

Axion-Like Particles in Radiative Quarkonia Decays

Xavier Ponce Díaz

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with Luca Di Luzio, Alfredo Guerrero and Stefano Rigolin



UNIVERSITÀ
DEGLI STUDI
DI PADOVA



Motivation

$$\mathcal{L}_a = \underbrace{\frac{\partial_\mu a}{2f_a} \sum_{f \neq t} c_{aff} \bar{f} \gamma^\mu \gamma_5 f}_{\text{Shift-symmetric}} + \underbrace{c_{a\gamma\gamma} \frac{\alpha_{em}}{4\pi} \frac{a}{f_a} F_{\mu\nu} \tilde{F}^{\mu\nu} + c_{agg} \frac{\alpha_s}{4\pi} \frac{a}{f_a} G_{\mu\nu}^a \tilde{G}_a^{\mu\nu} + \frac{1}{2} m_a^2 a^2}_{\text{Symmetry breaking}}$$

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Quarkonia states

$$J/\Psi \rightarrow m_{J/\Psi} \sim 3 \text{ GeV}$$

$$\Upsilon(nS) \rightarrow m_\Upsilon \sim 10 \text{ GeV}$$

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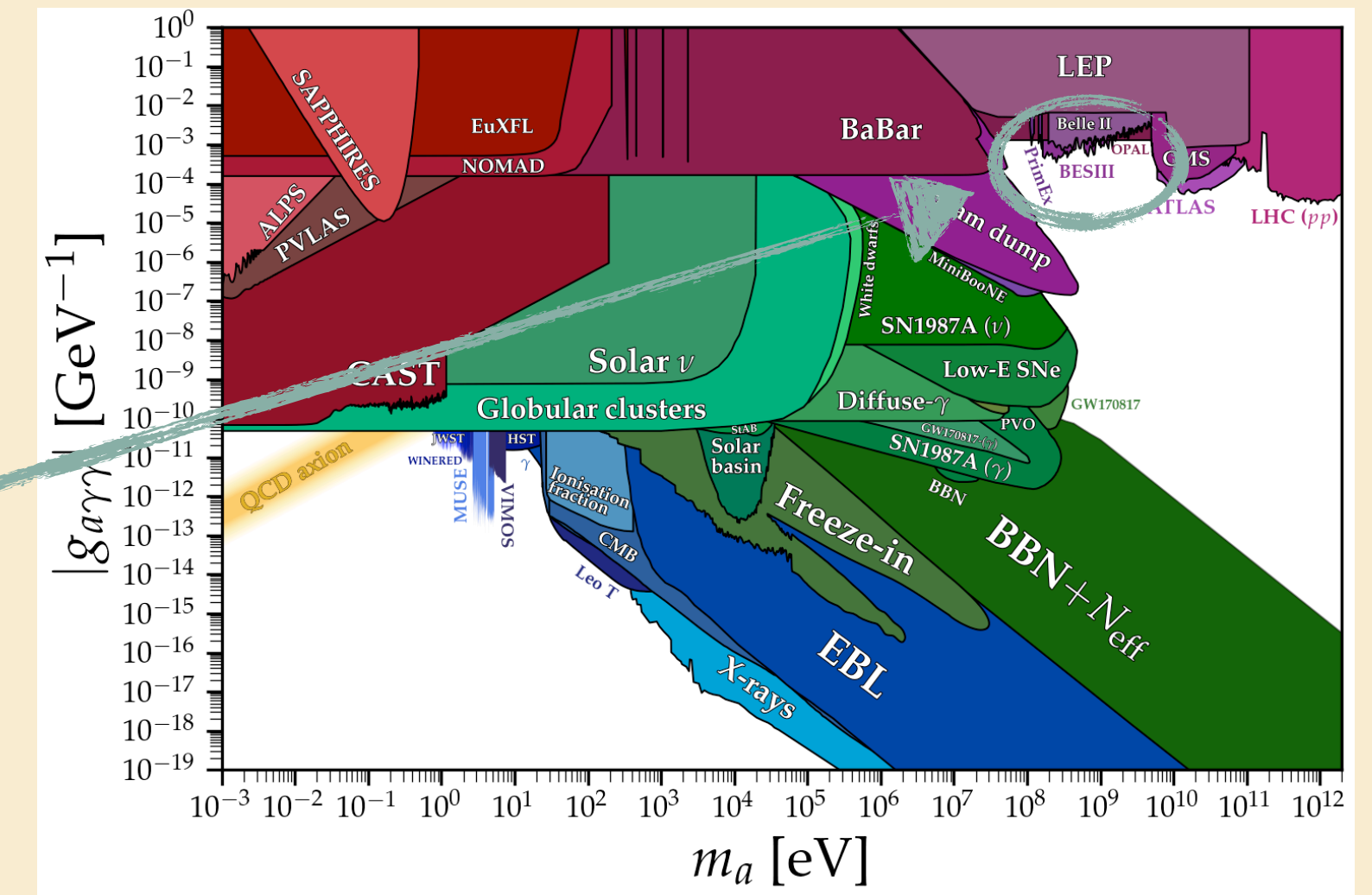
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$$J/\Psi(\Upsilon) \rightarrow a \gamma$$

$$m_a \in [100 \text{ MeV}, 10 \text{ GeV}]$$

Studied previously in [Pobbe, Merlo, Rigolin, Sumensari, JHEP 06 \(2019\) 091](#)



from [O'Hare](#)

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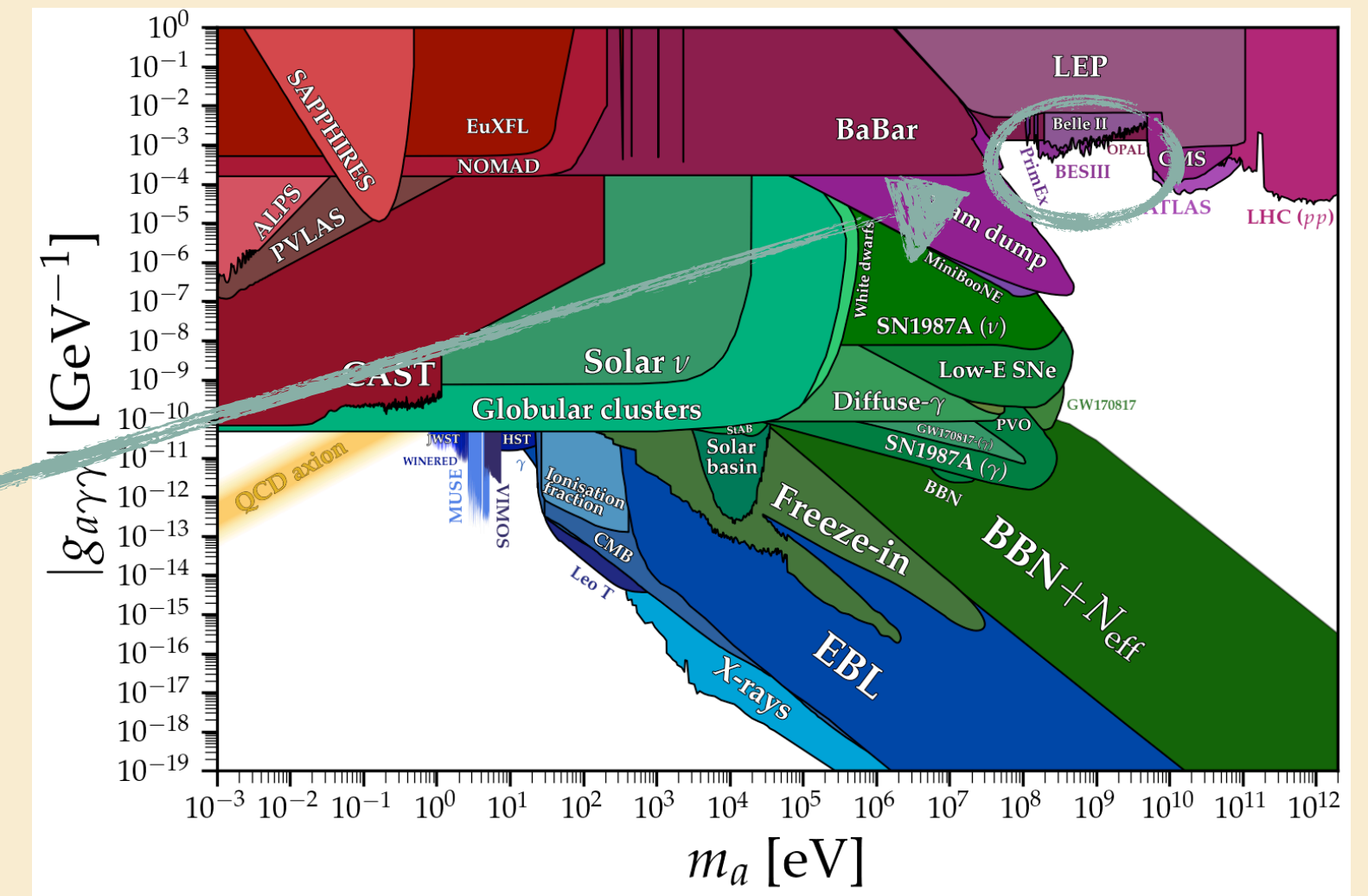
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New Experimental Results: Belle-II, BESIII

