

Cosmic Archeology with Primordial GW Backgrounds

Peera Simakachorn

(IFIC, University of Valencia)

peera.simakachorn@ific.uv.es



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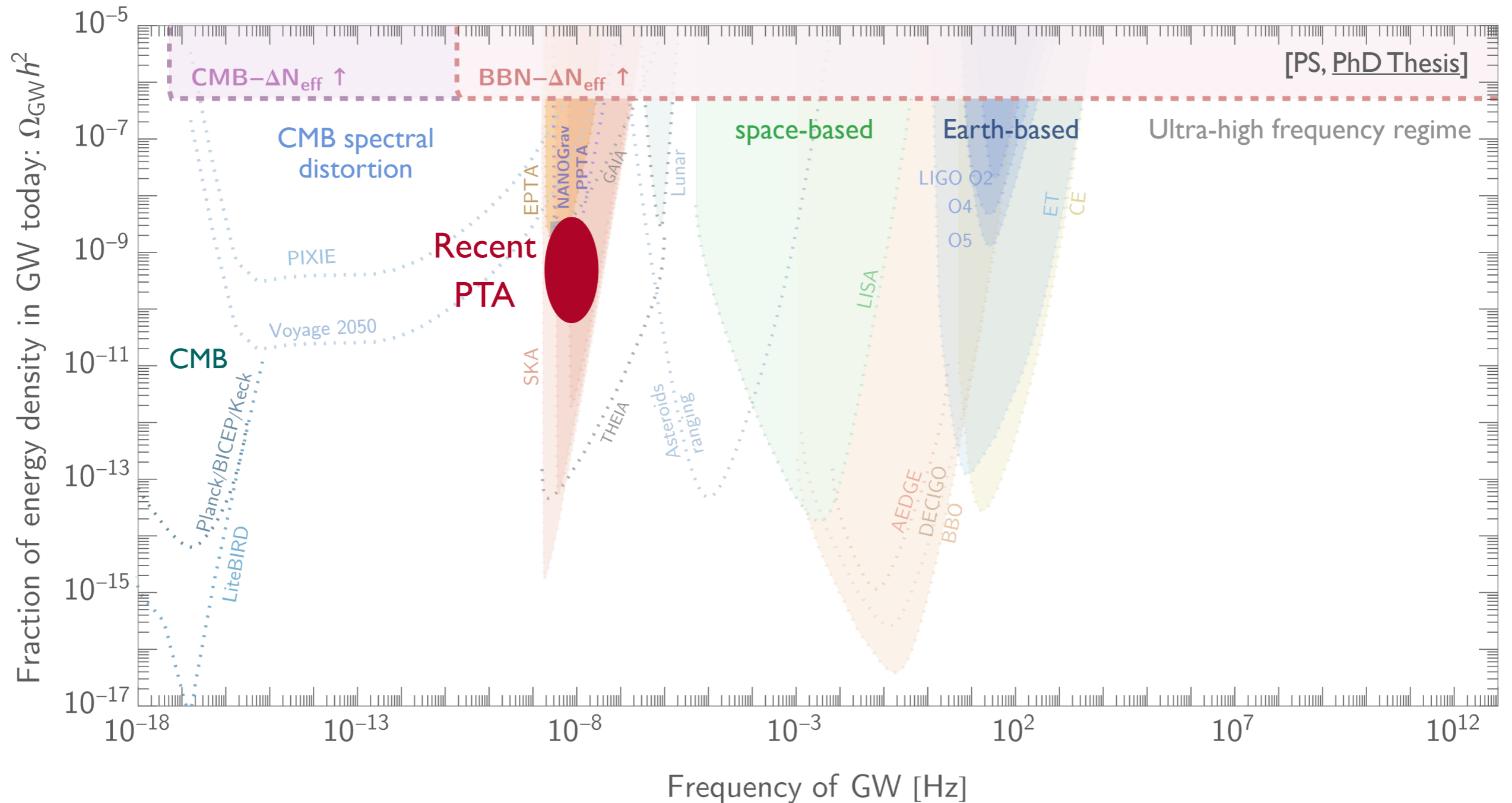
Cosmic Archeology with Primordial GW Backgrounds



Fundamental Physics and Gravitational Wave Detectors Workshop, Pollica 2024

16.09.2024

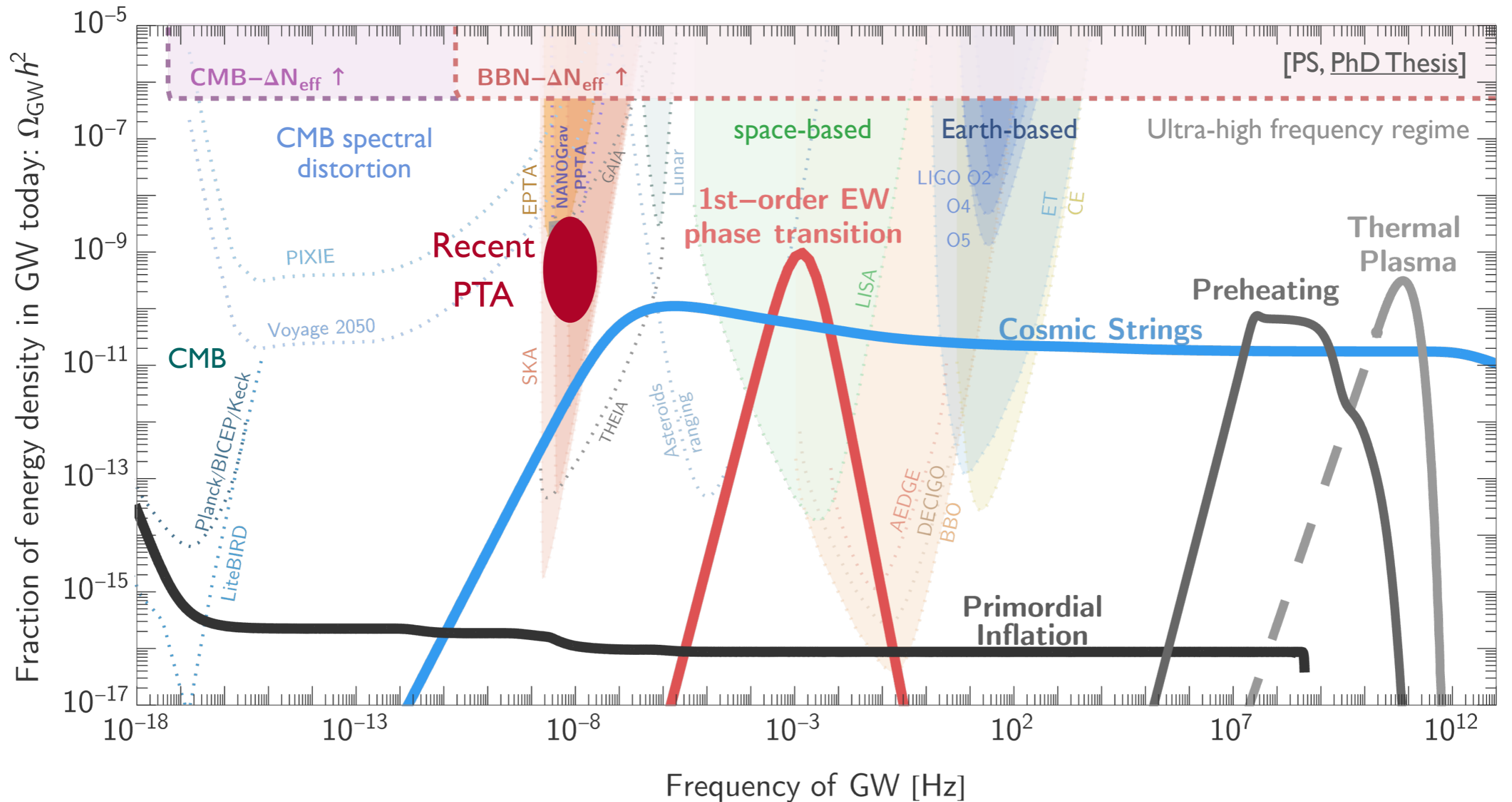
Landscape of Primordial Gravitational-Wave Background (GWB)



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$$\rho_{\text{today}}^{\text{GW}} = \rho_{\text{prod}}^{\text{GW}} \left(\frac{a_{\text{prod}}}{a_{\text{today}}} \right)^4$$

Most cosmological GWB \Leftrightarrow BSM of particle physics



[PS, PhD Thesis]

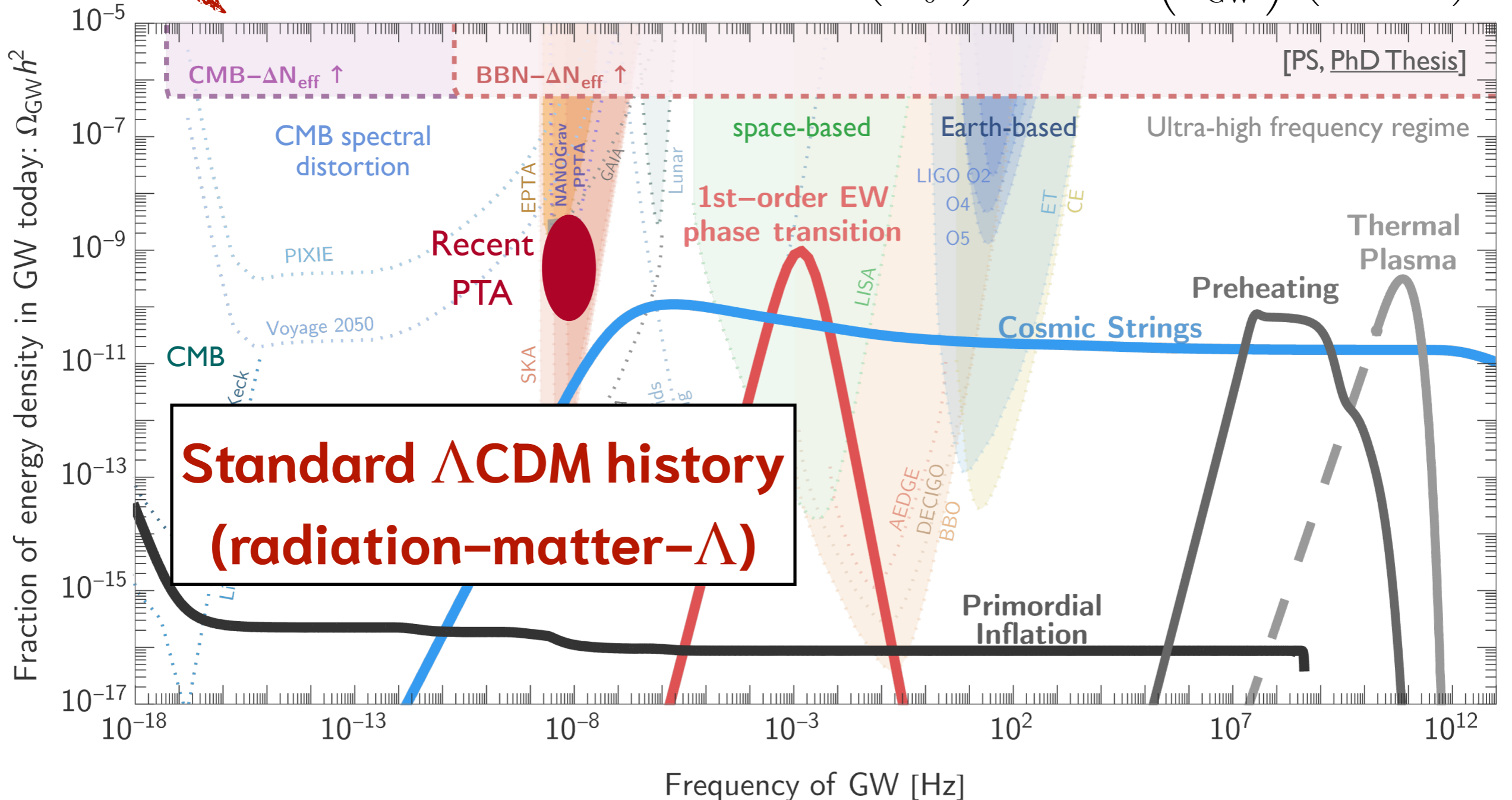
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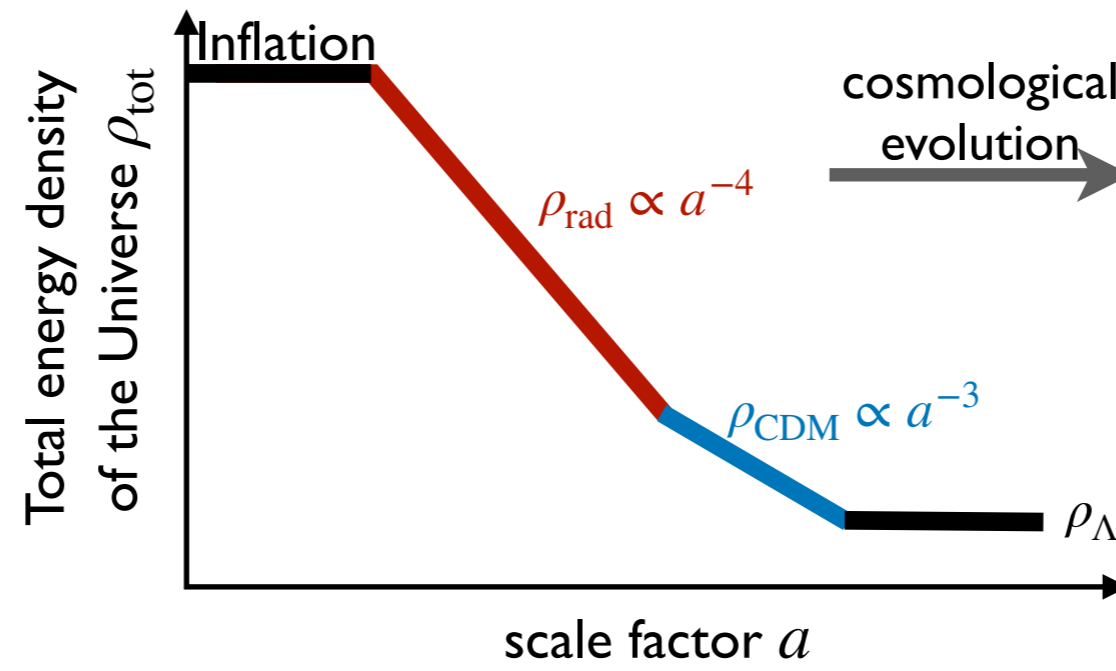
Most cosmological GWB \Leftrightarrow BSM of particle physics

← cosmic evolution

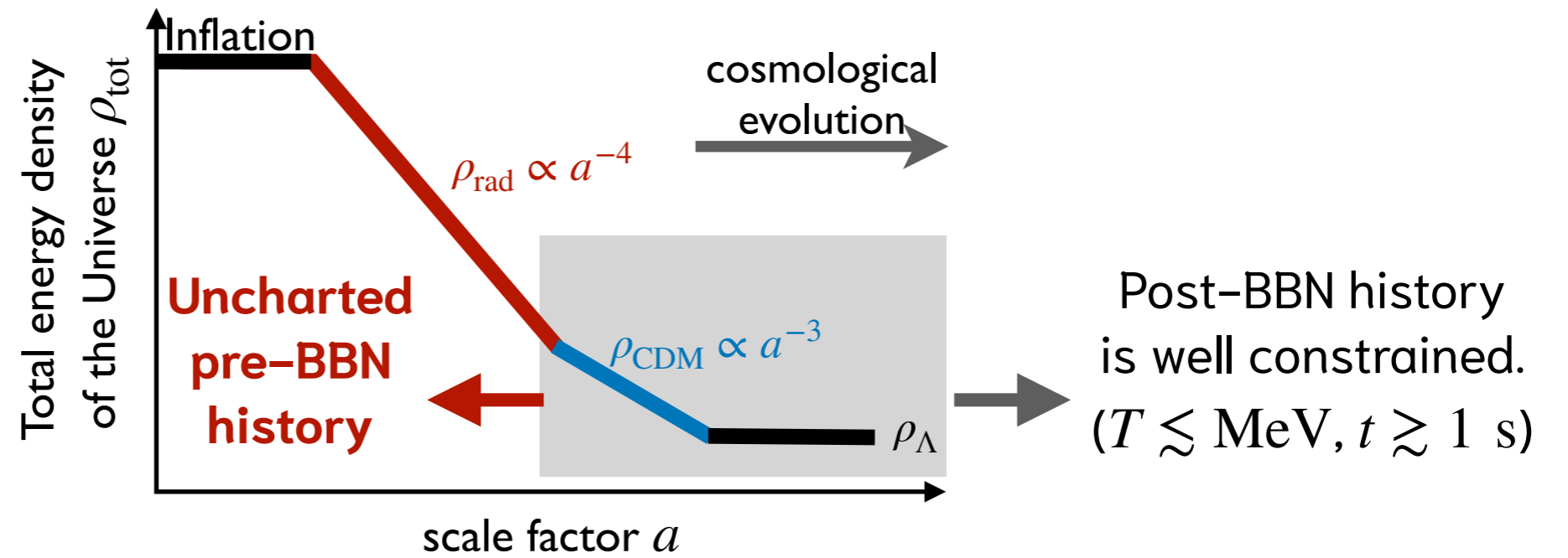
$$f_{\text{GW},0} = \lambda_{\text{GW}}^{-1} \left(\frac{a_{\text{prod}}}{a_0} \right) \simeq 10^{-6} \text{ Hz} \left(\frac{H_{\text{prod}}^{-1}}{\lambda_{\text{GW}}} \right) \left(\frac{T_{\text{prod}}}{100 \text{ GeV}} \right)$$



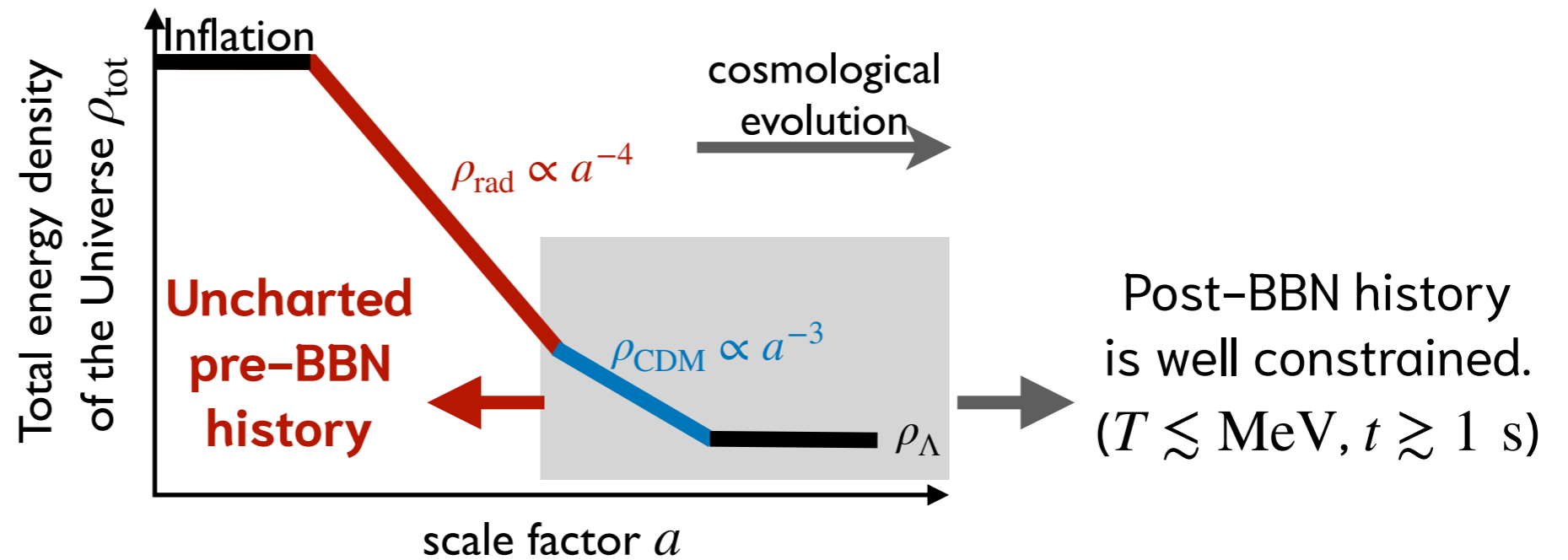
The Standard Λ CDM universe



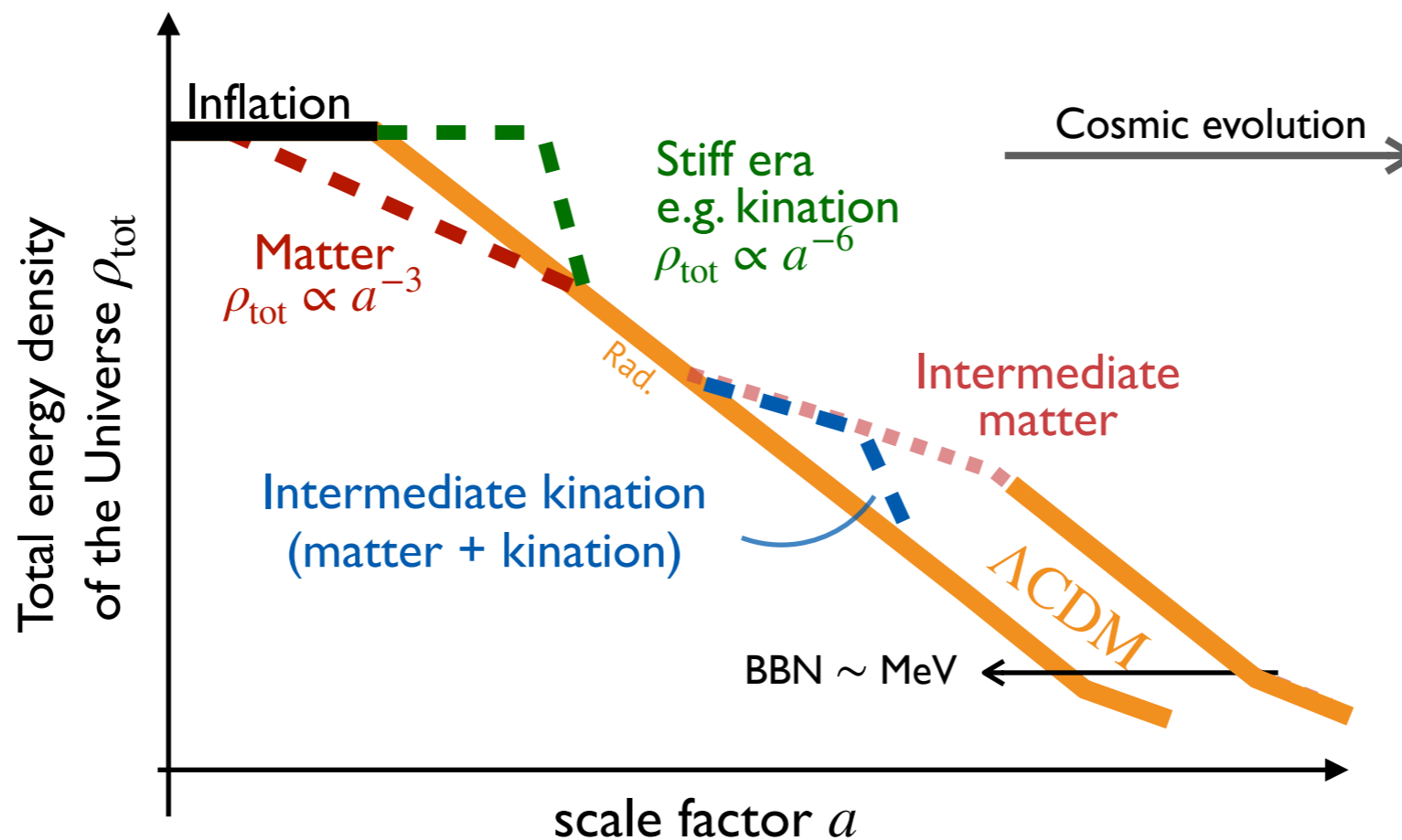
The Standard Λ CDM universe



The Standard Λ CDM universe



Cosmic histories beyond the standard (Λ CDM) picture.



