

# UHFGW @ Supax

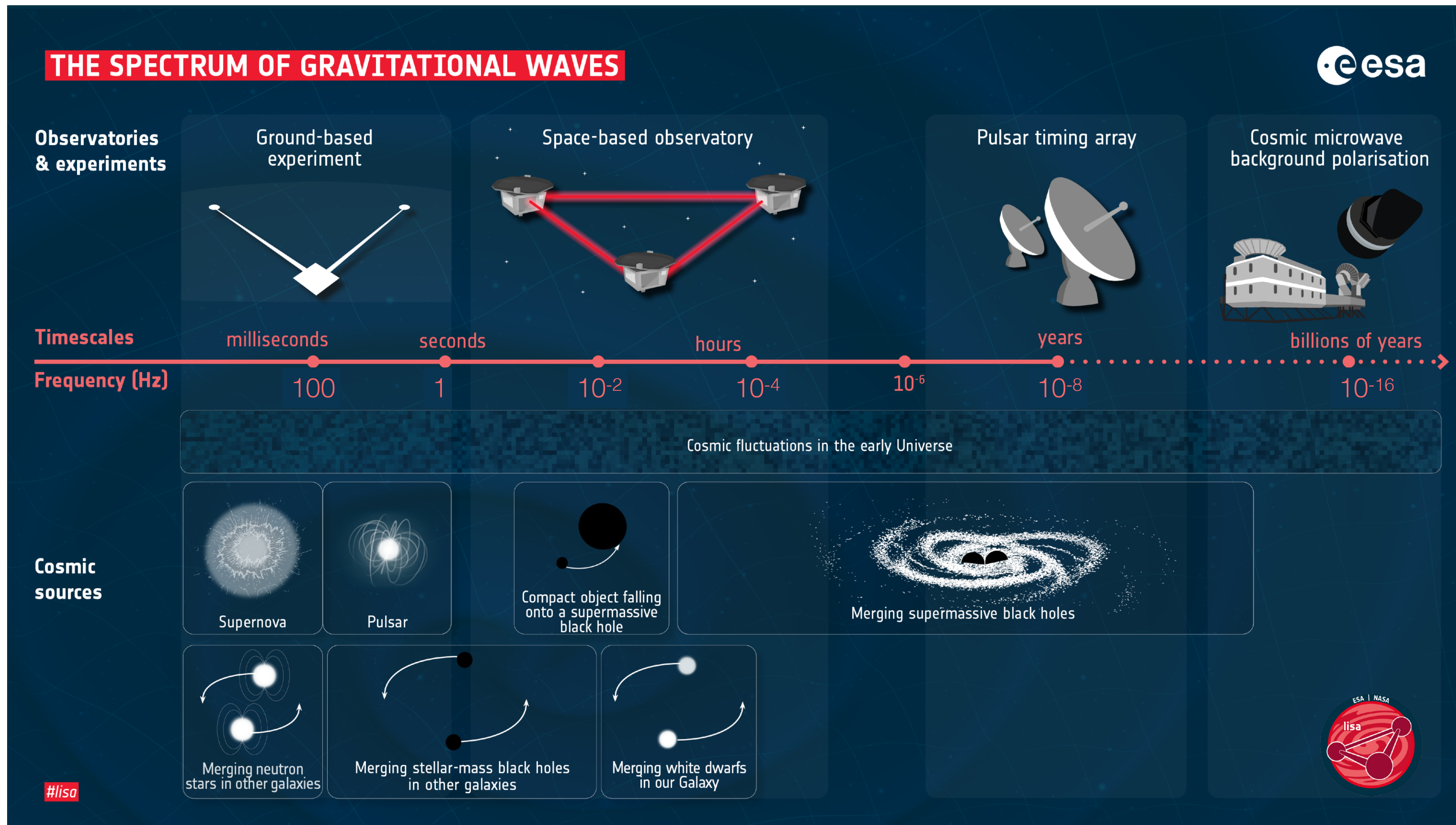
Cosmic Whipers WG4, 05/03/2024

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\*: University of Mainz, \*\*: University of Bonn

SUPA<sup>0</sup>X  
a RADES  
experiment



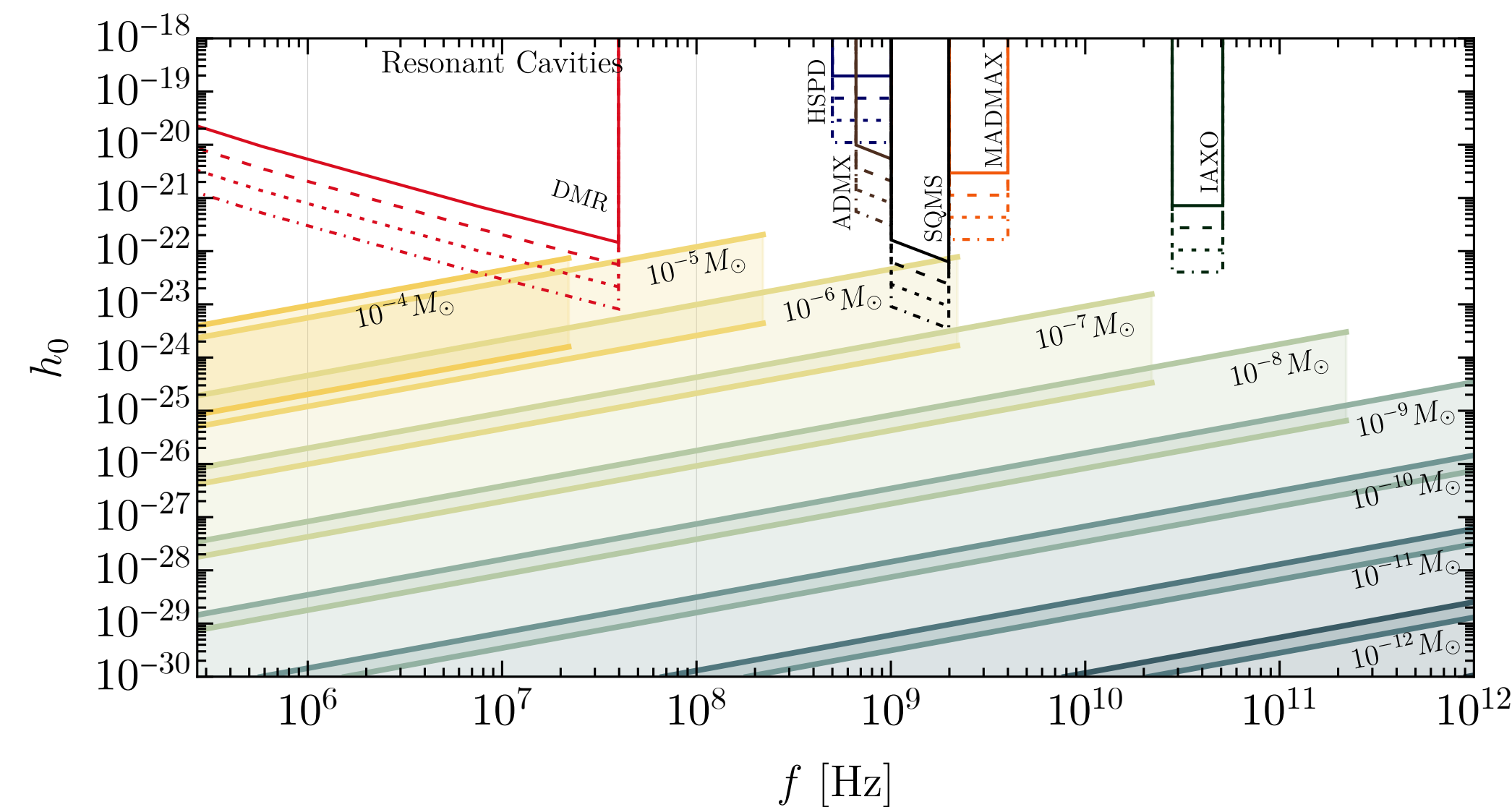


[ <https://www.esa.int/> ]

# High Frequency Gravitational Waves Sources

• Several well motivated beyond the standard model sources:

- Primordial black hole mergers
  - Chirp signals
- GW from boson clouds around BHs
  - **BH super radiance**
  - Monochromatic over long timescales

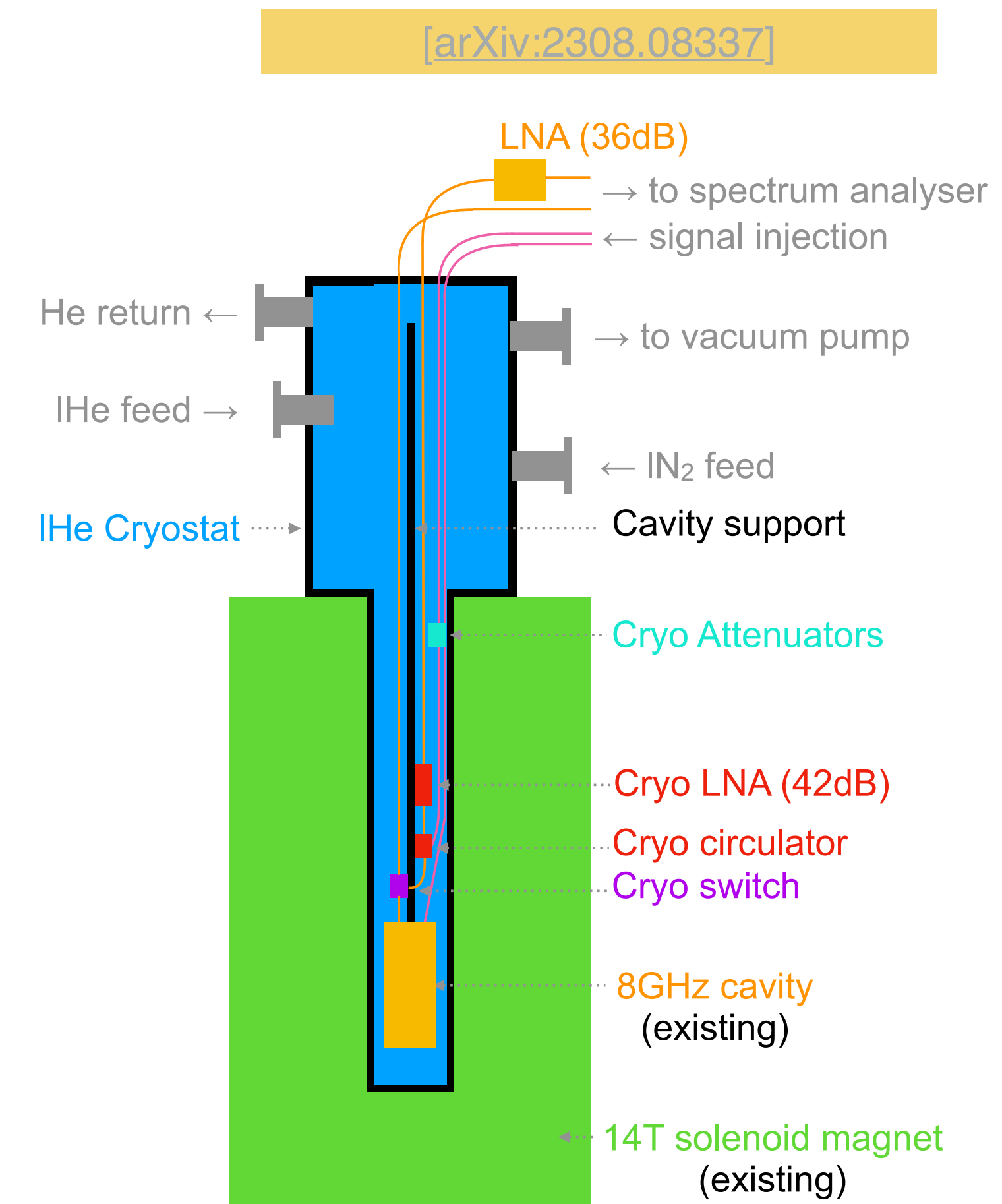


[Gabriele Franciolini, Anshuman Maharana, Francesco Muia; arXiv:2205.02153v1]

• Displayed expected experimental sensitivities for PBHs:

- Assuming GW signal long enough to ring up cavity
- E.g.: given for ADMX, SQMS @  $m_{PBH} \approx 10^{-10} M_{\odot}$

- **Supax:** superconducting axion (now GW) search @ Mainz
  - First results on dark photons (~commissioning) [[arXiv:2308.08337](https://arxiv.org/abs/2308.08337)]
- **Goals:**
  - Study of new **SC materials** for resonant cavity experiments
    - Brand new results on NbN
  - Study of **cavity geometries** optimised for **GW** searches
    - Together with Mainz theory section (P. Schwaller)



# What we do at Mainz: Typical setup

[arXiv:2308.08337]

