



# The Beehive Haloscope: A Strongly Coupled, Phase-Coherent Cavity Array for Axion Detection

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19th Patras Workshop on Axions, WIMPs, and  
WISPs

Patras, Greece

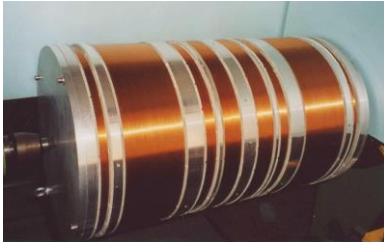
2024-09-16

[arXiv:2404.06627](https://arxiv.org/abs/2404.06627)

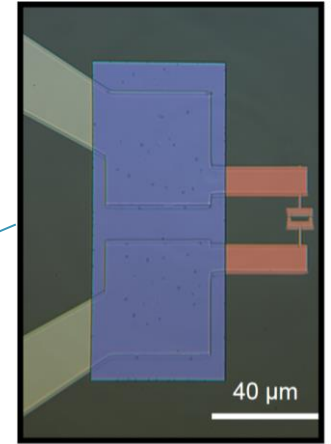
# Outline

- ADMX-VERA: Volume-Enhanced Haloscopes
- Beehive Haloscopes
- Progress on Working Prototype
- Future Plans

# High Frequency Haloscopes: Challenges and Opportunities

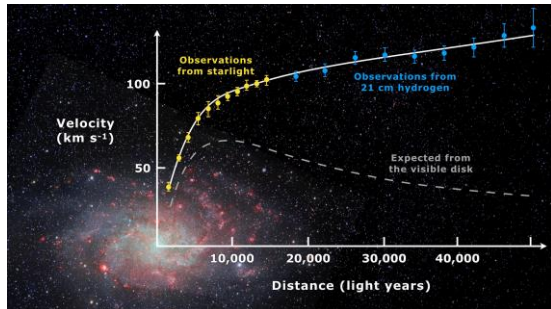


<https://s.mriquestions.com/superconductive-design.html>

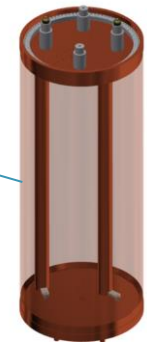


[https://indico.fnal.gov/event/10138/contributions/1020/attachments/551/642/eddins\\_axionWorkshopSlides\\_20150824pdf.pdf](https://indico.fnal.gov/event/10138/contributions/1020/attachments/551/642/eddins_axionWorkshopSlides_20150824pdf.pdf)

$$\frac{dv}{dt} \propto g_{\gamma}^4 \rho^2 \underbrace{B^4}_{\text{Magnet}} \underbrace{V^2 Q_L C^2}_{\text{Cavity}} \underbrace{T_{sys}^{-2}}_{\text{Detector}}$$

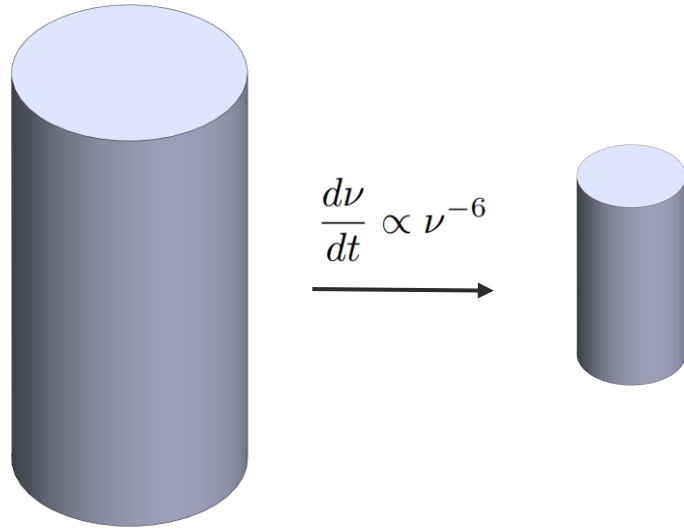


[https://en.wikipedia.org/wiki/Galaxy\\_rotation\\_curve](https://en.wikipedia.org/wiki/Galaxy_rotation_curve)

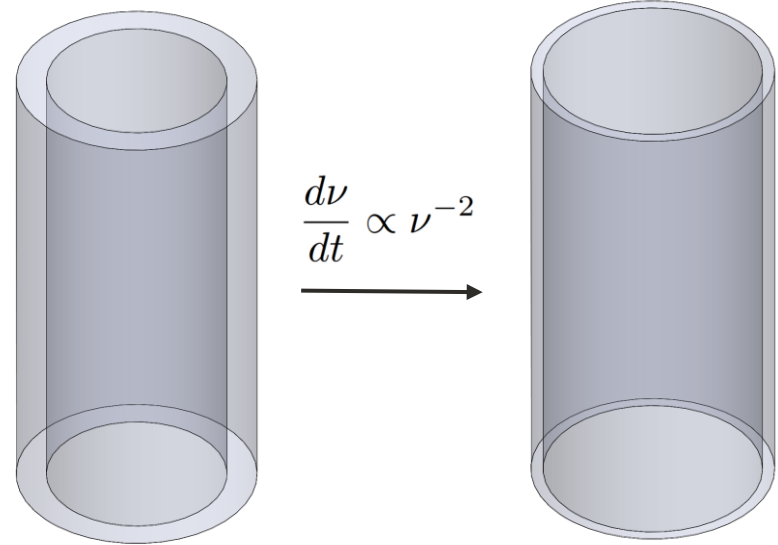


C. Boutan et al. (ADMX Collaboration) Phys. Rev. D 109, 012009

# ADMX-VERA: Solving the Scan Rate-Volume Scaling Problem

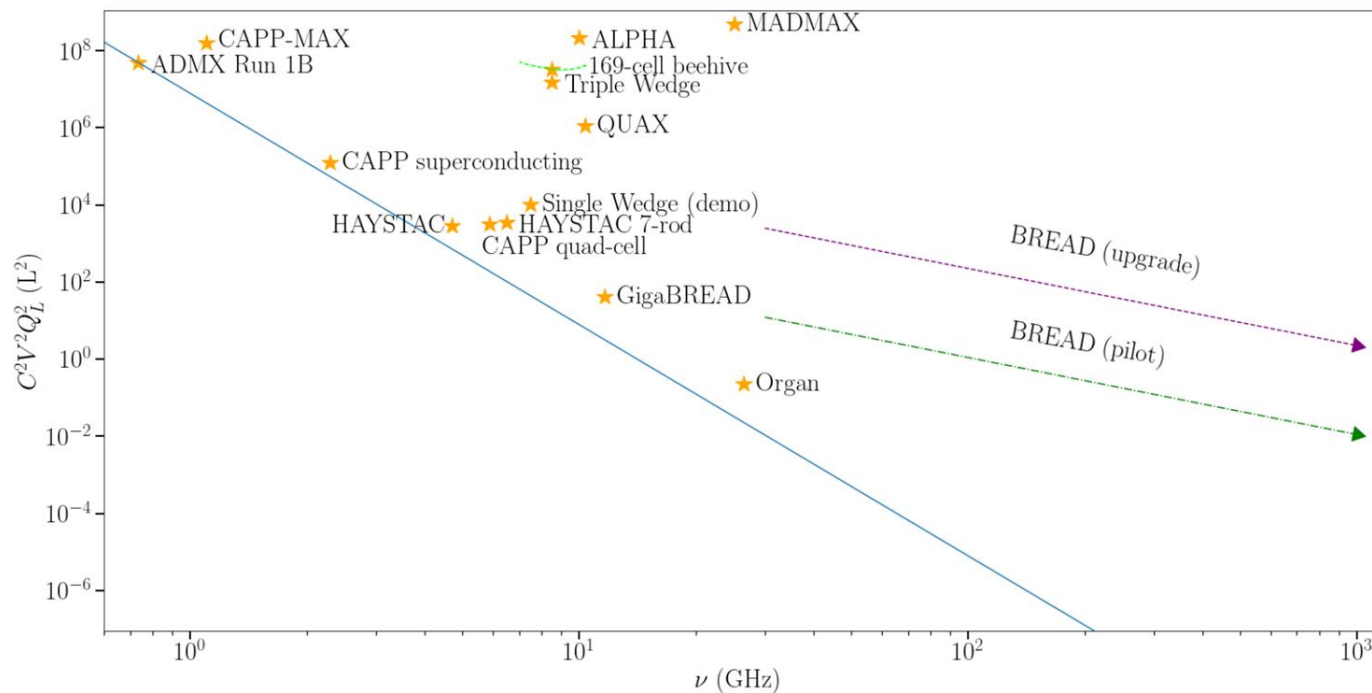


Traditional Haloscope  
Scale 3 Dimensions



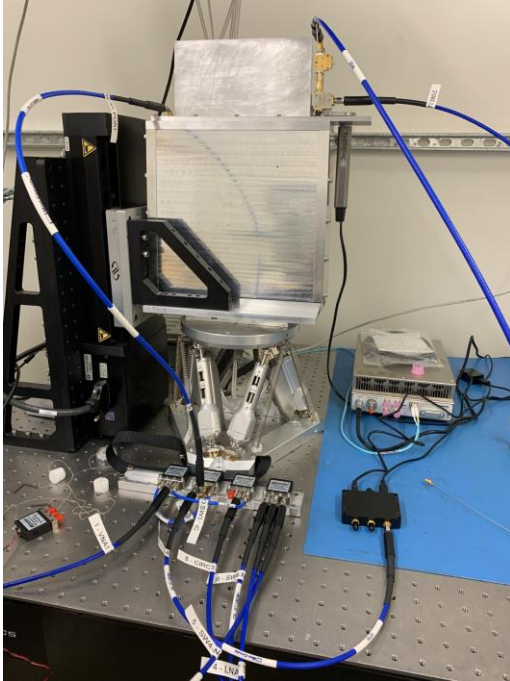
Thin-Shell Haloscope  
Scale 1 Dimension

