

Model-independent cosmology with Bright Sirens

1st TEONGRAV workshop - September 17- Rome

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in collaboration with

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Warm up

$$H(z) = H_0 \sqrt{\Omega_{m,0}(1+z)^3 + \Omega_{r,0}(1+z)^4 + \Omega_{k,0}(1+z)^2 + \Omega_{\text{DE},0} \exp \left[3 \int_0^z \frac{1 + w_{\text{DE}}(z')}{1+z'} dz' \right]}$$

$$w_{\text{DE}}(z) = \frac{P_{\text{DE}}(z)}{\rho_{\text{DE}}(z)}$$

Warm up

$$H(z) = H_0 \sqrt{\Omega_{m,0}(1+z)^3 + \Omega_{r,0}(1+z)^4 + \Omega_{k,0}(1+z)^2 + \Omega_{\text{DE},0} f_{\text{DE}}(z)}$$

$$w_{\text{DE}}(z) = \frac{P_{\text{DE}}(z)}{\rho_{\text{DE}}(z)}$$

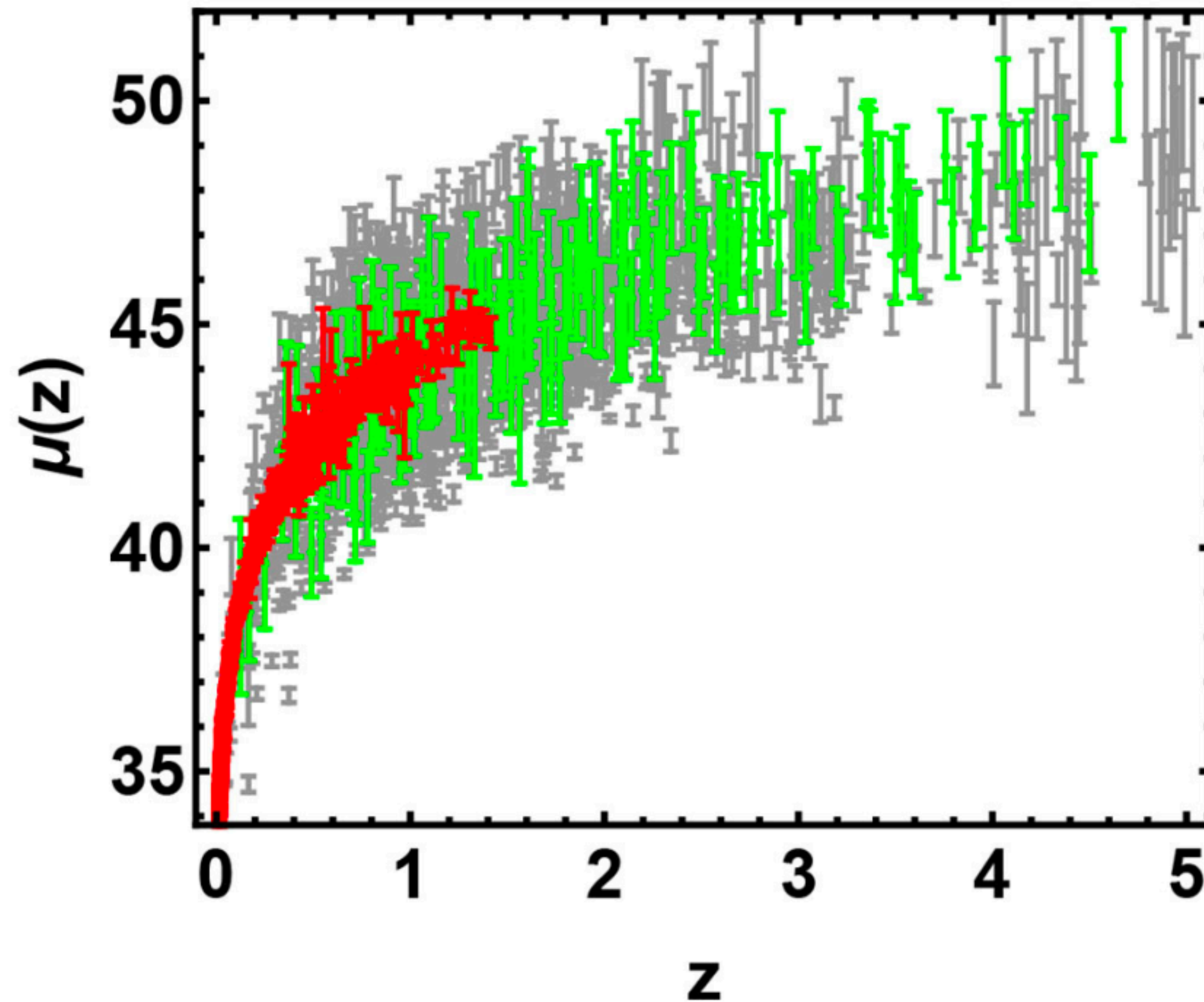
$$f_{\text{DE}}(z) = \frac{\Omega_{\text{DE}}(z)}{\Omega_{\text{DE},0}}$$

$$d_L(z) = c (1+z) \int_0^z \frac{dz'}{H(z')}$$

We want to trace the Hubble parameter $H(z)$

Standard candles

Demianski+ 2020



SN Ia (Cepheids)

GRBs (SN Ia)

QSOs ($F_X - F_{UV}$)

Why GWs

$$\tilde{h}_+(f) \propto \frac{\mathcal{M}^{5/6}}{2 d_L} f^{-7/6} e^{i\phi(\mathcal{M}, f)} (1 + \cos^2(\iota))$$

self-calibrated measure of distance

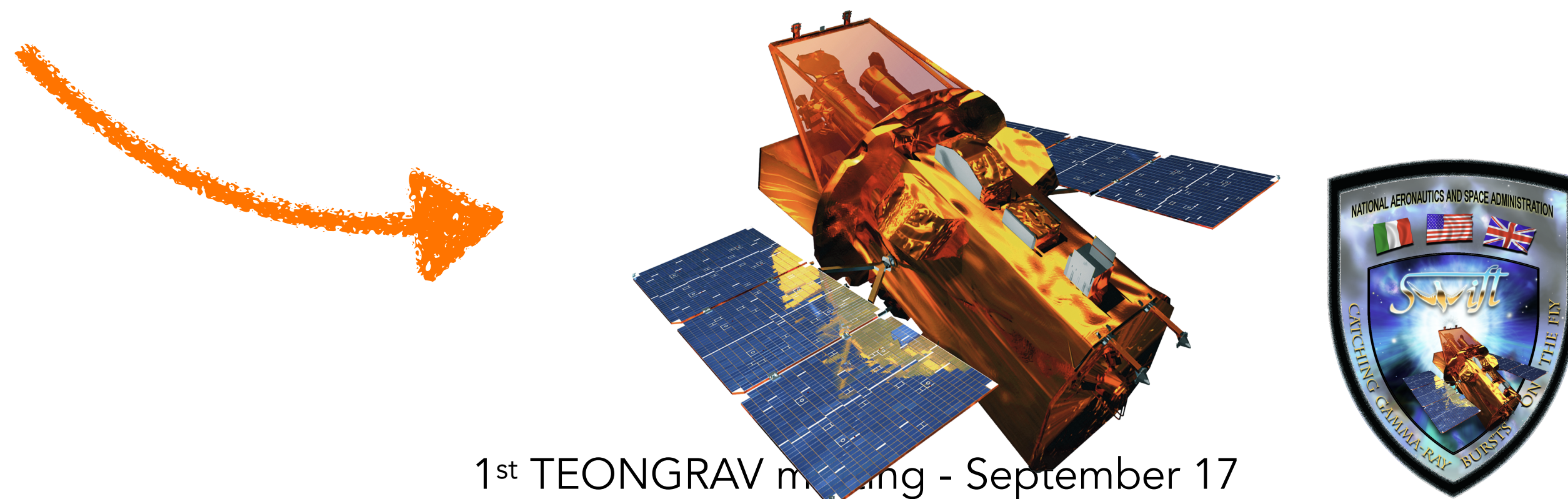
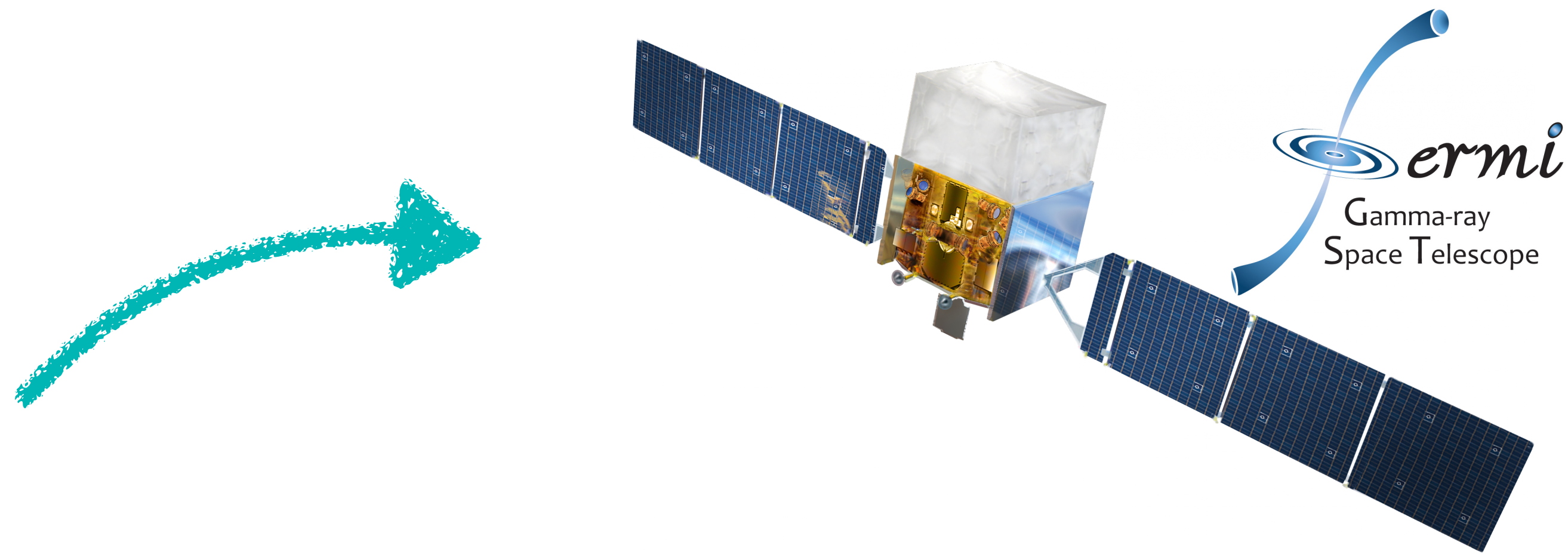
$$\tilde{h}_\times(f) \propto \frac{\mathcal{M}^{5/6}}{d_L} f^{-7/6} e^{i\phi(\mathcal{M}, f) + i\pi/2} \cos(\iota)$$

