

OPTIMAL ANTI-FERROMAGNETS FOR LIGHT DARK MATTER DETECTION

Angelo Esposito



SAPIENZA
UNIVERSITÀ DI ROMA

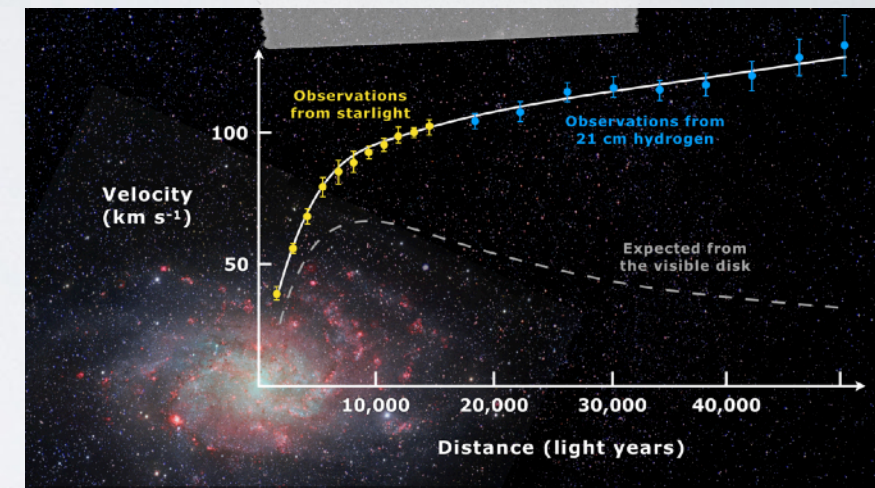
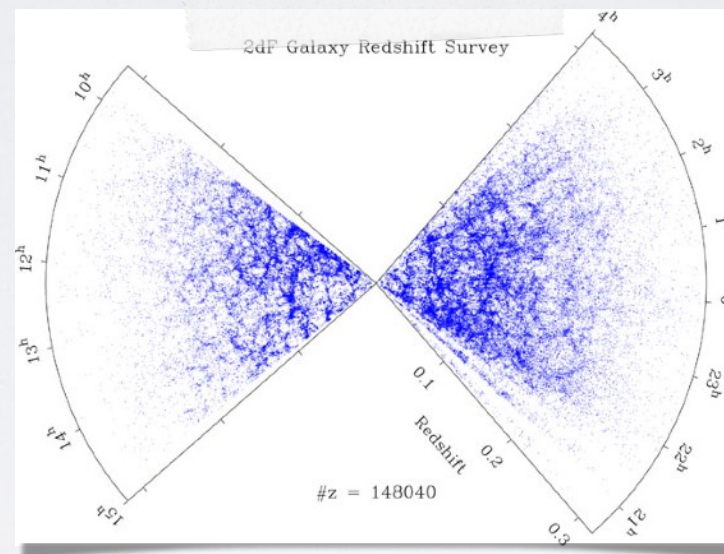
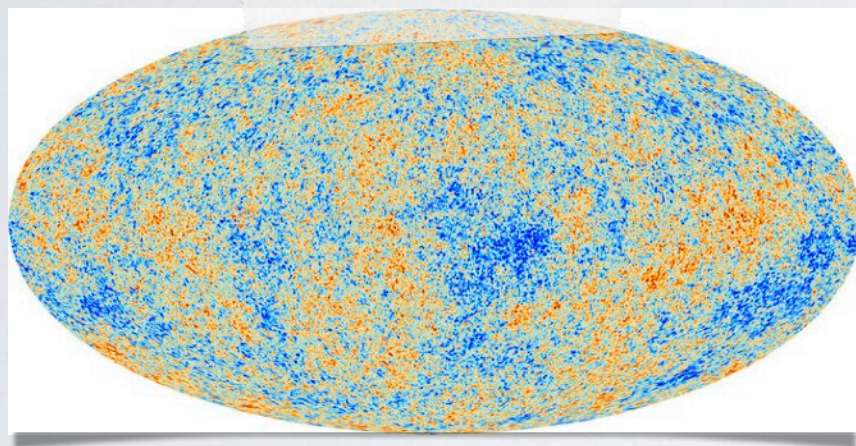


IDM, L'Aquila, July 2024

SUB-MEV DARK MATTER

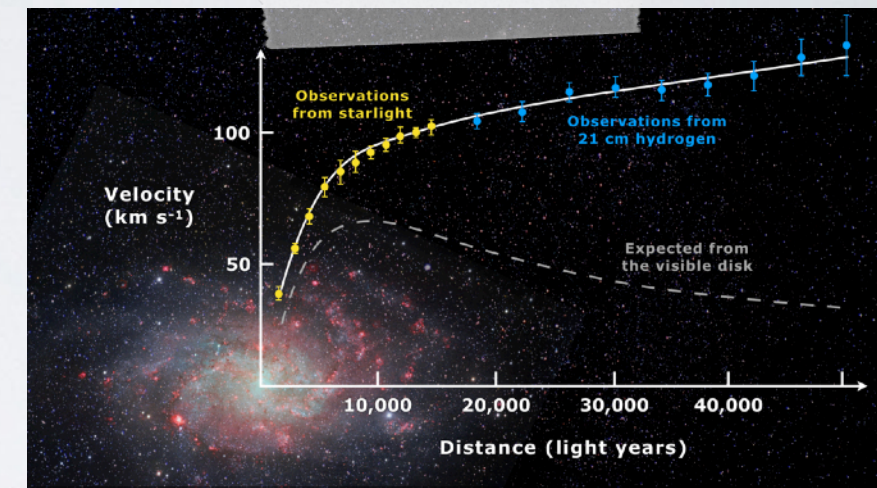
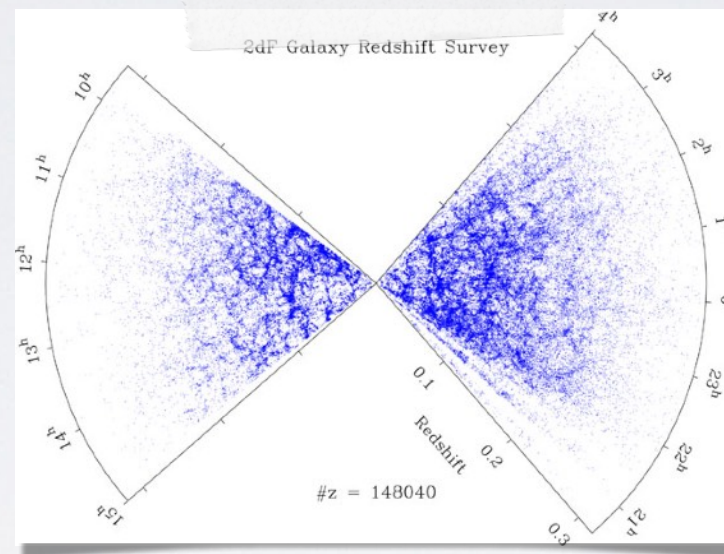
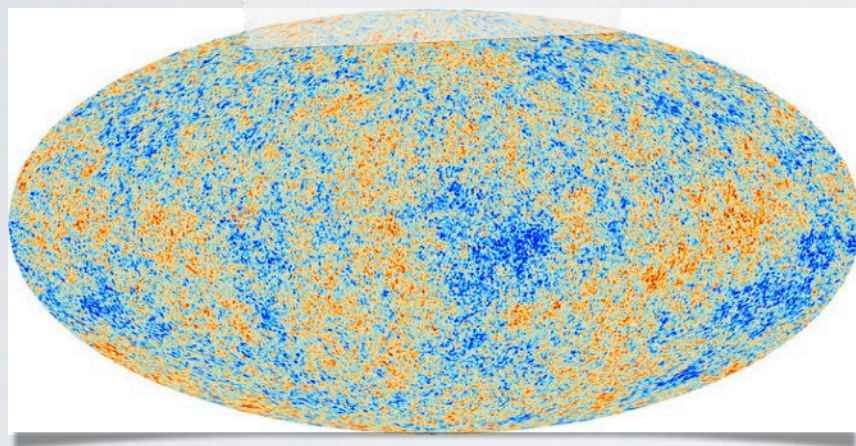
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- Most of the matter that interacts gravitationally is dark



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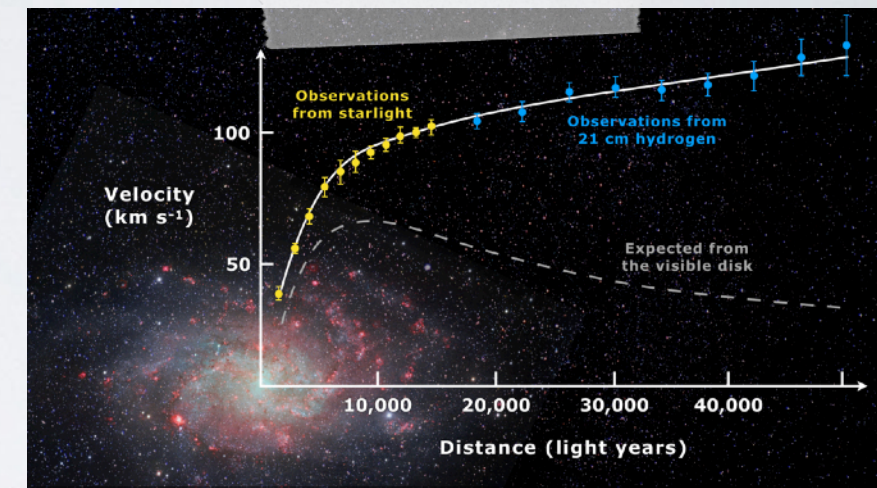
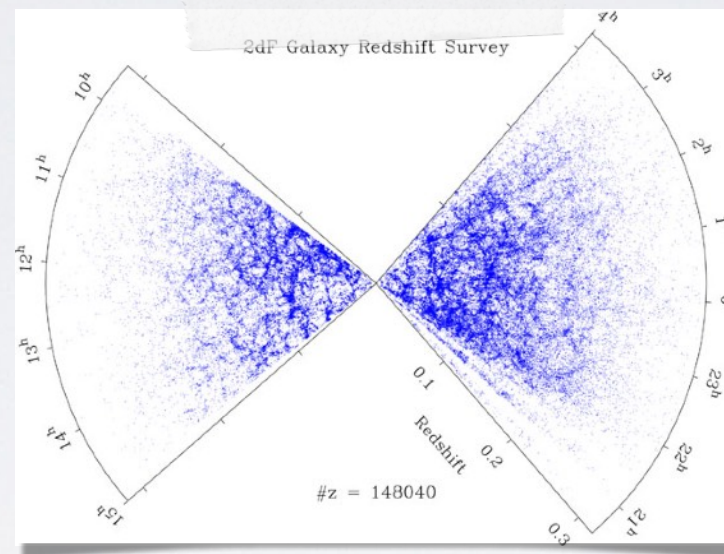
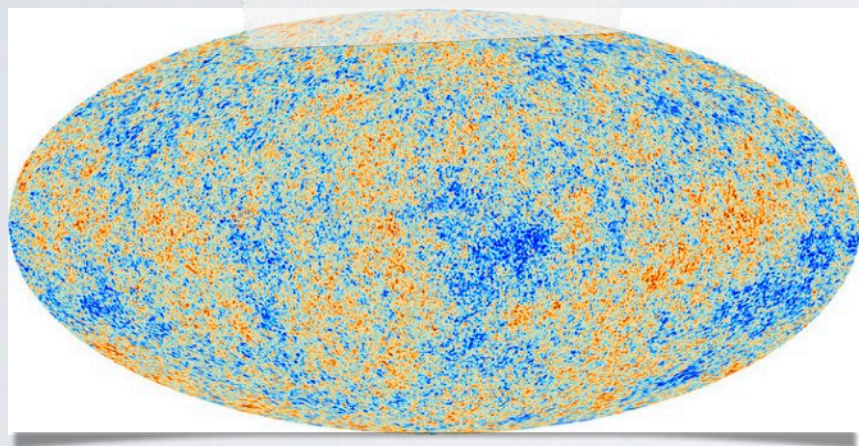
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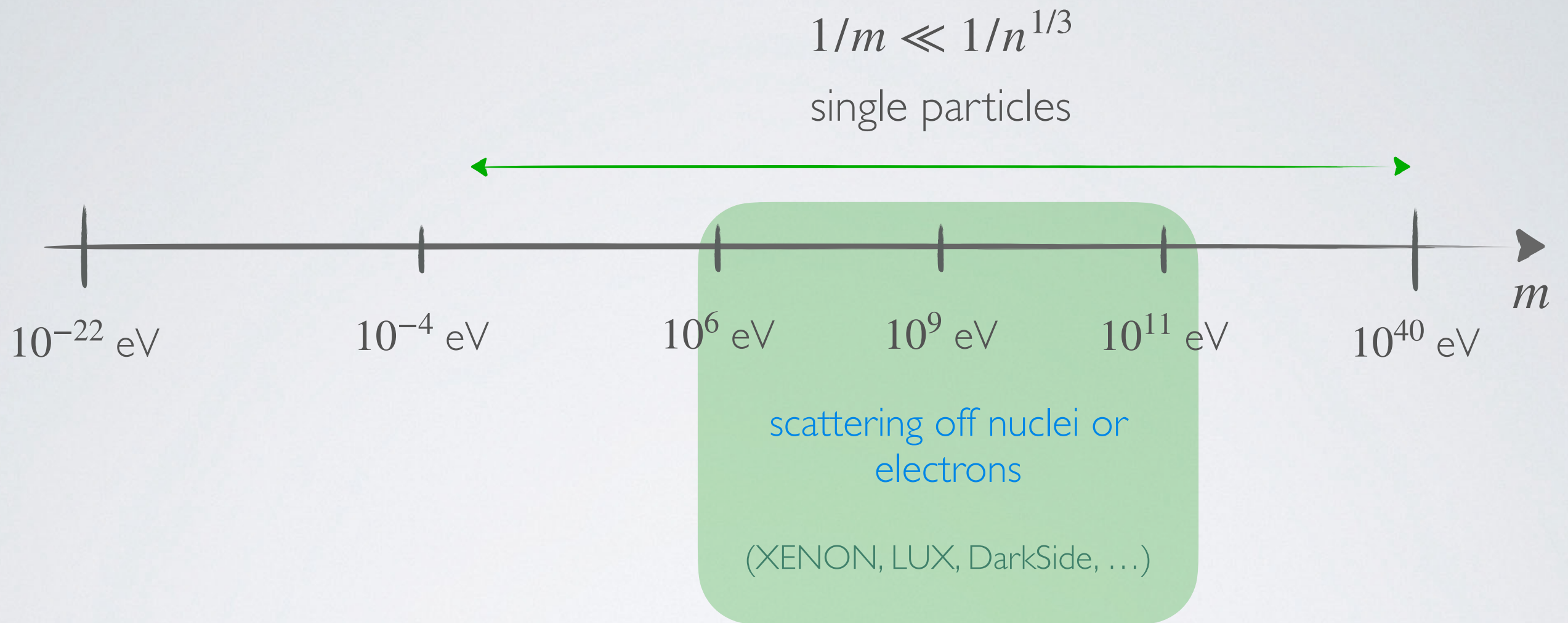
- One of the strongest evidences for physics beyond the Standard Model
- However... huge possible mass range → detection techniques vary widely depending on the dark matter mass