Charting cosmic history with primordial GWB

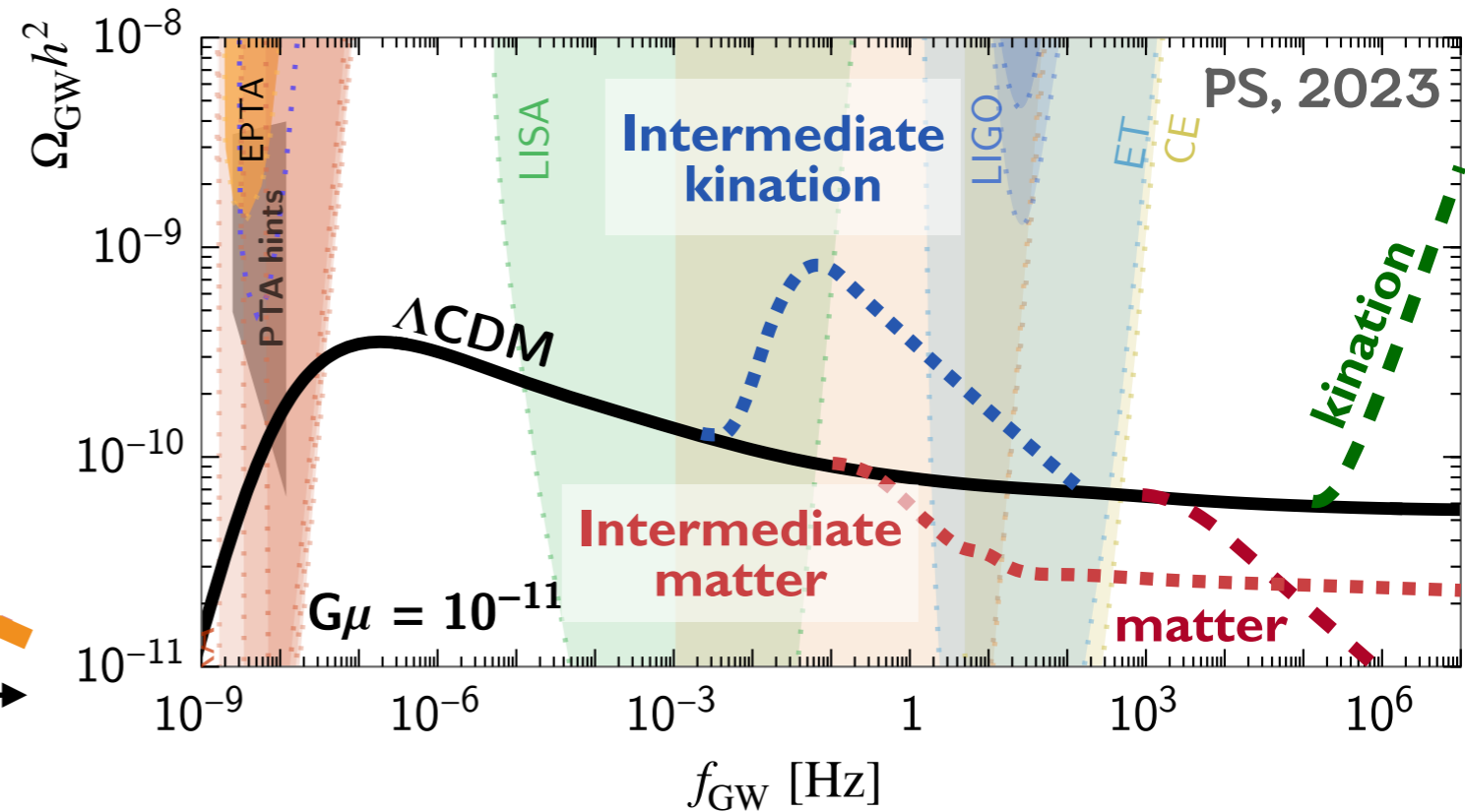
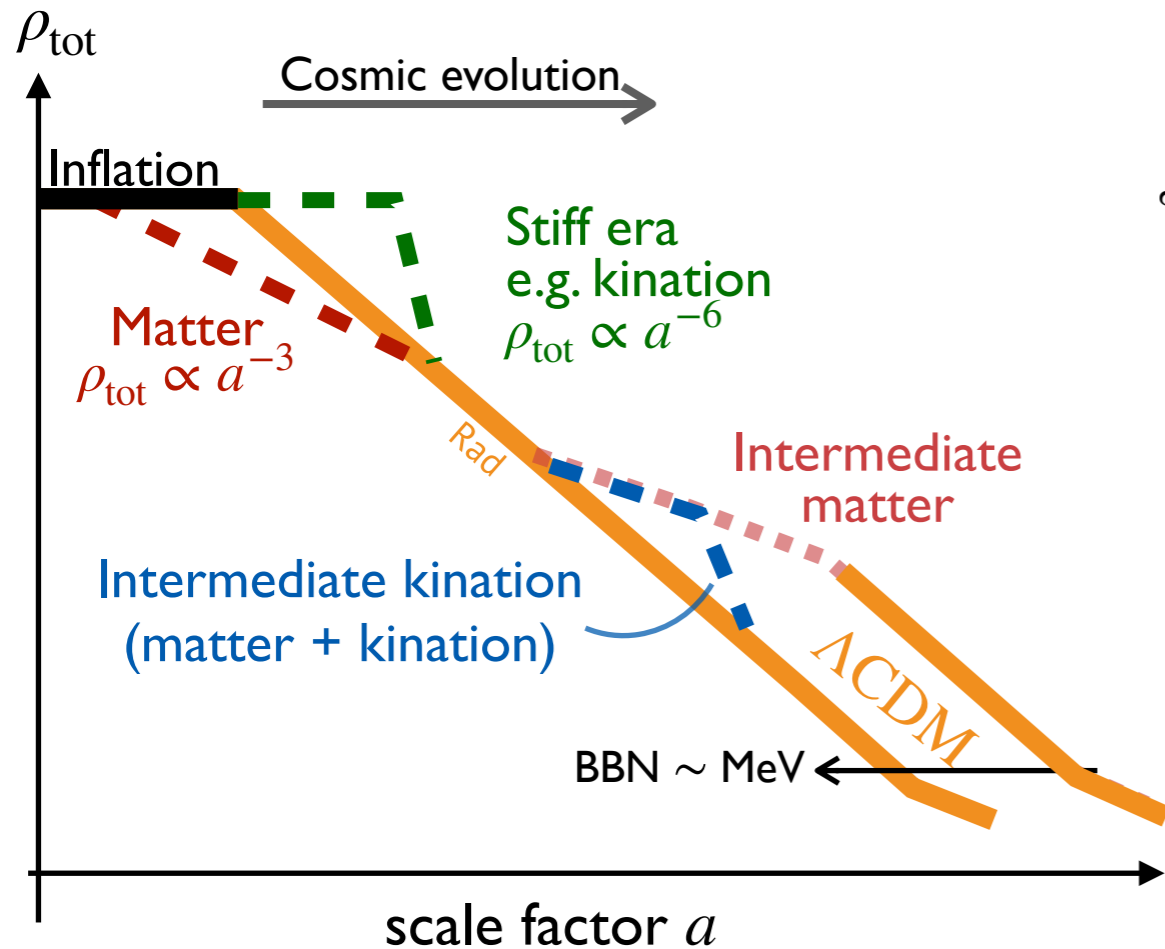
Non-standard cosmic history affects

- The GW sources
- The dilution from cosmic expansion

$$\rho_{\text{today}}^{\text{GW}} = \rho_{\text{prod}}^{\text{GW}} \left(\frac{a_{\text{prod}}}{a_{\text{today}}} \right)^4$$

“Non-standard” history beyond SM radiation era

⇒ “Features” in GW spectrum.



For long-lasting sources,
e.g., cosmic strings and inflation.

Several works...

- UV completions for non-standard cosmic histories
- how to probe with GWB from local & global cosmic strings, inflation, etc.

Matter/Stiff

e.g., reheating after inflation
 \Rightarrow Suppressed/enhanced

(Using cosmic-string GWB)

Cui, Lewicki, Wells, [1711.03104](#), [1808.08968](#)
 Servant, Gouttenoire, PS [1912.02569](#)

Intermediate Kination

e.g., “Rotating Axion”
 \Rightarrow “Peak” Signature

Co, Dunsky, Fernandez, et al. [2108.09299](#)
 Servant, Gouttenoire, PS [2108.10328](#), [2111.01150](#)

Intermediate Matter

e.g., oscillating moduli, dark photons, primordial black holes,

Servant, Gouttenoire, PS [1912.03245](#)

Blasi, Brdar, Schmitz, [2004.02889](#)

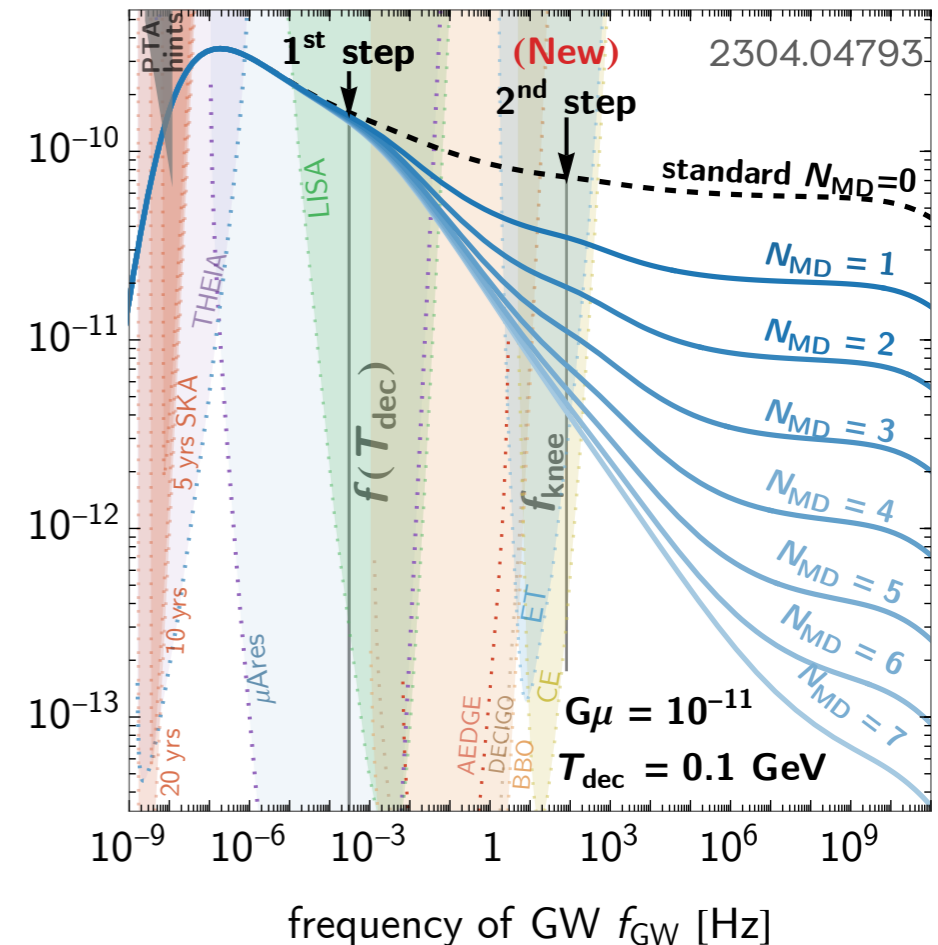
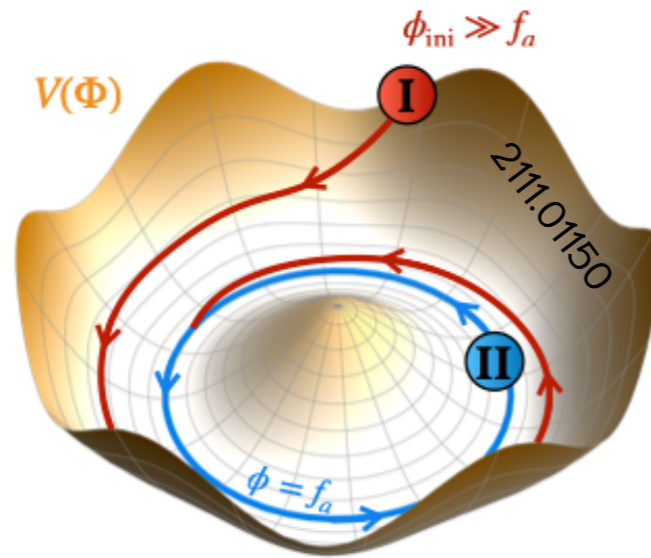
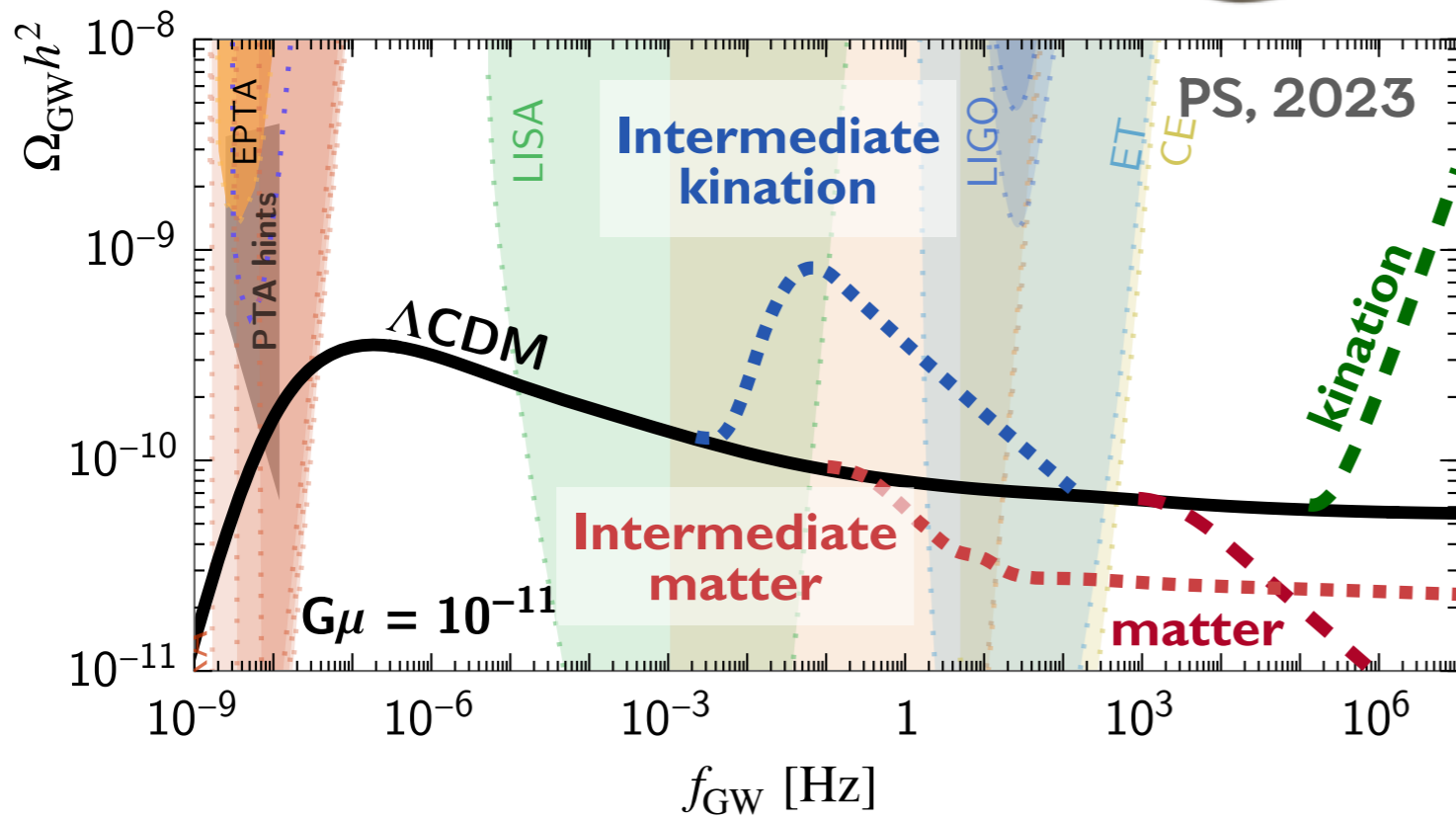
Ghoshal, Gouttenoire, Heurtier, PS, [2304.04793](#)

& Extra relativistic DOFs

Cui, Lewicki, Wells, [1808.08968](#),

Servant, PS, To appear

\Rightarrow (multi)-step signature



Other directions

PTA observations

GWB Interpretation

Many sources including scalar-induced GWB with non-Gaussianity.