$$d_L(z) = c \left(1 + \frac{?}{z}\right) \int_0^z \frac{dz'}{H(z')}$$

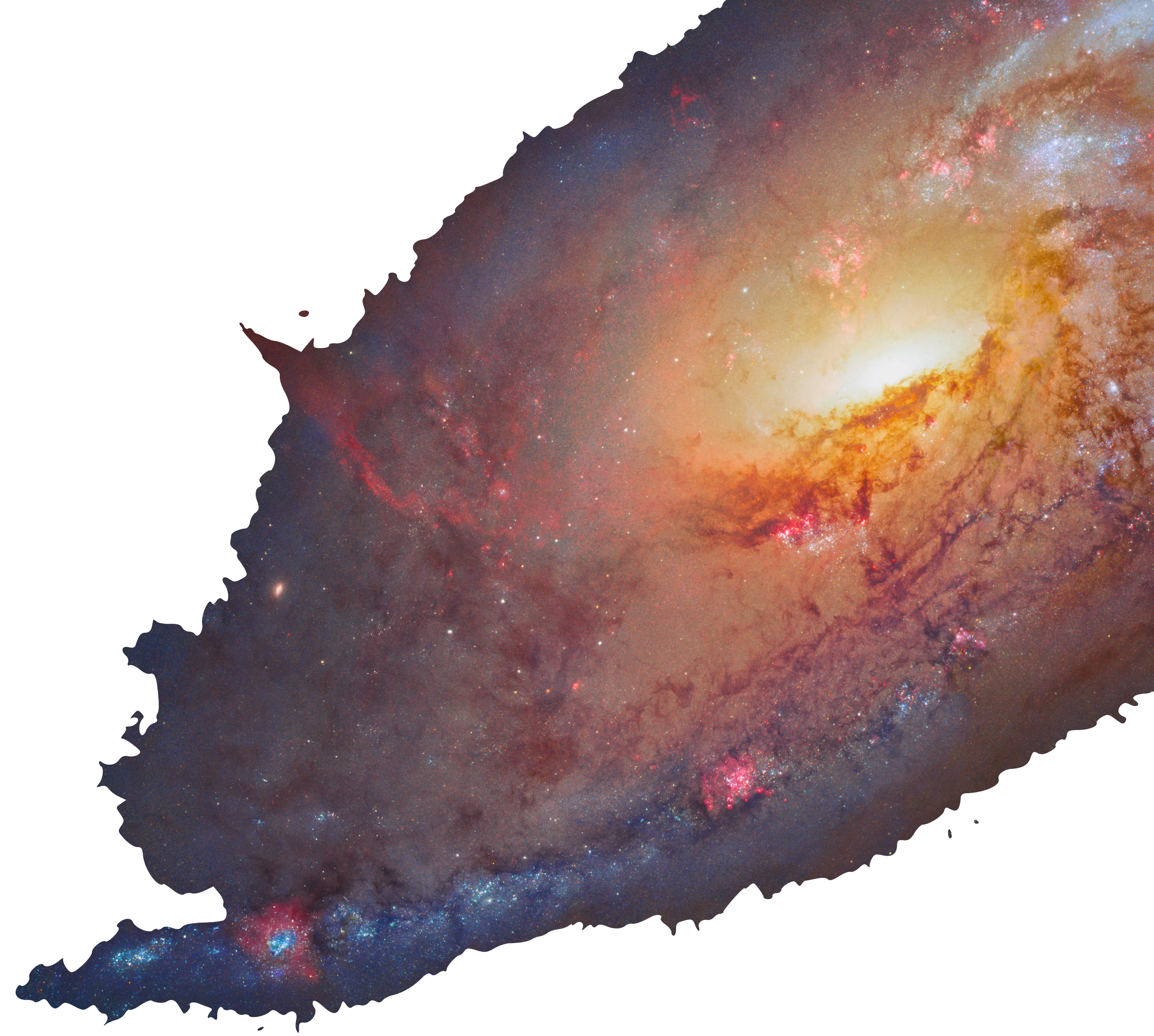
Why GRBs

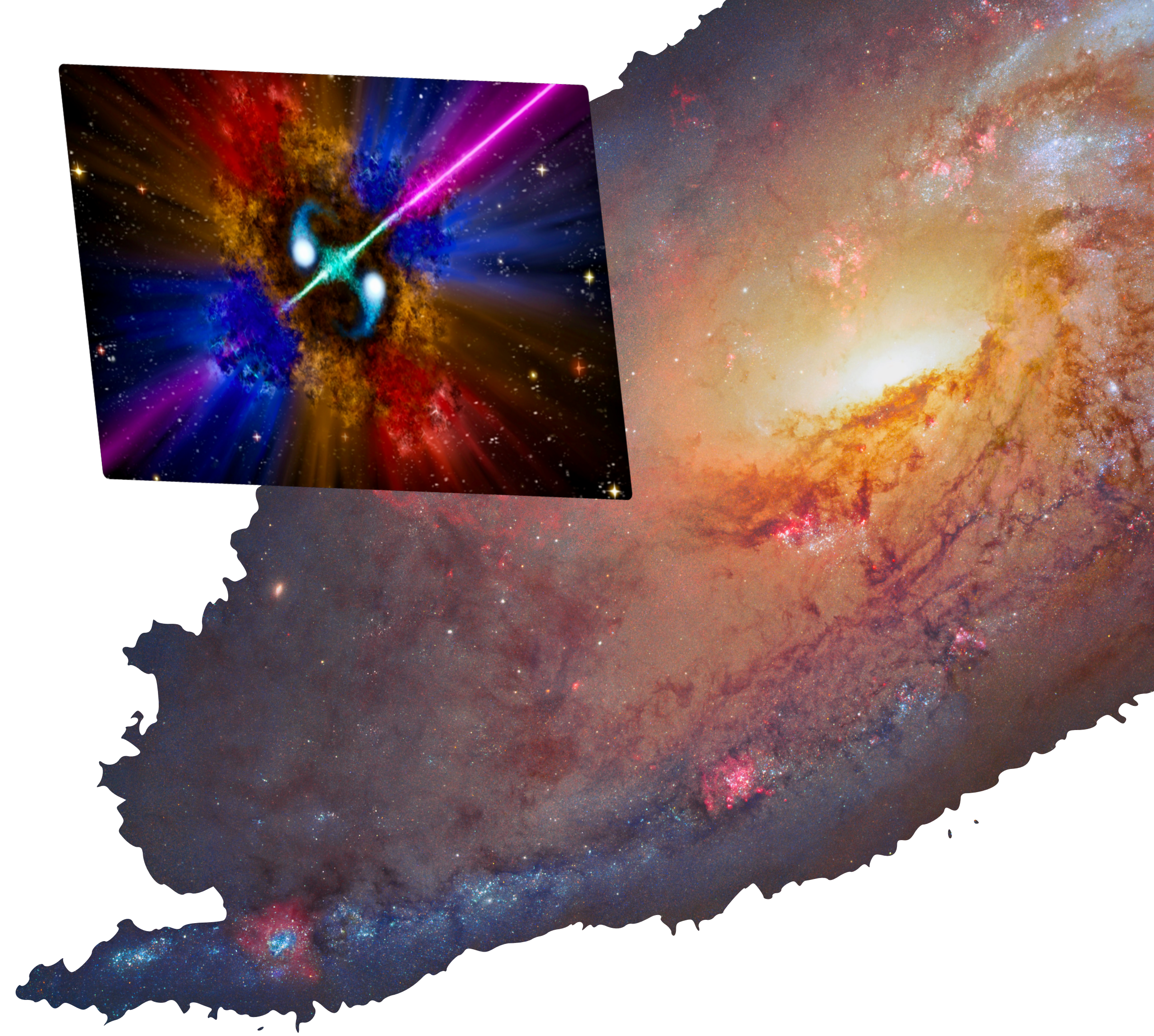
BNS are associated to GW and to the burst of γ -rays \longrightarrow Multi-messenger astrophysics

