

# Radiation of surface polaritons by an annular beam coaxially enclosing a cylindrical waveguide

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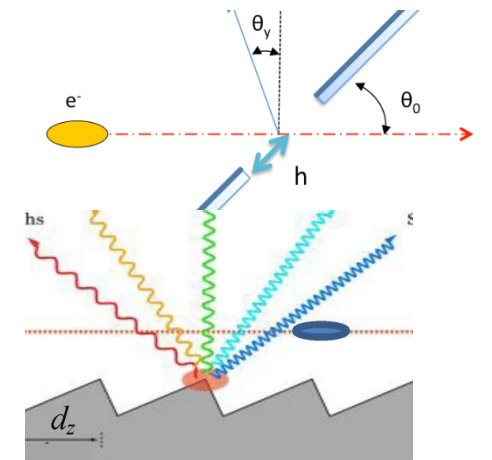
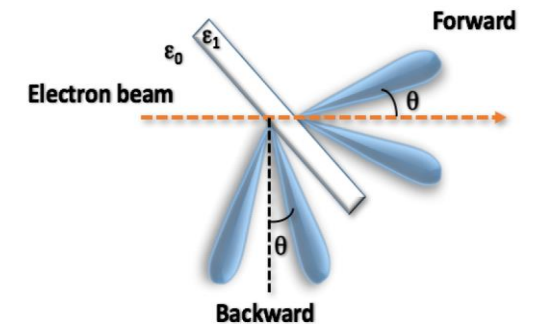
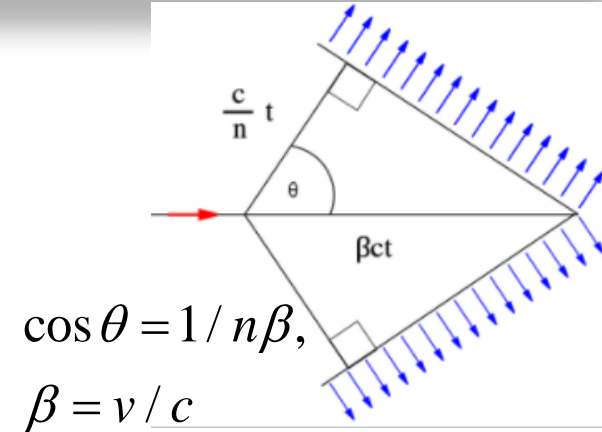
# Outline

- ❖ Radiation processes in media
- ❖ Surface plasmon polaritons
  - ❖ Annular beam around a cylinder
- ❖ Conclusions

# Radiation processes in media

Interaction of charged particles with media gives rise to various types of radiation processes

- ❖ **Cherenkov radiation:** charged particles passing through optically transparent media at speeds greater than the speed of light in that medium
- ❖ **Transition radiation:** charged particles pass the boundary between two media with different refractive index
- ❖ **Diffraction radiation:** charged particle moves in the vicinity of a dielectric medium
- ❖ **Smith-Purcell radiation/Resonance diffraction radiation**  
Diffraction radiation on periodic structures



# Surface Plasmon Polaritons

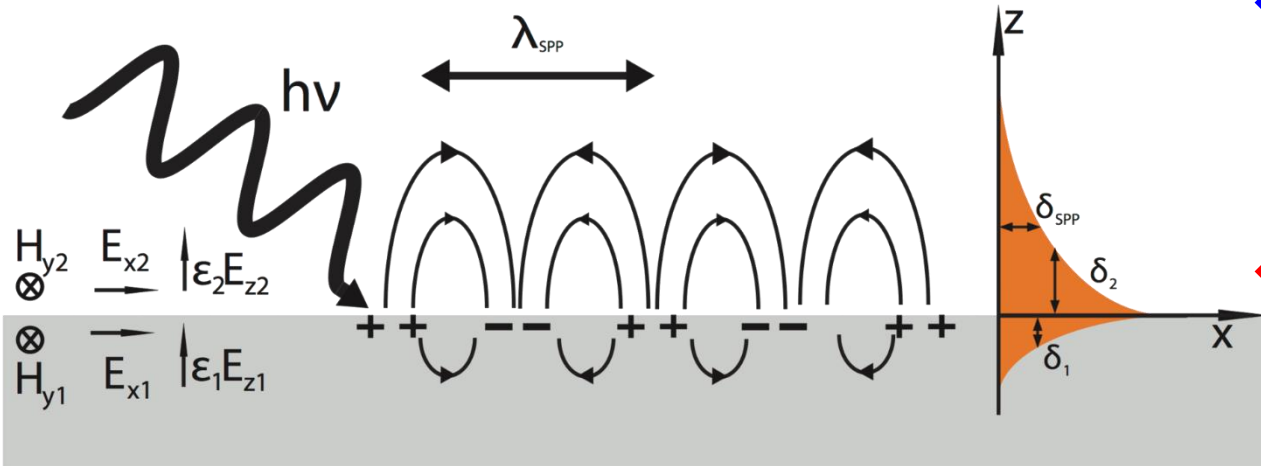
- ❑ Interfaces between two media with different electromagnetic characteristics give rise to **new types** of electromagnetic modes → **Surface modes**
- ❑ **Surface modes** depend on the geometry of the separating boundary and carry an important information on the electromagnetic properties of the contacting media
- ❑ Among the various types of surface waves, the **surface plasmon polaritons (SPP)** have been a powerful tool in the wide range of investigations including
  - **Surface imaging**
  - **Surface-enhanced Raman spectroscopy**
    - **Data storage and Biosensors**
    - **Plasmonic waveguides**
    - **Light-emitting devices**
    - **Plasmonic solar cells, etc.**

