



Charged & Neutral Particles Channeling

Phenomena

FEL performance and tolerance studies of the EuPRAXIA@SPARC_LAB beamline AQUA

F. Nguyen on behalf of the EuPRAXIA@SPARC_LAB Collaboration

With relevant inputs from L.Giannessi, M.Opromolla, A.Petralia



EuPRAXIA@SPARC_LAB: AQUA

1st international design of a plasma accelerator facility

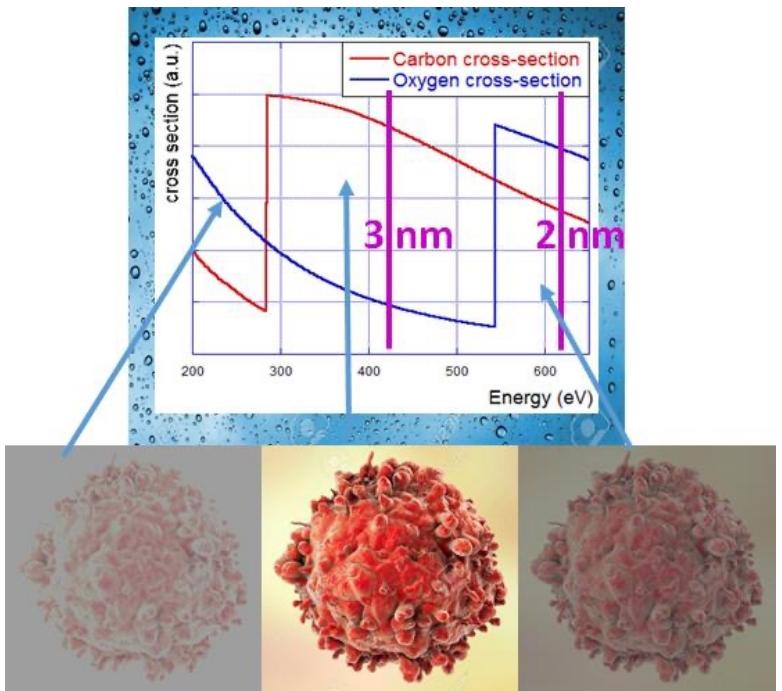
EuPRAXIA is designed to deliver at 10-100 Hz ultra-short pulses of

- Electrons (0.1-5 GeV, 30 pC)
- Positrons (0.5-10 MeV, 10^6)
- Positrons (GeV source)
- Lasers (100 J, 50 fs, 10-100 Hz)
- Betatron X rays (5-18 keV, 10^{10})
- FEL light (0.2-36 nm, 10^9 - 10^{13})

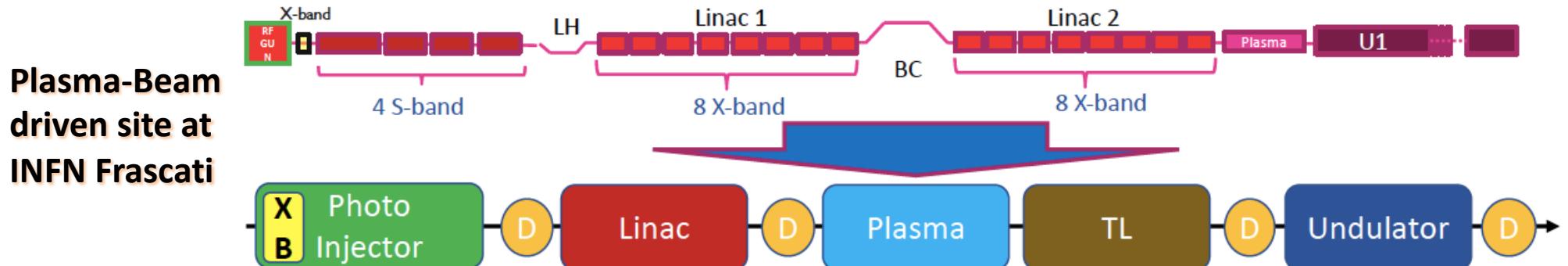
The **AQUA** (water in *Latin*) beamline of the EuPRAXIA@SPARC_LAB project is a **FEL facility** to be operated in Self-Amplified Stimulated Emission **SASE** for experiments around **3-4 nm wavelength**, i.e. **410-310 eV photon energy**, where water looks **transparent** differently from O or C which are absorbing and scattering → *water window* relevant to study biological samples with coherent imaging

Realistic intermediate goals at established labs:

- 150 MeV → 1 GeV → **5 GeV** (FEL + other applications)
- 1 plasma stage → **2 plasma stages** → multiple
- factor 3 facility size reduction → **factor 10** → ...
- Low charge, 10 Hz apps of e- (+ **positron** generation) → high charge, 10 Hz applications (**FEL**) → 100 Hz



FEL beamlines for EuPRAXIA@SPARC_LAB

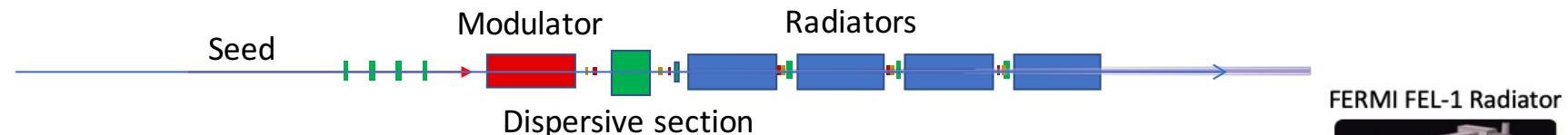


Two foreseen FEL beamlines:

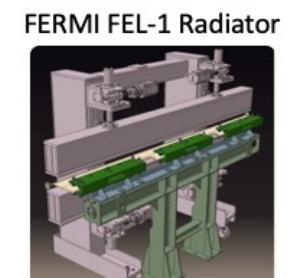
1) AQUA: Soft-X ray SASE FEL – Water window optimized for **4 nm** (baseline)

SASE FEL: 10 UM Modules, 2 m each – Two technologies under study: Apple-X PMU and planar SCU

2) ARIA: VUV seeded HGHG FEL beamline for gas phase

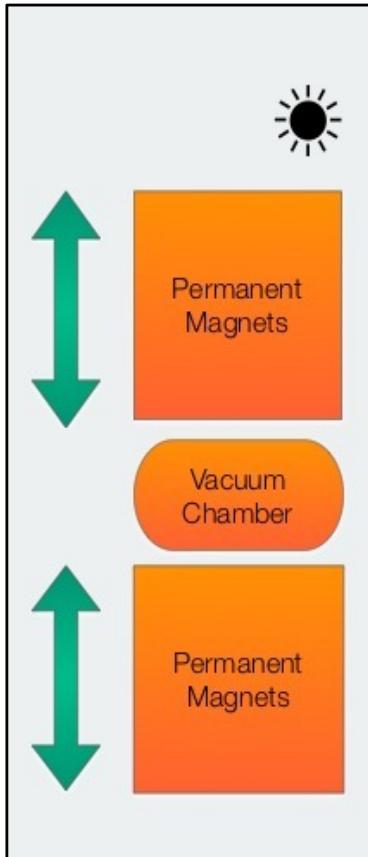


SEEDED FEL – Modulator 3 m + 4 Radiators APPLE II – variable pol. 2.2 m each – SEEDED in the range 290 – 430 nm – Undulator based on consolidated technology.

