

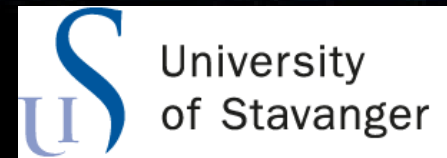
Gravitational Waves – Future Colliders

LFC24

SISSA, Sept. '24



**Germano
Nardini**

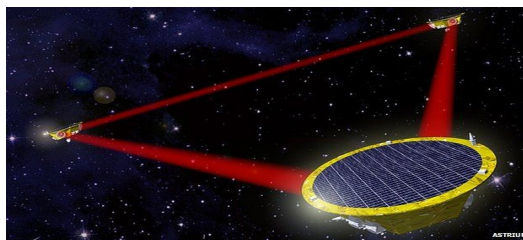
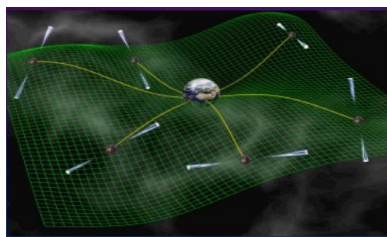
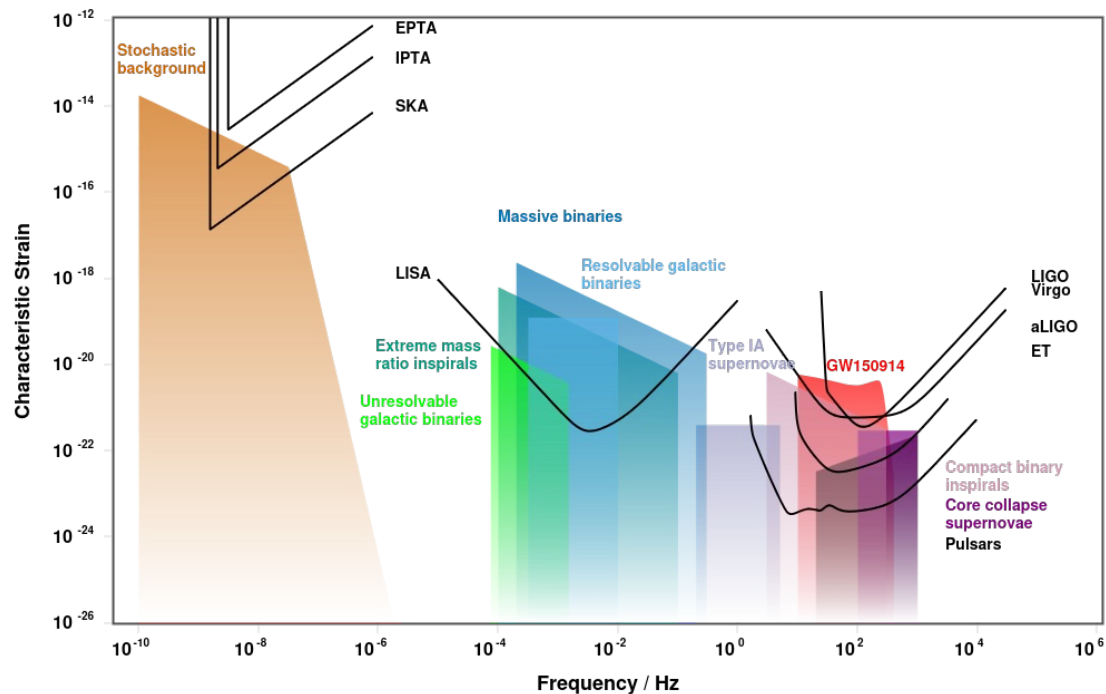


Gravitational Waves Detectors

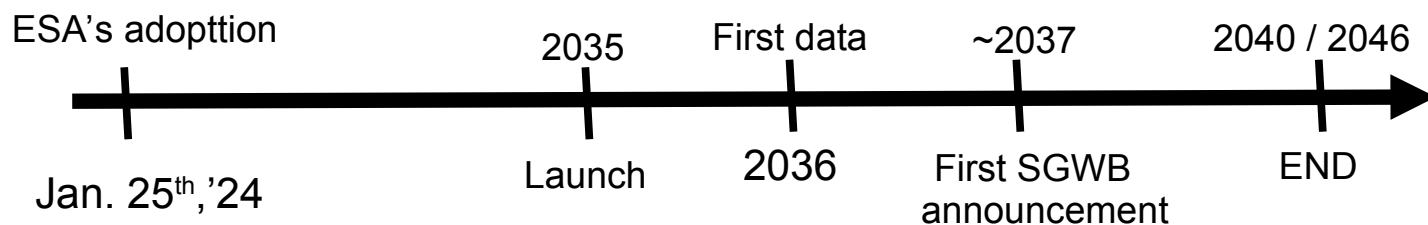
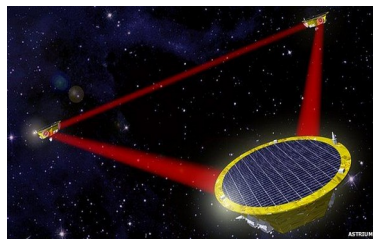
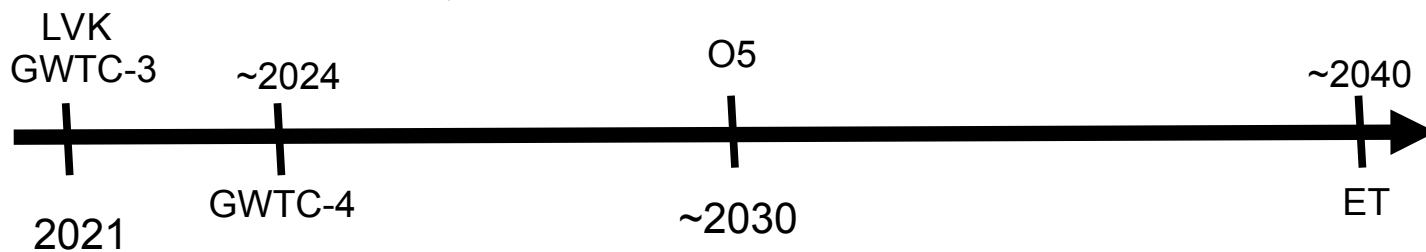
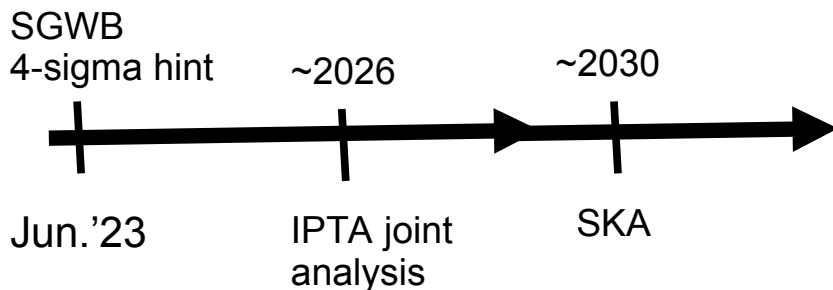
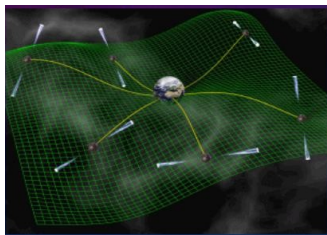
Pulsar timing arrays: GWs with 10^{-9} – 10^{-6} Hz

Space-based interferometers: GWs with 10^{-5} – 1 Hz

Ground-based interferometers: GWs with 1 – 10^4 Hz



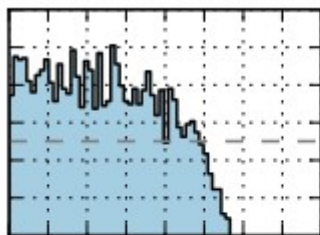
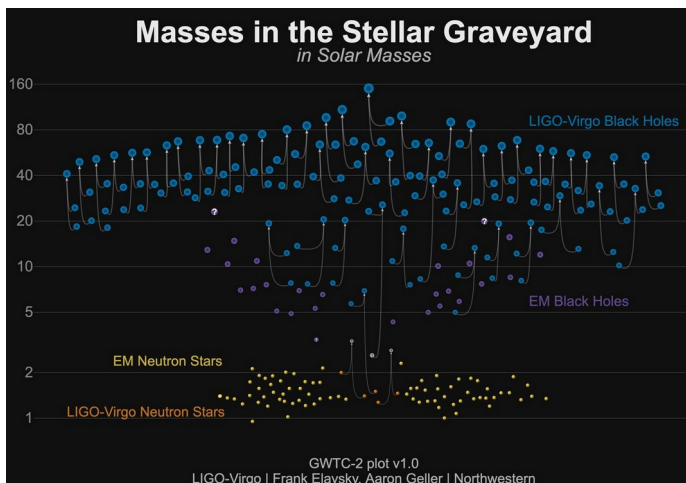
GW experiment and FCC timelines