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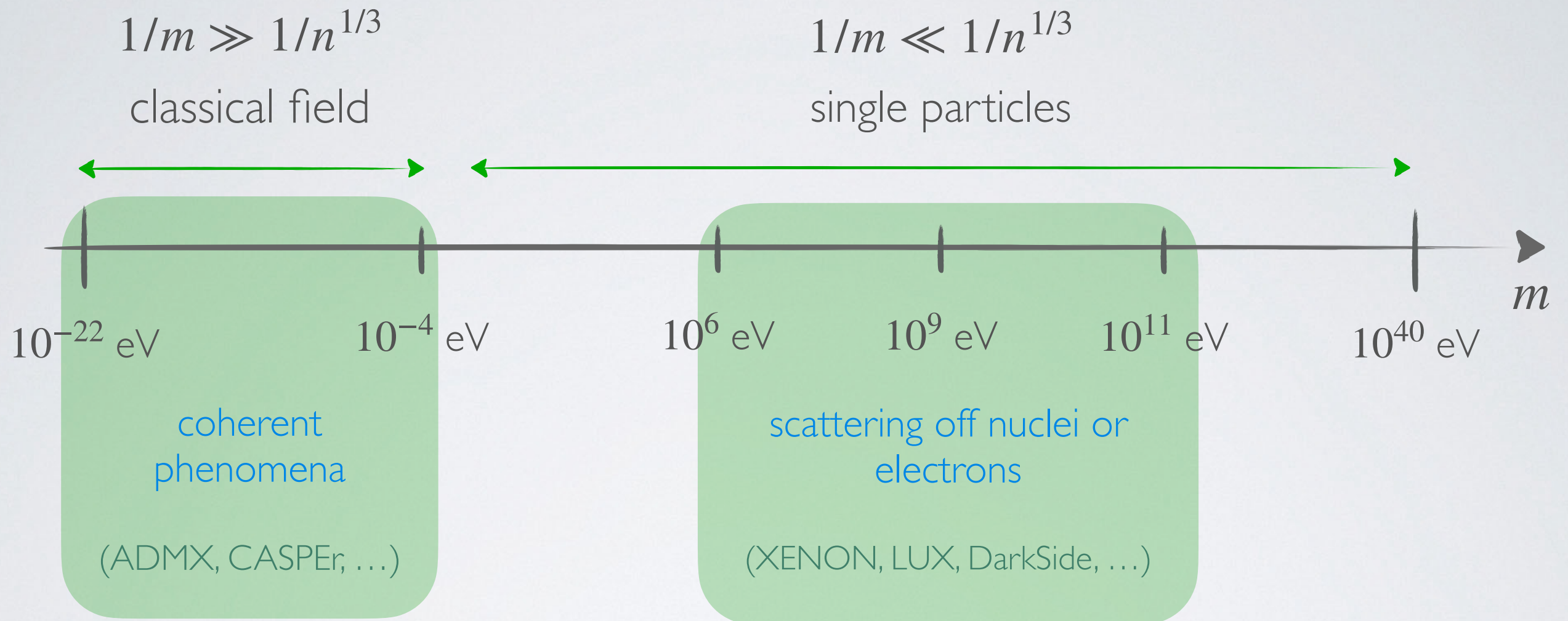
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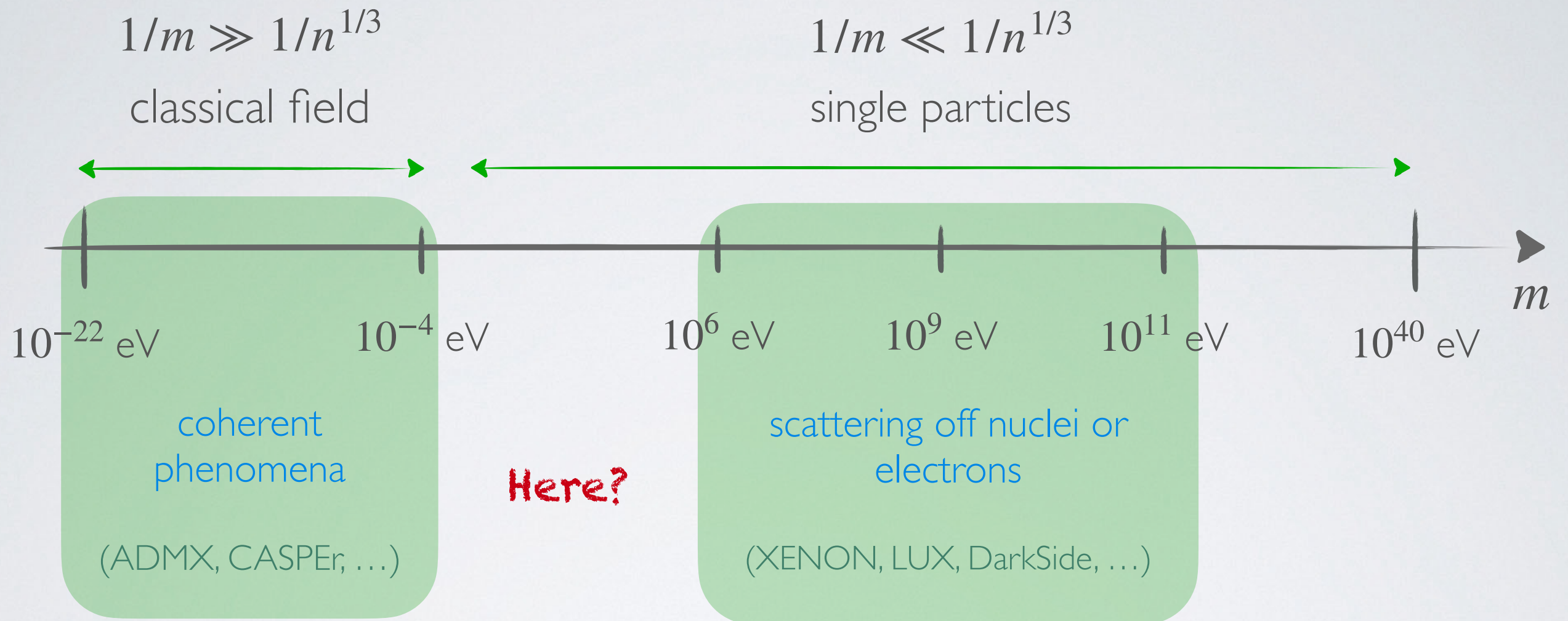
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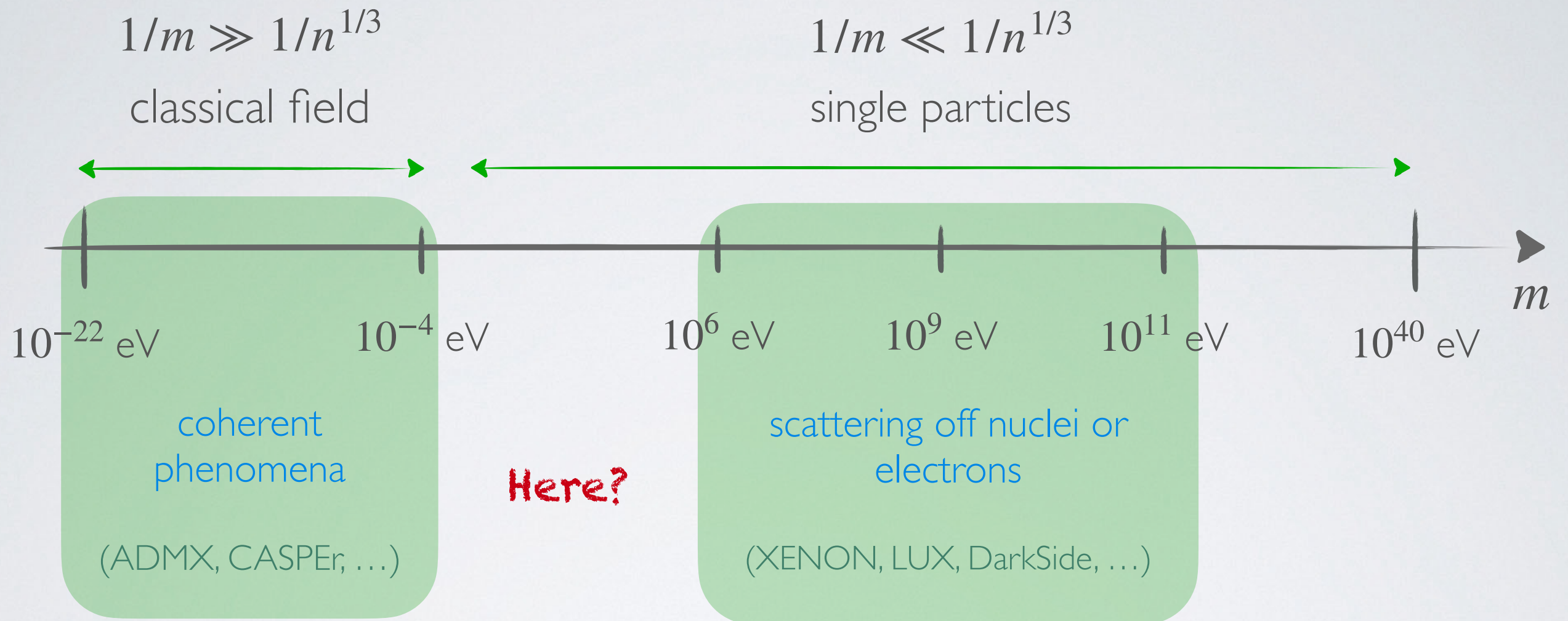
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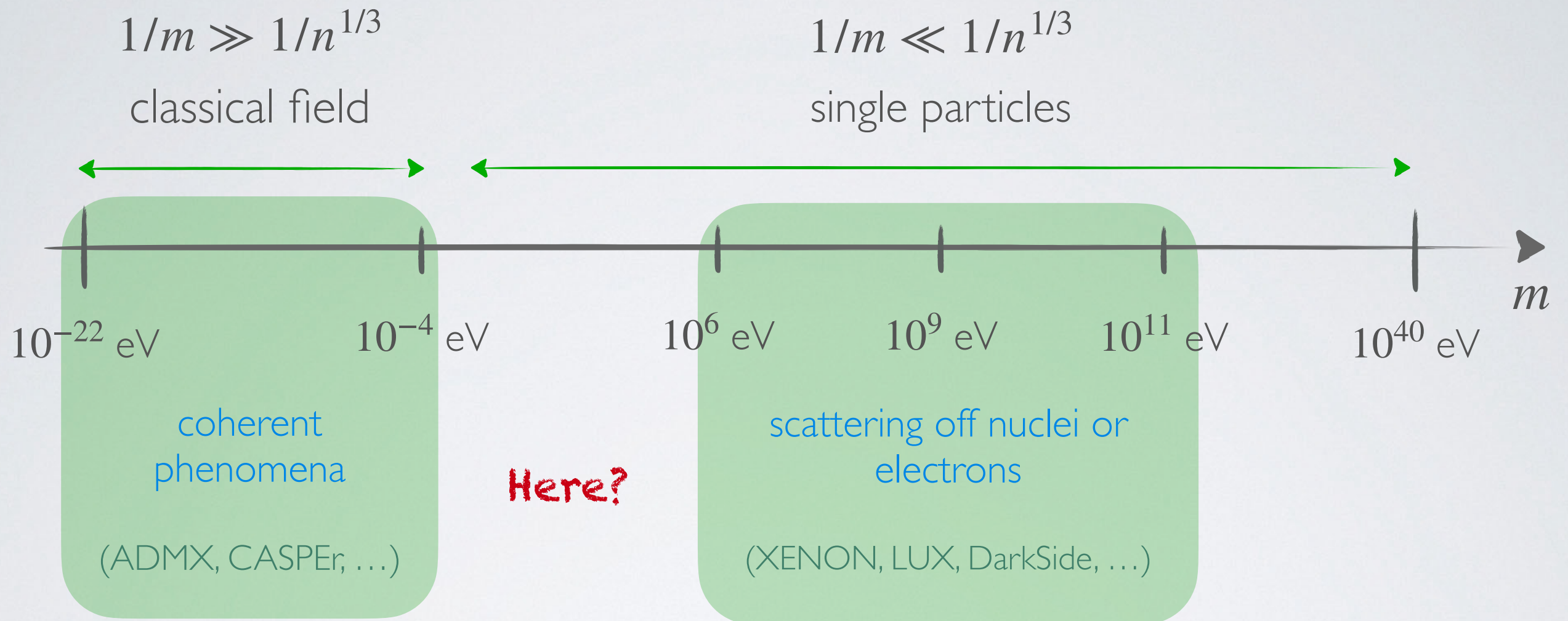


