



# GSI2021 analysis without tracking

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Collaboration Meeting

# Cross section measurement

With available data total integrated and angle differential cross section are achievable (no kinetic energy)

$$\Delta\sigma(Z) = \int_{\beta_{\min}}^{\beta_{\max}} \int_0^{\theta_{\max}} \left( \frac{\partial^2 \sigma}{\partial \theta \partial \beta} \right) d\theta d\beta = \frac{Y(Z)}{N_{\text{prim}} \cdot N_{\text{TG}} \cdot \epsilon(Z)}$$

Align FOOT detectors and estimate angular acceptance

Extract fragment yields from TW

Calculate MC efficiencies for fragments

Evaluate the beta range from data and put in MC for efficiency calculations

# Cross section measurement

With available data total integrated and angle differential cross section are achievable (no kinetic energy)

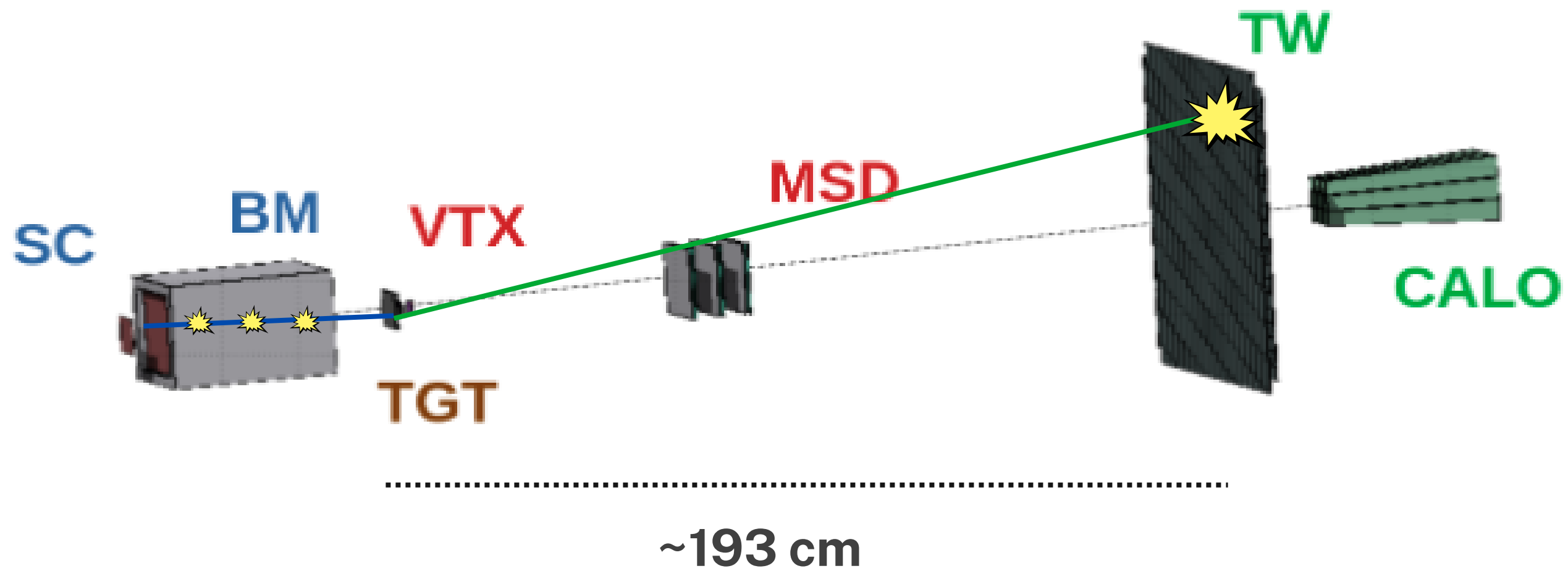
$$\frac{d\sigma}{d\theta}(Z) = \frac{Y(Z, \theta)}{N_{\text{prim}} \cdot N_{\text{TG}} \cdot \Delta\theta \cdot \varepsilon(Z, \theta)}$$

Align FOOT detectors and estimate angular acceptance

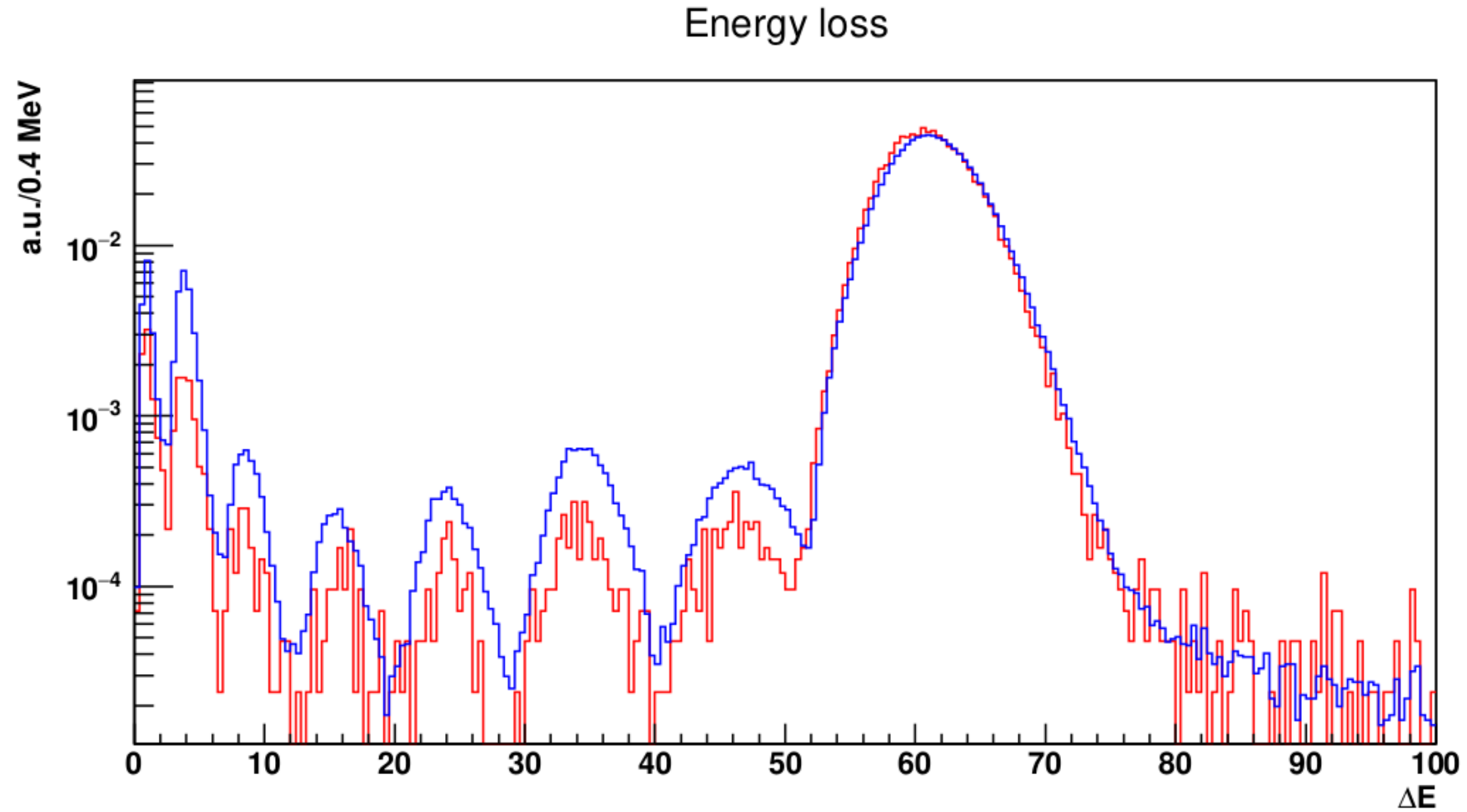
Extract fragment yields from TW

Calculate MC efficiencies for fragments

# Angle measurement



# Why background subtraction?





# Conclusions

**Background subtraction strategy seems to work also for angle differential cross sections**

**Purity correction implemented(very important for Li and Be)**

**Good agreement in MC closure test except for first bin of C and N**

**Angle unfolding machinery ready to be performed**

**Very few statistics for background reduces final number of bins**

**Comparison with “with tracking analysis” ongoing (and promising!) (Giacomo’s talk)**

# Conclusions

from Trento  
GM

**Background subtraction strategy seems to work also for angle differential cross sections**

**Purity correction implemented(very important for Li and Be)**

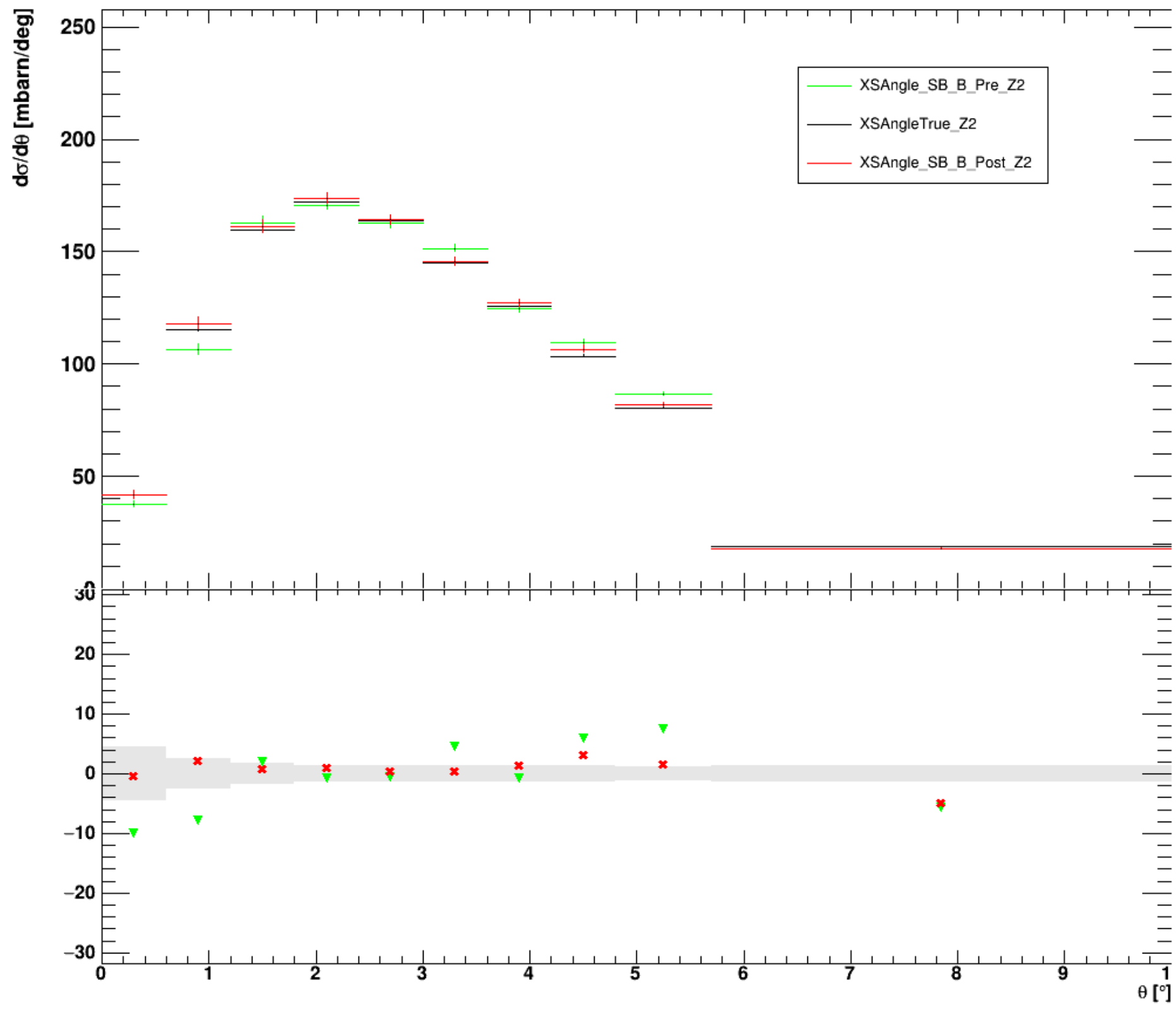
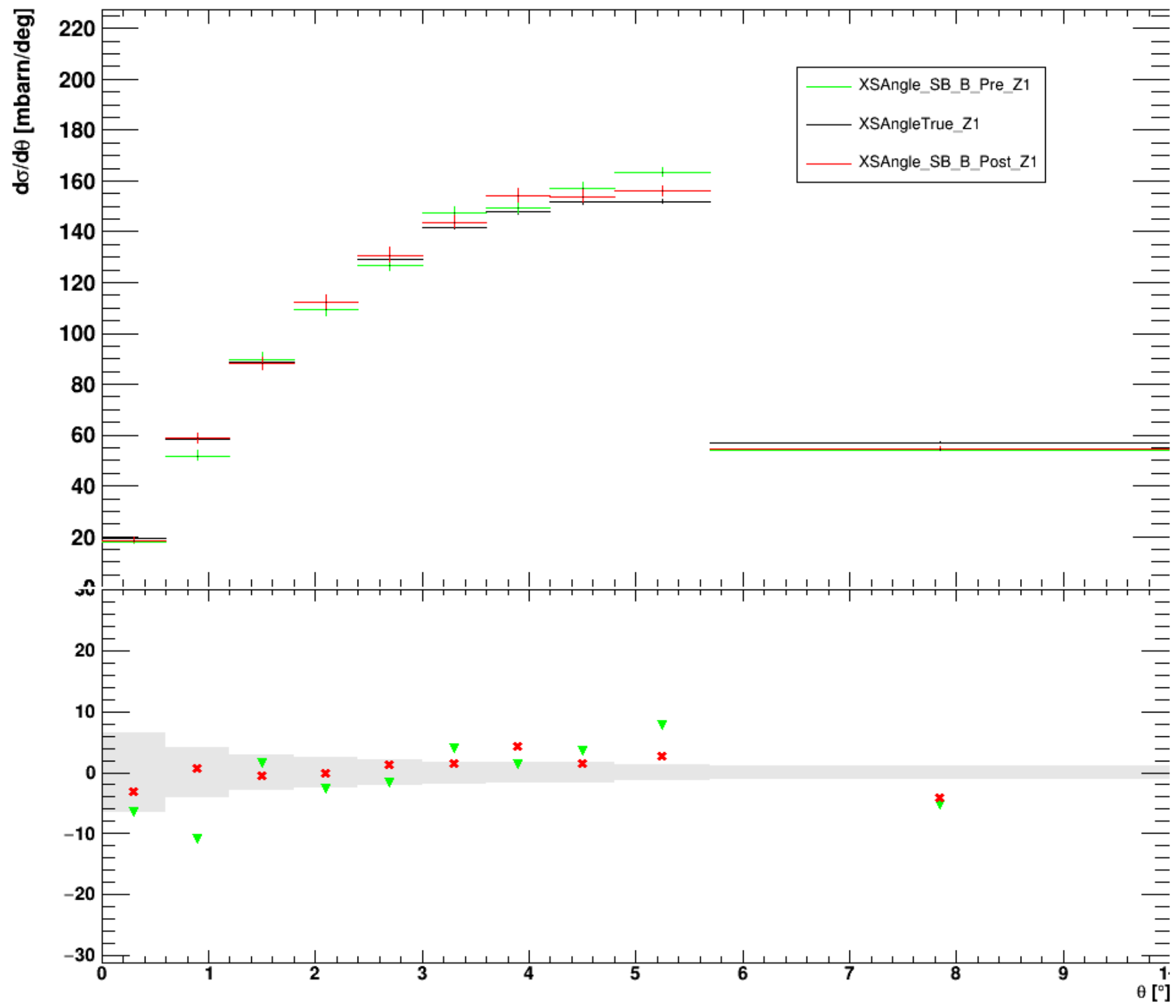
**Good agreement in MC closure test except for first bin of C and N**

**Angle unfolding machinery ready to be performed**

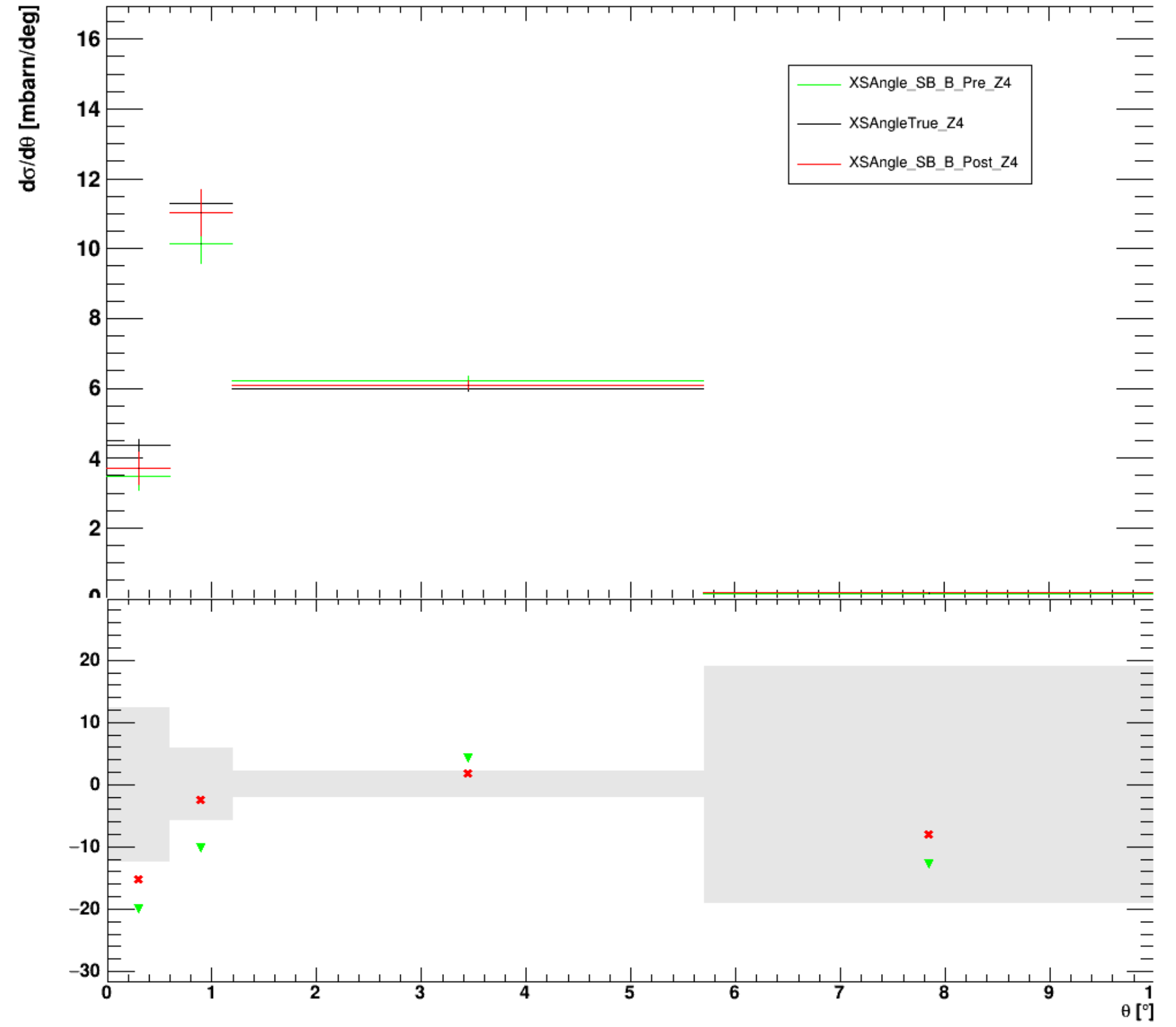
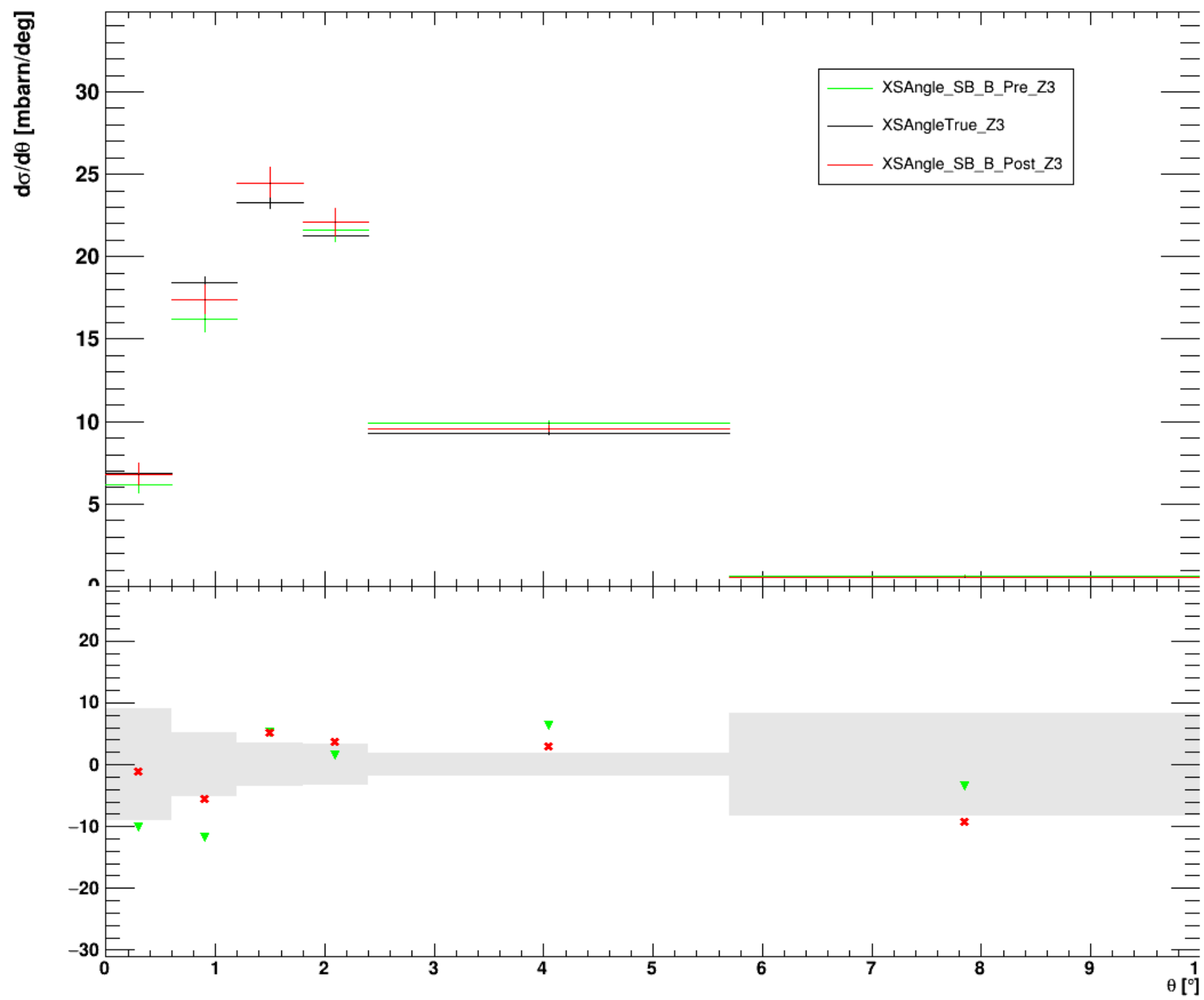
**Very few statistics for background reduces final number of bins**