BSM status at GW experiments (brutally brief and biased)

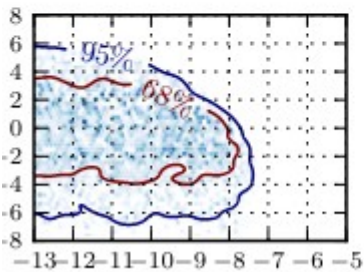


LVK

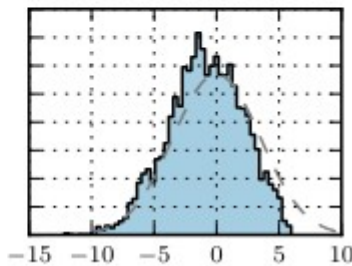


LVK, '21

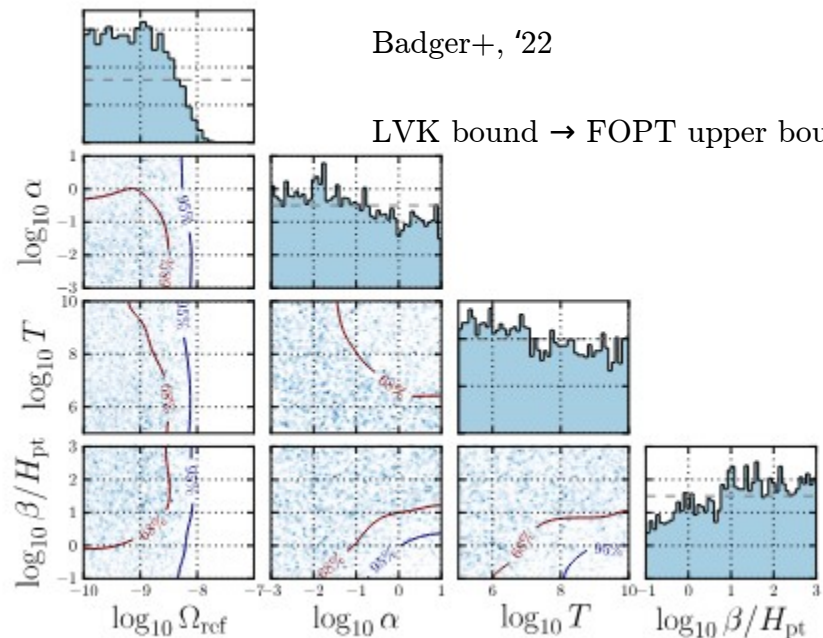
SGWB power-law upper bound



Amplitude



Tilt

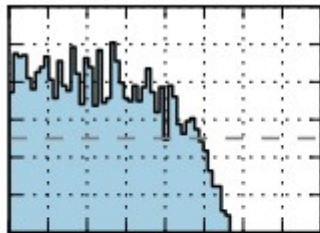


BSM status at GW experiments (brutally brief and biased)



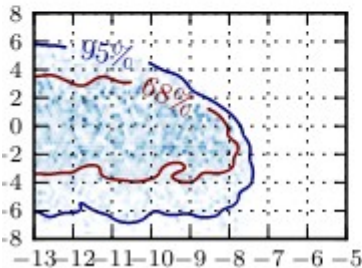
LVK

- Observations compatible with “expected” astronomy
- Recast observations give weak upper bounds on BSM physics at $\sim 10^{6-10}$ GeV
- Likely, no huge progress before ET due to the soonish-emerging binary foreground

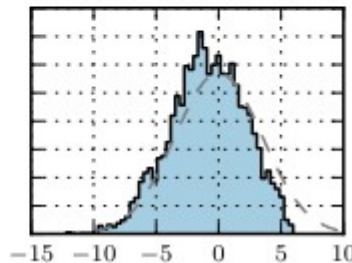


LVK, '21

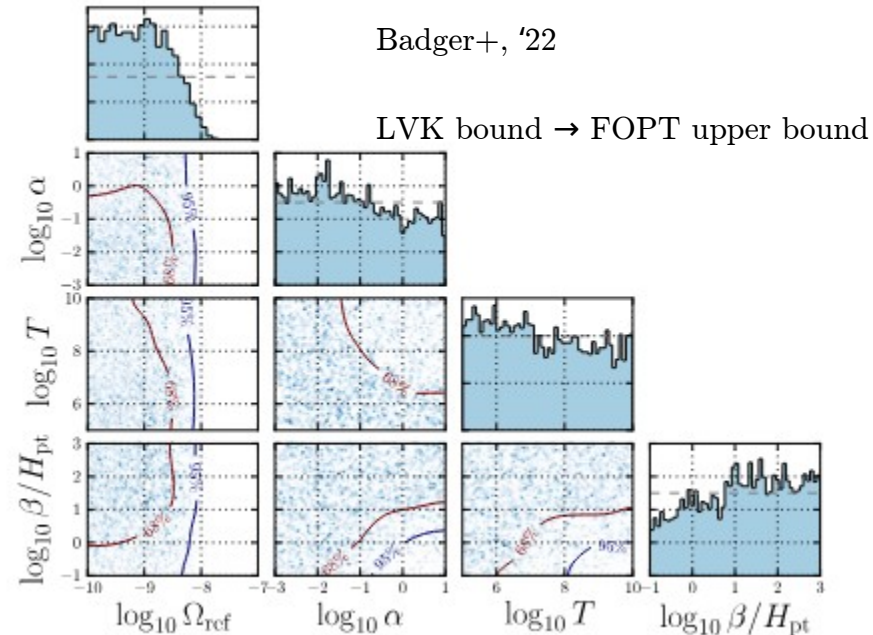
SGWB power-law upper bound



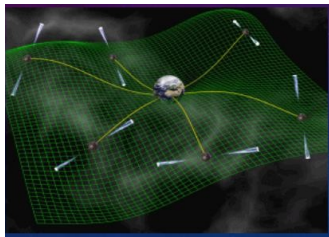
Amplitude



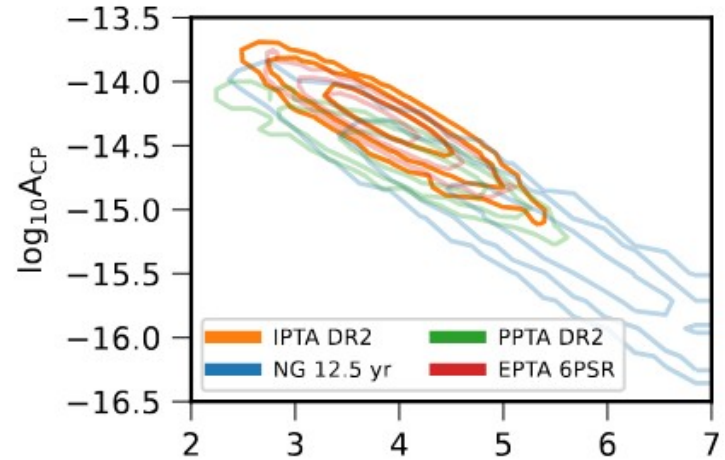
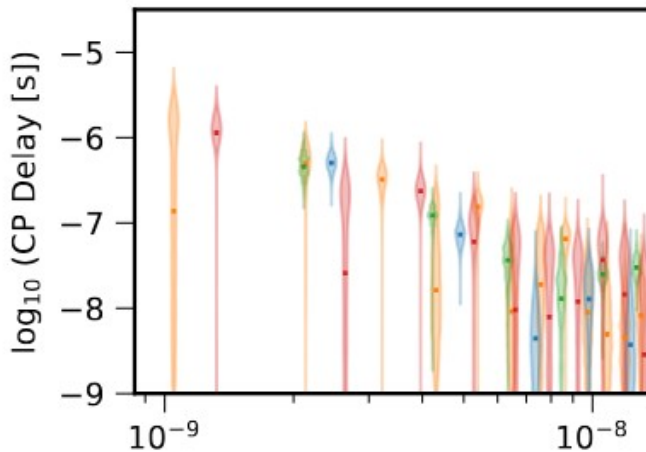
Tilt



BSM status at GW experiments (brutally brief and biased)