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- Dark matter is a particle but **too light for elastic recoil**
- Need **new materials and/or observables**

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- For an **elastic scattering**, it must be

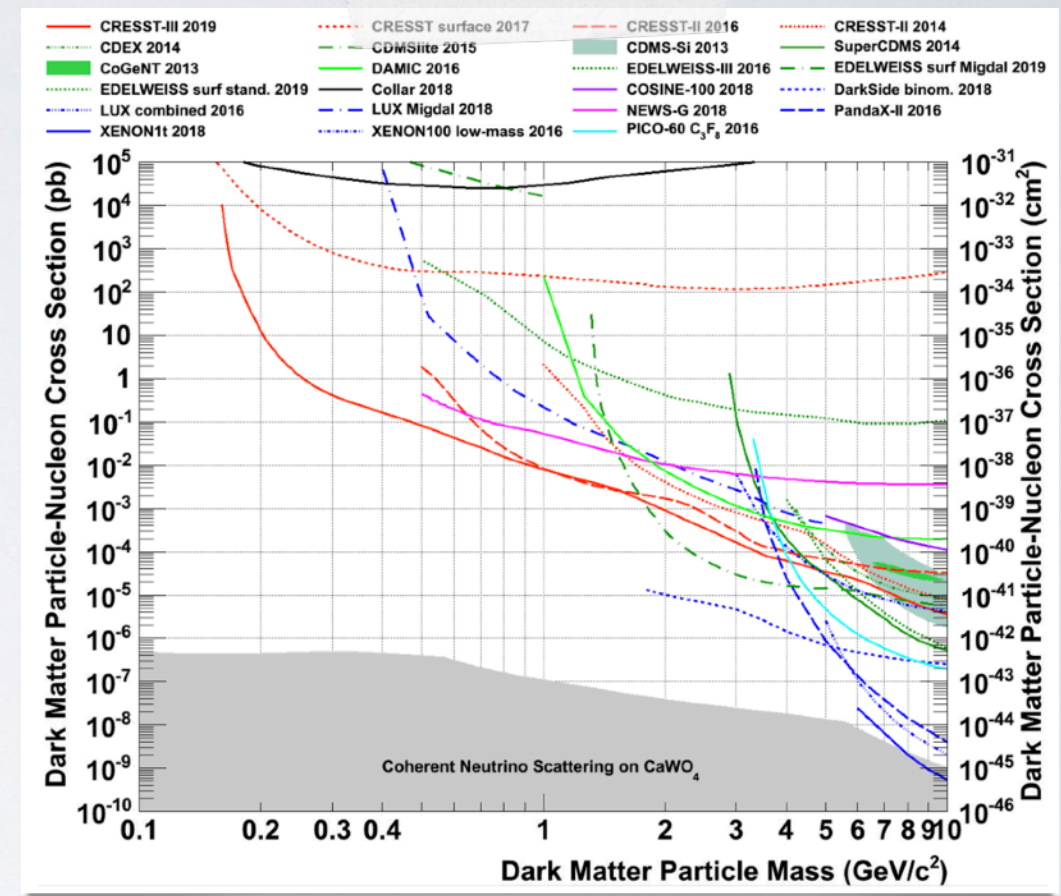
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[CRESST – PRD 2019, 1904.00498]

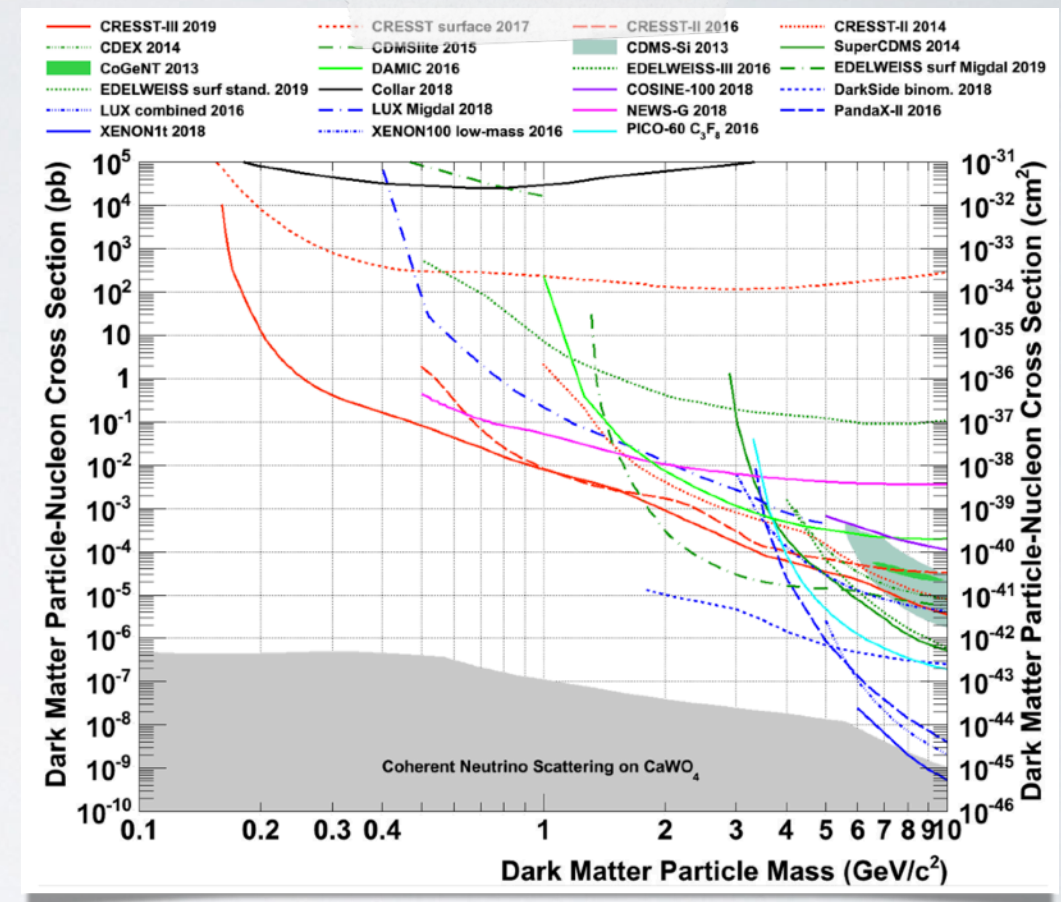
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- To evade this we must look into **inelastic processes**, which relax the kinematics constraints

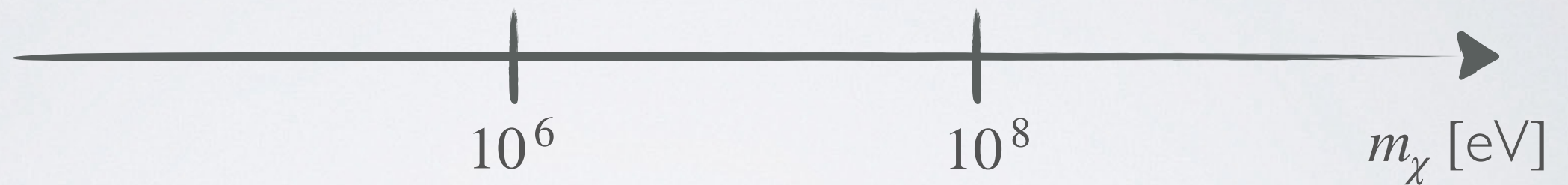


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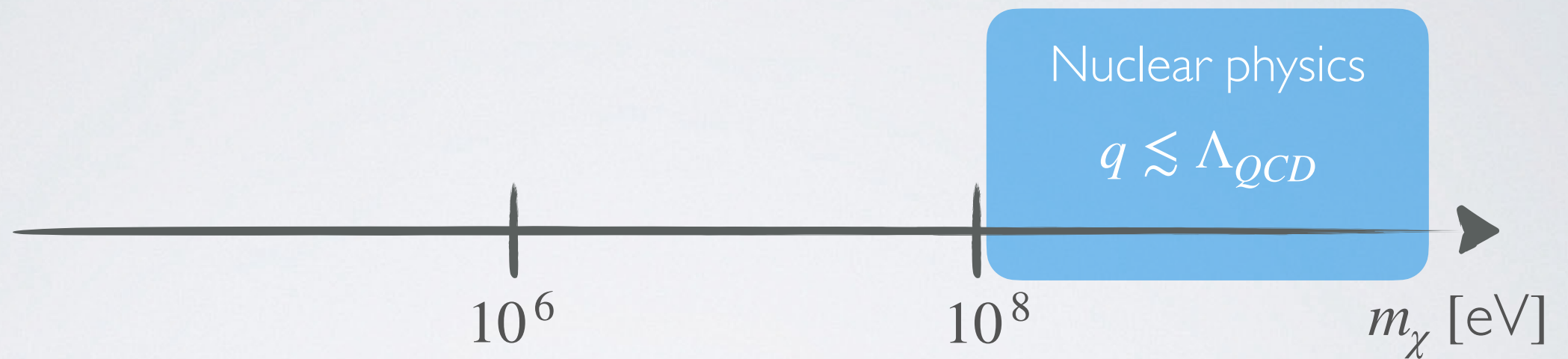
NASTY STUFF

