

A recipe to find Black holes and Neutron stars

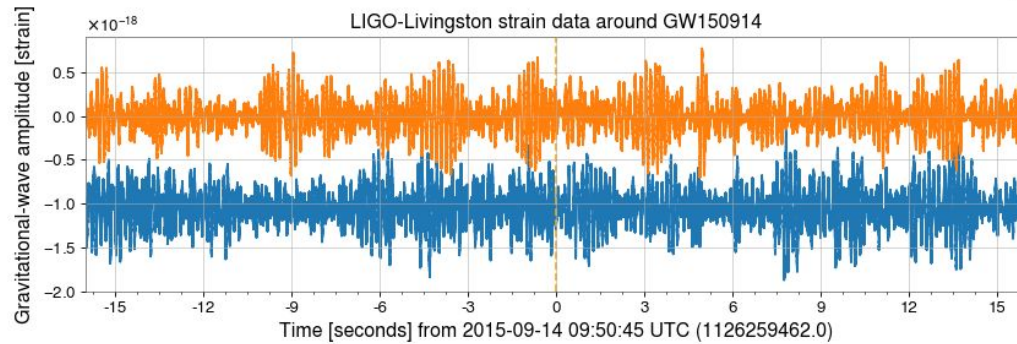
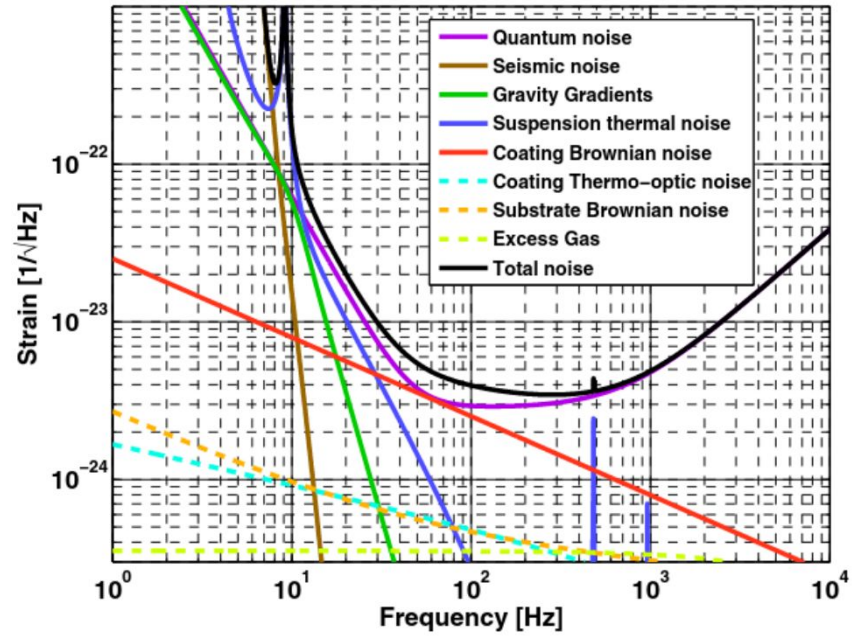
Sebastian Gomez Lopez - Feb 21, 2024.
PhD seminar



SAPIENZA
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Disclaimer



The problem of GW astronomy

1. Search for a signal $u(t)$ buried in stationary, frequency dependent, gaussian noise $n(t)$.
NOTE: we will focus on the case of signals $u(t)$ of known morphology.
2. Decide whether it is of astrophysical origin or not