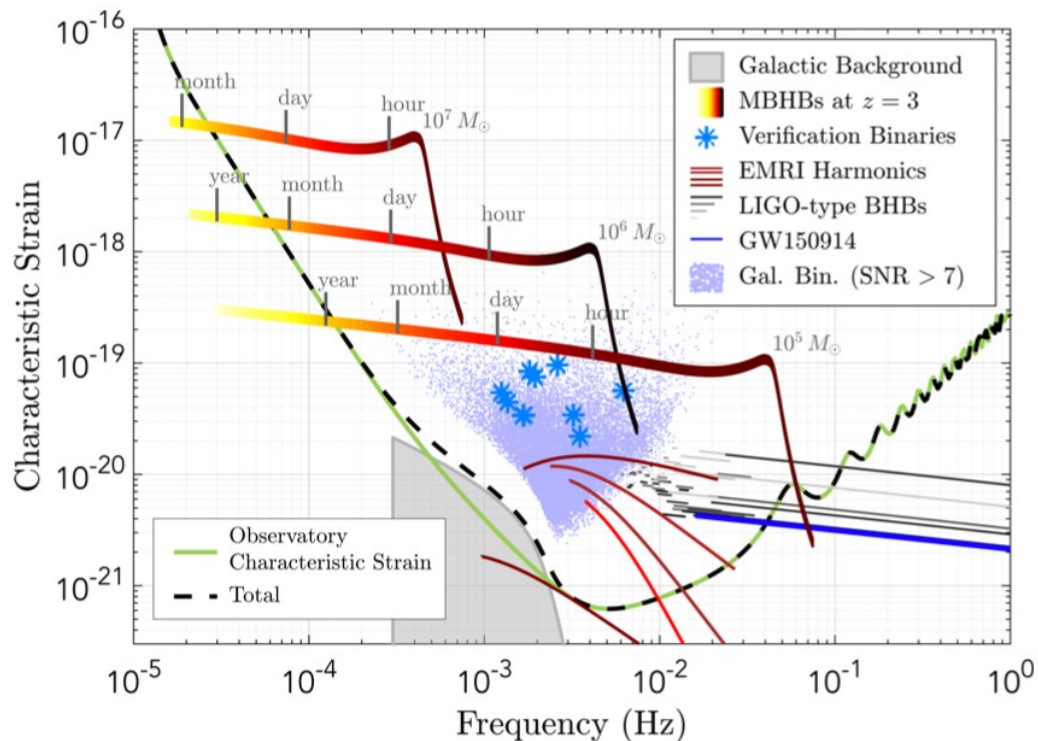
PTA



MAYBE A BSM HINT, MAYBE NOT

- > Compatible with SMBBH-only SGWB
(*non-circular binaries with environmental effects*)
- > A few sub-threshold SMBBHs + SMBBH SGWB
(*anisotropic contribution boosts the signal at some frequencies + weaker SGWB*)
- > If no BSM hint, low progress on BSM physics
(*you need to dig out the BSM signal from a strong SOBBH SGWB*)

What about LISA? The mission targets

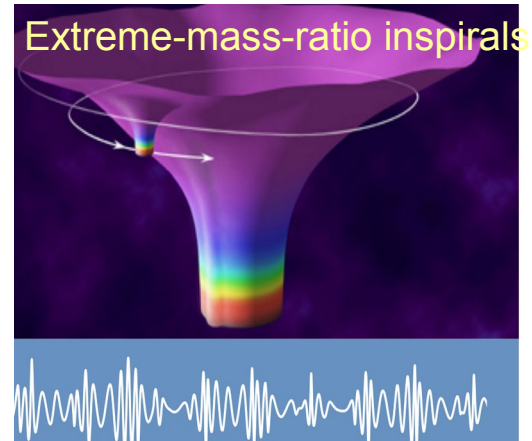
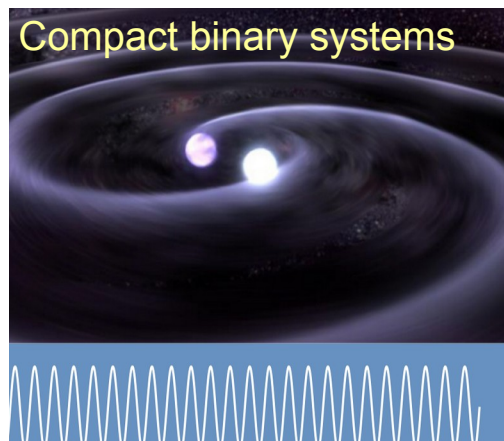
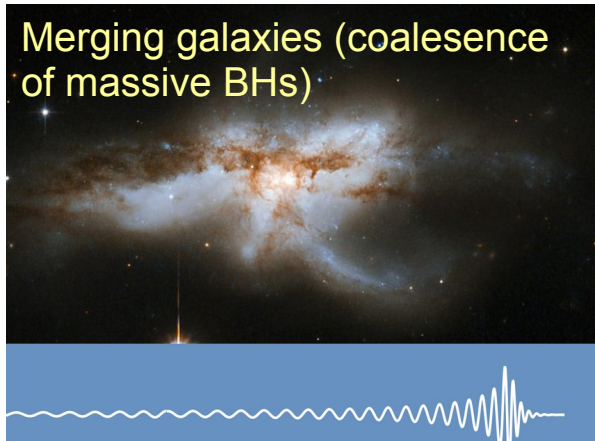


$O(10^4)$ resolv. galac. binaries

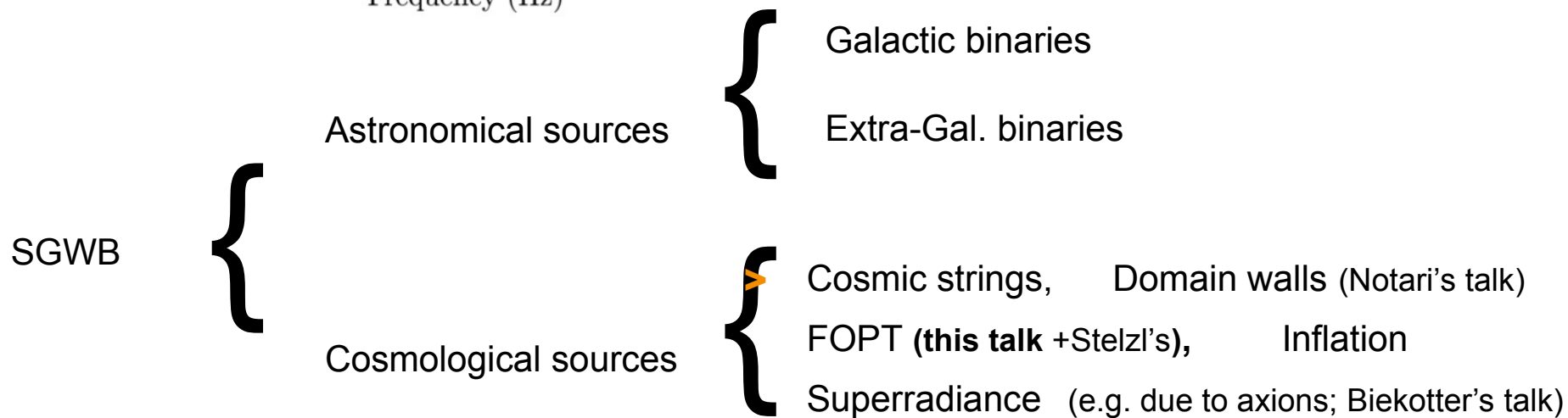
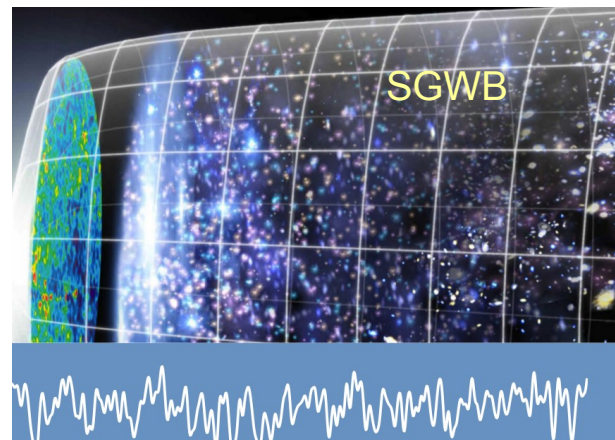
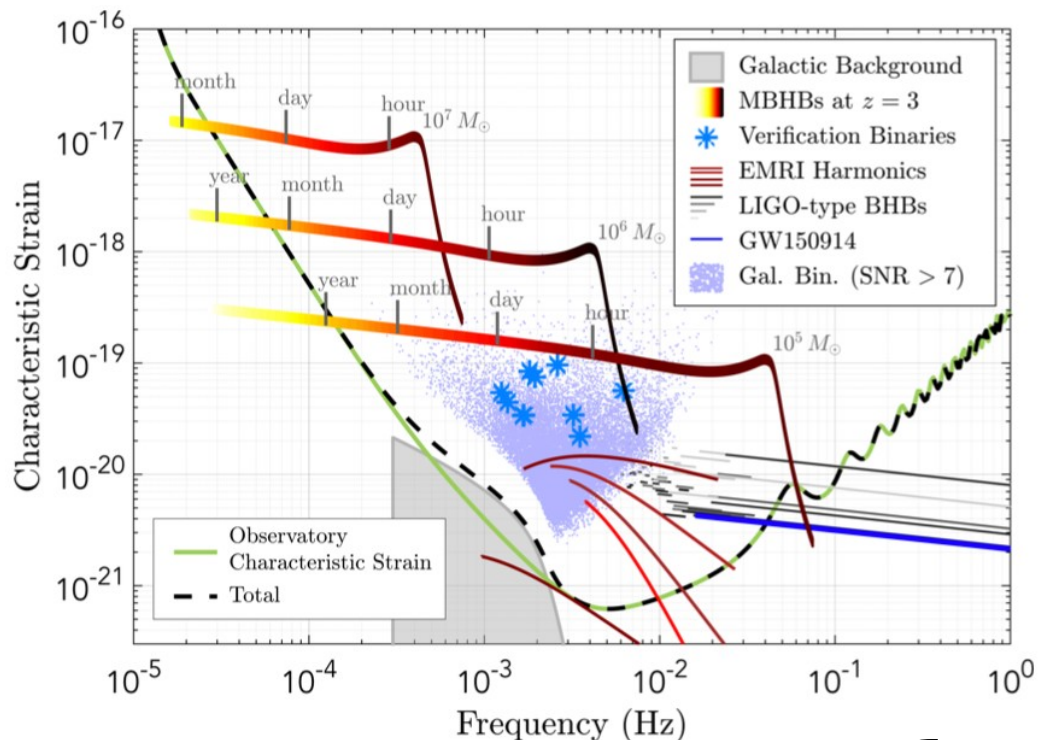
$O(10)$ extragal. BBHs of 10^0 – $10^2 M_{\odot}$

