

Recent developments in Flavor Physics, the Unitary Triangle Fit, Anomalies and all that

*Guido Martinelli
INFN Sezione di Roma
Università La Sapienza*

DIPARTIMENTO DI FISICA



SAPIENZA
UNIVERSITÀ DI ROMA

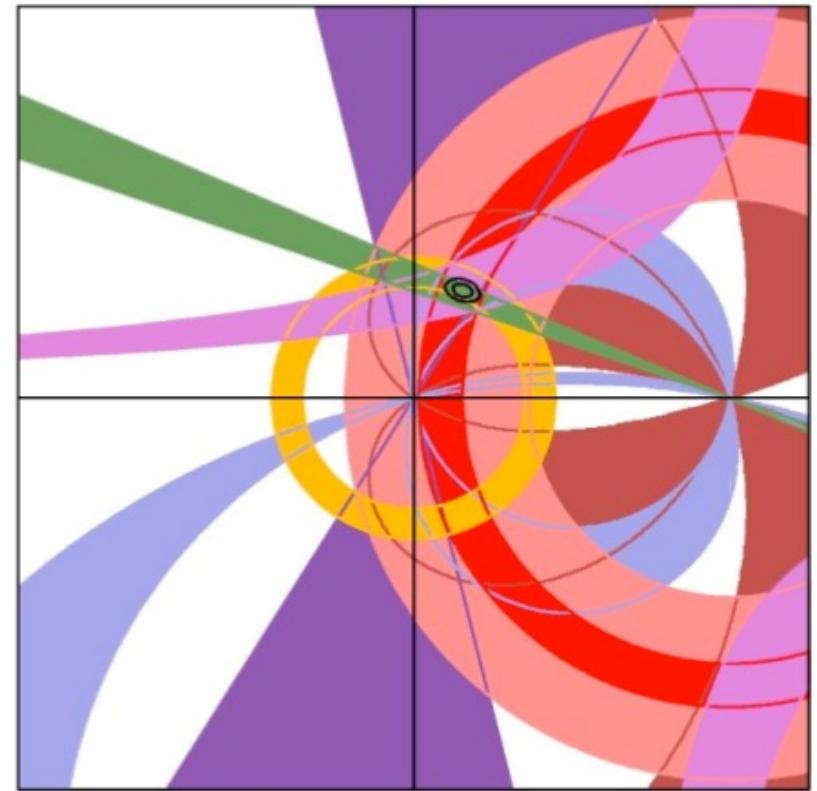


Roma September 24 2024



PLAN OF THE TALK

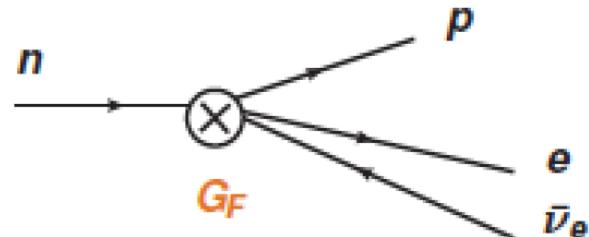
- *The lesson from the past*
- *Flavor in the SM*
- *Ufit Analysis, Tensions and unknown*
- *Flavor Beyond the SM*
- *Future directions, new/old ideas*
- *Conclusion*



Thanks to
R. Barbieri, M. Bona, A. Di Domenico,
G. Isidori, V. Lubicz, C. Sachrajda, L.
Silvestrini, S. Simula, L. Vittorio

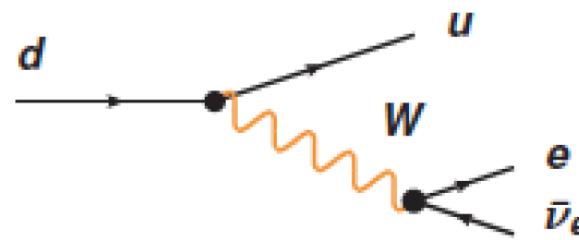
PAST of Flavour Physics

Historical example: β decay



Fermi constant

$$G_F \simeq 1.17 \times 10^{-5} \text{ GeV}^{-2}$$



W-boson exchange

$$\frac{G_F}{\sqrt{2}} = \frac{g_2^2}{8m_W^2}$$

E. Fermi, Attempt at a Theory of β -rays, *Il Nuovo Cimento*, Vol 11, p 1 (1934); *Zeitschrift fur Physik*, Vol 88, p 161 (1934)

*Unitarization of the Fermi theory:
New Physics at 10^2 GeV (indirect evidence)*

PAST of Flavour Physics

1963: Cabibbo Angle

1964: CP violation in K decays *

1970 GIM Mechanism

1973: CP Violation needs at least
three quark families (CKM) *

1975: discovery of the tau lepton –
3rd lepton family *

1977: discovery of the b quark -
3rd quark family

2003/4: CP violation in B meson
decays

* Nobel Prize



Discoveries from Flavor Physics

CP Violation

- ▶ the tiny branching ratio of the decay $K_L \rightarrow \mu^+ \mu^-$
led to the prediction of the charm quark to suppress FCNCs

(Glashow, Iliopoulos, Maiani 1970)

$$\Gamma(K \rightarrow \mu\mu) \ll \Gamma(K \rightarrow \mu\nu)$$

!!



- ▶ the measurement of the frequency of kaon anti-kaon oscillations

allowed a successful prediction of the charm quark mass

$$\Delta m_K$$

(Gaillard, Lee 1974)

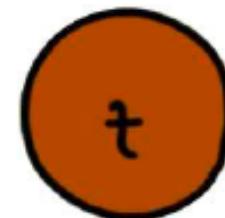
(direct discovery of the charm quark in 1974 at SLAC and BNL)

- ▶ the observation of CP violation in kaon anti-kaon oscillations

led to the prediction of the 3rd generation of quarks

(Kobayashi, Maskawa 1973)

$$\varepsilon_K$$



- ▶ the measurement of the frequency of $B - \bar{B}$ oscillations

allowed to predict the large top quark mass

$$\Delta m_B$$

(various authors in the late 80's)



(direct discovery of the bottom quark in 1977 at Fermilab)

(direct discovery of the top quark in 1995 at Fermilab)

indirect evidence

30 years of UT fit

- Since early '90s, the UT framework has been established to probe CP violation in the flavor sector

- $\sin 2\beta$ (CPV in $B_d \bar{B}_d$ mixing) the reference quantity

PREDICTIONS

- jump in accuracy ~ '95, when the first full statistical analysis was attempted, strongly benefiting of the first determination of the top mass. The UT analysis was born, predicting a few still unknown quantities

- $\sin 2\beta = 0.65 \pm 0.12$

- In 2000, Rome and Orsay/Genova groups (running similar fits) joined forces. This was the beginning of the UTfit collaboration

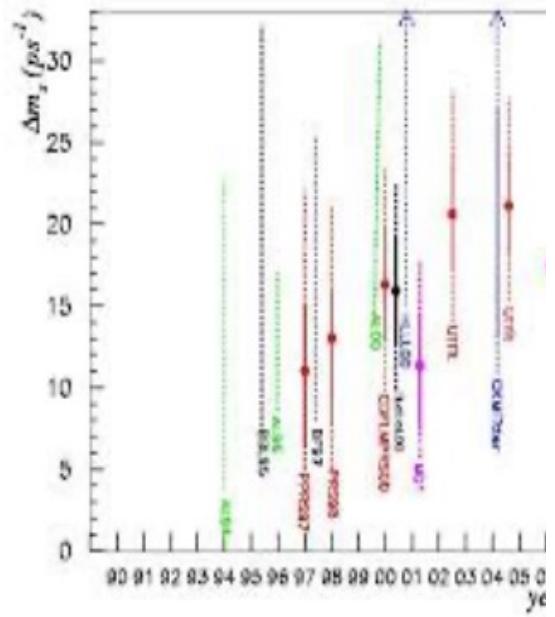
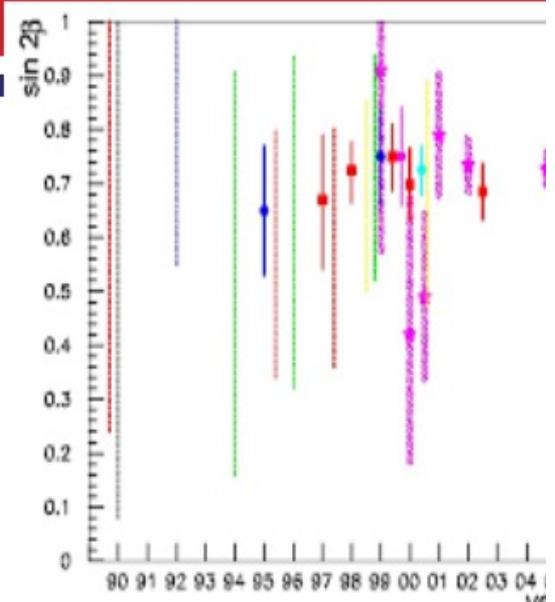
2000 CKM-TRIANGLE ANALYSIS
A Critical Review with Updated Experimental Inputs and Theoretical Parameters

M. Ciuchini^(a), G. D'Agostini^(b), E. Franco^(b), V. Lubicz^(a),
G. Martinelli^(b), F. Parodi^(c), P. Roudeau^(d) and A. Stocchi^(d)

- Flavour, EW fit: $m_t \sim 170$ GeV

- EW fit: $m_H = 100 \pm 30$ GeV

Courtesy by M. Pierini



PRESENT:the Standard Model and beyond

Vacuum
Energy

Hierarchy

Vacuum
Stability

$$\mathcal{L} = \Lambda^4 + \Lambda^2 H^2 + \lambda H^4 + (D_\mu H)^2 + \bar{\psi} \not{D} \psi + F_{\mu\nu}^2 + F_{\mu\nu} \tilde{F}_{\mu\nu}$$

Higgs meson 2012

neutral currents 1973

charm quark 1974

YH $\bar{\psi}\psi$ + $\frac{1}{\Lambda}(\bar{L}H)^2 + \frac{1}{\Lambda^2} \sum_i C_i O_i + \dots$

Buchmuller&Wyler '88

Flavor
puzzle

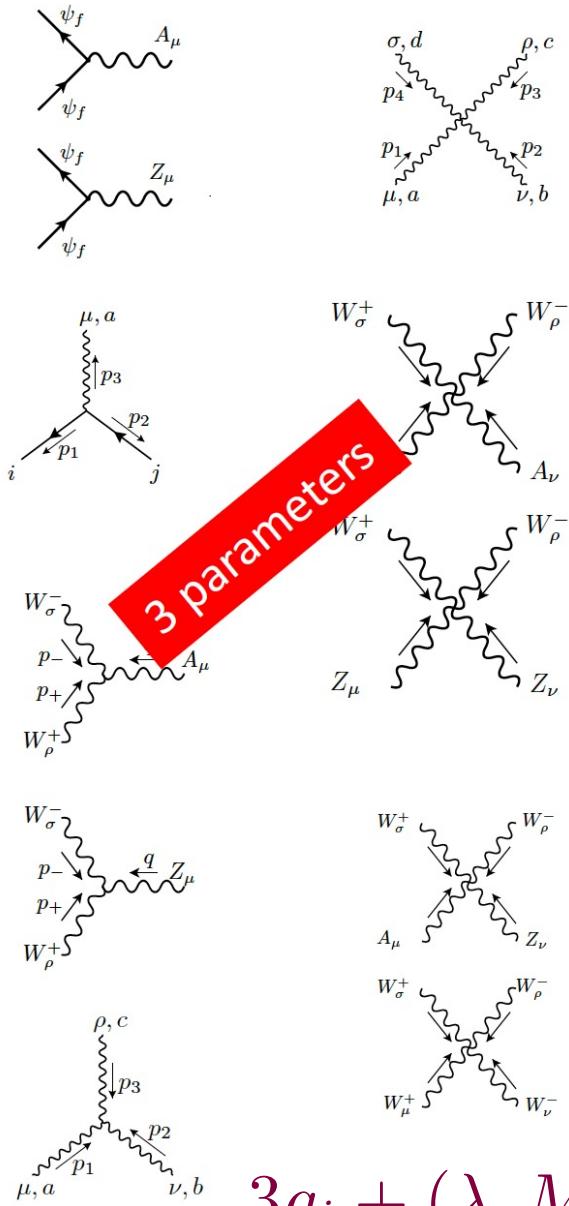
Neutrino
Masses

New Physics
Possible breaking of
accidental
symmetries

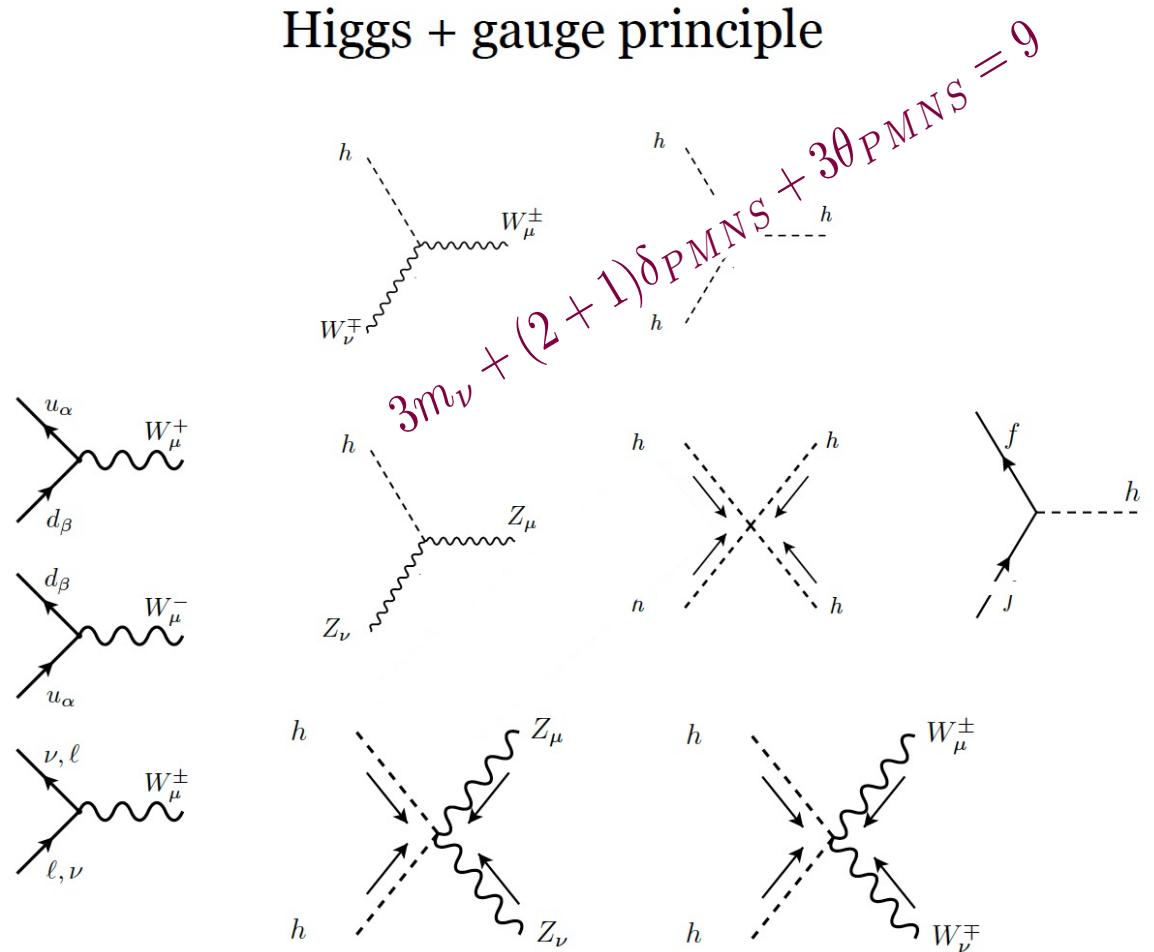
Only circled terms discussed in this talk

The Standard Model

$$SU(3) \times SU(2) \times U(1)_Y$$



Higgs + gauge principle



from elegance to caos !!

If we are looking for the suspect that could be hiding some secret obviously the higgs is the one!

$$3g_i + (\lambda, M_H) + 6m_q + 3m_\ell + \delta + 3\theta_{CKM} + \theta_{QCD} = 19$$

The Weirdness of the Standard Model

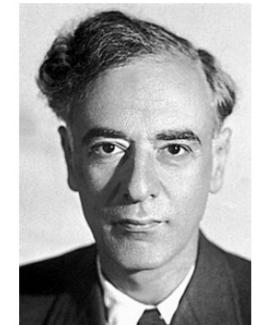
- Three families

$3m_\nu + (2+1)\delta_{PMNS} + 3\theta_{PMNS} = 9$
“who ordered that ?” I. Rabi



- Fundamental breaking of Parity

“space cannot be asymmetric!” L. Landau



- Predictivity: 3 gauge couplings + 16 higgs couplings (+ 7 higgs-neutrino) !
+ the coupling θ of strong CP violation

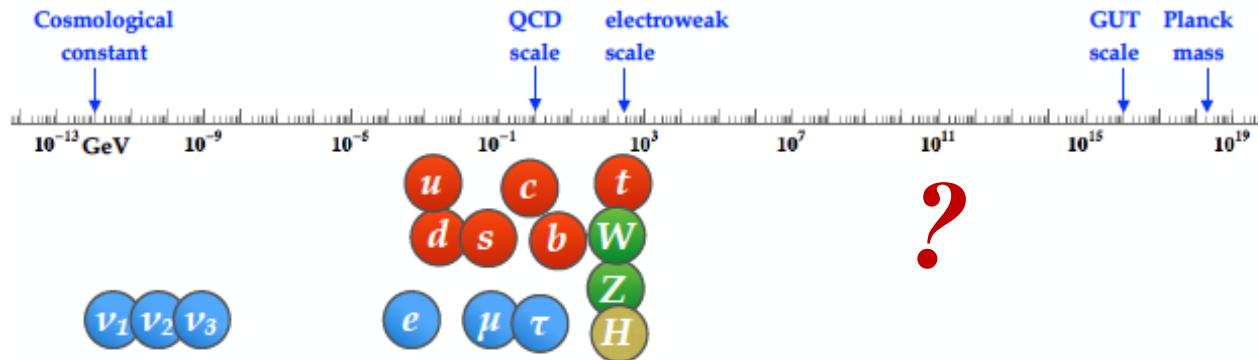


“has too many arbitrary features for [its] predictions
to be taken very seriously” S. Weinberg '67



$$3g_i + (\lambda, M_H) + 6m_q + 3m_\ell + \delta + 3\theta_{CKM} + \theta_{QCD} = 19$$

Zupan



J. ZUPAN

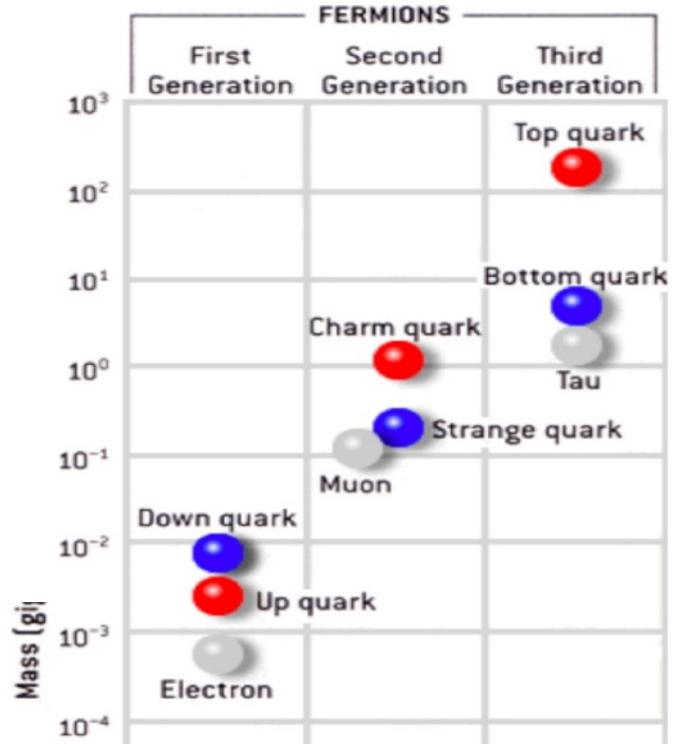


Illustration from a G. Isidori talk

$$m_\nu \leq 1 \text{ eV}$$

Quark Masses from Lattice QCD

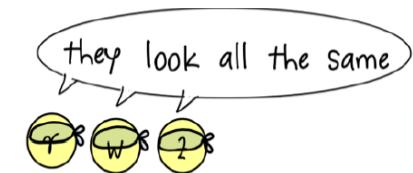
| Input | Lattice/Exp |
|--|---------------|
| $m_u^{\overline{\text{MS}}}(2 \text{ GeV})$ | 2.20(9) MeV |
| $m_d^{\overline{\text{MS}}}(2 \text{ GeV})$ | 4.69(2) MeV |
| $m_s^{\overline{\text{MS}}}(2 \text{ GeV})$ | 93.14(58) MeV |
| $m_c^{\overline{\text{MS}}}(3 \text{ GeV})$ | 993(4) MeV |
| $m_c^{\overline{\text{MS}}}(m_c^{\overline{\text{MS}}})$ | 1277(5) MeV |
| $m_b^{\overline{\text{MS}}}(m_b^{\overline{\text{MS}}})$ | 4196(19) MeV |
| $m_t^{\overline{\text{MS}}}(m_t^{\overline{\text{MS}}}) \text{ (GeV) to be updated}$ | 163.44(43) |

Table 3 Full lattice inputs. The values of the different quantities have been taking the weighted average of the $N_f = 2 + 1$ and $N_f = 2 + 1 + 1$ FLAG runs.

Hints of NP structure: Flavor symmetries of the SM

- Standard Model (SM) gauge sector is flavor blind and CP conserving

$$\mathcal{G}_F(\text{SM}) = U(3)^5 \equiv U(3)_q \times U(3)_u \times U(3)_d \times U(3)_\ell \times U(3)_e$$

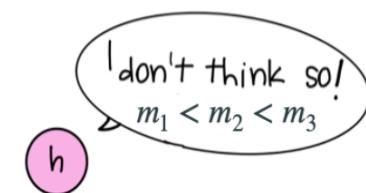


The Higgs introduces the only known non-gauge couplings

Turn on Yukawas



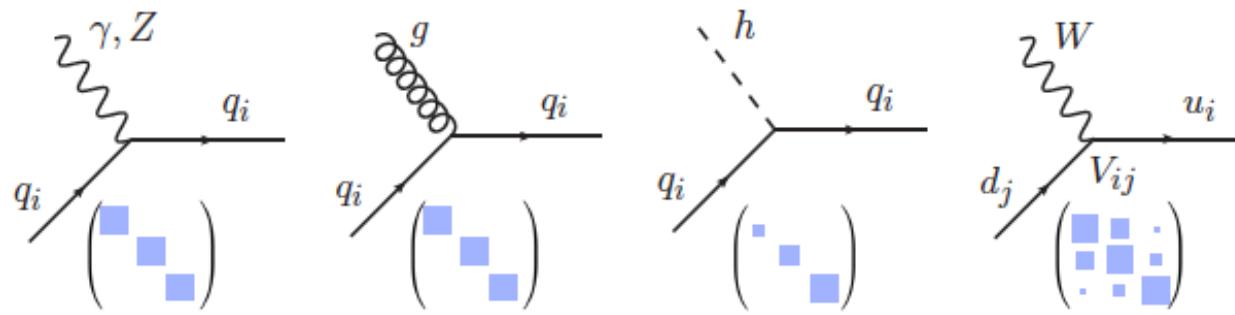
$$Y_{ij} \bar{\Psi}_L^i H \Psi_R^j$$



$$\mathcal{G}_F(\text{SM}) = U(1)_B \times U(1)_L$$

Higgs couplings are not flavor blind

courtesy of B.A. Stefanek
See talk by R. Barbieri



| electromagnetic | neutral currents | charged currents |
|--|------------------|------------------|
| | | |
| $\mathcal{L}_{int} = -e A^\mu J_\mu^{em} - \frac{g_W}{2 \cos \theta_W} Z^\mu J_\mu^Z - \frac{g_W}{2\sqrt{2}} [W^\mu (J^W)_\mu^\dagger + h.c.]$ | | |

$$J_\mu^Z = 2J_\mu^3 - 2 \sin^2 \theta_W J_\mu^{em}$$

$$\begin{aligned} L_{CC}^{weak int} &= \frac{g_W}{\sqrt{2}} (J_\mu^- W_\mu^+ + h.c.) \\ &\rightarrow \frac{g_W}{\sqrt{2}} (\bar{u}_L \mathbf{V}^{CKM} \gamma_\mu d_L W_\mu^+ + \dots) \end{aligned}$$

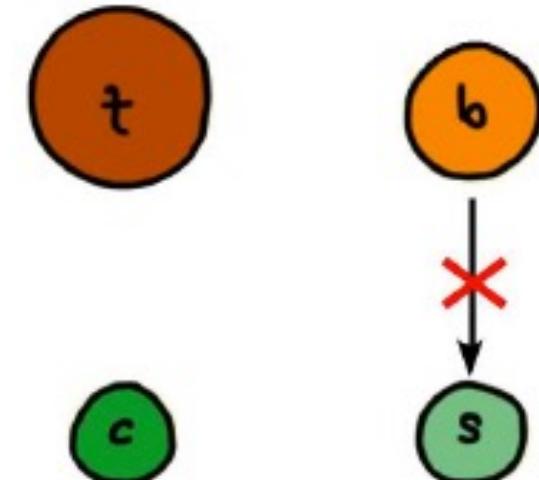
Absence of FCNC at tree level (& GIM suppression of FCNC @loop level)

Almost no CP violation at tree level

Tiny CP violation in K and D mesons due to small coupling between the third and the two first generations

Flavour Physics is extremely sensitive to New Physics (NP)

In competition with Electroweak Precision Measurements



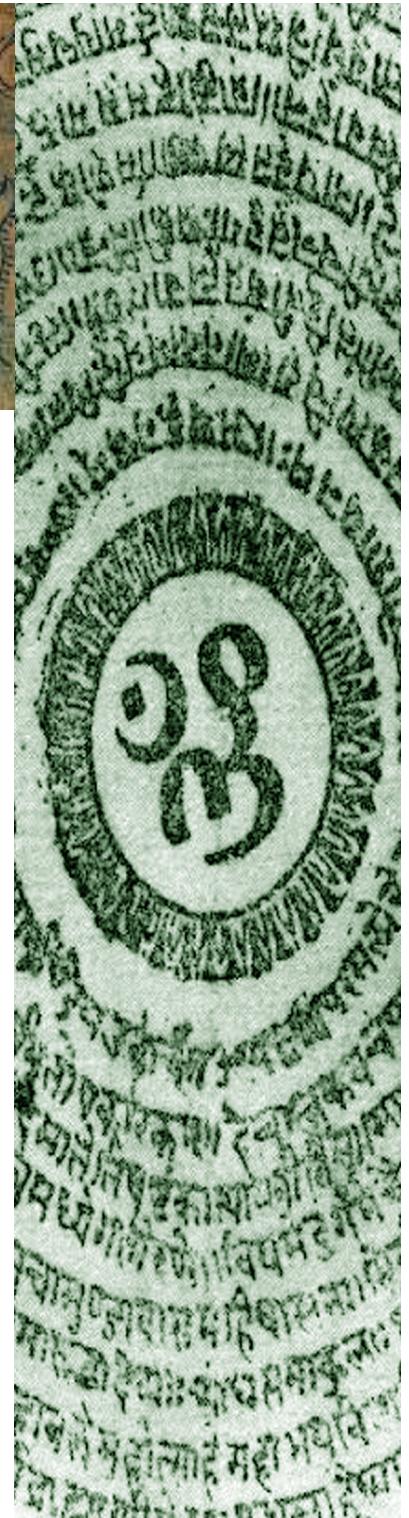
The usual mantra *reasons to go beyond the SM(s):*

“Experimental” evidence

1. *Neutrino Masses*
2. *Dark Matter and Dark Energy*
3. *Matter-Antimatter Asymmetry*

“Theoretical” evidence

1. *SM instability (hierarchy, naturalness)*
2. *Flavour Physics (families, Yukawa couplings, CP violation for both quarks and leptons)*
3. *Unification of forces and quantization of gravity*



Why Flavor Physics is so important:

It is sensitive to NP scales $\Lambda_{NP} \gg E_{\text{collider}}$ since FCNC are suppressed in the SM by loops and small $|V_{ij}|$

SM Flavor puzzle:

*Why flavor parameters are so small and hierarchical?
(and different from the neutrino sector)*

NP Flavor puzzle:

If NP is at the TeV scale, why FCNC effects are so small that they have not be detected yet?

WHY RARE DECAYS ?

