



Extreme-mass-ratio inspirals into black holes surrounded by boson clouds

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RB & Shreya Shah, arXiv:2307.16093 [gr-qc] Hassan Khalvati+, arXiv:2410.17310 [gr-qc]



Dark matter & Gravitational Waves



From: Bertone *et al*, arXiv:1907.10610

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Dark matter, ultralight bosons & black holes

Dark matter candidates all over the place...



Particles with masses ~ 10^{-21} eV – 10^{-11} eV have Compton wavelengths as large as the size of **astrophysical black holes** ranging from ~ $10M_{\odot} - 10^{10}M_{\odot}$.

$$\mathscr{L} = \frac{R}{16\pi} - \frac{1}{2} \nabla^{\mu} \Phi \nabla_{\mu} \Phi - \frac{\mu^2}{2} \Phi^2$$

 $\mu = m_b c/\hbar = \lambda_c^{-1} \qquad \qquad \alpha := M\mu = R_G/\lambda_C \approx 0.1 \left(\frac{M}{15M_\odot}\right) \left(\frac{m_b c^2}{10^{-12} \text{eV}}\right)$

Massive bosonic fields around black holes

Damour+ '76; Zouros & Eardley '79; Detweiler '80; Cardoso & Yoshida, '05; Dolan '07; Rosa & Dolan '12; Pani+'12; Witek+ '12; RB, Cardoso & Pani '13; Baryakthar, Lasenby & Teo '17; East '17; Cardoso+ '18; Frolov+ '18; Dolan '18; Baumann+ '19; RB, Grillo & Pani '20; Dias+ '23...

Massive bosonic fields can form bound states around black holes.



$$\Re(\omega_{nlm}) \approx \mu \left(1 - \frac{\alpha^2}{2n^2} + \cdots \right)$$

$$\mathfrak{F}(\omega_{nlm}) \propto (m\Omega - \mathfrak{R}(\omega_{nlm})) \alpha^{4l+5}$$

 $\alpha \equiv M\mu$, Ω – "BH's angular velocity"

$$\Re(\omega_{nlm}) < m\Omega \implies \Im(\omega_{nlm}) > 0$$

Superradiant (rotational) *energy extraction* drives instability.

Most unstable mode l = m = 1**maximized** when $\alpha \sim 0.5$.

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Evolution of the superradiant instability



Probing boson clouds with binary systems



From: Baumann+, PRD105, 115036 (2022)

- Some effects induced by the presence of a boson cloud studied using Newtonian approximations:
 - "Ionization" (dynamical friction) and accretion [Baumann+'21; Tomaselli+'23, '24]
 - Floating/Sicking orbits at specific orbital frequencies due to excitation of resonances [Baumann+'18, '19; Zhang&Yang '18; Tomaselli+'24]
 - Non-vanishing tidal Love numbers: $k_l \propto r_{cloud}^{2l+1} \propto 1/\alpha^{4l+2}$ [Baumann+ '18; de Luca+ '21, '22; Arana, RB & Castro '24]



Image credit: Riccardo della Monica

RB & Shah '23; C. Dyson, T. Spieksma+ *in preparation* (see also Duque+ '23)

$$S = \int d^4x \sqrt{-\mathbf{g}} \left(\frac{\mathbf{R}}{16\pi} - \nabla_{\mu} \Phi^* \nabla^{\mu} \Phi - \mu^2 |\Phi|^2 \right) - m_p \int_{\gamma} \sqrt{\mathbf{g}_{ab}} u^a u^b d\tau$$
Scalar field
"environment"
$$M = \text{Primary BH mass}$$

$$m_p = \text{Secondary object mass}$$

$$M_b = \text{total cloud's mass}$$

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 $\mathbf{g}_{\mu\nu} = g_{\mu\nu}^{\text{Kerr}} + qh_{\mu\nu}^{(1,0)} + \epsilon^2 h_{\mu\nu}^{(0,2)} + \epsilon^2 q h_{\mu\nu}^{(1,2)} + \dots, \qquad \mathbf{\Phi} = \epsilon \mathbf{\Phi}^{(0,1)} + q \epsilon \mathbf{\Phi}^{(1,1)} + \dots$

