



UNIVERSITÀ  
DI TRENTO



# Waveform consistency tests with cWB-2G

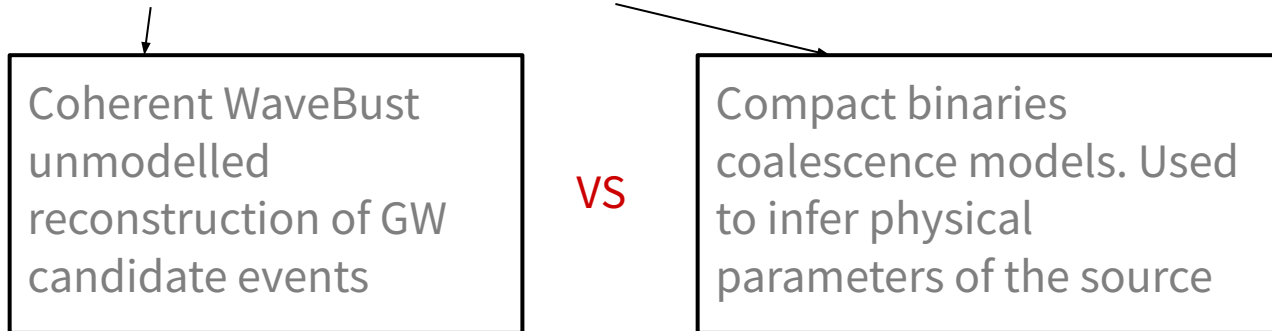
Trieste, 15 may 2024  
Sophie

# Outline

- waveform consistency test
  - O4a preliminary results
  - Three detectors network
- 
- Back-up slides: systematic error from previous run

# Waveform consistency test - goal

- Unmodeled searches can identify discrepancies between measured data and theoretical models



- Discrepancies might be due to noise artifacts, the influence of unknown binary parameters, missing physics in the waveform models, or deviations from General Relativity.

# Waveform consistency tests - method

This test computes:

1. The match between the waveform of the event reconstructed by cWB and the maximum likelihood CBC-PE waveform.

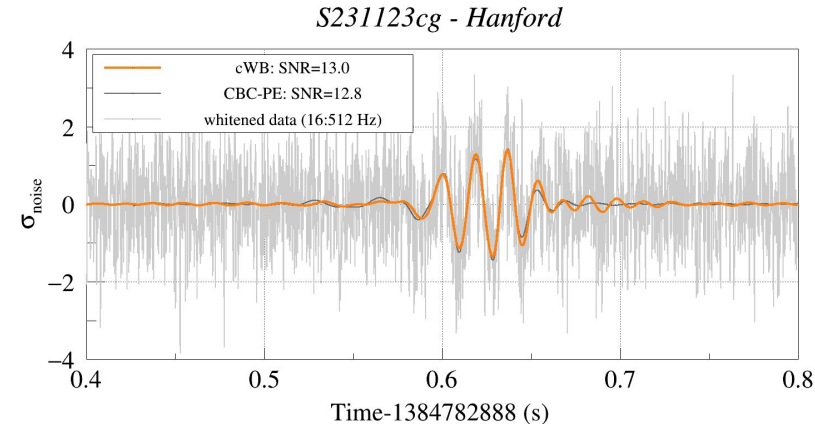
$$\text{Match}(x_{rec}(t), x_{inj}(t)) = \frac{(x_{rec}|x_{inj})}{\sqrt{(x_{rec}|x_{rec})}\sqrt{(x_{inj}|x_{inj})}}$$

$$(x_{rec}|x_{inj}) = \sum_i^{IFOs} \int_{t_{a,i}}^{t_{b,i}} x_{rec,i}(t)x_{inj,i}(t)dt$$

**Match in [0,1]**

whitened waveforms

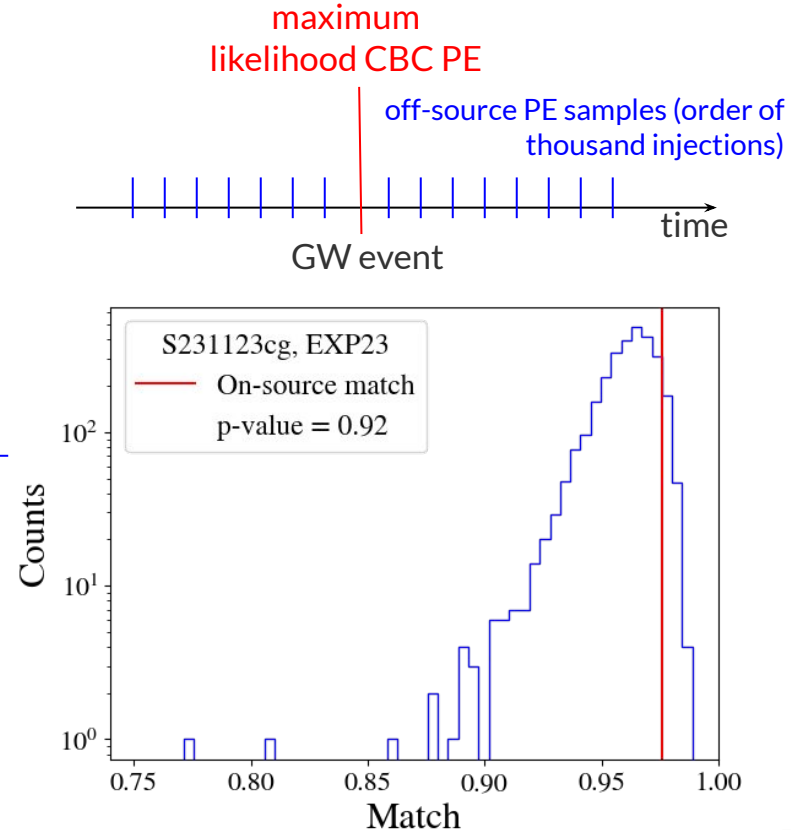
\*CBC-PE : parameter estimates inferred using compact binary coalescence models



# Waveform consistency tests - method

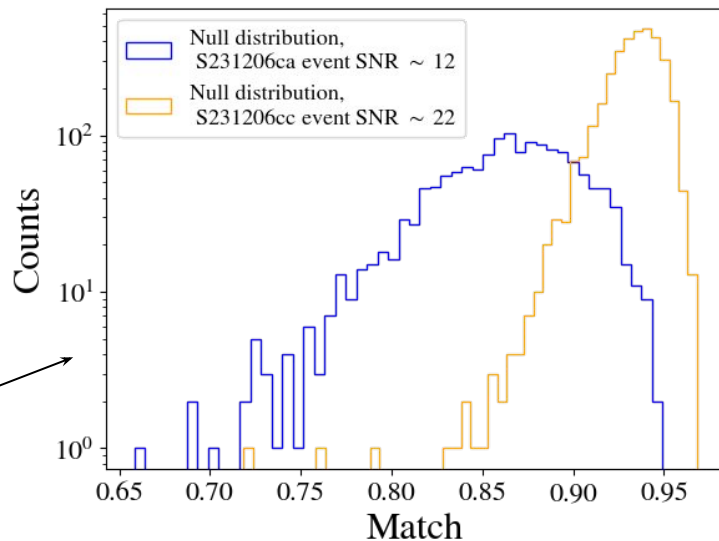
This test computes:

1. The match between the waveform of the event reconstructed by cWB and the maximum likelihood CBC-PE waveform.
2. The match distribution between injected CBC-PE samples and their cWB reconstruction.
3. p-value that quantifies if the discrepancy between the cWB waveform event and CBC-PE (point 1) is significant against the null hypothesis (point 2).



# Waveform consistency tests - match vs SNR

- This procedure accounts both for detector noise, the uncertainty of cWB reconstruction, and the PE variability.
- The lower the SNR of the event under investigation the broader the null distribution



Null-distributions for **S231206ca** and **S231206cc**. Similar chirp mass (40.6 vs 36), but different SNR.