This give us a $\Delta z \sim 0$

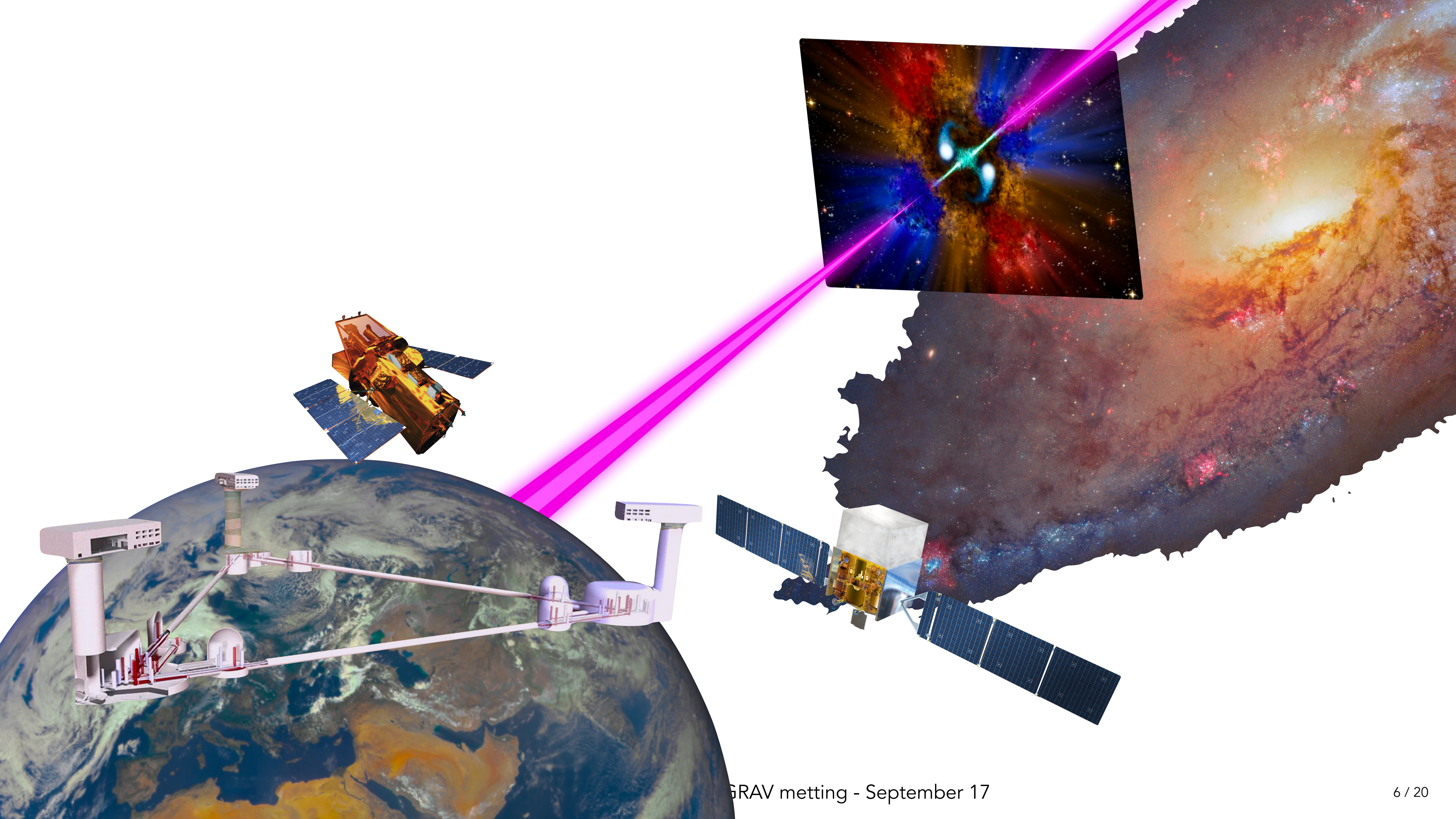


1st TEONGRAV meeting - September 17

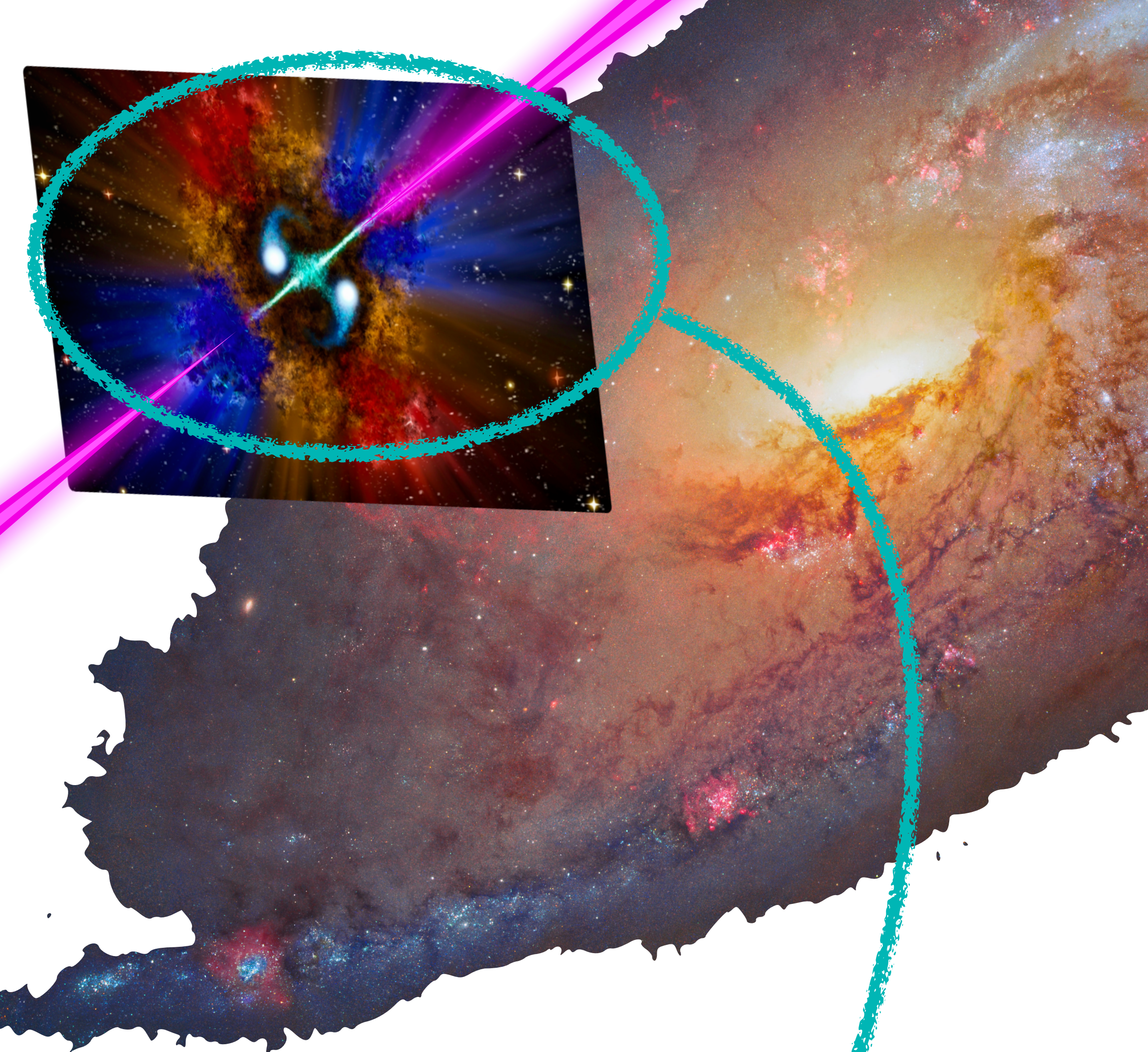
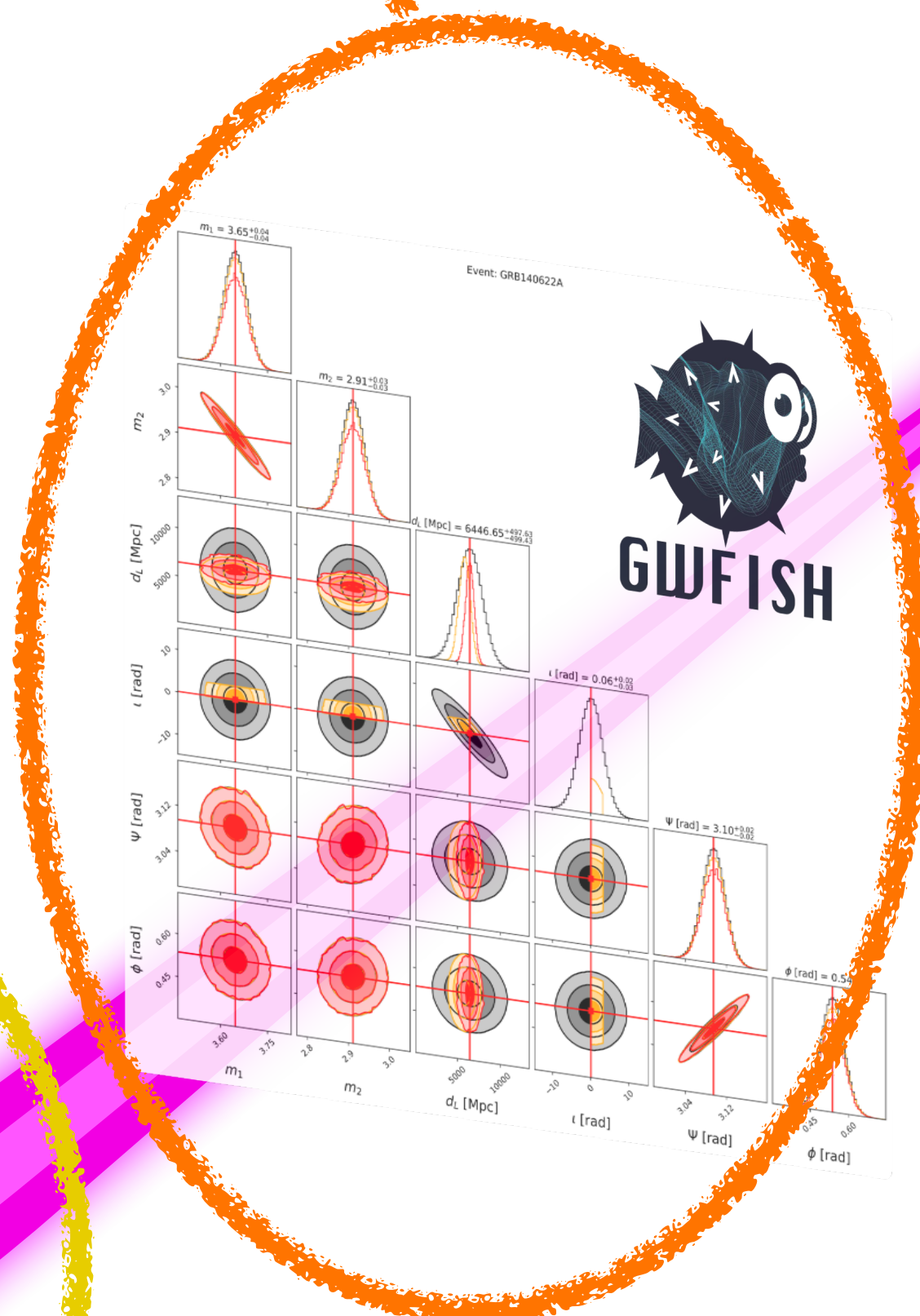
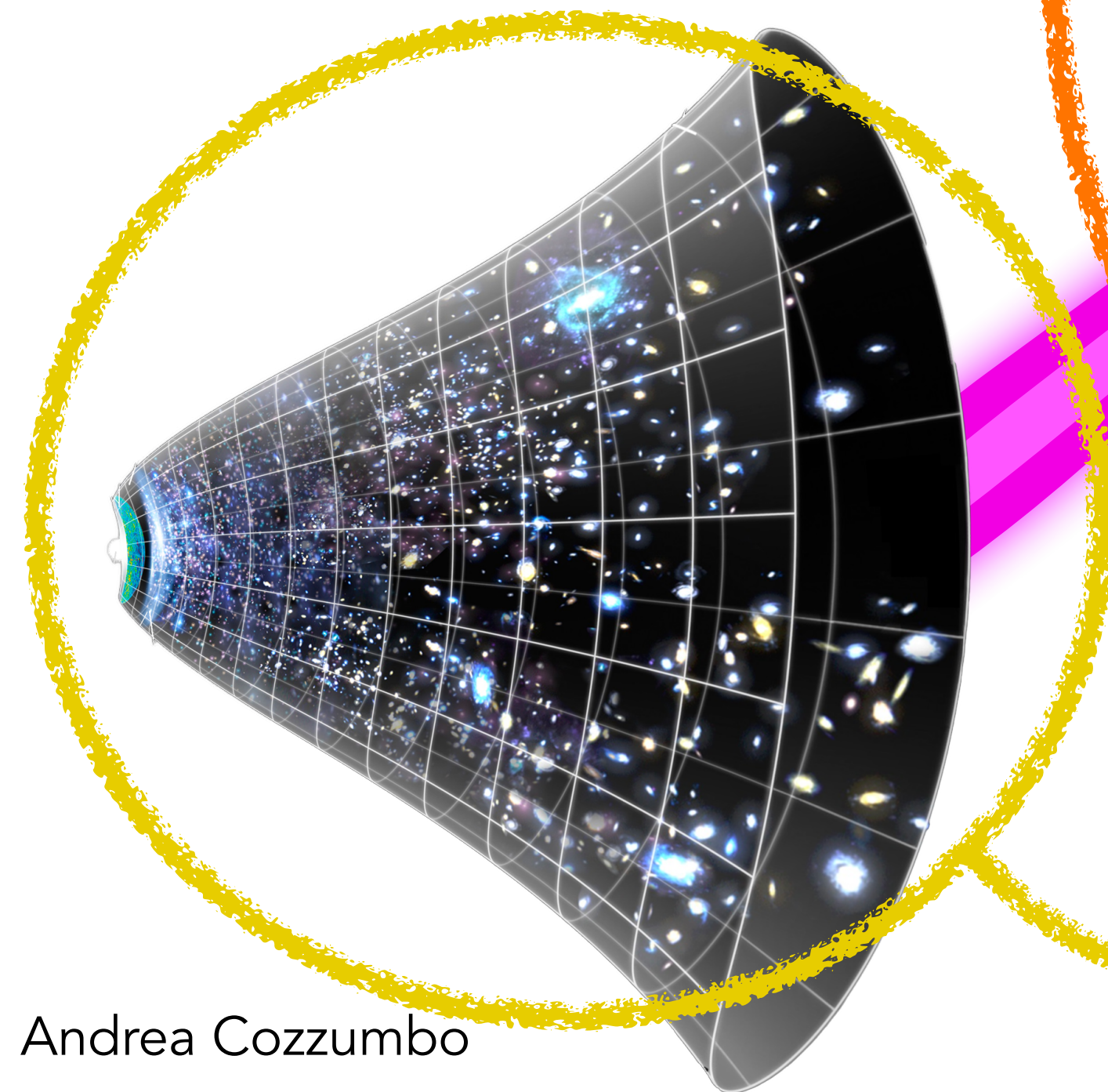








$$d_L(z)$$

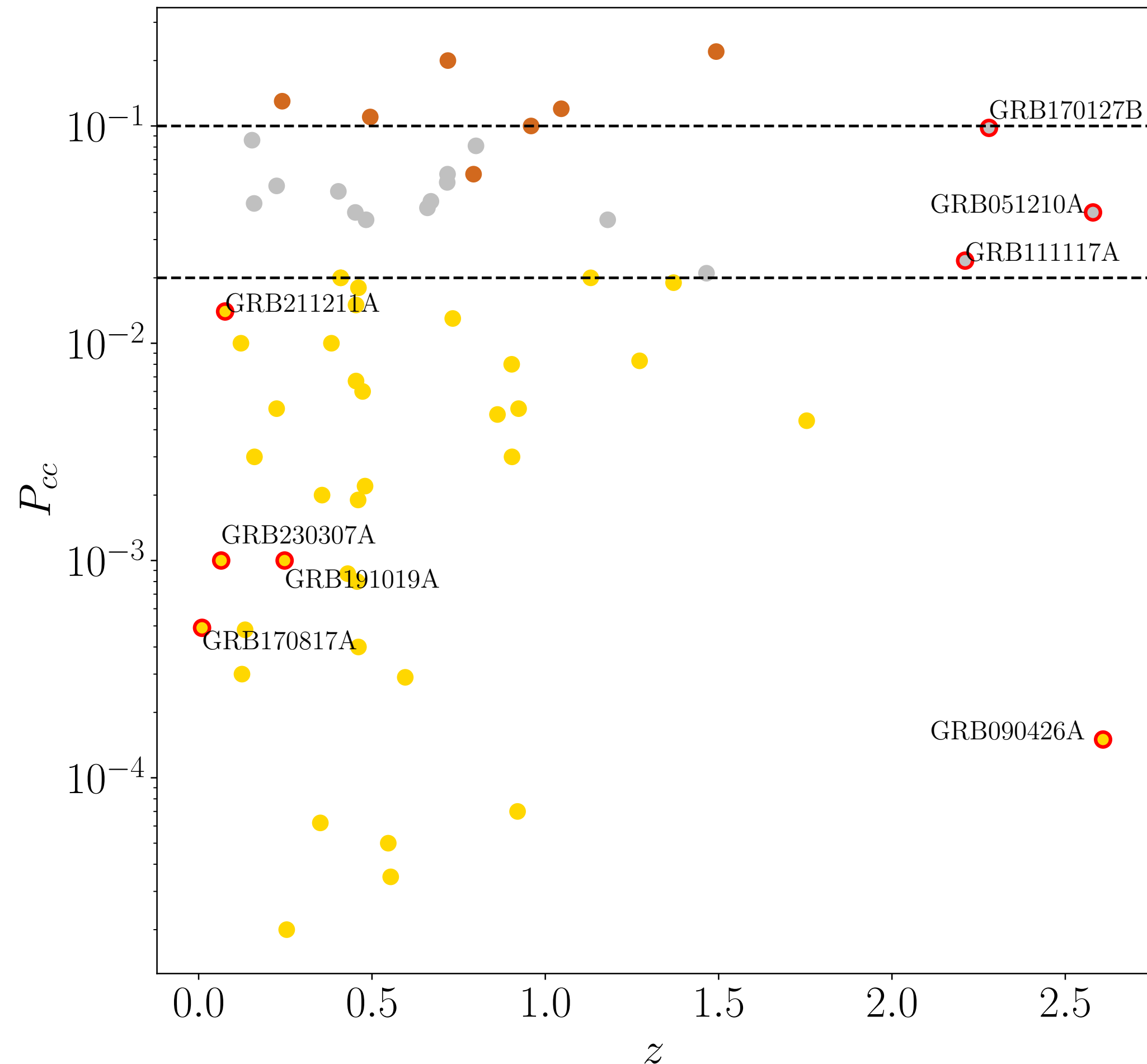


z

$$GP \sim \mathcal{N}(\mu, k)$$
$$H(z)$$

GRB data set

Cozzumbo+, in prep.

