



SAPIENZA
UNIVERSITÀ DI ROMA



Primordial Black Holes or else?

Tidal tests on subsolar gravitational-wave observations

Speaker:

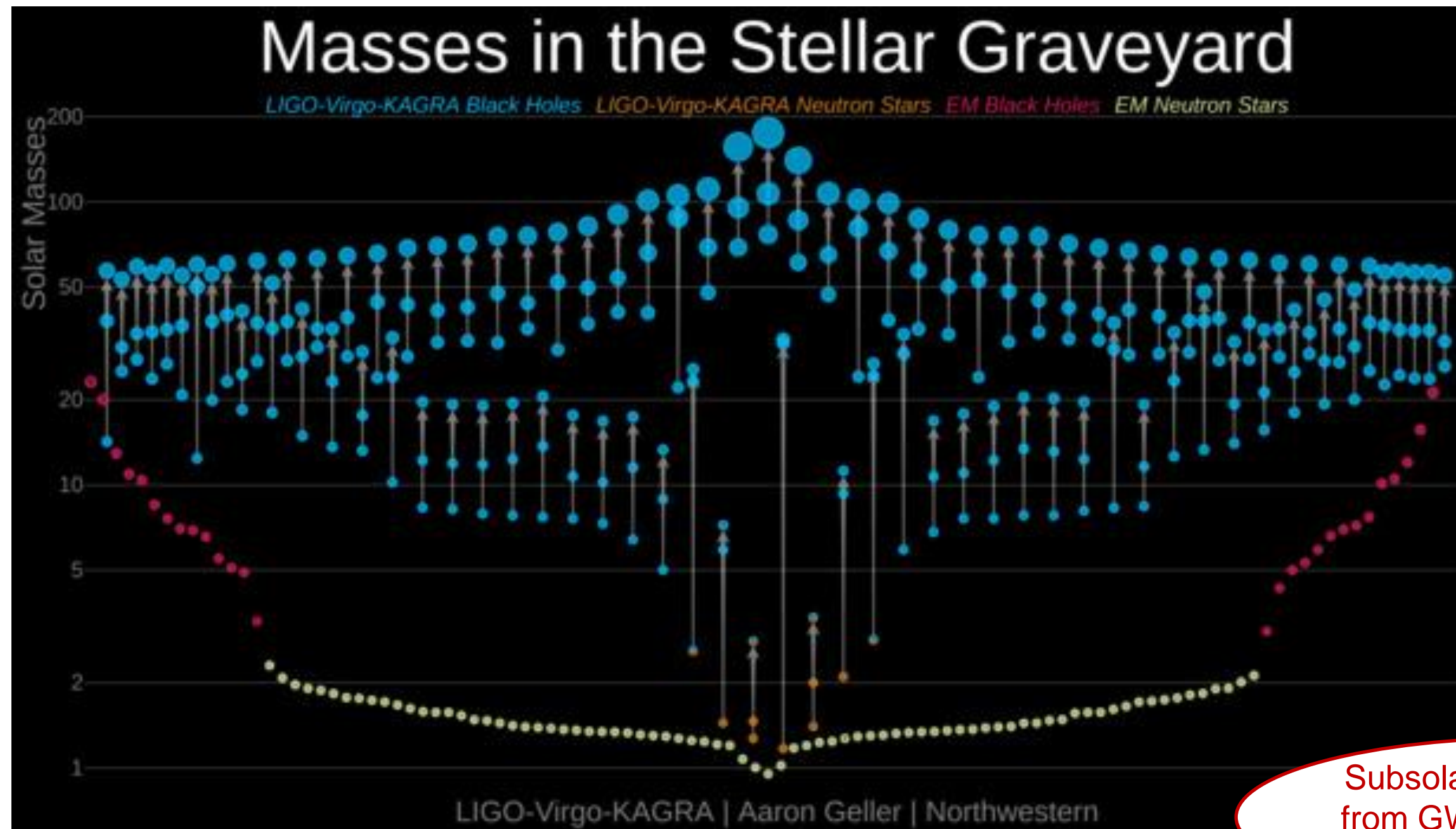
Francesco Crescimbeni

Based on:

F. Crescimbeni, G. Franciolini, P. Pani, and A. Riotto, *Phys.Rev.D* 109 (2024) 12, 124063.

Introduction

- During the first 3 observing runs, LVK collaboration detected nearly 90 events → nearly 100 hundred for the fourth observing runs, and many more are expected in the future with 3G detectors.

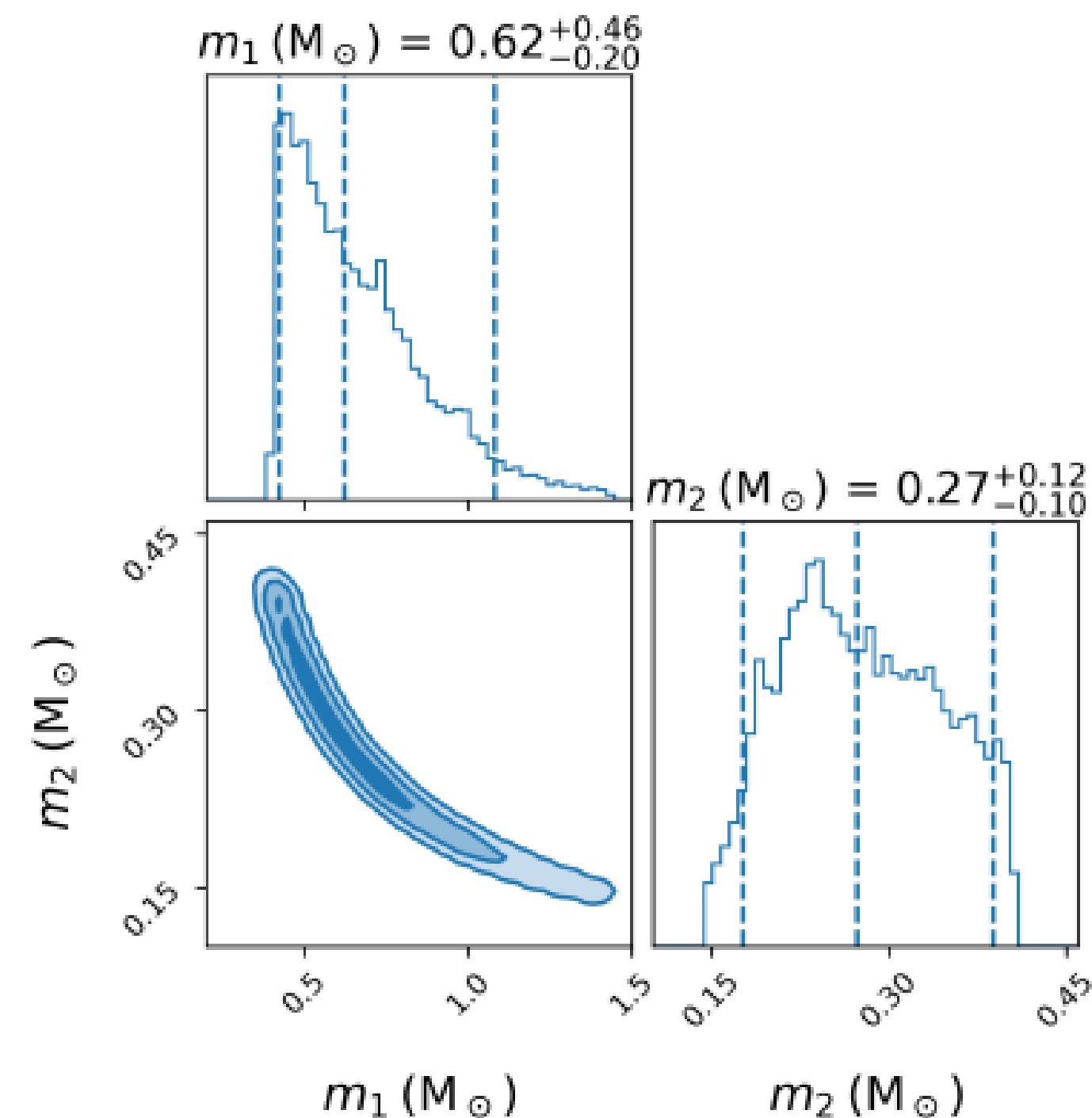


Source ref. www.ligo.caltech.edu/MIT/image/ligo20211107a

Subsolar compact objects
from GW observations still
missing!

Putative detections of subsolar binaries

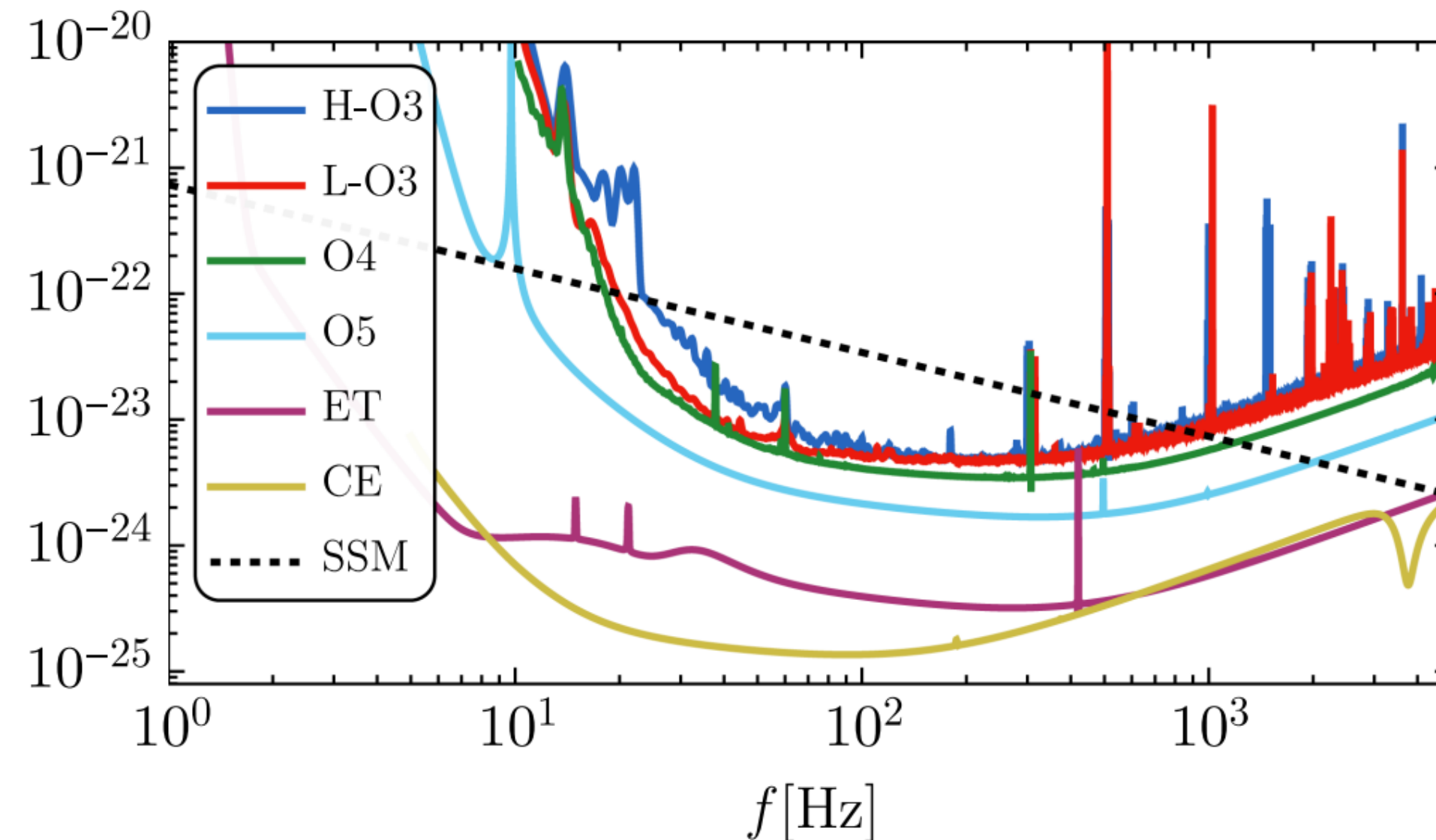
- The observation of at least a subsolar mass (SSM) object in a binary black hole merger could be a signature of primordial black holes (PBHs) detection.
- Subsolar mergers searches have been performed throughout the years, finding no conclusive evidences [LVK, '18; LVK '19; LVK '22; Nitz-Wang, 2102.00868].
- SSM-like trigger (denoted as SSM200308) detected during O3 was recently reanalyzed [Prunier+, 2311.16085] under the assumption that it was a binary of primordial black holes (PBHs).



