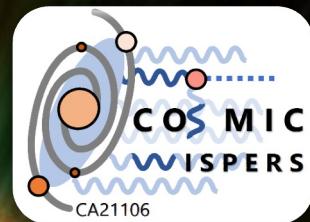




IDM2023

L'Aquila, 9th July 2024



Axion-like particles as probes of the SN core

Based on: AL., F. Calore, P. Carenza, C. Eckner, M. Giannotti, G. Lucente, A. Mirizzi,
“*Probing protoneutron stars with gamma-ray haloscopes*”, e-Print: 2405.02395



Alessandro Lella

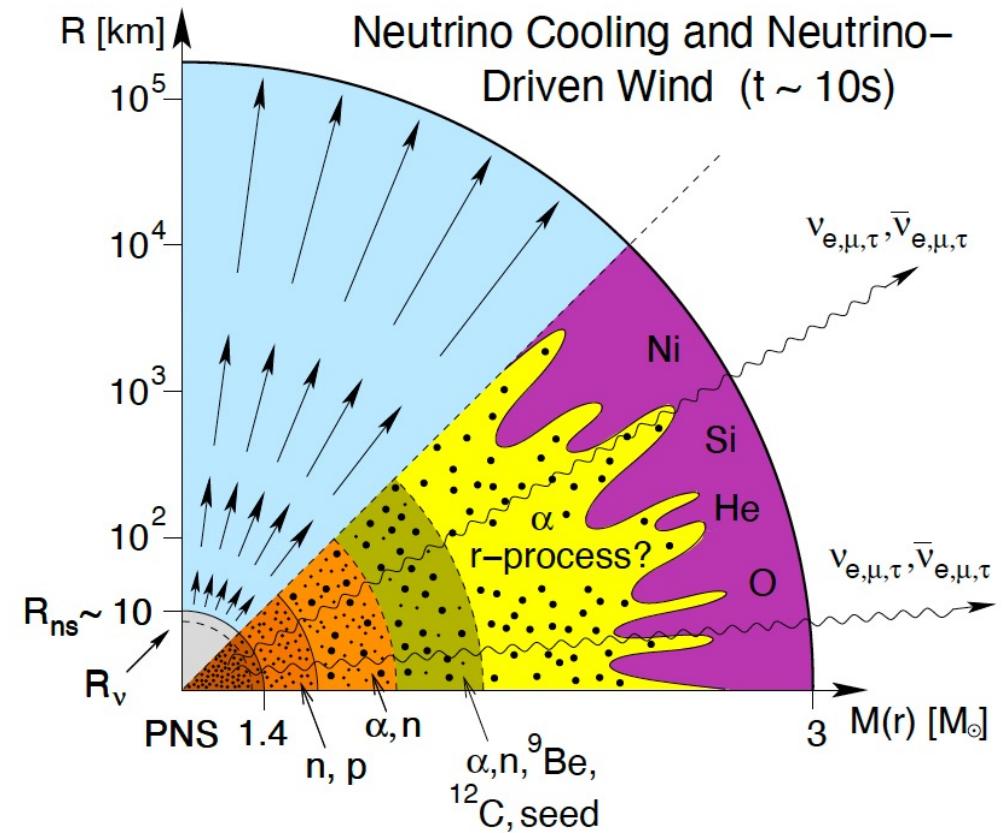
Physics Department of «Aldo Moro» University in Bari
Istituto Nazionale di Fisica Nucleare



Core-Collapse Supernovae

A core-collapse Supernova is the terminal phase of a massive star [$M \geq 8 M_{\odot}$].
After the gravitational collapse, a shock-wave driven explosion occurs.

- Formation of a Proto-Neutron star
 - $R \sim 30 \text{ km}, M \sim 1.5 M_{\odot}$
- Cooling via neutrino emission from neutrino sphere at $R_{\nu} \simeq 20 \text{ km}$
 - $E \sim 10^{53} \text{ erg}, t \sim 10 \text{ s}$
- Benchmark SN model employed:
GARCHING SFHo-s18.80
 - $M_{\text{PNS}} \simeq 1.35 M_{\odot}, M_{\text{prog}} \simeq 18.8 M_{\odot}$



<https://wwwmpa.mpa-garching.mpg.de/ccsnarchive//>

ALP production in the PNS

➤ Extreme conditions in the SN nuclear medium

- $T \sim 30 - 40 \text{ MeV}$, $\rho \sim 3 \times 10^{14} \text{ g/cm}^3$ → Enhancement in the emission of ALPs

ALP production in the PNS

➤ Extreme conditions in the SN nuclear medium

- $T \sim 30 - 40 \text{ MeV}, \rho \sim 3 \times 10^{14} \text{ g/cm}^3$ → Enhancement in the emission of ALPs

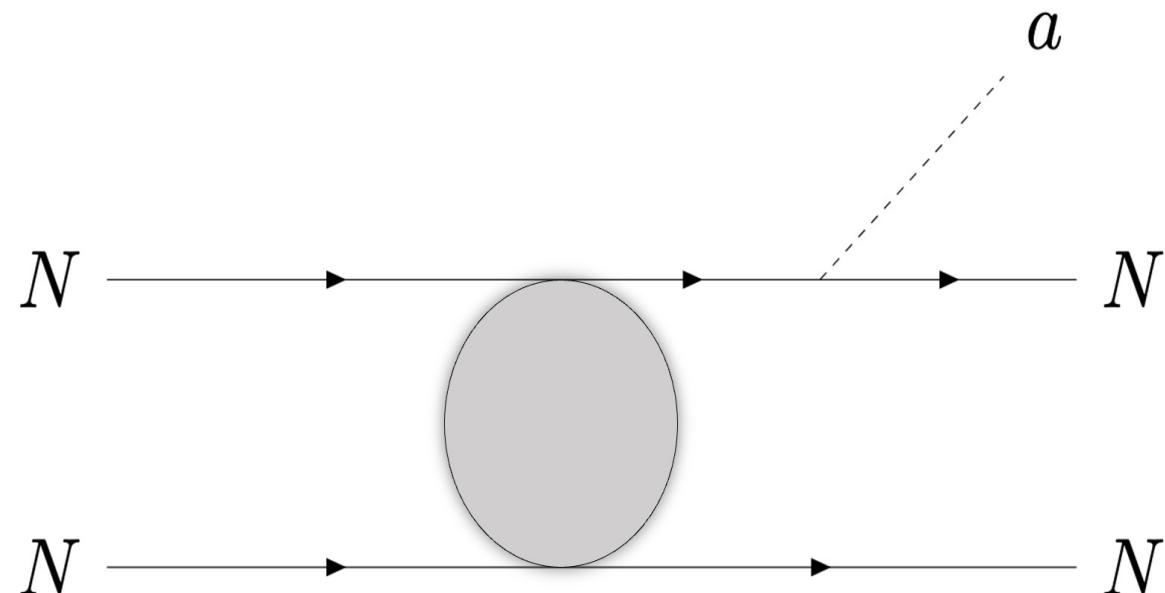
➤ In ChPT ALPs couple to nuclear matter [*Ho & al., Phys. Rev. D 107 (2023)*]

$$\begin{aligned}\mathcal{L}_{\text{int}} = & g_a \frac{\partial_\mu a}{2m_N} \left[C_{ap} \bar{p} \gamma^\mu \gamma_5 p + C_{an} \bar{n} \gamma^\mu \gamma_5 n + \right. \\ & + \frac{C_{a\pi N}}{f_\pi} (i\pi^+ \bar{p} \gamma^\mu n - i\pi^- \bar{n} \gamma^\mu p) + \\ & \left. + C_{aN\Delta} \left(\bar{p} \Delta_\mu^+ + \overline{\Delta_\mu^+} p + \bar{n} \Delta_\mu^0 + \overline{\Delta_\mu^0} n \right) \right]\end{aligned}$$

ALP production in SNe

- Nucleon-Nucleon bremsstrahlung

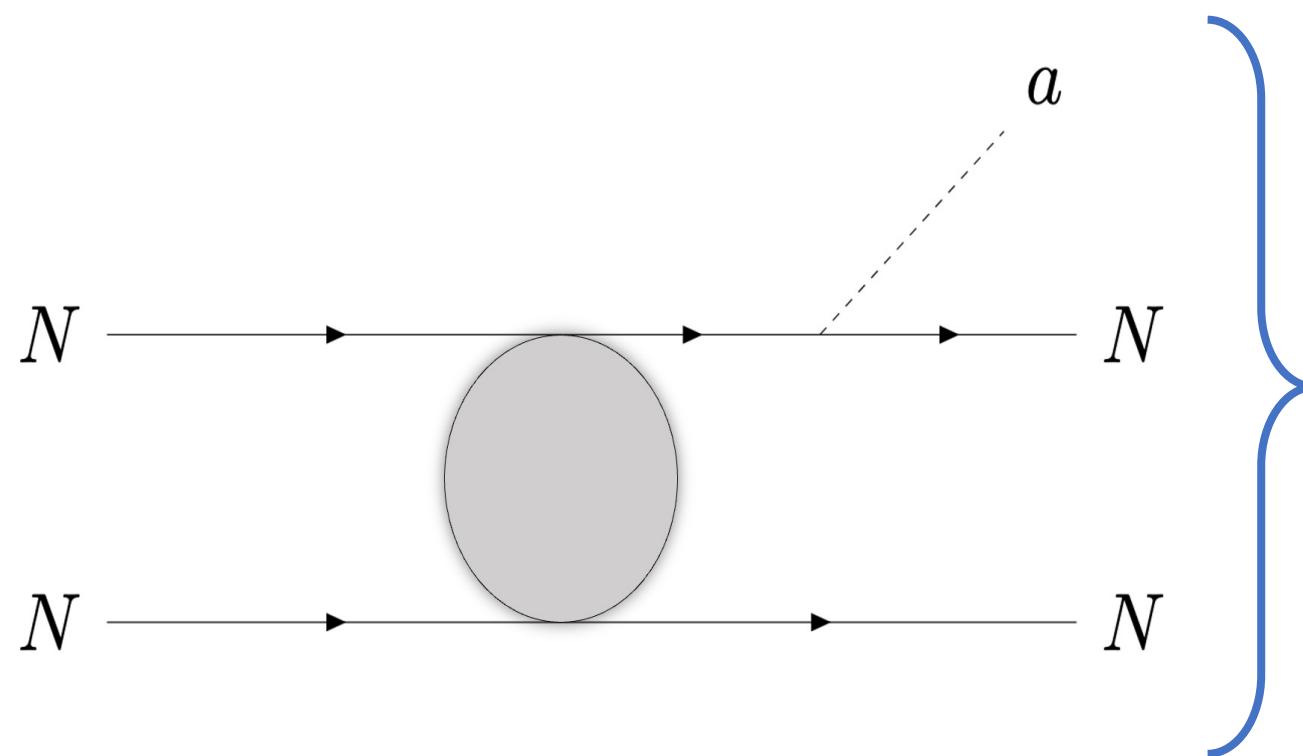
[Ericson and Mathiot, *Phys. Lett. B* 219 (1989),
Raffelt & Seckel, *Phys. Rev. D* 52 (1995),
Hempel, *Phys. Rev. C* 91 (2015),
Carenza & al., *JCAP* 10 (2019) 10]



ALP production in SNe

➤ Nucleon-Nucleon bremsstrahlung

[Ericson and Mathiot, *Phys. Lett. B* 219 (1989),
Raffelt & Seckel, *Phys. Rev. D* 52 (1995),
Hempel, *Phys. Rev. C* 91 (2015),
Carenza & al., *JCAP* 10 (2019) 10]



Strong dependence on SN conditions:

- Nuclear density in the core
- Effective nucleon masses $m_N \rightarrow m_N^*$
- Multiple scattering effects
- Nucleon momentum transfer dependent on T

ALP production in SNe

➤ Pion Conversions

[Carenza & al., Phys.Rev.Lett. 126 (2021),
Choi & al., JHEP 02 (2022) 143,
Ho & al., Phys. Rev. D 107 (2023)]

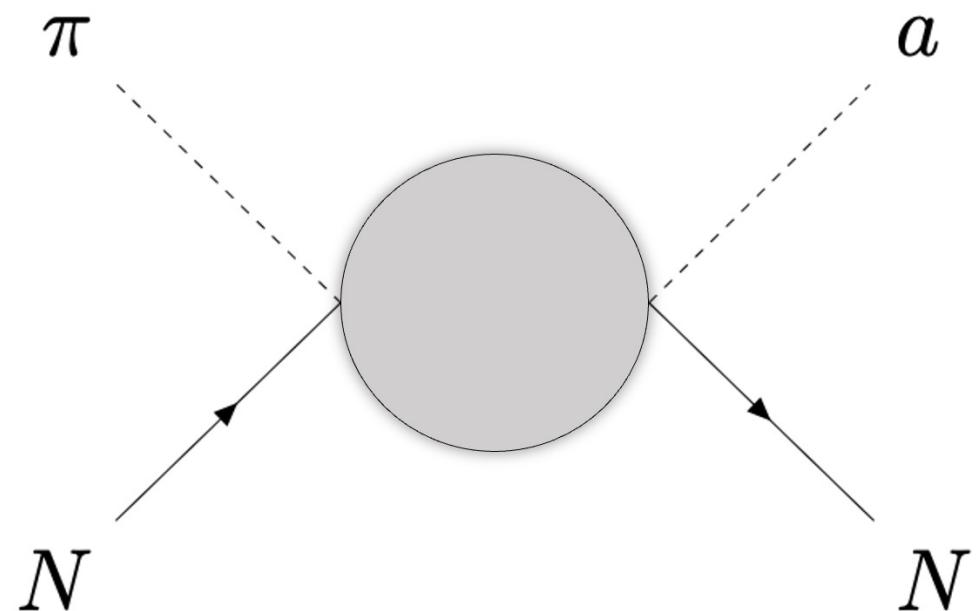
[Fore & Reddy, Phys.Rev.C 101 (2020) 3]

Strong interactions enhance the π^- abundance

$$Y_{\pi^-} \sim \mathcal{O}(10^{-2})$$



Pion conversion competitive with
NN bremsstrahlung



ALP production in SNe

➤ Pion Conversions

[Carenza & al., Phys.Rev.Lett. 126 (2021),
Choi & al., JHEP 02 (2022) 143,
Ho & al., Phys. Rev. D 107 (2023)]

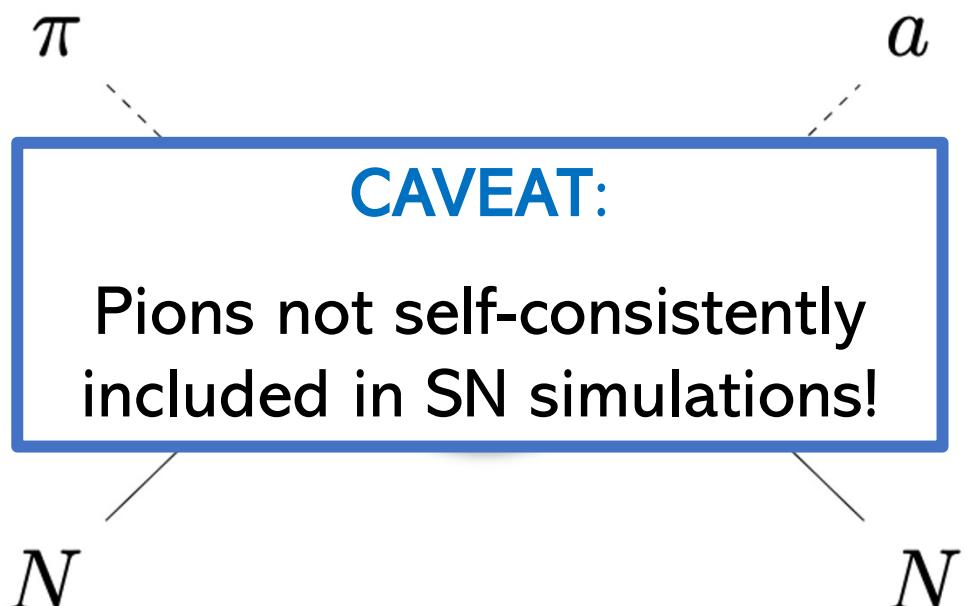
[Fore & Reddy, Phys.Rev.C 101 (2020) 3]

