

Thermal Axions: What's Next?

**Francesco
D'Eramo**



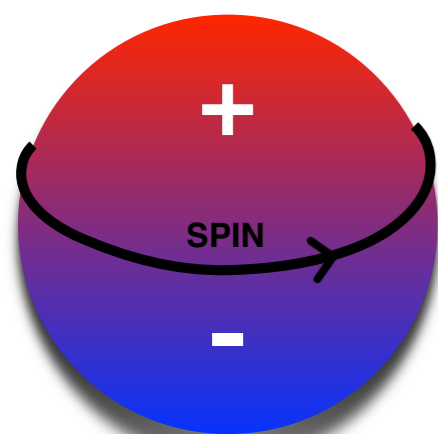
UNIVERSITÀ
DEGLI STUDI
DI PADOVA



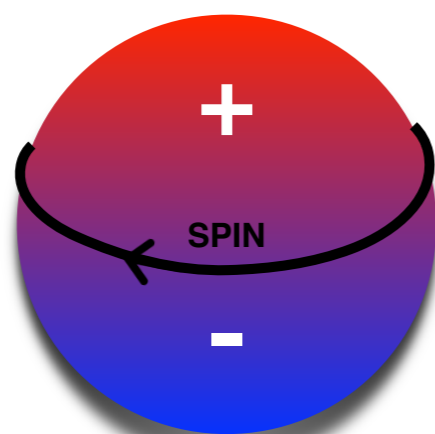
Virtues of the QCD Axion



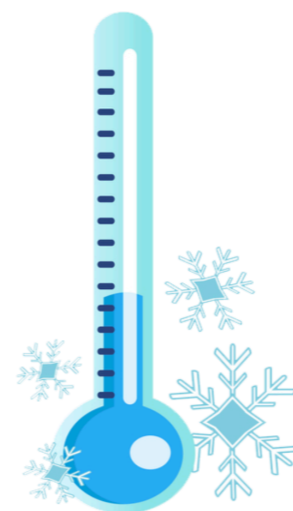
Strong CP



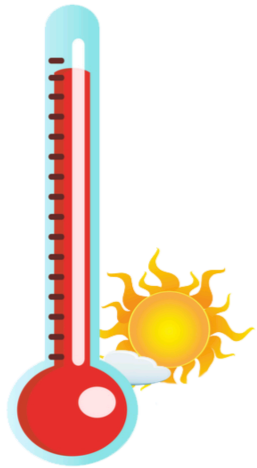
T
I
M
E
R
E
V
E
R
S
A
L



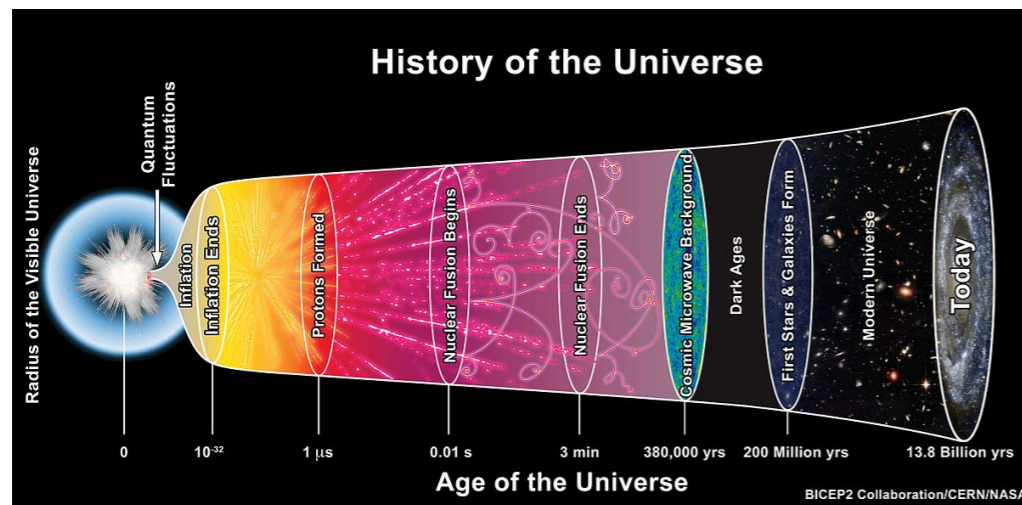
Cold Dark Matter



Plan for today: Hot Axions



Axions produced with kinetic energy much larger than their mass (i.e. “hot”)

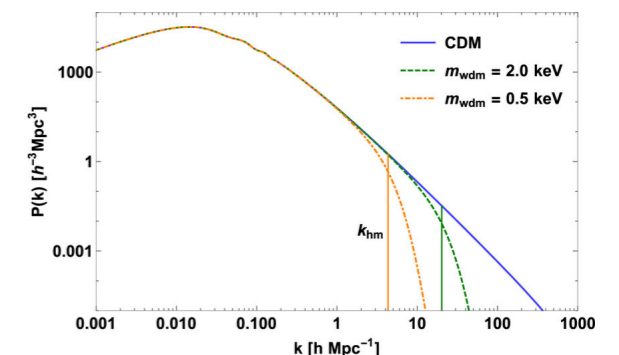
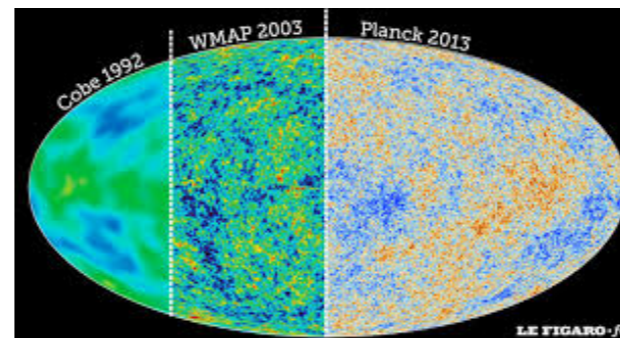


I. Production

Processes with particles from the primordial thermal bath

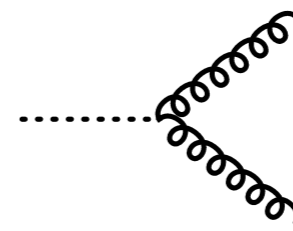
2. Signals

Dark radiation or warm dark matter

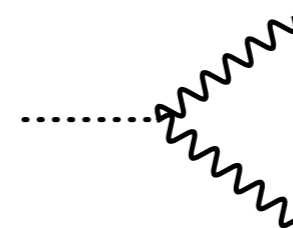


Thermal Production

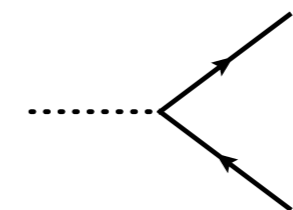
Scatterings and/or decays
involving primordial thermal
bath particles
(axion energy $\gg m_a$, i.e. “hot”)



$$\frac{\alpha_s}{8\pi} \frac{a}{f_a} G^{\mu\nu} \tilde{G}_{\mu\nu}$$



$$c_{\gamma\gamma} \frac{\alpha_{\text{em}}}{8\pi} \frac{a}{f_a} F^{\mu\nu} \tilde{F}_{\mu\nu}$$



$$c_\psi \frac{\partial_\mu a}{f_a} \bar{\psi} \gamma^\mu \gamma^5 \psi$$

Unavoidable
Production Source!

Observable Effects

Dark Radiation

Additional radiation at:

- BBN ($m_a \lesssim \text{MeV}$)
- CMB formation ($m_a \lesssim 0.3 \text{ eV}$)

$$\rho_{\text{rad}} = \left[1 + \frac{7}{8} \left(\frac{T_\nu}{T_\gamma} \right)^4 N_{\text{eff}} \right] \rho_\gamma$$

$$\Delta N_{\text{eff}} = \frac{8}{7} \left(\frac{11}{4} \right)^{4/3} \frac{\rho_a}{\rho_\gamma}$$

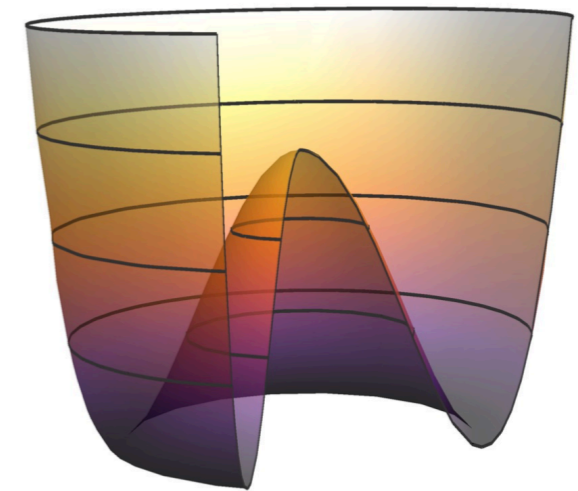
Warm Dark Matter

If $m_a \sim \text{eV}$ we have a warm dark matter component
(exactly as neutrinos in the standard model)

QCD Axion or ALPs?

Axion-Like-Particles (ALPs) are ubiquitous in extension of the standard model

- Pseudo-Nambu-Goldstone-bosons
- Axions in string theory



QCD Axion

$$m_a \simeq 5.7 \left(\frac{10^9 \text{ GeV}}{f_a} \right) \text{ meV}$$

ALPs

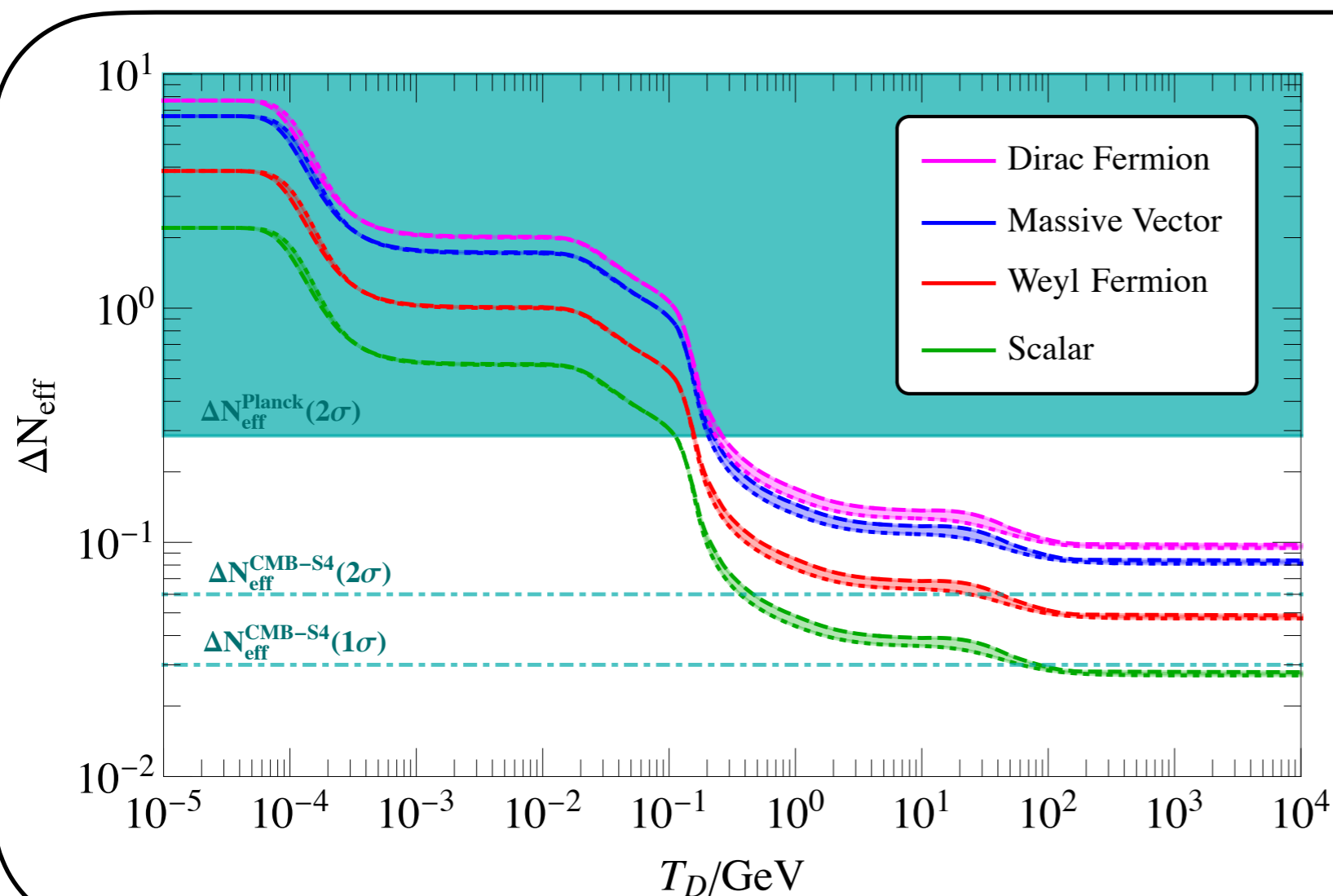
$$m_a \simeq \Lambda_X^2 / f_X$$

Results in this talk mostly about the QCD axion
(easily generalized when the mass is negligible)

