

Rare decays at Future Colliders

Aidan Wiederhold

On behalf of the FCC Phys. & Exp. & Dets Flavour group

University of Manchester,
United Kingdom

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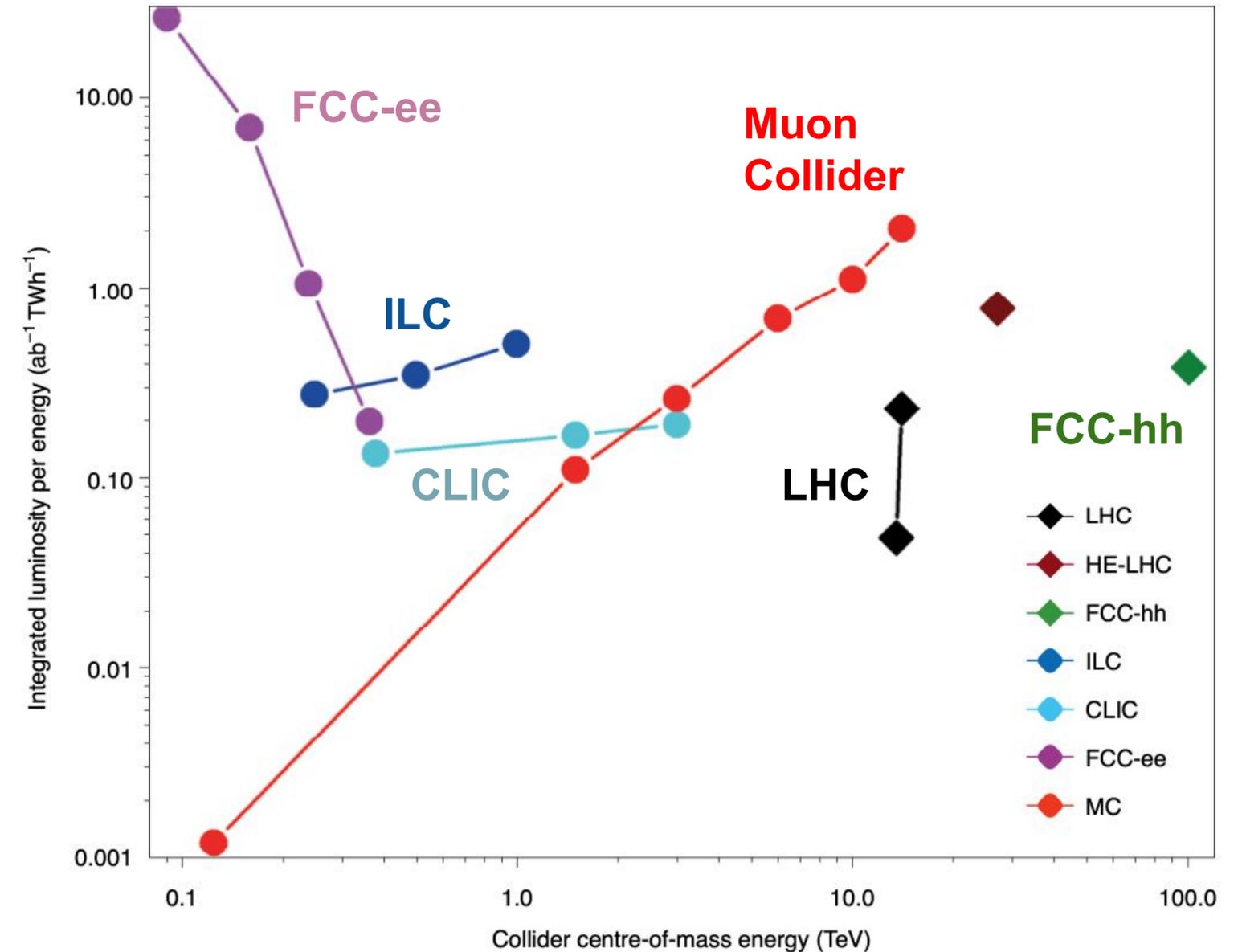
14th November 2024



The University of Manchester

Future high intensity machines?

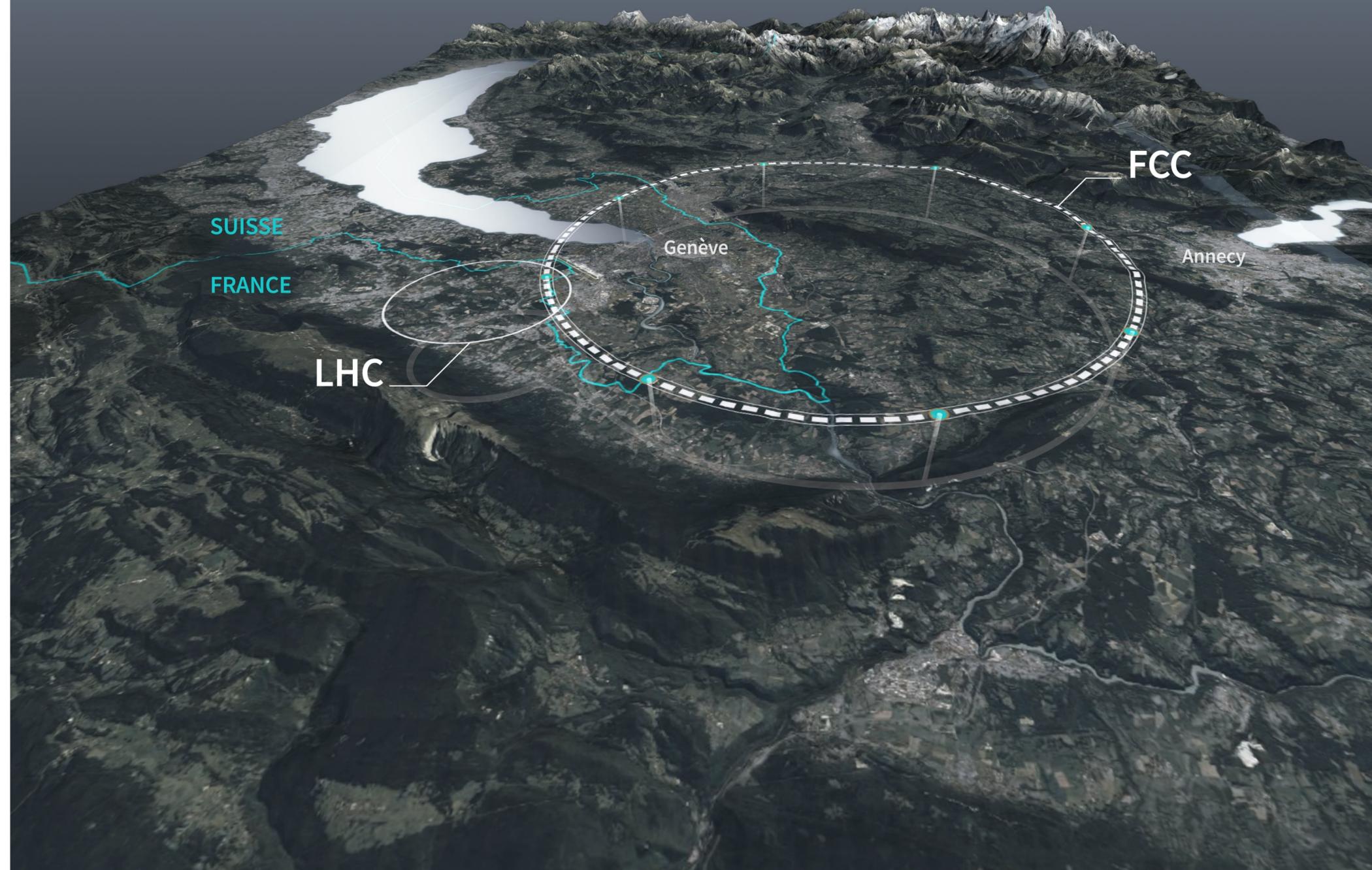
- **FCC-ee (CEPC)** is highly efficient at low COM
 - **High intensity** at the Z^0 -pole
- **Muon colliders** increase efficiency with energy
 - **High intensity** at the **energy frontier**
- pp colliders (**FCC-hh**) simpler for **high intensity** and **energy frontier**, tricky for missing energy final states
- **Linear colliders** are excellent for cost-effective **energy frontier/Higgs factory** but not the best option for high intensity
- Physics potential has plenty “back of the envelope” values available



Integrated luminosity/energy as a function of COM energy
[Federico Meloni / [arxiv:2007.15684](https://arxiv.org/abs/2007.15684)]

The FCC-ee

- 91 km circumference
- 4 collision points
- 16 years operation
- 4-running periods;
 Z^0 -pole, W^+W^- , Z^0H , $t\bar{t}$
- Most interest for rare decays is at the Z^0 -pole
- Can upgrade to FCC-hh



