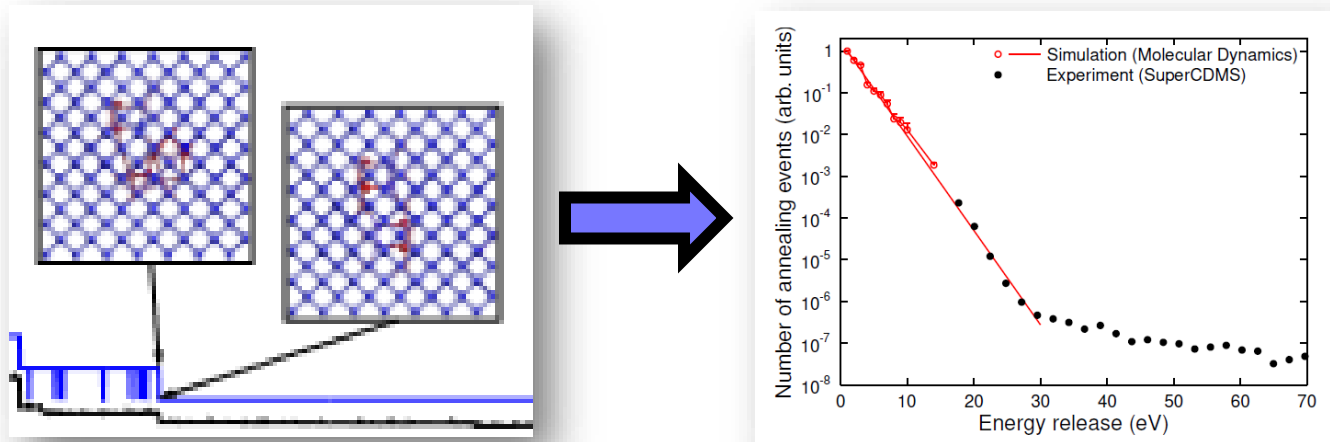




Energy release from recrystallization of amorphous pockets and low-energy excess signals



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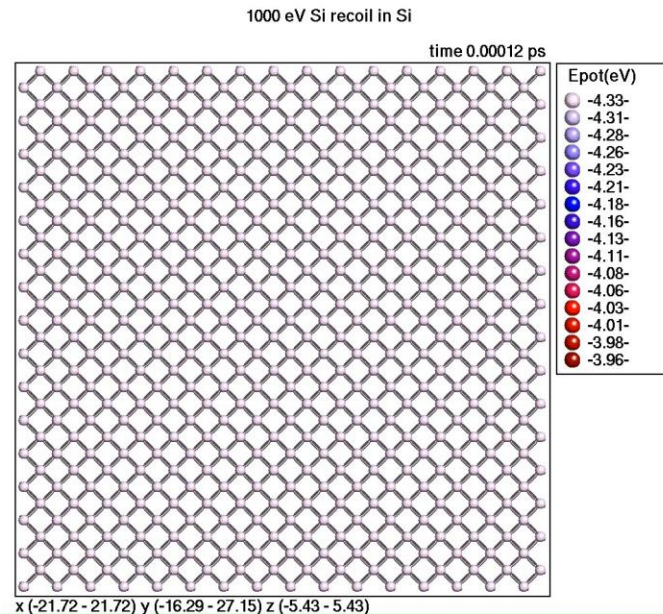
Contents

- Radiation damage in semiconductors: a very brief overview
- Results
 - Damage recombination at ns times after a cascade
 - Energy release spectrum of events
 - Avalanche mechanism of annealing
 - Time scale of annealing events at cryogenic temperatures
- Conclusion



Radiation damage in semiconductors: it is not Frenkel pairs

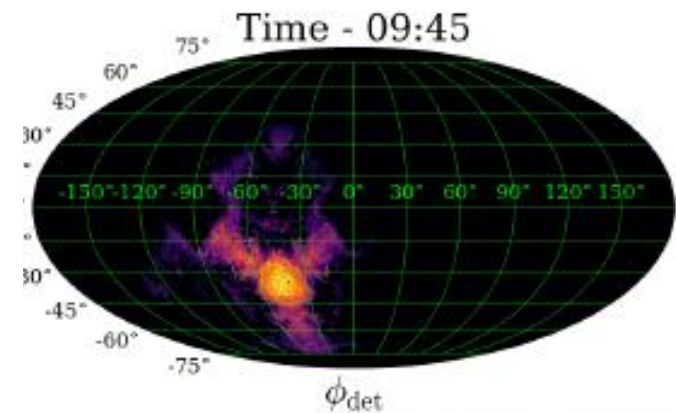
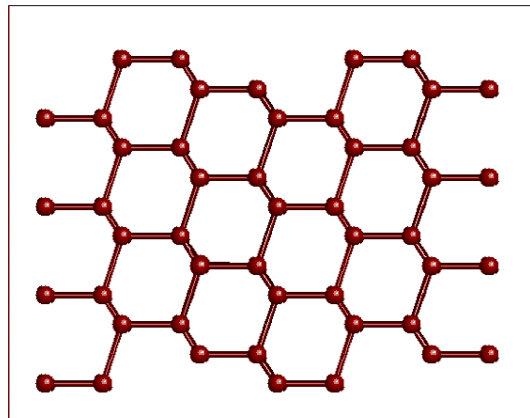
- We have studied damage in a wide range of metals, semiconductors and ionic material over the last 30 years
- For semiconductors, key message: primary damage is practically never simple Frenkel pairs (vacancies and interstitials)





Our previous works on relation of defects and dark matter

- We have previously shown that DM interactions with a single crystalline detector of known orientation may lead to a distinct daily variation in DM observations

