Measurement of charged fragments production cross sections ($d\sigma/dE$) in the interactions of C-ions with C,H,O targets

CNAO July 2017 Data Taking

IlaMi from Milano and Roma





Experimental Setup

- 3 thin targets (1-2 mm) based on C, H, O elements PMMA, C, CH
- 3 detection angles: 90°, 60°, 32°
- S Carbon lon beam energies: 115, 150, 221, 279, 351 MeV/u
- Fragments production (Z=1, A = 1, 2, 3) as a function of the production kinetic energy
- Time of Flight in thin plastic scintillators and energy deposit in the inorganic crystals for PID and Ekin measurements
- Experimental Data Monte Carlo simulation comparison



4 STSs 2mm thick for ToF measurement (time resolution \sim 400-600 ps) and Deposited Energy measurement (dE); 2 LYSOs 4x4x8 cm³ for Deposited Energy measurement (E);





Cross Section Formula

The 12 C fragmentation cross section for a ^A₇X fragment are obtained as:







Cross Section Formula: Normalization

The 12 C fragmentation cross section for a ^AX fragment are obtained as:

From CNAO Dose Delivery System

dose-current conversion systematic uncertainty. The relative uncertainty on N_{12C} (4%) is hence the convolution of the uncertainty on the stopping power determination [20] and on the dose measurements [21]. A possible additional contribution to the systematic uncertainty, coming from the monitoring system measurement stability [22], was found to be negligible

$N_{12}C$	$\cdot 10^{6}$	$\cdot 10^{6}$	$\cdot 10^{6}$	$\cdot 10^6$	$\cdot 10^6$
Target	115	153	222	281	353
	[MeV/u]	[MeV/u]	[MeV/u]	[MeV/u]	[MeV/u]
PMMA	49866	46512	49395	49601	42000
Graphyte	49454	46583	47484	47288	49328
Plast. Scint.	49728	50600	49347	49787	49653

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$\frac{d\sigma}{dE_k} {A \choose Z} = -$	$\frac{V_A (E)}{\Delta E_k}$	$\frac{k}{N}$	urity(E)	$\frac{1}{Y}$ $\frac{1}{\epsilon}$	-	
om CNAO elivery System tic uncertainty. The relative			Infori	mation or	n the tar	get
ence the convolution of the er determination [20] and on ossible additional contribution	Target	Composition	Thickness [mm]	Density $[g/cm^3]$		$\rho_{\mathbf{v}} \cdot th_{\mathbf{x}}$
oming from the monitoring [], was found to be negligible 0^6 $\cdot 10^6$ $\cdot 10^6$ $\cdot 10^6$	PMMA Graphite Plas.Scint.	$egin{array}{c} \mathrm{C}_5\mathrm{O}_2\mathrm{H}_8 & & \ \mathrm{C} & & \ \mathrm{C}_b\mathrm{H}_a & & \end{array}$	2 1 2	$ \begin{array}{c} 1.19\\ 0.94\\ 1.024 \end{array} $	$N_Y =$	$=\frac{\mu_{I}}{A_{Y}}$











• Particle identification (Z,A) from combining the information of QDC LYSO, QDC STSs, ToF STSs









 Unfolding technique (RooBayesUnfold) to obtain the fragments Ekin gen from Ekin meas









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number of particles selected as p (d,t)

number of true p (d,t) in p (d,t) selection





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Full simulation (FLUKA) (C on Targets ~1.e¹⁰ primaries) to compute the **PID efficiency** of PID selection on E (dE) vs ToF distributions, tuned from data