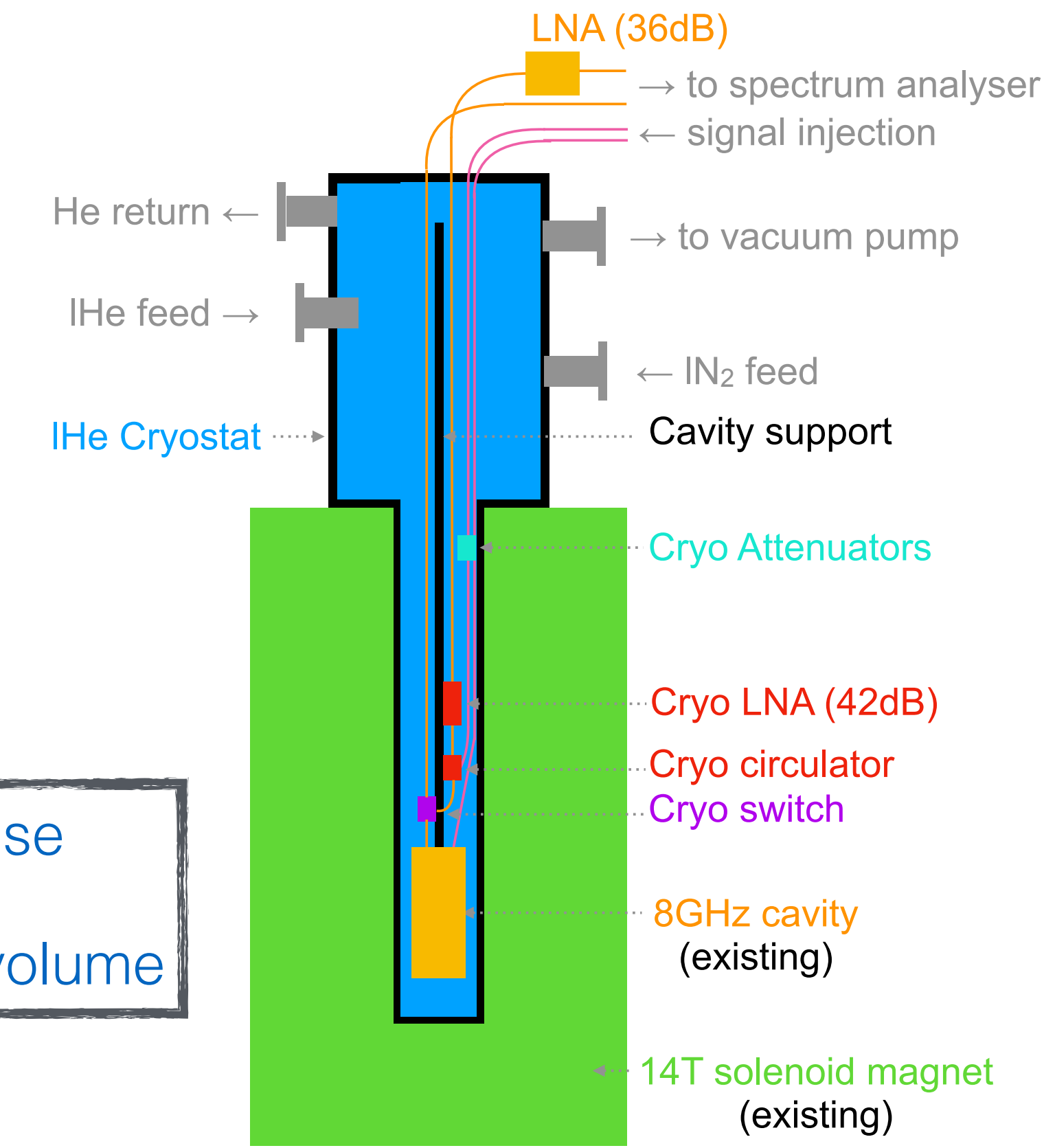
Metamaterials

Geometries

$$P_{sig} = \frac{1}{2} Q \omega_g^3 V^{5/3} (\eta_n h_0 B_0)^2 \frac{1}{\mu_0 c^2}$$

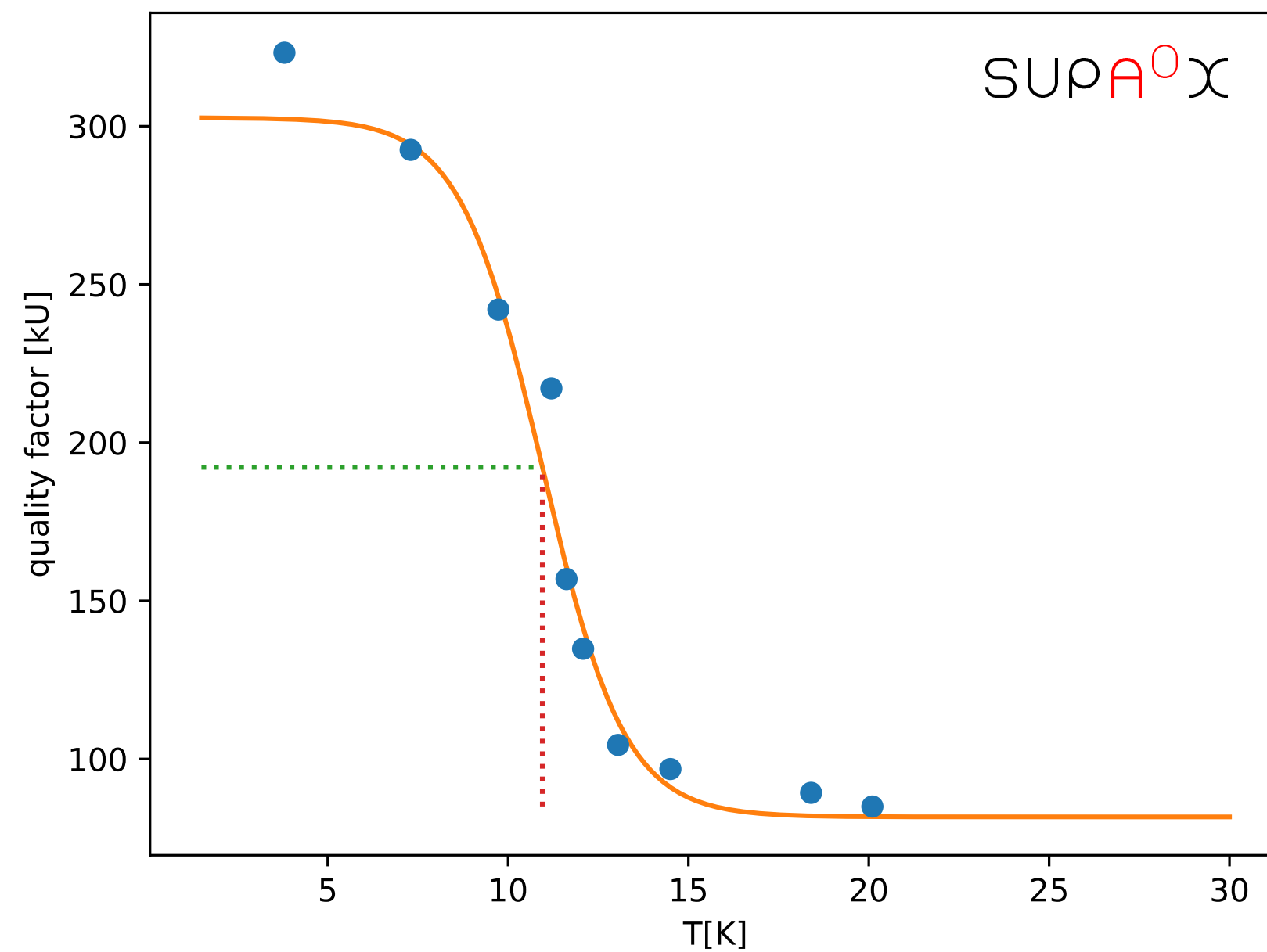
- Depends on cavity material:
  - High purity copper:  $\sim 5 \cdot 10^4$
- Superconducting: difficult in high magnetic field!
  - Target:  $10^6$
  - Achieved:  $3 \cdot 10^5$  (non tunable)
    - HTS [arXiv: 2002.08769](https://arxiv.org/abs/2002.08769)
    - Di-electric [arXiv: 2208.12670](https://arxiv.org/abs/2208.12670)
  - Materials under study: Nb<sub>3</sub>Sn, HTS materials (YBCO)
  - New: **NbN**

- Up to 14T magnets in use
  - Up to 20T envisioned
  - Larger fields - smaller volume



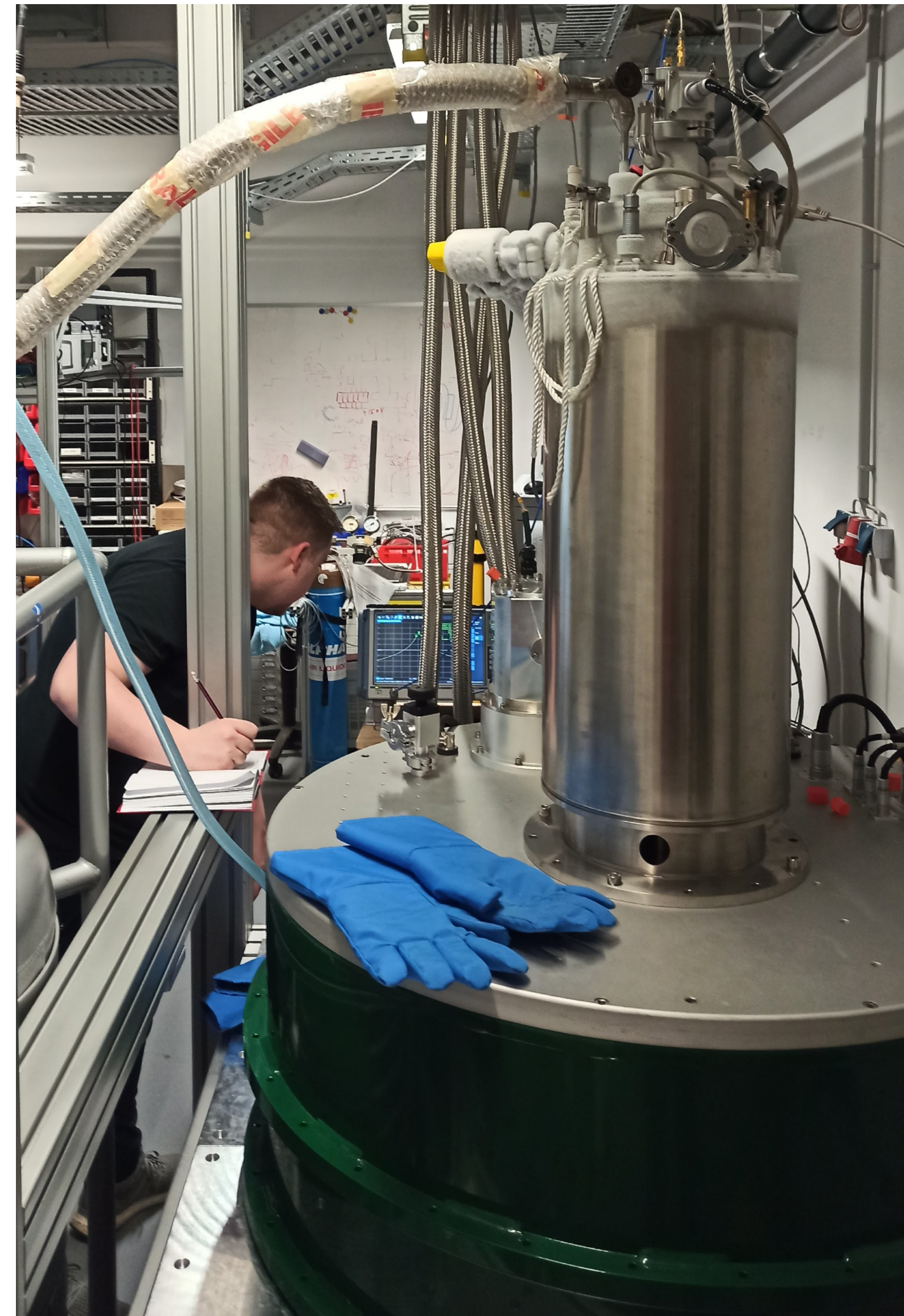
- **Supax:** new superconducting material for RF cavities:
  - **NbN**
  - $Q_0 = 3.1 \cdot 10^5$  @ 8.4 GHz, 4 K
  - Measurements within B-field finished last Friday