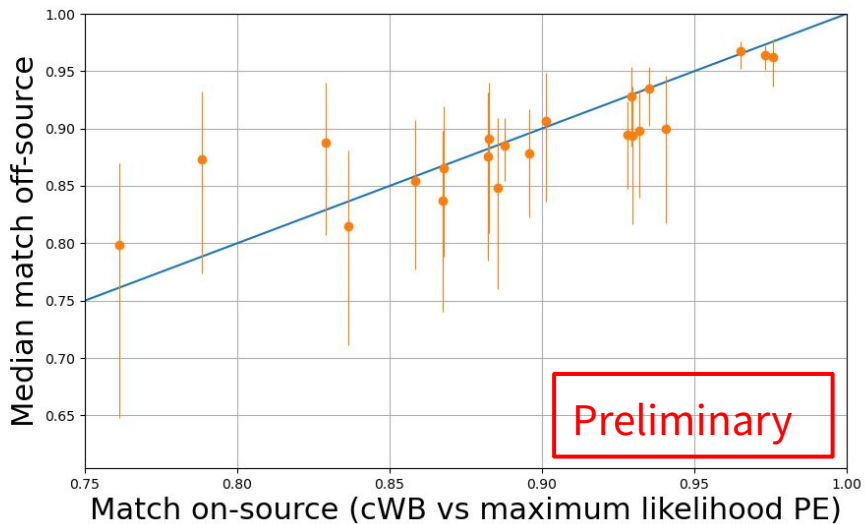
# Follow-up of O4a GW events

- follow-up of interesting events [wiki](#)
- preliminary p-values distribution on a subset of GW events

Recent presentations to burst group: DCC [G2302408](#), [G2302304](#), [G2301377](#))

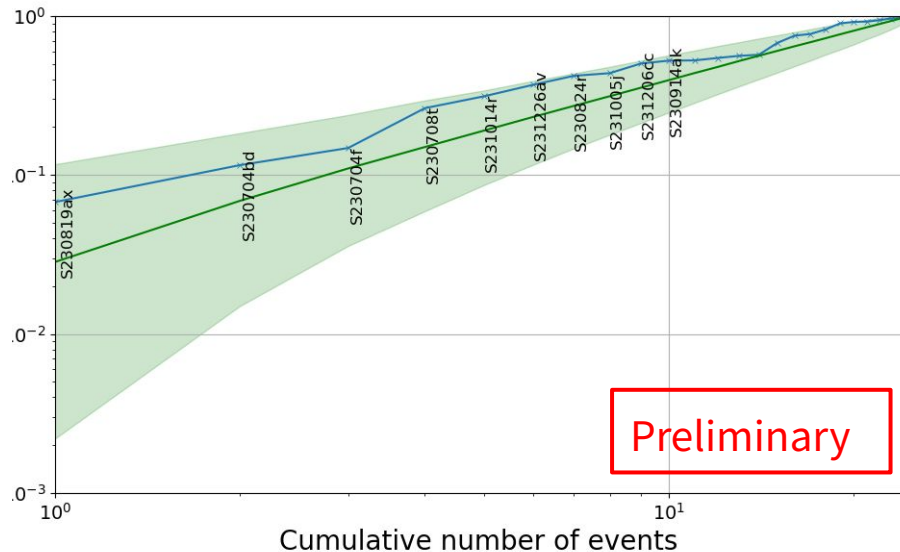
# O4a events

Plots as in GWTC-3



Off-source versus on-source match values. The blue line indicates the null hypothesis, and the error bars indicate the symmetric 90% confidence interval.

**No significant deviations**



Distribution of p-values, and symmetric 90% interval about the median (green). **No significant deviations**



# O4a events

Some open questions:

1. which GW events should be analysed? (O4a has about 80 candidate events. Should we apply a threshold in SNR? threshold in the variability of the off-source distribution? only 'interesting' events?)
2. do we have a systematic error (p-value often higher than expected)?
3. O4a catalog will have a different structure: likely this analysis will not be included there

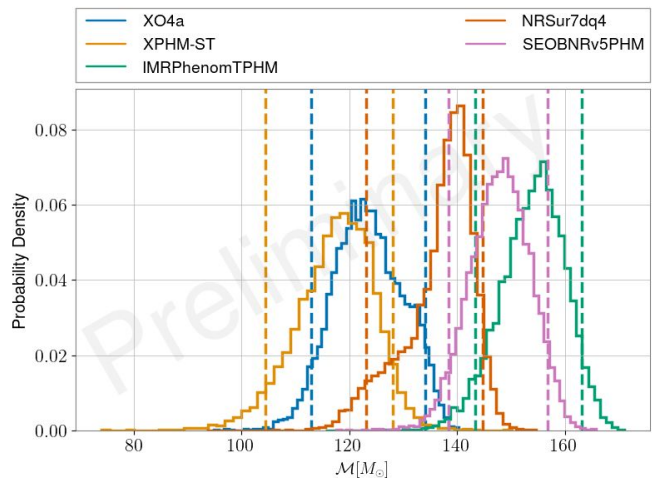
# Interesting event - S231123cg

study science case team started two weeks ago [git](#). scope: decide if this candidate event deserves a dedicated paper and understand the results of various analyses.

Brief summary:

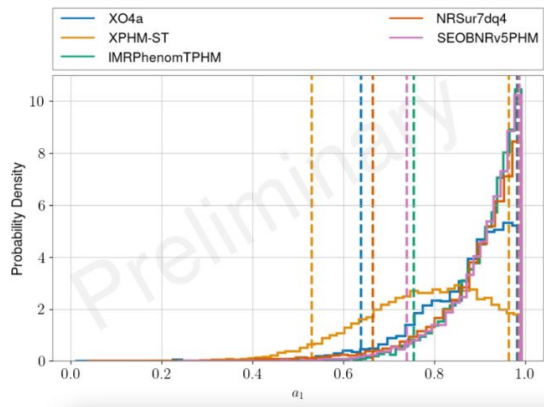
- **detection** : cWB 2G all-sky IFAR>490 years (saturated background [link](#)), cWB XP all-sky [link](#)  
IFAR = 481.8 yr , XP BBH IFAR >= 4581.1 year [link](#)
- **data quality** : no concern for detection, glitch [6,4]s before in H1 before than has been subtracted by BayesWave for PE [link](#)
- **parameter estimation: high mass, high spin**, inconsistencies between different waveform models (not solved) LVK [slides](#)
- **ringdown**: debate if there is evidence for multiple modes

# Interesting event - S231123cg

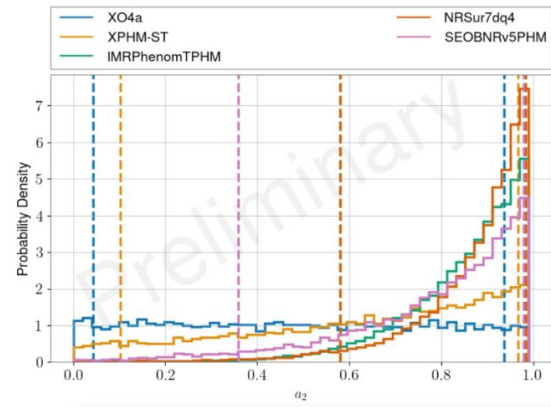


Detector frame total mass differs across approximants.

from [dcc](#)