- For light dark matter one needs to delve into the **condensed matter world**



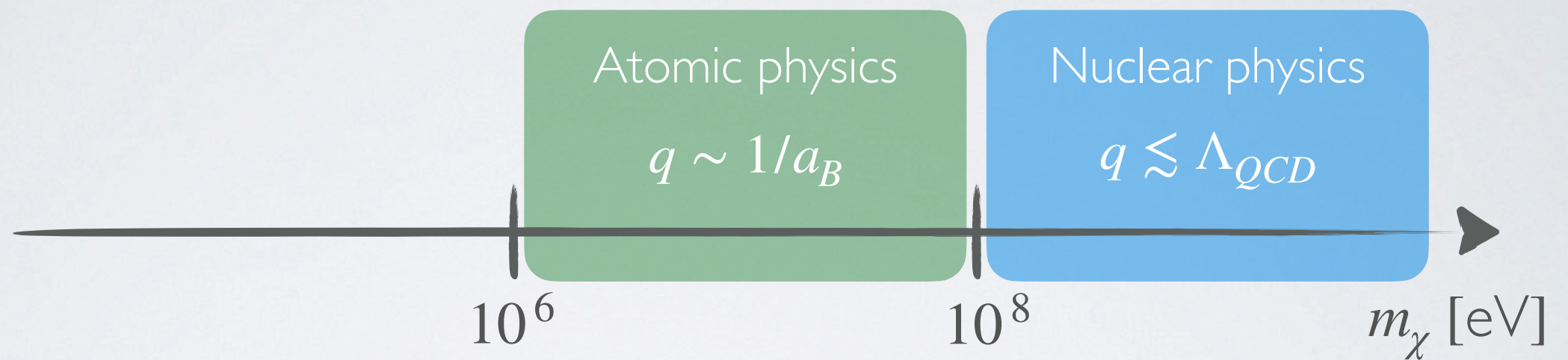
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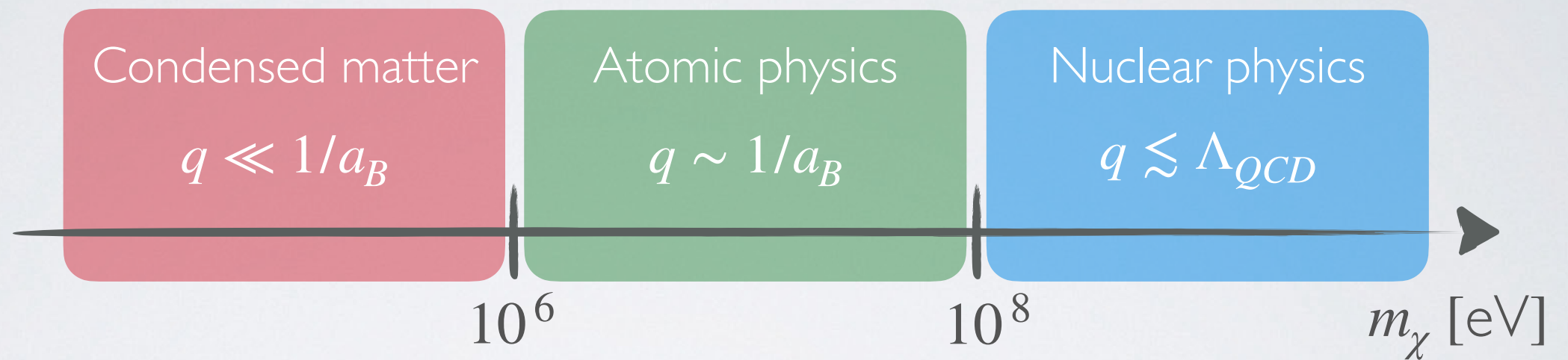
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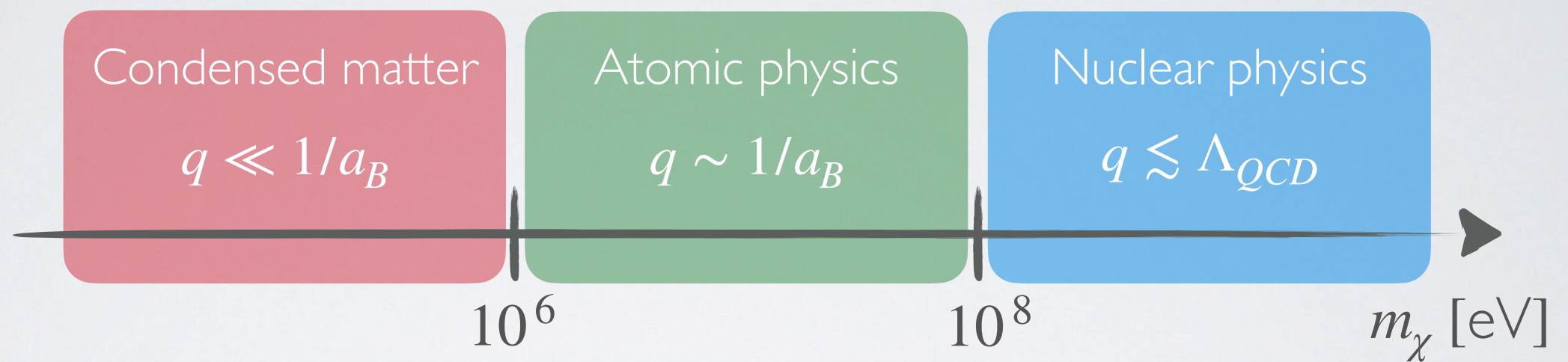
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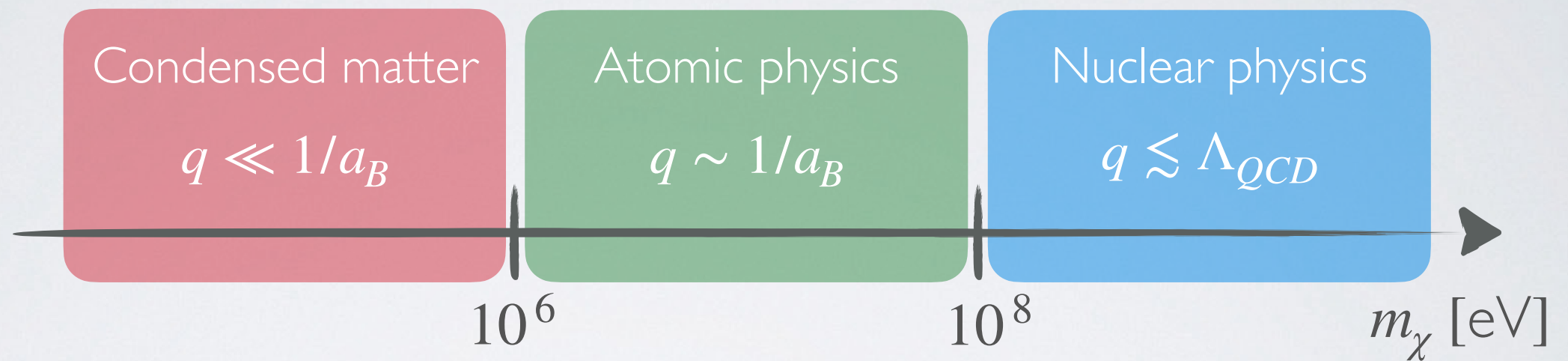
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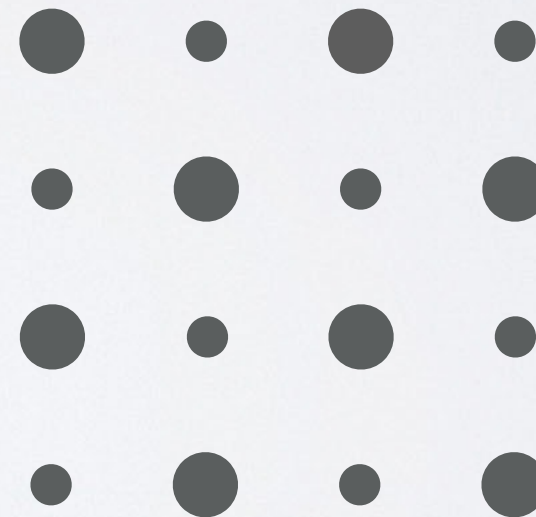
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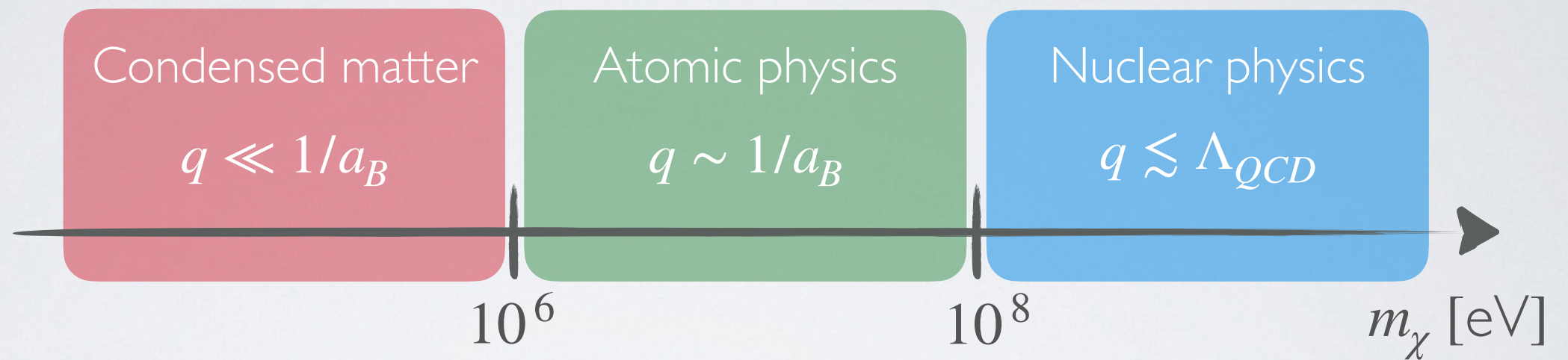


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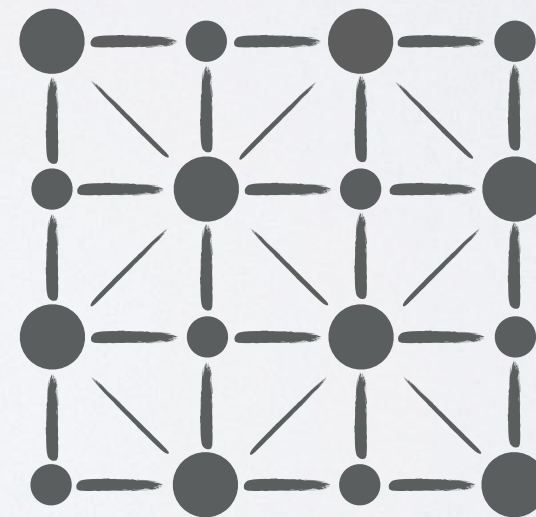


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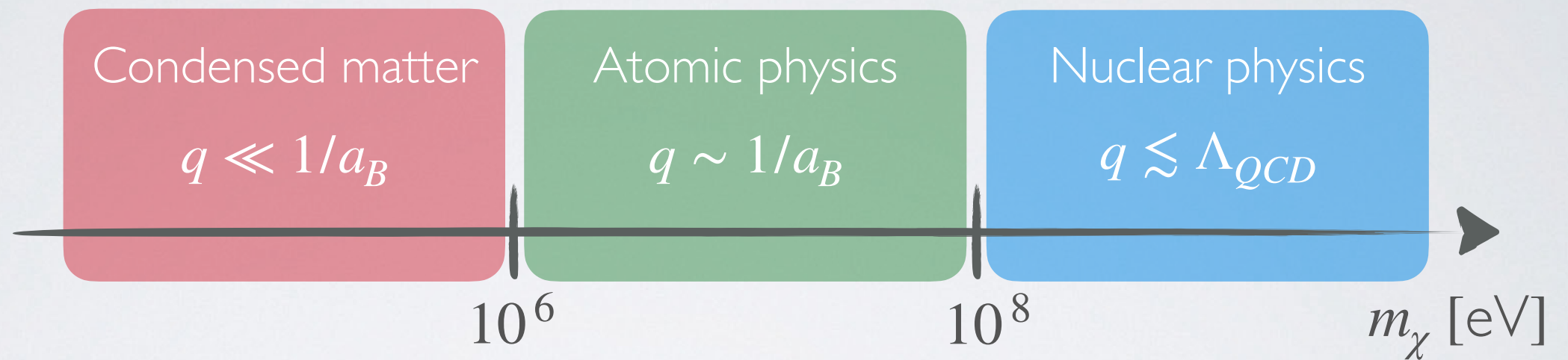


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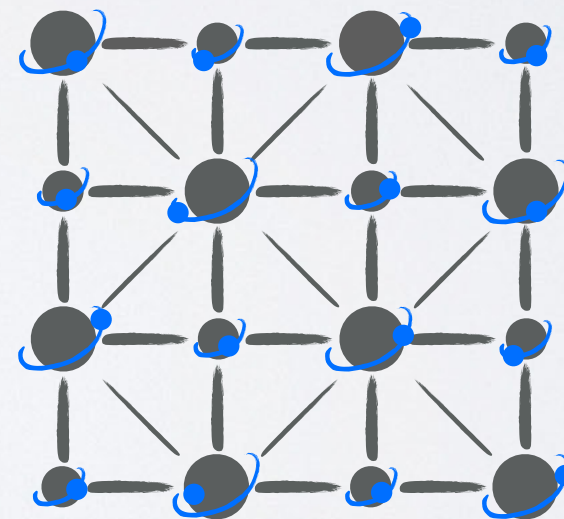


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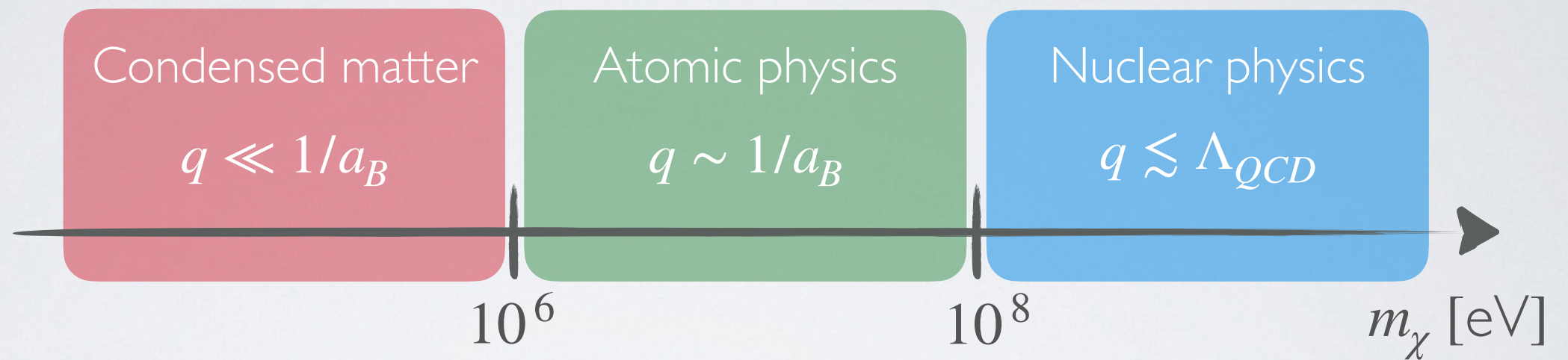


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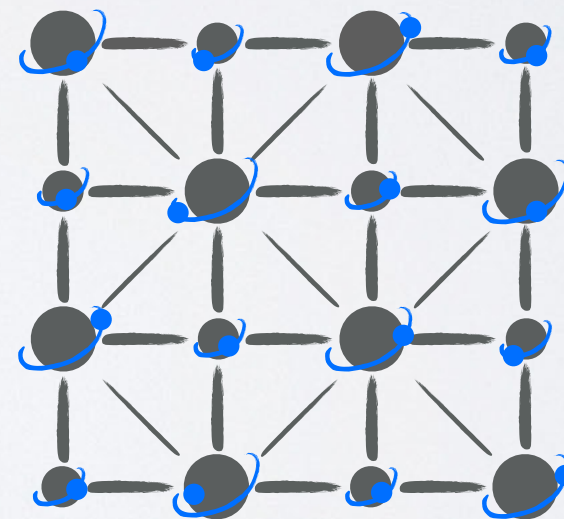


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- Need theoretical tools** that allow to solve or bypass these problems

COLLECTIVE EXCITATIONS

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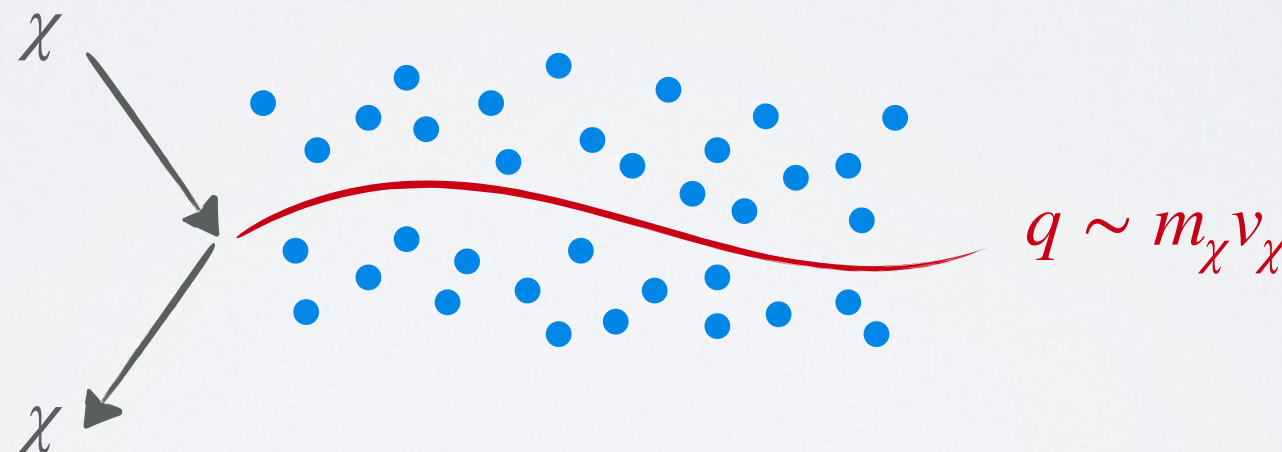
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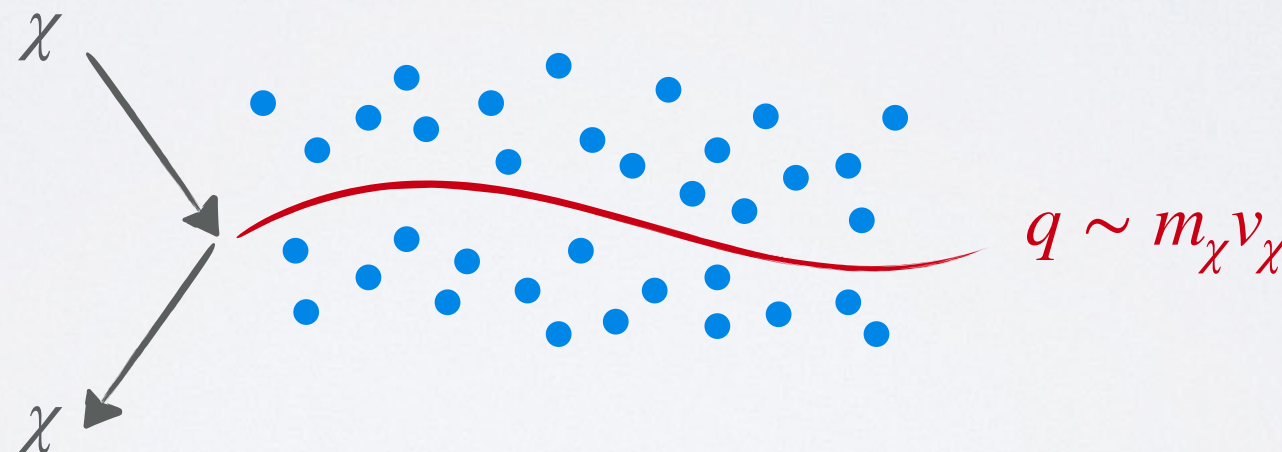