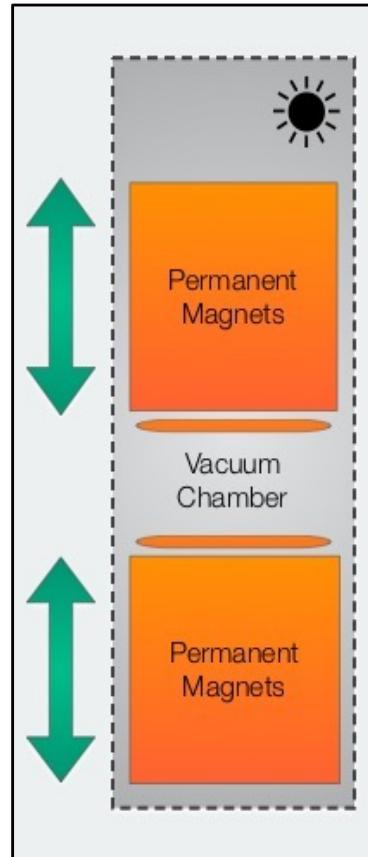


Undulator technologies: magnetic strength order

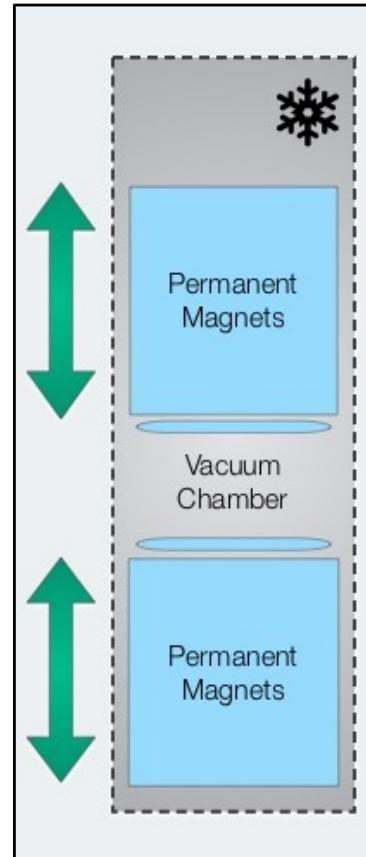
Out of vacuum PMU



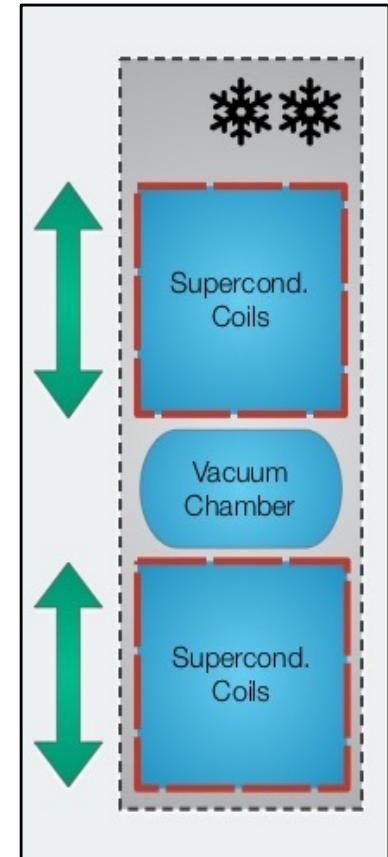
In vacuum PMU



Cryogenic PMU



Superconducting



Traditional and
cheapest design

Selectable Polarization

Magnets inside vacuum
but not cheap & no
polarization
Good performance

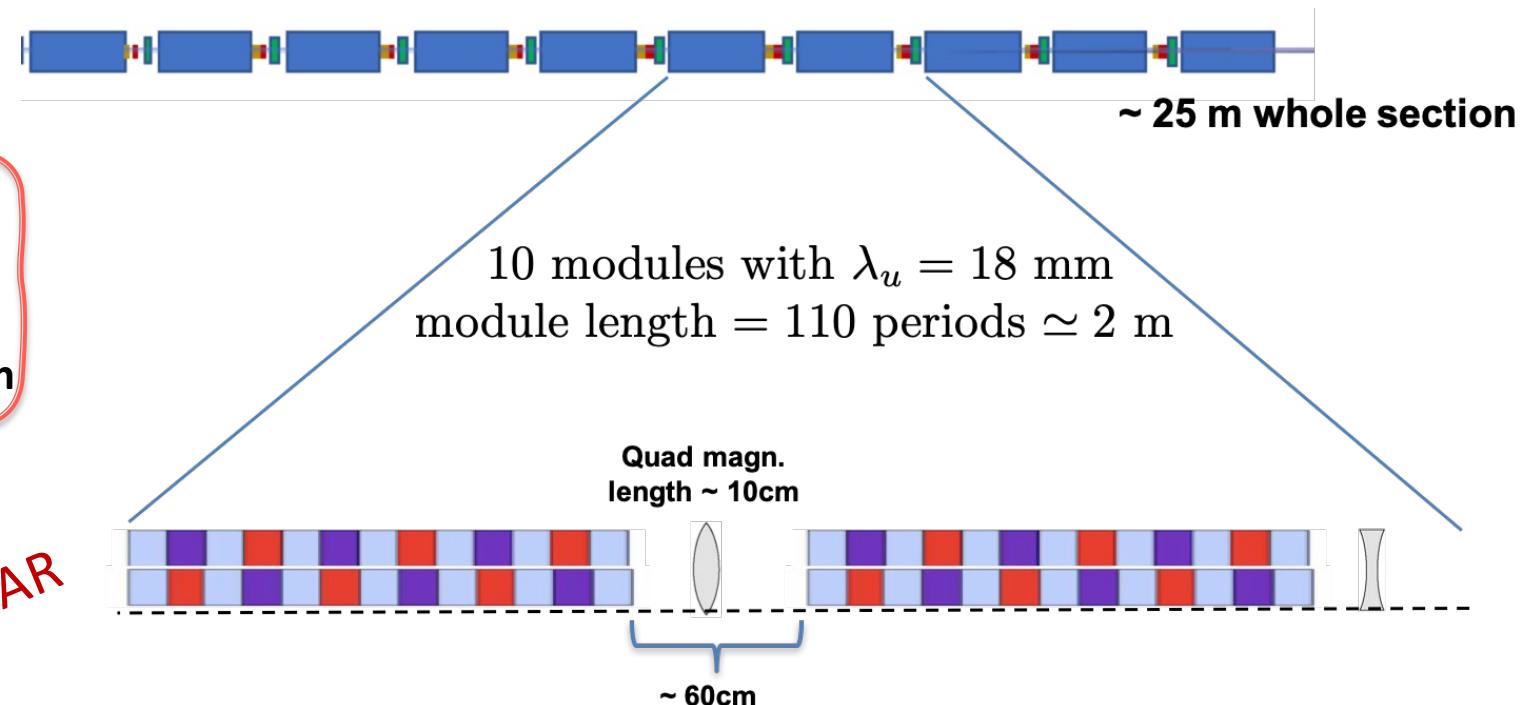
Improved B but not
cost-effective and
increased complexity
Better performance

Highest B and SC
electromagn. coils

Best performance

AQUA constraints on the FEL beamline

- Target wavelength 3-4 nm @ 1 GeV: relatively short period required (12-20 mm)
- Total available length ~ 25-30 m, depending on the linac: matching section, beam diagnostics and main beam dump.
- Hypotheses:
 - Optimize magnetic length/available length filling factor
 - Make sure gain length shorter than 1 undulator module length
 - 60-80 cm intra-undulator sections: Quads, BPMs, correctors, phase shifters, alignment diagnostics

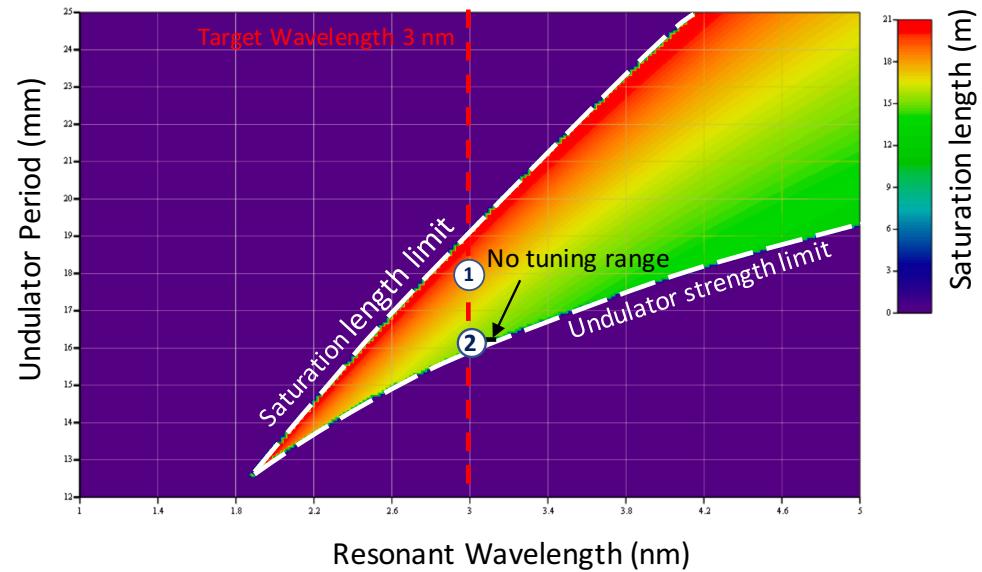


Tuning range: choice of the period λ_u

FEL performance evaluated with Ming Xie-Dattoli scaling formulae accounting for 60% filling factor

- Linac parameters to be finalized: peak current implies ~ large compression factor → en. spread
- Beta function constrains undulator module length and alignment tolerances

Parameter	Symbol	Units	D (CDR)
Charge	Q	pC	30
Energy	E	GeV	1
Peak current	I_{peak}	kA	1.8
Bunch length	σ_z	μm	2
Proj. norm. emittances (x/y)	$\epsilon_{n,x,y}$	mm-mrad	1.7
Slice, norm. emittances (x/y)	$\epsilon_{n,x,y}$	mm-mrad	0.8
Proj. energy spread	$\sigma_{\delta p}$	%	0.95
Slice Energy spread	$\sigma_{\delta s}$	%	0.05



$$\lambda_{\text{res}} = \frac{\lambda_u}{2\gamma^2} \left[1 + \frac{K^2(g_u)}{2} \right]$$

From the K vs. gap formulae of a planar PMU with remanent $B_r = 1.2\text{T}$, min. magnetic gap=6mm, beam stay clear=5mm:

- 18mm implies tuning range, plus saturation length contingency if operating at 4nm wavelength;
- 16mm improves the saturation length limit, but almost no tuning range

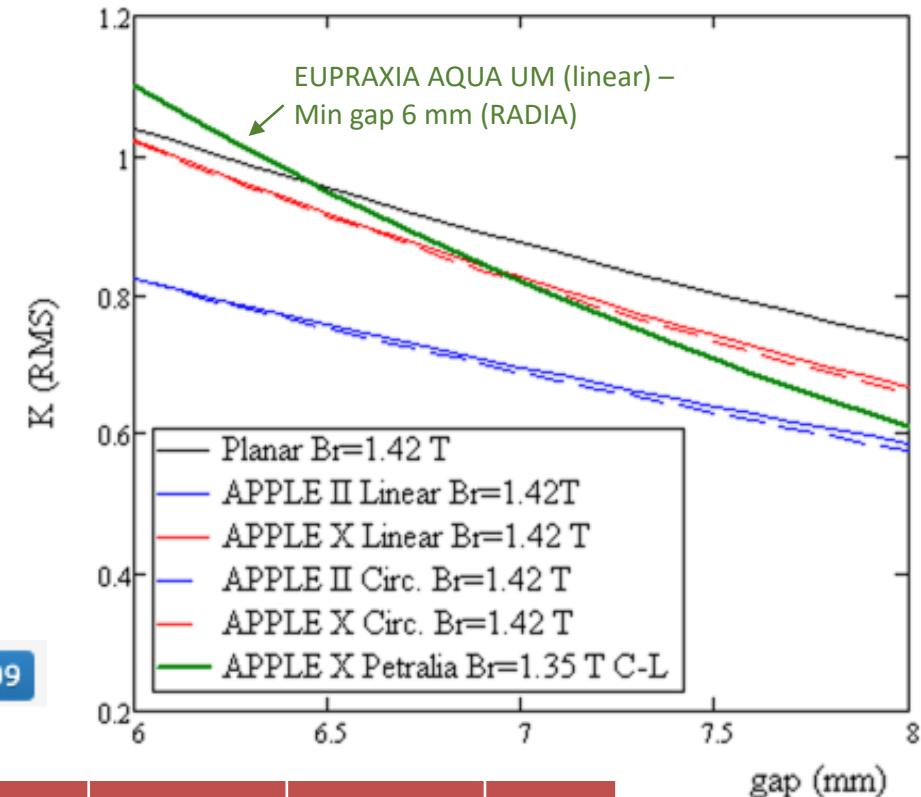
Variable polarization undulator for AQUA

Polarization: variable polarization is an asset as it meets the scientific case requests → undulator capability, circ. polar. guarantees high gain ($\sim L_{\text{mod}}$)

Advanced Planar Polarized Light Emitter-type:
APPLE-X substantially higher field at the same undulator aperture → extended tuning range, K_{max} independent of polarization → fully symmetric

Parametrization laws from:

D5.1: Technologies for the CompactLight Undulator,
F.Nguyen et al., XLS Deliverable (2019) [DOI 10.5281/zenodo.5024409](https://doi.org/10.5281/zenodo.5024409)



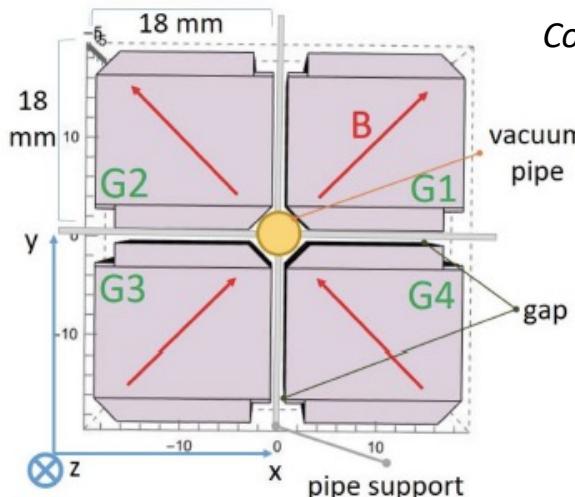
Model parameters:

- Remanent field $Br = 1.35$ T
- Undulator period $\lambda_u = 18$ mm
- 4 blocks / period, NdFeB
- # of periods (eff.) $N = 110$
($L_u=1990$ mm)

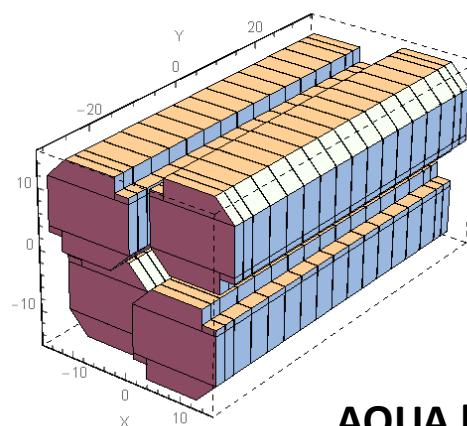
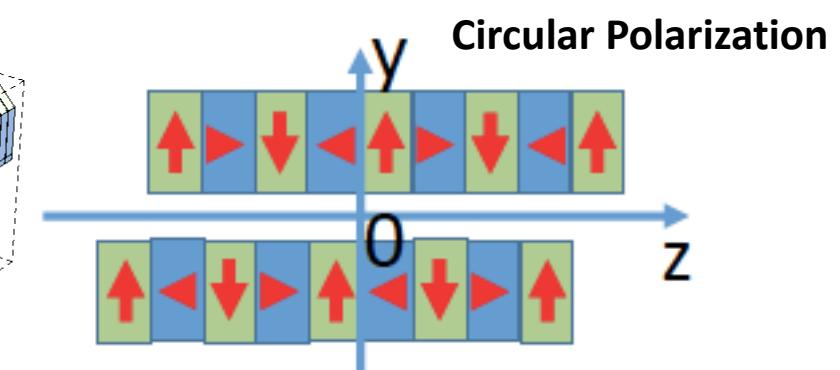
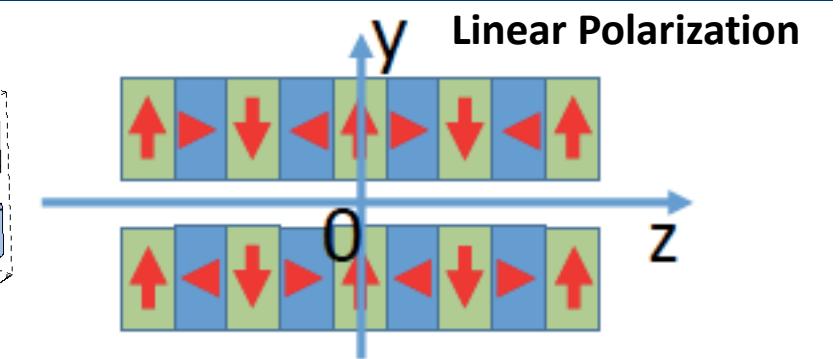
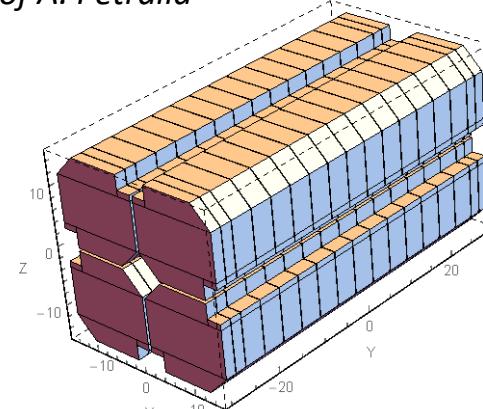
**Field Integrals
from RADIA**

	LP (h)	CP	LP (v)	units
$\int B_x$	0	0	0	G m
$\int B_y$	0.0119	-0.0095	0.4118	G m
$\iint B_x$	0	-0.0179	-0.1322	G m ²
$\iint B_y$	0	-0.0001	0	G m ²

APPLE-X undulator modeling



Courtesy of A. Petralia



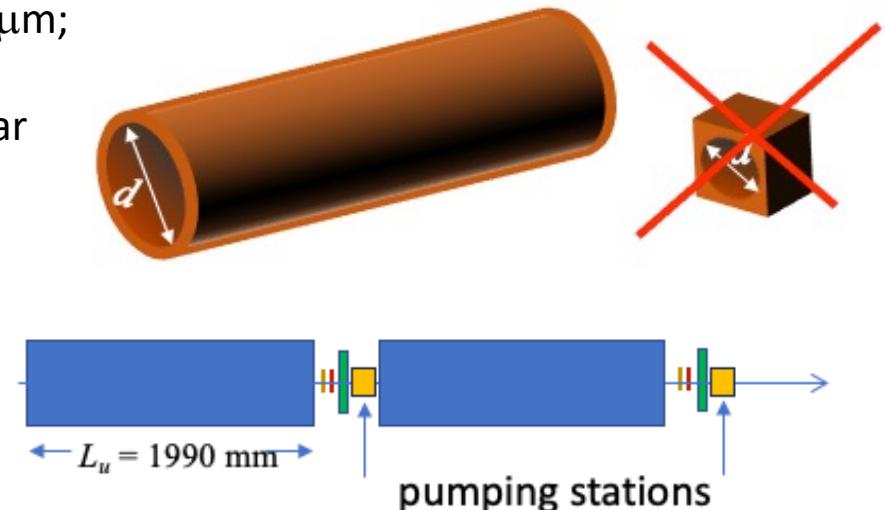
AQUA baseline radiator: 10 APPLE-X modules

A. Petralia et al., FEL2022 WEP38 Proceedings

Interplay among aperture, magnetic strength, wavelength tunability and inner diameter constrained by wakefield effects on **FEL performance**

Vacuum chamber inner radius: wakefields

- Vacuum pipe design: circular and uniform thickness < 300 μm ;
- Wakefield effects minimization requires smooth and regular surfaces → suppress apertures or other discontinuities: vacuum pumping access ports only available at undulator transitions → no coating (e.g. for vacuum sustain) – worsening resistive wall wakefields – is needed;
- Which diameter d value for the vacuum chamber?



Resistive wall (RW) wakefields: assuming cylindrical symmetry, the **longitudinal** (monopole) wakefield generates an energy loss and an increase in energy spread **independent of the beam orbit**, while the **transverse** (dipole) wakefield generates an emittance growth that **depends on the trajectory**

ISBN: 978-3-95450-231-8

14th International Particle Accelerator Conference, Venice, Italy

ISSN: 2673-5490

JACoW Publishing

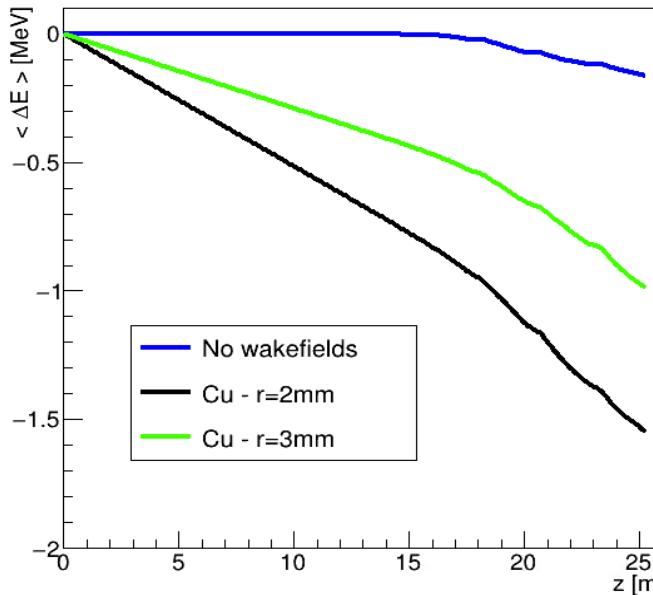
DOI: 10.18429/JACoW-IPAC2023-WEPL190

ADVANCED STUDIES FOR THE DYNAMICS OF HIGH BRIGHTNESS ELECTRON BEAMS WITH THE CODE MILES *

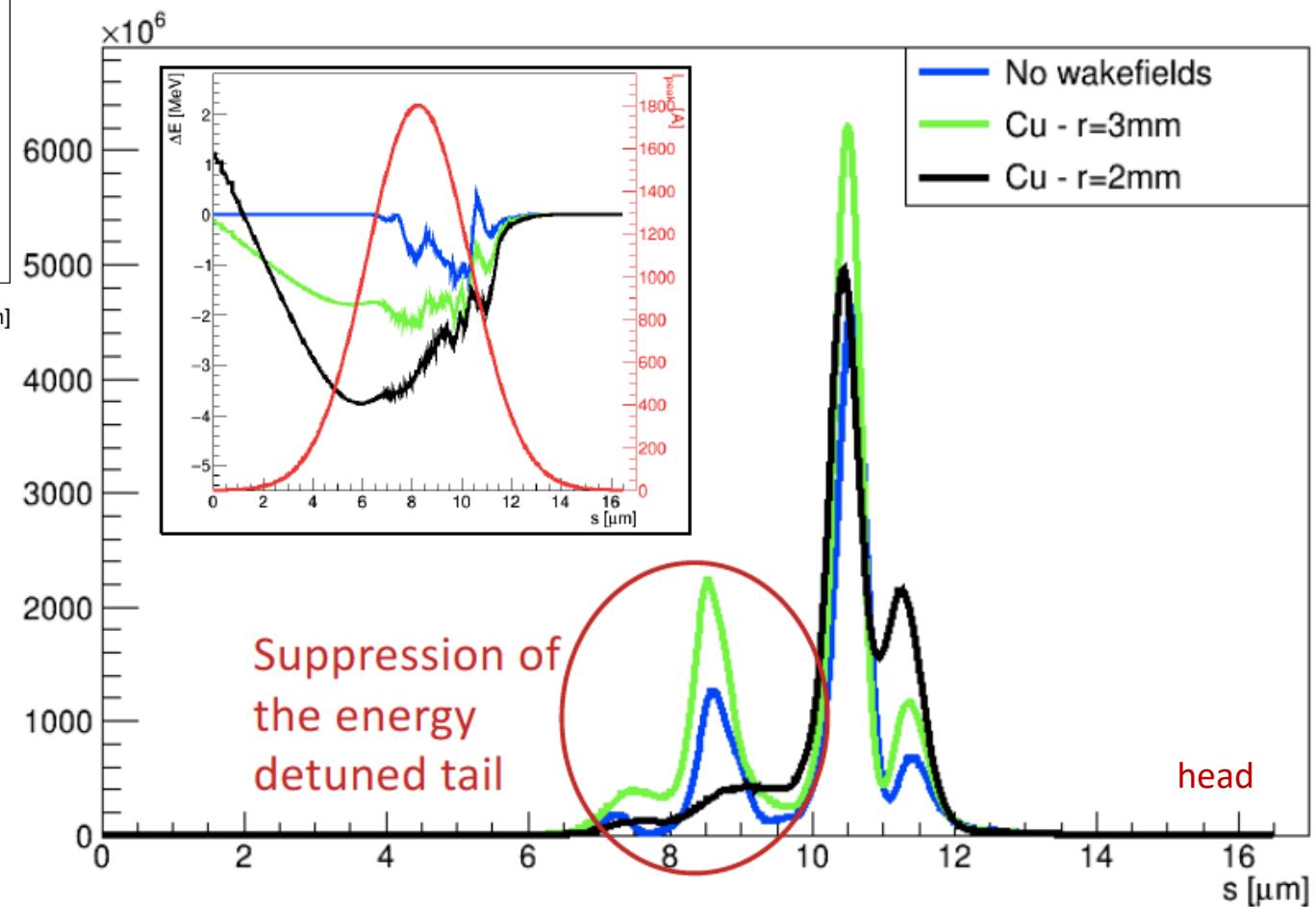
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Wakefield deterioration effects on the FEL performance are **analyzed as a function of the radius r** → energy loss due to the longitudinal RW wakefield provided from **M. Migliorati, F. Bosco *et al.* (Uni La Sapienza)** → plugged into 3D time dependent Genesis1.3 simulations for AQUA electron both short and long bunches

