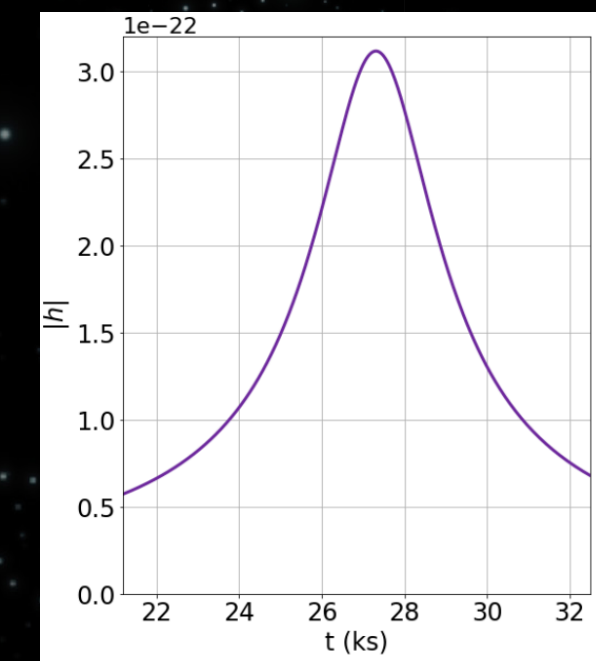
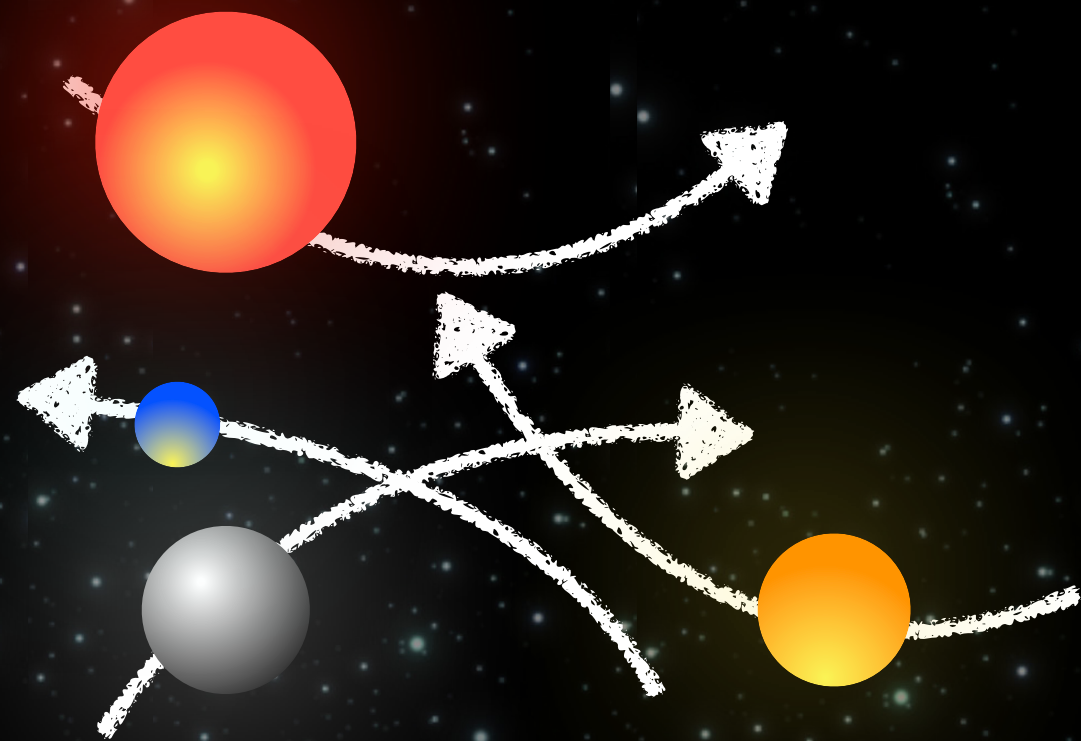


# Stars & Black Holes Encounters in Young Star Clusters



**Sara Rastello**

*In coll. with :* **Giuliano Iorio, Long Wang, Mark Gieles**



UNIVERSITAT DE  
BARCELONA



Institut de Ciències del Cosmos  
UNIVERSITAT DE BARCELONA



# Tidal Disruption Events (Macro-TDEs)

A star orbiting around a SMBH is disrupted during the first pericenter passage once the tidal forces of the SMBH exceed the self-gravity of the star

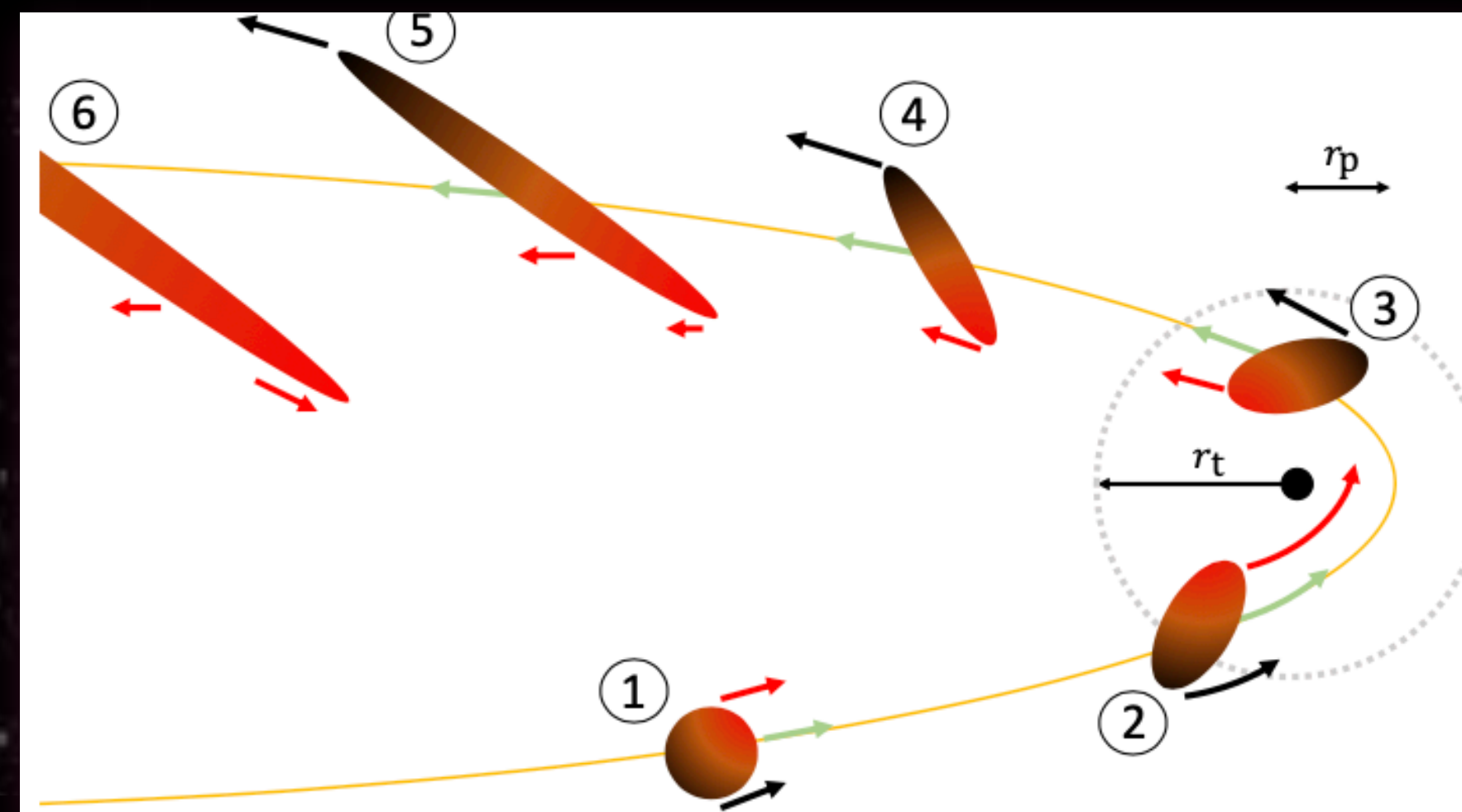
*Tidal Radius  $R_t$*

$$R_t = R_* \left( \frac{M_{\text{BH}}}{M_*} \right)^{1/3} \approx 7 \times 10^{12} \left( \frac{R_*}{R_\odot} \right) \left( \frac{M_*}{M_\odot} \right)^{-1/3} \left( \frac{M_{\text{BH}}}{10^6 M_\odot} \right)^{1/3} \text{ cm}$$

Hills 1975,  
Rees 1988

Kobayashi 2004  
Komossa 2015

$$M_{\text{SMBH}} = 1e6 M_\odot \quad M_s^* = 1M_\odot \quad R_s^* = 1R_\odot \quad R_t \sim 100 R_\odot$$

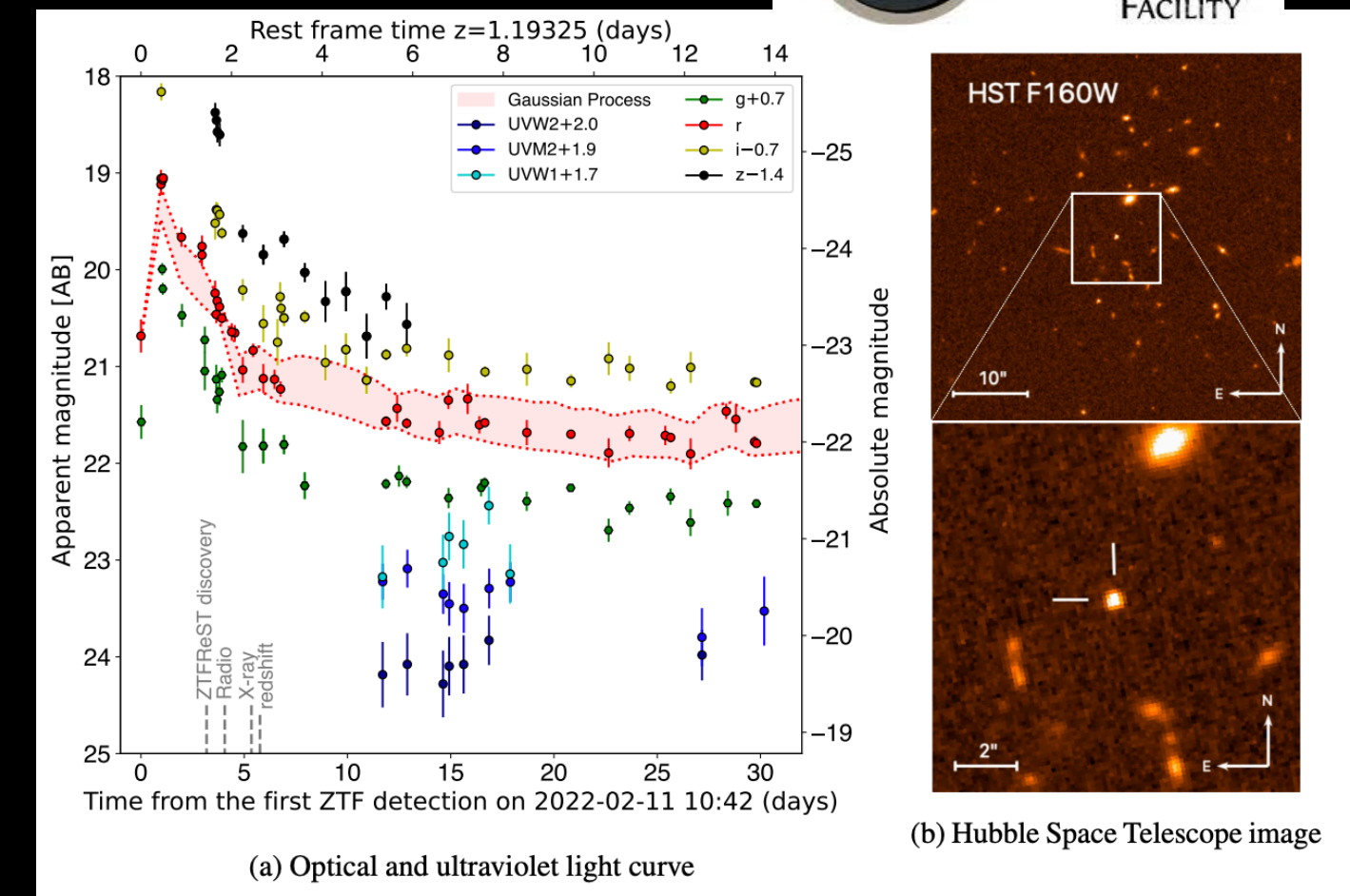
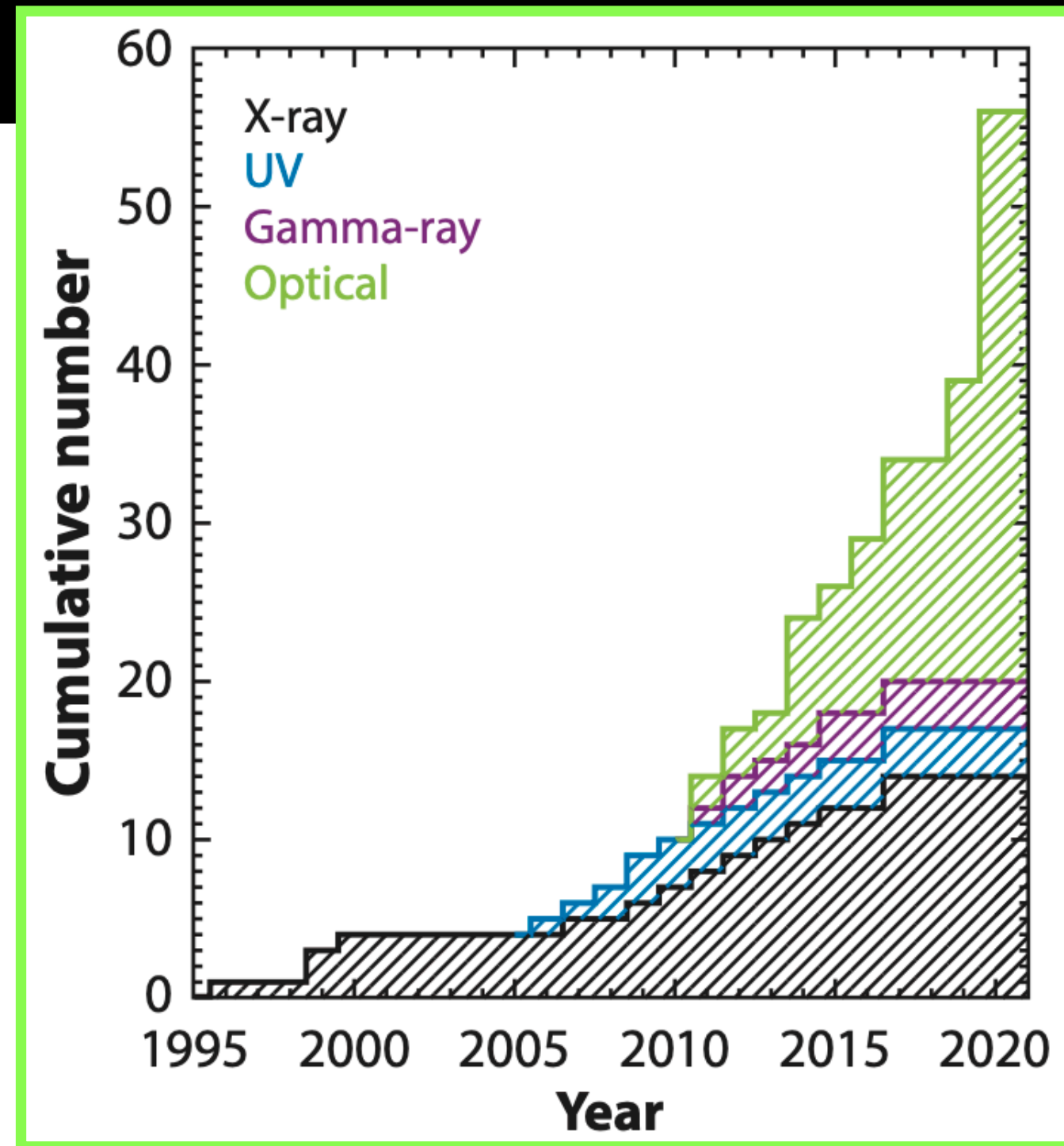
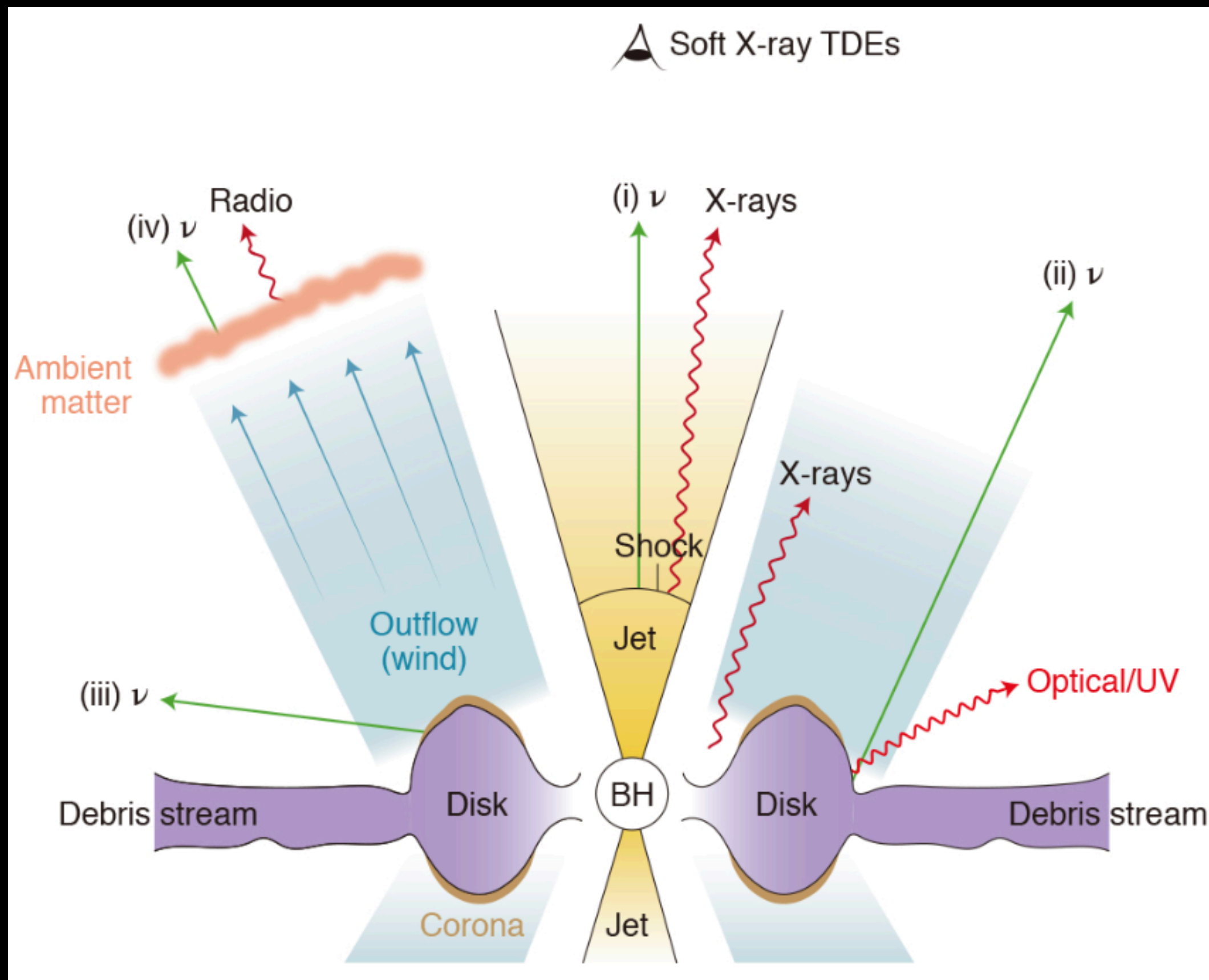


