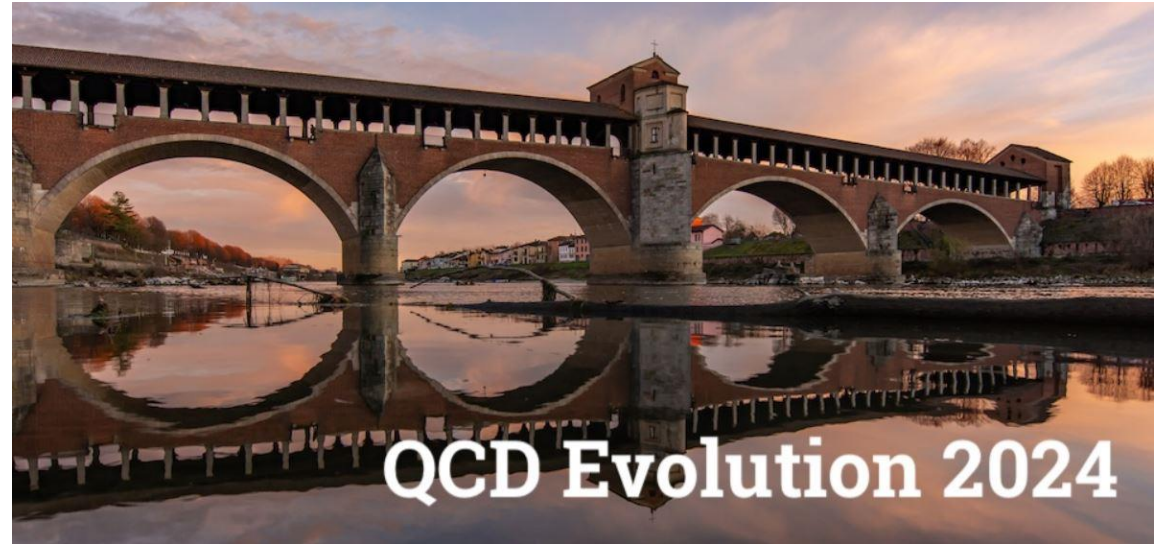


State of the art of observables for Generalized TMDs

Shohini Bhattacharya

Los Alamos National Laboratory

May 30, 2024



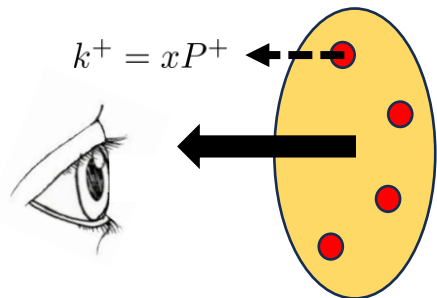
In Collaboration with:

Duxin Zheng, Jian Zhou (arXiv: 2312.01309)

Renaud Boussarie, Yoshitaka Hatta (arXiv: 2201.08709, 2404.04208, 2404.04209)



Wigner function - The “mother function”

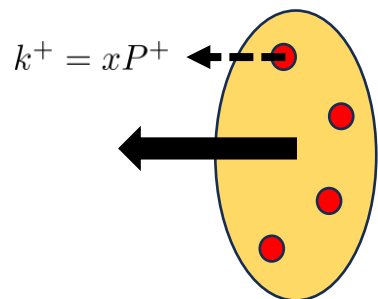


Parton Distribution Functions

PDFs (x)



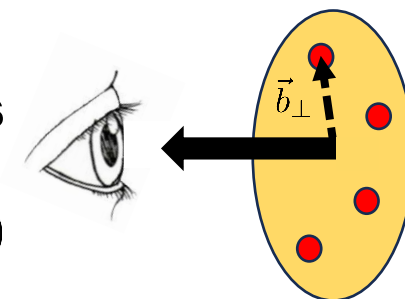
Wigner function - The “mother function”



PDFs (x)

Form Factors

FFs (Δ)

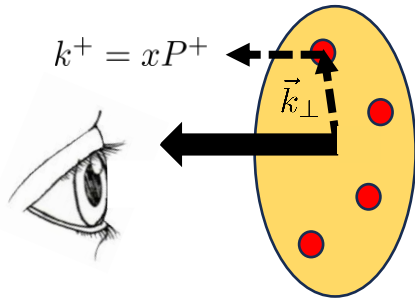




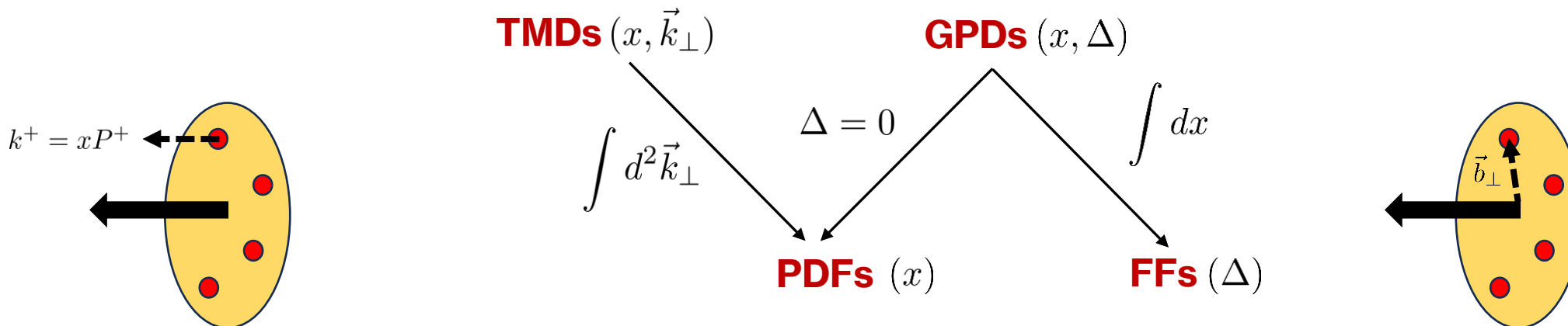
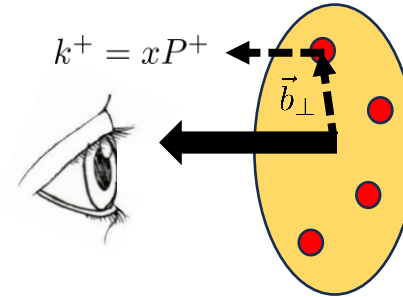
Wigner function - The “mother function”



Transverse Momentum-dependent Distributions



Generalized Parton Distributions



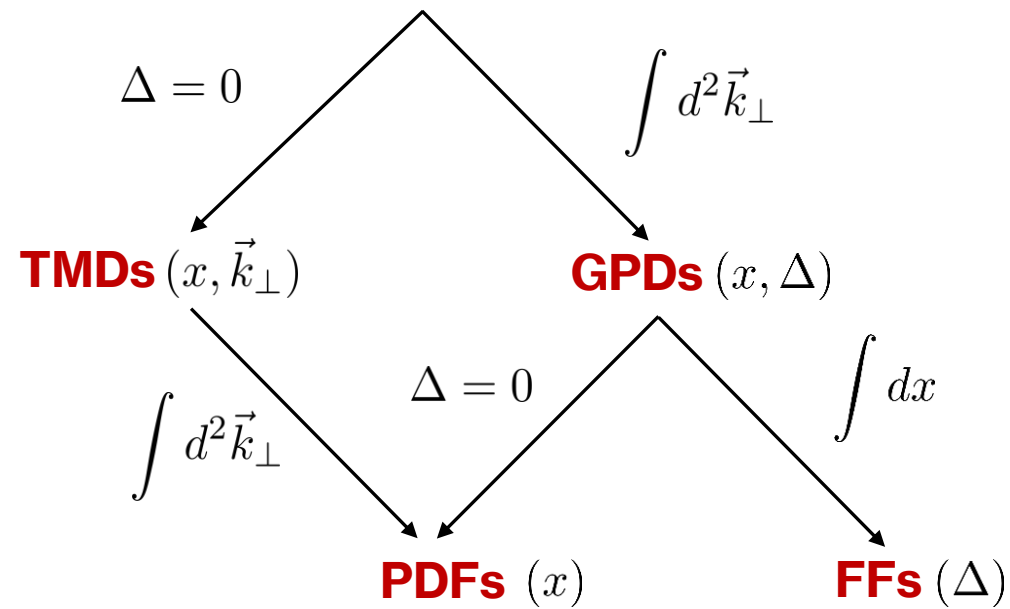


Wigner function - The “mother function”

Generalized **T**ransverse **M**omentum-dependent **D**istributions

(Meissner, Metz, Schlegel, 2009)

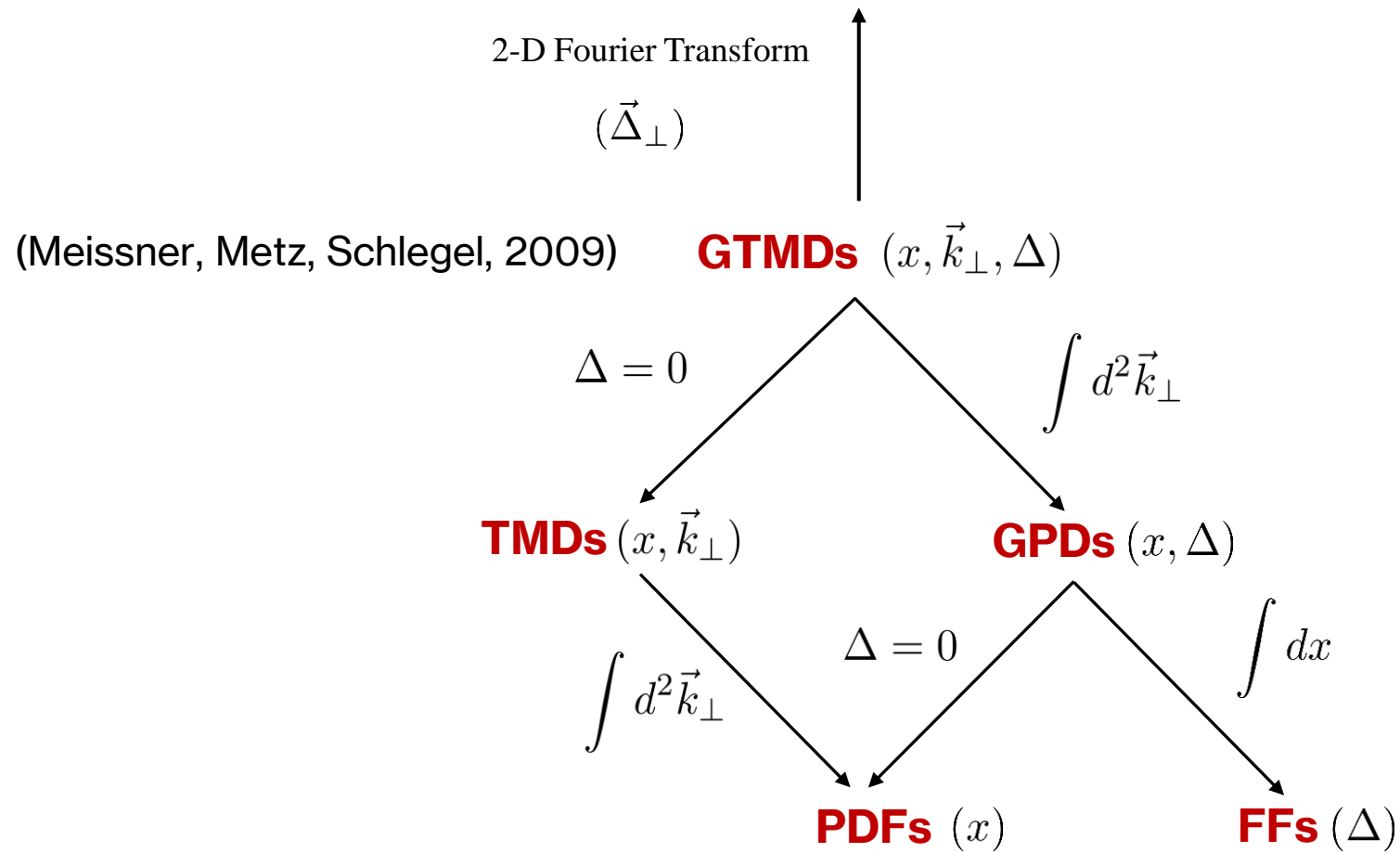
GTMDs $(x, \vec{k}_\perp, \Delta)$





Wigner function - The “mother function”

Wigner functions $(x, \vec{k}_\perp, \vec{b}_\perp)$ (Belitsky, Ji, Yuan, 2003)

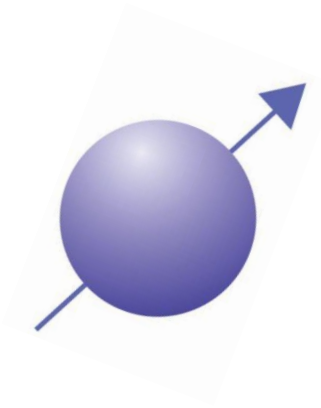


Spin of proton



Jaffe-Manohar spin decomposition

An incomplete story:



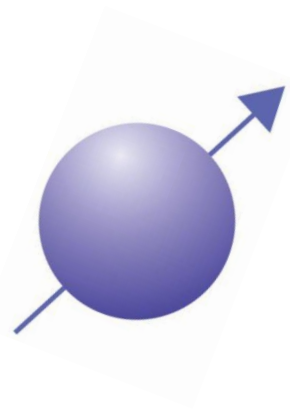
$$\frac{1}{2}$$



Spin of proton

Jaffe-Manohar spin decomposition

An incomplete story:



$$\frac{1}{2} = \frac{1}{2} \Delta\Sigma + \Delta G$$

Best known

How well do we know?