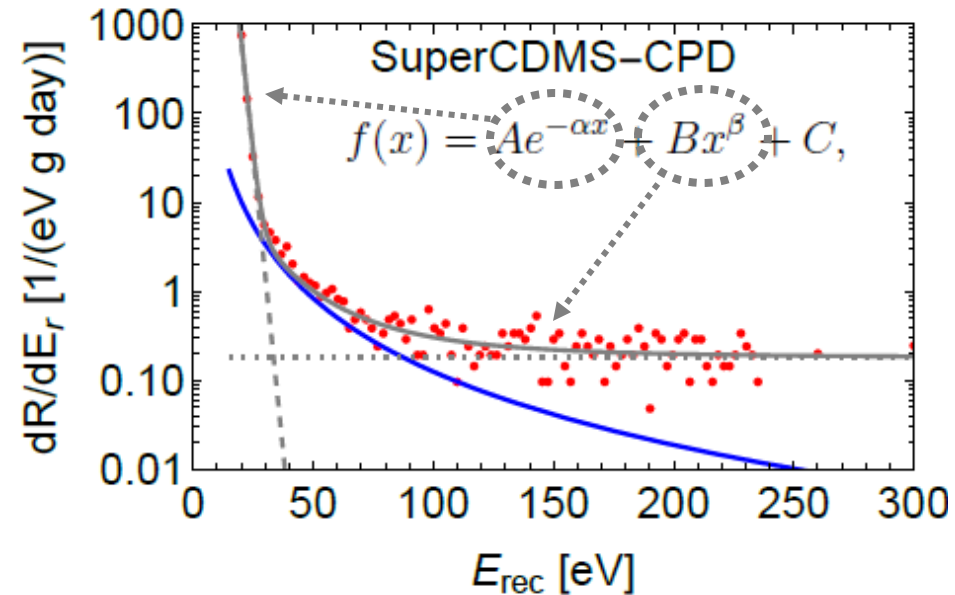
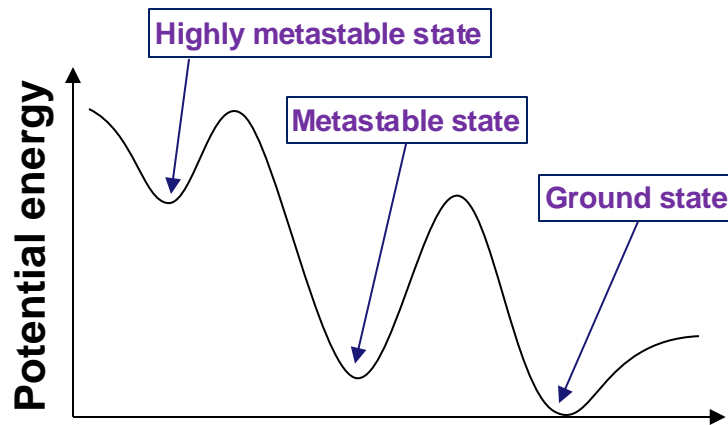


[F. Kadribasic et al., Phys. Rev. Lett. 120, 111301 (2018); F. Kadribasic et al, Journal of Low Temperature Physics 5-6, 1146 (2018); M. Heikinheimo et al., Phys. Rev. D 99, 103018 (2019); S. Sassi et al, Phys. Rev. D 104, 063307 (2021); S. Sassi et al, Phys. Rev. D. 106 (2022) 083009 M. Heikinheimo et a, Phys. Rev. D 106 (2022) 083009]



Recent observations: low-energy excess and defects in solids??

- Defects produced by radiation or other means store energy in solids
- Could the DM excess signal be somehow related to this?



[M. Heikinheimo et al, Phys. Rev. D **106**, 083009 (2022)]



Our hypothesis to be tested

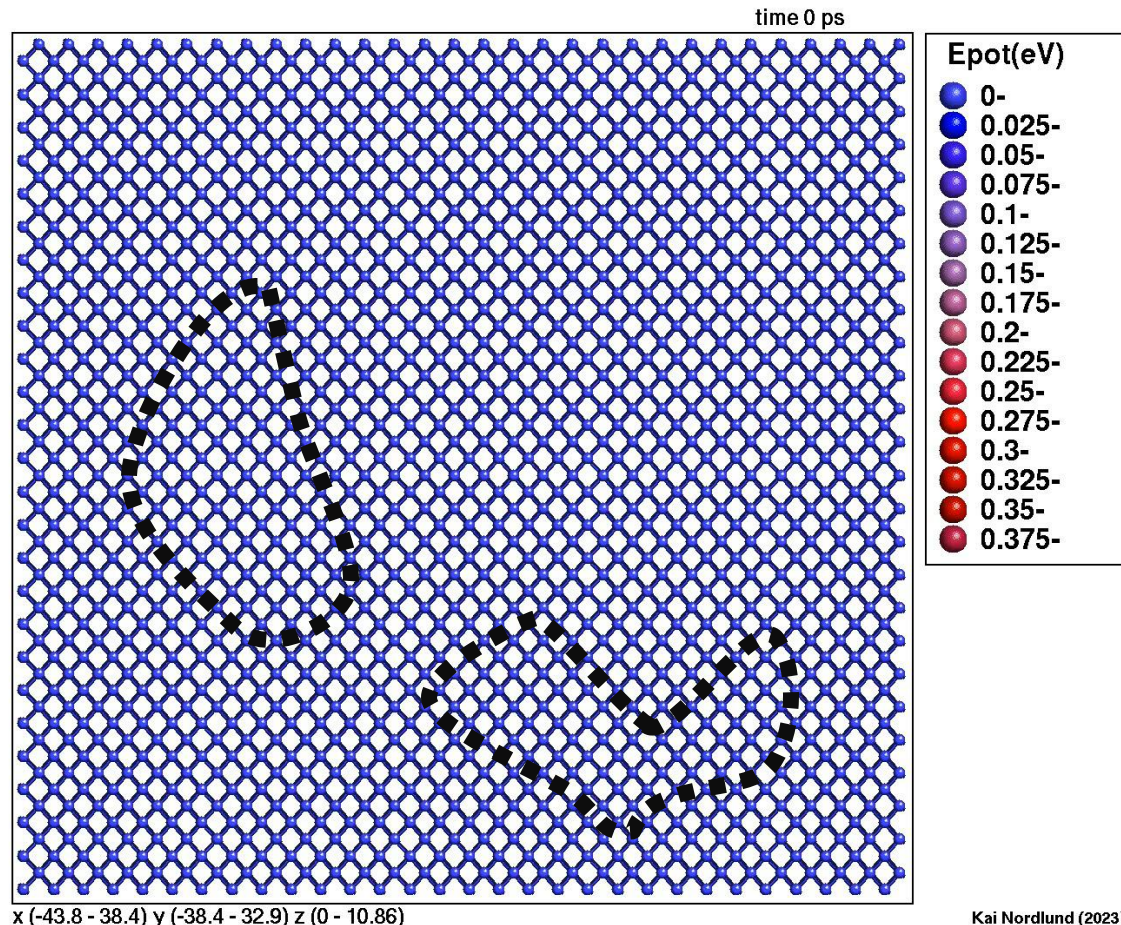
- Could recombination of damage induced by radioactive impurities in the materials or surroundings be a source of energy release
- Decay of radioactive impurity isotopes are a known source of background signal in detectors
- Radioactive impurities are practically impossible to avoid
- Could there be a delayed signal from the damage production?
- We set out to test this systematically, using our best understood material Si as a basis



Annealing simulations, example animation

- Cascade + its annealing at 300 K for 3 ns
 - Extent of damage after cascade shown with dashed lines
- Major annealing observed in the time intervals
 - 20-30 ps
 - 50-60 ps
 - 200-300 ps
 - 900 ps – 1 ns

