# Comparing gravitational waveform models for binary black hole mergers through a hypermodels approach

A. Puecher\*, A. Samajdar, G. Ashton, C. Van Den Broeck, T. Dietrich

Phys.Rev.D 109 (2024) 2, 023019

TEONGrav workshop 19th September 2024

\*anna.puecher@uni-potsdam.de





### Introduction





### Introduction



### Waveform models:

different approximations to build waveform models for parameter estimation analyses can lead to differences and biases in the results



### Introduction



### Waveform models:

different approximations to build waveform models for parameter estimation analyses can lead to differences and biases in the results



### Hypermodels

Introduced in Ashton&Dietrich, *Nature Astronomy*(2022)

Sample over the waveform model too, with a categorical parameter  $\omega$ :

parameters space =  $\{\vec{ heta}, \omega\}$   $\omega \in [0, m-1]$ source parameters waveform model

### Hypermodels

Introduced in Ashton&Dietrich, Nature Astronomy(2022)

Sample over the waveform model too, with a categorical parameter  $\omega$ :

parameters space =  $\{\vec{\theta}, \omega\}$   $\omega \in [0, m-1]$ source parameters waveform model

Probability for each waveform  $\ell$  :

$$p_\ell = rac{n_\ell}{N}$$

 $egin{aligned} n_\ell &
ightarrow & ext{number of samples} \ ext{for model } \ell \ N &
ightarrow & ext{total final posterior} \ ext{samples} \end{aligned}$ 

Odds ratio between two models A and B:

$$\mathcal{O}^A_B = rac{p_A}{p_B} = rac{n_A}{n_B}$$

# Analysis

• Four different models, all with precession and higher-order modes: NRSur7dq4, IMRPhenomXPHM, SEOBNRv4PHM, IMRPhenomTPHM

$$(\ell,m)=(2,2),(2,1),(3,3),(4,4),(2,-2),(2,-1),(3,-3),(4,-4)$$

• Heaviest events in GWTC-3 (  $M_{
m tot} \geq 59.4 M_{\odot}$  , NRSur7dq4 validity )

with significant SNR (  $ho_{
m net} \geq \sqrt{N_{
m d} * 8^2}$  ) -> 13 events

- bilby MCMC
- recover source parameters (chirp mass  $M_c$ , mass ratio q, effective inspiral spin  $\chi_{eff}$ , effective precessing spin  $\chi_p$ ) and probabilities for the different models

# **Results - Single events**

- For most events, no clearly favored model
- Only for 3 events we find a strong preference for some of the models

*but* -> not the same models are preferred -> short duration and data quality issues

### Models' probability

 $p_\ell = rac{n_\ell}{N}$ 

Event	NRSur	SEOB	IMRX	IMRT
GW150914	$27.55\pm0.7$	$16.22\pm0.8$	$23.34\pm0.7$	$32.88\pm0.7$
GW190519_153544	$20.82\pm0.6$	$20.95\pm0.6$	$40.87\pm0.5$	$17.35\pm0.6$
GW190521_074359	$14.76 \pm 1.2$	$40.50\pm1.0$	$17.53 \pm 1.2$	$27.22 \pm 1.1$
GW190620_030421	$32.98\pm0.6$	$19.48\pm0.6$	$20.22\pm0.6$	$27.32\pm0.6$
GW190630_185205	$33.79\pm0.6$	$15.36\pm0.6$	$18.90\pm0.6$	$31.95\pm0.6$
GW190910_112807	$22.86\pm0.6$	$25.92\pm0.6$	$27.85\pm0.6$	$23.37\pm0.6$
GW191222_033537	$28.11\pm0.5$	$20.58\pm0.6$	$18.78\pm0.6$	$32.53\pm0.5$
$GW200112\_155838$	$30.56\pm0.6$	$15.61\pm0.6$	$19.82\pm0.6$	$34.01\pm0.5$
GW200224_222234	$21.82\pm0.6$	$23.39\pm0.6$	$40.43\pm0.5$	$14.36 \pm 0.7$
GW200311_115853	$15.68\pm0.6$	$27.70\pm0.6$	$35.69\pm0.6$	$20.93\pm0.6$
GW190521	$31.78 \pm 0.6$	$26.39 \pm 0.6$	$4.60\pm0.7$	$37.23 \pm 0.5$
GW191109_010717	$7.54 \pm 1.6$	$62.29 \pm 1.0$	$5.06\pm1.7$	$25.11 \pm 1.5$
GW200129_065458	$46.94 \pm 1.4$	$0.66^{+1.9}_{-0.66}$	$51.14 \pm 1.3$	$1.25 \ ^{+1.9}_{-1.25}$

