

*Axion search goes deep underground:  
 $\theta$ -dependence of  $\alpha$ -decay half-lives*

Claudio Toni

based on the work w/  
Carlo Brogini, Giuseppe Di Carlo and Luca Di Luzio  
arxiv: 2404.18993, published on PLB

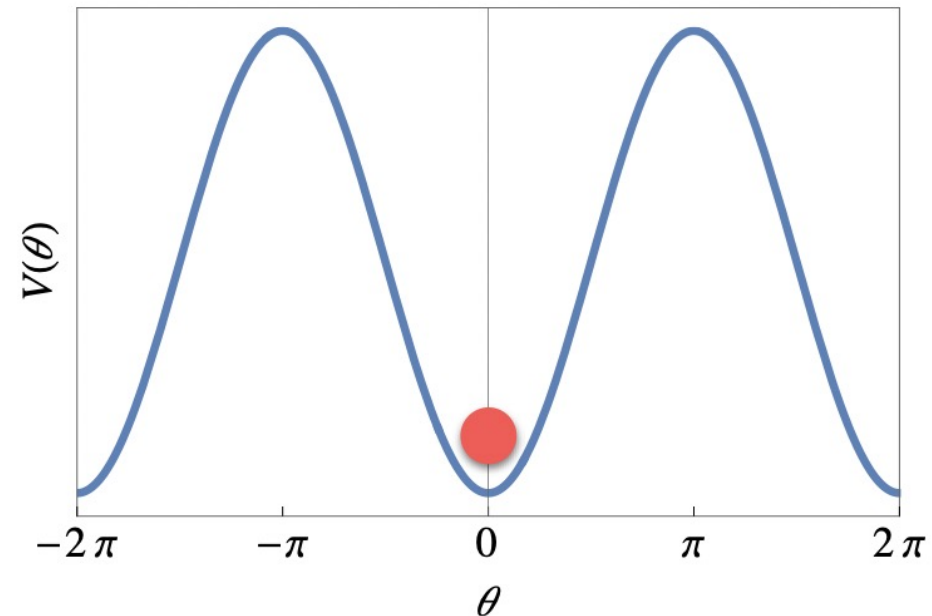
# QCD Axion

- Axion potentially addresses the Strong CP problem

$$\mathcal{L}_\theta = \frac{g^2 \theta}{32\pi^2} G_{\mu\nu} \tilde{G}^{\mu\nu} \quad |\theta| \lesssim 10^{-10}$$

- $\theta$  promoted to a dynamical field:  $\theta \rightarrow \frac{a}{f_a}$

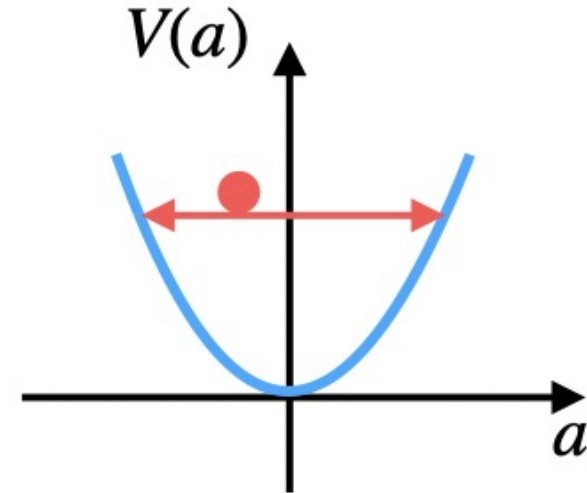
- QCD potential relaxed *dynamically* to zero:



# Oscillating axion DM

- An axion contribution to DM density is unavoidable so it is a natural DM candidate
- In a misalignment mechanism the DM axion field induces a time varying  $\theta$ -term

Preskill, Wise, Wilczek '83,  
Abbott, Sikivie '83,  
Dine, Fischler '83



$$\theta \simeq \sqrt{\frac{2\rho_{DM}}{m_a^2 f_a^2}} \cos(\omega t + \vec{p} \cdot \vec{x} + \phi)$$

# $\alpha$ -radioactivity and axion DM

➤ Search for time modulation of  $\alpha$ -radioactivity from axion DM

Broggini, Di Carlo, Di Luzio, CT  
arxiv:2006.12321

$$\mathcal{L}_\theta = \frac{g^2 \theta}{32\pi^2} G_{\mu\nu} \tilde{G}^{\mu\nu}$$



Non vanishing  $\theta$ -term impacts nuclear physics

Lee, Meißner, Olive, Shifman, Vonk arxiv:2006.12321

$$M_\pi^2(\theta) = M_\pi^2 \cos \frac{\theta}{2} \sqrt{1 + \varepsilon^2 \tan^2 \frac{\theta}{2}}$$

For its impact anthropic context, see  
Ubaldi arxiv:0811.1599

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Time modulation of radiative decays

