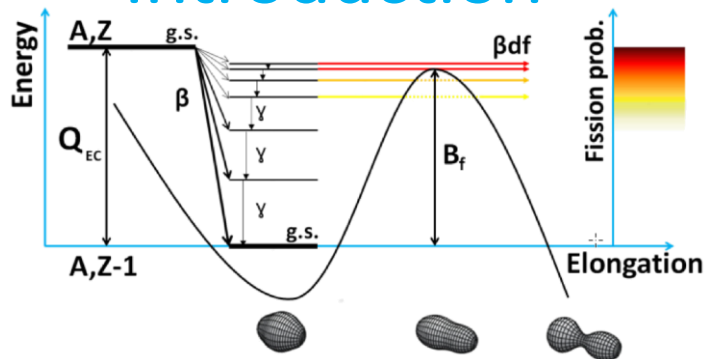
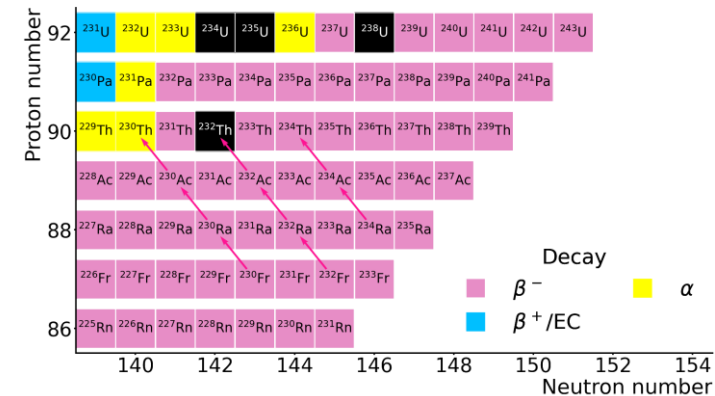
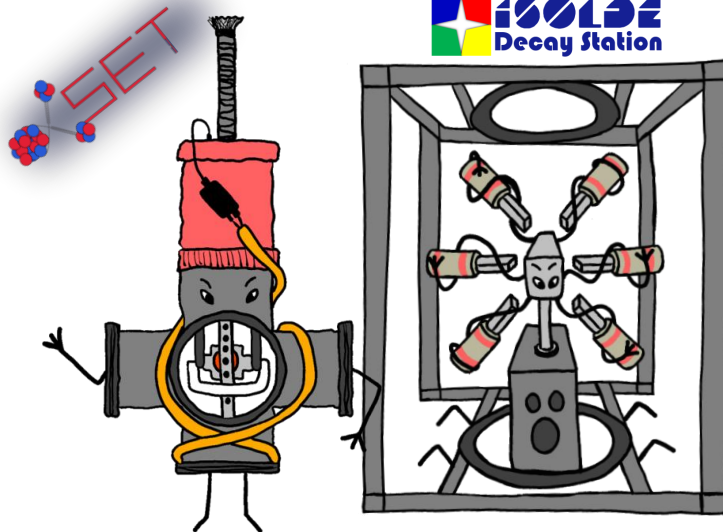


# Beta-delayed fission of neutron-rich actinides

## Introduction

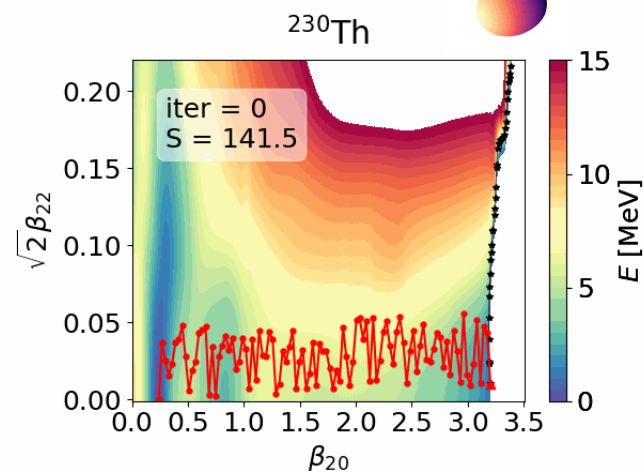


ISOLDE  
Decay Station

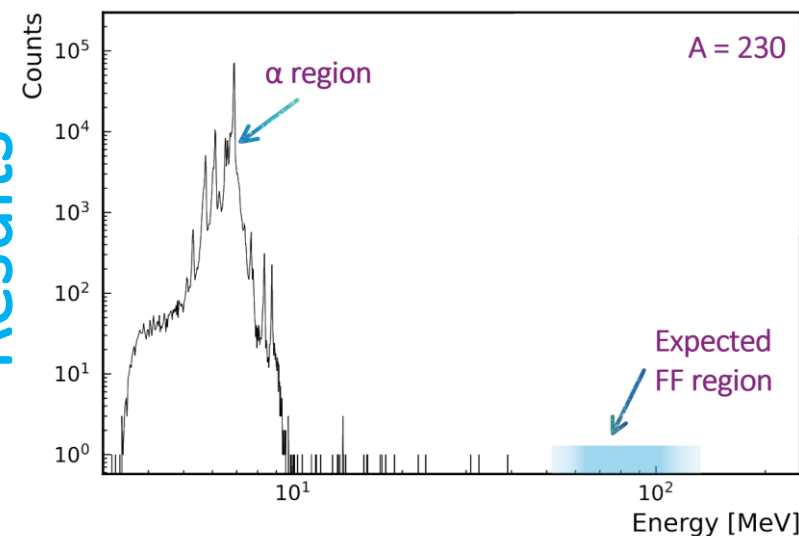


LOI216

## βDF with *PyneB*



## Results

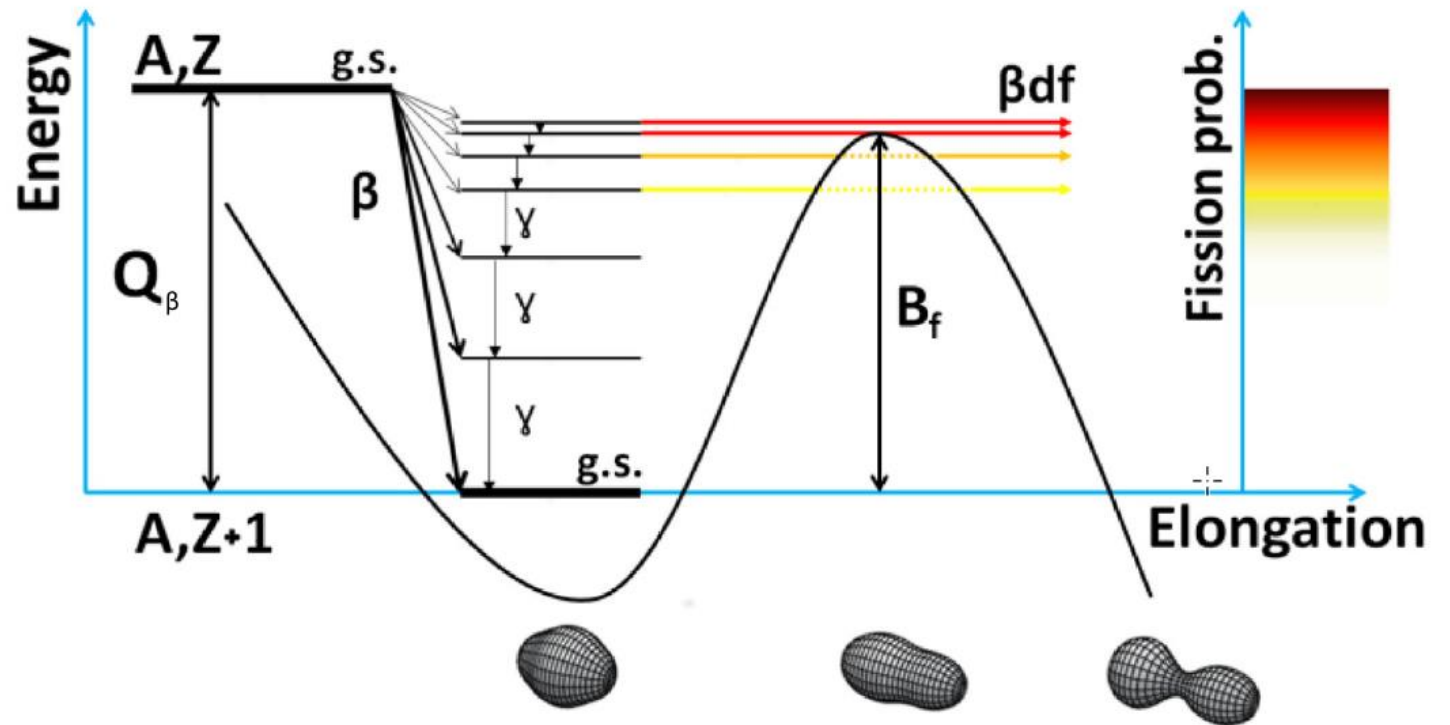


# $\beta$ -delayed fission

- Two-step process:
  1.  $\beta$ -decay
  2. fission

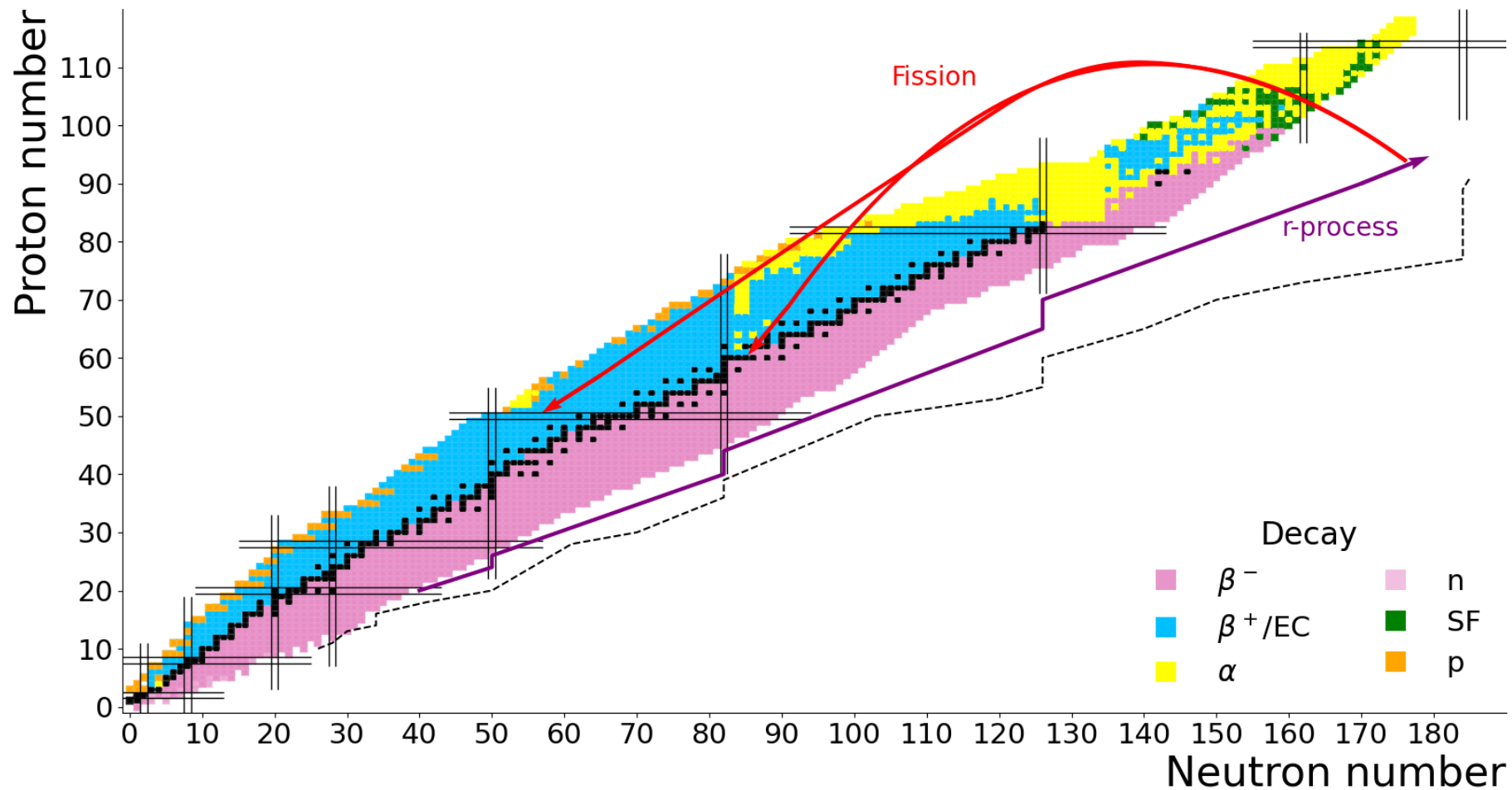
- Probability of  $\beta$ DF

$$P_{\beta\text{DF}} = \frac{N_{\beta\text{DE}}}{N_{\beta}}$$

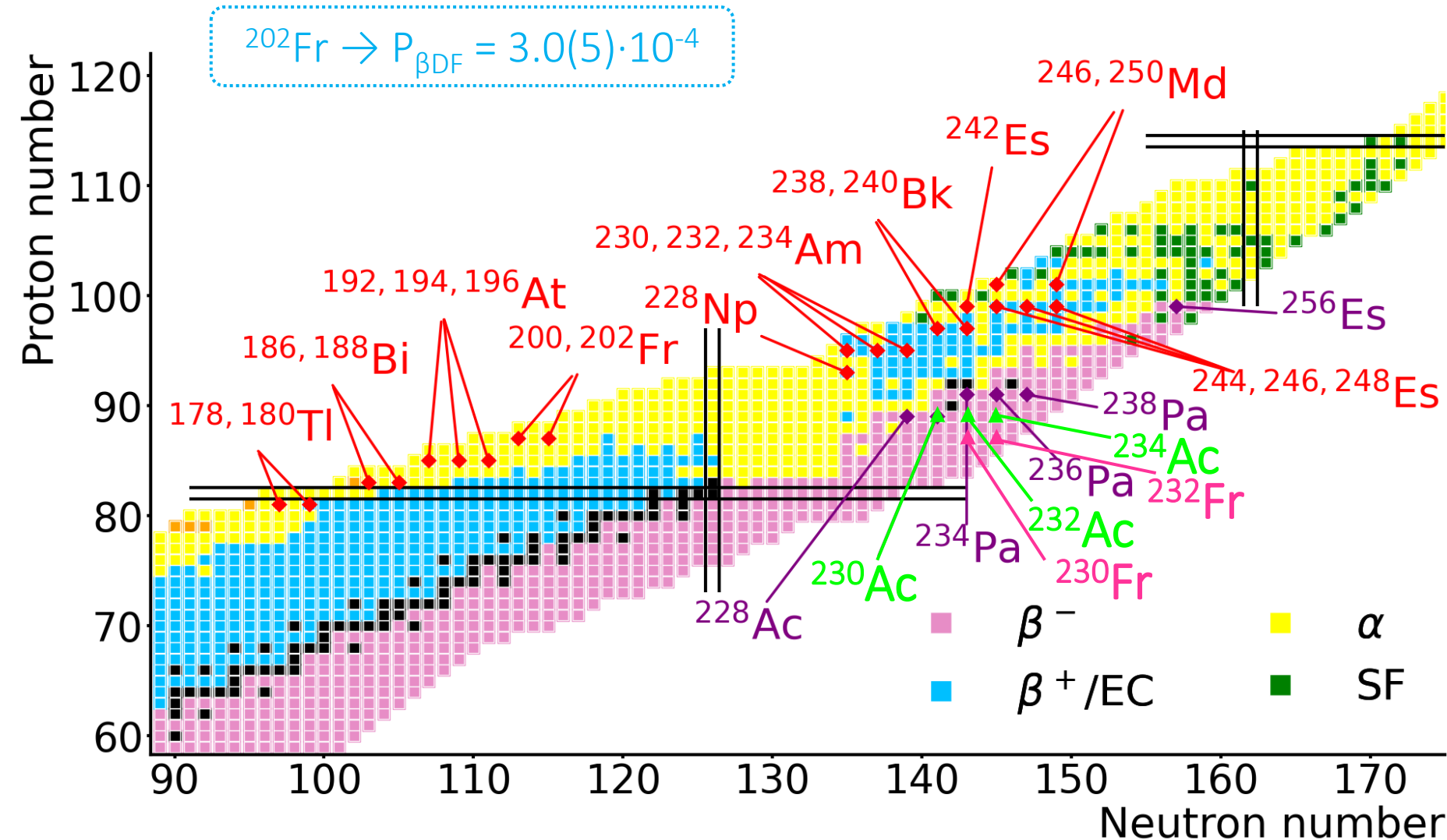


# Motivations

- r-process  $\rightarrow$   $P_{\beta\text{DF}}$  and fission fragments mass distribution



