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Sensitivity to WIMP-like Dark Matter

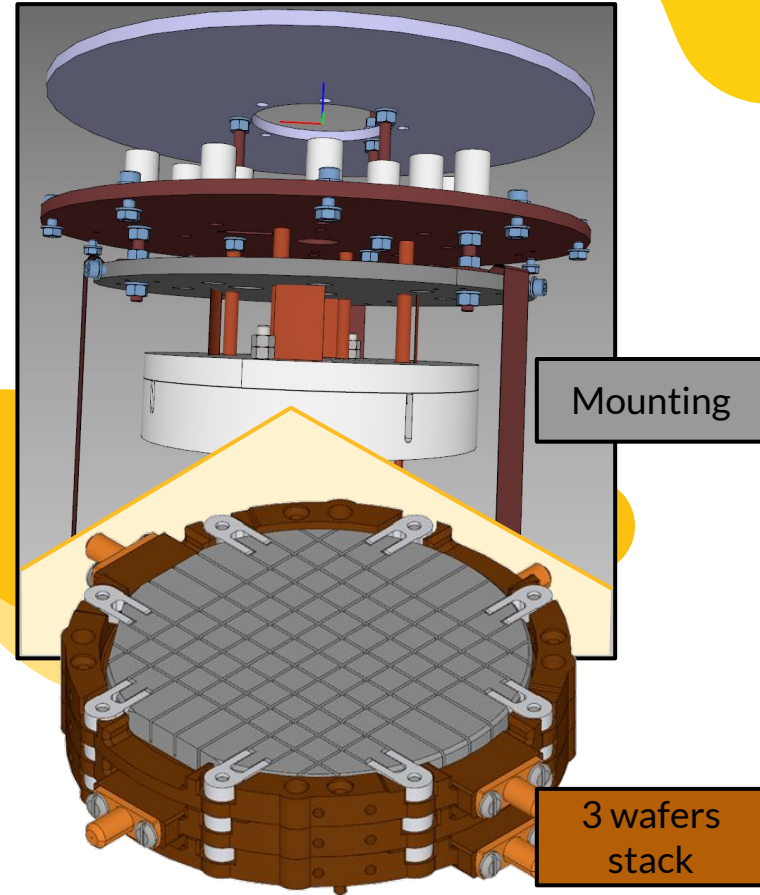
BULLKID-DM Meeting
March 19-20, 2024 LNGS

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Outline of the presentation

- Very brief introduction to WIMP Dark Matter
- Direct dark matter detection
- What is a dark matter exclusion plot
- State of the art in DM direct research
- Yellin method: working principle
- Yellin method: reproducing CRESST limits
- Sensitivity plots: Demonstrator & BULLKID-DM
- Toward a Bayesian credibility interval
- Conclusions

- References
- Backup slides



Introduction to dark matter

Dark matter (DM) is an elusive form of matter that doesn't interact with electromagnetic radiation

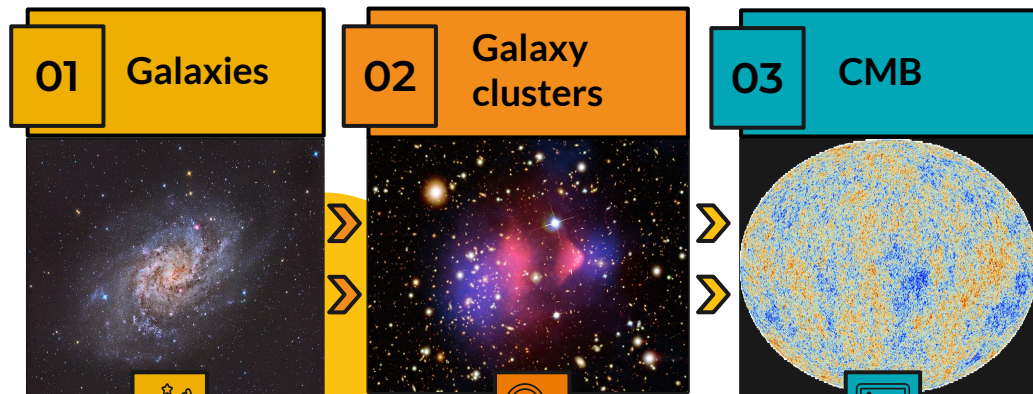
5 %
Ordinary matter

27%
Dark matter

68%
Dark energy

We have only gravitational hints of its existence

Larger scales

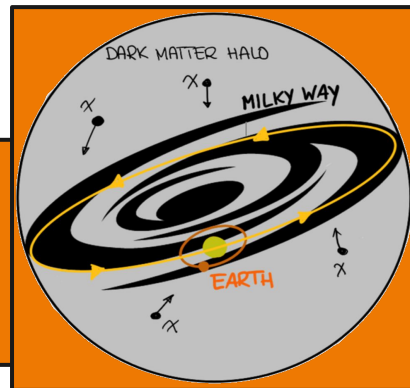


Cold Weakly interacting massive particles (WIMPs) in the GeV-TeV mass range could explain the DM abundance, and also they fit well in theories for physics beyond the Standard Model.

Dark matter direct detection

Direct detection aims to observe the transferred energy-momentum of WIMP particles scattering with **ordinary matter nuclei**.

We assume a DM distribution surrounding our Milky Way. The solar system is traveling in this halo hitting a DM wind coming from the Cygnus constellation.



$$E = 2 \frac{\mu^2}{m_N} v^2 \cos^2(\theta)$$

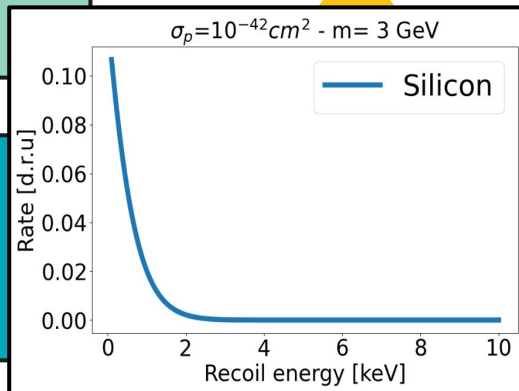
$$E \ll 1 \text{ keV}$$

$$\frac{dR}{dE} \sim \frac{R_0}{E_0} \exp\left(-\frac{E}{E_0}\right)$$

Order of
(1 evn/kg/yr)

$$\rho(\mathcal{R}_o) = 0.3 \text{ GeV/cm}^3 \quad v_C(\mathcal{R}_o) = 220 \text{ km/s}$$

