



# Precision physics

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**Dario Buttazzo**



# Disclaimer

 This talk is about **Physics** only.

 I will consider colliders that

- ◆ exist today (LHC, SuperKEKB, SPS)
- ◆ could be built today (FCC-ee, CEPC, CLIC, ILC)
- ◆ could be built tomorrow, after technological R&D  
(Muon collider, pp colliders)

 The physics potential of these machines is obviously very different.

The related ESPP decisions/considerations are also different...

# Why a future collider?

Independently of LHC results, a future collider will be necessary to make advancements in fundamental high-energy physics.

## *Where should we go??*

- ◆ No guaranteed discoveries: exploration of new domains
- ◆ High-energy collider has guaranteed science output: possibility to perform SM physics measurements in unknown energy domain.

Either validation of SM, or groundbreaking discovery.

- ◆ Expensive  $\implies$  need a big improvement in *as many as possible different directions*

# Why a future collider?

- ◆ What causes EWSB?

*i.e. is it the SM up to accessible energy scales?*

- ◆ What's the origin of Flavor (including leptons)?

*and what's the origin of CP violation?*

- ◆ What is Dark Matter?

- ◆ Unification

- ◆ Inflation

- ◆ Dark Energy

- ◆ Quantum gravity

Not clear if the solution lies at a scale accessible by colliders, and/or within particle physics...

# Why a future collider?

- ◆ What causes EWSB?

*i.e. is it the SM up to accessible energy scales?*

Clearly points to  
few TeV scale

- ◆ What's the origin of Flavor (including leptons)?

*and what's the origin of CP violation?*

Might point to  
few TeV scale,  
esp. if related to  
previous point

- ◆ What is Dark Matter?

- ◆ Unification

- ◆ Inflation

- ◆ Dark Energy

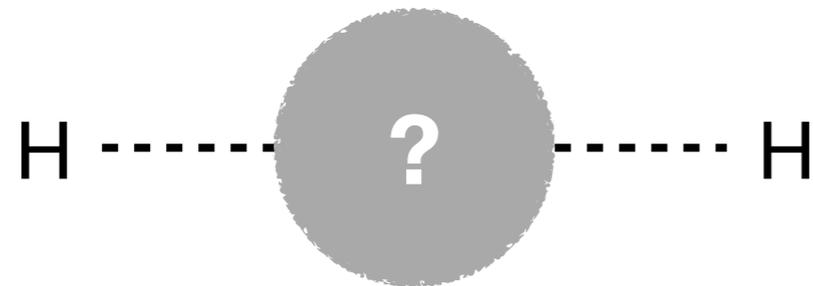
- ◆ Quantum gravity

Not clear if the solution  
lies at a scale accessible  
by colliders, and/or  
within particle physics...

# Why a few-TeV collider?

- ◆ Is it the SM up to the few TeV energy scale?

i.e. what causes EWSB?



Strong EWSB:

$$M_{\text{NP}} \approx g_{\star} f \leq 4\pi f, \quad f \gtrsim v$$

➔  $M_{\text{NP}} \lesssim 4\pi v \approx 3 \text{ TeV}$

Loops of (weakly coupled) new particles:

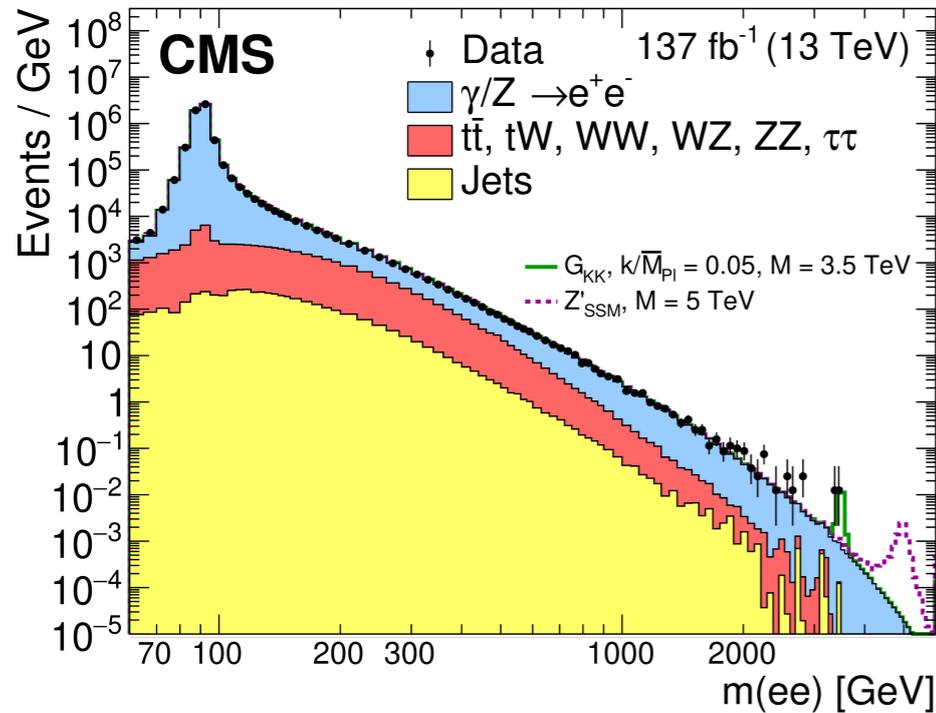
$$\delta m_H^2 \approx \frac{g^2}{16\pi^2} M_{\text{NP}}^2 \lesssim (gv)^2$$

rough estimate! there can easily be some O(1) factor!

goal: explore physics at least up to  $M_{\text{NP}} \approx 10 \text{ TeV}$ !

# Where do we stand?

- ◆ The SM works well at the TeV scale:  $M_{NP} \gtrsim$  few TeV directly



➔ see talk by R. Franceschini

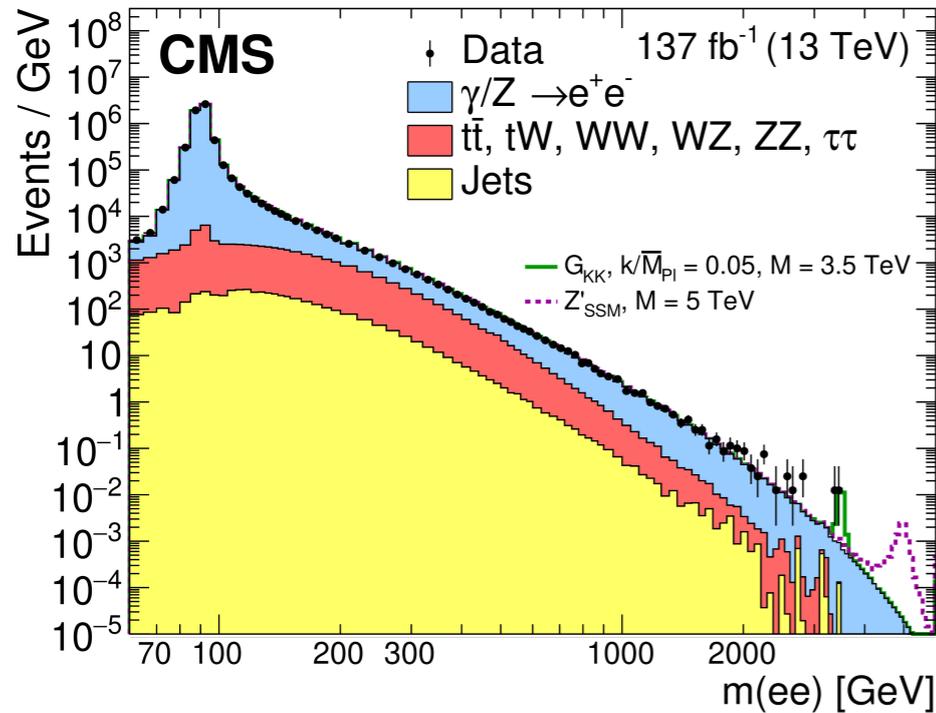
## ATLAS Heavy Particle Searches\* - 95% CL Upper Exclusion Limits

Status: March 2023

Gauge bosons	SSM $Z' \rightarrow \ell\ell$	$2 e, \mu$	-	-	139	$Z'$ mass	5.1 TeV
	SSM $Z' \rightarrow \tau\tau$	$2 \tau$	-	-	36.1	$Z'$ mass	2.42 TeV
	Leptophobic $Z' \rightarrow bb$	-	$2 b$	-	36.1	$Z'$ mass	2.1 TeV
	Leptophobic $Z' \rightarrow tt$	$0 e, \mu$	$\geq 1 b, \geq 2 J$	Yes	139	$Z'$ mass	4.1 TeV
	SSM $W' \rightarrow \ell\nu$	$1 e, \mu$	-	Yes	139	$W'$ mass	6.0 TeV
	SSM $W' \rightarrow \tau\nu$	$1 \tau$	-	Yes	139	$W'$ mass	5.0 TeV
	SSM $W' \rightarrow tb$	-	$\geq 1 b, \geq 1 J$	-	139	$W'$ mass	4.4 TeV
	HVT $W' \rightarrow WZ$ model B	$0-2 e, \mu$	$2 j / 1 J$	Yes	139	$W'$ mass	4.3 TeV
	HVT $W' \rightarrow WZ \rightarrow \ell\nu \ell' \ell'$ model C	$3 e, \mu$	$2 j$ (VBF)	Yes	139	$W'$ mass	340 GeV
	HVT $Z' \rightarrow WW$ model B	$1 e, \mu$	$2 j / 1 J$	Yes	139	$Z'$ mass	3.9 TeV
LRSM $W_R \rightarrow \mu N_R$	$2 \mu$	$1 J$	-	80	$W_R$ mass	5.0 TeV	
DM	Axial-vector med. (Dirac DM)	-	$2 j$	-	139	$m_{med}$	3.8 TeV
	Pseudo-scalar med. (Dirac DM)	$0 e, \mu, \tau, \gamma$	$1-4 j$	Yes	139	$m_{med}$	376 GeV
	Vector med. $Z'$ -2HDM (Dirac DM)	$0 e, \mu$	$2 b$	Yes	139	$m_{Z'}$	3.0 TeV
	Pseudo-scalar med. 2HDM+a	multi-channel	-	-	139	$m_a$	800 GeV
LQ	Scalar LQ 1 <sup>st</sup> gen	$2 e$	$\geq 2 j$	Yes	139	LQ mass	1.8 TeV
	Scalar LQ 2 <sup>nd</sup> gen	$2 \mu$	$\geq 2 j$	Yes	139	LQ mass	1.7 TeV
	Scalar LQ 3 <sup>rd</sup> gen	$1 \tau$	$2 b$	Yes	139	$LQ_3^u$ mass	1.49 TeV
	Scalar LQ 3 <sup>rd</sup> gen	$0 e, \mu$	$\geq 2 j, \geq 2 b$	Yes	139	$LQ_3^d$ mass	1.24 TeV
	Scalar LQ 3 <sup>rd</sup> gen	$\geq 2 e, \mu, \geq 1 \tau, \geq 1 j, \geq 1 b$	-	-	139	$LQ_3^d$ mass	1.43 TeV
	Scalar LQ 3 <sup>rd</sup> gen	$0 e, \mu, \geq 1 \tau, 0-2 j, 2 b$	Yes	139	$LQ_3^d$ mass	1.26 TeV	
	Vector LQ mix gen	multi-channel	$\geq 1 j, \geq 1 b$	Yes	139	$LQ_3^d$ mass	2.0 TeV
	Vector LQ 3 <sup>rd</sup> gen	$2 e, \mu, \tau$	$\geq 1 b$	Yes	139	$LQ_3^d$ mass	1.96 TeV
Vector-like fermions	VLQ $TT \rightarrow Zt + X$	$2e/2\mu/\geq 3e, \mu$	$\geq 1 b, \geq 1 j$	-	139	T mass	1.46 TeV
	VLQ $BB \rightarrow Wt/Zb + X$	multi-channel	-	-	36.1	B mass	1.34 TeV
	VLQ $T_{5/3} T_{5/3} T_{5/3} \rightarrow Wt + X$	$2(SS)/\geq 3 e, \mu$	$\geq 1 b, \geq 1 j$	Yes	36.1	$T_{5/3}$ mass	1.64 TeV
	VLQ $T \rightarrow Ht/Zt$	$1 e, \mu$	$\geq 1 b, \geq 3 j$	Yes	139	T mass	1.8 TeV
	VLQ $Y \rightarrow Wb$	$1 e, \mu$	$\geq 1 b, \geq 1 j$	Yes	36.1	Y mass	1.85 TeV
	VLQ $B \rightarrow Hb$	$0 e, \mu$	$\geq 2b, \geq 1j, \geq 1J$	-	139	B mass	2.0 TeV
	VLL $\tau' \rightarrow Z\tau/H\tau$	multi-channel	$\geq 1j$	Yes	139	$\tau'$ mass	898 GeV

# Where do we stand?

- ◆ The SM works well at the TeV scale:  $M_{NP} \gtrsim$  few TeV directly



see talk by R. Franceschini

- ◆ The Higgs boson is SM-like:

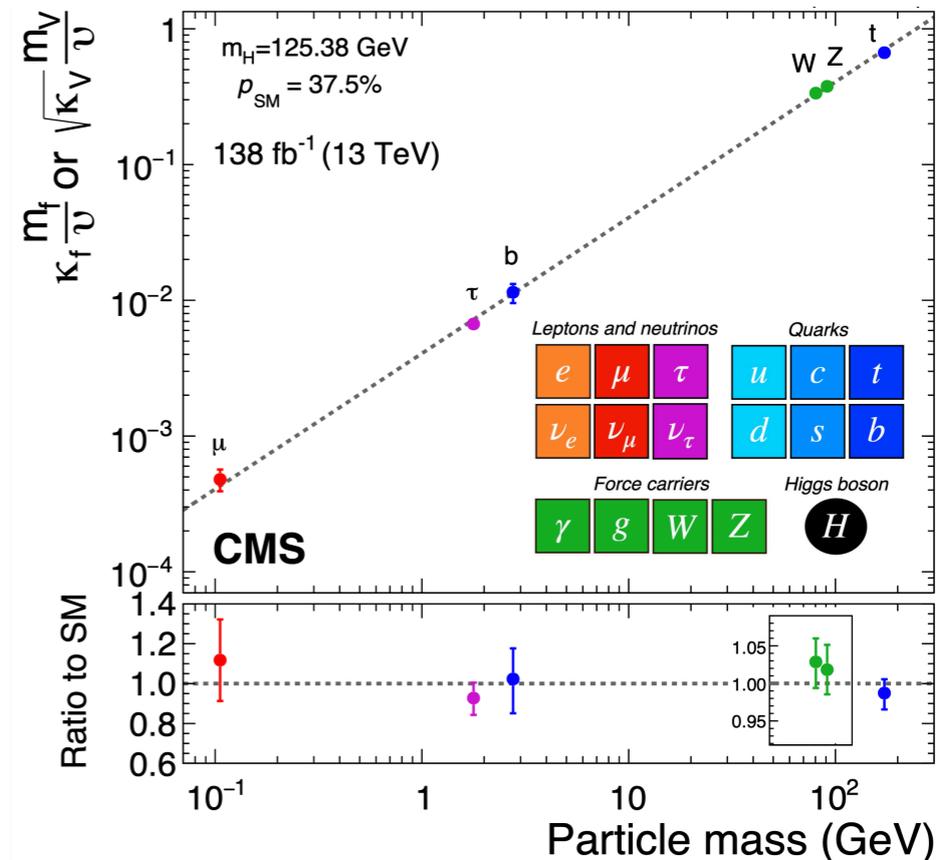
$$\delta\kappa \sim \frac{v^2}{M_{NP}^2} g_\star^2 \lesssim 5\%$$

$$\longrightarrow M_{NP} \gtrsim g_\star \text{ TeV}$$

## ATLAS Heavy Particle Searches\* - 95% CL Upper Exclusion Limits

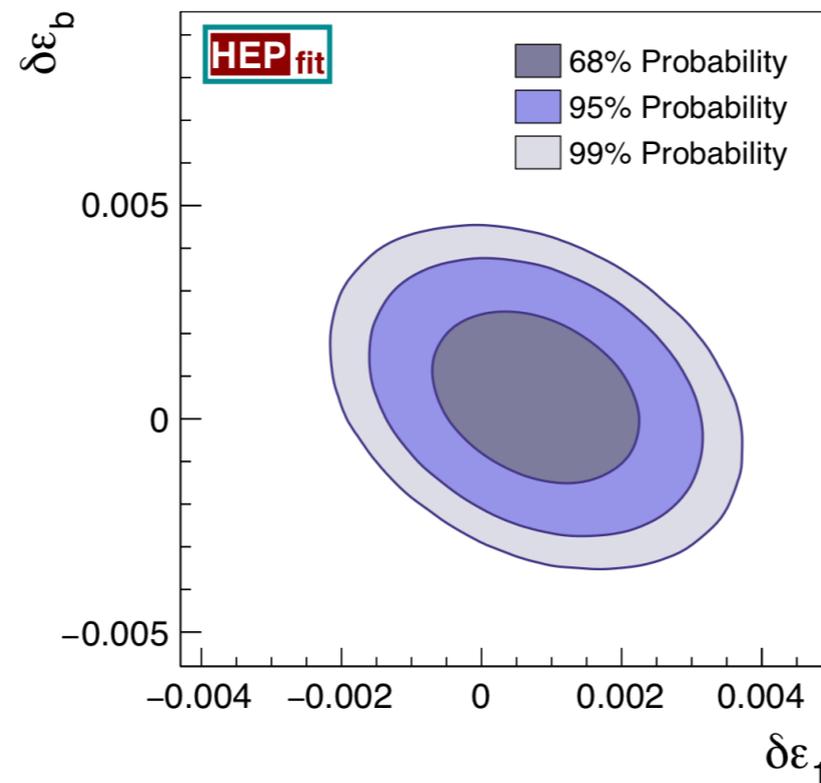
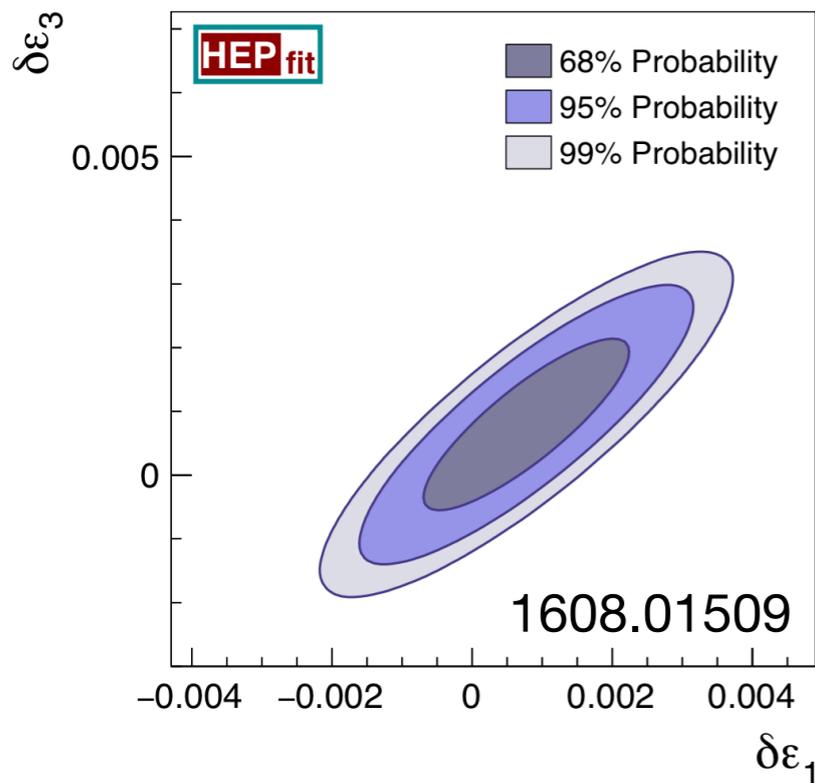
Status: March 2023

Category	Search	Final State	Signature	Efficiency	Upper Limit
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# Where do we stand?

- ◆ The EW sector is SM-like:  $M_{\text{NP}} \gtrsim \text{few TeV}$

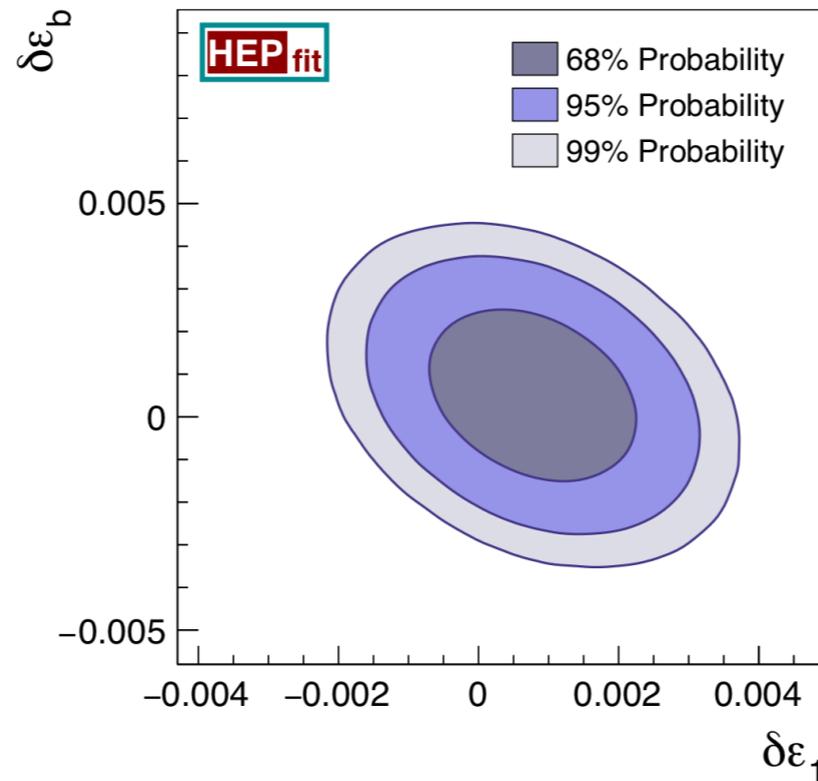
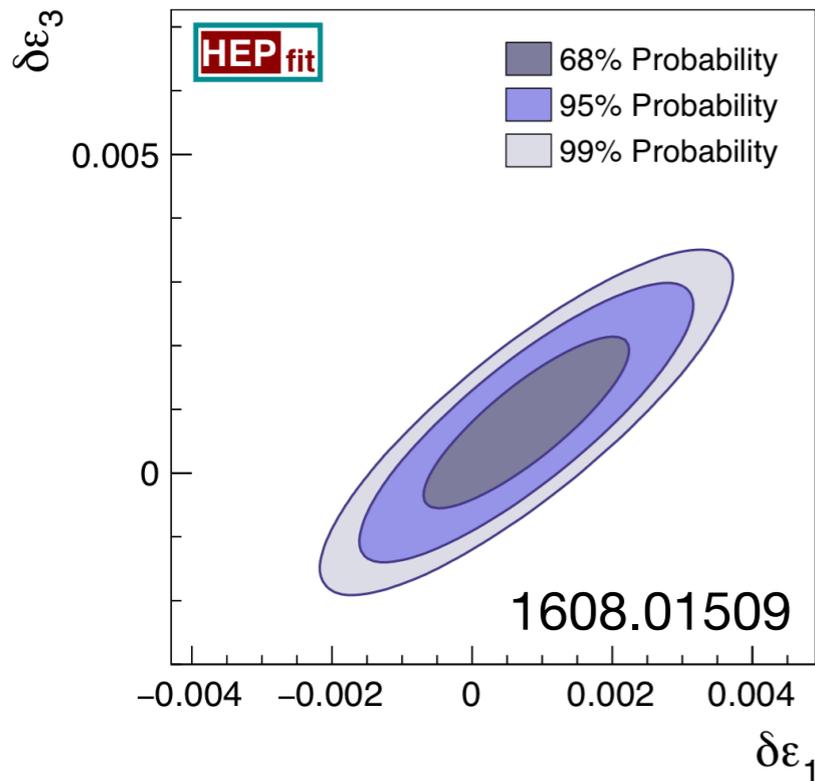


$$\delta\epsilon \sim \frac{m_W^2}{M_{\text{NP}}^2} \lesssim \text{few} \times 10^{-3}$$

➔  $M_{\text{NP}} \gtrsim 2 \text{ TeV}$

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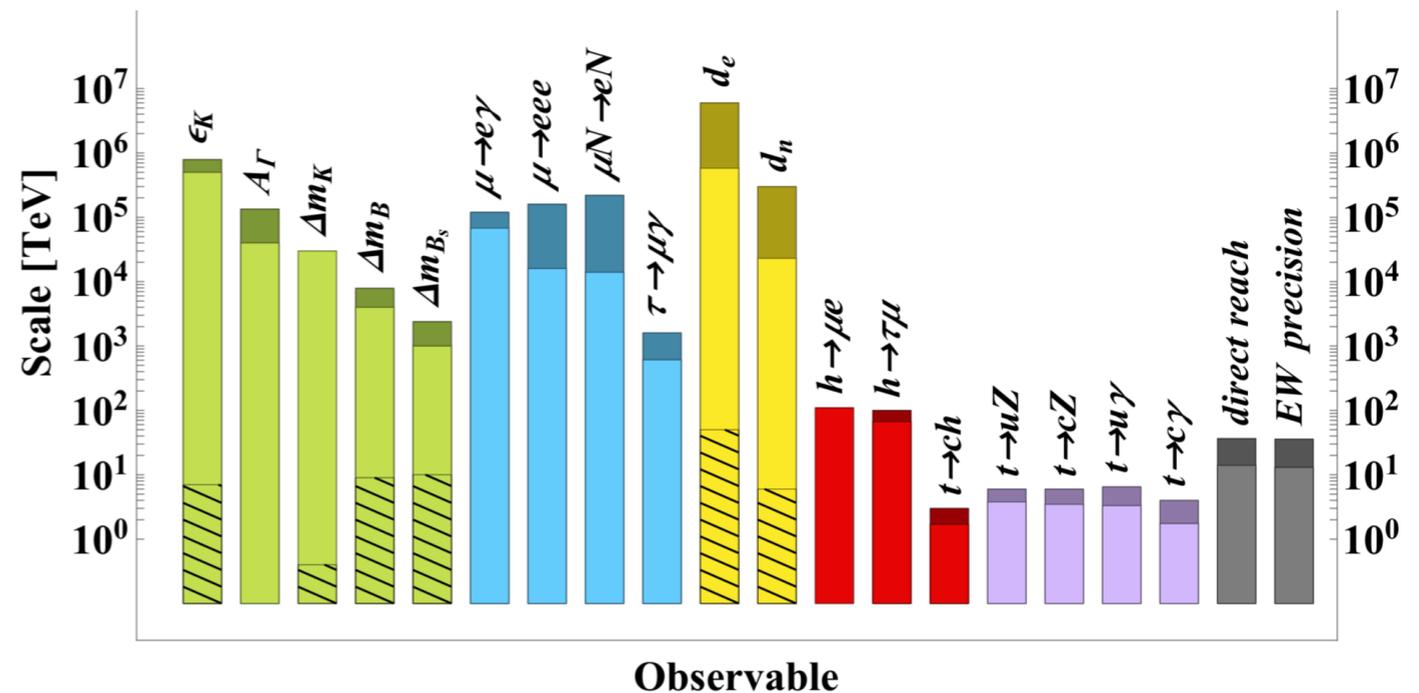
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➔  $M_{\text{NP}} \gtrsim 2 \text{ TeV}$

- ◆ The CKM picture of flavor physics works well; lepton flavor is conserved; no CPV besides CKM phase

$$\frac{\delta\mathcal{O}}{\mathcal{O}_{\text{SM}}} \sim \frac{v^2}{M_{\text{NP}}^2} \frac{4\pi}{\alpha} \frac{1}{\xi_{ij}} \lesssim 10\%$$

➔  $M_{\text{NP}} \gtrsim 3 \text{ TeV} / \sqrt{\xi_{ij}}$



# The flavor puzzle

- SM Yukawa couplings have an extremely hierarchical pattern

$$m_u \sim \begin{pmatrix} \cdot & \cdot & \text{large red circle} \end{pmatrix} \quad V_{\text{CKM}} \sim \begin{pmatrix} \text{large purple circle} & \text{small purple circle} & \text{tiny purple circle} \\ \text{small purple circle} & \text{large purple circle} & \text{tiny purple circle} \\ \text{tiny purple circle} & \text{tiny purple circle} & \text{large purple circle} \end{pmatrix} \quad m_\ell \sim \begin{pmatrix} \cdot & \cdot & \text{small blue circle} \end{pmatrix}$$

$$m_d \sim \begin{pmatrix} \cdot & \cdot & \text{small green circle} \end{pmatrix}$$

➡ What's the origin of this flavor structure? Why are there 3 families?

- Most likely NP in the Higgs sector couples to SM fermions in similar way...

$$Y_u \approx \begin{pmatrix} \text{small} & \text{dashed box with tiny red dot} \\ \text{dashed line} & \text{large red circle} \end{pmatrix} \quad \text{Diagram: fermion lines meeting at a purple dot} \quad \text{Diagram: fermion lines meeting at a purple dot with a grey oval labeled 'NP' in between} \quad \lambda_q \approx \begin{pmatrix} \text{small} & \text{dashed box with tiny red dot} \\ \text{dashed box with tiny red dot} & \text{large red circle} \end{pmatrix}$$

- Symmetries: e.g. MFV or U(2) models

[Barbieri et al. 2011](#); [Isidori et al. 2017](#); ...

- Dynamics: different NP scales for different families, related to Higgs

[Panico, Pomarol 2016](#); [Bordone et al. 2017](#), etc...

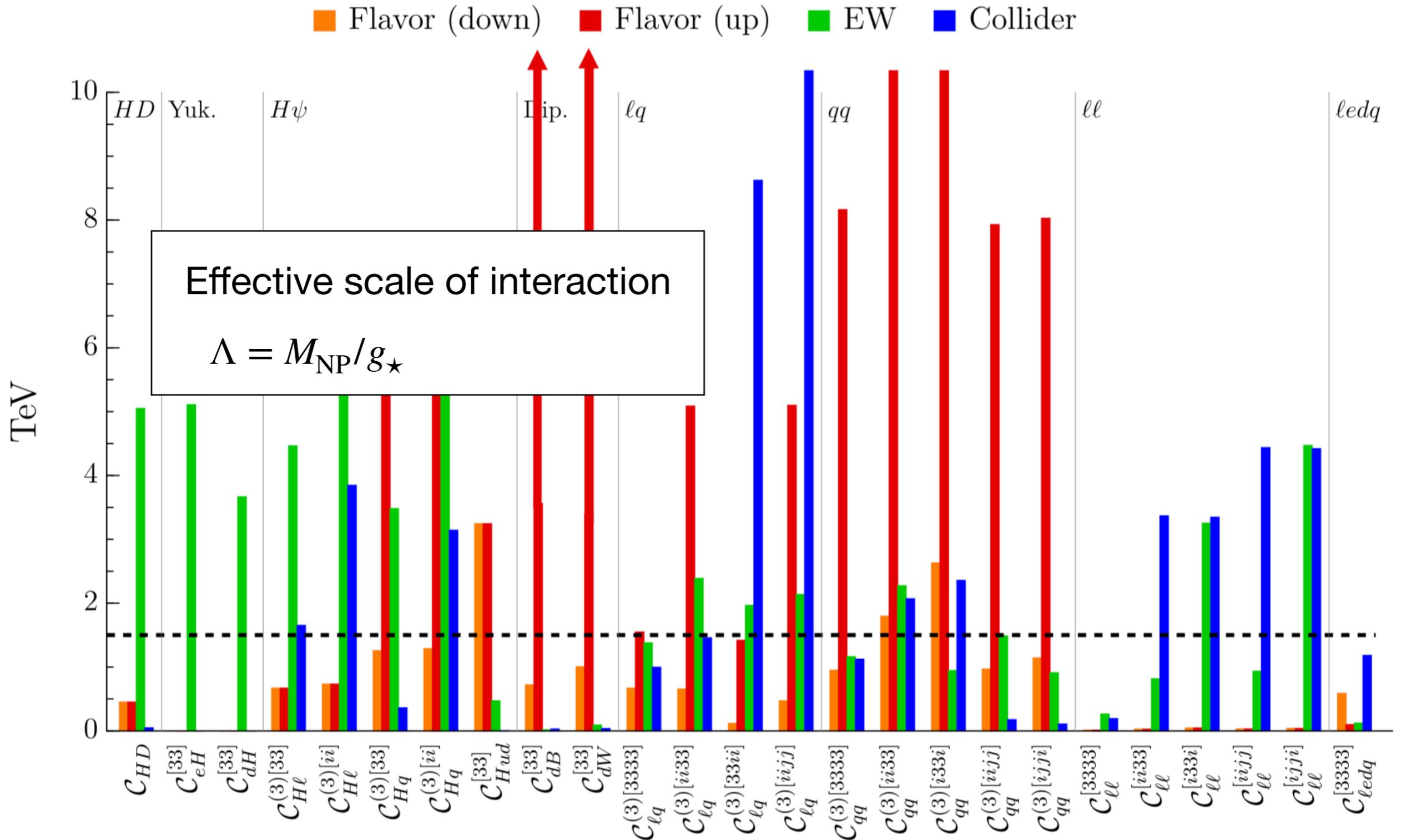


$$M_{\text{NP}} \lesssim 3 \text{ TeV}$$

with O(1) couplings

# Where do we stand?

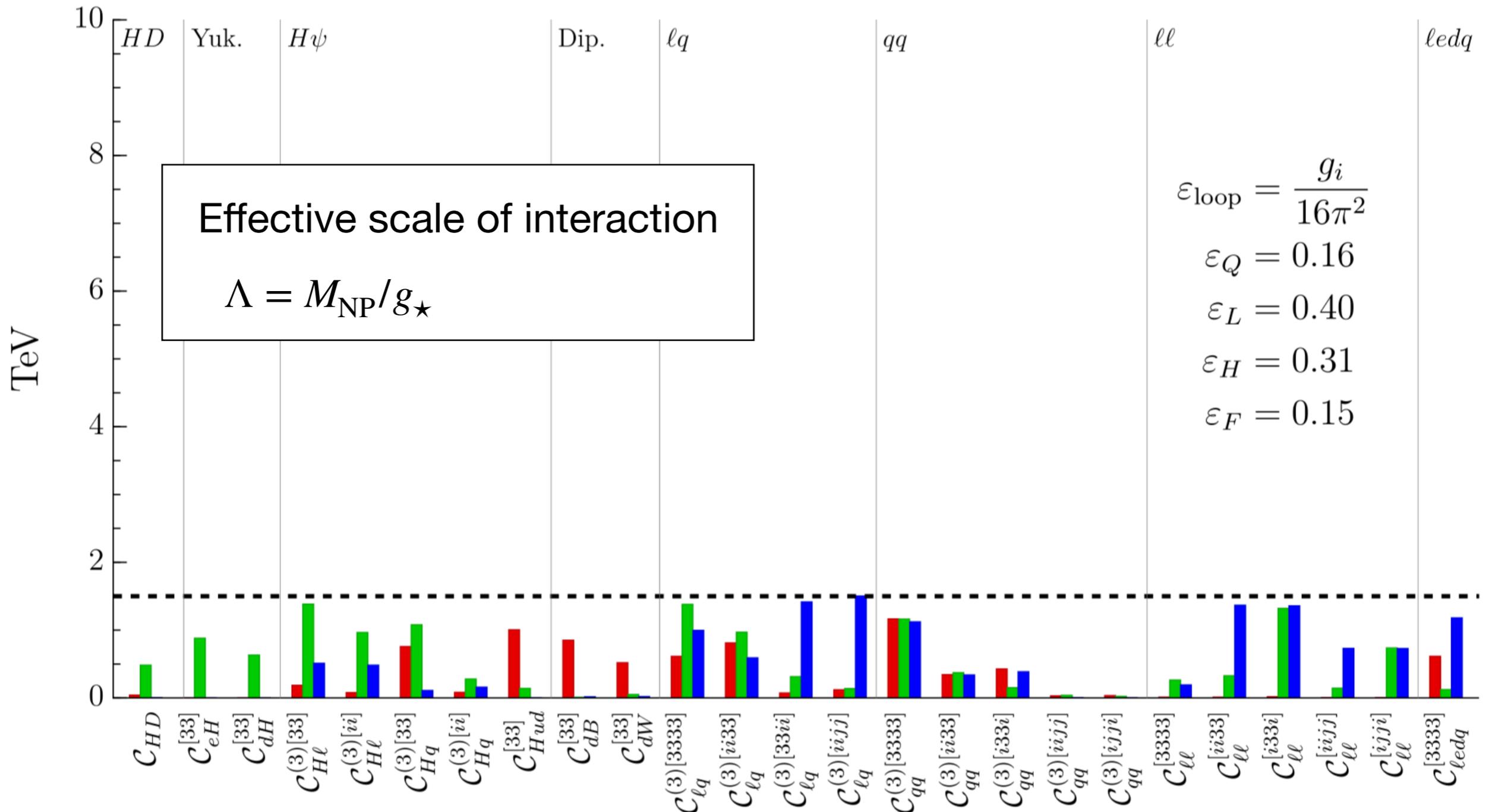
- With CKM-like suppression ( $U(2)^3$  flavor symmetry)



# Where do we stand?

- ◆ With CKM-like suppression ( $U(2)^3$  flavor symmetry)

■ Flavor ■ EW ■ Collider



# The next 15 years: Flavor

- ◆ Significant improvement in flavor measurements in the next (few) years!