# Previous studies



- Belov et al. and Gangrsky et al. (1976, 1978)<sup>[1,2]</sup>
  - $^{236}\text{Pa} \rightarrow P_{\beta\text{DF}} \sim 10^{-9} - 10^{-10}$
  - $^{238}\text{Pa} \rightarrow P_{\beta\text{DF}} \sim 10^{-7} - 10^{-8}$
- Baas-May et al. (1985)<sup>[3]</sup>
  - $^{238}\text{Pa} \rightarrow P_{\beta\text{DF}} < 10^{-8}$
- Shuanggui et al. (2001)<sup>[4]</sup>
  - $^{230}\text{Ac} \rightarrow P_{\beta\text{DF}} \sim 10^{-8}$
- Yanbing et al. (2006)<sup>[5]</sup>
  - $^{228}\text{Ac} \rightarrow P_{\beta\text{DF}} \sim 10^{-12}$

[1] G. Belov *et al.*, Report JINR P15-9795 (1976).

[2] Y. P. Gangrsky *et al.*, *Yad. Fiz.* 27, 894 (1978); *Sov. J. Nucl. Phys.* 27, 475 (1978).

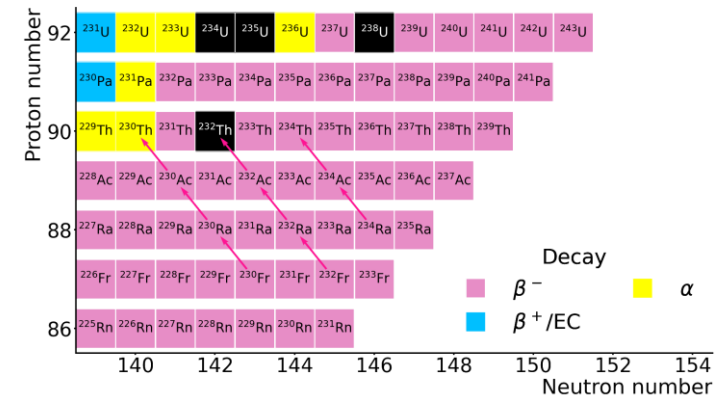
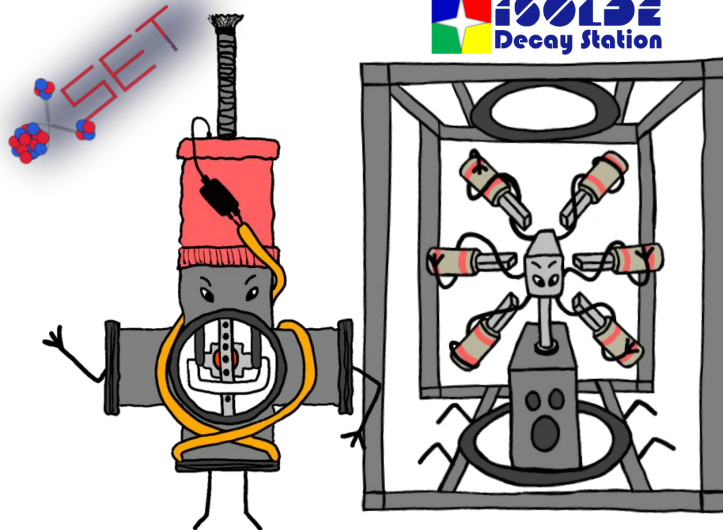
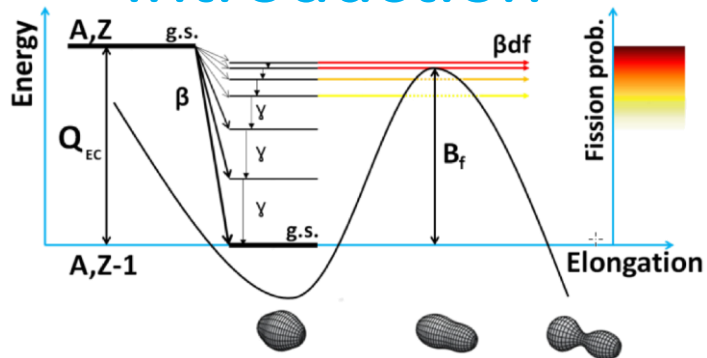
[3] A. Baas-May *et al.*, *Z. Phys. A* 322, 457-462 (1985).

[4] Y. Shuanggui *et al.*, *Eur. Phys. J. A* 10, 1-3 (2001).

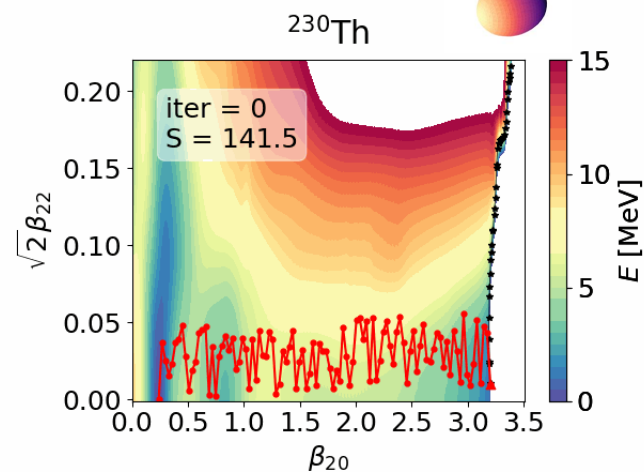
[5] X. Yanbing *et al.*, *Phys. Rev. C* 74, 047303 (2006).

# Beta-delayed fission of neutron-rich actinides

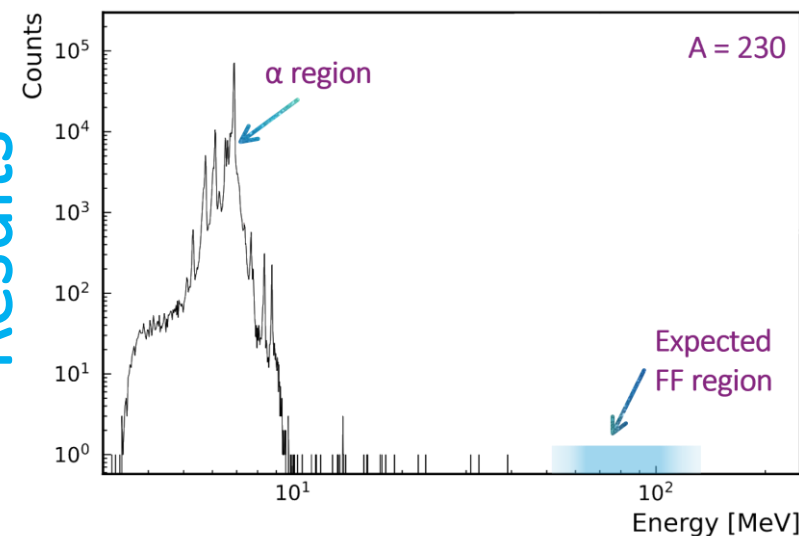
## Introduction

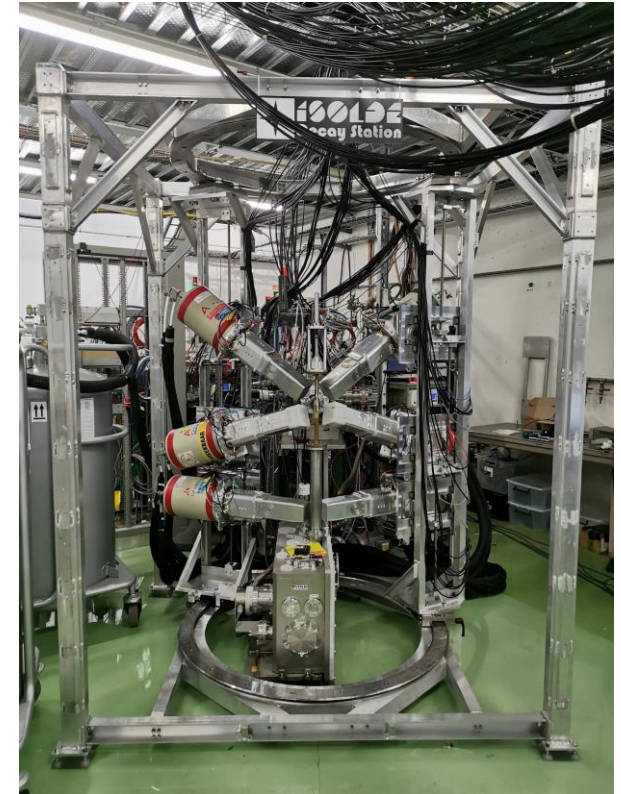
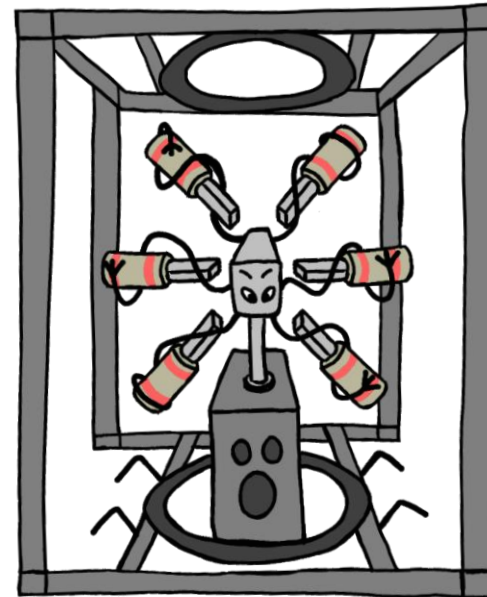
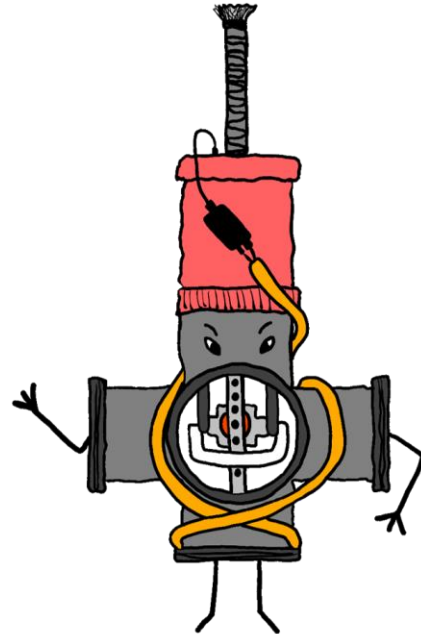
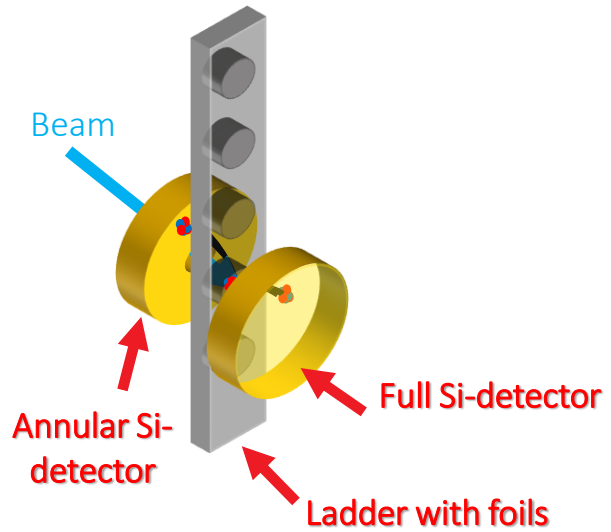
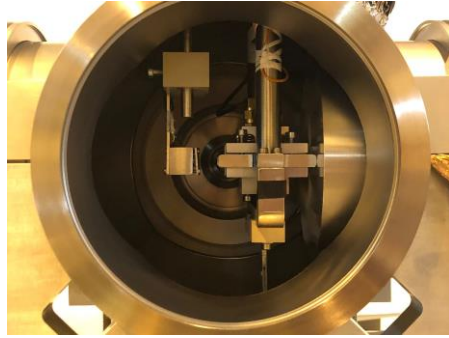
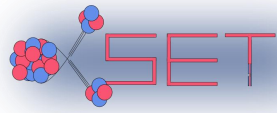