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	$32^o - \text{Ekin [MeV]}$	ϵ_{pp} [%]	ϵ_{dd} [%]	ϵ_{tt} [%]	
-	37.5 ± 2.5	97.9 ± 0.3	96.2 ± 0.8	87.4 ± 2.9	
	45.0 ± 5.0	98.2 ± 0.2	94.1 ± 0.7	85.7 ± 2.5	
<u>5</u>	55.0 ± 5.0	98.1 ± 0.2	94.8 ± 0.7	88.0 ± 2.6	
	65.0 ± 5.0	96.8 ± 0.3	93.7 ± 0.8	51.6 ± 8.8	
MA	75.0 ± 5.0	96.0 ± 0.4	92.4 ± 0.9	0.0 ± 2.8	
	85.0 ± 5.0	95.8 ± 0.4	88.3 ± 1.3	0.0 ± 4.5	
	95.0 ± 5.0	95.4 ± 0.4	59.4 ± 4.7	0.0 ± 5.6	
	107.5 ± 7.5	94.9 ± 0.4	19.2 ± 5.4	0.0 ± 8.3	
	122.5 ± 7.5	93.0 ± 0.6	3.2 ± 3.4	-	
	140.0 ± 10.0	90.0 ± 0.7	0.0 ± 3.3	-	
	165.0 ± 15.0	80.0 ± 1.2	0.0 ± 8.3	-	









FOOT General Meeting, June 2024

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Systematics to the measurement

1) Monte Carlo Closure Test:

- reconstruction of the MC with efficiencies applied (**MCreco**)
- comparison of MCreco with MC truth



study of the Monte Carlo reliability in assessing the efficiencies to be applied to experimental data: - define the **MCtruth** (EpsDet_DENO) = p(d, t), born in tgt, son of a primary particle, exiting the target, produced in $(\Theta \pm \triangle \Theta(4^{\circ}); \varphi \pm \triangle \varphi(4^{\circ}/6^{\circ} \otimes 32 \text{ deg}))$ [angular bin due to Multiple Scattering*]

[*the LYSO theoretical solid angle is $\Theta_{,\varphi} \pm 0.8^{\circ}$]







Systematics to the measurement

1) Monte Carlo Closure Test:

- mctrue = mc @ generation
- mcreco_meas = mc reco (no IDmatch) (Ekin MEAS)
- mcreco_true = mc reco IDmatch (Ekin GEN)
- mcreco_meas_cr = mc reco IDmatch (Ekin MEAS)
- mcTunf = mcreco_meas UNFOLDED with TUnfold (Ekin@gen)
- mcRoounf = mcreco_meas UNFOLDED with RooUnfold (Ekin@gen)







Systematics to the measurement

- 2) PID systematic: moving the p, d, t selection bands (hard and soft selection) and computing the average difference of XSec wrt the nominal selection (**syspid**)
- 3) EpsDet from a different simulation: instead of the FULL simulation use of the FLAT **simulation,** i.e. p,d,t produced within the target with a FLAT Ekin spectrum in the range [5 MeV/u - 1 GeV/u] (**sys**_{EpsDet})
- 4) Unfolding procedure: changing unfolding technique (RooUnfoldIDS) wrt the nominal one (RooUnfoldBayes) and compute the XSec difference (**sysunf**)
- 5) N¹²C from CNAO DDS: 4% relative error from dose-current conversion uncertainty (sys_{N12C})





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Protons detected at 90° Production XSection from 12C on PMMA target





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Protons detected at 60° Production XSection from 12C on PMMA target





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To compare with old data published in 2020, the XSections have to be normalized to the LYSO $\Delta\Omega$ ($\Theta \pm 4^{\circ}, \varphi \pm 4^{\circ}(6^{\circ}@32^{\circ})$)*:

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[*the LYSO theoretical solid angle is $\Theta_{,\varphi} \pm 0.8^{\circ}$]







PROTON PRODUCTION DIFFERENTIAL CROSS SECTION IN THE DIFFERENT ELEMENTS FROM CARBON ION BEAM ENERGY OF 221 MeV/u.