$O(1 - 10)$ extreme mass-ratio inspirals

$O(10 - 100)$ merging BBHs of 10^5 – $10^8 M_{\odot}$



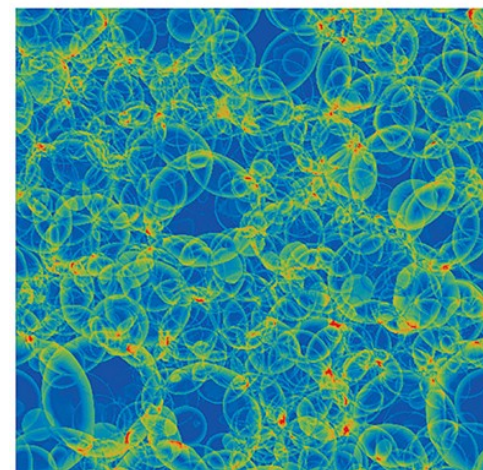
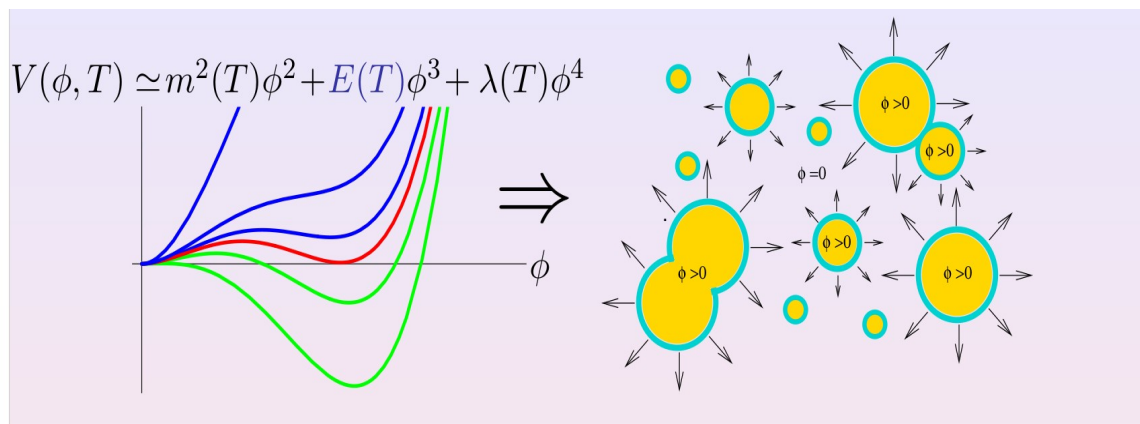
What about LISA? The mission targets



SGWB from a first-order phase transition (FOPT)

Some BSM models predict that, in the hot universe, some symmetries break via FOPTs

FOPT \rightarrow Many bubbles in a Hubble volume \rightarrow Isotropic SGWB



Parameters:

$K(\alpha)$: approx. max. energy that can be converted in GW radiation

β/H : inverse duration of the phase transition

T_* : universe temperature when bubbles collide

ξ_w : bubble wall velocity

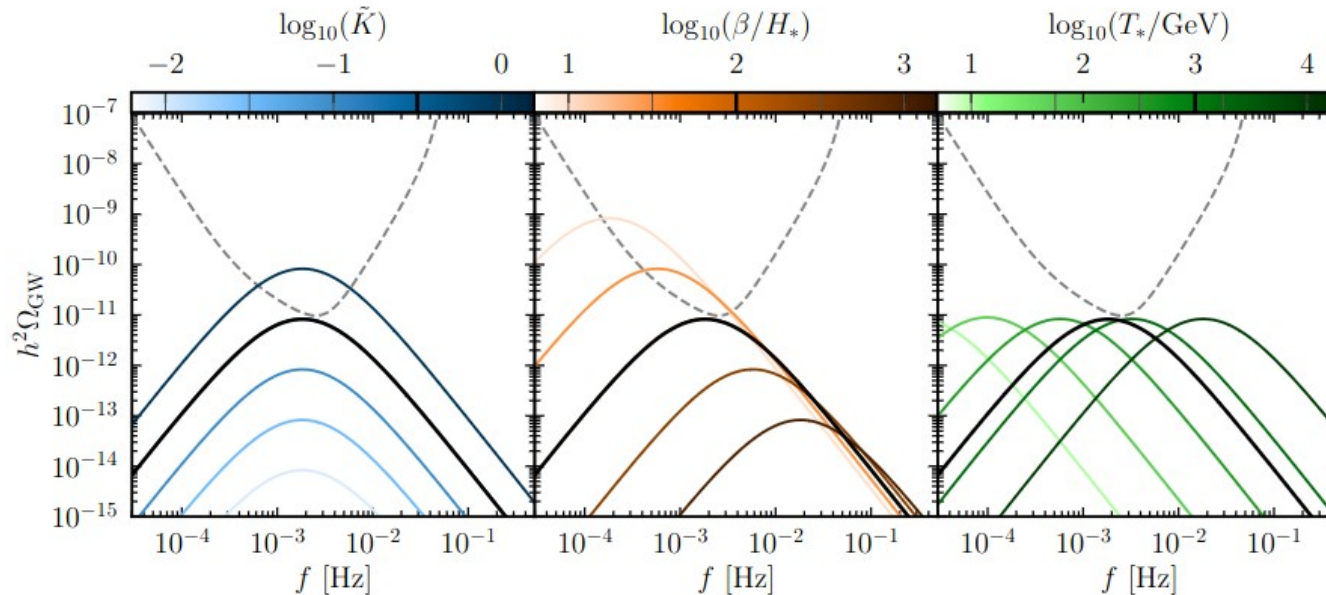
κ_i : efficiency factor of each contribution (**bubble wall**, sound wave, turbulence)

SGWB from a FOPT : templates

(for bubble coll.)

BSM leading to “relativistic bubbles”
 → SGWB broken power-law shape

($\xi_w \simeq 1$; $\kappa = 1$; free β/H , T_* , K)



Simulations hint to the geometric-param. template

$$\Omega_{\text{GW}}^{\text{BPL}}(f) = \Omega_b \left(\frac{f}{f_b} \right)^{n_1} \left[\frac{1}{2} + \frac{1}{2} \left(\frac{f}{f_b} \right)^{a_1} \right]^{\frac{n_2 - n_1}{a_1}}$$

$$n_1 = 2.4, \quad n_2 = -2.4, \quad a_1 = 1/2 \quad \text{Lewicki+Vaskonen, '23, Cutting+, '18}$$

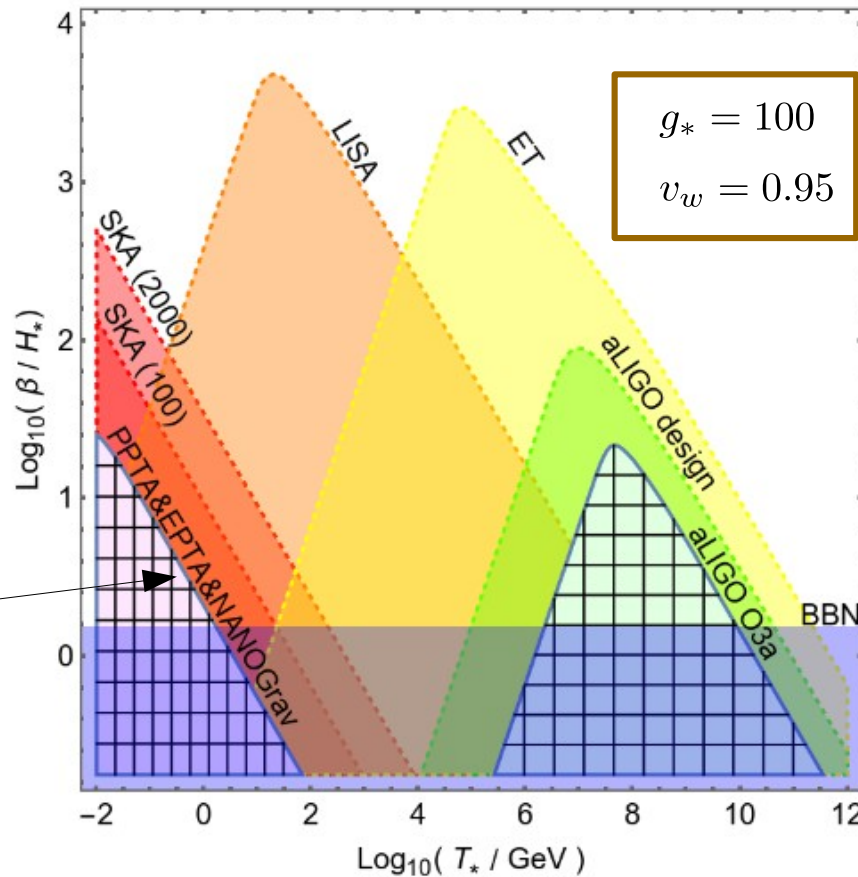
Param. reconstruction : 2 geom. vs 3 therm. param. **DEGENERACY!**

SGWB from a FOPT : parameter reach

(for bubble coll.)