Longitudinal wakefields – 30pC charge, 2μm length

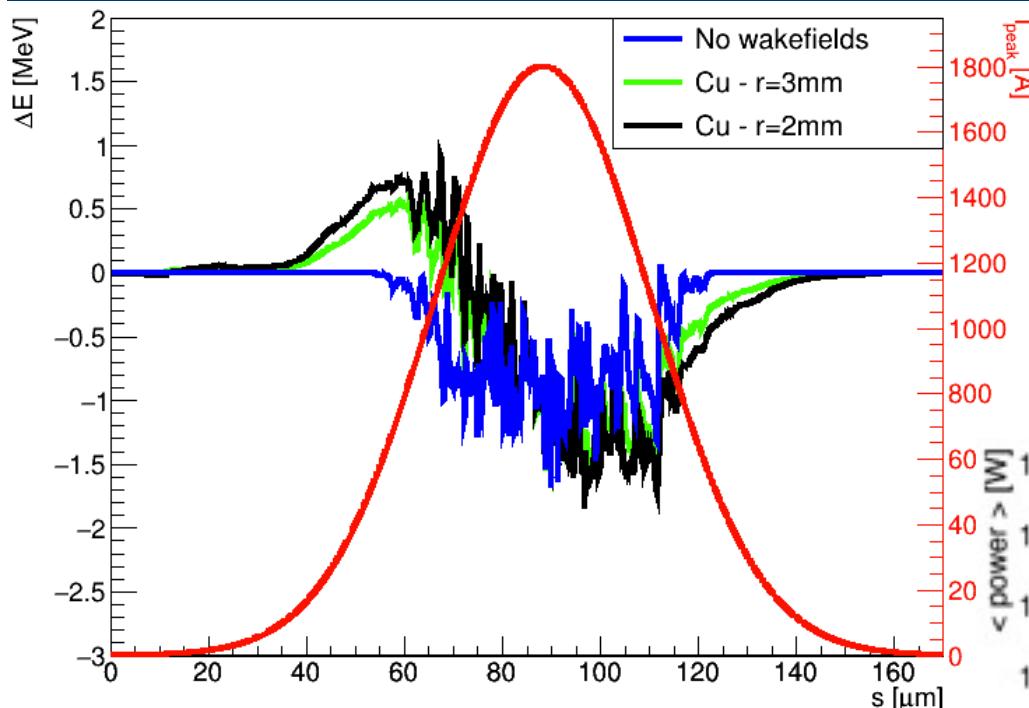


Average energy loss along FEL propagation coordinate: more severe at shorter Cu chamber radius → higher wakefield
At undulator exit: wakefield energy loss adds up to the FEL interaction loss, but the net peak power is marginally affected



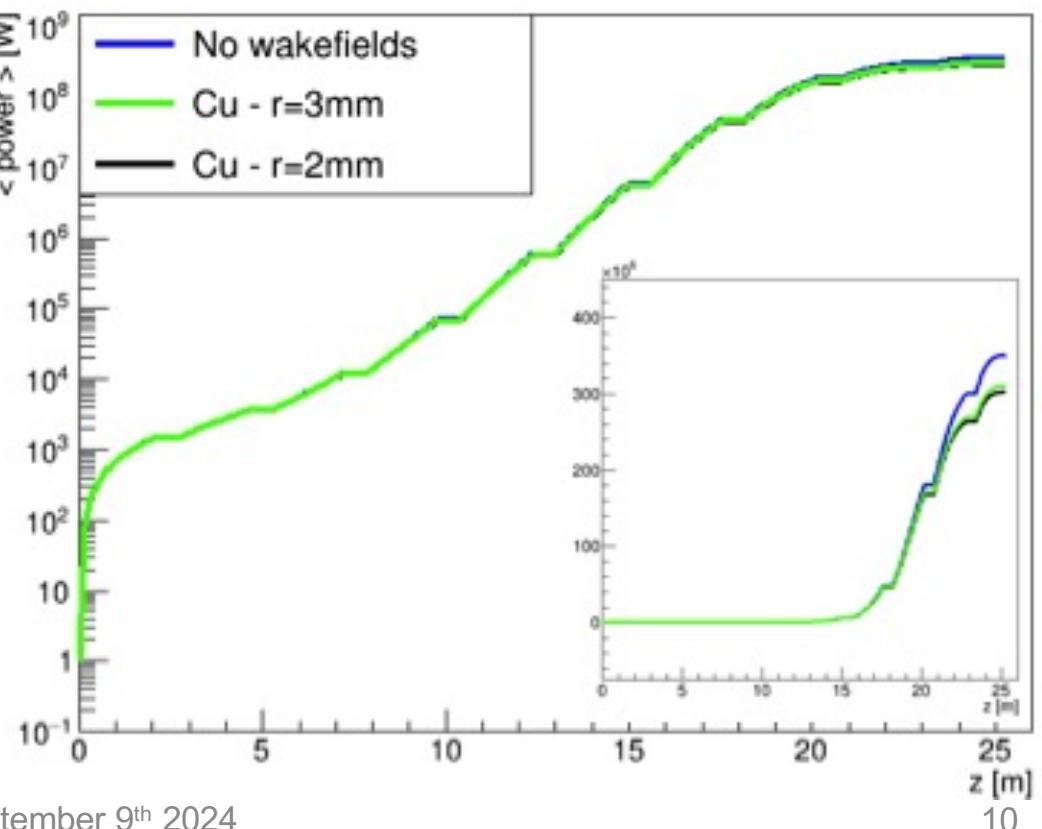
Conclusion: negligible difference in the output power between no RW wakefield and longitudinal degradation at both inner radii, even at $I_{\text{peak}} = 1.8 \text{ kA}$

Longitudinal wakefields – 300pC charge, 20μm length



Energy loss at undulator exit is dominated by the FEL interaction → almost negligible RW wakefield effects.

This behavior is confirmed looking at the average FEL output power along propagation coordinate (inset is the same in linear scale)



Conclusion: negligible difference in the energy loss and so on the power growth between no RW wakefield and longitudinal degradation at both inner radii

→ vacuum chamber with inner radius=2.5mm is safe against RW longitudinal wakefields

Transverse RW wakefields analysis

Transverse RW wakefields induced inside the **cylindrical Cu** vacuum chamber of radius $a = 2\ldots3\text{mm}$ affect the bunch orbit in undulators, depending on the **transverse offset** at entrance → **analytical treatment (complex conductivity+bunch length considerations)** based on K. Bane & G. Stupakov and the **relationship between transverse and longitudinal impedances** → estimate the kick κ_T angle/unit path length parameter, dependent on radius a and that scales linearly with the transverse offset

$$W_t(s) = \frac{2}{a^2} \int_0^s W_\ell(s') ds', \quad Z_t(k) = \frac{2}{a^2} \frac{Z_\ell(k)}{k}$$

$$W_\ell(s) \sim \frac{1}{a^2} e^{-s/(4c\tau)} \cos \left[s \sqrt{\frac{2\omega_p}{ac}} \right]$$

$$\kappa_T = \frac{\text{kick angle [rad]}}{\text{unit path length [m]}}$$

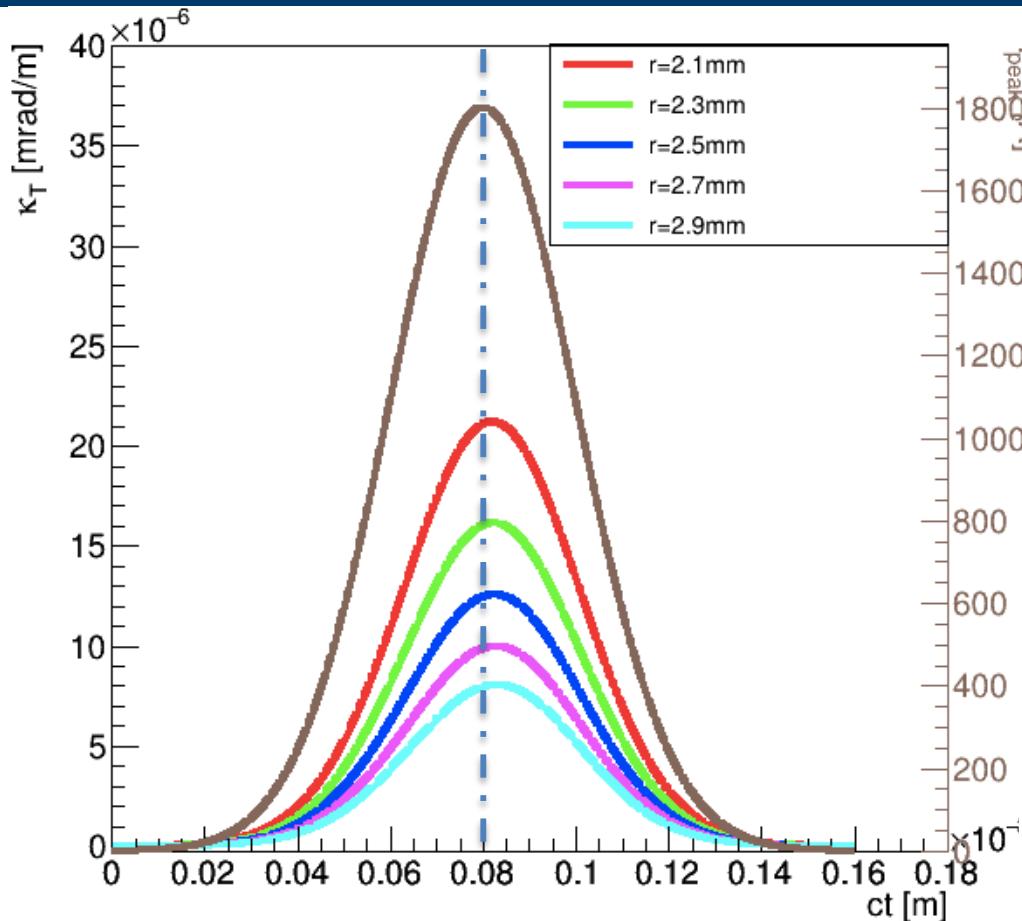
$$\sigma_{\kappa_{Tx}} = \varphi_T(a) \cdot \sigma_{x_{off}}$$

$$\sigma_{\kappa_{Ty}} = \varphi_T(a) \cdot \sigma_{y_{off}}$$

$$\varphi_T = \frac{\text{kick angle [rad]}}{\text{unit path length [m]} \times \text{unit transverse offset [m]}}$$