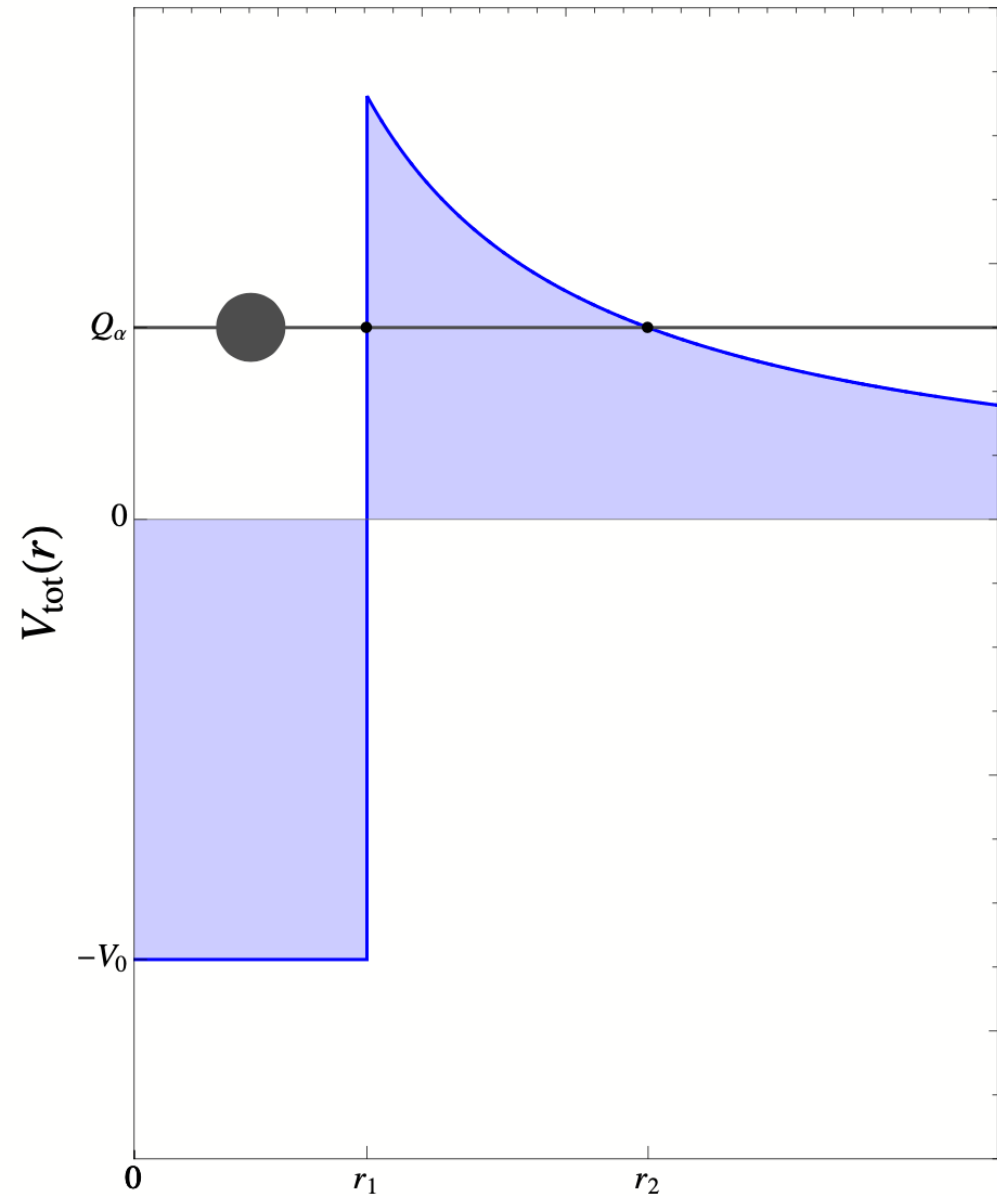
For a recent study of time modulation signals on  $\beta$ -decays, see  
Zhang, Houston, Li arxiv:2303.09865

# Theory of $\alpha$ -decay

## Gamow theory of $\alpha$ -decay

$$T_{1/2} = \frac{\ln 2}{\nu_0} \exp(K),$$

$$K = \frac{2}{\hbar} \int_{r_1}^{r_2} dr \sqrt{2\mu[V_{\text{tot}}(r) - Q_\alpha]}$$

