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PIANO NAZIONALE  
DI RIPRESA E RESILIENZA



# Betatron radiation from laser wakefield acceleration: ongoing experiments at SPARC\_LAB

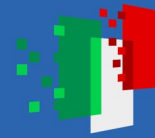


TOR VERGATA  
UNIVERSITÀ DEGLI STUDI DI ROMA

Gemma Costa  
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On behalf of SPARC\_LAB & EuAPS collaborations

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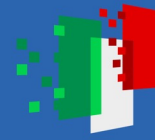
- ✓ Laser WakeField Acceleration: bubble regime
- Betatron radiation from LWFA
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- The EuAPS project @SPARC\_LAB and Experimental setup



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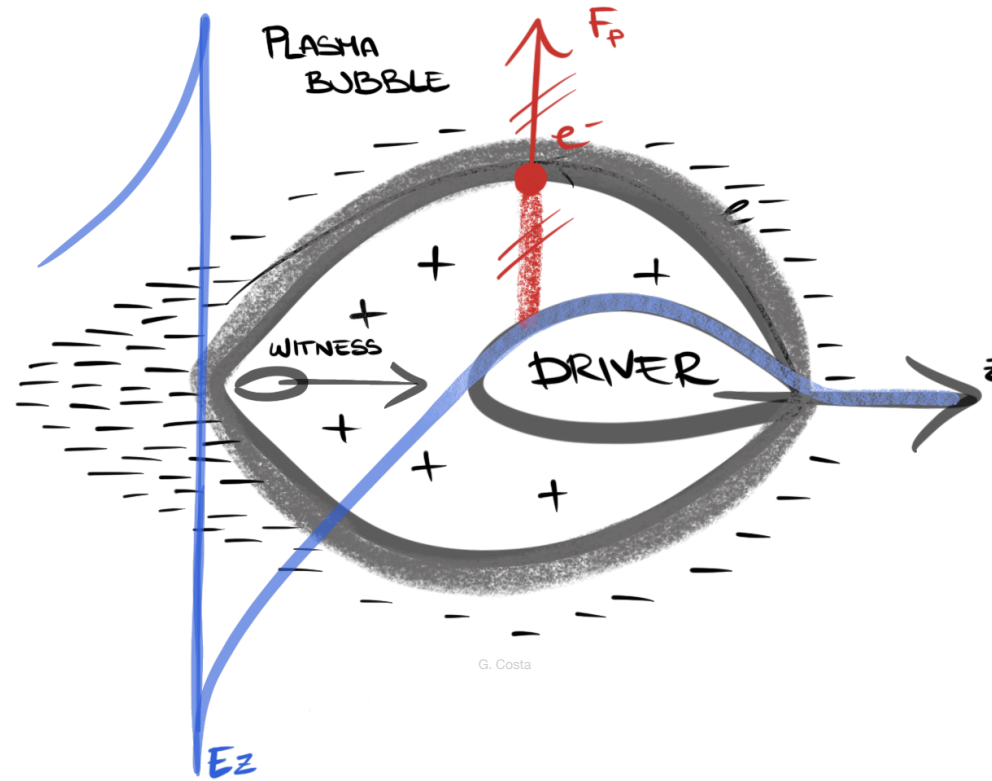
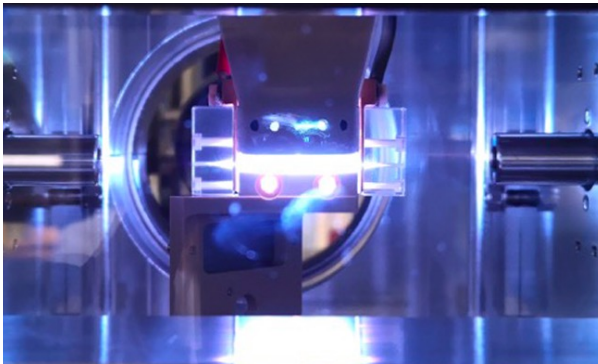
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Conventional RF structures:  
(20 – 40) MV/m  
range m - km



Plasma module:  
 $E \text{ [GV/m]} \approx 96 (n_e \text{ [cm}^{-3}\text{]})^{1/2}$   
 $n_e = 10^{18} \text{ cm}^{-3} \Rightarrow 100 \text{ GV/m}$   
range mm - cm



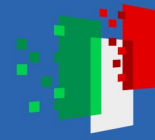
## LWFA

**Laser pulse**  
 $I = 10^{18} \text{ W/cm}^2$  and  $c\tau < \lambda_p/2$

**Plasma frequency**  
 $\omega_p = (n_e e^2 / \epsilon_0 m_e)^{1/2}$

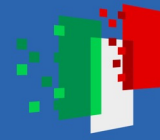
$a_0 \gg 1$   
non-linear regime  
Self-injection

Tajima and Dawson (1979)



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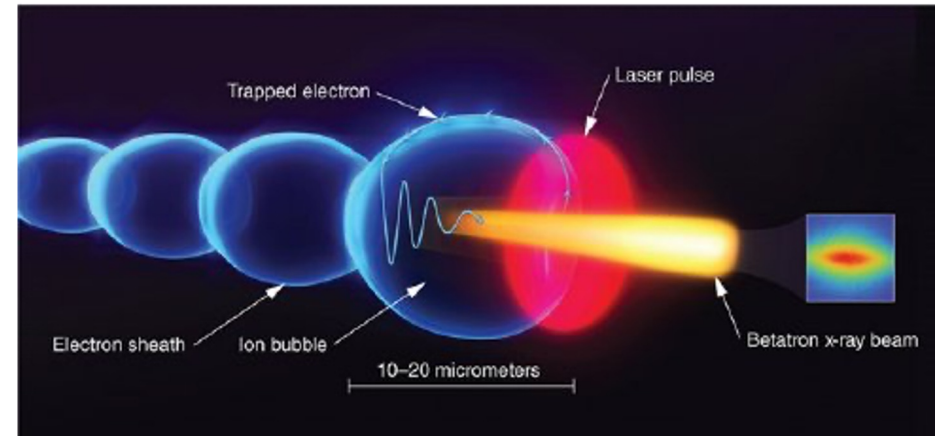
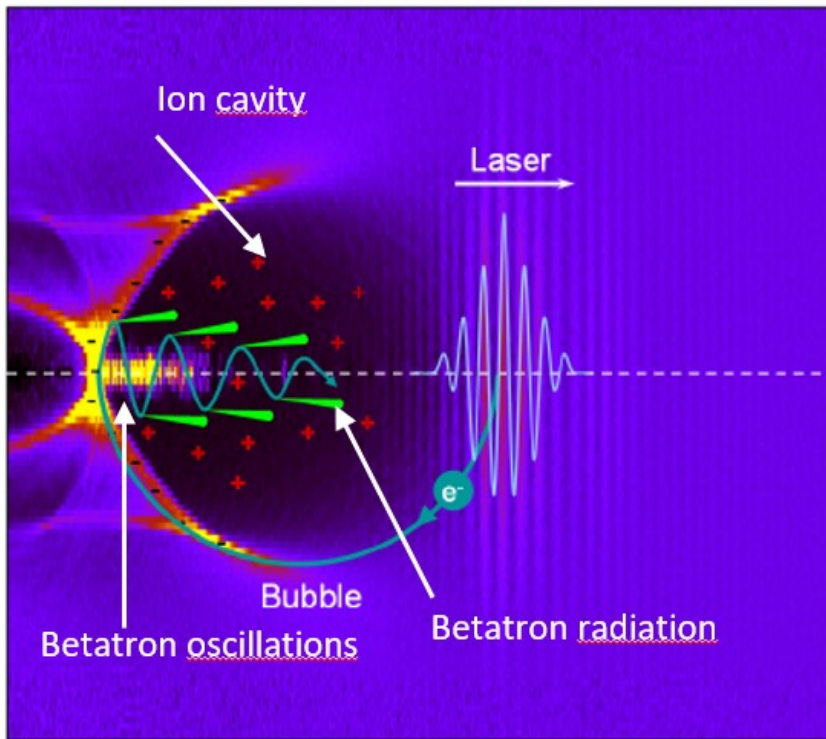