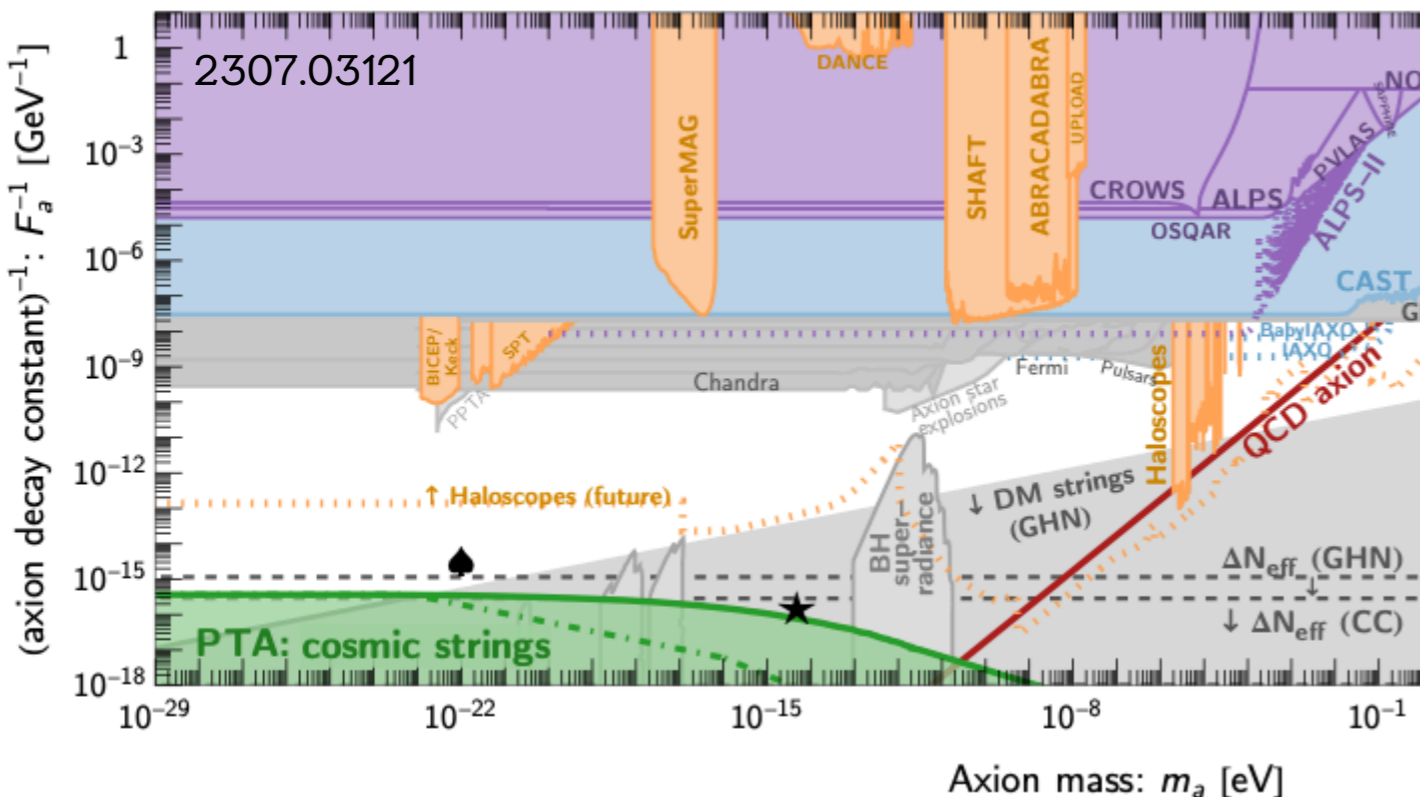
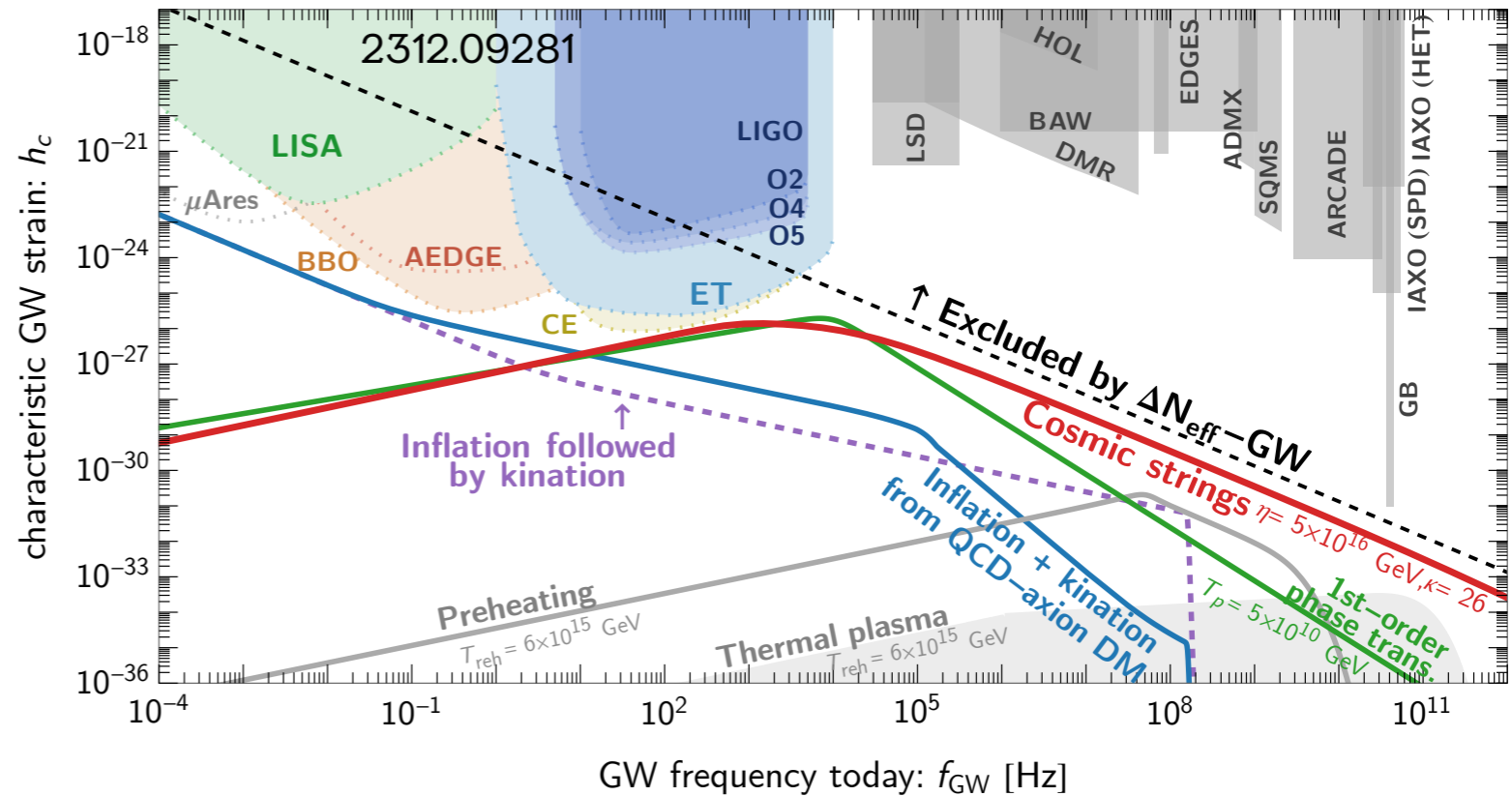
Figueroa, Pieroni, Ricciardone, PS
2307.02399

Constraints on postinflationary axion (from strings/domain-wall GWB)

Servant, PS 2307.03121

Ultra-high frequency (> kHz) GWB: the case of cosmic strings

Servant, PS
2312.09281



The signal from metastable local strings can be as high as ΔN_{eff} bound, allowing the scalar potential reconstruction.

Signals from global (axionic) strings are suppressed by heavy axions.

We really need UHF experiments that probe below ΔN_{eff} bound.

A Shameless Advertisement



Templates' Catalogue for cosmic-string GWB

Publicly available soon with *Simulation-based reconstruction of cosmic-string GWB*

Ongoing work [Figuerao, Dimitriou, PS, Zaldivar]

Faster inference!
Larger parameter-space exploration!

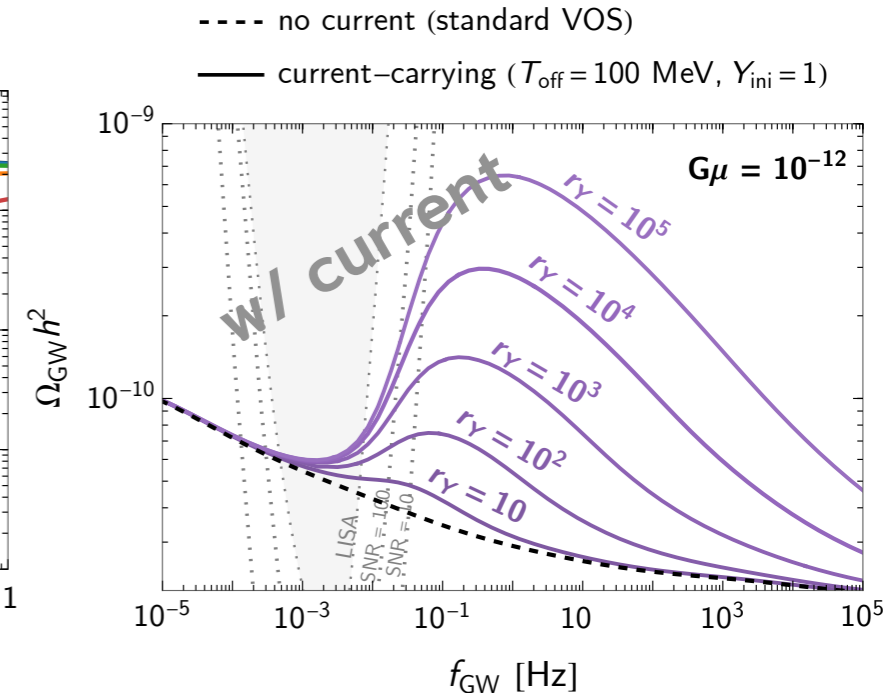
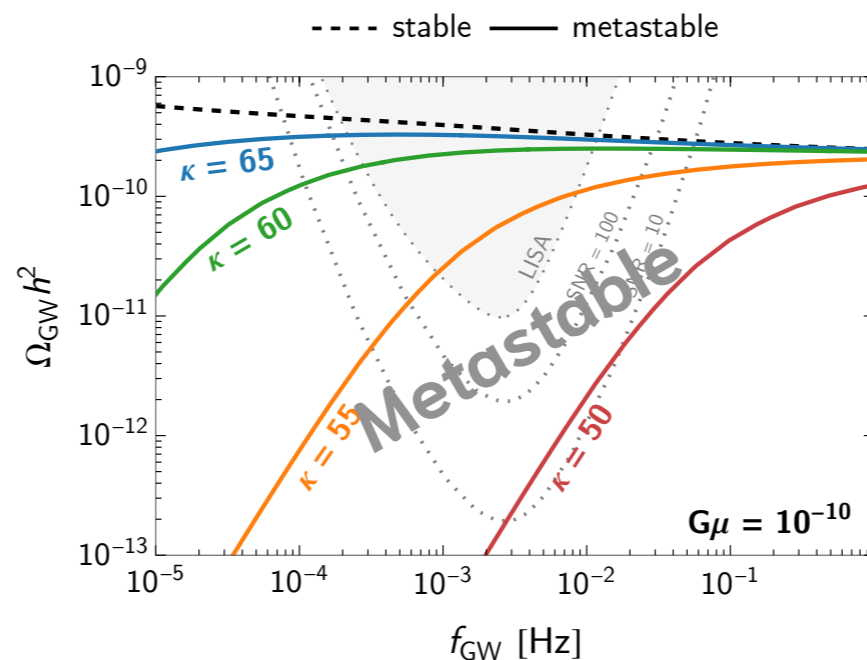
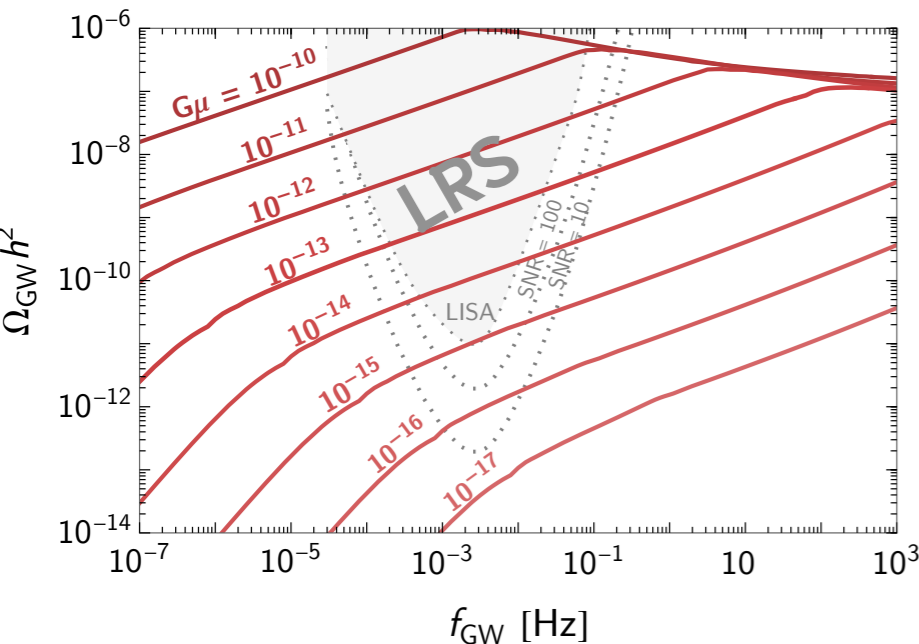
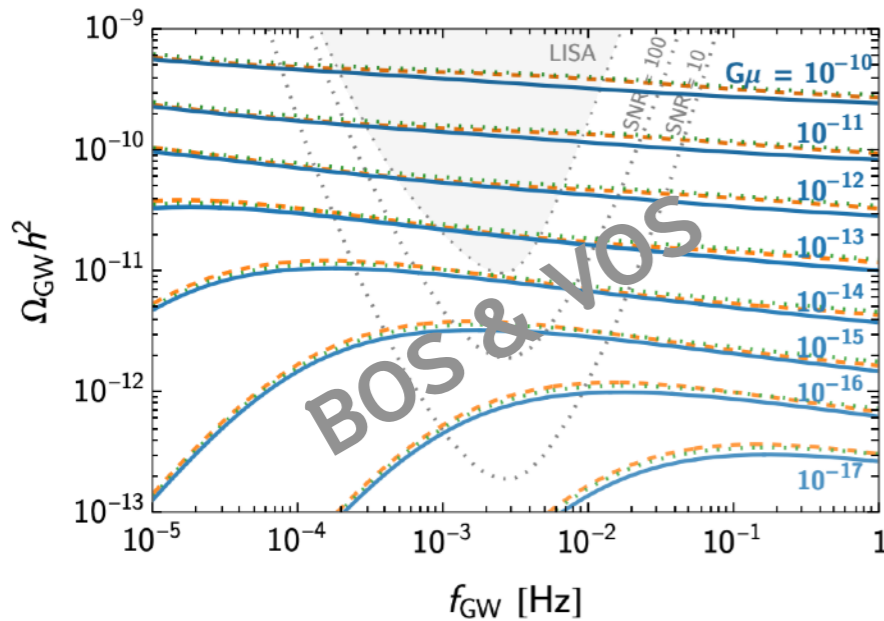
Extensive lists of models and non-standard scenarios.

Conventional

Semi-analytic (VOS)
Numerical (BOS & LRS)

Non-conventional

Non-standard GW emission (α, q),
Extra rela. DOFs., UV cutoffs, Non-ST cosmo
Metastable strings, Current-carrying strings

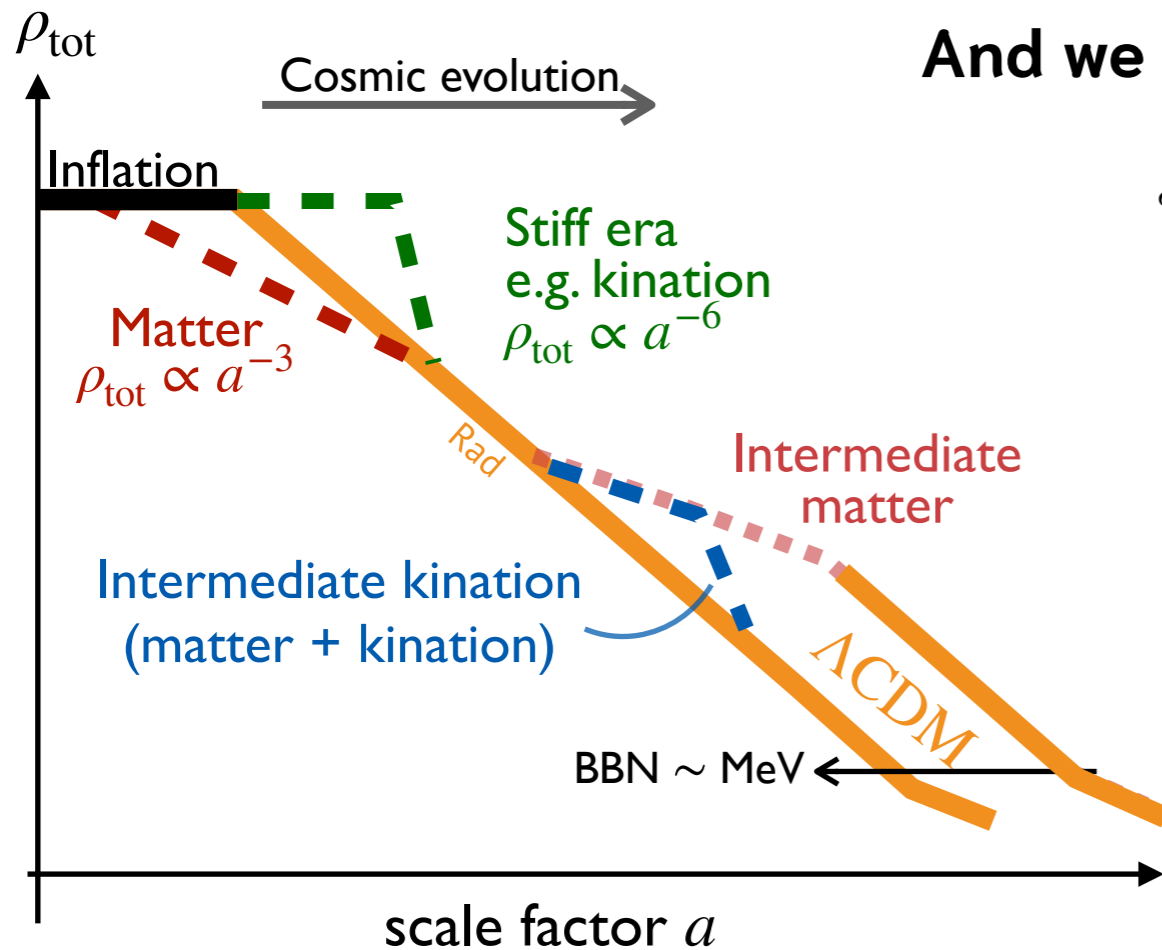


SUMMARY

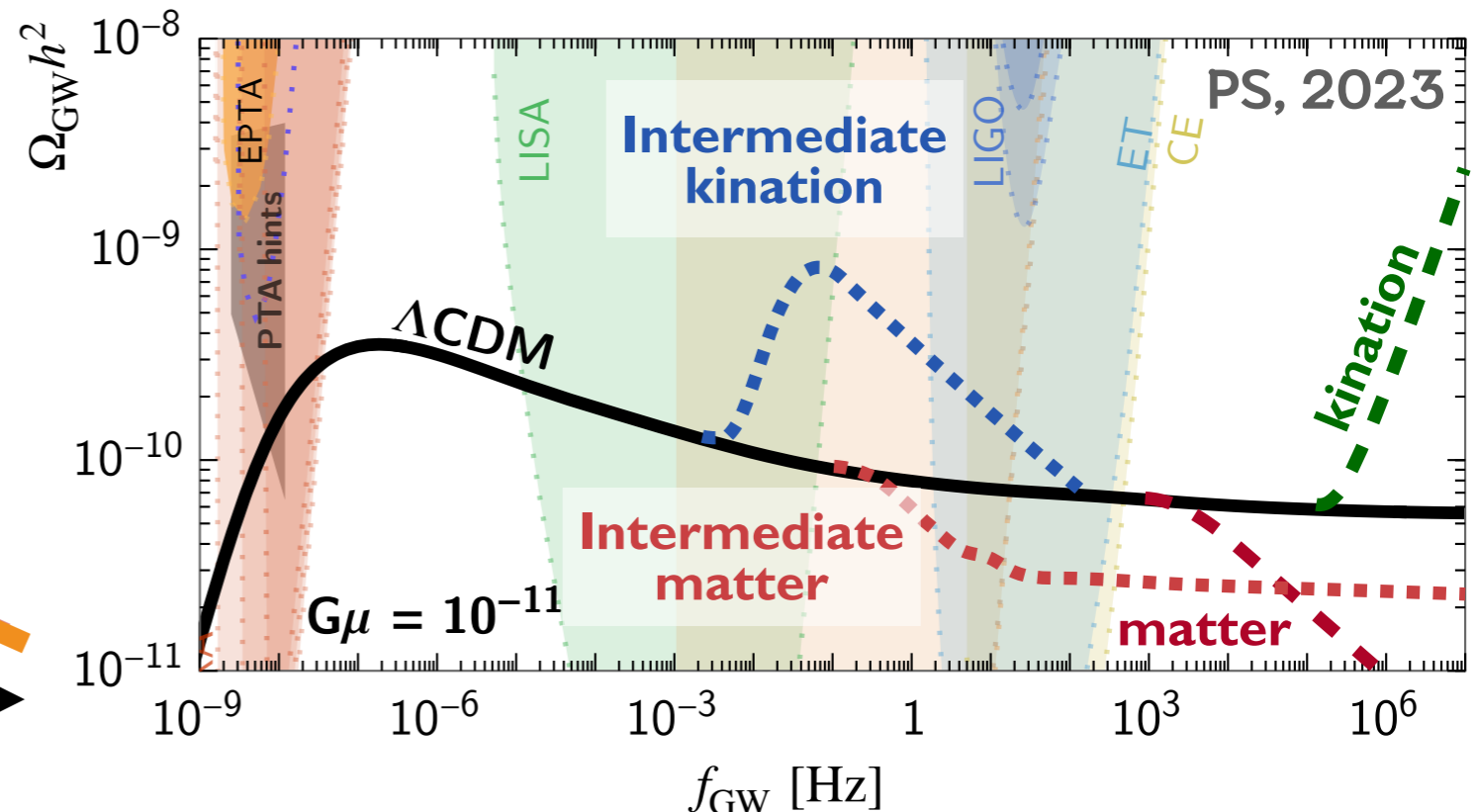
A new era for exploiting primordial GW as unique tools

for charting **the early-Universe cosmology** and **high-energy particle physics**.

- Physics beyond the SM induces **non-standard cosmological histories** (beyond the radiation era)
- Smoking-gun **spectral distortions** of primordial GW exist, detectable by future GW experiments.
(I.e., **matter era, extra DOFs** \Rightarrow **suppression**, **kination era** \Rightarrow **enhancement**)



And we need UHF experiments to probe primordial GWs.

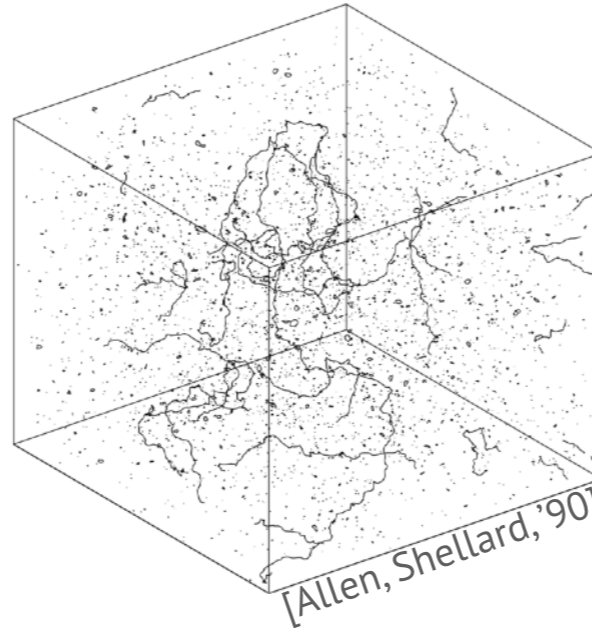


MORE STUFFS...