Wever & Ryu, 2023

#SMBHs

# TDEs as Multi-Messenger Sources I

## Electro Magnetic (EM) emission



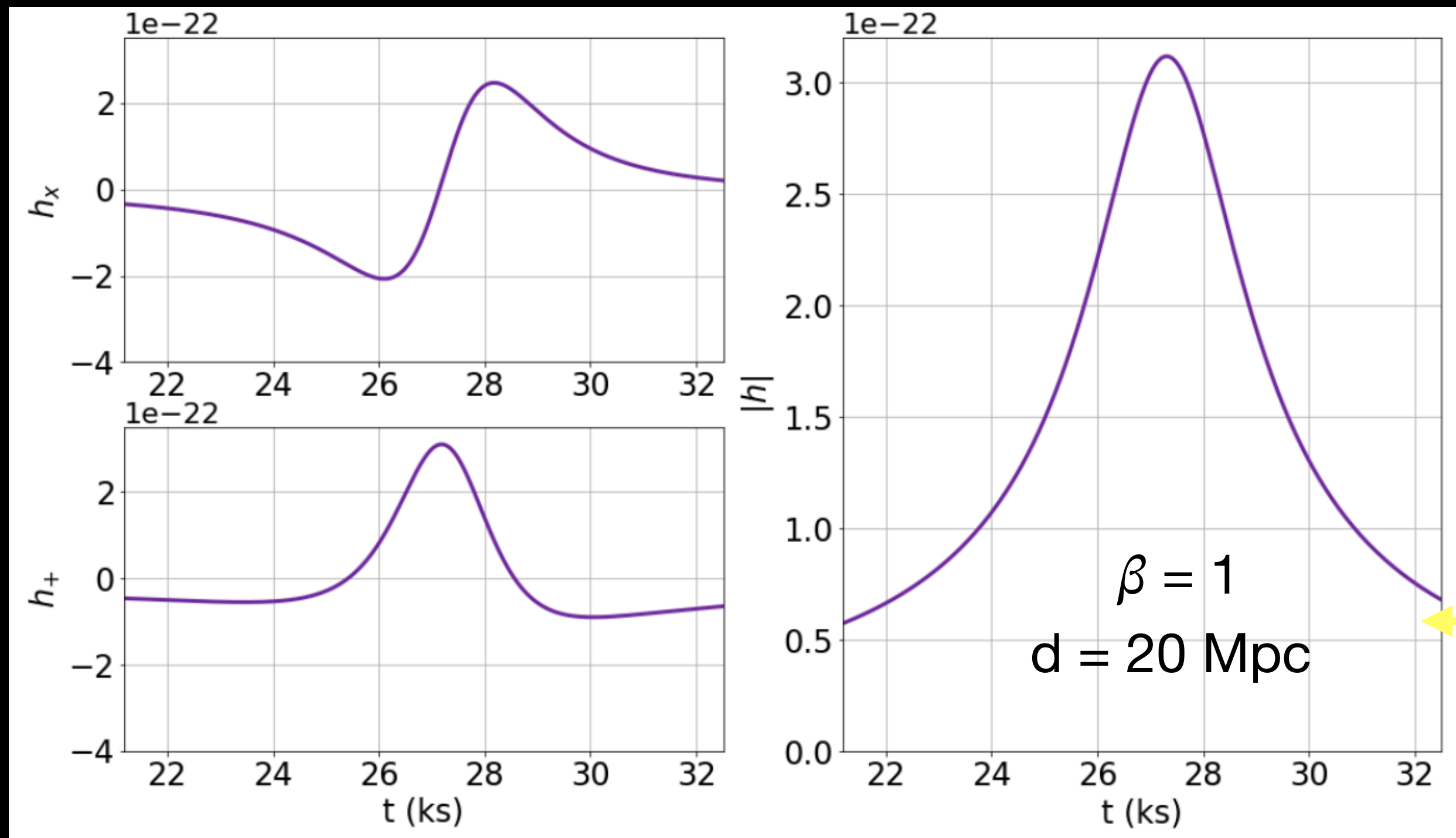
Andreoni et al., 2022

~ hundred of TDEs detected with EM

Gezari 2021

# TDEs as Multi-Messenger Sources II

## Gravitational wave (GW) signals



GW burst emitted when the star is torn apart [variation of the quadrupole mass of the BH-star system.]

*Kobayashi et al. 2004*

Free online catalog

<https://gwcataloguetdes.fisica.unimi.it/>

*Toscani et al., 2022*

Sun-like star on a parabolic orbit around a SMBH  $1e6 M_{\odot}$

*Guillochon et al. 2009; Stone et al. 2013; Toscani et al., 2019,2022*

GW frequency in  
the LISA band

# micro-TDEs ( $\mu$ -TDEs)

#BHs

Hills 1975;  
Rees 1988

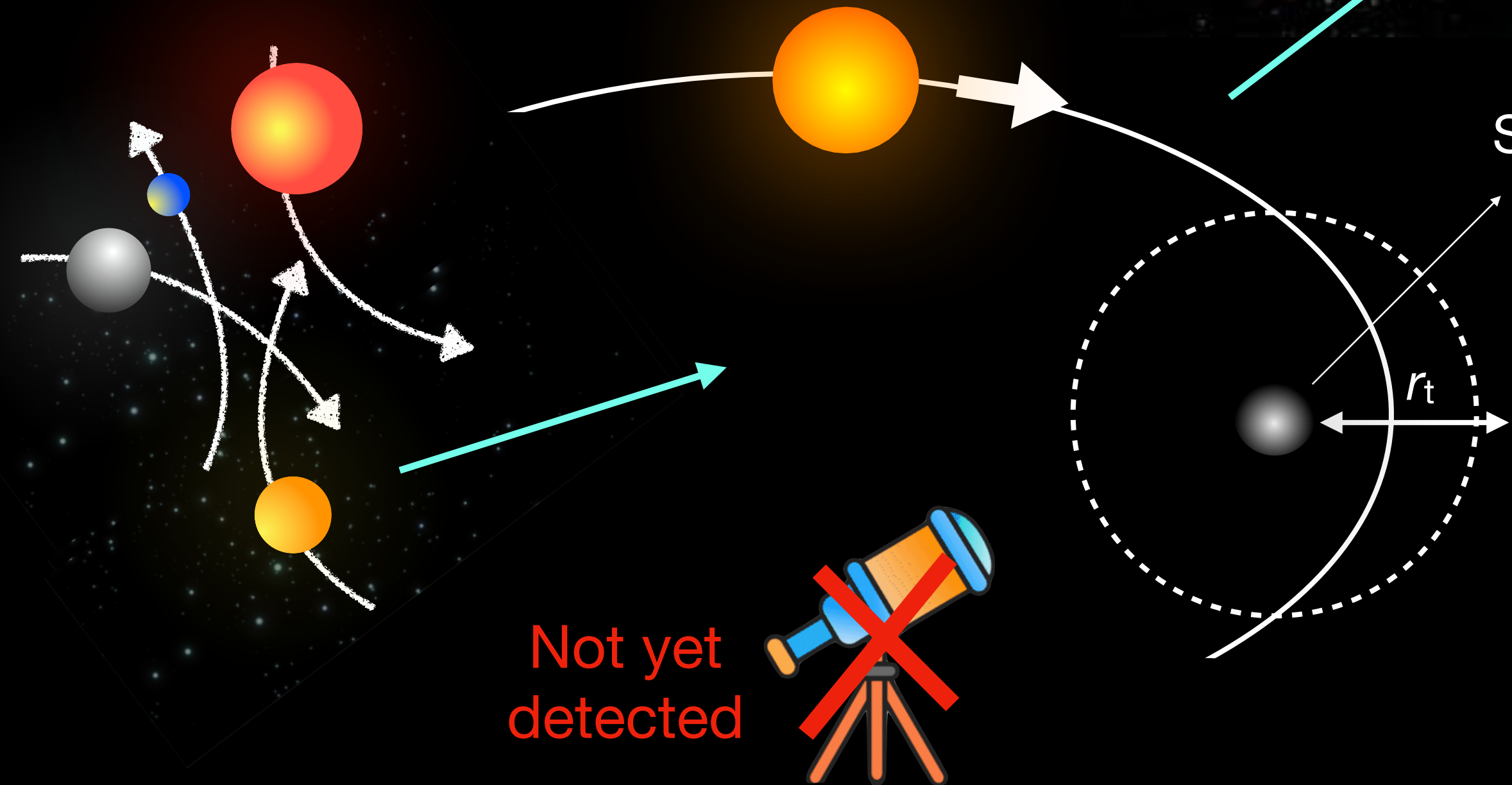
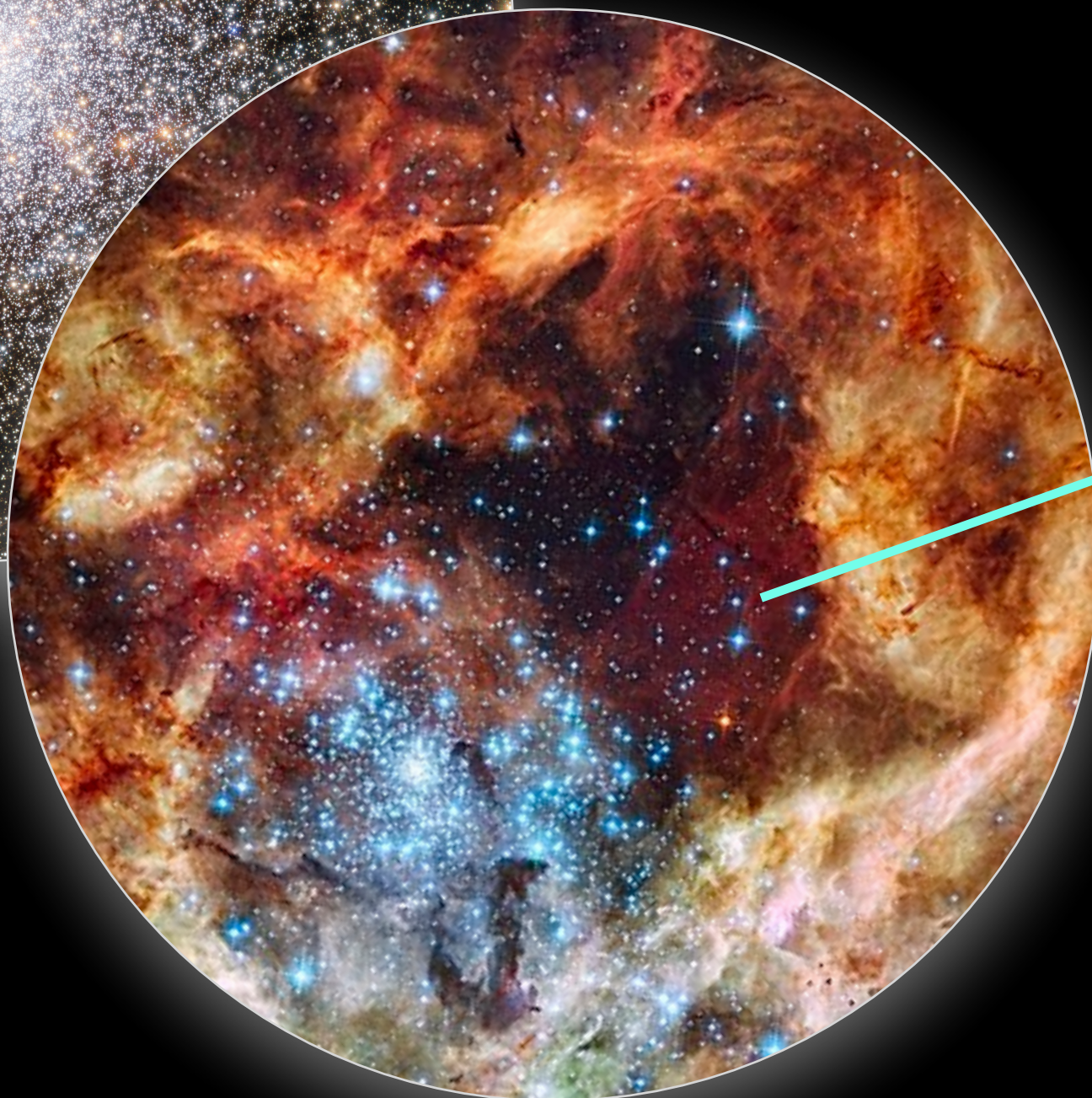
$$R_t = R_* \left( \frac{M_{\text{BH}}}{M_*} \right)^{1/3}$$