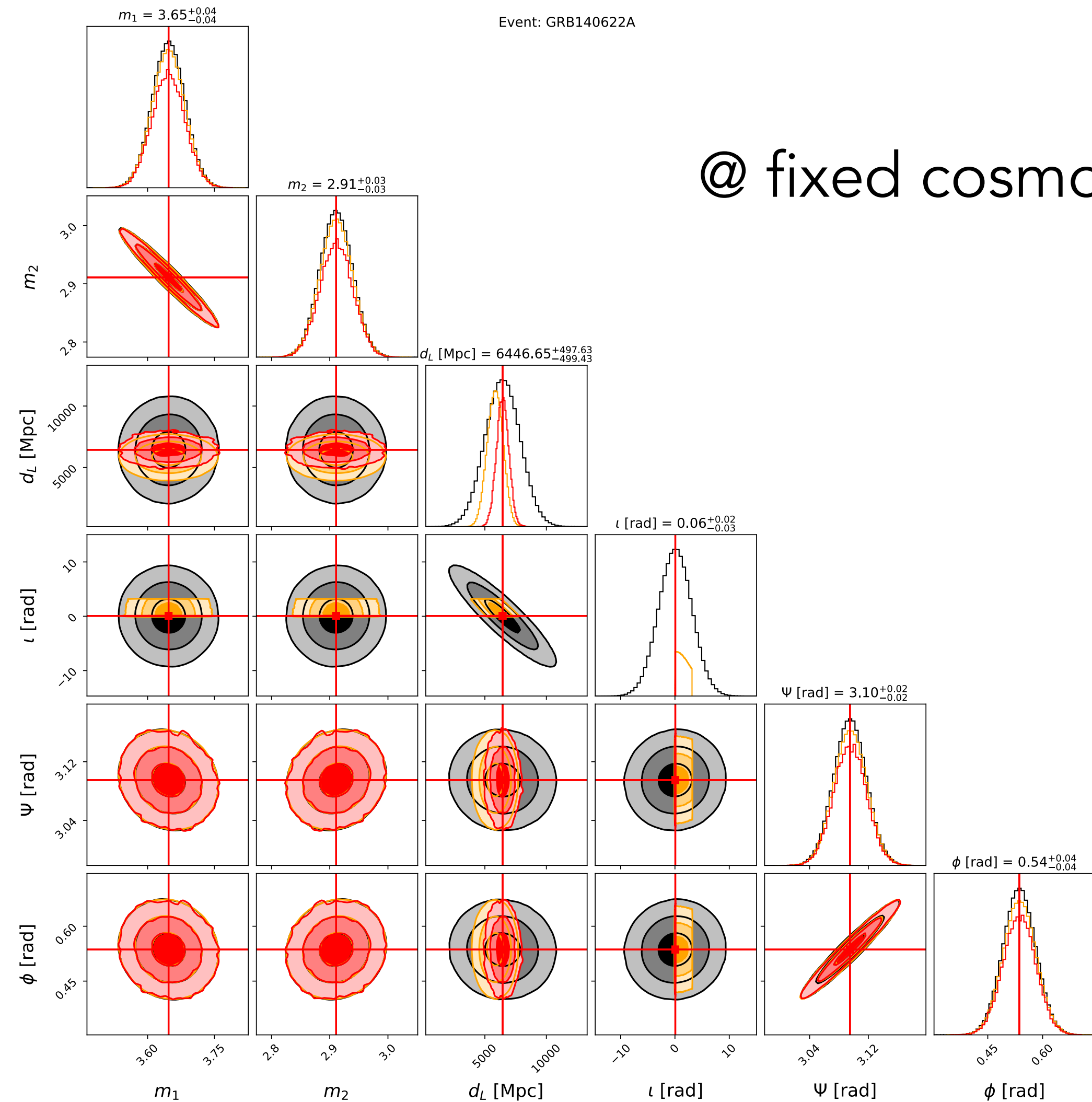


- Fermi-GBM & Swift-BAT/UVOT/XRT
- Merger-driven GRB events
- $\Delta z \leq 7\%$

If **Einstein Telescope** existed during the **Swift** and **Fermi** era, what new insights into cosmology would we have today?

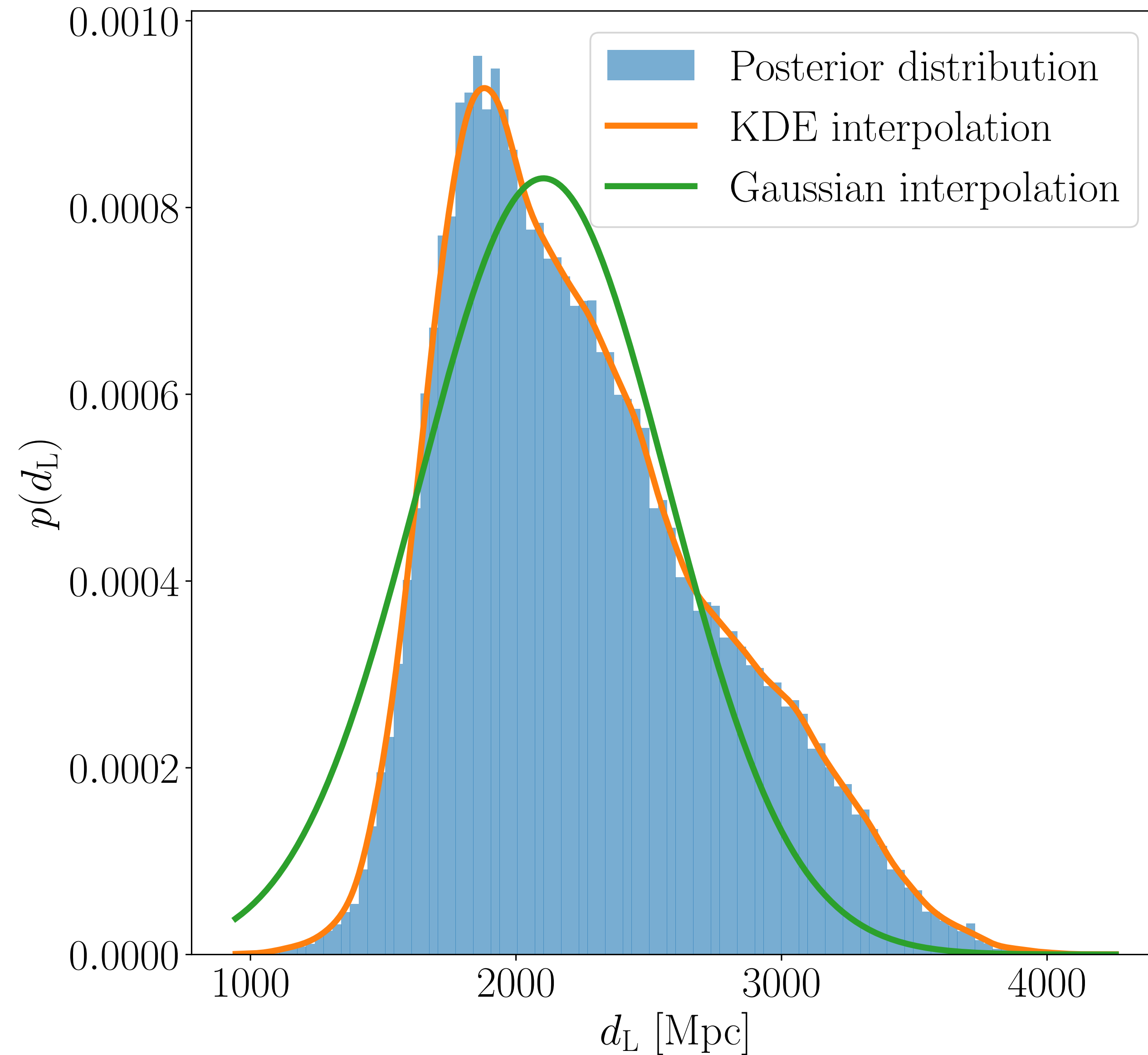
GW posteriors

Dupletsa+, 2024



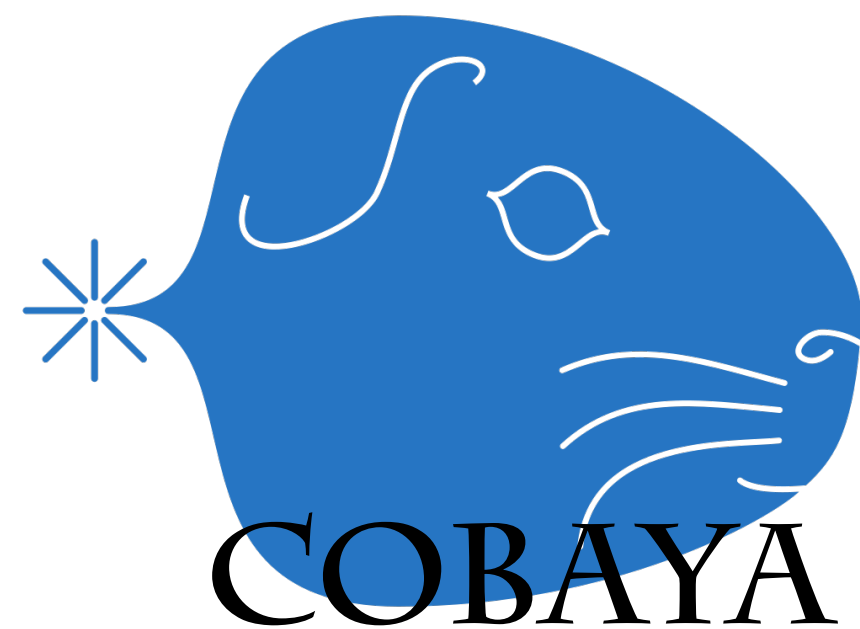
@ fixed cosmology

GW posteriors



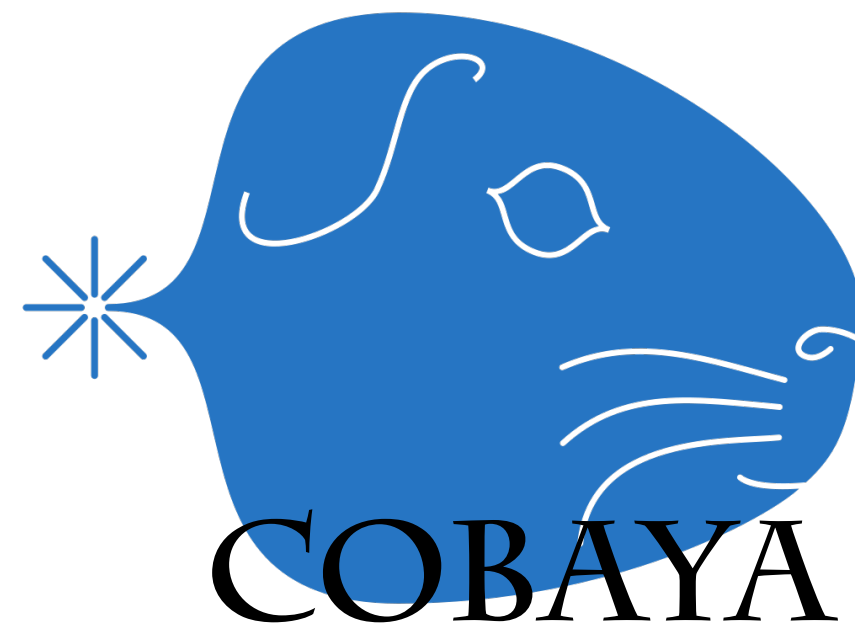
Cosmological MCMC

$$\log \mathcal{L}(\theta) \propto \sum_i^{N_{\text{events}}} - \frac{(d_L^{\text{th}}(\theta) - d_L^{\text{obs},i})^2}{2\sigma_{d_L,i}^2}$$



Cosmological MCMC

$$\log \mathcal{L}(\theta) \propto \sum_i^{N_{\text{events}}} \mathcal{K}^i(d_L^{\text{th}})$$



Our strategy

- We generate mock joint GW-GRB data assuming 2 different cosmologies

Λ CDM *Planck18*

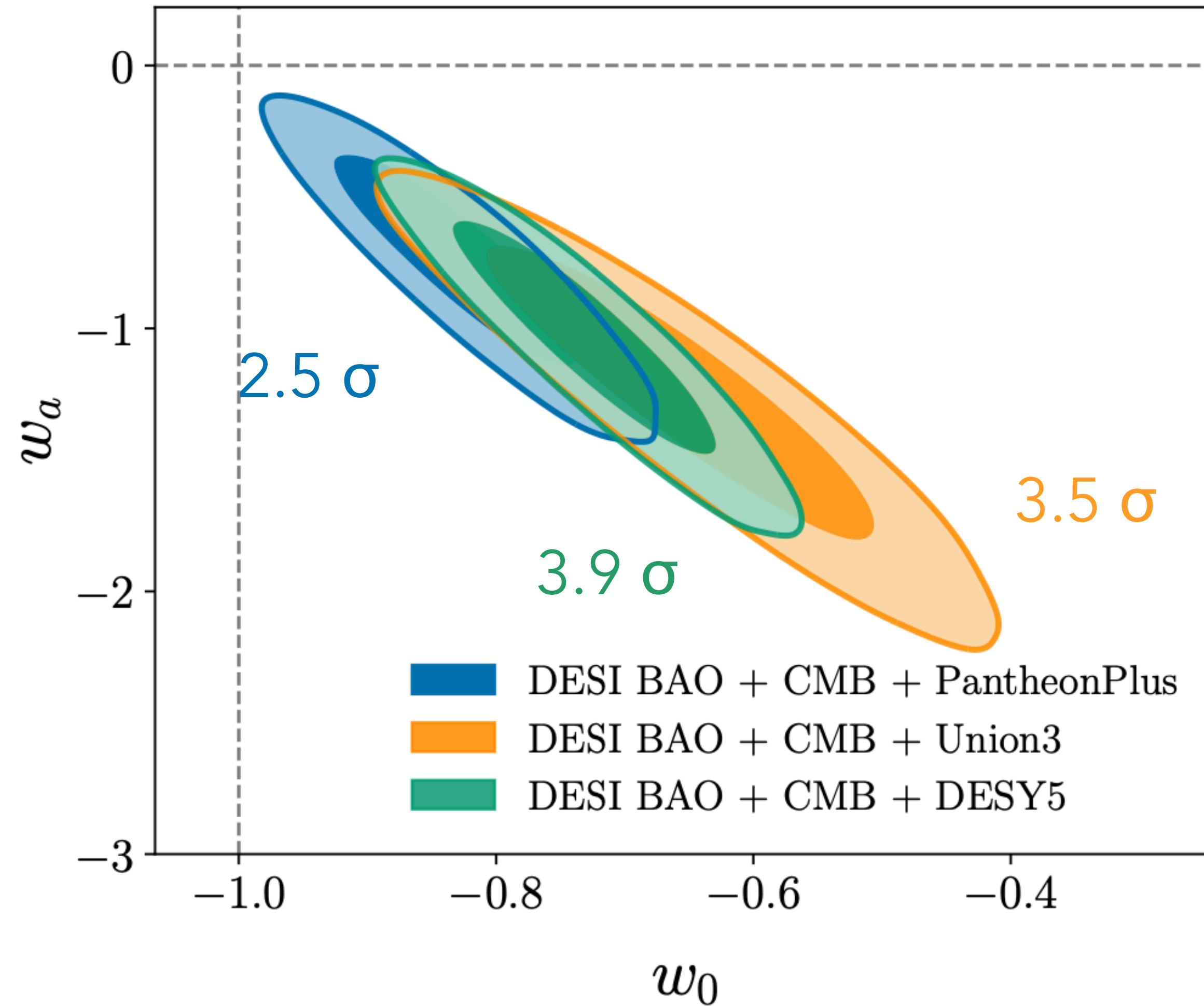
PEDE *Planck18, eBOSS, Pantheon+*

Li and Shafieloo, 2019

- We fit them with a parametric and a non-parametric approach with various observational configurations
- We compare the performances

