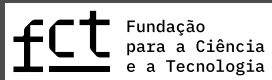


Long-lived particles at colliders

Jan Hajer

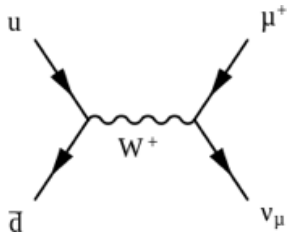
Centro de Física Teórica de Partículas, Instituto Superior Técnico, Universidade de Lisboa

LFC24 — Fundamental Interactions at Future Colliders

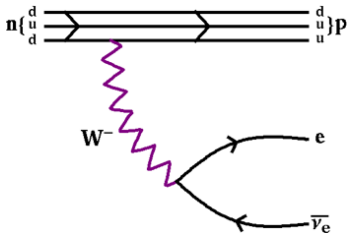


Long-lived particle (LLPs) in the Standard Model (SM)

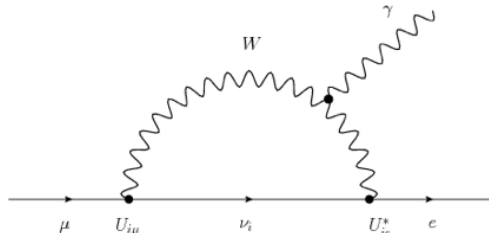
$$\pi^+ \rightarrow \mu^+ \nu_\mu$$



$$n \rightarrow p e \bar{\nu}_e$$



$$\mu \rightarrow e \gamma$$



Charged pion

- Decay via weak interactions
- Decay extremely off-shell

$$\Gamma_{\pi^+} \propto g_W^2 \left(\frac{m_\pi}{m_W} \right)^4 m_\pi$$

Muon

- Flavour changing neutral current
 - Lepton flavour only violated by neutrino masses and Yukawa couplings
- $$\text{BR}(\mu \rightarrow e \gamma) \propto 10^{-13}$$

Neutron

- Proton and neutron are almost mass degenerate due to isospin
- Decay extremely off-shell

$$\Gamma_n \propto g_W^2 \left(\frac{\Delta_{np}}{m_W} \right)^4 \Delta_{np}, \quad \Delta_{np} = m_n - m_p$$

Generically

- Off-shell decay
- Small mass splitting
- Small coupling due to hierarchy or loop suppression

$$\Gamma \propto \lambda^2 \left(\frac{m}{M} \right)^n m$$

LLPs beyond the SM

New Physics

Any model with such features can contain LLPs

- Supersymmetry
- Dark Matter models
- Extended Higgs sectors

Portals to hidden sectors

- Many extension to the SM feature hidden sectors
- Often motivated by DM candidates

Prime examples

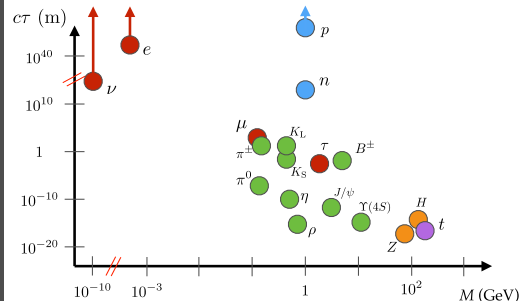
- Axion like particles
- Heavy neutral leptons (HNLs)
- Hidden U(1) / New gauge bosons

Search strategies

- Displaced tracks/vertices
- Emerging jets
- Disappearing tracks
- Kinked tracks
- Quasi-stable charged particles

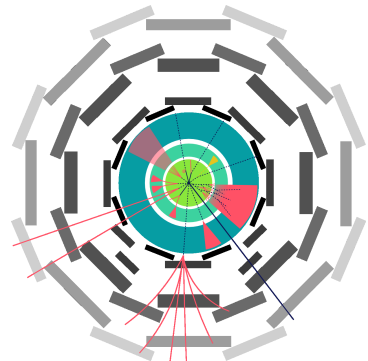
LLPs in the SM

[1903.04497]



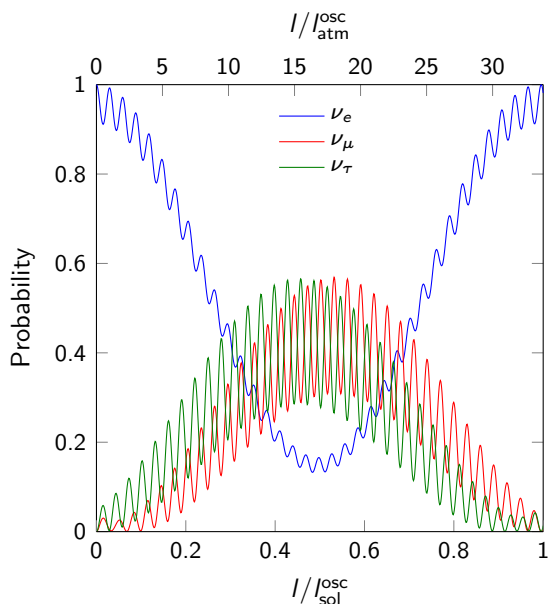
LLP signatures

[1903.04497]



Neutrino flavour oscillations and seesaw mechanism

Observed neutrino flavour oscillations



Can be explained by

at least two massive neutrinos

Right-handed Majorana neutrino N

$$\mathcal{L}_m = \begin{pmatrix} \vec{\nu} \\ N \end{pmatrix}^t \begin{pmatrix} 0 & \vec{m}_D \\ \vec{m}_D^T & m_M \end{pmatrix} \begin{pmatrix} \vec{\nu} \\ N \end{pmatrix}$$

Interaction governed by mixing parameter

$$\vec{\theta} = \frac{\vec{m}_D}{m_M} \quad \begin{array}{l} \text{Dirac mass} \\ \text{Majorana mass} \end{array}$$