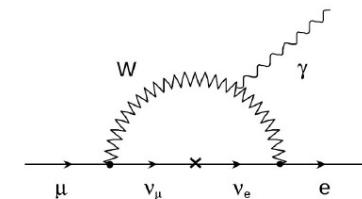
Rare decays are a manifestation of broken (accidental) symmetries e.g. of physics beyond the Standard Model

Proton decay

$$\mu \rightarrow e + \gamma$$

$$v_i \rightarrow v_k \text{ found !}$$

baryon and lepton number conservation
lepton flavor number



$$\mathcal{B}(\mu \rightarrow e\gamma) \sim \alpha \frac{m_\nu^4}{m_W^4} \sim 10^{-52}$$

Rare decays allowed in the SM

$$q_i \rightarrow q_k + \nu \bar{\nu}$$

$$q_i \rightarrow q_k + l^+ l^-$$

$$q_i \rightarrow q_k + \gamma$$

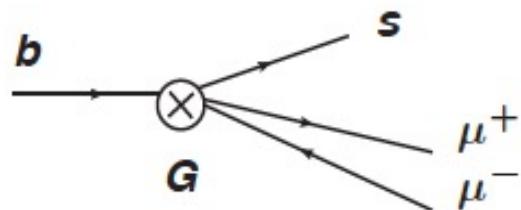
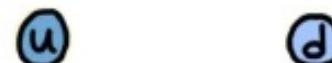
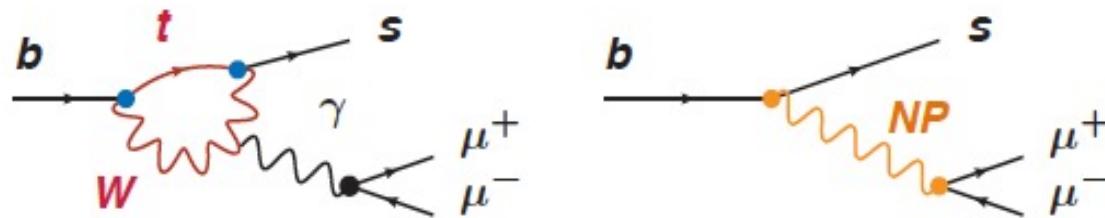
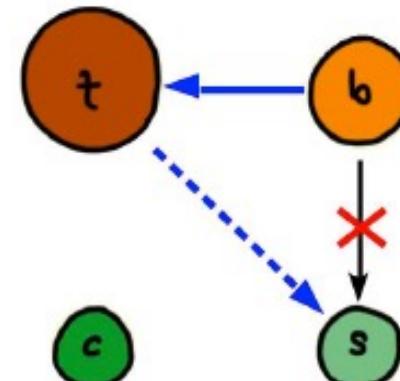
these decays occur only via loops and are suppressed by CKM because of GIM

THUS THEY ARE SENSITIVE TO
NEW PHYSICS

Flavor Changing Neutral Currents in the SM

In the SM, flavor changing neutral currents (FCNCs)
are absent at the tree level

FCNCs can arise at the **loop level**
they are suppressed by **loop factors**
and small **CKM elements**



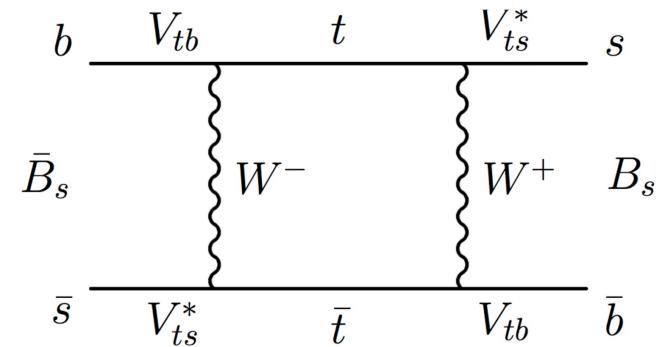
$$G \sim \frac{1}{16\pi^2} \frac{g^4}{m_W^2} \frac{m_t^2}{m_W^2} V_{tb} V_{ts}^* + \frac{C_{NP}}{\Lambda_{NP}^2}$$

→ measuring low energy flavor observables gives information
on new physics flavor couplings and the new physics mass scale

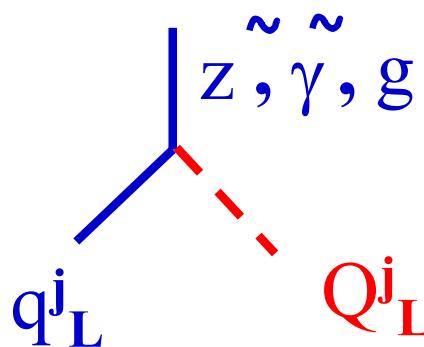
$B^0 - \bar{B}^0$ mixing

Standard Model CKM

$$\Delta m_{B_s} = \frac{G_F^2 M_W^2}{16\pi^2} A^2 \lambda^6 F_{tt} \left(\frac{m_t^2}{M_W^2} \right) \langle B_s | (\bar{s}\gamma_\mu(1-\gamma_5)b)^2 | \bar{B}_s \rangle$$



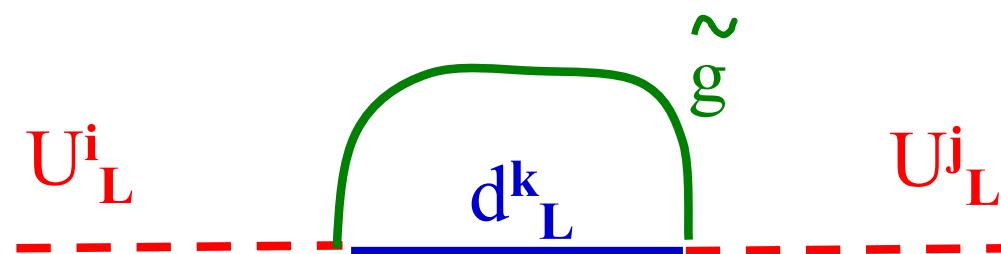
Hadronic matrix element



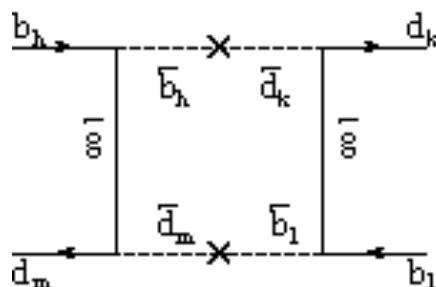
In general the mixing mass matrix of the SQuarks (SMM) is not diagonal in flavour space analogously to the quark case

We may either
Diagonalize the SMM

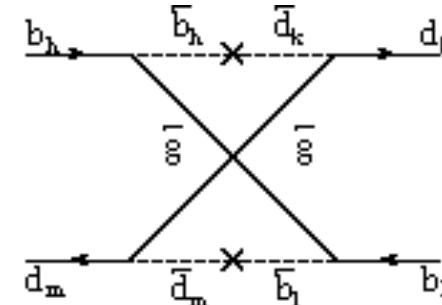
or Rotate by the same
Matrices the SUSY partners of
the u- and d-like quarks
 $(Q^j_L)' = U^{ij}_L Q^i_L$



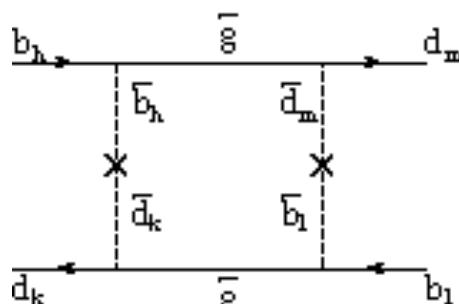
In the latter case the Squark Mass Matrix is not diagonal



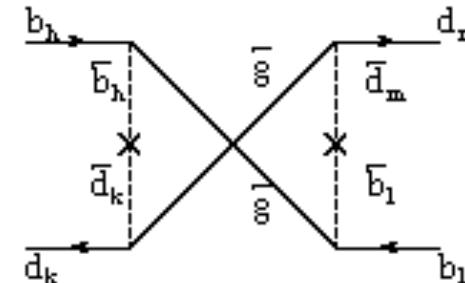
a)



c)



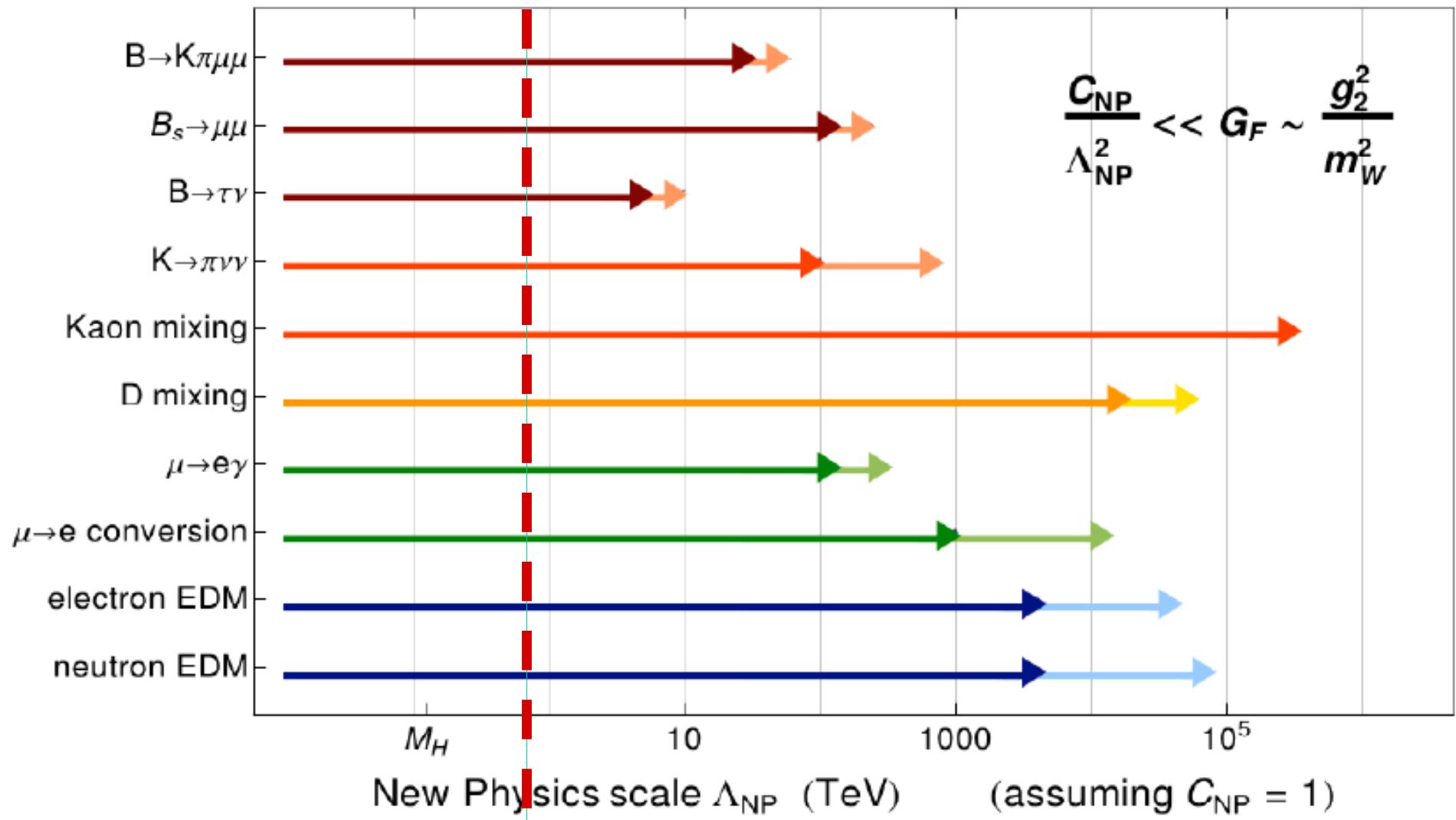
b)



d)

$$(m_Q^2)_{ij} = m_{average}^2 \mathbf{1}_{ij} + \Delta m_{ij}^2 \quad \delta_{ij} = \Delta m_{ij}^2 / m_{average}^2$$

Sensitivity to New Physics from Flavor I

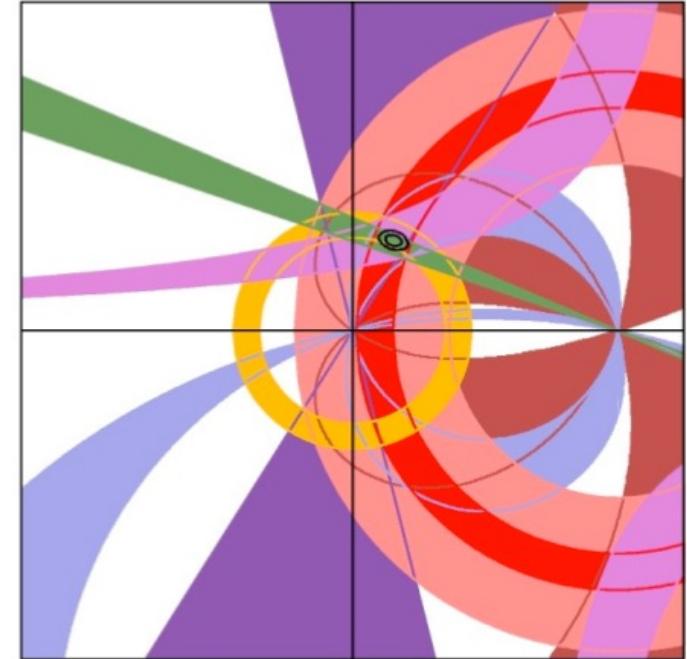


Approximate LHC direct reach

STANDARD MODEL UNITARITY TRIANGLE ANALYSIS Tensions and Unknown

1. Provides the best determination of the CKM parameters;
2. Tests the consistency of the SM ("direct" vs "indirect" determinations) @ the quantum level;
3. Provides predictions for SM observables (in the past for example $\sin 2\beta$ and Δm_S)
4. It could lead to new discoveries (CP violation, Charm, !?)
5. The discovery potential of precision flavor physics should not be underestimated

It is by now precision physics and we need precise lattice calculations



*New UTfit Analysis of the Unitarity Triangle
in the Cabibbo-Kobayashi-
Maskawa scheme*

*Rend.Lincei Sci.Fis.Nat. 34 (2023) 37-57
arXiv:2212.03894*

$$N(N-1)/2 \quad \text{angles} \quad \text{and} \quad (N-1)(N-2)/2 \quad \text{phases}$$

**N=3 3 angles + 1 phase KM
the phase generates complex couplings i.e. CP
violation;**

6 masses +3 angles +1 phase = 10 parameters

| V_{ud} | V_{us} | V_{ub} |
|----------|----------|----------|
| V_{cd} | V_{cs} | V_{cb} |
| V_{tb} | V_{ts} | V_{tb} |

$$\begin{aligned} L_{CC}^{weak\,int} &= \frac{g_W}{\sqrt{2}} (J_\mu^- W_\mu^+ + h.c.) \\ &\rightarrow \frac{g_W}{\sqrt{2}} (\bar{u}_L \mathbf{V}^{CKM} \gamma_\mu d_L W_\mu^+ + \dots) \end{aligned}$$

$$= \begin{bmatrix} c_{12}c_{13} & s_{12}c_{13} & s_{13}e^{-i\delta_{13}} \\ -s_{12}c_{23} - c_{12}s_{23}s_{13}e^{i\delta_{13}} & c_{12}c_{23} - s_{12}s_{23}s_{13}e^{i\delta_{13}} & s_{23}c_{13} \\ s_{12}s_{23} - c_{12}c_{23}s_{13}e^{i\delta_{13}} & -c_{12}s_{23} - s_{12}c_{23}s_{13}e^{i\delta_{13}} & c_{23}c_{13} \end{bmatrix}$$

STRONG CP VIOLATION

$$\mathcal{L}_\theta = \theta G^{\mu\nu a} \tilde{G}_{\mu\nu}^a$$

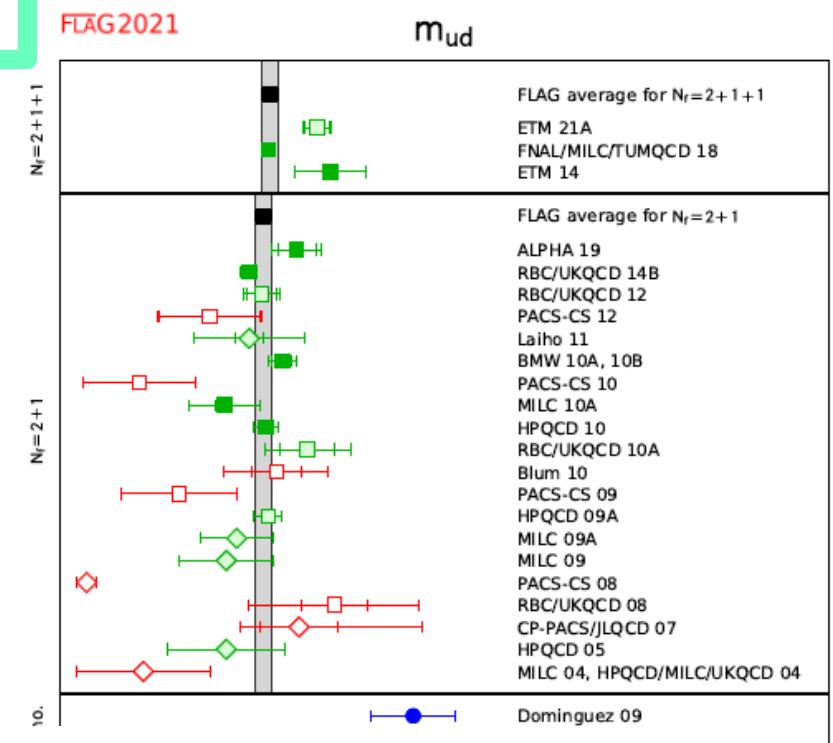
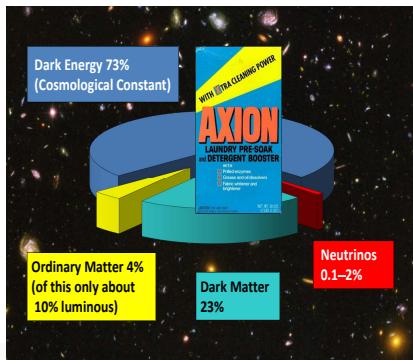
$$\tilde{G}_{\mu\nu}^a = \epsilon_{\mu\nu\rho\sigma} G_{\rho\sigma}^a$$

$$L_\theta \sim \theta \vec{E}^a \cdot \vec{B}^a$$

This term violates CP and gives a contribution to the electric dipole moment of the neutron

$$e_n < 3 \cdot 10^{-26} \text{ e cm}$$

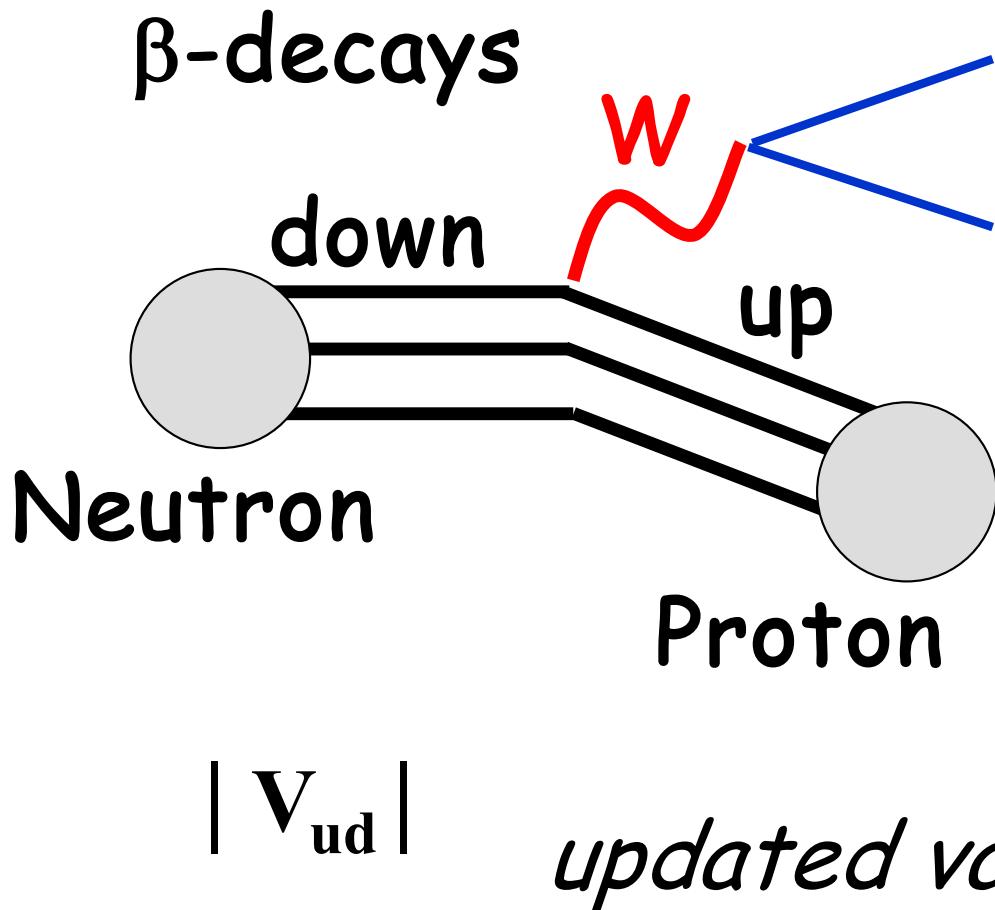
$\theta < 10^{-10}$ which is quite unnatural !!



| N_f | m_u | m_d | m_u/m_d | R | Q | MeV |
|-------|---------|---------|-----------|-----------|-----------|-----|
| 2+1+1 | 2.14(8) | 4.70(5) | 0.465(24) | 35.9(1.7) | 22.5(0.5) | |
| 2+1 | 2.27(9) | 4.67(9) | 0.485(19) | 38.1(1.5) | 23.3(0.5) | |

Quark masses & Generation Mixing

| | | |
|----------|----------|----------|
| V_{ud} | V_{us} | V_{ub} |
| V_{cd} | V_{cs} | V_{cb} |
| V_{td} | V_{ts} | V_{tb} |



| |
|---------------------------|
| $ V_{ud} = 0.9735(8)$ |
| $ V_{us} = 0.2196(23)$ |
| $ V_{cd} = 0.224(16)$ |
| $ V_{cs} = 0.970(9)(70)$ |
| $ V_{cb} = 0.0406(8)$ |
| $ V_{ub} = 0.00409(25)$ |
| $ V_{tb} = 0.99(29)$ |

The Wolfenstein Parametrization

| | | |
|--|-----------------------------|-----------------------------|
| $1 - \frac{1}{2} \lambda^2$ | λ | $A \lambda^3(\rho - i\eta)$ |
| $-\lambda$ | $1 - \frac{1}{2} \lambda^2$ | $A \lambda^2$ |
| $A \lambda^3 \times$ $(1 - \rho - i\eta)$ | $-A \lambda^2$ | 1 |

V_{ub}

$+ O(\lambda^4)$

It is really of
 $O(\lambda^3)$?

V_{td}

$$\lambda \sim 0.2 \quad A \sim 0.8$$

$$\eta \sim 0.2 \quad \rho \sim 0.3$$

| |
|--|
| $\sin \theta_{12} = \lambda$ |
| $\sin \theta_{23} = A \lambda^2$ |
| $\sin \theta_{13} = A \lambda^3(\rho - i\eta)$ |

The Unitarity Triangle Analysis

- Flavor-changing processes and CP violation in the SM ruled by 4 parameters in the 3x3 CKM (unitary) matrix

$$V_{\text{CKM}} = \begin{pmatrix} 1 - \lambda^2/2 & \lambda & A\lambda^3(\rho - i\eta) \\ -\lambda & 1 - \lambda^2/2 & A\lambda^2 \\ A\lambda^3(1 - \rho - i\eta) & -A\lambda^2 & 1 \end{pmatrix} + \mathcal{O}(\lambda^4)$$

- $A, \lambda, \bar{\rho}$ and $\bar{\eta}$

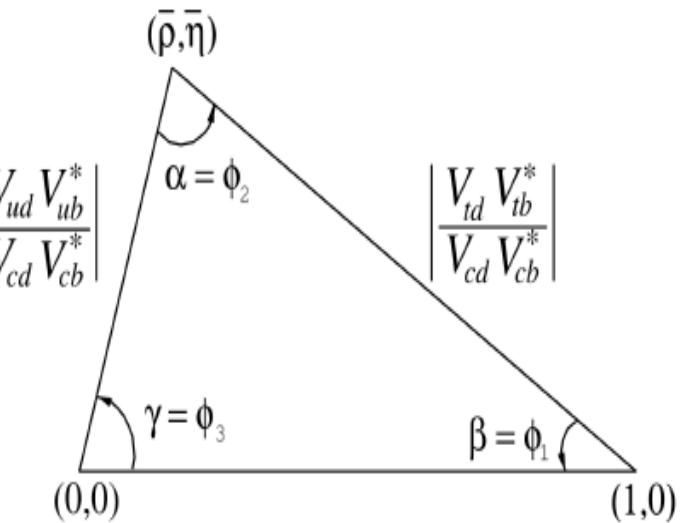
$$\bar{\rho} = \rho(1 - \lambda^2/2 + \dots) \quad \bar{\eta} = \eta(1 - \lambda^2/2 + \dots)$$

- Small value sin of Cabibbo angle (λ) makes the CKM matrix close to diagonal

- Unitarity implies relations between elements, that can be represented as a triangle in a plane

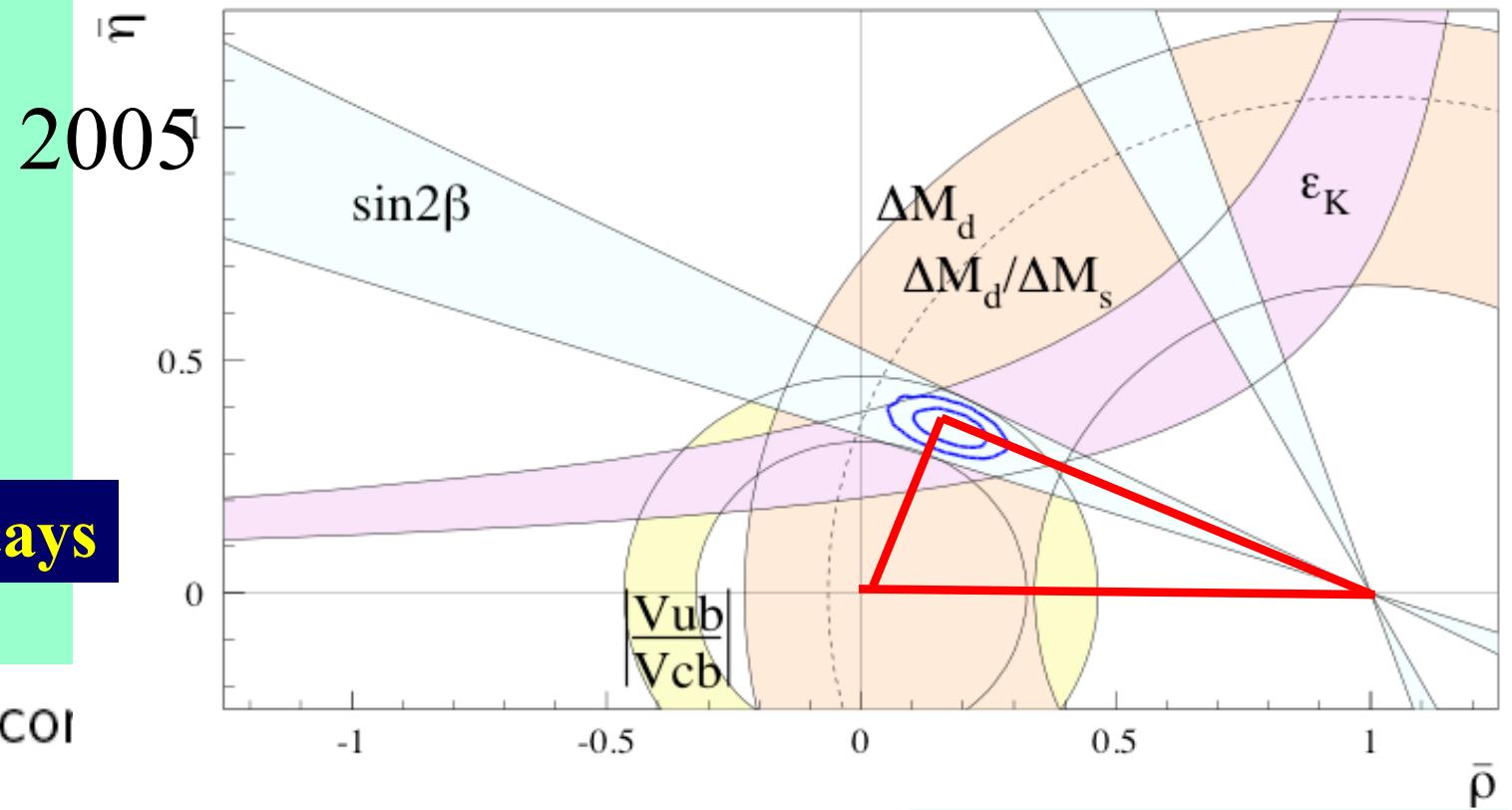
- By determining the CKM matrix

$$\begin{aligned} \sin \theta_{12} &= \lambda \\ \sin \theta_{23} &= A \lambda^2 \\ \sin \theta_{13} &= A \lambda^3(\rho - i\eta) \end{aligned}$$



$$\delta_{13} = \gamma = \phi_3$$

Unitary Triangle SM



semileptonic decays

Experimental cor

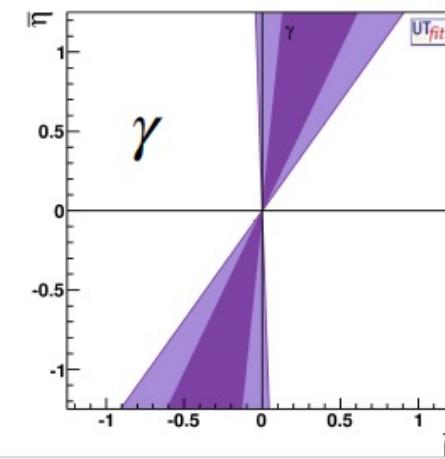
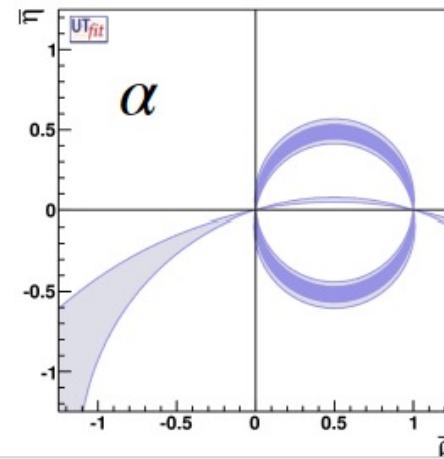
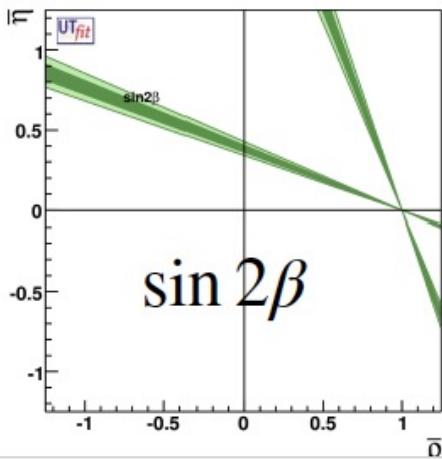
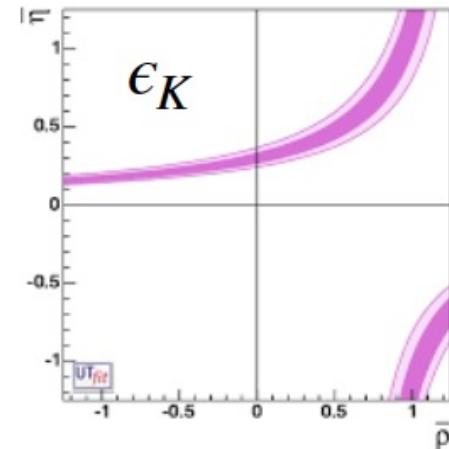
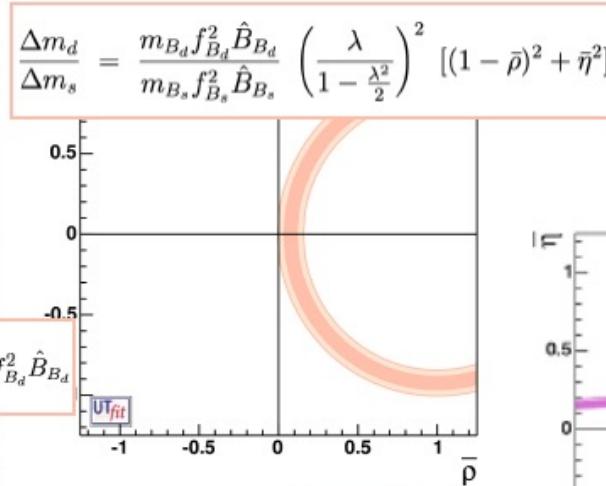
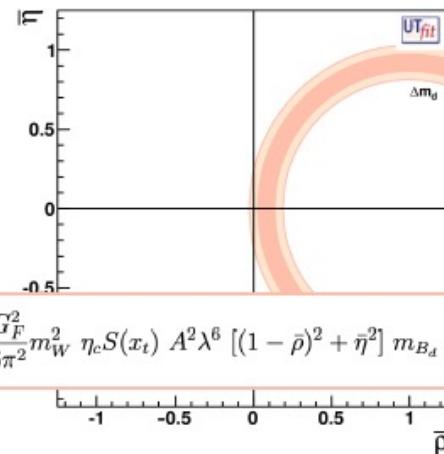
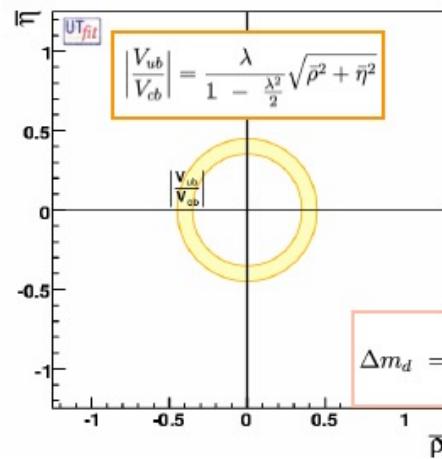
| Meas. | $V_{CKM} \times \text{other}$ | $(\bar{\rho}, \bar{\eta})$ |
|---|--|--|
| $\frac{b \rightarrow u}{b \rightarrow c}$ | $ V_{ub}/V_{cb} ^2$ | $\bar{\rho}^2 + \bar{\eta}^2$ |
| Δm_d | $ V_{td} ^2 f_{B_d}^2 B_{B_d}$ | $(1 - \bar{\rho})^2 + \bar{\eta}^2$ |
| $\frac{\Delta m_d}{\Delta m_s}$ | $\left \frac{V_{td}}{V_{ts}} \right ^2 \xi^2$ | $(1 - \bar{\rho})^2 + \bar{\eta}^2$ |
| ϵ_K | $f(A, \bar{\eta}, \bar{\rho}, B_K)$ | $\propto \bar{\eta}(1 - \bar{\rho})$ |
| $A(J/\psi K^0)$ | $\sin 2\beta$ | $\sqrt{\bar{\eta}^2 + (1 - \bar{\rho})^2}$ |

$B_{d,s}^0 - \bar{B}_{d,s}^0$ mixing

$K^0 - \bar{K}^0$ mixing

B_d

UT constraints



redundancy is the big strength of the UT analysis
 one can remove a subset of inputs and still determine the CKM
 one can exclude $\eta=0$ using only CP conserving processes

The ancestor of Utfit

M.Lusignoli, L.Maiani, G.Martinelli, L.Reina

MIXING AND CP-VIOLATION IN K AND B-MESONS: A LATTICE QCD POINT OF VIEW

(Revised version)

The main result of our analysis is that if m_t is not too small:

$$(1.2) \quad m_t > 140 \text{ GeV}$$

and if f_B is in the range:

$$(1.3) \quad 200 \text{ MeV} < f_B < 300 \text{ MeV}$$

the CP-violating asymmetry in the decay: $B_d \bar{B}_d \rightarrow J/\Psi + K_S + \text{tagging channel}$, should be considerably larger than previously expected.