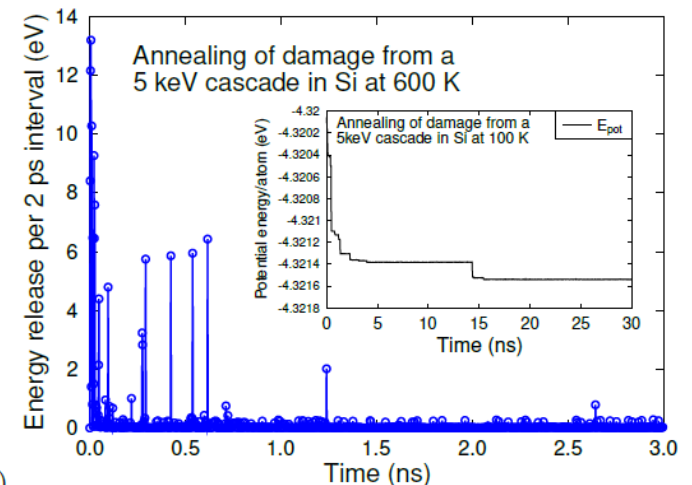
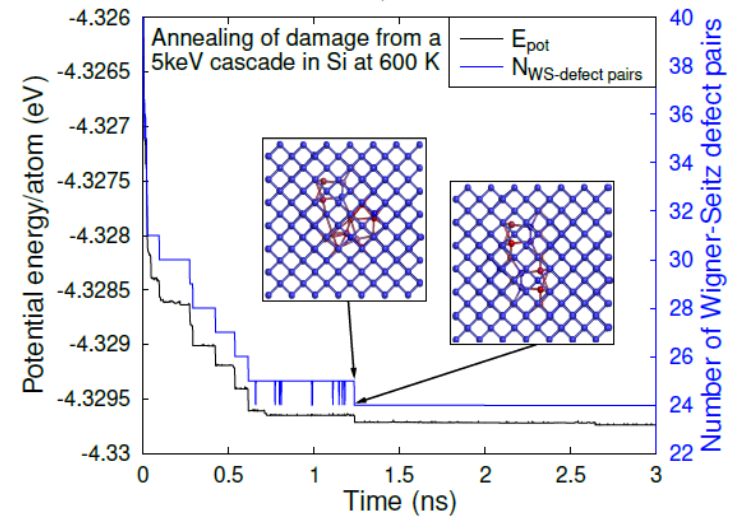
Segment of a cascade induced by a 5 keV recoil in Si + its annealing at 300 K





Systematic analysis of annealing energy release

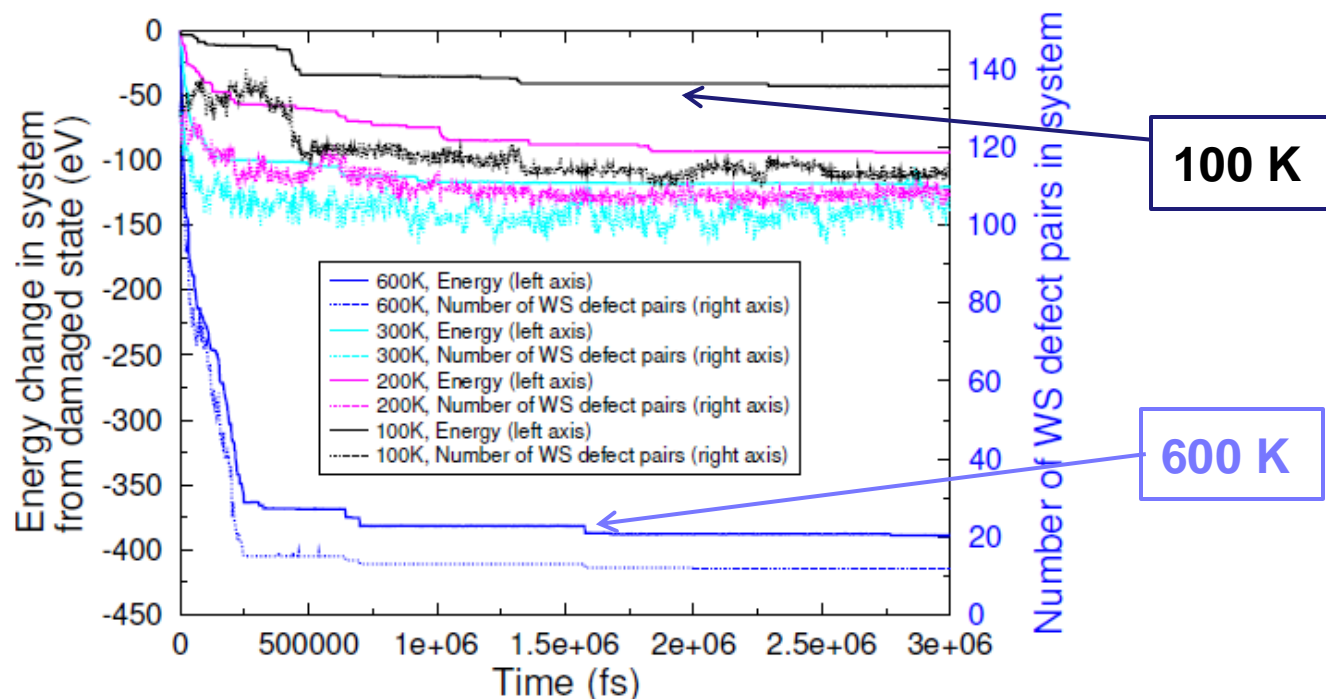
- The annealing runs were systematically analyzed for number of defects and potential energy
- The results show rapid annealing within first ~ 100 ps from damage event, but after that continued intermittent annealing events for as long the simulations were ran – up to 100 ns





Temperature dependence

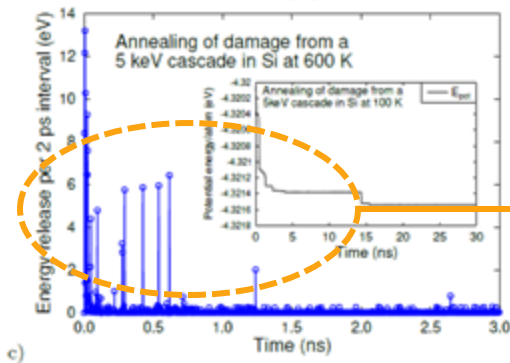
- At 600 K such annealing as been reported many times before
- What was surprising was that similar annealing events were observed even at 100 K and below!



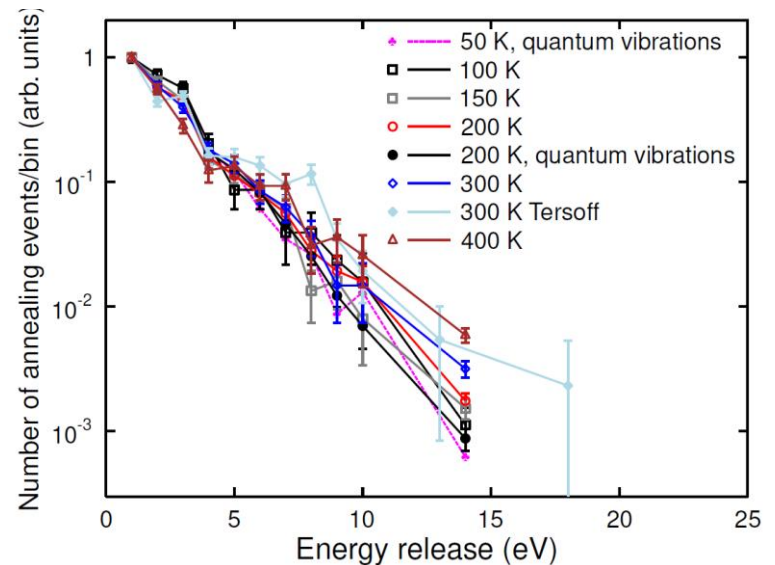


Statistics of energy release

- Taking the energy release peaks from all the independent annealing+quenching runs, one can get a statistical distribution of the energy release
- Remarkably, the slope almost independent of temperature
- Slope also remains the same when the quantum mechanical zero point vibrations are taken into account



