

Massive graviton dark matter searches with atom interferometers

John Carlton

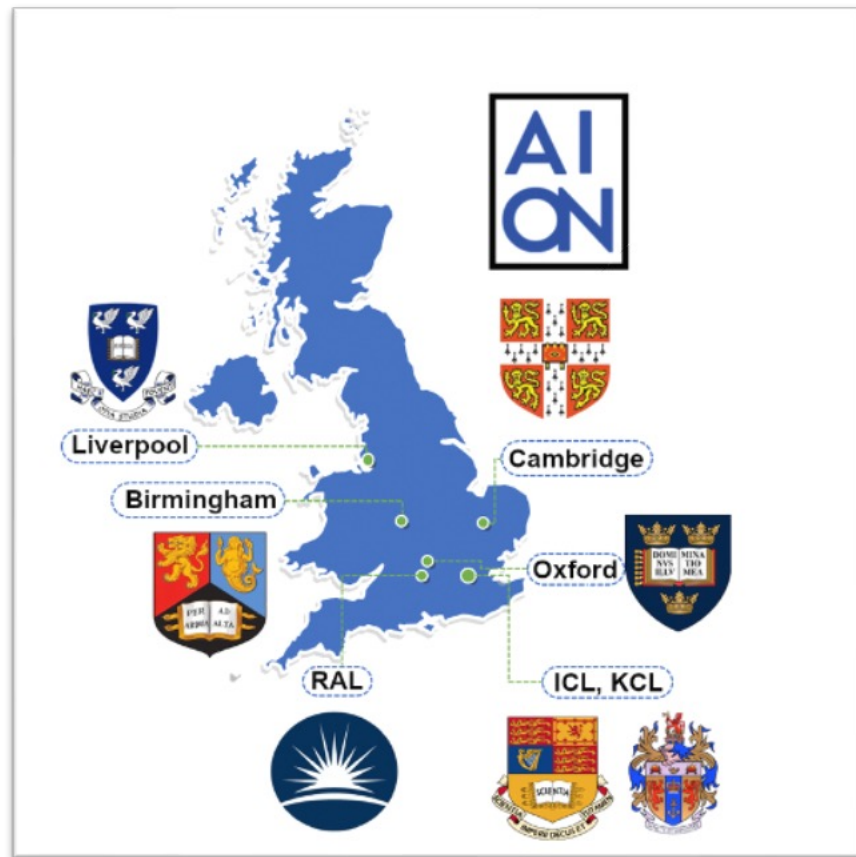
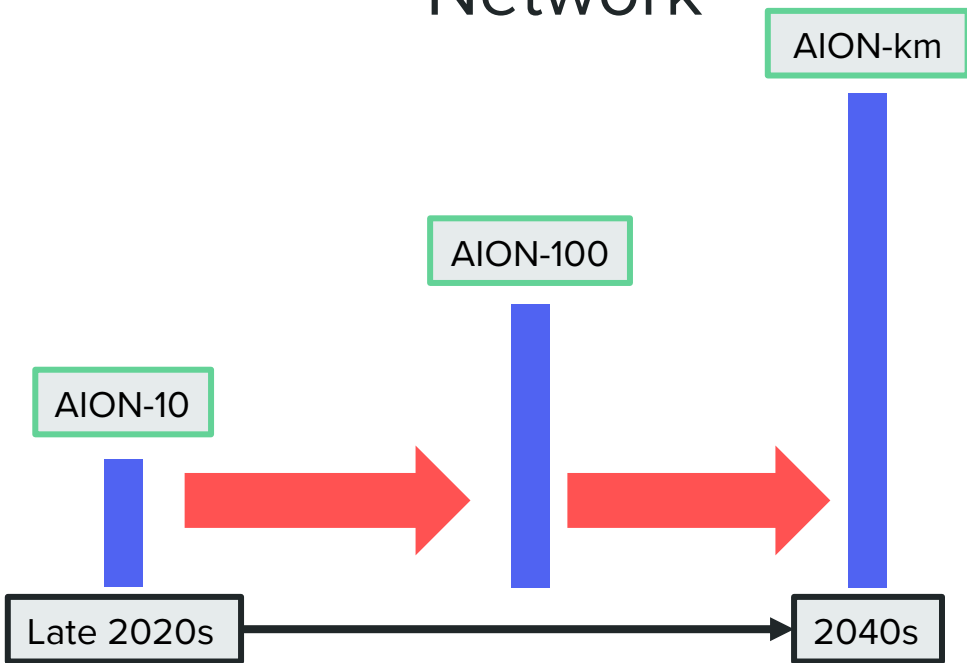
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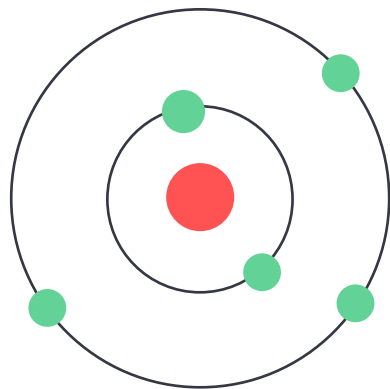
arXiv: 1911.11755

Atom Interferometer Observatory and Network



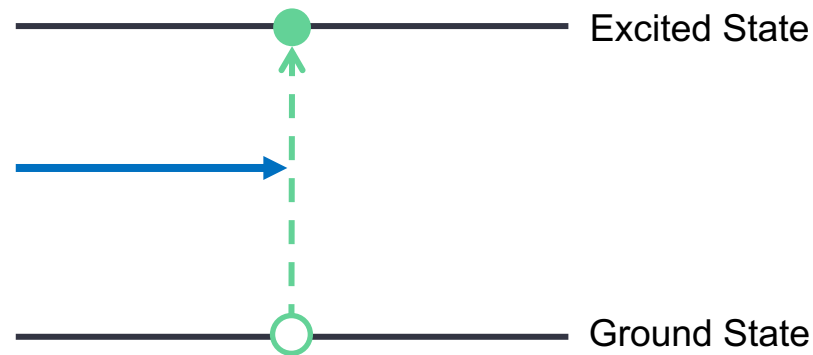
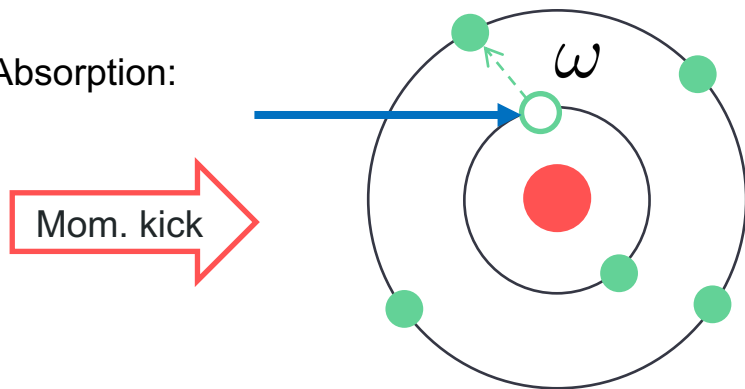
Atom interferometry

Consider a 2-level atom



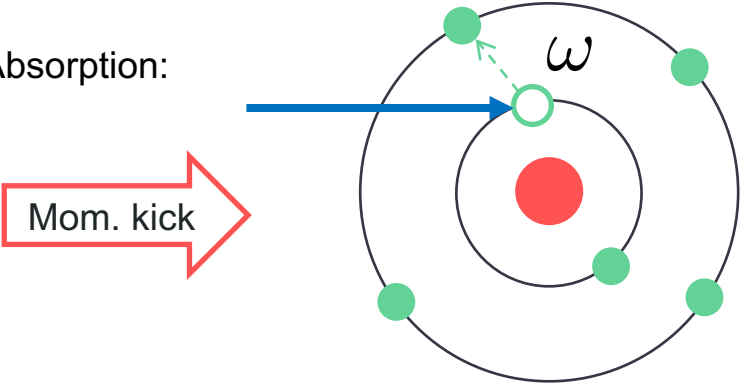
Consider a 2-level atom

Photon Absorption:

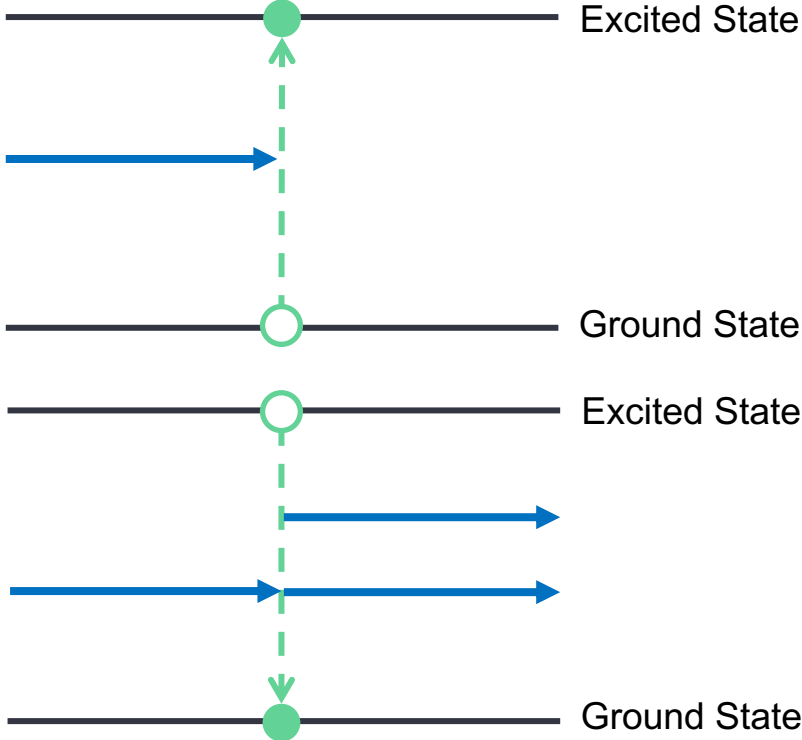
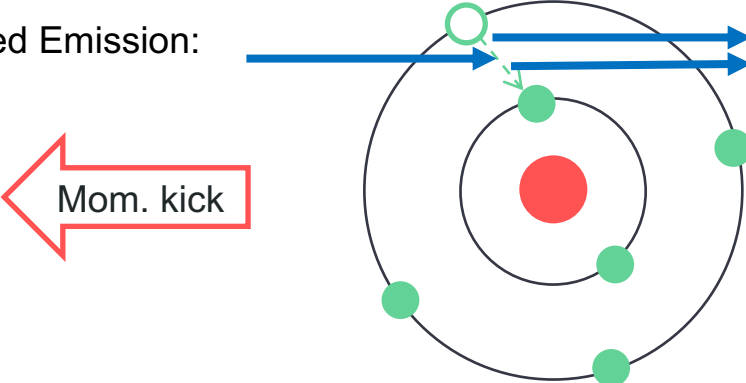


Consider a 2-level atom

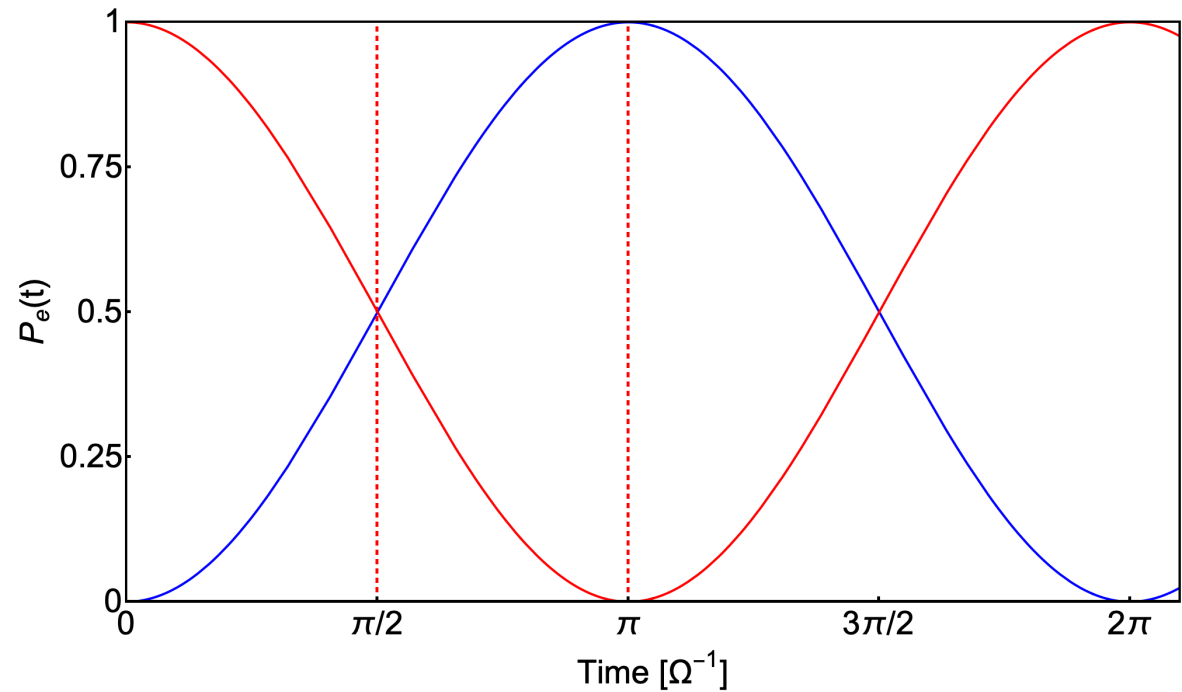
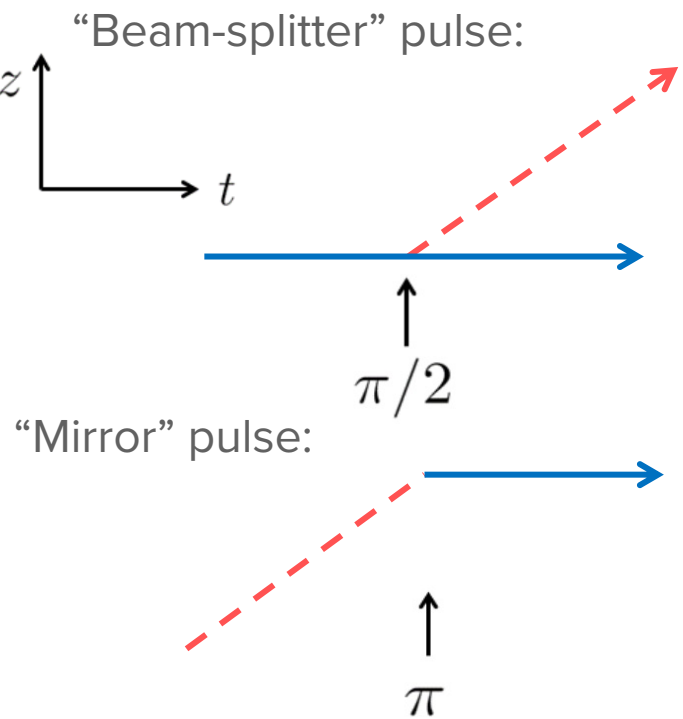
Photon Absorption:



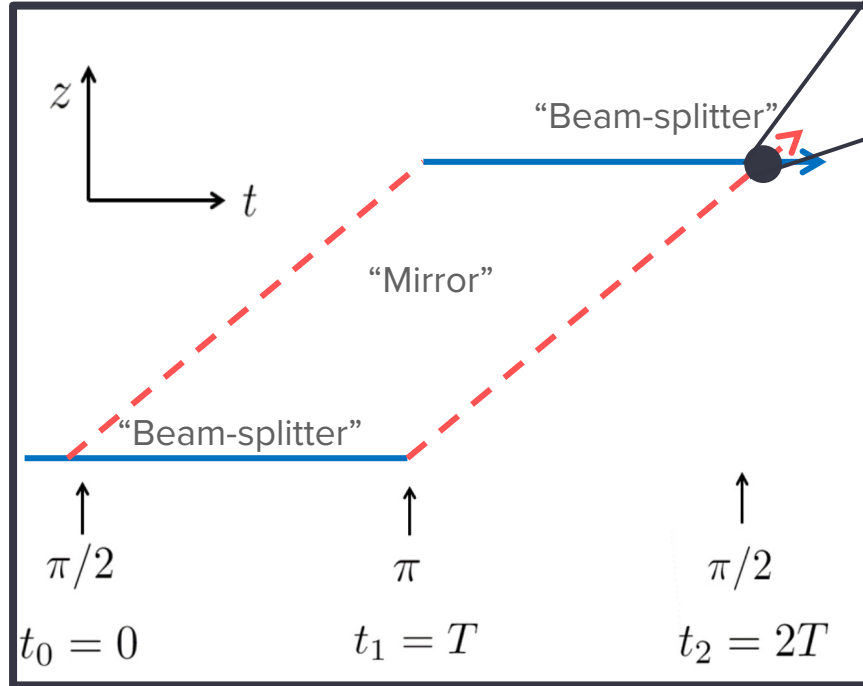
Stimulated Emission:



Rabi oscillations



Interferometer sequence



Mach-Zehnder
interferometer

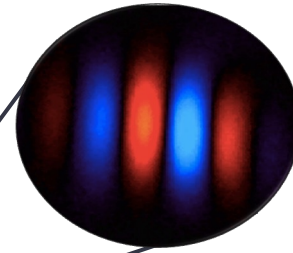


Image atom fringes
and measure phase

$$\phi_{\text{MZ}} = kgT^2$$

Leading order phase depends
on gravitational acceleration

What are we sensitive to?

What can we measure?

$$\phi_{\text{MZ}} = kgT^2$$

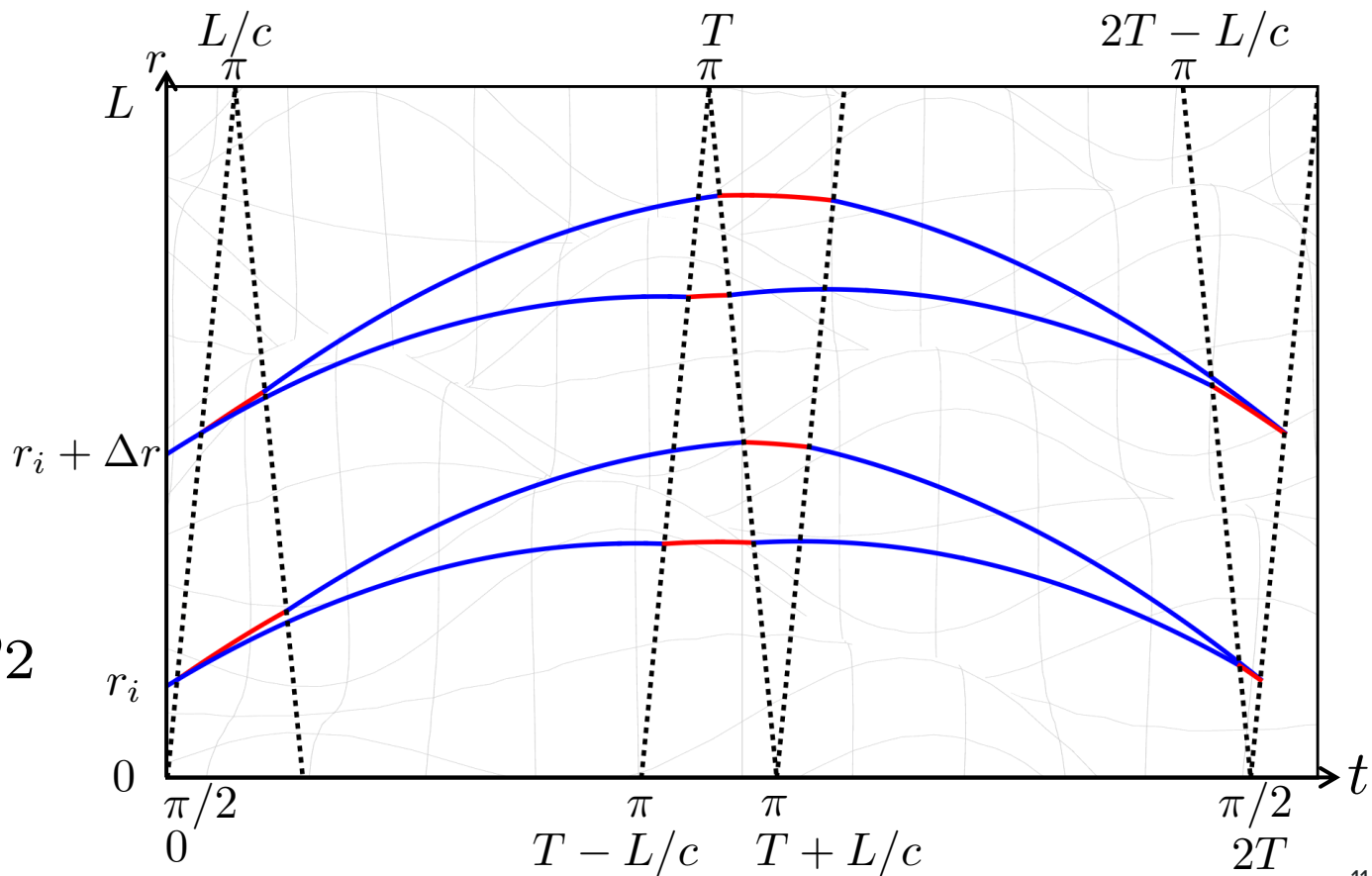
Atom-light
interactions

Gravitational field

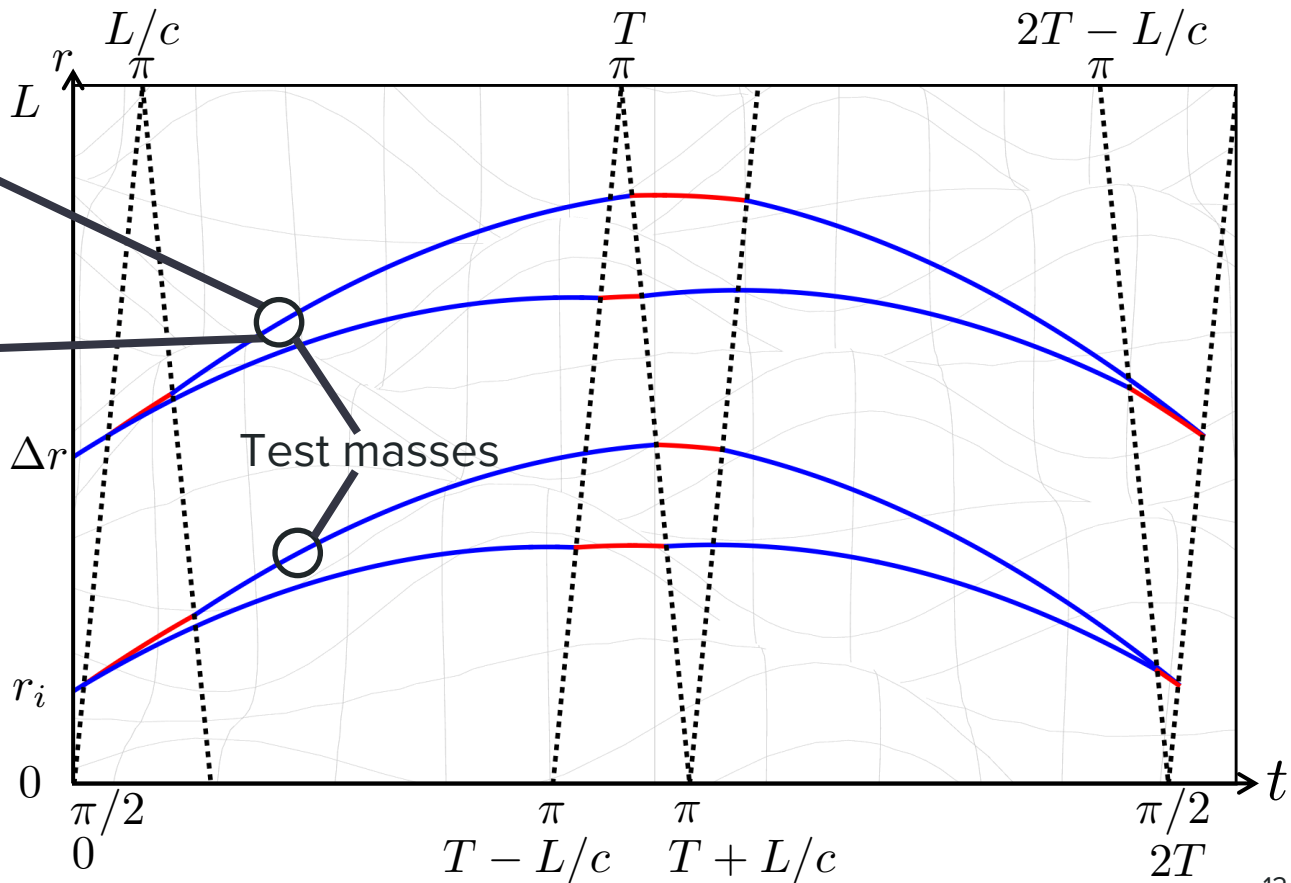
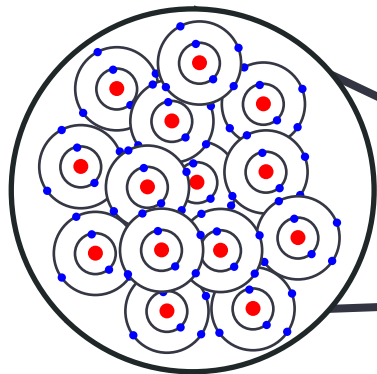
Time

Atom gradiometer

Gradiometer phase
 $\Delta\phi = \phi_1 - \phi_2$

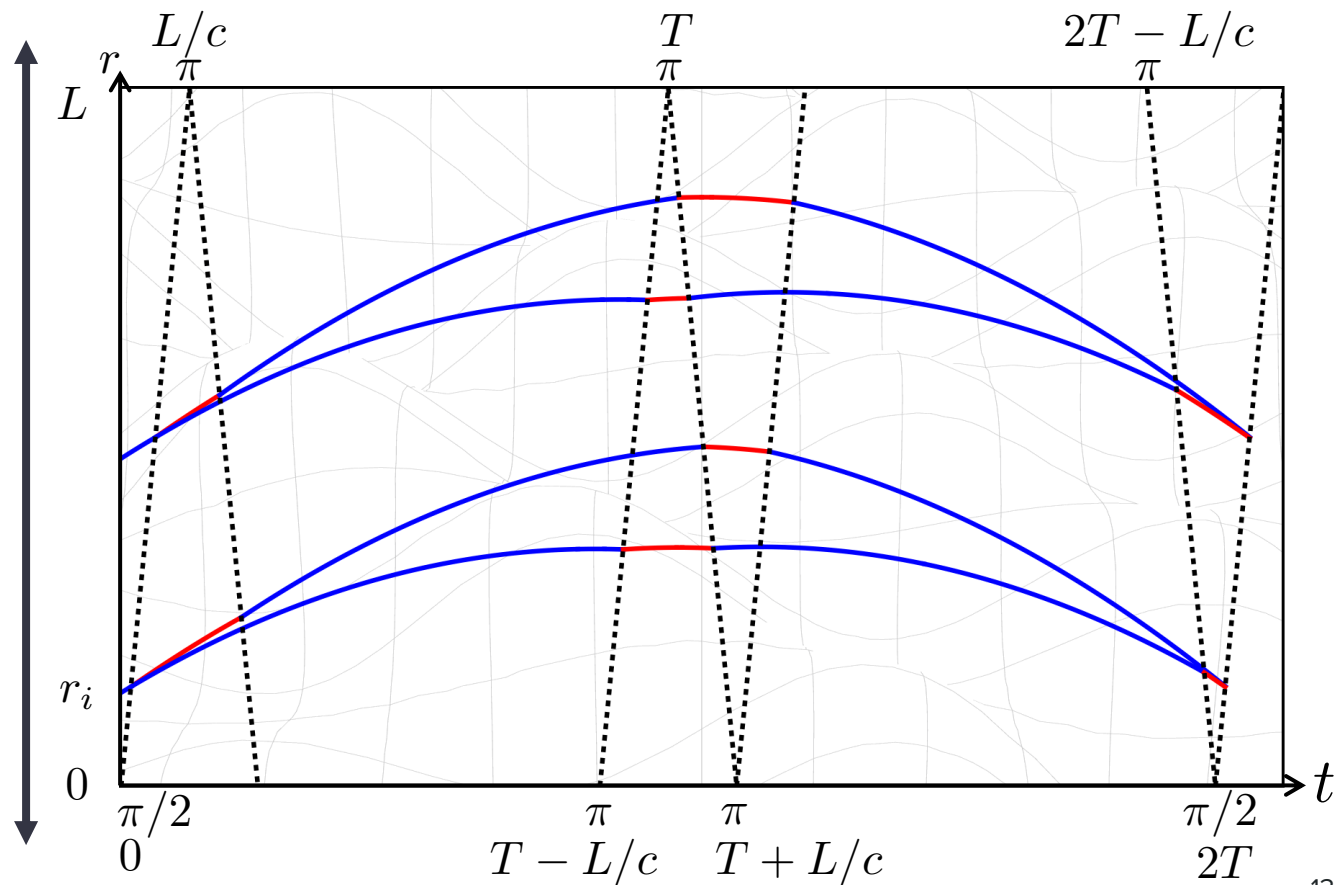
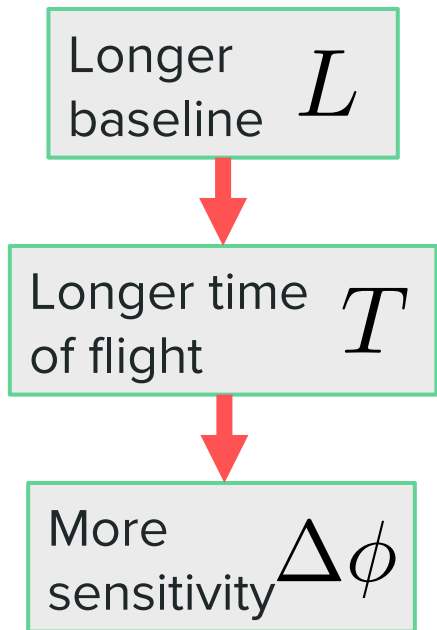


