

Species Cosmology

Marco Scalisi

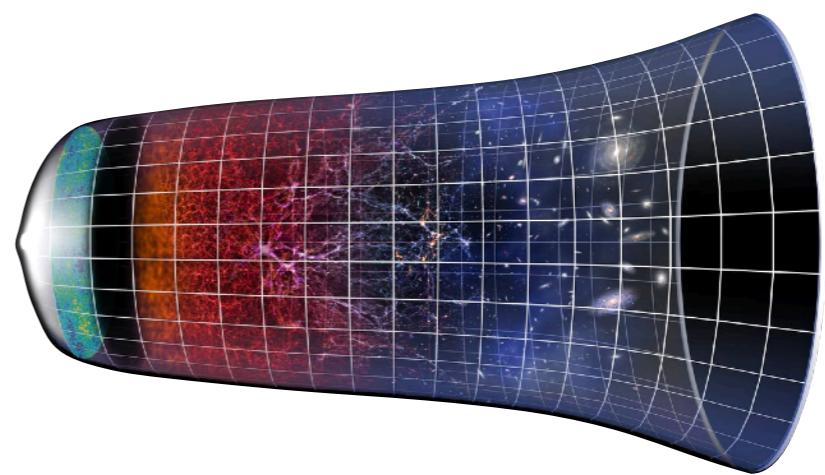
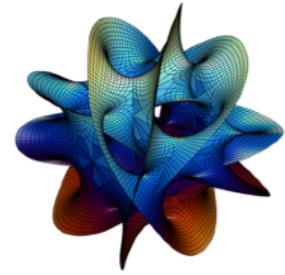
September 24th, 2024
TFI 2024, Napoli

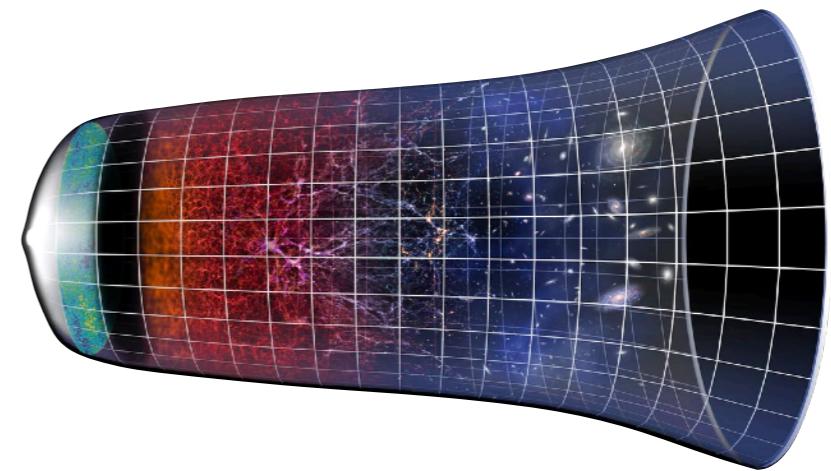
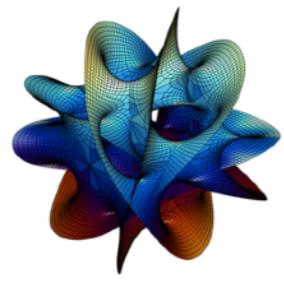
based on
2312.13210 Lüst, Masias, Muntz, MS
2401.09533 MS
2406.17851 Herraez, Lüst, Masias, MS
work in progress Lüst, Masias, Pieroni, MS

MAX-PLANCK-INSTITUT
FÜR PHYSIK



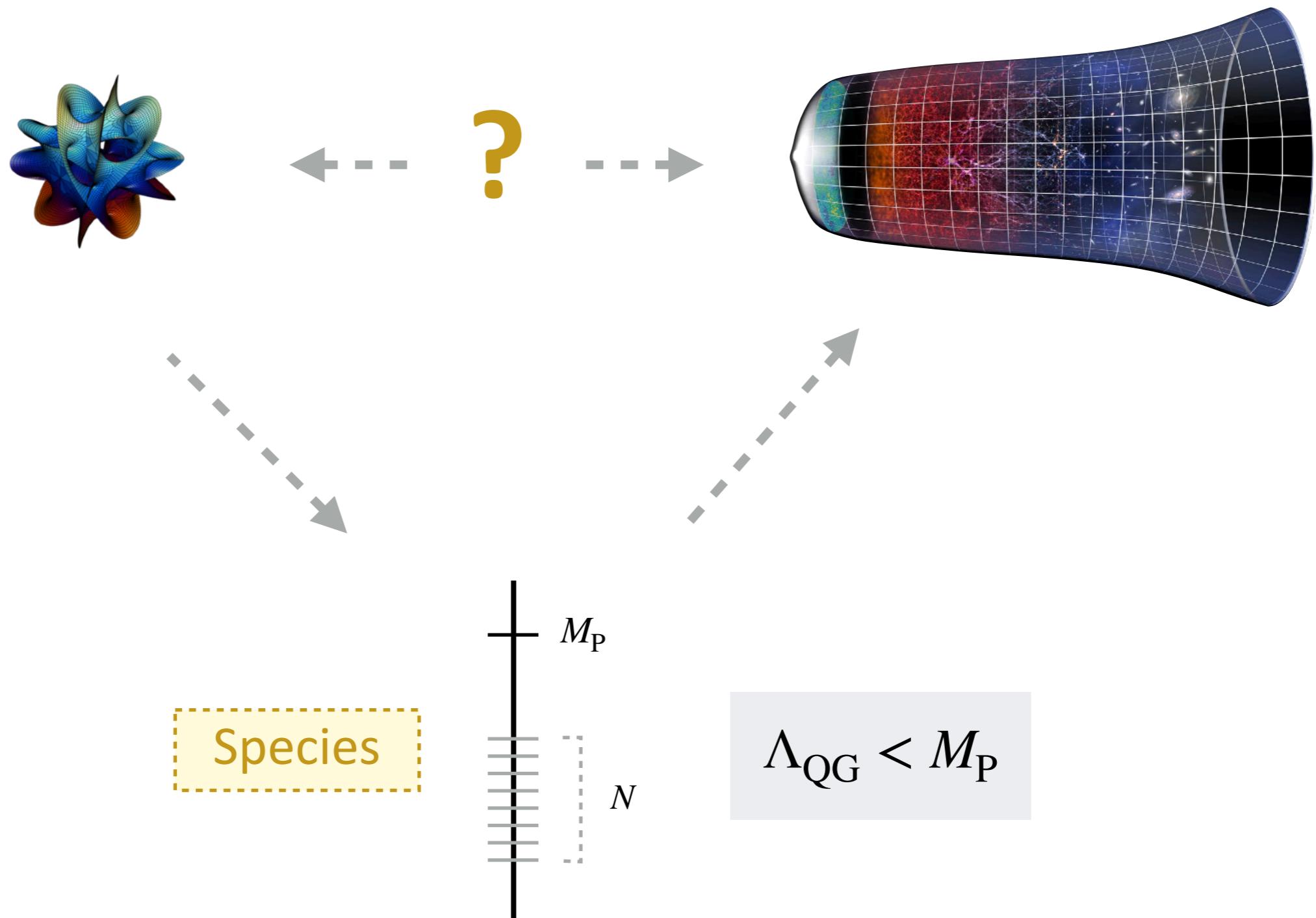
UNIVERSITÀ
degli STUDI
di CATANIA

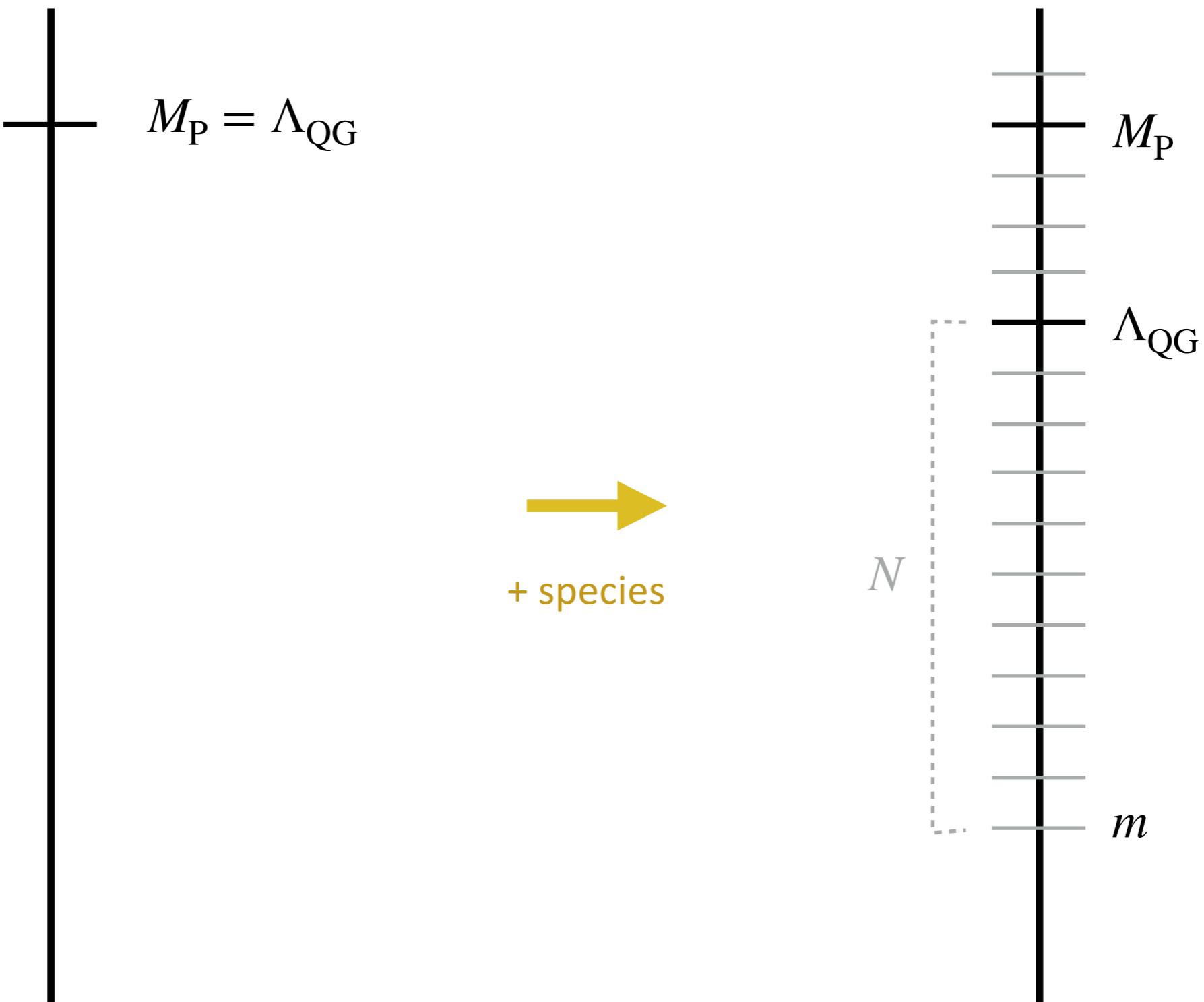




M_P

$H \lesssim 10^{-5} M_P$





OUTLINE

The Species Scale

Species → Cosmology

Species ← Cosmology

Species and R^2 - Inflation



The Species Scale

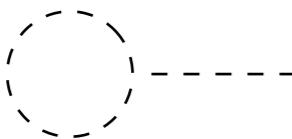
Species scale

Dvali, 2007

Dvali, Redi 2007

Perturbative argument

N light species weakly coupled to gravity



A dashed circle representing a loop, with a horizontal dash-dot line extending from its left side.

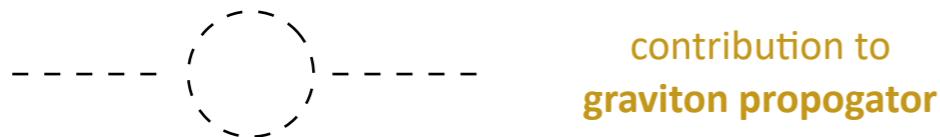
contribution to
graviton propagator

$$\pi^{-1}(p^2) = p^2 \left[1 - \frac{N p^2}{120\pi M_P^2} \log\left(-\frac{p^2}{\mu^2}\right) \right]$$

↑
tree level ↑
 1-loop

Perturbative argument

N light species weakly coupled to gravity



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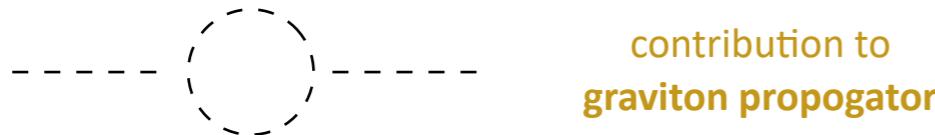
↑ ↑
tree level 1-loop

perturbation theory breaks down when
tree level = 1-loop

$$p \sim \frac{M_P}{\sqrt{N}} \equiv \Lambda_s$$

Perturbative argument

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Non-perturbative argument

Black hole with N species

What is its **minimal radius**?