A star is destroyed in a close encounter with a compact object (CO) as **stellar mass BH, NS or WD**

Perets et al., 2016

Occur in **dense star clusters** where *dynamical encounters* between stars and COs are frequent

Rastello et al., 2019; Kremer et al., 2019,2021,2023;  
Ryu et al., 2022,2023a,c,d; Vynatheya et al., 2024; Xin et al., 2024



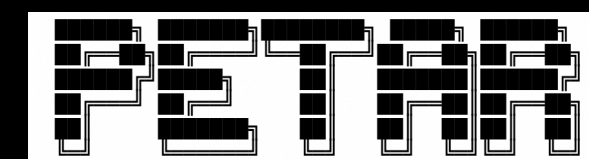
Stellar mass BH  
(few-100  $M_{\odot}$ )

# YSCs models: SCs prop.

Suite of numerical high-precision direct  $N$ -body simulations of massive collisional realistic

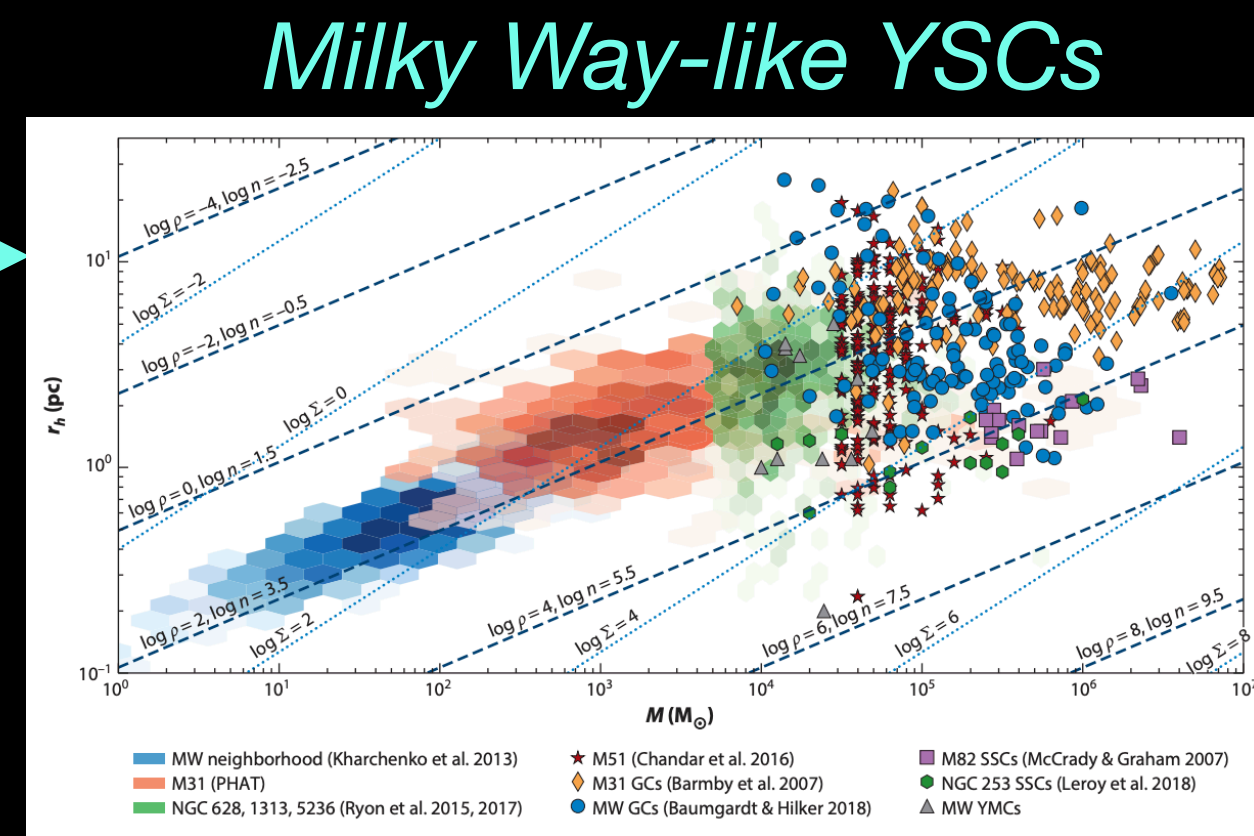
**Young Star Clusters** with the state-of-the-art  $N$ -body code **PE TAR** Wang et al., 2020

- $5e4 < M_{sc} (M_{\odot}) < 5e5$
- **King (1966)** Density profile ( $r_h$  &  $\rho$ ) with *limepy* lib. (**Gieles & Zocchi 2015**)
- $Z = 0.0002-0.02$
- MW2014 tidal field (Galpy, **Bovy 2014**)
- YSCs on a Sun-like circular orbit
- BSE as in PeTar (**Banerjee et al. 2020**)
- Delayed SN model
- Mass dependent binary fraction (**Moe & Di Stefano 2017**)



Wang et al., 2020

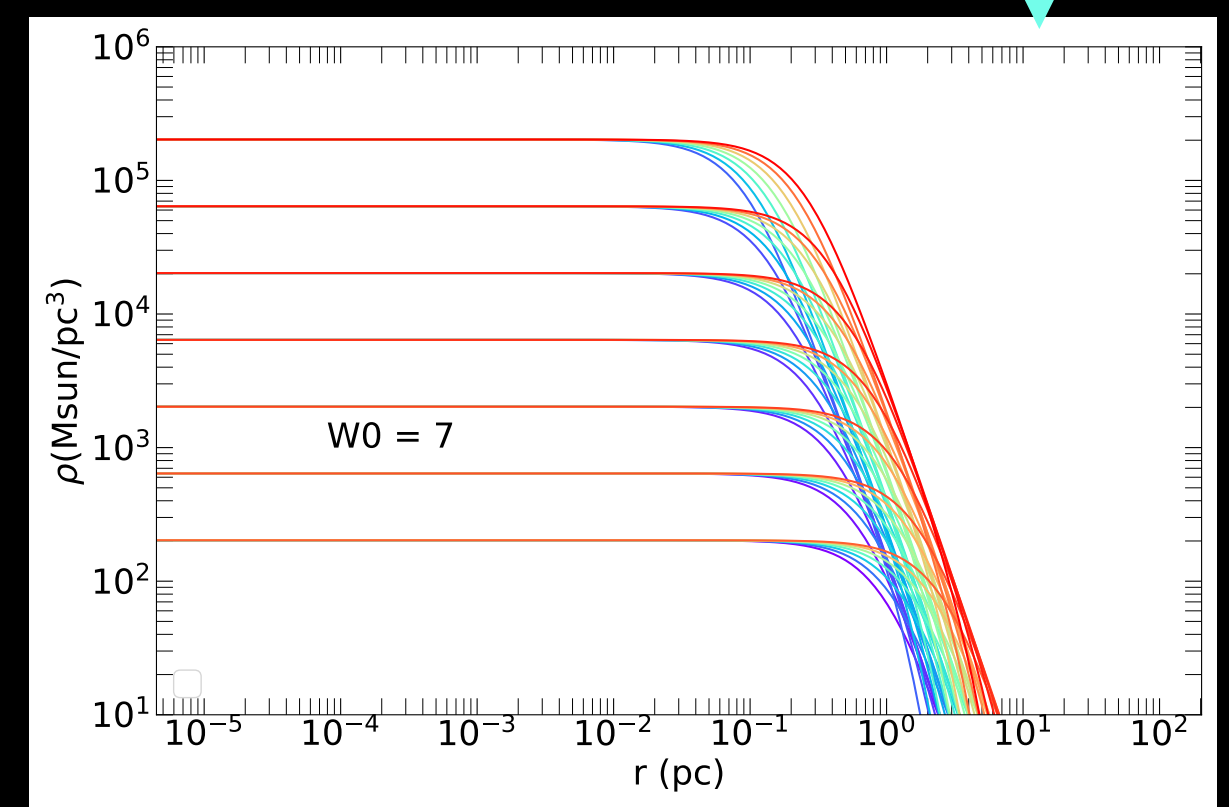
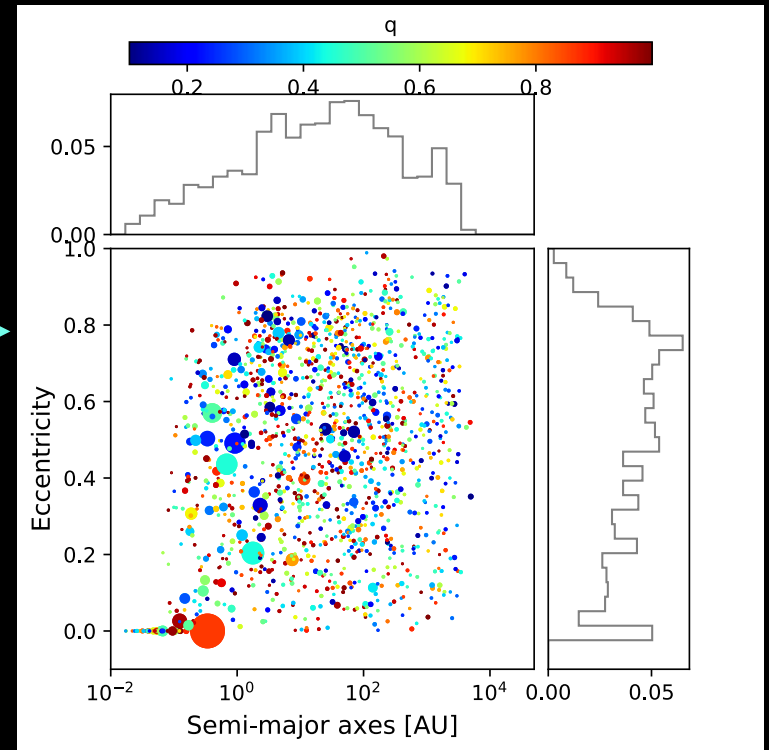
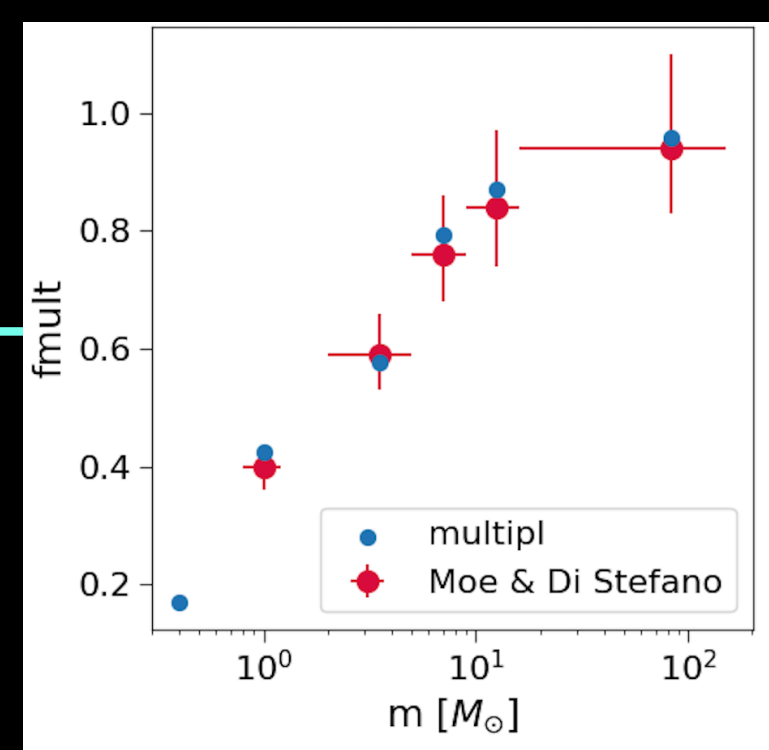
Customized Code Version



PI: S. Rastello  
~2 M at RES

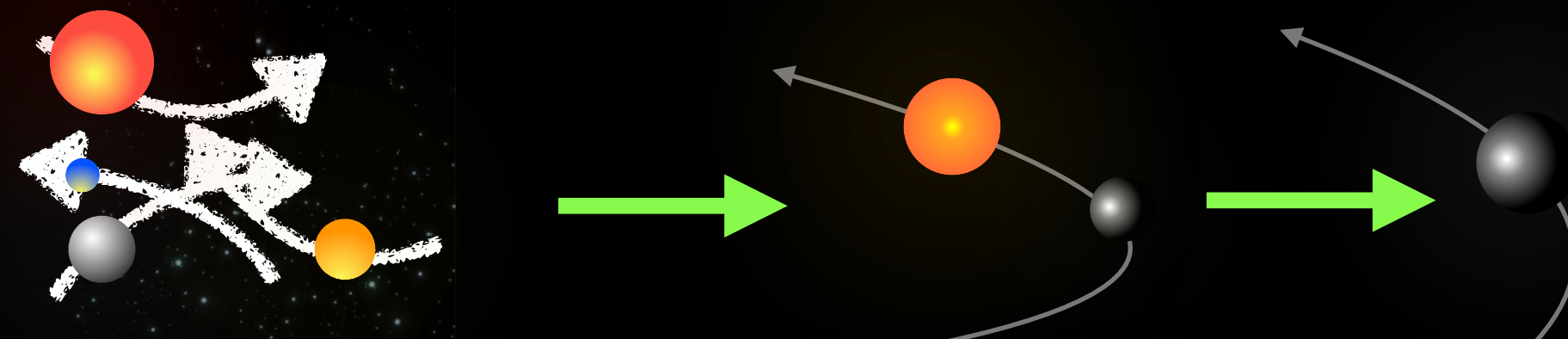


Rastello et al., in prep.