$E_{\rm him}^p$	δ_E	$d\sigma_{C}^{p}/dE_{k}$	-				\mathbf{p}	C 221			
[MeV]	[MeV]	[b/sr/MeV]									
90°		$\cdot 10^{-4}$	E_{kin}^p [MeV/u]	$rac{d\sigma^{MC}_{true}}{dE_k}$	$\operatorname{stat}_{reco}^{MC}$	sys_{PID}	sys_{reco}^{MC}	sys_{unf}^{MC}	$rac{d\sigma^{data}}{dE_k}$	$\operatorname{stat}^{data}$	sys^{data}
30-35	0	8.6 ± 1.3	000	10^{-5} [b/sr]	[%]	[%]	[%]	[%]	$.10^{-5}$ [b/sr]	[%]	[%]
35-40	2	5.2 ± 0.6	40 - 60	327 ± 0.4	8/		18.4		$\frac{10}{363 \pm 22 \pm 22}$	62	62
40-60	2	3.5 ± 0.2	60 - 80	165 ± 0.3	12 4		17.4	7.9	$30.5 \pm 2.2 \pm 2.2$ $21.2 \pm 1.0 \pm 1.8$	8.9	8.3
60-80	4	1.6 ± 0.1	80 - 100	81 ± 0.2	177	0.4	19.7	10.0	$11.9 \pm 1.6 \pm 1.3$	13.6	10.8
80-100	6	0.9 ± 0.1	100 - 120	4.0 ± 0.1	24.1	0.4	0.0	12.0	$4.6 \pm 0.8 \pm 0.6$	17.8	12.6
100-120	10	0.4 ± 0.1	120 - 140	2.2 ± 0.1	-0	0.4	-	-	$2.1 \pm 0.5 \pm 0.3$	23.8	12.6
120-140	14	0.2 ± 0.1	140 - 180	0.8 ± 0.0	-0	0.4	-	-	$1.0 \pm 0.3 \pm 0.1$	32.6	12.6
140-180	18	0.1 ± 0.1	180 - 250	0.2 ± 0.0	-0	0.4	-	_	-	-0	-
60°		$.10^{-4}$	250 - 350	-	-0	0.4	-	-	-	-0	-
30-35	2	244 + 34	350 - 550	-	-0	0.4	-	-	-	-0	-
35-40	2	184 ± 2.0	550 - 750	-	-0	0.4	-	-	-	-0	-
40-60		10.1 ± 2.0 14.4 ± 0.8	60°	$\cdot 10^{-5} \; [{\rm b/sr}]$	[%]	[%]	[%]	[%]	$\cdot 10^{-5}~\mathrm{[b/sr]}$	[%]	[%]
60-80		14.4 ± 0.0 10.0 ± 0.6	40 - 60	129.3 ± 0.8	4.1	1.1	9.1	5.6	$110.6 \pm 3.5 \pm 7.6$	3.2	6.9
80,100	5	63 ± 0.0	60 - 80	95.4 ± 0.7	4.9	1.1	8.2	3.1	$108.8 \pm 4.0 \pm 5.5$	3.7	5.0
100 120	9	0.3 ± 0.4 3.0 ± 0.2	80 - 100	67.2 ± 0.5	6.0	1.1	12.2	3.6	$81.1 \pm 3.5 \pm 4.4$	4.3	5.4
100-120	0	3.9 ± 0.2	100 - 120	42.7 ± 0.4	7.8	1.1	8.1	1.4	$59.4 \pm 3.3 \pm 2.5$	5.6	4.2
120-140	10	2.2 ± 0.1	120 - 140	24.1 ± 0.3	11.3	1.1	22.2	8.3	$44.8 \pm 3.4 \pm 4.1$	7.7	9.2
140-160	13	1.2 ± 0.1	140 - 160	13.2 ± 0.2	14.5	1.1	7.1	0.3	$34.9 \pm 3.7 \pm 1.4$	10.5	4.0
160-180	16	0.7 ± 0.1	160 - 180	7.0 ± 0.2	21.0	1.1	14.3	11.1	$25.2 \pm 3.9 \pm 3.0$	15.4	11.8
180-200	20	0.4 ± 0.1	180 - 200	4.1 ± 0.1	30.5		41.0	-	$23.3 \pm 5.5 \pm 2.8$	23.5	11.8
200-230	23	0.2 ± 0.1	200 - 230	1.9 ± 0.1	-0		-	-	$18.0 \pm 5.4 \pm 2.1$	30.0	11.8
230-260	27	0.1 ± 0.1	230 - 260	0.9 ± 0.1	-0		-	-	$9.7 \pm 4.3 \pm 1.2$	43.9	11.8
260-290	33	0.1 ± 0.1	260 - 290	0.5 ± 0.0	-0		-	-	$2.7 \pm 1.1 \pm 0.3$	41.2	11.8
290-350	40	-	290 - 350	0.2 ± 0.0	-0		-	-	$1.8 \pm 1.1 \pm 0.2$	60.6	11.8
	•	· · · · · · · · · · · · · · · · · · ·		0.0 ± 0.0	-0		-	-	-	-0	-
			450 - 050	-	-0		-	-	-	-0	-
			000 - 800	-	-0	1.1	-	-	- 	-0	-