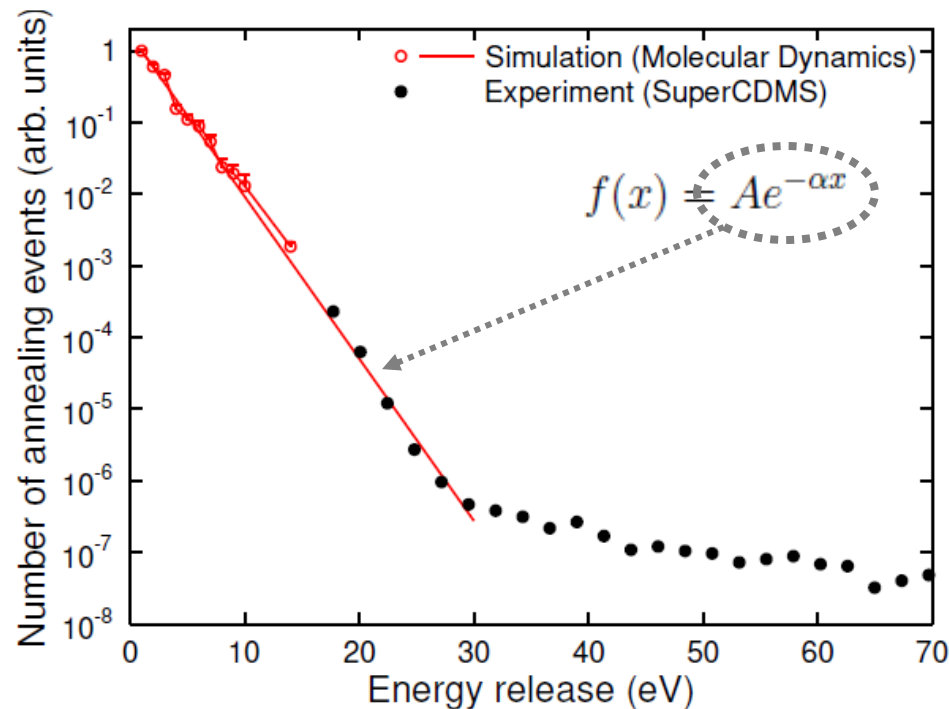
50-5000 runs





Statistics of energy release: comparison with experiments

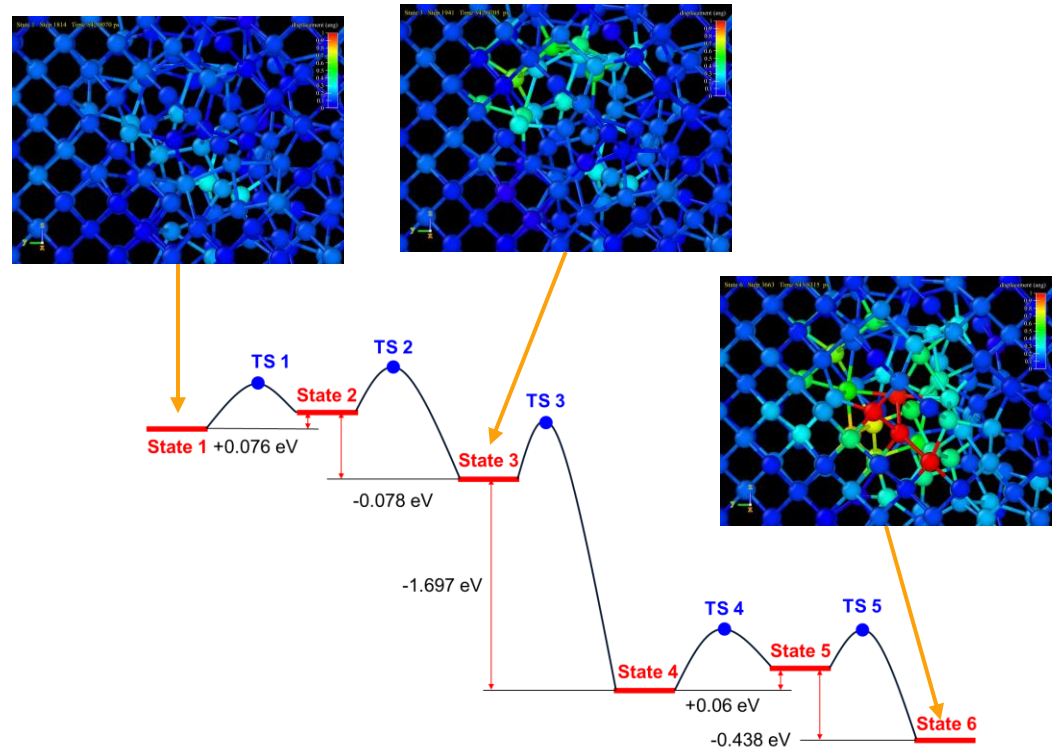
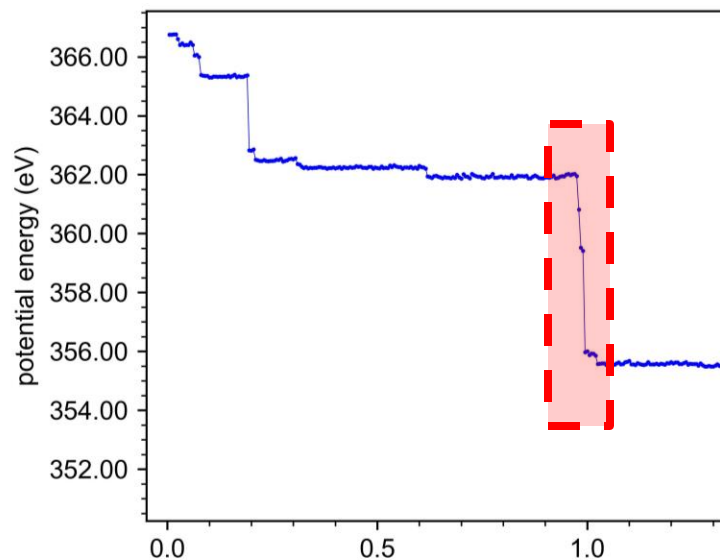
- This data can be compared directly with the experimental low-energy excess exponential tail
- Outstanding agreement!