Cu cavity, coated with NbN at university of Siegen



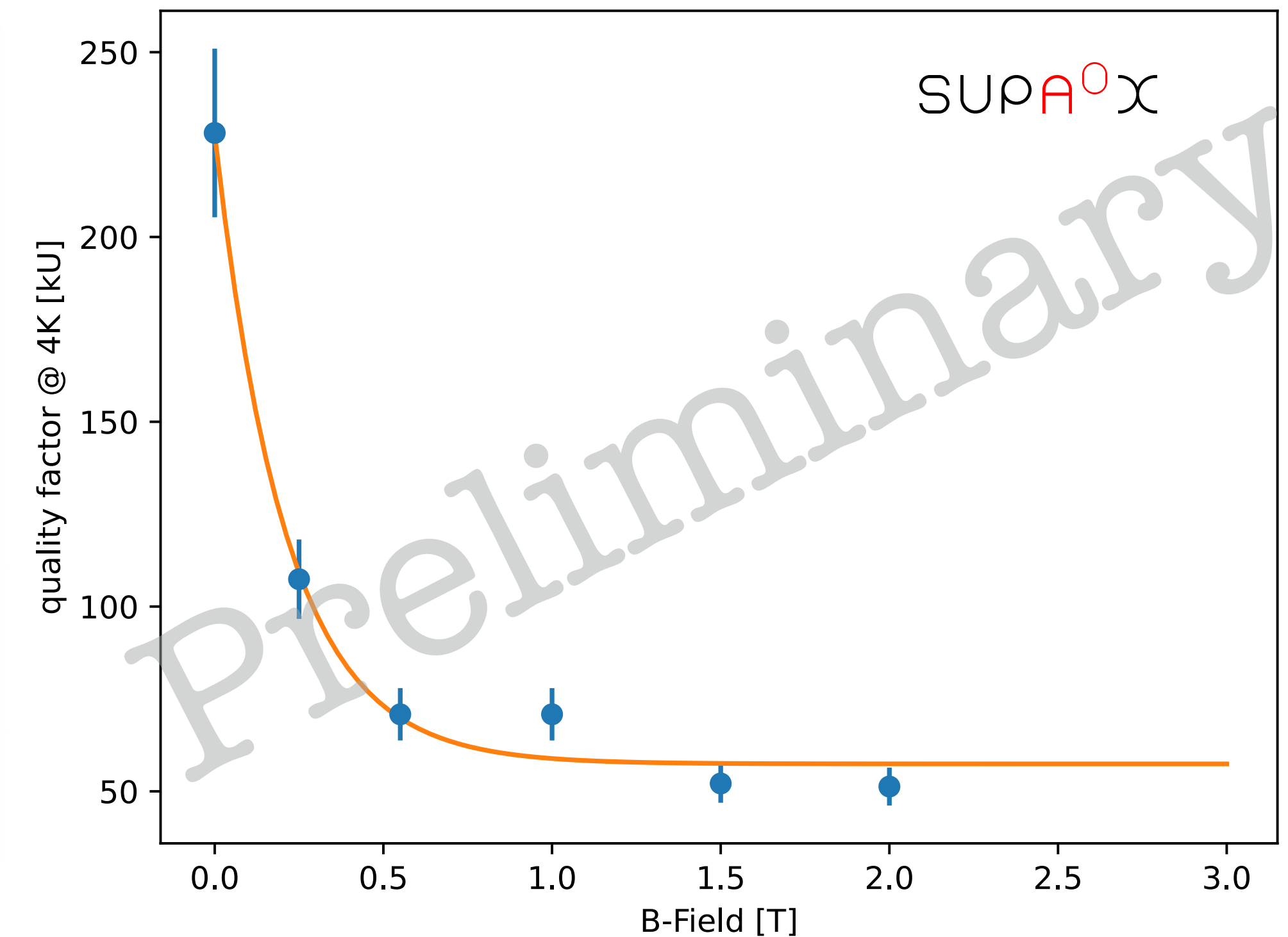
- Measurement at D. Budkers lab in Mainz

- **Supax:** new superconducting material for RF cavities:
  - **NbN**
  - $Q_0 = 3.1 \cdot 10^5$  @ 8.4 GHz, 4 K
  - Measurements within B-field finished last Friday
  - Analysis in progress. Preliminary results



- **NbN**

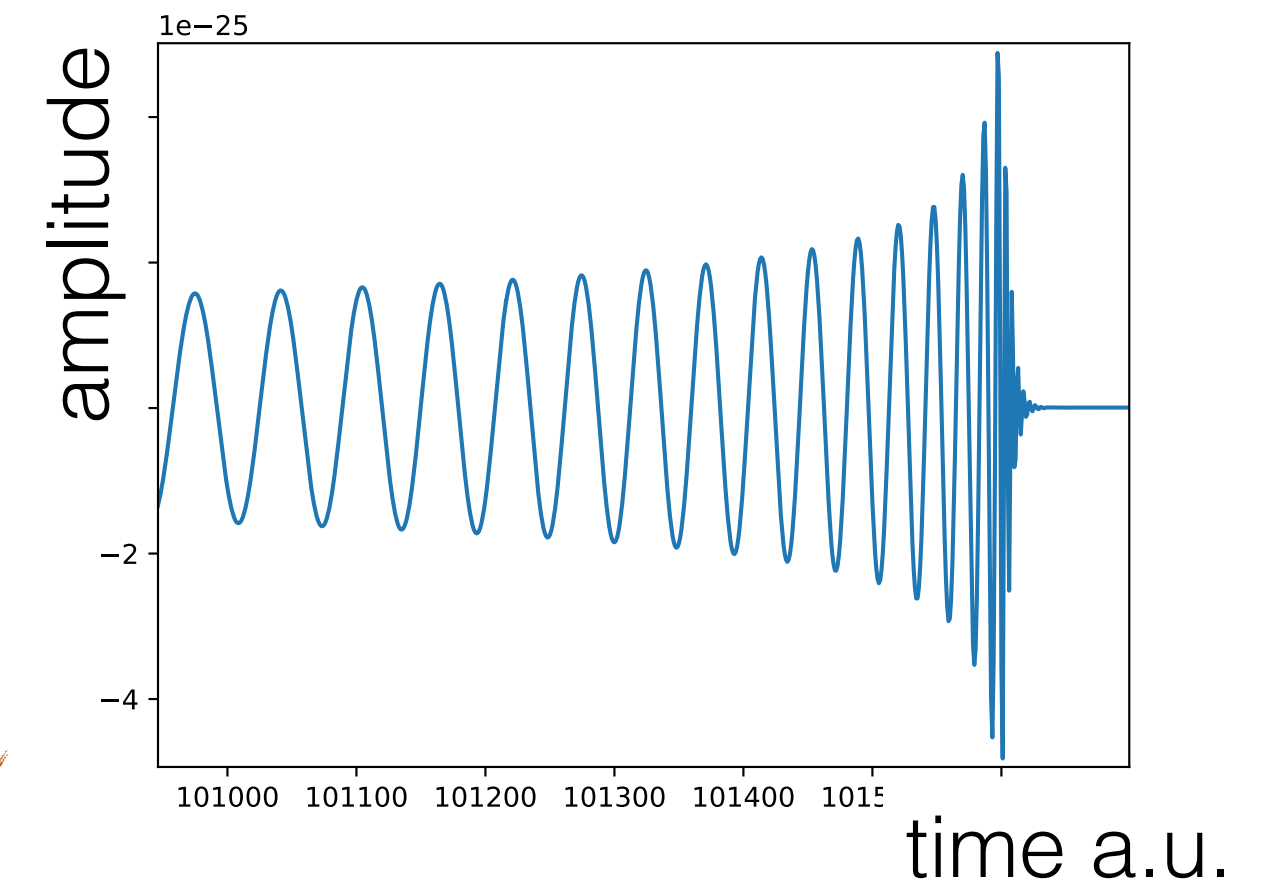
- Cavity largely over coupled during measurement
- Q0 around  $3 \cdot 10^5$  in previous measurement
- Q0 ~exponentially decaying with increasing B-field
  - Suggest reduction of Q max by factor 4.5 at 2T field
- Seems NbN not suitable for this purpose ...



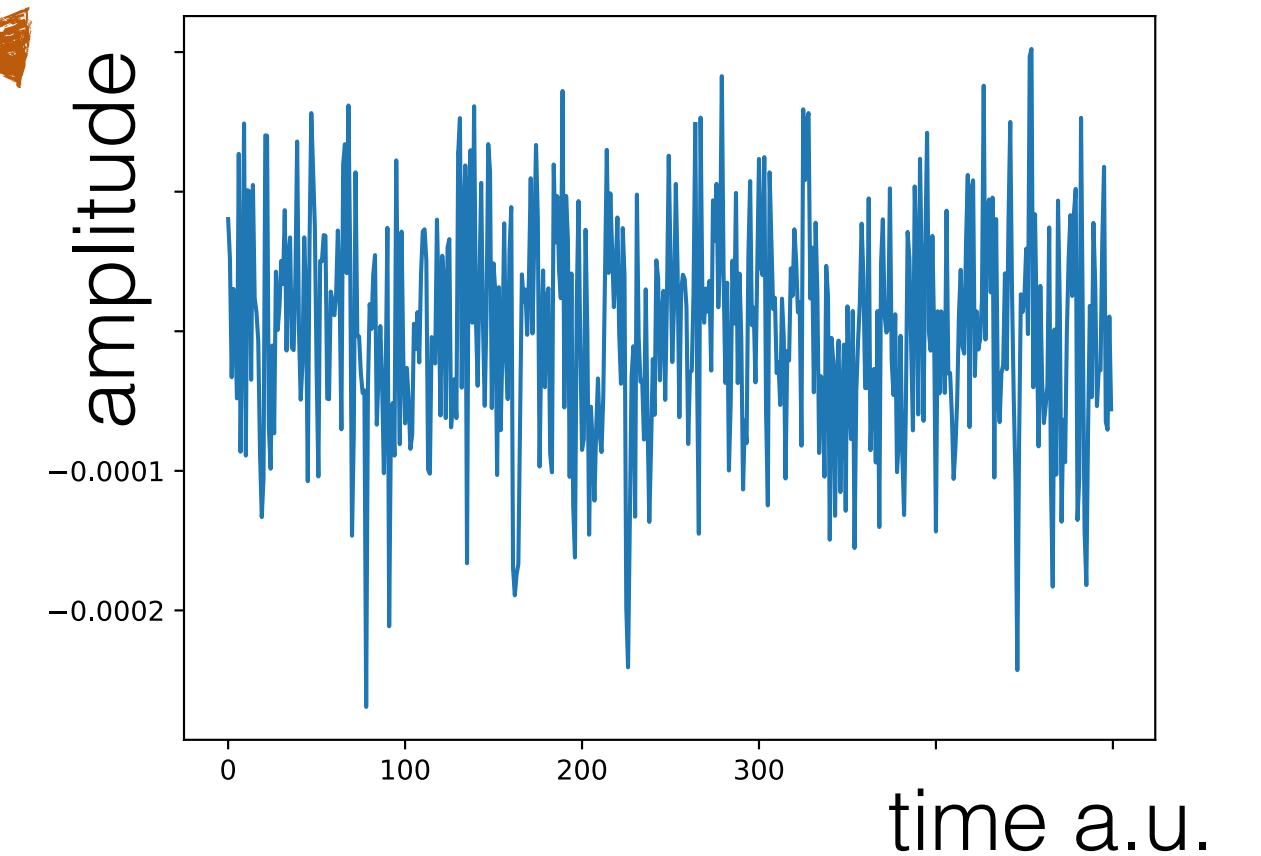


- **Spherical cavity:**
  - Prototype spherical cavity produced (4cm diameter, Cu)
  - To be characterised
- **MgB<sub>2</sub> as SC material:**
  - Investigating coating possibilities
- **Timeseries analysis of multiple cavity signals:**
  - Analysis of pseudo-data is currently in development
  - Targeting transient signals with  $O(10\text{ms})$  duration

- Similar approach as for low frequency BH mergers:
  - Analysis in **time domain**
  - Data rates:  $\sim 100\text{MB/s}$  per channel for 10MHz bandwidth
- Simultaneous fit of expected signal shape in all data streams
  - Exploiting all available information
    - + Increased sensitivity compared to time domain analysis
    - - Significant increase in storage & CPU requirement
  - **Sensitive to short transient** signals



Fit template



# Estimated Sensitivity Combining Cavities

- Phase aligned combination voltages from of N cavities
  - RF amplitude (voltage):

$$V_{comb} = \frac{it\omega}{\sqrt{N}} \sum_i V_i e^{i\phi_i} \propto \sqrt{N} V_0$$

$\uparrow$   
 $V_i = V, \phi_i = \phi$

- Hence the **signal power scales linearly in N!**

- **Assumed single setup**

- 14T B-field, about 10cm diam., 30cm long
- 3 spherical cavities @ 5GHz, SC, high Q
- 1s integration time

Setup	Supax	GravNet
Shape	cyl.	spher.
$f_0$ [GHz]	8.3	5.0
Volume [l]	0.128	0.21
$Q_0$	39600	$10^6$
$\eta$	0.08	0.6
$T_{sys}$ [K]	5	0.1
$B$ [T]		14
int. time		1 s
n cavities	1	3
noise power [W]	$1.5 \cdot 10^{-21} W$	$6.2 \cdot 10^{-23} W$
$h_0(P_{sig} = P_{noise})$	$7.1 \cdot 10^{-21}$	$5.2 \cdot 10^{-23}$

- Results in table for power integrating measurement

- **Timeseries analysis**

- Sensitive to shorter signals
- Expected to increase sensitivity by factor 2 - 4

