

*Primordial Black Holes:
Positivist Perspective and
Quantum Quiddity*

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Garching (near Munich), Germany*

— GEMMA 2, La Sapienza, Rome —

Tuesday, the 17th of September 2024

A decorative frame with scrollwork at the corners and a wavy top and bottom border. The text is centered within this frame.

Primordial Black Hole

Formation Primer

PBH Formation Mechanisms

★ Large density perturbations (inflation)

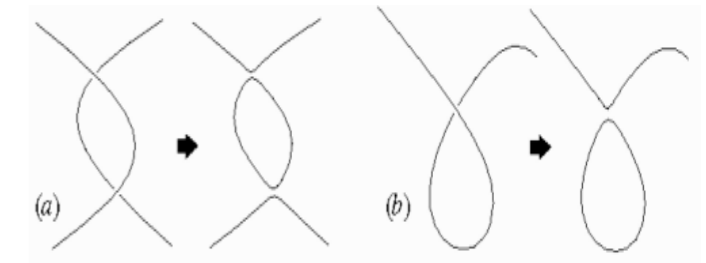
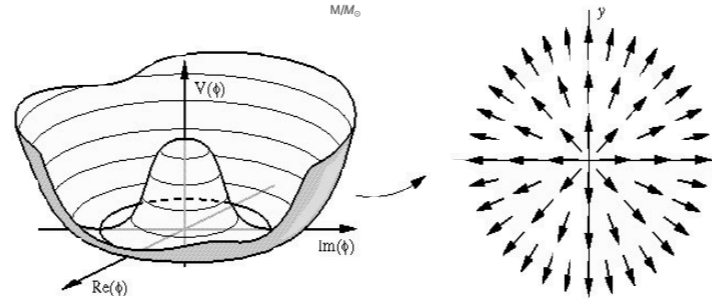
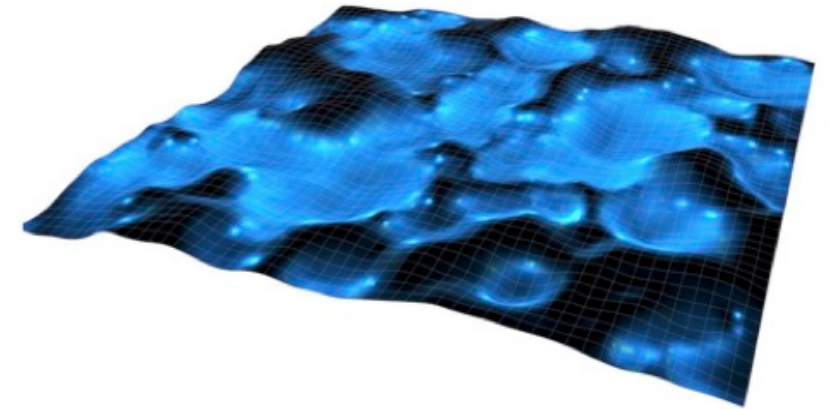
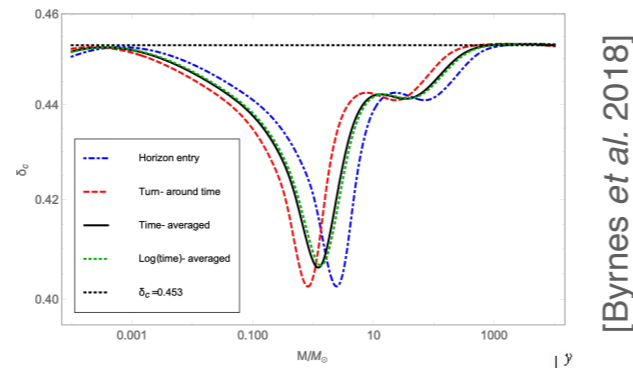
★ Pressure reduction

★ Cosmic string loops

★ Bubble collisions

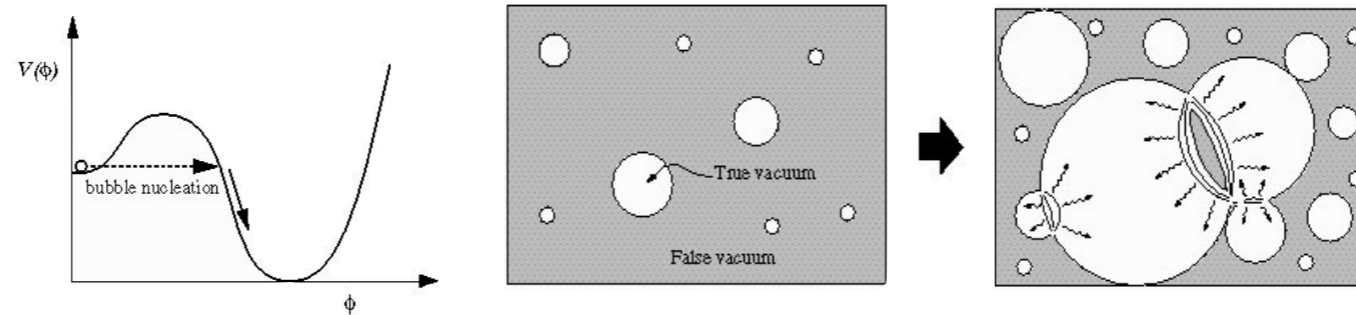
★ Quark confinement

★ Scalar-field fragmentation, ...

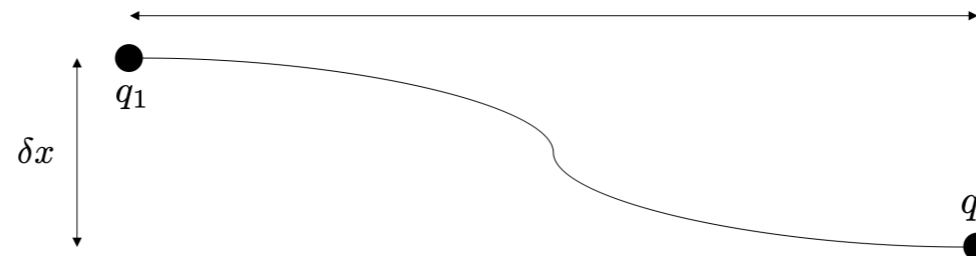


http://www.damtp.cam.ac.uk/research/gr/public/cs_phase.html

http://www.damtp.cam.ac.uk/research/gr/public/cs_top.html

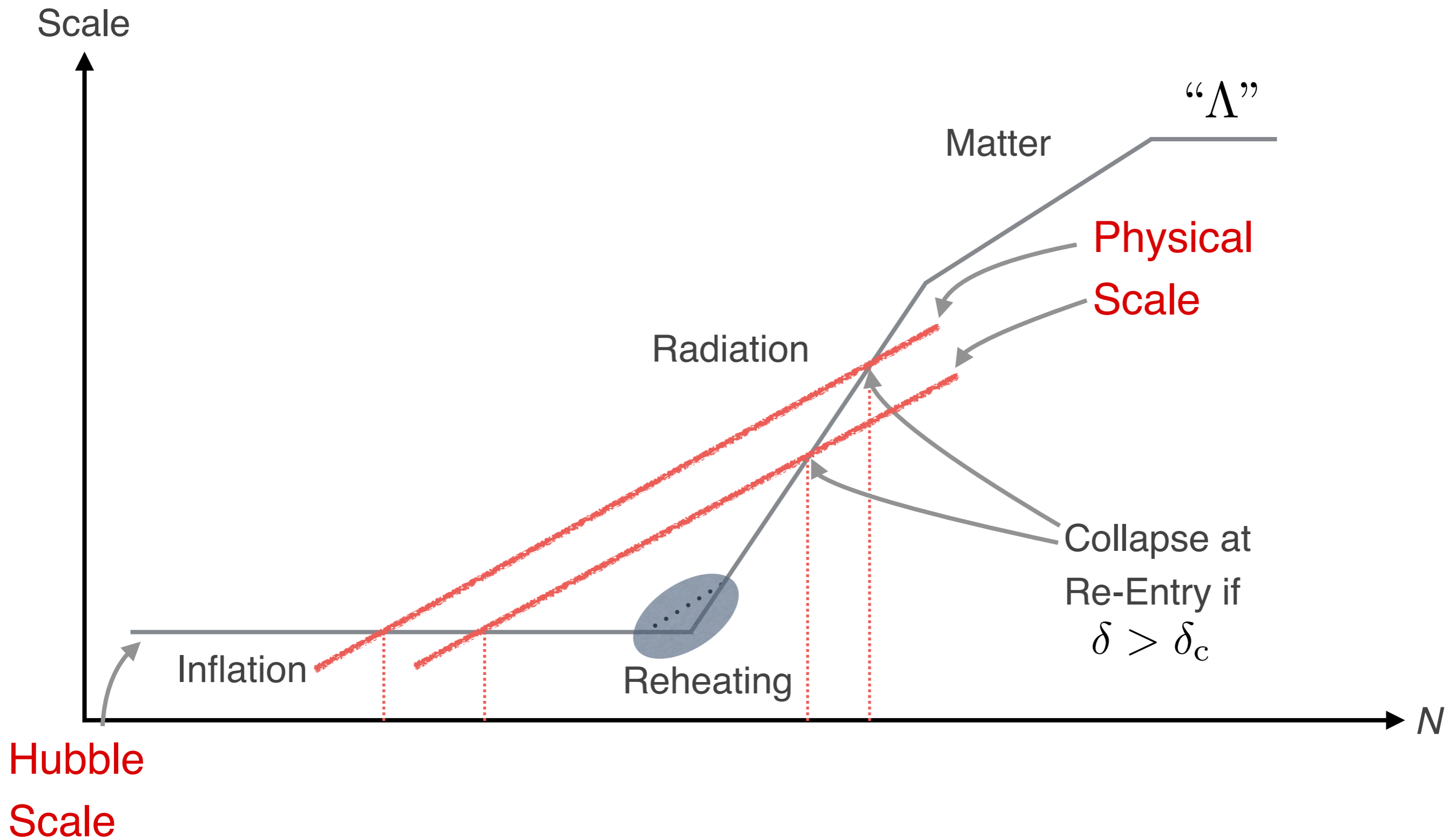


$d \simeq t$

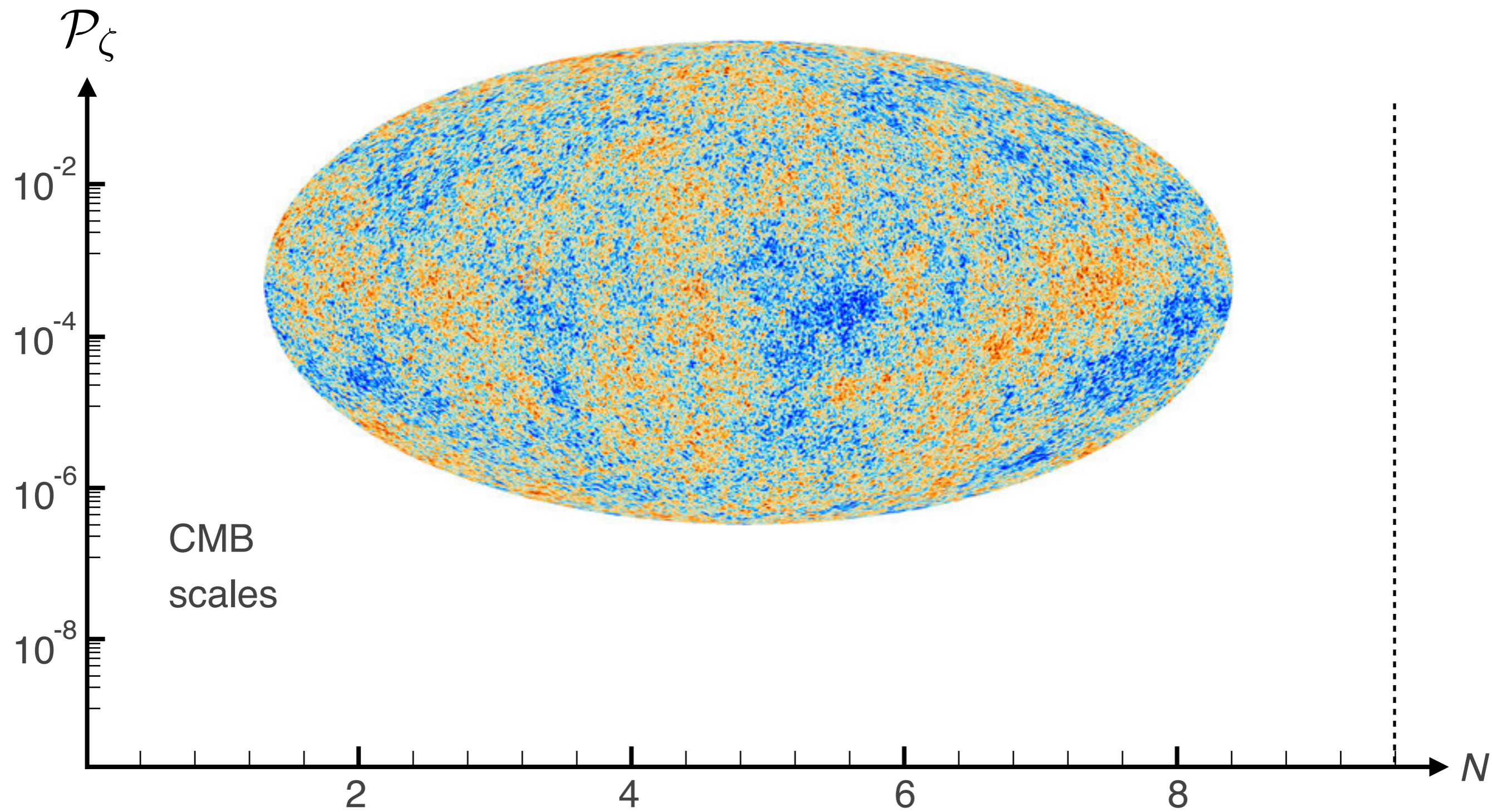


[Dvali, FK, Zantedeschi 2021]

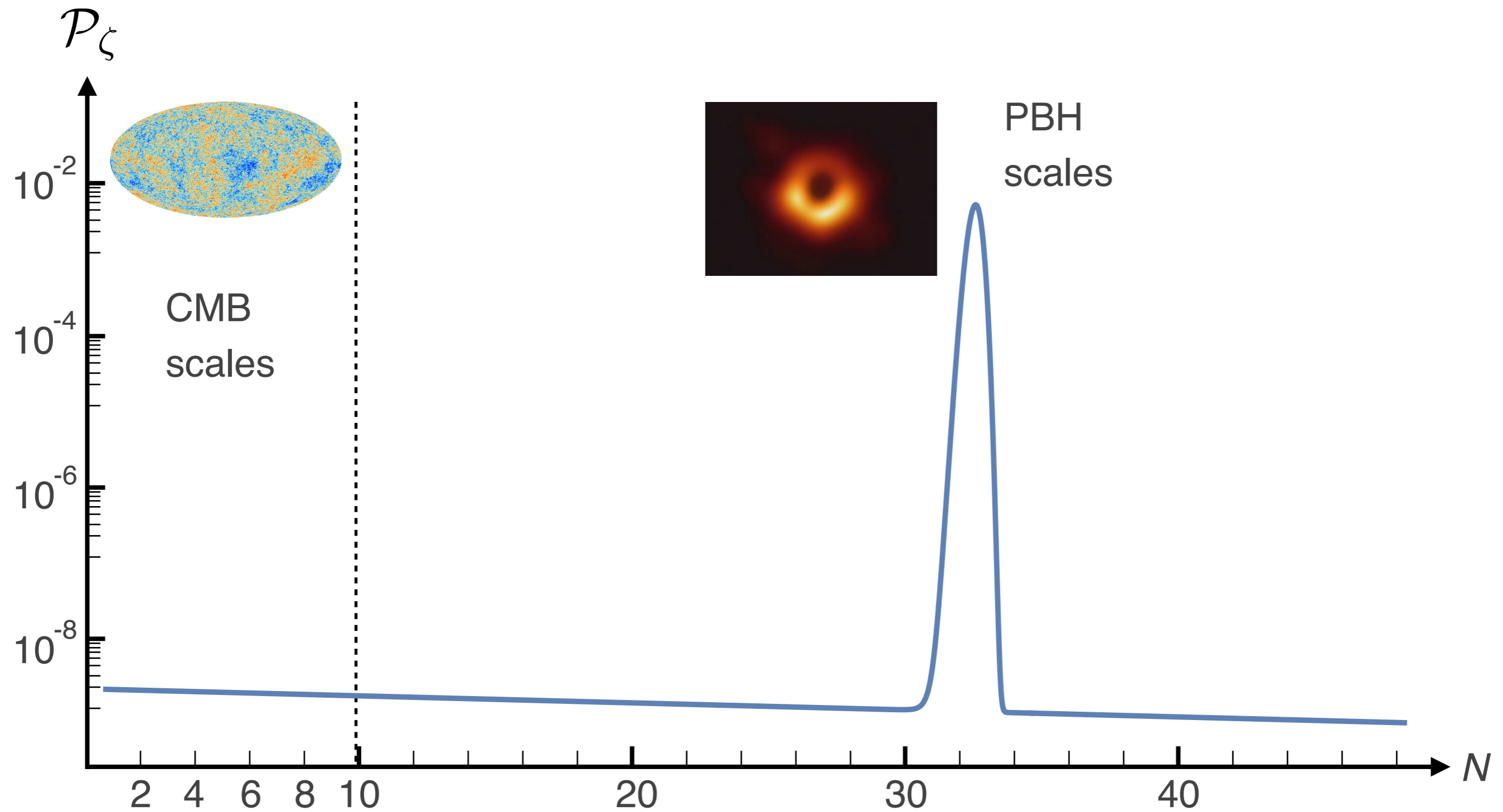
PBH Formation from Inflationary Overdensities



PBH Formation — Scales



PBH Formation — Scales



PBH Formation — Rare Events

Fraction of collapsed horizon patches:

$$\beta \sim \text{erfc} \left(\frac{\delta_c}{2\sigma} \right)$$

Latest research points towards a shallower tail (c.f. quantum diffusion).

rare events:
typically $\sim 10\sigma$

density contrast

$$\delta \equiv \frac{\rho - \rho_{\text{background}}}{\rho_{\text{background}}}$$

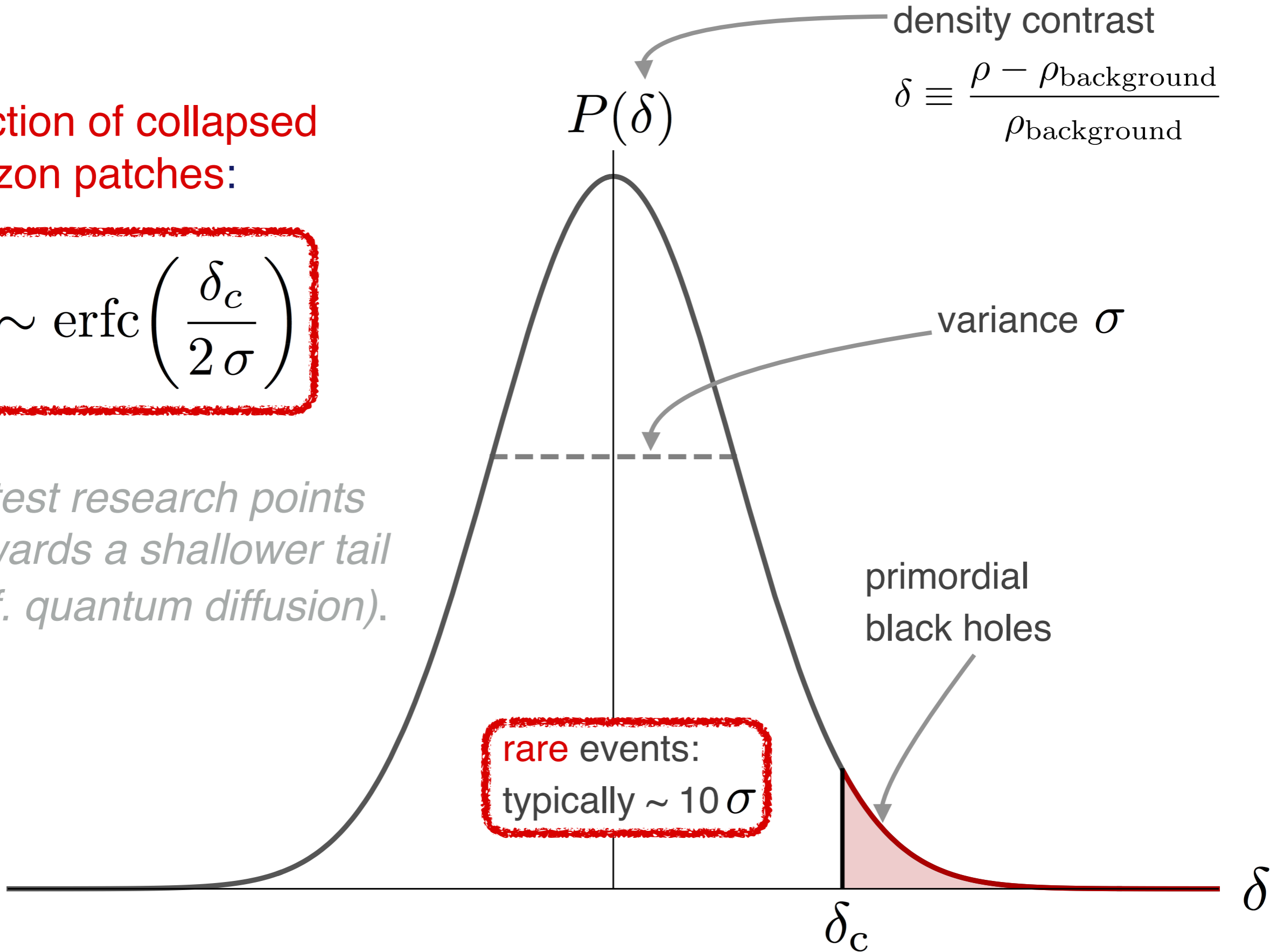
$P(\delta)$

variance σ

primordial black holes

δ_c

δ



PBHs — Some Numbers

★ If **primordial black holes** constituted **all** of the **dark matter**:

★ Assume that all PBH have mass: 10^{20} g



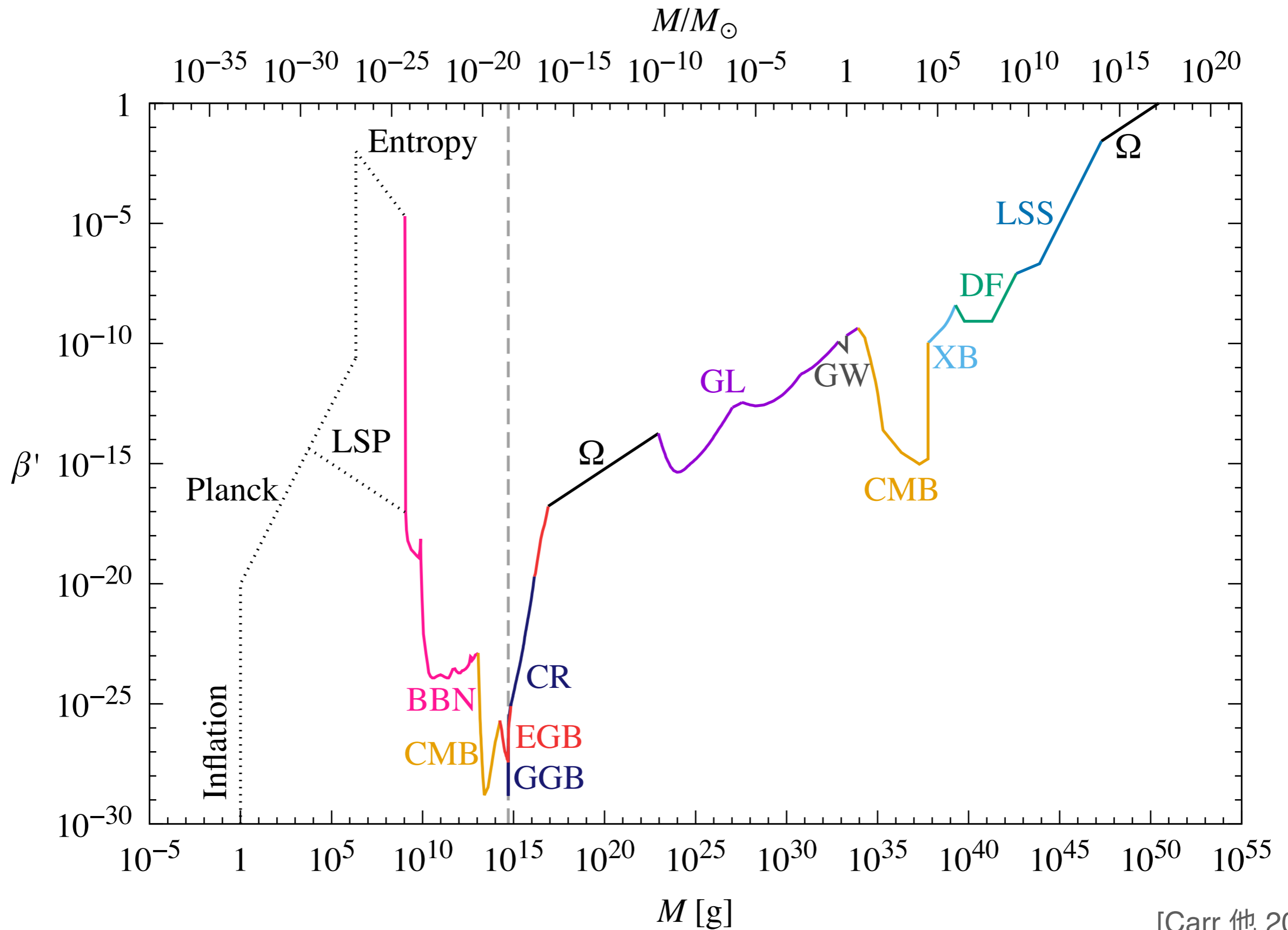
Saturn satellite
Prometheus



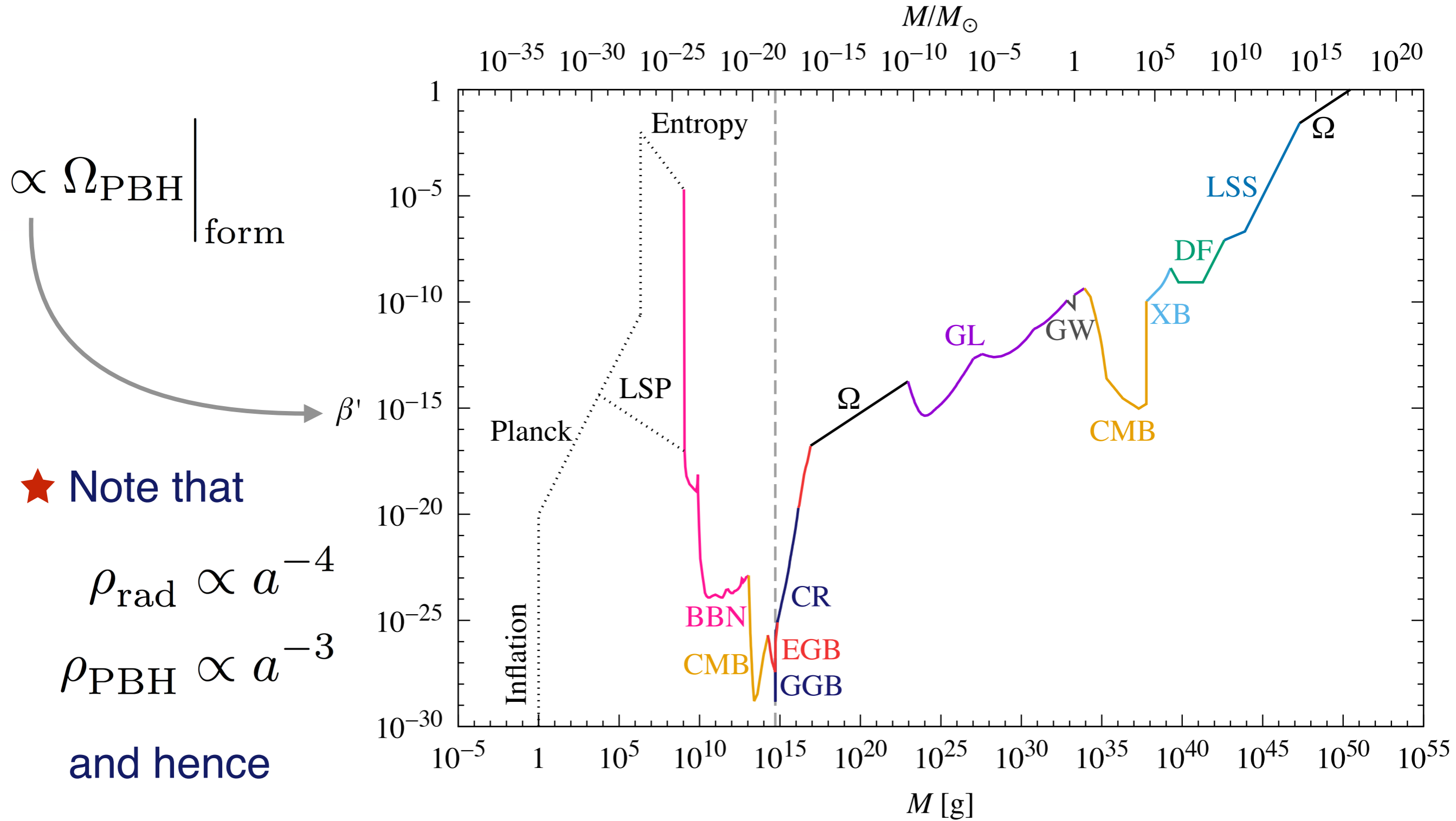
Primordial Black Hole

Constraints

PBH Constraints at Formation

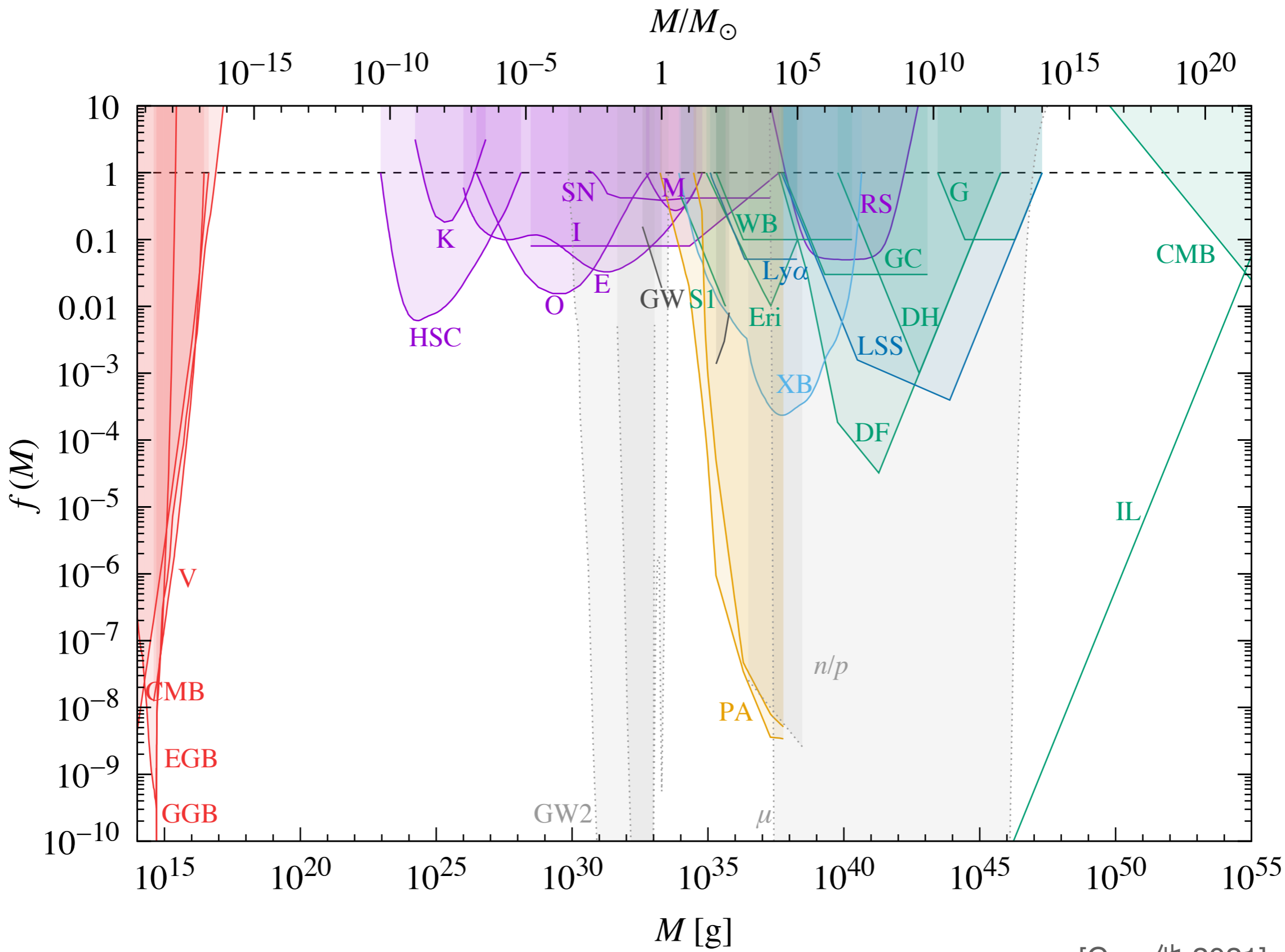


PBH Constraints at Formation



[Carr 他 2021]

Current PBH Constraints



[Carr 他 2021]



*Observational Hints for
Primordial Black Holes*



Evidence?
Observational ~~Hints~~ for
Primordial Black Holes

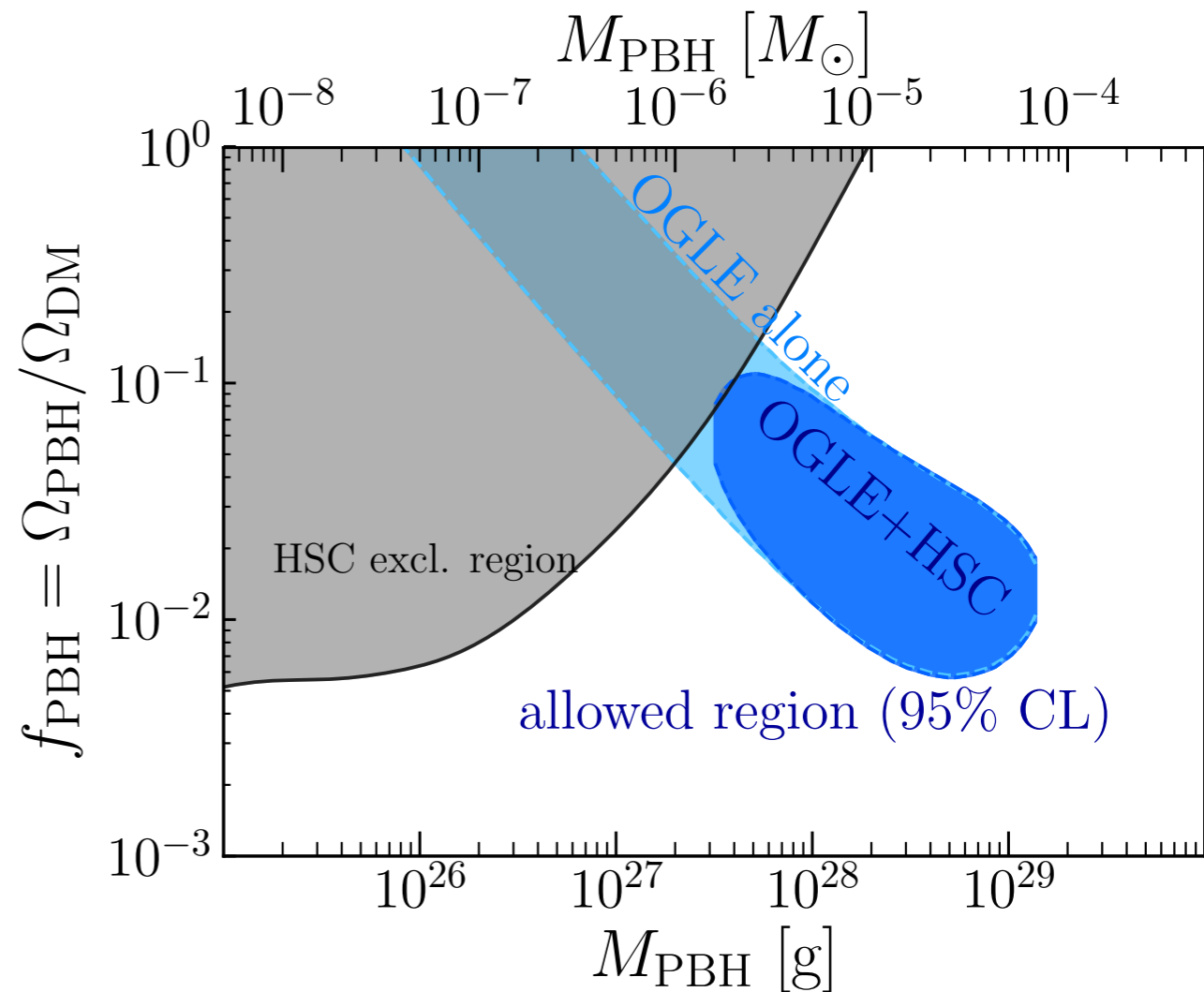
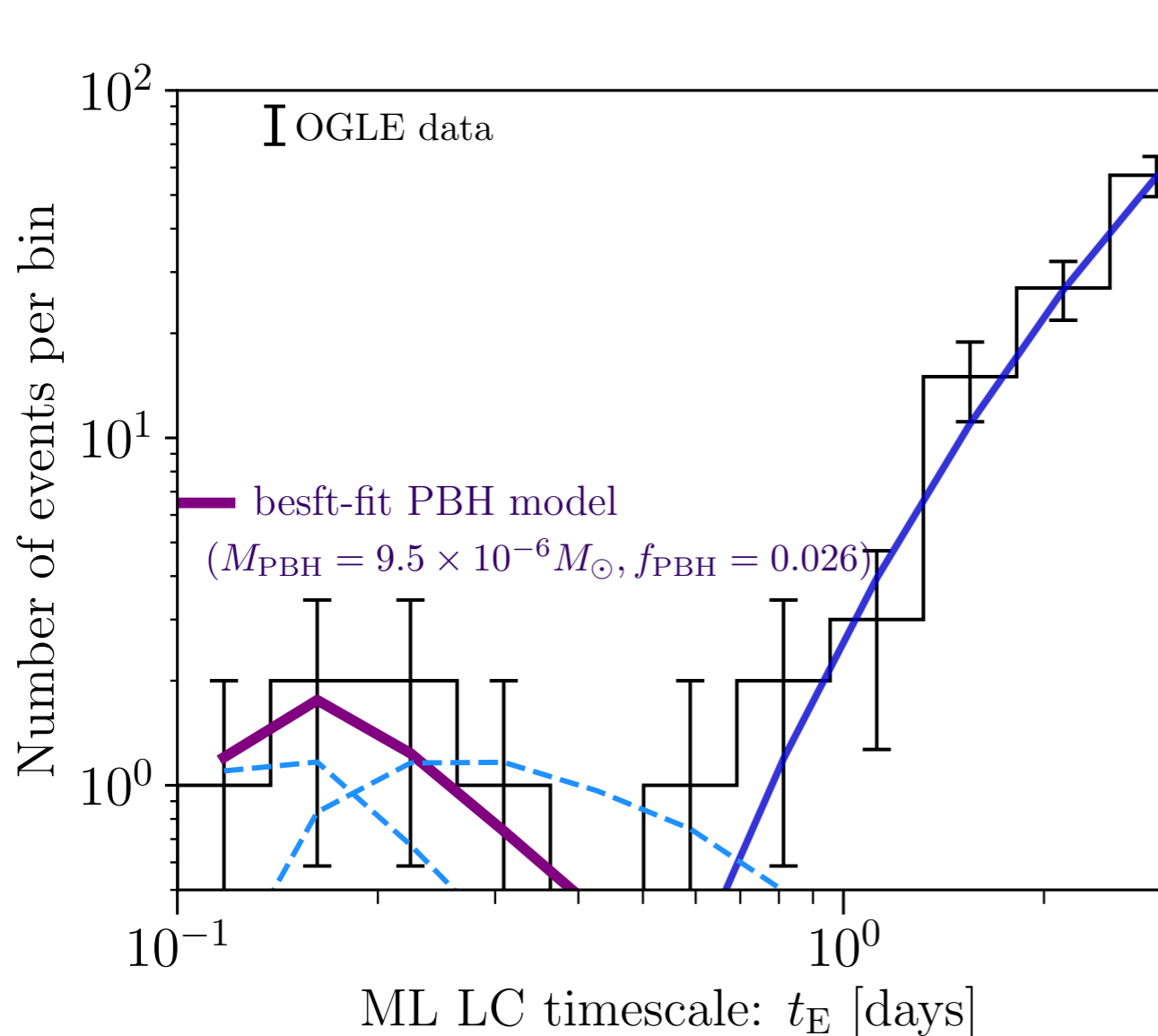
*work with Carr, Clesse,
García-Bellido, Hawkins

Planetary-Mass Microlensing

★ OGLE detected a particular **population** of microlensing events:

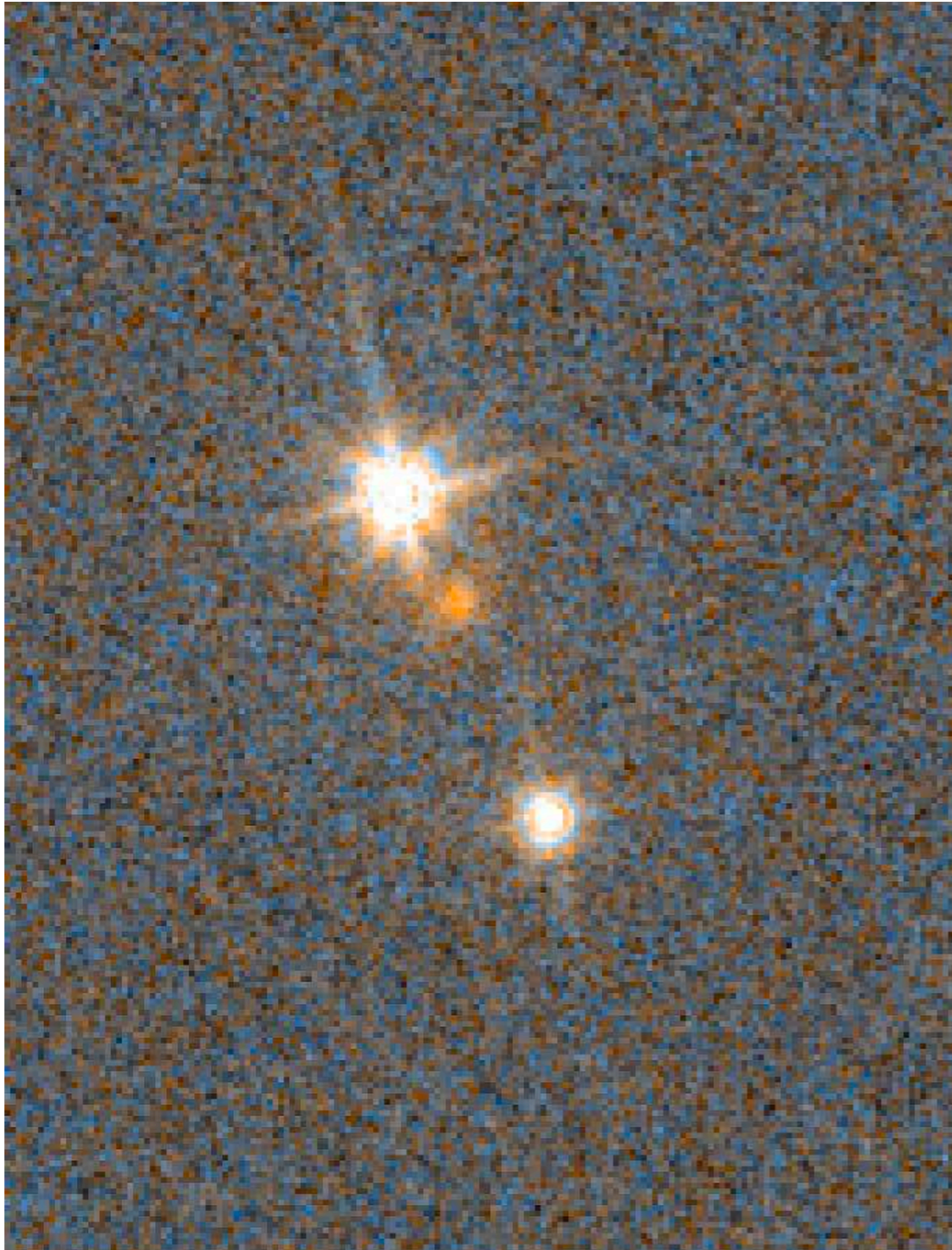
★ **0.1 - 0.3 days** light-curve timescale - origin **unknown!**

Could be free-floating planets... or **PBHs!**



[Niikura, Takada, Yokoyama, Sumi, Masaki 2019]

Quasar Microlensing



HST image of lensed quasar HE1104–1805

The signature of primordial black holes in the dark matter halos of galaxies

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Institute for Astronomy (IfA), University of Edinburgh, Royal Observatory, Blackford Hill, Edinburgh EH9 3HJ, UK
e-mail: mrsh@roe.ac.uk

ABSTRACT

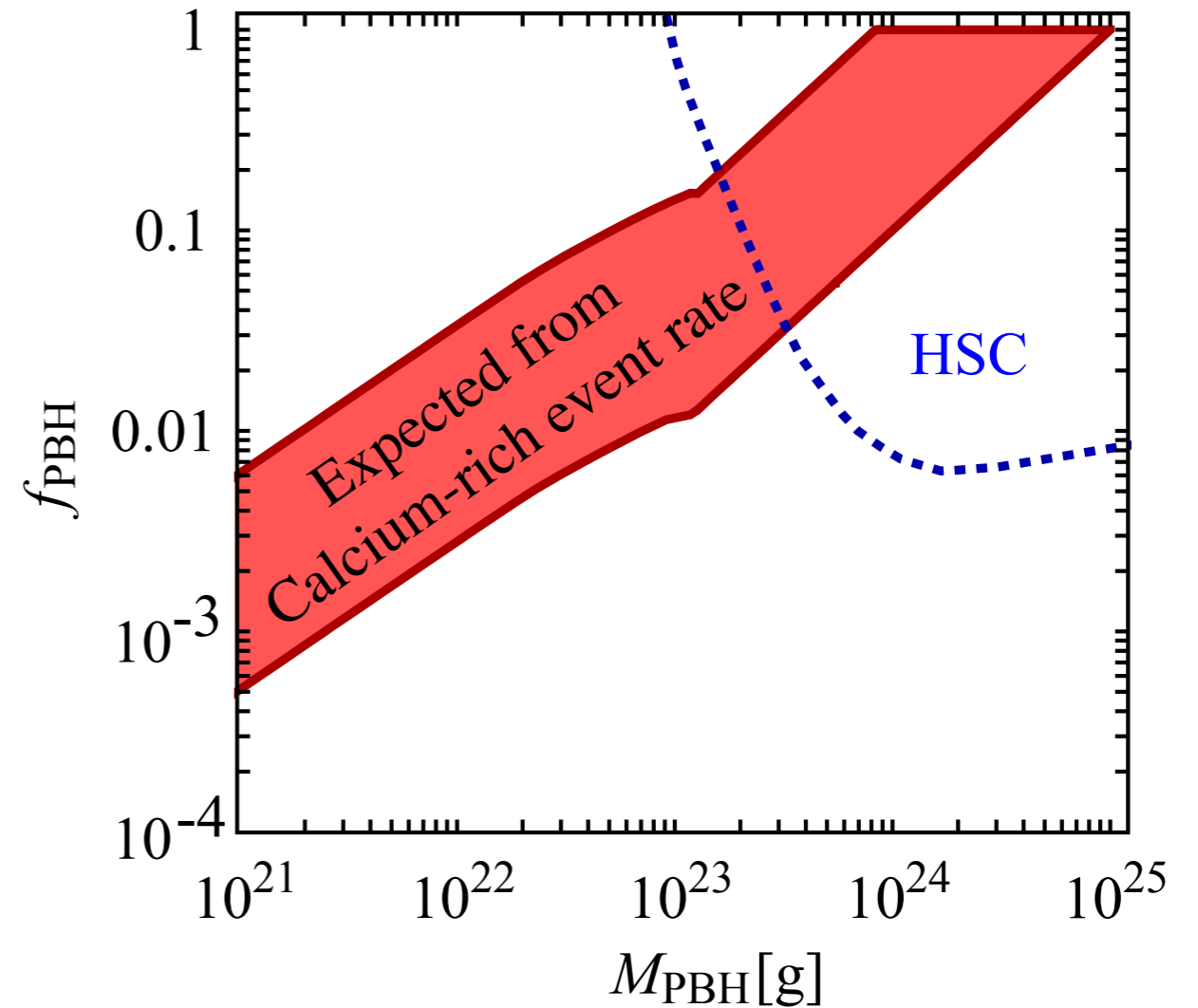
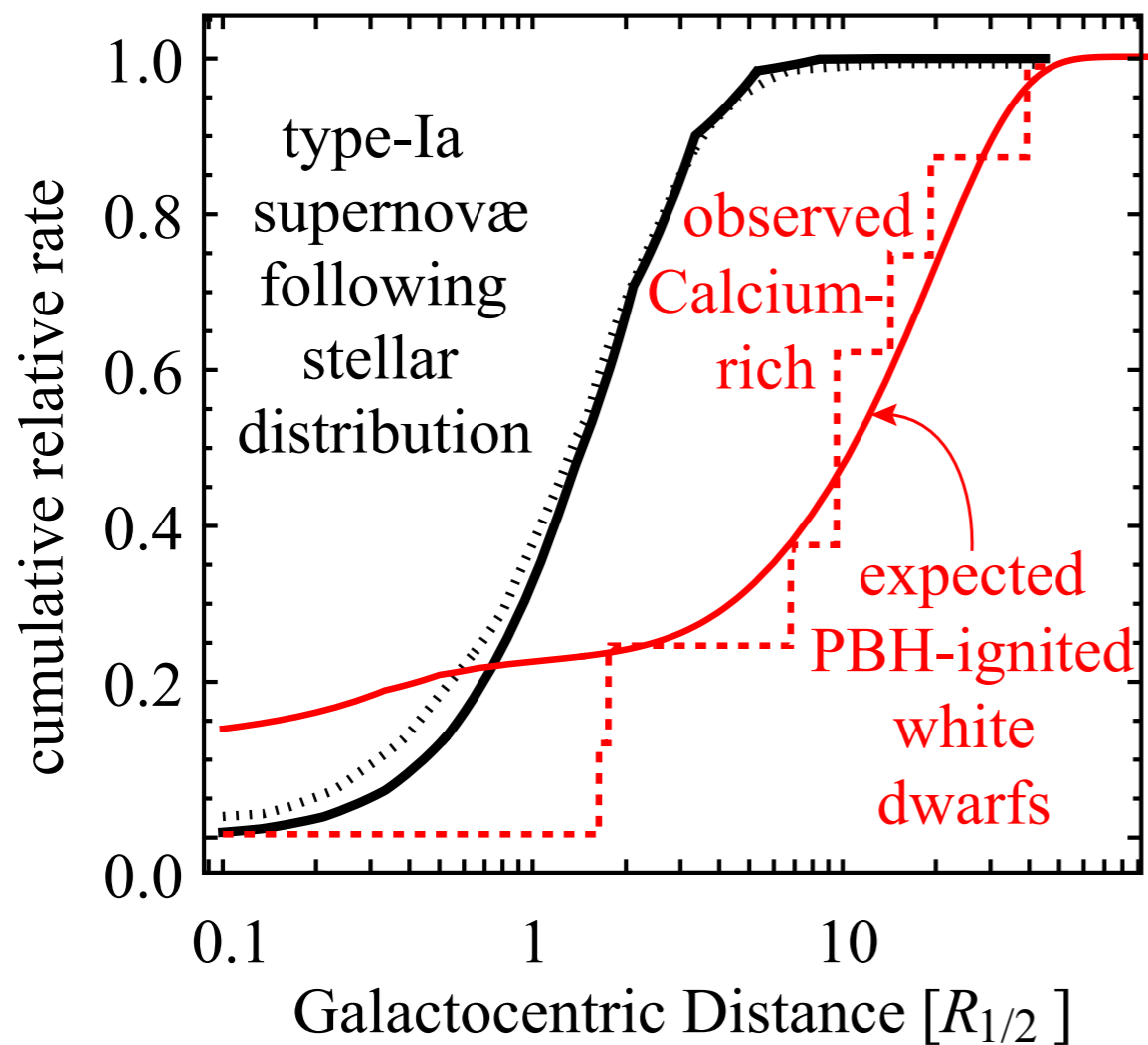
Aims. The aim of this paper is to investigate the claim that stars in the lensing galaxy of a gravitationally lensed quasar system can always account for the observed microlensing of the individual quasar images. [...]