To illustrate the results, we make reference to the central case:

$$m_t = 140 \text{ GeV}$$

Fig.2.b, gives the distribution of $\cos\delta_1$ and $\cos\delta_2$. A clear separation of positive and negative solutions is seen:

$$(8.1) \quad \cos\delta_1 = -0.89 \pm 0.09$$

$$(8.2) \quad \cos\delta_2 = +0.64 \pm 0.17$$

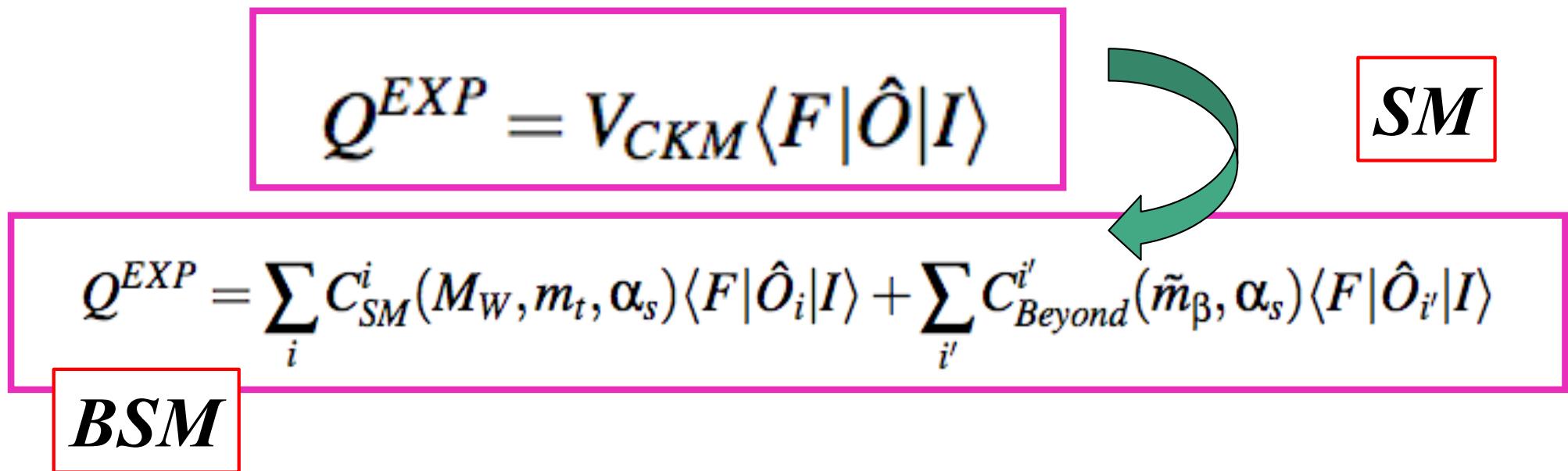
Figs.3.b and 4.b give the corresponding distributions of $\sin(2\beta)$ and $\sin(2\alpha)$. The two solutions for $\cos\delta$ correspond to two reasonably well separated regions in $\sin(2\beta)$:

$$(8.3) \quad \sin(2\beta_1) = +0.27 \pm 0.08$$

$$(8.4) \quad \sin(2\beta_2) = +0.82 \pm 0.11$$

The extraordinary progress of the experimental measurements requires accurate theoretical predictions

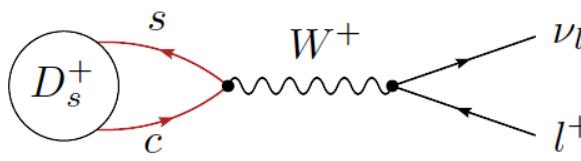
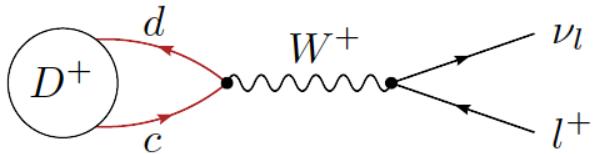
Precision flavor physics requires the control of hadronic effects for which lattice QCD simulations are essential



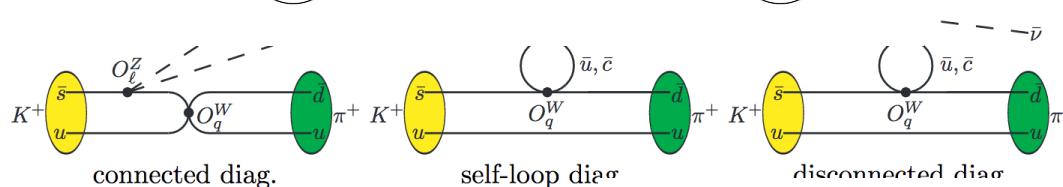
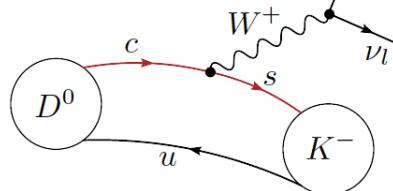
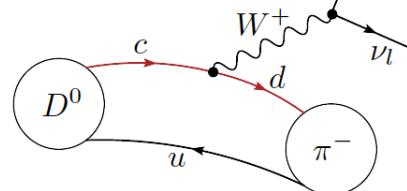
*What can be computed and
What cannot be computed*



Leptonic (π, K, D, B)



Semileptonic (K, D, B)

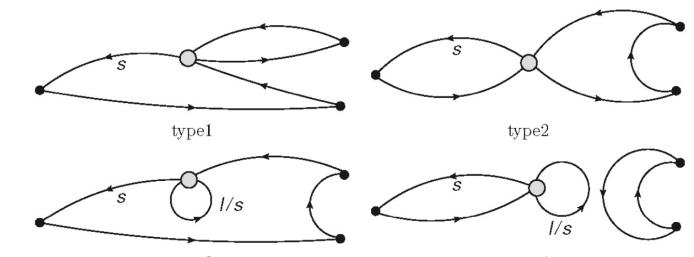


Neutral meson mixing (local)

(some) Radiative and Rare long distance effects
(also $K \rightarrow \pi l^+ l^-$)

Non-leptonic

but only below the inelastic threshold
(may be also
3 body decays) now changing



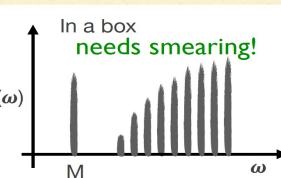
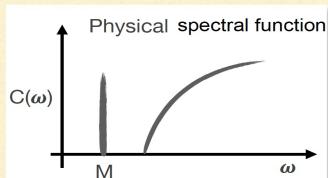
$B \rightarrow \pi\pi, K\pi$, etc. No- $>$ maybe!

INCLUSIVE DECAYS ON THE LATTICE

Inclusive processes impractical to treat directly on the lattice. Vacuum current correlators computed in euclidean space-time are related to $e^+e^- \rightarrow$ hadrons or τ decay via analyticity. In our case the correlators have to be computed in the B meson, but analytic continuation more complicated: two cuts, decay occurs only on a portion of the physical cut.

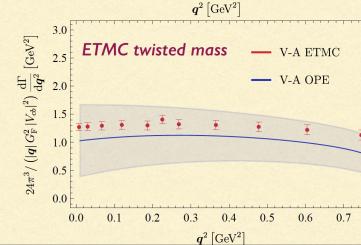
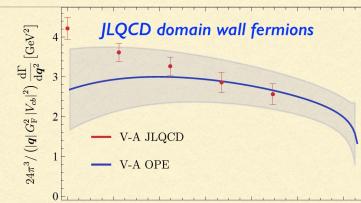
While the lattice calculation of the spectral density of hadronic correlators is an **ill-posed problem**, the spectral density is accessible after smearing

Hansen, Meyer, Robaina, Hansen, Lupo, Tantalo, Bailas, Hashimoto, Ishikawa



W. Jay @Snowmass workshop

LATTICE VS OPE



PG, Hashimoto, Maechler, Panero, Sanfilippo, Simula, Smecca, Tantalo, 2

| m_b^{kin} (JLQCD) | 2.70 ± 0.04 |
|------------------------------------|-------------------|
| $\bar{m}_c(2 \text{ GeV})$ (JLQCD) | 1.10 ± 0.02 |
| m_b^{kin} (ETMC) | 2.39 ± 0.08 |
| $\bar{m}_c(2 \text{ GeV})$ (ETMC) | 1.19 ± 0.04 |
| μ_F^2 | 0.57 ± 0.15 |
| ρ_D^3 | 0.22 ± 0.06 |
| $\mu_c^2(m_b)$ | 0.37 ± 0.10 |
| ρ_{PS}^3 | -0.13 ± 0.10 |
| $\alpha_s^{(4)}(2 \text{ GeV})$ | 0.301 ± 0.006 |

OPE inputs from fits to exp data (physical m_b), HQE of meson masses on lattice
1704.06105, JPhys.Conf.Ser. 11137 (2019) 1, 012005

We include $O(1/m_b^3)$ and $O(\alpha_s)$ terms

Hard scale $\sqrt{m_c^2 + \mathbf{q}^2} \sim 1 - 1.5 \text{ GeV}$

We do not expect OPE to work at high $|\mathbf{q}|$

Twisted boundary conditions allow for any value of \mathbf{q}^2

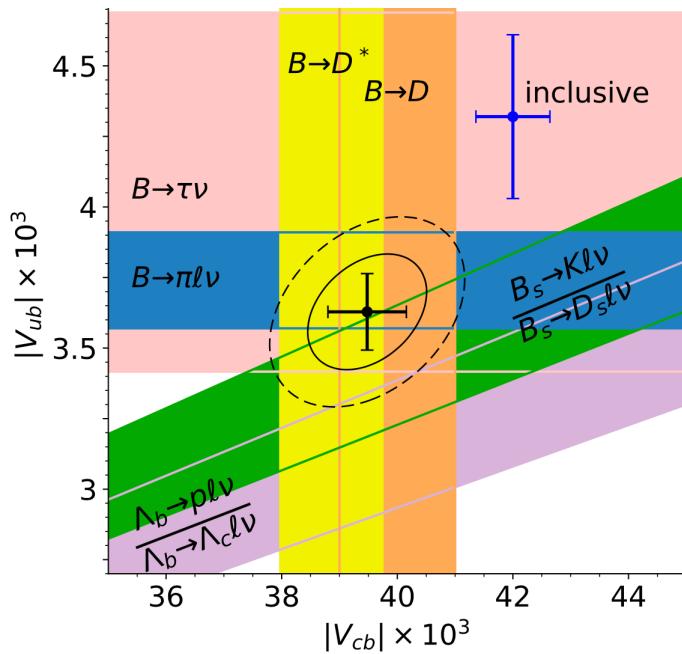
Smaller statistical uncertainties

What can be computed and What cannot be computed

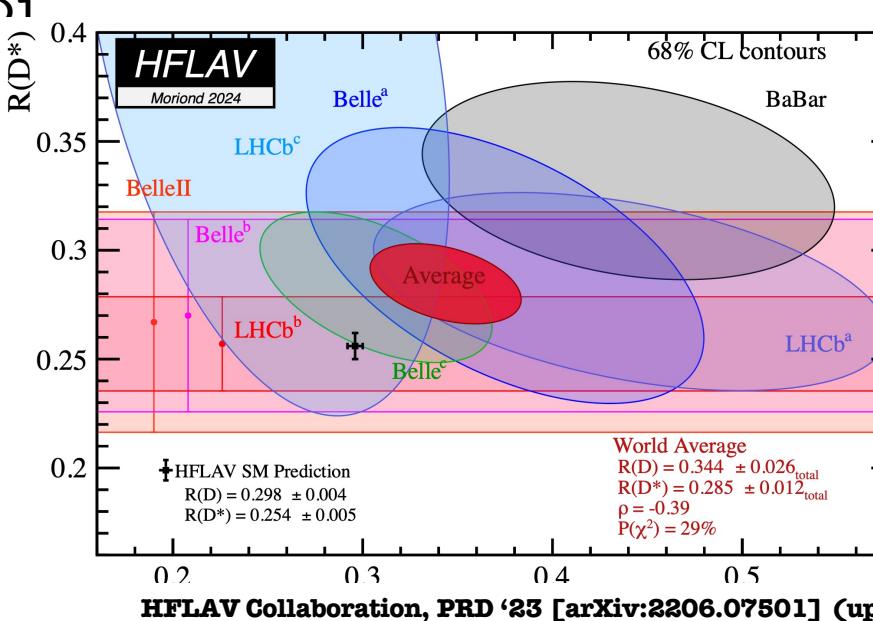
Tension(s) in $b \rightarrow c$ decays ? Charged Currents & Tree level

1. $|V_{cb}|$ (and $|V_{ub}|$) puzzle

FLAG Review 2021 [EPJC '22 (2111.09849)]



2. Lepton Flavor Universality Violation



HFLAV Collaboration, PRD '23 [arXiv:2206.07501] (updated plot)

$$\begin{aligned} \mathcal{R}(D) &= \frac{\mathcal{B}(B \rightarrow D\tau\nu_\tau)}{\mathcal{B}(B \rightarrow D\ell\nu_\ell)}, \\ \mathcal{R}(D^*) &= \frac{\mathcal{B}(B \rightarrow D^*\tau\nu_\tau)}{\mathcal{B}(B \rightarrow D^*\ell\nu_\ell)} \end{aligned}$$

An important CKM unitarity test is the Unitarity Triangle (UT) formed by

$$1 + \frac{V_{ud}V_{ub}^*}{V_{cd}V_{cb}^*} + \frac{V_{td}V_{tb}^*}{V_{cd}V_{cb}^*} = 0$$

V_{cb} plays an important role in UT

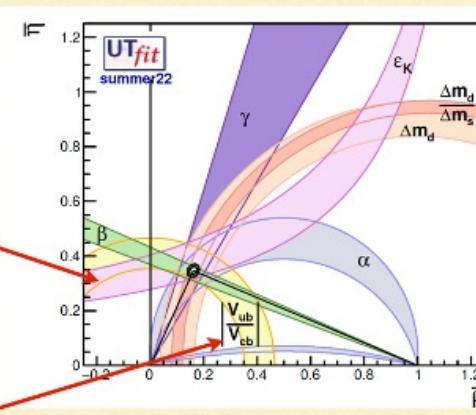
$$\varepsilon_K \approx x|V_{cb}|^4 + \dots$$

and in the prediction of FCNC:

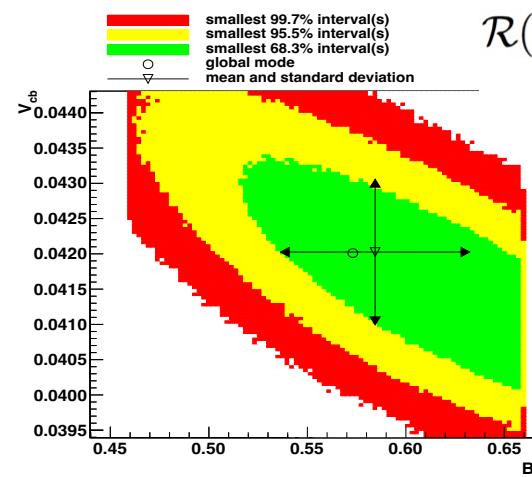
$$\propto |V_{tb}V_{ts}|^2 \simeq |V_{cb}|^2 [1 + O(\lambda^2)]$$

where it often dominates the theoretical uncertainty.

V_{ub}/V_{cb} constrains directly the UT



Our ability to determine precisely V_{cb} is crucial for indirect NP searches



The tension strongly depends on the method used in the theoretical analysis

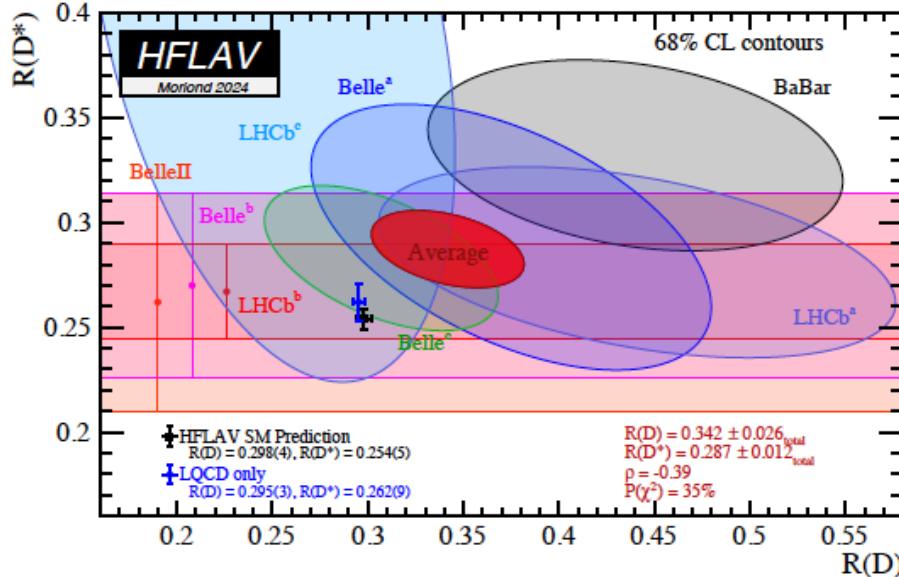
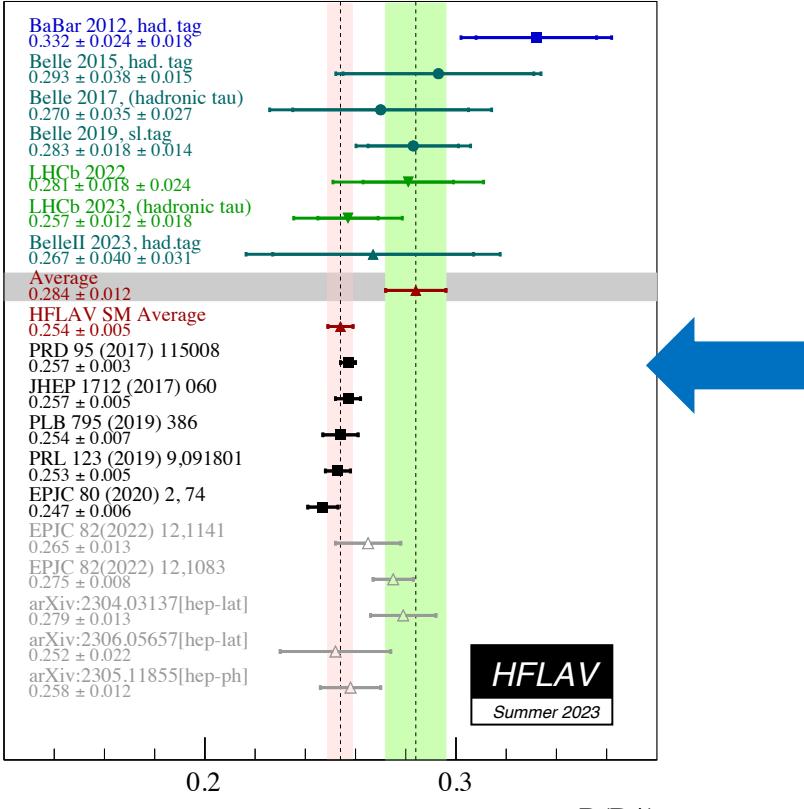
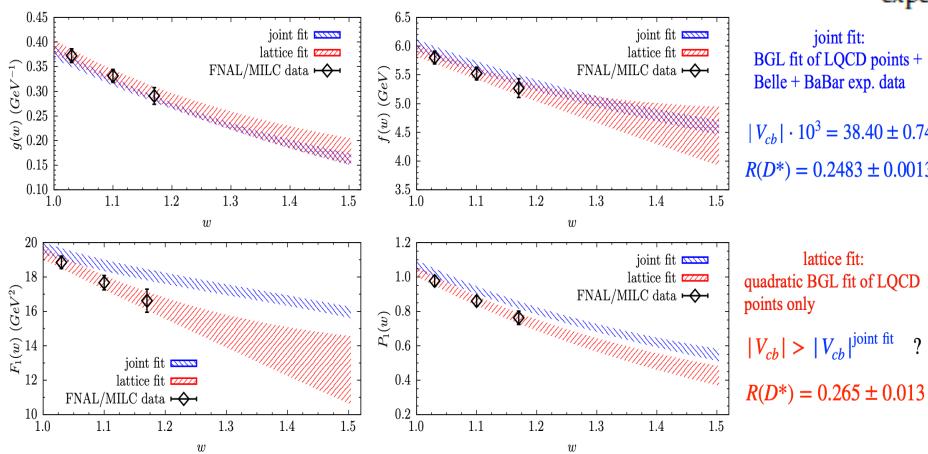


Figure 9. Measurements of $\mathcal{R}(D)$ and $\mathcal{R}(D^*)$ listed in Table 3 and their two-dimensional average. Contours correspond to 68% CL for both the bands and the ellipses. The black and blue points with error bars are two recent SM predictions for $\mathcal{R}(D^*)$ and $\mathcal{R}(D)$. The SM prediction reported is based on the results summarized in Table 1. This prediction and the experimental average deviate from each other by about 3.3σ . The SM prediction based only on LQCD calculations is also reported, where $\mathcal{R}(D)$ is taken from FLAG [25], while $\mathcal{R}(D^*)$ is taken from Ref. [28]. The deviation from the experimental average and this prediction is about 2.5σ . The measurements are listed in Table 3.

Klaver S & Rotondo M,
doi 10.3390/sym16080964



simultaneous fit of the lattice points and experimental data to determine the shape of the FFs and to extract $|V_{cb}|$

*** slope differences between exp's and theory → bias on $|V_{cb}|^{\text{joint fit}}$ ***

$$\begin{aligned} \mathcal{R}(D^*) &= \frac{\mathcal{B}(B \rightarrow D^* \tau \bar{\nu}_\tau)}{\mathcal{B}(B \rightarrow D^* \ell \bar{\nu}_\ell)}, \\ \mathcal{R}(D) &= \frac{\mathcal{B}(B \rightarrow D \tau \bar{\nu}_\tau)}{\mathcal{B}(B \rightarrow D \ell \bar{\nu}_\ell)}, \end{aligned} \quad 6$$

V_{cb} and V_{ub}

Latest inputs from arXiv:2310.03680

$$|V_{cb}| \text{ (excl)} = (40.13 \pm 0.55) 10^{-3}$$

$$|V_{cb}| \text{ (incl)} = (41.97 \pm 0.48) 10^{-3}$$

from arXiv:2310.20324

from arXiv:2202.10285

$$|V_{ub}| \text{ (excl)} = (3.57 \pm 0.23) 10^{-3}$$

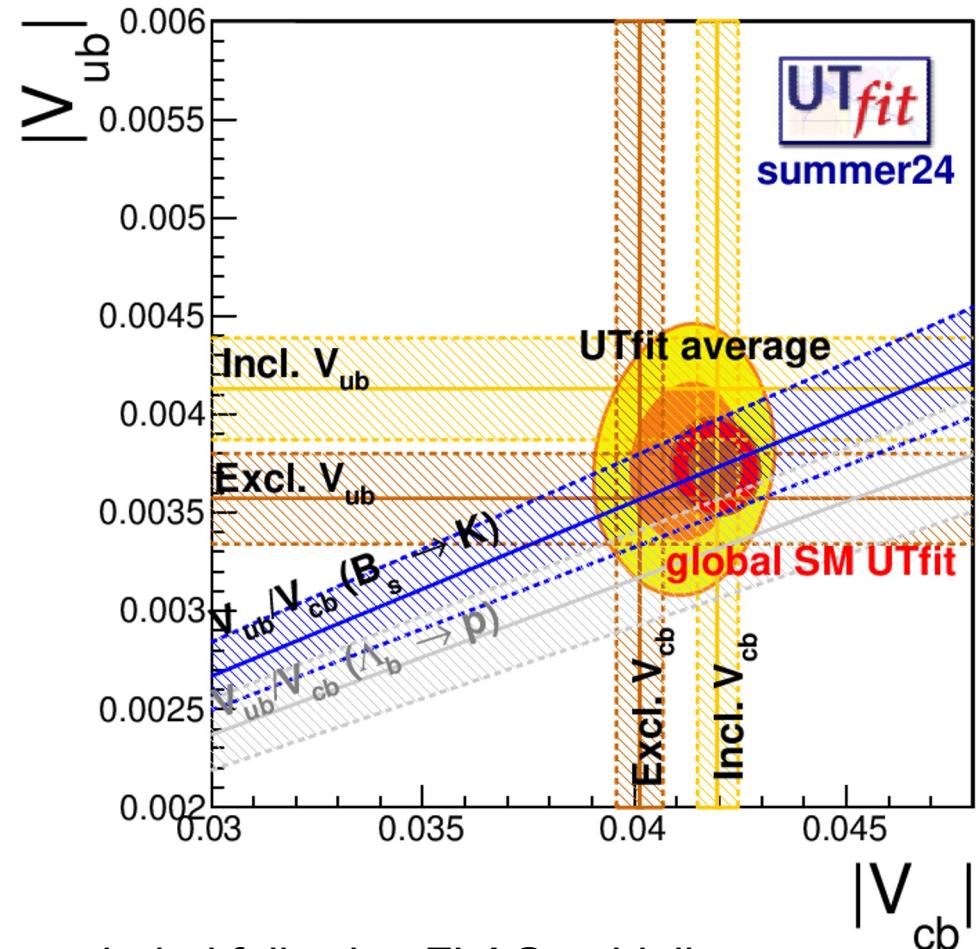
$$|V_{ub}| \text{ (incl)} = (4.13 \pm 0.26) 10^{-3}$$

PDG 2024

from arXiv:2310.03680

$$|V_{ub} / V_{cb}| = (8.7 \pm 0.9) 10^{-2}$$

$$|V_{ub} / V_{cb}| \text{ (LHCb)} = (7.9 \pm 0.6) 10^{-2}$$



Λ_b , excluded following FLAG guidelines

$$|V_{cb}| \text{ (incl)} = (42.00 \pm 0.47) 10^{-3}$$

M. Fael et al. Eur.Phys.J.ST 233 (2024) 2, 325-346

V_{cb} and V_{ub}

Inputs to the global fit
from 2D à la D'Agostini averages

$$|V_{cb}|_{\text{UTfit}} = (41.20 \pm 0.74) 10^{-3}$$

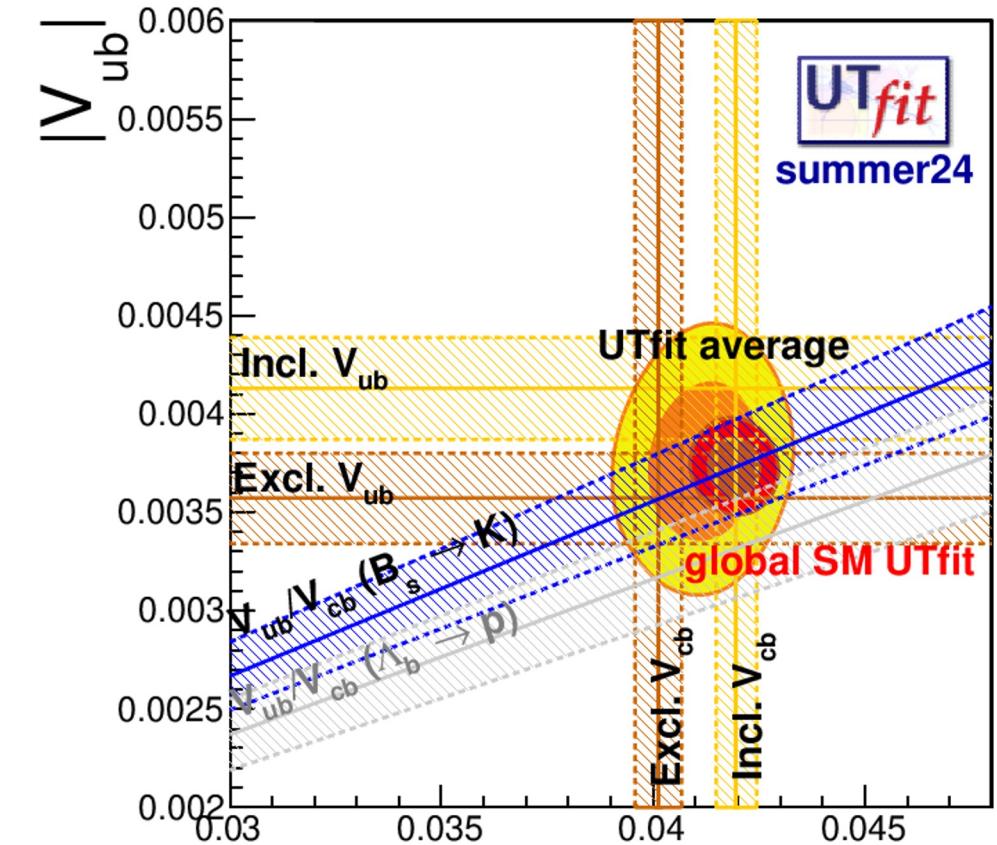
$$|V_{ub}|_{\text{UTfit}} = (3.84 \pm 0.35) 10^{-3}$$