Atom cloud



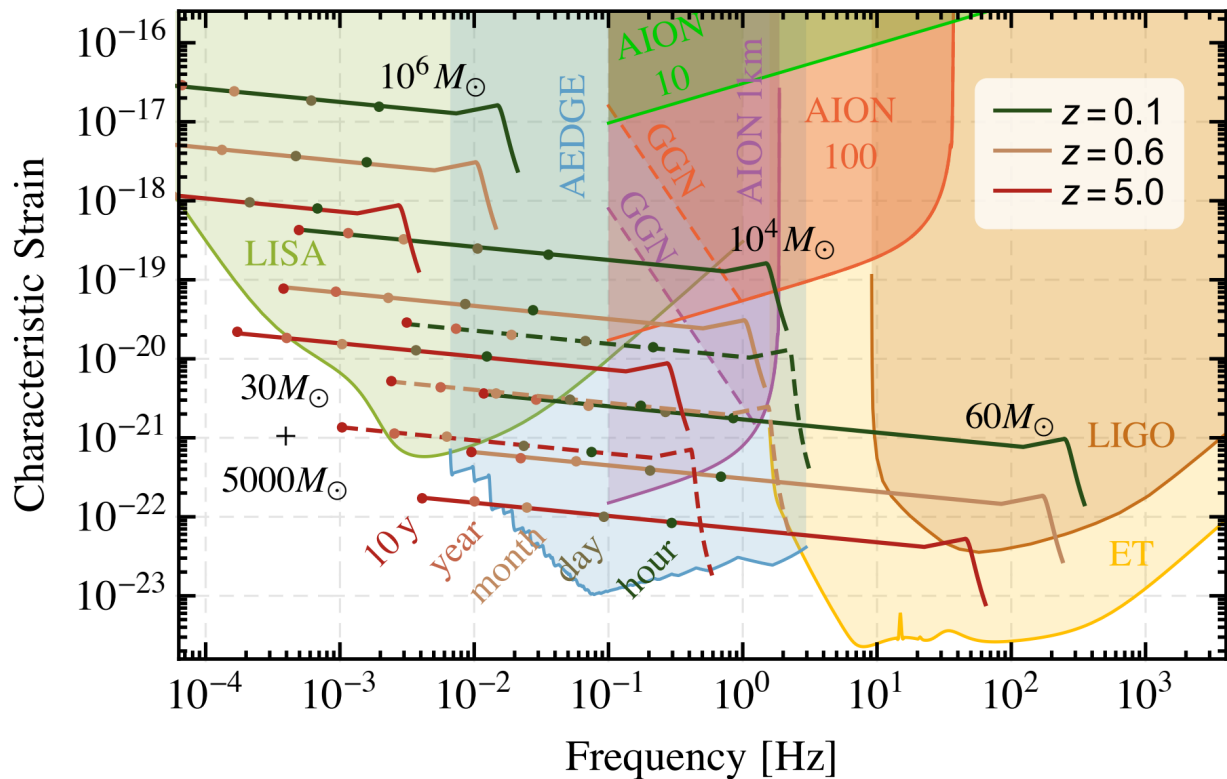
Gradiometer phase

$$\Delta\phi = \phi_1 - \phi_2$$



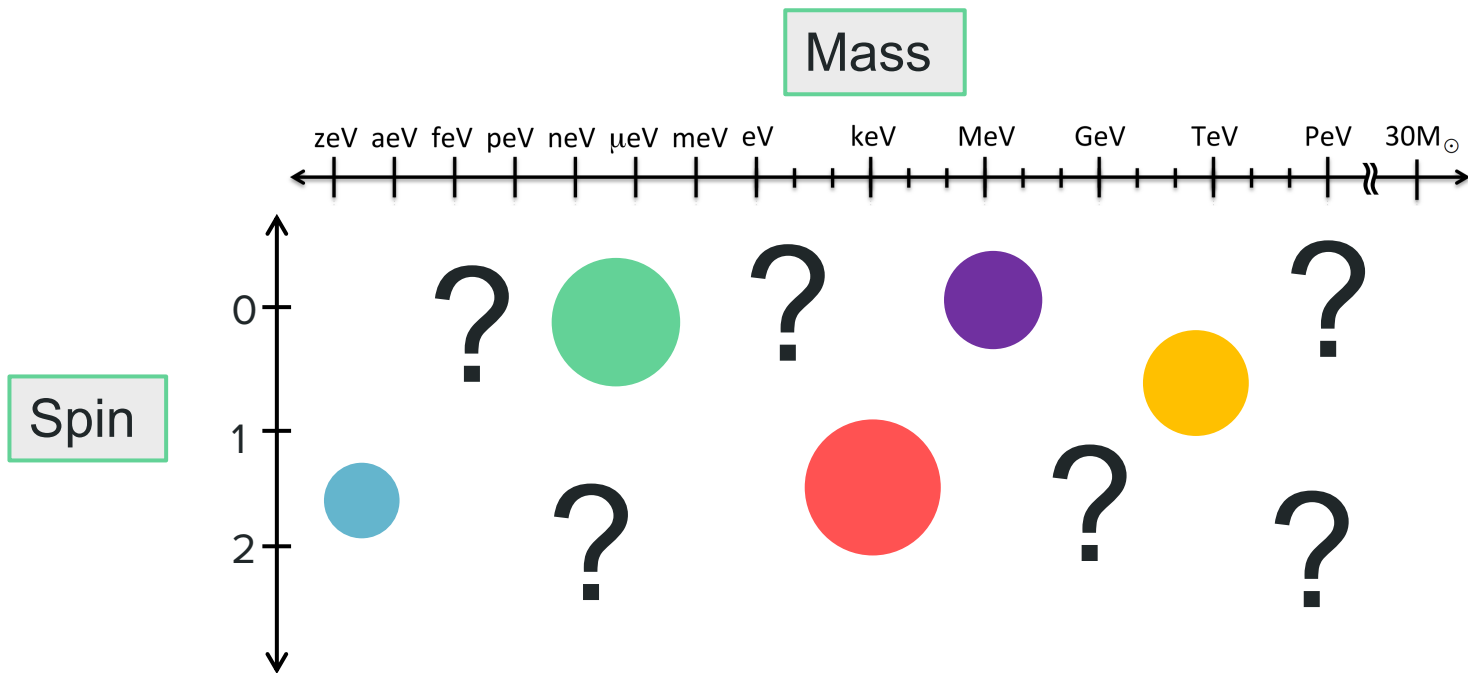
Gravitational waves

❖ 'Mid-band' sensitivity between LIGO and LISA.

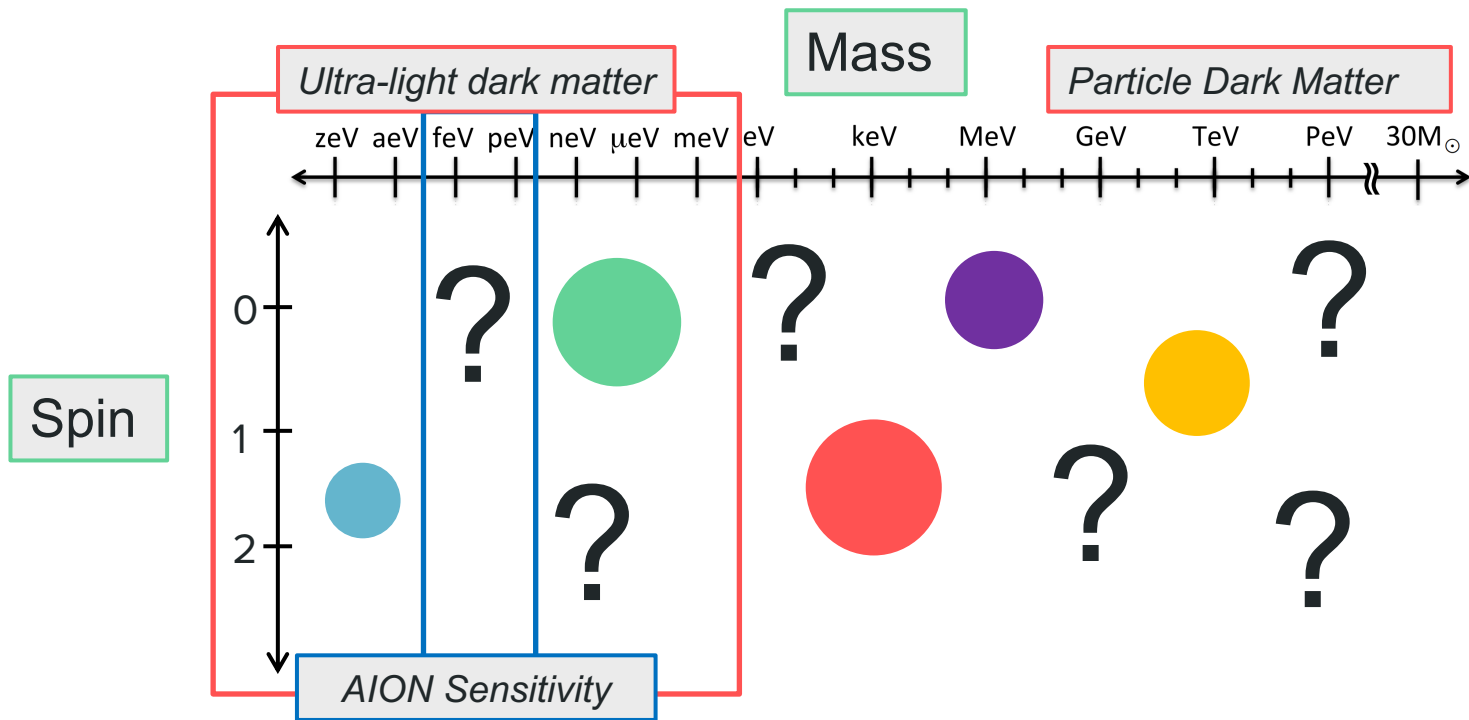


Dark matter

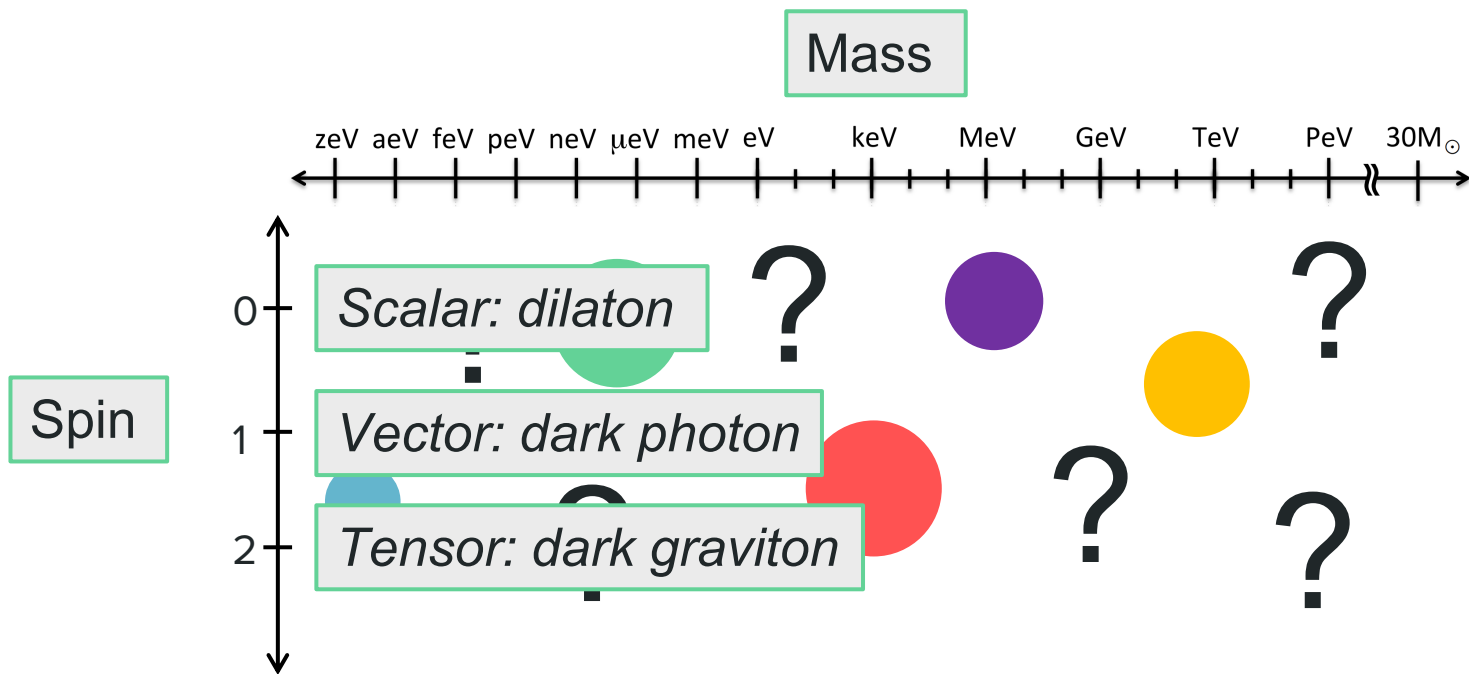
A lot of parameter space!



