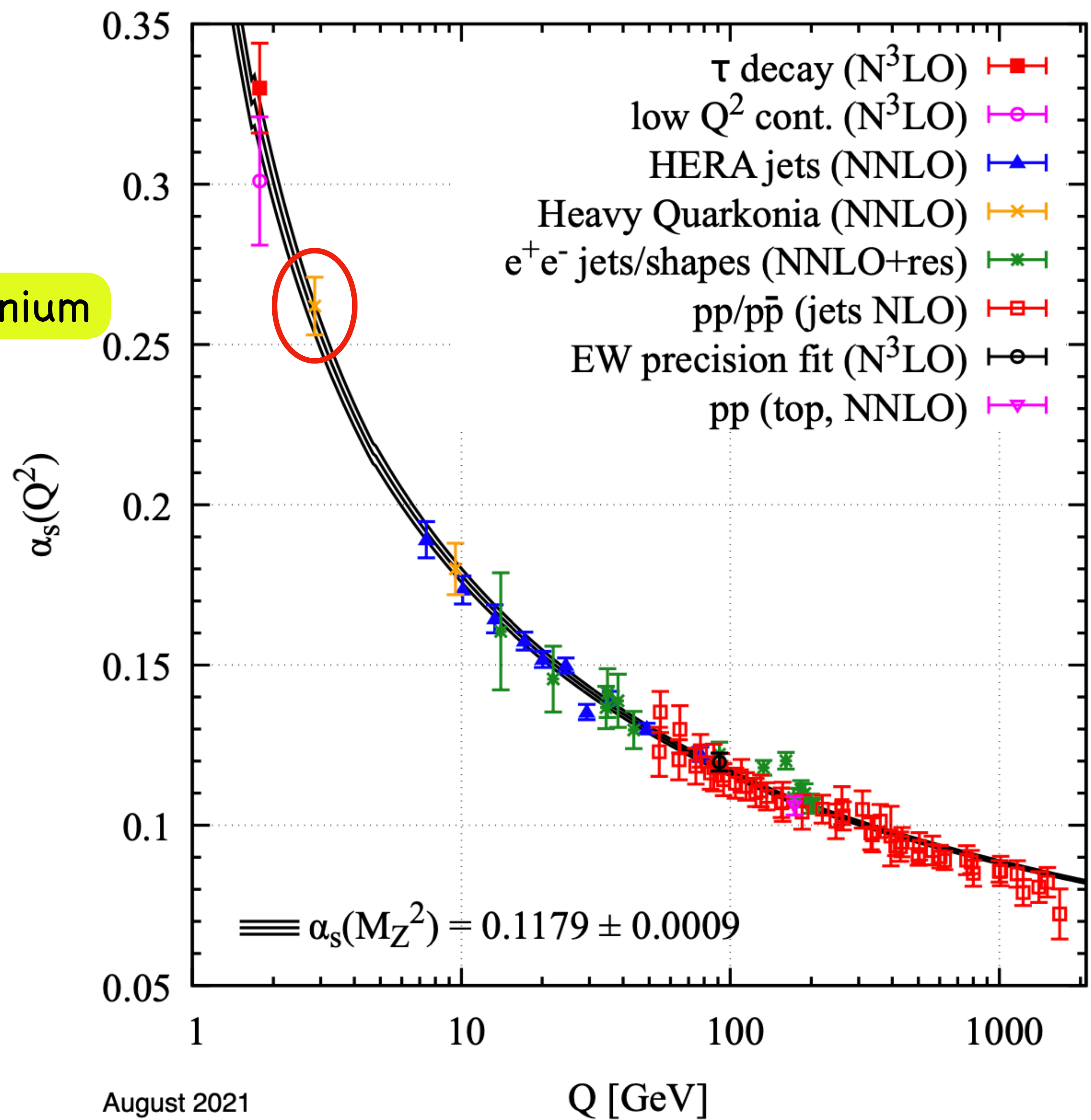
Riccardo Barbieri (CERN and Pisa, Scuola Normale Superiore), Michele Caffo (INFN, Bologna), Raoul Gatto (Geneva U.), E. Remiddi (Geneva U. and Bologna U. and INFN, Bologna) (Jul, 1980)

χ_0, χ_2

Published in: *Phys.Lett.B* 95 (1980) 93-95



Charmonium



PDG, 2021

August 2021

Flavour in the “mid term” of BSM

1. A brief view on BSM (my biases)
2. Minimal Flavour Deconstruction

0. Which rationale for matter quantum numbers?

$$\text{E.g.: } |Q_n - Q_p - Q_e| < 10^{-21} e$$

1. Phenomena unaccounted for

neutrino masses
Dark matter

matter-antimatter asymmetry
inflation?

2. Why $\theta \lesssim 10^{-10}$?

$$\theta G_{\mu\nu} \tilde{G}^{\mu\nu}$$

Axions? A discrete space-time symmetry?

3. $\mathcal{O}_i : d(\mathcal{O}_i) \leq 4$ only?

neutrino masses

Are the protons forever?

Gravity

What about individual L_i conservations?

4. Lack of calculability

the hierarchy problem
the flavour puzzle

none of the 15 masses
predicted in the SM

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⇒ the hierarchy problem
the flavour puzzle

← none of the 15 masses
predicted in the SM

A difference in the two sectors of the SM?

$$\mathcal{L}_{SM} = -\frac{1}{4}F_{\mu\nu}^a F^{a\mu\nu} + i\bar{\Psi}\not{D}\Psi$$

The "gauge sector"

$$+|D_\mu\phi|^2 + M^2|\phi|^2 - \lambda|\phi|^4 + \Lambda + \lambda_{ij}\phi\bar{\Psi}_i\Psi_j$$

The "Higgs sector"

(where the Fermi scale originates)

the hierarchy
problem

the CC problem

the flavour
problem

In EFT they look
much the same

No particle mass
calculable (15=17-2)

To me: the relatively best motivation for BSM in the MultiTeV
(and a strong motivation for the next HE collider)

An extreme summary in precision measurements

(European Strategy for PP, 2020)

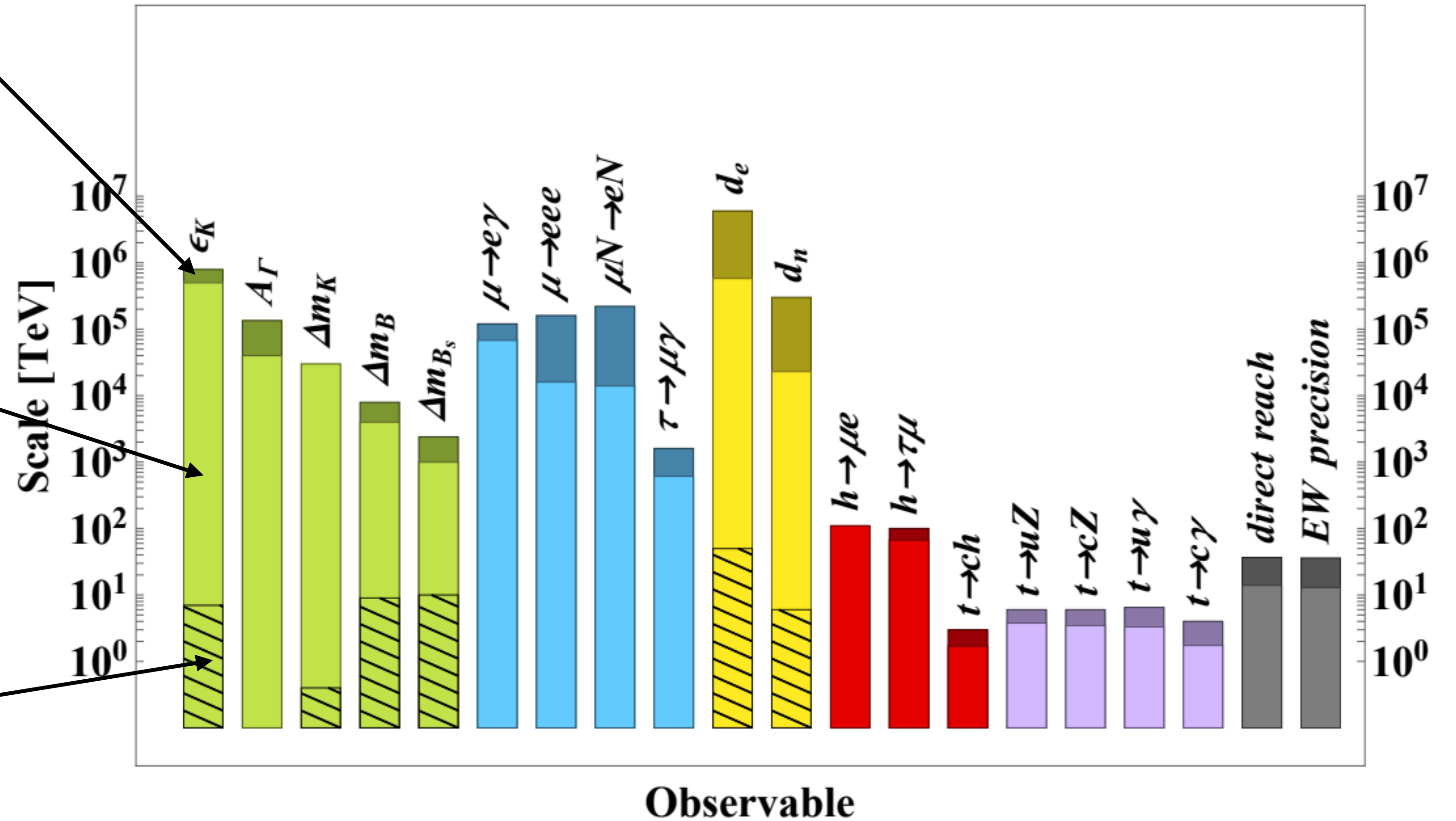
“Mid-term” prospects:
All approved exp.s + LHCb II

current

$$\mathcal{L} = \mathcal{L}_{SM} + \sum_i \frac{1}{\Lambda_i^2} \mathcal{O}_i$$

current

$$\mathcal{L} = \mathcal{L}_{SM} + \sum_i \frac{F_i^{SM}}{\Lambda_i^2} \mathcal{O}_i$$



Flavour and EDMs (CPV) dominate

A more detailed plot

(from actually measured flavour quantities only)

$$\mathcal{L} = \mathcal{L}_{SM} + \sum_i \frac{C_i}{\Lambda_i^2} \mathcal{O}_i$$

$$Q_1^{q_i q_j} = \bar{q}_{jL}^\alpha \gamma_\mu q_{iL}^\alpha \bar{q}_{jL}^\beta \gamma^\mu q_{iL}^\beta,$$

$$Q_2^{q_i q_j} = \bar{q}_{jR}^\alpha q_{iL}^\alpha \bar{q}_{jR}^\beta q_{iL}^\beta, \quad Q_4^{q_i q_j} = \bar{q}_{jR}^\alpha q_{iL}^\alpha \bar{q}_{jL}^\beta q_{iR}^\beta,$$

$$Q_3^{q_i q_j} = \bar{q}_{jR}^\alpha q_{iL}^\beta \bar{q}_{jR}^\beta q_{iL}^\alpha, \quad Q_5^{q_i q_j} = \bar{q}_{jR}^\alpha q_{iL}^\beta \bar{q}_{jL}^\beta q_{iR}^\alpha.$$

