



**INVISIBLES24**

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# HyperLSW: An ultimate experiment to Determine the amount of dark matter axions

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**HIDDe**  
Hunting Invisibles: Dark sectors, Dark matter and Neutrinos

Based on

S. Hoof, J. Jaeckel, GL, ArXiv:2407:XXXXX



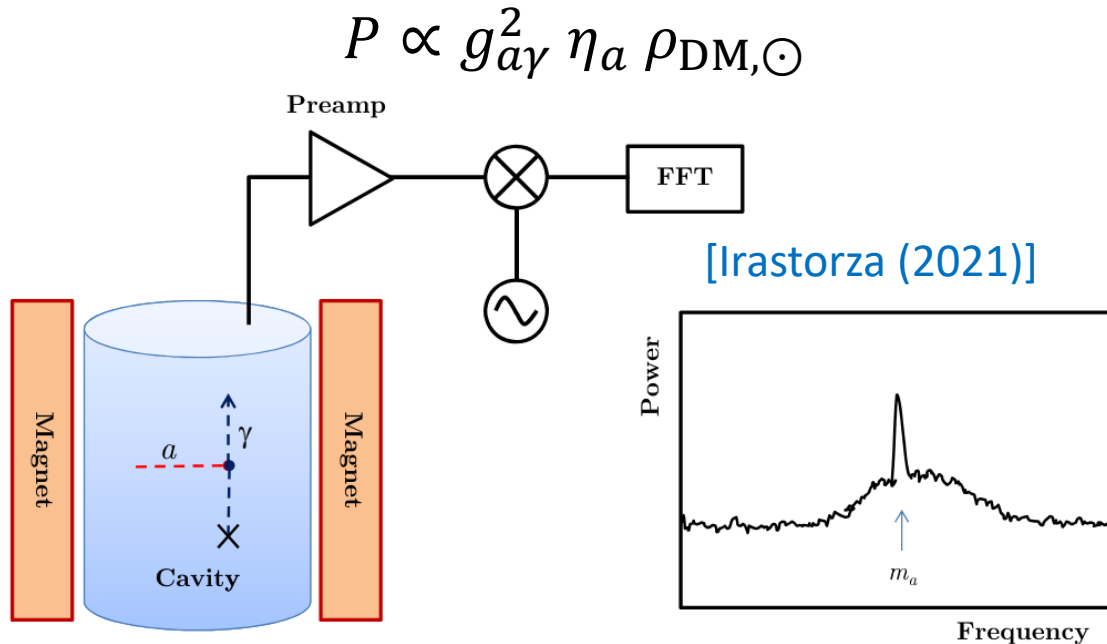
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# GENERAL STRATEGY

$$\mathcal{L}_{a\gamma} = -\frac{1}{4} g_{a\gamma} \tilde{F}^{\mu\nu} F_{\mu\nu} a$$

## HALOSCOPE DISCOVERY

[Sikivie (1983)]



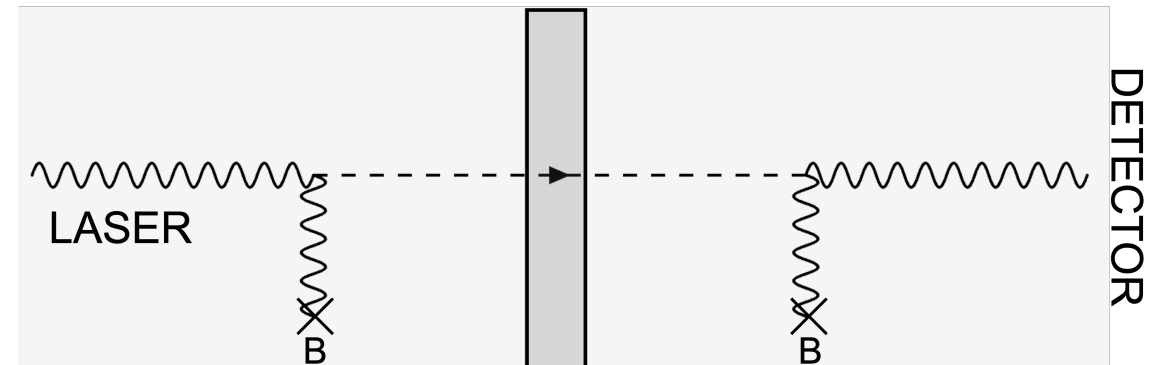
$m_a$  measured with extreme precision.