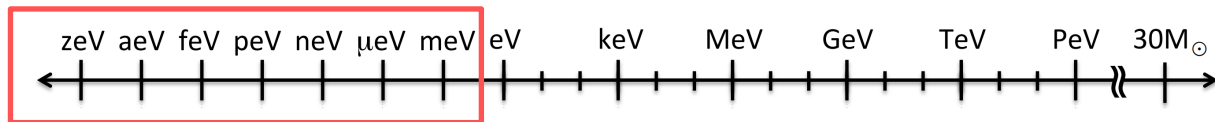
A lot of parameter space!



A lot of parameter space!



A classical ULDM field



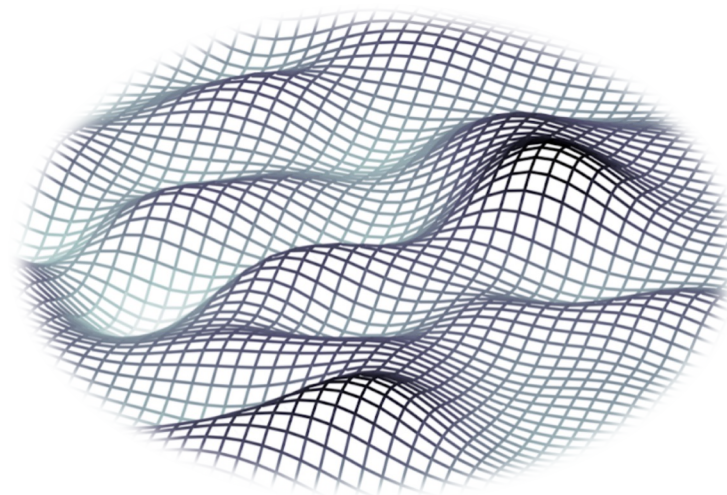
Ultralight mass means a high occupation number

Can describe as a classical field

$$\varphi(t, \mathbf{x}) \sim \cos(\omega_{\varphi} t - \mathbf{k}_{\varphi} \cdot \mathbf{x})$$

Frequency given by ULDM mass
(with small velocity correction)

$$\omega_{\varphi} \simeq m_{\varphi} \left(1 + \frac{v^2}{2} \right)$$



Atoms in a scalar ULDM field

$$\mathcal{L} \supset \mathcal{L}_{\text{SM}} + \mathcal{L}_\varphi \longrightarrow \mathcal{L}_\varphi \supset \varphi(t, \mathbf{x}) \sqrt{4\pi G_{\text{N}}} \left[\frac{d_e}{4e^2} F_{\mu\nu} F^{\mu\nu} - d_{m_e} m_e \bar{\psi}_e \psi_e \right]$$

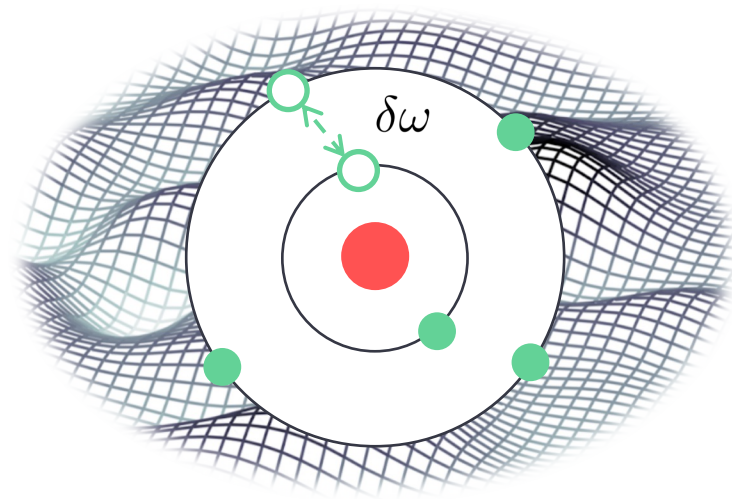
photon coupling
electron coupling

$$\alpha(t, \mathbf{x}) \approx \alpha \left[1 + d_e \sqrt{4\pi G_{\text{N}}} \varphi(t, \mathbf{x}) \right],$$

$$m_e(t, \mathbf{x}) = m_e \left[1 + d_{m_e} \sqrt{4\pi G_{\text{N}}} \varphi(t, \mathbf{x}) \right]$$

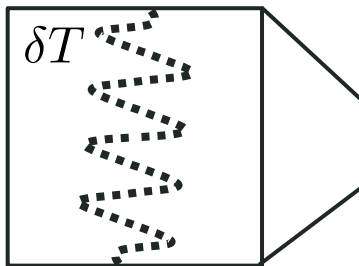
↓

$$\delta\phi \sim \delta\omega \sim \varphi(t, \mathbf{x})$$

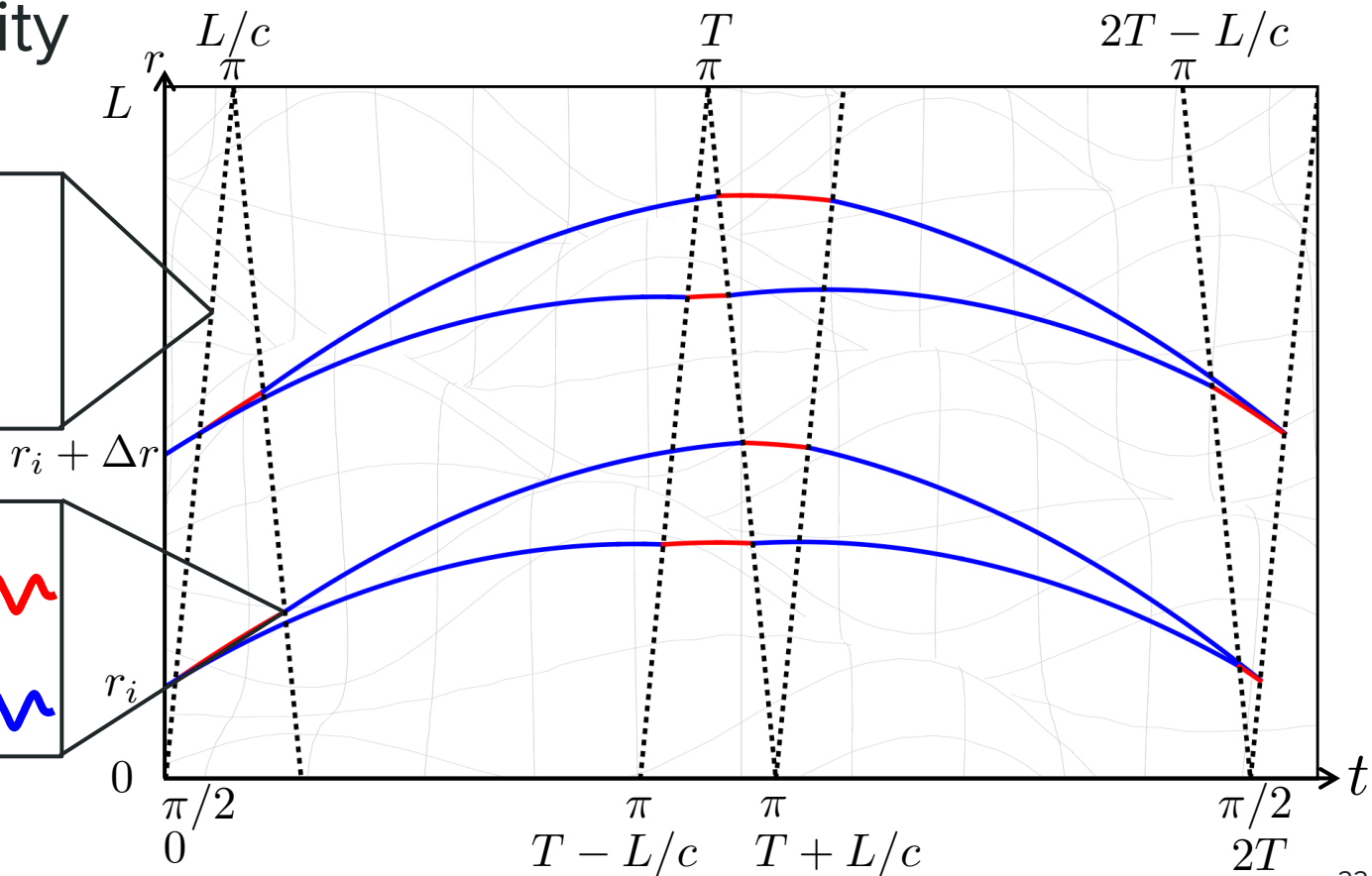
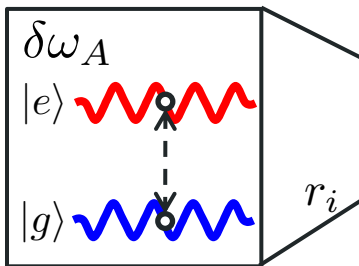


Two sensitivity channels

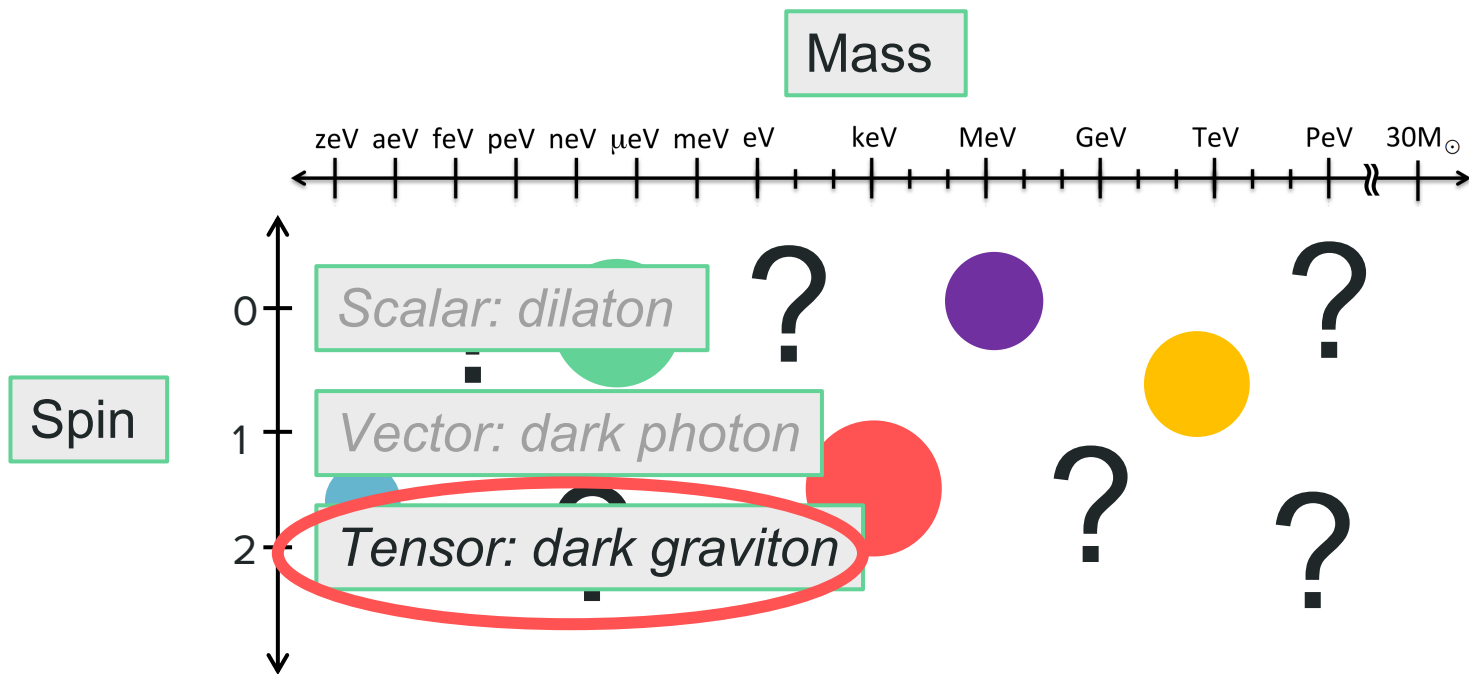
Interrogation time (GWs)



Atomic transition frequency (Scalar ULDM)



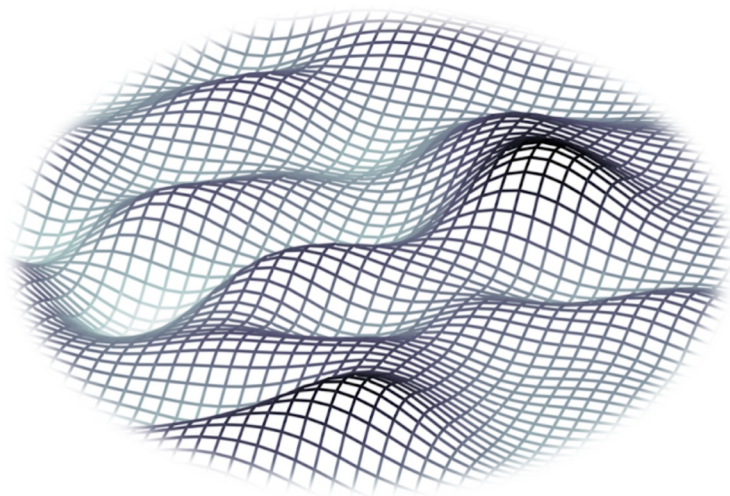
What about spin-2?