Neutrino masses

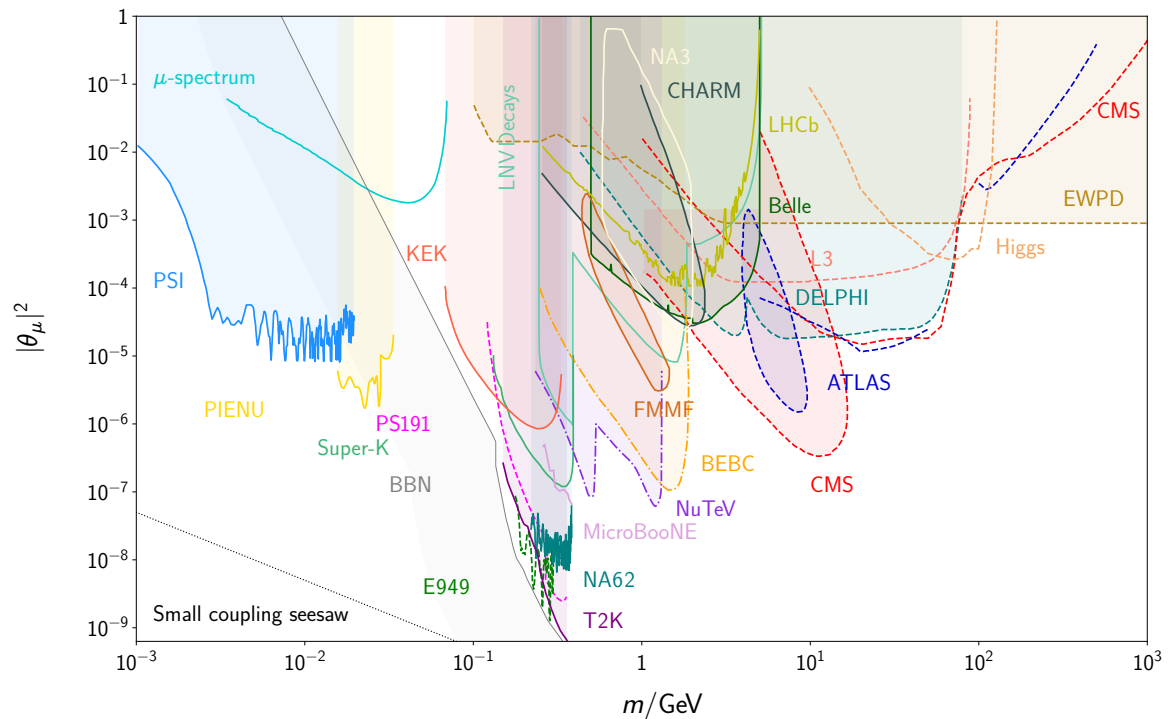
$$M_\nu = \frac{\vec{m}_D \vec{m}_D^T}{m_M} = m_M \vec{\theta} \vec{\theta}^T$$

Tiny neutrino masses are ensured for

- large m_M High scale seesaw
- small \vec{m}_D Small coupling seesaw

Sterile neutrinos/HNLs

- Inaccessibly heavy or
- Tiny interactions

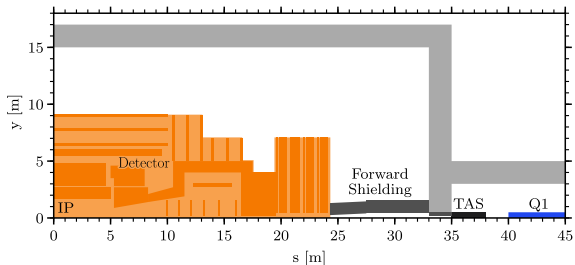


Inaccessible: ■ Small coupling seesaw ■ High scale seesaw (at the GUT scale)

FCC cavern and detector layout

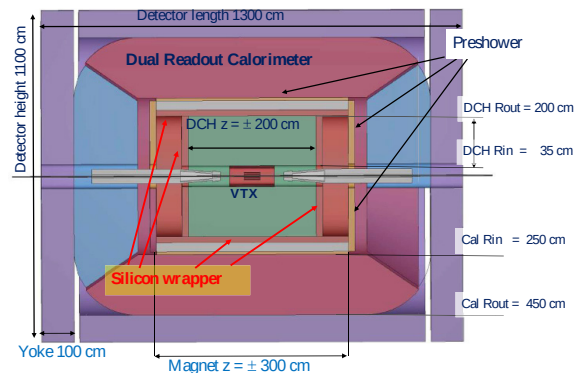
FCC caverns

[FCC-hh]



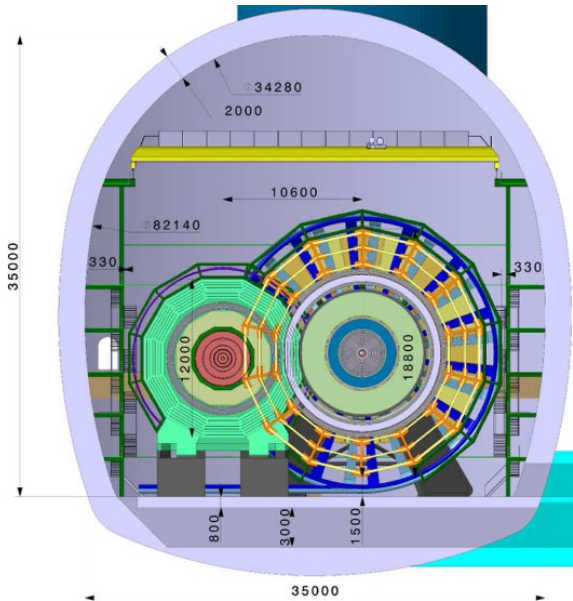
FCC-ee IDEA detector

[FCC-ee]



FCC-ee CLD vs. FCC-hh detector

[FCC-ee]



Comparison

- Cavern size: $r \approx 15$ m, $z \approx 50$ m
- Detector size: $\mathcal{O}(10$ m)

Idea

- Exploit the additional space surrounding the FCC-ee detectors in the FCC-*hh* caverns
- Build a 4π LLP detector

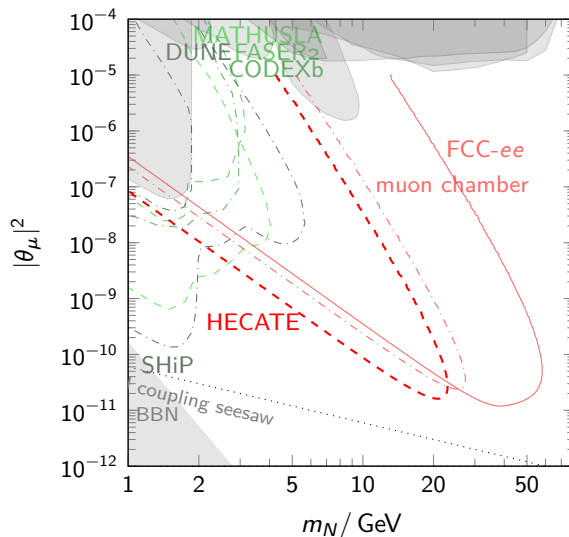
Layout

- Cover the cavern surface with detector material
- Minimum of two layers allows for timing
- Main detector serves as veto

For $\lambda \gg l_1 \gg l_0$

$$|\theta|^2 \propto \frac{1}{\sqrt{l_1}} \propto \frac{1}{\sqrt{L}}$$

Half a magnitude sensitivity gain in $|\theta|^2$



- | | | |
|-------|---------------|--|
| — | main detector | $l_0 = 5 \text{ mm}, l_1 = 1.22 \text{ m}$ |
| - - - | muon chambers | $l_0 = 1.22 \text{ m}, l_1 = 4 \text{ m}$ |
| - - - | HECATE | $l_0 = 4 \text{ m}, l_1 = 25 \text{ m}$ |

All efficiencies assumed to be 100 %

Symmetry-protected low-scale seesaw

Lepton number $L = n_\ell - n_{\bar{\ell}}$

Accidentally conserved in the SM

Generalisation: 'Lepton number'-like symmetry

e.g. $U(1)_L$	$\vec{\nu}$	N_1	N_2
with charges	L	$+1$	-1

Symmetry breaking in the mass matrix

$$\mathcal{L}_m = \begin{pmatrix} \vec{\nu} \\ N_1 \\ N_2 \end{pmatrix}^t \begin{pmatrix} 0 & \vec{m}_D & \vec{\mu}_D \\ \vec{m}_D^T & \mu'_M & m_M \\ \vec{\mu}_D^T & m_M & \mu_M \end{pmatrix} \begin{pmatrix} \vec{\nu} \\ N_1 \\ N_2 \end{pmatrix}$$