Quark helicity $\sim 30\%$

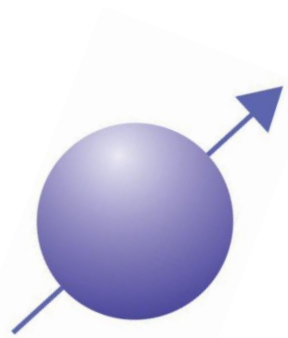
Gluon helicity $\sim 40\%$



Spin of proton

Jaffe-Manohar spin decomposition

An incomplete story:



$$\frac{1}{2} = \frac{1}{2} \Delta\Sigma + \Delta G + L^q + L^g$$

Best known

How well do we know?

????????

Quark helicity $\sim 30\%$

Gluon helicity $\sim 40\%$

OAM of quarks & gluons

Wigner functions & Orbital Angular Momentum



Wigner functions in Quantum Mechanics

(Wigner, 1932)

- Calculate from wave functions:

$$W(x, k) = \int \frac{dx'}{2\pi} e^{-ikx'} \psi\left(x + \frac{x'}{2}\right) \psi^*\left(x - \frac{x'}{2}\right)$$

- Expectation value of observables:

$$\langle \mathcal{O} \rangle = \int dx \int dk \mathcal{O}(x, k) W(x, k)$$

Wigner functions & Orbital Angular Momentum



Wigner functions in Quantum Mechanics

(Wigner, 1932)

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Wigner functions in parton physics

(Belitsky, Ji, Yuan, 2003)

- Calculate from fourier transform of GTMD correlator:

$$W^{[\Gamma]}(x, \vec{k}_\perp, \vec{b}_\perp)$$

- Application: **O**rbital **A**ngular **M**omentum (**OAM**)

$$L_z^{q,g} = \int dx \int d^2k_\perp d^2b_\perp (\vec{b}_\perp \times \vec{k}_\perp)_z W^{q,g}(x, \vec{b}_\perp, \vec{k}_\perp)$$

(Lorcé, Pasquini, 2011 / Hatta, 2011)

Wigner functions & Orbital Angular Momentum



Wigner functions in Quantum Mechanics

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Wigner functions in parton physics

(Belitsky, Ji, Yuan, 2003)

- Calculate from fourier transform of GTMD correlator:

$$W^{[\Gamma]}(x, \vec{k}_\perp, \vec{b}_\perp)$$

- Application: Relation between GTMD $F_{1,4}^{q,g}$ & OAM

$$L_z^{q,g} = - \int dx \int d^2 \vec{k}_\perp \frac{\vec{k}_\perp^2}{M^2} F_{1,4}^{q,g}(x, \vec{k}_\perp, \xi = 0, \Delta_\perp = 0)$$

(Lorcé, Pasquini, 2011 / Hatta, 2011)

Wigner functions & Orbital Angular Momentum



Wigner functions in Quantum Mechanics

(Wigner, 1932)

Wigner functions in parton physics

(Belitsky, Ji, Yuan, 2003)

- Calculate from wave function

$$W(x, k) = \int \frac{dx'}{2\pi} \psi(x-x')$$

Big question:
Experimental observable?

of GTMD correlator:

- Expectation value of observables:

$$\langle \mathcal{O} \rangle = \int dx \int dk \mathcal{O}(x, k) W(x, k)$$

- Application: Relation between GTMD $F_{1,4}^{q,g}$ & OAM

$$L_z^{q,g} = - \int dx \int d^2 \vec{k}_\perp \frac{\vec{k}_\perp^2}{M^2} F_{1,4}^{q,g}(x, \vec{k}_\perp, \xi = 0, \Delta_\perp = 0)$$

(Lorcé, Pasquini, 2011 / Hatta, 2011)

Developments



arXiv: 1612.02438 (2016)

Feng Yuan's talk

Hunting the Gluon Orbital Angular Momentum at the
Electron-Ion Collider

Xiangdong Ji,^{1,2} Feng Yuan,³ and Yong Zhao^{1,3}

Developments



arXiv: 1612.02438 (2016)

Hunting the Gluon Orbital Angular Momentum at the
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Xiangdong Ji,^{1,2} Feng Yuan,³ and Yong Zhao^{1,3}

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Generalized TMDs and the exclusive double Drell-Yan process

Shohini Bhattacharya,¹ Andreas Metz,¹ and Jian Zhou²

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Exclusive double quarkonium production and generalized TM

Shohini Bhattacharya,¹ Andreas Metz,¹ Vikash Kumar Ojha,² Jeng-Yuan Tsai,¹

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Probing the Weizsäcker-Williams gluon Wigner distribution in pp collisions

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arXiv: 1912.08182 (2019)

Probing the gluon Sivers function with an unpolarized target:
GTMD distributions and the Odderons

Renaud Boussarie,¹ Yoshitaka Hatta,¹ Lech Szymanowski,² and Samuel Wallon^{3,4}

Developments



arXiv: 1612.02438 (2016)

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arXiv: 2106.13466 (2021)

Probing the gluon tomography in photoproduction of di-pions

Yoshikazu Hagiwara, Cheng Zhang, Jian Zhou, and Ya-jin Zhou

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Signature of the gluon orbital angular momentum

Shohini Bhattacharya,^{1,*} Renaud Boussarie,^{2,†} and Yoshitaka Hatta^{1,3,‡}

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arXiv: 2205.00045 (2022)

Angular correlations in exclusive dijet photoproduction in
ultra-peripheral PbPb collisions at $\sqrt{s_{NN}} = 5.02$ TeV

Developments



arXiv: 1612.02438 (2016)

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arXiv: 1702.04387 (2017)

Generalized TMDs and the exclusive double Drell-Yan process

Shohini Bhattacharya,¹ Andreas Metz,¹ and Jian Zhou²

arXiv: 1802.10550 (2018)

arXiv

Exclusive double Drell-Yan:

Until now, this has been the sole known process sensitive to quark GTMDs

Renaud Boussarie,¹ Yoshitaka Hatta,¹ Lech Szymanowski,² and S

arXiv: 2201.08709 (2022/2024)

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Probing quark OAM through double Drell-Yan

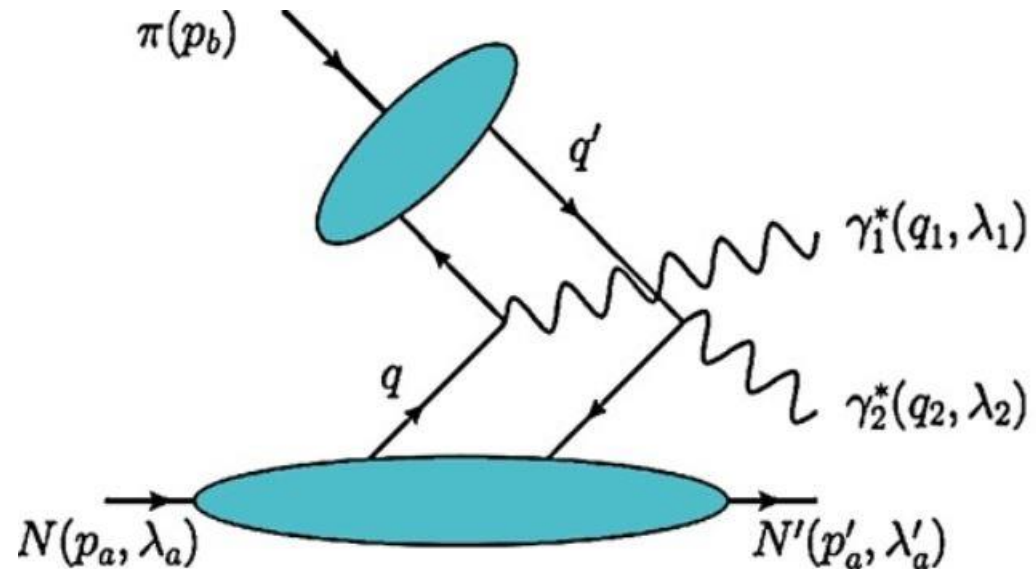


Main findings

arXiv: 1702.04387 (2017)

Generalized TMDs and the exclusive double Drell-Yan process

Shohini Bhattacharya,¹ Andreas Metz,¹ and Jian Zhou²



Probing quark OAM through double Drell-Yan



Main findings

Example of an observable sensitive to **OAM** & **spin-orbit correlation** :

$$\frac{1}{2}(\tau_{XY} - \tau_{YX}) = \frac{4}{M_a^2} (\varepsilon_{\perp}^{ij} \Delta q_{\perp}^i \Delta_{a\perp}^j) \text{Re.} \left\{ C^{(-)} [F_{1,1} \phi_{\pi}] C^{(+)} [\vec{\beta}_{\perp} \cdot \vec{k}_{a\perp} \mathbf{F}_{1,4}^* \phi_{\pi}^*] \right\}$$



Probing quark OAM through double Drell-Yan

Main findings

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Spin-orbit entanglement in the Color Glass Condensate

Shohini Bhattacharya,^{1,*} Renaud Boussarie,^{2,†} and Yoshitaka Hatta^{3,4,‡}

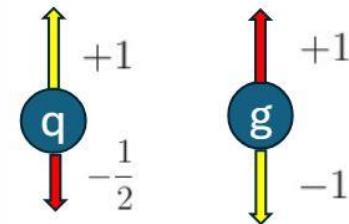
2404.04208

Recall Spin-Orbit coupling in H atom!



$$G_{1,1}^{q/g} \rightarrow L^{q/g} \cdot S^{q/g}$$

Perfect spin-orbit **anti**-correlation



Probing quark OAM through double Drell-Yan



Main findings

Challenges:

- Low count rate (Amplitude $\sim \alpha_{em}^2$)

Probing quark OAM through double Drell-Yan



Main findings

Challenges:

- Low count rate (Amplitude $\sim \alpha_{em}^2$)
- Sensitivity to GTMDs only in the ERBL region $-\xi < x < \xi$

$$\text{OAM density: } L^{q/g}(x, \xi) = - \int d^2 \vec{k}_\perp \frac{\vec{k}_\perp^2}{M^2} F_{1,4}^{q,g}(x, k_\perp, \xi, \Delta_\perp = 0)$$

$$\text{OAM: } L^{q/g} = \int dx L^{q/g}(x, \xi = 0)$$

The challenge lies in extrapolating the distribution to the forward limit, where the OAM equation is applicable

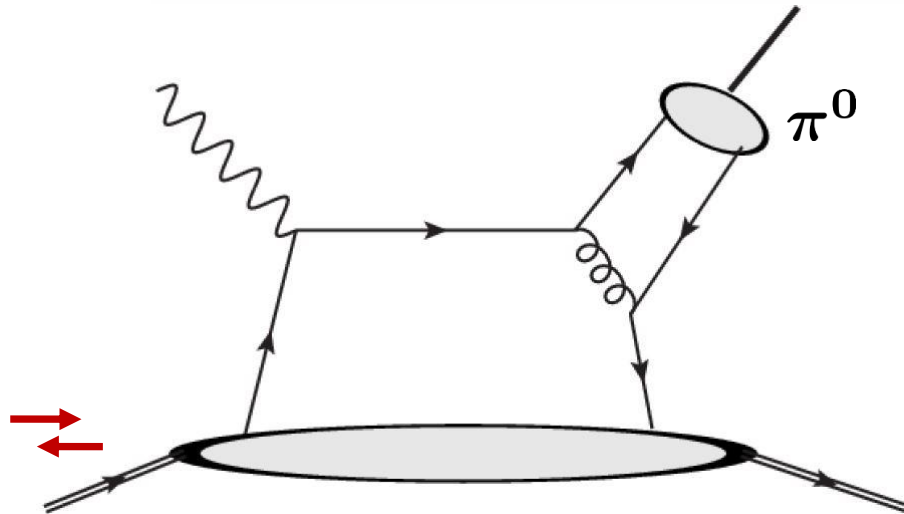


Our work

arXiv: 2312.01309 (2023)