# High Frequency Haloscopes: Challenges and Opportunities

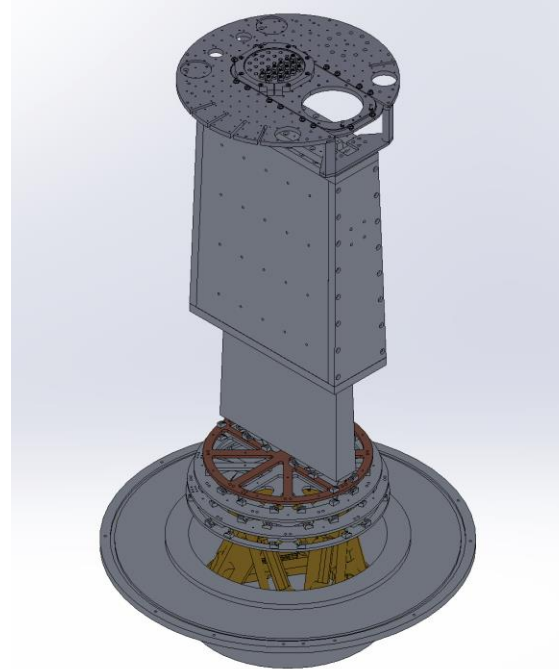


# ADMX-VERA: Current Prototypes

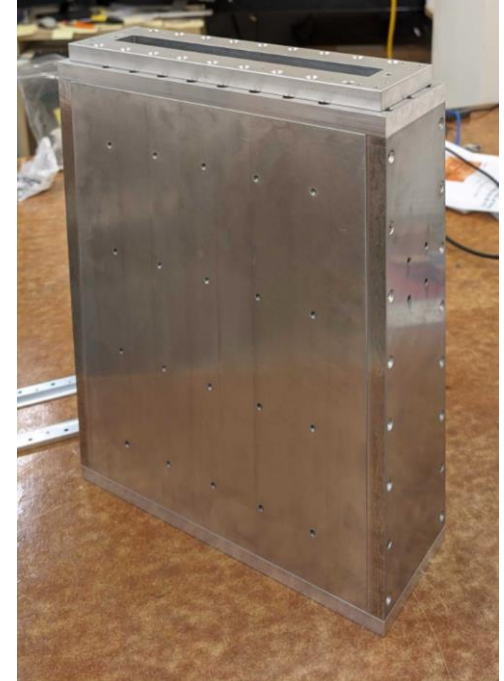
\* Includes work by T. Dyson, S. Ruppert, M. Salatino, and many summer students



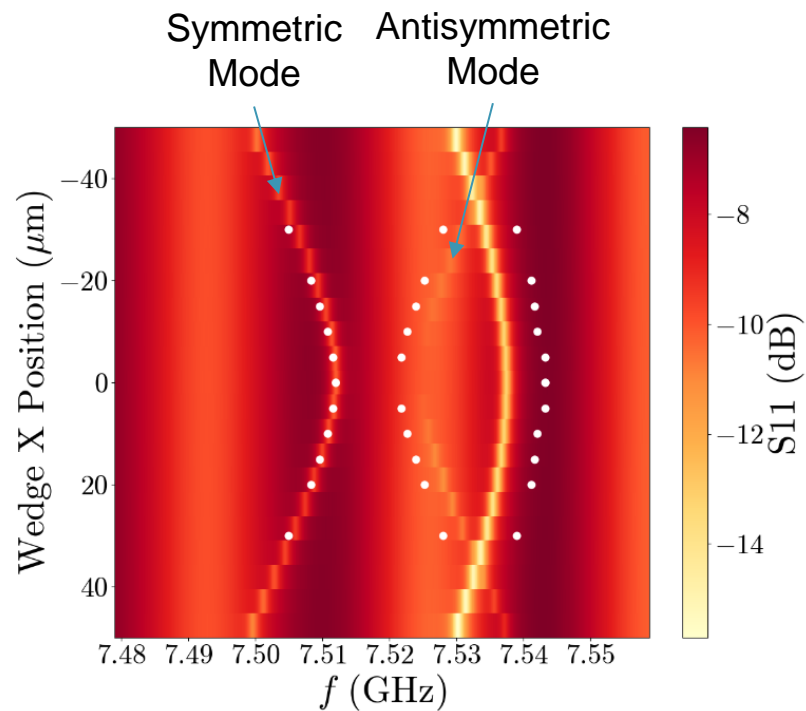
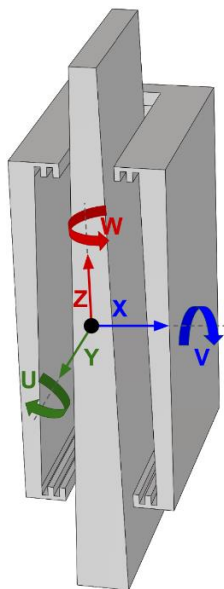
Warm “Single-Racetrack” Prototype



Cryogenic “Single-Racetrack”

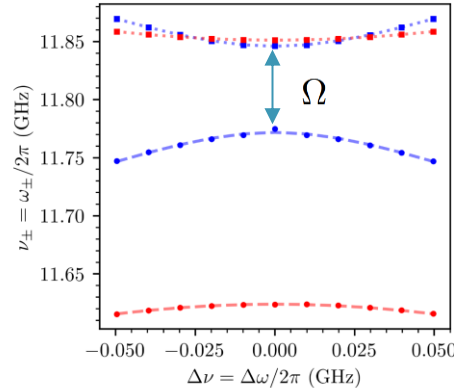
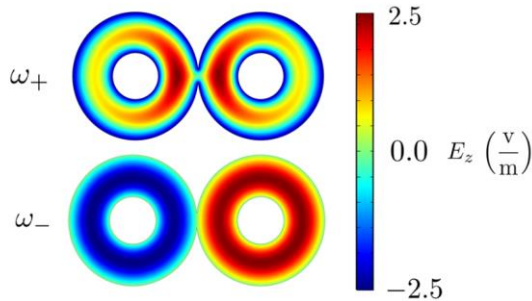
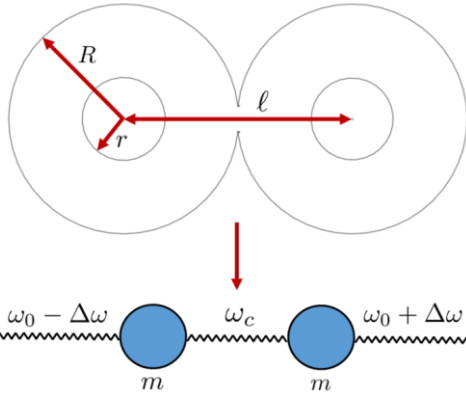


# Strong Coupling and Passive Coherence



Dyson T., et al. 2024 Phys. Rev. Applied 21, L041002

# Strong Coupling and Passive Coherence



Mode splitting depends on coupling:

$$\Omega \equiv \omega_- - \omega_+ \sim \frac{\omega_c^2}{\omega_0}$$

Form factor high when  $\Delta\omega < \Omega$ :

$$C_p = \frac{(1 + \sqrt{1 + \zeta^2} - \zeta)^2}{2[1 + (\sqrt{1 + \zeta^2} - \zeta)^2]}$$