UTfit predictions:

$$|V_{cb}|_{\text{UTfit}} = (42.19 \pm 0.48) 10^{-3}$$

$$|V_{ub}|_{\text{UTfit}} = (3.72 \pm 0.10) 10^{-3}$$

UTfit full fit



$$|V_{cb}|_{\text{UTfit}} = (41.91 \pm 0.40) 10^{-3}$$

$$|V_{ub}|_{\text{UTfit}} = (3.73 \pm 0.09) 10^{-3}$$

$|V_{cb}|$

New Analysis (G.M., S.Simula, L.Vittorio 2310.03680)

NEW EXCLUSIVE $V_{cb} = (39.92 \pm 0.64) 10^{-3}$ from $B \rightarrow D^*$

$|V_{cb}| \text{ (incl)} = (41.97 \pm 0.48) 10^{-3}$
 2.6 σ difference
 Finauri & Gambino 2310.20324

$|V_{cb}| \text{ (incl)} = (41.69 \pm 0.63) 10^{-3}$
 2.0 σ difference
 F. Bernlochner et al. 2205.10274

NEW $V_{ub}/V_{cb} = (8.7 \pm 0.9) 10^{-2}$
 FLAG UNDERESTIMATES OF THE UNCERTAINTY
The larger error reduces the correlation between V_{ub} and V_{cb}

| experiment | $ V_{cb} \cdot 10^3$ | | | |
|--------------------------|-----------------------|-------------|-------------|-------------|
| | FNAL/MILC | HPQCD | JLQCD | Average |
| Belle '18 [19] | 39.64 (74) | 39.11 (81) | 39.92 (74) | 39.58 (98) |
| $\chi^2/\text{(d.o.f.)}$ | 3.71 | 1.14 | 0.04 | 0.26 |
| Belle '23 [13] | 40.87 (115) | 41.03 (125) | 41.38 (134) | 41.11 (138) |
| $\chi^2/\text{(d.o.f.)}$ | 1.80 | 0.11 | 0.31 | 0.03 |
| BelleII '23 [14] | 39.35 (77) | 39.98 (102) | 40.20 (85) | 39.79 (94) |
| $\chi^2/\text{(d.o.f.)}$ | 0.63 | 0.09 | 0.42 | 0.29 |

Ufit Prediction $V_{cb} = (42.19 \pm 0.48) 10^{-3}$

$V_{ub} = (3.72 \pm 0.10) 10^{-3}$

see also
e-Print: [2409.10492](https://arxiv.org/abs/2409.10492)

Power corrections to the CP-violation parameter ε_K

M. Ciuchini^(a), E. Franco^(b), V. Lubicz^(c,a), $\varepsilon_K^{exp} = 2.228 \pm 0.011) \cdot 10^{-3}$
G. Martinelli^(d,b), L. Silvestrini^(b), C. Tarantino^(c,a)

*2021: an estimate from the $1/m_c$
expansion of the effective
Hamiltonian + UTfit*

$$\varepsilon_K = 2.00(15) \times 10^{-3}$$

Computing the long-distance contributions to ε_K

Ziyuan Bai
Columbia University, USA
bzyhty@gmail.com

Norman Christ*†
Columbia University, USA
E-mail: nhc@phys.columbia.edu

RBC and UKQCD Collaborations

*2015: a real
exploratory calculation
no physical masses, no
extrapolation to the continuum*

$$|\varepsilon| = (1.806(41) + 0.891(11) + 0.209(6) + 0.112(13)) \times 10^{-3} = 3.019(45) \times 10^{-3}$$

$$tt \quad ut_{SD} \quad ut_{LD} \quad \text{Im}(A_0),$$

Final result for ϵ'

- Combining our new result for $\text{Im}(A_0)$ and our 2015 result for $\text{Im}(A_2)$, and again using expt. for the real parts, we find

$$\begin{aligned}\text{Re}\left(\frac{\epsilon'}{\epsilon}\right) &= \text{Re} \left\{ \frac{i\omega e^{i(\delta_2 - \delta_0)}}{\sqrt{2}\epsilon} \left[\frac{\text{Im}A_2}{\text{Re}A_2} - \frac{\text{Im}A_0}{\text{Re}A_0} \right] \right\} \\ &= 0.00217(26)(62)(50)\end{aligned}$$

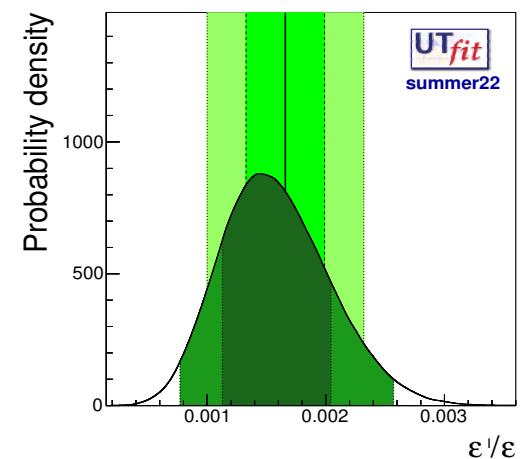
stat sys IB + EM

Consistent with experimental result:

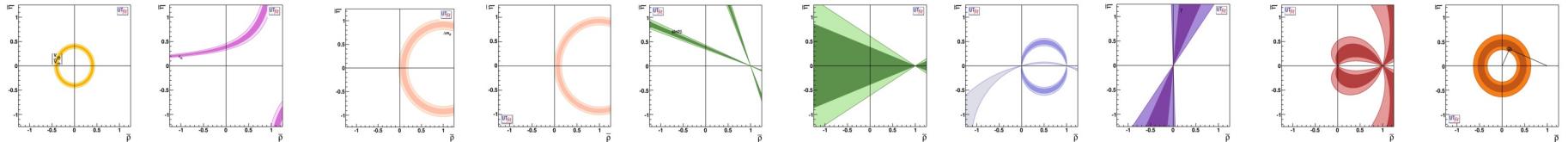
$$\text{Re}(\epsilon'/\epsilon)_{\text{expt}} = 0.00166(23)$$

RBC/UKQCD: $e'/e = 16.7 \times 10^{-4}$

Utfit: $e'/e = 15.2(4.7) \times 10^{-4}$



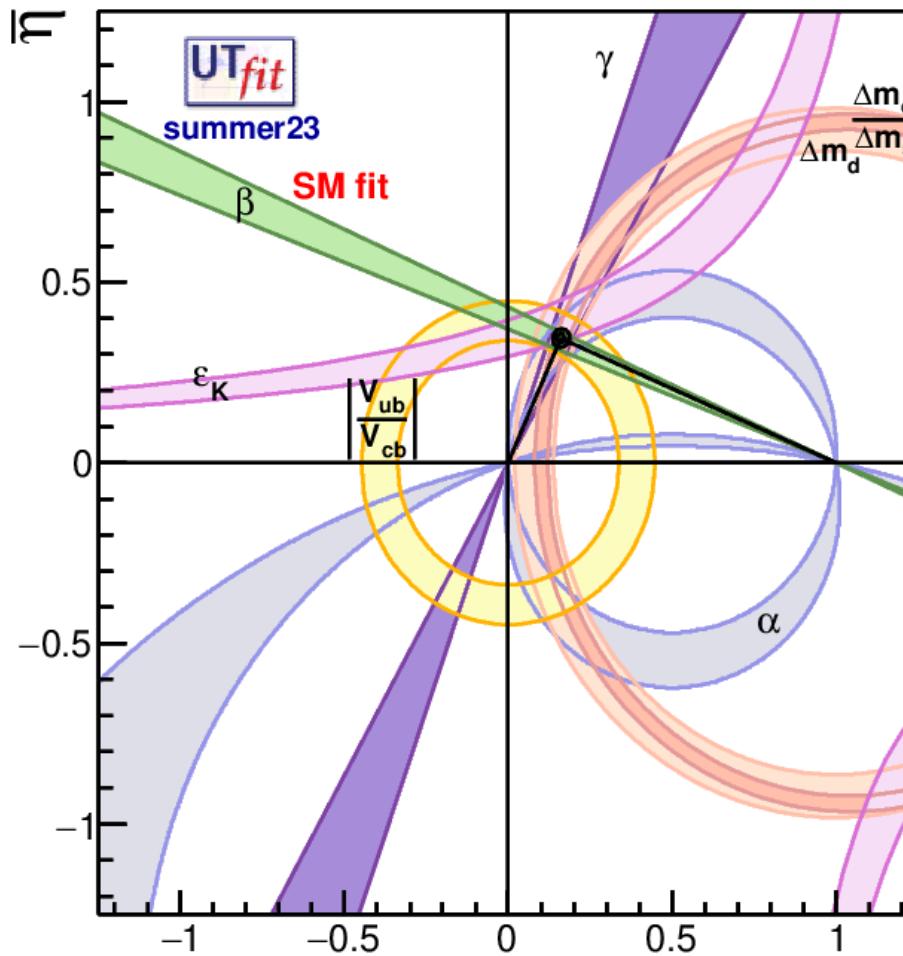
A second group should do this calculation!!



2023 results

$$\bar{\rho} = 0.160 \pm 0.009 \quad \bar{\eta} = 0.345 \pm 0.011$$

In the hadronic sector, the SM CKM pattern represents the principal part of the flavor structure and of CP violation

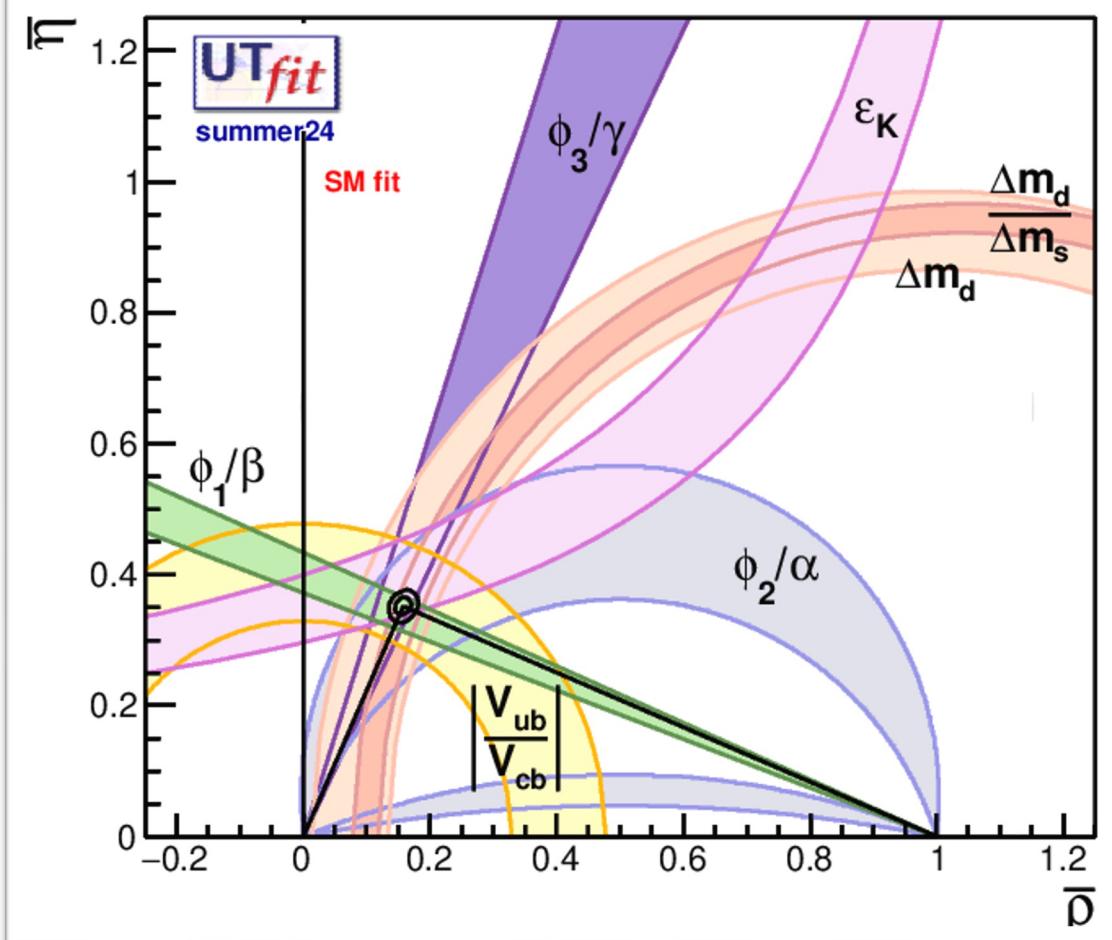


To be updated
 $\alpha = (92.4 \pm 1.4)^0$
 $\sin 2\beta = 0.703 \pm 0.014$
 $\beta = (22.46 \pm 0.68)^0$
 $\gamma = (65.1 \pm 1.3)^0$
 $A = 0.828 \pm 0.011$
 $\lambda = 0.22519 \pm 0.00083$
 2022

Consistency on an over constrained fit of the CKM parameters

CKM matrix is the dominant source of flavour mixing and CP violation

Unitarity Triangle analysis in the SM:



levels @
95% Prob

$$\rho = 0.158 \pm 0.009$$

$$\eta = 0.352 \pm 0.010$$

$$\lambda = 0.2250 \pm 0.0007$$

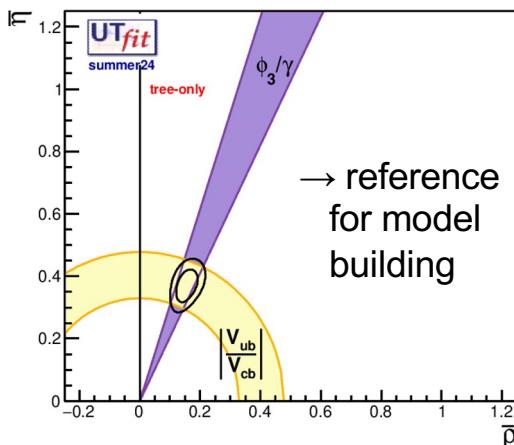
$$A = 0.826 \pm 0.009$$

Some interesting configurations

“Tree only”

$$\rho = \pm 0.156 \pm 0.024$$

$$\eta = \pm 0.372 \pm 0.035$$

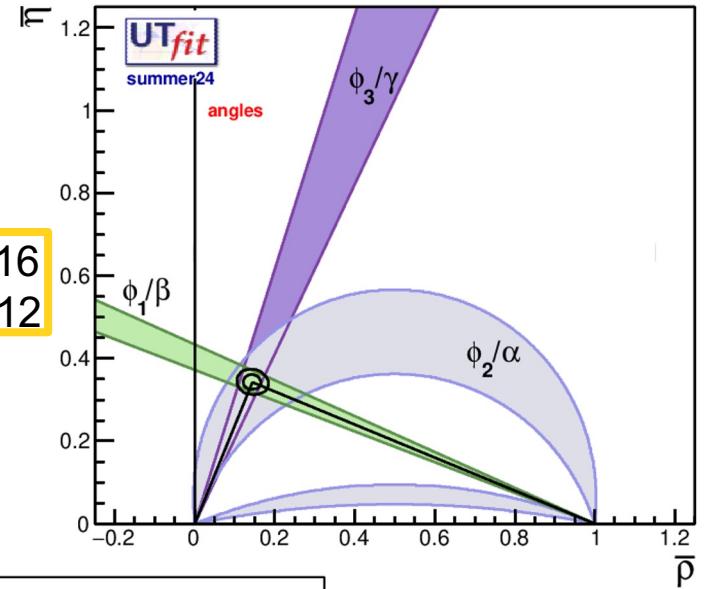


→ reference
for model
building

Angles only

$$\rho = 0.144 \pm 0.016$$

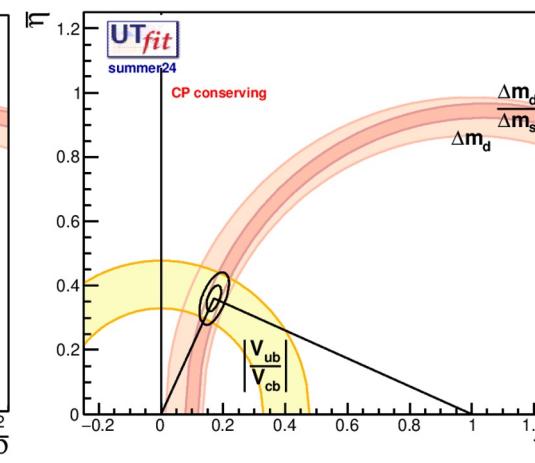
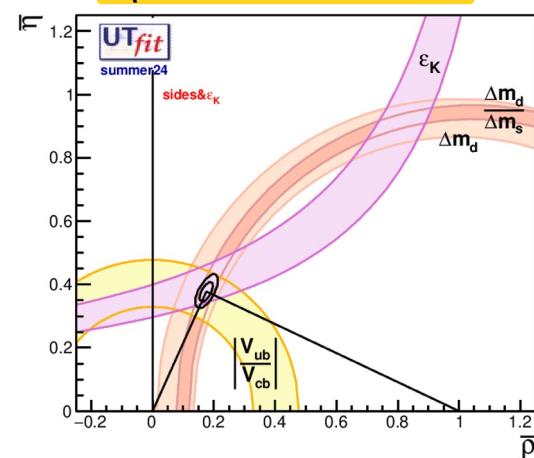
$$\eta = 0.343 \pm 0.012$$



Sides and e_K

$$\rho = 0.176 \pm 0.015$$

$$\eta = 0.377 \pm 0.022$$



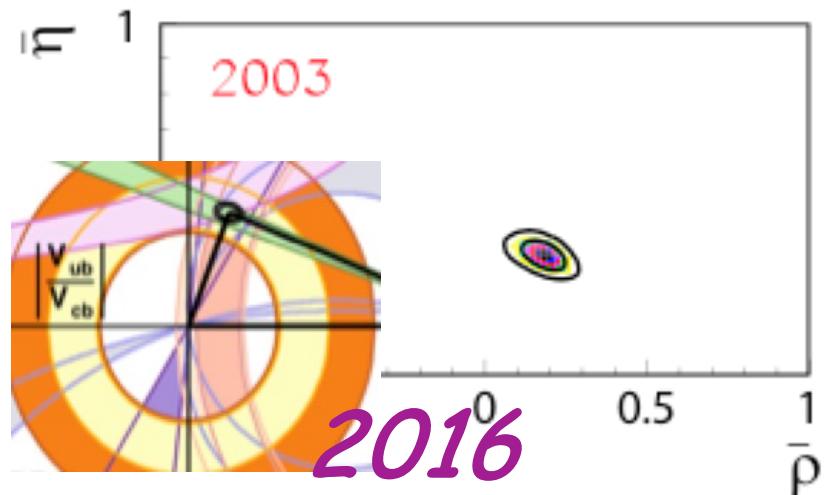
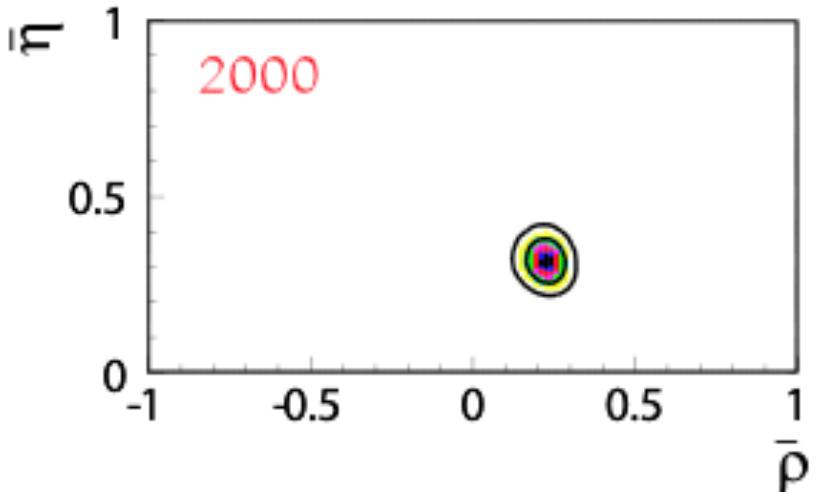
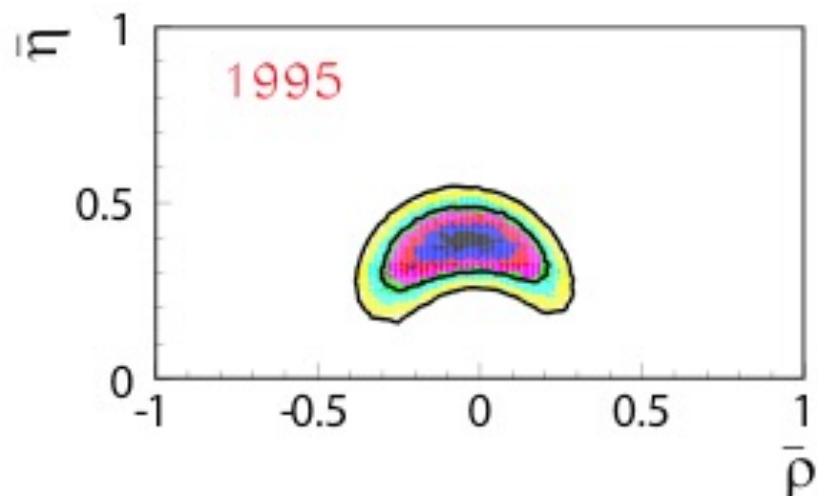
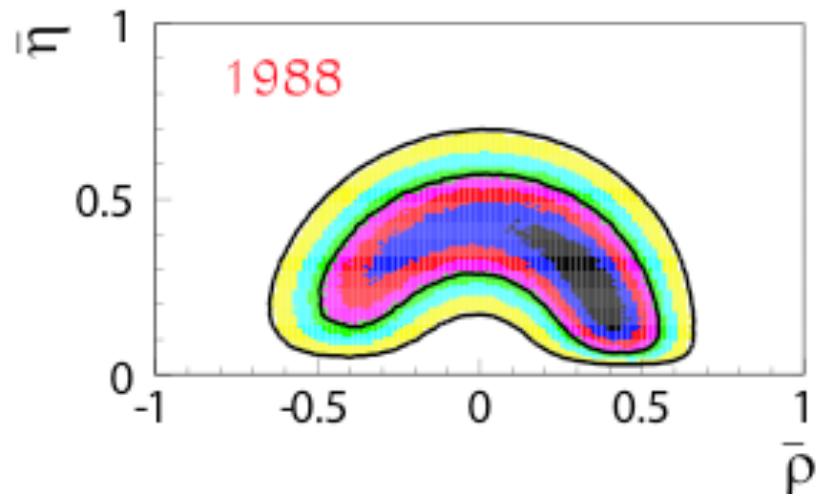
CP conserving
constraints

$$\rho = 0.170 \pm 0.017$$

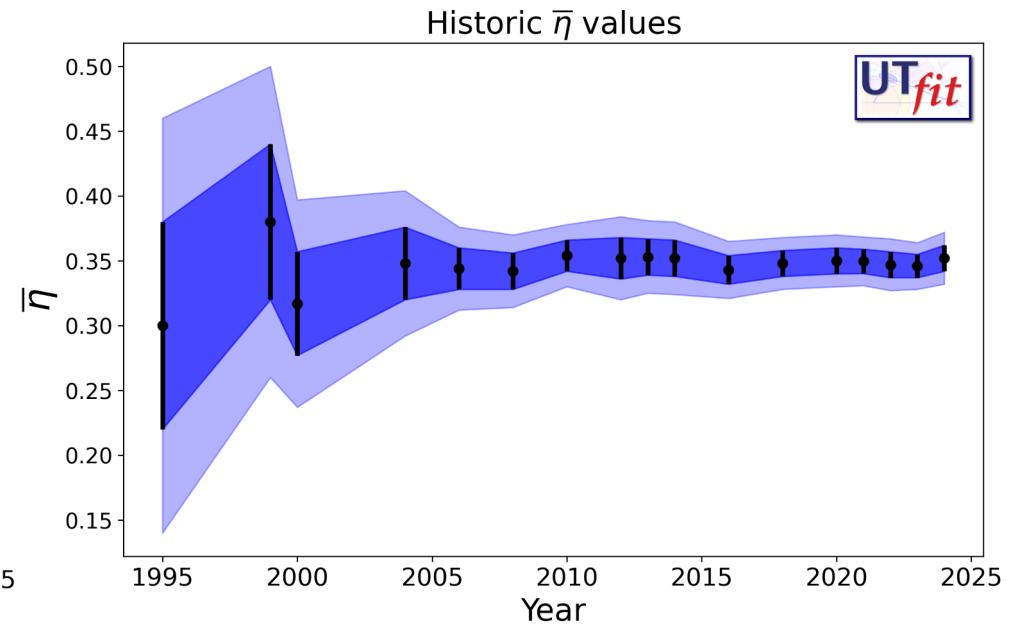
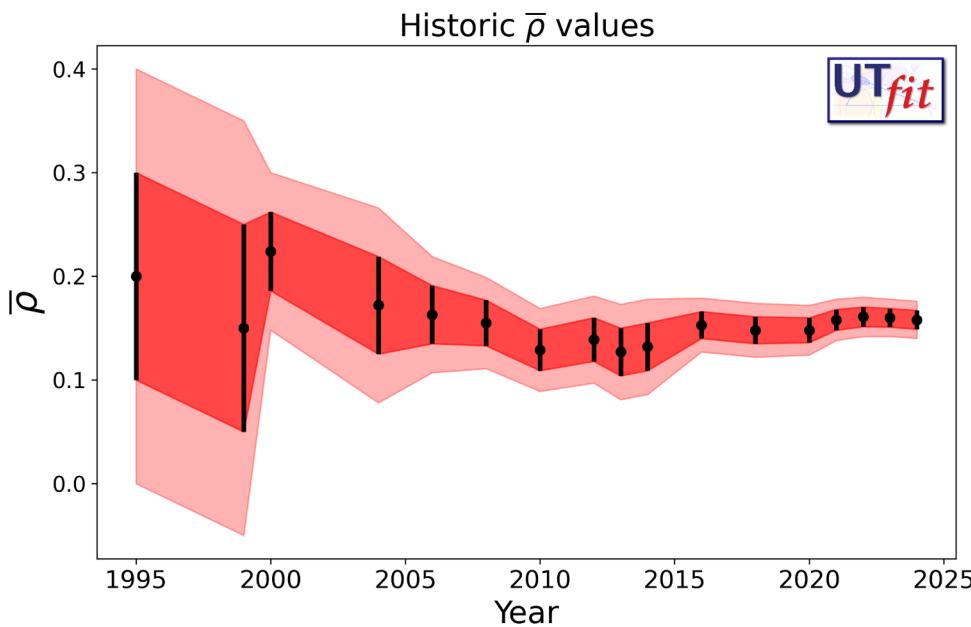
$$\eta = 0.361 \pm 0.035$$

PROGRESS SINCE 1988

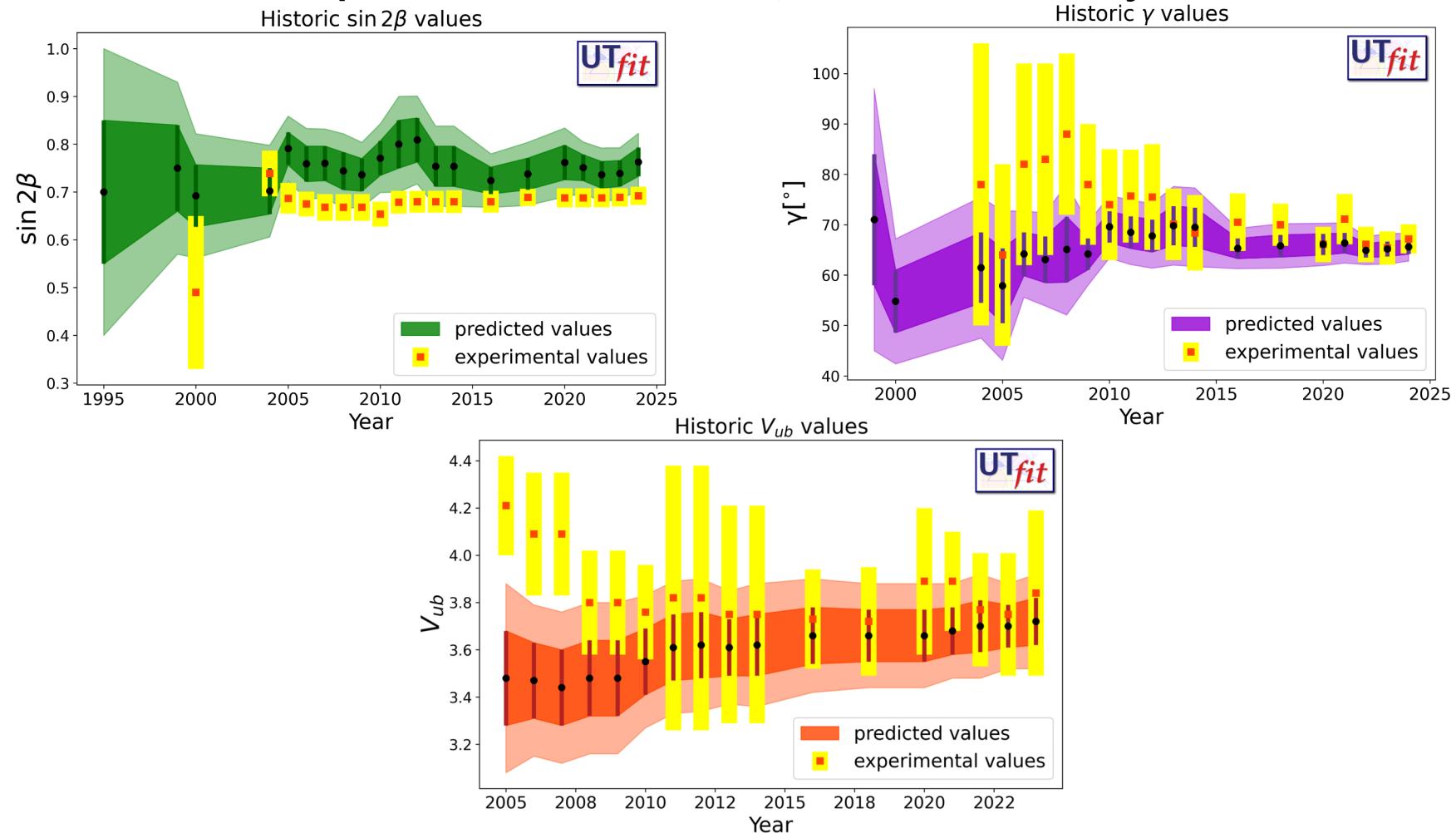
Experimental progress so impressive that we can fit the hadronic matrix elements (in the SM)



UTfit results across the years:



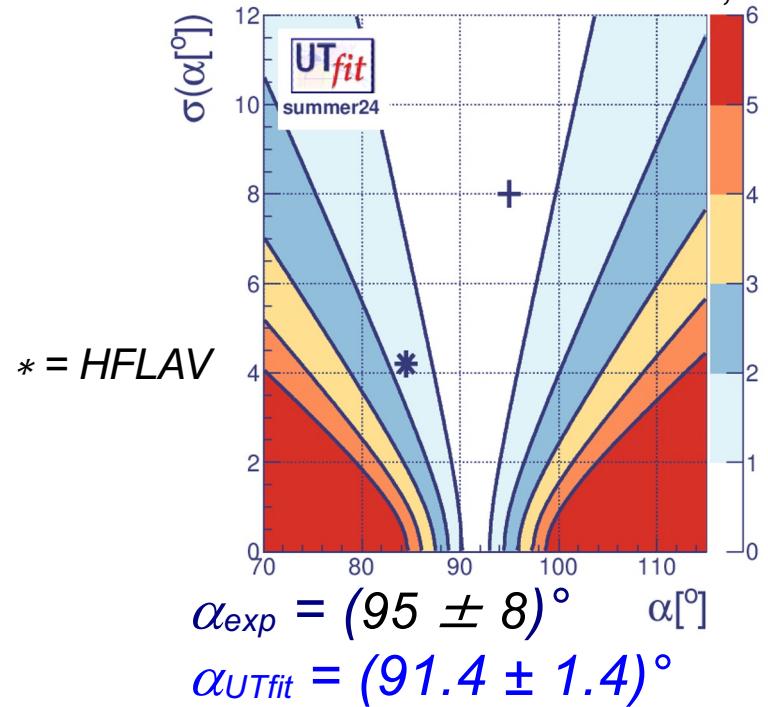
UTfit and experimental results across the years:



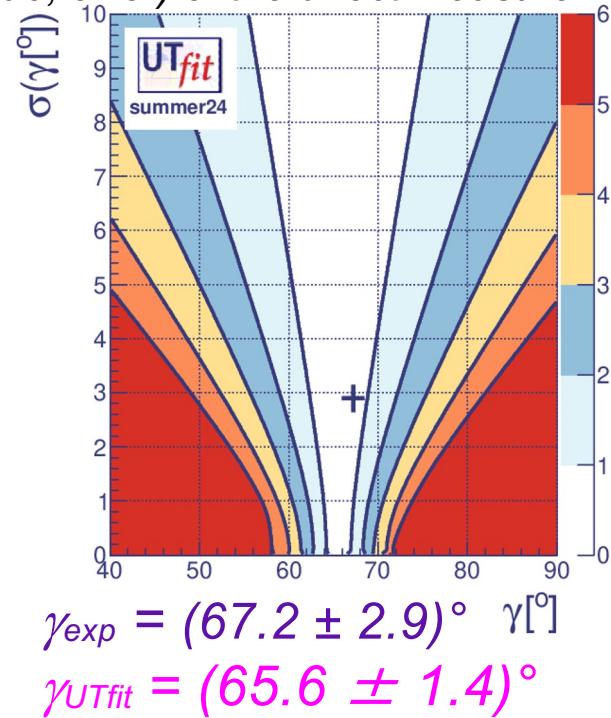
Compatibility plots

A way to “measure” the agreement of a single measurement with the indirect determination from the fit using all the other inputs: test for the SM description of the flavour physics

Colour code: agreement between the predicted values and the measurements at better than 1, 2,... $n\sigma$

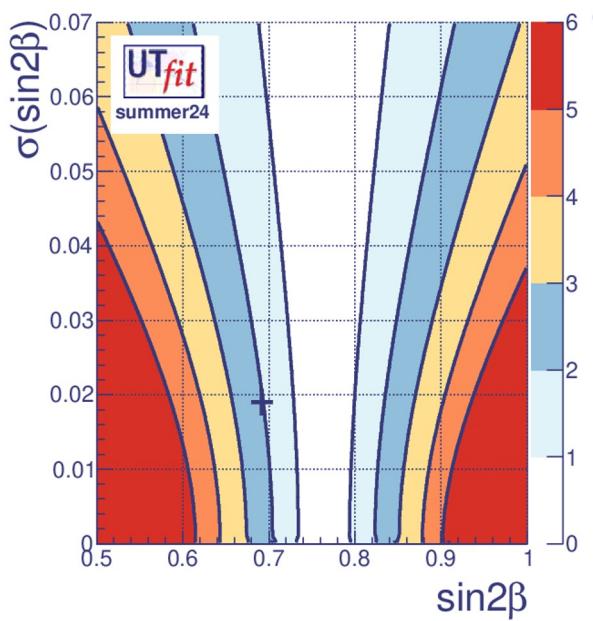


The cross has the coordinates $(x,y)=($ central value, error) of the direct measurement



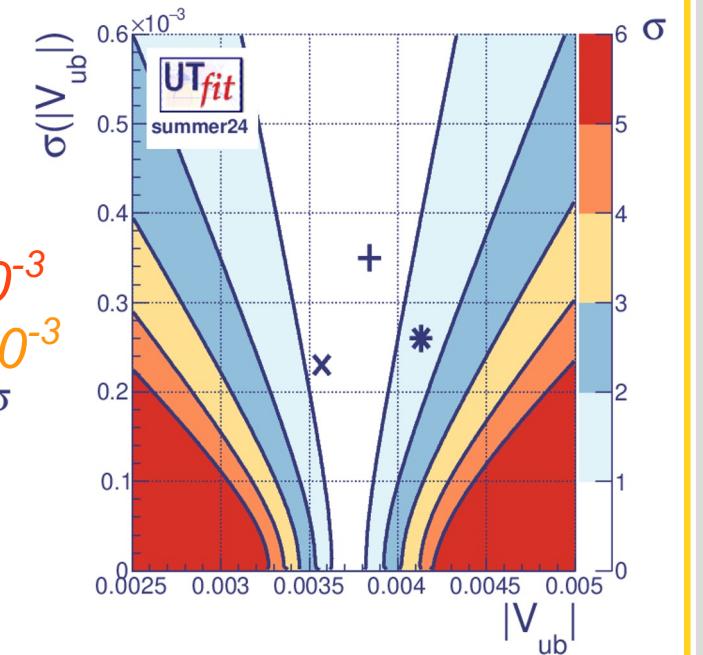
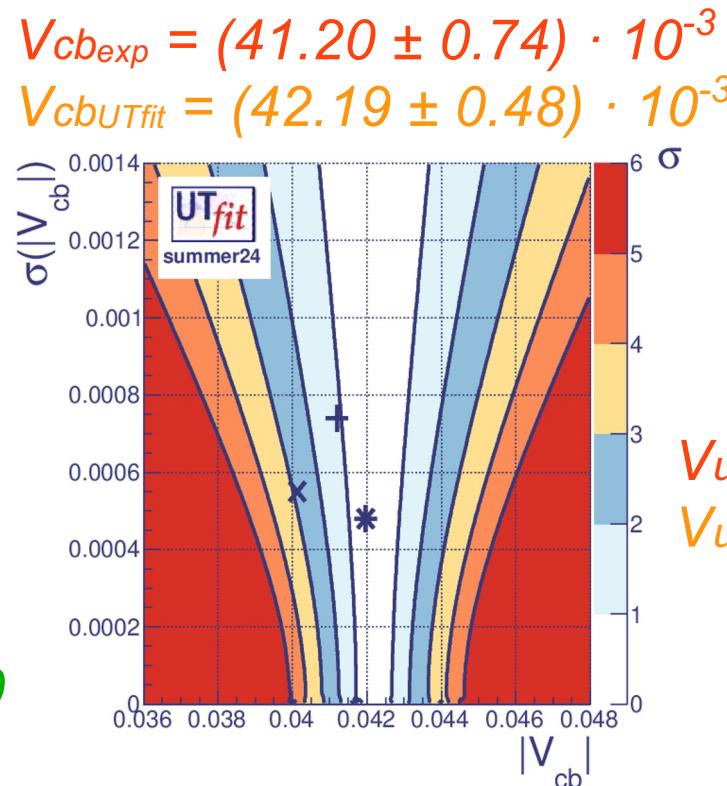
$\gamma = (68.4 \pm 2.6)^\circ$ F. Betti et al. e-Print: [2409.06449 \[hep-ph\]](https://arxiv.org/abs/2409.06449)

Checking the usual tensions..



$$\sin 2\beta_{\text{exp}} = 0.692 \pm 0.019$$

$$\sin 2\beta_{\text{UTfit}} = 0.763 \pm 0.030$$



$$V_{cb\text{exp}} = (41.20 \pm 0.74) \cdot 10^{-3}$$

$$V_{cb\text{UTfit}} = (42.19 \pm 0.48) \cdot 10^{-3}$$

$$V_{ub\text{exp}} = (3.84 \pm 0.35) \cdot 10^{-3}$$

$$V_{ub\text{UTfit}} = (3.72 \pm 0.10) \cdot 10^{-3}$$

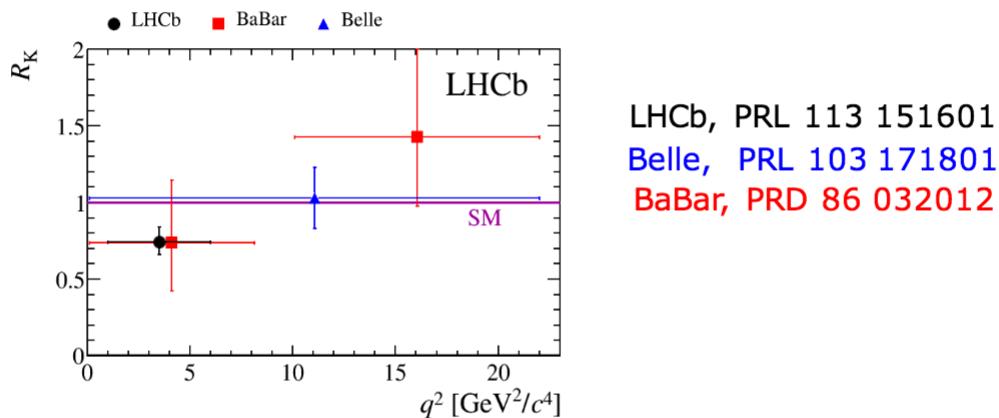
x = exclusive
** = inclusive*

Tension(s) in $b \rightarrow s$ decays ? Neutral Currents & Loop level

Reminder:

$$R_K = \frac{B(B^+ \rightarrow K^+ \mu^+ \mu^-)}{B(B^+ \rightarrow K^+ e^+ e^-)}$$

- Test of lepton universality : $R_K \sim 1$ in SM, with negligible theoretical uncertainties



LHCb, PRL 113 151601
 Belle, PRL 103 171801
 BaBar, PRD 86 032012

$$R_K(1 < q^2 < 6 \text{ GeV}^2) = 0.745^{+0.090}_{-0.074} (\text{stat}) \pm 0.036 (\text{syst})$$

- Compatible with SM at 2.6σ
- Experimentally challenging
 - lower trigger efficiency for electrons, resolution deteriorated by bremsstrahlung
- Other modes suitable for same test:
 $B^0 \rightarrow K^{*0} l^+ l^-$, $B_s \rightarrow \phi l^+ l^-$, $\Lambda_B \rightarrow \Lambda l^+ l^-$

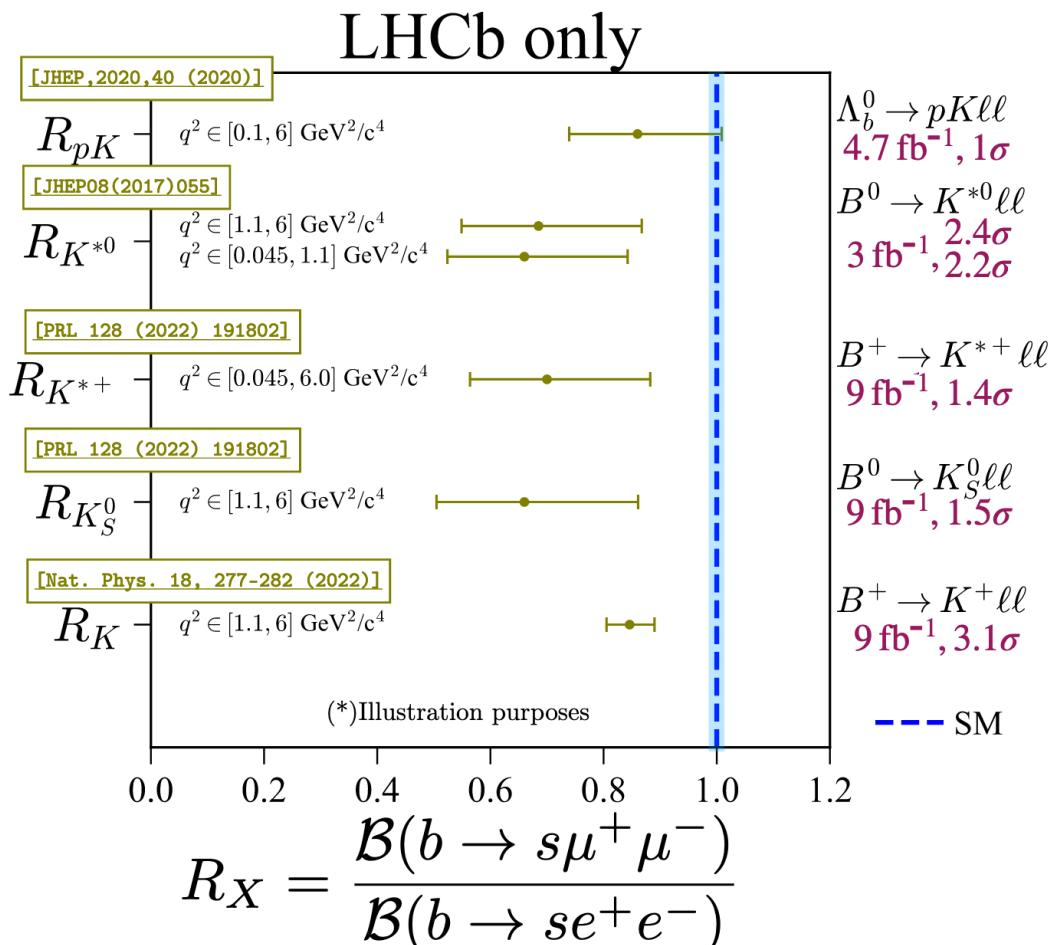
old slide

Excitement

Analysis

Lepton Flavour Universality (LFU) tests in $b \rightarrow s\ell^+\ell^-$

- ◆ Coherent pattern of tension to SM in LFU test with $b \rightarrow s\ell^+\ell^-$ transition:
- ◆ R_X ratio extremely well predicted in SM
 - ▶ Cancellation of hadronic uncertainties at 10^{-4}
 - ▶ $\mathcal{O}(1\%)$ QED correction [Eur.Phys.J.C 76 (2016) 8]
 - ▶ Statistically limited
- ◆ Any departure from unity is a clear sign of New Physics

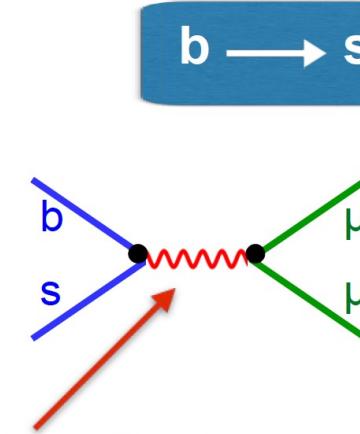


A EFT description

A relatively sizable New Physics effect...

~30% of the Standard Model contribution (arising at one loop)

...hinting towards a relatively low New Physics scale:



generic tree

$$\frac{1}{\Lambda_{NP}^2} (\bar{s} \gamma_\nu P_L b)(\bar{\mu} \gamma^\nu \mu)$$

$$\Lambda_{NP} \simeq 35 \text{ TeV} \times (C_9^{NP})^{-1/2}$$

MFV tree

$$\frac{1}{\Lambda_{NP}^2} V_{tb} V_{ts}^* (\bar{s} \gamma_\nu P_L b)(\bar{\mu} \gamma^\nu \mu)$$

$$\Lambda_{NP} \simeq 7 \text{ TeV} \times (C_9^{NP})^{-1/2}$$

generic loop

$$\frac{1}{\Lambda_{NP}^2} \frac{1}{16\pi^2} (\bar{s} \gamma_\nu P_L b)(\bar{\mu} \gamma^\nu \mu)$$

$$\Lambda_{NP} \simeq 3 \text{ TeV} \times (C_9^{NP})^{-1/2}$$

MFV loop

$$\frac{1}{\Lambda_{NP}^2} \frac{1}{16\pi^2} V_{tb} V_{ts}^* (\bar{s} \gamma_\nu P_L b)(\bar{\mu} \gamma^\nu \mu)$$

$$\Lambda_{NP} \simeq 0.6 \text{ TeV} \times (C_9^{NP})^{-1/2}$$

Harakiri!

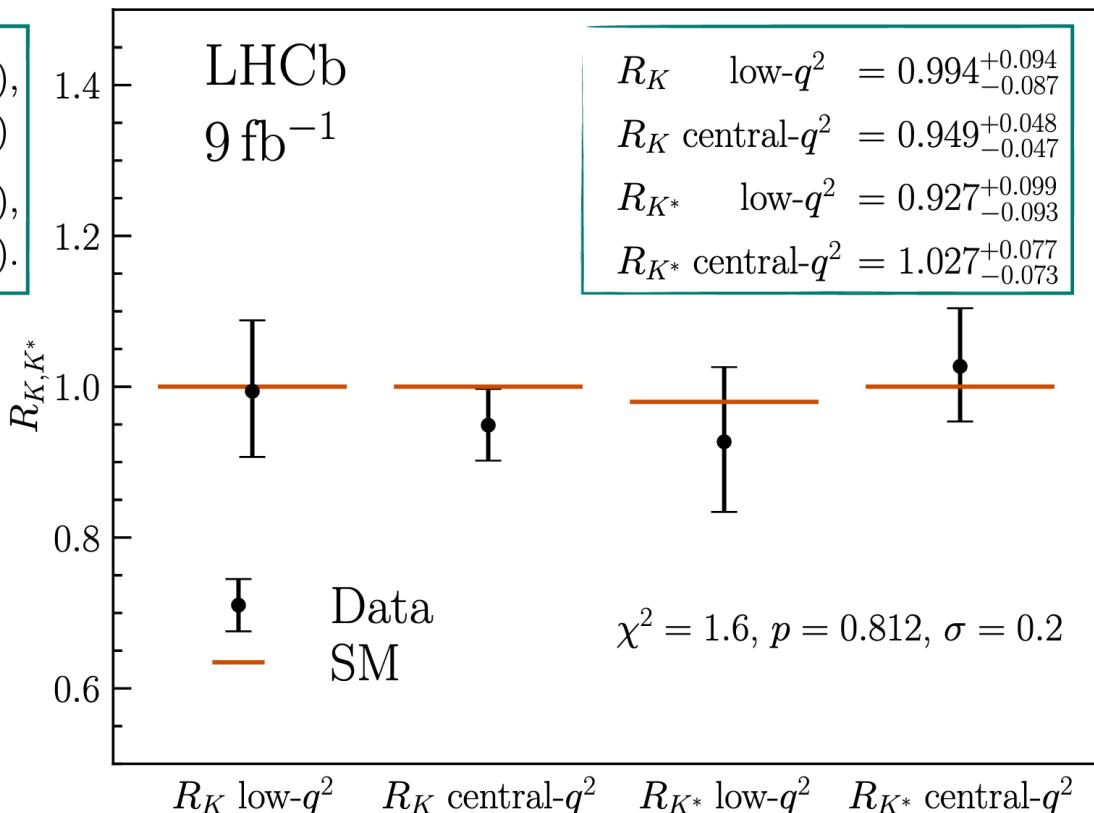
Analysis: results

Results



$$\begin{aligned} \text{low-}q^2 & \left\{ \begin{array}{l} R_K = 0.994^{+0.090}_{-0.082} \text{ (stat)}^{+0.027}_{-0.029} \text{ (syst)}, \\ R_{K^*} = 0.927^{+0.093}_{-0.087} \text{ (stat)}^{+0.034}_{-0.033} \text{ (syst)} \end{array} \right. \\ \text{central-}q^2 & \left\{ \begin{array}{l} R_K = 0.949^{+0.042}_{-0.041} \text{ (stat)}^{+0.023}_{-0.023} \text{ (syst)}, \\ R_{K^*} = 1.027^{+0.072}_{-0.068} \text{ (stat)}^{+0.027}_{-0.027} \text{ (syst)}. \end{array} \right. \end{aligned}$$

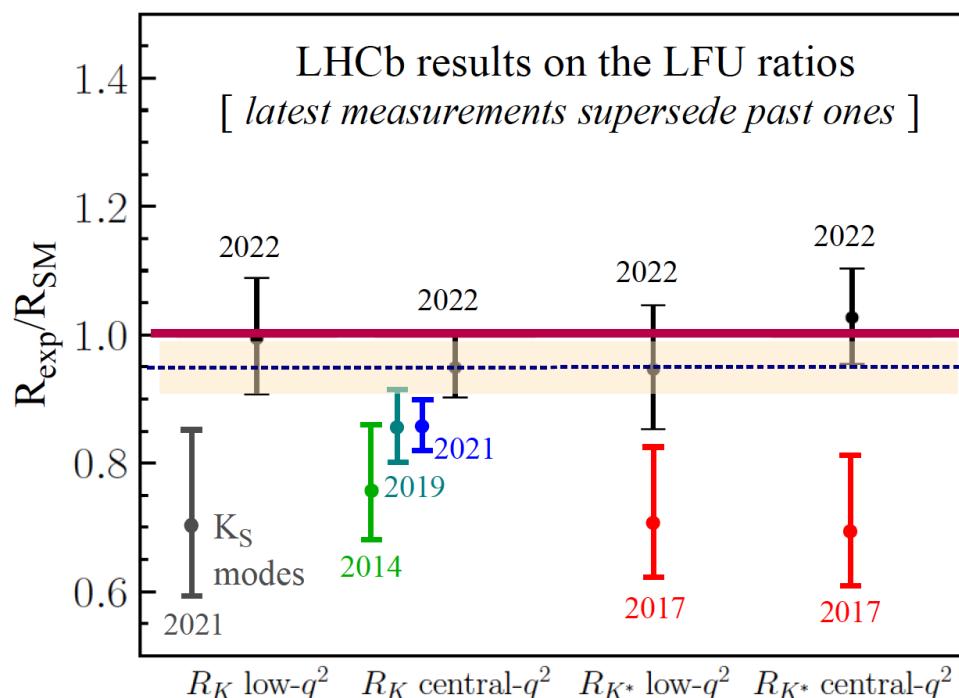
- ♦ Most precise and accurate LFU test in $b \rightarrow s\ell\ell$ transition
- ♦ Compatible with SM with a simple χ^2 test on 4 measurement at 0.2σ



► Hints of non-universality in B -physics

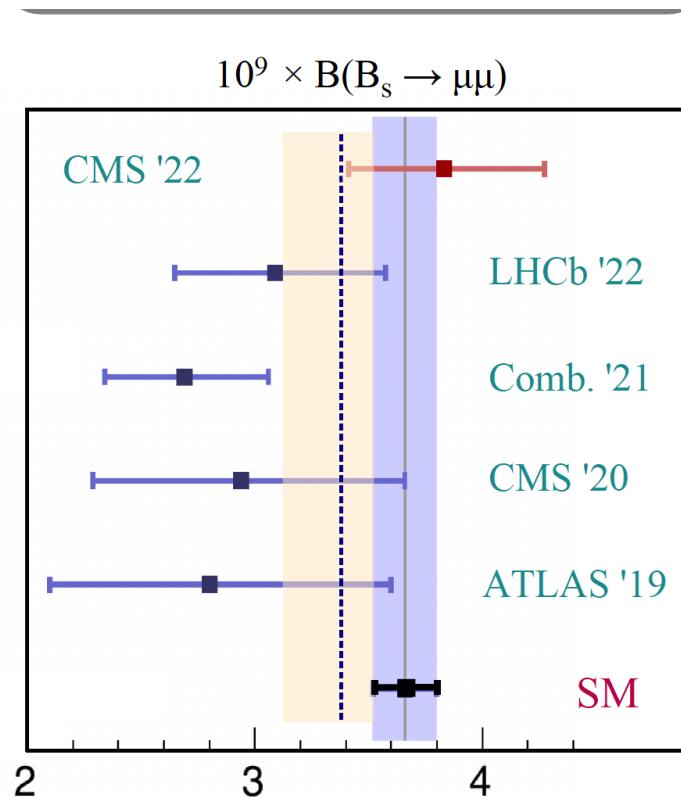
III. LFU anomaly in NC & BR($B_s \rightarrow \mu\mu$)

- Clean SM predictions
(LFU ratios + no long-distance in $B_s \rightarrow \mu\mu$)
- ~~Highest significance till summer 2022~~



$$\text{low-}q^2 \begin{cases} R_K = 0.994^{+0.090}_{-0.082} \text{ (stat)}^{+0.027}_{-0.029} \text{ (syst)}, \\ R_{K^*} = 0.927^{+0.093}_{-0.087} \text{ (stat)}^{+0.034}_{-0.033} \text{ (syst)} \end{cases}$$

$$\text{central-}q^2 \begin{cases} R_K = 0.949^{+0.042}_{-0.041} \text{ (stat)}^{+0.023}_{-0.023} \text{ (syst)}, \\ R_{K^*} = 1.027^{+0.072}_{-0.068} \text{ (stat)}^{+0.027}_{-0.027} \text{ (syst)}. \end{cases}$$



$$BR(B_s \rightarrow \mu\mu)_{exp} = (3.41 \pm 0.29) \times 10^{-9} \quad 9\%$$

$$BR(B_s \rightarrow \mu\mu)_{SM} = (3.47 \pm 0.14) \times 10^{-9} \quad 4\%$$

still

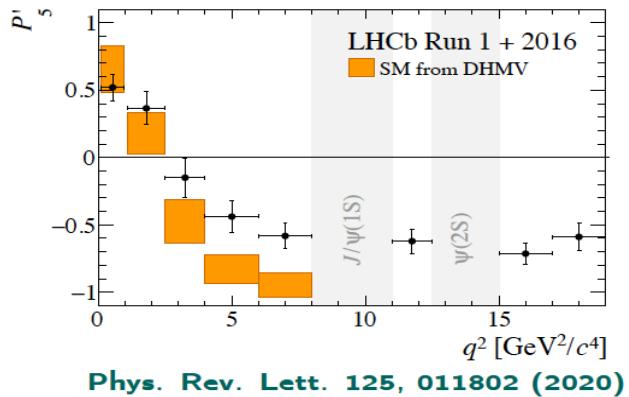
B anomalies in the post- R_K era

Nazila Mahmoudi

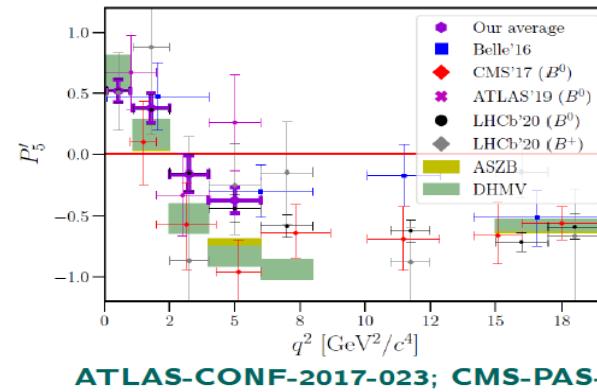
Corfu 2023

Tension in the angular observables - 2020 updates

$P'_5(B^0 \rightarrow K^{*0} \mu^+ \mu^-)$: 2020 LHCb update with 4.7 fb^{-1} : $\sim 2.9\sigma$ local tension



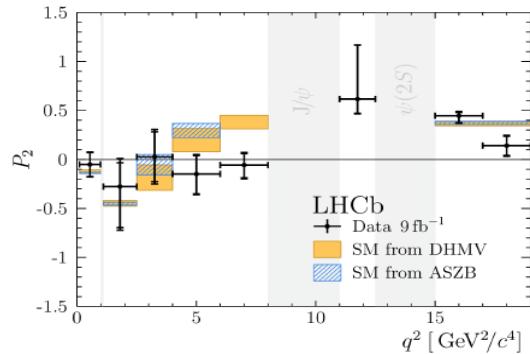
Phys. Rev. Lett. 125, 011802 (2020)



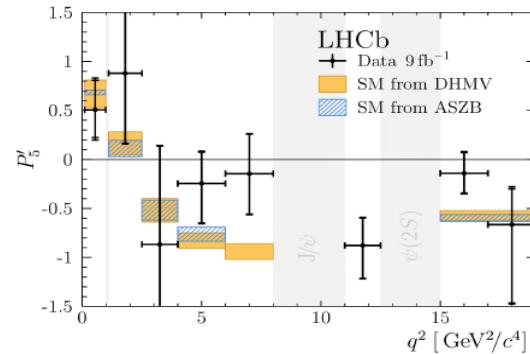
ATLAS-CONF-2017-023; CMS-PAS-BPH-16-098

*anomalies hunters never surrender
desperately seeking Susan—NP*

First measurement of $B^+ \rightarrow K^{*+} \mu^+ \mu^-$ angular observables using the full Run 1 and Run 2 dataset (9 fb^{-1}):



Phys. Rev. Lett. 126, 161802 (2021)



*theoretical estimates of
unown amplitudes*

The results confirm the global tension with respect to the SM!

Comparison of one-operator NP fits:

| All observables 2022 $(\chi^2_{\text{SM}} = 253.3)$ | | | |
|---|------------------|-----------------|--------------------|
| | b.f. value | χ^2_{\min} | Pull _{SM} |
| δC_9 | -0.95 ± 0.13 | 215.8 | 6.1σ |
| δC_9^e | 0.82 ± 0.19 | 232.4 | 4.6σ |
| δC_9^μ | -0.92 ± 0.11 | 195.2 | 7.6σ |
| δC_{10} | 0.08 ± 0.16 | 253.2 | 0.5σ |
| δC_{10}^e | -0.77 ± 0.18 | 230.6 | 4.8σ |
| δC_{10}^μ | 0.43 ± 0.12 | 238.9 | 3.8σ |
| δC_{LL}^e | 0.42 ± 0.10 | 231.4 | 4.7σ |
| δC_{LL}^μ | -0.43 ± 0.07 | 213.6 | 6.3σ |

| All observables 2023 $(\chi^2_{\text{SM}} = 231.3)$ | | | |
|---|------------------|-----------------|--------------------|
| | b.f. value | χ^2_{\min} | Pull _{SM} |
| δC_9 | -0.96 ± 0.13 | 230.7 | 6.3σ |
| δC_9^e | 0.21 ± 0.16 | 269.2 | 1.3σ |
| δC_9^μ | -0.69 ± 0.12 | 240.4 | 5.5σ |
| δC_{10} | 0.15 ± 0.15 | 270.0 | 1.0σ |
| δC_{10}^e | -0.18 ± 0.14 | 269.3 | 1.3σ |
| δC_{10}^μ | 0.16 ± 0.10 | 268.3 | 1.6σ |
| δC_{LL} | -0.54 ± 0.12 | 249.1 | 4.7σ |
| δC_{LL}^e | 0.10 ± 0.08 | 269.2 | 1.3σ |
| δC_{LL}^μ | -0.23 ± 0.06 | 257.4 | 3.7σ |

$\delta C_{\text{LL}}^\ell$ basis corresponds to $\delta C_9^\ell = -\delta C_{10}^\ell$.