The FCC-ee

- Z^0 -pole run will deliver 6×10^{12} Z^0 s in total
 - “LEP in a minute”
 - $\mathcal{O}(10^{12})$ beauty hadrons produced
 - About $10 \times$ Belle II [[arxiv:1808.10567](https://arxiv.org/abs/1808.10567)]
 - LHCb U11 expects $\mathcal{O}(10^{14})$ [[LHCB-TDR-023](https://arxiv.org/abs/1808.10567)]
- Fills a niche between LHCb and Belle II
- We must determine what kind of detectors we need

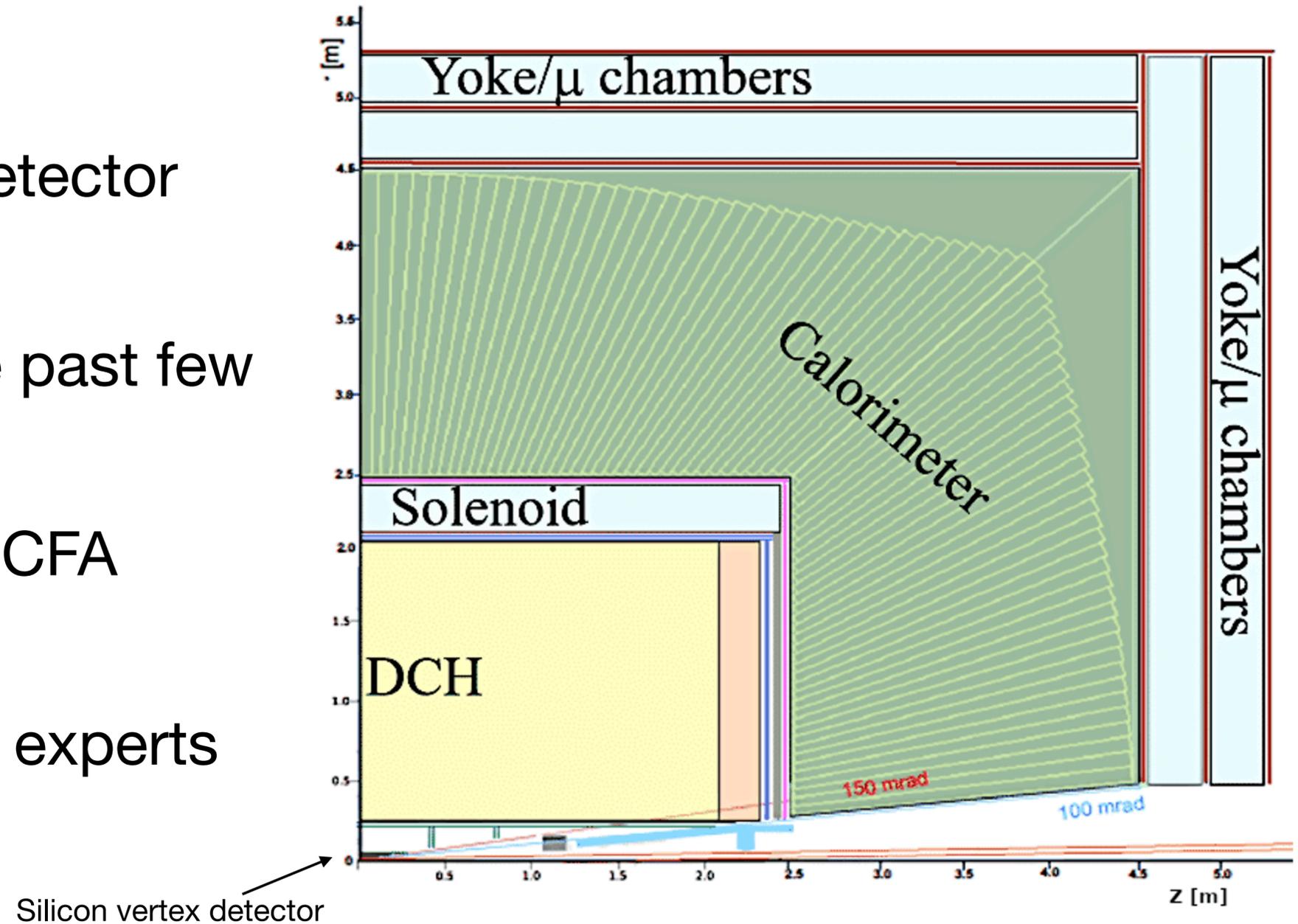
Attribute	$\Upsilon(4S)$	pp	Z^0
All hadron species		✓	✓
High boost		✓	✓
Enormous production cross-section		✓	
Negligible trigger losses	✓		✓
Low backgrounds	✓		✓
Initial energy constraint	✓		(✓)

Advantageous properties of Belle II ($\Upsilon(4S)$), LHC (pp) and FCC-ee (Z^0) [[arxiv:2106.01259](https://arxiv.org/abs/2106.01259)]

The IDEA detector

[Gabriella Gaudia: ICHEP 2022]

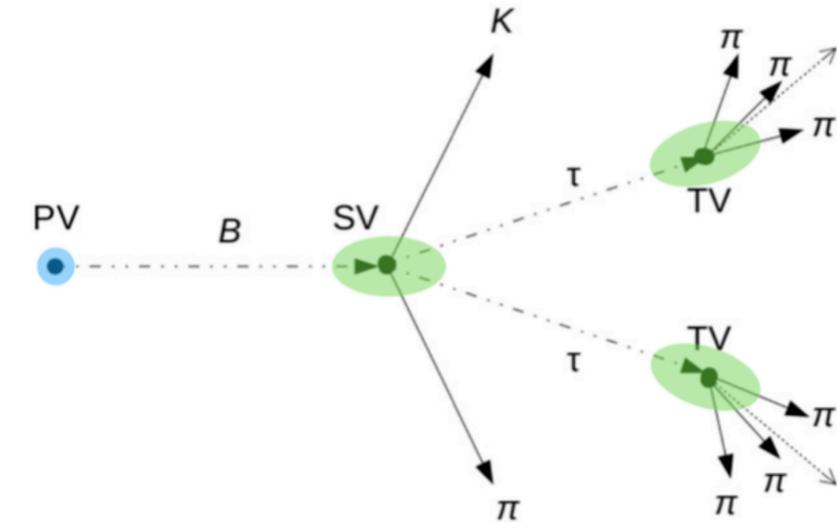
- One of the candidates for a future detector design
- Plenty development activity over the past few years
 - See talks at the FCC weeks and ECFA meetings
- Need to marry this work by detector experts with the physics requirements



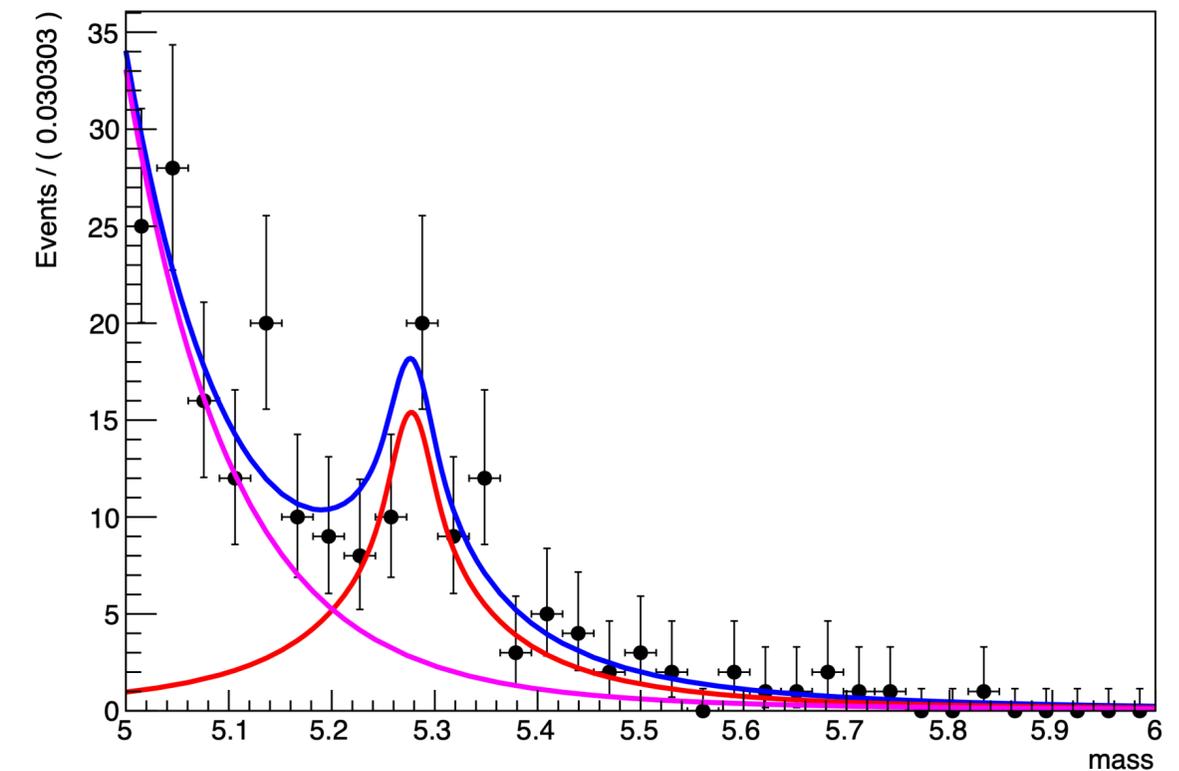
Quarter cross-section of the IDEA design