Hypothesis 1

$$h(t) = n(t)$$

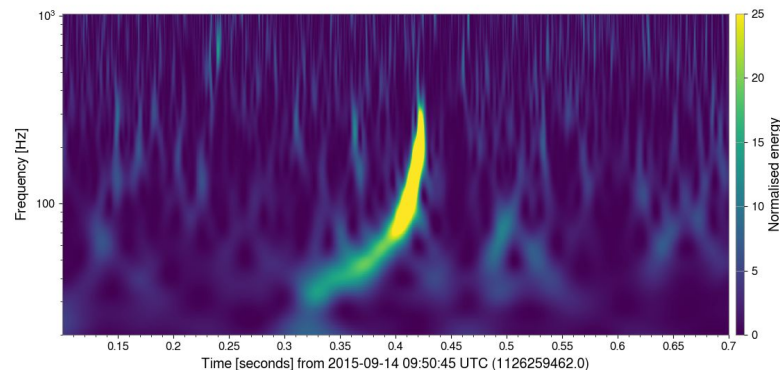
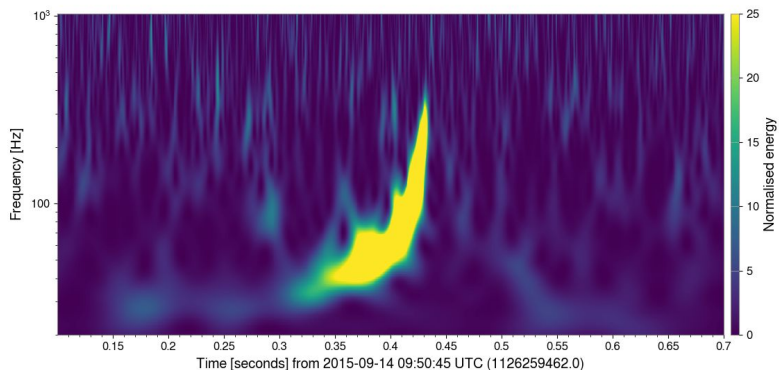
Hypothesis 2

$$h(t) = u(t) + n(t)$$

Note: not only very sensitive detectors are required, but optimal and **computationally affordable** data analysis techniques.

The popular q-scans are based on generic gaussian wavelet filtering.

Extremely useful, flexible and fast. But ... suboptimal.



GW150914 Handford and Livingston.
Source: GOWSC

- The theory of linear filtering can take 1. as input, and give us:

Quote 1: “ The optimal detection statistic when one looks for signals of known/partially known morphology in the presence of gaussian stationary noise is:”

The Matched Filter

Note: This is an optimization problem solved in the 60s. see ***L. A. Wainstein and V. D. Zubakov. Extraction of Signals from Noise***

The matched filter is the key to sentences like:

“... My model is great because, the signal to noise ratio(SNR) is above...”

“... LIGO/Virgo should see my favorite source, because their sensitivity will reach XYZ megaparsec.”

“... I want a grant because X-generation detectors will see this exotic source with SNR of 8.”

Quote 1, can be put in simpler terms as:

→ Template

If we have an estimation of detector's power spectral density.

And If we believe $q(t)$ is the best model for the signal $u(t)$

-> The optimal linear filter to find q in a noisy frequency dependent data stream $h(t)$ is:

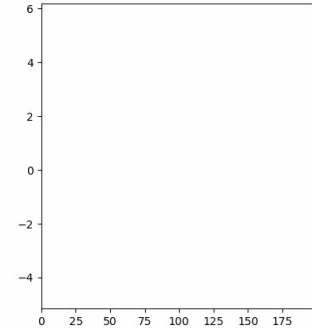
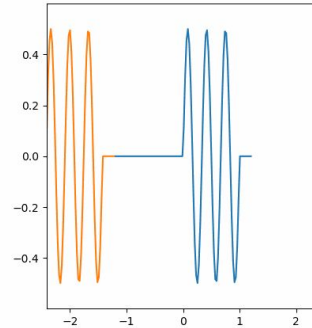
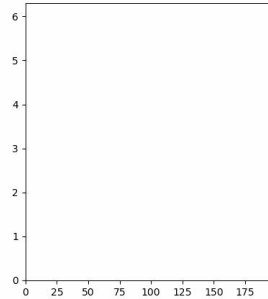
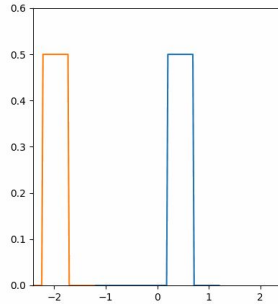
$$\langle h, q \rangle = 4\text{Re} \left(\int_0^\infty \frac{h(f) \cdot q^*(f)}{S_n(f)} \cdot df \right)$$



$$\langle n(f), n(f') \rangle = \delta(f' - f) \cdot S_n(f)$$

$$\int_{-\infty}^{\infty} x(t) \cdot y(t - \tau) d\tau = \int_{-\infty}^{\infty} X(f) \cdot Y(f) e^{i2\pi f\tau} df$$

$$\int_{-\infty}^{\infty} x^*(t) \cdot y(t + \tau) d\tau = \int_{-\infty}^{\infty} X^*(f) \cdot Y(f) e^{-i2\pi f\tau} df$$