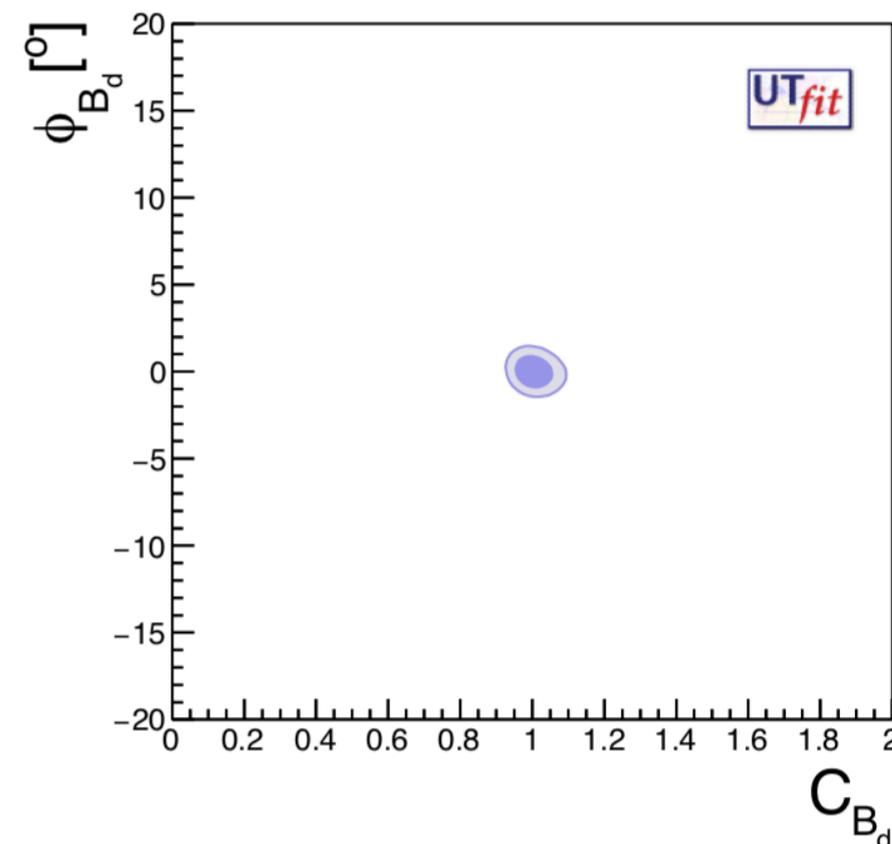
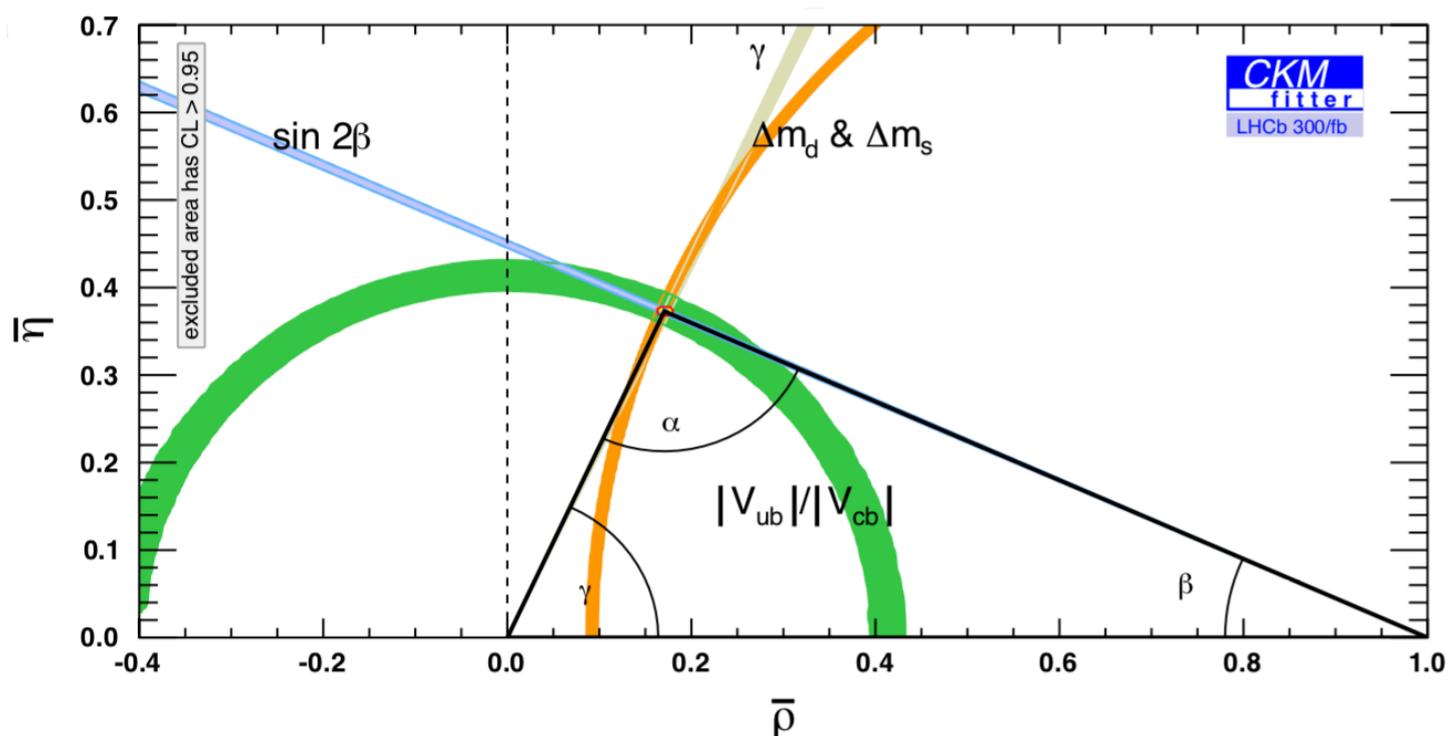


(upgrade 2)

- ▶  $O(10^{14})$  b and c hadrons
- ▶  $O(10^{11})$   $\tau$  leptons



- ▶  $O(10^{10})$  B mesons
- ▶  $O(10^{10})$   $\tau$ 's  
in clean environment



- ▶ Precision on CKM matrix elements  $< 1\%$   
(tree-level and loop)

- ▶ Needed as input of SM predictions in all other observables!

- ▶ CPV in Bs system. CPV in charm with extreme precision.

**$O(15 \text{ y})$  timescale!**

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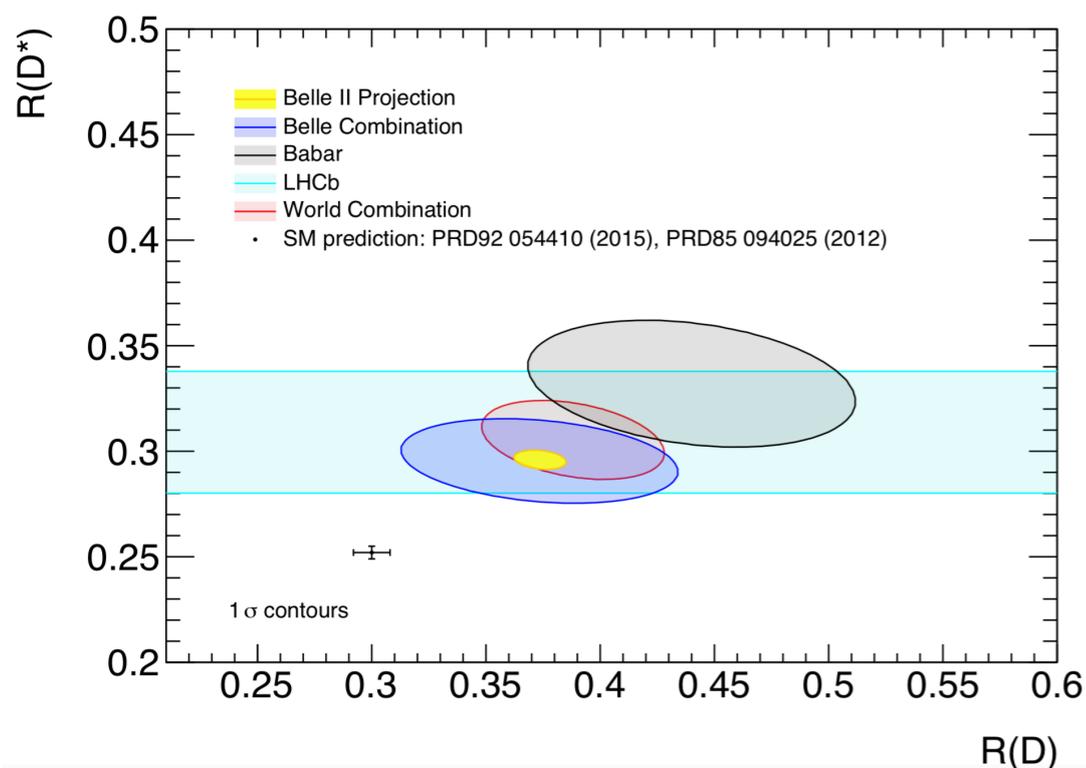


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**$O(15 \text{ y})$  timescale!**

- ▶ Semi-leptonic decays  $b \rightarrow q\ell\nu$
- ▶ Semi-tauonic decays @ few %  
 $\Rightarrow M_{\text{NP}} > 5 \text{ TeV} \times g_{\star}$   
 (today below 1 TeV)
- ▶ Rare leptonic & semi-leptonic B decays
  - ▶ Access to  $b \rightarrow d\ell\ell$  transitions
  - ▶ LFU below 1% precision
- ▶ Rare tau decays and LFV

For the first time precise measurements of rare processes for different flavors:  
 $b \rightarrow s$  vs  $b \rightarrow d$ ;  $\tau$  vs  $\mu, e$ ;  $\ell^{\pm}$  vs  $\nu_{\ell}$

Ultimate precision on all 'visible' B and D decay modes

# The next 15 years: Flavor

- Access to FCNC decays with neutrinos and taus for the first time!  
crucial to determine up vs. down alignment of NP: can suppress only one!

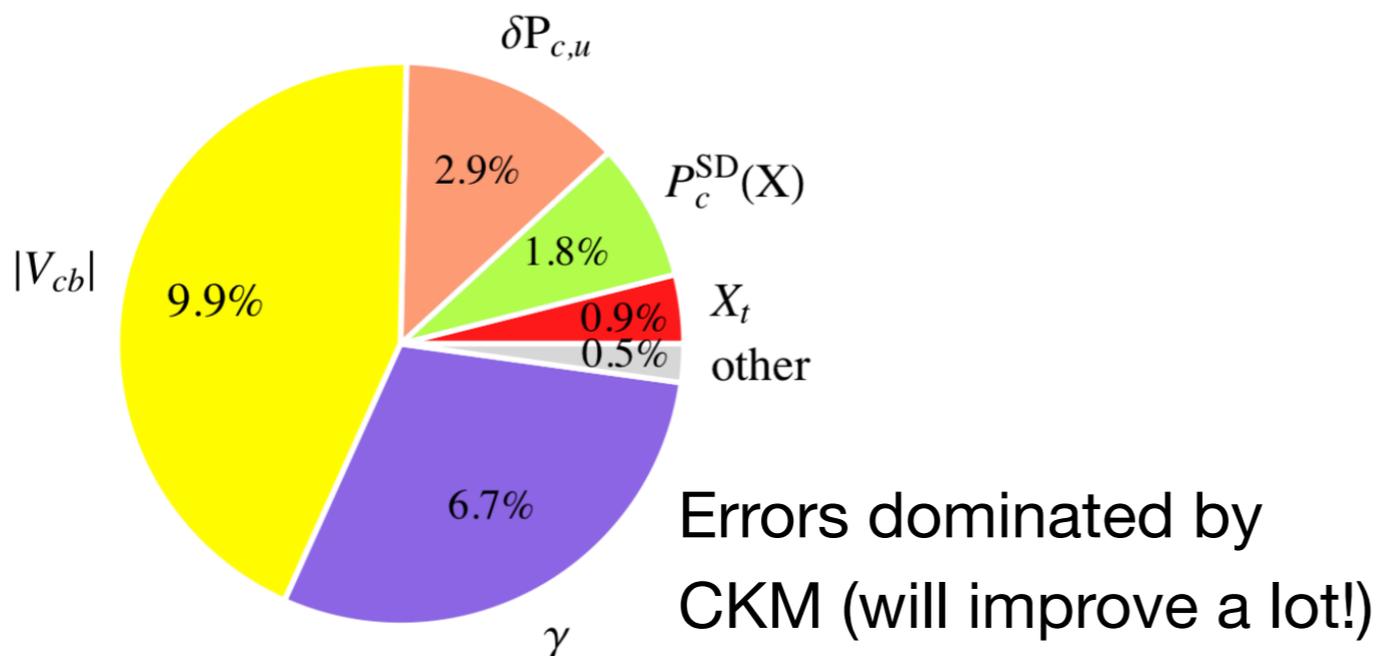
- Belle II will measure  $B \rightarrow K^{(*)}\nu\nu$  to 10%

O(10 y) timescale!

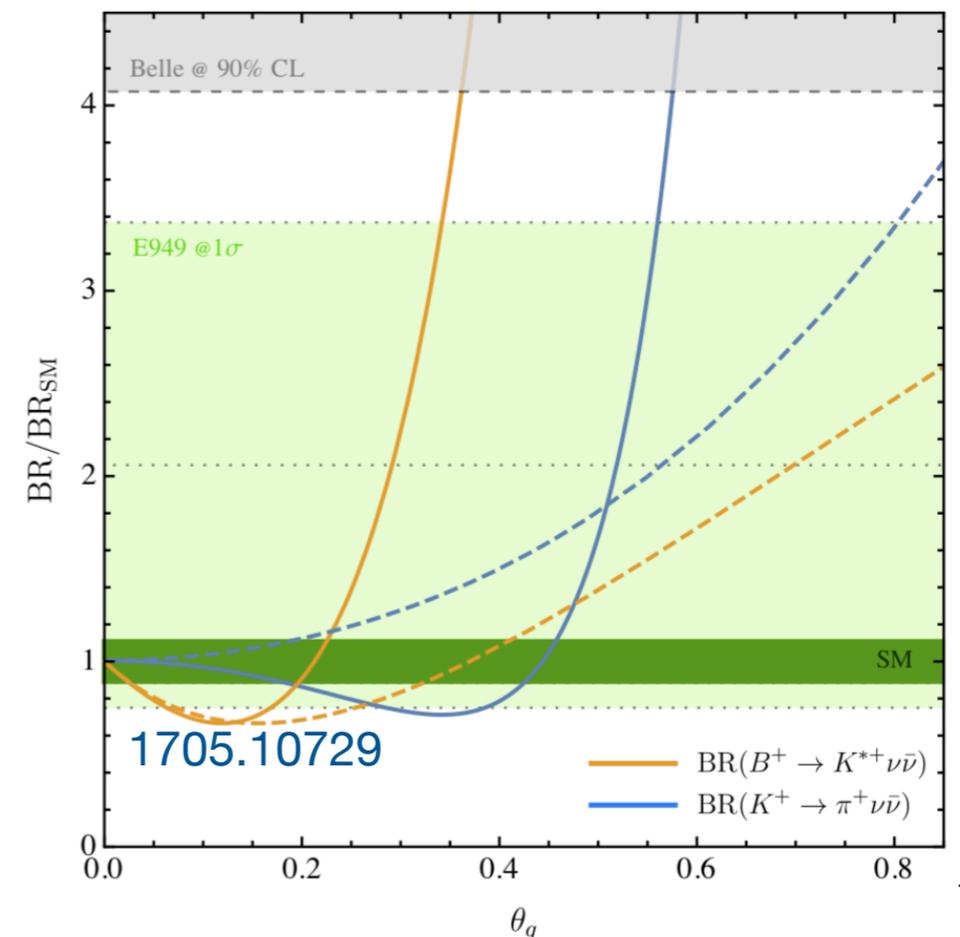


Observables	Belle II 50 ab <sup>-1</sup>
Br( $B^+ \rightarrow K^+\nu\bar{\nu}$ )	11%
Br( $B^0 \rightarrow K^{*0}\nu\bar{\nu}$ )	9.6%
Br( $B^+ \rightarrow K^{*+}\nu\bar{\nu}$ )	9.3%

- $K^+ \rightarrow \pi^+\nu\nu$  to 10% from NA62 and below 5% from HIKE



- $K_L \rightarrow \pi^0\nu\nu$  one of the few very clean modes (like  $B_s \rightarrow \mu\mu$ , or CP asymmetry in  $B \rightarrow \psi K_S$ ).



# What NP scales will we test with flavor?

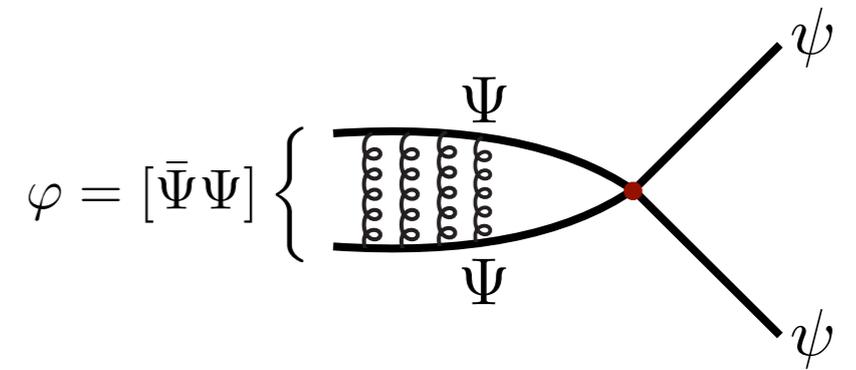
- ◆ A natural example: composite Higgs models.

Higgs is a Goldstone boson (like the pion in QCD)

composite at a scale  $M_\star = g_\star f$

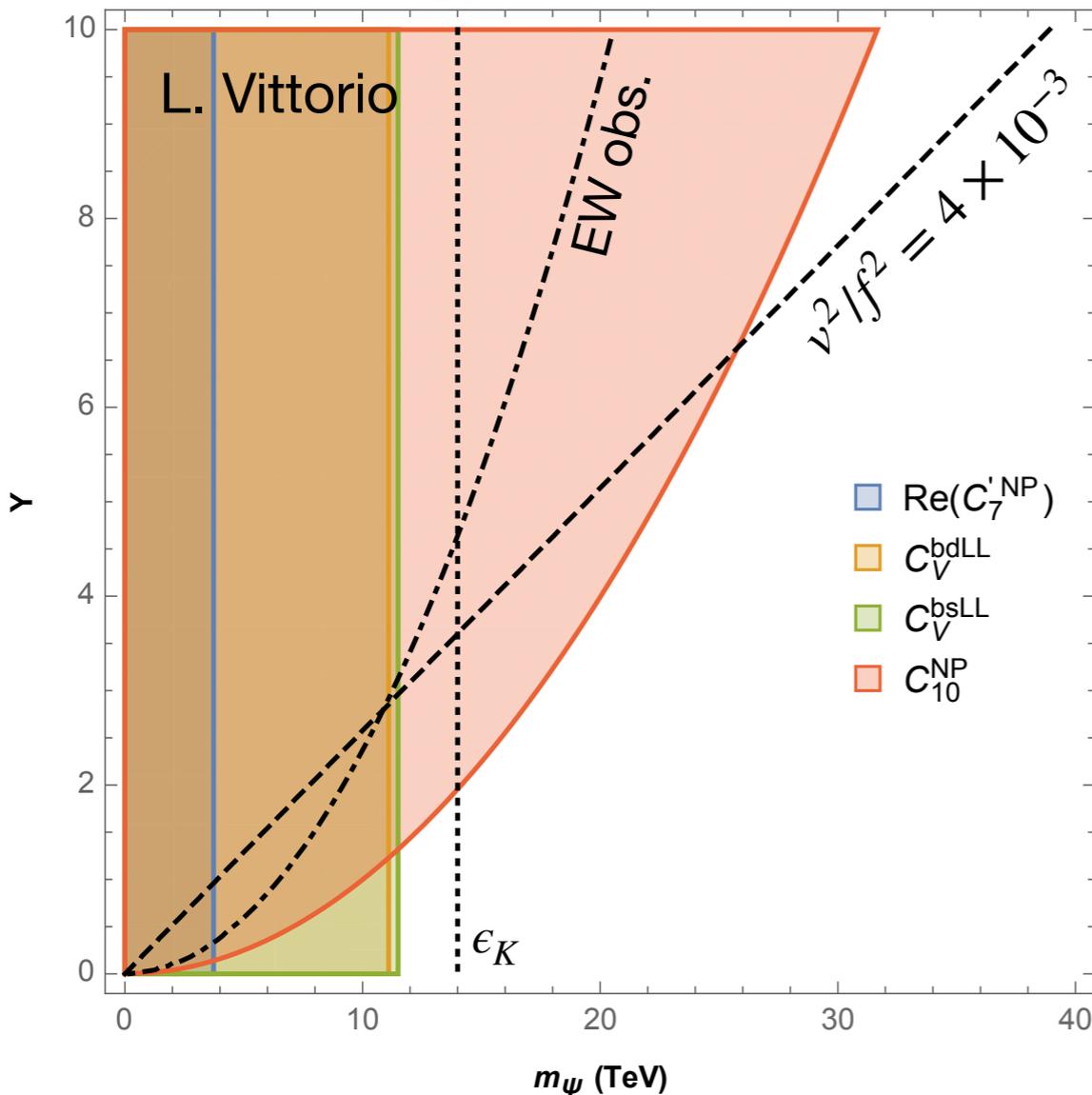
Size of the Higgs

Decay constant of the Higgs



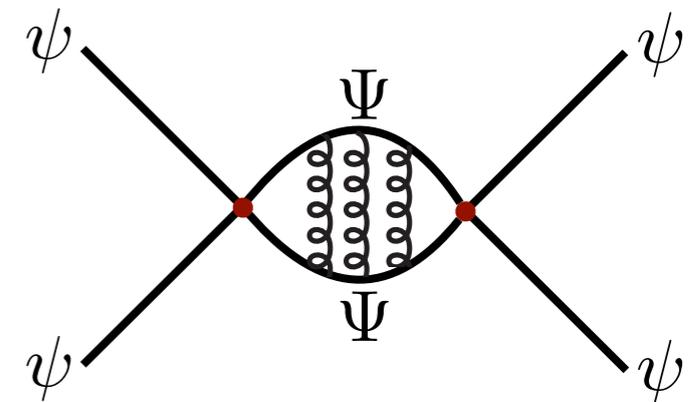
$$\kappa_h \sim v^2/f^2$$

Composite Higgs MCH5



Higgs couplings  $\sim 0.004$ , i.e.  $f > 4$  TeV

Flavor effects known to be important



projections for  
LHCb 300 fb<sup>-1</sup> & Belle II

**O(10 y) timescale!**

- ◆ Unique flavor physics program possible at FCC-ee!

2106.01259

Attribute	$\Upsilon(4S)$	$pp$	$Z^0$	
All hadron species		✓	✓	~ LHCb $\oplus$ B-factory
High boost		✓	✓	
Enormous production cross-section		✓		
Negligible trigger losses	✓		✓	
Low backgrounds	✓		✓	
Initial energy constraint	✓		(✓)	

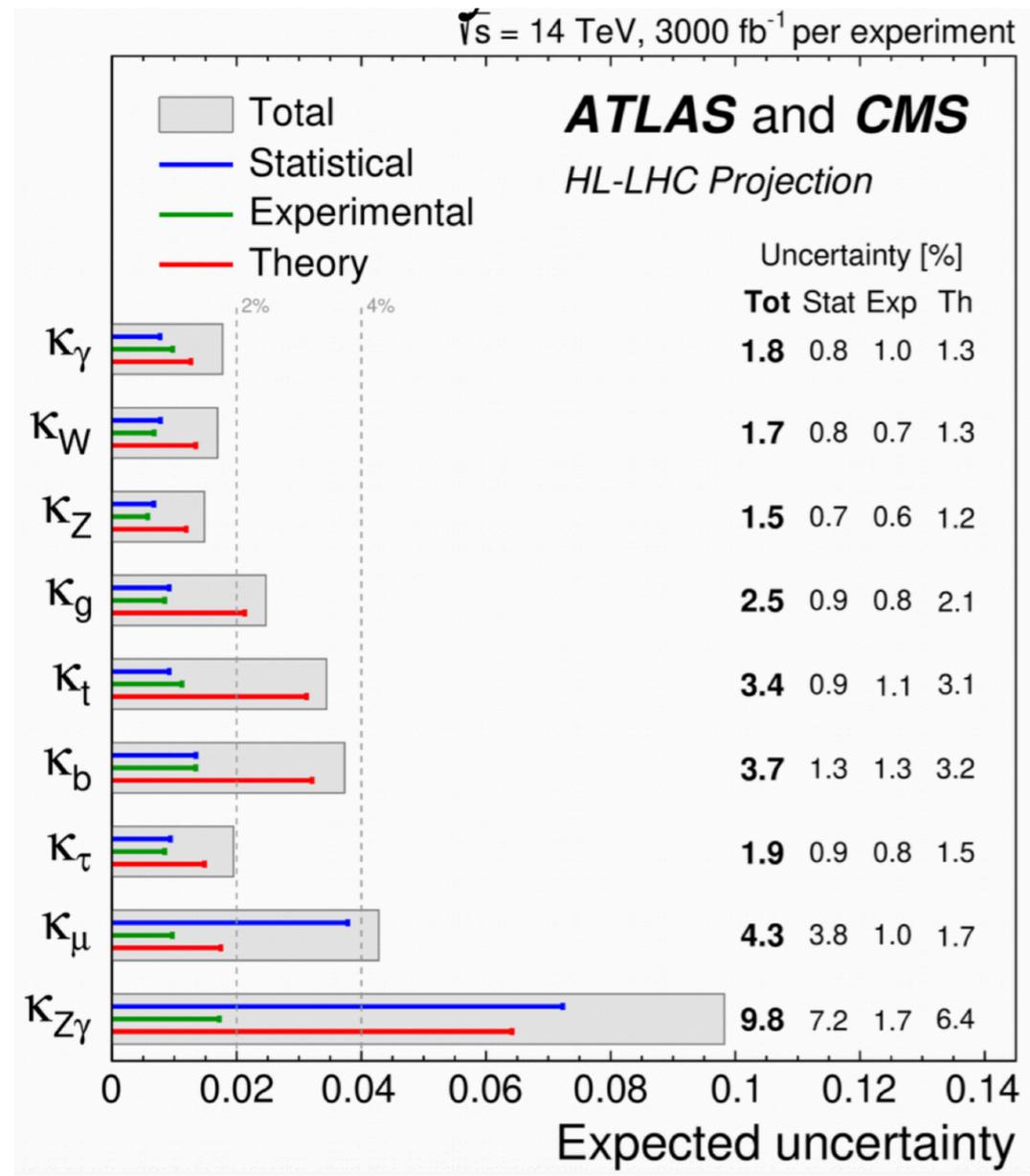
- ◆  $\sim 10^{12}$  b quark pairs (and  $10^{11}$  tau pairs) in a B-factory like environment from Z boson decays.

➡ can measure decay modes with missing energy (esp.  $\tau$ 's and  $\nu$ 's) with 100x more statistics than Belle II!

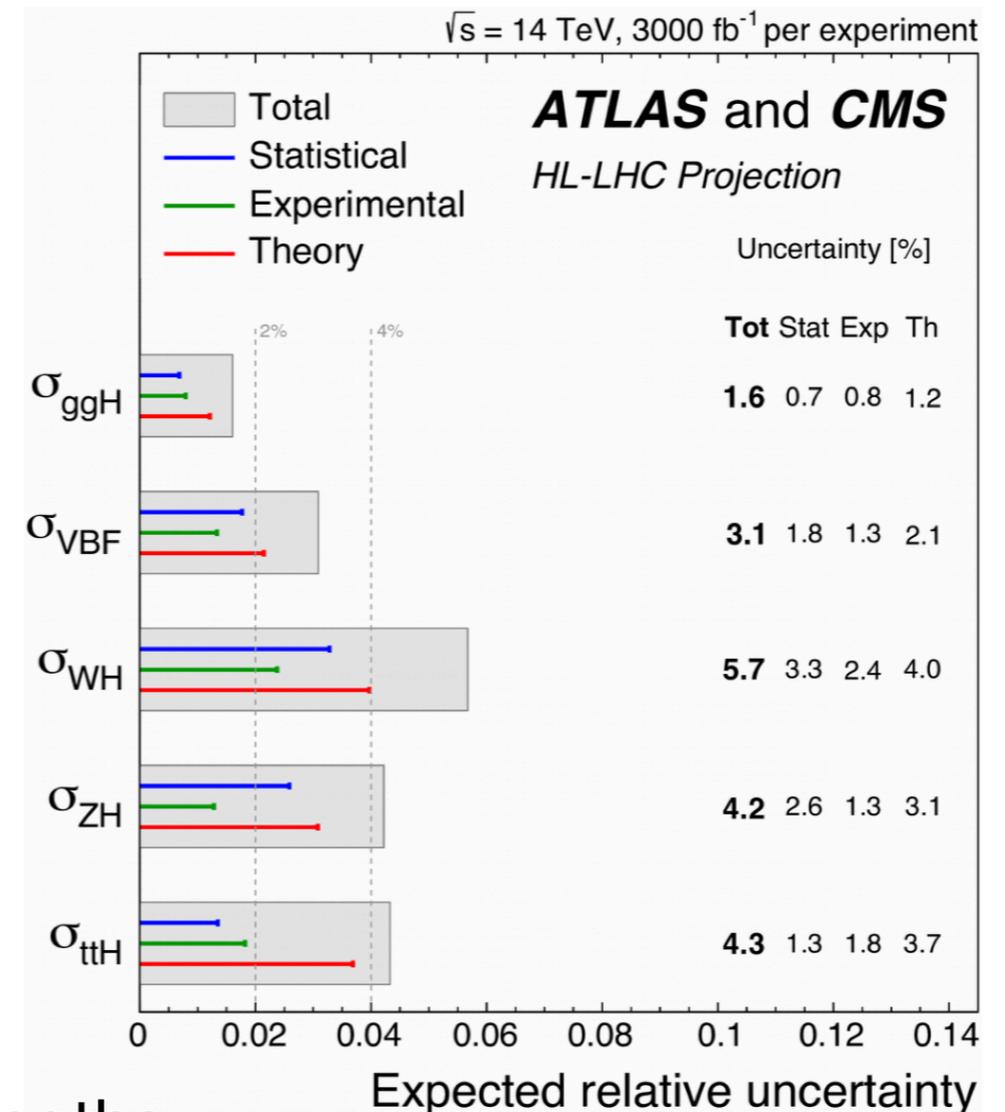
Example:  $10^3 B \rightarrow K^{(*)}\tau\tau$  events (vs. 10 @ Belle II). Few % precision!

➡  $M_{\text{NP}} \gtrsim$  several TeV for NP coupled to 3rd family, complementary with  $b \rightarrow s\nu\nu$

# The next 15 years: Higgs



- ◆ Various production modes (ttH @ few %) and differential cross-sections



- ◆ Factor 2-3 improvement in Higgs signal strengths

$$\delta\kappa \sim \frac{v^2}{M_{\text{NP}}^2} g_\star^2 \lesssim \mathbf{2\%} \quad \longrightarrow \quad M_{\text{NP}} \gtrsim g_\star \mathbf{2 \text{ TeV}}$$

# Higgs factories

- ◆ All proposed future colliders will be able to produce millions of Higgses  
→ study single Higgs couplings with below percent precision!