Results. Taken together, the probability that all the observed microlensing is due to stars was found to be $\sim 3 \times 10^{-4}$. Errors resulting from the surface brightness measurement, the mass-to-light ratio, and the contribution of the dark matter halo do not significantly affect this result.

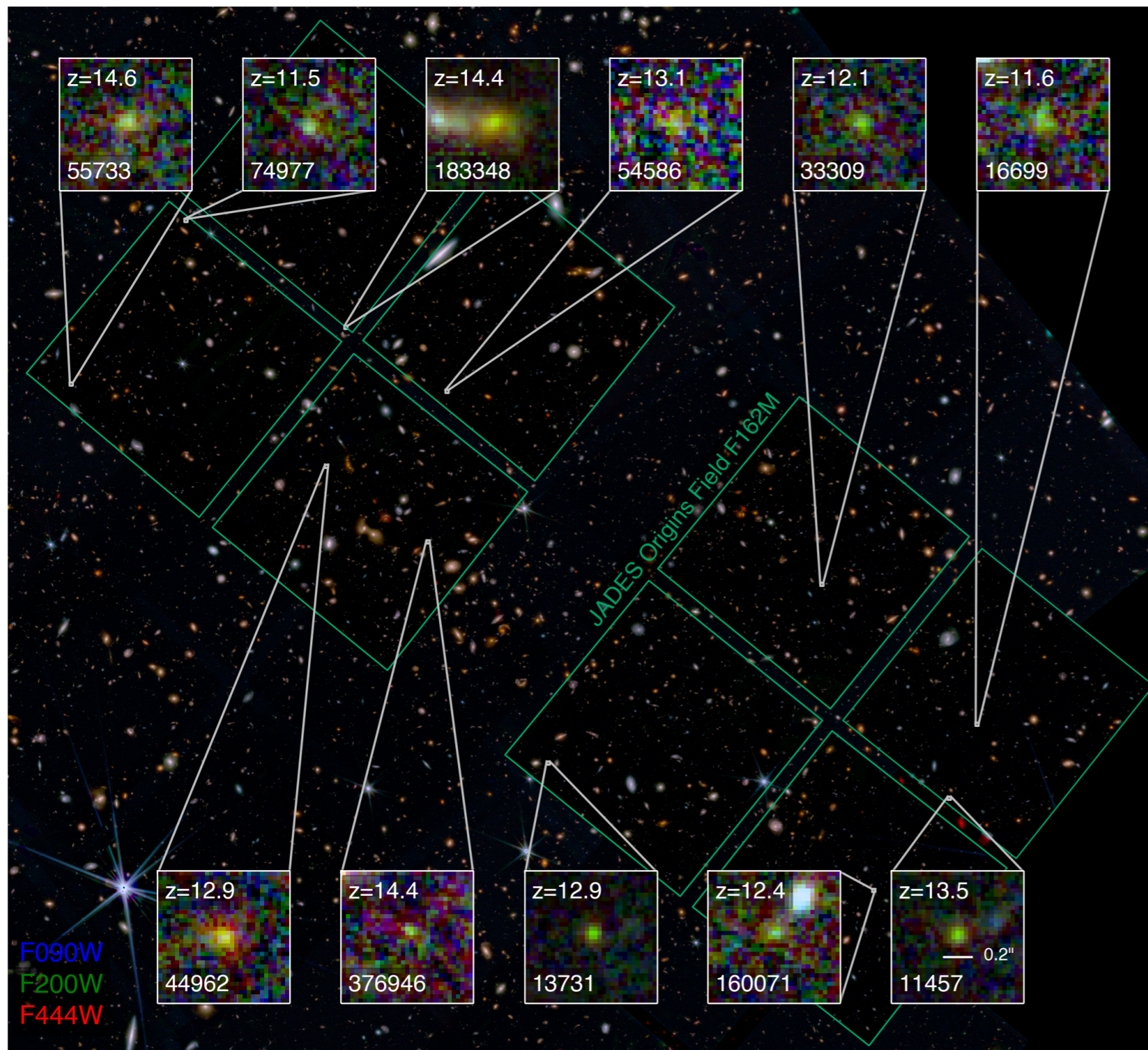
Conclusions. It is argued that the most plausible candidates for the microlenses are primordial black holes, either in the dark matter halos of the lensing galaxies, or more generally distributed along the lines of sight to the quasars.

Calcium-Rich Gap Transients

- ★ A supernova population of so-called calcium-rich gap transients has been shown to **clearly not to follow the stellar distribution but rather a would-be compact dark matter one.**



High-Redshift Galaxies



- ★ JWST confirmed a galaxy at $z \simeq 14$.
- ★ It is unclear whether baryonic physics alone could explain its evolution within only 300 Myr!
- ★ PBH dark matter would trigger early formation, easily ensuring compatibility with observations.

GRAVITATIONAL WAVE MERGER DETECTIONS

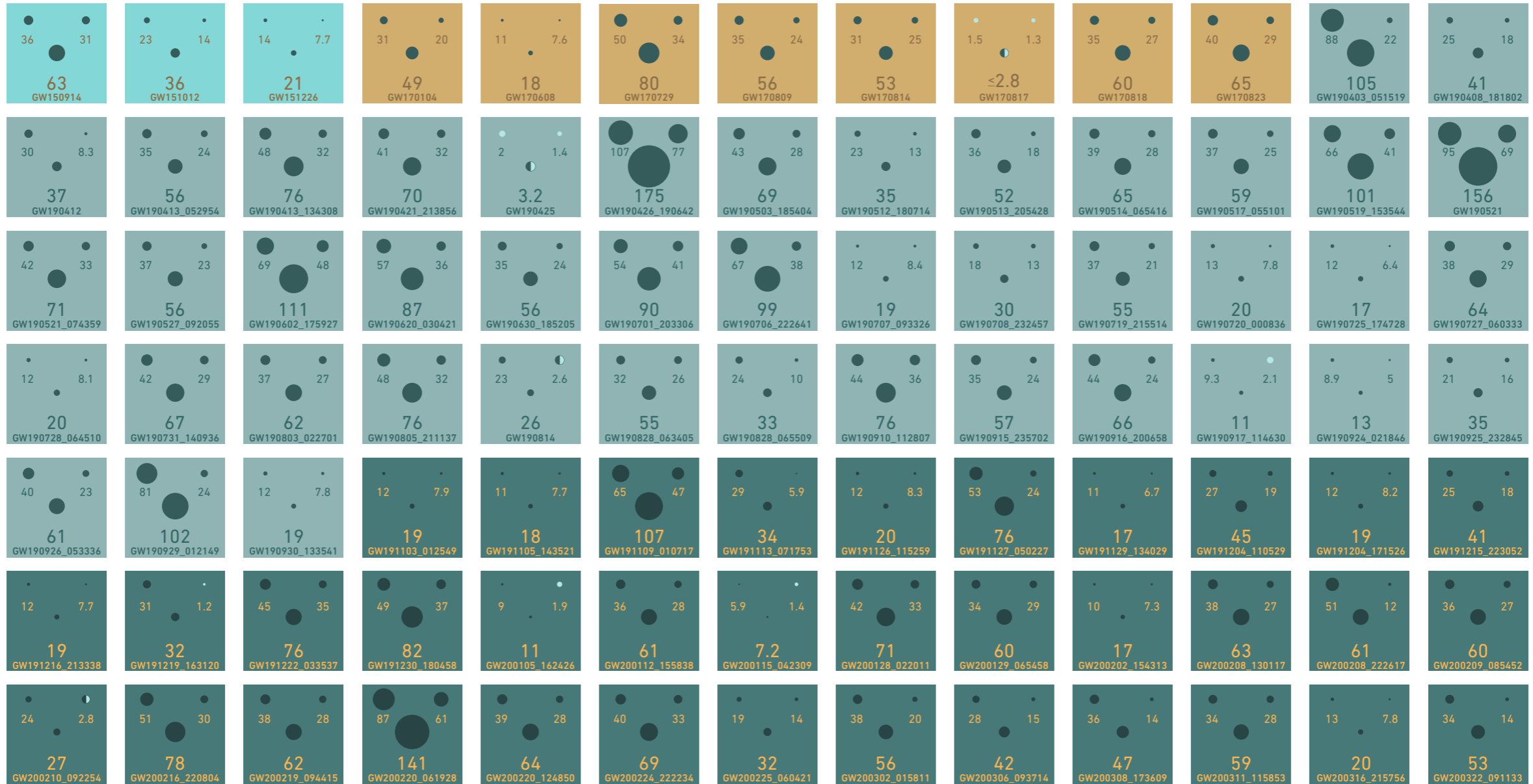
→ SINCE 2015

OBSERVING RUN

01 2015-2016

02 2016-2017

03a+b 2019-2020



GRAVITATIONAL WAVE MERGER DETECTIONS

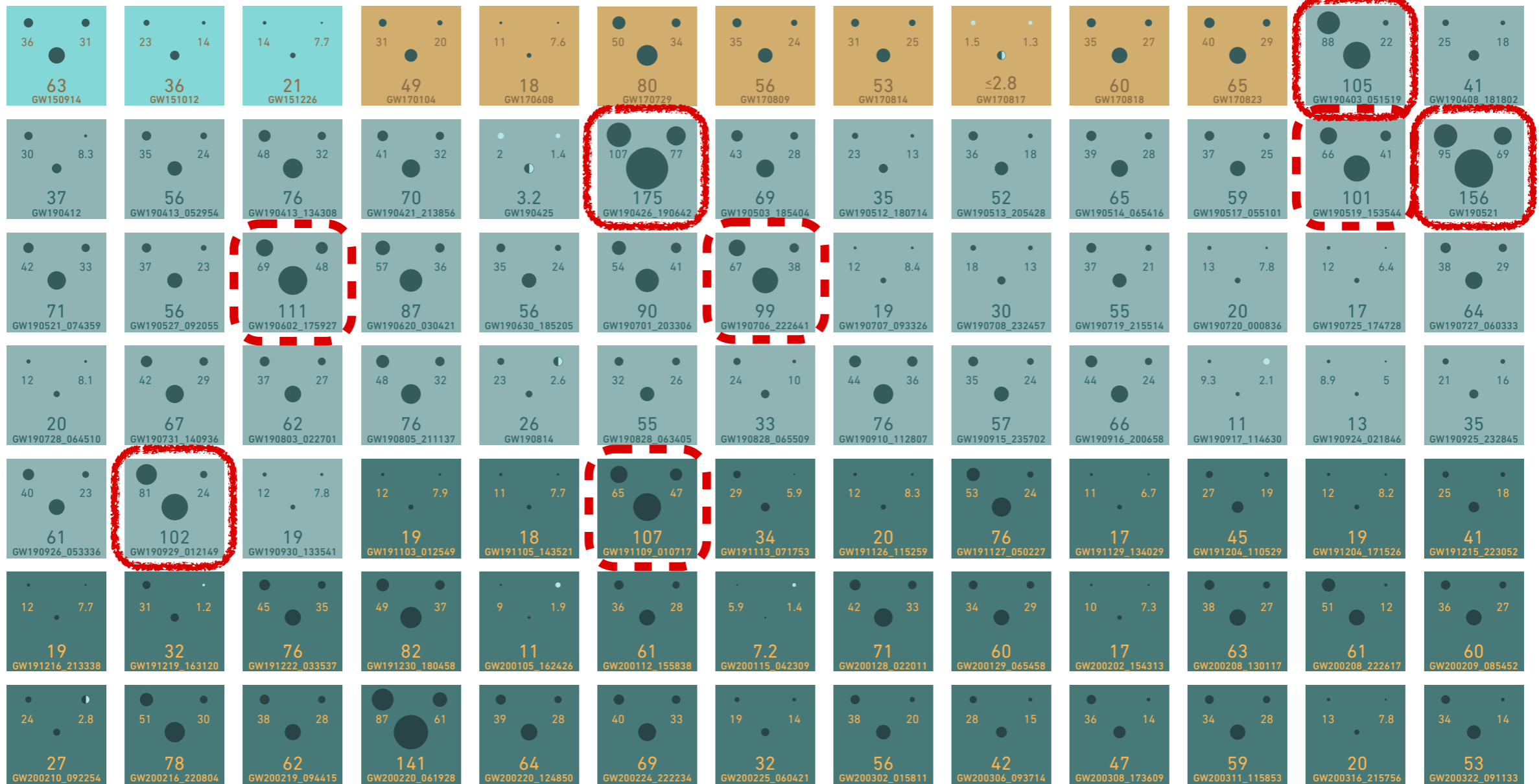
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★ Black hole progenitors in the **pair-instability mass gap** (i.e. above $\sim 60 M_{\odot}$)



Subsolar Black Holes - The Smoking Gun!

★ Recent reanalysis of LIGO data updated merger rates and low mass ratios:

Date	FAR [yr ⁻¹]	$m_1[M_\odot]$	$m_2[M_\odot]$	spin-1- z	spin-2- z	H SNR	L SNR	V SNR	Network SNR
2017-04-01	0.41	4.90	0.78	-0.05	-0.05	6.32	5.94	-	8.67
2017-03-08	1.21	2.26	0.70	-0.04	-0.04	6.32	5.74	-	8.54
2020-03-08	0.20	0.78	0.23	0.57	0.02	6.31	6.28	-	8.90
2019-11-30	1.37	0.40	0.24	0.10	-0.05	6.57	5.31	5.81	10.25
2020-02-03	1.56	1.52	0.37	0.49	0.10	6.74	6.10	-	9.10

[Phukon *et al.* 2021, Abbott *et al.* 2022]

★ Five strong subsolar candidates with SNR > 8 and a FAR < 2 yr⁻¹

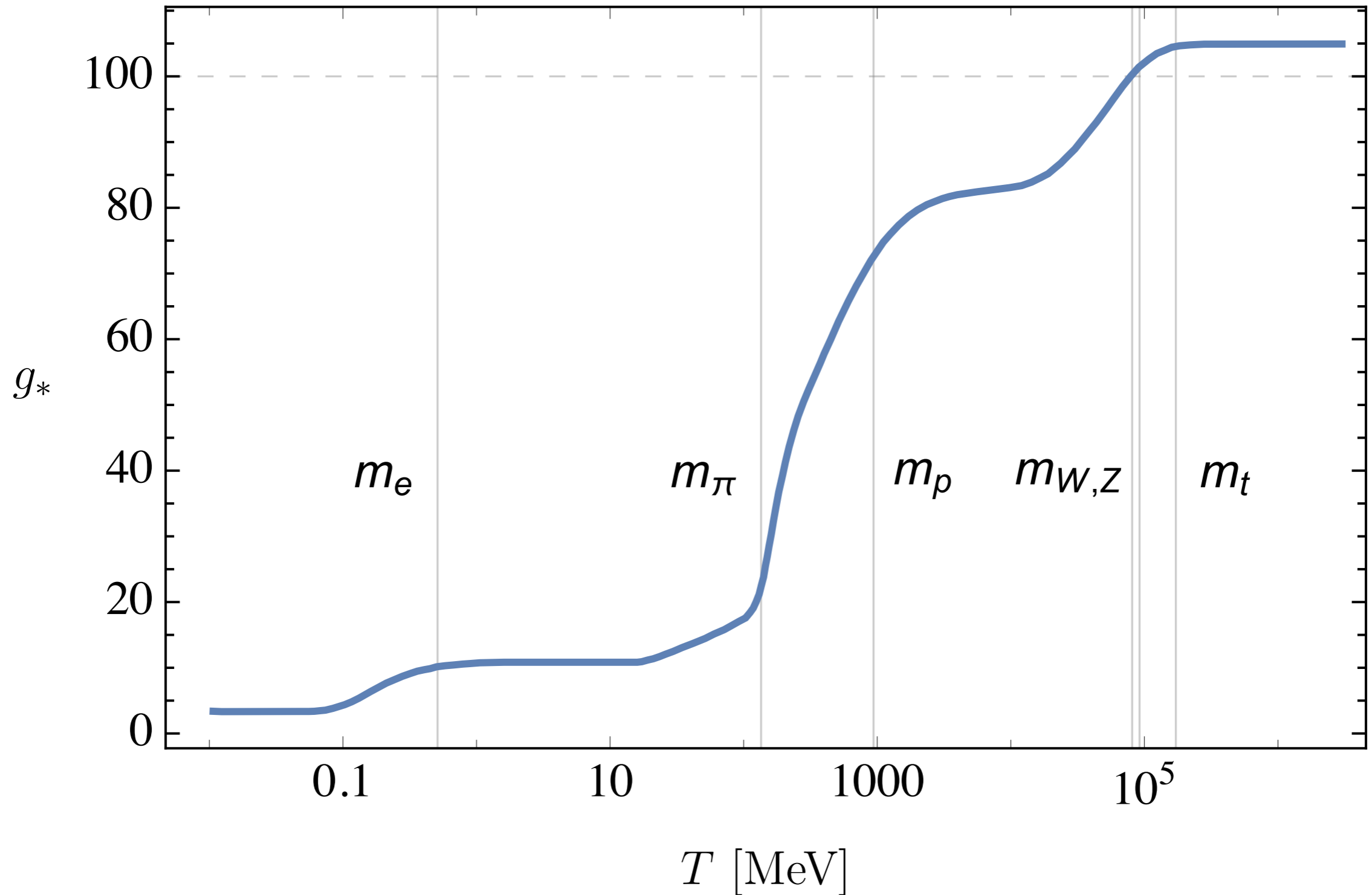


A Unified Scenario

*work with Carr, Clesse,
García-Bellido

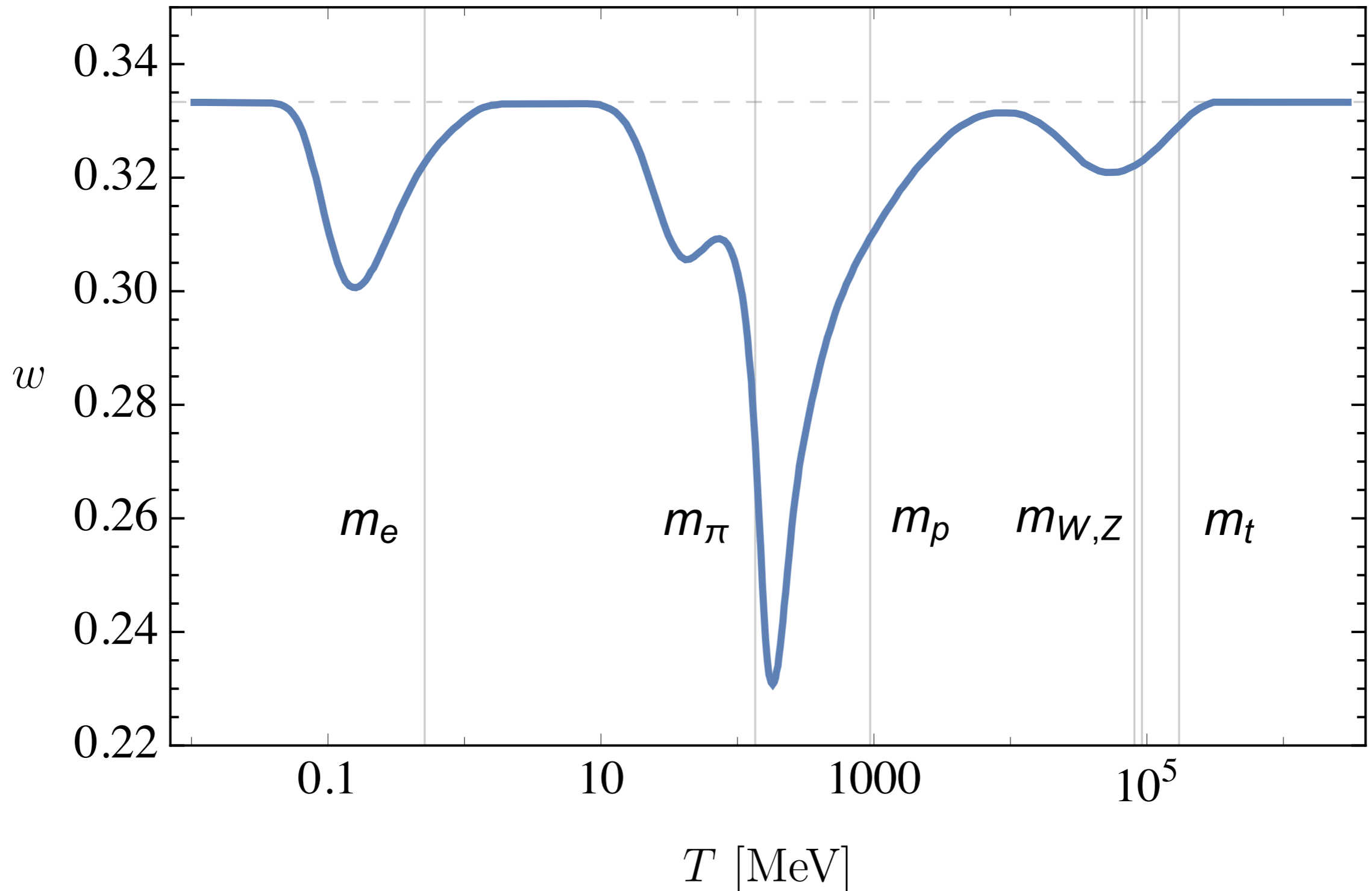
Thermal History of the Universe — Degrees of Freedom

★ Changes in the **relativistic degrees of freedom**:



Thermal History of the Universe — Equation of State

★ Changes in the **equation-of-state parameter** $w = p/\rho$:



Primordial Power Spectrum — Planck to PBH

- ★ Consider an essentially **featureless power spectrum**:

$$\mathcal{P}(k) \sim k^{n_s - 1} + \frac{1}{2} \alpha_s \ln(k/k_*)$$

as suggested by Planck, albeit on *large non-PBH scales*...

- ★ Connection to *small PBH scales* for instance by **critical Higgs inflation**.

[García-Bellido, Ruiz-Morales 2017]