$$B^0 \rightarrow K^{*0} \tau^+ \tau^-$$

- $b \rightarrow s \tau^+ \tau^-$ yet to be observed - $\mathcal{O}(10^{-7})$ BF
 - Not expected at Belle II, expect limit $\mathcal{O}(10^{-5})$ - $\mathcal{O}(10^{-4})$
 - Current limit from BABAR $\mathcal{O}(10^{-4})$ - $\mathcal{O}(10^{-3})$ [[arxiv:1605.09637](https://arxiv.org/abs/1605.09637)]
- Many NP models expect NP to couple primarily to the Higgs and the third generation Ben Stefanek: 2nd ECFA Workshop 2023
- Focus on the the 3-prong $\tau^+ \rightarrow \pi^+ \pi^- \pi^+ \bar{\nu}$ decay
- Use energy-momentum conservation to resolve ν kinematics
- BDT trained with candidate kinematics to reduce backgrounds
- Signal yield extracted with an unbinned ML fit to the candidate B mass

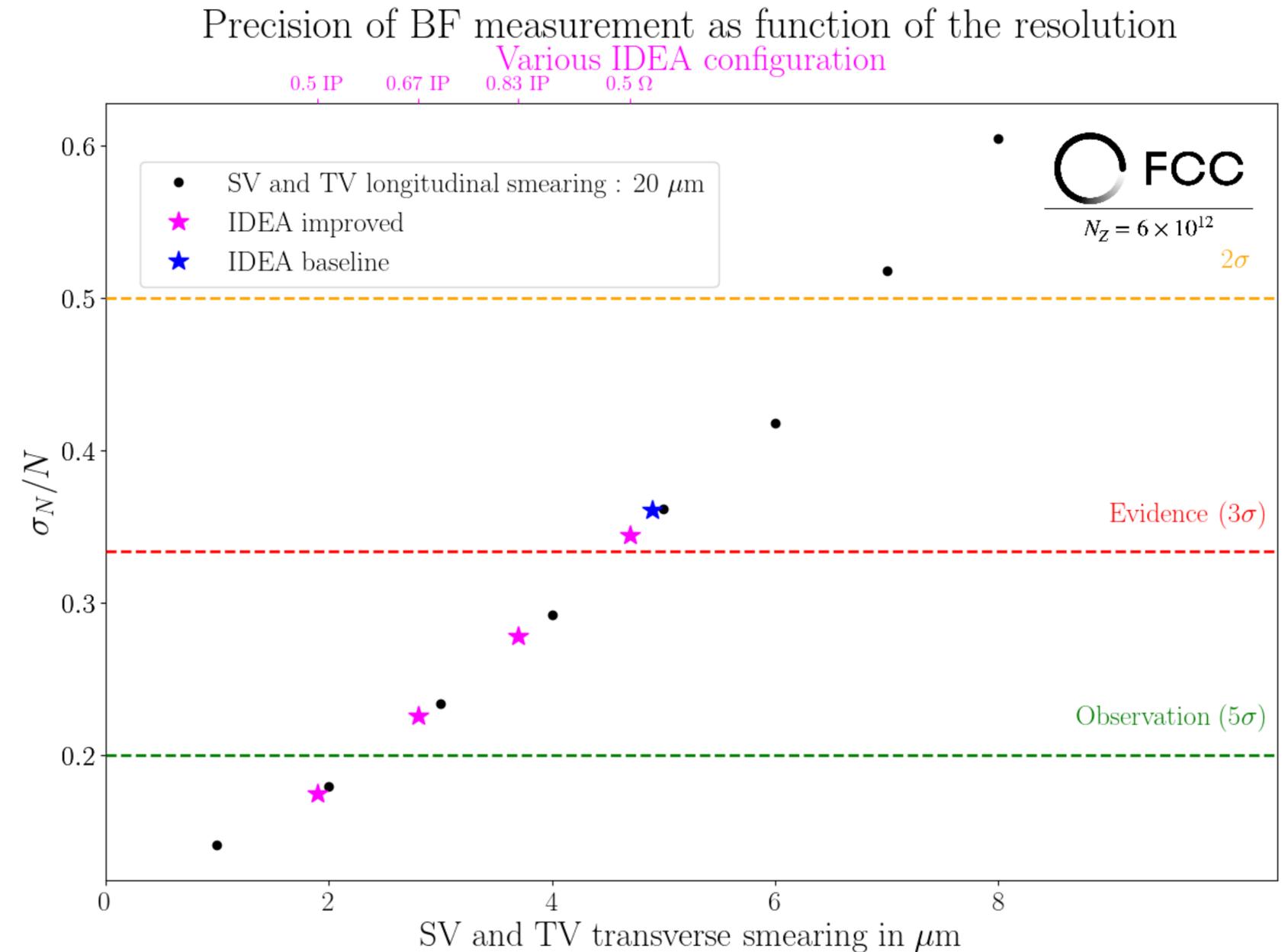


Schematic of the signal decay



B^0 candidate invariant mass fit to rescaled signal and background MC

- Emulate improved IP resolution
 - Significantly improves potential
- 30% improved single hit resolution
 $\implies > 3\sigma$
- Material budget found to be main limitation
- Very challenging



$$B^0 \rightarrow K^{*0} \tau^+ \tau^-$$

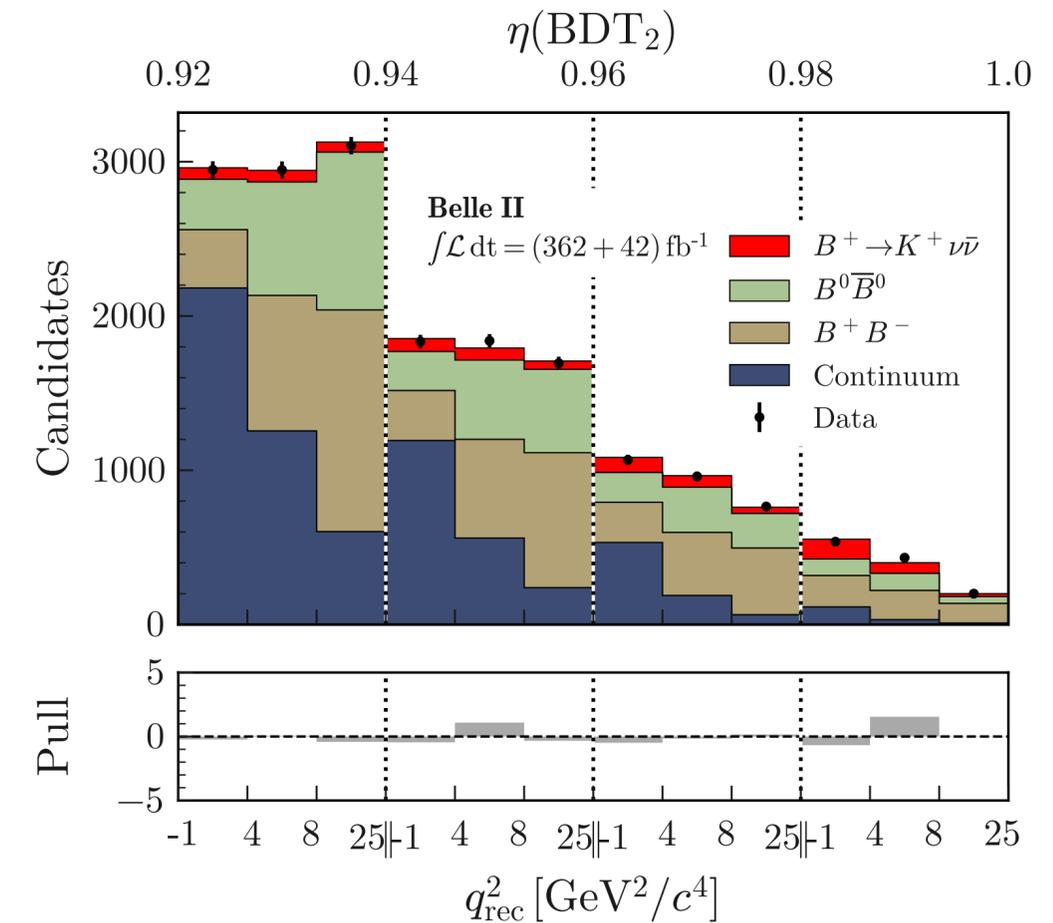
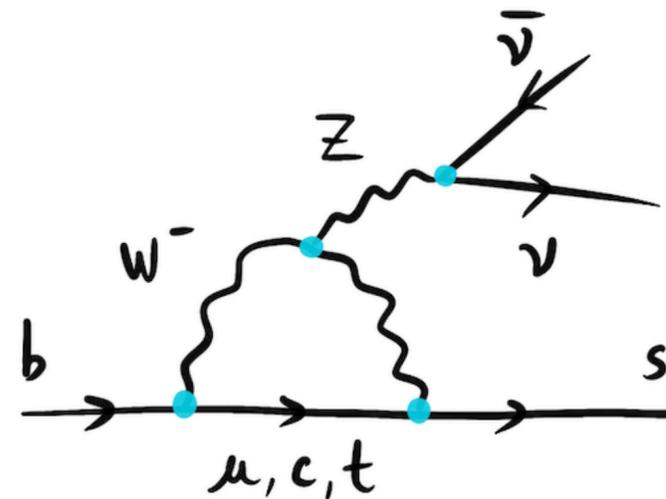
- Current FCC-ee and IDEA would not allow for discovery of this mode
 - Trying to play with detector performance - can get beyond 3 and even 5σ
- Clearly some work to do!
 - Better vertexing?
 - Easier said than done
 - Higher luminosity/longer run period?
 - Difficult/competition with other runs
 - **Consider other τ decays?**
 - **Leptonics harder to handle but would produce $\mathcal{O}(10)$ times the data**