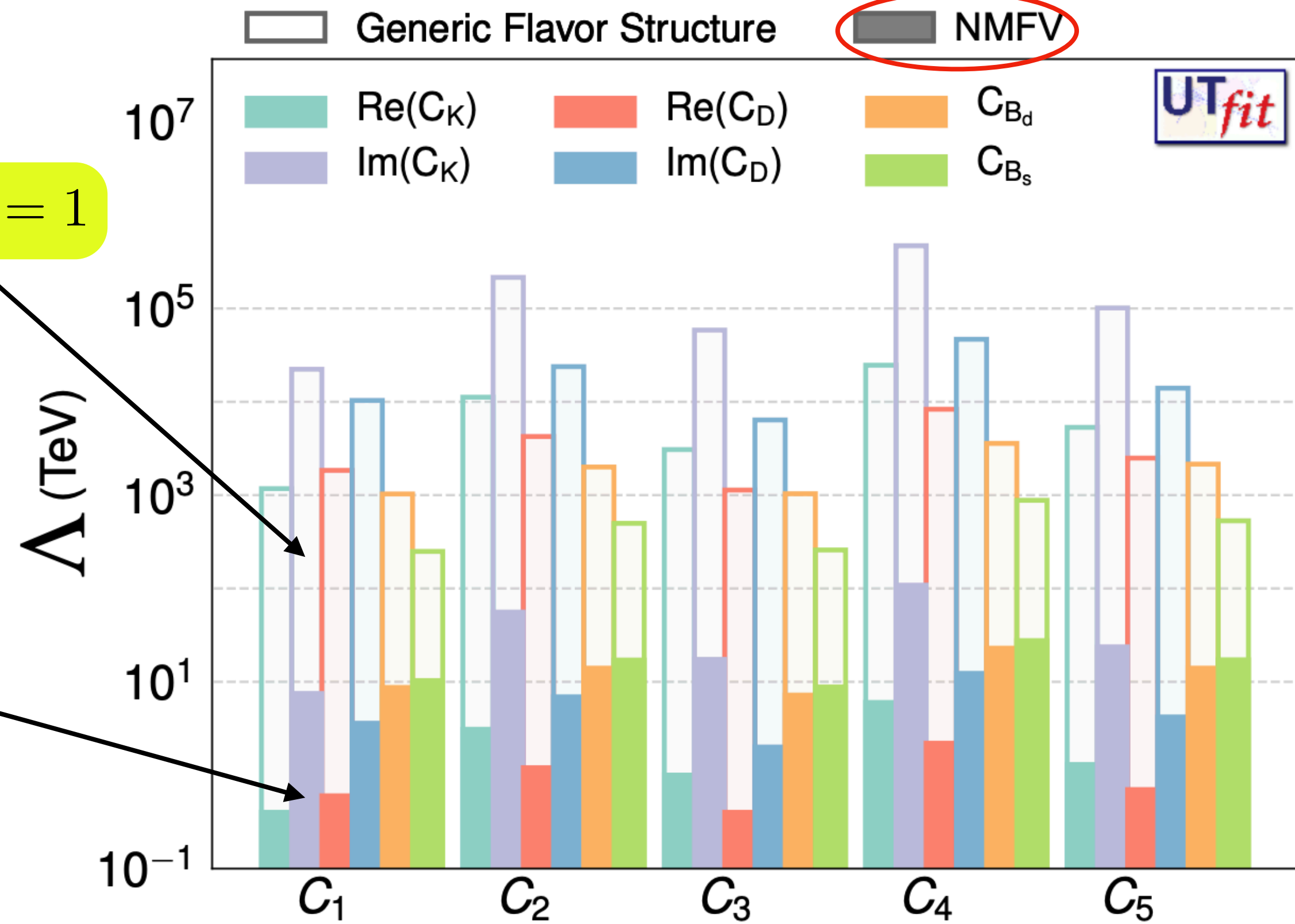
$$C_i = 1$$

NMFV

$$\mathcal{L} = \mathcal{L}_{SM} + \sum_i \frac{F_i^{SM}}{\Lambda_i^2} \mathcal{O}_i$$

$$F^{SM}(C_{K,D}) = (V_{td} V_{ts}^*)^2 e^{i\phi_{K,D}}$$

$$F^{SM}(C_{B_q}) = (V_{tq} V_{tb}^*)^2 e^{i\phi_{B_q}}$$



Pierini, 2023

Where is the actual scale of flavour physics Λ^f ?

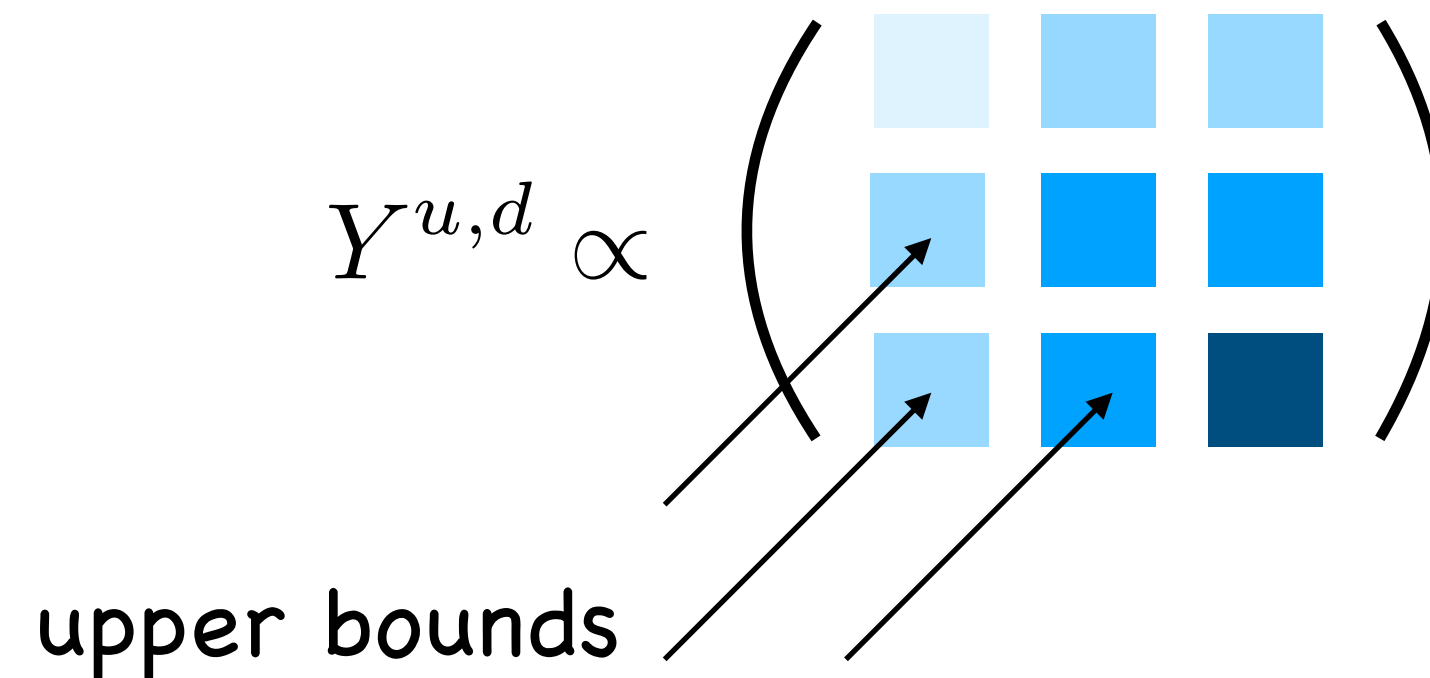
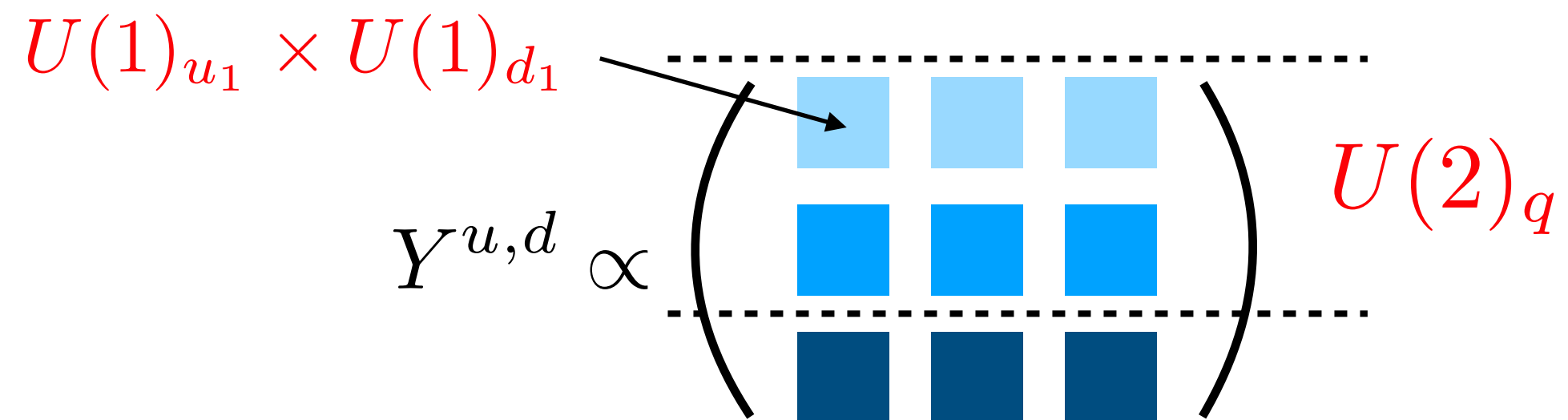
(approximate) symmetries of the Yukawa couplings

Charged fermion Yukawa couplings

$$Y \propto U_L^+ \begin{pmatrix} m_1/m_3 & 0 & 0 \\ 0 & m_2/m_3 & 0 \\ 0 & 0 & 1 \end{pmatrix} U_R \quad m_1/m_3 \ll m_2/m_3 \ll 1 \quad U_L^u (U_L^d)^+ = V_{CKM} \approx \begin{pmatrix} 1 & \lambda & \lambda^3 \\ \lambda & 1 & \lambda^2 \\ \lambda^3 & \lambda^2 & 1 \end{pmatrix}$$

1 IF $[U_L^{u,d}]_{i \neq j} \lesssim [V_{CKM}]_{i \neq j}$

2 IF 1 + $[U_R^{u,d}]_{i \neq j} \lesssim [U_L^{u,d}]_{i \neq j}$

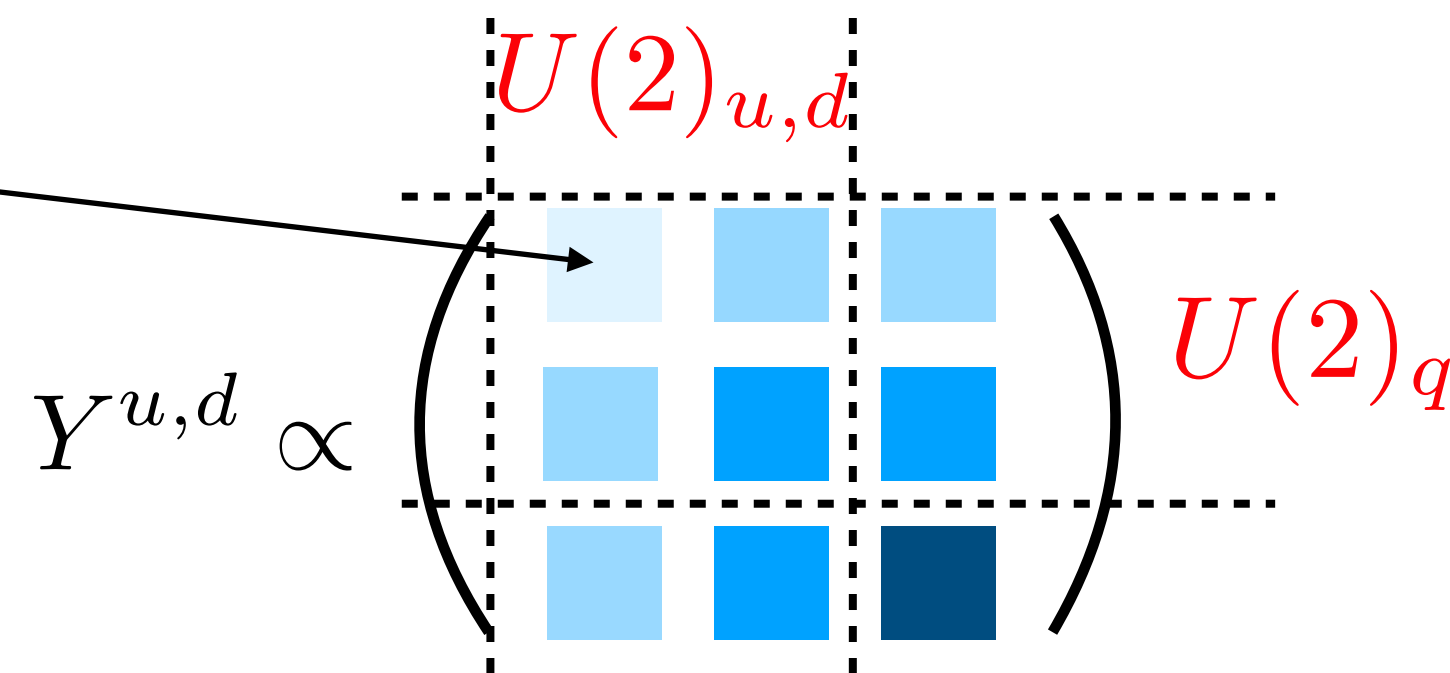


(approximate) symmetries of the Yukawa couplings

Charged fermion Yukawa couplings

IF $[U_L^{u,d}]_{i \neq j} \lesssim [V_{CKM}]_{i \neq j}$ and $[U_R^{u,d}]_{i \neq j} \lesssim [U_L^{u,d}]_{i \neq j}$