## **Results - Trends**

No trends with respect to source parameters or SNR





### **Results - Combined events**



		$\mathcal{O}_{ ext{SEOB}}^{ ext{NRSur}}$	$\mathcal{O}_{\mathrm{SEOB}}^{\mathrm{IMRX}}$	$\mathcal{O}_{ ext{seob}}^{ ext{IMRT}}$	$\mathcal{O}_{\mathrm{IMRX}}^{\mathrm{NRSur}}$	$\mathcal{O}_{\mathrm{IMRT}}^{\mathrm{NRSur}}$	$\mathcal{O}_{\mathrm{IMRT}}^{\mathrm{IMRX}}$
	All events	$29.43 \pm 1.11$	$4.70\pm0.07$	$5.09\pm0.08$	$6.26\pm0.11$	$5.78\pm0.10$	$0.92\pm0.01$
I	No GW200129_065458	$0.42 \pm 0.00$	$0.06 \pm 0.00$	$2.69\pm0.03$	$6.82\pm0.12$	$0.15\pm0.00$	$0.02 \pm 0.00$
	No GW190521	$24.44\pm0.84$	$26.99 \pm 0.97$	$3.61\pm0.05$	$0.91 \pm 0.01$	$6.77\pm0.12$	$7.48\pm0.14$
I	No GW191109_010717	$243.31\pm26.35$	$57.84 \pm 3.05$	$12.62\pm0.31$	$4.21\pm0.06$	$19.27\pm0.59$	$4.58\pm0.07$
	Without all three	$2.85\pm0.03$	$4.30\pm0.06$	$4.74\pm0.07$	$0.66 \pm 0.00$	$0.60 \pm 0.00$	$0.91\pm0.01$
	Without all three	$2.85\pm0.03$	$4.30\pm0.06$	$4.74\pm0.07$	$0.66\pm0.00$	$0.60\pm0.00$	$0.91 \pm 0.0$

NRSur favored over SEOB, but result mainly determined only by one event (GW200129\_065458)

Without the three events that significantly favor or disfavor one of the models, we find no preference for any of the approximants.

### **Results - Precession**

		Probability								
Event	NRSur	SEOB	IMRX	IMRT						
GW150914	$27.55\pm0.7$	$16.22\pm0.8$	$23.34\pm0.7$	$32.88\pm0.7$						
GW190519_153544	$20.82\pm0.6$	$20.95\pm0.6$	$40.87\pm0.5$	$17.35\pm0.6$						
GW190521_074359	$14.76 \pm 1.2$	$40.50\pm1.0$	$17.53 \pm 1.2$	$27.22 \pm 1.1$						
GW190620_030421	$32.98\pm0.6$	$19.48\pm0.6$	$20.22\pm0.6$	$27.32\pm0.6$						
GW190630_185205	$33.79\pm0.6$	$15.36\pm0.6$	$18.90\pm0.6$	$31.95\pm0.6$						
GW190910_112807	$22.86\pm0.6$	$25.92\pm0.6$	$27.85\pm0.6$	$23.37\pm0.6$						
GW191222_033537	$28.11\pm0.5$	$20.58\pm0.6$	$18.78\pm0.6$	$32.53\pm0.5$						
$GW200112\_155838$	$30.56\pm0.6$	$15.61\pm0.6$	$19.82\pm0.6$	$34.01\pm0.5$						
GW200224_222234	$21.82\pm0.6$	$23.39\pm0.6$	$40.43\pm0.5$	$14.36 \pm 0.7$						
GW200311_115853	$15.68\pm0.6$	$27.70\pm0.6$	$35.69\pm0.6$	$20.93\pm0.6$						
GW190521	$31.78 \pm 0.6$	$26.39 \pm 0.6$	$4.60 \pm 0.7$	$37.23 \pm 0.5$						
GW191109_010717	$7.54 \pm 1.6$	$62.29\pm1.0$	$5.06 \pm 1.7$	$25.11 \pm 1.5$						
GW200129 065458	$46.94 \pm 1.4$	$0.66^{+1.9}_{-0.66}$	$51.14 \pm 1.3$	$1.25 \ ^{+1.9}_{-1.25}$						