Expected a low rate of interactions with an exponentially decreasing energy spectrum



Exclusion bounds

Even nothing means something

Until we find evidences of DM, we can set exclusion limits

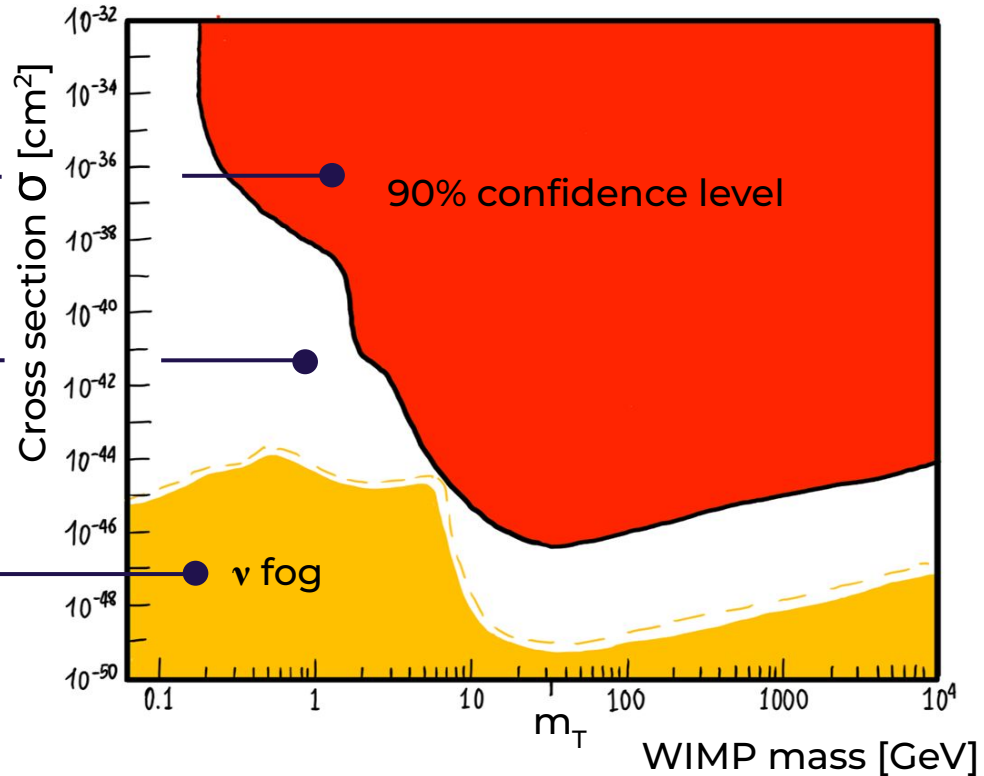
■ Excluded region

□ Still motivated region

■ Atmospheric and solar neutrinos constitute irreducible background with a rate comparable to WIMP-DM

Going down requires more exposure

Going left requires lower energy threshold



Exclusion bounds

State of the art

Until we find evidences of DM, we can set exclusion limits

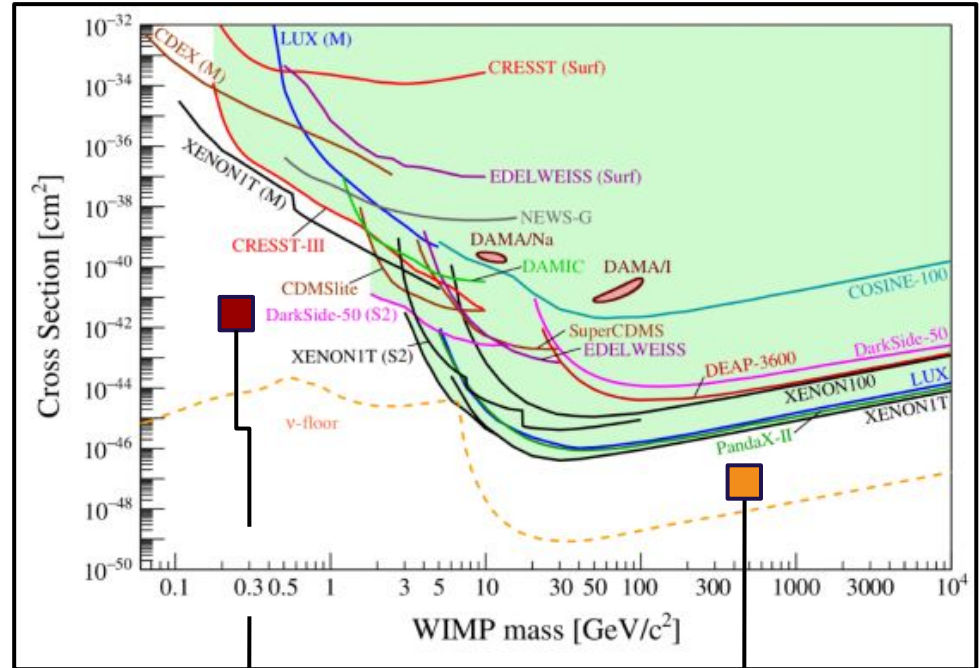
■ Excluded region

□ Still motivated region

■ Atmospheric and solar neutrinos constitute irreducible background with a rate comparable to WIMP-DM

