Maglev for Dark Matter



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Introduction



[Caputo et al., Phys. Rev. D. **104**, 095029 (2021)]

Introduction

- Ultralight DM interactions can generate AC magnetic fields:
 - Dark photon kinetic mixing
 - Axion-photon coupling
 - Axion-electron coupling
- Many experiments utilize EM resonances $\rightarrow f_{\rm DM} \gtrsim \rm kHz \ (m_{\rm DM} \gtrsim 10^{-12} \, eV)$
- Can use mechanical resonance for lower frequencies
- Mechanical system + sensitive to magnetic fields \rightarrow magnetic levitation

Outline

- Dark matter candidates
- Magnetic levitation
 - Levitated superconductors
 - Levitated ferromagnets
- Noise sources
- Sensitivity

Kinetically mixed dark photon

- Massive vector $A^{\prime\mu}$
- Non-relativistic $\rightarrow A'$ uniform in space, oscillates with frequency $m_{A'}$
- Coupled to EM via $\varepsilon m_{A'}^2 A'^{\mu} A_{\mu} \rightarrow$ effective current $J_{\text{eff}}^{\mu} = -\varepsilon m_{A'}^2 A'^{\mu}$

Can source EM fields via Ampère's Law

$$abla imes oldsymbol{B} - \partial_t oldsymbol{E} = oldsymbol{J}_{ ext{eff}}$$

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• When $\lambda_{\rm DM}$ larger than apparatus, E negligible ightarrow only B signal

Axionlike particle

- Massive pseudoscalar a (oscillates with mass m_a)
- Axion-photon coupling $g_{a\gamma} a F^{\mu\nu} \tilde{F}_{\mu\nu}$
 - Effective current $J_{
 m eff}=ig_{a\gamma}m_aaB_0$ ightarrow similar to dark photon
 - $\,\circ\,$ For levitated superconductor, trap can act as ${\boldsymbol B}_0!$
 - $\circ\,$ For levitated ferromagnet, magnet can act as $B_0!$

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- Axion-electron coupling $\frac{g_{ae}}{2m_e}\partial_{\mu}a\bar{\psi}_e\gamma^{\mu}\gamma_5\psi_e$
 - Causes precession of electron spins
 - Effective magnetic field $oldsymbol{B}_{ae} = -rac{g_{ae}}{e}
 abla a$

Levitated superconductors



Levitated superconductors



Levitated ferromagnets



Levitated ferromagnets (axion wind)







Effect of trapping potential

- Ferromagnet levitated in trapping potential $V(\boldsymbol{x}, \boldsymbol{\hat{n}})$, e.g.
 - $\,\circ\,$ Over superconductor $V\propto \frac{1+\cos^2\theta}{z^3}$
 - $\circ~$ In freefall $V\approx 0$
- Resonances and behavior depend on angular trapping $v_{\alpha\alpha} \equiv \frac{2}{N\hbar} \partial_{\alpha}^2 V$:
 - Trapped $(v_{\alpha\alpha} \gg \omega_I)$: only libration, resonances at $m_{\rm DM} = \sqrt{v_{\alpha\alpha}\omega_I}$

• Gyroscope $(v_{\alpha\alpha} \ll \omega_I)$: precession when $v_{\alpha\alpha} \ll m_{\rm DM} \ll \omega_I$, resonances at $m_{\rm DM} = \omega_I, \sqrt{v_{\theta\theta}v_{\phi\phi}}$ where $\omega_I = \frac{N\hbar}{2I}$

Noise sources

• Thermal: kicks from gas molecules

Noise sources

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- Imprecision: flux noise \rightarrow position/angle
- Back-action: current noise \rightarrow force/torque



[Hofer et al., Phys. Rev. Lett. 131, 043603 (2023)]

Noise sources

- Thermal: kicks from gas molecules
- Imprecision: flux noise \rightarrow position/angle
- Back-action: current noise \rightarrow force/torque
- If thermal subdominant, coupling trade-off
 - \circ Small coupling \rightarrow resonant detection
 - \circ Large coupling \rightarrow broadband detection



Dark photon sensitivity (SC)







Axion-electron sensitivity (ferromagnet)

 $f_a [Hz]$ 10^{-3} 10^{-2} 0.1 10^{2} 10^{3} Integration time: 1 yr 10 10^{-6} Magnetization: $7 \times 10^5 \, \text{A/m} \approx 0.9 \, \text{T}$ 10^{-7} Torsion 10^{-8} Comagnetometers Existing 10^{-9} Freefall Future ${}^{s}_{5}$ 10^{-10} Mass $250\,\mathrm{ng}$ $250\,\mathrm{mg}$ $250\,\mathrm{g}$ 10^{-11} XENONnT Temperature $4 \,\mathrm{K}$ $50\,\mathrm{mK}$ $300\,\mathrm{K}$ 10^{-12} Red Giants 10^{-13} Existing 10^{-14} Future Quality factors Freefall 10^{-15} 10^{-15} 10^{-12} 10^{-14} 10^{-16} 10^{-13} 10^{-17} $m_a \,[\mathrm{eV}]$

Dark photon sensitivity (ferromagnet)



Axion-photon sensitivity (ferromagnet)



Conclusion

- Maglev systems can probe ultralight DM with $m_{\rm DM} \lesssim 10^{-12} \, {\rm eV}$
- Dark photon or axion-photon coupling source oscillating magnetic fields
 - Causes translational motion of levitated superconductor
 - Rotational motion of levitated ferromagnet (also sensitive to axion-electron coupling)
- Ferromagnet dynamics affected by trapping potential and $m_{
 m DM}$
- Resonant and broadband schemes
- Dedicated setups can be leading laboratory probes of ultralight DM