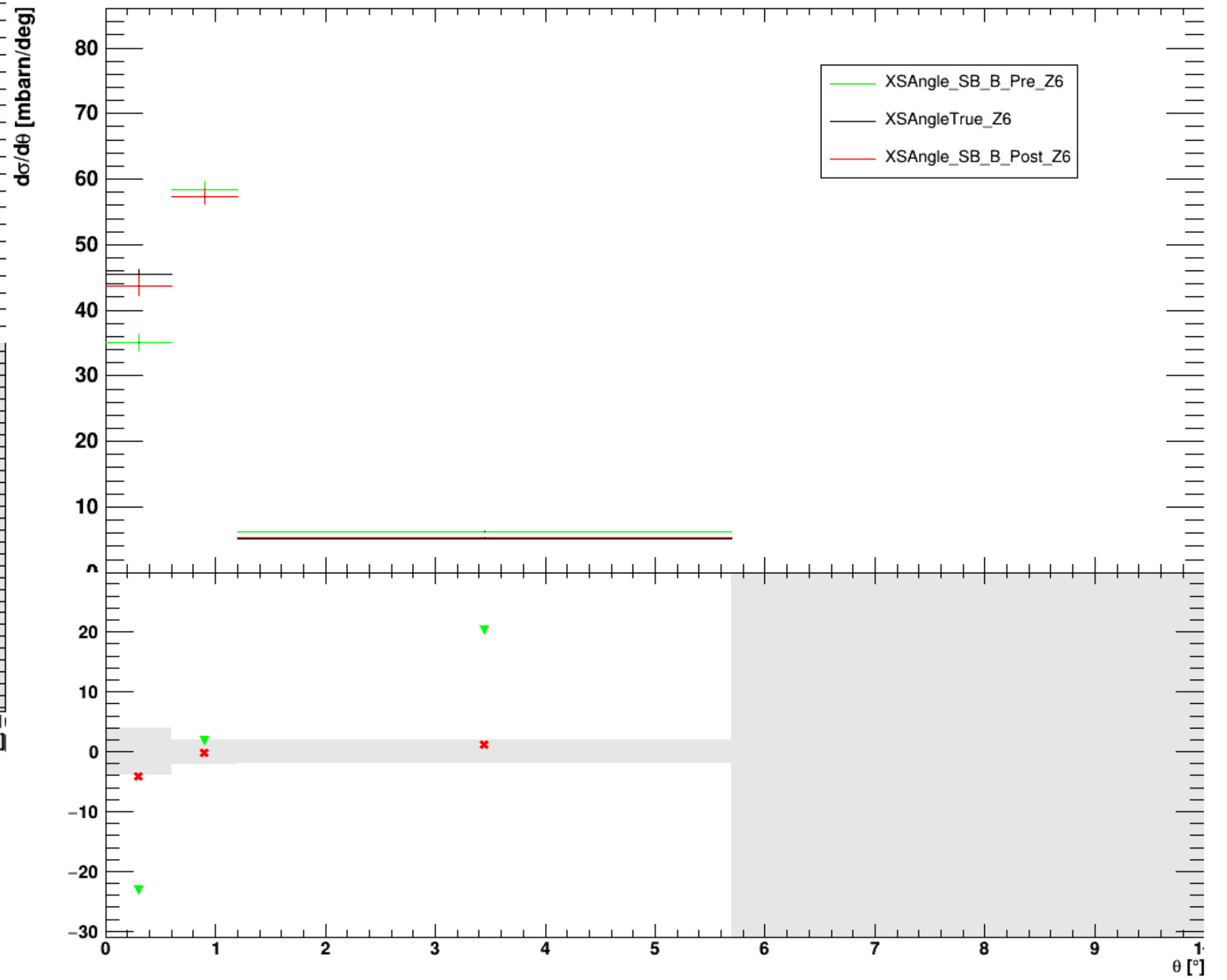
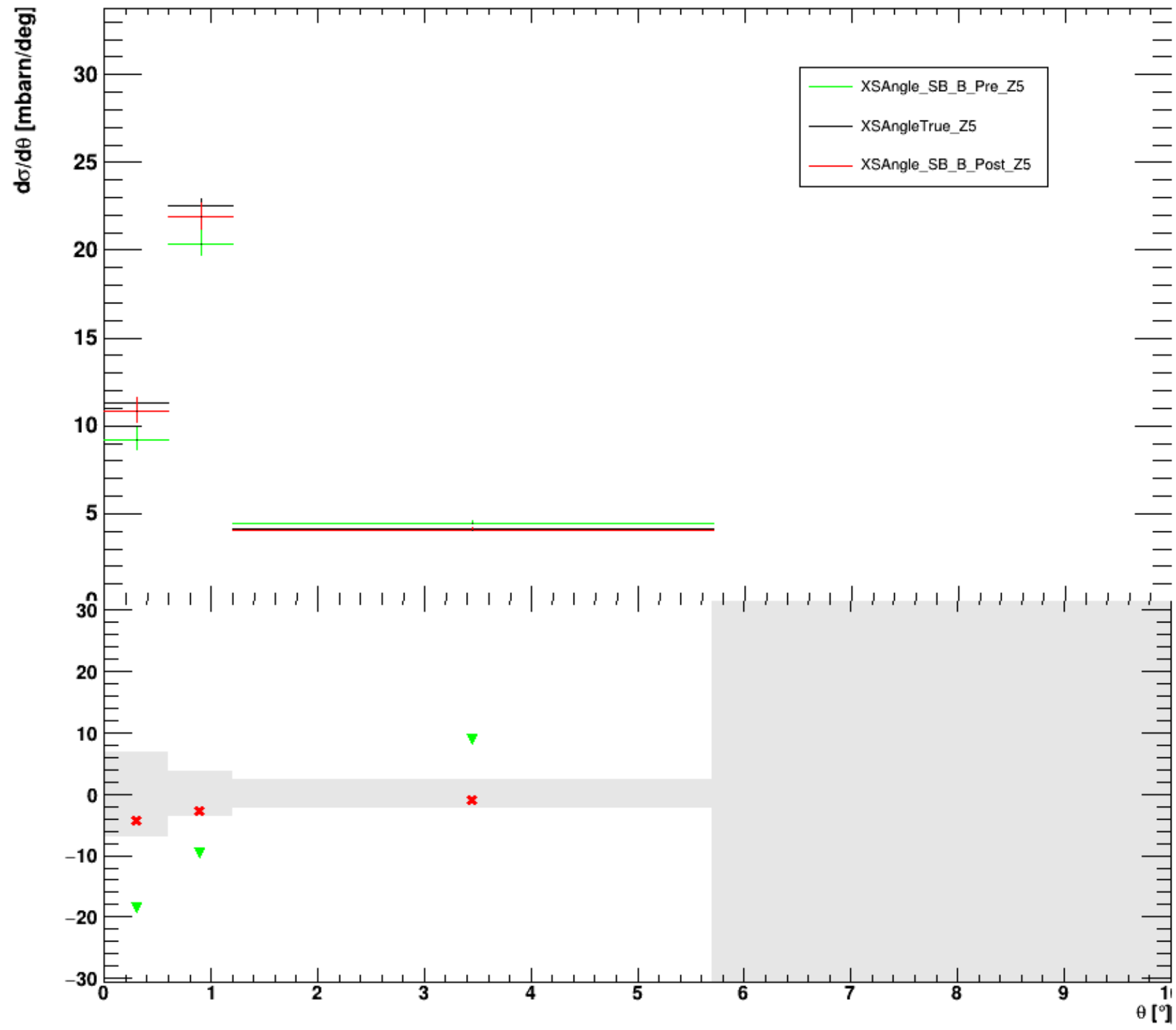
**Comparison with “with tracking analysis” ongoing (and promising!) (Giacomo’s talk)**

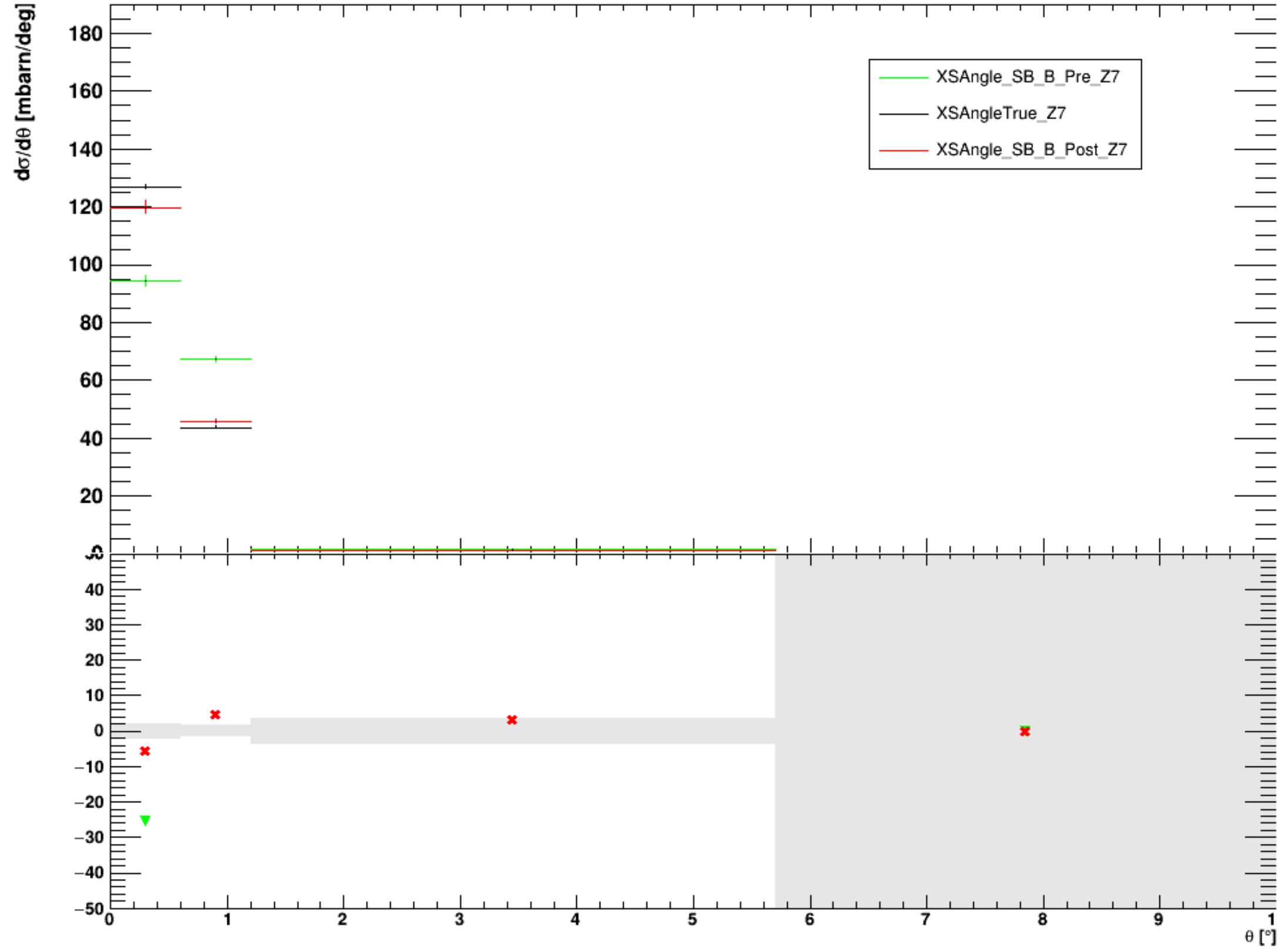


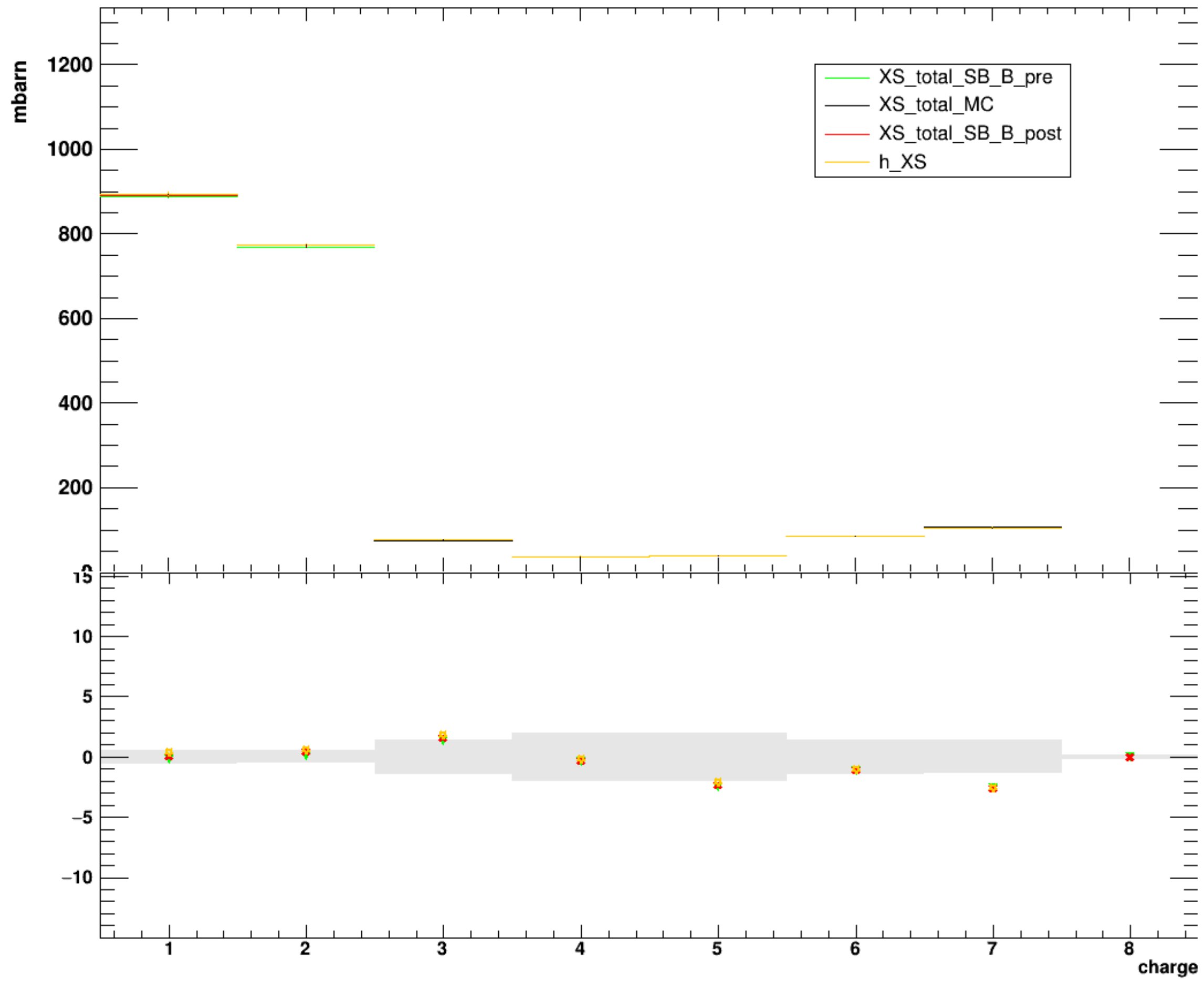












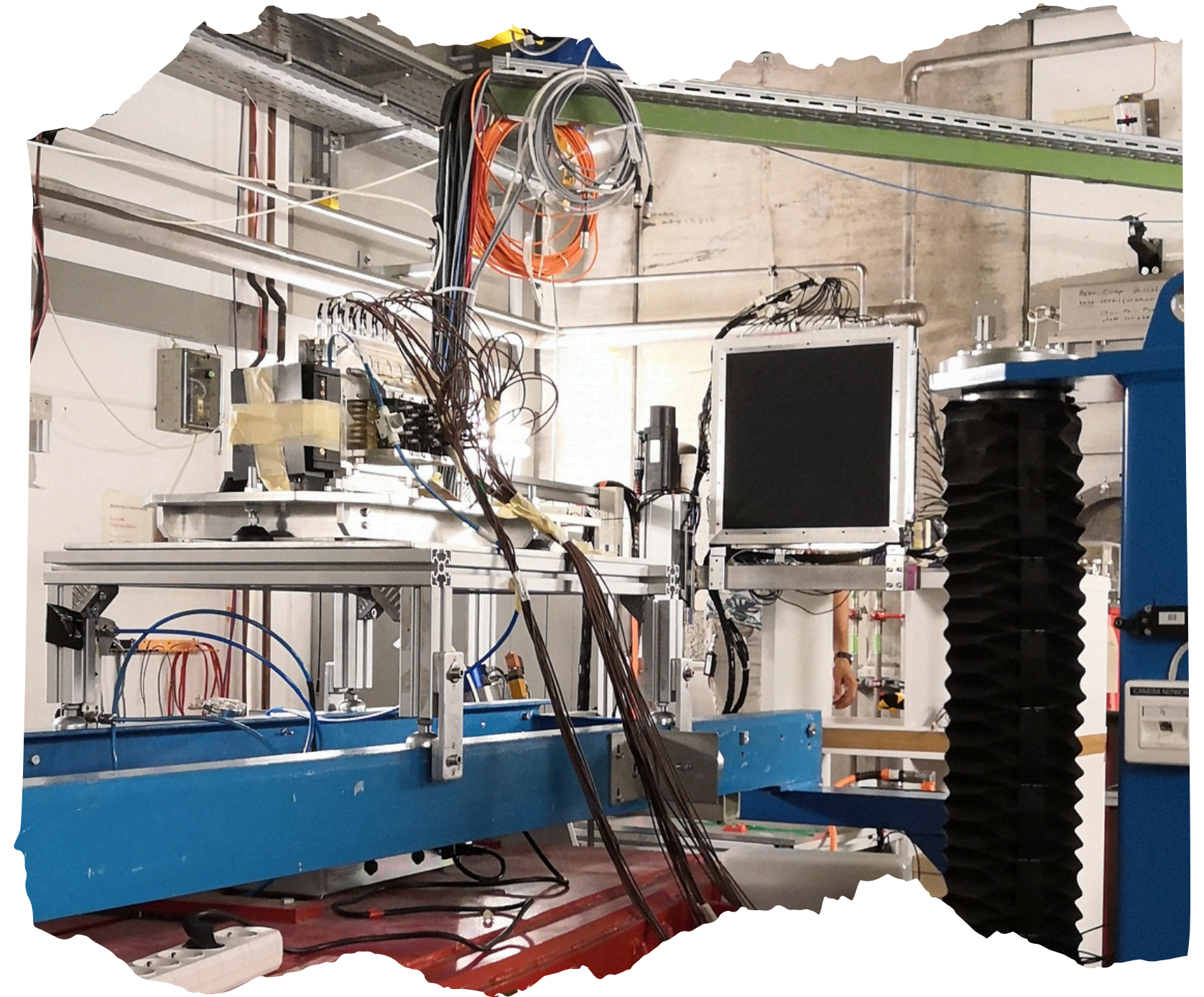


# Data analysis

Run on data with the same steps of MC analysis

400 MeV/u  $^{16}\text{O}$  beam on 5mm Carbon target

Run	Trigger type	Target	Events
4305	MB	C	162102
4306	MB	C	577096
4307	MB	C	513370
4308	Frag + MB	C	510169
4309	Frag + MB	C	531812
4310	Frag + MB	C	1012099
4313	MB	no	57133



# New analysis flow

Evaluate efficiencies and purities

Repeat for with and w/o target samples

Apply reconstruction cuts (SC, BM)

Normalize yields and subtract background

Apply efficiency and purity for fragmentation in target

Unfolding

Calculate angular cross sections

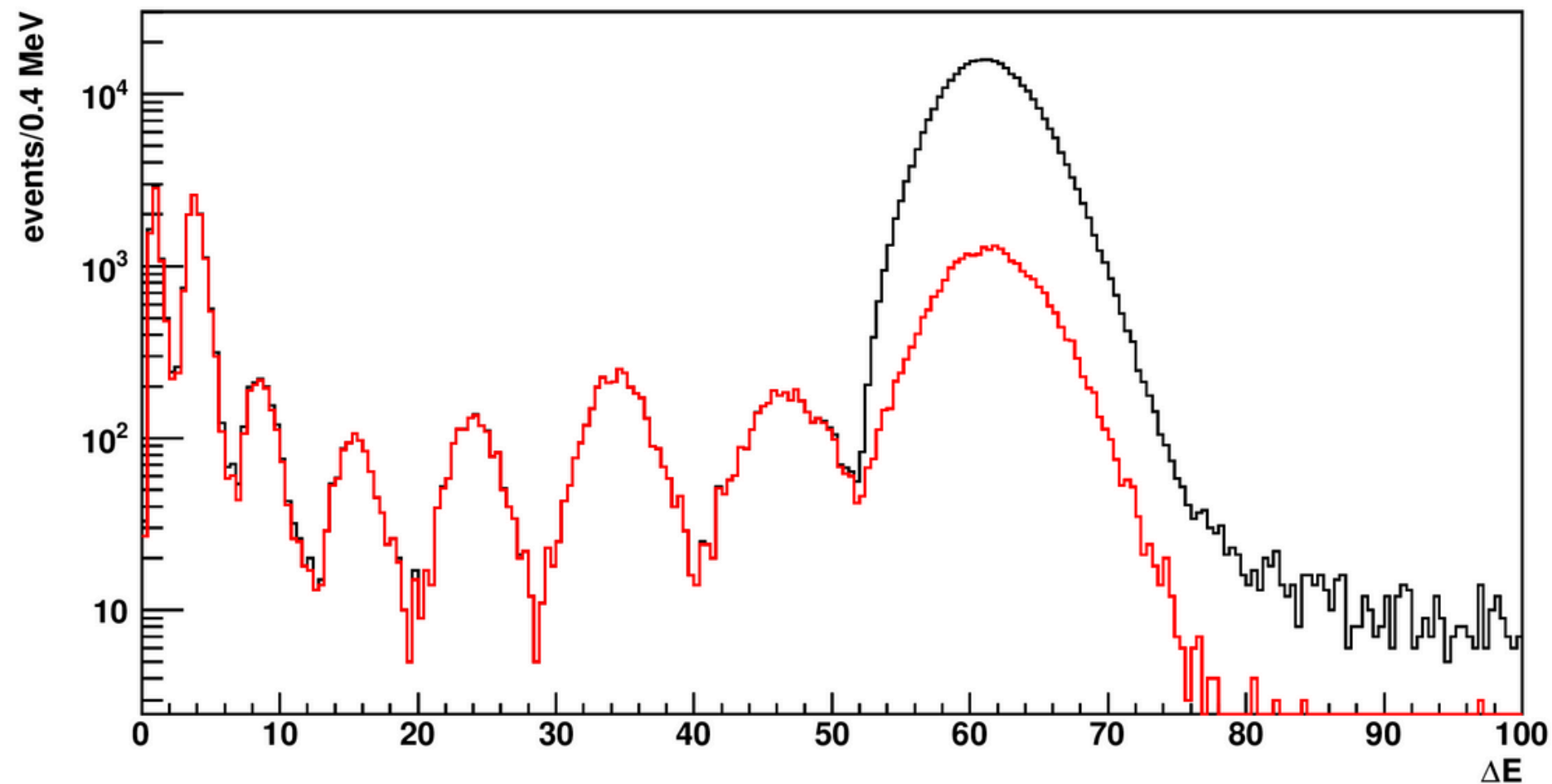
Add systematics uncertainties

# Data analysis

In MB runs the number of primaries is the number of events passing selection cuts

In fragmentation runs the number of primaries has to take into account the trigger rejection factor