[O'Hare & Green (2017)]

## LSW FOLLOW-UP

[Van Bibber et al. (1987), Arias et al. (2010)]

$$p_{\gamma \leftrightarrow a}^2 = \frac{\omega^2}{\omega^2 - m_a^2} \left( \frac{g_{a\gamma} B L}{2} \right)^4 |F|^4$$

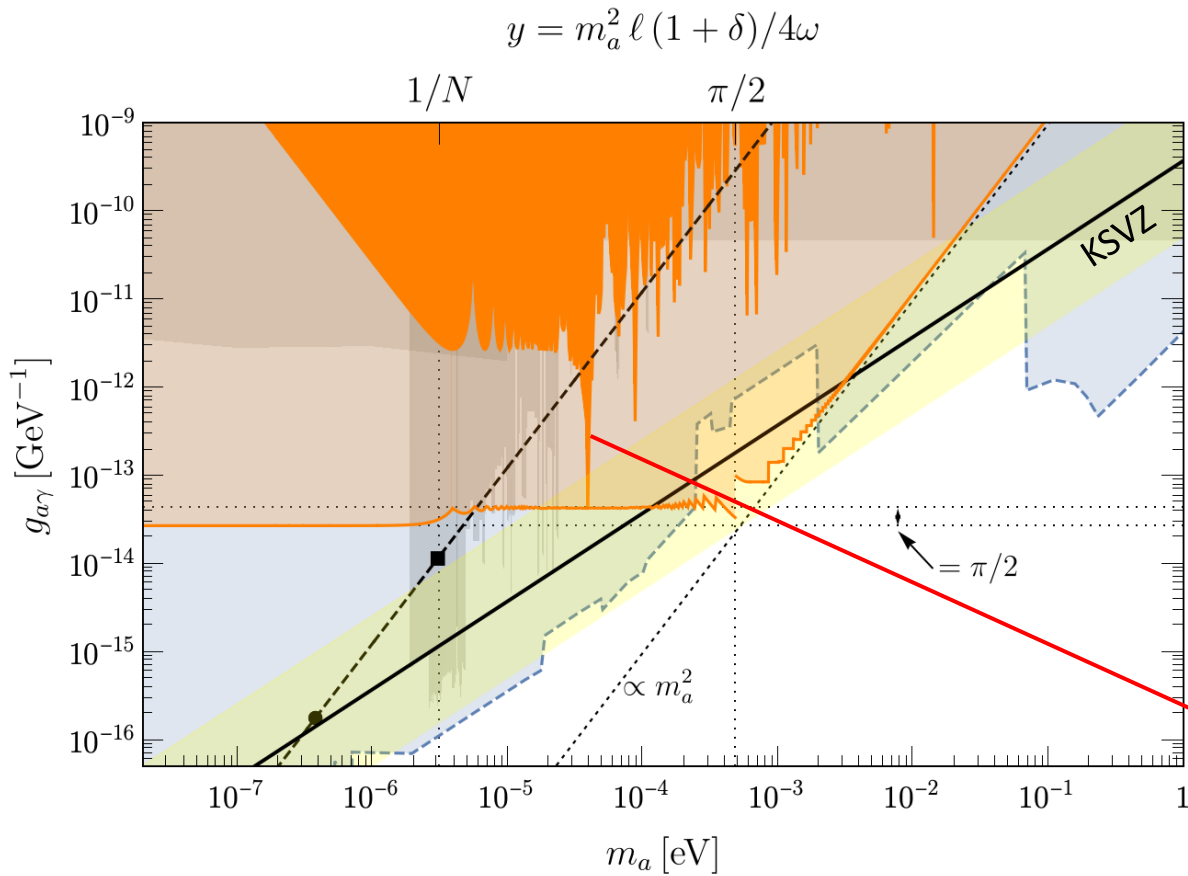


Pure laboratory experiment to measure  $g_{a\gamma}$ .

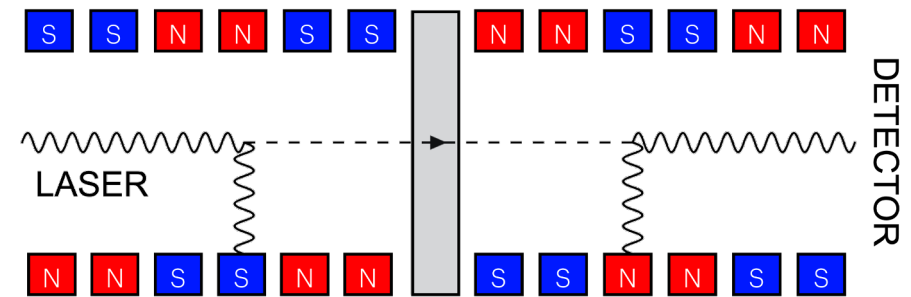
# OPTIMIZING LSW SETUPS

[Van Bibber et al. (1987), Arias et al. (2010)]

