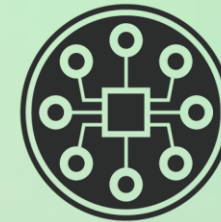


Precision Multi-mode Microwave Characterisation of Single Crystal Calcium Tungstate for Dark Matter Searches



THE UNIVERSITY OF
WESTERN AUSTRALIA



EQUS
Australian Research Council
Centre of Excellence for
Engineered Quantum Systems

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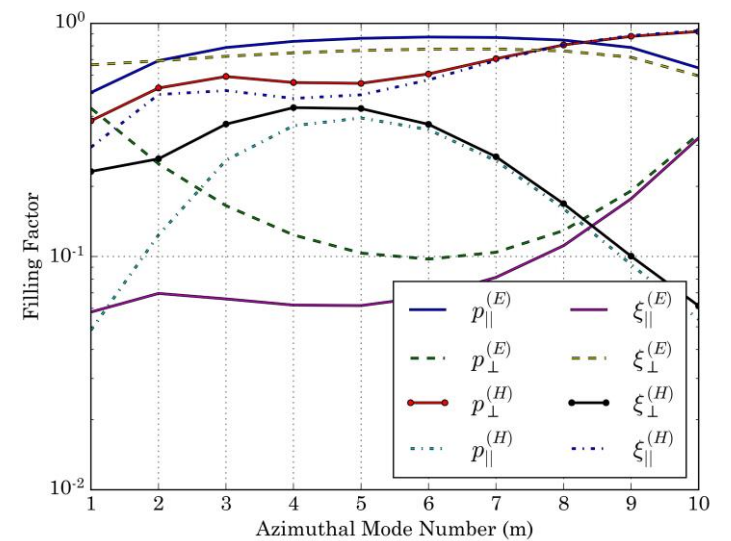
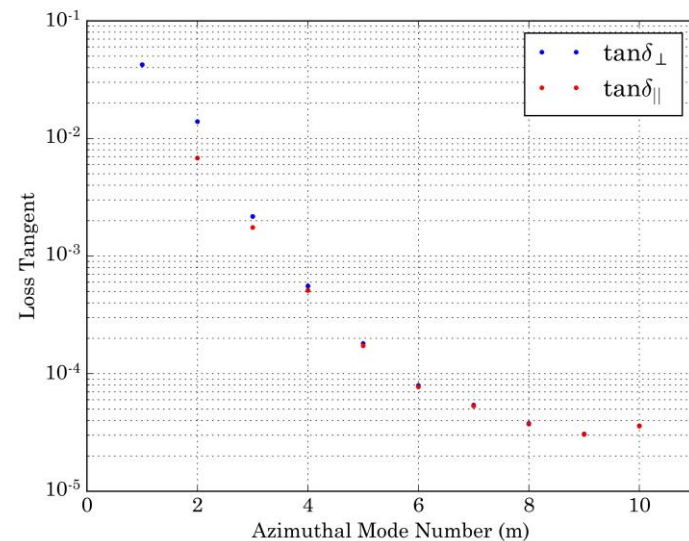
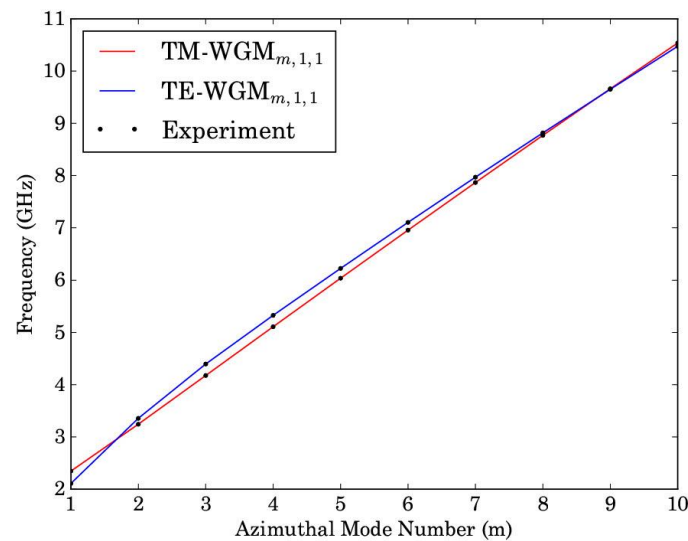
Supervisors: Michael Tobar, Maxim Goryachev, Ben McAllister