“Tantalizing suggestion” of dynamical DE

DESI collaboration, Adame+, 2024



Non-parametric approach

GP → Gaussian Process

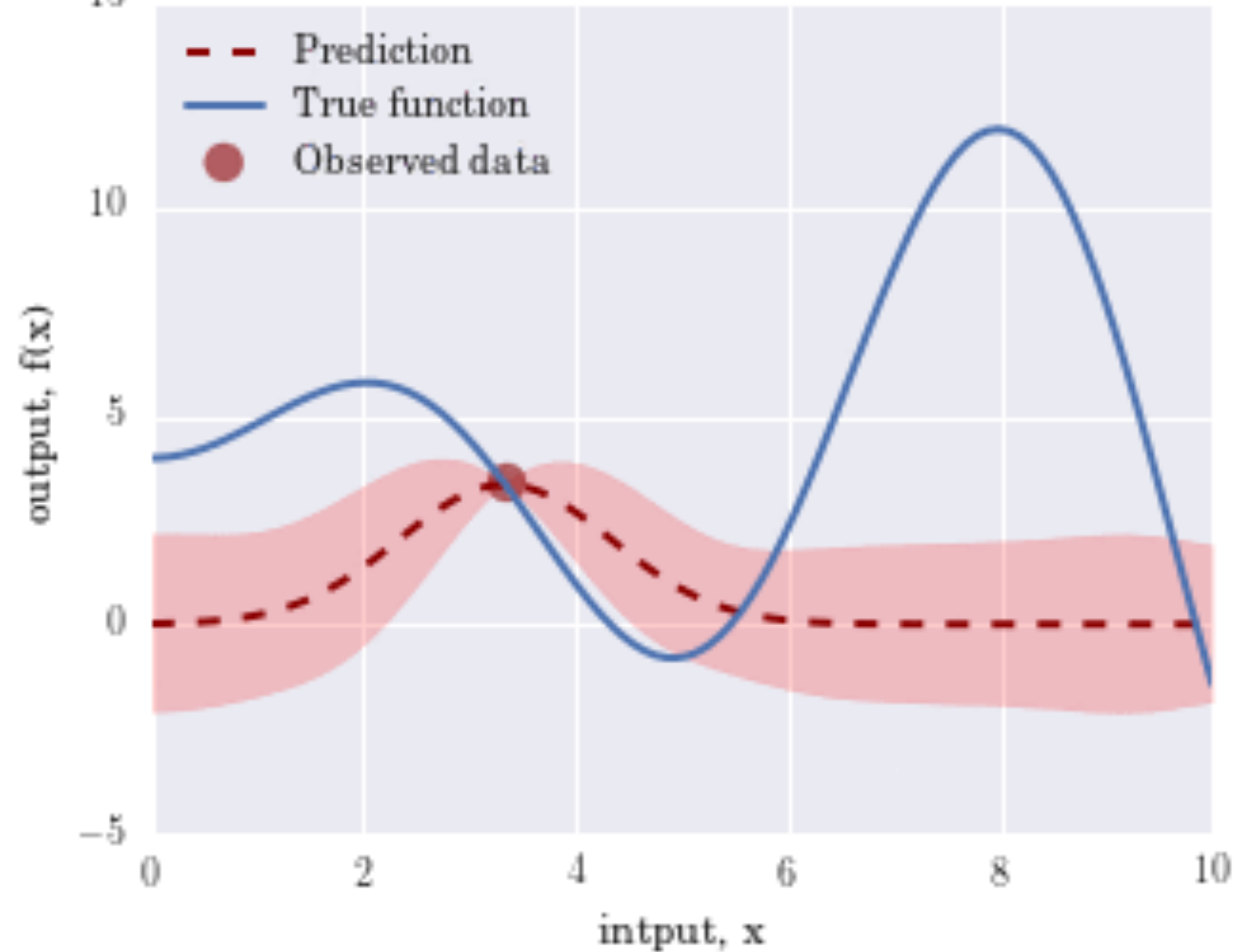
$$GP \sim \mathcal{N}(\mu, k)$$

$$h^2(z) = \frac{H^2(z)}{H_0^2} = \Omega_{m,0} (1+z)^3 + (1 - \Omega_{m,0}) f_{\text{DE}}(z)$$

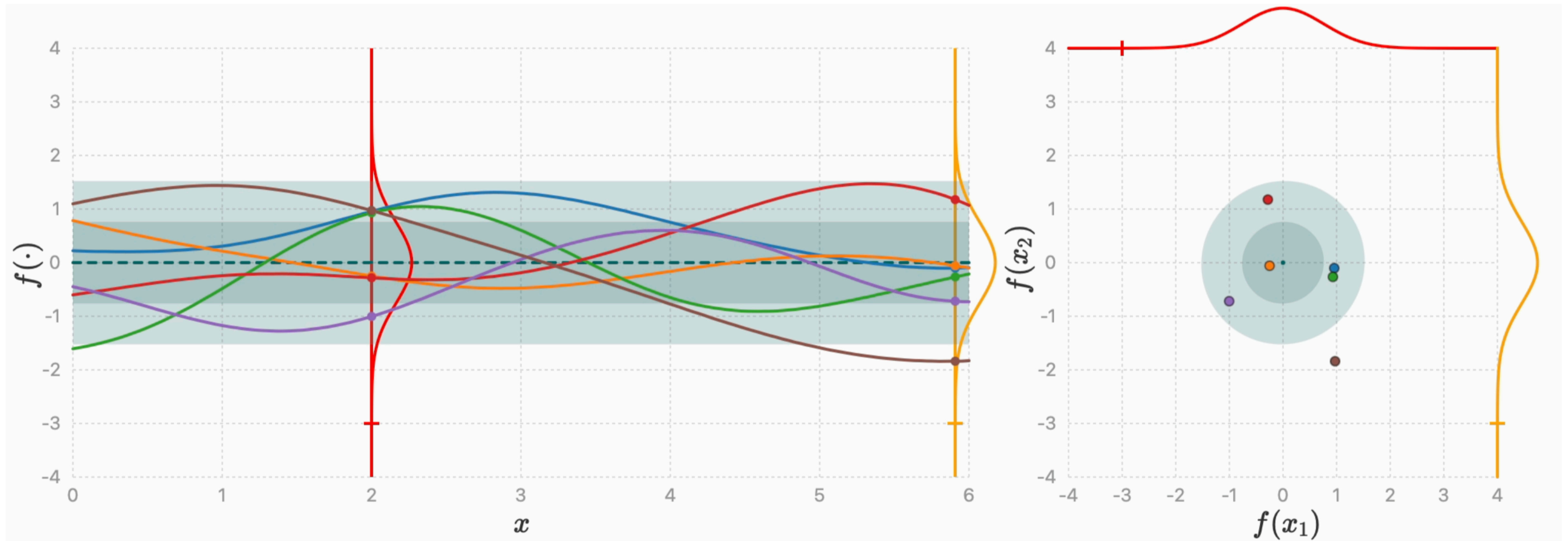
$$f_{\text{DE}}(z) \sim GP(\bar{f}_{\text{DE}} = 1, k(\sigma_f, l_f))$$

$$k(\sigma_f, l_f) = \sigma_f^2 e^{-\frac{(x-x')^2}{2l_f^2}}$$

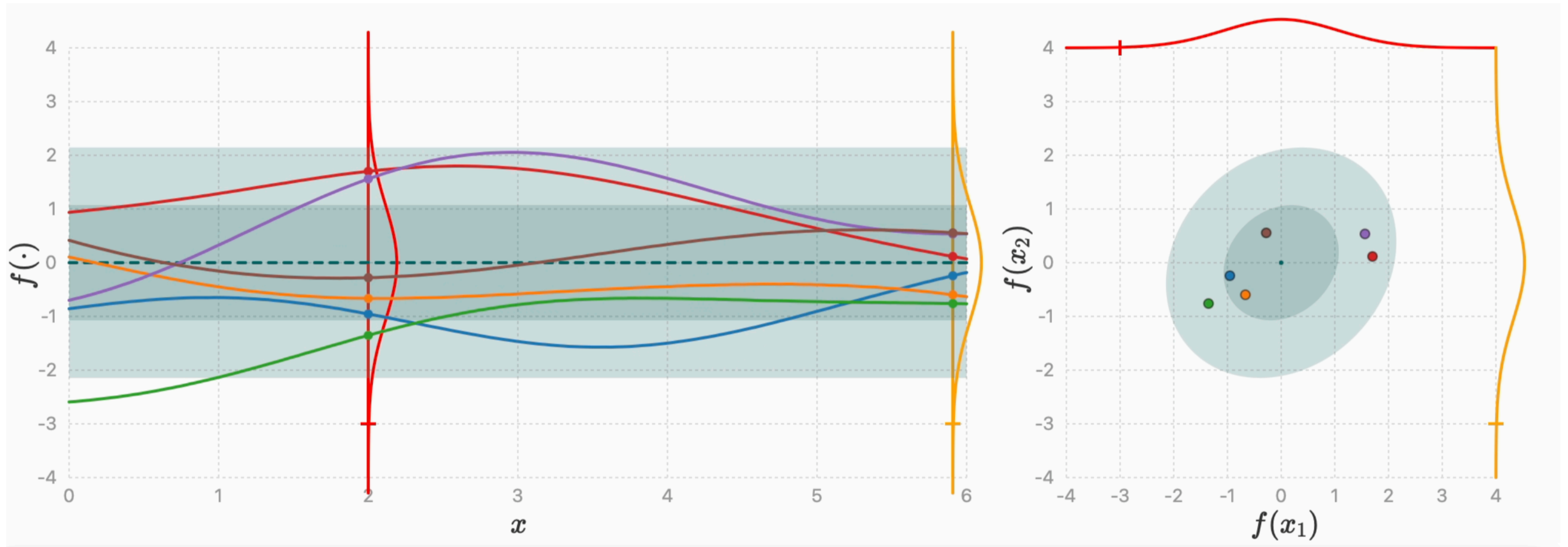
Approximating true function with more data