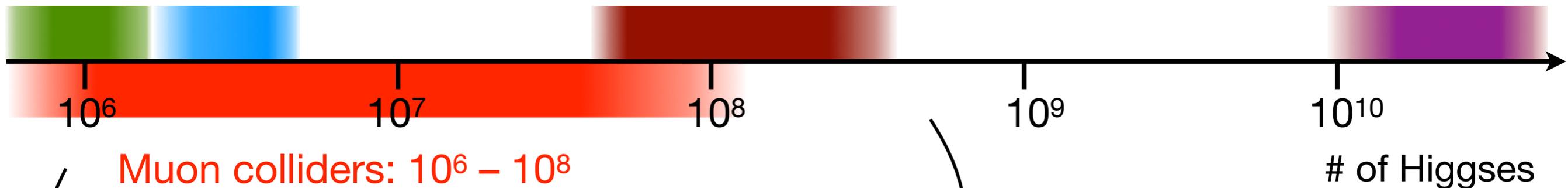
(as a comparison:  $1.7 \times 10^7$  Z bosons @ LEP)

Low energy  
 $e^+e^-$  factories  
(FCC-ee, CEPC,  
ILC, CLIC380)

TeV-scale  
 $e^+e^-$  factories  
(CLIC, ILC1000)

LHC: few  $\times 10^7$   
HL-LHC: few  $\times 10^8$

FCC-hh:  
few  $\times 10^{10}$



clean environment:  
can measure “large” Higgs  
BR w/ almost  $10^{-3}$  precision

large QCD backgrounds:  
only rare modes (BR  $< 10^{-3}$ )  
easily accessible

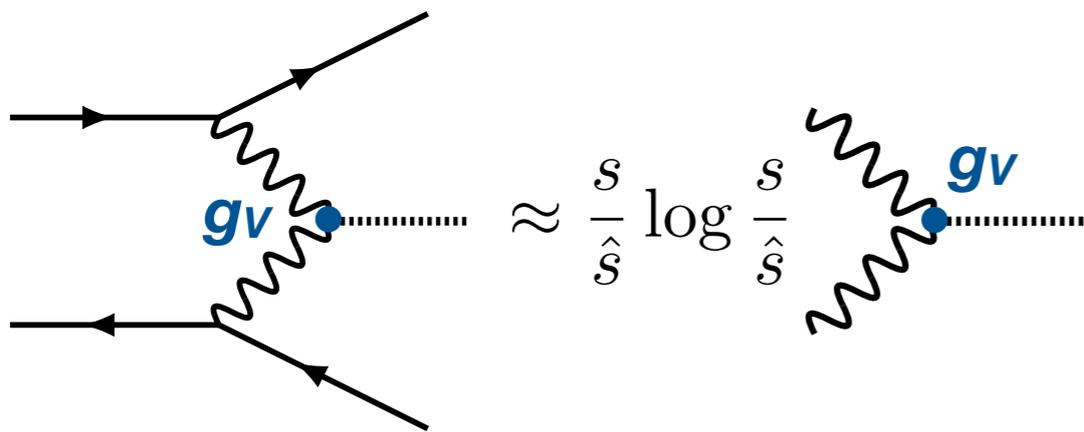
# Higgs factories

- ◆ **Low-energy e+e- factories:**  $e^+e^- \rightarrow Zh$  @ 240 GeV



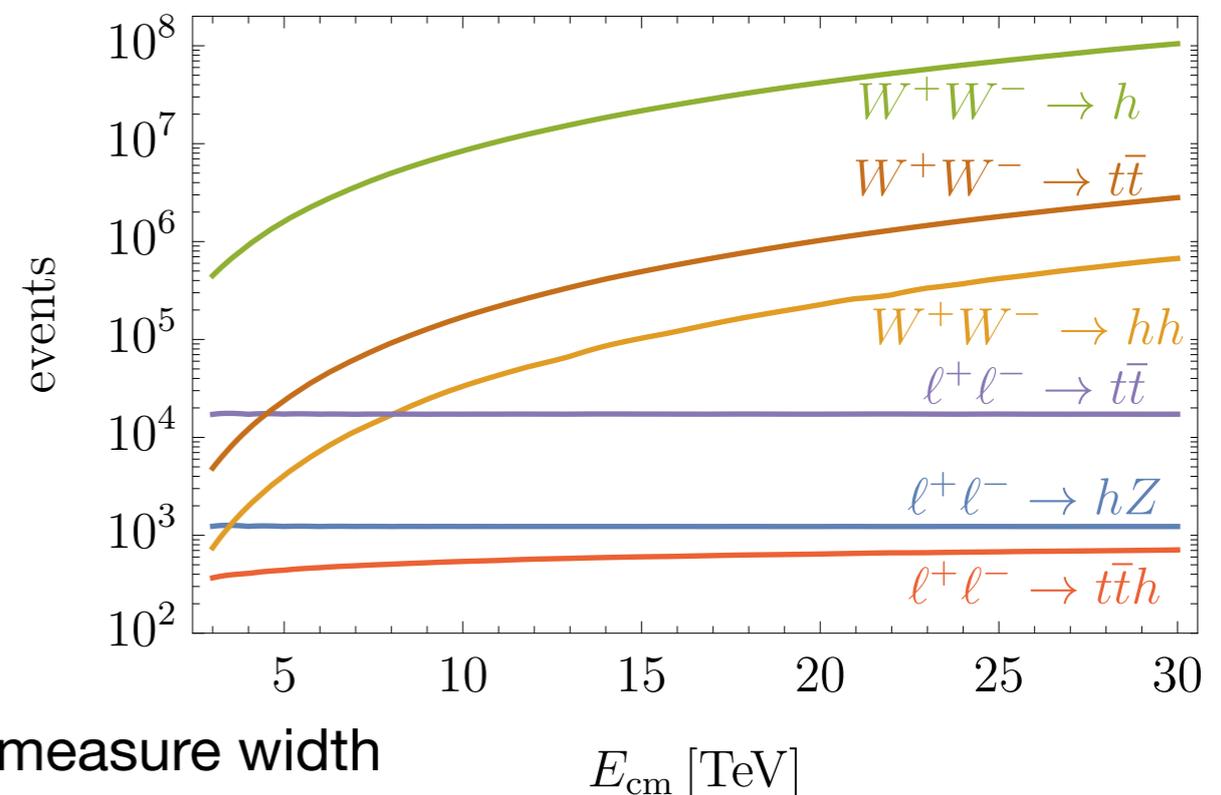
- ◆ measure the recoil (missing mass) of h against Z
- ◆ *direct* measurement of  $g_V \rightarrow$  other couplings + width

- ◆ **A high-energy lepton collider** is a “vector boson collider”



- ◆ potentially huge single H production ( $10^7$ - $10^8$  at 10-30 TeV)
- ◆ hard neutrinos from W-fusion not seen
- ZZ fusion (forward lepton tagging) could still measure width

For “soft” SM final state  $\hat{s} \sim m_{EW}^2$   
cross-section is enhanced



# Higgs factories

$\kappa-0$ fit	HL-LHC	LHeC	HE-LHC		ILC			CLIC			CEPC	FCC-ee		FCC-ee/ eh/hh	$\mu^+\mu^-$ <b>10000</b>
			S2	S2'	250	500	1000	380	1500	3000		240	365		
$\kappa_W$ [%]	1.7	0.75	1.4	0.98	1.8	0.29	0.24	0.86	0.16	0.11	1.3	1.3	0.43	0.14	0.1
$\kappa_Z$ [%]	1.5	1.2	1.3	0.9	0.29	0.23	0.22	0.5	0.26	0.23	0.14	0.20	0.17	0.12	0.4
$\kappa_g$ [%]	2.3	3.6	1.9	1.2	2.3	0.97	0.66	2.5	1.3	0.9	1.5	1.7	1.0	0.49	0.7
$\kappa_\gamma$ [%]	1.9	7.6	1.6	1.2	6.7	3.4	1.9	98*	5.0	2.2	3.7	4.7	3.9	0.29	0.8
$\kappa_{Z\gamma}$ [%]	10.	—	5.7	3.8	99*	86*	85*	120*	15	6.9	8.2	81*	75*	0.69	7.2
$\kappa_c$ [%]	—	4.1	—	—	2.5	1.3	0.9	4.3	1.8	1.4	2.2	1.8	1.3	0.95	2.3
$\kappa_t$ [%]	3.3	—	2.8	1.7	—	6.9	1.6	—	—	2.7	—	—	—	1.0	3.1
$\kappa_b$ [%]	3.6	2.1	3.2	2.3	1.8	0.58	0.48	1.9	0.46	0.37	1.2	1.3	0.67	0.43	0.4
$\kappa_\mu$ [%]	4.6	—	2.5	1.7	15	9.4	6.2	320*	13	5.8	8.9	10	8.9	0.41	3.4
$\kappa_\tau$ [%]	1.9	3.3	1.5	1.1	1.9	0.70	0.57	3.0	1.3	0.88	1.3	1.4	0.73	0.44	0.6

dominant channels  
~ other Higgs factories

rare modes better  
(~ hadron collider)

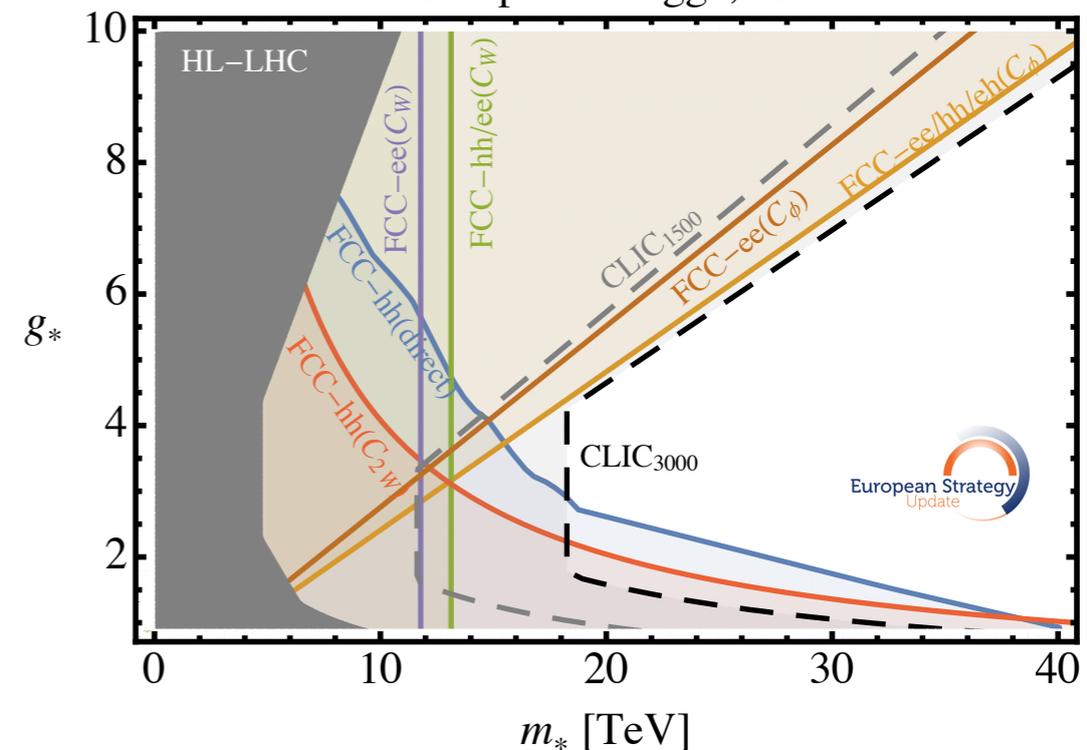
2103.14043

What NP scales will we test with the Higgs?

$$\delta\kappa \sim \frac{v^2}{M_{\text{NP}}^2} g_\star^2 \lesssim \mathbf{0.2\%}$$

→  $M_{\text{NP}} \gtrsim g_\star \mathbf{6 \text{ TeV}}$

Composite Higgs,  $2\sigma$

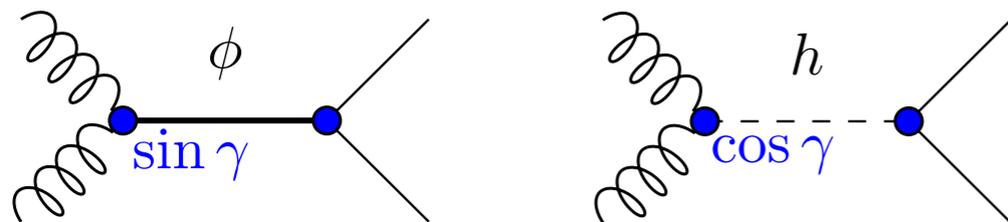


# Direct vs indirect

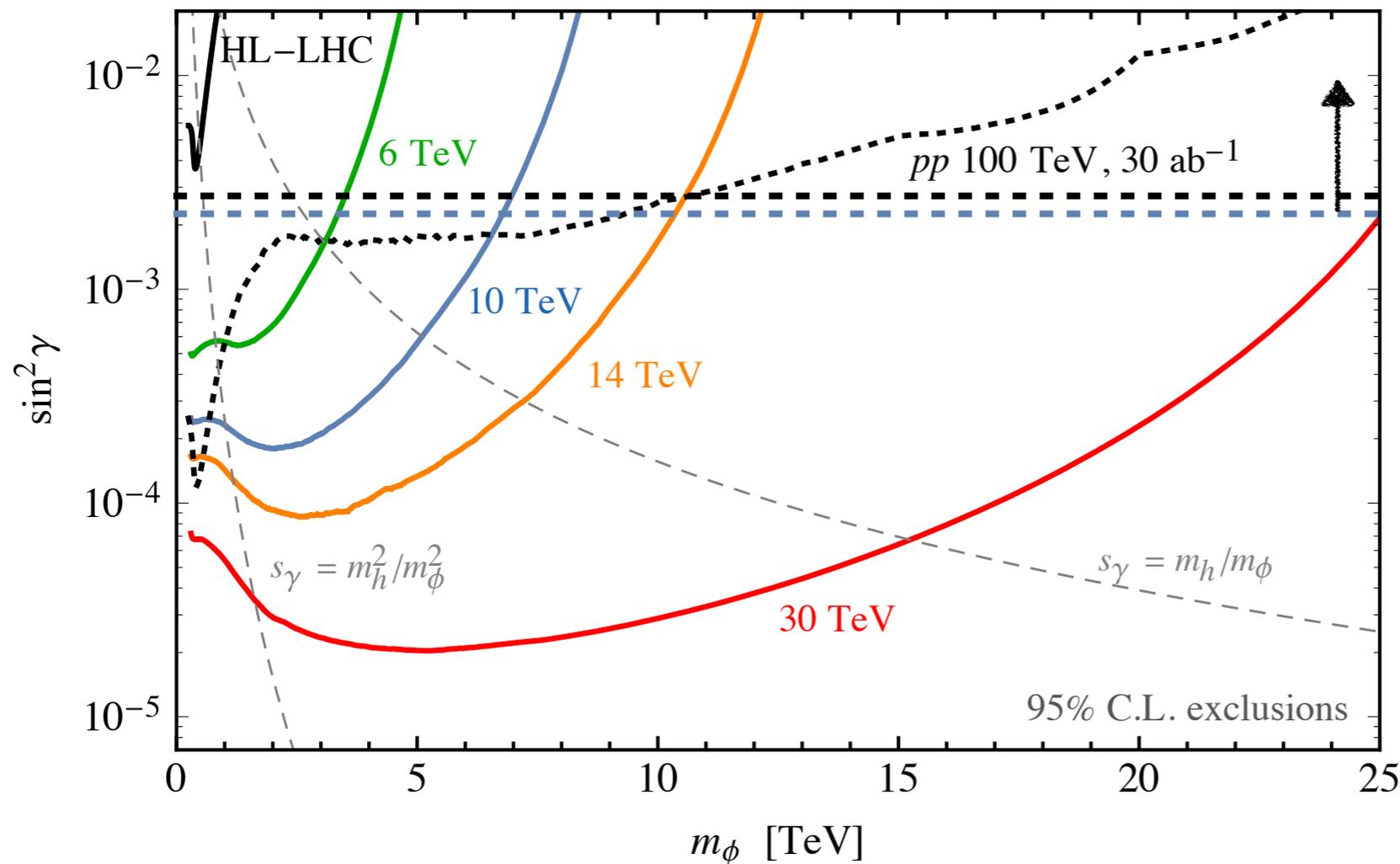
Compare single Higgs couplings measurements with reach of direct searches

- ▶ **Example: singlet scalar**  $\mathcal{L}_{\text{int}} \sim \phi |H|^2$

$\phi$  is like a heavy Higgs with narrow width +  $hh$  decay



one single parameter controls resonance production, decay, & Higgs coupling modifications



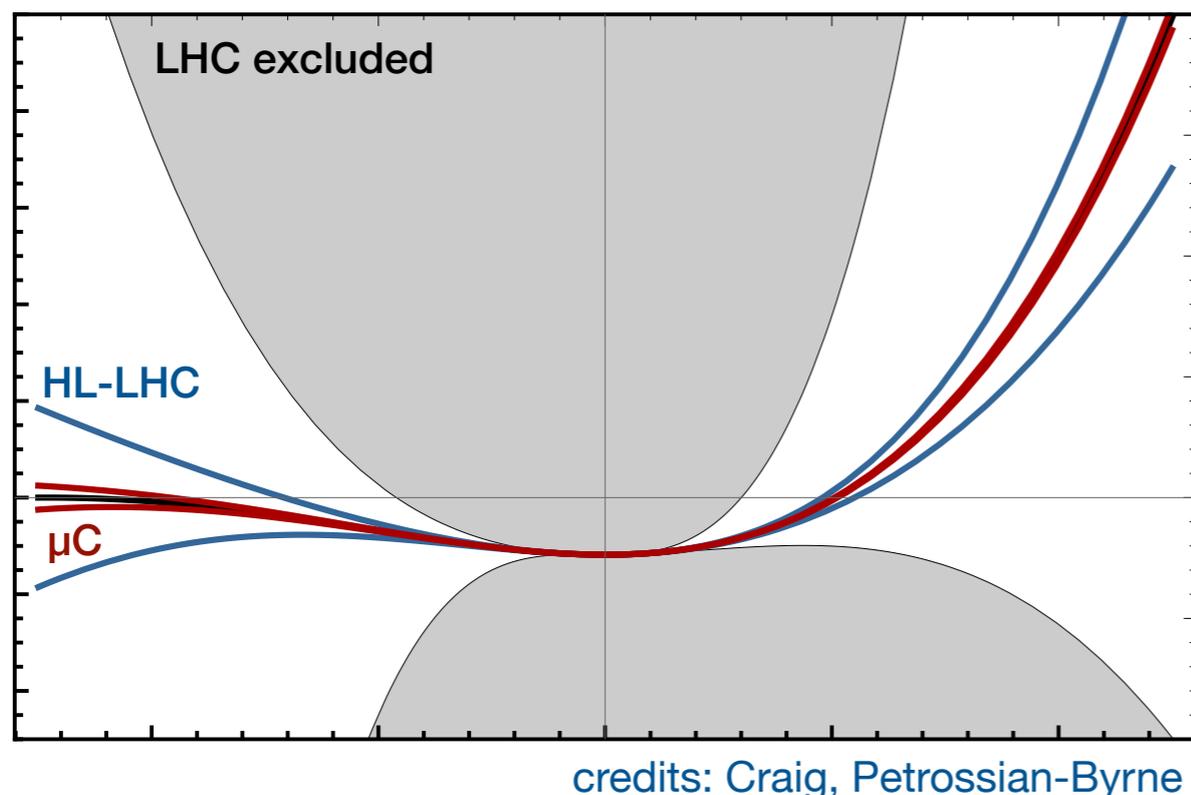
can be probed by single higgs

see talk by R. Franceschini

B, Redigolo, Sala, Tesi 1807.04743

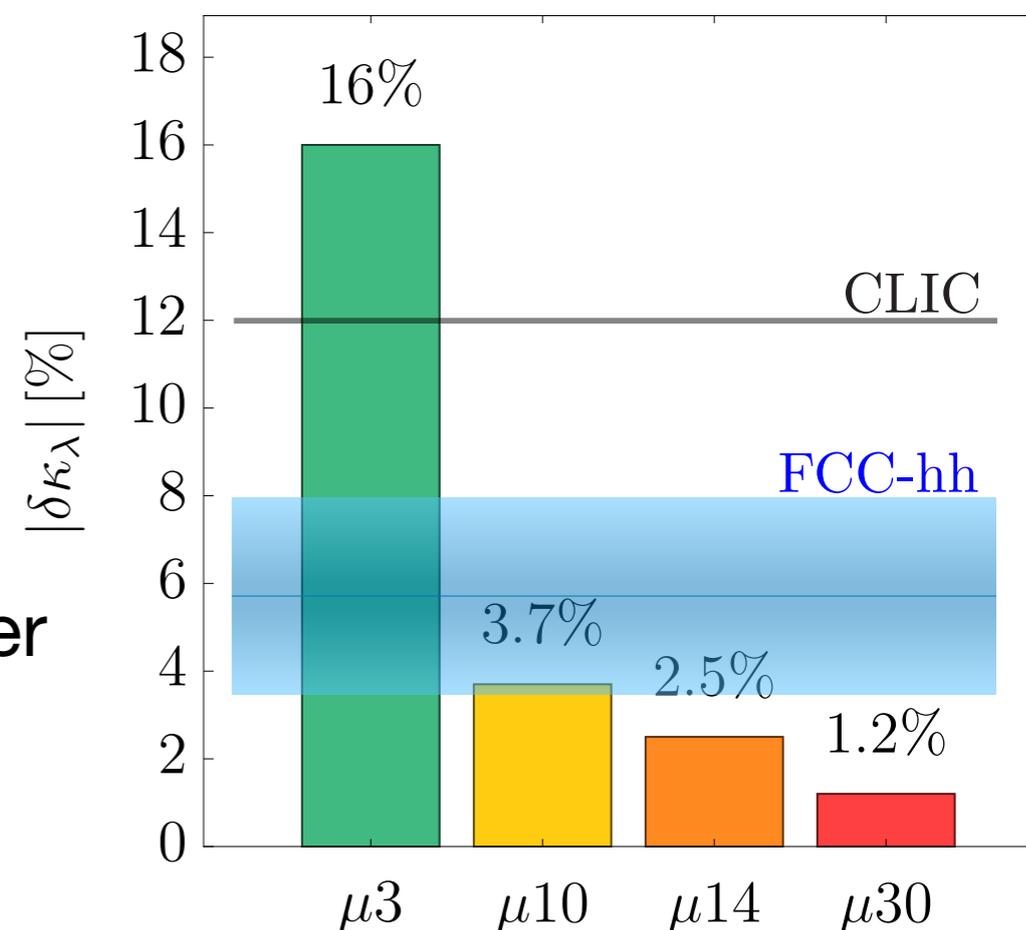
# Double Higgs production

- Measurement of trilinear coupling: access to the Higgs potential



- very poorly known today!
- HL-LHC will only reach 50% precision on SM value

- Precise determination *only* possible at high-energy machines:  
100 TeV FCC-hh or multi-TeV Muon collider

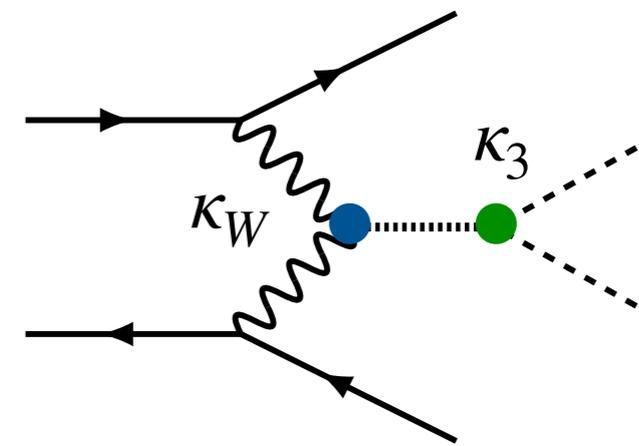
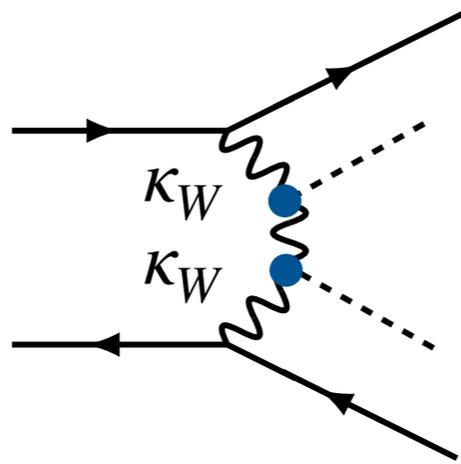
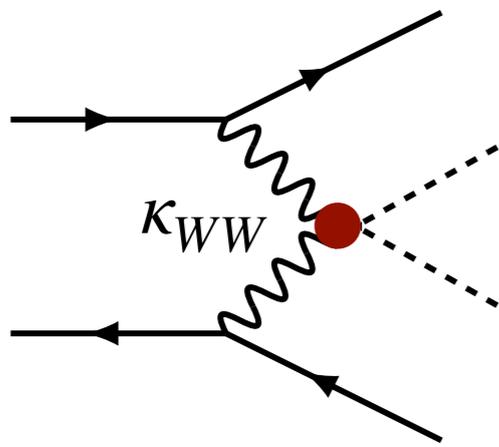


Mangano et al. 2004.03505  
B, Franceschini, Wulzer 2012.11555  
Costantini et al. 2005.10289

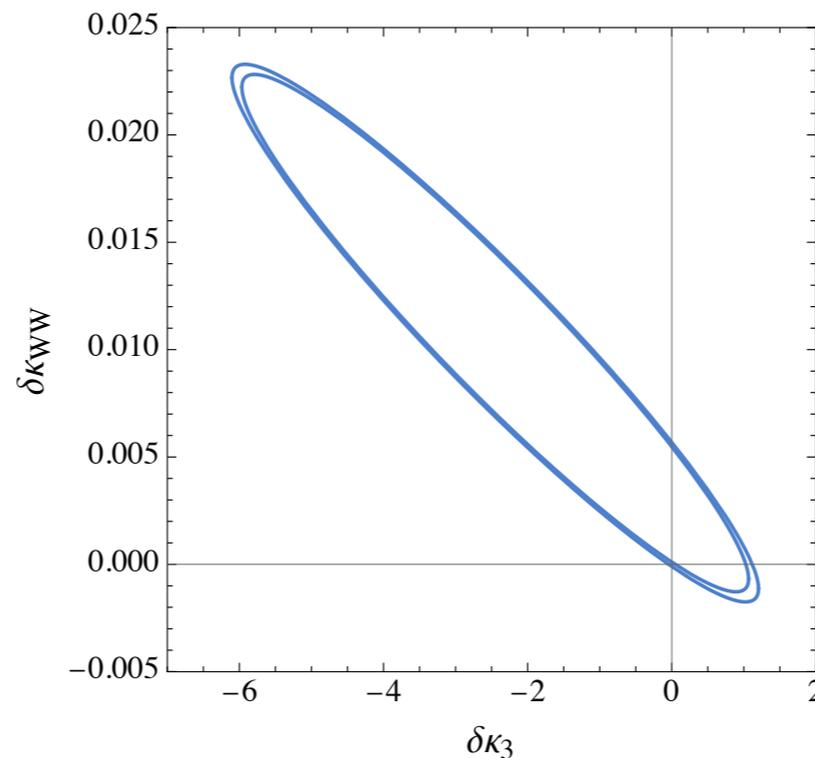
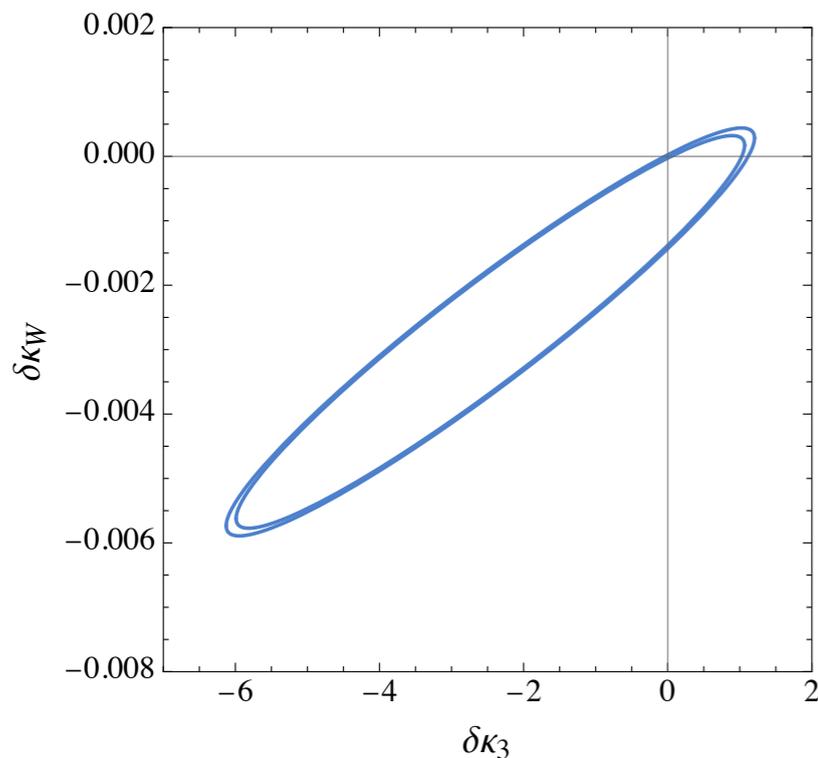
Han et al. 2008.12204  
CLIC 1901.05897

# Double Higgs production

- Double Higgs production depends on trilinear coupling  $\kappa_3$  but also on W-boson couplings  $\kappa_W, \kappa_{WW}$  that enter the production cross-section



large degeneracy in total cross-section:  
coefficients not determined  
from  $hh$  production alone

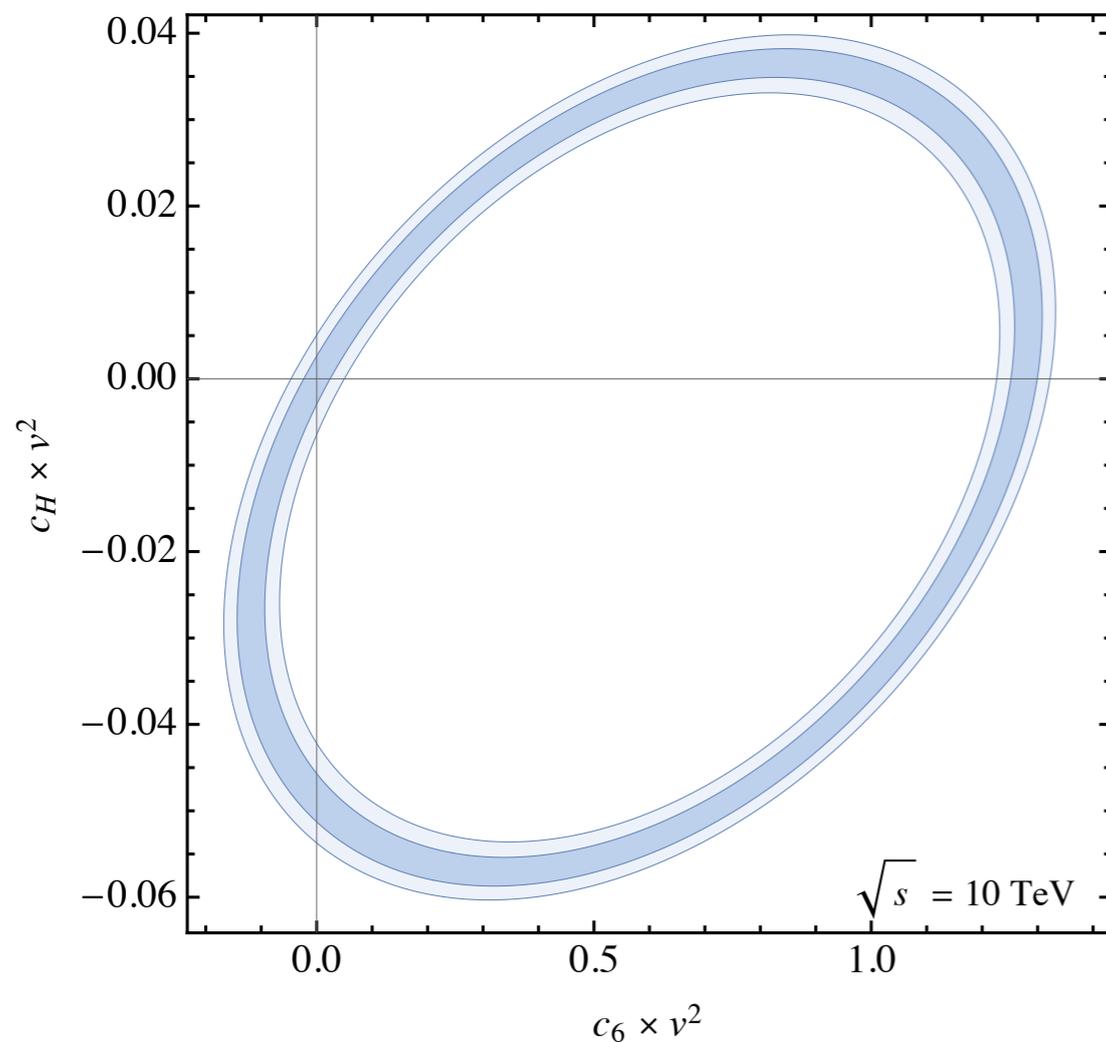


# Double Higgs production

- ◆ Double Higgs production depends on trilinear coupling  $\kappa_3$  but also on W-boson couplings  $\kappa_W, \kappa_{WW}$  that enter the production cross-section

- ◆ Two dim. 6 operators:  $\mathcal{O}_6 = -\lambda|H|^6$        $\mathcal{O}_H = \frac{1}{2} (\partial_\mu |H|^2)^2$

$$\kappa_3 = 1 + v^2 \left( C_6 - \frac{3}{2} C_H \right) \quad \kappa_W = 1 - v^2 C_H / 2 \quad \kappa_{WW} = 1 - 2v^2 C_H$$



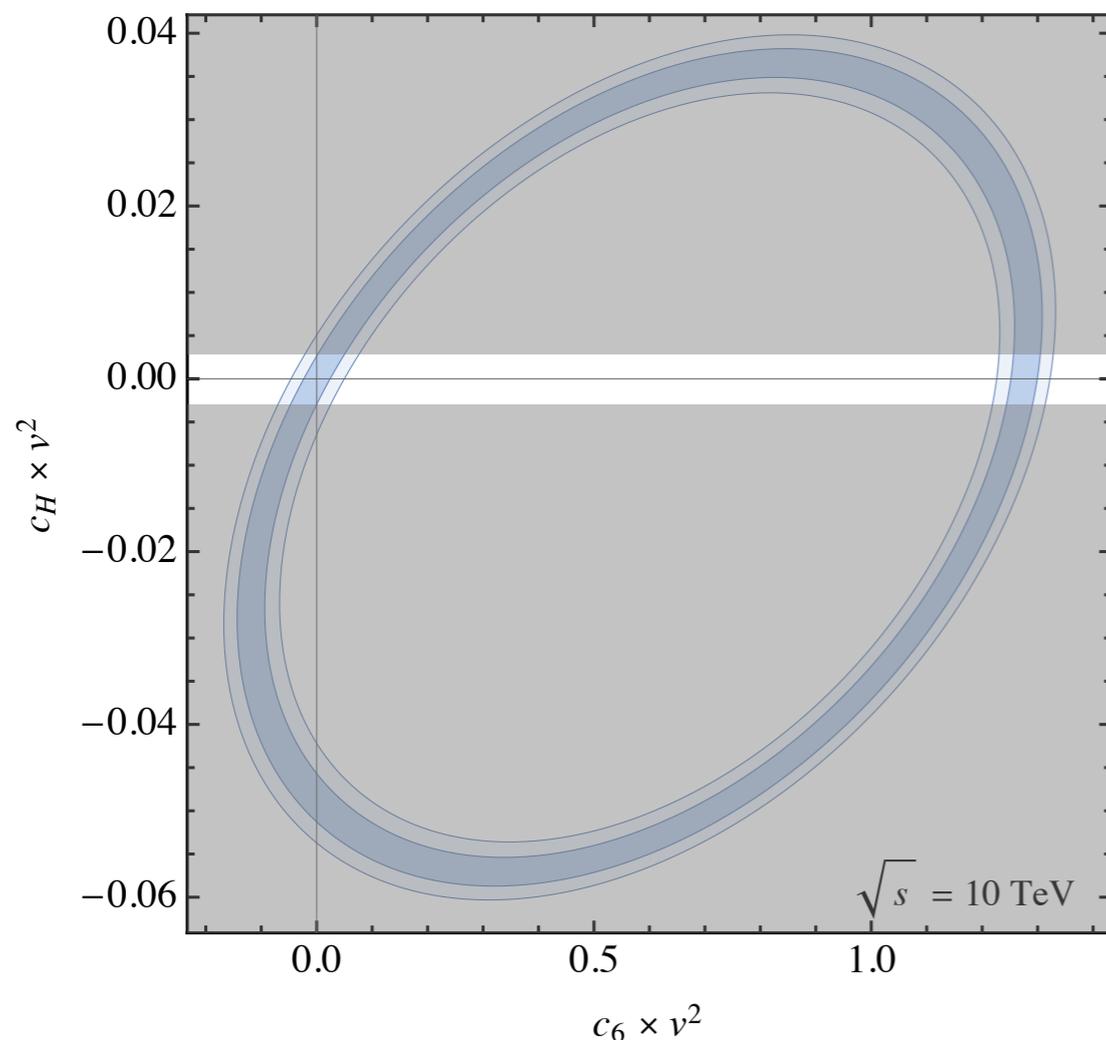
large degeneracy in total cross-section:  
coefficients not determined in general