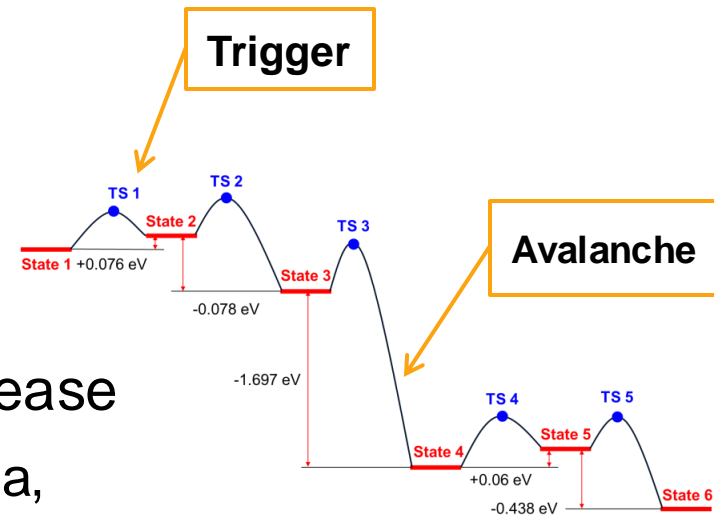
Why is the statistics of energy release independent of temperature?

- To understand why the energy release has practically no dependence on temperature, we analyzed in detail some individual recombination events
- Atoms plotted with displacement color scale



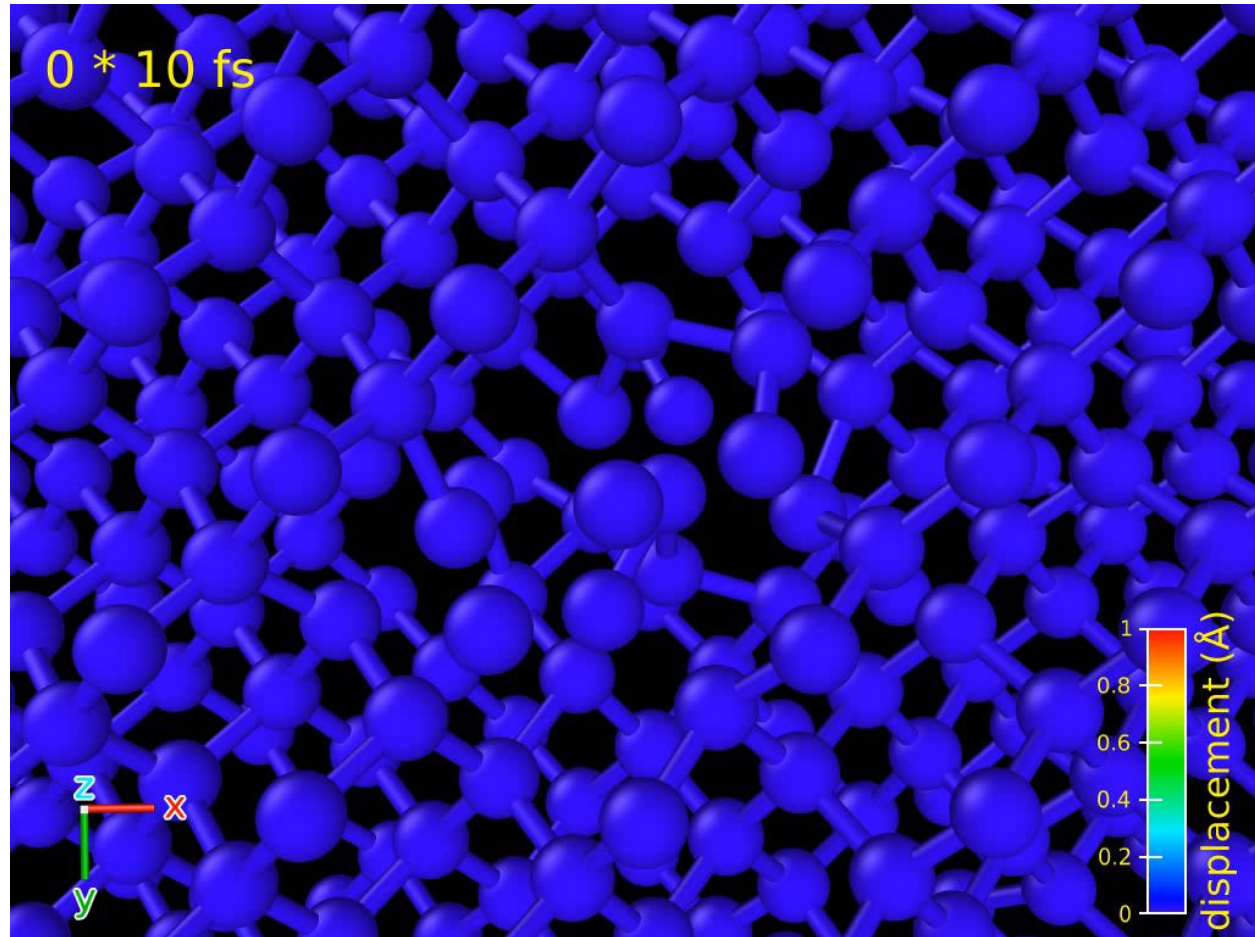
A recombination avalanche

- We observed that the large energy release events are always at low-temperatures preceded by crossing a very small (~ 0.1 eV) barrier
- This initial small rearrangement of atoms slightly heats up the immediate surroundings, which can **trigger** a much larger atom rearrangement and hence energy release
- This is analogous to critical phenomena, such as avalanches in sand piles or snow
- We hence call this a “recombination avalanche” effect
- Such events are observed up to the maximum simulation time of 30 ns – no reason there would be an upper time limit





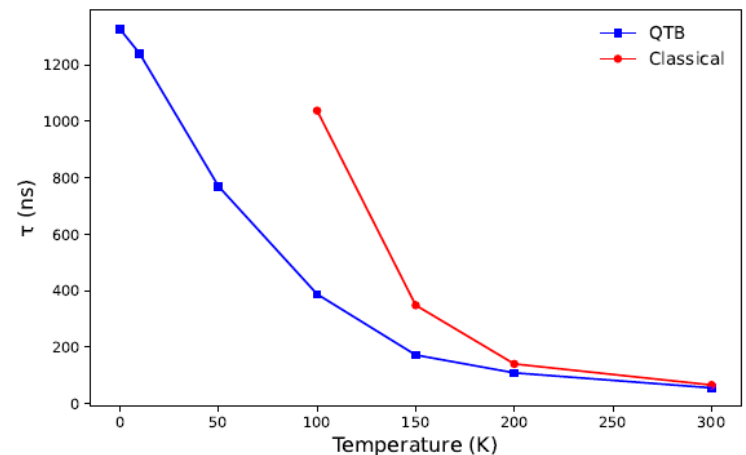
Animation of recombination avalanche





Timescale of events

- In purely classical molecular dynamics, the rate of energy release does slow down with temperature
- At the cryogenic detector temperature of 0.04 K, the rate would be astronomically high (pun intended)
- However, taking into account quantum vibrations, we observe annealing effects even at 0.05 K with a decay time constant of the order of microseconds
- If the **entire macroscopic** detector e.g. undergoes a radioactive decay **anywhere** at rates < 1 event/microsecond, this predicts a roughly constant signal if the time resolution of the detectors is above microseconds