- How sensitive can we get with **10 setups**, scattered around the globe

- Assumptions:

- Sampling of Waveform -> offline combination of phase aligned IQ data
- Setups as shown before
  - Effective signal power increased by factor 10
  - Strain sensitivity increased by factor  $\sqrt{10} \approx 3$

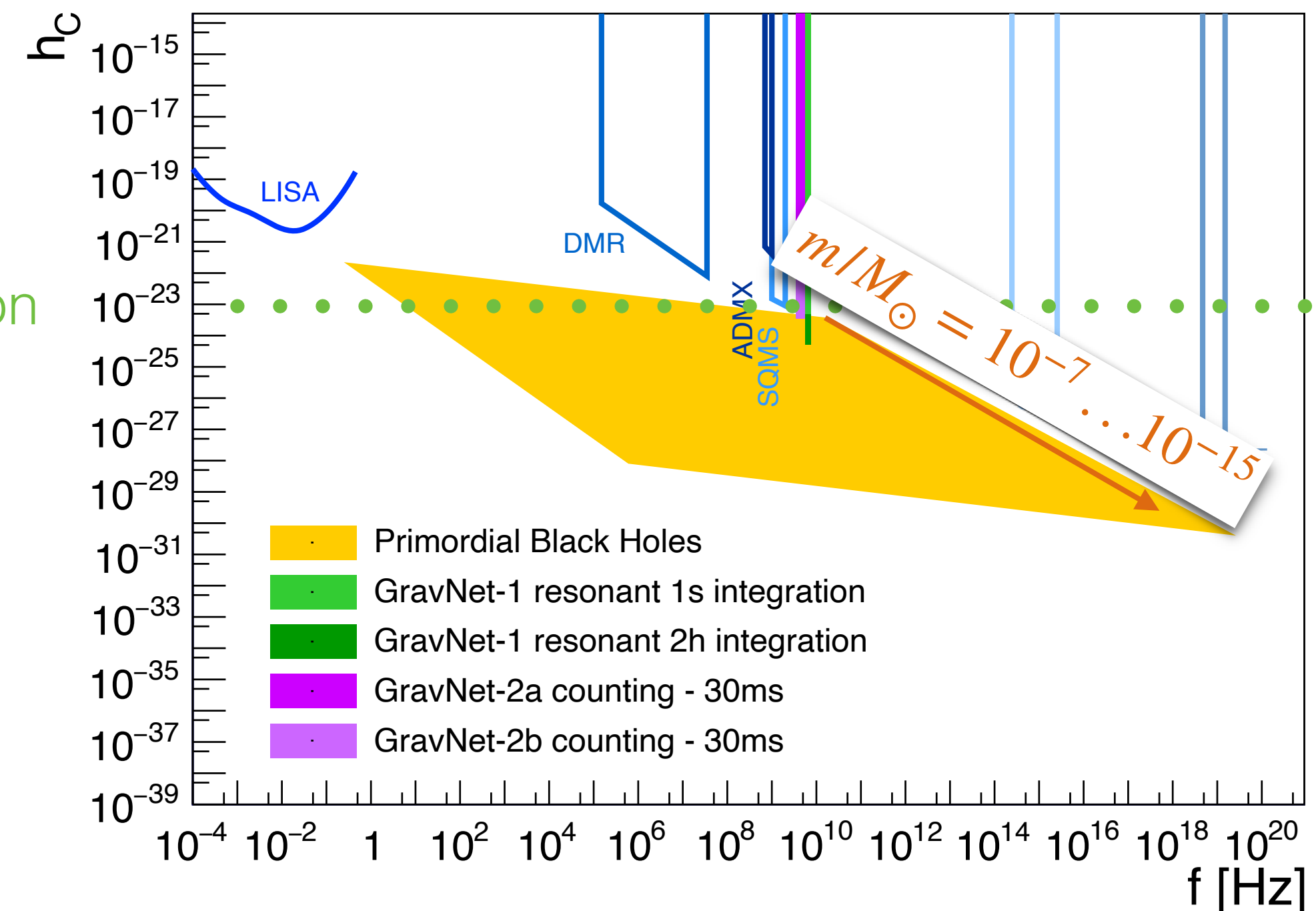
$$h_0 < 10^{-23}, \text{ 1 second integration time}$$

- Phase alignment for distributed setups:

- If signal seen in 3 cavities:
  - Direction of GW can be reconstructed
- Otherwise:
  - Scan through all possible directions and repeat combinations

- No frequency tuning needed:
  - PBH signals are fast transients
  - Single frequency sufficiency

1s integration



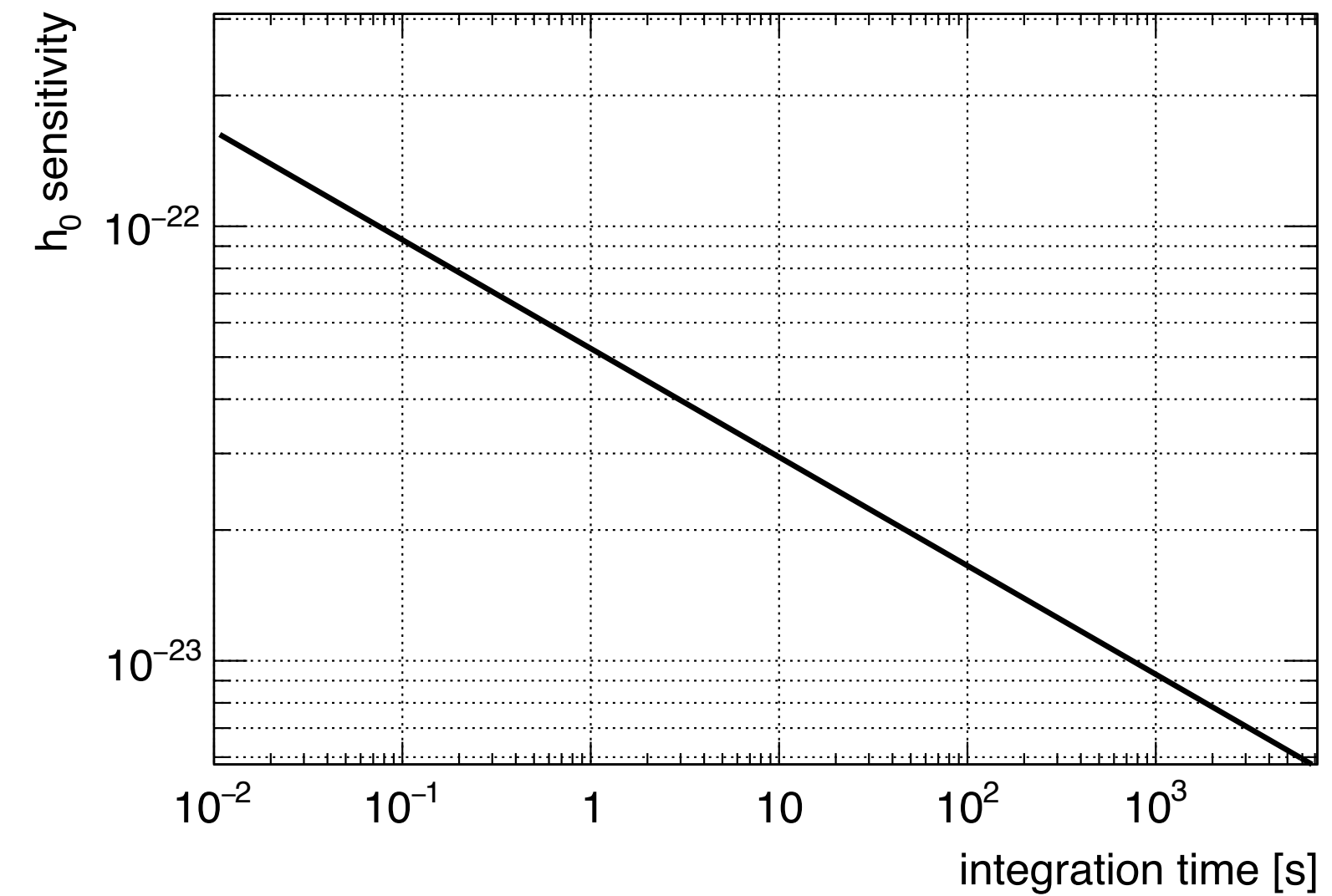
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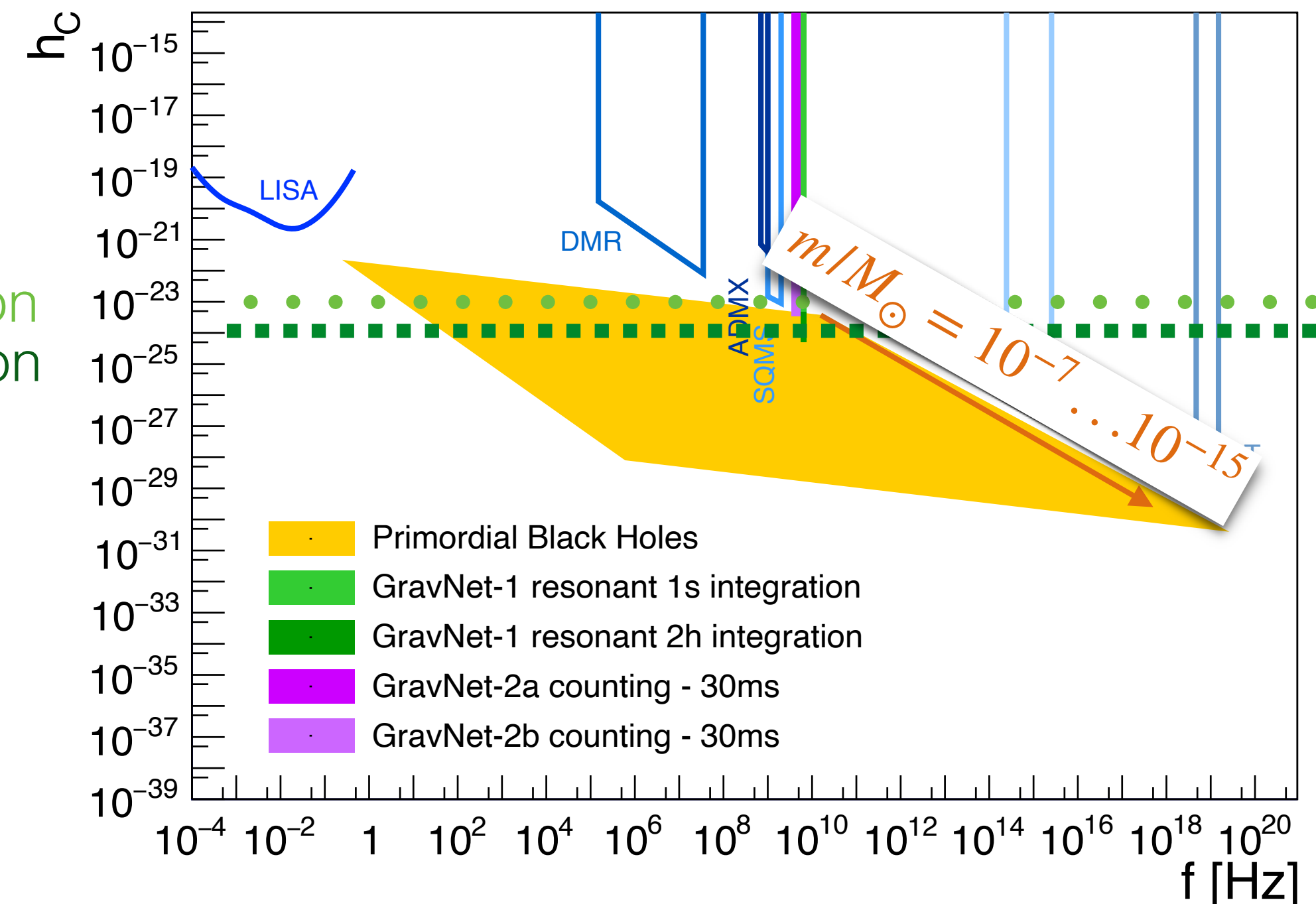
- Longer integration times