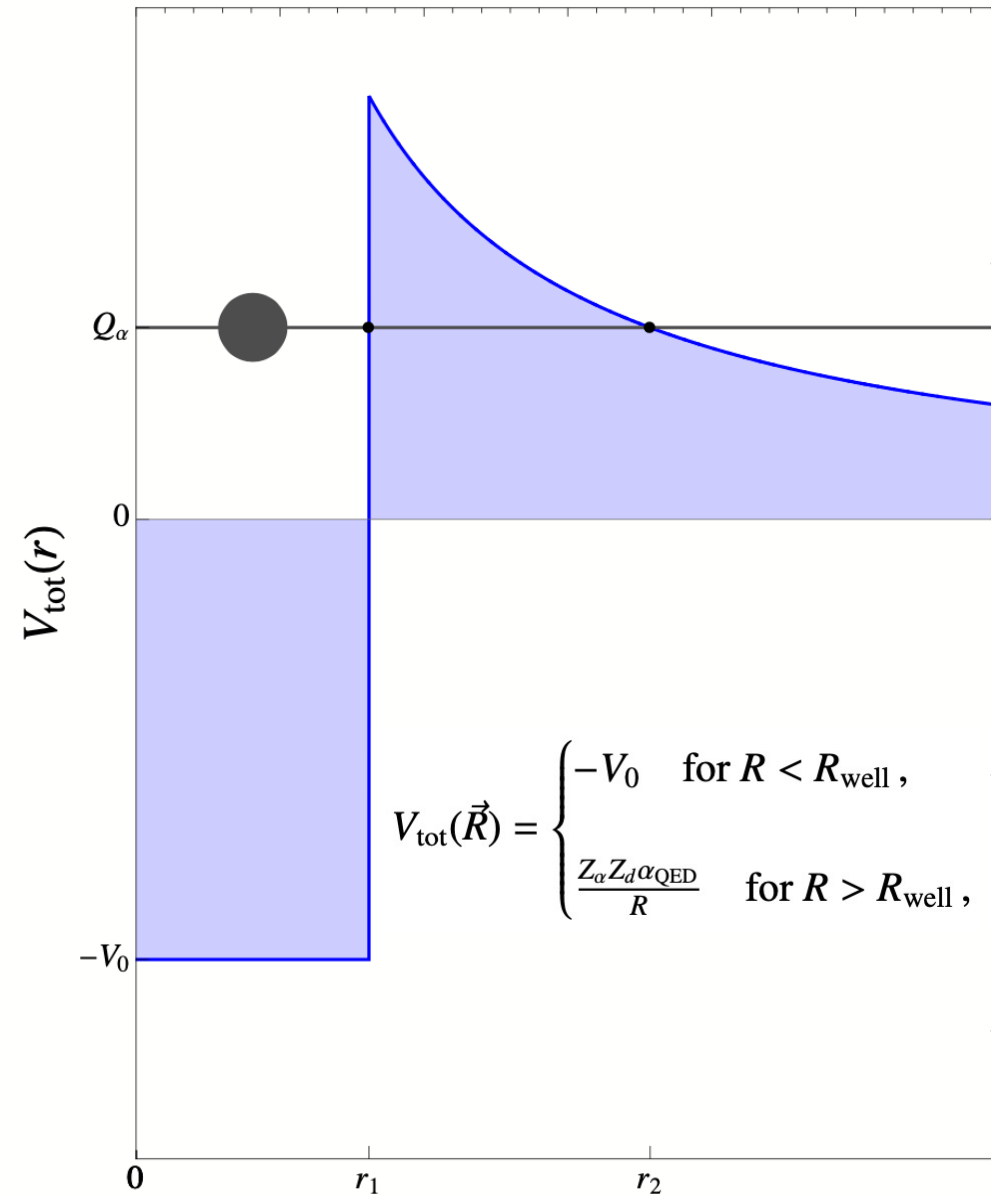


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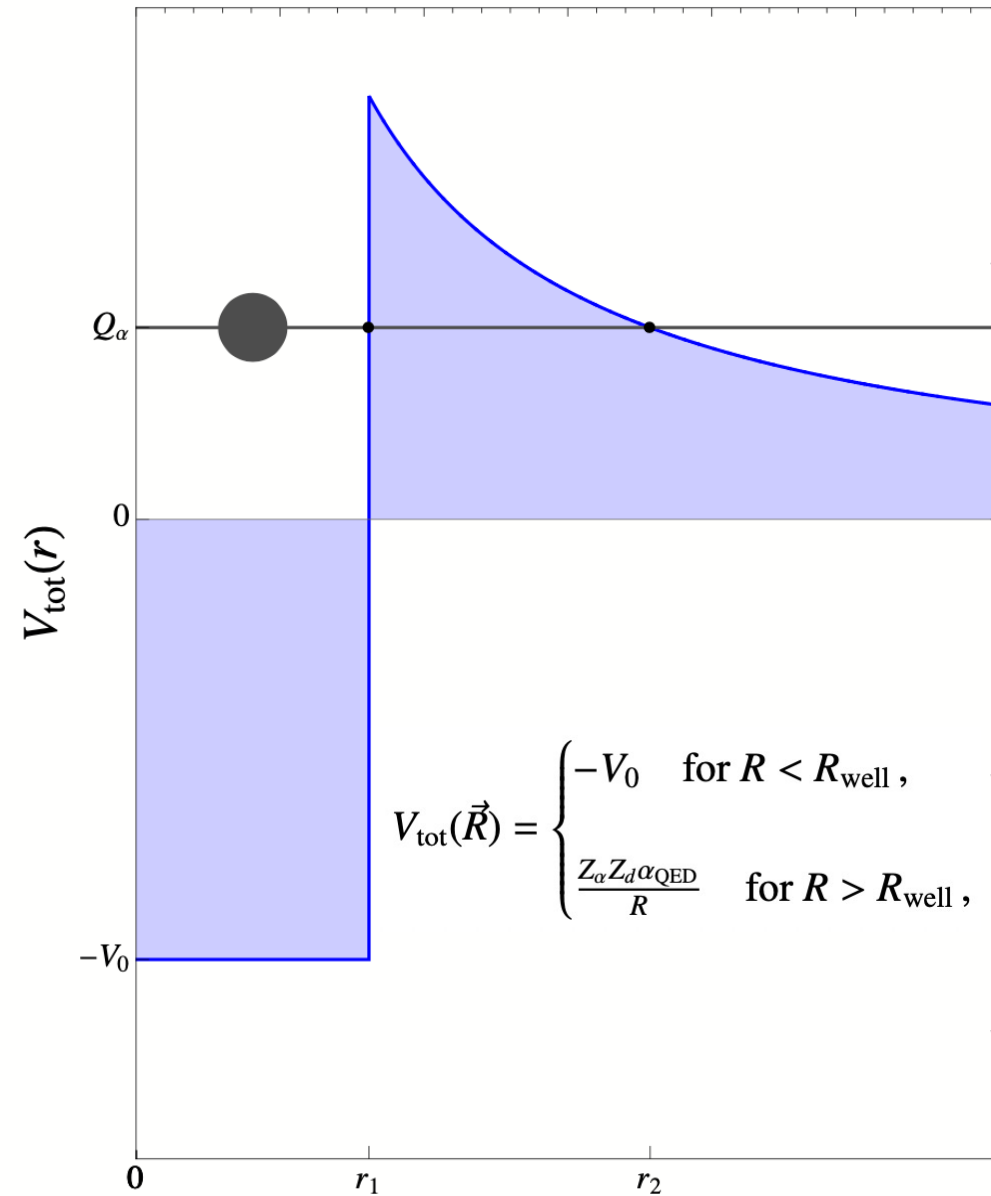
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$$K = Z_\alpha Z_d \alpha_{\text{QED}} \left( \frac{8\mu}{Q_\alpha} \right)^{1/2} F \left( \frac{Q_\alpha R_{\text{well}}}{Z_\alpha Z_d \alpha_{\text{QED}}} \right),$$

with

$$F(x) = \arccos \sqrt{x} - \sqrt{x} \sqrt{1-x} \approx \frac{\pi}{2} - 2\sqrt{x} + \dots,$$