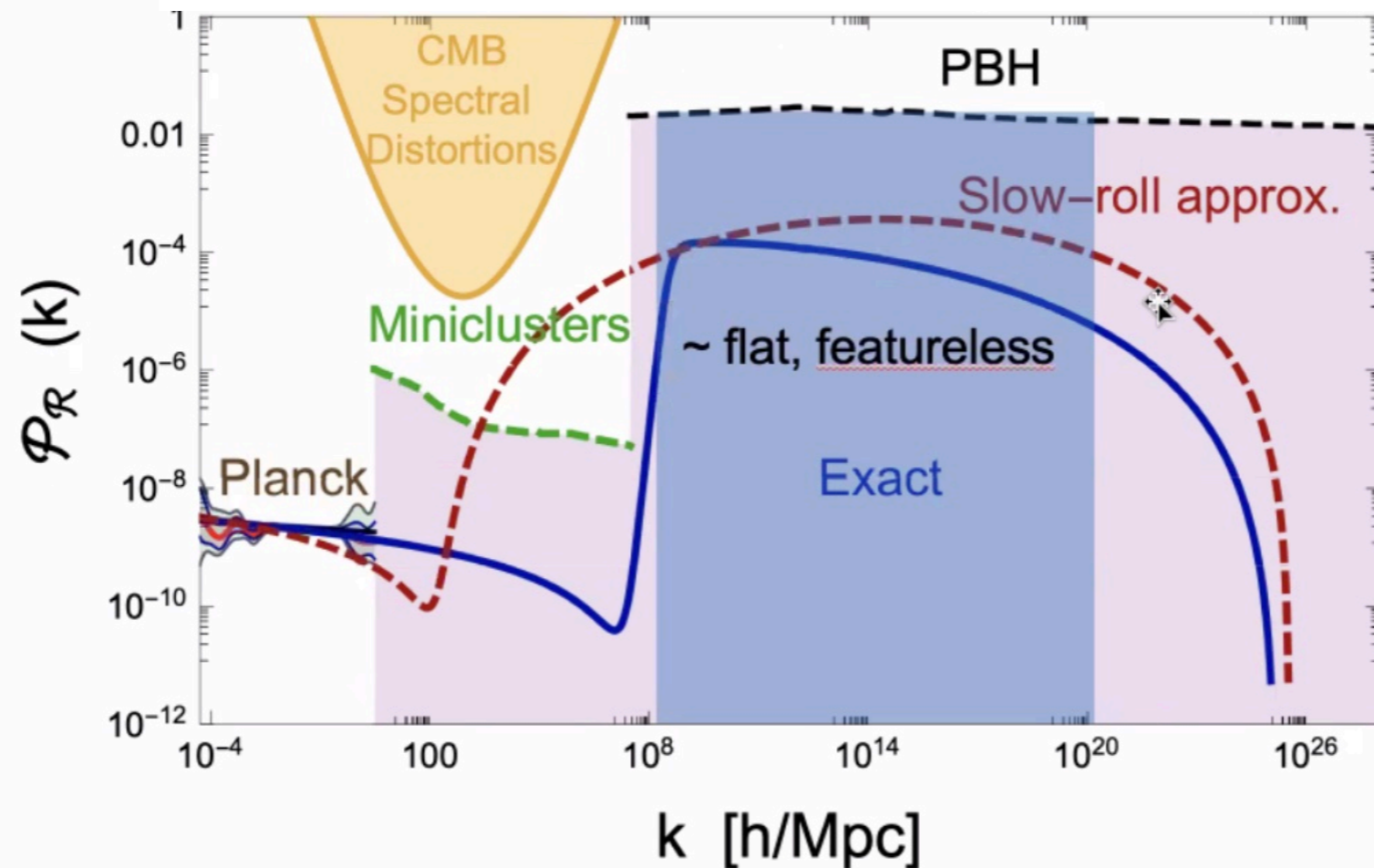
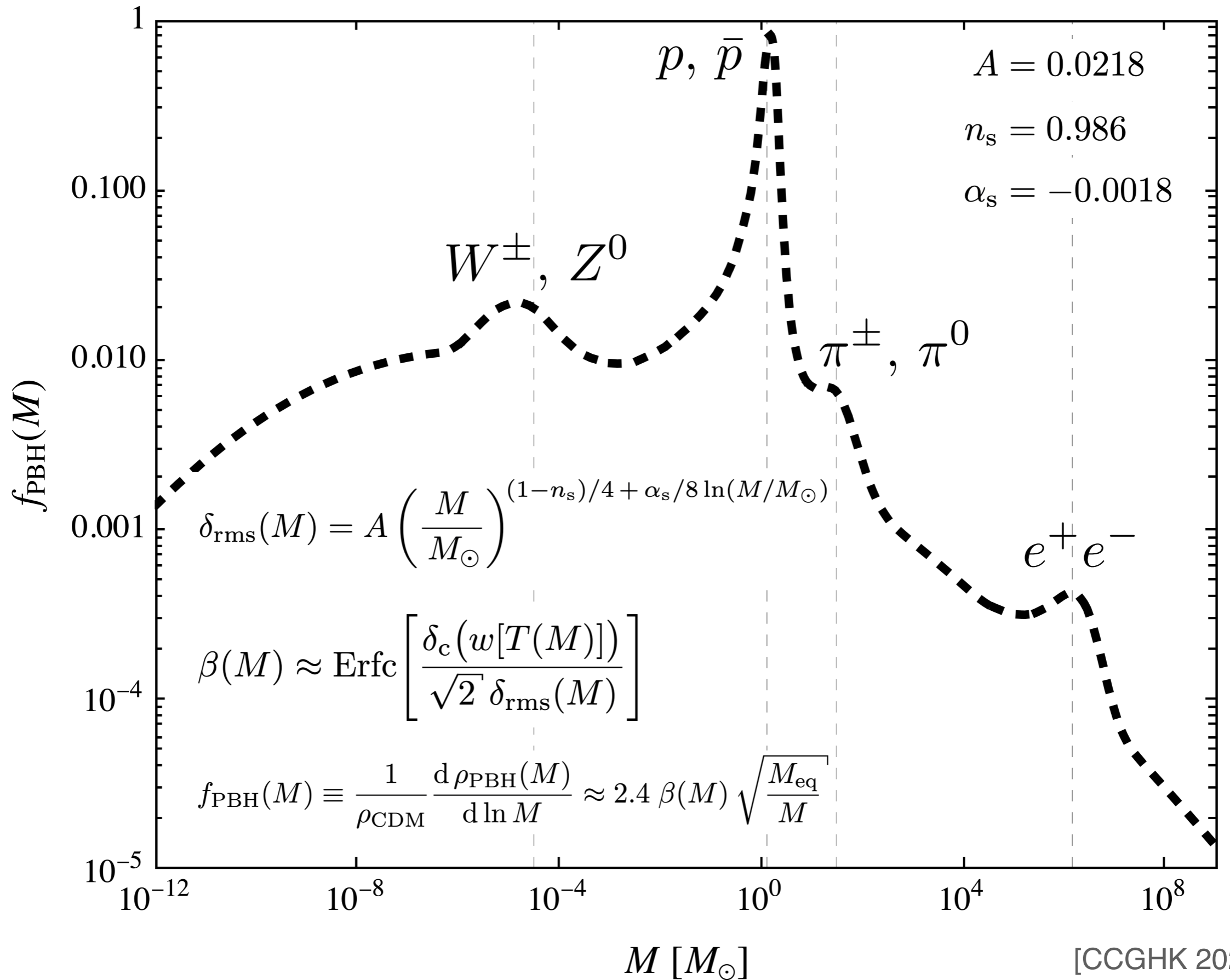
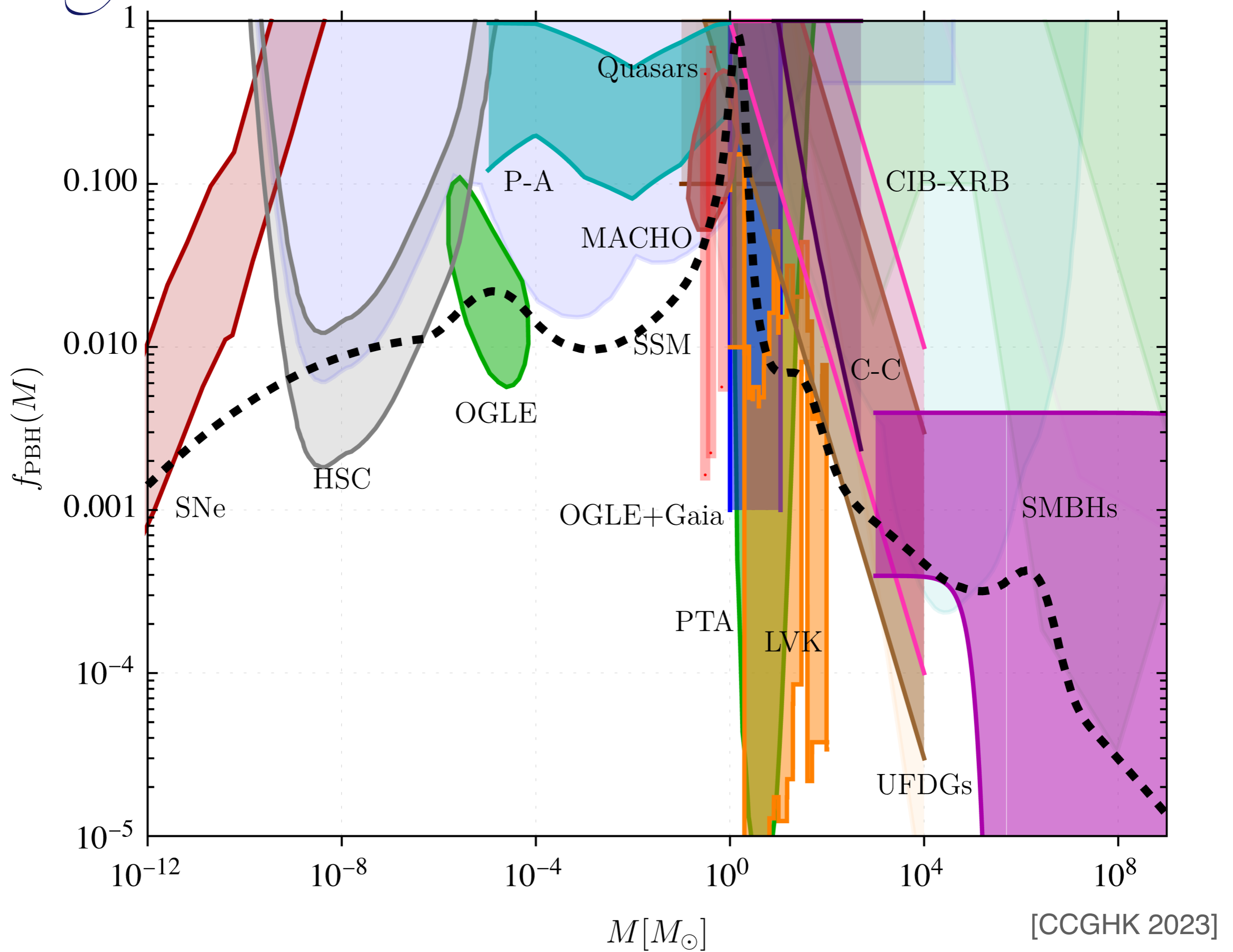


Figure from García-Bellido

PBH Mass Function



Connecting all Positive Evidences!



Shall Ye Become Positivists!

Physics Reports 1054 (2024) 1–68



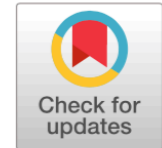
Contents lists available at [ScienceDirect](#)

Physics Reports

journal homepage: www.elsevier.com/locate/physrep



Observational evidence for primordial black holes: A positivist perspective



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^b Service de Physique Théorique, University of Brussels (ULB), Belgium

^c Instituto de Física Teórica UAM/CSIC, Universidad Autónoma de Madrid, Spain

^d Department of Physics and Astronomy, University of Edinburgh, United Kingdom

^e Max Planck Institute for Physics, Germany



Quantum Quiddity

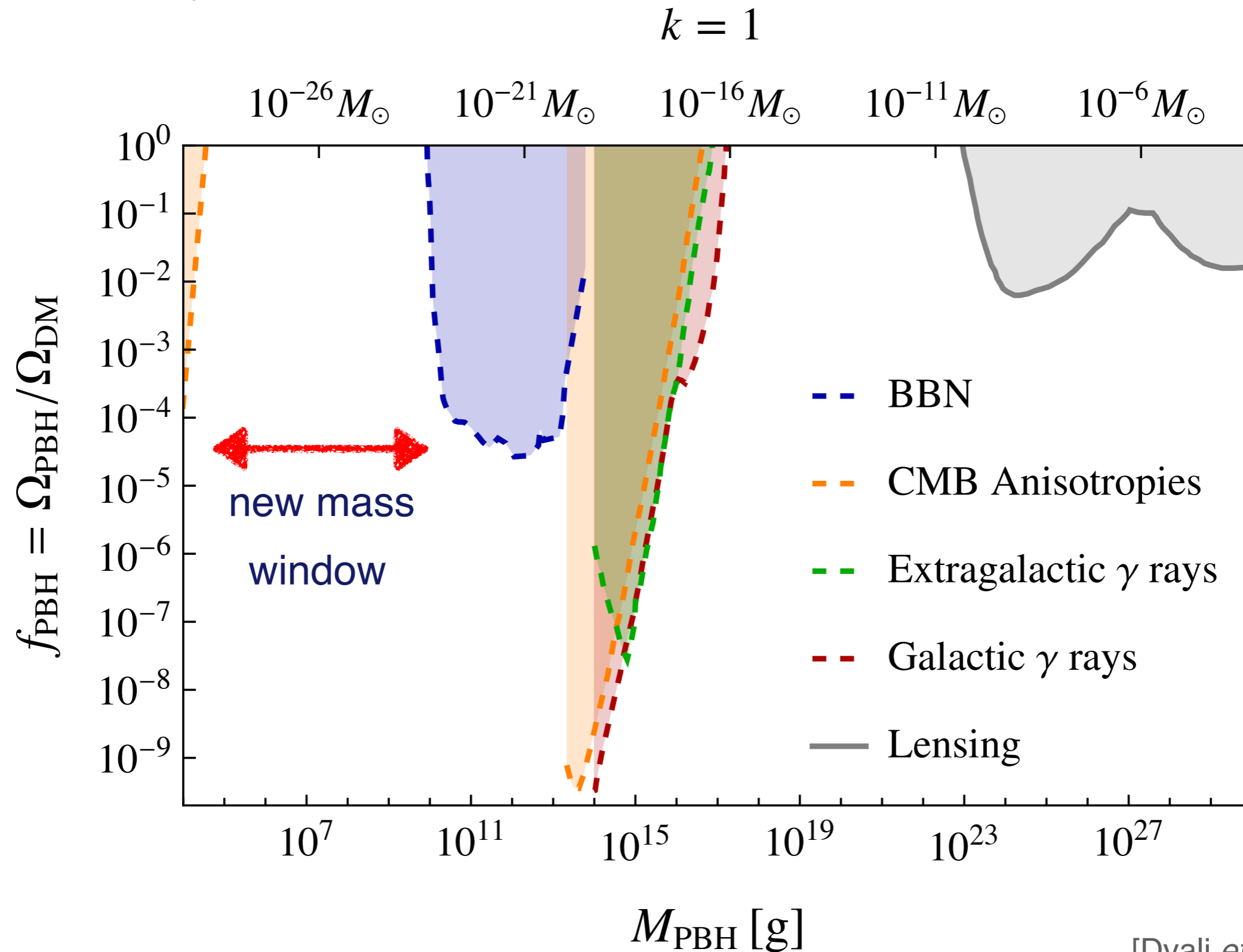
Quantum Aspects

- ★ Black Holes can be understood as *saturons*, ie. configuration of *maximum entropy compatible with unitarity* (cf. work by *Dvali*).
- ★ Black hole evaporation *leaves the semi-classical regime* at latest at half-mass, possibly much earlier.
- ★ Evaporation rate Γ become *entropy suppressed*

$$\Gamma \longrightarrow \frac{1}{S^k} \Gamma$$

- ★ This opens up a large mass range for *ultra-light PBHs* as (quasi) remnants!

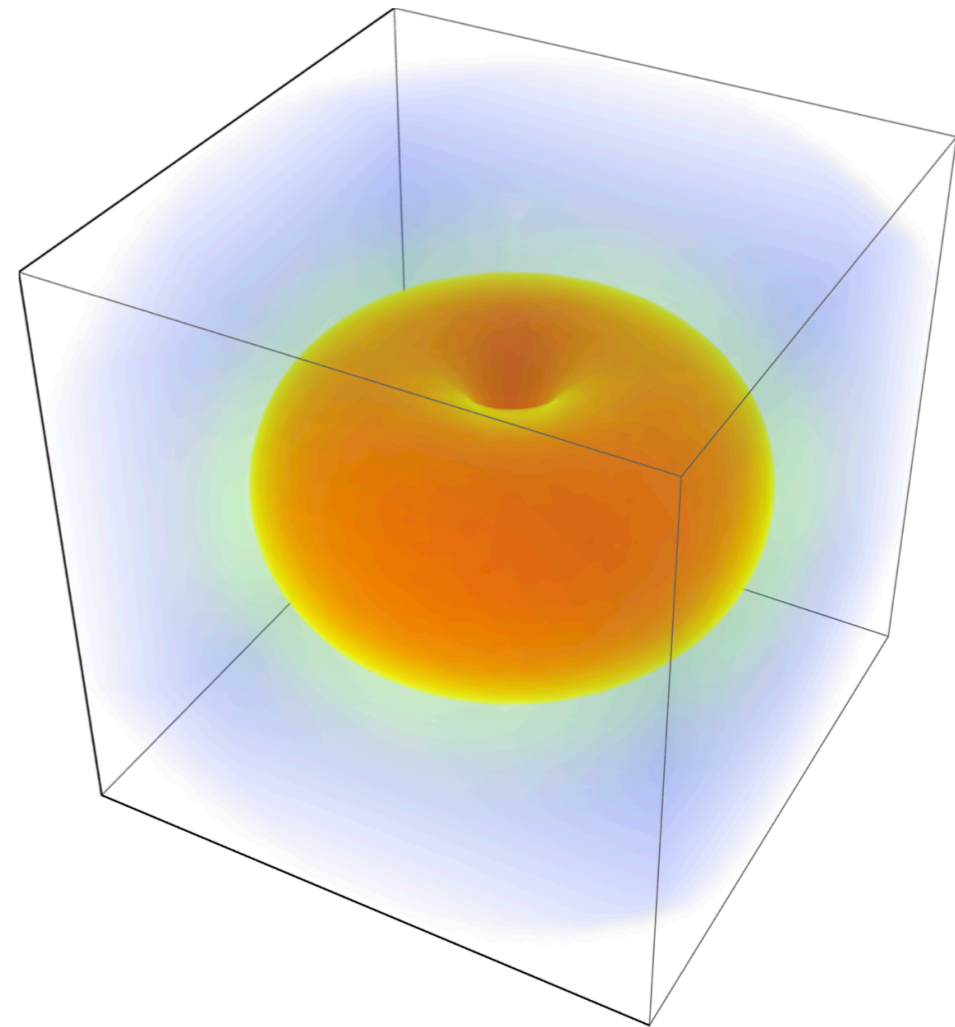
Quantum Aspects



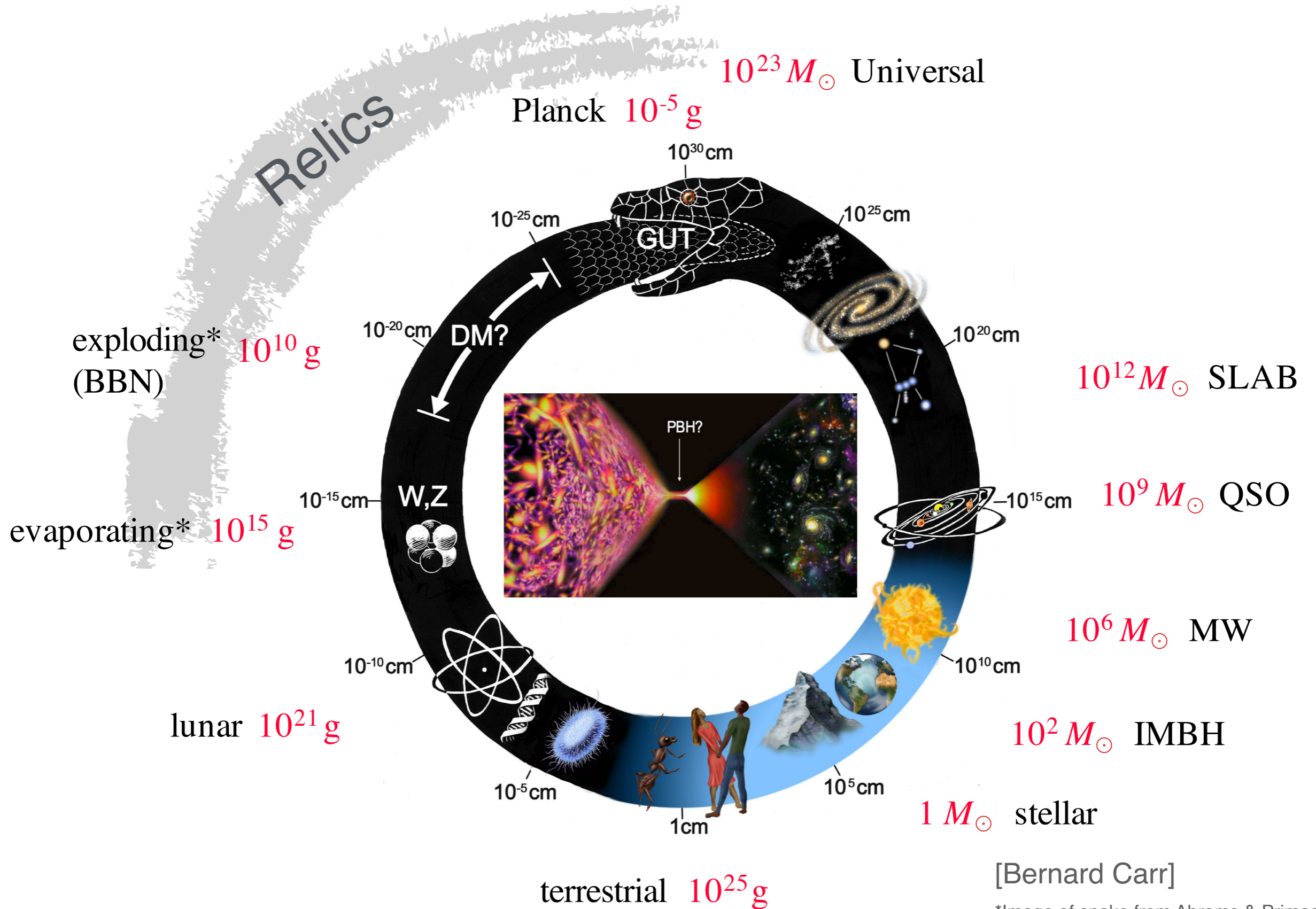
[Dvali et al. 2024]

Quantum Aspects

- ★ We showed that (near-)extremally-spinning black holes admit **vortex structure** (*Dvali, Kühnel, Zantedeschi*)
- ★ **PBHs from confinement** (*Dvali, Kühnel, Zantedeschi*) could provide **ideal prerequisites for vortex formation** due to highly spinning light PBHs.
- ★ If these PBHs provide the dark matter, their vorticity might explain **primordial magnetic fields**.
- ★ Besides, vorticity provides a **topological meaning to the stability of extremal black holes**.

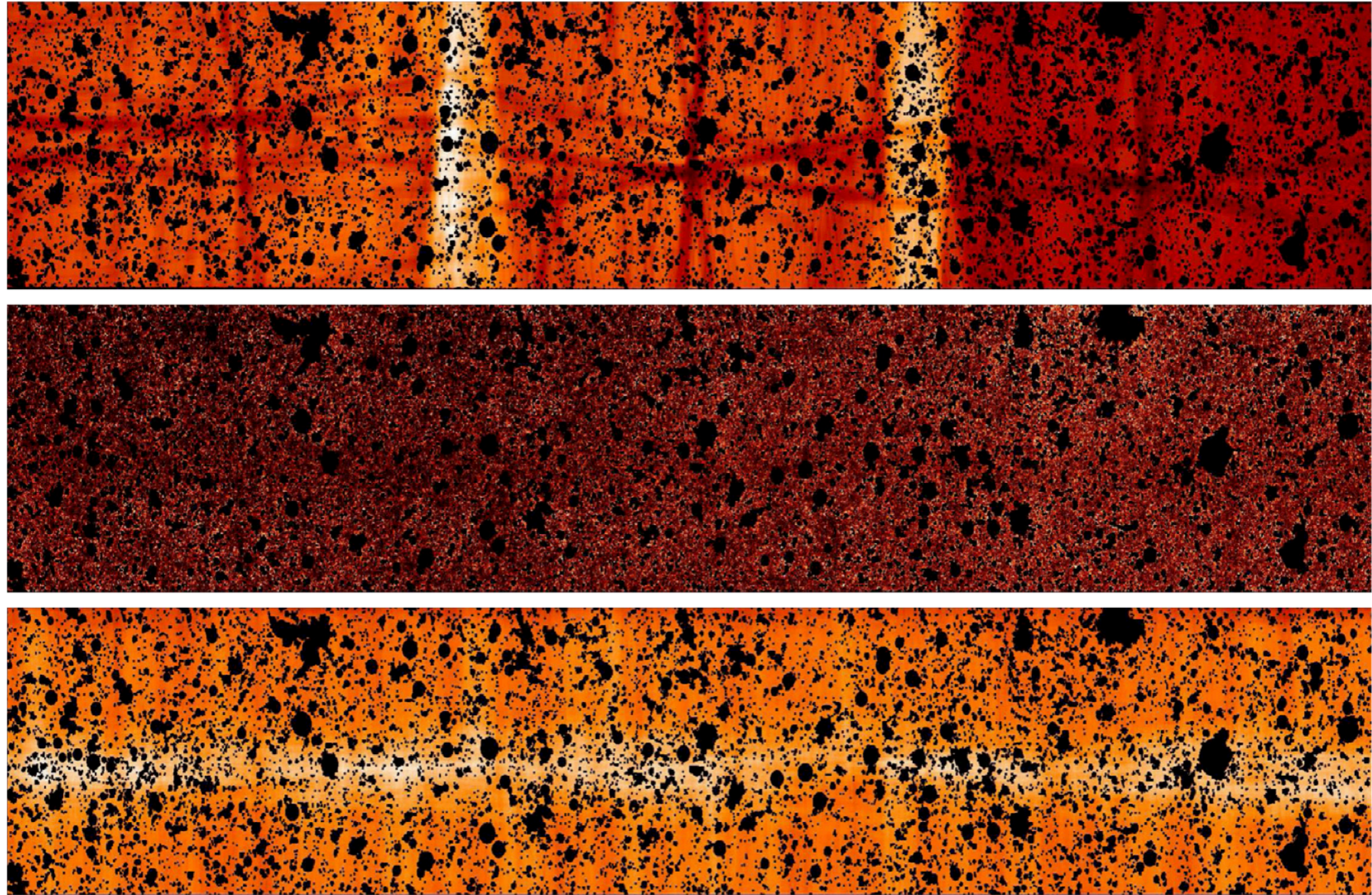


Black Holes as a Link between Micro and Macro Physics



[Bernard Carr]
 *Image of snake from Abrams & Primack 2012

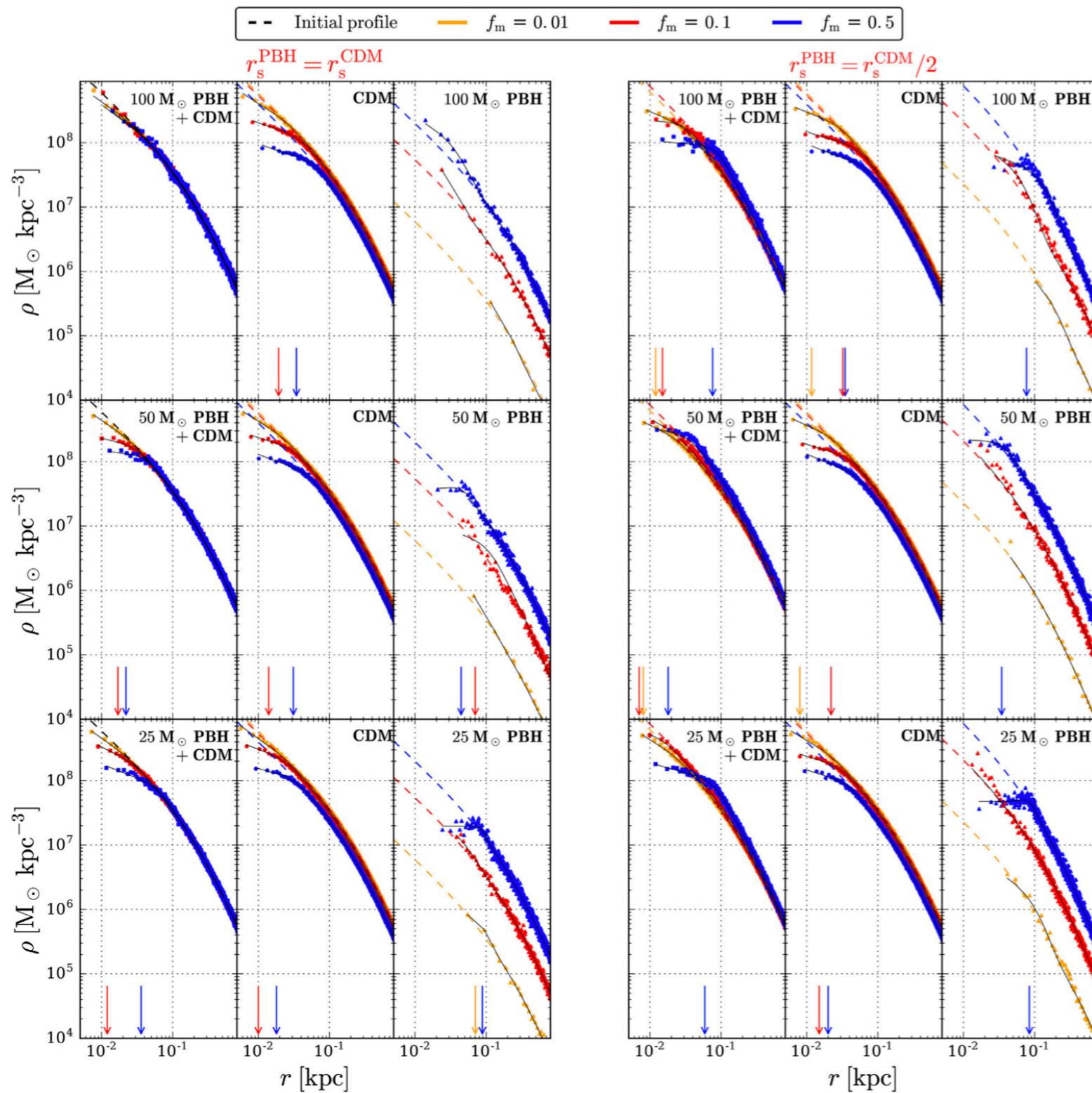
Correlations of Cosmic Infrared/X-Ray Backgrounds