Invisible Searches

Exp.	Mass range [GeV]	Type of search	Resonance	ALP Decay
BaBar	0 – 7.8	Mixed	$\Upsilon(3S)$	Invisible
BaBar	0 – 9.2	Resonant	$\Upsilon(1S)$	Invisible
Belle	0 – 8.97	Resonant	$\Upsilon(1S)$	Invisible
Belle II	0.2 – 9.7	Non-resonant	$\Upsilon(4S)$	$\gamma\gamma$ (recast)
BESIII	0 – 1.2	Resonant	J/ψ	Invisible
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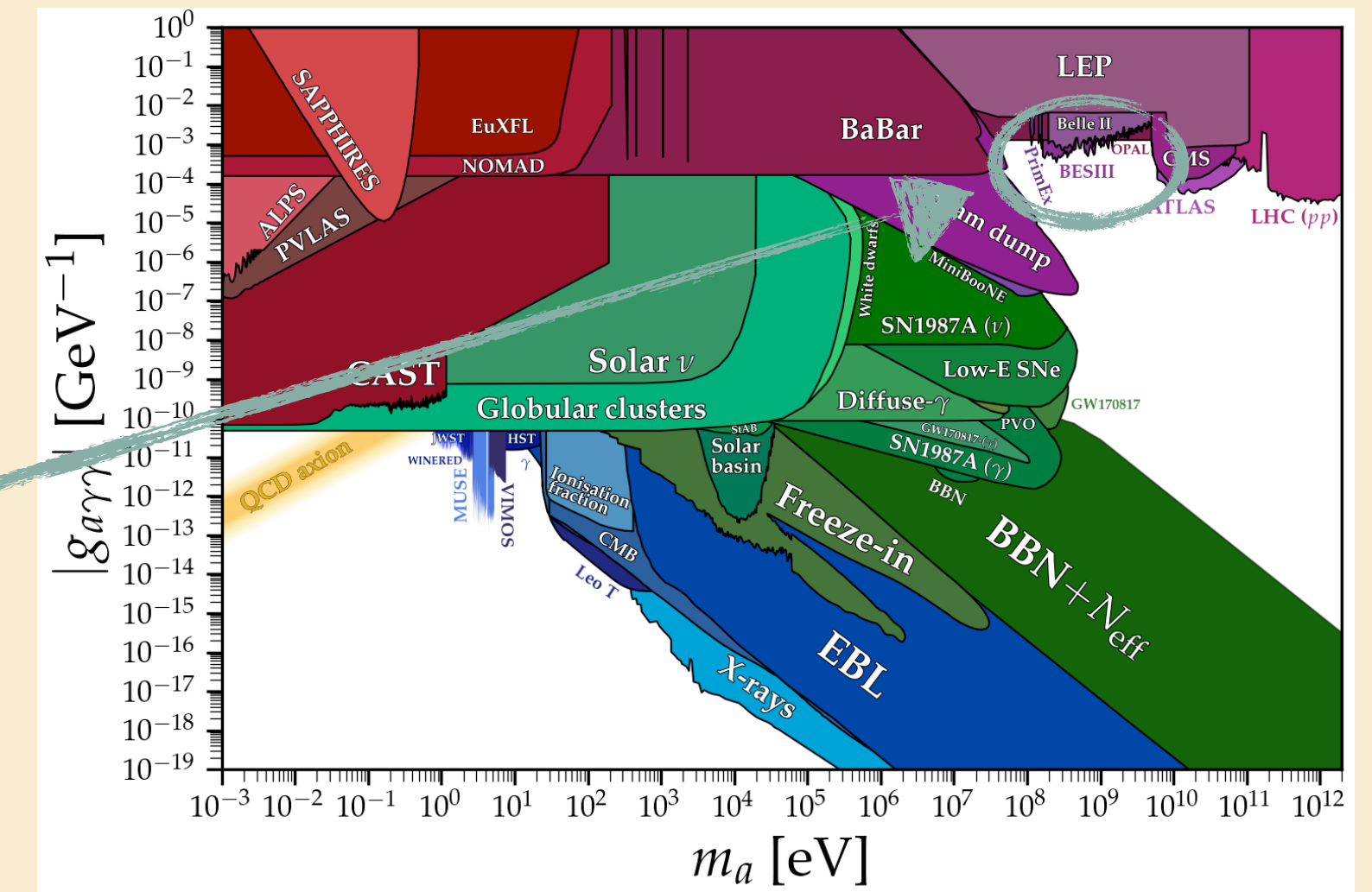
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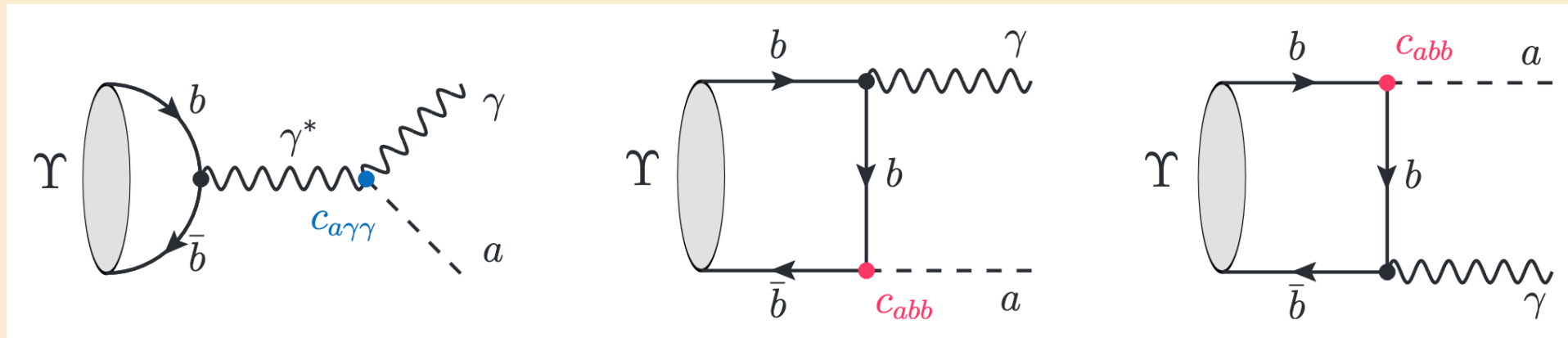
Include different visible channels from [O'Hare](#)

Visible Searches

Exp.	Mass range [GeV]	Type of search	Resonance	Decay
BaBar	0.3 – 7	Mixed	$\Upsilon(2S), \Upsilon(3S)$	Hadrons
BaBar	0.212 – 9.2	Resonant	$\Upsilon(1S)$	$\mu^+ \mu^-$
BaBar	4 – 9.25	Resonant	$\Upsilon(1S)$	$\bar{c}c$
Belle	$2m_\ell$ – 9.2	Resonant	$\Upsilon(1S)$	$\tau^+ \tau^-, \mu^+ \mu^-$
Belle II	0.2 – 9.7	Non-Resonant	$\Upsilon(4S)$	$\gamma\gamma$
BESIII	0.212 – 3	Mixed	J/ψ	$\mu^+ \mu^-$
BESIII	0.165 – 2.84	Resonant	J/ψ	$\gamma\gamma$

Production and decays

Resonant production

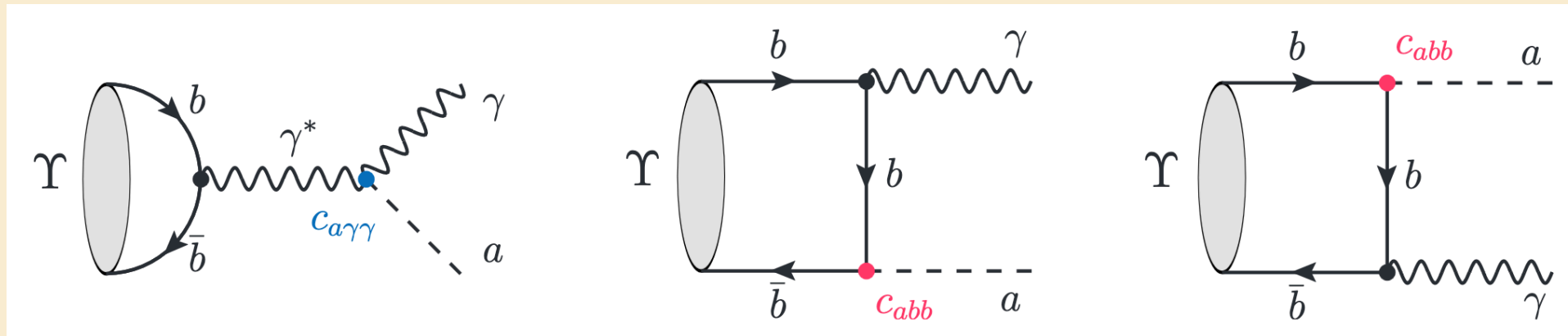


From [Pobbe, Merlo, Rigolin, Sumensari, JHEP 06 \(2019\) 091](#)

$$\mathcal{B}(V \rightarrow \gamma a) = \frac{\alpha_{\text{em}} Q_Q^2 m_V f_V^2}{24 \Gamma_V f_a^2} \left(1 - \frac{m_a^2}{m_V^2}\right) \left[c_{a\gamma\gamma} \frac{\alpha_{\text{em}}}{\pi} \left(1 - \frac{m_a^2}{m_V^2}\right) - 2 c_{aQQ} \right]^2$$