## βDF with

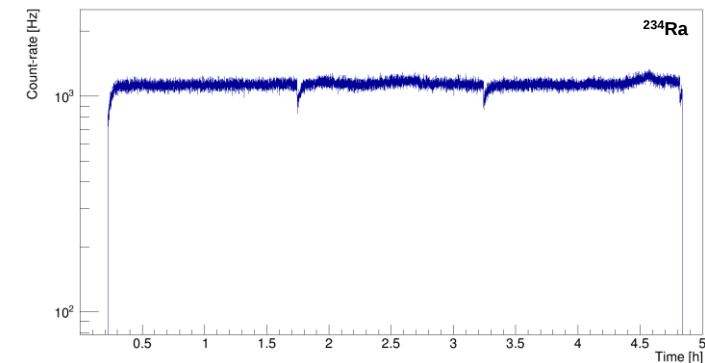
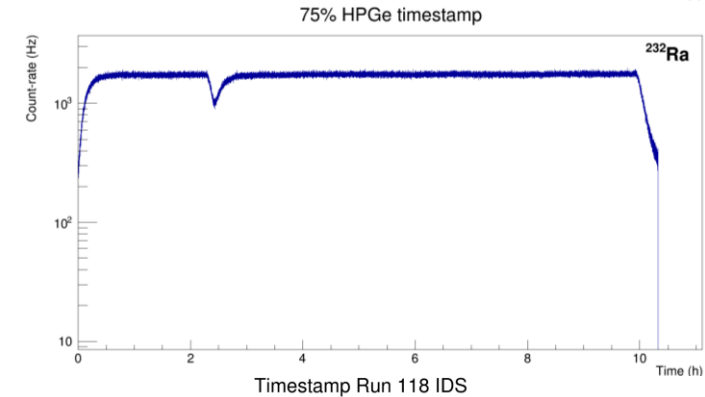
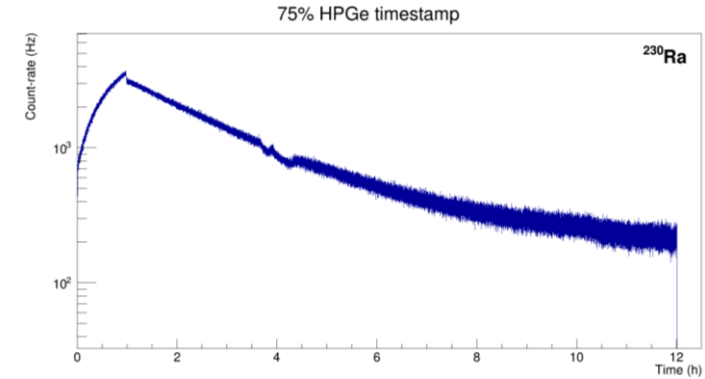
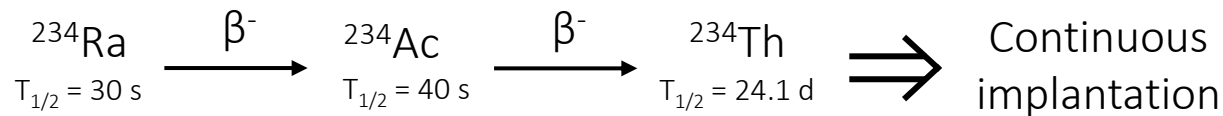
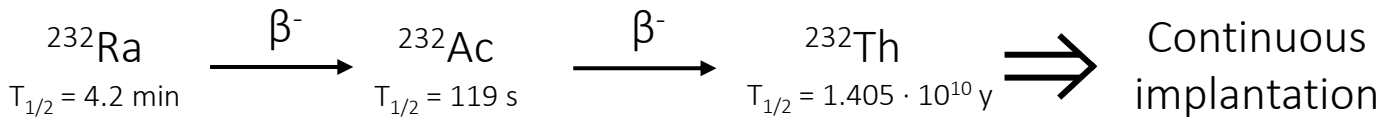
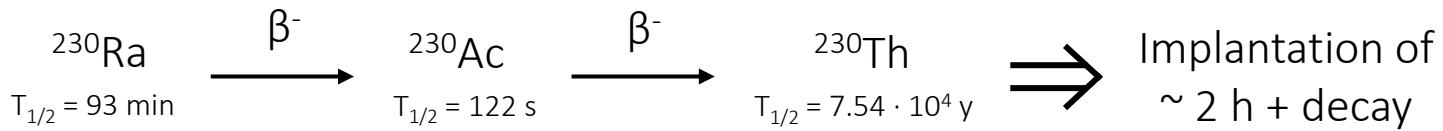
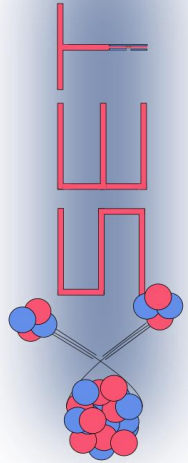
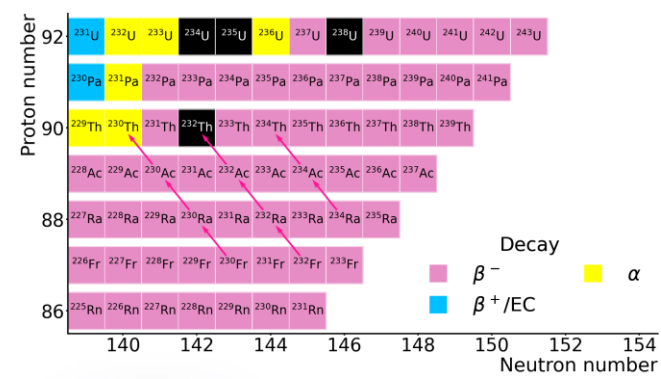


## Results

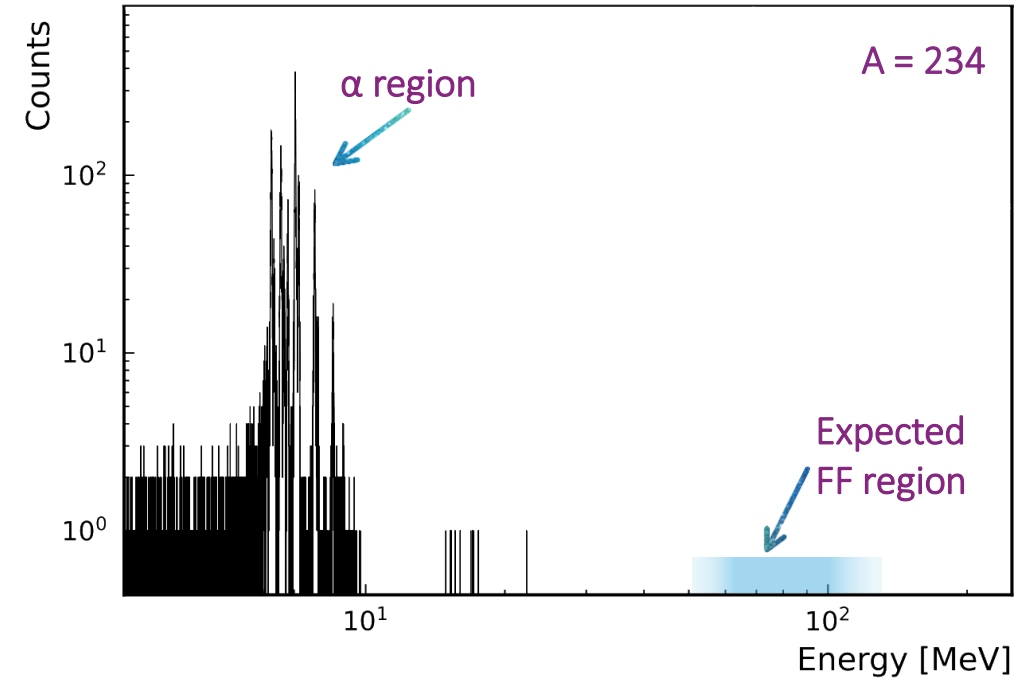
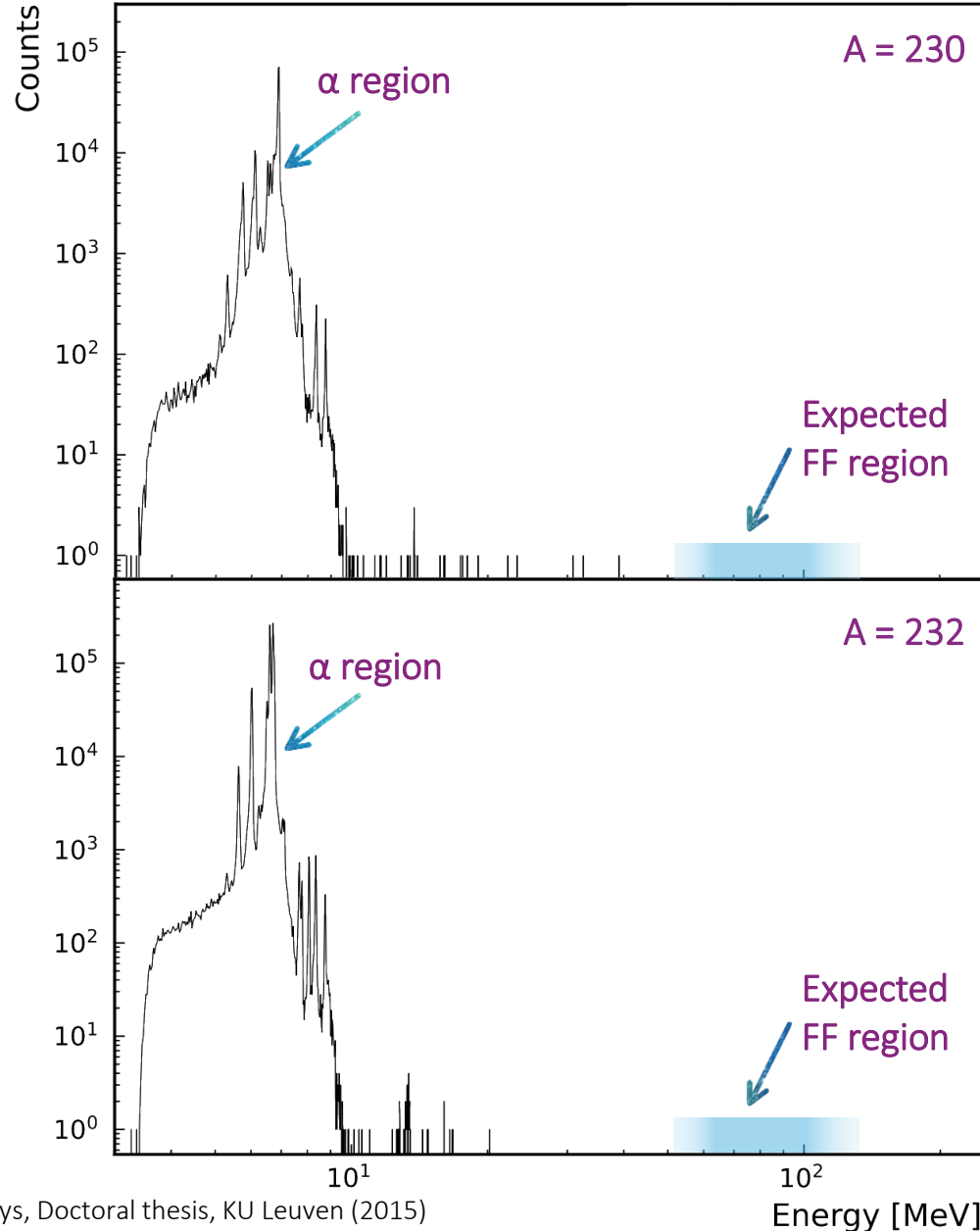




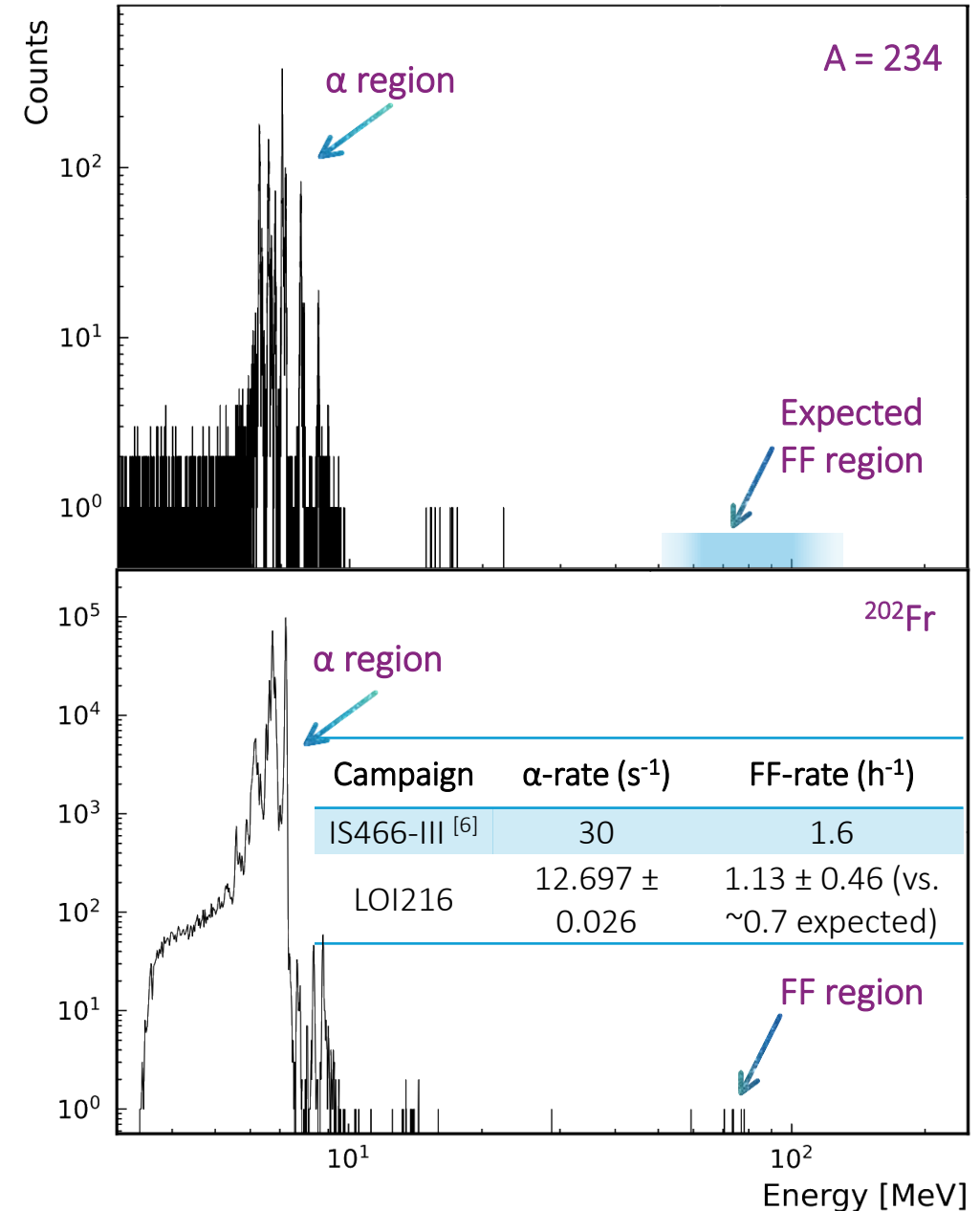
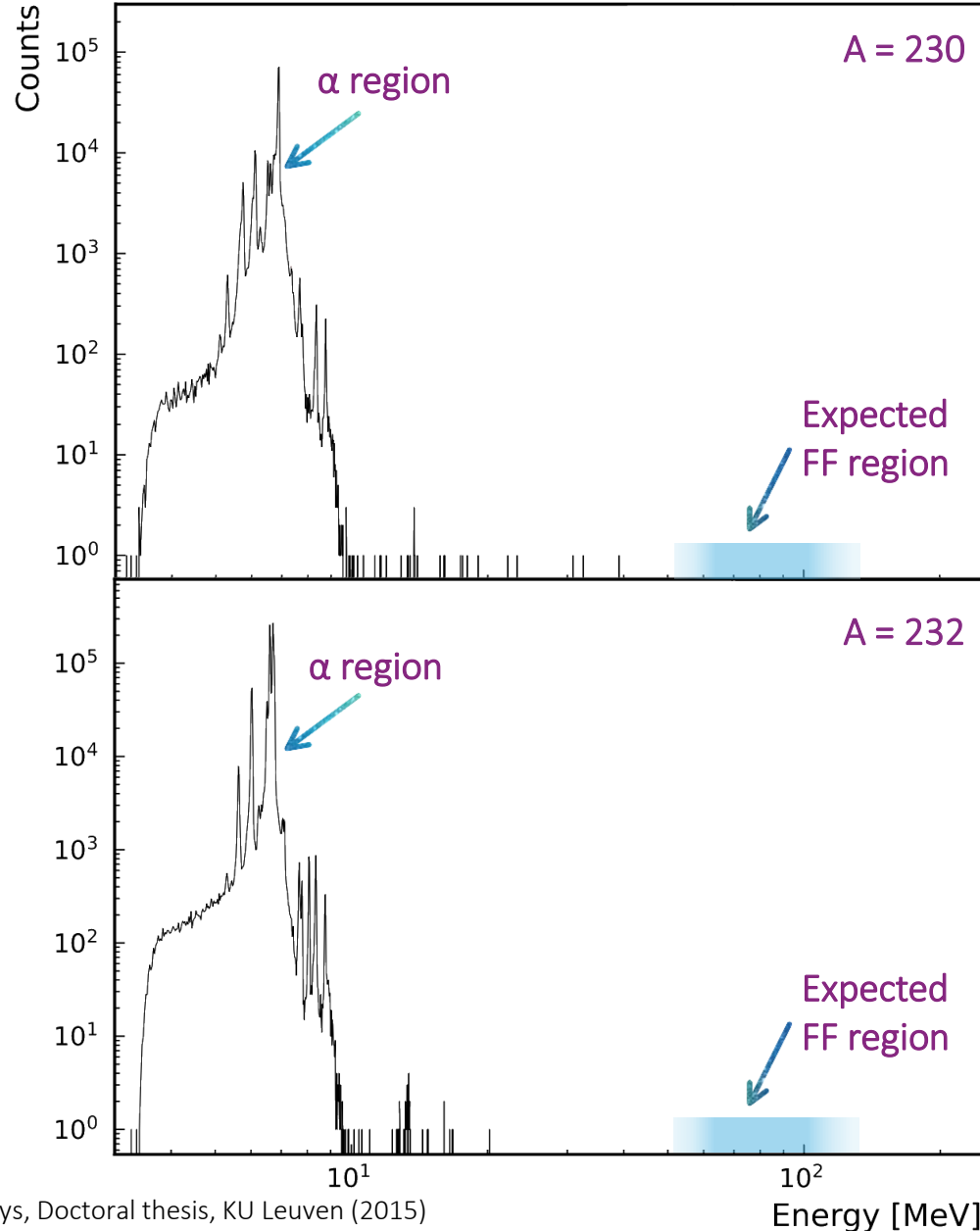
# LOI216: $\beta$ DF of $^{230,232,234}\text{Ac}$