## Betatron radiation emission

Longitudinal electric field → acceleration along the laser propagation axis

Radial electric field → oscillations around the reference trajectory

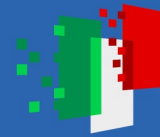
Emission of synchrotron-like radiation = **Betatron radiation**



- Energy from soft to hard X-rays
- High peak brilliance

- Spatially coherent
- Temporally incoherent
- Pulse ~ few fs

$$B \approx 10^{20} \frac{\text{Photons}}{\text{s} \cdot \text{mm}^2 \cdot \text{mrad}^2 \cdot 0.1\% \text{ BW}}$$

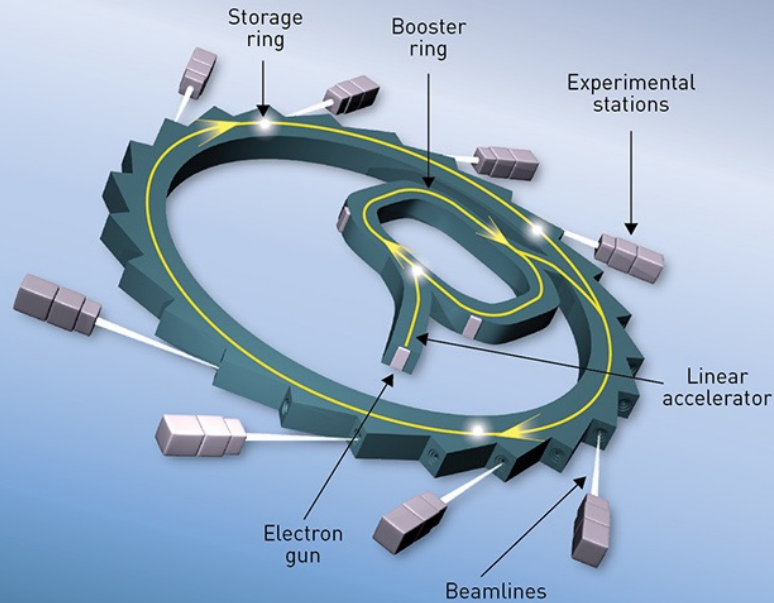


# Synchrotrons vs FELs

## Synchrotrons and X-ray FELs

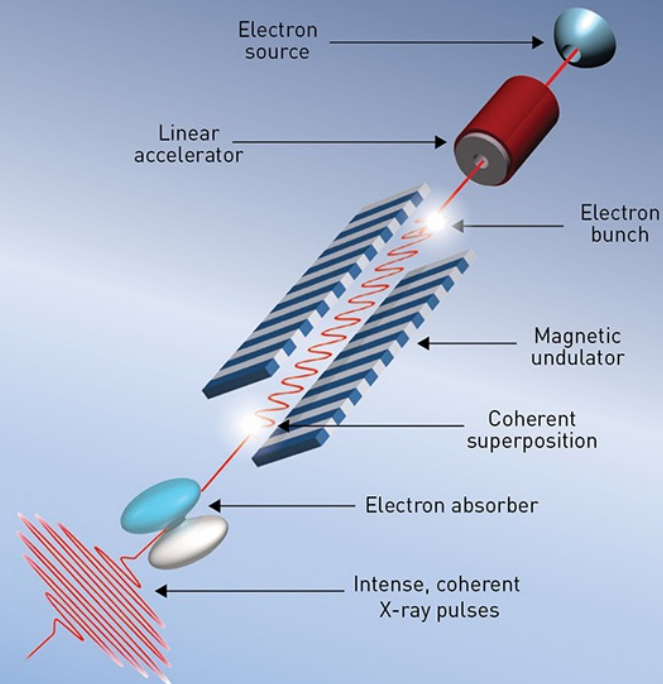
### Synchrotron light source

Electrons, accelerated to near light speed in a linear accelerator and booster ring, whirl around in a larger storage ring, creating X-rays that feed beamlines for multiple experimental stations



### X-ray free-electron laser (FEL)

In FELs, accelerated electron bunches are "wiggled" in a magnetic undulator, causing them to throw off coherent, bright and laser-like X-ray beams for experiments

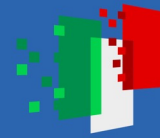


- Large bandwidth like a Synchrotrons
- Short pulse duration like a FEL

$$B = \frac{d^4 N}{dt d\Omega dS d\lambda / \lambda}$$

Ph/ (s mm<sup>2</sup> mrad<sup>2</sup> 0.1% of bandwidth)

Patricia Daukantas Synchrotron Light Sources for the 21st Century Optics & Photonics News Settembre 2021



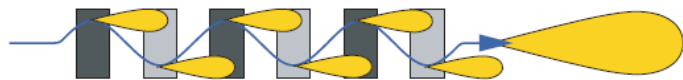
## Wiggler or undulator?

Betatron strength parameter for a single electron

$$K = \frac{eB_0}{m_e c k_u} = \frac{eB_0 \lambda_u}{2\pi m_e c} = 0.934 \cdot B_0 [T] \cdot \lambda_u [cm]$$

$$K = \gamma r_\beta k_\beta = \theta \gamma$$

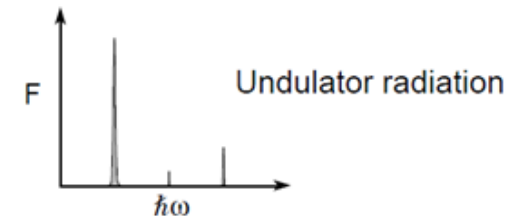
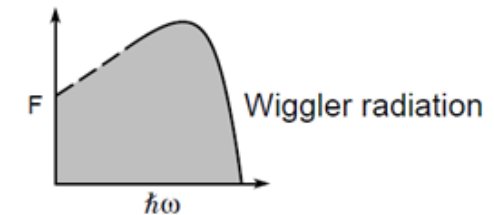
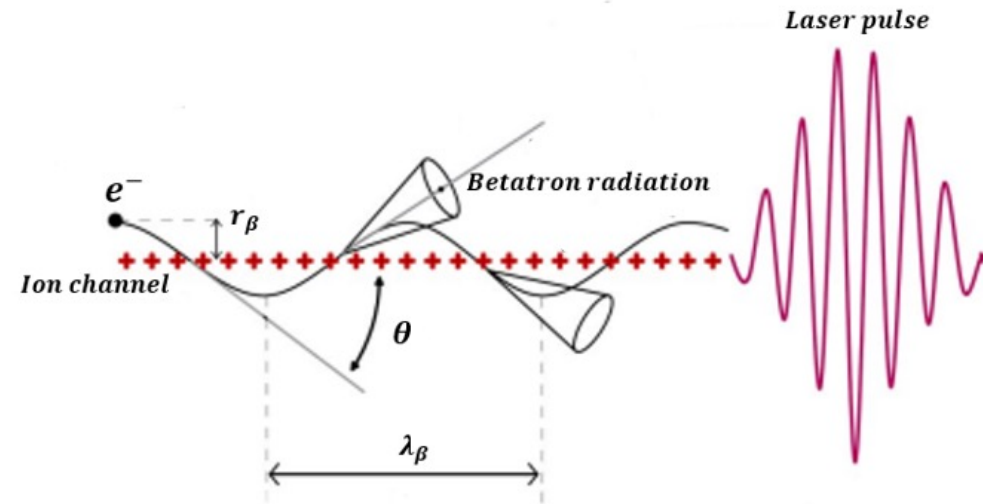
- $\theta$  radiation cone opening angle
- $k_\beta$  amplitude of the oscillation
- $k_\beta = \omega_\beta / c$  betatron wavenumber