# Signal estimate

- Halftimes are highly sensible to the Q-value, i.e. the energy released in the decay

Question: how the  $\theta$ -term impacts the  $Q$ ?

$$Q_\alpha = \text{BE}(A - 4, Z - 2) + \text{BE}(4, 2) - \text{BE}(A, Z),$$



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$$H = G_S(\bar{N}N)(\bar{N}N) + G_V(\bar{N}\gamma_\mu N)(\bar{N}\gamma^\mu N),$$

$$\eta_S = \frac{G_S(\theta)}{G_S(\theta = 0)}, \quad \eta_V = \frac{G_V(\theta)}{G_V(\theta = 0)}.$$

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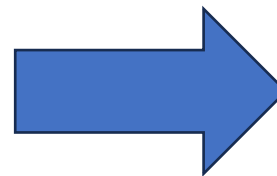
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$$Q_\alpha(\theta) = Q_\alpha(\theta = 0) - 97 \text{ MeV} (\eta_S(\theta) - 1) \times ((A - 4)^{2/3} + 4^{2/3} - A^{2/3}).$$

Damour, Donoghue arxiv:0712.2968

$$\eta_S(\theta) = 1.4 - 0.4 \frac{M_\pi^2(\theta)}{M_\pi^2}$$

# Exp. sensitivity

$$T_{1/2} = \frac{\ln 2}{\nu_0} \exp(K) \quad T_{1/2}(\theta) \approx T_{1/2}(0) + \dot{T}_{1/2}(0)\theta^2$$

$$\dot{f} \equiv df/d\theta^2$$

$$I(t) \equiv \frac{T_{1/2}^{-1}(\theta(t)) - \langle T_{1/2}^{-1} \rangle}{\langle T_{1/2}^{-1} \rangle}$$

$$\theta(t) = \theta_0 \cos(m_a t)$$

$$\approx -\frac{1}{2} \frac{\dot{T}_{1/2}(0)}{T_{1/2}(0)} \theta_0^2 \cos(2m_a t)$$

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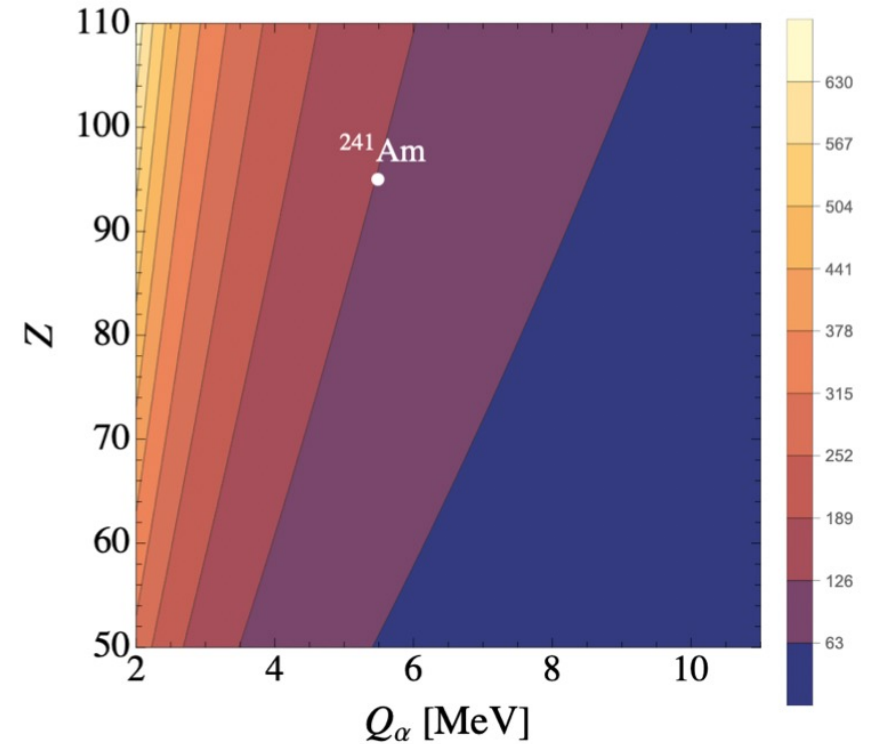


Figure A.3: Contours of  $\dot{T}_{1/2}(0)/T_{1/2}(0)$  in the  $(Q_\alpha, Z)$  plane for  $A = 241$ . The case of  $^{241}\text{Am}$  is indicated by a white dot.