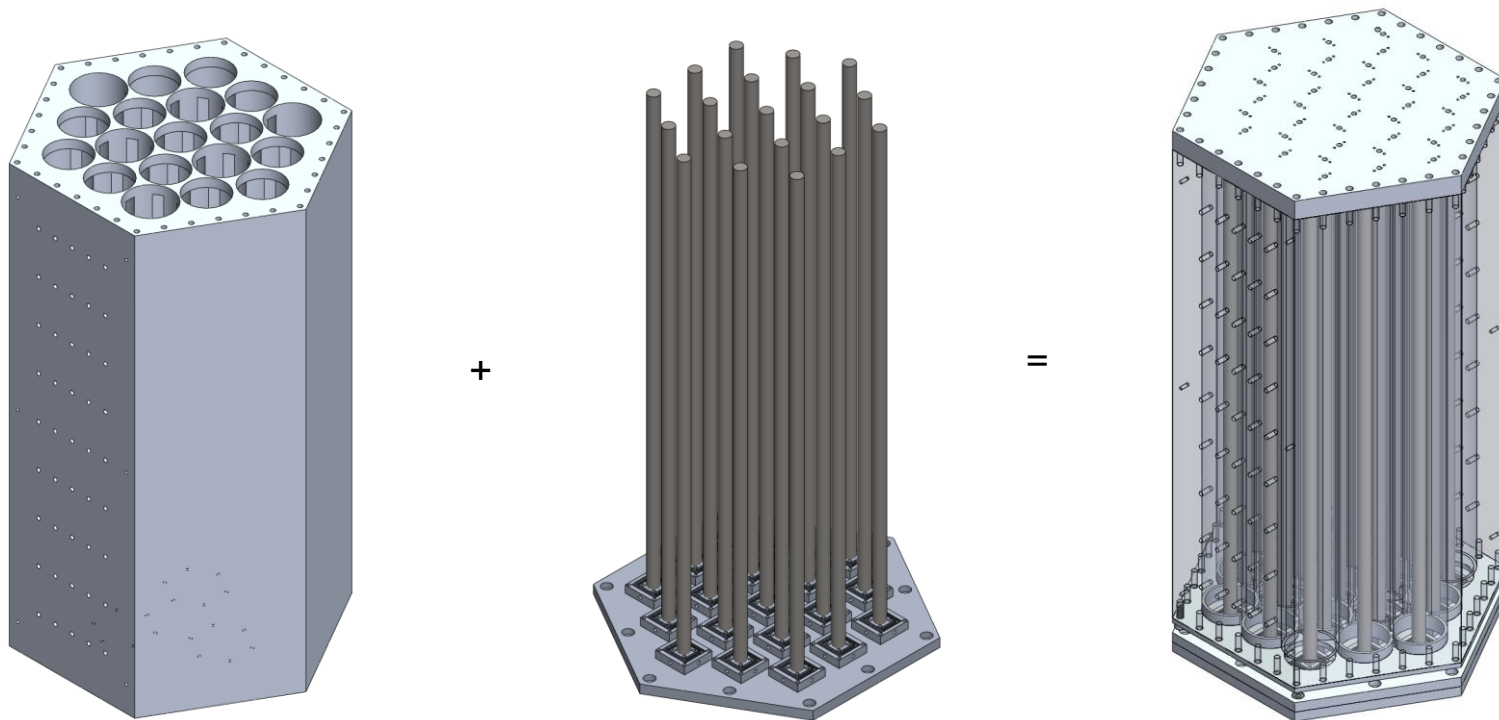
$$\zeta \equiv 2\omega_0 \frac{\Delta\omega}{\omega_c^2} \sim \frac{2\Delta\omega}{\Omega}$$

**Conclusion: Line width criterion replaced by mode splitting criterion**

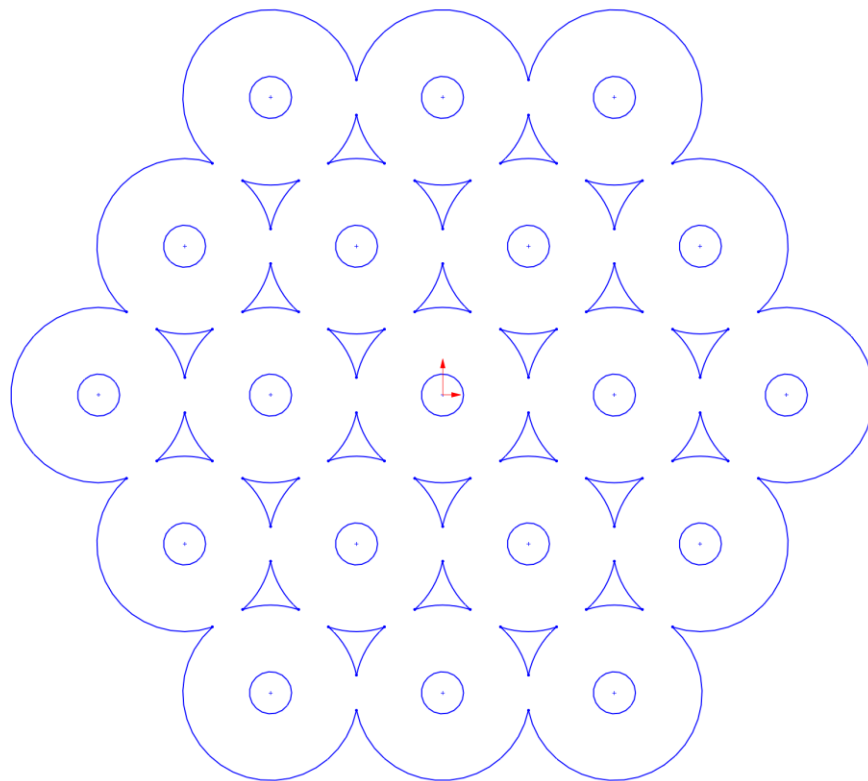
$$\Delta\omega < \frac{\omega_0}{Q} \longrightarrow \Delta\omega < \Omega \sim \frac{\omega_c^2}{\omega_0}$$



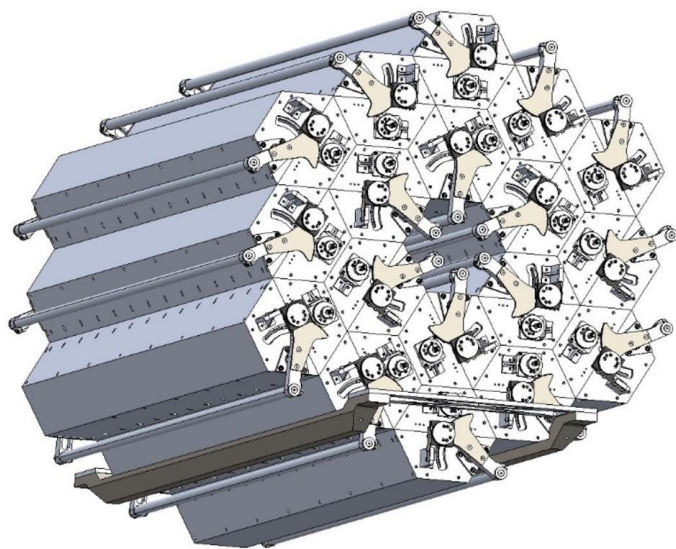
# Maximizing Passive Coherence: Beehive Geometry



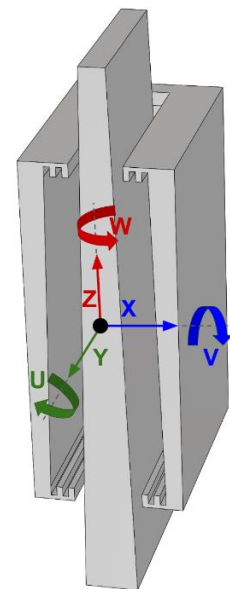
# Maximizing Passive Coherence: Beehive Geometry