How to Predict ΔN_{eff}

ΔN_{eff} - I: Instantaneous decoupling

- Assume they thermalize at early times
- Estimate the decoupling temperature from $\Gamma(T_D) = H(T_D)$



$$\Delta N_{\text{eff}} \simeq 0.027 \left(\frac{106.75}{g_{*s}(T_D)} \right)^{4/3}$$

How to Predict ΔN_{eff}

ΔN_{eff} - I: Instantaneous decoupling

- Assume they thermalize at early times
- Estimate the decoupling temperature from $\Gamma(T_D) = H(T_D)$

ΔN_{eff} - II: Boltzmann equation for n_a

- Track the number density of axions
- Convert the asymptotic result via the equilibrium distribution

$$\frac{dn_a}{dt} + 3Hn_a = \sum_{\alpha} \gamma_{\alpha}$$

$$\Delta N_{\text{eff}} \simeq 74.85 Y_a^{4/3}$$

$\alpha =$ Production processes

How to Predict ΔN_{eff}

ΔN_{eff} - I: Instantaneous decoupling

- Assume they thermalize at early times
- Estimate the decoupling temperature from $\Gamma(T_D) = H(T_D)$

ΔN_{eff} - II: Boltzmann equation for n_a

- Track the number density of axions
- Convert the asymptotic result via the equilibrium distribution



Equilibrium thermodynamics for the conversion to energy

Spectral distortions neglected

Maxwell-Boltzmann statistics (i.e., no quantum effects)

Static thermal bath (i.e., no energy exchanged)

Scenarios for Hot Axions

Single Coupling Switched On

Axion production controlled by its interaction with a given Standard Model field

Ferreira, Notari, **Phys.Rev.Lett.** **120** (2018)

FD et al, **JCAP** **11** (2018)

Arias-Aragón et al., **JCAP** **11** (2020)

and **JCAP** **03** (2021)

Green et al., **JCAP** **02** (2022)

UV Completions

FD, Hajkarim, Yun, **JHEP** **10** (2021)

- **KSVZ Axion:** Standard Model fields are PQ-neutral and color anomaly from heavy colored and PQ-charged fermion Ψ

Kim, PRL 43 (1979)

Shifman, Vainshtein, Zakharov, NPB 166 (1980)

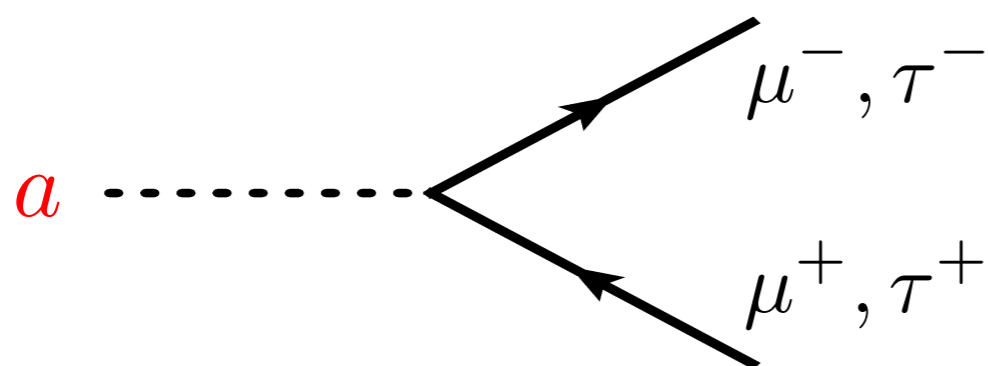
- **DFSZ Axion:** Standard Model fields charged (two Higgs doublets) and color anomaly from quarks

Zhitnitsky, SJNP 31 (1980)

Dine, Fischler, Srednicki, PLB 104 (1981)

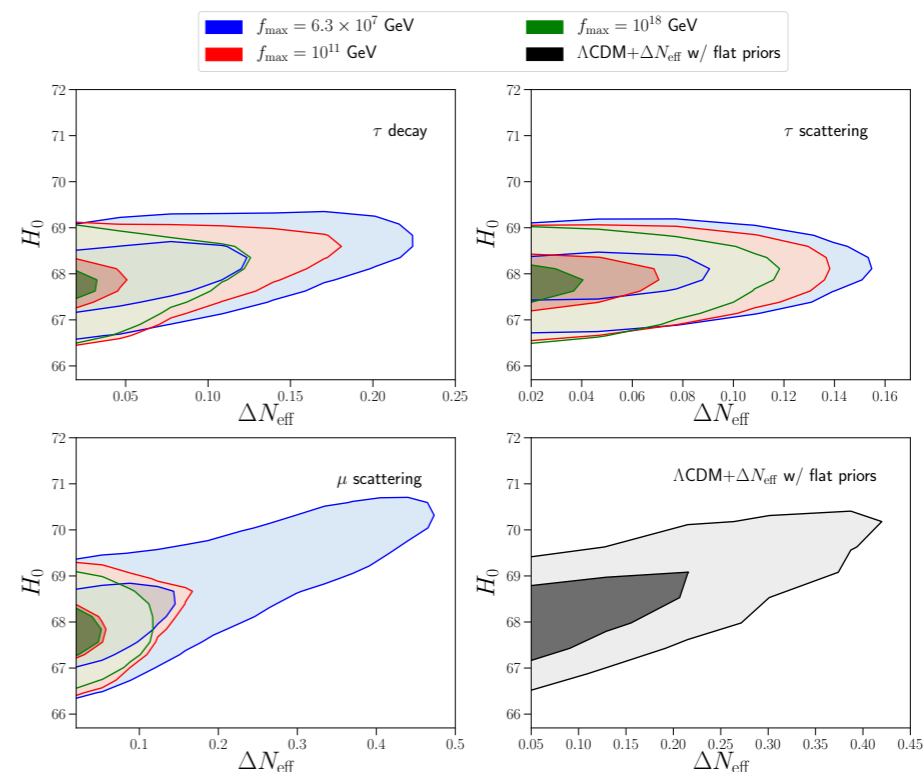
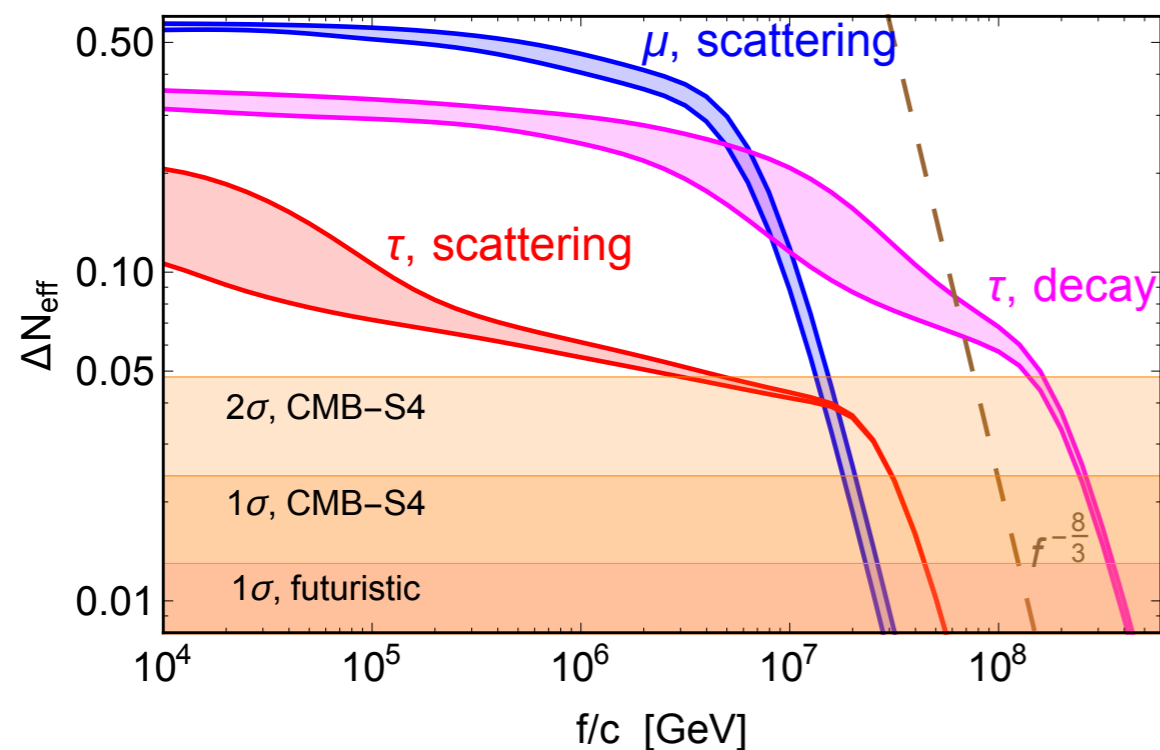
A Leptophilic Axion

Leptons



FD, Ferreira, Notari, Bernal, **JCAP 1811 (2018)**

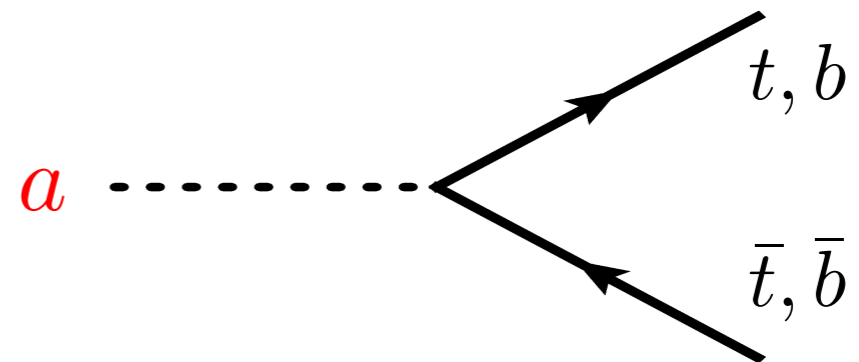
They can alleviate
**the Hubble
tension**