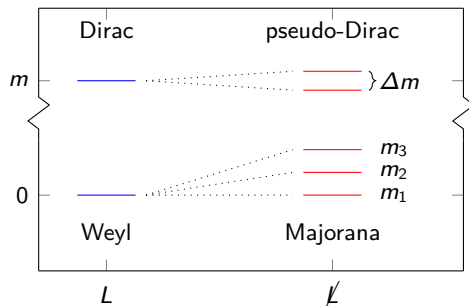
Symmetry L conserved

- Three massless neutrinos
 - Single Dirac heavy neutrino
- Corresponds to two degenerate Majoranas

Small symmetry breaking $\not\ll$

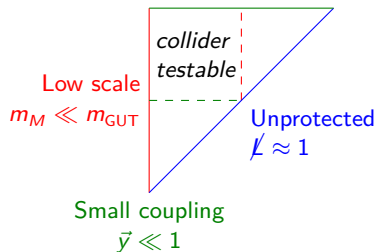
- Light neutrino masses $m_\nu \propto \not\ll$
- Heavy neutrino mass splitting $\Delta m \propto \not\ll$

Breaking induced neutrino mass splitting



Viable seesaw limits

Symmetry protected $\not\ll \ll 1$ Large coupling $\bar{y} \approx 1$ High scale $m_M \approx m_{\text{GUT}}$



Dirac vs. Majorana

Symmetry-protected benchmark models (BMs) contain pseudo-Dirac HNLs

With care some properties can be correctly approximated by simpler BMs

Dirac BM

- ✓ Correct production cross section
- ✓ Correct decay width
- ⚡ No lepton number violation (LNV)
- ⚡ No neutrino masses

Displaced vertex searches for Dirac HNLs

Generically correct

Majorana BM

- ✓ Correct production cross section
- ⚡ Wrong decay width
- ✓ LNV
- ⚡ Generically too much LNV

Prompt searches for LNV with Majorana HNLs

- Generically the bounds are too strong
 - In many cases no bounds can be extracted
 - Can be correct for some parameter points
- Model depended reinterpretation necessary

Heavy neutrino-antineutrino oscillations ($N\bar{N}$ Os)

[2210.10738]

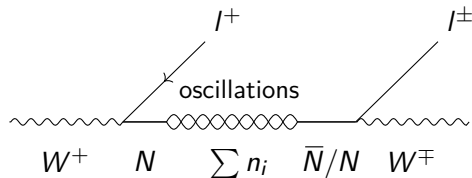
Oscillations between events that have

- Lepton number conservation (LNC) $I^\pm I^\mp$
- Lepton number violation (LNV) $I^\pm I^\pm$

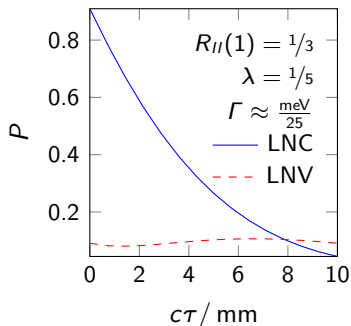
Oscillation frequency governed by Δm

$$P_{\text{osc}}^{\text{LNC/LNV}}(\tau) = \frac{1 \pm \cos(\Delta m \tau)}{2}$$

Oscillating mass eigenstates n_i

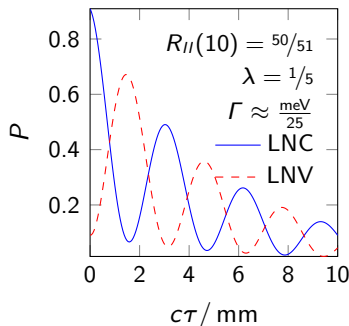


Almost Dirac limit



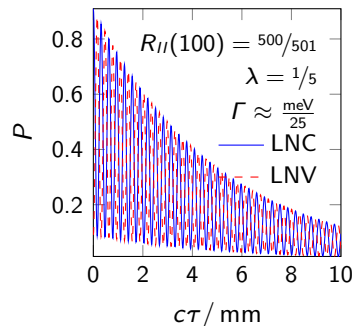
- Mostly LNC

Archetypical pseudo-Dirac



- Potentially resolvable

Double-Majorana limit



- Unresolvable
- LNV as frequent as LNC

HNLs can be long-lived particles

$$P_{\text{decay}}(\tau) = -\frac{d}{d\tau} \exp(-\Gamma\tau) = \Gamma \exp(-\Gamma\tau)$$

Since they are pseudo-Dirac they oscillate

$$P_{\text{osc}}^{\text{LNC/LNV}}(\tau) = \frac{1 \pm \cos(\Delta m\tau)}{2}$$

Collider signature: Decaying oscillations

$$P_{II}^{\text{LNC/LNV}}(\tau) = P_{\text{decay}}(\tau) P_{\text{osc}}^{\text{LNC/LNV}}(\tau)$$

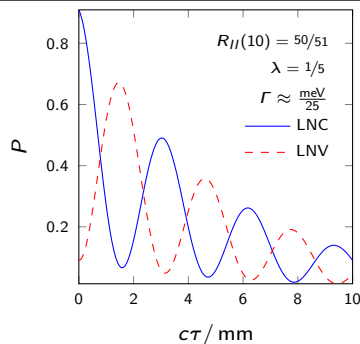
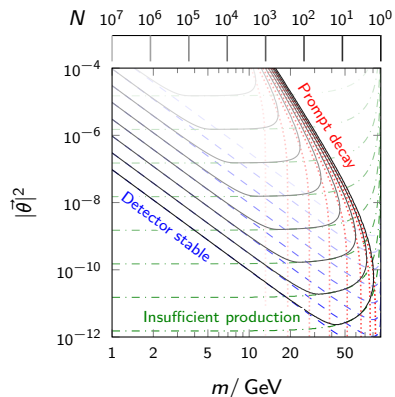
Time-integrated oscillations

[2307.06208]