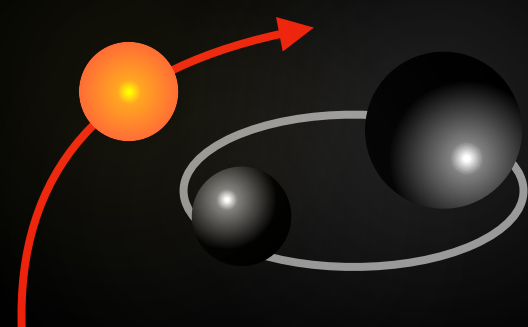


# How can we model $\mu$ -TDEs in SCs?

## 1. Close interactions between single stars and single COs



$$R_t = R_* \left( \frac{M_{\text{BH}}}{M_*} \right)^{1/3}$$

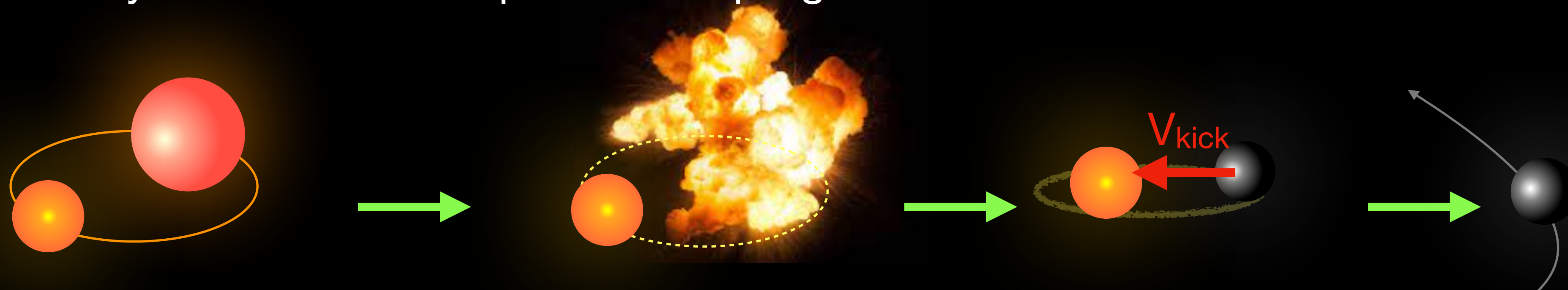


## 2. Close encounters involving binaries

i.e. Star-Star+ CO, CO-CO+Star, Star-CO + star, Star-CO +CO

## 3. Stars destroyed when the companion CO-progenitor receives a natal kick

*Perets et al., 2016;*  
*Michaely et al., 2016;*  
*Hirai & Podsiadlowski 2022;*



# Stellar disruptions : all candidates\*

\* Satisfy the disruption condition  $r_p \leq r_t$

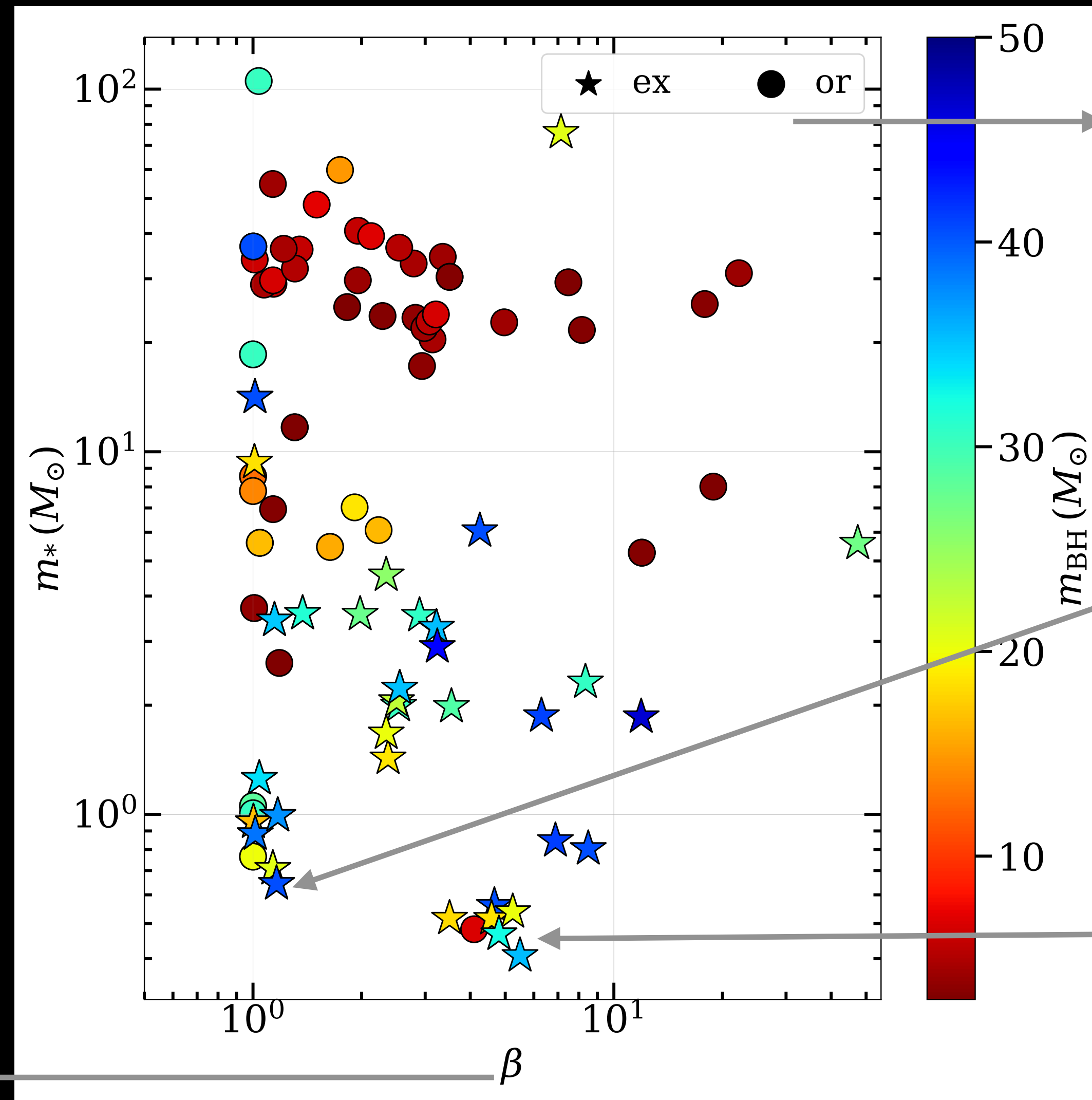
$$R_p \leq R_t = R_* \left( \frac{M_{\text{BH}}}{M_*} \right)^{1/3}$$

55 % or.  $t < 100 \text{ Myr}$

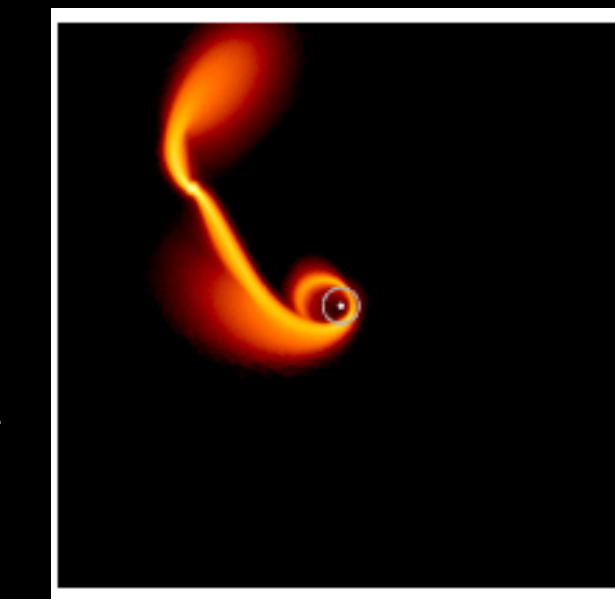
45 % ex.  $t > 100 \text{ Myr}$

$$\beta = \frac{r_t}{r_p}$$

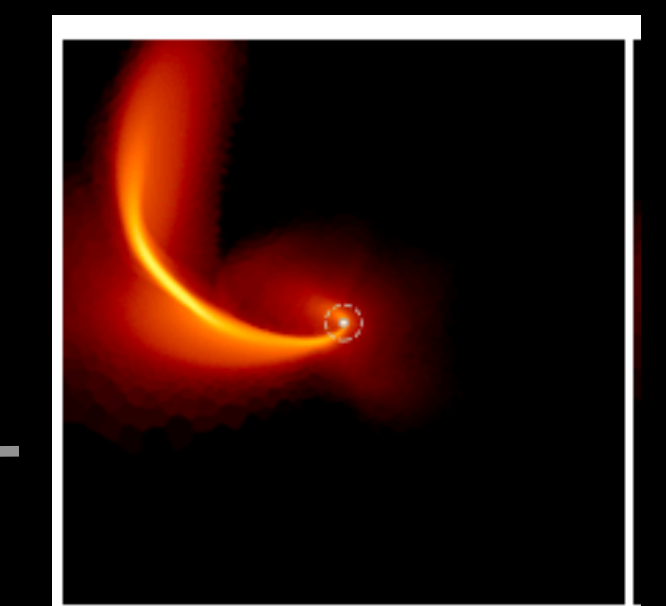
Penetration factor



Original binaries: paired since  $t=0 \text{ Myr}$   
 Exchanged binaries: paired through dynamics