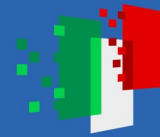


$K \gg 1$  wiggler regime



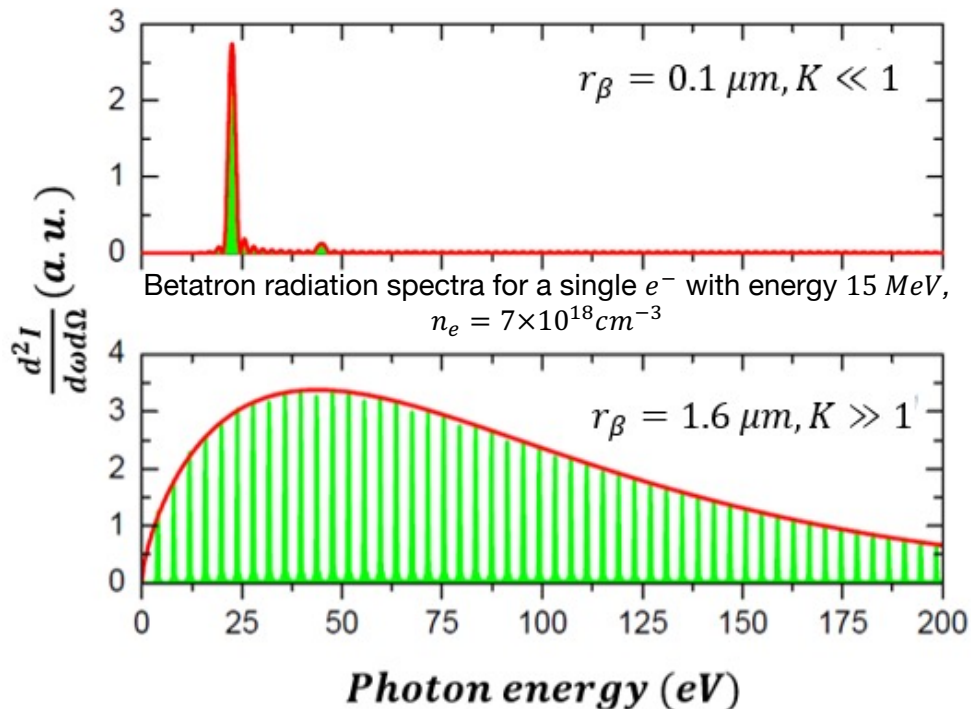
$K \leq 1$  undulator regime





## Spectral flux and critical energy

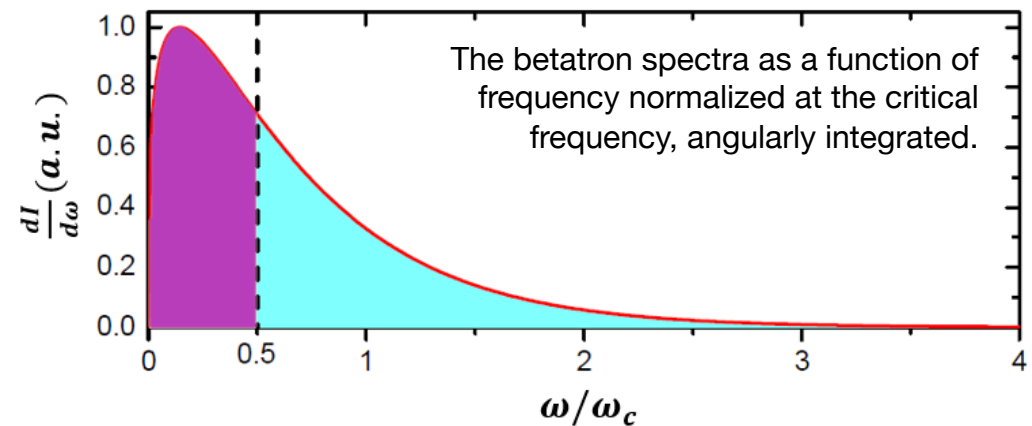
$$\frac{d^2 I}{d\omega d\Omega} \approx \frac{3e^2}{2\pi^3 \epsilon_0 c} N_\beta \gamma^2 K_{2/3}^2(\zeta) \zeta^2$$



- critical frequency  $\omega_c = 3\gamma^2 K_\beta \omega_\beta$

- critical energy  $E_c \propto \gamma^2 K \omega_\beta$

which divides the spectrum in two region each carrying the same amount of energy

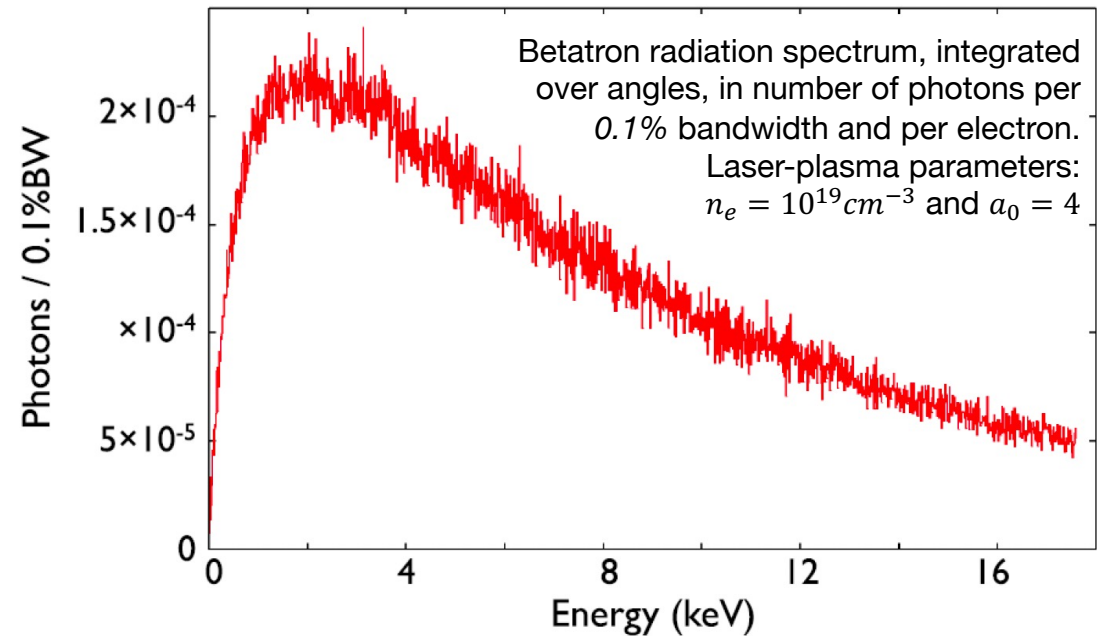
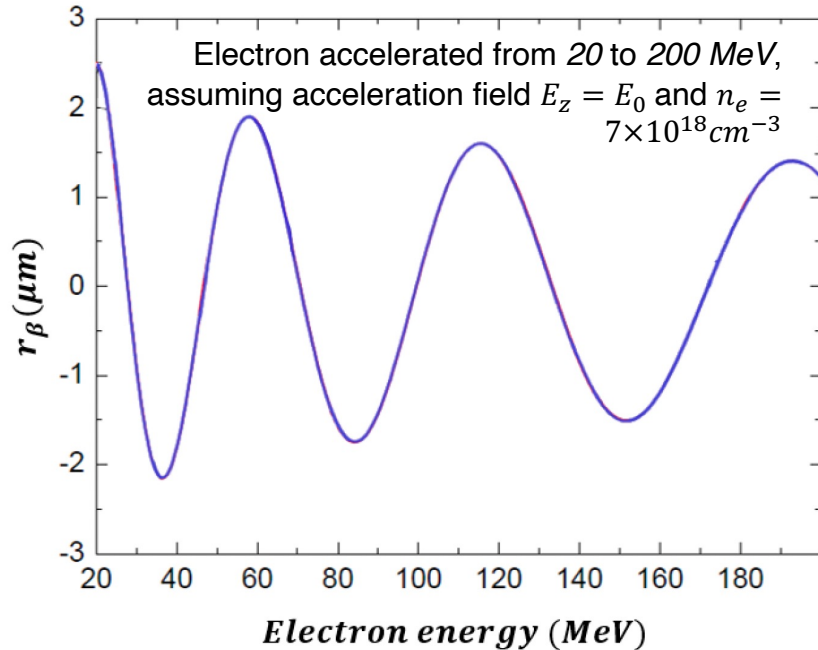