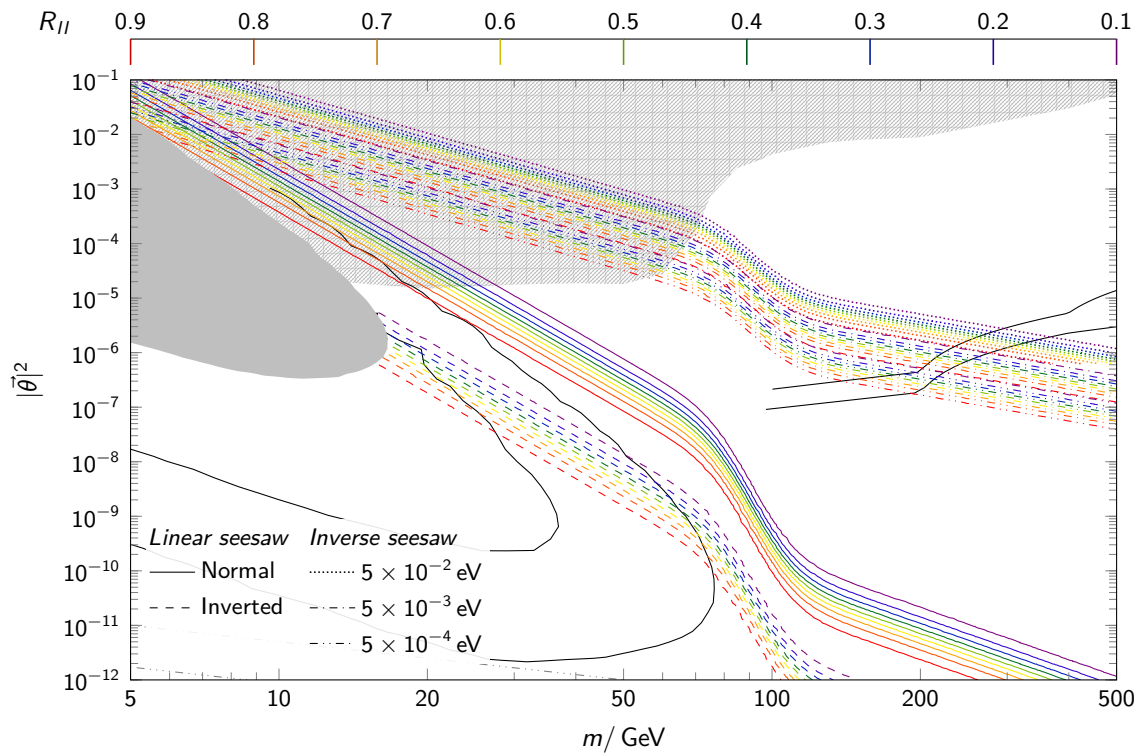
$$P_{II}^{\text{LNC/LNV}} = \frac{1}{2} \pm \frac{1}{2} \frac{\Gamma^2}{\Gamma^2 + \Delta m^2}$$

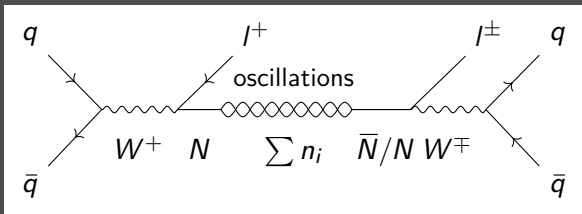
Charged lepton ratio

$$R_{II} = \frac{P_{II}^{\text{LNV}}}{P_{II}^{\text{LNC}}} = \frac{\Delta m^2}{\Delta m^2 + 2\Gamma^2}$$



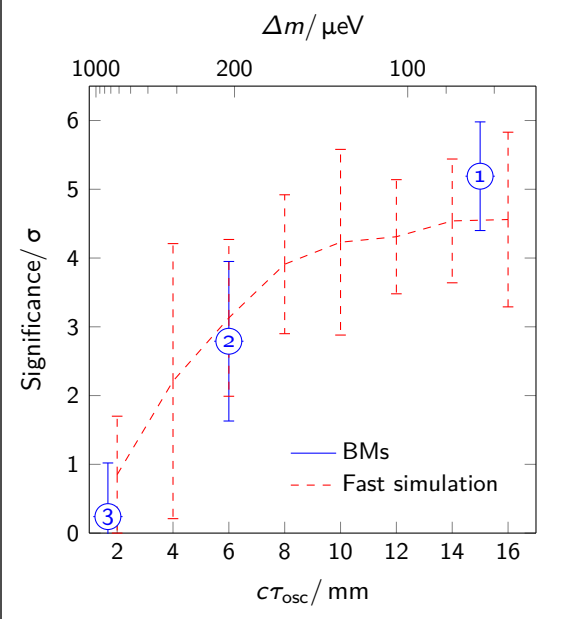
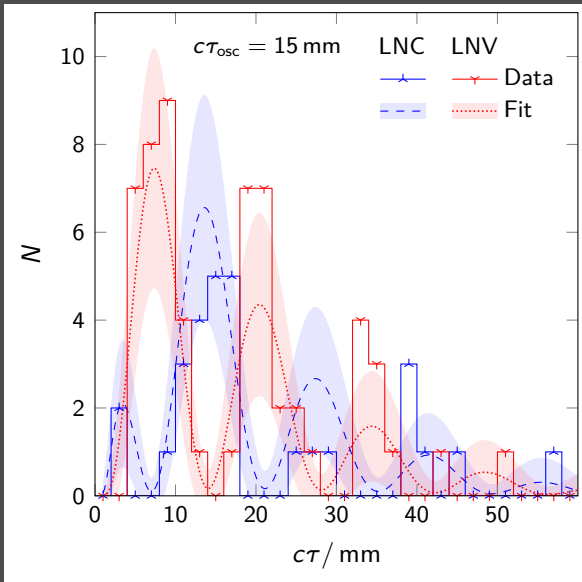
Naive lepton number violation for five BMs



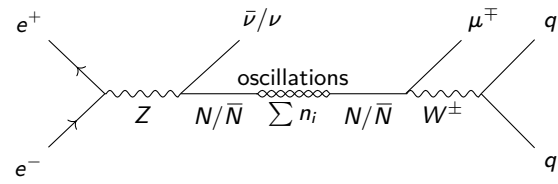


LNV can be measured
by counting the charges of the two leptons

Significance for a BM



Single charged lepton



Measurement

- LNV cannot be measured using two charges
- One can still measure angular distributions

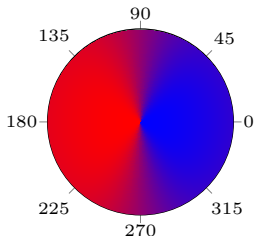
Angular dependent probability

$$P_{l^\mp}(\cos\theta, \tau) := \frac{1}{\sigma} \frac{d\sigma(\cos\theta)}{d\cos\theta} P_{\text{osc}}^{\text{LNC/LNV}}(\tau)$$

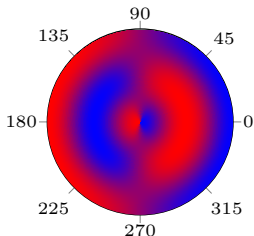
Probability of measuring charged leptons

- linked to forward backward asymmetry (FBA) of neutrino production (see 'almost Dirac limit')
- l^- from non-oscillating N or from oscillating \bar{N} (similar for l^+)

