

# Hubble constant estimation from GW and EM joint measures

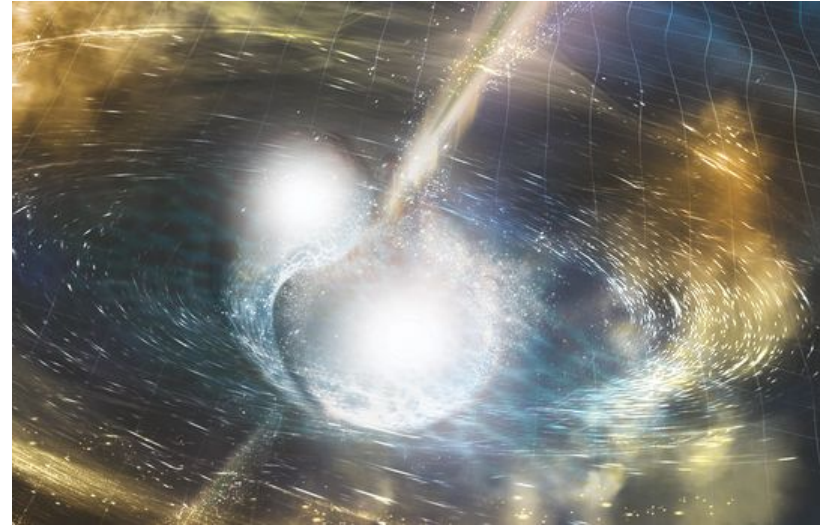
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and Luigi Piro (*IAPS/INAF*), Francesco Pannarale (*Sapienza*), Hendrik Van Eerten (*University of Bath*), Fulvio Ricci (*Sapienza*), Geoffrey Ryan (*Perimeter Institute for Theoretical Physics*)

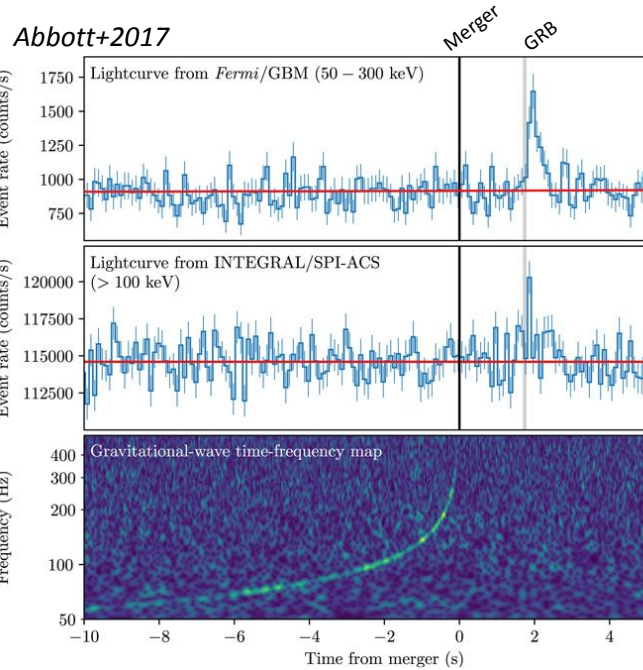


# Outline

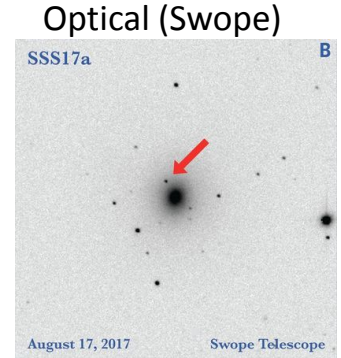
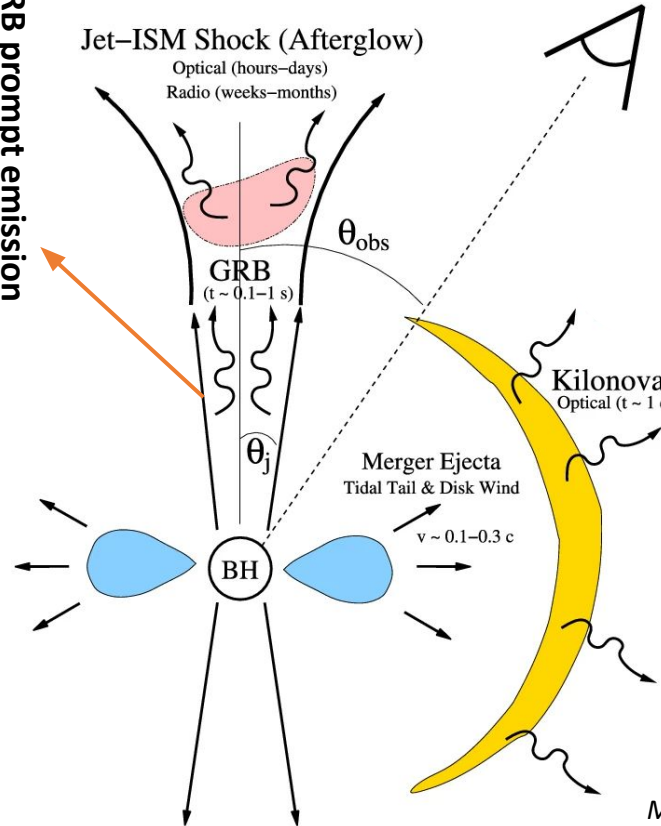
1. Introduction: binary neutron star mergers and GW170817
2. Methods: joint fit of gravitational waves (GW) and electromagnetic (EM) domains
3. GW170817: two types of analysis
4. GW170817: the estimation of the Hubble constant ( $H_0$ )
5. Future prospects
6. Conclusions



# Binary neutron star (BNS) mergers: GW170817

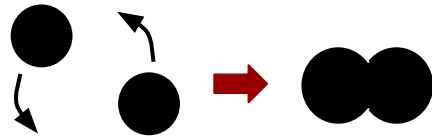


GRB prompt emission



**Kilonova**  
~11 hrs after the merger

Gravitational wave



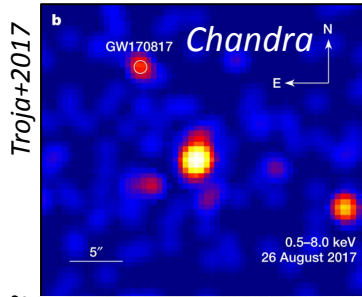
Neutron stars spiraling

Merger

*Coulter+2017*

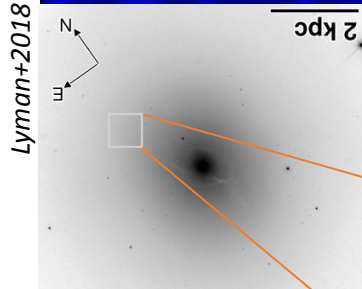
*Metzger, Berger+2012*

# Binary neutron star (BNS) mergers: GW170817

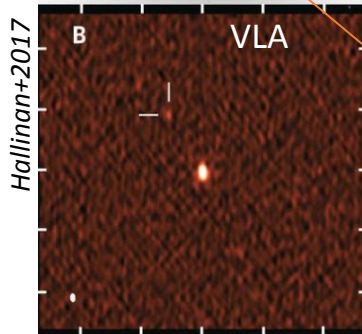
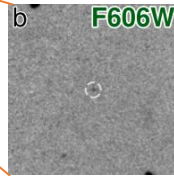