Kick angle/path length tolerance error **scales linearly with any misalignment** (e.g. between und. modules, vacuum chamber wrt its own und. module) **jitter source**

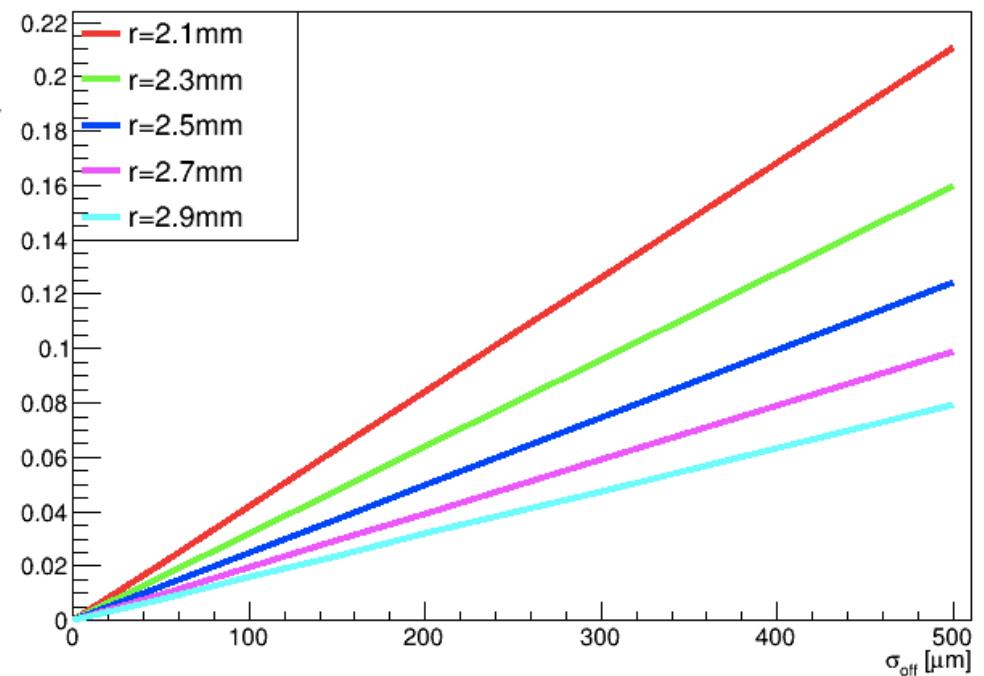
Transverse wakefields – 300pC charge, 20μm length



Kick angle/path length for different chamber radius values vs. **the current profile (brown)**

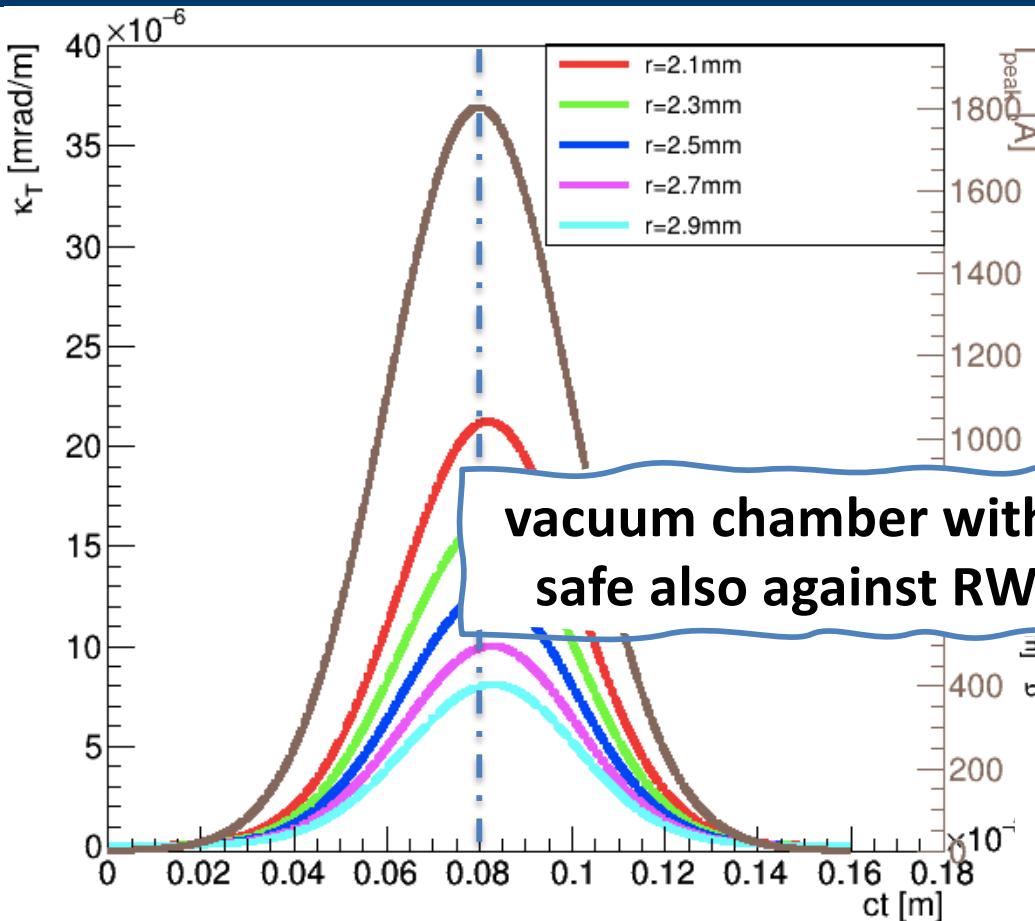
Assuming 50 μm vertical e-beam offset → max value $\sim 2 \times 10^{-2} \mu\text{rad}/\text{m}$ happens for r=2.1mm, exactly on the current peak!

The φ_T kick angle/m² is evaluated at the peak position → dot-dashed line



Transverse wakefields affect the peak current profile by max $\sim 1 \mu\text{rad}/\text{m}$ transverse kick, assuming to systematically find higher than 300 μm misalignment, for r=2.3mm

Transverse wakefields – 300pC charge, 20μm length



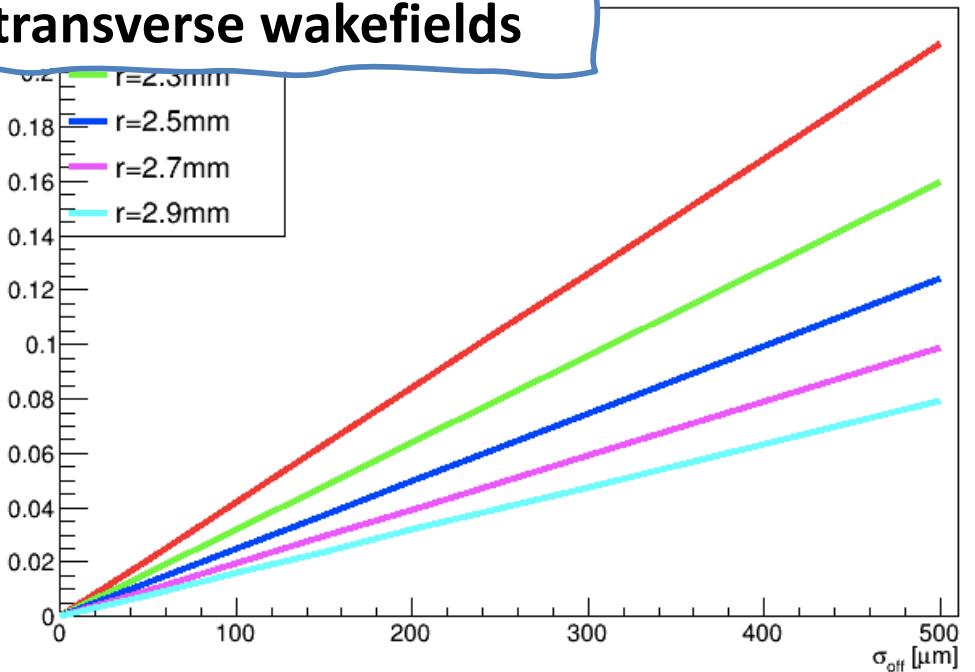
Kick angle/path length for different chamber radius values vs. **the current profile**

Assuming 50 μm vertical e-beam offset → max value $\sim 2 \times 10^{-2} \mu\text{rad}/\text{m}$ happens for $r=2.1\text{mm}$, exactly on the current peak!