- A “sort of” complex valued noise weighted cross correlation:

$$\langle h, qe^{i(2\pi f\tau + \phi_0)} \rangle_{\phi_0 = \phi_{opt}} = 4 \cdot \left(\left| \int_{-\infty}^{\infty} \theta(f) \frac{h(f) \cdot q^*(f)}{S_n(|f|)} \cdot e^{i2\pi f\tau} df \right| \right)$$

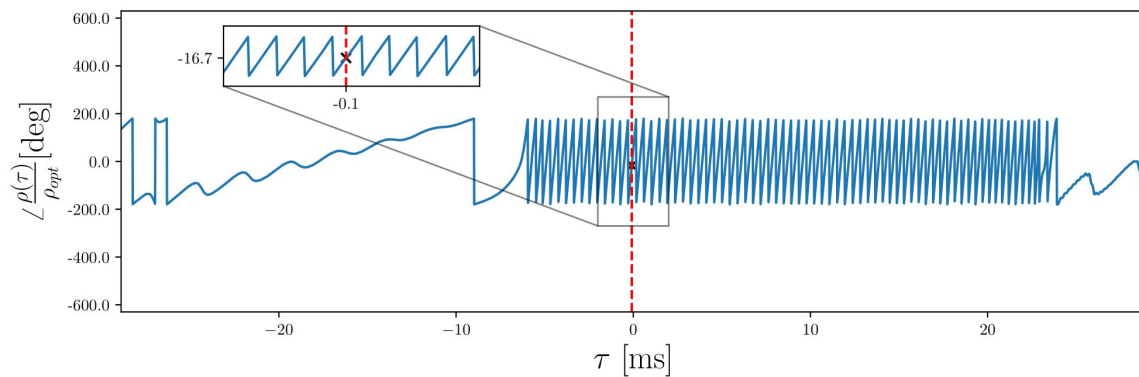
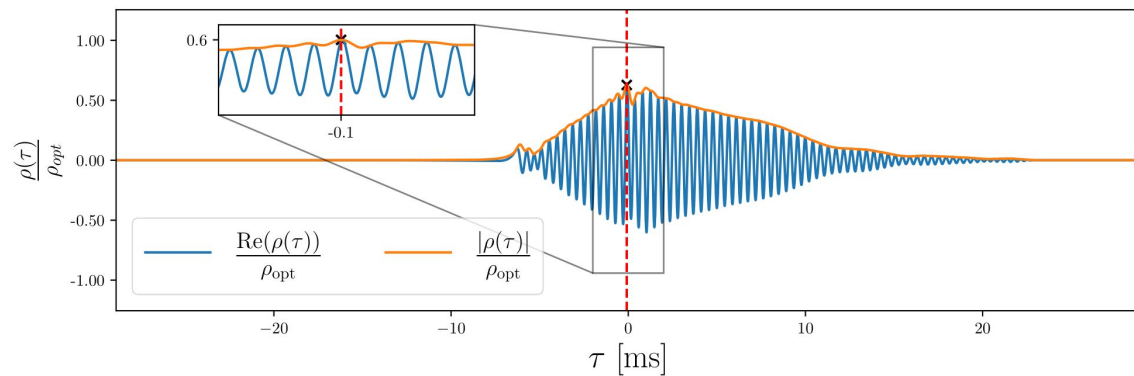
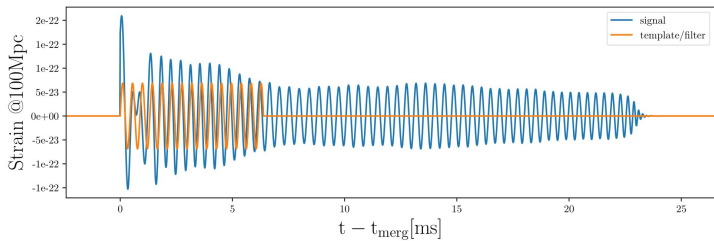
Signal-to-noise ratio “SNR”

$$\rho(\tau) = \frac{\langle h, qe^{i(2\pi f\tau + \phi_0)} \rangle_{\phi_0 = \phi_{opt}}}{\sqrt{\langle q, q \rangle}}$$