**Afterglow:**  
Long lasting emission:

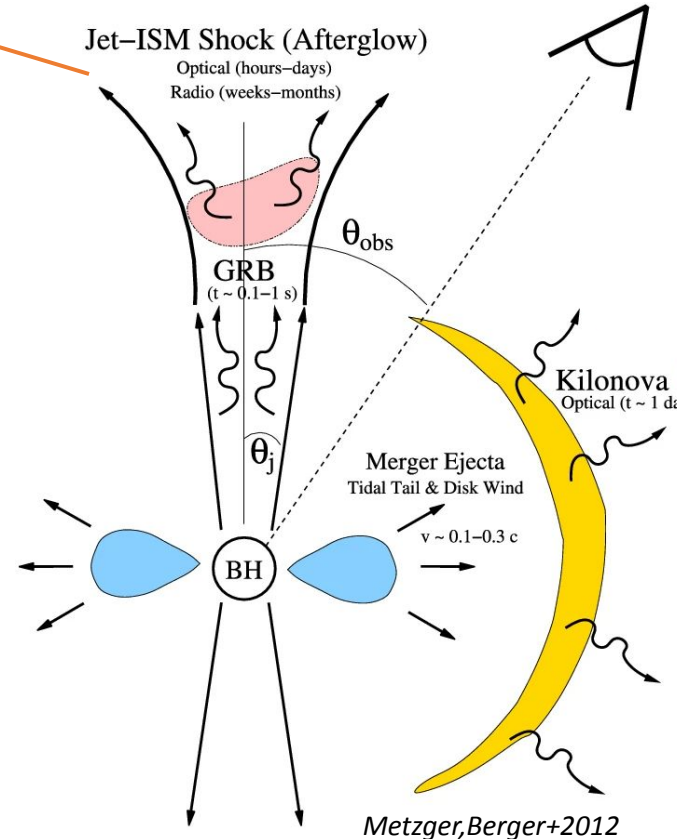
**X-rays**  
9 days after the merger



**Optical**  
Visible when the kilonova started fading  
~100 days after the merger

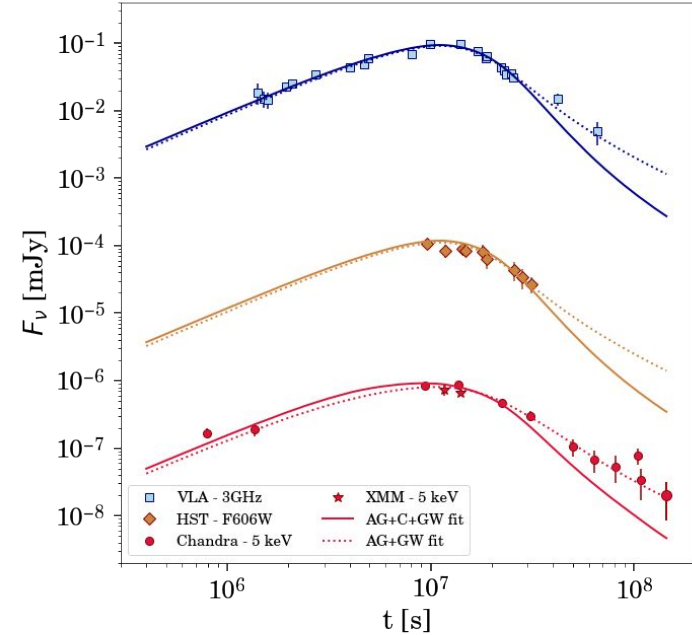
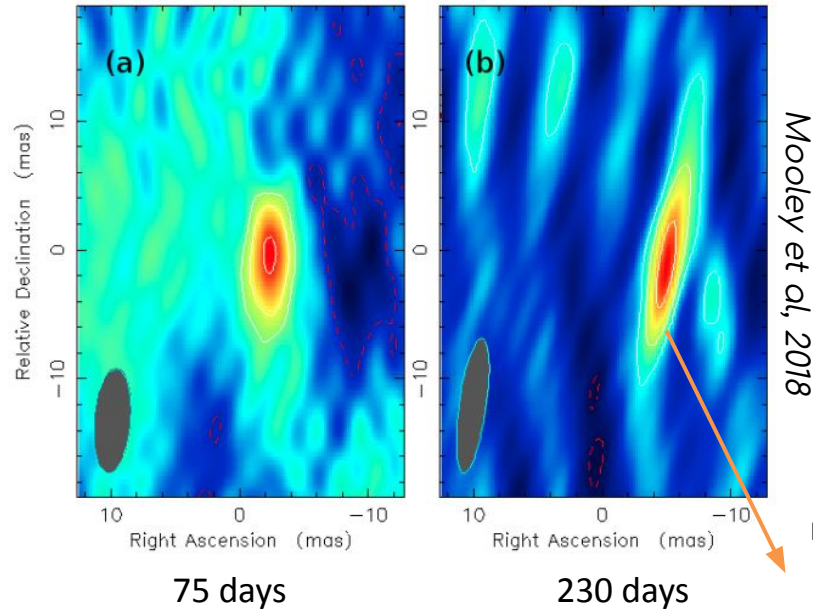


**Radio**  
16 days after the merger



# GW170817 observations

**Centroid motion of the relativistic jet**  
 Radio Observations taken with VLBI (Very Long Baseline Interferometry)  
 @ 75, 206, 230 days



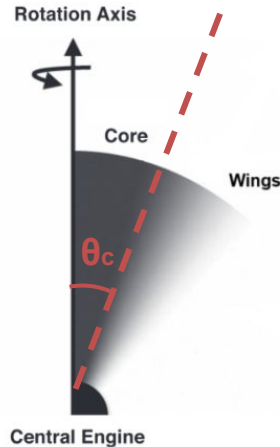
**Afterglow light curve**  
 Observations in X-rays, optical  
 and radio bands

# GW170817 jet type

Scenario i: Uniform Top-hat Jet



Scenario ii: Structured Jet

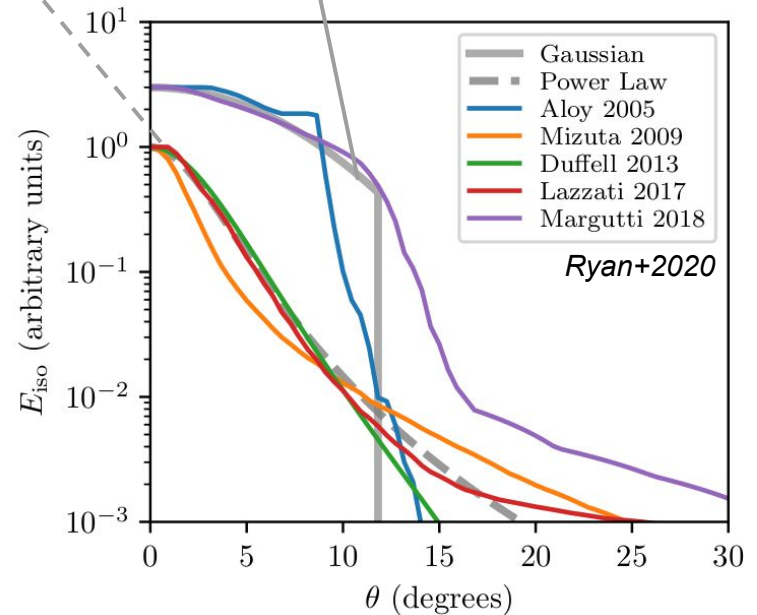


Power law jet:

$$E(\theta) = E_0 \left( 1 + \frac{\theta^2}{b\theta_c^2} \right)^{-b/2}$$

Gaussian jet:

$$E(\theta) = E_0 \exp\left(-\frac{\theta^2}{2\theta_c^2}\right)$$



# GW and afterglow modelling

A novel approach to asses these problems is a joint analysis of GW and EM domains:

## Afterglow

Synchrotron parameters

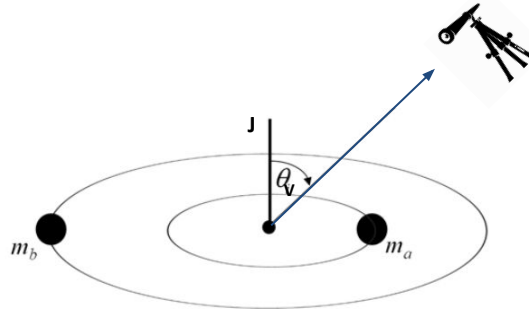
Energetics

Geometry:

*Jet core angle,*

*Viewing angle/Inclination*

*Luminosity distance*



## Gravitational Waves

Intrinsic parameters

*NS Masses, spins and tidal parameters*

Extrinsic parameters

*RA, Dec*

*Inclination*

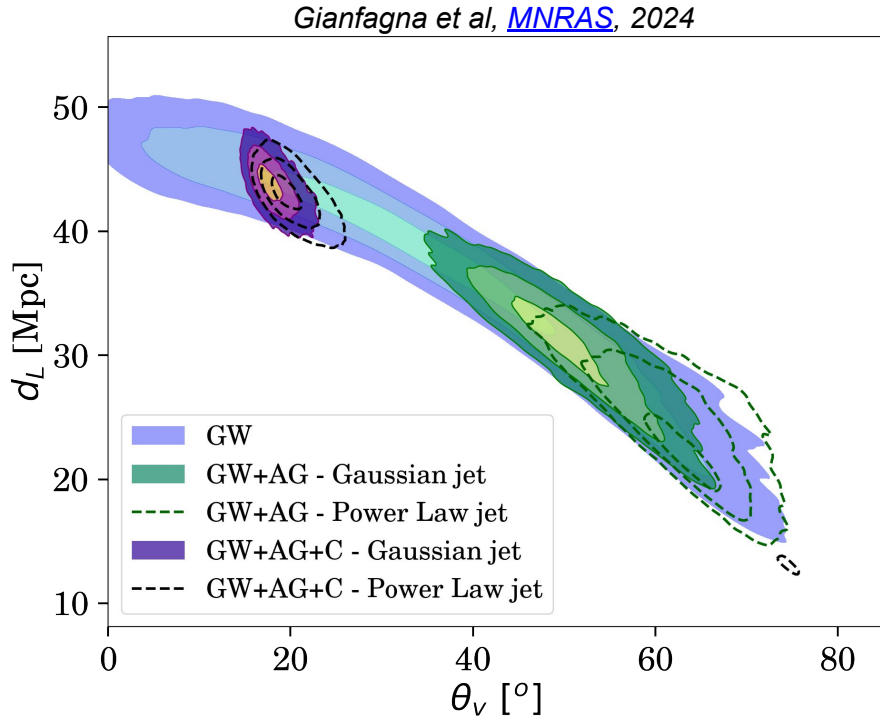
*Luminosity distance*

Shared parameters!





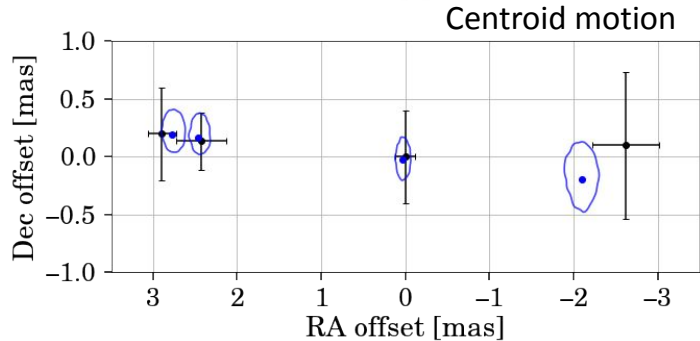
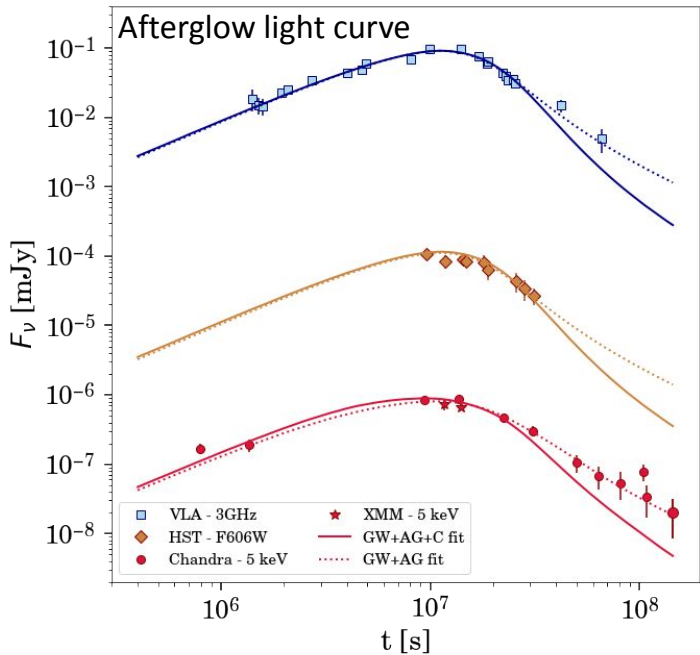
# The need for a joint analysis: $d_L - \theta_v$ degeneracy



- Far source
- Binary orbit facing Earth
- Close source
- Highly inclined

GW-only:  $H_0 = 77^{+21}_{-10} \text{ km s}^{-1} \text{ Mpc}^{-1}$

How to break this degeneracy?  
 With an independent dataset:  
**Afterglow**

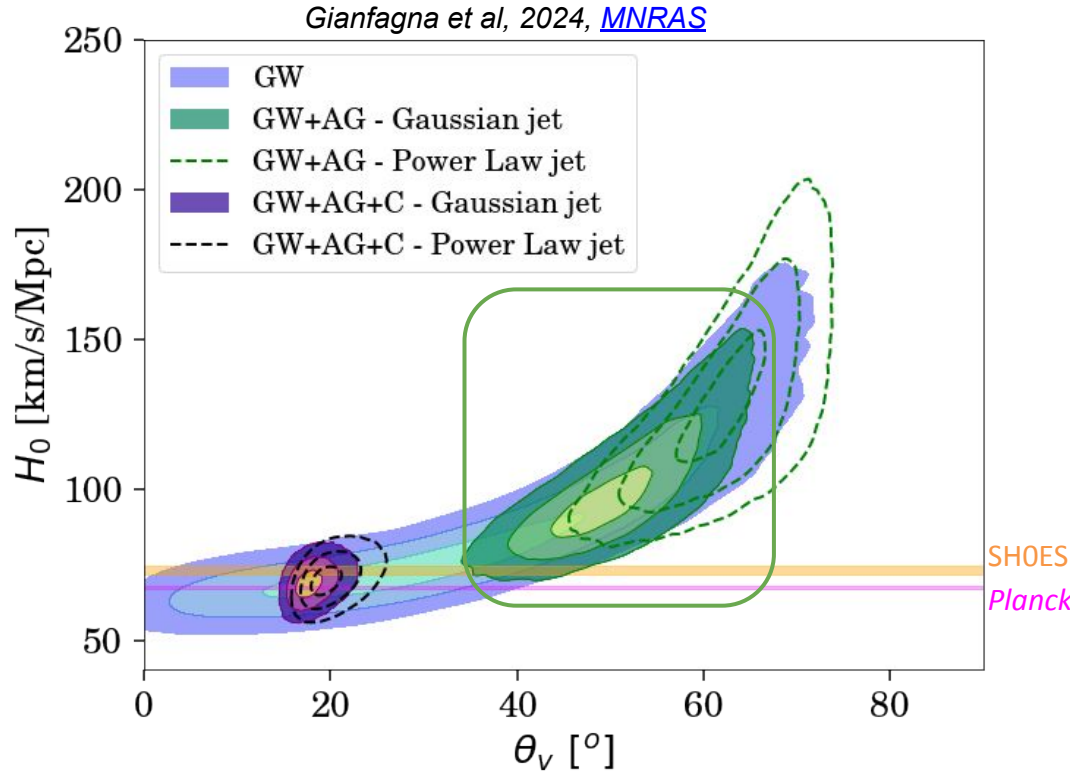


# Two kinds of analysis

1. GW and Afterglow light curve (**GW+AG**):
  - a. Wider jet
  - b. Less energy on the jet axis
  
2. GW, afterglow light curve and centroid motion (**GW+AG+C**):
  - a. Collimated jet
  - b. Energetic

Parameter	GW-only	GW + AG GJ	GW+AG + C GJ
$\log_{10} E_0$	–	$52.31^{+0.82}_{-0.80}$	$54.50^{+0.28}_{-0.33}$
$\theta_c [^\circ]$	–	$7.73^{+0.86}_{-0.80}$	$2.85^{+0.24}_{-0.20}$