BSM leading to “relativistic bubbles”
→ SGWB broken power-law shape

($\xi_w \simeq 1$; $\kappa = 1$; free β/H , T_* , K)



Taking SNR > 10 as
detection/non-detection
criterion

E. Megias, GN, M. Quiros, '18
LISA CosWG (P. Auclair, ..., GN et al.) '22

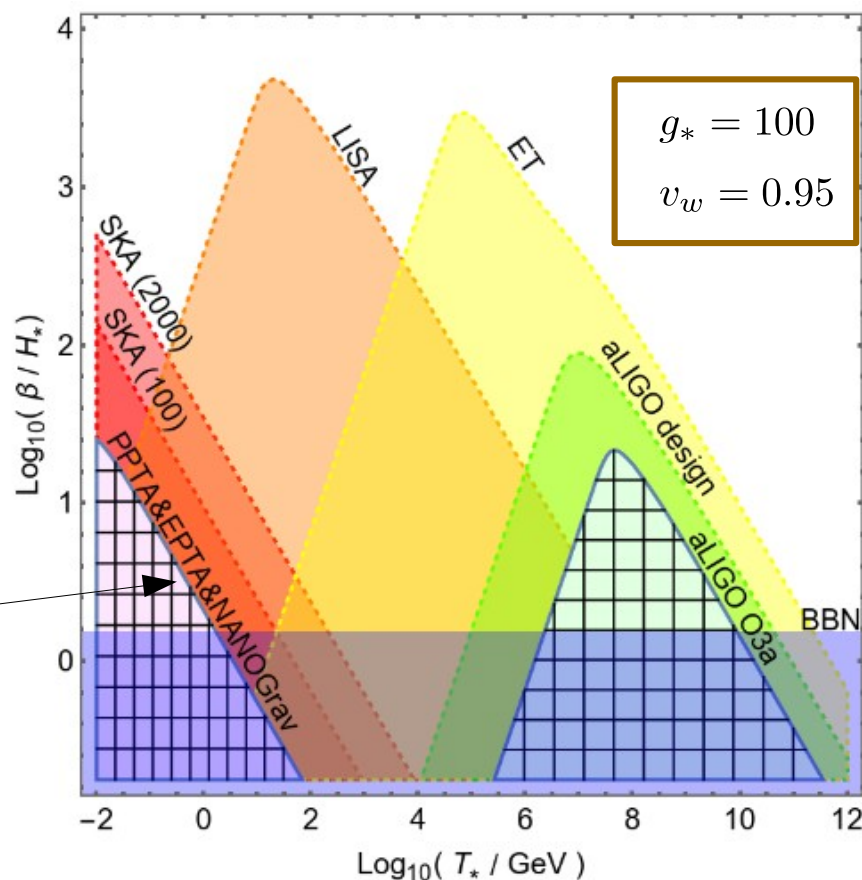
If no FOPT SGWB
signal in PTA

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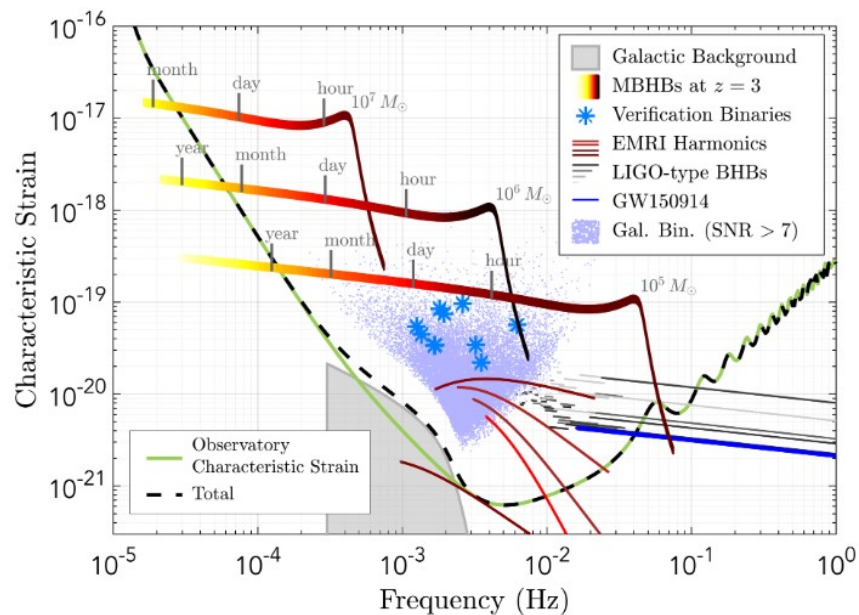
E. Megias, GN, M. Quiros, '18
LISA CosWG (P. Auclair, ..., GN et al.) '22

If no FOPT SGWB
signal in PTA

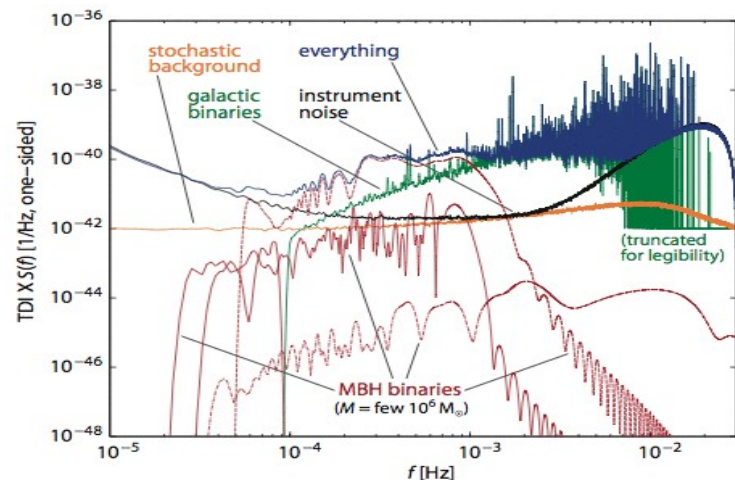
Knowing the parameter reach is nice,
but

it is the reconstruction accuracy that matters in understanding the underlying physics