Source ref. Prunier+, 2311.16085

Objectives of this work

- A signal compatible with a subsolar merger could be observed already during the ongoing O4 run of the LIGO/Virgo/Kagra (LVK) Collaboration.
- We investigate whether current and future experiments would have sufficient sensitivity required to detect SSM200308-like events.
- Distinguish PBHs from other astrophysical systems or more exotic competitors in the SSM range.



SSM candidates

- **Astrophysics objects:** Light neutron stars, white dwarfs;



- **Exotic compact objects:** Q-balls, boson stars, fermionic stars;

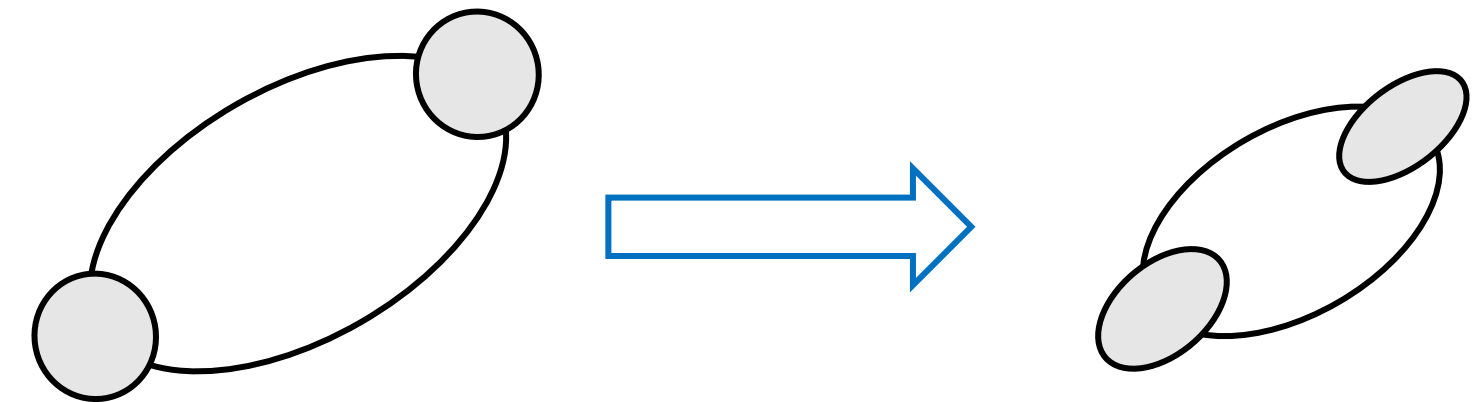


- **Primordial black holes.**



$$\Lambda = \frac{2}{3} k_2 \left(\frac{Gm}{R} \right)^{-5}$$

Non-zero tidal deformabilities



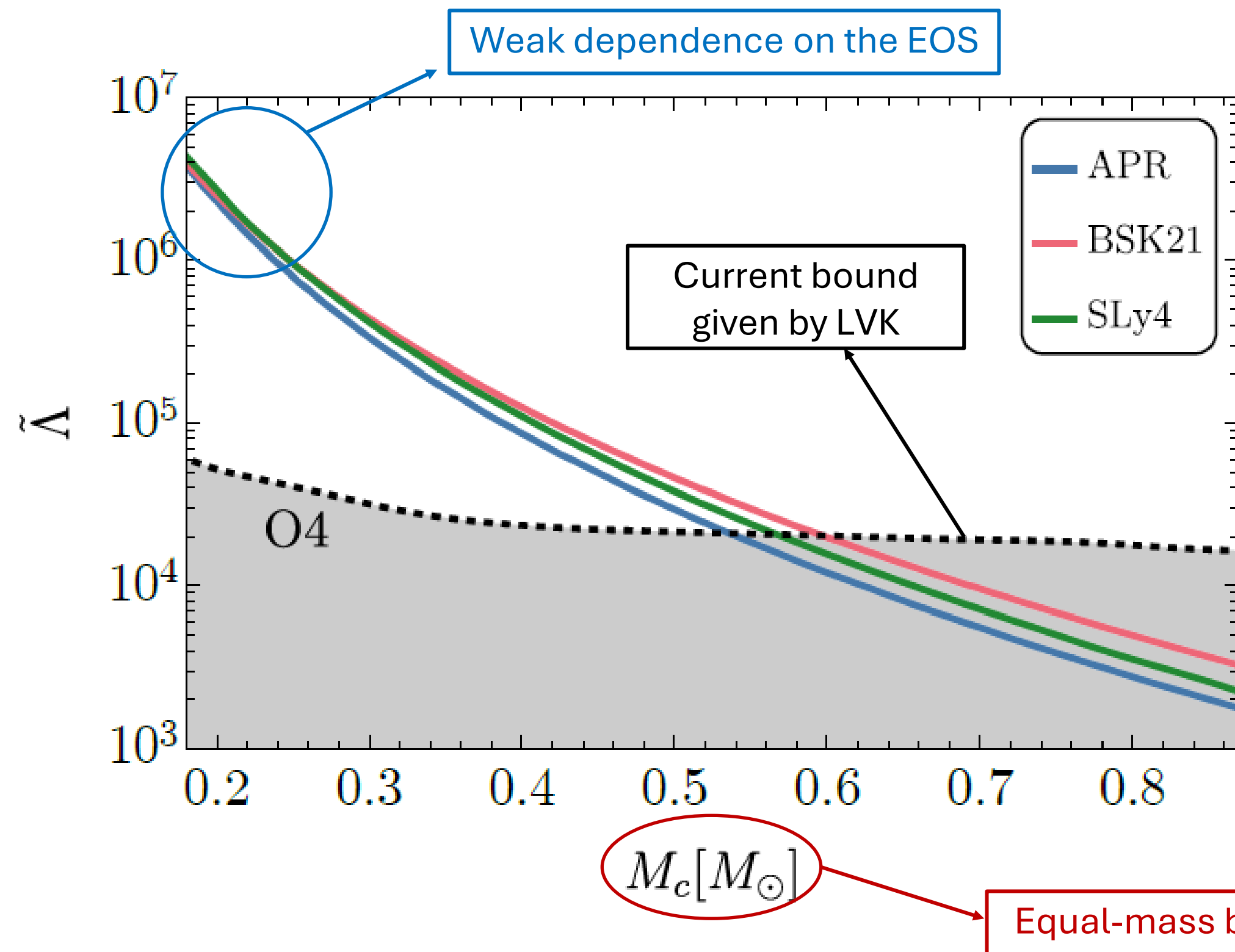
$$\Lambda = 0$$

Non-deformable (symmetry properties)

New physics

Tidal deformabilities for neutron stars

- Subsolar objects are less sensitive for EOS effects!



SLy4

$$\Lambda = 7.3 \cdot 10^4 \left(\frac{m}{0.5 M_\odot} \right)^{-4.7}$$

Tidal deformabilities for boson stars

- Assume for instance **boson stars** (BSs) with **quartic potential** [Pacilio+, 2007.05264]:

$$V(|\phi|) = \frac{\mu^2}{2} |\phi|^2 + \frac{\lambda}{4} |\phi|^4$$

$$\frac{m}{m_B} = \frac{\sqrt{2}}{8\sqrt{\pi}} \left[-0.828 + \frac{20.99}{\log \Lambda} - \frac{99.1}{(\log \Lambda)^2} + \frac{149.7}{(\log \Lambda)^3} \right] \longleftrightarrow \begin{array}{l} \lambda \gg \mu^2 \\ m_B = \sqrt{\lambda}/\mu^2 \end{array}$$

- Invert relation to find:

$$\Lambda = \Lambda(m/m_B)$$

- In this model, BSs exist for $m/m_B < 0.06$, which gives $\Lambda > 289$.
- Λ can **span many orders of magnitude** as the mass deviates from its maximum value (e.g., $\Lambda \approx 1.7 \times 10^6$ for $m/m_B = 0.02$).
- An **upper bound on Λ** can rule out some models!

Waveform modeling of SSM binaries

- We adopt a TaylorF2 waveform [Damour+, 0010009] which includes also possible tidal disruption effects modeling:

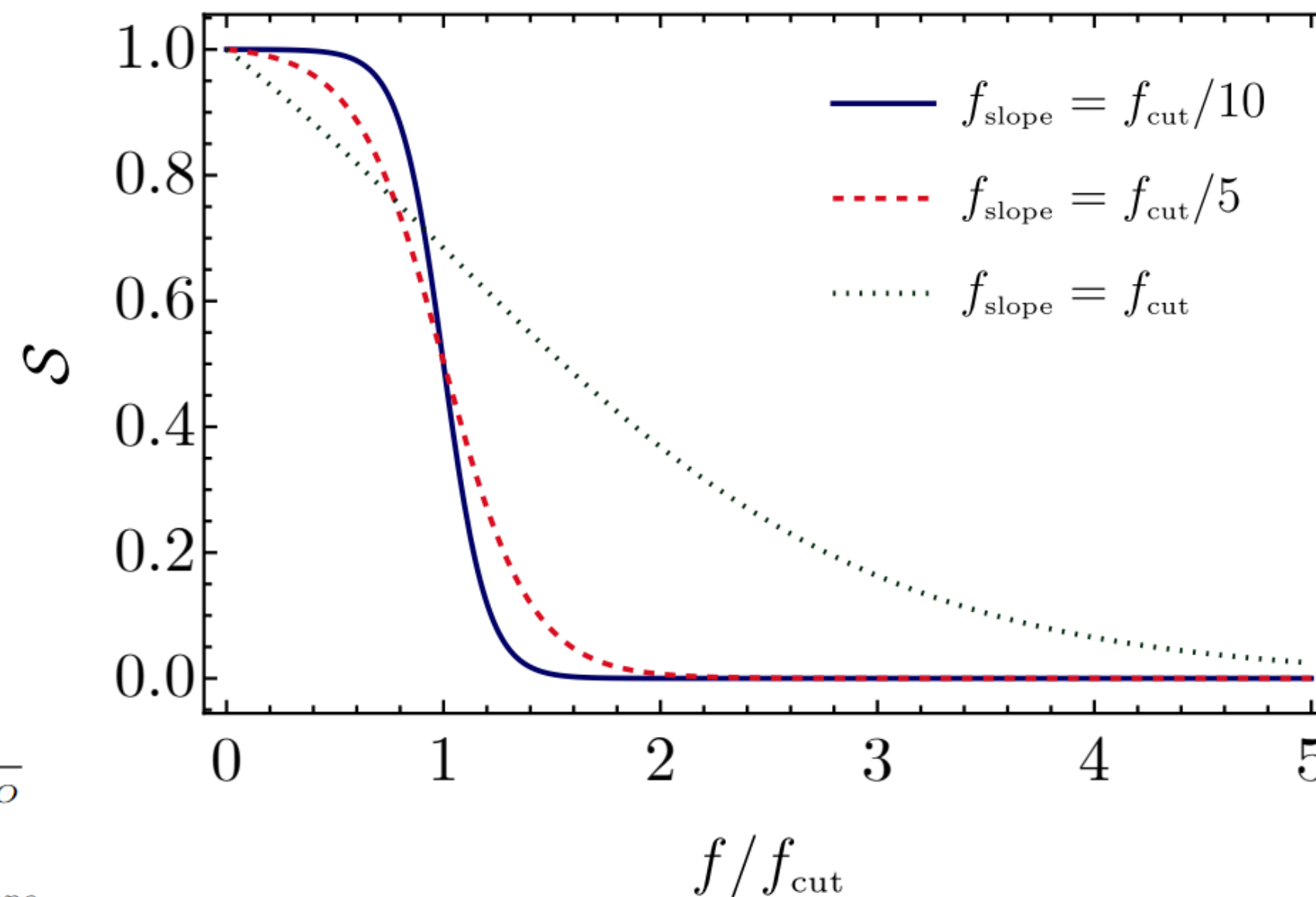
Amplitude: scales as the inverse of distance