Perturbative argument

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What is its **minimal radius**?

$$R_{\text{BH}} \simeq \frac{1}{M_P}$$

corresponds to

$$S_{\text{BH}} \simeq R_{\text{BH}}^{d-2} M_P^{d-2} = 1$$



Perturbative argument

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Conundrum resolved if

$$R_{\min} \simeq N^{\frac{1}{d-2}} M_P^{-1} = \Lambda_s^{-1}$$

$$\Lambda_s = \begin{array}{l} \text{- scale at which gravity becomes strongly coupled} \\ \text{- scale of the minimal size of BH} \\ \text{- scale of higher curvature corrections} \end{array} = \Lambda_{QG}$$

$$\Lambda_{QG} = \frac{M_P}{N_s^{\frac{1}{d-2}}}$$

(renormalization of the Planck mass)

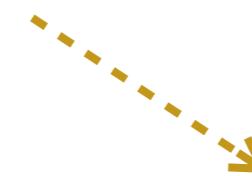
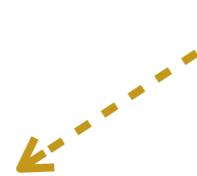
Species scale

Dvali, 2007

Dvali, Redi 2007

- $$\Lambda_s = \begin{array}{l} \text{- scale at which gravity becomes strongly coupled} \\ \text{- scale of the minimal size of BH} \\ \text{- scale of higher curvature corrections} \end{array} = \Lambda_{QG}$$

$$\Lambda_{QG} = \frac{M_P}{N_s^{\frac{1}{d-2}}}$$



in string theory

Kaluza-Klein modes

String oscillator modes

Lee, Lerche, Weigand 2019

At this scale

EFT has **holographic properties**

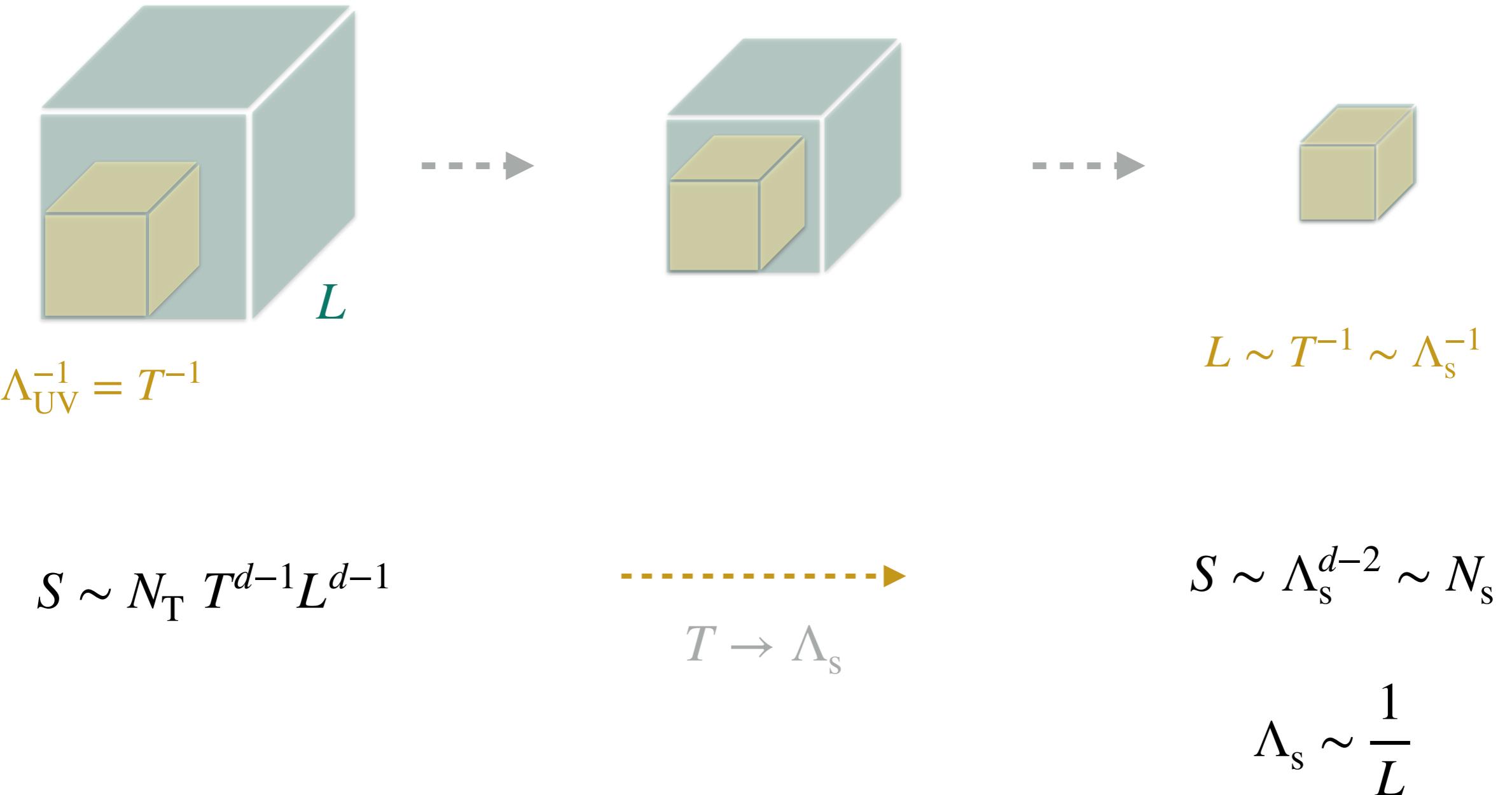
$$S \sim \Lambda_{QG}^{-(d-2)}$$

Cribiori, Lüst, Montella 2023

Herraez, Lüst, Masiás, MS - 2406.17851

Species thermodynamics and its origin

Herraez, Lust, Masias, MS - 2406.17851



Swampland Distance Conjecture

“Infinite scalar field variations Δ are always associated to
(at least) an infinite tower of states becoming exponentially light”

$$m = m_0 e^{-\gamma \Delta} \quad \Delta \rightarrow \infty$$

Swampland Distance Conjecture

“Infinite scalar field variations Δ are always associated to
(at least) an infinite tower of states becoming exponentially light”

$$m = m_0 e^{-\gamma \Delta} \quad \Delta \rightarrow \infty$$



exponential drop-off of the QG cut-off

$$\Lambda_{\text{QG}} = \Lambda_0 e^{-\lambda \Delta}$$

$\Lambda_0 \leq M_P$
original naive cut-off

Species and the Swampland

$$\frac{1}{\sqrt{(d-1)(d-2)}} \leq \lambda = \left| \frac{\Lambda'_{\text{QG}}}{\Lambda_{\text{QG}}} \right| \leq \frac{1}{\sqrt{d-2}}$$

van de Heisteeg, Vafa, Wiesner, Wu 2023

Calderón-Infante, Castellano, Herráez, Ibáñez 2023

van de Heisteeg, Vafa, Wiesner, 2023

van de Heisteeg, Vafa, Wiesner, Wu 2023

Lüst, Masias, Muntz, MS 2023

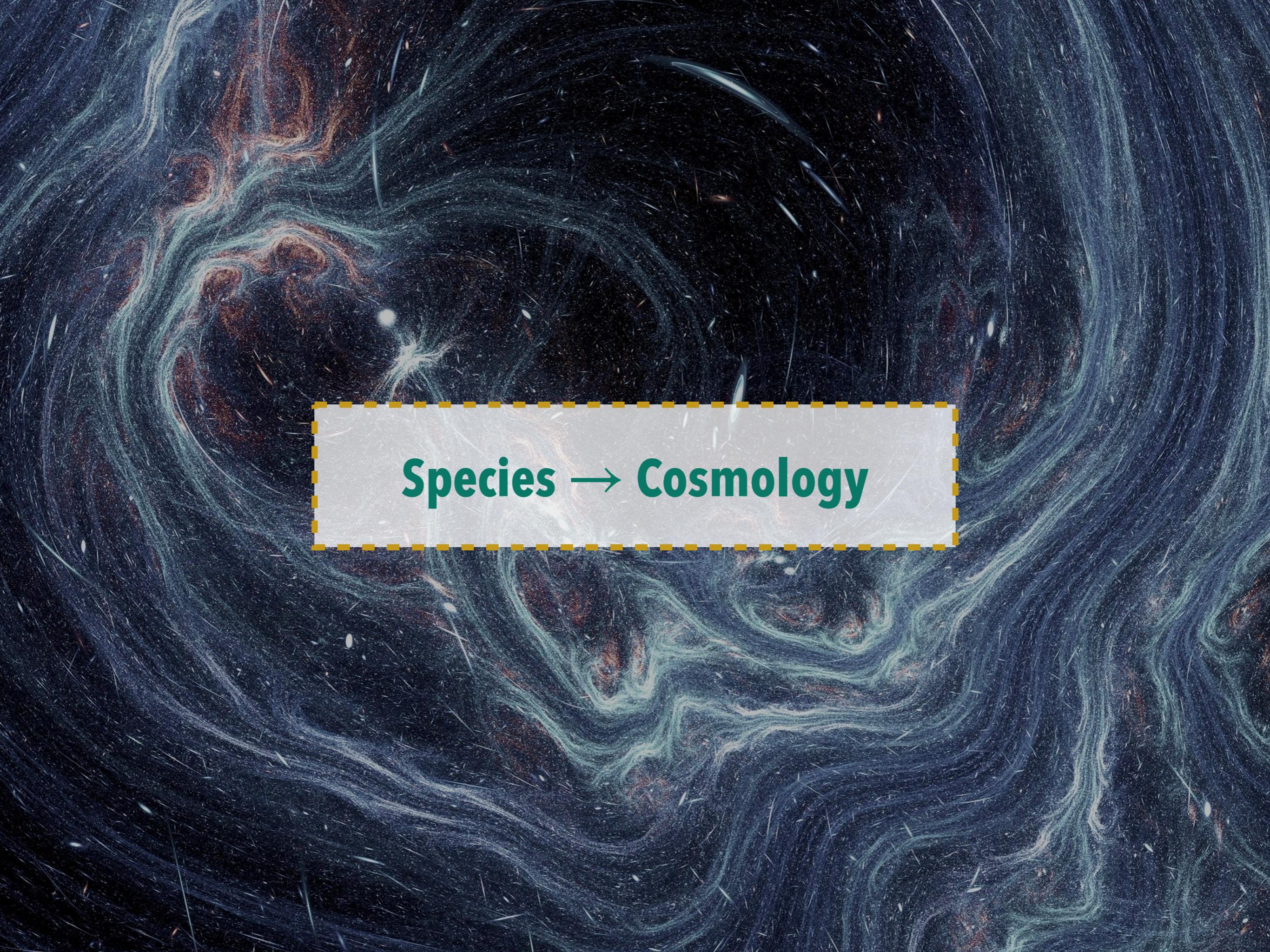
Main message

- ▶ **Towers of states lead to a renormalization of the quantum gravity cut-off**

$$\Lambda_{\text{QG}} = \frac{M_{\text{P}}}{N^{\frac{1}{d-2}}} < M_{\text{P}}$$

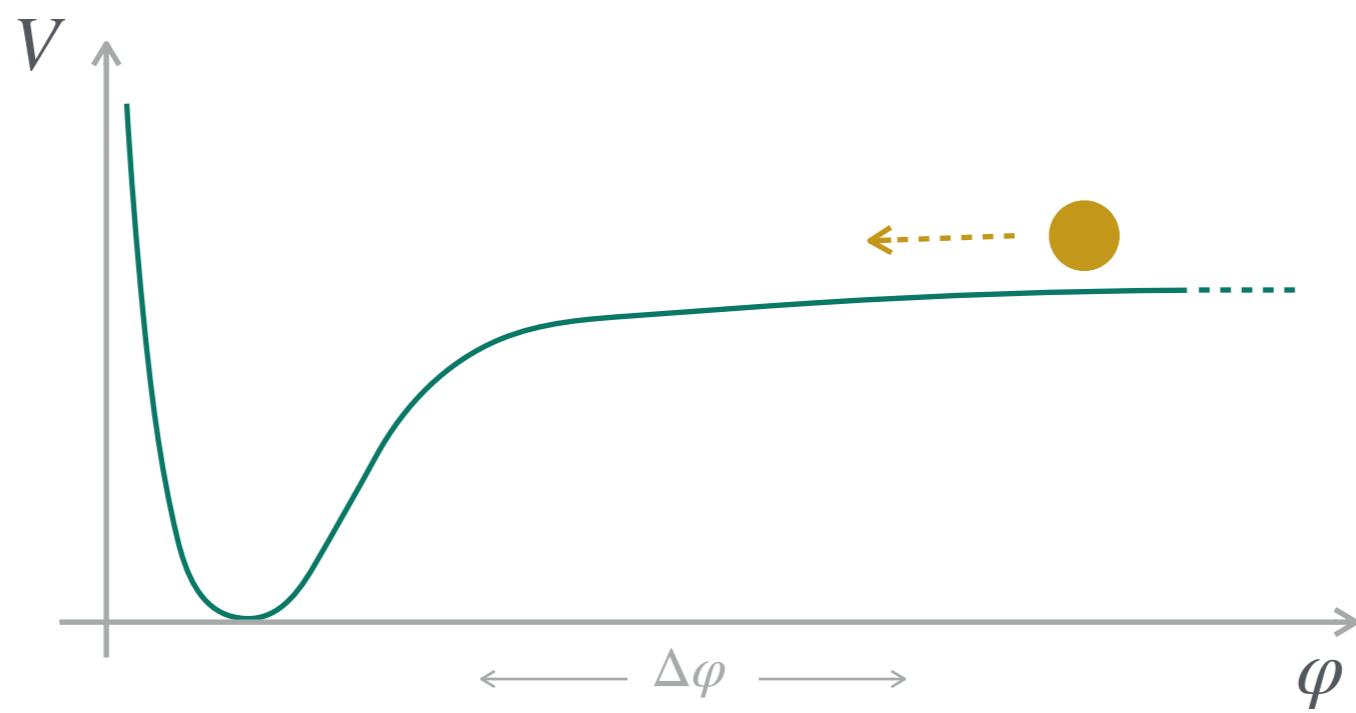
- ▶ **Distance conjecture implies exponential drop-off in field space of Λ_{QG}**