SGWB from a FOPT : LISA search based on template



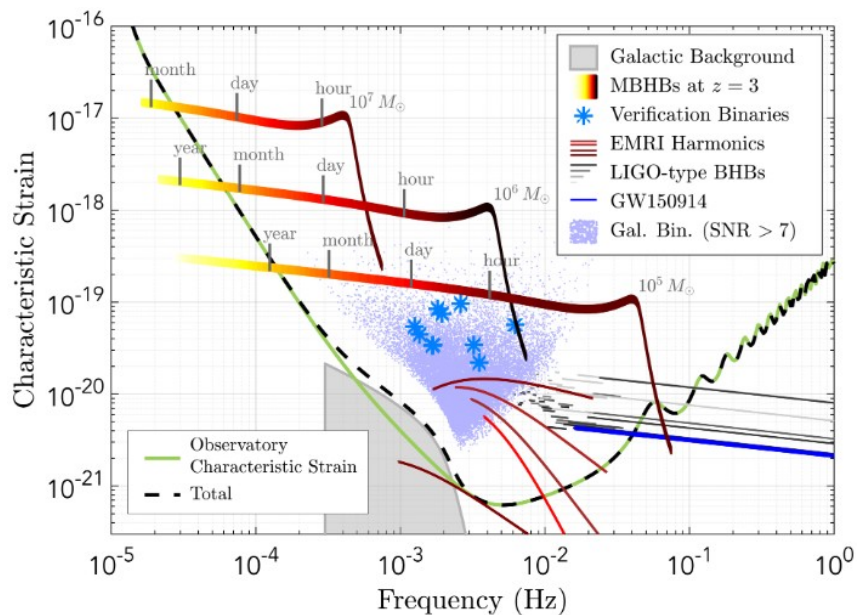
LISA is a signal-dominated experiment



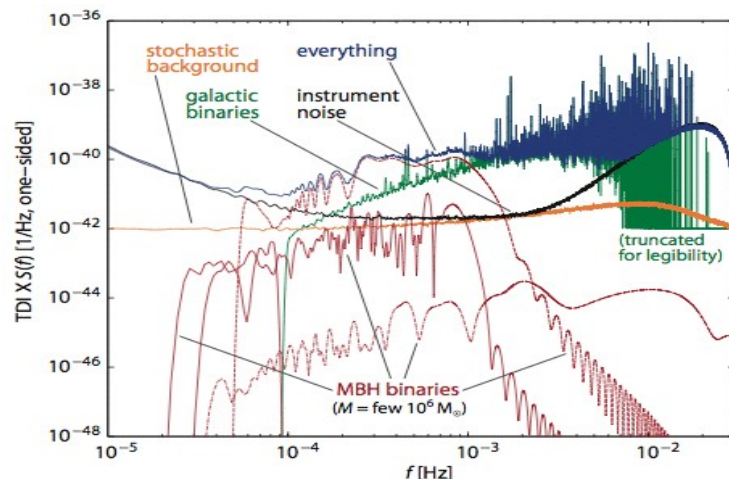
- Too many parameters to fit.
- Heavy-memory waveforms.

No hope to reach convergence in the parameter estimate by standard methods

SGWB from a FOPT : LISA search based on template

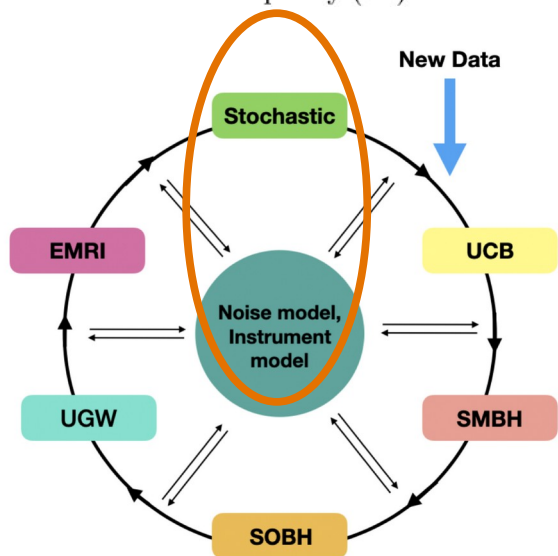


LISA is a signal-dominated experiment



- Too many parameters to fit.
- Heavy-memory waveforms.

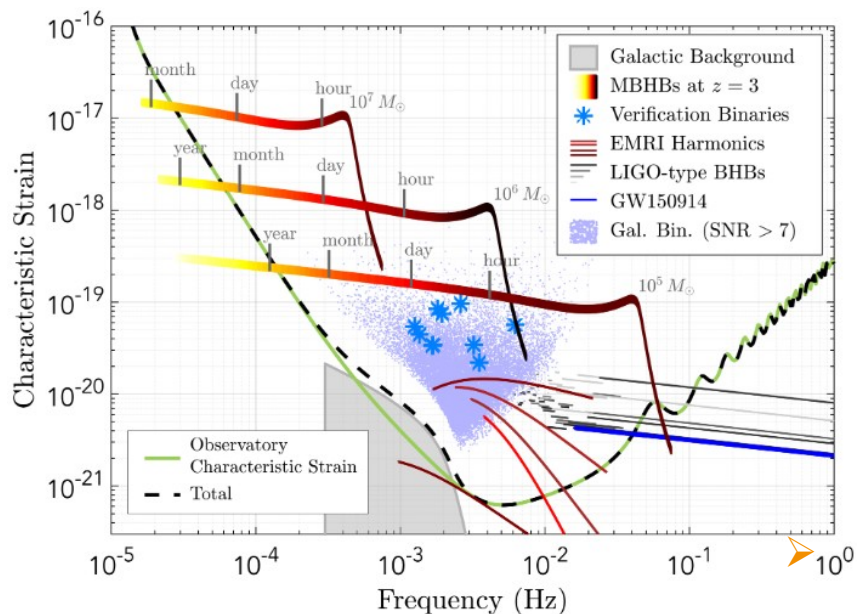
No hope to reach convergence in the parameter estimate by standard methods



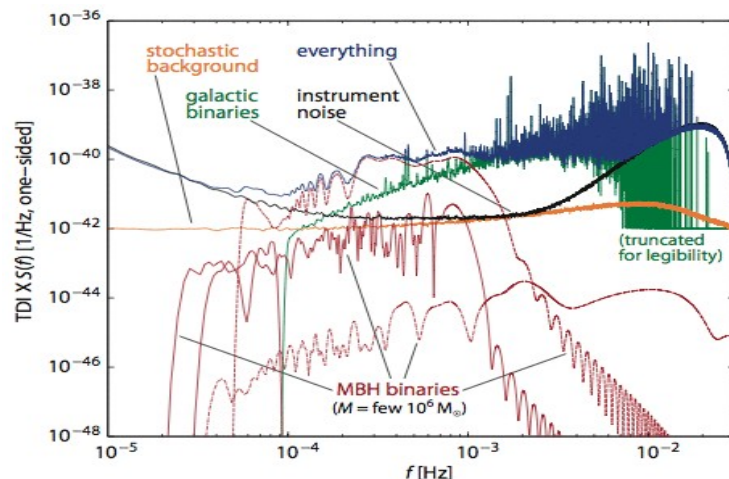
Iterative global fit.

Computational expensive!!! Simplified test: 50.000\$

SGWB from a FOPT : LISA search based on template

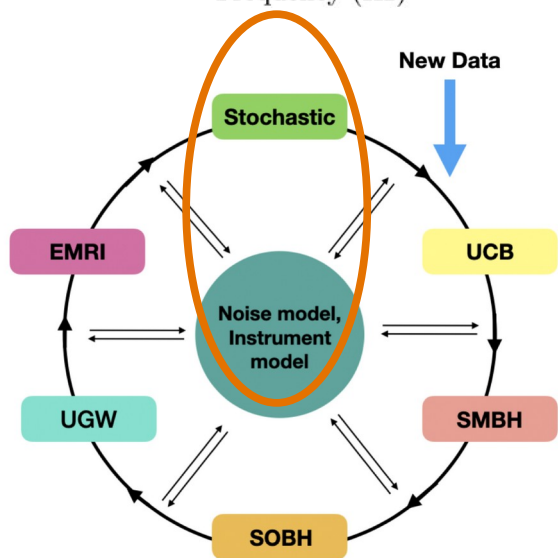


LISA is a signal-dominated experiment



We build the search and run it on data with

- The (faint) unresolved binaries
- The instrumental noise
- The FOPT SGWB



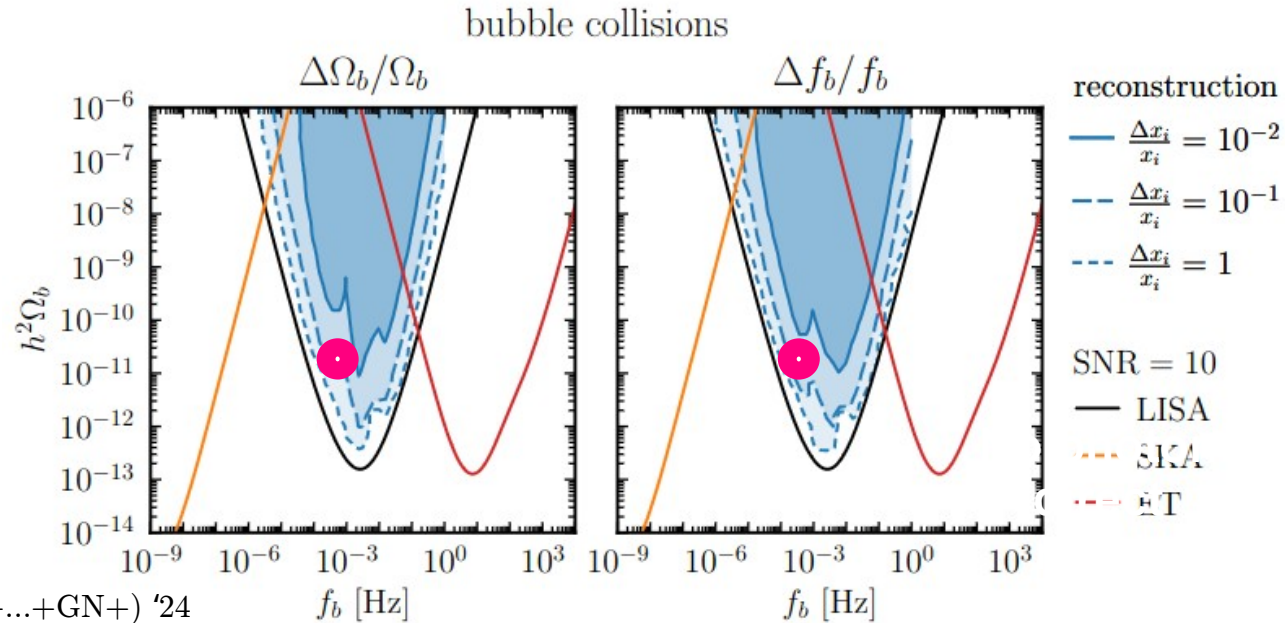
- Simplifications:
 - We neglect the likelihood correlations/systematics with the transient sources
 - Same template model for injection and recovery (no. theory systematics)

LISA FOPT search: forecast

(for bubble coll.)