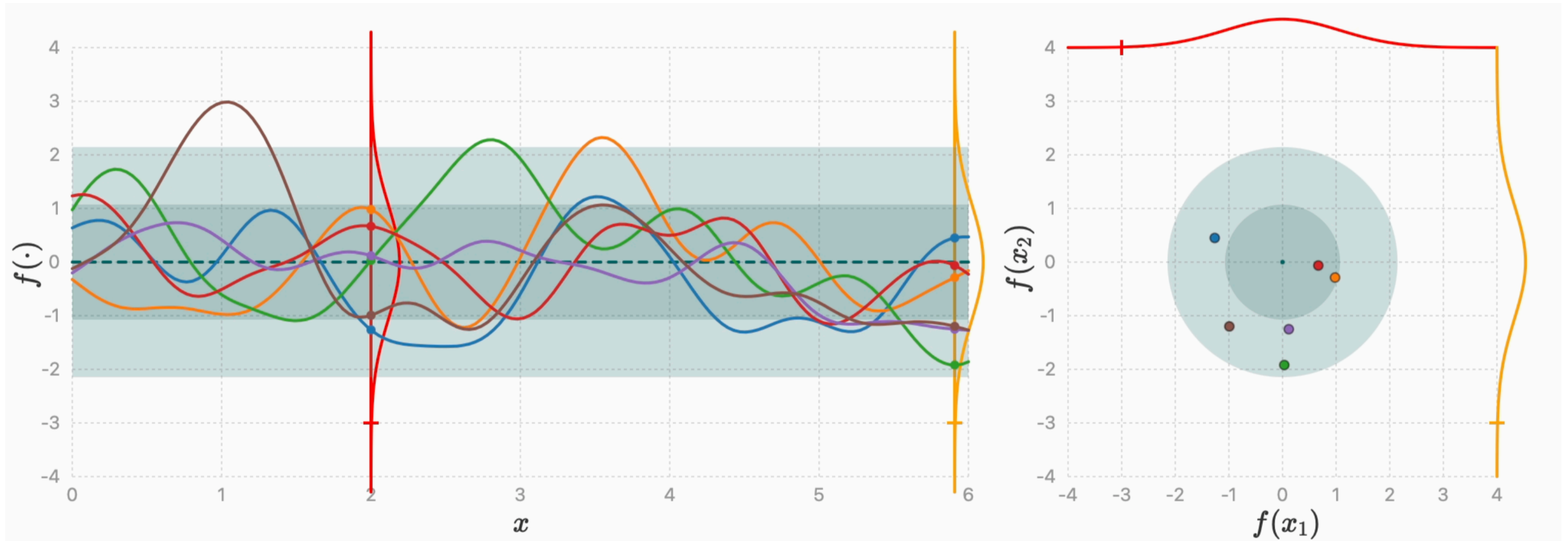
Non-parametric approach



Non-parametric approach



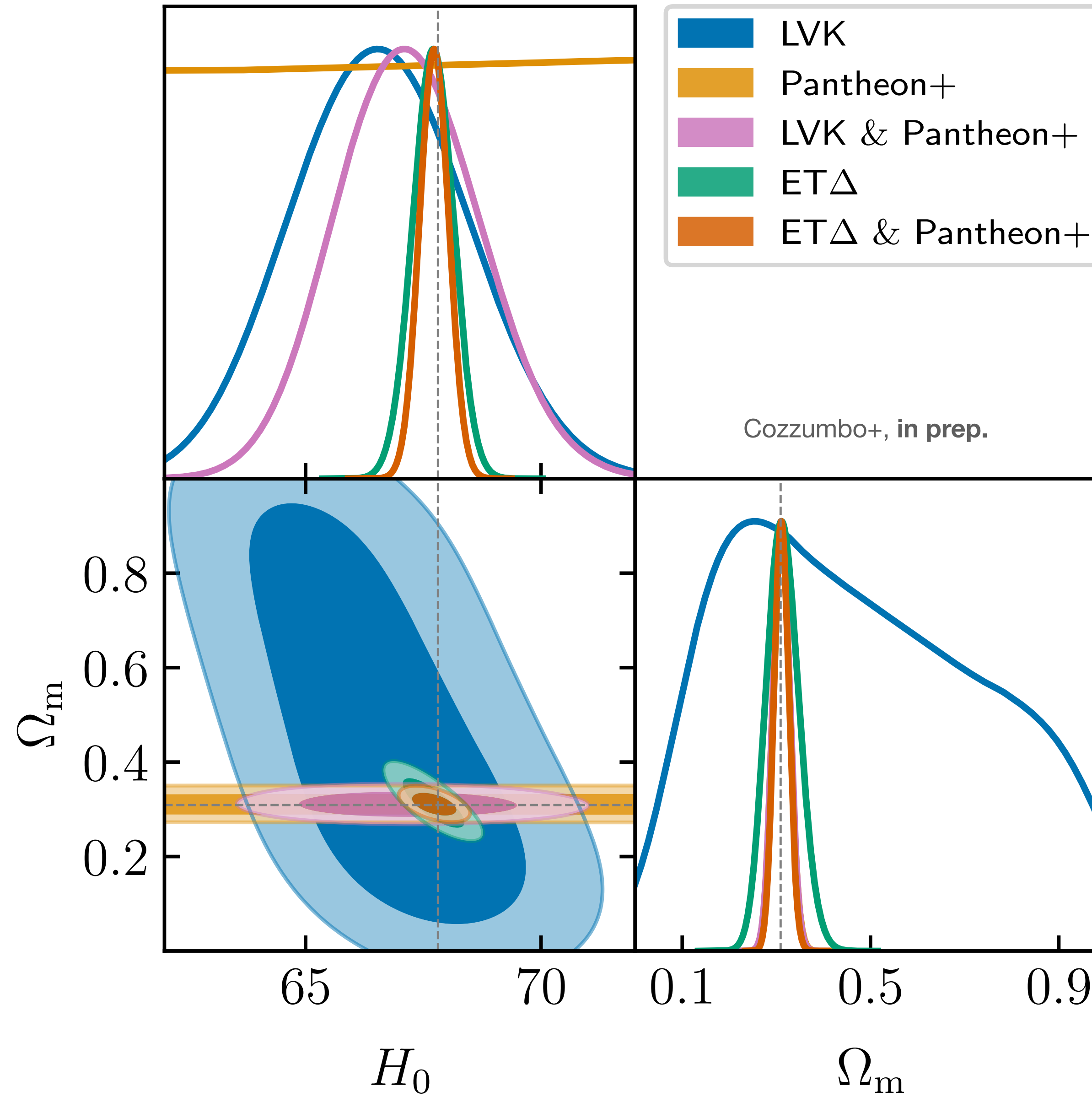
Non-parametric approach



Parametric approach

Injected

Λ CDM *Planck18*



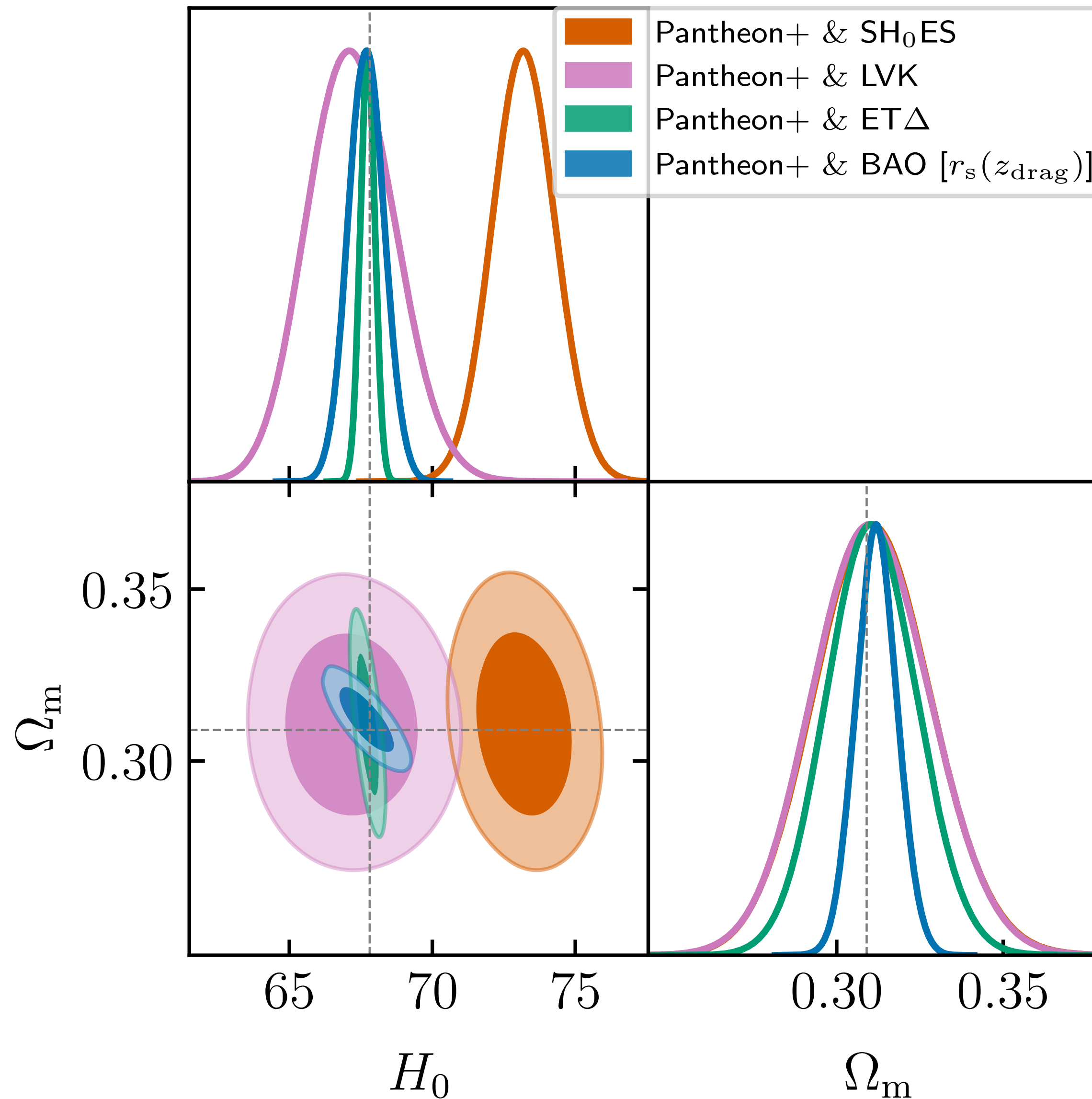
Fit

Λ CDM

Parametric approach

Injected

Λ CDM *Planck18*

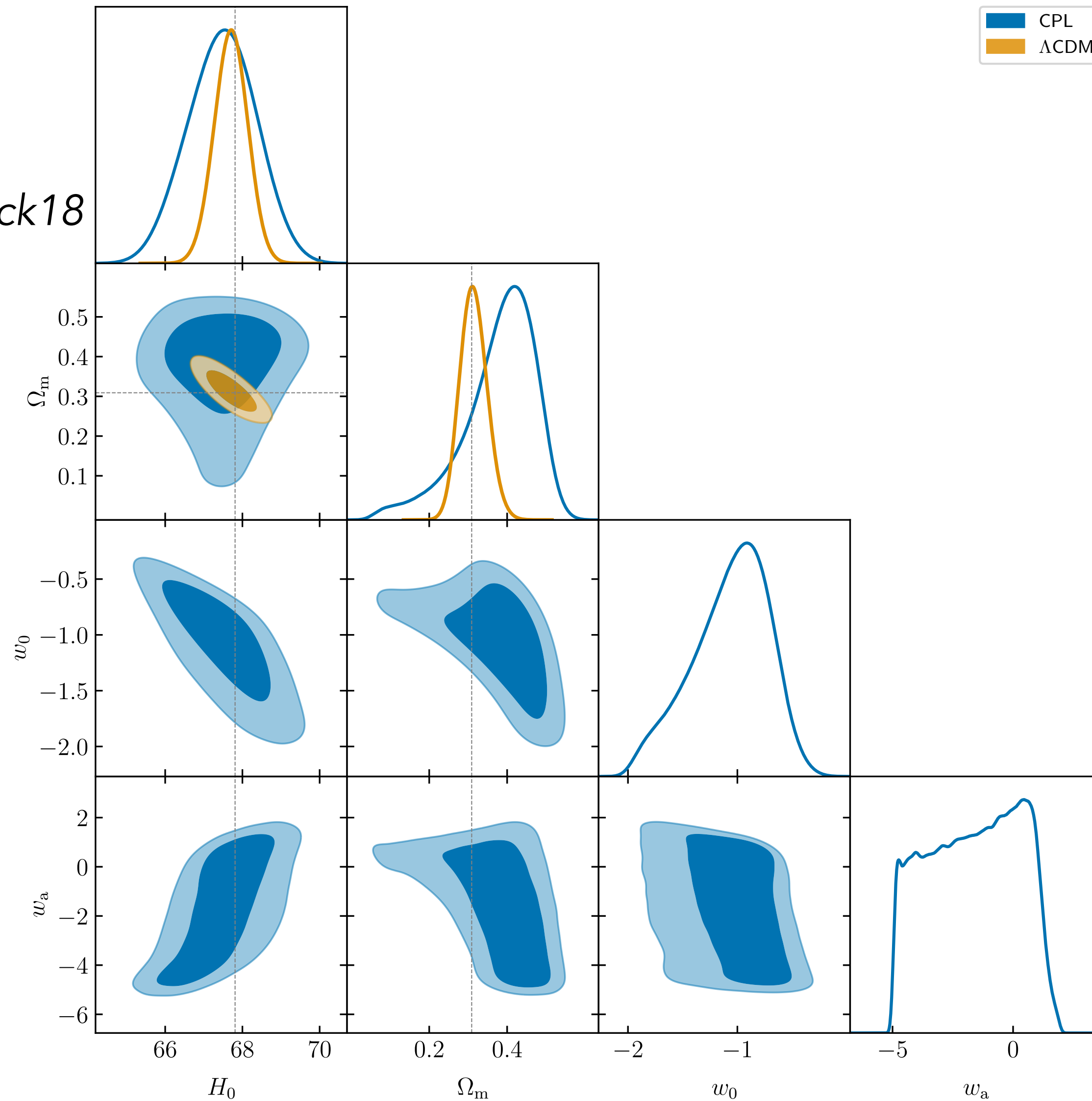


Fit

Λ CDM

Parametric approach

Injected
 Λ CDM Planck18



Fit
 CPL

$$h^2(z) = \frac{H^2(z)}{H_0^2} = \Omega_{m,0} (1+z)^3 + (1 - \Omega_{m,0}) f_{\text{DE}}(z)$$