Single long magnet not sufficient to probe the QCD band (coherence is lost when  $L \sim 2\pi \omega/m_a^2$ )



Optimize magnet configuration  $\rightarrow$  Alternating magnets



Resonance at  $m_a \approx \sqrt{\frac{2\pi\omega}{n_s \ell (1+\delta)}}$

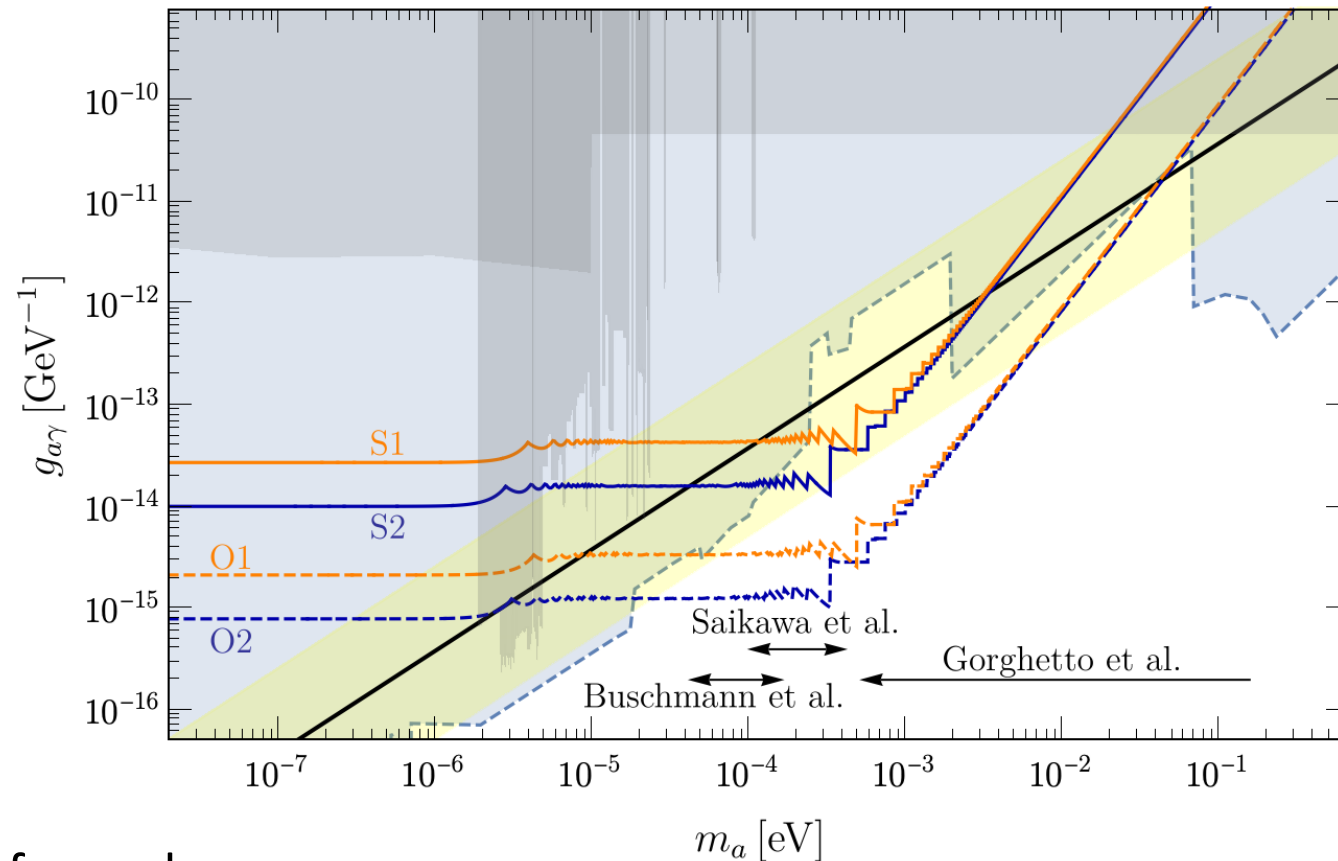
# SENSITIVITY FOR BENCHMARK SETUPS

Setup	$B$ [T]	$a$ [m]	$\ell$ [m]	$\Delta_{\min}$ [m]	$P_\lambda$ [W]	$\beta_g$	$\beta_r$	$\lambda$ [nm]	$\varepsilon_{\text{eff}}$	$\tau$ [h]	$b$ [s $^{-1}$ ]	$2z_{\text{opt}}$ [km]	$\mathcal{S}_{\text{crit}}$