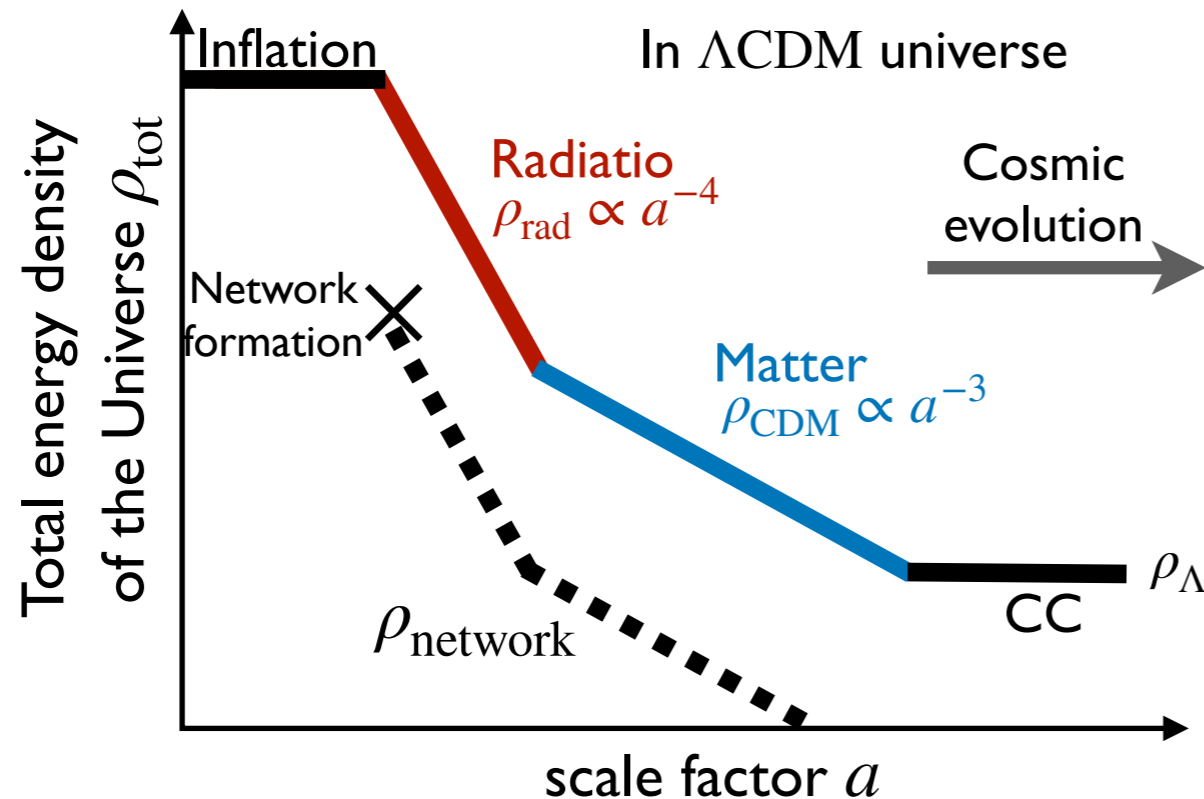
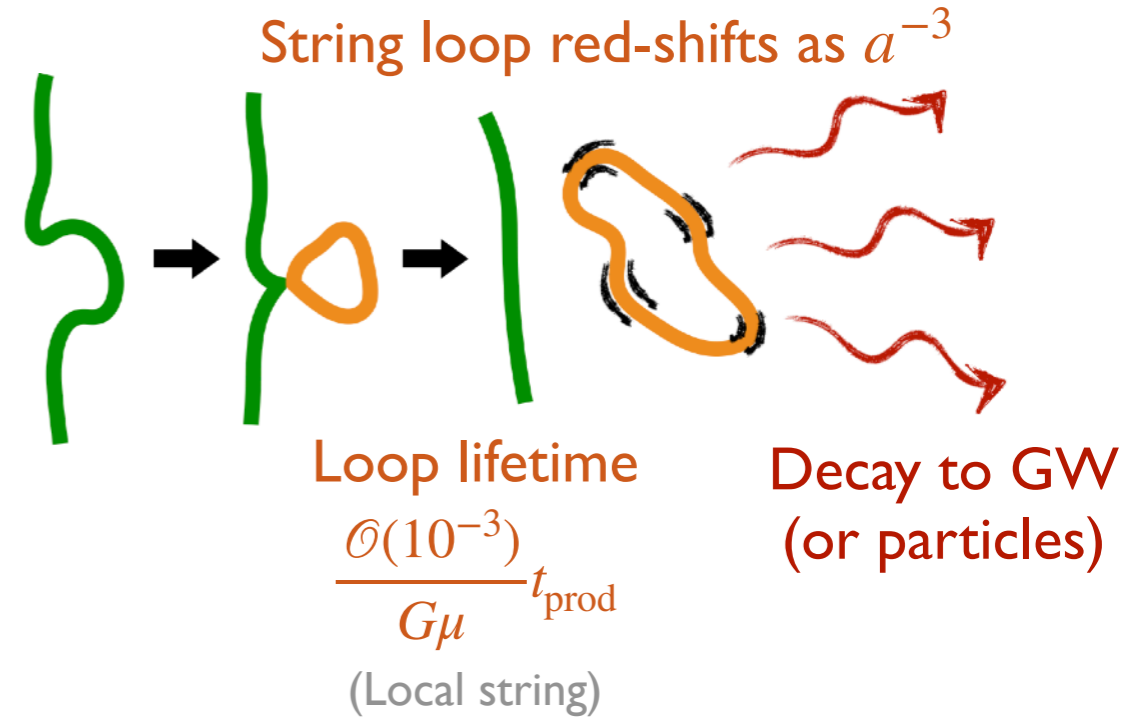
Cosmic Strings & their GW

Reviews e.g., [LISA Cosmo, I909.00819] and [Servant, Gouttenoire, PS, I912.02569]

A topological defect from spontaneous symmetry breaking at the energy scale η
[Kibble, '76]



String tension: $G\mu = \left(\frac{\eta}{m_{\text{Pl}}}\right)^2$



In the “scaling” regime:

$$\rho_{\text{network}} \simeq \mu/t^2 \sim G\mu\rho_{\text{tot}}$$

Total energy density of the universe

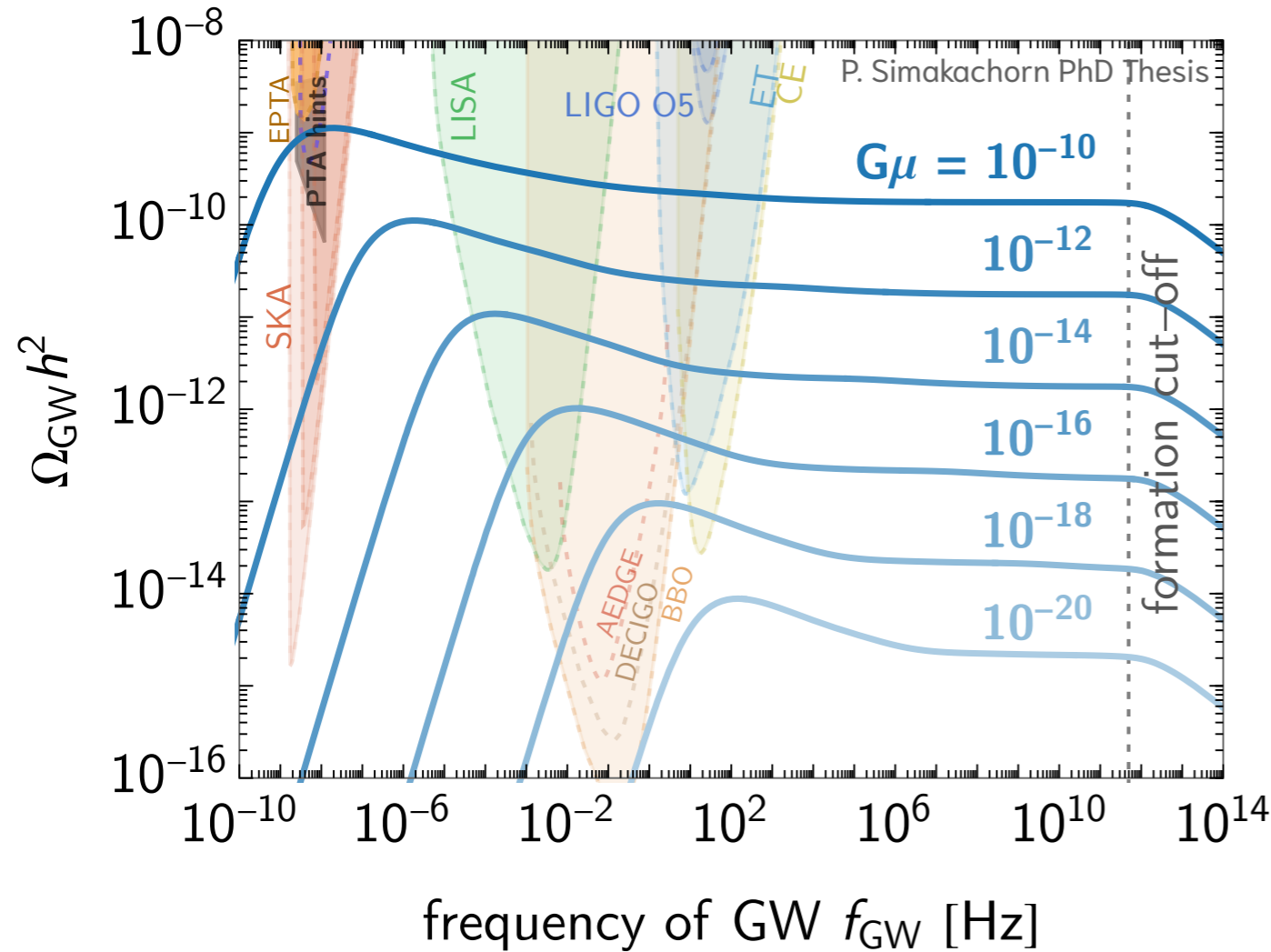
Local strings! and their GWB

Recent reviews, e.g., LISA cosmo [1909.00819], Gouttenoire, Servant, Simakachorn [1912.02569], Sousa '23

$$\Omega_{\text{GW}}(f_{\text{GW}}) = \frac{1}{\rho_{c,0}} \sum_{k=1}^{k_{\text{max}}} \frac{2k}{f_{\text{GW}}} \cdot \Gamma^{(k)} G\mu^2 \int_{t_{\text{form}}}^{t_0} n_{\text{loop}}(\tilde{t}) \left[\frac{a(\tilde{t})}{a(t_0)} \right]^5 d\tilde{t},$$

GW from a loop

of loops produced along cosmic history
(from production time until today)



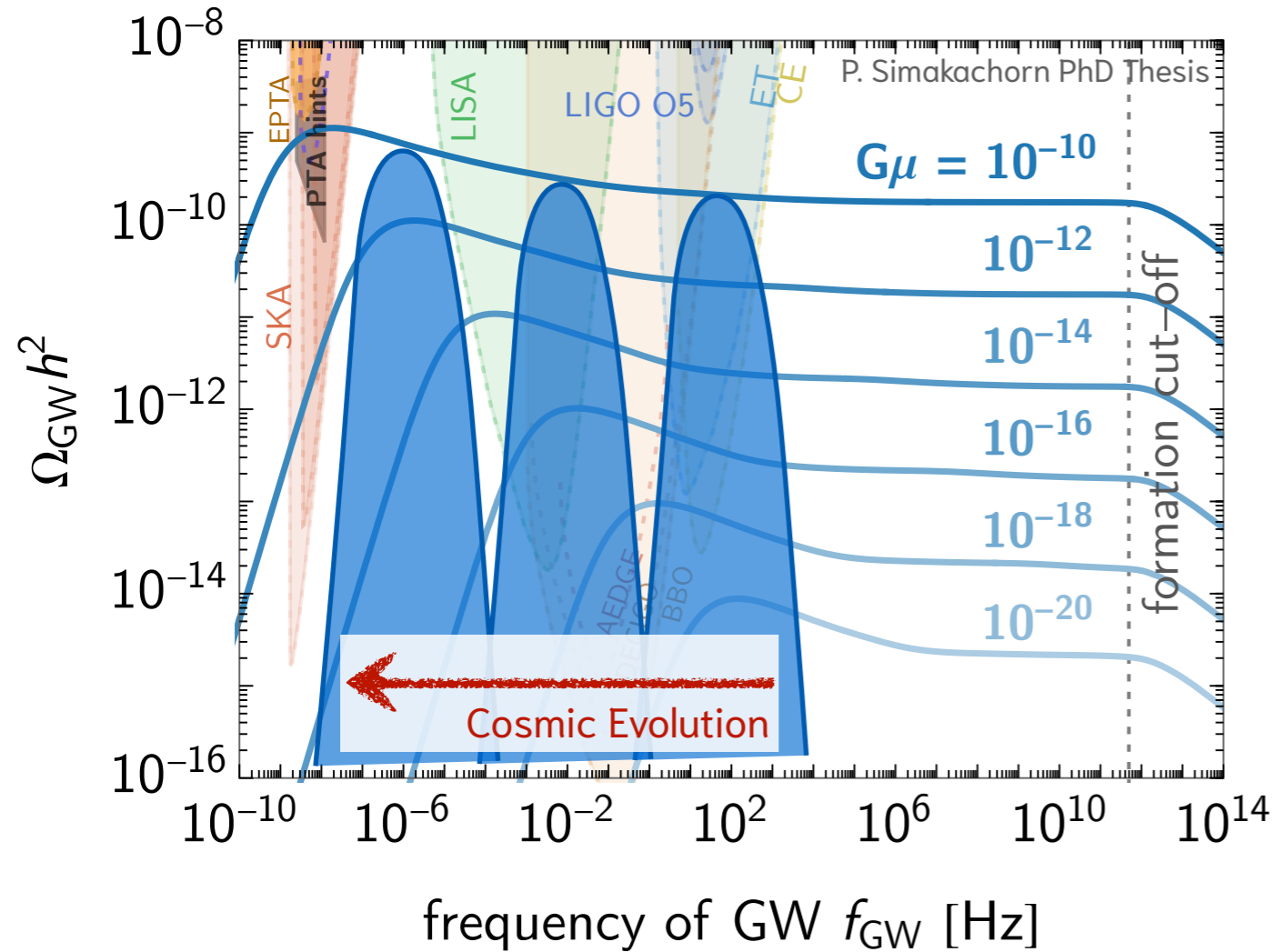
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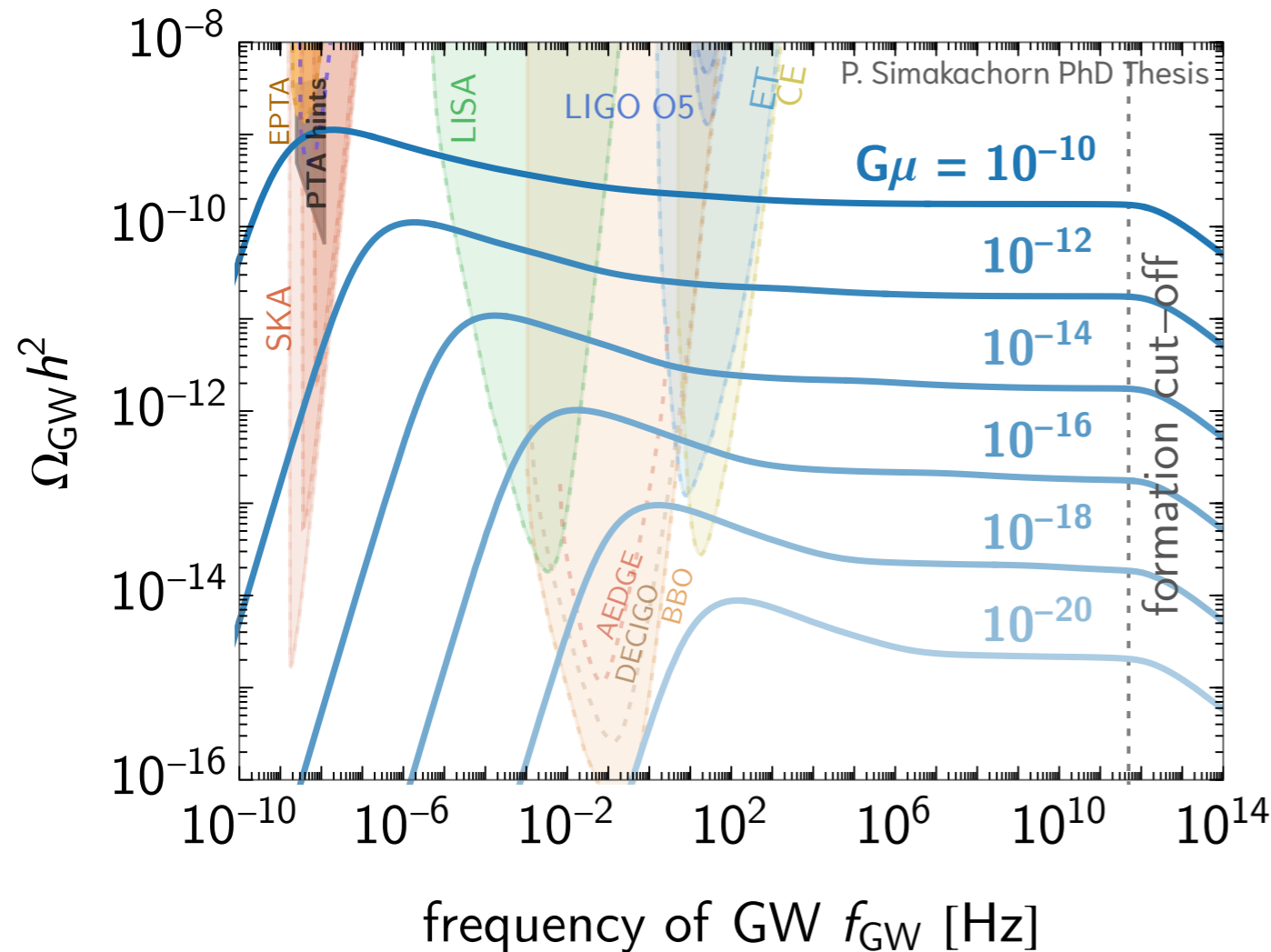
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Not so large UHF signals due to observations @ low-frequency.

