

# Axion-like particles at colliders

Anke Biekötter - JGU Mainz

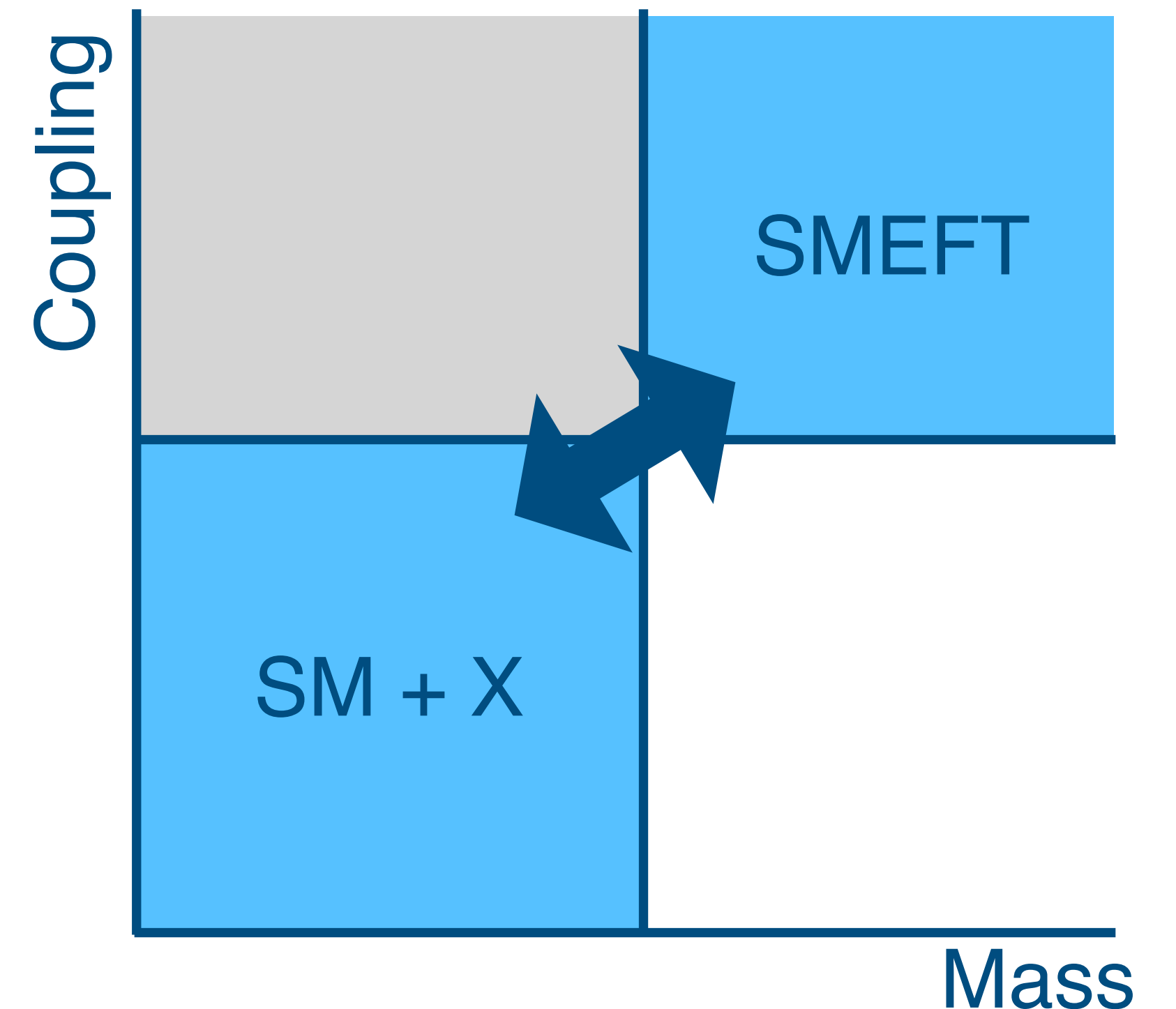
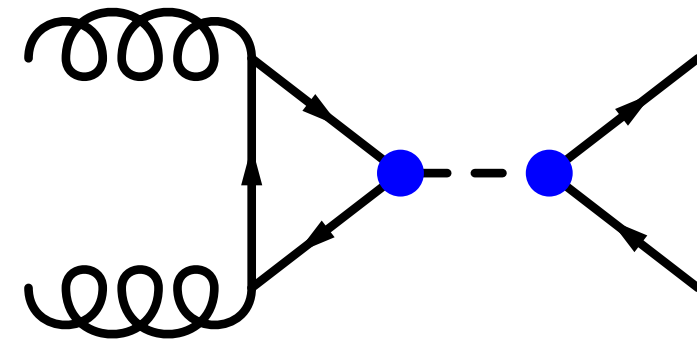
JOHANNES GUTENBERG  
UNIVERSITÄT MAINZ



LFC24 - Fundamental Interactions at Future Colliders, Sep 18, 2024

# Outline

- Axion-like particle (ALP) Effective Field Theory
  - ALP parameter space and colliders
- ALP couplings to top quarks
  - $t\bar{t}$  production
- Indirect bounds on ALP couplings from the SMEFT
  - FCC-ee limits



# Axions

$$\mathcal{L} = \theta \frac{\alpha_s}{8\pi} G_{\mu\nu}^a \tilde{G}^{a\mu\nu}$$

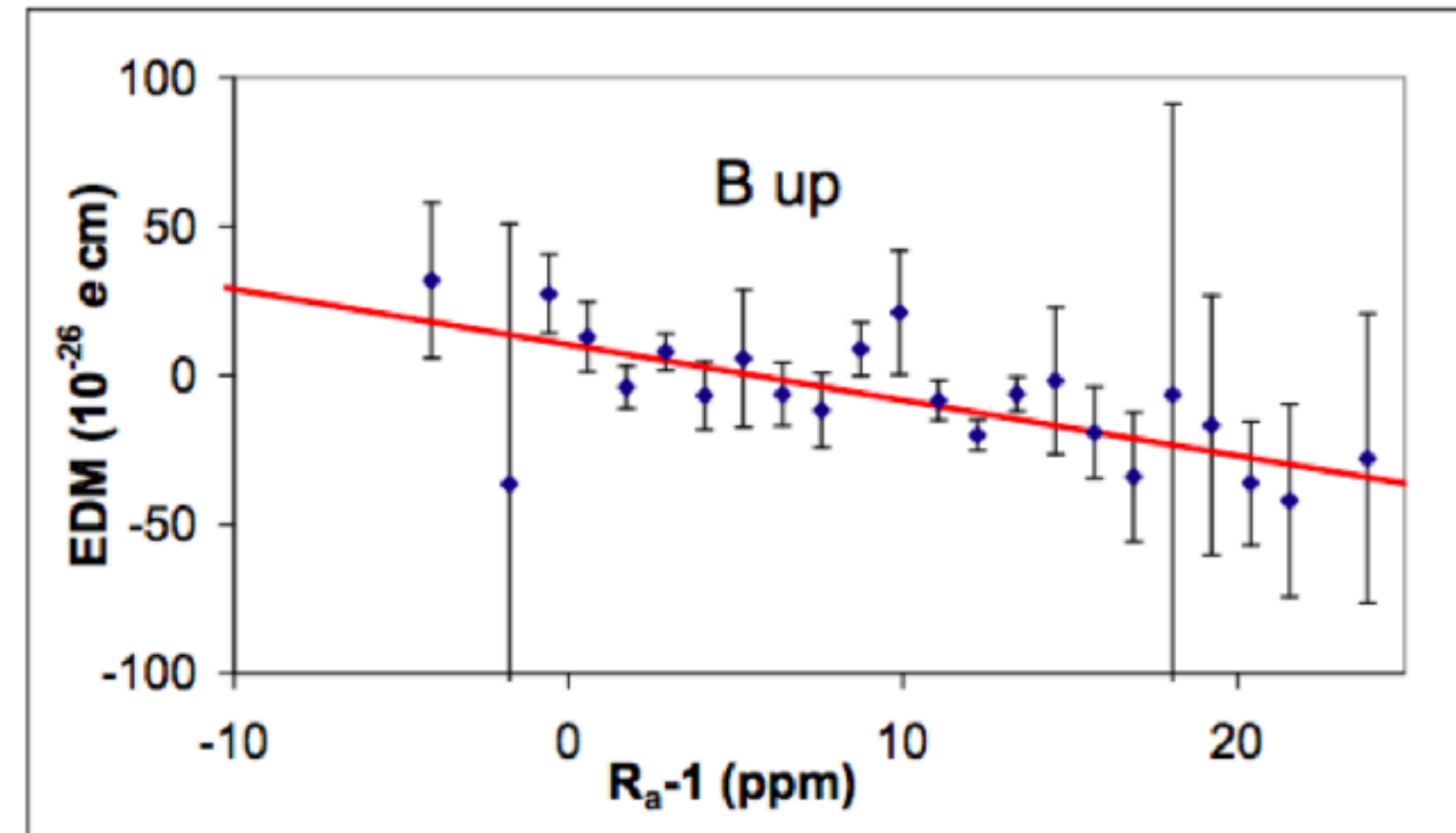
Why is the theta term so small?

$$\mathcal{L} = \left( \theta - \frac{a}{f_a} \right) \frac{\alpha_s}{8\pi} G_{\mu\nu}^a \tilde{G}^{a\mu\nu}$$

Dynamical solution to the strong CP problem

$$m_a f_a = \text{const.}$$

[Baker et al. ([hep-ex/0602020](#))]



Electric dipole moment of the neutron

[Peccei, Quinn ([ref1](#), [ref2](#))]

[[Weinberg](#)] [[Wilczek](#)]



# Axions

This talk is NOT about the QCD axion.

$$\mathcal{L} = \theta \frac{\alpha_s}{8\pi} G_{\mu\nu}^a \tilde{G}^{a\mu\nu}$$

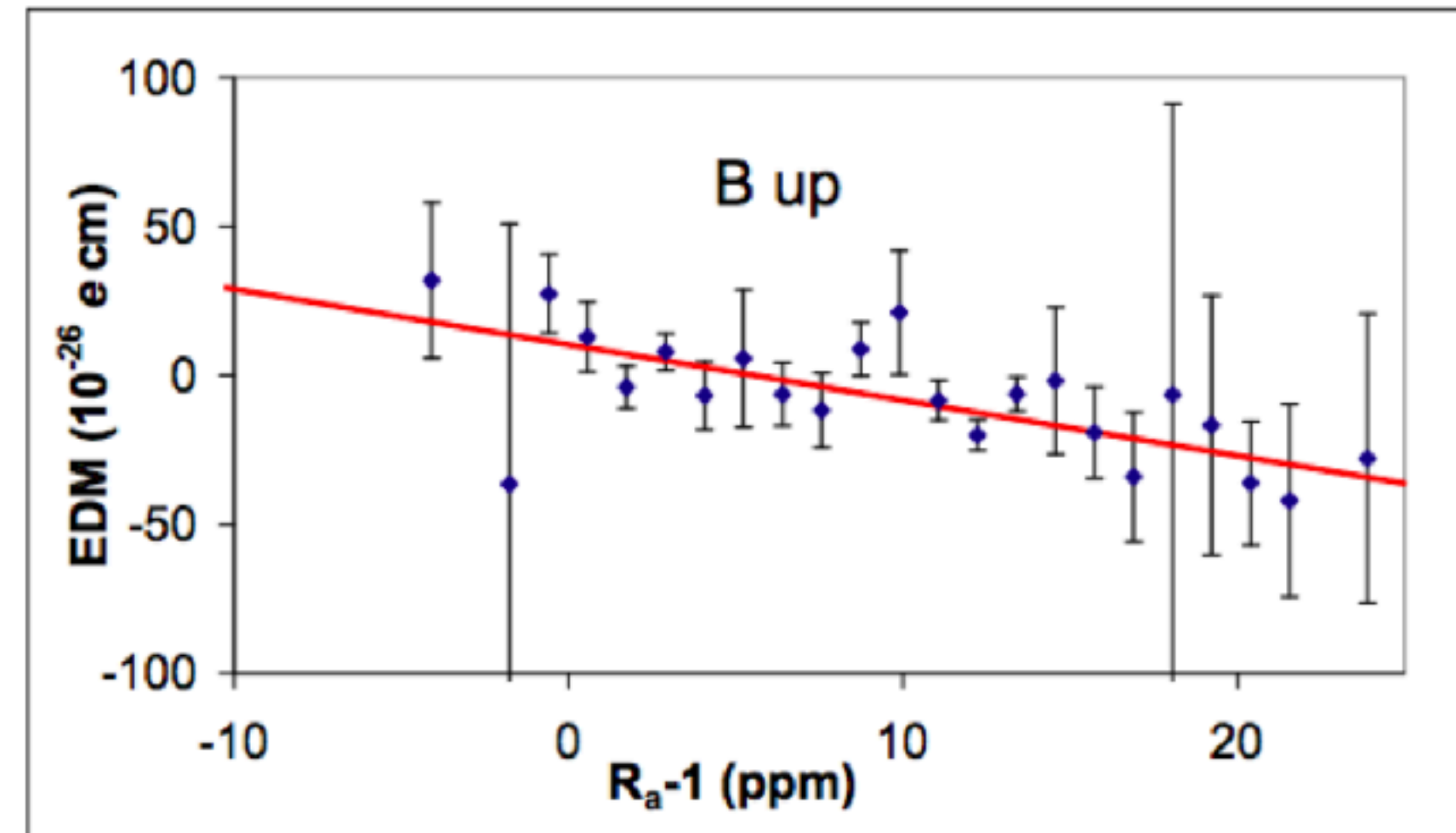
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[Weinberg] [Wilczek]



# Axion-like particles

EFT with an additional light d.o.f.  
and at dimension 5

- Featured in many BSM scenarios: “Higgs portal” dark matter, composite Higgs models, ...
- Consider a generic ALP with effective Lagrangian

[Peccei, Quinn ([ref1](#), [ref2](#))]  
[Weinberg] [Wilczek]

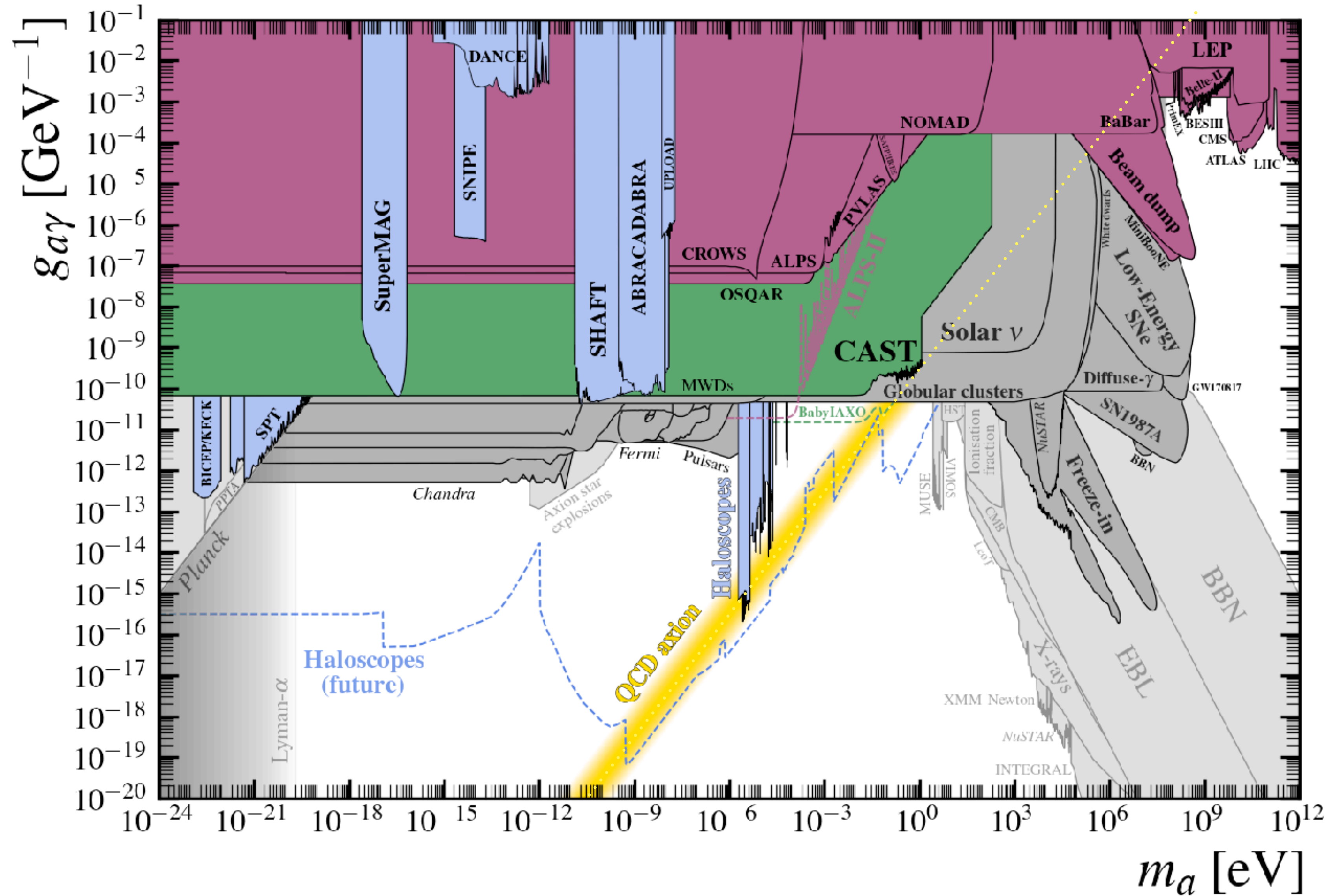
[Brivio et al. ([1701.05379](#))]  
[Bauer et al. ([1708.00443](#))]

- Shift symmetry  $a \rightarrow a + a_0$ , Lagrangian terms:  $\frac{\partial_\mu a}{f_a} (\text{SM})^\mu$

$$\mathcal{L}_{\text{eff}}^{D \leq 5} = \frac{1}{2} (\partial_\mu a)(\partial^\mu a) - \frac{m_{a,0}^2}{2} a^2 + \frac{\partial^\mu a}{f} \sum_F \bar{\psi}_F c_F \gamma_\mu \psi_F + c_\phi \frac{\partial^\mu a}{f} (\phi^\dagger i \overleftrightarrow{\mathbf{D}}_\mu \phi) \\ + c_{GG} \frac{\alpha_s}{4\pi} \frac{a}{f} G_{\mu\nu}^a \tilde{G}^{\mu\nu,a} + c_{WW} \frac{\alpha_2}{4\pi} \frac{a}{f} W_{\mu\nu}^A \tilde{W}^{\mu\nu,A} + c_{BB} \frac{\alpha_1}{4\pi} \frac{a}{f} B_{\mu\nu} \tilde{B}^{\mu\nu} .$$



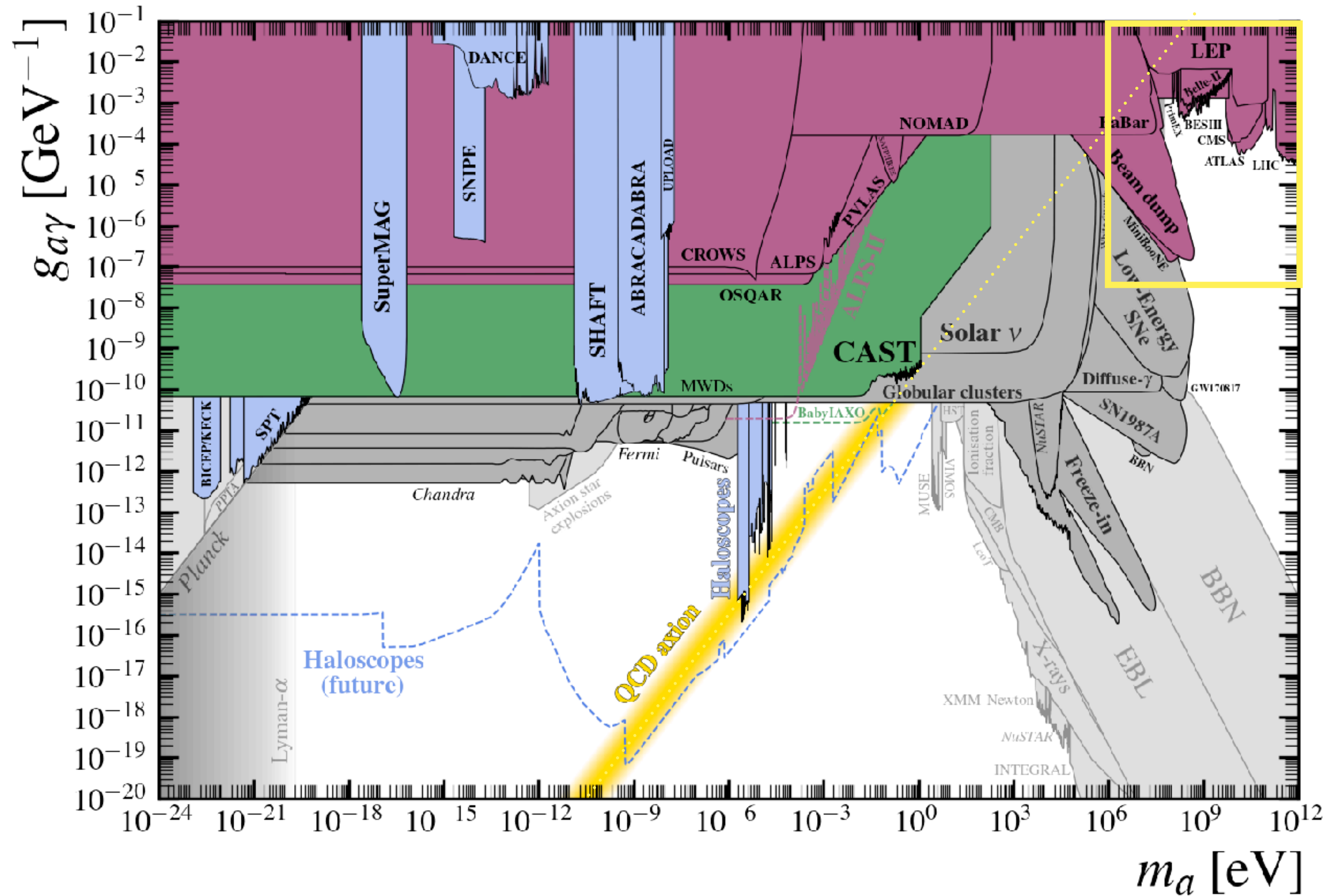
# ALP phenomenology



Interplay of experiments/  
observations crucial

[O'Hare (axion limits)]

# ALP phenomenology

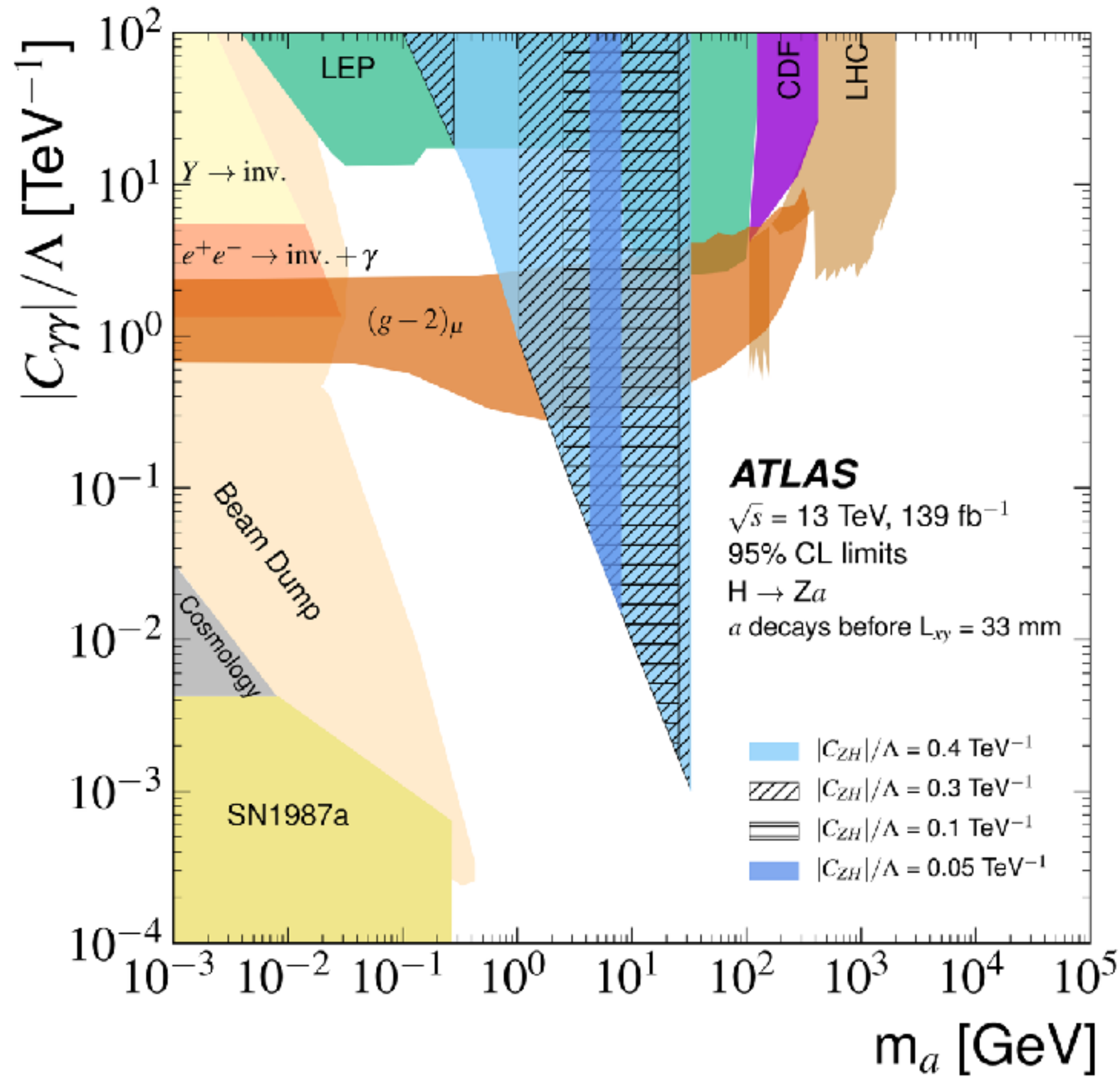


Interplay of experiments/  
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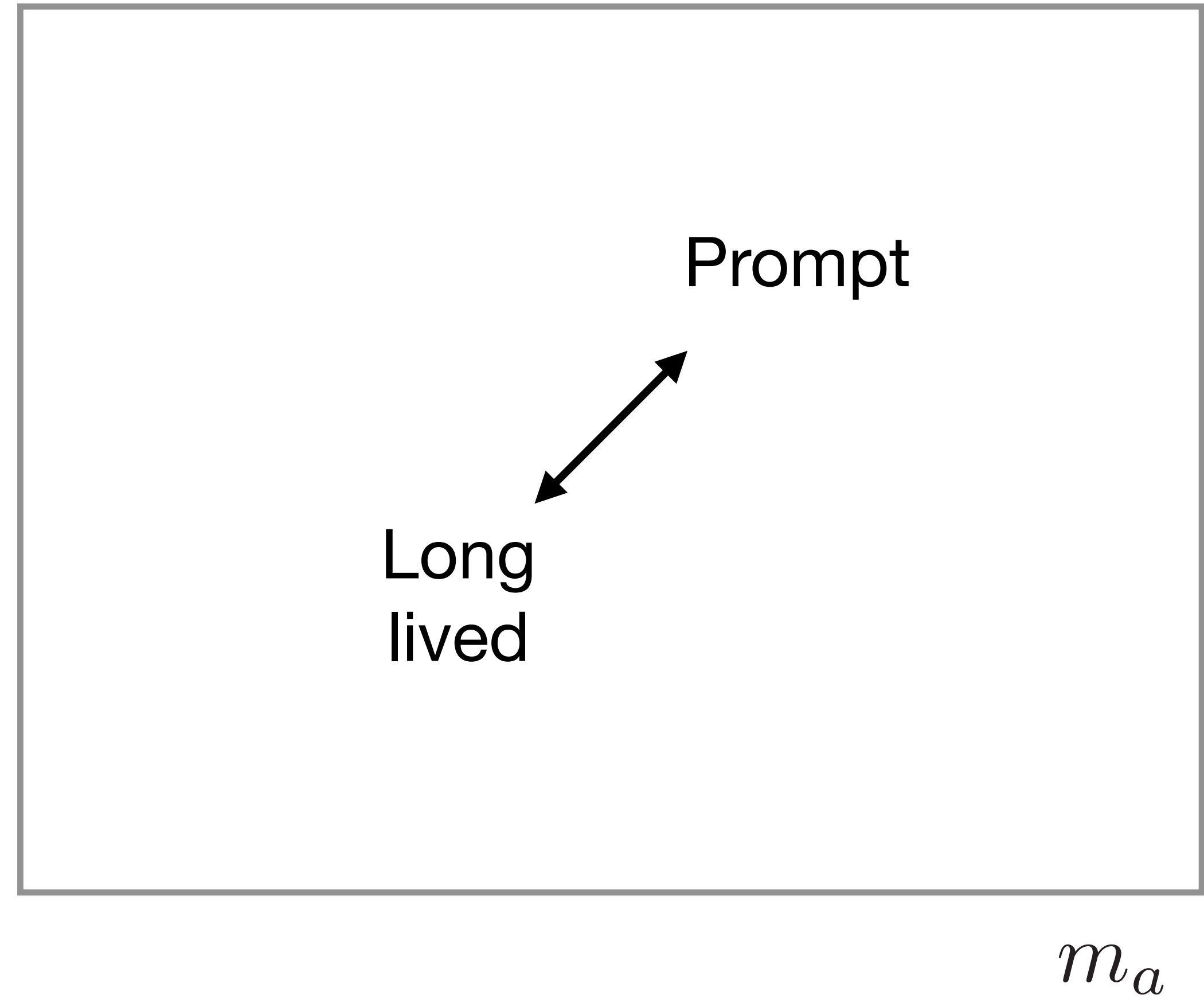
[O'Hare (axion limits)]