$b \rightarrow s\nu\bar{\nu}$ motivation

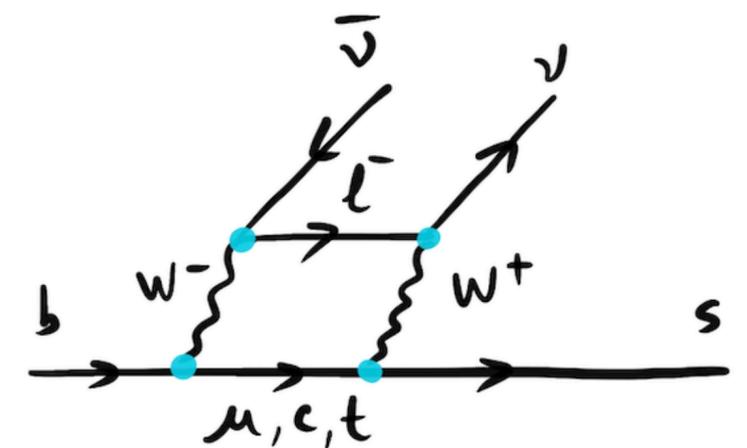
- Impossible at LHCb
- Yet to be observed, besides evidence for $B^+ \rightarrow K^+\nu\bar{\nu}$
 - 2.7σ tension with SM [arxiv:2311.14647]
- Theoretically cleaner than the corresponding $b \rightarrow sl^+l^-$
 - No long-distance charm loops!
 - Very nice for spotting BSM effects
 - Again 3rd generation leptons
- Plenty of theory interest, e.g. $R_Y^{ll\nu} = \frac{\mathcal{B}(B \rightarrow Yl^+l^-)}{\mathcal{B}(B \rightarrow Y\nu\bar{\nu})}$ [arxiv:2309.11353]
- Novel probes of CPV from new physics [arxiv:2208.10880]

Decay	B-factories	FCC-ee
$B^+ \rightarrow K^+\nu\bar{\nu}$	✓	✓
$B^+ \rightarrow K^{*+}\nu\bar{\nu}$	✓	✓
$B^0 \rightarrow K_S^0\nu\bar{\nu}$	✓	✓
$B^0 \rightarrow K^{*0}\nu\bar{\nu}$	✓	✓
$B_s^0 \rightarrow \phi\nu\bar{\nu}$	✗	✓
$\Lambda_b^0 \rightarrow \Lambda^{(*)0}\nu\bar{\nu}$	✗	✓

B decays accessible by B-factories and FCC-ee



Plot of the maximum likelihood fit for $B^+ \rightarrow K^+\nu\bar{\nu}$ from inclusive tagging



- Simulated datasets of the signal mode and inclusive background samples

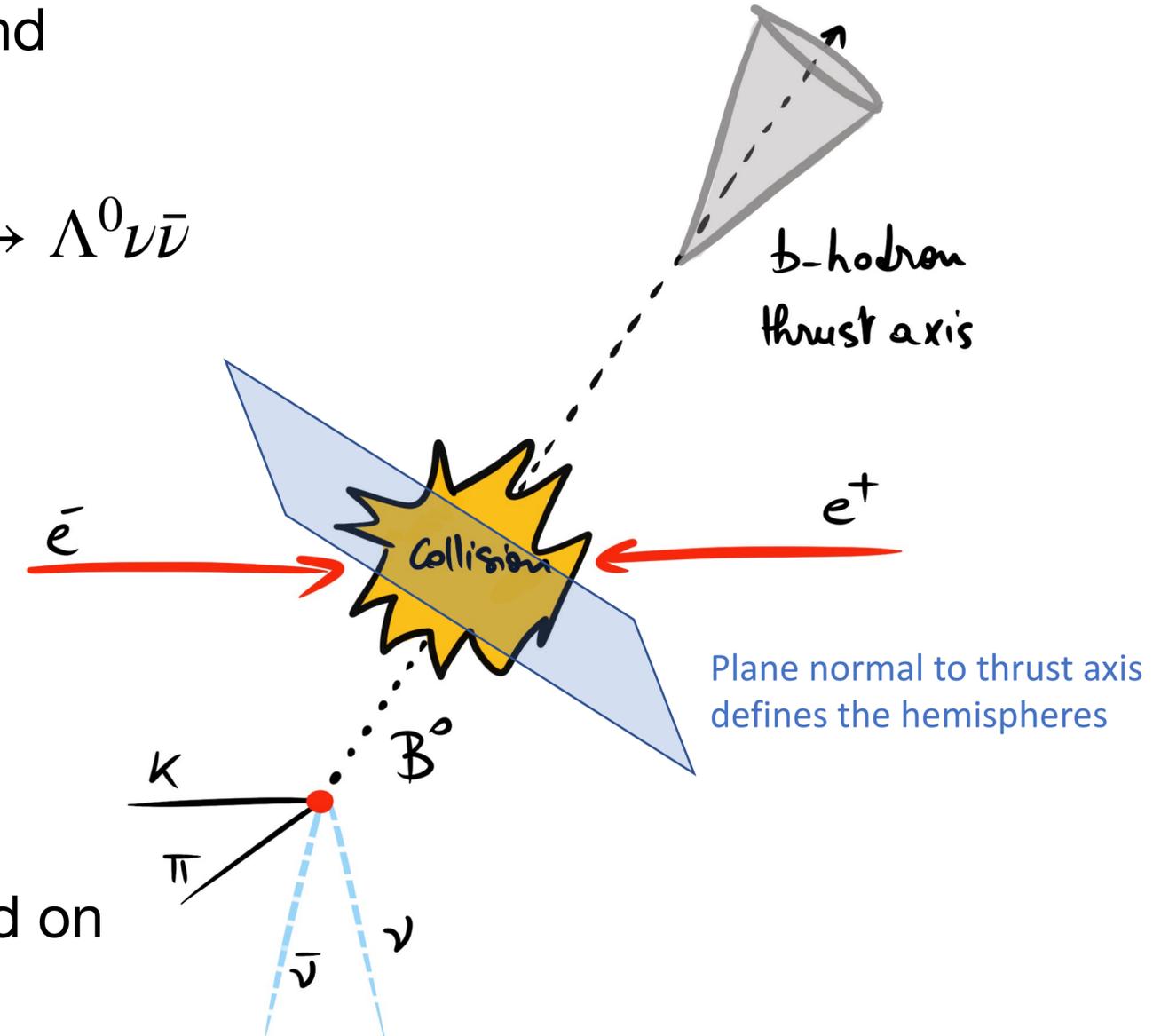
- Signal modes: $B^0 \rightarrow K^{*0} \nu \bar{\nu}$, $B_s^0 \rightarrow \phi \nu \bar{\nu}$, $B^0 \rightarrow K_S^0 \nu \bar{\nu}$, $\Lambda_b^0 \rightarrow \Lambda^0 \nu \bar{\nu}$

- $b\bar{b}$, $c\bar{c}$ and $q\bar{q}$ with $q \in \{u, d, s\}$

- Decay topology split into high- and low-energy hemispheres

- Defined by thrust axis $T = \sum_p \frac{|p \cdot \hat{n}|}{|p|}$

- Build s particle candidates from their expected final state based on vertex/track properties