# GW+AG: the Hubble constant



Problem of the flux excess  
at late times

$d_L$ [Mpc]	$31.3^{+3.0}_{-3.6}$
$\theta_v$ [deg]	$50^{+5}_{-5}$

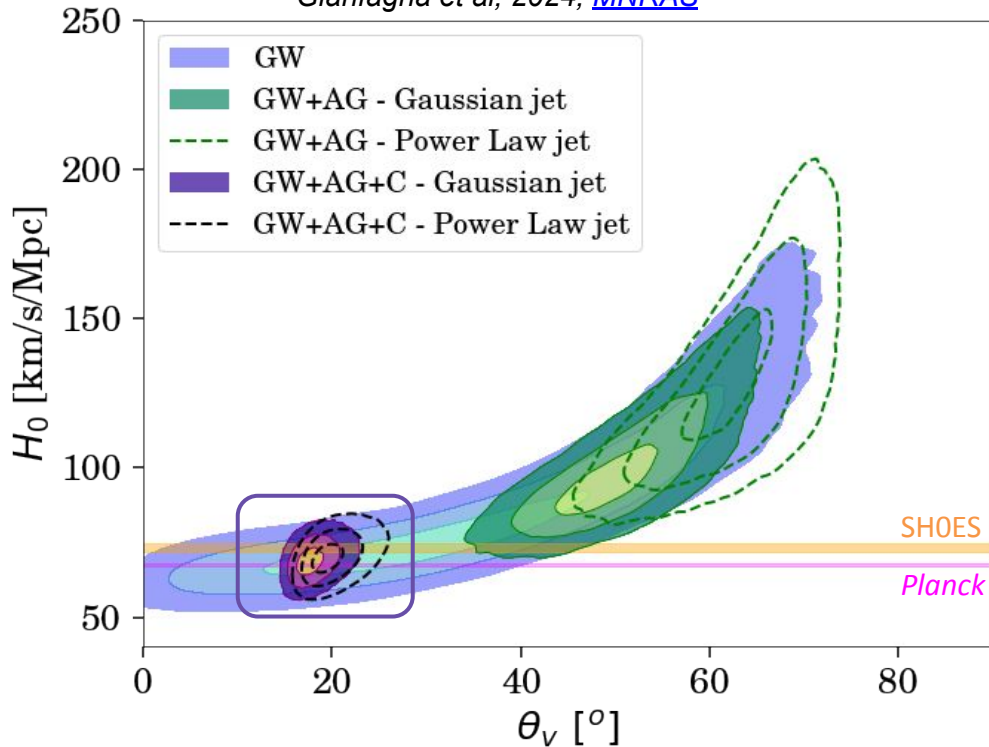
$$H_0 = 96^{+13}_{-10} \text{ km s}^{-1} \text{ Mpc}^{-1}$$

$$H_0 = 77^{+21}_{-10} \text{ km s}^{-1} \text{ Mpc}^{-1}$$

20% error

# GW+AG+C: The Hubble constant

Gianfagna et al, 2024, [MNRAS](#)



Afterglow and centroid **break** the degeneracy!

$$H_0 = 77^{+21}_{-10} \text{ km s}^{-1} \text{ Mpc}^{-1}$$

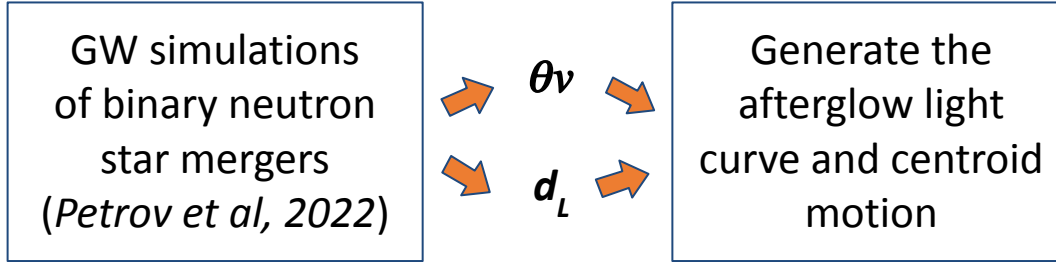
$$H_0 = 69.0^{+4.4}_{-4.3} \text{ km s}^{-1} \text{ Mpc}^{-1}$$

Seems to prefer  
*Planck*  $H_0$

3x more precise  
than GW

$d_L$ [Mpc]	$43.7^{+1.4}_{-1.4}$
$\theta_v$ [deg]	$18.2^{+1.2}_{-1.5}$

# How likely is a new centroid measurement?



Considering VLBI sensitivity (24  $\mu$ Jy) and resolution (1.5 mas)

$H_0$  uncertainty: 4 km/s/Mpc    10 km/s/Mpc

		GW rates	GW+AG+C rates	GW+AG rates
O5	~ 2027	$180^{+220}_{-100} \text{ yr}^{-1}$	$0.2^{+0.2}_{-0.1} \text{ yr}^{-1}$	$10^{+13}_{-6} \text{ yr}^{-1}$

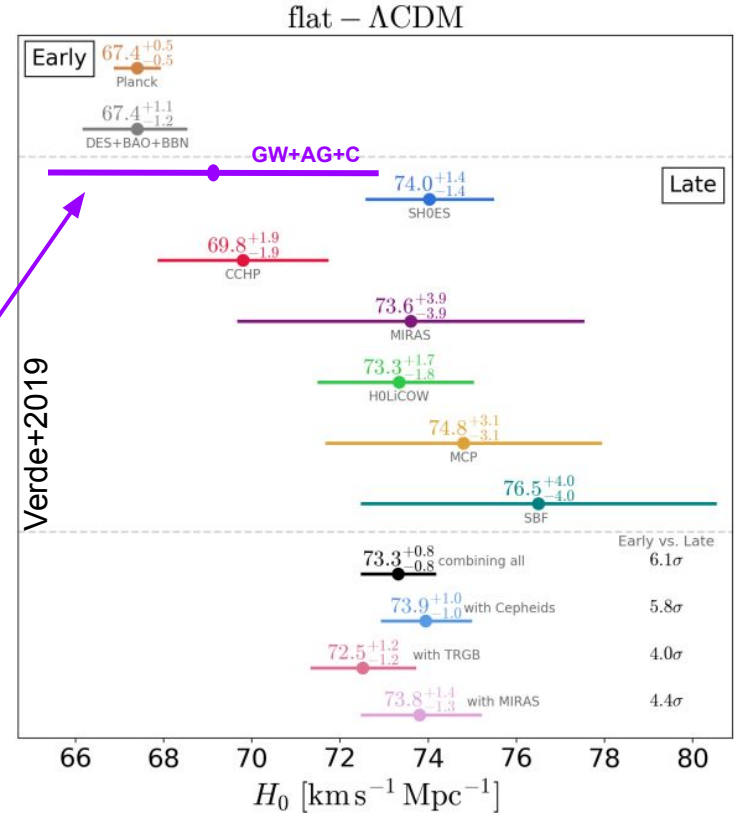
~10 events per year in **O5**.