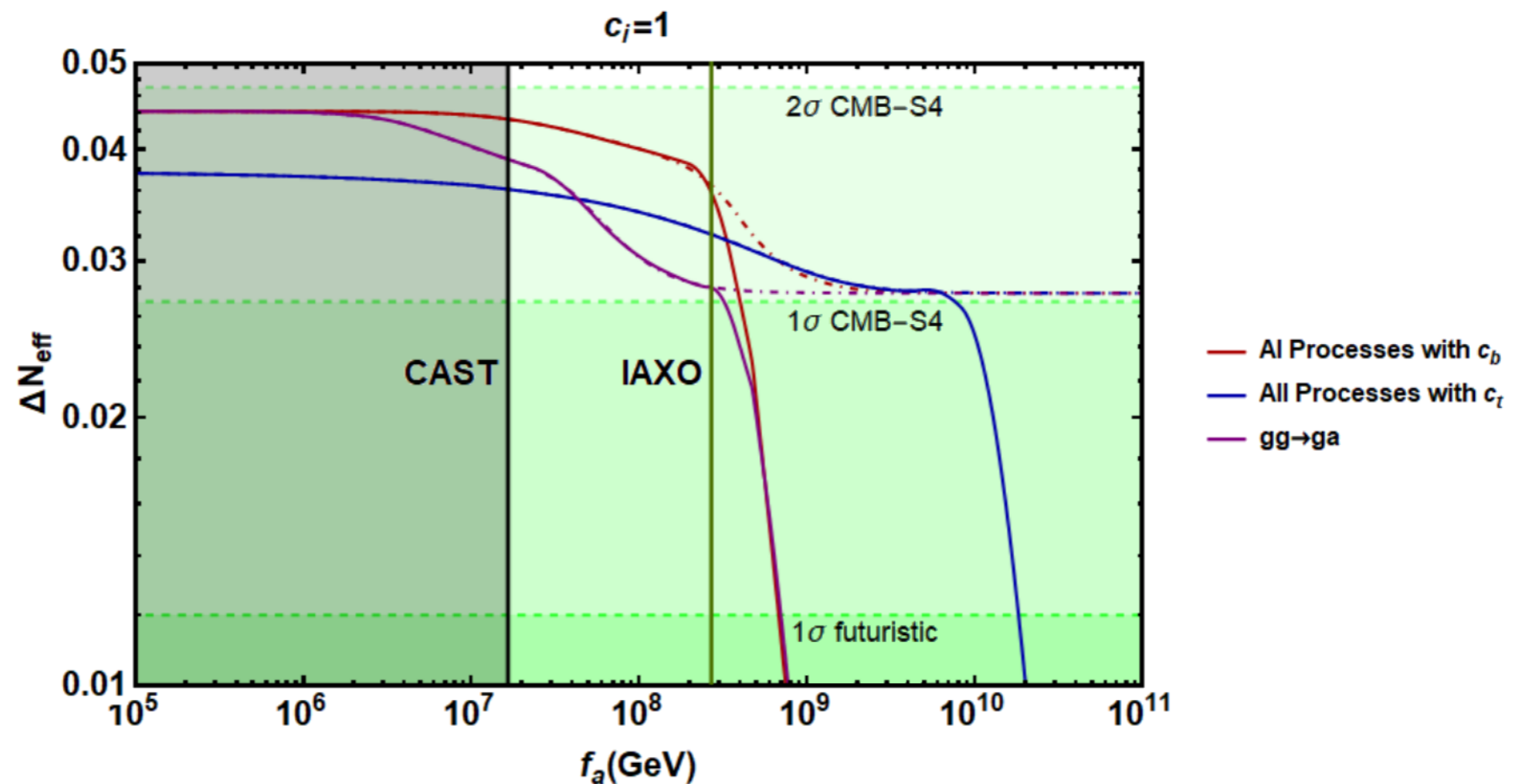
Axion Coupled to Heavy Quarks

Smooth rate
across EWPT,
within reach of
CMB-S4
surveys

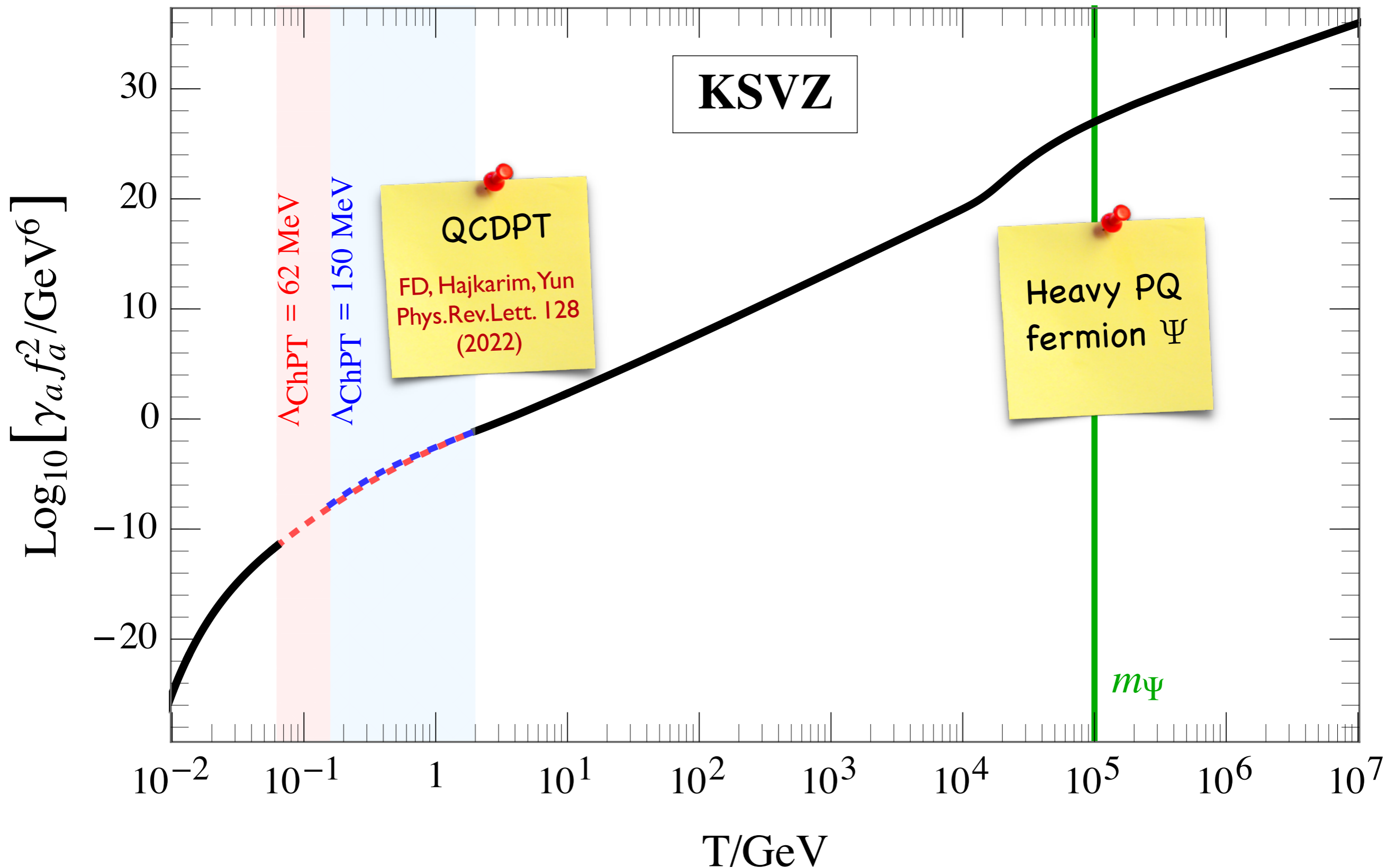
3rd Gen. Quarks



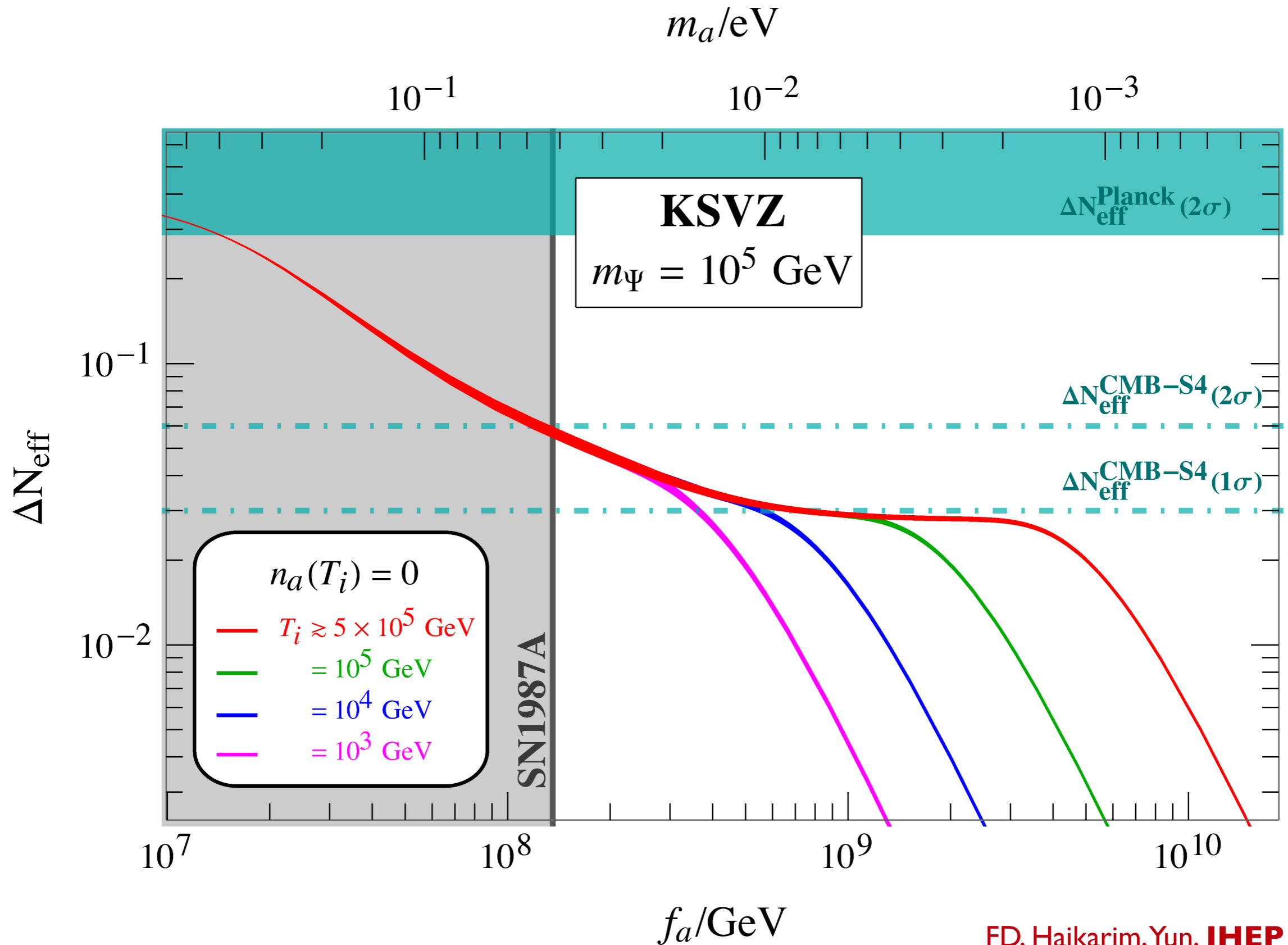
Arias-Aragon, FD, Ferreira, Merlo, Notari, **JCAP 03 (2021)**