$U(1)_{u_1} \times U(1)_{d_1}$



B, Dvali, Hall, 1995

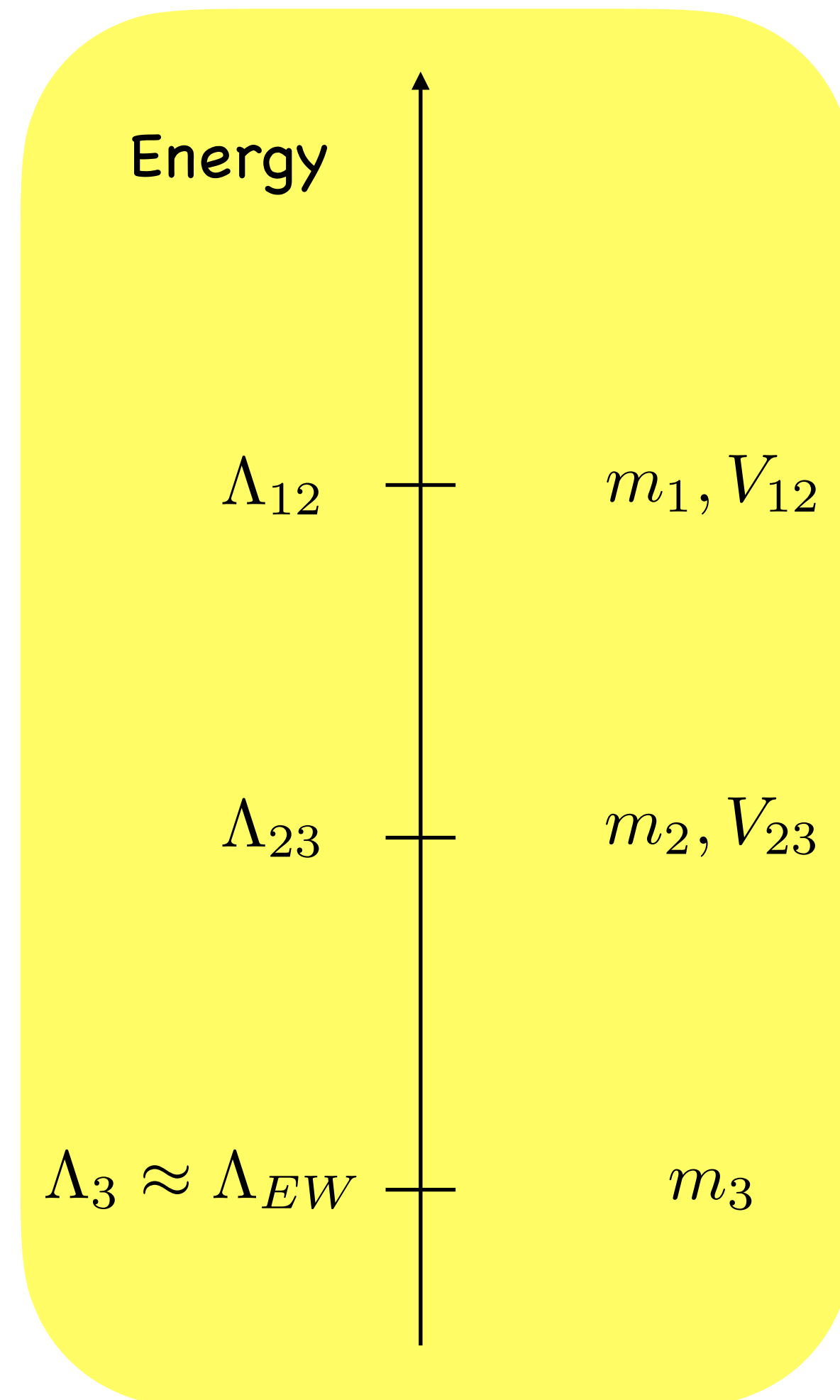
$\Rightarrow U(2)_q \times U(2)_u \times U(2)_d$

B, Isidori et al, 2011

Can $U(2)^n$ allow for Λ^f to be in the MultiTeV? YES, suitably broken

\Rightarrow Can $U(2)^n$ and $U(1)^n$ emerge as accidental symmetries? What breaks them? \Leftarrow

Flavour non-universal interactions



A broad idea:

Lighter fermion masses generated at higher scales,
protected by accidental symmetries due to

Flavour non-universal interactions

.....

Dvali, Shifman, 2000

.....

Panico, Pomarol, 2016

Bordone et al, 2017

B, 2021

In particular:

"Flavour Deconstruction" of the SM gauge symmetries

Davighi, Isidori, 2023

Davighi et al, 2023

Fernando-Navarro, King 2023

“Minimal Flavour Deconstruction” in 4d, explicit

B, Isidori, 2023

$$G = SU(3) \times SU(2) \times U(1)_Y^{[3]} \times U(1)_{B-L}^{[12]} \times U(1)_{T_{3R}}^{[2]} \times U(1)_{T_{3R}}^{[1]}$$

Scalars

Field	$U(1)_Y^{[3]}$	$U(1)_{B-L}^{[12]}$	$U(1)_{T_{3R}}^{[2]}$	$U(1)_{T_{3R}}^{[1]}$	$SU(3) \times SU(2)$
$H_{u,d}$	-1/2	0	0	0	(1, 2)
χ^q	-1/6	1/3	0	0	(1, 1)
χ^l	1/2	-1	0	0	(1, 1)
ϕ	1/2	0	-1/2	0	(1, 1)
σ	0	0	1/2	-1/2	(1, 1)

VectorLike fermions

		$U(1)_Y^{[3]}$	$U(1)_{B-L}^{[12]}$	$U(1)_{T_{3R}}^{[2]}$	$U(1)_{T_{3R}}^{[1]}$	$SU(3) \times SU(2)$
light VL ($\alpha = 1, 2$)	U_α	1/2	1/3	0	0	(3, 1)
	D_α	-1/2	1/3	0	0	(3, 1)
	E_α	-1/2	-1	0	0	(1, 1)
heavy VL	U_3	0	1/3	1/2	0	(3, 1)
	D_3	0	1/3	-1/2	0	(3, 1)
	E_3	0	-1	-1/2	0	(1, 1)

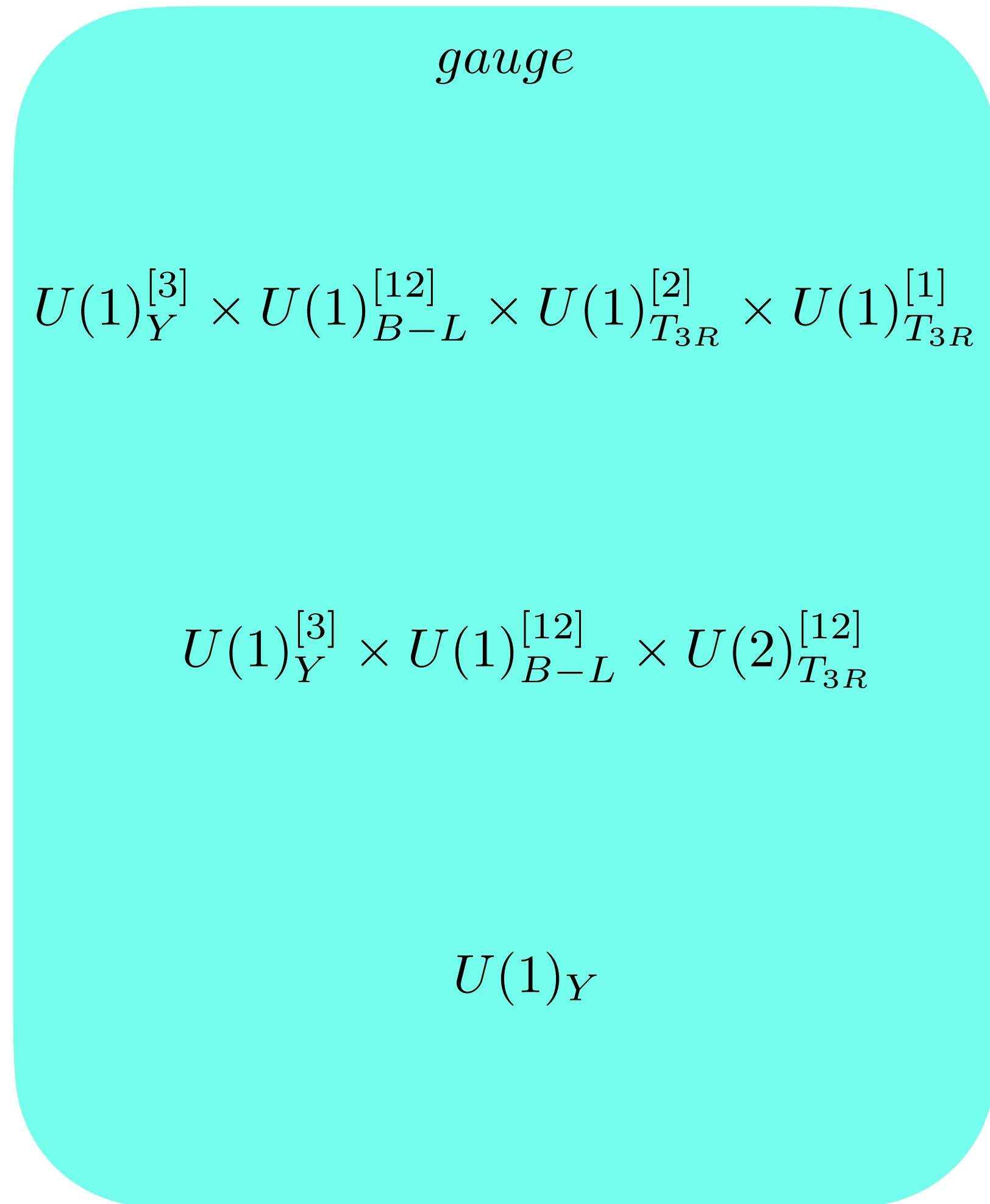
(a 16-plet/generation with neutrinos)