# ALPs at colliders



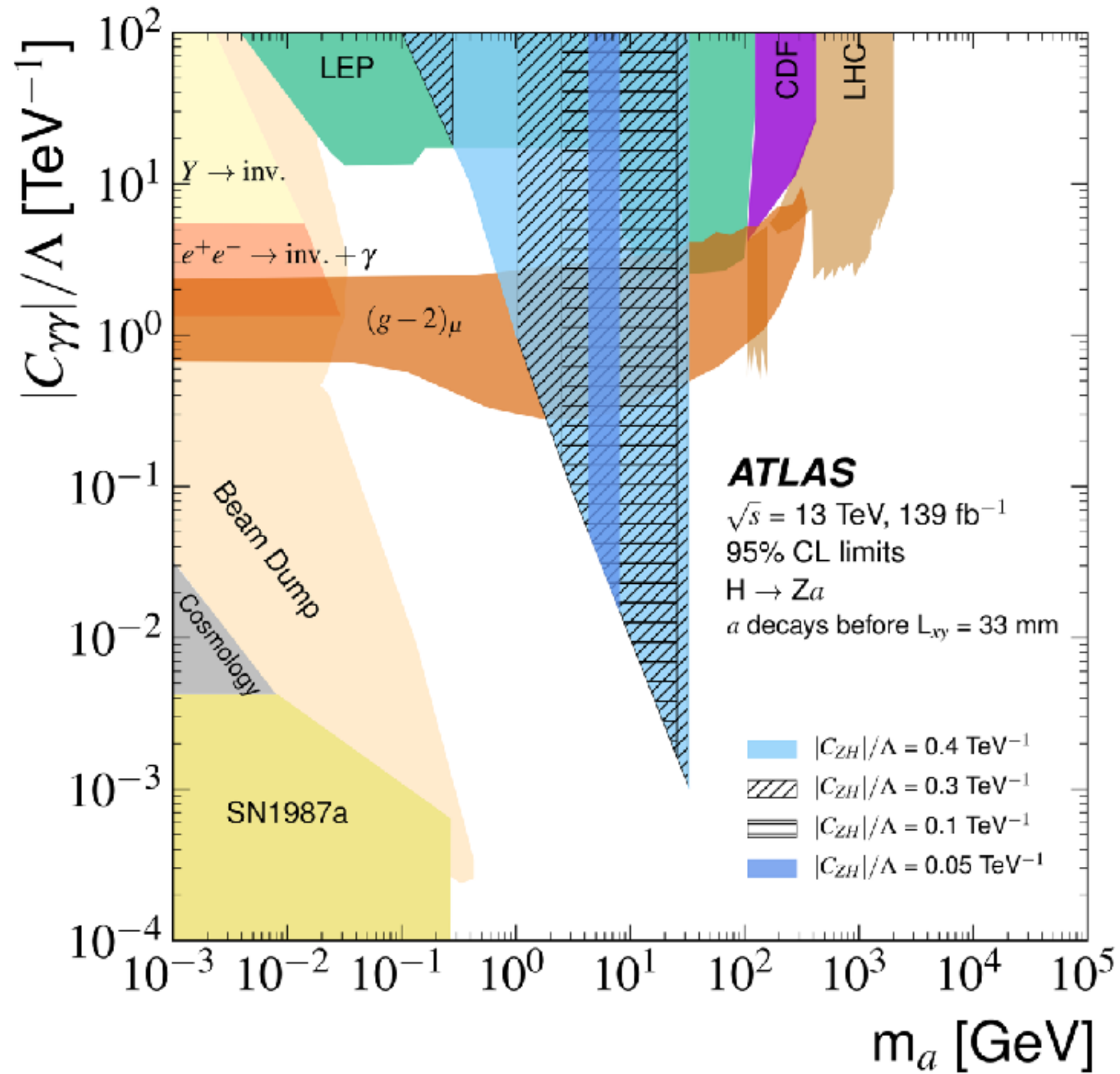
$g_{aXX}$



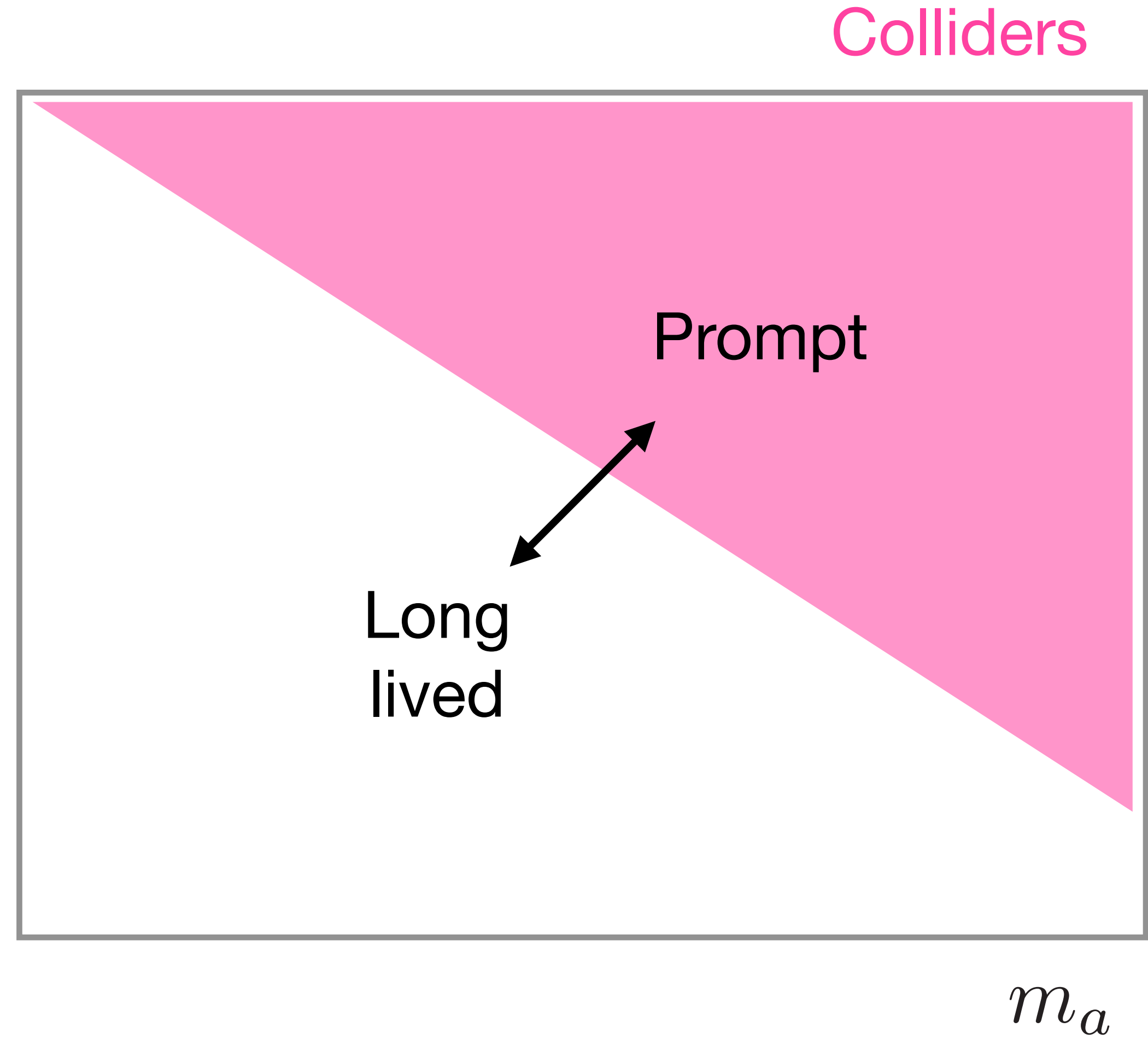
[ATLAS (2312.01942)]



# ALPs at colliders

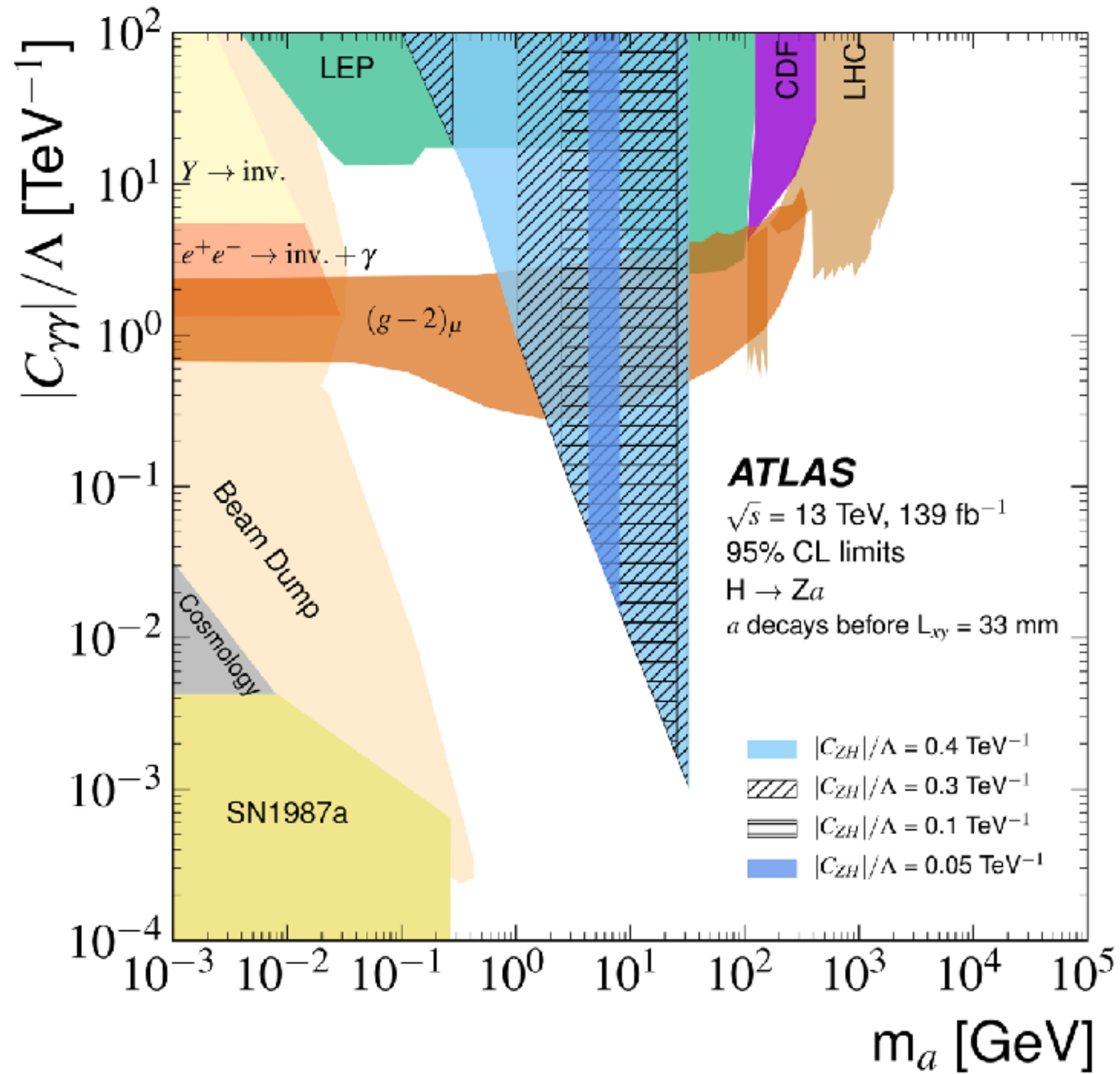


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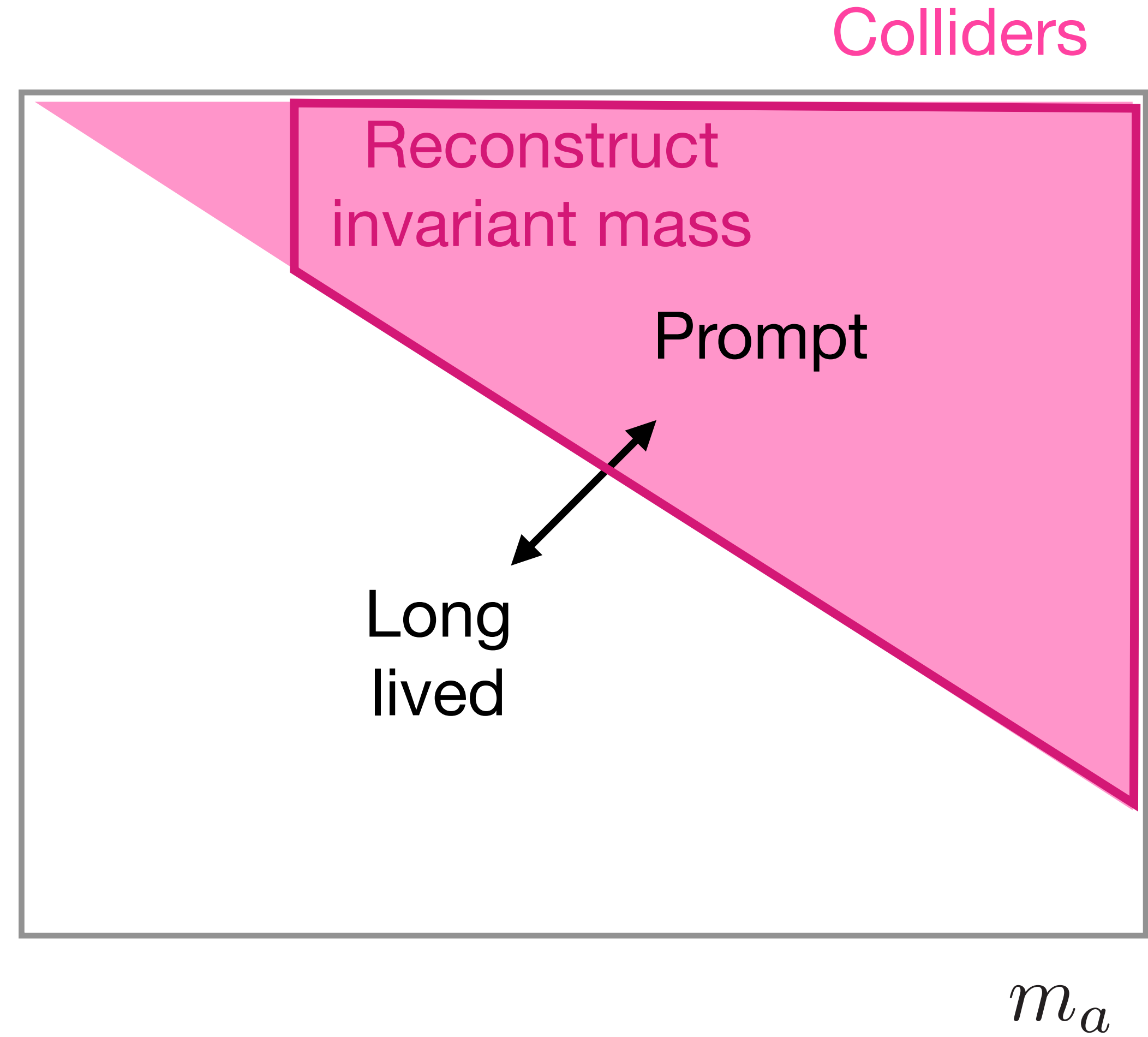
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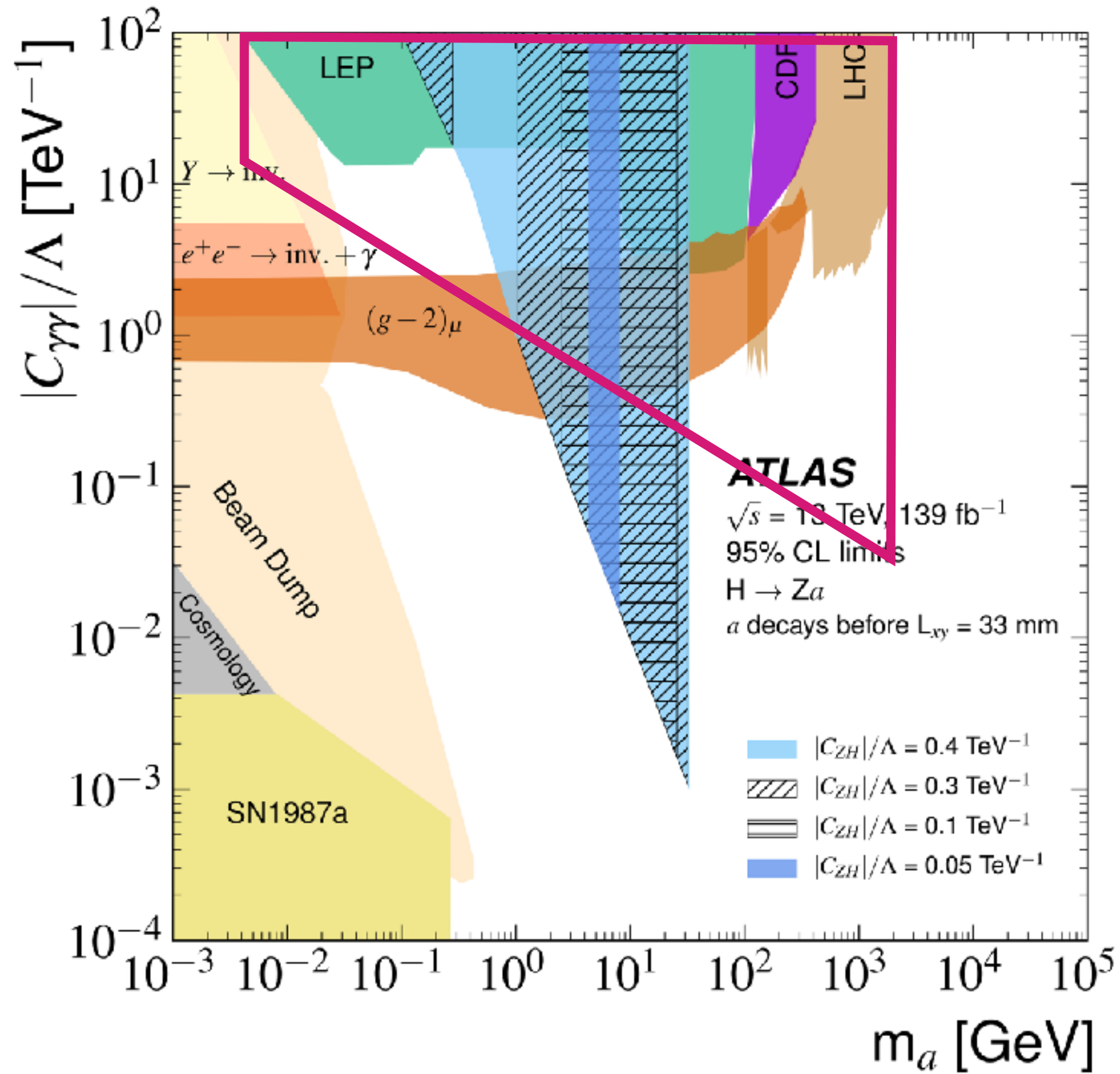


[ATLAS (2312.01942)]