Probing quark orbital angular momentum at EIC and EicC

Shohini Bhattacharya,¹ Duxin Zheng,² and Jian Zhou³



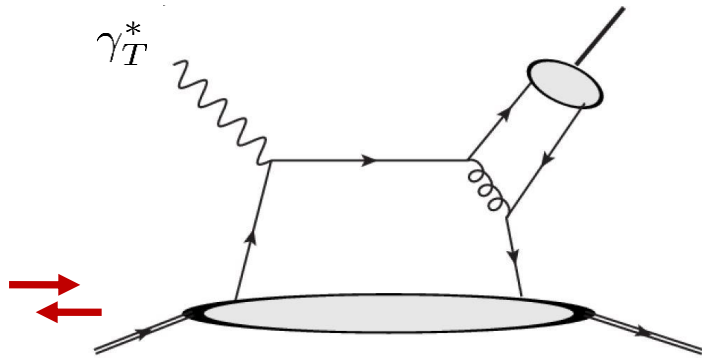
Main Observable:

**Longitudinal single-target spin
asymmetry**

Probing quark OAM through π^0 production in ep collisions



Scattering amplitude



4 leading-order Feynman diagrams

Probing quark OAM through π^0 production in ep collisions



Scattering amplitude

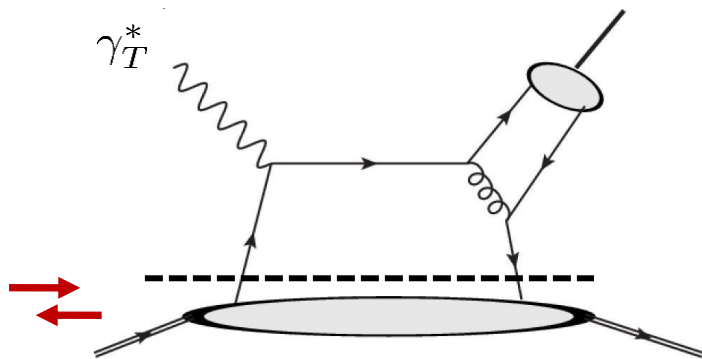
Scattering amplitude:

$$A \propto \int dx \int d^2 k_{\perp} H(x, \xi, z, k_{\perp}, \Delta_{\perp}) f^q(x, \xi, k_{\perp}, \Delta_{\perp}) \int dz \phi_{\pi}(z)$$

Hard part

Soft part from
proton

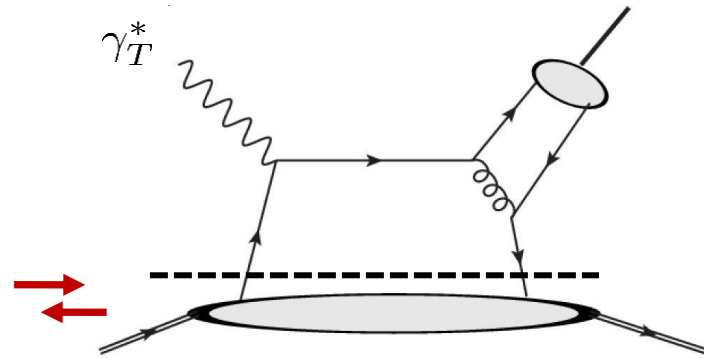
Pion Distribution
Amplitude



Probing quark OAM through π^0 production in ep collisions



Scattering amplitude



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Collinear twist-expansion of hard part:

$$H(k_{\perp}, \Delta_{\perp}) = H(k_{\perp} = 0, \Delta_{\perp} = 0) + \frac{\partial H(k_{\perp}, \Delta_{\perp} = 0)}{\partial k_{\perp}^{\mu}} \Big|_{k_{\perp} = 0} k_{\perp}^{\mu} + \frac{\partial H(k_{\perp} = 0, \Delta_{\perp})}{\partial \Delta_{\perp}^{\mu}} \Big|_{\Delta_{\perp} = 0} \Delta_{\perp}^{\mu} + \dots$$

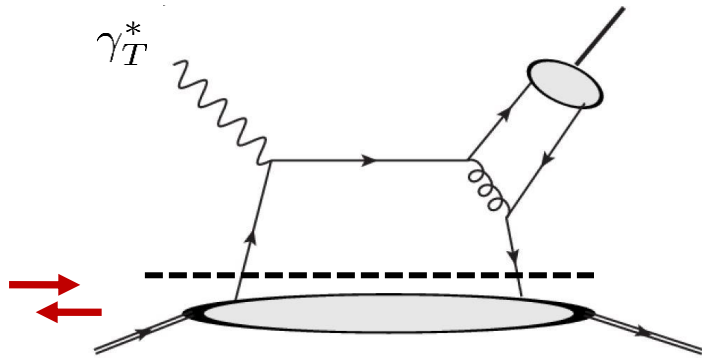
Probing quark OAM through π^0 production in ep collisions



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Twist 2 term vanishes

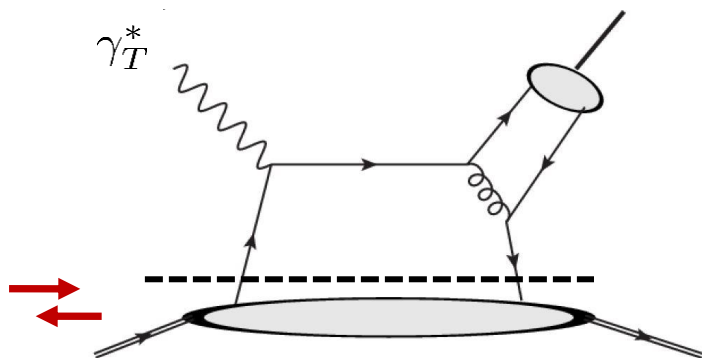
Probing quark OAM through π^0 production in ep collisions



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Collinear twist-expansion of hard part:

$$H(k_{\perp}, \Delta_{\perp}) = H(k_{\perp} = 0, \Delta_{\perp} = 0) + \underbrace{\frac{\partial H(k_{\perp}, \Delta_{\perp} = 0)}{\partial k_{\perp}^{\mu}} \Big|_{k_{\perp}=0} k_{\perp}^{\mu} + \frac{\partial H(k_{\perp} = 0, \Delta_{\perp})}{\partial \Delta_{\perp}^{\mu}} \Big|_{\Delta_{\perp}=0} \Delta_{\perp}^{\mu} + \dots}_{\text{Twist 3 term}}$$

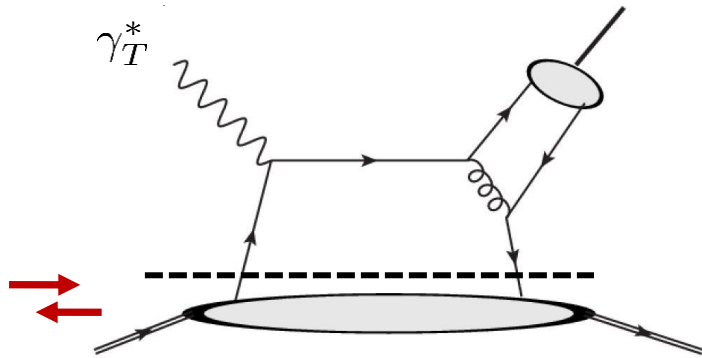
Use special-propagator technique to ensure electromagnetic gauge invariance

(J. W. Qiu, 1990)

Probing quark OAM through π^0 production in ep collisions



Scattering amplitude



Scattering amplitude:

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Collinear twist-expansion of hard part:

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$$A \propto \int d^2 k_{\perp} k_{\perp}^2 \text{GTMD}$$

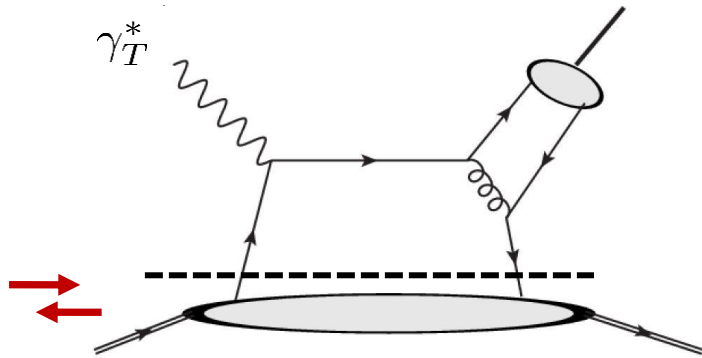
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$$A \propto \text{GPD}$$

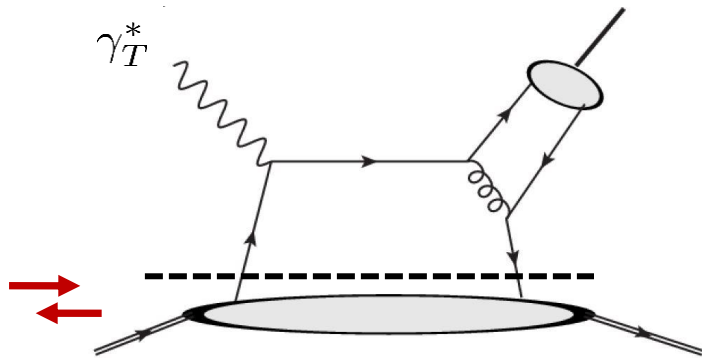
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Collinear twist-expansion of hard part:

Consequently, the scattering amplitudes are a convolution of moments of GTMDs and GPDs and are of twist-3 nature

Probing quark OAM through π^0 production in ep collisions



Angular correlations

Scattering amplitudes depend on different angular correlations:

$$\mathcal{M}_1 = \frac{g_s^2 e f_\pi (N_c^2 - 1) 2\xi}{2\sqrt{2} N_c^2 \sqrt{1 - \xi^2}} \delta_{\lambda\lambda'} \frac{\boldsymbol{\epsilon}_\perp \times \boldsymbol{\Delta}_\perp}{Q^2} \{\mathcal{F}_{1,1} + \mathcal{G}_{1,1}\}$$

$$\mathcal{M}_2 = \frac{g_s^2 e f_\pi (N_c^2 - 1) 2\xi}{2\sqrt{2} N_c^2 \sqrt{1 - \xi^2}} \delta_{\lambda, -\lambda'} \frac{M \boldsymbol{\epsilon}_\perp \cdot \boldsymbol{S}_\perp}{Q^2} \{\mathcal{F}_{1,2} + \mathcal{G}_{1,2}\} \quad S_\perp^\mu = (0^+, 0^-, -i, \lambda)$$

$$\mathcal{M}_4 = \frac{i g_s^2 e f_\pi (N_c^2 - 1) 2\xi}{2\sqrt{2} N_c^2 \sqrt{1 - \xi^2}} \lambda \delta_{\lambda\lambda'} \frac{\boldsymbol{\epsilon}_\perp \cdot \boldsymbol{\Delta}_\perp}{Q^2} \{\mathcal{F}_{1,4} + \mathcal{G}_{1,4}\}$$

Probing quark OAM

through π^0 production

Compton Form Factors:



Angular correlations

Scattering amplitudes depend on different angular correlations:

$$\mathcal{M}_1 = \frac{g_s^2 e f_\pi (N_c^2 - 1) 2\xi}{2\sqrt{2} N_c^2 \sqrt{1 - \xi^2}} \delta_{\lambda\lambda'} \frac{\epsilon_\perp \times \Delta_\perp}{Q^2} \{\mathcal{F}_{1,1} + \mathcal{G}_{1,1}\}$$

$$\mathcal{M}_2 = \frac{g_s^2 e f_\pi (N_c^2 - 1) 2\xi}{2\sqrt{2} N_c^2 \sqrt{1 - \xi^2}} \delta_{\lambda, -\lambda'} \frac{M \epsilon_\perp \cdot S_\perp}{Q^2} \{\mathcal{F}_{1,2} + \mathcal{G}_{1,2}\}$$

$$\mathcal{M}_4 = \frac{i g_s^2 e f_\pi (N_c^2 - 1) 2\xi}{2\sqrt{2} N_c^2 \sqrt{1 - \xi^2}} \lambda \delta_{\lambda\lambda'} \frac{\epsilon_\perp \cdot \Delta_\perp}{Q^2} \{\mathcal{F}_{1,4} + \mathcal{G}_{1,4}\}$$

$$\mathcal{F}_{1,1} = \int_{-1}^1 dx \frac{x^2 \int d^2 k_\perp F_{1,1}^{u+d}(x, \xi, \Delta_\perp, k_\perp)}{(x + \xi - i\epsilon)^2 (x - \xi + i\epsilon)^2} \times \int_0^1 dz \frac{\phi_\pi(z)(1 + z^2 - z)}{z^2(1 - z)^2}, \quad (8)$$

$$\mathcal{G}_{1,1} = \int_{-1}^1 dx \int_0^1 dz \frac{\phi_\pi(z)(x^2 + 2x^2z + \xi^2)}{z^2(x + \xi - i\epsilon)^2(x - \xi + i\epsilon)^2} \times \int d^2 k_\perp \frac{k_\perp^2}{M^2} G_{1,1}^{u+d}(x, \xi, \Delta_\perp, k_\perp), \quad (9)$$

$$\mathcal{F}_{1,2} = \int_{-1}^1 dx x \frac{\xi(1 - \xi^2) \int d^2 k_\perp k_\perp^2 F_{1,2}^{u+d}(x, \xi, \Delta_\perp, k_\perp)}{M^2(x + \xi - i\epsilon)^2(x - \xi + i\epsilon)^2} \times \int_0^1 dz \frac{\phi_\pi(z)(1 + z^2 - z)}{z^2(1 - z)^2}, \quad (10)$$

$$\mathcal{G}_{1,2} = \int_{-1}^1 dx \int_0^1 dz \frac{\phi_\pi(z)(x^2 + 2x^2z + \xi^2)(1 - \xi^2)}{z^2(x + \xi - i\epsilon)^2(x - \xi + i\epsilon)^2} \times \int d^2 k_\perp \frac{k_\perp^2}{M^2} G_{1,2}^{u+d}(x, \xi, \Delta_\perp, k_\perp), \quad (11)$$

$$\mathcal{F}_{1,4} = \int_{-1}^1 dx \frac{x\xi \int d^2 k_\perp k_\perp^2 F_{1,4}^{u+d}(x, \xi, \Delta_\perp, k_\perp)}{M^2(x + \xi - i\epsilon)^2(x - \xi + i\epsilon)^2} \times \int_0^1 dz \frac{\phi_\pi(z)(1 + z^2 - z)}{z^2(1 - z)^2}, \quad (12)$$

$$\mathcal{G}_{1,4} = \int_{-1}^1 dx \int_0^1 dz \frac{x(4\xi^2z + \xi^2 - 2x^2z + x^2)}{z^2\xi(x + \xi - i\epsilon)^2(x - \xi + i\epsilon)^2} \phi_\pi(z) \times \int d^2 k_\perp G_{1,4}^{u+d}(x, \xi, \Delta_\perp, k_\perp). \quad (13)$$