Going down requires more exposure

Going left requires lower energy threshold



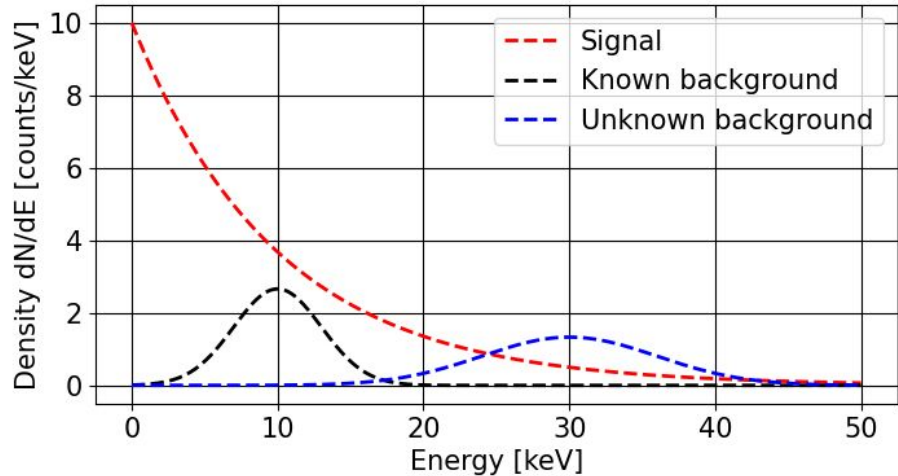
Sub-GeV range still mostly unexplored even if still theoretically valuable

High WIMP masses largely excluded by multi-ton liquid scintillators

Yellin's optimum interval method

“The optimum interval method produces a true, though possibly conservative, classical (frequentist) confidence interval” [1]

It works even in presence of a too poorly understood background contaminating the data, putting a stronger limit than would be possible if it were ignored”

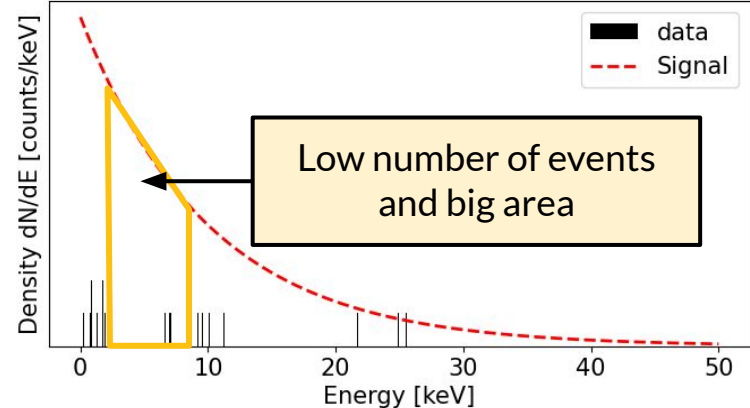


Working principle

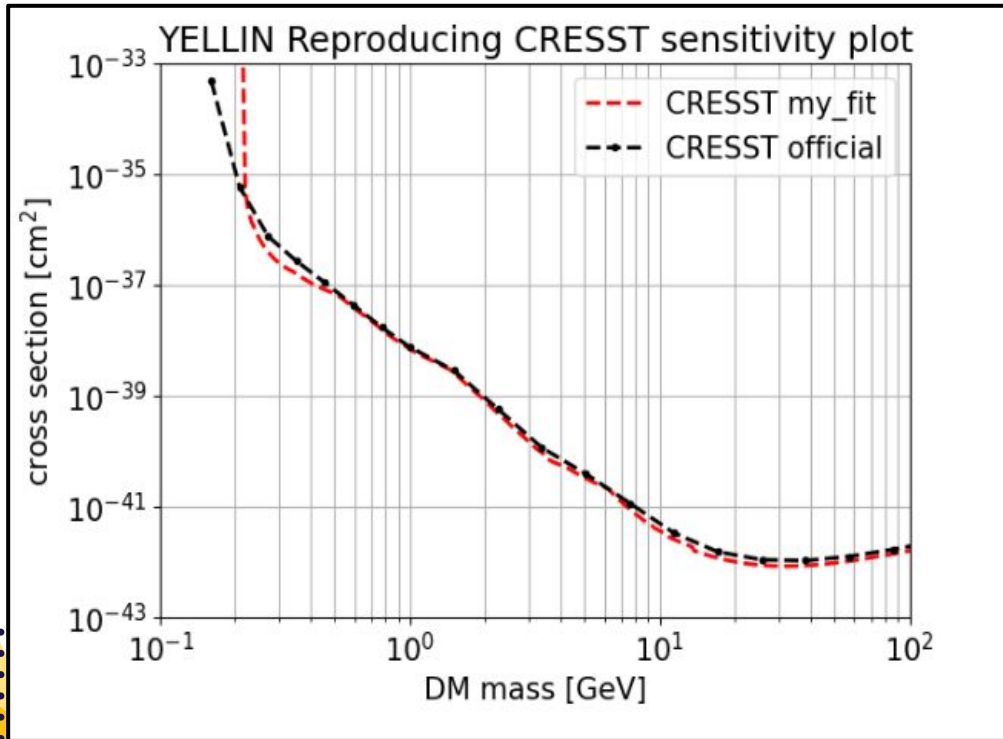
The energy ranges with less recorded events should also be the ranges less affected by the unknown background.

Hence I put the limit in one of such ranges where, on the other hand, I expect to see more signal.

The limit can be estimated through the use of a MC toy.

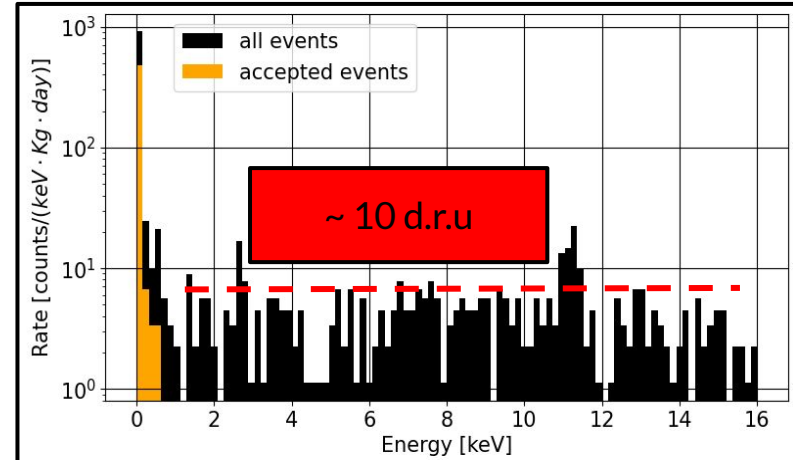


Reproducing CRESST results



The differences between the two curves are believed to be due to a different algorithm for evaluating the WIMP rate

One of the main reasons we adopt Yellin's method is the fact that the CRESST experiment adopts it for its limits