- Sensitivity gain with integration time  $t^{1/4}$

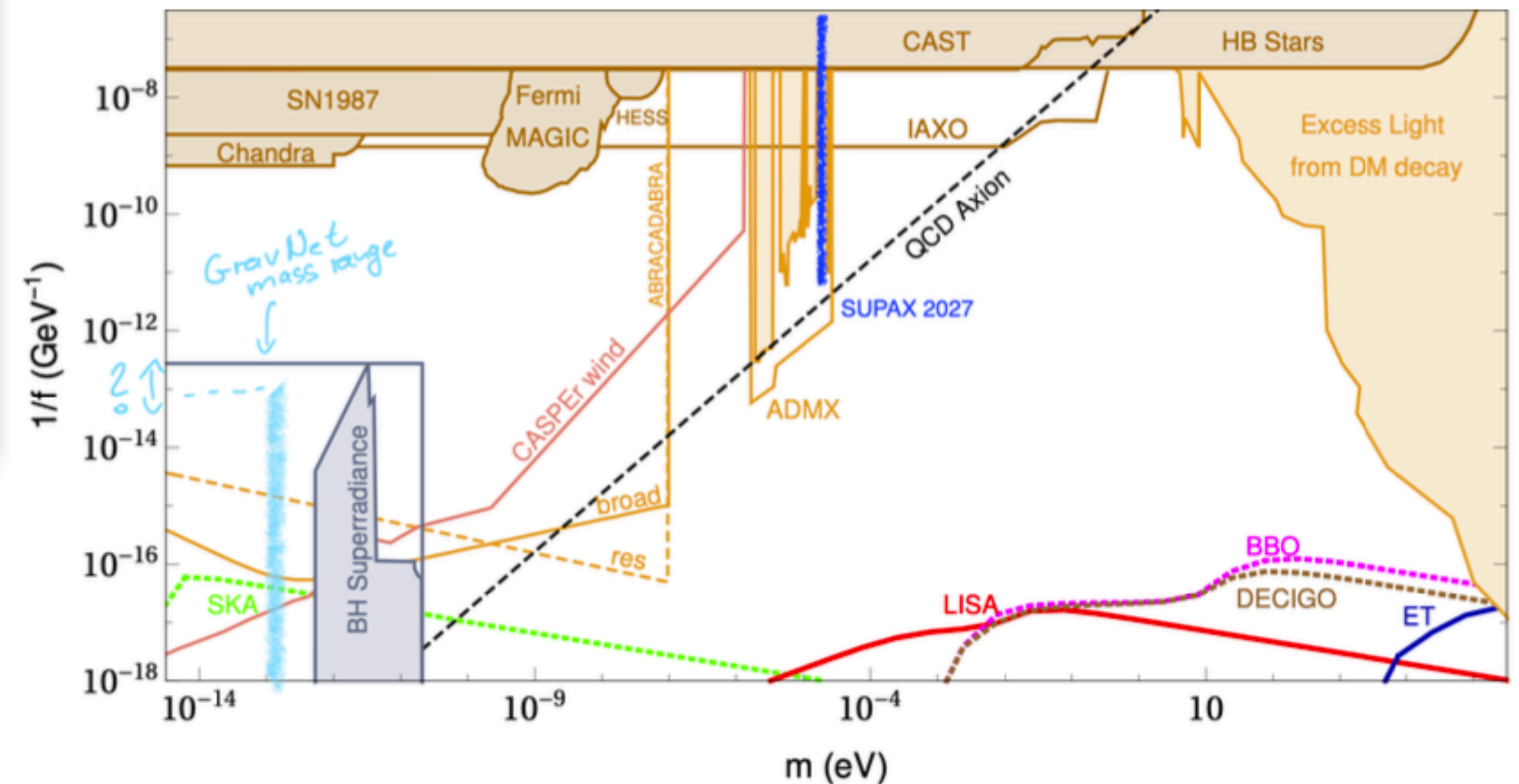
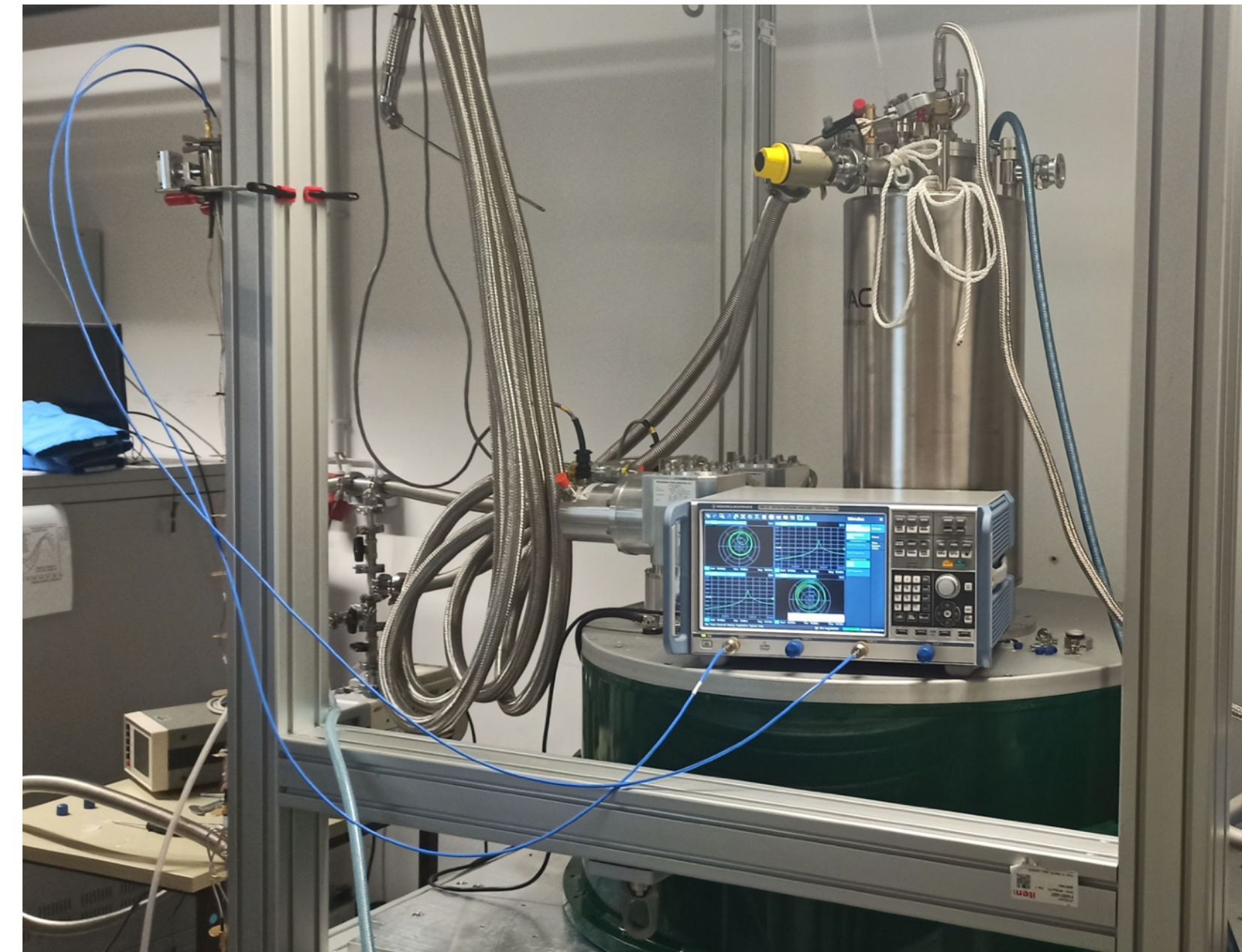
$$h_0 < 10^{-24}, \text{ 2h integration time}$$



1s integration  
2h integration



- Working **4K setup @ Mainz** with **14T** magnet
- R&D on SC high Q cavities in B-field ongoing
  - **First results on NbN**
- Optimisation of cavity geometry for GW started
- Combination of multiple cavities next
- **Target sensitivity:**
  - Strain  $< 10^{-23}$  for 1s integration times
- Ultimately working towards a network of GW detectors reaching strains of  $10^{-24}$  for transient signals  $O(10\text{ms})$



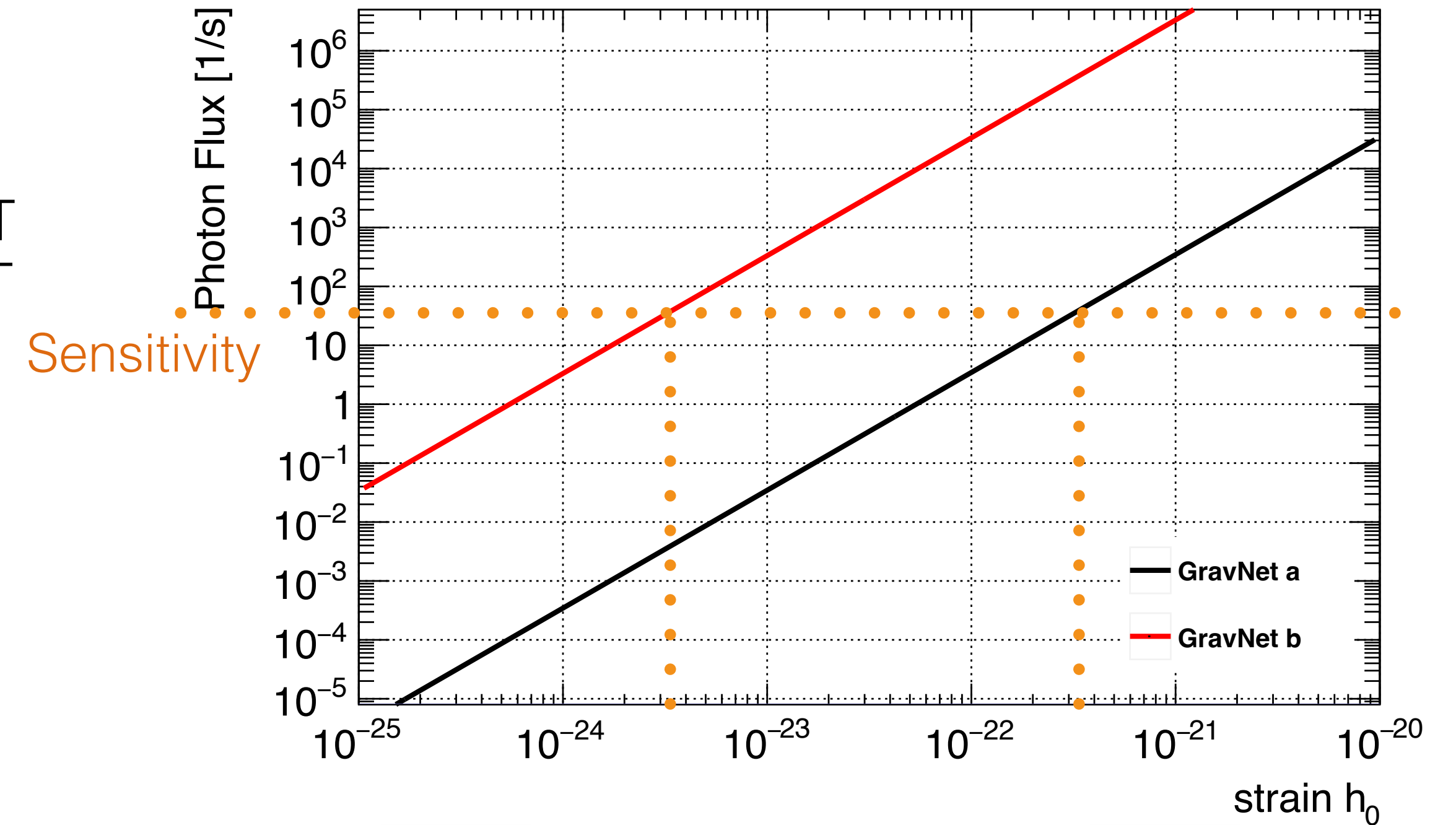
BACKUP

- With 20 detectors a photon flux of 40 Hz can be detected with an efficiency of 1 within a coincidence interval of 32ms

- Signal photon flux depends on conversion region:

- a) Magnet dimensions as before (9cm diameter),  $B = 14\text{T}$
- b) Assuming large NMR magnet (80cm diameter),  $B = 9\text{T}$

Setup	GravNet-a	GravNet-b
radius	40 mm	40 cm
length	12cm	50 cm
Volume [ $m^3$ ]	$6 \times 10^{-4}$	0.25
$Q_0$	$10^6$	$10^5$
$T_{\text{sys}}$ [K]	0.1	0.1
$B$ [T]	14	9



Global network of HFGW detectors will be able to reach into the interesting region for PBH with existing technologies!

- Achievable sensitivity:

- $h_0 < 3 \times 10^{-22} \dots 3 \times 10^{-24}$

- With coincidence time of 32ms!