At the end of O5 we could be able to reach the **SHOES** sensitivity of **1.5 km/s/Mpc**

# Conclusions

From GW and afterglow emission from **binary neutron star mergers**, we can estimate the Hubble constant, independently from any distance ladder:

- $\theta v-d_L$  degeneracy: plays a crucial role in its estimation;
- Considering the complete dataset, the **uncertainty** on  $H_0$  is still **large** ( $\sim 4$  km/s/Mpc), with respect to the *Planck* and SHOES measurements ( $< 1.5$  km/s/Mpc);
- We need more events ( $\sim 30$ ) to get to the SHOES precision.





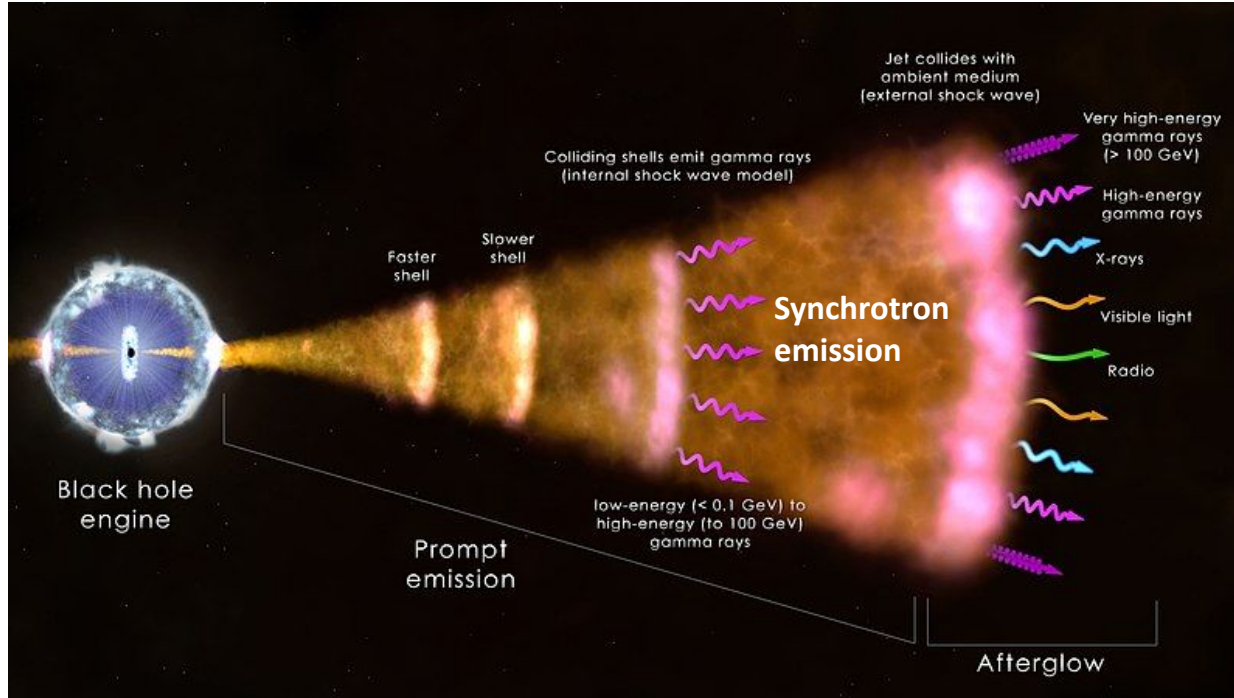
Vulcano Workshop 2024 - Frontier Objects in Astrophysics and Particle Physics

*THANK YOU for your attention!*

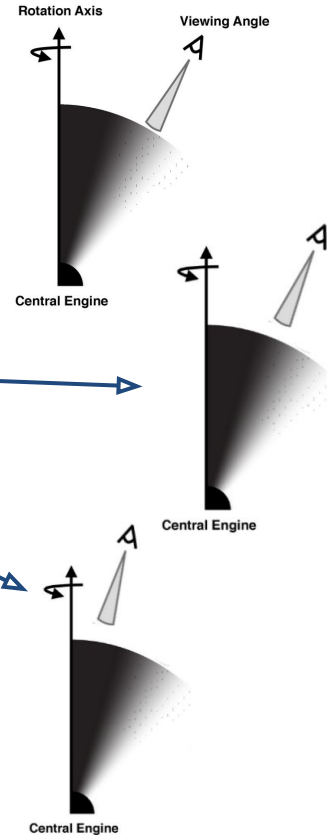
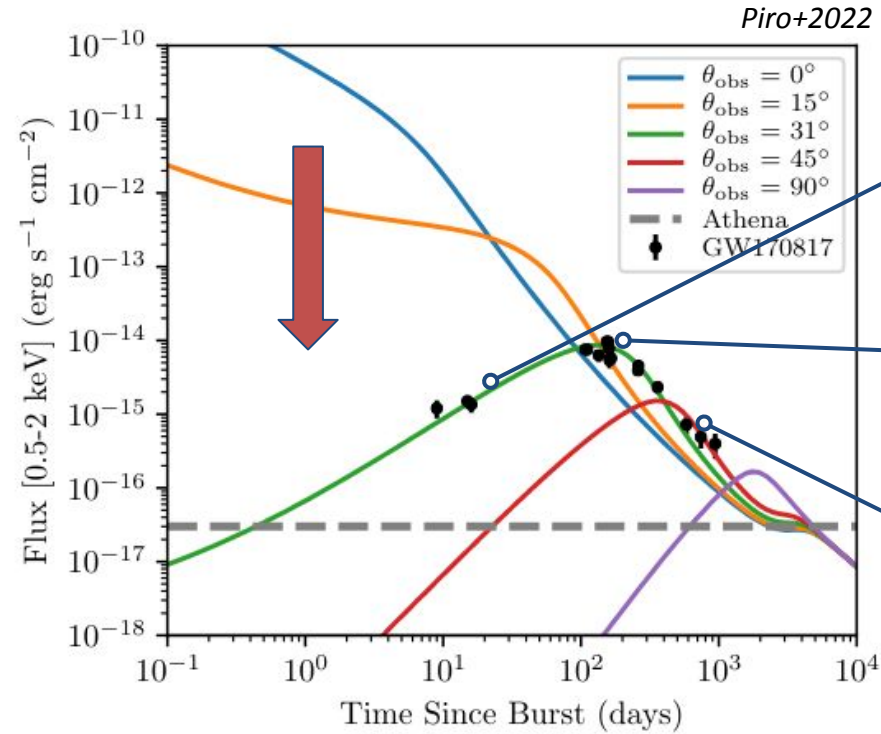
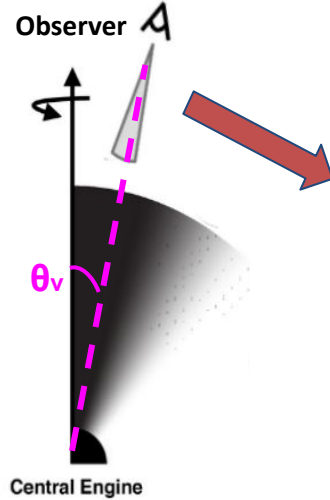
# Backup slides