$$q \equiv m_p/M \ll 1 \,, \quad \epsilon \propto \sqrt{M_b/M} \ll 1$$

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$$\mathcal{O}(q^0, \epsilon^1): \left(\Box_{g^{\mathrm{Kerr}}} - \mu^2 \right) \Phi^{(0,1)} = 0 \quad \longrightarrow \quad \Phi_{\ell_b m_b} = R_{\ell_b m_b}(r) S_{\ell_b m_b}(\theta) e^{-i(\omega t - m_b \varphi)}$$

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$$\mathcal{O}(q^1, \epsilon^0): \quad \delta G_{\mu\nu}[h^{(1,0)}] = \int u_{\mu}u_{\nu} \frac{\langle r \rangle}{\sqrt{-g^{\mathrm{Kerr}}}} d\tau \quad \longrightarrow \quad h_{\mu\nu} = \sum_{\ell_g m_g} \int \mathrm{d}\sigma \,, h_{\mu\nu}^{\ell_g m_g}(r, \theta) e^{-i(\sigma t - m_g \phi)}$$

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Scalar energy fluxes

RB & Shah, PRD108, 084019 (2023)



Note: Results for circular, equatorial orbits, **neglecting BH spin.** Kerr BH case is ongoing work (C. Dyson+, *in prep*.)



Power lost due to the presence of the boson cloud can **dominate** over GW emission at large orbital separations.

Orbital dephasing due to scalar clouds

H. Khalvati+, 2410.17310



Credit: Hassan Khalvati, Alessandro Santini & Francisco Duque

EMRIs in clouds: parameter estimation

H. Khalvati+, 2410.17310

FEW: see Chapman-Bird's talk



Credit: Hassan Khalvati, Alessandro Santini & Francisco Duque Scalar fluxes included in **FEW**.

Proof-of-principle bayesian analysis in LISA:

$$\sigma_{M_b}/M_b \sim 5\%$$

$$\sigma_{\alpha_b}/\alpha_b \sim 0.5\%$$

Distinguishable from other environments (e.g. disks, dark matter spikes)? Probably yes. See P.S. Cole+ '23 Presence of **boson clouds** around black holes could leave imprint in GWs emitted by binary black hole systems.

We proposed a **fully relativistic, perturbative framework** to study EMRIs in the presence of boson clouds.

Proof-of-principle results (neglecting BH spin, circular equatorial orbits) promising. **Extension to equatorial, circular orbits in Kerr** being worked out now.

We considered scalar clouds only, but formalism could be useful for **other environments** as well.

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Thank you!

Backup slides

Black hole superradiance

Zel'dovich, '71; Misner '72; Press and Teukolsky ,'72-74; Review: RB, Cardoso & Pani "Superradiance" Lect. Notes Phys. 971 (2020), 2nd ed.



Ionization: Newtonian vs Relativistic

Dashed - Newtonian approximation

Baumann+'21; Tomaselli+'23, '24

Solid - Relativistic (neglecting BH spin, data only up to $R_* = 100M$)



Specific application: axion-like particles

 $\mathscr{L} = -\frac{1}{2}\partial_{\mu}a\partial^{\mu}a - V(a) - \frac{g_{a\gamma}}{2}aF_{\mu\nu}\tilde{F}^{\mu\nu} + \dots, \quad V(a) \approx \frac{m_a^2 a^2}{2} + \mathcal{O}(a^4/f_a^4)$



Purple: lab/collider constraints

Green: lack of solar axions

Blue: direct dark matter searches

Light grey: astro/cosmo constraints that assume axions to be dark matter

Dark grey: astro/cosmo constraints that do not assume axions to be dark matter

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First proposed in Arvanitaki+, "String axiverse", PRD81, 123530 (2010)