Significant room for improvements:  
more detectors, larger volumes, higher detector efficiency



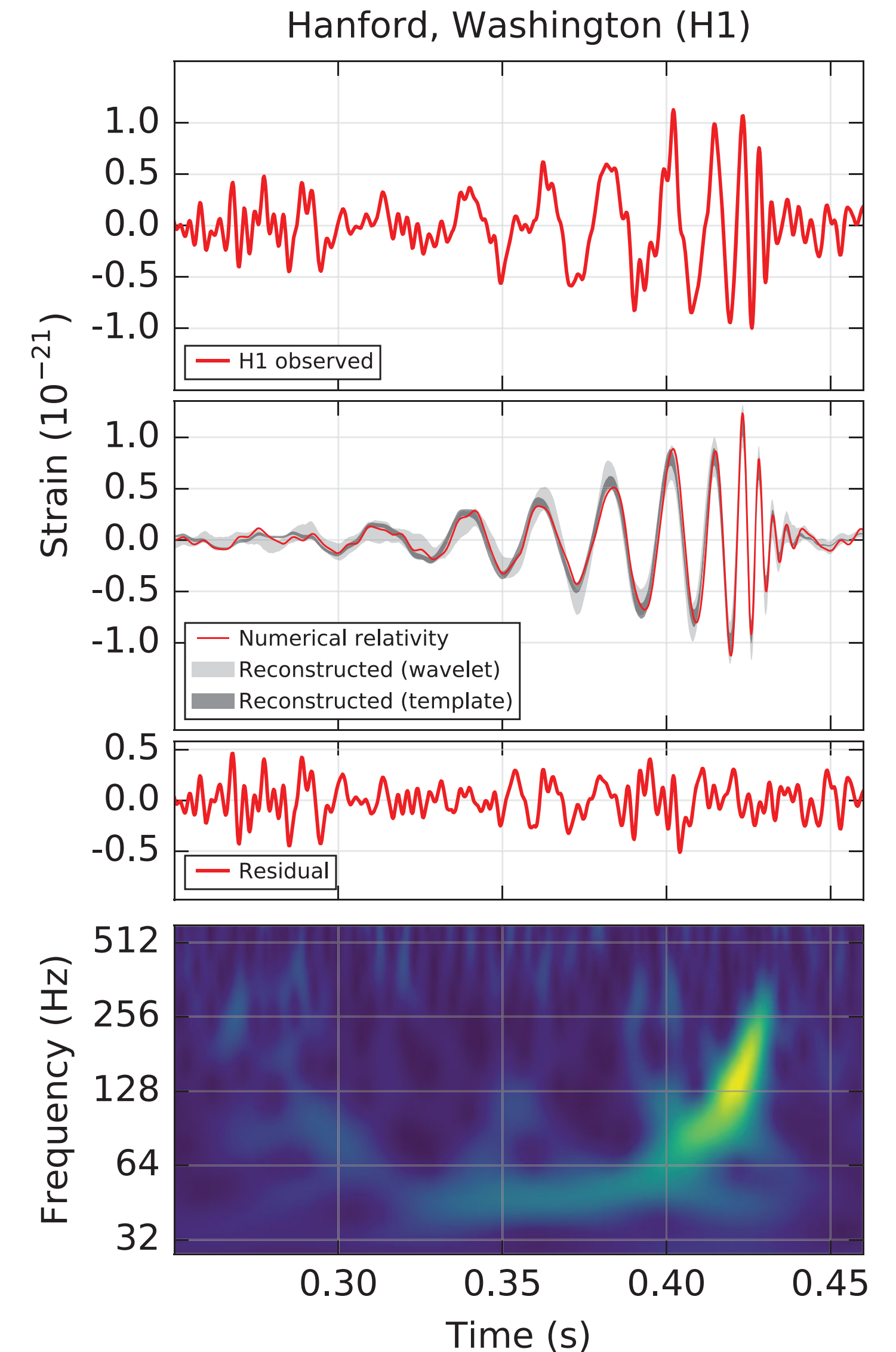
# Introduction - Gravitational Waves

- Observation of gravitational waves by LIGO/Virgo is certainly a breakthrough in fundamental physics!

- However, there should/could be **other sources** of gravitational waves
  - Primordial black hole merges
  - Boson clouds (BH superradiance)
  - ...
- Those GW would have **frequencies in the GHz regime**
  - **Should search for high frequency GW**

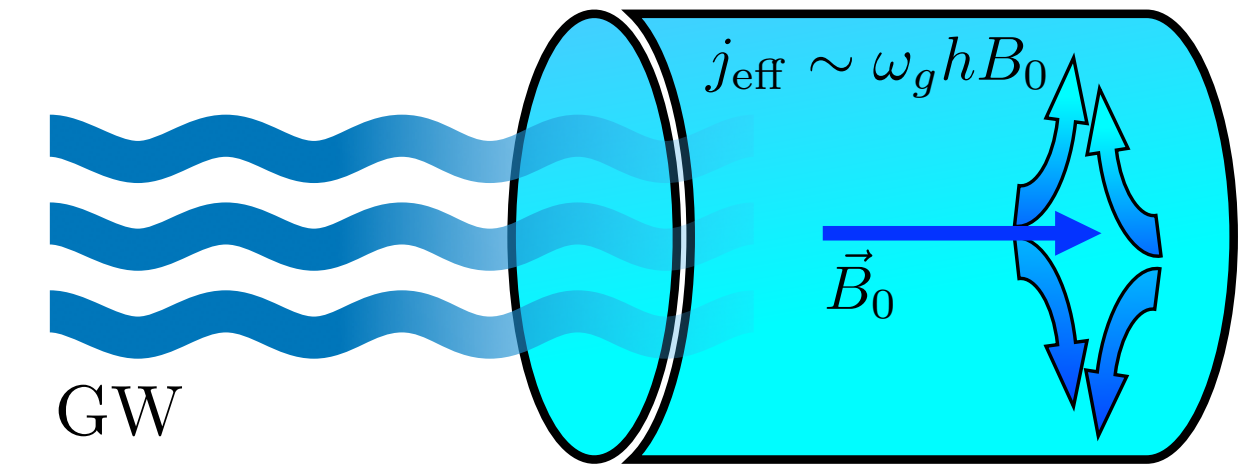
**But how?**

- Frequency range: 10-1000 Hz



[PRL 116, 061102 (2016)]

[arXiv:2112.11465]



- Two contributing effects
  - Assuming conversion cavity with volume  $V$  within static B-Field

- GW deforms cavity

- Oscillating change of magnetic flux
- Excitation of EM field

- Direct conversion of gravitons to photons via the inverse Gertsenshtein effect

- Resonant excitation of EM field in Cavity

- Produced EM power given by:

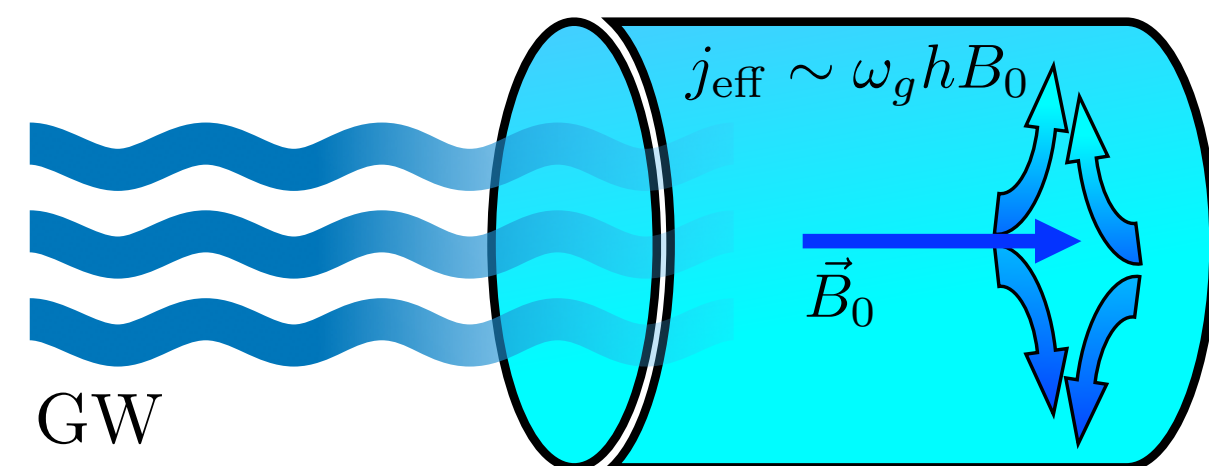
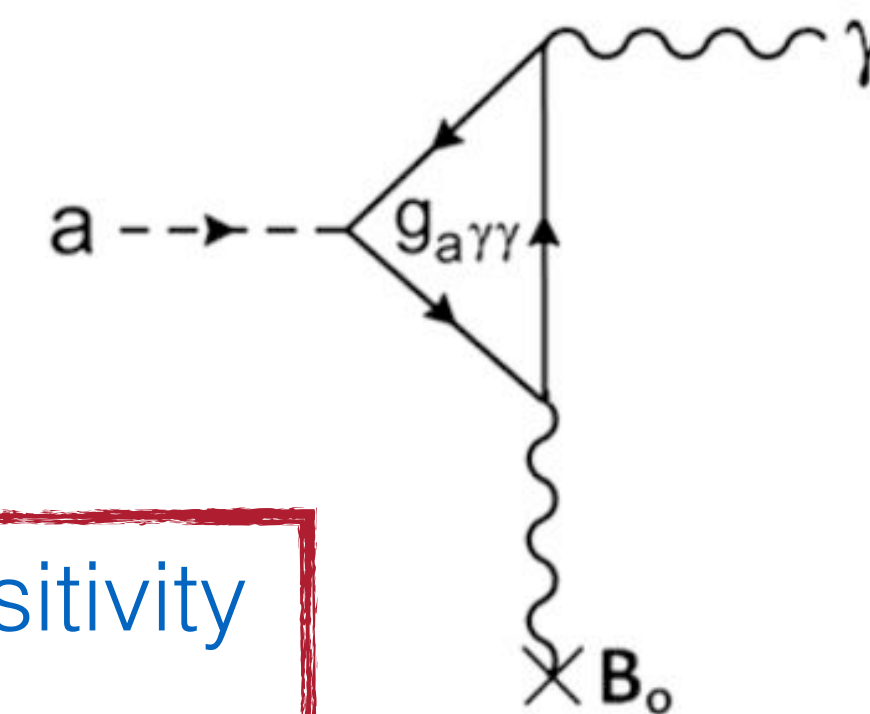
$$P_{sig} = \frac{1}{2} Q \omega_g^3 V^{5/3} (\eta_n h_0 B_0)^2 \frac{1}{\mu_0 c^2}$$

# Similarity to Axion Searches

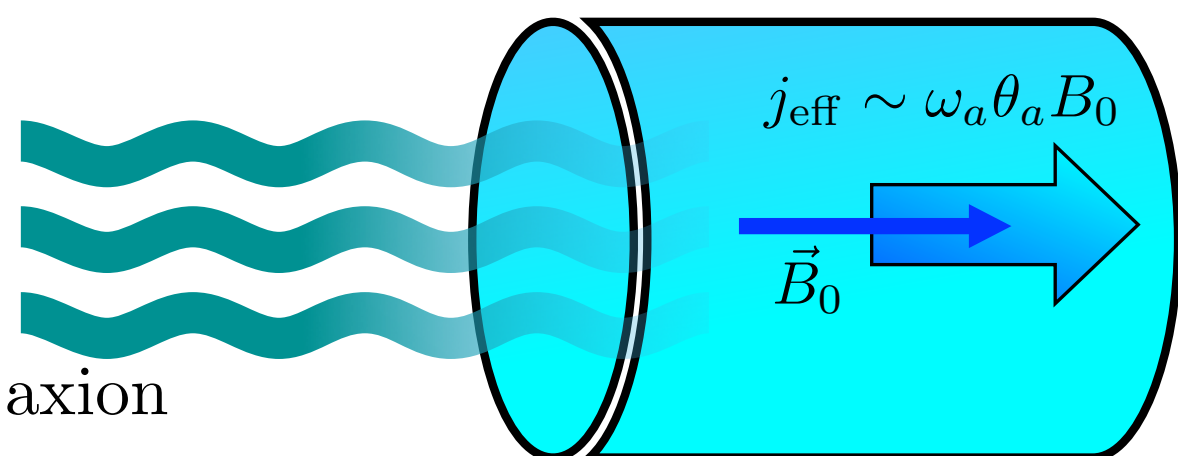
- Axion Haloscopes:

- RF cavity in magnetic field → Primakov conversion of axions to photons
- Resonant excitation of cavity mode