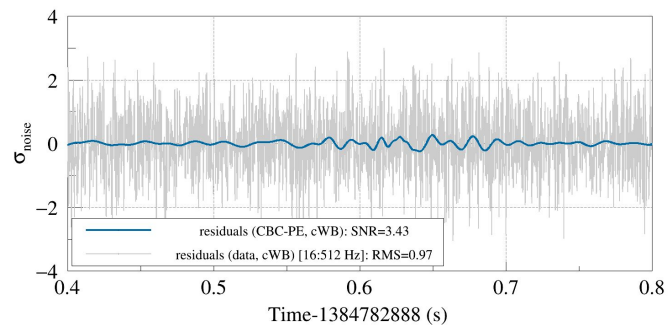
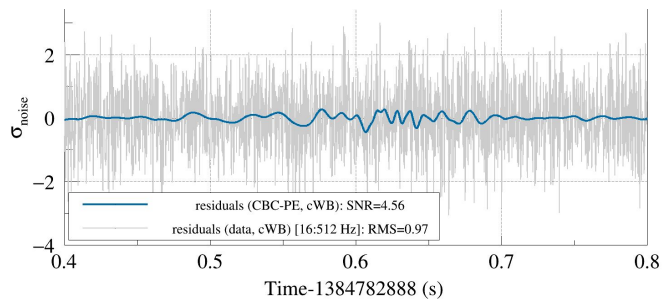
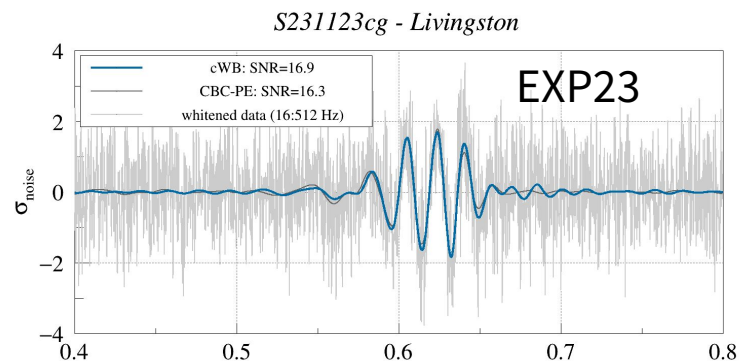
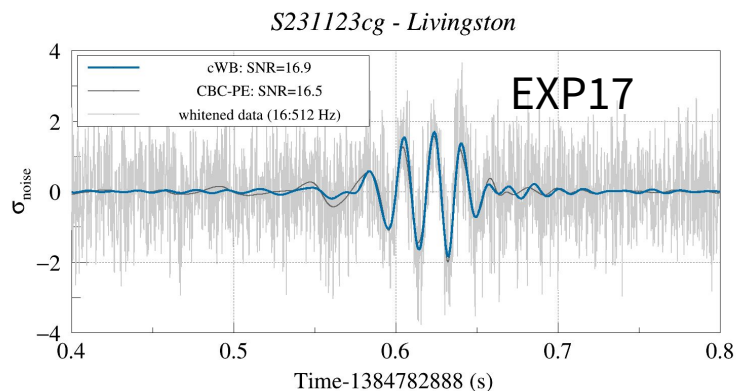


High individual spins preferred by most models. We see some differences in the measurements with the FD models



# S231123cg - waveform consistency

- Several PE runs, **no** significant discrepancy found with latest PE using different waveform models (IMRPhenomXPHM EXP23, NRSur7dq4 EXP17) [wiki](#)



# S231123cg

can we provide more info / strength to the detection?

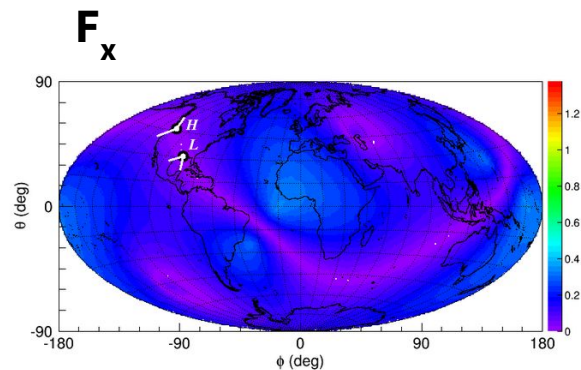
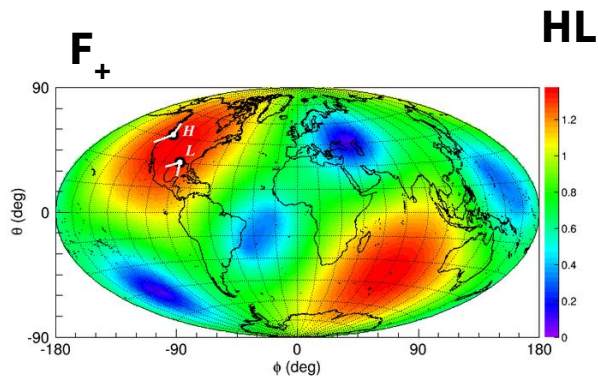
- 1) increase background?
- 2) morphological comparison with loudest background triggers? (now only by eyes)
- 3) to be done: comparison with final PE

# Waveform consistency

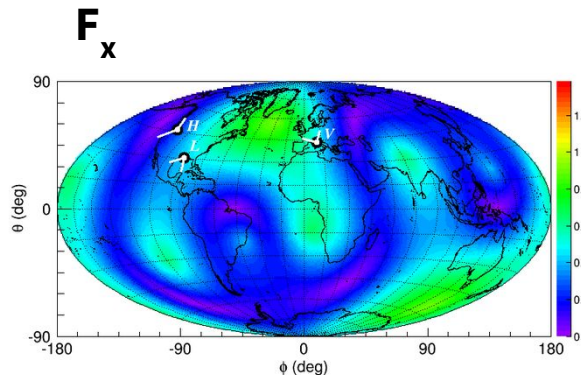
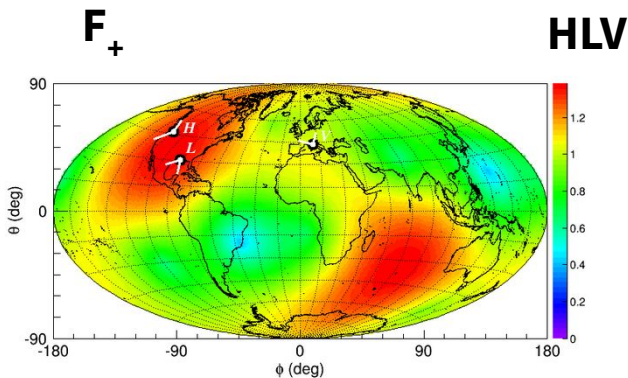
three detectors network (LIGO+Virgo)

# HL and HLV antenna patterns

LIGO detectors are coaligned, and so they (almost) sense only one GW polarization ( $F_+$ )



The addition of Virgo improves the sky coverage and the response to the second polarization ( $F_x$ )



# Three detectors network

cWB uses likelihood regulators to reject the reconstruction of the GW component NOT observed by the LIGO aligned detectors ( $F_x$ ). These regulators successfully reduce the false alarm rate of the HL coherent analysis.

To make full use of a third, not-aligned detectors, the likelihood regulators should be released.

In GWTC3 we report the waveform consistency test using HL network,

**does the waveform reconstruction improve using HLV network?**



# Waveform consistency HL vs HLV

Two examples:

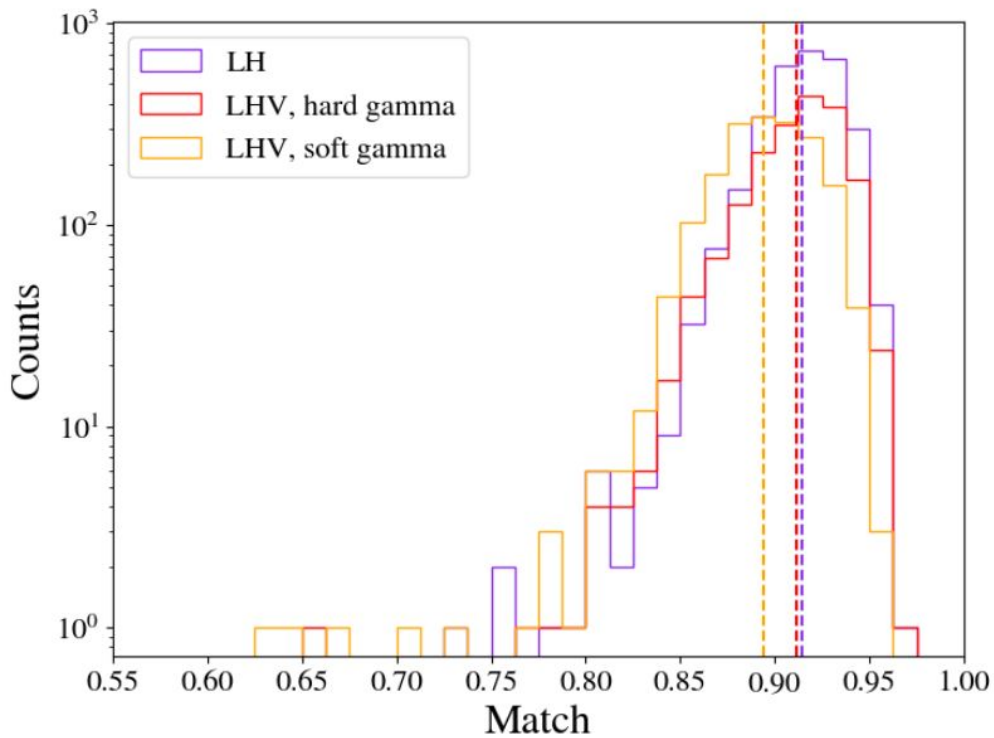
- **GW200224ca** (vanilla BBH,  $m_1 = 40$   $m_2 = 32$ , cWB SNR=20)
- **GW200311bg** (vanilla BBH,  $m_1 = 34$ ,  $m_2 = 27$ , cWB SNR=17)(in GWTC3 catalog 200311\_115853)