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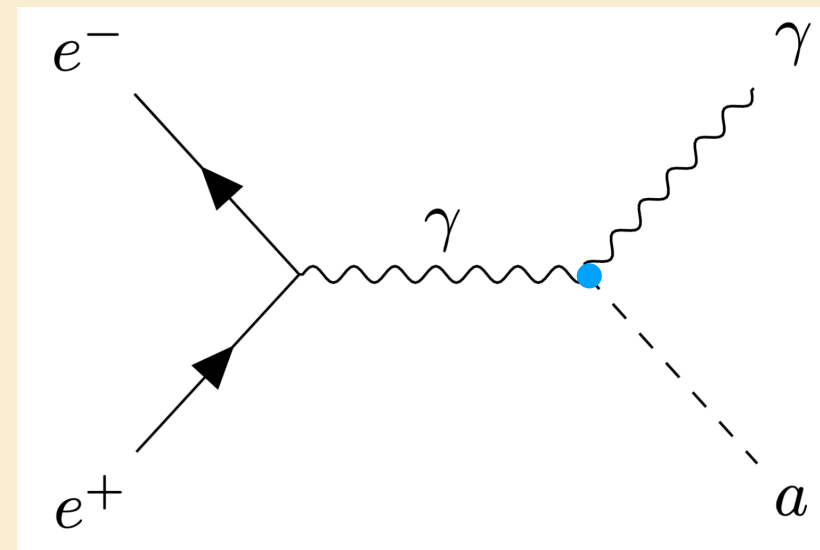


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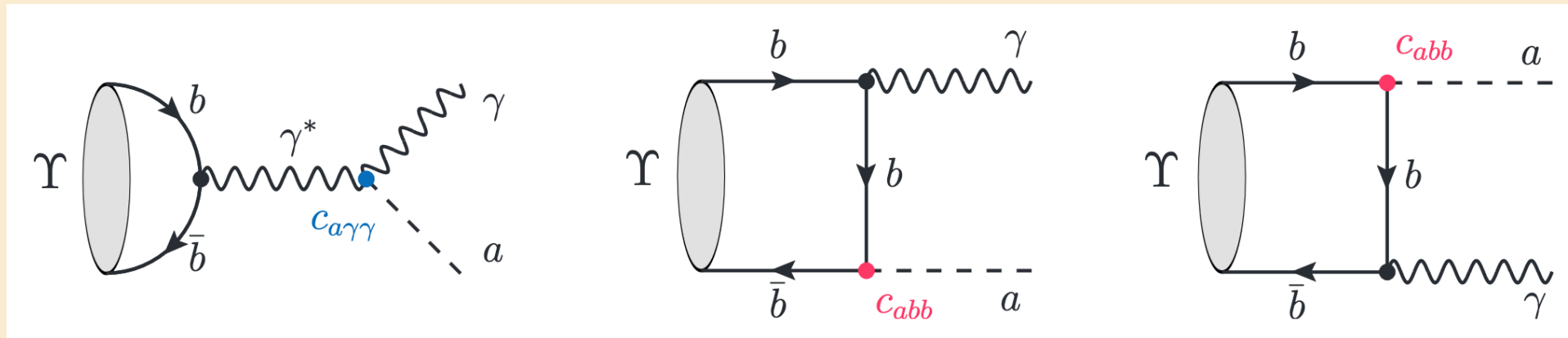
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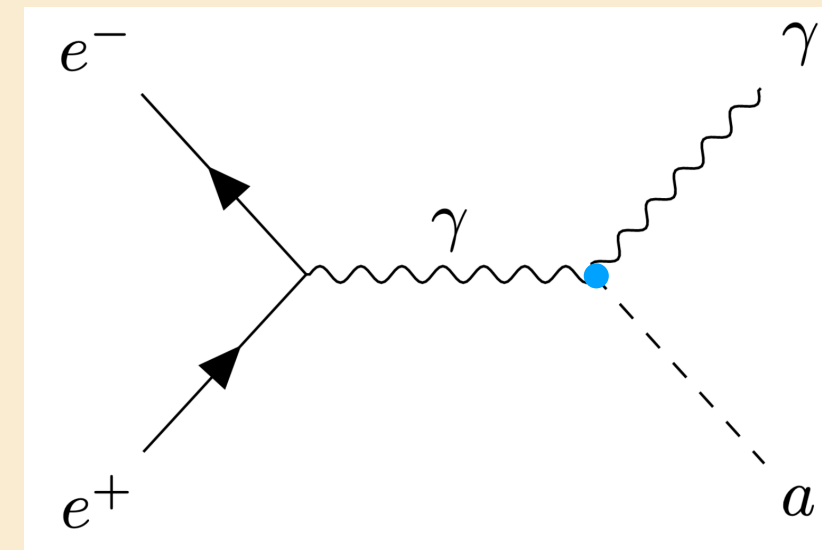


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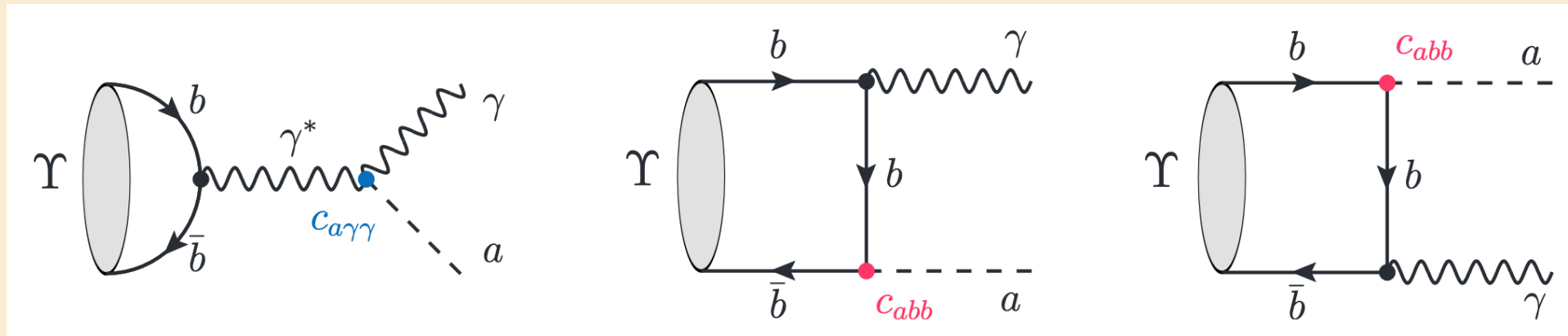


Mixed production

$$\langle \sigma_{\text{mix}}(s) \rangle \approx \sigma_{\text{NR}}(s) + \langle \sigma_{\text{R}}(s) \rangle_{\text{exp}}$$

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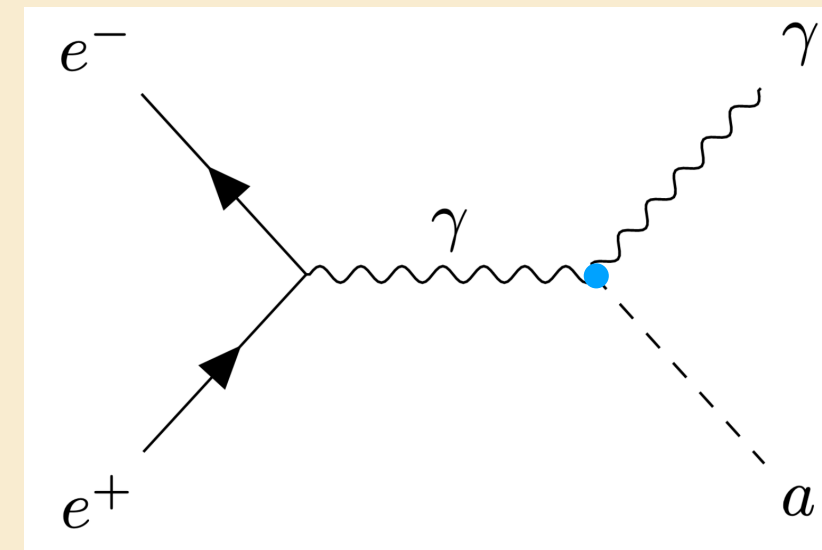