- **Cavity based haloscopes are sensitive to GWs**



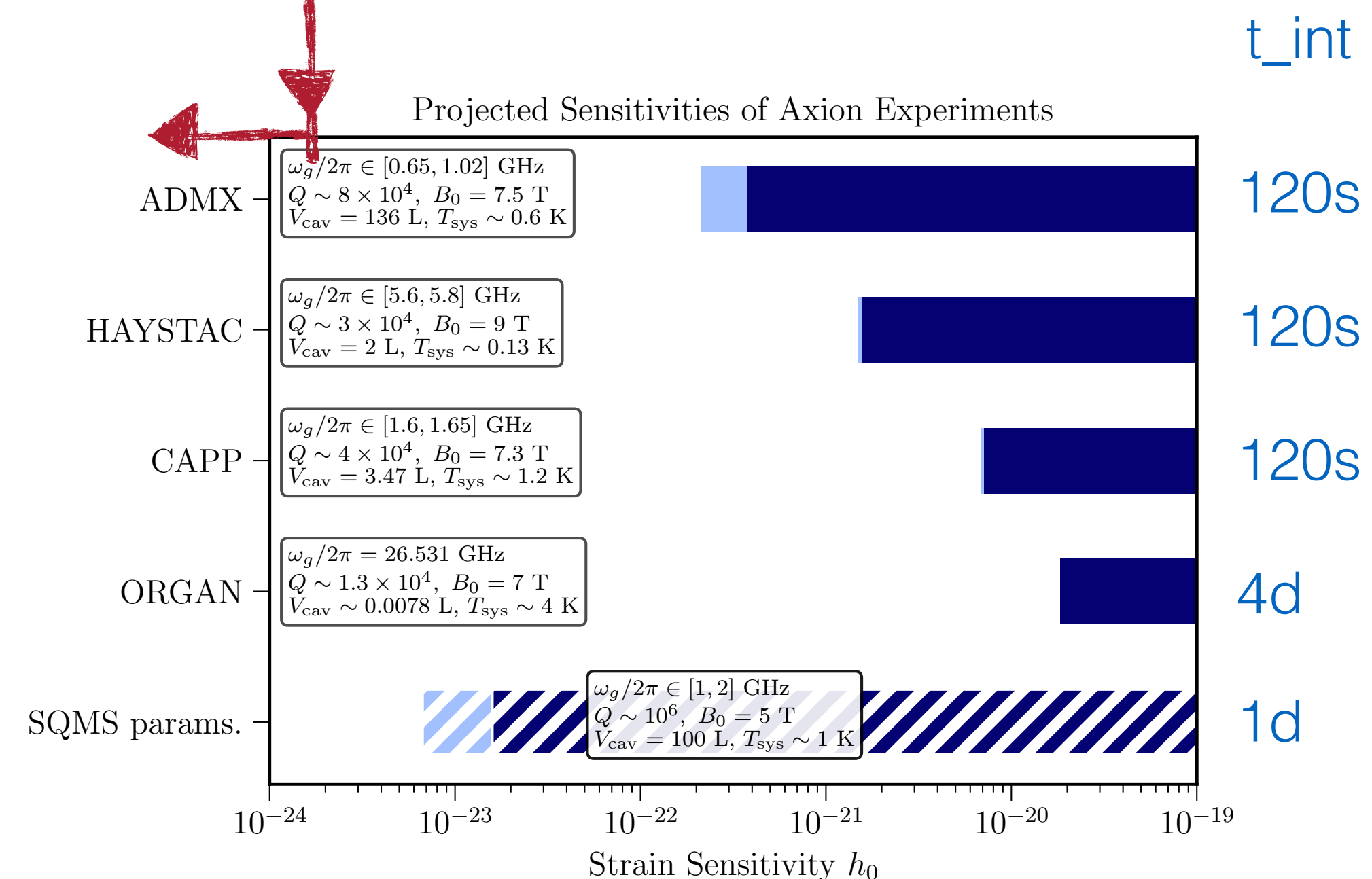
- **GW:**
  - Typical quadruple structure
  - Preferred mode: TM 020
  - Current direction dependent on GW



- **Axions:**
  - Preferred mode: TM 010
  - Current dependent on B-field direction
  - Little overlap with GW mode

[arXiv:2112.11465]

Interesting sensitivity range for PBH



[Detecting high-frequency gravitational waves with microwave cavities  
Asher Berlin, Diego Blas, Raffaele Tito D'Agnolo, Sebastian A.R. Ellis  
arXiv:2112.11465]

- GW strain: largest if merging is imminent (closest to innermost stable circular orbit)

- Frequency drift large

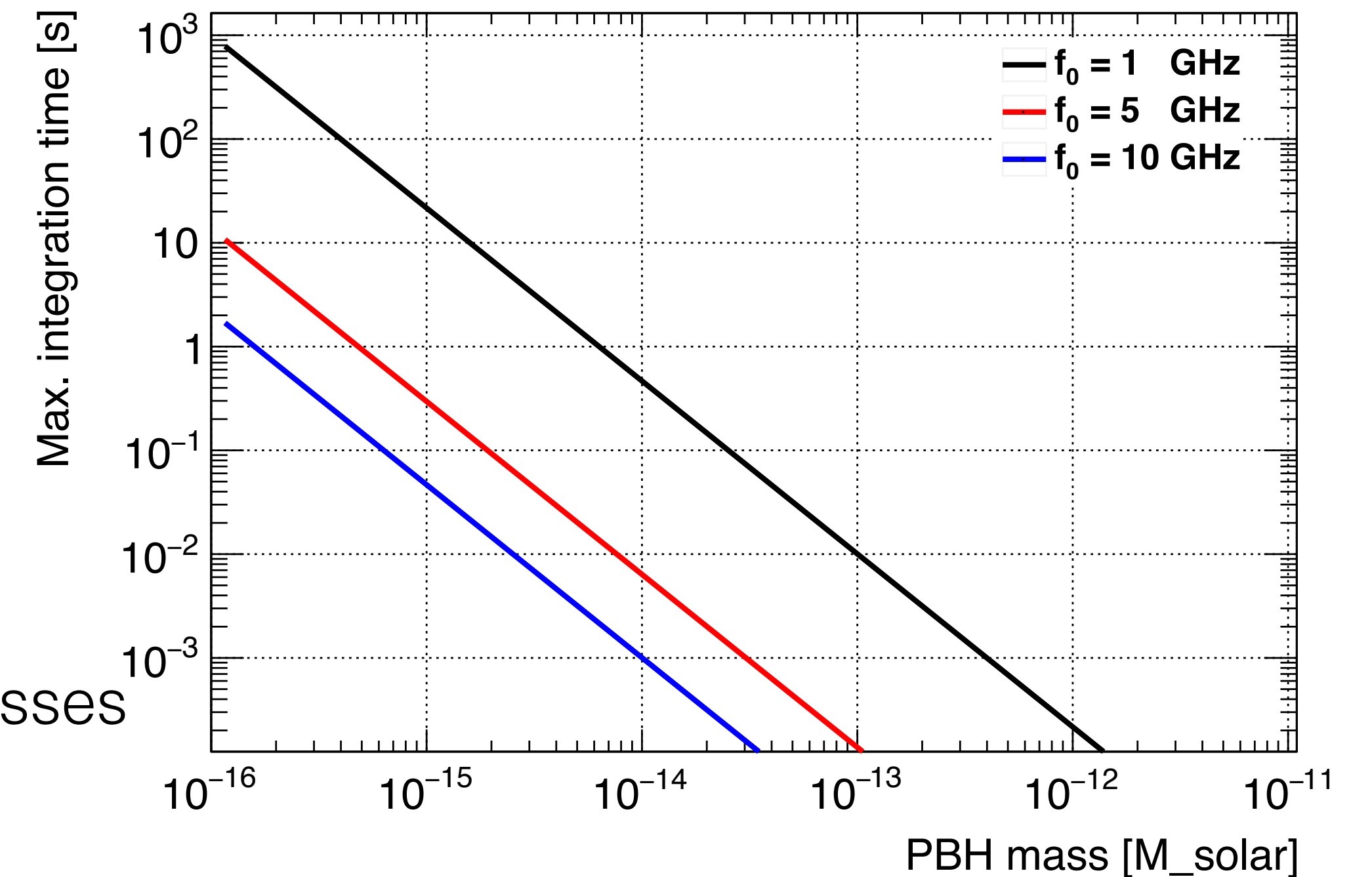
$$\dot{f} = \frac{96}{5} \pi^{8/3} m_c^{5/3} f^{11/3} \simeq 4.62 \times 10^{11} \text{ Hz}^2 \left( \frac{m_{\text{PBH}}}{10^{-9} M_\odot} \right)^{5/3} \left( \frac{f}{\text{GHz}} \right)^{11/3}$$

- To resonantly excite a cavity:

- GW frequency must stay within resonator bandwidth

- $\omega/Q \approx 10^{10} \text{ Hz} / 10^6 = 10 \text{ kHz}$

- Very short integration times O(ms) or below for larger PBH masses



- No improvement with longer integration times!

- Alternative?

- Recent progress in R&D for single RF photon counters

- Several technologies under study

- Current Biased Josephson Junctions
- Kerr Josephon Parametric amplifiers
- Transmon Q-Bit readout

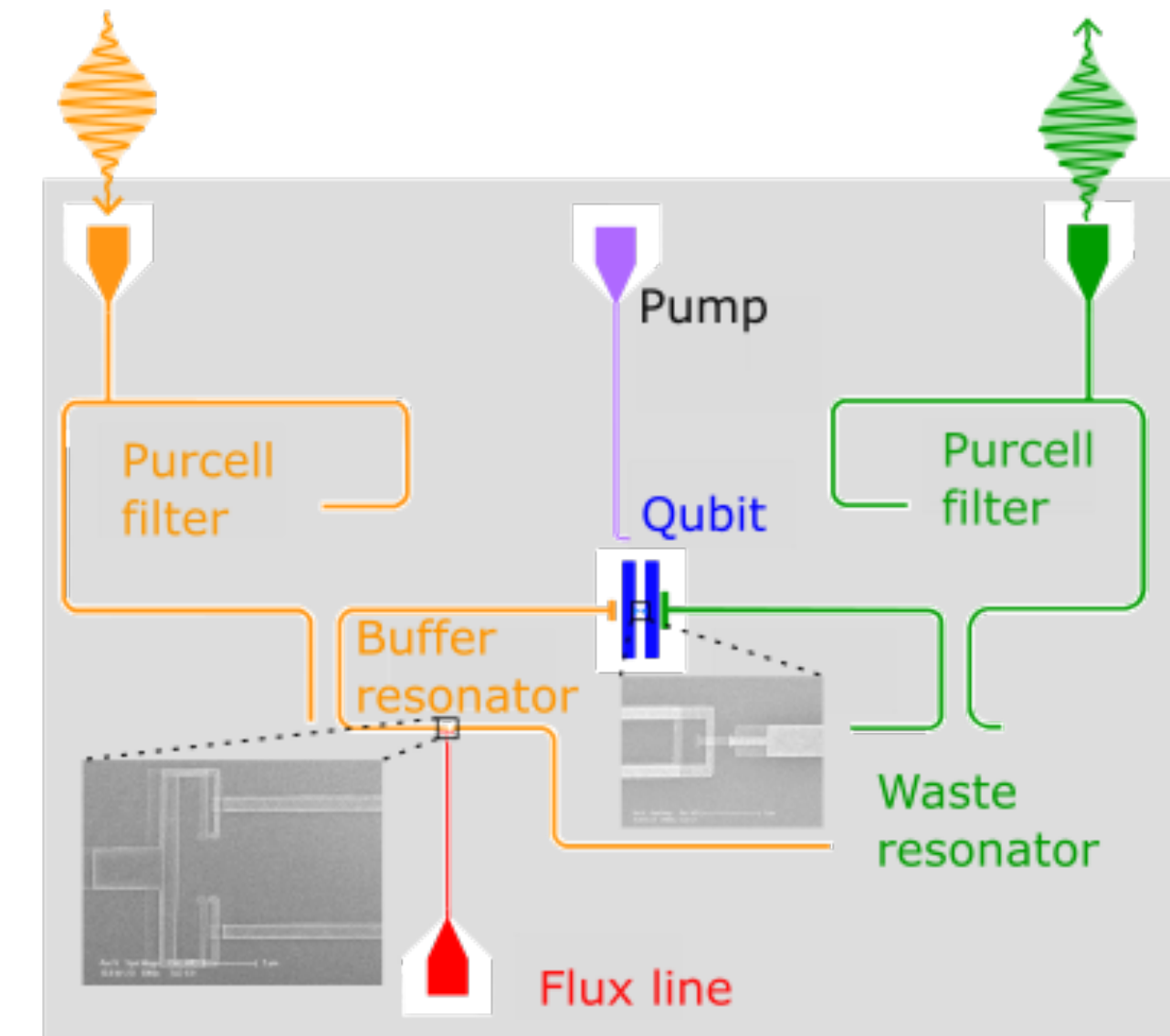
[arXiv:2302.07556 ]

[arXiv:2308.07084 ]

[arXiv:2307.03614 ]



- Shown **single photon efficiency: 43% @ 90 Hz dark count rate**
  - Big R&D effort ongoing [ERC syn.: “Dark Quantum” ]



[arXiv:2307.03614 ]

- Measurement boils down to a **coincidence measurement** !