$$\frac{dN}{d\omega} = N_e \frac{\sqrt{3}}{2\pi} \frac{e^2 \gamma}{\epsilon_0 c \omega_c} \int_{2\omega/\omega_c}^{\infty} K_{5/3}(x) dx$$



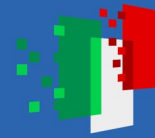


## Acceleration lead to damped oscillations and inhomogenous broadening



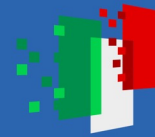
$$\left. \frac{d^2 I_{acc}}{d\omega d\Omega} \right|_{\theta=0} = \frac{3e^2}{2\pi^3 \epsilon_0 c} \int_{\epsilon_i}^{\epsilon_f} d\gamma^2 \zeta^2 K_{2/3}^2(\zeta)$$

Electron's strength parameter in a plasma focusing channel depends on the **oscillation amplitude**, leading to inhomogeneous broadening of the radiation spectrum and suppression of the spectral-angular correlations.



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# FLAME LASER

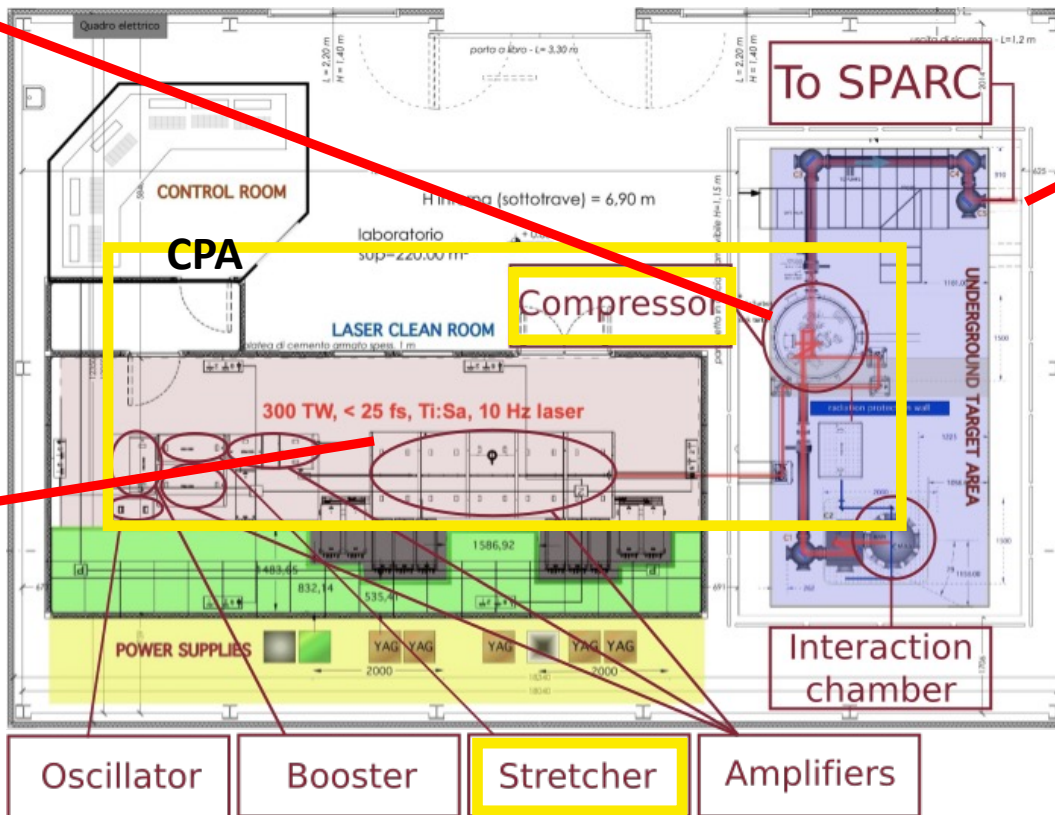
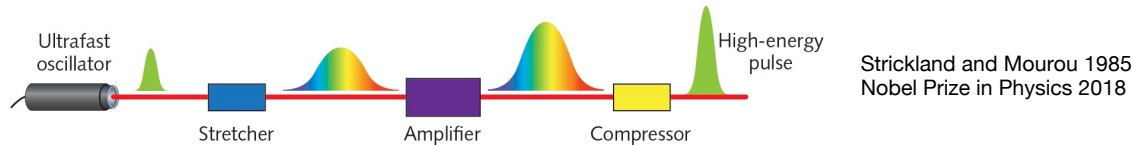
## MAIN PULSE

Peak power	250 TW
Energy on target	7 J
Rep. rate	10 Hz
Temporal length	25 fs
FW 1/e <sup>2</sup> @ focus	20 μm
Intensity	10 <sup>19</sup> W/cm <sup>2</sup>
Contrast-ratio	10 <sup>10</sup>

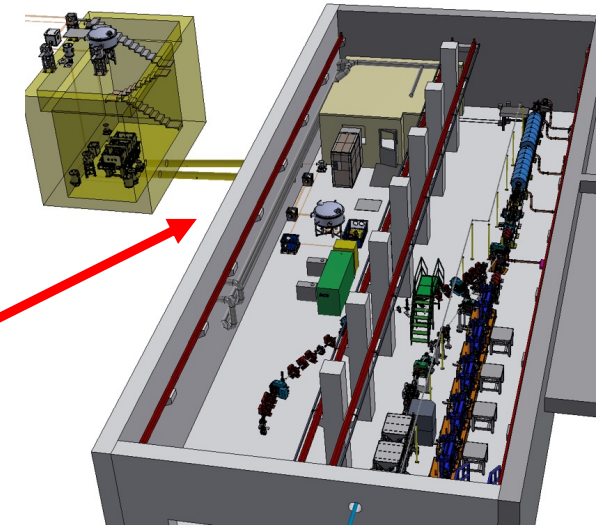
## PROBE PULSE

Energy on target	10 mJ
Temporal length	50 fs
FW 1/e <sup>2</sup> @ focus	120 μm
Intensity	10 <sup>16</sup> W/cm <sup>2</sup>