The φ_T kick angle/ m^2 is evaluated at the end line

vacuum chamber with inner radius=2.5mm is safe also against RW transverse wakefields

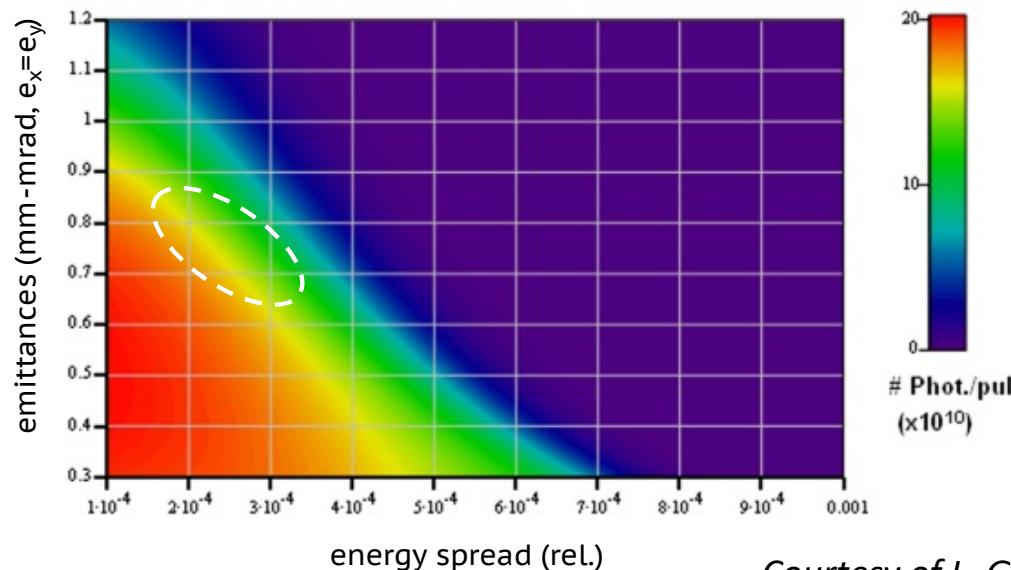
Transverse wakefields affect the peak current profile by max $\sim 1 \mu\text{rad}/\text{m}$ transverse kick, assuming to systematically find higher than 300 μm misalignment, for $r=2.3\text{mm}$



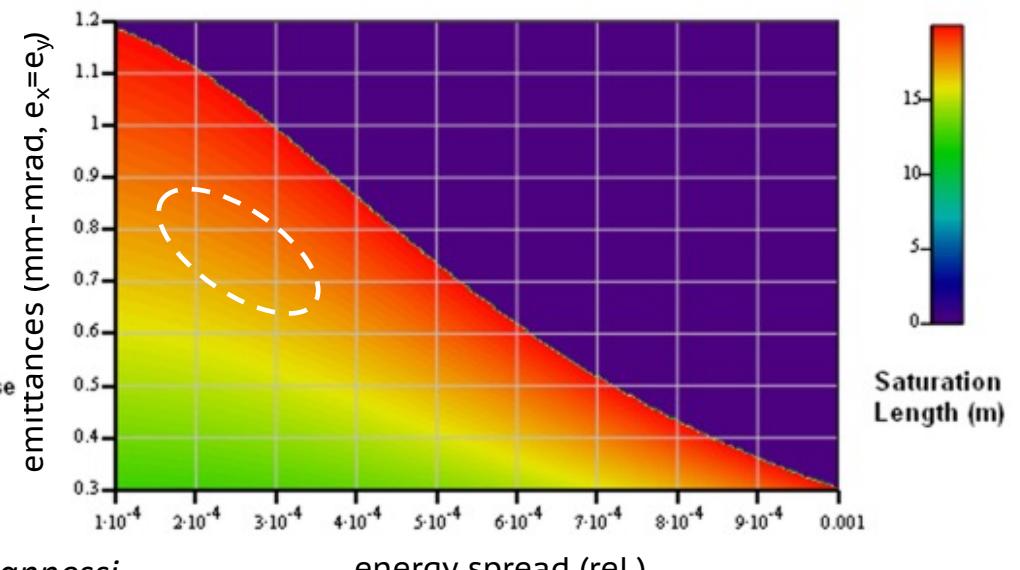
FEL parameter acceptance – Linear polarization

- Modified Ming Xie-Dattoli model to analyze the FEL performance **in linear polarization**
- Working point: photon energy of 4 nm = 310 eV at 1 GeV
- Gaussian beam in current, energy, energy spread, transverse momenta and spatial distributions
- Peak current 1.5 kA, FWHM bunch duration 5 fs, average $\beta_x = \beta_y = 10$ m, and $\epsilon_x = \epsilon_y$.

Photon yield $N_\gamma/\text{pulse} \sim 10^{11}$



Sat. length $\sim 25\text{-}28$ meters

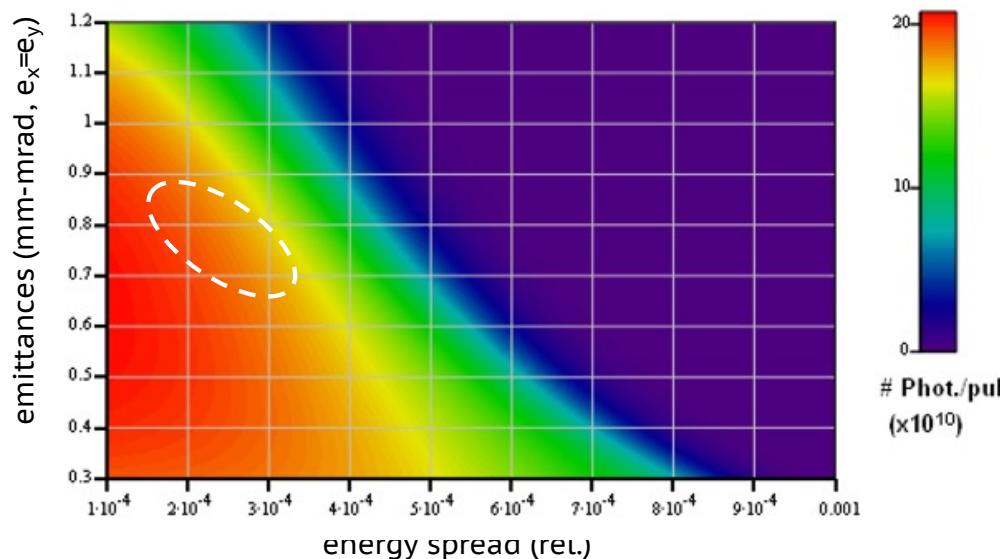


Courtesy of L. Giannessi

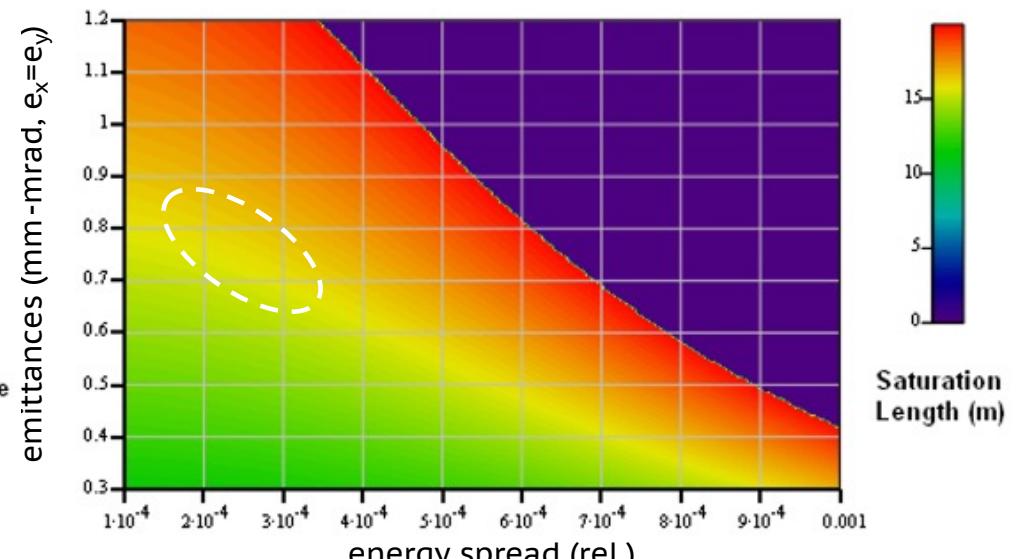
FEL parameter acceptance – Circular polarization

- Modified Ming Xie-Dattoli model to analyze the FEL performance **in circular polarization**
- Working point: photon energy of 4 nm = 310 eV at 1 GeV
- Gaussian beam in current, energy, energy spread, transverse momenta and spatial distributions
- Peak current 1.5 kA, FWHM bunch duration 5 fs, average $\beta_x = \beta_y = 10$ m, and $\epsilon_x = \epsilon_y$.

Higher $N_\gamma/\text{pulse} \gtrsim 2 \times 10^{11}$

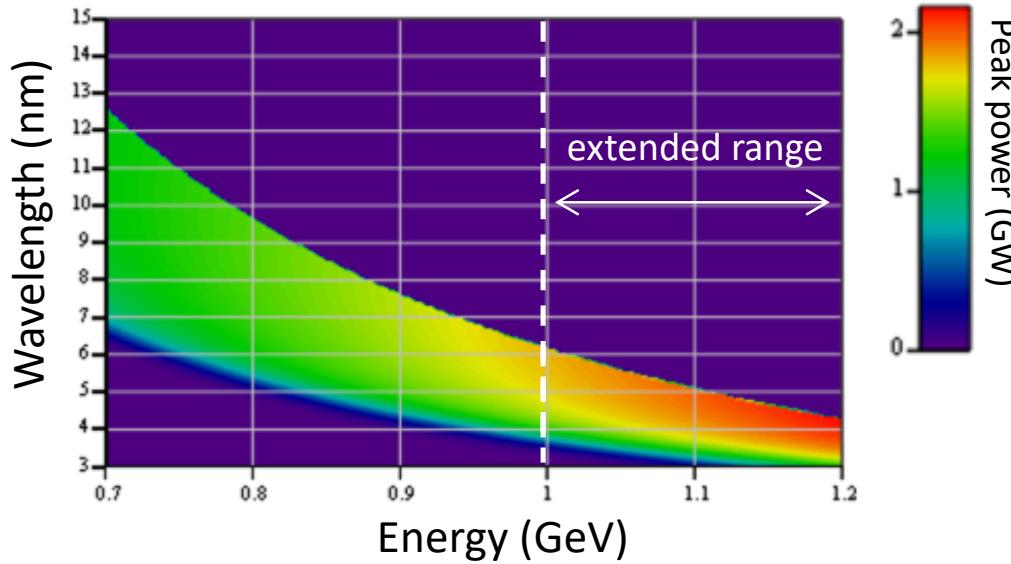


Shorter Sat. length $\sim 15\text{-}20$ meters

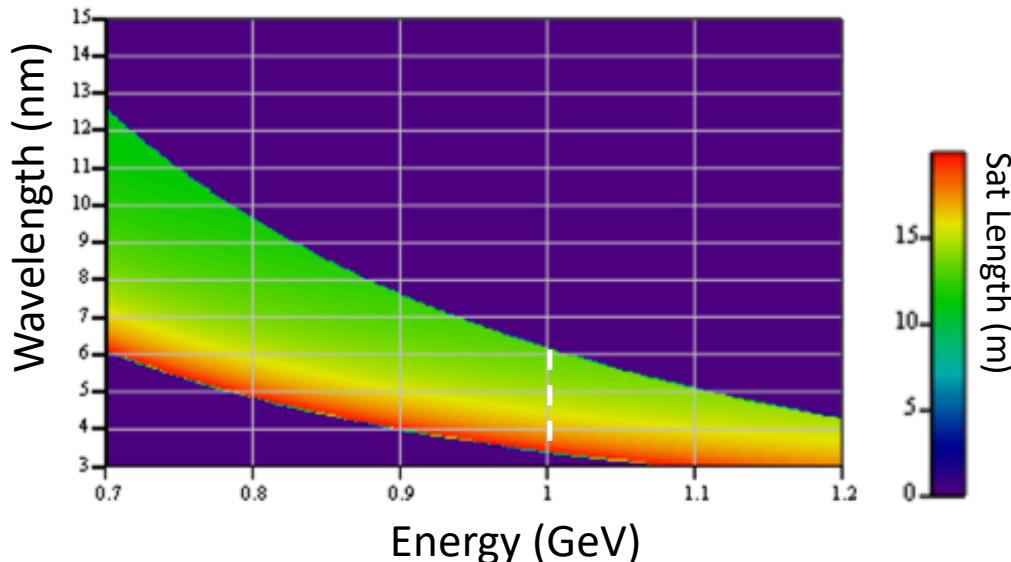


Courtesy of L. Giannessi

FEL performance vs. E_{beam} – Linear polarization



Courtesy of L. Giannessi



$$\lambda_{\text{res}} = \frac{\lambda_u}{2\gamma^2} \left[1 + \frac{K^2(g_u)}{2} \right]$$