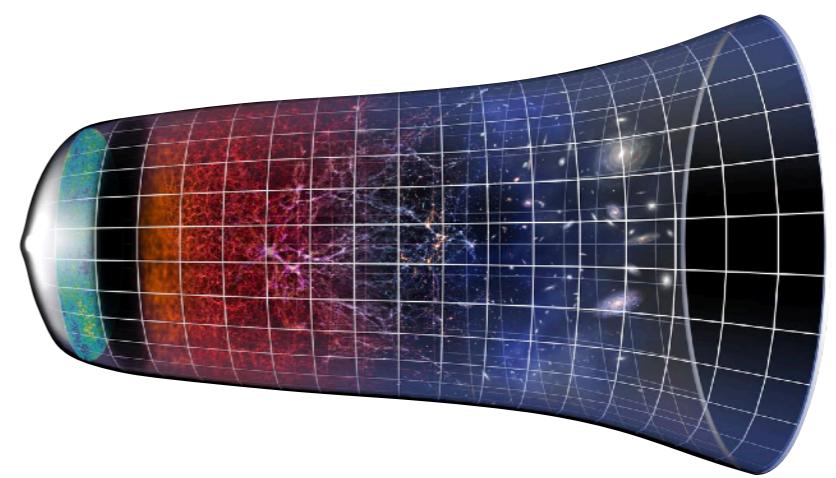
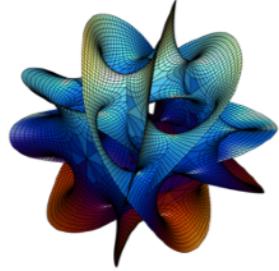
$$\Lambda_{\text{QG}} \sim e^{-\lambda \Delta}$$

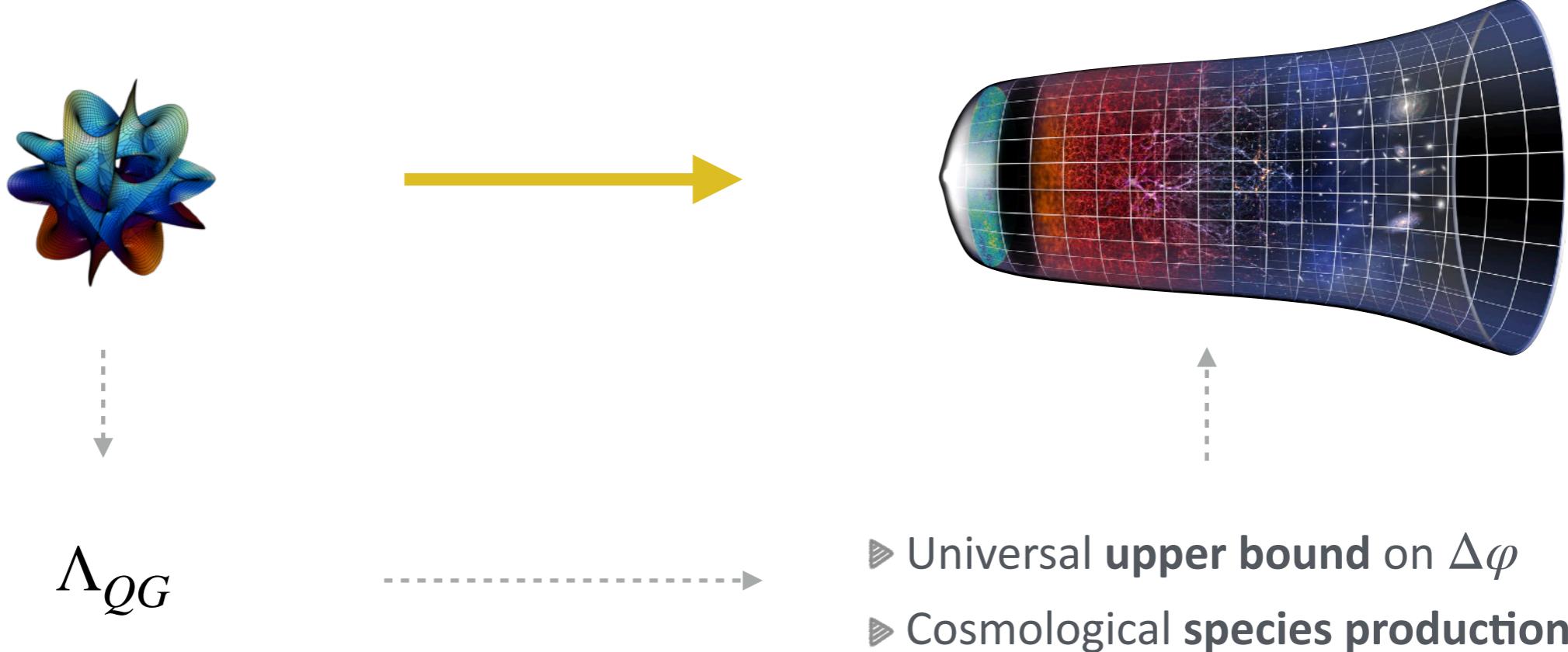


Species → Cosmology

Focus on **time-dependent** cosmic acceleration







Universal upper bound on scalar field range

MS, Valenzuela 2018

$$H < \Lambda_{QG} \leq M_P e^{-\lambda \Delta \varphi}$$



consistency of EFT



implication of the SDC

Universal upper bound on scalar field range

MS, Valenzuela 2018

see also

van de Heisteeg, Vafa, Wiesner, Wu 2023

$$H < \Lambda_{QG} \leq M_P e^{-\lambda \Delta\varphi}$$

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upper bound on field displacement

$$\Delta\varphi < \frac{1}{\lambda} \log \frac{M_P}{H}$$

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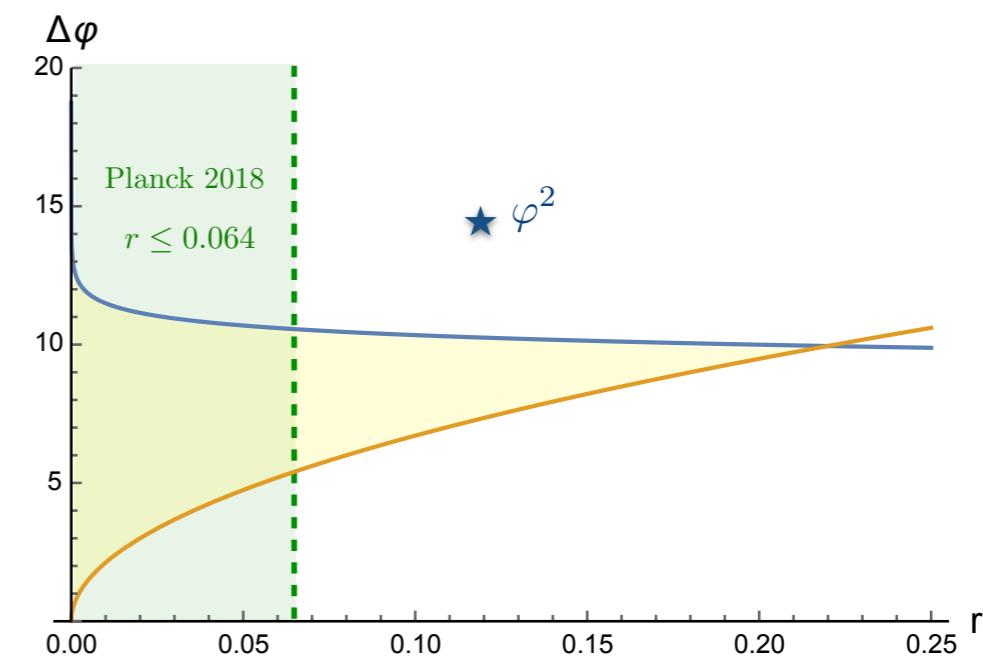
implication of the SDC

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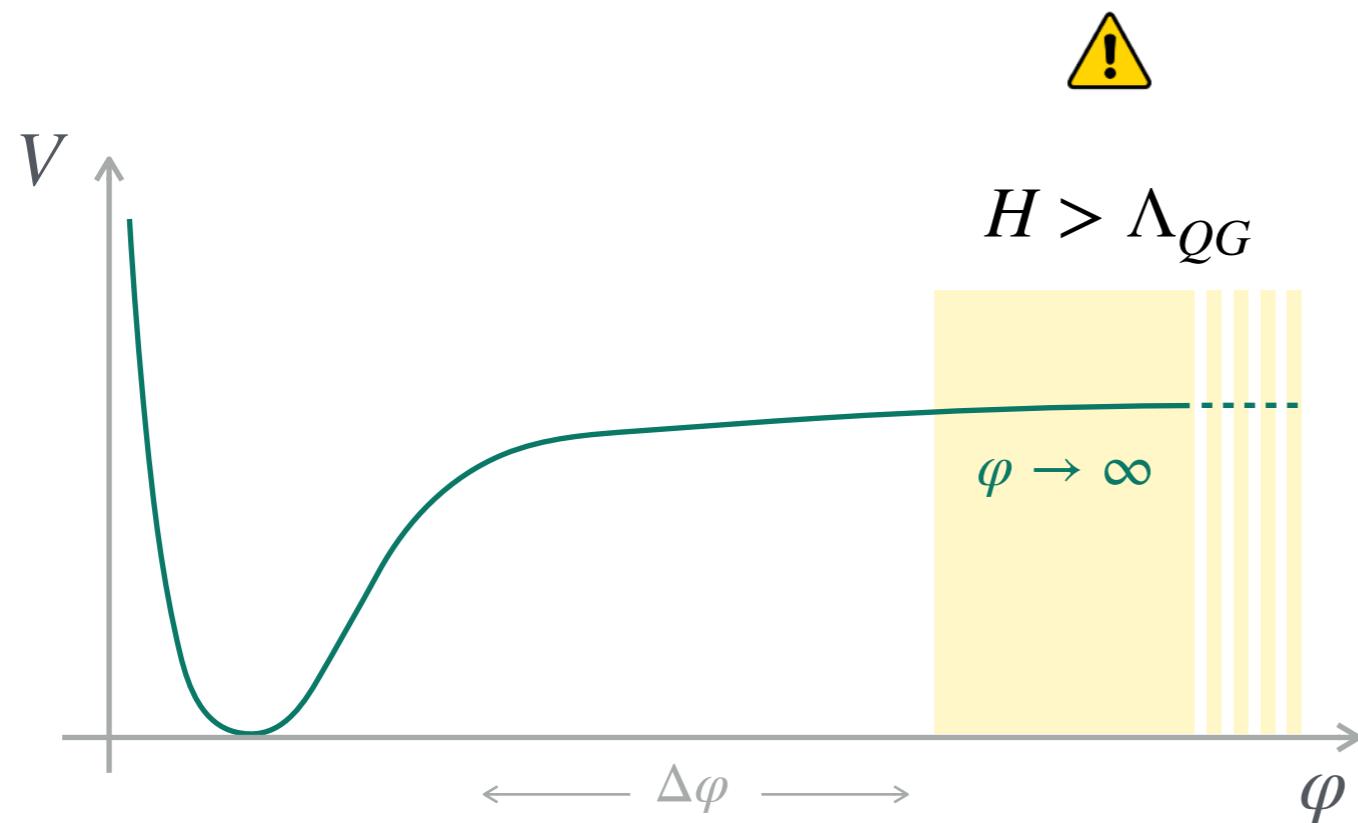
inflation

$$\Delta\varphi < \frac{1}{2\lambda} \left(\log \frac{\pi^2 A_s}{2} + \log r \right)$$