Most general $d \leq 4$

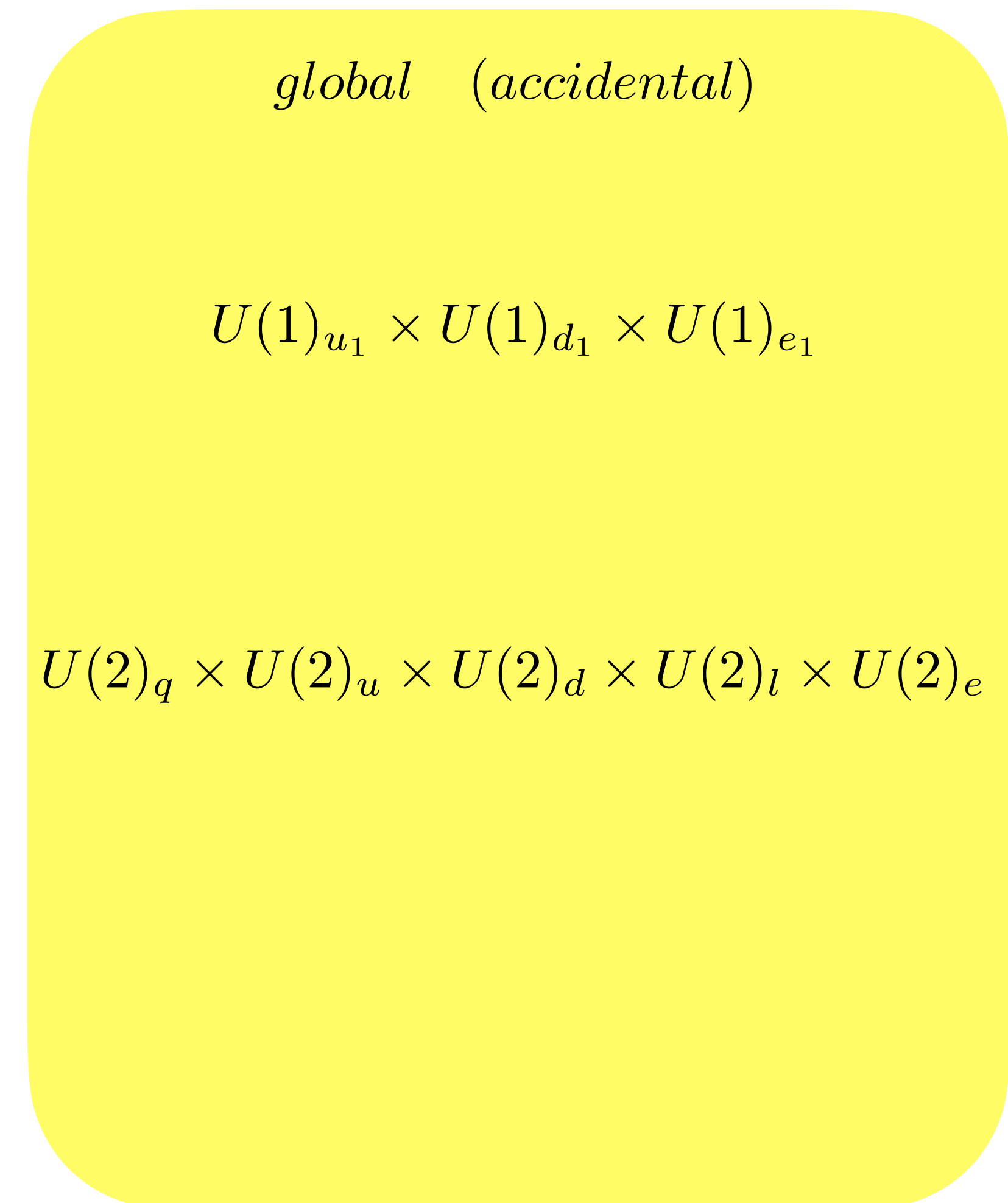
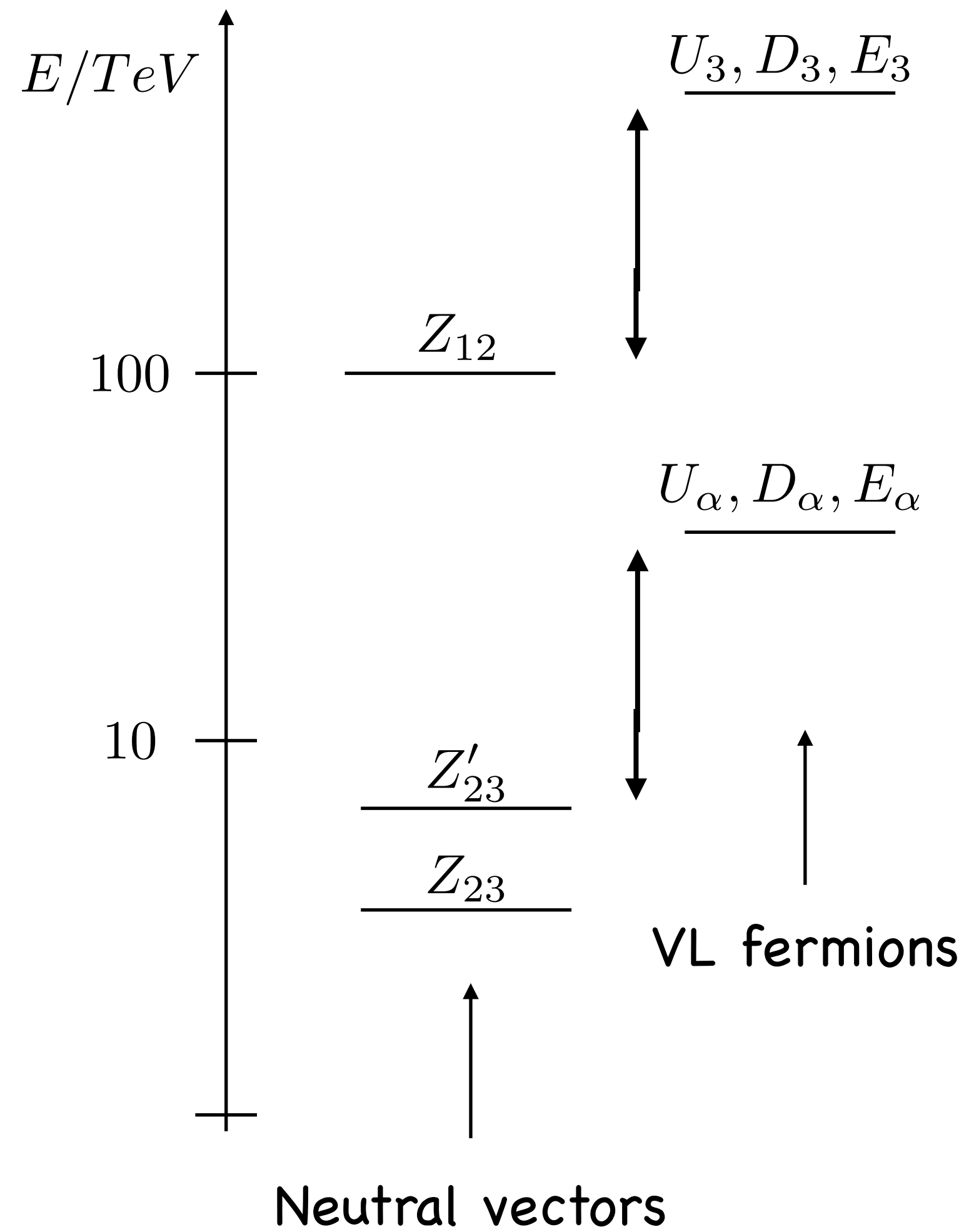
$$\mathcal{L}_Y^u = (y_3^u \bar{q}_3 u_3 H_u + y_{i\alpha}^u \bar{q}_i U_\alpha H_u + y_\alpha^{\chi^u} \bar{U}_\alpha u_3 \chi^q + y_{\alpha 2}^{\phi_u} \bar{U}_\alpha u_2 \phi + y_{\alpha 3}^{\phi_u} \bar{U}_{R\alpha} U_{L3} \phi + \hat{y}_{\alpha 3}^{\phi_u} \bar{U}_{L\alpha} U_{R3} \phi + y_1^{\sigma_u} \bar{U}_3 u_1 \sigma + \text{h.c.}) + M_{U_3} \bar{U}_3 U_3 + M_{U_\alpha} \bar{U}_\alpha U_\alpha$$

And similarly for $Y_{d,e}$ with $H_u \rightarrow H_d$

The overall picture



Universal $SU(3) \times SU(2)$
left understood



Universal $U(1)_B \times U(1)_L$
left understood

Yukawa couplings

Most general

$$d \leq 4$$

$$\mathcal{L}_Y^u = \left(y_3^u \bar{q}_3 u_3 H_u + y_{i\alpha}^u \bar{q}_i U_\alpha H_u + y_\alpha^{\chi u} \bar{U}_\alpha u_3 \chi^q + y_{\alpha 2}^{\phi u} \bar{U}_\alpha u_2 \phi + y_{\alpha 3}^{\phi u} \bar{U}_{R\alpha} U_{L3} \phi + \hat{y}_{\alpha 3}^{\phi u} \bar{U}_{L\alpha} U_{R3} \phi + y_1^{\sigma u} \bar{U}_3 u_1 \sigma + \text{h.c.} \right) + M_{U_3} \bar{U}_3 U_3 + M_{U_\alpha} \bar{U}_\alpha U_\alpha$$

By integrating out the VL fermions

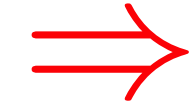


$$Y_u \approx \begin{pmatrix} y_{1\alpha}^u \hat{y}_{\alpha 3}^{\phi u} y_1^{\sigma u} \epsilon_\sigma \epsilon_\phi & y_{1\alpha}^u y_{\alpha 2}^{\phi u} \epsilon_\phi & y_{12}^u y_2^{\chi u} \epsilon_\chi \\ y_{2\alpha}^u \hat{y}_{\alpha 3}^{\phi u} y_1^{\sigma u} \epsilon_\sigma \epsilon_\phi & y_{2\alpha}^u y_{\alpha 2}^{\phi u} \epsilon_\phi & y_{22}^u y_2^{\chi u} \epsilon_\chi \\ \approx 0 & \approx 0 & y_3^u \end{pmatrix}$$

$$\begin{aligned} \epsilon_\chi &= \frac{\langle \chi \rangle}{M_\alpha} \\ \epsilon_\phi &= \frac{\langle \phi \rangle}{M_\alpha} \\ \epsilon_\sigma &= \frac{\langle \sigma \rangle}{M_3} \end{aligned}$$

And similarly
for $Y_{d,e}$

Yukawa couplings



$$Y_u \approx \begin{pmatrix} y_{1\alpha}^u \hat{y}_{\alpha 3}^{\phi_u} y_1^{\sigma_u} \epsilon_\sigma \epsilon_\phi & y_{1\alpha}^u y_{\alpha 2}^{\phi_u} \epsilon_\phi & y_{12}^u y_2^{\chi_u} \epsilon_\chi \\ y_{2\alpha}^u \hat{y}_{\alpha 3}^{\phi_u} y_1^{\sigma_u} \epsilon_\sigma \epsilon_\phi & y_{2\alpha}^u y_{\alpha 2}^{\phi_u} \epsilon_\phi & y_{22}^u y_2^{\chi_u} \epsilon_\chi \\ \approx 0 & \approx 0 & y_3^u \end{pmatrix}$$

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And similarly
for $Y_{d,e}$

All charged fermion masses and V_{CKM} reproduced with

$$\frac{v_u}{v_d} \approx 10 \quad \epsilon_\chi, \epsilon_\phi, \epsilon_\sigma = (0.5 \div 2) \cdot 10^{-1} \quad \text{and} \quad y's = 0.1 \div 1$$



$$U_L^{u,d,e} \approx V_{CKM} \quad (U_L^u U_L^{d+} = V_{CKM}) \quad [U_R^{u,d,e}]_{i \neq j} \ll [U_L^{u,d,e}]_{i \neq j}$$

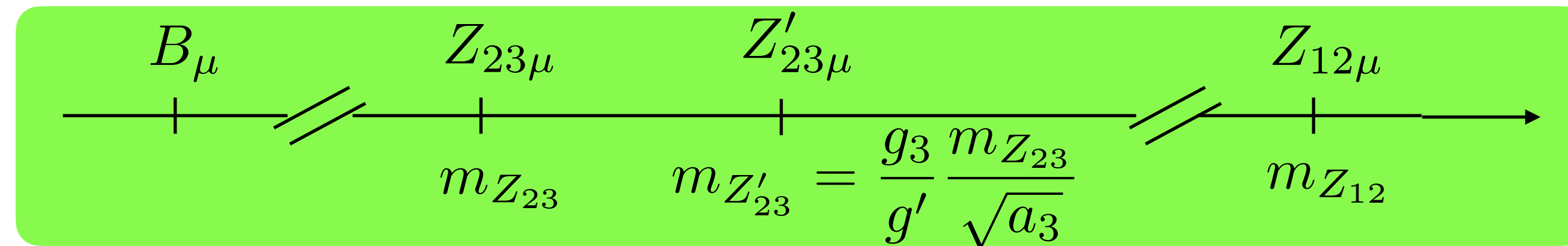
Vector masses and couplings

B, 2024

$$D_\mu \equiv \partial_\mu - i(g_3 Y^{[3]} A_{3\mu} + g_B \frac{(B-L)^{[12]}}{2} A_{B\mu} + g_2 T_{3R}^{[2]} A_{2\mu} + g_1 T_{3R}^{[1]} A_{1\mu})$$

Take $\langle \sigma \rangle \gg \langle \chi \rangle$, $\langle \phi \rangle \equiv \sqrt{b} \langle \chi \rangle$ and $g_3 \gg g_B, g_2, g_1$ Define $\frac{g_B \sqrt{g_1^2 + g_2^2}}{g_1 g_2} = \tan \alpha \equiv t_\alpha$

Before EWSB



$$a_3 = \frac{b(1 + t_\alpha^2)^2}{t_\alpha^2(1 + b)^2}$$

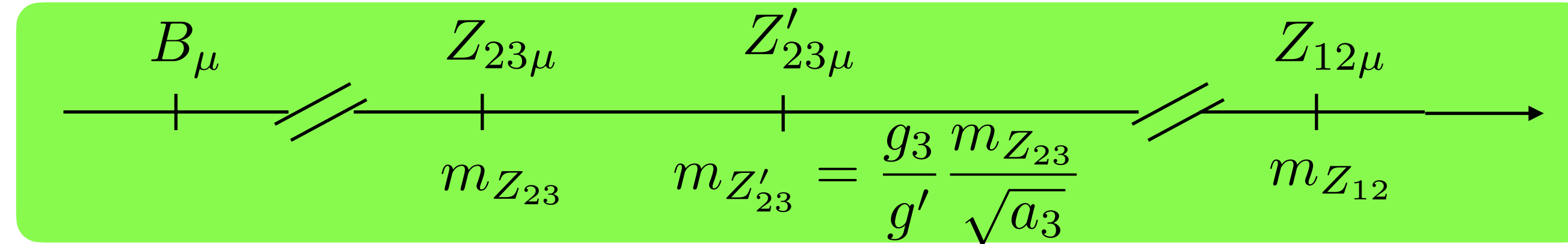
$$a_{23} = \frac{1 - bt_\alpha^2}{t_\alpha(1 + b)}$$

$$D_\mu(B, Z_{23}, Z'_{23}) = -i[g' B_\mu Y + g' Z_{23\mu} (a_{23} Y^{[3]} + \frac{1}{t_\alpha} \frac{(B-L)^{[12]}}{2} - t_\alpha T_{3R}^{[12]}) + g_3 Z'_{23\mu} Y^{[3]}]$$