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- Typically, no more single particle final states \rightarrow signatures involve one or more collective excitations

[e.g., Trickle et al. – JHEP 2020, 1910.08092; Griffin et al. – PRD 2020, 1910.10716]

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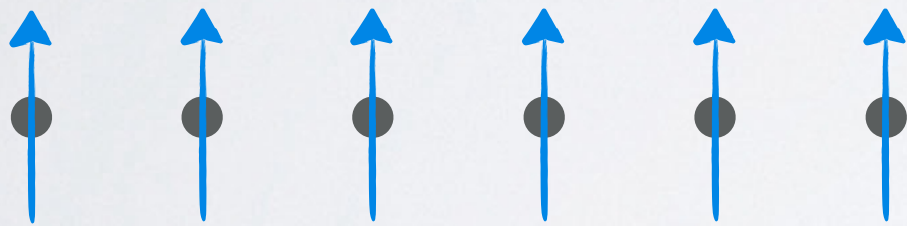
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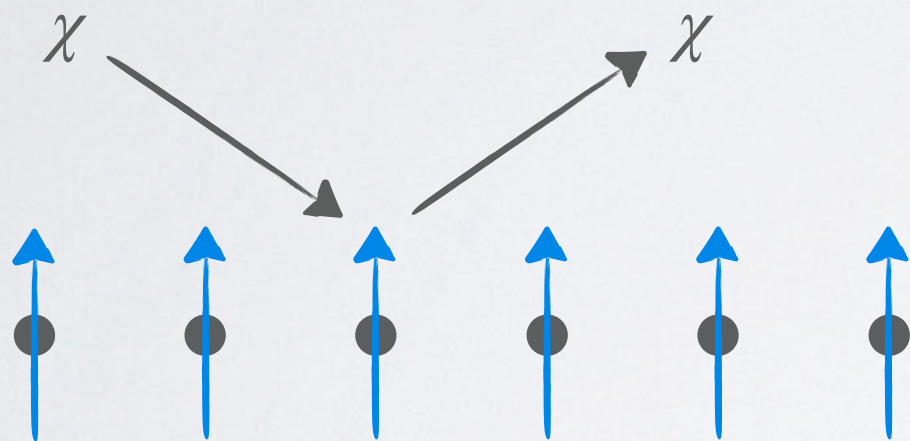
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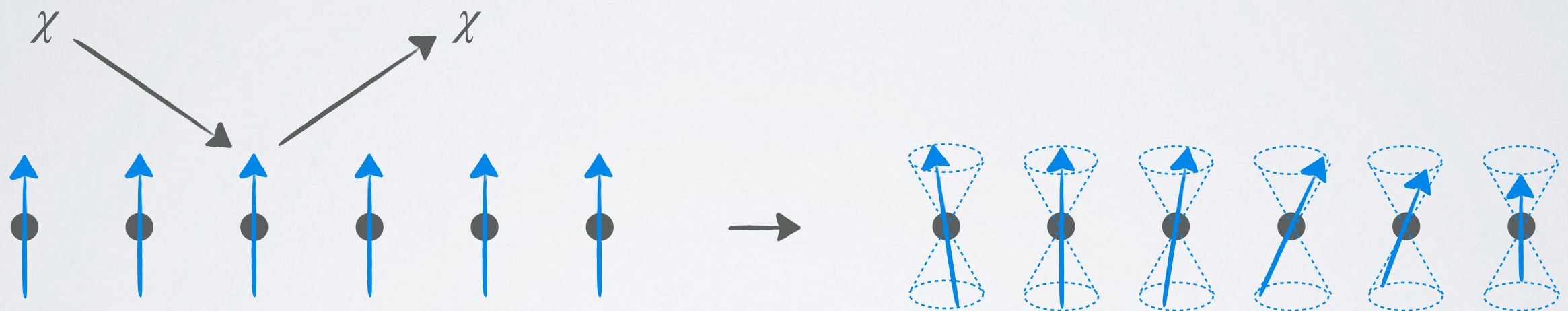
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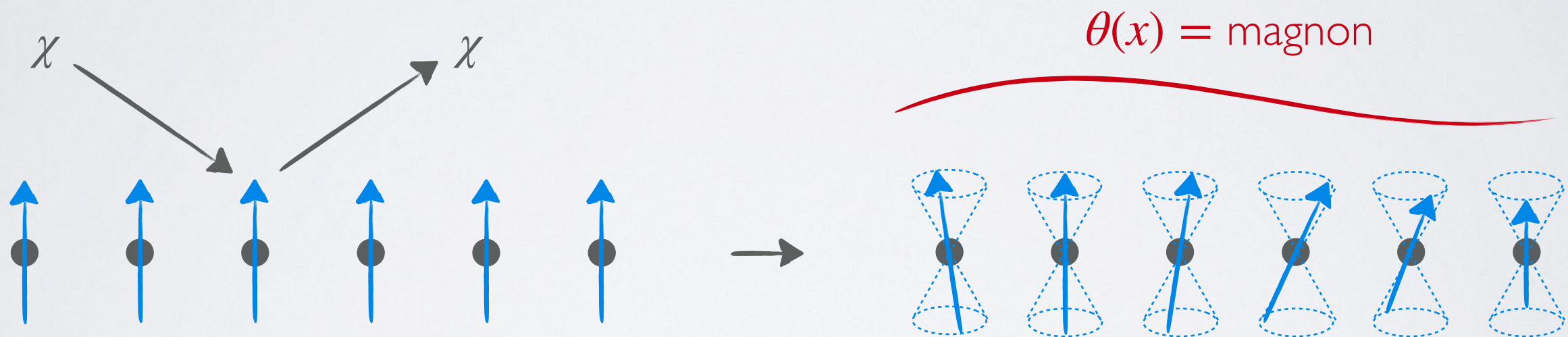
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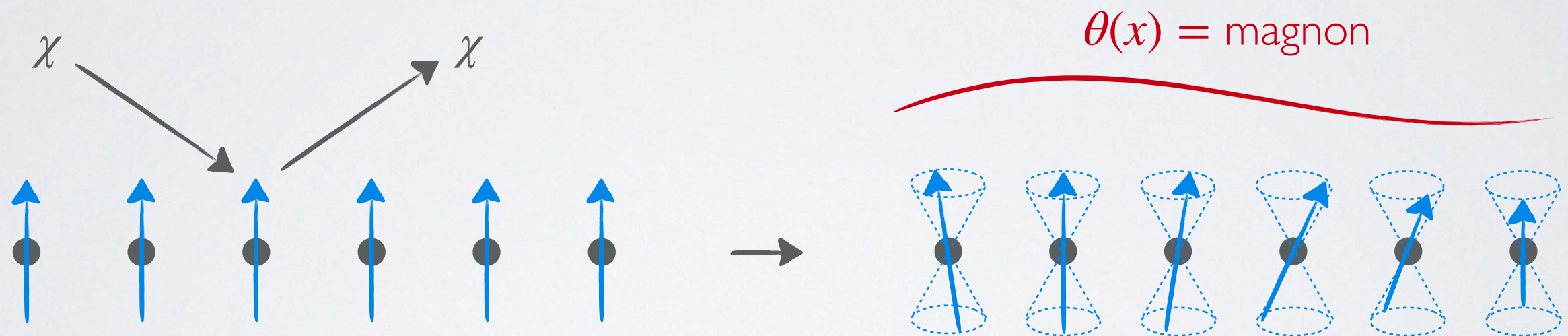
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- Ways to detect few magnons have already been proposed (TES, MKID, quantum sensors)

[Trickle, Zhang, Zurek – PRL 2020, 1905.13744; Lachance-Quirion et al. – Science Advances 2017; Lachance-Quirion et al. – Science 2020]