Phase: contains tidal deformability

$$\tilde{h}(f) = \mathcal{A} f^{-\frac{7}{6}} \mathcal{S}(f) e^{i\psi(f)}$$

Tapering smoothing: keeps into account possible tidal disruption

$$\mathcal{S}(f) = \left[\frac{1 + e^{-\tilde{\lambda}_f / \delta \tilde{\lambda}_f}}{1 + e^{(f/f_{ISCO} - \tilde{\lambda}_f) / \delta \tilde{\lambda}_f}} \right] \longleftrightarrow \begin{cases} \tilde{\lambda}_f = \frac{f_{cut}}{f_{ISCO}} \\ \delta \tilde{\lambda}_f = \frac{f_{slope}}{f_{ISCO}} \end{cases}$$



Source ref. De Luca+, 2212.03343

Waveform modeling of SSM objects

- GW phase (augmented at 5PN and 6PN) [Kidder-Will, 9211025; Wade+, 1402.5156]:

$$\psi(x) = \underbrace{\psi_{\text{pp}}(x)}_{\text{Point-particle phase}} + \underbrace{\delta\psi_{\text{tidal}}(x)}_{\text{Tidal phase}} \longleftrightarrow \delta\psi_{\text{tidal}} = \frac{3}{128\eta x^{5/2}} \left[\left(-\frac{39}{2} \tilde{\Lambda} \right) x^5 + \left(-\frac{3115}{64} \tilde{\Lambda} + \frac{6595}{364} \sqrt{1-4\eta} \delta\tilde{\Lambda} \right) x^6 \right]$$

- Some definitions...

$$\tilde{\Lambda} = \frac{8}{13} \left[(1 + 7\eta - 31\eta^2) (\Lambda_1 + \Lambda_2) + \sqrt{1-4\eta} (1 + 9\eta - 11\eta^2) (\Lambda_1 - \Lambda_2) \right]$$

$$\delta\tilde{\Lambda} = \frac{1}{2} \left[\sqrt{1-4\eta} \left(1 - \frac{13272}{1319}\eta + \frac{8944}{1319}\eta^2 \right) (\Lambda_1 + \Lambda_2) + \left(1 - \frac{15910}{1319}\eta + \frac{32850}{1319}\eta^2 + \frac{3380}{1319}\eta^3 \right) (\Lambda_1 - \Lambda_2) \right]$$

Injection simulations of SSM200308-like systems

PBH binary injections + recovery (Bayesian inference + Fisher analysis):

- Inject SSM200308 parameters + zero tides and neglect tapering $\rightarrow \tilde{\Lambda} = \delta\tilde{\Lambda} = 0$ and $\tilde{\lambda}_f = 1$

NS binary injections + recovery (Fisher):

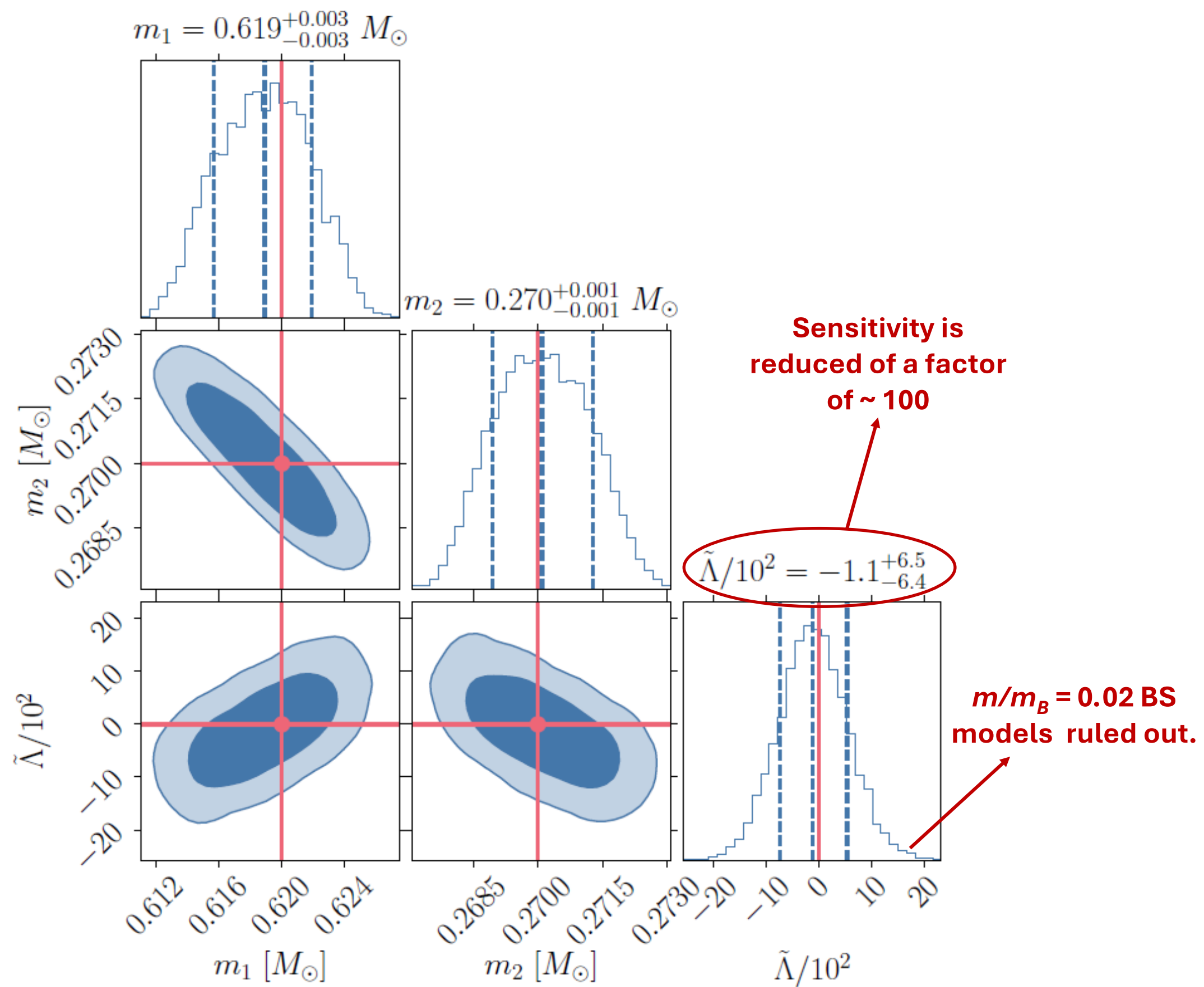
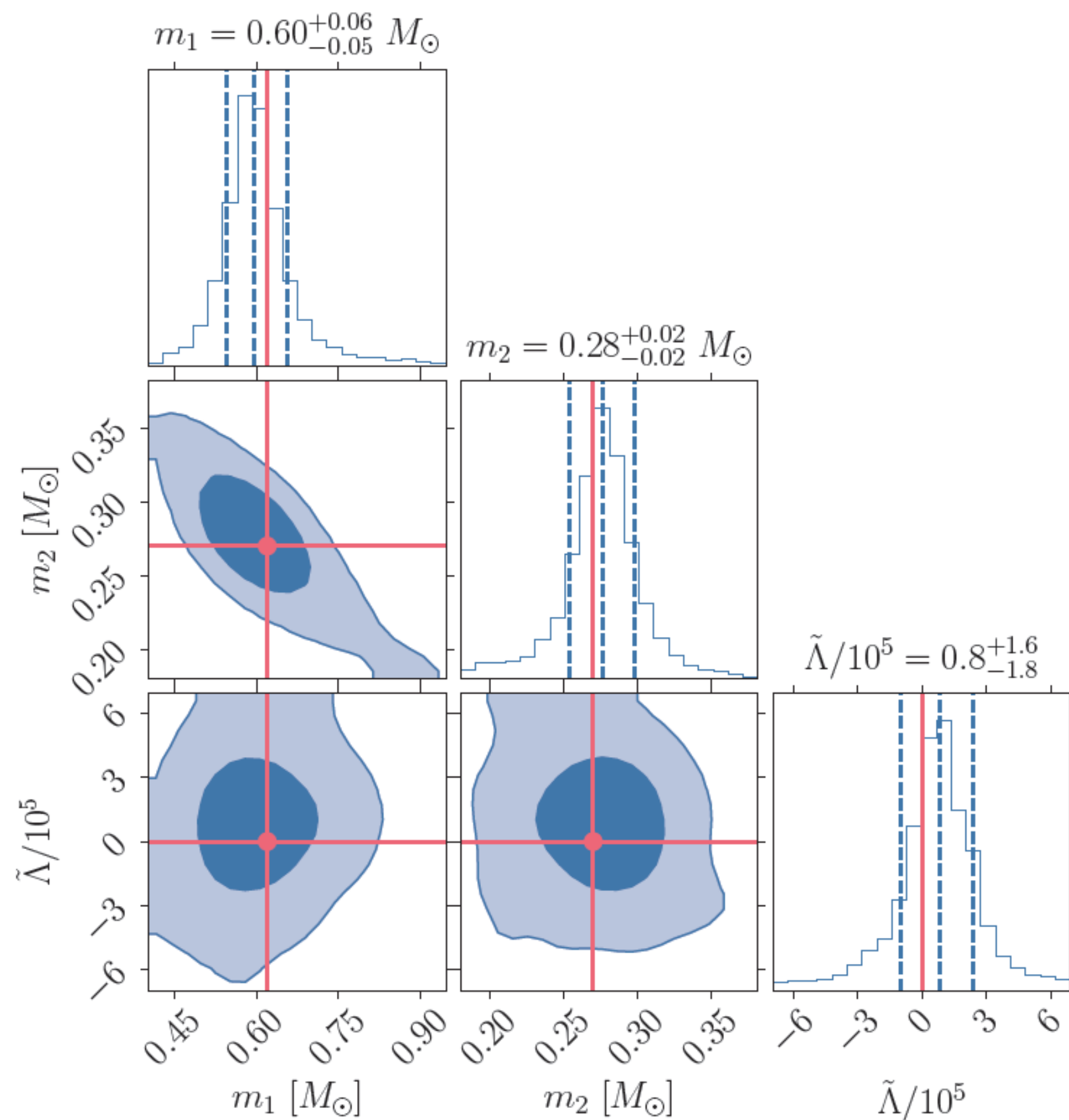
- Inject non-zero tides assuming **SLy4 EOS** $\rightarrow \tilde{\Lambda} = 1.5 \cdot 10^5 \quad \delta\tilde{\Lambda} = 4.9 \cdot 10^4 \quad \tilde{\lambda}_f = 0.075$

General requirements:

- **SSM constraint** [Franciolini+, 2112.10660] $\leftrightarrow m_i + 3\Delta m_i < M_\odot$

- **Exclude PBH nature** $\leftrightarrow \begin{aligned} \tilde{\Lambda} - 3\Delta\tilde{\Lambda} &> 0, \quad \text{and/or} \\ \tilde{\lambda}_f + 3\Delta\tilde{\lambda}_f &< 1 \end{aligned}$