LVK (LIGO-VIRGO-KAGRA) @ ~10 Hz

$$\Omega_{\text{GW}} h^2 \lesssim 10^{-8} \Rightarrow G\mu \lesssim 10^{-7}$$

PTA (pulsar-timing arrays) @ ~ nHz

$$\Omega_{\text{GW}} h^2 \lesssim 10^{-10} \Rightarrow G\mu \lesssim 10^{-10}$$

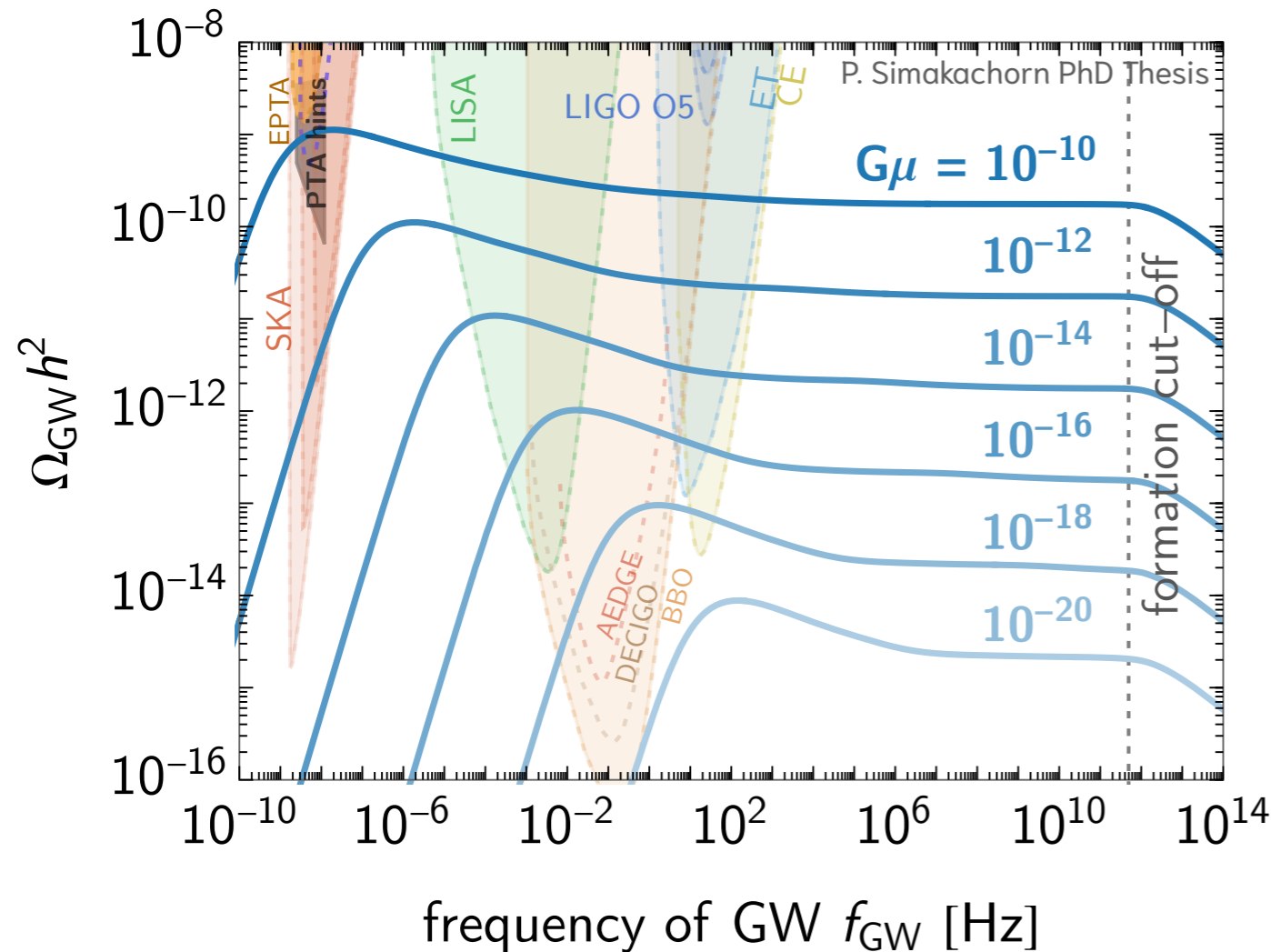
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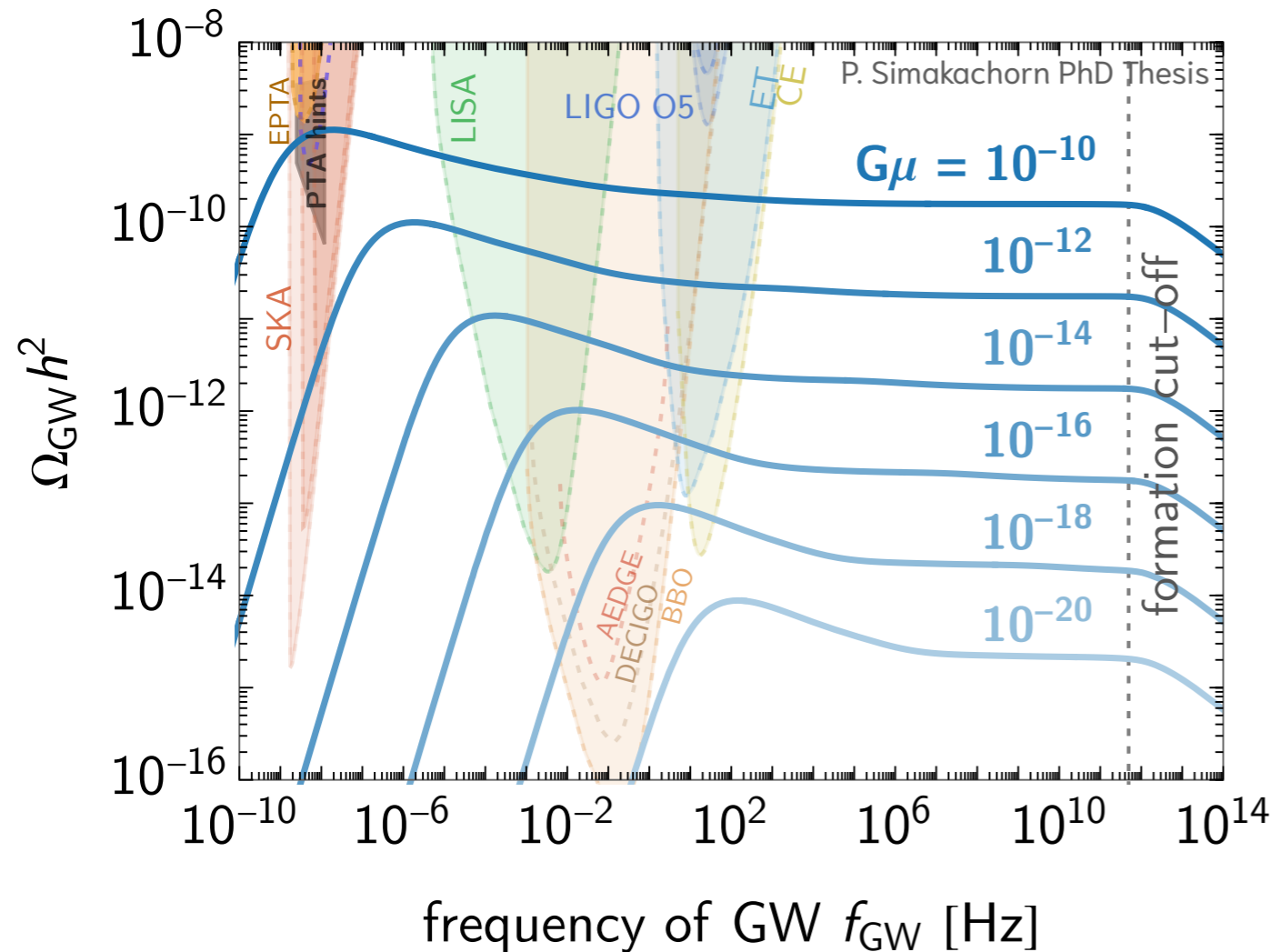
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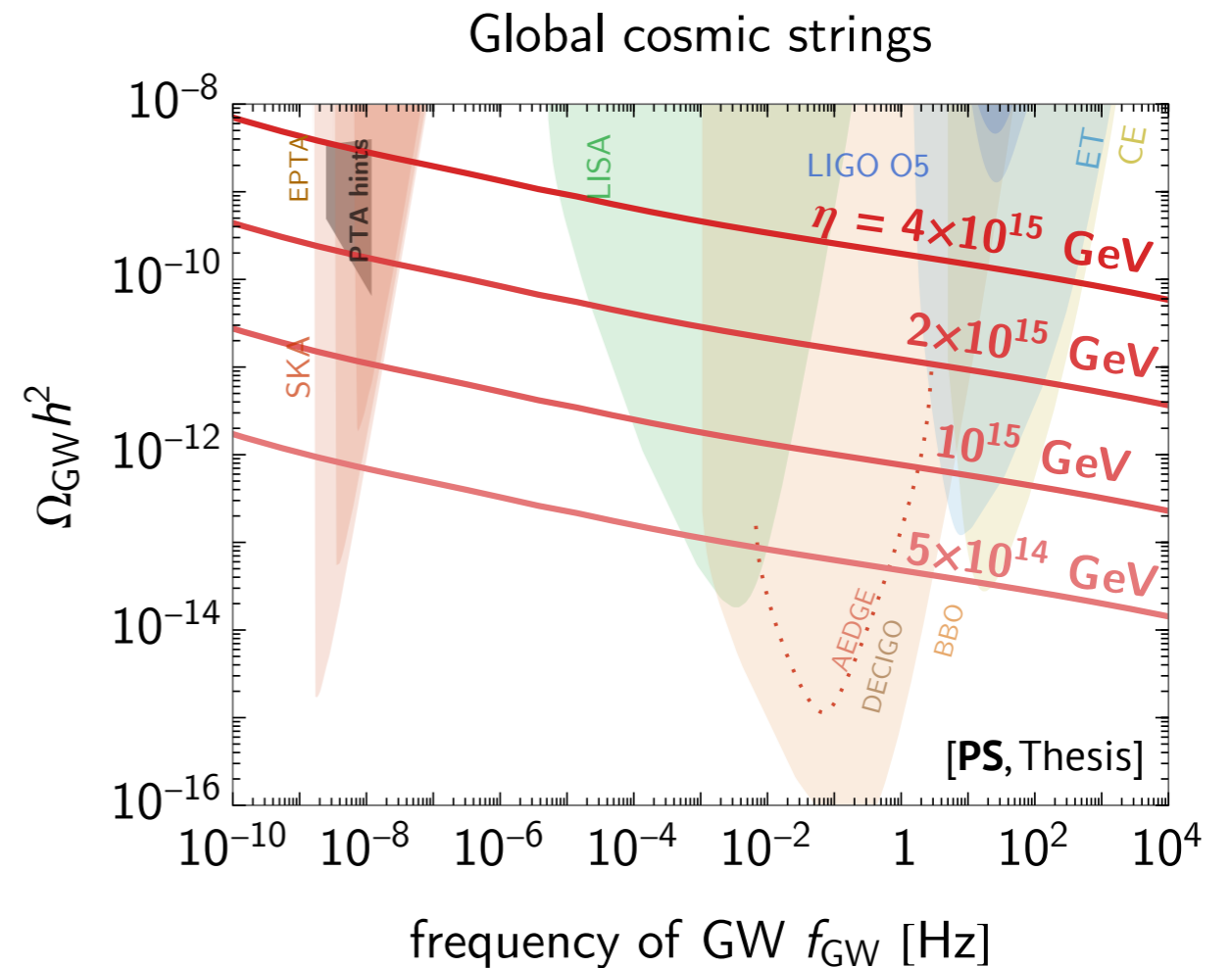
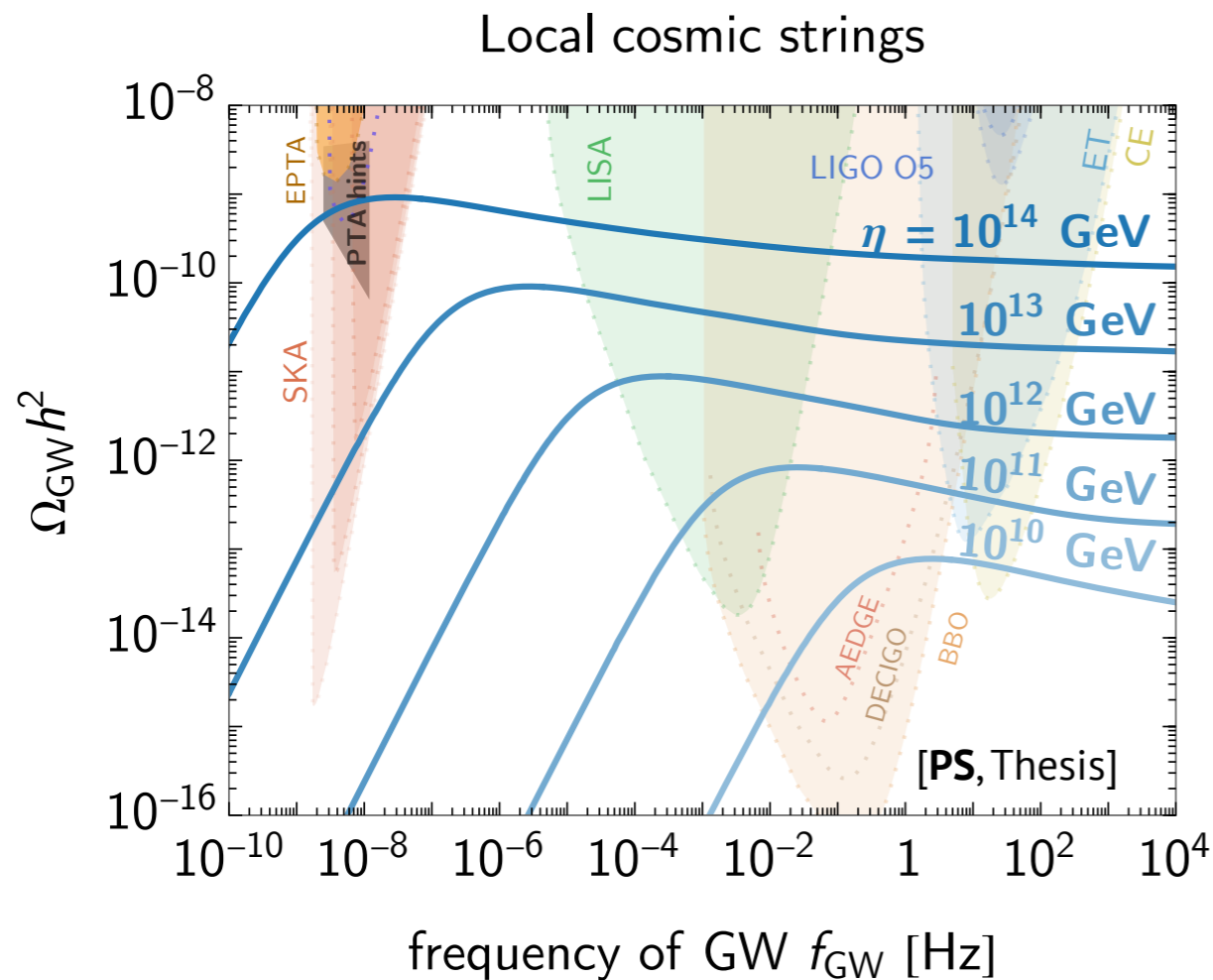
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These low-frequency constraints do not apply if strings shut down the GW production at later times.

String network decays!

GW from cosmic strings

generated from spontaneous symmetry breaking at an energy scale η



$$\Omega_{\text{GW}}^{\text{local}} \propto \sqrt{G\mu} \propto \eta$$

$$\Omega_{\text{GW}}^{\text{global}} \propto \eta^4$$

$$f_{\text{GW}}(T) \simeq \begin{cases} (2 \times 10^{-3} \text{ Hz}) \left(\frac{0.1 \times 50 \times 10^{-11}}{\alpha \times \Gamma G\mu} \right)^{1/2} \left(\frac{T}{\text{GeV}} \right) \left[\frac{g_*(T)}{g_*(T_0)} \right]^{1/4} & \text{(local strings),} \\ (4.7 \times 10^{-6} \text{ Hz}) \left(\frac{0.1}{\alpha} \right) \left(\frac{T}{\text{GeV}} \right) \left[\frac{g_*(T)}{g_*(T_0)} \right]^{1/4} & \text{(global strings),} \end{cases}$$

Temperature of the Universe

The scale-invariant local-string GWB during radiation-domination (simple argument)

Fraction of energy density
in GW today

$$\Omega_{\text{GW},0} = \left(\frac{\rho_{\text{GW,prod}}}{\rho_{\text{tot},0}} \right) \left(\frac{a_{\text{prod}}}{a_0} \right)^4 = \left(\frac{\rho_{\text{GW,prod}}}{\rho_{\text{tot,prod}}} \right) \left(\frac{\rho_{\text{tot,prod}}}{\rho_{\text{tot},0}} \right) \left(\frac{a_{\text{prod}}}{a_0} \right)^4$$

constant

Long-lasting

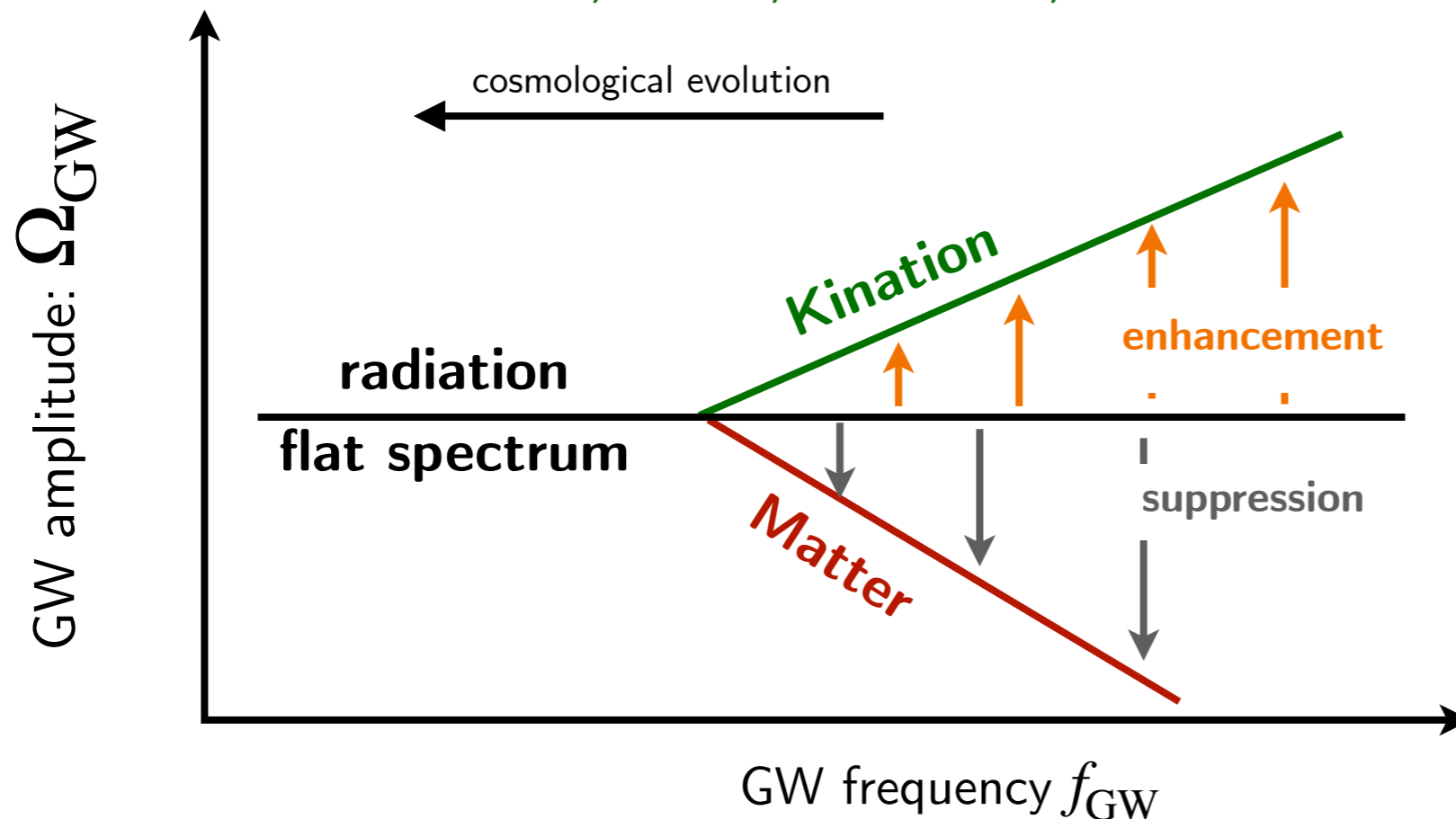
Inflationary GW

(scale-invariant) tensor perturbation: $\Delta_h^2 \simeq (H/M_{\text{Pl}})^2$
 $(\rho_{\text{GW}}/\rho_{\text{tot}})_{\text{prod}} = \text{constant}$

Cosmic-string GW:

$\rho_{\text{GW}} \propto \rho_{\text{string-network}} \propto \rho_{\text{tot}}$
 in the so-called “scaling regime”

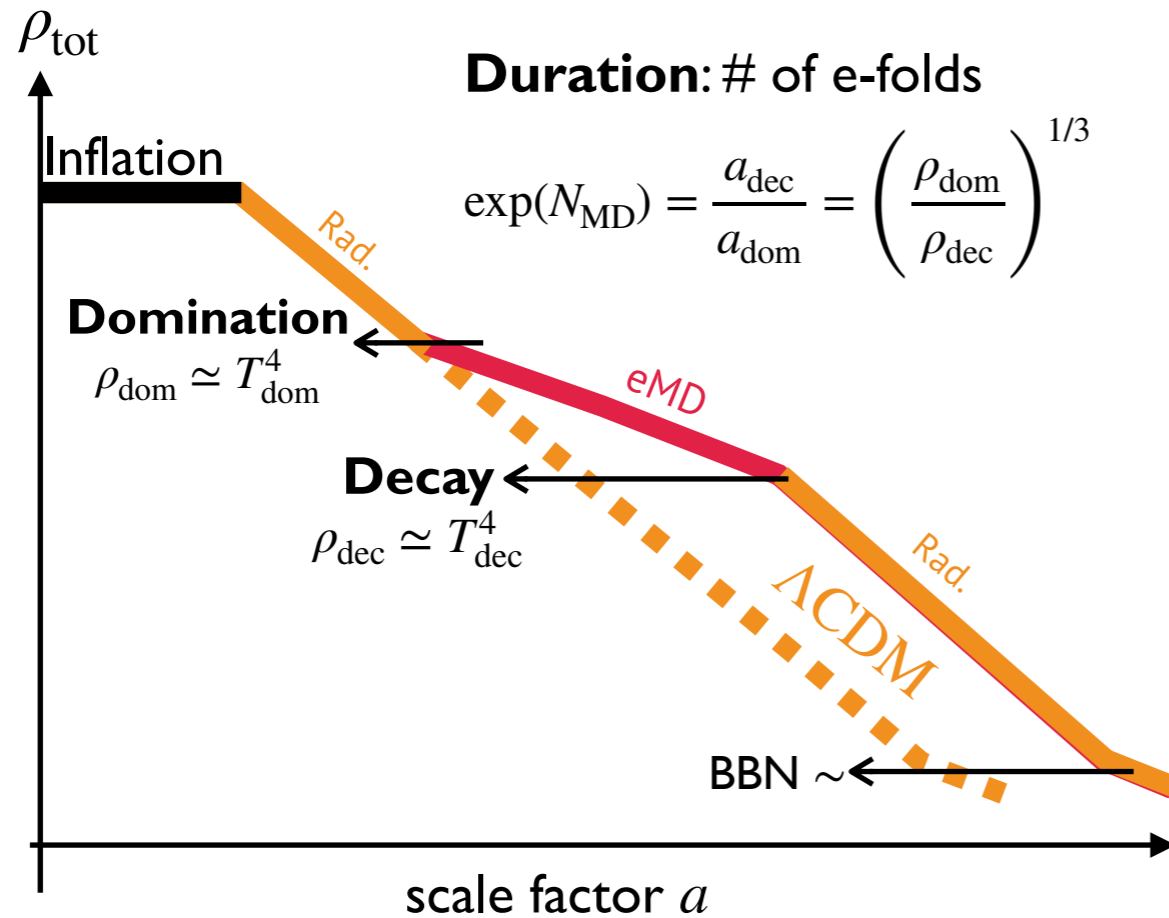
Gouttenoire, Servant, Simakachorn, 2111.01150



$$\rho_{\text{tot}} \propto \begin{cases} a^{-3} & \text{for matter era,} \\ a^{-4} & \text{for radiation era,} \\ a^{-6} & \text{for kination era} \end{cases}$$