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spin density



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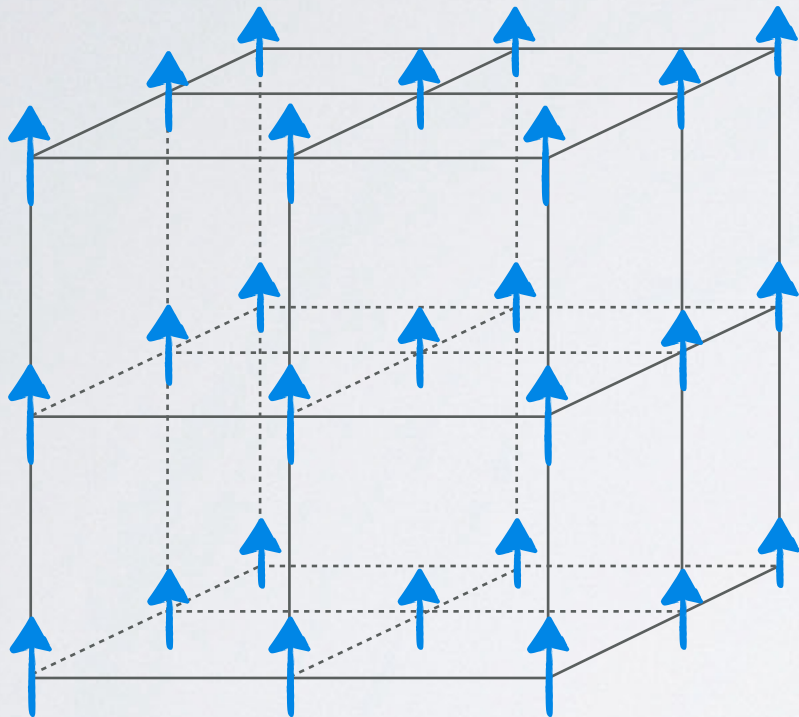
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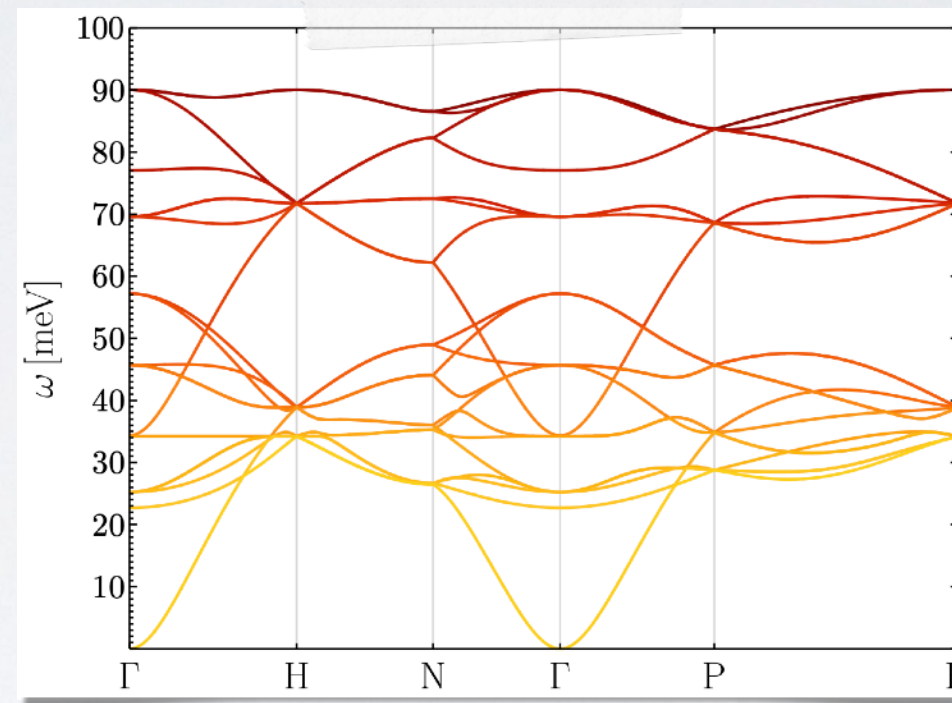
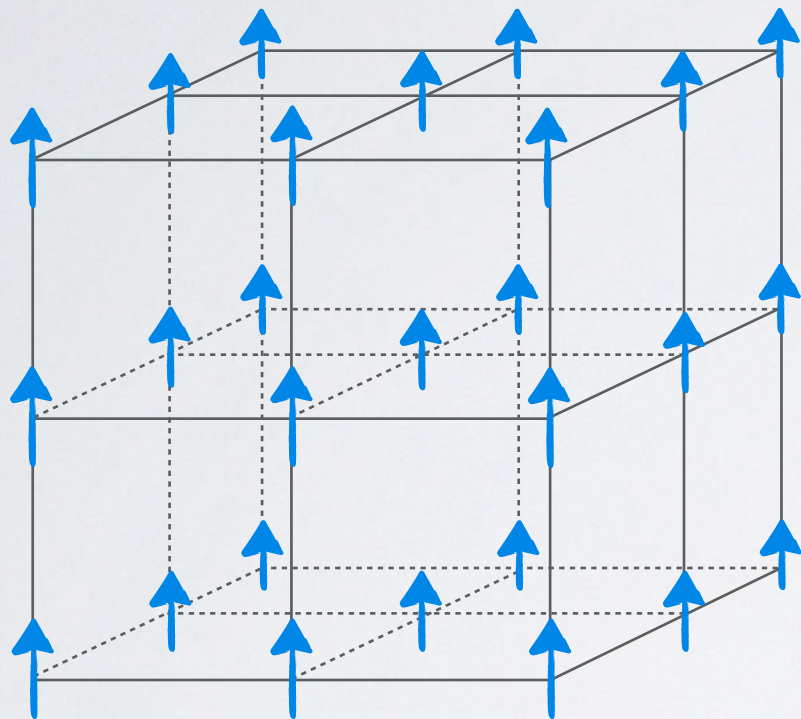
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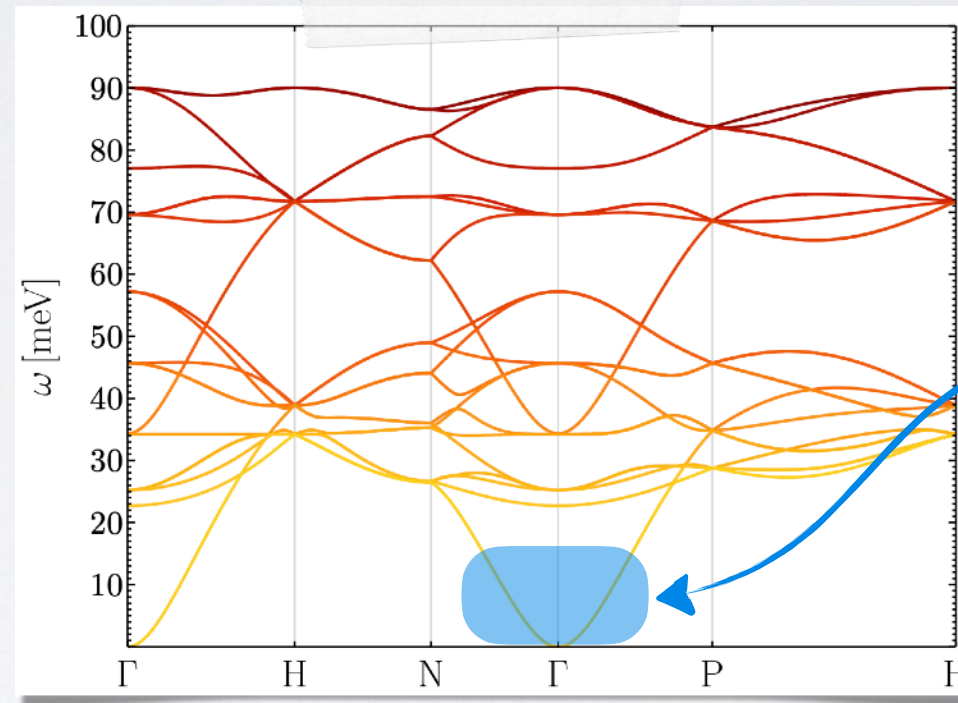
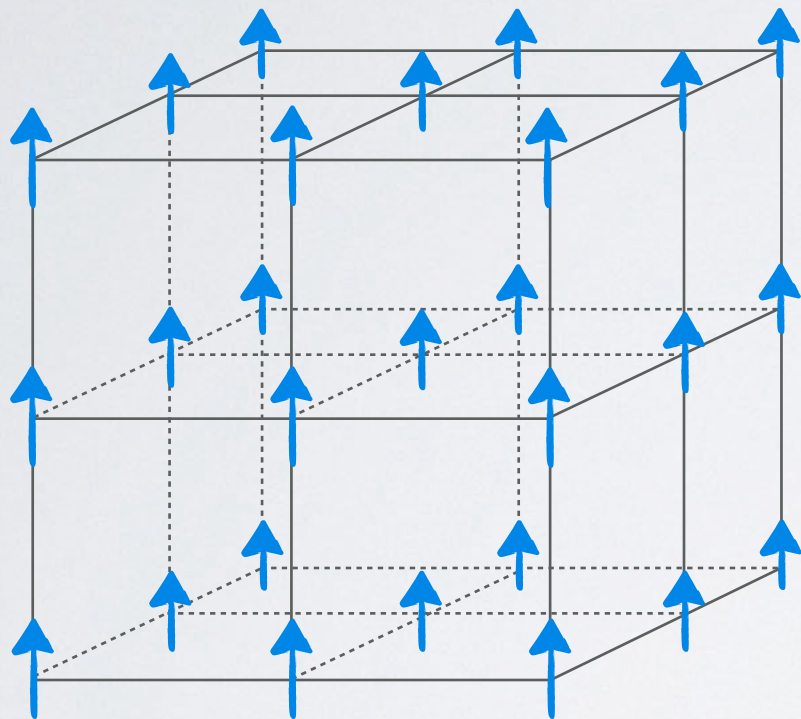
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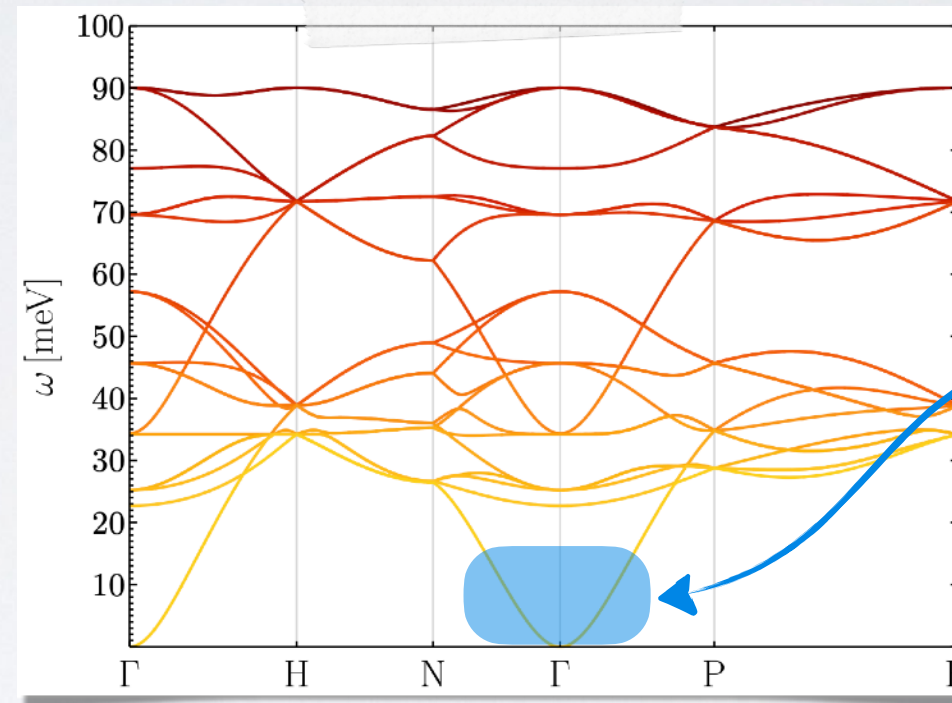
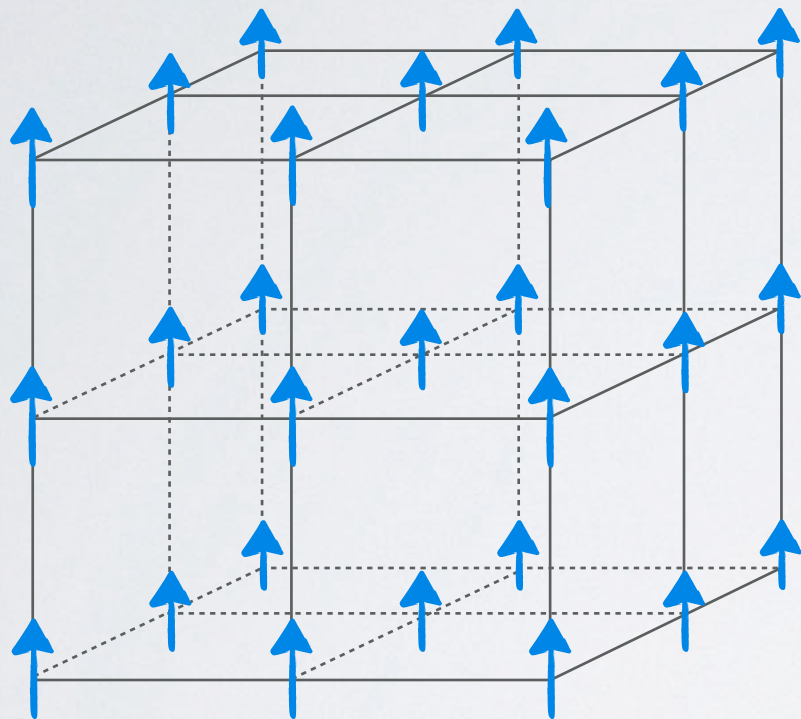


for $m_\chi \lesssim 10$ MeV only
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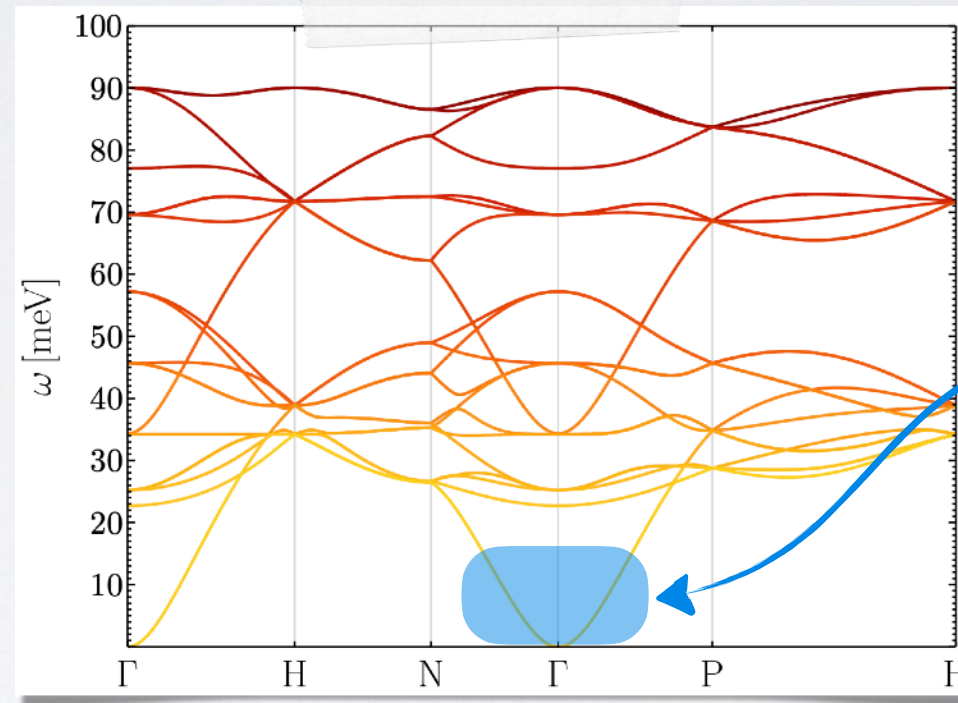
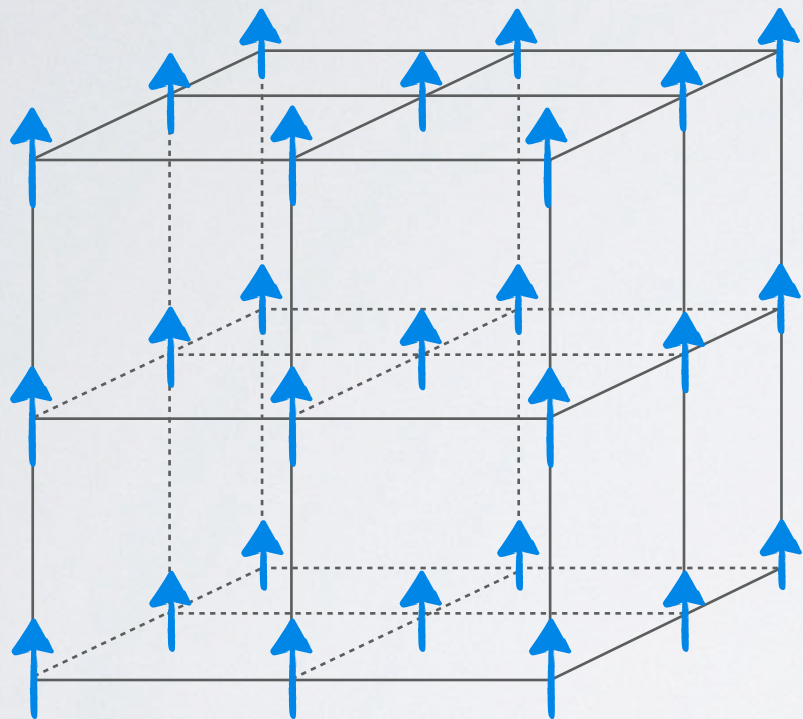
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 $\omega(q) = q^2 / (2m_\theta)$