Strong interactions enhance the π^- abundance

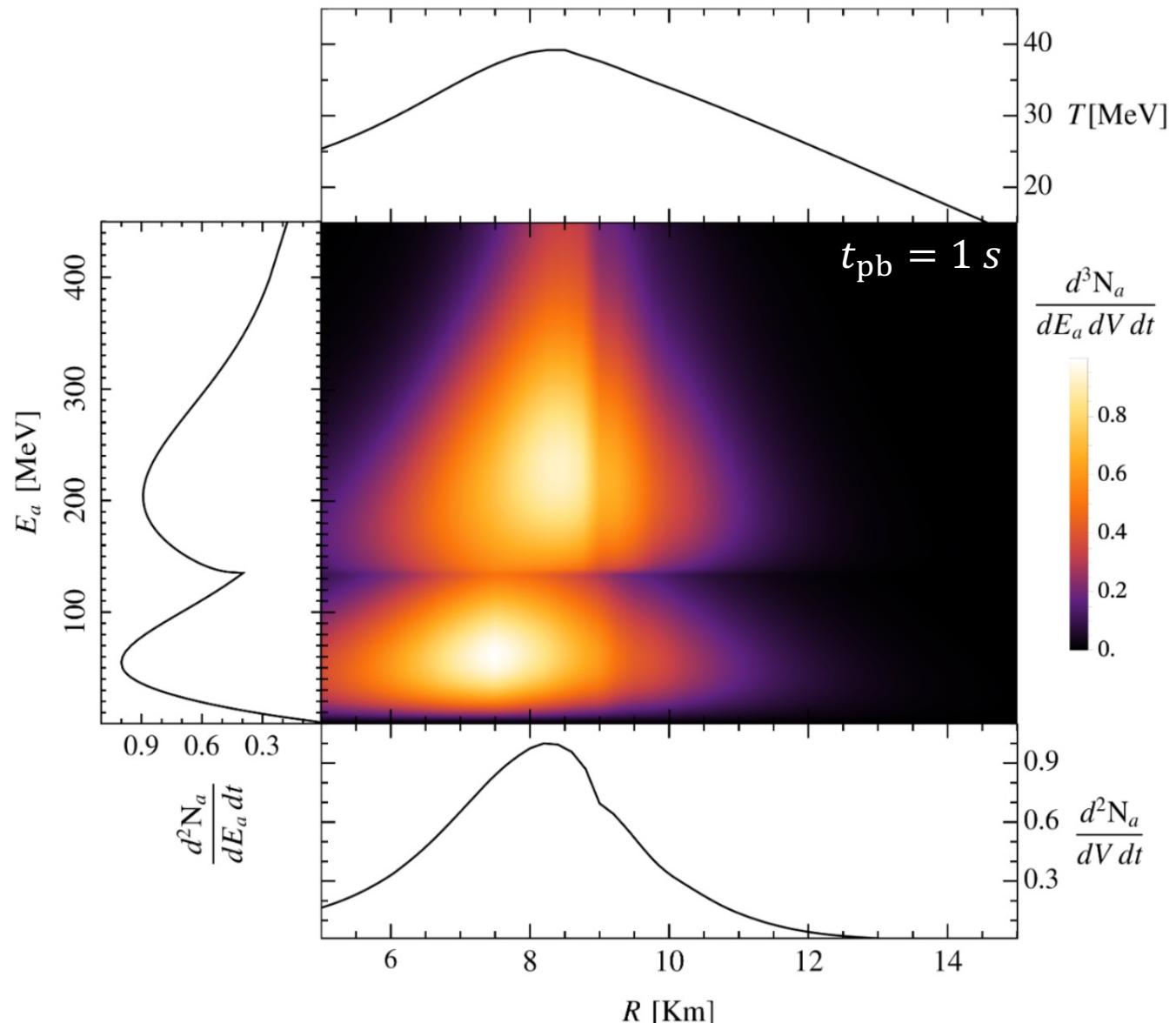
$$Y_{\pi^-} \sim \mathcal{O}(10^{-2})$$



Pion conversion competitive with
NN bremsstrahlung

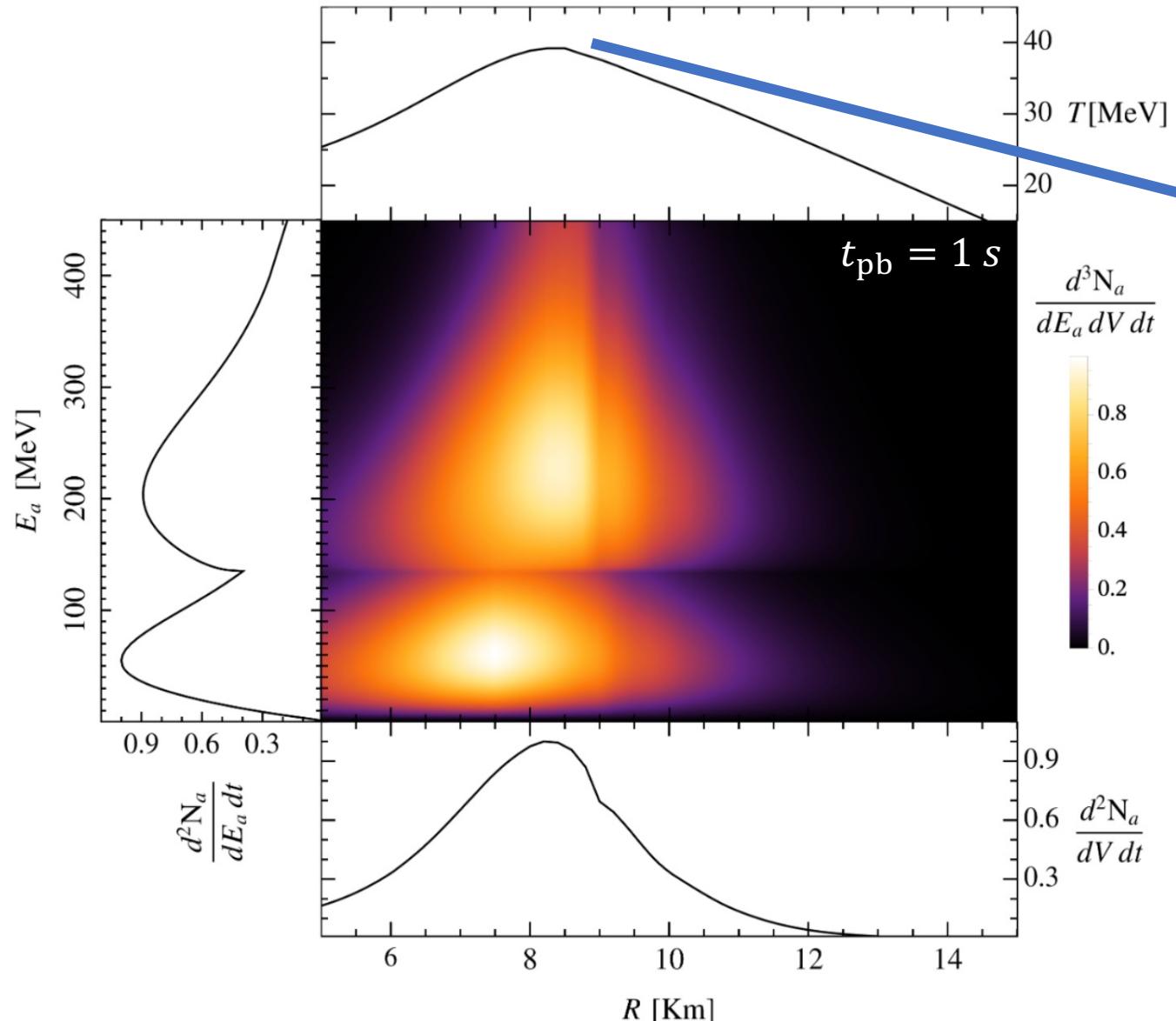


ALPs as messengers of PNS



ALPs can provide a lot of information about the PNS [\[AL et al., e-Print: 2405.02395\]](#)

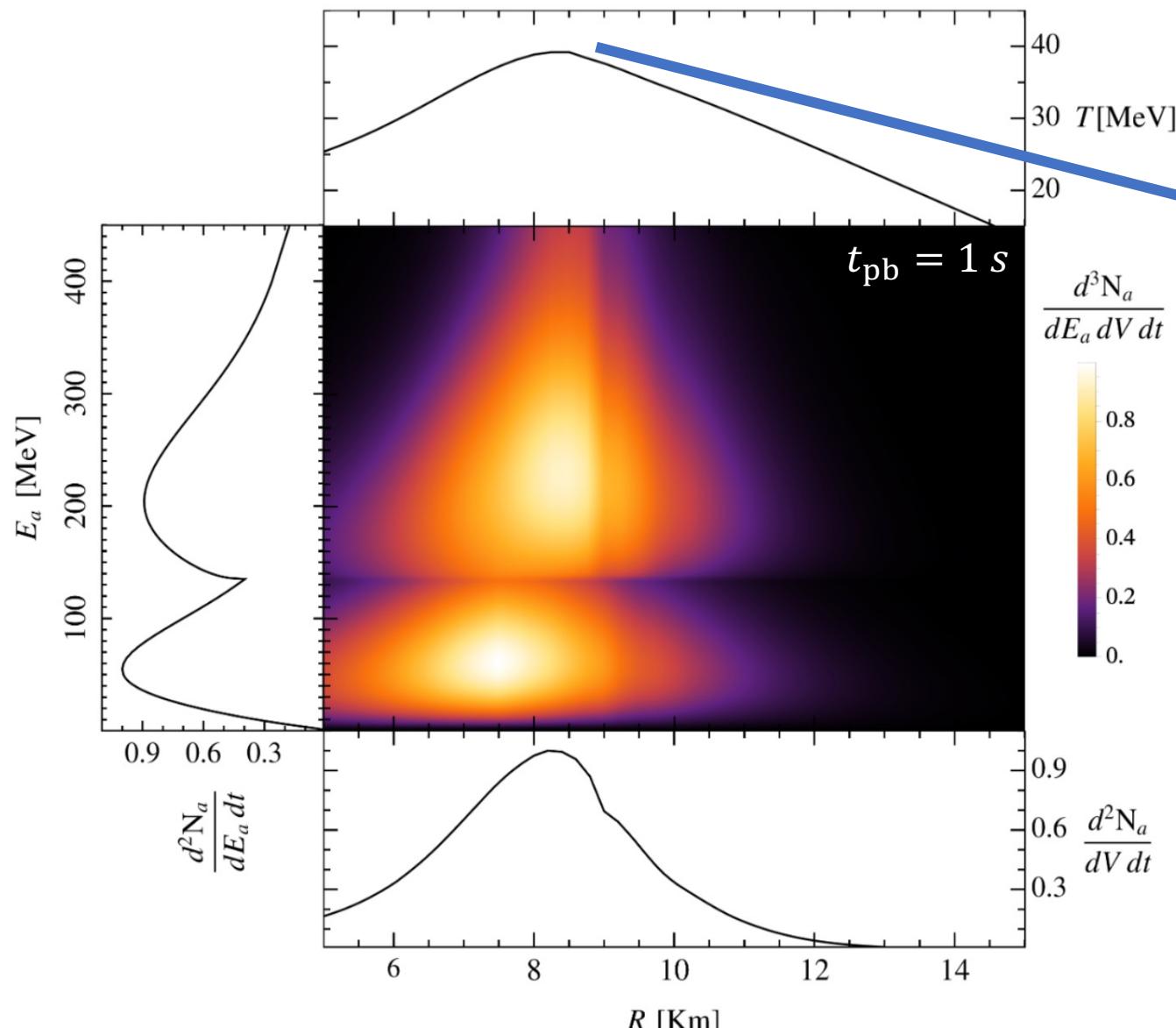
ALPs as messengers of PNS



ALPs can provide a lot of information about the PNS [\[AL et al., e-Print: 2405.02395\]](#)

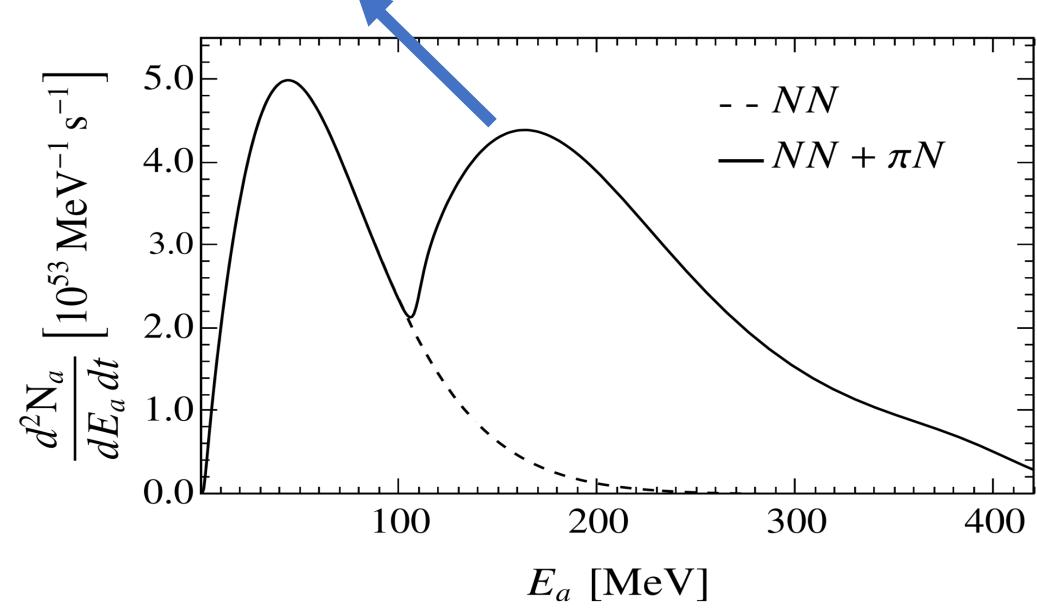
- ALP production sensitive to the PNS temperature peak