Bayesian inference result of PBH binary injections: O3 vs ET+2CE



Fisher results of NS binary injections

Network	LVK O3	LVK O4	LVK O5	ET+2CE
BNS SSM200308 ($\tilde{\Lambda} = 1.5 \cdot 10^5, \delta\tilde{\Lambda} = 4.9 \cdot 10^4, \tilde{\lambda}_f = 0.075$)				
SNR	7.90	12.8	22.4	398
$\Delta m_1/m_1$	0.47	0.22	0.082	0.0017
$\Delta m_2/m_2$	0.39	0.19	0.070	0.0015
$\Delta\tilde{\Lambda}/\tilde{\Lambda}$	0.86	0.66	0.55	0.047
$\Delta\tilde{\lambda}_f/\tilde{\lambda}_f$	0.38	0.24	0.13	0.015

$$m_i + 3\Delta m_i < M_\odot$$

$$\tilde{\Lambda} - 3\Delta\tilde{\Lambda} > 0$$

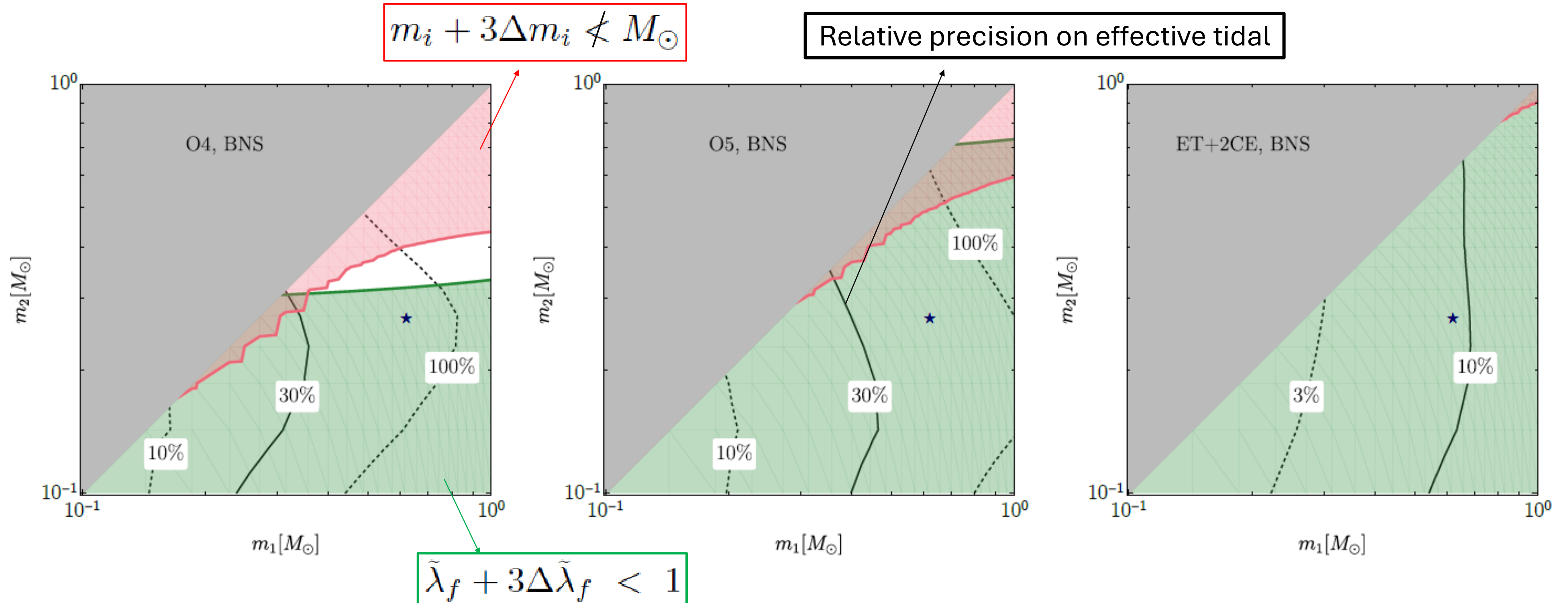
$$\tilde{\lambda}_f + 3\Delta\tilde{\lambda}_f < 1$$

Results:

- we can be certain that the binary is **subsolar** from O5 on;
- **tidal deformability** distinguishes PBHs from BNSs only with 3G detectors;
- **tidal disruption** is well constrained from O3 on.

Exploring the Fisher parameter space: the NS binary case

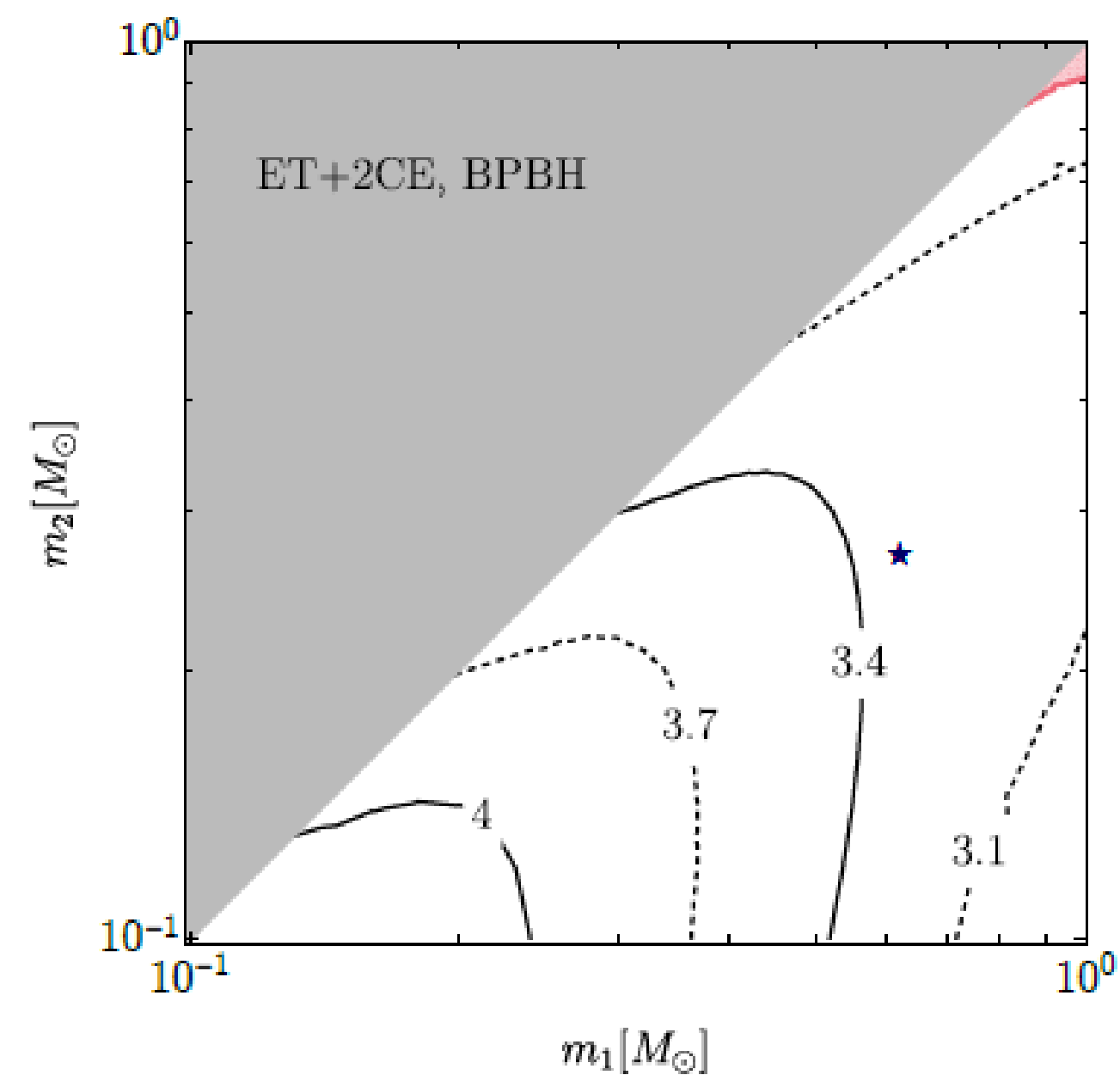
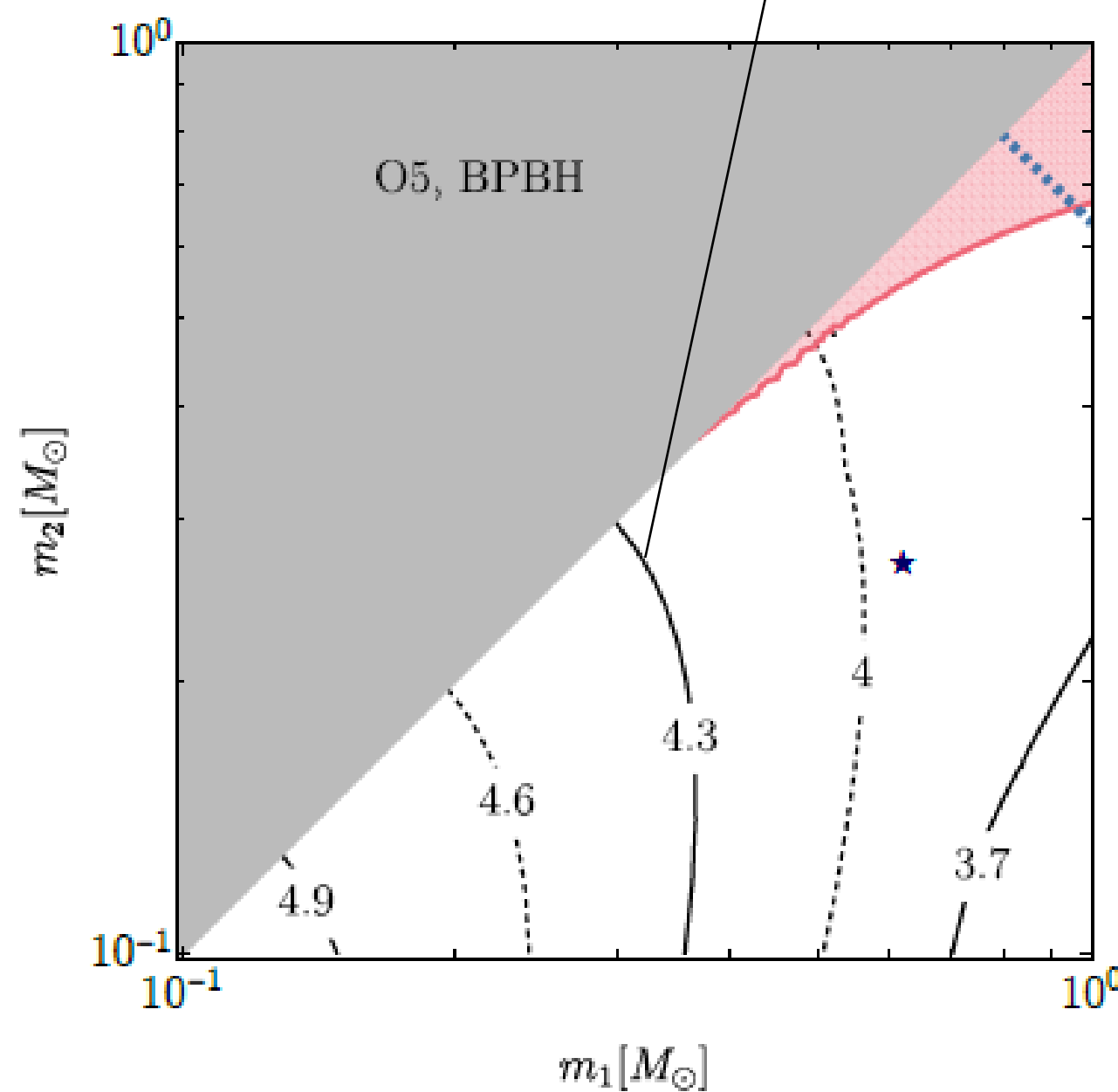
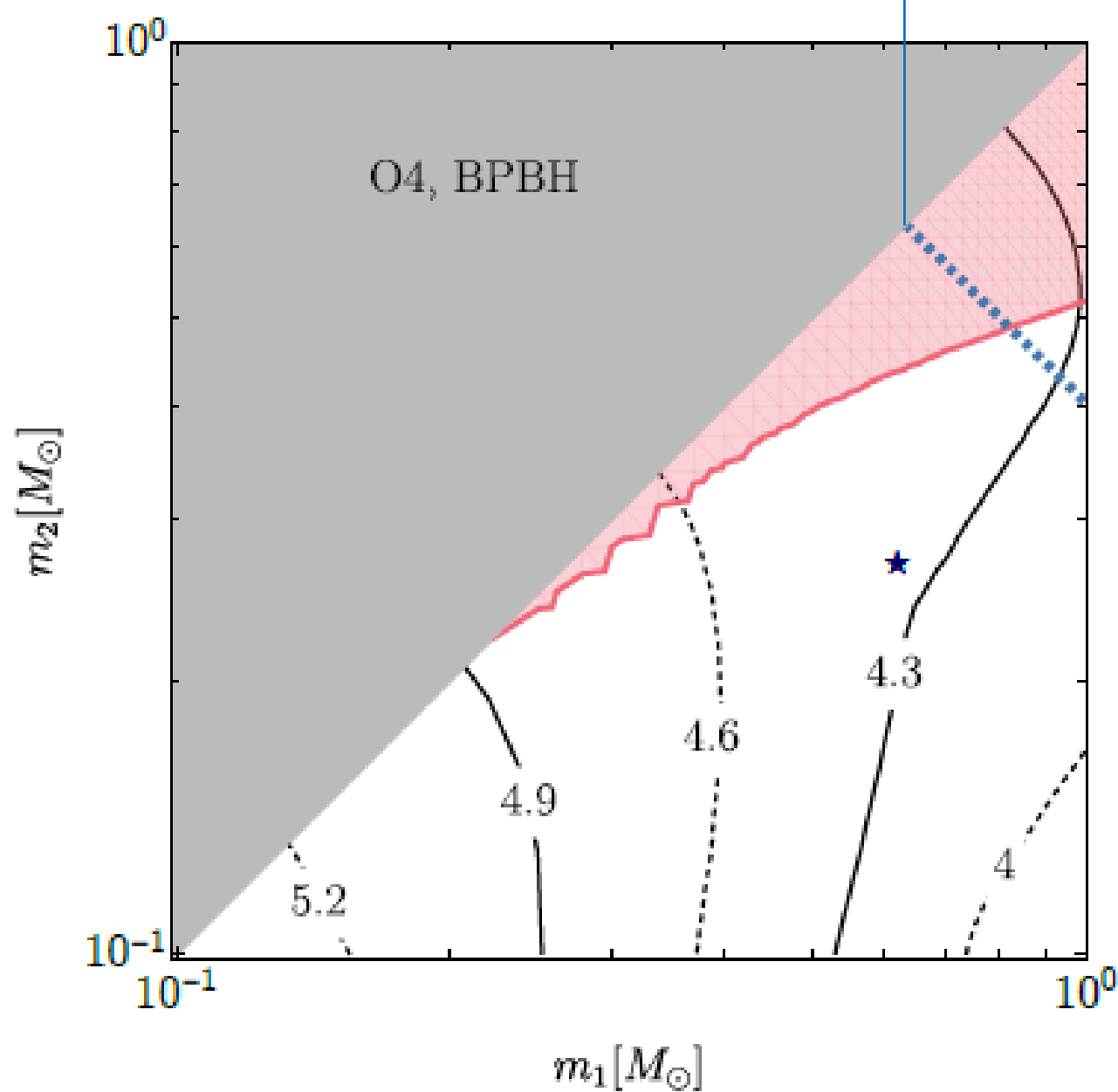
- We scan the parameter space where both masses are in the range $m_1, m_2 \in [0.1; 1]$.
- We assume optimally oriented binaries at a distance corresponding to the threshold for detection with O4 sensitivity.