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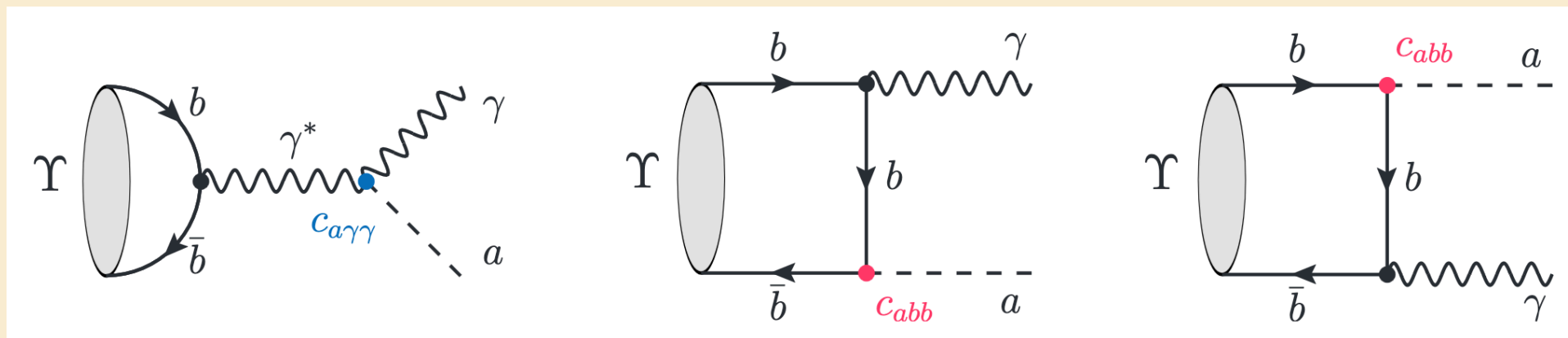
Invisible Channel

The ALP is long-lived/stable and it is detected as missing energy

$$J/\Psi \rightarrow \gamma + E_{\text{mis.}} \quad \Upsilon \rightarrow \gamma + E_{\text{mis.}}$$

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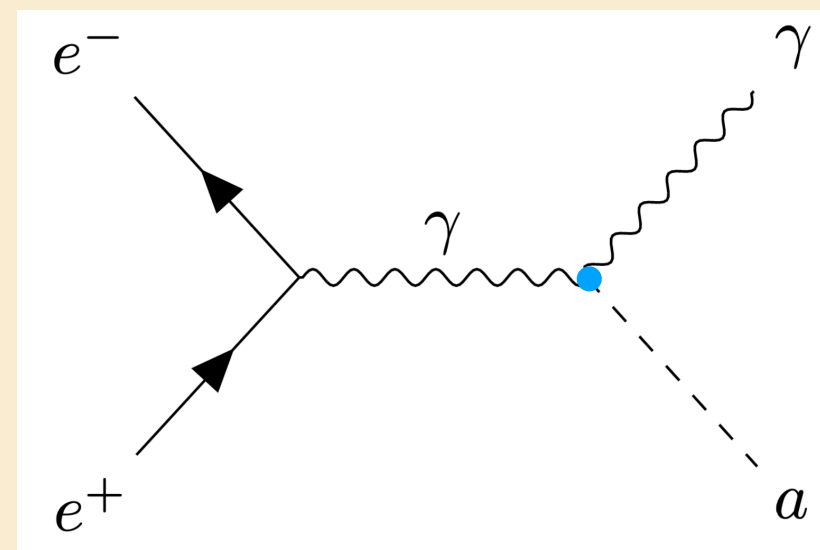


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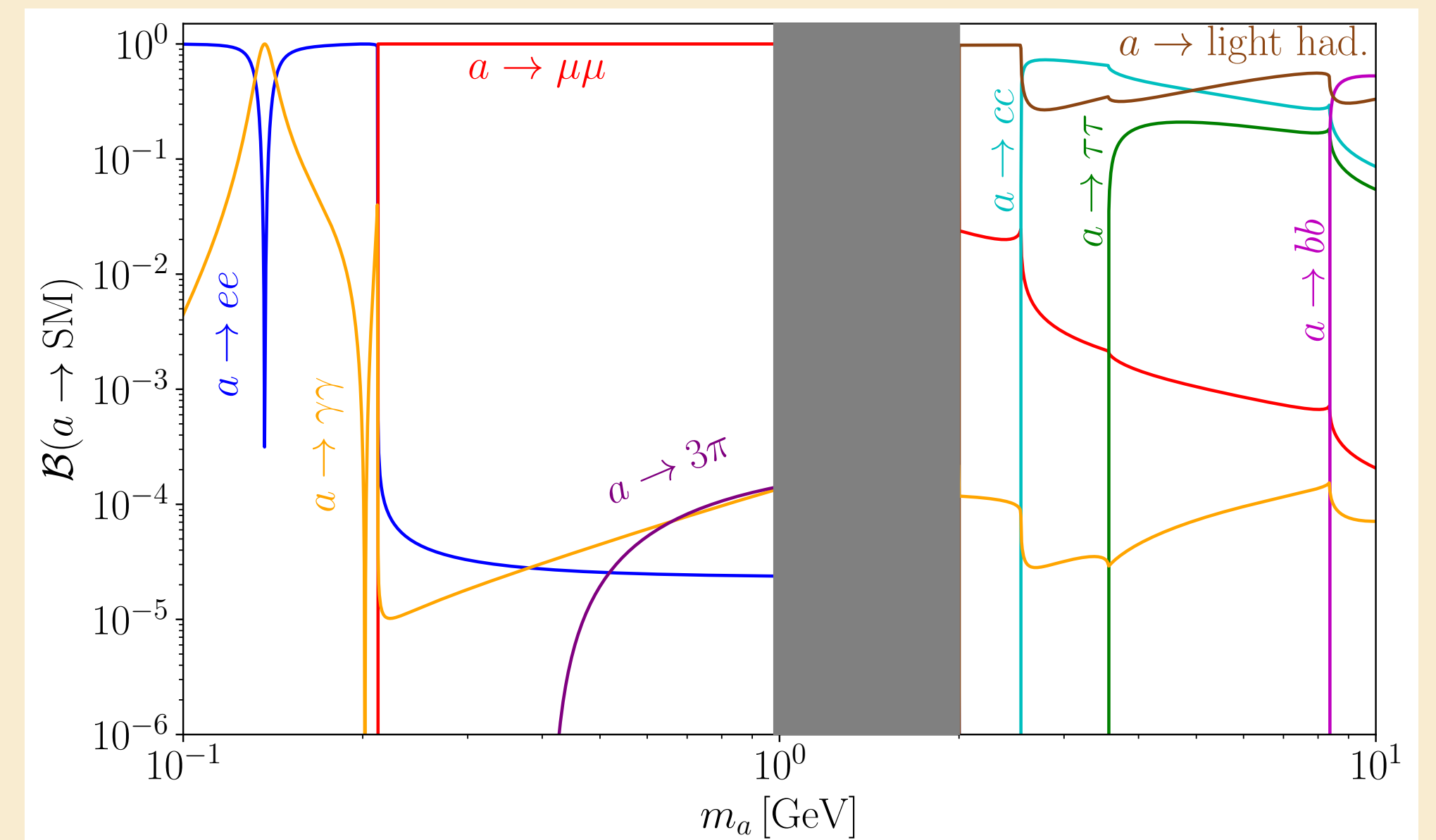
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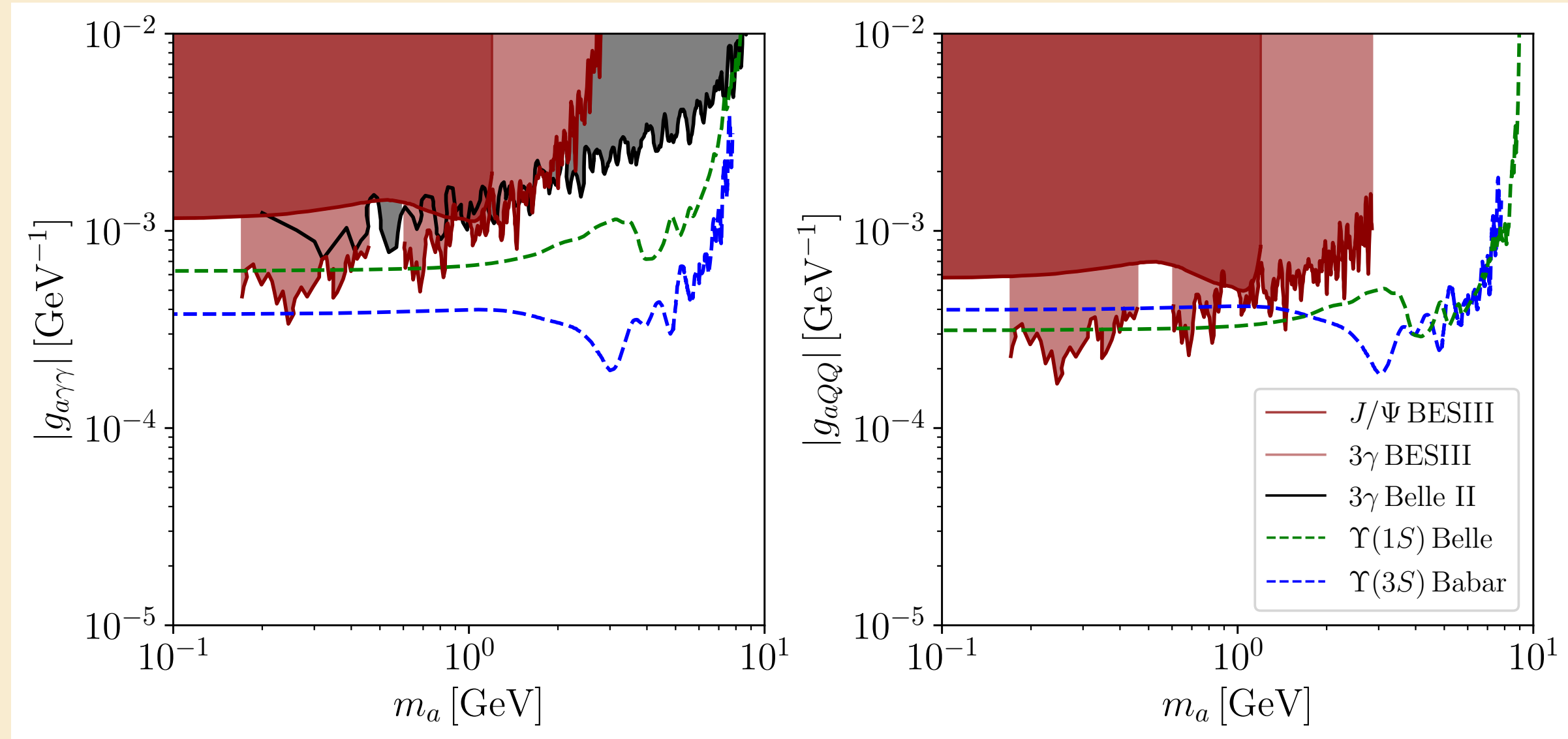