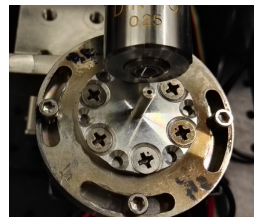
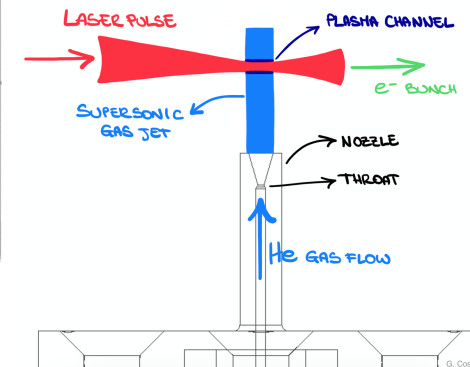
High-power Ti:Sa based laser, ultra-short CPA based pulse

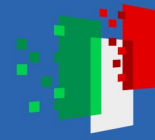


80 MHz, 220 mW

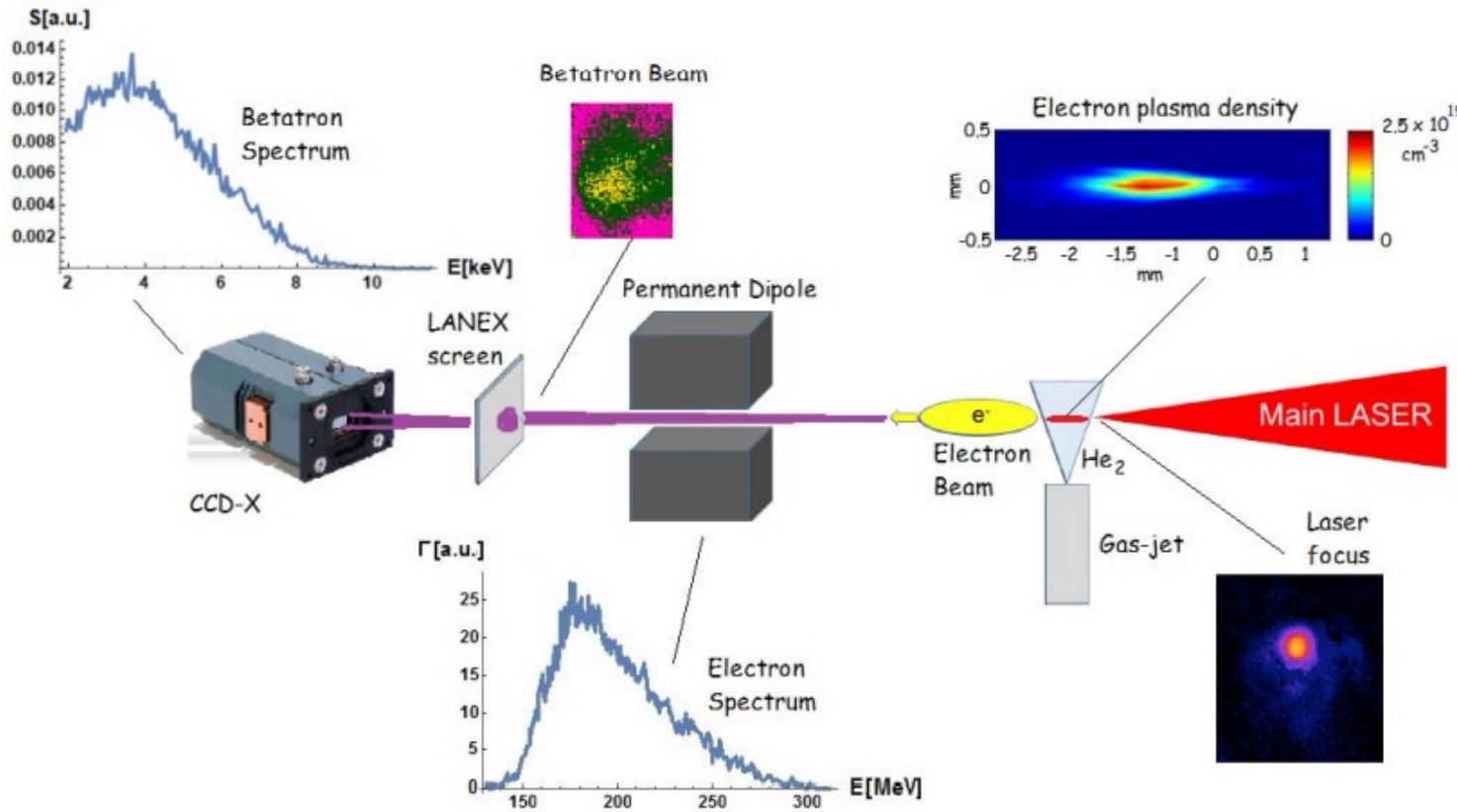


supersonic nozzle for self-injection experiments and X-rays radiation emission

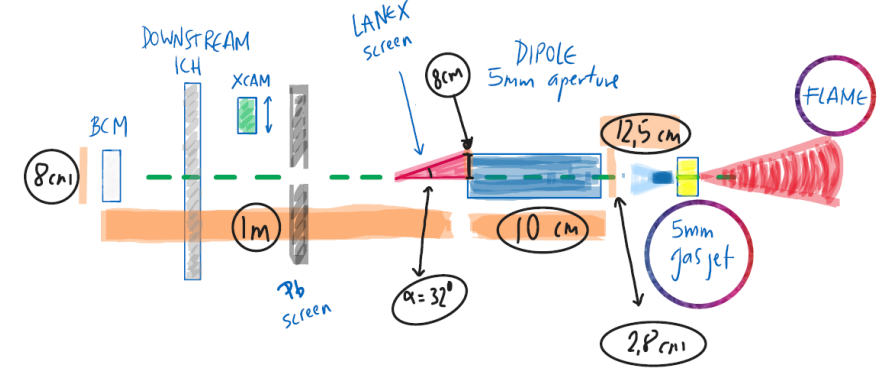




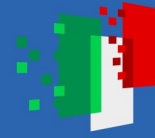
# FLAME experimental setup for betatron radiation source



- Laser energy 6 J
- Laser temporal length 30 fs FWHM
- Laser focal spot 18-20  $\mu m$  FWHM



Courtesy M Galletti



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## The PNRR EuAPS Project WP2

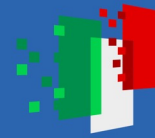
EuAPS will be the first brick of EuPRAXIA, a user facility based on the radiation emitted by electrons plasma accelerated

- The source will be hosted at LNF-INFN
- Several parts will be realized at CNR (Photon Diagnostics) and at Tor Vergata (User end Station)
- INFN-Mi will take care of simulation and data analysis
- Trieste University focuses on applications