CRESST experimental settings [2]

ROI: [0.0301, 16] keV Resolution: ~ 46 eV

Exposure: 0.015 kg Y

Efficiency: ~50% + efficiency of the cuts

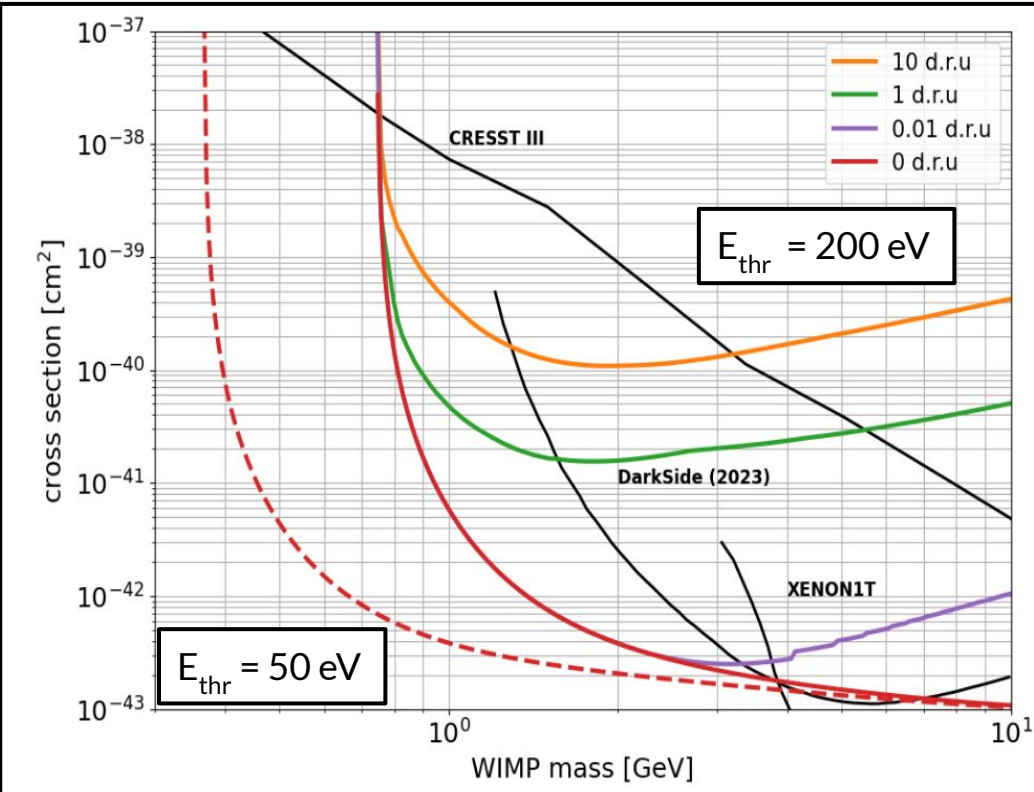
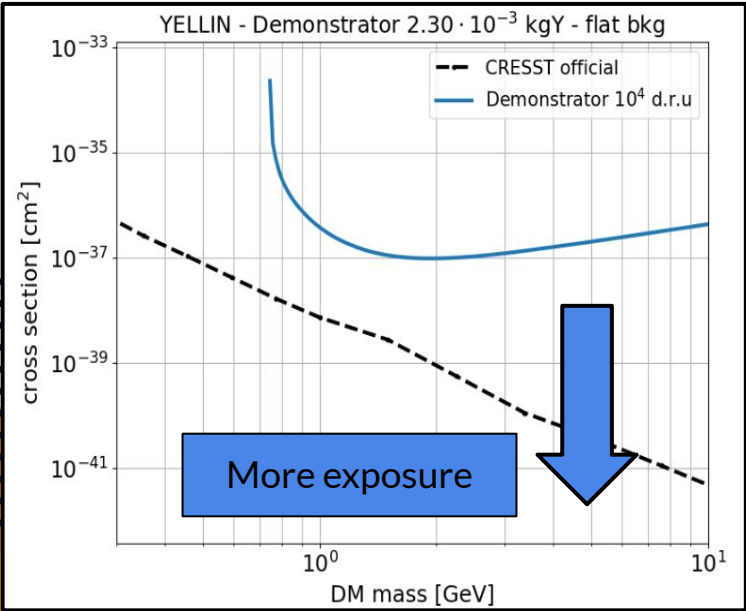
Target material: CaWO_4

Rate: ~ 10 d.r.u

BULLKID sensitivity plots

Demonstrator - Flat background
ROI : [0.2, 16] keV Target material: Silicon
Time: 2 weeks Target mass: 0.06 Kg

BULLKID-DM - Flat background at different rates
ROI : [E_{thr} , 16] keV Target material: Silicon
Time: 1 year Target mass: 0.6 Kg



Notes
0 d.r.u means we expect less than 1 event @ 90% C.L

Toward a Bayesian credibility interval

The next goal is to adopt a Bayesian approach to infer the upper bound and to estimate the expected experimental sensitivities to the interaction of DM candidates with ordinary matter.

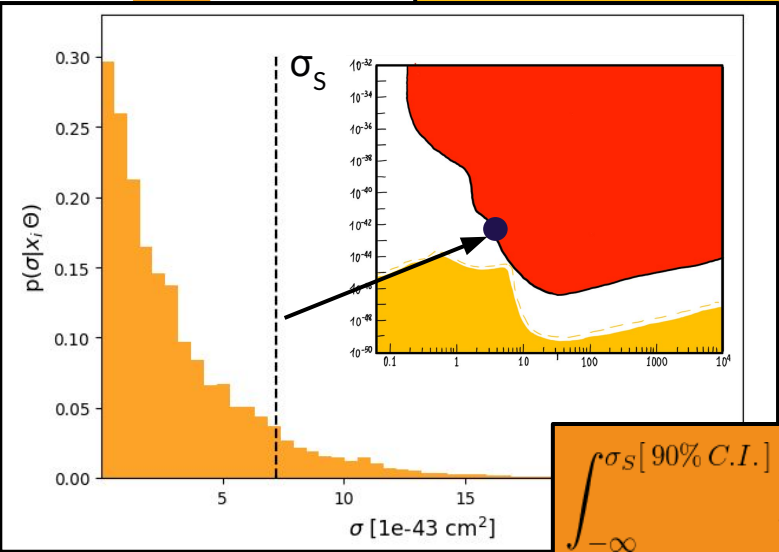
posterior

$$p(r_s, \vec{\theta} | x_i) = \frac{p(x_i | r_s, \vec{\theta}) \pi(r_s, \vec{\theta})}{\int_{\Omega} \int_0^{\infty} p(x_i | r_s, \vec{\theta}) \pi(r_s, \vec{\theta})}$$

likelihood (my model)

prior

normalization (0 < P < 1)



$$\int_{-\infty}^{\sigma_S [90\% C.I.]} p(\sigma | x_i; \vec{\theta}) d\sigma = 0.90$$