ALPs as messengers of PNS



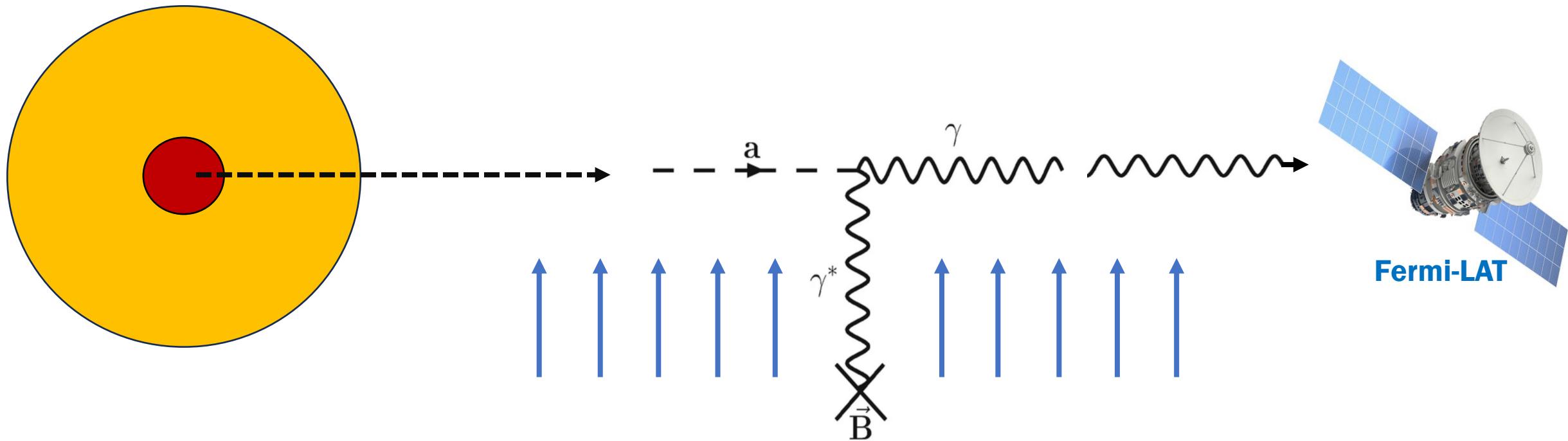
ALPs can provide a lot of information about the PNS [\[AL et al., e-Print: 2405.02395\]](#)

- ALP production sensitive to the PNS temperature peak
- Evidence for the presence of pions



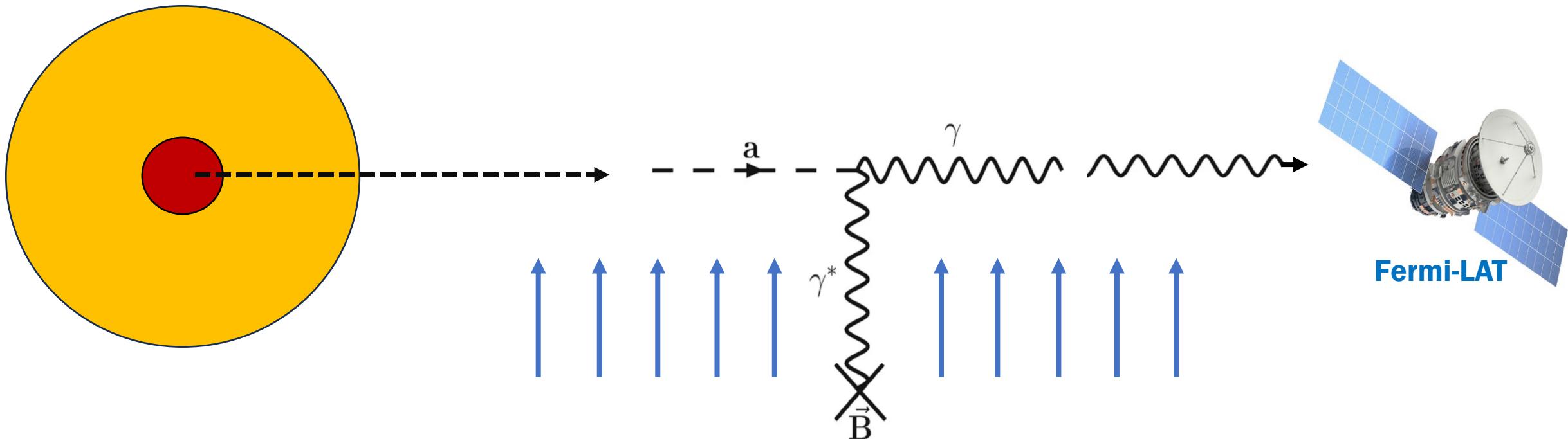
Ultra-light ALP conversions

Once emitted from SNe, ultra-light ALPs ($m_a \leq \mathcal{O}(1) \text{ neV}$) can convert into photons in Galactic Magnetic fields



Ultra-light ALP conversions

Once emitted from SNe, ultra-light ALPs ($m_a \leq \mathcal{O}(1) \text{ neV}$) can convert into photons in Galactic Magnetic fields



➤ Additional coupling to photons required

$$\mathcal{L}_{a\gamma} = -\frac{1}{4}g_{a\gamma}F_{\mu\nu}\tilde{F}^{\mu\nu}a$$



It emerges naturally for ALPs coupled to nuclear matter!

AL & al., e-Print: 2405.00153

Ultra-light ALP conversions

Ultra-light ALPs can convert into photons in Galactic Magnetic fields

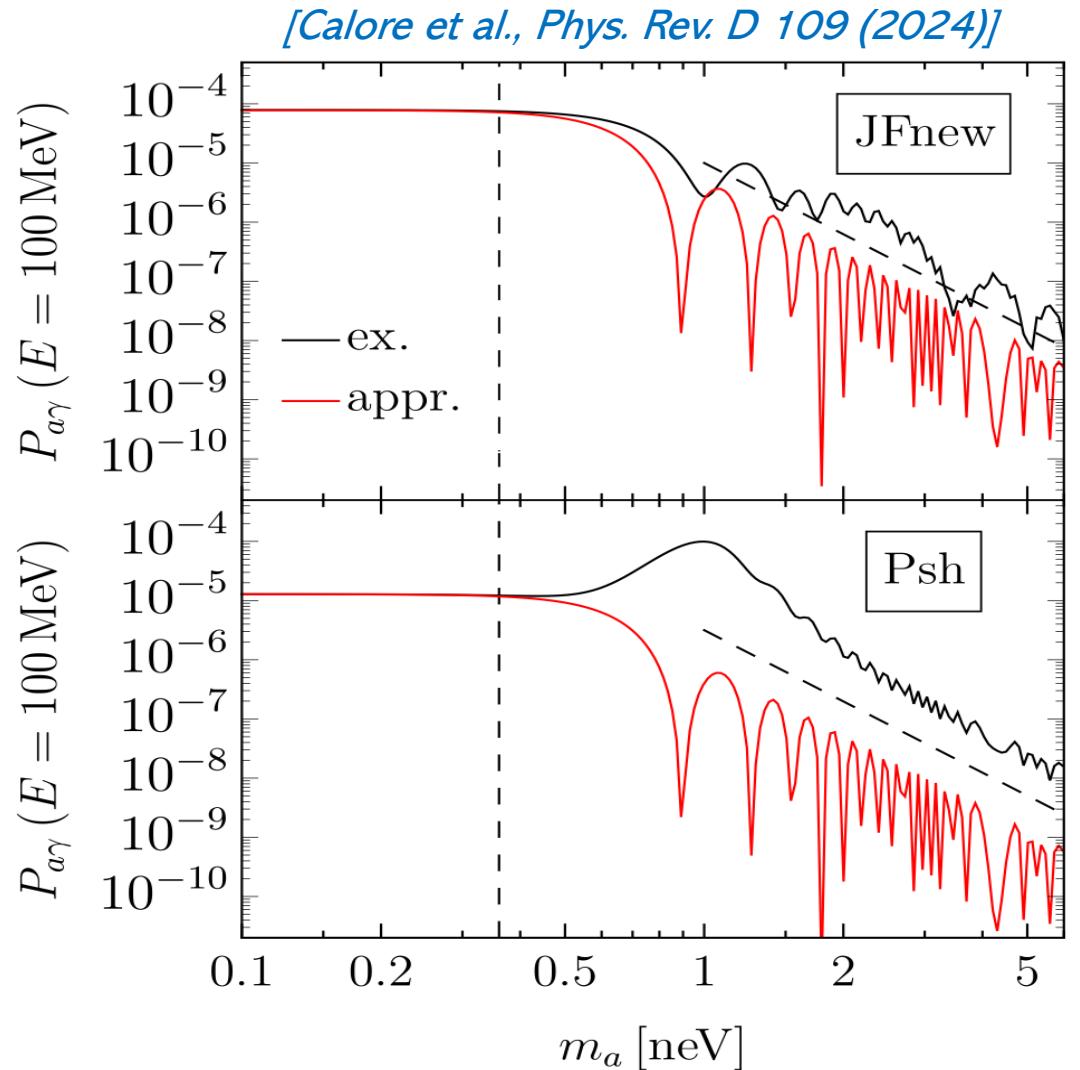
$$P_{a\gamma} = (\Delta_{a\gamma} L)^2 \frac{\sin^2(\Delta_{\text{osc}} L/2)}{(\Delta_{\text{osc}} L/2)^2}$$

$$\Delta_{\text{osc}} \equiv [(\Delta_a - \Delta_{\text{pl}})^2 + 4\Delta_{a\gamma}^2]^{1/2}$$

$$\Delta_{a\gamma} \simeq 1.5 \times 10^{-3} \left(\frac{g_{a\gamma}}{10^{-12} \text{ GeV}^{-1}} \right) \left(\frac{B_T}{10^{-6} \text{ G}} \right) \text{kpc}^{-1},$$

$$\Delta_a \simeq -7.8 \times 10^{-5} \left(\frac{m_a}{10^{-11} \text{ eV}} \right)^2 \left(\frac{E}{100 \text{ MeV}} \right)^{-1} \text{kpc}^{-1}.$$

$$\Delta_{\text{pl}} \simeq -7.8 \times 10^{-7} \left(\frac{\omega_{\text{pl}}}{10^{-12} \text{ eV}} \right)^2 \left(\frac{E}{100 \text{ MeV}} \right)^{-1} \text{kpc}^{-1}.$$



Ultra-light ALP conversions

Ultra-light ALPs can convert into photons in Galactic Magnetic fields

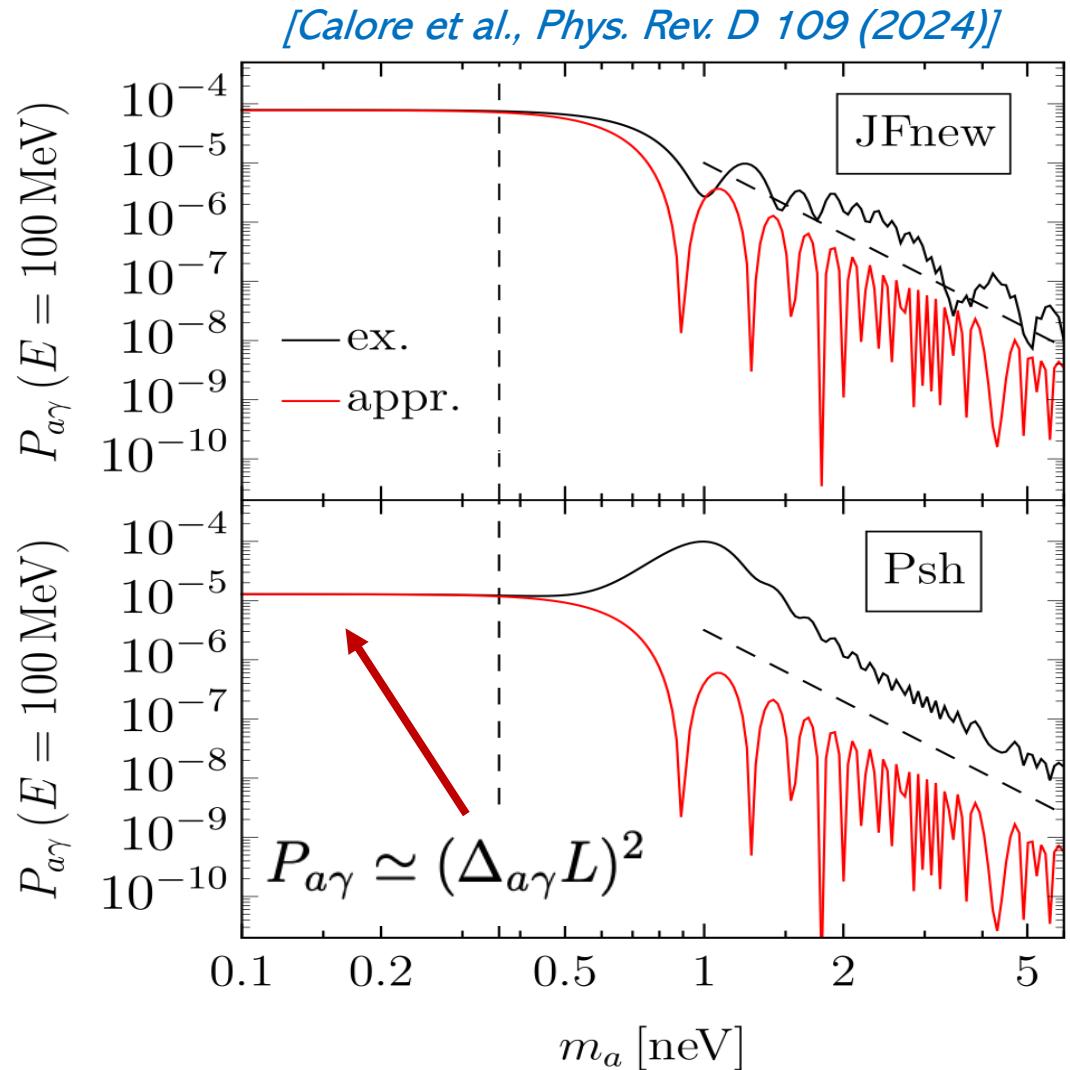
$$P_{a\gamma} = (\Delta_{a\gamma} L)^2 \frac{\sin^2(\Delta_{\text{osc}} L/2)}{(\Delta_{\text{osc}} L/2)^2}$$

$$\Delta_{\text{osc}} \equiv [(\Delta_a - \Delta_{\text{pl}})^2 + 4\Delta_{a\gamma}^2]^{1/2}$$

$$\Delta_{a\gamma} \simeq 1.5 \times 10^{-3} \left(\frac{g_{a\gamma}}{10^{-12} \text{ GeV}^{-1}} \right) \left(\frac{B_T}{10^{-6} \text{ G}} \right) \text{kpc}^{-1},$$

$$\Delta_a \simeq -7.8 \times 10^{-5} \left(\frac{m_a}{10^{-11} \text{ eV}} \right)^2 \left(\frac{E}{100 \text{ MeV}} \right)^{-1} \text{kpc}^{-1}$$

$$\Delta_{\text{pl}} \simeq -7.8 \times 10^{-7} \left(\frac{\omega_{\text{pl}}}{10^{-12} \text{ eV}} \right)^2 \left(\frac{E}{100 \text{ MeV}} \right)^{-1} \text{kpc}^{-1}.$$