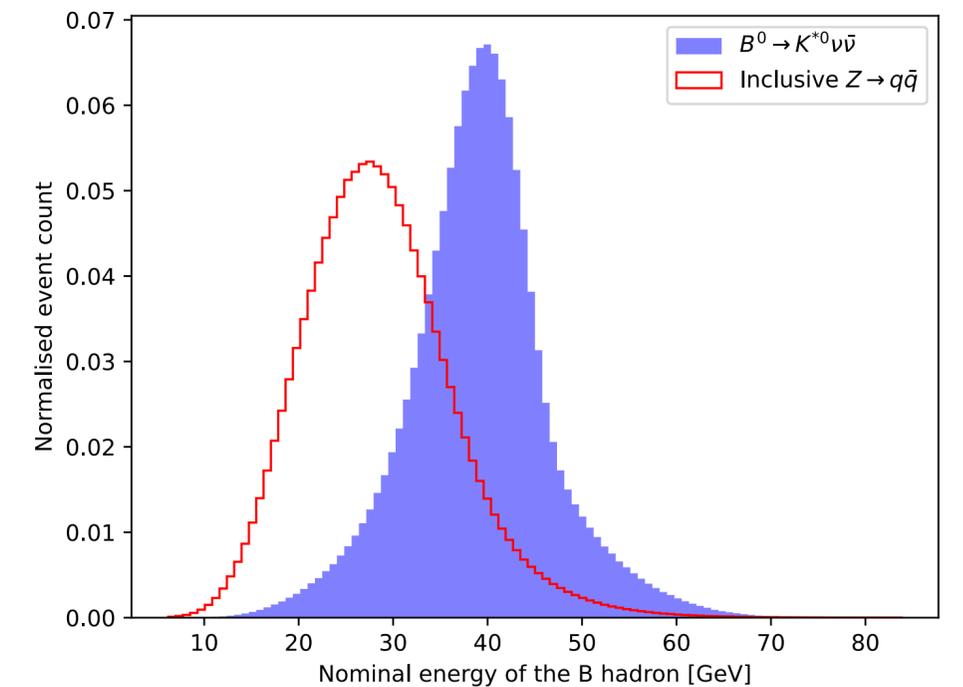
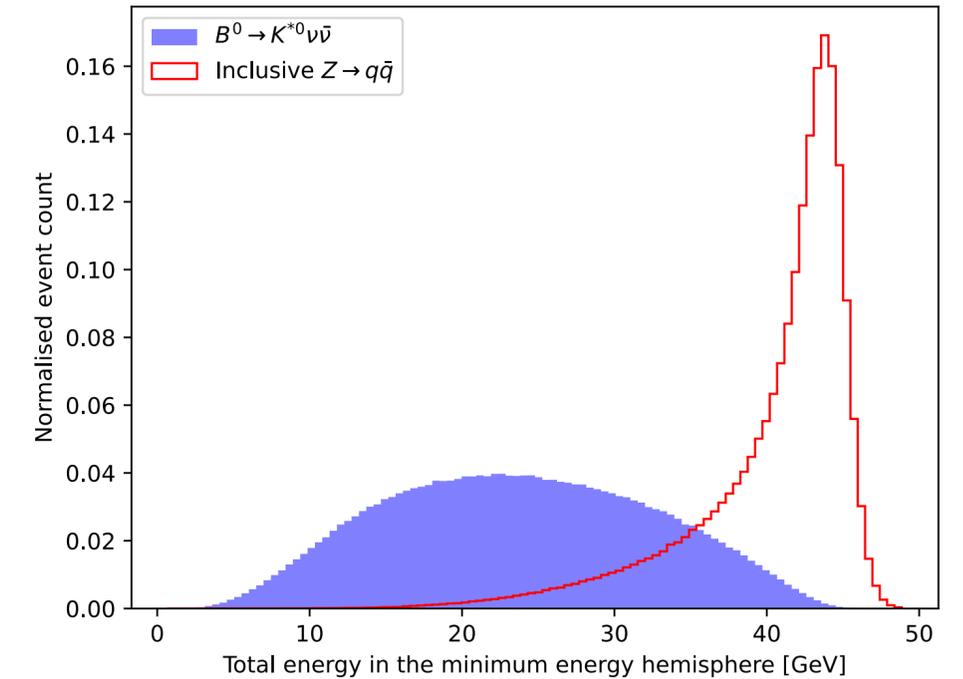
Sketch of a $B^0 \rightarrow K^* \nu \bar{\nu}$ event

- “Simple” analysis
- 2-stage BDT selection: Hemisphere properties followed by candidate properties
- Use bi-cubic splines to build efficiency maps of BDT cuts

- $S(\epsilon_{\text{BDTs}}^S) = 2N_Z \mathcal{B}(Z \rightarrow b\bar{b}) f_B \mathcal{B}(B \rightarrow Y\nu\bar{\nu}) \mathcal{B}(Y \rightarrow f) \epsilon_{\text{pre}}^S \epsilon_{\text{BDT}}^S$

- $B(\epsilon_{\text{BDTs}}^x) = \sum_{x \in \{b\bar{b}, c\bar{c}, q\bar{q}\}} 2N_Z \mathcal{B}(Z \rightarrow x) \epsilon_{\text{pre}}^x \epsilon_{\text{BDTs}}^x$

- Optimise $S/\sqrt{S+B}$ as a function of ϵ_{BDTs}^S , ϵ_{BDTs}^x in the efficiency maps

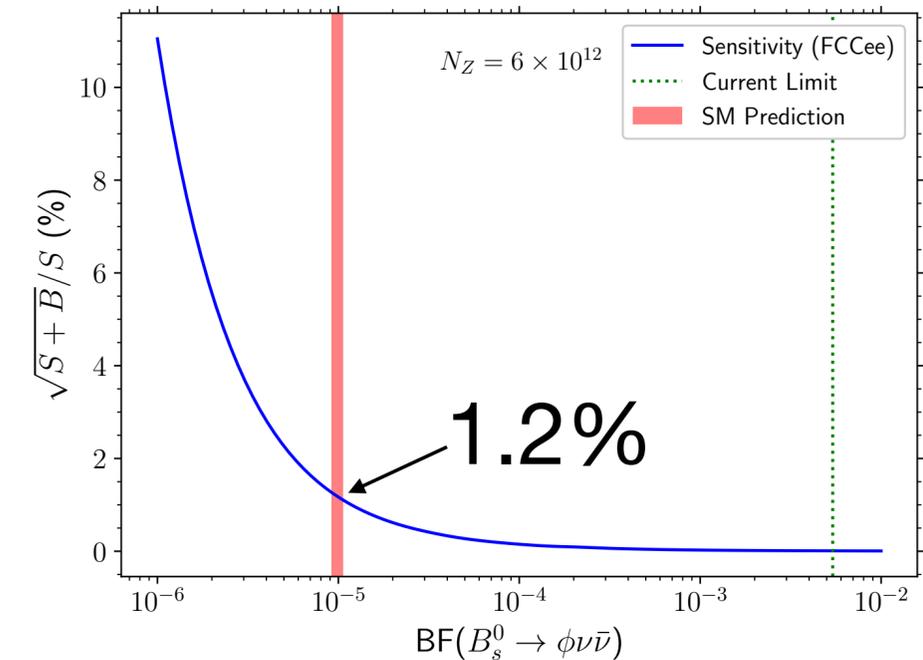
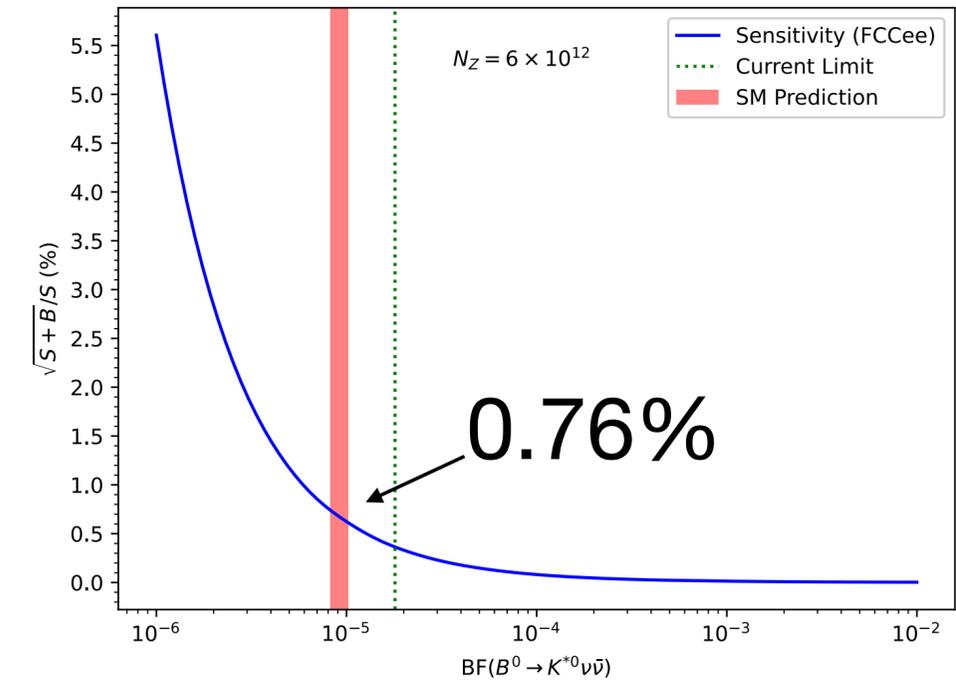