Analysis implemented through the Bayesian Analysis Toolkit (BAT)

Conclusions

BULLKID-DM - Flat background at different rates

ROI : $[E_{thr}, 16]$ keV

Target material: Silicon

Time: 1 year

Target mass: 0.6 Kg

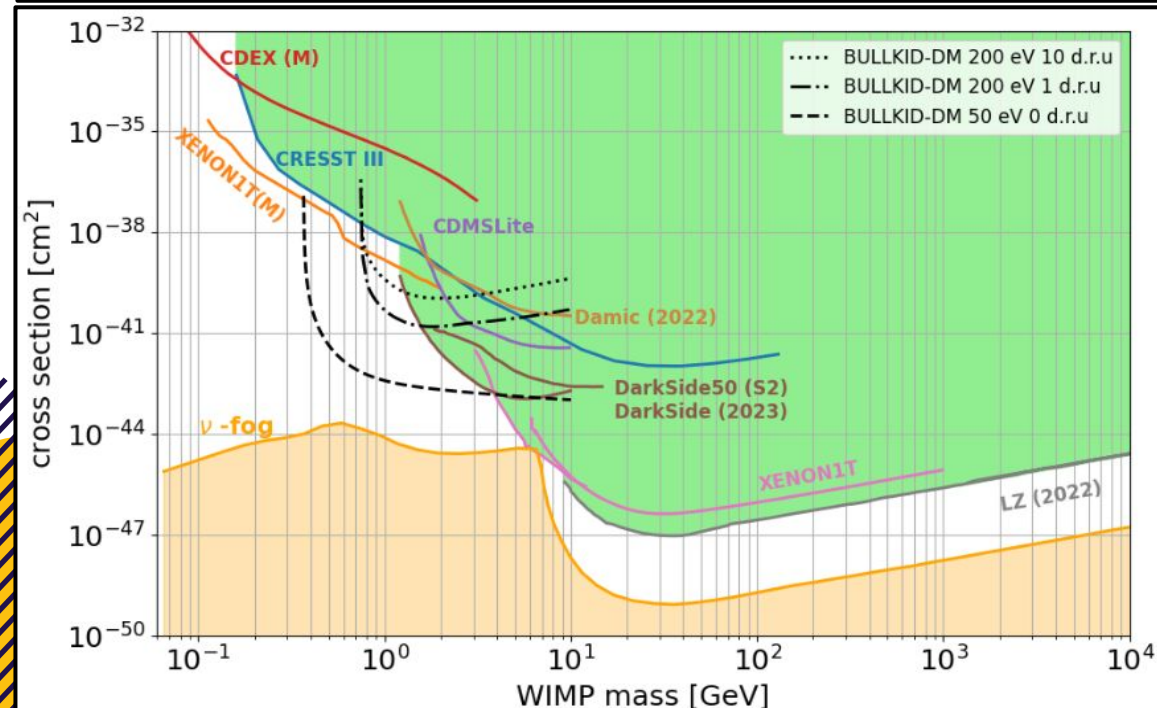
References for the plot [5]-[8]

The BULLKID-DM sensitivity limits have been presented for a **wide range of scenarios**.

In all these cases, a future limit in an **unexplored range** of the WIMP's parameter space has been estimated.

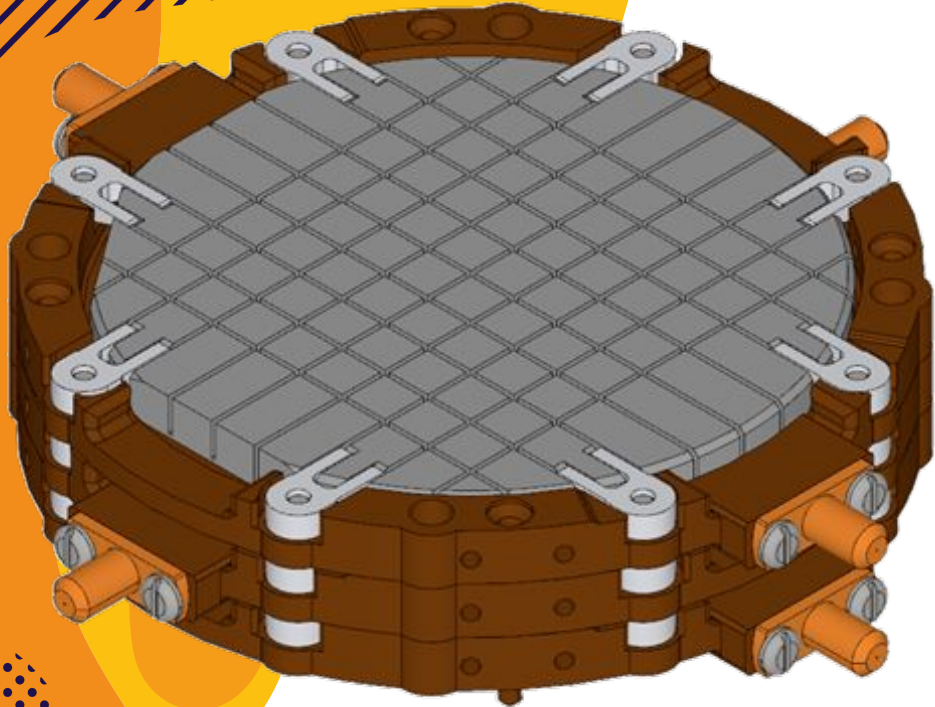
We are developing a **Bayesian algorithm** for the evaluation of the future credibility limits.