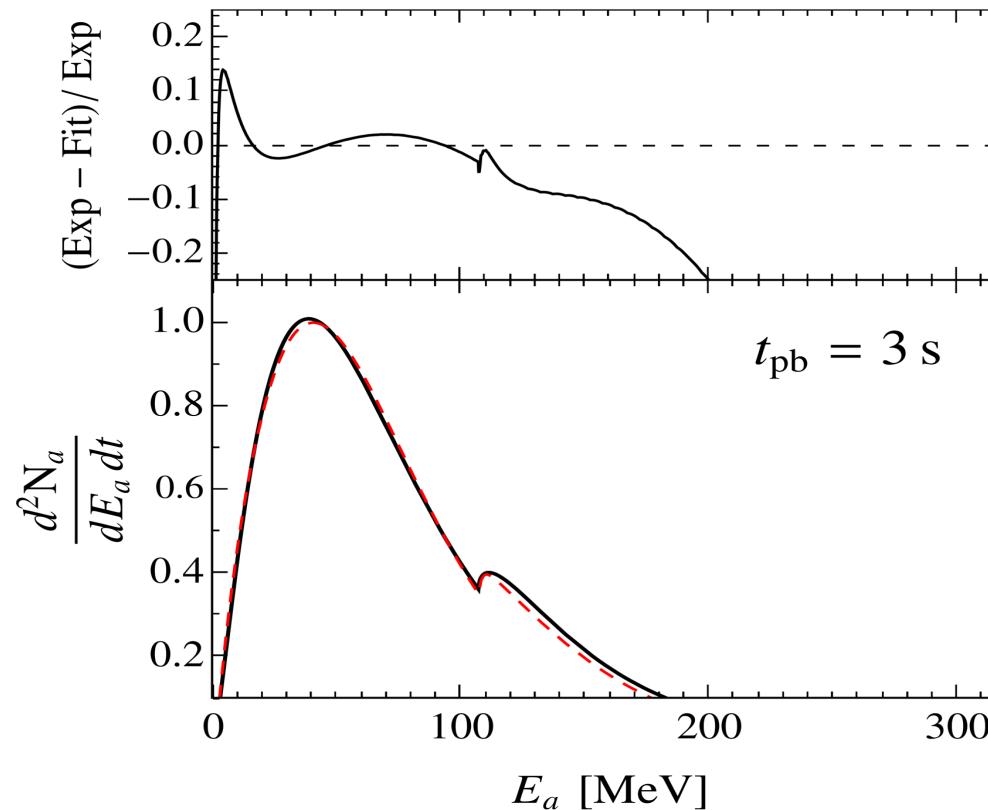
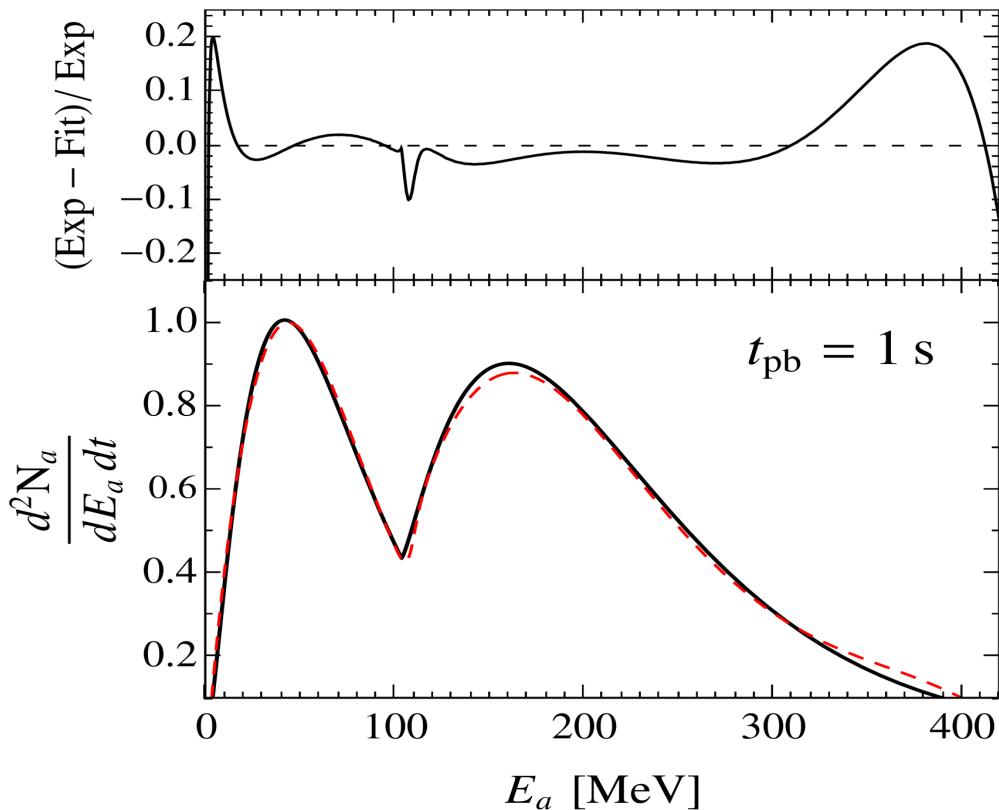


ALPs emission spectra

Complex ALP spectra functional forms can be fitted employing α -fits [\[AL et al., e-Print: 2405.02395\]](#)

$$\left(\frac{d^2 N_a}{d E_a dt} \right)_{NN} \propto \left(\frac{E_a}{E_{NN}^0} \right)^{\beta_{NN}} \exp \left[-(\beta_{NN} + 1) \frac{E_a}{E_{NN}^0} \right]$$

$$\left(\frac{d^2 N_a}{d E_a dt} \right)_{\pi N} \propto \left(\frac{E_a - \omega_c}{E_{\pi N}^0} \right)^{\beta_{\pi N}} \exp \left[-(\beta_{\pi N} + 1) \frac{E_a - \omega_c}{E_{\pi N}^0} \right]$$



ALPs emission spectra

Complex ALP spectra functional forms can be fitted employing α -fits [\[AL et al., e-Print: 2405.02395\]](#)

$$\left(\frac{d^2 N_a}{d E_a dt} \right)_{NN} \propto \left(\frac{E_a}{\overline{E}_{NN}^0} \right)^{\beta_{NN}} \exp \left[-(\beta_{NN} + 1) \frac{E_a}{\overline{E}_{NN}^0} \right]$$

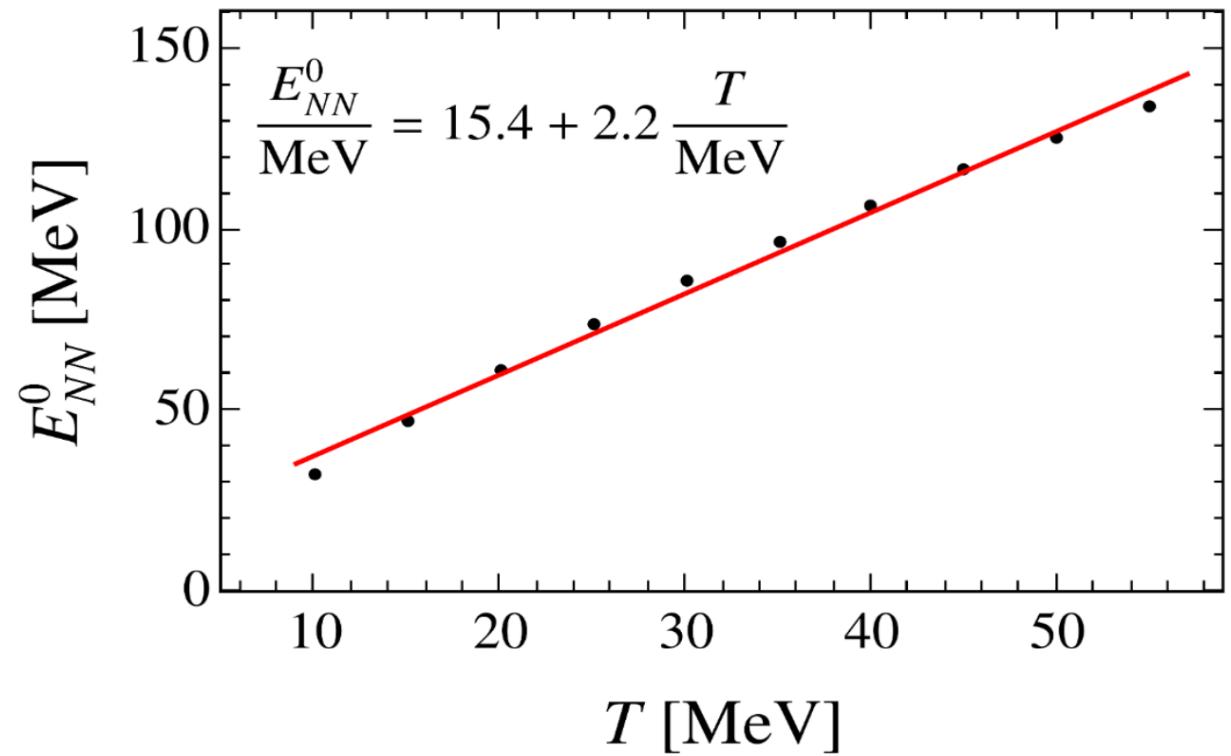
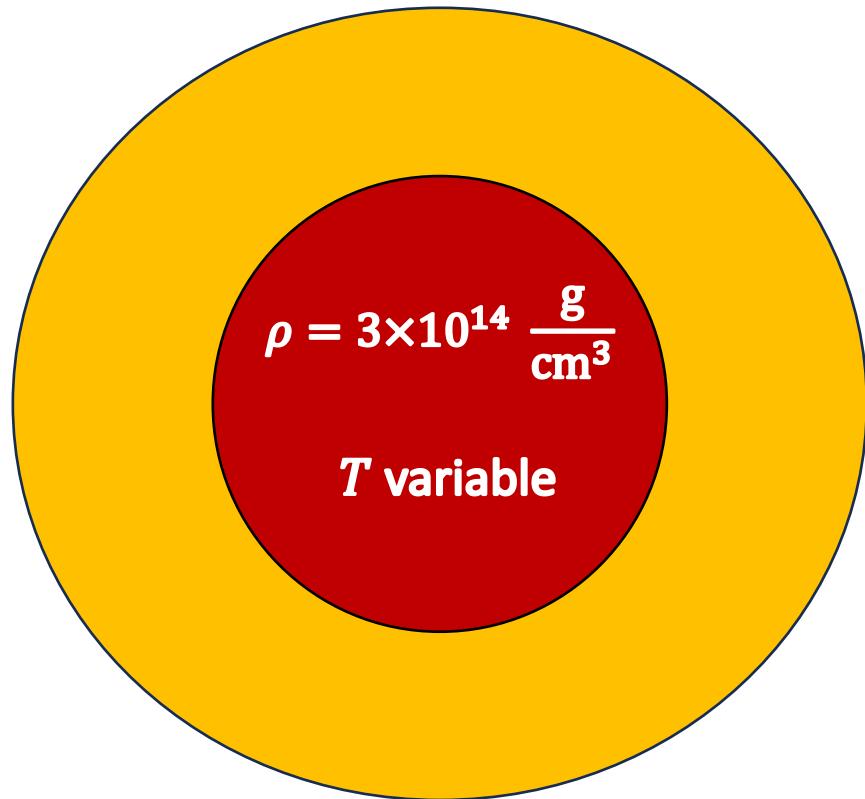
Bremsstrahlung is a thermal process $E_{NN}^0 \propto T$

ALPs emission spectra

Complex ALP spectra functional forms can be fitted employing α -fits [\[AL et al., e-Print: 2405.02395\]](#)

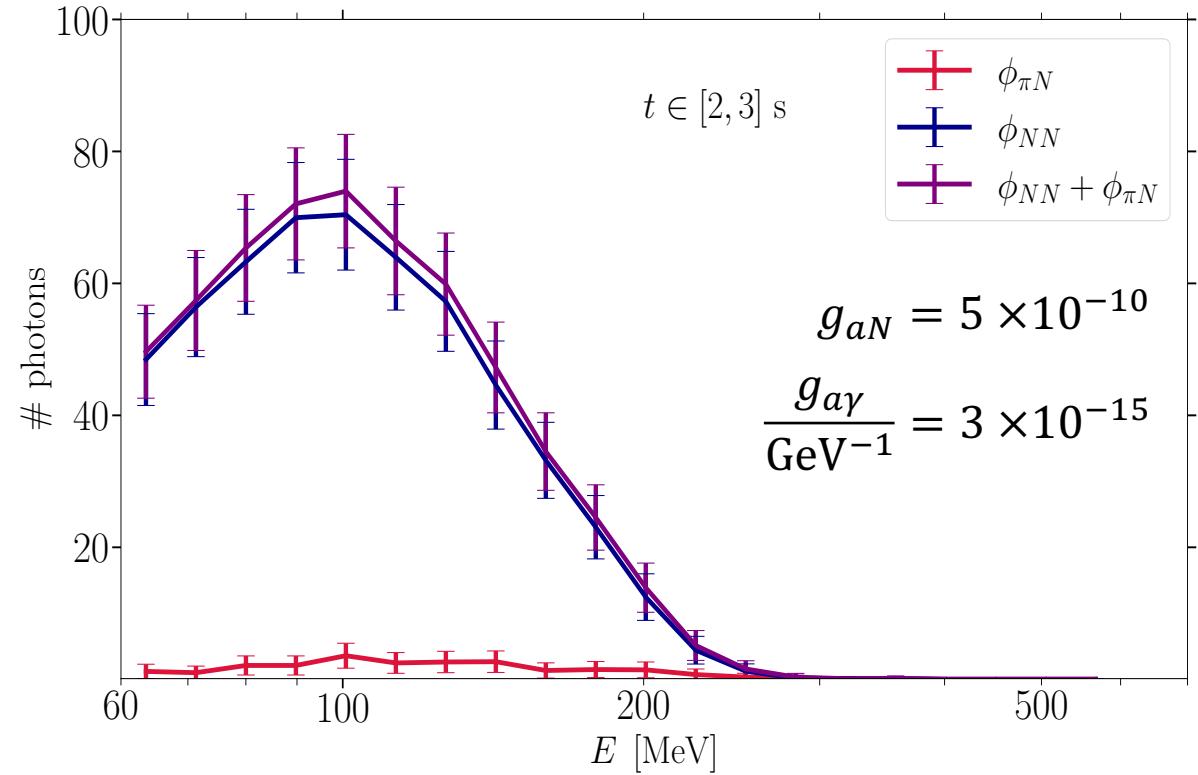
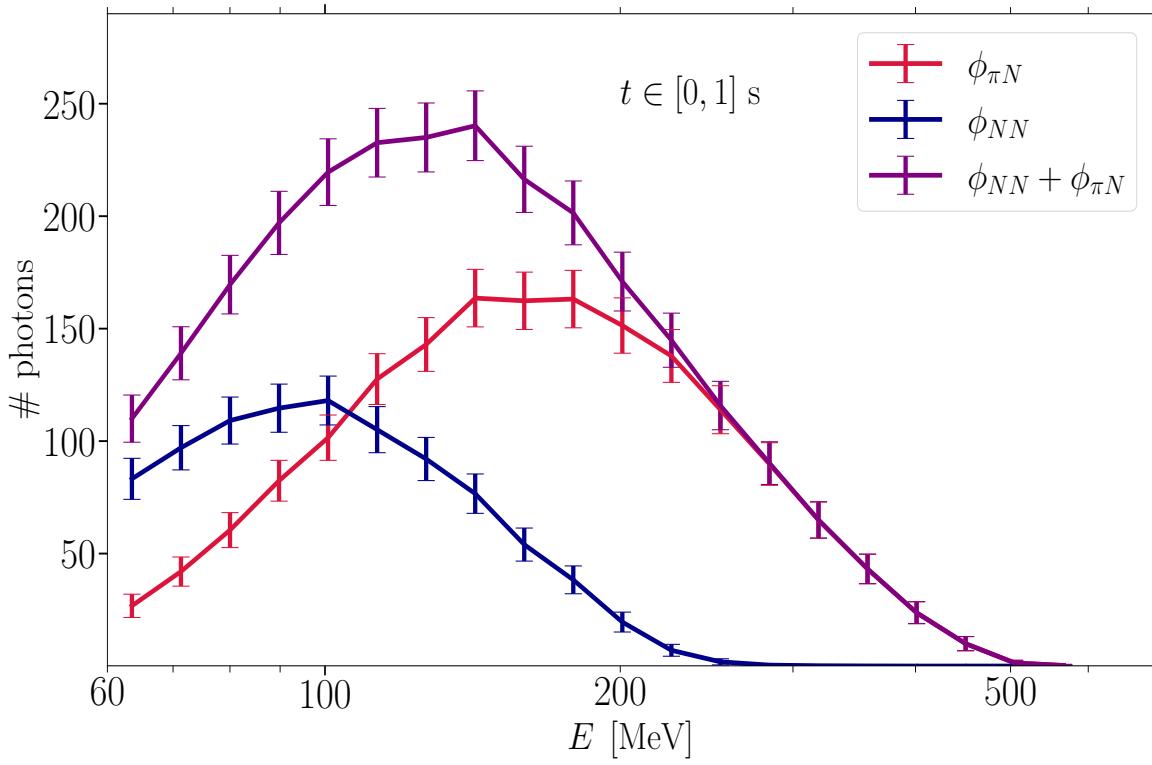
$$\left(\frac{d^2 N_a}{d E_a dt} \right)_{NN} \propto \left(\frac{E_a}{E_{NN}^0} \right)^{\beta_{NN}} \exp \left[-(\beta_{NN} + 1) \frac{E_a}{E_{NN}^0} \right]$$