*But ... really a reliable estimate of uncertainties
is missing and theory must be improved otherwise
we will continue to generate anomalies out of
our ignorance*

Known unknowns in $B \rightarrow K^*\mu\mu$

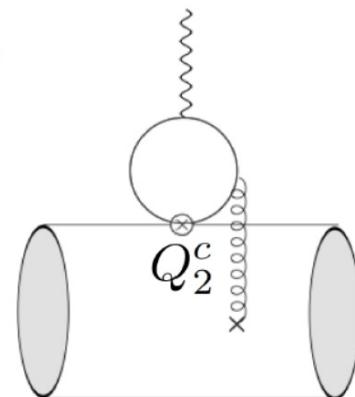
$$H_V^\lambda = \frac{4iG_F m_B}{\sqrt{2}} \frac{e^2}{16\pi^2} \lambda_t \left\{ C_9^{\text{eff}} \tilde{V}_{L\lambda} + \frac{m_B^2}{q^2} \left[\frac{2m_b}{m_B} C_7^{\text{eff}} \tilde{T}_{L\lambda} - 16\pi^2 h_\lambda \right] \right\}$$

$$h_\lambda(q^2) = \frac{\epsilon_\mu^*(\lambda)}{m_B^2} \int d^4x e^{iqx} \langle \bar{K}^* | T\{j_{\text{em}}^\mu(x) \mathcal{H}_{\text{eff}}^{\text{had}}(0)\} | \bar{B} \rangle$$

Non-factorizable power-suppressed contributions of 4-quark operators to the matrix element

- dominated by

| | | |
|---------|-----|--|
| Q_1^c | $=$ | $(\bar{s}_L \gamma_\mu T^a c_L)(\bar{c}_L \gamma^\mu T^a b_L)$, |
| Q_2^c | $=$ | $(\bar{s}_L \gamma_\mu c_L)(\bar{c}_L \gamma^\mu b_L)$, |



the charm pair can be close to the resonant region

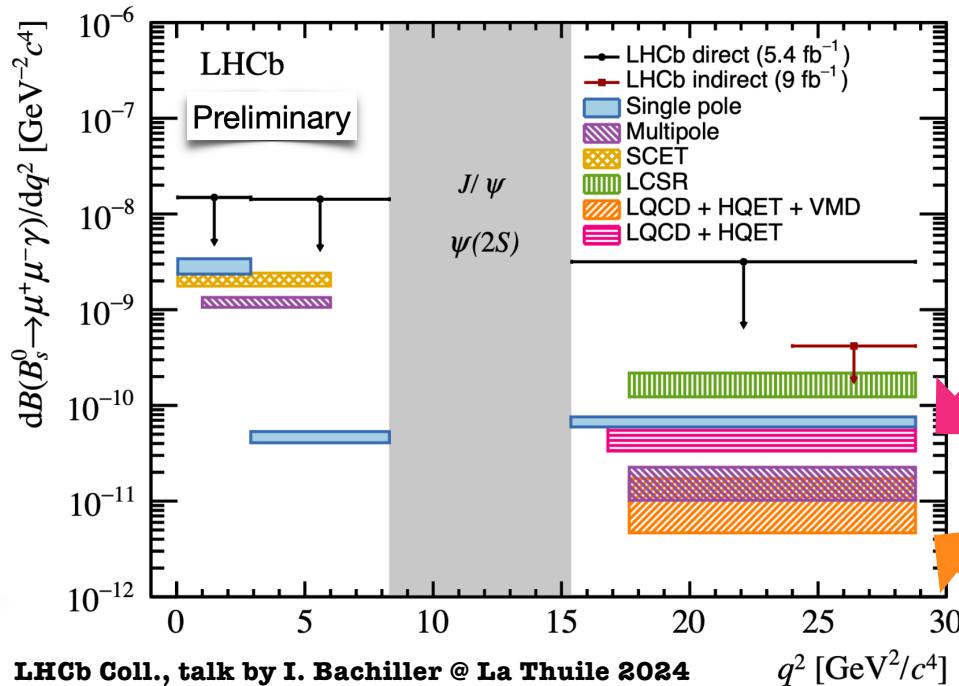
Do we know how to compute them?

In general, no!

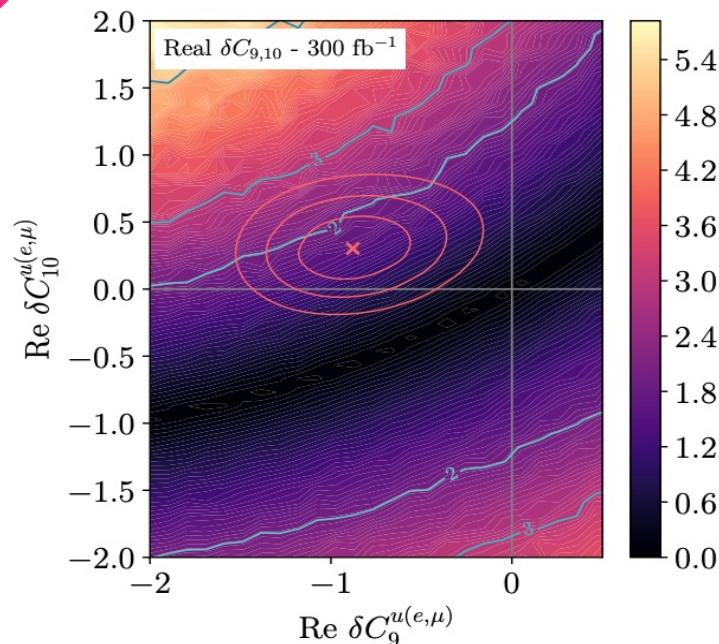
Courtesy by L. Silvestrini

Look for complementary $b \rightarrow s$ transitions

$B_s \rightarrow \mu\mu\gamma$ @ high- q^2 : in this range the observables depend on the same short distance effects as those present in $B \rightarrow K^{(*)} l^+l^-$ but long distance contributions are expected to be rather small



Theoretical progresses:
First lattice calculation by the
Rome-Southampton Collaboration
G. Gagliardi et al. (2402.03262)



Guadagnoli, Normand, Simula, Vittorio,
JHEP '23 [2308.00034]

Look for complementary $b \rightarrow s$ transitions

$B \rightarrow K^{(*)}vv$: short distance contributions dominate

Main uncertainties

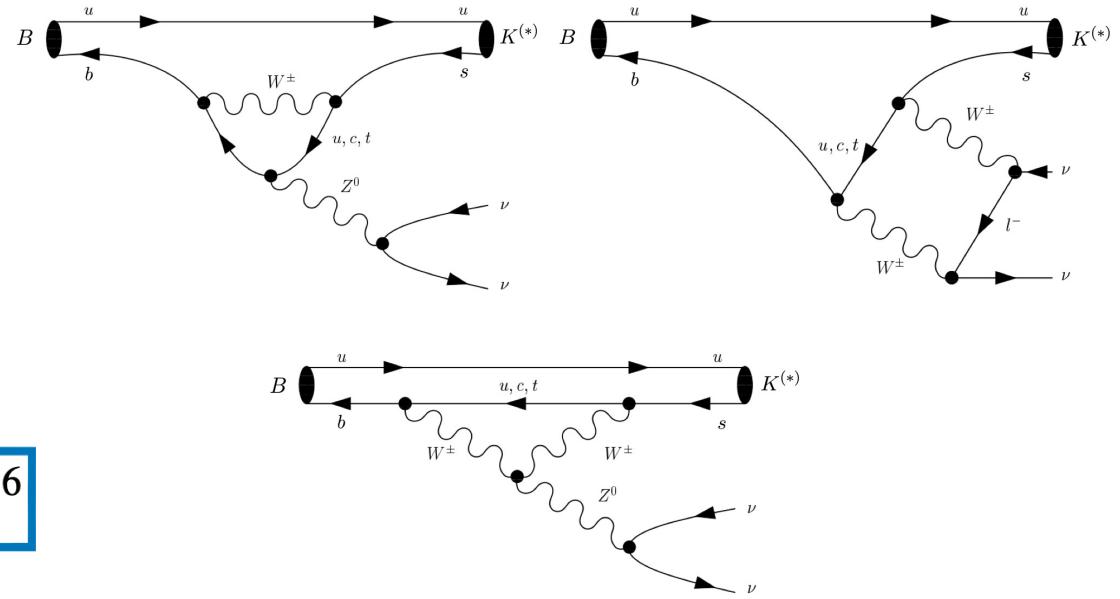
1. $|V_{cb}|$
2. Form factors

*SM prediction **

$$\mathcal{B}(B^\pm \rightarrow K^\pm \nu \bar{\nu}) = (4.44 \pm 0.30) \times 10^{-6}$$

Jernej F. Kamenik(Frascati) Christopher Smith(Karlsruhe U., TTP)
 Phys.Lett.B 680 (2009) 471-475 [0908.1174](#) [hep-ph]

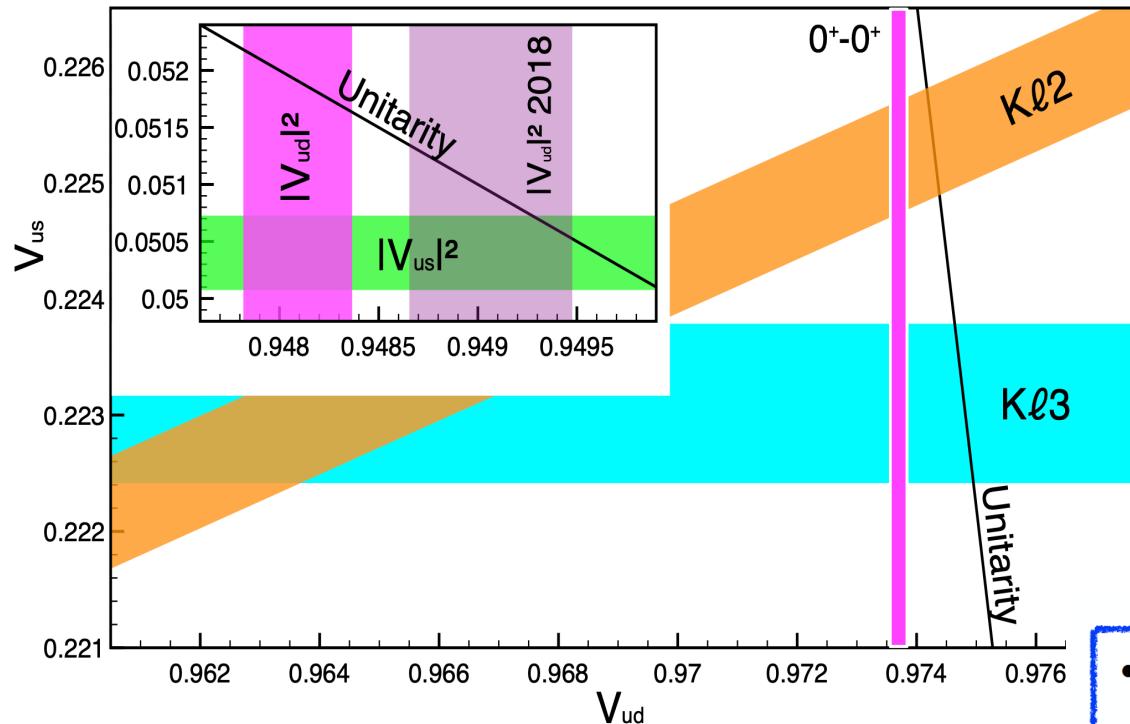
D. Becirevic, G. Piazza & O. Sumensari, EPJC '23 [arXiv:2301.06990]
 Phys.Lett.B 848 (2024) 138411 [2309.02246](#) *



Tension in $B \rightarrow Kvv$:
 2.8σ

$$\mathcal{B}(B^+ \rightarrow K^+ vv) \Big|_{\text{Belle-II}} = (2.4 \pm 0.7) \times 10^{-5}$$

Tensions with the unitarity of the first CKM row ?



M. Gorshteyn, talk @ CKM23 conference

Both theory and experiments demands a closer scrutiny of systematic errors

TO THE ORGANIZERS

- Until ~2018, bands *did* intersect in the same region on the unitarity circle ($< 2\sigma$)
- *Main* changes since then:
 - V_{us} from KI3 decreased ($\langle V \rangle$ increased with smaller uncertainty, 2+1+1 lattice QCD)
 - V_{ud} decreased (radiative corrections in nuclear & neutron increased with smaller uncertainty, dispersive)

$$|V_{ud}|^2 + |V_{us}|^2 + |V_{ub}|^2 = 0.9985(6)_{V_{ud}}(4)_{V_{us}}$$

~ 0.95 ~ 0.05 $\sim 10^{-5}$

Determination of $|V_{ud}|$ and $|V_{us}|$

$|V_{ud}|$

M. Gorshteyn, talk @ CKM23 conference

- Nuclear decays $0^+ - 0^+$ (es.: ${}^{14}\text{O} \rightarrow {}^{14}\text{N}$)

$$|V_{ud}^{0^+-0^+}| = 0.97370(1)_{exp, nucl}(3)_{NS}(1)_{RC}[3]_{total}$$

- Neutron β decay

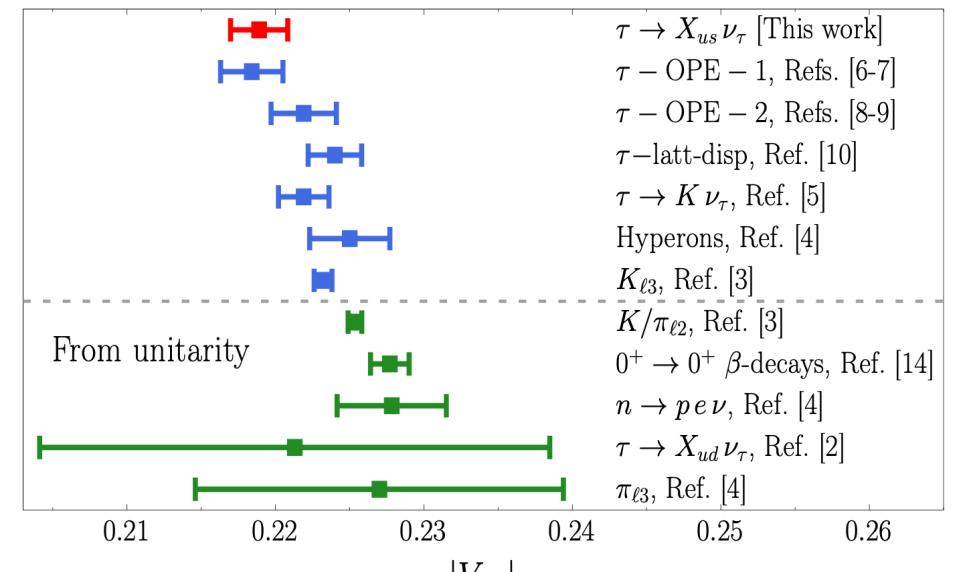
$$|V_{ud}^{\text{free n}}| = 0.9733(2)_{\tau_n}(3)_{g_A}(1)_{RC}[4]_{total}$$

- $\pi^+ \rightarrow \pi^0 e^+ \nu$:

$$|V_{ud}^{\pi\ell 3}| = 0.9739(27)_{exp}(1)_{RC}$$

improvable in the future with PIONEER (2203.01981)

$|V_{us}|$

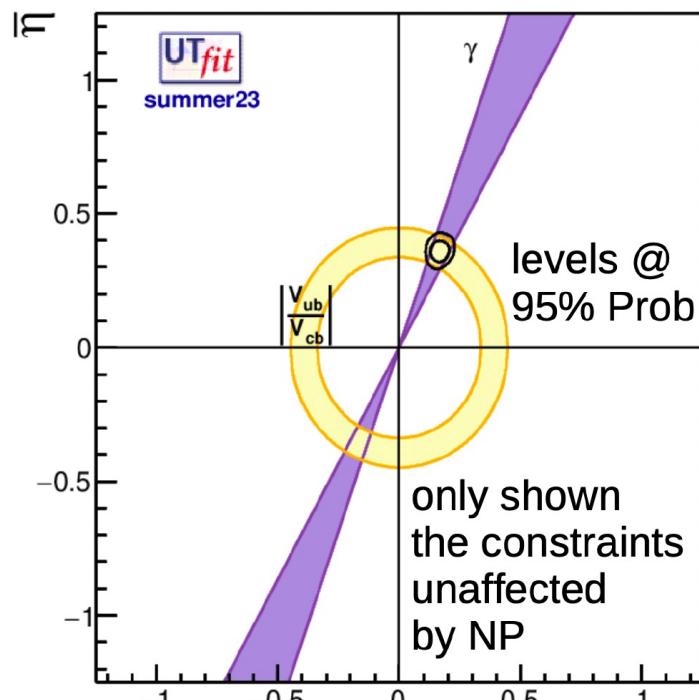


ETMC Collaboration [arXiv:2403.05404]



.... beyond
the Standard Model

Results of BSM analysis: CKM parameters

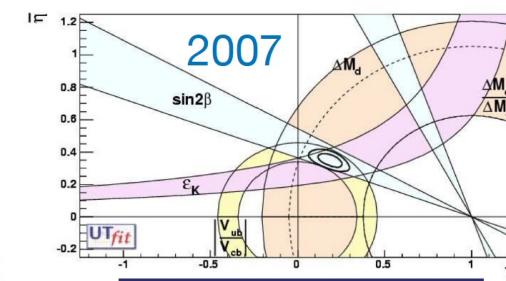


CKM parameters from BSM analysis

$$\bar{\rho} = 0.167 \pm 0.025$$

$$\bar{\eta} = 0.361 \pm 0.027$$

CKM parameters known (even in presence of NP effects) with similar precision of pre-LHC SM analysis 2004



$$\bar{\rho} = 0.164 \pm 0.028$$

$$\bar{\eta} = 0.340 \pm 0.016$$

1. The CKM phase is different from zero
2. The CKM phase is the dominant source of CP violation at low energy
3. No evidence for corrections to CKM
4. NP contributions to observed FCNC at most comparable (smaller) than the CKM ones
5. NP contributions very small in $s \rightarrow d$, $c \rightarrow u$, $b \rightarrow d$, $b \rightarrow s$

$$Q^{EXP} = V_{CKM} \langle F | \hat{O} | I \rangle$$

Constrains on NP from UTfit

$$Q^{EXP} = \sum_i C_{SM}^i(M_W, m_t, \alpha_s) \langle F | \hat{O}_i | I \rangle + \sum_{i'} C_{Beyond}^{i'}(\tilde{m}_\beta, \alpha_s) \langle F | \hat{O}_{i'} | I \rangle$$

UT generalization Beyond the Standard Model

- fit simultaneously for the CKM and the NP parameters (generalized UT analysis)
- parameterize BSM effects in $\Delta F = 2$ Hamiltonian in model-independent
- use all available experimental information
- find out NP contributions to $\Delta F=2$ transitions

$$A_q = C_{B_q} e^{2i\Phi_{B_q}} A_q^{SM} e^{2i\phi_q^{SM}} = \left(1 + \frac{A_q^{NP}}{A_q^{SM}} e^{2i(\Phi_q^{NP} - \phi_q^{SM})} \right) A_q^{SM} e^{2i\phi_q^{SM}}$$

$$\begin{aligned} \Delta m_{q/K} &= C_{B_q/\Delta m_K} (\Delta m_{q/K})^{SM} \\ A_{CP}^{B_d \rightarrow J/\psi K_s} &= \sin 2(\beta + \Phi_{B_d}) \\ A_{SL}^q &= \text{Im} \left(\Gamma_{12}^q / A_q \right) \\ \varepsilon_K &= C_\varepsilon \varepsilon_K^{SM} \\ A_{CP}^{B_s \rightarrow J/\psi \phi} &\sim \sin 2(-\beta_s + \Phi_{B_s}) \\ \Delta \Gamma^q / \Delta m_q &= \text{Re} \left(\Gamma_{12}^q / A_q \right) \end{aligned}$$



New local four-fermion operators are generated

$$Q_1 = (\bar{b}_L^A \gamma_\mu d_L^A) (\bar{b}_L^B \gamma_\mu d_L^B) \quad \text{SM}$$

$$Q_2 = (\bar{b}_R^A d_L^A) (\bar{b}_R^B d_L^B)$$

$$Q_3 = (\bar{b}_R^A d_L^B) (\bar{b}_R^B d_L^A)$$

$$Q_4 = (\bar{b}_R^A d_L^A) (\bar{b}_L^B d_R^B)$$

$$Q_5 = (\bar{b}_R^A d_L^B) (\bar{b}_L^B d_R^A)$$

+ those obtained by $L \leftrightarrow R$

Similarly for the s quark e.g.

$$(\bar{s}_R^A d_L^A) (s_R^B d_L^B)$$

$$\langle \bar{K}^0 | O_1(\mu) | K^0 \rangle = \frac{8}{3} M_K^2 f_K^2 B_1(\mu) ,$$

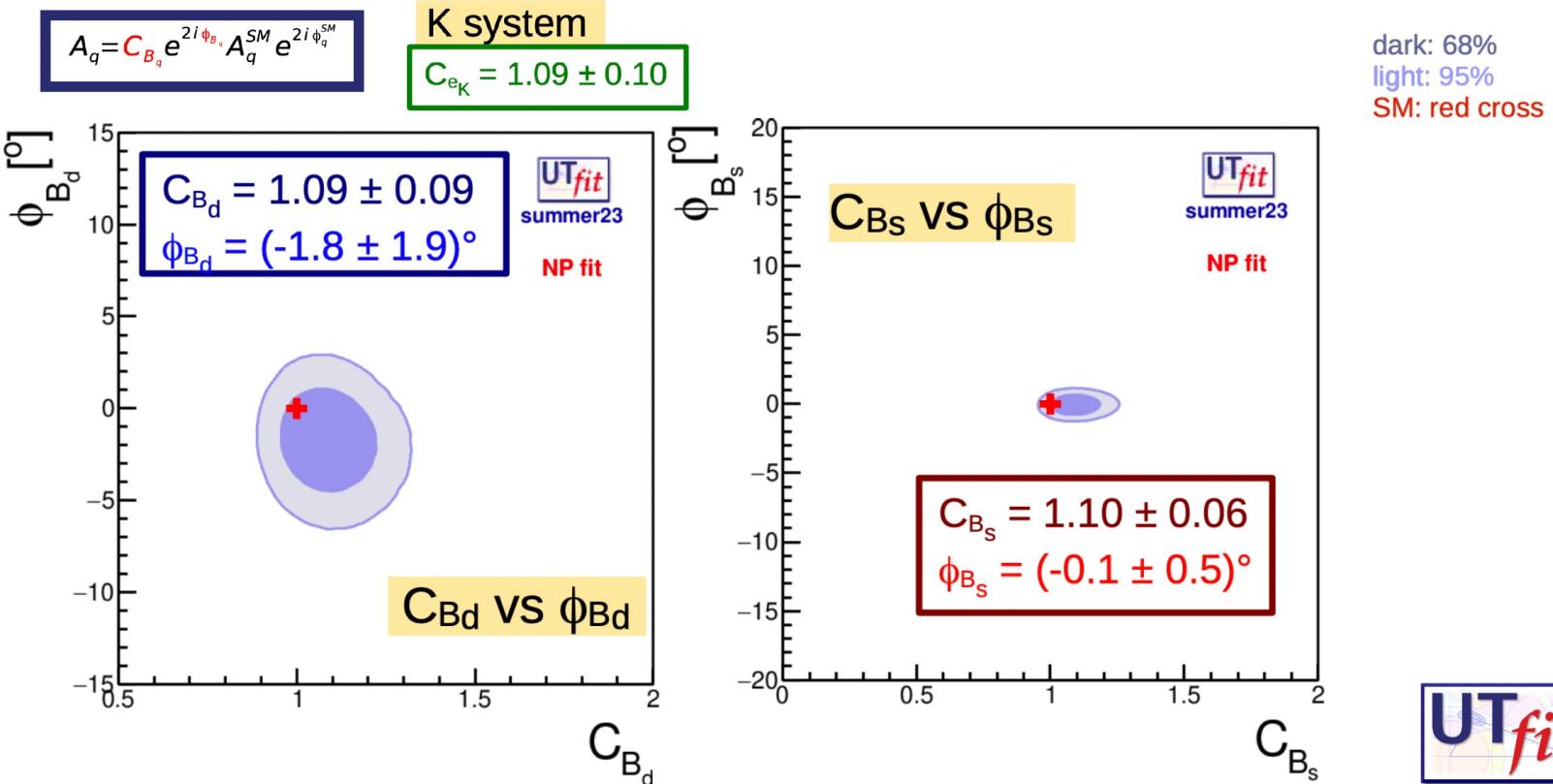
$$\langle \bar{K}^0 | O_2(\mu) | K^0 \rangle = -\frac{5}{3} \left(\frac{M_K}{m_s(\mu) + m_d(\mu)} \right)^2 M_K^2 f_K^2 B_2(\mu) ,$$

$$\langle \bar{K}^0 | O_3(\mu) | K^0 \rangle = \frac{1}{3} \left(\frac{M_K}{m_s(\mu) + m_d(\mu)} \right)^2 M_K^2 f_K^2 B_3(\mu) ,$$

$$\langle \bar{K}^0 | O_4(\mu) | K^0 \rangle = 2 \left(\frac{M_K}{m_s(\mu) + m_d(\mu)} \right)^2 M_K^2 f_K^2 B_4(\mu) ,$$

$$\langle \bar{K}^0 | O_5(\mu) | K^0 \rangle = \frac{2}{3} \left(\frac{M_K}{m_s(\mu) + m_d(\mu)} \right)^2 M_K^2 f_K^2 B_5(\mu) ,$$

Results of BSM analysis: New Physics parameters

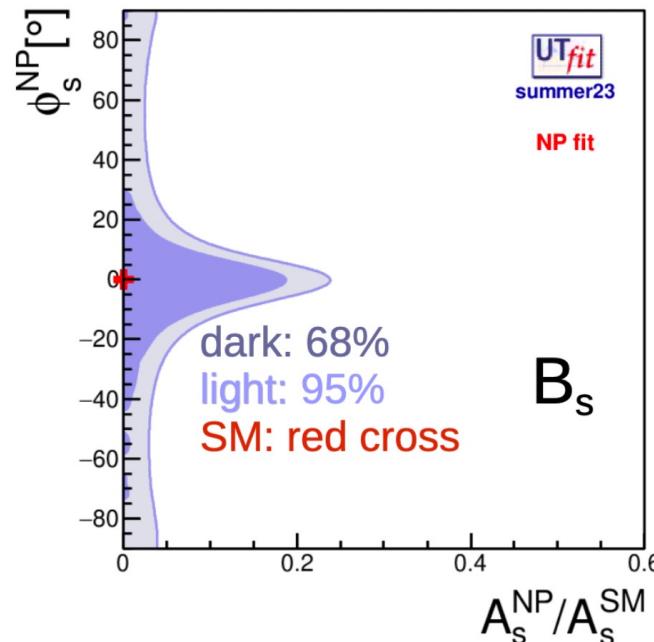
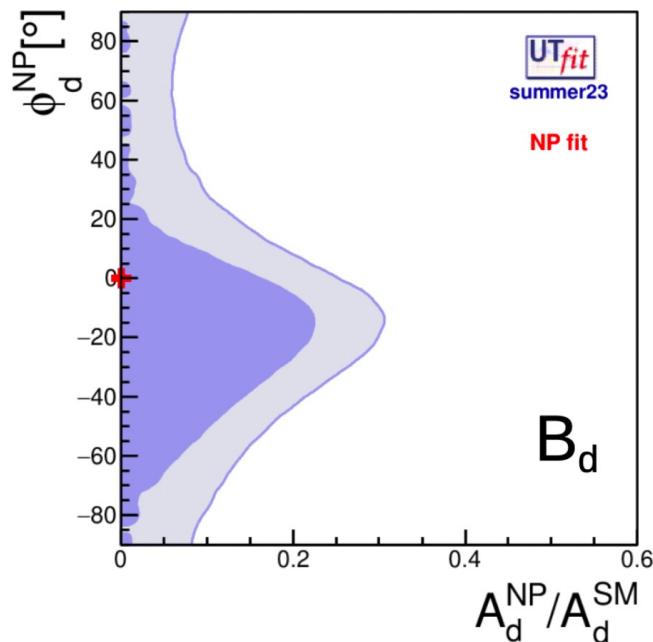


Results of BSM analysis: New Physics parameters

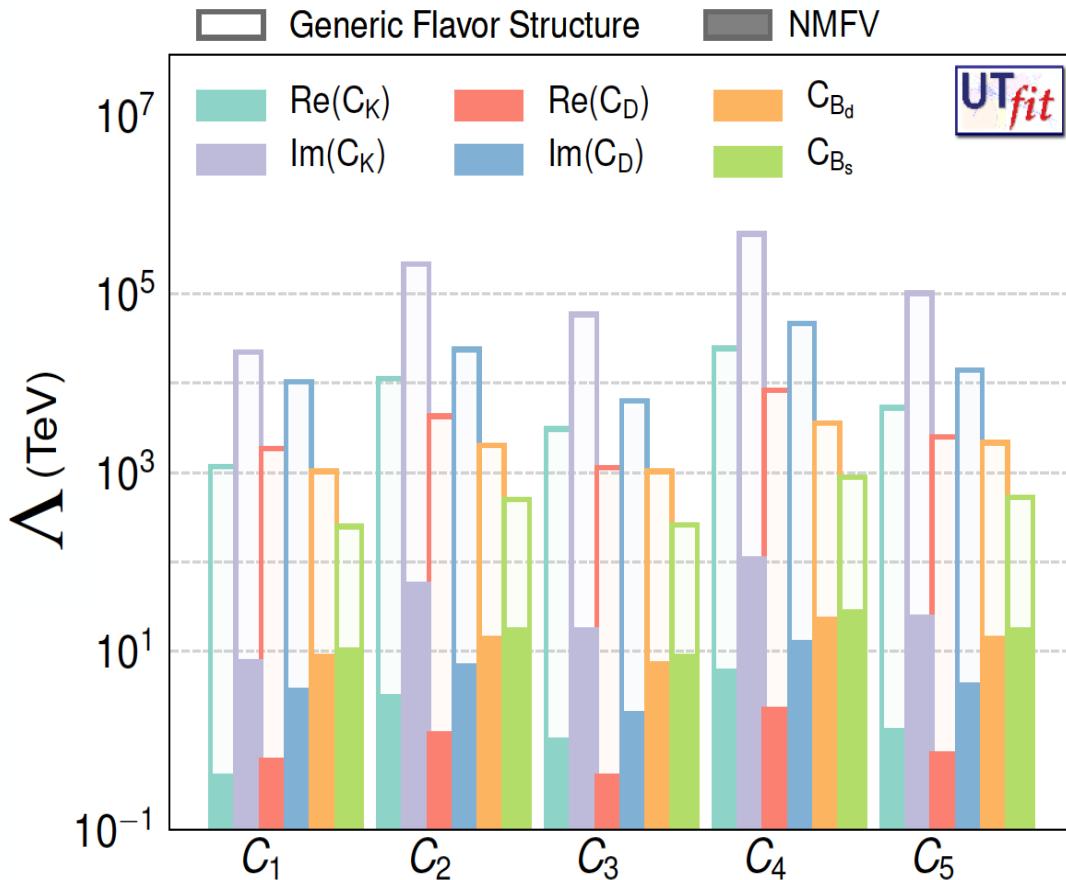
$$A_q = \left(1 + \frac{A_q^{NP}}{A_q^{SM}} e^{2i(\phi_q^{NP} - \phi_q^{SM})} \right) A_q^{SM} e^{2i\phi_q^{SM}}$$