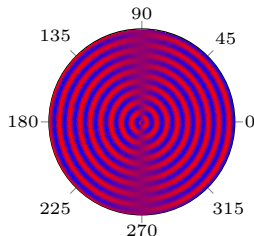
Almost Dirac limit



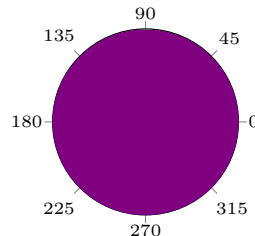
Slow oscillation



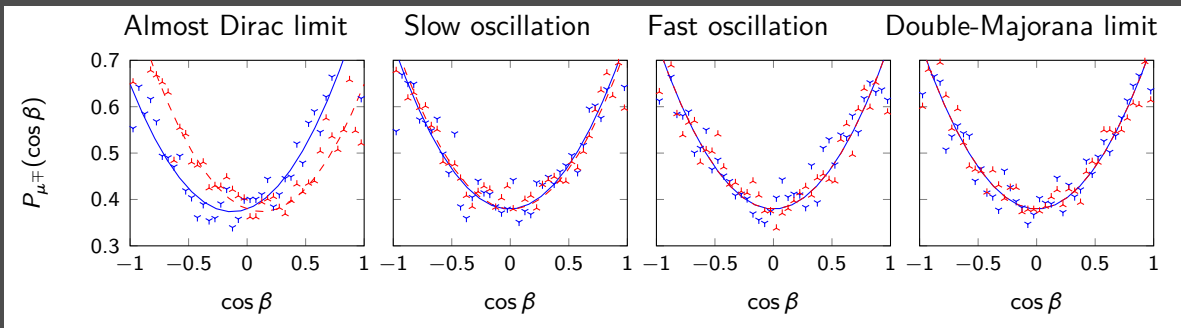
Fast oscillation



Double-Majorana limit



Time and angular integrated observable

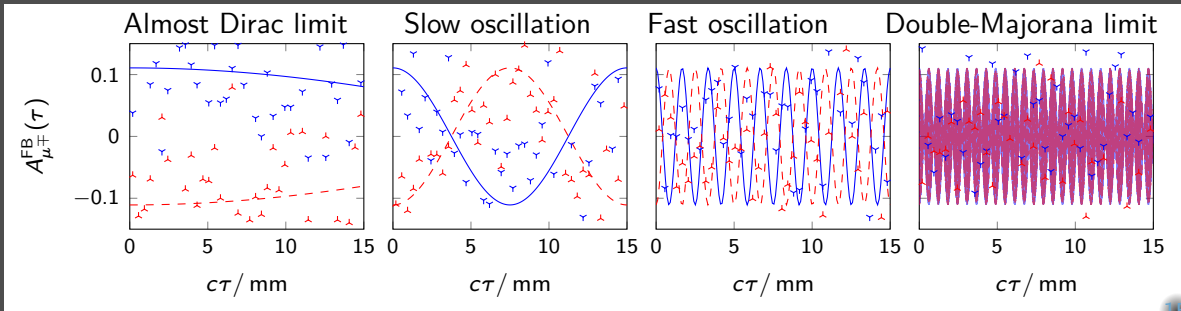


Time integrated probability

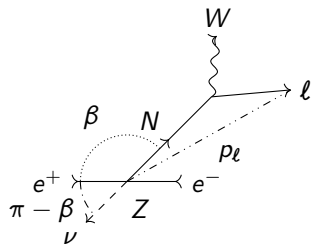
$$P_{I^\mp}(\cos \beta) := \int_0^\infty P_{I^\mp}(\tau, \cos \beta) d\tau$$

Angular integrated probability

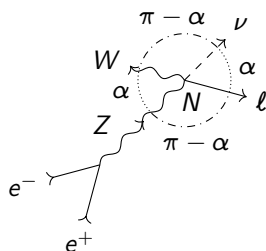
$$P_{I^\mp}^{[\beta_{\min}, \beta_{\max}]}(\tau) := \int_{\cos \beta_{\min}}^{\cos \beta_{\max}} P_{I^\mp}(\tau, \cos \beta) d \cos \beta$$



FBA



Opening angle asymmetry (OAA)