Invisible Searches

Using the following definitions:

$$g_{aff} = \frac{c_{aff}}{f_a}, \quad g_{a\gamma\gamma} = c_{a\gamma\gamma} \frac{\alpha_{em}}{\pi f_a}, \quad g_{agg} = c_{agg} \frac{\alpha_s}{\pi f_a}.$$

One Coupling

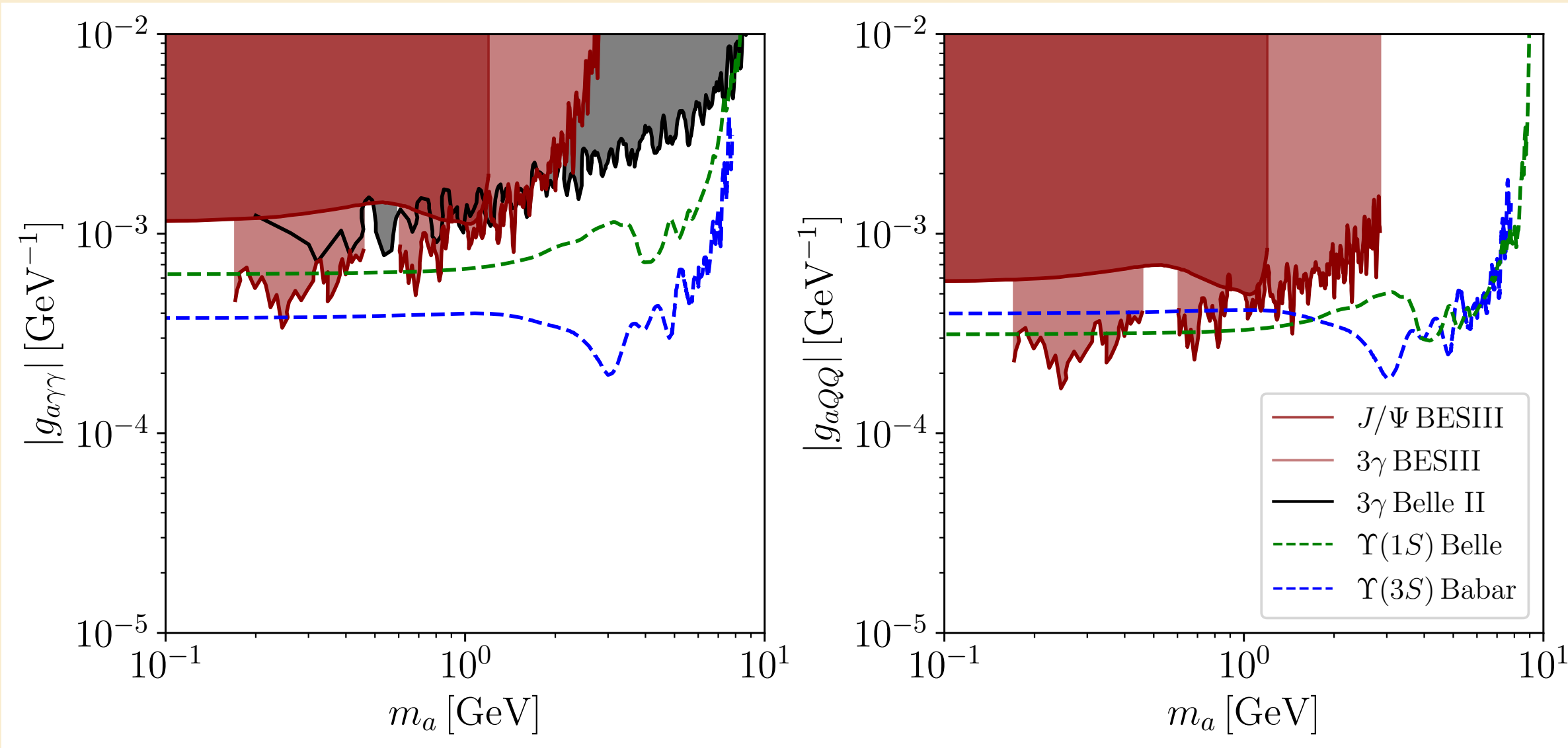


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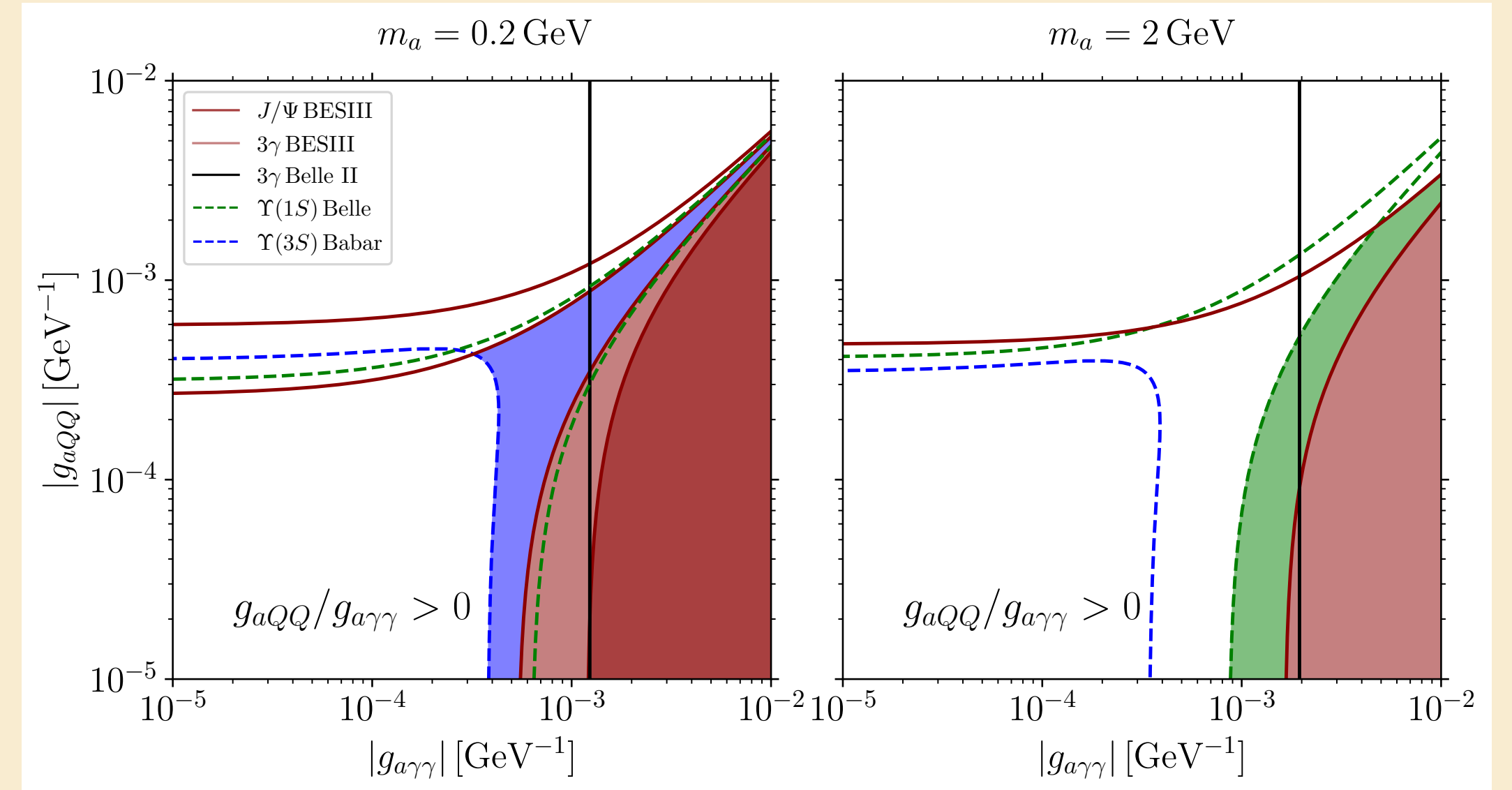