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90°	RATIO NE
40-60	1.0
60-80	1.3
80-100	1.3
100-120	1.1
120-140	1.0
140-180	1.0
180-250	_

60°	RATIO N
40-60	0.7
60-80	1.(
80-100	1.2
100-120	1.5
120-140	2.0
140-160	2.9
160-180	3.6
180-200	5.8
200-230	9.(
230-260	9.7
260-290	2.7
290-350	-







$\begin{bmatrix} \mathrm{E}_{kin}^{C} \\ [MeV/u] \end{bmatrix}$	σ_C^p [barn /sr]	σ_O^p [barn /sr]	σ_{H}^{p} [barn /sr]		90°	RATIO NEW/OLD bin s	um RATIO NEW/OLD 1 bi	n
90°	10^{-3}	10^{-3}	10^{-5}		115	0.62	0.67	
115	8.97 ± 0.63	12.77 ± 2.48	11.44 ± 7.88		153	0.77	0.78	
153	12.45 ± 0.89	19.52 ± 3.29	6.25 ± 9.43		221	0.83	0.83	
221	18.87 ± 1.22 23.58 ± 1.50	27.43 ± 4.48 33.17 ± 5.24	16.28 ± 19.0 6.78 ± 19.62	8	281	0.84	0.79	
353	28.23 ± 1.76	44.35 ± 6.08	25.05 ± 29.1	5	252	0.04	0.70	
60 ^o	$\cdot 10^{-2}$	$\cdot 10^{-2}$	$.10^{-2}$		303	0.03	0.03	
115	5.84 ± 0.52	7.68 ± 1.06	0.50 ± 0.23			60°	RATIO NEW/OLD bin sum	RATIO NEW/OLD
153 221	7.90 ± 0.74 10.99 ± 1.02	9.90 ± 1.36 15.12 ± 1.90	$\begin{array}{c c} 0.69 \pm 0.29 \\ 1.10 \pm 0.37 \end{array}$			115	0.89	0.86
281	12.92 ± 1.19 14.75 ± 1.36	18.10 ± 2.19 21.36 \pm 2.48	1.38 ± 0.40 1.38 ± 0.44			153	0.86	0.82
	14.75 ± 1.50	21.30 ± 2.40	1.50 ± 0.44			221	0.98	0.90
			$\mathbf{p} \mathbf{C}$	1 bi	n - eff ave	281	0.99	0.90
						353	1.08	0.95