[Cappelluti *et al.* 2013]

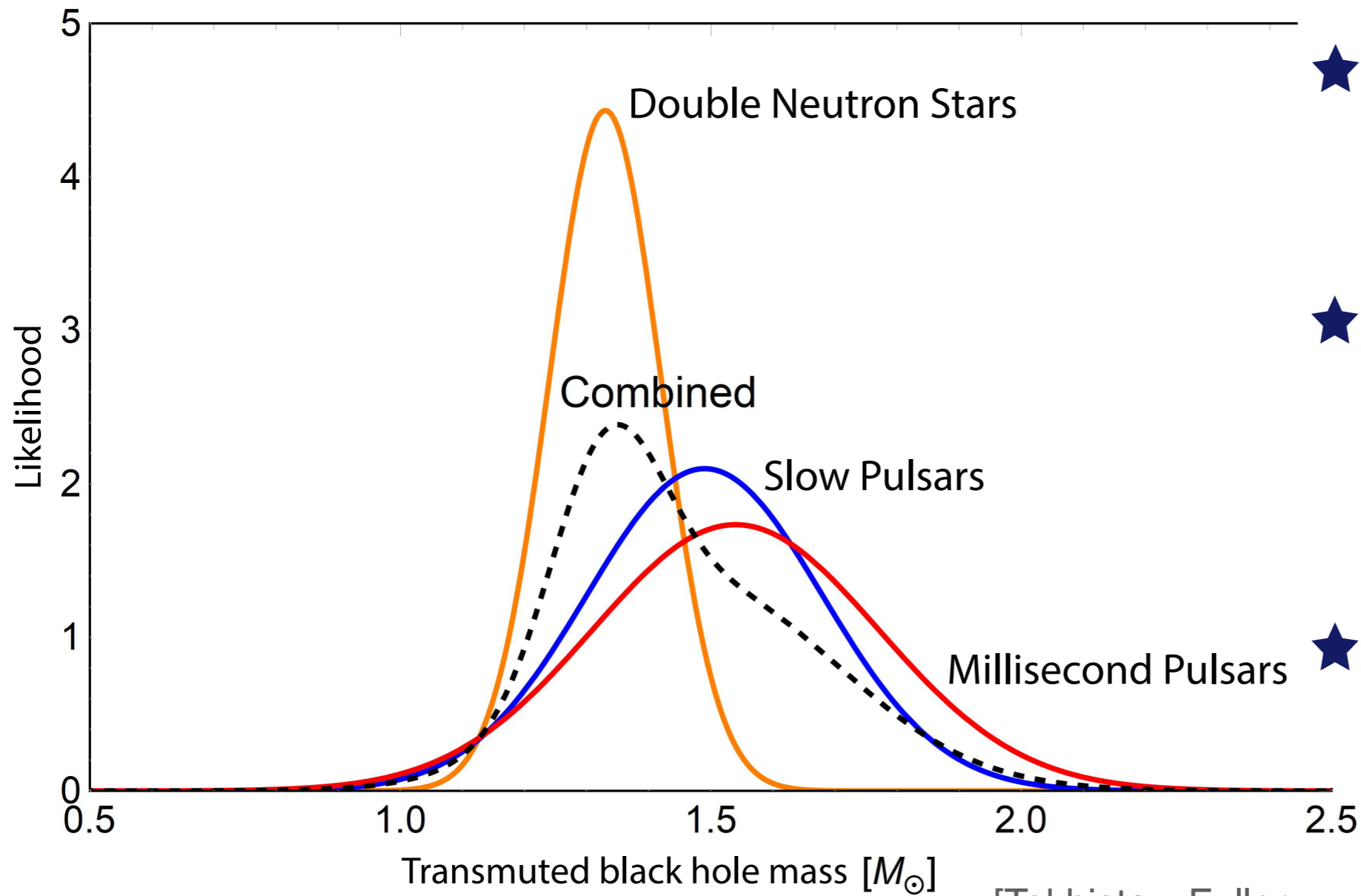
★ PBHs generate early structure and respective backgrounds

Ultra-faint Dwarf Galaxies



- ★ **Non-detection** of dwarf galaxies smaller than $\sim 10 - 20$ pc
- ★ Ultra-faint dwarf galaxies are **dynamically unstable** below some critical radius in the presence of PBH dark matter!
- ★ This works with **a few percent** of PBH dark matter of $25 - 100 M_{\odot}$.

Transmuted Solar-Mass Black Holes



[Takhistov, Fuller,
Kusenko 2017]

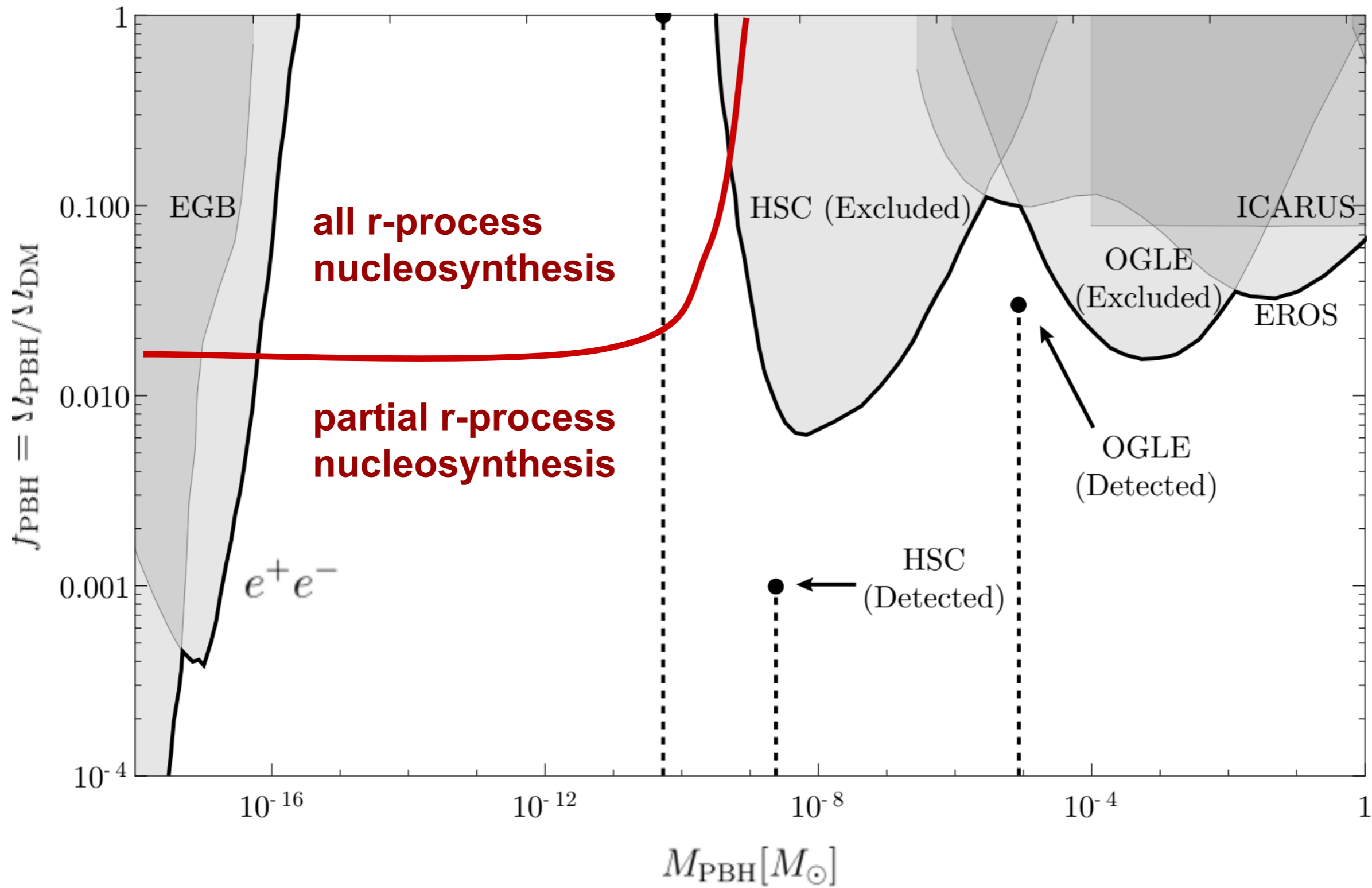
★ Small PBH + Neutron Star = $\mathcal{O}(1) M_{\odot}$ black hole.

★ Besides such a **characteristic mass distribution** of black holes

★ **this can explain all r-process elements in the Universe, including gold**

(... of which a single neutron star could generate up to 10 Earth masses $\sim 10^{30}$ GBP).

r-Process Elements

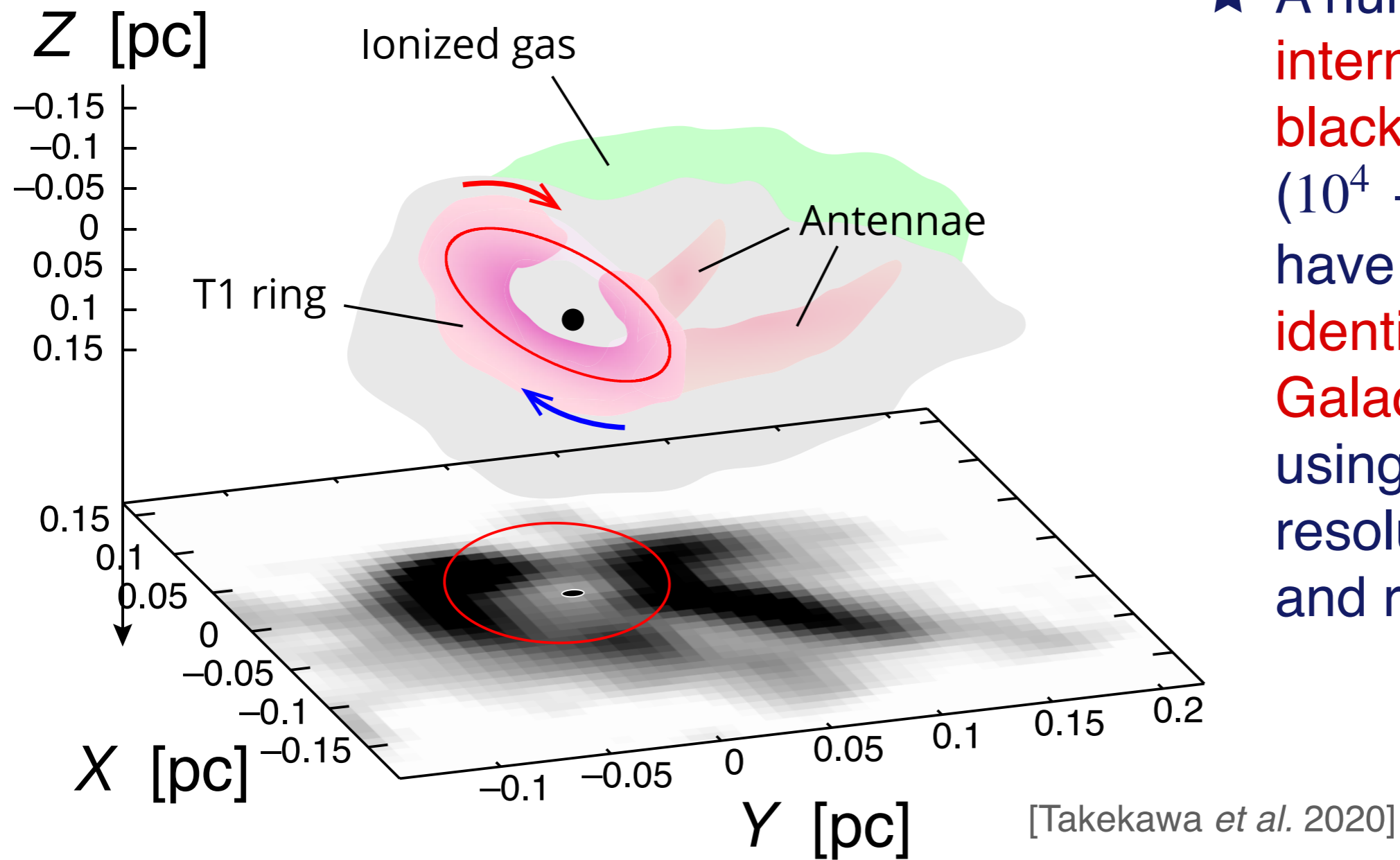


(*from talk by Alex Kusenko)

G Objects

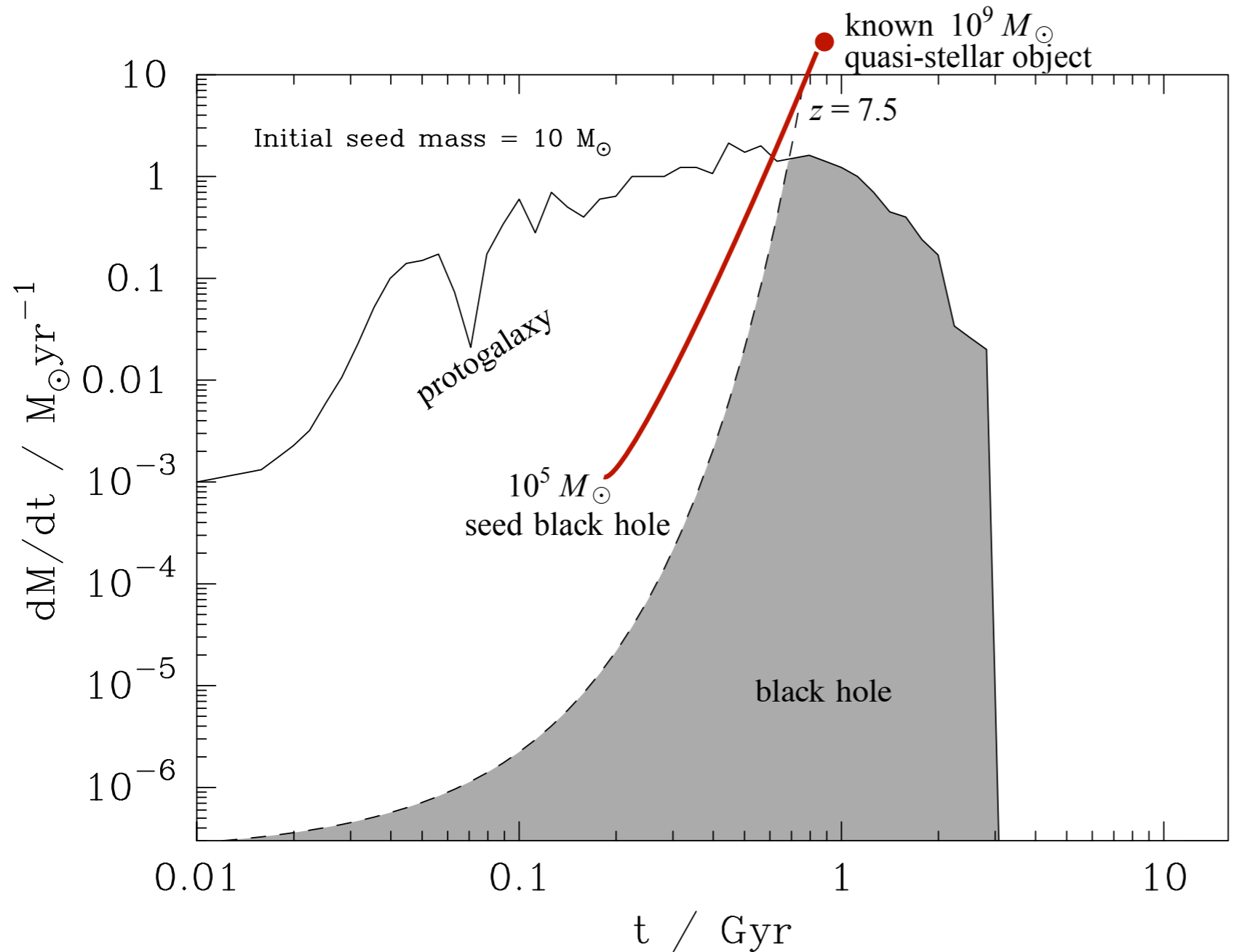
- ★ Population of unresolved objects which show both thermal and dust emission.
- ★ **18 of these** cannot be main-sequence stars and **are very likely black holes**.
- ★ Their mass function overlaps the **low mass gap** from **2 to 5 M_{\odot}** .
- ★ These are **not expected** to form as the endpoint of **stellar evolution**.

Evidence for Intermediate-Mass Black Holes



- ★ A number of **intermediate-mass black holes** ($10^4 - 10^5 M_{\odot}$) have been **identified in the Galactic Centre**, using high-angular resolution ALMA and radio data.

Massive Objects at high Redshifts



[Archibald *et al.* 2002];
(Hasinger *priv. comm.*)

- ★ Detection of QSOs at high redshifts, such as $\sim 10^9 M_{\odot}$ at $z \approx 7.5$

[Wang *et al.* 2021]

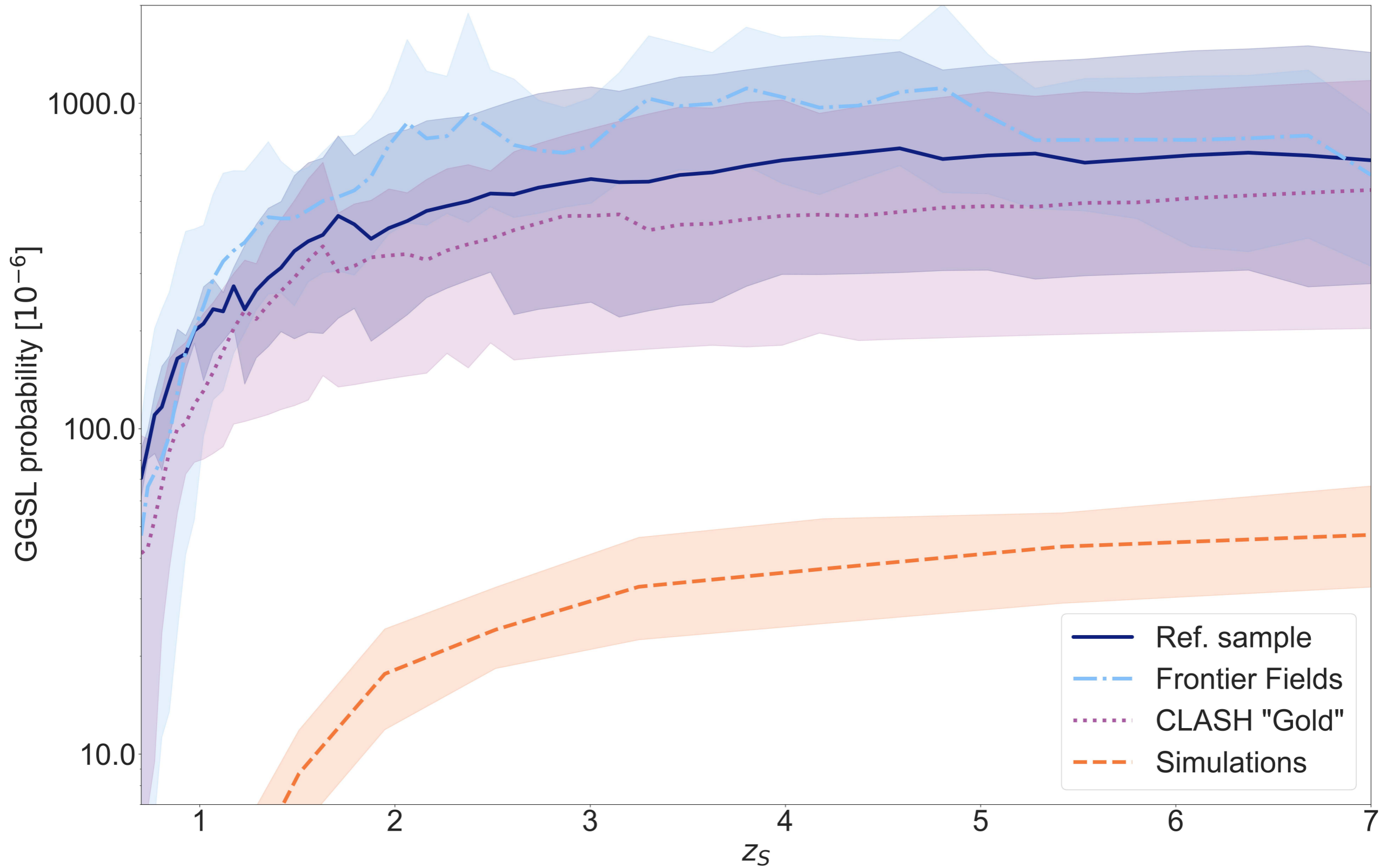
- or $\sim 10^8 M_{\odot}$ at $z \approx 13$.

[Pacucci *et al.* 2022]

and numerous others.

- ★ Need massive black holes $\sim 10^{4-5} M_{\odot}$ in the early Universe.

Evidence of Dark Matter Clumping with HST

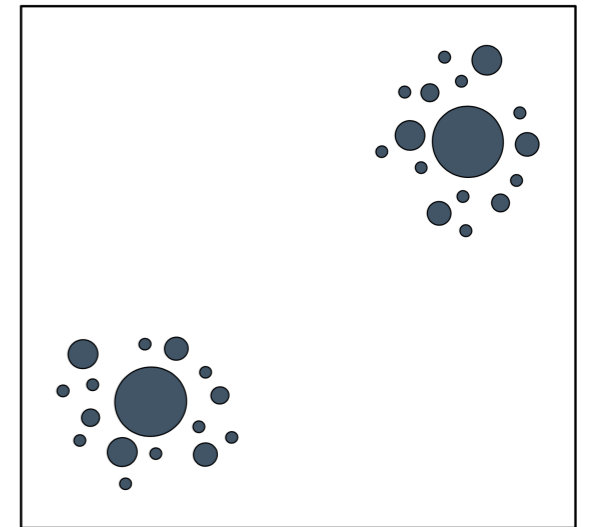
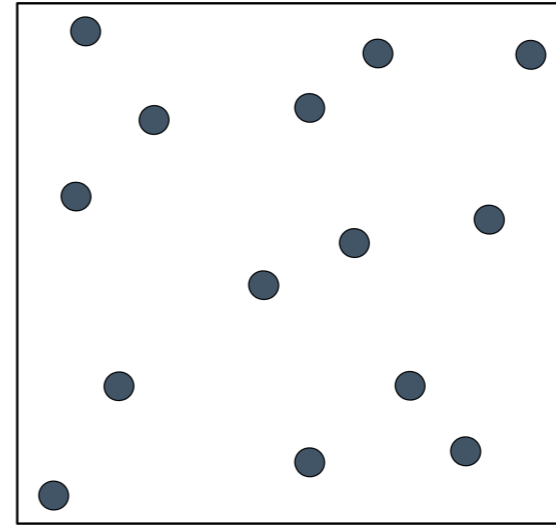


[Meneghetti, Natarajan, Downer 2020]

Evidence of Dark Matter Clumping with HST



[Meneghetti, Natarajan, Downer 2020]



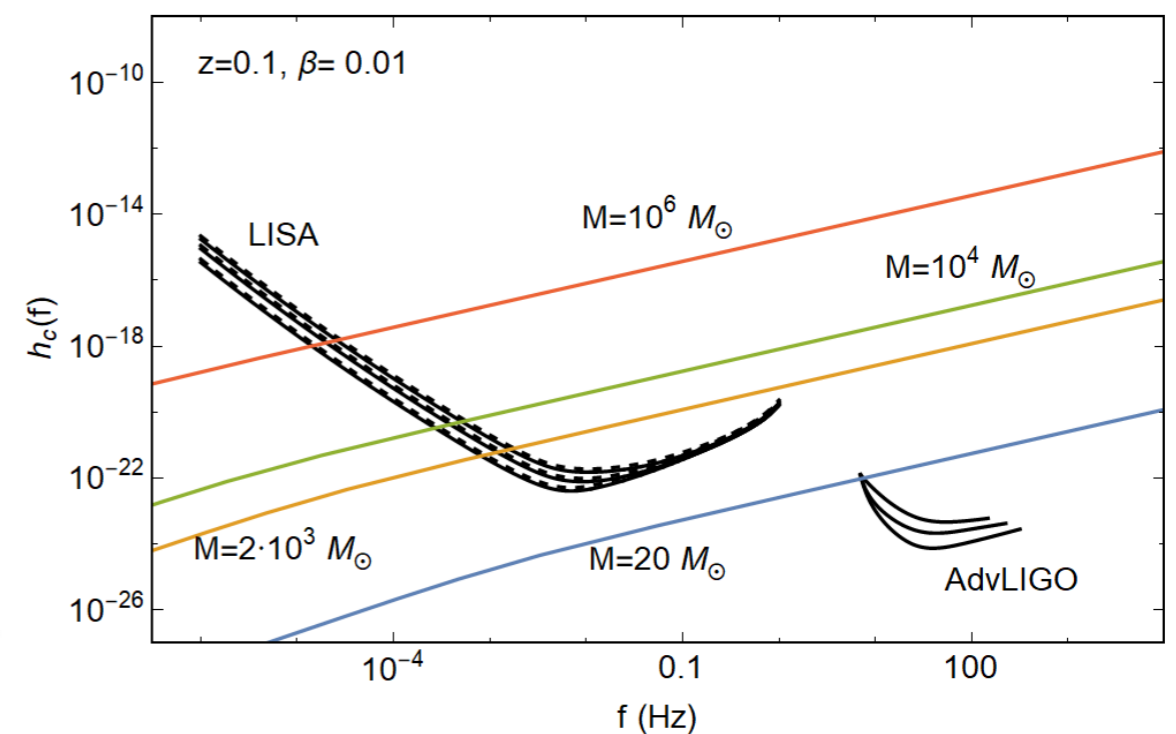
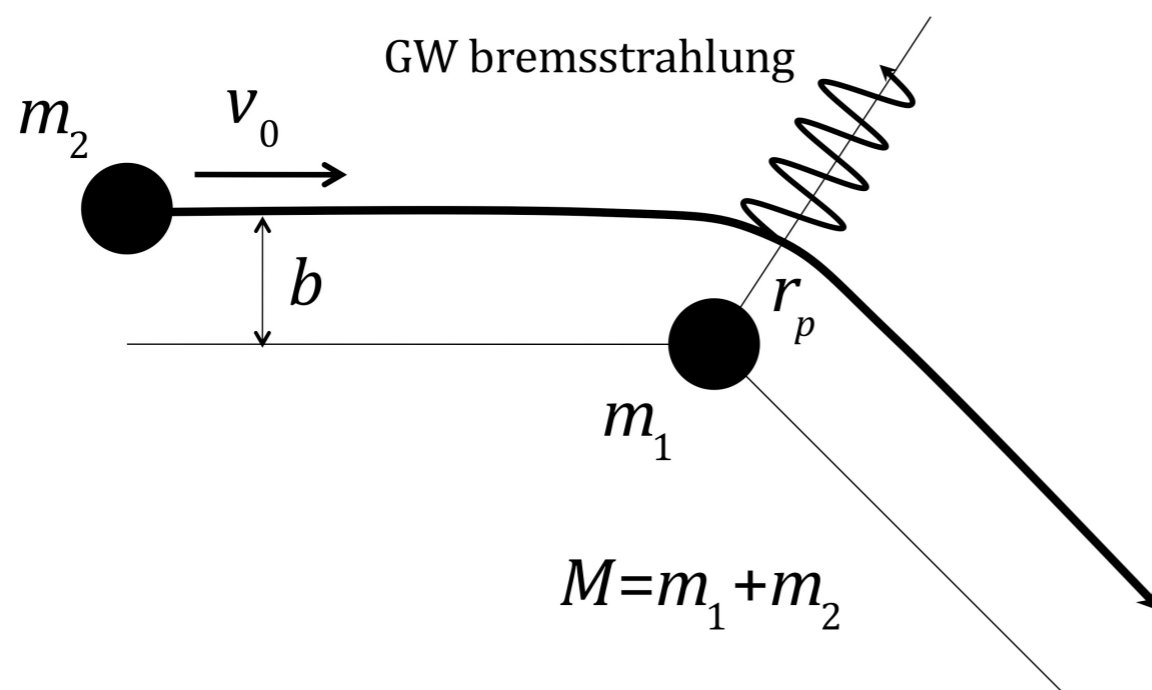
[García-Bellido 2018]

homogeneous versus clumped
dark matter distribution

★ This is the **norm** for **PBHs!**

Gravitational Waves from PBHs

- ★ PHBs can emit gravitational waves in various instances and times.
 - ★ Gravitational waves from **PBH formation**.
 - ★ Gravitational-wave emission from **PBH binaries**:
 - 1) Stochastic GW background
 - 2) Individual mergers
 - ★ Gravitational-wave emission from **hyperbolic PBH encounters**.