Vector masses and couplings

B, 2024

Before EWSB



$$D_\mu(B, Z_{23}, Z'_{23}) = -i[g' B_\mu Y + g' Z_{23\mu} (a_{23} Y^{[3]} + \frac{1}{t_\alpha} \frac{(B-L)^{[12]}}{2} - t_\alpha T_{3R}^{[12]}) + g_3 Z'_{23\mu} Y^{[3]}]$$

$$a_3 = \frac{b(1+t_\alpha^2)^2}{t_\alpha^2(1+b)^2}$$

$$a_{23} = \frac{1-bt_\alpha^2}{t_\alpha(1+b)}$$

After EWSB

$$\mathcal{L}_H^{gauge} = |(\partial_\mu - ig\vec{T} \cdot \vec{W}_\mu - ig_3 Y^{[3]} A_{3\mu})H|^2$$

$$\frac{\delta m_Z^2}{m_Z^2} \equiv s_W^2 \frac{m_Z^2}{m_{Z_{23}}^2} (a_{23}^2 + a_3)$$

and

$$\delta D_\mu(Z) = -iZ_\mu g' s_W \frac{m_Z^2}{m_{Z_{23}}^2} [(a_{23}^2 + a_3)Y^{[3]} + a_{23}(\frac{1}{t_\alpha} \frac{(B-L)^{[12]}}{2} - t_\alpha T_{3R}^{[12]})]$$

Parameters at the lowest new scale $m_{Z_{23}}; t_\alpha, b$

Phenomenology at the lowest new scale 1

B, 2024

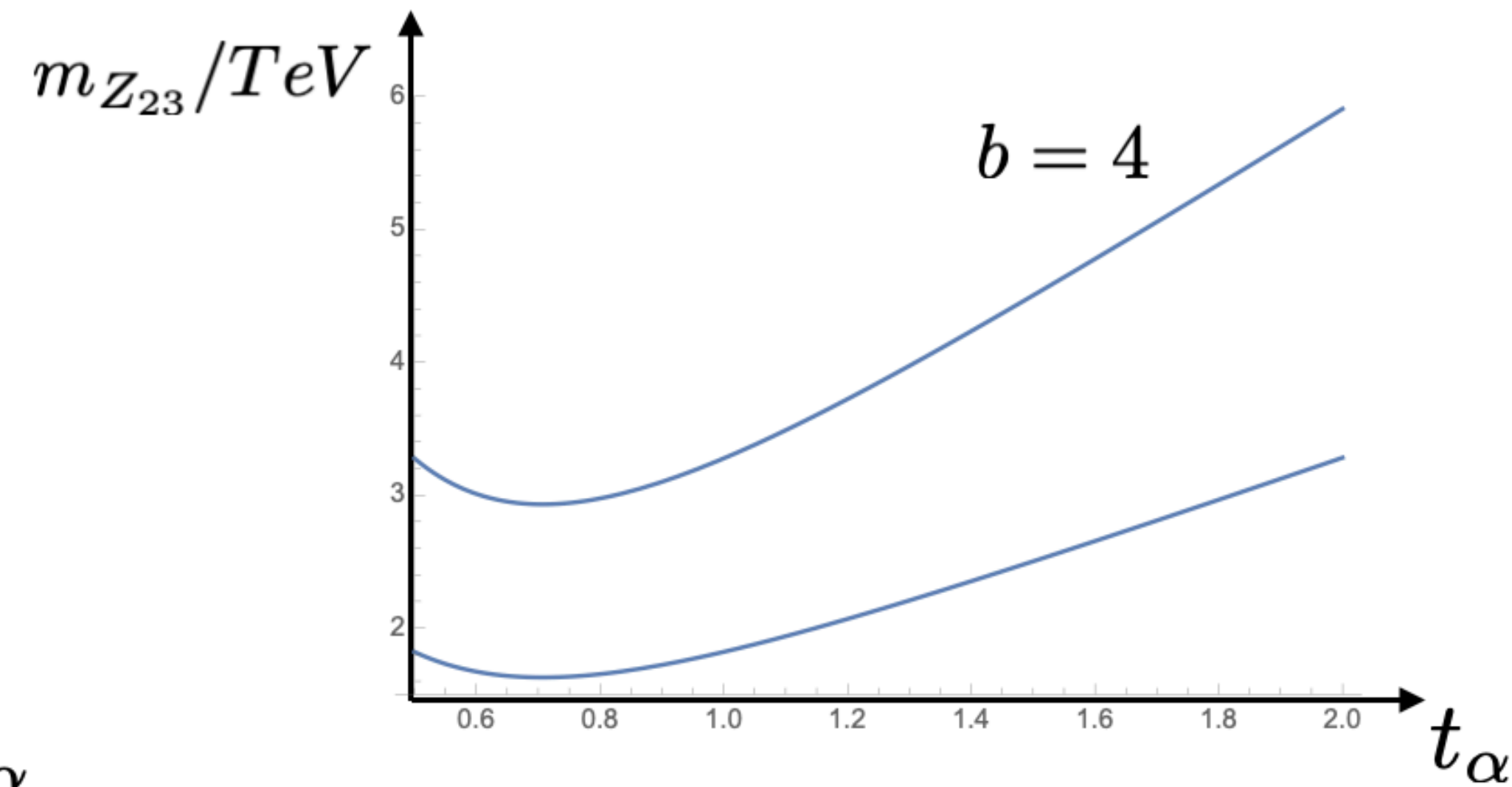
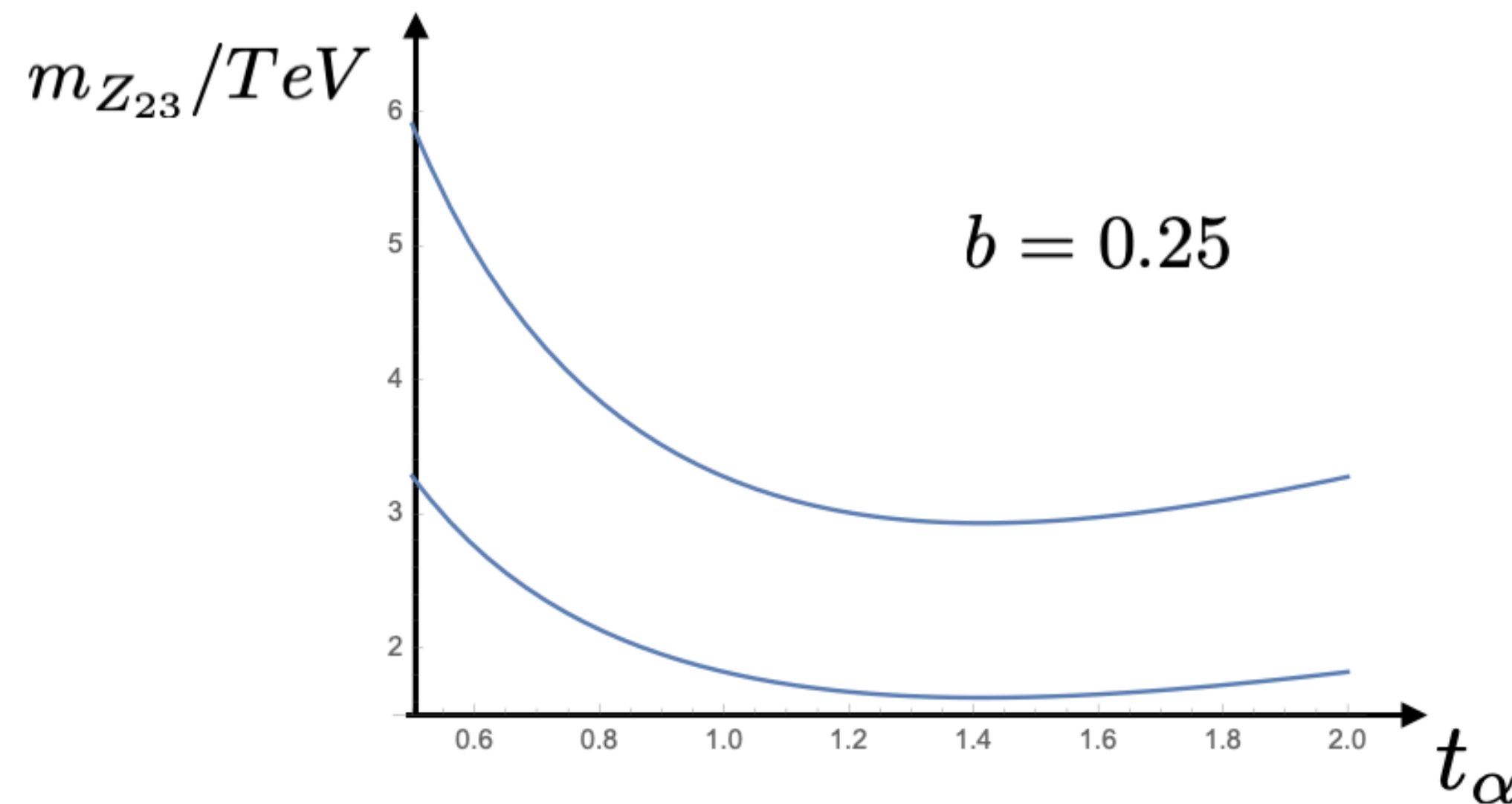
EWPT

$$\frac{\delta m_Z^2}{m_Z^2} \equiv s_W^2 \frac{m_Z^2}{m_{Z_{23}}^2} (a_{23}^2 + a_3)$$

$$\frac{\delta m_Z^2}{m_Z^2} = \left(\frac{m_Z(SM)}{m_Z(exp)} \right)^2 - 1 = (38 \pm 20) \cdot 10^{-5}$$

De Blas et al, 2022

To reproduce the 1σ interval above



Phenomenology at the lowest new scale 2

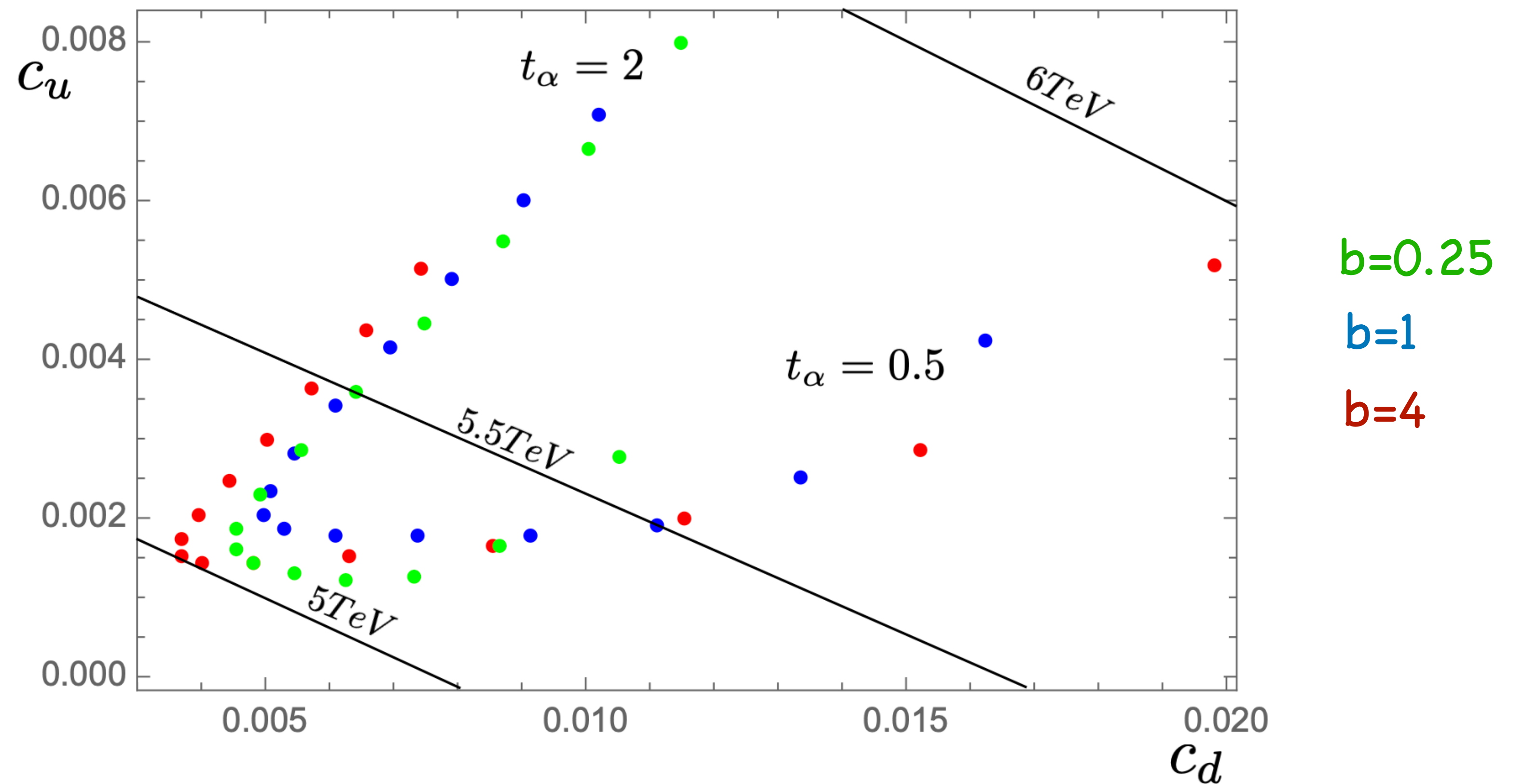
High- p_T Drell-Yan $pp \rightarrow l^+l^-$, $l = e, \mu$