The ratio of NP/SM amplitudes is:
 < 25% @ 68% prob. (35% @ 95%) in B_d mixing
 < 25% @ 68% prob. (30% @ 95%) in B_s mixing

dark: 68%
 light: 95%
 SM: red cross



Results of BSM analysis: probing New Physics Scale



- $\alpha \sim \alpha_w$ in case of loop coupling through weak interactions*

$$\Lambda > 1.3 \times 10^4 \text{ TeV}$$

$$\mathcal{H}_{\text{eff}}^{\Delta B=2} = \sum_{i=1}^5 C_i Q_i^{bq} + \sum_{i=1}^3 \tilde{C}_i \tilde{Q}_i^{bq}$$

$$Q_1^{q_i q_j} = \bar{q}_{jL}^\alpha \gamma_\mu q_{iL}^\alpha \bar{q}_{jL}^\beta \gamma^\mu q_{iL}^\beta ,$$

$$Q_2^{q_i q_j} = \bar{q}_{jR}^\alpha q_{iL}^\alpha \bar{q}_{jR}^\beta q_{iL}^\beta ,$$

$$Q_3^{q_i q_j} = \bar{q}_{jR}^\alpha q_{iL}^\beta \bar{q}_{jR}^\beta q_{iL}^\alpha ,$$

$$Q_4^{q_i q_j} = \bar{q}_{jR}^\alpha q_{iL}^\alpha \bar{q}_{jL}^\beta q_{iR}^\beta ,$$

$$Q_5^{q_i q_j} = \bar{q}_{jR}^\alpha q_{iL}^\beta \bar{q}_{jL}^\beta q_{iR}^\alpha .$$

$$C_i(\Lambda) = F_i \frac{L_i}{\Lambda^2}$$

- **Generic:** $C(\Lambda) = \alpha/\Lambda^2$ $F_i \sim 1$, arbitrary phase
- **NMFV:** $C(\Lambda) = \alpha \times |F_{\text{SM}}|/\Lambda^2$ $F_i \sim |F_{\text{SM}}|$, arbitrary phase

- $\alpha \sim \alpha_w$ in case of loop coupling through weak interactions*

$$\Lambda > 2.7 \text{ TeV}$$

- 1) NP must explain the strong hierarchy of the Fermion couplings/masses
- 2) If the scale of NP it is not too high it must suppresses FCNC processes at an acceptable level

$$Y_t \sim 1$$

$$Y_c \sim 10^{-2}$$

$$Y_u \sim 10^{-5}$$

$$Y_b \sim 10^{-2}$$

$$Y_s \sim 10^{-3}$$

$$Y_d \sim 10^{-5}$$

$$Y_\tau \sim 10^{-2}$$

$$Y_\mu \sim 10^{-3}$$

$$Y_e \sim 10^{-6}$$

$$|V_{us}| \sim 0.2$$

$$|V_{cb}| \sim 0.04$$

$$|V_{ub}| \sim 0.004$$

$$\delta \sim 1$$

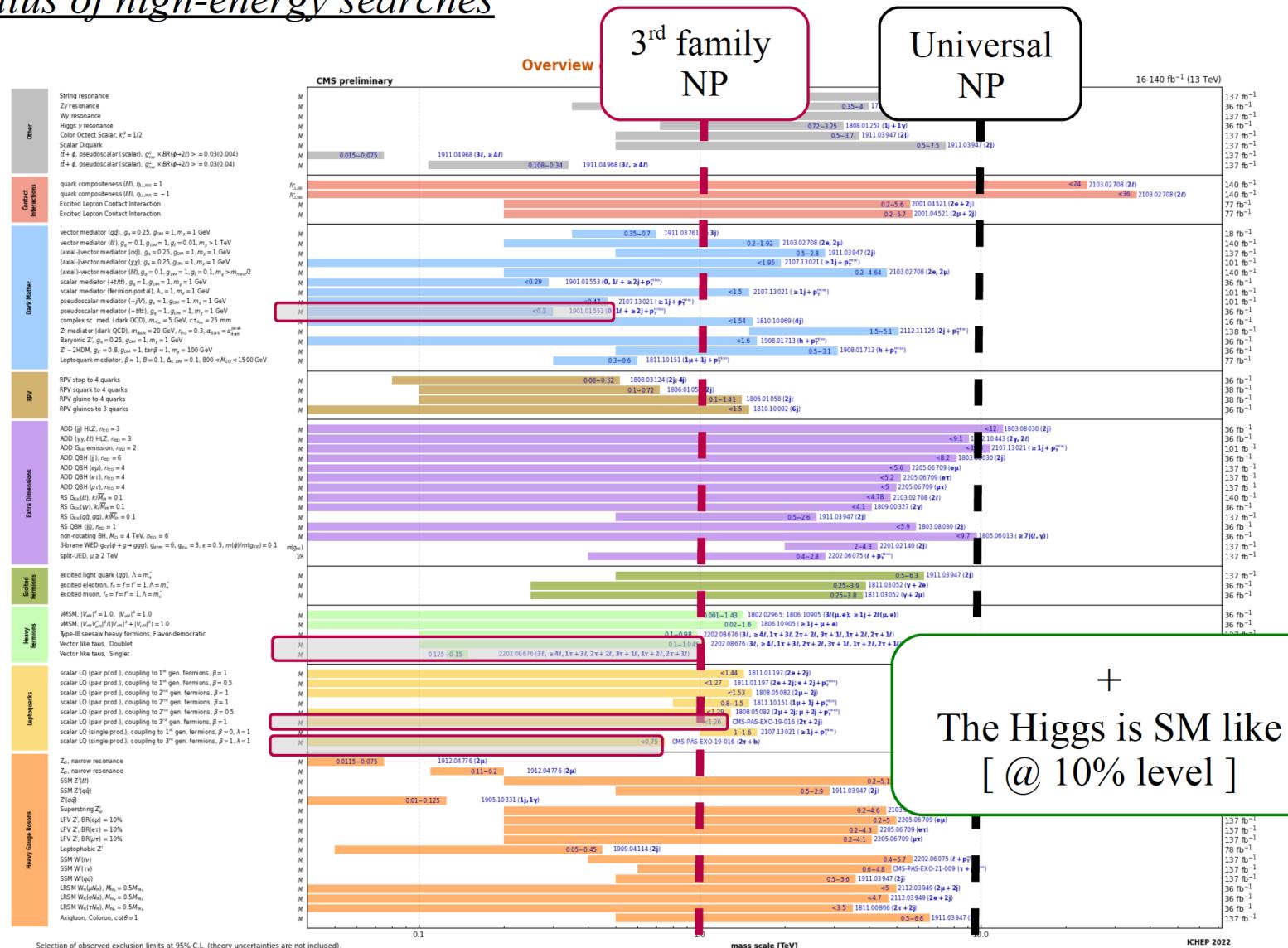
$$0.1 \sim g' , \quad g , \quad g_s , \quad \lambda \quad \sim 1.$$

*FUTURE, BSM: It is difficult to make predictions,
especially about the future*

*It is time to
leave you in
the hands of
R. Barbieri*



Status of high-energy searches



If these ideas corrects, new non-standard effects should emerge soon both at low and at high energies (→ very interesting opportunities for run-3...).

absence says more than presence

FRANK HERBERT

(Dune)

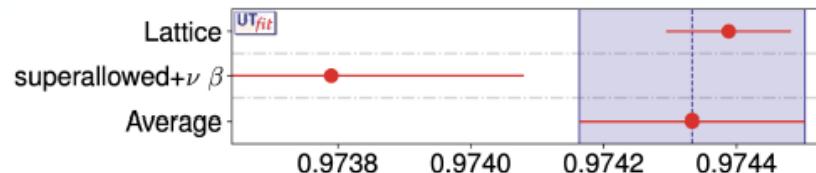
THANKS FOR YOUR ATTENTION



What's new for EPS23

• Theory updates:

- New V_{ud} extraction from neutron decays, following [V. Cirigliano et al. arXiv:2306.03138](#)



- New lattice values for masses

- New lattice form factors for exclusive
 $b \rightarrow q\ell\nu$

• Experiment updates:

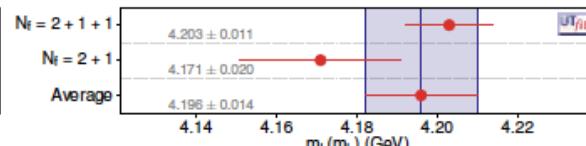
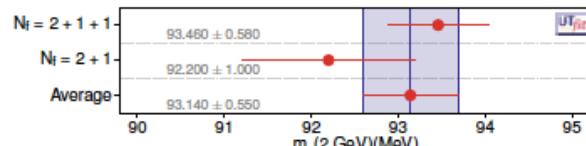
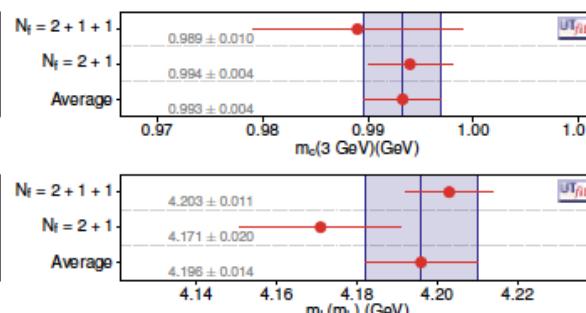
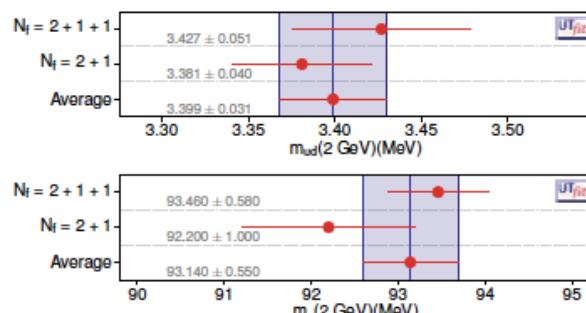
- New $\sin 2\beta$ by LHCb

- New γ by LHCb

- New a

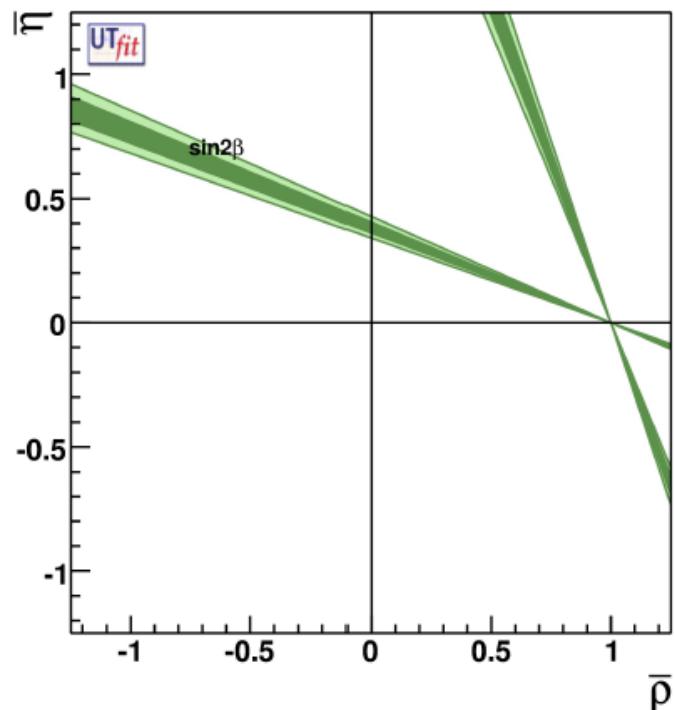
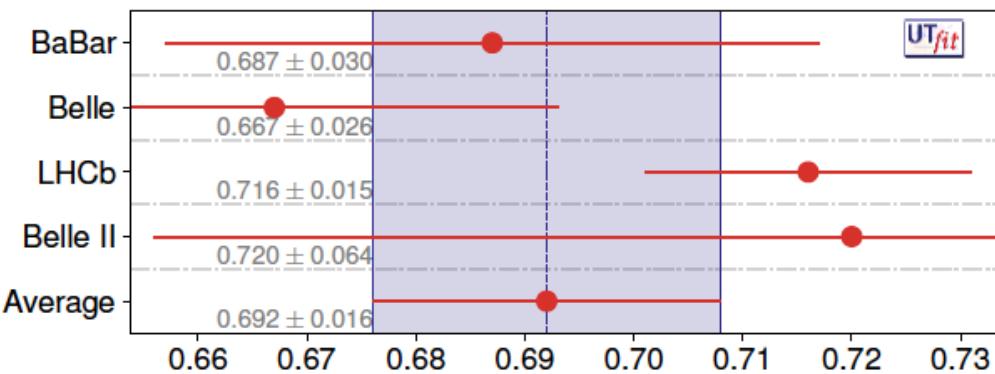


All masses computed in $\overline{\text{MS}}$ and averaged with PDG scale factors



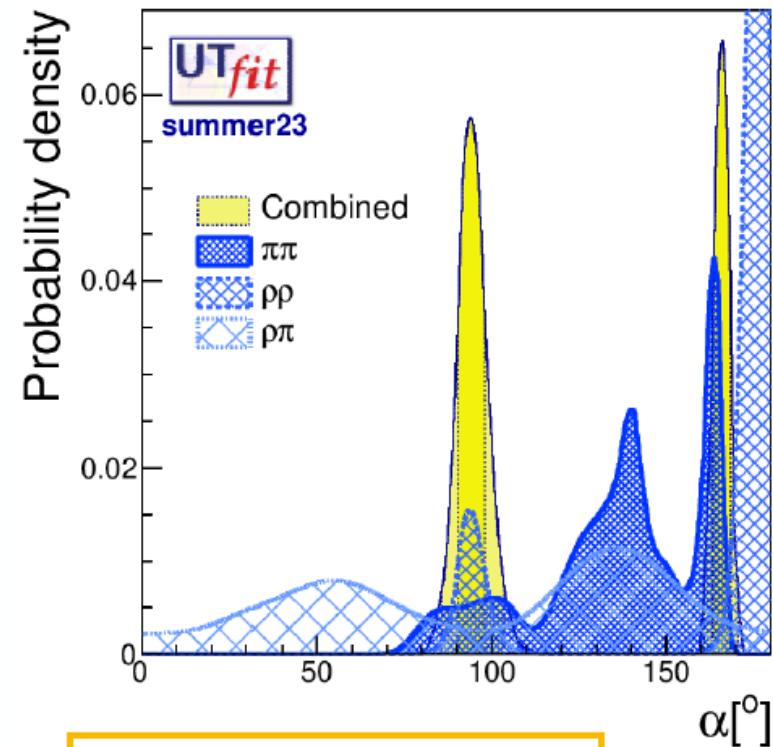
What's new for EPS23: $\sin(2\beta)$

- Averaged charmonium values
- New $\sin 2\beta$ from LHCb
- Average including correction due to Cabibbo-suppressed penguin contribution:
- Most recent estimate $\Delta(\sin 2\beta) = -0.1 \pm 0.1$
- Theoretical uncertainty comparable to experimental error



What's new for EPS23

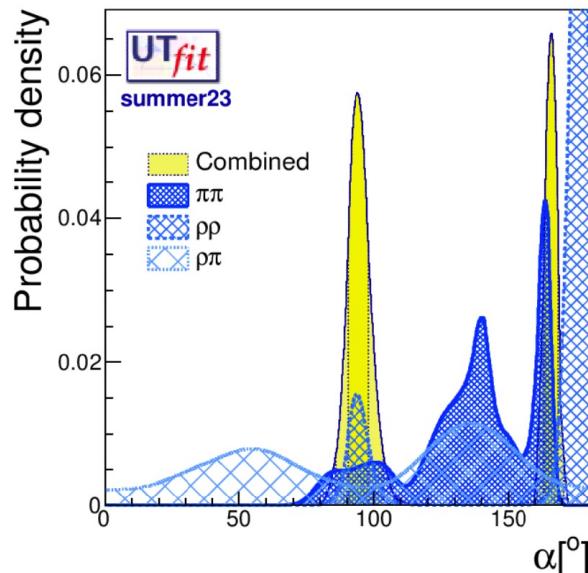
- Updated the bound on α with
 - Bounds from $\pi\pi$ and pp derived from PDG averages (including PDG rescaling of the error)
 - Bound from $p\pi$ derived from same inputs used by HFLAV
- As usual, main difference wrt other combinations is in the treatment of the multiple solutions
- Profiling vs marginalization: in our case, multiple overlapping solutions counts more than a single solution when integrating out the other quantities (T , P , and strong phases)



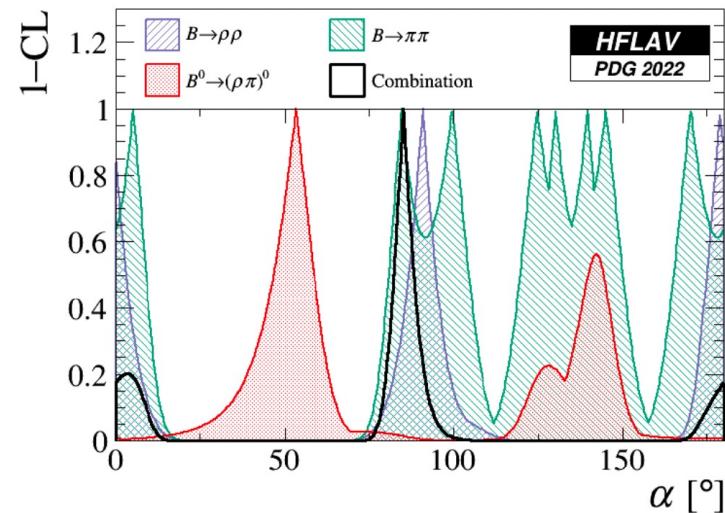
$$\alpha = (93.8 \pm 4.5)^\circ$$



More on α



$$\alpha^{\text{exp}} = 93.8^\circ \pm 4.5^\circ$$



$$\alpha_{\text{HFLAV}} = 85.5 \pm 4.6$$

Inputs are slightly different from what HFLAV because for the BR averages we use the PDG (with the error inflation if there is a tension), while HFLAV would use their averages without error inflation.

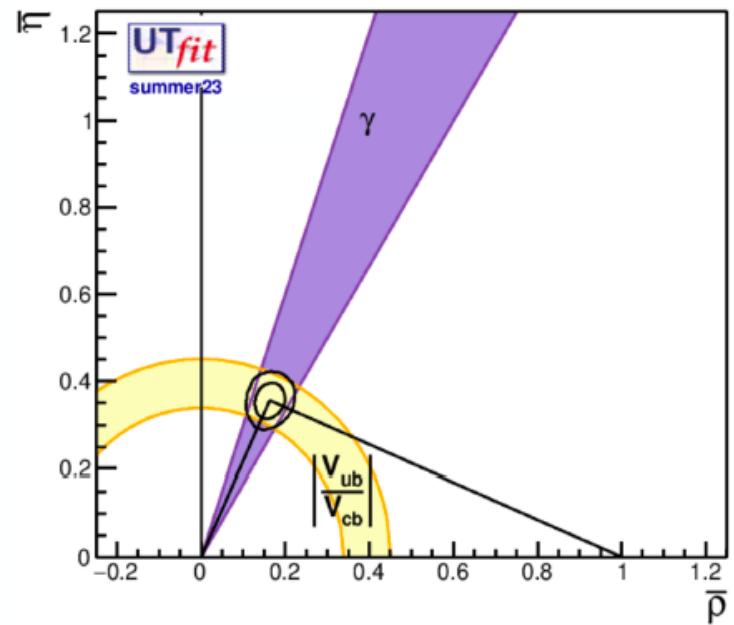
So the pipi BR inputs are slightly different. We also use the updated rho pi.

HFLAV

It seems that the reason why the combination falls on the pipi solution on the left of the rho rho peak (while the right solution would be just as probable and even not distinguishable) is due to the small bump from the rho pi distribution which instead goes to zero for the pipi solution on the right.

What's new for EPS23

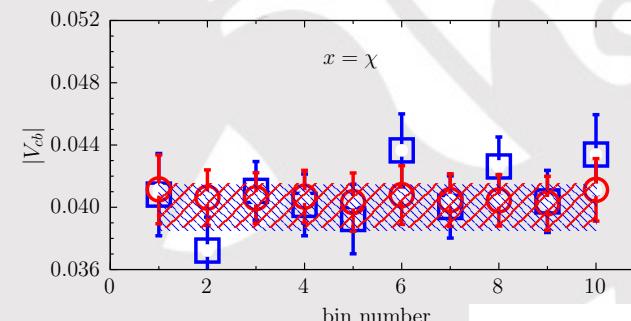
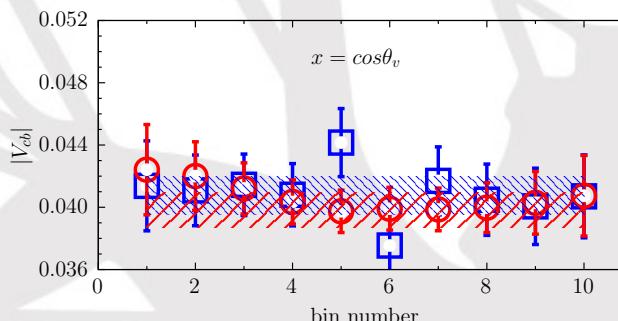
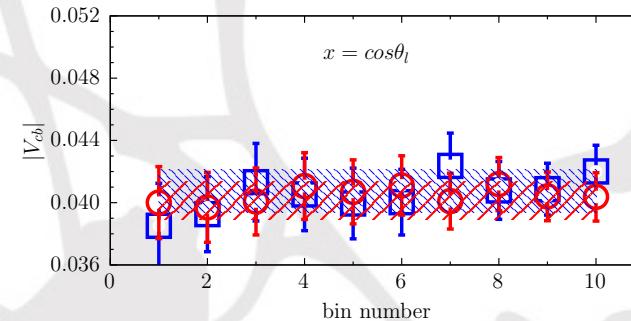
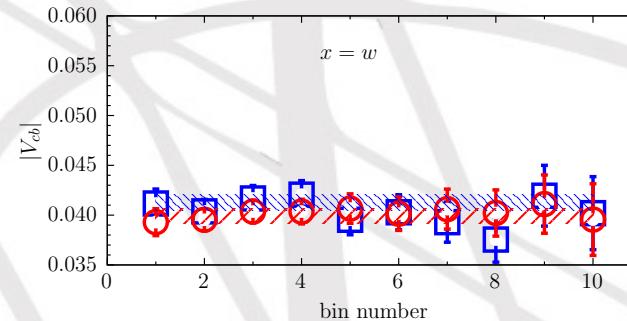
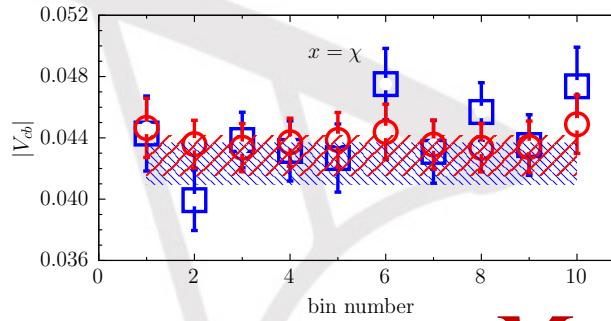
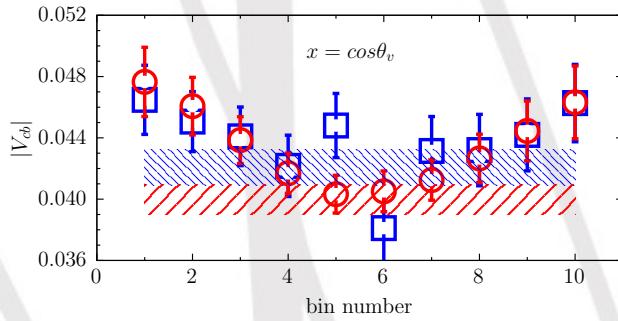
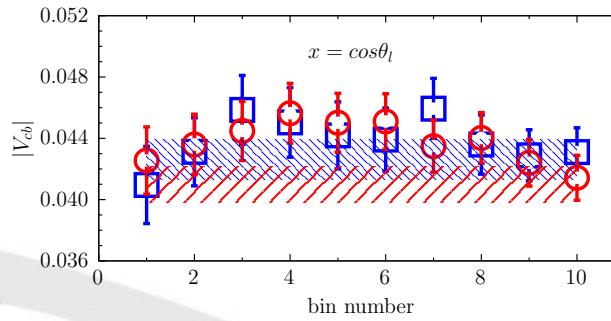
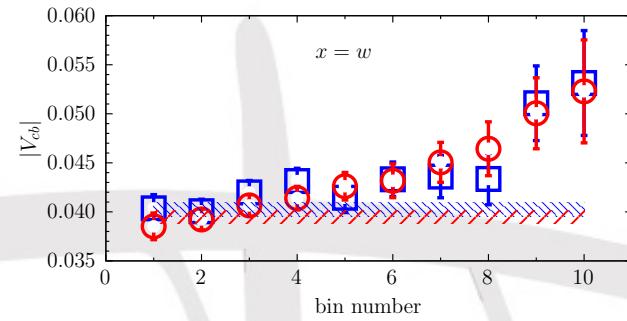
- Determination combining all $D^{(*)}K^{(*)}$ modes
- Simultaneous extraction of γ and $D\bar{D}$ mixing parameters (which enter the BSM analysis)
- Details are given in dedicated [talk by R. Di Palma on Friday](#)
- Tree-level determination
- Baseline determination of CP violation in the SM, assuming BSM effects enter only at loop
- With $|V_{ub}/V_{cb}|$, allows for a robust fit of the CKM parameters in the SM, even in presence of new physics



$$\begin{aligned}\bar{\rho} &= \pm 0.163 \pm 0.024 \\ \bar{\eta} &= \pm 0.356 \pm 0.027\end{aligned}$$



See talk by G. D'Ambrosio



FNAL/MILC

Mainly due to $F_1(w)$

JLQCD

GM,S. Simula,L.Vittorio

compatibility plots

A way to “measure” the agreement of a single measurement with the indirect determination from the fit using all the other inputs: test for the SM description of the flavour physics

2022

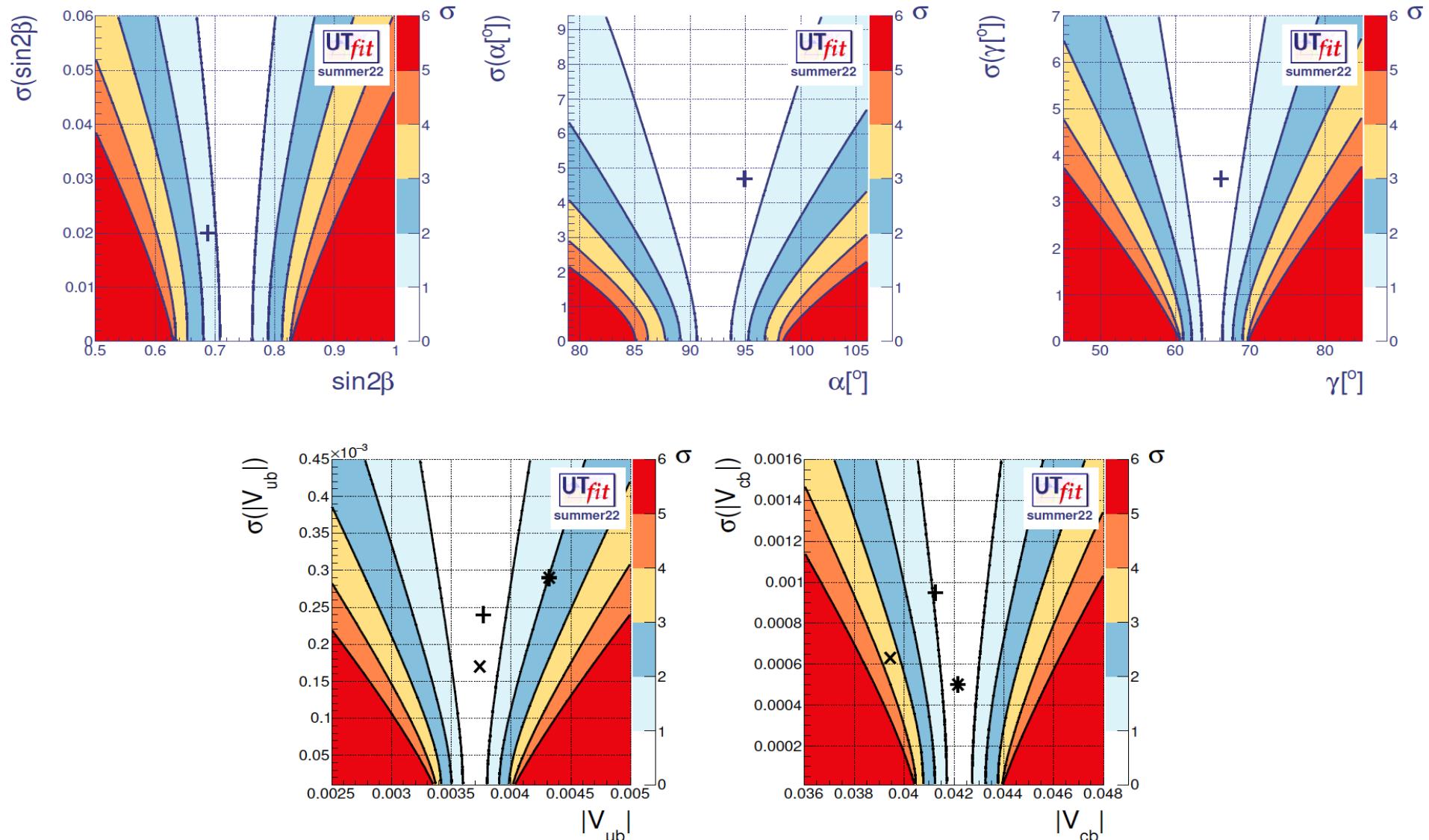


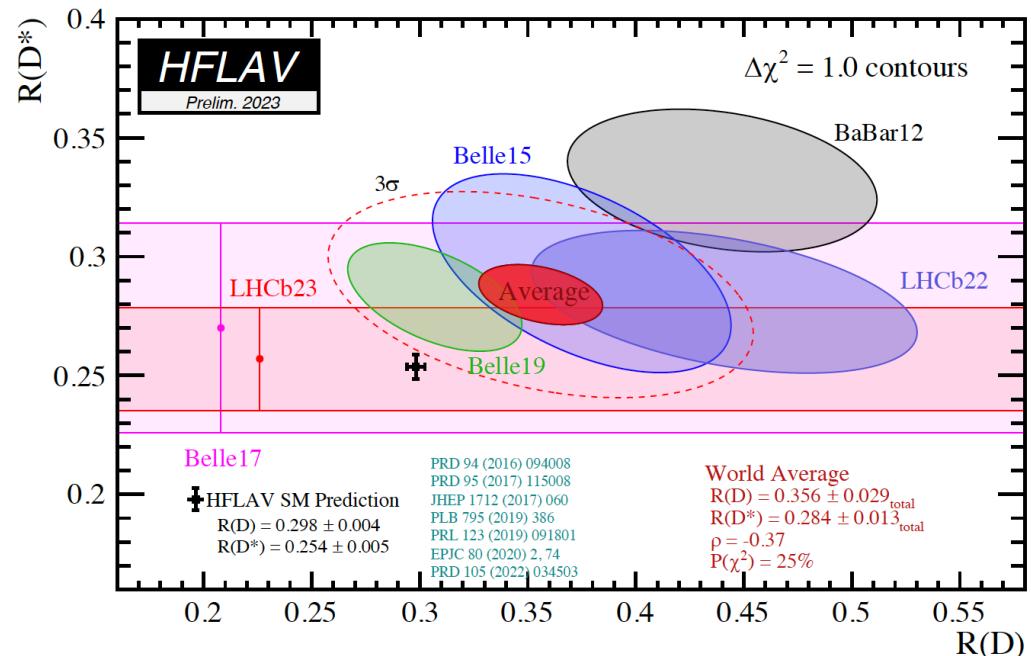
FIG. 5. Pull plots (see text) for $\sin 2\beta$ (top-left), α (top-centre), γ (top-right), $|V_{ub}|$ (bottom-left) and $|V_{cb}|$ (bottom-right) inputs. The crosses represent the input values reported in Table I. In the case of $|V_{ub}|$ and $|V_{cb}|$ the x and the * represent the values extracted from exclusive and inclusive semileptonic decays respectively.