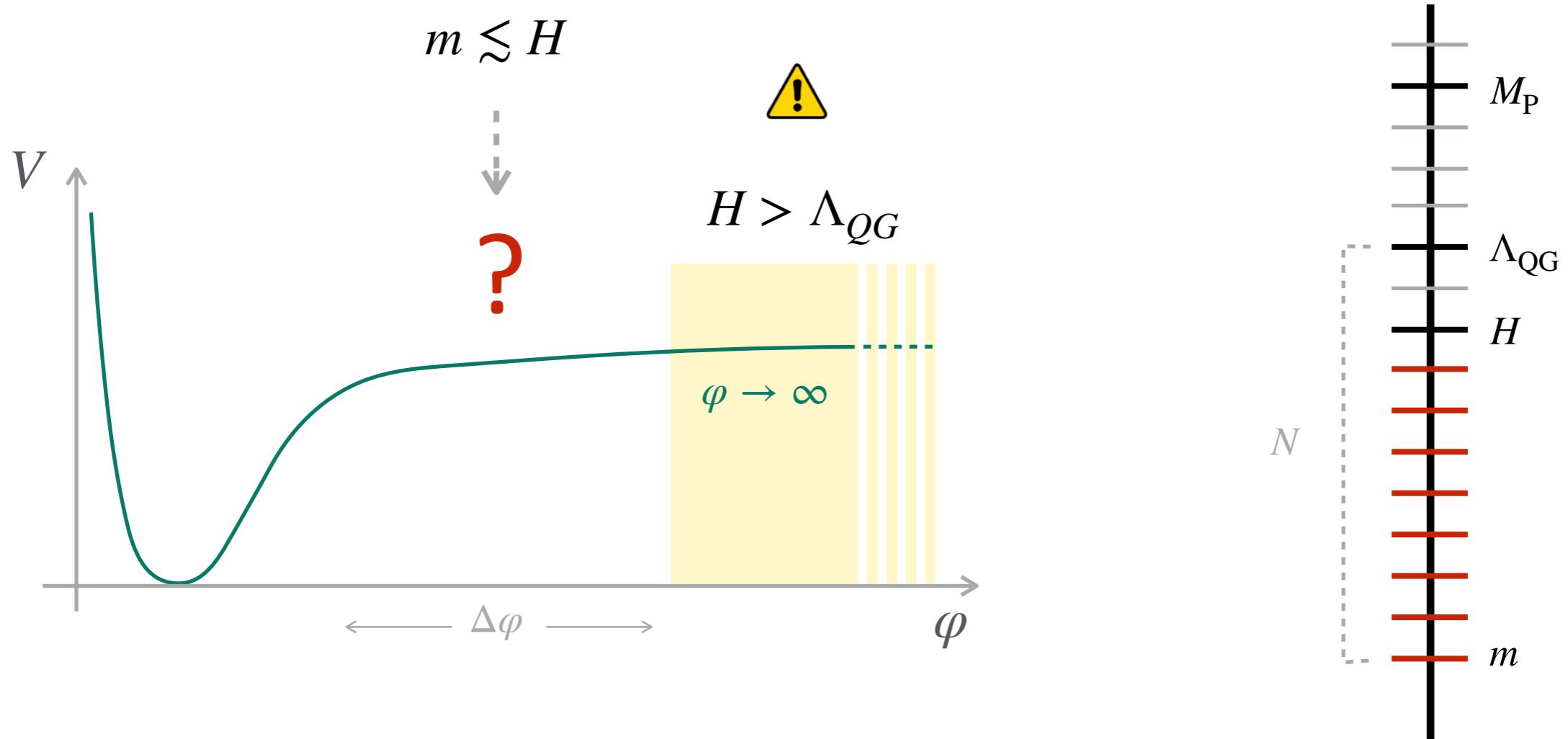
Inflationary particle production and the Swampland

Lüst, Masić, Pieroni, MS - work in progress



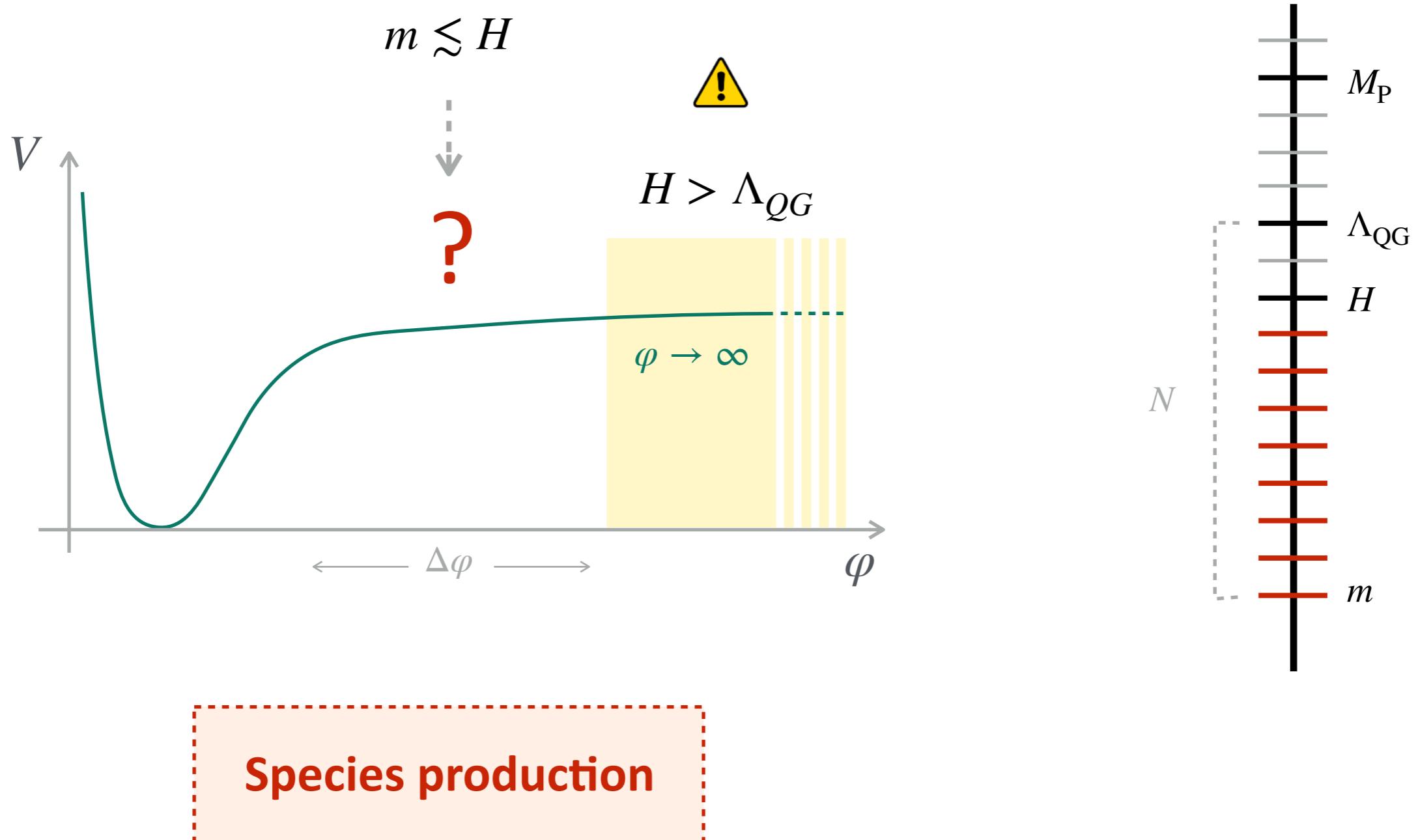
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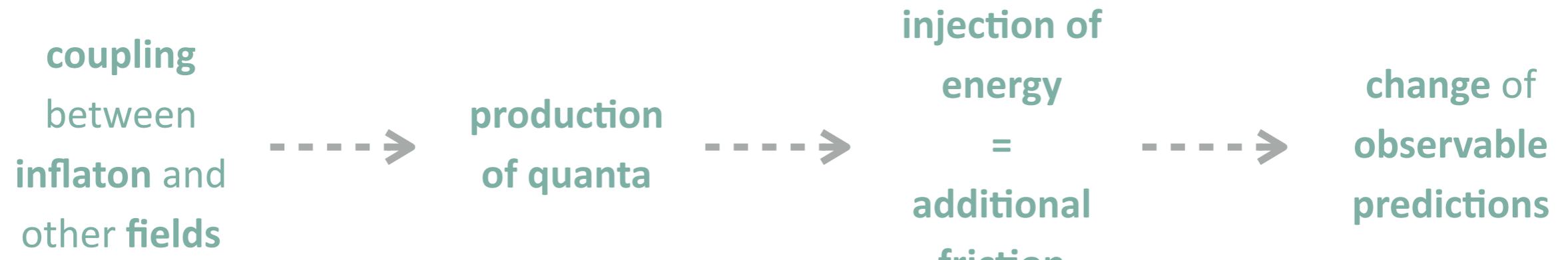
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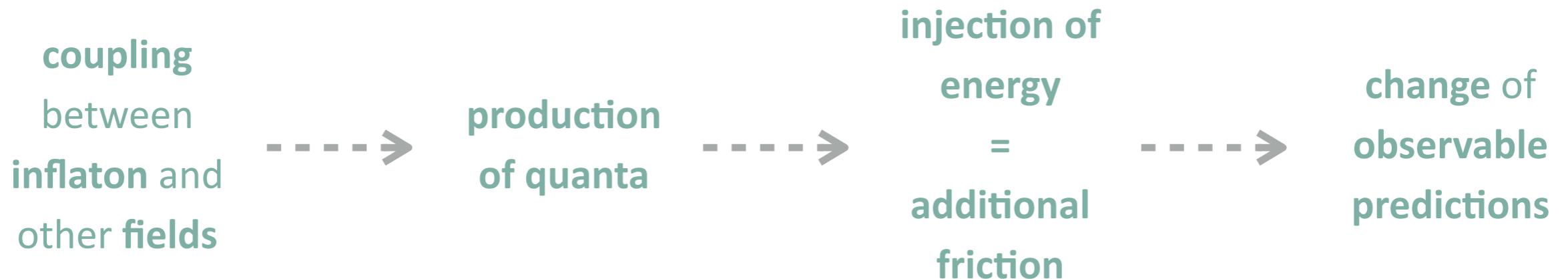
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Inflationary particle production and the Swampland

Lüst, Masias, Pieroni, MS - work in progress



► Inflaton-gauge fields coupling *Anber, Sorbo 2010*

$$\mathcal{L} = -\frac{1}{2}(\partial\varphi)^2 - V(\varphi) - \varphi F\tilde{F}$$

► Inflaton-scalar fields coupling *Green, Horn, Senatore, Silverstein 2009* "Trapped inflation"

$$\mathcal{L} = -\frac{1}{2}(\partial\varphi)^2 - V(\varphi) - \frac{1}{2} \sum_n [(\partial\chi_n)^2 - g^2(\varphi - \varphi_{0n})^2 \chi_n^2]$$

Inflationary particle production and the Swampland

Lüst, Masias, Pieroni, MS - work in progress

$$\mathcal{L} = -\frac{1}{2}(\partial\varphi)^2 - V(\varphi) - \frac{1}{2} \sum_n \left[(\partial\chi_n)^2 - \textcolor{red}{m_n^2 e^{-2\gamma\varphi}} \chi_n^2 \right]$$

mass of the SDC tower



$$m \sim e^{-\gamma\varphi}$$

Inflationary particle production and the Swampland

Lüst, Masias, Pieroni, MS - work in progress

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$$m \sim e^{-\gamma\varphi}$$

$$\xi_n''(\tau, \vec{k}) + \left[k^2 - \frac{2 - \delta_n}{\tau^2} \right] \xi_n(\tau, \vec{k}) = 0 \quad \text{with} \quad \delta_n = \frac{m_n^2}{H^2} e^{-2\gamma\varphi}$$


$$\xi_n \equiv a(\tau)\chi_n$$

$$\boxed{\xi_n(\tau, \vec{k}) = \frac{\sqrt{-\pi}}{2} \exp \left[\frac{i\pi}{4} \sqrt{9 - 4\delta_n} + \frac{i\pi}{4} \right] \sqrt{-\tau} H_{\frac{1}{2}\sqrt{9 - 4\delta_n}}^{(1)}(-k\tau)}$$

