# Improved bounds on the hot QCD axion



Istituto Nazionale di Fisica Nucleare Laboratori Nazionali del Gran Sasso

based on: F. Bianchini,  $G^2 dC$ , M. Valli, arXiv: 2310.08169

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## Set a robust and conservative upper bound on the QCD axion mass using cosmological datasets (Planck, DESI-Y1) and primordial abundances.

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 $\mathscr{L}_{\text{QCD}} \supset \bar{q}(i\partial_{\mu}\gamma^{\mu} - m_q e^{i\theta_q\gamma_5})q - \frac{1}{\Lambda}$  $\theta \rightarrow \theta = \theta - \text{Arg}[\text{Det}(M_{\mu}M_{d})]$ **Neutron EDM**  $|d_n| \simeq 2.4 \cdot 10^{-16} \overline{\theta} \, \mathrm{e} \cdot \mathrm{cm} < 1.8 \cdot 10^{-26} \, \mathrm{e} \cdot \mathrm{cm} \quad \text{implying} \quad |\overline{\theta}| \lesssim 10^{-10}$ 

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$$-G^{a,\mu\nu}G^{a}_{\mu\nu} + \Theta \frac{\alpha_{s}}{8\pi}G^{a,\mu\nu}\tilde{G}^{a}_{\mu\nu}$$
$$\tilde{G}_{\mu\nu} = \frac{1}{2}\epsilon_{\mu\nu\rho\sigma}G^{\rho\sigma}$$



# The QCD axion

 $\mathscr{L} \supset \mathscr{L}_{QCD} + \frac{1}{2} (\partial_{\mu} a) (\partial^{\mu} a) + \frac{\alpha_s}{8\pi} \frac{a}{f_s} G^{a,\mu\nu} \tilde{G}^a_{\mu\nu} + \mathscr{L}_{\text{int}} (\partial_{\mu} a, q, \ell)$ 



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A theorem by Vafa and Witten (1984)

$$e^{-V_4 E(\bar{\theta})} = \int \delta[\phi] e^{-S_0 + i\bar{\theta}Q} = \left| \int \delta[\phi] e^{-S_0 + i\bar{\theta}Q} \right|$$
$$\leq \left| \delta[\phi] \left| e^{-S_0 + i\bar{\theta}Q} \right| = e^{-V_4 E(0)}$$

implies that the axion will relax to the minimum of the potential



## Non-thermal production



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## Thermal production



 $k_a \sim T \gg m_a$ 

The axion behave similarly to neutrino and contributes to dark radiation. It can only be a small fraction of the dark matter.









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$$\Delta N_{\rm eff} = \frac{8}{7} \left(\frac{11}{4}\right)^{\frac{4}{3}} \left(\frac{\rho_a}{\rho_\gamma}\right)_{\rm CMB} \simeq 0.027 \left(\frac{106.75}{g_{*,s}(T_d)}\right)^{4/3}$$

Solve Boltzmann equations

Caveats

$$\frac{dY}{d\log x} = (Y^{\text{eq}} - Y)\frac{\Gamma}{H}\left(1 - \frac{1}{3}\frac{d\log g_{*S}}{d\log x}\right)$$



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This formula may not be precise enough:

- 1. if the cross section depends on momentum, since different momenta will decouple at different times;
- 2. if the number of degrees of freedom decrease rapidly, higher momenta will be less diluted, leading to spectral distortions;
- 3. because production may be never in thermal equilibrium.

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Momentum-dependent **Boltzmann equation** 

$$\frac{\partial \mathcal{F}_{a}}{\partial t} - H |\mathbf{k}| \frac{\partial \mathcal{F}_{a}}{\partial |\mathbf{k}|} = \Gamma_{a} \left( \mathcal{F}_{a}^{eq} - \mathcal{F}_{a} \right)$$

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## Hot axions from pions

 $\mathscr{L}_{a\pi} \supset \frac{\mathcal{C}_{a\pi}}{f_a f_{\pi}} \partial^{\mu} a \left( 2 \partial_{\mu} \pi^0 \pi^+ \pi^- - \pi^0 \partial_{\mu} \pi^+ \pi^- - \pi^0 \pi^+ \partial_{\mu} \pi^- \right)$ 



### How do you fix this issue?

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$$\mathcal{L}_{LO}|^2 = \left(\frac{C_{a\pi}}{f_a f_\pi}\right)^2 \frac{9}{4} \left(s^2 + t^2 + u^2 - 3m_\pi^4\right)$$
[Chang, Choi 1993]

[Di Luzio, Martinelli, Piazza 2021] NLO: breaks down at T~60 MeV

## Hot axions from pions



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### Inverse amplitude method [Truong 1988]

$$t_{\ell}^{I}(s) = \frac{t_{\ell}^{I(2)}(s)}{1 - t_{\ell}^{I(4)}(s)/t_{\ell}^{I(2)}(s)}$$



# How to constrain light axions?



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# Results



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### [Bianchini, $G^2 dC$ , Valli 2023]



### [Yeh, Shelton, Olive, Fields 2022]



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# Results



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### [Bianchini, $G^2 dC$ , Valli 2023]

We use PRyMordial [Burns, Tait, Valli 2023] to obtain a likelihood for  $Y_p$ , D/H and He<sup>3</sup>/H as a function of  $N_{\rm eff}$  and  $\Omega_B$ .

# ...and large multipole?



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# Results



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![](_page_20_Picture_4.jpeg)

![](_page_21_Picture_0.jpeg)

Robust bound on  $m_a$  from up-to-date measurements of CMB, ground-based telescopes and abundances from BBN

 $m_a \le 0.16 \text{ eV}$  at 95 % CL

Forecast for future surveys (Simons Observatory and CMB-S4) in the  $m_a$  vs  $\sum m_{\nu}$  plane competitive with current constraints from astrophysics.

![](_page_21_Figure_9.jpeg)