Dielectric Characterisation

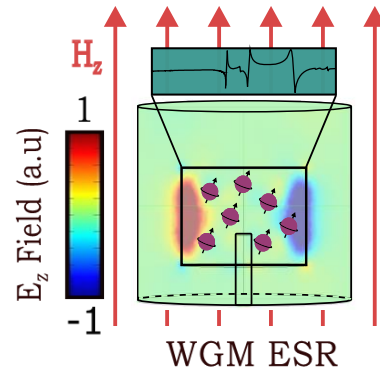
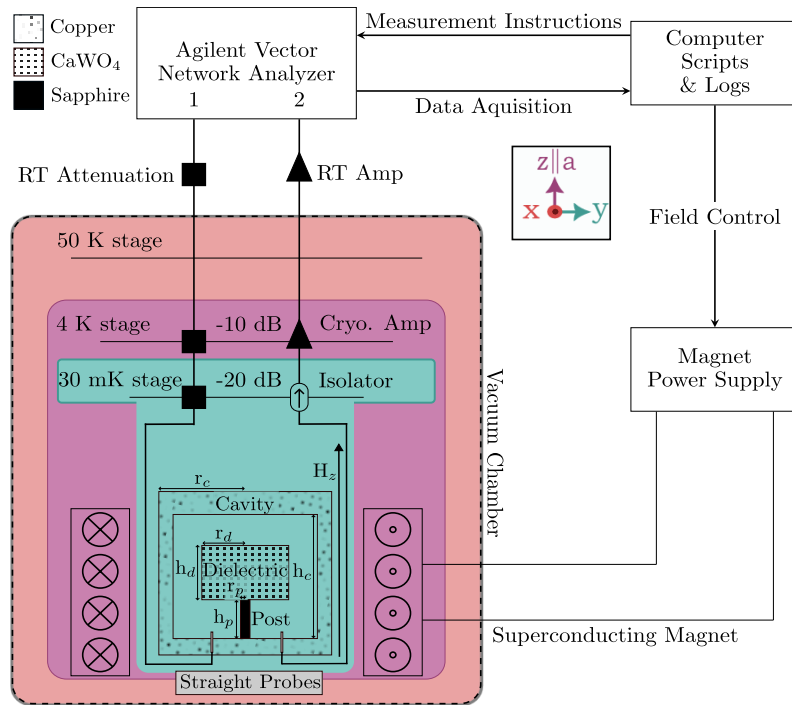
Permittivity at room temperature:

$$\epsilon_{\parallel} = 9.0249 \pm 0.0005$$

$$\epsilon_{\perp} = 10.737 \pm 0.0005$$

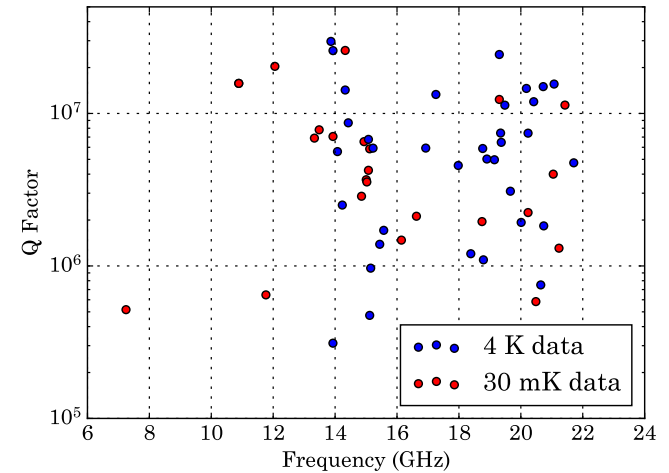


ESR Spectroscopy Methods

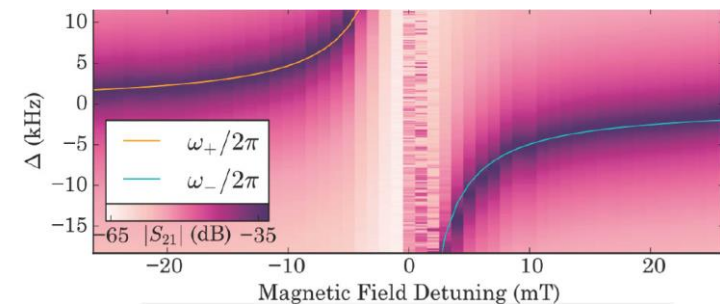


Dimensions of dielectrically loaded cavity resonator:

$$\begin{aligned}
 r_c &= 25 \text{ mm}, h_c = 40 \text{ mm} \\
 r_d &= 14.98 \text{ mm}, h_d = 20 \text{ mm} \\
 r_n &= 1.75 \text{ mm}, h_n = 14.5 \text{ mm}
 \end{aligned}$$