### $\chi_{\rm p}$ JS divergence with prior

Event	NRSur	SEOB	IMRX	IMRT	Combined
GW150914	0.008	0.010	0.050	0.017	0.015
$GW190519\_153544$	0.010	0.017	0.010	0.011	0.011
$GW190521\_074359$	0.037	0.029	0.027	0.029	0.029
$GW190620\_030421$	0.010	0.006	0.016	0.012	0.006
$GW190630\_185205$	0.030	0.067	0.049	0.065	0.050
$GW190910\_112807$	0.023	0.012	0.009	0.014	0.014
${\rm GW191222}\_033537$	0.012	0.011	0.014	0.012	0.011
$GW200112\_155838$	0.012	0.015	0.011	0.014	0.012
GW200224_222234	0.008	0.011	0.024	0.010	0.010
${\rm GW200311}\_115853$	0.026	0.018	0.041	0.038	0.031
GW190521	0.243	0.158	0.007	0.264	0.202
GW191109_010717	0.095	0.227	0.070	0.422	0.243
$GW200129\_065458$	0.459	0.005	0.330	0.051	0.378

# **Results - Precession**

Probability				$\chi_{ m p}$ .	JS div	regen	ce wi	th prior		
Event	NRSur	SEOB	IMRX	IMRT	Event	NRSur	SEOB	IMRX	IMRT	Combined
GW150914	$27.55\pm0.7$	$16.22\pm0.8$	$23.34\pm0.7$	$32.88\pm0.7$	GW150914	0.008	0.010	0.050	0.017	0.015
GW190519_153544	$20.82\pm0.6$	$20.95\pm0.6$	$40.87\pm0.5$	$17.35\pm0.6$	$GW190519_{153544}$	0.010	0.017	0.010	0.011	0.011
GW190521_074359	$14.76 \pm 1.2$	$40.50\pm1.0$	$17.53 \pm 1.2$	$27.22 \pm 1.1$	GW190521_074359	0.037	0.029	0.027	0.029	0.029
GW1					CIW100200 080401	0.010	0.000	0.010	0.010	0.006

# <sup>GW1</sup> Models that recover precession have a higher probability

GW191222_033537	$28.11 \pm 0.5$	$20.58\pm0.6$	$18.78\pm0.6$	$32.53\pm0.5$	
GW200112_155838	$30.56\pm0.6$	$15.61\pm0.6$	$19.82\pm0.6$	$34.01\pm0.5$	
GW200224_222234	$21.82\pm0.6$	$23.39\pm0.6$	$40.43\pm0.5$	$14.36 \pm 0.7$	
GW200311_115853	$15.68\pm0.6$	$27.70\pm0.6$	$35.69\pm0.6$	$20.93\pm0.6$	
GW190521	$31.78 \pm 0.6$	$26.39 \pm 0.6$	$4.60 \pm 0.7$	$37.23 \pm 0.5$	
GW191109_010717	$7.54 \pm 1.6$	$62.29\pm1.0$	$5.06 \pm 1.7$	$25.11 \pm 1.5$	
GW200129_065458	$46.94 \pm 1.4$	$0.66^{+1.9}_{-0.66}$	$51.14 \pm 1.3$	$1.25 \ ^{+1.9}_{-1.25}$	

GW191222_033537	0.012	0.011	0.014	0.012	0.011
${\rm GW200112}\_155838$	0.012	0.015	0.011	0.014	0.012
$GW200224_{222234}$	0.008	0.011	0.024	0.010	0.010
$GW200311\_115853$	0.026	0.018	0.041	0.038	0.031
GW190521	0.243	0.158	0.007	0.264	0.202
GW191109_010717	0.095	0.227	0.070	0.422	0.243
$GW200129\_065458$	0.459	0.005	0.330	0.051	0.378

### Conclusions

- We analyzed the 13 heaviest events with significant SNR in GWTC-3 with a hypermodels approach to quantify model preferences
- Overall, no model is consistently preferred or disfavored
- No trends of model preference based on source parameters or signal SNR
- For three events (GW190521, GW191109, GW200129) we find strong preference for some of the models, *but* 
  - different models
  - these events have short duration or potential data quality issues
- Combining results from all the events:  $\mathcal{O}_{SEOB}^{NRSur} = 29.43$ , but this result is determined only by GW200129. Without the three events above, no significant preference for any model
- However, for all the events with a strong preference, we find that the preferred models are the ones which recover precession

### Backup -Parameters Posteriors



## **Backup - Injections**



logL