$H^{(1)}$ = Bessel function of the 3rd kind (or Hankel function of the 1st kind)

Inflationary particle production and the Swampland

Lüst, Masias, Pieroni, MS - work in progress

$$\mathcal{L} = -\frac{1}{2}(\partial\varphi)^2 - V(\varphi) - \frac{1}{2} \sum_n [(\partial\chi_n)^2 - \textcolor{red}{m_n^2 e^{-2\gamma\varphi}} \chi_n^2]$$

mass of the SDC tower

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main result

$$\text{corrections} \propto \left(\frac{H}{\Lambda_{\text{QG}}} \right)^{2+p}$$

Inflationary particle production and the Swampland

Lüst, Masić, Pieroni, MS - work in progress

► Scalar power spectrum

$$P_\zeta(k) = P_\zeta^h + P_\zeta^s = \frac{H^4}{(2\pi)^2 \dot{\phi}_0^2} \left(1 + 0.0025 \frac{H^3}{\Lambda_{QG}^3} \gamma^2 \right)$$

$$p = 1$$

► Non Gaussianities

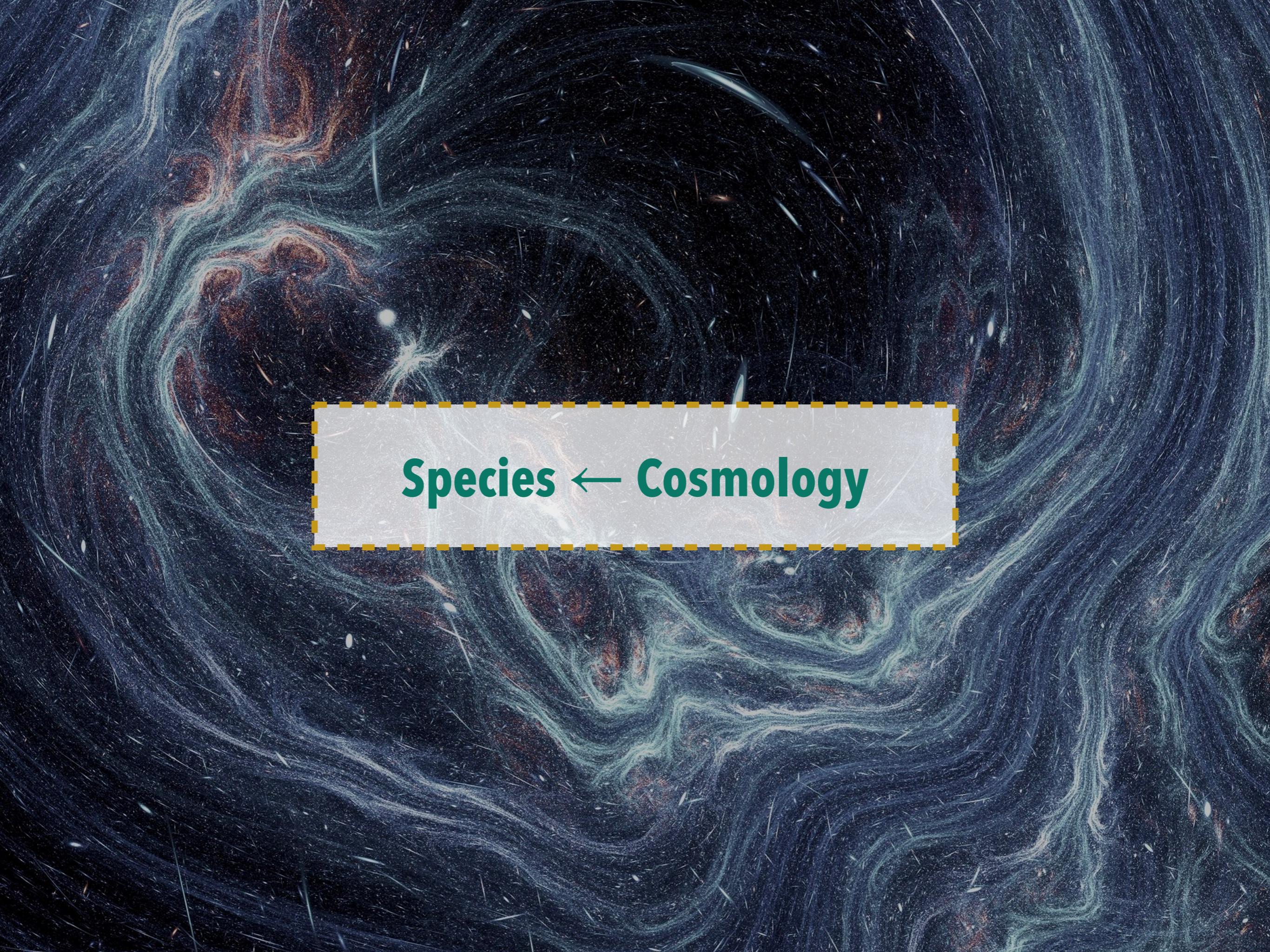
$$f_{NL,equil} \simeq 0.0007 \frac{\gamma \dot{\phi}}{H} (\gamma M_P)^2 \left[1 + 0.0025 (\gamma M_P)^2 \left(\frac{H}{\Lambda_{QG}} \right)^3 \right]^{-2} \left(\frac{H}{\Lambda_{QG}} \right)^3$$

► Tensor-to-scalar ratio

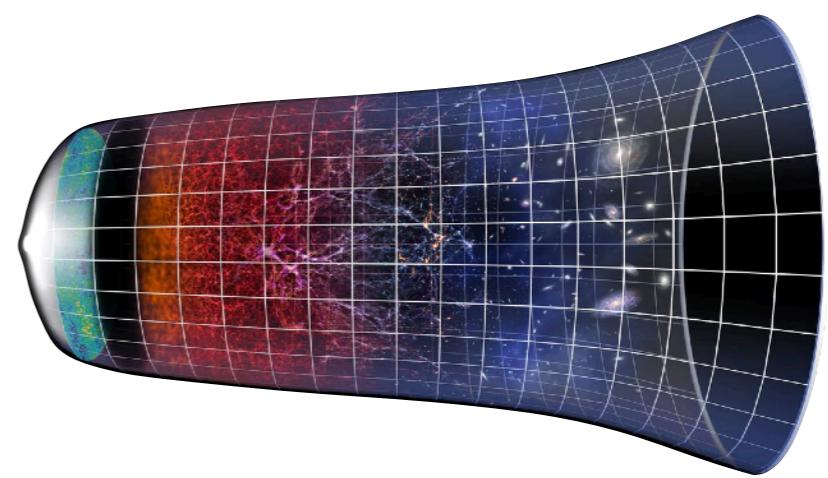
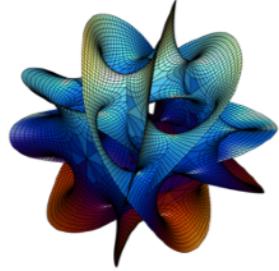
$$r = 9.2 \cdot 10^7 \frac{H^2}{M_P^2} \left[1 + 0.17 \left(\frac{H}{\Lambda_{QG}} \right)^3 \right]$$

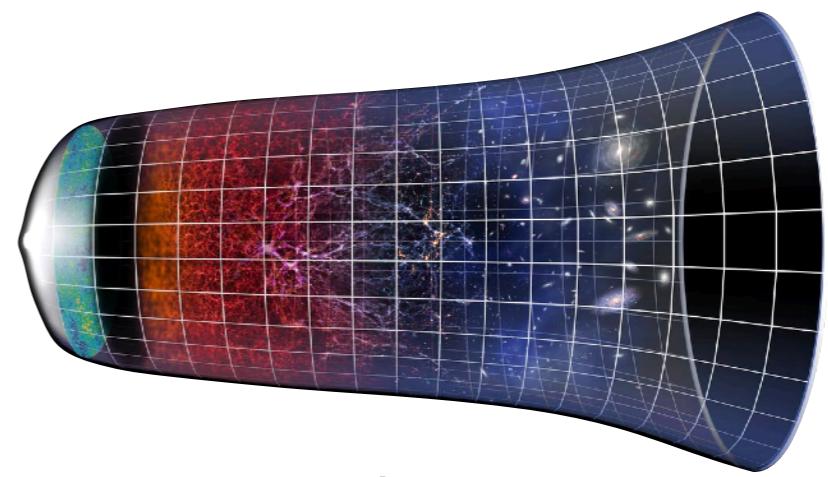
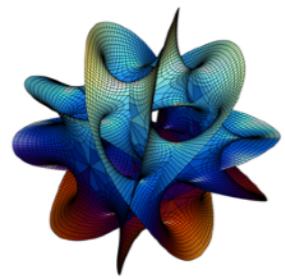
► Scalar spectral tilt

$$n_s - 1 = (-2\epsilon - \eta) \left[1 - \left(\frac{\gamma M_P}{20} \right)^2 \left(\frac{H}{\Lambda_{QG}} \right)^3 \right] - \left(5\epsilon + \sqrt{2\epsilon} \gamma M_P \right) \left(\frac{\gamma M_P}{20} \right)^2 \left(\frac{H}{\Lambda_{QG}} \right)^3$$



Species ← Cosmology





↓

r

$$\left| \frac{\Lambda'_s}{\Lambda_s} \right| \leq \frac{c}{\sqrt{r}} \log \frac{10^8}{r}$$

Species scale and primordial gravitational waves

MS - 2401.09533

EFT consistency

$$H \leq \Lambda_s \sim e^{-\lambda \Delta \varphi}$$

Distance Conjecture



$$\lambda = \left| \frac{\Lambda'_s}{\Lambda_s} \right| \leq \frac{1}{\Delta \varphi} \log \frac{M_P}{H}$$



$$\boxed{\left| \frac{\Lambda'_s}{\Lambda_s} \right| \leq \frac{1}{2\Delta \varphi} \log \frac{10^8}{r}}$$

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MS - 2401.09533

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$$\boxed{\left| \frac{\Lambda'_s}{\Lambda_s} \right| \leq \frac{1}{2\Delta \varphi} \log \frac{10^8}{r}}$$

$$\Delta \varphi(r) = ?$$

Species scale and primordial gravitational waves

MS - 2401.09533

$$\epsilon(N) = \frac{\beta}{N^p}$$

Species scale and primordial gravitational waves

MS - 2401.09533

$$p = 1$$

Monomial potentials

$$V(\varphi) \sim \varphi^n$$

$$p = 2$$

Starobinsky-like potentials

$$V(\varphi) \sim [1 - e^{-n\varphi} + \dots]$$

$$\epsilon(N) = \frac{\beta}{N^p}$$

$$1 < p < 2$$

$$p > 2$$

*Inverse-hilltop-like potentials
(brane inflation)*

$$V(\varphi) \sim \left[1 - \left(\frac{\mu}{\varphi} \right)^n + \dots \right]$$

Hilltop-like potentials

$$V(\varphi) \sim \left[1 - \left(\frac{\varphi}{\mu} \right)^n + \dots \right]$$