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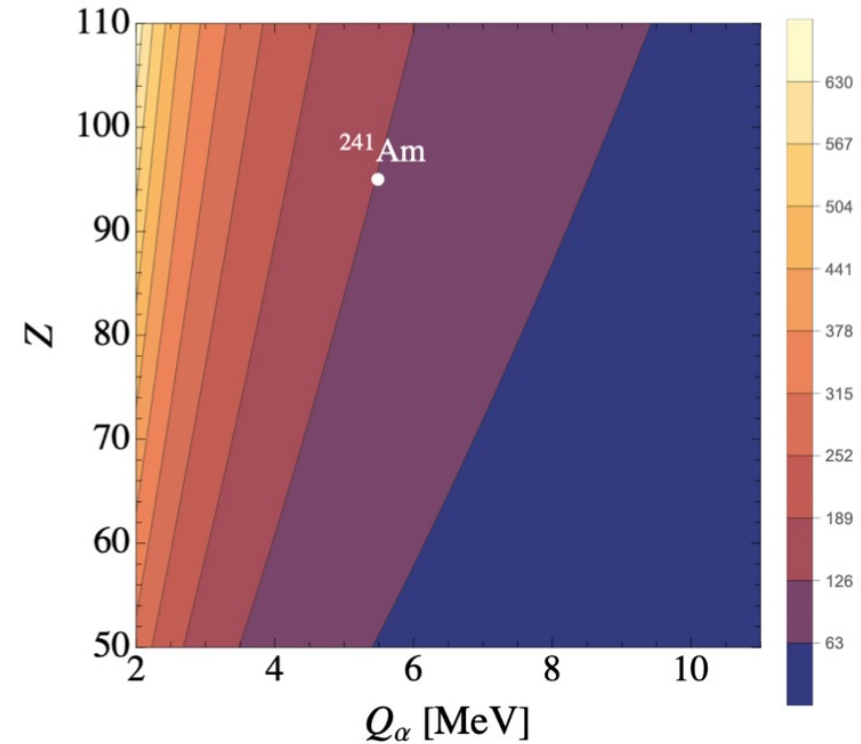


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$$= -4.3 \times 10^{-6} \cos(2m_a t) \left( \frac{\rho_{\text{DM}}}{0.45 \text{ GeV/cm}^3} \right)$$

$$\times \left( \frac{10^{-16} \text{ eV}}{m_a} \right)^2 \left( \frac{10^8 \text{ GeV}}{f_a} \right)^2, \quad \theta_0 = \frac{\sqrt{2\rho_{\text{DM}}}}{m_a f_a}$$