Most significant Stage 1 (top) and Stage 2 (bottom) features

$b \rightarrow s\nu\bar{\nu}$ BF sensitivity

[arxiv:2309.11353]

- Belle II expects $\mathcal{O}(10\%)$ uncertainty on $\mathcal{B}(B \rightarrow K^{(*)}\nu\bar{\nu})$ with 50 ab^{-1}
 - Exciting potential with $B^+ \rightarrow K^+\nu\bar{\nu}$
- FCC-ee assuming perfect vertex seeding and PID:
 - $\mathcal{O}(1\%)$ uncertainty for $B^0 \rightarrow K^{*0}\nu\bar{\nu}$ & $B_s^0 \rightarrow \phi\nu\bar{\nu}$
 - $\mathcal{O}(3\%)$ uncertainty for $B^0 \rightarrow K_S^0\nu\bar{\nu}$
 - $\mathcal{O}(10\%)$ uncertainty for $\Lambda_b^0 \rightarrow \Lambda^0\nu\bar{\nu}$
- CEPC study for $B_s^0 \rightarrow \phi\nu\bar{\nu}$ [arxiv:2201.07374]



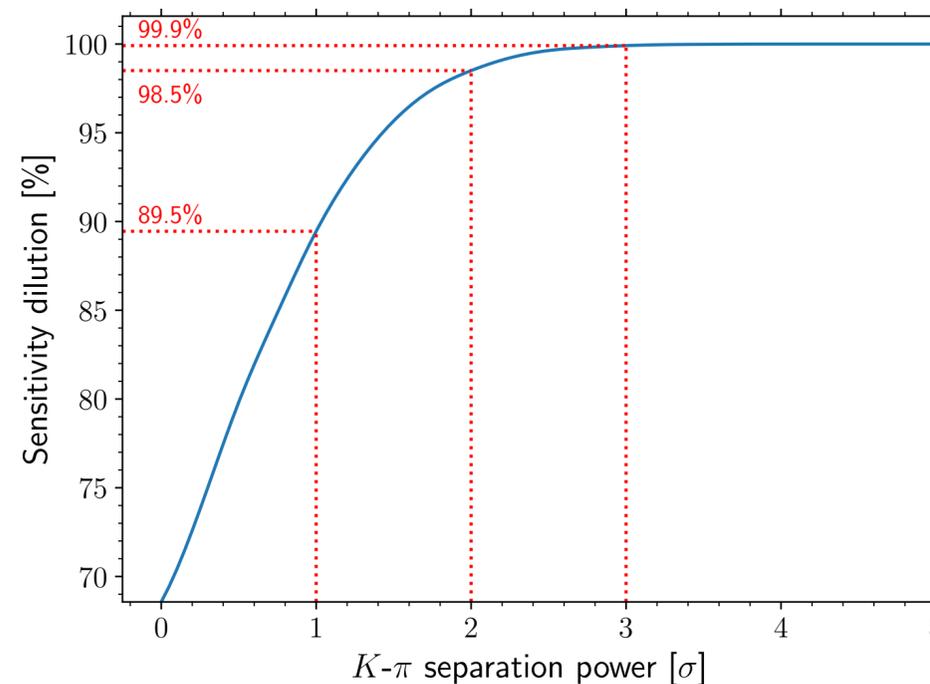
Sensitivity estimate as a function of BF for $B^0 \rightarrow K^{*0}\nu\bar{\nu}$ (top) & $B_s^0 \rightarrow \phi\nu\bar{\nu}$ (bottom)

$b \rightarrow s\nu\bar{\nu}$ detector requirements

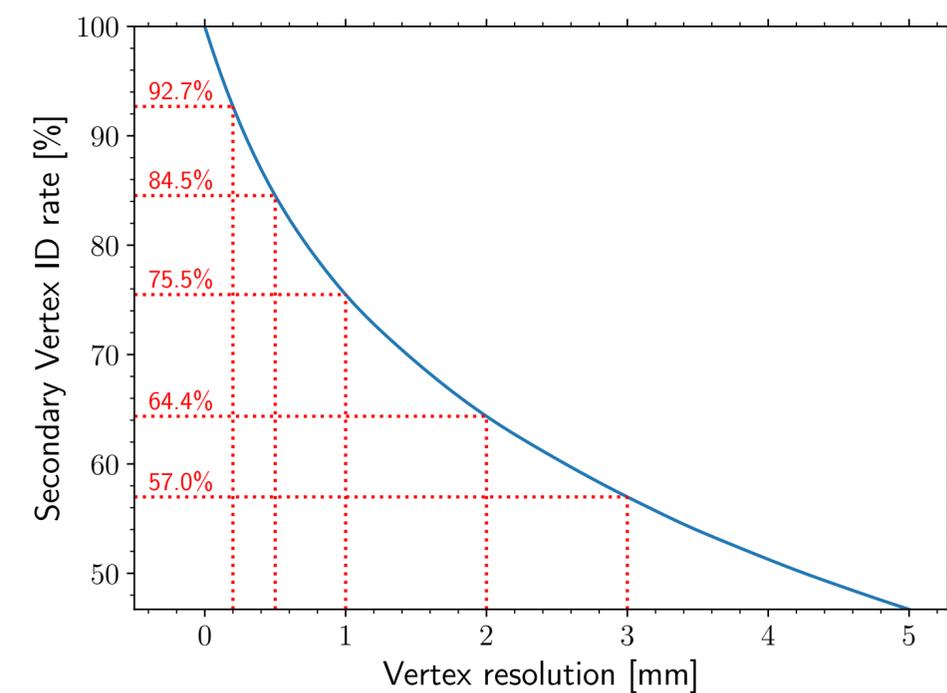
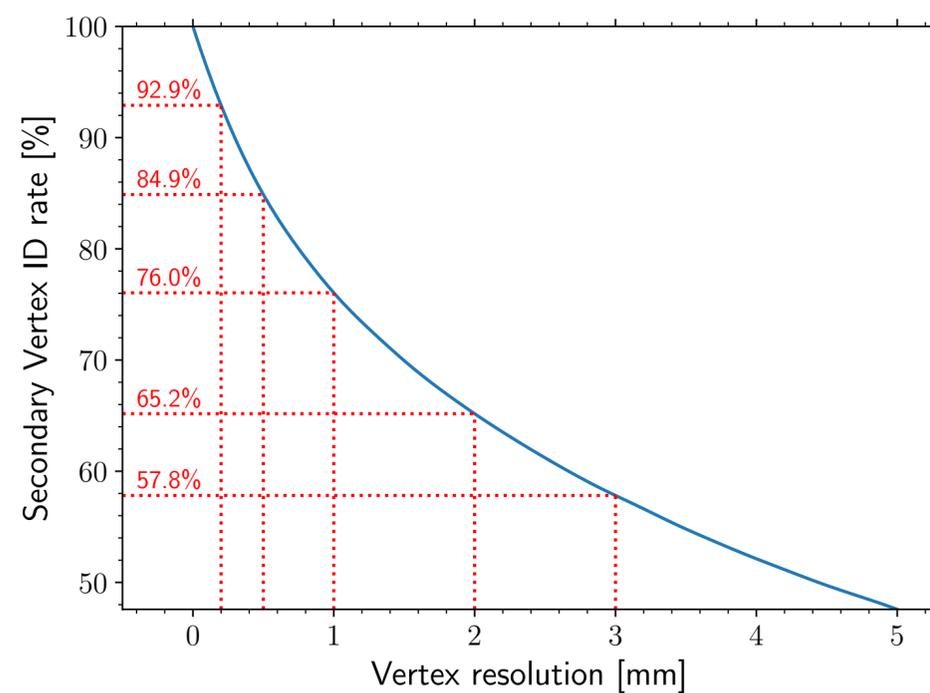
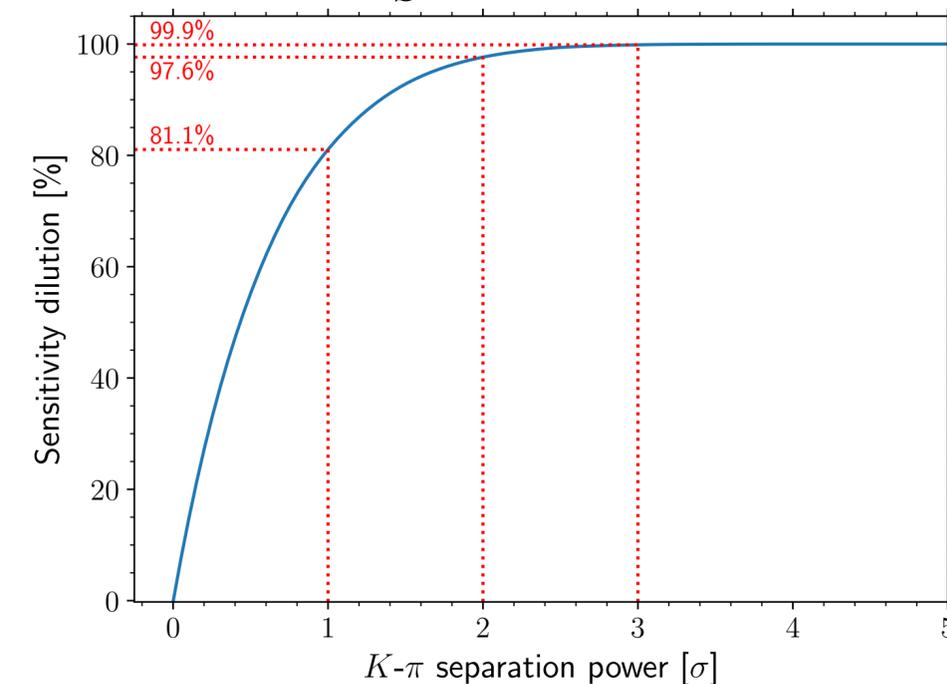
[arxiv:2309.11353]