S1	9	1.3	4.0	2.0	3	$10^5$	$10^5$	1064	0.95	100	$10^{-4}$	$2 \times 94$	186.42
S2	11	1.8	10.0	3.0	3	$10^5$	$10^5$	1064	0.95	100	$10^{-4}$	$2 \times 181$	186.42
O1	9	1.3	4.0	2.0	300	$10^5$	$10^6$	1064	0.95	5000	$10^{-6}$	$2 \times 79$	172.55
O2	11	1.8	10.0	3.0	300	$10^5$	$10^6$	1064	0.95	5000	$10^{-6}$	$2 \times 152$	172.55

Avoid clipping losses:

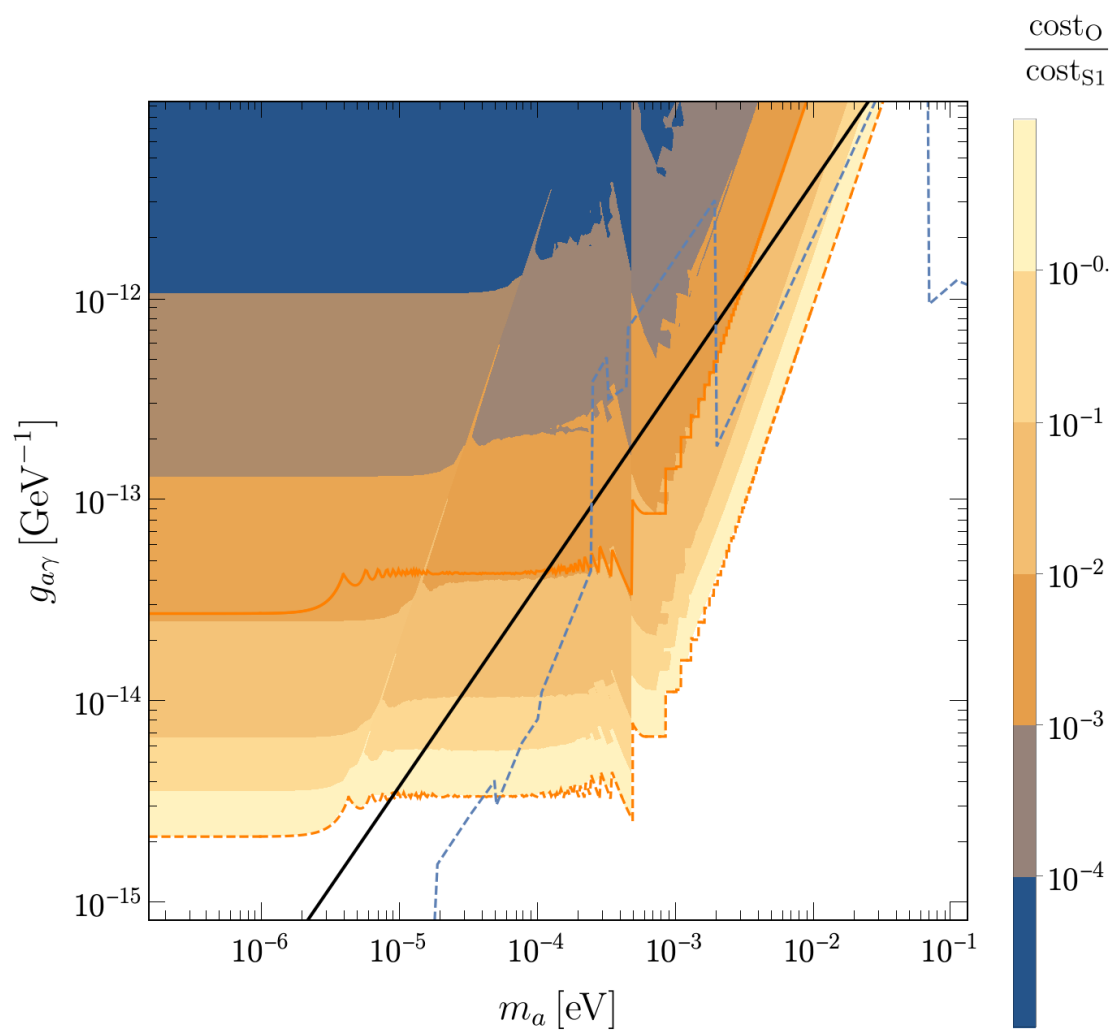
$$z_{\text{opt}} \approx 94.2 \text{ km} \frac{1064 \text{ nm}}{\lambda} \left( \frac{a}{1.3 \text{ m}} \right)^2$$

[Arias et al. (2010)]



Optimal configurations for each  $m_a$ .