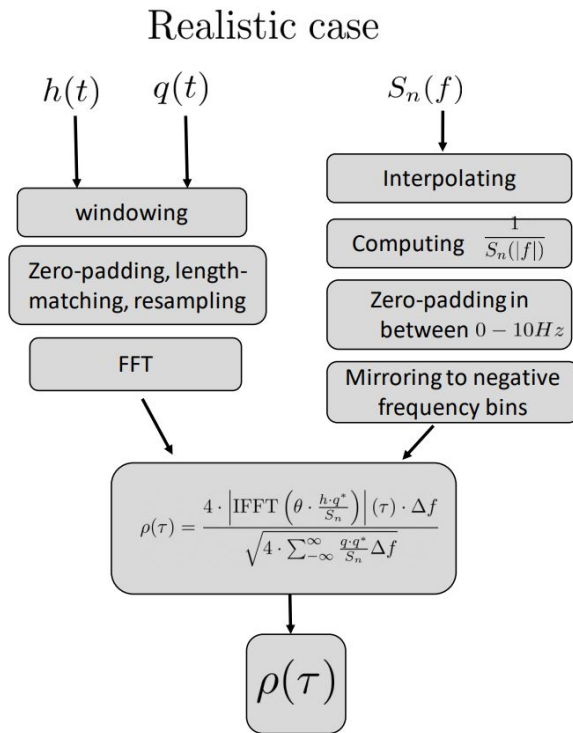
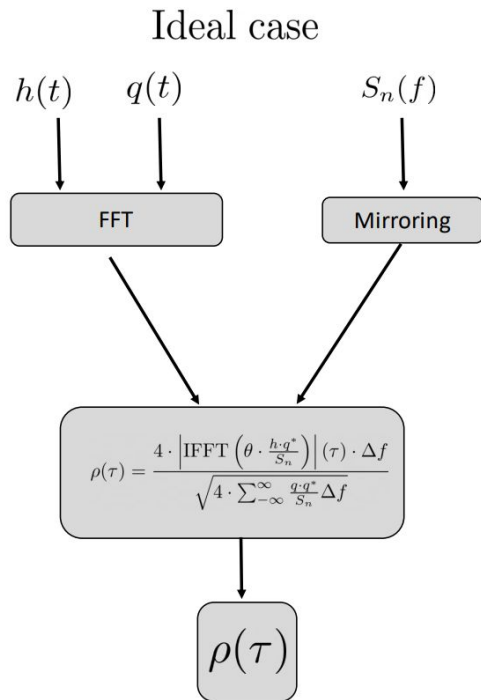
→ (Its a complex timeseries, not a single scalar quantity)

$$\rho(\tau) = \frac{4 \cdot \left| \text{IFFT} \left(\theta \cdot \frac{h \cdot q^*}{S_n} \right) \right|(\tau) \cdot \Delta f}{\sqrt{4 \cdot \sum_{-\infty}^{\infty} \frac{q \cdot q^*}{S_n} \Delta f}}$$

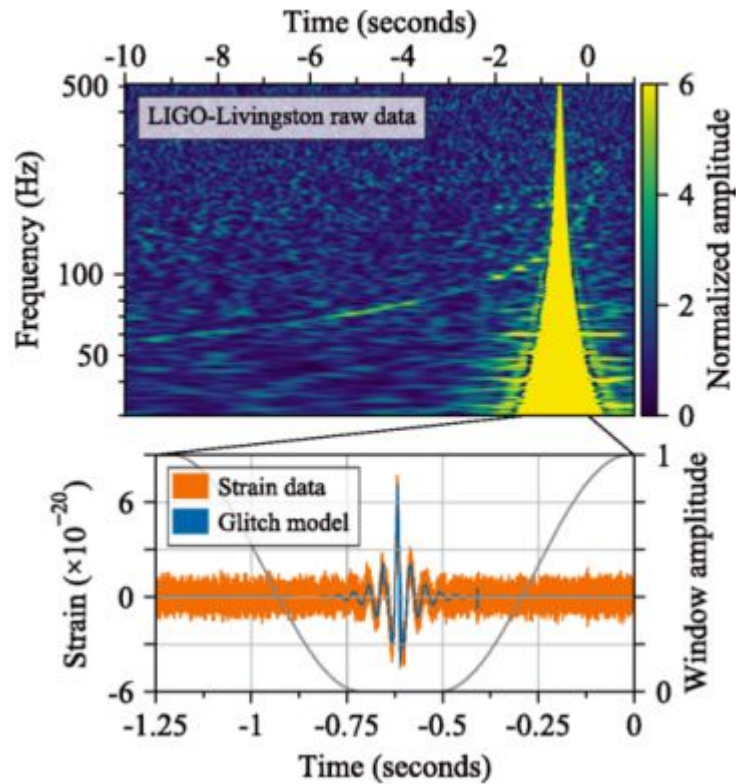
- Gives info about:
 - Signal power
 - Signal phase***



In a real search...