- Robust against $\pi - K$ mis-ID with at least $\sim 2\sigma$ separation
- Require $\leq 0.2\text{mm}$ vertex resolution
 - Well above the expected resolution $\mathcal{O}(10\mu\text{m})$
- More detailed studies in the future to evaluate the full detector requirements

$$B^0 \rightarrow K^{*0}\nu\bar{\nu}$$

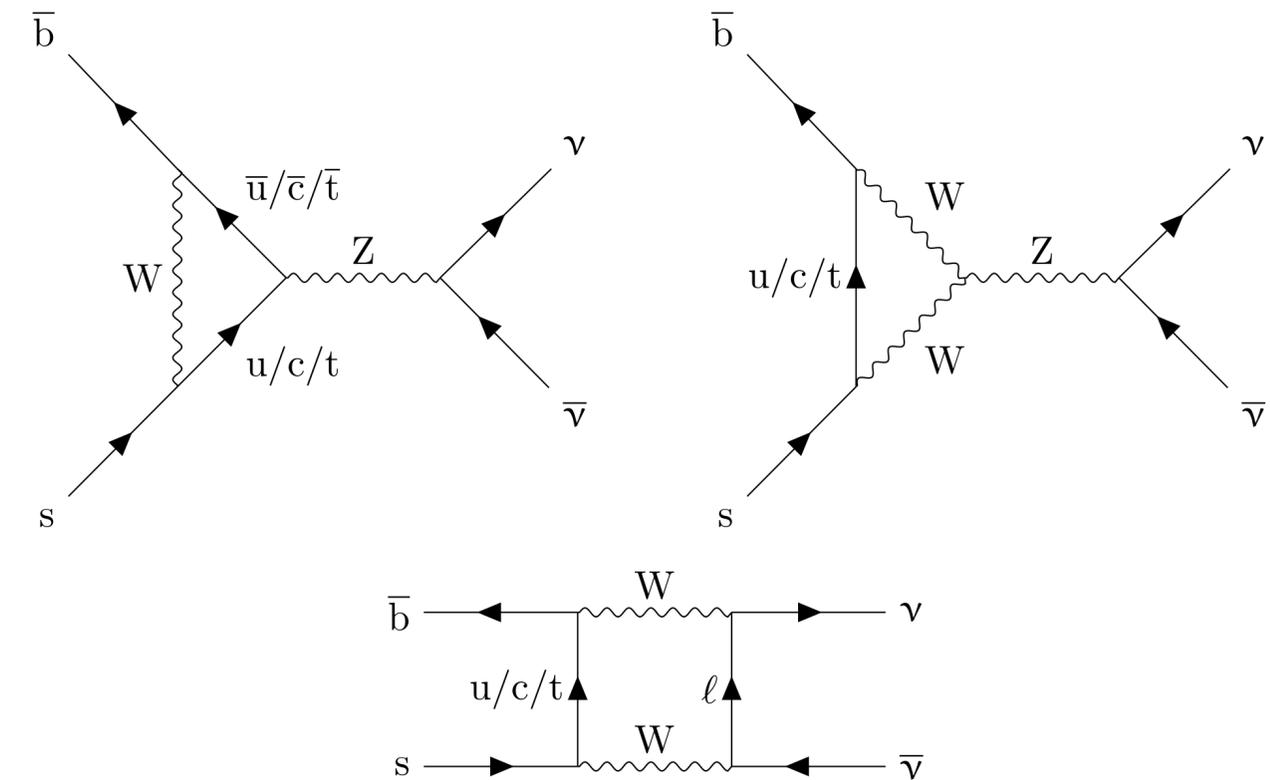


$$B_s^0 \rightarrow \phi\nu\bar{\nu}$$



$$B_{(s)}^0 \rightarrow \nu\bar{\nu}(\nu\bar{\nu})(\gamma)$$

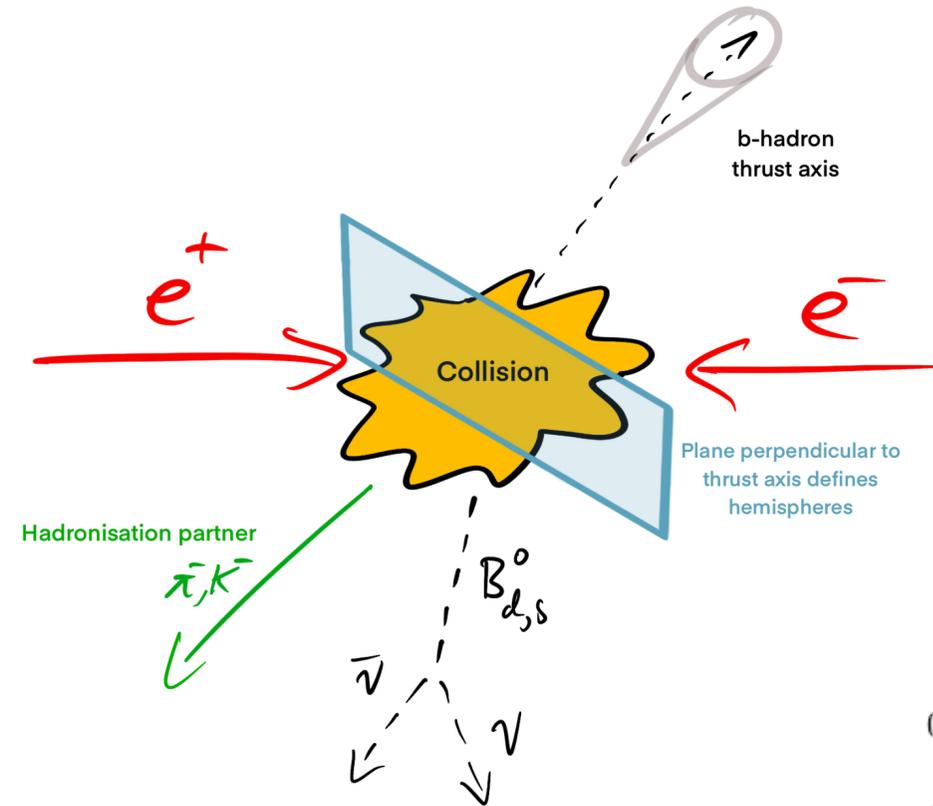
- All are yet to be observed
 - Assuming $m_\nu = 0$
helicity suppression $\implies \mathcal{B}(B_{(s)}^0 \rightarrow \nu\bar{\nu}) = 0$
 - With $m_\nu > 0$ suppressed $\propto (m_\nu/m_B)^2 - \mathcal{O}(10^{-25})$
 - $\mathcal{B}(B_{(s)}^0 \rightarrow \nu\bar{\nu}\nu\bar{\nu}) - \mathcal{O}(10^{-15})$ [[arxiv:1809.04606](#)]
 - $\mathcal{B}(B_{(s)}^0 \rightarrow \nu\bar{\nu}\nu\bar{\nu}\gamma) - \mathcal{O}(10^{-9})$ [[arxiv:9604378](#)]
- Belle II expect sensitivity down to 10^{-6} for B^0 and 10^{-5} for B_s^0
- γ mode potentially in reach of a Tera-Z facility with SM conditions
- Otherwise observation \implies **unambiguous new physics**