Massive graviton dark matter

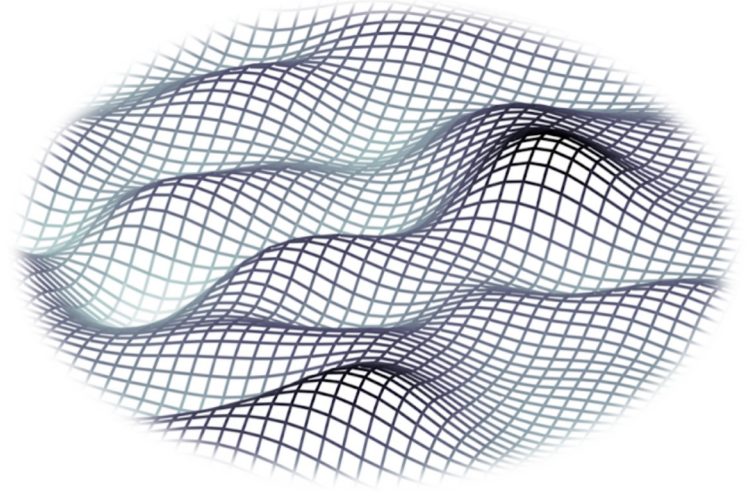
Massive gravity field theory

Let's consider a massive spin-2 ultra-light field $\varphi_{\mu\nu}$



Massive gravity field theory

Let's consider a massive spin-2 ultra-light field $\varphi_{\mu\nu}$



Express as irreducible fields:

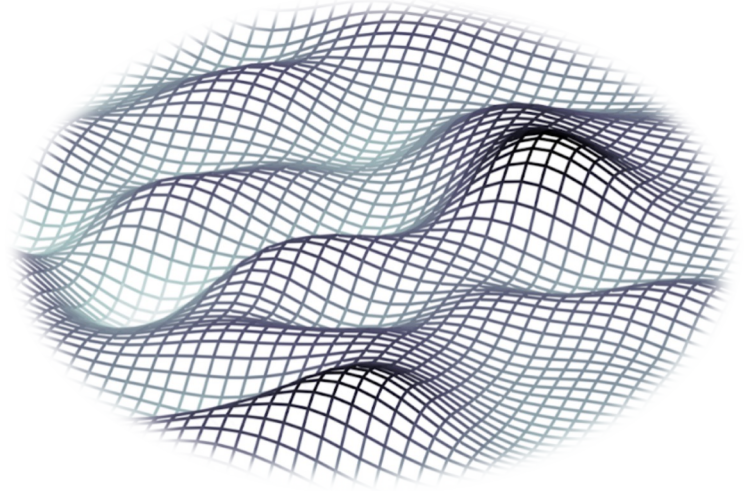
$$\varphi_{00} = \Psi$$

$$\varphi_{0i} = u_i + \partial_i v$$

$$\varphi_{ij} = \varphi_{ij}^{\text{TT}} + 2\partial_{(i} A_{j)} + \partial_i \partial_j \sigma + \delta_{ij} \pi$$

Massive gravity field theory

Let's consider a massive spin-2 ultra-light field $\varphi_{\mu\nu}$



Express as irreducible fields:

$$\varphi_{00} = \Psi$$

Tensor

$$\varphi_{0i} = u_i + \partial_i v$$

Vector

Scalar

$$\varphi_{ij} = \varphi_{ij}^{\text{TT}} + 2\partial_{(i} A_{j)} + \partial_i \partial_j \sigma + \delta_{ij} \pi$$

Three normalised fields

Tensor $\mathcal{L}_t = \frac{1}{2} \left(\tilde{\varphi}_{ij} \square \tilde{\varphi}_{ij} - m_t^2 \tilde{\varphi}_{ij} \tilde{\varphi}_{ij} \right)$

Vector $\mathcal{L}_v = \frac{1}{2} \left(\tilde{A}_i \square \tilde{A}_i - m_v^2 \tilde{A}_i \tilde{A}_i \right)$

Scalar $\mathcal{L}_s = \frac{1}{2} \left(\tilde{\pi} \square \tilde{\pi} - m_s^2 \tilde{\pi}^2 \right)$

Three classical oscillating fields...

Tensor $\tilde{\varphi}_{ij}(t, \mathbf{x}) = \sum_{\lambda} \tilde{\varphi}_{0,\lambda} e_{ij}^{\lambda}(\mathbf{k}_t) \cos(\omega_t t - \mathbf{k}_t \cdot \mathbf{x})$

Vector $\tilde{A}_i(t, \mathbf{x}) = \sum_{\lambda} \tilde{A}_{0,\lambda} e_i^{\lambda}(\mathbf{k}_v) \cos(\omega_v t - \mathbf{k}_v \cdot \mathbf{x})$

Scalar $\tilde{\pi}(t, \mathbf{x}) = \tilde{\pi}_0 \cos(\omega_s t - \mathbf{k}_s \cdot \mathbf{x})$

Three classical oscillating fields...

Tensor $\tilde{\varphi}_{ij}(t, \mathbf{x}) = \sum_{\lambda} \tilde{\varphi}_{0,\lambda} e_{ij}^{\lambda}(\mathbf{k}_t) \cos(\omega_t t - \mathbf{k}_t \cdot \mathbf{x})$

Sum over polarisations

Vector $\tilde{A}_i(t, \mathbf{x}) = \sum_{\lambda} \tilde{A}_{0,\lambda} e_i^{\lambda}(\mathbf{k}_v) \cos(\omega_v t - \mathbf{k}_v \cdot \mathbf{x})$

Scalar $\tilde{\pi}(t, \mathbf{x}) = \tilde{\pi}_0 \cos(\omega_s t - \mathbf{k}_s \cdot \mathbf{x})$

... each contributing to the local dark matter

Tensor

$$\tilde{\varphi}_0 = \frac{\sqrt{2f_t\rho_{\text{DM}}}}{m_t}$$

Vector

$$\tilde{A}_0 = \frac{\sqrt{2f_v\rho_{\text{DM}}}}{m_v}$$

Scalar

$$\tilde{\pi}_0 = \frac{\sqrt{2f_s\rho_{\text{DM}}}}{m_s}$$

... each contributing to the local dark matter

Tensor

$$\tilde{\varphi}_0 = \frac{\sqrt{2} f_t \rho_{\text{DM}}}{m_t}$$

Vector

$$\tilde{A}_0 = \frac{\sqrt{2} f_v \rho_{\text{DM}}}{m_v}$$

Scalar

$$\tilde{\pi}_0 = \frac{\sqrt{2} f_s \rho_{\text{DM}}}{m_s}$$

Fraction of total
dark matter

$$f_t + f_v + f_s = 1$$

Coupling to matter

$$\mathcal{L}_{\text{int}} = \kappa^\phi \varphi^{\mu\nu} \mathcal{O}_{\mu\nu}$$



Symmetric Standard Model operator

Coupling to matter

$$\mathcal{L}_{\text{int}} = \kappa^\phi \varphi^{\mu\nu} \mathcal{O}_{\mu\nu} \longrightarrow \overset{\text{Tensor}}{\kappa_t \varphi^{ij} \mathcal{O}_{ij}^t} + \overset{\text{Vector}}{\kappa_v \varphi^{0i} \mathcal{O}_{0i}^v} + \overset{\text{Scalar}}{\kappa_s \varphi^{00} \mathcal{O}^s}$$

Coupling to matter

$$\mathcal{L}_{\text{int}} = \kappa^\phi \varphi^{\mu\nu} \mathcal{O}_{\mu\nu} \longrightarrow \overset{\text{Tensor}}{\kappa_t \varphi^{ij} \mathcal{O}_{ij}^t} + \overset{\text{Vector}}{\kappa_v \varphi^{0i} \mathcal{O}_{0i}^v} + \overset{\text{Scalar}}{\kappa_s \varphi^{00} \mathcal{O}^s}$$

Non-relativistic limit

$$\downarrow \qquad \qquad \qquad \downarrow$$
$$\frac{\alpha}{M_{\text{Pl}}} \tilde{\varphi}^{ij} T_{ij} \qquad \qquad \qquad \frac{\beta}{M_{\text{Pl}}} \tilde{\pi} T$$

Tensor modes

Field theory picture:

$$\mathcal{L} \supset \mathcal{L}_{\text{SM}} + \mathcal{L}_{\tilde{\varphi}} \longrightarrow \mathcal{L}_{\tilde{\varphi}} \supset \frac{\alpha}{M_{\text{Pl}}} \tilde{\varphi}^{ij} T_{ij}$$

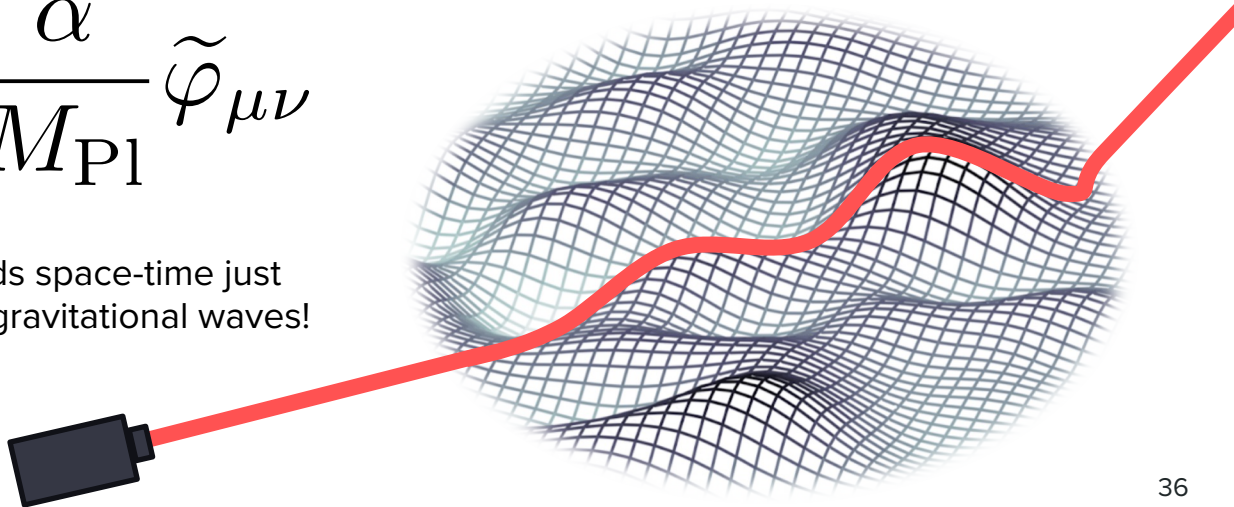
coupling const.

stress-energy tensor

Linearised gravity picture:

$$g_{\mu\nu} = \eta_{\mu\nu} + \frac{\alpha}{M_{\text{Pl}}} \tilde{\varphi}_{\mu\nu}$$

Bends space-time just
like gravitational waves!



Scalar mode

Field theory picture:

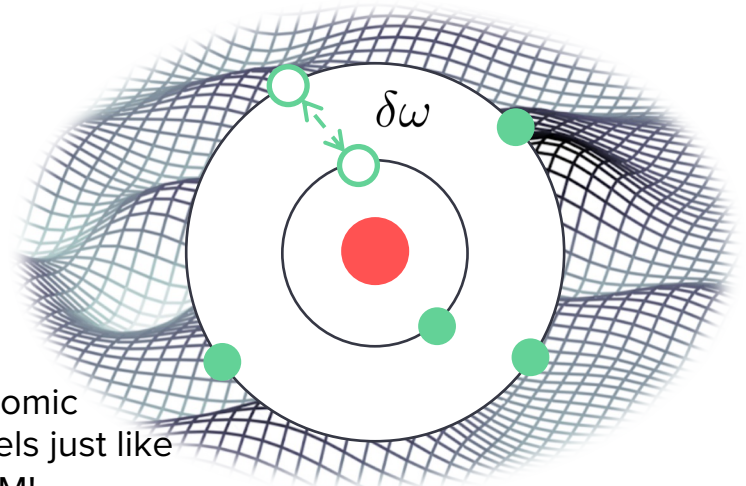
$$\mathcal{L} \supset \mathcal{L}_{\text{SM}} + \mathcal{L}_{\tilde{\pi}} \longrightarrow \mathcal{L}_{\tilde{\pi}} \supset \frac{\beta}{M_{\text{Pl}}} \tilde{\pi} T \quad T \rightarrow m_{\psi} \bar{\psi} \psi$$

coupling const. trace of stress-energy tensor

$$m_e(t) = m_{e,0} \left[1 - \frac{\beta}{M_{\text{Pl}}} \tilde{\pi}(t) \right]$$

↓

$$\delta\phi \sim \delta\omega \sim \varphi(t, \mathbf{x})$$



Modifies atomic energy levels just like scalar ULDM!