$g_a X X$

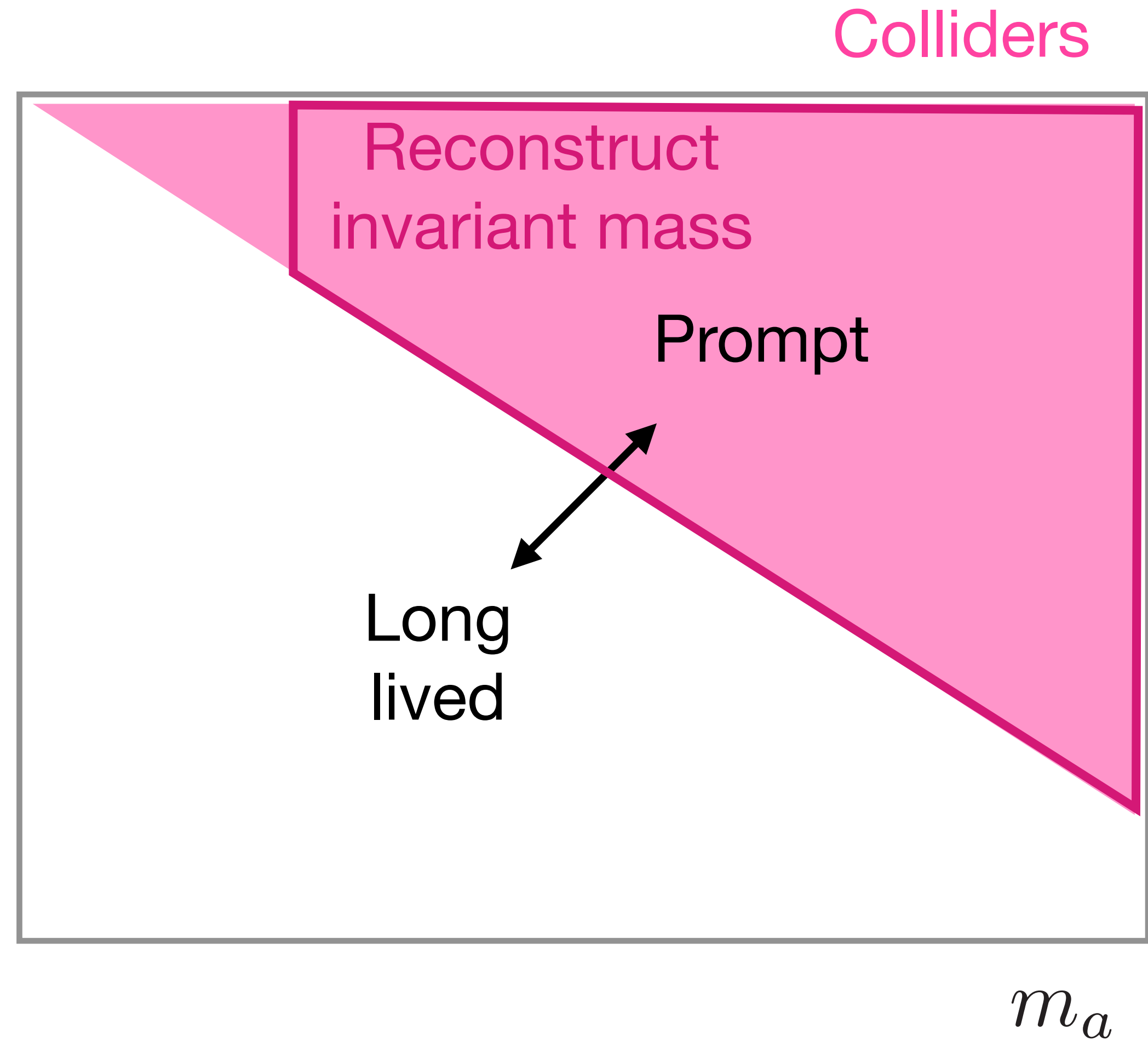


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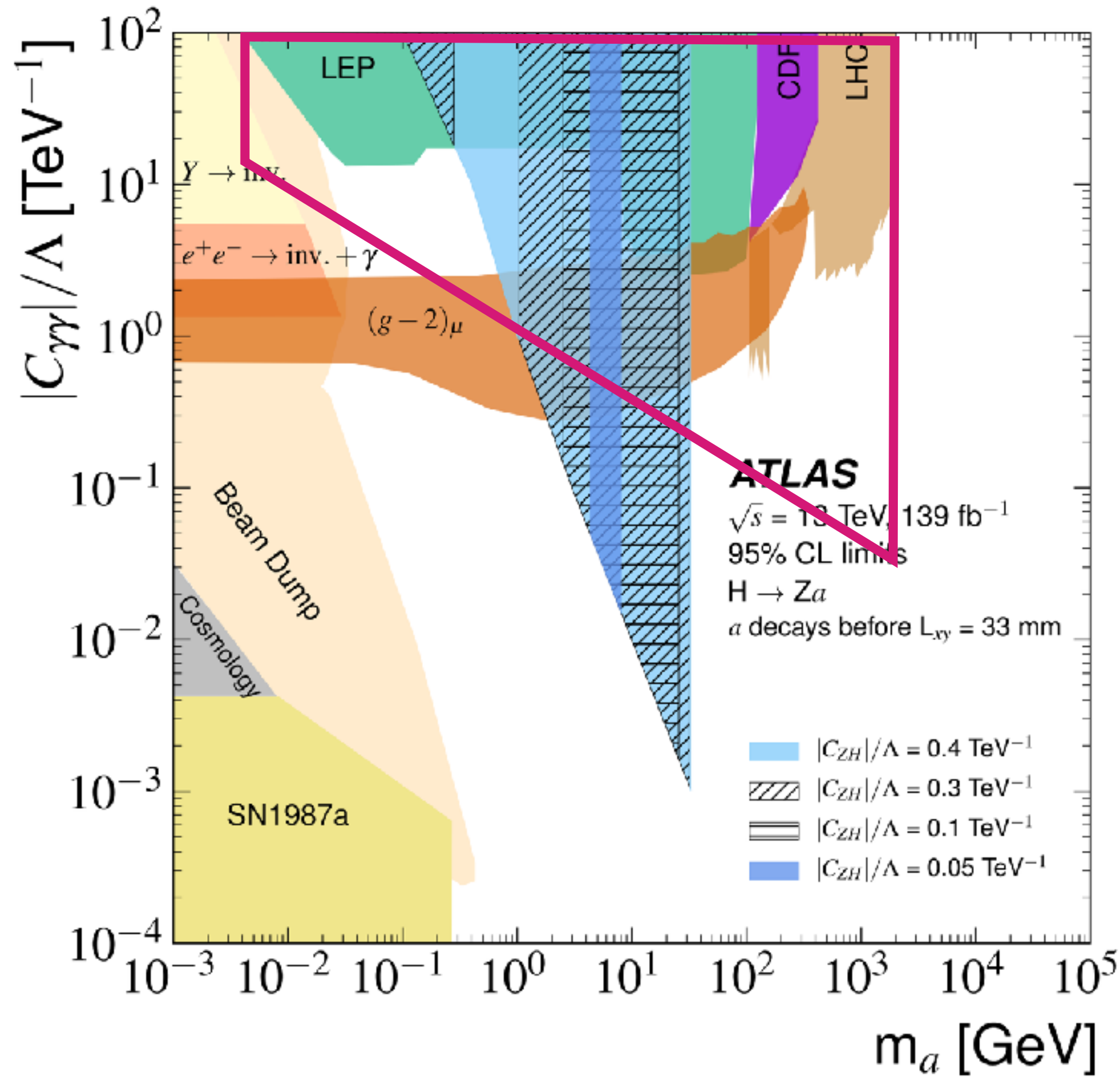
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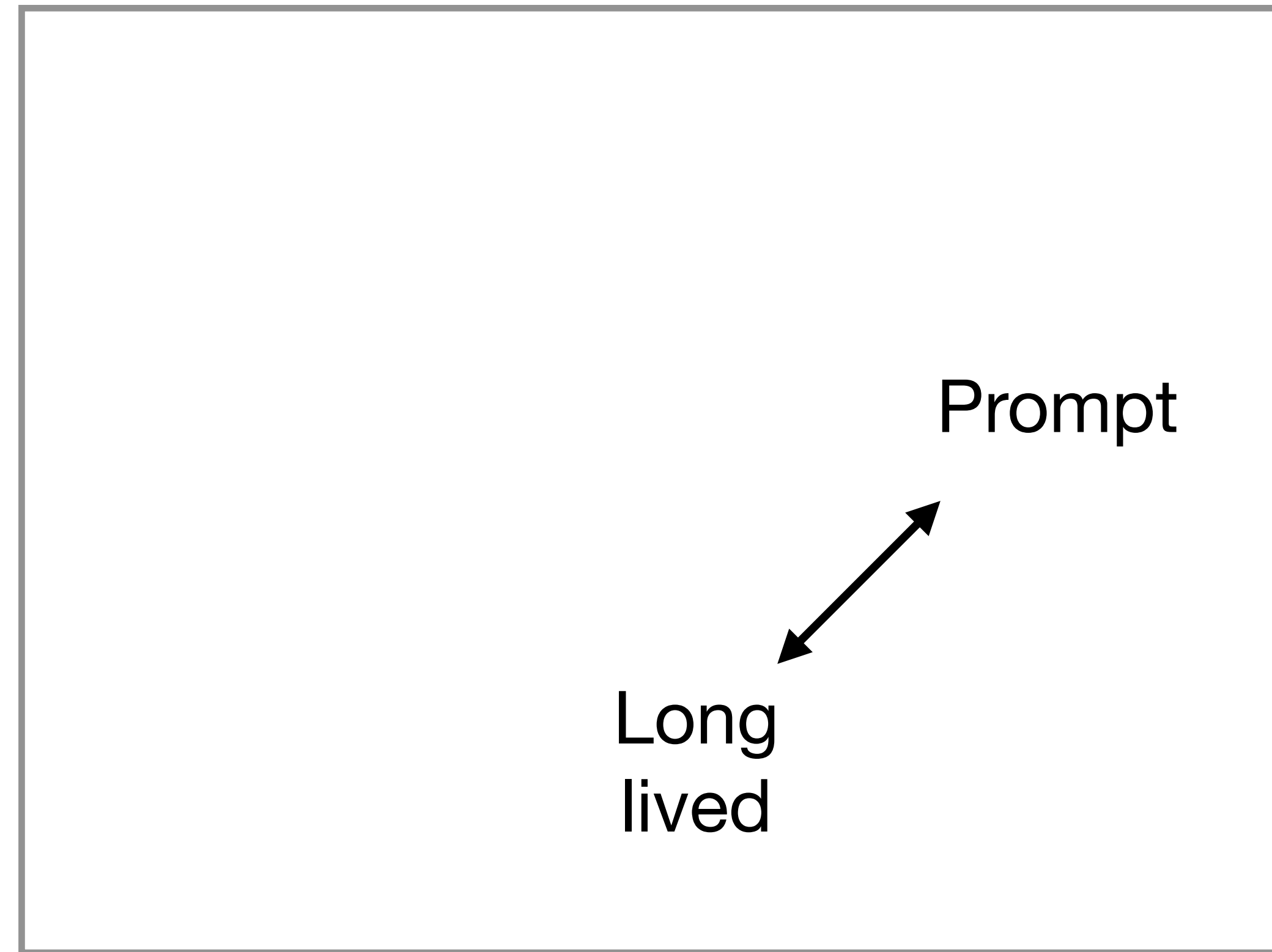


# ALPs at colliders



$g_a X X$

Beam dumps



Prompt

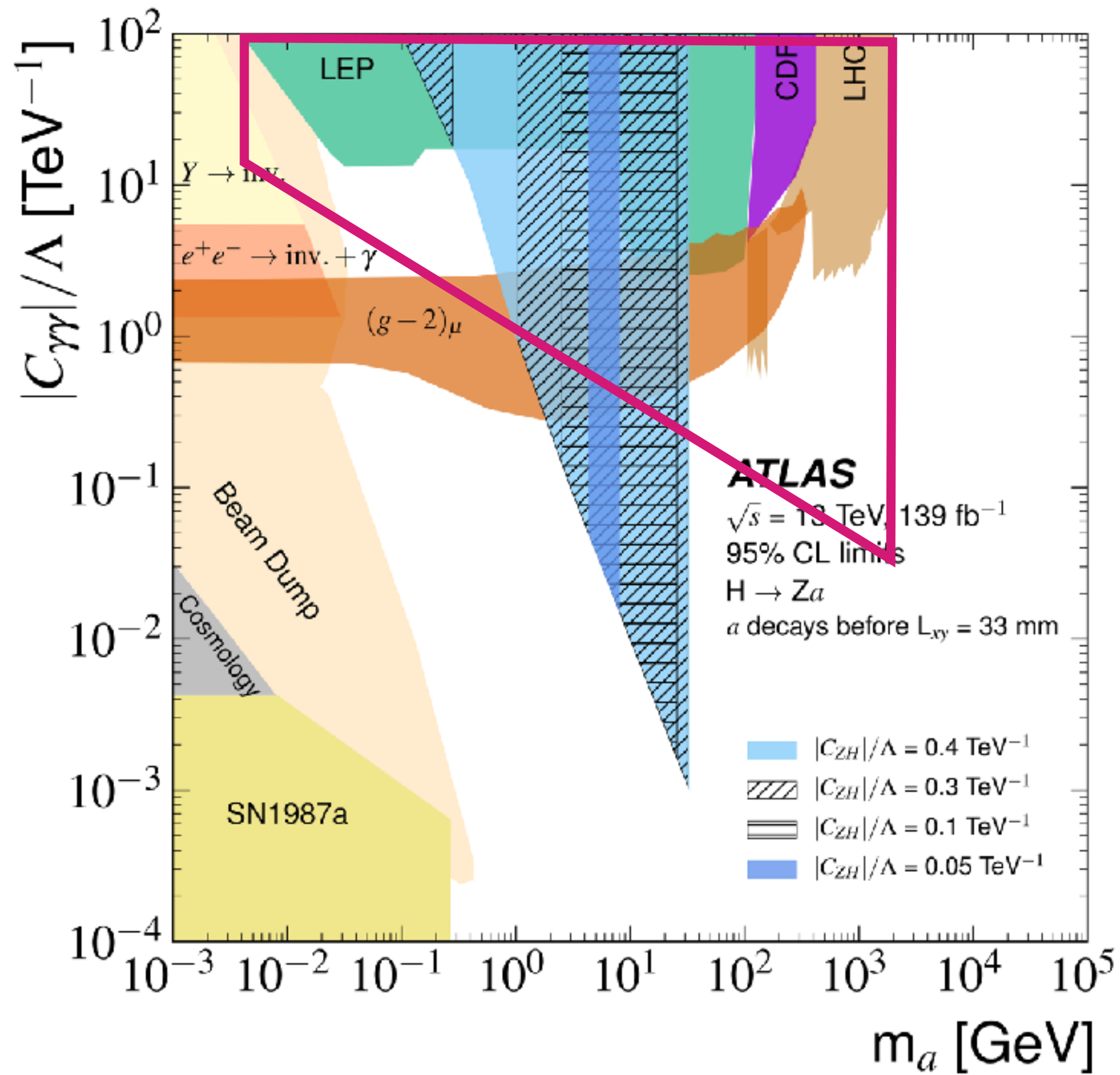
Long lived

$m_a$

[ATLAS (2312.01942)]



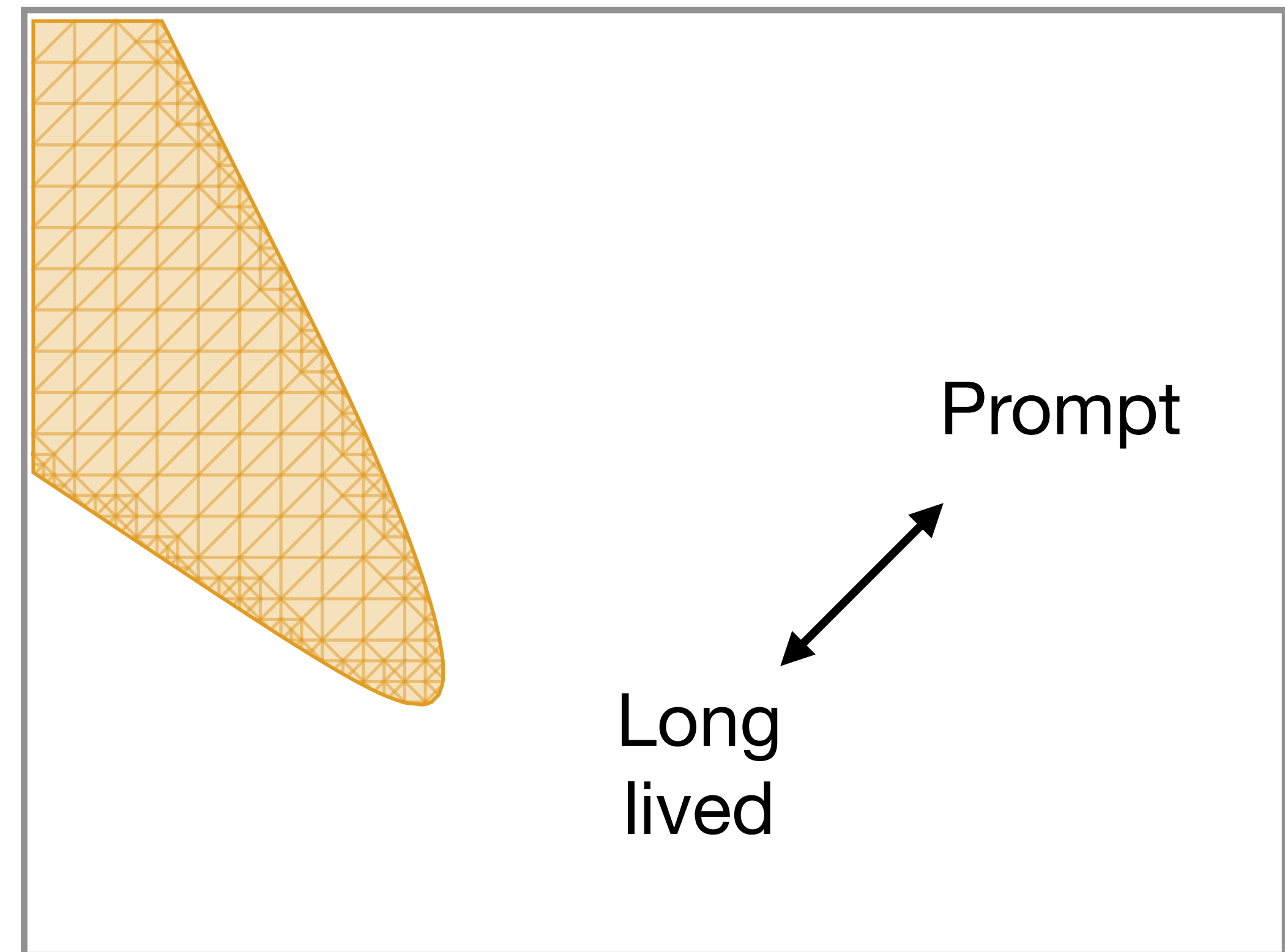
# ALPs at colliders



[ATLAS (2312.01942)]

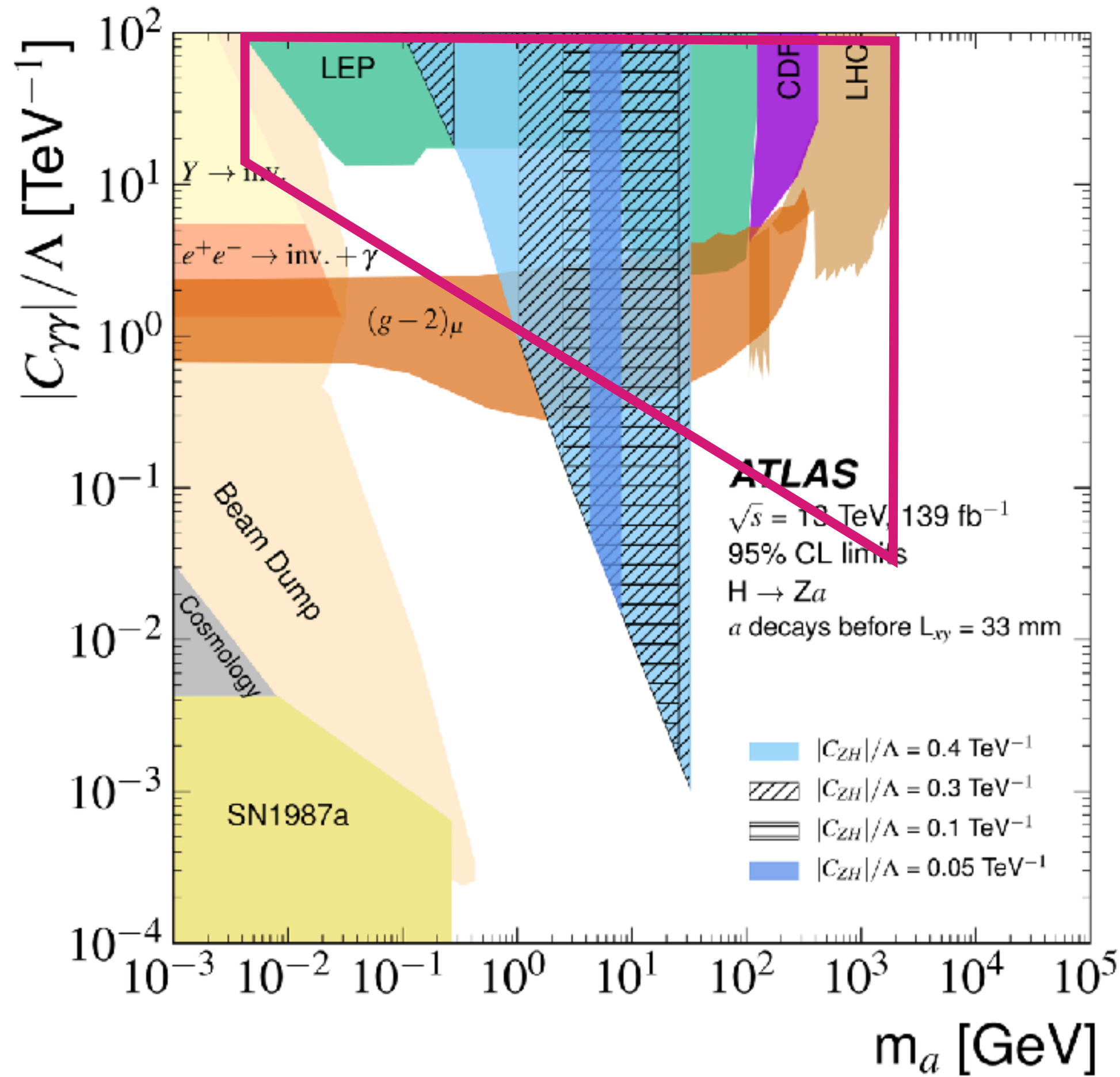
Beam dumps

$g_a X X$



$$\exp\left(-\frac{L_a}{L_{\text{det}}}\right) = \exp\left(-\frac{\beta c}{\Gamma_a L_{\text{det}}}\right)$$

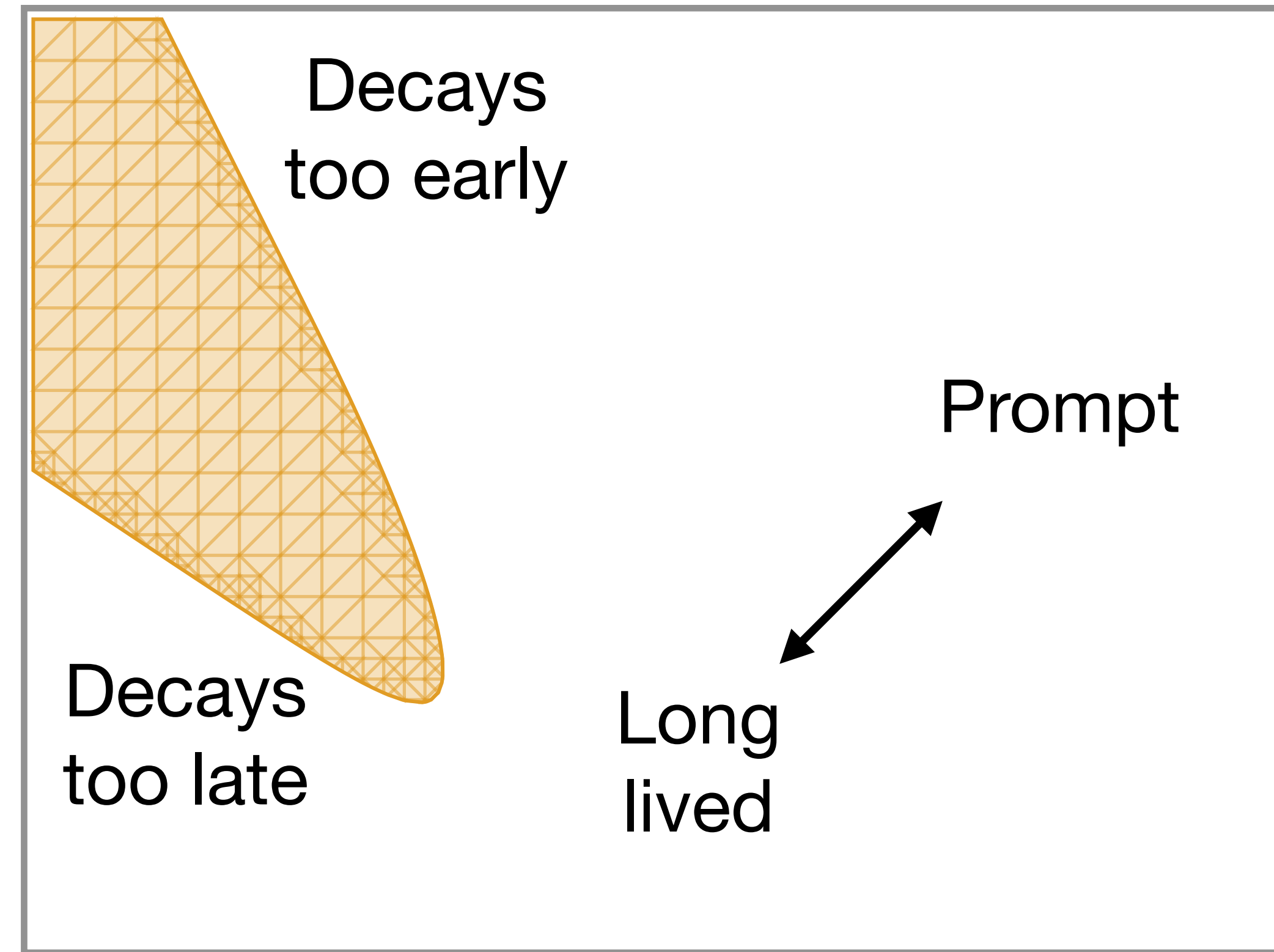
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[ATLAS (2312.01942)]

Beam dumps

$g_a X X$

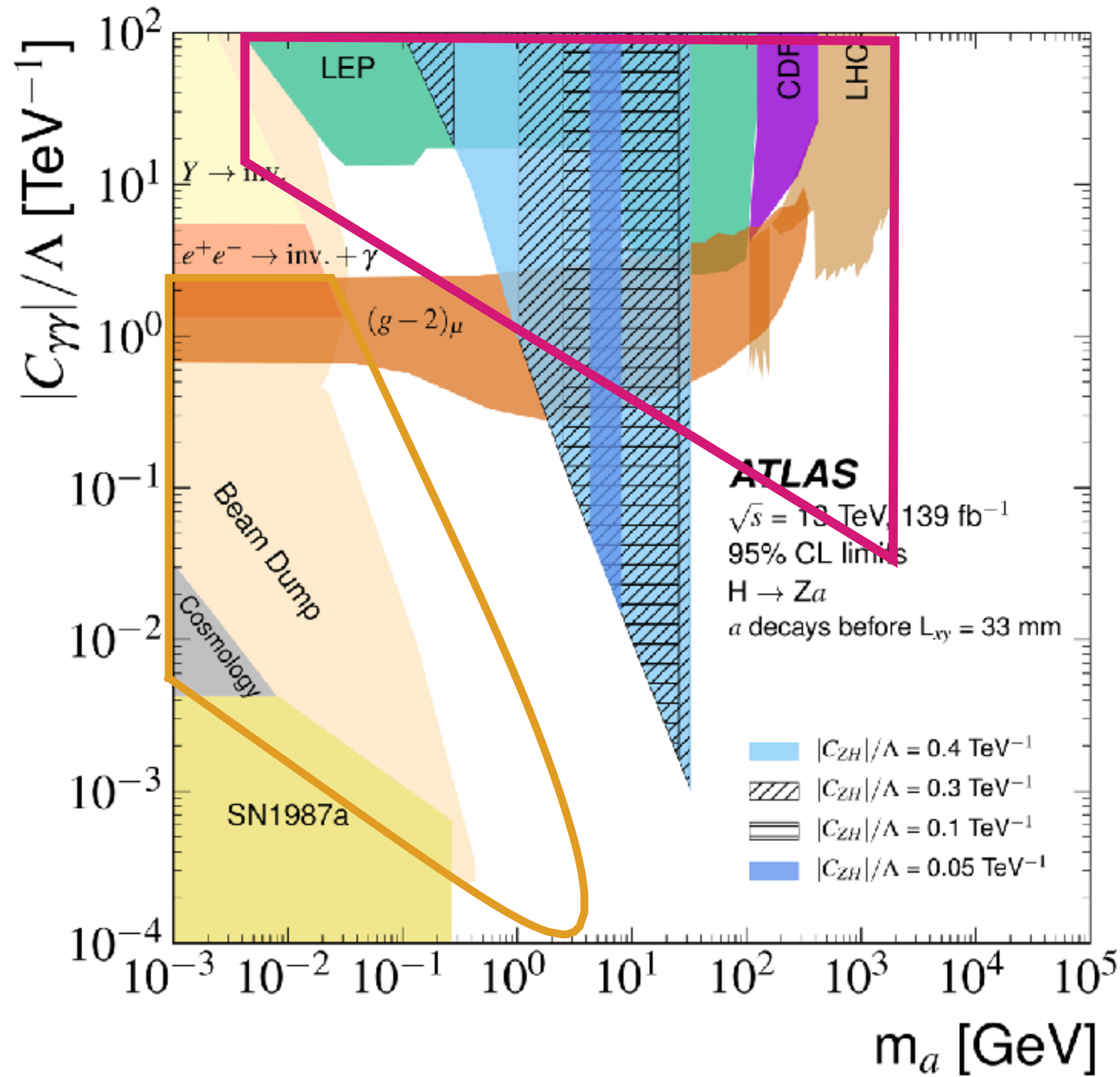


Decay length  $L_a$

$m_a$

$$\exp\left(-\frac{L_a}{L_{\text{det}}}\right) = \exp\left(-\frac{\beta c}{\Gamma_a L_{\text{det}}}\right)$$

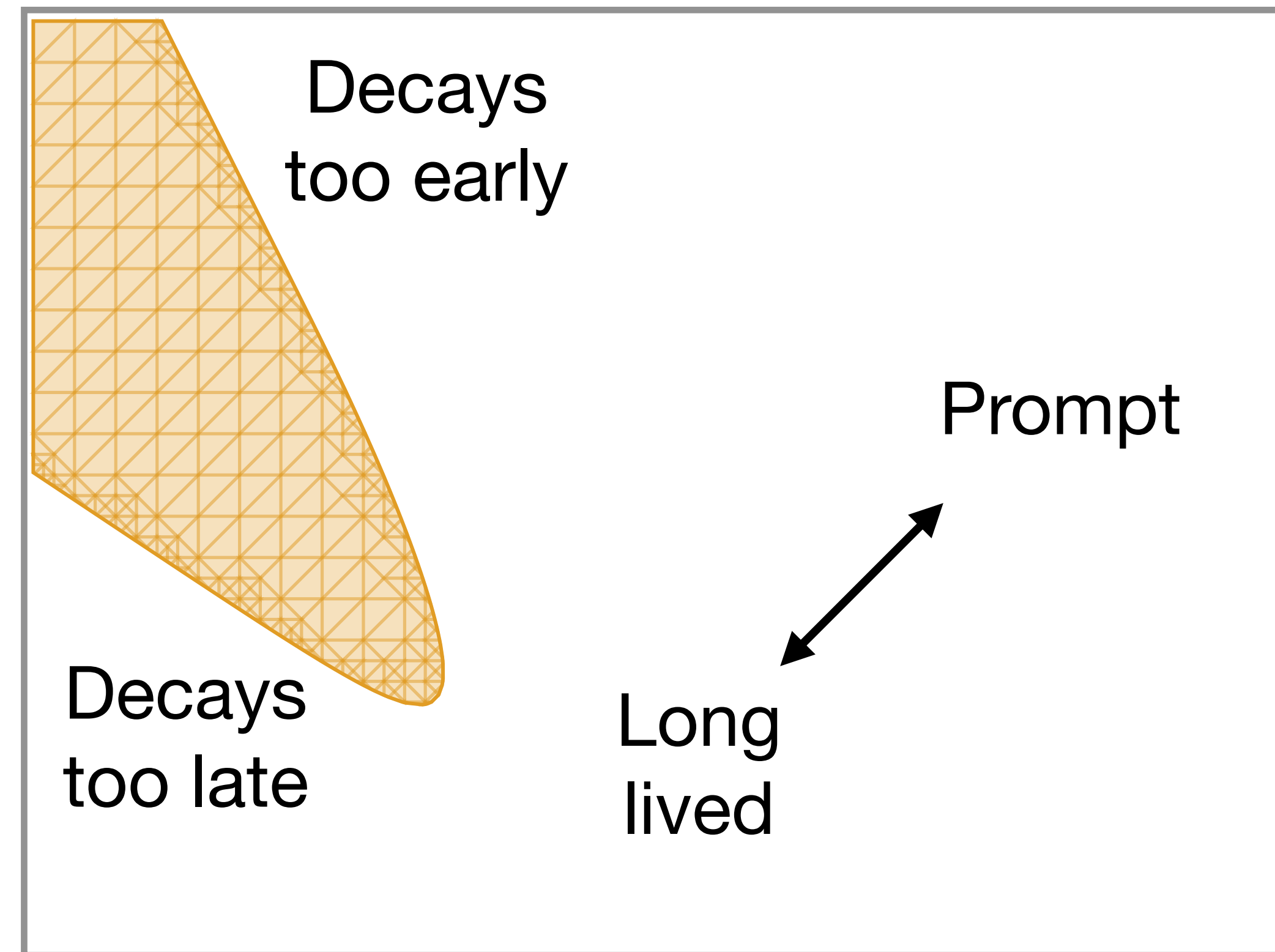
# ALPs at colliders



[ATLAS (2312.01942)]