Probing quark OAM through π^0 production in ep collisions



Angular correlations

Scattering amplitudes depend on different angular correlations:

$$\mathcal{M}_1 = \frac{g_s^2 e f_\pi (N_c^2 - 1) 2\xi}{2\sqrt{2} N_c^2 \sqrt{1 - \xi^2}} \delta_{\lambda\lambda'} \frac{\boldsymbol{\epsilon}_\perp \times \boldsymbol{\Delta}_\perp}{Q^2} \{\mathcal{F}_{1,1} + \mathcal{G}_{1,1}\}$$

$$\mathcal{M}_2 = \frac{g_s^2 e f_\pi (N_c^2 - 1) 2\xi}{2\sqrt{2} N_c^2 \sqrt{1 - \xi^2}} \delta_{\lambda, -\lambda'} \frac{M \boldsymbol{\epsilon}_\perp \cdot \boldsymbol{S}_\perp}{Q^2} \{\mathcal{F}_{1,2} + \mathcal{G}_{1,2}\}$$

$$\mathcal{M}_4 = \frac{i g_s^2 e f_\pi (N_c^2 - 1) 2\xi}{2\sqrt{2} N_c^2 \sqrt{1 - \xi^2}} \lambda \delta_{\lambda\lambda'} \frac{\boldsymbol{\epsilon}_\perp \cdot \boldsymbol{\Delta}_\perp}{Q^2} \{\mathcal{F}_{1,4} + \mathcal{G}_{1,4}\}$$

Sensitivity to quark OAM

$$\mathcal{F}_{1,1} = \int_{-1}^1 dx \frac{x^2 \int d^2 k_\perp F_{1,1}^{u+d}(x, \xi, \Delta_\perp, k_\perp)}{(x + \xi - i\epsilon)^2 (x - \xi + i\epsilon)^2} \times \int_0^1 dz \frac{\phi_\pi(z)(1 + z^2 - z)}{z^2(1 - z)^2}, \quad (8)$$

$$\mathcal{G}_{1,1} = \int_{-1}^1 dx \int_0^1 dz \frac{\phi_\pi(z)(x^2 + 2x^2z + \xi^2)}{z^2(x + \xi - i\epsilon)^2 (x - \xi + i\epsilon)^2} \times \int d^2 k_\perp \frac{k_\perp^2}{M^2} G_{1,1}^{u+d}(x, \xi, \Delta_\perp, k_\perp), \quad (9)$$

$$\mathcal{F}_{1,2} = \int_{-1}^1 dx x \frac{\xi(1 - \xi^2) \int d^2 k_\perp k_\perp^2 F_{1,2}^{u+d}(x, \xi, \Delta_\perp, k_\perp)}{M^2(x + \xi - i\epsilon)^2 (x - \xi + i\epsilon)^2} \times \int_0^1 dz \frac{\phi_\pi(z)(1 + z^2 - z)}{z^2(1 - z)^2}, \quad (10)$$

$$\mathcal{G}_{1,2} = \int_{-1}^1 dx \int_0^1 dz \frac{\phi_\pi(z)(x^2 + 2x^2z + \xi^2)(1 - \xi^2)}{z^2(x + \xi - i\epsilon)^2 (x - \xi + i\epsilon)^2} \times \int d^2 k_\perp \frac{k_\perp^2}{M^2} G_{1,2}^{u+d}(x, \xi, \Delta_\perp, k_\perp), \quad (11)$$

$$\mathcal{F}_{1,4} = \int_{-1}^1 dx \frac{x\xi \int d^2 k_\perp k_\perp^2 F_{1,4}^{u+d}(x, \xi, \Delta_\perp, k_\perp)}{M^2(x + \xi - i\epsilon)^2 (x - \xi + i\epsilon)^2} \times \int_0^1 dz \frac{\phi_\pi(z)(1 + z^2 - z)}{z^2(1 - z)^2}, \quad (12)$$

$$\mathcal{G}_{1,4} = \int_{-1}^1 dx \int_0^1 dz \frac{x(4\xi^2z + \xi^2 - 2x^2z + x^2)}{z^2\xi(x + \xi - i\epsilon)^2 (x - \xi + i\epsilon)^2} \phi_\pi(z) \times \int d^2 k_\perp G_{1,4}^{u+d}(x, \xi, \Delta_\perp, k_\perp). \quad (13)$$

Probing quark OAM through π^0 production in ep collisions



Cross section

$$\begin{aligned} \frac{d\sigma}{dtdQ^2dx_Bd\phi} &= \frac{(N_c^2 - 1)^2 \alpha_{em}^2 \alpha_s^2 f_\pi^2 \xi^3 \Delta_\perp^2}{2N_c^4 (1 - \xi^2) Q^{10} (1 + \xi)} [1 + (1 - y)^2] \\ &\times \left\{ \left[|\mathcal{F}_{1,1} + \mathcal{G}_{1,1}|^2 + |\mathcal{F}_{1,4} + \mathcal{G}_{1,4}|^2 + 2 \frac{M^2}{\Delta_\perp^2} |\mathcal{F}_{1,2} + \mathcal{G}_{1,2}|^2 \right] + \cos(2\phi) a \left[-|\mathcal{F}_{1,1} + \mathcal{G}_{1,1}|^2 + |\mathcal{F}_{1,4} + \mathcal{G}_{1,4}|^2 \right] \right. \\ &\quad \left. + \lambda \sin(2\phi) 2a \operatorname{Re} \left[(i\mathcal{F}_{1,4} + i\mathcal{G}_{1,4}) (\mathcal{F}_{1,1}^* + \mathcal{G}_{1,1}^*) \right] \right\} \\ &\quad \uparrow \\ &\quad a = \frac{2(1-y)}{1+(1-y)^2} \end{aligned}$$

Probing quark OAM through π^0 production in ep collisions



Cross section

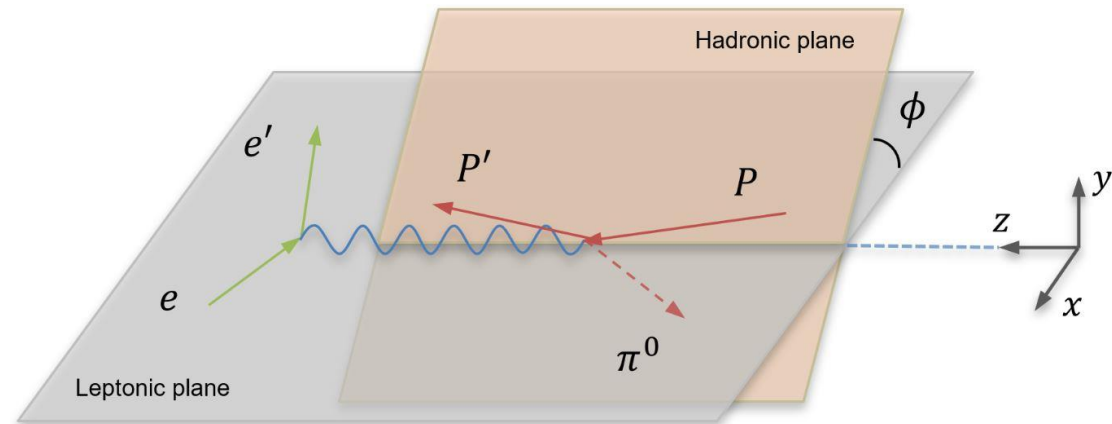
$$\frac{d\sigma}{dtdQ^2dx_Bd\phi} = \frac{(N_c^2 - 1)^2 \alpha_{em}^2 \alpha_s^2 f_\pi^2 \xi^3 \Delta_\perp^2}{2N_c^4 (1 - \xi^2) Q^{10} (1 + \xi)} [1 + (1 - y)^2]$$

$$\times \left\{ \left[|\mathcal{F}_{1,1} + \mathcal{G}_{1,1}|^2 + |\mathcal{F}_{1,4} + \mathcal{G}_{1,4}|^2 + 2 \frac{M^2}{\Delta_\perp^2} |\mathcal{F}_{1,2} + \mathcal{G}_{1,2}|^2 \right] + \cos(2\phi) a \left[-|\mathcal{F}_{1,1} + \mathcal{G}_{1,1}|^2 + |\mathcal{F}_{1,4} + \mathcal{G}_{1,4}|^2 \right] \right.$$

$$\left. + \lambda \sin(2\phi) 2a \operatorname{Re} \left[(i\mathcal{F}_{1,4} + i\mathcal{G}_{1,4}) (\mathcal{F}_{1,1}^* + \mathcal{G}_{1,1}^*) \right] \right\}$$

Distinguished experimental signature of quark OAM

$$\phi = \phi_{l_\perp} - \phi_{\Delta_\perp}$$



Probing quark OAM through π^0 production in ep collisions



Cross section

$$\frac{d\sigma}{dtdQ^2dx_Bd\phi} = \frac{(N_c^2 - 1)^2 \alpha_{em}^2 \alpha_s^2 f_\pi^2 \xi^3 \Delta_\perp^2}{2N_c^4 (1 - \xi^2) Q^{10} (1 + \xi)} [1 + (1 - y)^2]$$

$$\times \left\{ \left[|\mathcal{F}_{1,1} + \mathcal{G}_{1,1}|^2 + |\mathcal{F}_{1,4} + \mathcal{G}_{1,4}|^2 + 2 \frac{M^2}{\Delta_\perp^2} |\mathcal{F}_{1,2} + \mathcal{G}_{1,2}|^2 \right] + \cos(2\phi) a \left[-|\mathcal{F}_{1,1} + \mathcal{G}_{1,1}|^2 + |\mathcal{F}_{1,4} + \mathcal{G}_{1,4}|^2 \right] \right.$$

$$\left. + \lambda \sin(2\phi) 2a \operatorname{Re} \left[(i\mathcal{F}_{1,4} + i\mathcal{G}_{1,4}) (\mathcal{F}_{1,1}^* + \mathcal{G}_{1,1}^*) \right] \right\} \quad \uparrow \quad \text{Surprise!}$$

- Probe quark Sivers function through an unpolarized target

$$\operatorname{Im} [F_{1,2}]|_{\Delta=0} = -f_{1T}^\perp$$

(Similar to the gluon GTMD $F_{1,2}$, as discussed in Boussarie, Hatta, Szymanowski, Wallon, 2019)

Probing quark OAM through π^0 production in ep collisions



Cross section

$$\frac{d\sigma}{dt dQ^2 dx_B d\phi} = \frac{(N_c^2 - 1)^2 \alpha_{em}^2 \alpha_s^2 f_\pi^2 \xi^3 \Delta_\perp^2}{2N_c^4 (1 - \xi^2) Q^{10} (1 + \xi)} [1 + (1 - y)^2]$$

$$\times \left\{ \left[|\mathcal{F}_{1,1} + \mathcal{G}_{1,1}|^2 + |\mathcal{F}_{1,4} + \mathcal{G}_{1,4}|^2 + 2 \frac{M^2}{\Delta_\perp^2} |\mathcal{F}_{1,2} + \mathcal{G}_{1,2}|^2 \right] + \cos(2\phi) a \left[-|\mathcal{F}_{1,1} + \mathcal{G}_{1,1}|^2 + |\mathcal{F}_{1,4} + \mathcal{G}_{1,4}|^2 \right] \right.$$

$$\left. + \lambda \sin(2\phi) 2a \operatorname{Re} \left[(i\mathcal{F}_{1,4} + i\mathcal{G}_{1,4}) (\mathcal{F}_{1,1}^* + \mathcal{G}_{1,1}^*) \right] \right\} \quad \uparrow \quad \text{Surprise!}$$