$m_{\text{BH}} = 40.0 M_{\odot}$   
 $m_* = 0.5 M_{\odot}$



Vynatheya et al., 2024

83 % MS, 9 % HG, 7% naked He, 1% WD

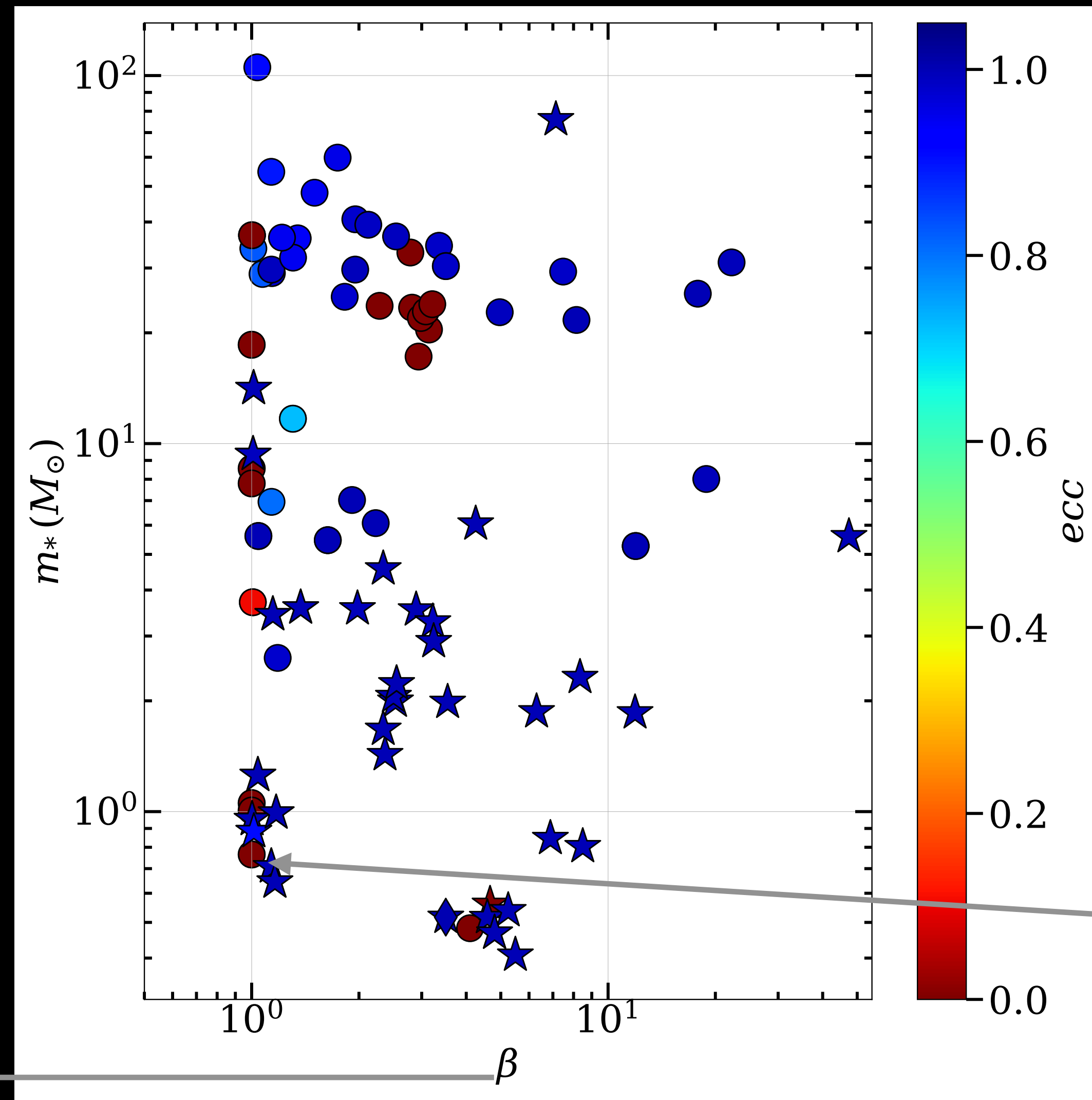


# Stellar disruptions : eccentricity

Most (%) events occur on almost parabolic orbits

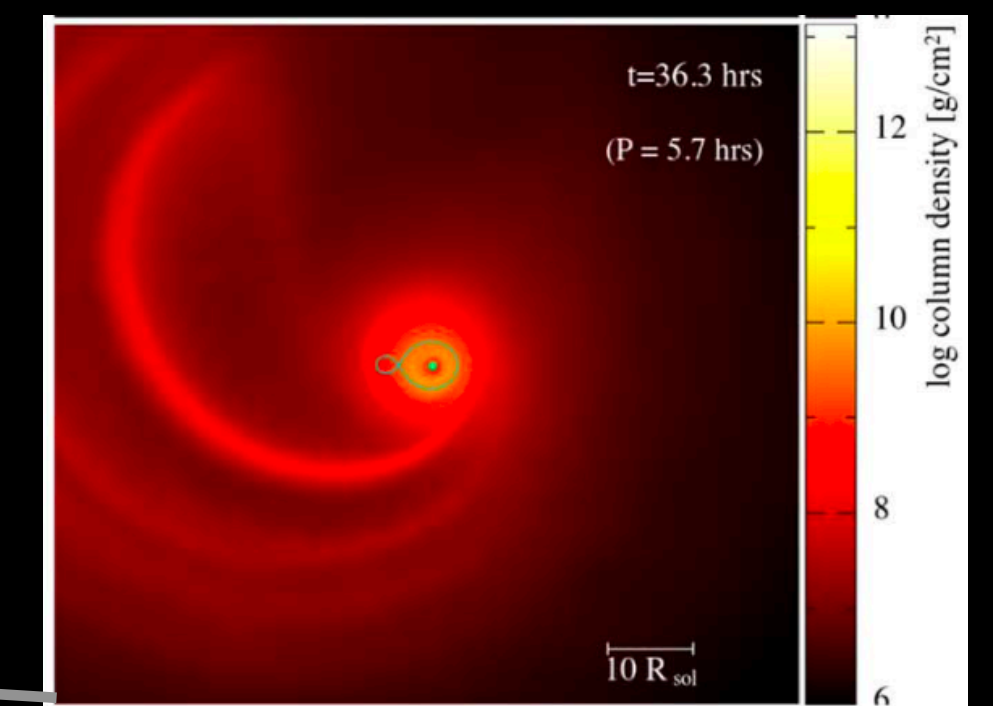
85 %  $0.99 < ecc < 1.1$

$$\beta = \frac{r_t}{r_p}$$



TPE (tidal peeling events) candidates?

$0 < ecc < 0.6$



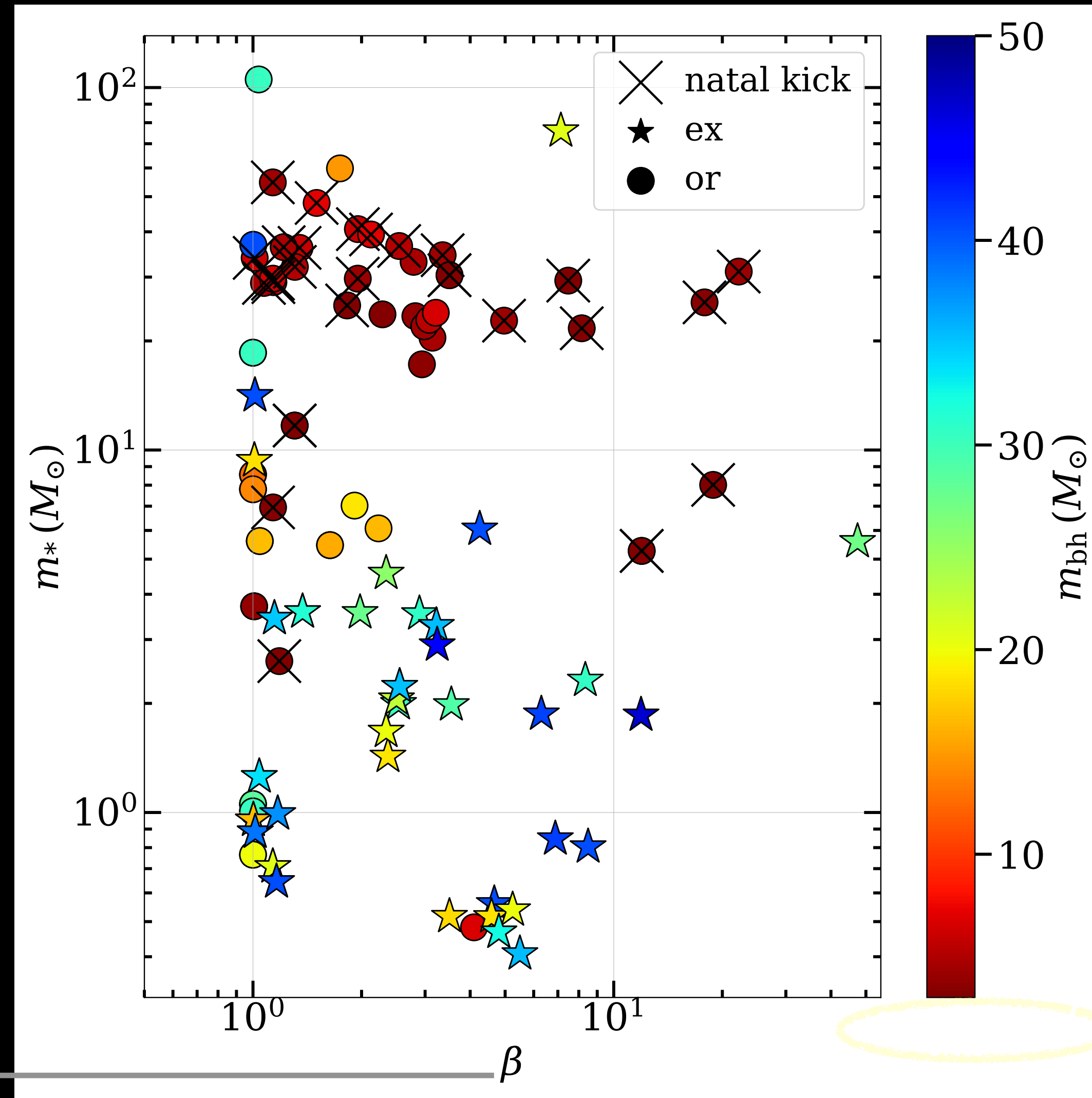
*Xin et al., 2024*

# Stellar disruptions : BH natal kick

Stars disruption induced by orbital change at BH formation

~ 30 %

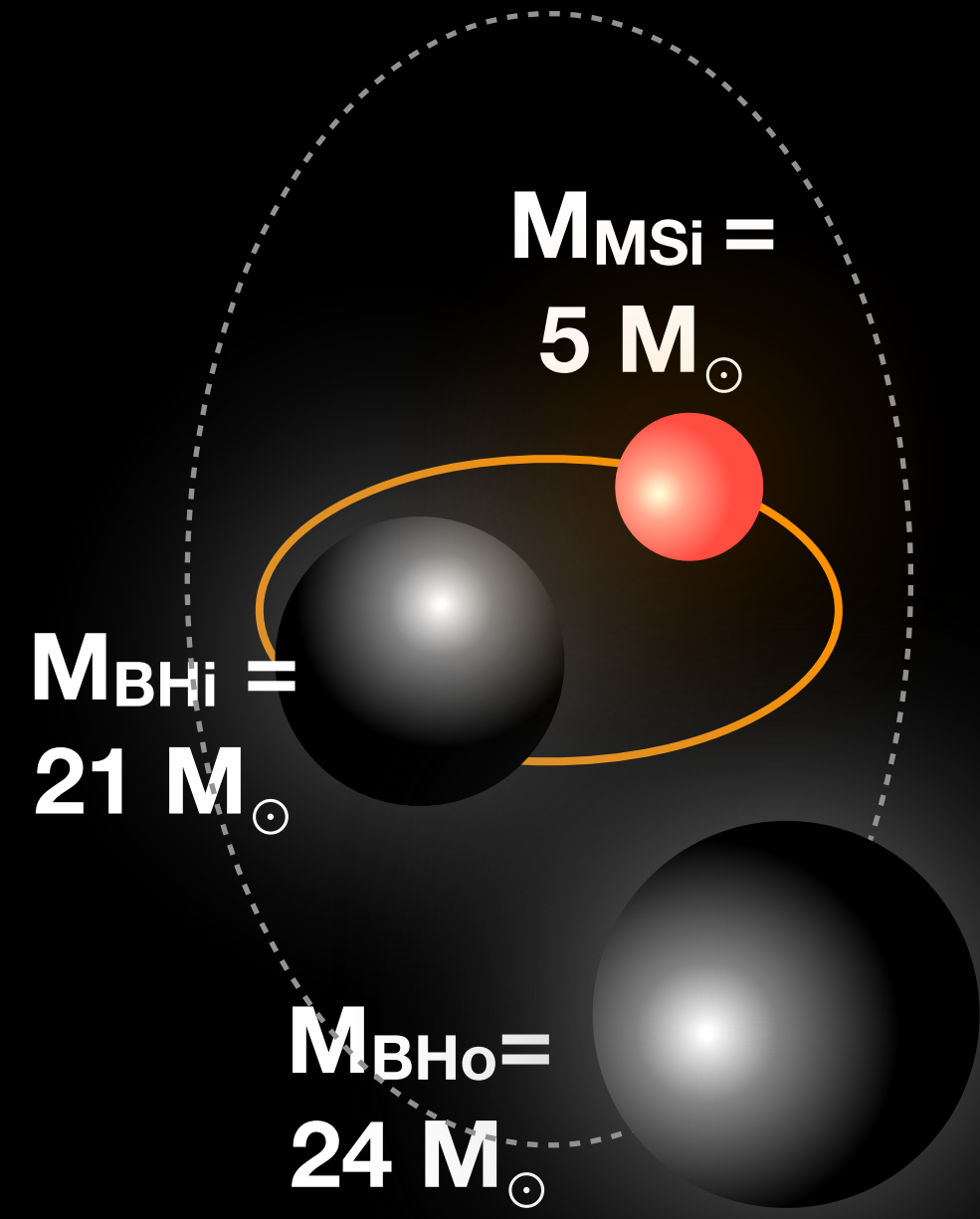
$$\beta = \frac{r_t}{r_p}$$





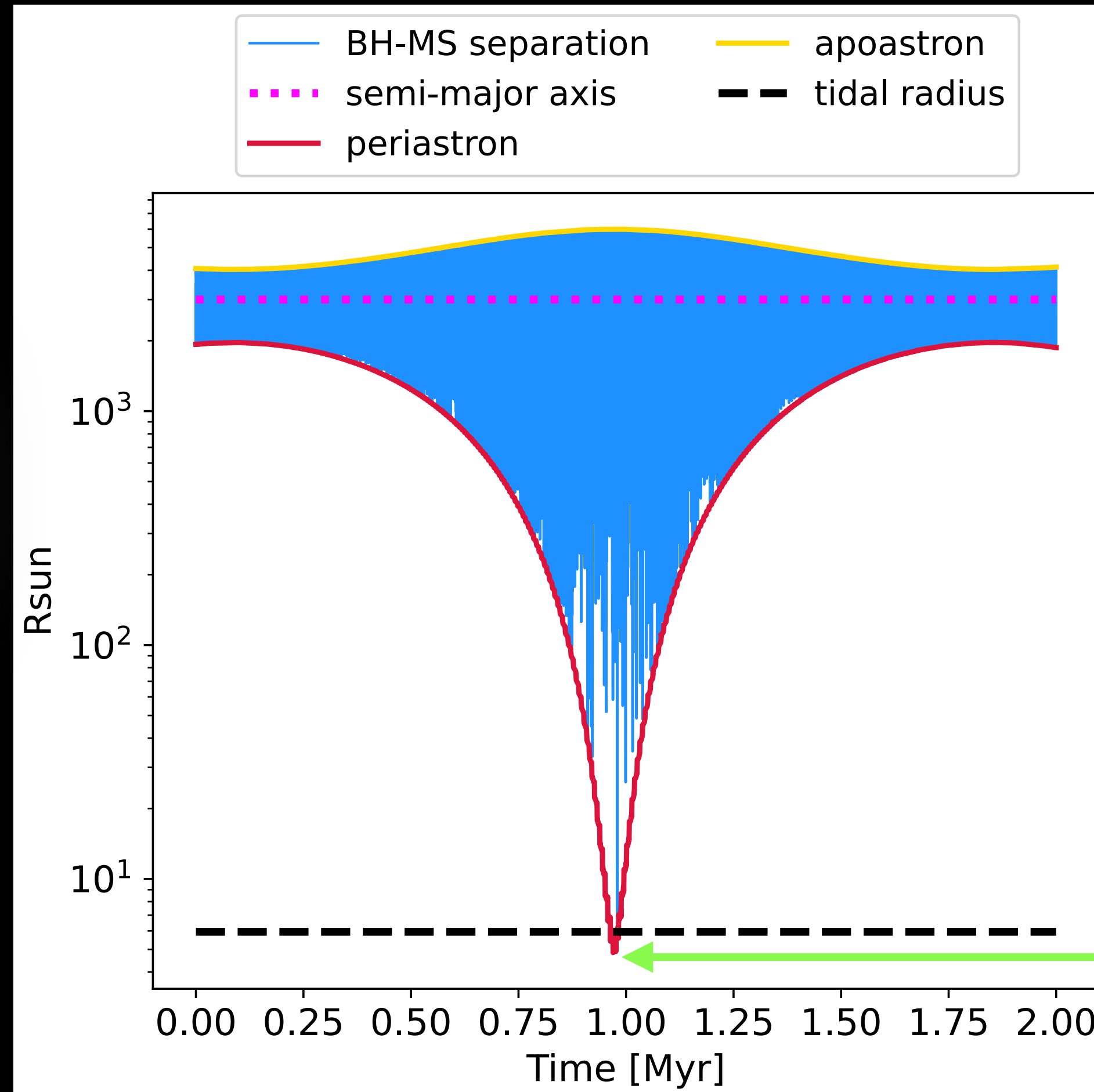
# Stellar disruptions : an example of a triple

TSUNAMI code (*Trani & Spera 2022*)