What can we measure?

$$\phi_{\text{MZ}} = kgT^2$$

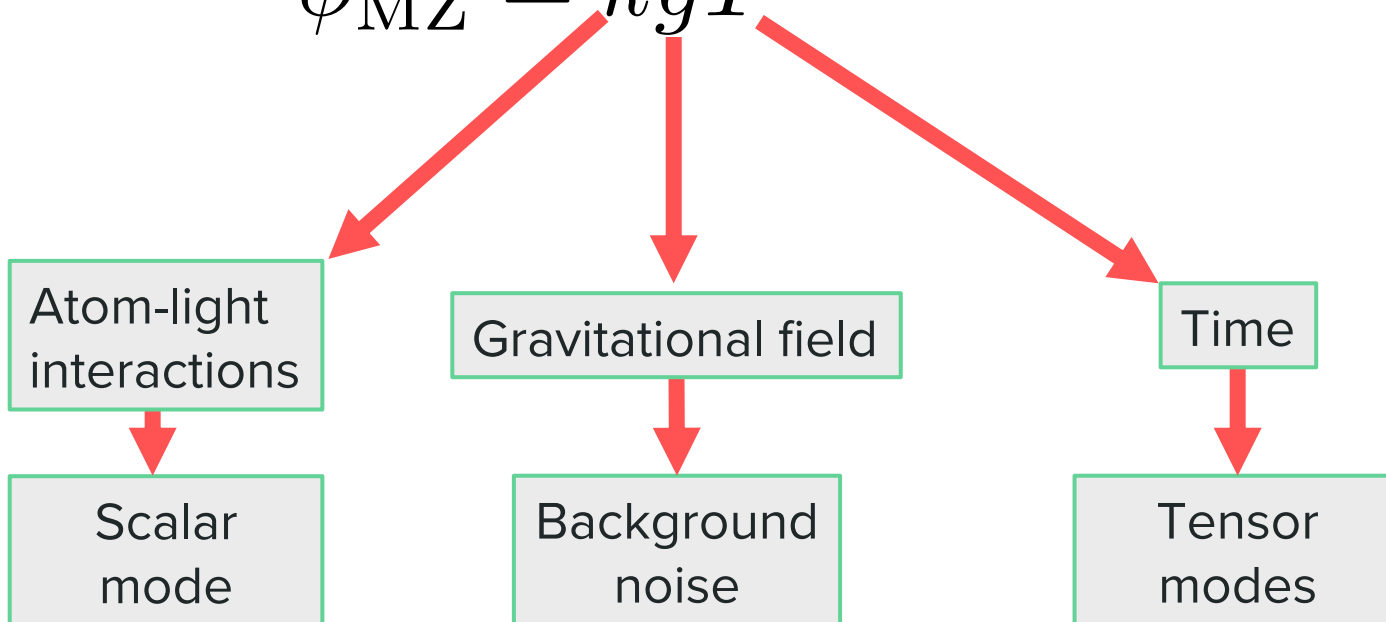
Atom-light
interactions

Gravitational field

Time

What can we measure?

$$\phi_{\text{MZ}} = kgT^2$$



Projected detection limits

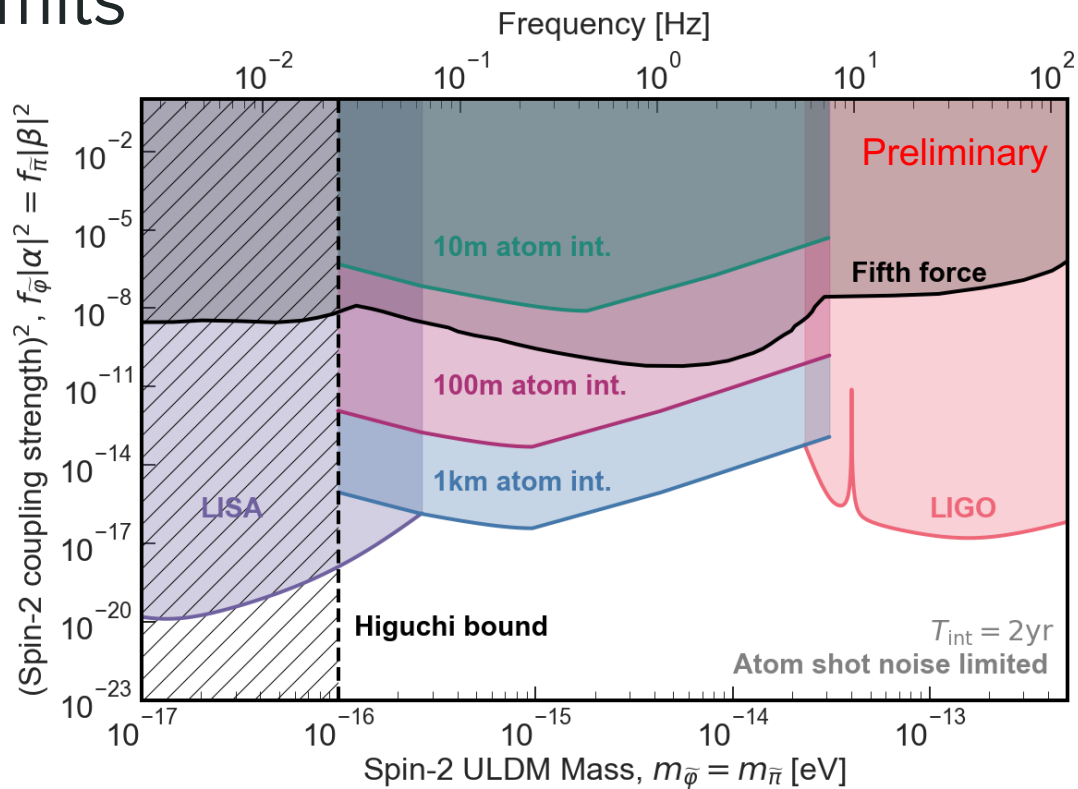
10m, 100m and 1km example
atom interferometers

Assume Lorentz invariance:

$$m_t = m_v = m_s$$

$$\kappa_t = \kappa_v = \kappa_s$$

$$f_t = f_v = f_s$$

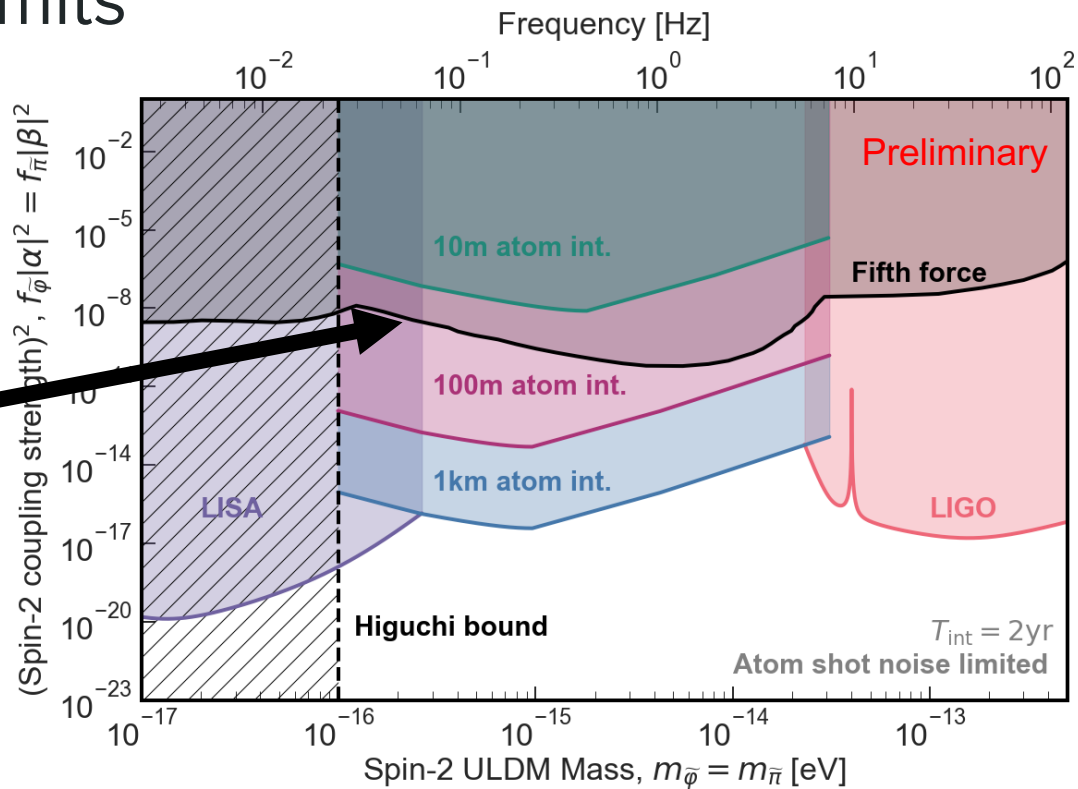


Projected detection limits

Leading constraints on tensor mode come from 'fifth force' experiments

$$\delta V_{\text{Newt}} \propto \alpha^2 e^{-m_{\tilde{\varphi}} r}$$

In this range, from lunar laser ranging



Projected detection limits

Leading constraints on tensor mode come from 'fifth force' experiments

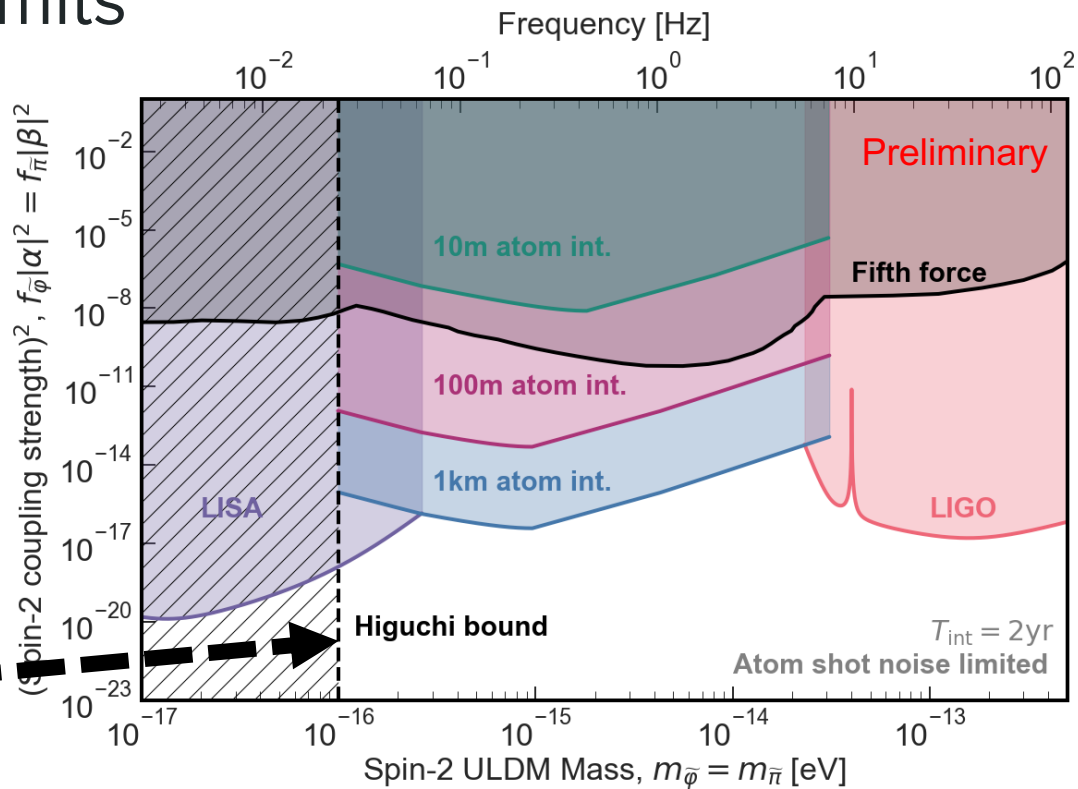
$$\delta V_{\text{Newt}} \propto \alpha^2 e^{-m_{\tilde{\varphi}} r}$$

In this range, from lunar laser ranging

Higuchi bound sets a lower bound for mass of spin-2 field

$$m^2 \geq 2H^2$$

Least stringent bound from BBN



Projected detection limits

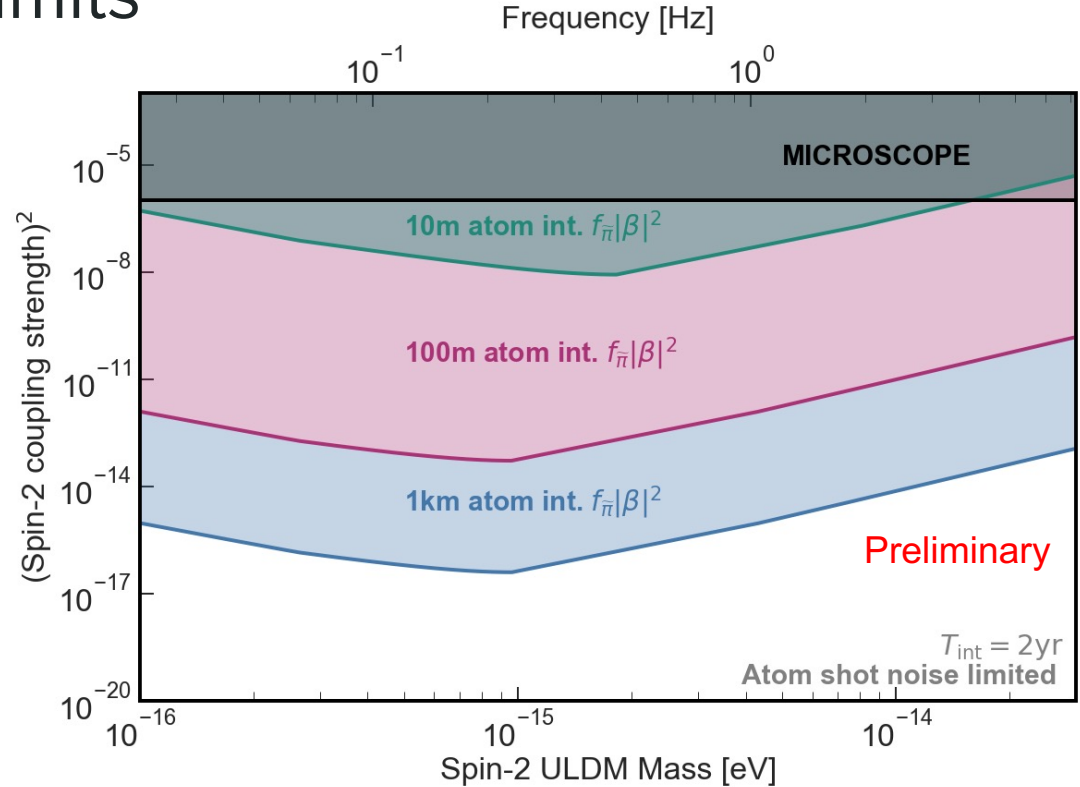
Consider the tensor and scalar couplings independently in the Lorentz violating case.

$$m_t \neq m_s$$

$$\alpha \neq \beta$$

$$f_t \neq f_s$$

Scalar mode constrained by tests of equivalence principle



Advantages of networking!

AION plans to network with MAGIS-100 to enhance sensitivity in ULDM/GW searches.