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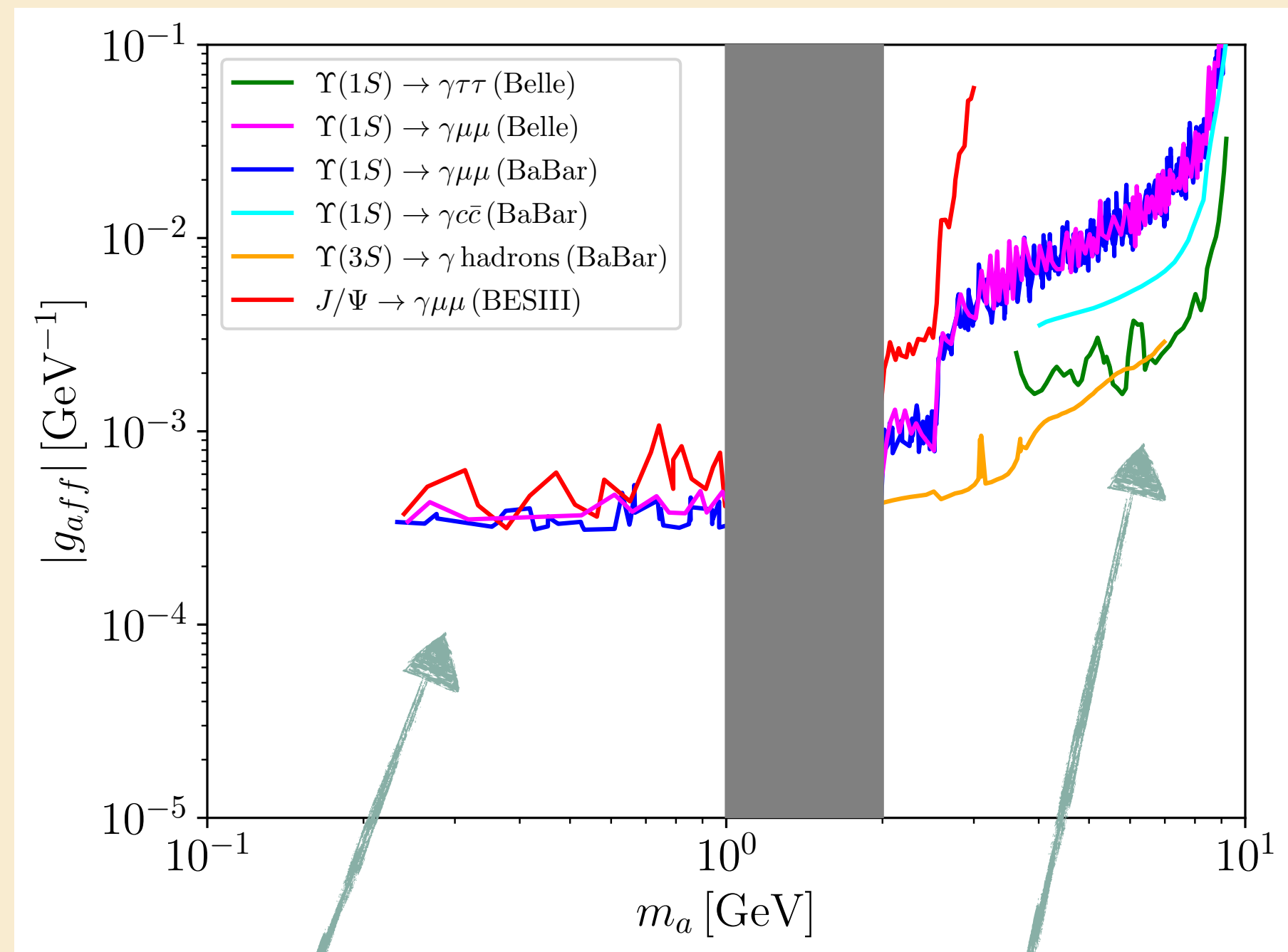
Two independent couplings



There may be cancellations in resonant production. Non-resonant or mixed searches needed to constrain the full parameter space.

Visible Searches

Universal fermion coupling

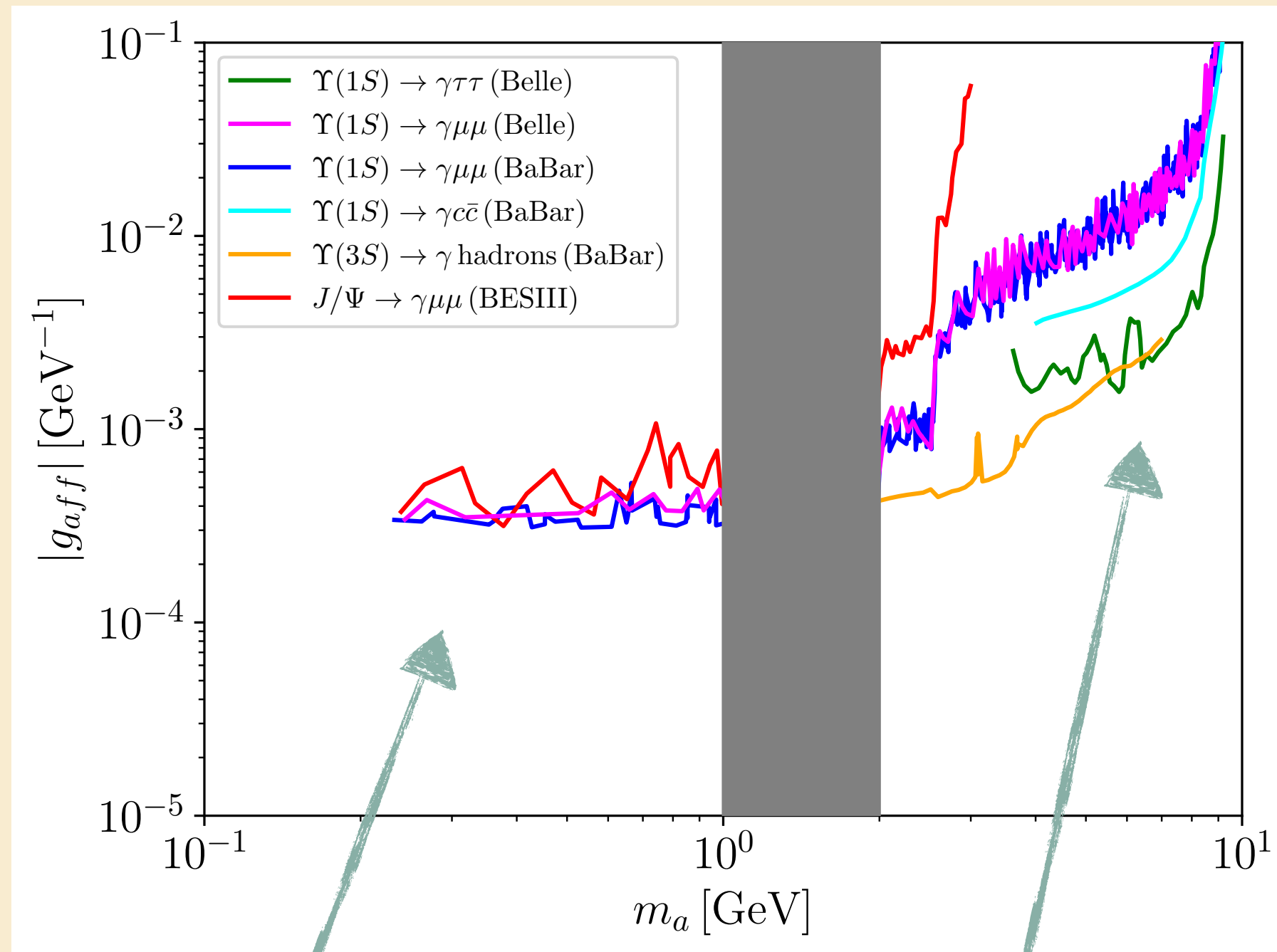


Muon decays set the best bound for lower masses.