Species scale and primordial gravitational waves

MS - 2401.09533

$$p = 1$$

Monomial potentials

$$\left| \frac{\Lambda'_s}{\Lambda_s} \right| \lesssim \frac{1}{60\sqrt{2r}} \log \frac{10^8}{r}$$

$$p = 2$$

Starobinsky-like potentials

$$\left| \frac{\Lambda'_s}{\Lambda_s} \right| \lesssim \frac{1}{30 \log(60)\sqrt{2r}} \log \frac{10^8}{r}$$

$$1 < p < 2$$

$$\epsilon(N) = \frac{\beta}{N^p}$$

*Inverse-hilltop-like potentials
(brane inflation)*

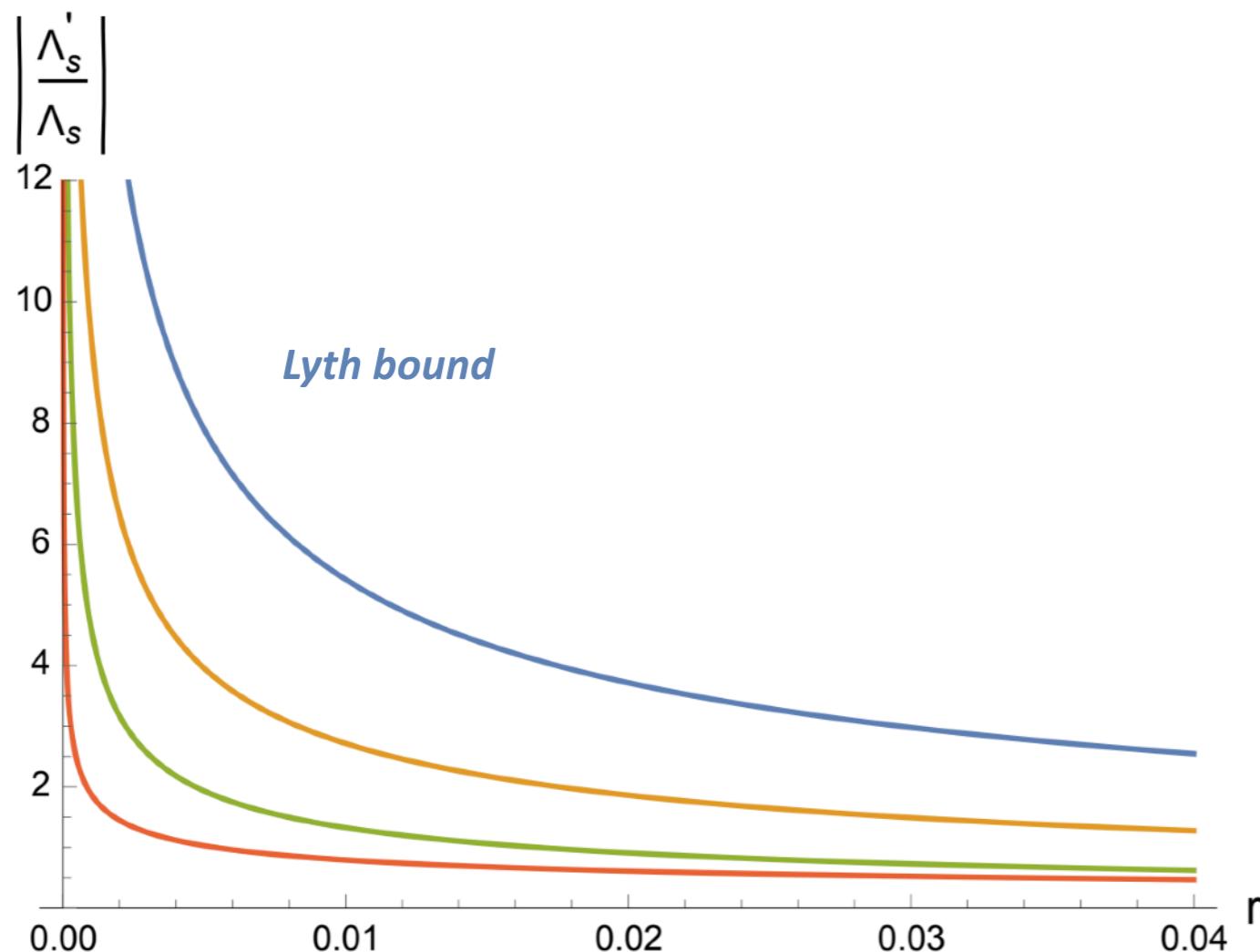
$$\left| \frac{\Lambda'_s}{\Lambda_s} \right| \lesssim \frac{1}{(2+n)30\sqrt{2r}} \log \frac{10^8}{r}$$

Hilltop-like potentials

$$\left| \frac{\Lambda'_s}{\Lambda_s} \right| \lesssim 2^{\frac{4}{p}-\frac{7}{2}} \frac{p-2}{15} r^{-\frac{1}{p}} \log \frac{10^8}{r}$$

Species scale and primordial gravitational waves

MS - 2401.09533



$p = 1$

Monomial potentials

$p = 2$

Starobinsky-like potentials

$p = 3$

Hilltop-like potentials

Species scale and primordial gravitational waves

MS - 2401.09533

e.g.

$D3 - \overline{D3}$ inflation

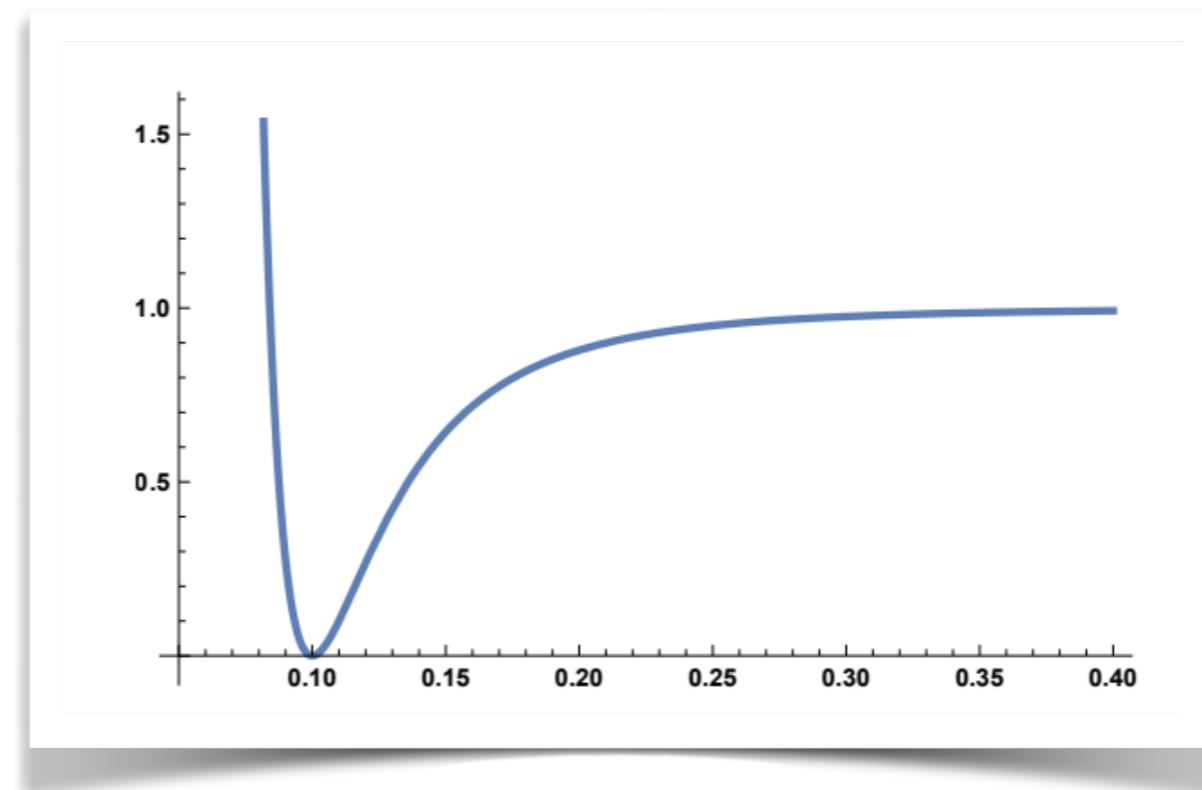
$$V(\varphi) \sim \left[1 - \left(\frac{\mu}{\varphi} \right)^4 + \dots \right]$$



$$\left| \frac{\Lambda'_s}{\Lambda_s} \right| \lesssim 0.5$$

$$(r \lesssim 0.036)$$

Kachru, Kallosh, Linde, Maldacena, McAllister, Trivedi 2003
Burgess, Quevedo 2022



plot taken from Burgess, Quevedo 2022



Species and R^2 -Inflation

R^2 - Inflation and the species scale

Lüst, Masias, Muntz, MS - 2312.13210

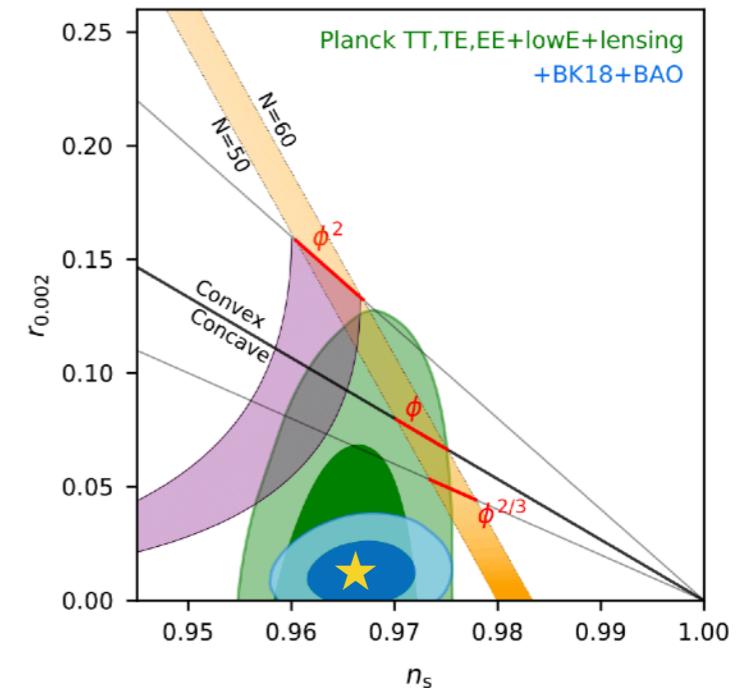
R^2 - Inflation and the species scale

Lüst, Masias, Muntz, MS - 2312.13210

$$S = \int d^4x \sqrt{-g} \left[\frac{M_P^2}{2} \left(R + \frac{R^2}{M^2} \right) \right]$$

Starobinsky 1980

Starobinsky 1984



R^2 - Inflation and the species scale

Lüst, Masias, Muntz, MS - 2312.13210

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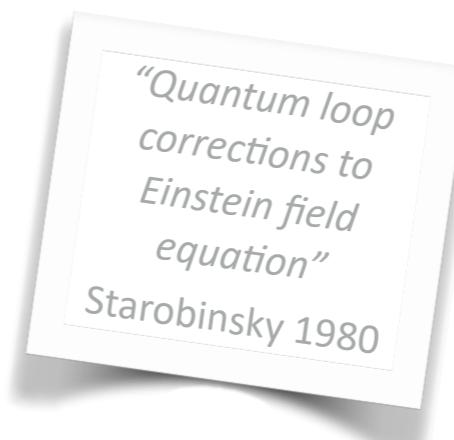
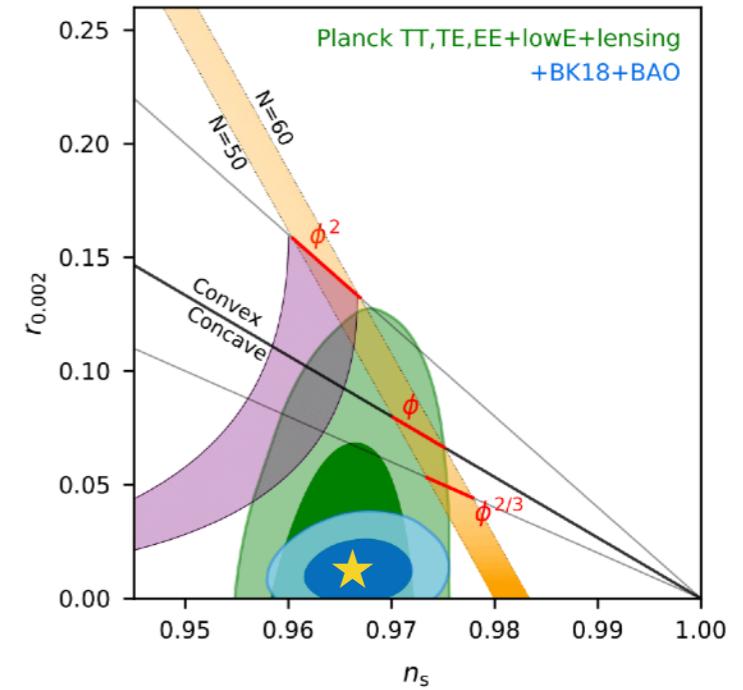
$$M = 10^{14} \text{ GeV}$$

fixed by CMB observation



$M = ?$
origin?