Bremsstrahlung is a thermal process $E_{NN}^0 \propto T$



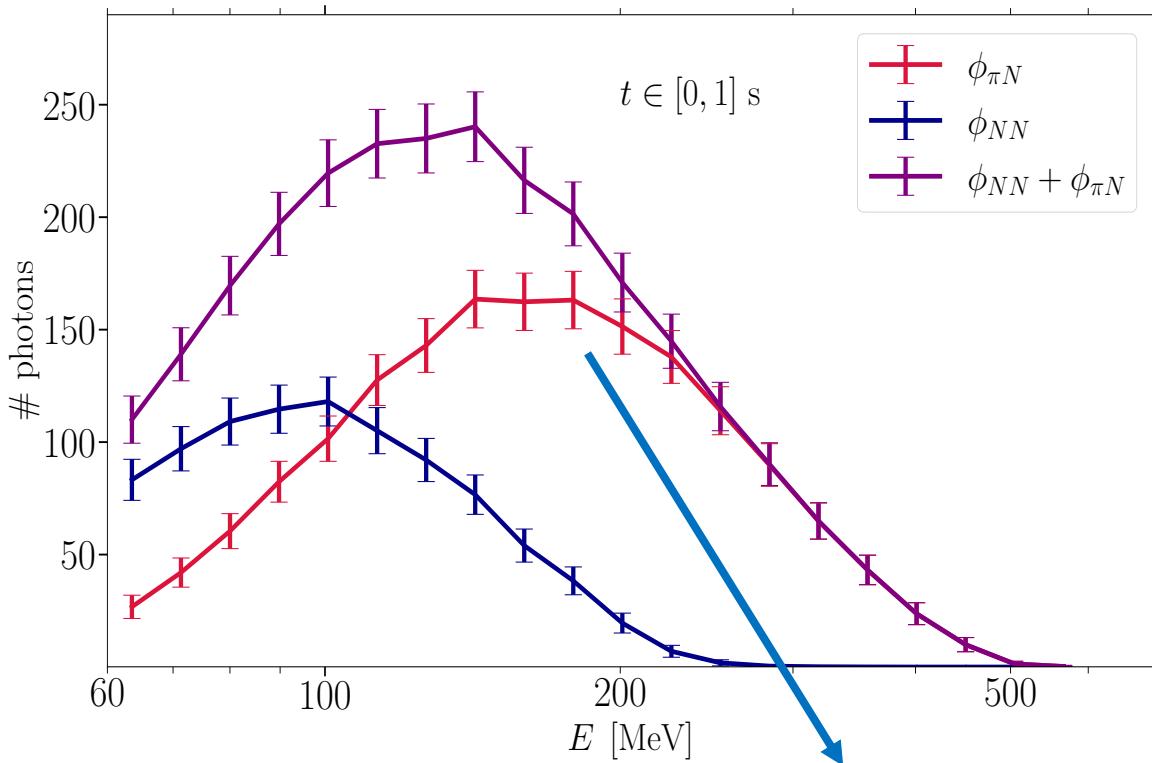
Fermi-LAT reconstruction of the signal

The expected SN ALP-induced gamma-ray signal simulated for 8 seconds with the Fermi Science Tools. $d_{SN} = 10$ kpc, $(l, b) = (199.79^\circ, -8.96^\circ)$. fermi.gsfc.nasa.gov/ssc/data/analysis/software/

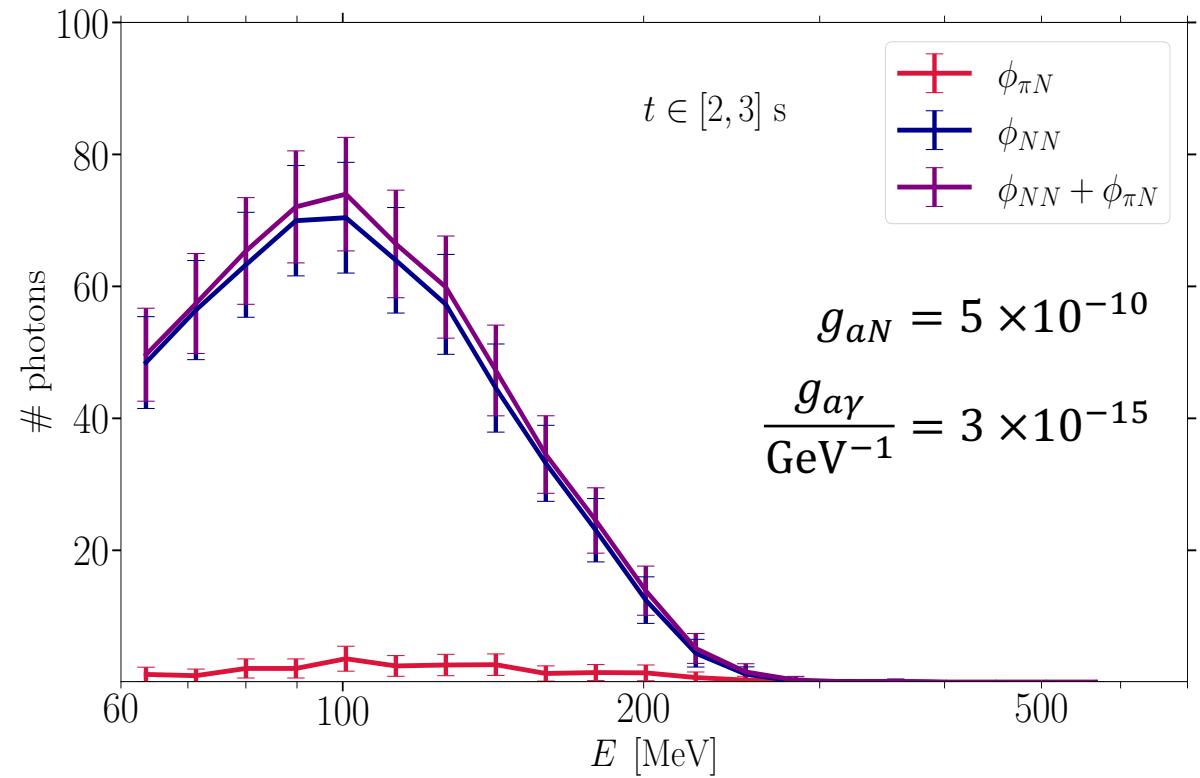


Fermi-LAT reconstruction of the signal

The expected SN ALP-induced gamma-ray signal simulated for 8 seconds with the Fermi Science Tools. $d_{SN} = 10$ kpc, $(l, b) = (199.79^\circ, -8.96^\circ)$. fermi.gsfc.nasa.gov/ssc/data/analysis/software/



Bayesian evidence for the presence of pions in the core

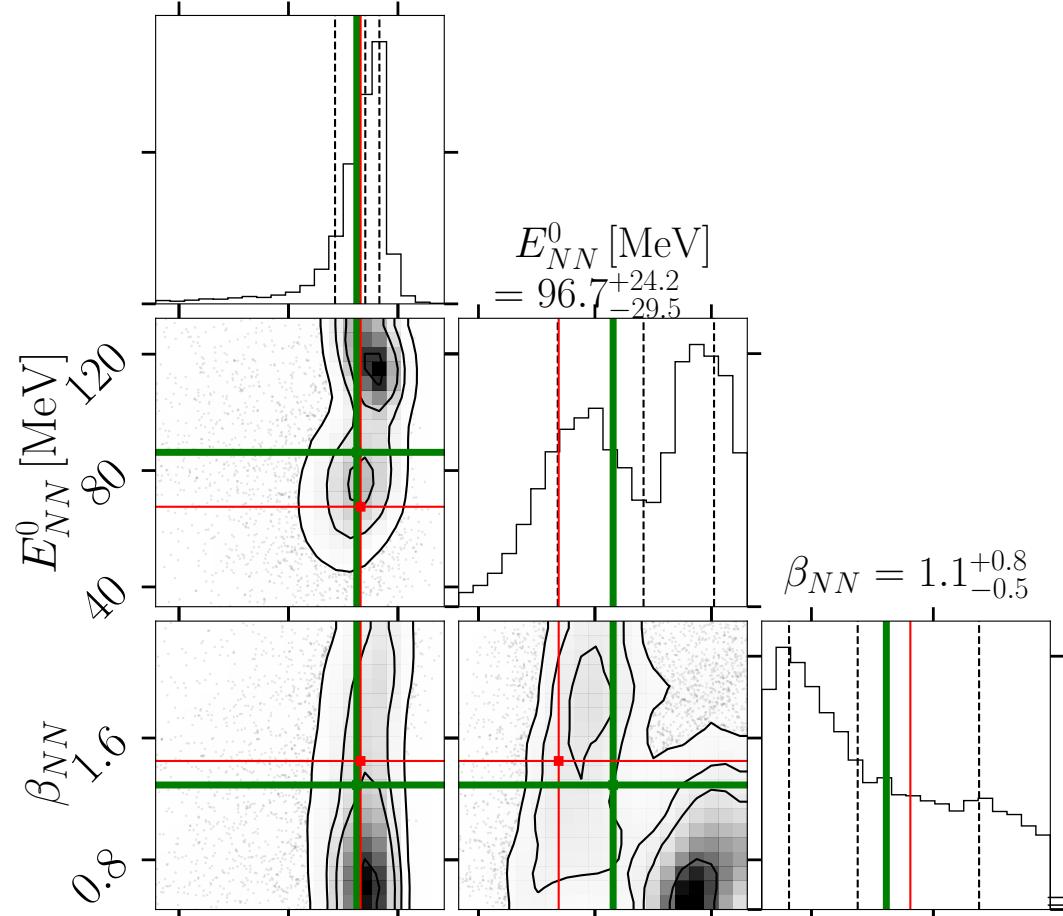


Suppression of πN peak at $t_{pb} > 2$ s.

Fermi-LAT reconstruction of the signal

Parameter reconstruction $NN + \pi N$

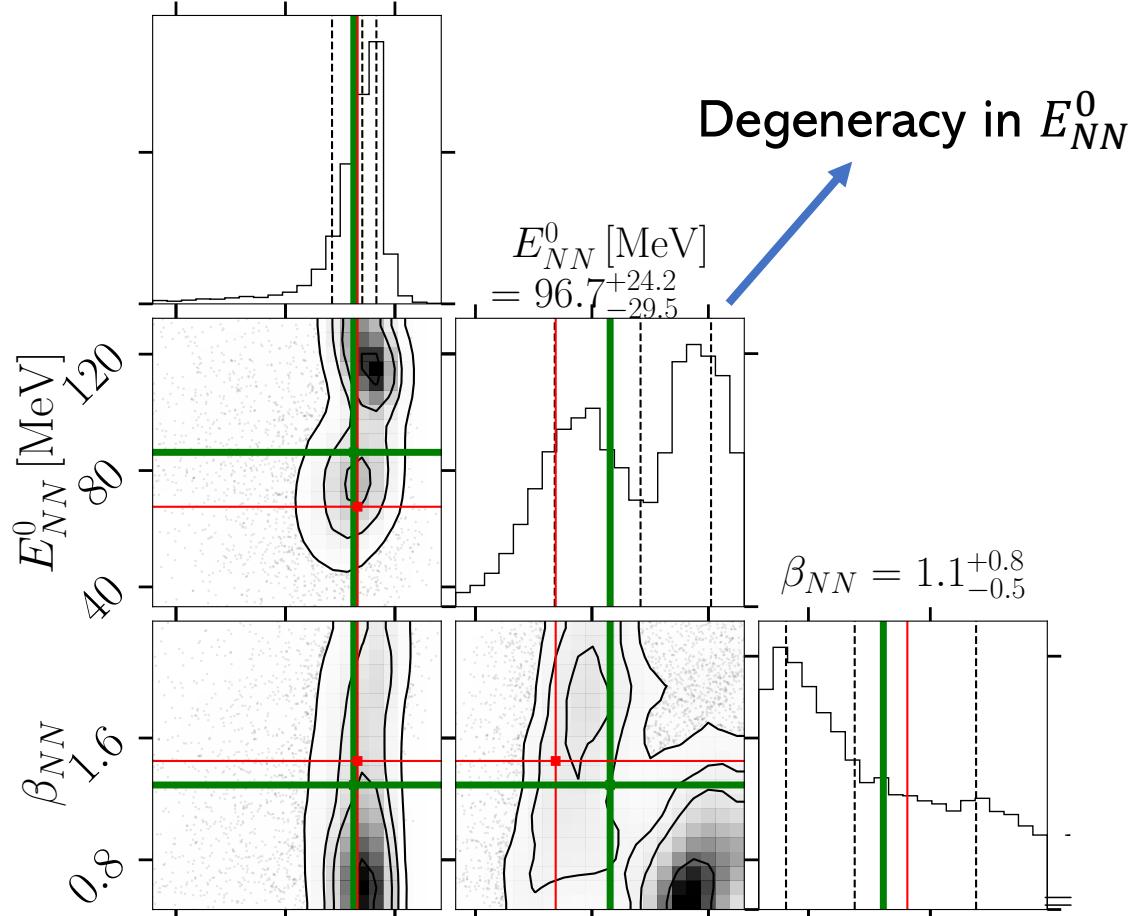
$$\log_{10}(A_{NN} \text{ MeV s}) = -0.3^{+0.1}_{-0.3}$$