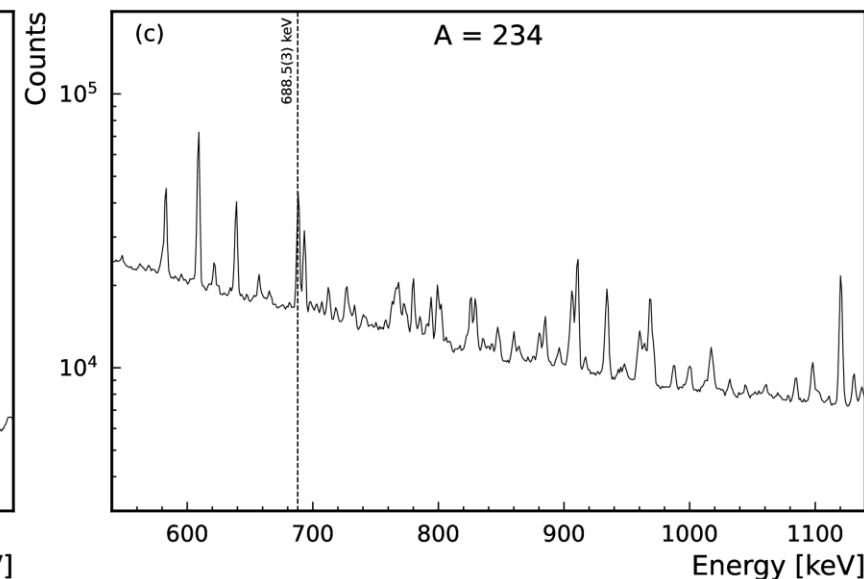
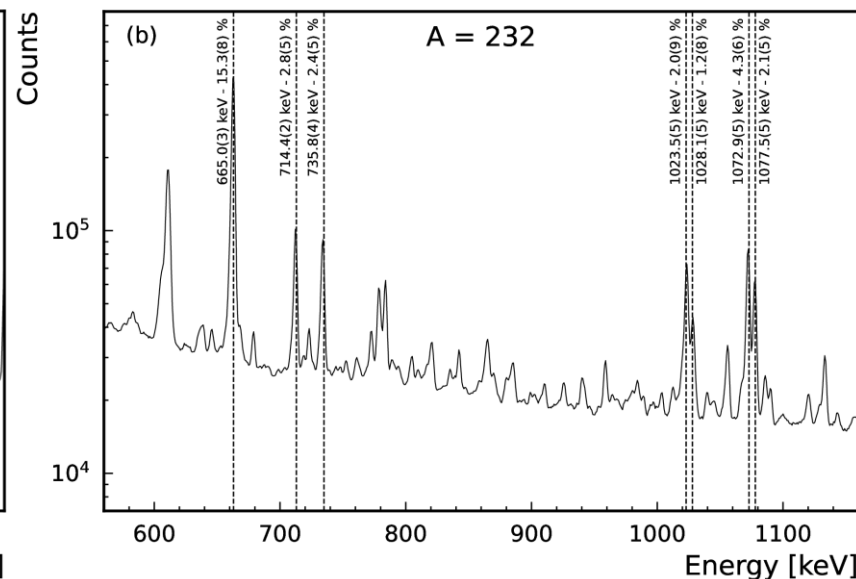
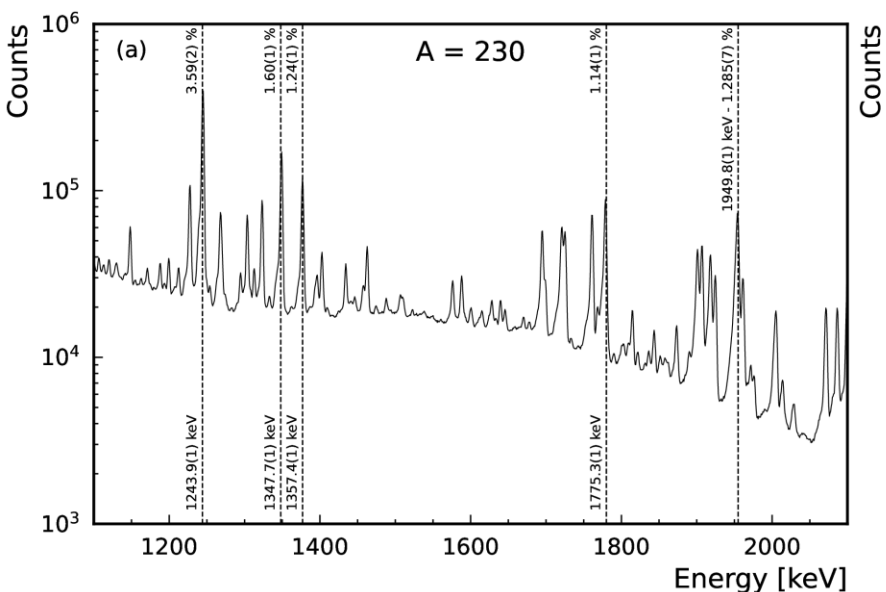


# LOI216: $\beta$ DF of $^{230,232,234}\text{Ac}$



# LOI216: $\beta$ DF of $^{230,232,234}\text{Ac}$





$$P_{\beta\text{DF}} = \frac{1.84^*}{\frac{N_{\gamma}}{I_{\gamma} \cdot \epsilon_{\gamma}} \cdot \epsilon_{\text{FF}}}$$

$$T_{1/2p, \beta\text{DF}} = \frac{T_{1/2}}{P_{\beta\text{DF}}}$$

\* 1.84 is the upper limit of Poisson's distribution of 0 observed events with a confidence level of 84% [8]

| Isotope           | $N_{\beta}$             | $P_{\beta\text{DF}}$         |                        | $T_{1/2p, \beta\text{DF}}$ |
|-------------------|-------------------------|------------------------------|------------------------|----------------------------|
|                   |                         | Lit.                         | This work [**]         |                            |
| $^{230}\text{Fr}$ | $1.4(1) \cdot 10^8$     | $< 3 \cdot 10^{-6}$ [7]      | $< 3.3 \cdot 10^{-8}$  | $> 5.8 \cdot 10^8$         |
| $^{232}\text{Fr}$ | $4.3(10) \cdot 10^7$    | $< 2 \cdot 10^{-6}$ [7]      | $< 1.3 \cdot 10^{-7}$  | $> 4.2 \cdot 10^7$         |
| $^{230}\text{Ac}$ | $1.02(4) \cdot 10^{10}$ | $1.19(40) \cdot 10^{-8}$ [4] | $< 4.3 \cdot 10^{-10}$ | $> 2.8 \cdot 10^{11}$      |
| $^{232}\text{Ac}$ | $1.50(8) \cdot 10^9$    | $< 10^{-6}$ [7]              | $< 2.7 \cdot 10^{-9}$  | $> 4.4 \cdot 10^{10}$      |
| $^{234}\text{Ac}$ | $8.4(29) \cdot 10^6$    | /                            | $< 4.9 \cdot 10^{-6}$  | $> 9.0 \cdot 10^6$         |

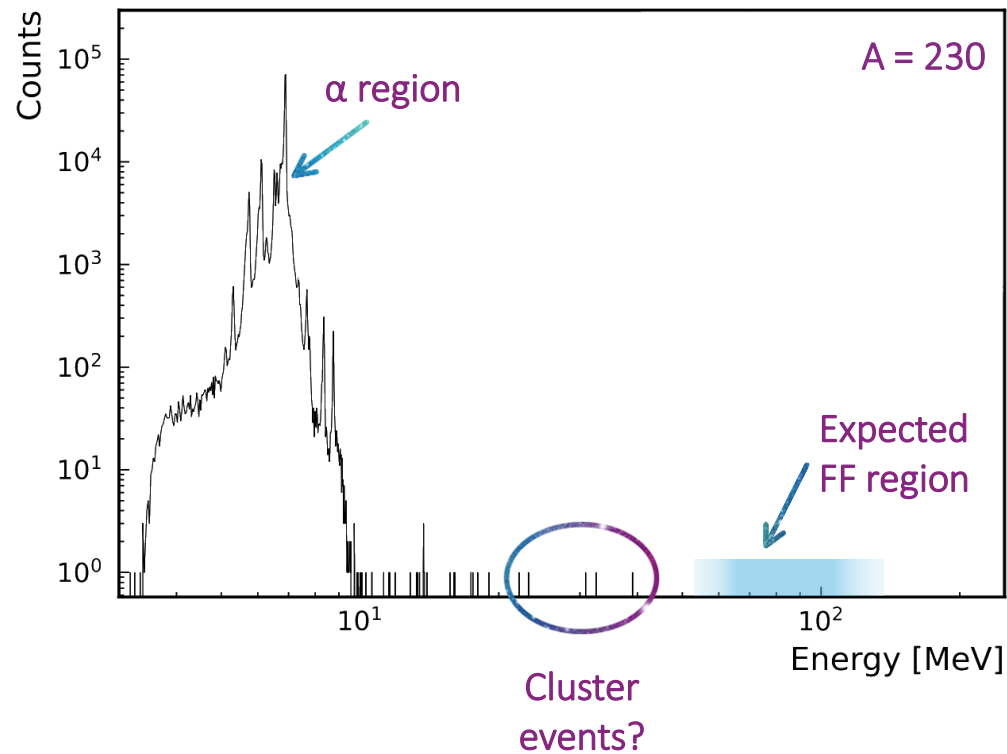
[4] Y. Shuanggui *et al.*, Eur. Phys. J. A 10, 1-3 (2001).

[7] K. A. Mezilev *et al.*, Zeitschrift für Physik A Atomic Nuclei 337, 109 (1990).

[8] K.-H. Schmidt *et al.*, Z. Phys. A – Atoms and Nuclei 316, 19-26 (1984).

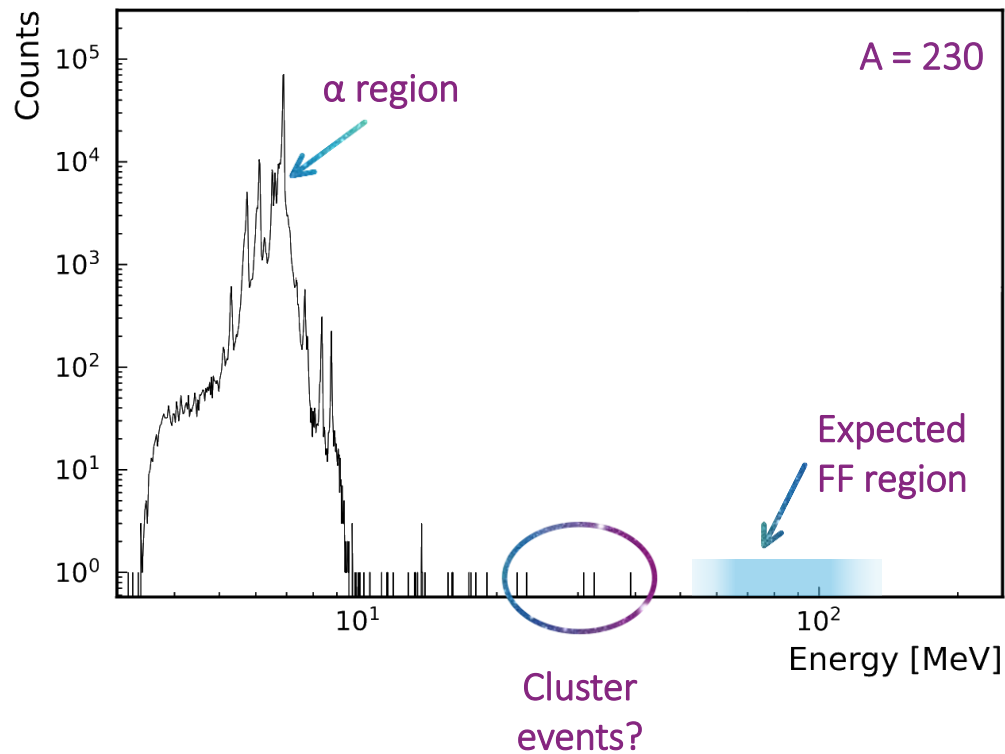
[\*\*] S. Bara *et al.*, Phys. Rev. C, submitted (2025)