1. $h(t)$ may have deviations from the “gaussian stationary” case. We call them **glitches**.
2. Signals $h(t)$, $q(t)$ have to discretely sampled and must have compact support.
 - Vetoing
 - Zero-padding
 - resampling
 - Windowing
 - Length matching
 - Mirroring

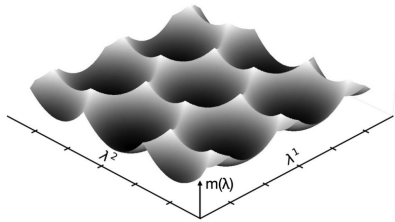


BNS event GW170817: LIGO Livingston

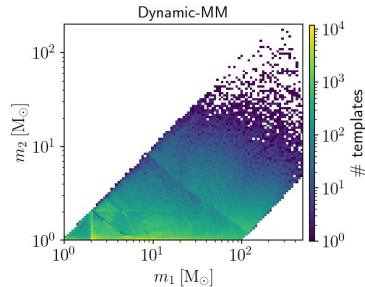
Doing a real search becomes high dimensional problem

$$\langle h, qe^{i(2\pi f\tau + \phi_0)} \rangle_{a_1, \dots, a_n, \phi_0 = \phi_{opt}} = 4 \cdot \left(\left| \int_{-\infty}^{\infty} \theta(f) \frac{h(f) \cdot q_{a_1, \dots, a_n}^*(f)}{S_n(|f|)} \cdot e^{i2\pi f\tau} df \right| \right) (\tau)$$