- Probe quark Sivers function through an unpolarized target

$$\operatorname{Im} [\mathbf{F}_{1,2}]|_{\Delta=0} = -\mathbf{f}_{1T}^\perp$$

- Probe quark worm gear function through an unpolarized target

$$\operatorname{Re} [\mathbf{G}_{1,2}]|_{\Delta=0} = \mathbf{g}_{1T}$$

Probing quark OAM through π^0 production in ep collisions



Cross section

$$\frac{d\sigma}{dtdQ^2dx_Bd\phi} = \frac{(N_c^2 - 1)^2 \alpha_{em}^2 \alpha_s^2 f_\pi^2 \xi^3 \Delta_\perp^2}{2N_c^4 (1 - \xi^2) Q^{10} (1 + \xi)} [1 + (1 - y)^2]$$

$$\times \left\{ \left[|\mathcal{F}_{1,1} + \mathcal{G}_{1,1}|^2 + |\mathcal{F}_{1,4} + \mathcal{G}_{1,4}|^2 + 2 \frac{M^2}{\Delta_\perp^2} |\mathcal{F}_{1,2} + \mathcal{G}_{1,2}|^2 \right] + \cos(2\phi) a \left[-|\mathcal{F}_{1,1} + \mathcal{G}_{1,1}|^2 + |\mathcal{F}_{1,4} + \mathcal{G}_{1,4}|^2 \right] \right.$$

$$\left. + \lambda \sin(2\phi) 2a \operatorname{Re} \left[(i\mathcal{F}_{1,4} + i\mathcal{G}_{1,4}) (\mathcal{F}_{1,1}^* + \mathcal{G}_{1,1}^*) \right] \right\}$$



Helicity flip terms persist even when $\Delta_\perp \rightarrow 0$

Probing quark OAM through π^0 production in ep collisions



Cross section

$$\begin{aligned} \frac{d\sigma}{dtdQ^2dx_Bd\phi} &= \frac{(N_c^2 - 1)^2 \alpha_{em}^2 \alpha_s^2 f_\pi^2 \xi^3 \Delta_\perp^2}{2N_c^4 (1 - \xi^2) Q^{10} (1 + \xi)} [1 + (1 - y)^2] \\ &\times \left\{ \left[|\mathcal{F}_{1,1} + \mathcal{G}_{1,1}|^2 + |\mathcal{F}_{1,4} + \mathcal{G}_{1,4}|^2 + 2 \frac{M^2}{\Delta_\perp^2} |\mathcal{F}_{1,2} + \mathcal{G}_{1,2}|^2 \right] + \cos(2\phi) a \left[-|\mathcal{F}_{1,1} + \mathcal{G}_{1,1}|^2 + |\mathcal{F}_{1,4} + \mathcal{G}_{1,4}|^2 \right] \right. \\ &\quad \left. + \lambda \sin(2\phi) 2a \operatorname{Re} \left[(i\mathcal{F}_{1,4} + i\mathcal{G}_{1,4}) (\mathcal{F}_{1,1}^* + \mathcal{G}_{1,1}^*) \right] \right\} \end{aligned}$$

Since both unpolarized and polarized cross sections contribute at twist-3, the magnitudes of the asymmetries are not power-suppressed

Probing quark OAM through π^0 production in ep collisions



Model input for numerical estimations

Probing quark OAM through π^0 production in ep collisions



Model input for numerical estimations

Ingredients for non-perturbative functions:

- Model (H^q, \tilde{H}^q) according to the Double distribution approach (see Radyushkin, 9805342)

Example:

$$H^q(x, \xi, t) = \int_{-1}^1 d\beta \int_{-1+|\beta|}^{1-|\beta|} d\alpha \delta(\beta + \xi\alpha - x) \times \frac{3}{4} |\beta|^{-1.3 t} \frac{[(1 - |\beta|)^2 - \alpha^2]}{(1 - |\beta|)^3} q(|\beta|)$$



Probing quark OAM through π^0 production in ep collisions



Model input for numerical estimations

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The t-dependence is determined based on a fit to CLAS data

Probing quark OAM through π^0 production in ep collisions



Model input for numerical estimations

Ingredients for non-perturbative functions:

- Model (H^q, \tilde{H}^q) according to the Double distribution approach (see Radyushkin, 9805342)
- Model for OAM:
 1. “OAM density”: (Hatta, Yoshida, 1207.5332)

$$L_{can}^q(\boldsymbol{x}) = x \int_x^1 \frac{dx'}{x'} q(x') - x \int_x^1 \frac{dx'}{x'^2} \Delta q(x') + \text{genuine twist-three}$$

Probing quark OAM through π^0 production in ep collisions



Model input for numerical estimations

Ingredients for non-perturbative functions:

- Model (H^q, \tilde{H}^q) according to the Double distribution approach (see Radyushkin, 9805342)
- Model for OAM:
 1. “OAM density”: (Hatta, Yoshida, 1207.5332)

$$L_{can}^q(\boldsymbol{x}) \stackrel{\text{WW approx}}{=} x \int_x^1 \frac{dx'}{x'} q(x') - x \int_x^1 \frac{dx'}{x'^2} \Delta q(x') + \text{genuine twist-three}$$

Probing quark OAM through π^0 production in ep collisions



Model input for numerical estimations

Ingredients for non-perturbative functions:

- Model (H^q, \tilde{H}^q) according to the Double distribution approach (see Radyushkin, 9805342)
- Model for OAM:
 1. “OAM density”: (Hatta, Yoshida, 1207.5332)

$$L_{can}^q(\boldsymbol{x}) \stackrel{\text{WW approx}}{=} x \int_x^1 \frac{dx'}{x'} q(x') - x \int_x^1 \frac{dx'}{x'^2} \Delta q(x') + \text{genuine twist-three}$$

2. Use the Double distribution approach to construct $xL^q(x, \boldsymbol{\xi})e^{t/\Lambda}$ from $xL^q(x)$

Probing quark OAM through π^0 production in ep collisions



Model input for numerical estimations

Ingredients for non-perturbative functions:

- Pion distribution amplitude:

Asymptotic form

$$\phi_{\pi}(z) = 6z(1 - z)$$

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Model input for numerical estimations

End-point singularity & discontinuity:

$$\mathcal{F}_{1,4} = \int_{-1}^1 dx \frac{x\xi \int d^2k_{\perp} k_{\perp}^2 F_{1,4}^{u+d}(x, \xi, \Delta_{\perp}, k_{\perp})}{M^2(x + \xi - i\epsilon)^2(x - \xi + i\epsilon)^2} \times \int_0^1 dz \frac{\phi_{\pi}(z)(1 + z^2 - z)}{z^2(1 - z)^2}$$

Model-dependent method:

$$\int_{\langle p_{\perp}^2 \rangle / Q^2}^{1 - \langle p_{\perp}^2 \rangle / Q^2} dz$$

$\langle p_{\perp}^2 \rangle = 0.04 \text{ GeV}^2$ determined based on a fit to CLAS data

S. V. Goloskokov and P. Kroll, 2005

Probing quark OAM through π^0 production in ep collisions



Model input for numerical estimations

End-point singularity & discontinuity:

$$\mathcal{F}_{1,4} = \int_{-1}^1 dx \frac{x\xi \int d^2k_\perp k_\perp^2 F_{1,4}^{u+d}(x, \xi, \Delta_\perp, k_\perp)}{M^2 (x + \xi - i\epsilon)^2 (x - \xi + i\epsilon)^2} \times \int_0^1 dz \frac{\phi_\pi(z)(1 + z^2 - z)}{z^2(1 - z)^2}$$

Model-dependent method:

$$\int_{\langle p_\perp^2 \rangle / Q^2}^{1 - \langle p_\perp^2 \rangle / Q^2} dz$$

S. V. Goloskokov and P. Kroll, 2005

$$\frac{1}{(x - \xi + i\epsilon)^2} \rightarrow \frac{1}{(x - \xi - \langle p_\perp^2 \rangle / Q^2 + i\epsilon)^2}$$

I. V. Anikin, O. V. Teryaev, 2003

Probing quark OAM through π^0 production in ep collisions



Numerical results

Kinematics:

	$Q^2(\text{GeV}^2)$	$\sqrt{s_{ep}}(\text{GeV})$
EIC	10	100
EicC	3	16

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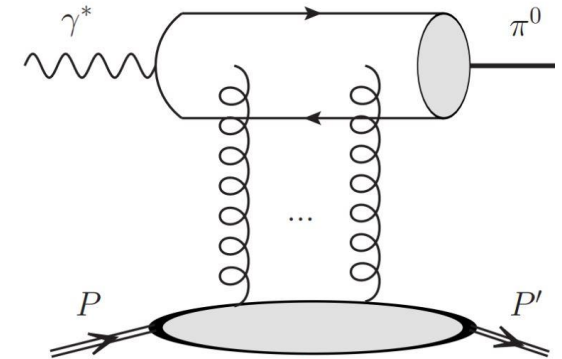


Numerical results

Kinematics:

	$Q^2(\text{GeV}^2)$	$\sqrt{s}_{ep}(\text{GeV})$
EIC	10	100
EicC	3	16

- We focus on large skewness (ξ) region to suppress gluon contribution



Probing quark OAM through π^0 production in ep collisions

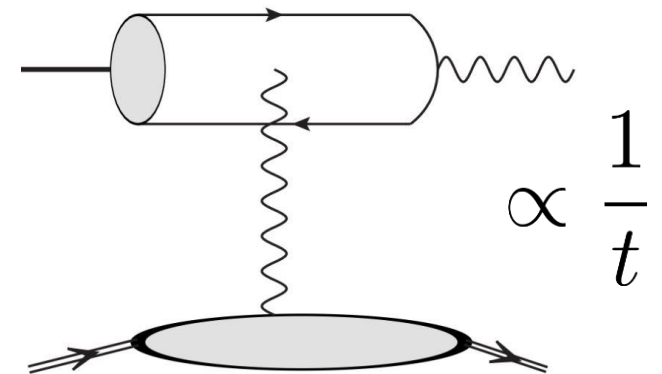


Numerical results

Kinematics:

	$Q^2(\text{GeV}^2)$	$\sqrt{s_{ep}}(\text{GeV})$
EIC	10	100
EicC	3	16

- We focus on large skewness (ξ) region to suppress gluon contribution
- We focus on large momentum transfer (t) region to suppress contribution from Primakoff process



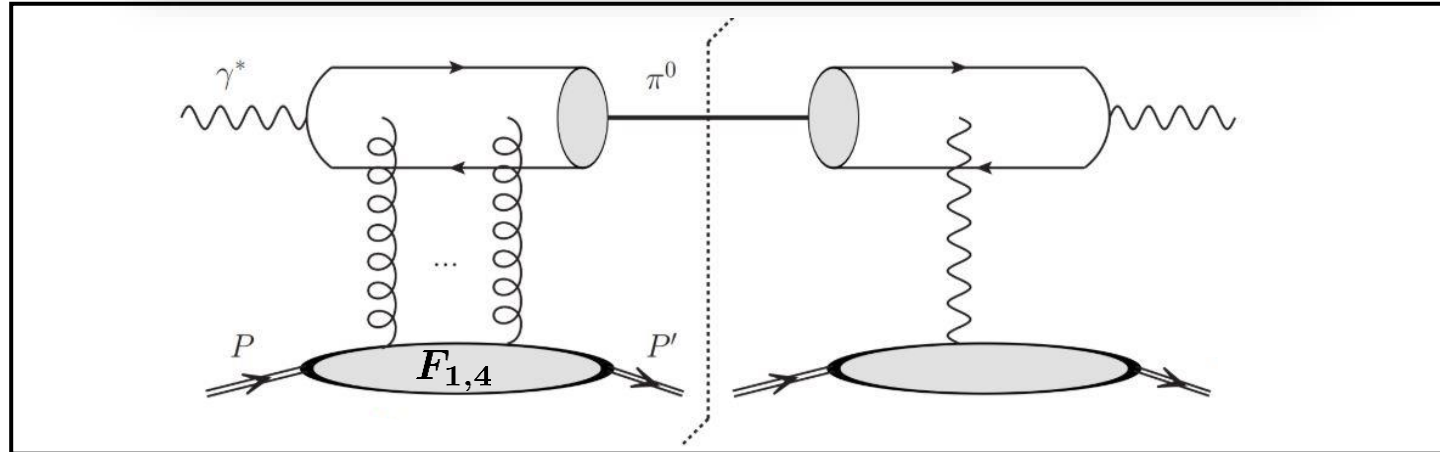
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Remark:

Accessing the gluon GTMD $F_{1,4}$ in exclusive π^0 production in ep collisions

Shohini Bhattacharya,¹ Duxin Zheng,² and Jian Zhou³



$$\frac{d\Delta\sigma}{dt dQ^2 dx_B d\phi} = -\sin(2\phi) \frac{\alpha_{em}^3 \alpha_s f_\pi^2 (1-y) \xi x_B \mathcal{F}(t)}{3Q^8 N_c} \left[\int_0^1 dz \frac{\phi_\pi(z)}{z(1-z)} \right]^2 \text{Im} \left[\int_{-1}^1 dx \frac{F_{1,4}^{(1)}(x, \xi, \Delta_\perp) / M^2}{(x + \xi - i\epsilon)^2 (x - \xi + i\epsilon)^2} \right]$$