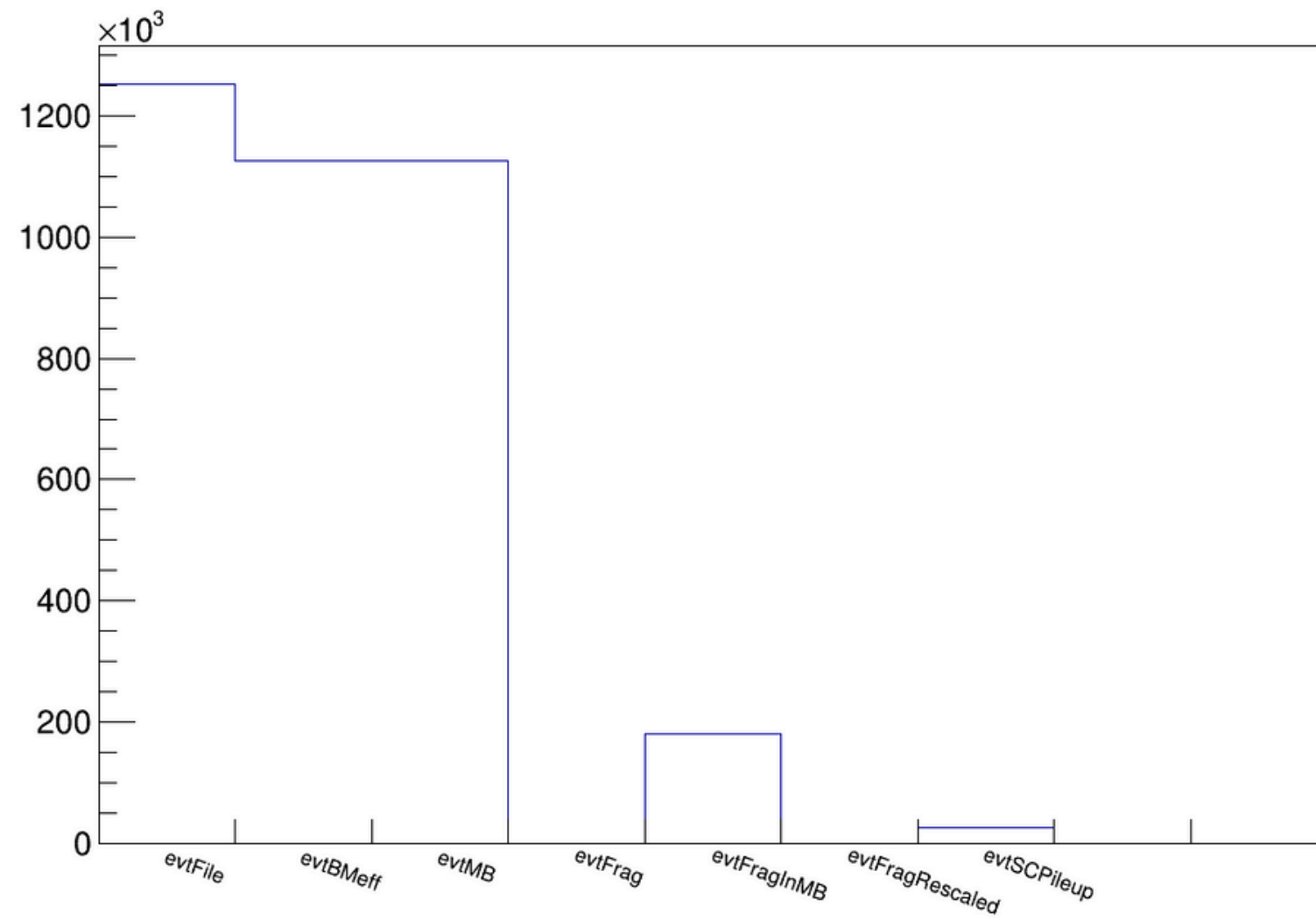
It can be evaluated from MB runs (fragmentation flag: ON)



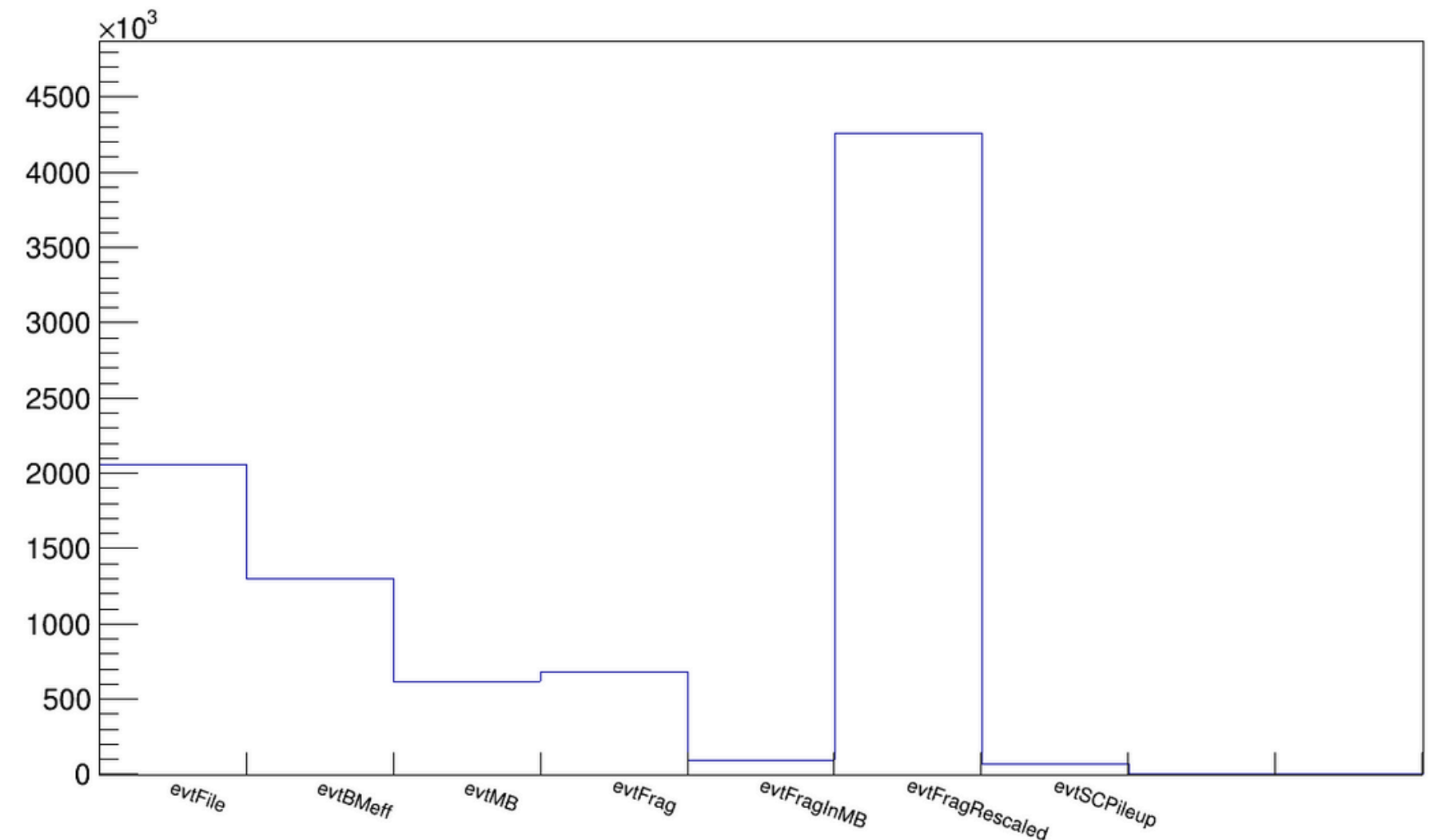


# Number of events

Minimum bias (4305,4306,4307)



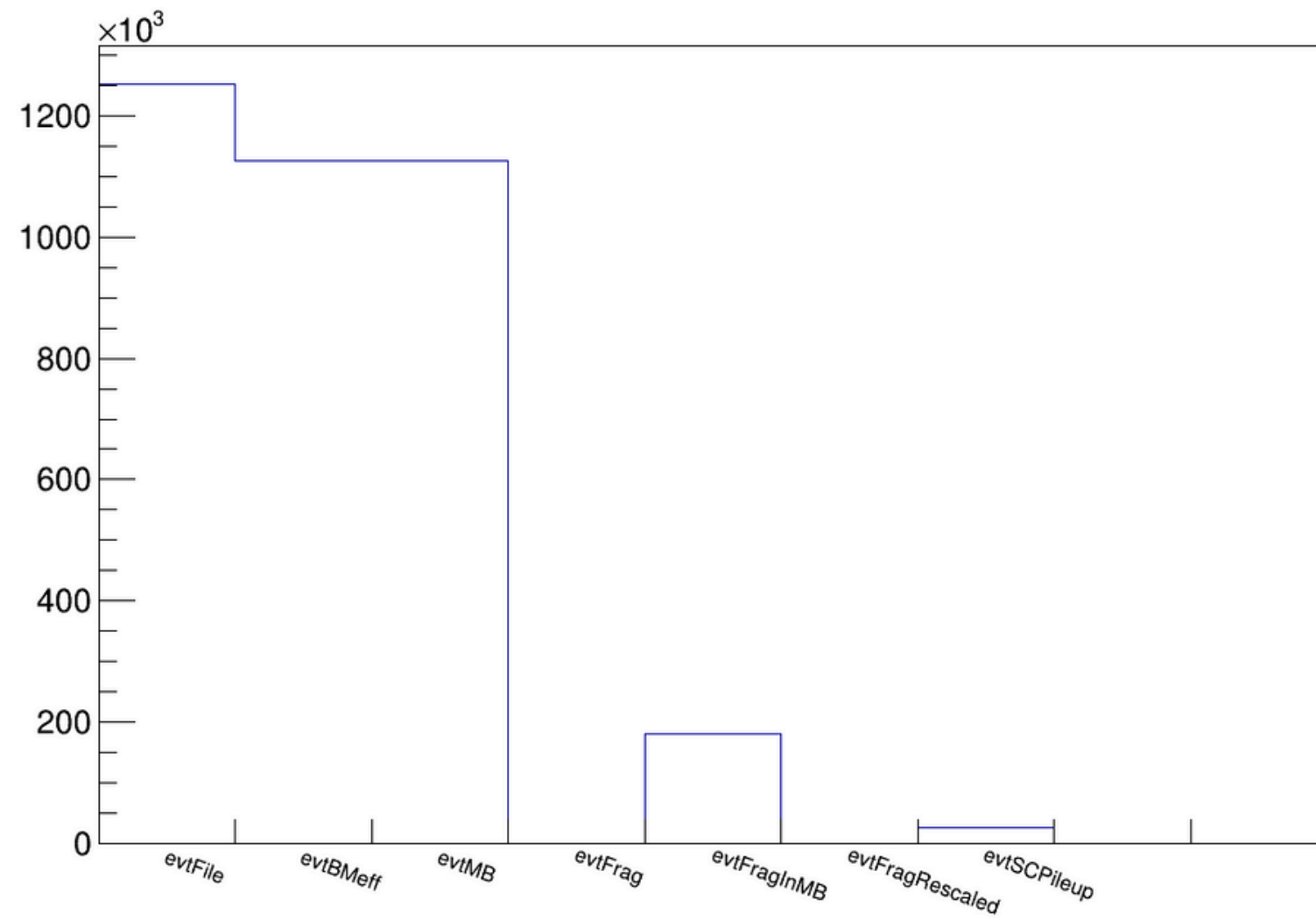
Fragmentation+MB (4308, 4309, 4310)



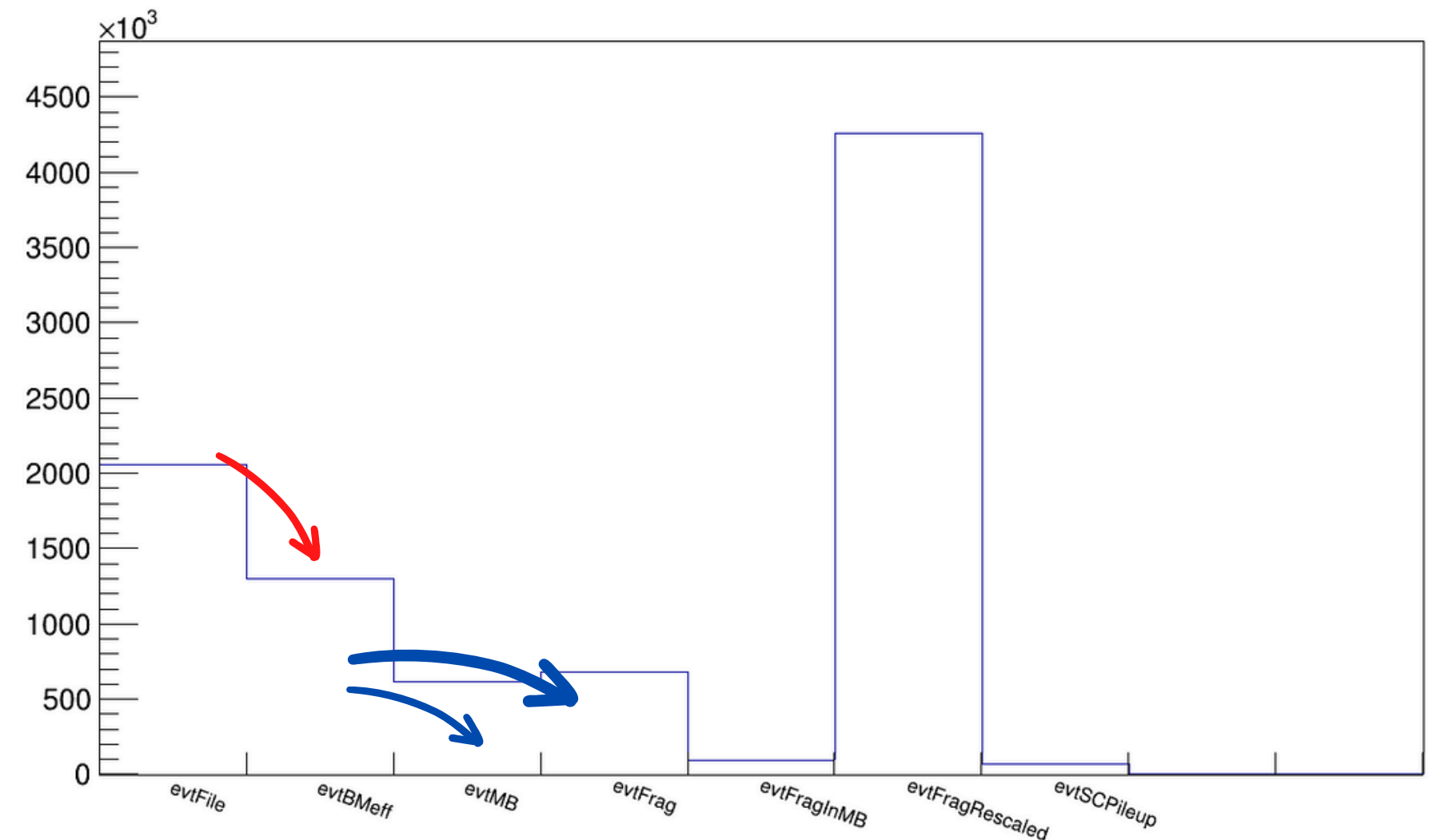


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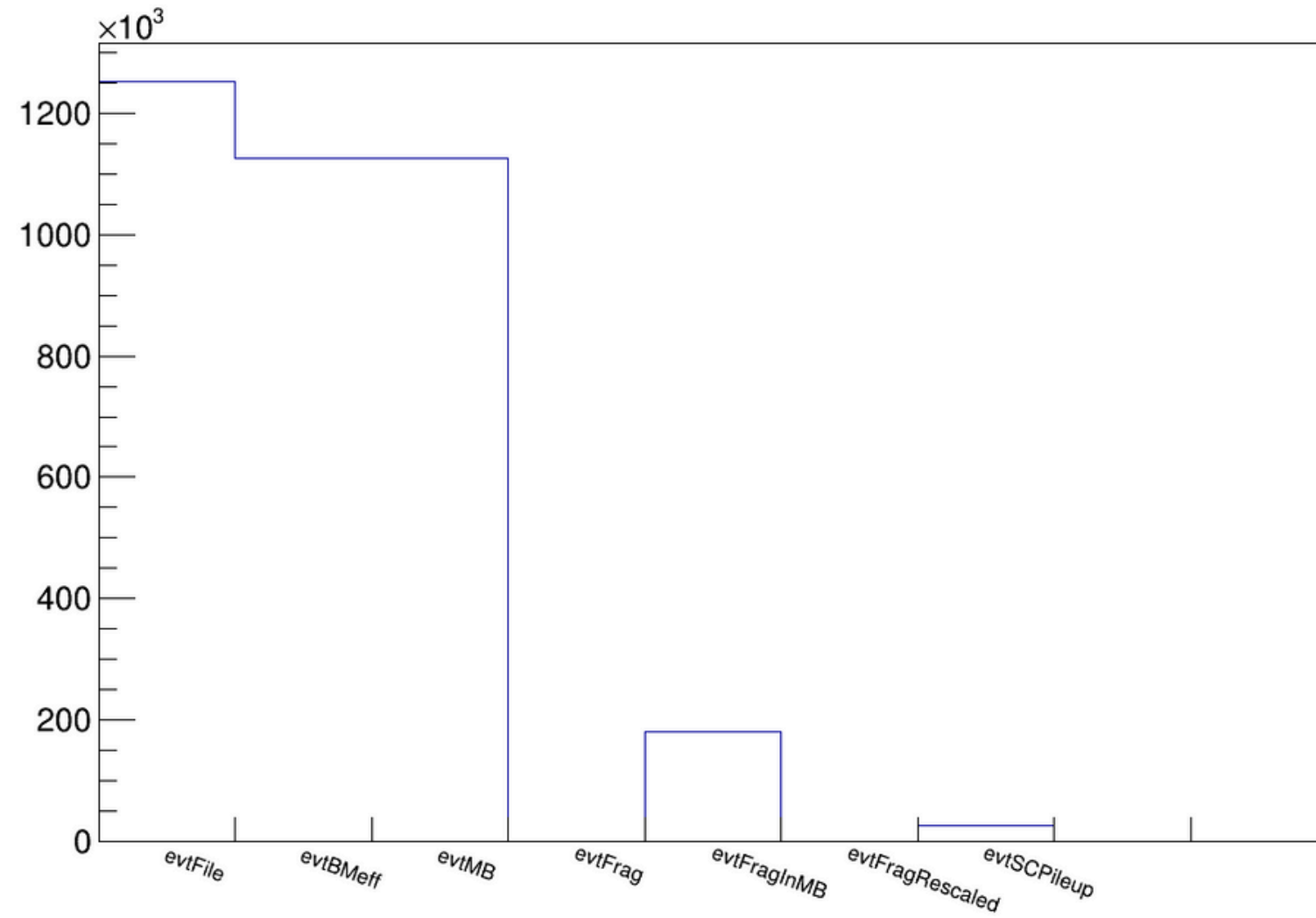


Fragmentation+MB (4308, 4309, 4310)

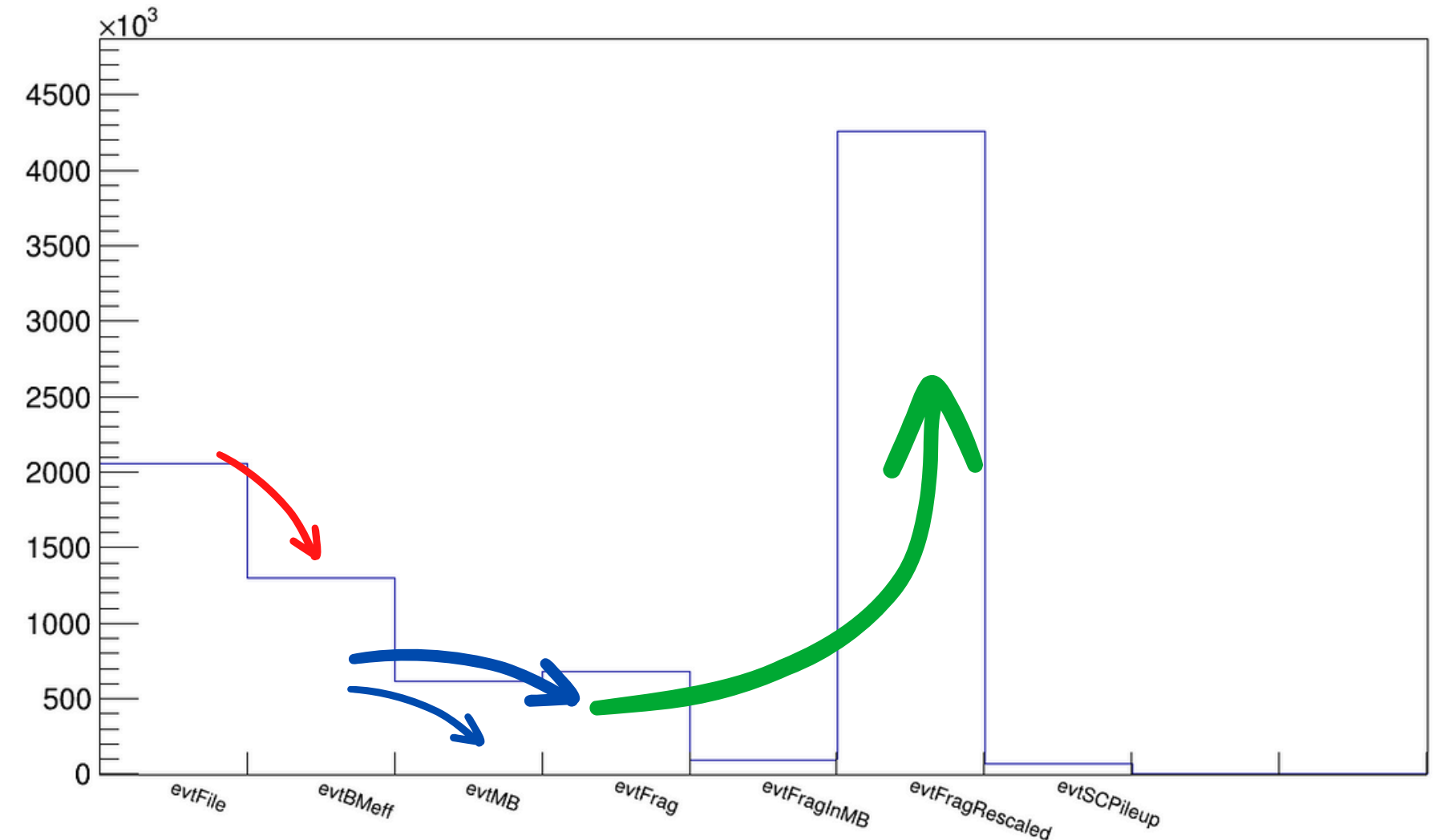


# Number of events

Minimum bias (4305,4306,4307)



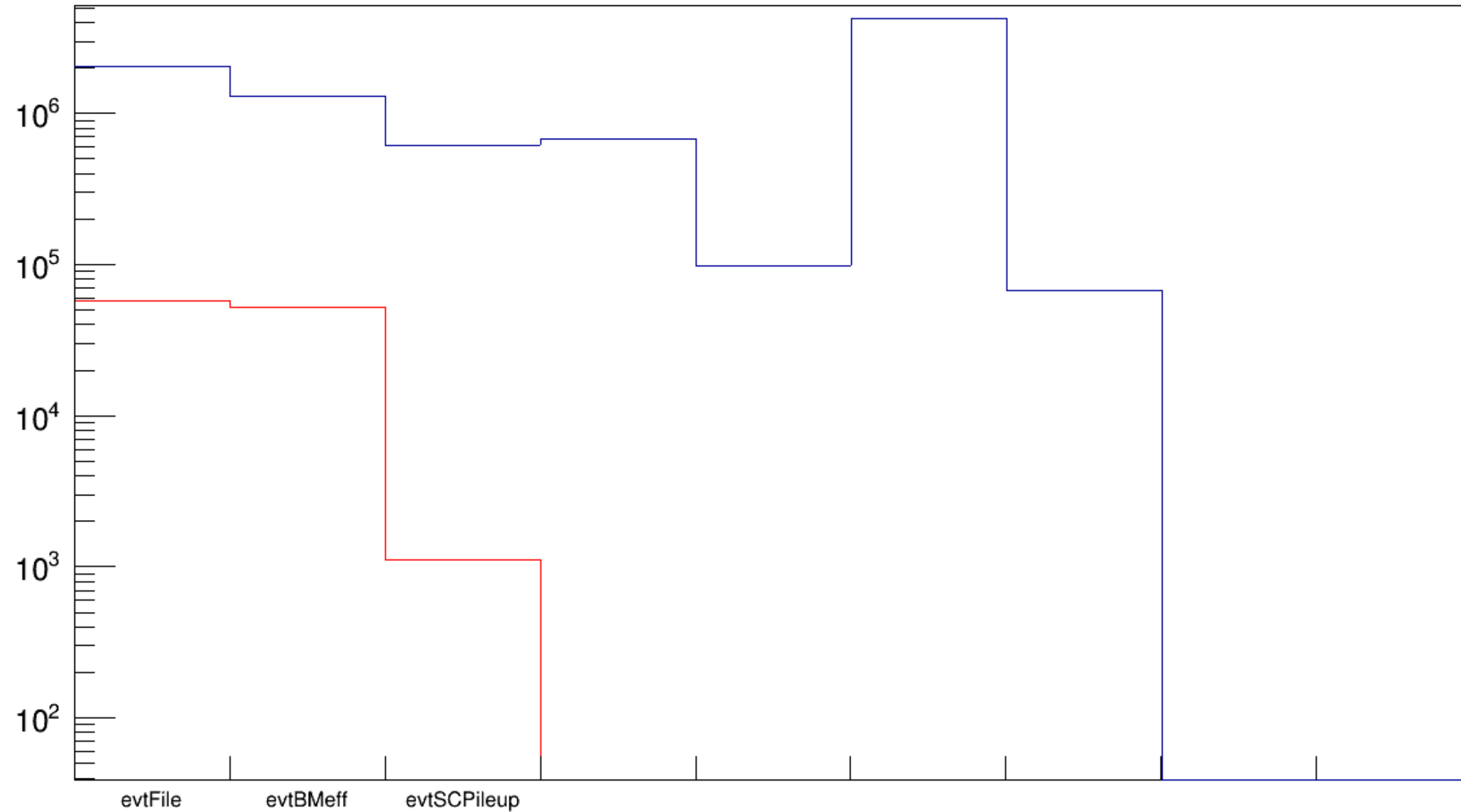
Fragmentation+MB (4308, 4309, 4310)