To evaluate cWB goodness of reconstruction, we inject the PE samples of these two BBH events off-source, and we compute the match between the injected waveforms and cWB reconstructions

# GW200224ca

off-source match distribution (as a measure of the goodness of the waveform reconstruction)

- LH: highest match mean
- LHV hard regulator: similar matches as LH
- LHV soft regulator: lower mean and has some very low matches ( $<0.75$ )

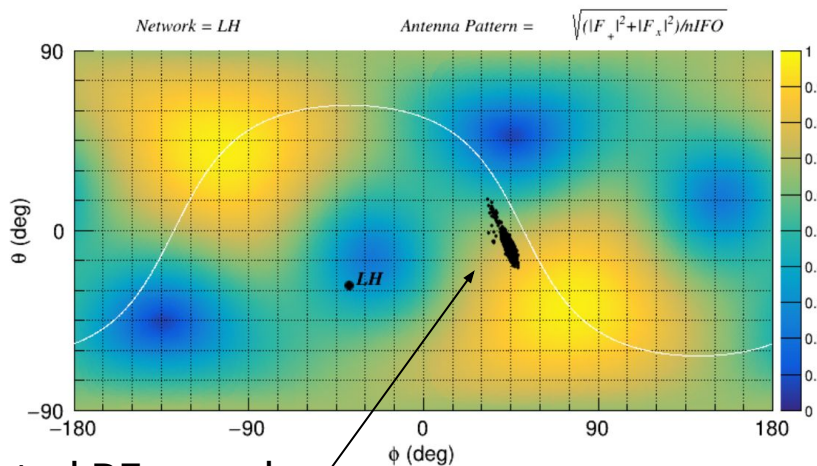


# GW200224ca - HL

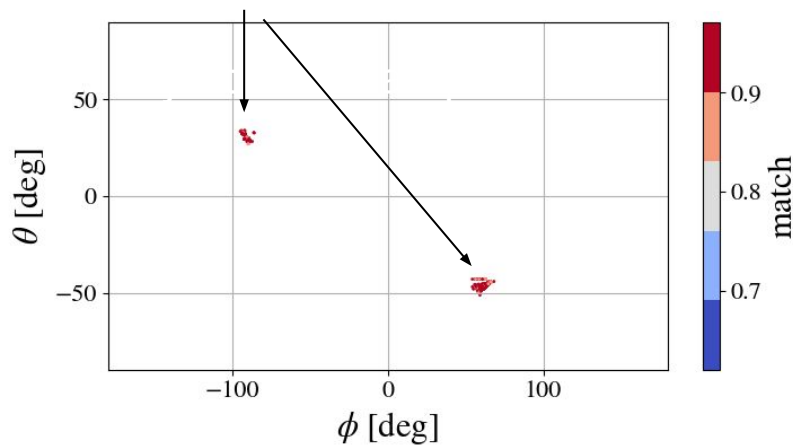
cWB SNR = 20 (sSNR L1 13.4, H1 13.4),

LH waveform consistency match on-source = 0.93, off-source  $0.917^{+0.026}_{-0.040}$

ced [link](#), LH off-source [report](#)



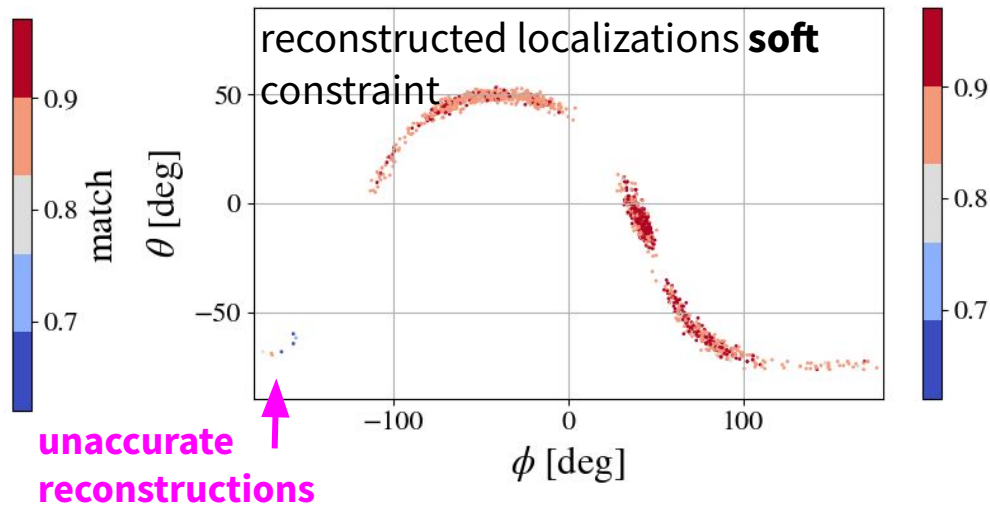
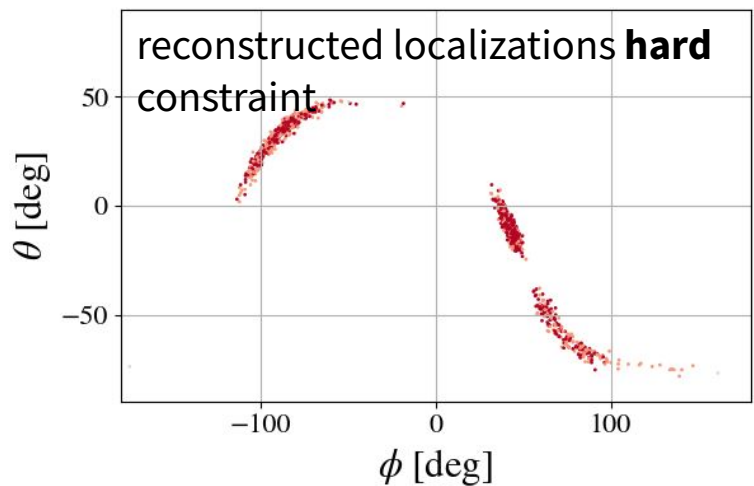
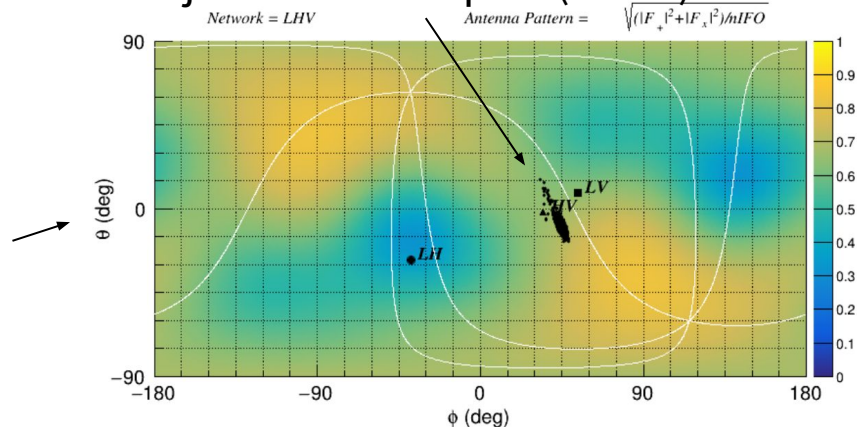
reconstructed localizations