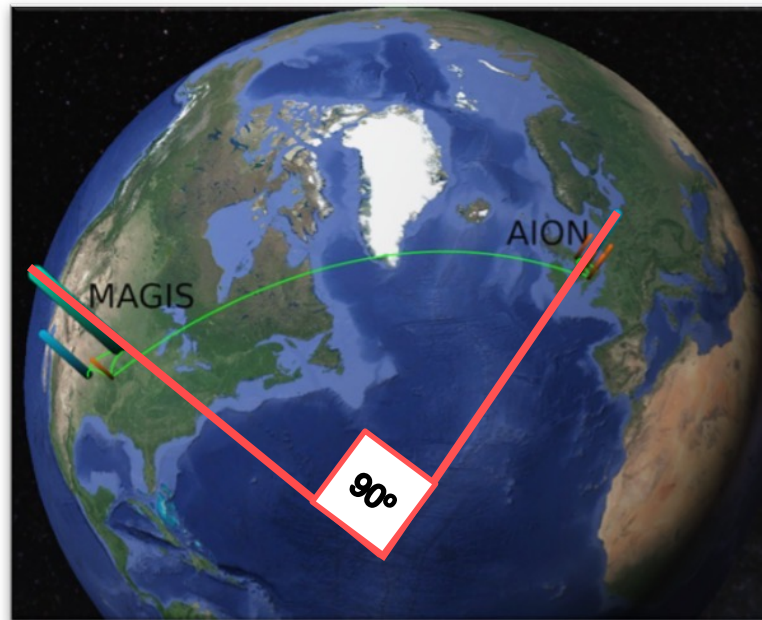


Advantages of networking!

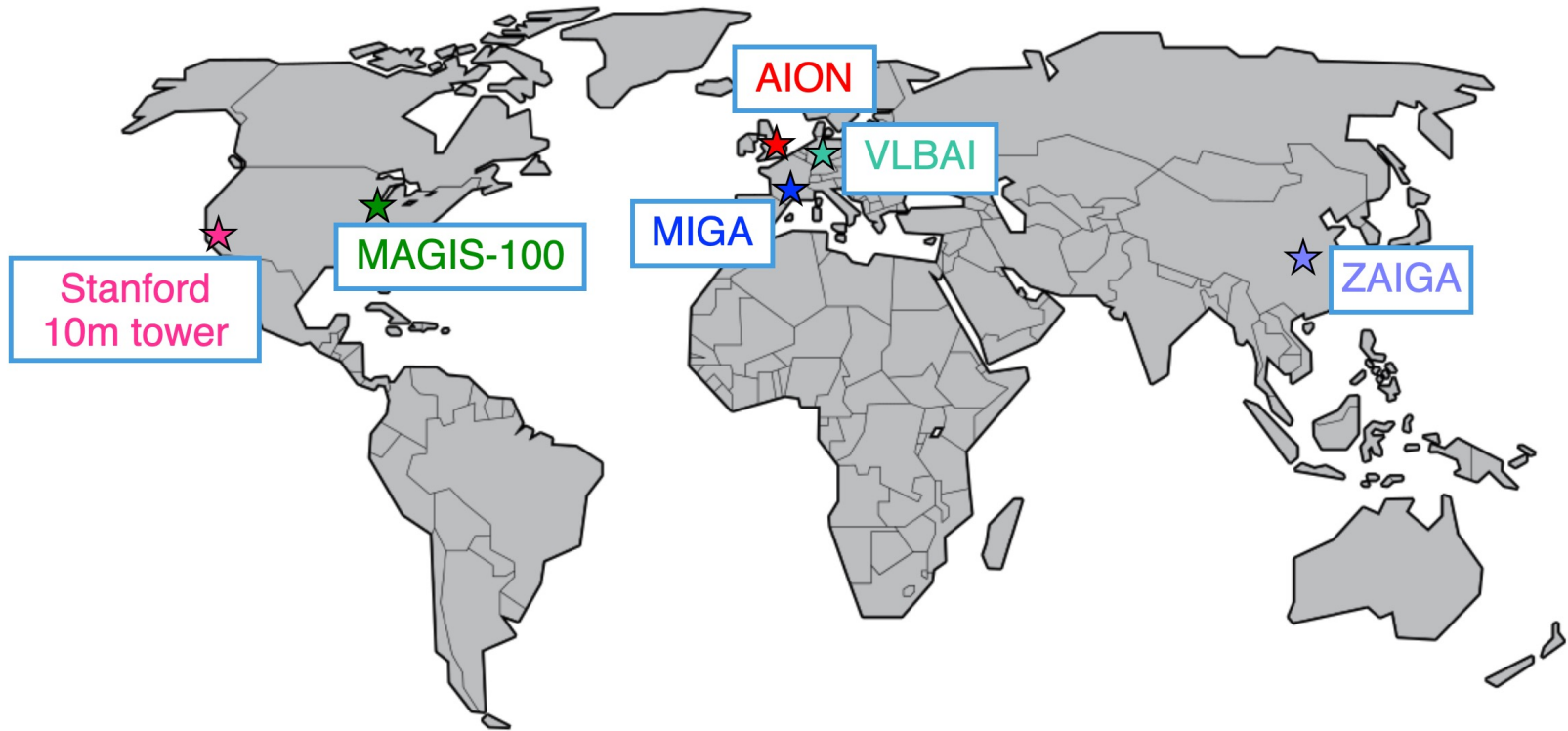
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Distinguish dark matter models through directional dependence.



Progress towards a global network!



Summary



AION is an upcoming atom interferometer experiment, using quantum sensors for detecting ultralight dark matter and gravitational waves – in the ‘mid-band’ between LISA and LIGO.

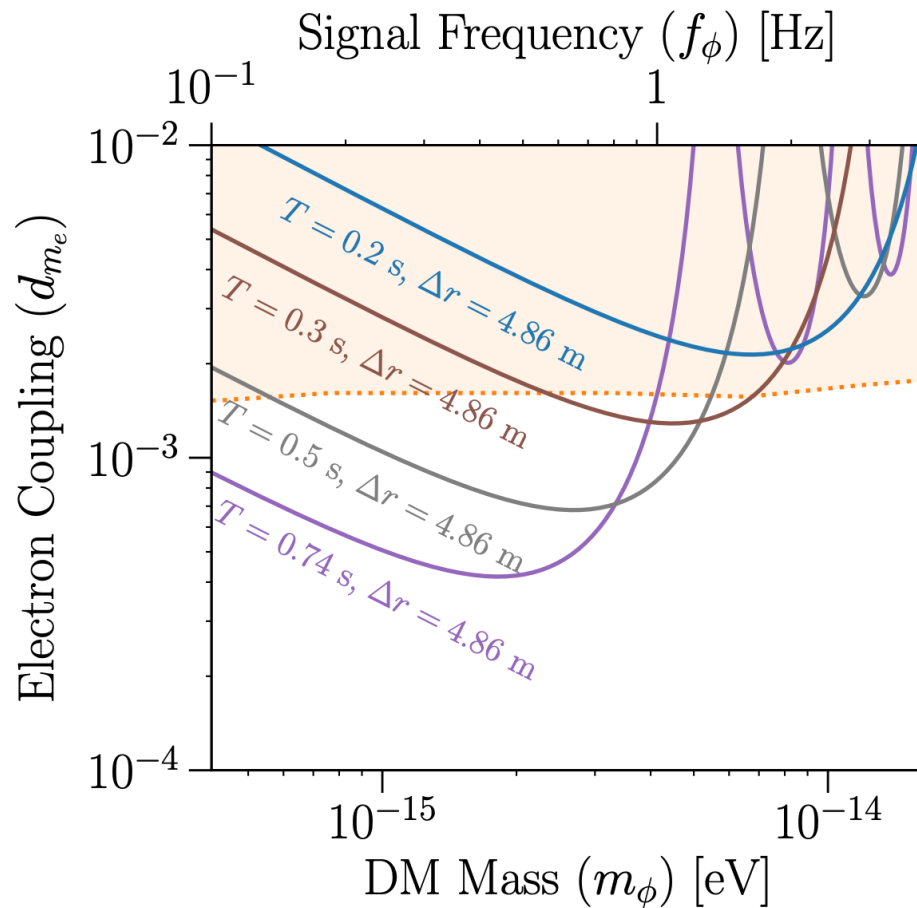
Spin-2 ULDM can be probed by gravitational wave detectors – however, atom interferometers can detect it through two different channels without altering any of the experimental design!

A global network of atom interferometers will enhance these searches further, probing the directional dependence of the field.

Backup

Scalar ULDM sensitivity

❖ *ULDM mass/frequency sensitivity depends on T .*



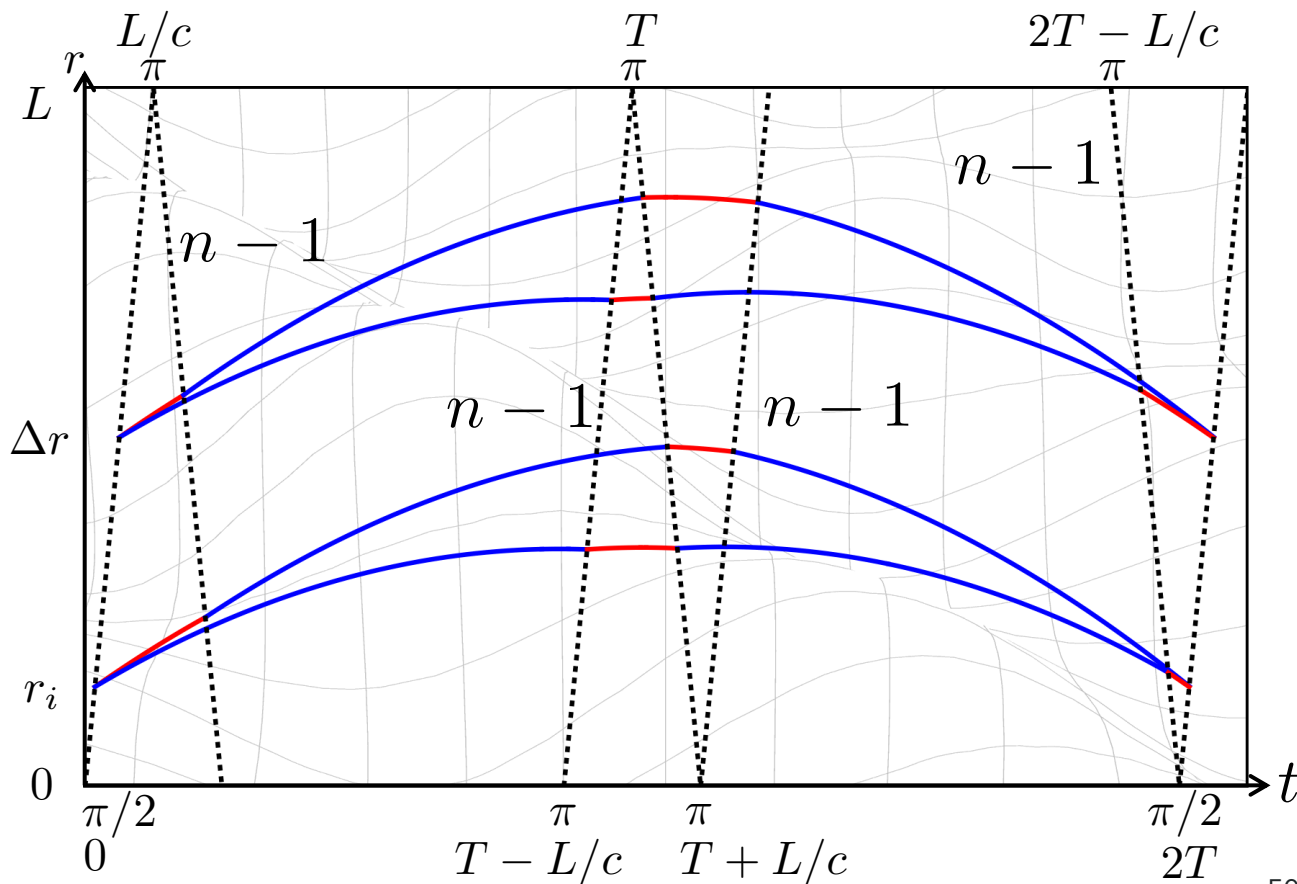
LMT pulses

Additional pulses
enhance sensitivity

$$n = 2$$

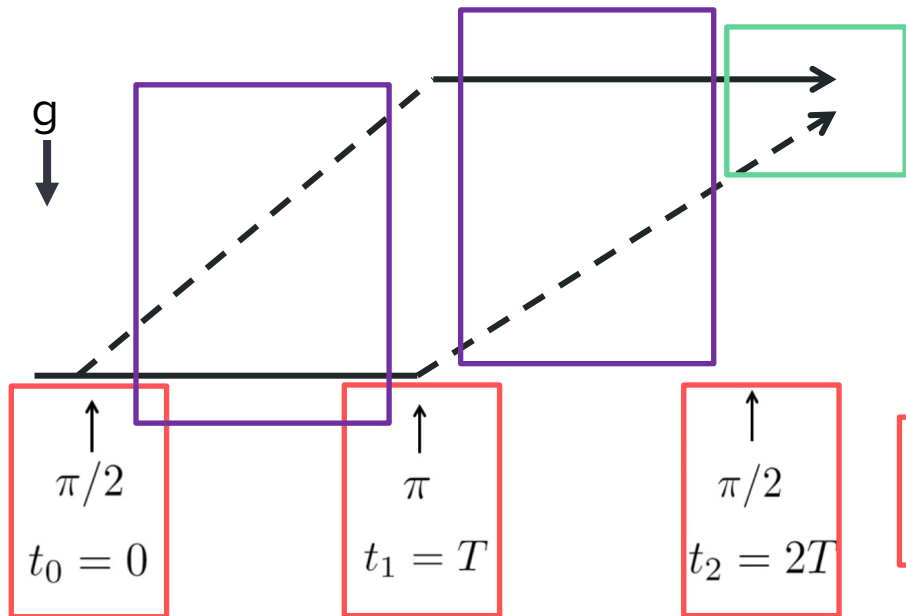
Atom gradiometer

$$\Delta\phi = \phi_1 - \phi_2$$



Phase shifts

$$\phi = \phi_{\text{prop}} + \phi_{\text{sep}} + \phi_{\text{laser}} = kgT^2$$



$$\phi_{\text{prop}} = \frac{1}{\hbar} \left[\sum_u \left(\int_{t_i}^{t_f} (L_c - E_i) dt \right) - \sum_l \left(\int_{t_i}^{t_f} (L_c - E_i) dt \right) \right]$$