- Conservation of magnetization → only one magnon emitted

FERROMAGNETS

- First proposed to use ferromagnets

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$$\omega_{max} = E_\chi \frac{4 m_\theta / m_\chi}{(1 + m_\theta / m_\chi)^2} \quad \text{with} \quad m_\theta \sim 1 \text{ MeV}$$

inefficient for
 $m_\chi \lesssim \mathcal{O}(\text{MeV})$

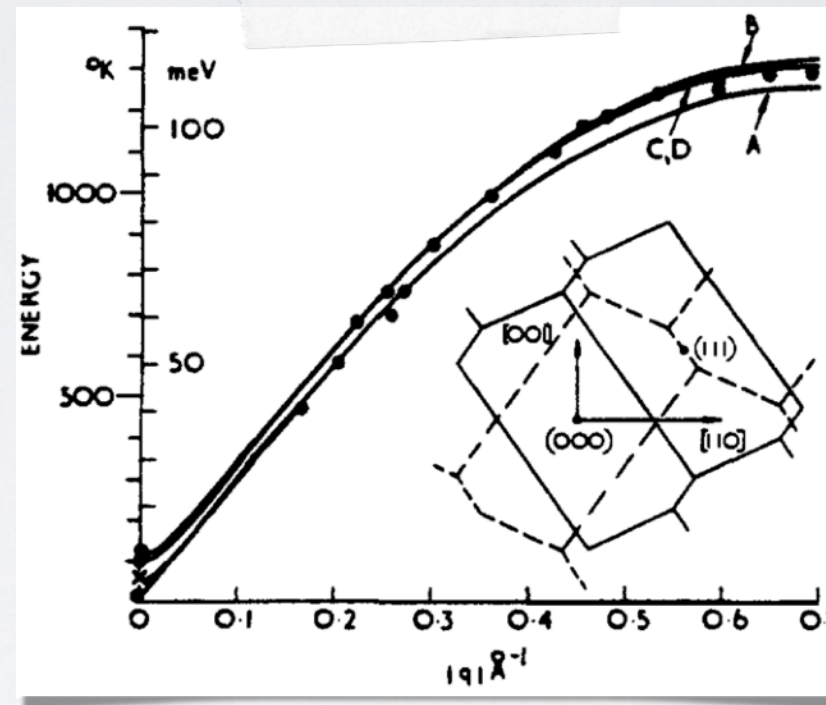
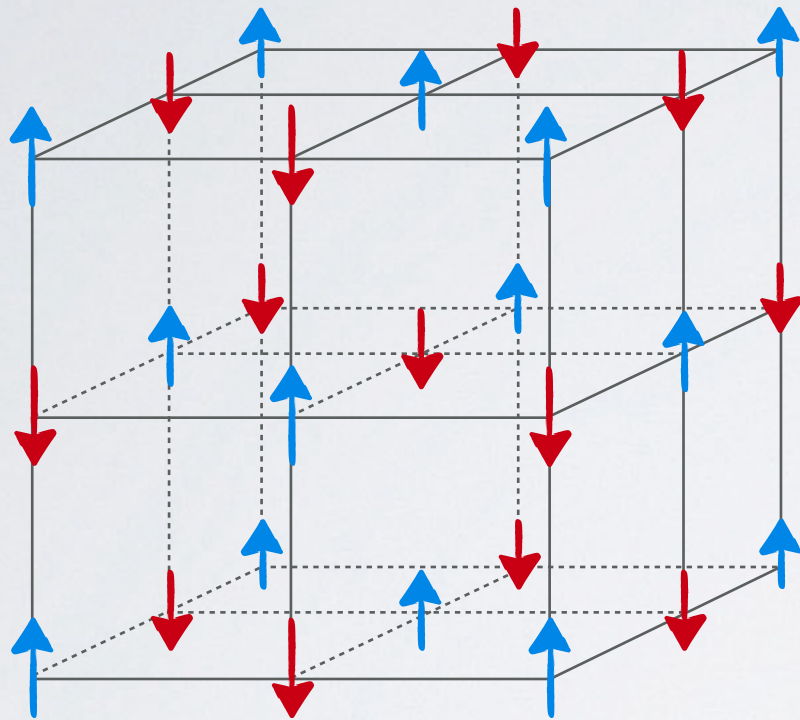
ANTI-FERROMAGNETS

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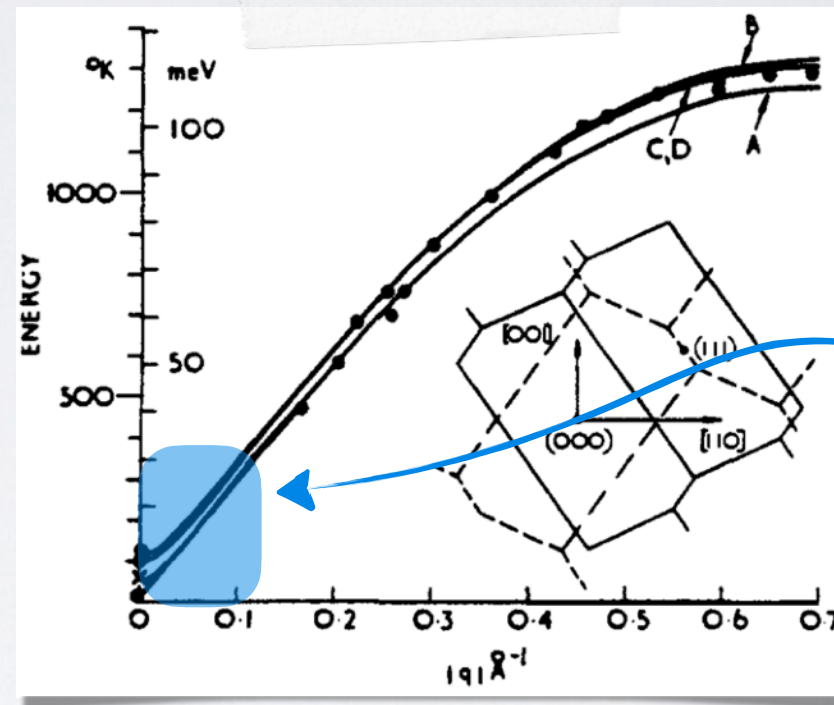
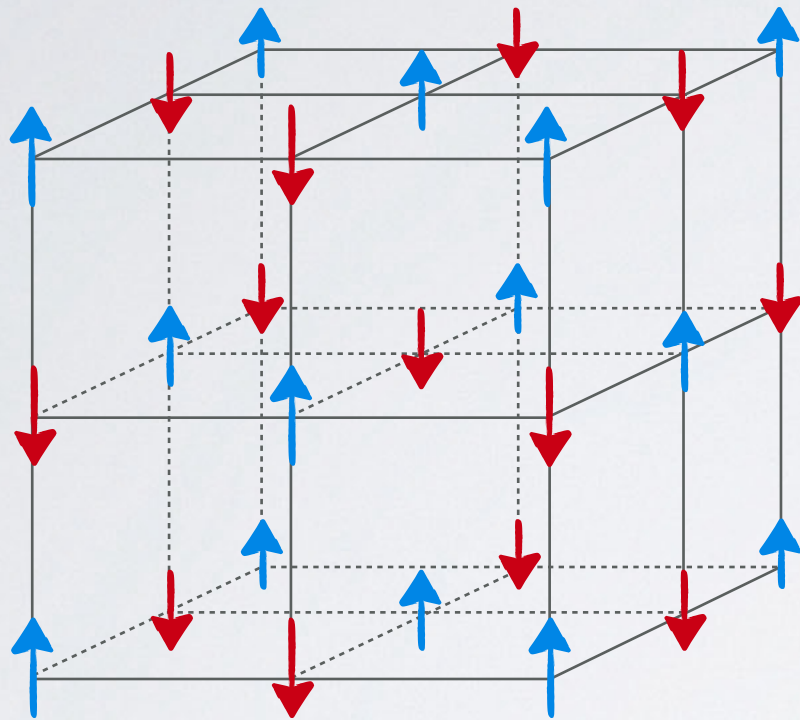
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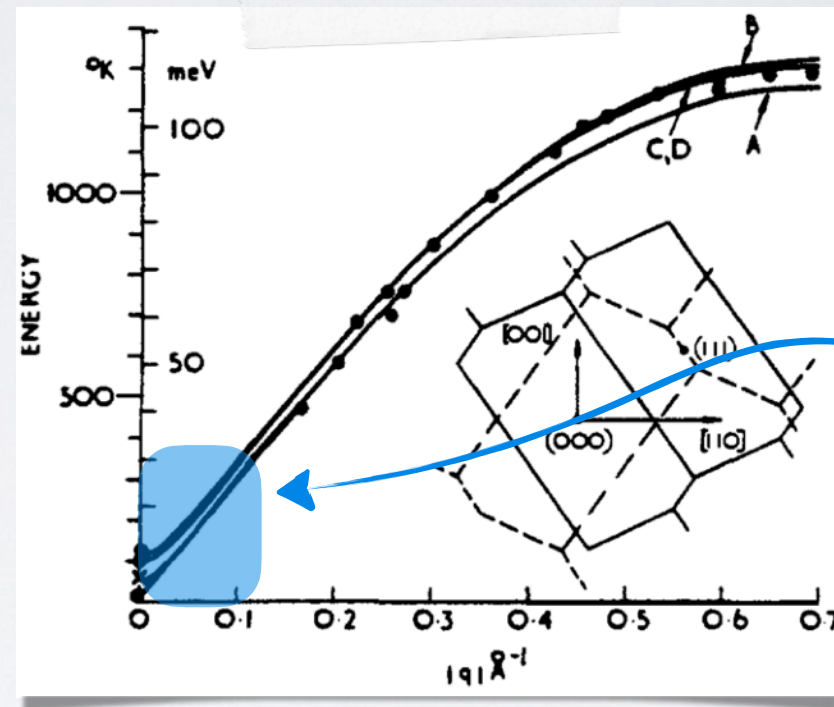
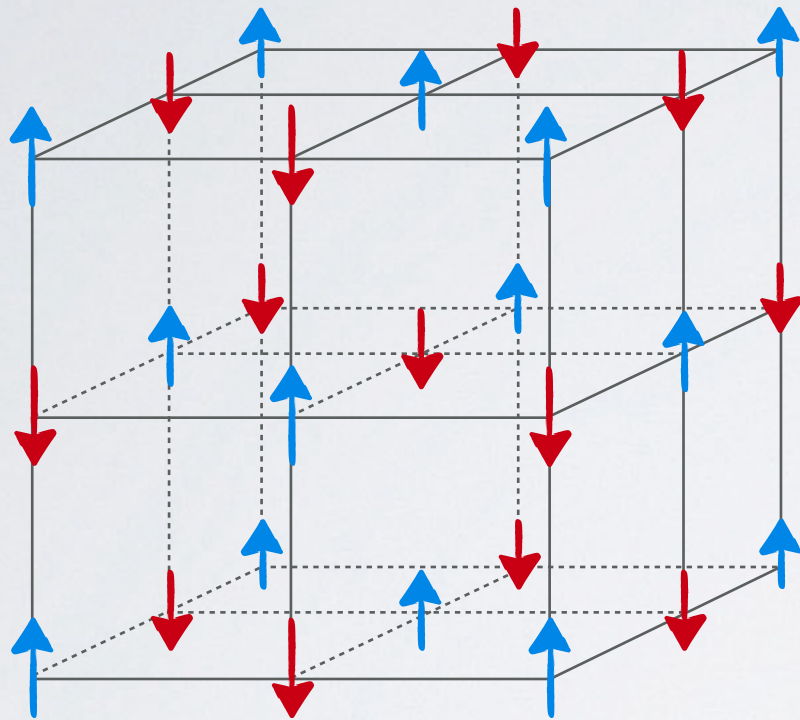
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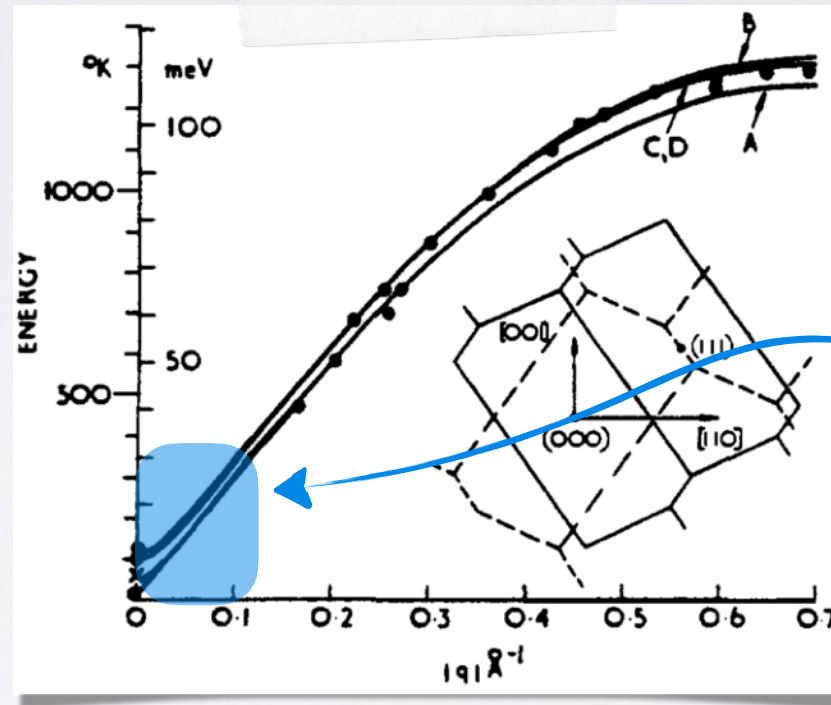
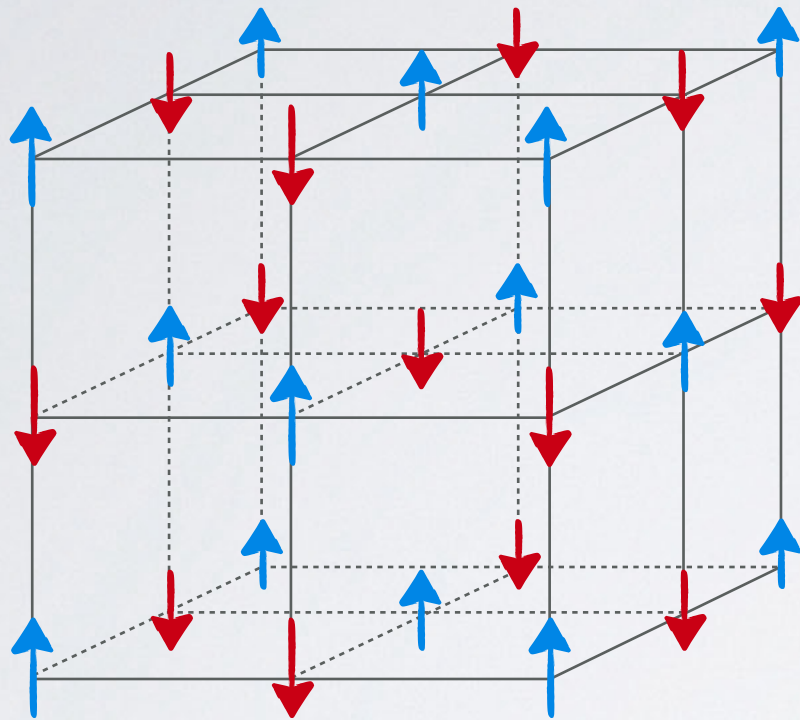