# GW200224ca - HLV

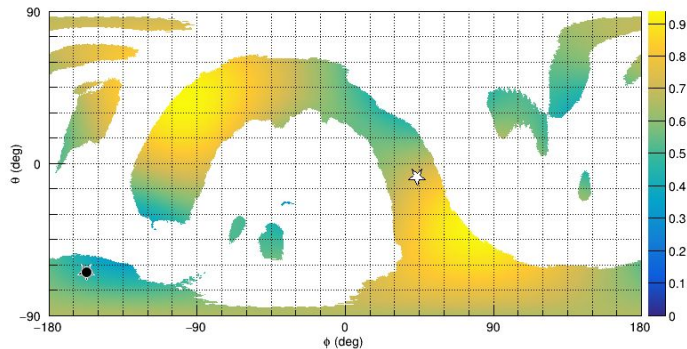
- more uniform antenna pattern
- HLV hard  $0.915^{+0.028}_{-0.051}$ , [link](#)
- HLV soft  $0.896^{+0.036}_{-0.044}$  [link](#)
- sSNR in Virgo .1 with hard, 7.7 with soft

injected PE samples (as HL)

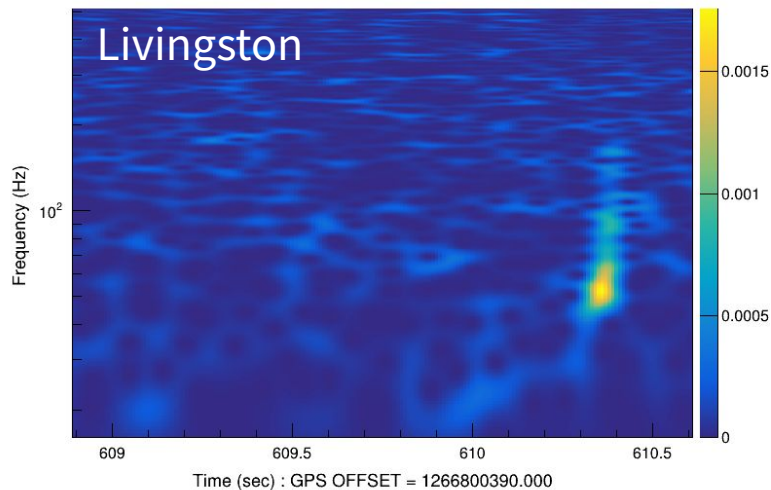


# GW200224ca - HLV lowest match

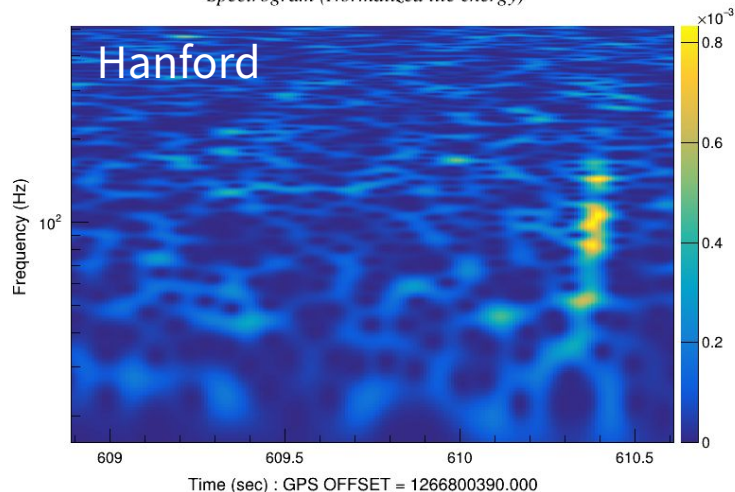
Spectrogram of the worst match using soft regulator. There is a low frequency glitch in Virgo [ced](#).



*Spectrogram (Normalized tile energy)*



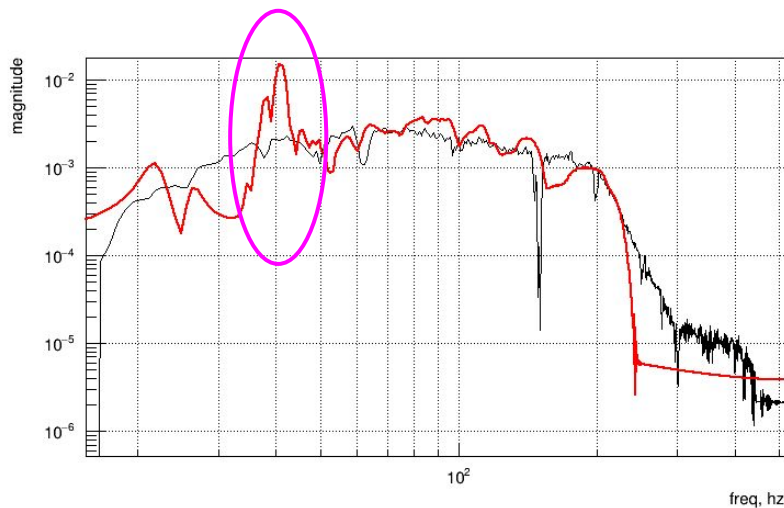
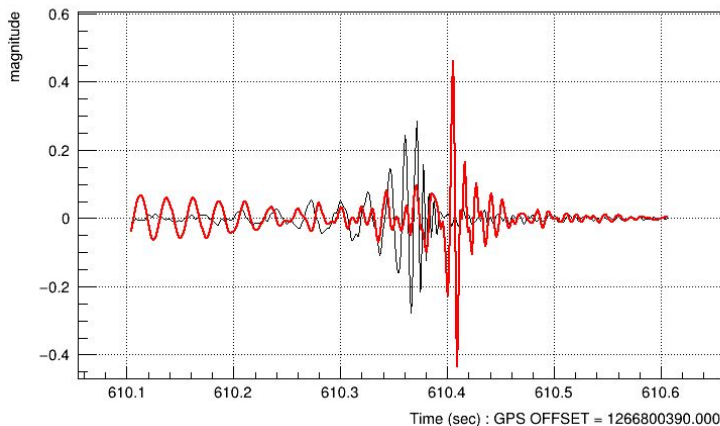
*Spectrogram (Normalized tile energy)*



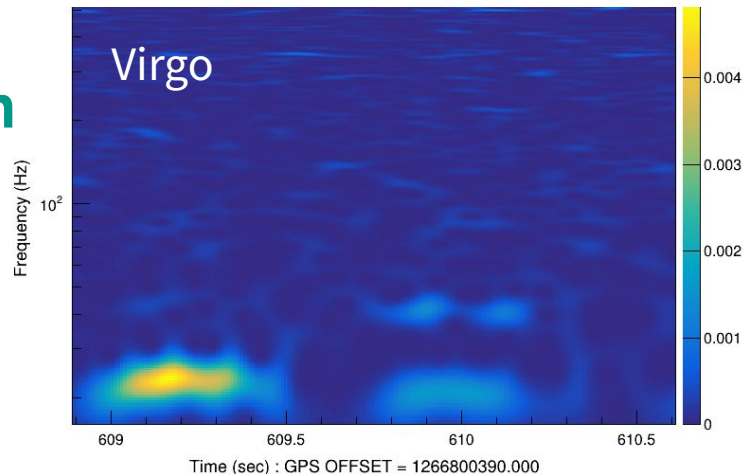
# GW200224ca - HLV lowest match

Spectrogram of the worst match using soft regulator. There is a low frequency glitch in Virgo [ced](#)

Virgo reconstruction in time and frequency domain.  
Black:injected, red cWB reconstruction



Spectrogram (Normalized tile energy)