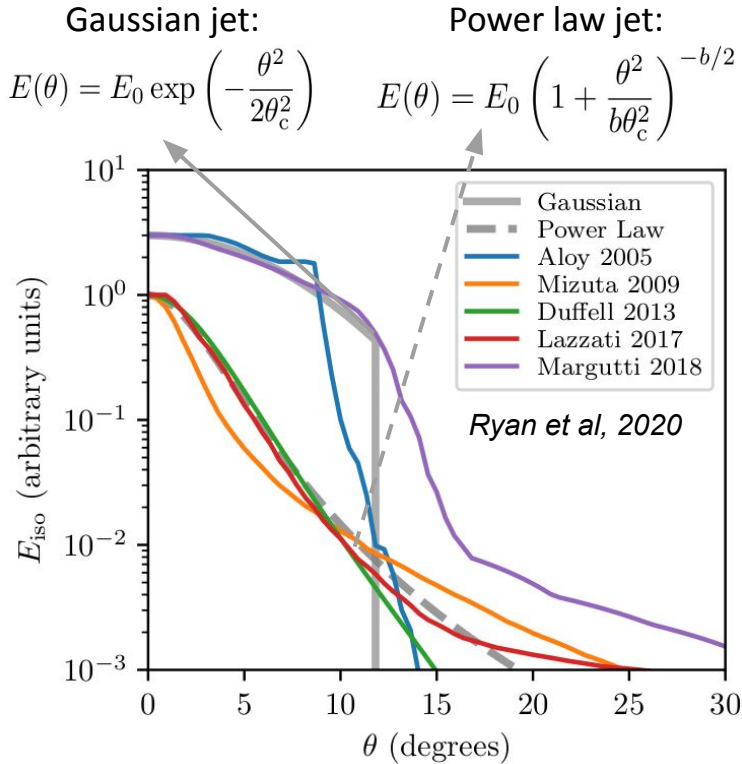
# Gamma Ray Bursts (GRBs)



# Off-axis observers



# Afterglow modeling



•Model: **afterglowpy** (Ryan et al, 2020)

$\theta_V$  Jet orientation

$\theta_c$  Opening angle of the jet

$E_0$  Isotropic equivalent energy

$n_0$  homogeneous circumburst medium number density

$\theta_W$  Jet total width

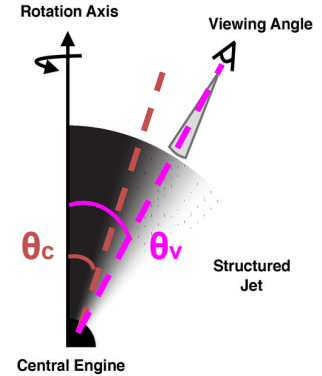
$p$  power-law slope of the electron population

$\epsilon_e$  fraction of post-shock internal energy in the accelerated electron population

$\epsilon_B$  fraction of post-shock internal energy in magnetic field

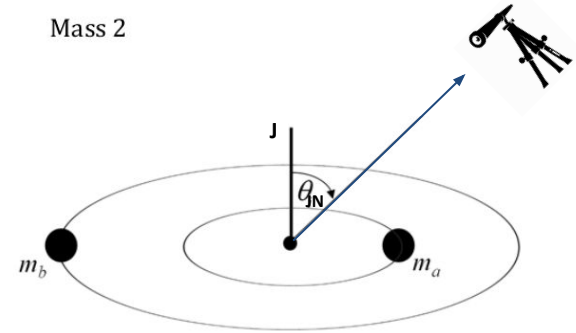
$b$  power law index (only for power law jet)

$d_L$  luminosity distance



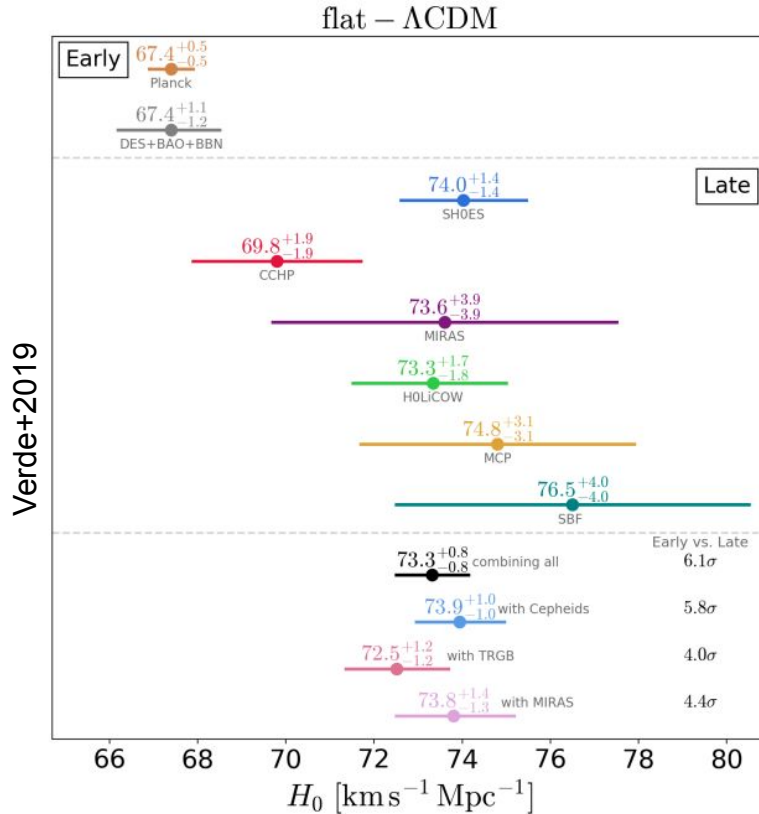
# GW modeling

Intrinsic	1	$\mathcal{M}$	Chirp mass	} or {	$m_1$	Mass 1
	2	$q$	Mass ratio		$m_2$	Mass 2
	3	$a_1$	Spin amplitude 1			
	4	$a_2$	Spin amplitude 2			
	5	$\theta_1$	Tilt angle between the spin 1 and the orbital angular momentum			
	6	$\theta_2$	Tilt angle between the spin 2 and the orbital angular momentum			
	7	$\phi_{1,2}$	Azimuthal angle between the spin vectors			
	8	$\phi_{jl}$	Azimuthal angle between total angular momentum and orbital angular momentum			
Extrinsic	9	$d_L$	Luminosity distance	} FIXED to NGC 4993		
	10	DEC	Declination			
	11	RA	Right ascension			
	12	$\cos(\theta_{JN})$	Cosine of the inclination angle	} or {	$\theta_{JN}$	Inclination angle
	13	$\psi$	Polarization angle			
	14	$\phi$	Phase			
	15	$\Lambda_1$	Tidal deformability parameters of the primary neutron star	} or {	$\tilde{\Lambda}$	Dimensionless tidal parameters
	16	$\Lambda_2$	Tidal deformability parameters of the secondary neutron star		$\tilde{\delta\Lambda}$	



EM+GW parameters

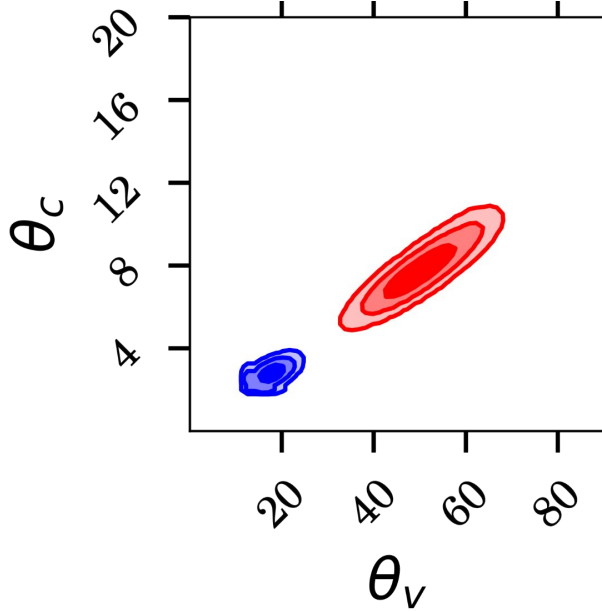
# Hubble tension



$\sim 5$  sigma **tension** between the **Hubble constant  $H_0$**  estimated with:

- Late time Universe (for example SH0ES);
- Early time Universe (for example *Planck*).