Exploring the Fisher parameter space: the PBH binary case

BNS tidal bound assuming SLy4 EOS

\log_{10} upper bounds of the effective tidal at 3σ C.L.



Take-home messages and future works

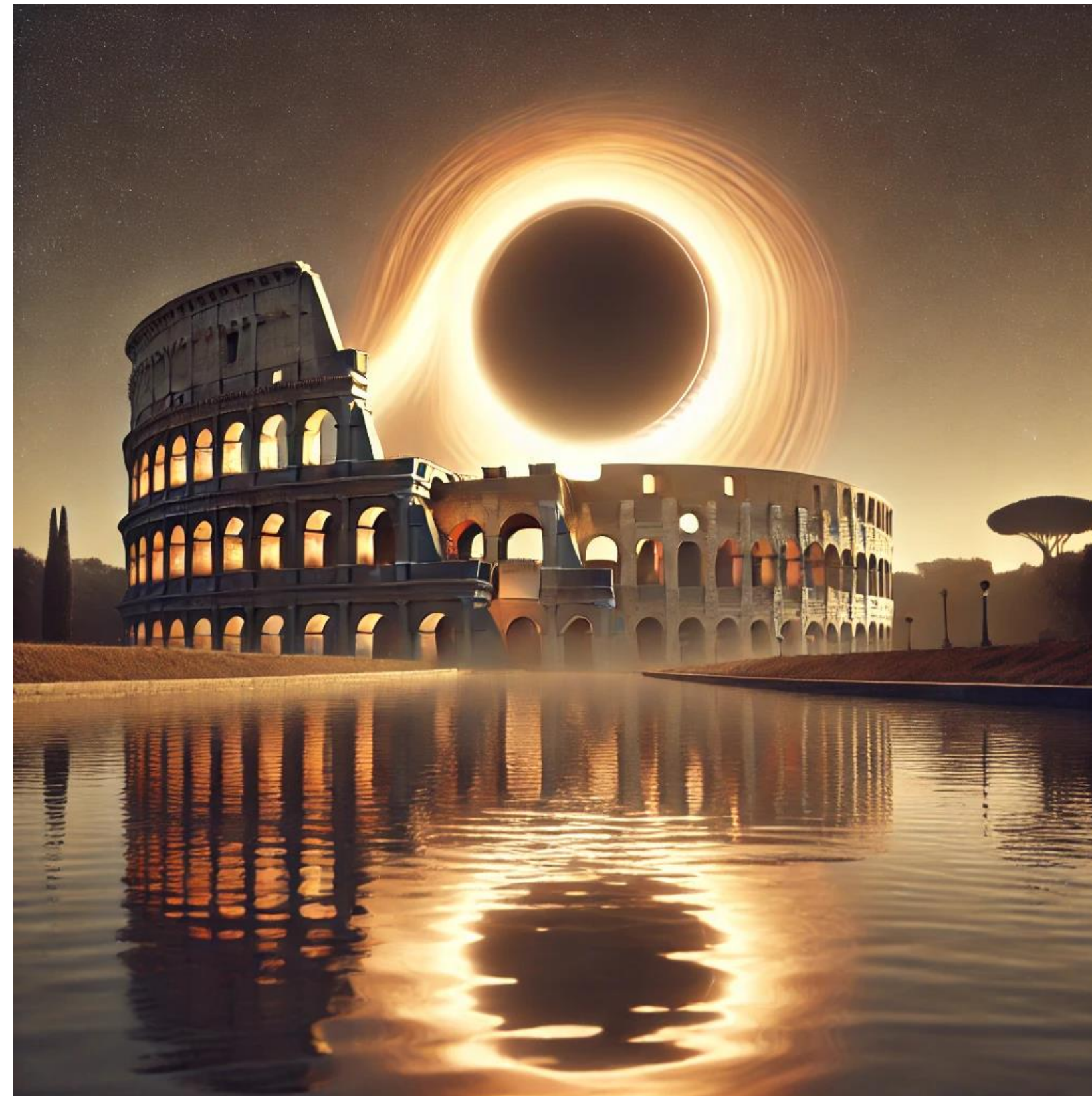
Take-home messages:

- SSM binary events could be **detectable** starting from O4 → very high precision with ET!
- Effective tidal parameter will be well-constrained, at least to compare the **PBH hypothesis** against the subsolar NS one, or even against more **exotic hypotheses**.

Future works on this topic:

- Build a more accurate **waveform** (demanding, important effects due to the tidal disruptions);
- Studying implications of **cosmology** and **nuclear physics** for SSM objects [Crescimbeni+, 2408.14287]
see M. Vaglio's talk!

Thank you for your attention!



Back-up slides

Binary maximum frequency of material compact objects

- A GW signal has a **maximum frequency** of the order of **ISCO**:

$$f_{\text{ISCO}} = \frac{c^3}{(6^{3/2}\pi GM)} = 4.4 \text{ kHz} \left(\frac{M_{\odot}}{M} \right)$$

- binaries of **stellar objects** are typically characterized by **smaller maximal frequencies** (hard surface, tidal disruption,...)

$$r_{T,i} = \left(\frac{2m_j}{m_i} \right)^{1/3} r_i \quad \longrightarrow \quad f_T = \frac{1}{\pi} \sqrt{\frac{GM}{(\max[r_{T,1}, r_{T,2}])^3}}$$

Binary maximum frequency of material compact objects

- White dwarfs:

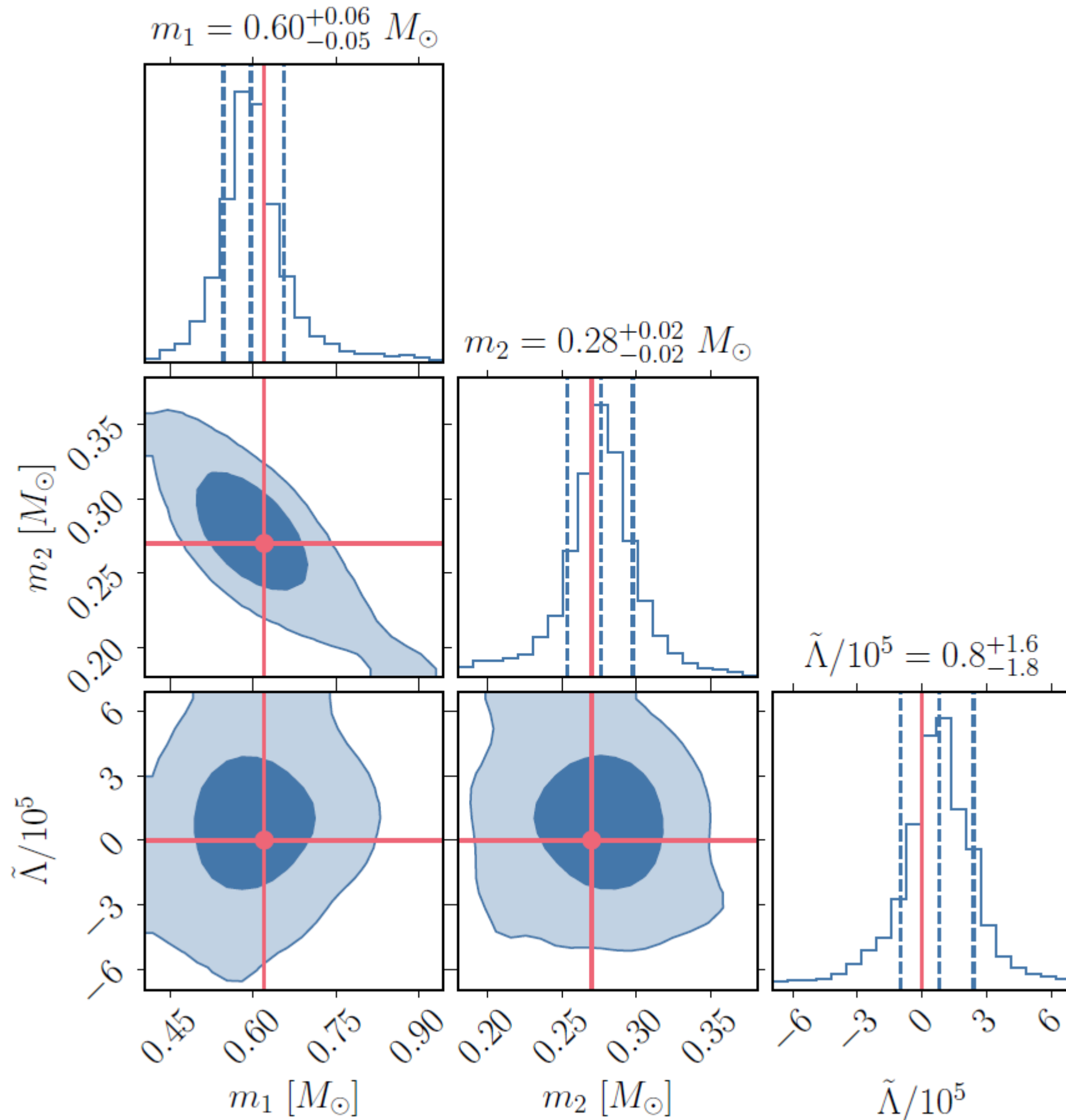
$$r_{\text{WD}} = 0.013 r_{\odot} \left(\frac{m_{\text{WD}}}{M_{\odot}} \right)^{-1/3} \quad \longrightarrow \quad f_{\text{max}}^{\text{WD}} = 0.13 \text{ Hz} \left(\frac{m_{\text{WD}}}{M_{\odot}} \right) \quad \longrightarrow \quad \boxed{\text{Detectable by deci-Hz detectors}}$$