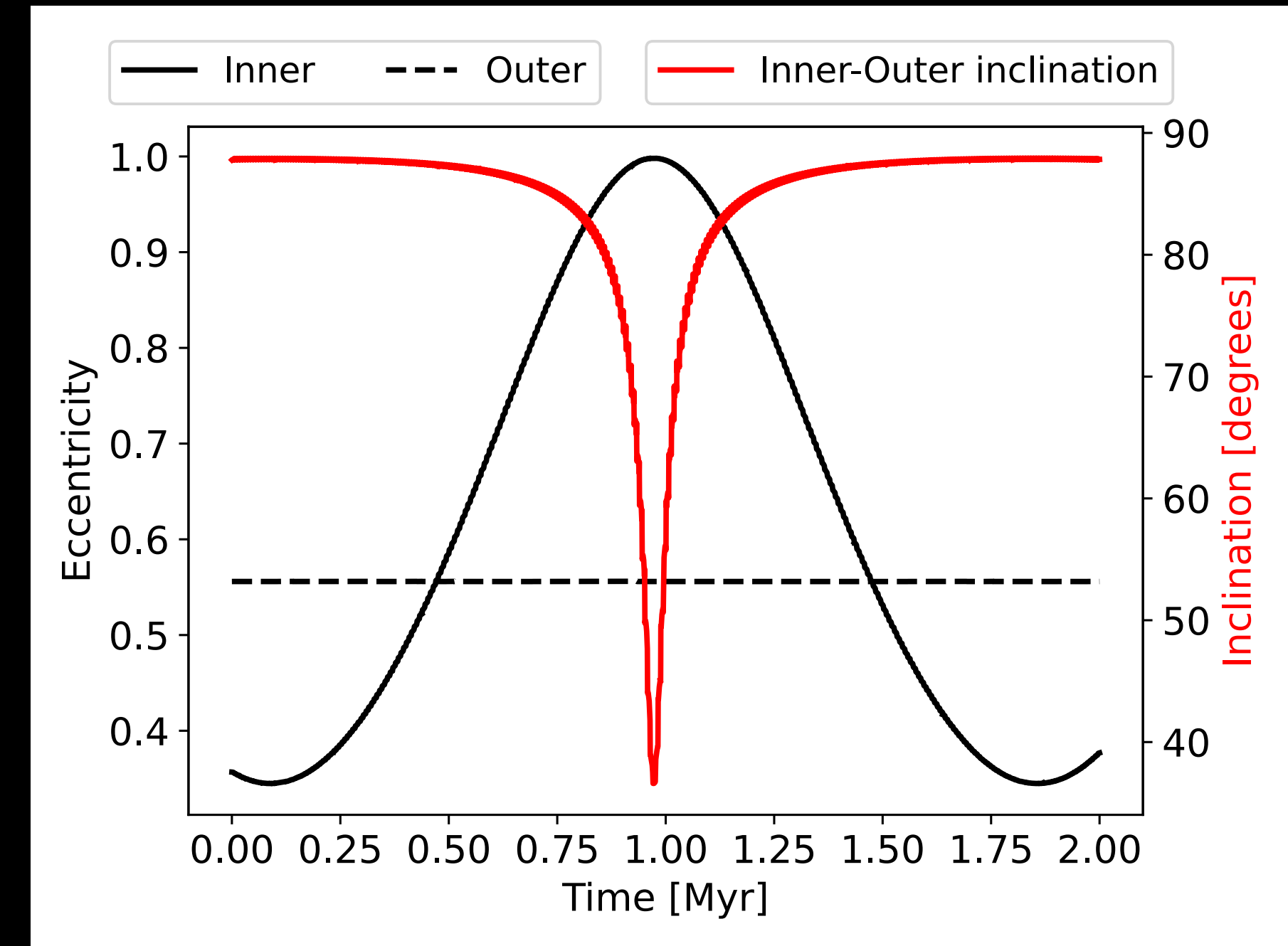


$ecc_i = 0.35$   
 $a_i = 3000 R_{\odot}$

*KZL effect*



Ecc<sub>i</sub> & *i* variation on a period of ~ 2 Myr



$$R_p \leq R_t = R_* \left( \frac{M_{BH}}{M_*} \right)^{1/3}$$

# Implications: Multi-Messenger Astronomy I

#BHs

EM: ~Fast Blue Optical Transients (FBOT)

LSST  
exp. 2025



ZTF  
ongoing



ULTRASAT  
exp. 2026

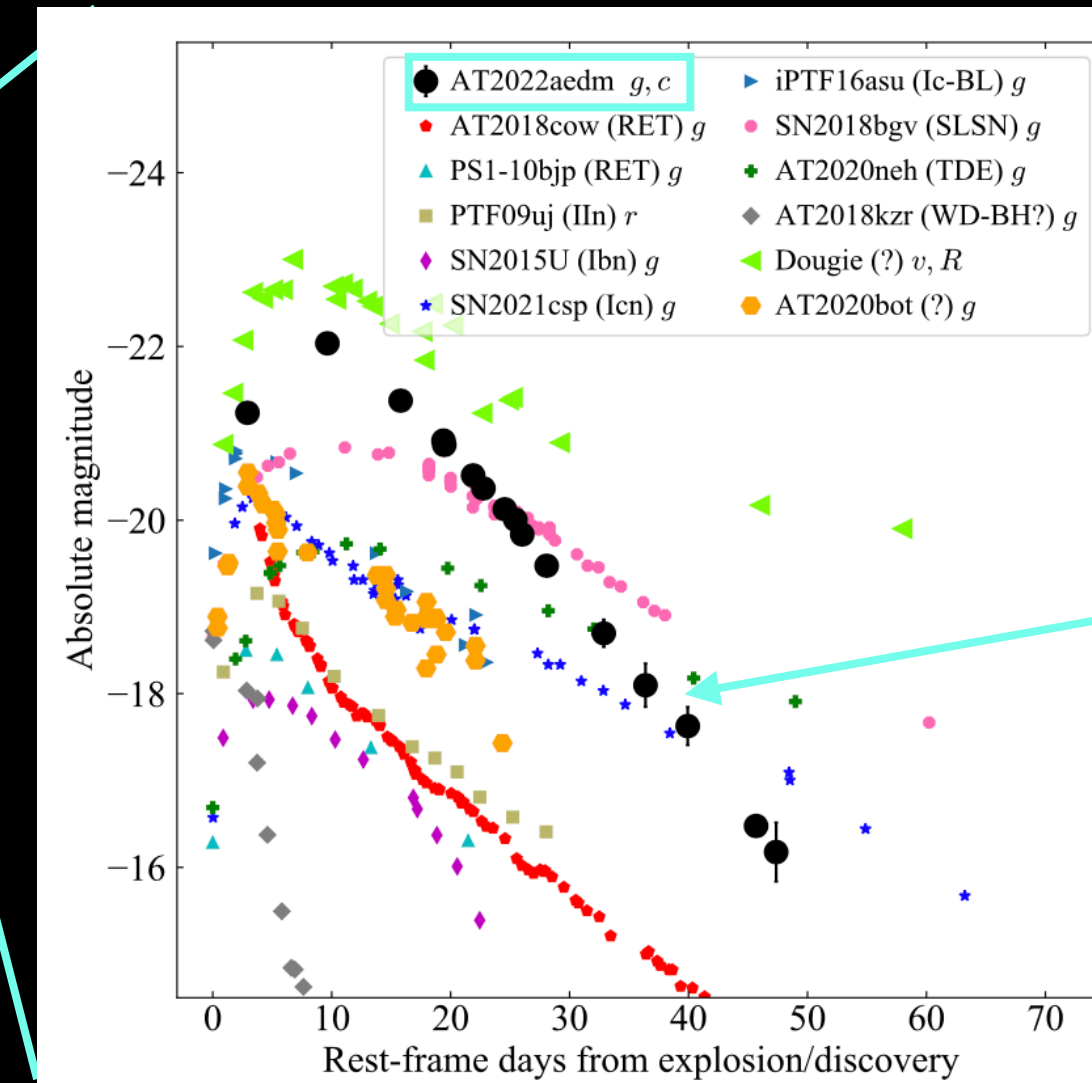


Optical transients  
UV transients

Detection rate estimate:

$10-10^5 \text{ yr}^{-1}$  (Rubin),  $1 - 50 \text{ yr}^{-1}$  (ZTF),  
and  $0.3-10^3 \text{ yr}^{-1}$  (ULTRASAT)

*Kremer et al., 2023*



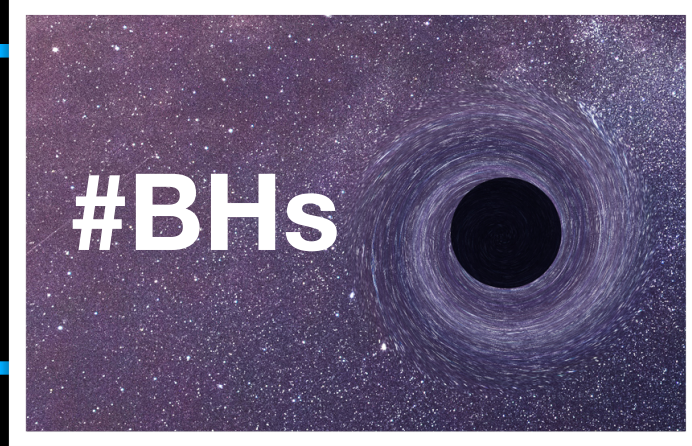
Maybe the first  
“candidate”  $\mu$ -TDE ?