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- Nickel-oxide has $v_{\theta} \sim v_{\chi}$ → very efficient at absorbing dark matter energy

[AE, Pavaskar – PRD (2023), 2210.13516]

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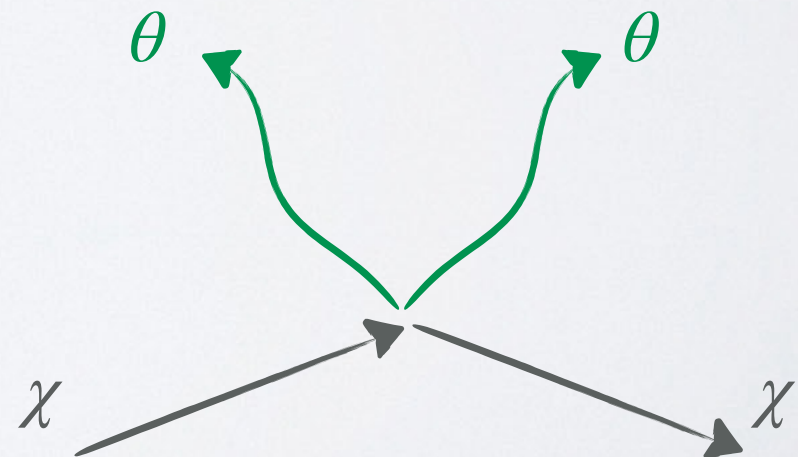
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- **Multi-magnon emission process** evade the kinematical constraints and **get down to $m_\chi \sim \mathcal{O}(\text{keV})$**



MAGNONS

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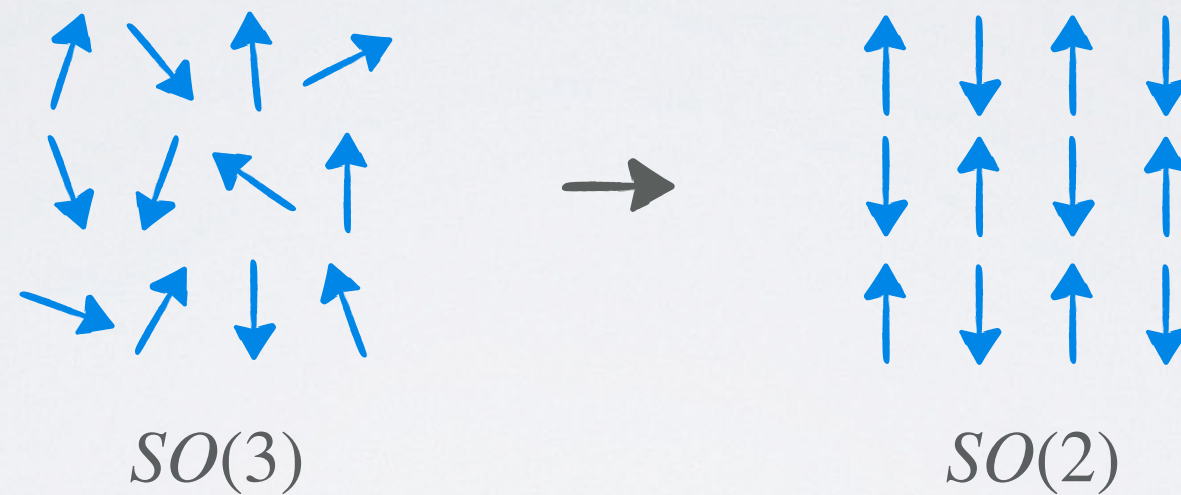
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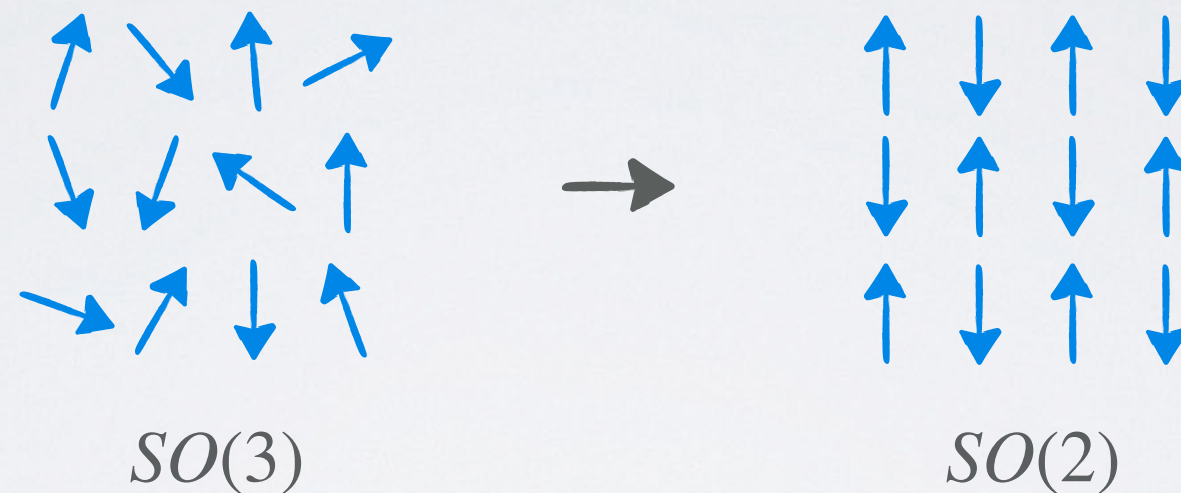
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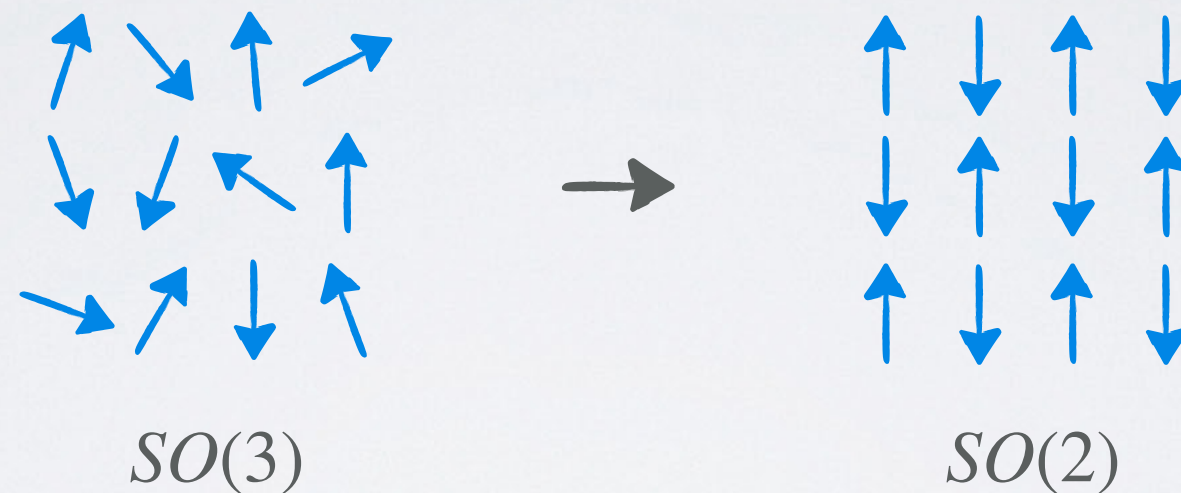
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- At low energies/momenta magnons can be described by an EFT, invariant under the full symmetry group

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can be extracted from
dispersion relation +
neutron scattering data

$$v_\theta = c_2/c_1$$

$$\sigma_n \propto c_1$$

[Burgess – Phys. Rept. (2000), hep-th/9808176; **AE**, Pavaskar – PRD (2023), 2210.13516]

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- This allows to **bypass difficulties in the standard treatment** (failure of the Holsten-Primakoff approach) [Dyson – Phys. Rev. 1956]

IDEAL REACH

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[[AE](#), Pavaskar – PRD (2023), 2210.13516]

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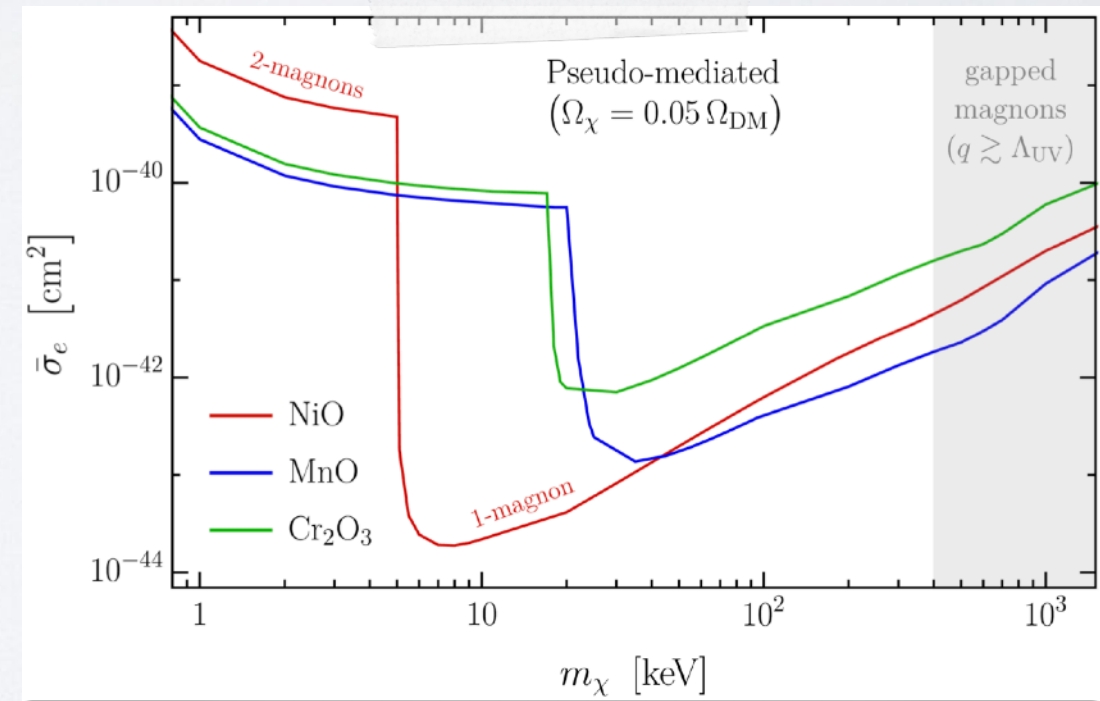
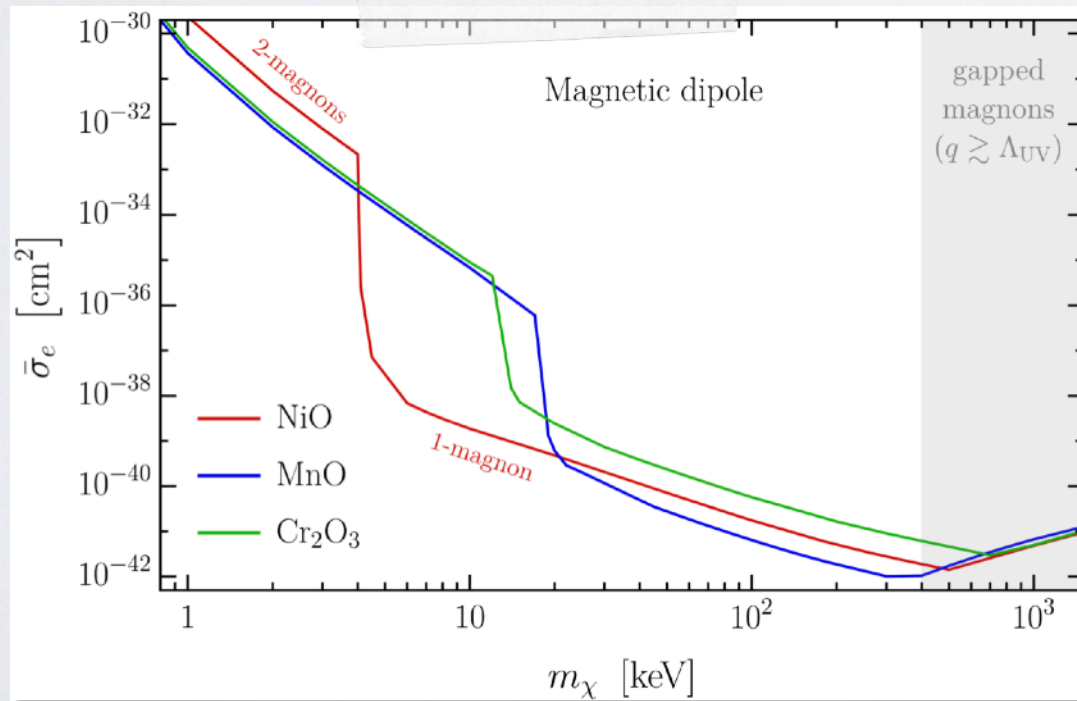
$$\begin{aligned}
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Thank you for the attention!