$$w(z)^{\text{CPL}} = w_0 + w_a \frac{z}{1+z}$$

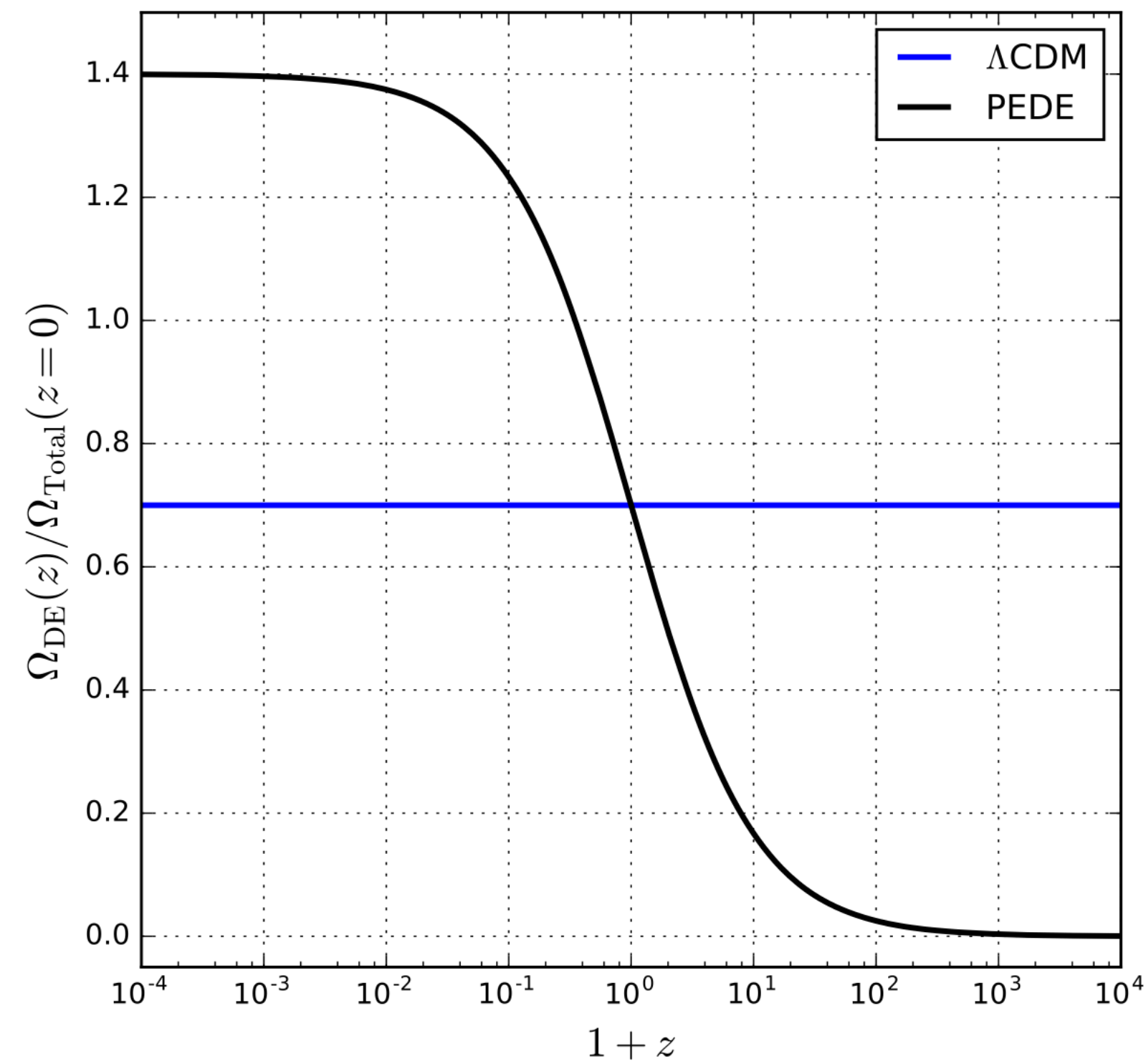
$$f_{\text{DE}}(z) = (1+z)^{3(1+w_0+w_a)} \exp\left[\frac{-3w_a z}{1+z}\right]$$

1b0+, in prep.

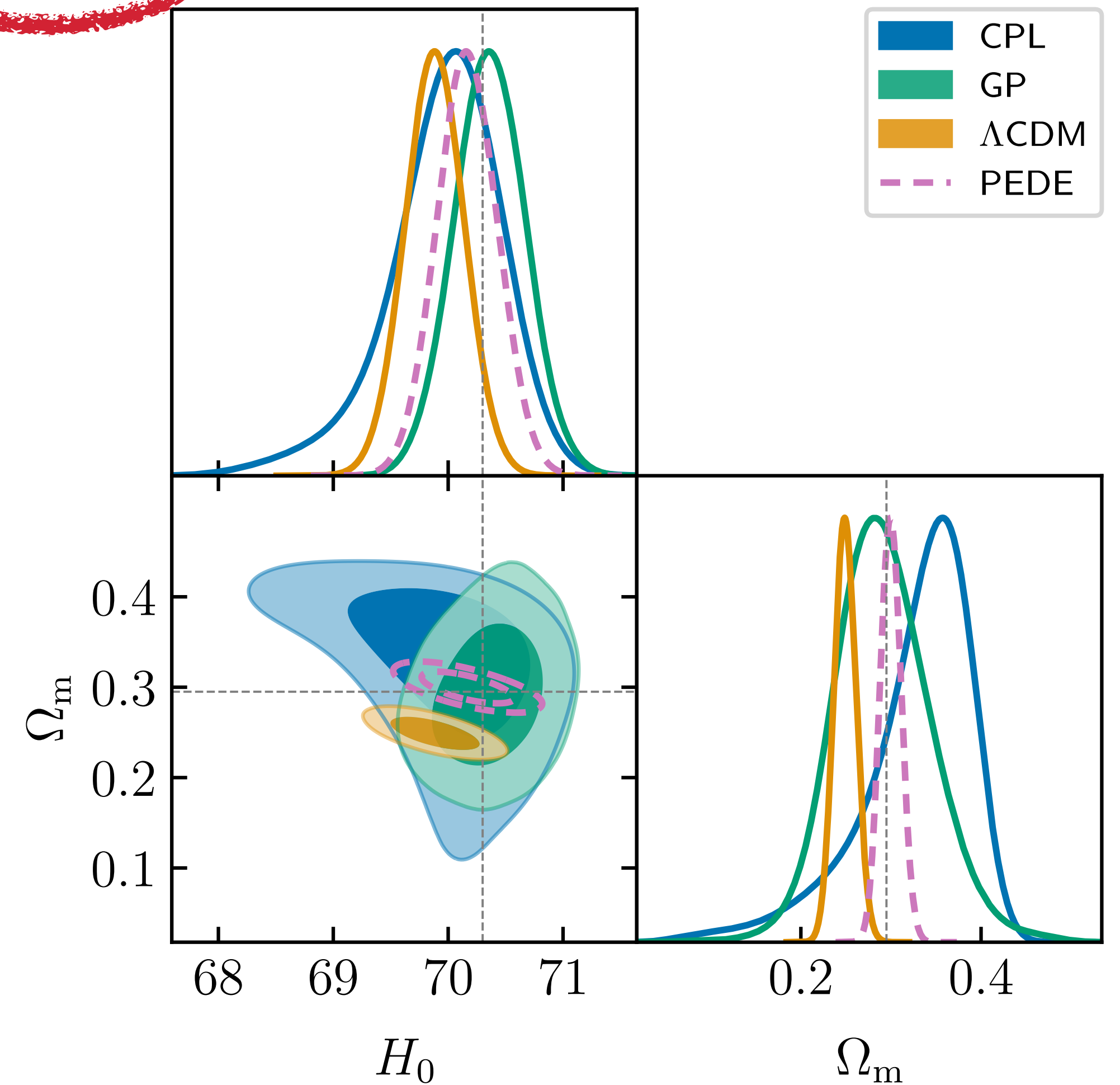
Non-parametric approach

PEDE Universe | Pantheon+ & ET Δ + CE

Phenomenologically Emergent Dark Energy

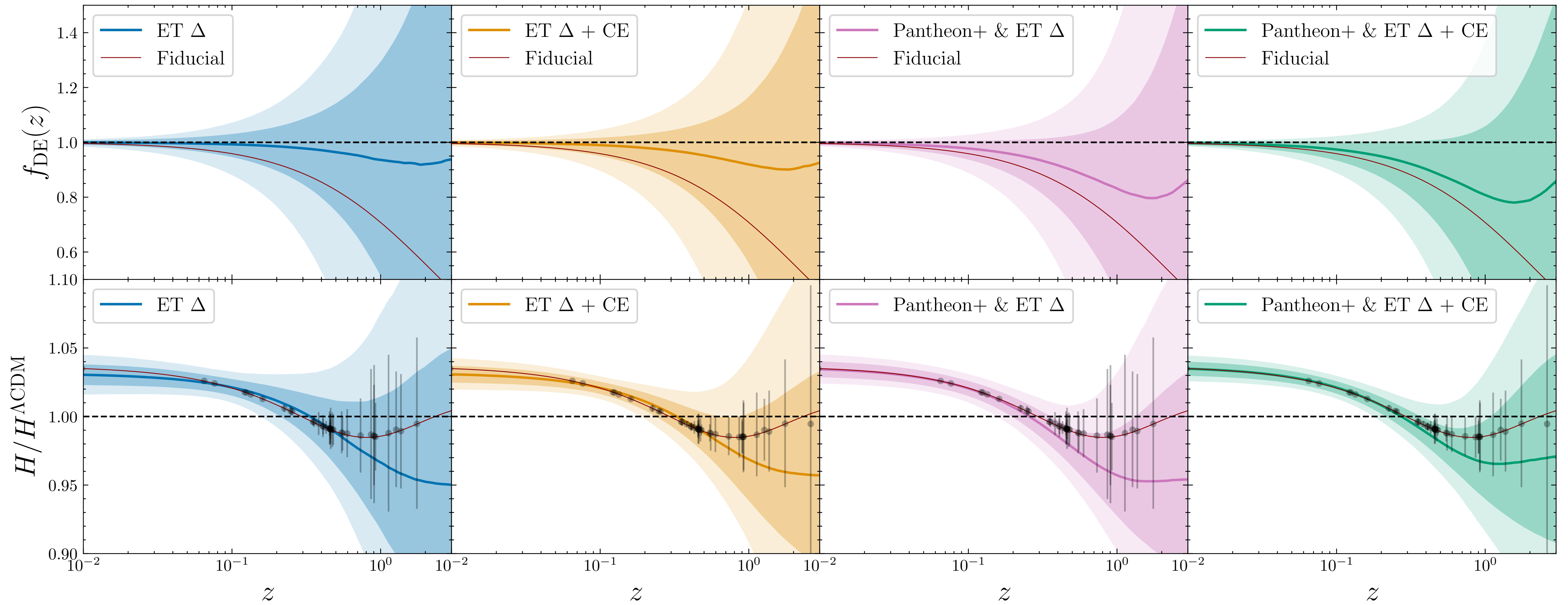


Li and Shafieloo, 2019



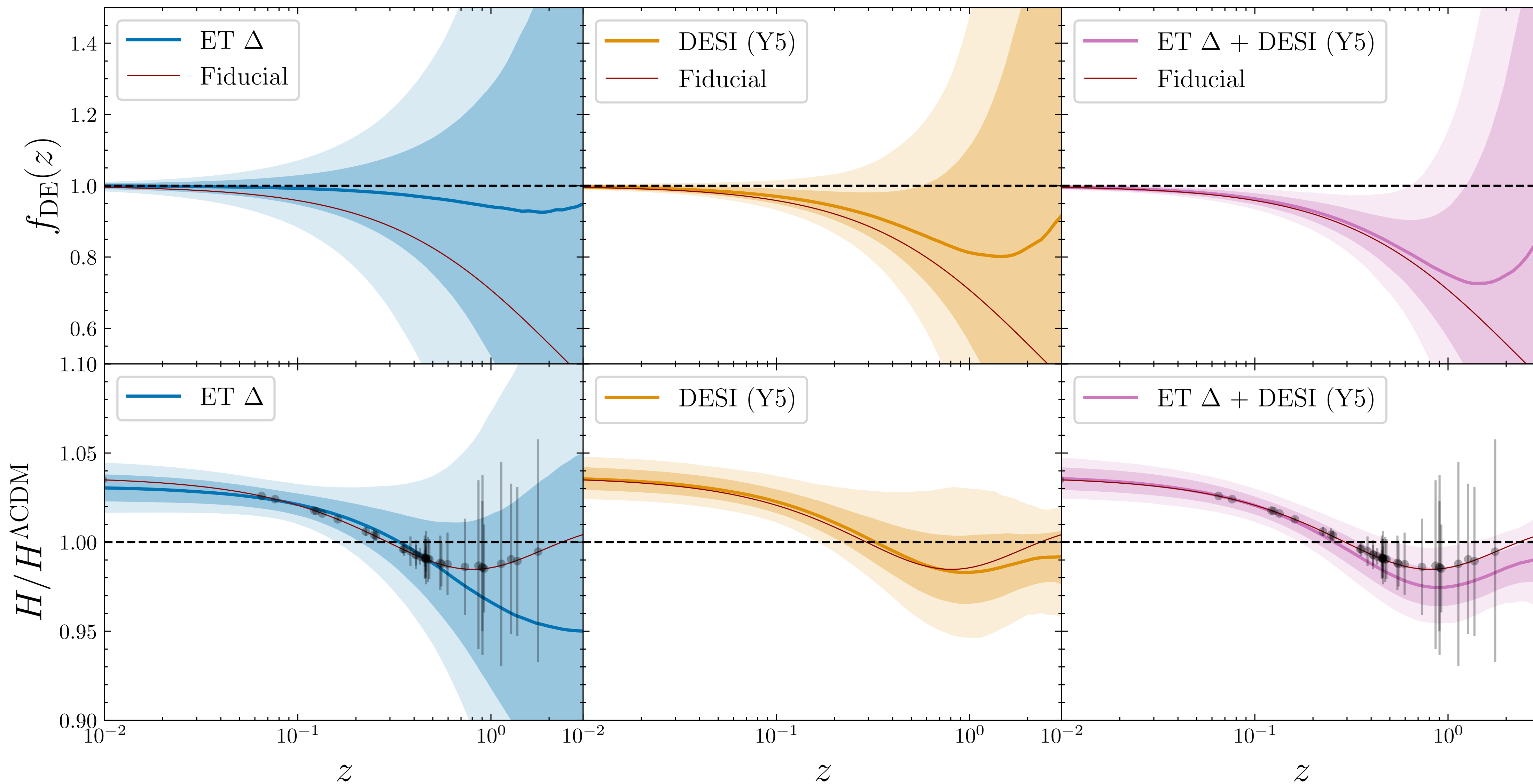
Cozzumbo+, in prep.