$q_{a_1, \dots, a_n}(t)$



B. Allen 2021



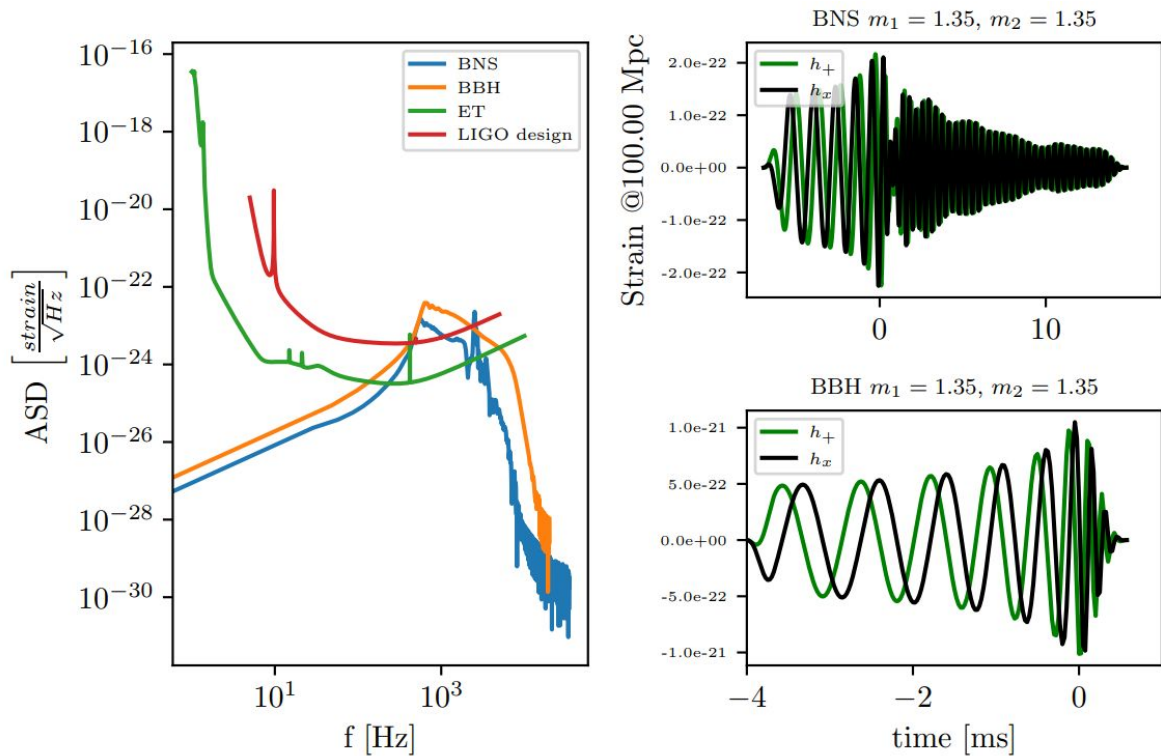
LVK collaboration 2023

Template banks

- Can not be defined **continuously** at every point of $a_1 \times a_2 \dots \times a_n$
- Geometrically motivated ways have been invented to sample that space **discretely** without losing too much SNR. (Using manifold theory)

Searching for black holes and neutron star mergers

- We know their GW signature!



- We can get exact solutions to the 3+1 Einstein's Field equations
- There are several methods to extract accurately gravitational radiation from such simulated events.
- As of today, using the most powerful supercomputers and large amounts of RAM. It is possible to complete one simulation run in weeks of clock time.

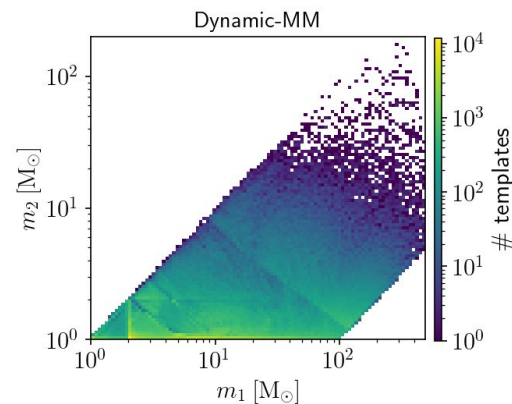
The problem:

- Template banks require hundreds of thousands of signals. This is not computationally achievable.

A solution:

- Find analytical/semianalytical expressions to model the “easy part”.
- We need fewer numerical solutions to “calibrate” these models.