# LOI216: $\beta$ DF of $^{230,232,234}\text{Ac}$



|                                                                                                                 |                                                                                                         |                                                                                                                                   |                                                                                                                              |                                                                                                                              |                                                                                                                                          |
|-----------------------------------------------------------------------------------------------------------------|---------------------------------------------------------------------------------------------------------|-----------------------------------------------------------------------------------------------------------------------------------|------------------------------------------------------------------------------------------------------------------------------|------------------------------------------------------------------------------------------------------------------------------|------------------------------------------------------------------------------------------------------------------------------------------|
| $^{230}\text{U}$<br>20.8 d<br>$\alpha = 100.00\%$<br>SF < $1\text{E-}10\%$<br>$^{24}\text{Ne} = 5\text{E-}12\%$ | $^{231}\text{U}$<br>4.2 d<br>$\epsilon = 100.00\%$<br>$\alpha \approx 4.0\text{E-}3\%$                  | $^{232}\text{U}$<br>68.9 y<br>$\alpha = 100.00\%$<br>$^{24}\text{Ne} = 9\text{E-}10\%$<br>SF = $3\text{E-}12\%$                   | $^{233}\text{U}$<br>$1.592\text{E+}5$ y<br>$\alpha = 100.00\%$<br>$^{24}\text{Ne} = 9\text{E-}10\%$<br>SF < $6\text{E-}11\%$ | $^{234}\text{U}$<br>$2.455\text{E+}5$ y<br>0.0054%<br>$\alpha = 100.00\%$<br>SF = $1.6\text{E-}9\%$<br>Mg = $1\text{E-}11\%$ | $^{235}\text{U}$<br>$7.04\text{E+}8$ y<br>0.7204%<br>$\alpha = 100.00\%$<br>SF = $7.0\text{E-}9\%$<br>$^{28}\text{Mg} = 8.\text{E-}10\%$ |
| $^{229}\text{Pa}$<br>1.50 d<br>$\epsilon = 99.52\%$<br>$\alpha = 0.48\%$                                        | $^{230}\text{Pa}$<br>17.4 d<br>$\epsilon = 92.20\%$<br>$\beta^- = 7.80\%$<br>$\alpha = 3.2\text{E-}3\%$ | $^{231}\text{Pa}$<br>$3.276\text{E+}4$ y<br>$\alpha = 100.00\%$<br>SF < $3\text{E-}10\%$                                          | $^{232}\text{Pa}$<br>1.32 d<br>$\beta^- = 100.00\%$<br>$\epsilon$                                                            | $^{233}\text{Pa}$<br>26.975 d<br>$\beta^- = 100.00\%$                                                                        | $^{234}\text{Pa}$<br>6.70 h<br>$\beta^- = 100.00\%$                                                                                      |
| $^{228}\text{Th}$<br>1.9125 y<br>$\alpha = 100.00\%$<br>$^{20}\text{O} = 1\text{E-}11$ 0%                       | $^{229}\text{Th}$<br>7932 y<br>$\alpha = 100.00\%$                                                      | $^{230}\text{Th}$<br>$7.54\text{E+}4$ y<br>$\alpha = 100.00\%$<br>$^{24}\text{Ne} = 6\text{E-}11$ 0%<br>SF $\leq 4\text{E-}12$ 0% | $^{231}\text{Th}$<br>25.52 h<br>$\beta^- = 100.00\%$<br>$\alpha \approx 4\text{E-}11\%$                                      | $^{232}\text{Th}$<br>$1.40\text{E+}10$ y<br>100%<br>$\alpha = 100.00\%$<br>SF = $1.1\text{E-}9\%$                            | $^{233}\text{Th}$<br>21.83 min<br>$\beta^- = 100.00\%$                                                                                   |
| $^{227}\text{Ac}$<br>21.772 y<br>$\beta^- = 98.62\%$<br>$\alpha = 1.38\%$                                       | $^{228}\text{Ac}$<br>6.15 h<br>$\beta^- = 100.00\%$                                                     | $^{229}\text{Ac}$<br>62.7 min<br>$\beta^- = 100.00\%$                                                                             | $^{230}\text{Ac}$<br>122 s<br>$\beta^- = 100.00\%$<br>BF = $1.2\text{E-}6\%$                                                 | $^{231}\text{Ac}$<br>7.5 min<br>$\beta^- = 100.00\%$                                                                         | $^{232}\text{Ac}$<br>119 s<br>$\beta^- = 100.00\%$                                                                                       |
| $^{226}\text{Ra}$<br>1600 y<br>$\alpha = 100.00\%$<br>$^{14}\text{C} = 3.2\text{E-}9\%$                         | $^{227}\text{Ra}$<br>42.2 min<br>$\beta^- = 100.00\%$                                                   | $^{228}\text{Ra}$<br>5.75 y<br>$\beta^- = 100.00\%$                                                                               | $^{229}\text{Ra}$<br>4.0 min<br>$\beta^-$                                                                                    | $^{230}\text{Ra}$<br>93 min<br>$\beta^- = 100.00\%$                                                                          | $^{231}\text{Ra}$<br>104 s<br>$\beta^- = 100.00\%$                                                                                       |
| $^{225}\text{Fr}$<br>3.95 min<br>$\beta^- = 100.00\%$                                                           | $^{226}\text{Fr}$<br>49 s<br>$\beta^- = 100.00\%$                                                       | $^{227}\text{Fr}$<br>2.47 min<br>$\beta^- = 100.00\%$                                                                             | $^{228}\text{Fr}$<br>38 s<br>$\beta^- < 100.00\%$                                                                            | $^{229}\text{Fr}$<br>50.2 s<br>$\beta^- = 100.00\%$                                                                          | $^{230}\text{Fr}$<br>19.1 s<br>$\beta^- = 100.00\%$                                                                                      |

# LOI216: $\beta$ DF of $^{230,232,234}\text{Ac}$



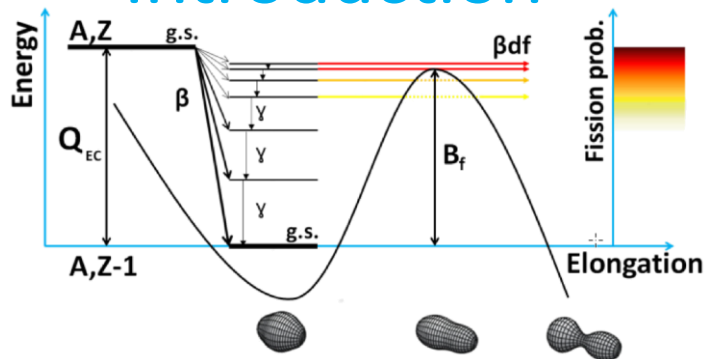
|                                                                                                                        |                                                                                                         |                                                                                                                                          |                                                                                                                                     |                                                                                                                                            |                                                                                                                                                |
|------------------------------------------------------------------------------------------------------------------------|---------------------------------------------------------------------------------------------------------|------------------------------------------------------------------------------------------------------------------------------------------|-------------------------------------------------------------------------------------------------------------------------------------|--------------------------------------------------------------------------------------------------------------------------------------------|------------------------------------------------------------------------------------------------------------------------------------------------|
| $^{230}\text{U}$<br>20.8 d<br>$\alpha = 100.00\%$<br>$\text{SF} < 1\text{E-}10\%$<br>$^{24}\text{Ne} = 5\text{E-}12\%$ | $^{231}\text{U}$<br>4.2 d<br>$\epsilon = 100.00\%$<br>$\alpha \approx 4.0\text{E-}3\%$                  | $^{232}\text{U}$<br>68.9 y<br>$\alpha = 100.00\%$<br>$^{24}\text{Ne} = 9\text{E-}10\%$<br>$\text{SF} = 3\text{E-}12\%$                   | $^{233}\text{U}$<br>$1.592\text{E}+5$ y<br>$\alpha = 100.00\%$<br>$^{24}\text{Ne} = 9\text{E-}10\%$<br>$\text{SF} < 6\text{E-}11\%$ | $^{234}\text{U}$<br>$2.455\text{E}+5$ y<br>0.0054%<br>$\alpha = 100.00\%$<br>$\text{SF} = 1.6\text{E-}9\%$<br>$\text{Mg} = 1\text{E-}11\%$ | $^{235}\text{U}$<br>$7.04\text{E}+8$ y<br>0.7204%<br>$\alpha = 100.00\%$<br>$\text{SF} = 7.0\text{E-}9\%$<br>$^{28}\text{Mg} = 8\text{E-}10\%$ |
| $^{229}\text{Pa}$<br>1.50 d<br>$\epsilon = 99.52\%$<br>$\alpha = 0.48\%$                                               | $^{230}\text{Pa}$<br>17.4 d<br>$\epsilon = 92.20\%$<br>$\beta^- = 7.80\%$<br>$\alpha = 3.2\text{E-}3\%$ | $^{231}\text{Pa}$<br>$3.276\text{E}+4$ y<br>$\alpha = 100.00\%$<br>$\text{SF} < 3\text{E-}10\%$                                          | $^{232}\text{Pa}$<br>1.32 d<br>$\beta^- = 100.00\%$<br>$\epsilon$                                                                   | $^{233}\text{Pa}$<br>26.975 d<br>$\beta^- = 100.00\%$                                                                                      | $^{234}\text{Pa}$<br>6.70 h<br>$\beta^- = 100.00\%$                                                                                            |
| $^{228}\text{Th}$<br>1.9125 y<br>$\alpha = 100.00\%$<br>$^{230}\text{O} = 1\text{E-}11$ 0%                             | $^{229}\text{Th}$<br>7932 y<br>$\alpha = 100.00\%$                                                      | $^{230}\text{Th}$<br>$7.54\text{E}+4$ y<br>$\alpha = 100.00\%$<br>$^{24}\text{Ne} = 6\text{E-}11$ 0%<br>$\text{SF} \leq 4\text{E-}12$ 0% | $^{231}\text{Th}$<br>25.52 h<br>$\beta^- = 100.00\%$<br>$\alpha \approx 4\text{E-}11\%$                                             | $^{232}\text{Th}$<br>$1.40\text{E}+10$ y<br>100%<br>$\alpha = 100.00\%$<br>$\text{SF} = 1.1\text{E-}9\%$                                   | $^{233}\text{Th}$<br>21.83 min<br>$\beta^- = 100.00\%$                                                                                         |
| $^{227}\text{Ac}$<br>21.772 y<br>$\beta^- = 98.62\%$<br>$\alpha = 1.38\%$                                              | $^{228}\text{Ac}$<br>6.15 h<br>$\beta^- = 100.00\%$                                                     | $^{229}\text{Ac}$<br>62.7 min<br>$\beta^- = 100.00\%$                                                                                    | $^{230}\text{Ac}$<br>122 s<br>$\beta^- = 100.00\%$<br>$\text{BF} = 1.2\text{E-}6\%$                                                 | $^{231}\text{Ac}$<br>7.5 min<br>$\beta^- = 100.00\%$                                                                                       | $^{232}\text{Ac}$<br>119 s<br>$\beta^- = 100.00\%$                                                                                             |
| $^{226}\text{Ra}$<br>1600 y<br>$\alpha = 100.00\%$<br>$^{14}\text{C} = 3.2\text{E-}9\%$                                | $^{227}\text{Ra}$<br>42.2 min<br>$\beta^- = 100.00\%$                                                   | $^{228}\text{Ra}$<br>5.75 y<br>$\beta^- = 100.00\%$                                                                                      | $^{229}\text{Ra}$<br>4.0 min<br>$\beta^-$                                                                                           | $^{230}\text{Ra}$<br>93 min<br>$\beta^- = 100.00\%$                                                                                        | $^{231}\text{Ra}$<br>104 s<br>$\beta^- = 100.00\%$                                                                                             |
| $^{225}\text{Fr}$<br>3.95 min<br>$\beta^- = 100.00\%$                                                                  | $^{226}\text{Fr}$<br>49 s<br>$\beta^- = 100.00\%$                                                       | $^{227}\text{Fr}$<br>2.47 min<br>$\beta^- = 100.00\%$                                                                                    | $^{228}\text{Fr}$<br>38 s<br>$\beta^- < 100.00\%$                                                                                   | $^{229}\text{Fr}$<br>50.2 s<br>$\beta^- = 100.00\%$                                                                                        | $^{230}\text{Fr}$<br>19.1 s<br>$\beta^- = 100.00\%$                                                                                            |

- $\text{BR} \approx 4.1(4) \cdot 10^{-11}$
- Cluster:  $^{22}\text{O}$  from  $^{230}\text{Ra}$

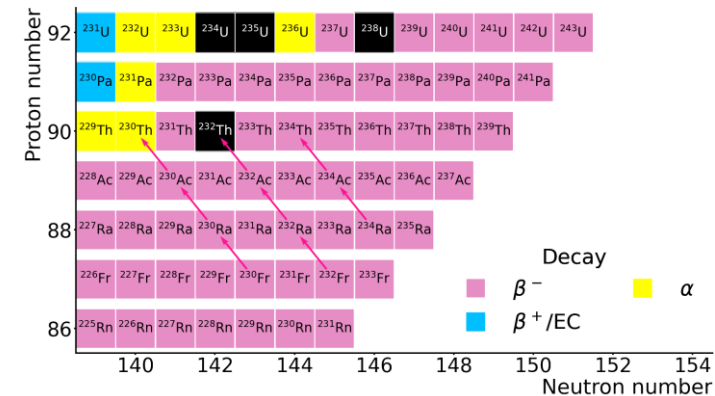
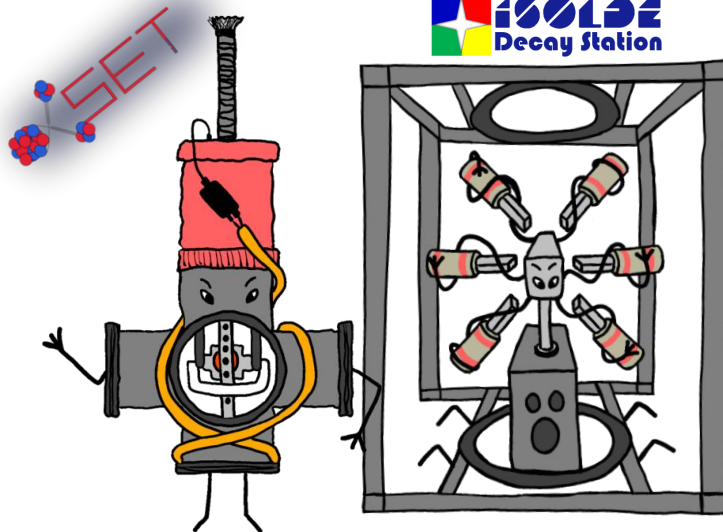
Tentative!