*Nicholl et al., 2023*

*Not yet confirmed*

# Implications: Multi-Messenger Astronomy II

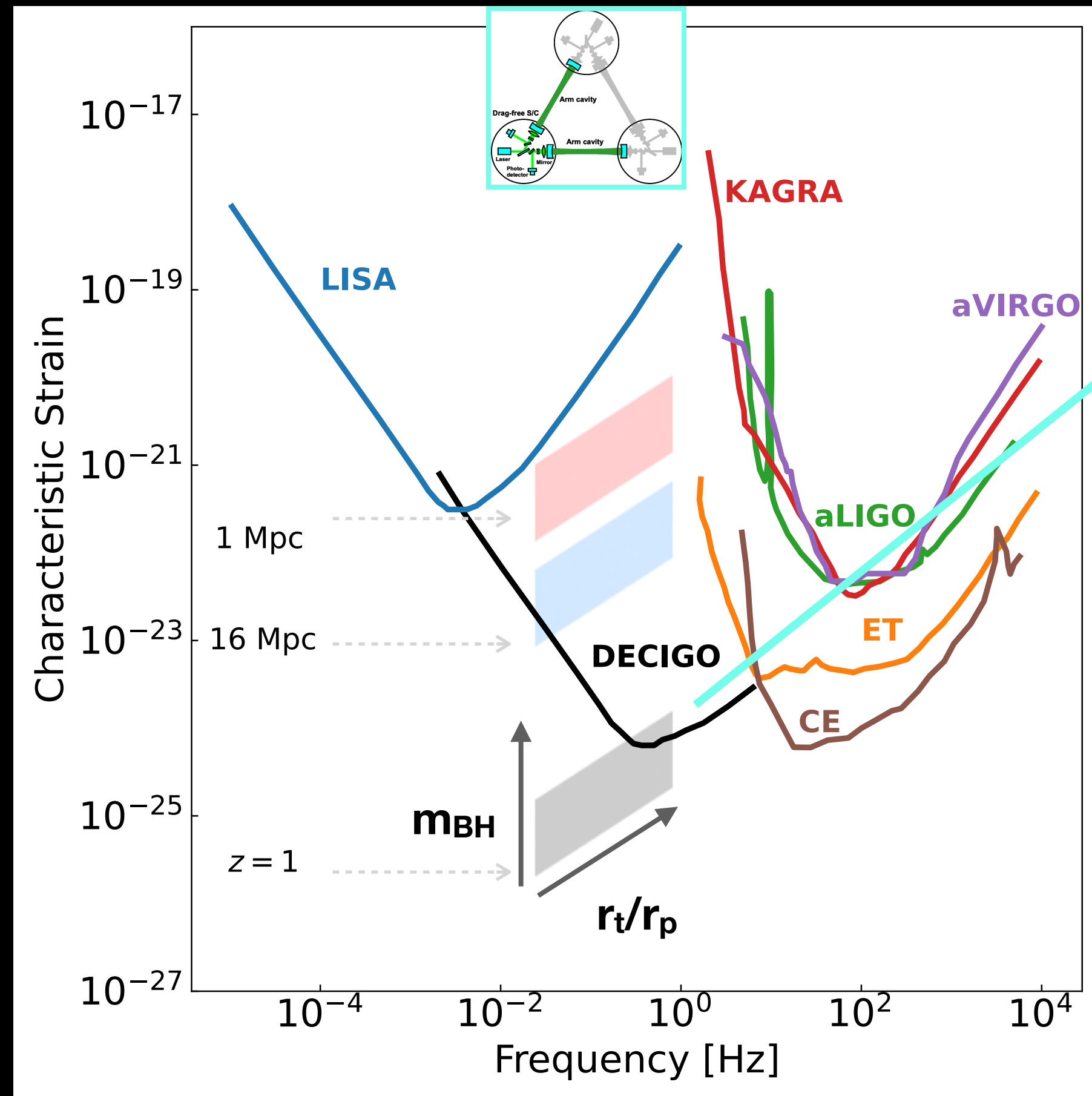
#BHs



GW: Burst emitted when the star is torn apart

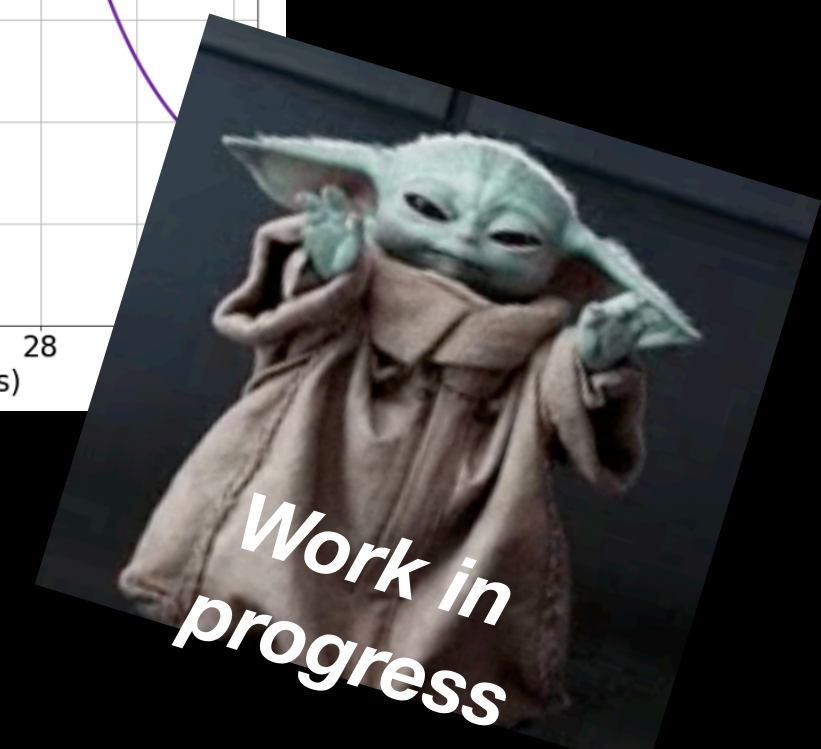
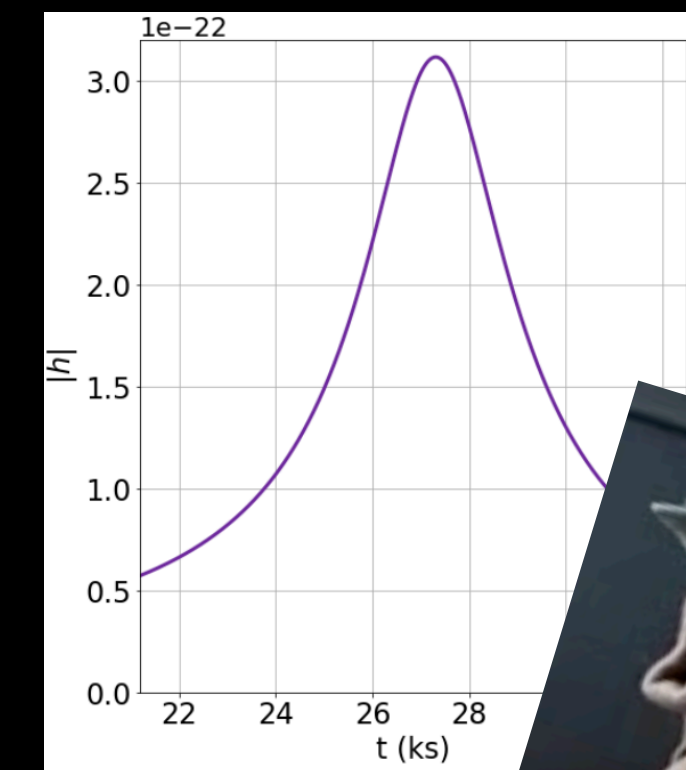
Sensitivity Curves:  
 Amaro-Seoane et al., 2017;  
 Sato et al., 2017;  
 Abbott et al., 2020a;  
 Maggiore et al., 2021;  
 Ng et al., 2021

$$m_{\text{BH}} = 5-100 M_{\odot}$$



1  $M_{\odot}$  Stars destroyed  
 by stellar mass BHs

Catalogue of GW waveforms  
 from micro-TDEs

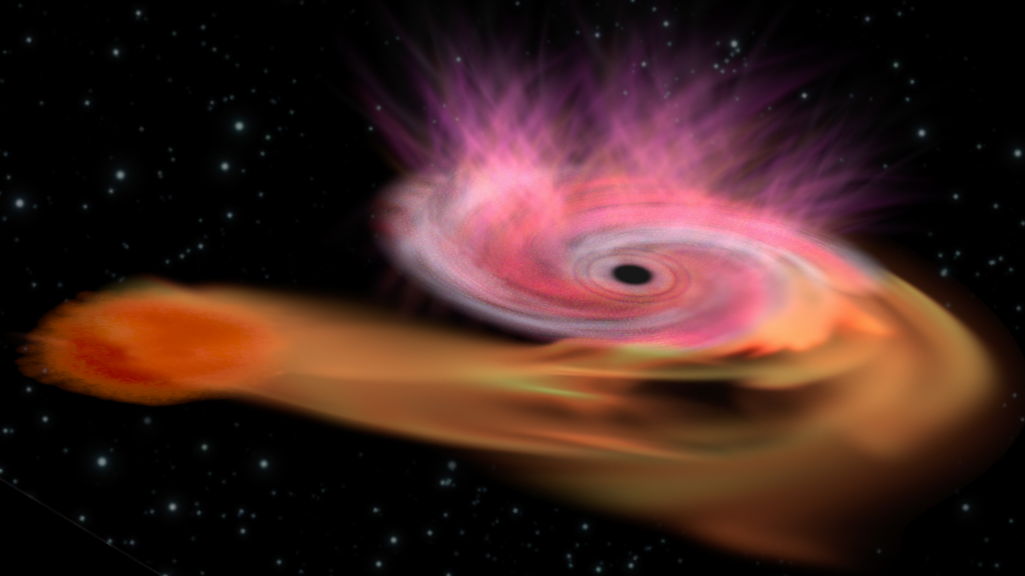


# Take home message

Macro-micro TDEs are promising multi-messenger sources expected to be detected soon (EM+GW)

micro-TDEs involve a large variety of configurations (BCOs+star, binary stars+COs etc)

Timely need for a catalogue of template of micro-TDEs waveforms in preparation for next GW data



SCHOOL

# Gravitational Waves in Astrophysics: From Theory to Observations

November 18-22, 2024

## Invited Courses

### Gravitational Waves Data Analysis

Tomás Andrade  
Universitat de Barcelona, Spain  
Macarena Lagos  
Universidad Andrés Bello, Chile

### Binary Stellar Evolution and Star Clusters

Giuliano Iorio  
Universitat de Barcelona, Spain  
Sara Rastello  
Universitat de Barcelona, Spain

### Gravitational Wave Ringdown

Lam Hui  
Columbia University, USA

## Organizing Committee

Hanne Van Den Bosch  
CMM – Universidad de Chile

Paola Rioseco  
CMM – Universidad de Chile

Tomás Andrade  
Universitat de Barcelona, Spain

Macarena Lagos  
Universidad Andrés Bello, Chile

M. Celeste Artale  
Universidad Andrés Bello, Chile

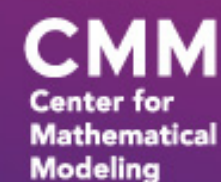
Center for Mathematical Modeling  
Universidad de Chile  
Beauchef 851  
Santiago – Chile

Know more / Apply:



<https://go.cmm.uchile.cl/waves2024>

Further information: [waves@cmm.uchile.cl](mailto:waves@cmm.uchile.cl)



FACULTAD DE CIENCIAS FÍSICAS Y MATEMÁTICAS  
UNIVERSIDAD DE CHILE



# GW SCHOOL

Center for Mathematical Modeling (CMM),  
Universidad de Chile, from Monday, November 18 to Friday,  
November 22, 2024.

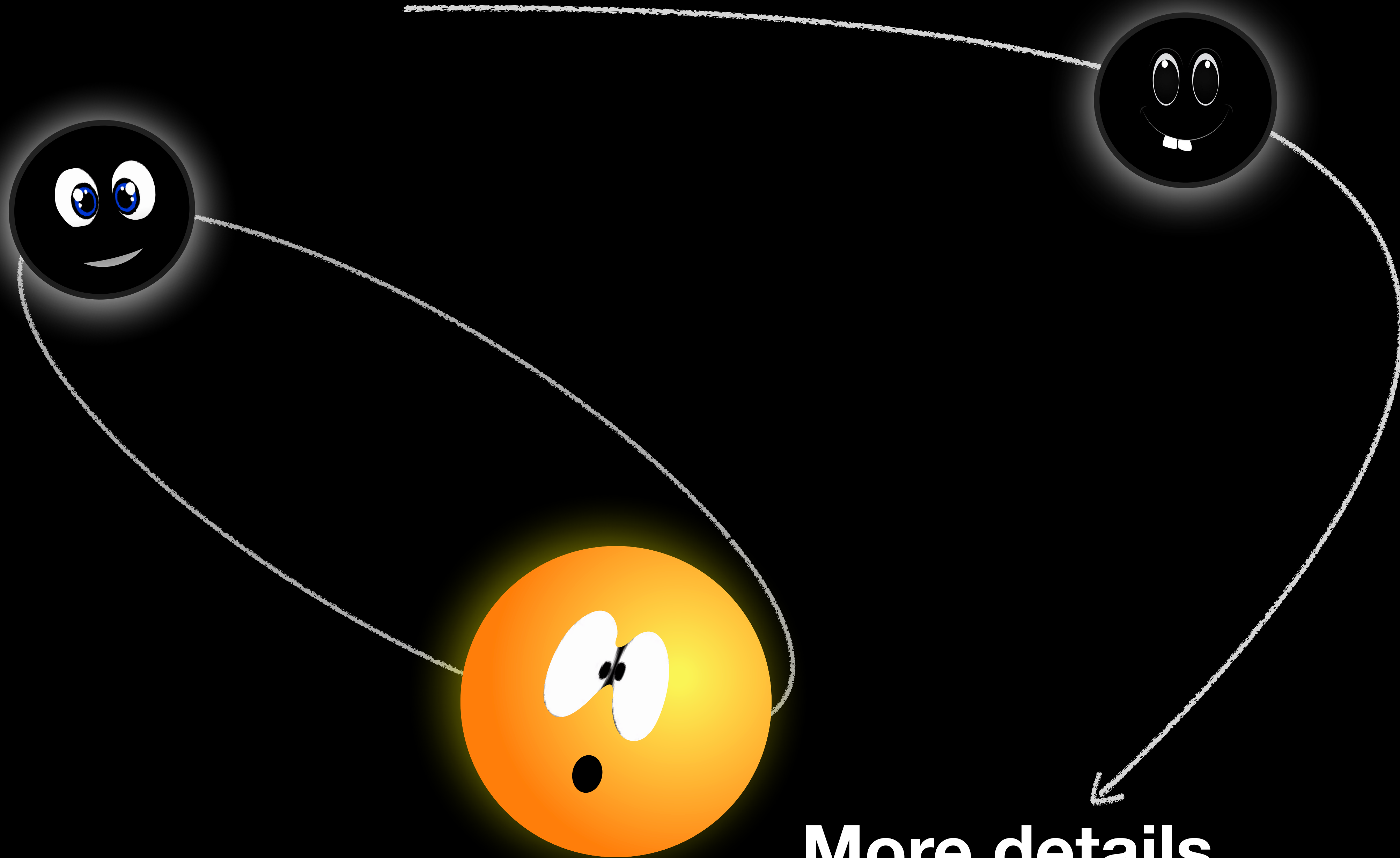
<https://eventos.cmm.uchile.cl/waves2024/>

## Apply / Register

**Apply now to participate in the School if you are a master's or doctoral student, or register to attend as a postdoc, researcher, or other professional.**

The registration deadline is **September 22nd**, with results announced during the **second week of October**.

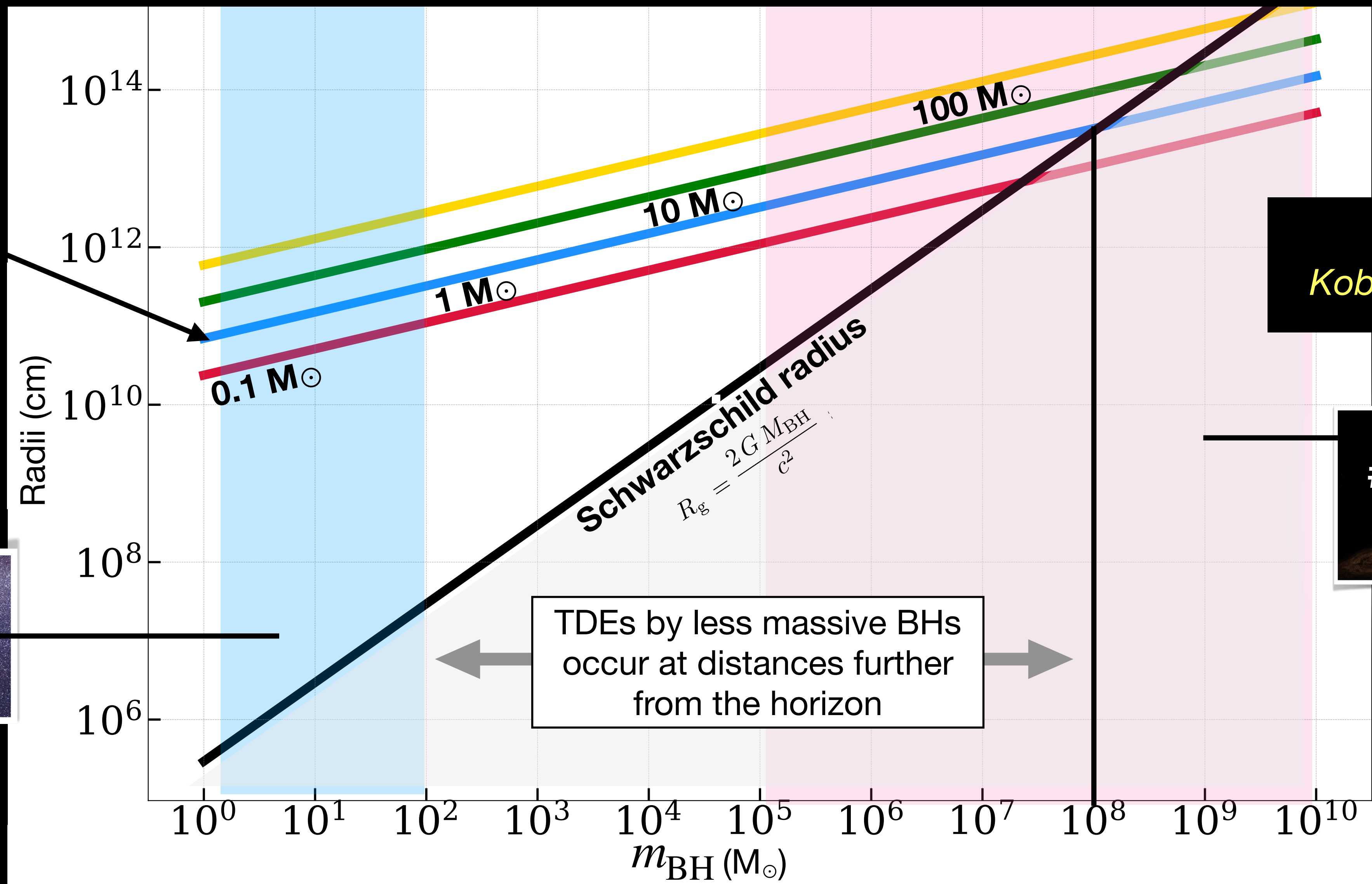




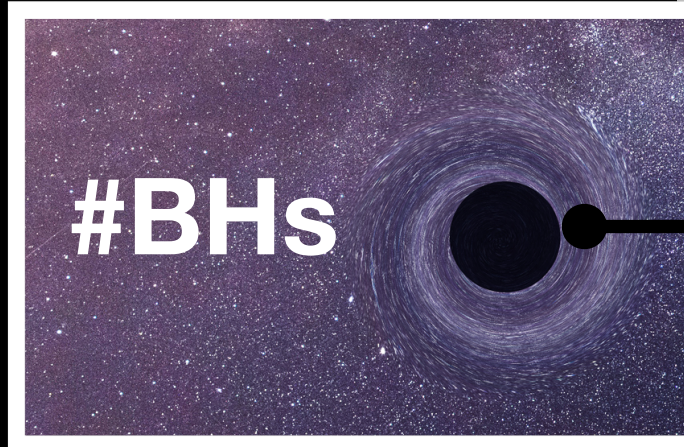
**More details...**



# Radius vs Mass: Macro vs micro-TDEs

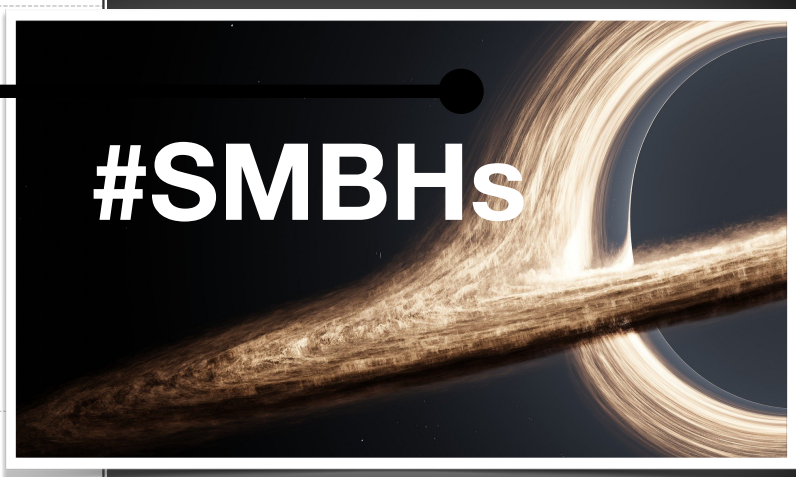


MS stars  
( $r \sim m^{0.8}$ )



