Maglev for Dark Matter

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Based on arXiv:2310.18398 and arXiv:2408.15330

Introduction

Introduction

- Ultralight DM interactions can generate AC magnetic fields:
	- Dark photon kinetic mixing
	- Axion-photon coupling
	- Axion-electron coupling
- Many experiments utilize EM resonances $\rightarrow f_{\rm DM} \gtrsim k \rm Hz$ $(m_{\rm DM} \gtrsim 10^{-12} \, \rm eV)$
- Can use mechanical resonance for lower frequencies
- Mechanical system + sensitive to magnetic fields \rightarrow magnetic levitation

Outline

- Dark matter candidates
- Magnetic levitation
	- Levitated superconductors
	- Levitated ferromagnets
- Noise sources
- Sensitivity

Kinetically mixed dark photon

- Massive vector $A^{\prime\mu}$
- Non-relativistic \rightarrow A' uniform in space, oscillates with frequency $m_{A'}$
- Coupled to EM via ϵm_A^2 , $A^{\prime\mu} A_\mu \rightarrow$ effective current $J_{\text{eff}}^\mu = -\epsilon m_A^2$, $A^{\prime\mu}$
- Can source EM fields via Ampère's Law

$$
\nabla \times \boldsymbol{B} - \partial_t \boldsymbol{E} = \boldsymbol{J}_{\text{eff}}
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$$

• When $\lambda_{\rm DM}$ larger than apparatus, E negligible \rightarrow only B signal

Axionlike particle

- Massive pseudoscalar a (oscillates with mass m_a)
- Axion-photon coupling $g_{a\gamma}aF^{\mu\nu}F_{\mu\nu}$
	- Effective current $J_{\text{eff}} = ig_{a\gamma} m_a a \boldsymbol{B}_0 \rightarrow \text{similar to dark photon}$
	- For levitated superconductor, trap can act as $B_0!$
	- For levitated ferromagnet, magnet can act as $B_0!$

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- Axion-electron coupling $\frac{g_{ae}}{2m_e}\partial_\mu a\bar{\psi}_e\gamma^\mu\gamma_5\psi_e$
	- Causes precession of electron spins
	- Effective magnetic field $B_{ae} = -\frac{g_{ae}}{e} \nabla a$

Levitated superconductors

Levitated superconductors

Levitated ferromagnets

Levitated ferromagnets (axion wind)

Effect of trapping potential

- Ferromagnet levitated in trapping potential $V(\boldsymbol{x}, \boldsymbol{\hat{n}})$, e.g.
	- Over superconductor $V \propto \frac{1+\cos^2\theta}{z^3}$
	- In freefall $V \approx 0$
- Resonances and behavior depend on angular trapping $v_{\alpha\alpha} \equiv \frac{2}{N\hbar} \partial^2_{\alpha} V$.
	- Trapped $(v_{\alpha\alpha} \gg \omega_I)$: only libration, resonances at $m_{\text{DM}} = \sqrt{v_{\alpha\alpha} \omega_I}$
	- Gyroscope $(v_{\alpha\alpha} \ll \omega_I)$: precession when $v_{\alpha\alpha} \ll m_{\text{DM}} \ll \omega_I$, resonances at $m_{\text{DM}} = \omega_I, \sqrt{v_{\theta\theta}v_{\phi\phi}}$ where $\omega_I = \frac{N\hbar}{2I}$

Noise sources

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- Imprecision: flux noise \rightarrow position/angle
- Back-action: current noise → force/torque

[Hofer et al., Phys. Rev. Lett. 131, 043603 (2023)]

Noise sources

- Thermal: kicks from gas molecules
- Imprecision: flux noise \rightarrow position/angle
- Back-action: current noise → force/torque
- If thermal subdominant, coupling trade-off
	- Small coupling → resonant detection
	- Large coupling → broadband detection

Dark photon sensitivity (SC)

Axion-electron sensitivity (ferromagnet)

 f_a [Hz] Integration time: 1 yr 10^{-3} 10^{-2} 0.1 $10²$ $10³$ 10 10^{-6} Magnetization: 7×10^5 A/m ≈ 0.9 T 10^{-7} Torsion 10^{-8} Comagnetometers Existing Future Freefall 10^{-9} $\frac{8}{5}$ 10^{-10} Mass 250 ng $250 \,\mathrm{mg}$ $250 g$ 10^{-11} EXENONnT **Temperature** $4K$ $50 \,\mathrm{mK}$ $300\,\mathrm{K}$ 10^{-12} Red Giants 10^{-13} 3×10^8 5×10^{13} 5×10^{11} Existing 10^{-14} Future Quality factors 7×10^6 5×10^{10} 5×10^{11} Freefall 10^{-15} $\frac{1}{10^{-12}}$ 10^{-15} 10^{-14} 10^{-16} 10^{-13} 10^{-17} m_a [eV]

Dark photon sensitivity (ferromagnet)

Axion-photon sensitivity (ferromagnet)

Conclusion

- Maglev systems can probe ultralight DM with $m_{\rm DM} \lesssim 10^{-12} \, {\rm eV}$
- Dark photon or axion-photon coupling source oscillating magnetic fields
	- Causes translational motion of levitated superconductor
	- Rotational motion of levitated ferromagnet (also sensitive to axion-electron coupling)
- Ferromagnet dynamics affected by trapping potential and m_{DM}
- Resonant and broadband schemes
- Dedicated setups can be leading laboratory probes of ultralight DM

Backup Slides

Physical considerations

• Vertical displacement:

$$
\Delta z = \frac{g}{4\pi^2 f_z^2} \sim 3 \,\text{cm} \cdot \left(\frac{3 \,\text{Hz}}{f_z}\right)^2
$$