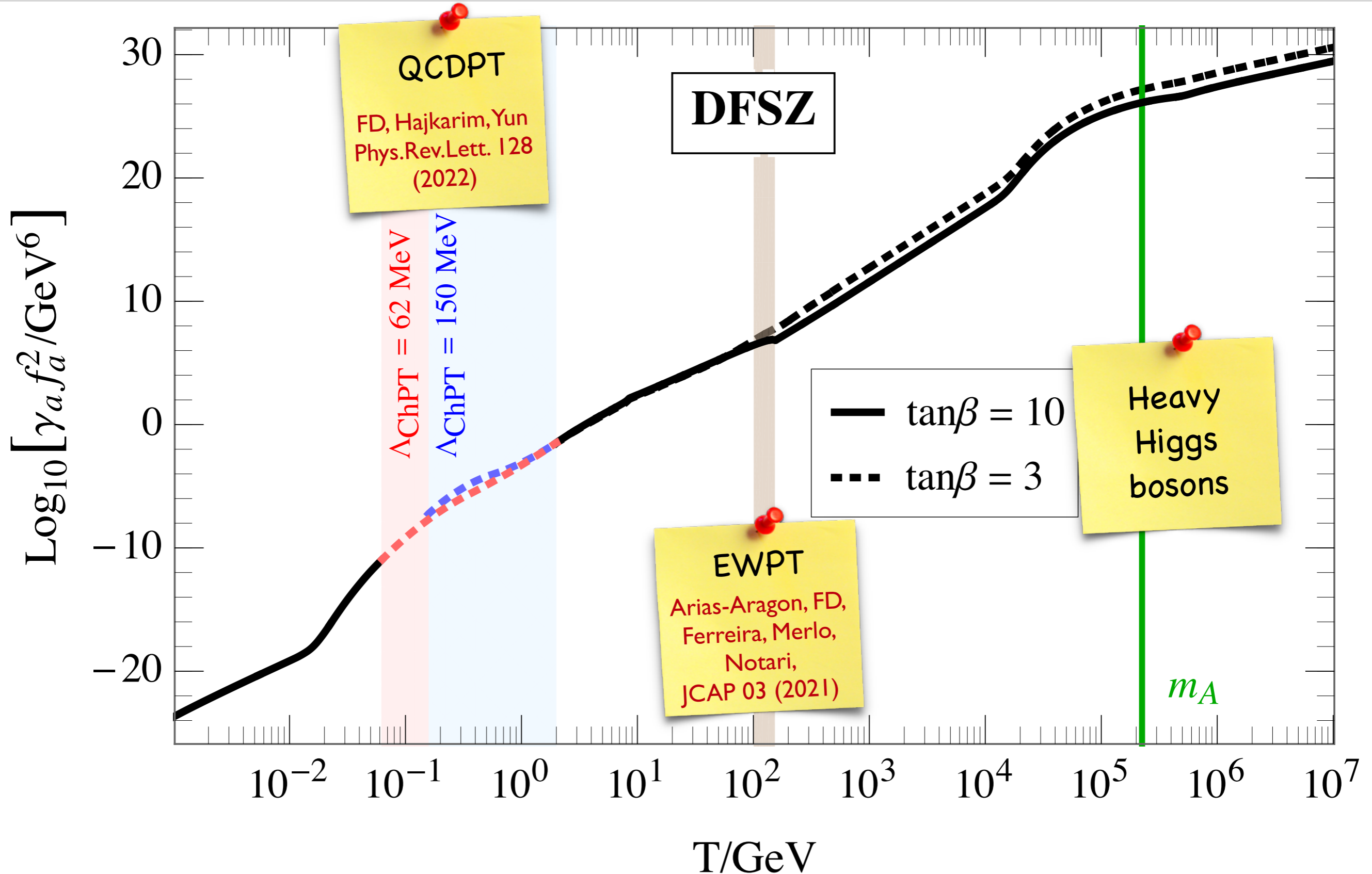
KSVZ Axion — Production Rate



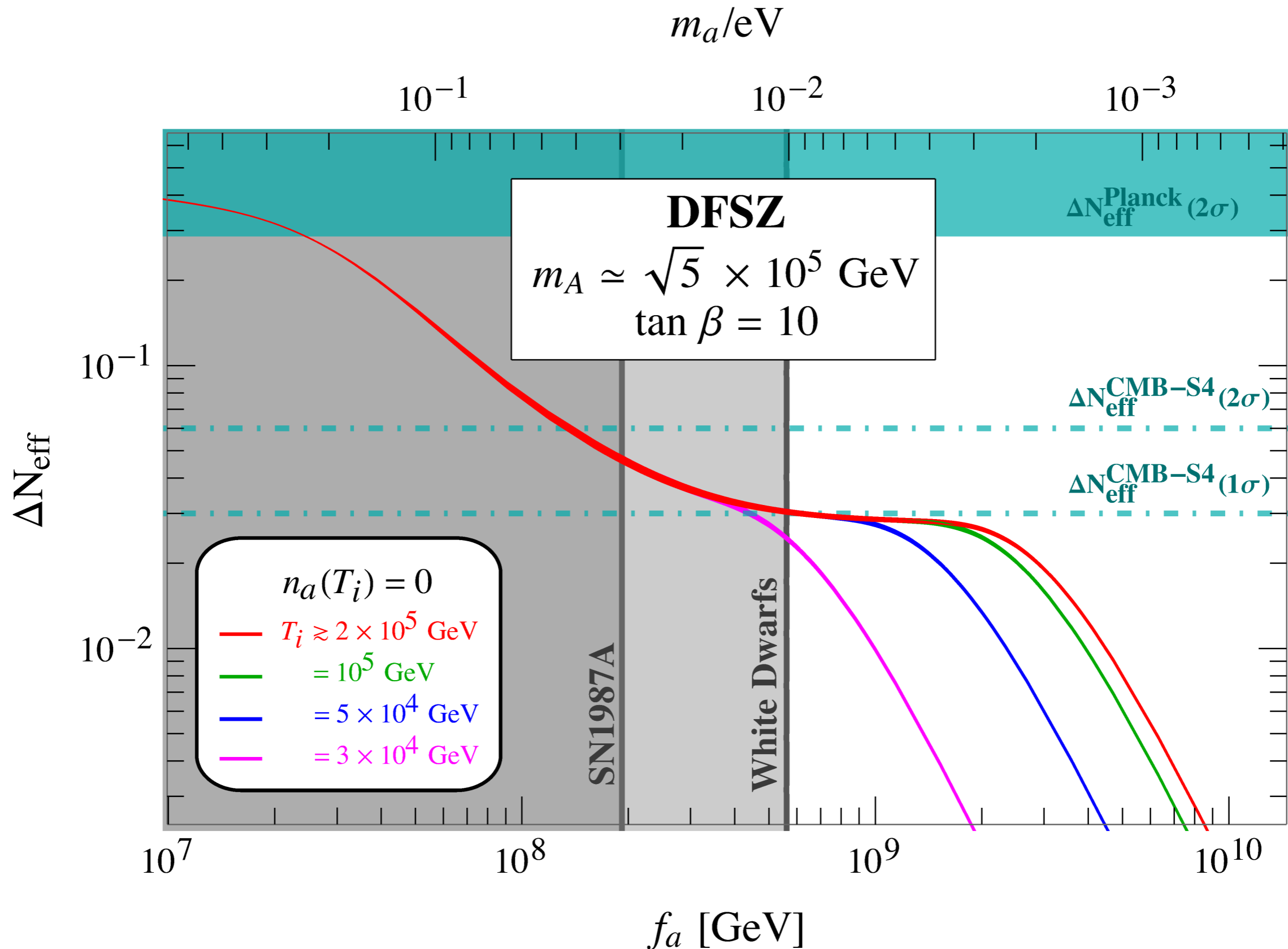
KSVZ Axion — Results for ΔN_{eff}



DFSZ Axion — Production Rate



DFSZ Axion — Results for ΔN_{eff}



Finite QCD Axion Mass Effects?