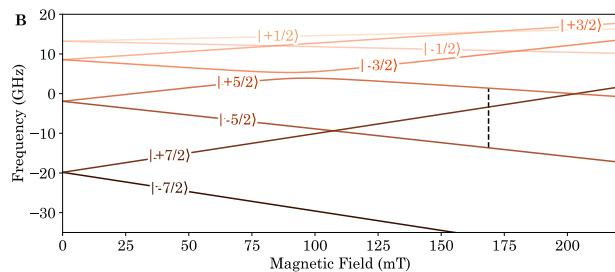
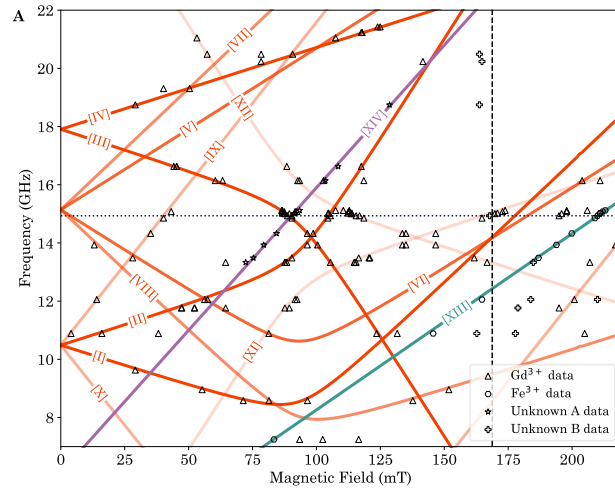


$f_0 = 14.934048 \text{ GHz}$



$$\omega_{\pm} = \frac{1}{\sqrt{2}} \sqrt{\omega_s^2 + \omega_p^2 \pm \sqrt{\omega_s^4 - 2\omega_s^2\omega_p^2 + 4\Delta_{ps}\omega_s^2\omega_p^2 - \omega_p^4}}$$

ESR Spectroscopy Results



Species	ΔS_z	Line	ZFS (GHz)	Transition	
CaWO ₄ :Gd ³⁺ $g_L = 1.99$	1	I	10.49	$ +5/2\rangle \rightarrow +3/2\rangle$	
		II		$ -5/2\rangle \rightarrow -3/2\rangle$	
		III	17.90	$ +7/2\rangle \rightarrow +5/2\rangle$	
		IV		$ -7/2\rangle \rightarrow -5/2\rangle$	
	2	V	15.14	$ -5/2\rangle \rightarrow -1/2\rangle$	
		VI		$ +5/2\rangle \rightarrow +1/2\rangle$	
	3	VII	15.14	$ -5/2\rangle \rightarrow +1/2\rangle$	
		VIII		$ +5/2\rangle \rightarrow -1/2\rangle$	
	4	IX	10.49	$ -5/2\rangle \rightarrow +3/2\rangle$	
		X		$ +5/2\rangle \rightarrow -3/2\rangle$	
		5	XI	0.0	$ -5/2\rangle \rightarrow +5/2\rangle$
			XII		$ +7/2\rangle \rightarrow -3/2\rangle$
CaWO ₄ :Fe ³⁺ $g_L = 4.3$	-	XIII	2.20	-	
Unknown A $g_L = 7$	-	XIV	6.10	-	

TABLE I. Properties of spin transitions calculated from the multi-mode spectroscopy results. Here, ΔS_z is the change in spin quantum number.

$$g = g_L \mu_B \sqrt{\frac{\mu_0 \omega_p n \xi_{\perp}}{4\hbar}}$$

where;

g_L is the Landé g factor,

μ_B is the Bohr Magnetron,

\hbar is the reduced Planck's constant,

ξ_{\perp} is the perpendicular magnetic filling factor,

and μ_0 is the permeability of free space.

$n = 8.28 \pm 1.24 \times 10^{13} \text{ cm}^{-3}$ which is on the order of ppb.

$$\mathcal{H} = g_L \mu_B H_z S_z + B_2^0 O_2^0 + B_4^0 O_4^0 + B_4^4 O_4^4 + B_6^0 O_6^0 + B_6^4 O_6^4$$