Defining $c_u = g'^2(g_L^{u2} + g_R^{u2})Br_{Z_{23}}(l^+l^-)$, $c_d = g'^2(g_L^{d2} + g_R^{d2})Br_{Z_{23}}(l^+l^-)$

from Z_{23} exchange $c_u w_u + c_d w_d = \frac{6}{\pi} \sigma_{l+l^-}$

ATLAS, CMS $140fb^{-1}$

Current lower bound on $m_{Z_{23}}$



Phenomenology at the lowest new scale 3

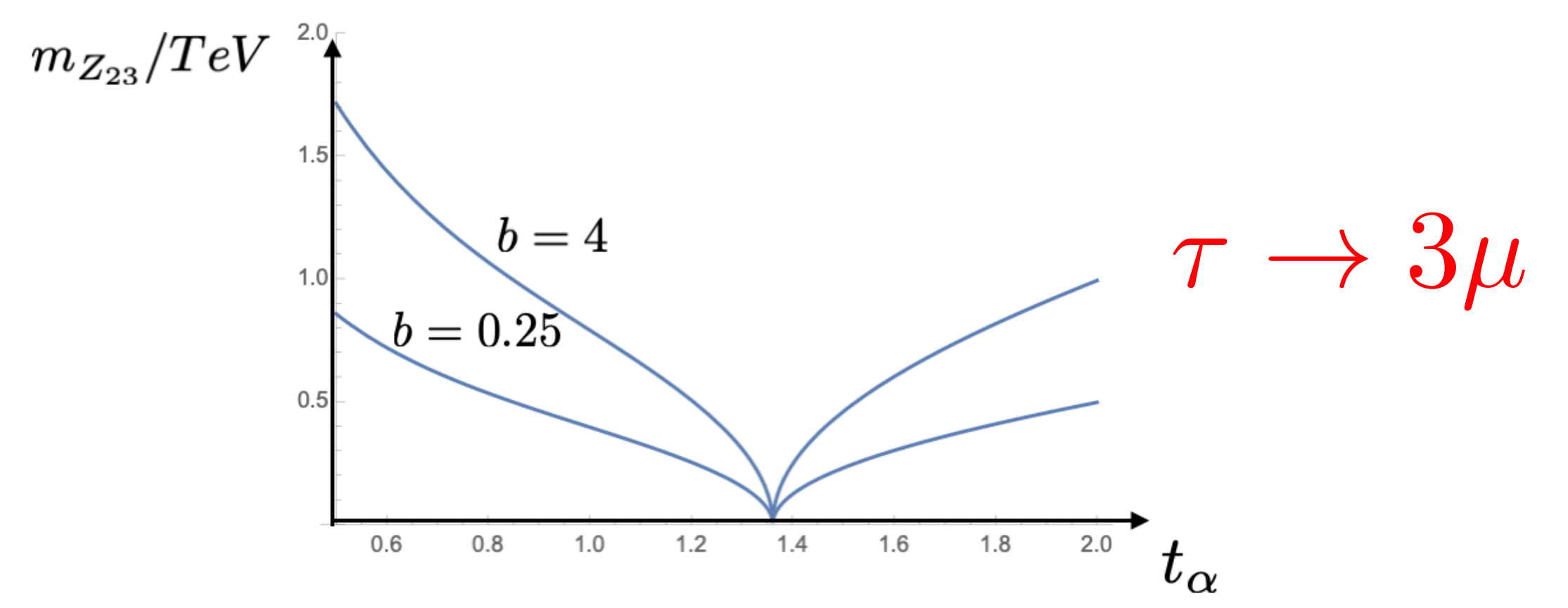
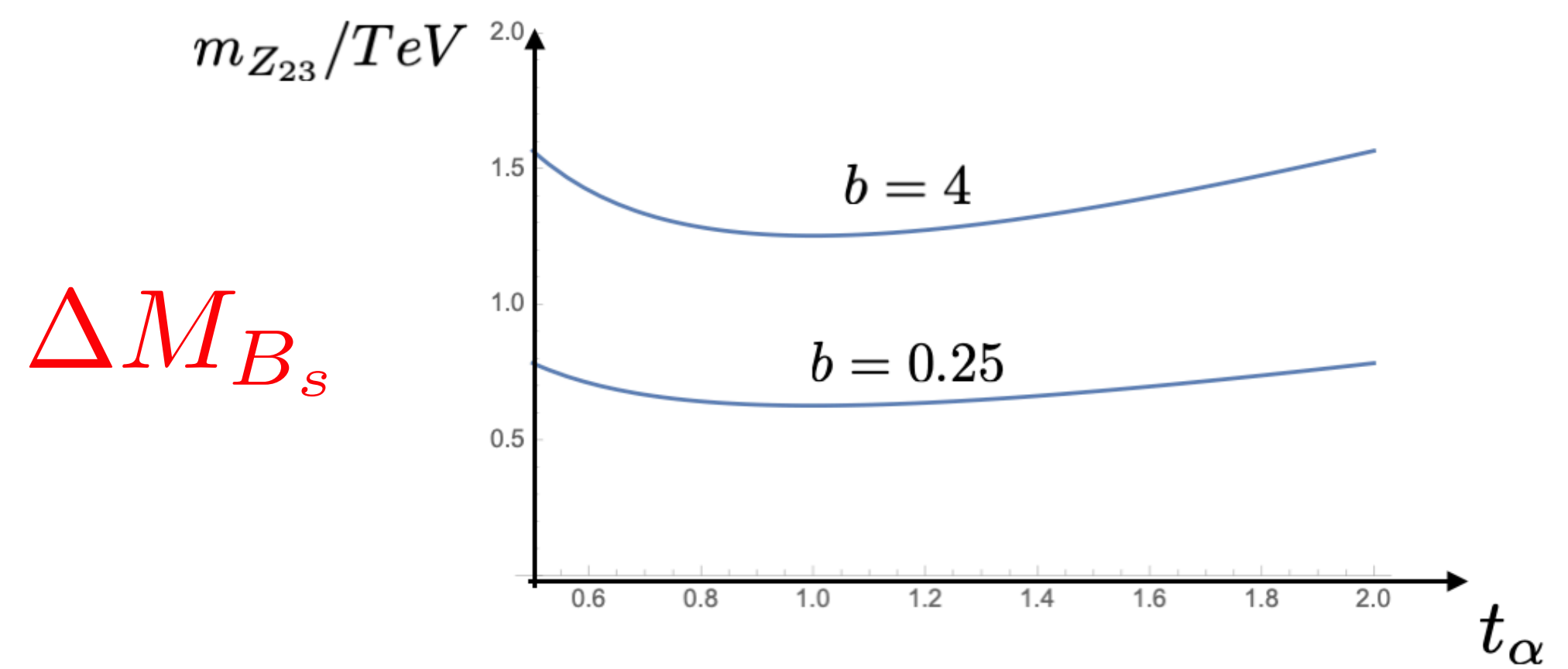
Flavour Changing effects $\Delta F = 2, b \rightarrow sll, K \rightarrow \pi\nu\nu, \tau \rightarrow 3\mu, \mu \rightarrow 3e, etc$

From the different couplings of Z, Z_{23}, Z'_{23} to the third generation versus the first two, after going to the mass basis: $f_L = U_L^f f_L^{(0)}, f_R \approx f_R^{(0)}$

$$\mathcal{L}^{(FC)} = [g'(a_{23} - \frac{1}{t_\alpha})Z_{23\mu} + g_3 Z'_{23\mu} + s_W g' \frac{m_Z^2}{m_{Z_{23}}^2} (a_{23}^2 - \frac{a_{23}}{t_\alpha} + a_3) Z_\mu] J^\mu,$$

$$J^\mu = \frac{1}{6} J_u^\mu + \frac{1}{6} J_d^\mu - \frac{1}{2} J_e^\mu, \quad J_f^\mu = \sum_{i \neq j} [U_L^f]_{i3} [U_L^f]_{j3}^* \bar{f}_{Li} \gamma^\mu f_{Lj}$$

Current lower bounds on $m_{Z_{23}}$ with $U_L^e = U_L^d = V_{CKM}^+$



Flavour precision tests, a partial list (2022)

Input	Reference	Measurement	UTfit Prediction	Pull
$\sin 2\beta$	[22], UTfit	0.688(20)	0.736(28)	-1.4
γ	[22]	66.1(3.5)	64.9(1.4)	+0.29
α	UTfit	94.9(4.7)	92.2(1.6)	+0.6
$\varepsilon \cdot 10^3$	[38]	2.228(1)	2.00(15)	+1.56
$ V_{ud} $	UTfit	0.97433(19)	0.9738(11)	+0.03
$ V_{ub} \cdot 10^3 \bullet$	UTfit	3.77(24)	3.70(11)	+0.25
$ V_{ub} \cdot 10^3$ (excl)	[39]	3.74(17)		
$ V_{ub} \cdot 10^3$ (incl)	[22]	4.32(29)		
$ V_{cb} \cdot 10^3 \bullet$	UTfit	41.25(95)	42.22(51)	-0.59
$ V_{cb} \cdot 10^3$ (excl)	UTfit	39.44(63)		
$ V_{cb} \cdot 10^3$ (incl)	[40]	42.16(50)		
$ V_{ub} / V_{cb} $	[39]	0.0844(56)		
$\Delta M_d \times 10^{12} \text{ s}^{-1}$	[38]	0.5065(19)	0.519(23)	-0.49
$\Delta M_s \times 10^{12} \text{ s}^{-1}$	[38]	17.741(20)	17.94(69)	-0.30
$\text{BR}(B_s \rightarrow \mu\mu) \times 10^9$	[38]	3.41(29)	3.47(14)	-0.14
$\text{BR}(B \rightarrow \tau\nu) \times 10^4$	[38]	1.06(19)	0.869(47)	+0.96
$\text{Re}(\varepsilon'/\varepsilon) \times 10^4$	[38]	16.6(3.3)	15.2(4.7)	+0.27
$(q/p _D - 1) \times 10^2$		0.05(2.50)	0.8(4.0)	-0, 15
$\text{BR}(B^+ \rightarrow K^+ \nu\nu) 10^6$		23(7)	5.58(37)	+2.5
$\text{BR}(K^+ \rightarrow \pi^+ \nu\nu) 10^{11}$		10.6(4.0)	9.31(76)	+0, 3
R_D		0.344(26)	0.298(4)	+1.7
R_{D^*}		0.285(12)	0.254(5)	+2.3

UTfit Collaboration
with some little integration

(No EDM's, $\mu \rightarrow e\gamma$, etc.)