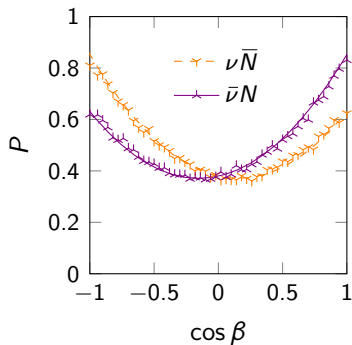


Sensitivity

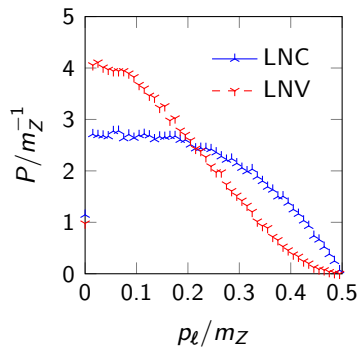
FBA N/\bar{N}
 OAA LNC/LNV

Lepton momentum modulus
 same analysis power as OAA

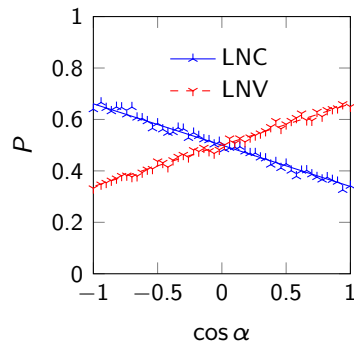
FBA

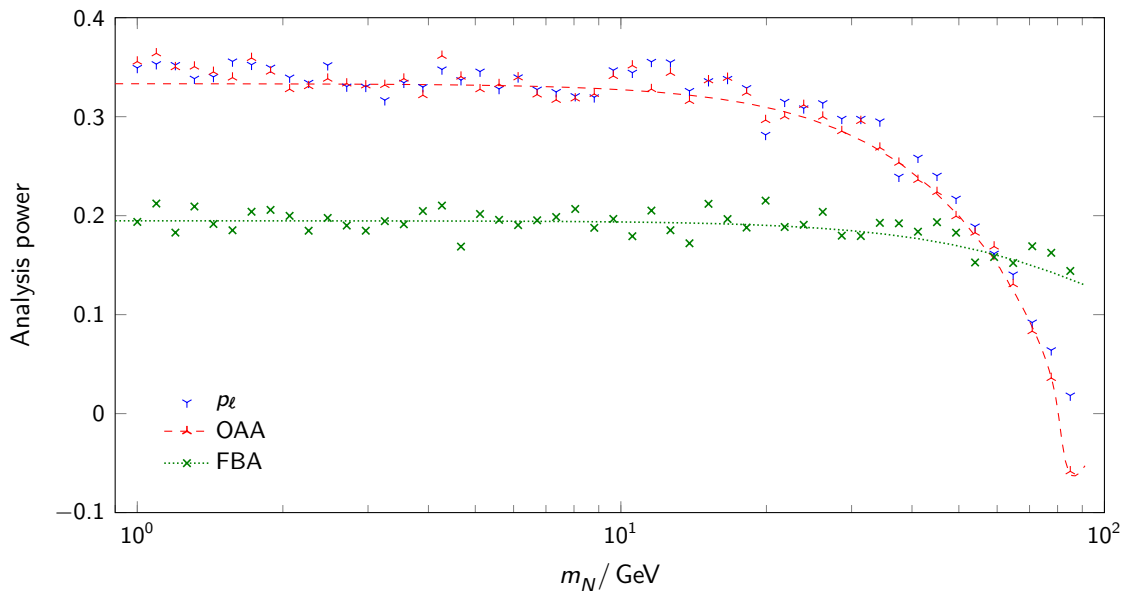


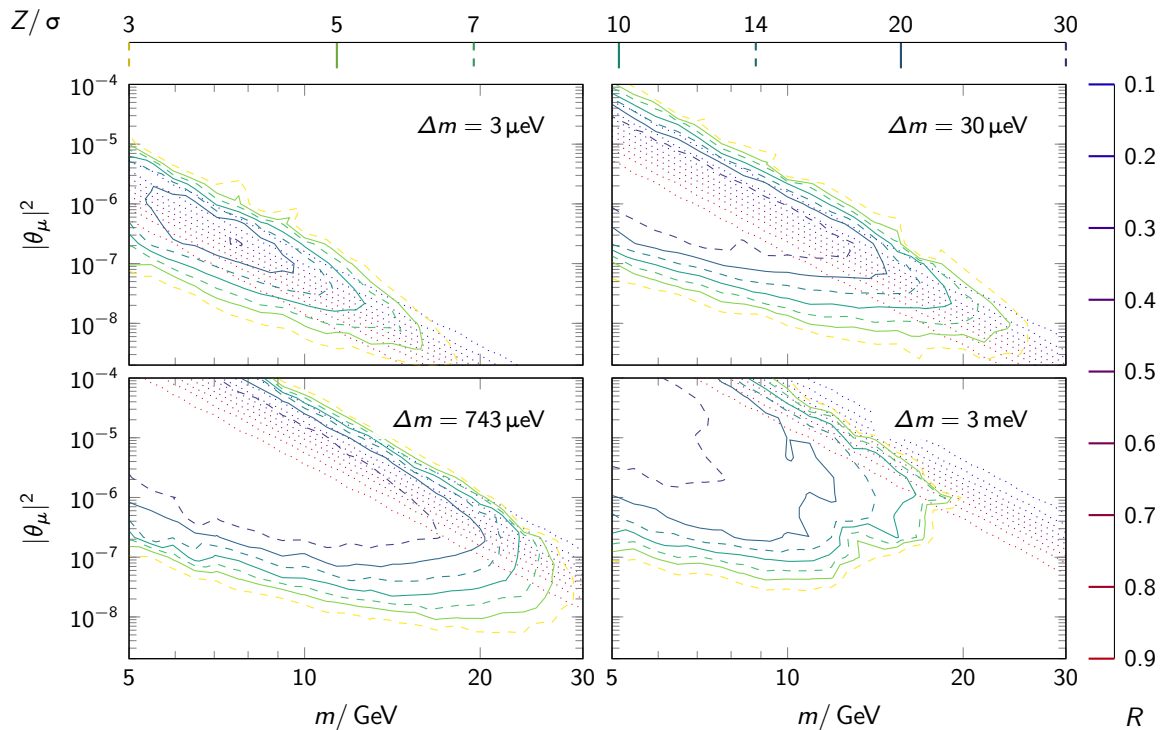
Lepton momentum modulus



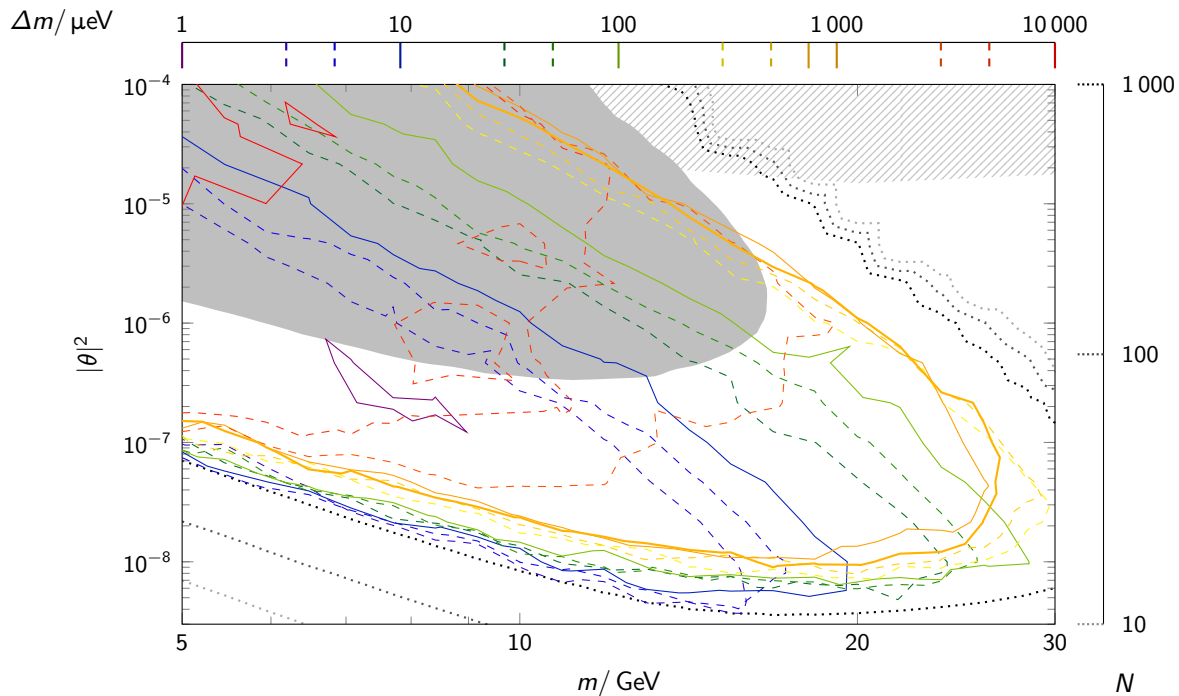
OAA



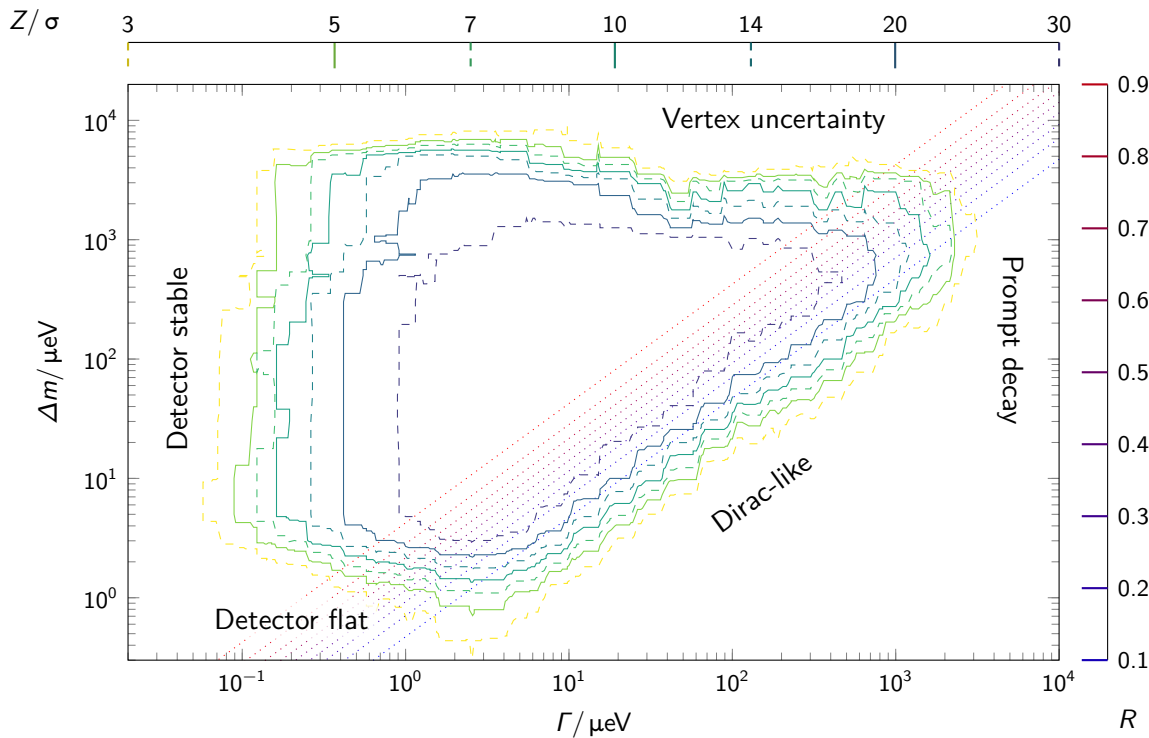


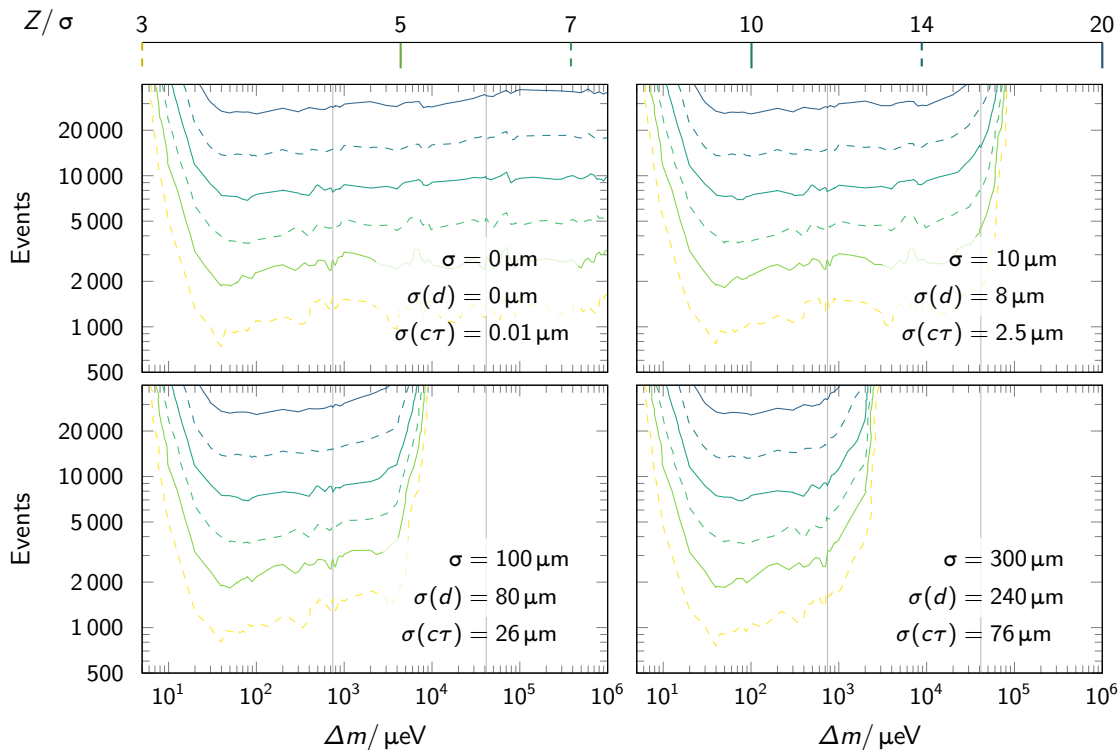


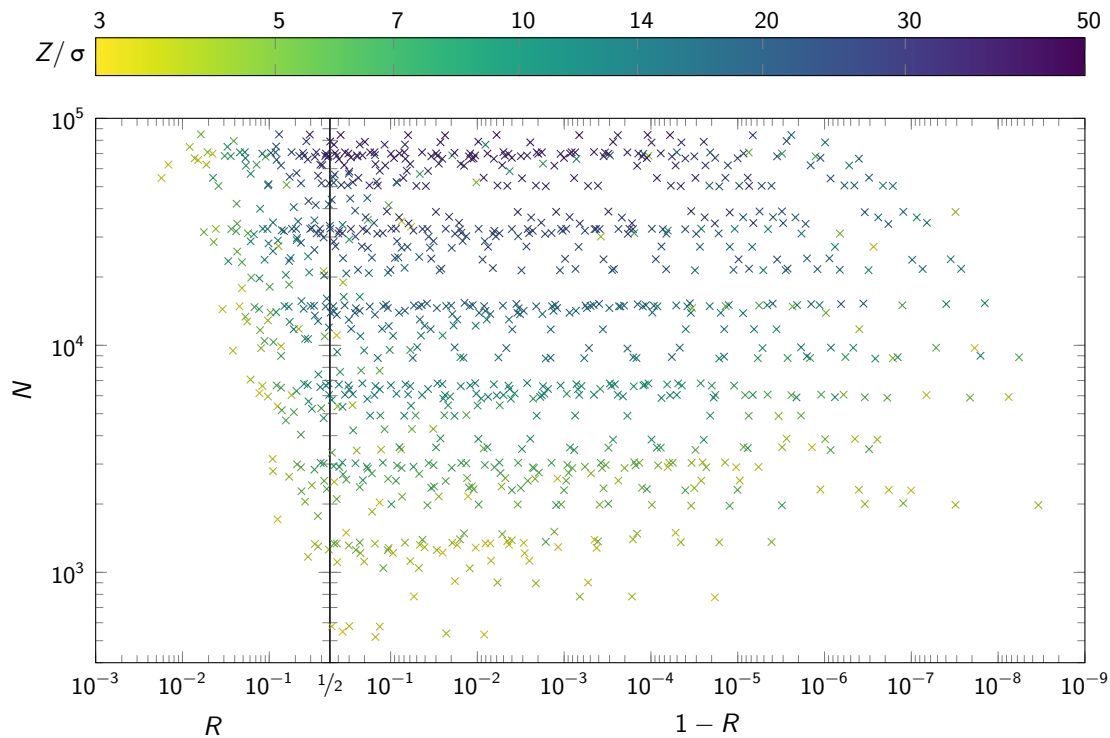
5σ discovery reach of the FCC-ee



Maximal significance of the FCC-ee







- Long-lived particles (LLP) are prevalent in the SM and expected to also appear in new physics
- One typical benchmark model scenario consists of HNLs
- Collider testable Type I seesaw models predict pseudo-Dirac HNLs
- Pseudo-Dirac HNLs can oscillate between LNC and LNV events
- These $N\bar{N}O$ s are detectable at the HL-LHC and future lepton colliders

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[FCC-hh] DOI: 10.1140/epjst/e2019-900087-0. In: *Eur. Phys. J. ST* 228.4 (2019), pp. 755–1107

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S. Antusch, J. Hajer, and J. Roszkopp. 'Simulating lepton number violation induced by heavy neutrino-antineutrino oscillations at colliders'.

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S. Antusch, J. Hajer, and J. Roszkopp. 'Decoherence effects on lepton number violation from heavy neutrino-antineutrino oscillations'.