$$\phi_{\text{sep}} = \frac{1}{\hbar} \bar{\mathbf{p}} \cdot \Delta \mathbf{z}$$

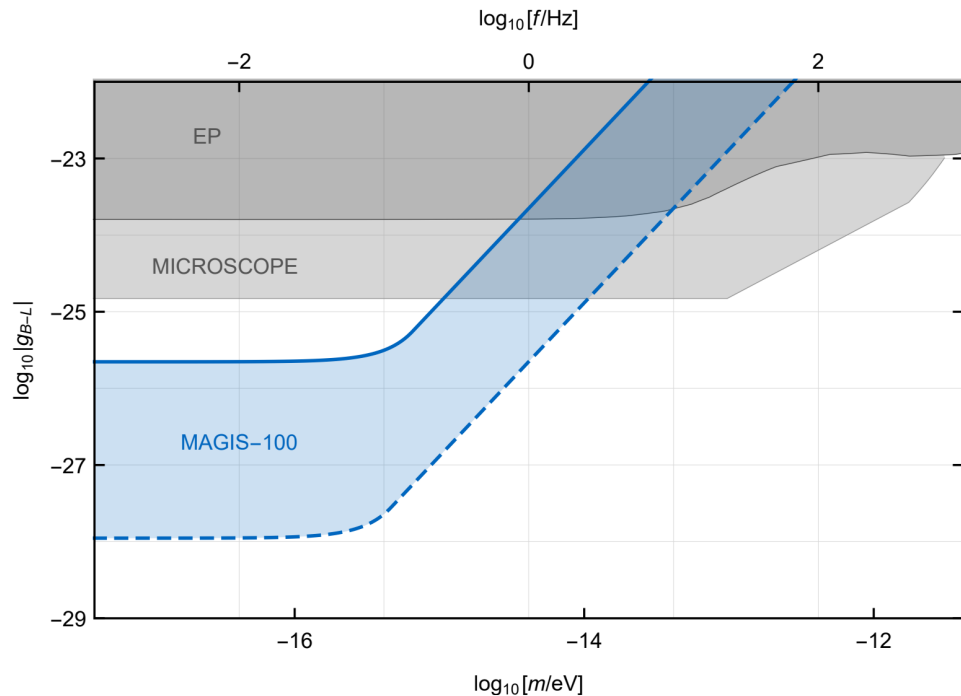
$$\phi_{\text{laser}} = \left(\sum_j \pm \phi_L(t_j, \mathbf{z}_u(t_j)) \right)_u - \left(\sum_j \pm \phi_L(t_j, \mathbf{z}_l(t_j)) \right)_l$$

Spin-1 dark matter

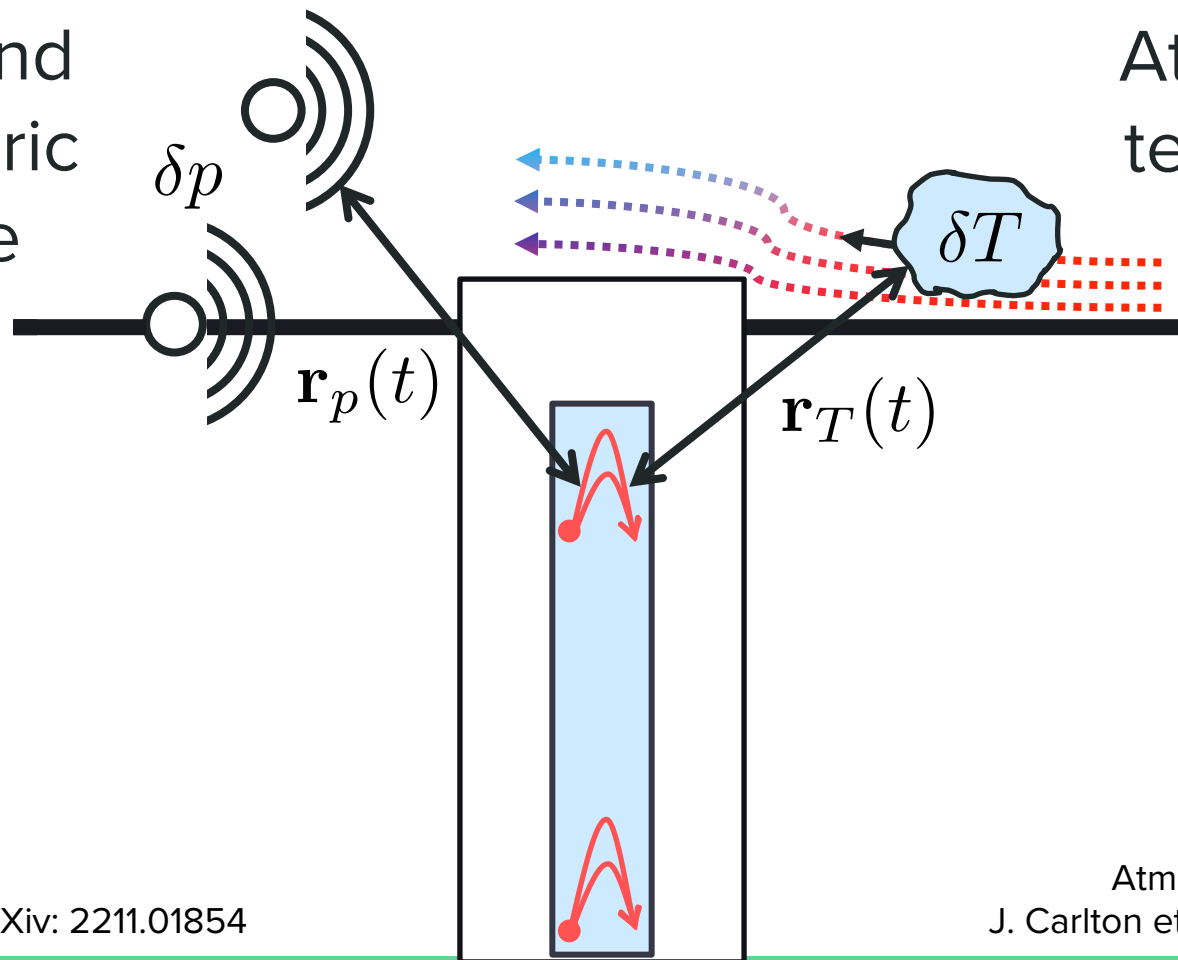
B-L coupling, which generates a 'dark' electric field

$$\Delta F_{B-L} \sim g_{B-L} \left(\frac{Z_1}{A_1} - \frac{Z_2}{A_2} \right) E_{B-L}$$

Probe with a dual-species interferometer



Seismic and
atmospheric
pressure



Atmospheric
temperature

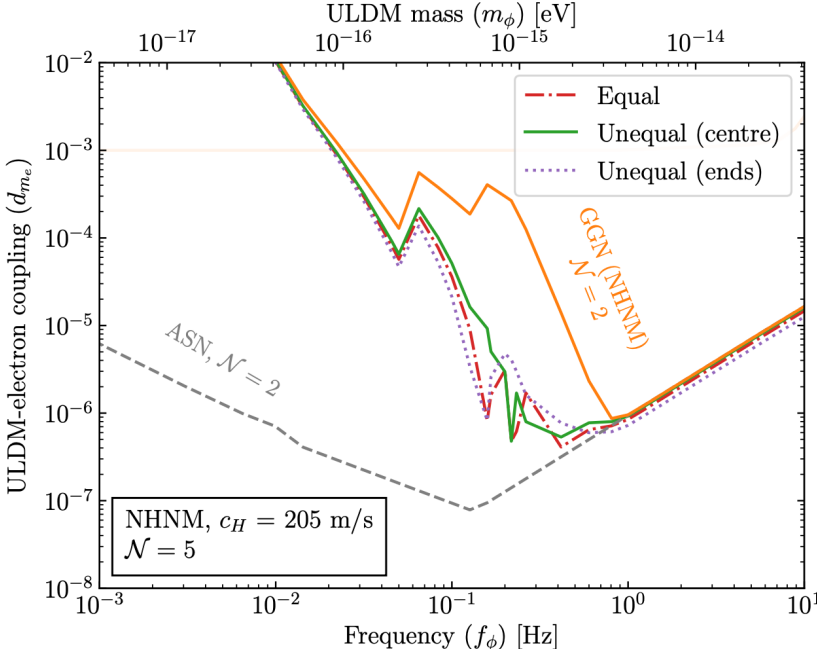
Seismic noise:

L. Badurina et al. arXiv: 2211.01854

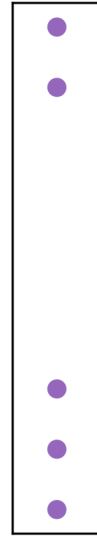
Atmospheric noise:

J. Carlton et al. *In progress*

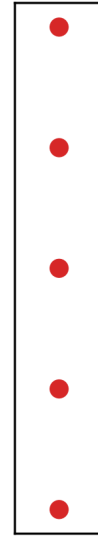
GGN vs Multi-gradiometry



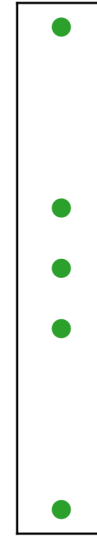
Unequal (ends)



Equal



Unequal (centre)



Height

The AION-10 Experiment



University of Oxford, Beecroft Building

The AION-10 Experiment



The AION-10 Experiment



All these people
are a problem!



Anthropogenic and synanthropic noise

Many potential sources of noise surround the detector:

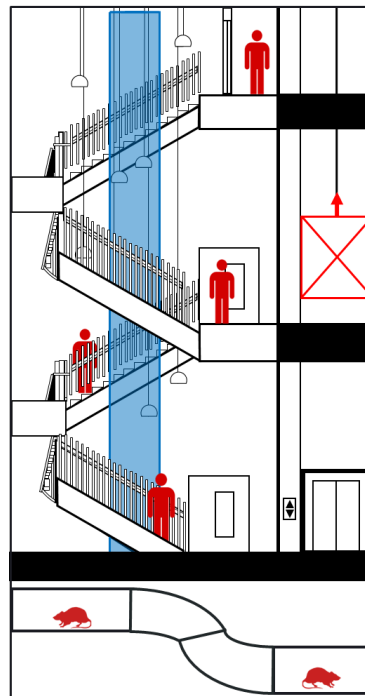
Large anthropogenic sources

- People walking on the stairs/in the foyer
- Traffic on the road outside
- Lift moving next to the tower

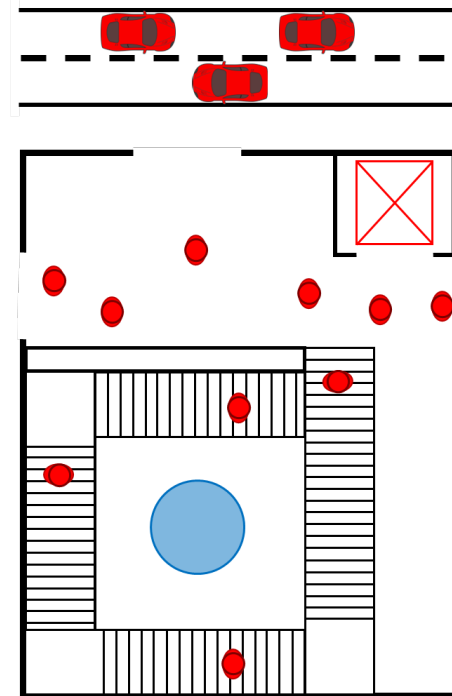
Small synanthropic sources

- Random animal transients (RATs)

Side-on view



Top-down view



Anthropogenic and synanthropic noise

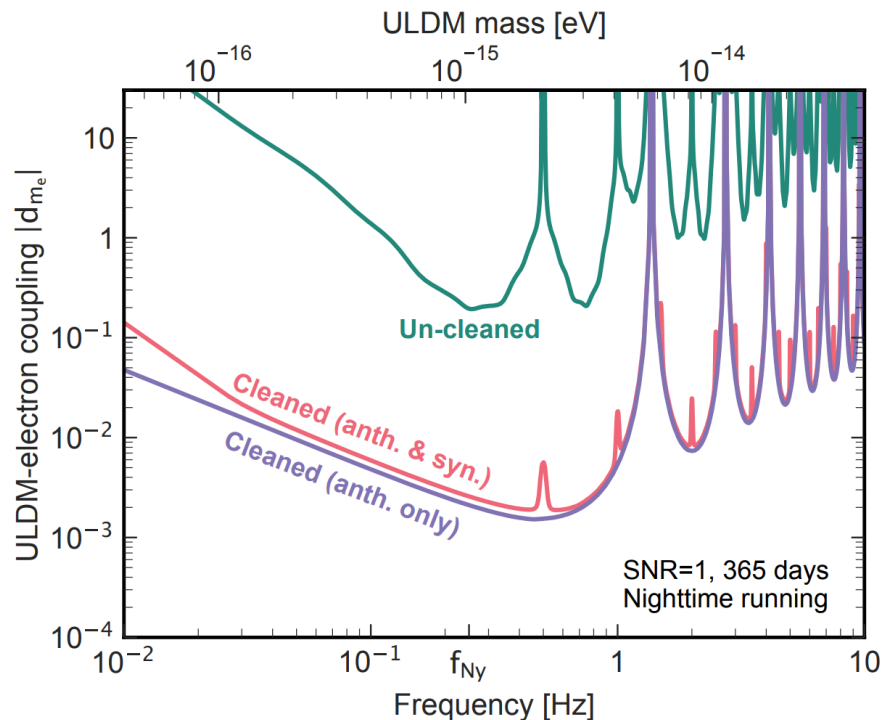
Many potential sources of noise surround the detector:

Large anthropogenic sources

People walking on the stairs/in the foyer
Traffic on the road outside
Lift moving next to the tower

Small synanthropic sources

Random animal transients (RATs)



J. Carlton, C. McCabe

Phys.Rev.D (108, 123004); arXiv: 2308.10731 [astro-ph.CO]

AION-10 sensitivity projections

$$d_{m_e}^{\text{best}} \sim \left(\frac{1}{T}\right)^{5/4} \frac{1}{C n \Delta r} \left(\frac{\Delta t}{N_a}\right)^{1/2} \left(\frac{1}{T_{\text{int}}}\right)^{1/4}$$

Handles to optimise (in order of priority):

$T \sim 1$ s (interrogation time)

$C \sim 0.1 - 1$ (contrast)

$n \sim 1000$ (LMT)

$\Delta r \sim \text{AI separation}$

$\Delta t \sim \text{sampling time}$

$N_a \sim \text{atoms in cloud}$

$T_{\text{int}} \sim 10^7$ s (integration time)