BSM leading to “relativistic bubbles”
 → SGWB broken power-law shape

($\xi_w \simeq 1$; $\kappa = 1$; free β/H , T_* , K)



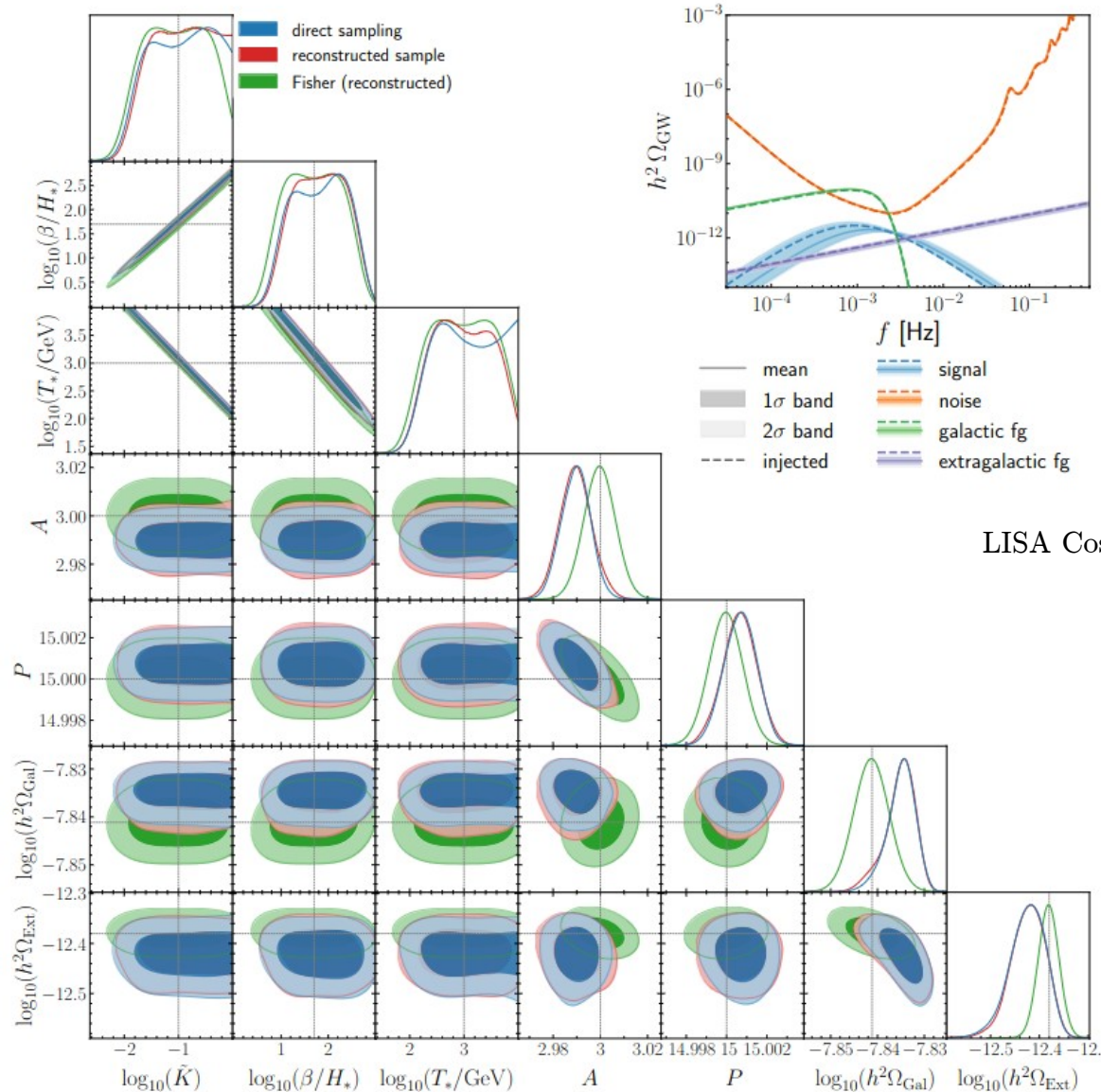
LISA CosWG (Caprini+...+GN+) '24

$$\Omega_{\text{GW}}^{\text{BPL}}(f) = \Omega_b \left(\frac{f}{f_b} \right)^{n_1} \left[\frac{1}{2} + \frac{1}{2} \left(\frac{f}{f_b} \right)^{a_1} \right]^{\frac{n_2 - n_1}{a_1}}$$

$$n_1 = 2.4, \quad n_2 = -2.4, \quad a_1 = 1/2$$

LISA FOPT search: forecast for benchmark (for bubble coll.)

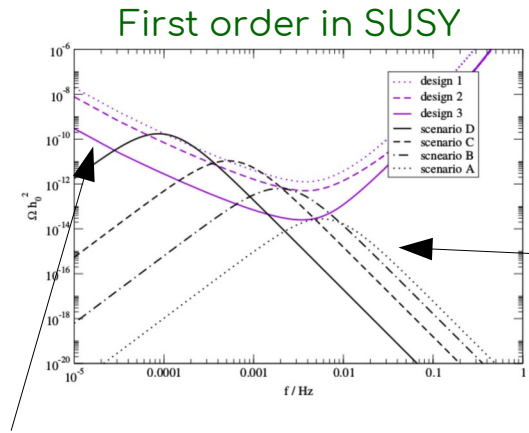
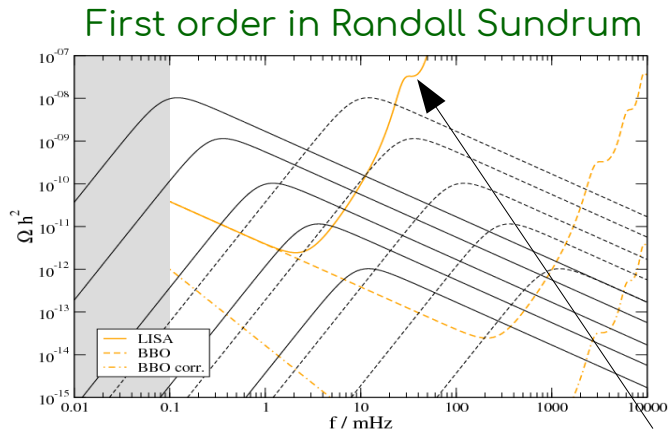
Noise + astro. SGWB + FOPT thermodynamic parameters



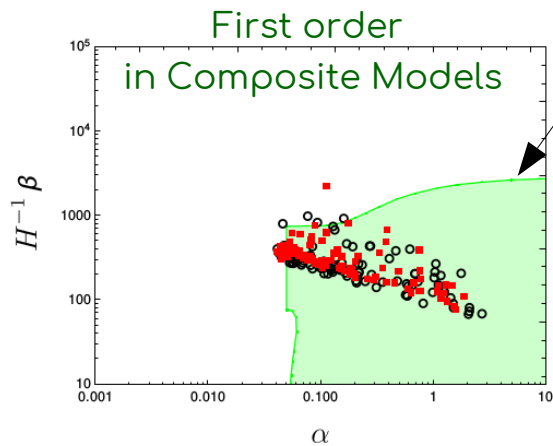
LISA CosWG (Caprini+...+GN+) '24

What BSM behind the FOPT SGWB ?