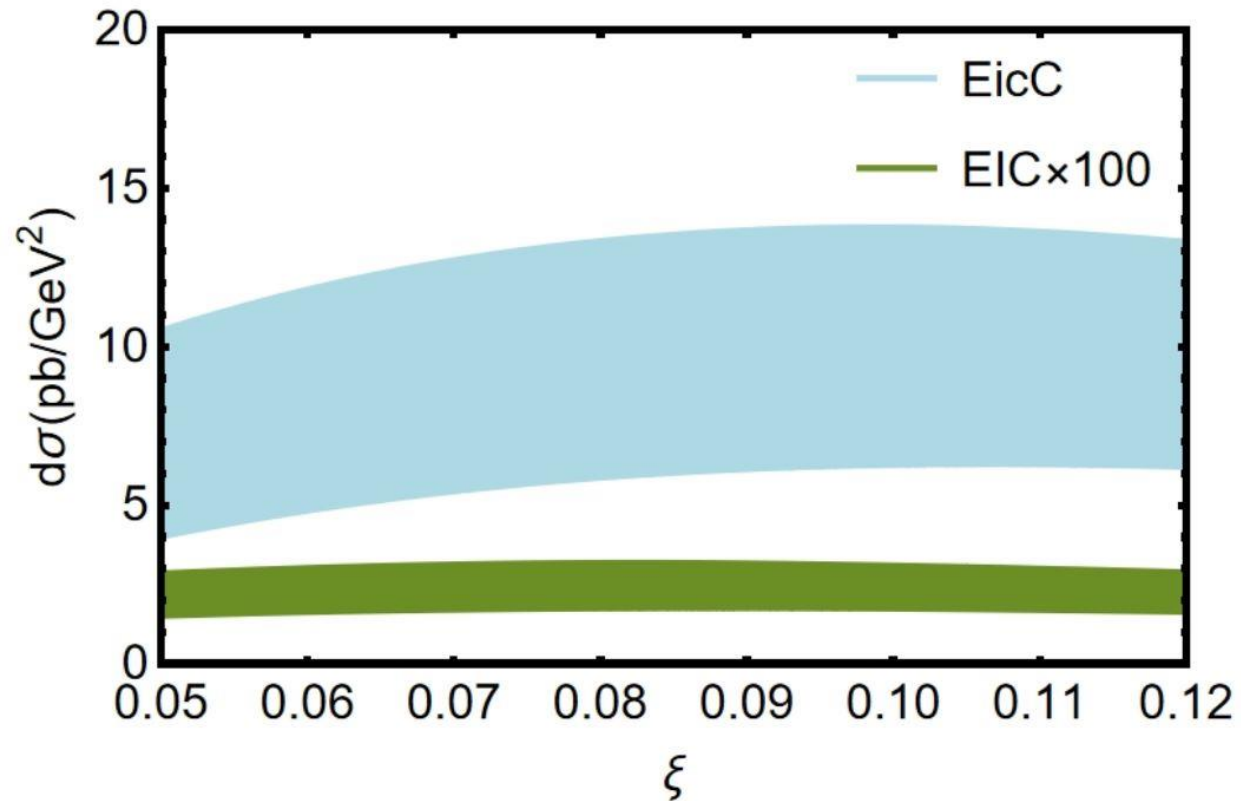
The same azimuthal asymmetry, precisely mirroring what we observe in this study, emerges from the interference between the Primakoff process and the contribution from the gluon GTMD

Probing quark OAM through π^0 production in ep collisions



Numerical results

Unpolarized cross section



Findings:

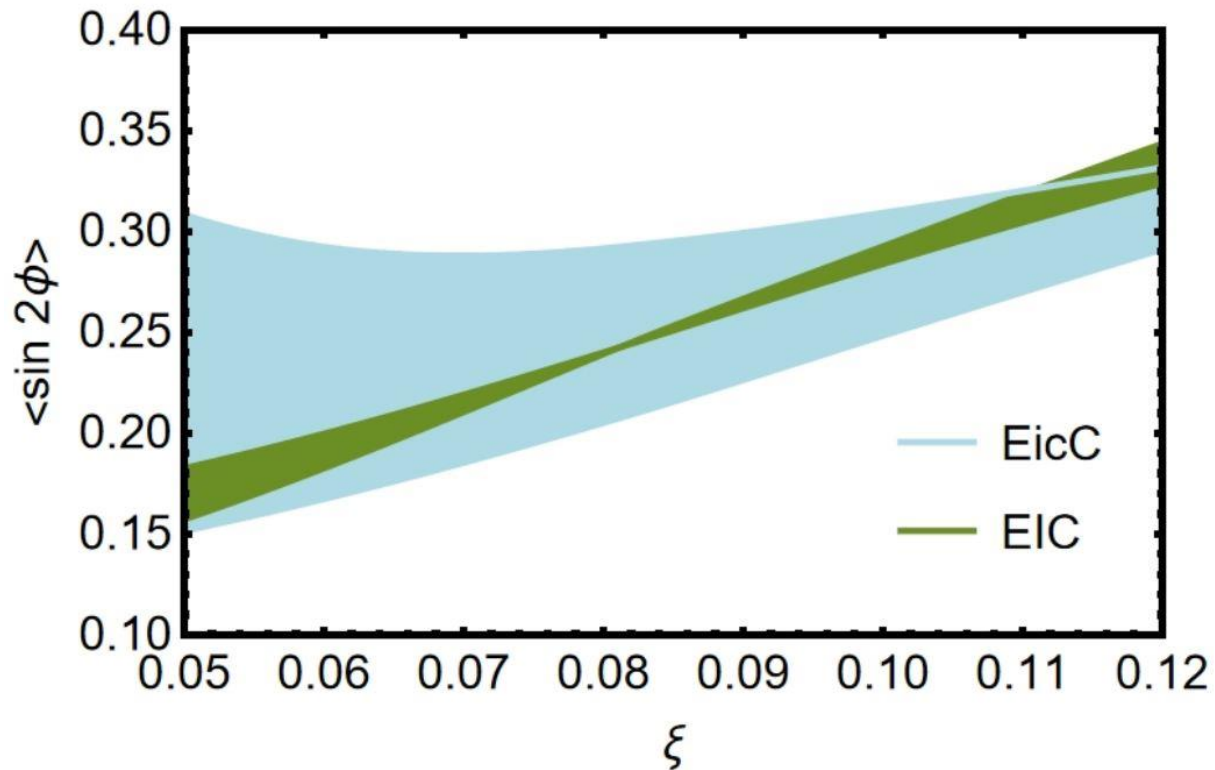
- The unpolarized cross section exhibits a notable magnitude at EicC energy
- Relatively small at EIC energy

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Numerical results

Asymmetry



$$\langle \sin(2\phi) \rangle = \frac{\int \frac{d\Delta\sigma}{d\mathcal{P}.S.} \sin(2\phi) d\mathcal{P}.S.}{\int \frac{d\sigma}{d\mathcal{P}.S.} d\mathcal{P}.S.}$$

Findings:

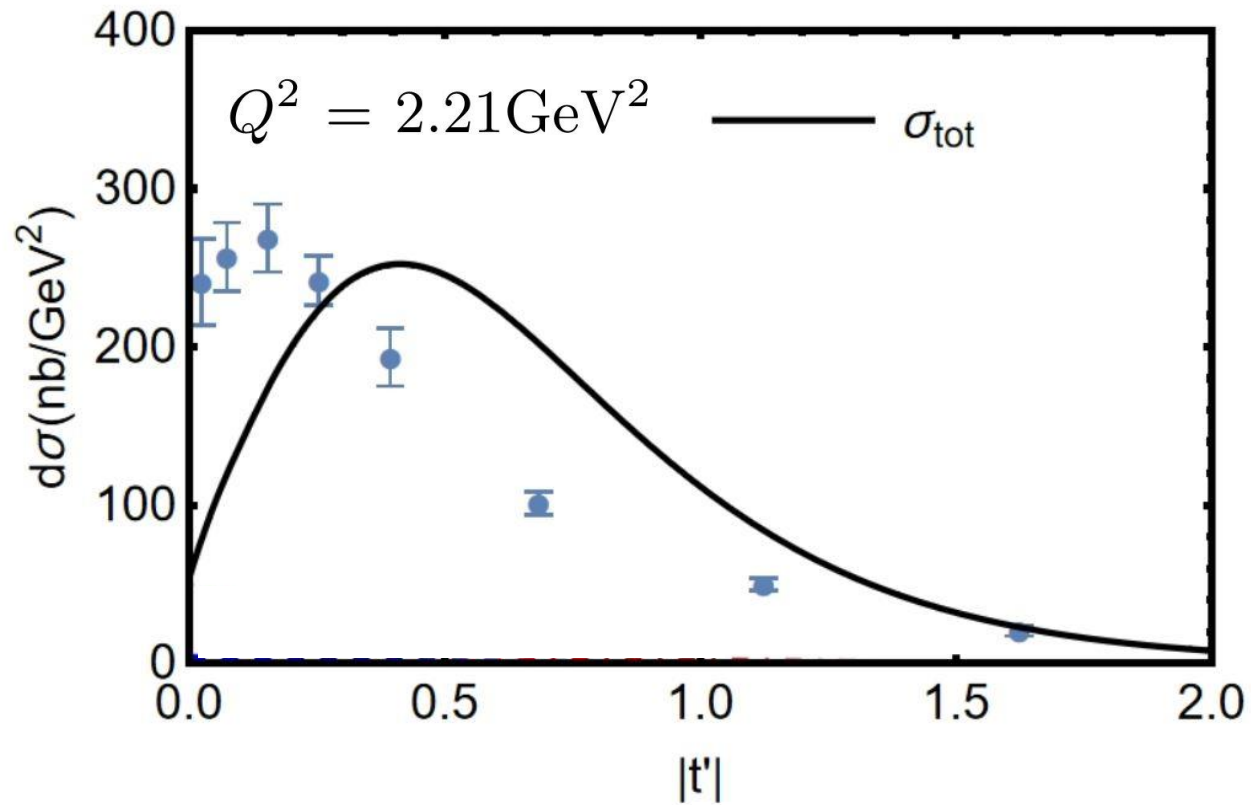
The asymmetries are substantial for both EIC & EicC kinematics

Probing quark OAM through π^0 production in ep collisions



Numerical results

Comparison with CLAS data



Unpolarized cross section:

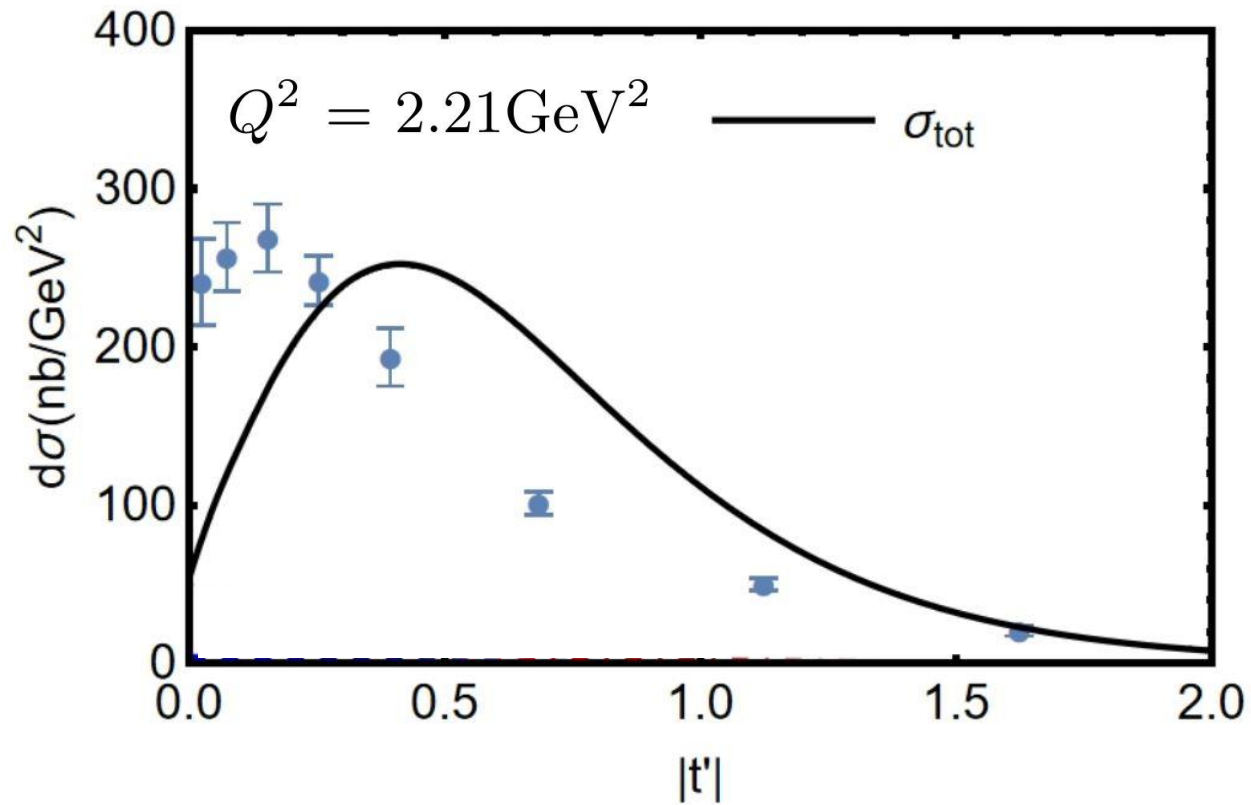
$$\frac{d\sigma_T}{dt} + a \frac{d\sigma_L}{dt}$$