• Maximum magnetic field:

$$
B_{\text{max}} \sim b_0 \mathcal{R} \sim 80 \,\text{mT} \cdot \left(\frac{m}{1 \,\text{g}}\right)^{1/3} \left(\frac{\rho}{0.1 \,\text{g/cm}^3}\right)^{1/6} \left(\frac{f_0}{100 \,\text{Hz}}\right)
$$

• Pb and Ta have critical fields of $\sim 80 \,\mathrm{mT}$

Sources of dissipation

• Gas collisions:

$$
\gamma \sim \frac{PA}{m\bar{v}_{\rm gas}} \sim 2\pi \cdot 10^{-8} \,\mathrm{Hz} \cdot \left(\frac{P}{10^{-7} \,\mathrm{Pa}}\right) \left(\frac{1 \,\mathrm{g}}{m}\right)^{1/3} \cdot \left(\frac{0.1 \,\mathrm{g/cm}^3}{\rho}\right)^{2/3} \sqrt{\left(\frac{m_{\rm gas}}{4 \,\mathrm{Da}}\right) \left(\frac{10 \,\mathrm{mK}}{T}\right)}
$$

• Flux creep: movement of unpinned flux lines in type-II SC \rightarrow use type-I SC

• Eddy current damping in nearby conductors \rightarrow use only SCs and dielectrics

DPDM magnetic field signal

$$
BR \sim \oint \mathbf{B} \cdot d\ell = \iint \mathbf{J}_{\text{eff}} \cdot d\mathbf{A} \sim \varepsilon m_{A'}^2 R^2 A'
$$

Noise trade-off

• Imprecision and back-action noise determined by coupling η :

$$
S_{BB}^{\text{imp}} = \frac{2\rho S_{\phi\phi}}{3m^2\omega_0^2\eta^2|\chi(\omega)|^2} \qquad S_{BB}^{\text{back}} = \frac{2\rho\eta^2 S_{JJ}}{3m^2\omega_0^2}
$$

• Flux and current noise satisfy uncertainty relation $\sqrt{S_{\phi\phi}S_{JJ}} = \kappa \ge 1$

• Can define
$$
\tilde{\eta} = \eta \sqrt[4]{\frac{S_{JJ}}{S_{\phi\phi}}}
$$
, so that
\n
$$
S_{BB}^{\text{imp}} = \frac{2\rho\kappa}{3m^2\omega_0^2} \cdot \tilde{\eta}^{-2} |\chi(\omega)|^{-2} \qquad S_{BB}^{\text{back}} = \frac{2\rho\kappa}{3m^2\omega_0^2} \cdot \tilde{\eta}^2
$$

Noise trade-off (cont.)

• If
$$
S_{BB,\alpha\alpha}^{\text{th}} < \sqrt{S_{BB,\alpha\alpha}^{\text{imp}}(\omega=0)} \cdot S_{BB,\alpha\alpha}^{\text{back}}
$$
 [or $\tilde{\eta}^{\text{(res)}} \ge \tilde{\eta}^{\text{(broad)}}$], then either:

- Resonant detection: $\tilde{\eta}^{\text{(res)}} = \sqrt{\frac{4m\gamma T}{\kappa}}$
- Broadband detection: $\tilde{\eta}^{(broad)} = \sqrt{m}\omega_0$
- Otherwise, can choose any $\tilde{\eta}^{(res)} \geq \tilde{\eta} \geq \left[\tilde{\eta}^{(broad)} \right]^2 / \tilde{\eta}^{(res)}$
	- Larger $\tilde{\eta}$ is better for higher frequencies

Signal-to-noise ratio

• Coherent:

$$
SNR = \frac{B_{\rm DM}^2}{S_{BB}^{\rm tot}/t_{\rm int}}
$$

• Incoherent:

$$
\text{SNR} = \frac{B_{\text{DM}}^2}{S_{BB}^{\text{tot}}/t_{\text{coh}}} \cdot \sqrt{\frac{t_{\text{int}}}{t_{\text{coh}}}}
$$

• Multiple scans:

$$
\text{SNR}^2 = \sum_i \text{SNR}_i^2
$$

Bandwidth

• Bandwidth defined by:

$$
S_{BB}^{\text{tot}}\left(\omega_0 + \frac{\delta \omega}{2}\right) = 2S_{BB}^{\text{tot}}(\omega_0)
$$

• For resonant coupling,

$$
\delta\omega = \frac{4\sqrt{2}\gamma T}{\kappa\omega_0} \sim 2\pi \cdot 0.2 \,\mathrm{Hz} \left(\frac{\gamma}{2\pi \cdot 10^{-8}\,\mathrm{Hz}} \right) \cdot \left(\frac{T}{10 \,\mathrm{mK}} \right) \left(\frac{5}{\kappa} \right) \left(\frac{10 \,\mathrm{Hz}}{f_0} \right)
$$

• Total scan takes

$$
\sum_{i} t_{\text{int},i} = \frac{\kappa \pi}{2\sqrt{2}\gamma T v_{\text{DM}}^2} \Delta \omega \sim 1 \text{ yr} \left(\frac{\kappa}{5}\right) \left(\frac{2\pi \cdot 10^{-8} \text{ Hz}}{\gamma}\right) \cdot \left(\frac{10 \text{ mK}}{T}\right) \left(\frac{\Delta f}{74 \text{ Hz}}\right)
$$

Libration vs. Precession

Ferromagnet readout

Ferromagnet noise curves