Current precision

Input	Reference	Measurement	UTfit Prediction	Pull
$\sin 2\beta$	[22], UTfit	0.688(20)	0.736(28)	-1.4
γ	[22]	66.1(3.5)	64.9(1.4)	+0.29
α	UTfit	94.9(4.7)	92.2(1.6)	+0.6
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$ V_{ub} \cdot 10^3$ (incl)	[22]	4.32(29)		
$ V_{cb} \cdot 10^3 \bullet$	UTfit	41.25(95)	42.22(51)	-0.59
$ V_{cb} \cdot 10^3$ (excl)	UTfit	39.44(63)	Ciao.	
$ V_{cb} \cdot 10^3$ (incl)	[40]	42.16(50)		
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R_{D^*}		0.285(12)	0.254(5)	+2.3

current

4%th/exp

5%exp

5%exp

8%th

0.1%th

8%exp/th

2%exp/th

5%th/exp

4%th

9%exp

20%exp

30%th

100%th*

35%exp

40%exp

8%exp

4%exp

Conceivable progress in the “mid-term” of flavour

Input	Reference	Measurement	UTfit Prediction	Pull
$\sin 2\beta$	[22], UTfit	0.688(20)	0.736(28)	-1.4
γ	[22]	66.1(3.5)	64.9(1.4)	+0.29
α	UTfit	94.9(4.7)	92.2(1.6)	+0.6
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R_D		0.344(26)	0.298(4)	+1.7
R_{D^*}		0.285(12)	0.254(5)	+2.3

current

4%th/exp

5%exp

5%exp

8%th

0.1%th

8%exp/th

2%exp/th

5%th/exp

4%th

9%exp

20%exp

30%th

100%th*

35%exp

40%exp

8%exp

4%exp

mid-term

0.6%

0.8%

0.4%

1%

0.5%

2%

1.5%

4%

4%

30%*

10%

20%

4%

2.5%

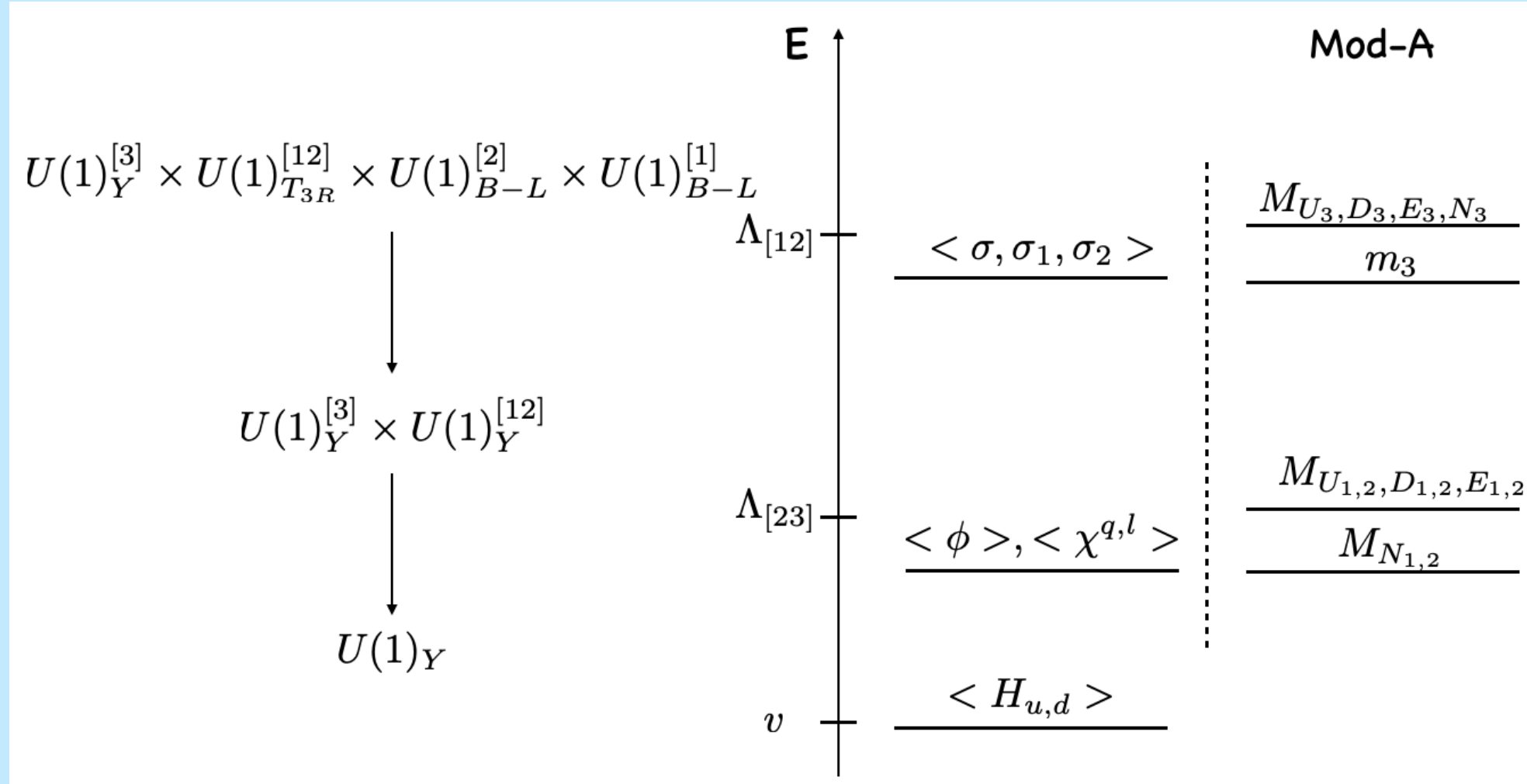
with strong correlations!

(No EDM's, $\mu \rightarrow e\gamma$, etc.)

Summary

1. Flavour symmetries ($U(2)^n$) can:
 - allow for flavour changing $\frac{1}{\Lambda^{n-4}} \mathcal{O}^{n>4}$ with $\Lambda \approx \text{MultiTeV}$
 - be related to the pattern of $Y^{u,d,e}$ and **arise accidentally**
2. In an explicit 4d gauge model, MFD, increased precision in the “mid term” of EWPT, Drell-Yan, flavour observables can in each case find evidence for motivated new physics in the MultiTeV
3. A convincing deviation from the SM in any of these areas would motivate an overall fit along the lines as described

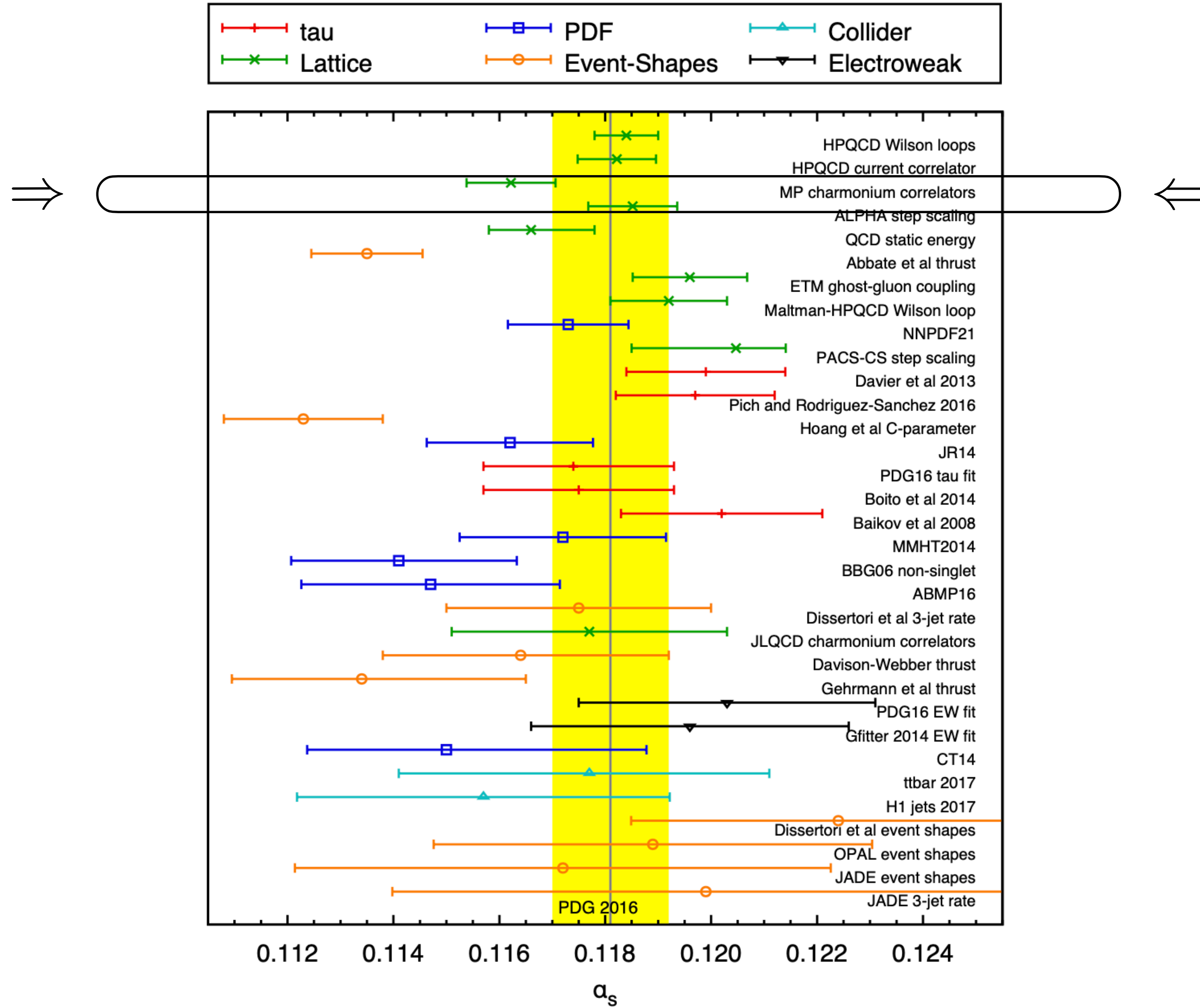
Extension to neutrinos



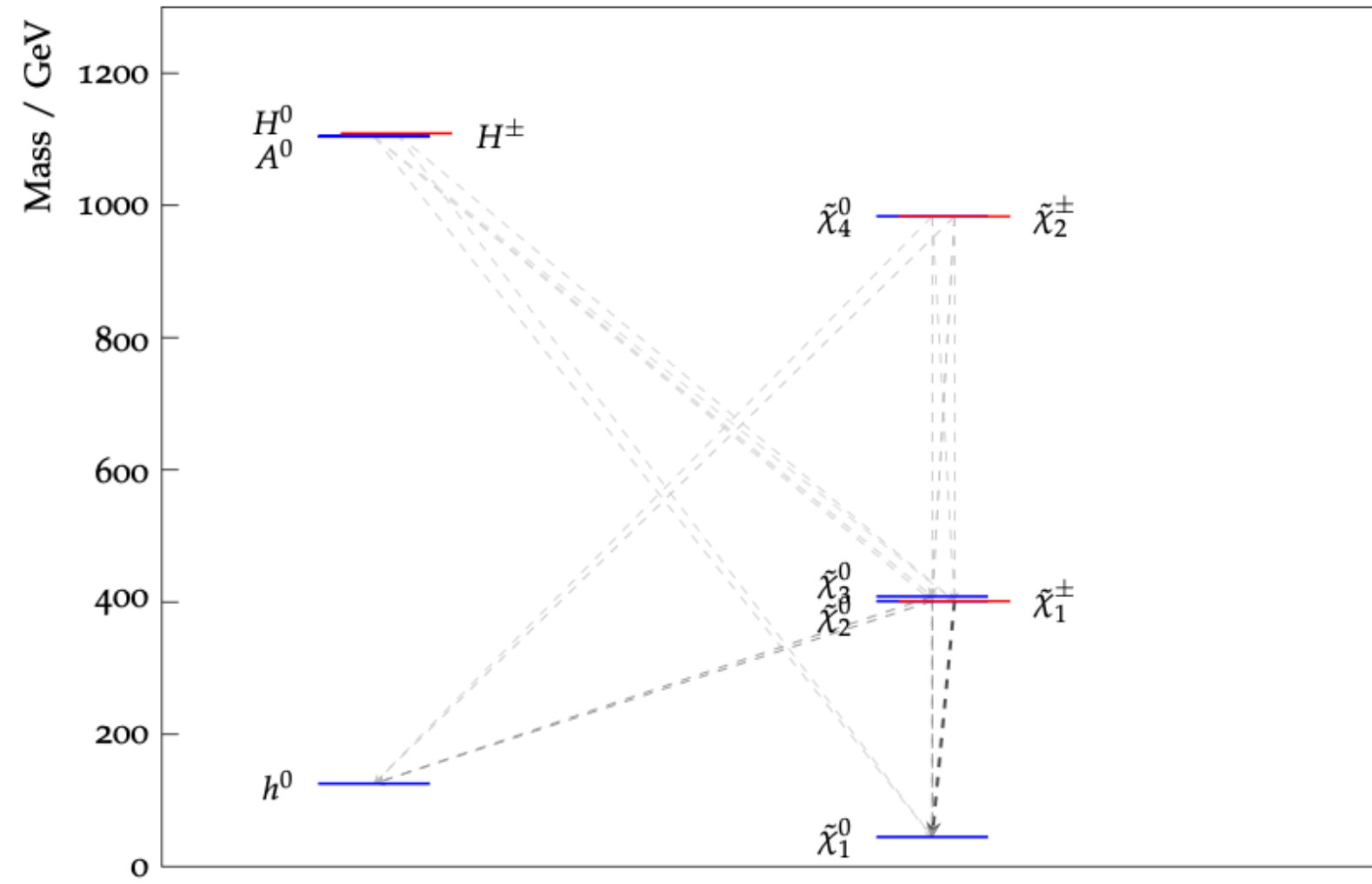
		$U(1)_Y^{[3]}$	$U(1)_{B-L}^{[12]}$	$U(2)_{T_{3R}}^{[2]}$	$U(1)_{T_{3R}}^{[1]}$	$SU(3) \times SU(2)$
light VL	$N_{1,2}$	1/2	-1	0	0	(1, 1)
heavy VL	N_3	0	-1	0	1/2	(1, 1)
scalars	σ_1	0	2	0	-1	(1, 1)
	σ_2	0	2	-1	0	(1, 1)

$$m_{LL}^\nu |_{\text{Mod. A}} \approx v_u^2 \begin{pmatrix} \frac{y^4}{y^{\sigma_2} \langle \sigma_2 \rangle} + \frac{y^4}{m_3} & \frac{y^4}{y^{\sigma_2} \langle \sigma_2 \rangle} + \frac{y^4}{m_3} & \frac{y^5}{y^{\sigma_2} \langle \sigma_2 \rangle} + \frac{y^3}{m_3} \\ \frac{y^4}{y^{\sigma_2} \langle \sigma_2 \rangle} + \frac{y^4}{m_3} & \frac{y^4}{y^{\sigma_2} \langle \sigma_2 \rangle} + \frac{y^4}{m_3} & \frac{y^5}{y^{\sigma_2} \langle \sigma_2 \rangle} + \frac{y^3}{m_3} \\ \frac{y^5}{y^{\sigma_2} \langle \sigma_2 \rangle} + \frac{y^3}{m_3} & \frac{y^5}{y^{\sigma_2} \langle \sigma_2 \rangle} + \frac{y^3}{m_3} & \frac{y^5}{y^{\sigma_2} \langle \sigma_2 \rangle} + \frac{y^2}{m_3} \end{pmatrix}$$