Fermi-LAT reconstruction of the signal

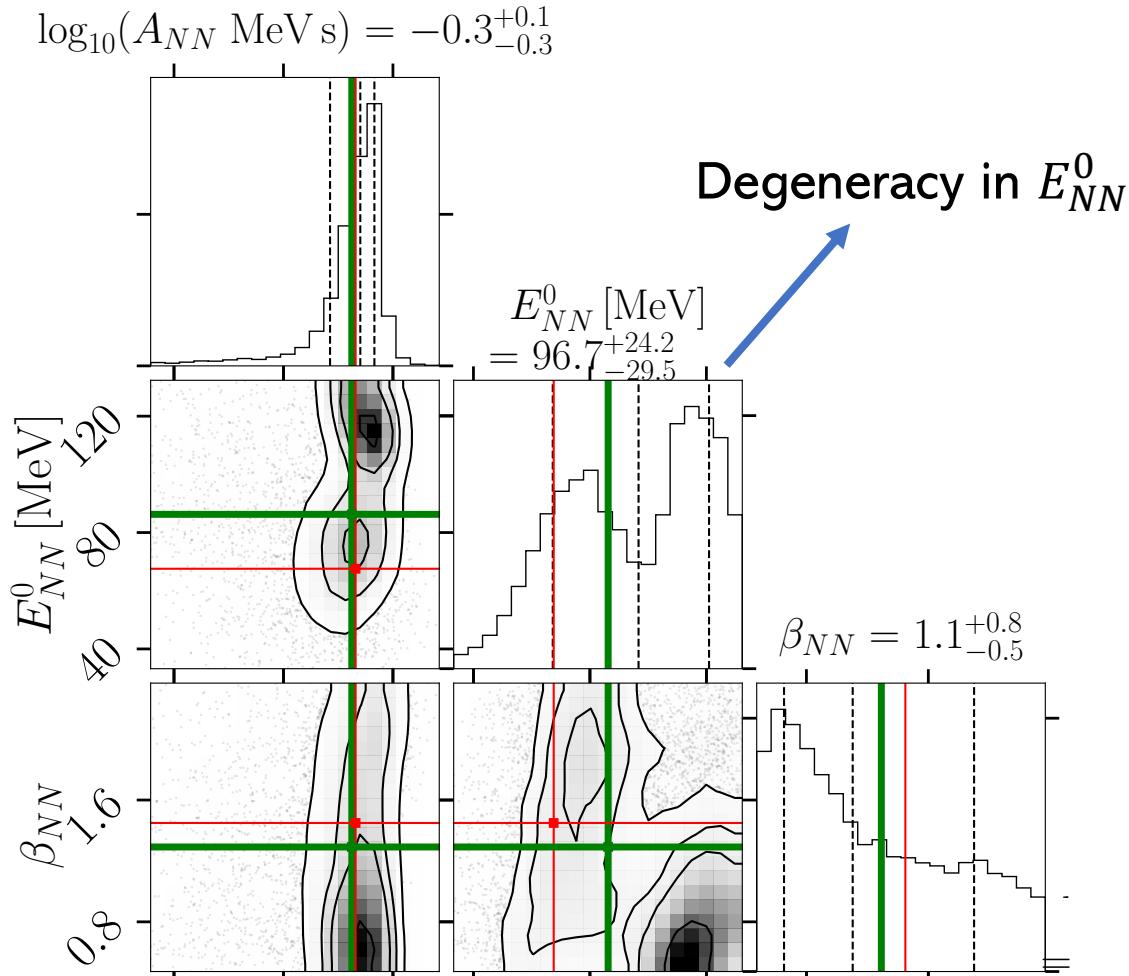
Parameter reconstruction $NN + \pi N$

$$\log_{10}(A_{NN} \text{ MeV s}) = -0.3^{+0.1}_{-0.3}$$

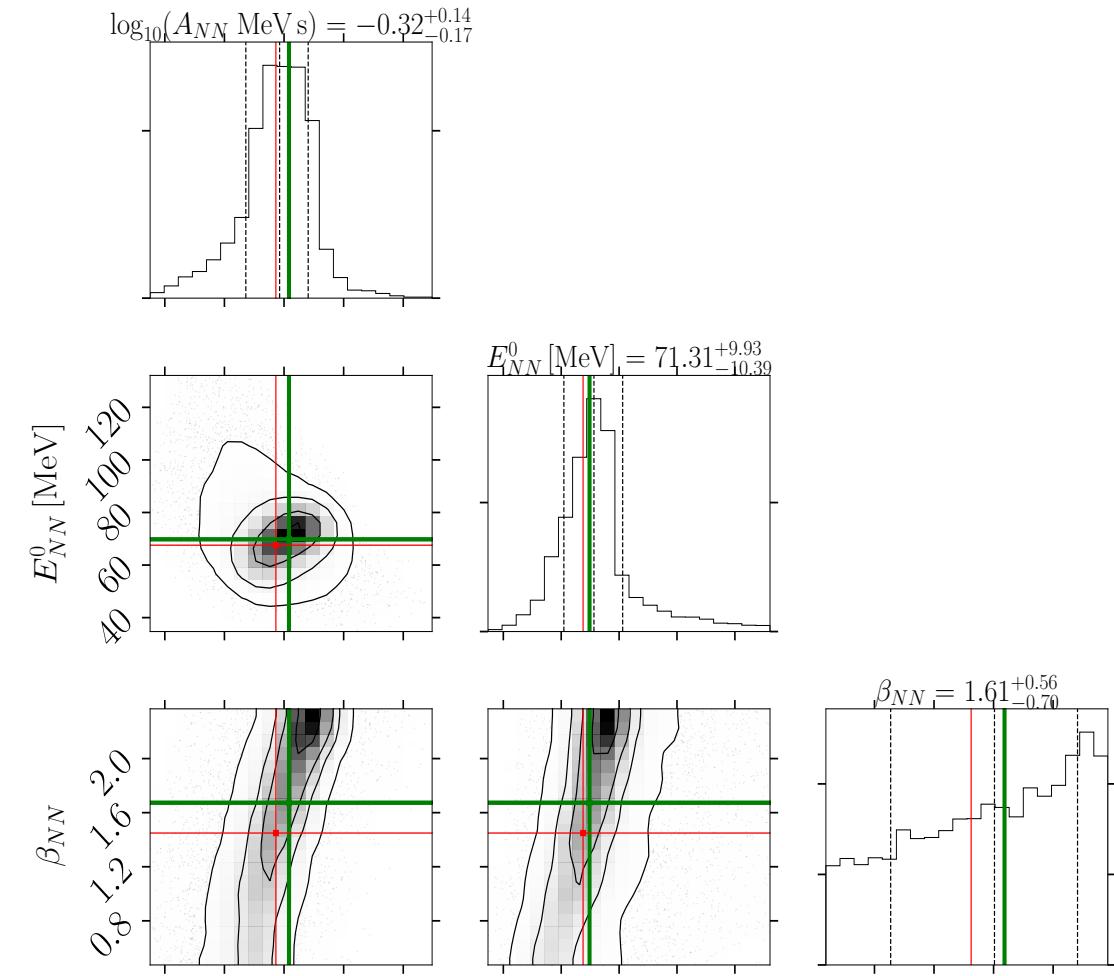


Fermi-LAT reconstruction of the signal

Parameter reconstruction $NN + \pi N$

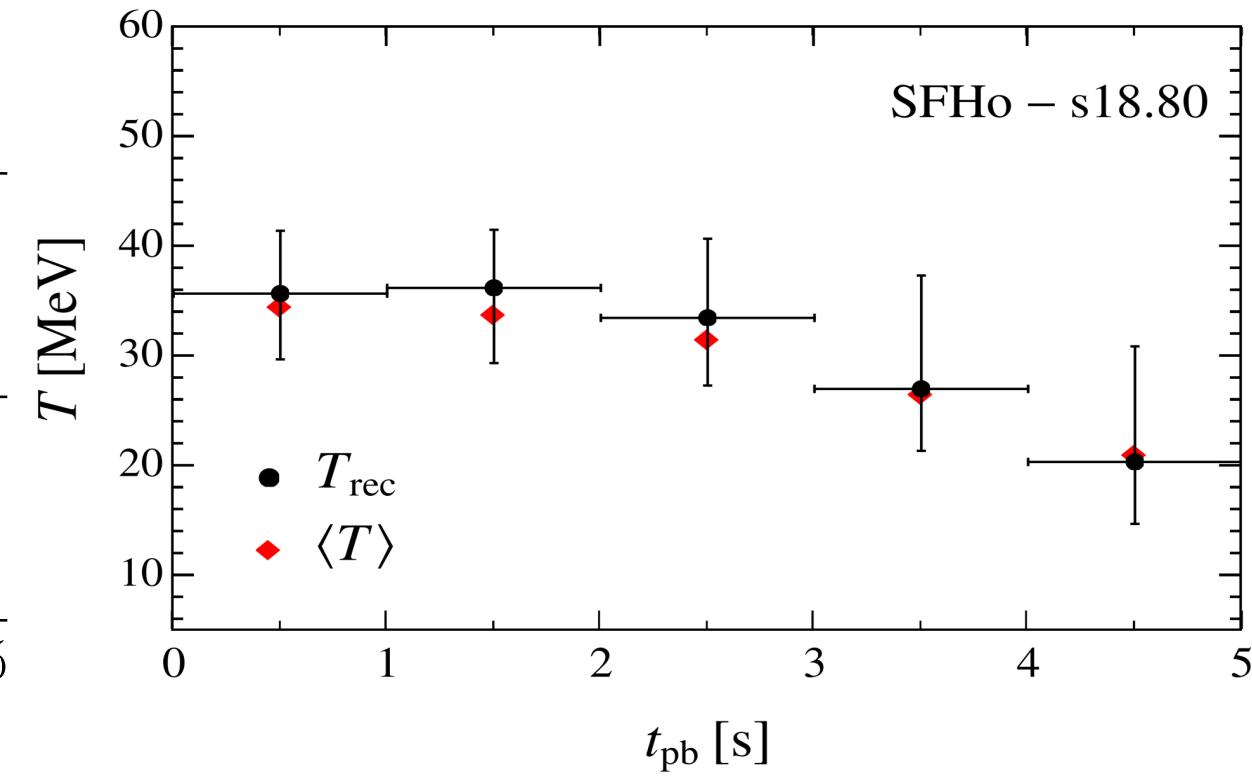
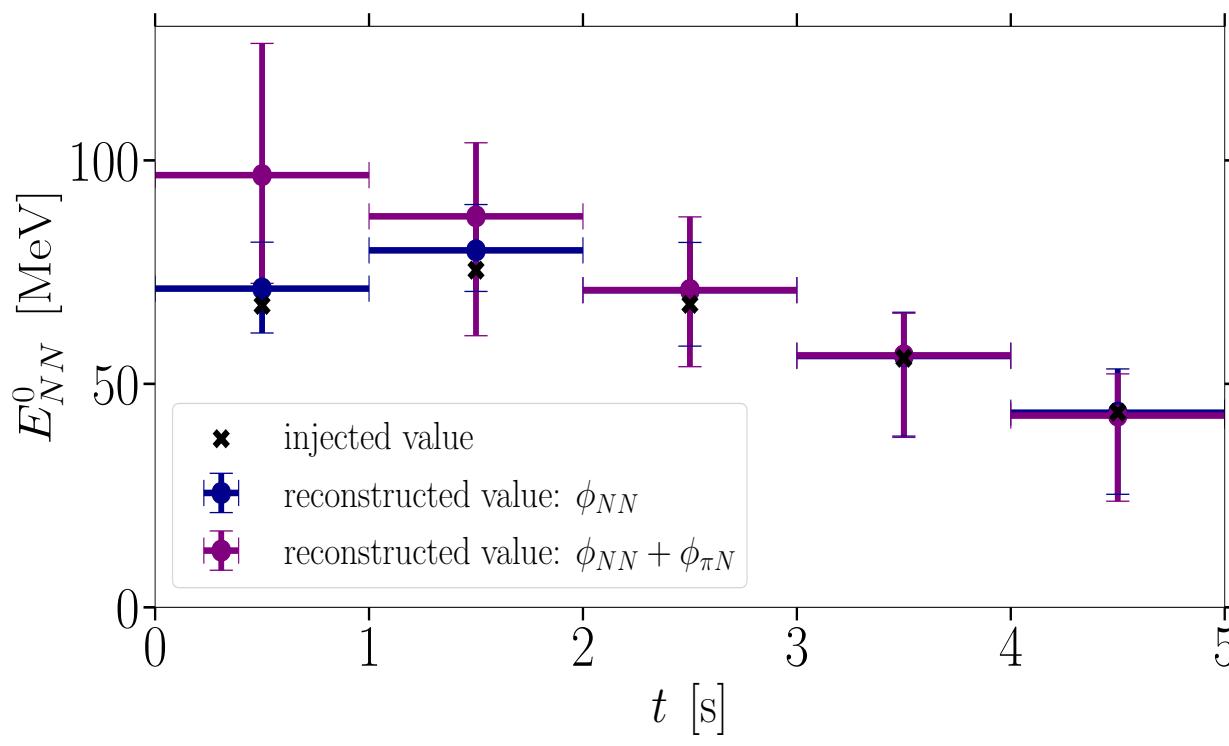