# Number of events

Fragmentation+MB (4308, 4309, 4310)

Background MB (4313)



# Impact of statistics on XS resolution

## Relative uncertainties in XS (only stat)

$$\sigma(Z) = \frac{1}{N_{\text{TG}} \cdot \varepsilon(Z)} \cdot \left( \frac{Y_S(Z)}{N_S} - \frac{Y_B(Z)}{N_B} \right) = \frac{1}{N_{\text{TG}} \cdot \varepsilon(Z)} \cdot (S(Z) - B(Z))$$

$$\frac{\Delta\sigma}{\sigma} \approx \left( \frac{1}{S - B} \right) \cdot \sqrt{S^2 \cdot \left[ \left( \frac{\Delta Y_S}{Y_S} \right)^2 + \left( \frac{\Delta N_S}{N_S} \right)^2 \right] + B^2 \cdot \left[ \left( \frac{\Delta Y_B}{Y_B} \right)^2 + \left( \frac{\Delta N_B}{N_B} \right)^2 \right]}$$

Fragmentation physics

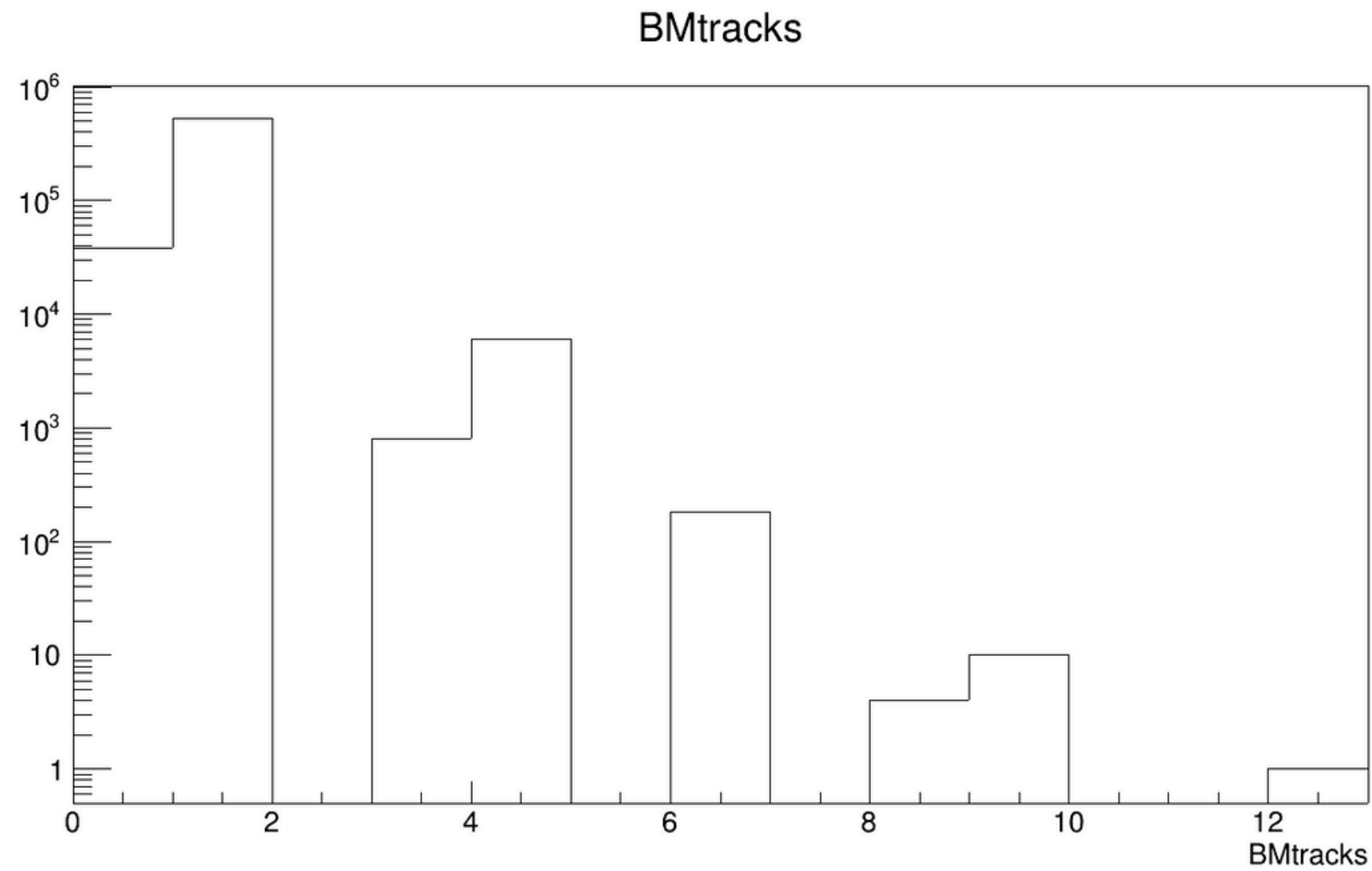
Available Statistics

$$S = \frac{Y_S}{N_S} \quad B = \frac{Y_B}{N_B}$$

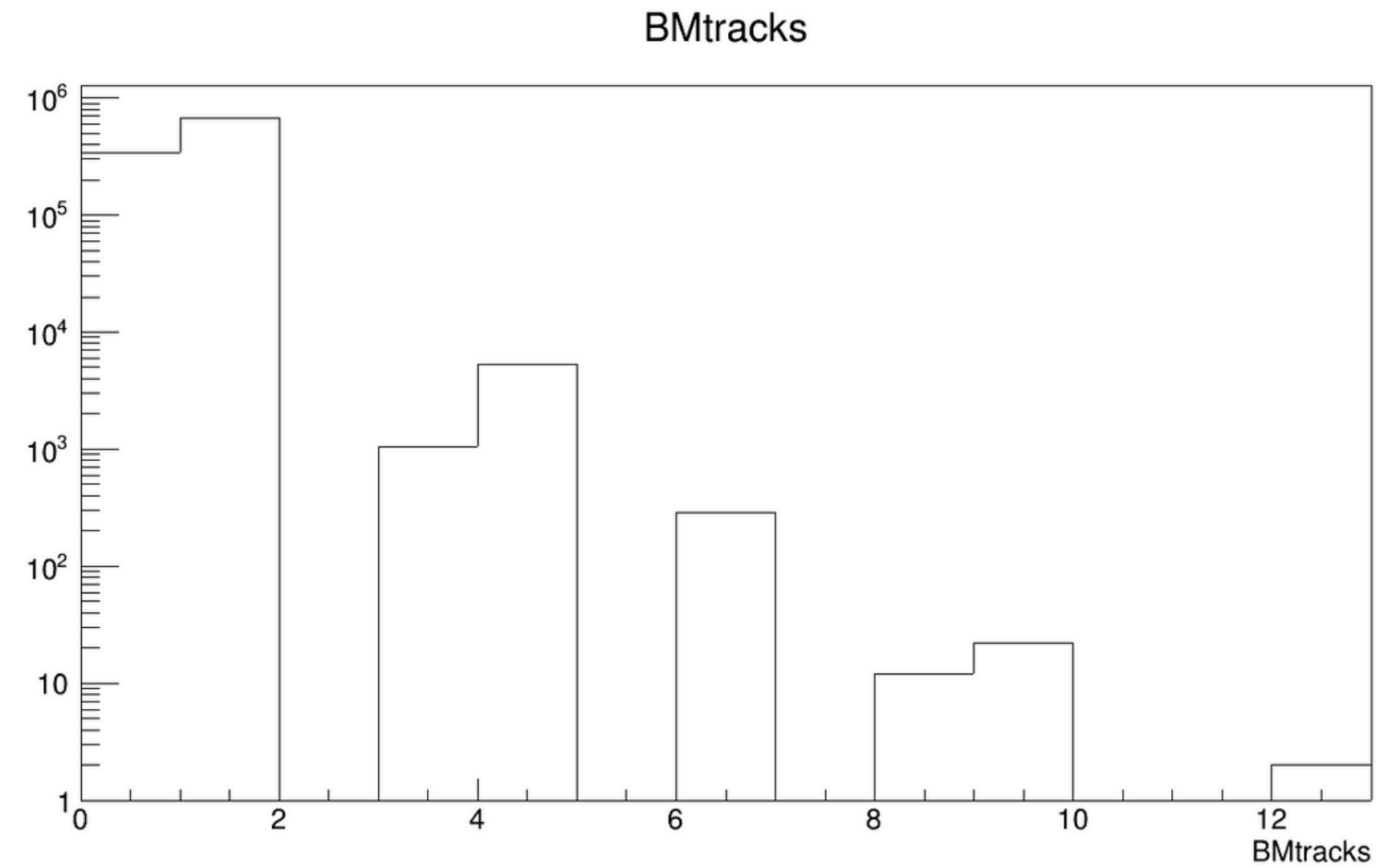
- $Y_S$  fragments yields in TG runs (S->S+B)
- $N_S$  primaries in TG runs (S->S+B)
- $Y_B$  fragments yields in NO TG runs
- $N_B$  primaries in NO TG runs

# Selection cuts

Minimum bias (4306)



Fragmentation+MB (4310)

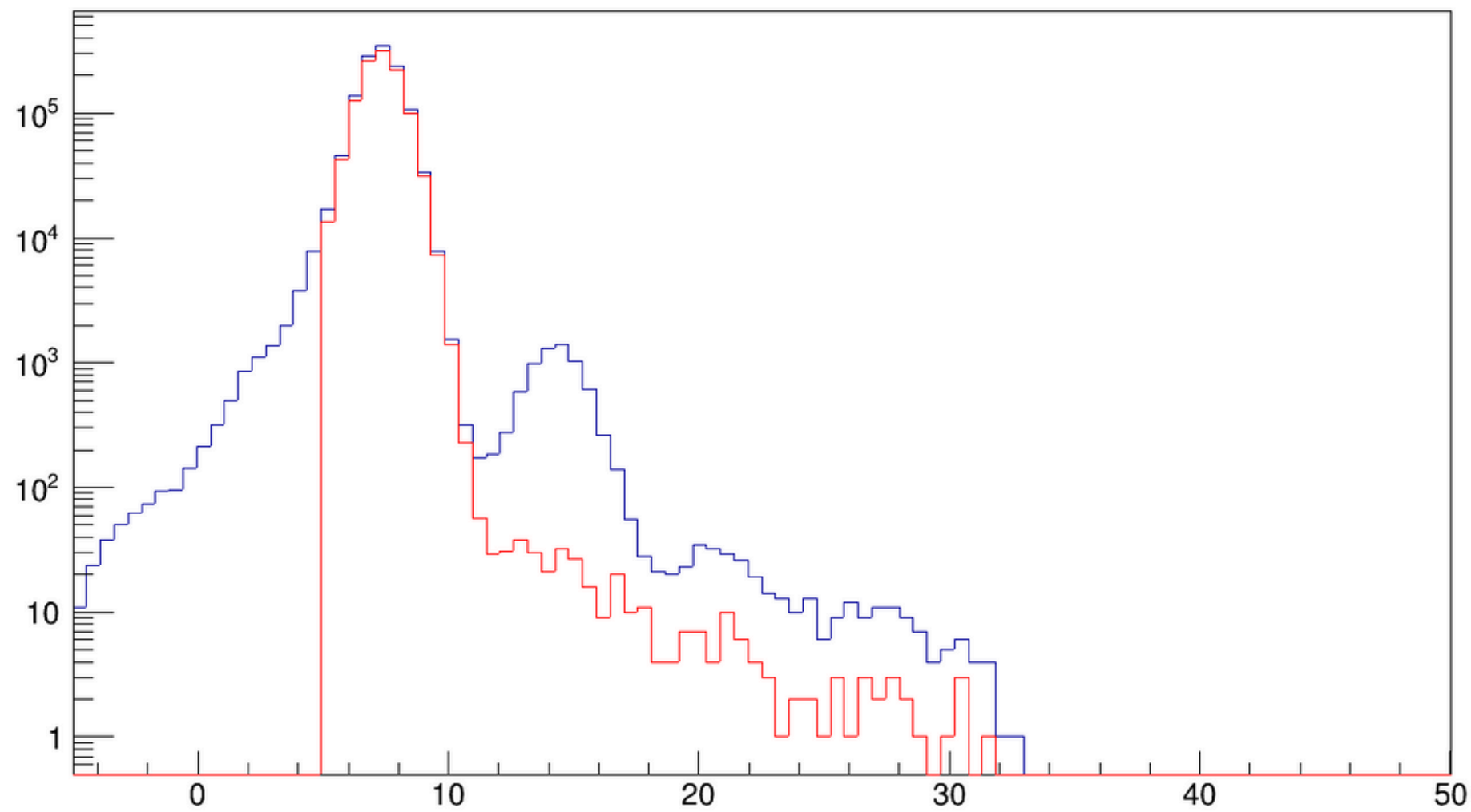


# Selection cuts

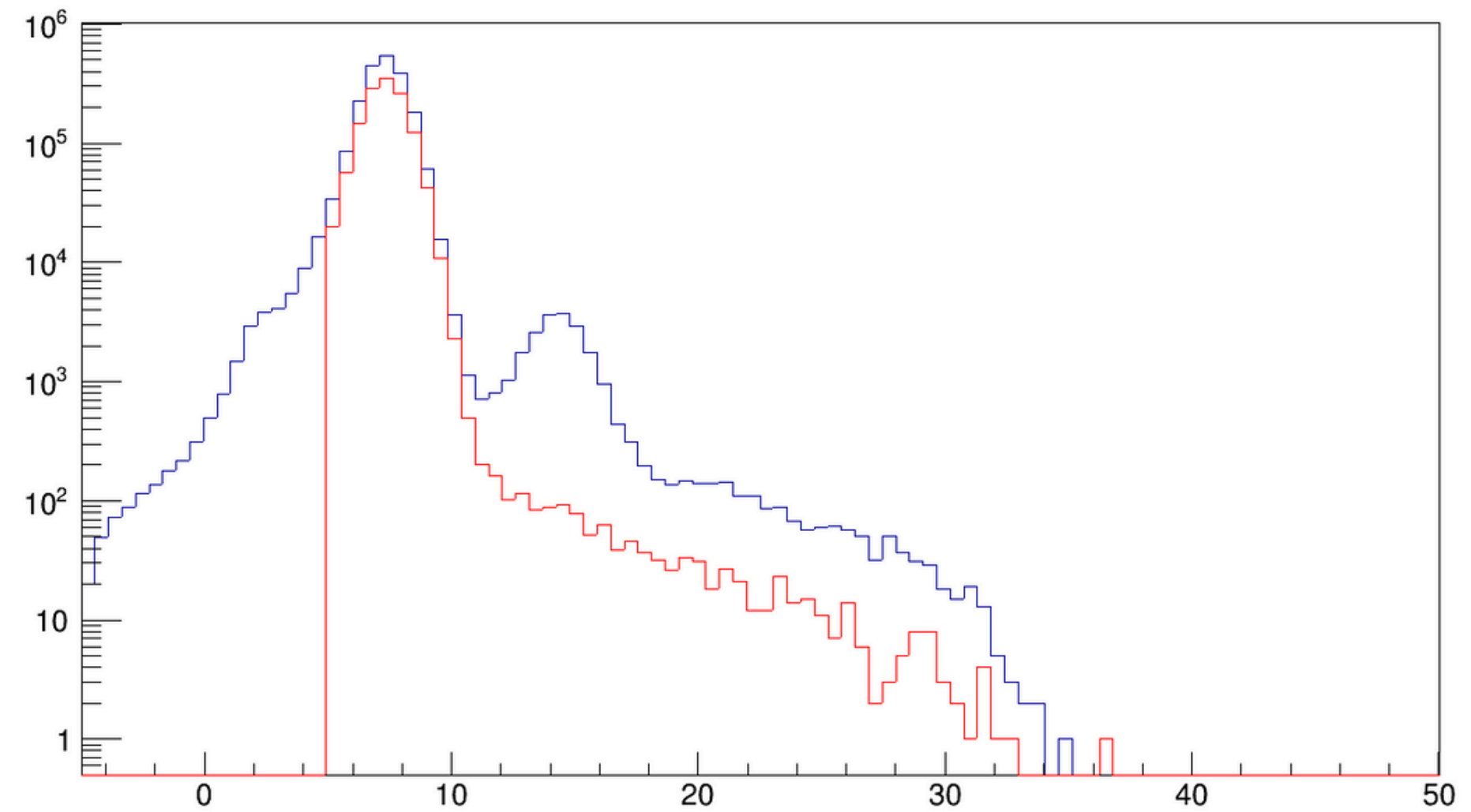
Minimum bias (4305, 4306, 4307)

Fragmentation+MB (4308, 4309, 4310)

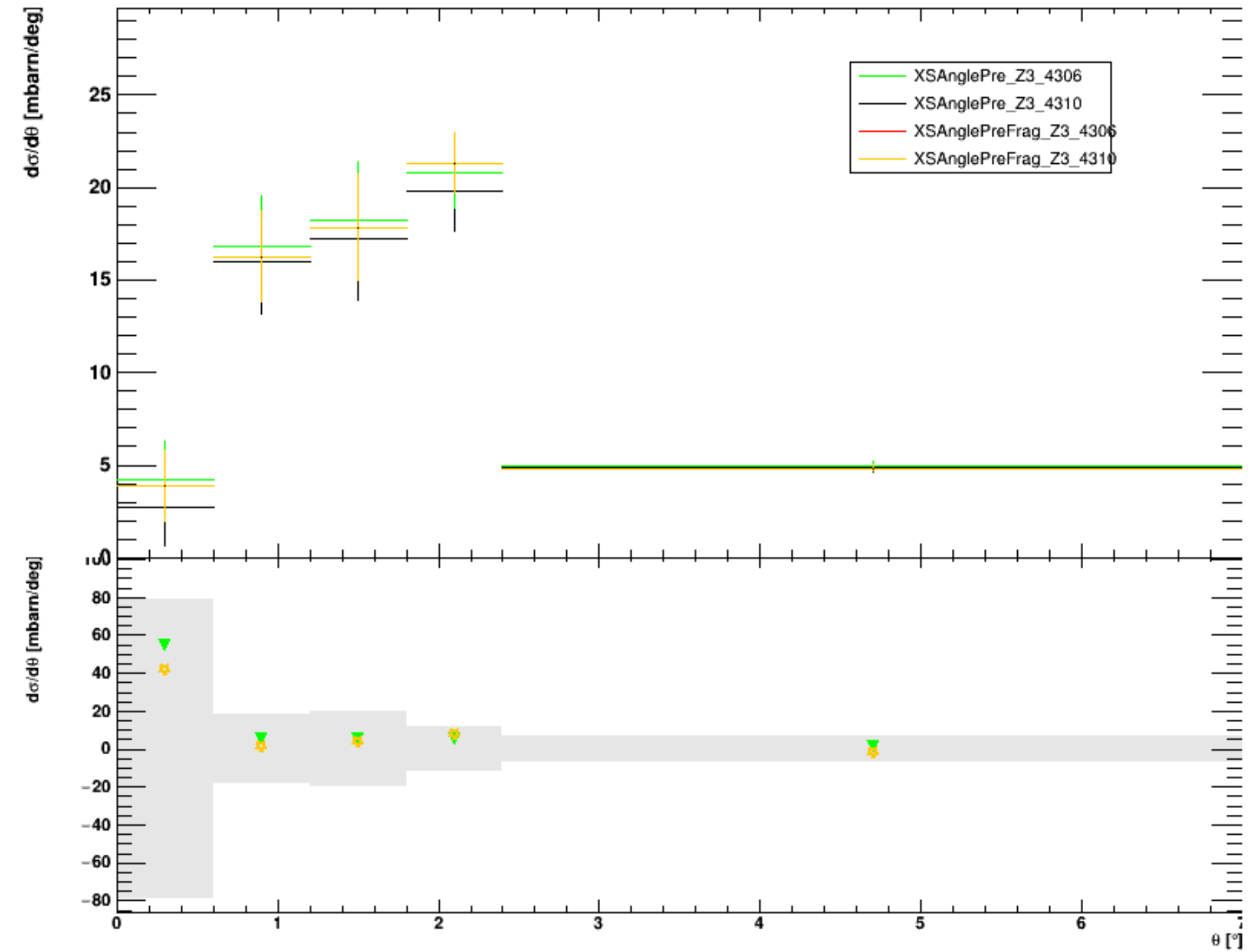
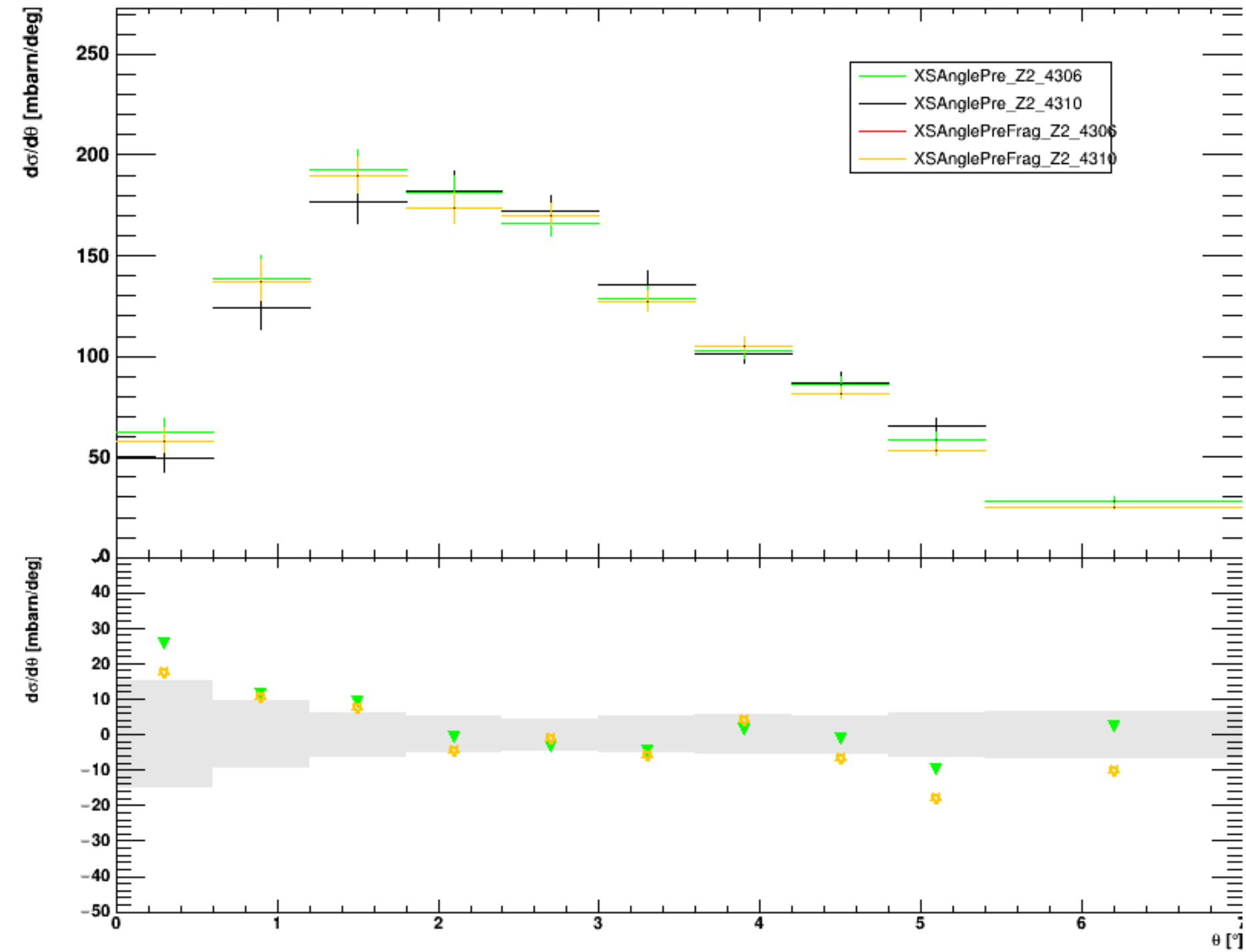
SCChargeBeforeCutSig