Conclusion

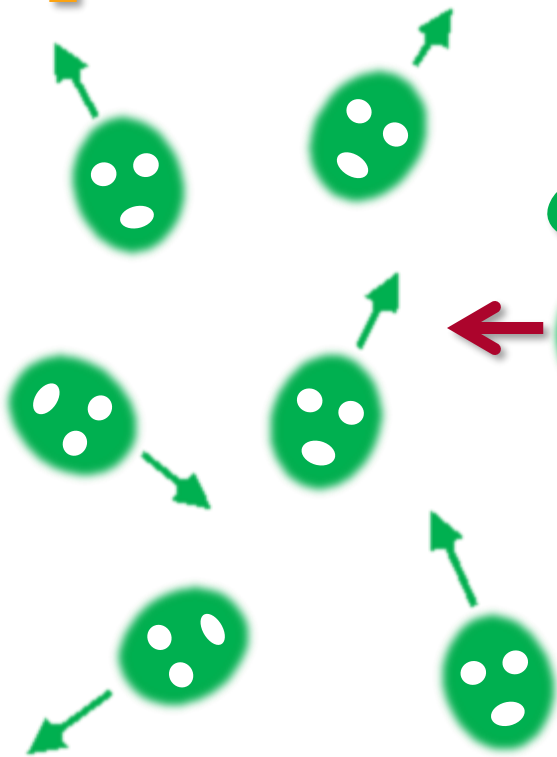


- Energy release from defects in Si follow a very similar exponential energy dependence as the experimentally observed “low-energy excess” in semiconductor detectors
- Defects could be induced by radioactive impurities or possibly also be associated with cracks or other inherent defects
- The energy release is almost independent of temperature due to a “recombination avalanche” effect
- Outlook: nanocalorimetry and/or pulsed ion beam experiments could be used to confirm the effect?



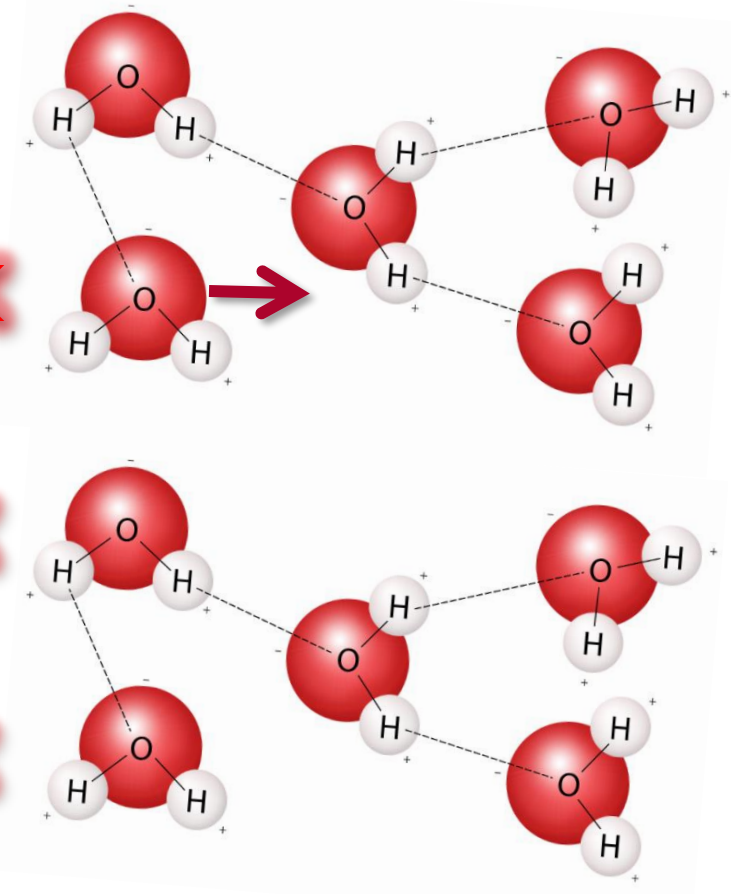
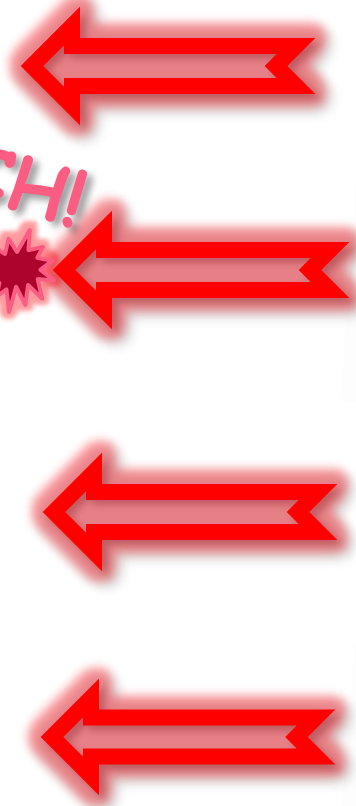
Backup slides

Actually: we are the energetic particles hitting the dark matter!



230 km/s

OUCH!





Kinetic energy transfer from dark matter to ordinary atom nucleus

- Estimation of order of magnitude of energy transfer:
- **Assume** dark matter particle of mass $m_1 = 1 \text{ GeV}/c^2$
- 220 km/s corresponds to $E_{DM} = 269 \text{ eV}$
 - A typical low-energy ion gun energy!
 - From DM density of $\sim 1 \text{ GeV}/\text{cm}^3$ given by astronomical models, we can deduce our bodies pass **through 30 billion DM particles per second.**
- Then we can calculate the energy transfer in a head on collision from basic kinematics to a Si atom ($m_2 = 28 \text{ u}$):

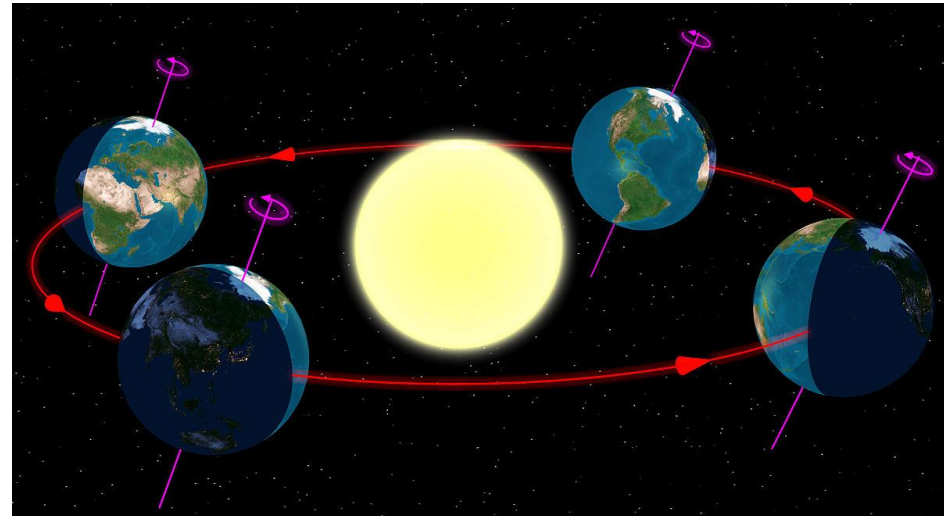
$$T = \frac{4m_1m_2}{(m_1+m_2)^2} E_{DM} = 38 \text{ eV}$$

- This is in the range of threshold displacement energies in Si!