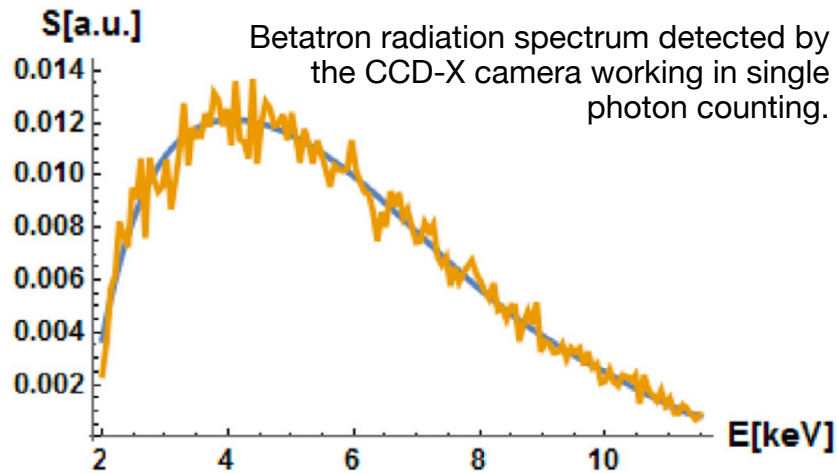
Where	Target
INFN-Mi	Simulation & Data Analysis
LNF-INFN	Plasma source
LNF-INFN	Synchronization
CNR-Potenza	Photon Diagnostics
Tor Vergata	End user station
CNR- Montelibretti	Photon time diagnostics

Parameter	Value	unit
Electron beam Energy	100 - 500	MeV
Plasma Density	$10^{18} - 10^{19}$	$cm^{-3}$
Photon Critical Energy	1 - 10	keV
Number of Photons/pulse	$10^6 - 10^9$	
Repetition rate	1 - 5	Hz
Beam divergence	3 - 20	mrad

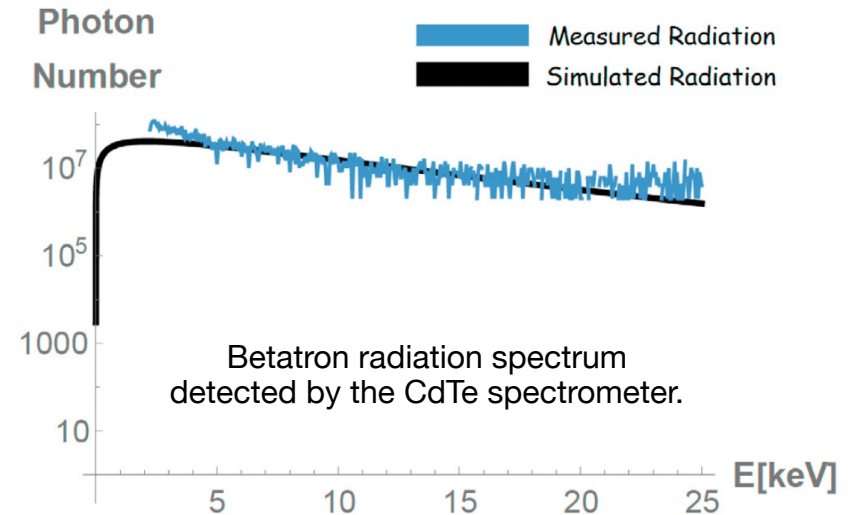
Courtesy A Cianchi



## First Betatron test @FLAME 2016

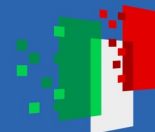


- Laser energy 1 J - temporal length 30 fs - focal spot rms 5  $\mu\text{m}$
- Plasma density  $10^{19} \text{ cm}^{-3}$  - acceleration length 1.1 mm
- $e^-$  energy 300 MeV - energy spread 20% - bunch charge 5 pC



- Laser energy 1.5 J - temporal length 35 fs - focal spot rms 5  $\mu\text{m}$
- Plasma density  $6 \times 10^{18} \text{ cm}^{-3}$  - acceleration length 1 mm
- $e^-$  energy 200 MeV - energy spread 30% - bunch charge 5 pC

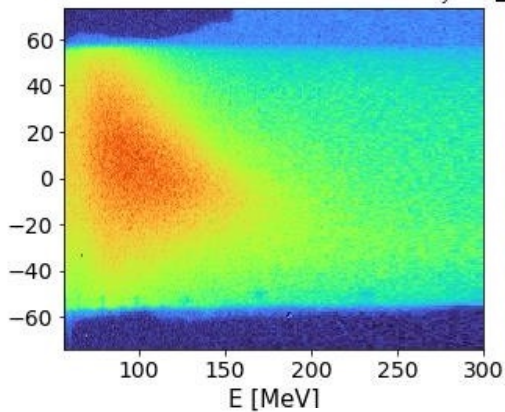
A. Curcio et al., First measurements of betatron radiation at FLAME laser facility, Nucl. Instr. Meth. B (2017), <http://dx.doi.org/10.1016/j.nimb.2017.03.106>



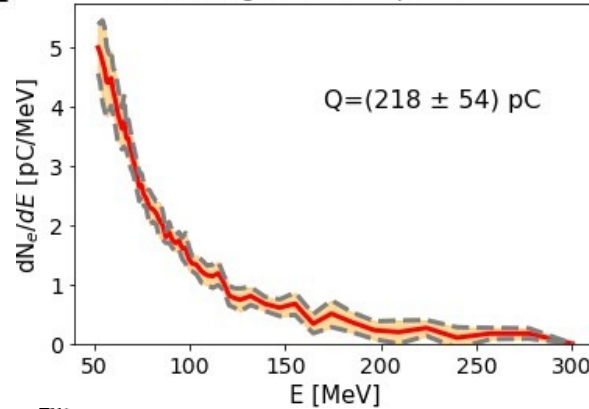
## Ongoing experiments @FLAME

90% He and 10% N

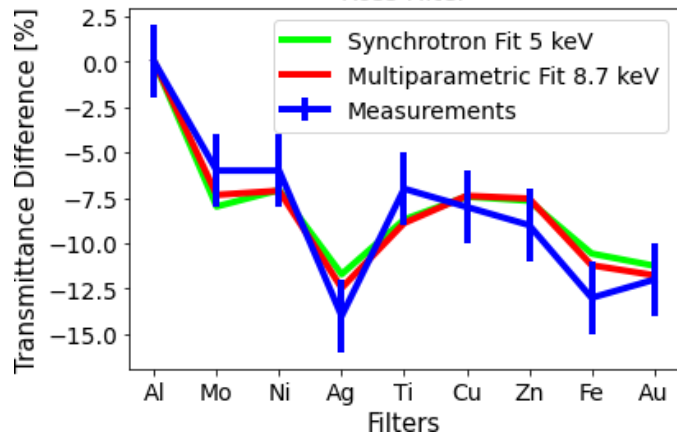
$$\frac{d^2Q}{d\theta_y dE} \left[ \frac{\text{pC}}{\text{mradMeV}} \right]$$