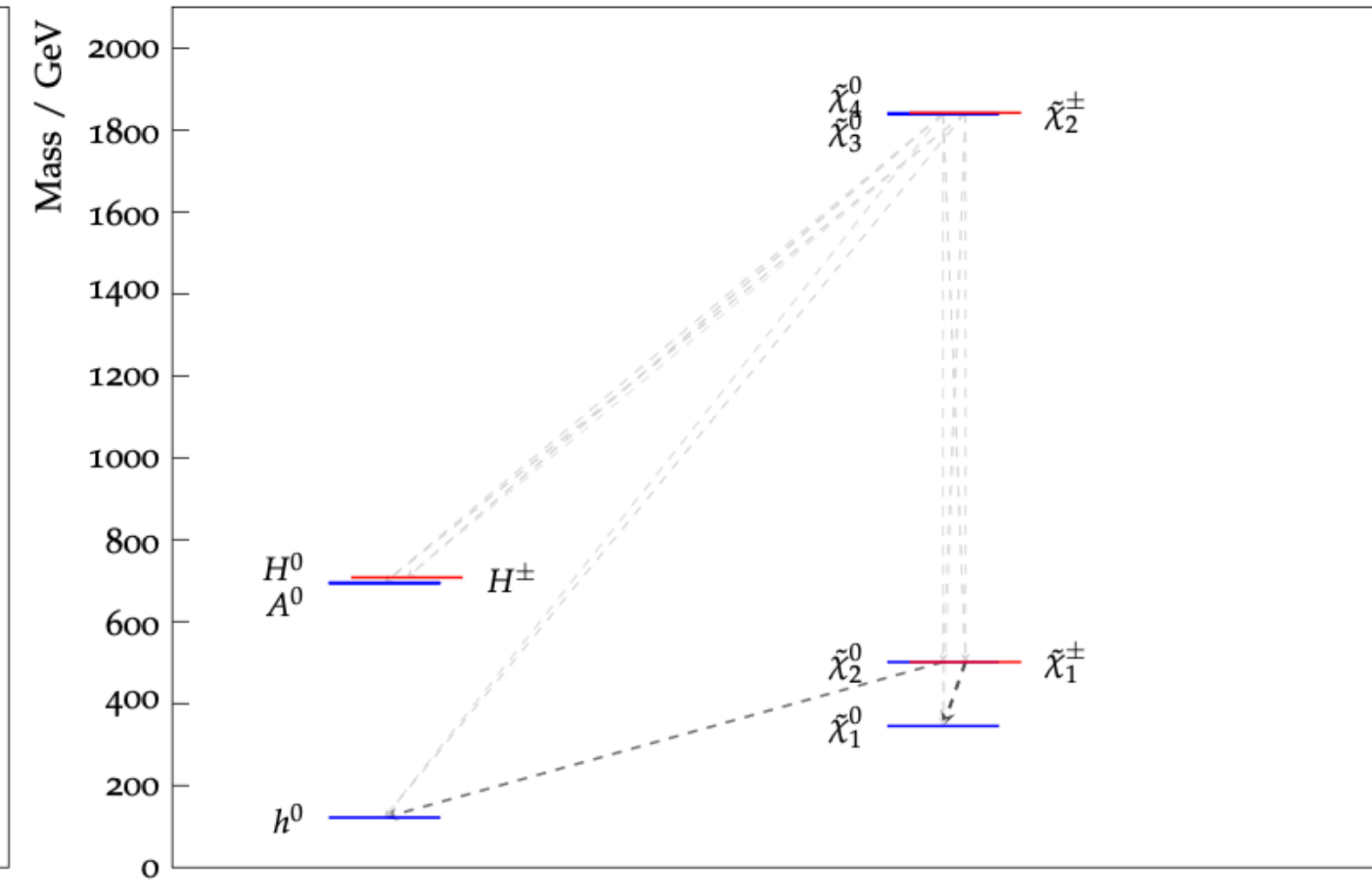
$$\langle \sigma \rangle \approx (y_H^\nu)^2 \cdot 10^{14 \div 15} \text{GeV}$$



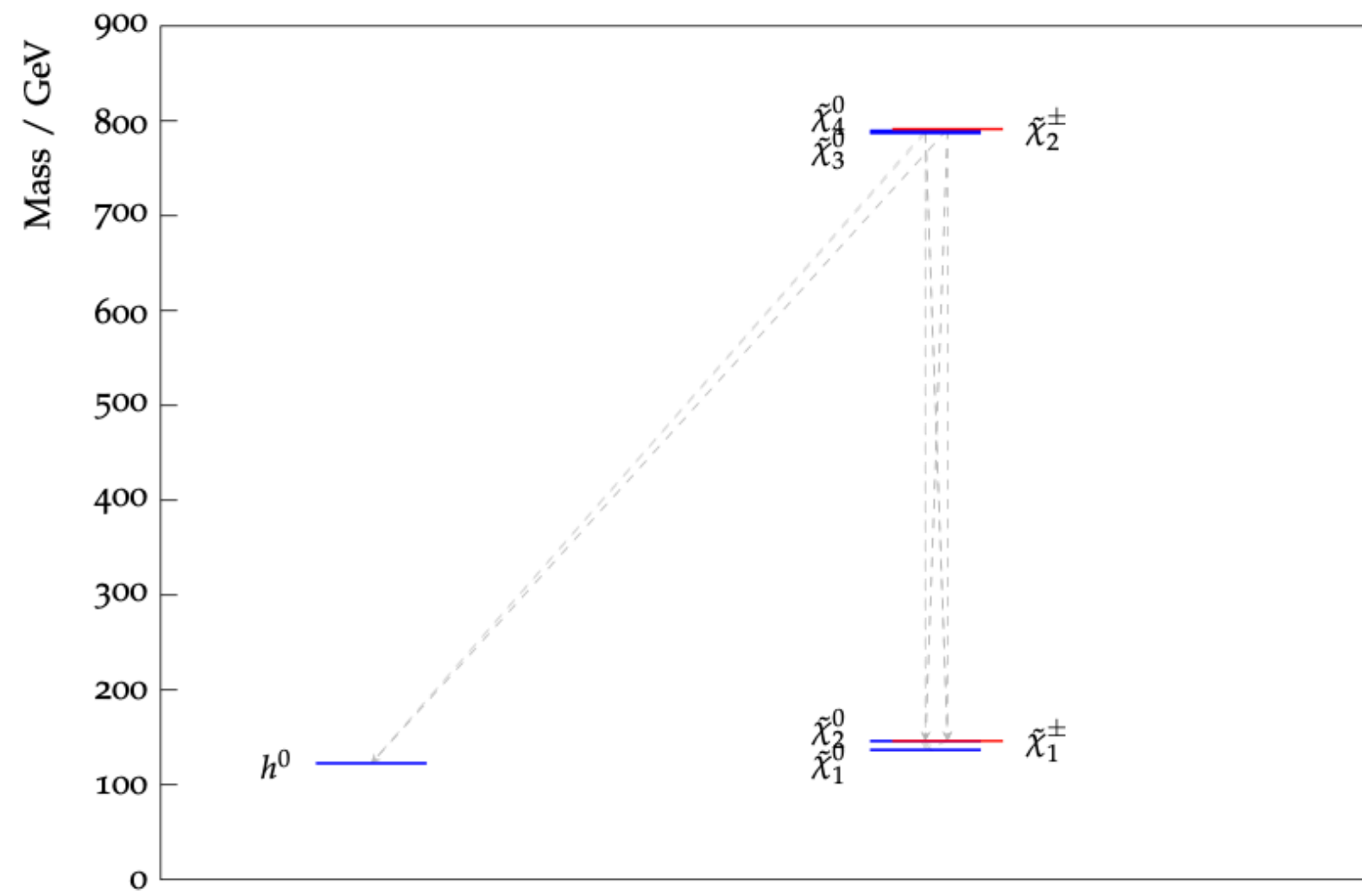
ATLAS, 2024



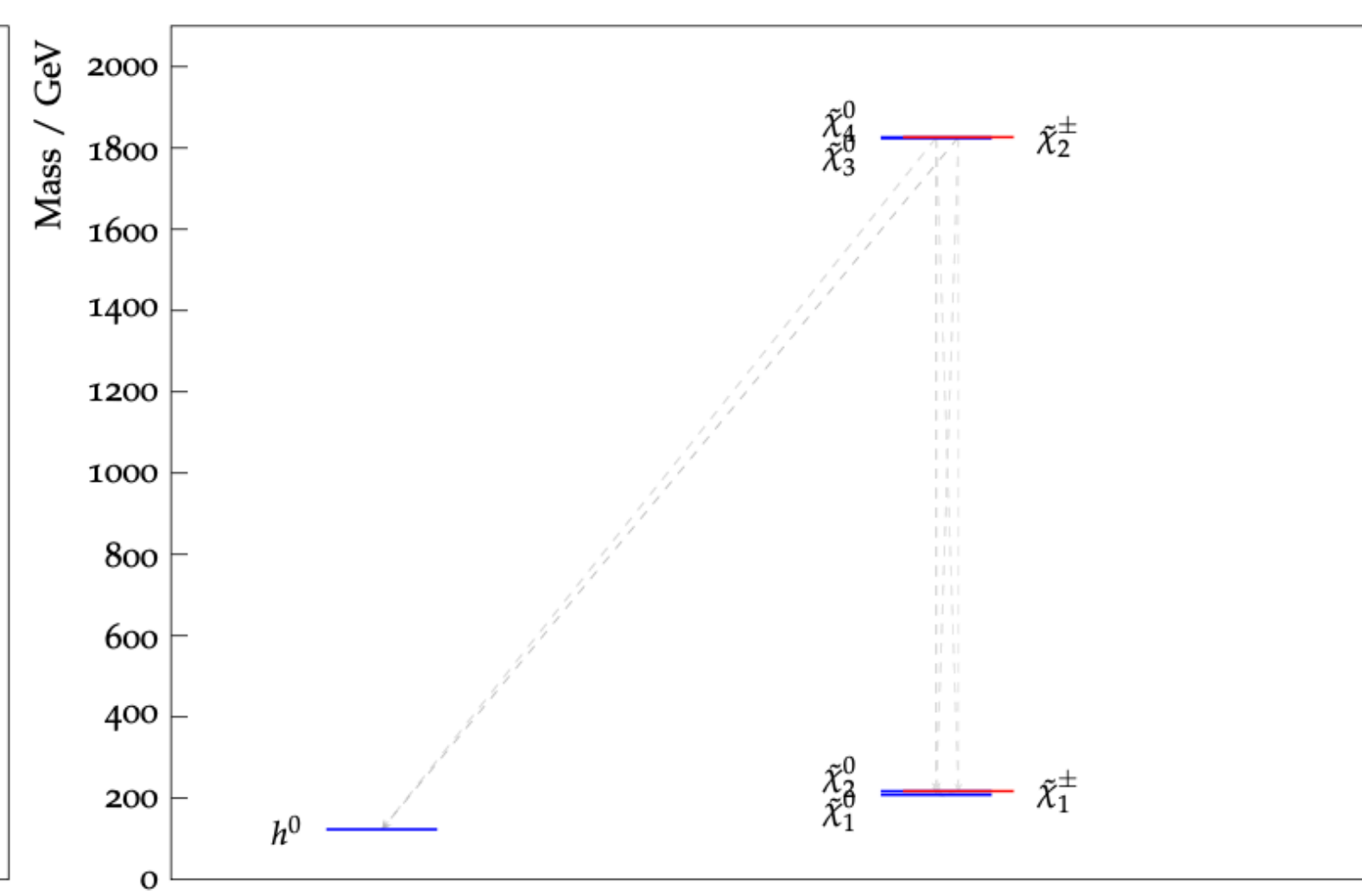
(a) Z/h funnel region



(b) A/H funnel region



(c) Compressed region



(d) Compressed region