It would represent a more robust **probabilistic approach** and would also allow a validation of our background model, **as done in DarkSide [4]**.





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Thank you for the attention!

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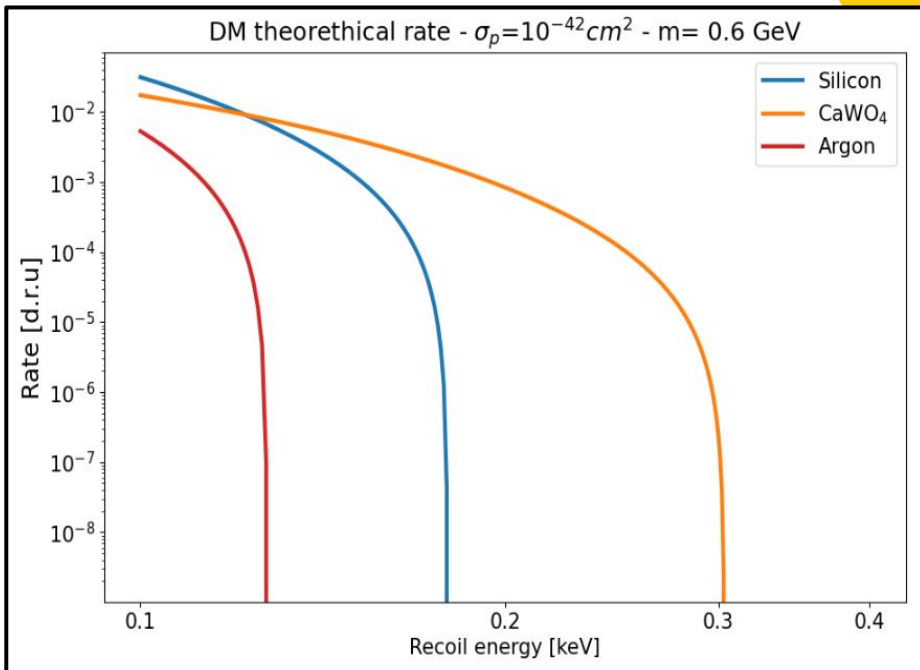
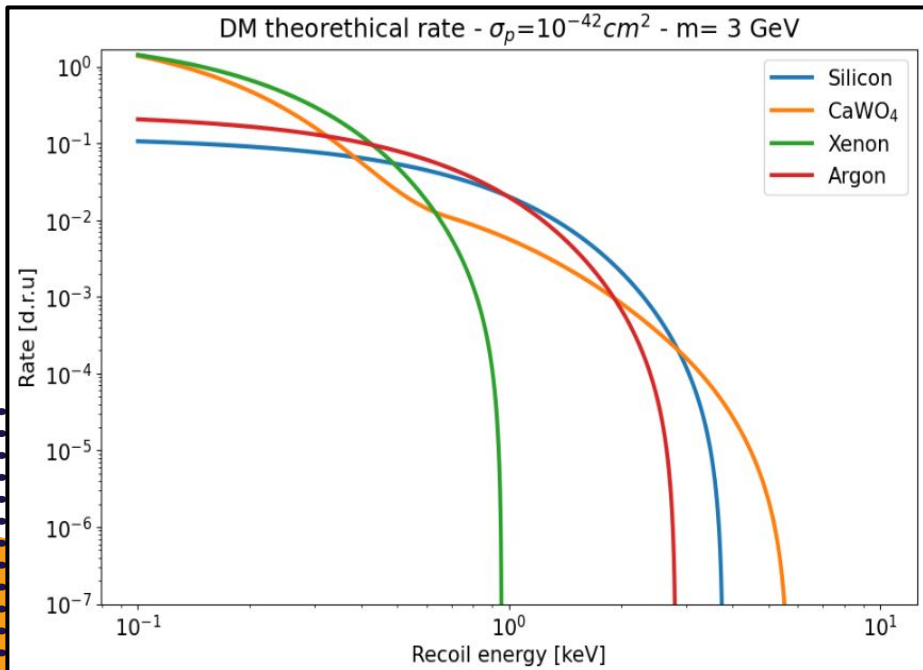
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References

- [1] Finding an upper limit in presence of an unknown background, S. Yellin (2002), [arXiv:physics/0203002](https://arxiv.org/abs/physics/0203002)
- [2] Description of CRESST-III Data, CRESST collaboration (2019), [arXiv:1905.07335](https://arxiv.org/abs/1905.07335)
- [3] A synthetic summary about the probabilistic concepts, used in this presentation, can be found in the following review from the Particle data Group
<https://pdg.lbl.gov/2020/reviews/rpp2020-rev-statistics.pdf>
- [4] DarkSide Bayesian network approach: <https://arxiv.org/pdf/2302.01830.pdf>
- [5] Direct Detection of Dark Matter -- APPEC Committee Report [arXiv:2104.07634](https://arxiv.org/abs/2104.07634)
- [6] LUX-ZEPLIN (LZ) Experiment: <https://arxiv.org/pdf/2207.03764.pdf>
- [7] Damic at SNOLAB: <https://arxiv.org/pdf/2007.15622.pdf>
- [8] DarkSide 50 (2023): <https://journals.aps.org/prd/pdf/10.1103/PhysRevD.107.063001>

BACKUP

WIMP-DM rate



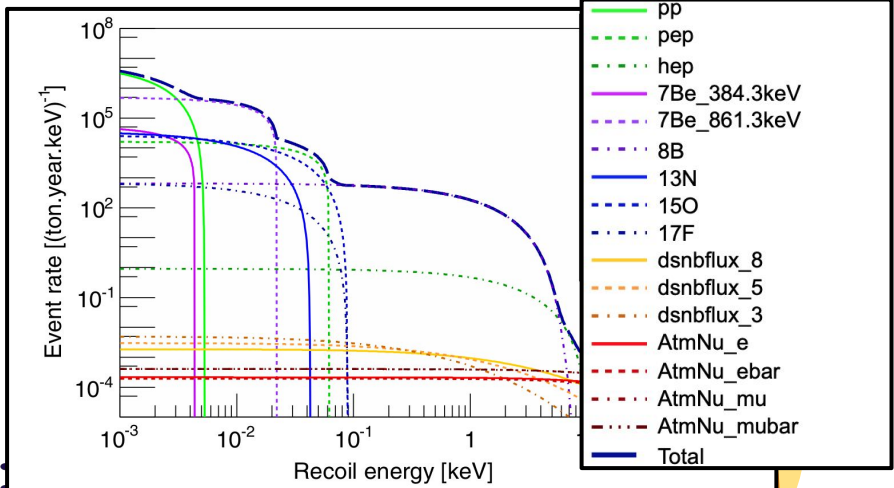
[9] Rates evaluated with the [WIMpy](#) package