- Neutron stars:

$$f_{\text{max}}^{\text{NS}} \approx 1.4 \text{ kHz} \left(\frac{m_{\text{NS}}}{0.5 M_{\odot}} \right)^{1/2} \left(\frac{15 \text{ km}}{r_{\text{NS}}} \right)^{3/2} \quad \xrightarrow{\boxed{\text{More accurate expression}}} \quad f_{\text{RO}}/\text{Hz} = -26.9 - 35.5 \left(\frac{m_1}{M_{\odot}} \right) - 3.02 \left(\frac{m_1}{M_{\odot}} \right)^2 + 1690 \left(\frac{m_2}{M_{\odot}} \right) - 575 \left(\frac{m_2}{M_{\odot}} \right)^2$$

[Bandopadhyay+, 2212.03855]

Bayesian inference vs Fisher for BPBHs: O3

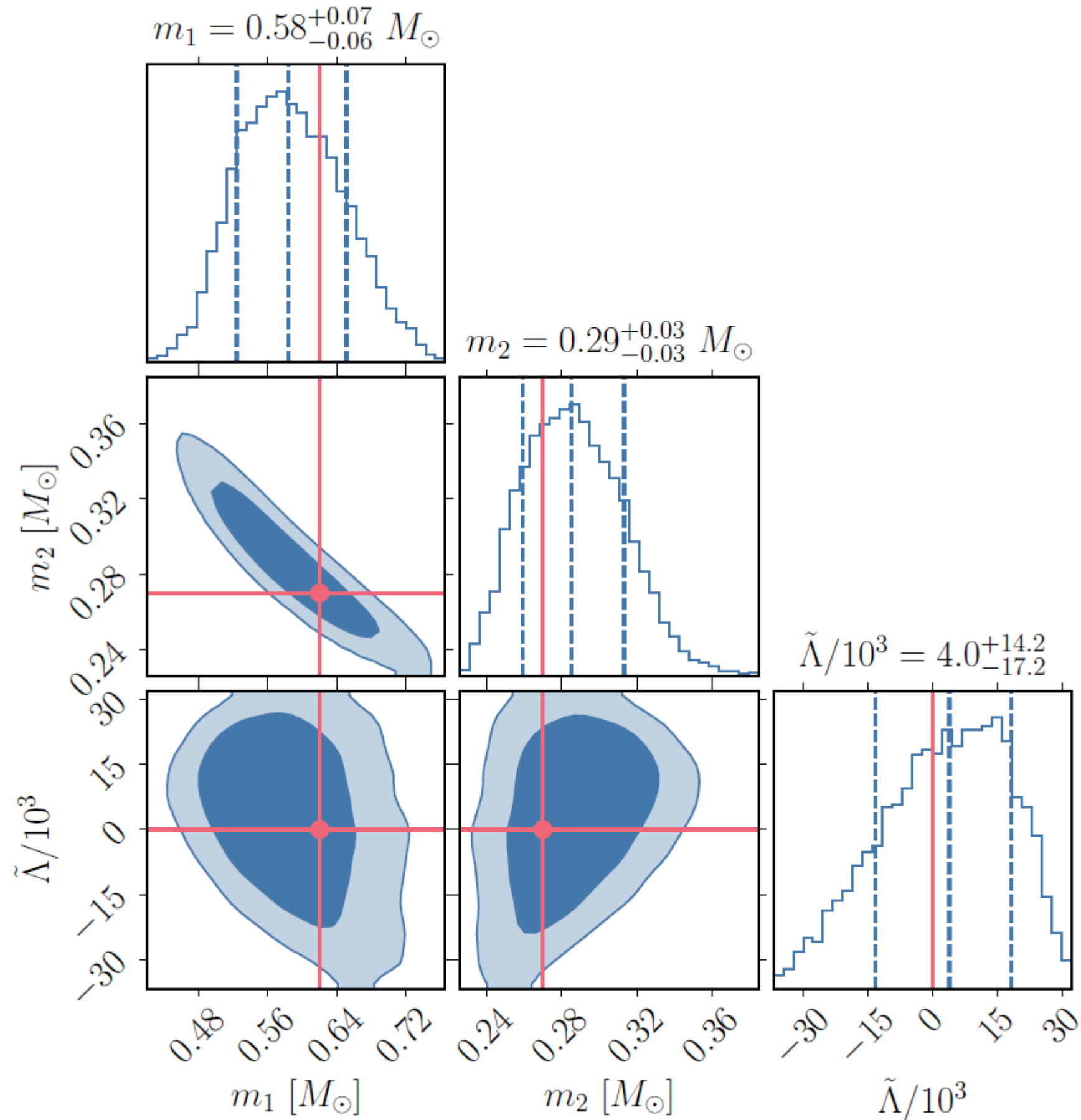


Network	LVK O3	LVK O4	LVK O5	ET+2CE
BPBH SSM200308 ($\tilde{\Lambda} = \delta\tilde{\Lambda} = 0, \tilde{\lambda}_f = 1$)				
SNR	8.76	14.6	24.8	430
$\Delta m_1/m_1$	0.21	0.14	0.053	$6.4 \cdot 10^{-3}$
$\Delta m_2/m_2$	0.18	0.12	0.046	$5.5 \cdot 10^{-3}$
$\Delta \tilde{\Lambda}$	$1.9 \cdot 10^4$	$1.3 \cdot 10^4$	$7.8 \cdot 10^3$	$7.7 \cdot 10^2$

Example of exclusion of BS model

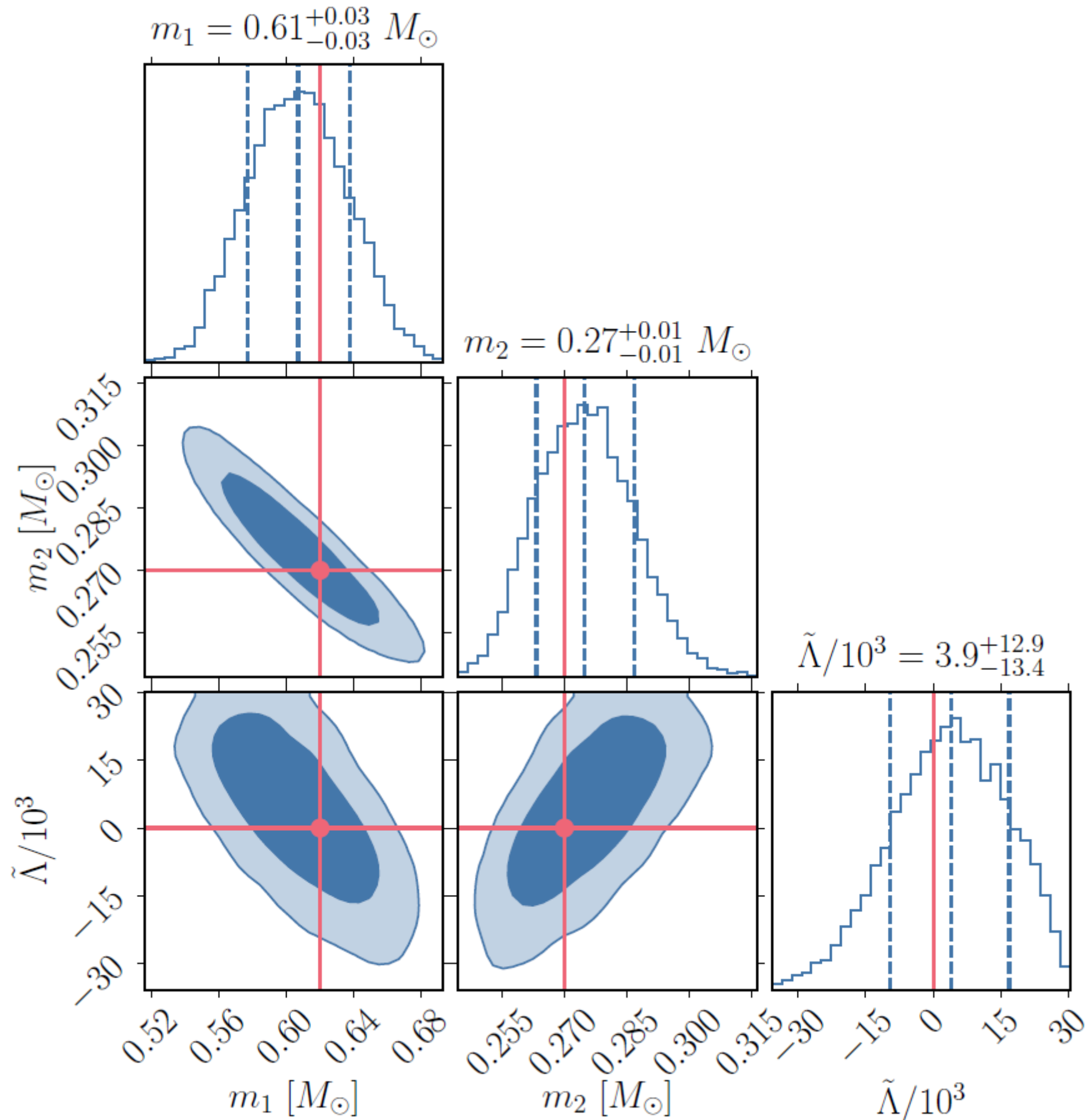
$$m_1 = m_2 = 0.62 M_\odot \quad \tilde{\Lambda} > 3 \cdot 10^4 \quad m_B \gtrsim 15 M_\odot$$