# Beta-delayed fission of neutron-rich actinides

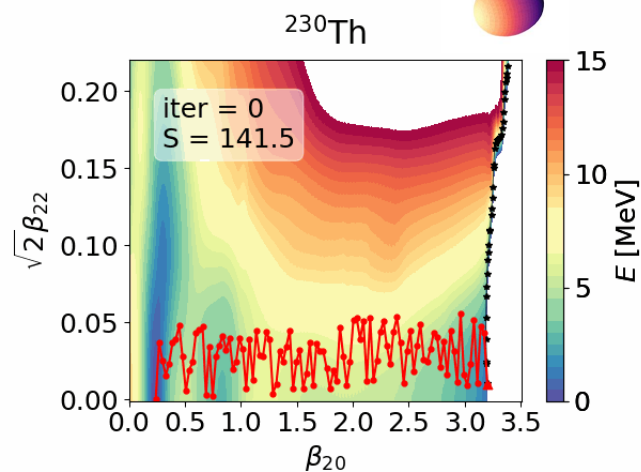
## Introduction



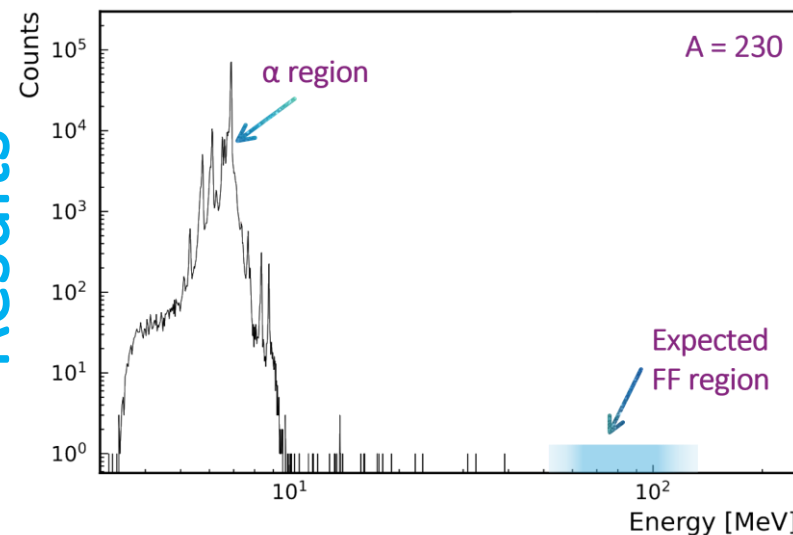
ISOLDE Decay Station



## βDF with *PyneB*

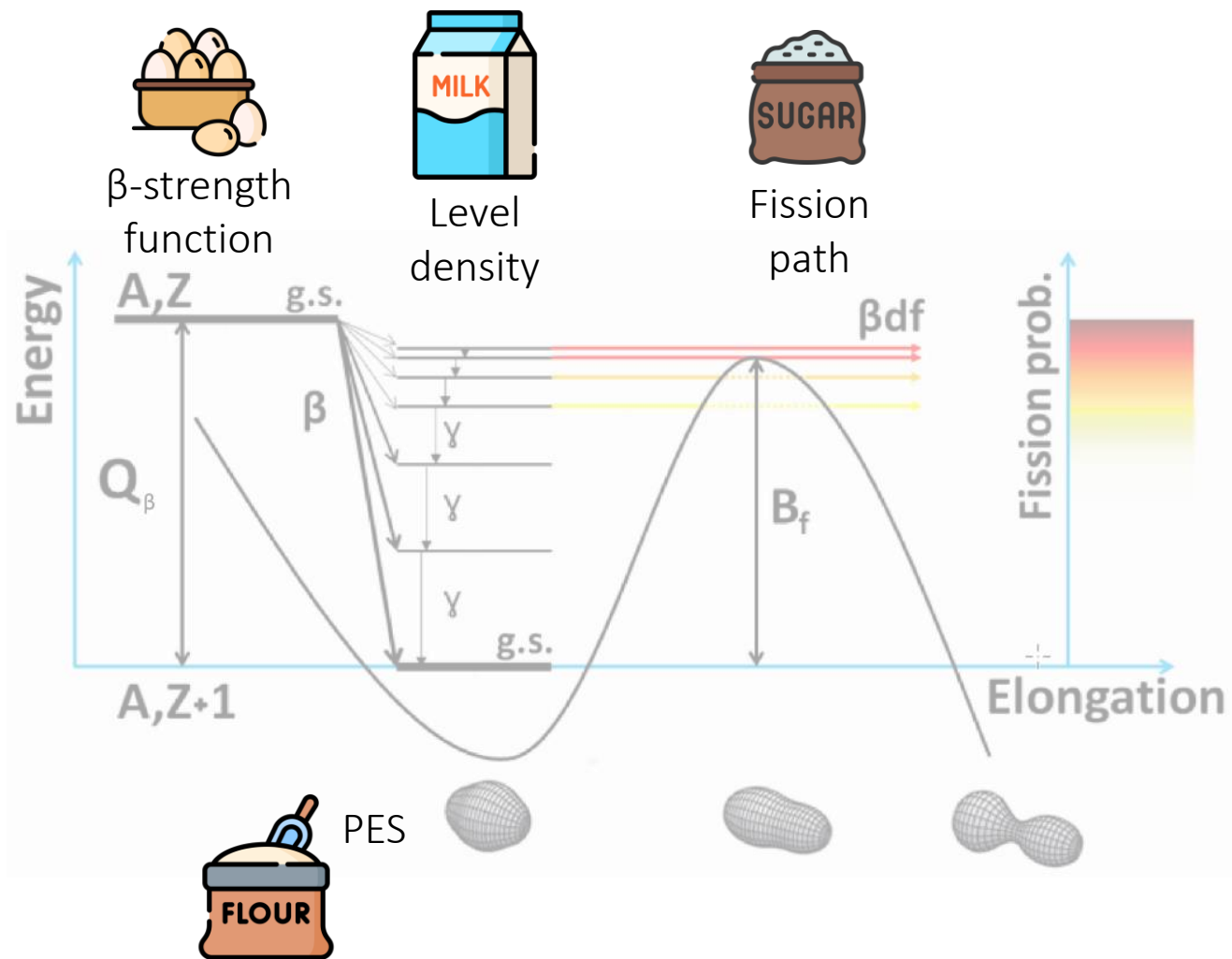


## Results





# The recipe



TALYS



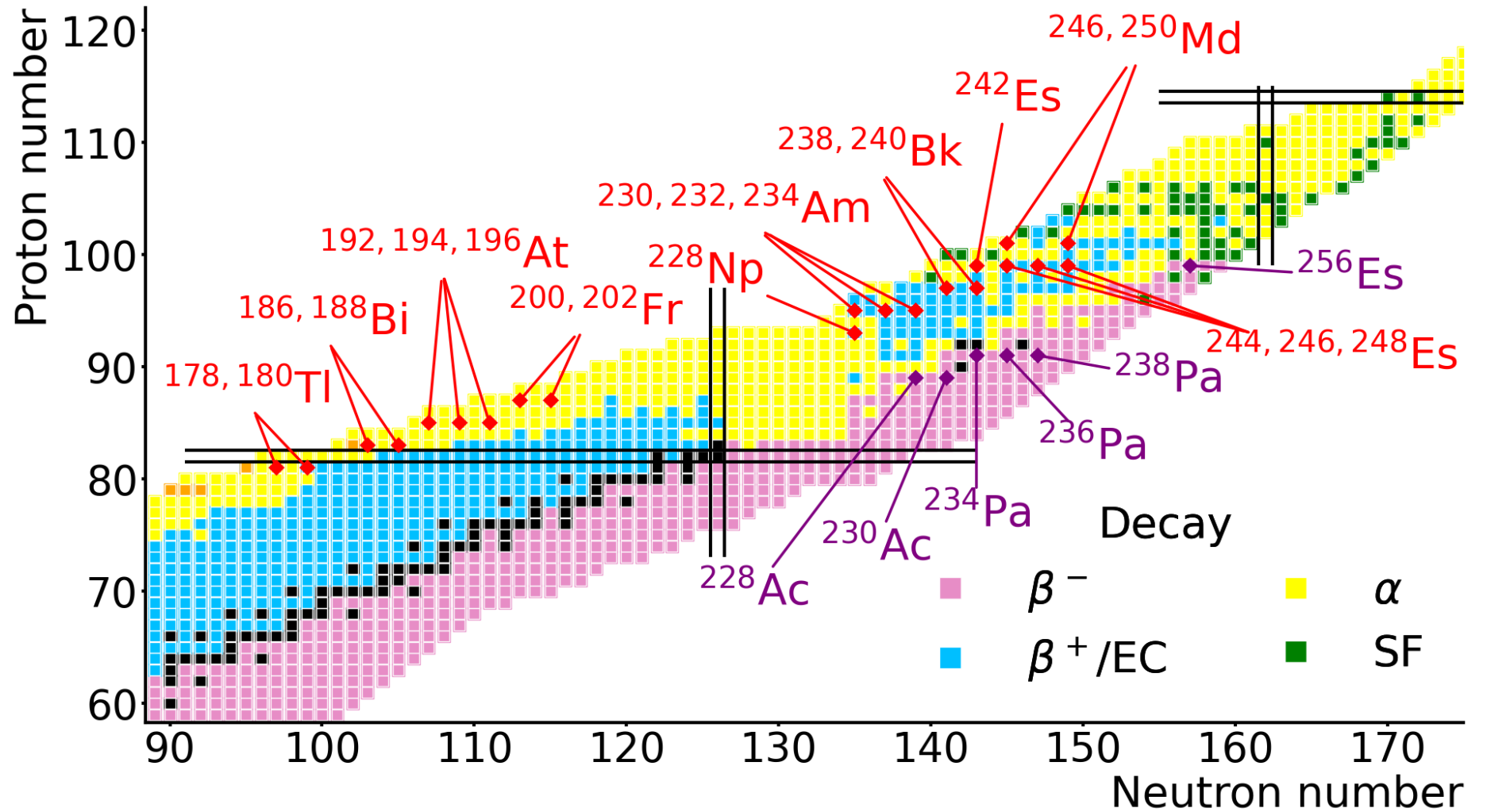
$P_{\beta DF}$



# The recipe



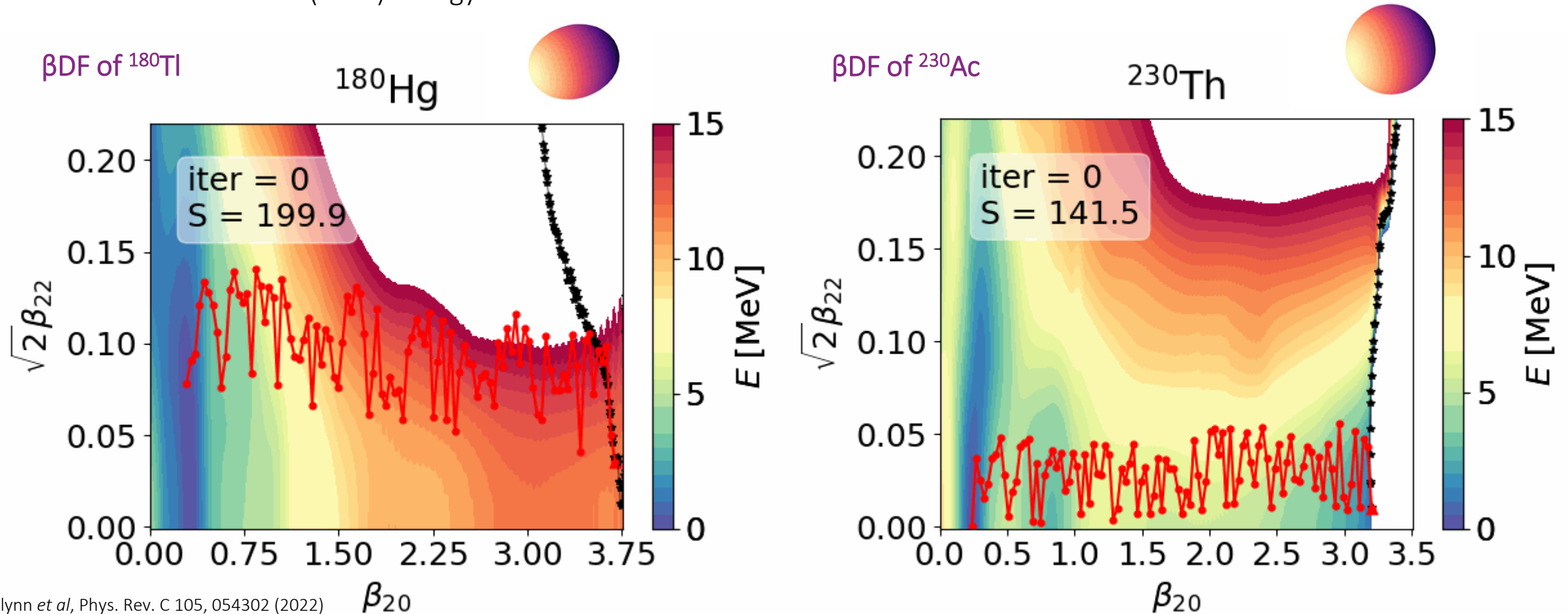
$P_{\beta\text{DF}}$



# Fission path with

Python Nudged Elastic Band, PyNEB, on PES calculated with BSkG3.

- LAP = Least Action Path
- MEP = Minimum (least) Energy Path



[9] E. Flynn *et al*, Phys. Rev. C 105, 054302 (2022)