# GW200224ca - HLV lowest match

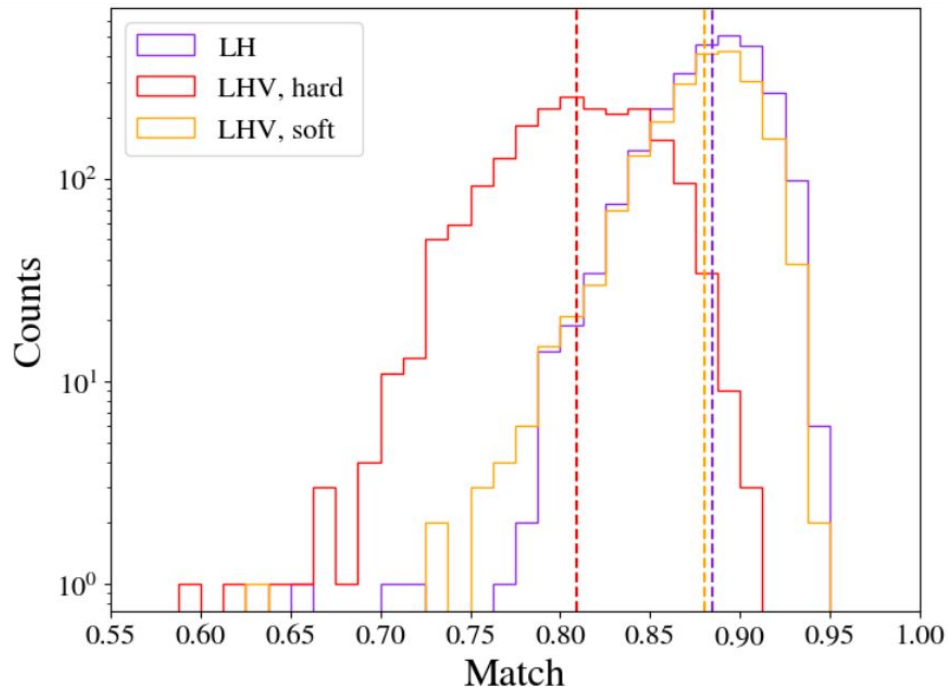
From the study of this event, we found that:

- the distribution of off-source matches does not improve using HLV network (similar or lower mean)
- the HLV network weakens the statistical power of the waveform consistency test giving few very inaccurate waveform reconstructions

# GW200311bg

off-source match distribution (as a measure of the goodness of the waveform reconstruction)

- LH: highest match mean
- LHV hard regulator: worst matches
- LHV soft regulator: slightly worse than HL, better than hard regulator



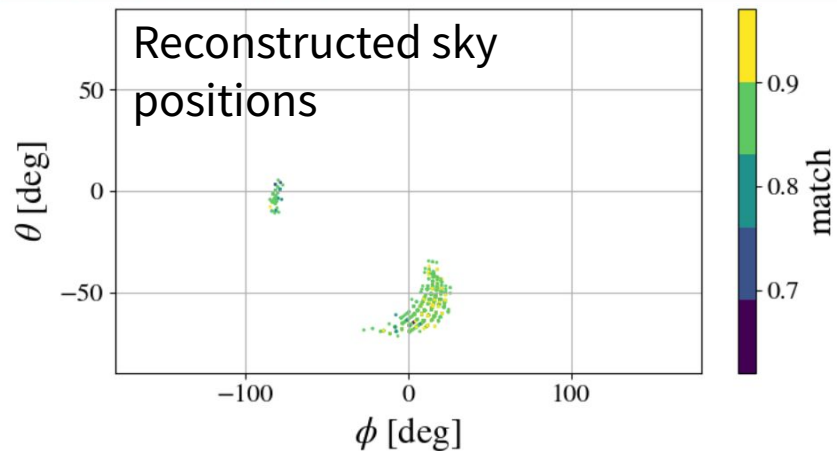
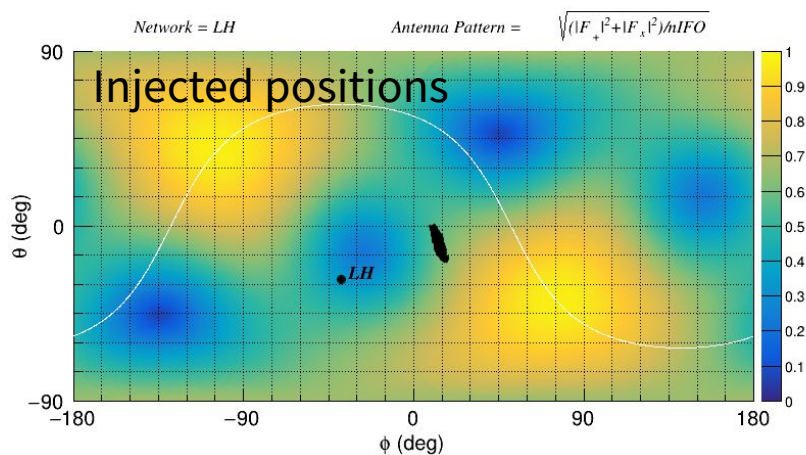


# GW200311bg - LH network

cWB SNR = 17 (L1 10.7, H1 12),

off-source =  $0.888^{+0.035}_{-0.052}$

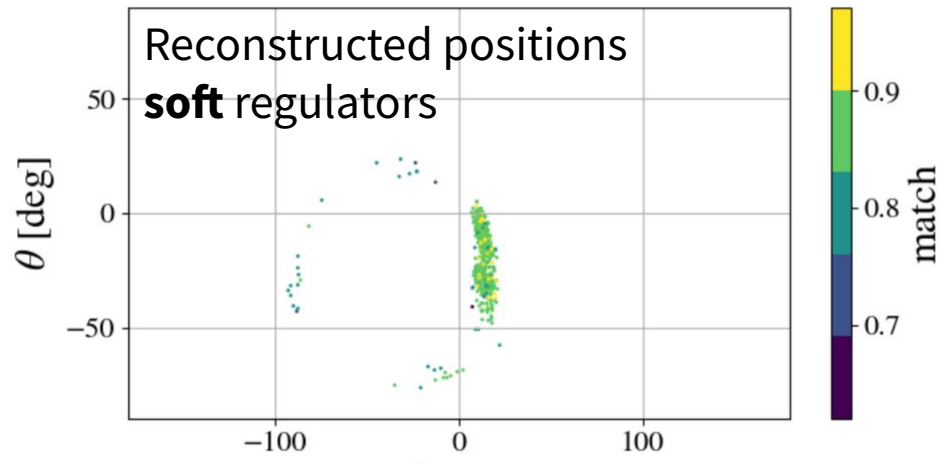
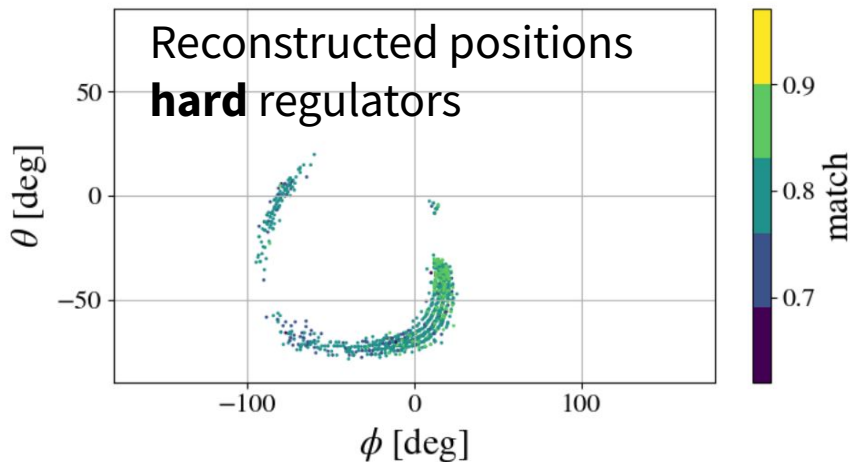
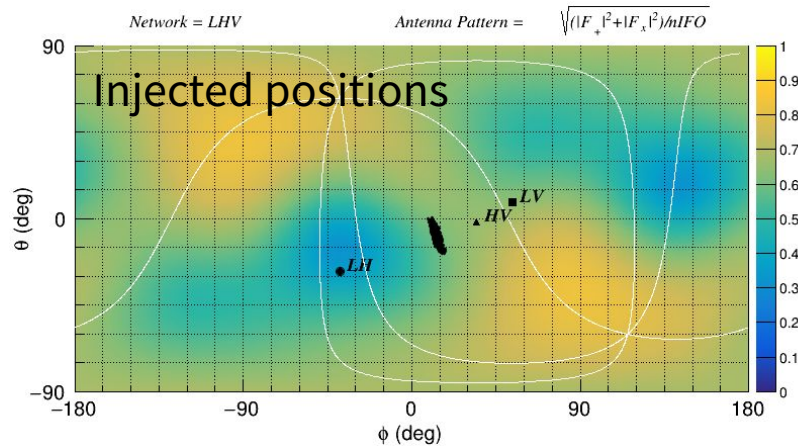
ced [link](#) , off-source [report](#)



# GW200311bg - HLV network

off source matches:

- hard:  $0.811^{+0.056}_{-0.07}$
- soft:  $0.884^{+0.034}_{-0.054}$



# Conclusions

- Three detectors network: we study two GW events from O3. we found that the HLV network does not improve the statistical power of waveform consistency test.
- cWB-2G is performing the waveform consistency test on O4a events. No significant discrepancy between cWB reconstructed waveform and PE samples has been observed. There are open questions.
- S231123cg: could we provide more in depth analyses?