State-of-the-art of the semileptonic $B \rightarrow \{D^*, \pi\}$ decays

Two critical issues

- V_{cb} - exclusive/inclusive $|V_{cb}|$ puzzle:
 exclusive (FLAG '21): $|V_{cb}|(BGL) \cdot 10^3 = 39.36(68)$ inclusive (HFLAV '21): $|V_{cb}| \cdot 10^3 = 42.19(78)$
 difference of $\sim 2.7 \sigma$ $|V_{cb}| \cdot 10^3 = 42.16(50)$
 (Bordone et al. 2107.00604)
- $R_{D^(*)}$

$$\begin{aligned} \mathcal{R}(D) &= \frac{\mathcal{B}(B \rightarrow D\tau\nu_\tau)}{\mathcal{B}(B \rightarrow D\ell\nu_\ell)}, \\ \mathcal{R}(D^*) &= \frac{\mathcal{B}(B \rightarrow D^*\tau\nu_\tau)}{\mathcal{B}(B \rightarrow D^*\ell\nu_\ell)} \end{aligned}$$

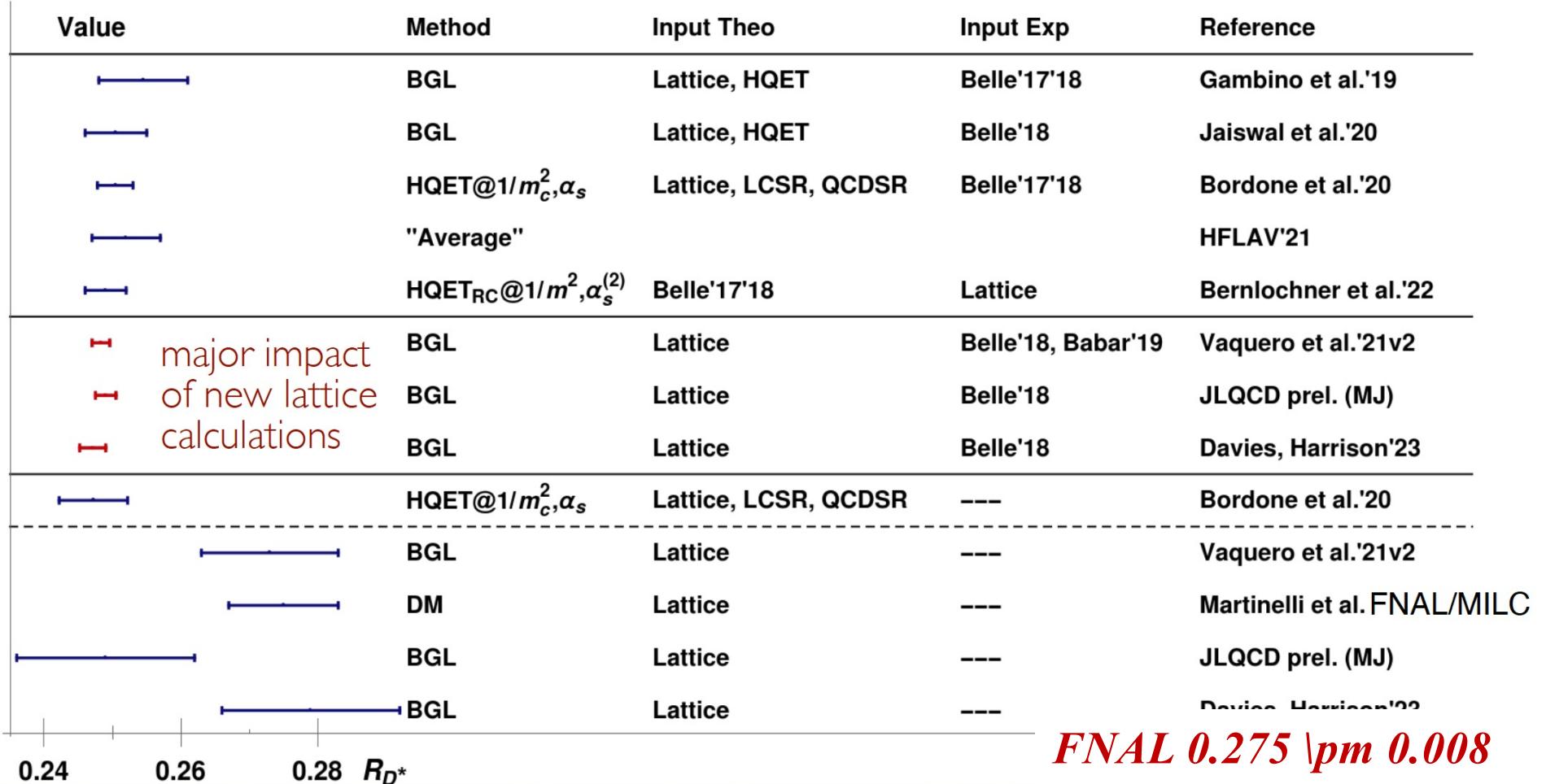


HFLAV Collaboration, PRD '23 [arXiv:2206.07501] ([updated plot](#))

2022

3.2σ tension

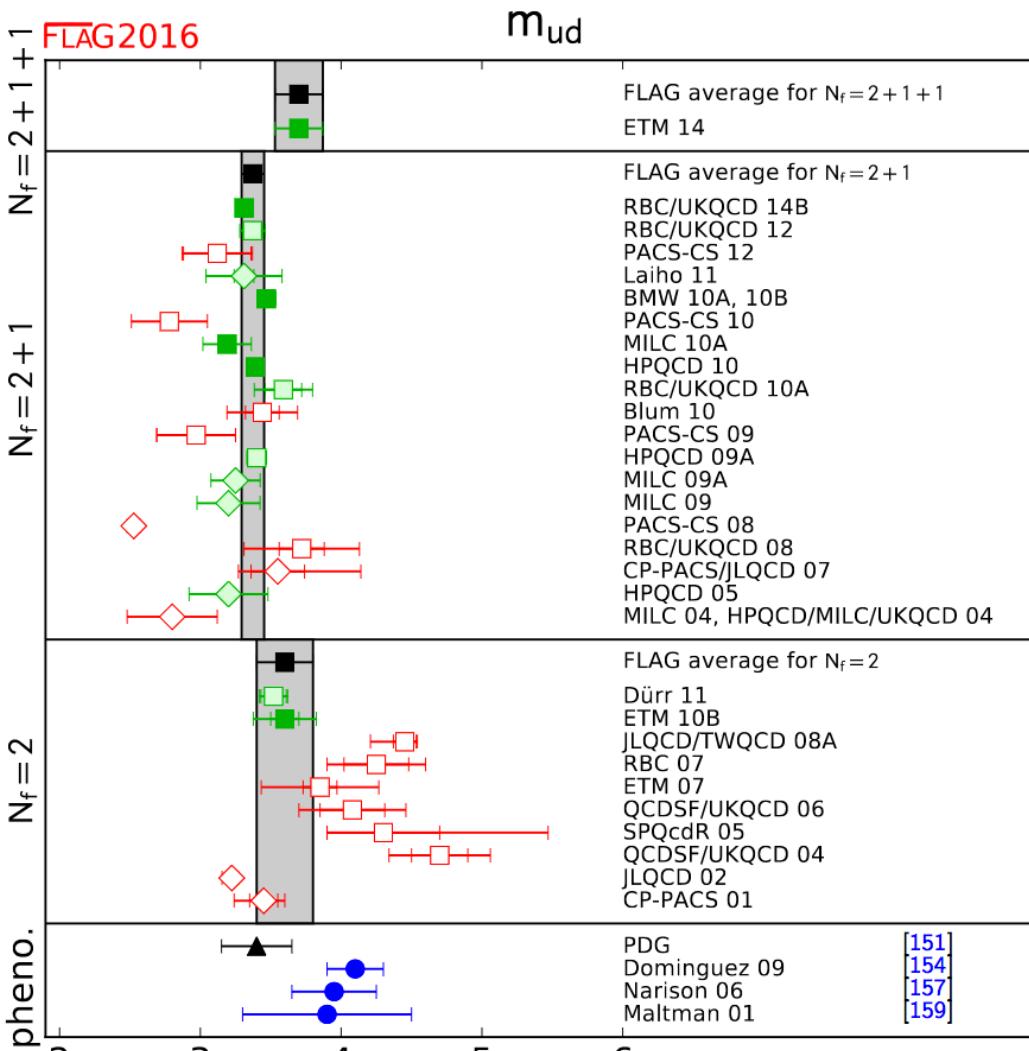
Overview over predictions for $R(D^*)$



FNAL 0.275 \pm 0.008
JLQCD 0.248 \pm 0.008
HPQCD 0.276 \pm 0.009

Predictions based only on Fermilab & HPQCD lead to large agreement with exp, mostly because of the suppression at high m_c of the denominator.

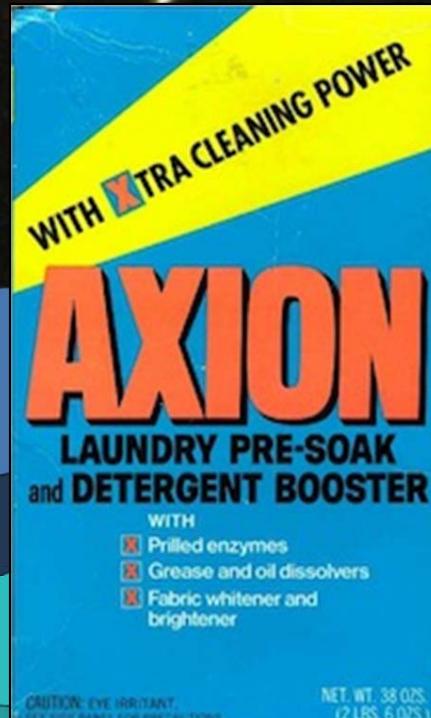
I see no reason not to use experimental data for a SM test, especially in presence of tensions in lattice data.



| N_f | m_u | m_d | m_u/m_d | R | Q |
|-------|------------|-------------|------------|----------------|----------------|
| 2+1+1 | 2.36(24) | 5.03(26) | 0.470(56) | 35.6(5.1) | 22.2 (1.6) |
| 2+1 | 2.16(9)(7) | 4.68(14)(7) | 0.46(2)(2) | 35.0(1.9)(1.8) | 22.5(6)(6) |
| 2 | 2.40(23) | 4.80(23) | 0.50(4) | 40.7(3.7)(2.2) | 24.3(1.4)(0.6) |

Raffelt

Dark Energy 73%
(Cosmological Constant)



See several
talks on axions
tomorrow

Ordinary Matter 4%
(of this only about
10% luminous)

Dark Matter
23%

Neutrinos
0.1–2%

B meson real photon emissions

Factorization at leading power in an expansion of the decay amplitude in $\Lambda_{\text{QCD}}/E_\gamma$ and $\Lambda_{\text{QCD}}/\text{mb}$ has been established to all orders in the strong coupling α_s . In this approximation, the branching fraction depends only on the leading-twist B-meson light-cone distribution amplitude (LCDA)

More precisely, it is proportional to $1/\lambda_B$, the most important LCDA parameter in exclusive decays, is uncertain by a large factor ranging from 200 MeV favoured by non-leptonic decays to 460 MeV from QCD sum rules.

The radiative leptonic decay has therefore been suggested as a measurement of λ_B

$$\phi_+(\omega, \mu)$$

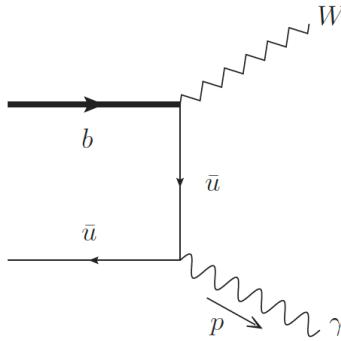


Figure 1. Leading contribution to $B \rightarrow \gamma \ell \nu_\ell$.

For large photon energies the form factors can be written as [9]

$$\begin{aligned} F_V(E_\gamma) &= \frac{e_u f_B m_B}{2 E_\gamma \lambda_B(\mu)} R(E_\gamma, \mu) + \xi(E_\gamma) + \Delta\xi(E_\gamma), \\ F_A(E_\gamma) &= \frac{e_u f_B m_B}{2 E_\gamma \lambda_B(\mu)} R(E_\gamma, \mu) + \xi(E_\gamma) - \Delta\xi(E_\gamma). \end{aligned} \quad (2.7)$$

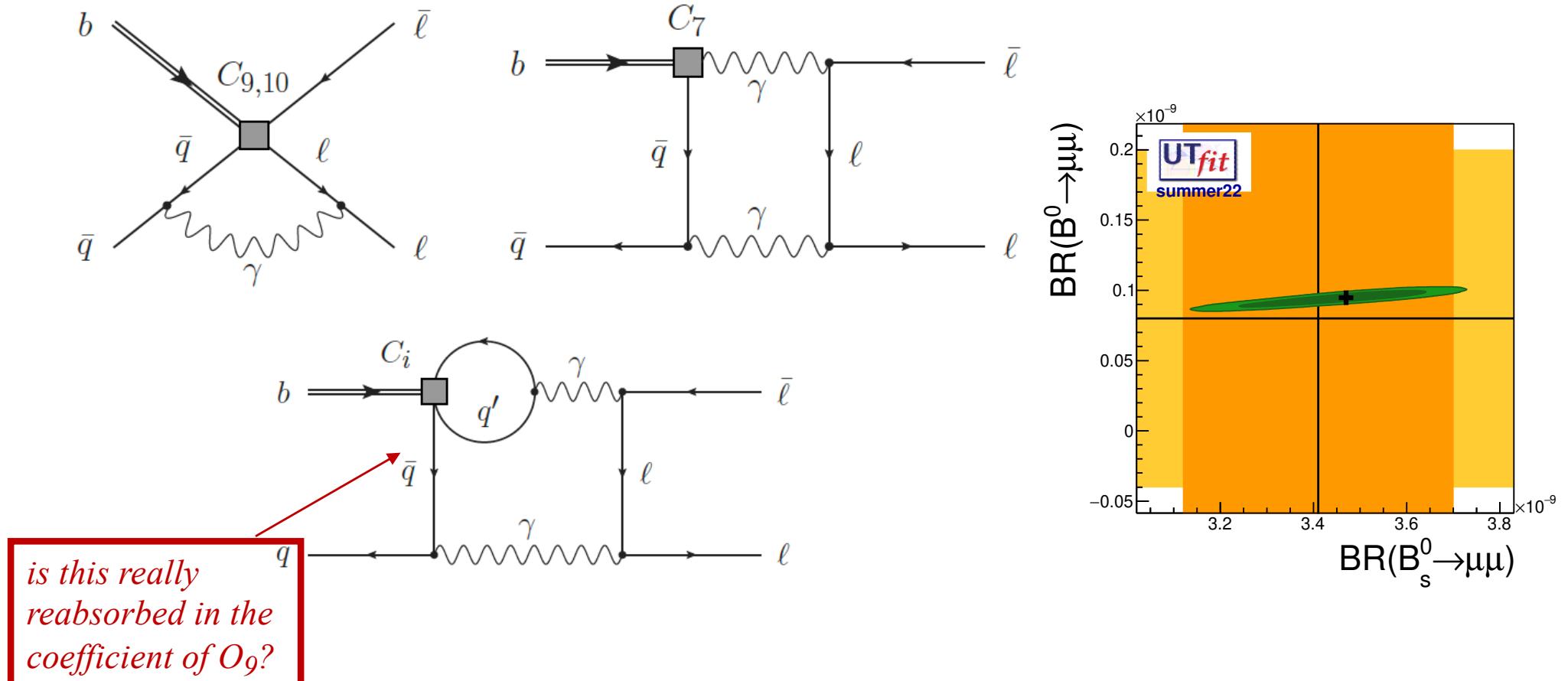
The first term is equal in both expressions and represents the leading-power contribution in the heavy-quark expansion (HQE). It originates only from photon emission from the light spectator quark in B meson (Fig. 1). In the above, f_B is the decay constant of B meson, and the quantity λ_B is the first inverse moment of the B -meson LCDA,

$$\frac{1}{\lambda_B(\mu)} = \int_0^\infty \frac{d\omega}{\omega} \phi_+(\omega, \mu). \quad (2.8)$$

Further applications in decays of heavy neutral B mesons: Virtual corrections (some questions still open)

Enhanced electromagnetic correction to the rare B -meson decay $B_{s,d} \rightarrow \mu^+ \mu^-$

Martin Beneke,¹ Christoph Bobeth,^{1,2} and Robert Szafron¹



Further applications in decays of heavy neutral B mesons: real corrections (some questions still open)

$$B_s^0 \rightarrow \mu^+ \mu^- \gamma \text{ from } B_s^0 \rightarrow \mu^+ \mu^-$$

Francesco Dettori^a, Diego Guadagnoli^b and Méril Reboud^{b,c}

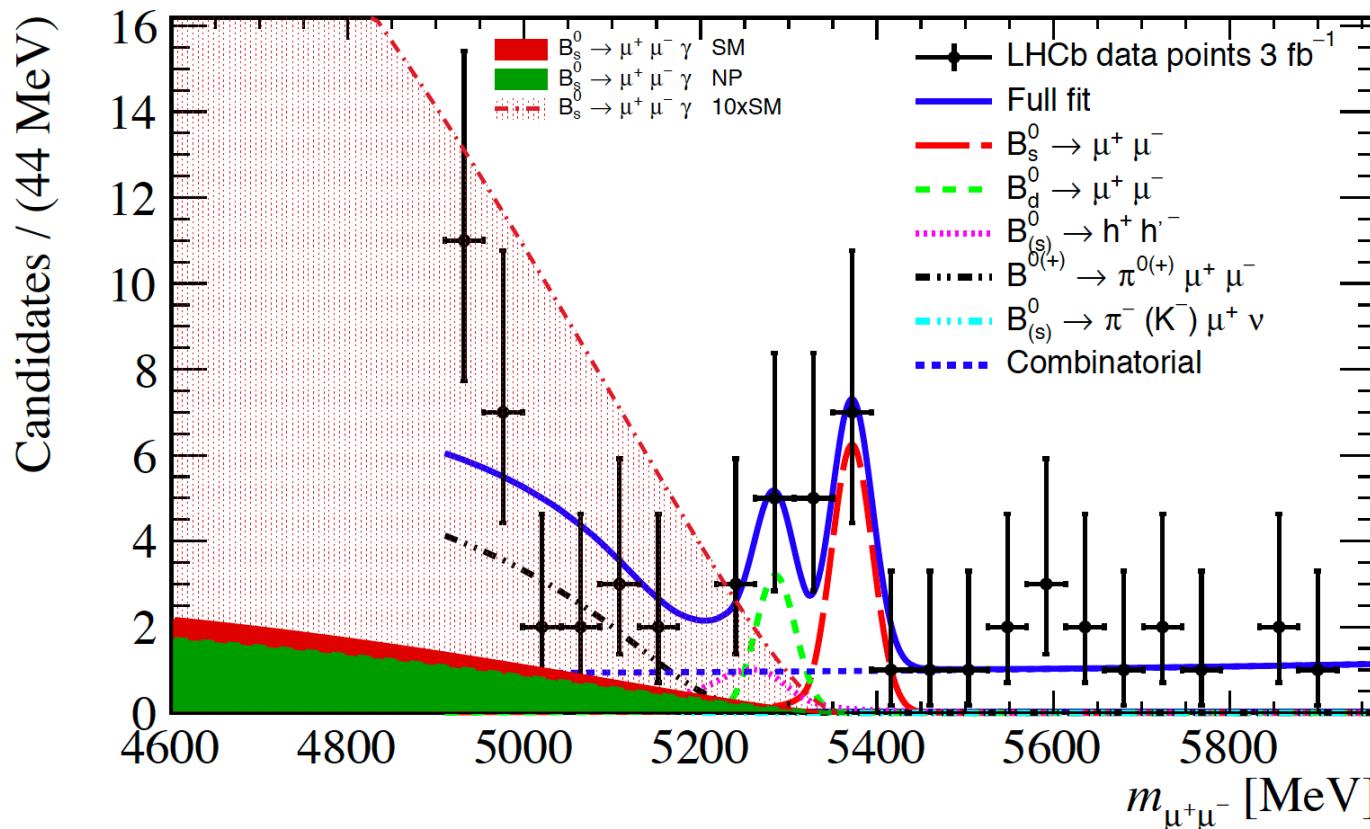
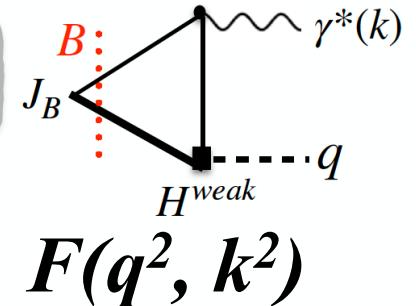


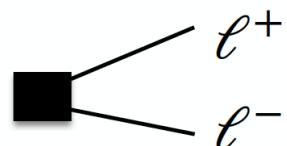
Figure 3: Dimuon invariant mass distribution from LHCb's measurement of $\mathcal{B}(B_s^0 \rightarrow \mu^+ \mu^-)$ [52] overlayed with the contribution expected from $B_s^0 \rightarrow \mu^+ \mu^- \gamma$ decays (ISR only). Assumes flat efficiency versus $m_{\mu^+\mu^-}$. The line denoted as ' $B_s^0 \rightarrow \mu^+ \mu^- \gamma$ NP' refers to the $V - A$ case with $\delta C_9 = -12\% C_9^{\text{SM}}$ (see also Fig. 2). The two filled curves are not stacked onto each other.

Particle(s) from weak vertex with momenta q



- **FCNC** $Q_b = Q_q$ (need long distance in addition) :

$$F(q^2, k^2)$$



$$H^{weak} \sim O_{9,10} : B_{d,s} \rightarrow \ell^+ \ell^- \gamma$$

$$F(q^2) = F(q^2, 0)$$

Bobeth's talk



$$H^{weak} \sim O_7 : B_{d,s} \rightarrow \ell^+ \ell^- \gamma$$

$$F^*(k^2) = F(0, k^2)$$



$$H^{weak} \sim \bar{q} \gamma_\mu b_L \partial^\mu a : B_{d,s} \rightarrow \ell^+ \ell^- a$$

$$F(m_a^2, k^2) \rightarrow F^*(k^2)$$

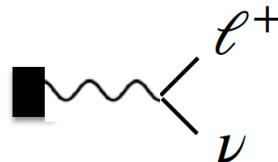
Ziegler's talk

or dark photon, scalar DM, ...

Xin-Yu Tuo et al. arXiv:2103.11331

G. Gagliardi et al. arXiv:2202.03833 [hep-lat]

- **FCCC** $Q_b \neq Q_q$:



$$H^{weak} \sim V_{ub} \bar{u} \gamma_\mu b_L \ell \gamma^\mu \nu_L : B_u \rightarrow \ell^+ \nu \gamma$$

- Physics: helicity suppression of $B \rightarrow f_i \bar{f}_j$ relieved in radiative decay!

Roman Zwicky@ Tenerife

$B_s \rightarrow \mu^+ \mu^- \gamma$ at large q^2 from lattice QCD

Giuseppe Gagliardi, INFN Sezione di Roma Tre

In collaboration with:

R. Frezzotti, V. Lubicz, G. Martinelli, C.T. Sachrajda,
F. Sanfilippo, S. Simula, N. Tantalo

[pre-print: arXiv:2402.03262]

Why $B_s \rightarrow \mu^+ \mu^- \gamma$ at large q^2 ?

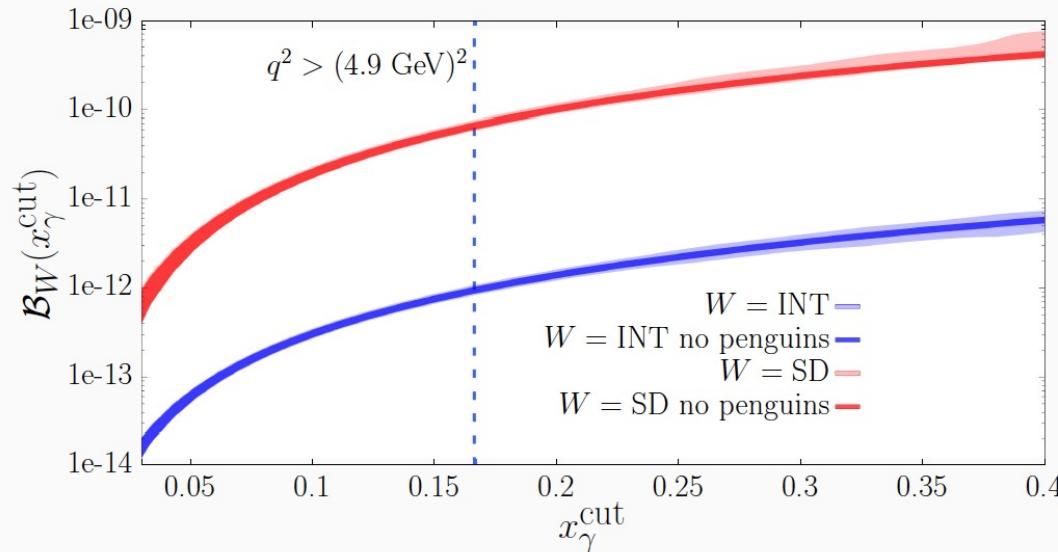
- The $B_s \rightarrow \mu^+ \mu^- \gamma$ decay allows for a new test of the SM predictions in $b \rightarrow s$ FCNC transitions.
- Despite the $\mathcal{O}(\alpha_{\text{em}})$ -suppression w.r.t. the widely studied $B_s \rightarrow \mu^+ \mu^-$, removal of **helicity-suppression** makes the two decay rates comparable in magnitude.
- At very high $\sqrt{q^2}$ = **invariant mass of the $\mu^+ \mu^-$** , the contributions from penguin operators appearing in the weak effective-theory, which are difficult to compute on the lattice, are suppressed [Guadagnoli, Reboud, Zwicky, JHEP '17] ✓.

In this talk I will present the first, (\simeq) first-principles lattice QCD calculation of the $B_s \rightarrow \mu^+ \mu^- \gamma$ decay rate for $q^2 \gtrsim (4.2 \text{ GeV})^2$.

The branching fractions

$$\mathcal{B}(x_\gamma^{\text{cut}}) = \int_0^{x_\gamma^{\text{cut}}} dx_\gamma \frac{d\mathcal{B}}{dx_\gamma} \quad x_\gamma^{\text{cut}} \equiv 1 - \frac{q_{\text{cut}}^2}{m_{B_s}^2}$$

- $E_\gamma^{\text{cut}} = x_\gamma^{\text{cut}} m_{B_s}/2$ is the **upper-bound** on the measured photon energy.

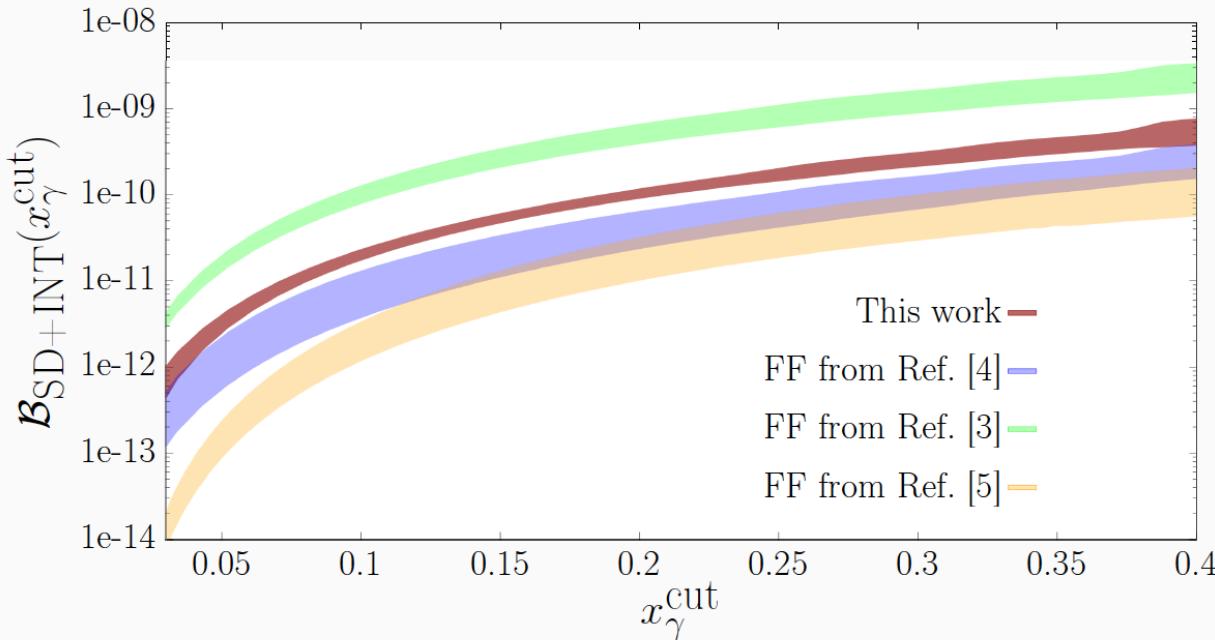


- SD contribution dominated by **vector form factor F_V** . Tensor form-factor contributions suppressed by small Wilson coefficient $C_7 \ll C_9, C_{10}$.
- At $x_\gamma^{\text{cut}} \sim 0.4$ our estimate of charming-penguins uncertainties is **around 30%** [previous works quoted few percent uncertainties].

Comparison with current LHCb upper-bound for $x_\gamma^{\text{cut}} \sim 0.166$.

$$\mathcal{B}_{\text{SD}}^{\text{LHCb}}(0.166) < 2 \times 10^{-9}, \quad \mathcal{B}_{\text{SD}}(0.166) = 6.9(9) \times 10^{-11} \quad [\text{This work}]$$

Comparison with previous works



- Ref. [3] = Janowski, Pullin , Zwicky , JHEP '21 , light-cone sum rules.
- Ref. [4] = Kozachuk, Melikhov, Nikitin , PRD '18 , relativistic dispersion relations.
- Ref. [5] = Guadagnoli, Normand, Simula, Vittorio, JHEP '23, VMD/Lattice.

Differences with earlier estimates can be traced back to the fact that our determination of F_V (which gives the dominant contribution to the branching) is larger (smaller) than the one of Refs. [4-5] (Ref. [3]) by a factor of about 1.5 - 2.

Conclusions

- We have presented a first-principles lattice calculation of the form factors F_V, F_A, F_{TV}, F_{TA} entering the $\bar{B}_s \rightarrow \mu^+ \mu^- \gamma$ decay, in the **electroquenched approximation**.
- Systematic errors have been controlled thanks to the use of gauge configurations produced by the **ETM Collaboration**, which correspond to four values of the lattice spacing $a \in [0.057 : 0.09]$ fm, and through the use of five different heavy-strange masses $m_{H_s} \in [m_{D_s} : 2m_{D_s}]$.
- Presently our result for the branching fractions have uncertainties ranging from $\sim 15\%$ at $\sqrt{q_{\text{cut}}^2} = 4.9$ GeV to $\sim 30\%$ at $\sqrt{q_{\text{cut}}^2} = 4.2$ GeV.
- At small q_{cut}^2 uncertainty dominated by the charming-penguins which we included using a phenomenological parameterization.

Outlook:

- Evaluate electro-unquenching effects.
- Evaluate charming-penguins contributions from first-principles.
- Simulate on finer lattice spacings to be able to reach higher m_{H_s} and reduce the impact of the mass-extrapolation.