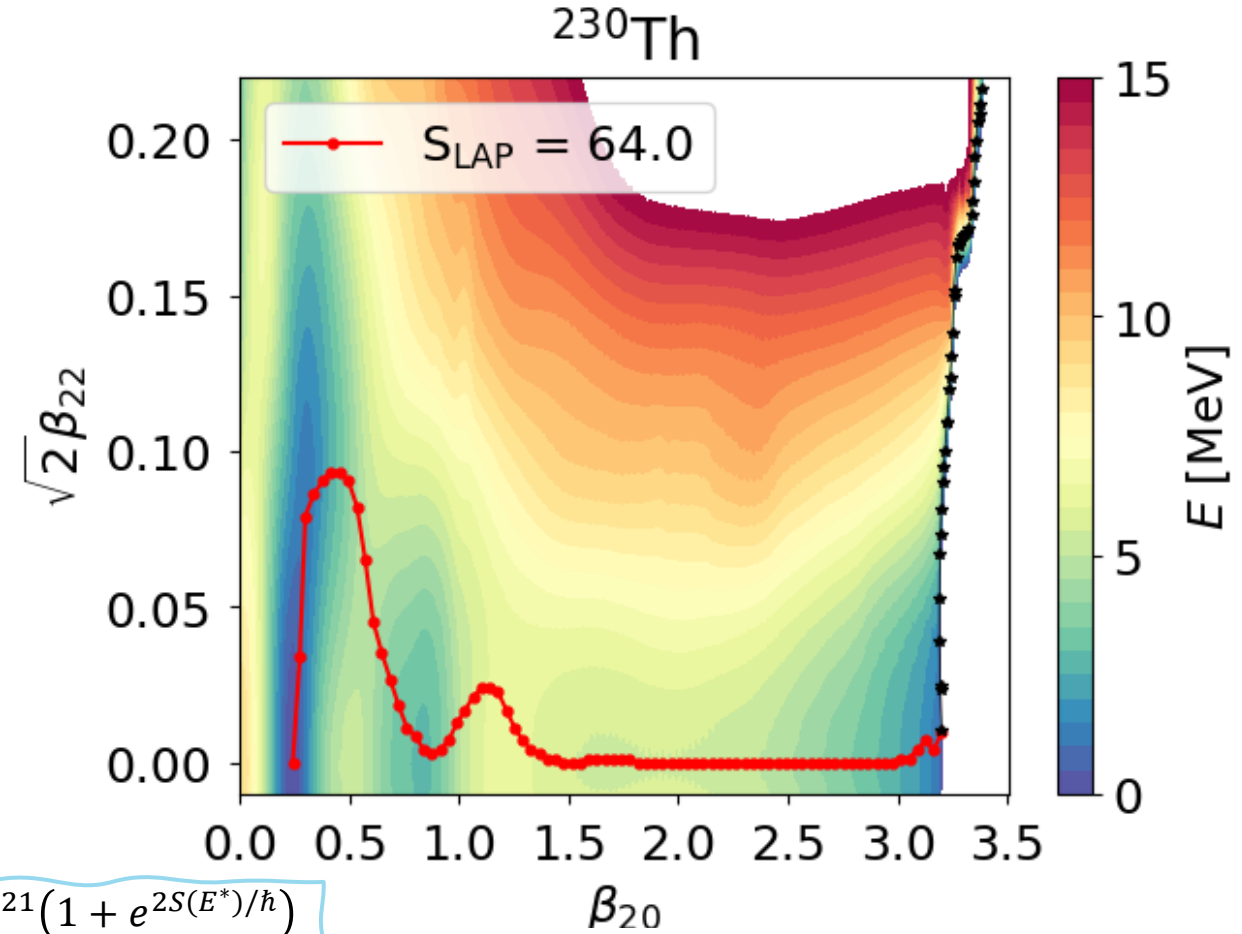
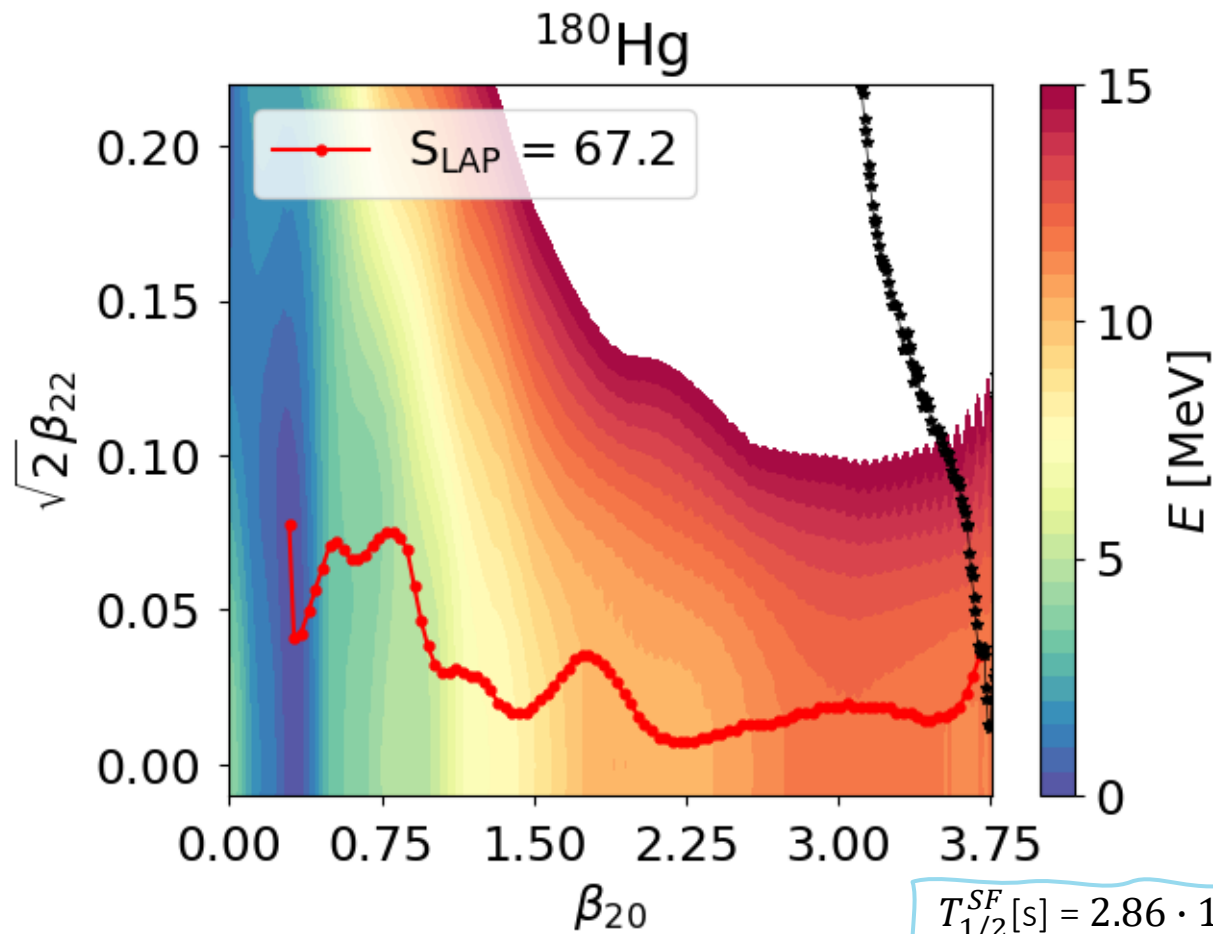
[10] G. Grams *et al*, Eur. Phys. J. A 59, 270 (2023).

Shape plots thanks to W. Ryssens.

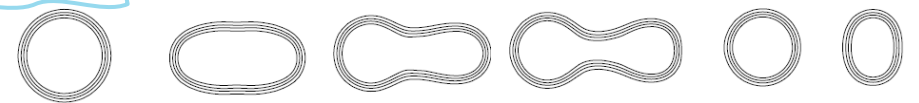
# Fission path with

$\beta$ DF of  $^{180}\text{Tl}$

$\beta$ DF of  $^{230}\text{Ac}$



$$T_{1/2}^{SF}[\text{s}] = 2.86 \cdot 10^{-21} (1 + e^{2S(E^*)/\hbar})$$



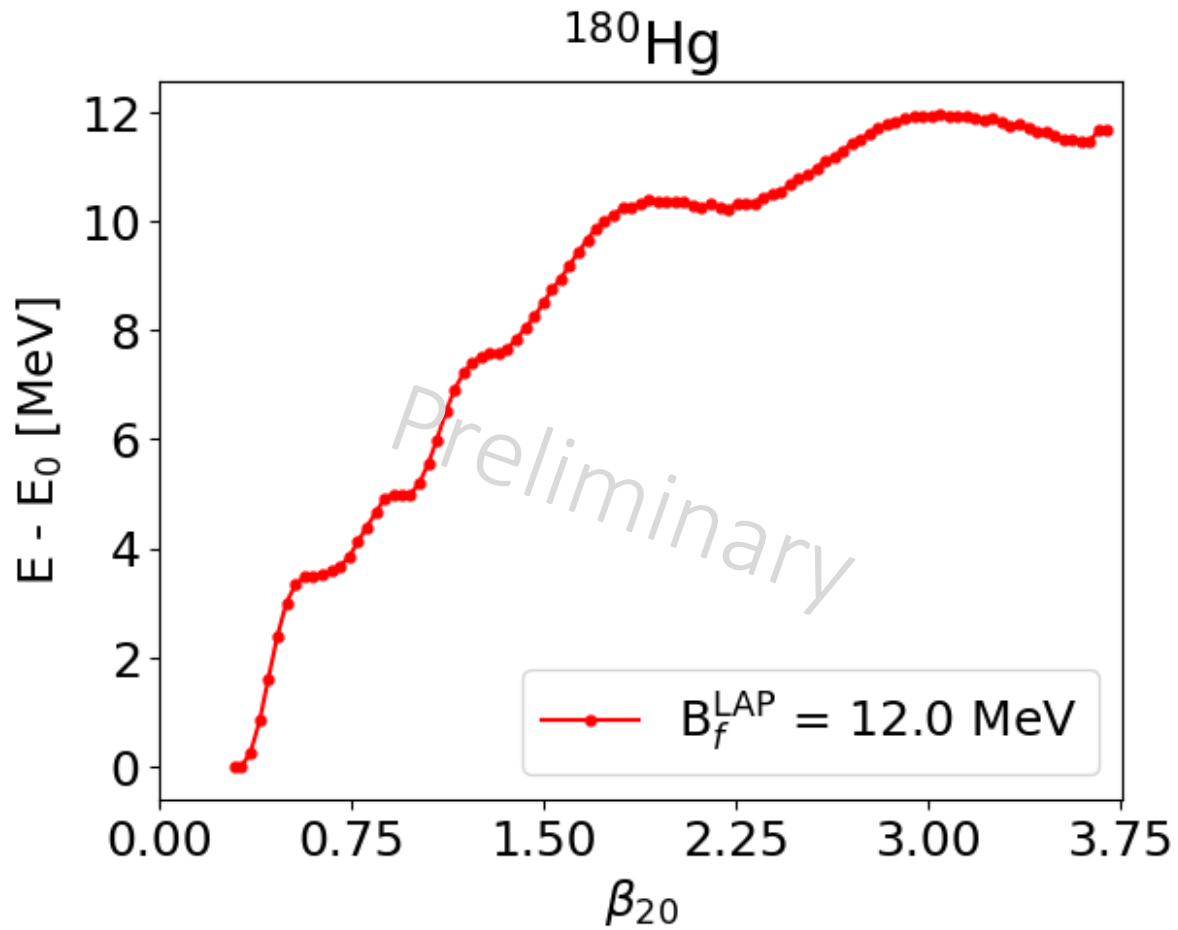
[9] E. Flynn *et al*, Phys. Rev. C 105, 054302 (2022)

[12] J. Lemaître *et al*, Phys. Rev. C 98, 024623 (2018)

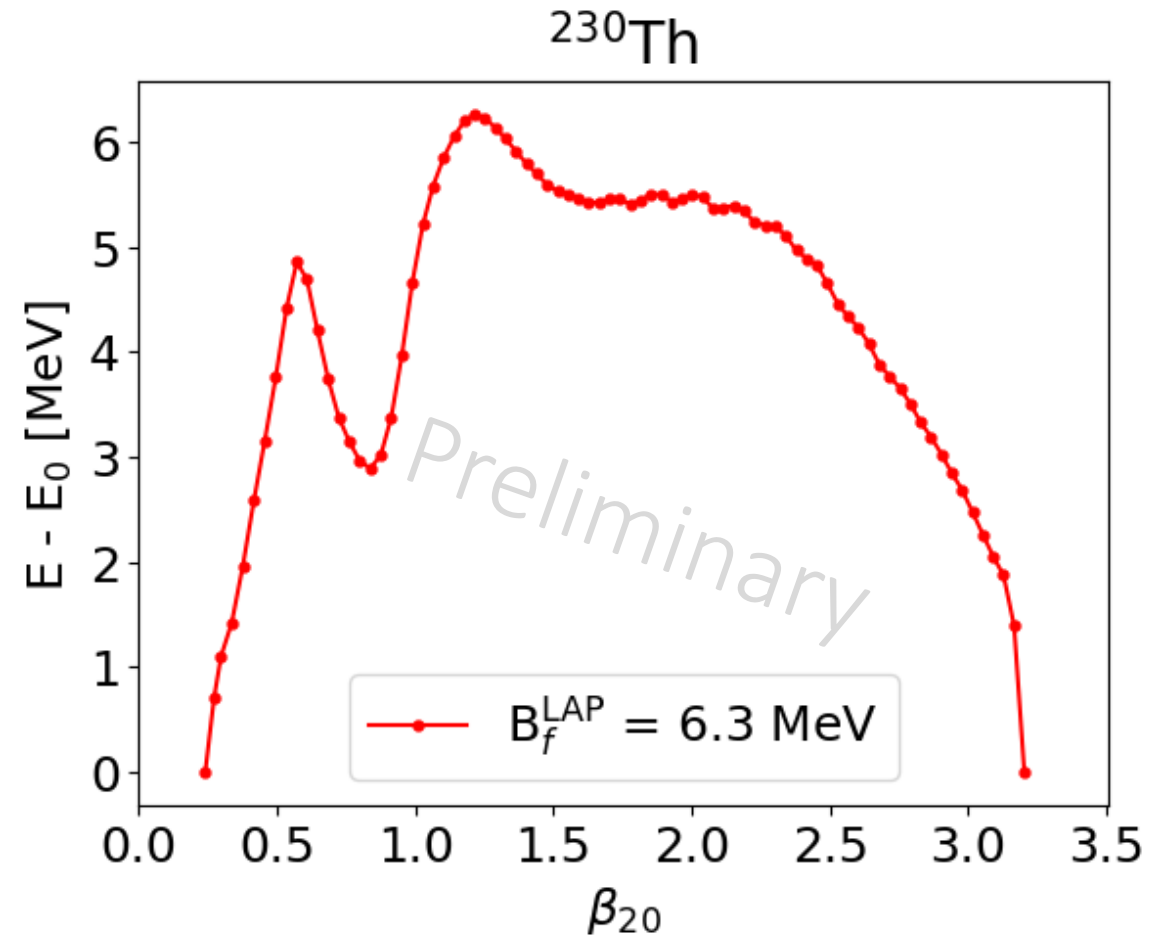
Shape plots thanks to W. Ryssens.