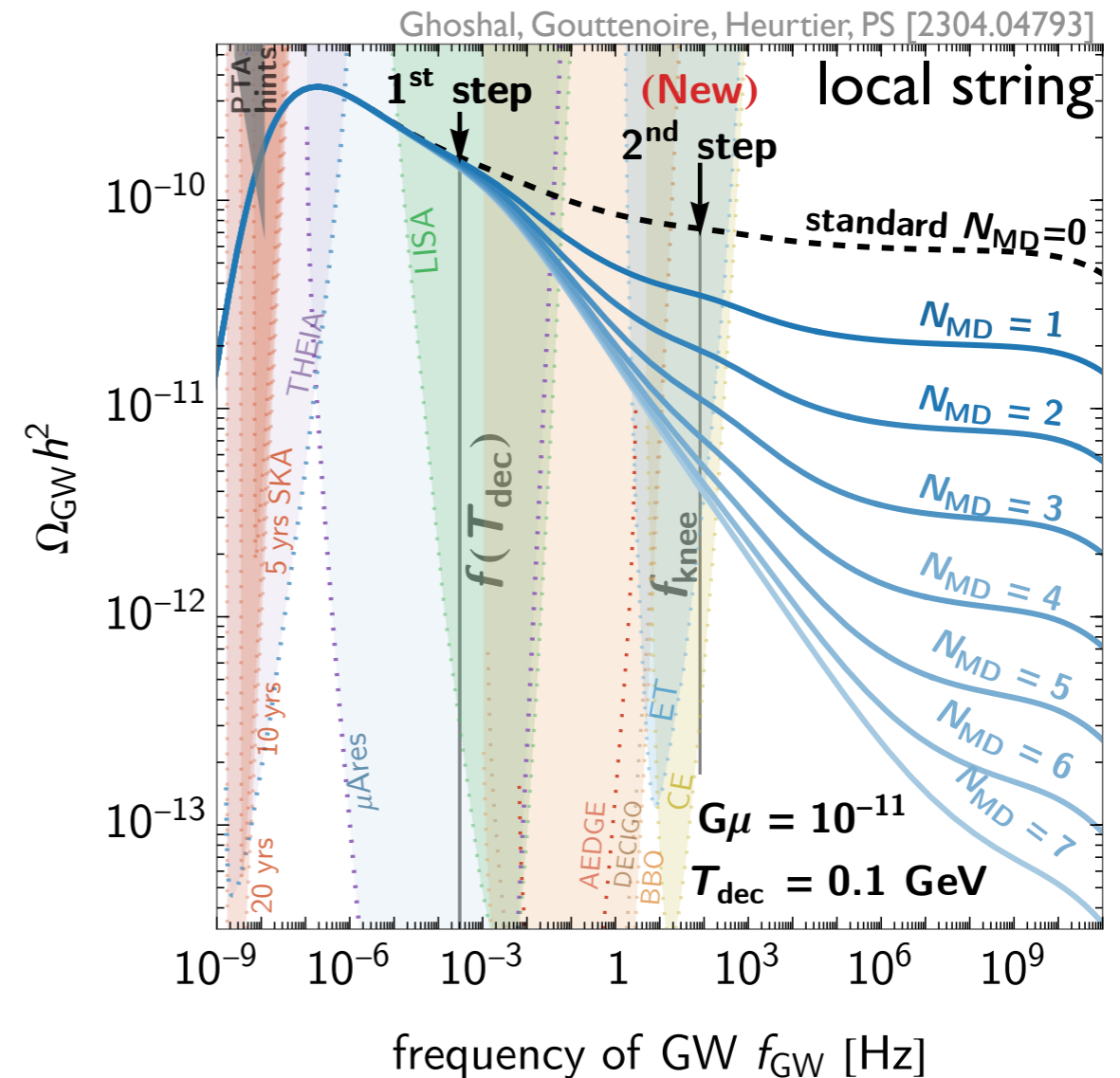
Intermediate early matter-domination era (eMD)

dominates at temp. T_{dom} , later decays and reheats the radiation to T_{dec} .



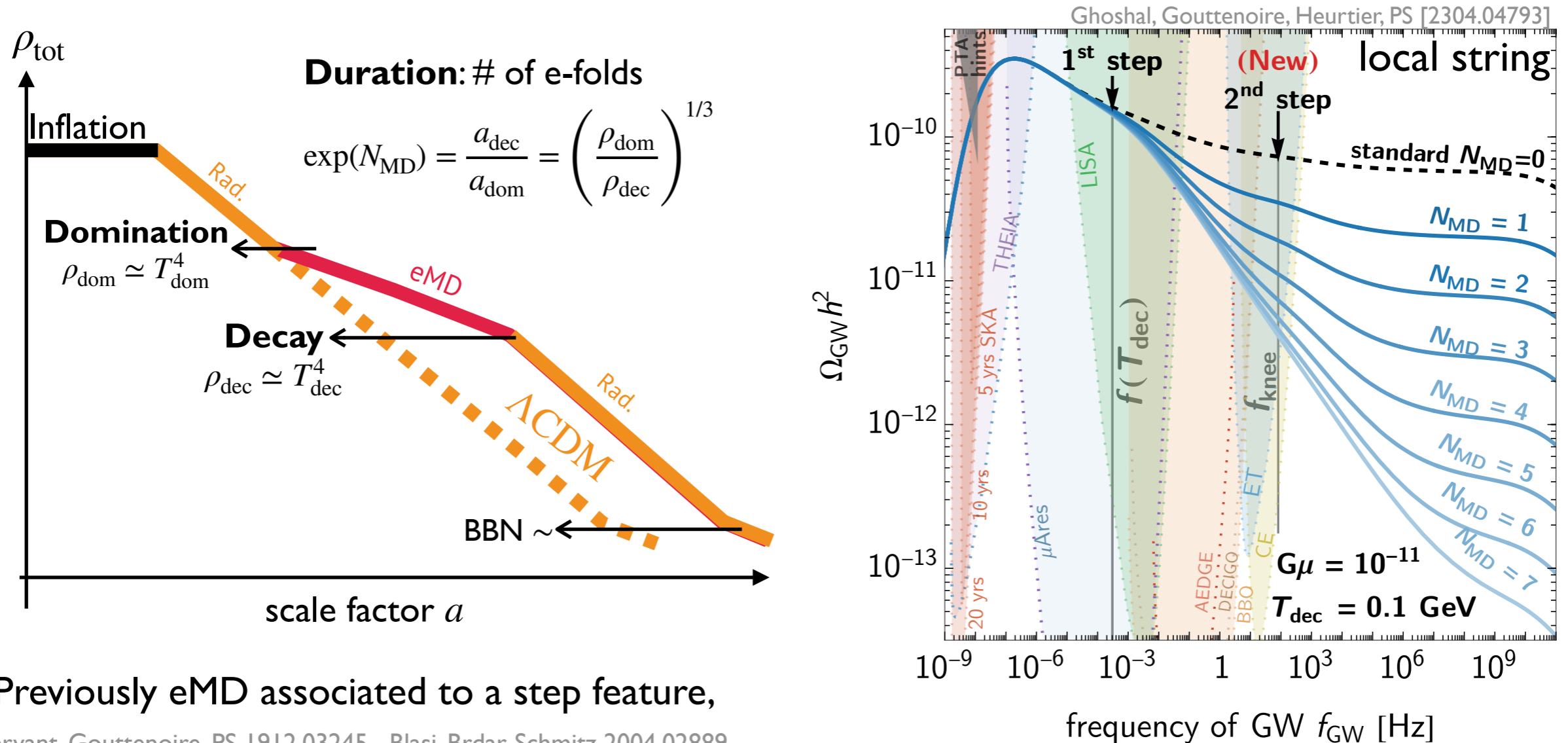
Previously eMD associated to a step feature,

Servant, Gouttenoire, PS 1912.03245 Blasi, Brdar, Schmitz 2004.02889



Intermediate early matter-domination era (eMD)

dominates at temp. T_{dom} , later decays and reheats the radiation to T_{dec} .



Recently, eMD \Rightarrow “double-step” with a “knee”

associated with loop populations “produced before” and “decay after” eMD.

I.e., $\rho_{\text{loop}} \propto a^{-3}$ and $\rho_{\text{loop}}/\rho_{\text{tot}}$ does not dilute during eMD, unlike loops decaying before eMD.

Ghoshal, Gouttenoire, Heurtier, PS 2304.04793

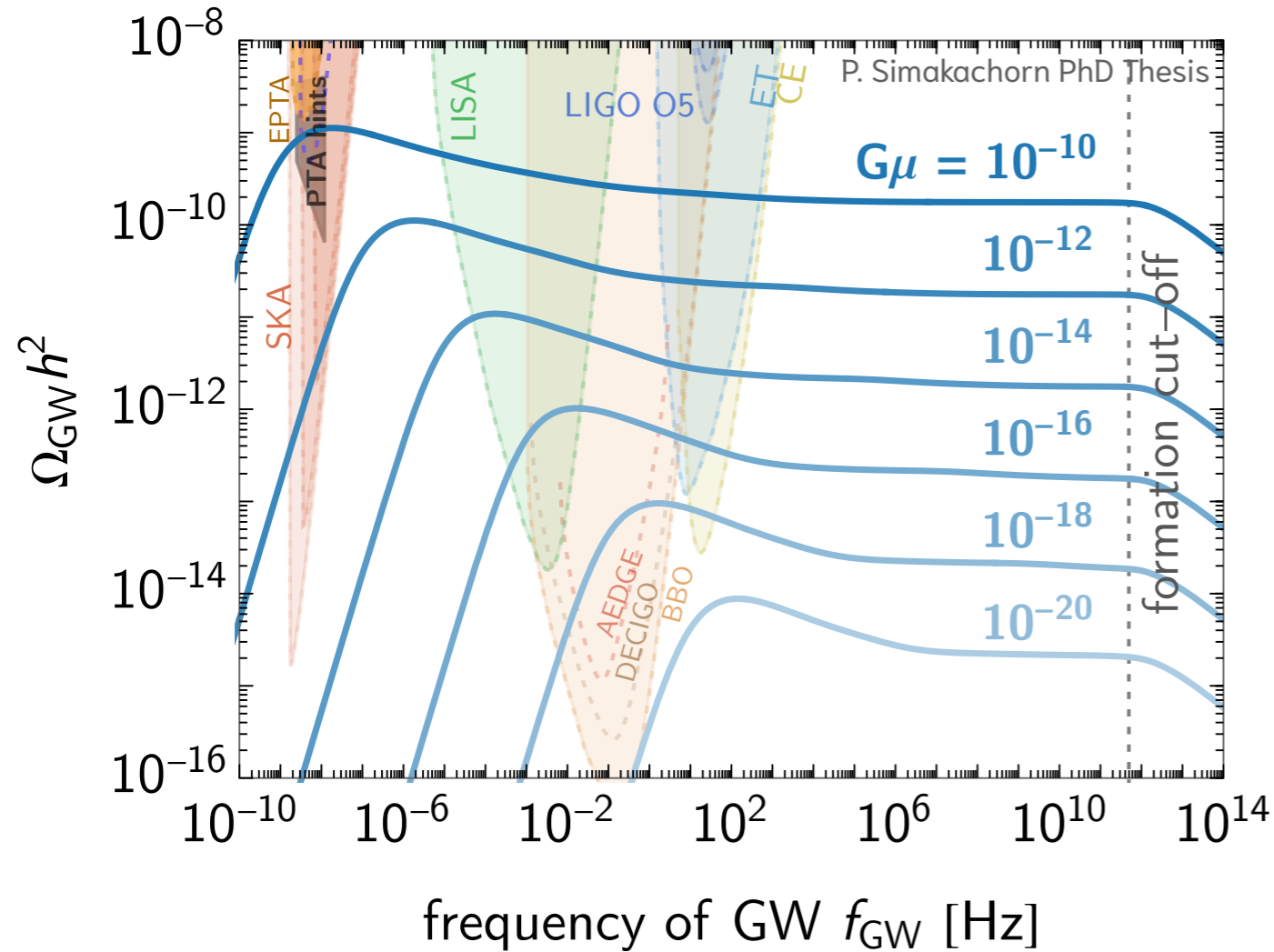
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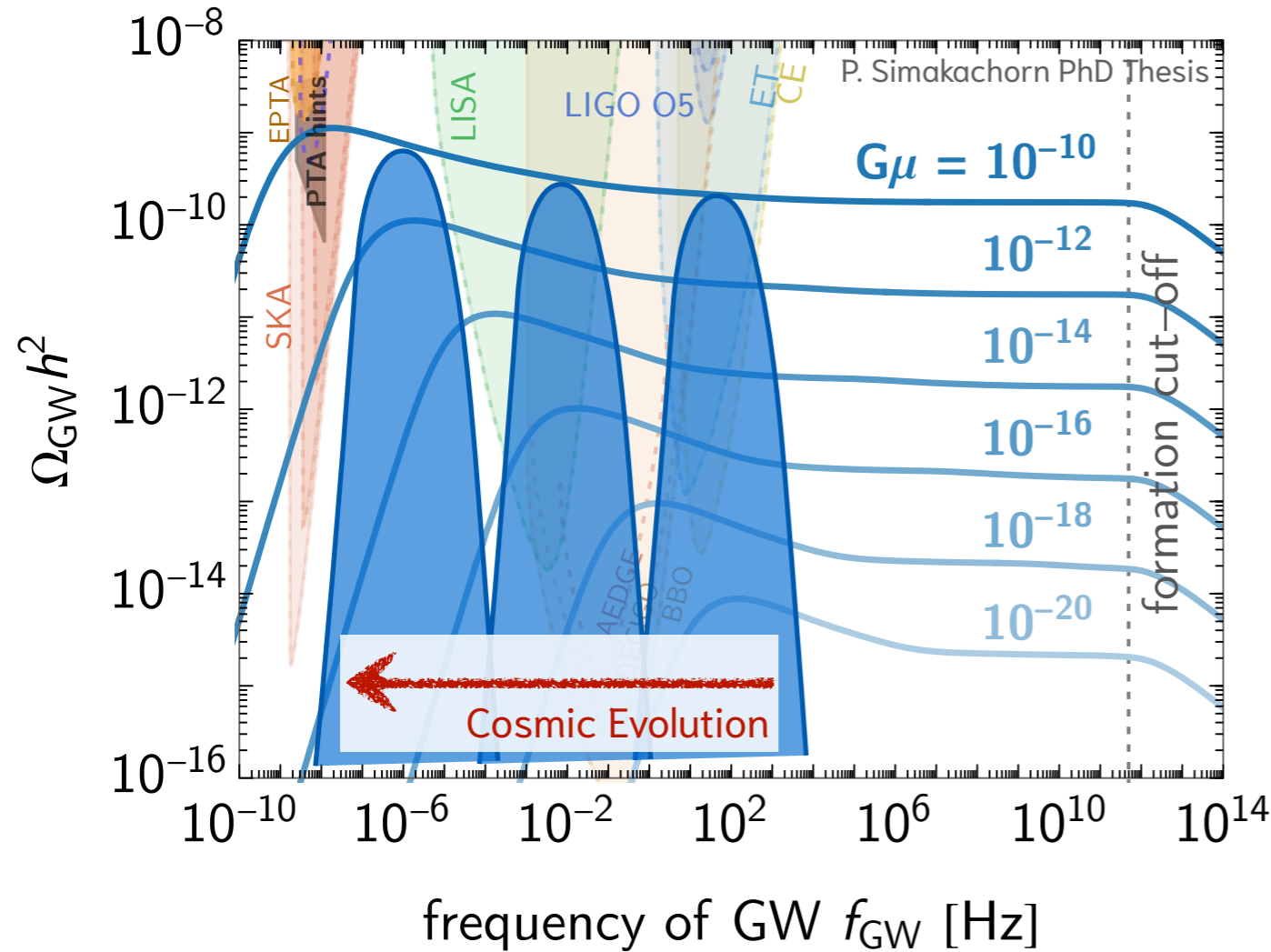
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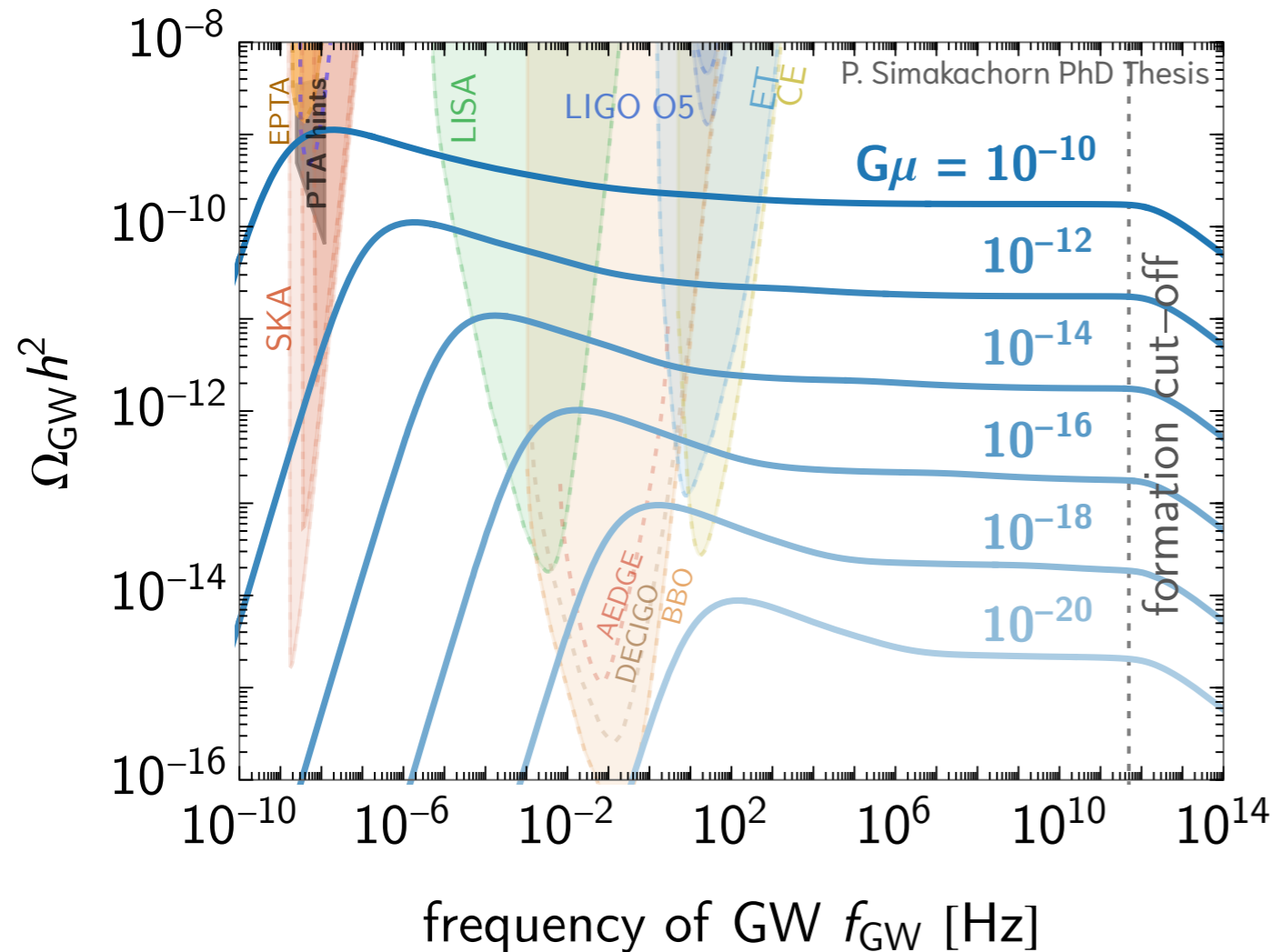
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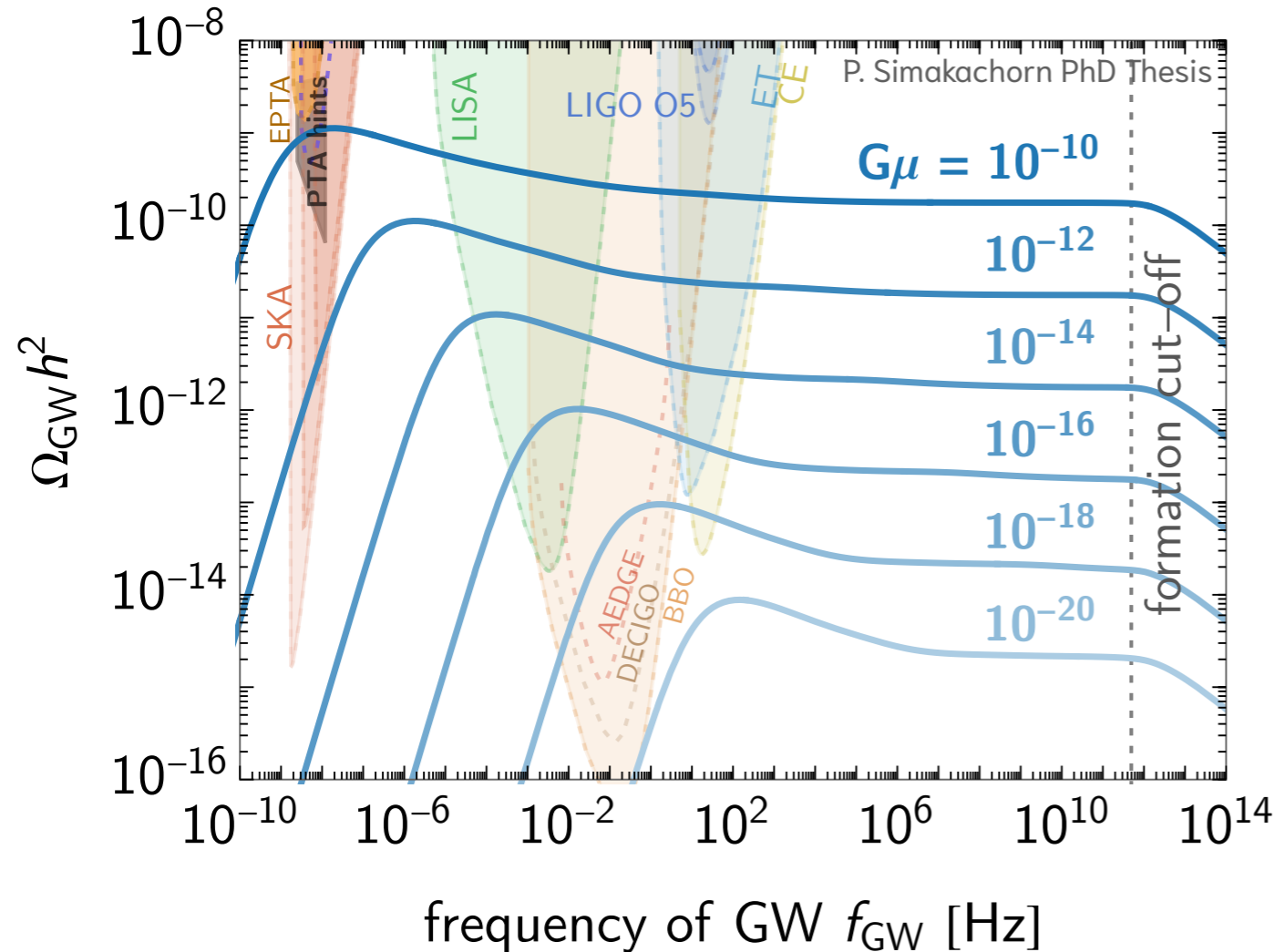
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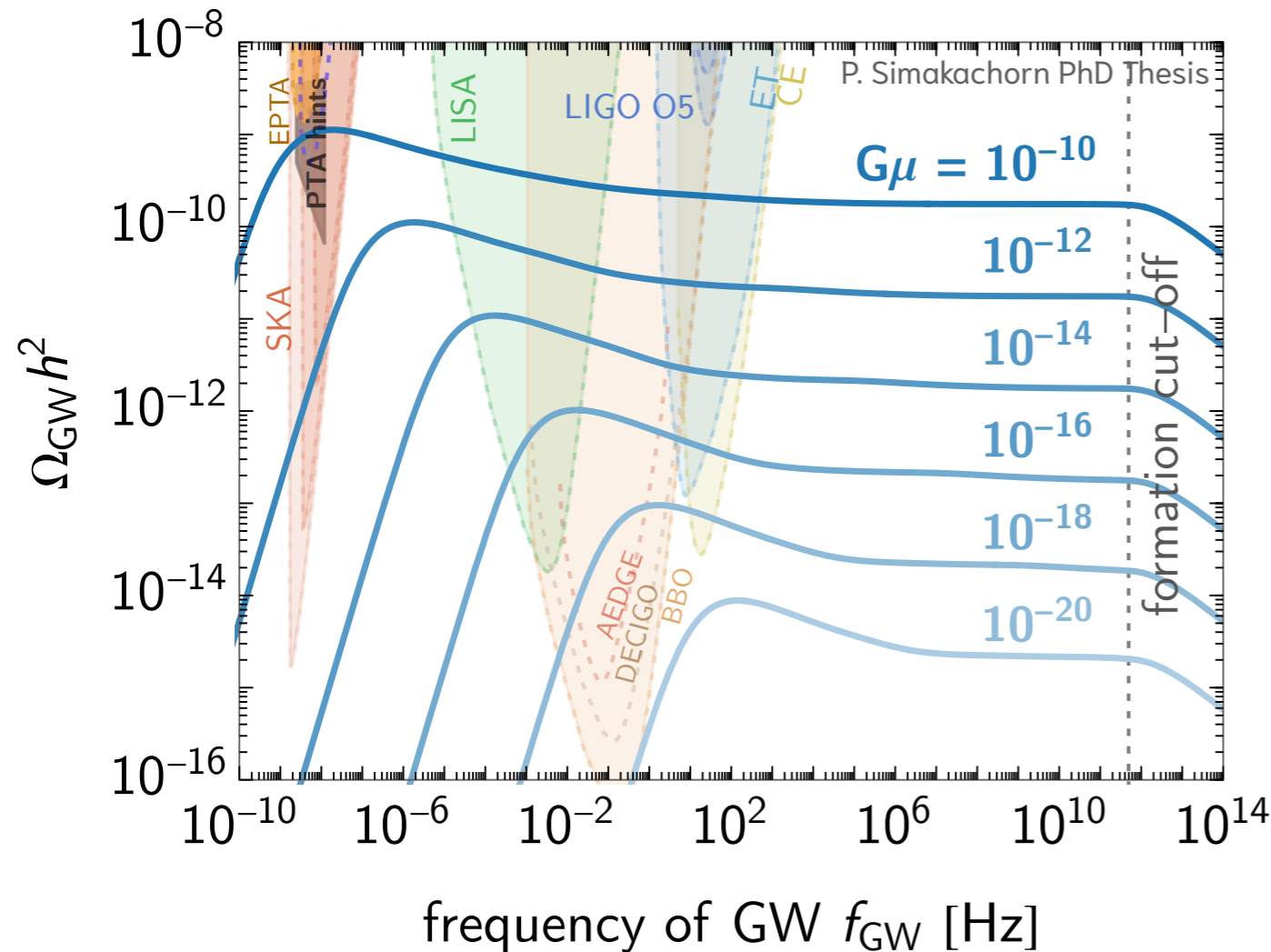
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Not so large UHF signals due to observations @ low-frequency.