# Beehive: Combining Cavity Arrays and Thin Shell Haloscopes



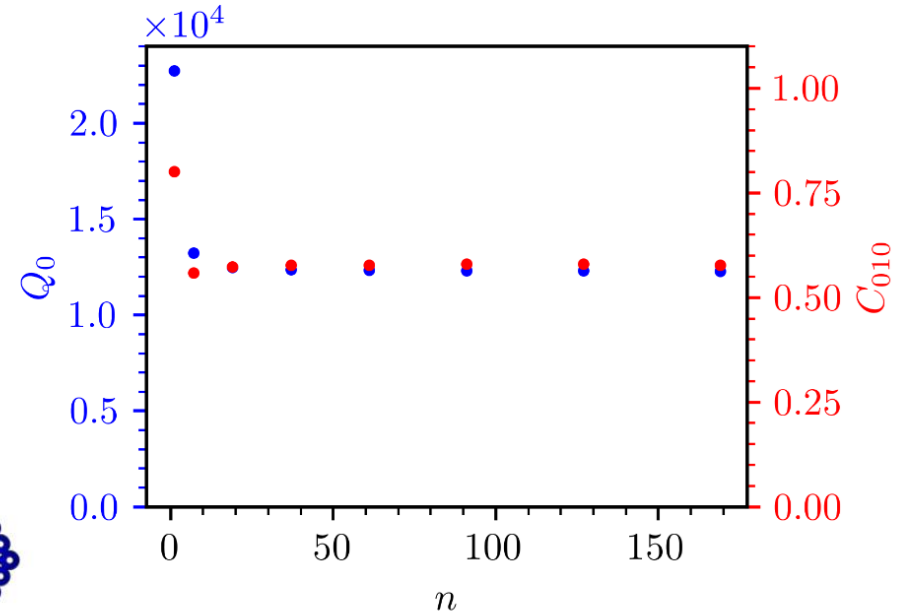
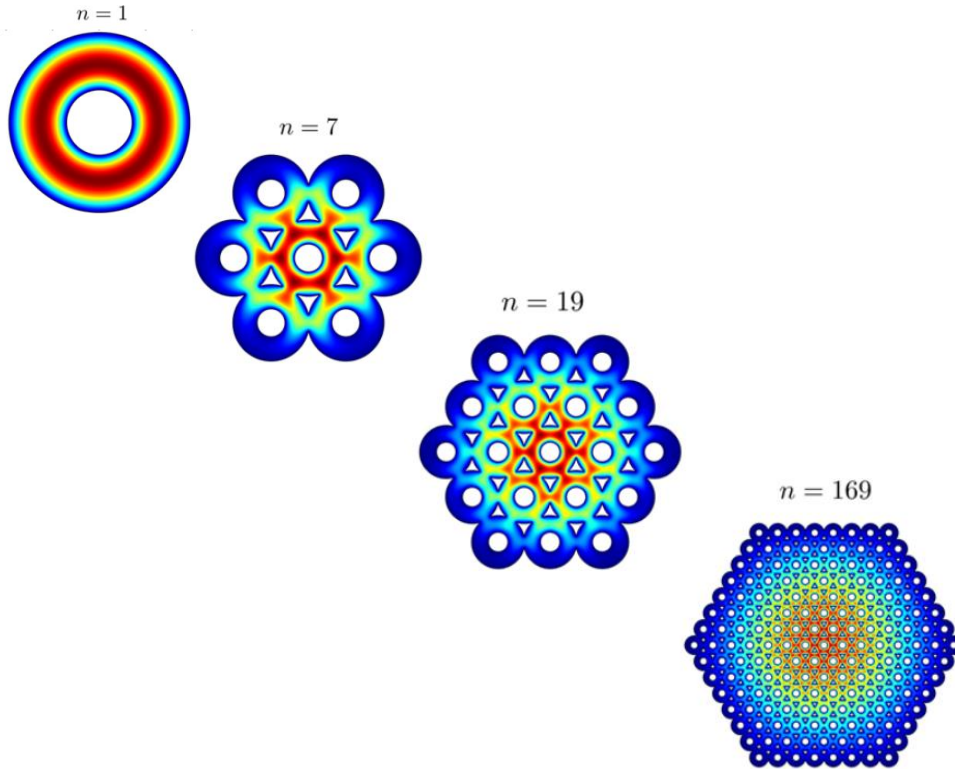
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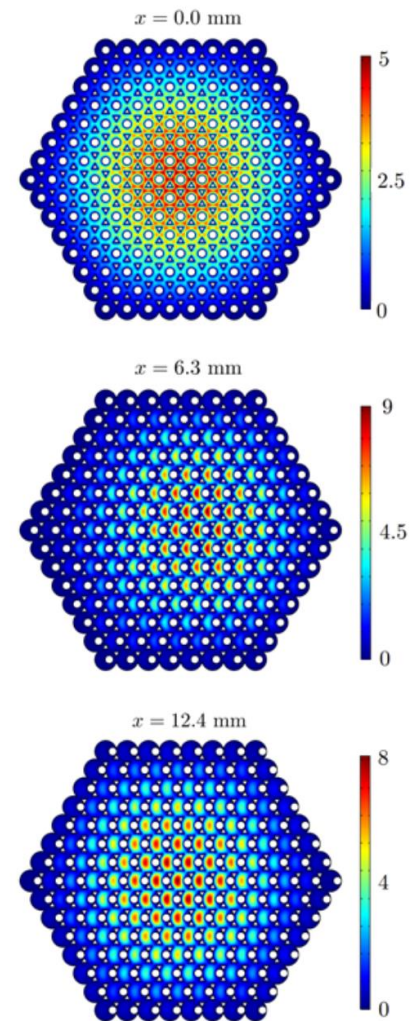
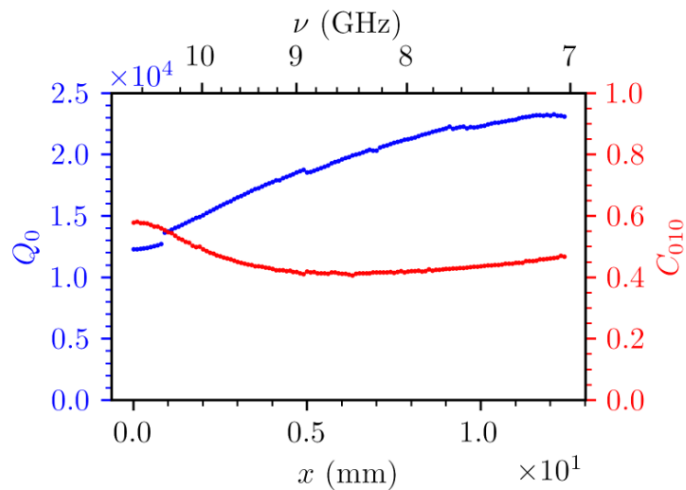
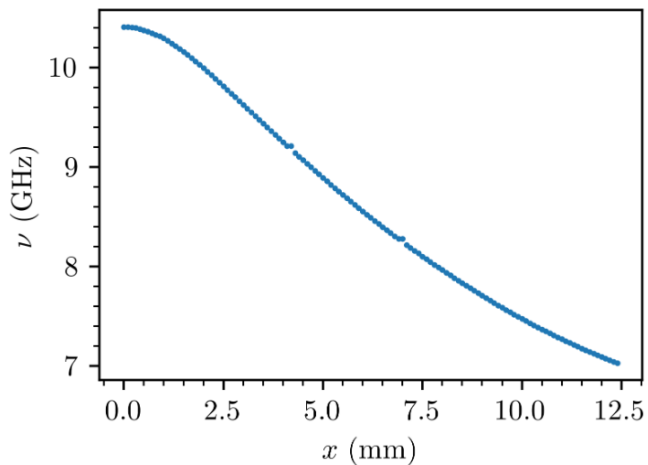
ADMX Collaboration. 2023.  
arXiv:2203.14923v3

Dyson T., et al. 2024 Phys. Rev.  
Applied 21, L041002

# Beehive Features: Scalability

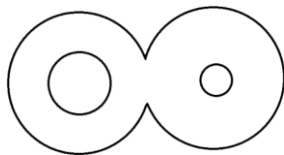
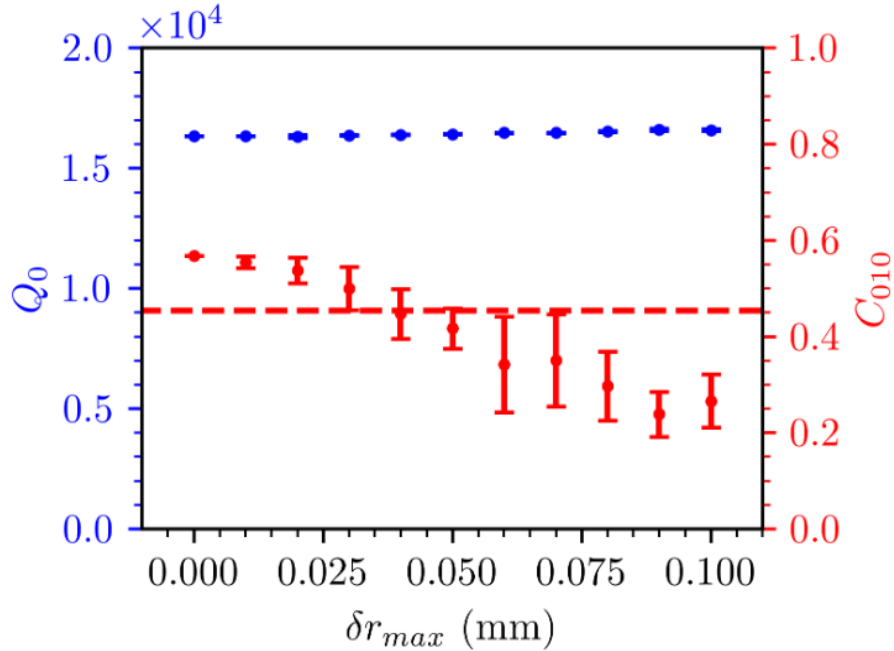


# Beehive Features: Tunability

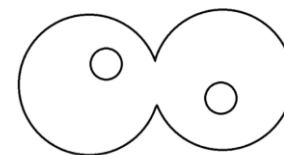
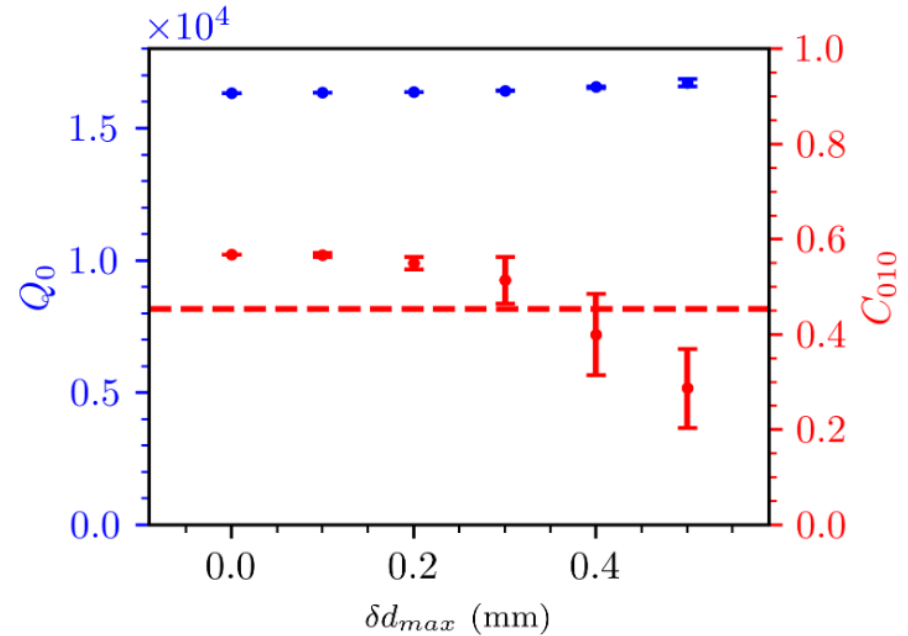