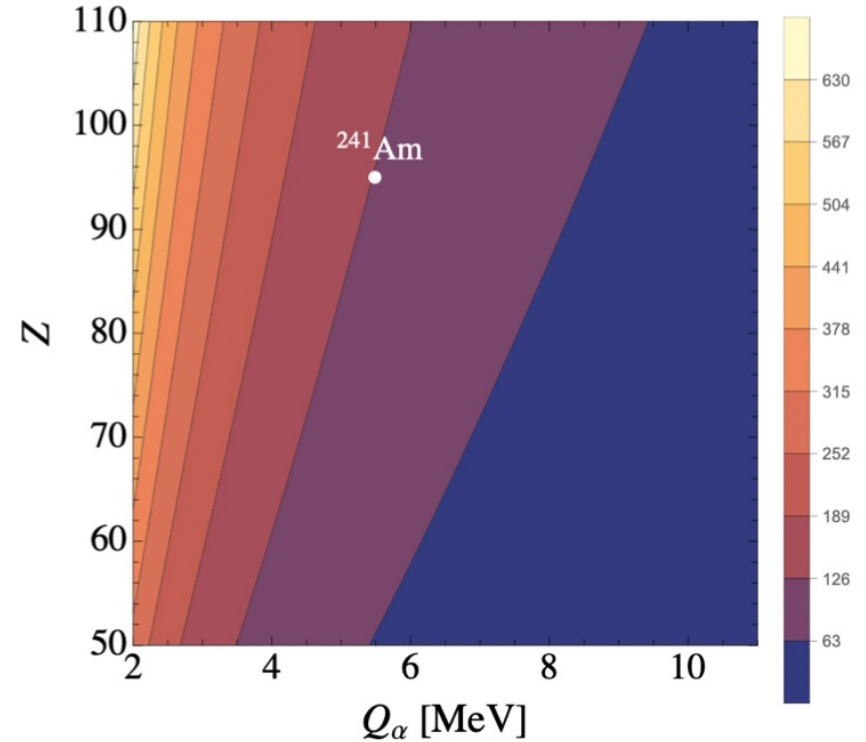


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# Exp. set-up

A picture of our experiment, based on Americium-241, placed under Gran Sasso



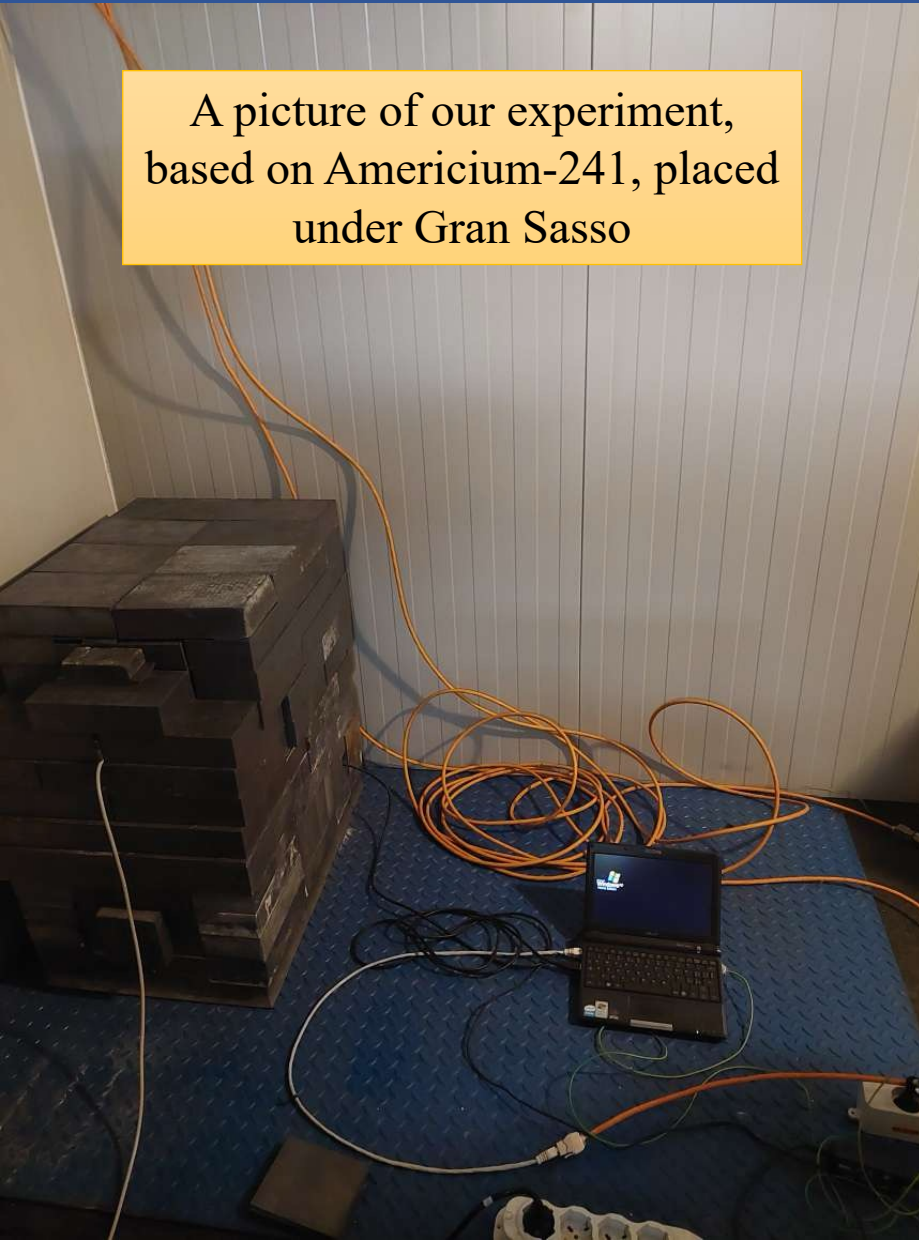
- A 3”x3” NaI crystal detects the gamma rays which are subproducts of the  $\alpha$ -decays, primarily (85% of the time) at 59.5 keV
- The crystal is closed inside a cooper-lead shield

Similar studies have already been performed, see for example:  
Bellotti, Broggin, Di Carlo,  
Laubenstein, Menegazzo  
arxiv:1802.09373