Planck: tension with astrophysics and axion mass non-negligible

Finite axion mass

- Pion scatterings

Ferreira et al., **Phys.Rev.D 103 (2021)**

Notari et al., **Phys.Rev.Lett. 131 (2023)**

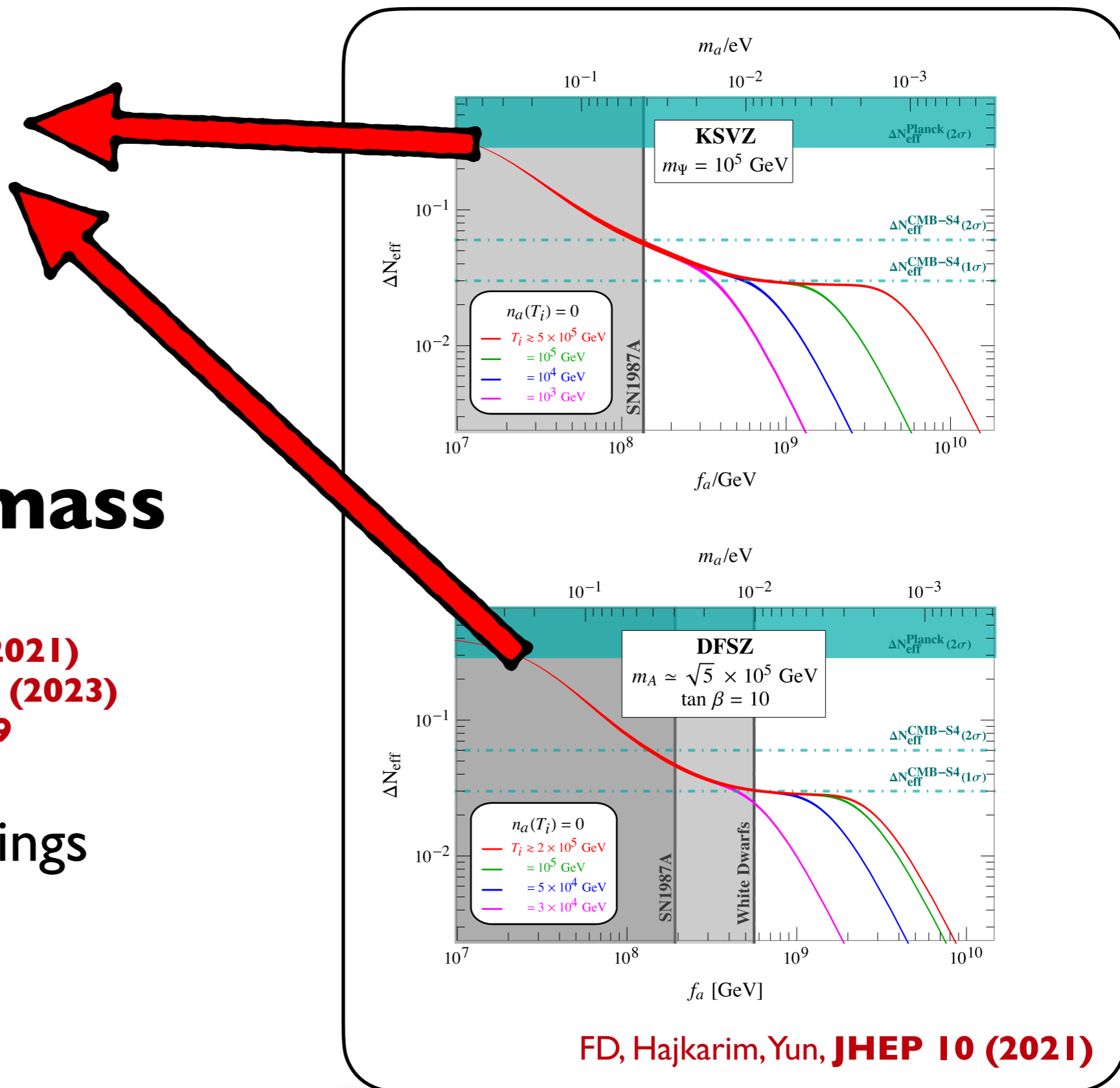
Bianchini et al., **arXiv:2310.08169**

- Gluon, photon couplings

Caloni et al., **JCAP 09 (2022)**

- KSVZ and DFSZ

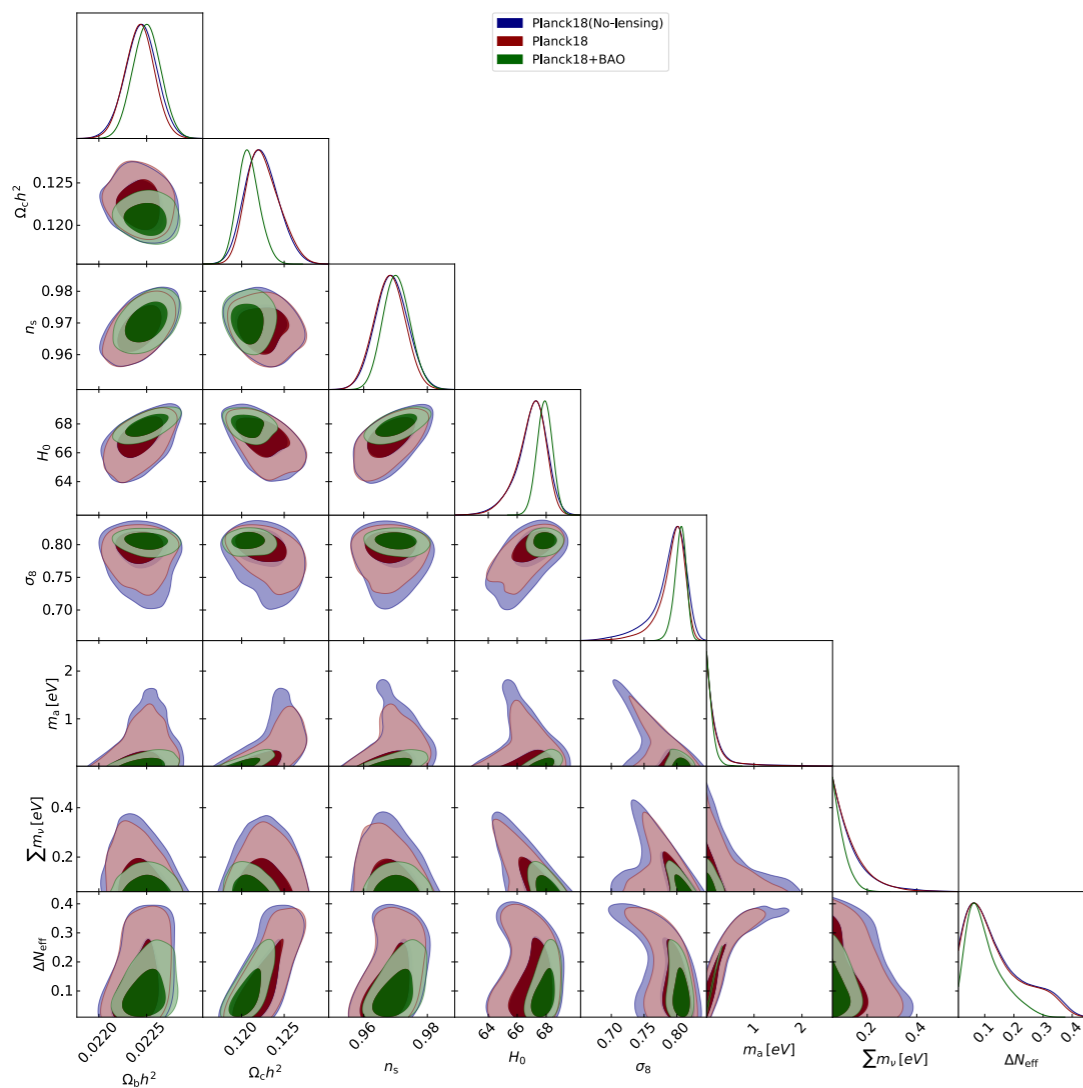
FD et al., **JCAP 09 (2022)**



FD, Hajkarim, Yun, **JHEP 10 (2021)**

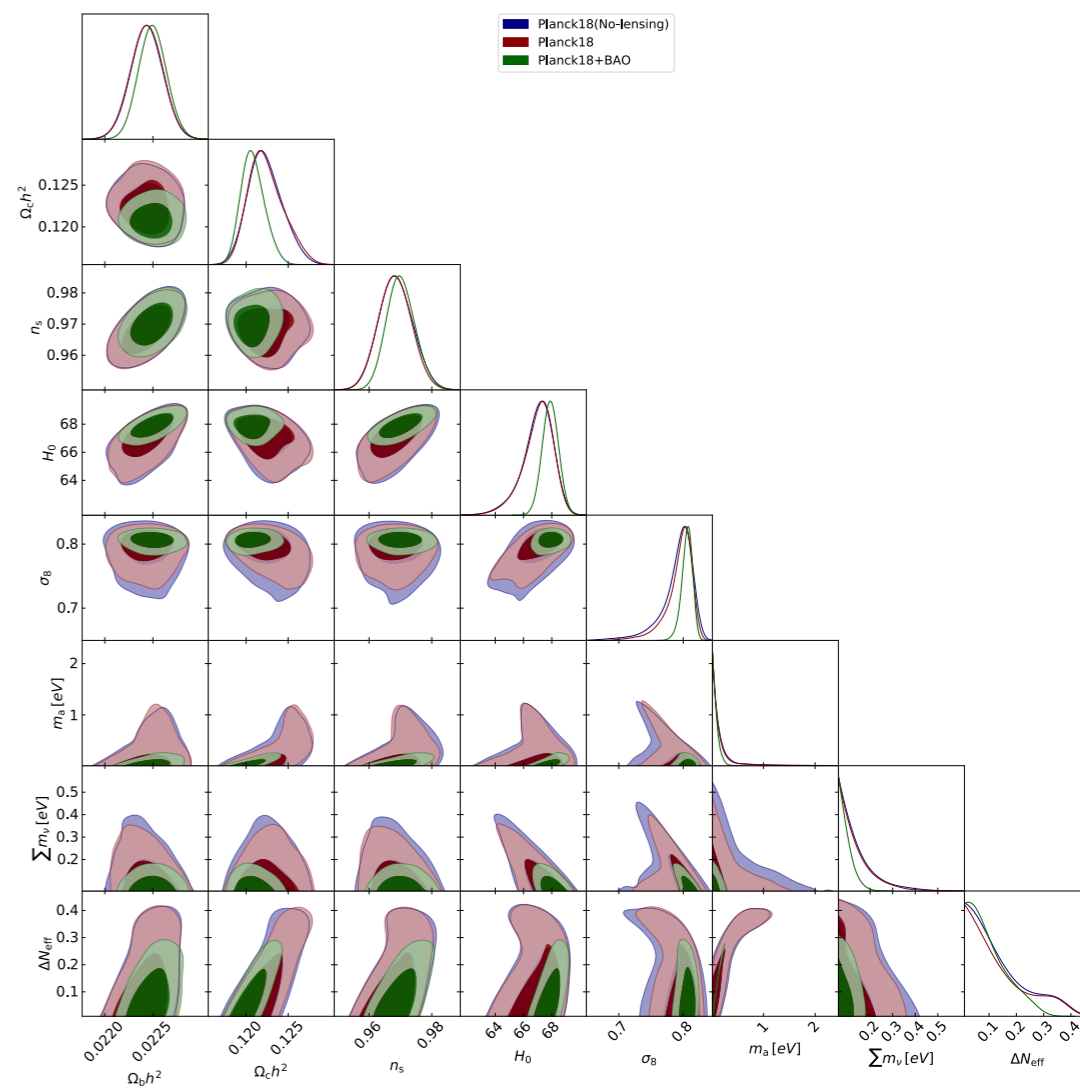
Axion Mass Bound

KSVZ



$$m_a \leq 0.282(0.420) \text{ eV}$$

DFSZ



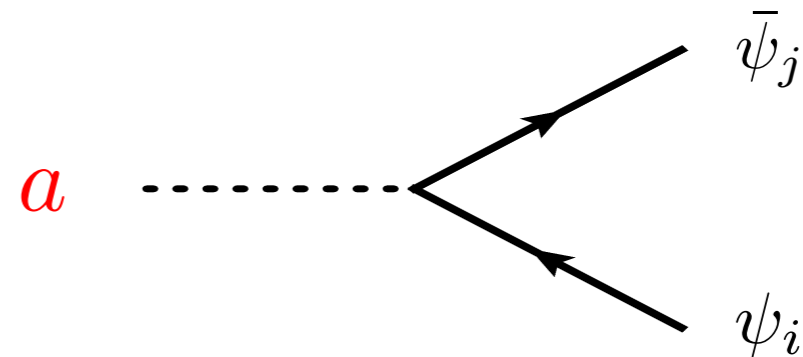
$$m_a \leq 0.209(0.293) \text{ eV}$$

A Minor Variation: FV Axions

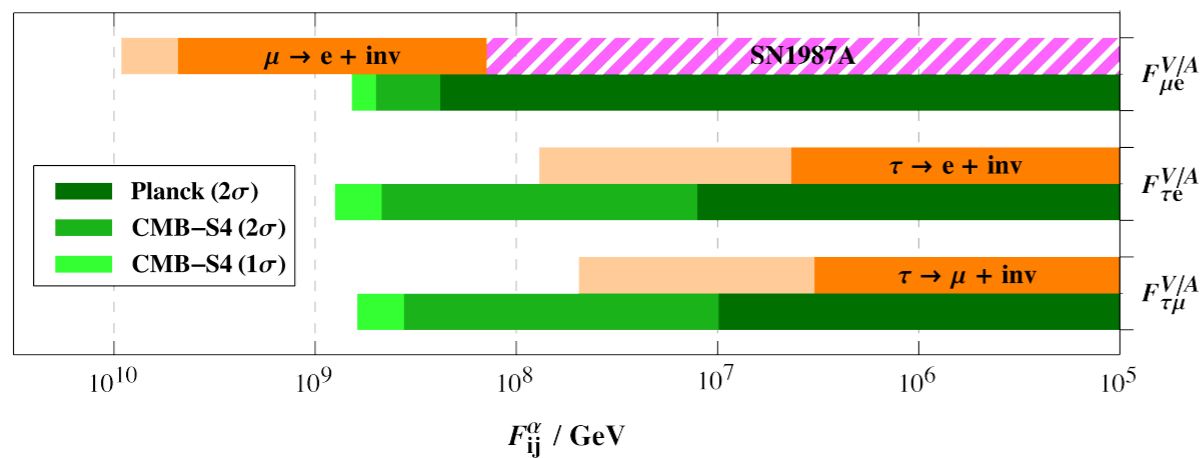
Target of several terrestrial experiments

What about their role in the early universe?

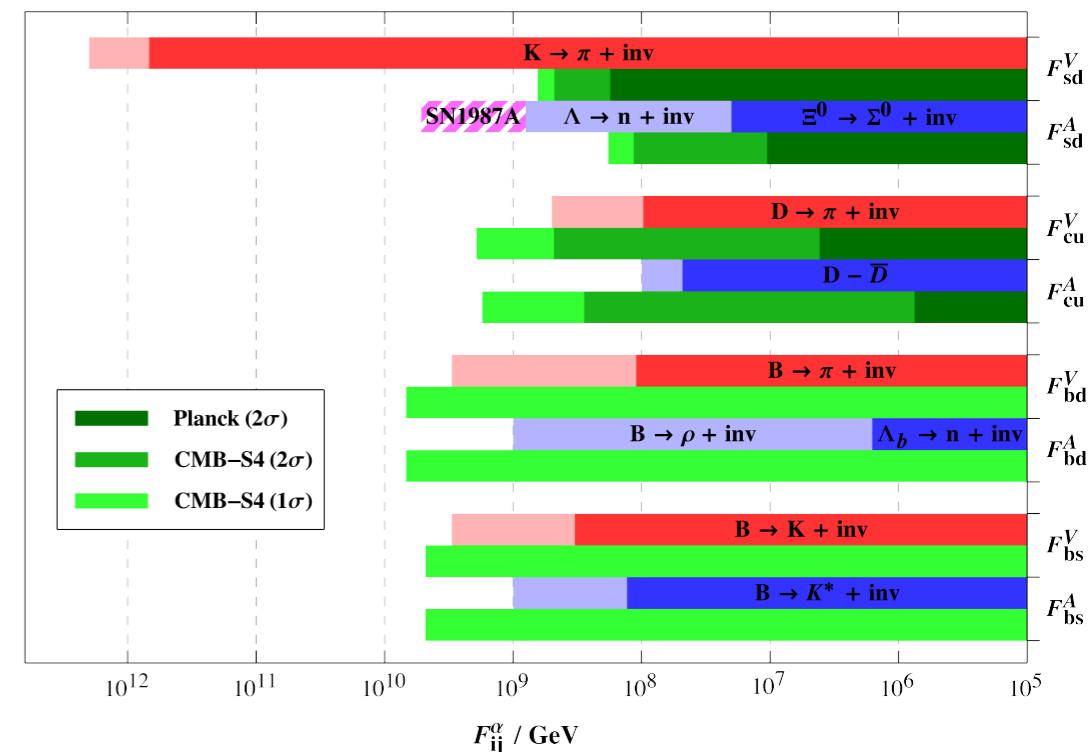
$$\mathcal{L}_{\text{FV}}^{(a)} = \frac{\partial_\mu a}{2f_a} \sum_{\psi_i \neq \psi_j} \bar{\psi}_i \gamma^\mu \left(c_{\psi_i \psi_j}^V + c_{\psi_i \psi_j}^A \gamma^5 \right) \psi_j$$