# Beehive Features: Resilience

Machining Tolerance Example:  
Rod Radius Variation

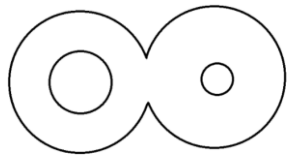
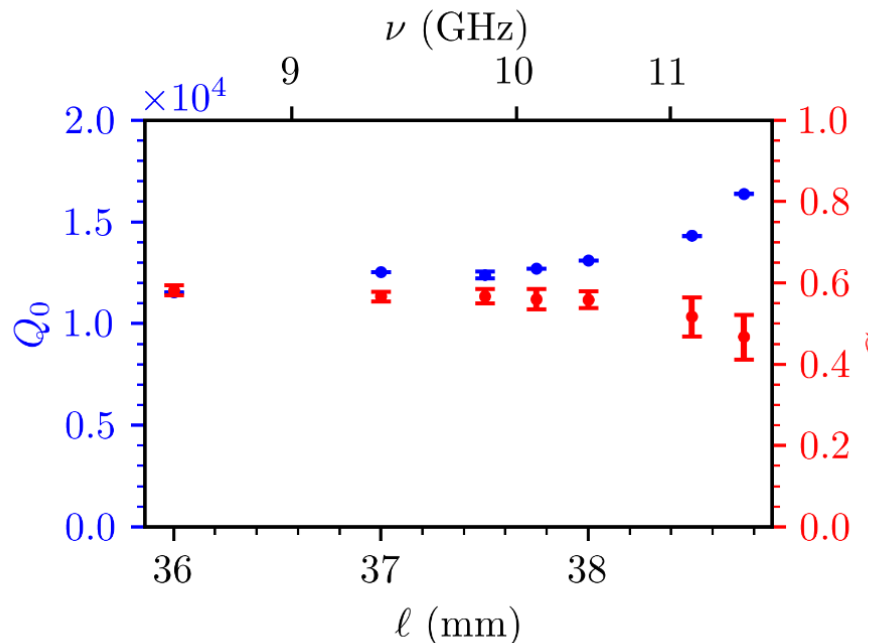


Assembly Tolerance Example:  
Rod Position Variation

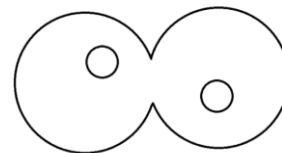
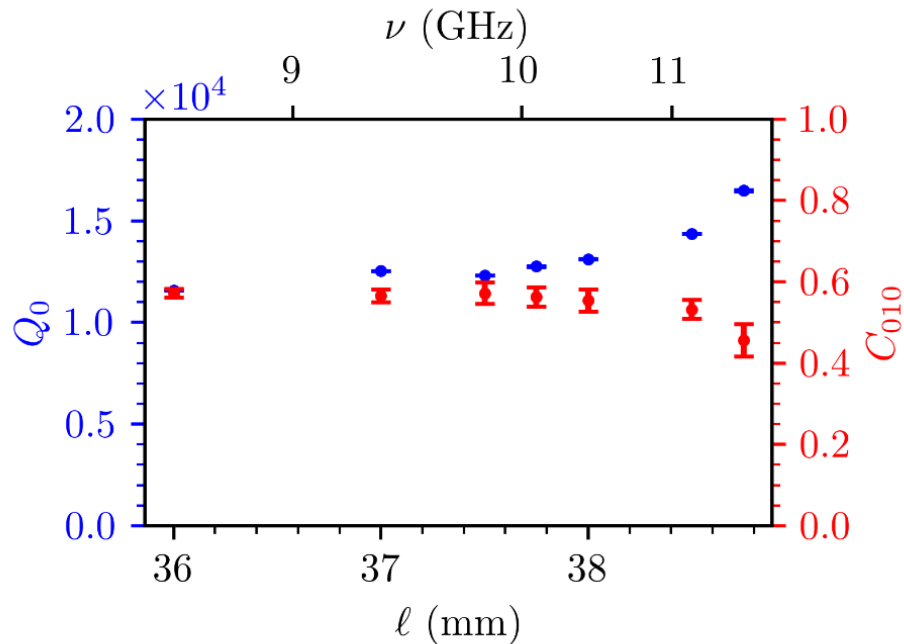


# Beehive Features: Resilience

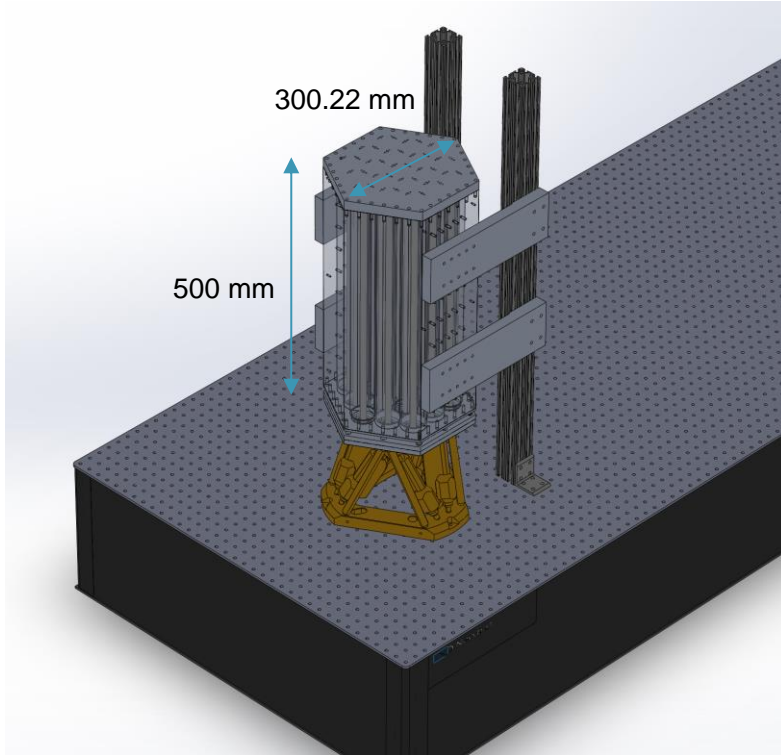
Machining Tolerance Example:  
Rod Radius Variation



Assembly Tolerance Example:  
Rod Position Variation



# Production Model



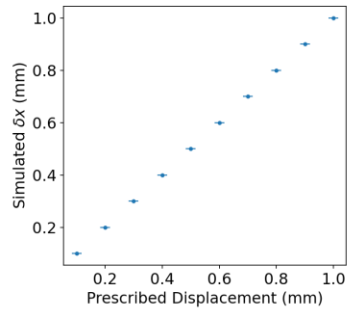
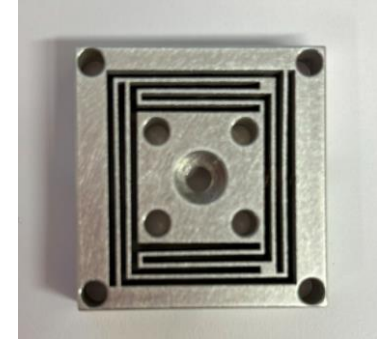
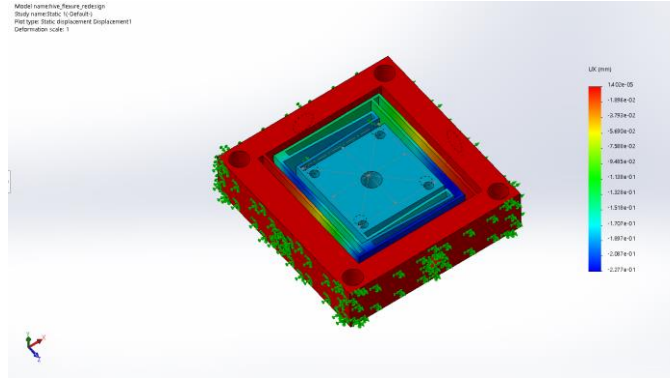
Quick Statistics:

Parameter	Value
Tuning Range (GHz)	5-7 GHz
Q (center of tuning range; Cu at cryogenic temp.)	24,897
C (center of tuning range)	0.34
V (L)	16.73 (19 cells)

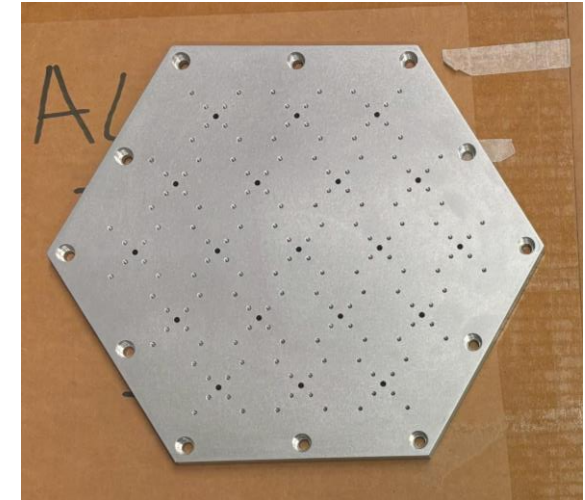
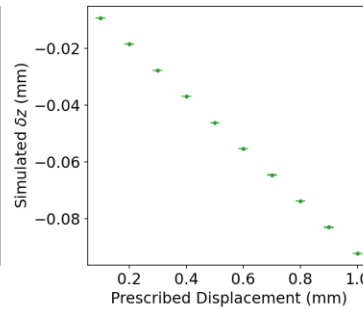
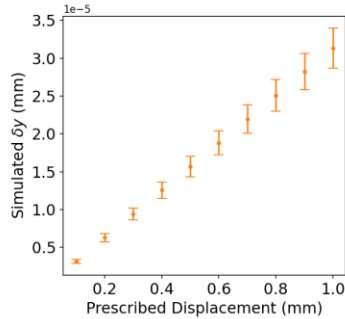