LVK (LIGO-VIRGO-KAGRA) @ ~10 Hz

$$\Omega_{\text{GW}} h^2 \lesssim 10^{-8} \Rightarrow G\mu \lesssim 10^{-7}$$

PTA (pulsar-timing arrays) @ ~ nHz

$$\Omega_{\text{GW}} h^2 \lesssim 10^{-10} \Rightarrow G\mu \lesssim 10^{-10}$$

These low-frequency constraints do not apply if strings shut down the GW production at later times.

String network decays!

Reconstruction of the scalar potential via GW

Servant, Simakachorn [2312.09281]

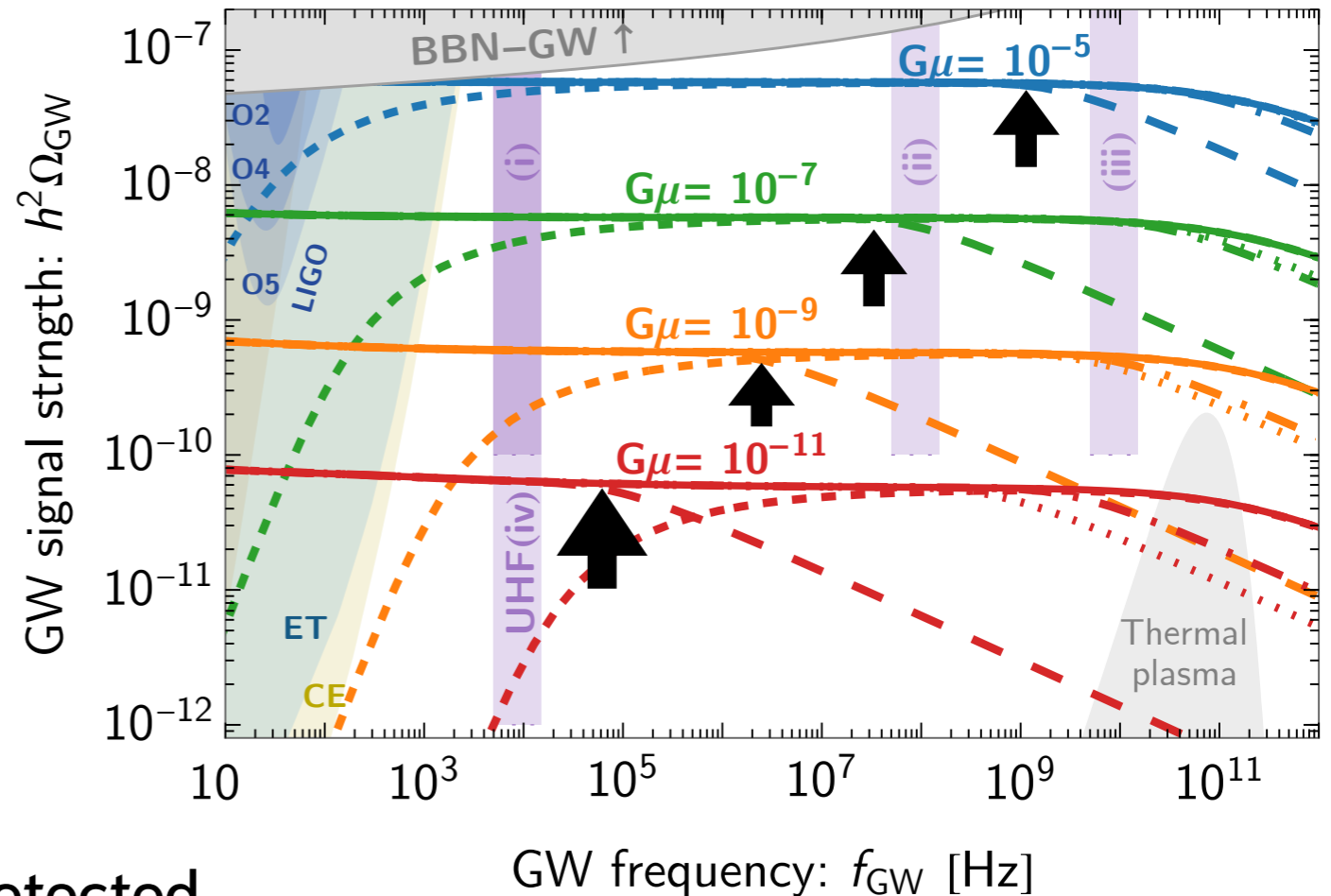
UV cutoff in the GW spectrum
e.g., from cusp,
moves with the string's fatness

$$w \simeq m_{\Phi}^{-1} \simeq (\sqrt{\lambda}\eta)^{-1}$$

$$f_{\text{GW}}^{\text{cusp}} \simeq \text{GHz} \lambda^{1/8} \left(\frac{G\mu}{10^{-5}} \right)^{3/4}$$



$$V(\Phi) \simeq \lambda(|\Phi|^2 - \eta^2)^2$$



How to extract the UV cutoff if GWB is detected.

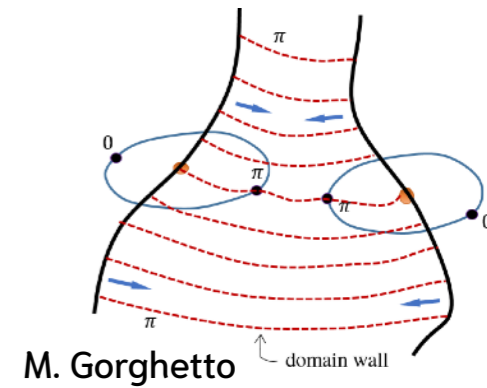
- Detect directly the cutoff (need some luck)
- Several detectors at different frequencies.
Detect the flat part and the UV slope, \Rightarrow UV cutoff at the intersection (more generic)

Axionic (or global) strings

$$\Omega_{\text{GW}} \propto \eta^4 \text{ or } f_a^4 \quad \text{with } f_a: \text{Peccei-Quinn symmetry-breaking scale}$$

Strings attach to domain walls and collapse: $T_{\text{dec}} \sim 10^9 \text{ GeV} \sqrt{m_a / \text{GeV}}$

String-domain wall



Light axion ($m_a \lesssim 10^{-22} \text{ eV}$)

\Rightarrow \sim stable strings

Small UHF signal

- ΔN_{eff} -Goldstone bound

$$f_a \lesssim \mathcal{O}(1 - 3) \times 10^{15} \text{ GeV}$$

Cui, Chang '21, Hardy, Nicoleuscu, Gorghetto '21

- Pulsar-timing arrays

$$f_a \lesssim 2.8 \times 10^{15} \text{ GeV}$$

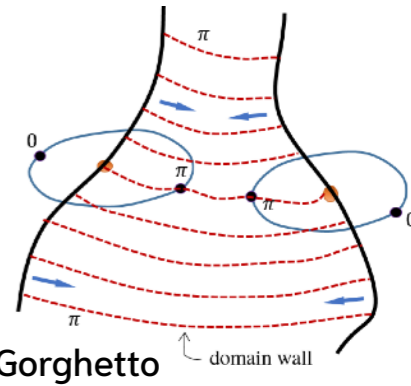
Servant, Simakachorn [2307.03121]

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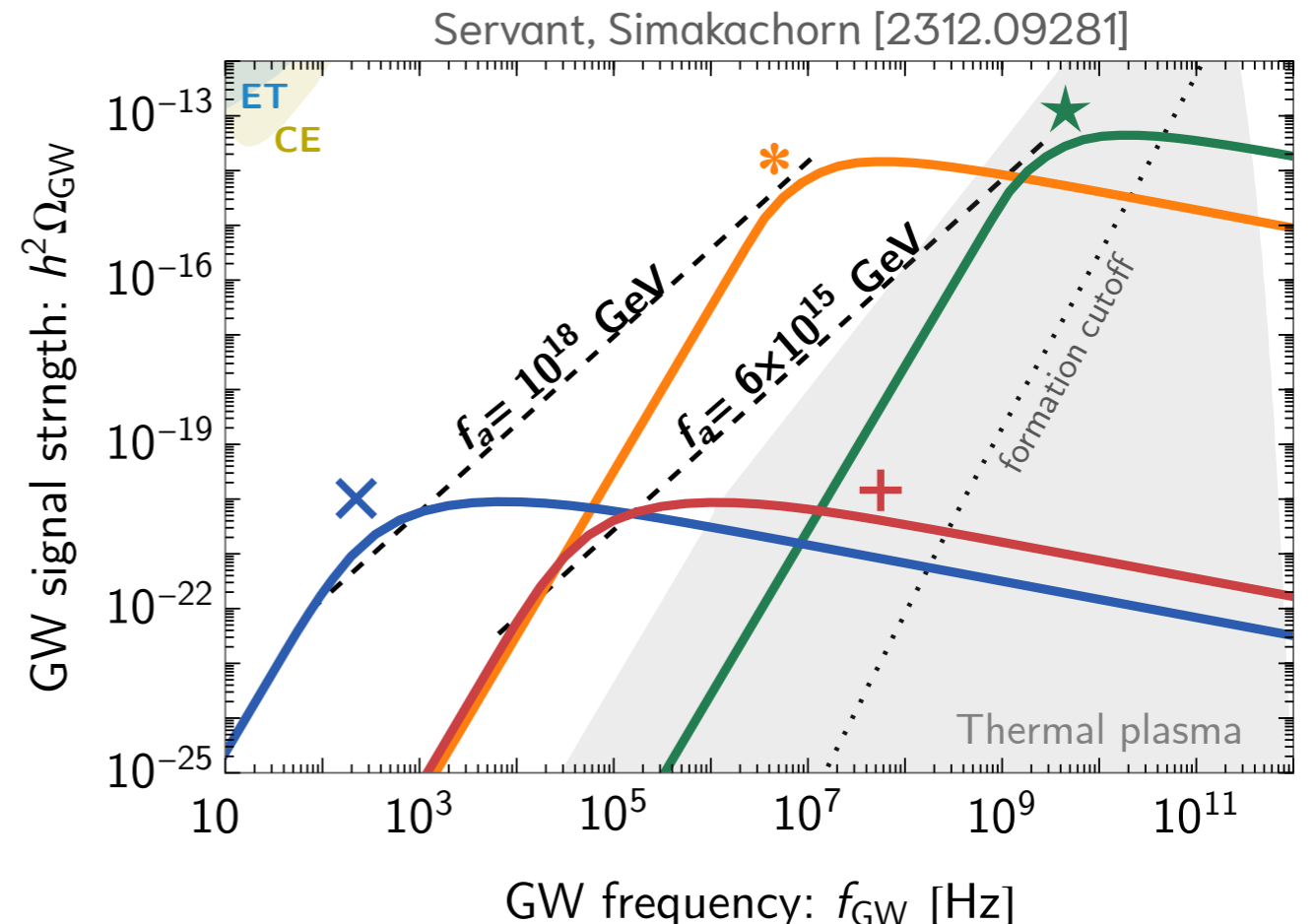
Servant, Simakachorn [2307.03121]

Heavy axion ($m_a \gtrsim \text{GeV}$)

\Rightarrow IR cutoff in UHF

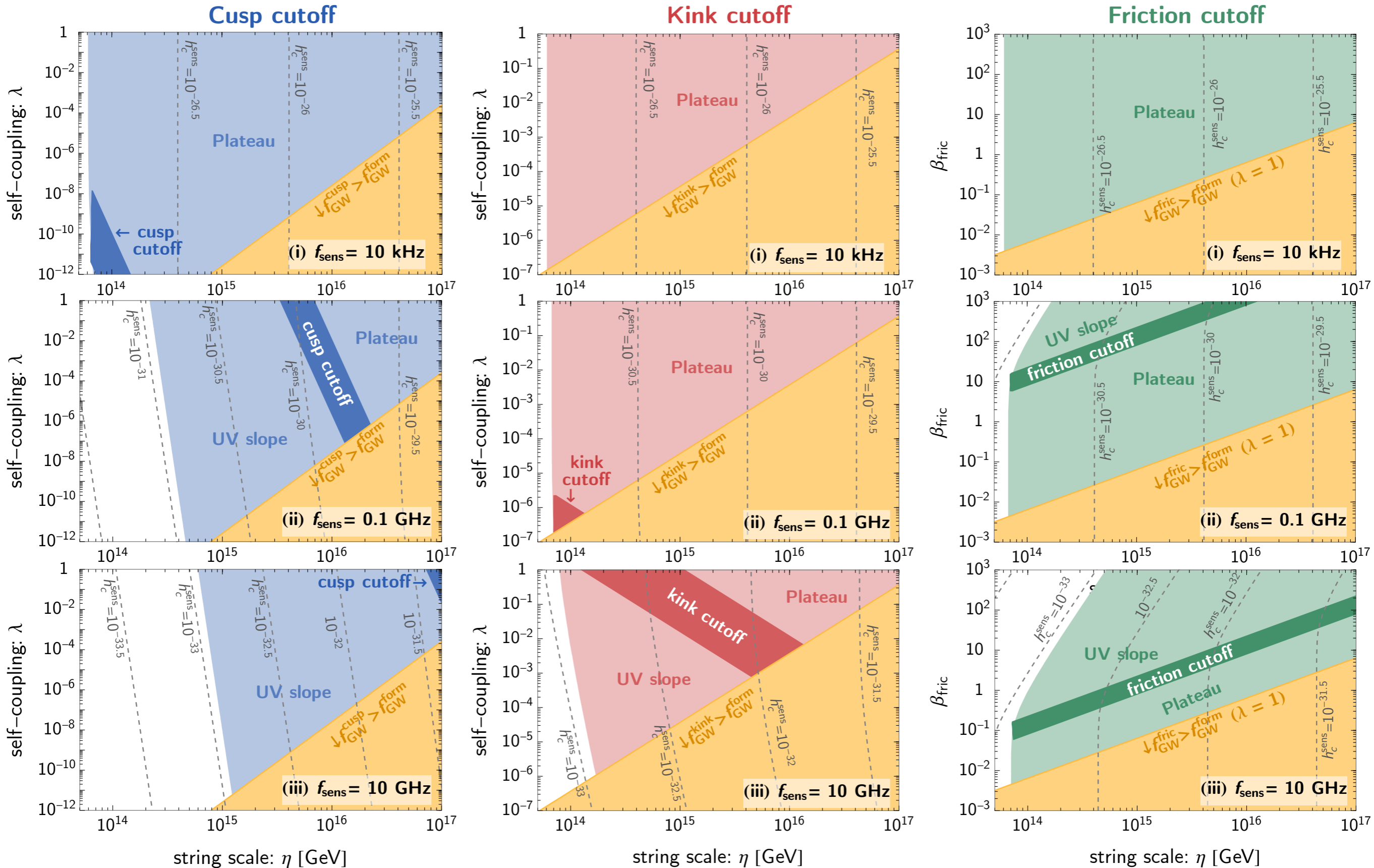
Small signal, even for **large** f_a .

GWB is diluted by matter domination from axions produced from string collapse.