Tunability in beam energy $\gamma m_e c^2$ and in undulator gap g_u weighted in terms of peak power and saturation length

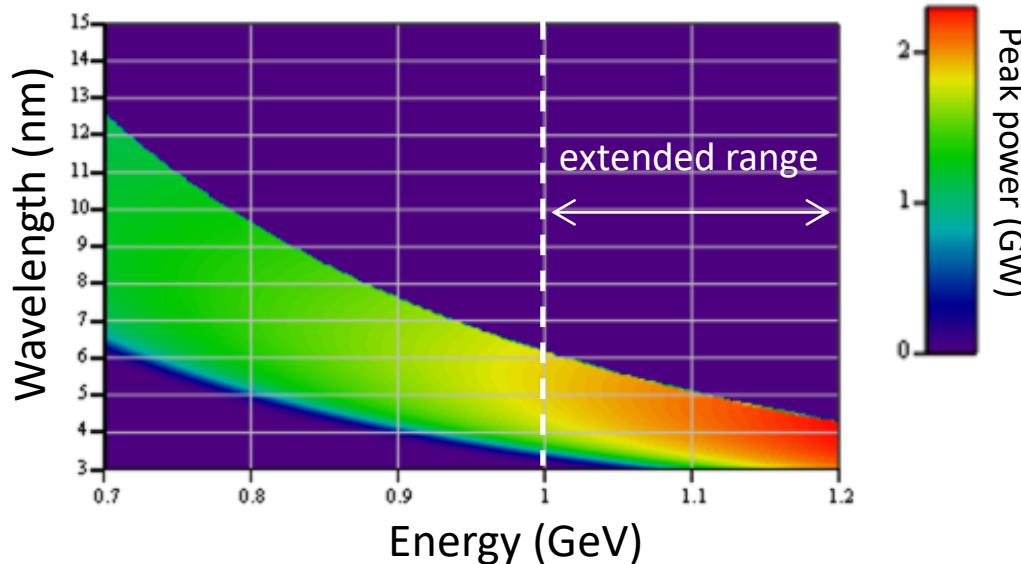
Linear Polarization:
undulator gap gives limited lever arm

shorter λ_{res} → lower K values
→ lower power and longer saturation

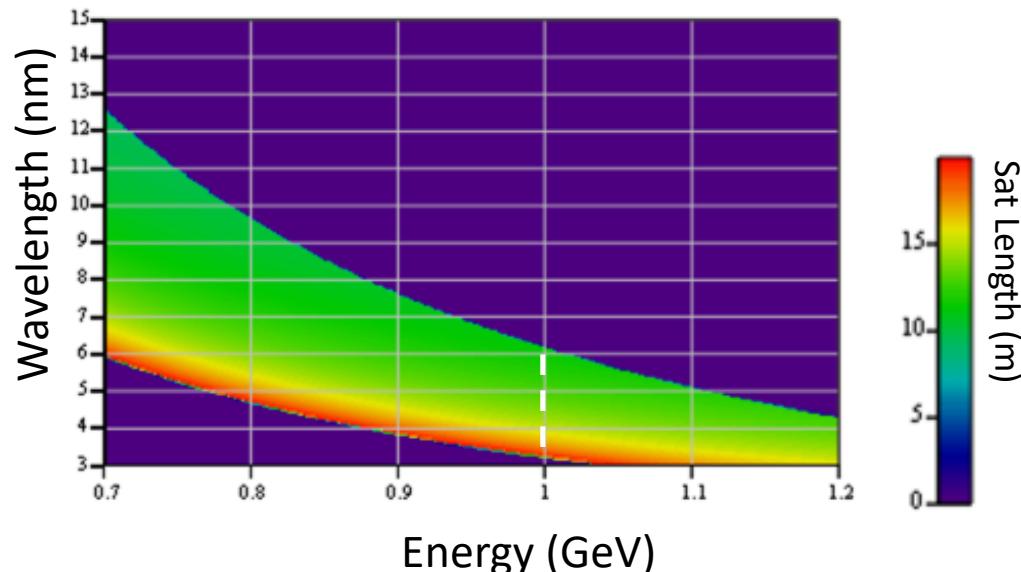
By increasing beam energy
(other parameters constant) →

chance to make 4nm with performance
similar to longer wavelengths

FEL performance vs. E_{beam} – Circular polarization



Courtesy of L. Giannessi



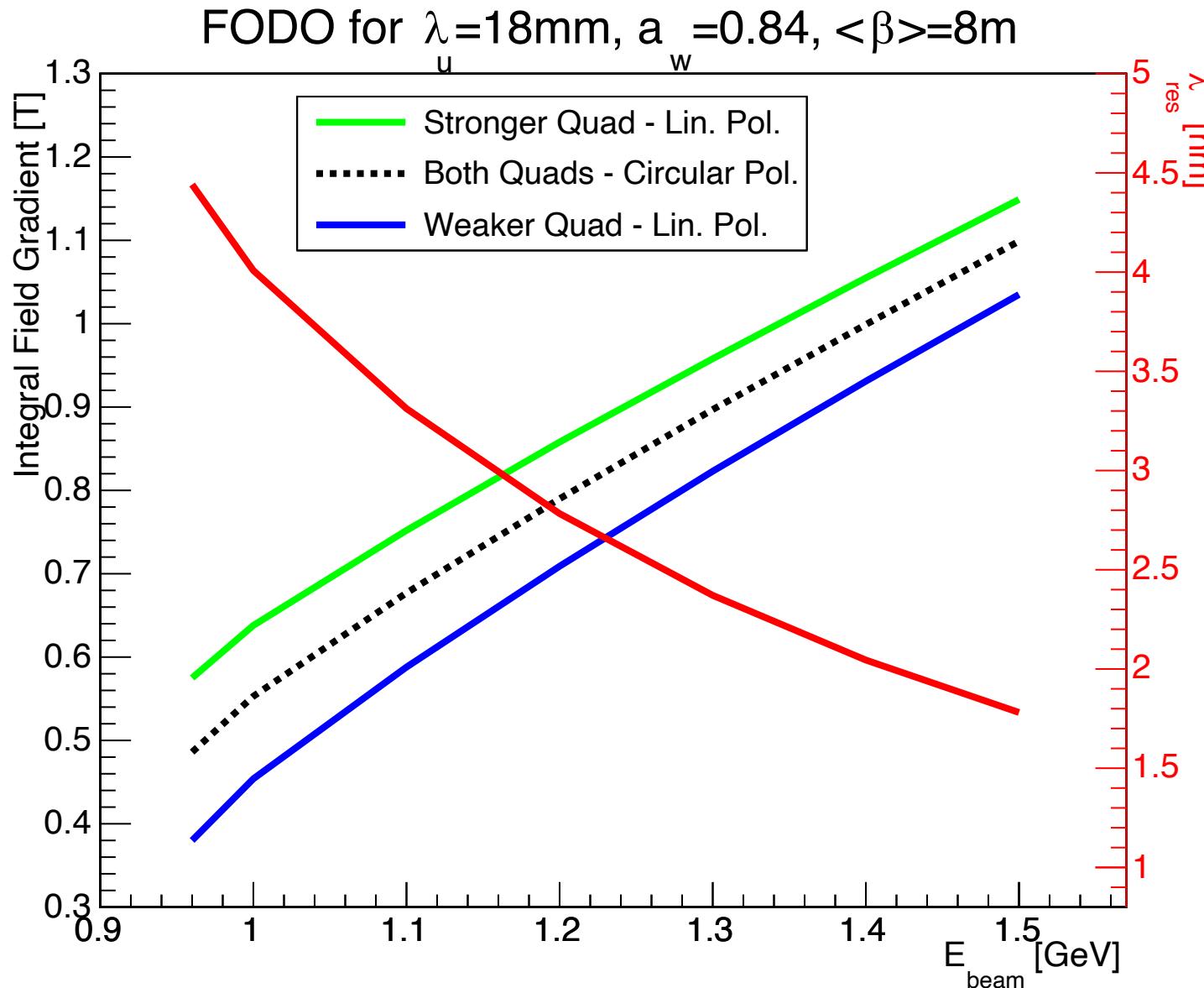
$$\lambda_{\text{res}} = \frac{\lambda_u}{2\gamma^2} [1 + K^2(g_u)]$$

Tunability in beam energy $\gamma m_e c^2$ and in undulator gap g_u weighted in terms of peak power and saturation length

Circular Polarization:
wider undulator gap tunability than Linear
→ “water window” wavelengths probed with higher photon power yields and shorter saturation lengths

By increasing beam energy (other parameters constant) →
saturation length below ~ 20 m most of the available spectrum;
chance to reach for 3nm

Trajectory matching for both polarizations vs. E_{beam}



Matching quad strengths at each E_{beam} value:

undulator focuses on 1 plane only in Linear Polar.