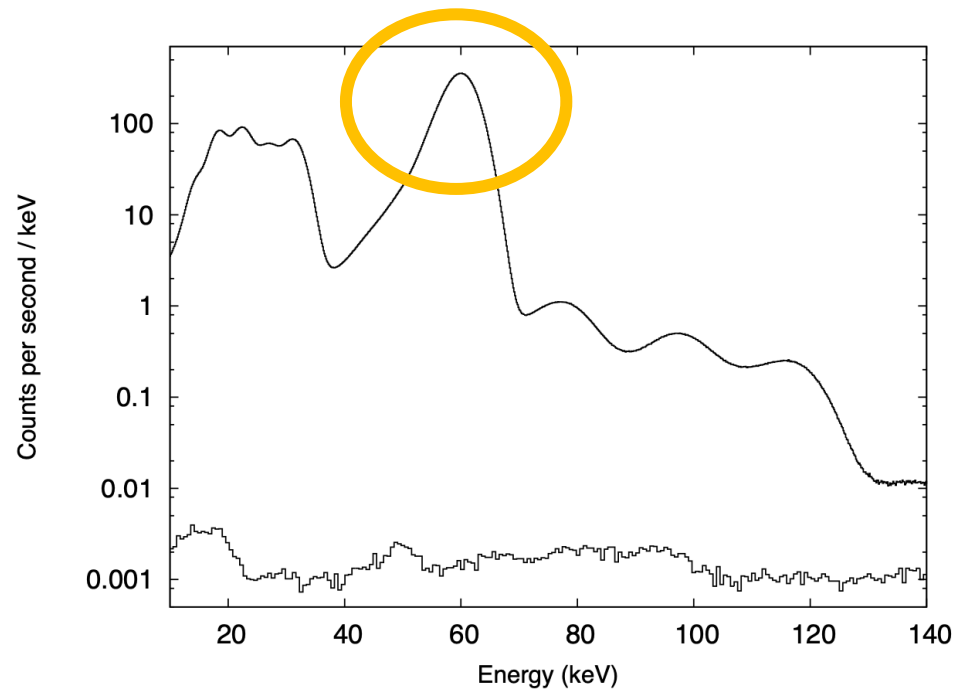


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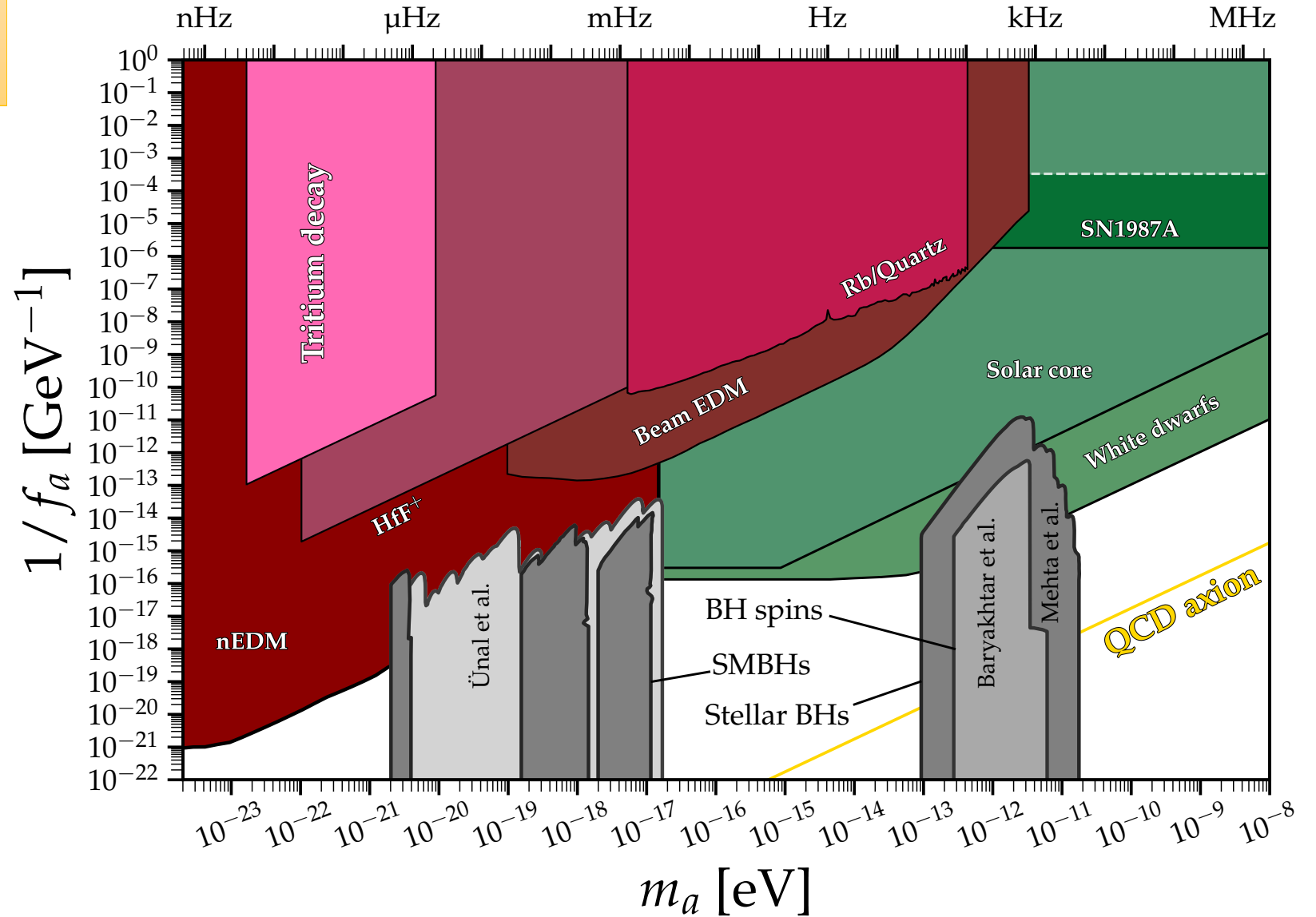


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Figure 1:  $\gamma$ -spectrum (counts per second per keV) of the  $^{241}\text{Am}$  source (upper curve) compared to the background (lower curve). The dominant contribution arises from the  $\gamma$  at 59.5 keV.