# Improving Form Factor: Precise Rod Alignment

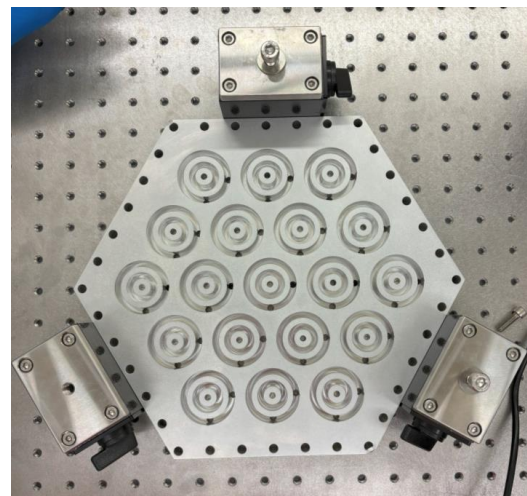
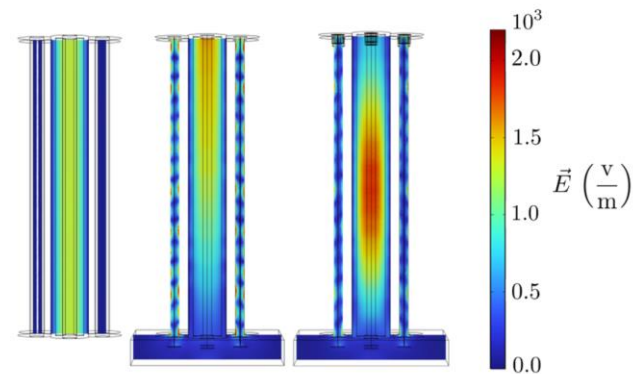
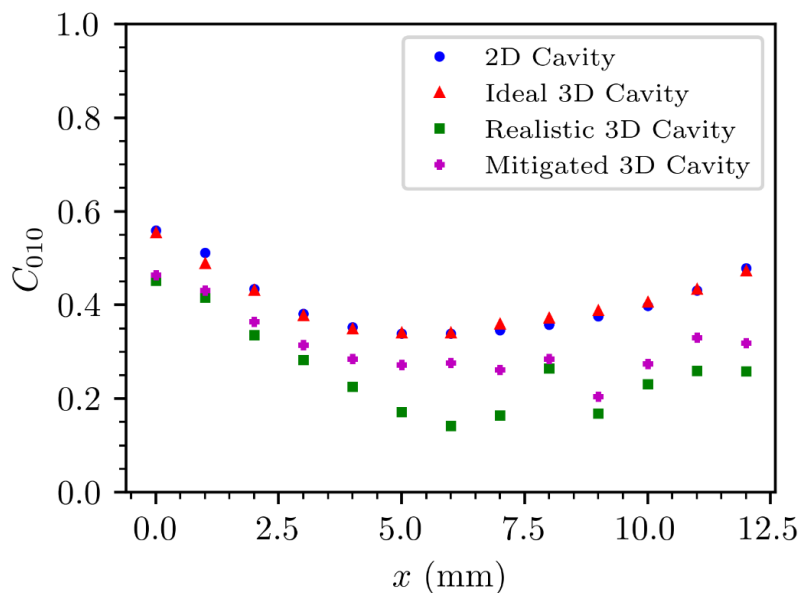
\* Building on and in conjunction with work by Sephora Ruppert (Stanford graduate student)



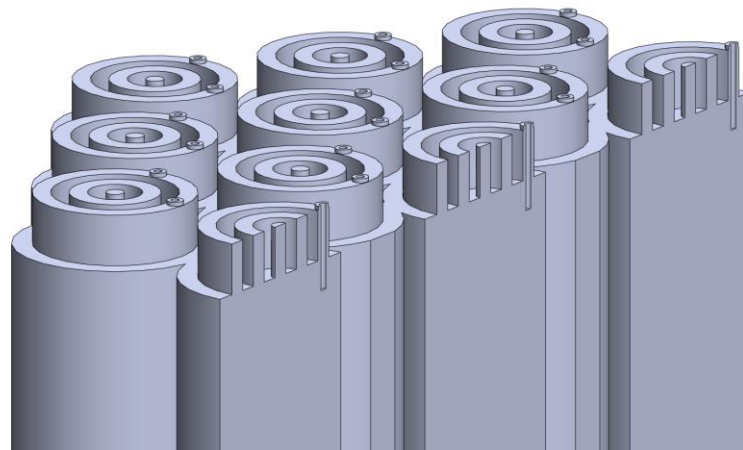
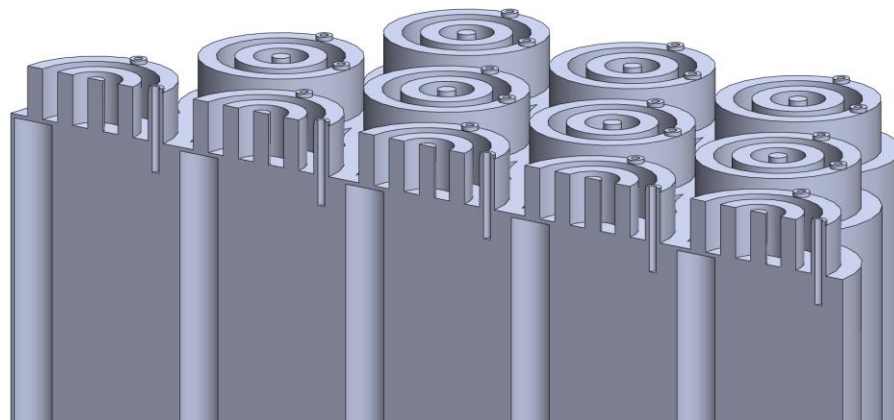
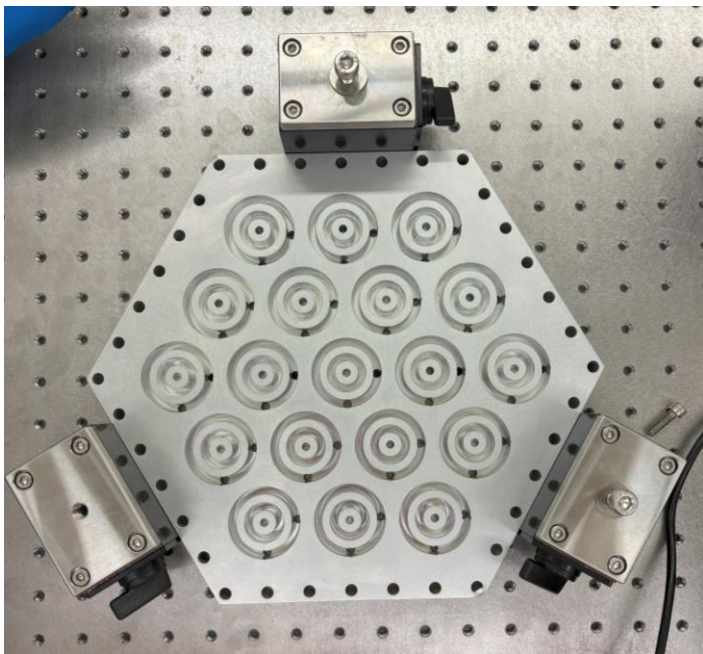
x-Displacement; Design 0



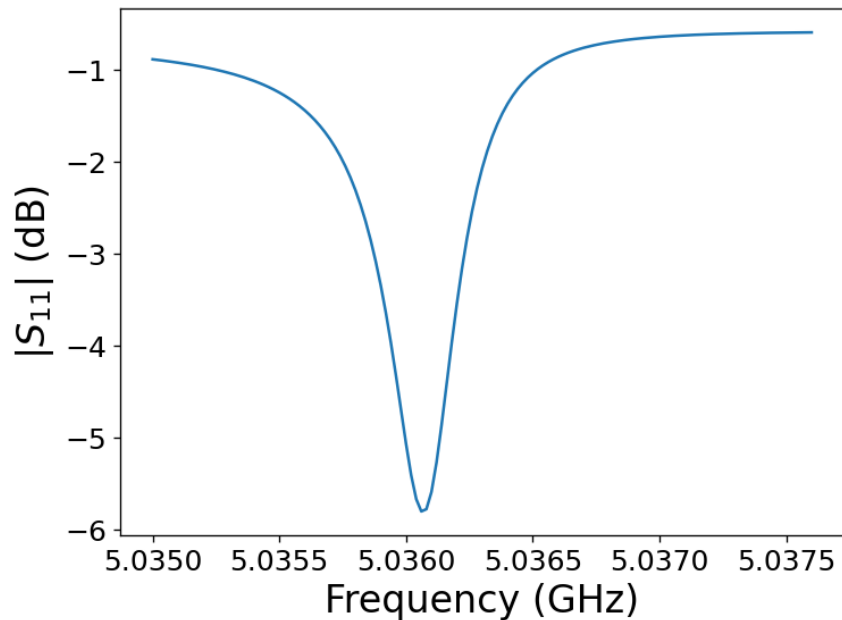
# Improving Form Factor: Mode Shaping with Corrugations