Average Electron Spectrum



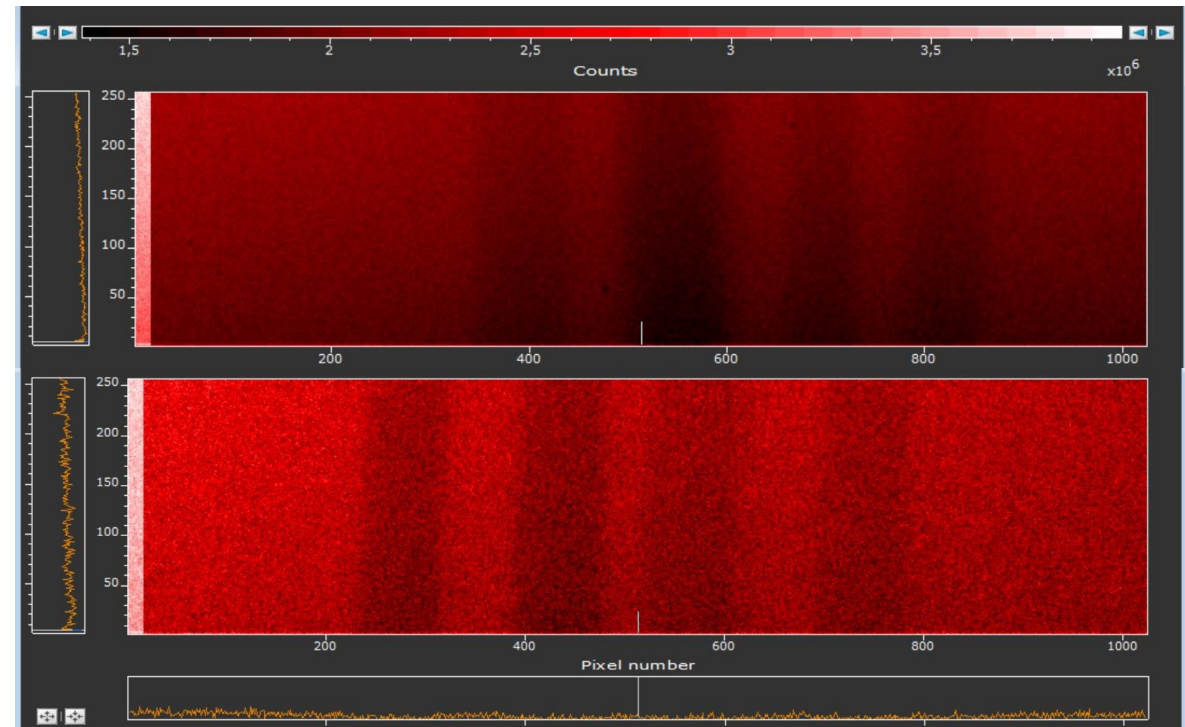
Ross Filter



Ross-filter:

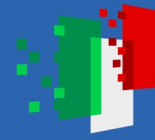
Ti 15  $\mu\text{m}$  – Ag 33  $\mu\text{m}$  – Ni 7  $\mu\text{m}$  – Mo 4  $\mu\text{m}$

Au 6  $\mu\text{m}$  – Fe 25  $\mu\text{m}$  – Zn 10  $\mu\text{m}$  – Cu 8  $\mu\text{m}$

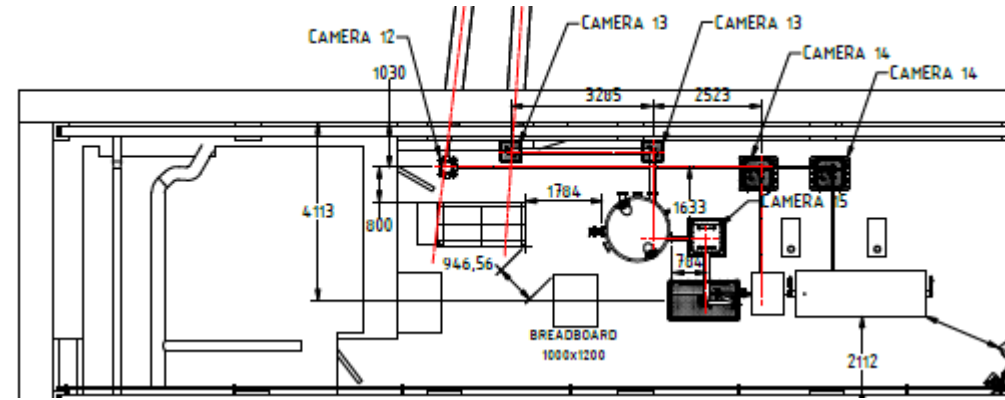
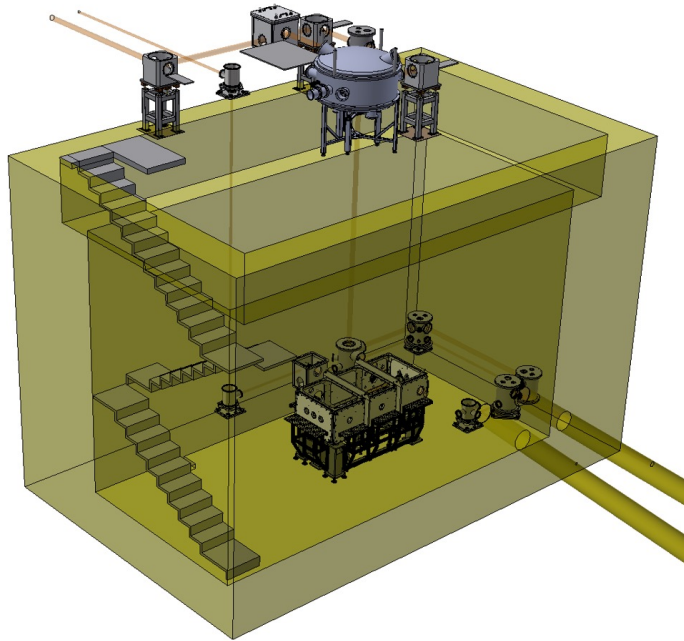