GRAVITATIONAL WAVE MERGER DETECTIONS

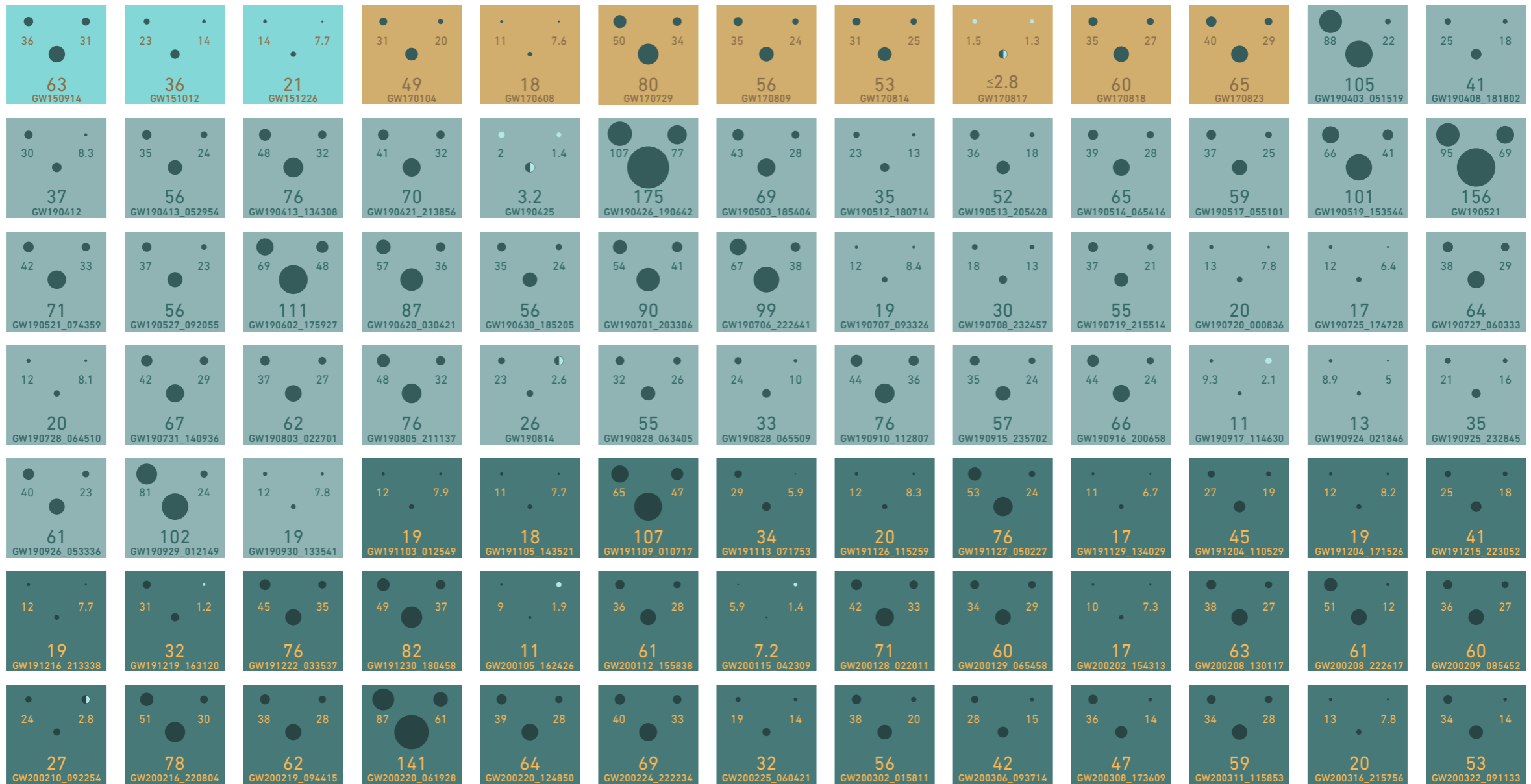
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GRAVITATIONAL WAVE MERGER DETECTIONS

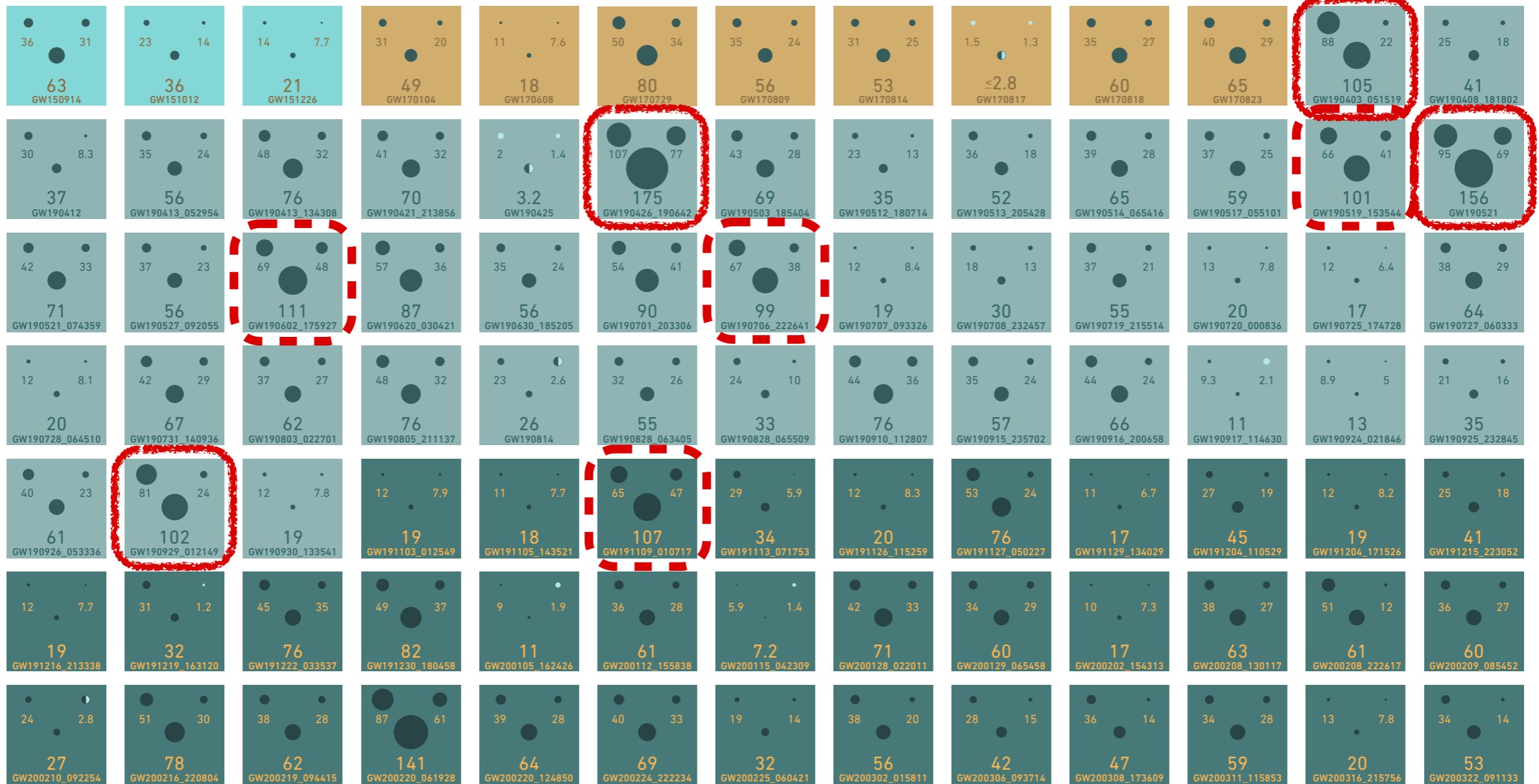
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★ Black hole progenitors in the **pair-instability mass gap** (i.e. above $\sim 60 M_{\odot}$)



GRAVITATIONAL WAVE MERGER DETECTIONS

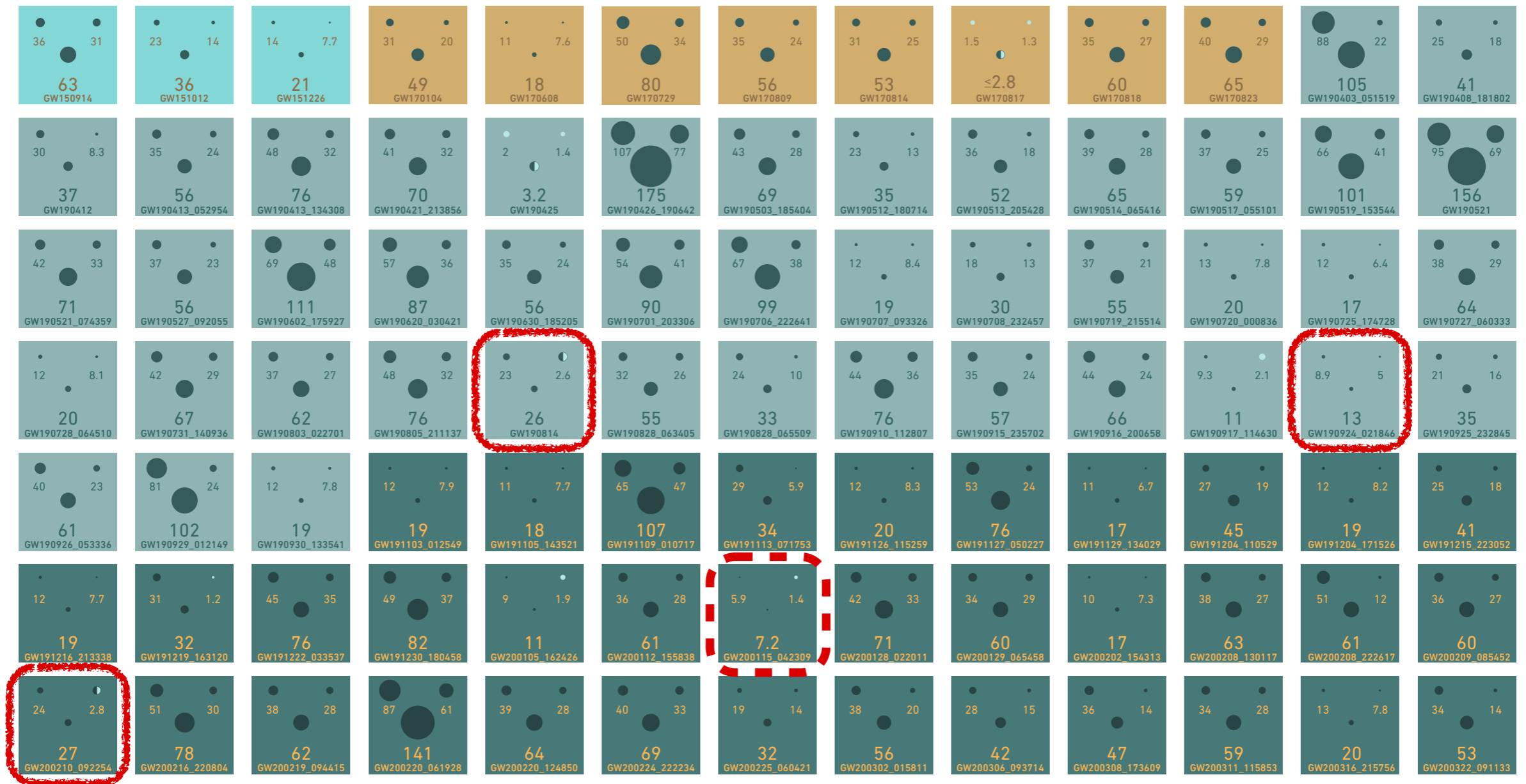
→ SINCE 2015

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03a+b 2019-2020



★ Black hole progenitors in the **lower mass gap** (i.e. between 2 and 5 M_{\odot})





GW190814: Gravitational Waves from the Coalescence of a 23 Solar Mass Black Hole with a 2.6 Solar Mass Compact Object

R. Abbott¹, [...]

Abstract

We report the observation of a compact binary coalescence involving a $22.2\text{--}24.3 M_{\odot}$ black hole and a compact object with a mass of $2.50\text{--}2.67 M_{\odot}$ [...] **the combination of mass ratio, component masses, and the inferred merger rate for this event challenges all current models of the formation and mass distribution of compact-object binaries.**

★ **Asymmetric** black hole progenitors (mass ratio $q < 0.25$)



Subsolar Black Holes - The Smoking Gun!

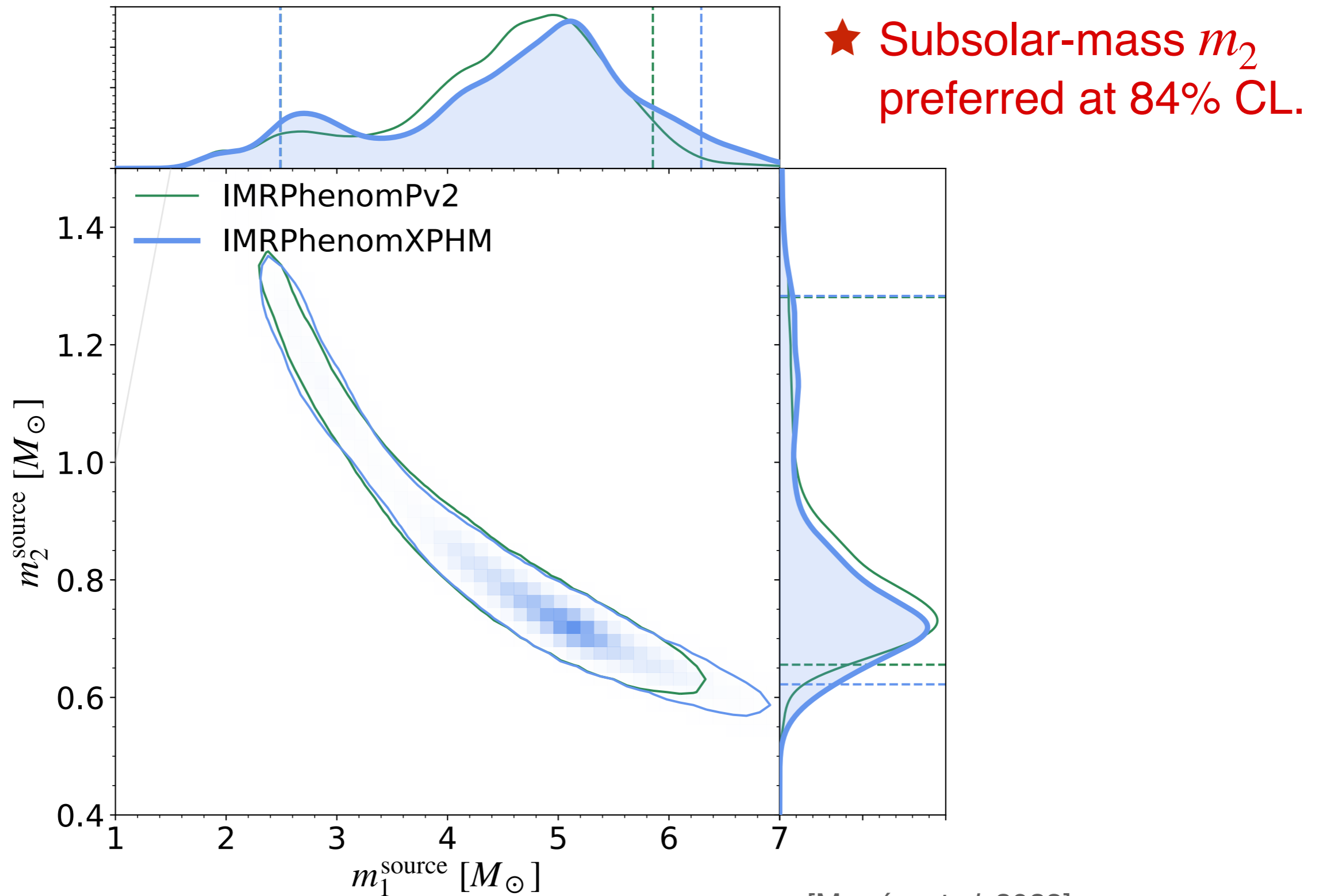
- ★ Recent reanalysis of LIGO data updated merger rates and low mass ratios:

Date	FAR [yr ⁻¹]	$m_1[M_\odot]$	$m_2[M_\odot]$	spin-1-z	spin-2-z	H SNR	L SNR	V SNR	Network SNR
2017-04-01	0.41	4.90	0.78	-0.05	-0.05	6.32	5.94	-	8.67
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2020-03-08	0.20	0.78	0.23	0.57	0.02	6.31	6.28	-	8.90
2019-11-30	1.37	0.40	0.24	0.10	-0.05	6.57	5.31	5.81	10.25
2020-02-03	1.56	1.52	0.37	0.49	0.10	6.74	6.10	-	9.10

[Phukon *et al.* 2021, Abbott *et al.* 2022]

- ★ Five strong subsolar candidates with SNR > 8 and a FAR < 2 yr⁻¹
- ★ Possibly the first confirmed detection of a subsolar mass PBH with the next 24 months!

Posterior probability for SSM170401



Subsolar PBHs Discovered in the next 24 Months?



[Chris van den Broeck]

contra



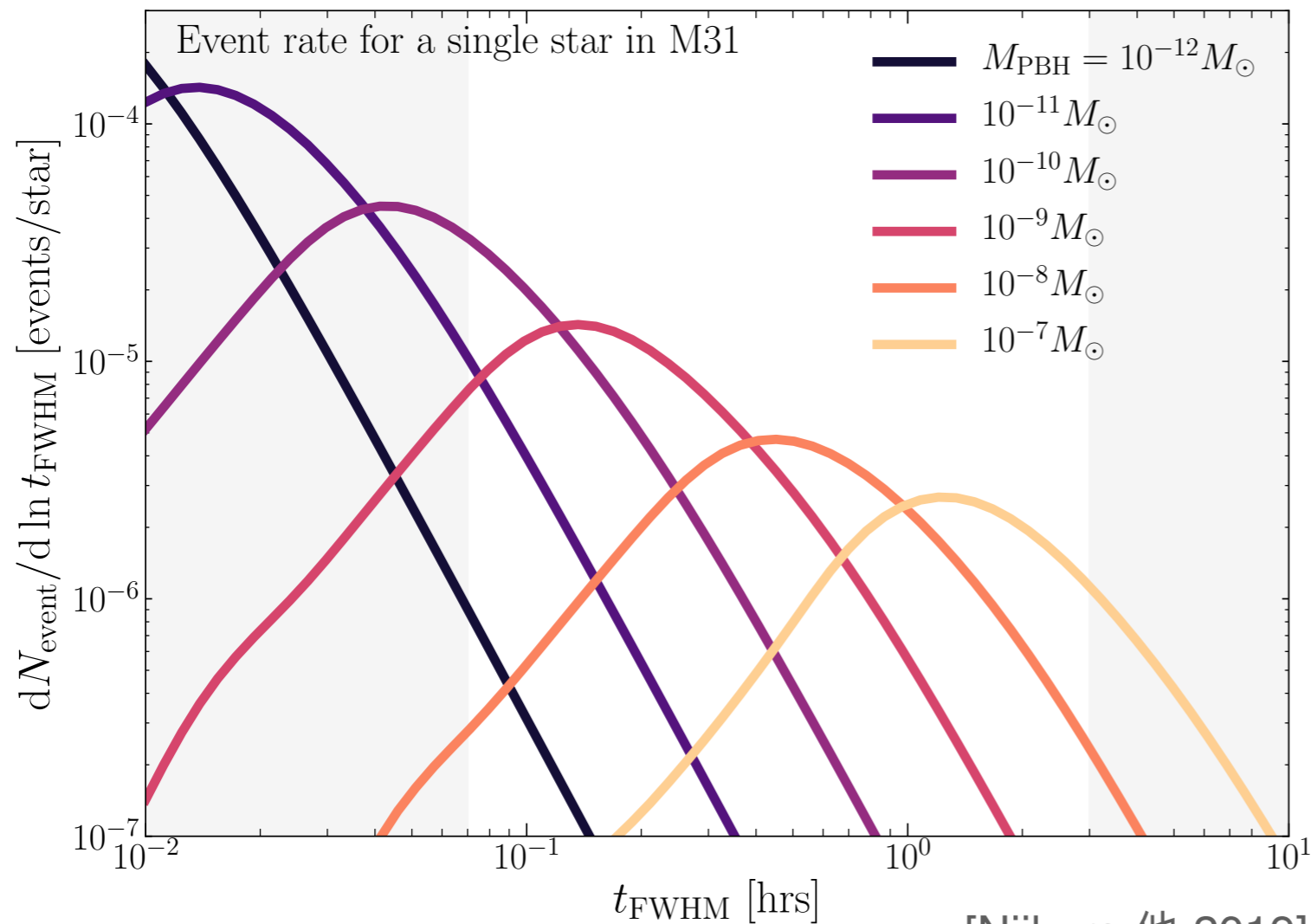
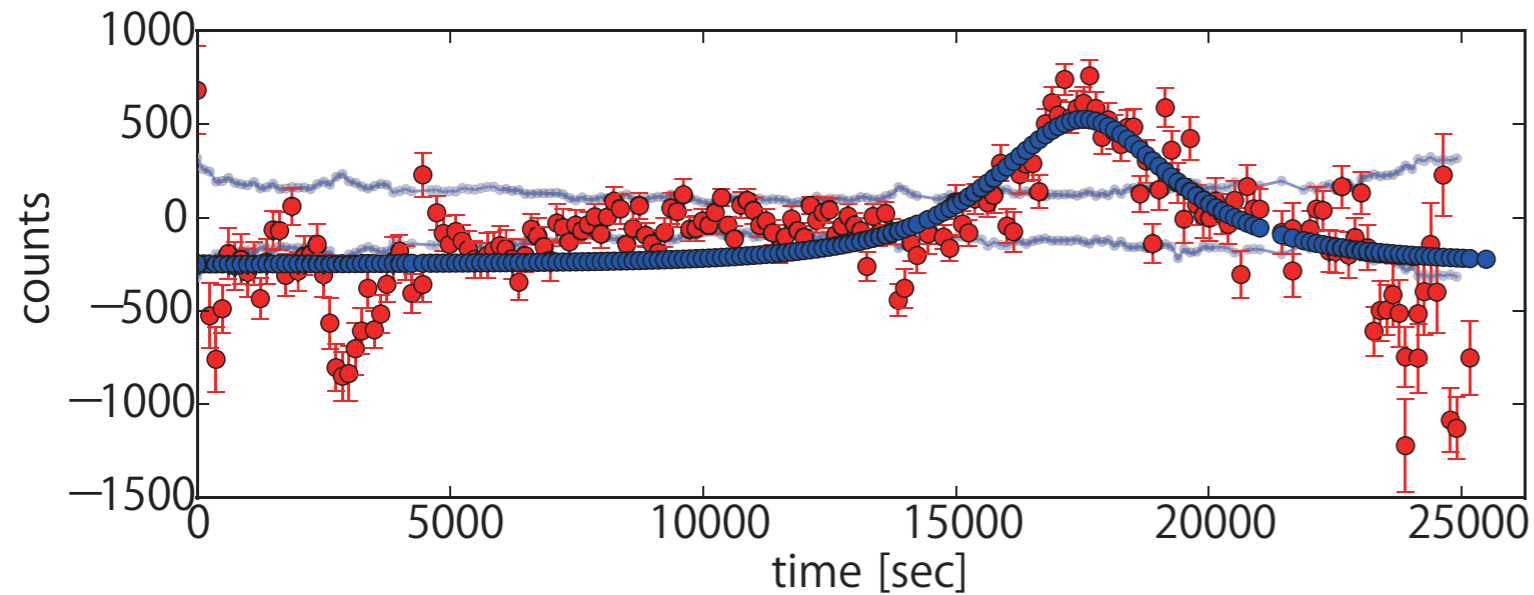
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Pixel Lensing by Subaru Hyper Suprime-Camera (HSC)



[Niikura 他 2019]

- ★ Seven-hour observation of M31 with the **Subaru HSC**...
- ★ ... using pixel-lensing technique to **search for microlensing of stars by PBHs** in the Milky Way or Andromeda.
- ★ 15,571 candidate variable stars were extracted from the difference images...
- ★ ... and **one event** by a compact body with mass $10^{-11} - 10^{-5} M_{\odot}$ could **be identified**.