# Surface Plasmon Polaritons

- ❖ SPPs are evanescent electromagnetic waves propagating along a **metal-dielectric interface** as a result of collective oscillations of **electron subsystem** coupled to **electromagnetic field**
- ❖ SPPs exist in frequency ranges where the real part of the permittivity undergoes a **change of the sign** at the interface
- ❖ Perpendicular to the interface SPPs have **subwavelength-scale** confinement

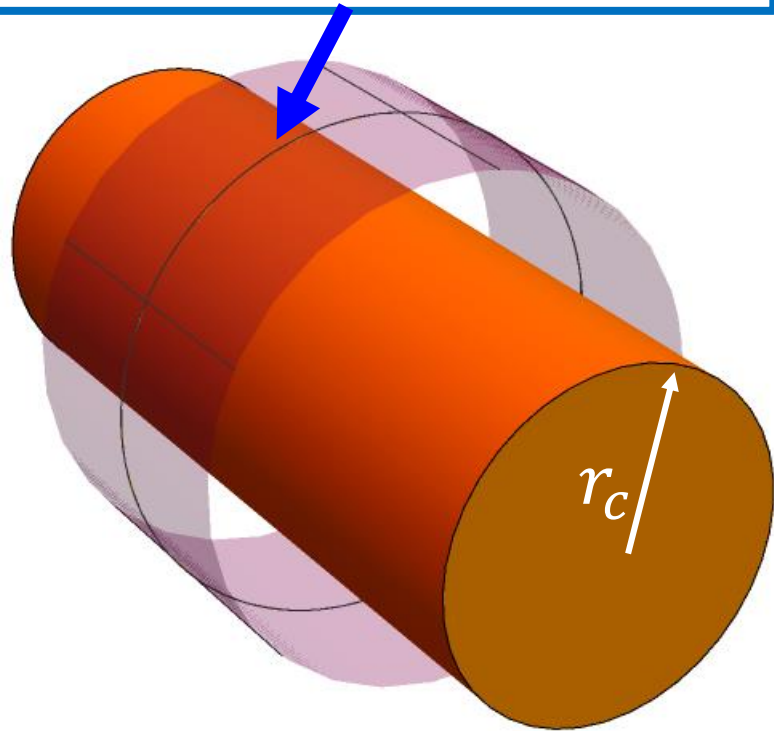
❖ Remarkable properties of SPPs include

- ❖ Possibility of concentrating electromagnetic fields **beyond the diffraction** limit of light waves
- ❖ **Enhancing the local field strengths** by orders of magnitude



# Problem setup

$$j_l(x) = \delta_{3l} \frac{qv}{r} \delta(r - r_0) \delta(z - vt)$$



- ❑ **Cylindrical waveguide** with permittivity  $\varepsilon_0$  immersed into a homogeneous medium with permittivity  $\varepsilon_1$
- ❑ An **annular beam** coaxially moves outside the cylinder
- ❑ The radiation from annular beams of arbitrary distribution (**negligible overlaps with the dielectric cylinder**) can also be obtained (by means of integration)