Leptonic FV

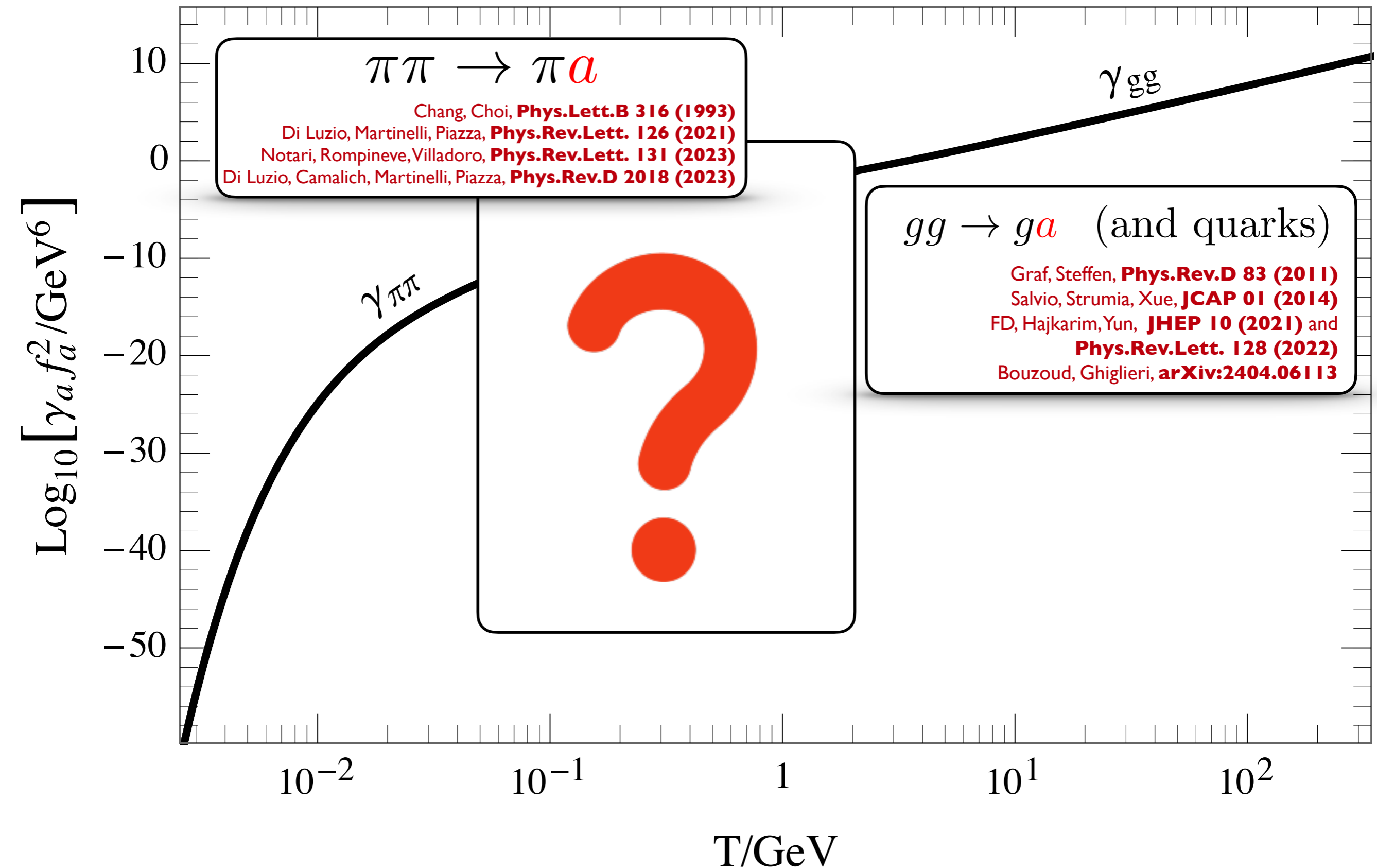


Hadronic FV

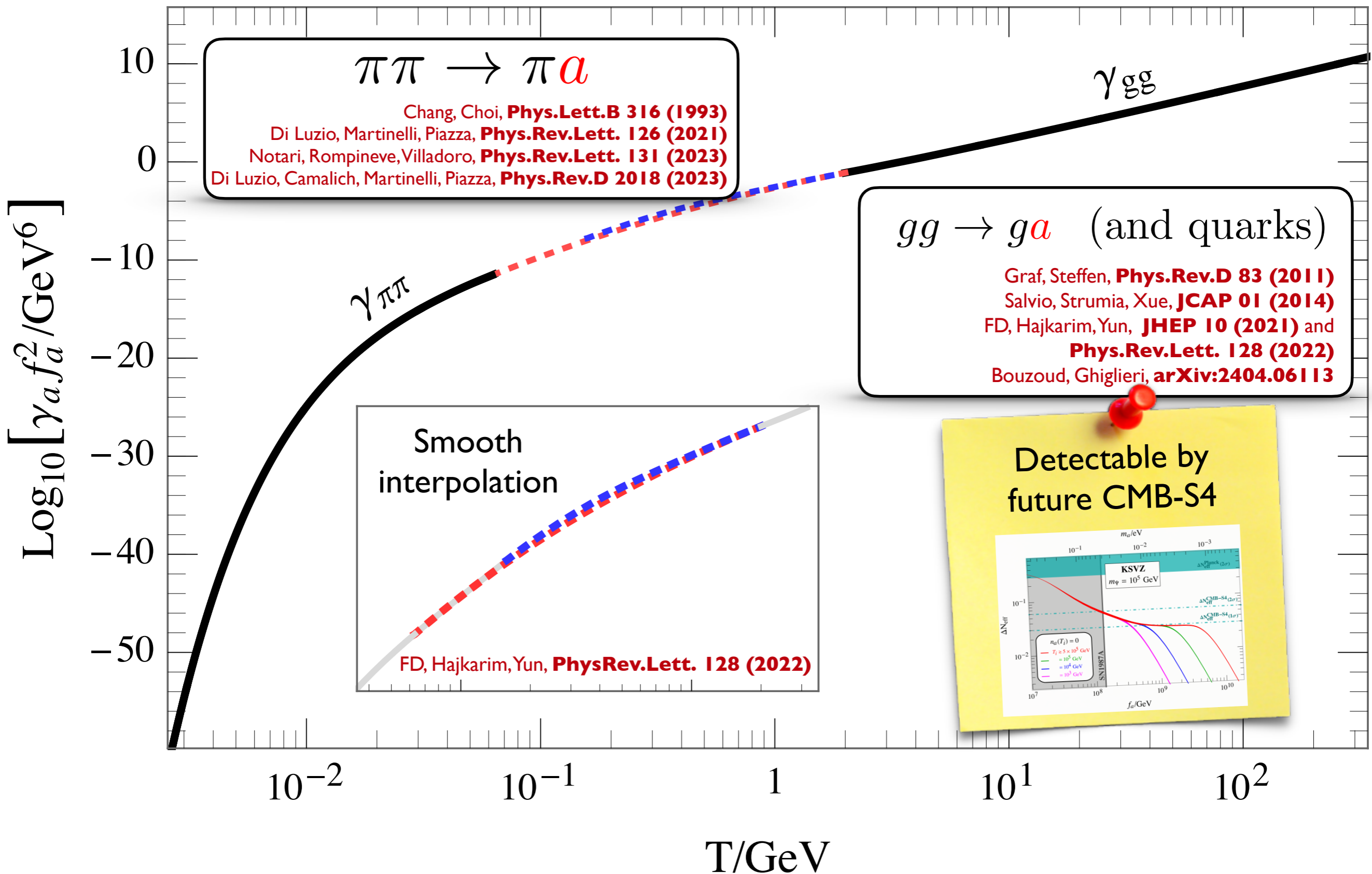


Current and future cosmological bounds competitive (or sometimes even better!) than terrestrial searches

Where Do We Stand?



Where Do We Stand?



What's Next?

Axion production rate
across the confinement scale still unknown

$$\gamma_a = n_i n_j \times \langle \sigma_{ij \rightarrow ja} v_{\text{rel}} \rangle$$

Thermal bath

Particle Physics

1. Pion cross section beyond LO? Other hadrons?
2. Thermal bath description between 150 MeV and fews GeV?
3. Boltzmann equation evolution and cosmological observables?

Back to the Phase-Space

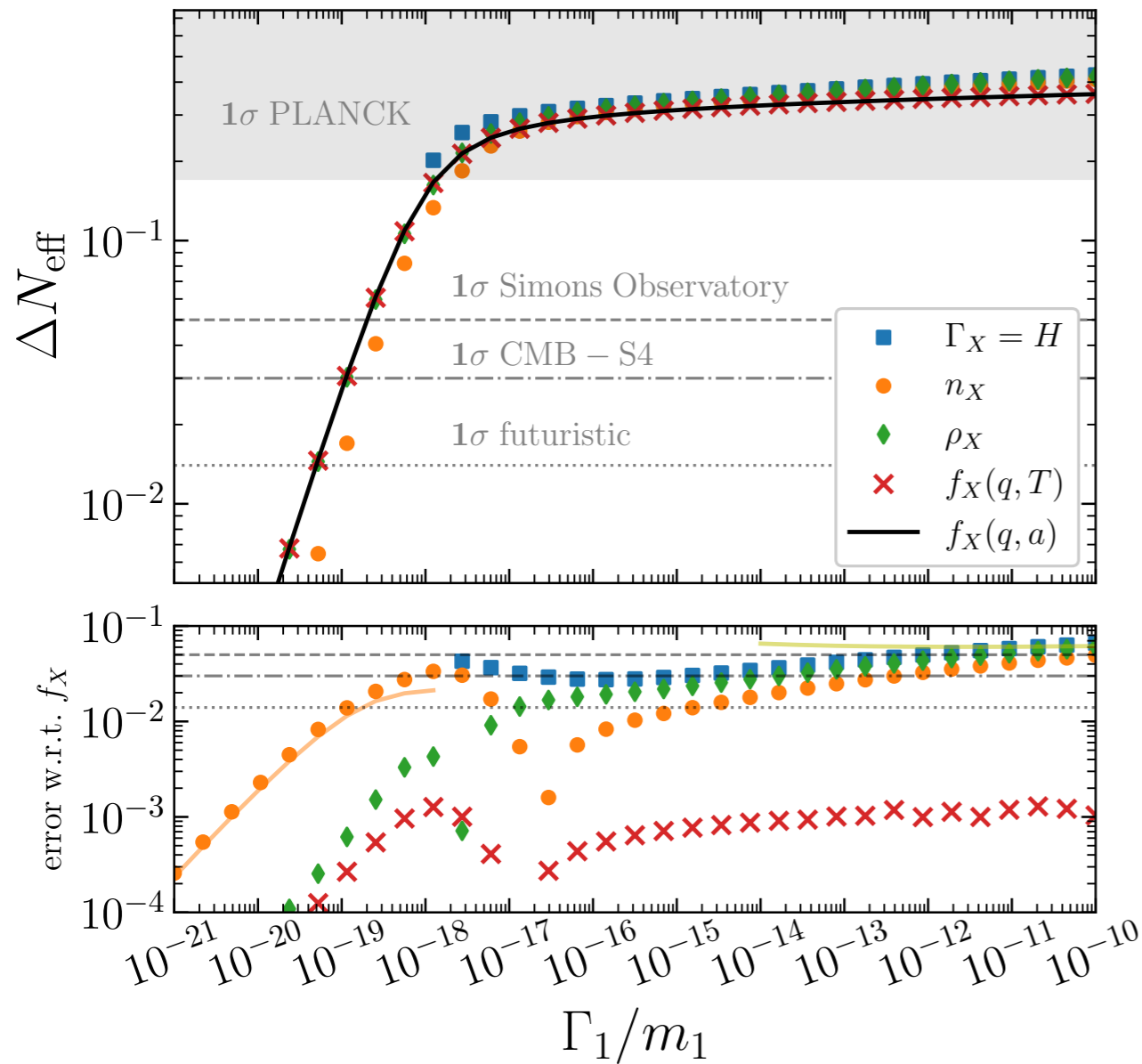
Model-independent analysis: $\mathcal{B}_1 \dots \mathcal{B}_n \rightarrow \mathcal{B}_{n+1} \dots \mathcal{B}_m X$
generic production of a light X

$$\frac{df_X(k, t)}{dt} = \left(1 - \frac{f_X(k, t)}{f_X^{\text{eq}}(k, t)} \right) \mathcal{C}_{n \rightarrow m X}(k, t)$$

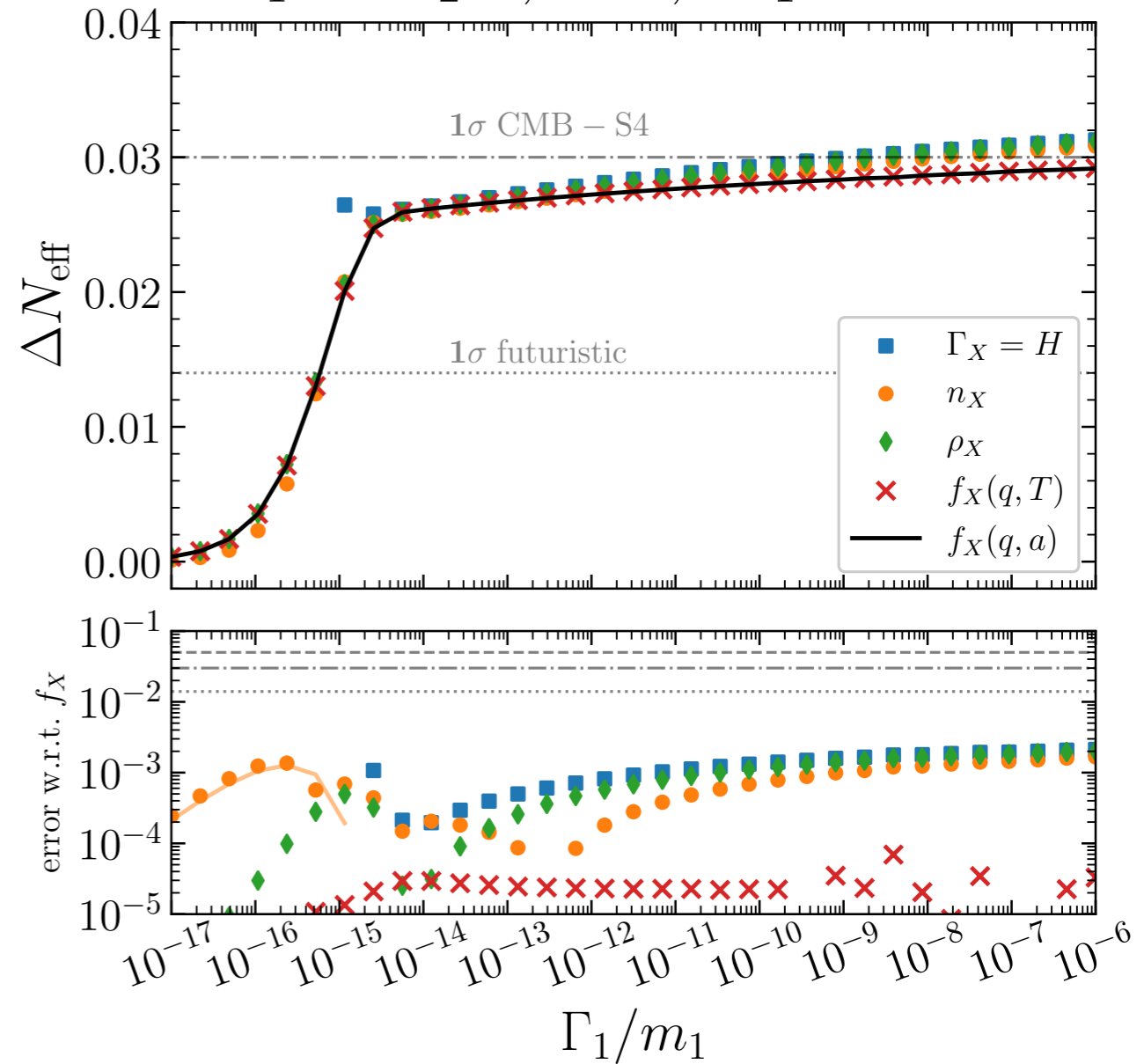
1. Keep track of phase-space and compute the energy density
2. Quantum statistical effects take into account
3. Energy exchanged with the thermal bath accounted for