Parameter reconstruction only NN



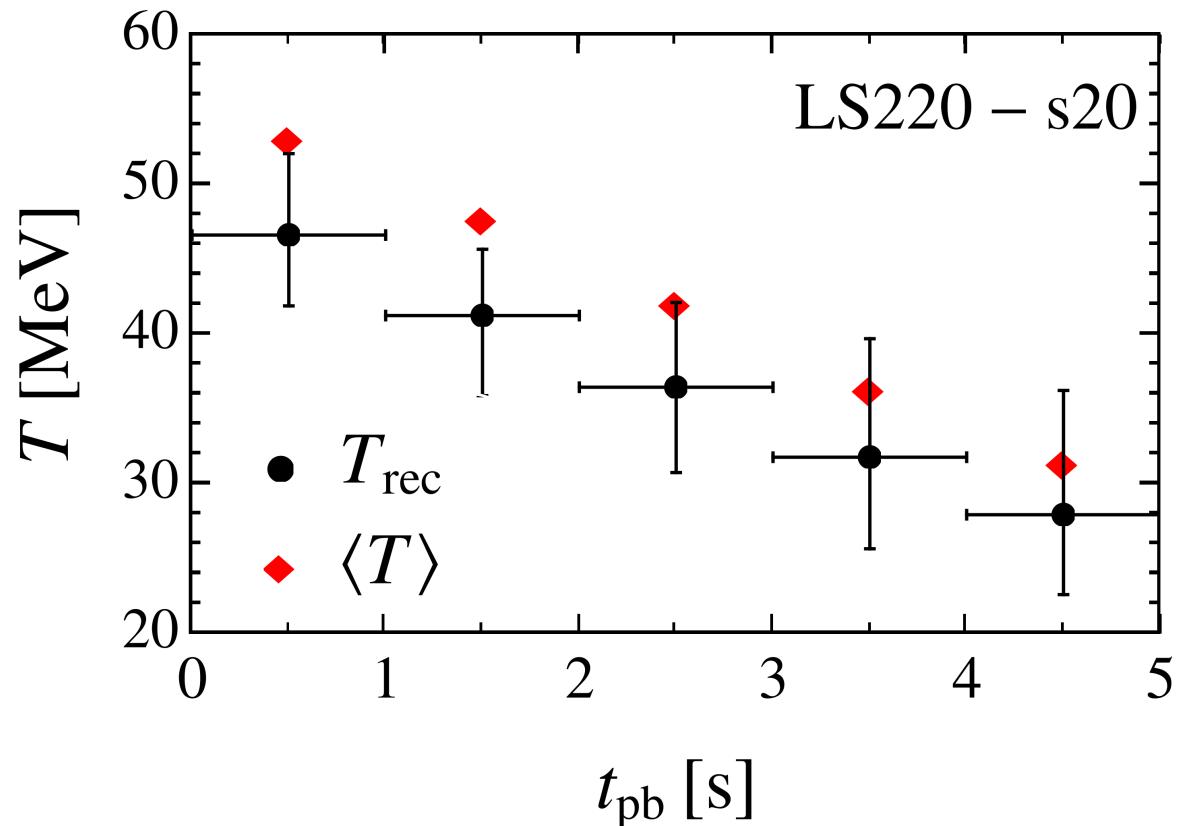
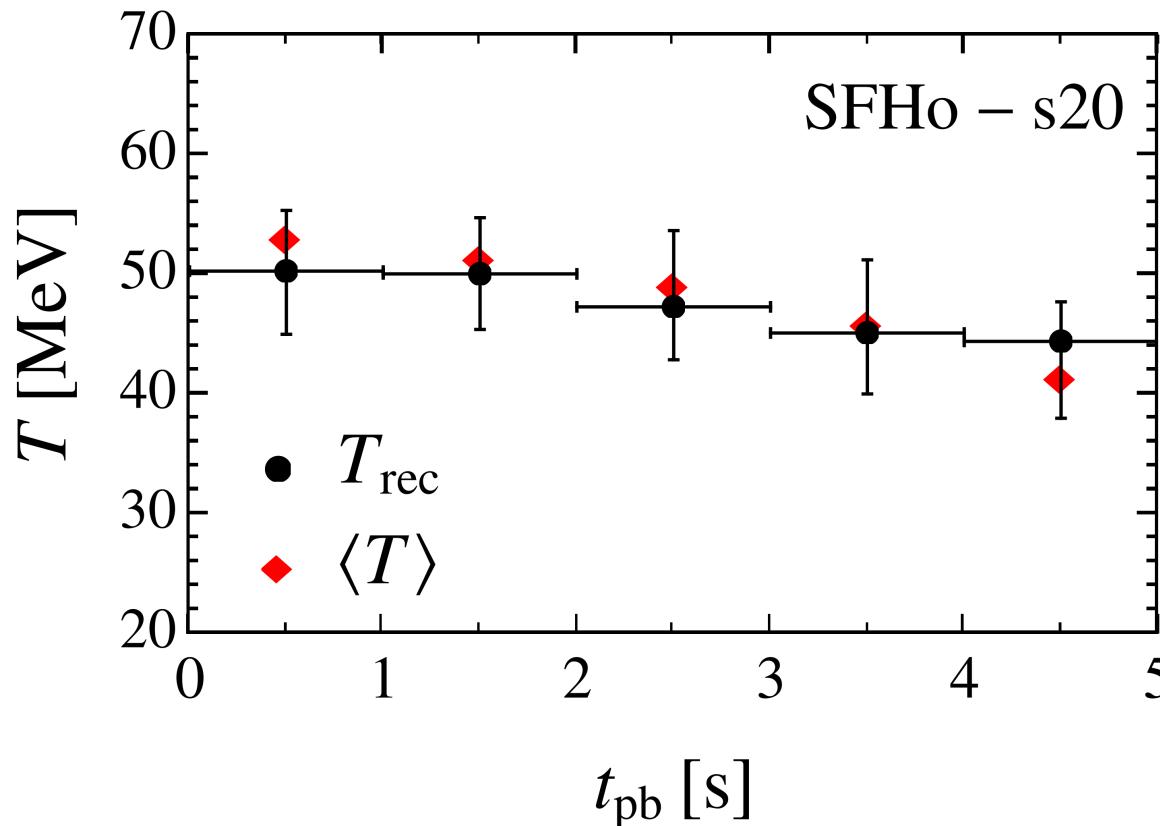
Fermi-LAT reconstruction of the signal

From parameter reconstruction one can estimate the average PNS temperature with high precision



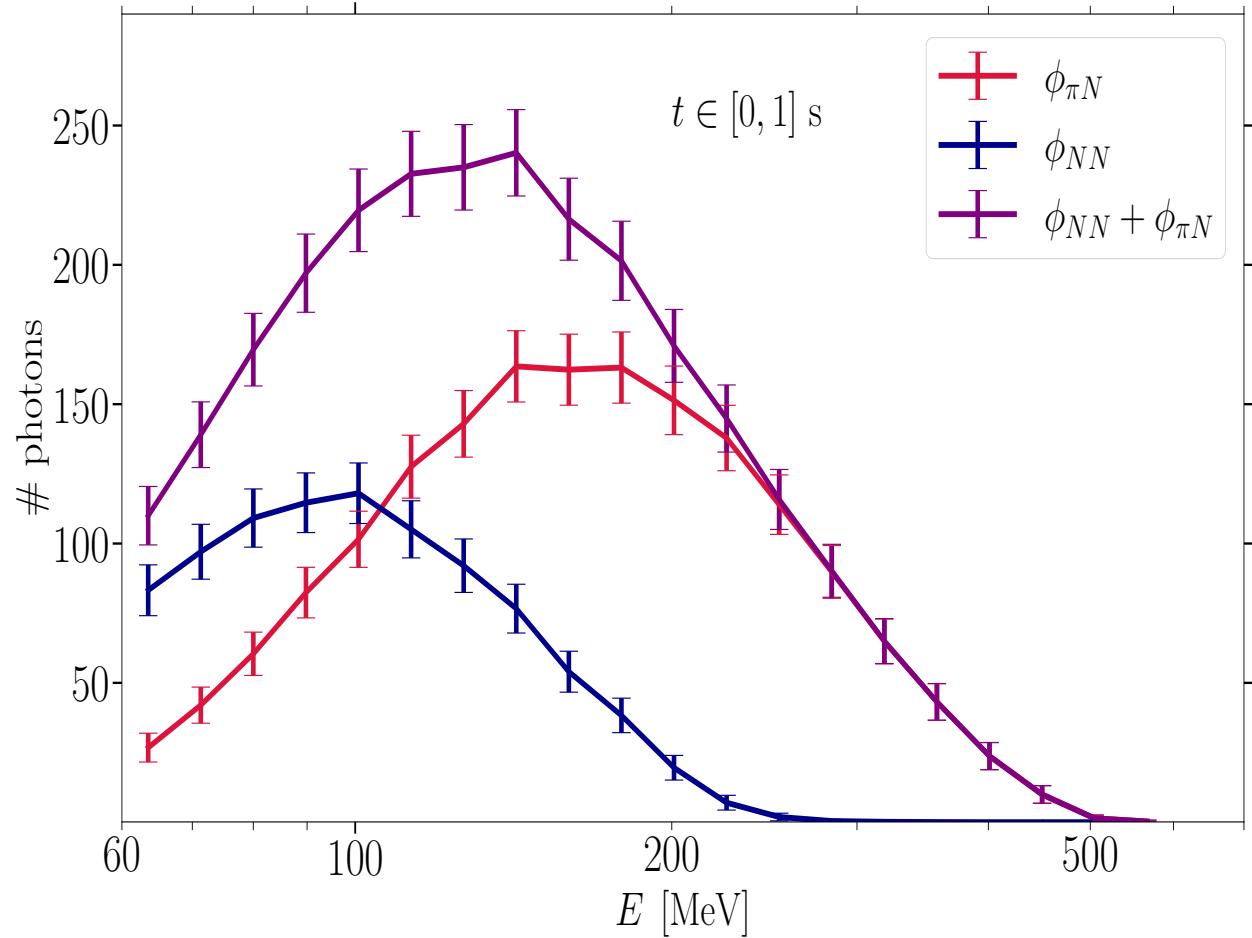
Fermi-LAT reconstruction of the signal

The procedure for temperature reconstruction has been applied also to SN models with different temperature profiles [$M_{PNS} \simeq 1.95 M_{\odot}$].



Take-home messages

- Ultralight ALPs could be copiously produced in SNe via nuclear processes.
- ALP production spectra encode many properties of the inner SN core.
- Fermi-LAT experiment able to reconstruct the ALP-induced signal
- ALPs as probes for SN pion abundance and PNS temperature.



A wide-angle photograph of a dark night sky. The Milky Way galaxy is visible in the upper center, appearing as a dense, glowing band of stars. Numerous smaller stars are scattered across the dark blue and black sky. In the lower right foreground, the silhouette of a large, leafless tree is visible against the lighter sky. The horizon shows a faint glow from distant lights or the setting sun.

Thank you for your
attention

ALP emission spectra

- If ALPs interact weakly with nuclear matter, they can *free-stream* through the SN volume

$$\frac{d^2 N_a}{d E_a dt} = \int_0^\infty 4\pi r^2 dr \frac{d^2 n_a}{d E_a dt}$$

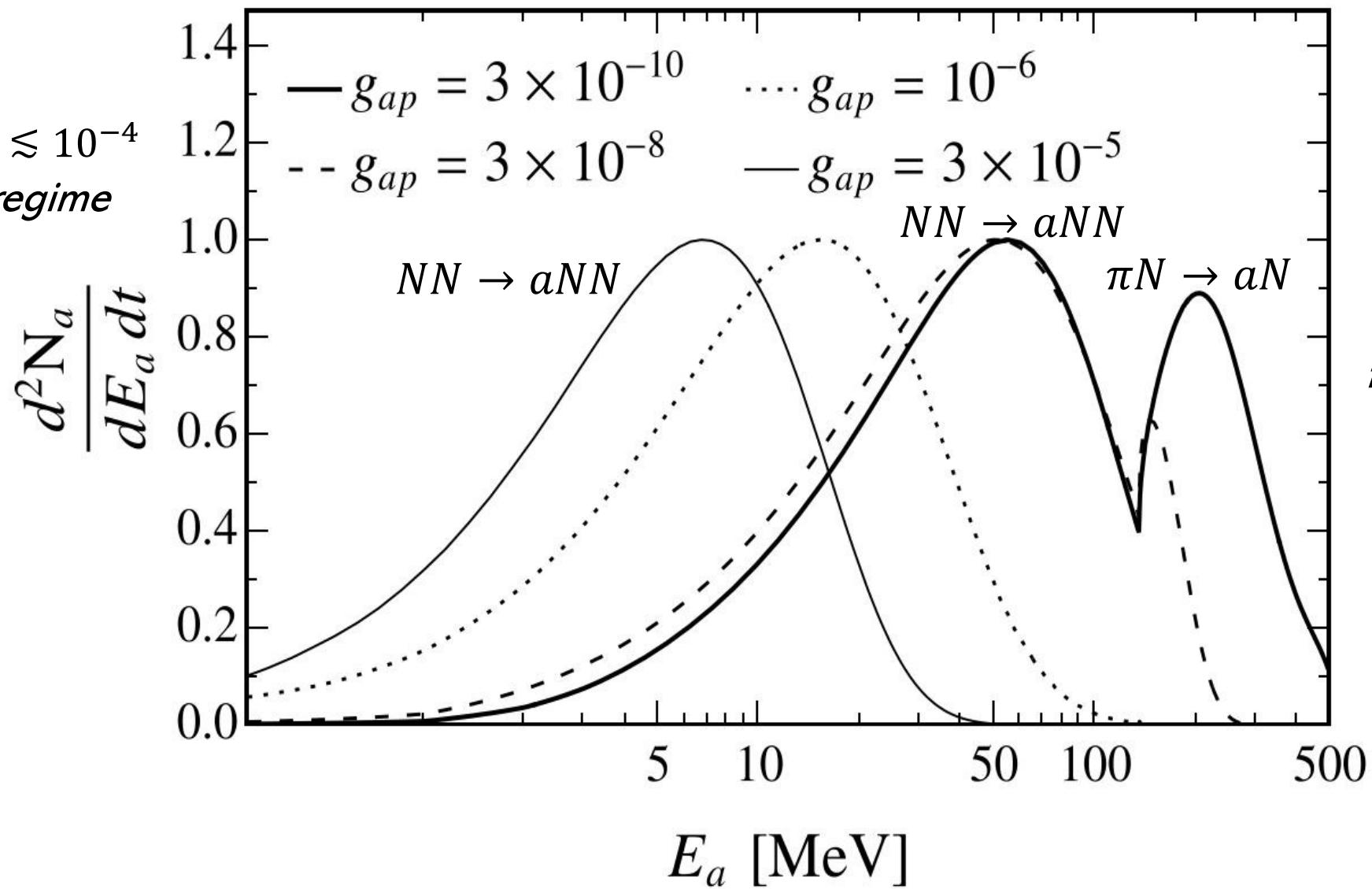
- In case of strongly coupled ALPs, they could enter the *Trapping regime*
[Caputo & al., Phys. Rev. D 105 (2022)]

$$\frac{d^2 N_a}{d E_a dt} = \int_0^\infty 4\pi r^2 dr \left\langle e^{-\tau(E_a, r)} \right\rangle \frac{d^2 n_a}{d E_a dt}$$