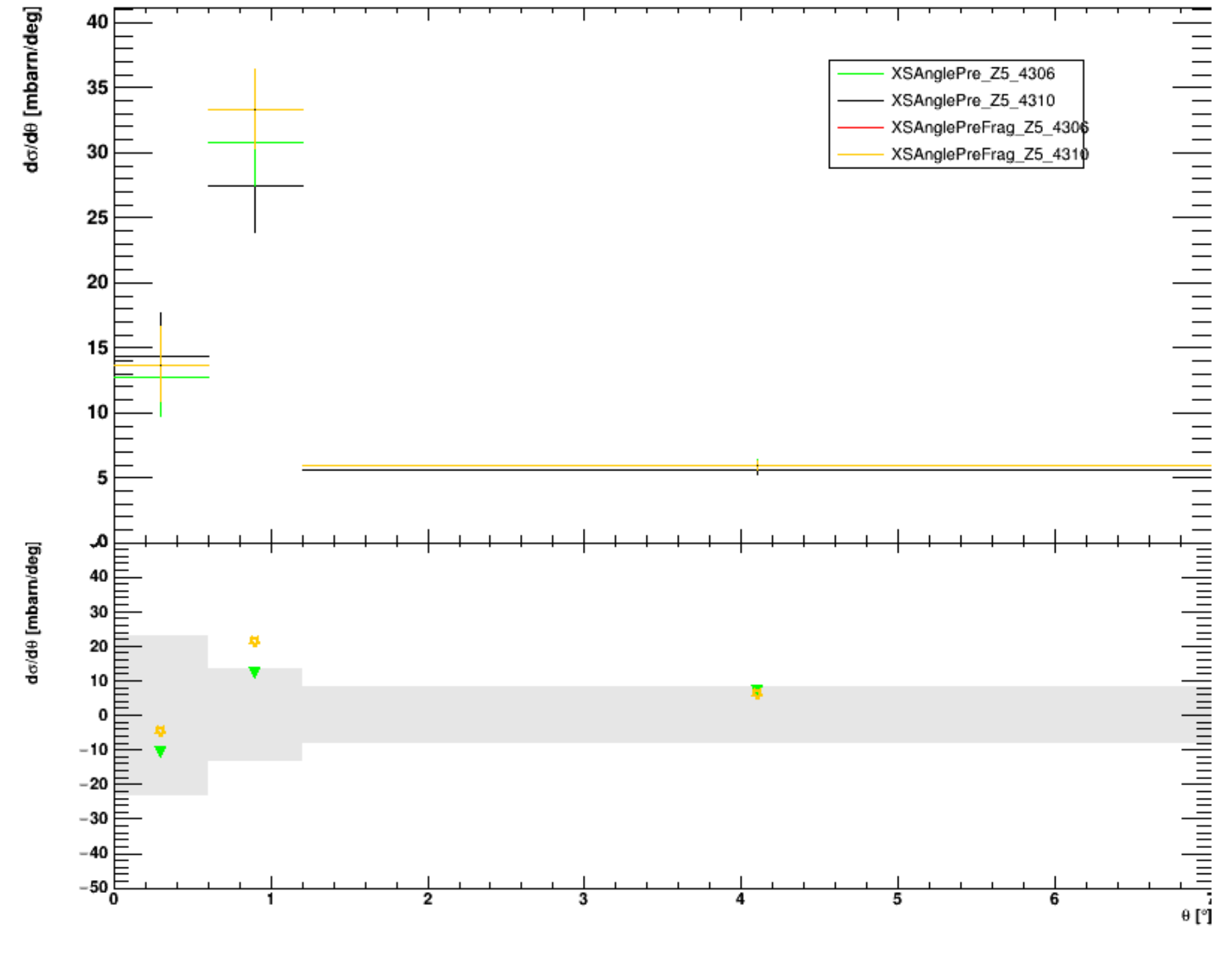
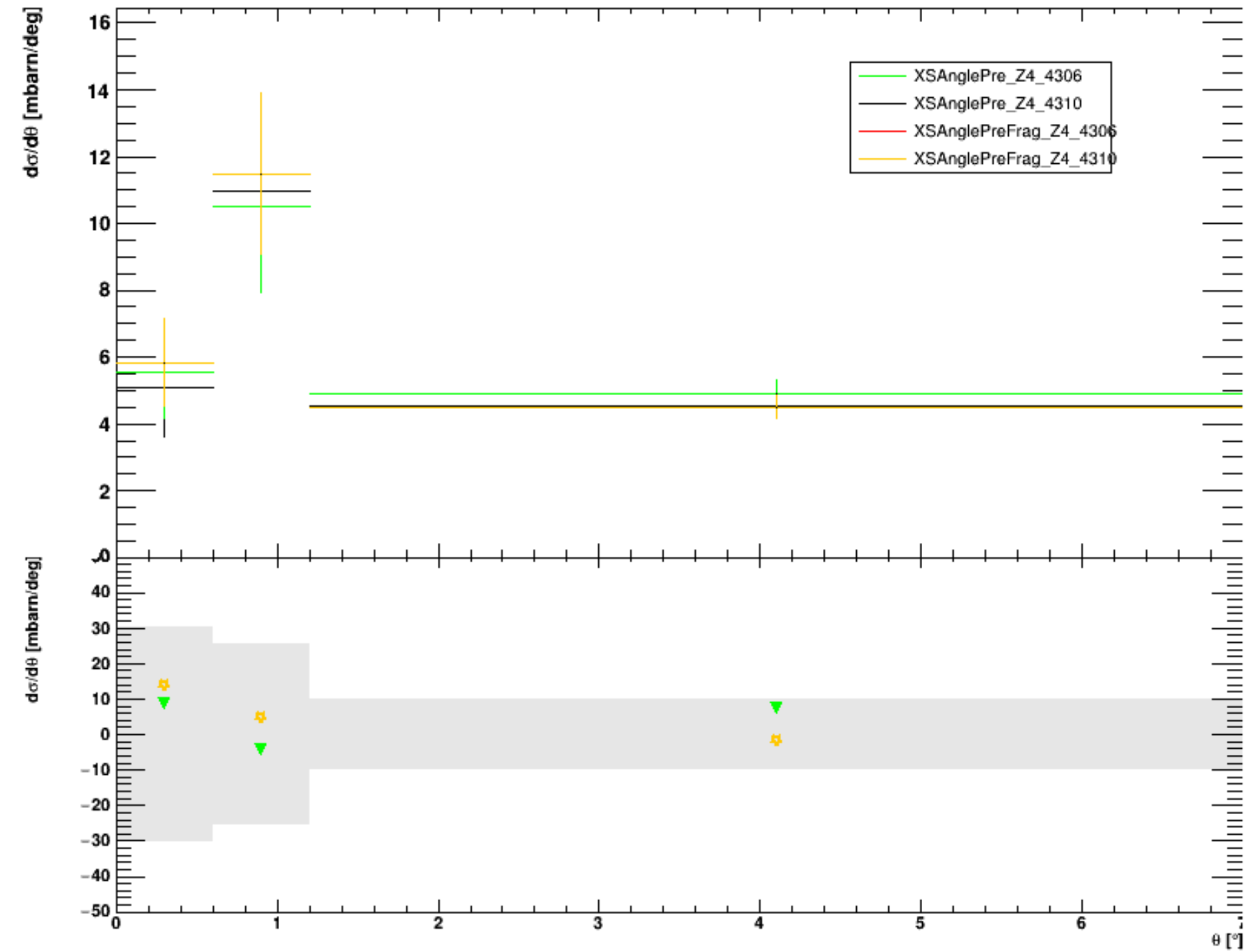
SCChargeBeforeCutSig



# Consistency checks on data

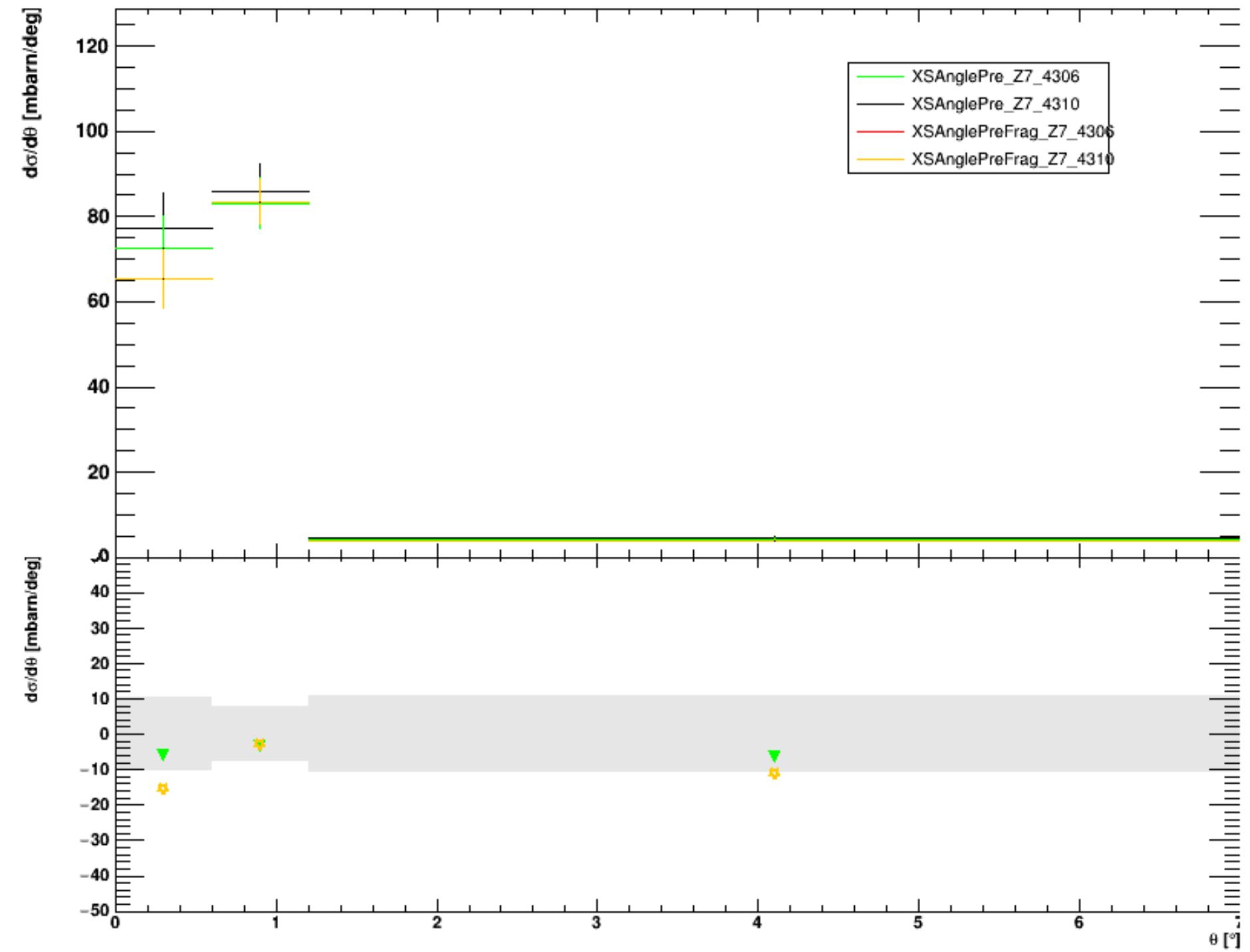
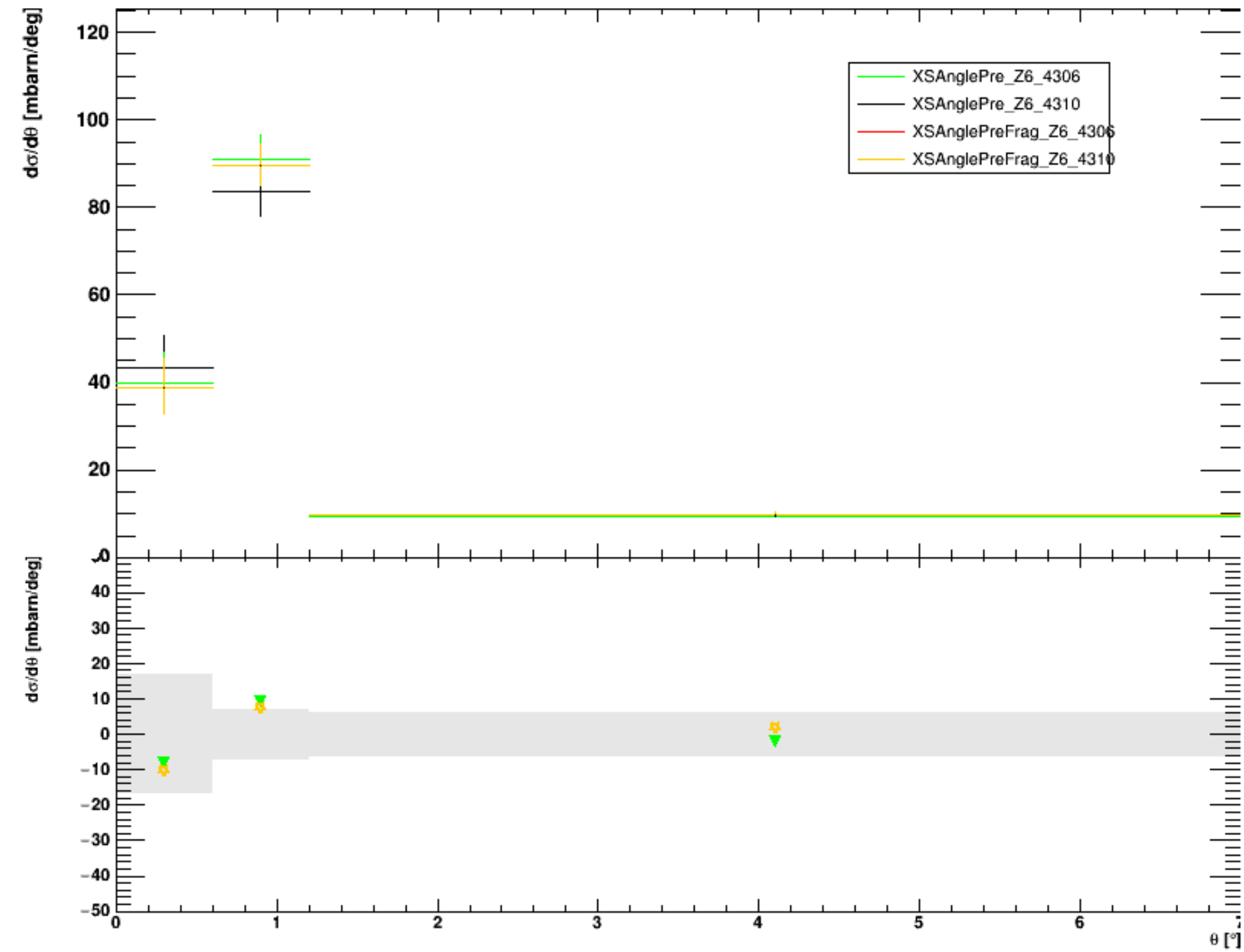