Starobinsky 1980
Starobinsky 1984



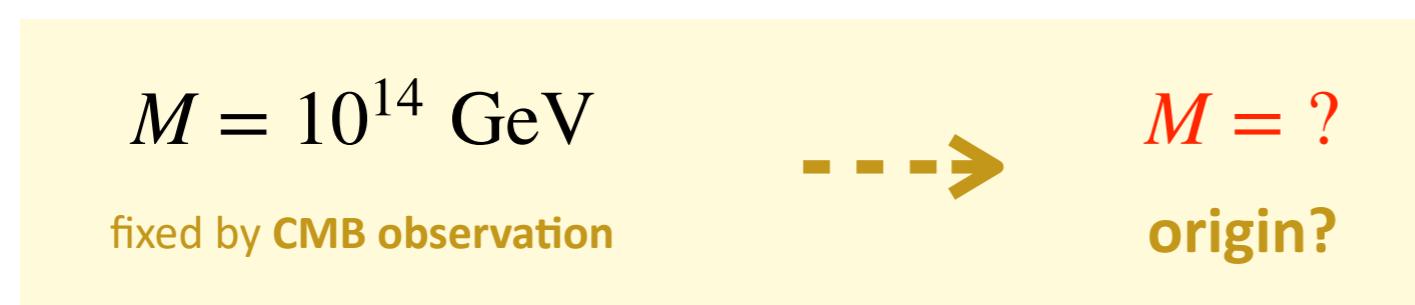
R^2 - Inflation and the species scale

Lüst, Masias, Muntz, MS - 2312.13210

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Starobinsky 1980

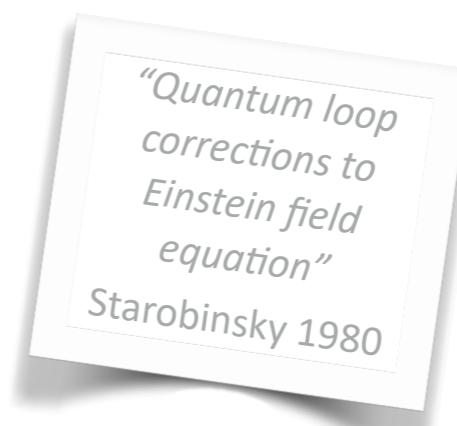
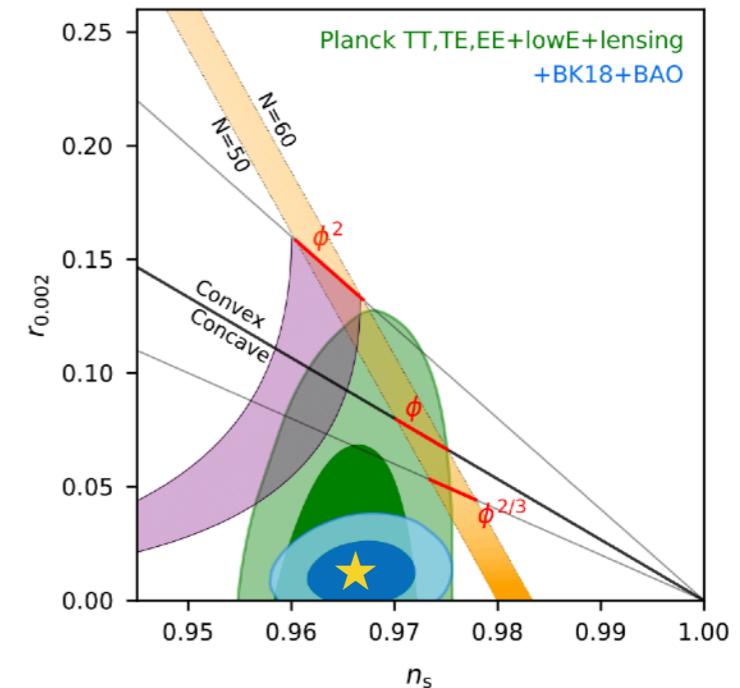
Starobinsky 1984



we argue

$$M \simeq \Lambda_s$$

originated by quantum effects of
towers of light species



Consequences on inflationary EFT

► Energy scale

$$M \simeq \Lambda_s$$

but also

$$M \simeq H$$

(in the Starobinsky model)



$$\boxed{\Lambda_s \simeq H}$$

boundary of the EFT validity

Consequences on inflationary EFT

► Energy scale

$$M \simeq \Lambda_s$$

but also

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$$\boxed{\Lambda_s \simeq H}$$

boundary of the EFT validity

► KK modes

$$M \simeq \Lambda_s \simeq 10^{14} \text{ GeV}$$



$$N_s \simeq 10^{10}$$



$$\boxed{m_{kk} \simeq 10^4 \text{ GeV}}$$

10 orders below H

Consequences on inflationary EFT

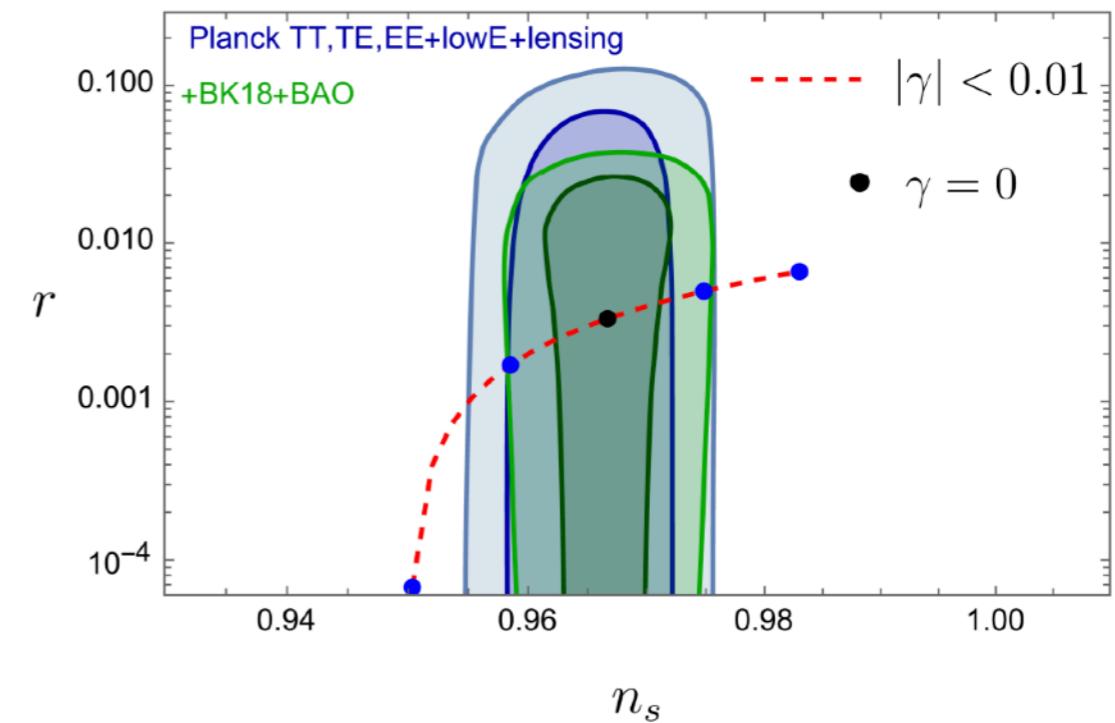
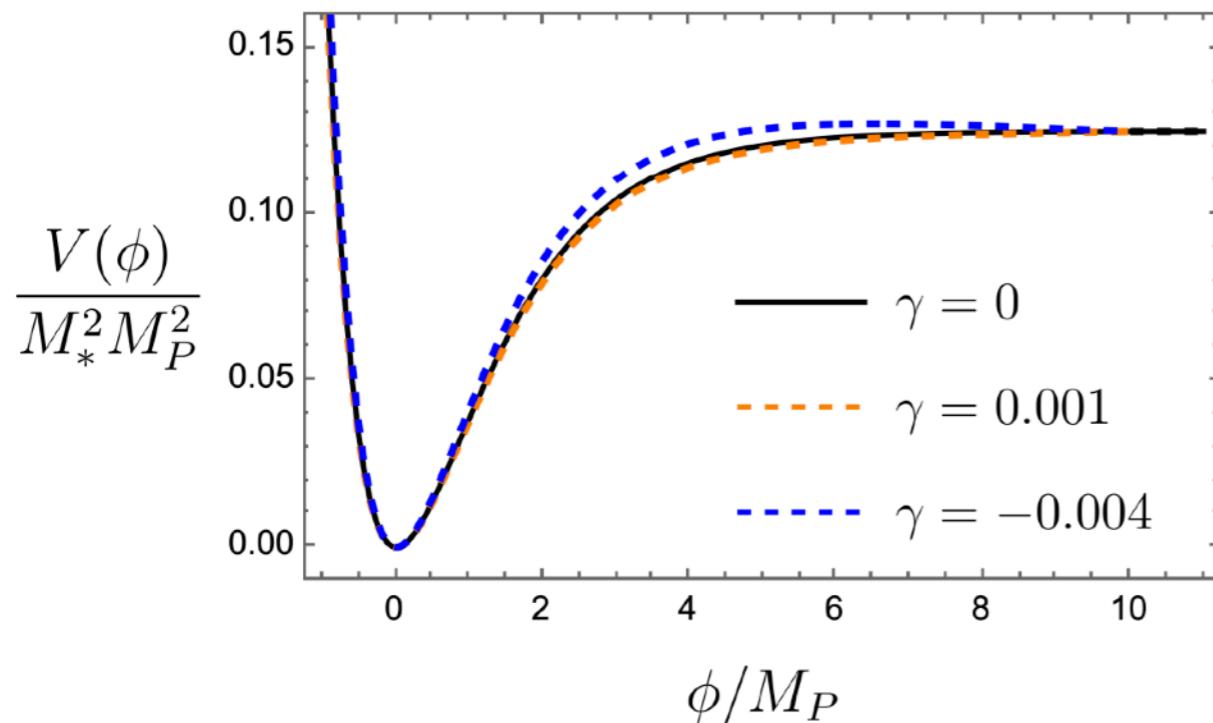
- ▶ Cosmology constrains Species Scale decay rate

$$\Lambda_s = M_* e^{-\gamma\phi} \quad \longrightarrow \quad V(\phi) = \frac{M_*^2 M_P^2}{8} e^{-2\gamma\phi} \left(1 - e^{-\sqrt{\frac{2}{3}}\phi/M_P} \right)^2$$

Consequences on inflationary EFT

- Cosmology constrains Species Scale decay rate

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Consequences on inflationary EFT

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$$n_s - 1 \simeq -\frac{2}{N_e} - 2\gamma\sqrt{\frac{2}{3}} + \mathcal{O}(\gamma^2)$$

$$r \simeq \frac{12}{N_e^2} - \gamma \frac{8\sqrt{6}}{N_e} + \mathcal{O}(\gamma^2)$$

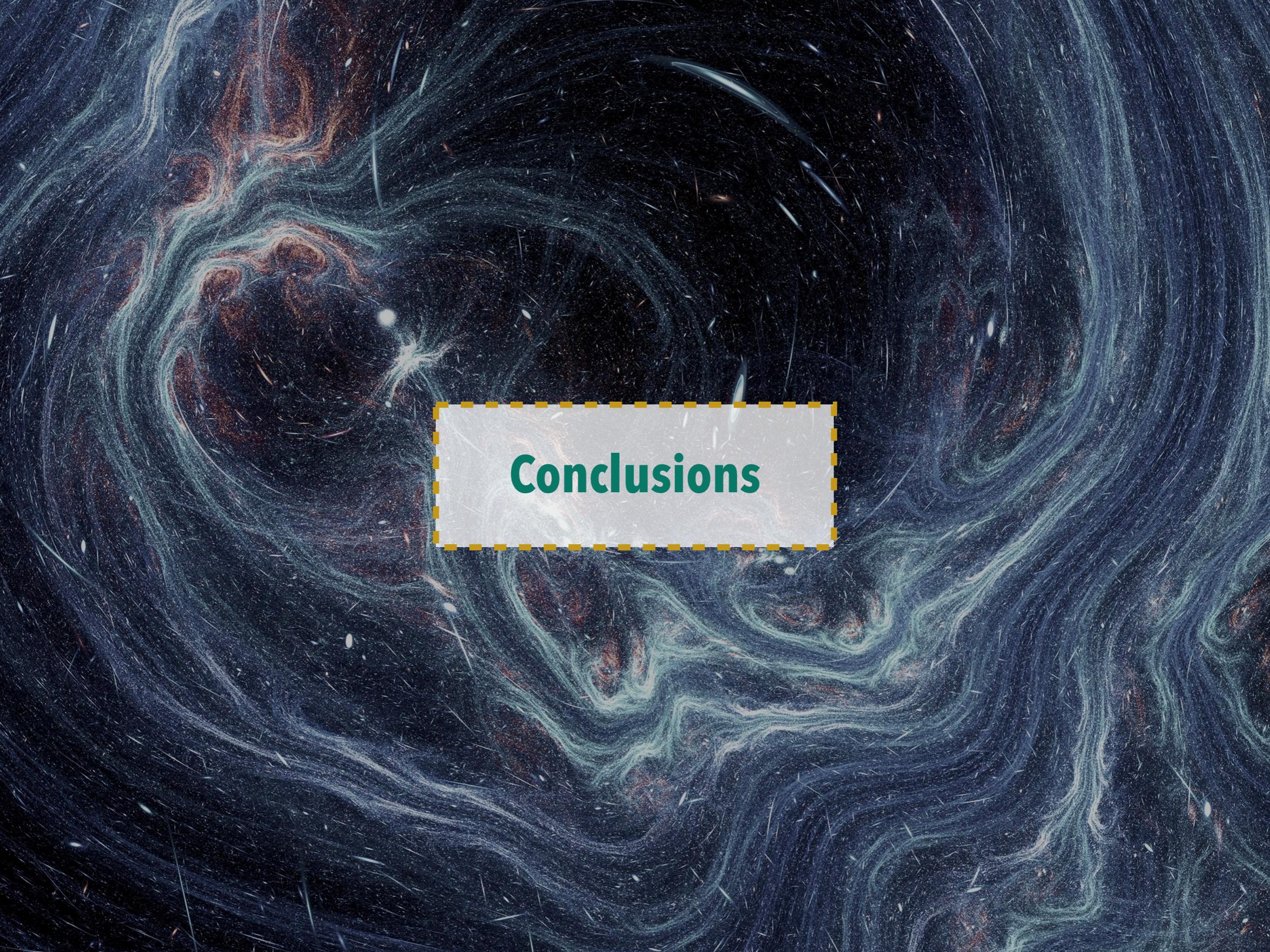
CMB data \longrightarrow

$$-0.001 \leq \gamma \leq 0.004$$



too small

$$|\gamma| \geq \frac{1}{\sqrt{(d-1)(d-2)}} = \frac{1}{\sqrt{6}}$$



Conclusions

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Conclusions

1

Towers of species lead to a renormalization of the quantum gravity cut-off

$$\Lambda_{\text{QG}} = \frac{M_{\text{P}}}{N^{\frac{1}{d-2}}}$$

Dvali 2007

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Universal upper bound on the scalar field range

$$\Delta \lesssim -\log H$$

MS, Valenzuela 2018

MS 2019

Conclusions

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Universal upper bound on the scalar field range