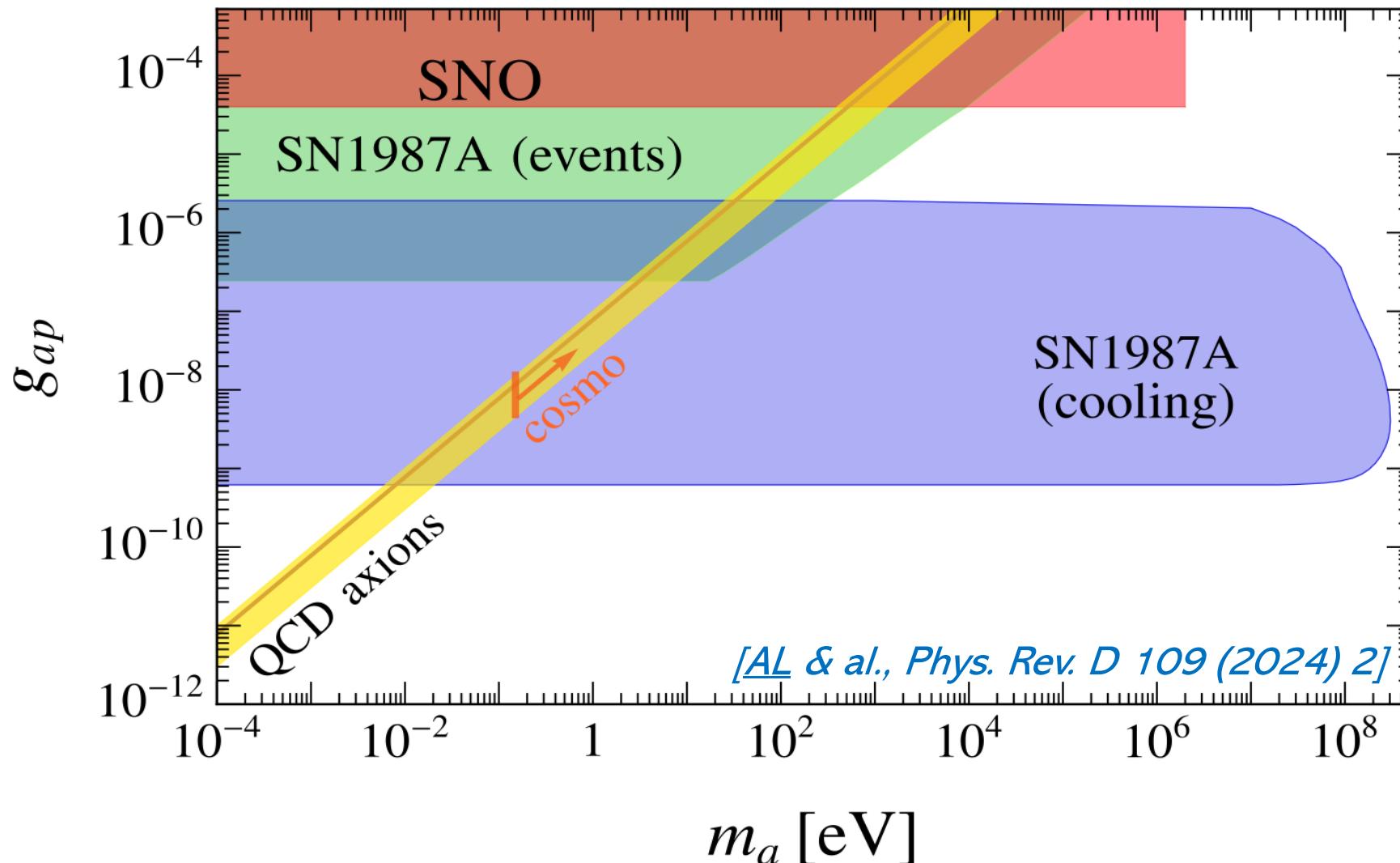
$$\tau \sim \int_0^\infty dr \lambda_a^{-1} \text{ optical depth for nuclear processes}$$

ALP emission spectra

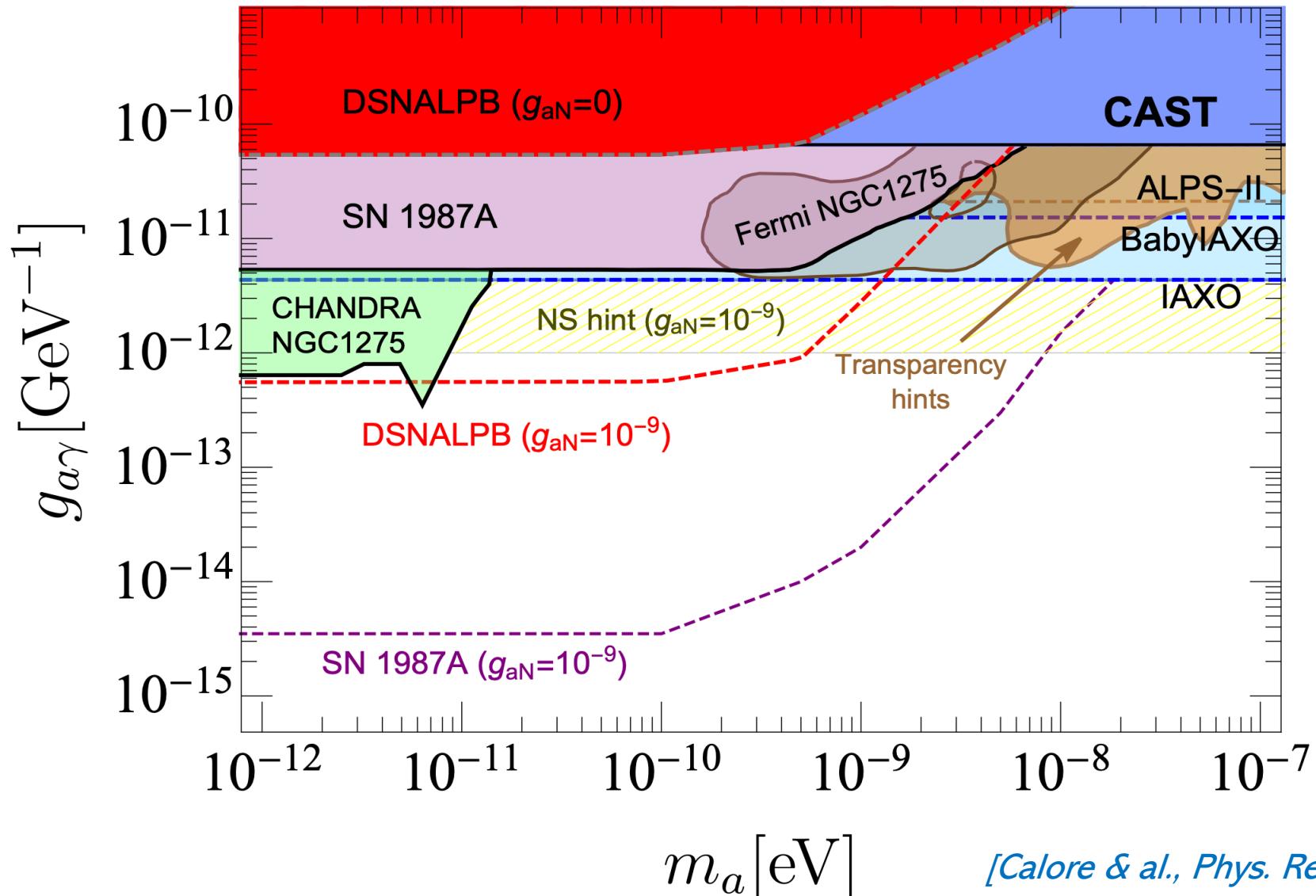
$10^{-7} \lesssim g_{ap} \lesssim 10^{-4}$
trapping regime



SN bounds on ALPs coupled to nucleons



SN bounds on ALPs coupled to nucleons



NN Bremsstrahlung emission rate

$$\left(\frac{d^2 n_a}{d\omega_a dt} \right)_{NN} = \frac{g_a^2}{16\pi^2} \frac{n_B}{m_N^2} (\omega_a^2 - m_a^2)^{\frac{3}{2}} \exp\left(-\frac{\omega_a}{T}\right) \\ \times S_\sigma\left(\frac{\omega_a}{T}\right) \Theta(\omega_a - m_a),$$

$$S_\sigma = \frac{\Gamma_\sigma}{\omega^2} s\left(\frac{\omega_a}{T}\right)$$

$$s(x) = s_{nn}(x) + s_{pp}(x) + s_{np}(x)$$

$$s_{nn}(x) = \frac{1}{3} Y_n^2 C_{an}^2 (s_{\mathbf{k}} + s_{\mathbf{l}} + s_{\mathbf{k}\mathbf{l}} - 3s_{\mathbf{k}\cdot\mathbf{l}})$$

$$s_{pp}(x) = \frac{1}{3} Y_p^2 C_{ap}^2 (s_{\mathbf{k}} + s_{\mathbf{l}} + s_{\mathbf{k}\mathbf{l}} - 3s_{\mathbf{k}\cdot\mathbf{l}})$$

$$s_{np}(x) = \frac{4}{3} Y_n Y_p (C_+^2 + C_-^2) s_{\mathbf{k}} + \frac{4}{3} Y_n Y_p (4C_+^2 + 2C_-^2) s_{\mathbf{l}} + \\ - \frac{8}{3} Y_n Y_p [(C_+^2 + C_-^2) s_{\mathbf{k}\mathbf{l}} - (3C_+^2 - C_-^2) s_{\mathbf{k}\cdot\mathbf{l}}].$$

$$s_{\mathbf{k}} = \int \frac{d\cos\delta}{2} \frac{d\phi}{2\pi} \frac{\sqrt{w}dw}{\frac{\sqrt{\pi}}{2}} \frac{dz}{2} du \left[\frac{\rho Y_1}{2m_N} \left(\frac{2\pi}{m_N T} \right)^{\frac{3}{2}} \right]^{-1} \left[\frac{\rho Y_2}{2m_N} \left(\frac{2\pi}{m_N T} \right)^{\frac{3}{2}} \right]^{-1} \\ e^{u-\eta_3} e^{w-\eta_4} \sqrt{u(u-x)} [H_u^+ H_u^- H_v^+ H_v^- F_+^2]_{v=u-x} \quad (3.49)$$

$$s_{\mathbf{l}} = \int \frac{d\cos\delta}{2} \frac{d\phi}{2\pi} \frac{\sqrt{w}dw}{\frac{\sqrt{\pi}}{2}} \frac{dz}{2} du \left[\frac{\rho Y_1}{2m_N} \left(\frac{2\pi}{m_N T} \right)^{\frac{3}{2}} \right]^{-1} \left[\frac{\rho Y_2}{2m_N} \left(\frac{2\pi}{m_N T} \right)^{\frac{3}{2}} \right]^{-1} \\ e^{u-\eta_3} e^{w-\eta_4} \sqrt{u(u-x)} [H_u^+ H_u^- H_v^+ H_v^- F_-^2]_{v=u-x} \quad (3.50)$$

$$s_{\mathbf{k}\mathbf{l}} = \int \frac{d\cos\delta}{2} \frac{d\phi}{2\pi} \frac{\sqrt{w}dw}{\frac{\sqrt{\pi}}{2}} \frac{dz}{2} du \left[\frac{\rho Y_1}{2m_N} \left(\frac{2\pi}{m_N T} \right)^{\frac{3}{2}} \right]^{-1} \left[\frac{\rho Y_2}{2m_N} \left(\frac{2\pi}{m_N T} \right)^{\frac{3}{2}} \right]^{-1} \\ e^{u-\eta_3} e^{w-\eta_4} \sqrt{u(u-x)} [H_u^+ H_u^- H_v^+ H_v^- F_+ F_-]_{v=u-x} \quad (3.51)$$

$$s_{\mathbf{k}\cdot\mathbf{l}} = \int \frac{d\cos\delta}{2} \frac{d\phi}{2\pi} \frac{\sqrt{w}dw}{\frac{\sqrt{\pi}}{2}} \frac{dz}{2} du \left[\frac{\rho Y_1}{2m_N} \left(\frac{2\pi}{m_N T} \right)^{\frac{3}{2}} \right]^{-1} \left[\frac{\rho Y_2}{2m_N} \left(\frac{2\pi}{m_N T} \right)^{\frac{3}{2}} \right]^{-1} \\ e^{u-\eta_3} e^{w-\eta_4} \sqrt{u(u-x)} \left[H_u^+ H_u^- H_v^+ H_v^- F_+ F_- \frac{\xi}{3} \right]_{v=u-x} \quad (3.52)$$

Pion conversion emission rate

$$\begin{aligned} \left(\frac{d^2 n_a}{d E_a dt} \right)_{N\pi} &= \frac{g_a^2 T^{1.5}}{2^{1.5} \pi^5 m_N^{0.5}} \left(\frac{g_A}{2 f_\pi} \right)^2 (E_a^2 - m_a^2)^{\frac{1}{2}} \\ &\times \mathcal{C}_a^{p\pi^-} \frac{\Theta(E_a - \max(m_a, m_\pi))}{\exp(x_a - y_\pi - \hat{\mu}_\pi) - 1} (E_a^2 - m_\pi^2)^{\frac{1}{2}} \frac{E_a^2}{E_a^2 + \Gamma^2} \\ &\times \int_0^\infty dy y^2 \frac{1}{\exp(y^2 - \hat{\mu}_p) + 1} \frac{1}{\exp(-y^2 + \hat{\mu}_n) + 1}, \end{aligned}$$

$$\mathcal{C}_a^{p\pi^-} = \frac{m_N^2}{g_A^2} \beta_a^2 \mathcal{G}_a(|\mathbf{p}_\pi|)$$

$$\begin{aligned} \mathcal{G}_a(|\mathbf{k}_\pi|) &= \frac{2g_A^2(2C_+^2 + C_-^2)}{3} \left(\frac{|\mathbf{k}_\pi|}{m_N} \right)^2 + C_{a\pi N}^2 \left(\frac{E_\pi}{m_N} \right)^2 + \frac{8\sqrt{2}g_A C_{a\pi N} C_-}{3} \left(\frac{|\mathbf{k}_\pi|}{m_N} \right)^2 \left(\frac{E_\pi}{m_N} \right) \\ &+ \frac{4C_{aN\Delta}^2 \mathcal{C}^2}{81} \frac{E_\pi^2 (\Delta m^2 + 2E_\pi^2 + \bar{\Gamma}_\Delta^2)}{[(\Delta m - E_\pi)^2 + \bar{\Gamma}_\Delta^2] [(\Delta m + E_\pi)^2 + \bar{\Gamma}_\Delta^2]} \left(\frac{|\mathbf{k}_\pi|}{m_N} \right)^2 \\ &- \frac{8\sqrt{3}g_A C_{aN\Delta} \mathcal{C} E_\pi}{27} \frac{[(\Delta m^2 - E_\pi^2)(C_+ \Delta m + C_- E_\pi) + \bar{\Gamma}_\Delta^2 (C_+ \Delta m - C_- E_\pi)]}{[(\Delta m - E_\pi)^2 + \bar{\Gamma}_\Delta^2] [(\Delta m + E_\pi)^2 + \bar{\Gamma}_\Delta^2]} \left(\frac{|\mathbf{k}_\pi|}{m_N} \right)^2 \\ &- \frac{16\sqrt{6}C_{a\pi N} C_{aN\Delta} \mathcal{C}}{27} \frac{E_\pi^2 (\Delta m^2 - E_\pi^2 - \bar{\Gamma}_\Delta^2)}{[(\Delta m - E_\pi)^2 + \bar{\Gamma}_\Delta^2] [(\Delta m + E_\pi)^2 + \bar{\Gamma}_\Delta^2]} \left(\frac{|\mathbf{k}_\pi|}{m_N} \right)^2 \left(\frac{E_\pi}{m_N} \right) \quad (39) \end{aligned}$$

The UV theory

Above $\Lambda_{QCD} \simeq 200$ MeV interactions with quark and gluons

$$\mathcal{L}_{\text{aQCD}} = c_g \frac{g_s^2}{32\pi^2} \frac{a}{f_a} G_{\mu\nu}^a \tilde{G}^{a\mu\nu} + \sum_q c_q \frac{\partial_\mu a}{2f_a} \bar{q} \gamma^\mu \gamma_5 q + \frac{(m_{a,0})^2}{2} a^2$$

Then, at loop level [Bauer et al., JHEP 12 (2017)]

$$C_\gamma(c_g, c_u, c_d) = -1.92 c_g - \frac{m_a^2}{m_\pi^2 - m_a^2} \left[c_g \frac{m_d - m_u}{m_d + m_u} + (c_u - c_d) \right]$$

Irreducible photon coupling related to nuclear couplings ($C_n = 0, c_g = 1$)

$$g_{a\gamma} \simeq -9.5 \times 10^{-4} \text{ GeV}^{-1} \left[\frac{1.53}{c_d - 0.33} + \frac{c_d + 0.24}{c_d - 0.33} \frac{m_a^2}{m_\pi^2 - m_a^2} \right] g_{ap}$$

Time-behavior of fitting parameters