[10] A wonderful manual on theory of direct dark matter detection can be found at [arXiv:2104.12785](#)

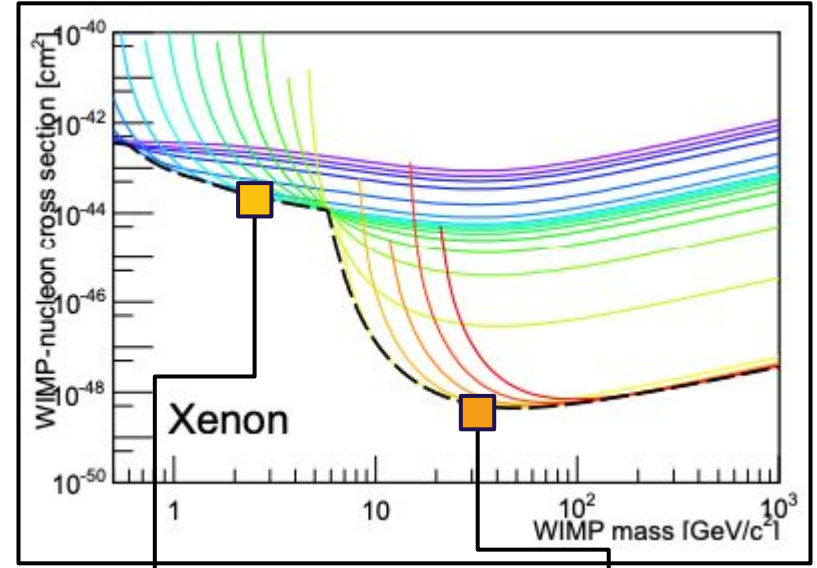
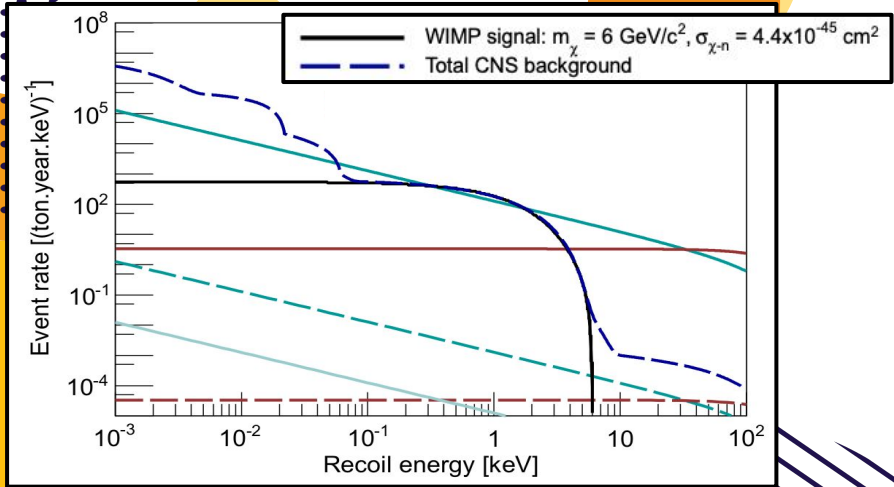
$$v_0 = 220 \text{ km/s} \quad v_{\text{esc}} = 544 \text{ km/s}$$

$$\rho = 0.3 \text{ GeV/cm}^3 \quad v_{\text{lab}} = 238 \text{ km/s}$$

Neutrino Fog



The **Neutrino Fog** is identified, for a certain target element, as the convolution of all background-free exclusion limits with varying threshold. The exposure of such curves is adjusted such that a single neutrino event is expected.

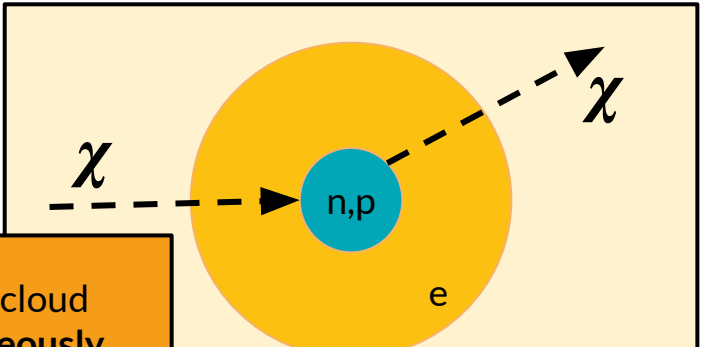


hep and ^8B neutrinos dominant

atmospheric neutrinos dominant

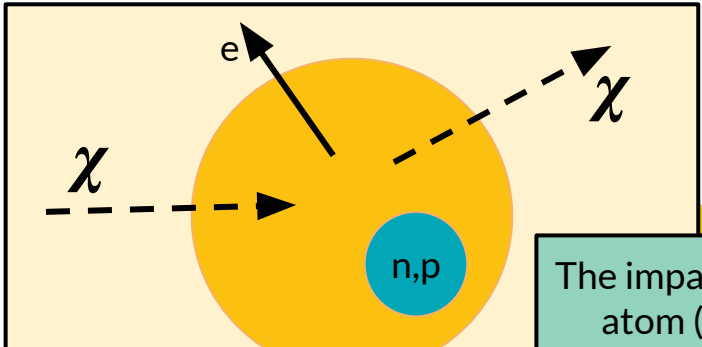
Migdal effect

Standard Nuclear recoil (NR)