Beam dumps

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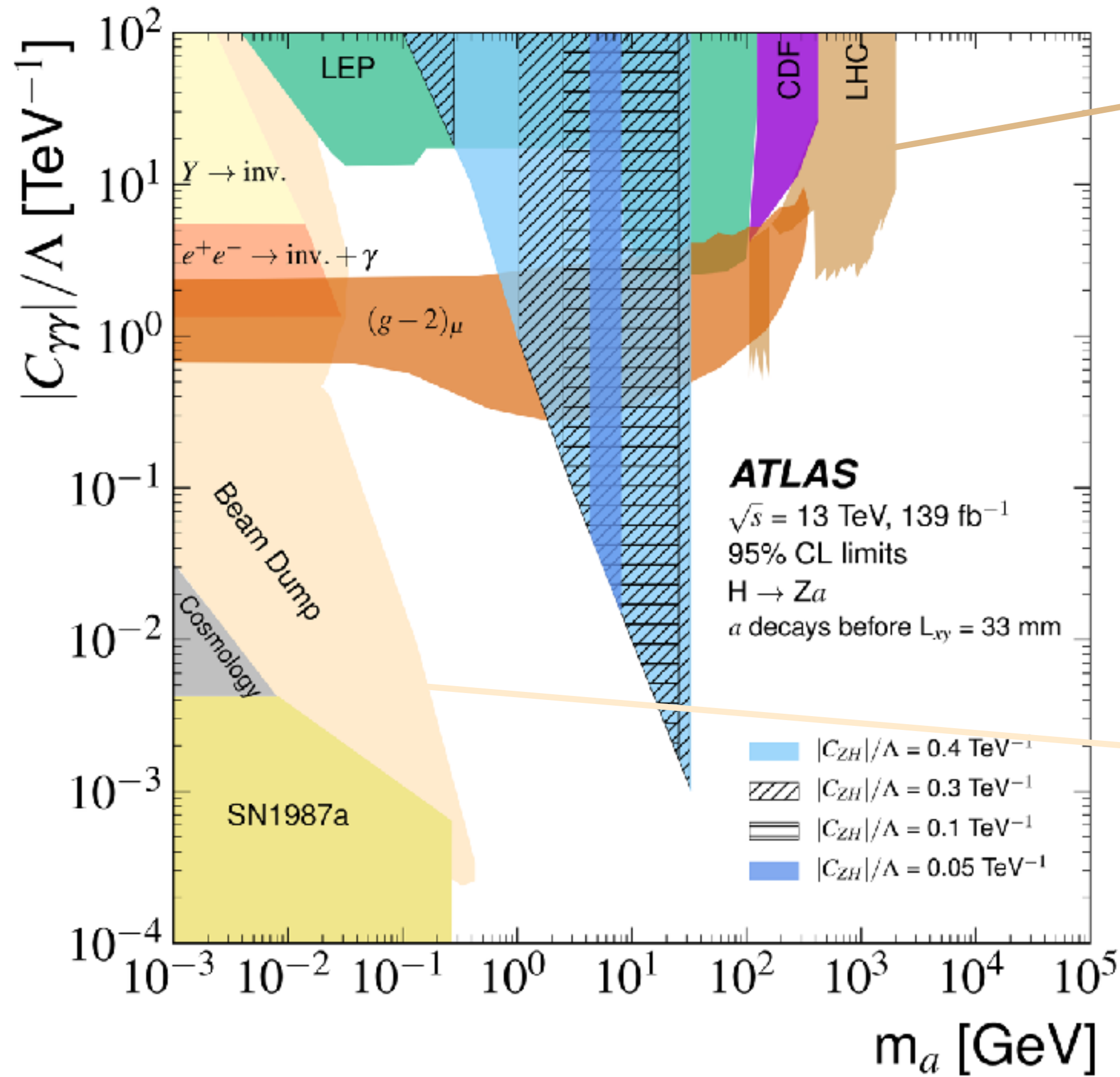
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$$\exp\left(-\frac{L_a}{L_{\text{det}}}\right) = \exp\left(-\frac{\beta c}{\Gamma_a L_{\text{det}}}\right)$$



# 2D ALP bounds



[ATLAS (2312.01942)]

## LHC limits

$$pp \rightarrow a \rightarrow \gamma\gamma$$

Mass-dependent (resonance search)

Assuming  $\text{BR}(a \rightarrow \gamma\gamma) = 100\%$

$\text{BR}(a \rightarrow ZZ)?$

$\text{BR}(a \rightarrow Z\gamma)?$

## Beam dump limits

Can be changed (or invalidated) if  
 $a \rightarrow e^+e^-$  decay possible

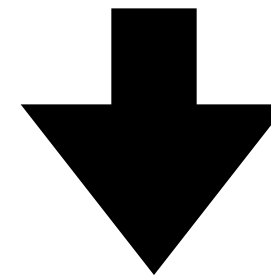


# ALPs and top quarks

# ALP Lagrangian

derivative  
basis

$$\mathcal{L}_{\text{SM}+\text{ALP}}^{D\leq 5} = c_{GG} \frac{a}{f} G_{\mu\nu}^a \tilde{G}^{a,\mu\nu} + c_{WW} \frac{a}{f} W_{\mu\nu}^A \tilde{W}^{A,\mu\nu} + c_{BB} \frac{a}{f} B_{\mu\nu} \tilde{B}^{\mu\nu} + \frac{\partial^\mu a}{f} \sum_F \bar{\psi}_F \mathbf{c}_F \gamma_\mu \psi_F$$

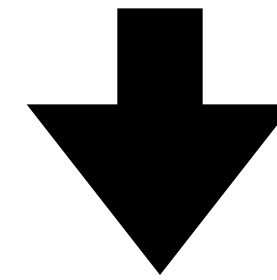


$$\psi_F \rightarrow \psi_F + i \frac{a}{f} \mathbf{c}_F \psi_F$$

# ALP Lagrangian

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$$\psi_F \rightarrow \psi_F + i \frac{a}{f} \mathbf{c}_F \psi_F$$

pseudoscalar  
basis

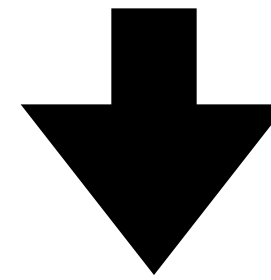
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$$\tilde{Y}_u = i(Y_u c_u - c_Q Y_u), \quad \tilde{Y}_d = i(Y_d c_d - c_Q Y_d), \quad \tilde{Y}_e = i(Y_e c_e - c_L Y_e)$$

# ALP Lagrangian

derivative  
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$$\tilde{c}_X = c_X \mathbb{1}_3 \quad \text{Flavor universal}$$

$$\tilde{Y}_u = i(c_u - c_Q) Y_u = -iC_u Y_u, \quad \tilde{Y}_d = i(c_d - c_Q) Y_d = -iC_d Y_d, \quad \tilde{Y}_e = i(c_e - c_L) Y_e = -iC_e Y_e$$



# ALP couplings to top quarks

$$\mathcal{L}_{\text{ferm}} = -\frac{a}{f} \left( C_u i\bar{Q}\tilde{H} Y_u u_R + C_d i\bar{Q}H Y_d d_R + C_e i\bar{L}H Y_e e_R + \text{h.c.} \right)$$

- ALP-top quark couplings naturally dominant
- Consistent with minimal flavor violation (MFV)
- Promising candidate at colliders
- Recent activities:

[Esser, Madigan, Sanz, Ubiali ([2303.17634](#))]

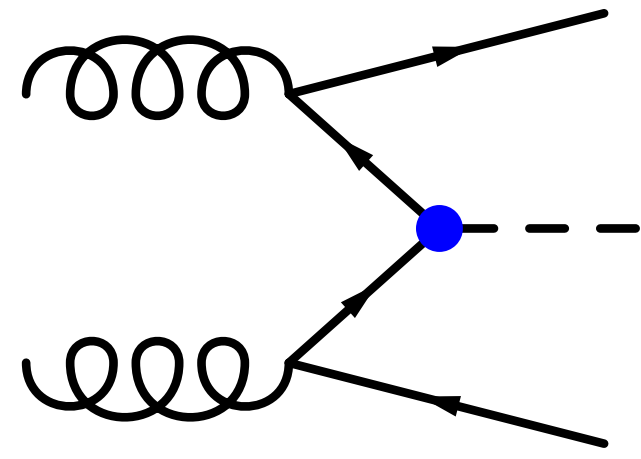
[Blasi, Maltoni, Mariotti, Mimasu, Pagani, Tentori ([2311.16048](#))]

[Phan, Westhoff ([2312.00872](#))]

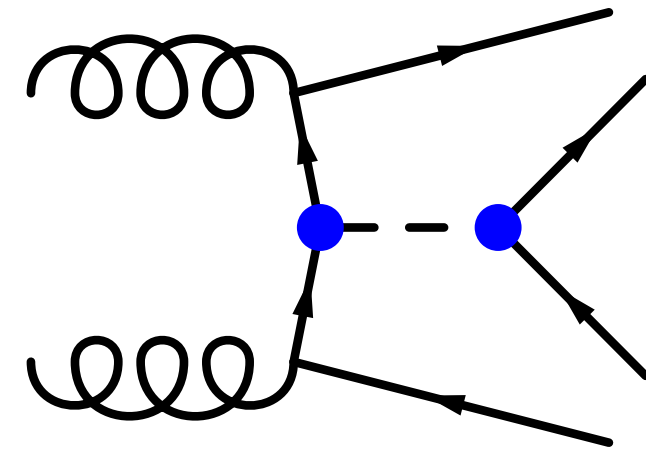
[Cheung, Lu, Ouseph, Sarmah ([2404.14833](#))]

[Anuar, AB, Biekötter, Grohsjean, Heinemeyer, Jeppe, Schwanenberger, Weiglein ([2404.19014](#))]

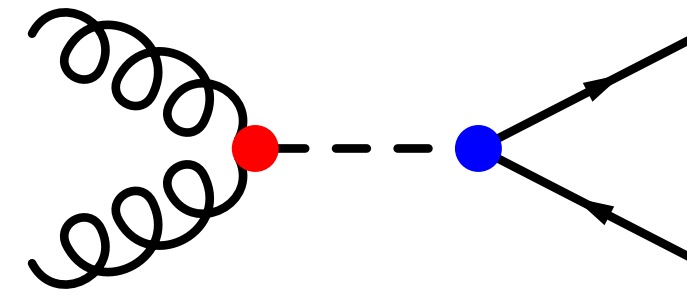
# ALPs and tops @ colliders



$t\bar{t}a$

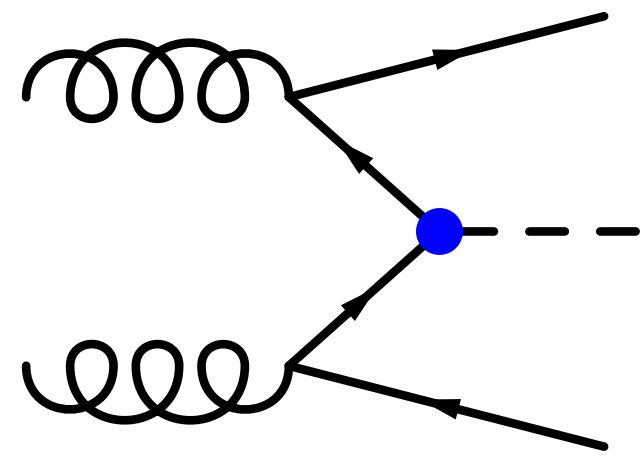


$t\bar{t}t\bar{t}$



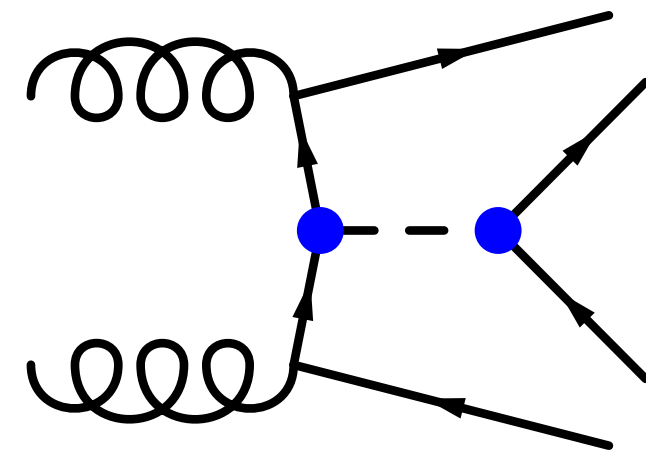
$t\bar{t}$

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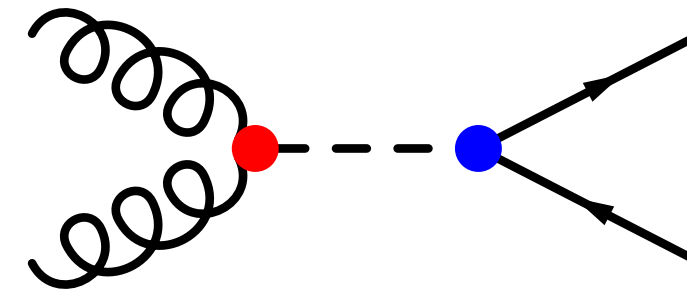


$$t\bar{t}a \rightarrow t\bar{t}(f\bar{f})$$

$$\rightarrow t\bar{t} + \text{MET}$$

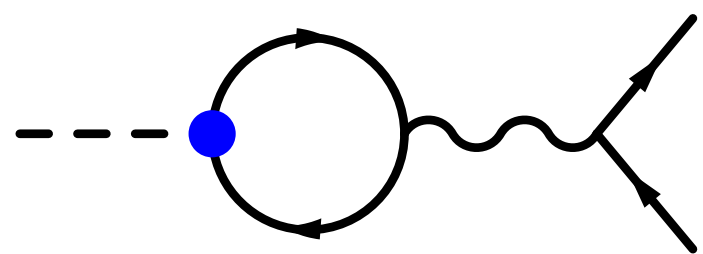


$$t\bar{t}t\bar{t}$$

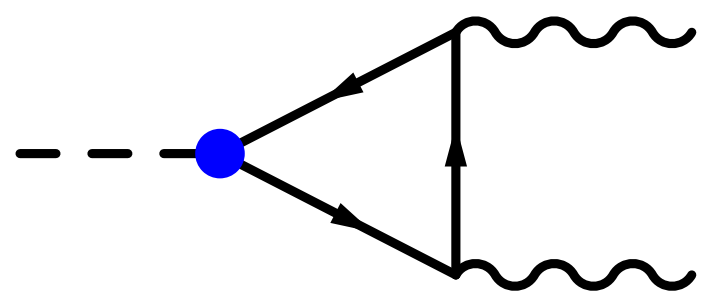


$$t\bar{t}$$

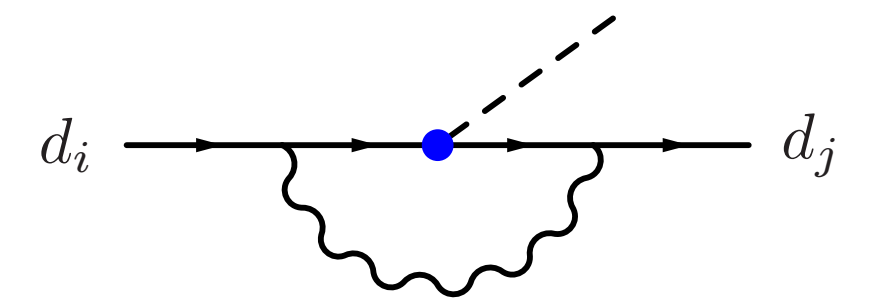
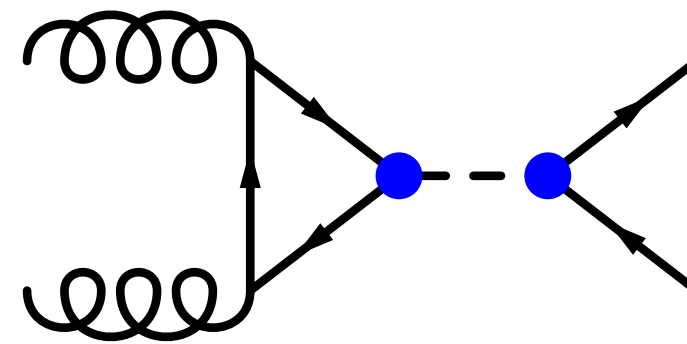
## Loop effects



$$a \rightarrow f\bar{f}$$



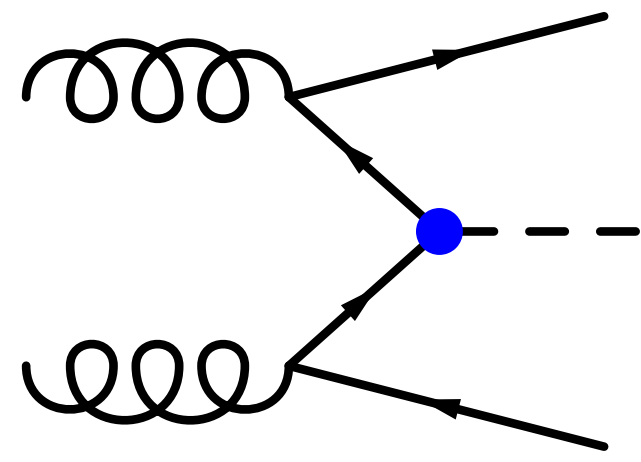
$$a \rightarrow VV$$



$$B \rightarrow Ka$$

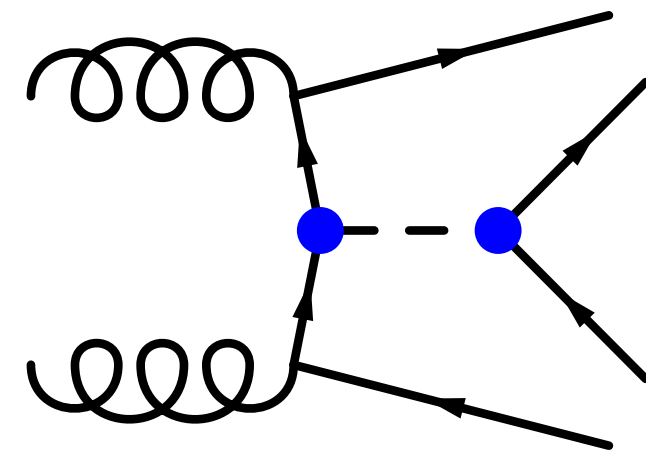
$$K \rightarrow \pi a$$

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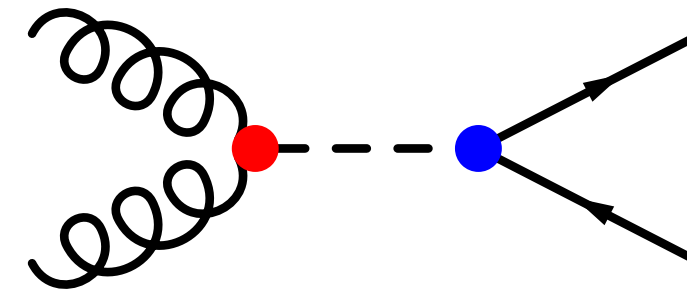


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$$t\bar{t}t\bar{t}$$



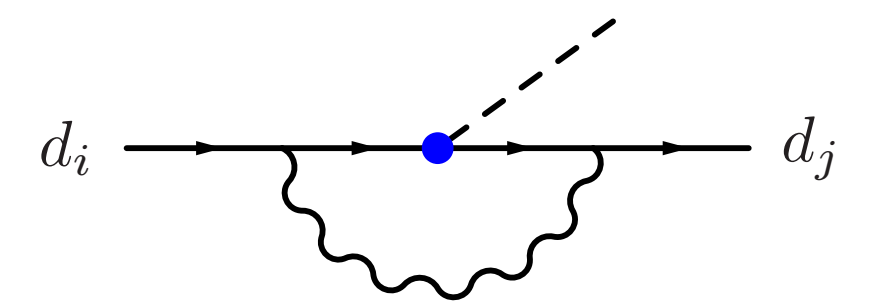
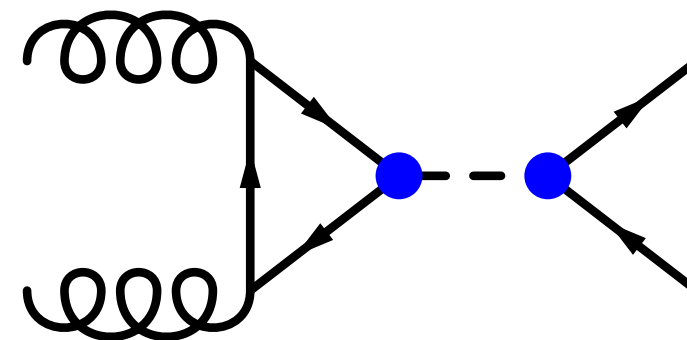
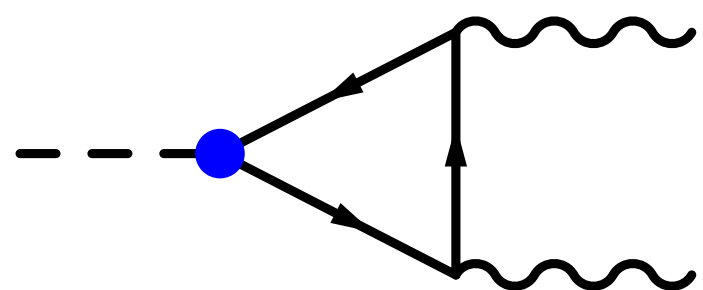
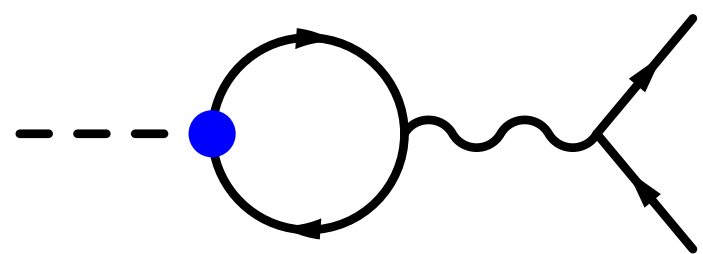
$$t\bar{t}$$

## Loop effects

$$c_f(m_t) \sim \frac{y_t^2}{16\pi^2} \log \frac{\Lambda}{m_t}$$

$$a \rightarrow f\bar{f}$$

$$a \rightarrow VV$$



$$B \rightarrow Ka$$

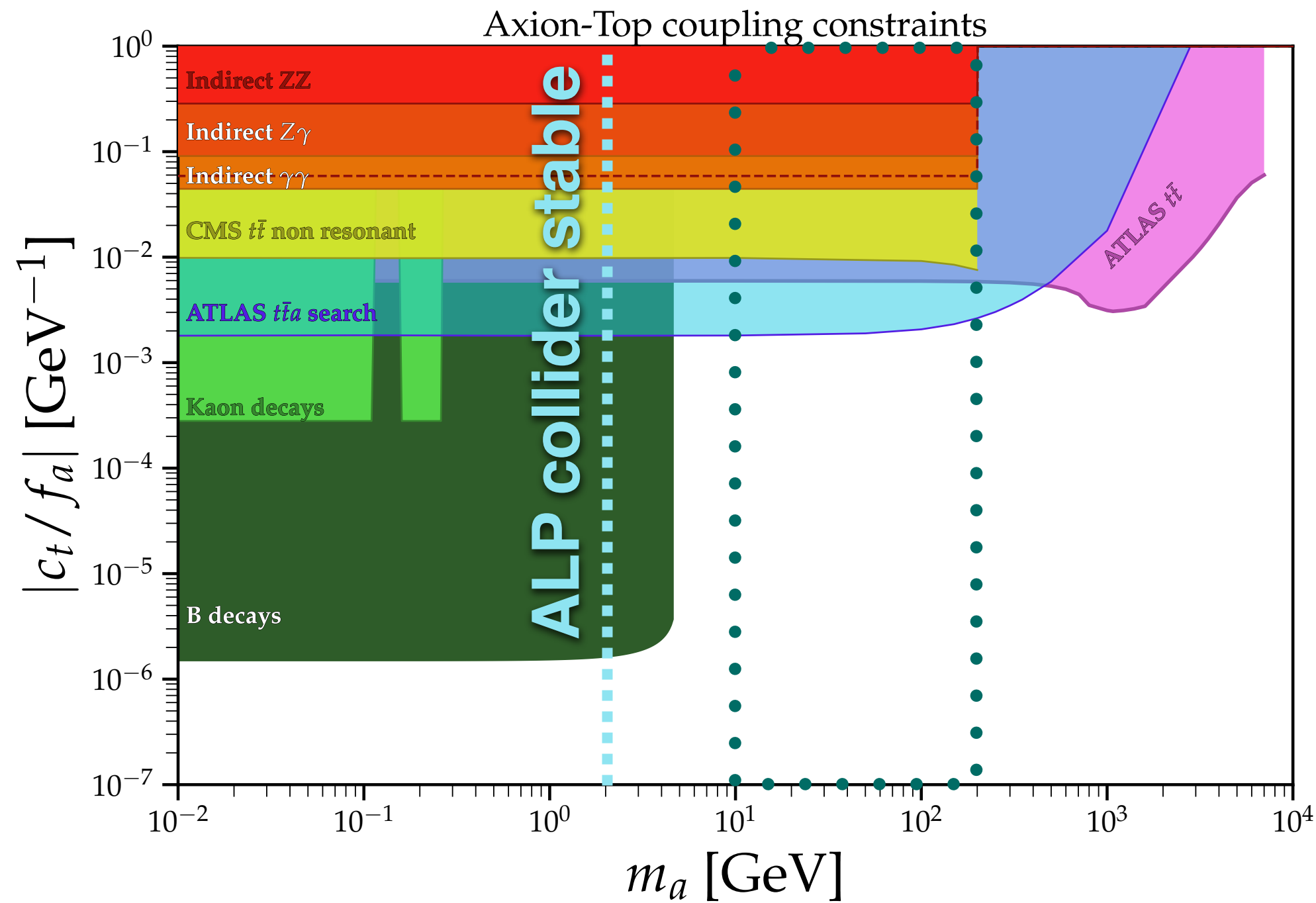
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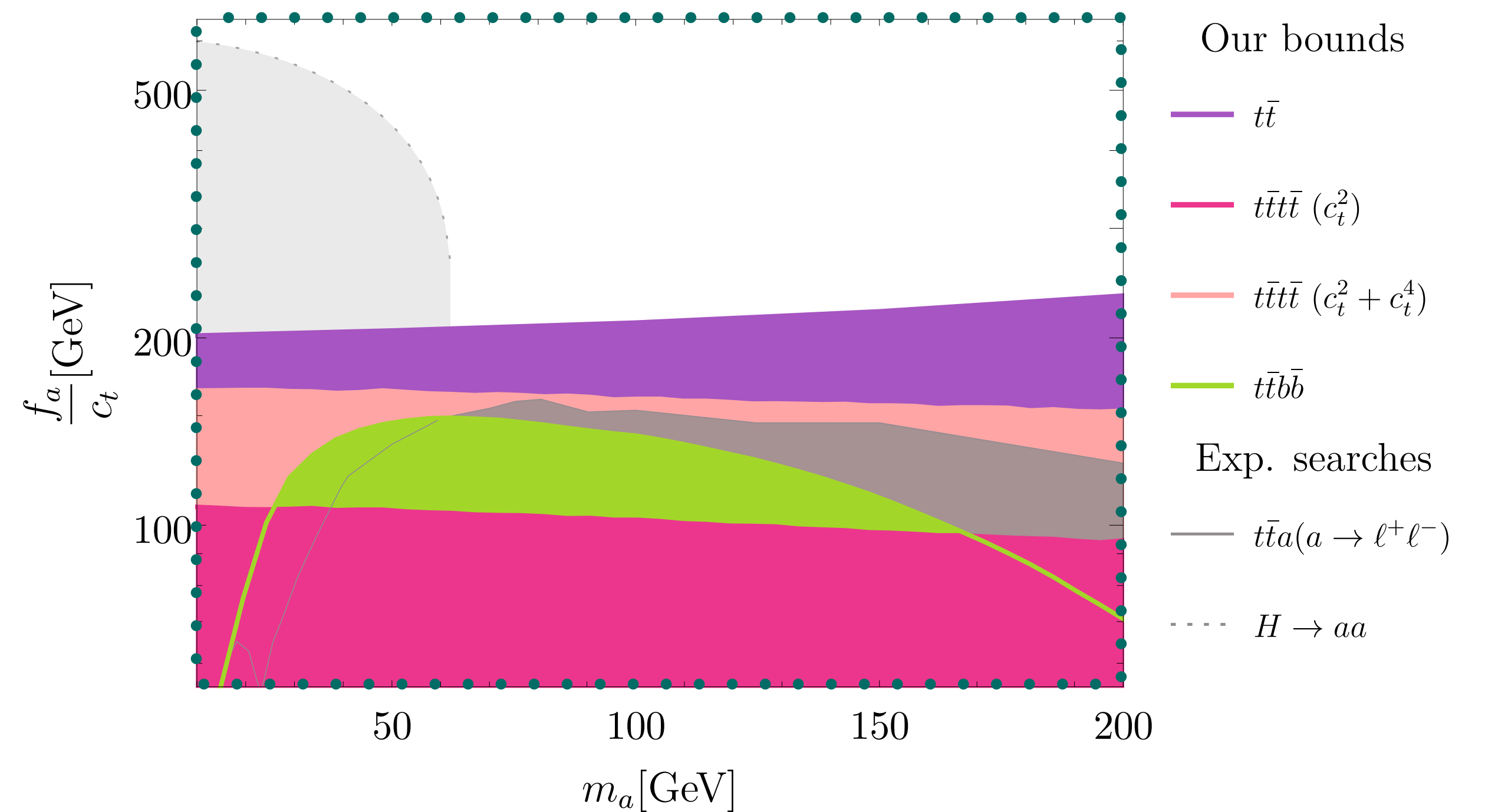
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see also [Phan, Westhoff ([2312.00872](#))]