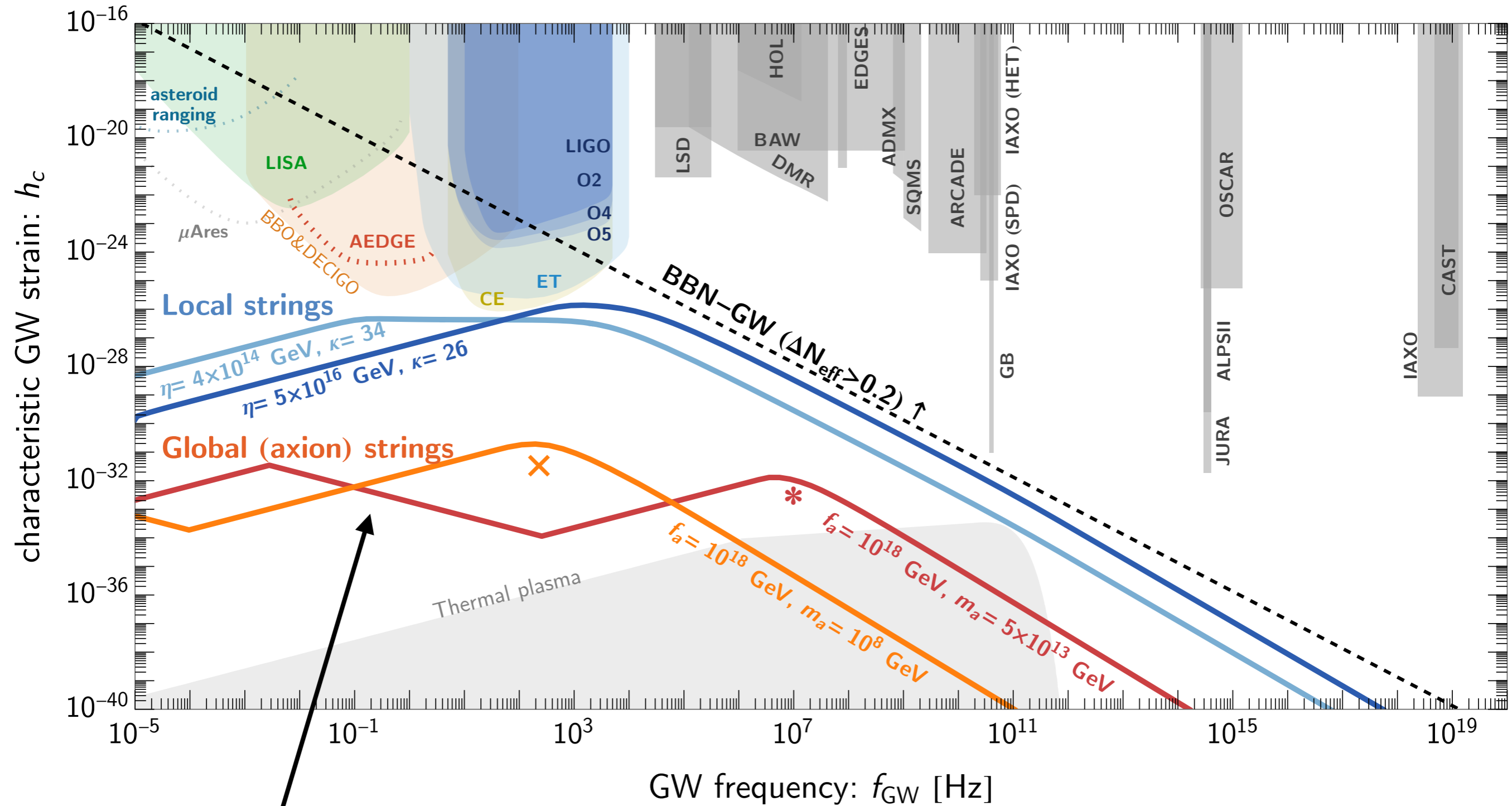
Reconstruction of scalar potential with UHF GWB

Servant, Simakachorn [2312.09281]



UHF GWB from local and global (axionic) strings (Best cases)

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Low-frequency slope is changed by the modified causality tail during the axion matter domination.

Axion matter domination from axionic string decay

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Axion string-wall system decays.

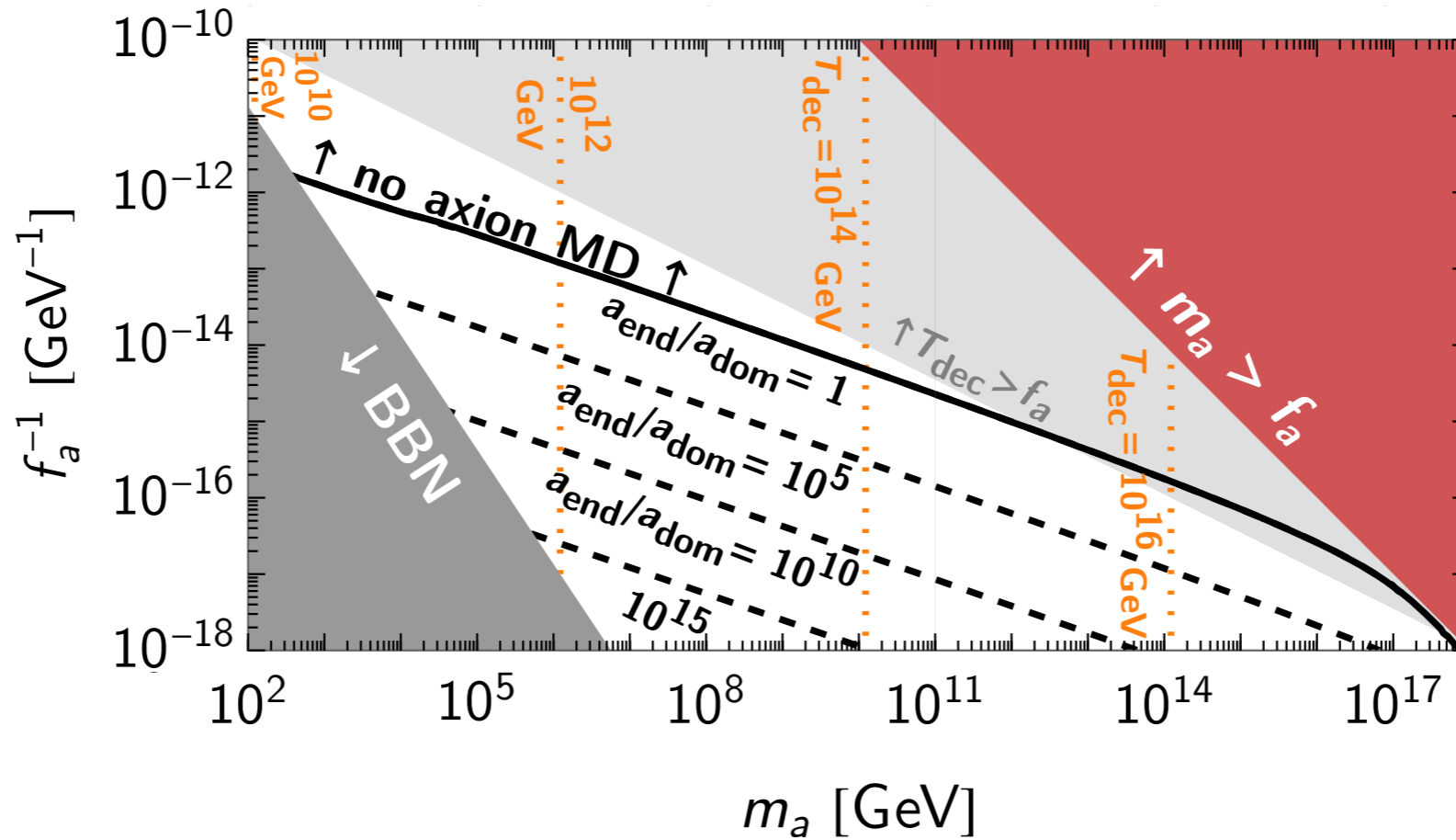
$$T_{\text{dec}} \sim 10^9 \text{ GeV} \sqrt{m_a/\text{GeV}}$$

Axion-matter domination

$$T_{\text{dom}} \simeq T_{\text{dec}} G\mu(T_{\text{dec}})$$

Axions decay into photons

$$T_{a\gamma} \simeq 4.2 \text{ MeV} \left[\frac{106.75}{g_*(T_{a\gamma})} \right]^{\frac{1}{4}} \left(\frac{m_a}{\text{TeV}} \right)^{\frac{3}{2}} \left[\frac{10^{12} \text{ GeV}}{f_a} \right]$$



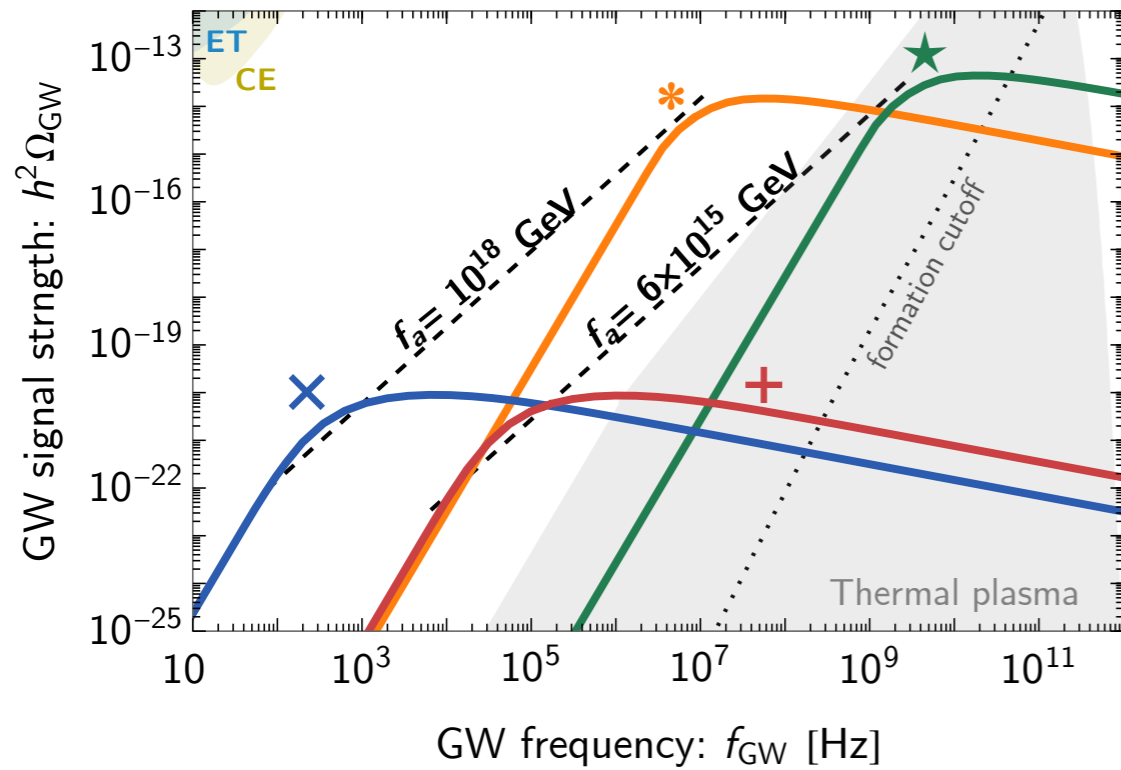
Duration of Axion matter domination

$$\mathcal{B} \equiv \frac{a_{\text{dom}}}{a_{\text{end}}} = \left[\left(\frac{3\sqrt{10}}{64\pi^2} \right) \frac{m_a^3 g_{a\gamma}^2 M_{\text{Pl}}}{g_*^{1/2}(T_{\text{dom}}) T_{\text{dom}}^2} \right]^{\frac{2}{3}} \leq 1,$$

$$g_{a\gamma} = 1.92\alpha_{\text{em}}/(2\pi f_a)$$

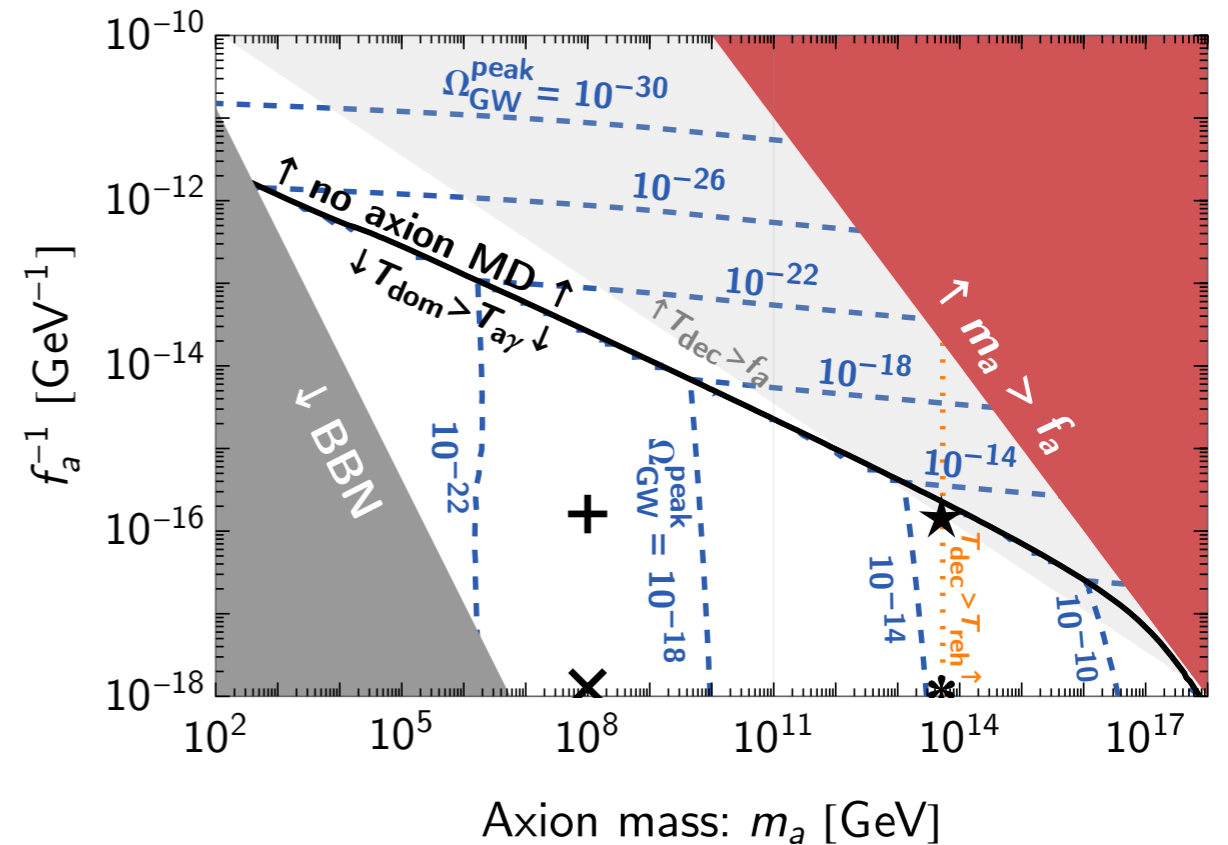
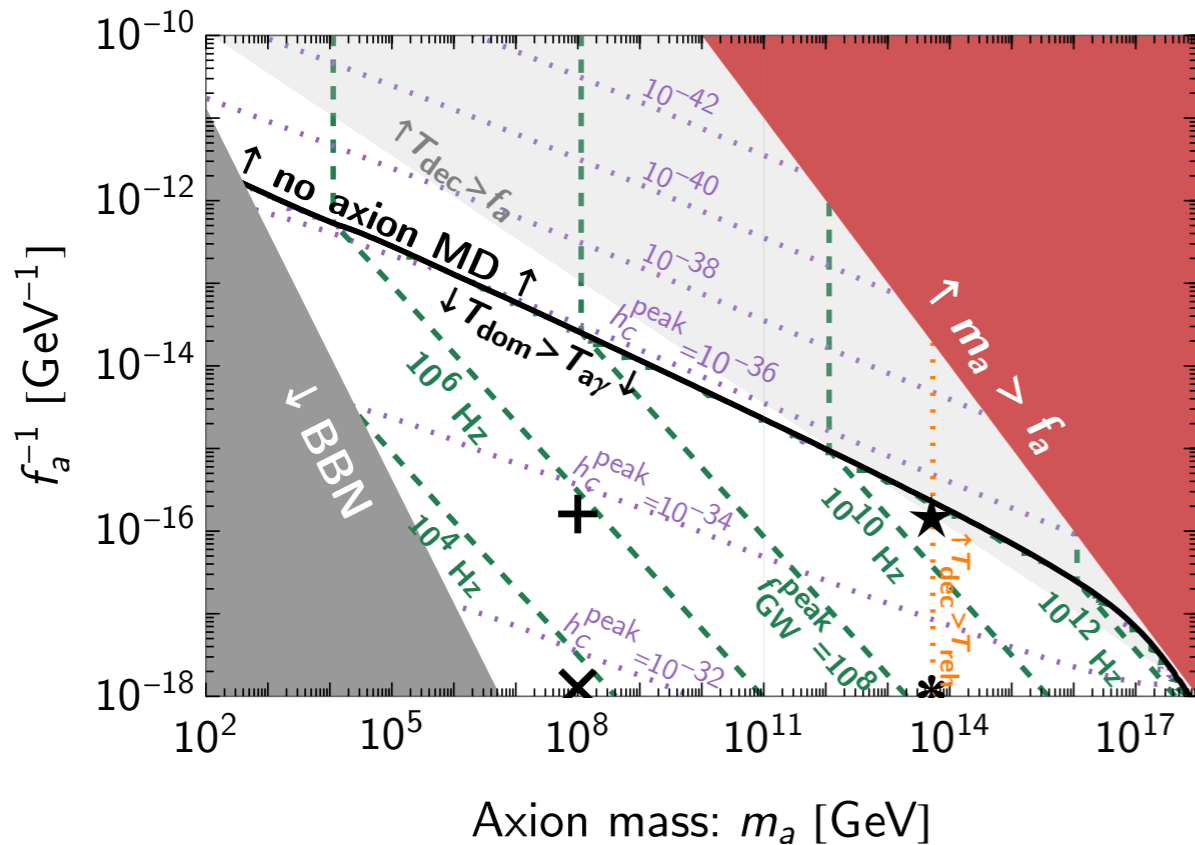
Suppressed UHF GWB from axion strings

Servant, Simakachorn [2312.09281]



$$\Omega_{\text{GW}}(f_{\text{GW}}) = \Omega_{\text{GW}}^{\text{RD}}[f_{\text{GW}}^{\text{RD}}(f_{\text{GW}})] \frac{\mathcal{G}(T_{\text{end}})}{\mathcal{G}(T_{\text{dom}})} \mathcal{B}.$$

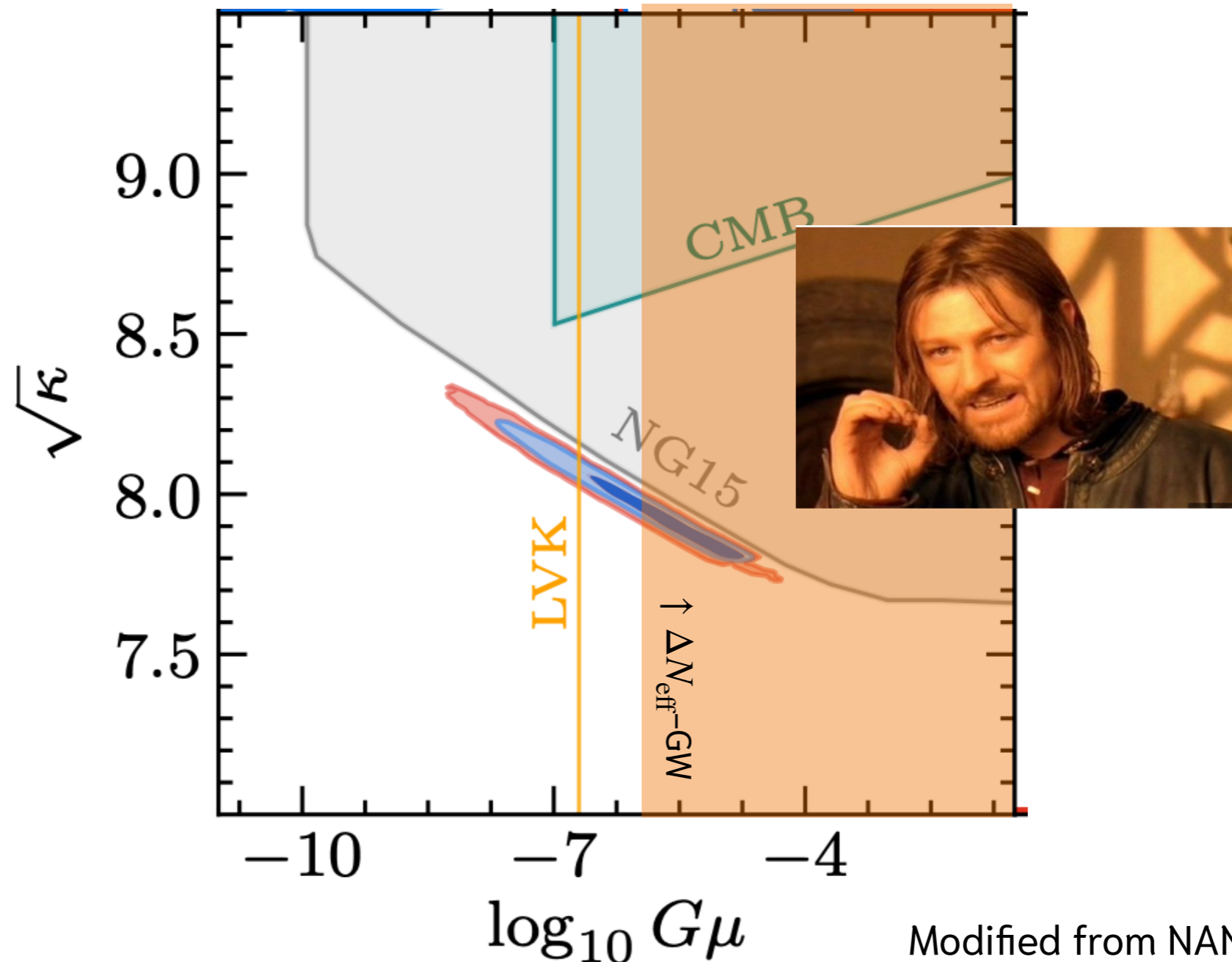
$$f_{\text{GW}} = f_{\text{GW}}^{\text{RD}} \left[\frac{\mathcal{G}(T_{\text{end}})}{\mathcal{G}(T_{\text{dom}})} \right]^{\frac{1}{4}} \mathcal{B}^{\frac{1}{4}}.$$



Local metastable strings can explain PTA data super well?

The best-fit region is excluded by LVK bound,
and on top of that the strings with $G\mu > 10^{-5}$ are in tension with ΔN_{eff} -GW bound

The Bayes factor for explaining the PTA data should be smaller than NG15 analysis.



Modified from NANOGrav [2306.16219]