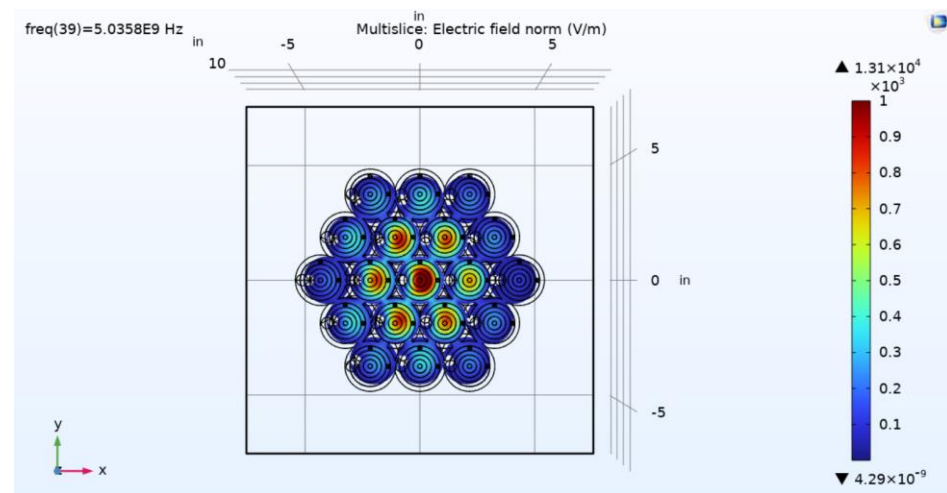
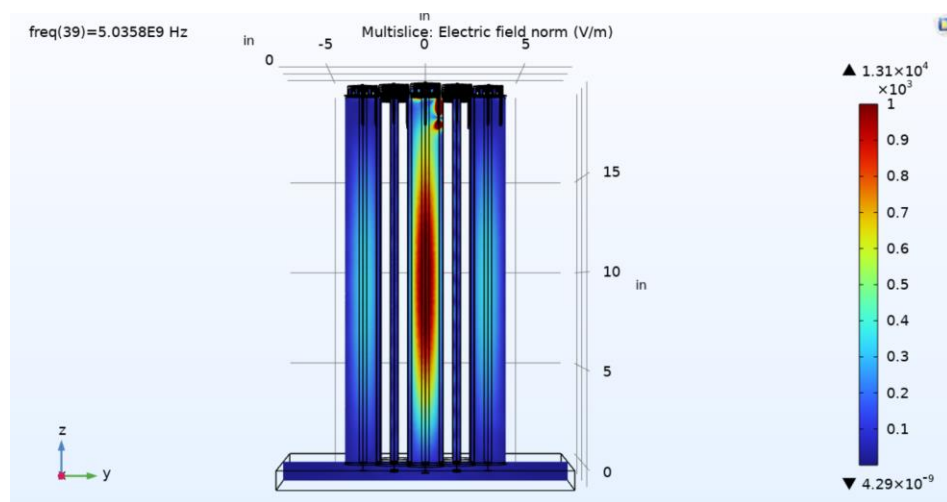
# Coupling Scheme



# Simulating Coupling: $S_{11}$



$$Q_0 = 26372$$
$$Q_L = 13252$$
$$\beta = 0.9899$$

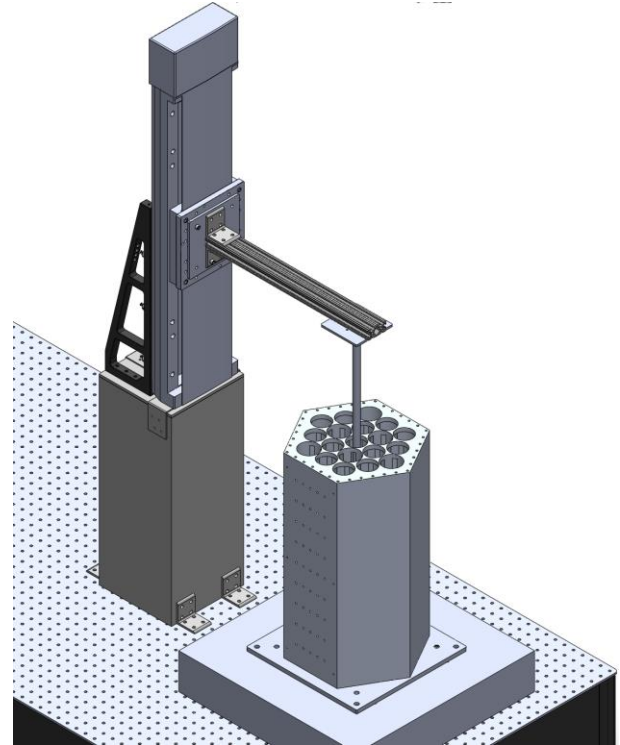


# Metrology Plan



<https://hexagon.com/products/absolute-arm-compact>

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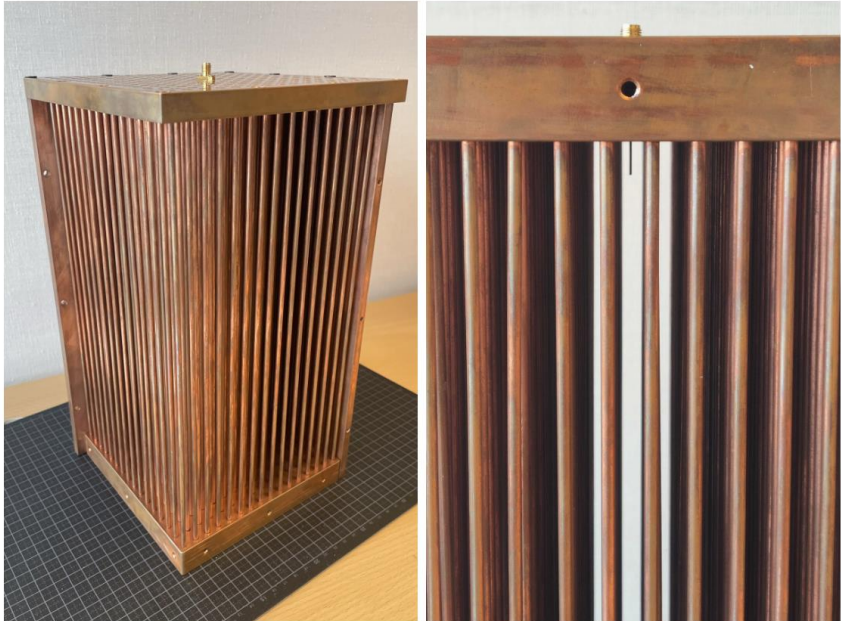
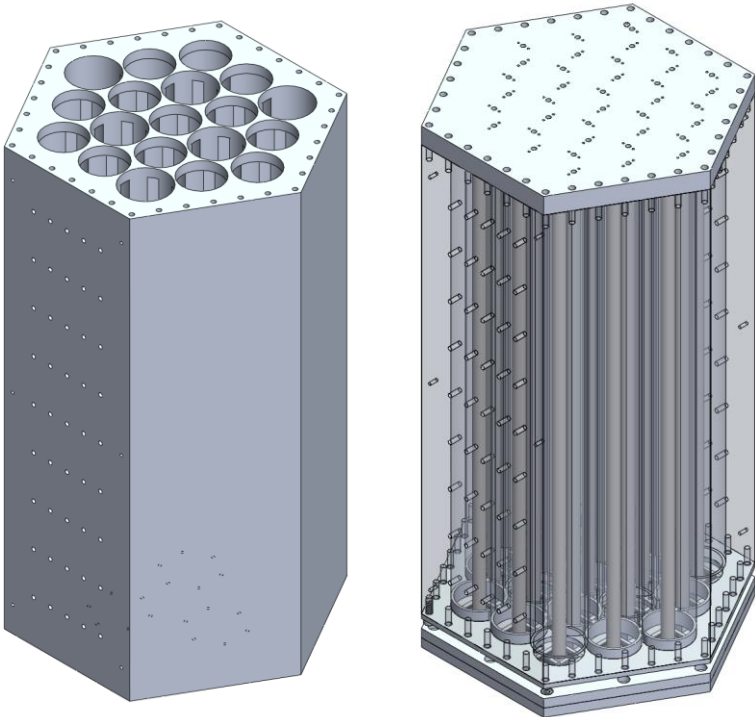
# Future Experiment Plans

- Shell machining under consultation
- Assembly and metrology of shell and tuning mechanism
- Cavity parameter measurements:
  - Quality factor
  - Electric field maps
  - Mode maps
- Dark photon exclusion limit run