Bayesian inference vs Fisher for BPBHs : O4



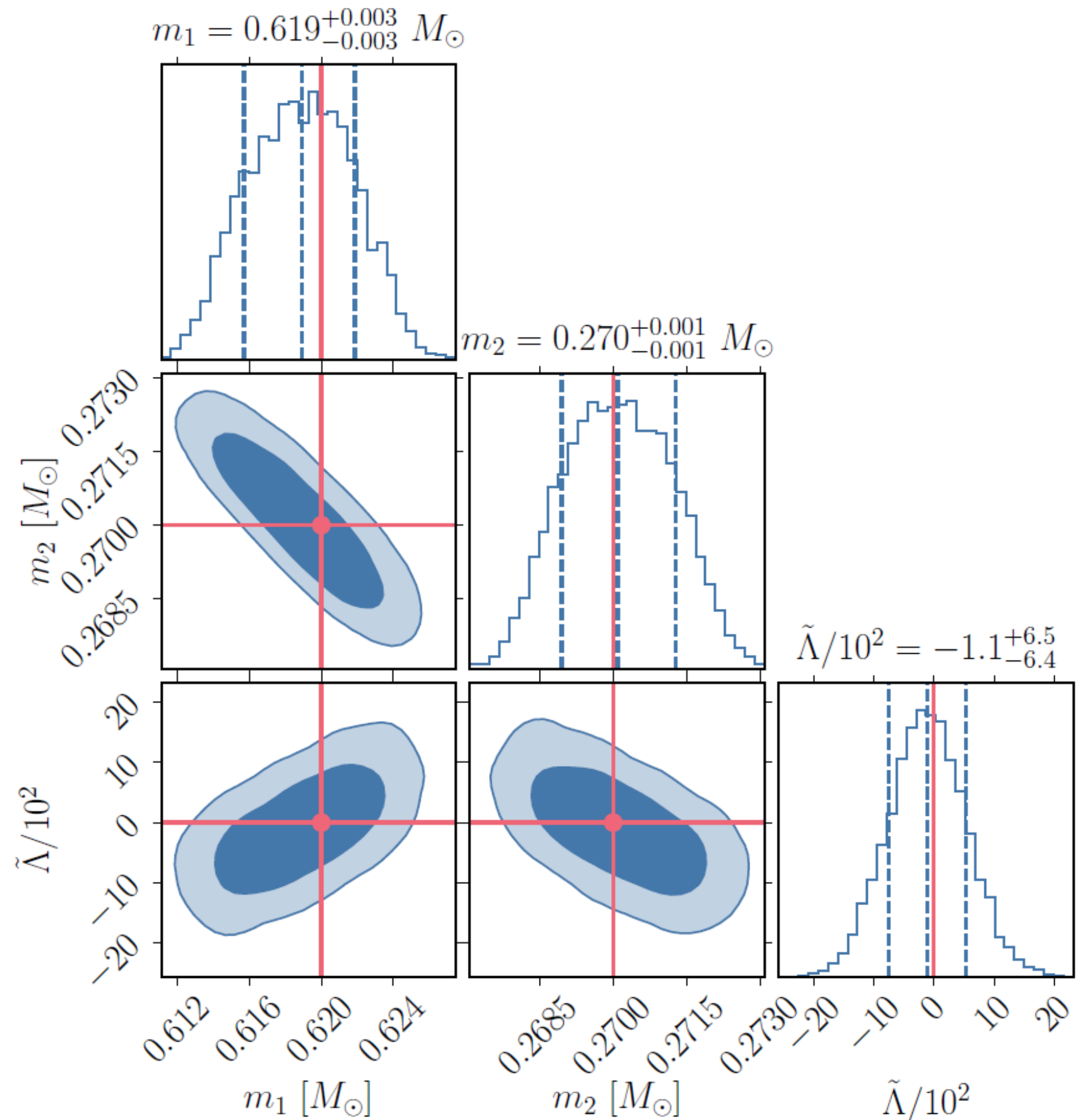
Network	LVK O3	LVK O4	LVK O5	ET+2CE
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$\Delta\tilde{\Lambda}$	$1.9 \cdot 10^4$	$1.3 \cdot 10^4$	$7.8 \cdot 10^3$	$7.7 \cdot 10^2$

Bayesian inference vs Fisher for BPBHs: O5



Network	LVK O3	LVK O4	LVK O5	ET+2CE
BPBH SSM200308 ($\tilde{\Lambda} = \delta\tilde{\Lambda} = 0, \tilde{\lambda}_f = 1$)				
SNR	8.76	14.6	24.8	430
$\Delta m_1 / m_1$	0.21	0.14	0.053	$6.4 \cdot 10^{-3}$
$\Delta m_2 / m_2$	0.18	0.12	0.046	$5.5 \cdot 10^{-3}$
$\Delta \tilde{\Lambda}$	$1.9 \cdot 10^4$	$1.3 \cdot 10^4$	$7.8 \cdot 10^3$	$7.7 \cdot 10^2$

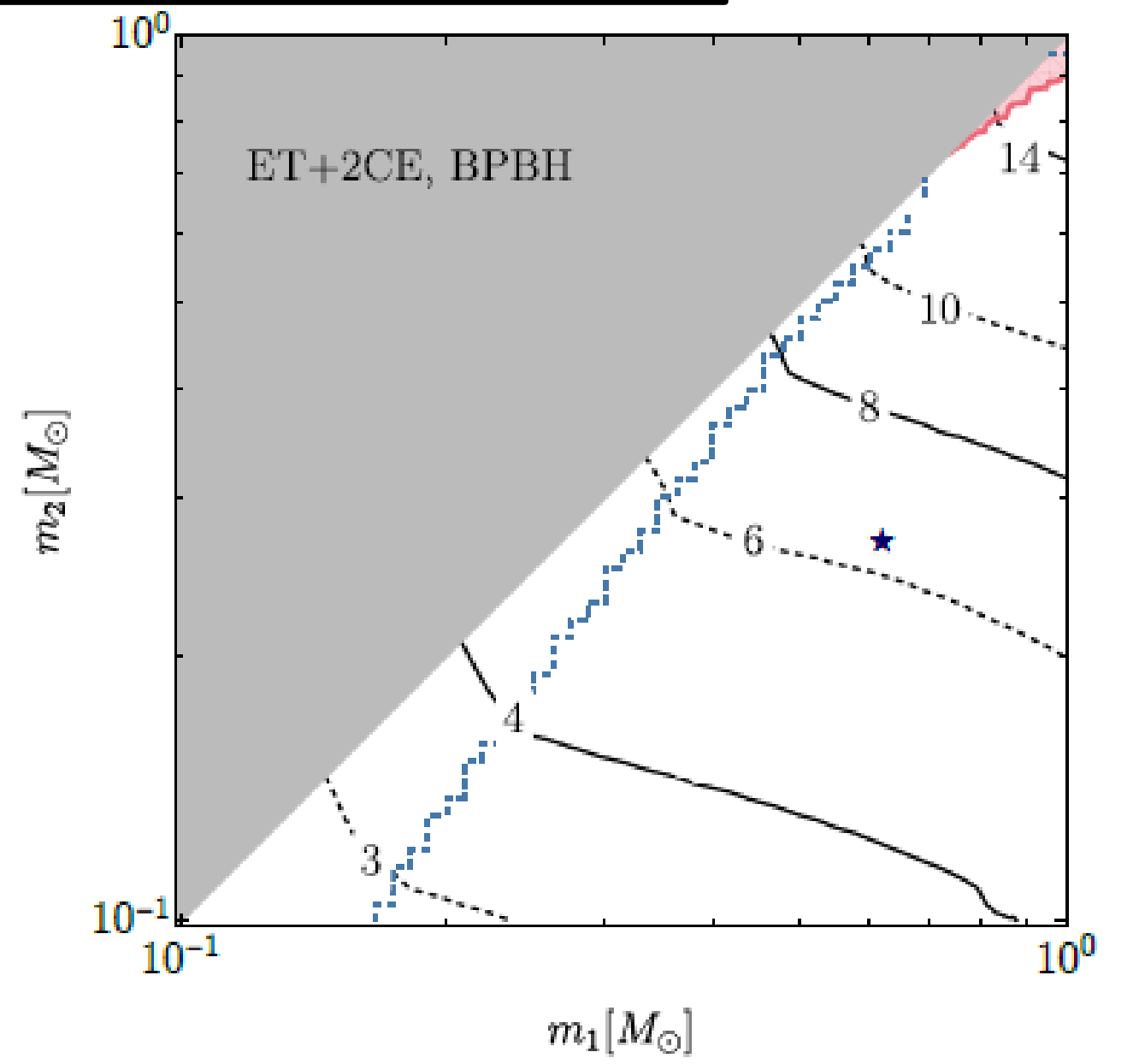
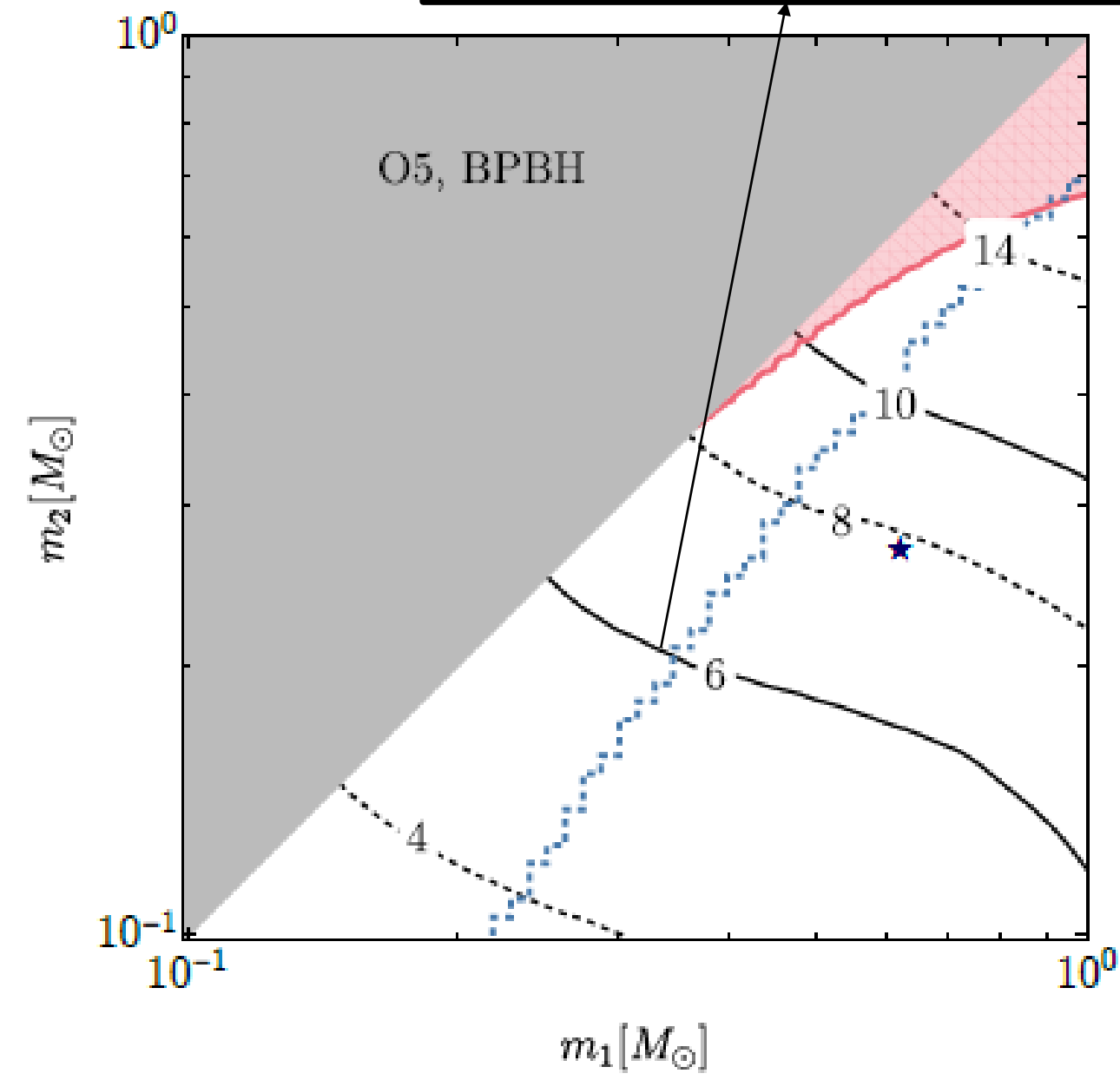
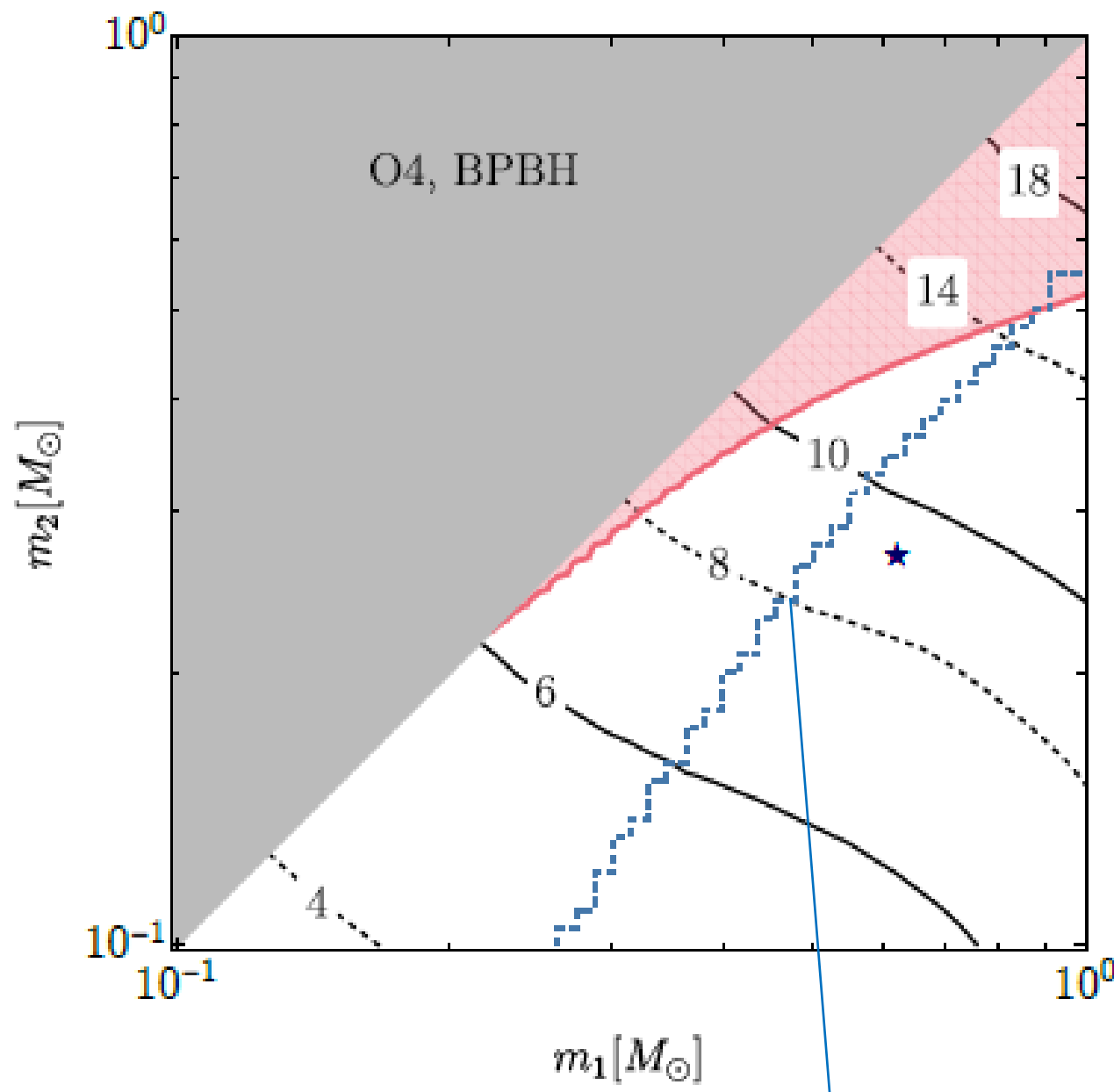
Bayesian inference vs Fisher for BPBHs: ET+2CE