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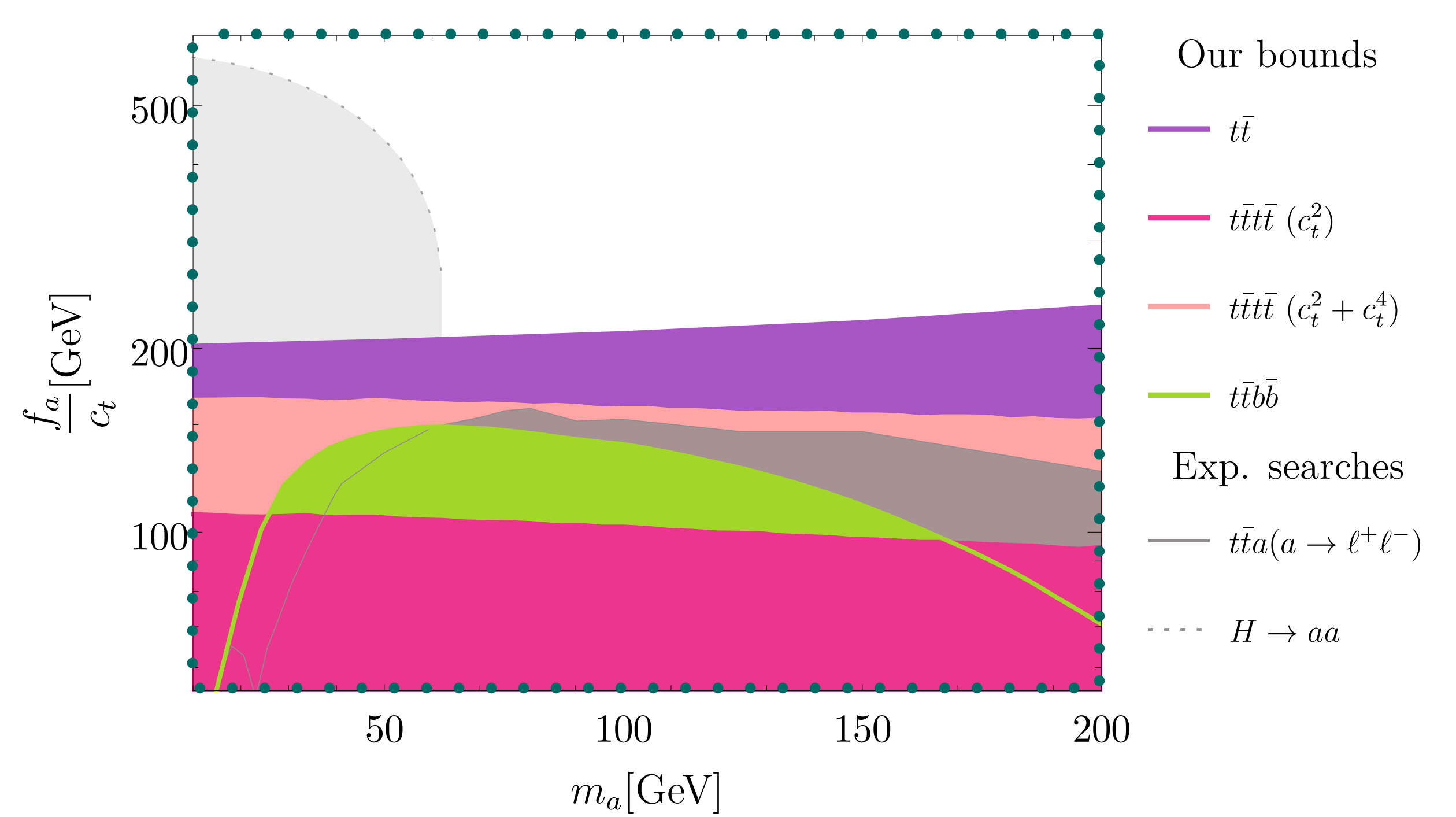
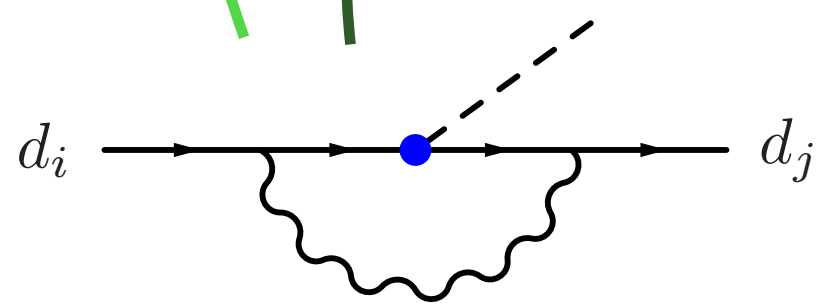
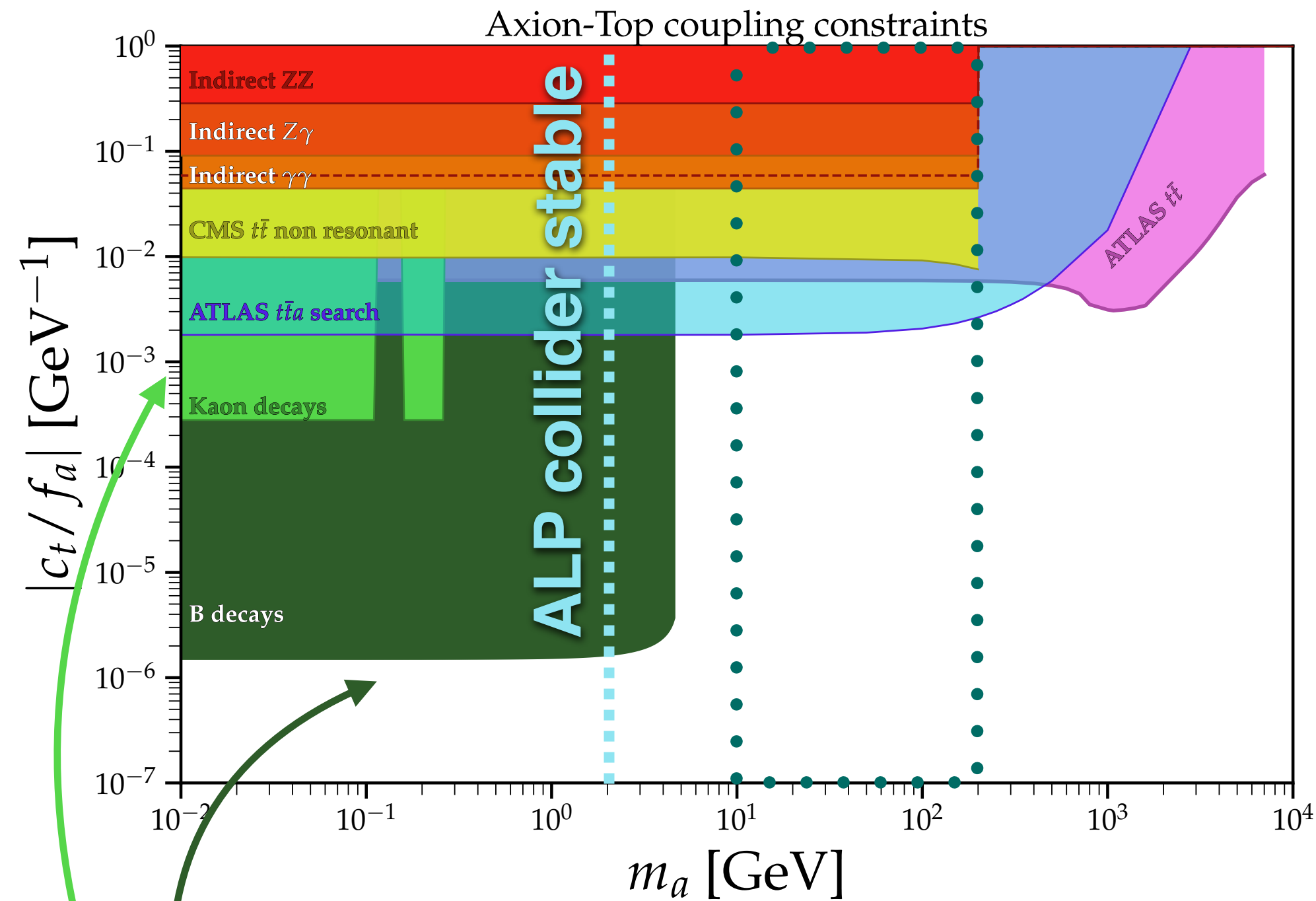
$c_t$  in derivative basis

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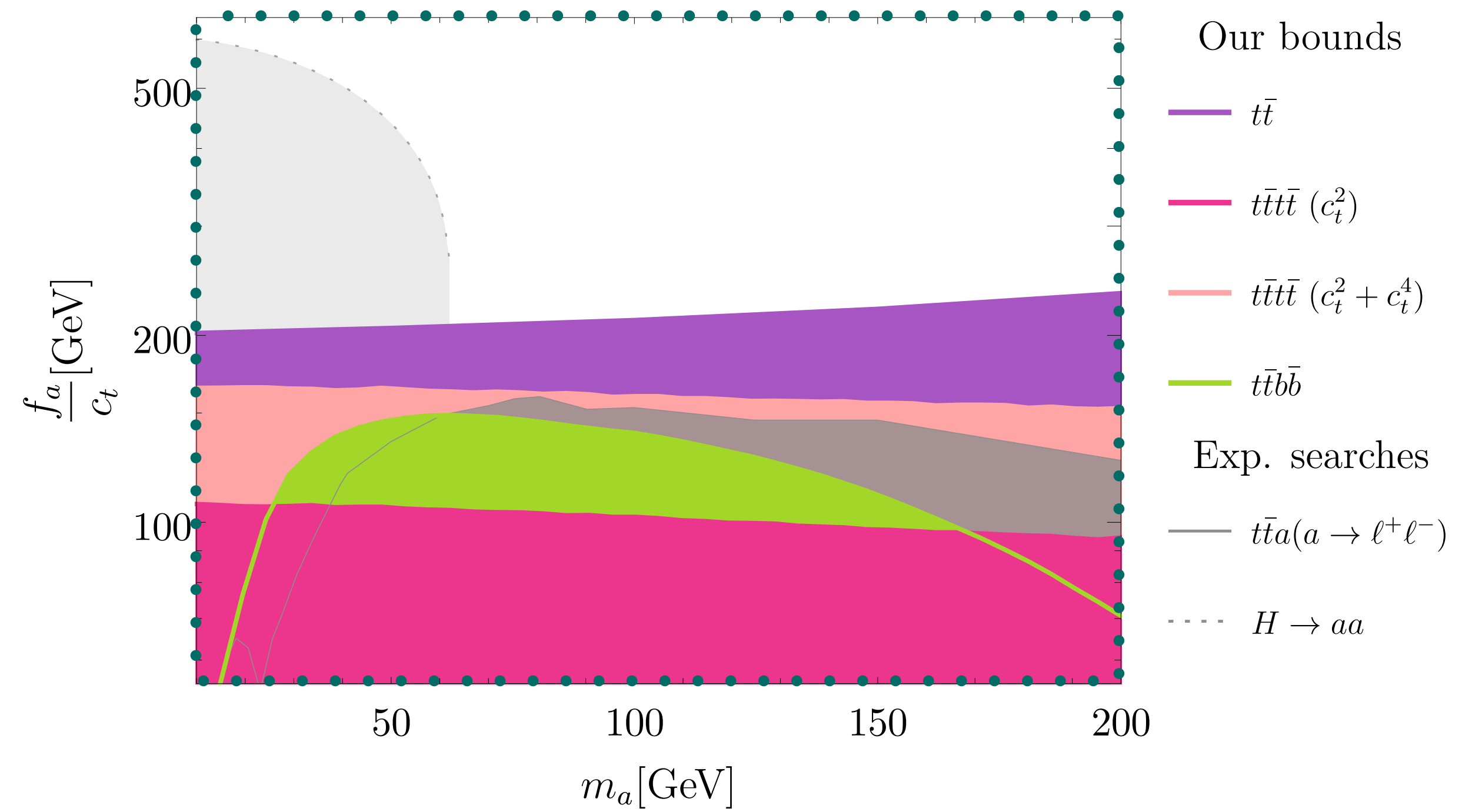
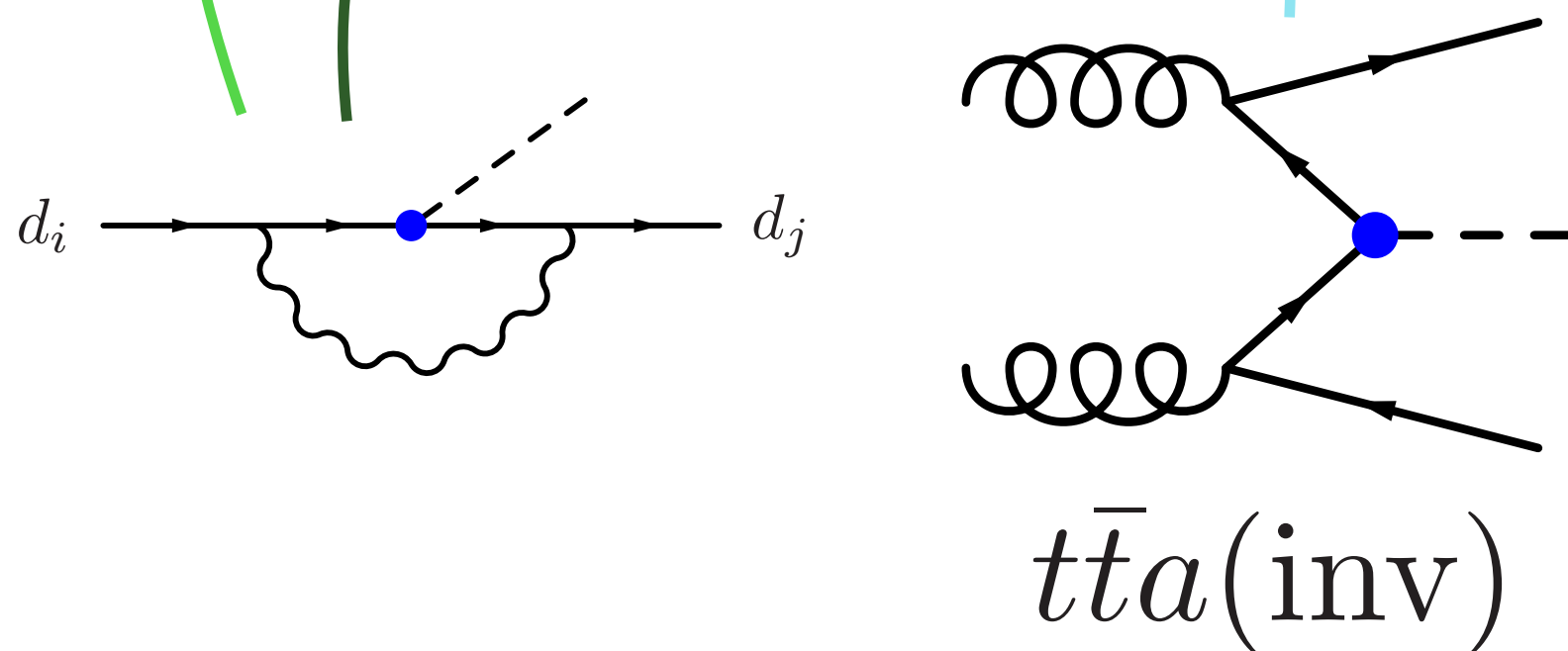
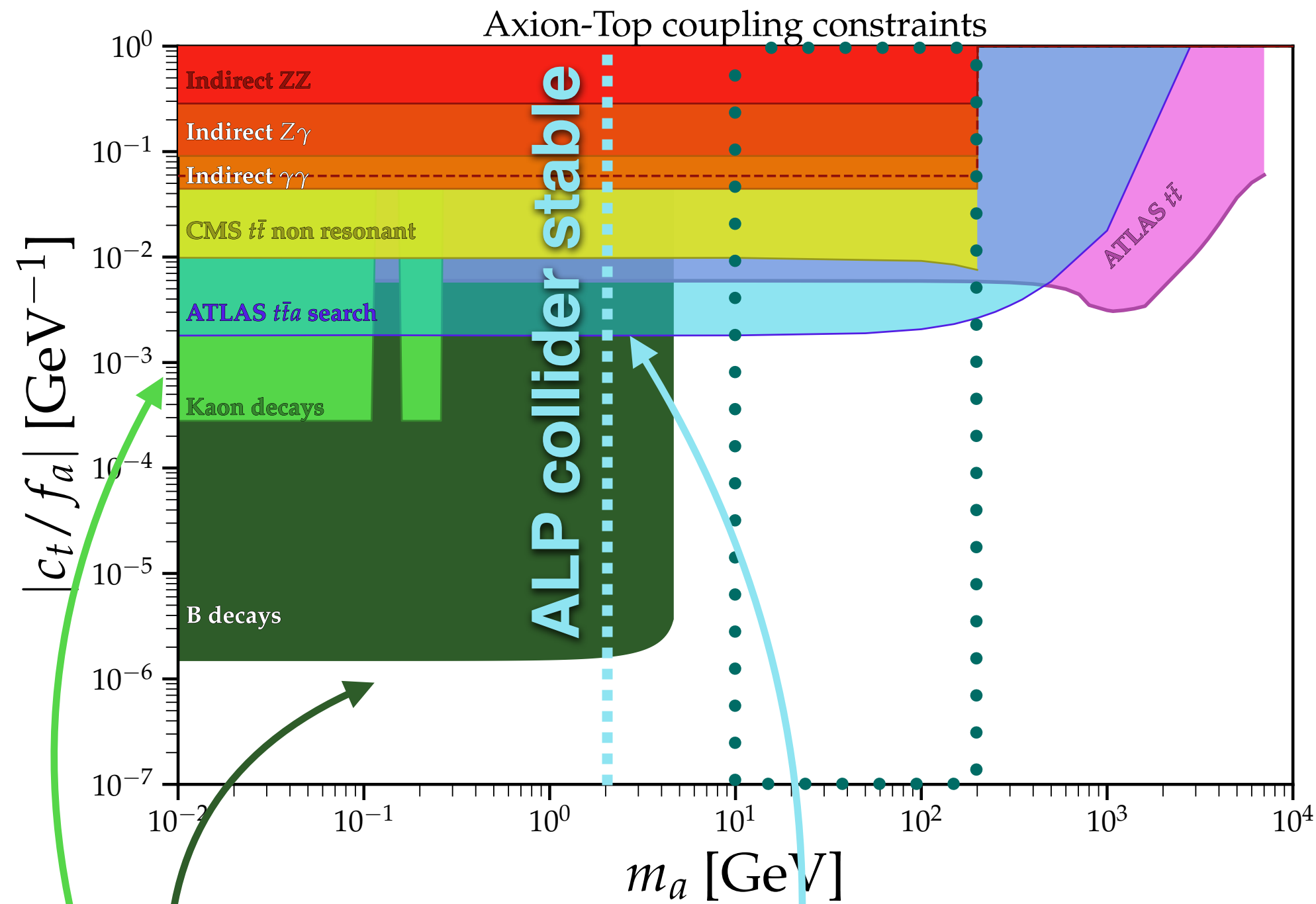
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[Blasi, Maltoni, Mariotti, Mimasu, Pagani, Tentori ([2311.16048](#))]



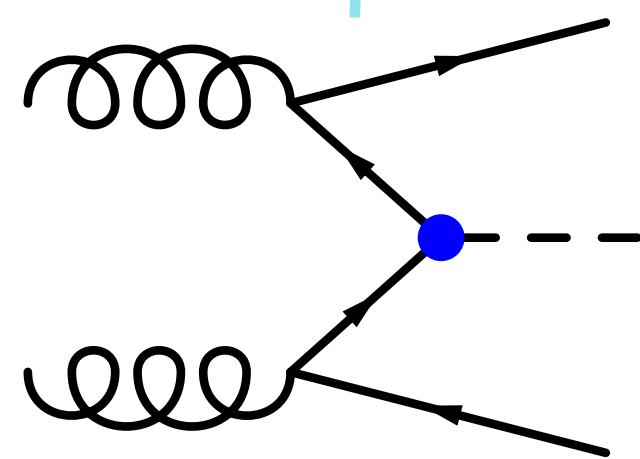
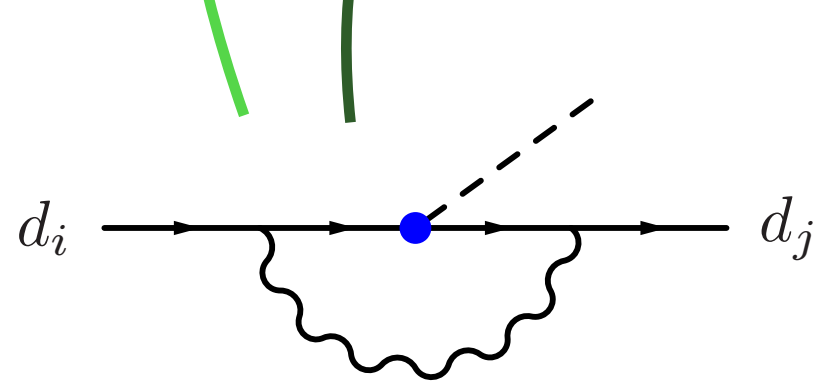
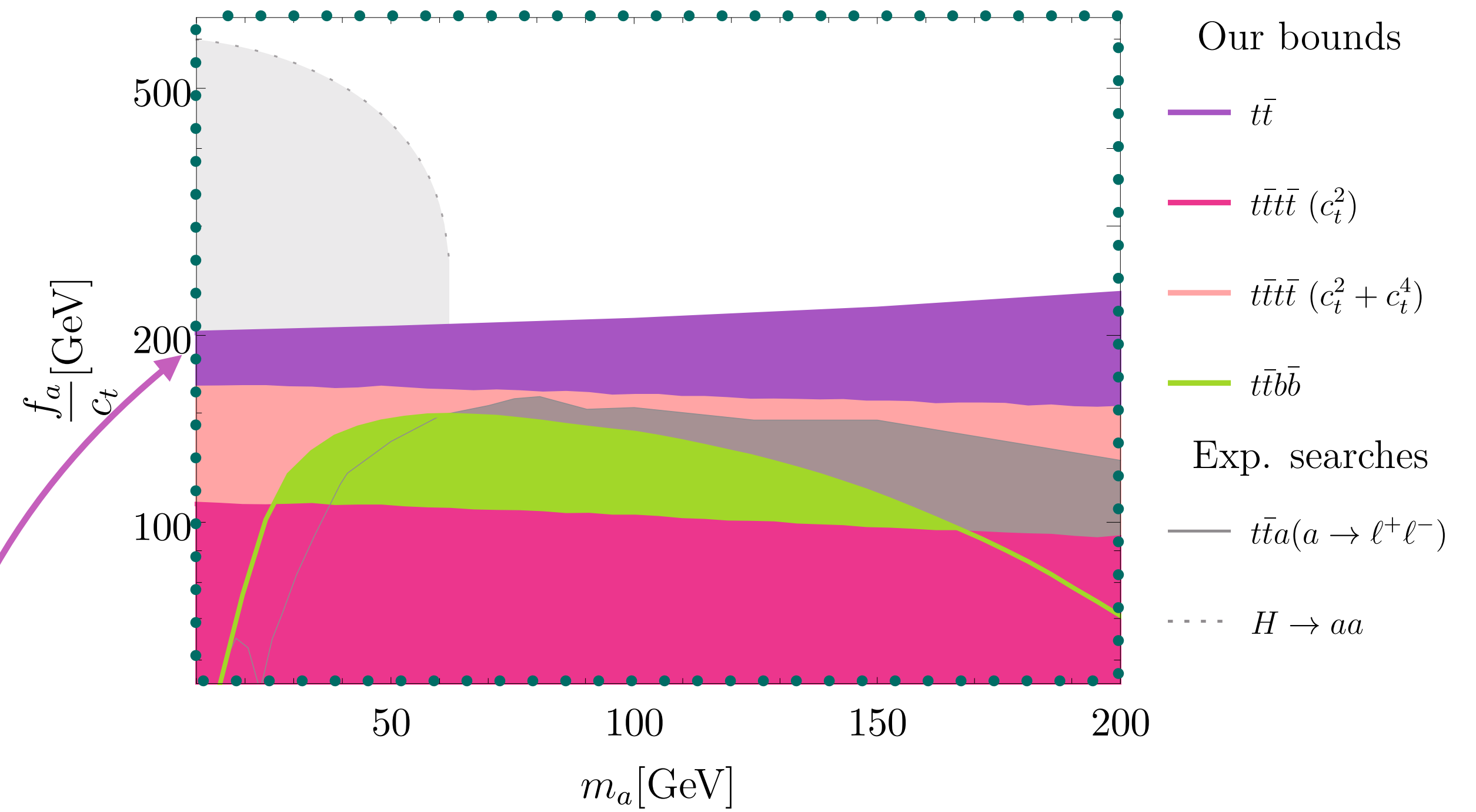
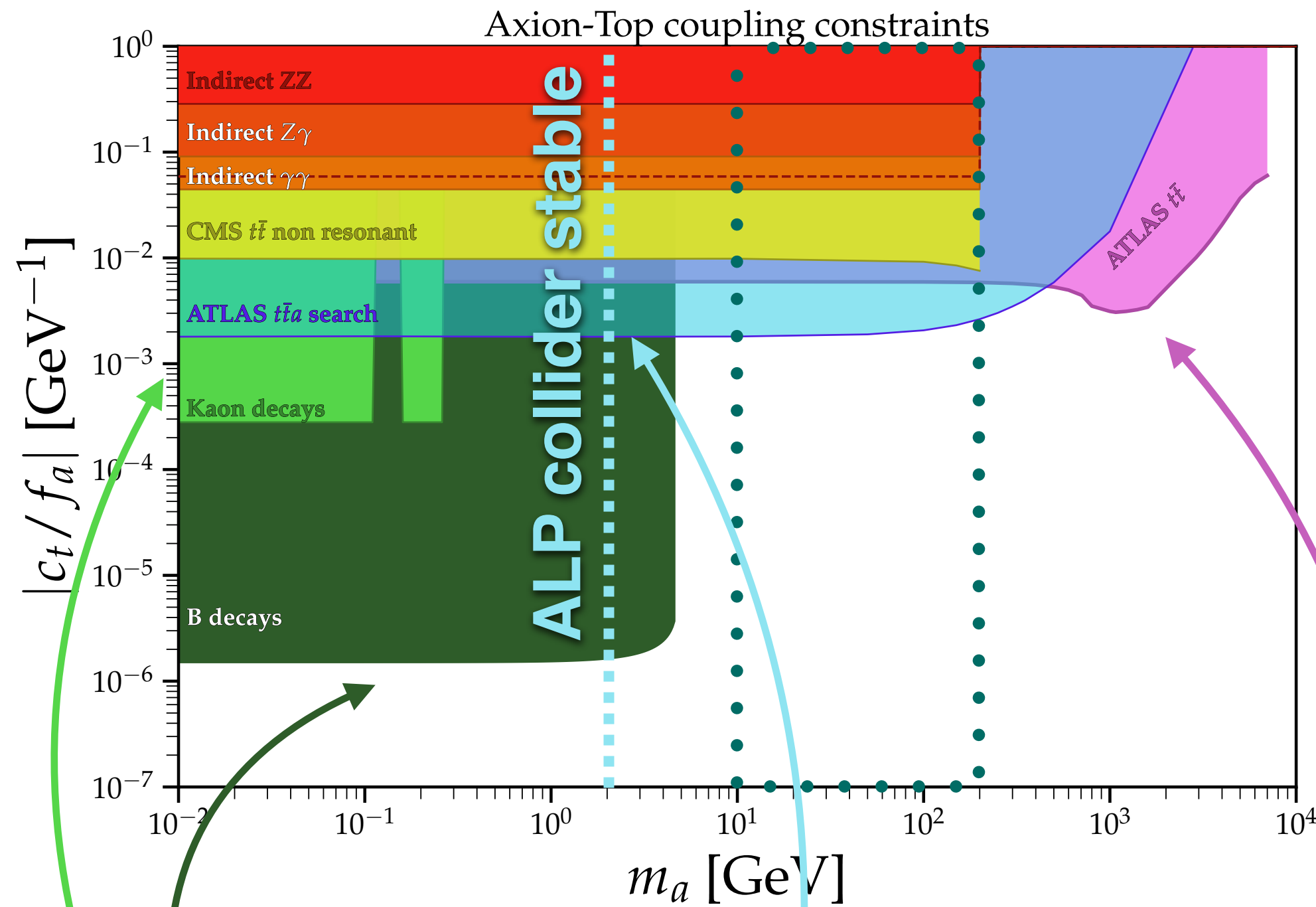
$c_t$  in derivative basis