# Consistency checks on data

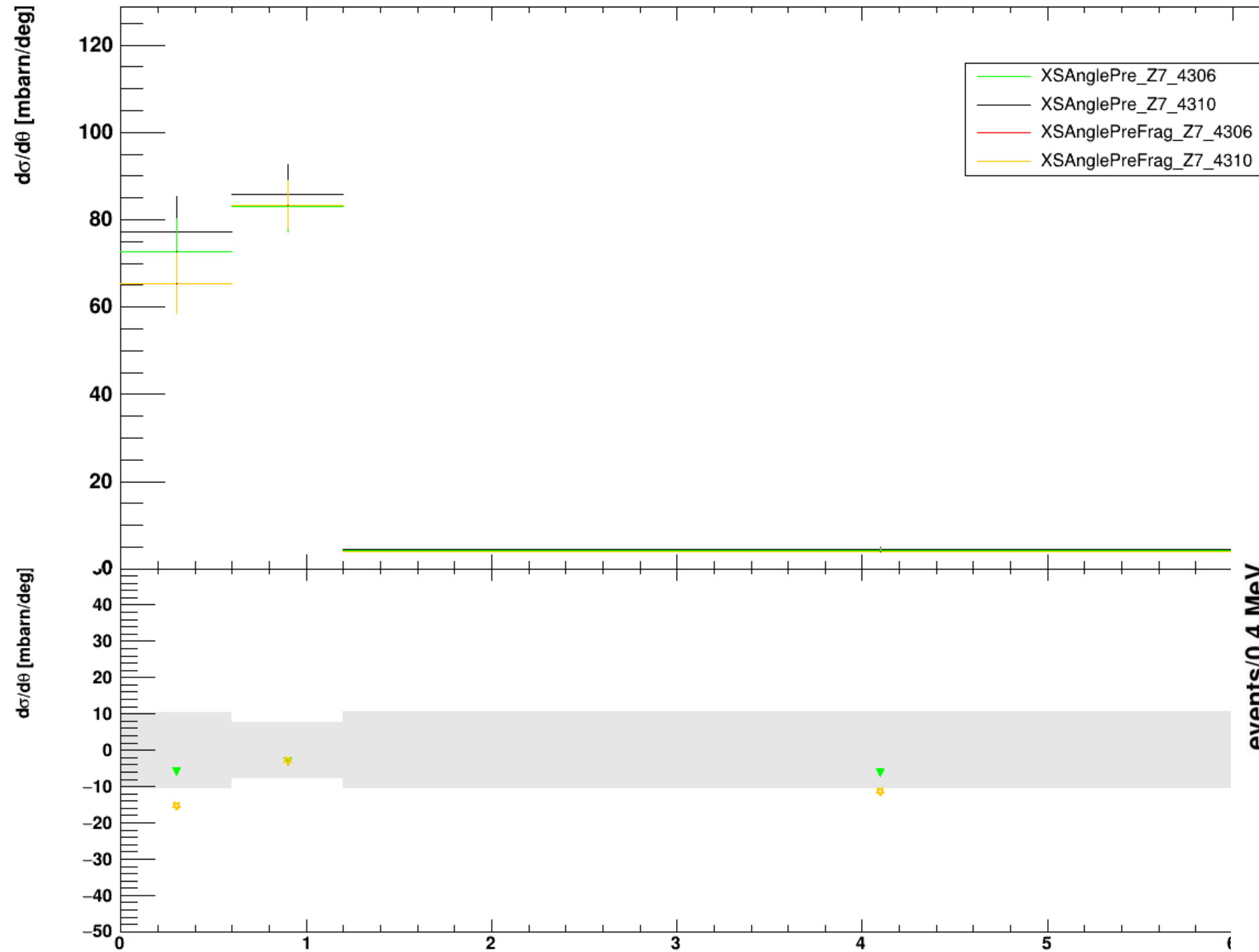




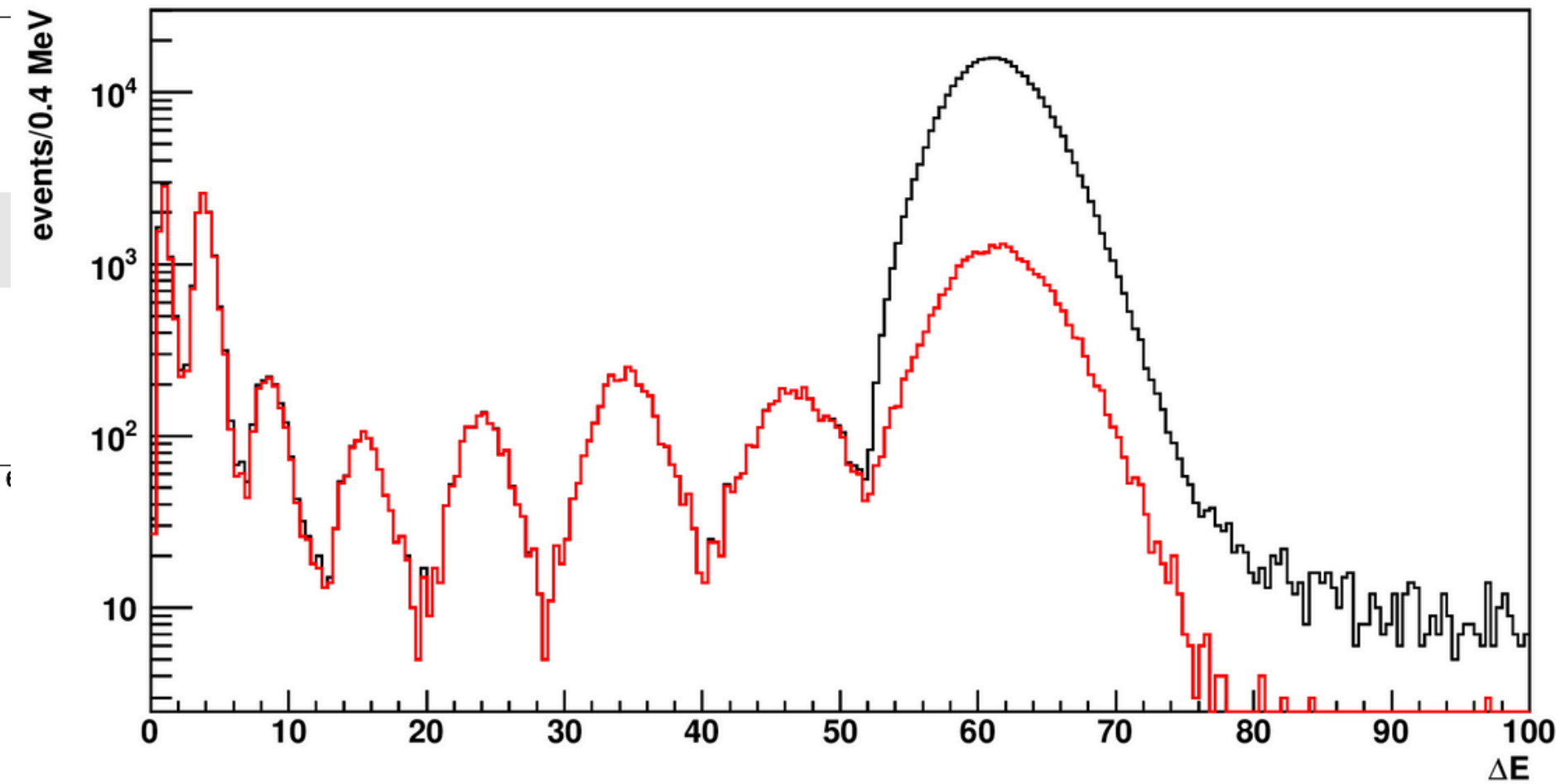
# Consistency checks on data



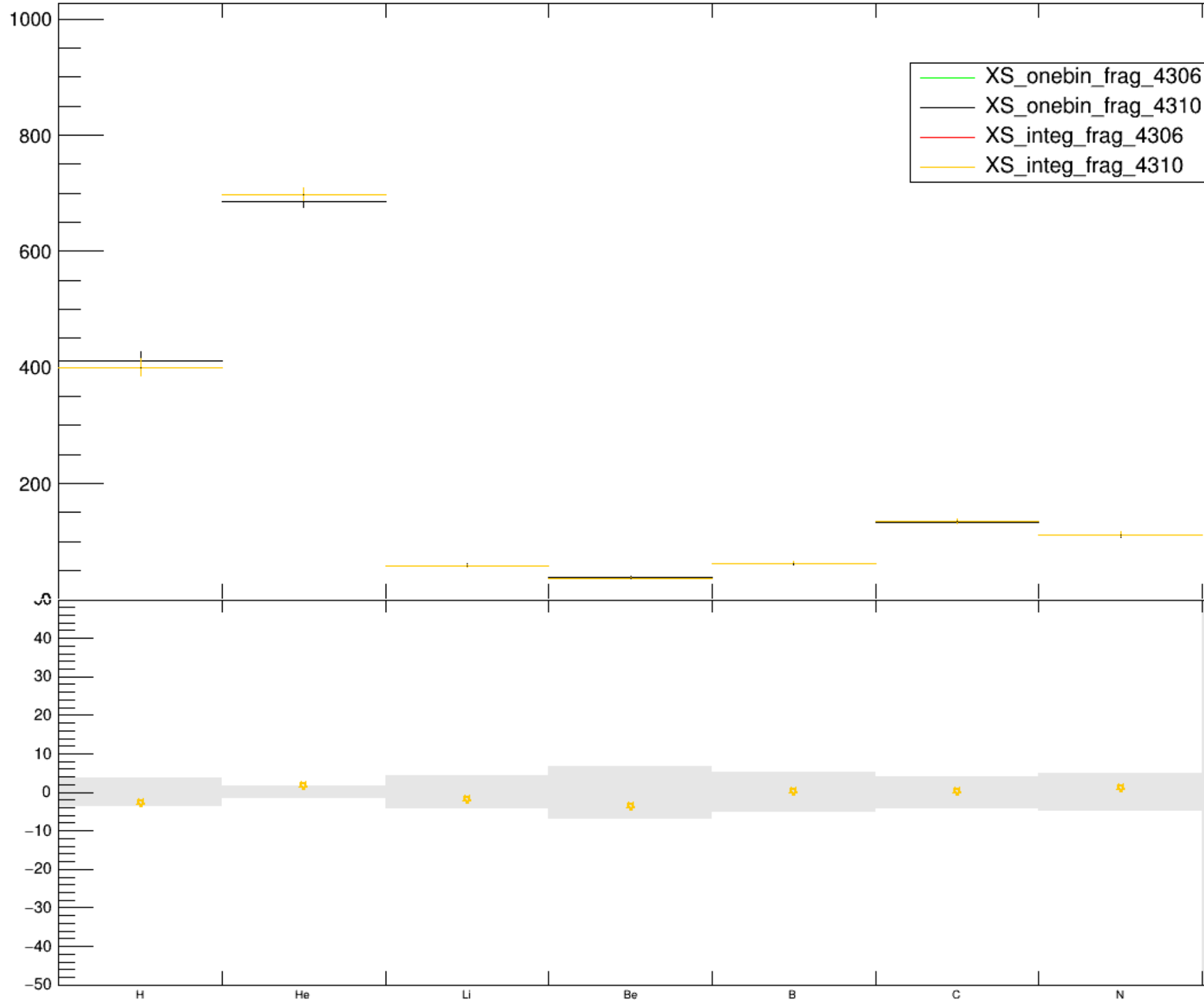
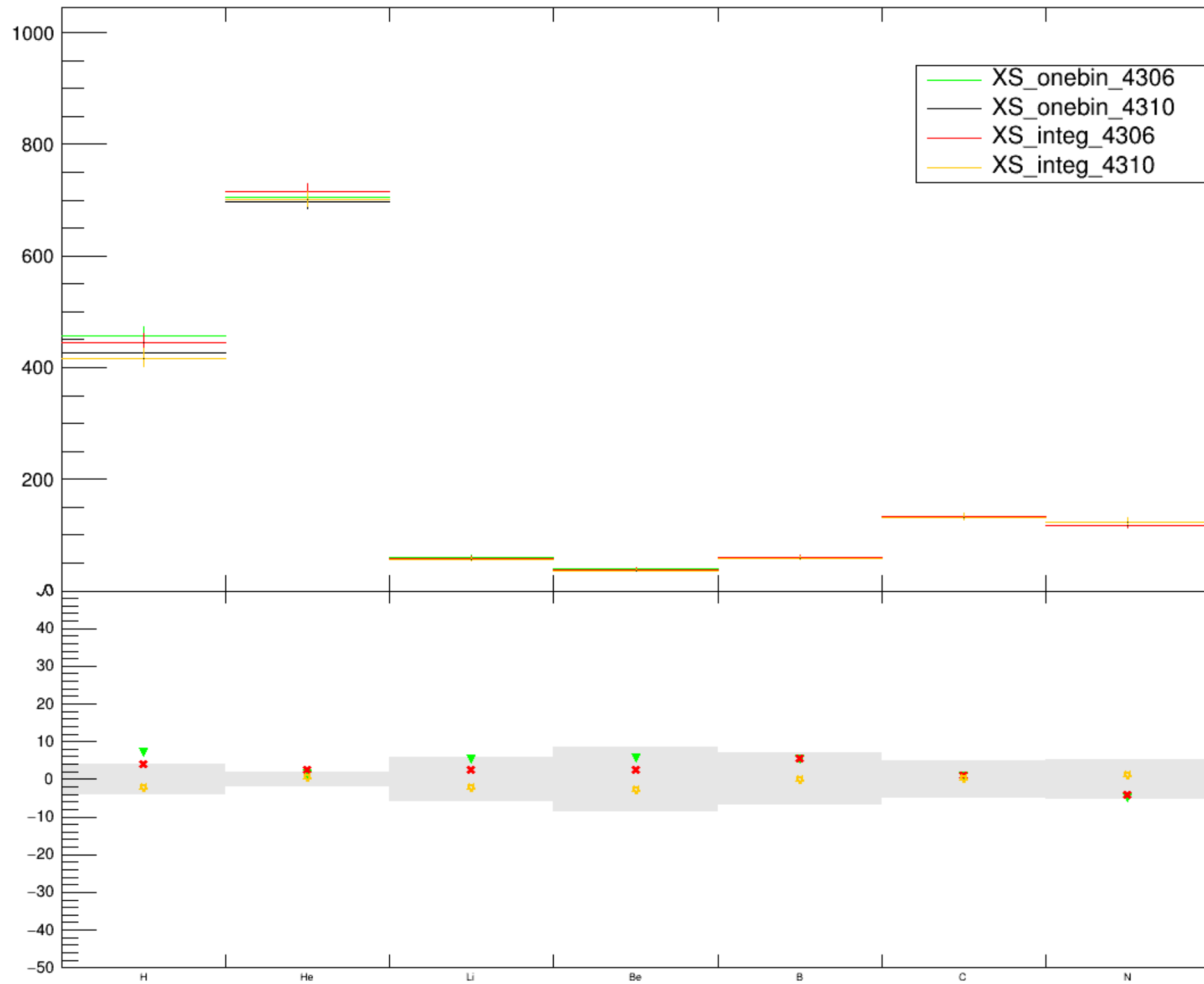
# Consistency checks on data



Fragment rescaling maybe useful for N if outside our uncertainties (it seems not)



# Consistency checks on data

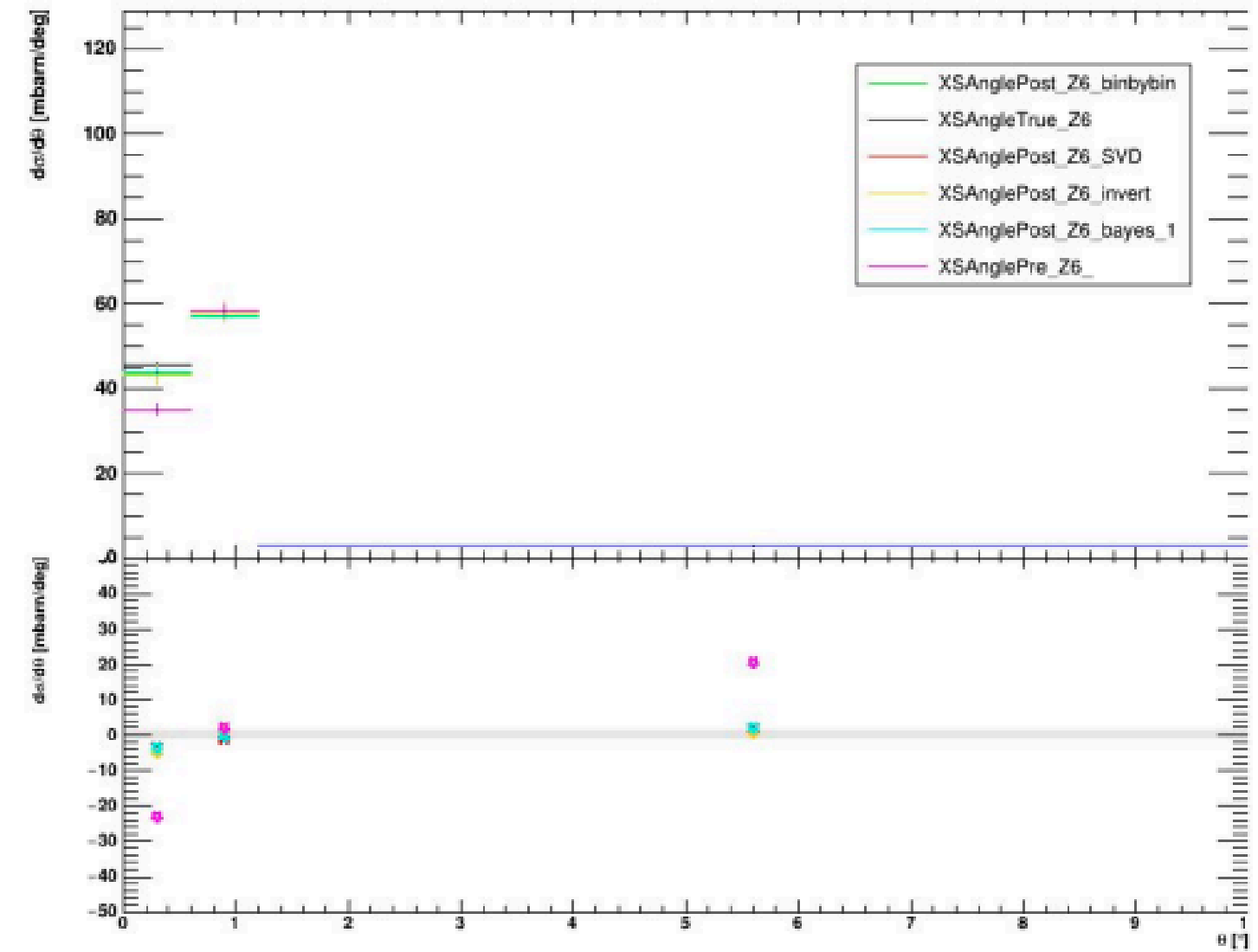
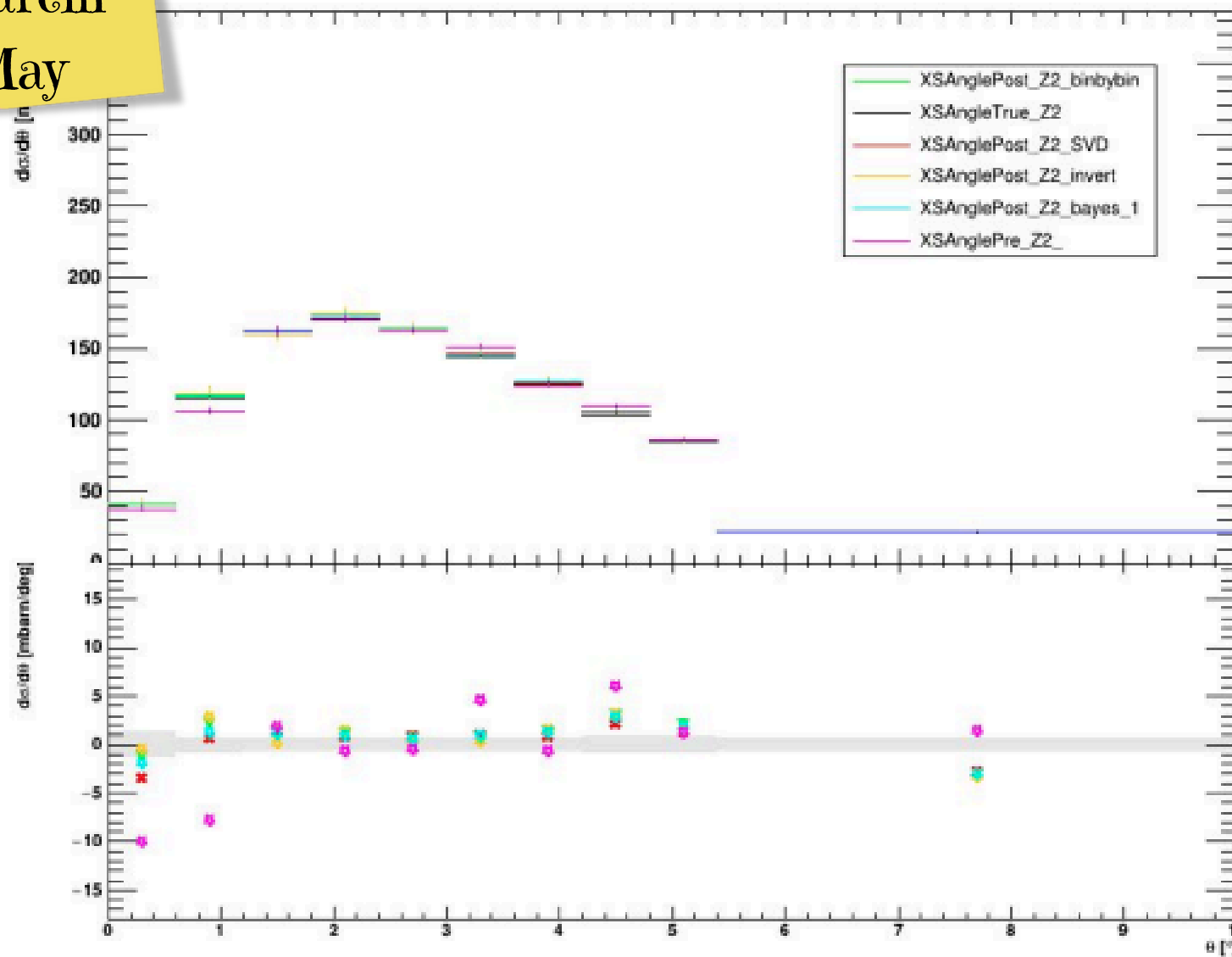


# Unfolding Method Comparison

Z=2

Z=6

Alberto Mengarelli  
21 May



Different methods behave the same way



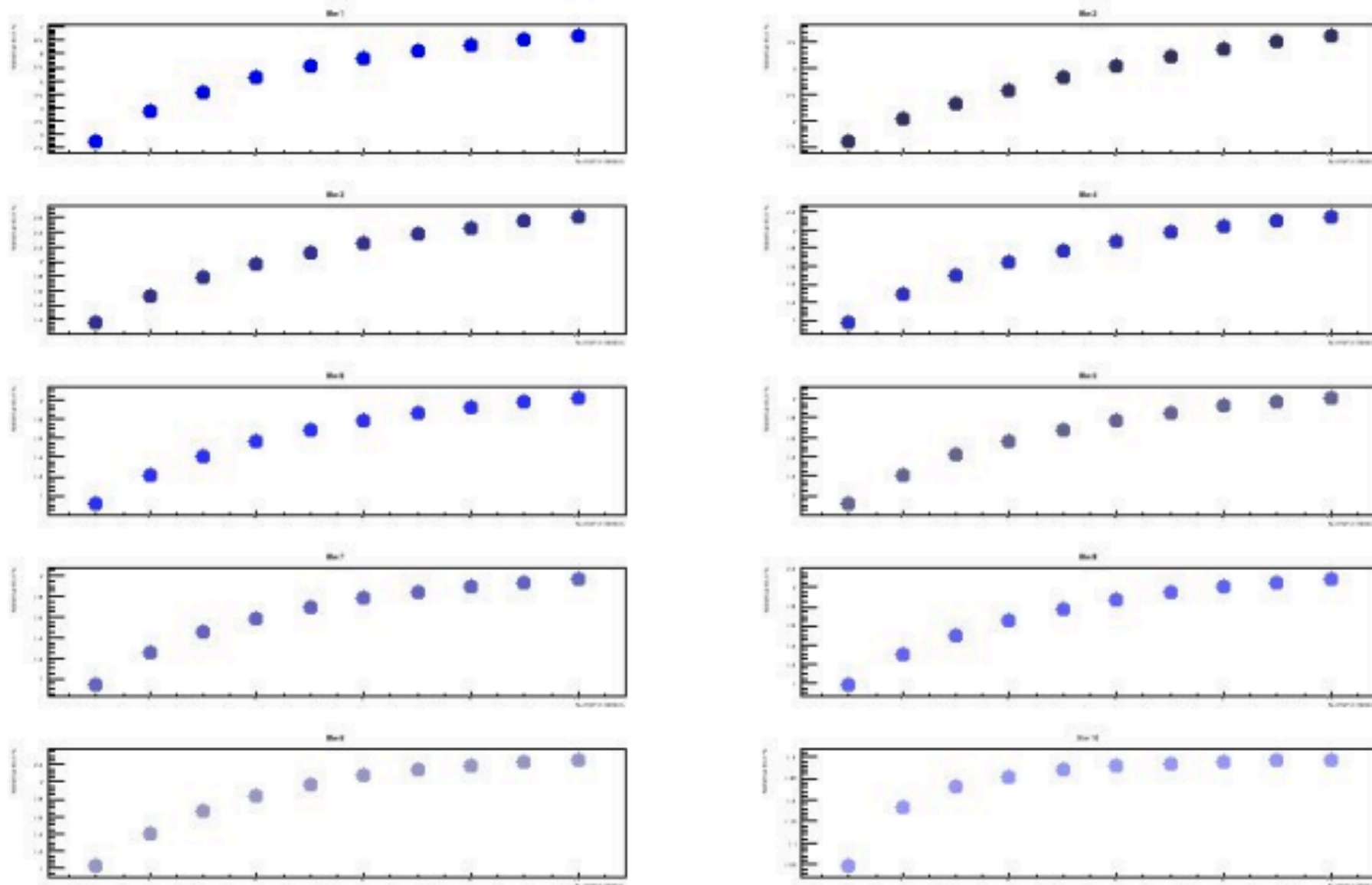
Bayes Iterative method chosen

# Studies on the number of iterations: Statistical uncertainty

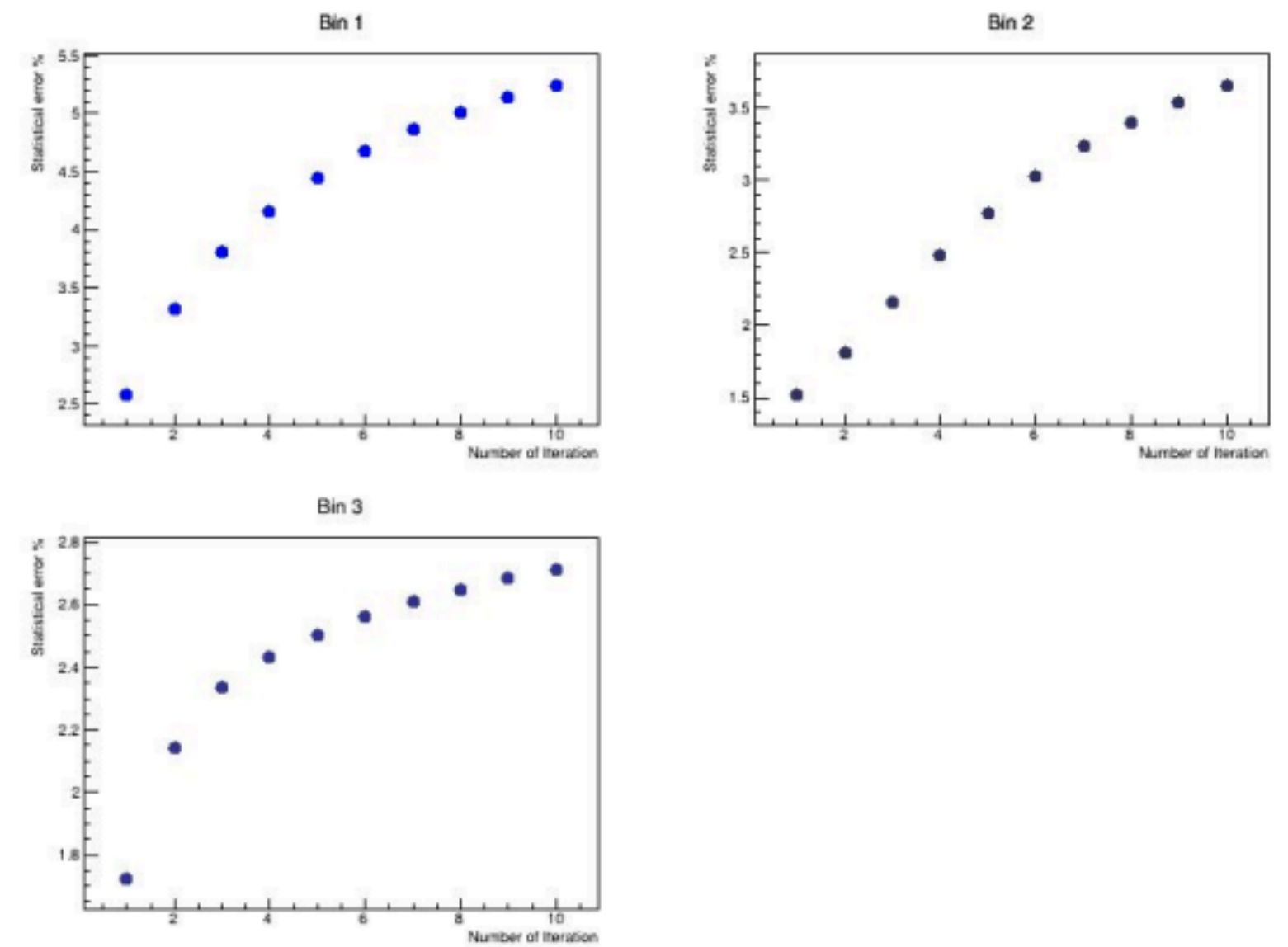
Alberto  
Mengarelli  
21 May

The degree of convergence of the iterative procedure is checked by comparing each iteration to the previous one. In particular, the parameters taken into account are the bin-wise statistical error (it increases with the number of iterations, reaching a sort of plateau)