# Double Higgs production

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large degeneracy in total cross-section:  
coefficients not determined in general

$\mathcal{O}_H$  also affects all single Higgs couplings universally:

$$\kappa_{V,f} = 1 - v^2 C_H / 2$$

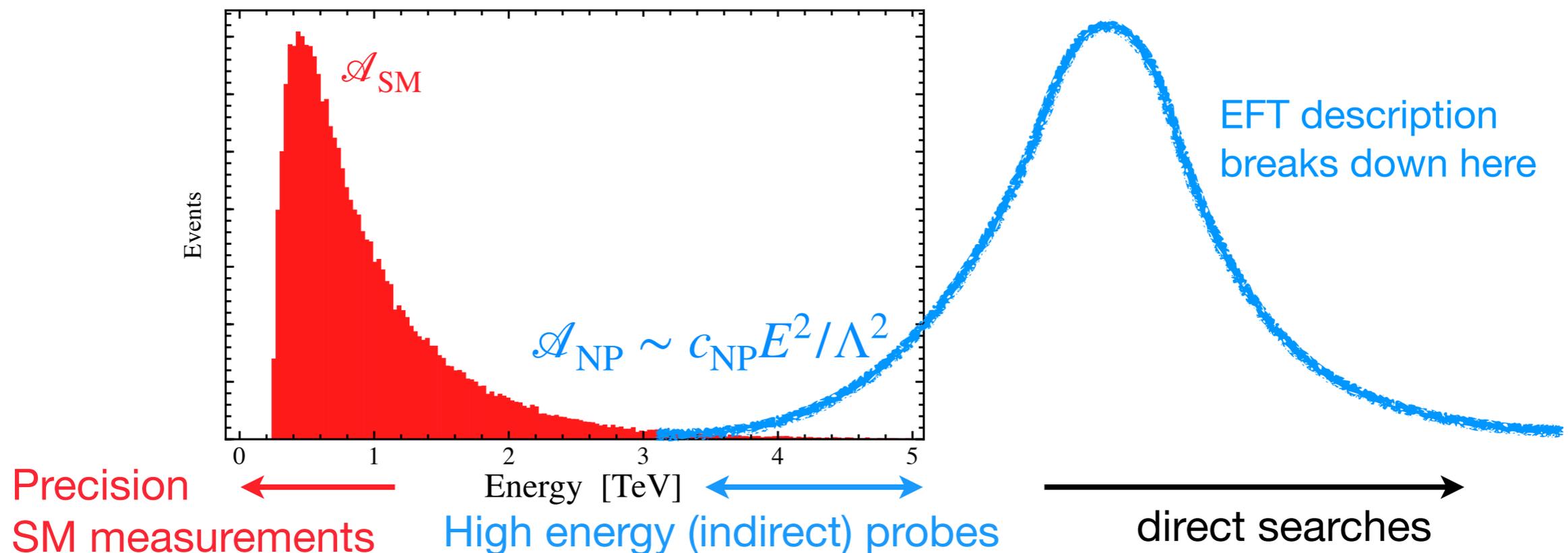
$C_H$  can be constrained from Higgs couplings  $\Delta\kappa_V \sim C_H v^2 \lesssim \text{few} \times 10^{-3}$

# Higgs at high-energy

- ◆ Higgs physics doesn't mean just couplings. There's much more information in the energy dependence of the interactions! (form factors)

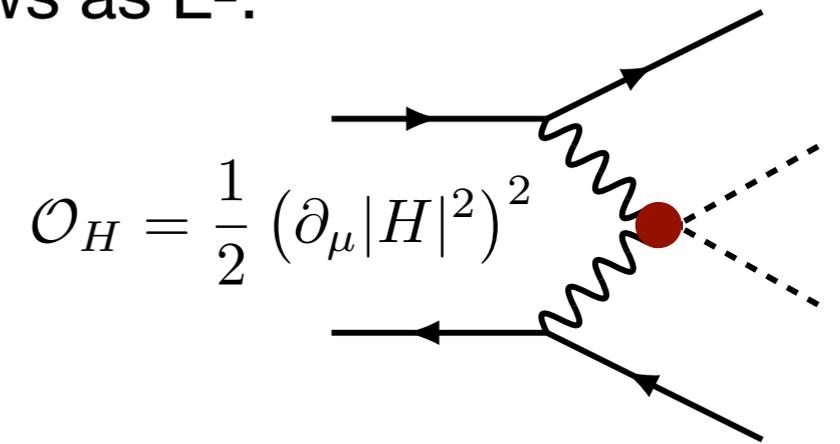


- ◆ NP effects are more important at high energies ( $\approx$  high- $p_T$  tails at LHC)



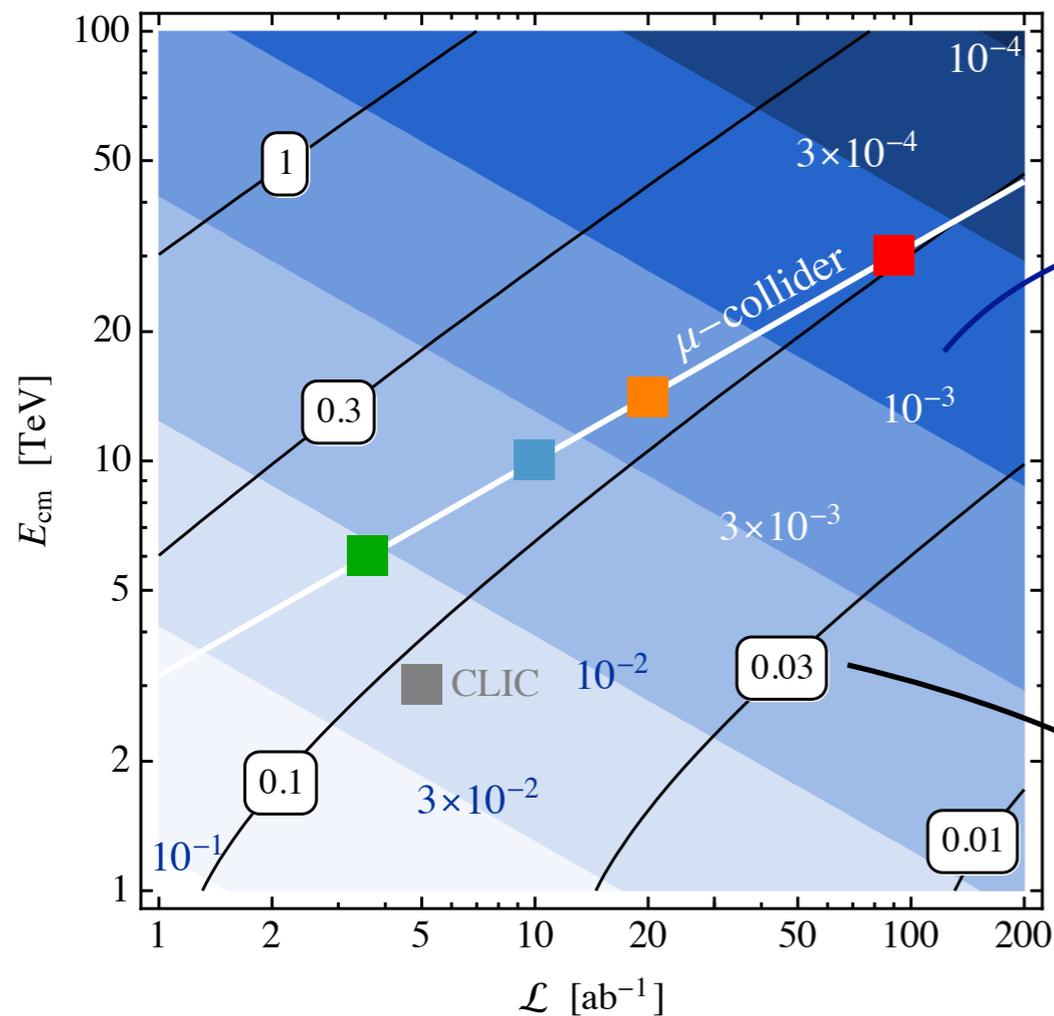
# Double Higgs at high mass

- NP contribution from  $\mathcal{O}_H$  (equivalently  $\kappa_W, \kappa_{WW}$ ) grows as  $E^2$ :  
high mass tail gives a *direct* measurement of  $C_H$



$$\mathcal{O}_H = \frac{1}{2} (\partial_\mu |H|^2)^2$$

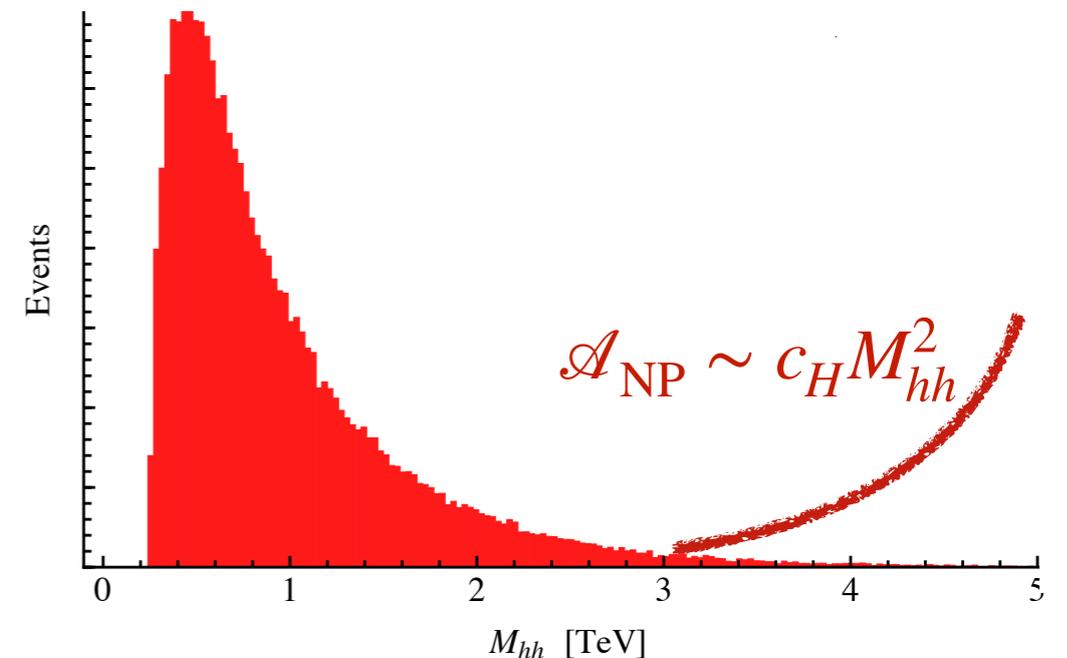
High-energy  $WW \rightarrow hh$  more sensitive than Higgs pole physics at energies  $\gtrsim 10$  TeV



$$\xi \equiv C_H V^2$$

**S/B** low-precision measurement

$$\mu^+ \mu^- \rightarrow hh \nu \bar{\nu}$$



(see also Contino et al. 1309.7038)

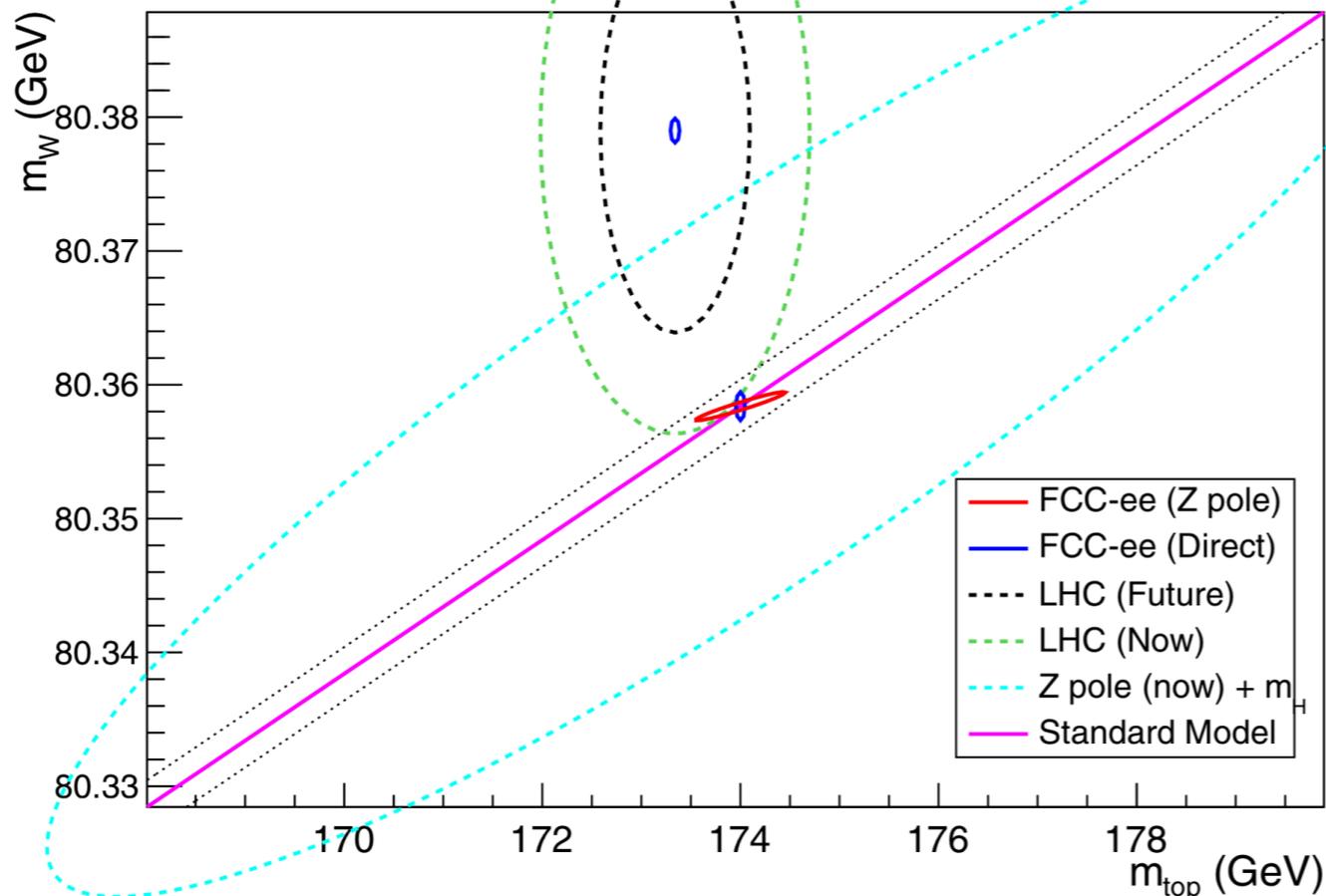
# EW precision

- ◆ Higgs & EWSB physics  $\longleftrightarrow$  Ew precision measurements

$$\mathcal{O}_T = (H^\dagger D^\mu H)^2 \quad \Delta\rho$$

$$\mathcal{O}_W = (H^\dagger \sigma^a D^\mu H) D^\nu W_{\mu\nu}^a \quad \sin^2 \theta_{\text{eff}}$$

$$\mathcal{O}_B = (H^\dagger D^\mu H) \partial^\nu B_{\mu\nu}$$



- ◆ FCC-ee:  $6 \times 10^{12}$  Z bosons  
ultimate precision at the Z pole,  
limited by syst. and th. errors

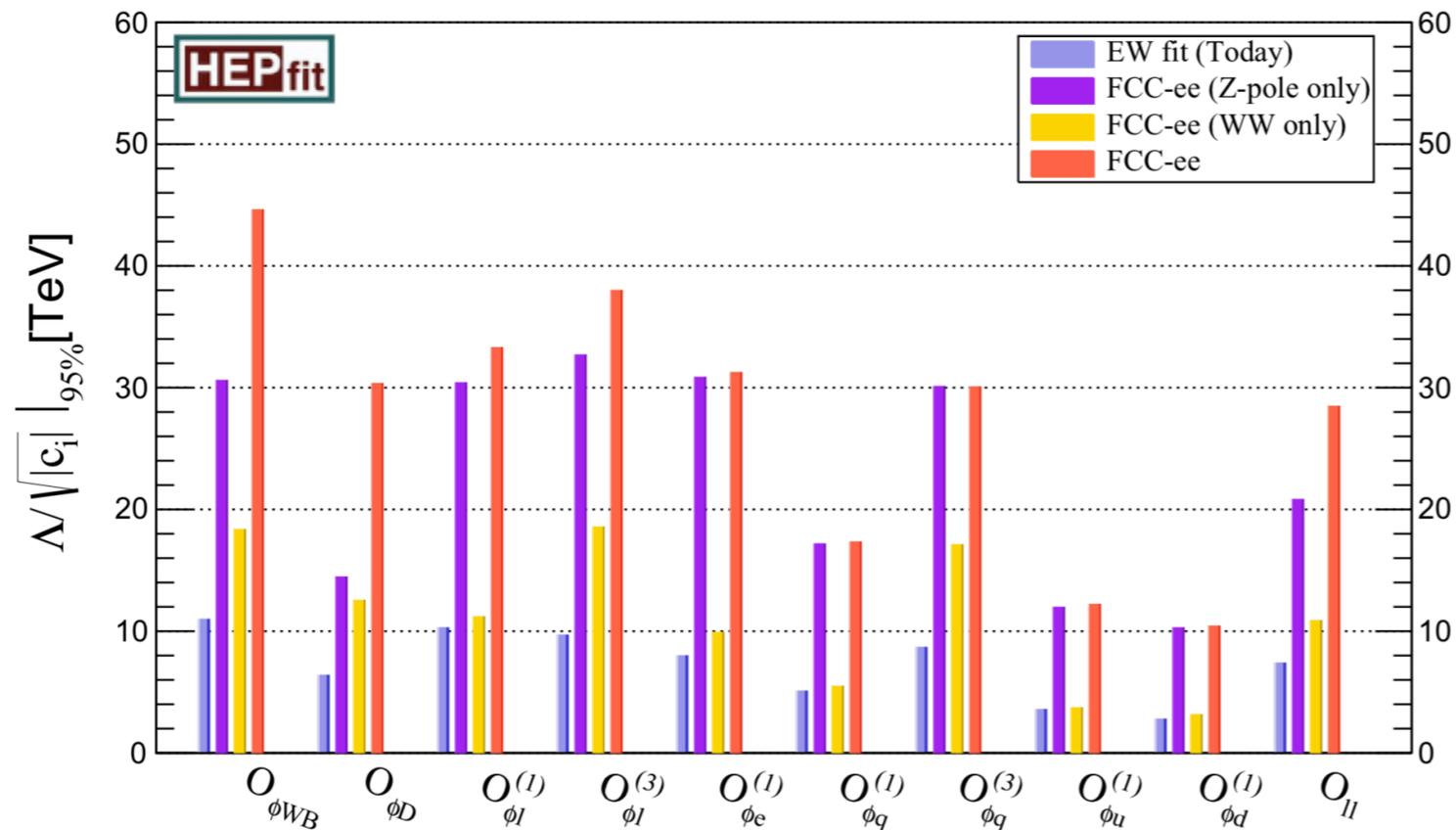
$$\Delta \hat{S} \sim \frac{m_W^2}{M_{\text{NP}}^2} \lesssim \text{few} \times 10^{-5}$$

$$\longrightarrow M_{\text{NP}} \gtrsim 12 \text{ TeV}$$

	Current	HL-LHC	ILC <sub>250</sub> (& ILC <sub>91</sub> )		CEPC	FCC-ee	CLIC <sub>380</sub> (& CLIC <sub>91</sub> )	
<i>S</i>	0.13	0.053	0.012	0.009	0.0068	0.0038	0.032	0.011
<i>T</i>	0.08	0.041	0.014	0.013	0.0072	0.0022	0.023	0.012

# EW precision

- ◆ In general, several more operators enter the EW fit

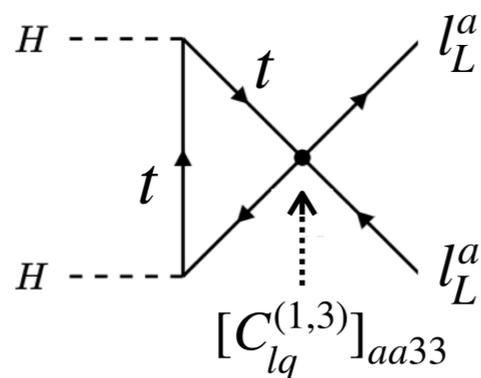


effective scales  $\sim 30$  TeV

$$M_{\text{NP}}^{\text{EW}} = \Lambda \times g_{\star} \approx 12 \text{ TeV} \left( \frac{g_{\star}}{g_2} \right)$$

Several 4-fermion interactions enter through one loop RGE

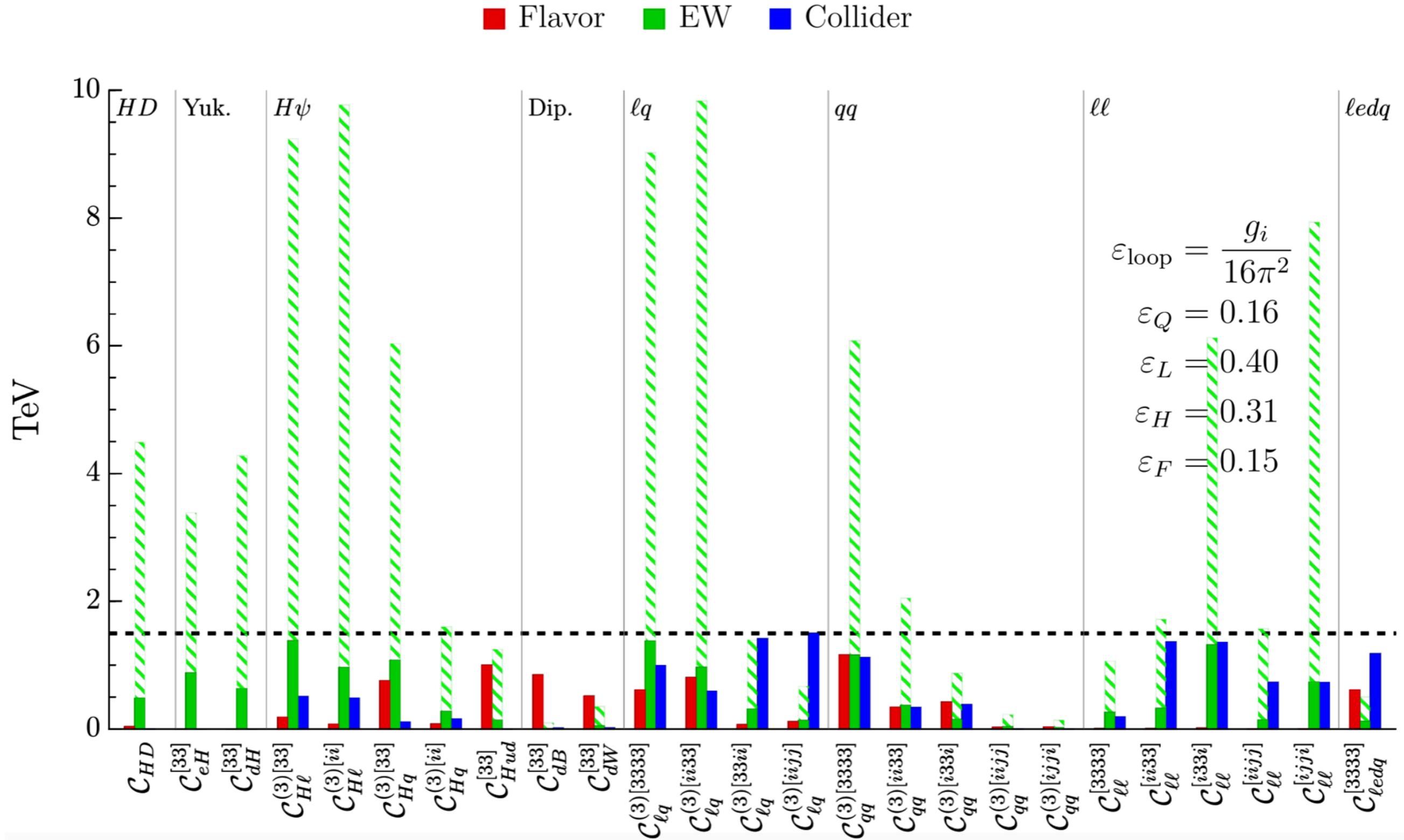
2311.00020, 1704.04504



$$\dots \rightarrow [C_{Hl}^{(1,3)}]_{aa}$$

$$M_{\text{NP}}^{4f} \gtrsim 10 \text{ TeV} \times g_{\star}$$

# EW precision



# Challenges

- ◆ Precision measurements need to be matched with theory predictions of comparable precision

$$\Delta\hat{S} \lesssim 10^{-5} \quad \longrightarrow \quad \text{NNLO EW corrections required}$$

- ◆ Already now, huge rates of b, c hadrons at LHC not always reflected in improvement of physics reach, due to QCD (e.g. hadronic channels,  $V_{cb}$  puzzle in semi-leptonic decays, K and D mixing, ...)

- ◆ High rate measurements eventually limited by systematics

- ◆ Why  $10^{12}$  Z bosons?

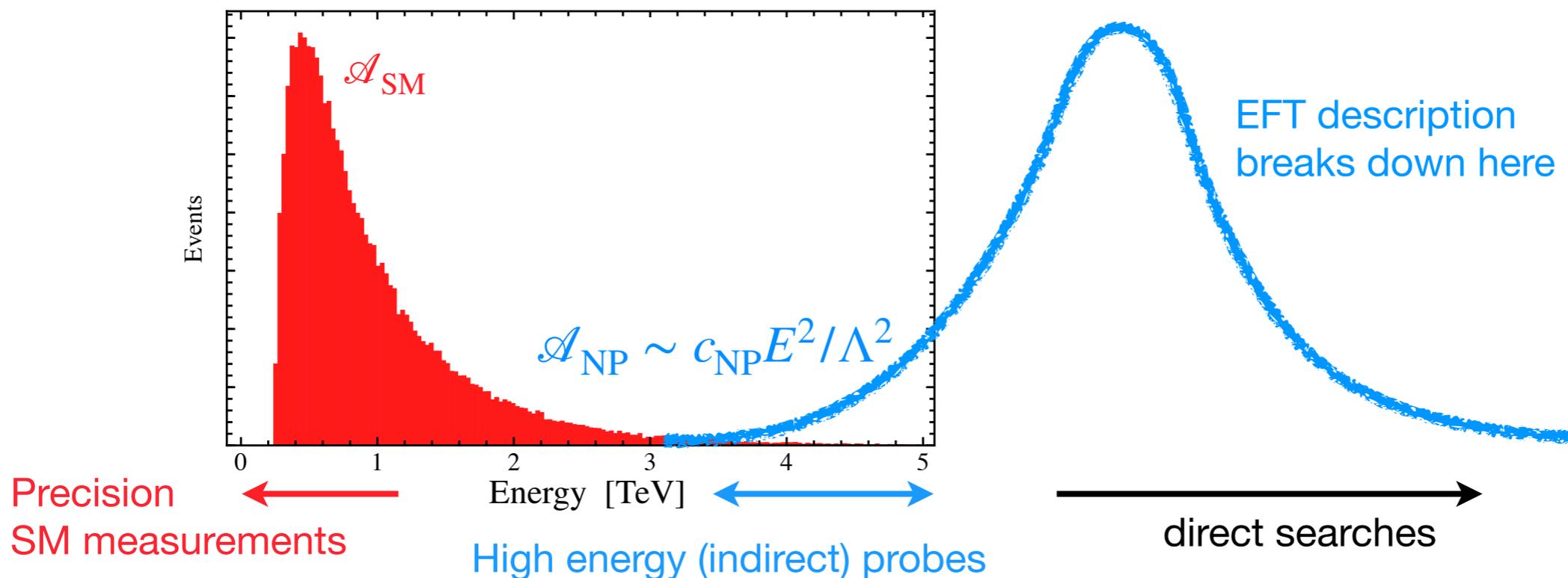
$$\text{Lepton asymmetries: } N_{\text{events}} = N_Z \times \text{BR}(Z \rightarrow \ell^+ \ell^-) \times A_\ell \sim 3 \times 10^{-4} N_Z$$

$$\implies N_Z \approx 10^{12} \text{ for } 10^{-4} \text{ precision}$$

- ◆ *Eventually, we'll need to measure physics at higher energy to improve!*

# EW precision at high-energy

- NP effects are more important at high energies  $\mathcal{L} = \mathcal{L}_{\text{SM}} + \frac{1}{\Lambda^2} \sum C_i \mathcal{O}_i$



$$\frac{\Delta\sigma(E)}{\sigma_{\text{SM}}(E)} \propto \frac{E^2}{\Lambda_{\text{BSM}}^2} \approx \begin{cases} 10^{-6}, & E \sim 100 \text{ GeV} \\ 10^{-2}, & E \sim 10 \text{ TeV} \end{cases}$$

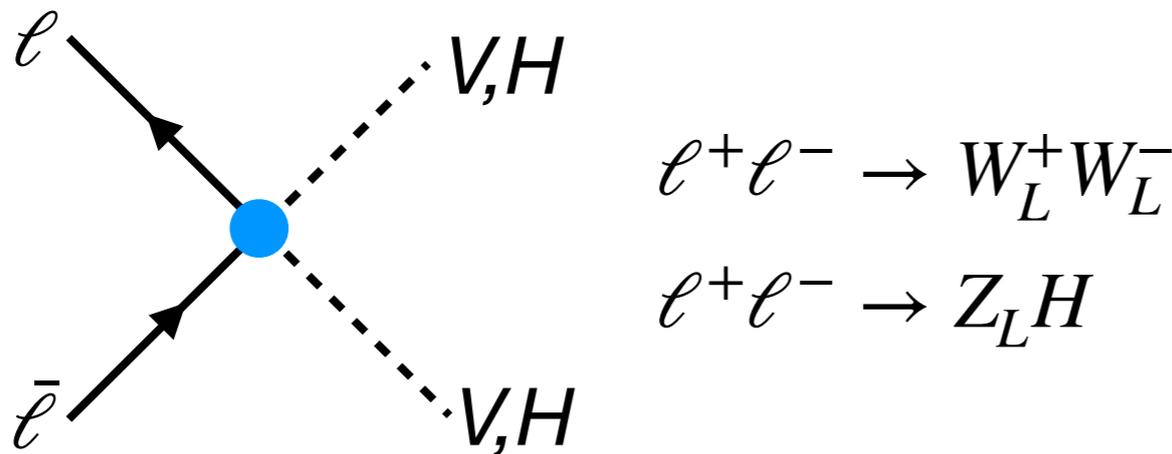
- Effective at LHC, FCC-hh, CLIC: “energy helps accuracy”...

Farina et al. 1609.08157, Franceschini et al. 1712.01310, ...

... taken to the extreme at a  $\mu$ -collider with 10's of TeV!