Charge density:  $\rho(x) = q\delta(r - r_0)\delta(z - vt) / r$

Total charge of the beam:  $Q = 2\pi q$

# Green's tensor

## The components of the Green's tensor

$$G_{l3}(r, r_0) = G_{l3}^{(0)}(r, r_0) + i^{2-l} \sum_p p^{l-1} \overline{C}_n^{(3p)}(r_c, r_0) H_{n+p}(\lambda_1 r),$$

$$G_{33}(r, r_0) = G_{33}^{(0)}(r, r_0) - \frac{\pi}{2i} H_n(\lambda_1 r_0) \frac{V_n^J}{V_n^H} H_n(\lambda_1 r),$$

$$\overline{C}_n^{(3p)}(r_c, r') = k_z \frac{J_n(\lambda_0 r_c)}{2\alpha_n} \frac{H_n(\lambda_1 r')}{V_n^H} \frac{J_{n+p}(\lambda_0 r_c)}{r_c V_{n+p}^H}$$

$$V_n^F = \lambda_1 J_n(\lambda_0 r_c) F'_n(\lambda_1 r_c) - \lambda_0 F_n(\lambda_1 r_c) J'_n(\lambda_0 r_c).$$

$$\lambda_j^2 = k_z^2 (\beta^2 \varepsilon_j - 1), \quad j = 0, 1,$$

$$\alpha_n = \frac{\varepsilon_0}{\varepsilon_1 - \varepsilon_0} - \frac{\lambda_0}{2} J_n(\lambda_0 r_1) \sum_{l=\pm 1} l \frac{H_{n+l}(\lambda_1 r_1)}{V_{n+l}^H}.$$

$\alpha_n = 0$ : eigenmodes of the dielectric cylinder

# The Vector and Scalar Potentials

$$A_i(x) = -\frac{1}{2\pi^2 c} \int d^4x' \sum_{l=1}^3 G_{il}(x, x') j_l(x')$$

$$\begin{aligned} A_1(k_z, r) &= \frac{2qv}{ic} D H_0(\lambda_1 r_0) H_1(\lambda_1 r), \\ A_3(k_z, r) &= \frac{i\pi qv}{c} \left[ J_0(\lambda_1 r_{<}) H_0(\lambda_1 r_{>}) - \frac{V_0^J}{V_0^H} H_0(\lambda_1 r_0) H_0(\lambda_1 r) \right], \end{aligned}$$

for  $r > r_c$

$$\begin{aligned} A_1(k_z, r) &= \frac{2qv}{ic} D H_0(\lambda_1 r_0) J_1(\lambda_0 r), \\ A_3(k_z, r) &= -\frac{2qv}{c} \frac{H_0(\lambda_1 r_0)}{r_c V_0^H} J_0(\lambda_0 r), \end{aligned}$$

for  $r < r_c$

Where

$$D = \frac{k_z J_0(\lambda_0 r_c)}{r_c \alpha_0(\omega, k_z) V_0^H V_1^H} \begin{cases} H_1(\lambda_1 r_c), & r < r_c \\ J_1(\lambda_0 r_c), & r > r_c \end{cases}$$

$$\varphi(k_z, r) = -\frac{2qv}{\omega \epsilon_0} \left( \lambda_0 D + \frac{k_z}{r_c V_0^H} \right) H_0(\lambda_1 r_0) J_0(\lambda_0 r) = -\frac{2q}{\epsilon_0} \left( \sqrt{\beta^2 \epsilon_0 - 1} D + \frac{1}{r_c V_0^H} \right) H_0(\lambda_1 r_0) J_0(\lambda_0 r).$$

for  $r < r_c$

$$\varphi(k_z, r) = -\frac{\pi q}{i\epsilon_1} \left[ J_0(\lambda_1 r_{<}) H_0(\lambda_1 r_{>}) + \left( \frac{2i}{\pi} \sqrt{\beta^2 \epsilon_1 - 1} D - \frac{V_0^J}{V_0^H} \right) H_0(\lambda_1 r_0) H_0(\lambda_1 r) \right].$$

for  $r > r_c$



# Radiation of Surface Polaritons

For surface polaritons the real parts of the permittivities  $\epsilon_0$  and  $\epsilon_1$  should have opposite signs.

$$\epsilon'_0 < 0 < \epsilon'_1 \text{ and } \beta^2 \epsilon'_1 < 1$$

$$\gamma_j = \sqrt{1 - \beta^2 \epsilon_j}$$

$$\lambda_j r_c = i \gamma_j u, \quad u = k_z r_c = \omega r_c / v$$

Drude model

$$\epsilon_0(\omega) = 1 - \frac{\omega_p^2}{\omega^2 + i\gamma\omega}$$

The dispersion for the permittivity  $\epsilon_1$  is weak in the spectral range under consideration