Relative movement effects

- The motion of the sun around the galaxy would give a constant level of recoil energies to ordinary matter from the “WIMP wind”
 - This would be difficult to distinguish from any number of regular background radiation sources
- However, any position on earth rotates around its axis
 - This should give a daily variation in the signal if measured **in a direction sensitive way** from a crystal fixed on earth
- Moreover: the earth rotates around the sun at 30 km/s
 - This should give an annual variation in the signal in a given direction



[Fig: wikipedia]



Key idea: utilize the threshold displacement energy in detection

- In case it so happens that the energy transfer from dark matter to ordinary matter is **around the threshold displacement energy**, then:
 - If you make a single-crystal highly sensitive detector, and fix it on earth, the dark matter detection signal should vary daily!
 - Simplified argument: if the relative motion of the detector w.r.t. the dark matter background is in a direction such that the energy transfer is just below the threshold, no signal, above: clear signal
 - In reality it is of course a convolution of the kinetic energy distribution of dark matter itself, the movement of the earth and the threshold displacement energy surface



Our work: systematic analysis of effect

- Formulate a way to calculate transfer of dark matter particles to ordinary ones
- 1. Distribution of dark matter particle velocities (with galactic escape velocity truncation) in galaxy

$$f_{\text{gal}}(\mathbf{v}) = \begin{cases} \frac{1}{N_{\text{esc}}(2\pi\sigma_v^2)^{3/2}} \exp\left[-\frac{\mathbf{v}^2}{2\sigma_v^2}\right] & \text{if } |\mathbf{v}| < v_{\text{esc}} \\ 0 & \text{if } |\mathbf{v}| \geq v_{\text{esc}} \end{cases}$$

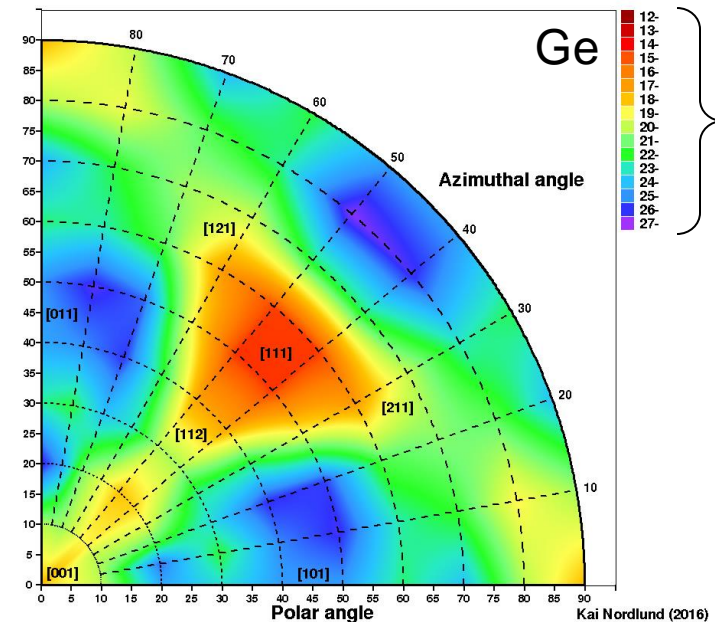
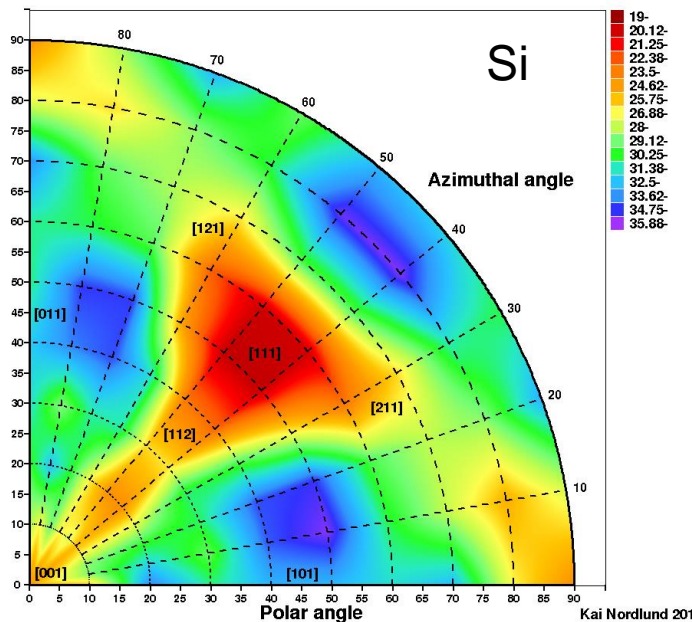
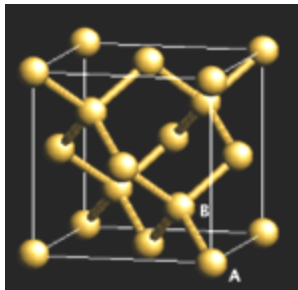
- 2. Radon transform to get to lab coordinates on Earth from motion and rotation of Earth, and movement of solar system around the galaxy

$$\hat{f}_{\text{lab}}(v_{\text{min}}, \hat{\mathbf{q}}; t) = \frac{1}{N_{\text{esc}} \sqrt{2\pi\sigma_v^2}} \times \left[\exp\left(-\frac{|v_{\text{min}} + \hat{\mathbf{q}} \cdot \mathbf{v}_{\text{lab}}|^2}{2\sigma_v^2}\right) - \exp\left(-\frac{v_{\text{esc}}^2}{2\sigma_v^2}\right) \right]$$



Our work: full 3D surface from classical potentials

- We used the DFT results to find which classical interatomic potentials are closest to them
- For Si original Stillinger-Weber potential, for Ge Stillinger-Weber potential modified by Nordlund in 1998
- Then systematic simulations of 85 000 directions in Ge, 24 000 in Si and 5000 in diamond. Results:



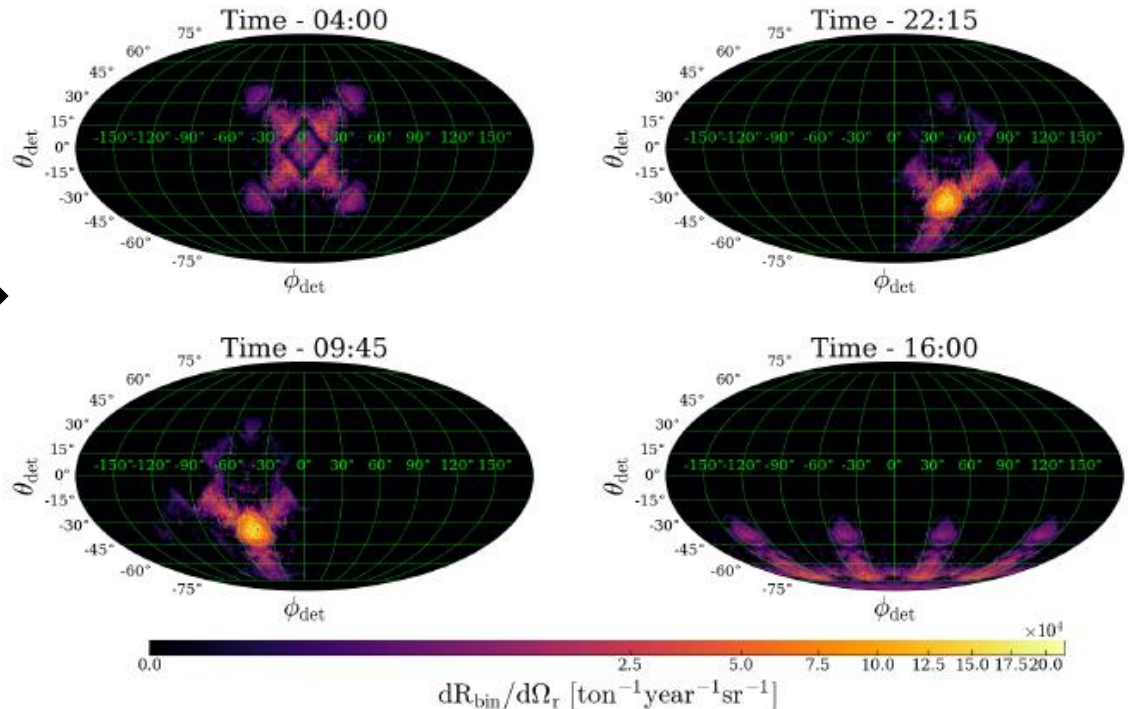
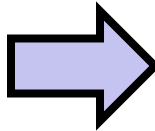
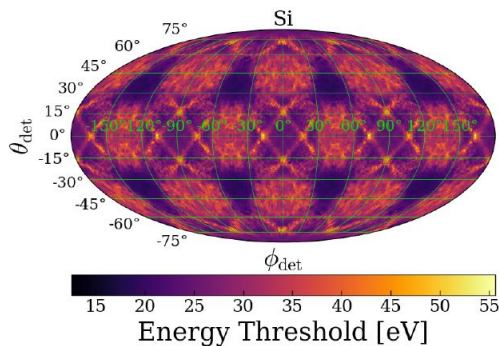
Threshold (eV)



From threshold to signal

- A computer code implementing the numerical convolution integrals 1-4 then allows predicting the dark matter signal for a given (assumed) mass
- Note major differences per time of day

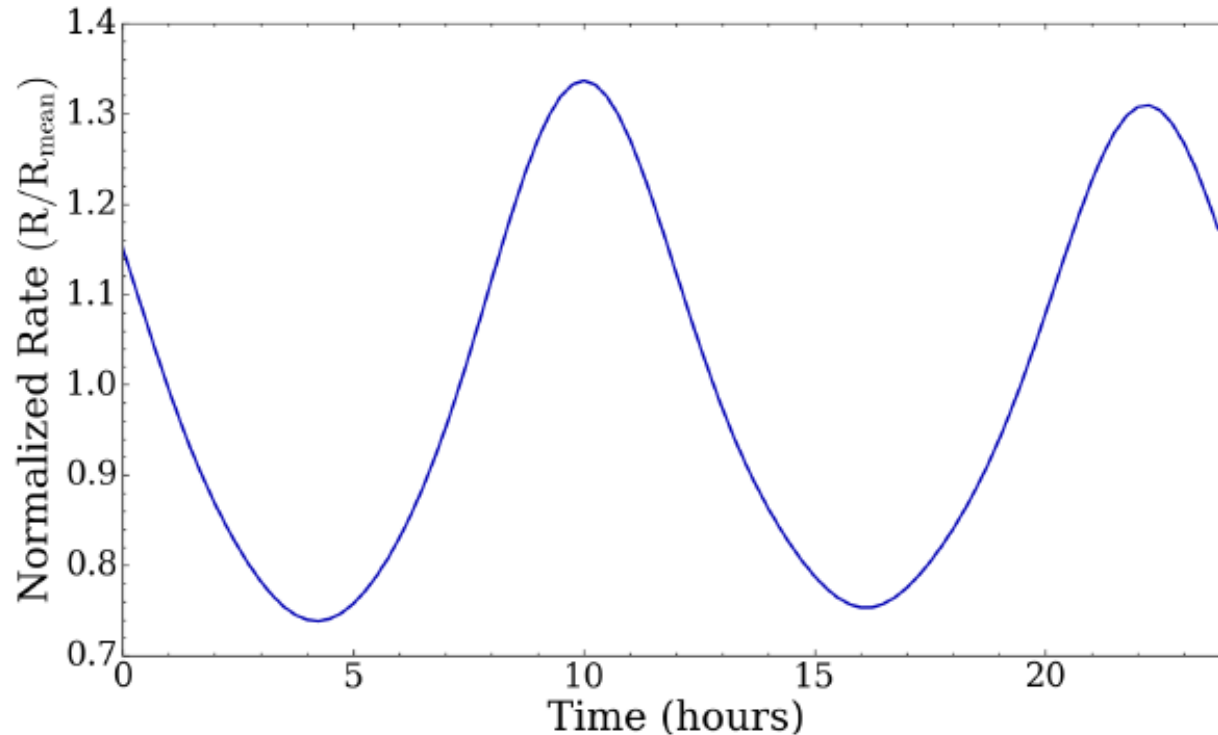
Same Si data in Mollweide plot





Daily variation

- Example for 300 MeV/c² dark matter particle



[F. Kadribasic, N. Mirabolfathi, K. Nordlund, A. E. Sand, E. Holmström, and F. Djurabekova, Phys. Rev. Lett. **120**, 111301 (2018)]



Conclusion

➤ **If:**

- Dark matter exists
- It is composed of particles
- The particles interact with ordinary matter with other means except gravity
- The interaction follows Newton's law of momentum transfer
- The interaction cross section is large enough
- The dark matter particle mass is roughly in the 100 MeV/c² to 10 GeV/c² range
- The detector can actually be built
- **Then:** the approach we developed should be able to detect dark matter, and distinguish it from other particles thanks to a distinct diurnal variation
- **Else:** even if dark matter is never detected, **the detectors developed are incredible and will certainly be useful for other purposes!**

Probability??

- 99%
- 99%
- 1%
- 99%
- 1%
- 4%
- 99%
= 4×10^{-6}