Error in predicting ΔN_{eff}

$\mathcal{B}_1 \rightarrow \mathcal{B}_2 X$, MB, $m_1 = 1 \text{ GeV}$



$\mathcal{B}_1 \rightarrow \mathcal{B}_2 X$, MB, $m_1 = 1 \text{ TeV}$



Axion-Fermion Interactions

$$\mathcal{L}_{\text{int}} = \frac{\partial_{\mu} a}{2f_a} \sum_{\psi} c_{\psi} \bar{\psi} \gamma^{\mu} \gamma_5 \psi$$

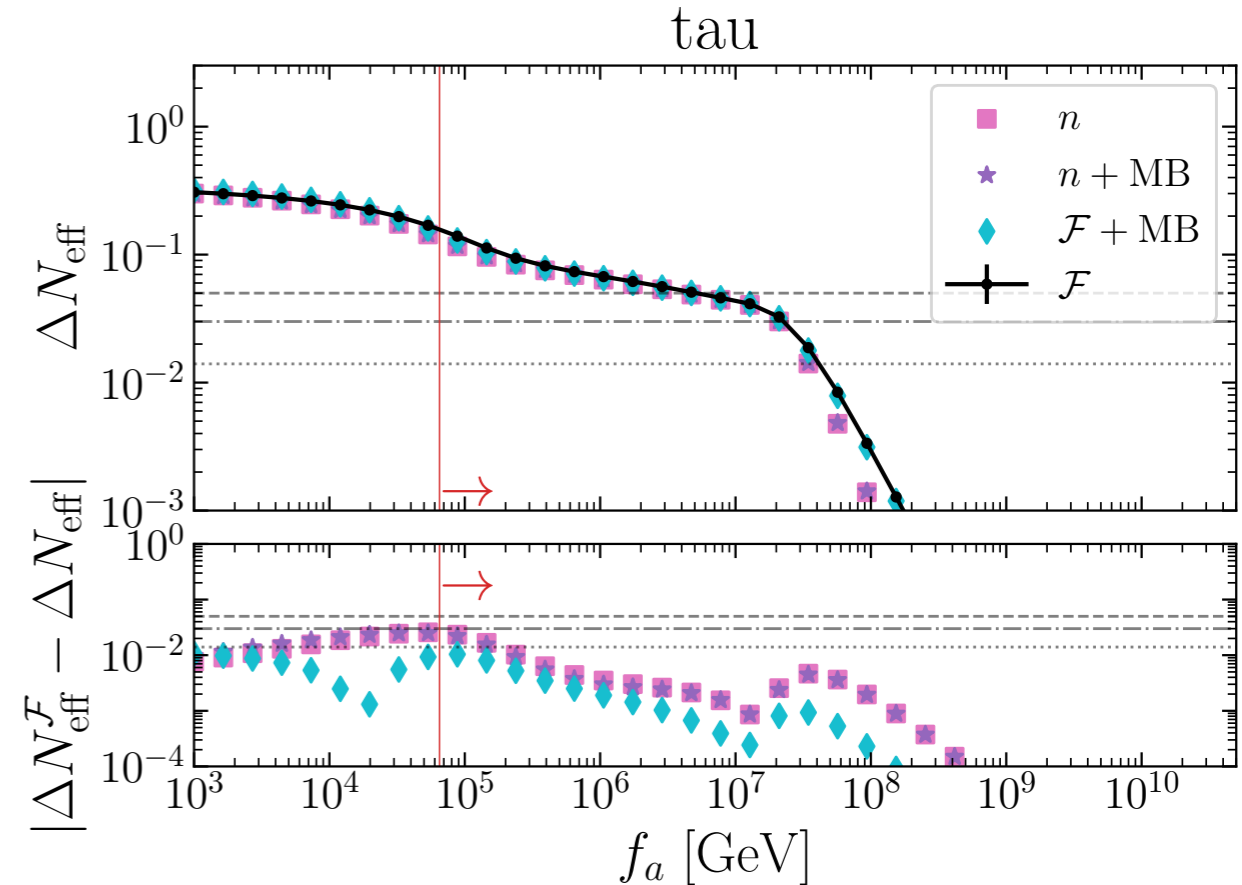
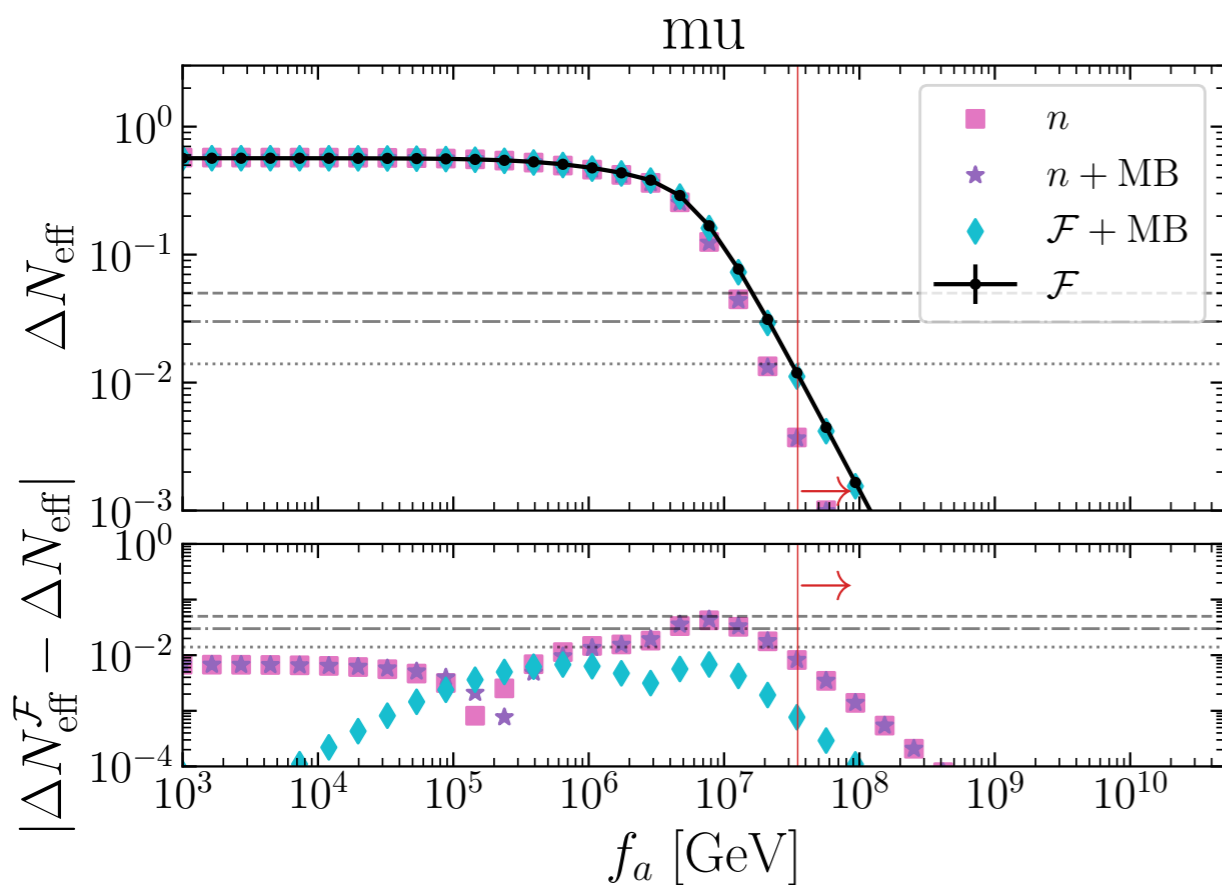
Recent studies performed
by tracking the axion
number density

Baumann et al, **Phys.Rev.Lett.** **117** (2016)
Ferreira, Notari, **Phys.Rev.Lett.** **120** (2018)
FD et al, **JCAP** **11** (2018)
Arias-Aragón et al., **JCAP** **11** (2020)
Arias-Aragón et al., **JCAP** **03** (2021)
Green et al., **JCAP** **02** (2022)

Will it change if we go back to the phase space?

Axion-Fermion Interactions

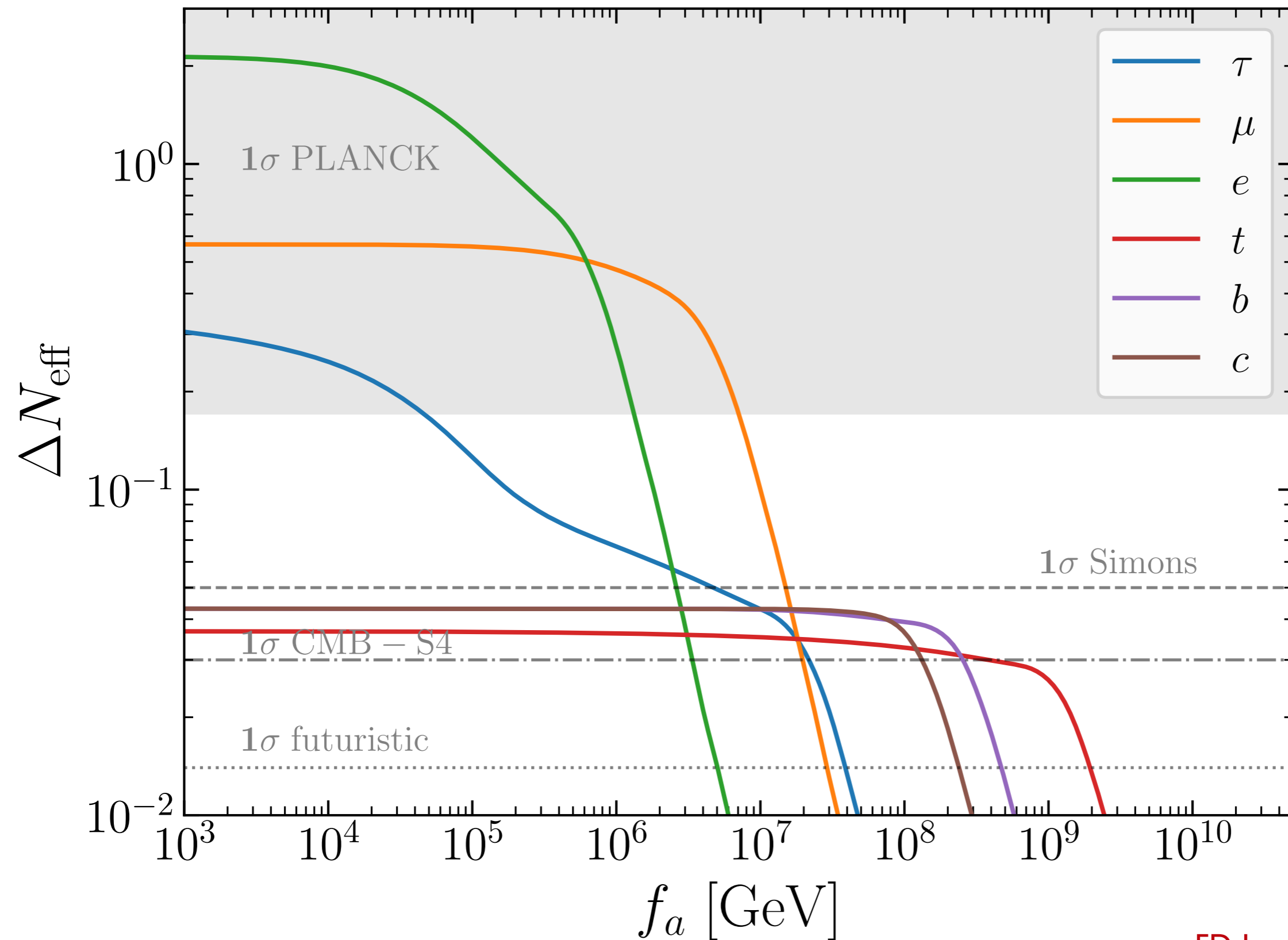
PRELIMINARY



Difference detectable by future CMB-S4 surveys!

