Black-hole ringdown and their progenitors:

from numerical relativity to tests of GR

Costantino Pacilio (U. of Milano Bicocca)

Rome – September 18 2024

with: Swetha Bhagwat, Francesco Nobili, Davide Gerosa

Pacilio+ (2024) arXiv: [2408.05276]





PYTHON software available at: https://github.com/cpacilio/postmerger

Kerr Black Holes



EHT Collaboration (2019), arxiv 1906.11238

Uniqueness Theorem

Stationary black holes in vacuum in GR are uniquely described by the Kerr spacetime metric

$$ds^{2} = -\left(1 - \frac{2Mr}{\Sigma}\right)dv^{2} + 2dvdr + \Sigma d\theta^{2} + \frac{(r^{2} + a^{2})^{2} - \Delta a^{2}\sin^{2}\theta}{\Sigma}\sin^{2}\theta d\bar{\phi}^{2} - 2a\sin^{2}\theta drd\bar{\phi} - \frac{4Mra}{\Sigma}\sin^{2}\theta dvd\bar{\phi}.$$

Roy P. Kerr Phys. Rev. Lett. 11, 237 (1963)

Quasi-normal modes



Simulation by The SXS (Simulating eXtreme Spacetimes) Project

Black-hole perturbations

Linear perturbations about black holes are described by Teukolsky's equations

Black-hole spectrum

A perturbed black hole emits gravitational waves with a characteristic frequency spectrum

Teukolsky 2014, <u>arxiv 1410.2130</u> Berti+ (2009), <u>arxiv 0905.2975</u> Pani (2013), <u>arxiv 1305.6759</u>



Simulation by Georgia Tech, MAYA Collaboration

Quasi normal modes and the no-hair theorem



As a consequence of the no-hair theorem, **the quasi normal modes depend only on the mass and spin** of the BH remnant

 $f_{lmn}\equiv f_{lmn}(M,\chi)$ $au_{lmn}\equiv au_{lmn}(M,\chi)$

Black hole spectroscopy

Measure **at least two** quasi-normal modes Check that they are consistently inverted into mass and spin



Ringdown excitation amplitudes



Cotesta+ (2018) 1803.10701



Amplitudes depend on the intrinsic parameters of the progenitors Kamaretsos+ (2012) 1207.0399

Surrogates for ringdown amplitudes

Multipole fits for the ringdown amplitudes

Kamaretsos+ (2012) <u>1207.0399</u> London (2018) <u>1801.08208</u> Forteza+ (2022) <u>2205.14910</u> Cheung+ (2023) <u>2310.04489</u>

The are all in closed form



- Parametric-free: does not did ansatze
- Outputs also uncertainties over predictions

GPR used to build the most accurate surrogate fon final mass and spin Varma+ (2018) <u>1809.09125</u> Boschini+ (2023) <u>2307.03435</u>



We extend the surrogate to ringdown amplitudes of **non-precessing quasi-circular** binaries

See also Zertuche+ (2024) 2408.05300

Results: comparison with NR data



Deviation of mean GPR predictions from NR data is order 10E-3

NR data are comprised within ~1 GPR standard deviations

Results: comparison with previous fits (I)



Overall agreement with the most updated fits: London (2018) and Cheung et al. (2023)

Results: comparison with previous fits (II)





GW190521: a case study for LVK



GW190521: amplitude-spin consistency

GR is a deterministic theory

- Final spin and ringdown amplitudes are determined by the same initial params
- We have surrogate fits for both final spin and ringdown amplitudes

Amplitude-spin consistency

- Measure amplitudes and final spin as independent parameters in ringdown
- Map amplitudes to initial params
- Map initial params to final spin
- Compare with measured final spin



GW190521: amplitude-spin consistency

GR is a deterministic theory

- Final spin and ringdown amplitudes are determined by the same initial params
- We have surrogate fits for both final spin and ringdown amplitudes

Amplitude-spin consistency

- Measure amplitudes and final spin as independent parameters in ringdown
- Map amplitudes to initial params
- Map initial params to final spin
- Compare with measured final spin