# EM degeneracy



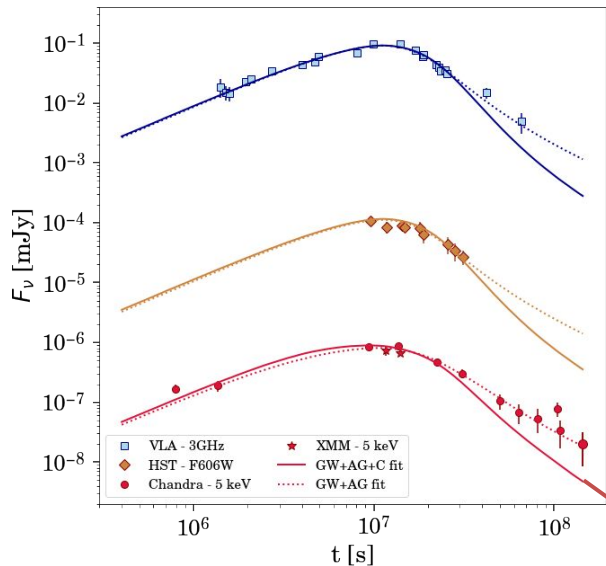
$\theta_c$ : jet opening angle

$\theta_v$ : viewing angle

GW+AG+C analysis

GW+AG analysis

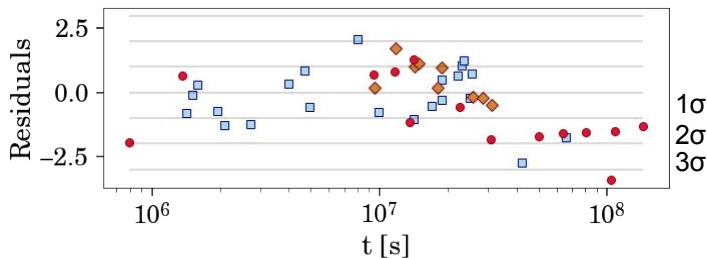
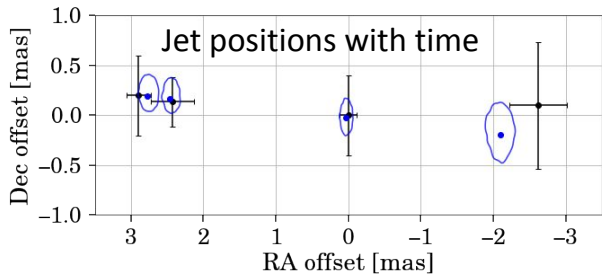
# GW+AG+C



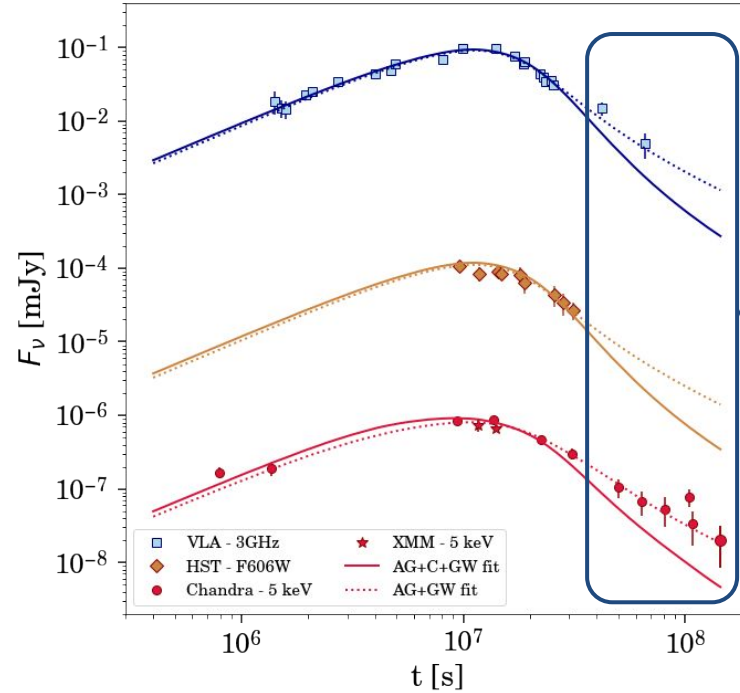
EM degeneracy	GW+AG	GW+AG+C
	GJ	GJ
$\theta_c$ [deg]	$7.73^{+0.86}_{-0.80}$	$2.85^{+0.24}_{-0.20}$
$d_L$ [Mpc]	$31.3^{+3.0}_{-3.6}$	$43.7^{+1.4}_{-1.4}$
$\theta_v$ [deg]	$50.1^{+5.1}_{-5.4}$	$18.2^{+1.2}_{-1.5}$
$\theta_{JN}$ [deg]	$129.9^{+5.1}_{-5.4}$	$161.8^{+1.2}_{-1.5}$

Wide jet      Collimated jet

Jet features in agreement with population studies ( $\theta_c$  in [3,6] deg).



# Why are they so different?



Excess in the flux at late times?



There are other degeneracies (proper of the light curve modeling) that influence:

$\theta_v$  (viewing angle)



$d_L$  (luminosity distance)



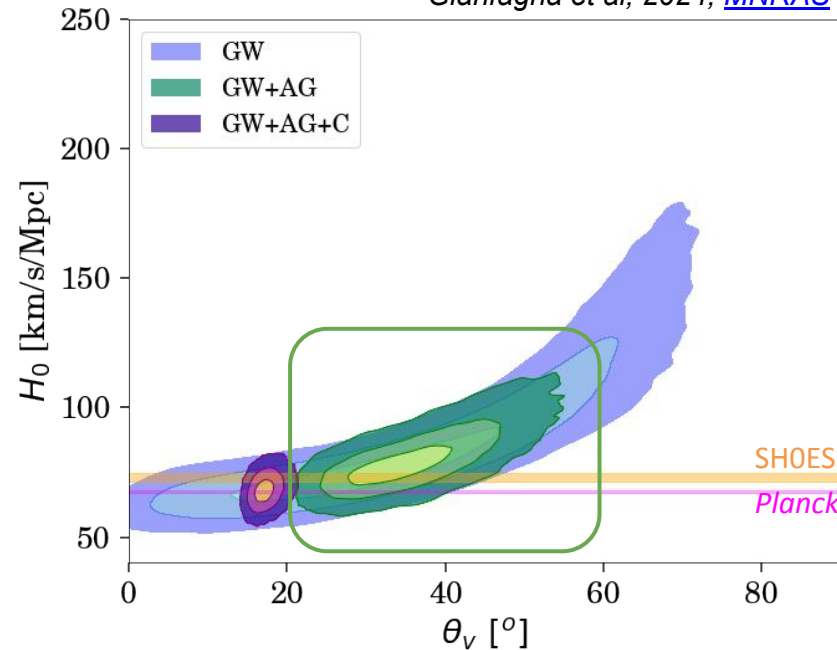
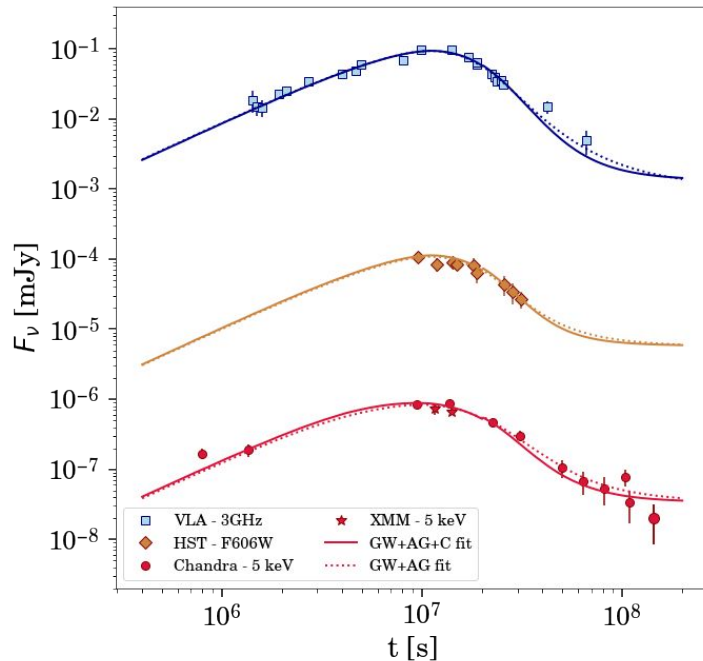
$H_0$  (Hubble constant)