# Backup Slides



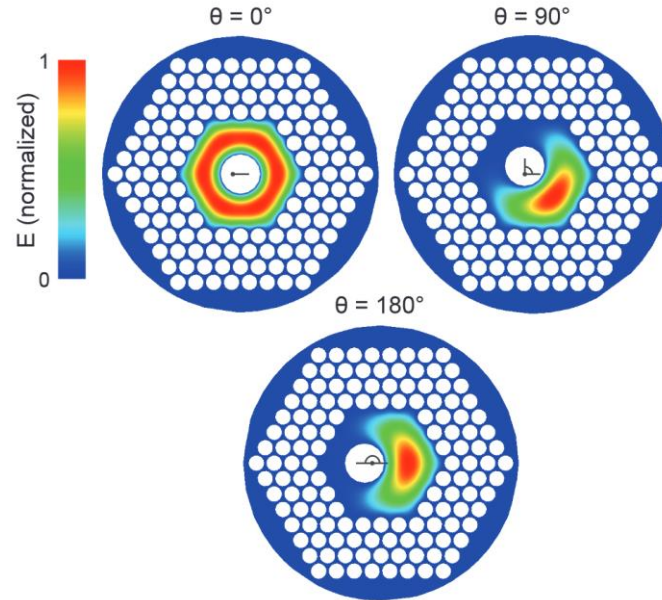
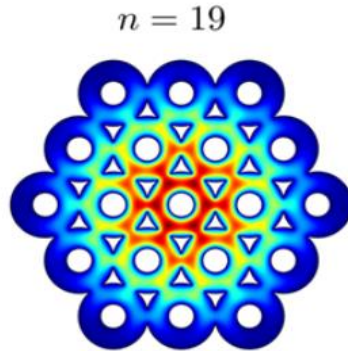
# Beehive vs. Plasma Haloscopes



Alpha Collaboration. 2023. <https://arxiv.org/pdf/2210.00017>

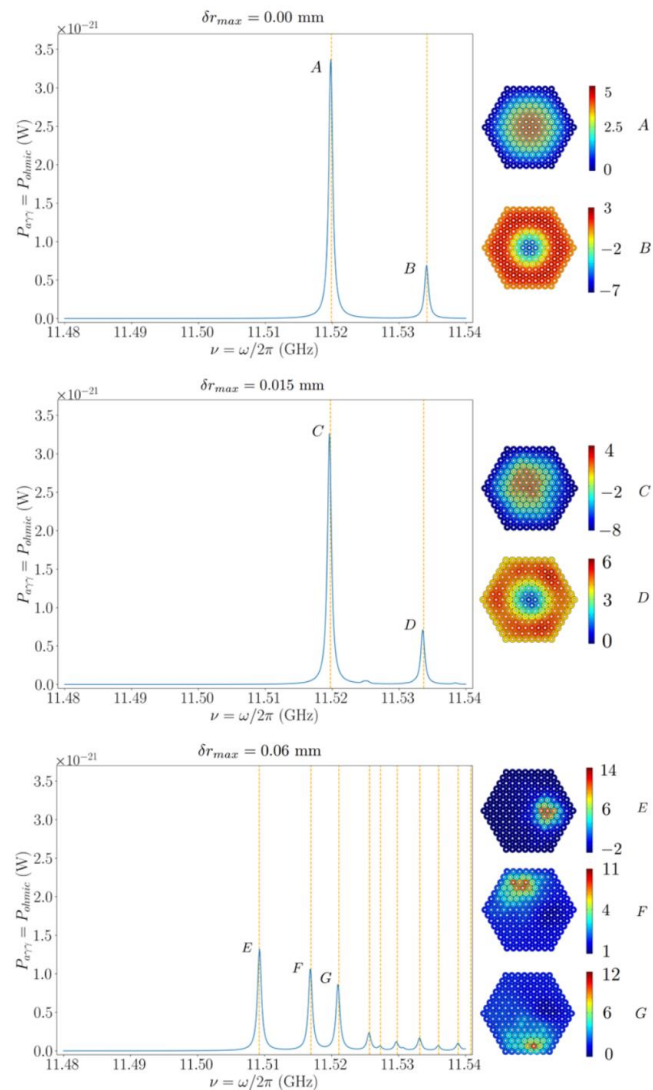
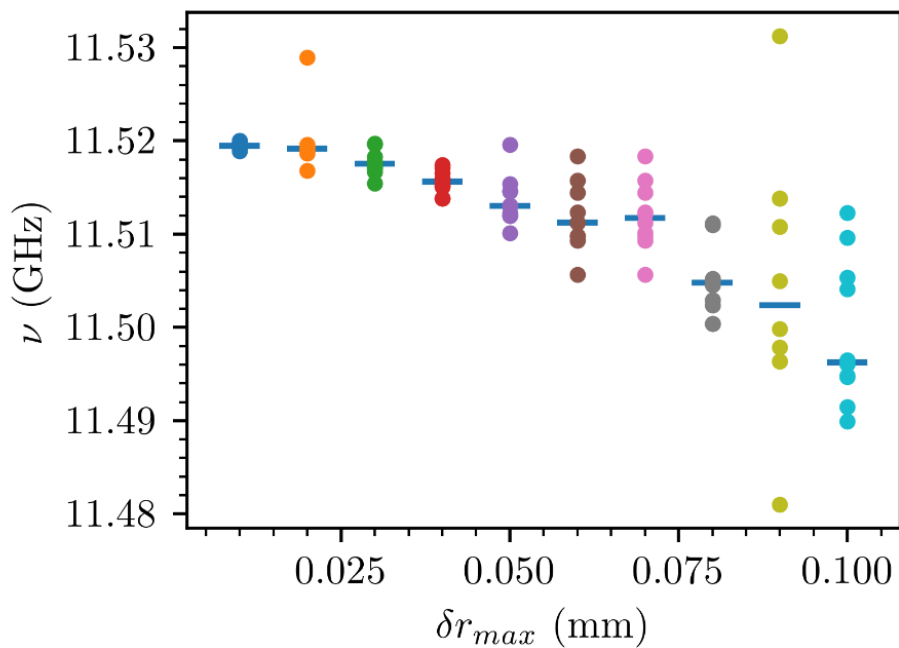


# Beehive vs. Photonic Band Gap Haloscopes

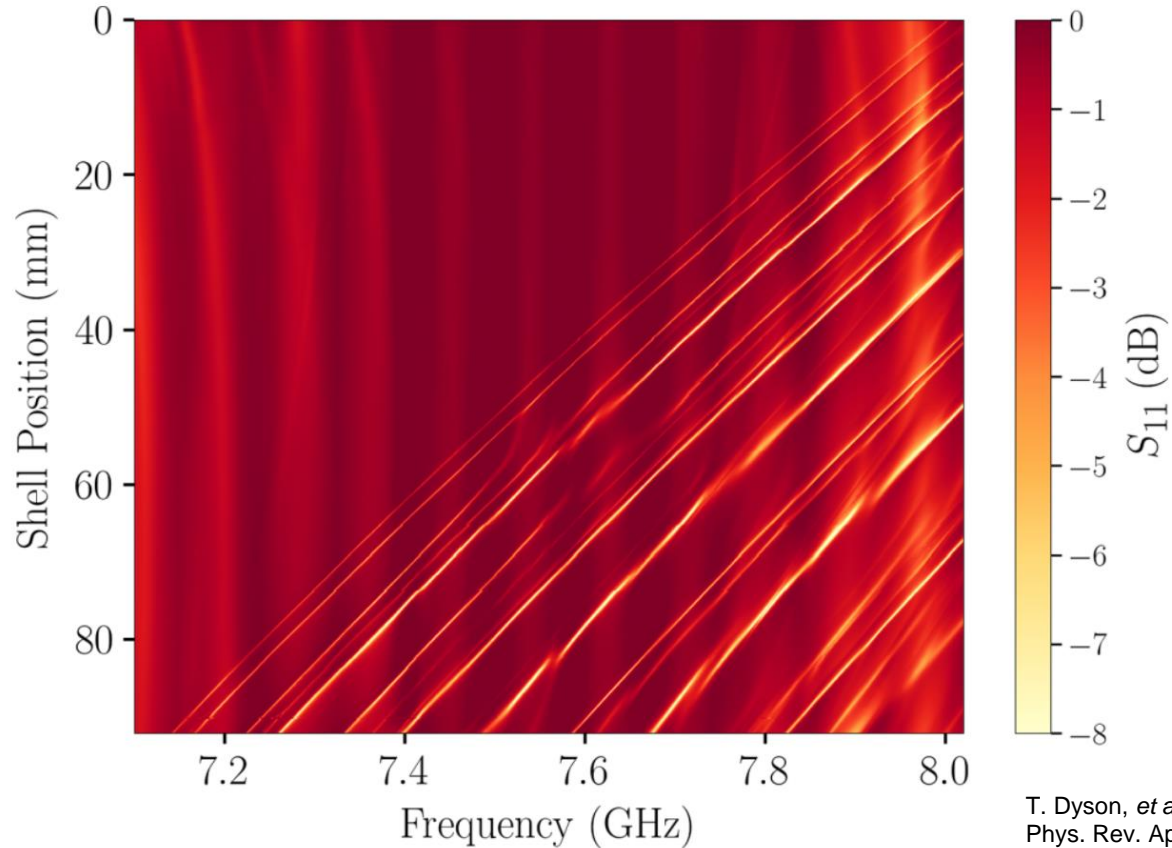


S. M. Lewis, *et al.* 2024. <https://arxiv.org/pdf/2408.03861v1>

# Cavity Decoherence



# Thin-Shell Mode Map



T. Dyson, *et al.*  
Phys. Rev. Applied 21, [L041002](#)