$Z=2$



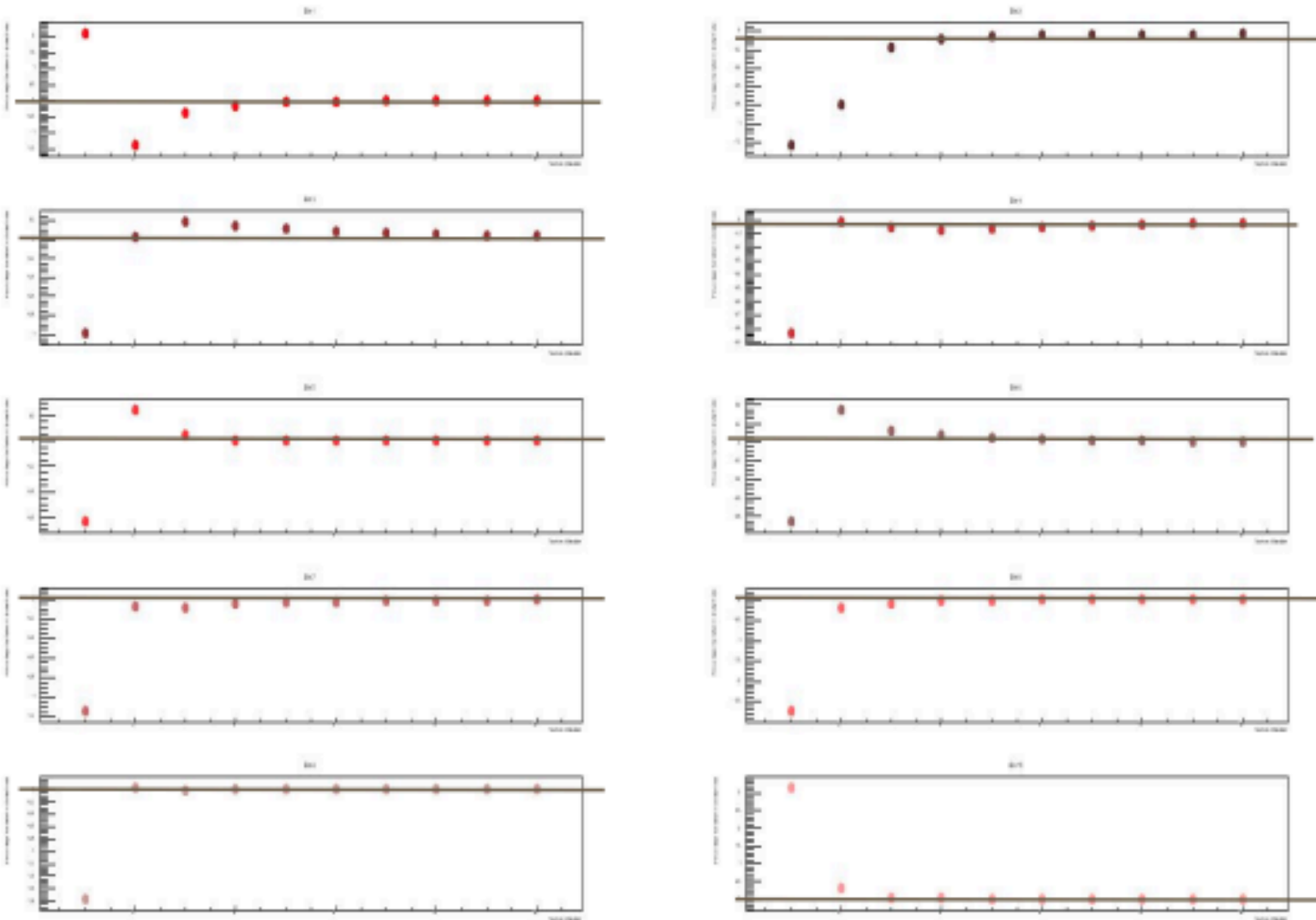
$Z=6$



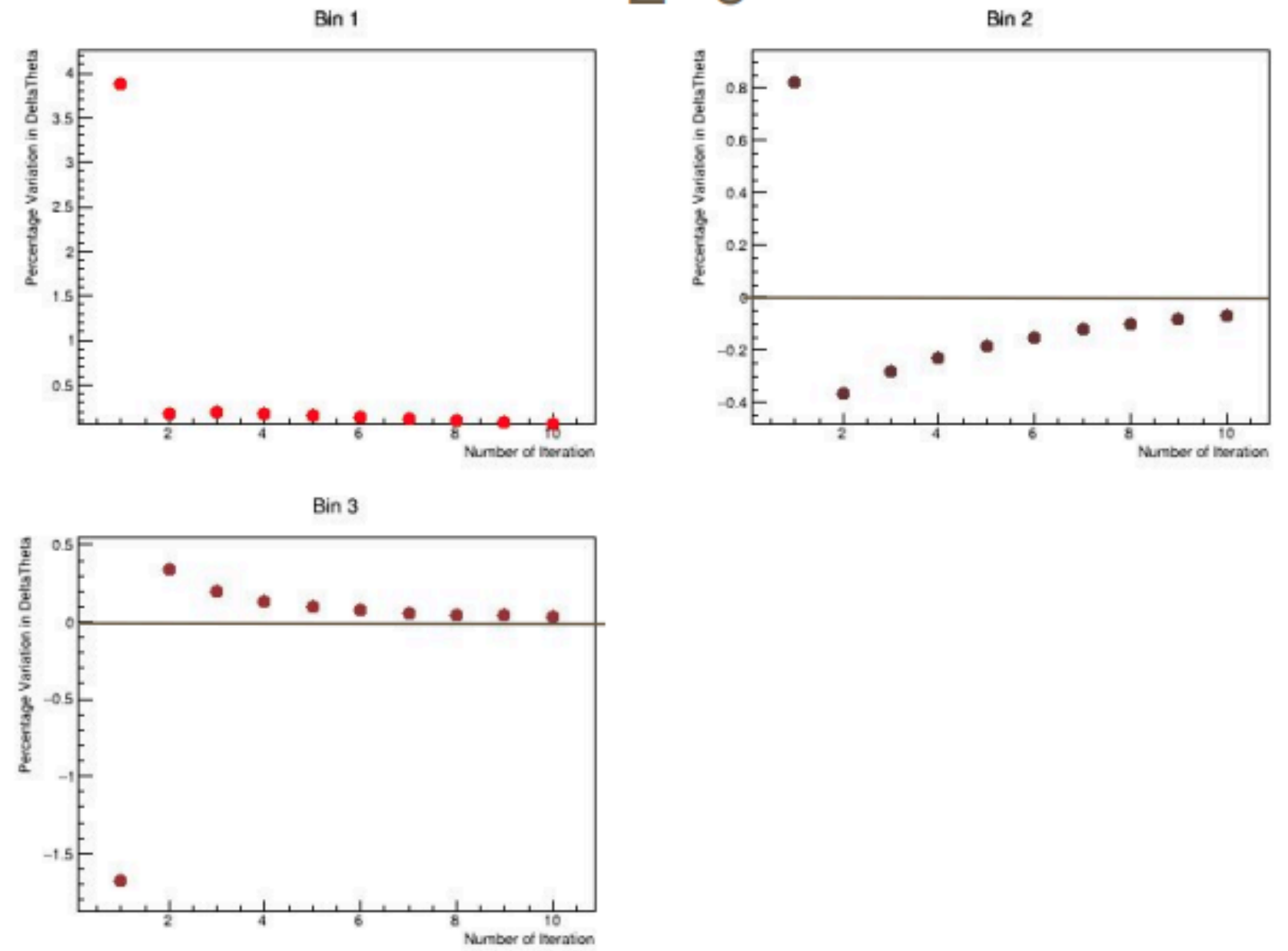
# Studies on the number of iterations: bin residuals

bin-wise residuals (the bin-by-bin difference between the unfolded distribution at the  $i$ -th iteration and the unfolded distribution at the  $i - 1$ -th iteration, which must converge to 0).

Z=2



Z=6



Alberto  
Mengarelli  
21 May

# Studies on the number of iterations: Average correlation

An optimal choice of the regularization parameter is the one that minimizes the average correlation factor:

$$\rho_{\text{avg}} = \frac{1}{M_x} \sum_{j=1}^{M_x} \rho_j.$$

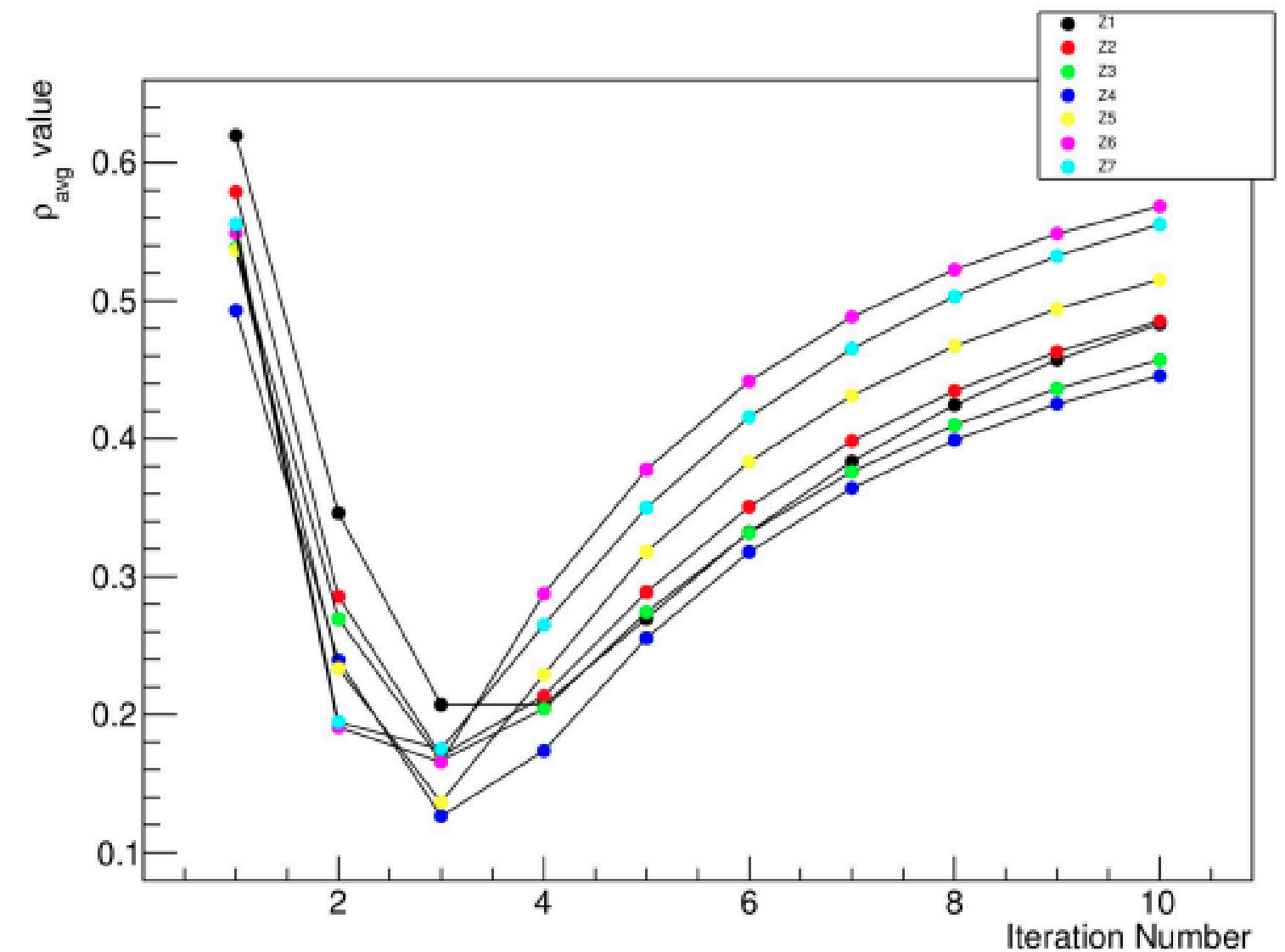
where  $\rho_j$  global correlation coefficient of bin  $j$  is defined as

$$\rho_j = \sqrt{1 - \left( (V_{xx})_{jj} (V_{xx}^{-1})_{jj} \right)^{-1}}.$$

$M_x$ : ndof;  $V_{xx}$ : Cov. matrix

$$\rho_{\text{avg}} = \frac{1}{N_{\text{bins}}} \sum_{i=1}^{N_{\text{bins}}} \rho_i \quad \rho_i = \sqrt{1 - [C_{ii} (C^{-1})_{ii}]^{-1}}.$$

S. Schmitt, Data Unfolding Methods in High Energy Physics, EPJ Web Conf. 137 (2017) 11008, ed. by Y. Foka, N. Brambilla and V. Kovalenko, arXiv: 1611.01927

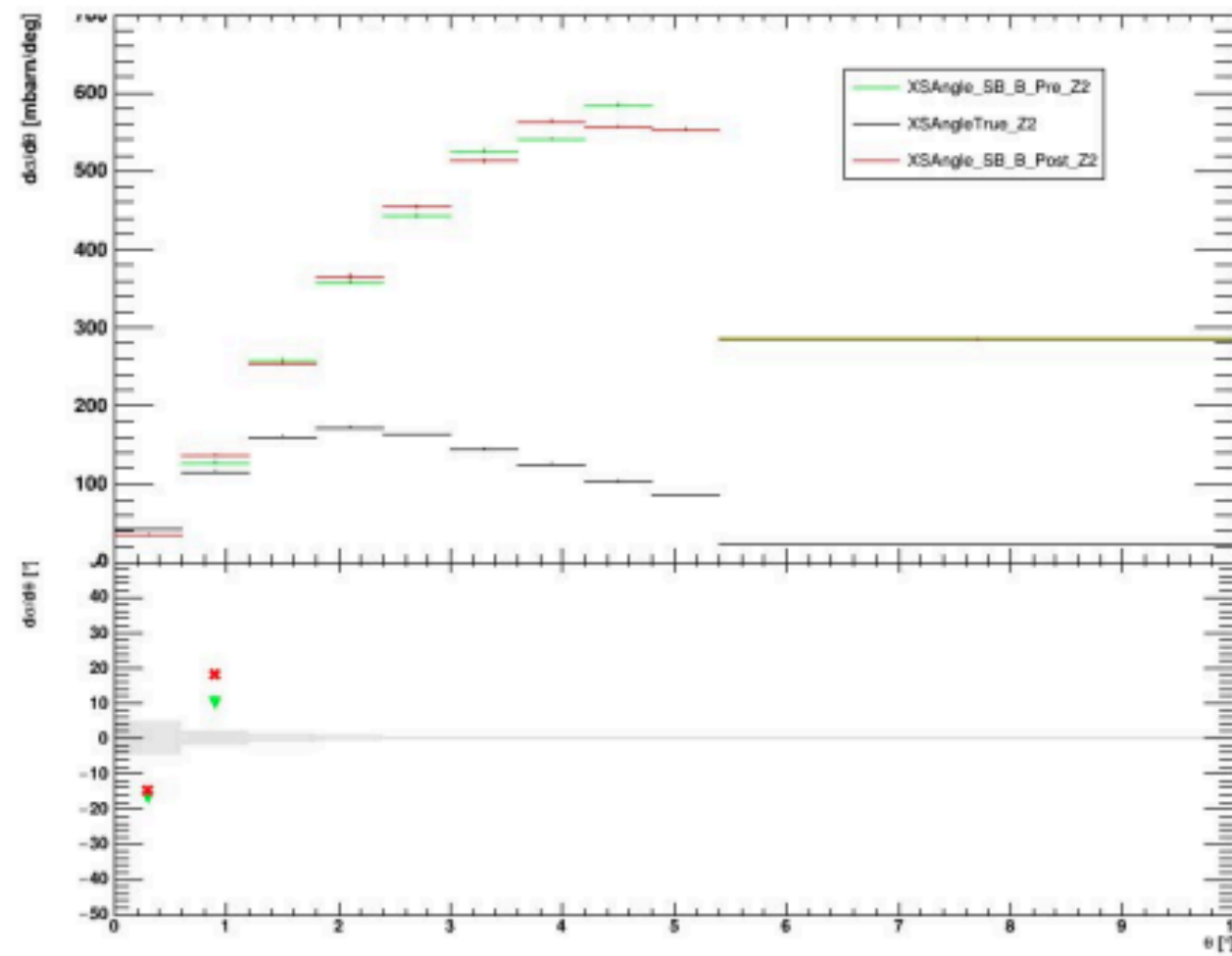




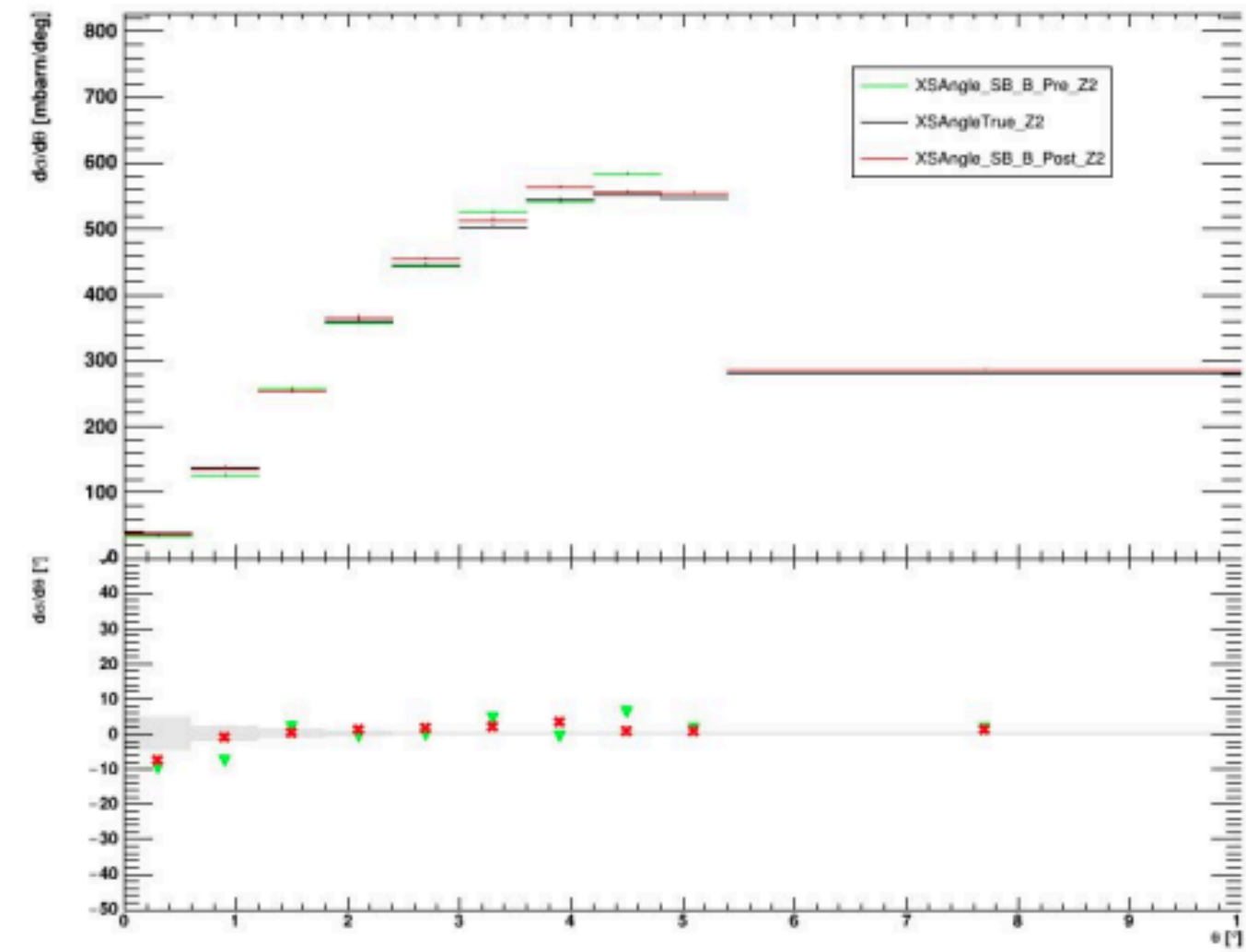
# Stress tests

Due to the specific choice of the Monte Carlo sample for the training of the unfolding, it is necessary to check whether this choice could introduce a bias via the unfolding. To do this check the MC reweighting is required, in order to change the shapes of the distributions and get a varied distribution used as pseudo-data.

### Only pseudo-data reweighted



### Both pseudo-data and truth reweighted

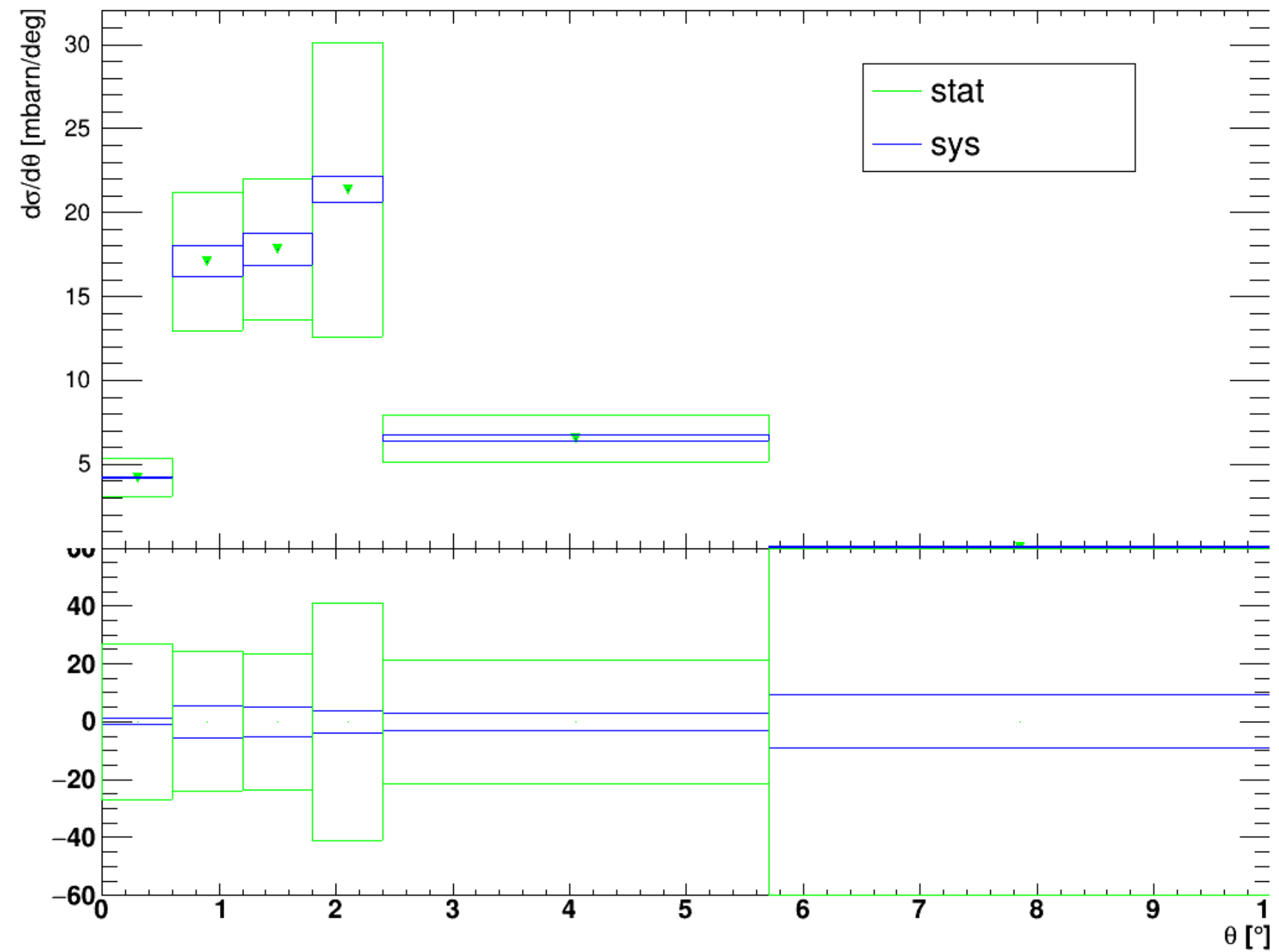
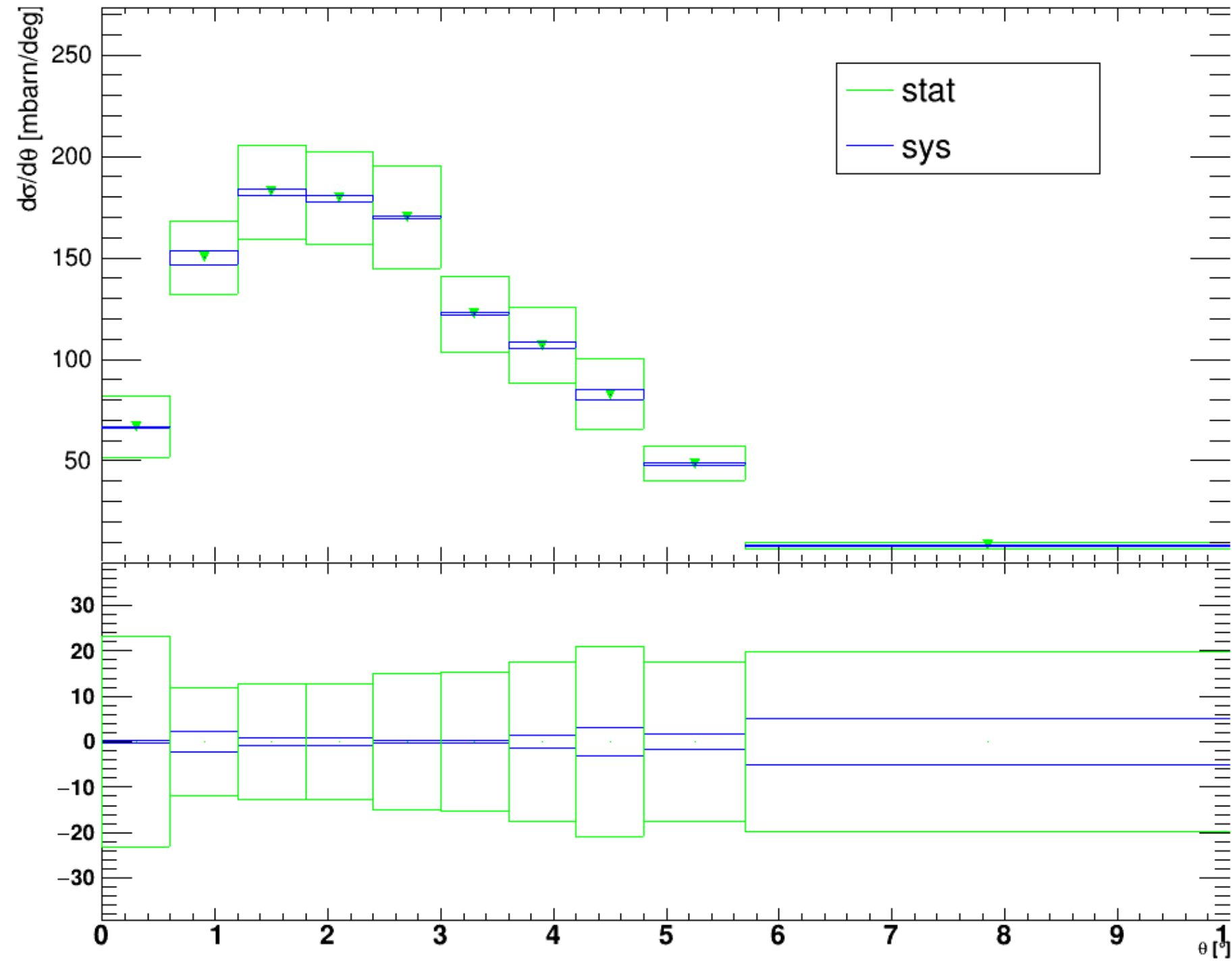