# Example: high-energy di-bosons

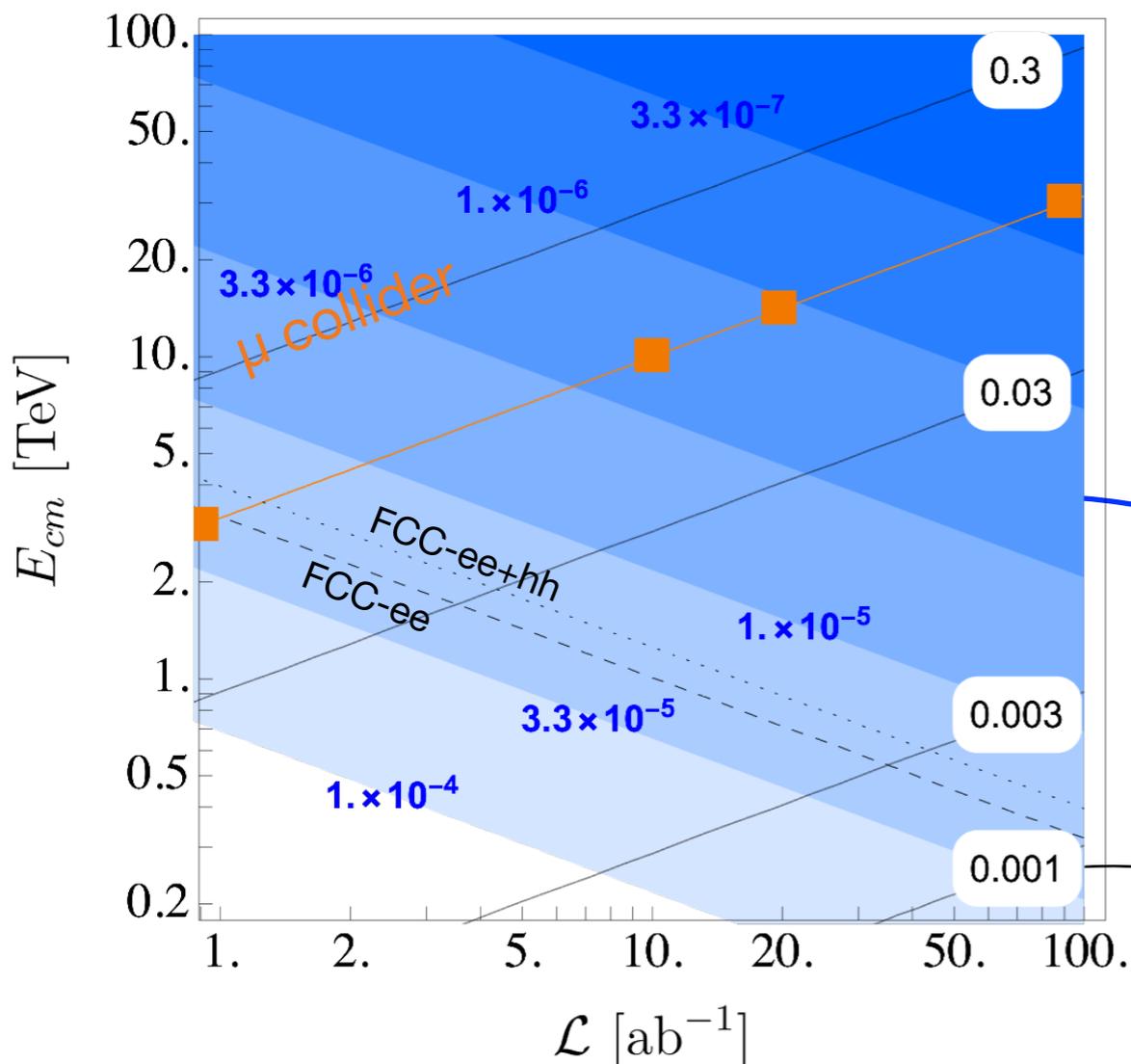
- Longitudinal  $2 \rightarrow 2$  scattering amplitudes at high energy:



Determined by the same two operators that affect also EWPT (in flavor-universal theories):

$$\mathcal{O}_W = \frac{ig}{2} \left( H^\dagger \sigma^a \overleftrightarrow{D}^\mu H \right) D^\nu W_{\mu\nu}^a$$

$$\mathcal{O}_B = \frac{ig'}{2} \left( H^\dagger \overleftrightarrow{D}^\mu H \right) \partial^\nu B_{\mu\nu}$$



related with Z-pole observables

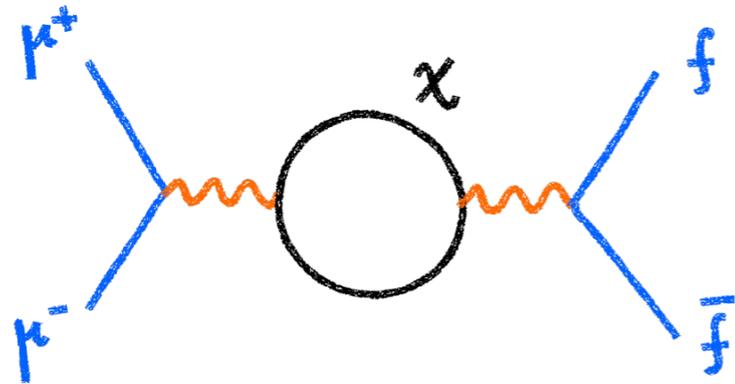
$$\hat{S} = m_W^2 (C_W + C_B)$$

LEP:  $10^{-3}$ , FCC: few  $10^{-5}$  **MuC:  $10^{-6}$**

precision of measurement

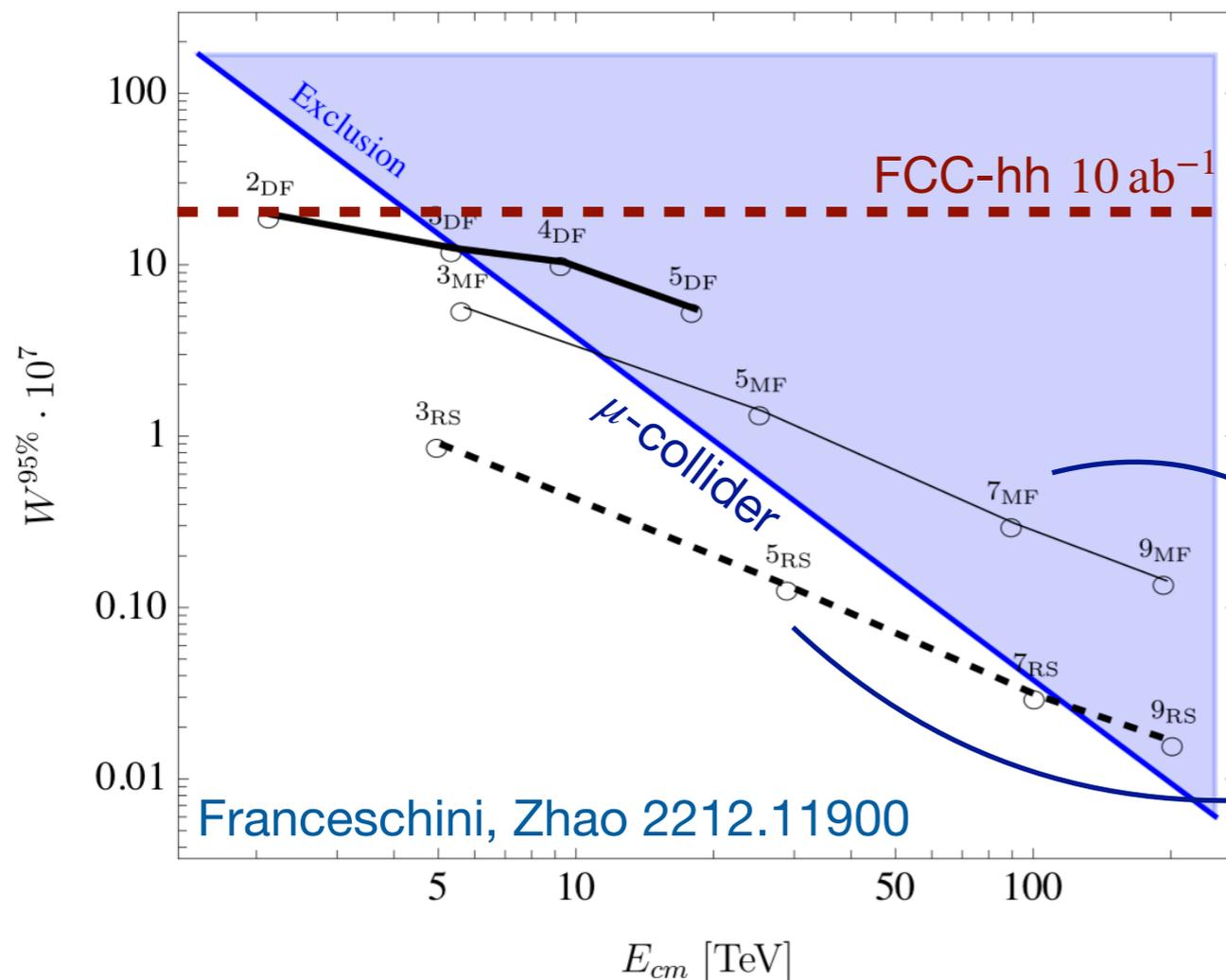
# EW-charged matter

- ♦ All EW multiplets contribute to high-energy  $2 \rightarrow 2$  fermion scattering: effects that grow with energy, can be tested at  $\mu$  collider



can be WIMP dark matter if  $M \sim \text{few TeV}$

see talk by R. Franceschini



$$\hat{W} \approx 10^{-7} \times \left( \frac{1 \text{ TeV}}{M_{\text{DM}}} \right)^2 n^3 \propto 1/n^2$$

$$\hat{Y} \approx 10^{-7} \times \left( \frac{1 \text{ TeV}}{M_{\text{DM}}} \right)^2 Y^2 n \propto 1/n^4$$

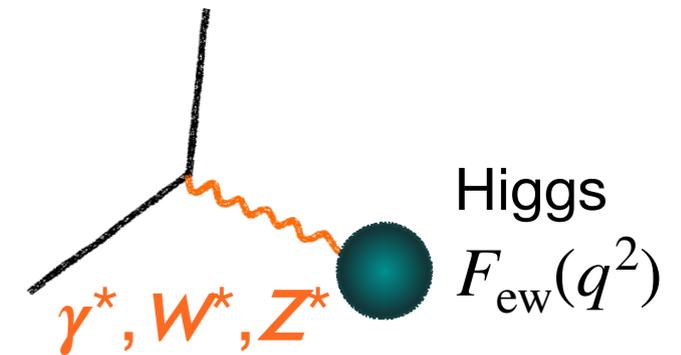
right of blue line: can be tested indirectly

left of blue line: can be tested directly

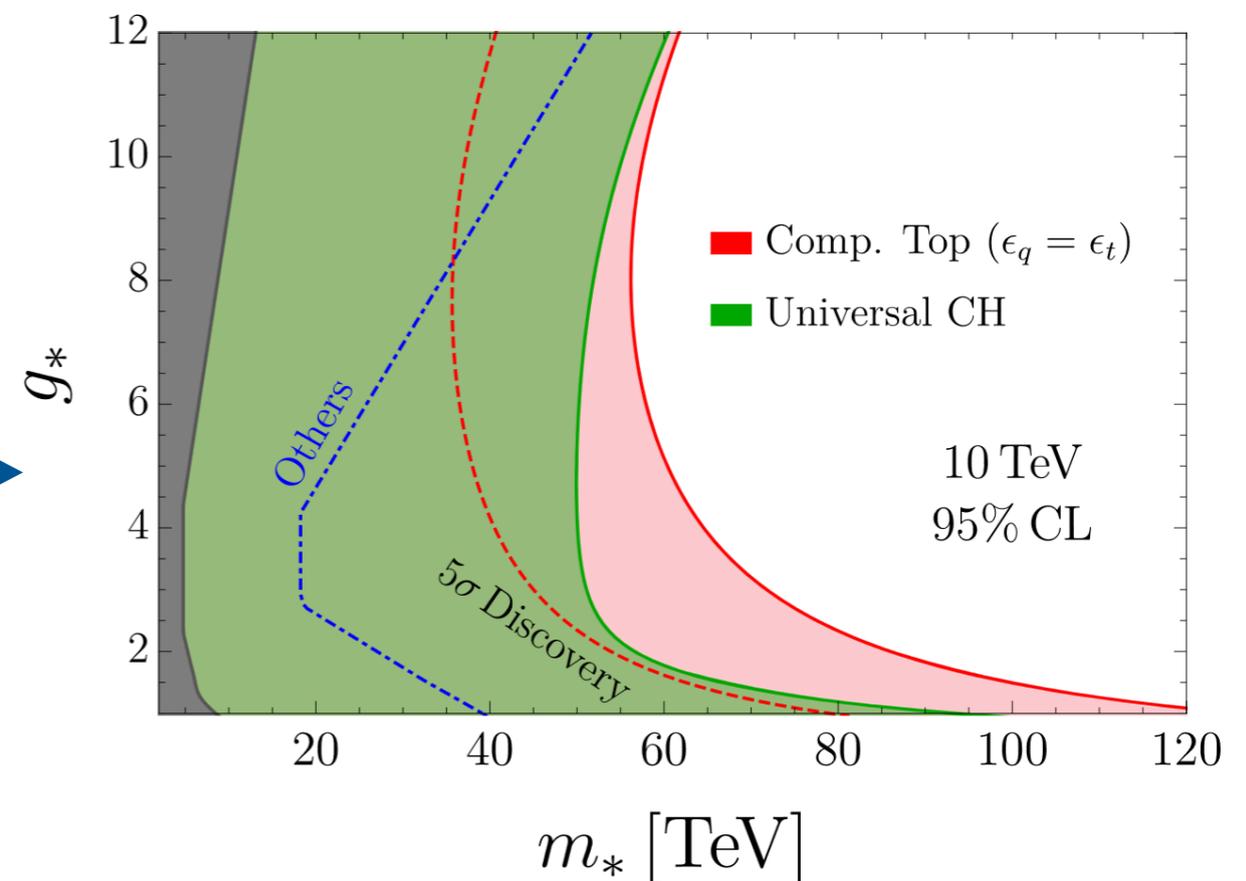
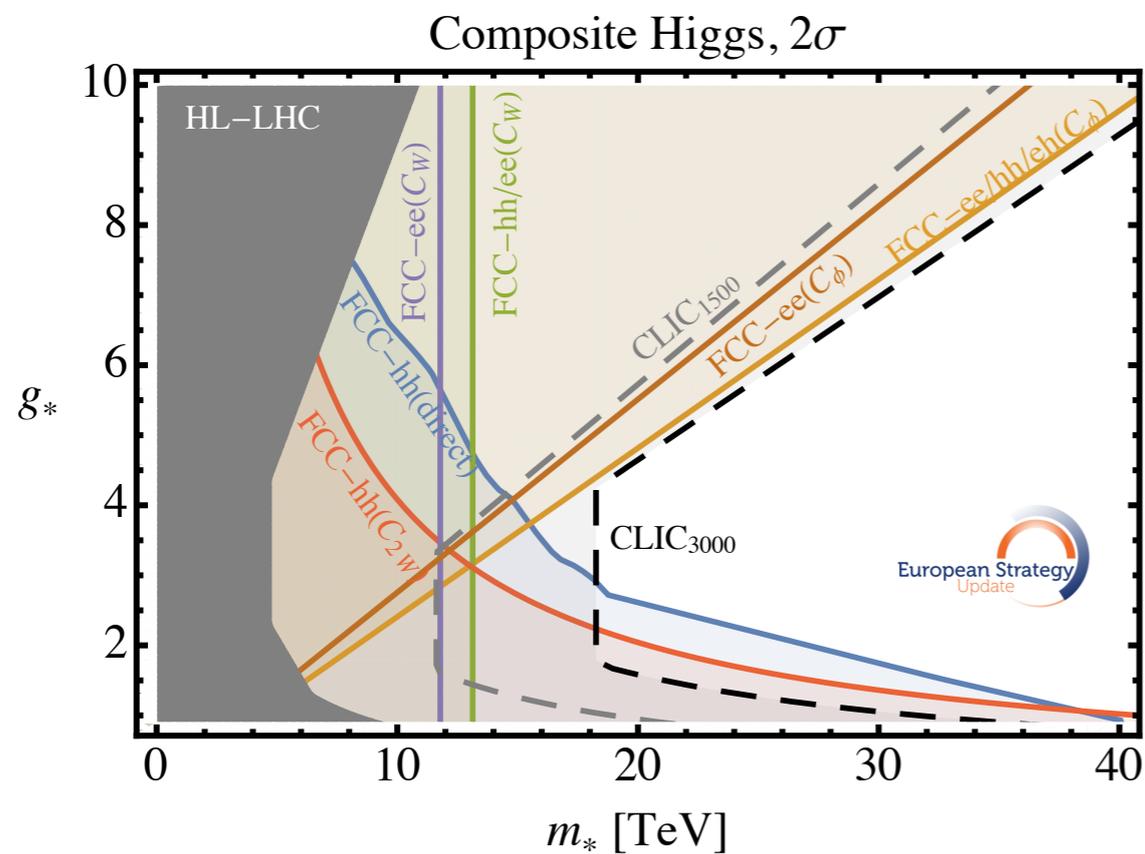
# High-energy probes: EW & Higgs physics

- High-energy processes at a 10–30 TeV lepton collider are able to probe EW new physics scales of 100 TeV or more.

- 10x higher than ultimate precision at Z pole



- Example:** new physics with mass  $m_*$  and coupling  $g_*$



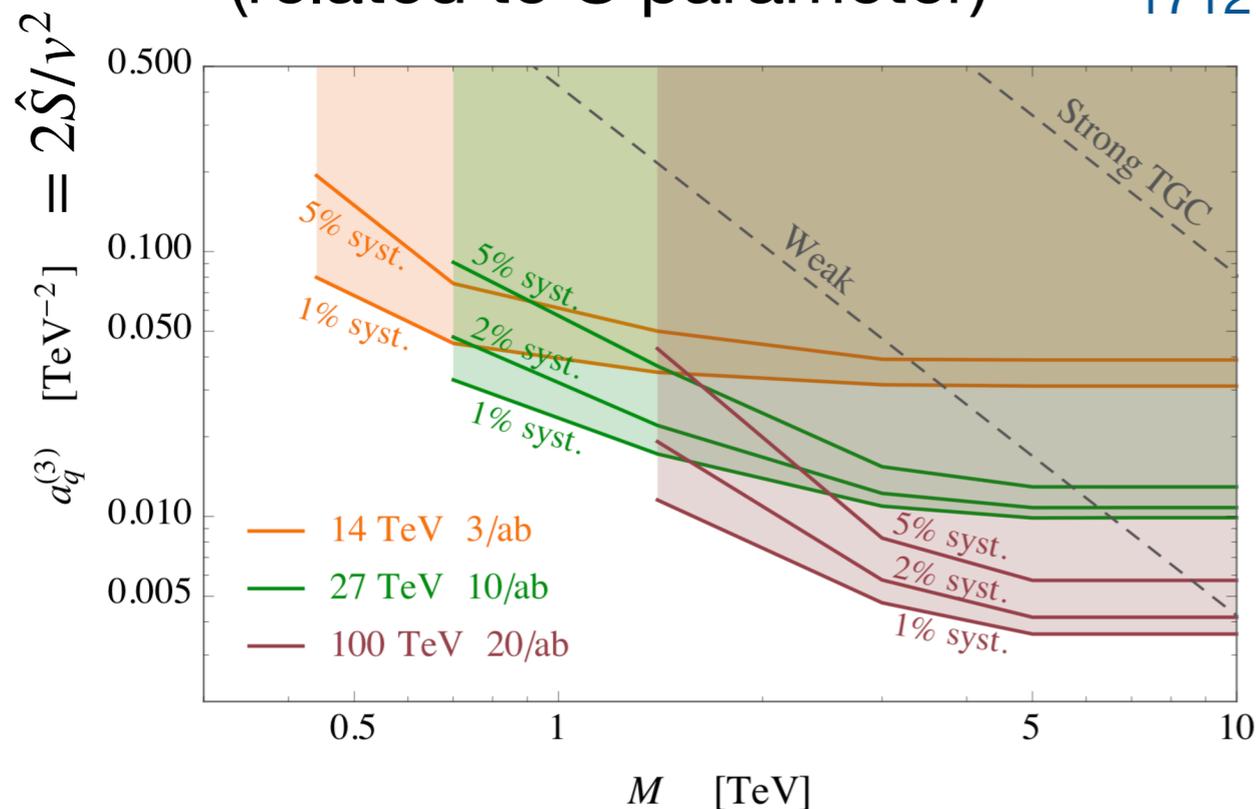
# EW physics at hadron colliders

- ◆ A similar strategy can be used at a high-energy hadron collider

- ◆  $pp \rightarrow \ell\ell, \ell\nu$  constrains  $W, Y$  parameters

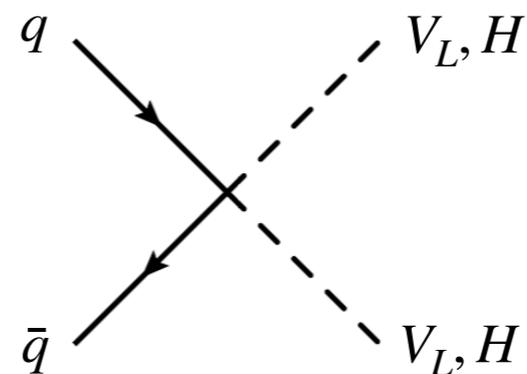
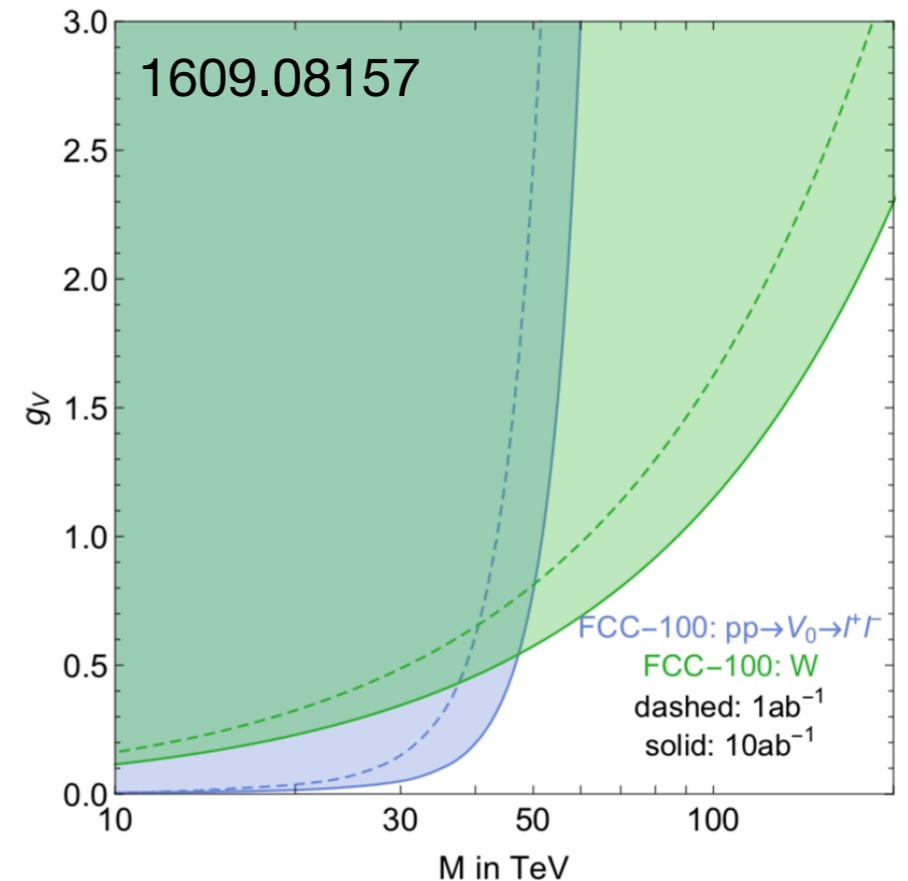
		LHC 13		100 TeV
luminosity		$0.3 \text{ ab}^{-1}$	$3 \text{ ab}^{-1}$	$10 \text{ ab}^{-1}$
NC	$W \times 10^4$	$\pm 1.5$	$\pm 0.8$	$\pm 0.04$
	$Y \times 10^4$	$\pm 2.3$	$\pm 1.2$	$\pm 0.06$
CC	$W \times 10^4$	$\pm 0.7$	$\pm 0.45$	$\pm 0.02$

- ◆  $pp \rightarrow Vh, VV$  constrains  $C_W, C_B$   
(related to  $S$  parameter)



1609.08157

1712.01310

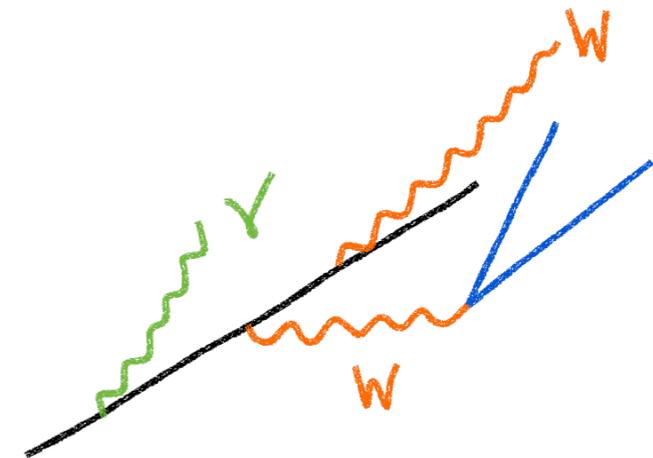


- ◆ Strong PDF suppression at high  $p_T$ : lower reach

# Challenges/opportunities

**EW radiation** becomes important at multi-TeV energies!

Especially relevant for muon collider, but also FCC-hh...

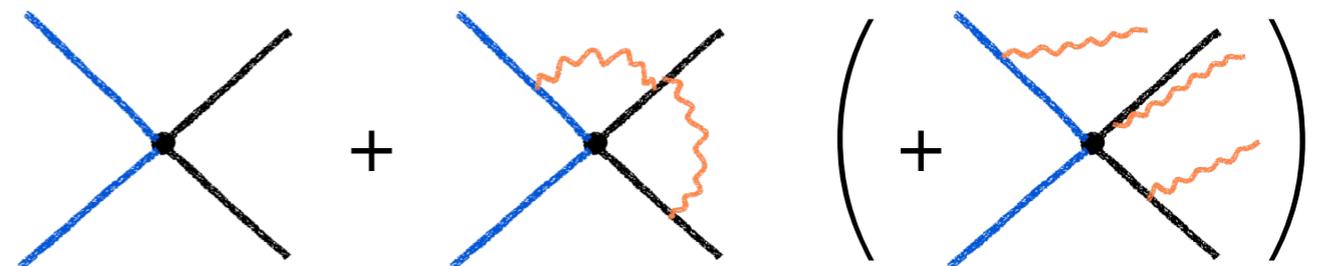


- ◆  $m_{W,Z} \ll E$ :  $\gamma$ ,  $W$ ,  $Z$  are all similar!
- ◆ Multiple gauge boson emission is not suppressed

$$\text{Sudakov factor } \frac{\alpha}{4\pi} \log^2\left(\frac{E^2}{m_W^2}\right) \times \text{Casimir} \approx 1 \text{ for } E \sim 10 \text{ TeV}$$

- Which cross-section? Exclusive, (semi-)inclusive, depending on amount of radiation included

see [Chen, Glioti, Rattazzi, Ricci, Wulzer 2202.10509](#)



- Initial state is EW-charged:

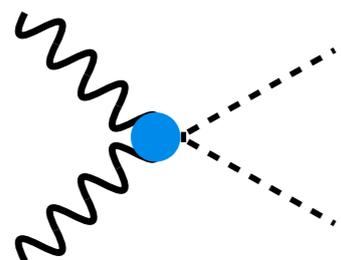
(Precise) resummation of double logs needed. Goal: % or ‰ precision

- Could one define EW jets? Neutrino “jet tagging”?

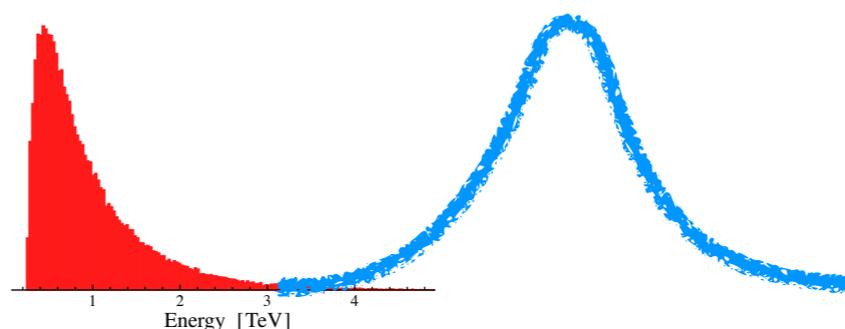
# Summary

- ◆ One of the priorities for our field in the next decades will be to **explore the 10+ TeV scale**. Precision measurements might be the quickest way...

- ◆ Two complementary paths to precision measurements:



High rate



High energy

- ◆ **“Near” future:** flavor physics, Higgs physics at %, high-pT LHC.

Scales of few TeV, EW particles below few 100 GeV

- ◆ **e+e- factory:** Higgs physics at  $10^{-3}$ , EW physics at  $10^{-5}$ , flavor.

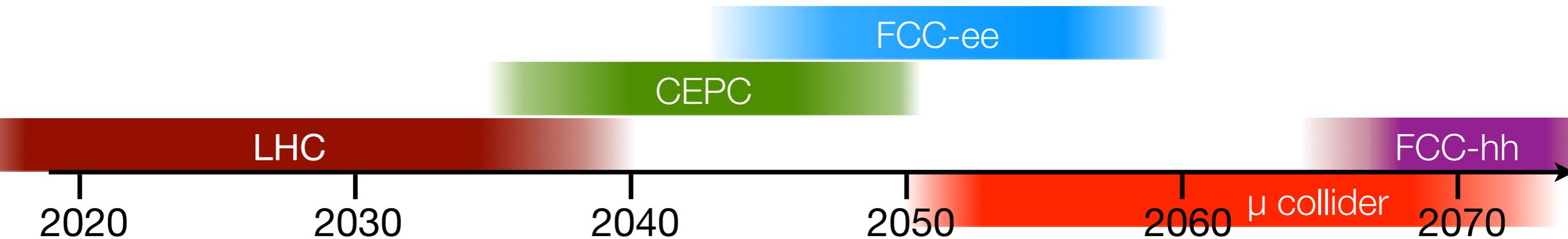
Scales  $> 10$  TeV, EW particles at few TeV

- ◆ **Ultimate goal:** collide elementary particles at the 10+ TeV energy frontier.

WW factory: Higgs physics at  $10^{-3}$ , Higgs self-coupling.

High-energy: EWPT at  $10^{-7}$ , i.e. scales  $> 100$  TeV. EW particles at 10+ TeV

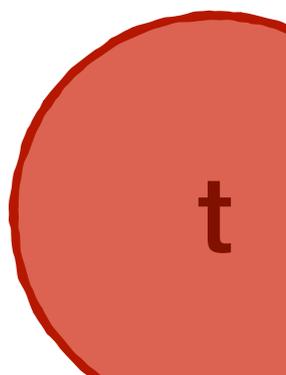
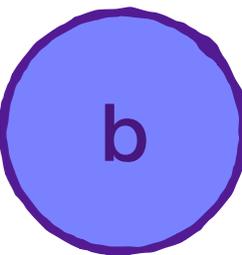
# The importance of precision measurements



The next 25+ years of particle physics will (mostly) be precision physics!

Several examples of great indirect discoveries in the past:

- ◆  $K_L \rightarrow \mu\mu$  branching ratio, K-K oscillations: prediction of charm mass  
Glashow, Iliopoulos, Maiani 1970    Lee, Gaillard 1974
- ◆ CPV in K system: existence of 3rd generation  
Kobayashi, Maskawa 1973
- ◆  $e^+e^-$  scattering below the EW scale: prediction of W, Z masses  
early 1980's
- ◆ Frequency of B-B oscillations: prediction of large top mass  
late 1980's
- ◆ ElectroWeak Precision Tests: prediction of Higgs mass  
late 1990's

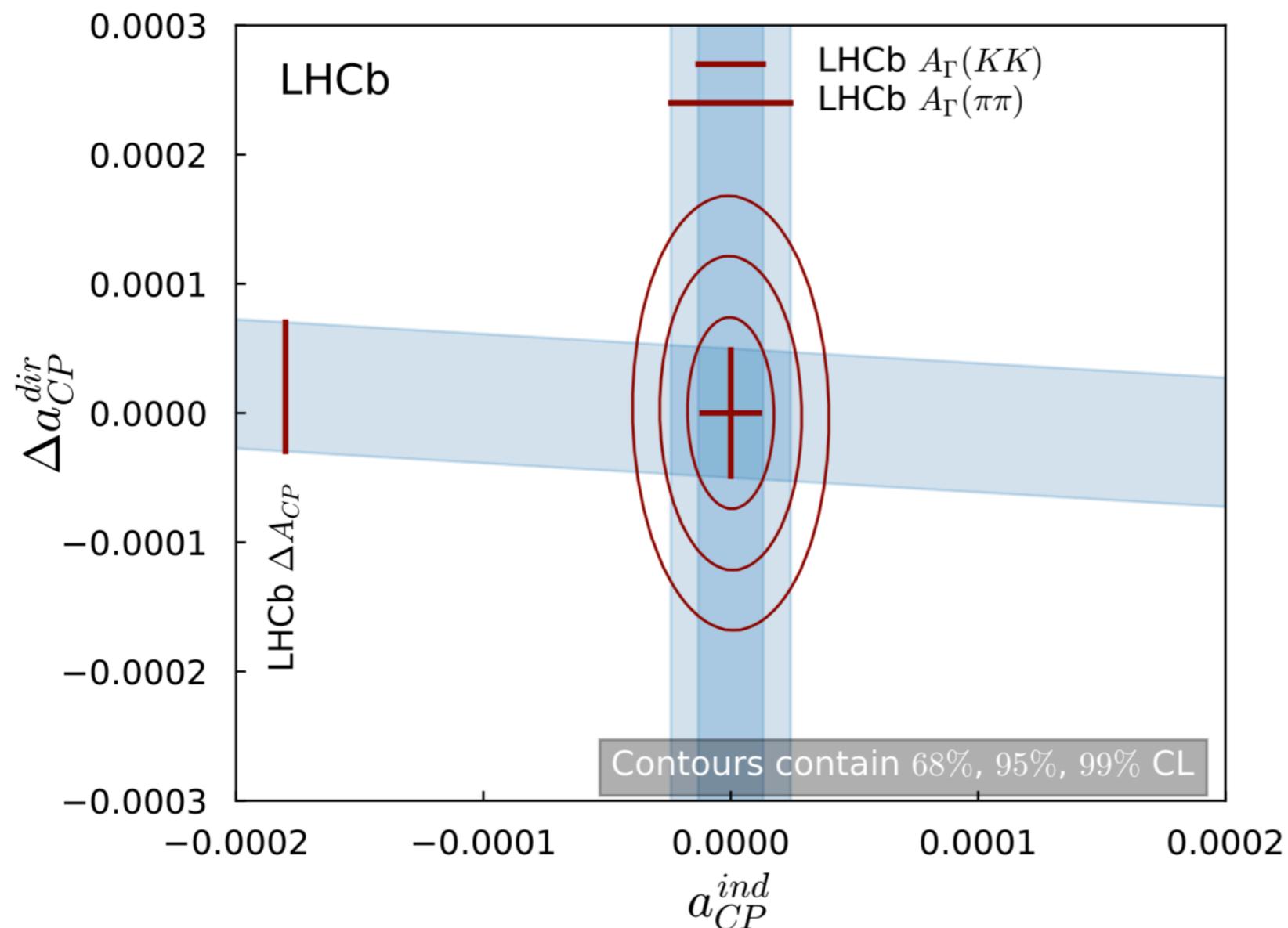




**Backup**

# Charm physics @ LHCb

- Huge sample of charmed mesons, will allow first precise measurement of CPV in D system.
- Needs big advancement in theory understanding to extract NP limit (situation similar to  $K \rightarrow \pi\pi$ )



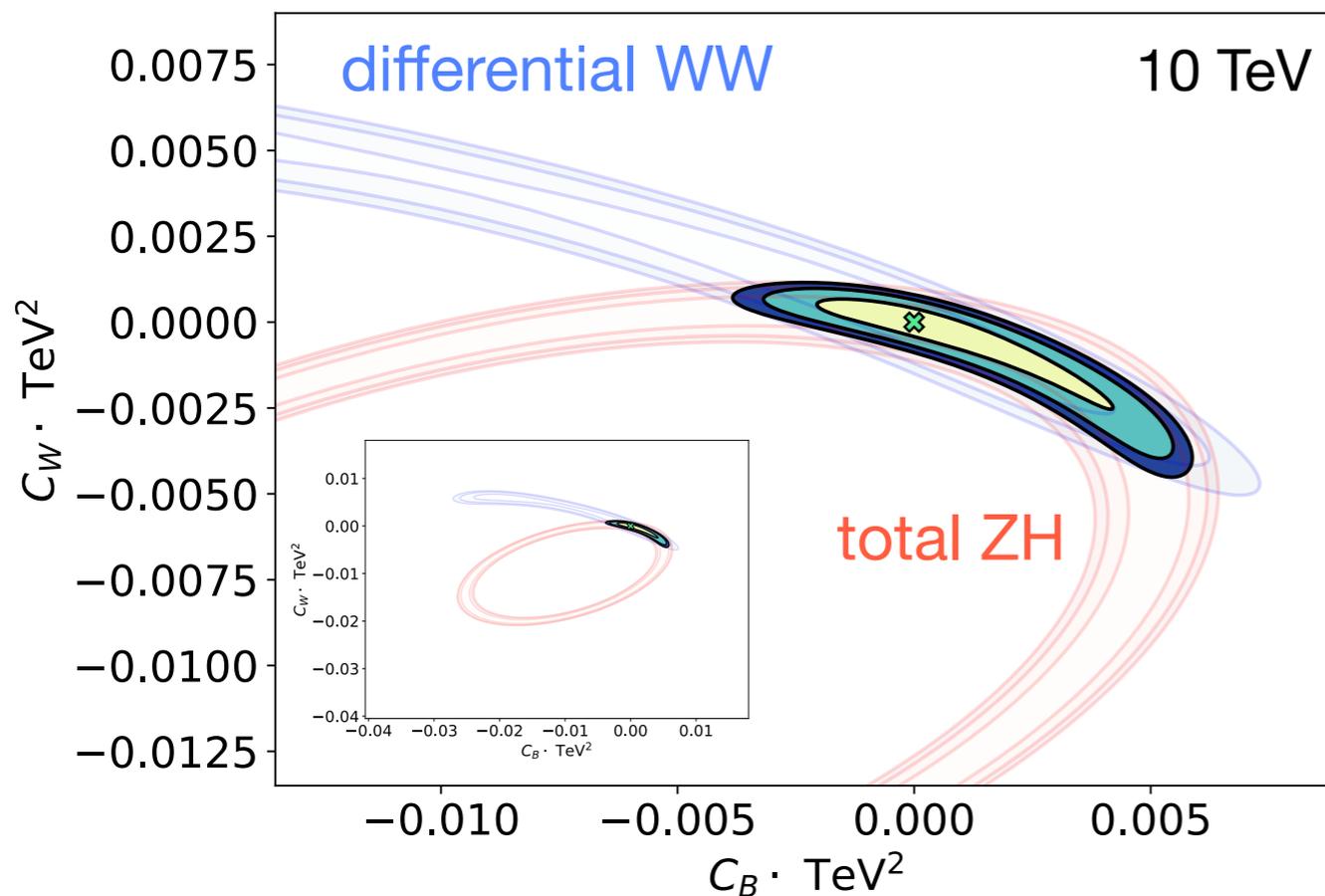
# High-energy di-bosons

- ◆  $C_W$  and  $C_B$  determined from high-energy  $\mu^+\mu^- \rightarrow ZH, W^+W^-$  cross-sections

$$\sigma_{\mu\mu \rightarrow ZH} \approx 122 \text{ ab} \left( \frac{10 \text{ TeV}}{E_{\text{cm}}} \right)^2 \left[ 1 + \# E_{\text{cm}}^2 C_W + \# E_{\text{cm}}^4 C_W^2 \right]$$