Probing quark OAM through π^0 production in ep collisions



Numerical results

Comparison with CLAS data



Findings:

- Our theoretical model is in reasonable agreement with experimental data

Developments



arXiv: 1612.02438 (2016)

Hunting the Gluon Orbital Angular Momentum at the Electron-Ion Collider

Xiangdong Ji,^{1,2} Feng Yuan,³ and Yong Zhao^{1,3}

arXiv: 1702.04387 (2017)

Generalized TMDs and the exclusive double Drell-Yan process

Shohini Bhattacharya,¹ Andreas Metz,¹ and Jian Zhou²

arXiv: 1802.10550 (2018)

Exclusive double quarkonium production and generalized TM

Shohini Bhattacharya,¹ Andreas Metz,¹ Vikash Kumar Ojha,² Jeng-Yuan Tsai,¹

arXiv: 1807.08697 (2018)

Probing the Weizsäcker-Williams gluon Wigner distribution in pp collisions

Renaud Boussarie,¹ Yoshitaka Hatta,² Bo-Wen Xiao,^{3,4} and Feng Yuan⁵

arXiv: 1912.08182 (2019)

Probing the gluon Sivers function with an unpolarized GTMD distributions and the Odderons

Renaud Boussarie,¹ Yoshitaka Hatta,¹ Lech Szymanowski,² and S

arXiv: 2106.13466 (2021)

Probing the gluon tomography in photoproduction of di-pions

Yoshikazu Hagiwara, Cheng Zhang, Jian Zhou, and Ya-jin Zhou

arXiv: 2201.08709 (2022/2024)

Signature of the gluon orbital angular momentum

Shohini Bhattacharya,^{1,*} Renaud Boussarie,^{2,†} and Yoshitaka Hatta^{1,3,‡}

arXiv: 2205.00045 (2022)

Angular correlations in exclusive dijet photoproduction in ultra-peripheral PbPb collisions at $\sqrt{s_{NN}} = 5.02$ TeV



Selected works on gluon GTMDs

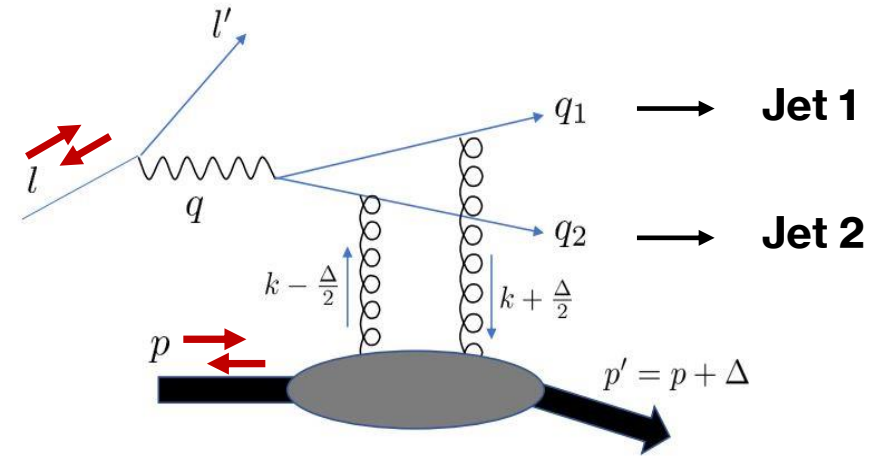
Probing gluon OAM through exclusive di-jet production

PHYSICAL REVIEW LETTERS **128**, 182002 (2022)

DOE Highlight

Signature of the Gluon Orbital Angular Momentum

Shohini Bhattacharya^{1,*}, Renaud Boussarie^{2,†} and Yoshitaka Hatta^{1,3,‡}





Selected works on gluon GTMDs

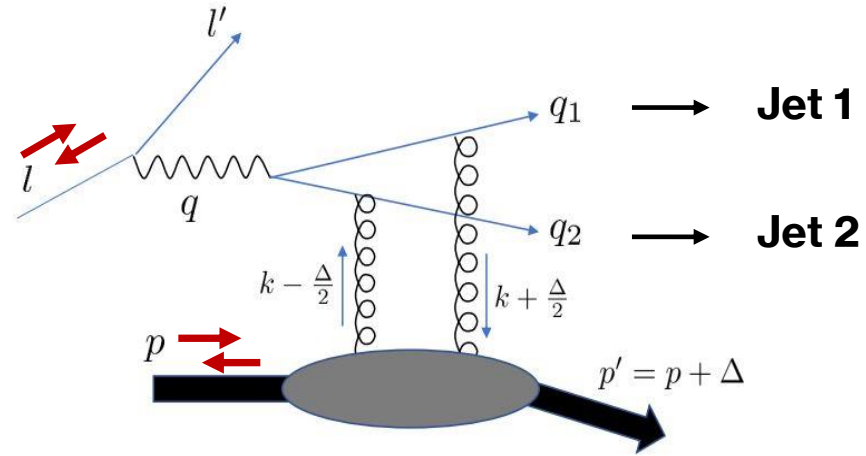
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Main result (double spin asymmetry):

Signature of gluon OAM is cosine angular modulation

$$d\sigma^{\text{asym}} \sim -\text{Re} \left[\left\{ \mathcal{H}_g^{(1)*}(\xi) + \frac{4q_{\perp}^2}{q_{\perp}^2 + \mu^2} \mathcal{H}_g^{(2)*}(\xi) \right\} \mathcal{L}_g(\xi) \right] \cos(\phi_{l_{\perp}} - \phi_{\Delta_{\perp}}) \\ + \text{Re} \left[\mathcal{H}_g^{(1)*}(\xi) \tilde{\mathcal{H}}_g^{(2)}(\xi) \right] \cos(\phi_{l_{\perp}} - \phi_{\Delta_{\perp}})$$



Selected works on gluon GTMDs

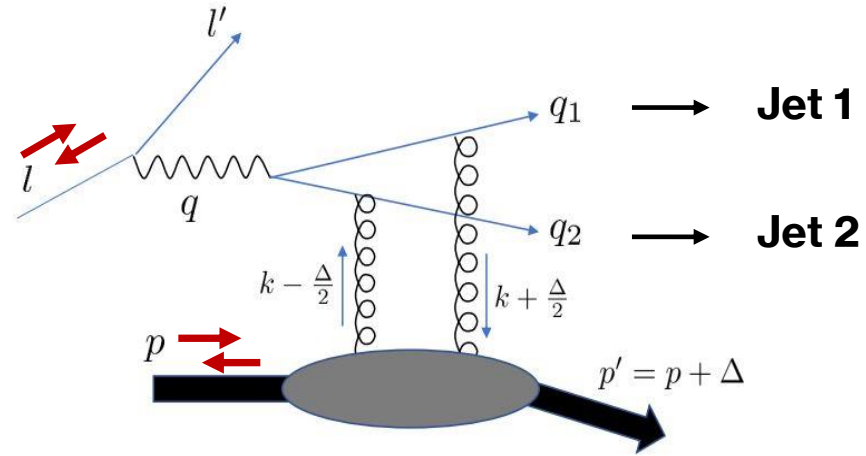
Probing gluon OAM through exclusive di-jet production

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Signature of the Gluon Orbital Angular Momentum

Shohini Bhattacharya^{1,*}, Renaud Boussarie^{2,†} and Yoshitaka Hatta^{1,3,‡}



Gluon helicity contributes to the same angular modulation as that of OAM

$$d\sigma^{\text{asym}} \sim -\text{Re} \left[\left\{ \mathcal{H}_g^{(1)*}(\xi) + \frac{4q_\perp^2}{q_\perp^2 + \mu^2} \mathcal{H}_g^{(2)*}(\xi) \right\} \mathcal{L}_g(\xi) \right] \cos(\phi_{l_\perp} - \phi_{\Delta_\perp})$$

Helicity GPD
(intrinsic spin)

$$+\text{Re} \left[\mathcal{H}_g^{(1)}(\xi) + \tilde{\mathcal{H}}_g^{(2)}(\xi) \right] \cos(\phi_{l_\perp} - \phi_{\Delta_\perp})$$



Selected works on gluon GTMDs

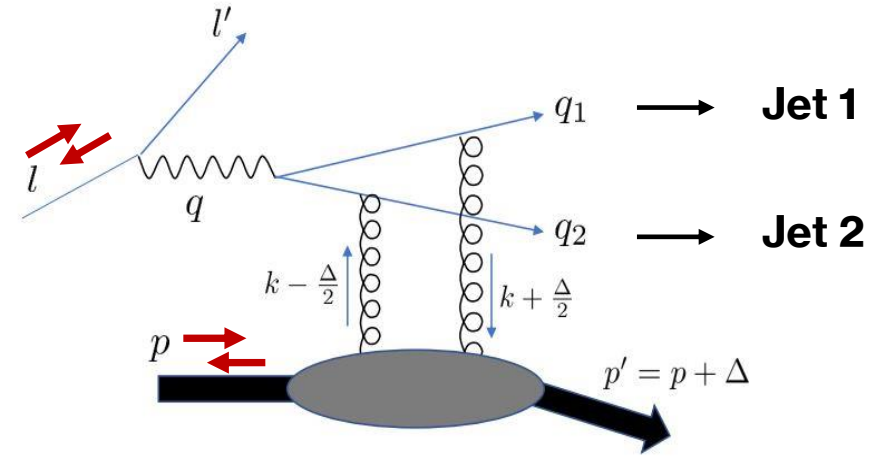
Probing gluon OAM through exclusive di-jet production

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DOE Highlight

Signature of the Gluon Orbital Angular Momentum

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Our observable is a simultaneous probe of gluon OAM & it's helicity

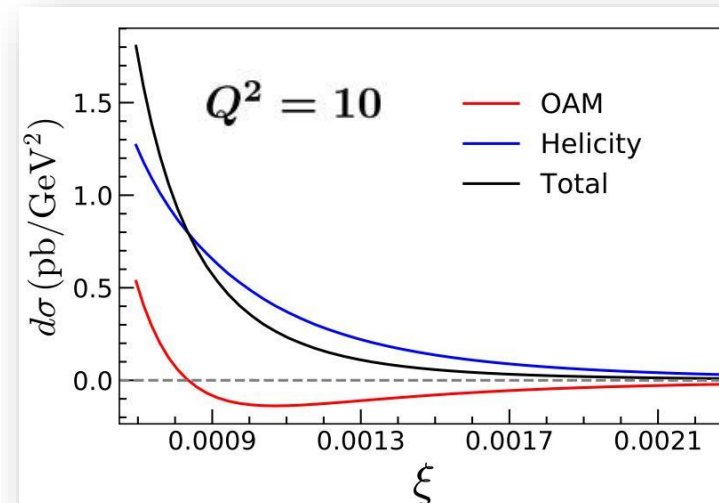
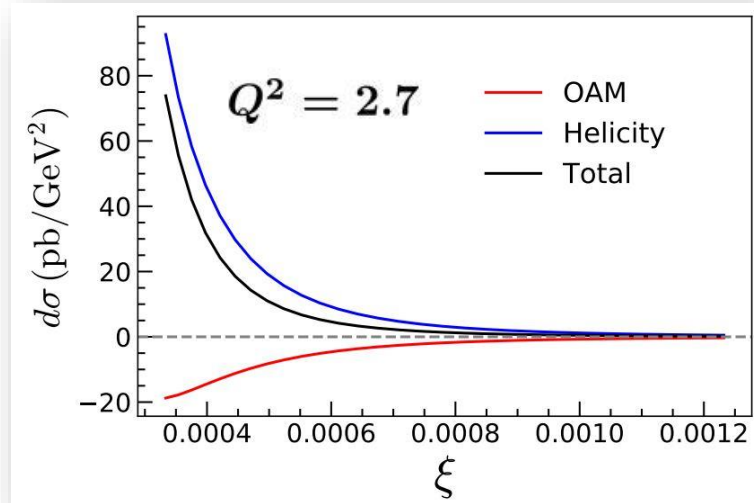
$$d\sigma^{\text{asym}} \sim -\text{Re} \left[\left\{ \mathcal{H}_g^{(1)*}(\xi) + \frac{4q_\perp^2}{q_\perp^2 + \mu^2} \mathcal{H}_g^{(2)*}(\xi) \right\} \mathcal{L}_g(\xi) \right] \cos(\phi_{l_\perp} - \phi_{\Delta_\perp})$$

$$+ \text{Re} \left[\mathcal{H}_g^{(1)*}(\xi) \tilde{\mathcal{H}}_g^{(2)}(\xi) \right] \cos(\phi_{l_\perp} - \phi_{\Delta_\perp})$$