GW190521: amplitude-spin consistency





Miller+ (2021), <u>2310.01544</u>

GW190521: mass-ratio from A330/A220



Conclusions

PYTHON software available at:

State of the art:

https://github.com/cpacilio/postmerger

- Surrogate of NR ringdown from the SXS public catalog
- Only quasi-circular and non-spinning

Improving the model:

- Flexible machine learning regression: easier to extend than closed-form ansatzes
- Extension to eccentricity [see Carullo 2024] and precession [see Zhu+ 2023] is ongoing

Extend consistency tests:

- Switch to a NR-informed template
- Relax consistency between initial parameters and final mass/spin

$$h = \sum_{l,m,n} \mathcal{A}_{lmn} e^{-i\omega_{lmn}(t-t_0)}$$

Testing no-hair with black hole spectroscopy

BH spectroscopy:

measuring the frequency and damping times of a BH from its GW signal

GR test:

check that there is no "third" independent frequency or damping time Berti, Cardoso, Will (2006), <u>arxiv</u> <u>gr-qc/0512160</u>

Berti+ (2016), <u>arxiv 1605.09286</u>

Baibhav+ (2023), <u>arxiv</u> 2302.03050

Gossan+ (2011), <u>arxiv</u> <u>1111.5819</u>

Meidam+ (2014), <u>arxiv</u> <u>1406.3201</u>

Even if the background is Kerr, no-hair is violated if the perturbation dynamics differ from Teukolsky's Barausse & Sotriou (2004), <u>arxiv 0803.3433</u>

Tattersall+ (2017), <u>arxiv 1711.01992</u>

Quasi normal modes and the no-hair theorem

If no-hair is violated, you have dependence from (at least one) further scale

Recent progresses in computing modified spectra: Cano+ (2023) <u>arxiv 2304.02663</u> Ghosh+ (2023) <u>arxiv 2303.00088</u>

 $f_{lmn} \equiv f_{lmn}(M,\chi,lpha) \ au_{lmn} \equiv au_{lmn}(M,\chi,lpha)$

Relation to black hole uniqueness

Uniqueness theorem – Stationary black holes are axisymmetric and are described by a member of the Kerr family

Kerr hypothesis – a black hole formed from gravitational collapse or from a binary merger will asymptotically settle to a member of the Kerr family, by emitting all charges except mass and angular momentum (aka the 'no hair' theorem) [as reviewed e.g. in Teukolsky 2014 https://arxiv.org/abs/1410.2130]

Assuming the Kerr hypothesis, the quasi-normal mode spectrum follows from Teukolsky's equation and depends only on the final mass and the final spin of the black hole [as reviewed in e.g. Berti+2009 <u>https://arxiv.org/abs/0905.2975</u>]

$$\omega_{lmn}\equiv\omega_{lmn}~(M_f,\chi_f)$$

What black hole spectroscopy tests (1)

Ringdown tests probe general relativity in the strong field regime

Quasi-normal modes can be approximated by the frequency and damping times of perturbed light rays at the innermost stable circular orbit for null geodesics (aka the 'photon sphere') [Cardoso+2009 <u>https://arxiv.org/abs/0812.1806</u> and ref.s therein]

Higher order WKB methods refine this approximation and reinforce the physical connection between quasi-normal modes and the photon sphere

Black hole spectroscopy tests the BH structure in the vicinity of the photon sphere

What black hole spectroscopy tests (2)

The **uniqueness theorem** holds in several gravitational theories beyond GR. Examples: shift-symmetric Horndeski

However, the dynamics of perturbations is different, hence **the quasi-normal modes are different**

Here you only test the dynamics of the theory but not the metric of the asymptotic solution Some gravitational theories beyond GR admit black hole solutions **different from Kerr**. Examples: Einstein–dilaton–Gauss-Bonnet, dynamical Chern-Simons

Here, you test the structure of the black hole in the vicinity of the photon sphere* and the dynamics of the perturbations at the same time

*In modified gravity, the connection with photon sphere is still under study, especially for rotating black holes [see Yagi 2022 <u>https://arxiv.org/abs/2201.06186</u> and ref.s therein]