Hadrons and tau channels best for larger masses.

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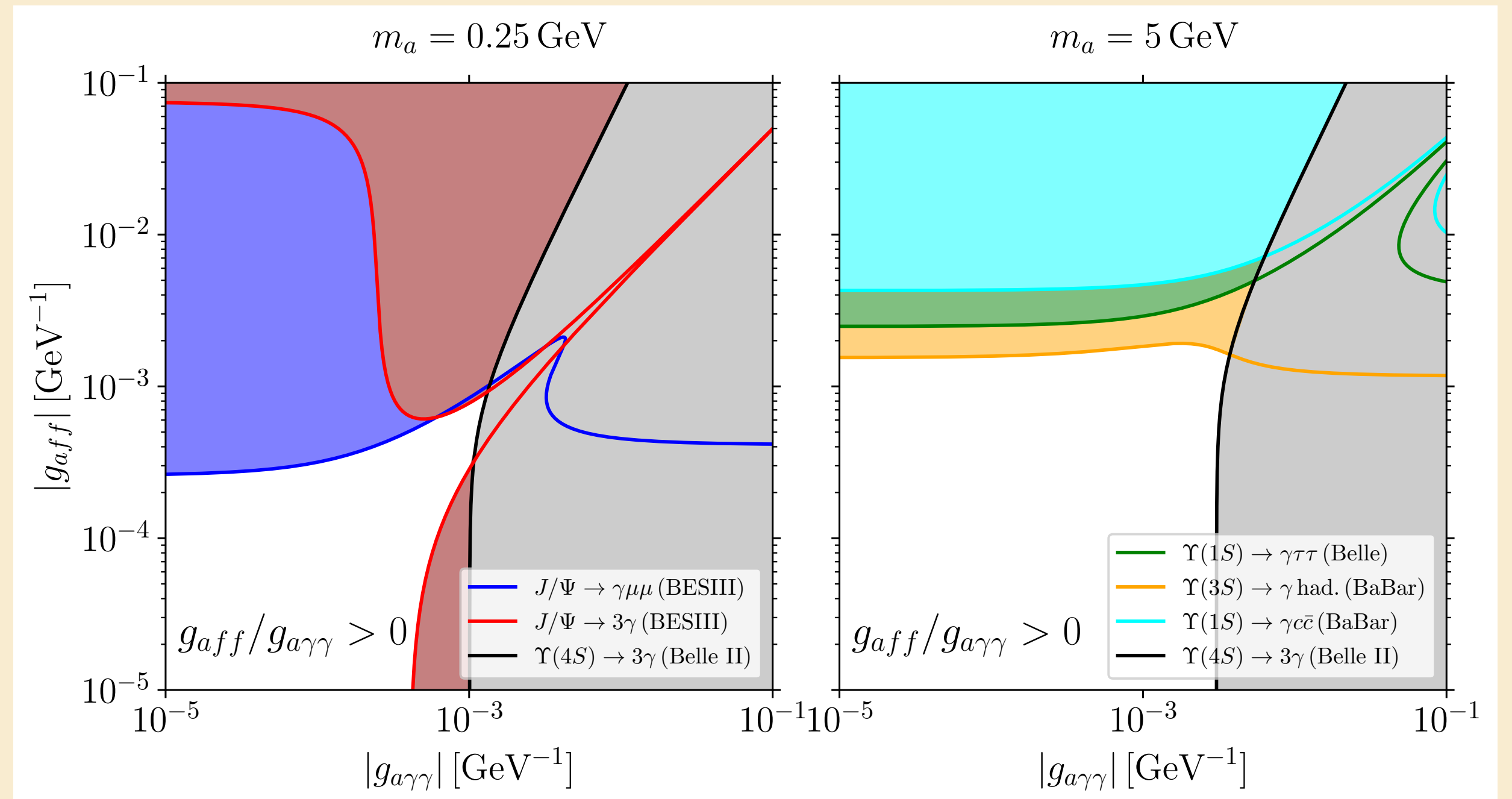
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Again, the combination of searches is important to constrain all parameter space!

Conclusions

- We have explored the ALP parameter space bounded by quarkonia radiative decays
 - Different production channels are necessary to constrain possible flat directions.
 - Invisible scenario $c_{a\gamma\gamma}, c_{aQQ} \lesssim \mathcal{O}(1) \times 10^{-4} \text{ GeV}^{-1}$
 - Visible scenario $\begin{cases} c_{a\mu\mu} \lesssim 3 \times 10^{-4} \text{ GeV}^{-1} \text{ for } m_a \lesssim 1 \text{ GeV} \\ c_{aff} \lesssim \mathcal{O}(1) \times 10^{-3} \text{ GeV}^{-1} \text{ for } m_a \gtrsim 2 \text{ GeV} \end{cases}$
 - If you are interested in more details come to the poster!

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Thanks for your attention!



This project has received funding from the European Union's [Horizon 2020](#) research and innovation programme under the [Marie Skłodowska-Curie](#) grant agreement [No 860881](#).

Production Details

Resonant production

$$\sigma_{\text{R}}(s) = \sigma_{\text{peak}} \frac{m_V^2 \Gamma_V^2}{(s - m_V^2)^2 + m_V^2 \Gamma_V^2} \mathcal{B}(V \rightarrow \gamma a)$$

$$\sigma_{\text{peak}} = \frac{12\pi \mathcal{B}(V \rightarrow e^+ e^-)}{m_V^2}$$

When producing the resonance there is an uncertainty in the beam energy

$$\sigma_W \approx 2 - 5 \text{ MeV}$$

$$\langle \sigma_{\text{R}}(s) \rangle_{\text{exp}} = \frac{1}{\sqrt{2\pi}} \int dq \frac{\sigma_{\text{R}}(q^2)}{\sigma_W} \exp \left[-\frac{(q - \sqrt{s})^2}{2\sigma_W^2} \right]$$

$V(nS)$	m_V [GeV]	Γ_V [keV]	σ_{peak} [nb]	ρ	$\langle \sigma_{\text{R}} \rangle_{\text{exp}} / \sigma_{\text{NR}} _{s=m_V^2}$
$J/\Psi(1S)$	3.096	92.6	$91.2(5) \times 10^3$	31×10^{-3}	0.92(1)
$\Upsilon(1S)$	9.460	54.02	$3.9(2) \times 10^3$	6.1×10^{-3}	0.53(5)
$\Upsilon(2S)$	10.023	31.98	$2.8(2) \times 10^3$	3.7×10^{-3}	0.21(3)
$\Upsilon(3S)$	10.355	20.32	$3.0(3) \times 10^3$	2.3×10^{-3}	0.16(3)
$\Upsilon(4S)$	10.580	20.5×10^3	2.1(1)	0.83	$3.0(3) \times 10^{-5}$

Details on ALP Decays

Decays

$$\Gamma(a \rightarrow \text{SM}) = \frac{\alpha_{\text{em}}^2}{64\pi^3 f_a^2} |c_{a\gamma\gamma}^{\text{eff}}|^2 m_a^3 + \sum_f \frac{N_c^f |c_{aff}|^2}{8\pi f_a^2} m_a m_f^2 \sqrt{1 - \frac{4m_f^2}{m_a^2}} \Theta(m_a - 2m_f) + \Gamma_{a \rightarrow \text{lh}},$$

Photons

Leptons and heavy quarks

Light Hadrons

Light Hadrons

$$\Gamma_{a \rightarrow \text{lh}} = \begin{cases} \frac{m_a m_\pi^4}{6144\pi^3 f_\pi^2 f_a^2} |c_{a\pi}|^2 \left(g_{00} \left(\frac{m_\pi^2}{m_a^2} \right) + g_{+-} \left(\frac{m_\pi^2}{m_a^2} \right) \right) & m_a \lesssim 1 \text{ GeV}, \\ \frac{\alpha_s^2}{8\pi^3 f_a^2} |c_{agg}^{\text{eff}}|^2 m_a^3 \left(1 + \frac{\alpha_s}{4\pi} \frac{291 - 14n_q}{12} \right) & m_a \gtrsim 2 \text{ GeV}, \end{cases} \quad c_{a\pi} = - \left(2c_{agg} \frac{m_d - m_u}{m_d + m_u} + c_{auu} - c_{add} \right),$$

$$c_{agg}^{\text{eff}} = c_{agg} + \frac{1}{2} \sum_{q \neq t} c_{aqq} B_1 \left(\frac{4m_q^2}{m_a^2} \right)$$