# Merge all statistics

Z=2

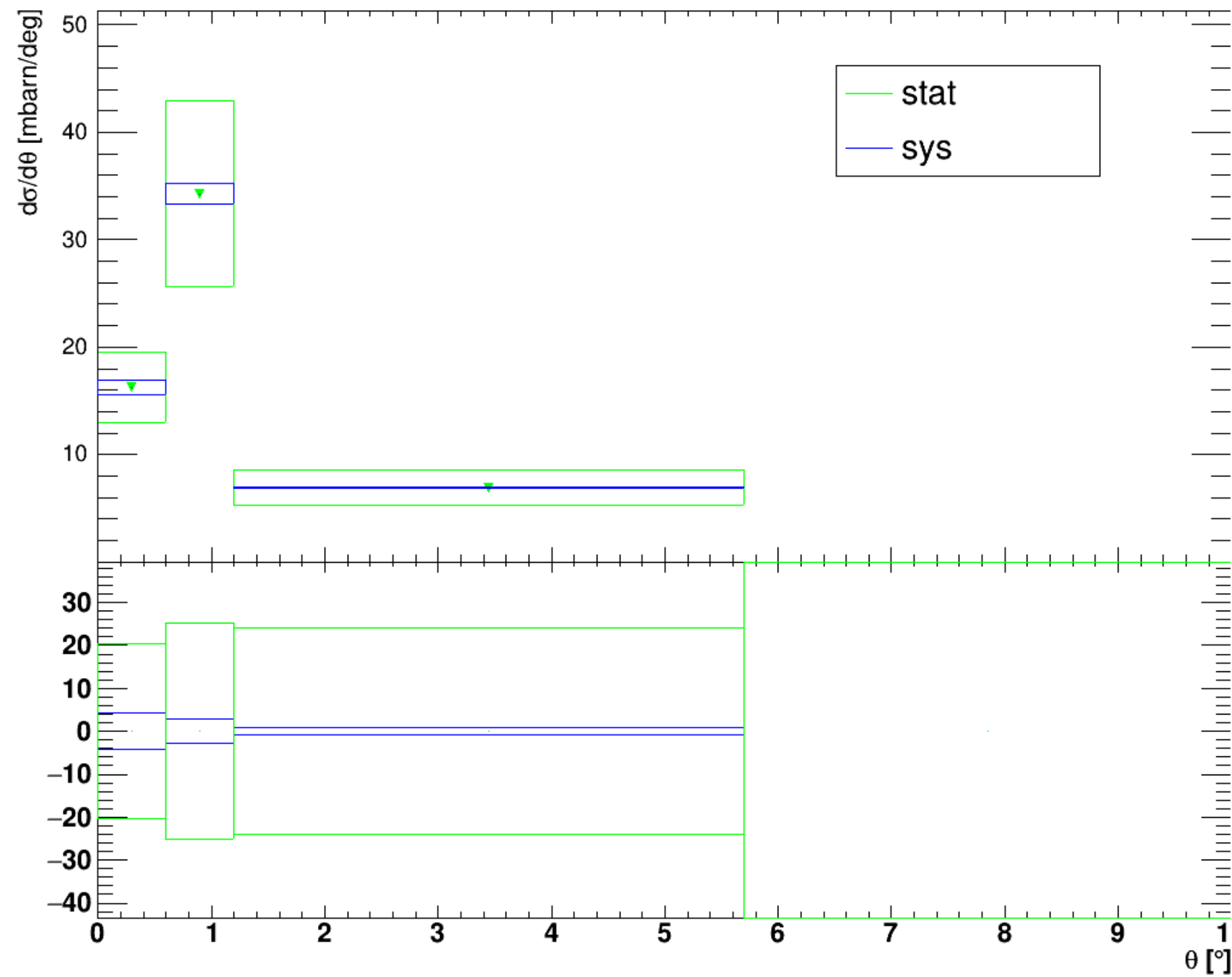
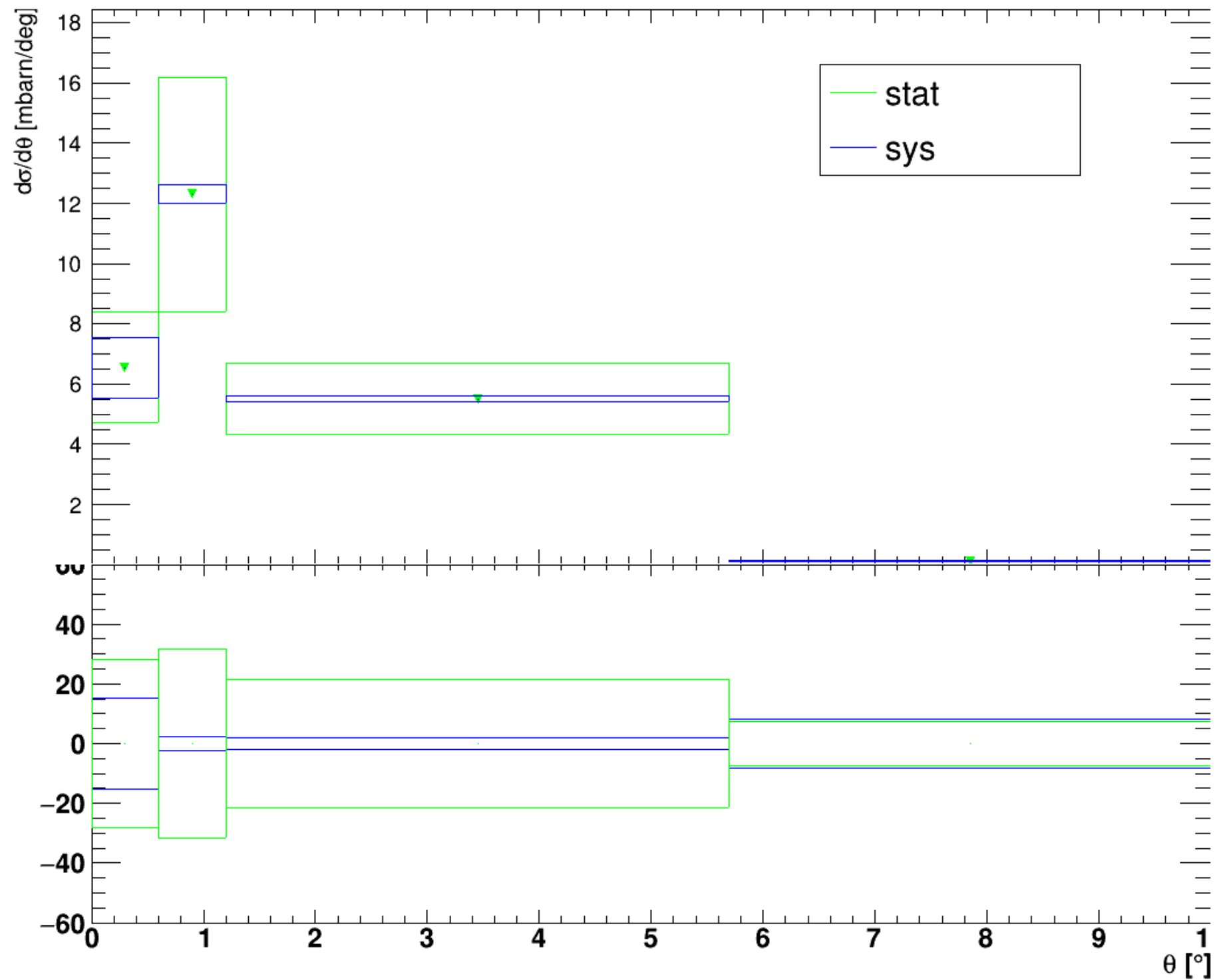
Z=3



# Merge all statistics

Z=4

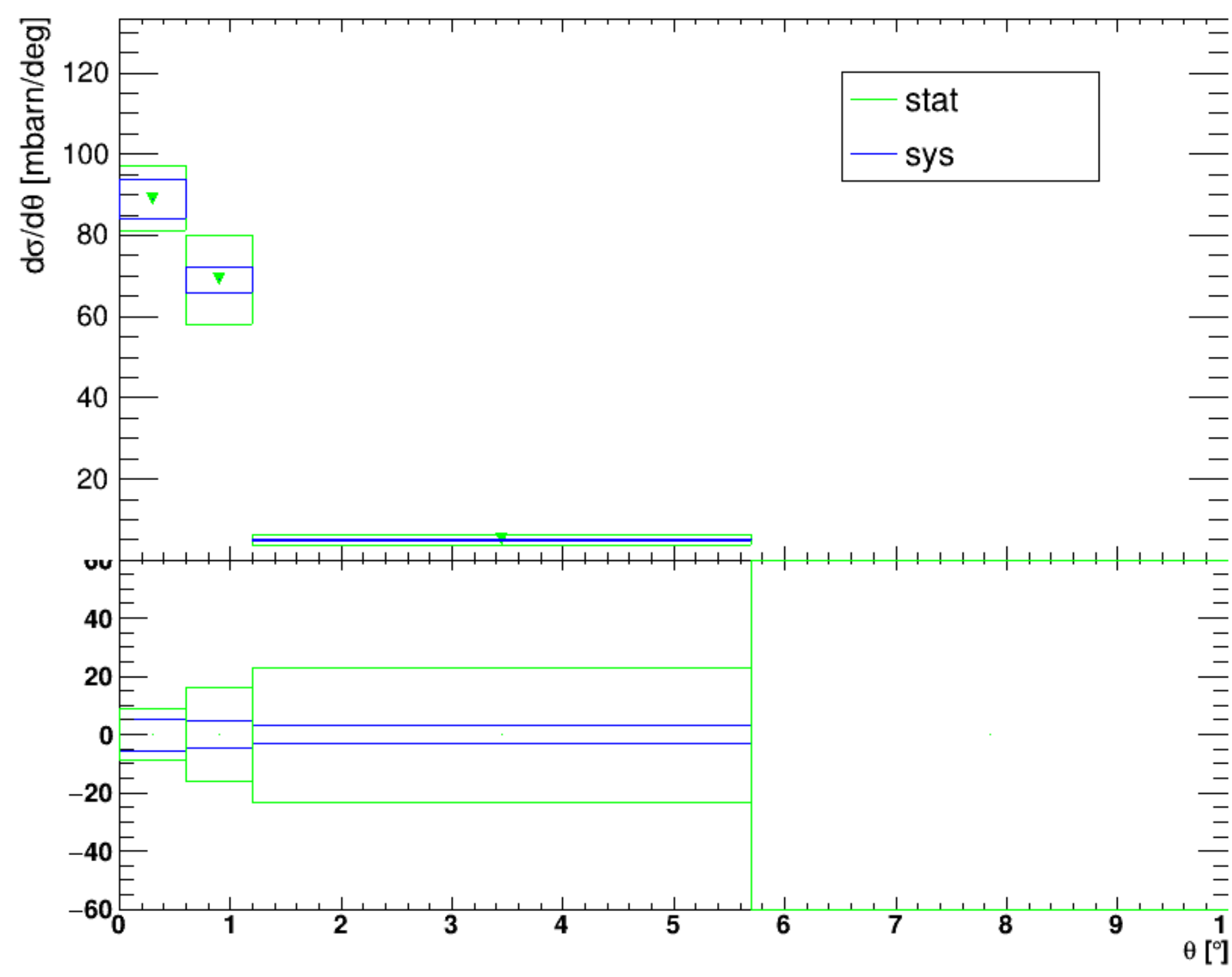
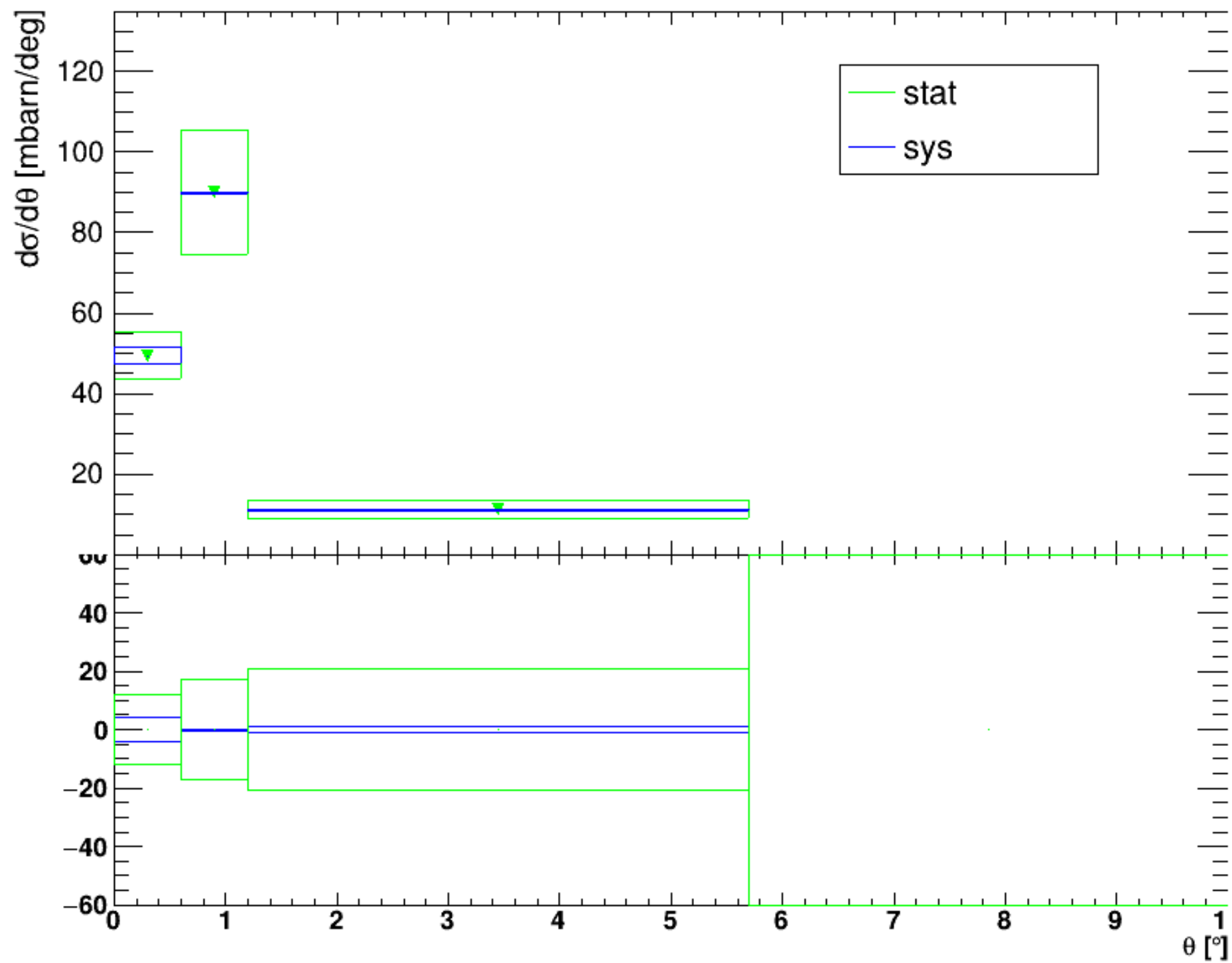
Z=5



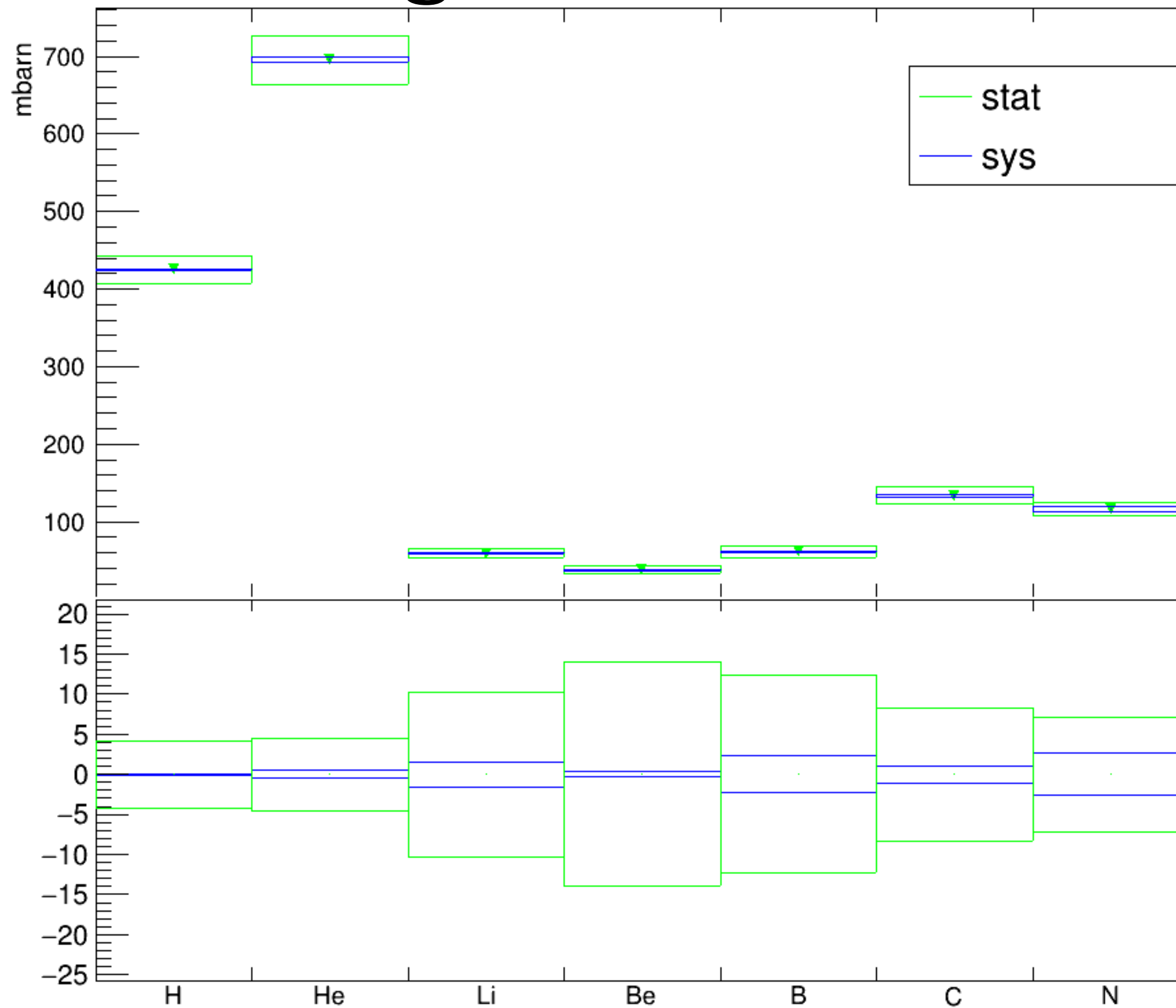
# Merge all statistics

Z=6

Z=7



# Merge all statistics



# Comparison with our GSI2019 article

TABLE 4 Elemental fragmentation cross sections measured in this work, for a 400 MeV/u  $^{16}\text{O}$  beam interacting with a 5 mm graphite target. The energy of the  $^{16}\text{O}$  beam at target center is 393 MeV/u. The results are compared with FLUKA MC predictions (last column).

Element	$\sigma_{frag} \pm \Delta_{stat} \pm \Delta_{sys}$ [mbarn]	$\Delta_{stat}/\sigma_{frag}$	$\Delta_{sys}/\sigma_{frag}$	$\sigma_{MC}$ [mbarn]
He	$789 \pm 35 \pm 67$	4.4%	8.5%	$705 \pm 2$
Li	$101 \pm 13 \pm 10$	12.5%	10.4%	$74.9 \pm 0.6$
Be	$33 \pm 9 \pm 3$	26%	10.3%	$37.5 \pm 0.4$
B	$78 \pm 11 \pm 6$	14%	8.5%	$41.8 \pm 0.4$
C	$131 \pm 14 \pm 4$	11%	2.8%	$87.7 \pm 0.6$
N	$117 \pm 14 \pm 6$	12%	4.8%	$110.3 \pm 0.7$

<b>He</b>	<b><math>695 \pm 31 \pm 4</math></b>
<b>Li</b>	<b><math>59 \pm 6 \pm 1</math></b>
<b>Be</b>	<b><math>38 \pm 5 \pm 1</math></b>
<b>B</b>	<b><math>61 \pm 8 \pm 2</math></b>
<b>C</b>	<b><math>134 \pm 11 \pm 2</math></b>
<b>N</b>	<b><math>116 \pm 8 \pm 3</math></b>

# Conclusions and perspectives

Data seem to agree among runs

Merged all the statistics with target

Added systematics of the subtraction method

Bayes selected as unfolding method, others in systematics

To add: geometric efficiency for  $Z=2$

**We started writing!**

**Thanks for listening!**