◆ Limits on  $C_{W,B}$  scale as  $E^2$

B, Franceschini, Wulzer 2012.11555



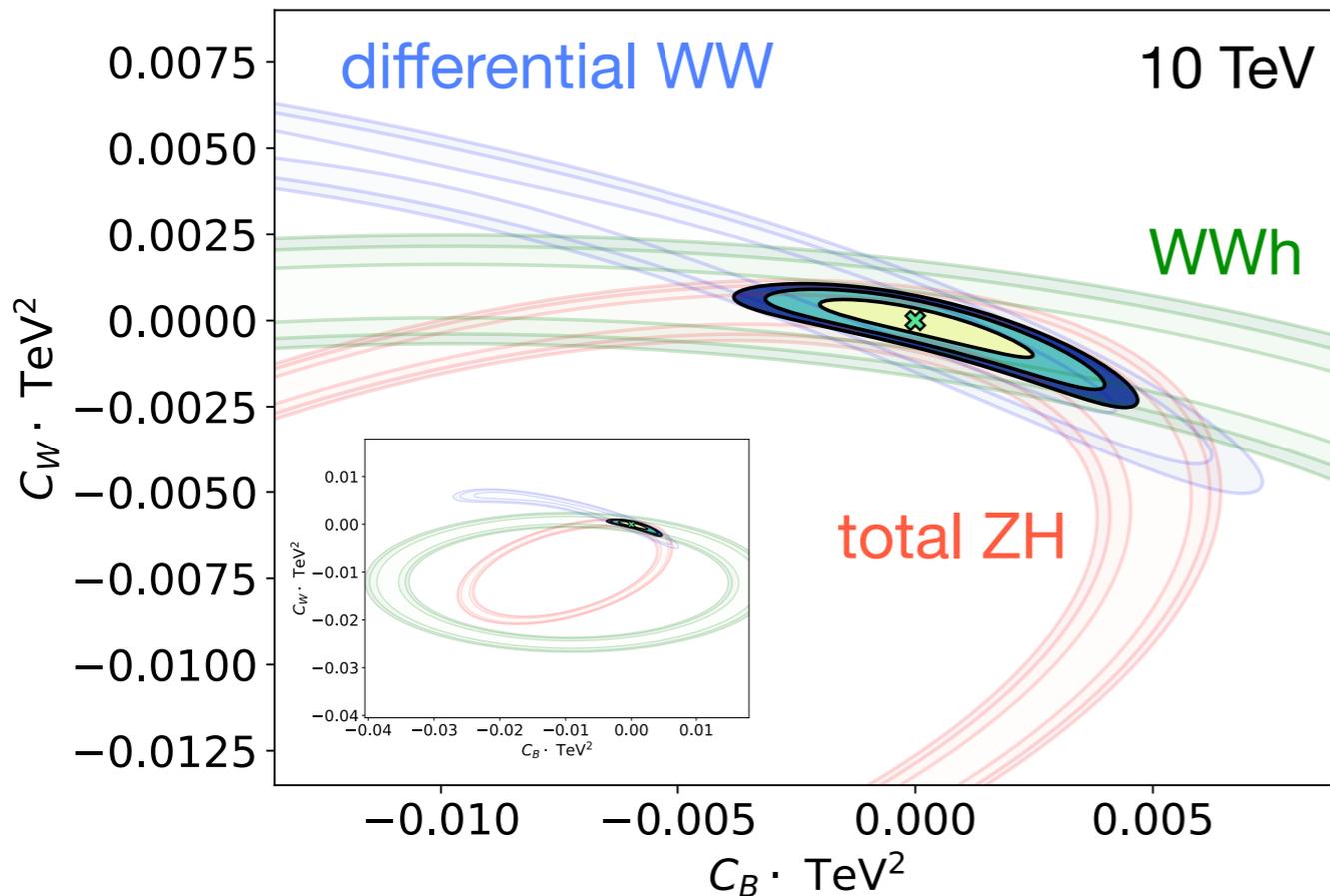
- ◆ Fully differential WW cross-section in scattering and decay angles: can exploit the interference with transverse polarization amplitude

# High-energy di-bosons

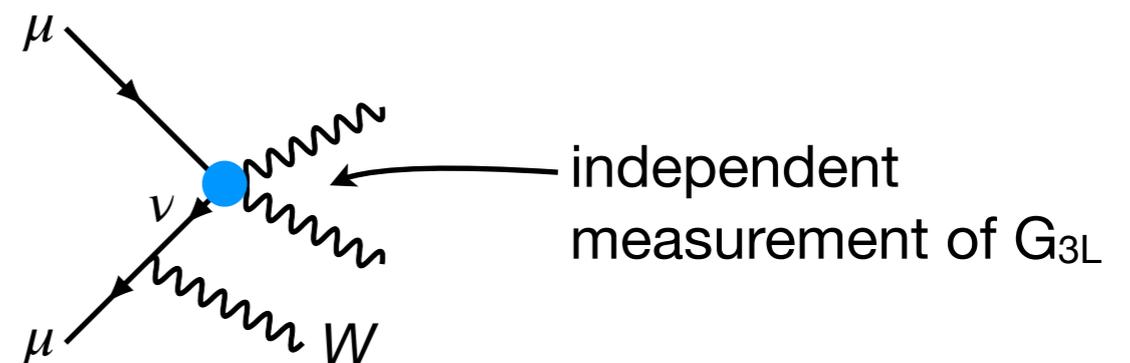
- ◆  $C_W$  and  $C_B$  determined from high-energy  $\mu^+\mu^- \rightarrow ZH, W^+W^-$  cross-sections

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B, Franceschini, Wulzer 2012.11555



- ◆ Gauge boson radiation important at high energies: soft W emission allows to access the charged processes  $\ell^\pm \nu \rightarrow W^\pm Z, W^\pm H$



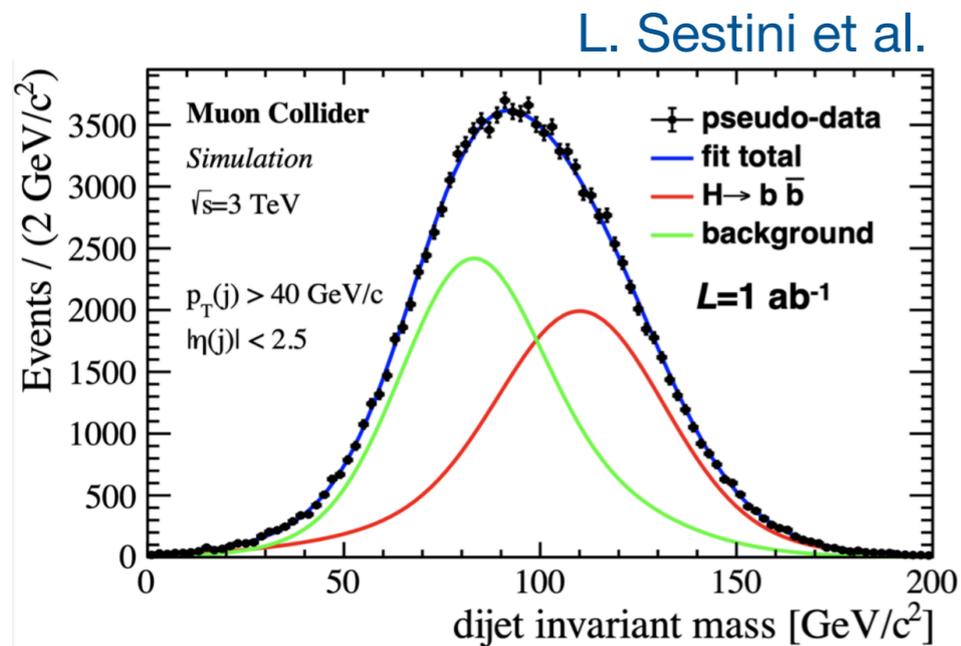
need to properly include higher-order effects  
inclusive observables, resummation, ...

“effective neutrino approximation”

# Single Higgs: backgrounds

- ◆ Physics backgrounds (including the Higgs itself!)

- ◆ Beam-induced background



- ◆ Detector performance
- ◆ “soft” and forward particles

Forslund, Meade  
2203.09425

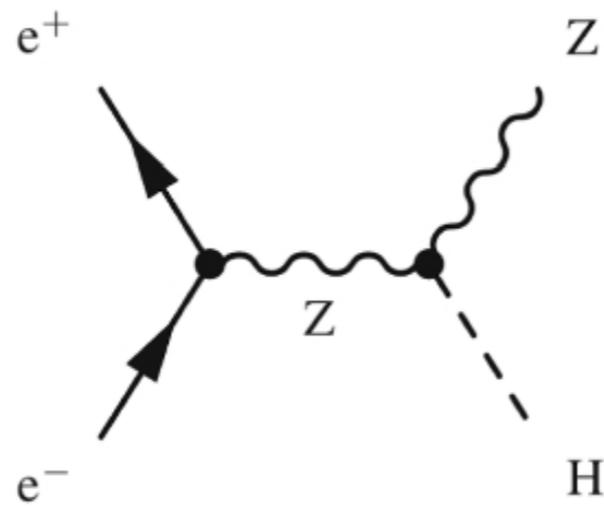
Production	Decay	$\Delta\sigma/\sigma$ (%)		Signal Only
		3 TeV	10 TeV	10 TeV
$W^+W^-$ fusion	$bb$	0.80	0.22	0.17
	$cc$	12	3.6	1.7
	$gg$	2.8	0.79	0.19
	$\tau^+\tau^-$	3.8	1.1	0.54
	$WW^*(jj\nu)$	1.6	0.42	0.30
	$WW^*(4j)$	5.4	1.2	0.49
	$ZZ^*(4\ell)$	48	13	12
	$ZZ^*(jj\ell\ell)$	12	3.4	2.3
	$ZZ^*(4j)$	65	15	1.4
	$\gamma\gamma$	6.4	1.7	1.3
	$Z(jj)\gamma$	45	12	2.0
	$\mu^+\mu^-$	28	5.7	3.9
$ZZ$ fusion	$bb$	2.6	0.77	0.49
	$cc$	72	17	-
	$gg$	14	3.3	-
	$\tau^+\tau^-$	21	4.8	-
	$WW^*(jj\nu)$	8.4	2.0	-
	$WW^*(4j)$	17	4.4	1.3
	$ZZ^*(jj\ell\ell)$	34	11	-
$\gamma\gamma$	23	4.8	-	
$ttH$	$bb$	61	53	12

# Degeneracy: invisible Higgs search

- ◆ Caveat: single Higgs at  $\mu\text{C}$  can access only

$$\mu_f = \sigma_h \times \text{BR}_{h \rightarrow f} \sim \frac{g_W^2 \times g_f^2}{\Gamma_h} \quad (\text{similar to LHC})$$

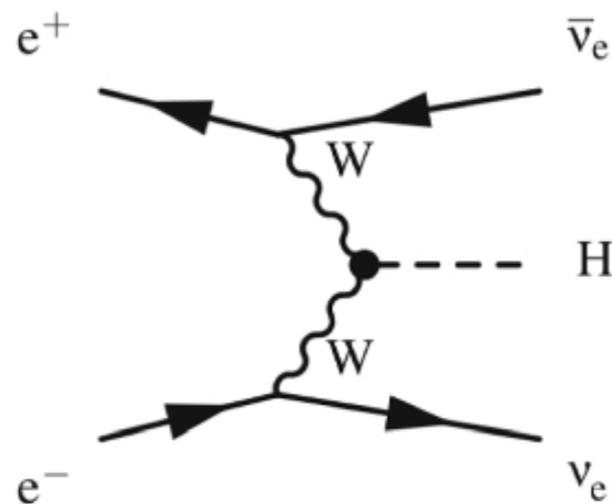
Higgsstrahlung



$$s = (p_h + p_Z)^2$$

Inclusive measurement,  $\sigma_h \sim g_Z^2$

WW fusion

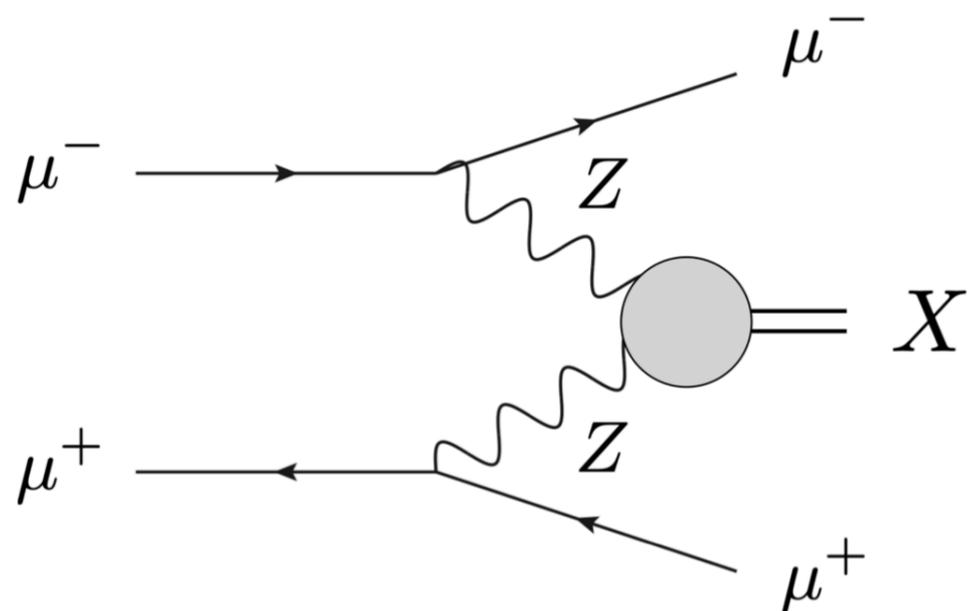


Hard neutrinos not seen,  
 $WW \rightarrow h \rightarrow WW$  depends  
 on  $g_W$  and  $\Gamma$

# Inclusive Higgs search

- Try to do an inclusive single Higgs measurement with  $ZZ \rightarrow h$

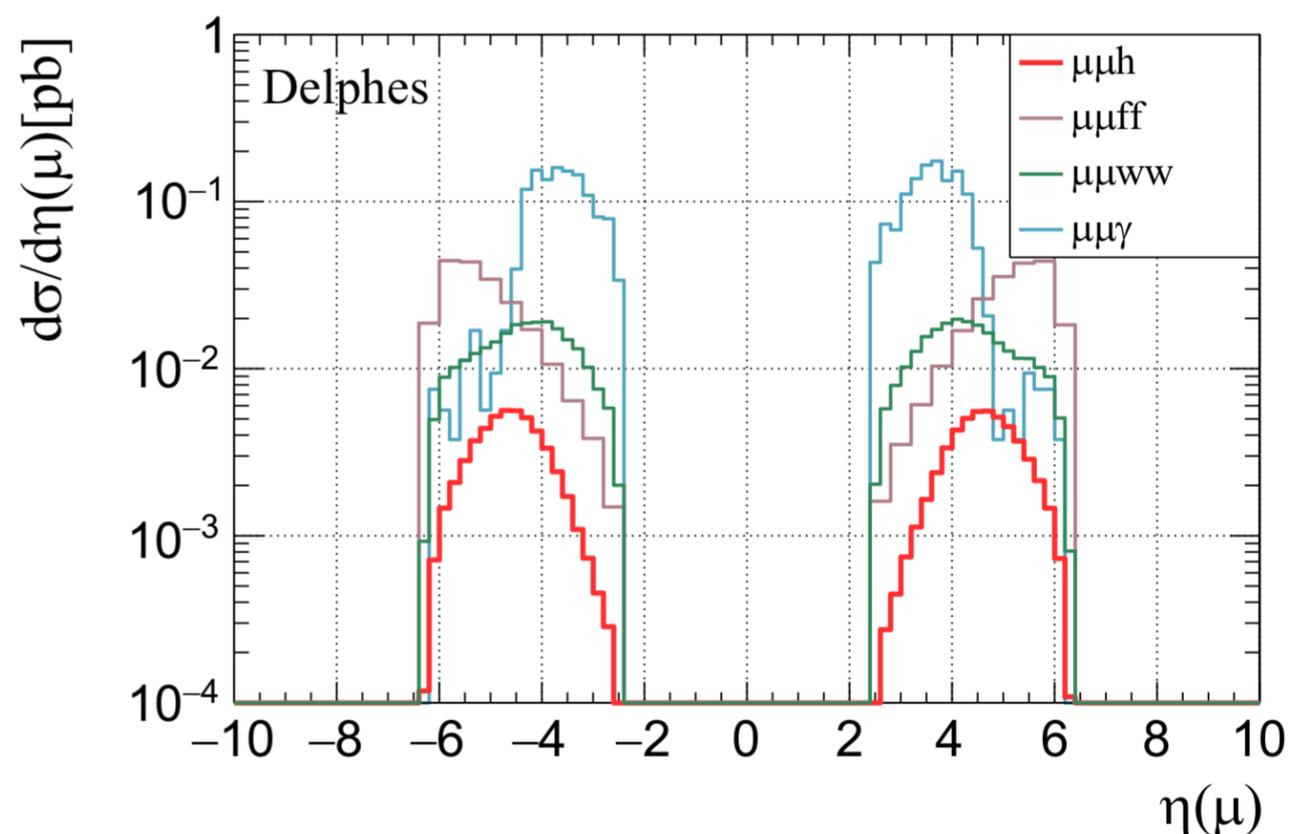
P. Li, Z. Liu, K. Lyu 2401.08756



- cross-section  $\sim 10x$  lower than  $WW$
- needs forward muon detection!**

$$s = (p_h + p_{\mu 1} + p_{\mu 2})^2$$

	$\eta < 4$	$\eta < 6$
$Br_{inv}^{95\%}(\%)$	+0.64 0	+0.10 0
$Br_{unt}^{95\%}(\%)$	+27 0	+2.0 0
$\kappa_{\Gamma}(\%)$	+34 -0.45	+2.1 -0.41



# Invisible Higgs @ muon collider

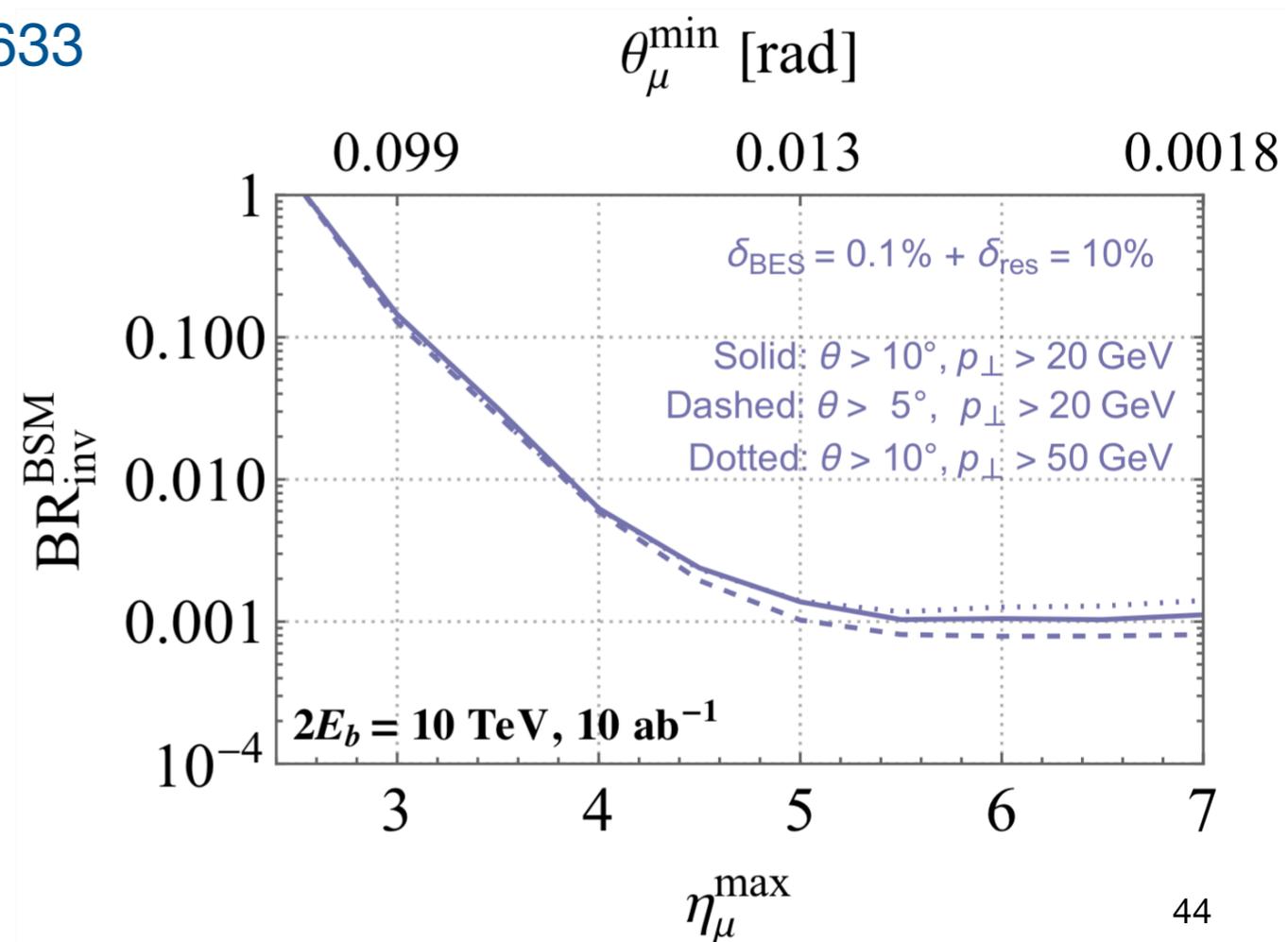
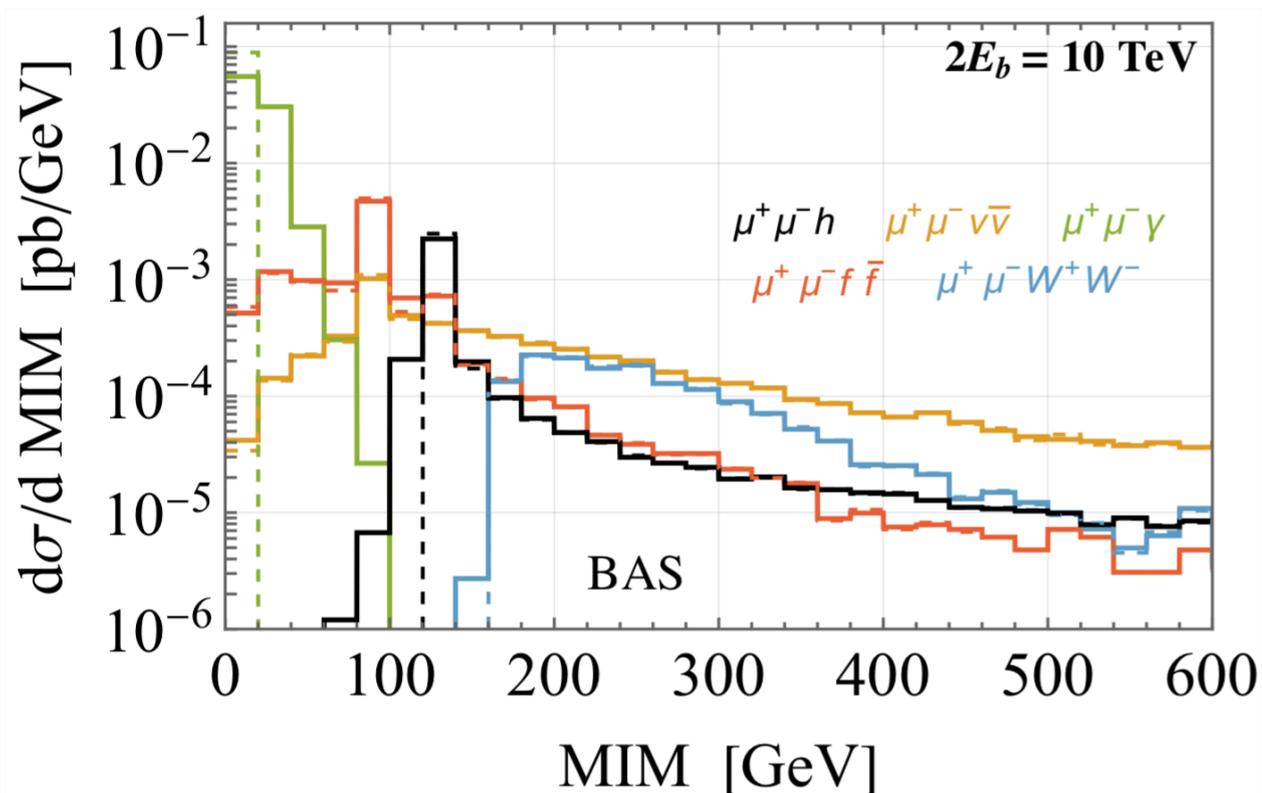
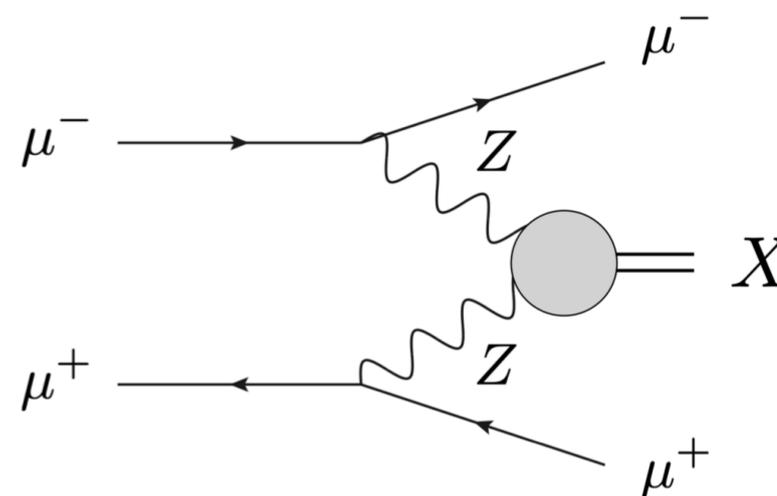
- ◆ Invisible BSM Higgs Branching Ratio can be one of the contributions to total width  $\Gamma$ .

- ◆ Can also be studied in ZZ-fusion:  
 $10^{-3}$  sensitivity *if we can detect muons*

at  $\eta \gtrsim 5$

Ruhdorfer, Salvioni, Wulzer 2303.14202

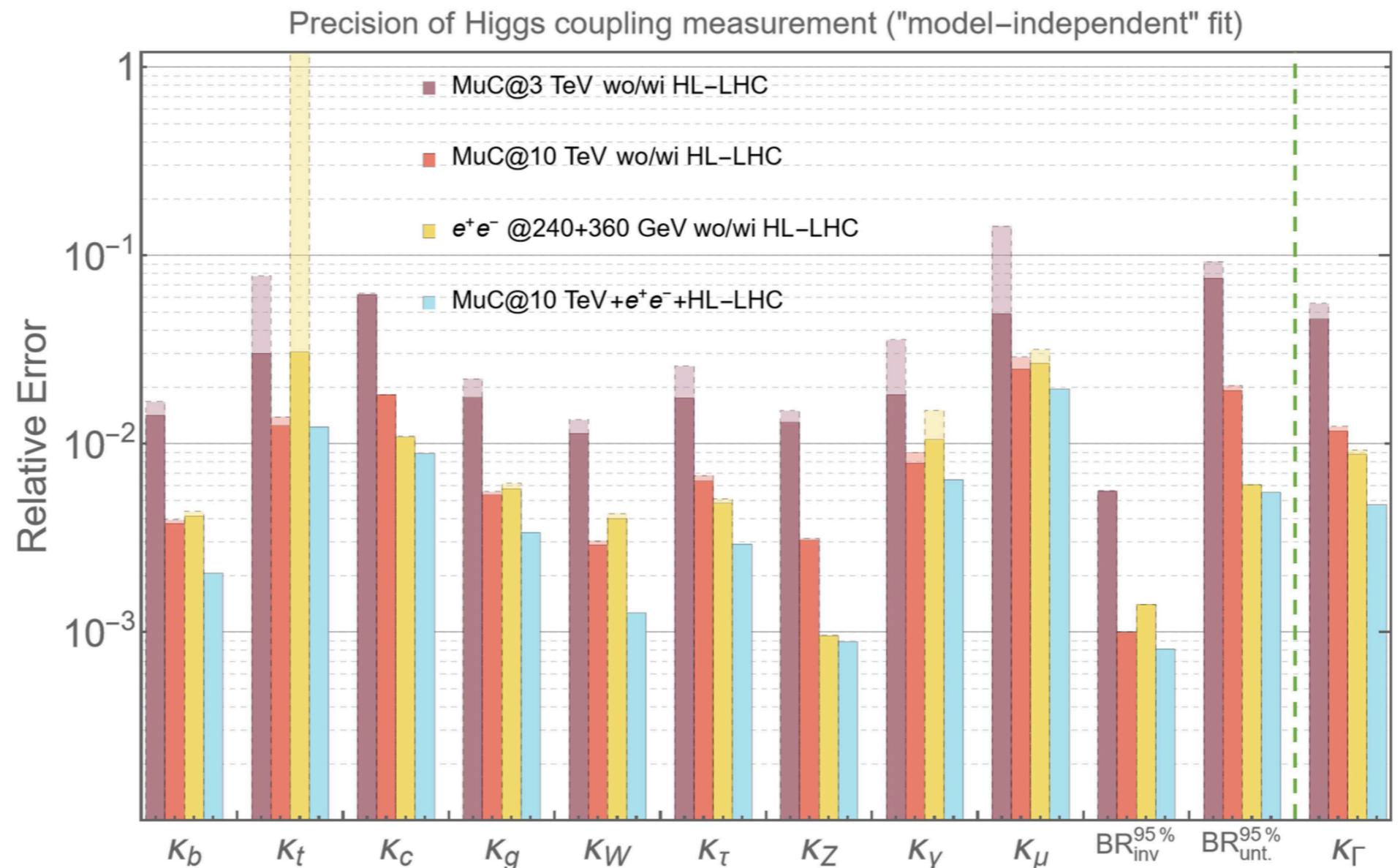
Forslund, Meade 2308.02633



# Higgs couplings at muon collider

- ◆ A full-fledged Higgs-physics program is possible at a  $\mu\text{C}$

- ◆ Single Higgs couplings can more easily be studied at  $e^+e^-$  factory! (*most likely before a  $\mu\text{C}$ !*)



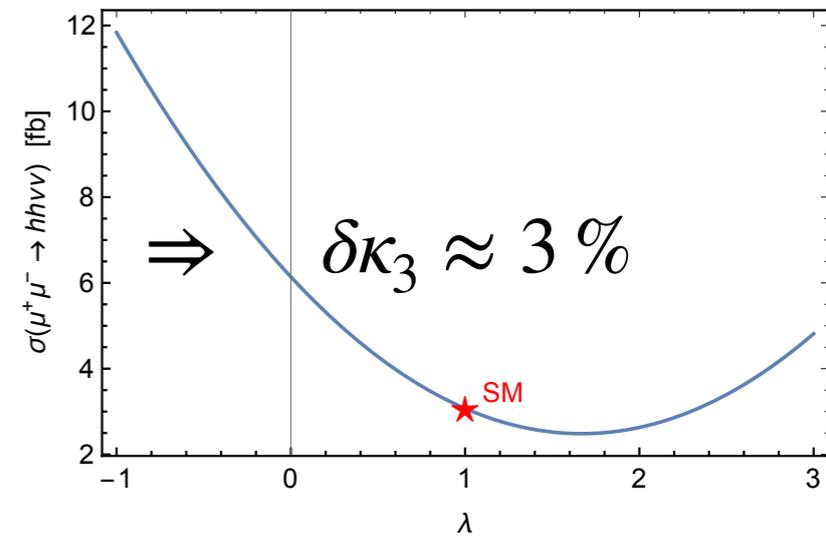
P. Li, Z. Liu, K. Lyu 2401.08756

# Double Higgs production

Number of events  $\sim s \log(s/m_h^2) \approx 10^5$  at 14 TeV

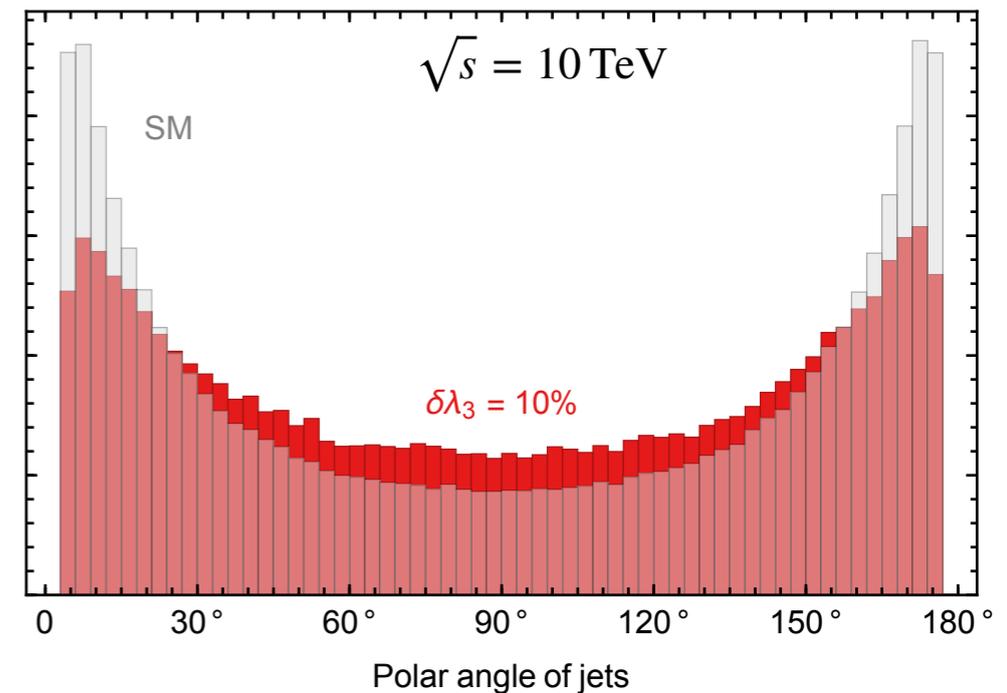
**Naïve estimate of the reach:**  $\delta\sigma \sim (N \times \epsilon)^{-1/2} \approx 1\%$

reconstruction eff.  $\sim 30\%$   
 $BR(hh \rightarrow 4b) = 34\%$  }  $\epsilon \sim 10\%$