#BHs

Adapted from  
Kobayashi et al., 2004

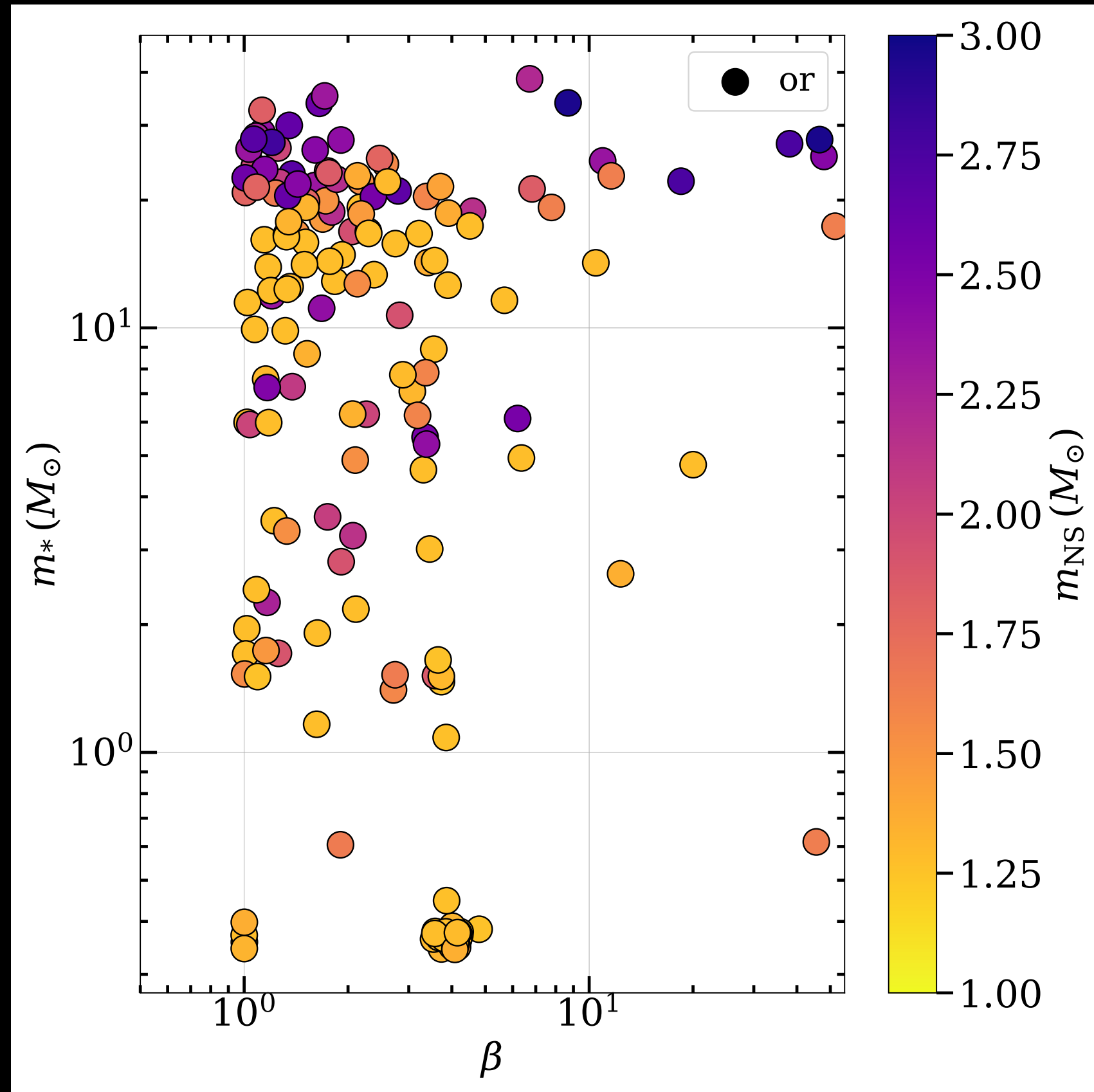


#SMBHs

TDEs by less massive BHs  
occur at distances further  
from the horizon

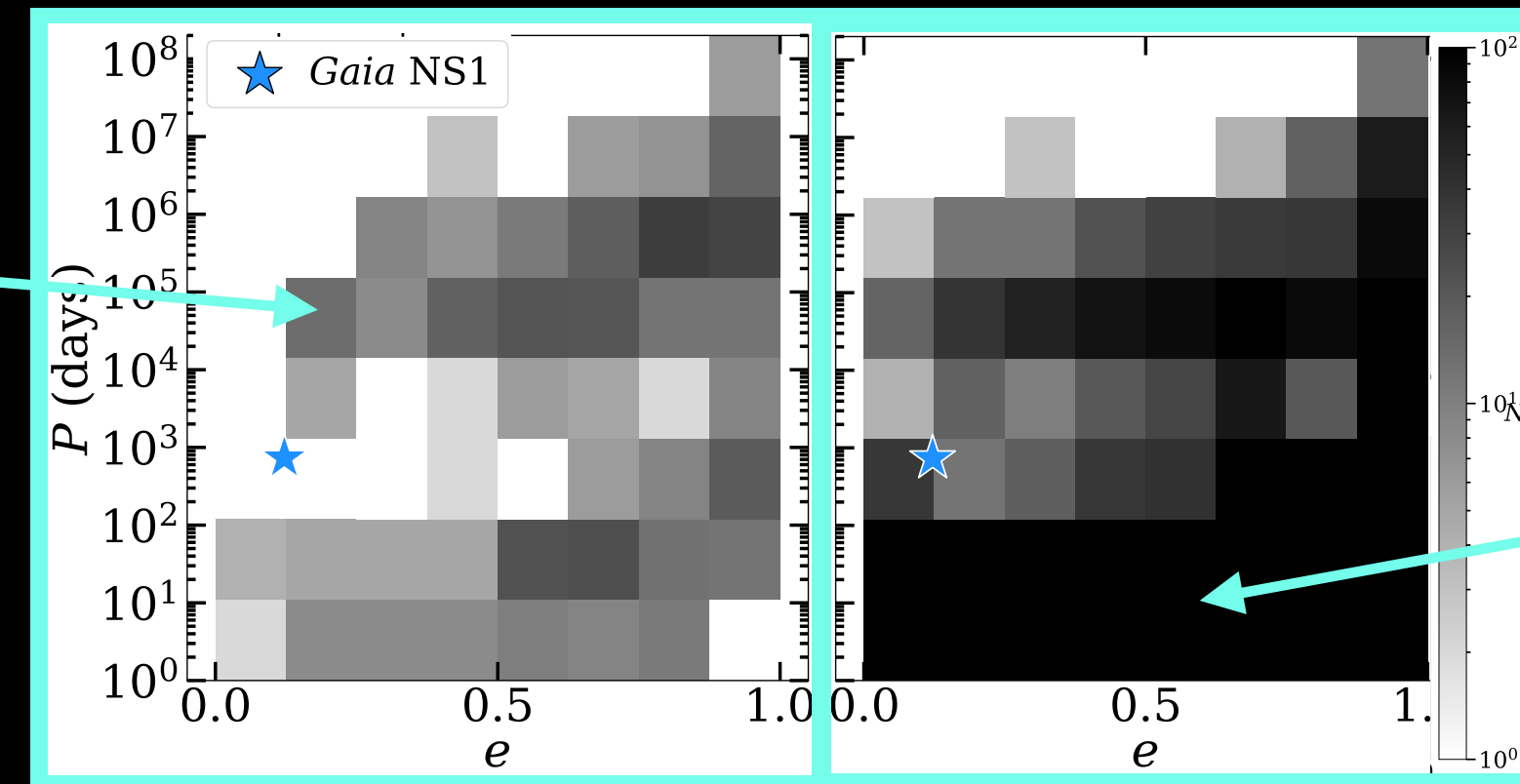
# What about Stars & NS ?

Stars disrupted by NS kicks in YSCs



Dynamical binaries

**Gaia NS1**  
*El-Badry et al., 2024*



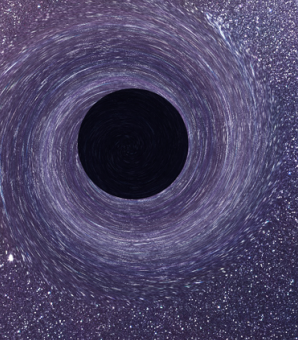
Isolated binaries  
(Petar.BSE)



*Tanikawa et al., 2024*

# $\mu$ -TDEs rate & detectability

#BHs

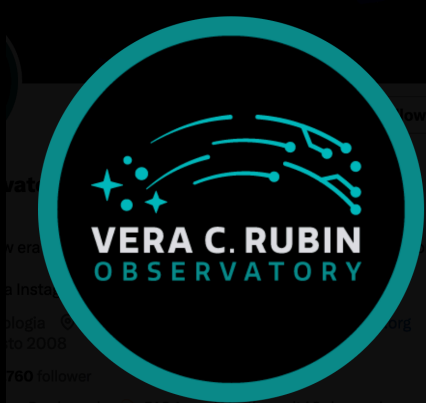


Rate in the local Universe:

- 10 Gpc<sup>-3</sup> yr<sup>-1</sup> in GCs (*Perets et al. 2016; Kremer et al. 2019d*);
- 20-200 Gpc<sup>-3</sup> yr<sup>-1</sup> in YSCs & OCs (*Rastello et al., 2019; Kremer et al., 2021*)
- 1-10 Gpc<sup>-3</sup> yr<sup>-1</sup> in NSCs (*Fragione et al. 2020*)

*Kremer et al., 2023*

LSST  
exp. 2025  
*synoptic  
astronomical survey*



ZTF ongoing  
**ZWICKY**  
TRANSIENT  
FACILITY  
*Optical transients*

ULTRASAT  
exp. 2026



*UV transients*

Environment	Intrinsic rate (Gpc <sup>-3</sup> yr <sup>-1</sup> )	<i>s</i>	Rubin (g-band) (yr <sup>-1</sup> )	ZTF (g-band) (yr <sup>-1</sup> )	ULTRASAT (NUV) (yr <sup>-1</sup> )
(1)	(2)	(3)	(4)	(5)	(6)
Globular clusters	~10 (Perets et al. 2016; Kremer et al. 2019b)	0.2	6.8 × 10 <sup>3</sup>	4.3	133
		0.5	50	0.1	1.2
		0.8	0.9	0.004	0.03
Young massive clusters	~100 (Kremer et al. 2021)	0.2	6.8 × 10 <sup>4</sup>	53.9	1.3 × 10 <sup>3</sup>
		0.5	490	1.1	12
		0.8	9.1	0.9	0.3

Detection rate estimate: 10–10<sup>5</sup> yr<sup>-1</sup> (Rubin), 1 – 50 yr<sup>-1</sup> (ZTF), and 0.3–10<sup>3</sup> yr<sup>-1</sup> (ULTRASAT)

# 1) GW burst from BH-Star

Estimate of the GW strain emitted by the source derived from quadrupole approximation to the Einstein field equations [Toscani et al., 2021, 2022](#)

$$h \approx \frac{1}{d} \frac{4G}{c^2} \frac{E_{\text{kin}}}{c^2} \quad d = \text{distance from Earth}$$

$$E_{\text{kin}} = M_* \frac{GM_h}{r_p} \quad \text{kinetic energy}$$

$r_s$  BH Schwarzschild radius  
 $r_t$  tidal radius  
 $r_p$  pericenter distance

$M_h$  mass of the BH  
 $M_*$  mass of the star  
 $R_*$  radius of the star

The **GW strain** is thus:

$$\begin{aligned} h &\approx \beta \times \frac{r_s r_{s*}}{r_t d} \\ &\approx \beta \times 2 \times 10^{-22} \left( \frac{M_*}{M_\odot} \right)^{4/3} \left( \frac{M_h}{10^6 M_\odot} \right)^{2/3} \\ &\quad \times \left( \frac{R_*}{R_\odot} \right)^{-1} \left( \frac{d}{16 \text{ Mpc}} \right)^{-1}, \end{aligned}$$

The associated **frequency** is thus:

$$\begin{aligned} f &\approx \frac{\beta^{3/2}}{2\pi} \left( \frac{GM_h}{r_t^3} \right)^{1/2} \\ &\approx \beta^{3/2} \times 10^{-4} \text{ Hz} \times \left( \frac{M_*}{M_\odot} \right)^{1/2} \left( \frac{R_*}{R_\odot} \right)^{-3/2} \end{aligned}$$

The dependence on  $M_*$ ,  $R_*$  and  $M_h$  indicates that more compact stars (such as WDs) will produce stronger GW signals.

For  $\beta = 1$  and a Sun-like star disrupted by a  $10^6 M_\odot$  static BH at  $\approx 16$  Mpc from us,  $h \approx 10^{-22}$  and  $f \approx 10^{-4}$  Hz