Network	LVK O3	LVK O4	LVK O5	ET+2CE
BPBH SSM200308 ($\tilde{\Lambda} = \delta\tilde{\Lambda} = 0, \tilde{\lambda}_f = 1$)				
SNR	8.76	14.6	24.8	430
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Exploring the Fisher parameter space: constraints on BSs with large quartic interaction

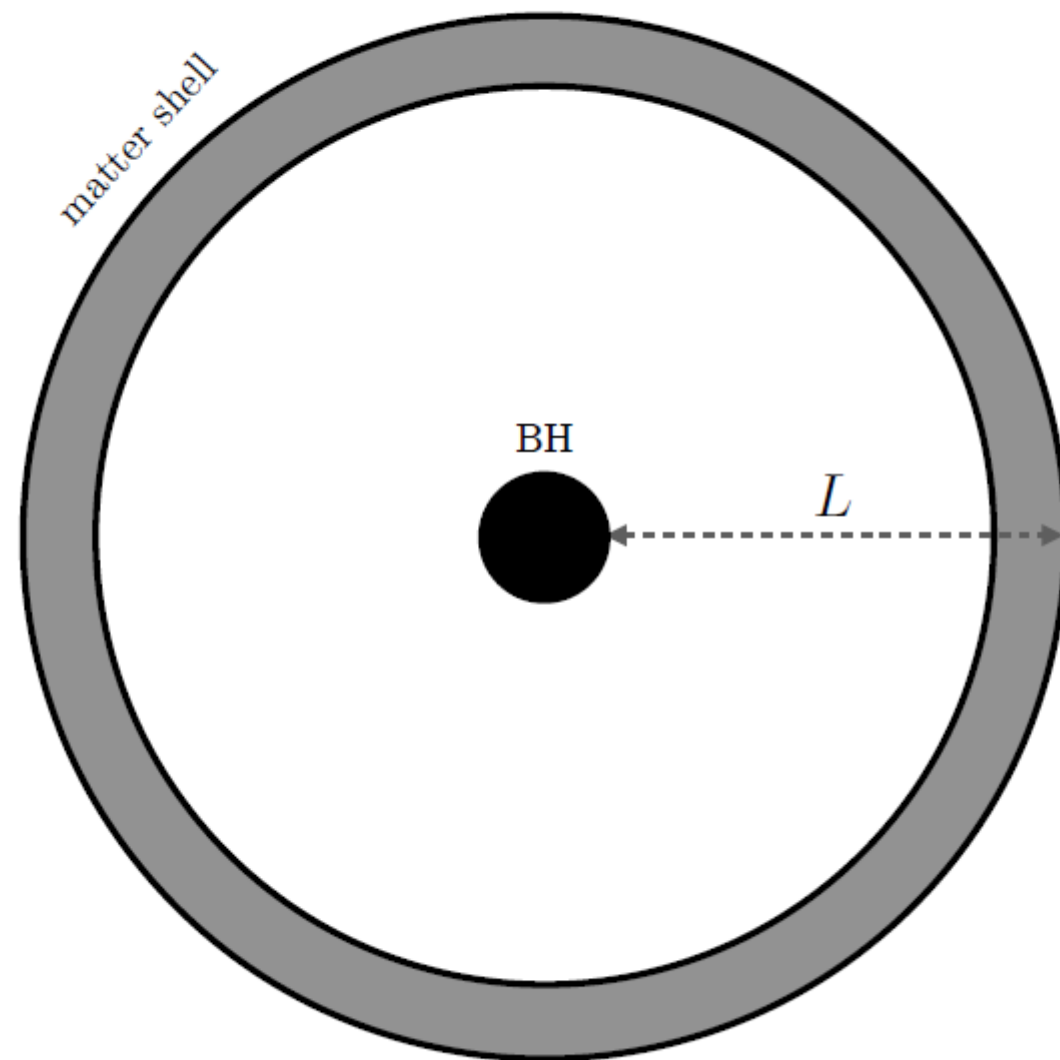
values of m_B/M_\odot above which the tidal deformability would be incompatible with future upper bounds (at 3σ C.L.)



BS existence bound: $m_i < 0.06 m_B$

Do we exclude BPBHs if $\Lambda=0$?

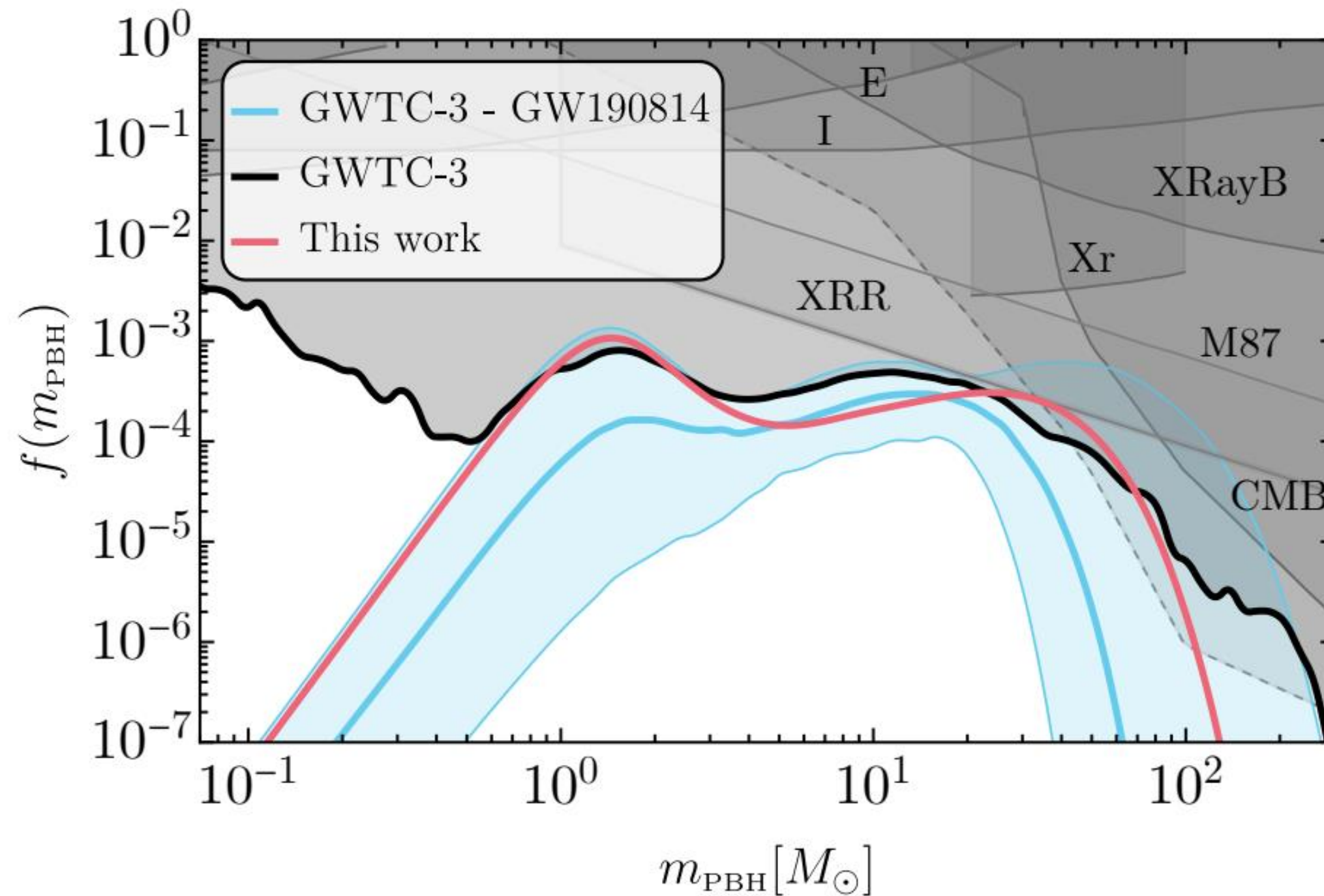
- Having $\Lambda=0$ may not exclude PBHs at all.
- If a PBH presents an astrophysical environment, tidal deformabilities will be different from zero.



$$k_2 = -\frac{\epsilon}{5} \left(\frac{L}{r_s} \right)^6$$

- Distinguish between BPBHs with environment and 'naked' PBHs [De Luca, Franciolini, Riotto, 2408.14207].

Subsolar event rates vs PBH abundance



Source ref. Iacovelli+, 2304.03160

$$f(m_{\text{PBH}}) \equiv \frac{1}{\Omega_{\text{DM}}} \frac{d\Omega_{\text{PBH}}}{d \ln m_{\text{PBH}}} = m_{\text{PBH}} f_{\text{PBH}} \psi(m_{\text{PBH}})$$

PBH abundance ← ← Mass function distribution
↓ Dark matter fraction