[pSPSS]

DOI: 10.5281/zenodo.7268418 (Oct. 2022)

S. Antusch, J. Hajer, B. M. S. Oliveira, and J. Roskopp. 'pSPSS: Phenomenological symmetry protected seesaw scenario'. FeynRules model file. URL: feynrules.irmp.ucl.ac.be/wiki/pSPSS

[2212.00562]

DOI: 10.1007/JHEP09(2023)170. In: *JHEP* 09 (2023), p. 170

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[2308.07297]

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S. Antusch, J. Hajer, and B. M. S. Oliveira. 'Heavy neutrino-antineutrino oscillations at the FCC-ee'.

[2408.01389]

(Aug. 2024)

S. Antusch, J. Hajer, and B. M. S. Oliveira. 'Discovering heavy neutrino-antineutrino oscillations at the Z-pole'.

Problems measuring R_{II}

Integration limits correspond to

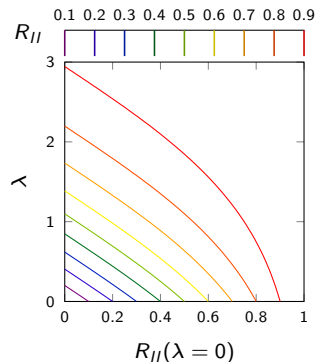
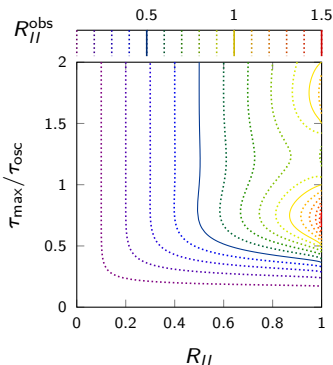
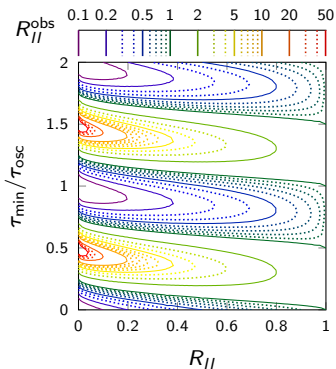
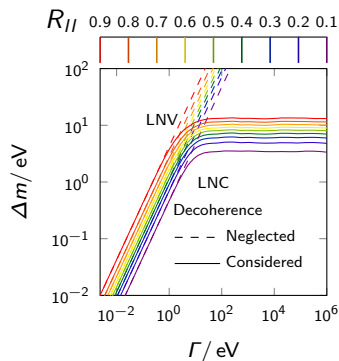
[2210.10738]

- Minimal distance cut
- Maximal measurable vertex distance

Decoherence

[2307.06208]

- Quantum mechanical oscillations can suffer from decoherence
- Calculation in external wave packet formalism
- Can increase measurable LNV drastically
- Captured by single parameter λ



Inadequate frameworks for oscillating relativistic particles

- Quantum mechanics
- Plane-wave QFT

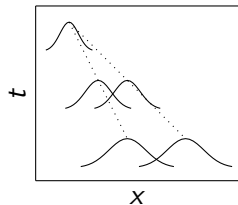
QFT with external wave packets

- Gaussian wave packets with width σ
- External widths are experiment depended parameters
- Internal widths are calculated

Transition amplitude in QFT with external wave packets Φ

$$zA(x) = \left\langle \Phi(x'') \left| \mathcal{T} \exp \left[-i \int \mathcal{H}(x') d^4x' \right] - \mathbb{1} \right| \Phi(x') \right\rangle$$

Decoherence



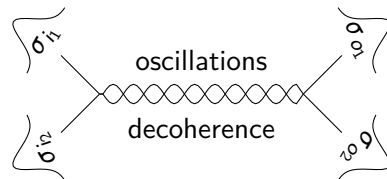
Result can be expressed with effective damping parameter λ

Damped oscillations

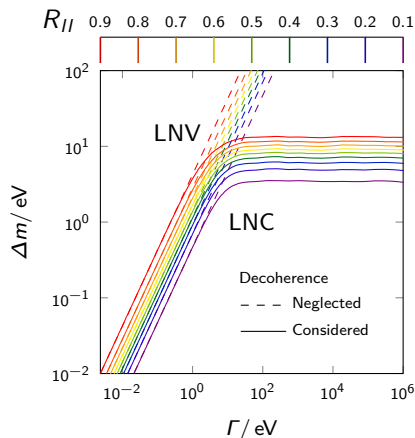
$$P_{\text{osc}}^{\text{LNC/LNV}}(\tau) = \frac{1 \pm \cos(\Delta m \tau) e^{-\lambda}}{2}$$

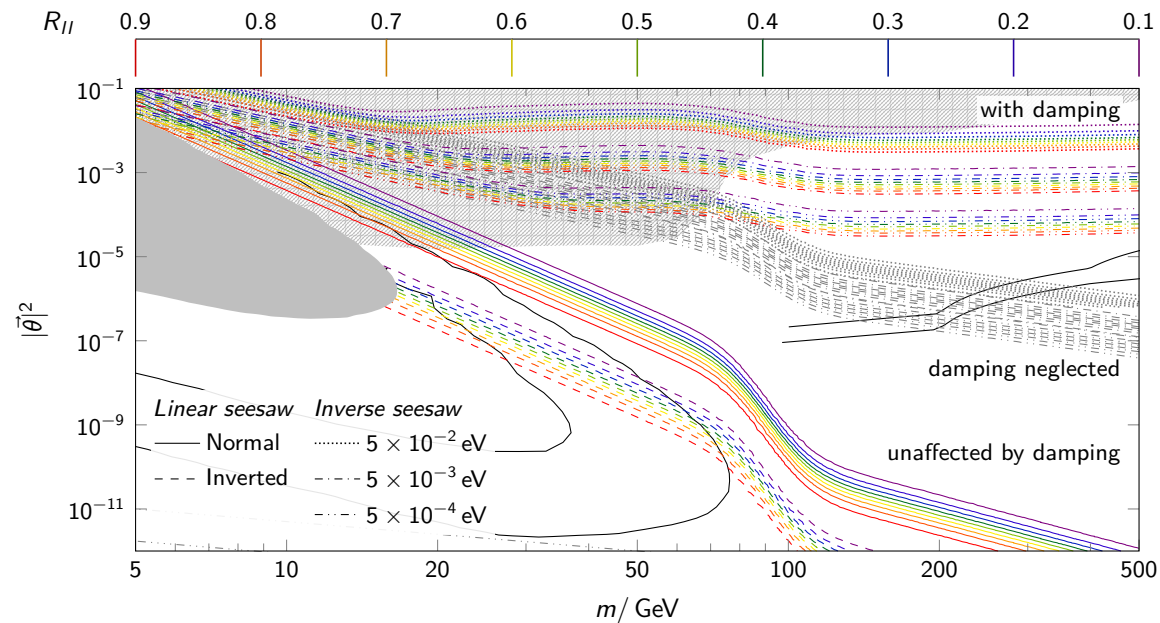
LNV can be drastically enhanced

Width of external wave packets σ



Impact on $N\bar{N}O$ s





Minimal linear seesaw

Not affected by decoherence

Inverse seesaw

LNV significantly increased