**Thanks!**

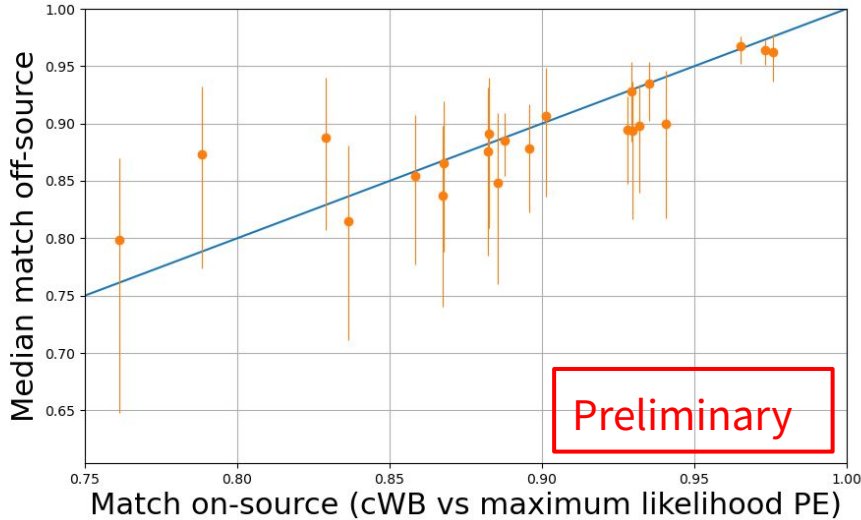
# Extra slides

# Waveform consistency test

## Systematic error

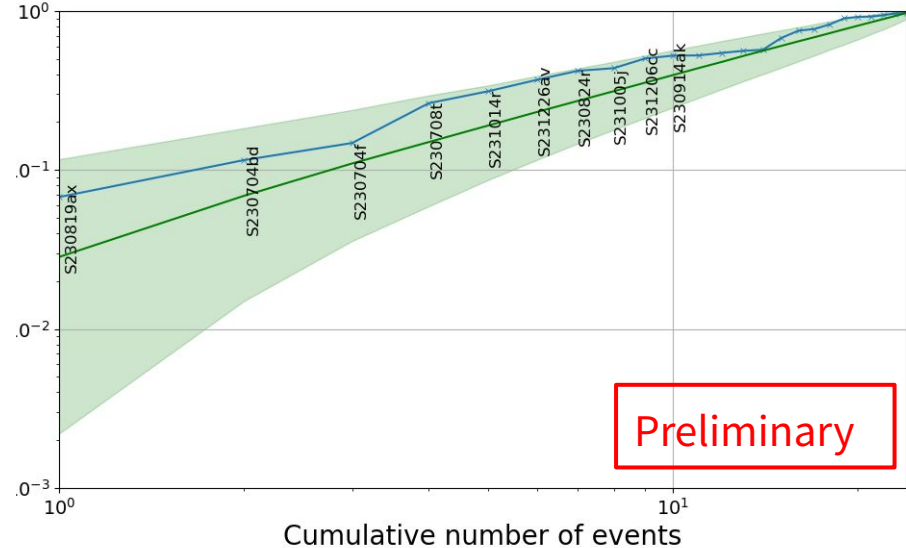
# (preliminary) set of O4a events

Plots as in GWTC-3



Off-source versus on-source match values. The blue line indicates the null hypothesis, and the error bars indicate the symmetric 90% confidence interval.

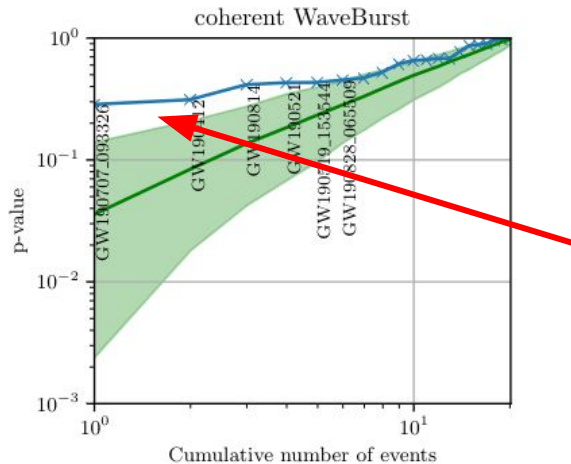
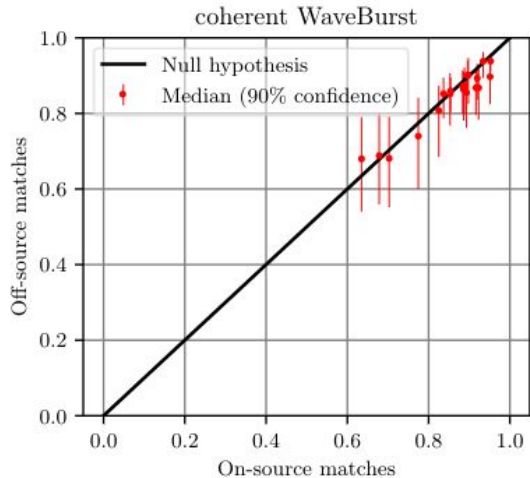
**No significant deviations**



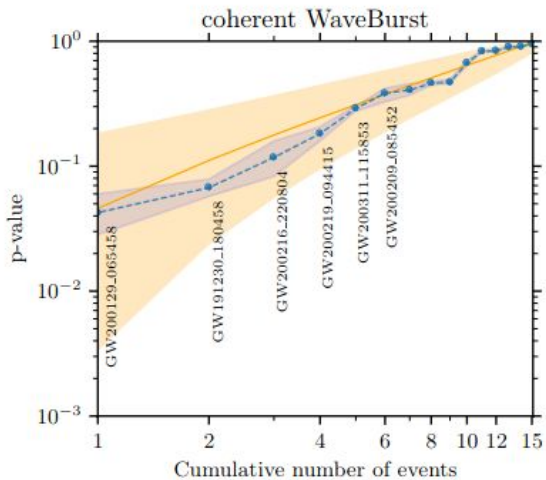
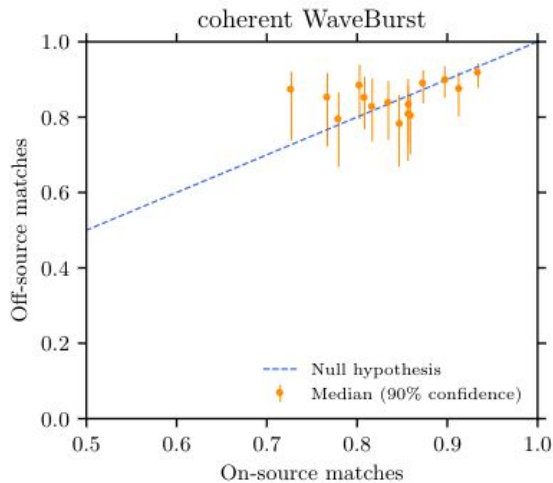
Distribution of p-values, and symmetric 90% interval about the median (green). **No significant deviations**