Non-parametric approach



Cozzumbo+, in prep.

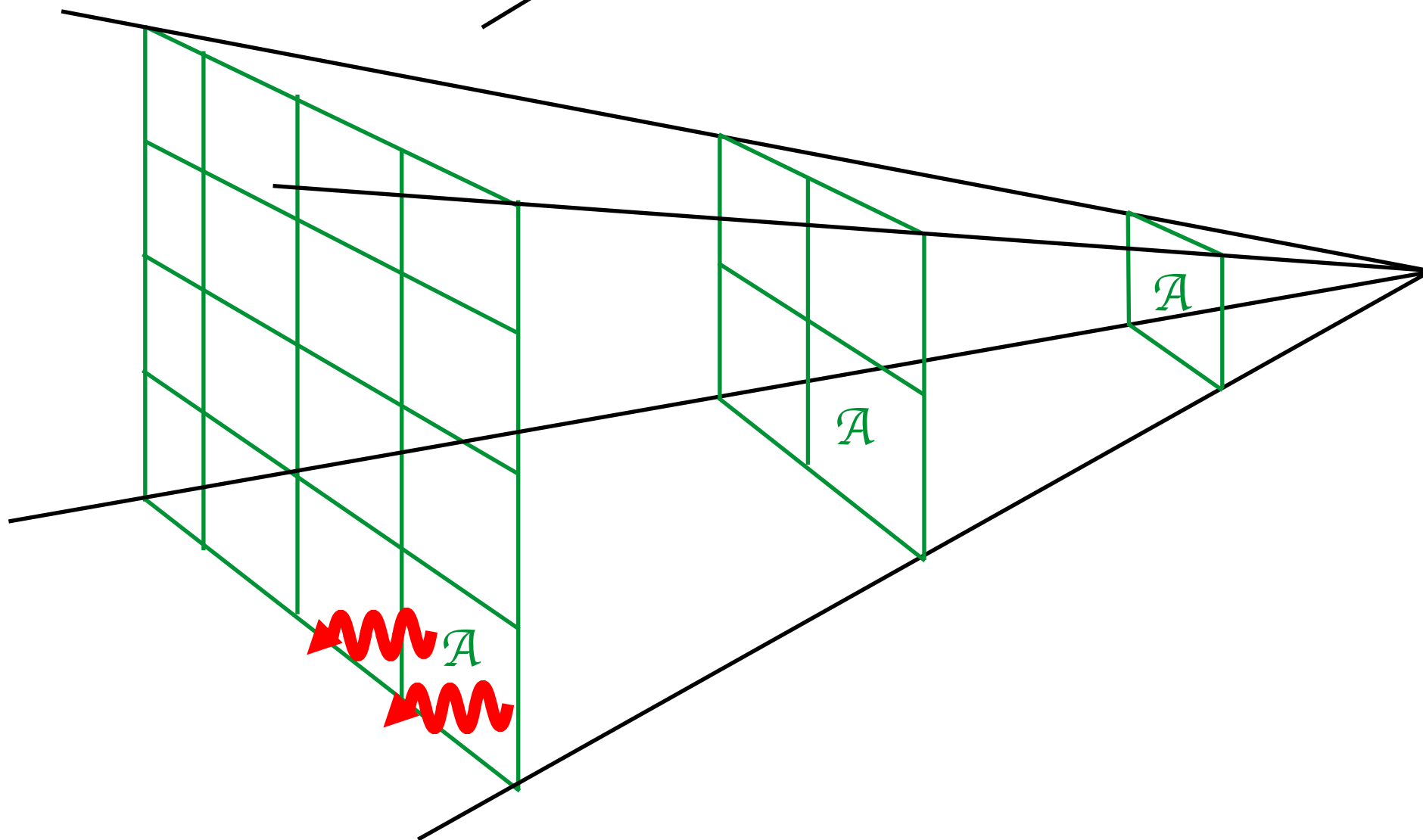
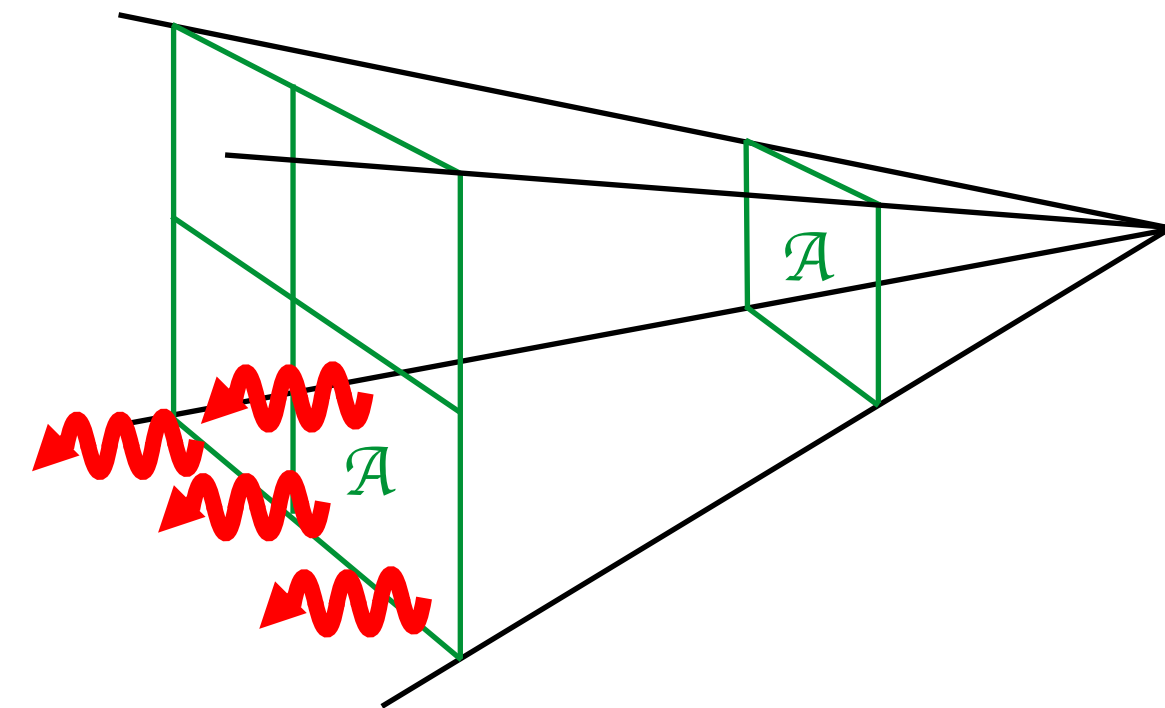
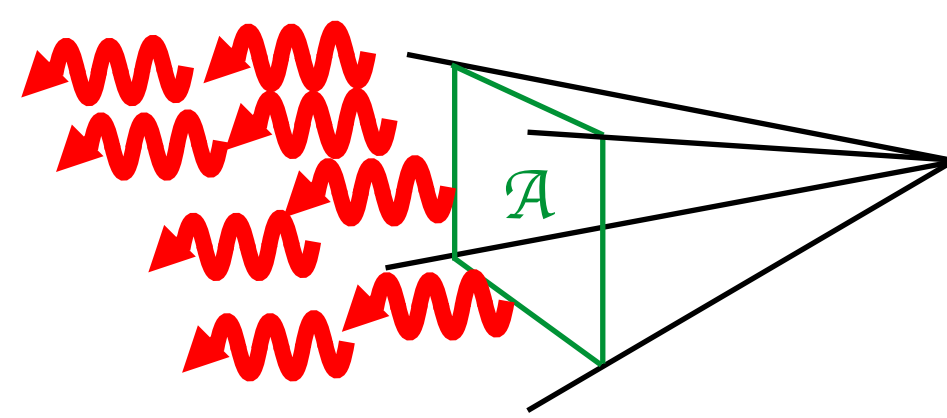
Non-parametric approach



Conclusions

- We compare different catalogs of GRBs and configuration of 3G GW detectors to understand the **future prospects of cosmological constraints with Bright Sirens**
- We compare parametric and non-parametric approaches, underlining the **biases incurring when choosing the wrong fitting model**.
The non-parametric reconstruction is a factor **~ 1.5 better** than the parametric one.
- We show the potential of a model-independent reconstruction for **Einstein Telescope and next generation cosmological probes**.
With less than **40 GRBs** we will be able to achieve unprecedented precision on H_0 and Ω_m and accurately reconstruct the DE density evolution.

Standard candles



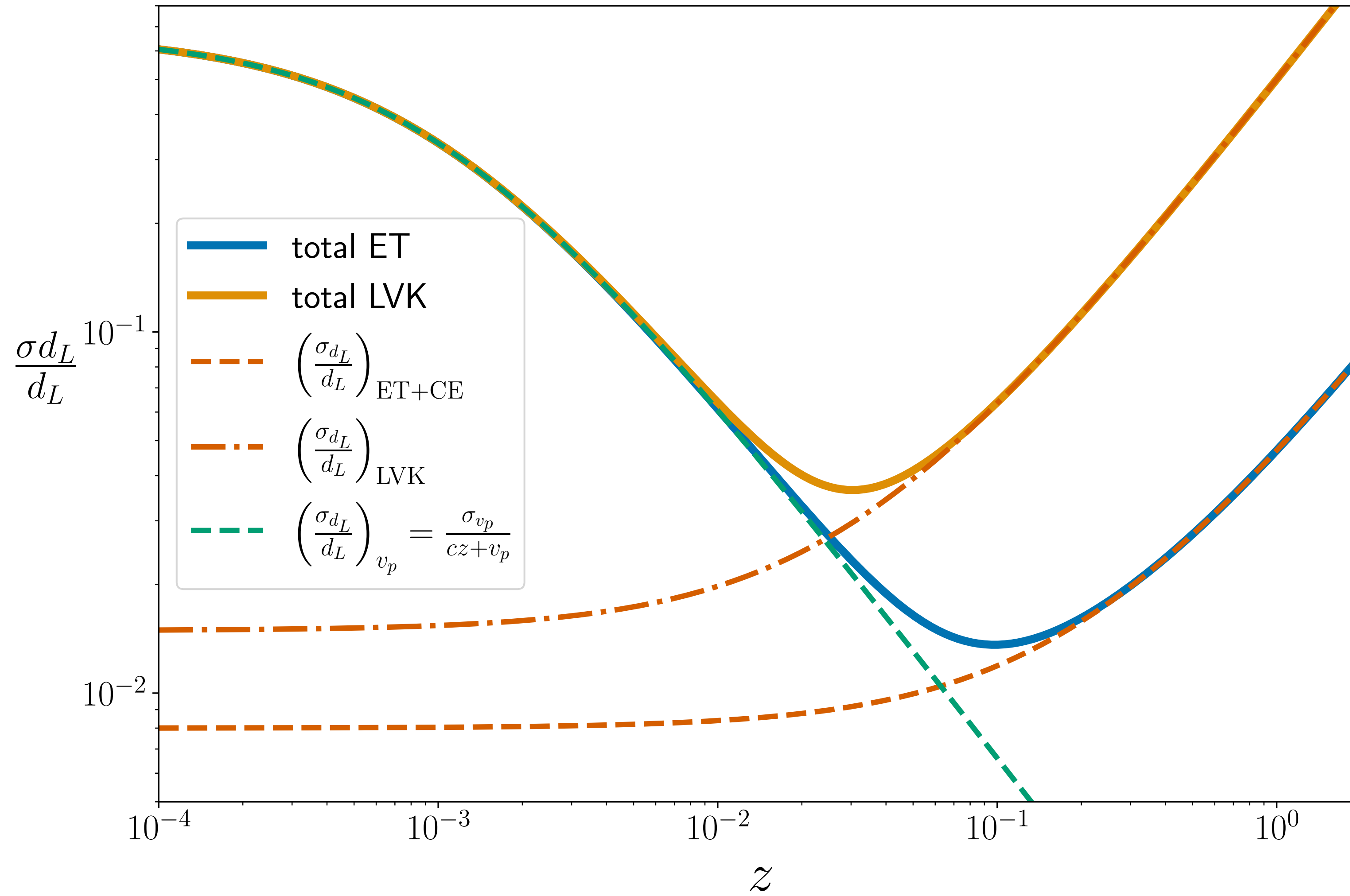
Related to absolute magnitude (M)

$$d_L^2 = \frac{L}{4\pi F}$$

Measured

$$m - M = \mu = 5 \log_{10} \left(\frac{d_L}{1 \text{Mpc}} \right) + 25$$

Systematics



Systematics