- Inspiral phenomenological waveforms:
 - BBH: yes
 - BNS: yes

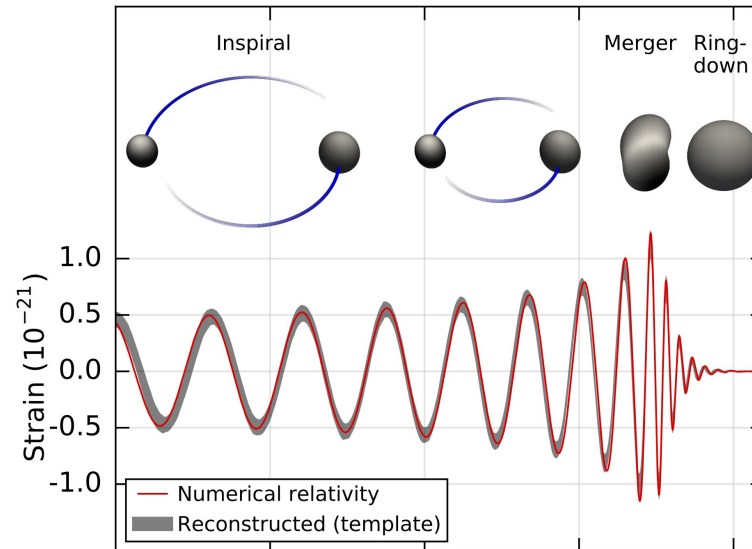


LVK O4a template bank:
approx. 700 thousand templates

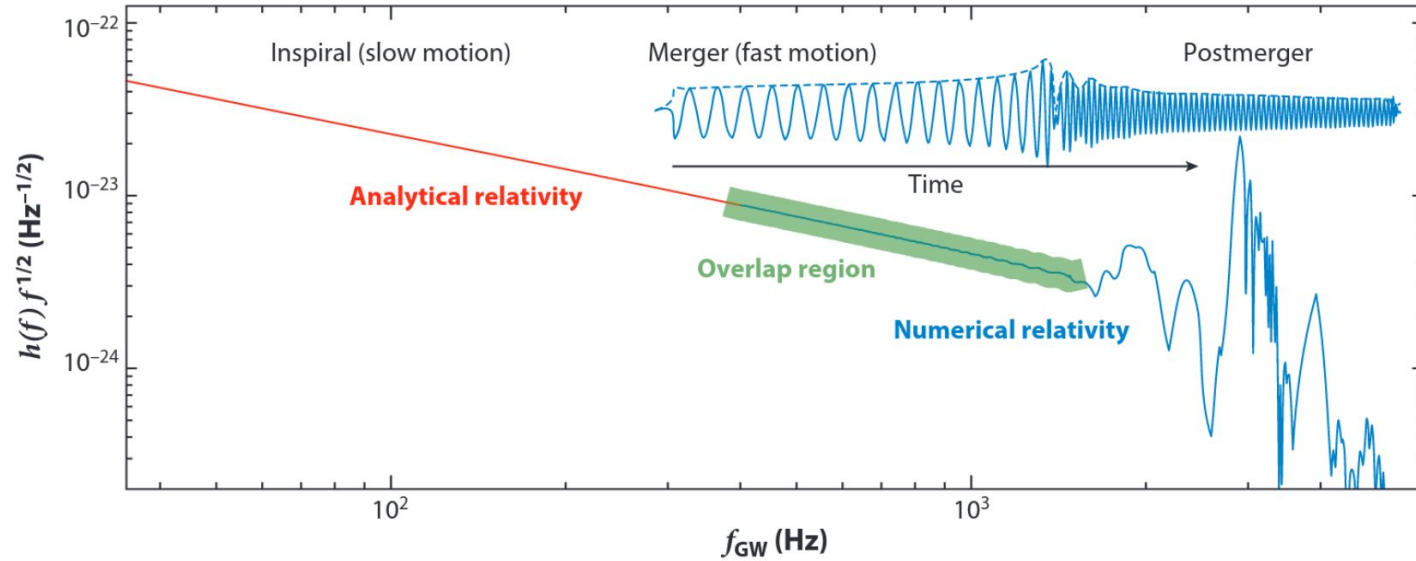
An incomplete solution:

Quasicircular inspiral-merger-postmerger waveforms:

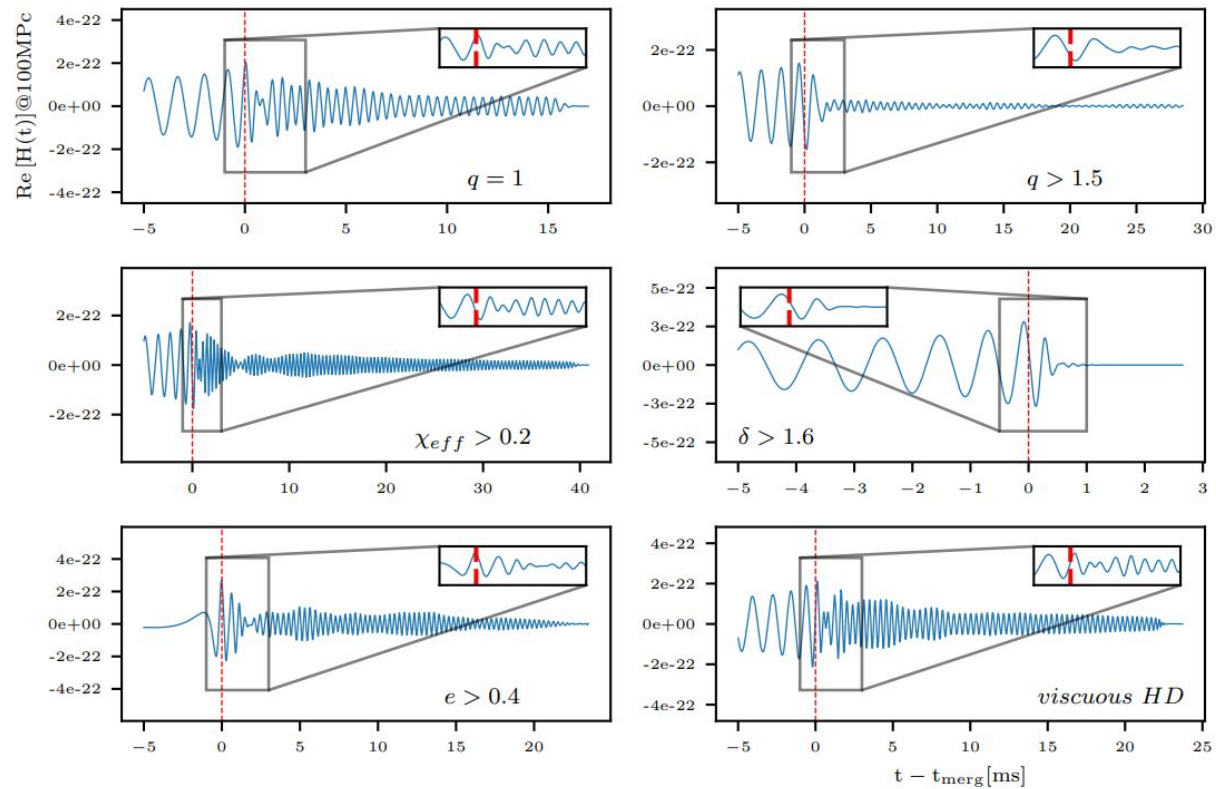
- BBH and yes, but...