Electron cloud instantaneously follows the nucleus

Migdal effect

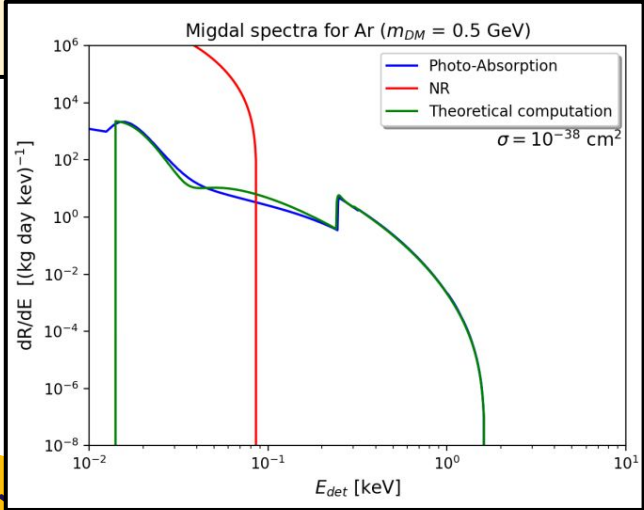


The impact ionizes the atom (electronic recoil (ER) signal)

The Migdal effect allows an indirect detection of sub-threshold NR interactions through ERs

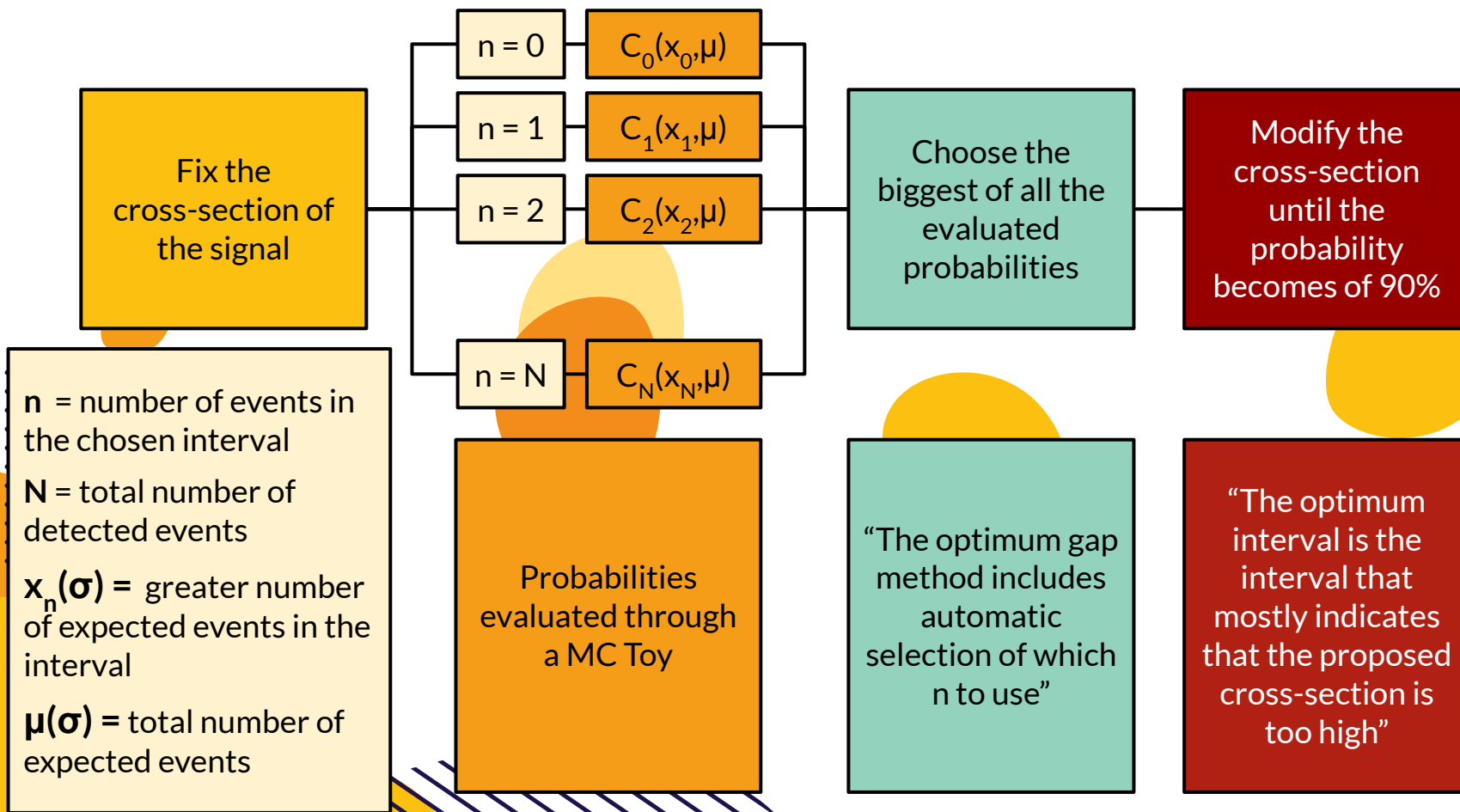
Migdal effect observed?

- ✓ α decay: <https://doi.org/10.1103/PhysRevC.11.1740>
- ✓ β decay: <https://doi.org/10.1103/PhysRevA.97.023402>
- ✗ NR: not yet observed



Plot from [12] <https://hdl.handle.net/11573/1641306>

Yellin method



Bayesian network approach

19

Eur. Phys. J. C (2023) 83:322
<https://doi.org/10.1140/epjc/s10052-023-11410-4>

THE EUROPEAN
PHYSICAL JOURNAL C



Regular Article - Experimental Physics

Search for low mass dark matter in DarkSide-50: the bayesian network approach

DarkSide-50 Collaboration

Improved iterative Bayesian unfolding

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Two fundamental papers regarding the application of Bayesian Networks in physics and in direct dark matter research

[13] [arXiv:2302.01830](https://arxiv.org/abs/2302.01830)

[14] [arXiv:1010.0632](https://arxiv.org/abs/1010.0632)

This technique has the advantage, over the widely used profiling methods, to be **exact in terms of uncertainty propagation**, to **not rely on template morphing**, and to **properly take into account cross correlations between parameters and phase space regions**. In addition, if the physical parameters describing the detector response model and constrained by calibrations are retained as parameters inside the likelihood function, this method gives the possibility of **verifying the goodness of the calibrations and, a posteriori, further constrains the detector response model**.