Modified Bessel functions

$$J_0(\lambda_0 r_c) = I_0(\gamma_0 u), \quad J_1(\lambda_0 r_c) = i I_1(\gamma_0 u),$$
$$H_0(\lambda_1 r_c) = \frac{2}{\pi i} K_0(\gamma_1 u), \quad H_1(\lambda_1 r_c) = -\frac{2}{\pi} K_1(\gamma_1 u)$$

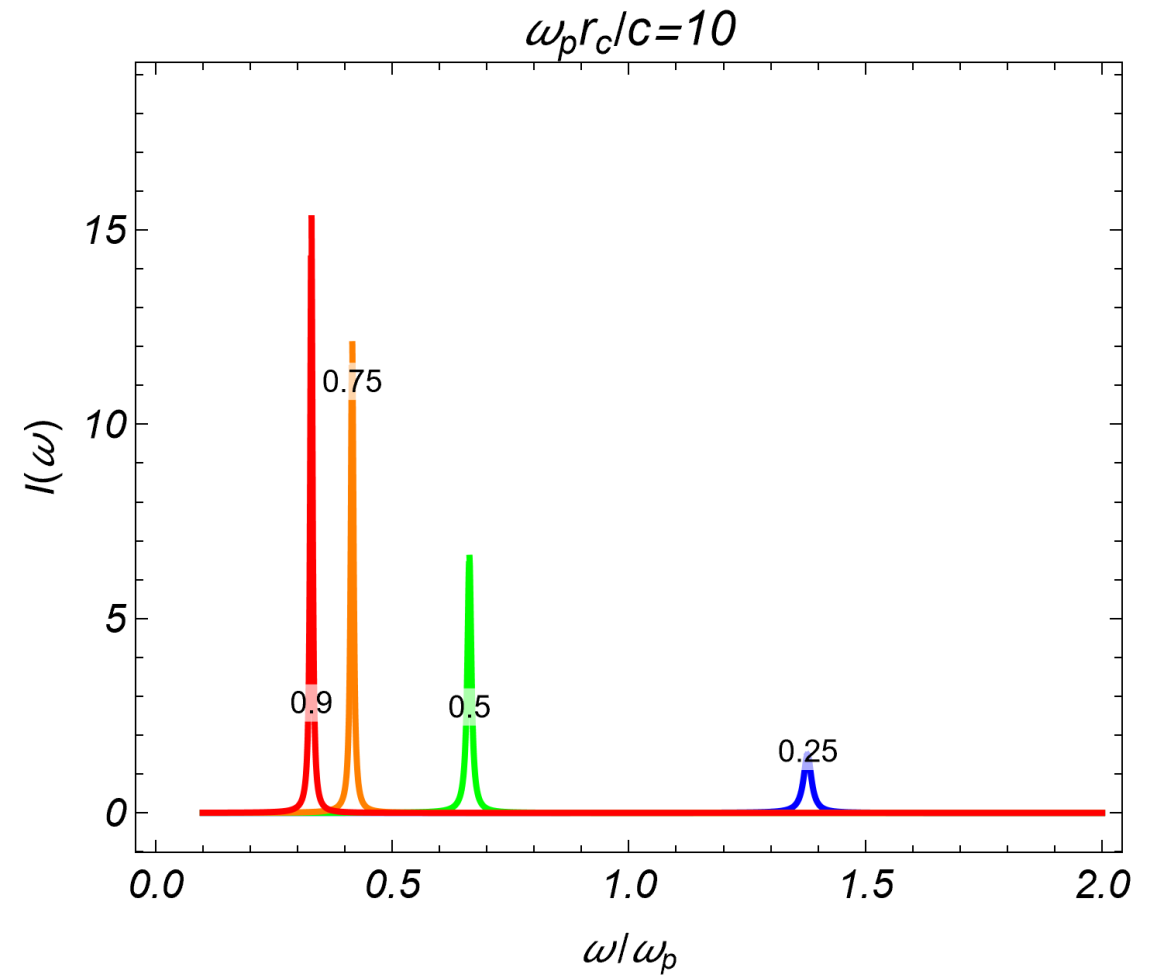
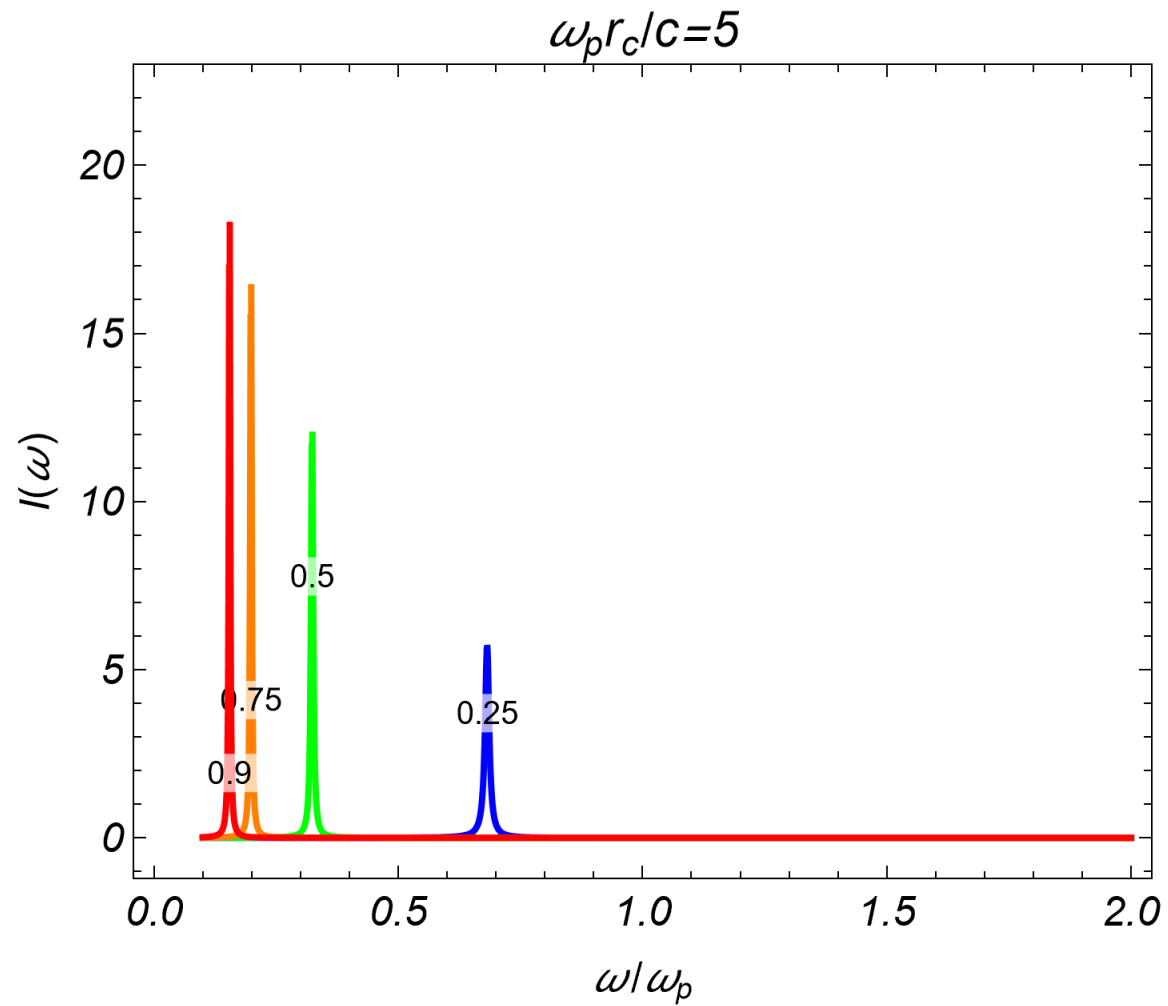
The dimensionless quantity associated with the energy loss spectral density