# ALPs and tops @ colliders

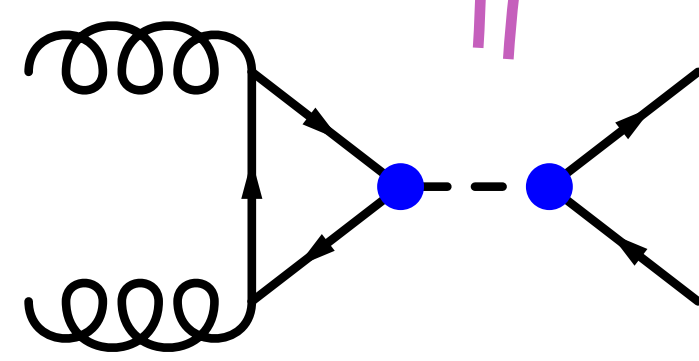
see also [Phan, Westhoff ([2312.00872](#))]

[Esser, Madigan, Sanz, Ubiali ([2303.17634](#))]

[Blasi, Maltoni, Mariotti, Mimasu, Pagani, Tentori ([2311.16048](#))]



$t\bar{t}a(\text{inv})$

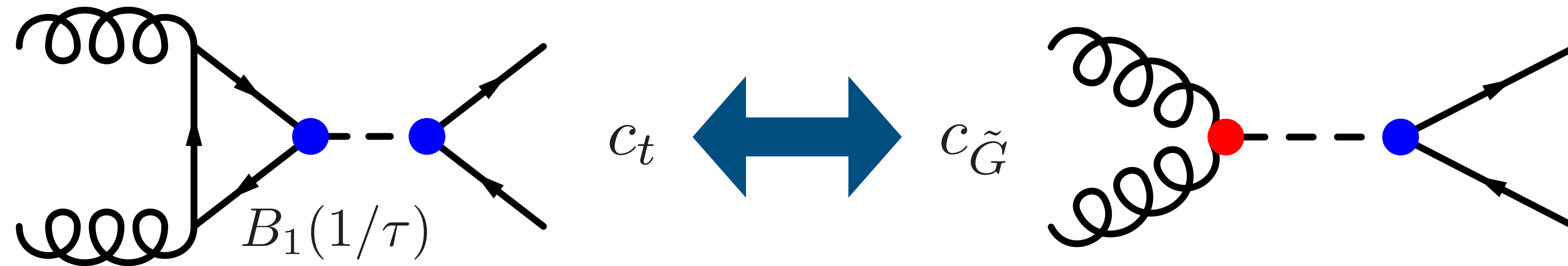


$t\bar{t}$  most relevant at high ALP masses

$c_t$  in derivative basis



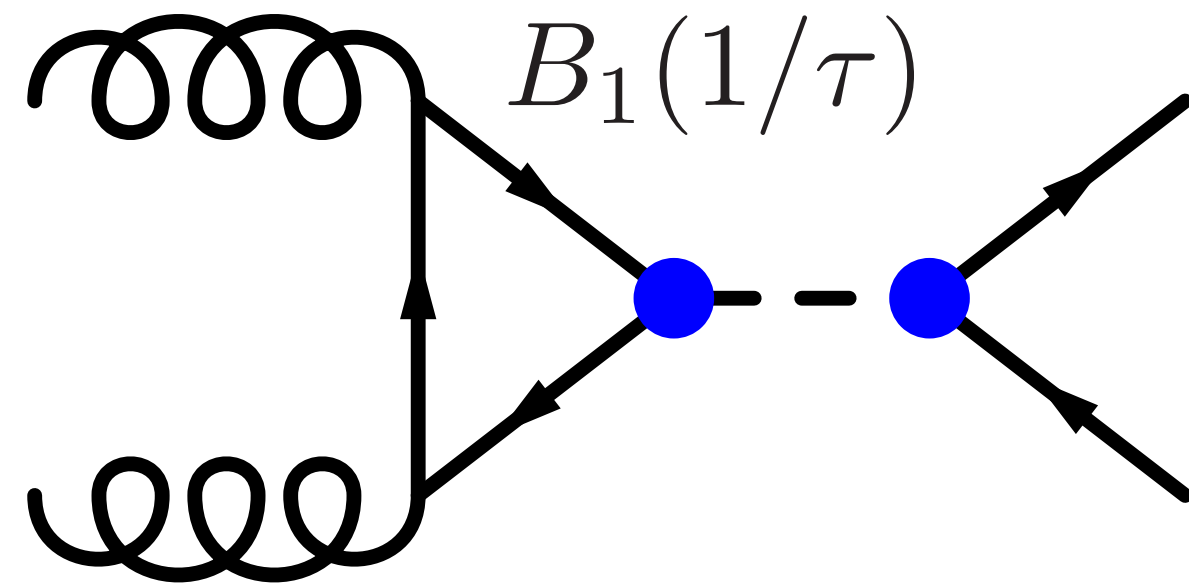
# ALP contribution to $t\bar{t}$ production



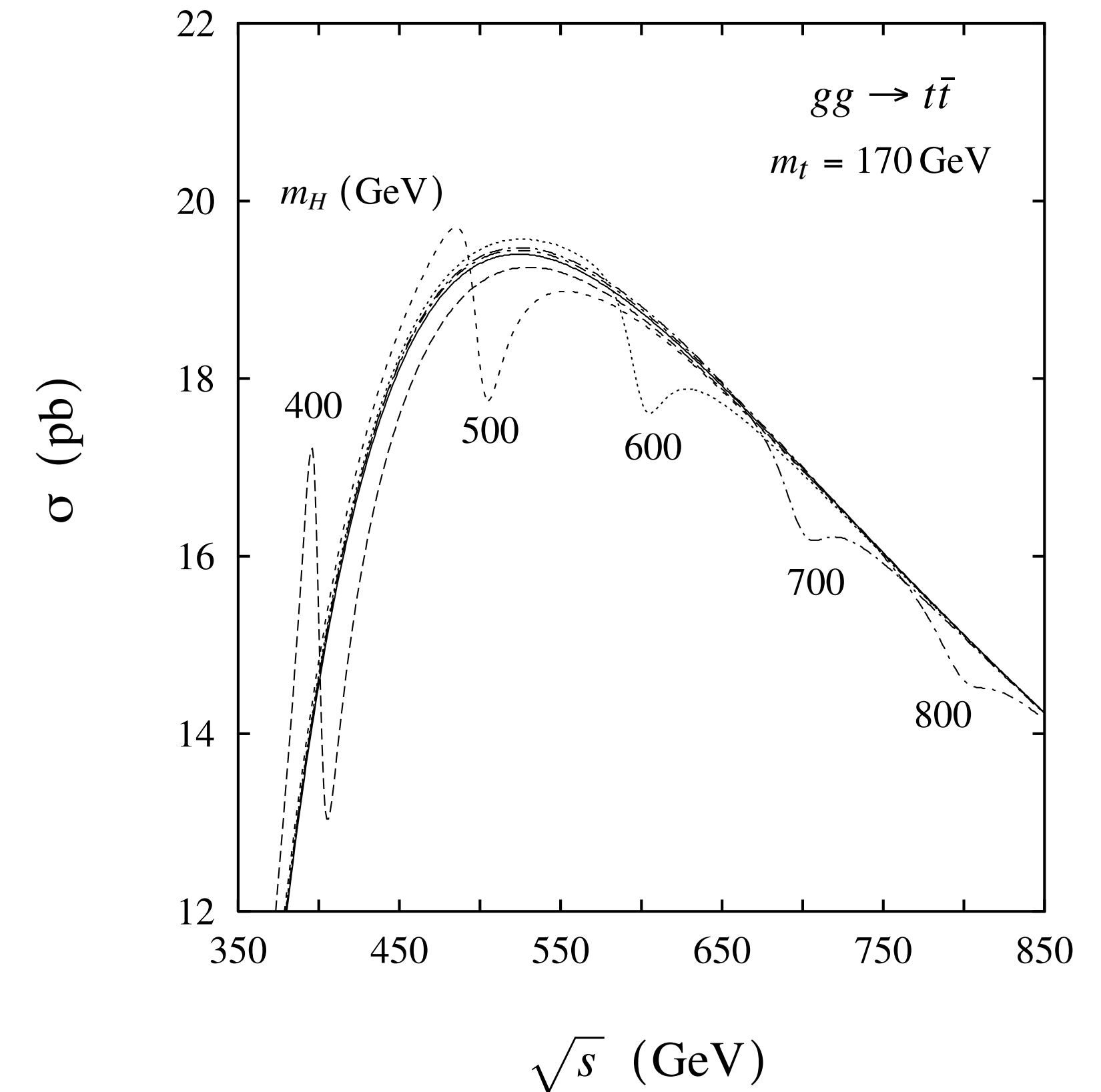
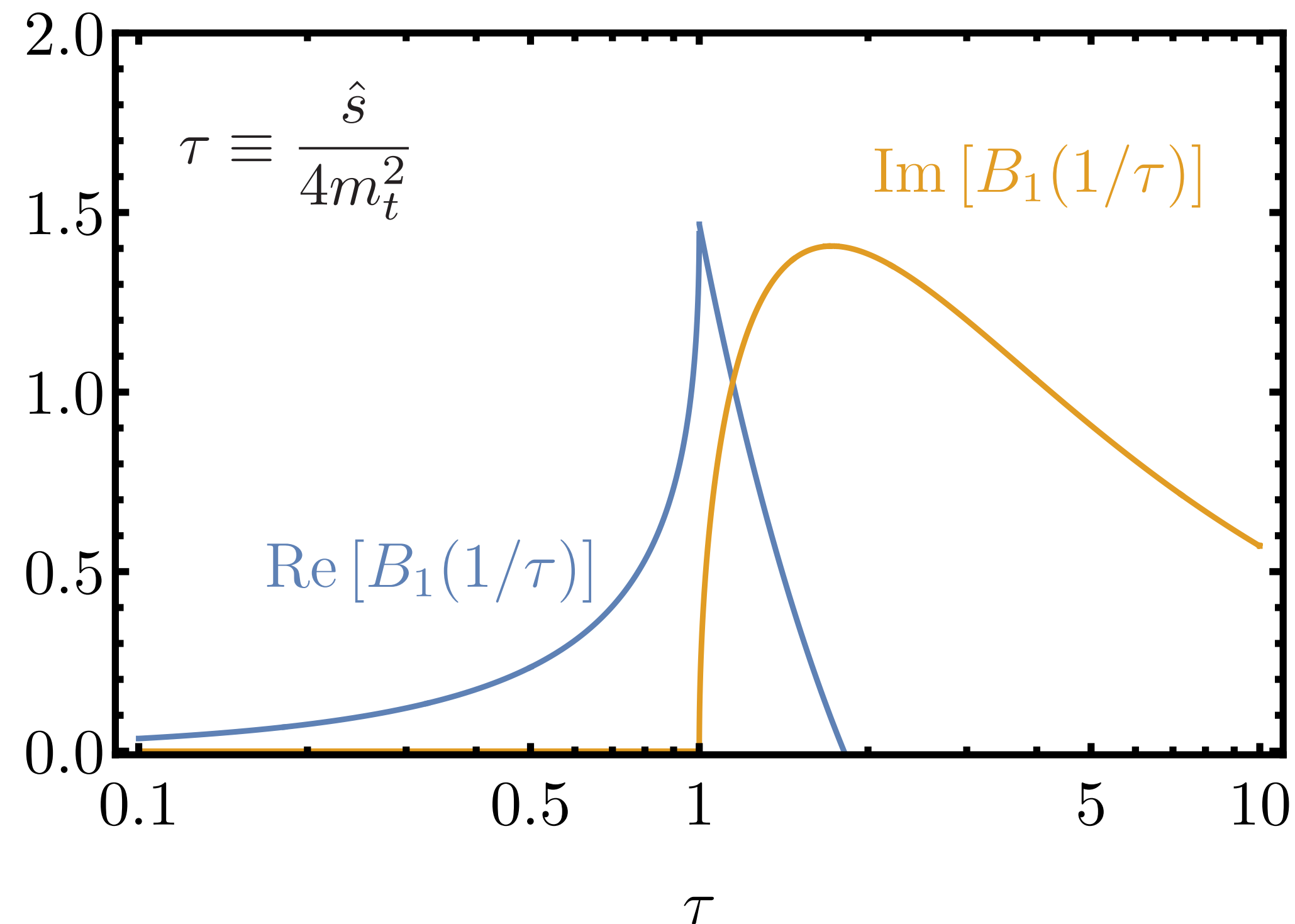
$$\tau \equiv \frac{\hat{s}}{4m_t^2} \quad \frac{1}{\hat{s} - m_a^2 + im_a\Gamma_a}$$

- Loop function develops imaginary part above the  $t\bar{t}$  threshold
- Interference contribution  $\sim \text{Im} [B_1(1/\tau)] m_a\Gamma_a$
- Peak-dip (or dip-peak) structure in  $m_{t\bar{t}}$

# ALP peaks and dips in $t\bar{t}$ production



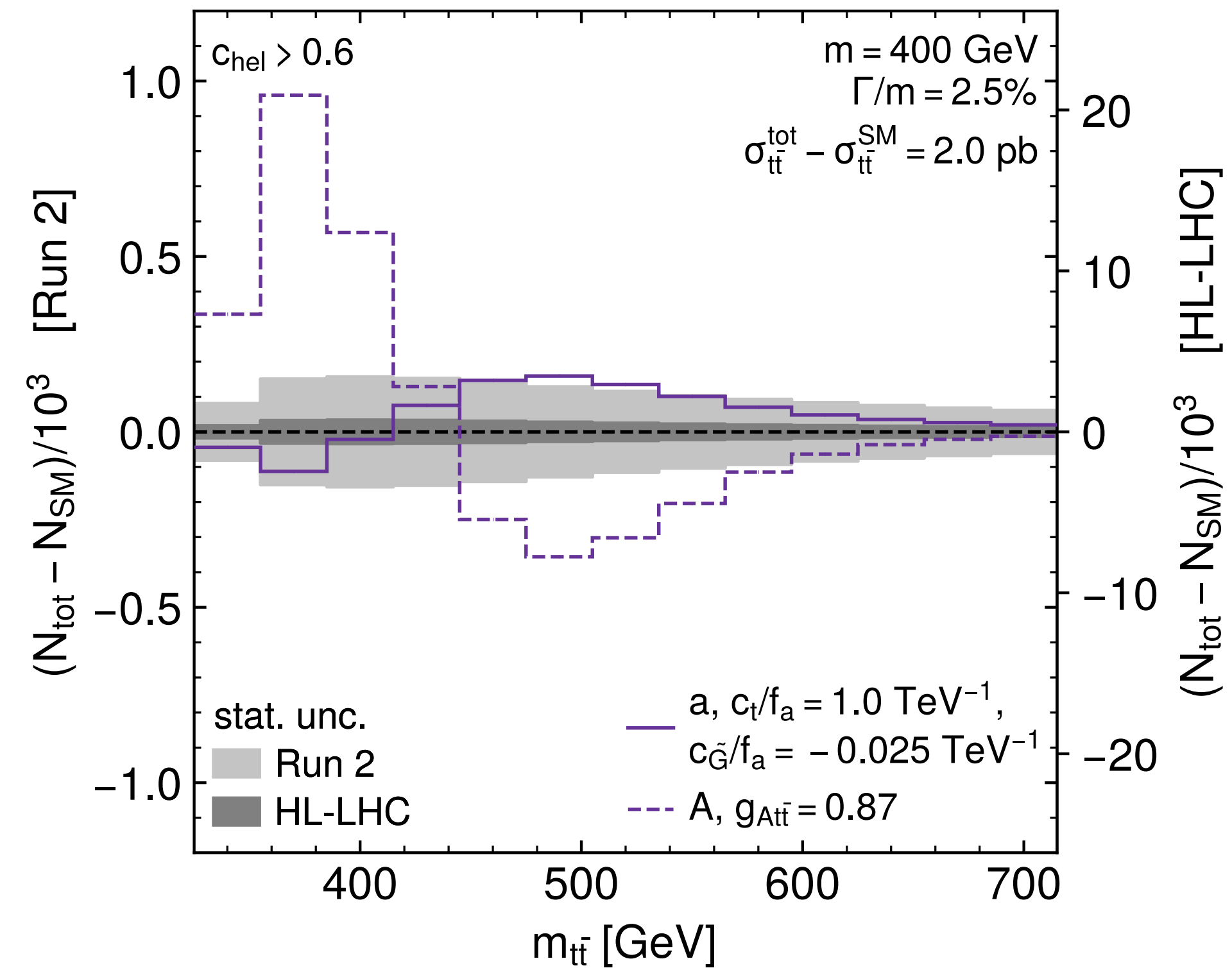
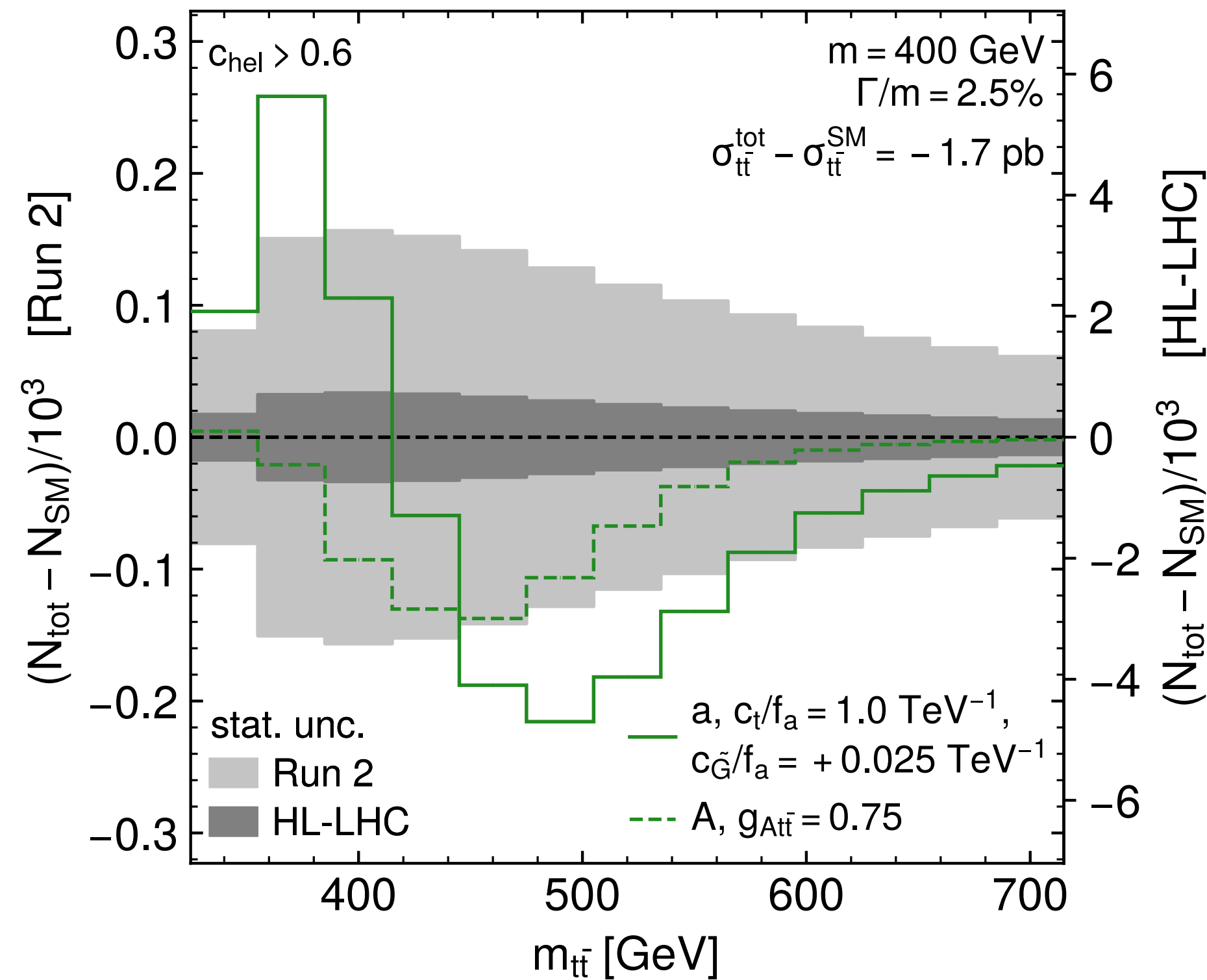
[Dicus, Stange, Willenbrock ([hep-ph/9404359](https://arxiv.org/abs/hep-ph/9404359))]



# ALP-top vs ALP-gluon coupling

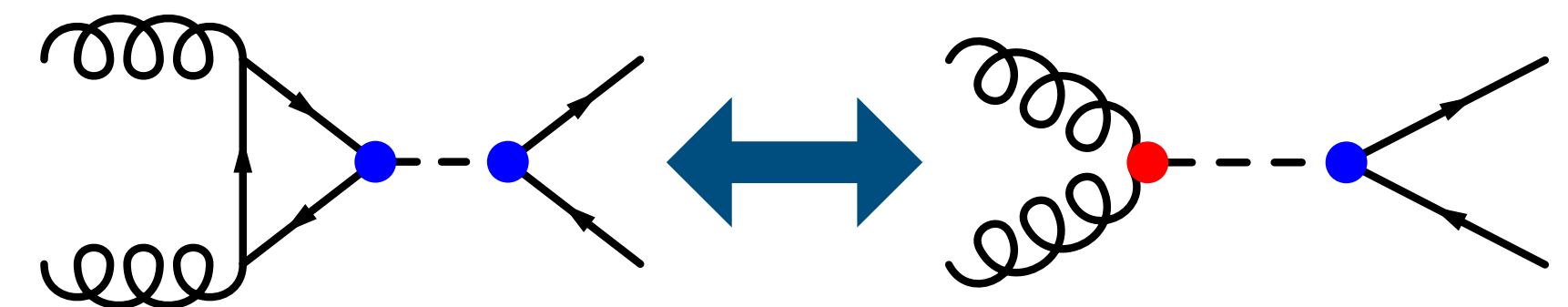
$c_t$  in **pseudoscalar** basis

[Anuar, AB, Biekötter, Grohsjean, Heinemeyer, Jeppe, Schwanenberger, Weiglein (2404.19014)]