# CHALLENGING REALIZATION



$\frac{\text{cost}_O}{\text{cost}_{S1}}$  Long tunnel + many strong magnets  $\approx O(100)$  GEur  
[Grose (2021)] [Calvelli et al. (2020, 2023)]

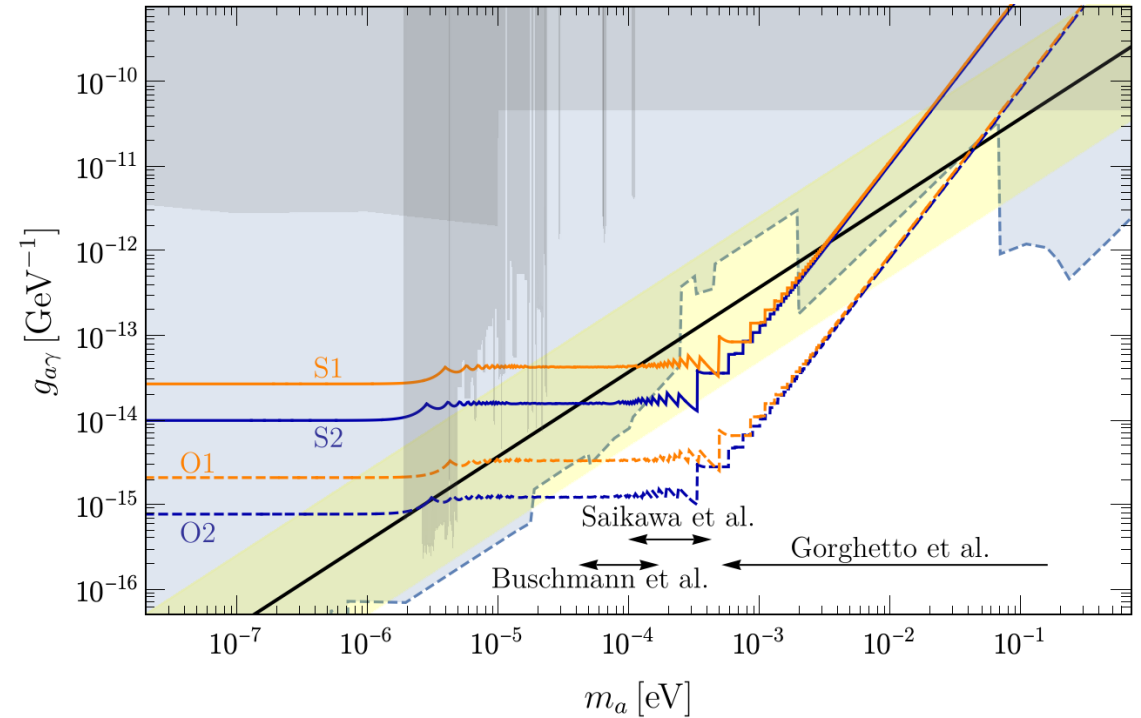
Improvements in the optical setup can help:  
pick the cheapest solution!

## TAKE-AWAY MESSAGES

- HyperLSW experiments sensitive to KSVZ axions with  $3 \mu\text{eV} \lesssim m_a \lesssim 45 \text{ meV}$ .
- Very costly, error control and magnetic field profiling required.
- BUT No technological breakthroughs needed and infrastructure useful for non-axion physics!

Thank you and  
Come to see my poster!

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# BACKUP

# FORM FACTOR

[Arias et al. (2010)]

$$F \equiv \frac{1}{L} \int_0^L dz f(z) e^{iqz}$$

$$q \equiv n_r \omega - \sqrt{\omega^2 - m_a^2} \approx (n_r - 1) \omega + \frac{m_a^2}{2\omega}$$