# From previous runs

GWTC2

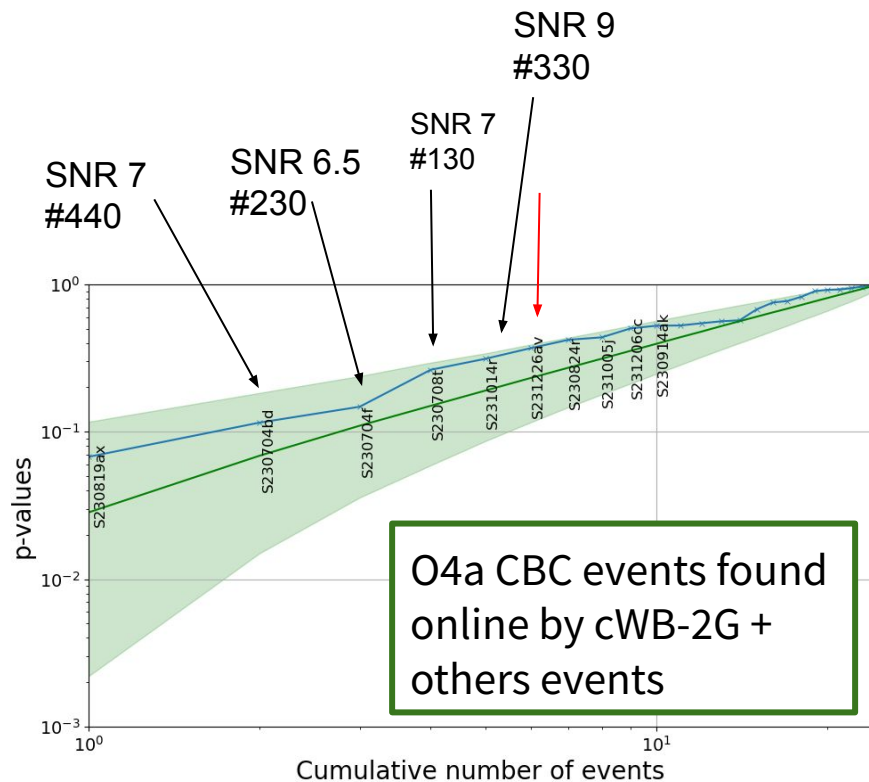
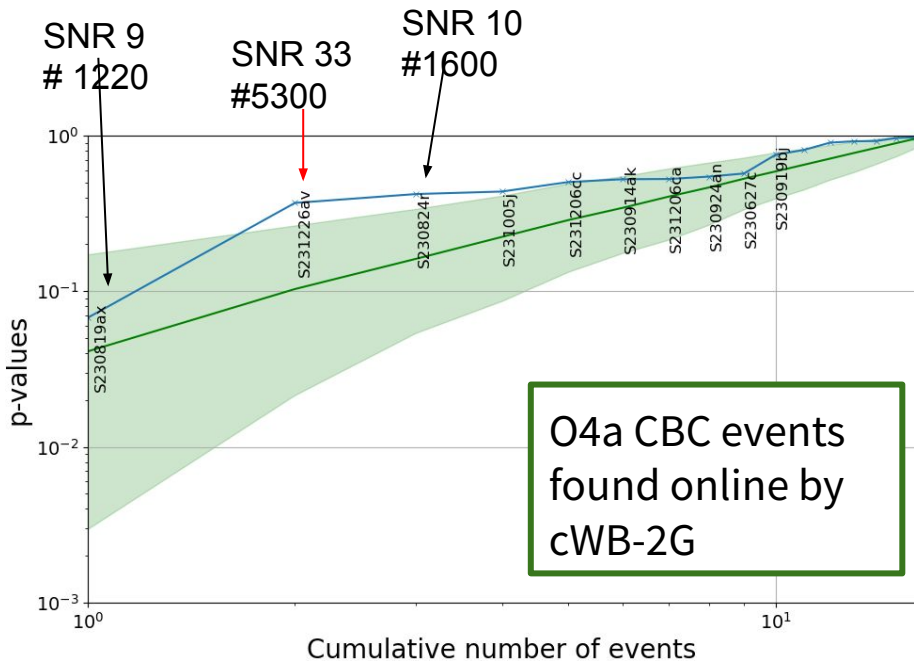


GWTC3





# Systematic error - O4a



- Low-SNR events have a statistical uncertainty > systematic uncertainty
- Adding more low-SNR events, 'hide' our systematic error?

Which events should we analyse? Should we set a threshold on SNR?

# Systematic error

Tests already performed by cWB-2G (no effect on the p-values distributions):

- off-source injections in a smaller/larger data segment
- PSD variability < variability PE samples
- cWB selection thresholds/post-processing

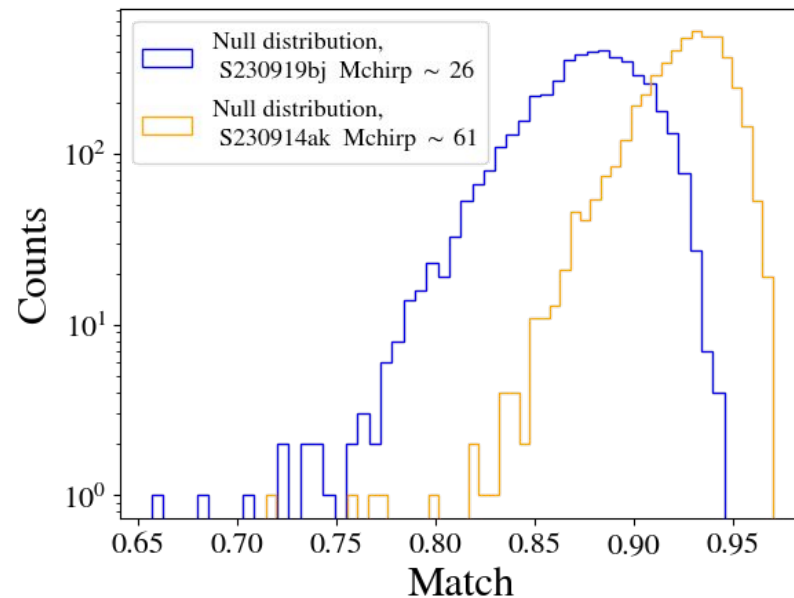
# Systematic error

From Edoardo's presentation([dcc](#)):

- **Problem:** Since the p-values tend to be larger than expected for the null hypothesis, this seems to indicate that our null-hypothesis histogram is too wide, i.e., we are overestimating the variance of the null hypothesis.
- **Possible cause:** the on-source and off-source experiments are not the same. We implicitly assume that the samples in the PE distribution are all very similar, and it is a computationally economical replacement for the ideal procedure, where we should produce a new maximum-likelihood estimate for each injection.

# Waveform consistency tests - match vs chirp mass

- Comparison between null distributions for two events with similar SNR, but different chirp masses

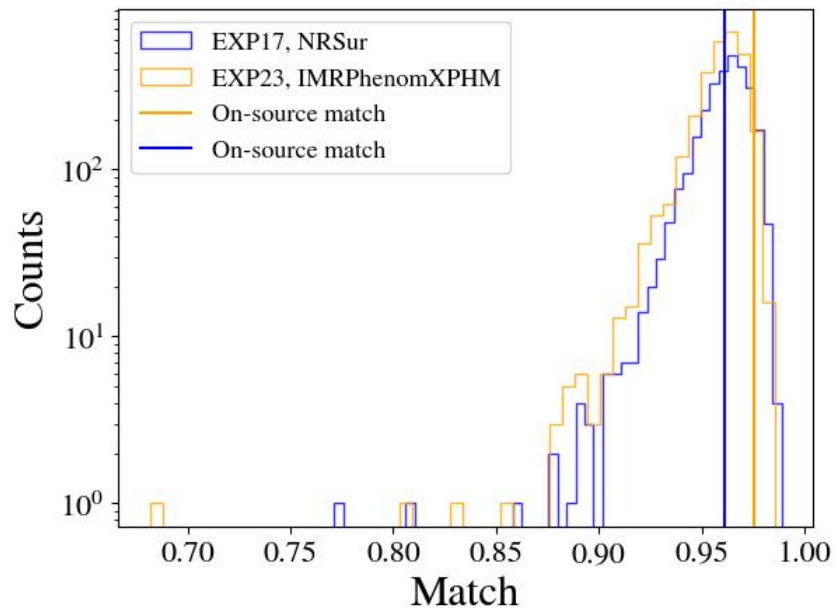


Null-distribution for [S230919bj](#) and [S230914ak](#). Similar SNR (17 vs 16.9), but different chirp mass.

# S231123cg - waveform consistency

Several PE runs, **no** significant discrepancy found with latest PE using different waveform models (IMRPhenomXPHM, NRSur7dq4)

- EXP17 (NRSur7dq4): match 0.9611, p-value = 0.51
- EXP23 (IMRPhenomXPHM): match 0.976, p-value = 0.92



On-source match (vertical line) and null-distribution considering PE samples obtained with two different waveforms

# comparison injected directions between two events