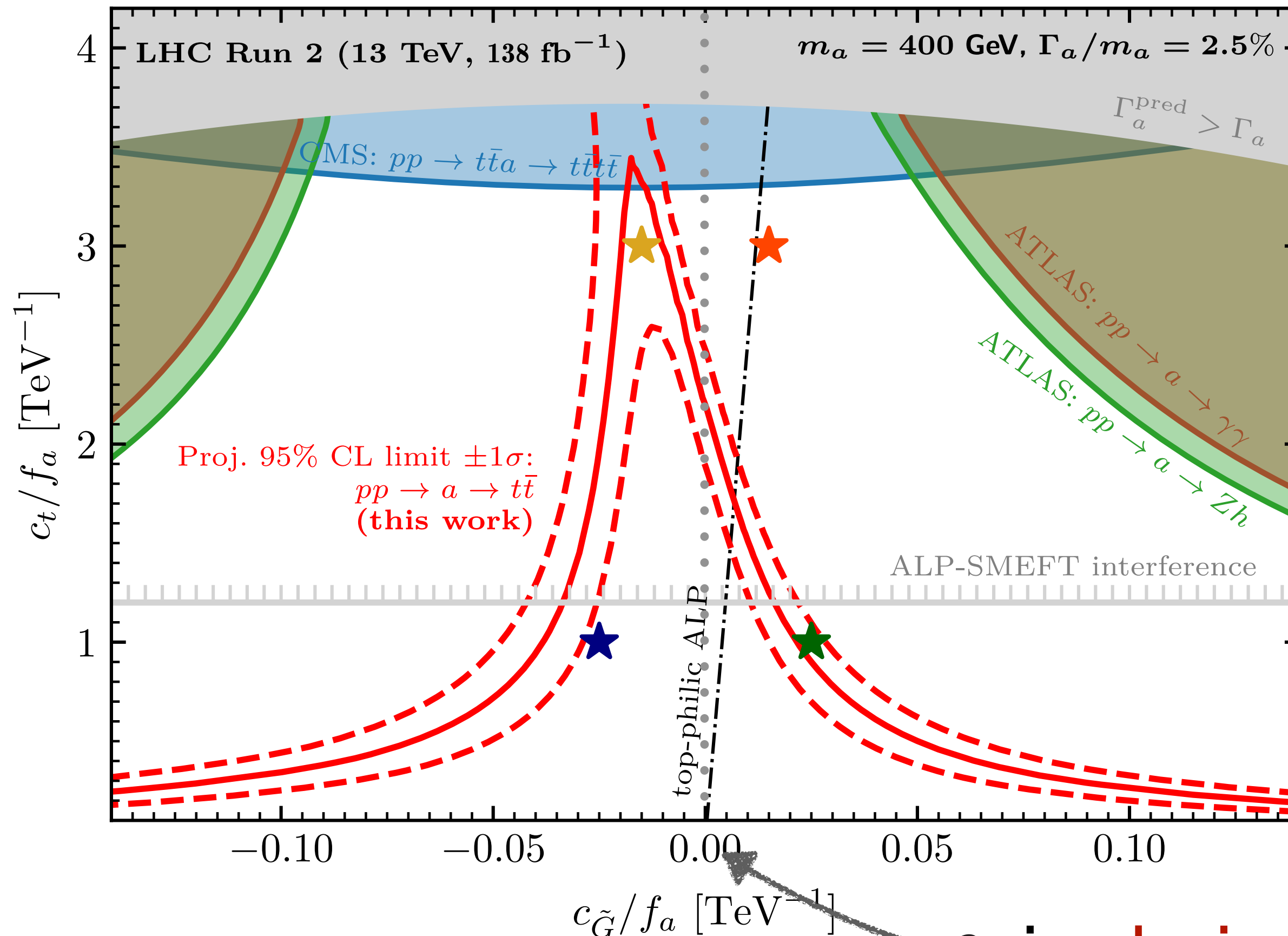
Solid:  $c_t, c_{\tilde{G}}$

Dashed:  $c_t$  only (same total cross section)



# ALP-top vs ALP-gluon coupling

[Anuar, AB, Biekötter, Grohsjean, Heinemeyer, Jeppe, Schwanenberger, Weiglein (2404.19014)]



Complementary limits from

- $t\bar{t}t\bar{t}$
- $a \rightarrow \gamma\gamma$
- $a \rightarrow Zh$

$c_t$  in derivative basis



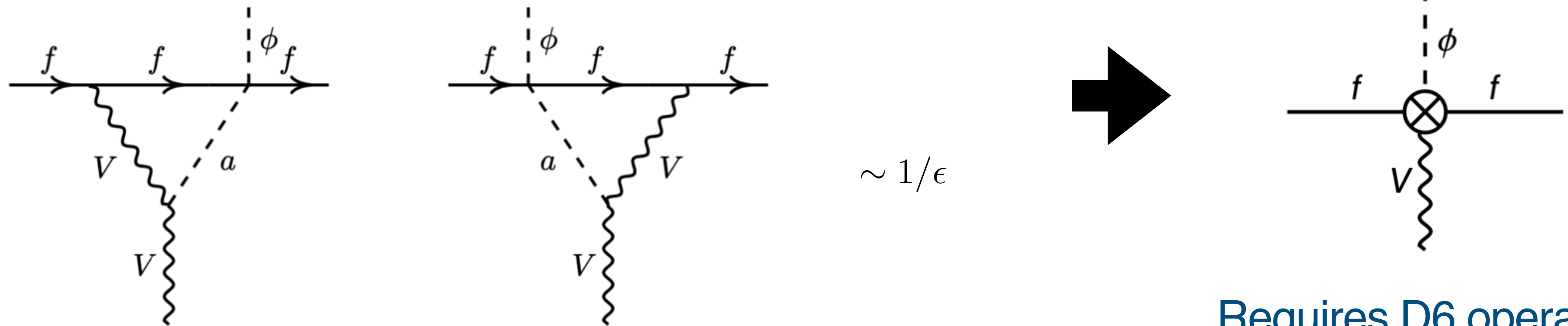
Indirect limits on ALPs  
-  
ALP-SMEFT interference

# Indirect ALP effects

[Marciano, Masiero, Paradisi, Passera ([1607.01022](#))]

[Bauer, Neubert, Thamm ([1704.08207](#))]

- Virtual ALP exchange induces UV-divergent one-loop graphs
- Dimension-6 operators required as counterterms



ALP as a solution for  $g - 2$  discrepancy

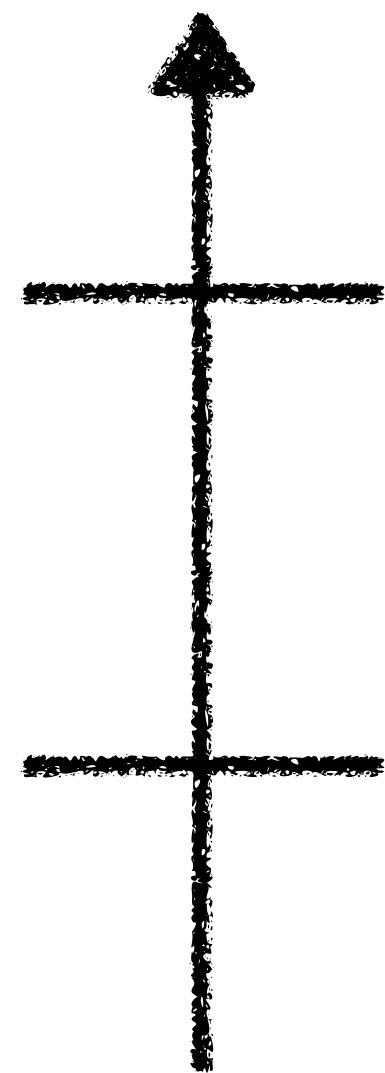
Requires D6 operator  
as counterterm

**SMEFT!**

# ALP-SMEFT interference

[Galda, Neubert, Renner ([2105.01078](#))]

$$\frac{d}{d \log \mu} C_i^{\text{SMEFT}} - \gamma_{ji}^{\text{SMEFT}} C_j^{\text{SMEFT}} = \frac{S_i}{(4\pi f)^2}$$



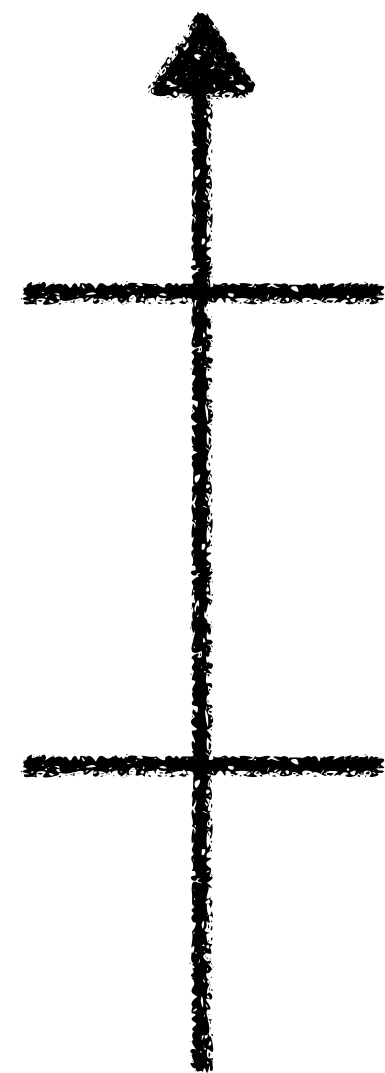
$$C^{\text{ALP}}(\Lambda) \neq 0,$$
$$C^{\text{SMEFT}}(\Lambda) = 0$$

$$C^{\text{ALP}}(\mu) \neq 0$$
$$C^{\text{SMEFT}}(\mu) \neq 0$$

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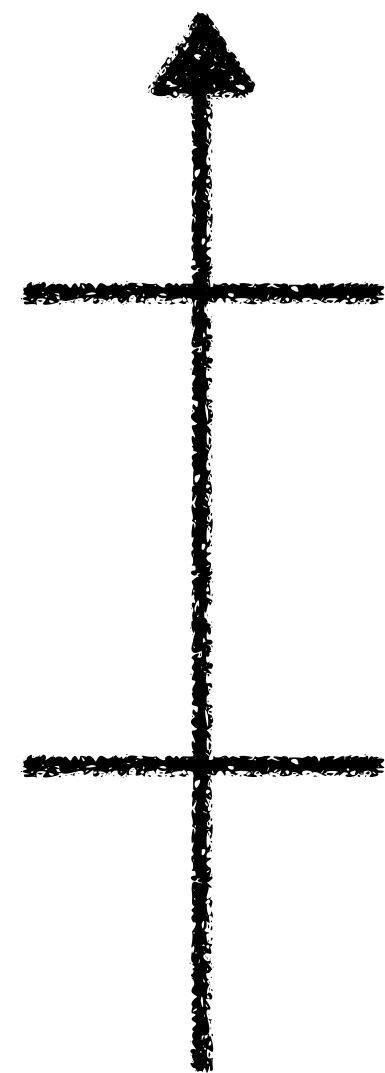
ALP running induces non-zero SMEFT coefficients!



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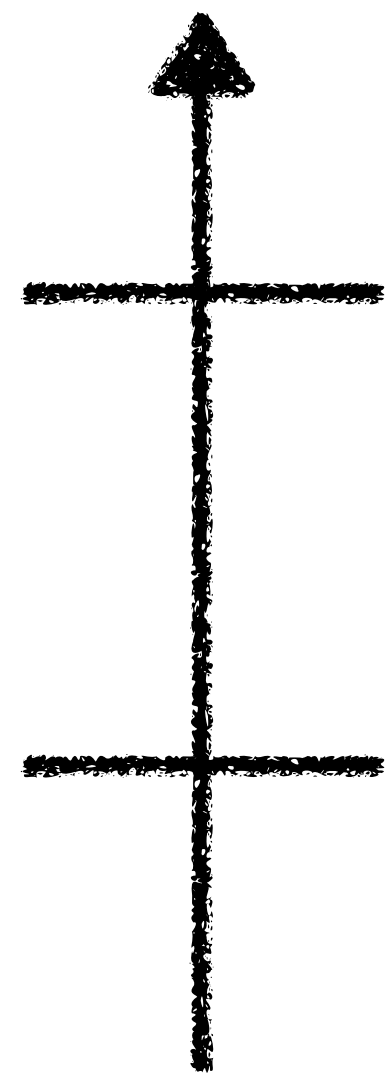
ALP source terms for D6 SMEFT Wilson coefficients are **ALP mass independent**

$$\begin{aligned} S_{HG} &= 0, & S_{H\tilde{G}} &= 0, \\ S_{HW} &= -2g_2^2 C_{WW}^2, & S_{H\tilde{W}} &= 0, \\ S_{HB} &= -2g_1^2 C_{BB}^2, & S_{H\tilde{B}} &= 0, \\ S_{HWB} &= -4g_1g_2 C_{WW}C_{BB}, & S_{H\tilde{W}B} &= 0. \end{aligned}$$

# ALP-SMEFT interference

[Galda, Neubert, Renner ([2105.01078](#))]

$$\frac{d}{d \log \mu} C_i^{\text{SMEFT}} - \gamma_{ji}^{\text{SMEFT}} C_j^{\text{SMEFT}} = \frac{S_i}{(4\pi f)^2}$$



$$C^{\text{ALP}}(\Lambda) \neq 0, \\ C^{\text{SMEFT}}(\Lambda) = 0$$

$$C^{\text{ALP}}(\mu) \neq 0 \\ C^{\text{SMEFT}}(\mu) \neq 0$$

ALP running induces non-zero SMEFT coefficients!

ALP source terms for D6 SMEFT Wilson coefficients are **ALP mass independent**

Can we use SMEFT constraints to obtain mass-independent constraints on the ALP Wilson coefficients?

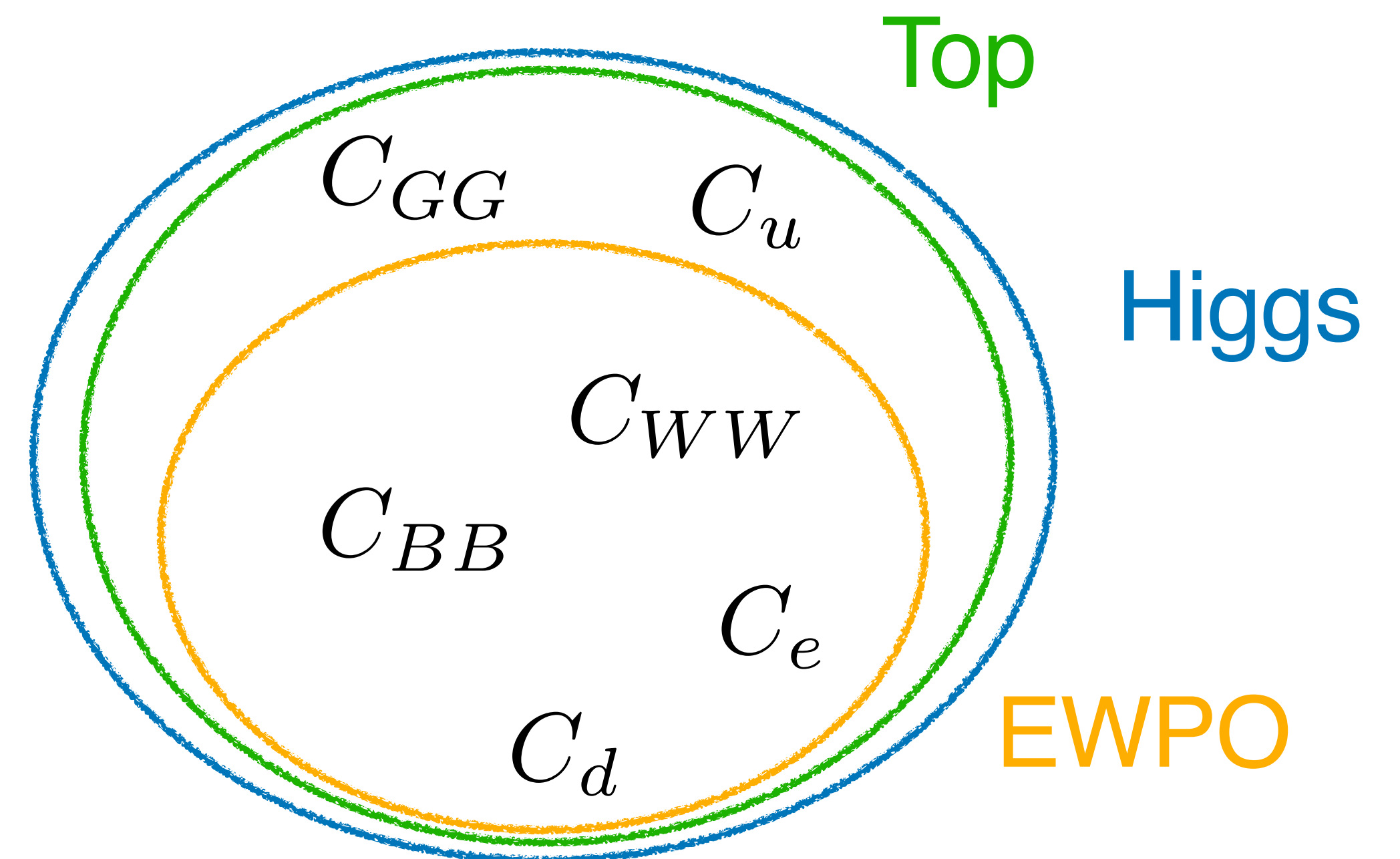
# Exploiting the ALP-SMEFT interference

## Observables used

- Low energy:
  - Electroweak precision observables (EWPO)
  - Parity violation experiments
  - Lepton scattering
- Higgs [Falkowski et al. (1706.03783)]
- Top [Ellis et al. (2012.02779)]

## Six free parameters

$$C_{GG}, C_{WW}, C_{BB}, C_u, C_d, C_e$$

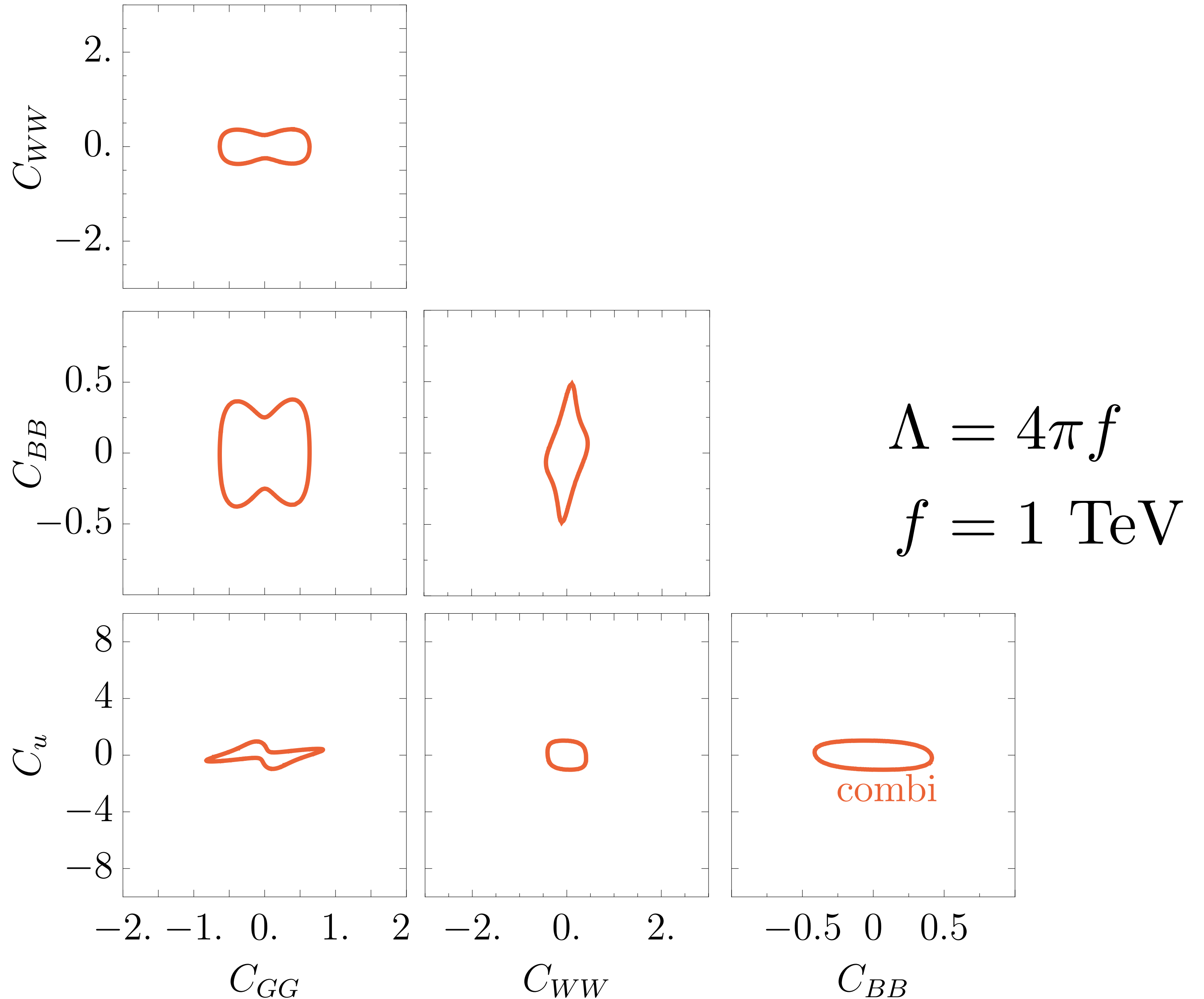


# 2D limits

## Dominant constraints

- $C_{GG}$  : Higgs + Top
- $C_{WW}$  : LE + Higgs
- $C_{BB}$  : low energy
- $C_u$  : low energy
- $C_d$  : low energy
- $C_e$  : low energy