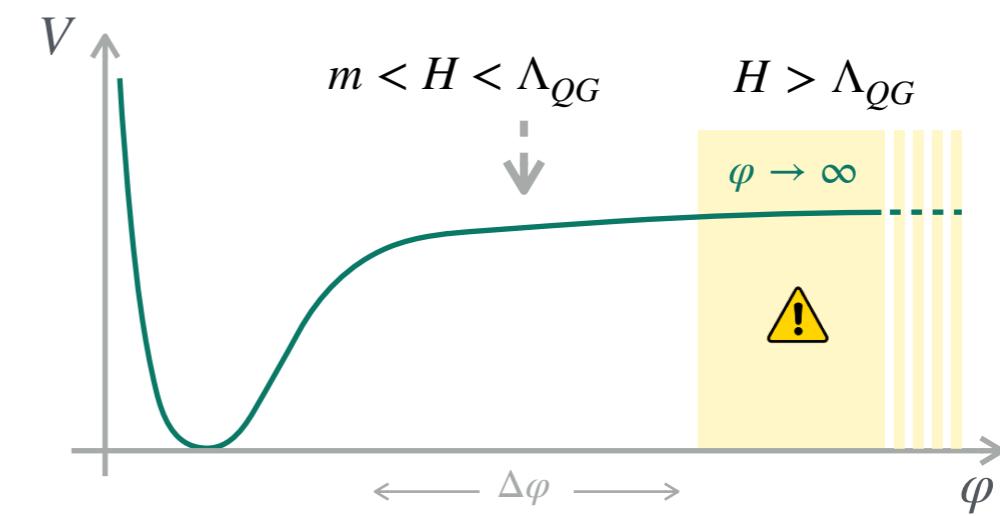
$$\Delta \lesssim -\log H$$

MS, Valenzuela 2018

MS 2019

3

Effects of species on inflationary observables



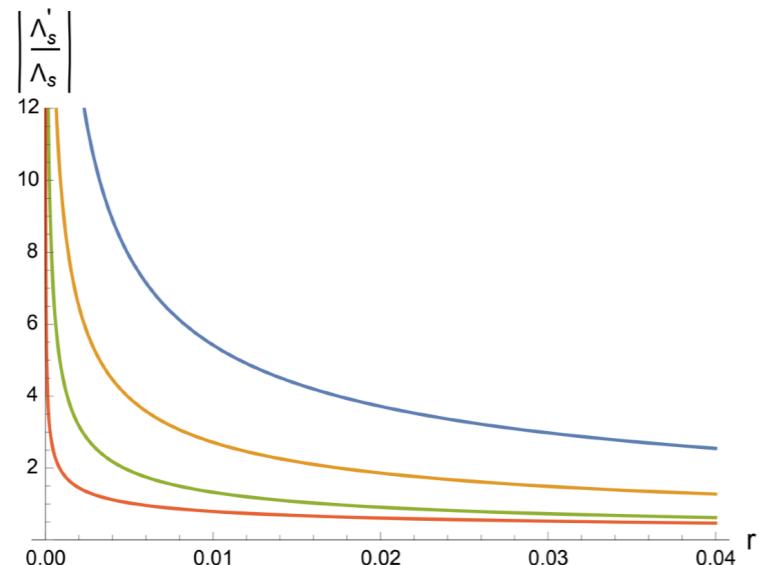
$$\delta\{n_s, r, f_{NL}\} \propto \left(\frac{H}{\Lambda_{QG}}\right)^{2+p}$$

Luest, Masias, Pieroni, MS - work in progress

Conclusions

4

Detection of PGWs sets **upper bound** on decay rate of Λ_{QG}



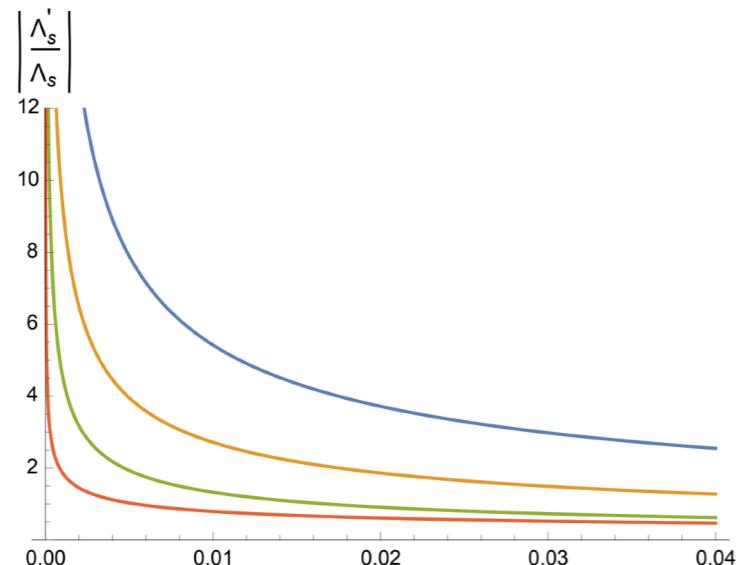
$$\left| \frac{\Lambda'_{\text{QG}}}{\Lambda_{\text{QG}}} \right| \lesssim \frac{c}{\sqrt{r}} \log \frac{10^8}{r}$$

MS 2024

Conclusions

4

Detection of PGWs sets **upper bound on decay rate of Λ_{QG}**



$$\left| \frac{\Lambda'_{\text{QG}}}{\Lambda_{\text{QG}}} \right| \lesssim \frac{c}{\sqrt{r}} \log \frac{10^8}{r}$$

MS 2024

5

R^2 -inflation
(generated by species)
in the **Swampland**

$$H \simeq \Lambda_s \simeq 10^{14} \text{ GeV}$$

$$m_{kk} \simeq 10^4 \text{ GeV}$$

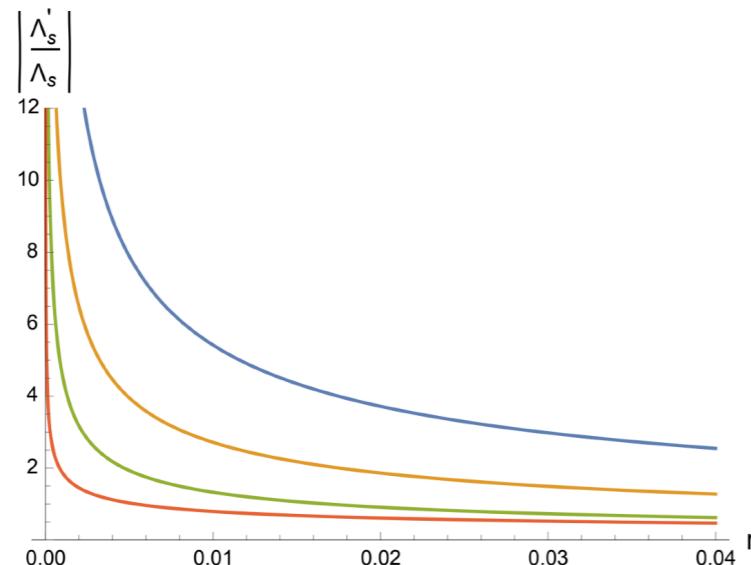
γ too small

Lüst, Masias, Muntz, MS - 2312.13210

Conclusions

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Lüst, Masias, Muntz, MS - 2312.13210

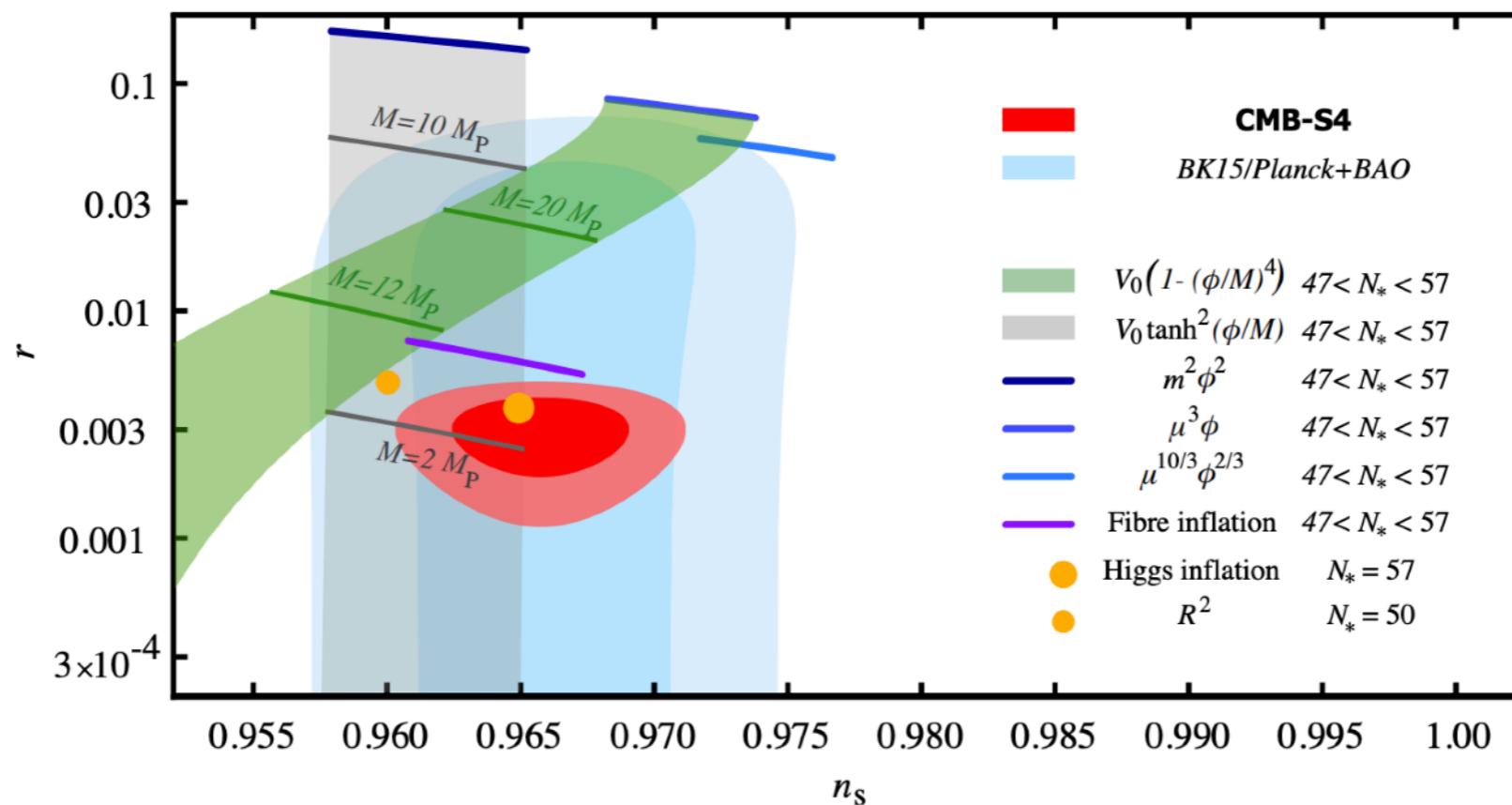
thanks!



Extra slides

Species scale and primordial gravitational waves

MS - 2401.09533



Lyth bound $\Delta\phi \gtrsim \sqrt{\frac{r}{0.002}}$ \rightarrow $\Delta\phi \gtrsim M_P$ Super-Planckian field range

Species scale and primordial gravitational waves

MS - 2401.09533

$$\Delta\varphi = \int \sqrt{2\epsilon} \, dN$$