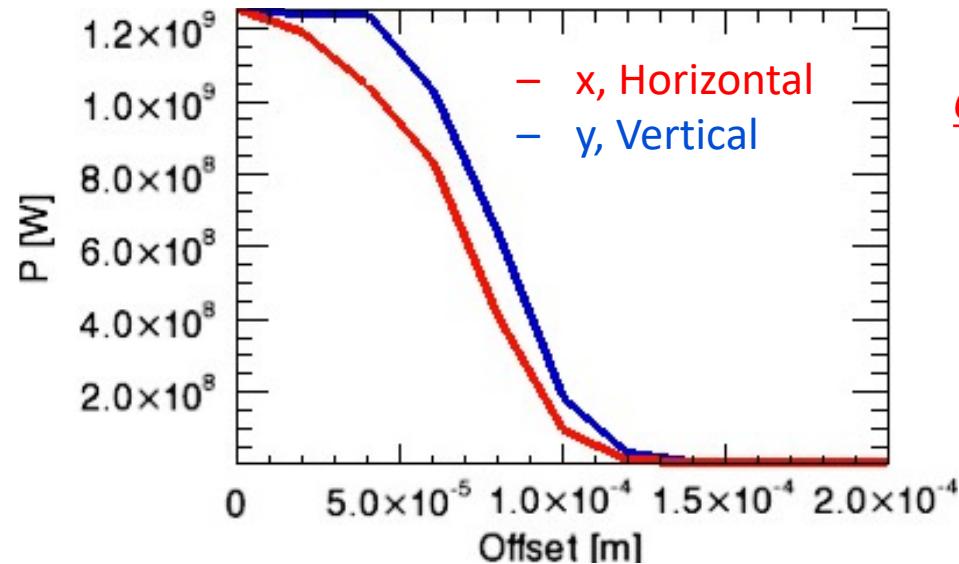
Quad (~ 10 cm magn. length) integral field gradients are such to sustain even higher beam energies →

Possible to reach for 3nm with the same undulator and quadrupole devices, if $E_{\text{beam}} \sim 1.2 \text{ GeV}$

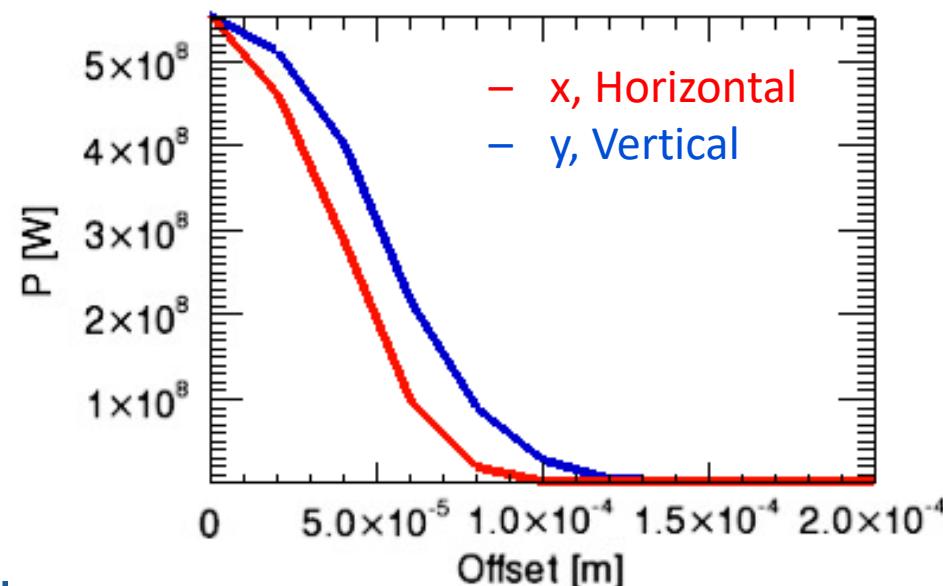
Quad. offset errors (up to ~ 400 μm) lead to an off-axis beam wander to be compensated with a corrector magnet

FEL tolerance on injection transverse offsets

Quad. offsets can be corrected by steering the trajectory, **angle and position inj. jitters** can't be compensated



FEL power reduction in
Circular polarization APPLE-X



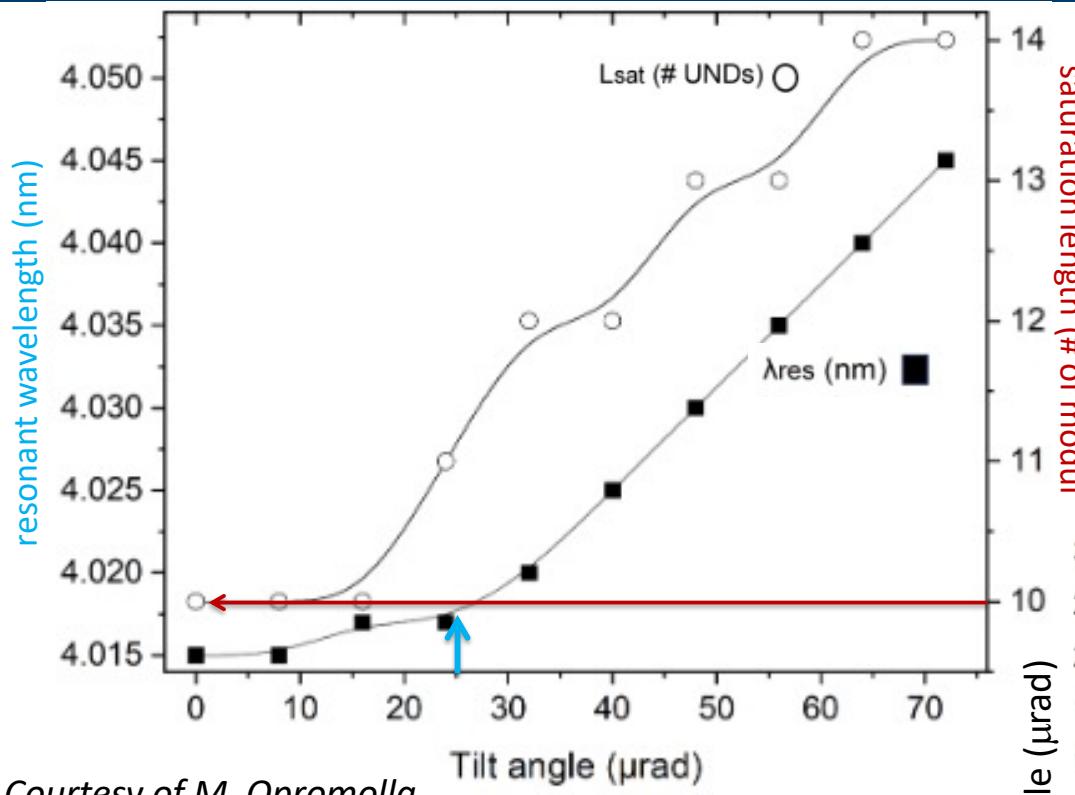
FEL power reduction in
Linear polarization APPLE-X

Conclusion

Circular Polarization: $50\mu\text{m}$ offset results in ~ 67% of the ideal power yield

Linear Polarization: the reduction is steeper and $50\mu\text{m}$ leads to ~ 20% power decrease

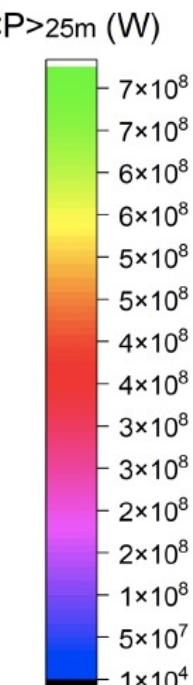
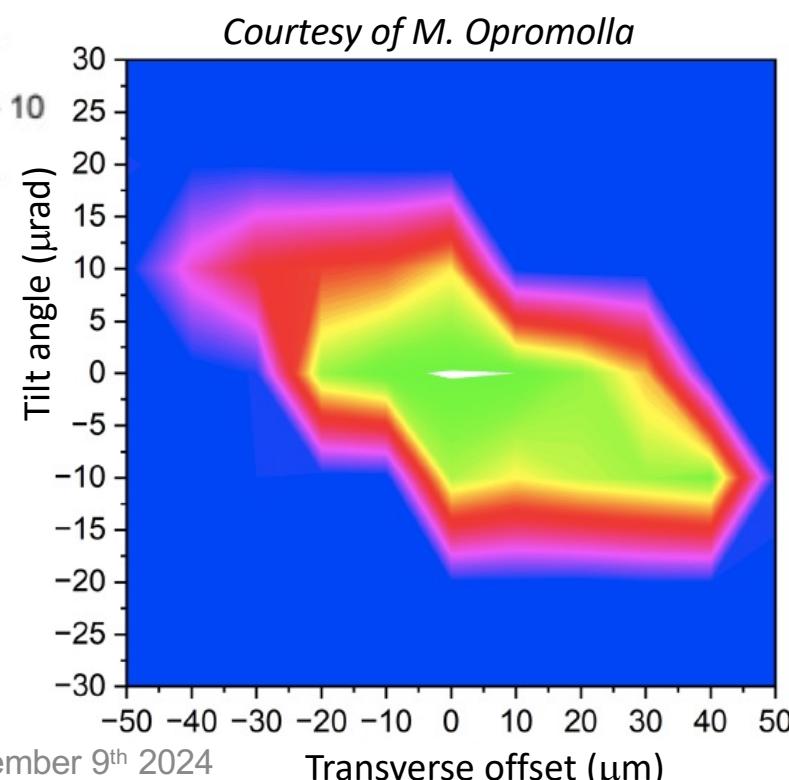
FEL tolerance on injection tilt angles



Courtesy of M. Opronolla

Cross-correlation between tilt angle and transverse offset results in more severe constraints: to stay in the > 60% of the ideal FEL power \rightarrow tilt angle $< \pm 6 \mu\text{rad}$ and offset position $< \pm 25 \mu\text{m}$

Electron beam misalignments due to tilted injections detune the resonant wavelength and increase sat. length: 10 und. modules demand tilt angle $< 25 \mu\text{rad} \rightarrow \sim 0.06\%$ wavelength detuning!
Even if accepted, such an angle affects FEL power at undulator exit!



Conclusions

- ✓ The undulator adopted for the AQUA beamline consists of an out-of-vacuum APPLE-X: a well-known technology that allows selectable polarization and fine tuning in the water window
- ✓ Extensive studies on RW wakefield effects – both longitudinal in energy loss and transverse in the e-beam trajectory – show that chamber $r=2.5\text{mm}$ is safe
- ✓ Ideal reference electron beam values allow to enter the realm of $O(10^{11}) \text{ N}_\gamma/\text{pulse}$ for both polarizations at $4\text{nm} \rightarrow$ shorter λ to be covered with either improved e-beam quality or higher E_{beam} → same beamline is able to sustain even $E > 1 \text{ GeV}$ energies
- ✓ FEL tolerance 3D simulations on e-beam injection misalignments result in parameter values acceptance for both transverse offset positions and tilt angles – analyzed in terms of λ detuning, saturation length and power
- ✓ Full time-dependent results with S2E particle distributions under realistic conditions are on-going towards the TDR delivery

Please, stay FEL-tuned!
Thank you 4 your attention