Backup Slides

Physical considerations

• Vertical displacement:

$$\Delta z = \frac{g}{4\pi^2 f_z^2} \sim 3 \,\mathrm{cm} \cdot \left(\frac{3 \,\mathrm{Hz}}{f_z}\right)^2$$

• Maximum magnetic field:

$$B_{\rm max} \sim b_0 \mathcal{R} \sim 80 \,\mathrm{mT} \cdot \left(\frac{m}{1 \,\mathrm{g}}\right)^{1/3} \left(\frac{\rho}{0.1 \,\mathrm{g/cm^3}}\right)^{1/6} \left(\frac{f_0}{100 \,\mathrm{Hz}}\right)$$

- Pb and Ta have critical fields of $\,\sim 80\,{\rm mT}$

Sources of dissipation

• Gas collisions:

$$\gamma \sim \frac{PA}{m\bar{v}_{\rm gas}} \sim 2\pi \cdot 10^{-8} \,\mathrm{Hz} \cdot \left(\frac{P}{10^{-7} \,\mathrm{Pa}}\right) \left(\frac{1 \,\mathrm{g}}{m}\right)^{1/3} \cdot \left(\frac{0.1 \,\mathrm{g/cm^3}}{\rho}\right)^{2/3} \sqrt{\left(\frac{m_{\rm gas}}{4 \,\mathrm{Da}}\right) \left(\frac{10 \,\mathrm{mK}}{T}\right)}$$

• Flux creep: movement of unpinned flux lines in type-II SC \rightarrow use type-I SC

• Eddy current damping in nearby conductors \rightarrow use only SCs and dielectrics

DPDM magnetic field signal



$$BR \sim \oint \mathbf{B} \cdot d\ell = \iint \mathbf{J}_{\text{eff}} \cdot d\mathbf{A} \sim \varepsilon m_{A'}^2 R^2 A'$$

• Imprecision and back-action noise determined by coupling η :

$$S_{BB}^{\rm imp} = \frac{2\rho S_{\phi\phi}}{3m^2\omega_0^2\eta^2 |\chi(\omega)|^2} \qquad \qquad S_{BB}^{\rm back} = \frac{2\rho\eta^2 S_{JJ}}{3m^2\omega_0^2}$$

• Flux and current noise satisfy uncertainty relation $\sqrt{S_{\phi\phi}S_{JJ}} = \kappa \ge 1$

• Can define
$$\tilde{\eta} = \eta \sqrt[4]{\frac{S_{JJ}}{S_{\phi\phi}}}$$
, so that

$$S_{BB}^{imp} = \frac{2\rho\kappa}{3m^2\omega_0^2} \cdot \tilde{\eta}^{-2} |\chi(\omega)|^{-2} \qquad S_{BB}^{back} = \frac{2\rho\kappa}{3m^2\omega_0^2} \cdot \tilde{\eta}^2$$

• If
$$S_{BB,\alpha\alpha}^{\mathrm{th}} < \sqrt{S_{BB,\alpha\alpha}^{\mathrm{imp}}}(\omega = 0) \cdot S_{BB,\alpha\alpha}^{\mathrm{back}}$$
 [or $\tilde{\eta}^{(\mathrm{res})} \ge \tilde{\eta}^{(\mathrm{broad})}$], then either:

- Resonant detection: $\tilde{\eta}^{(\mathrm{res})} = \sqrt{\frac{4m\gamma T}{\kappa}}$
- Broadband detection: $\tilde{\eta}^{(\mathrm{broad})} = \sqrt{m}\omega_0$
- Otherwise, can choose any $\tilde{\eta}^{(\text{res})} \geq \tilde{\eta} \geq \left[\tilde{\eta}^{(\text{broad})}\right]^2 / \tilde{\eta}^{(\text{res})}$
 - Larger $\tilde{\eta}$ is better for higher frequencies

Signal-to-noise ratio

• Coherent:

$$\mathrm{SNR} = \frac{B_{\mathrm{DM}}^2}{S_{BB}^{\mathrm{tot}}/t_{\mathrm{int}}}$$

• Incoherent:

$$\mathrm{SNR} = \frac{B_{\mathrm{DM}}^2}{S_{BB}^{\mathrm{tot}}/t_{\mathrm{coh}}} \cdot \sqrt{\frac{t_{\mathrm{int}}}{t_{\mathrm{coh}}}}$$

• Multiple scans:

$$\mathrm{SNR}^2 = \sum_i \mathrm{SNR}_i^2$$

Bandwidth

• Bandwidth defined by:

$$S_{BB}^{\text{tot}}\left(\omega_0 + \frac{\delta\omega}{2}\right) = 2S_{BB}^{\text{tot}}(\omega_0)$$

• For resonant coupling,

$$\delta\omega = \frac{4\sqrt{2}\gamma T}{\kappa\omega_0} \sim 2\pi \cdot 0.2 \operatorname{Hz}\left(\frac{\gamma}{2\pi \cdot 10^{-8} \operatorname{Hz}}\right) \cdot \left(\frac{T}{10 \operatorname{mK}}\right) \left(\frac{5}{\kappa}\right) \left(\frac{10 \operatorname{Hz}}{f_0}\right)$$

• Total scan takes

$$\sum_{i} t_{\text{int},i} = \frac{\kappa \pi}{2\sqrt{2}\gamma T v_{\text{DM}}^2} \Delta \omega \sim 1 \operatorname{yr}\left(\frac{\kappa}{5}\right) \left(\frac{2\pi \cdot 10^{-8} \operatorname{Hz}}{\gamma}\right) \cdot \left(\frac{10 \operatorname{mK}}{T}\right) \left(\frac{\Delta f}{74 \operatorname{Hz}}\right)$$



Libration vs. Precession



Ferromagnet readout



Ferromagnet noise curves