Black Holes @ Cosmology

2024

International Conference
11th to 15th of March 2024

University of The Bahamas, Nassau

Opening Talk by Nobel Laureate

Professor Reinhard Genzel

Public Lecture by

Professor Matt Caplan

Professor Matt Caplan

Confirmed Invited Speakers include:

Andreas Albrecht

Gia Dvali

Michela Mapelli

Earl Bellinger

Glennys Farrar

Emil Mogola

Gianfranco Bertone

Juan García-Bellido

Samaya Nissanke

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Lárus Thorlacius

Organisational Committee:

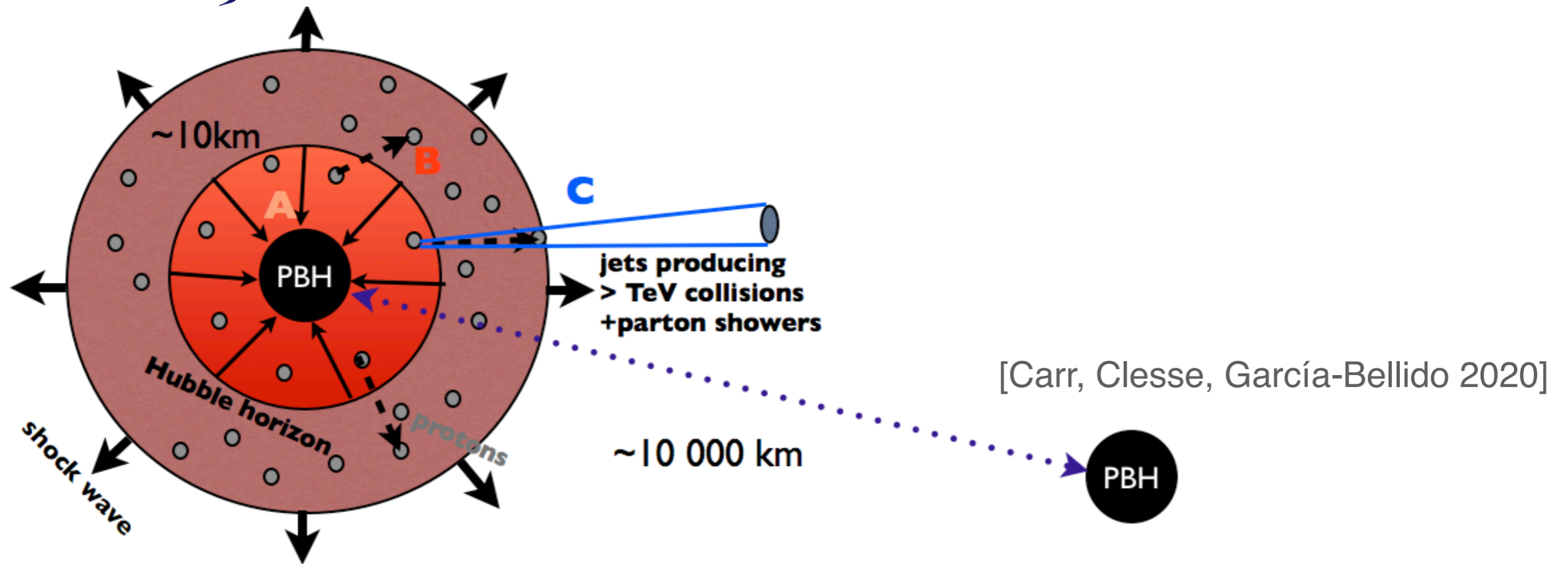
*Florian Kühnel (Chair), Jaco de Swart, Katherine Freese, Pandora Johnson,
Eduardo Guendelman, Claude McNamara, Remo Ruffini, Carlton Watson*



See you at BHCos '26!



Primordial Supernovae



- ★ PBH collapse during the QCD transition **accelerates** particles **over several orders of magnitude** above their rest mass.
- ★ Interactions in the surrounding high-density plasma lead to **electro-weak sphaleron** processes.
- ★ This *locally* yields an $\mathcal{O}(1)$ **baryon asymmetry**.
- ★ The fraction of PBHs 10^{-9} in turn **explains** the observed **baryon asymmetry of the Universe!**

*Primordial Black Holes
from Confinement*

work with Dvali & Zantedeschi

Important Issues

★ The standard approach of PBH formation has **two main issues**:

★ In order to have a given percentage of PBH dark matter requires **exponential fine-tuning**.

★ PBH formation happens in the **strong-coupling regime**.

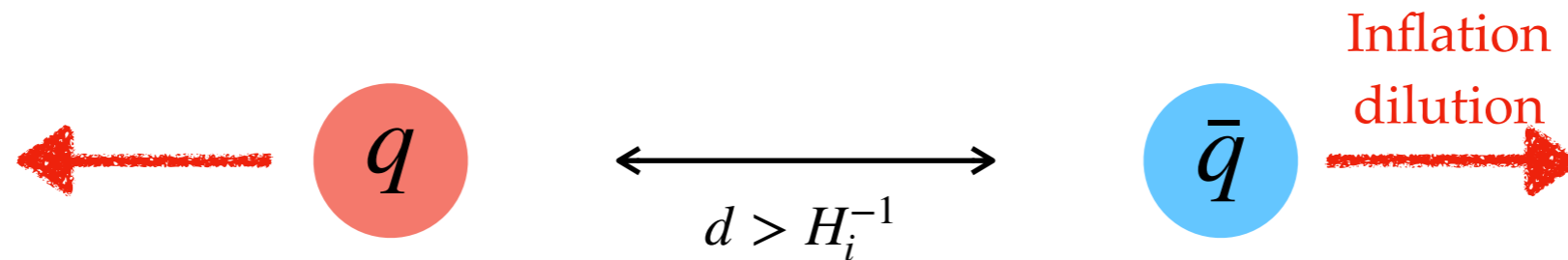
A New Approach

★ We propose a novel PBH formation mechanism which is

- ★ assumption-minimal,
- ★ free of exponential fine-tuning,
- ★ avoids strong coupling,
- ★ works with standard QCD*,
- ★ compatible with observations.

Confinement Formation Mechanism

★ **1. Ingredient:** de Sitter fluctuations produce quarks during inflation.



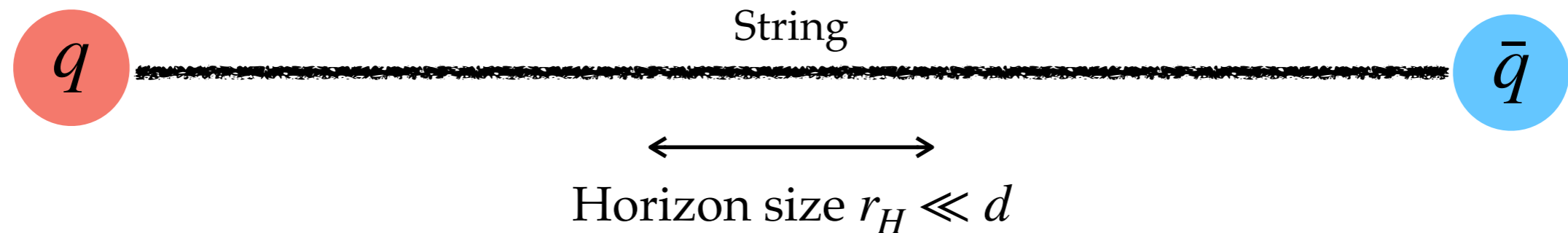
★ Focus on a simple pair case.

★ Distance grows as $d \propto e^{N_e}$.

★ Quarks quickly move out of causal contact.

Confinement Formation Mechanism

★ 2. Ingredient: **Confinement** at energy scale Λ_c , $M_q/\Lambda_c \gg 1$



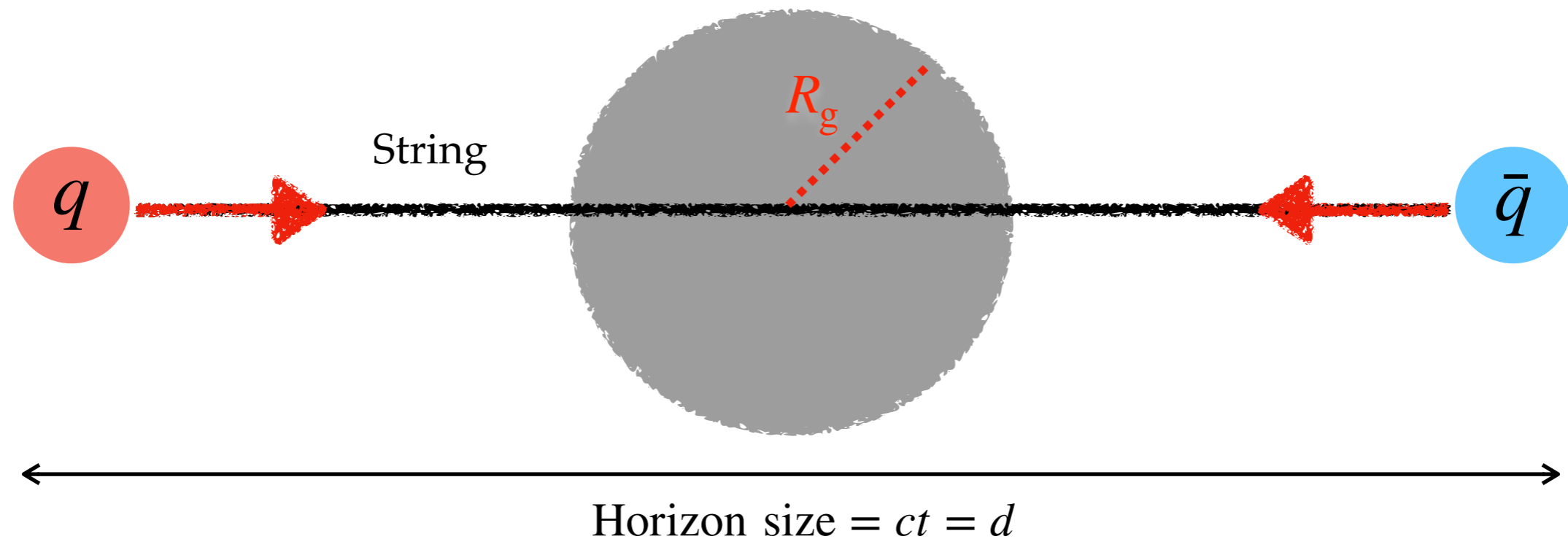
★ Flux tubes form connecting quark/anti-quark pairs.

★ The system cannot collapse as long as $d > r_H$.

★ String breaking into quarks pair, $P_{\text{tunnel}} \propto e^{-\pi \left(M_q/\Lambda_c \right)^2}$,
suppressed as long as $M_q/\Lambda_c \gg 1$.

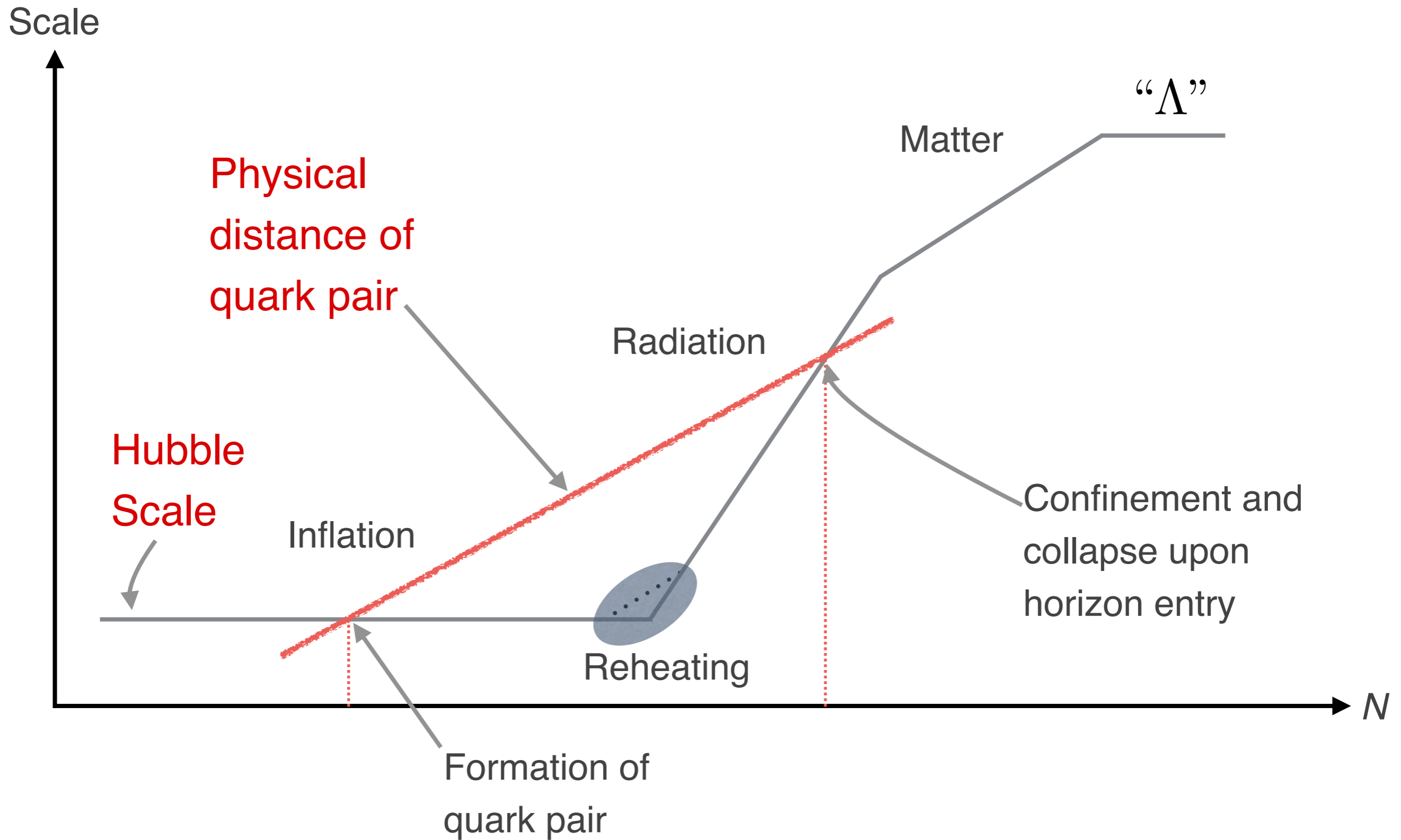
Confinement Formation Mechanism

★ 3. Ingredient: **Black hole formation** upon horizon entry



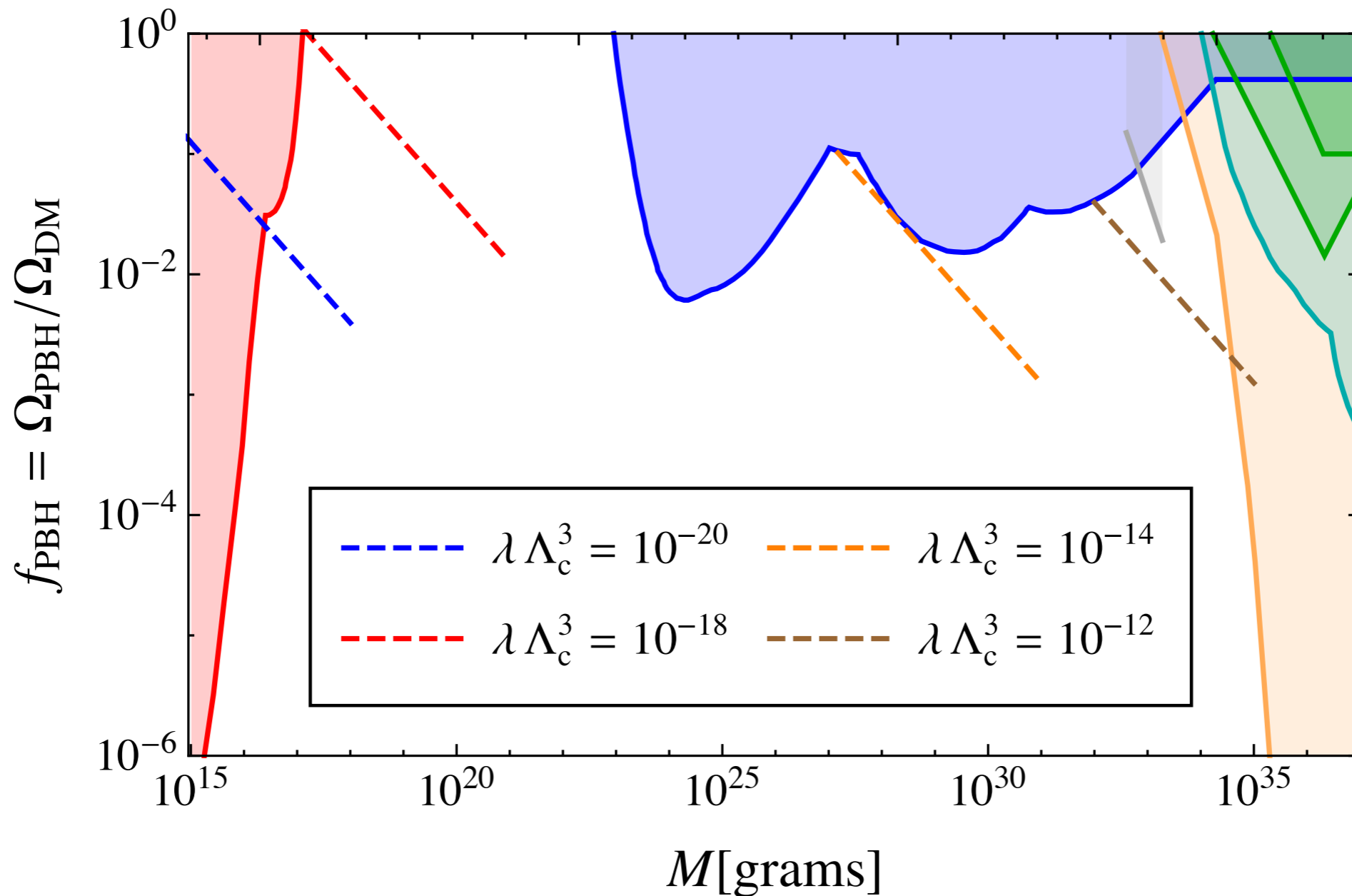
- ★ Acceleration of the quarks $a = \Lambda_c^2/m_q$ quickly leads to their ultra-relativistic motion.
- ★ The energy stored in the string is $E \simeq \Lambda_c^2 t \simeq M_g$, $R_g \gg \Lambda_c^{-1}$.
- ★ PBHs from inflationary overdensities are heavier by a factor $\sim \Lambda_c^2$.

Formation Scales



Dark Matter from Confinement

★ Present-day **dark matter distribution** vs *monochromatic* constraints:

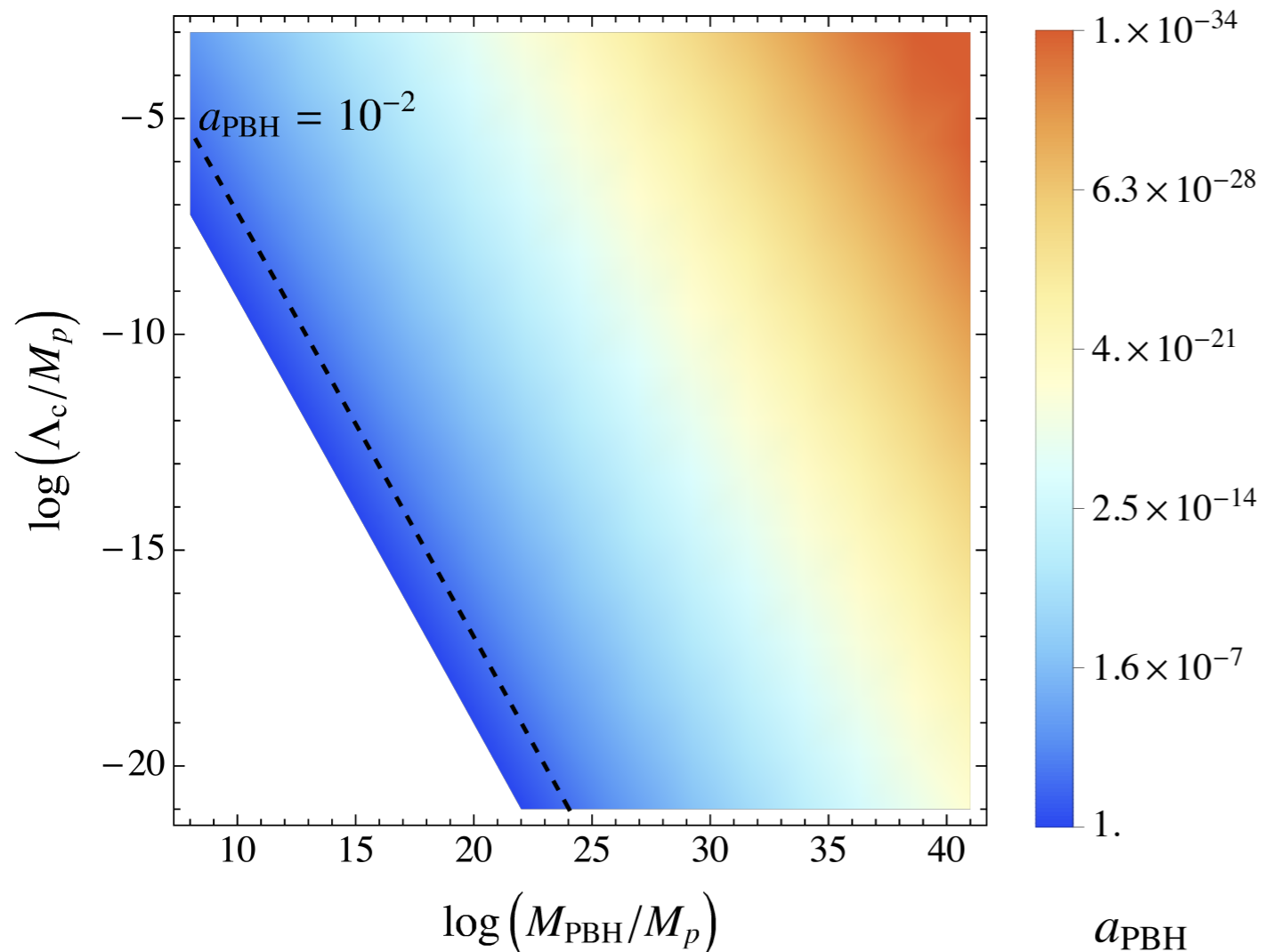
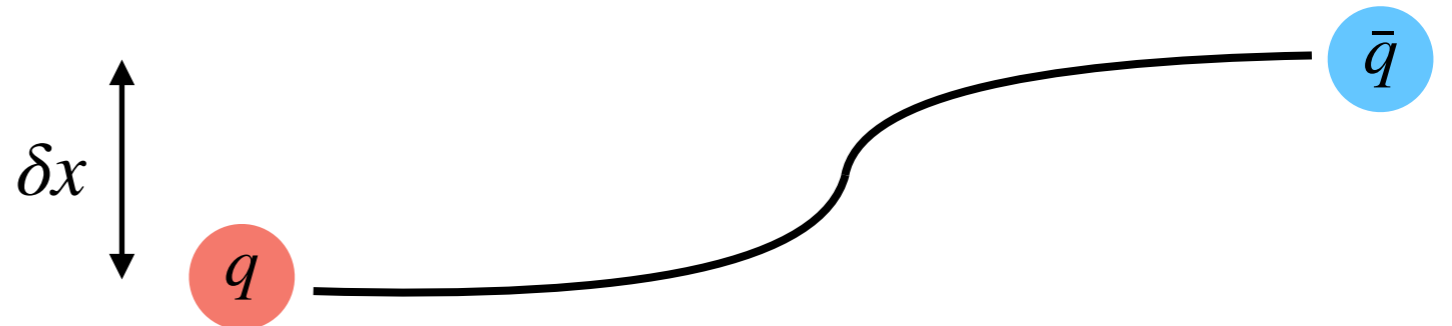


★ Find:
$$f_{\text{PBH}} \equiv \frac{\rho_{\text{PBH}}(t)}{\rho_{\text{CDM}}(t)} = \frac{32\pi}{3} \lambda \Lambda_c^3 \left(\frac{M_{\text{PBH}}}{M_{\text{eq}}} \right)^{-1/2}$$