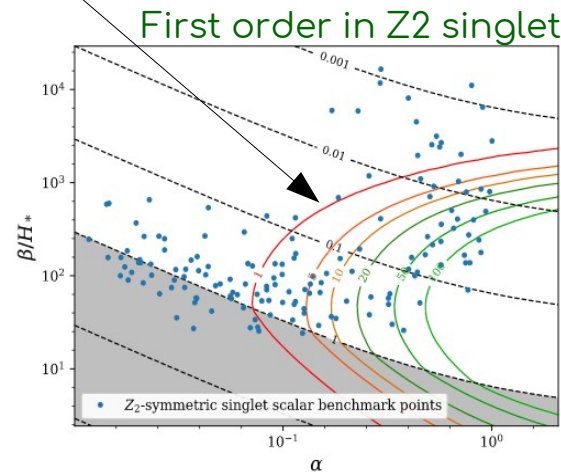
A multitude



SGWB signal above sensitivity



LISA sensitive region



But also 2HDM, B-L model, dark sector,

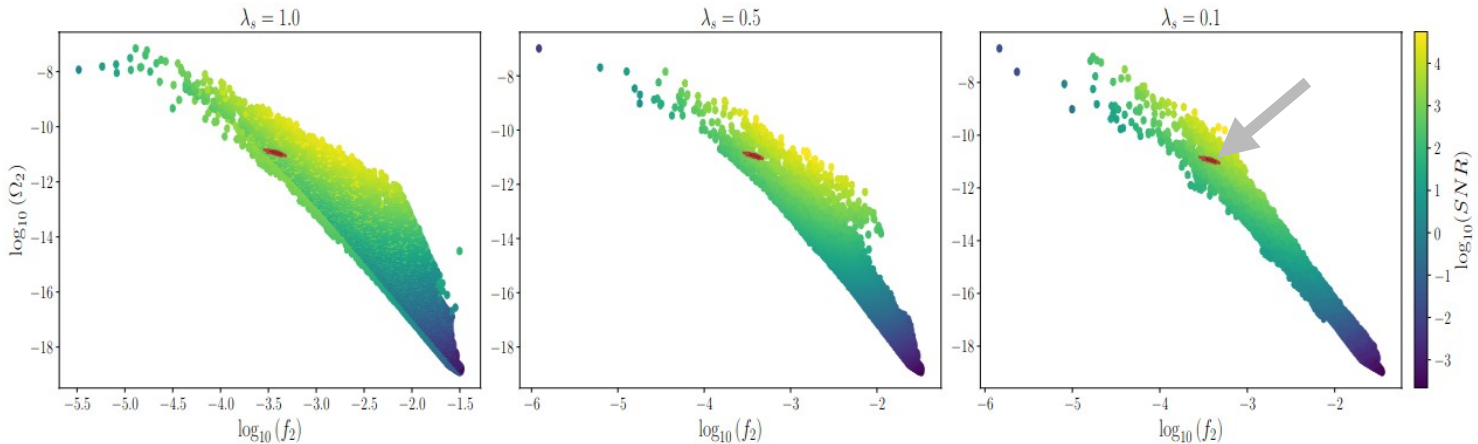
Many models with different pheno!

Figs. from:
Konstandin, GN et al.'10
Huber, GN et al.'15
Chala, GN et al.'16

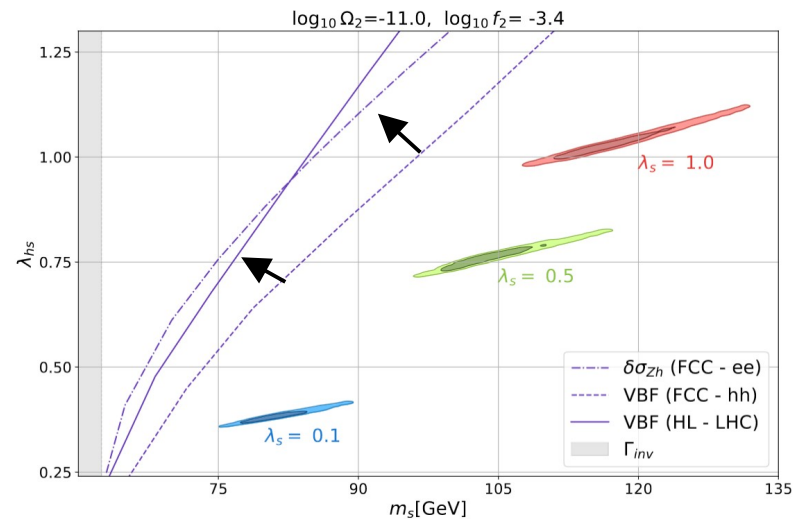
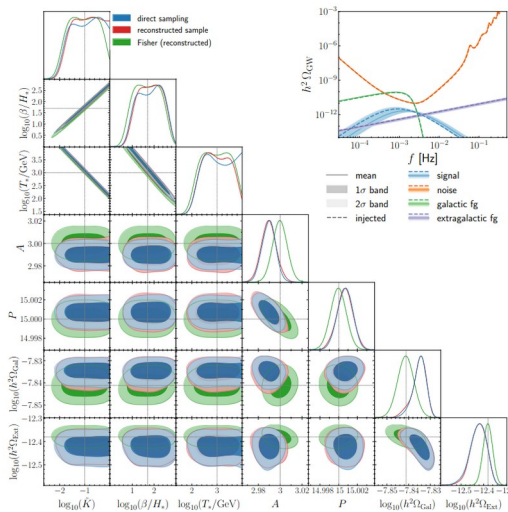
More examples in:
LISA CosWG (Caprini, ..., GN et al.)'16
LISA CosWG (Caprini, ..., GN et al.)'20

If nature is described by the Z_2 singlet model ...

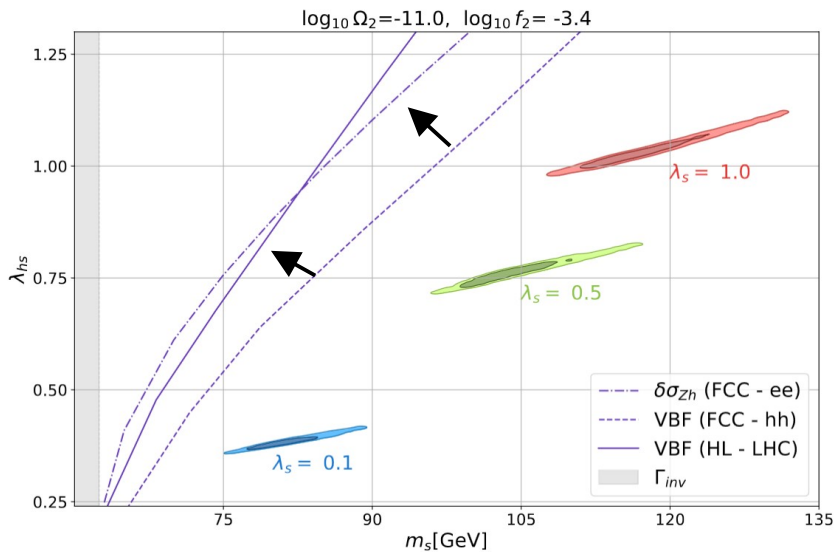
- FOPT SGWB parameter region compatible with the Z_2 singlet model



LISA detection benchmark recast into the Z_2 singlet model

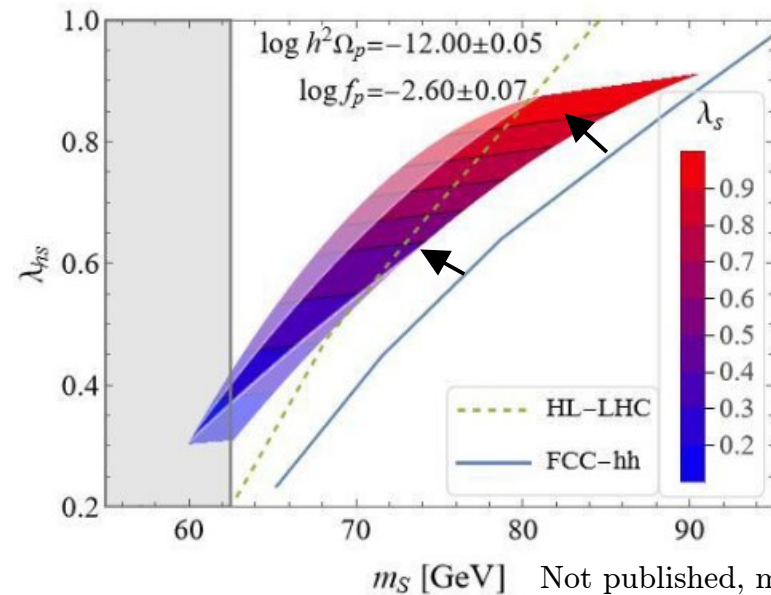


If nature is described by the Z_2 singlet model ...



LISA CosWG (Caprini+...+GN+) '24

For collider bounds: Craig+,14 ; Ellis+, '18



Not published, minor mistakes

- Synergy/complementarity between LISA and colliders
- LISA reconstruction accuracy rather good
- This accuracy allows for some model selection (benchmark and model dependent conclusion)

Singlet is just an example. In general:

- *Does the synergy efficiently break degeneracies ?*
- *Ways to improve the FCC design if LISA sees the signal in ~2036 ?*

Conclusions and outlook

- LISA can accurately reconstruct a FOPT signal
- Results based on some simplifications. Need to test results with more realistic simulations (although expensive)
- Reconstruction interpretation done only for two BSM models. Rationale can be followed for other models (with caution to the par. space dimensionality)

- Clear synergy/complementarity with colliders. But IMO synergy should be quantified with an exhaustive list of representative models:
 - × How much does LISA constrain the param. space of a model? And the FCC? And LISA and FCC together ?
 - × Is the achieved accuracy relevant? Breaks degeneracies? Helps for model selection?
 - × Are there bottlenecks limiting the synergy? Feasible ways to improve them? Still on time to implement them if LISA sees a signal ?