- **General configuration**

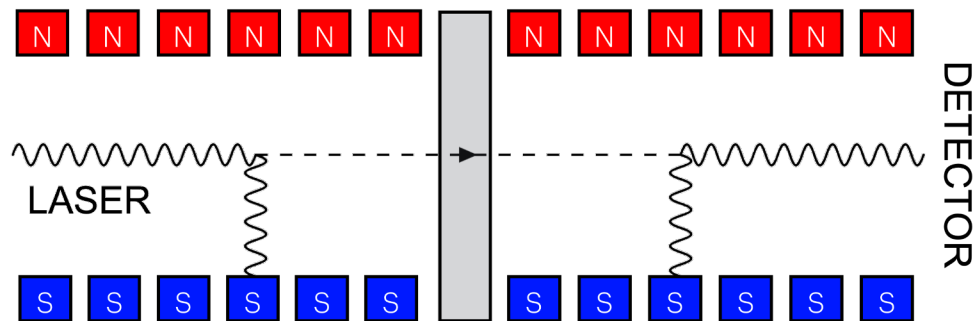
$$F_{n_s, n_g}(x; \delta) = \frac{\text{sinc}(x)}{n_g n_s} \frac{\tan(n_s y)}{\sin(y)} \begin{cases} \sin(n_s n_g y) & \text{if } n_g \text{ is even} \\ \cos(n_s n_g y) & \text{if } n_g \text{ is odd} \end{cases}$$

where  $\text{sinc}(x) \equiv \sin(x)/x$ ,  $x \equiv q\ell/2$ ,  $y \equiv x(1 + \delta)$ , and  $\delta \equiv \Delta/\ell$

Maxima close to  $x_k = \frac{(2k+1)\pi}{2n_s(1+\delta)}$  for  $k \in \mathbb{N}_0$   $\longrightarrow$   $\left| \frac{F_{n_s, n_g}(x; \delta)}{F_{1,1}(x; \delta)} \right| \rightarrow \left| \frac{1}{n_s \sin(\pi/2n_s)} \right| \simeq \frac{2}{\pi} \quad (x \rightarrow x_0)$ ,