							303			1.06	0.95)
E_{kin}^C [MeV/u]	σ^{MC}_{true}	$\operatorname{stat}_{reco}^{MC}$	sys_{PID}	sys_{reco}^{MC}	sys_{unf}^{MC}	σ^{data}	$stat^{data}$	sys^{data}				
90°	$\cdot 10^{-3} [\rm b/sr]$	[%]	[%]	[%]	[%]	$\cdot 10^{-3} [\rm b/sr]$	[%]	[%]	Bin s	um σ^{data}	$stat^{data}$	sys^d
115	6.3 ± 0.1	8.3	0.3	7.1	3.4	$6.0 \pm 0.4 \pm 0.3$	6.3	5.3		$\cdot 10^{-3} [{\rm b/sr}]$	[%]	[%
150	9.0 ± 0.1	7.2	0.4	6.4	3.1	$9.7 \pm 0.5 \pm 0.5$	5.4	5.1		$5.6 \pm 0.4 \pm 0.3$	6.5	5.
221	13.1 ± 0.1	6.0	0.4	8.3	1.3	$15.6 \pm 0.7 \pm 0.7$	4.5	4.2		$9.6 \pm 0.5 \pm 0.5$	5.6	5.
279	16.3 ± 0.1	5.1	0.5	5.8	3.5	$18.7 \pm 0.7 \pm 1.0$	3.9	5.3		$15.6 \pm 0.7 \pm 0.7$	4.5	4.
351	20.1 ± 0.1	4.7	0.6	6.4	2.0	$23.5 \pm 0.8 \pm 1.1$	3.5	4.5		$19.9 \pm 1.0 \pm 1.1$		5.
60 ^o	$\cdot 10^{-2} [b/sr]$	[%]	[%]	[%]	[%]	$\cdot 10^{-2} [b/sr]$	[%]	[%]	·	$\frac{24.0 \pm 0.9 \pm 1.1}{\cdot 10^{-2} \text{ [b/sr]}}$	[%]	[27]
115	4.2 ± 0.0	3.4	0.6	13.2	0.5	$5.0 \pm 0.1 \pm 0.2$	2.5	4.0		1000000000000000000000000000000000000	4.2	4.
150	4.0 ± 0.0	3.4	0.8	10.3	1.2	$6.5 \pm 0.2 \pm 0.3$	2.4	4.2		$6.8 \pm 0.3 \pm 0.3$	3.9	4.
221	7.8 ± 0.0	2.5	1.1	8.5	2.5	$9.9 \pm 0.2 \pm 0.5$	1.8	4.7		$10.8 \pm 0.3 \pm 0.5$	2.9	4.
279	10.6 ± 0.0	2.1	1.3	7.6	1.7	$11.6 \pm 0.2 \pm 0.5$	1.6	4.4		$12.8 \pm 0.4 \pm 0.6$	2.8	4.
351	12.9 ± 0.0	2.0	1.5	5.3	2.0	$14.0 \pm 0.2 \pm 0.6$	1.5	4.5		$15.9 \pm 0.4 \pm 0.7$	2.3	4.
			1 10.13	80.43	80.43					FOOT Generation	al Meeting, J	une





The **remaining difference** between the **old** published analysis and the new analysis is due to the Multiple Scattering that has been taken into account in the detection efficiency of new analysis and has NOT in the old analysis



[*the LYSO theoretical solid angle is $\Theta, \varphi \pm 0.8^{\circ}$]

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Conclusions

- Small effort more to assess the 32deg analysis normalization
- The systematic errors from detection efficiency and PID selection have to be added to the total systematic error