ALP-top



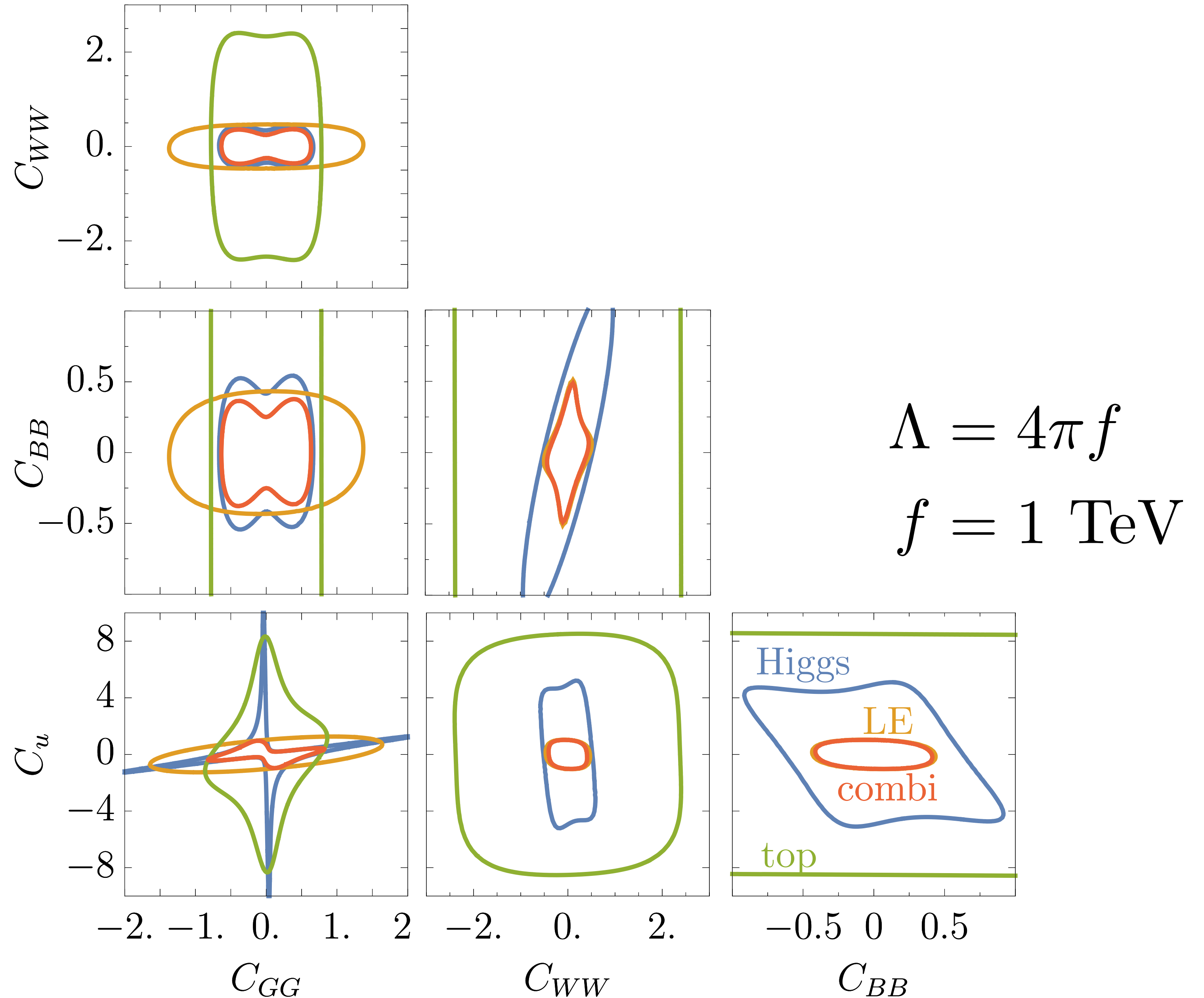


# 2D limits

## Dominant constraints

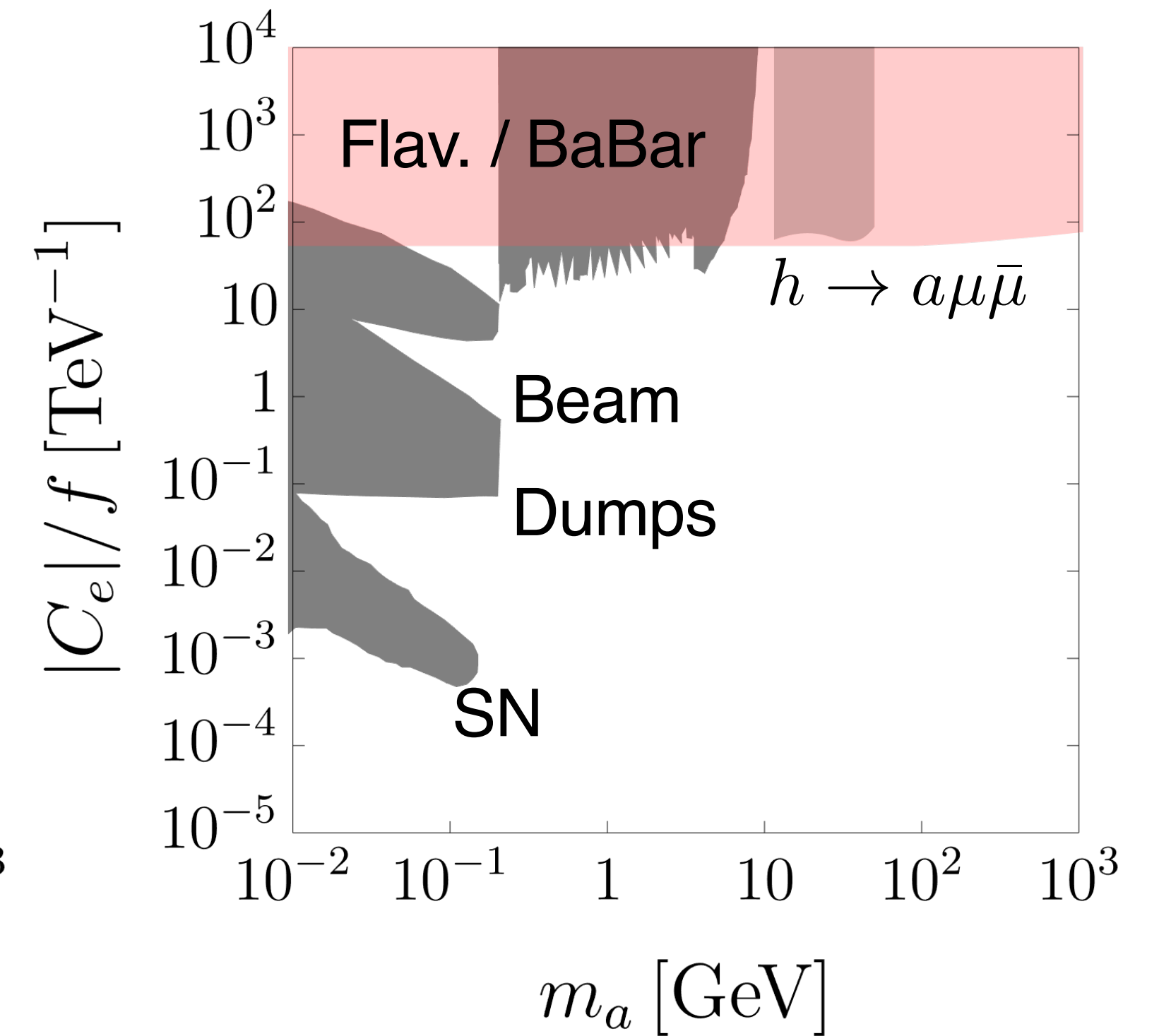
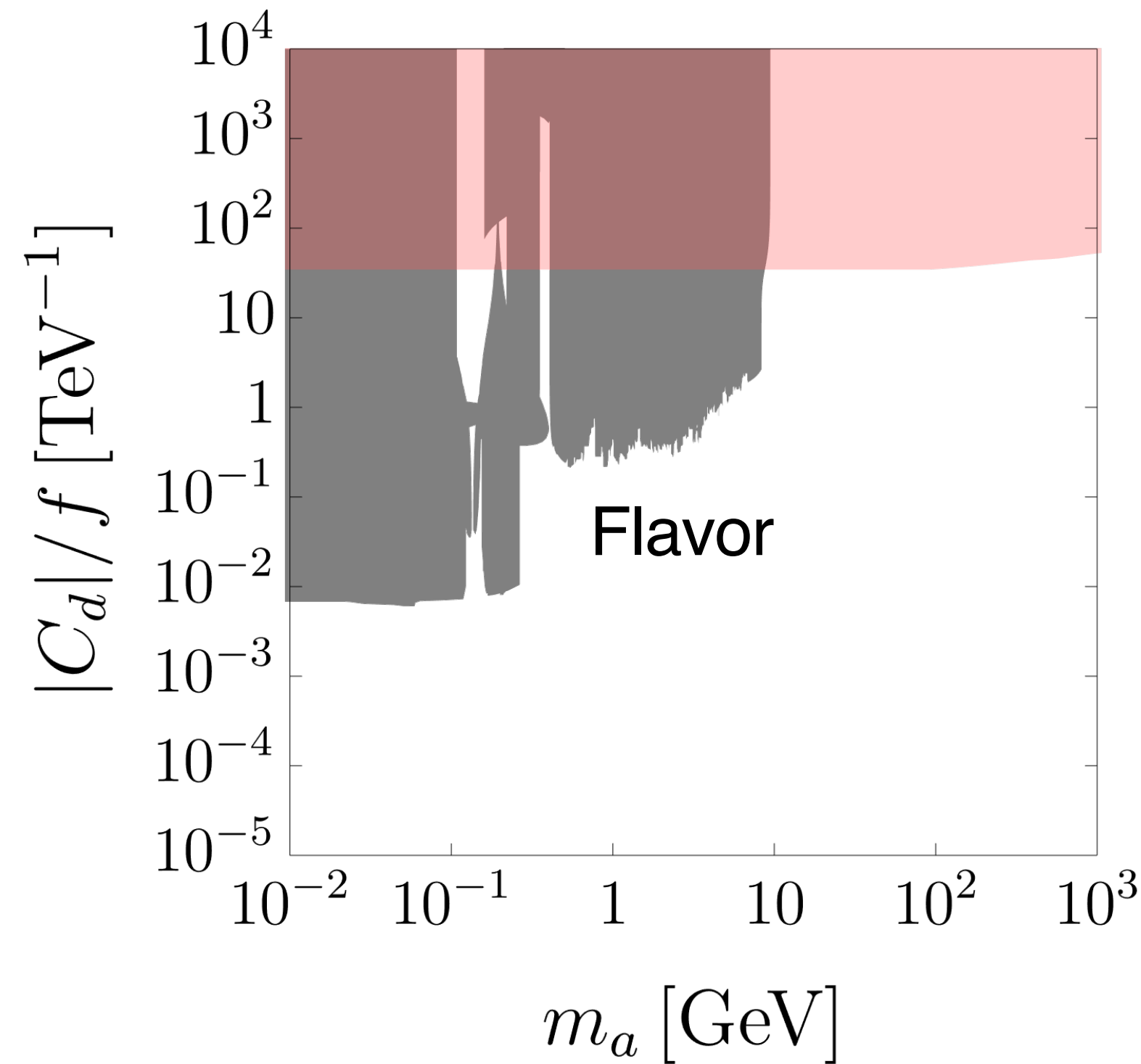
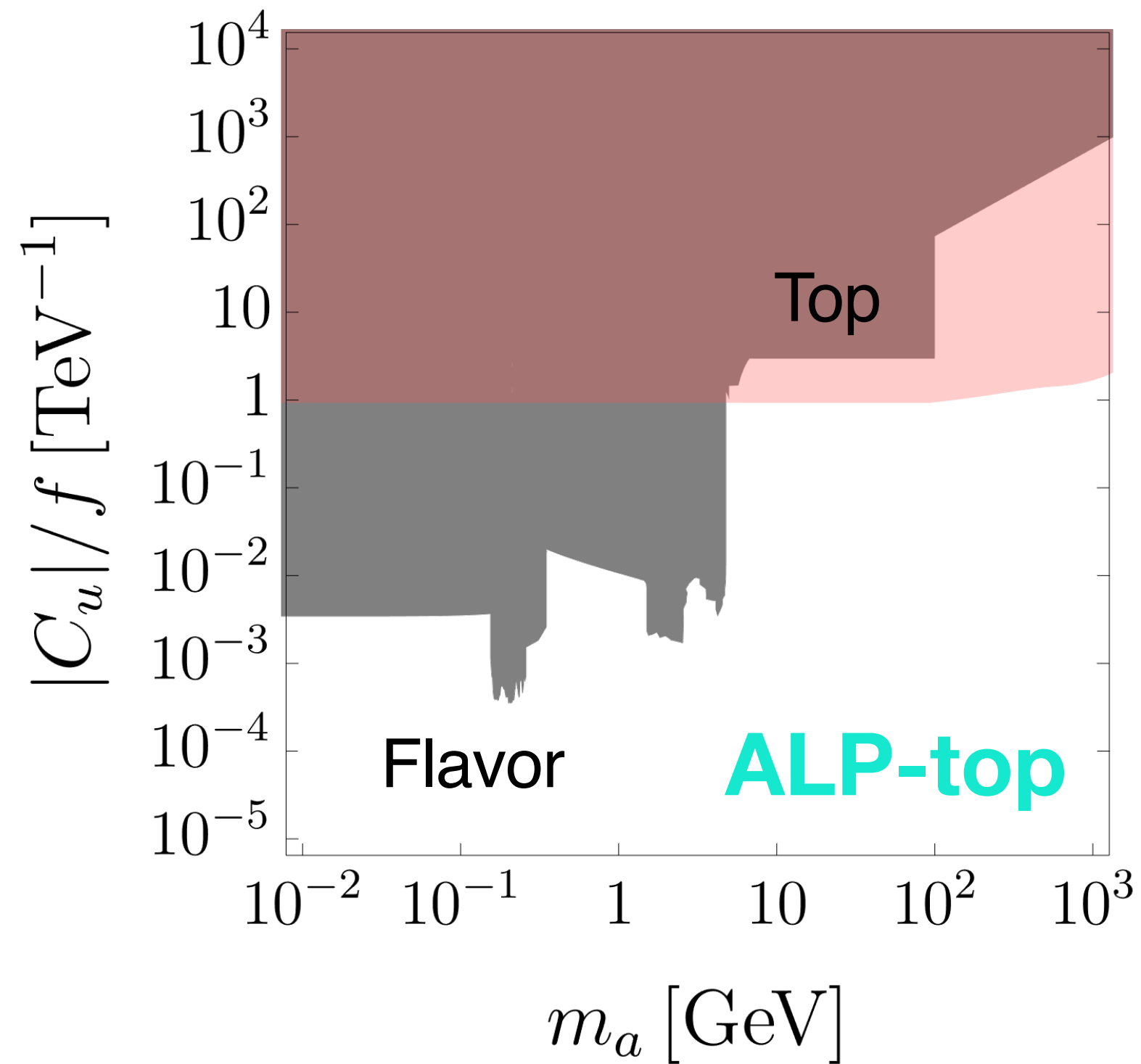
- $C_{GG}$  : Higgs + Top
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- $C_{BB}$  : low energy
- $C_u$  : low energy
- $C_d$  : low energy
- $C_e$  : low energy

ALP-top



# Comparison with direct bounds - fermions

[AB, Fuentes Martín, Galda, Neubert ([2307.10372](#))]



[BaBar ([1406.2980](#))]

[Esser, Madigan, Sanz, Ubiali ([2303.17634](#))]

[AB, Chala, Spannowski ([2203.14984](#))]

[Bauer, Neubert, Renner, Schnubel, Thamm ([2110.10698](#))]

[Lucente, Carezza ([2107.12393](#))]

[Essig, Harnik, Kaplan, Toro ([1008.0636](#))]

# FCC-ee Tera-Z

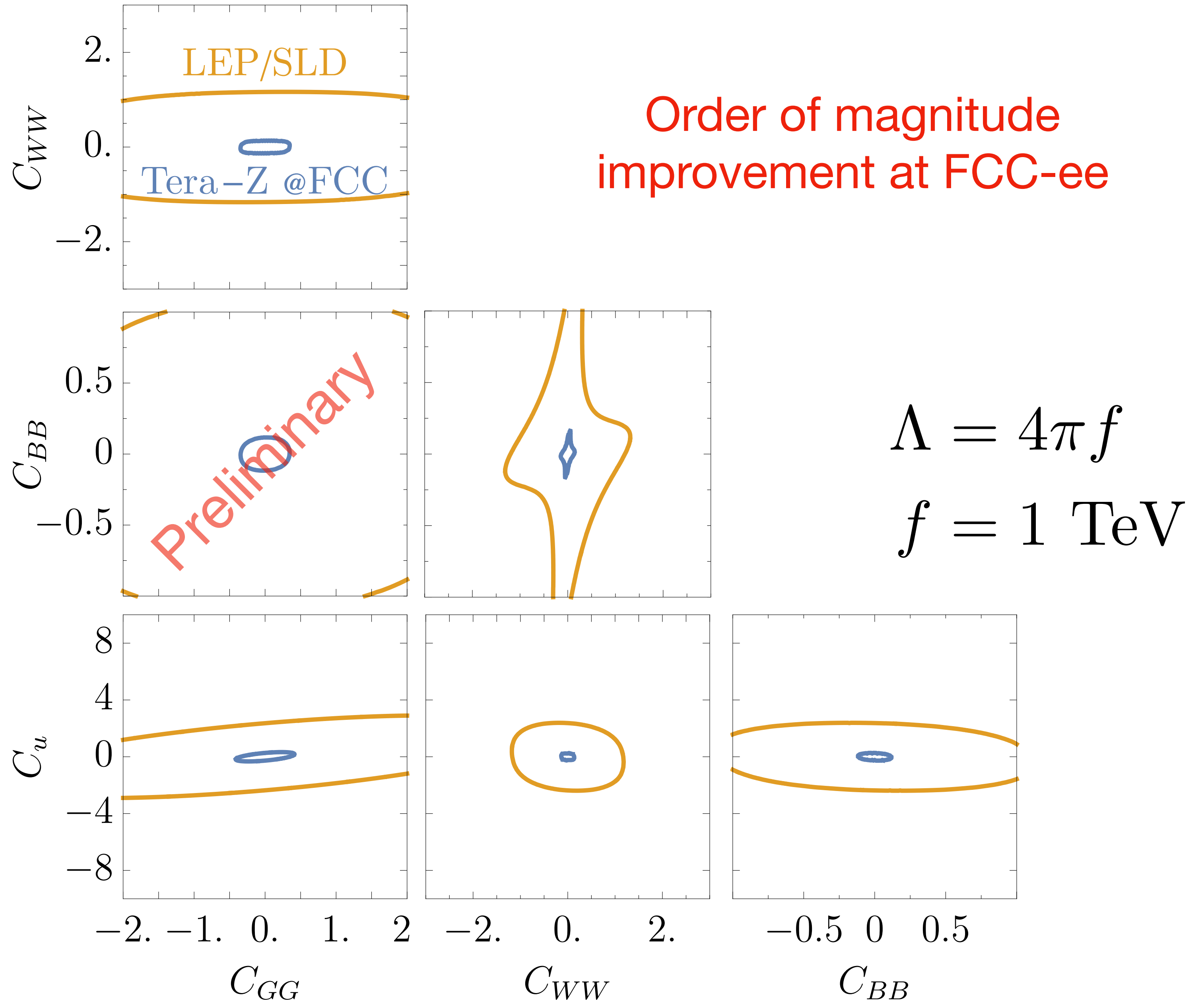
FCC-ee sensitivity estimates from FCC midterm report

see also:

[de Blas, Durieux, Grojean, Gu, Paul ([1907.04311](#))]

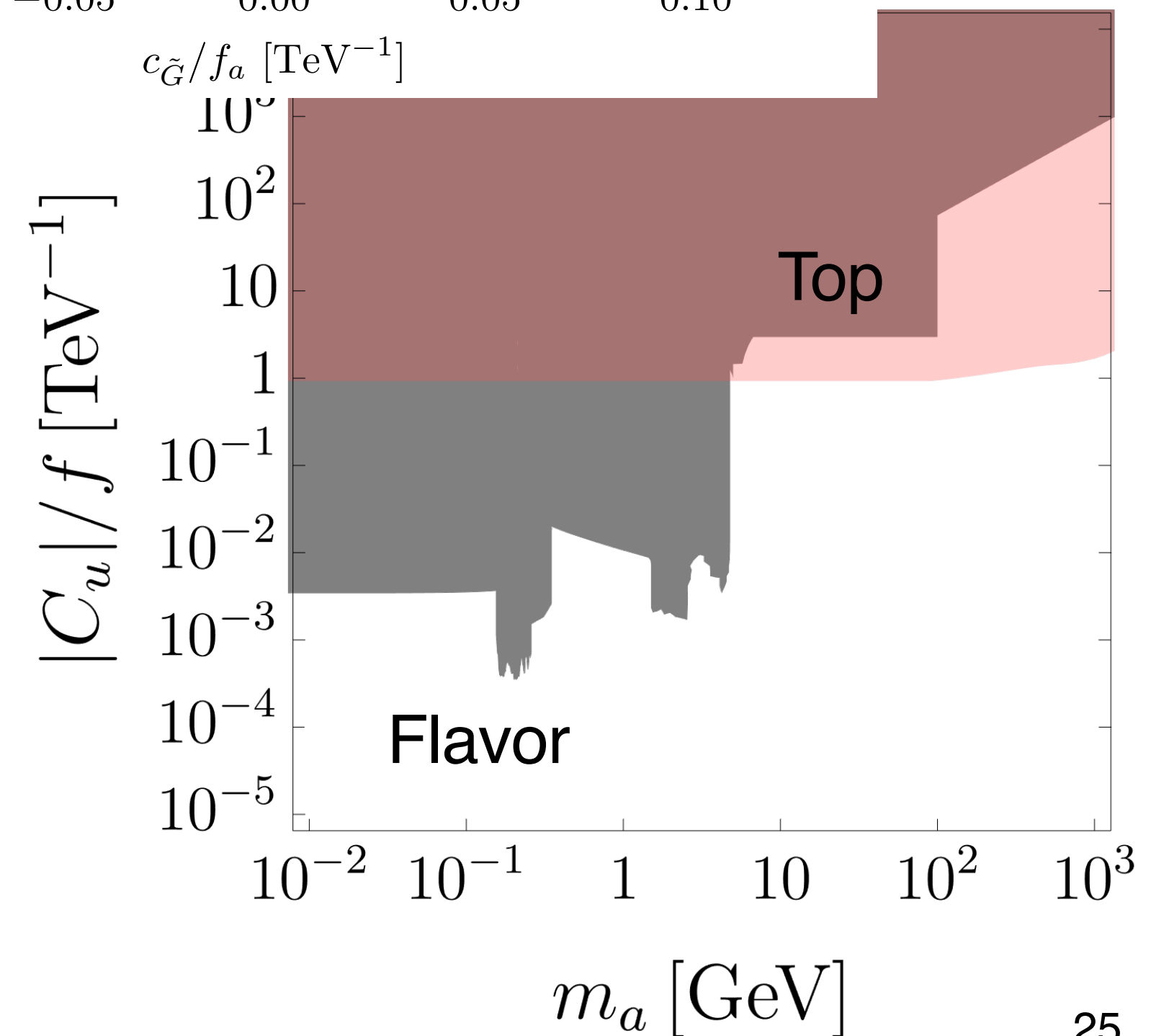
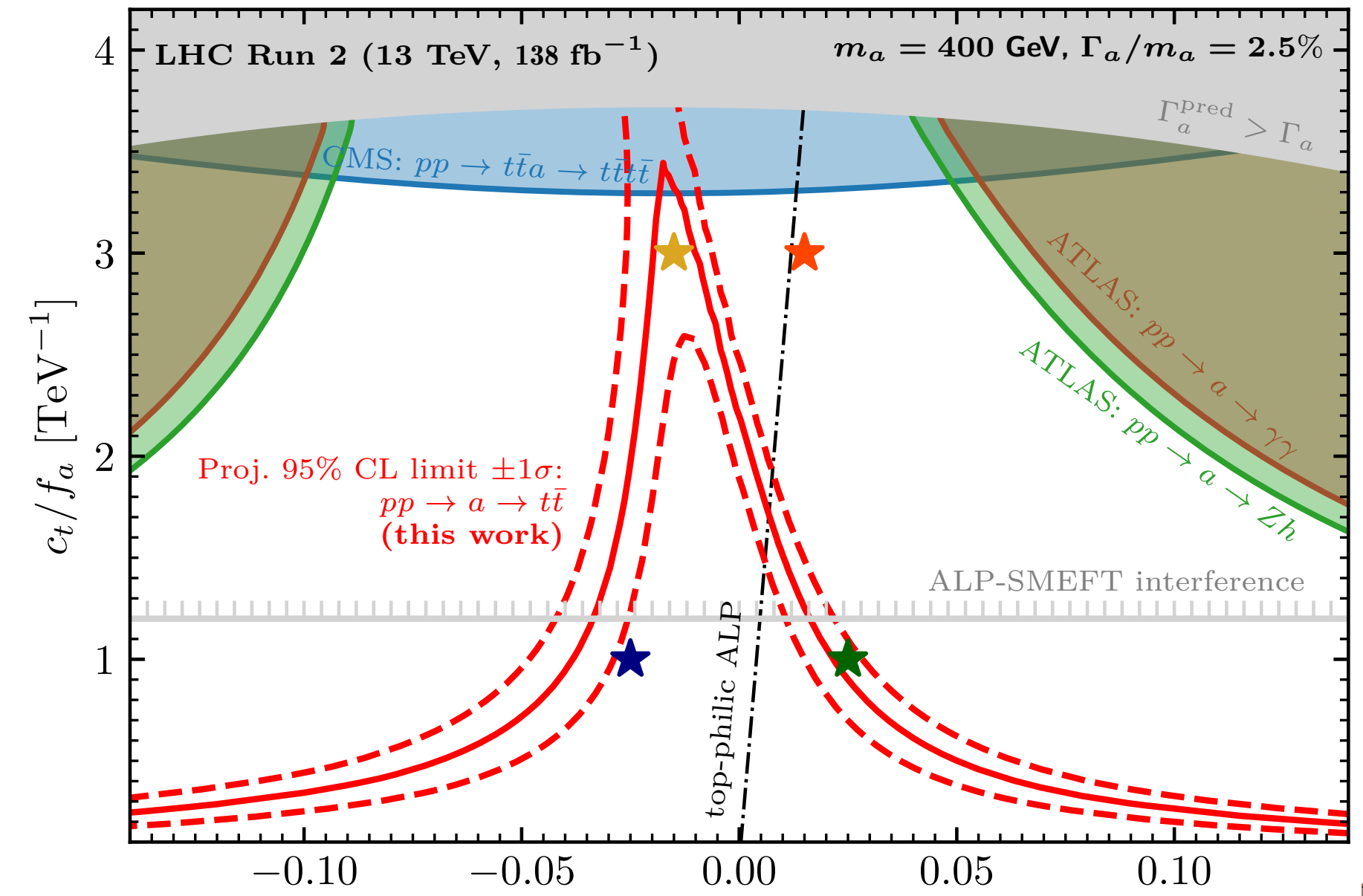
[FCC Snowmass ([2203.06520](#))]

[Dubovyk, Freitas, Gluza, Grzanka, Jadach, Riemann, Usovitsch ([1809.01830](#))]



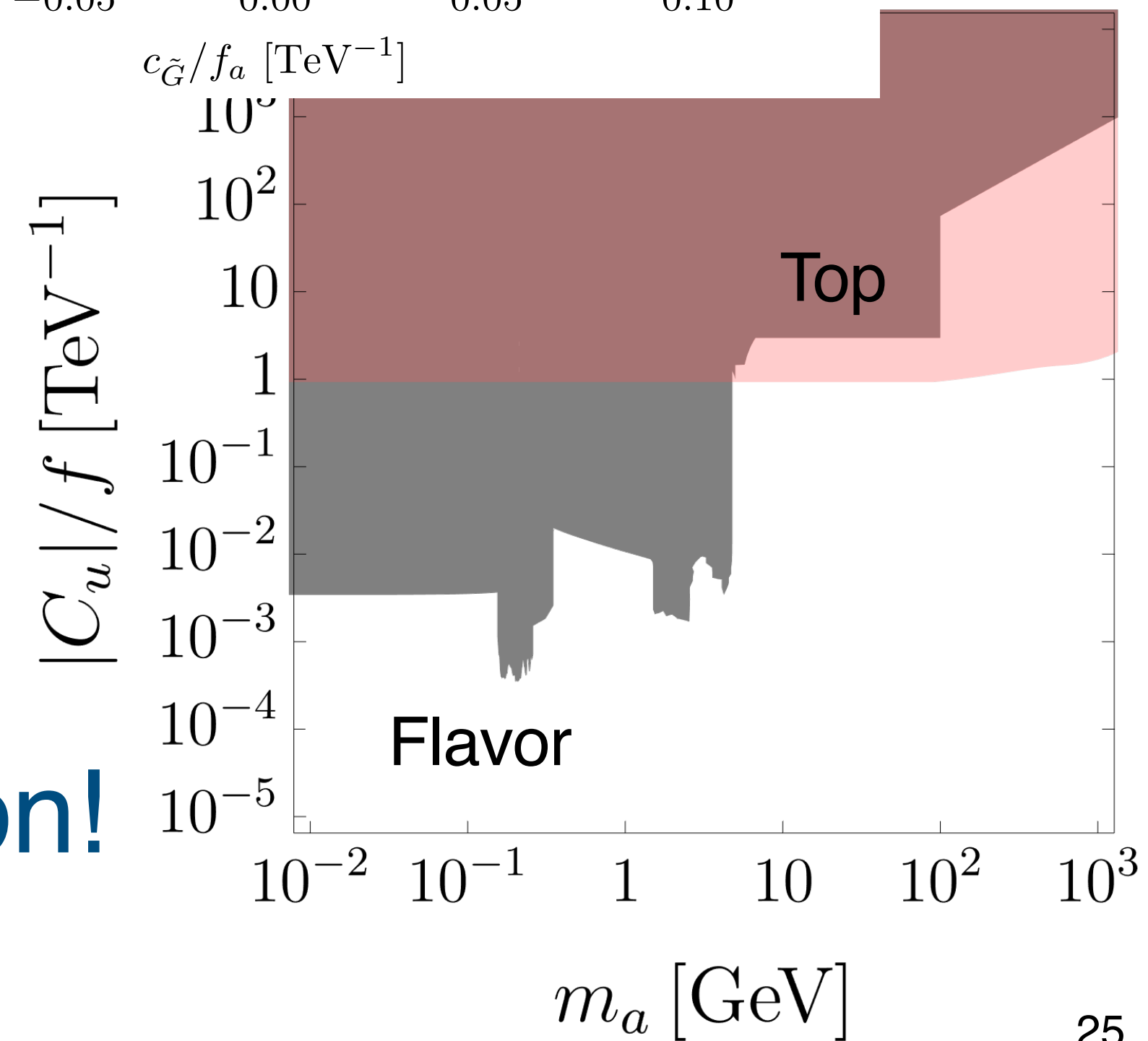
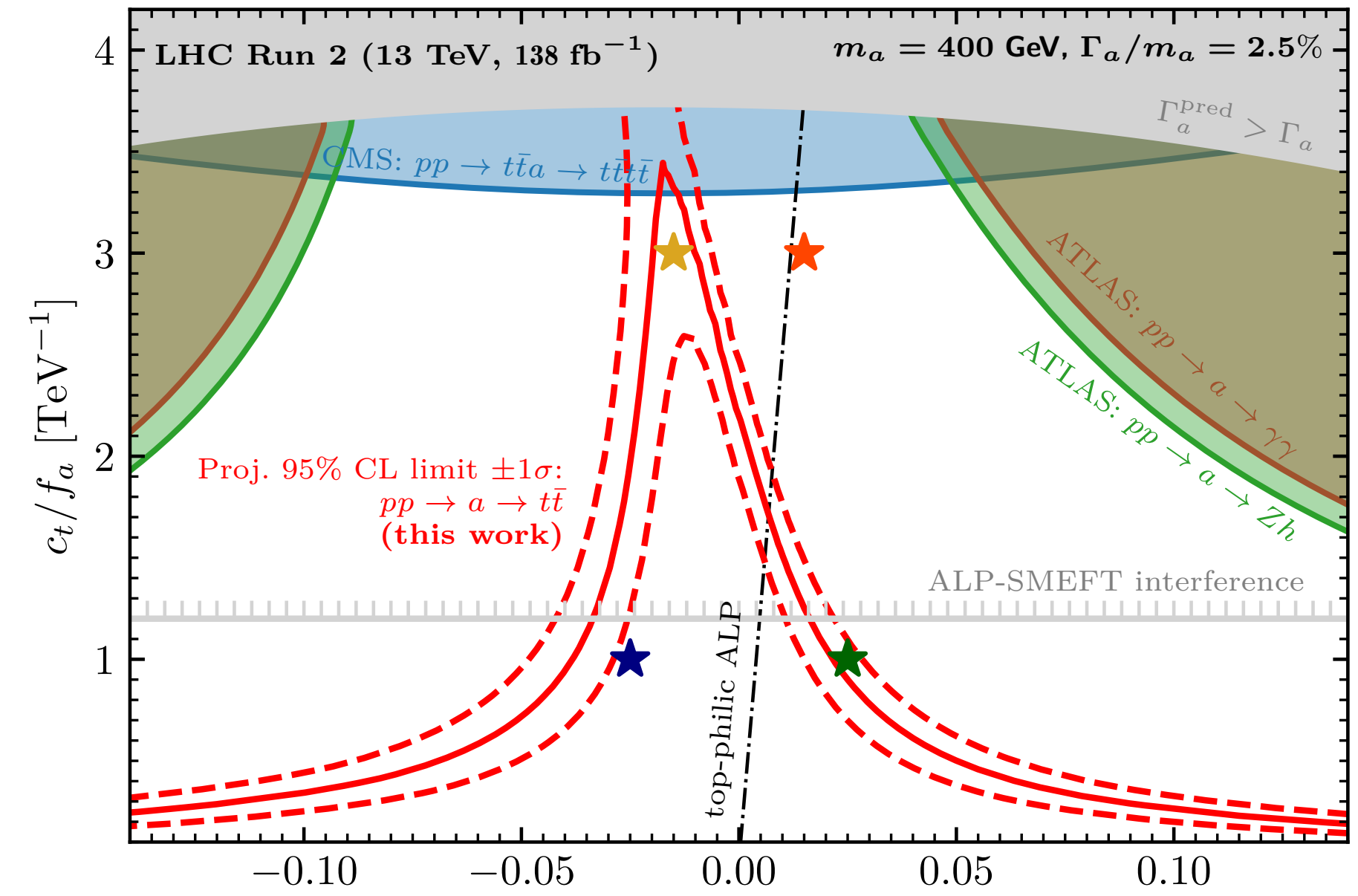
# Conclusions

- Very rich ALP phenomenology
- ALP-top coupling
  - Complementarity of flavor,  $t\bar{t}a$ ,  $t\bar{t}$  production
- Complementary of direct and indirect bounds



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Thank you for your attention!