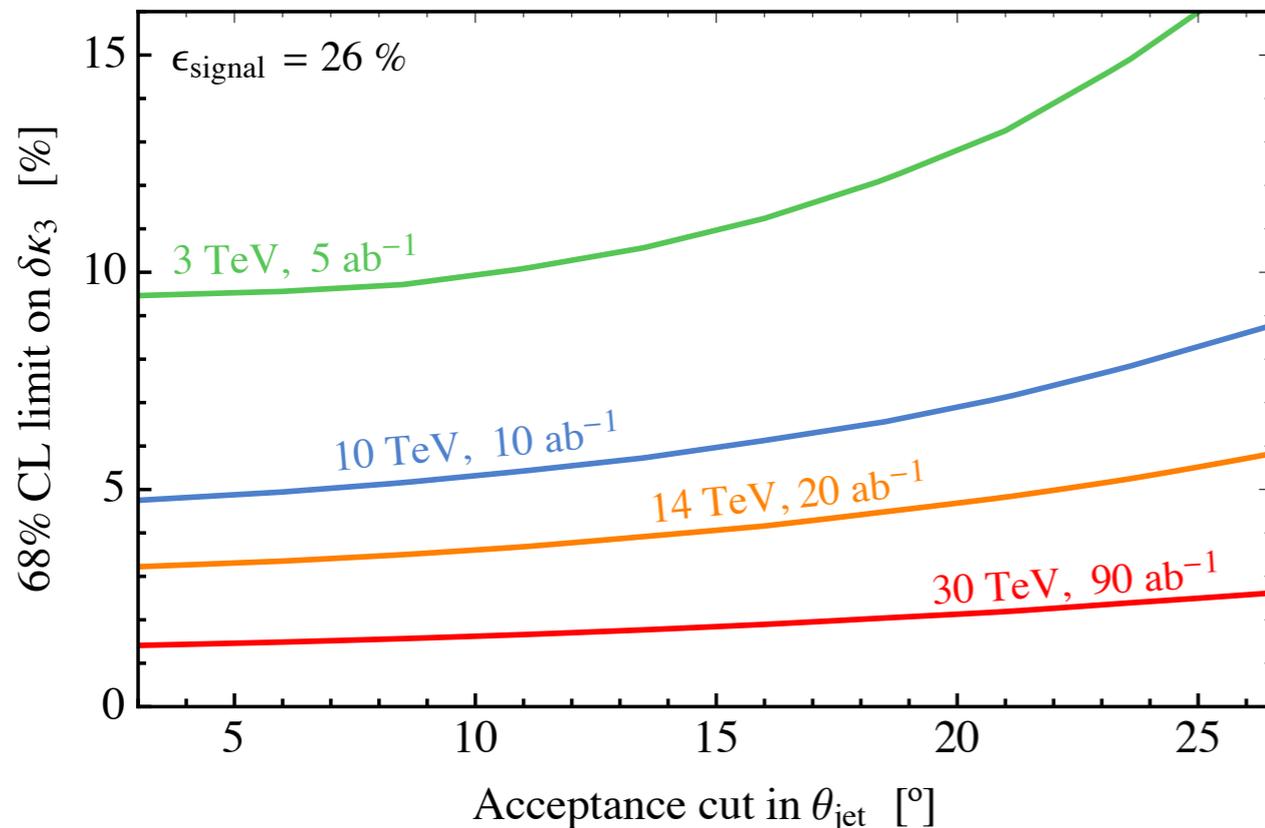


♦ **Acceptance cuts** in polar angle  $\theta$  and  $p_T$  of jets:

►  $hh$  signal is strongly peaked in forward region



B, Franceschini, Wulzer 2012.11555



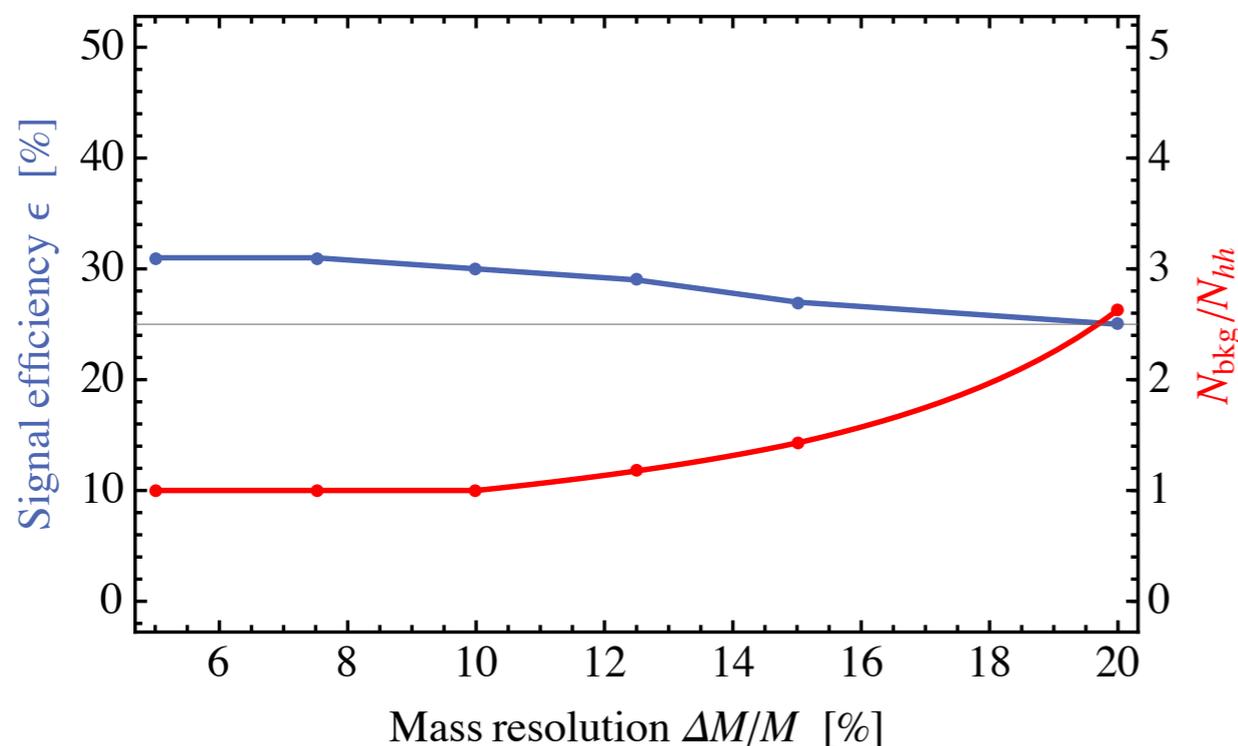
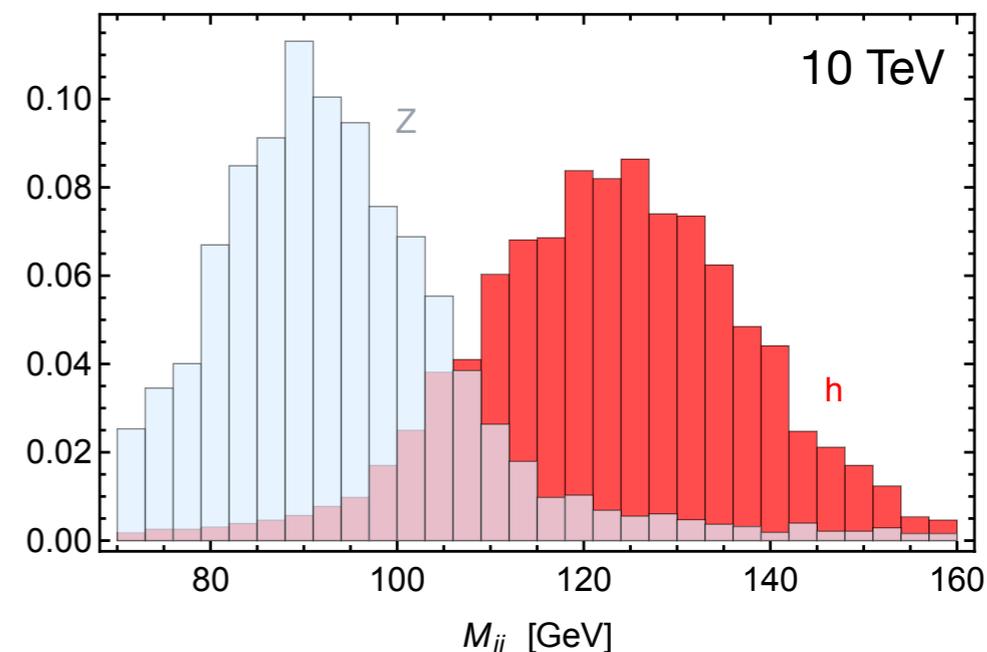
► Contribution from trilinear coupling is more central: loss due to angular cut is less important

# Double Higgs production

- ◆ **Backgrounds are important** and cannot be neglected

(see also CLIC study 1901.05897)

- ▶ Mainly VBF di-boson production: Zh & ZZ, but also WW, Wh, WZ...
- ▶ Precise invariant mass reconstruction is crucial to isolate signal



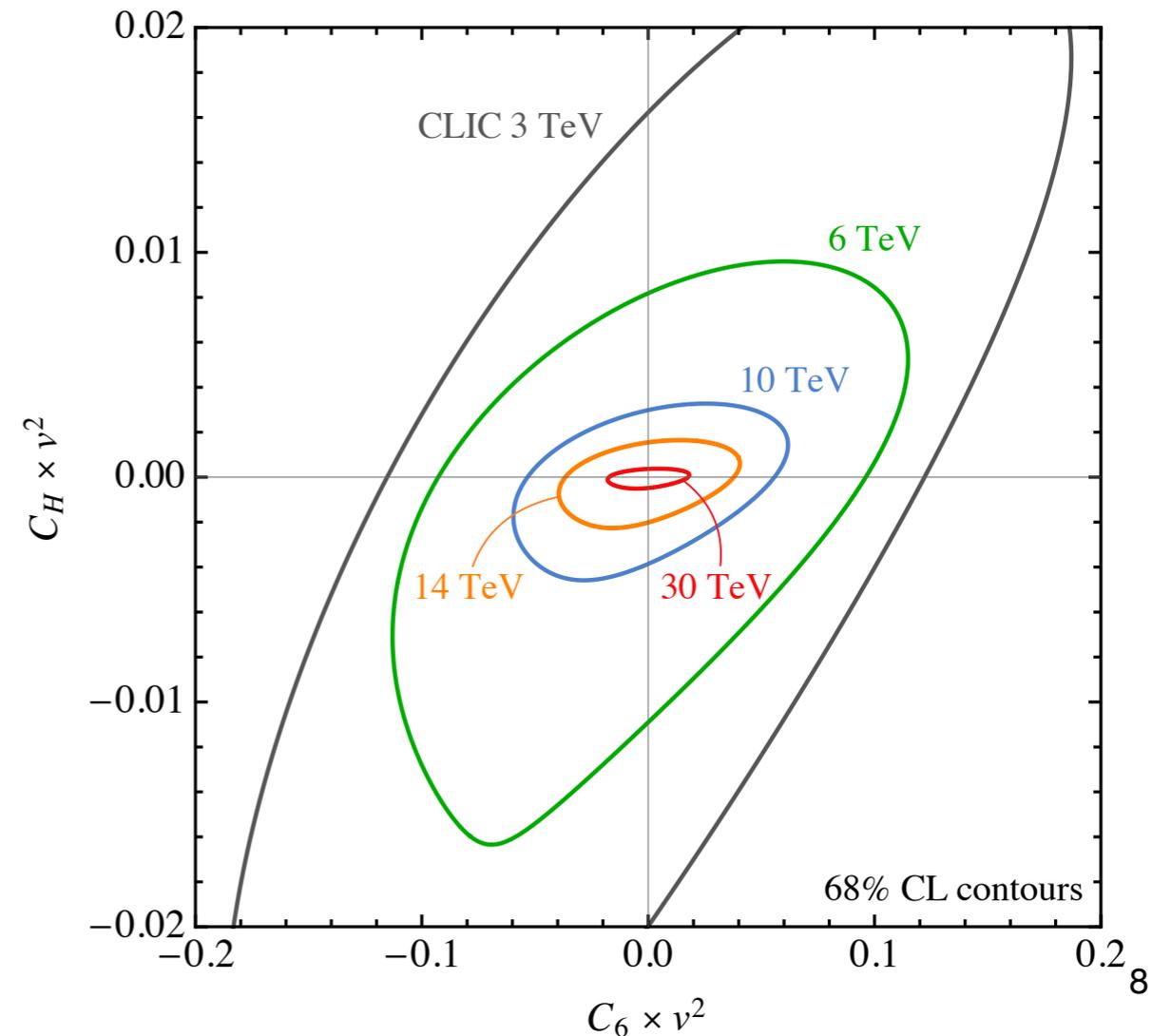
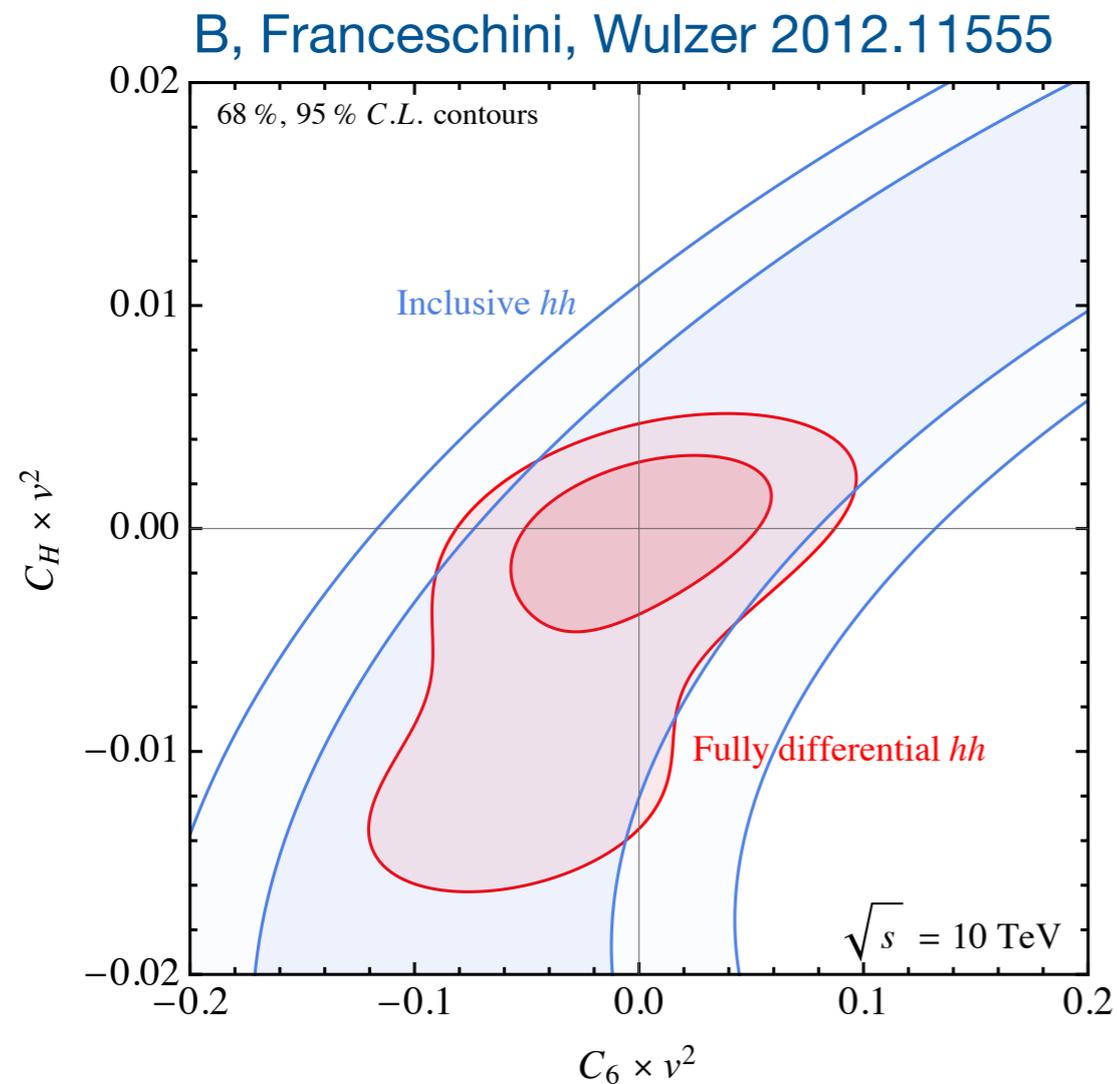
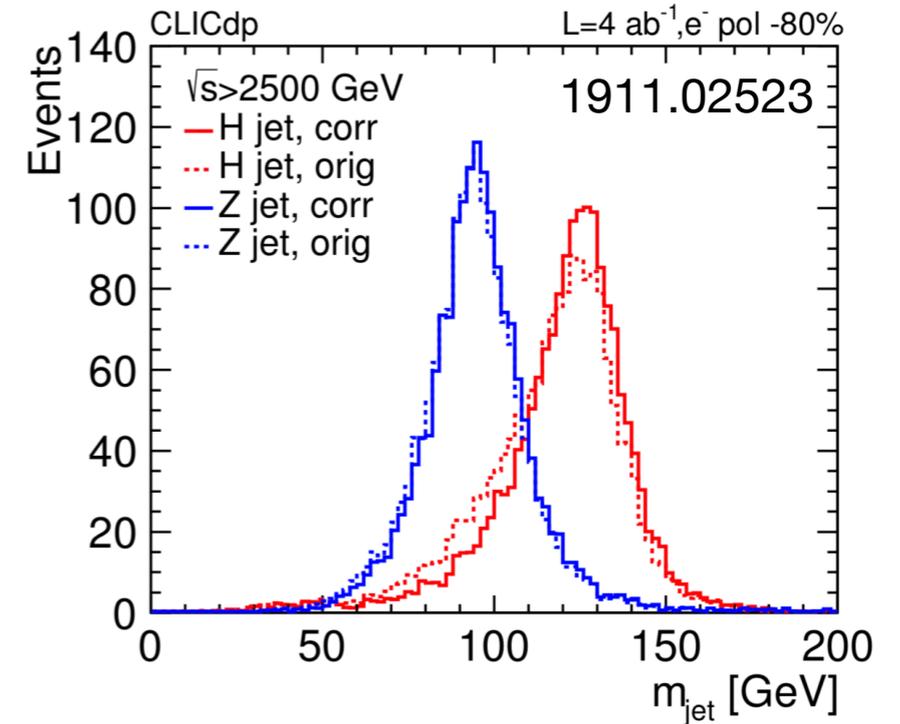
**NB:** (Very!) simplified background analysis (*at parton level!*)

All this should be done properly with a detector simulation

However, perfect agreement with 1901.05897! (3 TeV CLIC)

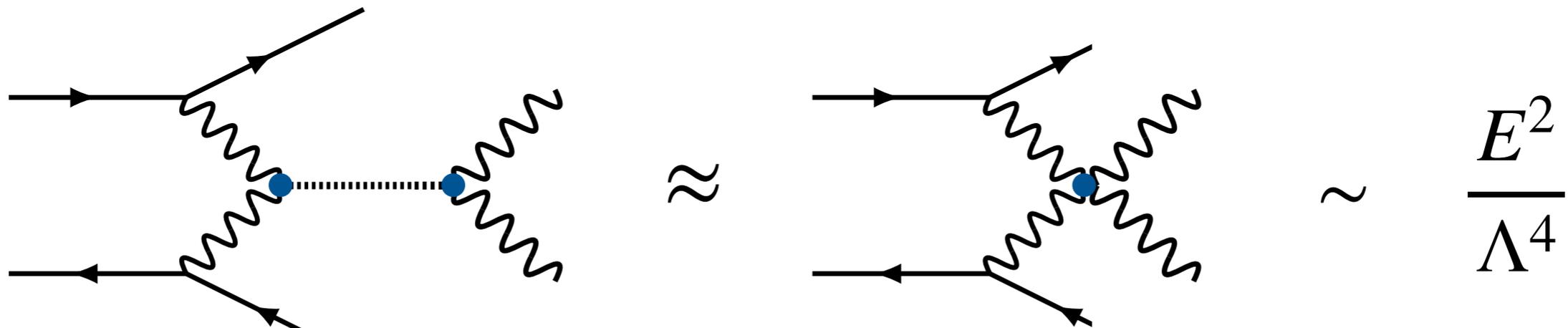
# Double Higgs at high mass

- ◆ Fully differential analysis in  $p_T$  and  $M_{hh}$  to optimize combined sensitivity to  $C_H$  and  $C_6$
- ◆ Very boosted Higgs bosons: treat them as a single h-jet, without reconstructing the 4 b's. We assumed a boosted-H tagging efficiency  $\sim 50\%$

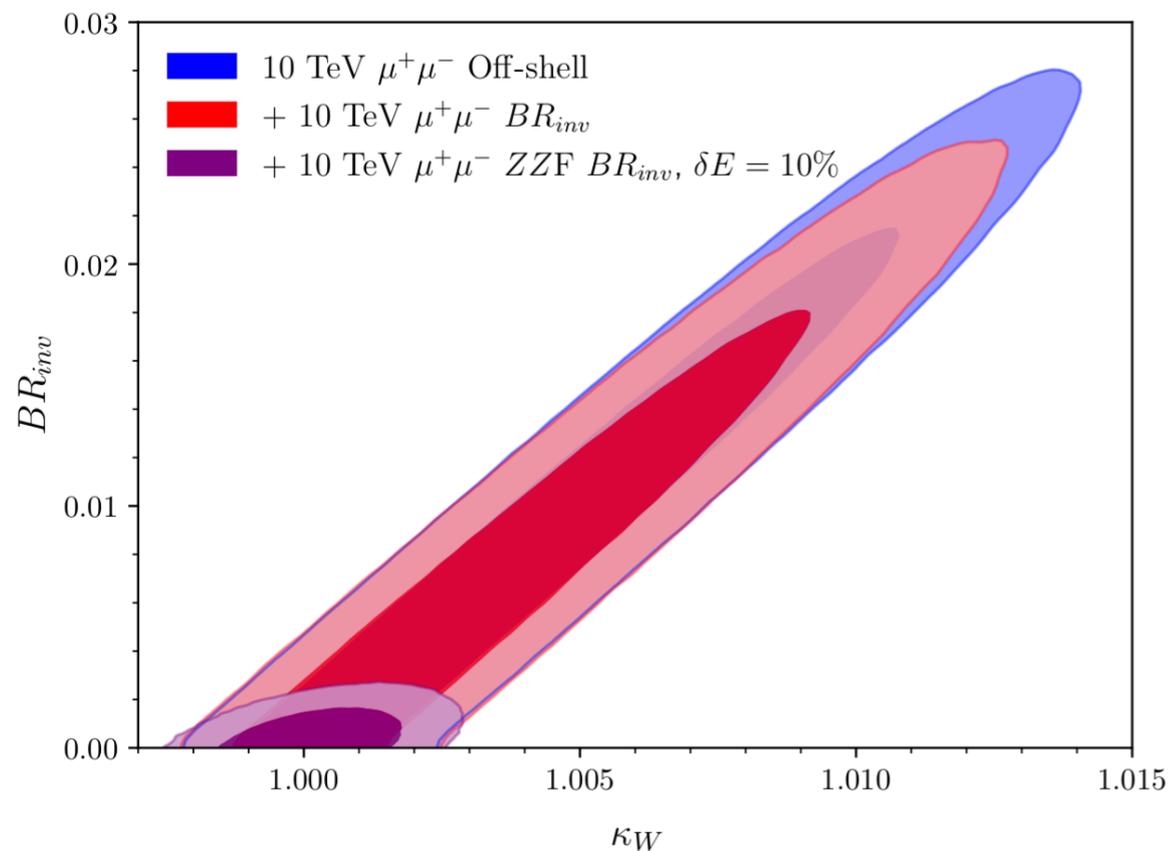


# Single Higgs at high mass (off-shell)

- ◆ Off-shell single Higgs production: independent of width



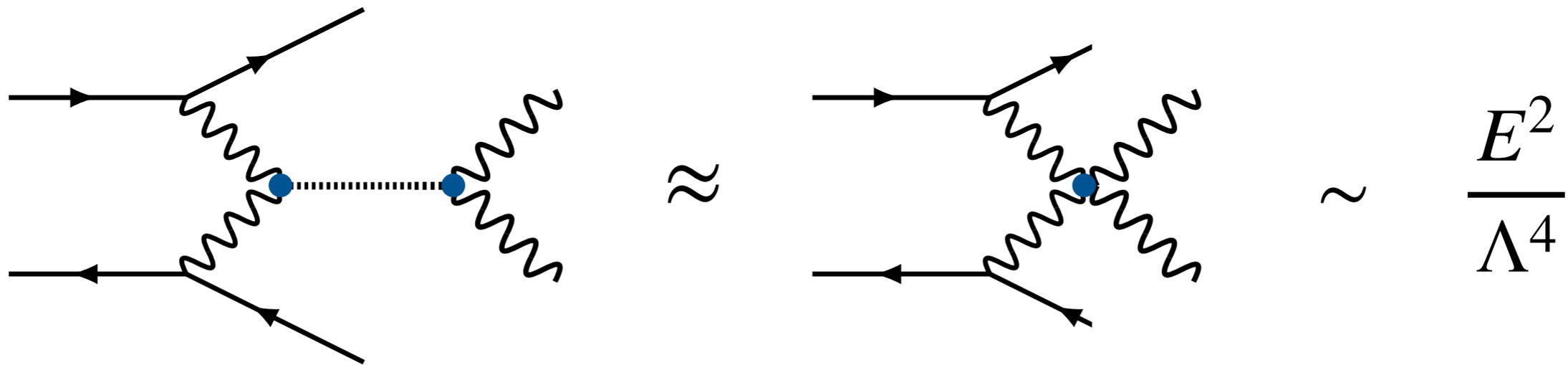
Forslund, Meade 2308.02633



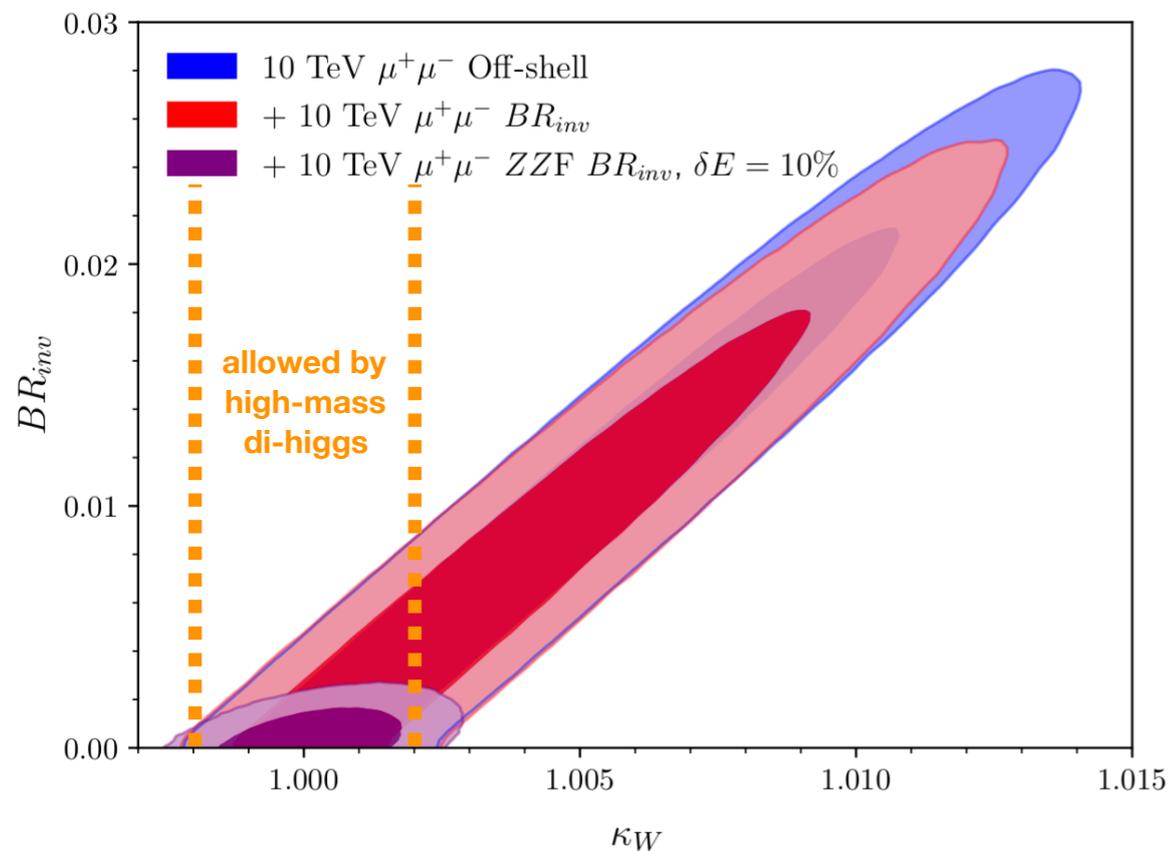
precision limited ( $\sim 3\%$ ) due to  
backgrounds: not possible to  
determine  $\kappa_W$  precisely  
through WW scattering  
→ correlation width vs. coupling

# Single Higgs at high mass (off-shell)

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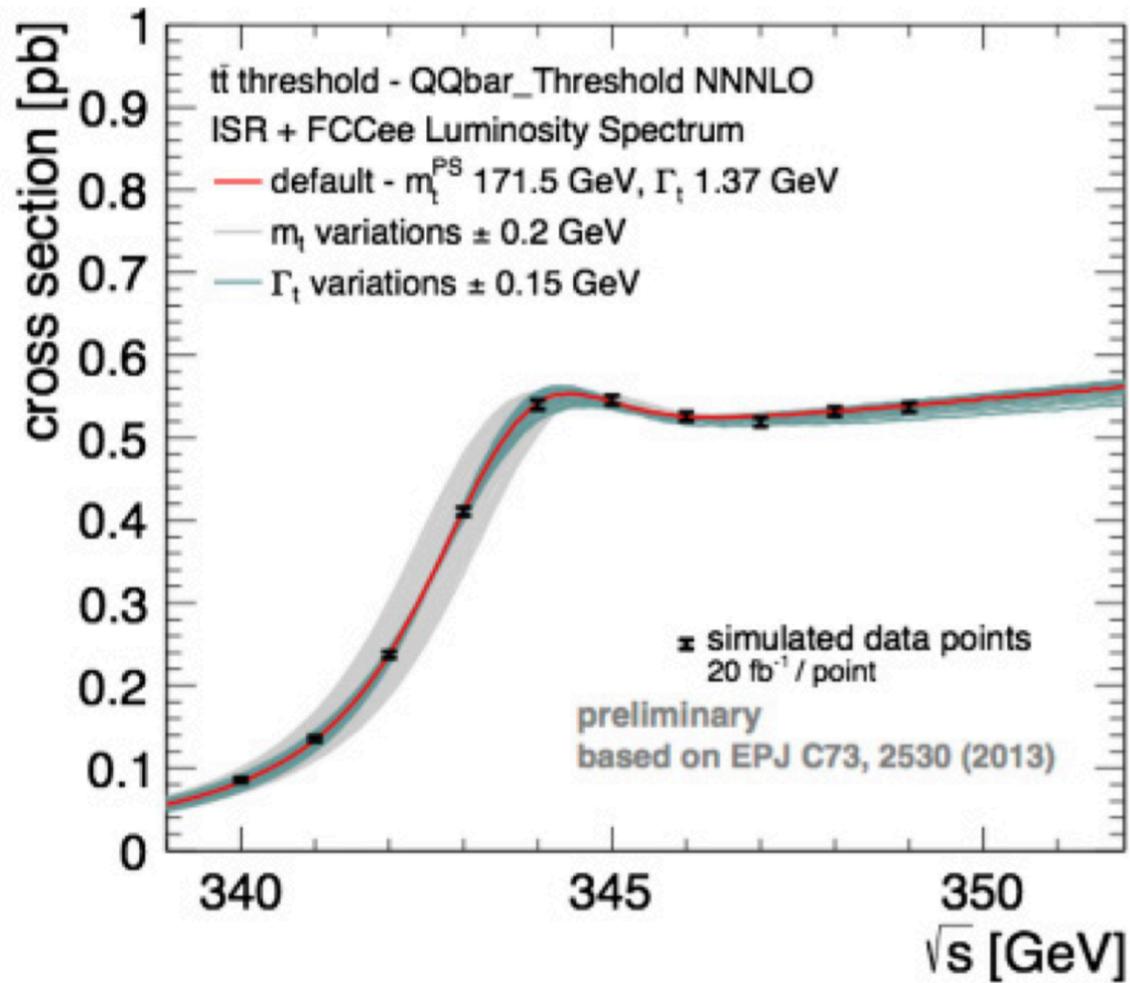


Forslund, Meade 2308.02633



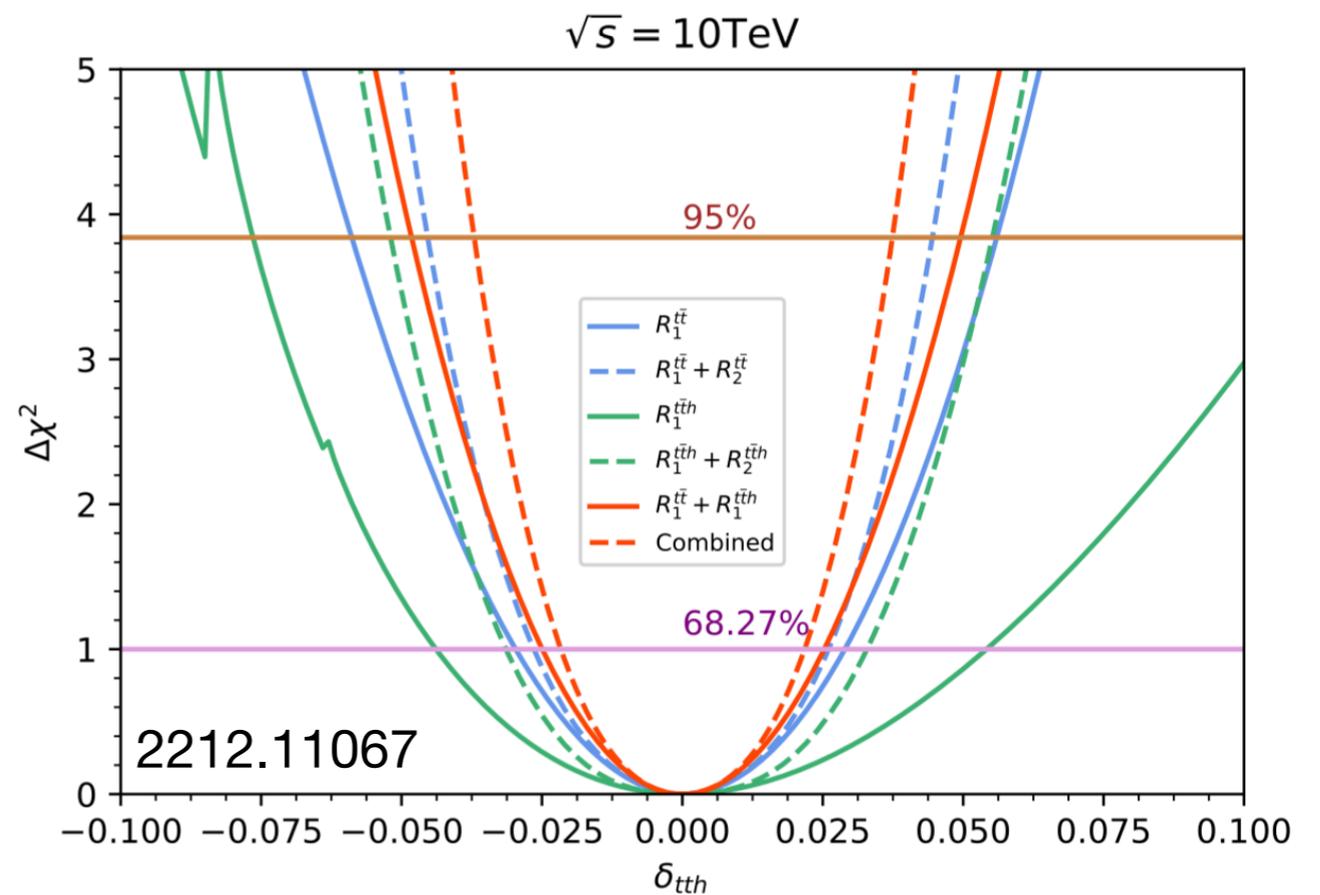
precision limited ( $\sim 3\%$ ) due to backgrounds: not possible to determine  $\kappa_W$  precisely through WW scattering  
 → correlation width vs. coupling

# Top quark Yukawa



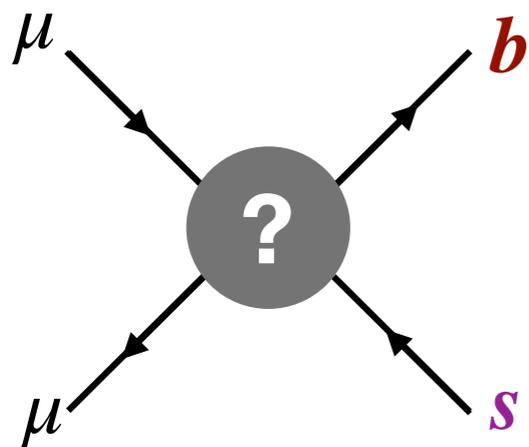
threshold scan @ FCC

tth @ muon collider



(a)  $\mu^+ \mu^- \rightarrow t\bar{t}\nu\bar{\nu}$  with  $\sqrt{s} = 10 \text{ TeV}$   
and  $L = 10 \text{ ab}^{-1}$ .