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	E_{kin}^p [MeV/u]	$\frac{d\sigma^{MC}_{true}}{dE_k}$	$\operatorname{stat}_{reco}^{MC}$	sys_{PID}	sys_{reco}^{MC}	sys_{unf}^{MC}	$rac{d\sigma^{data}}{dE_k}$	$\operatorname{stat}^{data}$
	90°	$\cdot 10^{-6}$ [b]	[%]	[%]	[%]	[%]	$\cdot 10^{-6}$ [b]	[%]
	40 - 60	3.5 ± 0.1	11.1	0.5	20.9	2.4	$3.6 \pm 0.3 \pm 0.2$	8.0
15	60 - 80	1.4 ± 0.0	17.1	0.5	0.0	6.0	$1.4\pm0.2\pm0.1$	13.1
	80 - 100	0.7 ± 0.0	26.1	0.5	7.1	6.4	$0.4\pm0.1\pm0.0$	20.4
	100 - 120	0.3 ± 0.0	-	0.5	-	-	-	-
	120 - 140	0.1 ± 0.0	-	0.5	-	-	-	-
	140 - 180	0.0 ± 0.0	-	0.5	-	-	-	-
n	180 - 250	-	-	0.5	-	-	-	-
	250 - 350	-	-	0.5	-	-	-	-
	350 - 550	-	-	0.5	-	-	-	-
	550 - 750	-	-	0.5	-	-	-	-
	60°	$\cdot 10^{-6} [b]$	[%]	[%]	[%]	[%]	$\cdot 10^{-6} [b]$	[%]
	40 - 60	15.1 ± 0.1	5.1	0.7	16.7	0.8	$15.7 \pm 0.6 \pm 0.6$	3.8
	60 - 80	10.0 ± 0.1	6.6	0.7	16.5	4.3	$12.0 \pm 0.6 \pm 0.7$	4.7
	80 - 100	5.3 ± 0.1	9.1	0.7	1.5	8.7	$7.0 \pm 0.5 \pm 0.7$	6.7
_	100 - 120	2.4 ± 0.0	13.3	0.7	11.0	4.2	$3.5 \pm 0.3 \pm 0.2$	9.5
	120 - 140	1.2 ± 0.0	18.9	0.7	15.0	13.9	$1.7\pm0.2\pm0.2$	13.1
	140 - 160	0.6 ± 0.0	28.9	0.7	28.6	29.8	$1.4\pm0.3\pm0.4$	21.9
	160 - 180	0.3 ± 0.0	-	0.7	-	-	$0.5 \pm 0.1 \pm 0.2$	25.3
L	180 - 200	0.2 ± 0.0	-	0.7	-	-	$0.3 \pm 0.1 \pm 0.1$	33.6
	200 - 230	0.1 ± 0.0	-	0.7	-	-	$1.0\pm1.0\pm0.3$	97.0
	230 - 260	0.0 ± 0.0	-	0.7	-	-	-	-
	260 - 290	0.0 ± 0.0	-	0.7	-	-	-	-
	290 - 350	-	-	0.7	-	-	-	-
	350 - 450	-	-	0.7	-	-	-	-
250 //u]	450 - 650	-	-	0.7	-	-	-	-
	650 - 850	-	-	0.7	-	-	-	-
	32^{o}	$\cdot 10^{-6}$ [b]	[%]	[%]	[%]	[%]	$\cdot 10^{-6}$ [b]	[%]
	40 - 50	4.2 ± 0.0	4.1	1.3	10.8	0.5	$3.1\pm0.1\pm0.1$	3.8
	50 - 60	3.9 ± 0.0	4.2	1.3	2.0	7.4	$3.7 \pm 0.2 \pm 0.3$	4.1
	60 - 70	3.7 ± 0.0	4.2	1.3	6.7	4.7	$2.9 \pm 0.1 \pm 0.2$	4.2
	70 - 80	3.4 ± 0.0	4.6	1.3	4.8	5.8	$2.7\pm0.1\pm0.2$	4.5
	80 - 90	3.1 ± 0.0	4.9	1.3	5.4	0.9	$2.3\pm0.1\pm0.1$	4.6
	90 - 100	2.7 ± 0.0	5.2	1.3	10.9	7.4	$1.6 \pm 0.1 \pm 0.1$	4.9
	100 - 115	2.3 ± 0.0	4.9	1.3	8.0	0.9	$1.2\pm0.1\pm0.0$	5.1
	115 - 130	1.7 ± 0.0	5.8	1.3	12.1	8.0	$0.8 \pm 0.0 \pm 0.1$	5.7
	130 - 150	1.1 ± 0.0	6.2	1.3	7.1	3.4	$0.6 \pm 0.0 \pm 0.0$	6.3
	150 - 180	0.5 ± 0.0	7.7	1.3	3.0	2.6	$0.3 \pm 0.0 \pm 0.0$	8.8

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Conclusions

- Small effort more to assess the 32deg analysis normalization
- The systematic errors from detection efficiency and PID selection have to be added to the total systematic error
- Comparison with FLUKA model and other published data can be shown...



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Conclusions

- Small effort more to assess the 32deg analysis normalization
- The systematic errors from detection efficiency and PID selection have to be added to the total systematic error
- Comparison with FLUKA model and other published data can be shown...

...But the analysis is done :)

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Thank you for the Attention

(...and the patience...)

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