- **Fully-aligned setup**

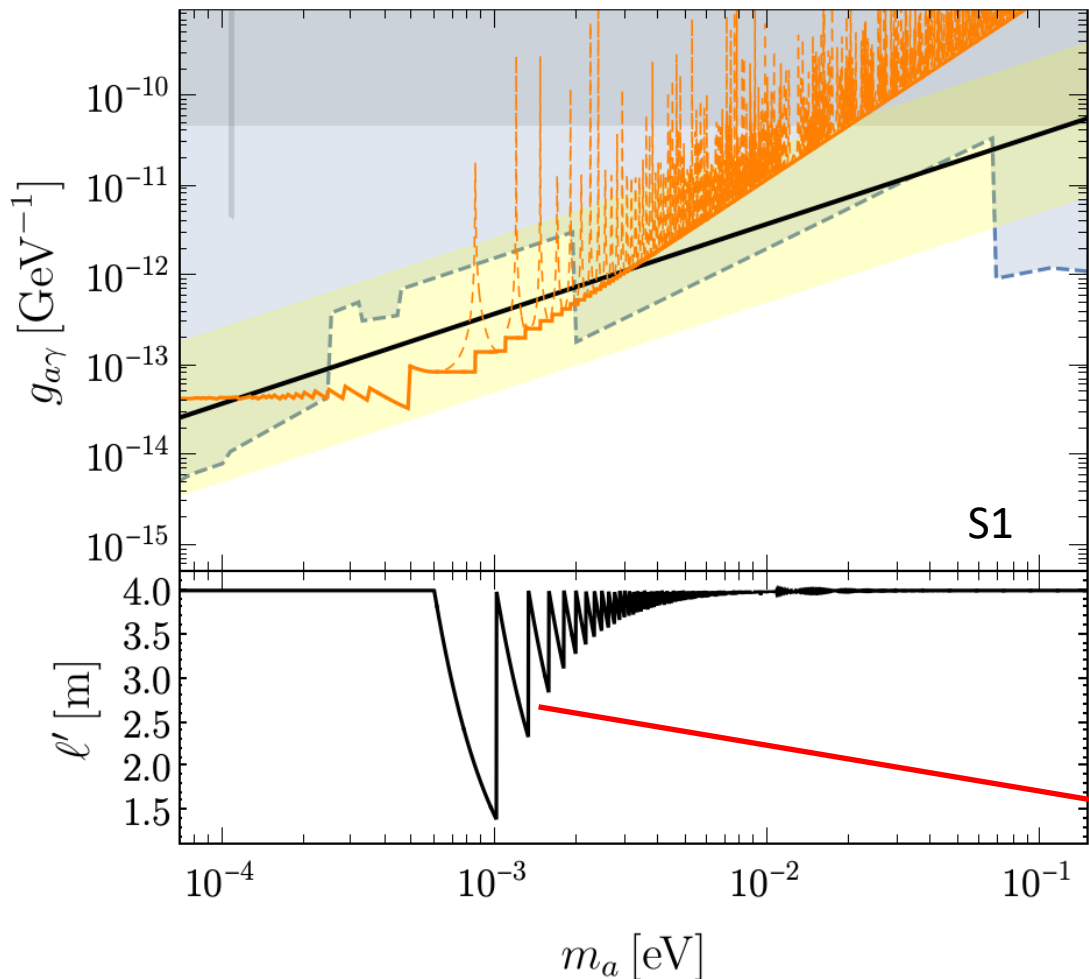
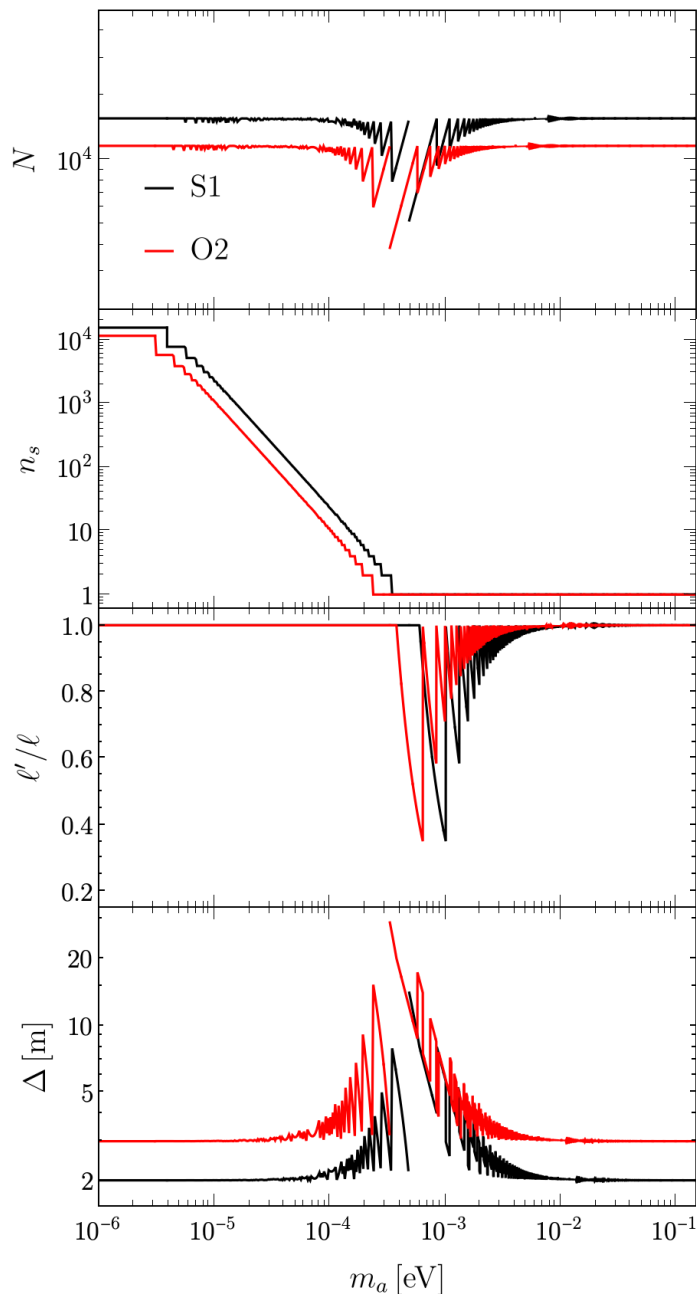
$$F_{N,1}(x) = \frac{\text{sinc}(x)}{N} \frac{\sin(Ny)}{\sin(y)}$$





# OPTIMAL SETUP

At large masses we modify  $\ell \rightarrow \ell'$  to maximize the single magnet form factor.



$$F_{1,N}(x) \rightarrow F_{1,1}(x) \quad (x \rightarrow x_k)$$

$$F_{1,1} = \text{sinc}(x)$$

$$x_k = \frac{(2k+1)\pi}{2n_s(1+\delta)} \quad \text{for } k \in \mathbb{N}_0$$

$$(1) \quad \ell(1+\delta) = \ell'(1+\delta')$$

$\text{sinc}(x')$  maximized at

$$(2) \quad x'_{k'} = \frac{\pi}{2} + k'\pi \quad \text{for } k' \in \mathbb{N}$$

where  $x' = q \frac{\ell'}{2}$

Find the largest  $\ell' \leq \ell$  satisfying (1) and (2).