# Fission path with

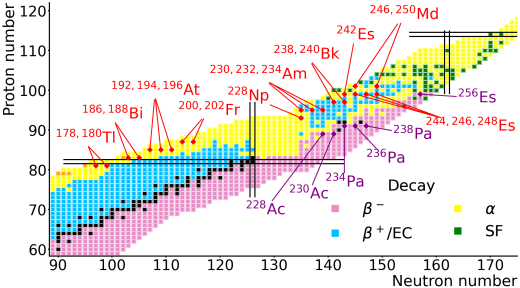
$\beta$ DF of  $^{180}\text{Tl}$



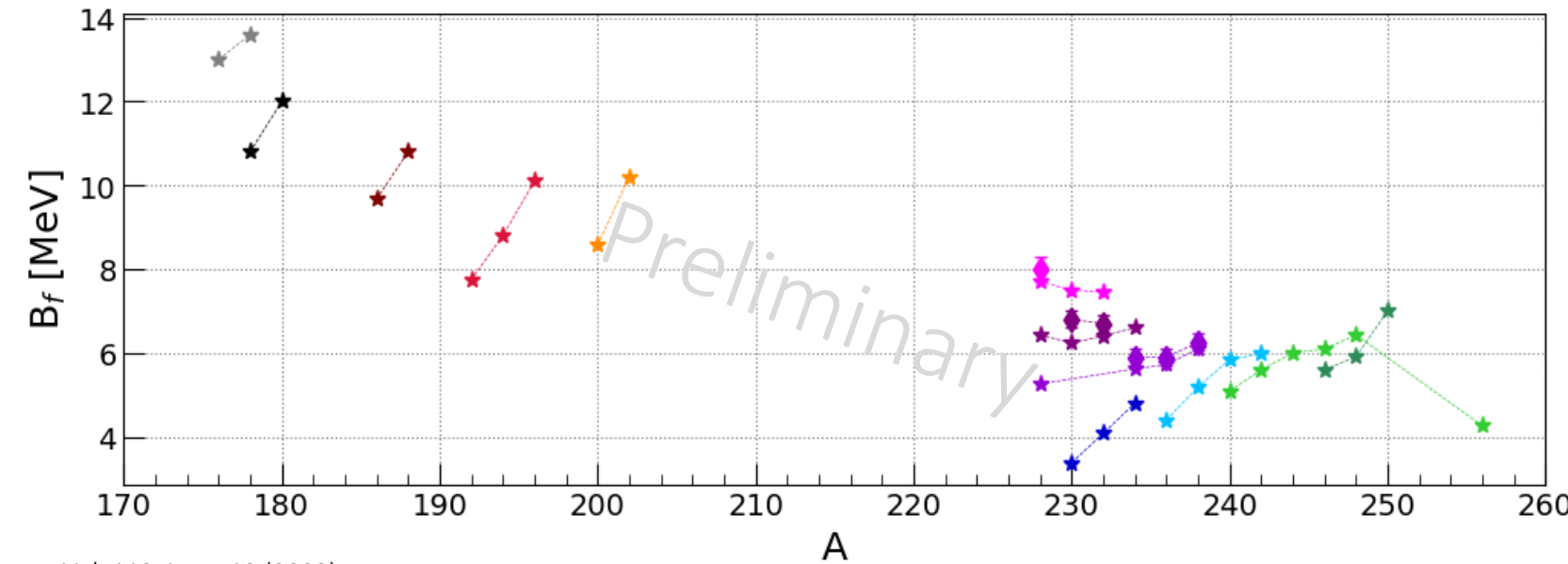
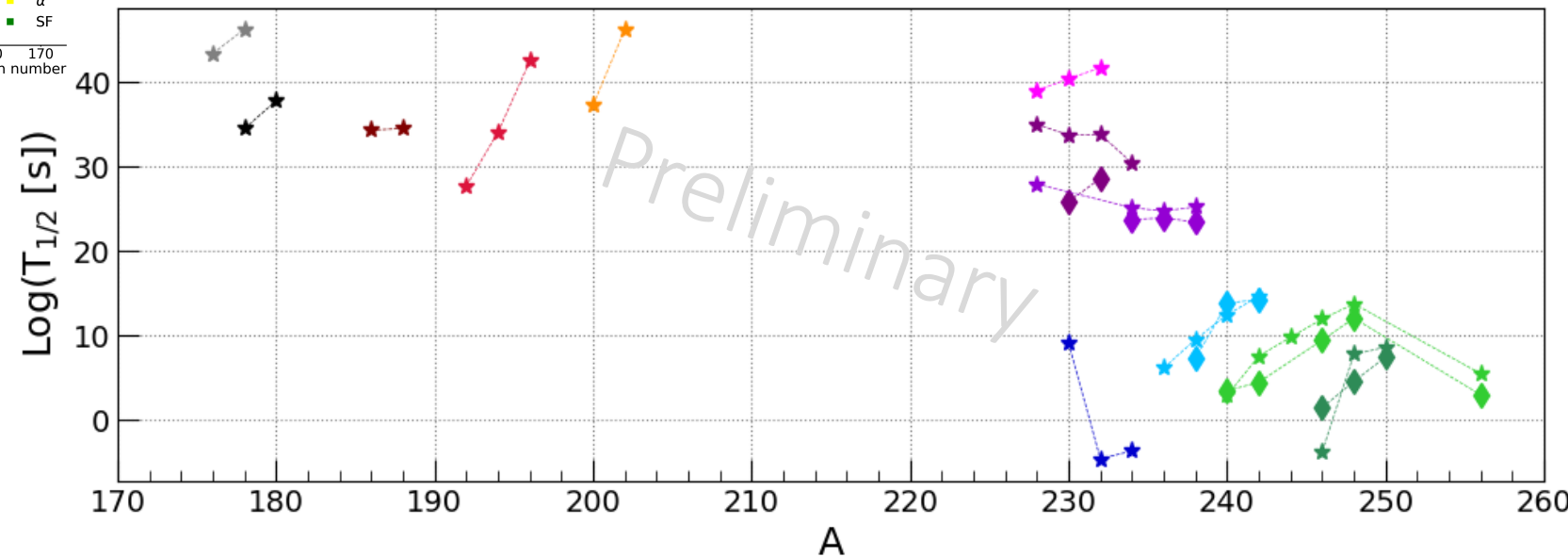
$\beta$ DF of  $^{230}\text{Ac}$



# Fission path with

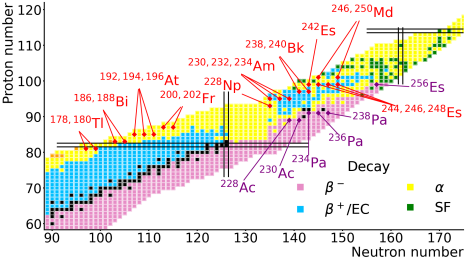


- Pt LAP
- Hg LAP
- Pb LAP
- Po LAP
- Rn LAP

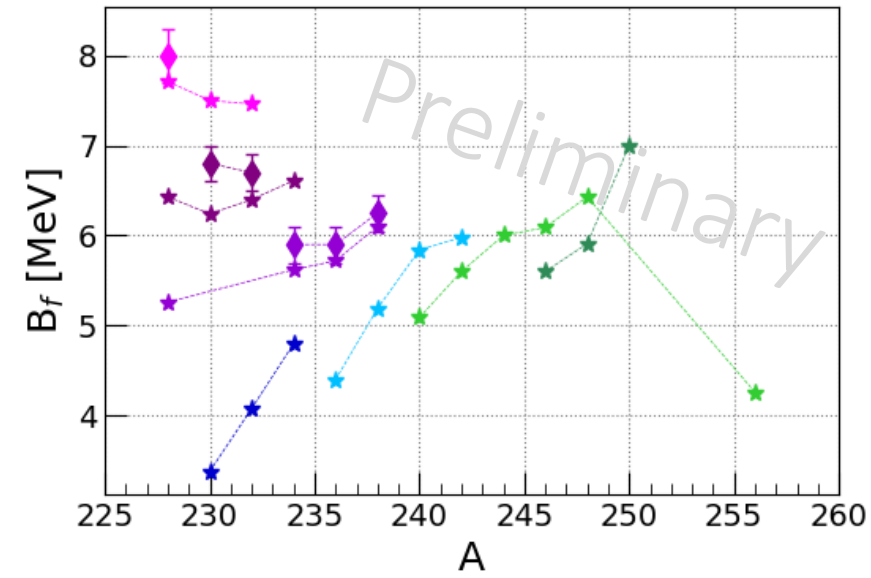
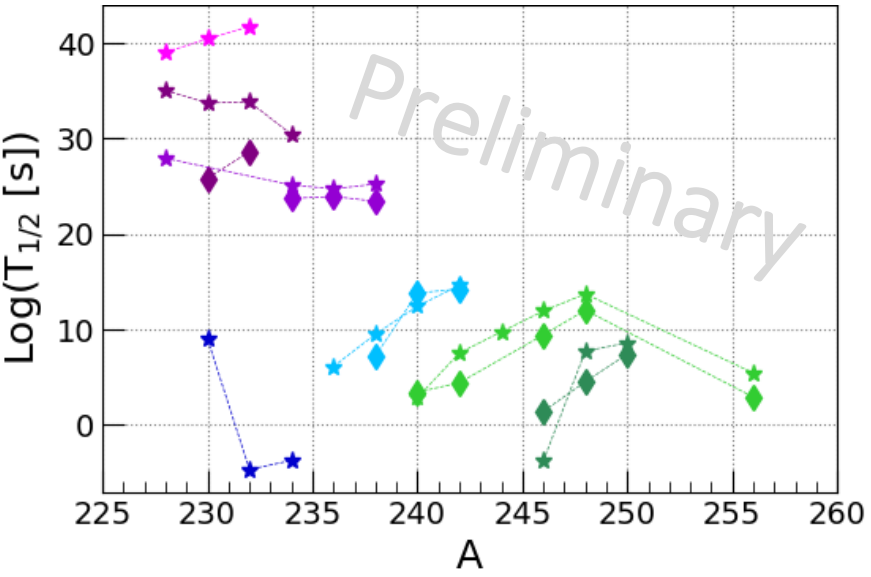
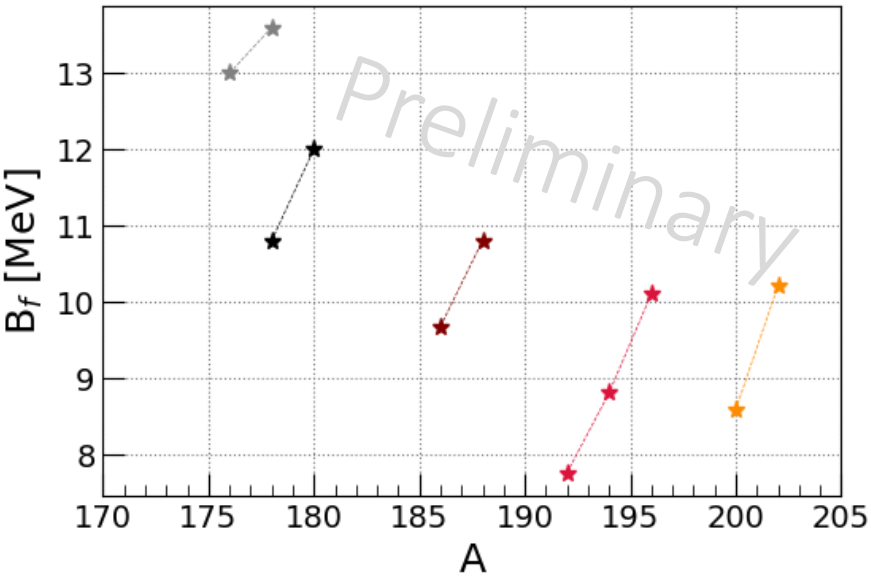
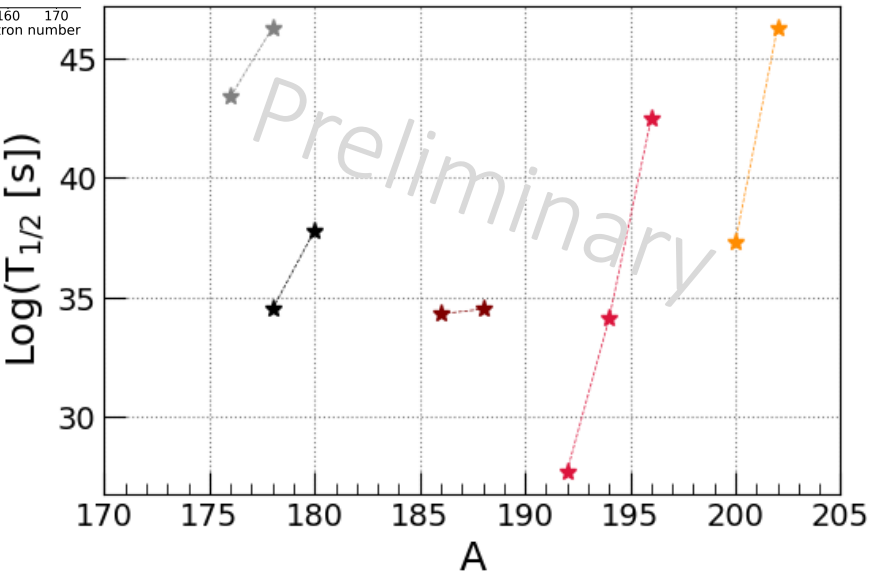


- Ra LAP
- Ra exp
- Th LAP
- Th exp
- U LAP
- U exp
- Pu LAP
- Cm LAP
- Cm exp
- Cf LAP
- Cf exp
- Fm LAP
- Fm exp

# Fission path with



- Pt LAP
- Hg LAP
- Pb LAP
- Po LAP
- Rn LAP



- Ra LAP
- Ra exp
- Th LAP
- Th exp
- U LAP
- U exp
- Pu LAP
- Cm LAP
- Cm exp
- Cf LAP
- Cf exp
- Fm LAP
- Fm exp

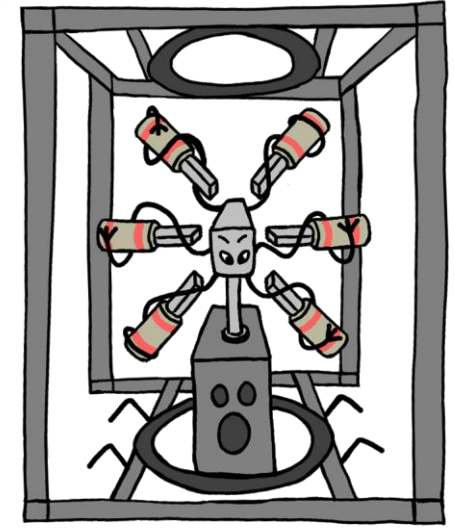
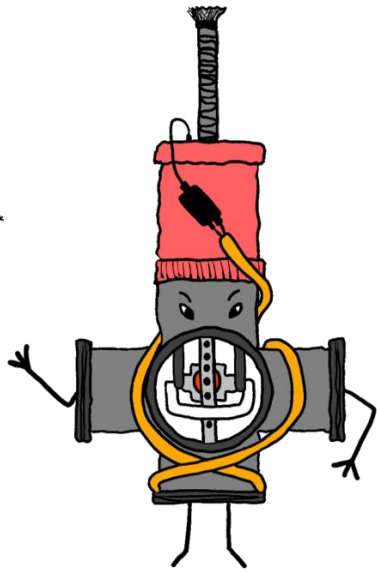
# Conclusions & Outlook

## Conclusions

- Determination of new upper limits for the  $\beta$ DF probabilities of  $^{230,232,234}\text{Ac}$  and  $^{230,232}\text{Fr}$  with particular focus on the  $^{230}\text{Ac}$  one that turned out to be two orders of magnitude lower than the value in literature.
- Observation of events that might hint at cluster emission at mass  $A = 230$ .
- Development of a theoretical procedure to calculate  $\beta$ DF probabilities.

## Outlook

- Calculate  $\beta$ DF probabilities for previously studied cases and compare with experimental results.



# Thank you for the attention

*S. Bara, A. Algora, B. Andel, A. N. Andreyev, S. Antalic, R. A. Bark, M. J. G. Borge, A. Camaiani, T. E. Cocolios, J. G. Cubiss, H. De Witte, C. M. Fajardo-Zambrano, Z. Favier, L. M. Fraile, H. O. U. Fynbo, S. Goriely, R. Grzywacz, M. Heines, F. Ivandikov, J. D. Johnson, P. M. Jones, D. S. Judson, J. Klimo, A. Korgul, M. Labiche, R. Lica, M. Madurga, N. Marginean, C. Mihai, J. Mišt, E. Nácher, C. Neacsu, J. N. Orce, C. Page, R. D. Page, J. Pakarinen, P. Papadakis, A. Perea, M. Piersa-Siřkowska, Zs. Podolyák, R. Raabe, W. Ryssens, A. Sánchez Fernández, A. Sitarčík, O. Tengblad, N. Thomas, J. M. Udías, V. Van Den Bergh, P. Van Duppen, N. Warr, A. Youssef, and Z. Yue*