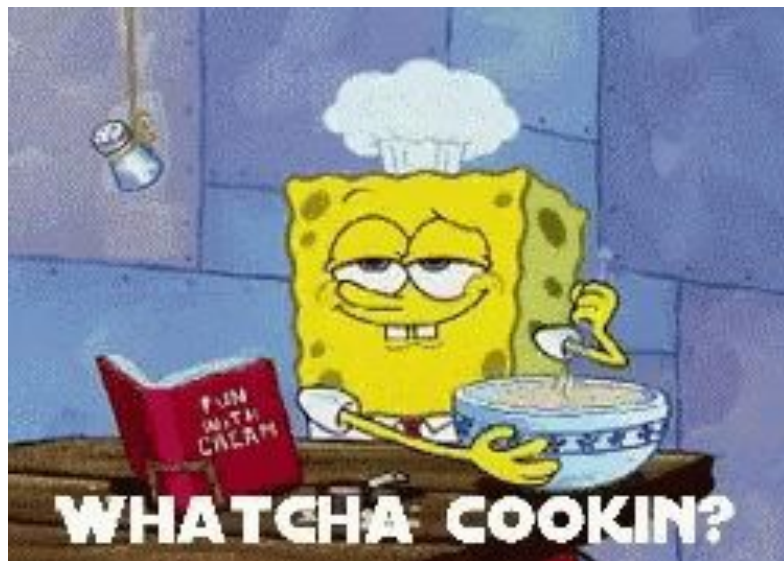
- BNS: Not ready



source: Radice et. al. 2020



source: CoRe BNS catalog



WHATCHA COOKIN?



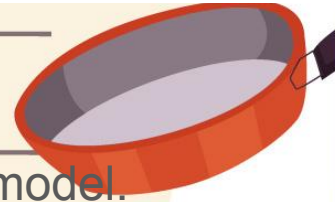
Recipe

Ingredients:

- 1 spoon of NR waveforms(a few hundred)
- 1 template bank with enough waveforms
- A few days of detector data
- A bowl of CPU cores
- A highly paralellized matched filtering engine

Directions:

- step1 Grab a phenomenological waveform model.
- step2. Use the spoon of NR waveforms to calibrate it. And build a template bank.
- step3. Stir your detector data while removing glitches, zeropadding its edges and resampling it as needed.
- step4. Estimate the PSD at runtime.
- step5. Put everything together in the bowl of CPU cores.
- step6. Let the MF engine burn a few thousand cores
- step7. Collect your astrophysically interesting triggers



Conclusions:

- Matched filtering, requires:
 - Theory(phenomenological models)
 - Numerics(to solve Einstein's equations)
 - Highly parallelized signal processing Techniques.
- Implementing this operations in modern computers is a very challenging task:
 - Many cores doing fast fourier transforms are needed.
- Numerical relativity is still needed, otherwise we would not know for sure how good are our banks.
- Looking for “complete” waveforms is beyond the capabilities current computational infrastructure. Specially the BNS case.
- Find tutorials for doing this yourself in:

<https://github.com/gwastro/PyCBC-Tutorials>