- Coincidence window and needed number of coincident detectors optimised depending on

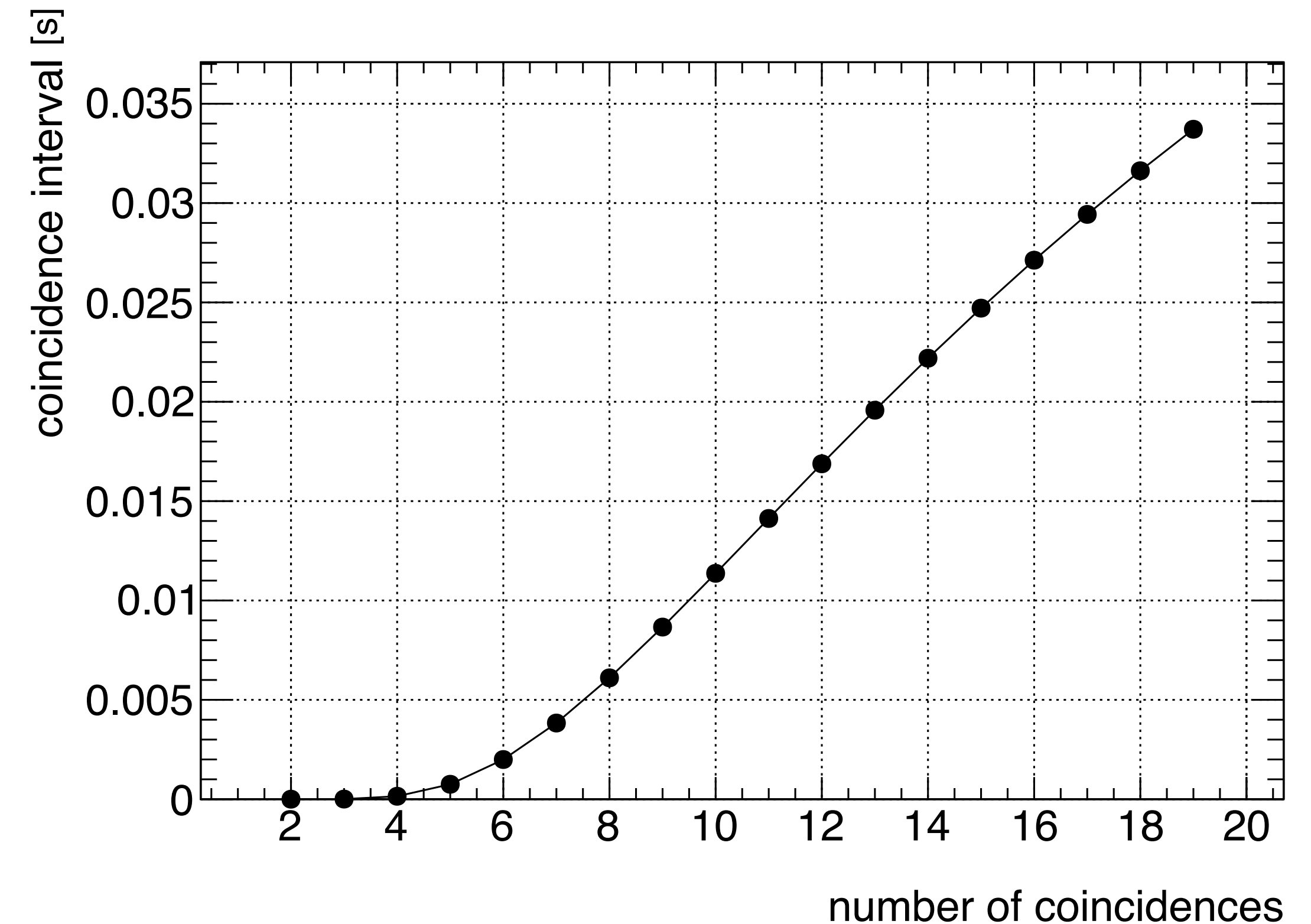
- Background rate (thermal, detector noise)
- Signal Rate

- Background rate:

- Average thermal power in cavity @ 0.1K  $\sim 4 \times 10^{-23}$  W, corresponding to 10 photons / s @ 5 GHz
- Could be lowered going to lower temperatures
- Assuming advances in the near future on the single photon sensors:
  - Detector dark count rate will drop significantly -> negligible

- Parameter used for Calculation:

- Allowed accidental coincidence rate:  $\leq 1/\text{year}$
- Background rate: 10 Hz
- N detectors: 20



# Photon Counting - Signal efficiency

- Overall signal efficiency dependent on detector efficiency, coincidence window and signal photon flux:

- $\epsilon_{single} = \epsilon_{det} \Delta t_{coincidence} \Phi_{sig}$        $\Phi_{sig}$  = signal photon flux

- $\epsilon_{tot} = \sum_{i>k} \binom{N}{k} p^k (1-p)^{N-k}$ ,  $p = \epsilon_{single}$ ,  $k$  = number of required coincidences,  $N$  = number of detectors

- Parameter used for Calculation:

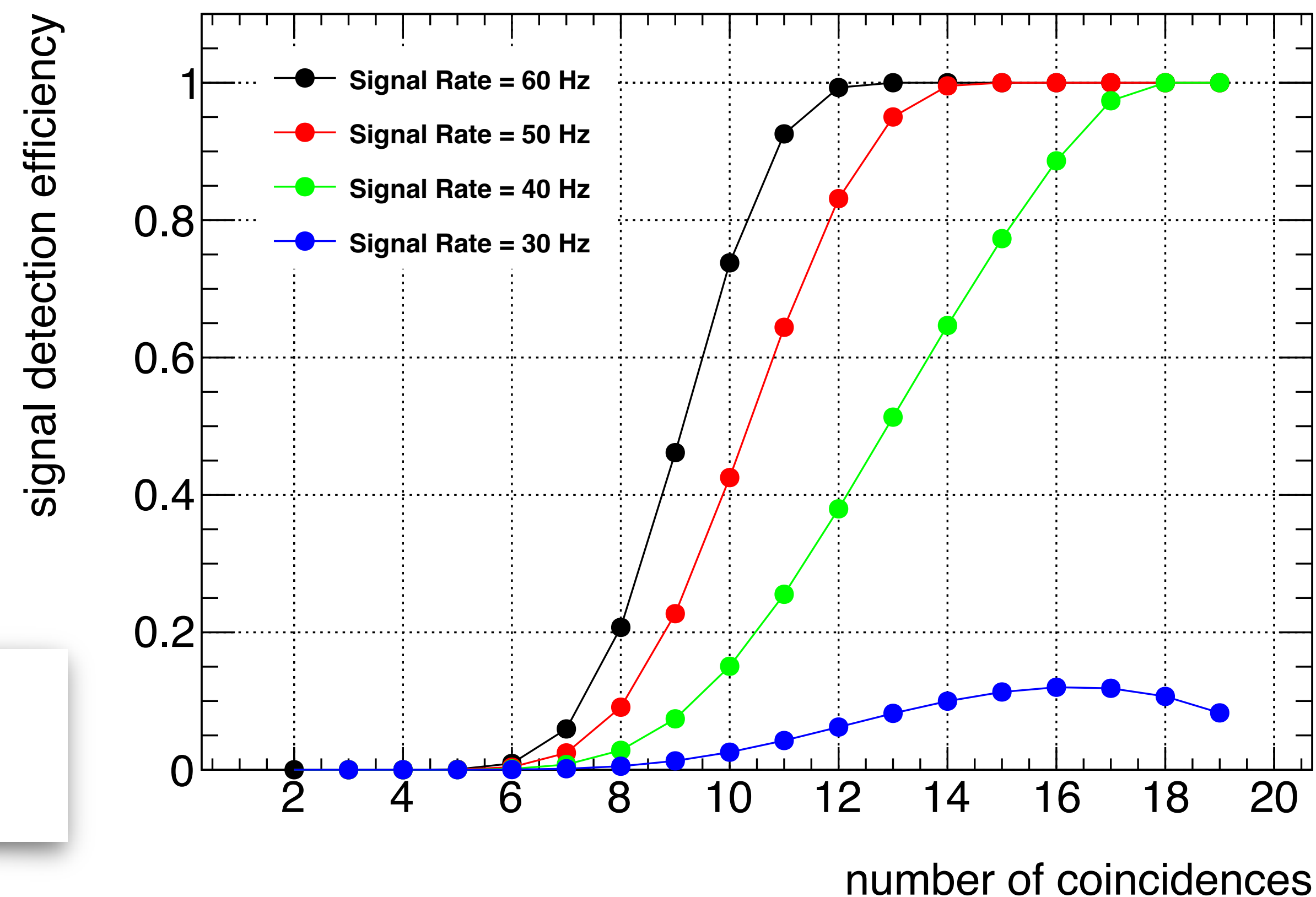
- Allowed accidental coincidence rate:  $\leq 1/\text{year}$

- Background rate: 10 Hz

- N detectors: 20

- $\epsilon_{det}$ : 0.5

• With **20 detectors** a photon flux of **40 Hz** can be detected with an efficiency of 1 within a coincidence interval of **32ms**



- To increase the sensitivity of halo scope style experiments we suggest to build a **global network of detectors**
  - Remember: SNR scales linear with number of detectors!
- **Integrating measurement:**
  - Sample RF data, combine phase aligned, integrate
- Typical integration times too long to be sensitive to BH merges!

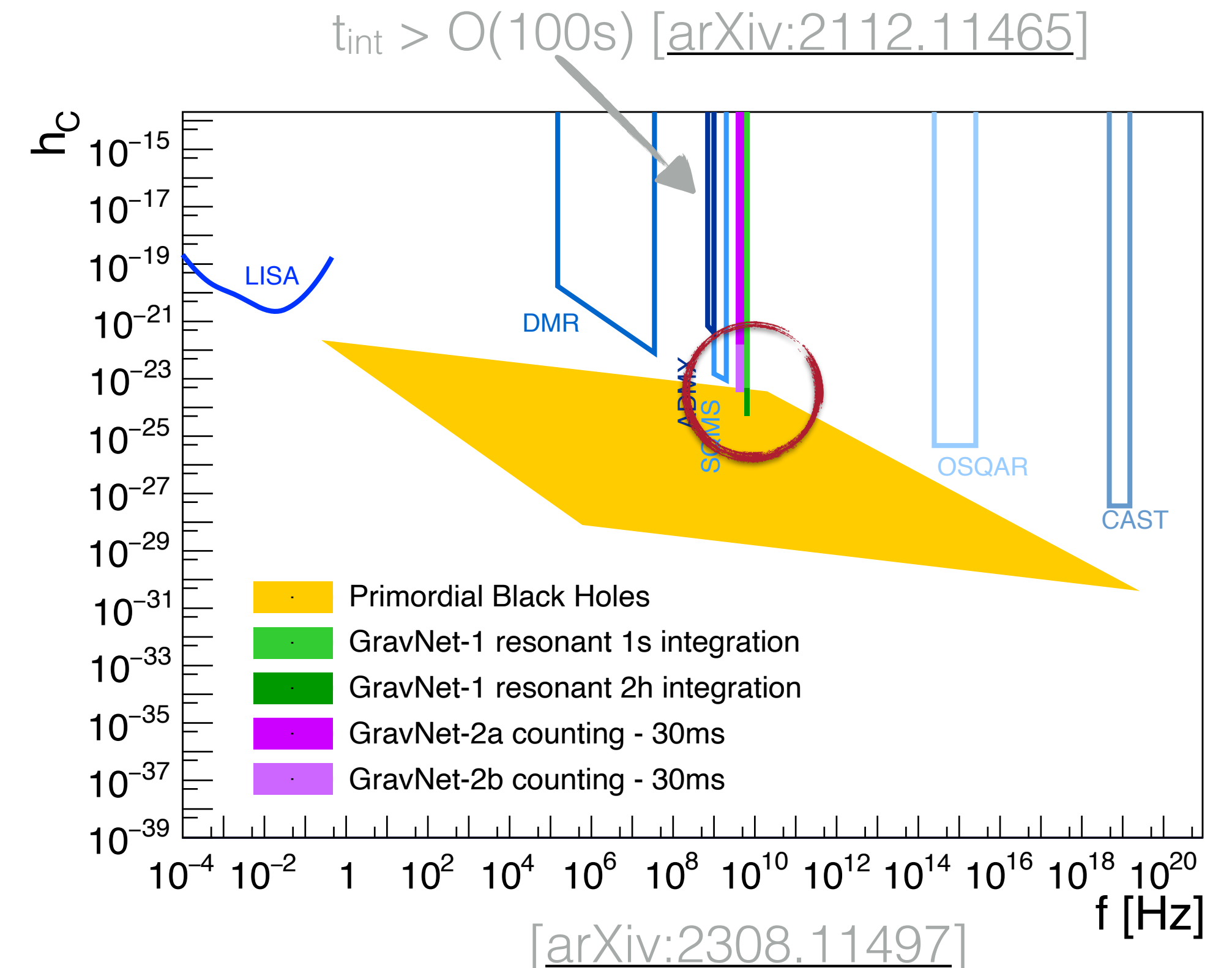
- Single frequency sufficient to hunt for PBH mergers!
- Could even combine measurements at different frequencies

- **Photon counting style experiments:**
  - Recent advancements in single RF photon detection allows to use coincidences of several detectors
- Using 20 independent detectors:

• Sensitivity:  $h_0 < 3 \times 10^{-22}$  ....  $3 \times 10^{-24}$



Requires large meta material cavities  
( high frequency @ large volume)





GravNet is an idea up for discussion

- Many advantages in **combining efforts searching for UHFGWs** in coordinated way
- GravNet would significantly improve the sensitivity on high frequency gravitational waves
- Based on commercial magnet systems, which is comparatively cheap
- Worldwide collaboration would share costs automatically with local lab-based experiments
- Easy exchange of R&D results and integration at all locations
- Sensitivity to the PBH parameter space with existing technologies!