High-Spin Subsolar PBHs

- ★ During inflation, the string undergoes a **Brownian motion**, induced by de Sitter quantum fluctuations, leading to **deviation from straightness**:

$$\delta x \simeq \sqrt{N_e} H_i^{-1}$$

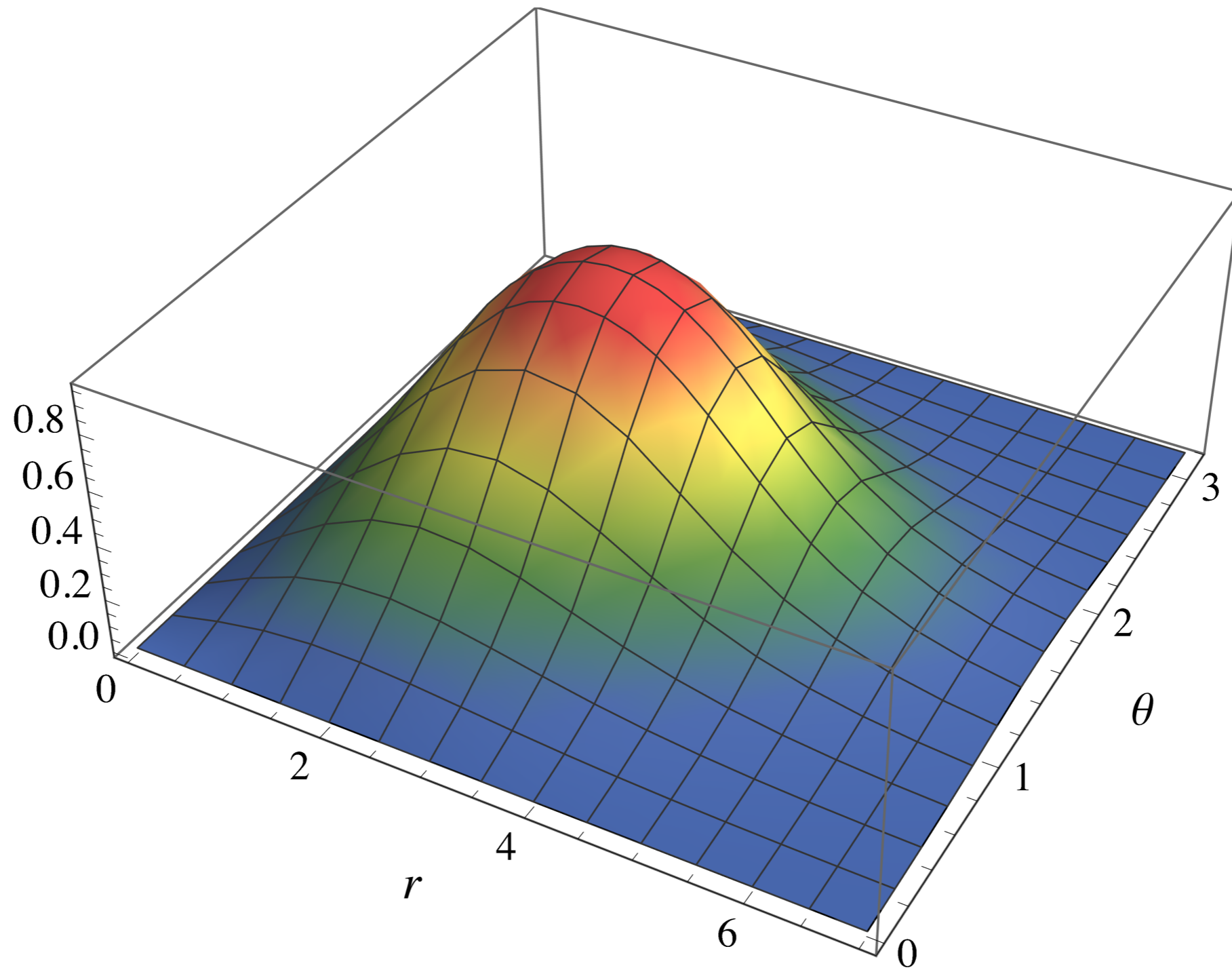


- ★ This leads to potentially **significant spin**:

$$a_{\text{PBH}} \simeq \frac{\delta x}{R_g}$$

$$\simeq \frac{1}{H M_{\text{PBH}}} \log\left(\frac{H M_{\text{PBH}}}{\Lambda_c^2}\right)^{1/2}$$

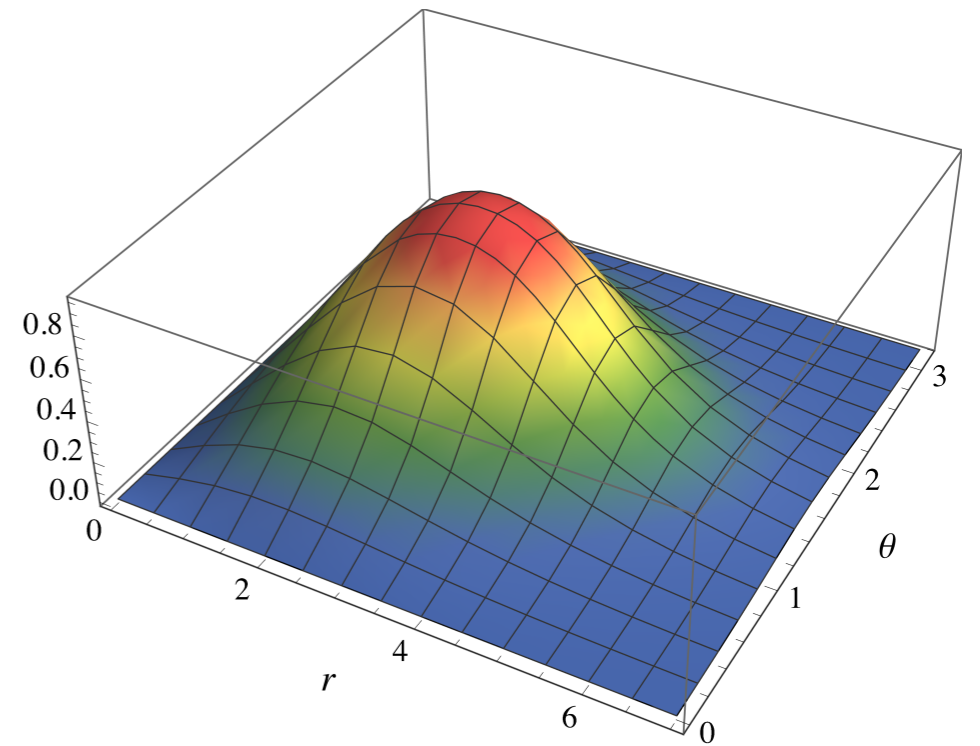
Formation of Vortices



[Dvali, FK, Zantedeschi 2021]

Formation of Vortices

- ★ Black Holes can be understood as **saturons**.
- ★ We showed that these admit **vortex structure**, in the case of near-extremal spin.
- ★ PBHs from confinement could provide **ideal prerequisites for vortex formation** due to highly spinning light PBHs.
- ★ If these PBHs provide the dark matter, their vorticity might explain **primordial magnetic fields**.
- ★ Besides, vorticity provides a **topological meaning to the stability of extremal black holes**.



[Dvali, FK, Zantedeschi 2021]

A decorative frame with scrollwork at the corners and top/bottom curves, enclosing the text.

Primordial Black Holes

and

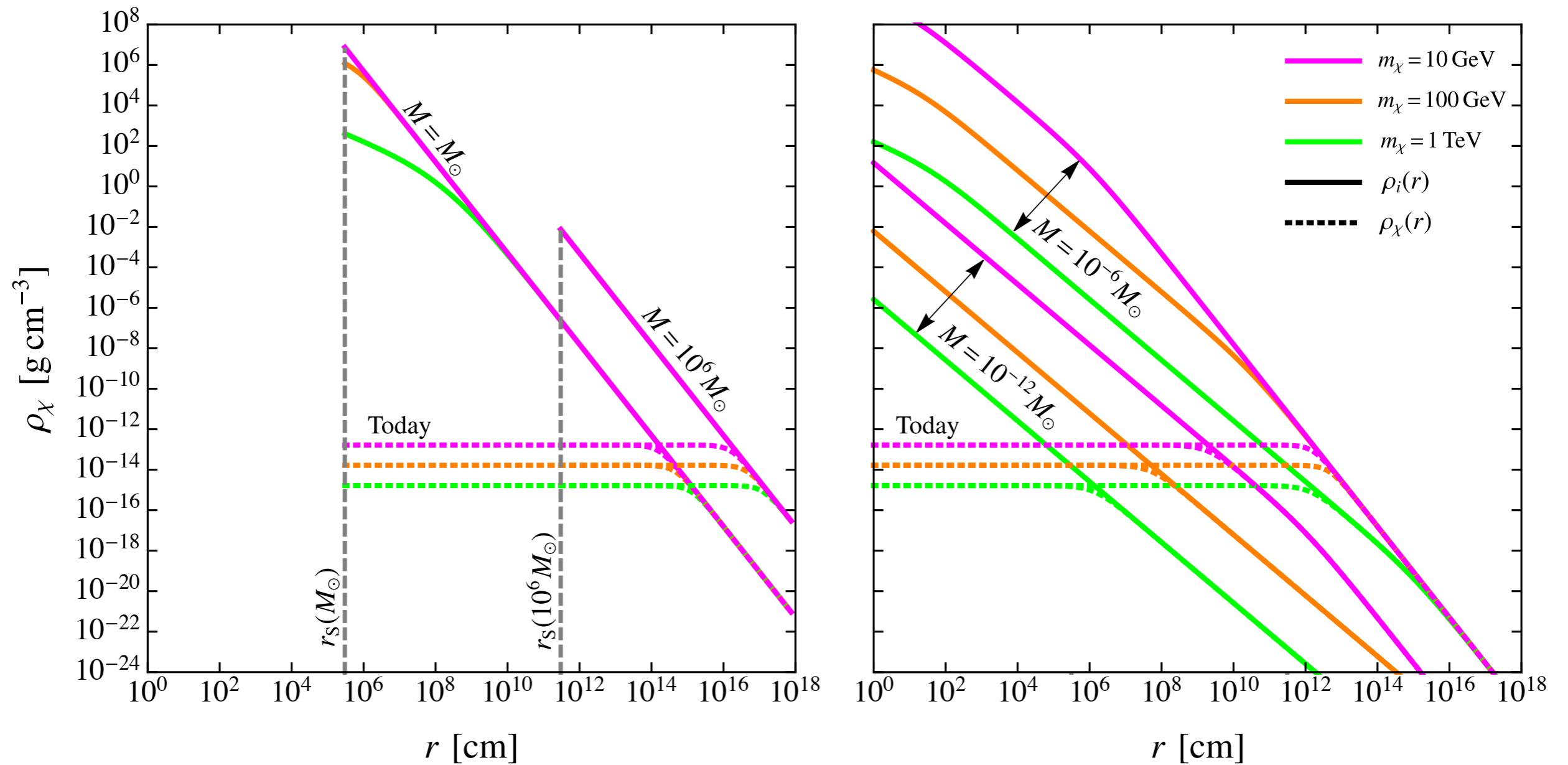
Particle Dark Matter

PBH @ Particle Dark Matter

- ★ Always when $f_{\text{PBH}} < 1$ there **must** be another dark matter component!
- ★ Study a **combined** scenario: **Dark Matter = PBHs + Particles**
 - ★ The latter will be **accreted** by the former; **formation of halos**.
 - ★ Study **WIMP annihilations** in PBH halos:
 - ★ The annihilation rate $\Gamma \propto n^2$.
 - ★ Halo profile does matter; **enhancement** of Γ in density spikes.
 - 1) Derive the **density profile** of the captured WIMPs;
 - 2) calculate the **annihilation rate**;
 - 3) and **compare to data**.

[Eroshenko 2016, Boucenna *et al.* 2017, Adamek *et al.* 2019, Carr, FK, Visinelli 2020 & 2021, Witte *et al.* 2022]

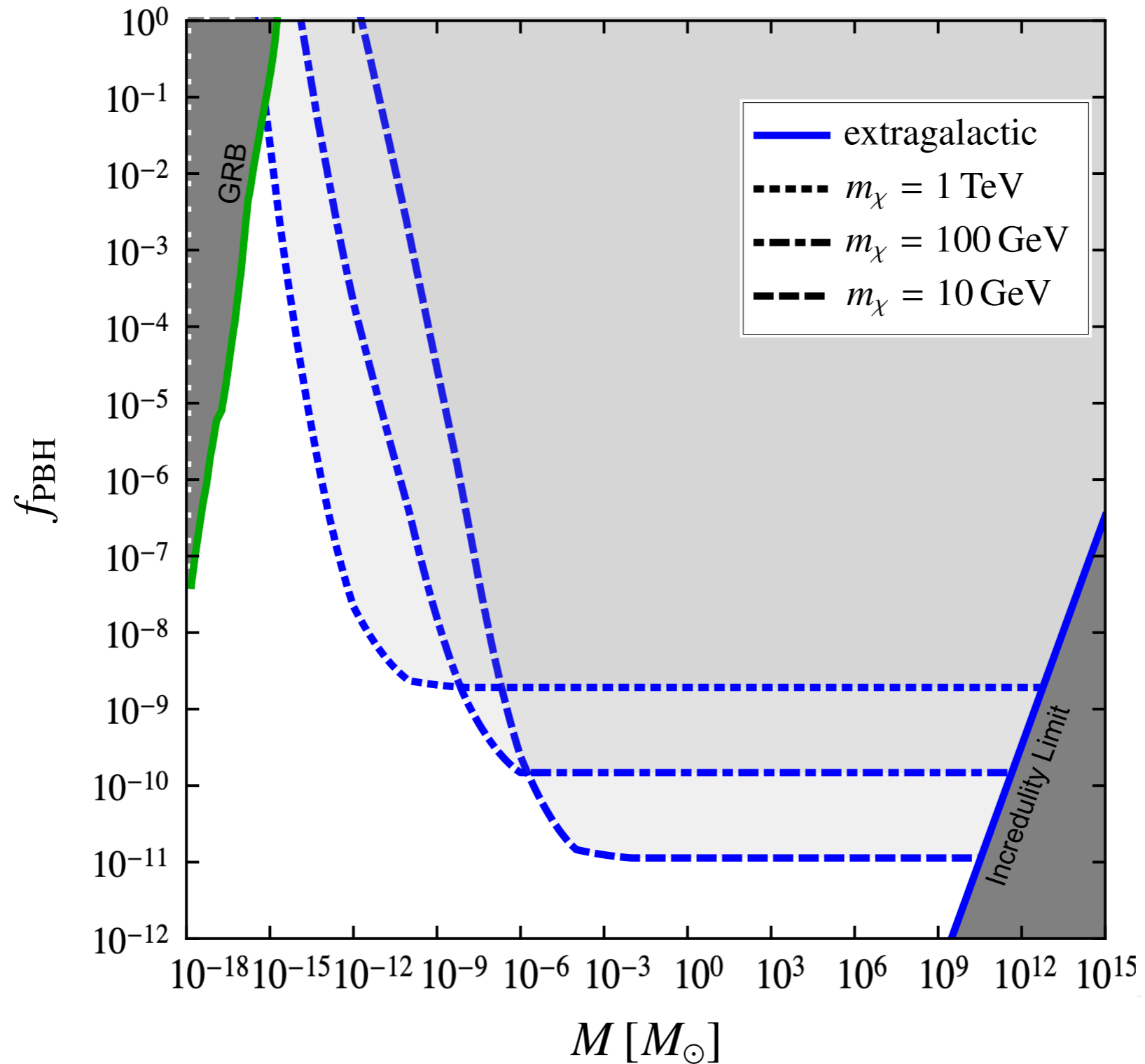
PBHs @ WIMPs



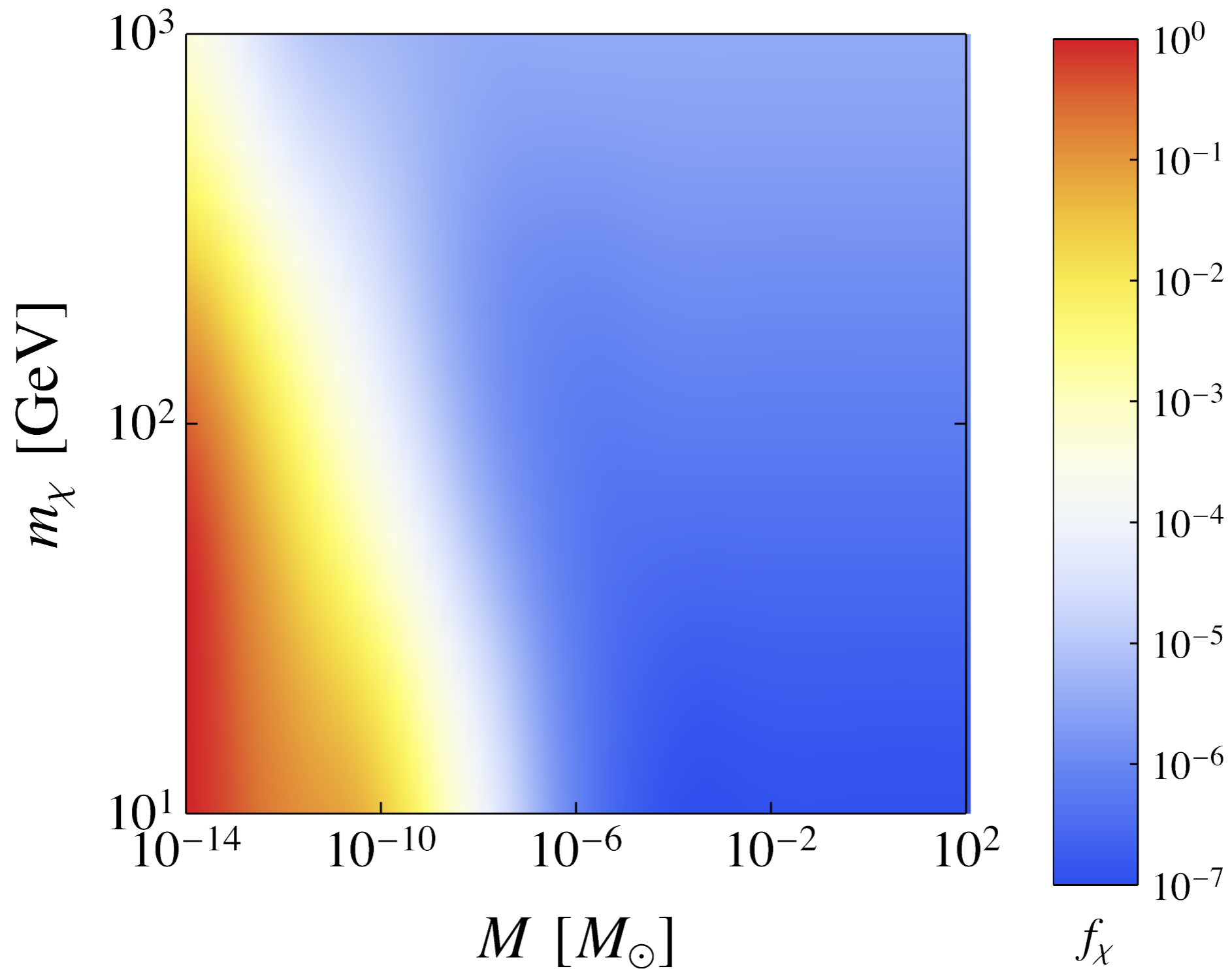
[Carr, FK, Visinelli 2021]

★ **Annihilations** lead to **plateaux** in the present-day halos.

PBHs @ WIMPs



PBHs @ WIMPs





Monochromatic

versus

Extended Mass Spectra

Critical Collapse

★ Usually: Assume

$$M_{BH} \propto M_H$$

↑
horizon mass

★ Critical scaling:

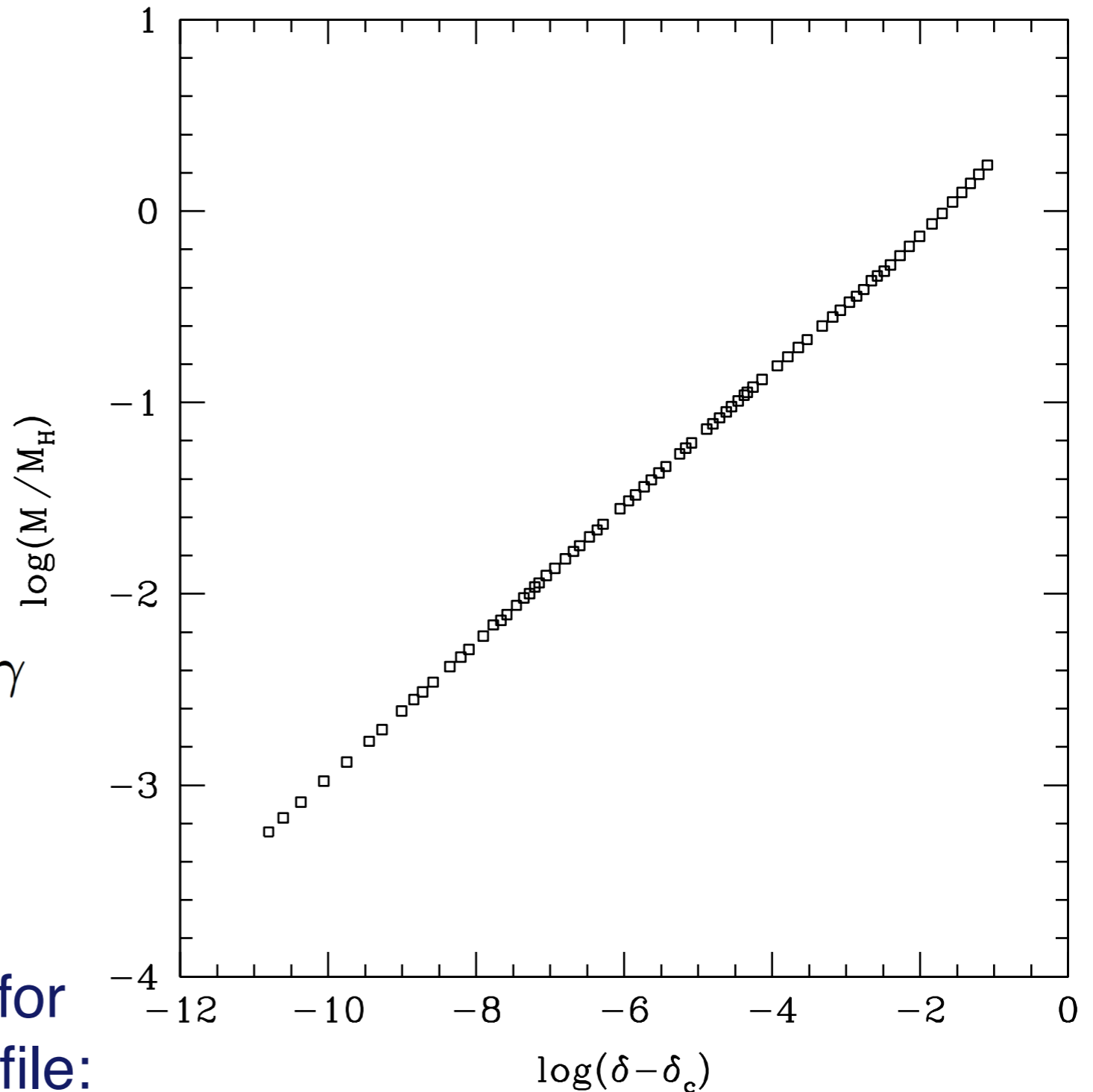
[Choptuik '93]

$$M_{BH} = k M_H (\delta - \delta_c)^\gamma$$

↑
density contrast

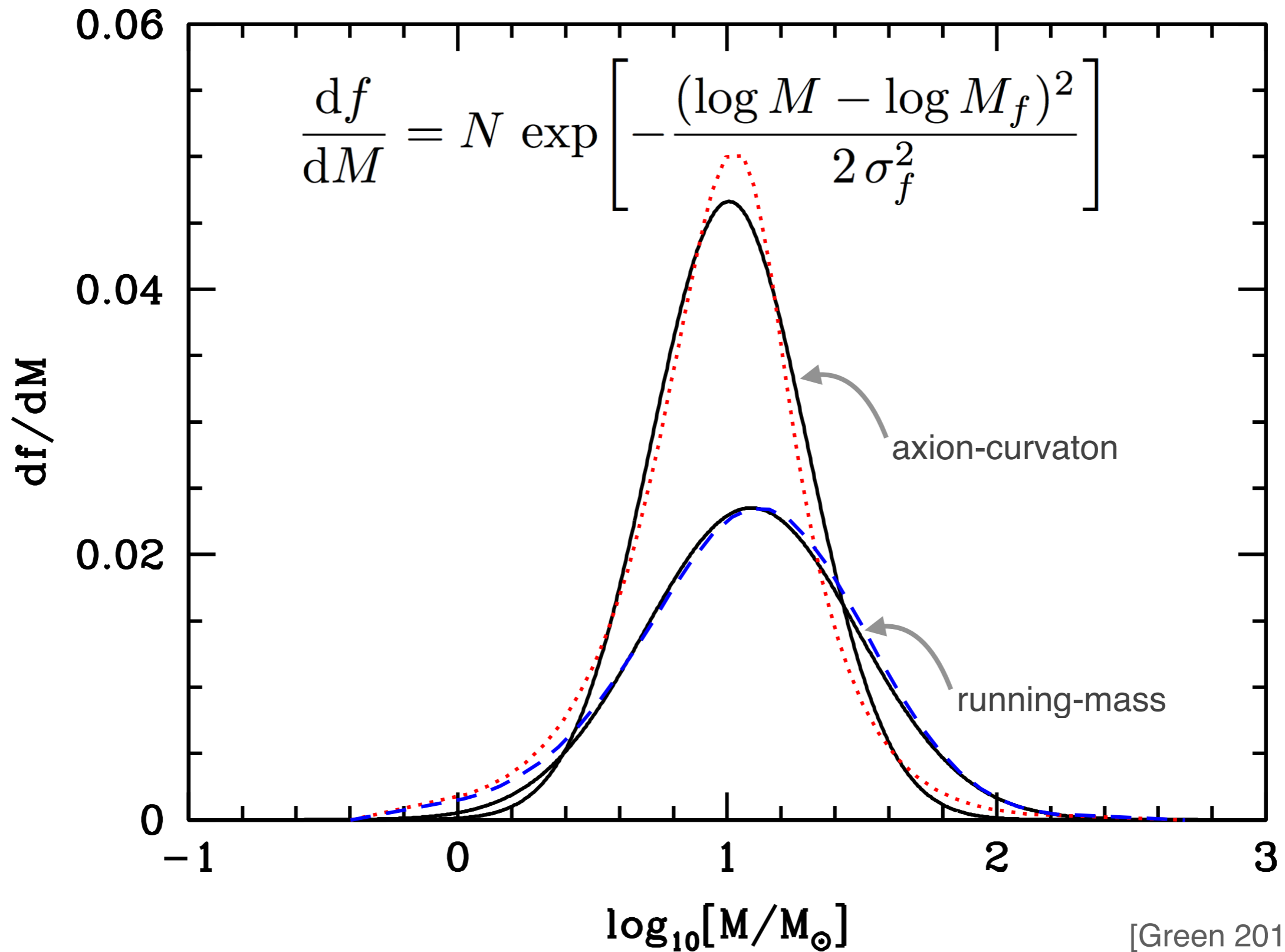
★ Radiation domination and for spherical Mexican-hat profile:

$$k \approx 3.3, \quad \delta_c \approx 0.45, \quad \gamma \approx 0.36$$



[Musco, Miller, Polnarev 2008]

More Systematic Study



More Systematic Study