$$I(\omega) = \frac{r_c}{Q^2} \frac{d\mathcal{E}}{d\omega}$$

$$I(\omega) = \frac{2v r_c \omega}{\pi c^2} \operatorname{Re} \left[ i \left( 1 - \frac{1}{\beta^2 \epsilon_1} \right) \frac{\epsilon_0 \gamma_1 I_1(\gamma_0 u) I_0(\gamma_1 u) - \epsilon_1 \gamma_0 I_0(\gamma_0 u) I_1(\gamma_1 u)}{\epsilon_1 \gamma_0 I_0(\gamma_0 u) K_1(\gamma_1 u) + \epsilon_0 \gamma_1 I_1(\gamma_0 u) K_0(\gamma_1 u)} K_0^2(\gamma_1 u r_0 / r_c) \right]$$

# Numerical results

$$r/r_c = 1.05$$



# Conclusions

- ❑ We have considered an annular beam coaxially moving outside a cylindrical waveguide.
- ❑ A change of the sign in the dielectric permittivity  $\varepsilon$  leads to the generation of **surface plasmon-polaritons** localised on the boundary of two media.
- ❑ Sharp peaks in the surface plasmon-polariton intensity appear.
- ❑ The characteristics of the peaks can be controlled by the choice of the **velocity of the annular beam** and the **plasma frequency**.



***Thank you for your  
attention!***