# SENSITIVITY

$$\mathcal{S} = \varepsilon_{\text{eff}} \frac{P_{\lambda} \tau}{\omega} \beta_g \beta_r p_{\gamma \leftrightarrow a}^2$$

Figure of merit  $\Phi = \frac{\mathcal{S}}{\sqrt{\mathcal{S} + \mathcal{B}}}$

$$p_{\gamma \leftrightarrow a}^2 = \frac{\omega^2}{\omega^2 - m_a^2} \left( \frac{g_{a\gamma} B L}{2} \right)^4 |F|^4 \rightarrow \mathcal{S} \propto g_{a\gamma}^4 \rightarrow \Pi = \frac{\Delta g_{a\gamma}}{g_{a\gamma}} = \frac{1}{4\Phi}$$

Signal threshold for precision  $\Pi$ :  $\mathcal{S}_{\text{crit}} = \frac{1}{32 \Pi^2} \left( 1 + \sqrt{1 + 64 \mathcal{B} \Pi^2} \right)$

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S1	9	1.3	4.0	2.0	3	10 <sup>5</sup>	10 <sup>5</sup>	1064	0.95	100	10 <sup>-4</sup>	2 × 94	186.42
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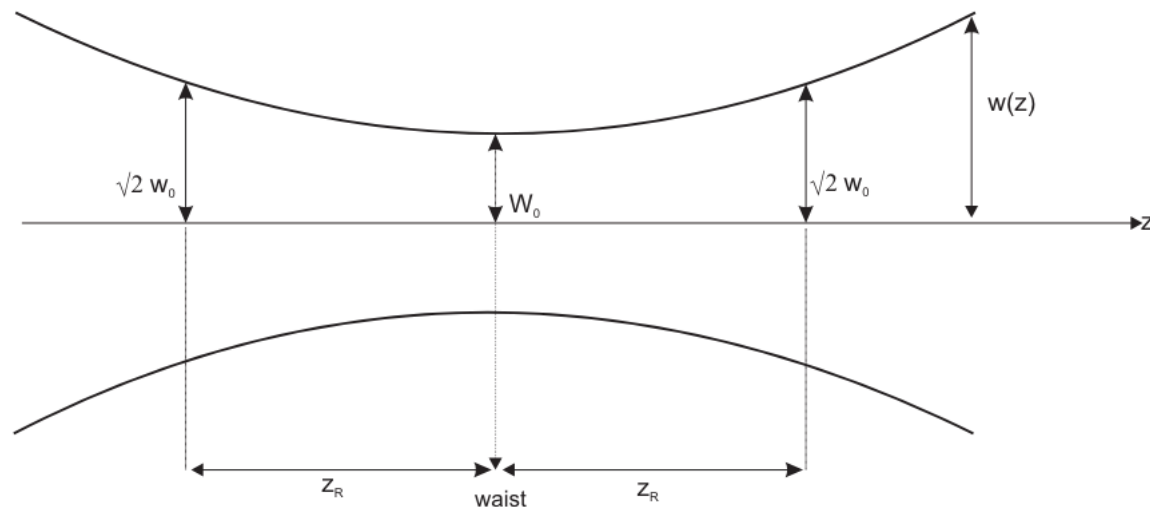
$\Pi = 2\%$

# OPTIMAL LENGTH

[Arias et al. (2010)]

$$\frac{w(z)}{w_0} = \sqrt{1 + \left(\frac{z - z_N}{z_R}\right)^2} \quad z_R = \pi w_0^2 / \lambda$$

Fraction of power transmitted through a circular aperture of diameter  $a$ :  $1 - e^{-a^2/2w^2}$



$$g_{\text{sens}} \propto L^{-1} \beta^{-1/2} = L^{-1} (\beta_0^{-1} + e^{-\zeta})^{1/2} \quad L \sim Z \quad \rightarrow \quad \text{Minimum at } e^{-\zeta} \left(\frac{\zeta}{2} - 1\right) - \beta_0^{-1} = 0, \quad \zeta = \pi a^2 / 4\lambda Z$$

$$\beta \approx \beta_0 = 10^5: \quad z_{\text{opt}} \approx 94.2 \text{ km} \frac{1064 \text{ nm}}{\lambda} \left(\frac{a}{1.3 \text{ m}}\right)^2$$

Setup	$B$ [T]	$a$ [m]	$\ell$ [m]	$\Delta_{\text{min}}$ [m]	$P_\lambda$ [W]	$\beta_g$	$\beta_r$	$\lambda$ [nm]	$\epsilon_{\text{eff}}$	$\tau$ [h]	$b$ [s <sup>-1</sup> ]	$2z_{\text{opt}}$ [km]	$\mathcal{S}_{\text{crit}}$
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