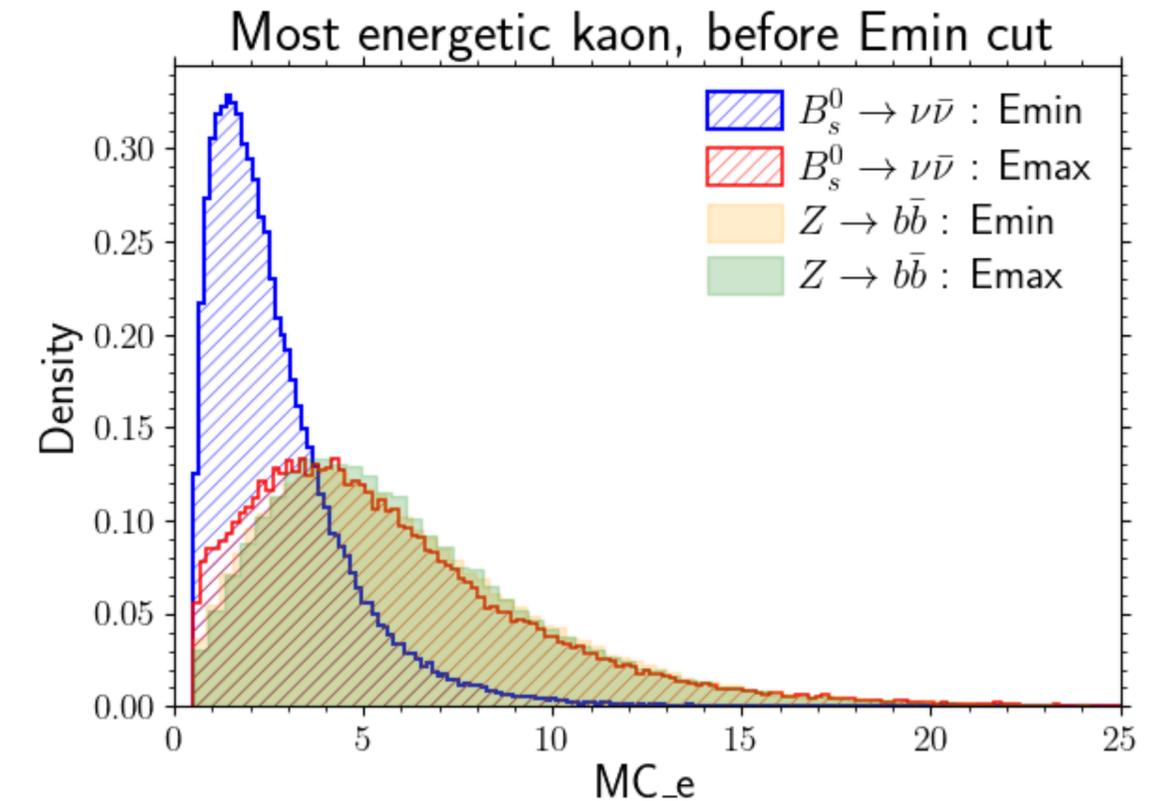
Simplest Feynman diagrams for $B_s^0 \rightarrow \nu\bar{\nu}$

$$B_{(s)}^0 \rightarrow \nu\bar{\nu}(\nu\bar{\nu})(\gamma)$$

- Study is WIP - just B_s^0 for now
- Analysis setup like $b \rightarrow s\nu\bar{\nu}$
- No s candidate to build
 - Signal hemisphere \implies hardest h from hadronisation: low p , from PV
 - Other \implies hardest h from a decay: high p , displaced vertex



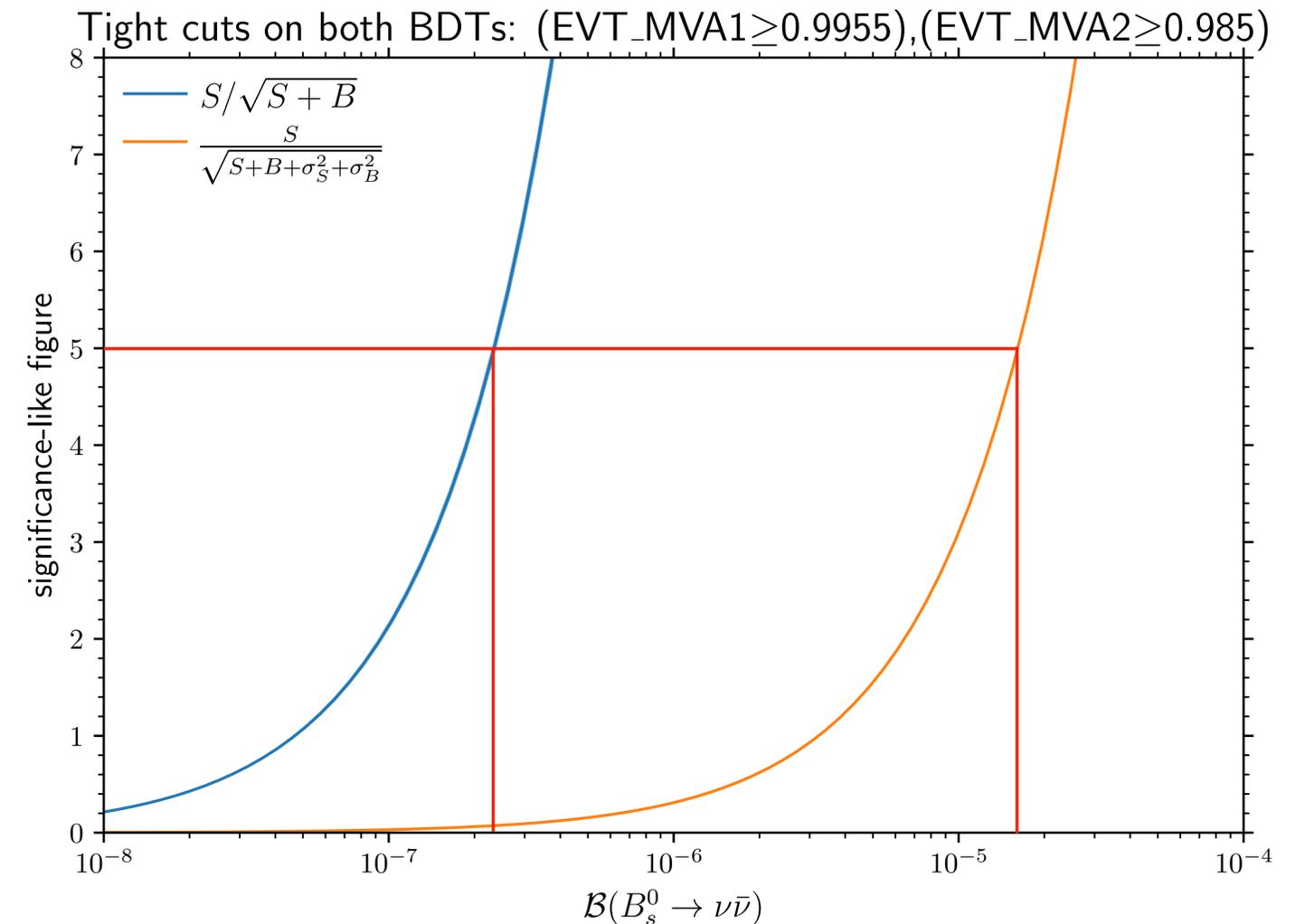
Sketch of a $B_{(s)}^0 \rightarrow \nu\bar{\nu}$ event



Signal and background separation from hadronisation partner kinematics

$$B_{(s)}^0 \rightarrow \nu\bar{\nu}(\nu\bar{\nu})(\gamma)$$

- Clearly needs more work to squeeze down below 10^{-5}
- Highly dependent on efficiency of background rejection
- Considering exclusive MC samples



Dependence of significance on BF: with perfect background expectation (blue) and including the error on the S, B expectations (orange)

Not an exhaustive list

- Ratio of $B_{(s)}^0 \rightarrow \mu^+ \mu^-$, powerful test of minimal flavour violation
- $b \rightarrow s \mu^+ \mu^-$ beyond the HL-LHC high- p_T searches (FCC-hh/ μ) [[arxiv:2205.13552](https://arxiv.org/abs/2205.13552)]
- $b \rightarrow s \gamma, b \rightarrow s e^+ e^-$
- Other flavour rare decays
- $H/t\bar{t}$ runs
 - Flavour violation - $H \rightarrow bs, cu$ & $H \rightarrow \tau\mu, \tau e$ (similar for Z^0) [[arxiv:1209.1397](https://arxiv.org/abs/1209.1397), [arxiv:1202.5704](https://arxiv.org/abs/1202.5704)]
 - $t \rightarrow Hc, Hu$
- Muon colliders
 - $\mu^+ \mu^- \rightarrow b\bar{s} + s\bar{b}$ complementary probes to $b \rightarrow s \mu^+ \mu^-$

Summary

- FCC-ee can fill the niche between LHCb and Belle II
 - Rely on building from previous knowledge - e.g. SuperKEKB luminosity struggles
- Never before observed processes will be possible
 - $B_s^0 \rightarrow \phi \nu \bar{\nu}$, $\Lambda_b^0 \rightarrow \Lambda^0 \nu \bar{\nu}$
 - $b \rightarrow s \tau^+ \tau^-$
 - Potential for differential measurements, novel CPV searches etc...
- Existing limits and branching fractions will be improved upon
- Future work
 - Consider $B^+ \rightarrow K^+ \nu \bar{\nu}$ and $B_c^+ \rightarrow D^+ \nu \bar{\nu}$
 - Detailed detector requirement studies
- Muon colliders can provide complementary high intensity experiments

Thanks for listening

- Inspiration from
 - Matt Kenzie - [ECFA-UK](#)
 - Yasmine Amhis - [QCD@LHC 2024](#)
 - Jure Zupan - [Inaugural US Muon Collider Meeting](#)