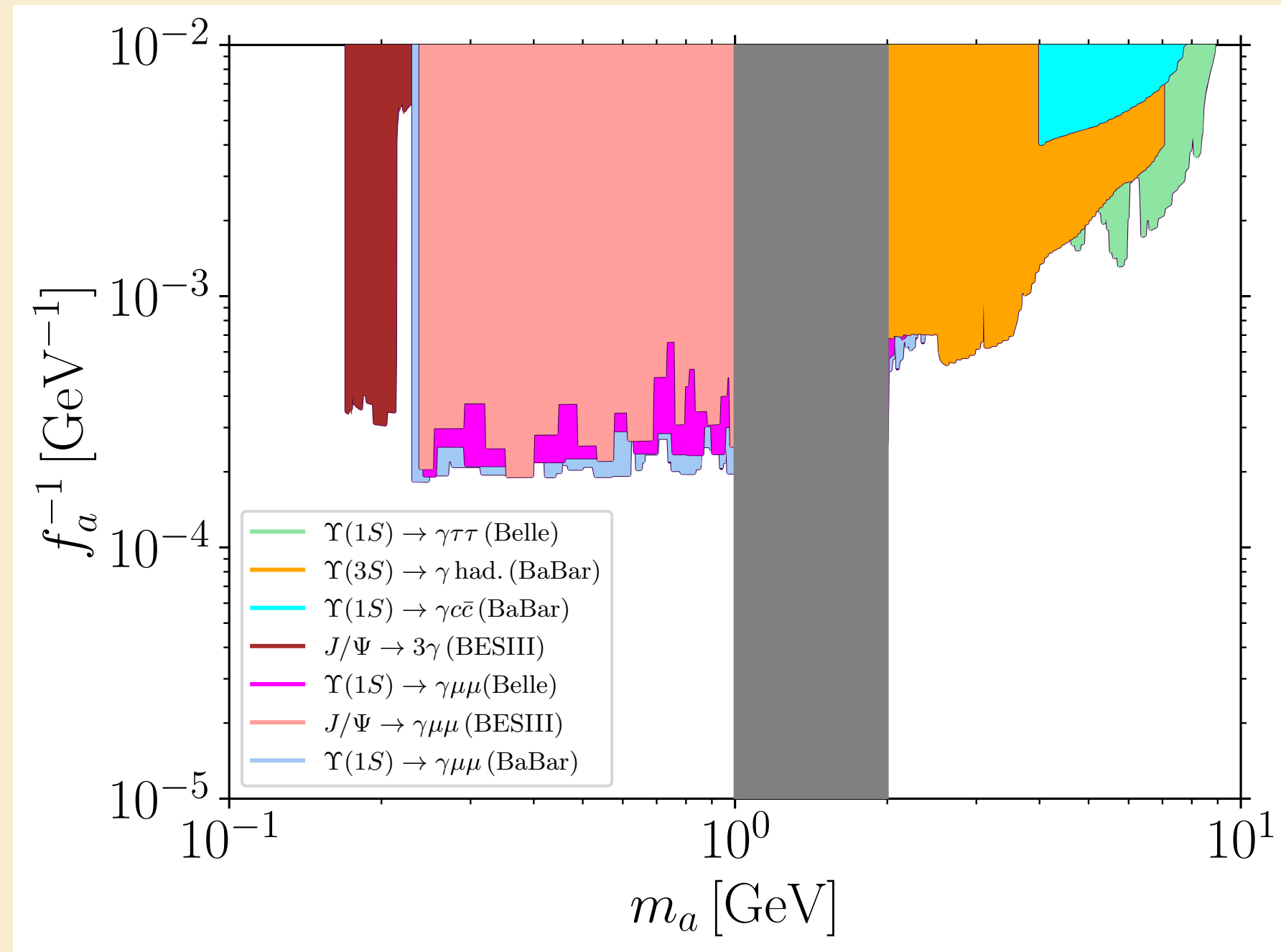
Photon Coupling

$$c_{a\gamma\gamma}^{\text{eff}} = \begin{cases} c_{a\gamma\gamma} - 1.92 c_{agg} + \frac{f_a}{f_\pi} U_{a\pi} + \sum_{f=l,c,b} N_c^f Q_f^2 c_{aff} B_1(\tau_f) & , \\ c_{a\gamma\gamma} + \sum_{f \neq t} N_c^f Q_f^2 c_{aff} B_1(\tau_f) & \end{cases} \quad \tau_f = \frac{4m_f^2}{m_a^2}$$

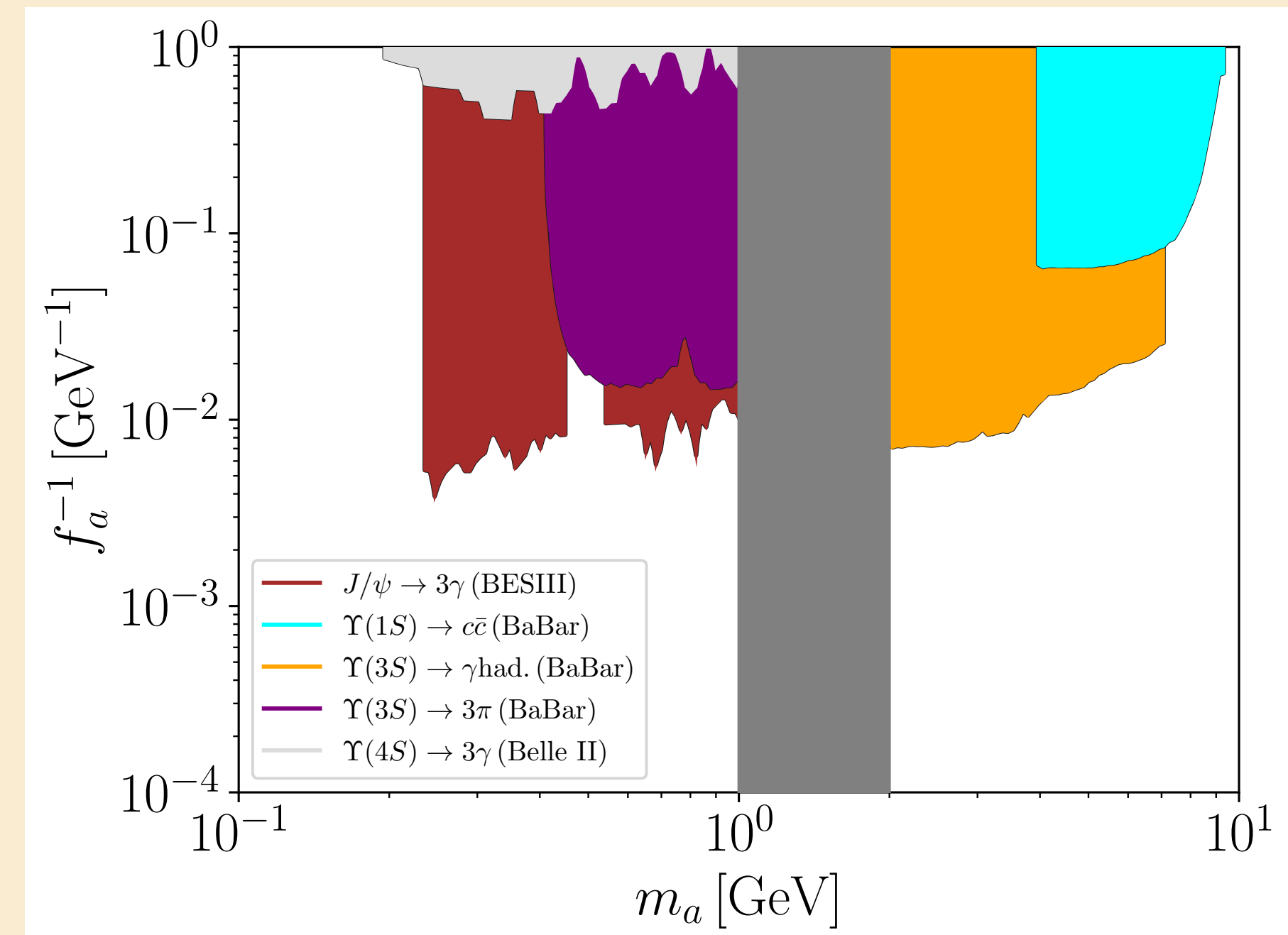
$$B_1(\tau) = 1 - \tau f(\tau)^2 \quad \text{with} \quad f(\tau) = \begin{cases} \arcsin\left(\frac{1}{\sqrt{\tau}}\right) & \tau \geq 1, \\ \frac{\pi}{2} + \frac{i}{2} \log\left(\frac{1 + \sqrt{1-\tau}}{1 - \sqrt{1-\tau}}\right) & \tau < 1, \end{cases}$$

Benchmark Models

DFSZ-like ALP



KSVZ-like ALP



DFSZ-like: $c_{auu} = -c_{add} = -2s_\beta^2$, $c_{aee} = -2c_\beta^2$, $c_{a\gamma\gamma} = 6$, $c_{agg} = 0$,

KSVZ: $c_{auu} = c_{add} = c_{aee} = 0$, $c_{a\gamma\gamma} = 0$, $c_{agg} = 1/2$.