Centroid motion strongly constraints  $\theta_v$  !



# Including a constant flux component at late times

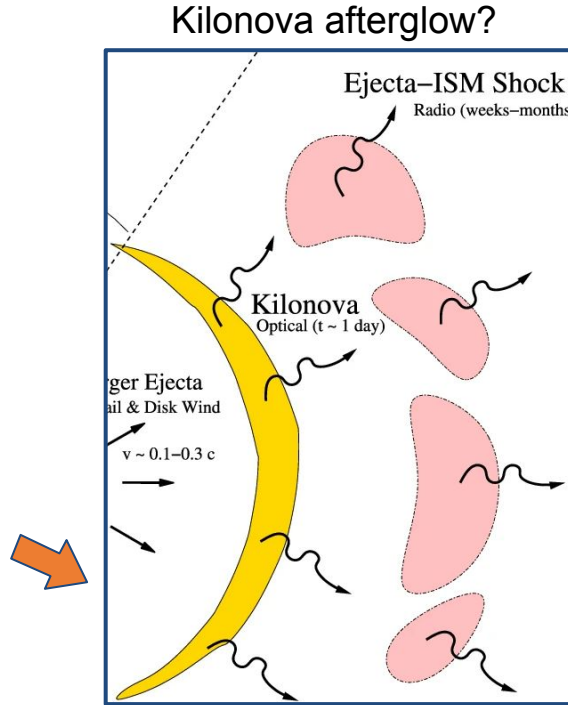
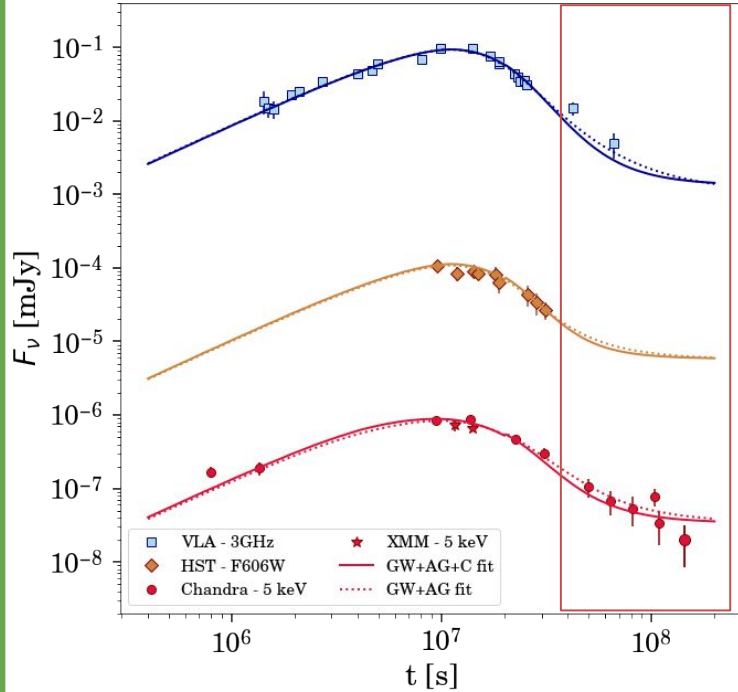
Gianfagna et al, 2024, [MNRAS](#)



$d_L$ [Mpc]	$38.6^{+2.5}_{-3.0}$
$\theta_v$ [deg]	$35.2^{+5.7}_{-6.2}$
$\theta_{JN}$ [deg]	$144.8^{+5.7}_{-6.2}$

$$H_0 = 78.5^{+7.9}_{-6.4} \text{ km s}^{-1} \text{ Mpc}^{-1}$$

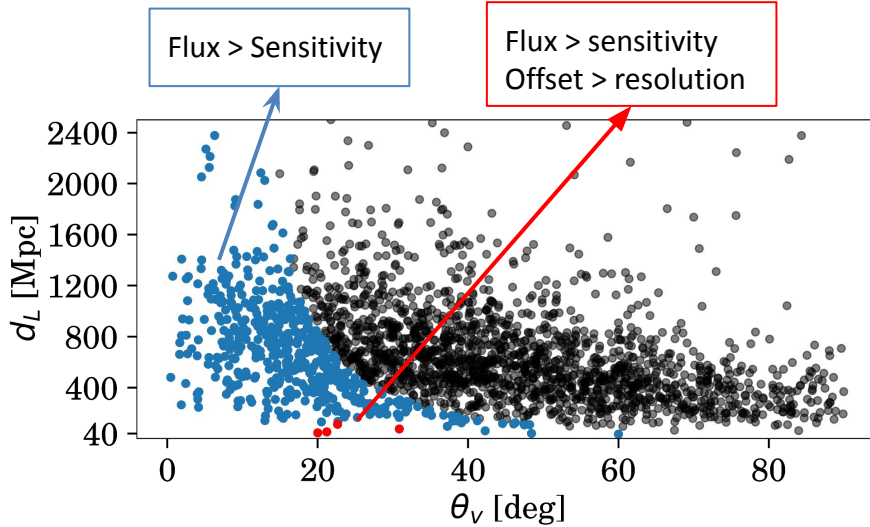
# Kilonova afterglow



	GW+AG	GW+AG+C
$d_L$ [Mpc]	$38.6^{+2.5}_{-3.0}$	$44.3^{+1.4}_{-1.3}$
$\theta_v$ [deg]	$35.2^{+5.7}_{-6.2}$	$17.2^{+1.1}_{-1.2}$

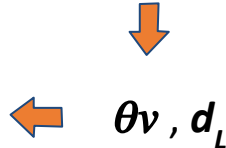
Gives information about velocity and mass of the ejecta!

# Future rates



GW simulations of binary neutron star mergers  
*Petrov+2022*

Generate the afterglow light curve and centroid motion



$\theta_v, d_L$

No uncertainty:  
4 km/s/Mpc 10 km/s/Mpc

		Considering VLBI sensitivity (24 $\mu$ Jy) and resolution (1.5 mas)		
		GW rates	GW+AG+C rates	GW+AG rates
<b>O5</b>	2027	$34^{+78}_{-25} \text{yr}^{-1}$	$0.05^{+0.11}_{-0.03} \text{yr}^{-1}$	$2.4^{+5.5}_{-1.8} \text{yr}^{-1}$

~10 events per year in **O5**.  
At the end of O5 we could be able to reach the **SHOES** sensitivity of **1.5 km/s/Mpc**