# Quark flavor violation



**Four-fermion interactions:** muon current coupled to flavor-violating bilinear

$$\frac{c_{bs}}{\Lambda^2} (\bar{b}_{L,R} \gamma^\rho s_{L,R}) (\bar{\mu}_{L,R} \gamma_\rho \mu_{L,R})$$

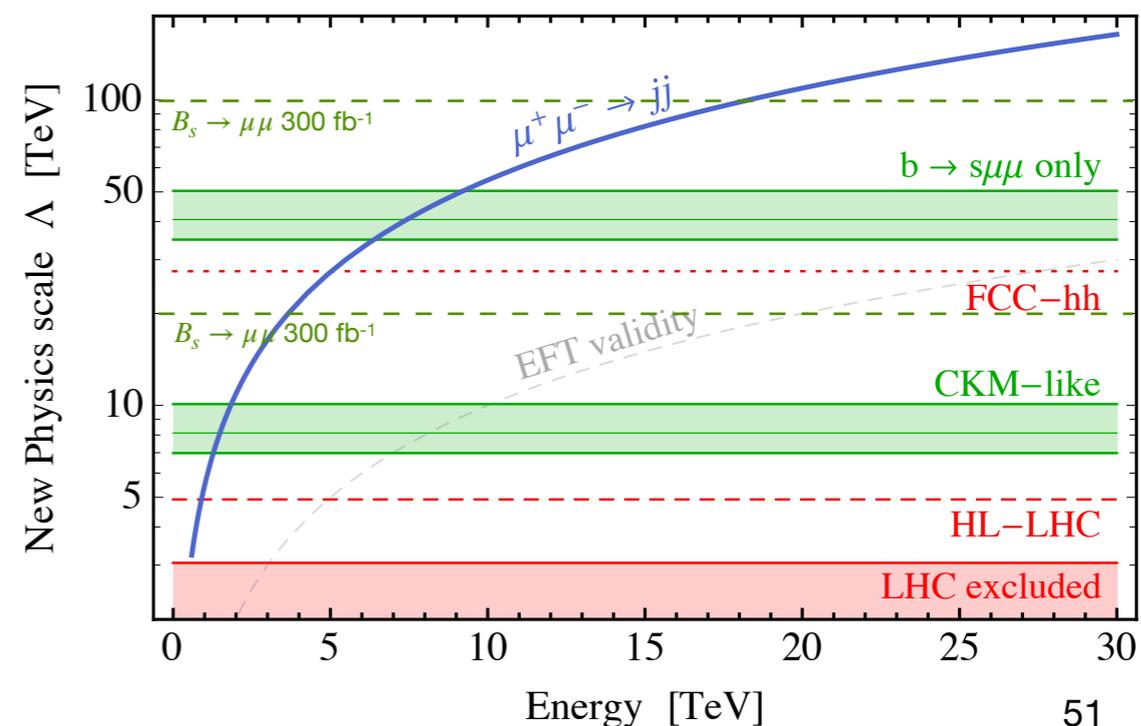
- ◆ Contributes to (semi-)leptonic rare B decays  $b \rightarrow s \mu \mu$ : branching ratios & angular observables of various hadronic processes

$$B_s \rightarrow \mu\mu, \quad B \rightarrow K^{(*)} \mu\mu, \quad B_s \rightarrow \phi \mu\mu, \quad \Lambda_b \rightarrow \Lambda \mu\mu$$

- ◆ Theory uncertainties: cannot improve indefinitely with rare decays

$$\text{BR}(B \rightarrow K \mu\mu) \sim \frac{m_W^4}{\Lambda^4}, \quad \sigma(\mu\bar{\mu} \rightarrow jj) \sim \frac{E^2}{\Lambda^4}$$

Azatov, Garosi, Greljo, Marzocca,  
Salko, Trifinopoulos 2205.13552



# Muon g-2 @ muon collider

- ◆ If new physics is light enough (i.e. weakly coupled), a Muon Collider can directly produce the new particles ➡ direct searches: model-dependent

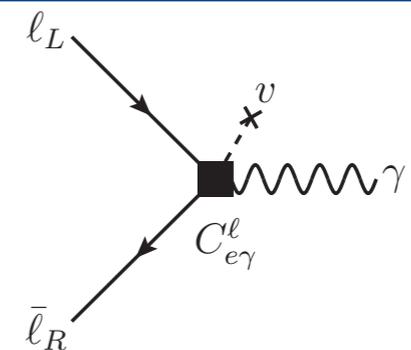
Capdevilla et al. 2006.16277

- ◆ If new physics is heavy: EFT!

One dim. 6 operator contributes at tree-level:  $\mathcal{L}_{g-2} = \frac{C_{e\gamma}}{\Lambda^2} H (\bar{\ell}_L \sigma_{\mu\nu} e_R) e F^{\mu\nu} + \text{h.c.}$

At low energy

$$\Delta a_\mu = \frac{4m_\mu v}{\Lambda^2} C_{e\gamma} \approx 3 \times 10^{-9} \times \left( \frac{140 \text{ TeV}}{\Lambda} \right)^2 C_{e\gamma}$$



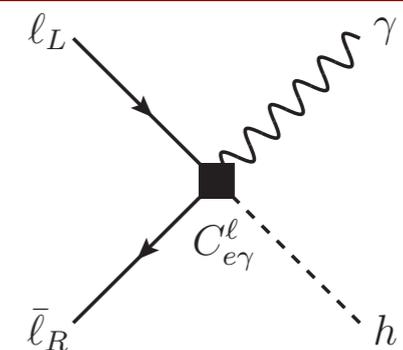
Dipole operator generates both  $\Delta a_\mu$  and  $\mu\mu \rightarrow h\gamma$

B, Paradisi 2012.02769

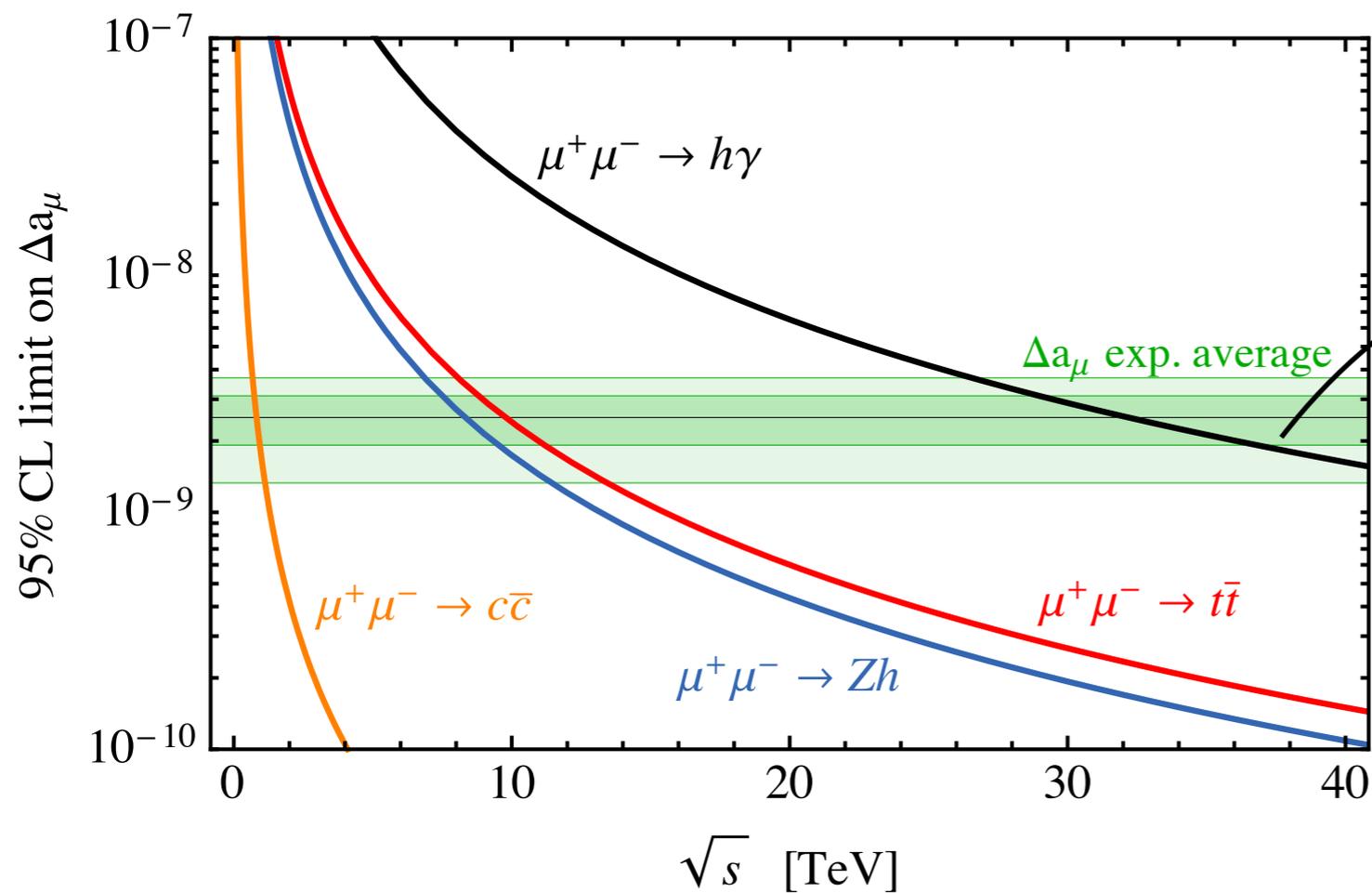
At high energy

$$\sigma_{\mu^+\mu^- \rightarrow h\gamma} = \frac{s}{48\pi} \frac{|C_{e\gamma}|^2}{\Lambda^4} \approx 0.7 \text{ ab} \left( \frac{\sqrt{s}}{30 \text{ TeV}} \right)^2 \left( \frac{\Delta a_\mu}{3 \times 10^{-9}} \right)^2$$

$$N_{h\gamma} = \sigma \cdot \mathcal{L} \approx \left( \frac{\sqrt{s}}{10 \text{ TeV}} \right)^4 \left( \frac{\Delta a_\mu}{3 \times 10^{-9}} \right)^2 \quad \text{need } E > 10 \text{ TeV}$$



# Muon g-2 @ muon collider



Exp. value of  $\Delta a_\mu$  can be tested at 95% CL at a 30 TeV collider!  
(with reasonable assumptions on detector performance)

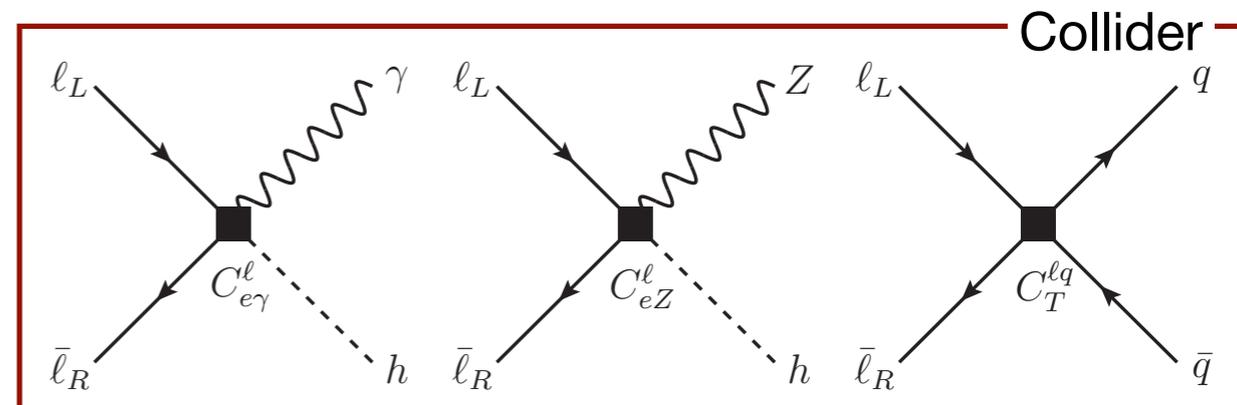
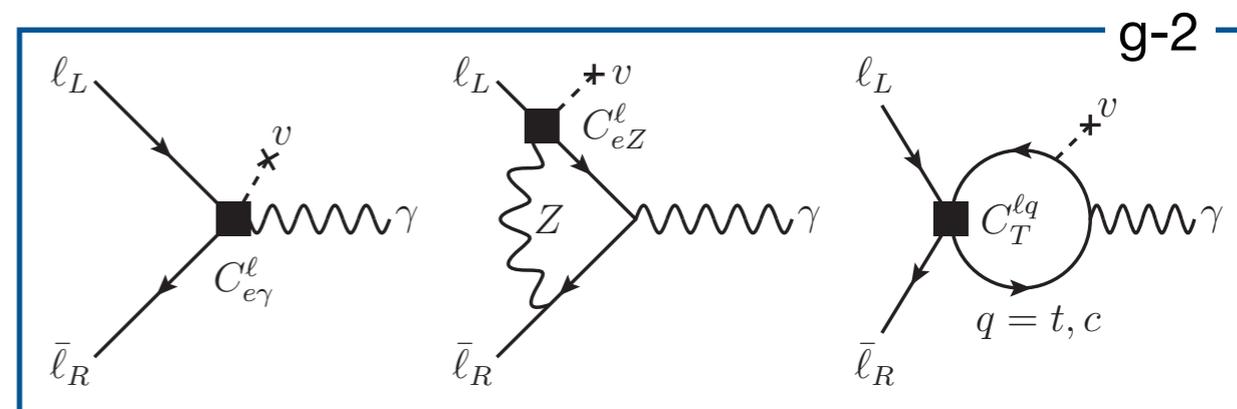
**This result is completely model-independent!**

B, Paradisi 2012.02769

- ◆ Other operators enter g-2 at 1 loop:

$$\Delta a_\mu \approx \left( \frac{250 \text{ TeV}}{\Lambda^2} \right)^2 \left( C_{e\gamma} - \frac{C_{Tt}}{5} - \frac{C_{Tc}}{1000} - \frac{C_{eZ}}{20} \right)$$

- ◆ Full set of operators with  $\Lambda \gtrsim 100 \text{ TeV}$  can be probed at a high-energy muon collider



# Lepton $g-2$ from rare Higgs decays

- ◆ Tau magnetic dipole moment: enhanced due to the larger mass

$$\Delta a_\tau = \frac{4v m_\tau}{\Lambda^2} C_{e\gamma}^\tau \approx \Delta a_\mu \frac{m_\tau^2}{m_\mu^2} \approx 10^{-6}$$

if  $C_{e\gamma}^\ell$  scales as  $y_\ell$

Present bound:  $\Delta a_\tau \lesssim 10^{-2}$

from LEP  $e^+e^- \rightarrow e^+e^-\tau^+\tau^-$

hep-ex/0406010

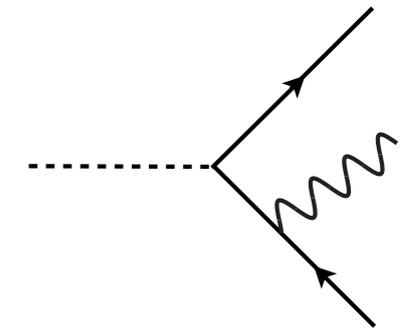
Can be improved to few  $10^{-3}$

at HL-LHC

1908.05180

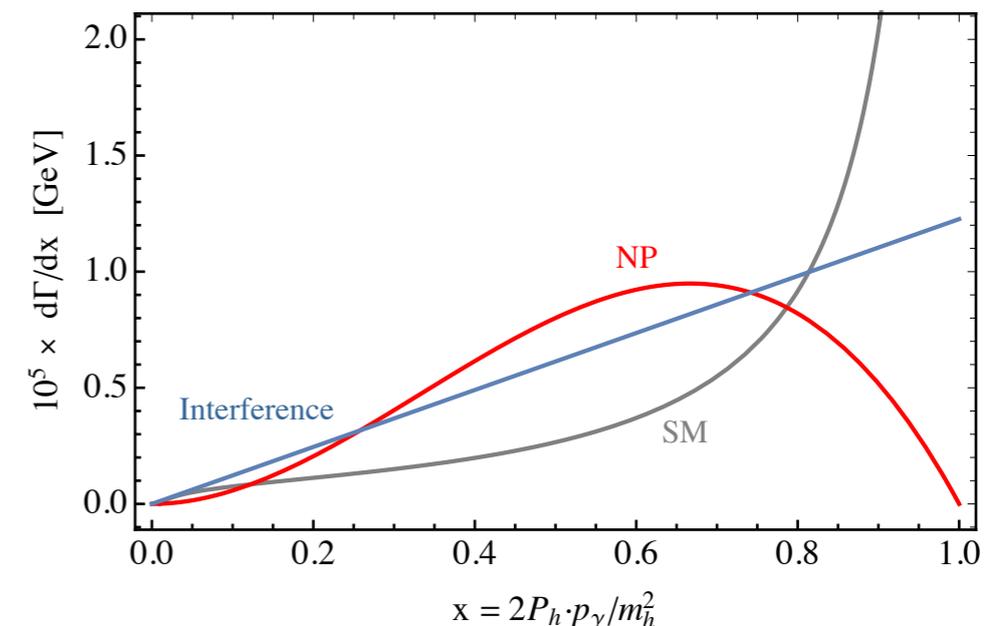
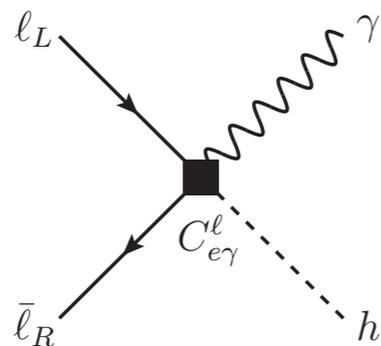
- ◆ Contribution to  $h \rightarrow \tau\tau\gamma$  decays:

$$\text{BR}_{h \rightarrow \tau^+\tau^-\gamma}^{(\text{SM})} \approx 5 \times 10^{-4} \quad (\text{with cut on soft collinear photon})$$



could be measured at few % level by Higgs factory

$$\text{BR}_{h \rightarrow \tau^+\tau^-\gamma}^{(\text{NP})} \approx 0.2 \times \Delta a_\tau$$

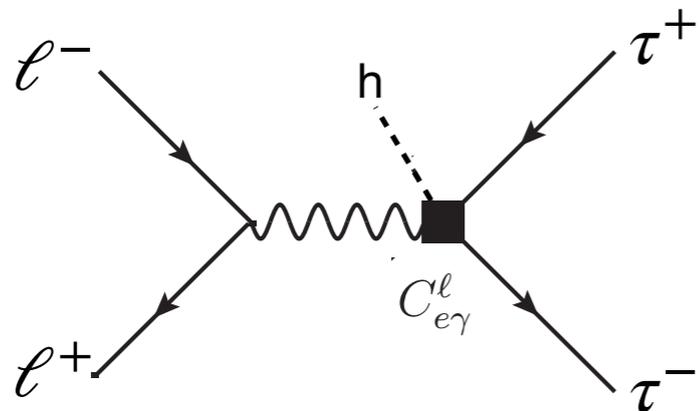


# Tau g-2 from high-energy probes

Further possibilities to measure  $\Delta a_\tau$  precisely from high-energy probes

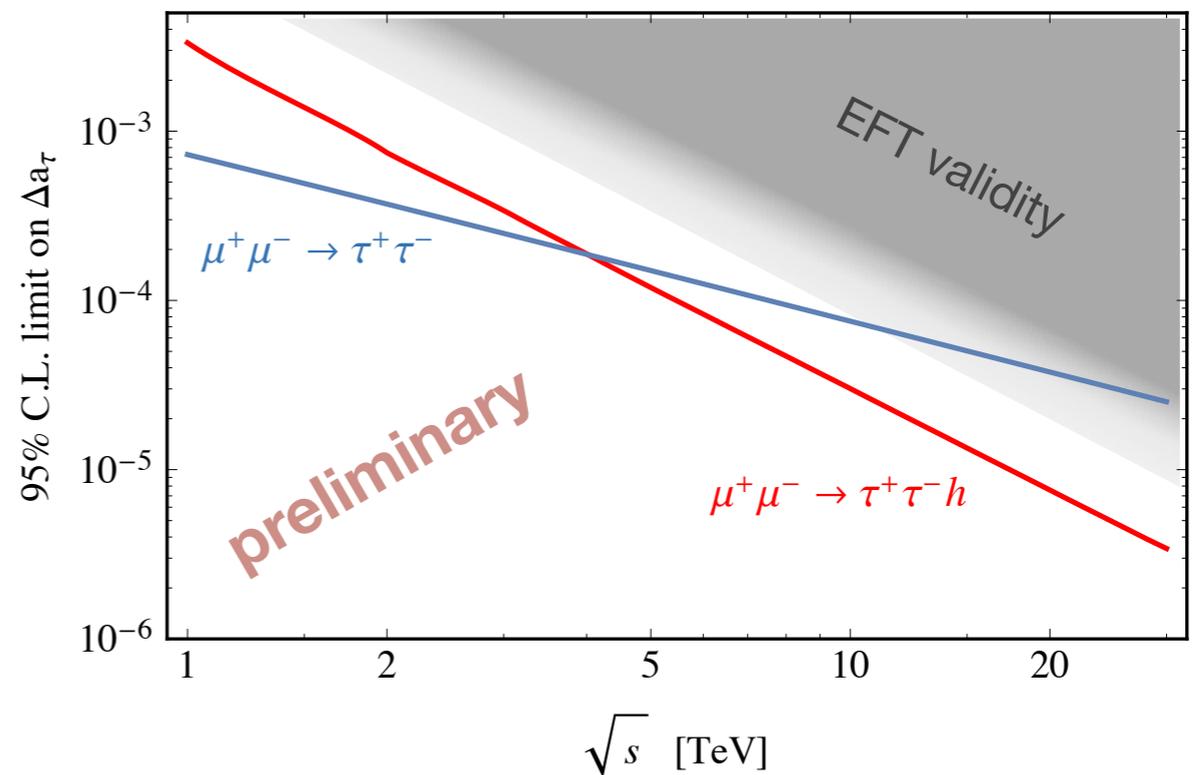
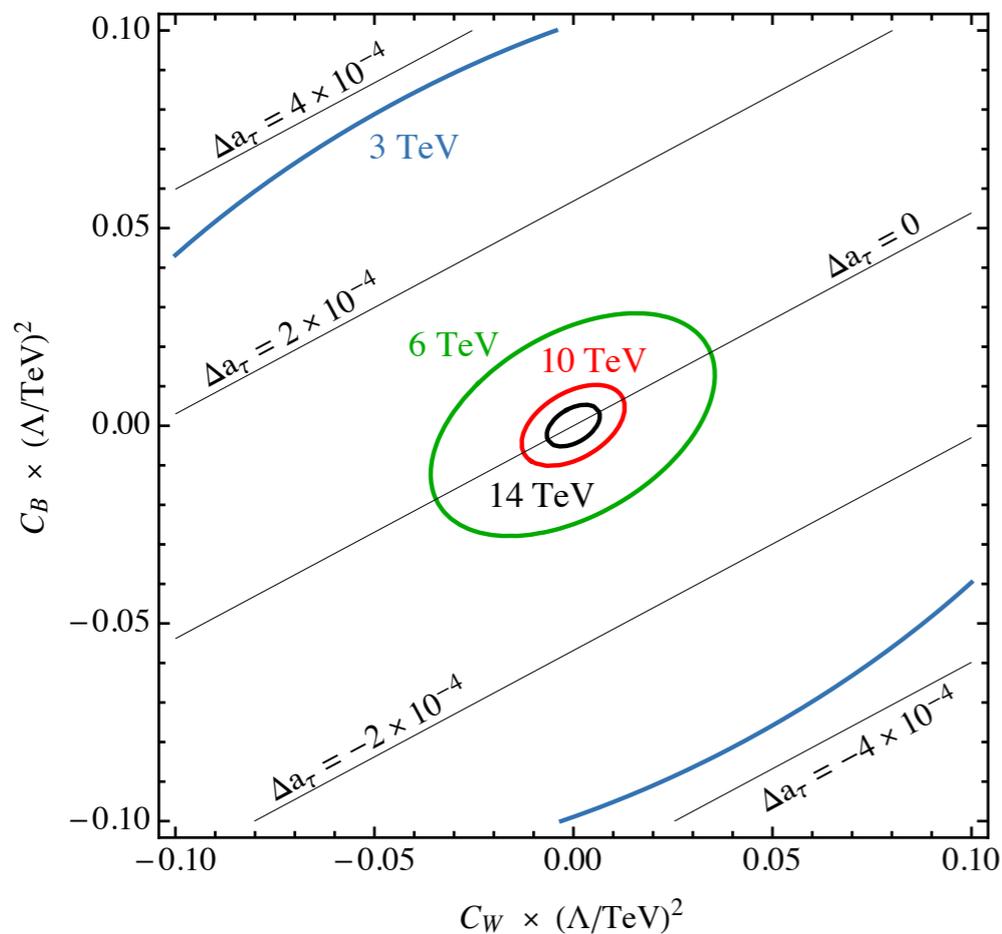
◆  $H\tau\tau$  associated production

work in progress with Levati, Paradisi, Maltoni, Wang



- ▶ Main background from  $\mu\mu \rightarrow Z\gamma$  (where Z is mistaken for H)

Could probe  $\Delta a_\tau \sim 10^{-5}$  @ 10 TeV



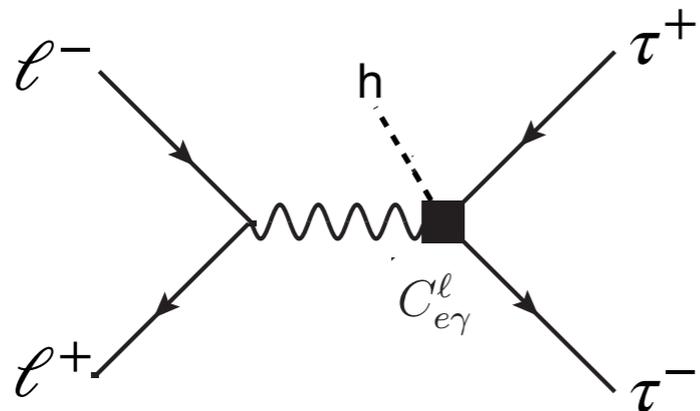
also a bound on tau EDM!

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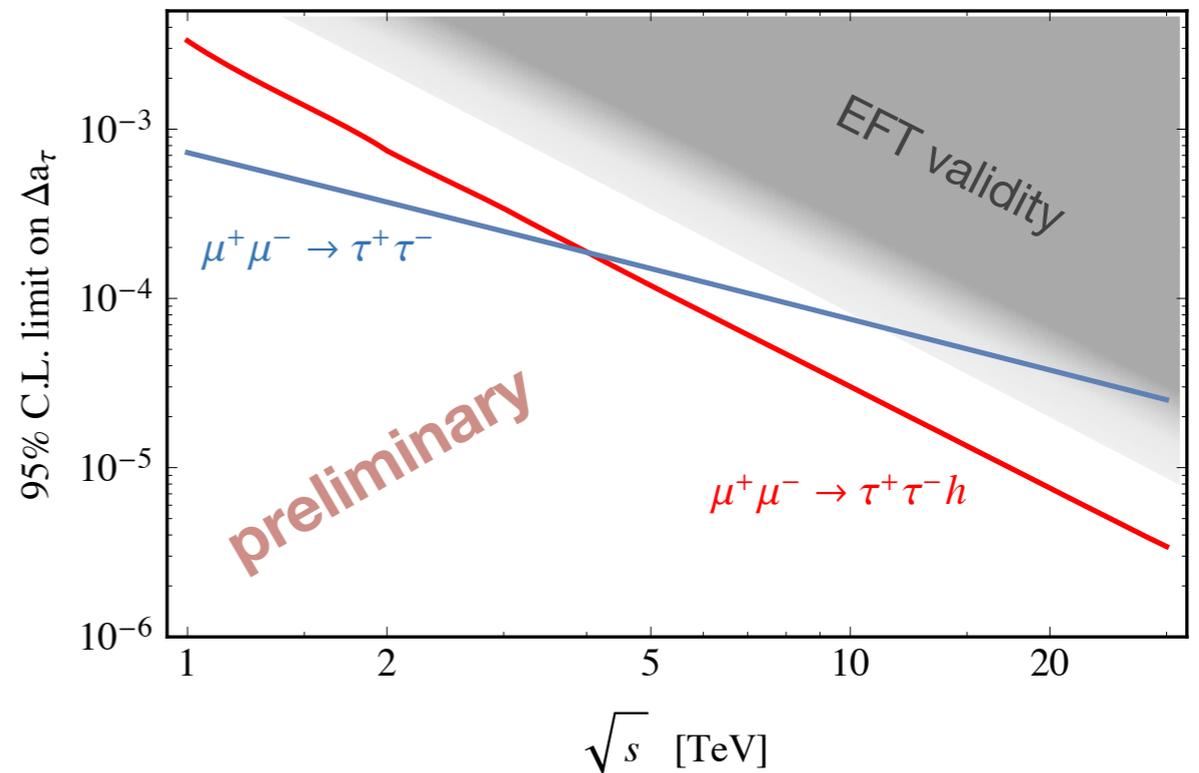
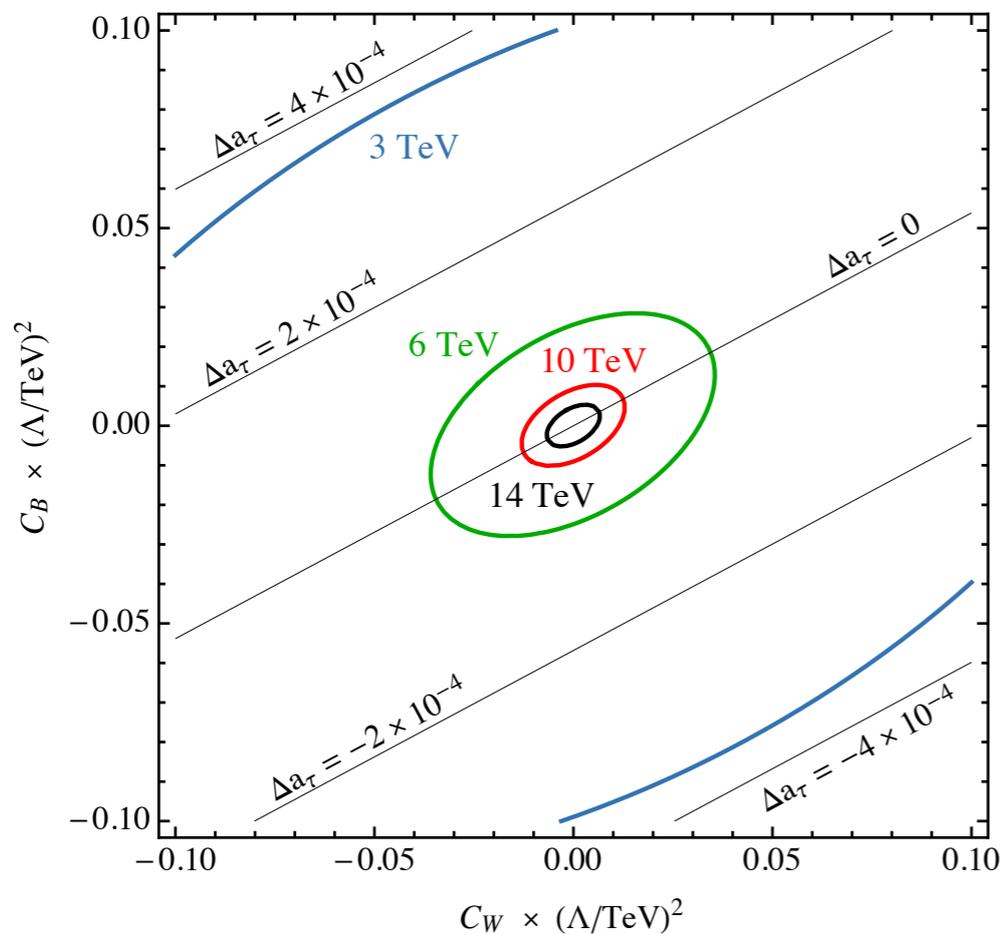
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