# Exp. prospects

Prospect limits from measurements of Americium-241  $\alpha$ -decay



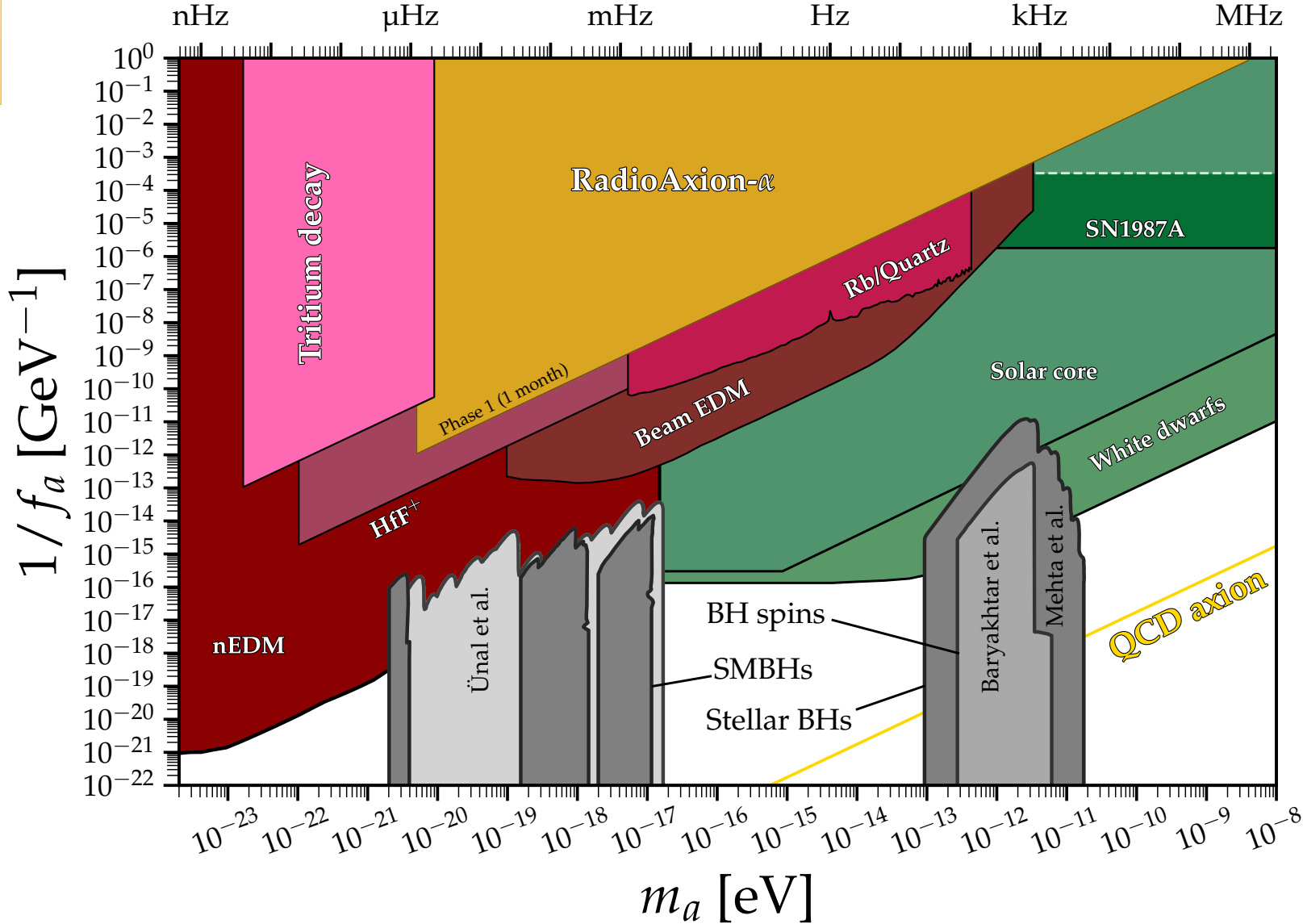
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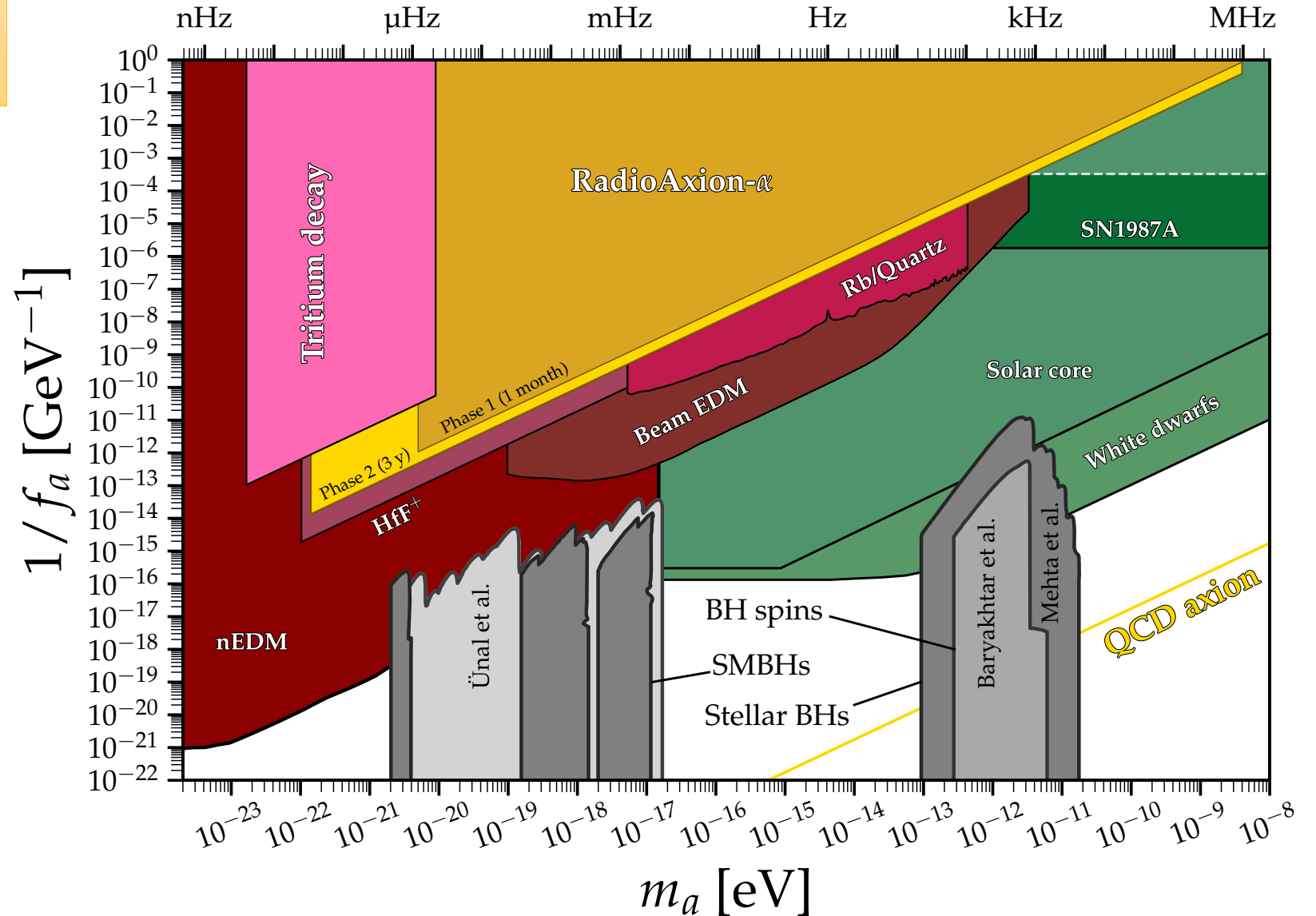
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➤ Phase II, three years of data:

$$1 \mu\text{s} < \Delta t < 1 \text{ yr}$$

$$I_{\text{exp}} = 4 \times 10^{-6} \text{ at } 2\sigma$$



# The End