G Costa, A Curcio, M Del Giorno, V Dompè, M Galletti, F Stocchi

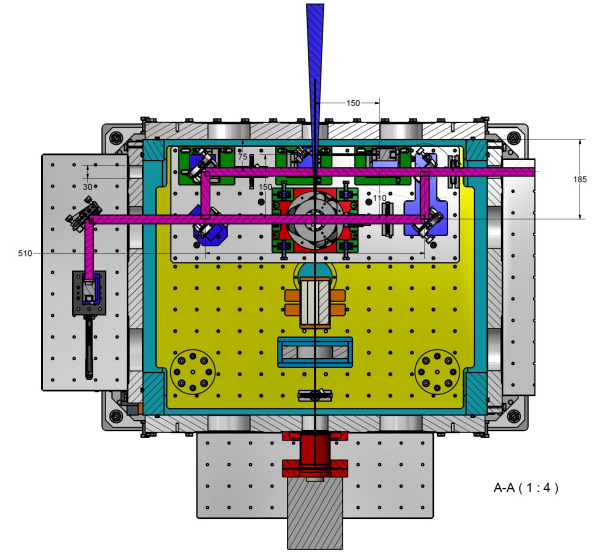




# The EuAPS Layout: FLAME and SPARC bunker

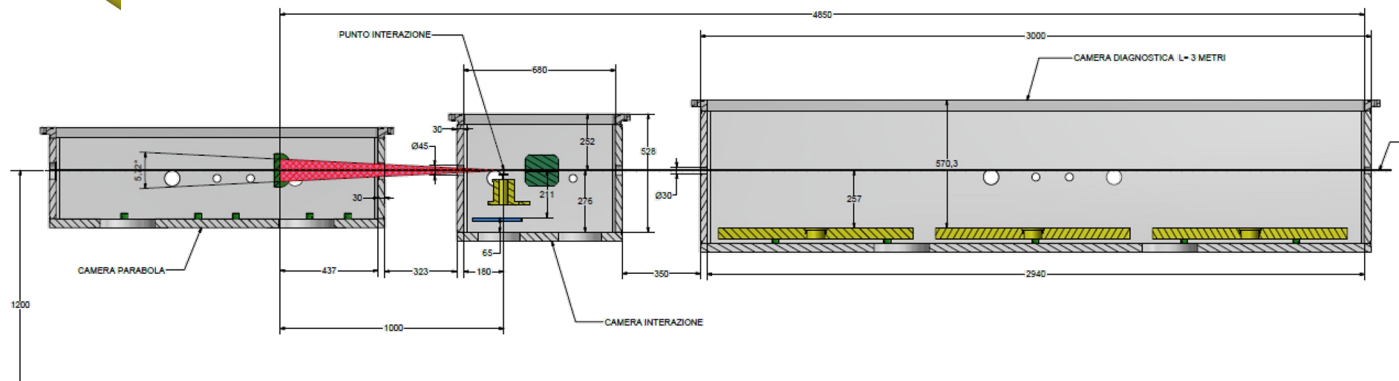


EuAPS beam line in SPARC



Interaction and user chamber

New configuration for EuAPS tests in FLAME

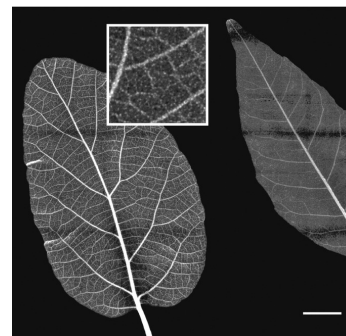


Courtesy S Lauciani

# Photon Science @EuAPS

- Imaging of biological and cultural heritage samples:  
Exploits the brilliance and coherence of betatron radiation, requires small divergence and good focusing
- Static X-ray Spectroscopy and Ultra-fast X-ray spectroscopies:  
The second one requires timing between pump and probe pulses, exploits the fs pulse duration
- Wide angle scattering, diffraction:  
Requires monochromatic beams with high flux

## Imaging – The pilot experiment

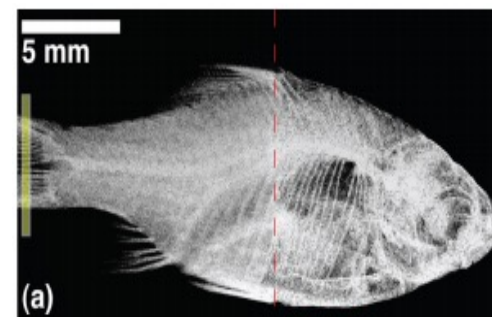


X-ray imaging of leaves (and wood) aiming at the (tens of) microns resolution.

Experiments performed with the broad radiation spectrum filtered by different materials to obtain difference maps emphasizing the presence of heavy metal contaminants → pollution control.

Reale et al. - MIDIX Soft X-rays microradiography

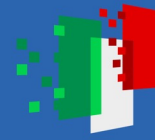
## Single shot phase contrast X-ray imaging:



X-ray absorption contrast image of an orange tetra fish. The spectrum is synchrotron like with a critical energy  $E_c \sim 10$  keV. The phase contrast images are taken in a single shot 30 fs exposure.

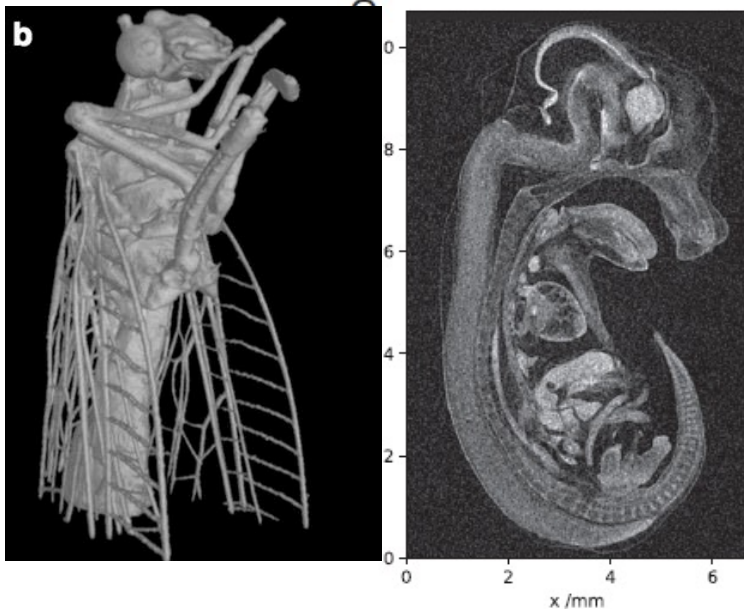
Ref. Kneip, S., et al. "X-ray phase contrast imaging of biological specimens with femtosecond pulses of betatron radiation from a compact laser plasma wakefield accelerator." **APL** 99.9 (2011): 093701.

Courtesy F Stellato



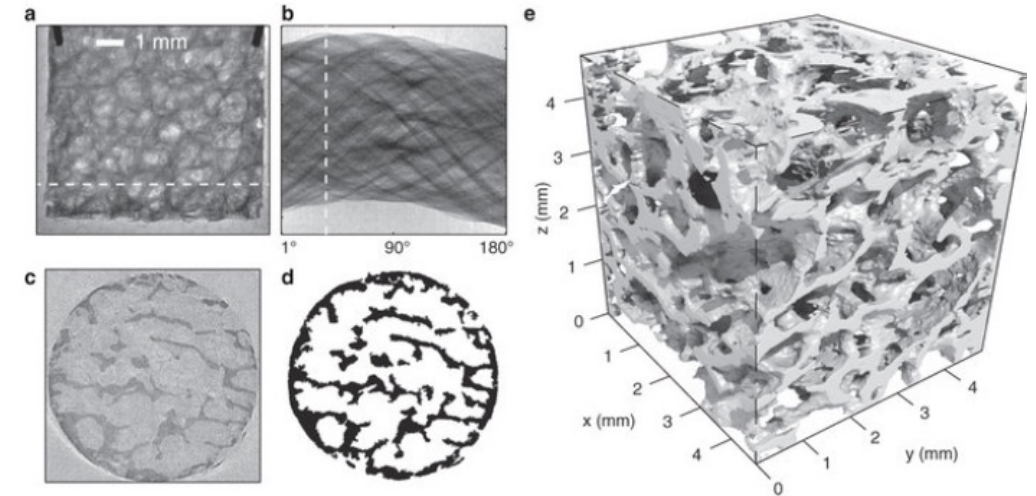
## Imaging, Tomography and Phase Contrast

Betatron sources can fill the gap between synchrotrons and X-ray tubes for imaging and **Computer Tomography (CT)**



Betatron sources have a spatial coherence that allows performing Phase Contrast Imaging (PCI). In PCI, it is measured the difference in wavefront, while in traditional imaging, it is measured the difference in the X-ray absorption coefficient between different objects.

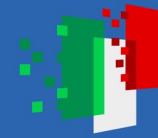
PCI provides better contrast than radiography, especially when dealing with biological samples.



**3D medical imaging:** Tomographic reconstruction of bone sample: (a) A raw image of the bone sample recorded on the xray camera. (c) Application of the inverse Radon transform to the sinogram in (b). (d) Pixels are classified as bone (black) or vacuum (white). (e) Stacking together 1300 slices generates a 3 D voxel map of the bone sample. An isosurface marking the detailed structure of the bone surface is constructed, rendered using a ray-tracing method.

Ref. Cole, J. M., et al. "Laser-wakefield accelerators as hard x-ray sources for 3D medical imaging of human bone." *Scientific reports* 5.1 (2015): 1-7.

Guo *et al.* Scientific Reports 2019  
Cole *et al.* PNAS 2018  
Wenz *et al.* Nature communications 2015



## References on Betatron radiation – SPARC\_LAB Group

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