- MUON: effect maximum in regions in tension with stellar bounds
- TAU: effect maximum in allowed regions

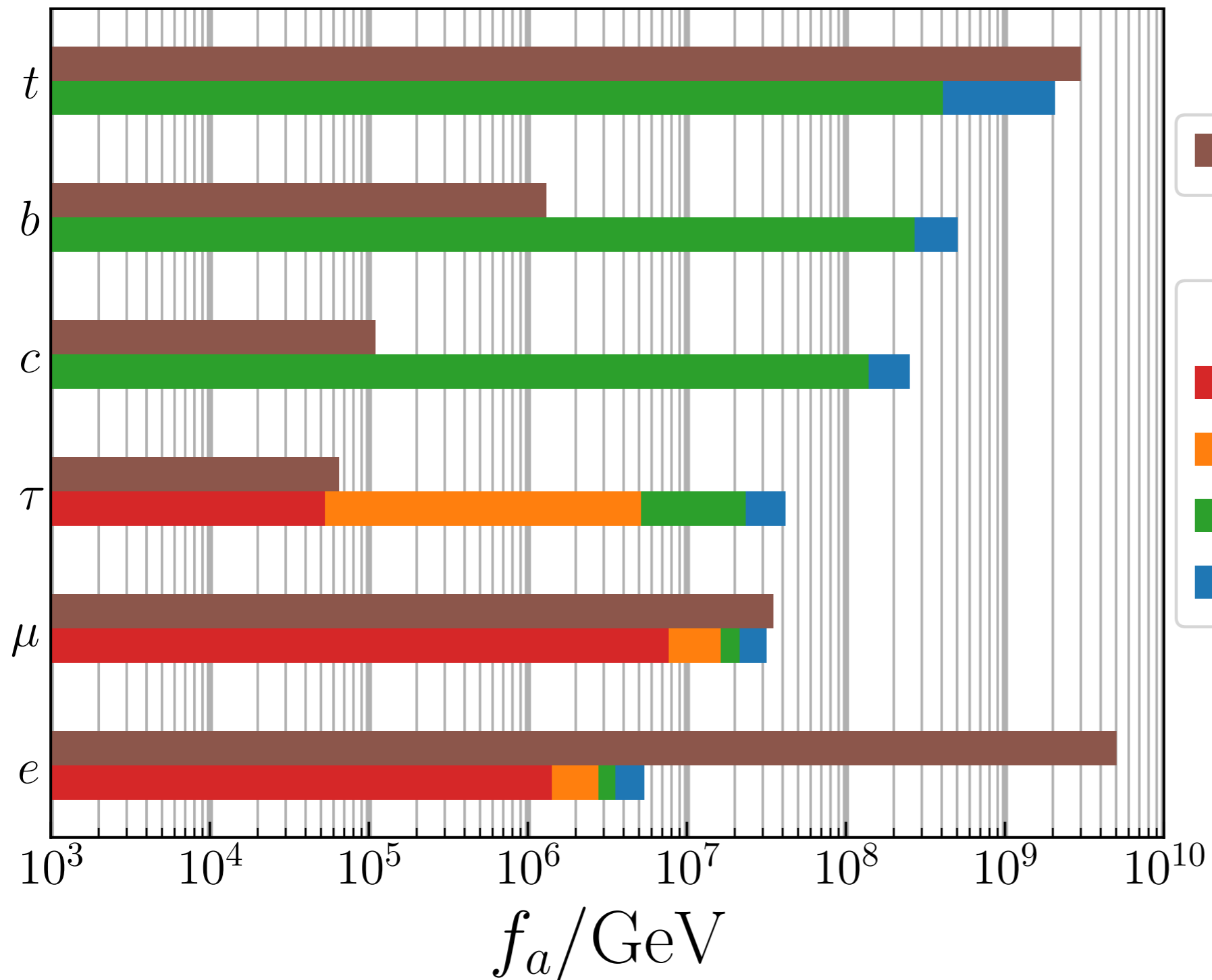
Axion-Fermion Interactions



PRELIMINARY

Axion-Fermion Interactions

PRELIMINARY



Outlook



Peccei-Quinn Mechanism and the QCD Axion

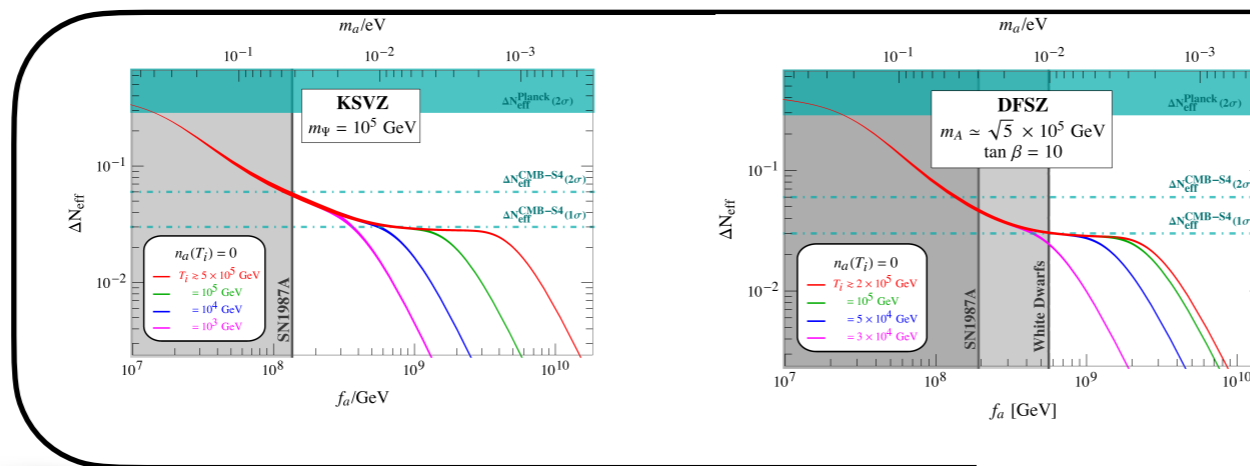
Motivated and testable scenario rich of cosmological consequences

Thermal Axions

Complementary to other probes of the PQ mechanism

Distinct signatures of ALPs coupled to standard model particles

Outlook



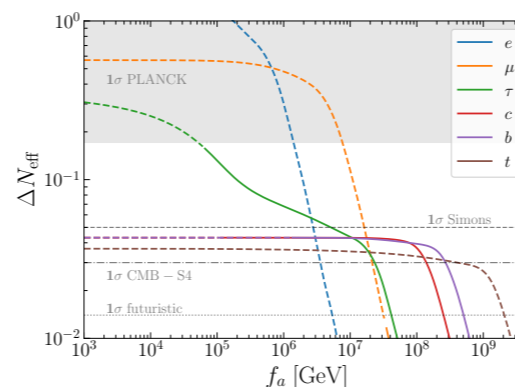
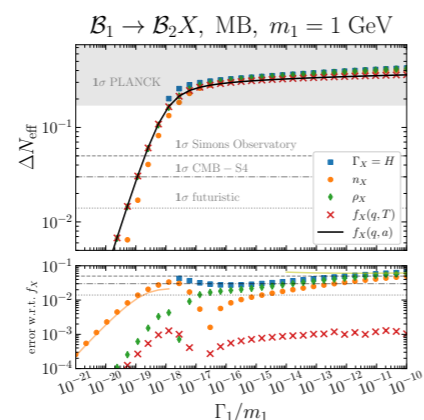
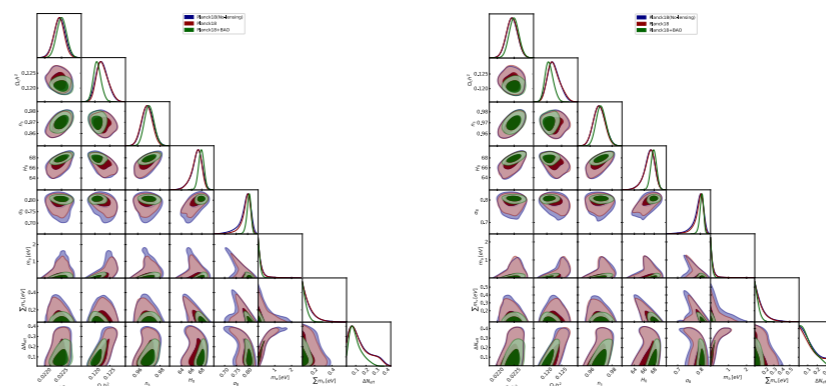
ΔN_{eff} tracking the number density

FD, Hajkarim, Yun, **JHEP 10 (2021)**

FD, Hajkarim, Yun, **Phys.Rev.Lett. 128 (2022)**

FD, Di Valentino, Giarè, Hajkarim, Melchiorri, Mena, Renzi, Yun, **JCAP 09 (2022)**

Axion cosmological mass bound

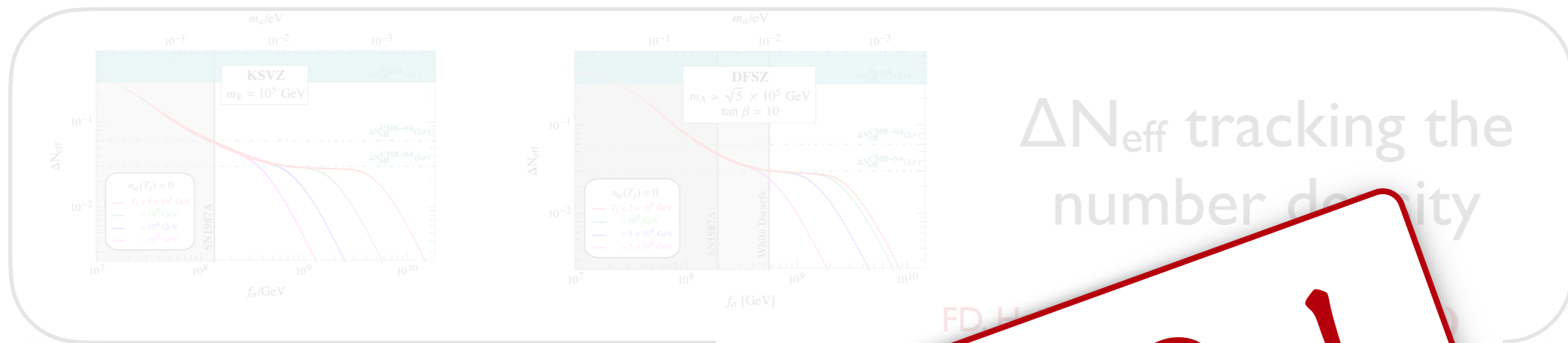


Importance of a phase space analysis

FD, Hajkarim, Lenoci, **JCAP 03 (2024)**

FD, Lenoci, **in preparation**

Outlook

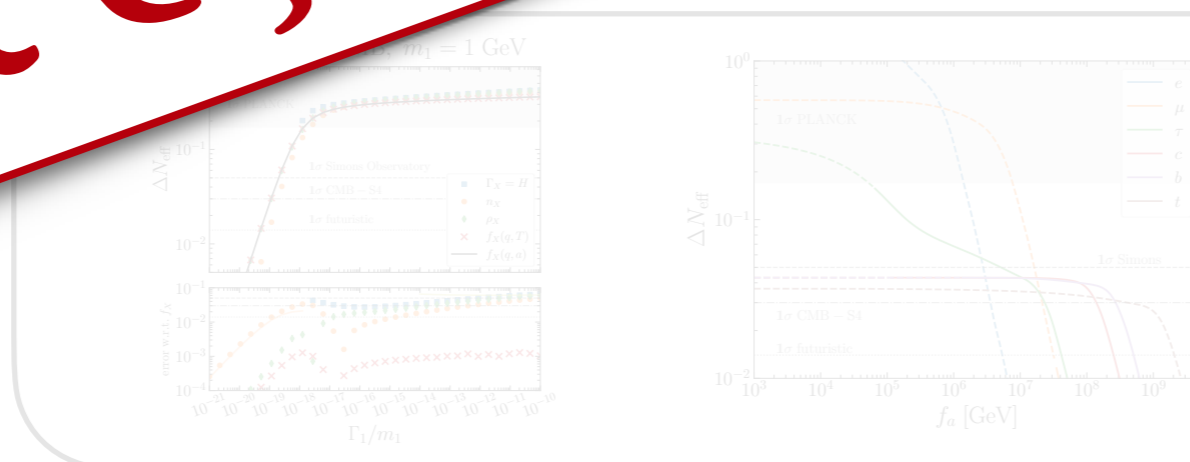


ΔN_{eff} tracking the number density

FD, Di Valentino, Giarè, Hajkarim, Melchiorri, Mena, Renzi, Yun, **JCAP 09 (2022)**

Axion cosmological mass bounds

TEŞEKKÜRLER!



Importance of a phase space analysis

FD, Hajkarim, Lenoci, **JCAP 03 (2024)**
FD, Lenoci, in preparation