Selected works on gluon GTMDs



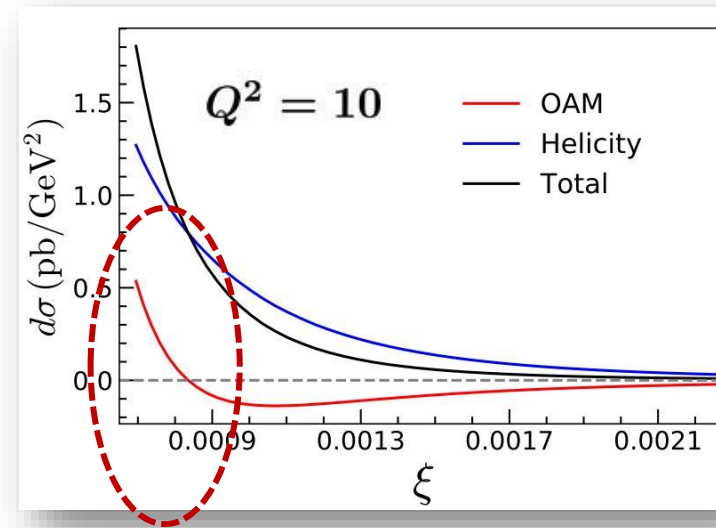
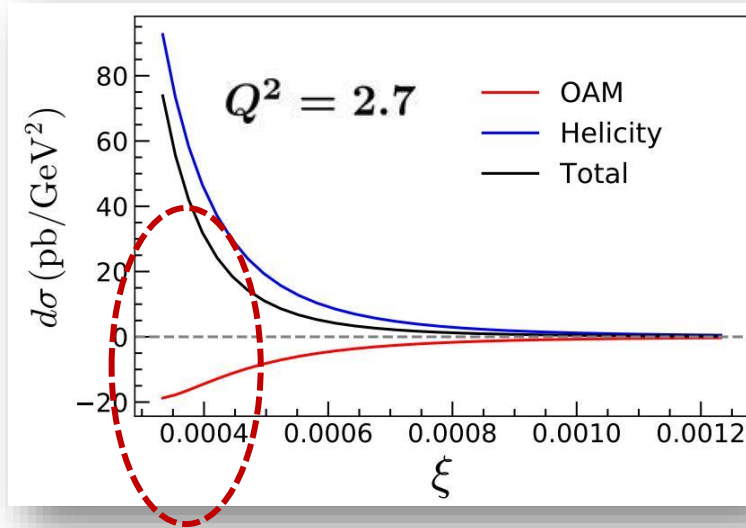
Interplay between OAM and helicity at small x





Selected works on gluon GTMDs

Interplay between OAM and helicity at small x



Schematic structure of our observable:

$$d\sigma^{\text{asym}} \sim \mathcal{H}_g^{(1)*}(\xi) \left(\tilde{\mathcal{H}}_g^{(2)}(\xi) + \frac{q_{\perp}^2 - Q^2/4}{q_{\perp}^2 + Q^2/4} \mathcal{L}_g(\xi) \right)$$

\downarrow
 $\Delta G(x)$

\downarrow
 $L_g(x)$

Yuri Kovchegov's talk

Cancellation expected between helicity & OAM at small x

$$\Delta G(x) \approx -L_g(x)$$

Boussarie, Hatta, Yuan (2019)
Kovchegov, Manley (2023, 2024)

Selected works on gluon GTMDs



Contribution from spin-orbit correlation at small x ?

Yet another contribution to the process:

$$d\sigma^{\text{asym}} \sim \frac{4q_{\perp}^2}{q_{\perp}^2 + \mu^2} C_g^{(2)}(\xi) \tilde{\mathcal{H}}_g^{(2)}(\xi)$$

Spin-orbit correlation:

$$C^g(x) = \int d^2\vec{k}_{\perp} \frac{\vec{k}_{\perp}^2}{M^2} G_{1,1}^g(x, \vec{k}_{\perp}^2)$$

Selected works on gluon GTMDs



Contribution from spin-orbit correlation at small x ?

Yet another contribution to the process:

$$d\sigma^{\text{asym}} \sim \frac{4q_{\perp}^2}{q_{\perp}^2 + \mu^2} C_g^{(2)}(\xi) \tilde{\mathcal{H}}_g^{(2)}(\xi)$$

First insight into the small- x behavior of spin-orbit correlation:

$$C^g(x) \approx -2x \int_x^1 \frac{dx'}{x'^2} G(x') + \dots \propto -G(x)$$

(SB, Boussarie, Hatta,
2404.04208 , 2404.04209)

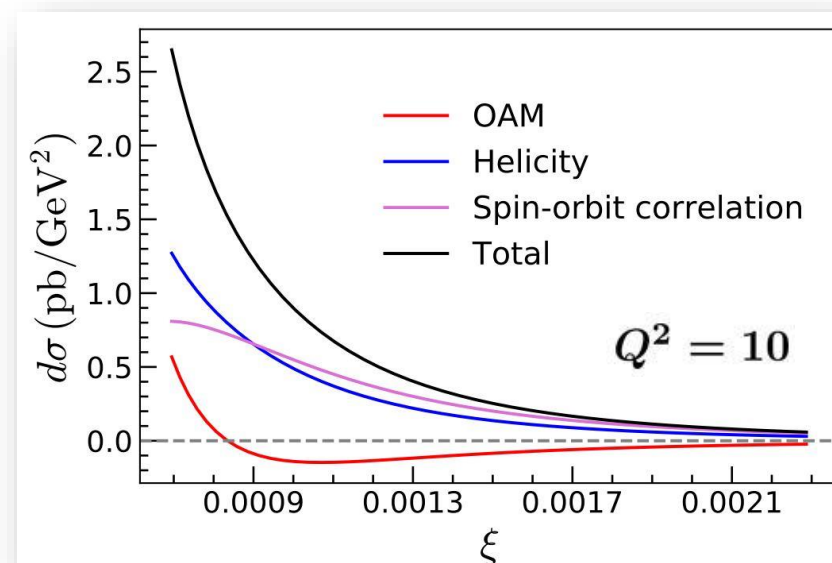
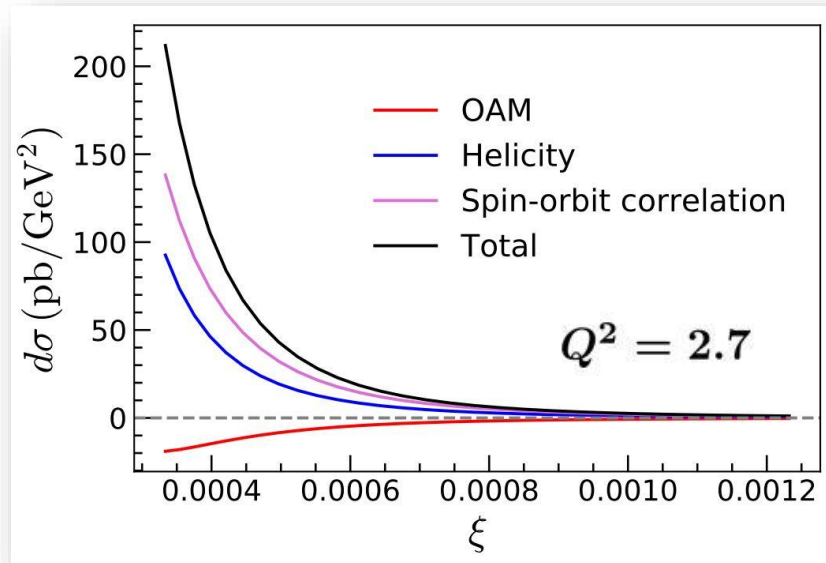
For a complete twist structure of spin-orbit correlation, see Hatta, Schoenleber, 2404.18872



Selected works on gluon GTMDs

Probing gluon OAM & spin-orbit correlation at small x

Updated numerical results (SB, Boussarie, Hatta, 2404.04209):



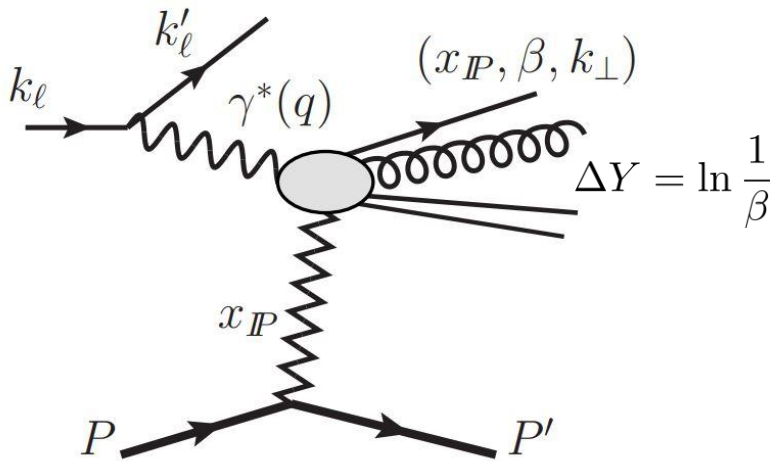
Spin-orbit correlation is more accurately constrained than **OAM** because the latter necessitates the precise determination of both unpolarized and polarized gluon distributions



Selected works on gluon GTMDs

Probing gluon OAM through Semi Inclusive Diffractive Deep Inelastic Scattering

Feng Yuan's talk



- Measure invariant mass of diffractively produced system instead of reconstructing jets

$$M_X^2 = \frac{q_\perp^2}{z\bar{z}} = \frac{1-\beta}{\beta} Q^2$$

- Tag hadron species out of the diffractively produced system

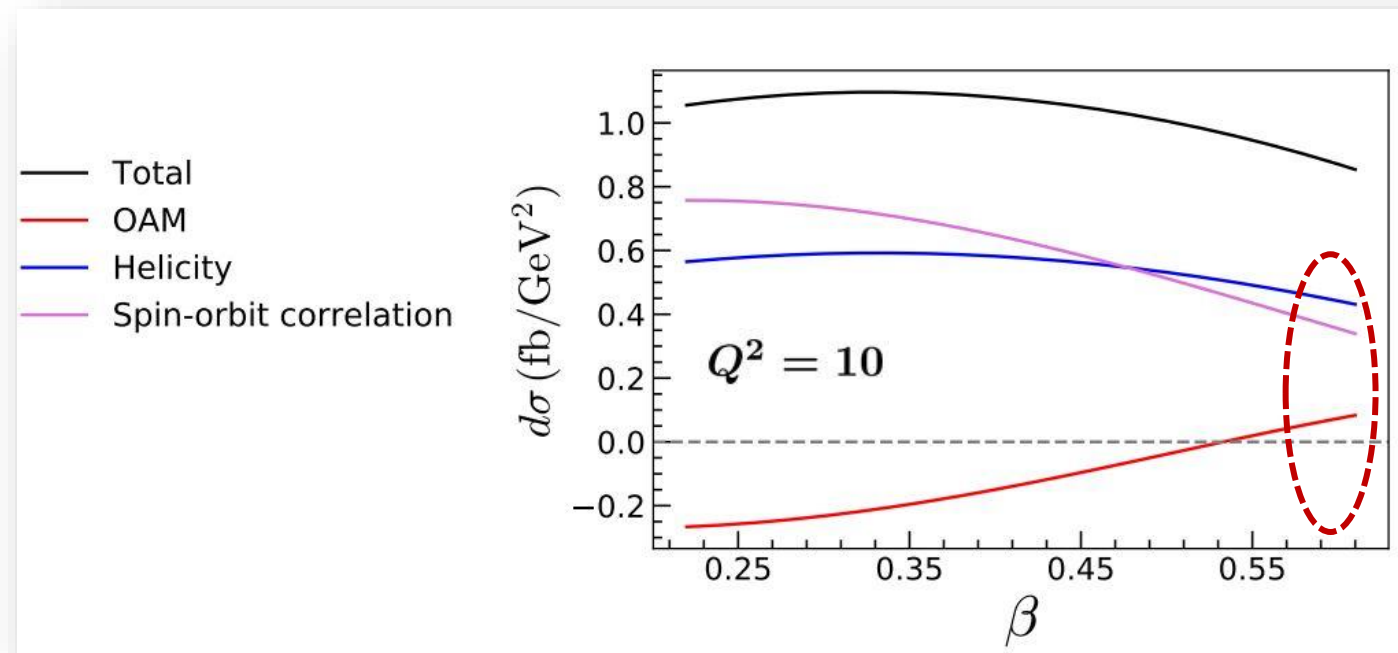
Hatta, Xiao, Yuan (2022)



Selected works on gluon GTMDs

Probing gluon OAM through Semi Inclusive Diffractive Deep Inelastic Scattering

Numerical results (SB, Boussarie, Hatta, 2404.04209):



Challenging, yet there is no requirement to reconstruct jets & we still maintain sensitivity to OAM



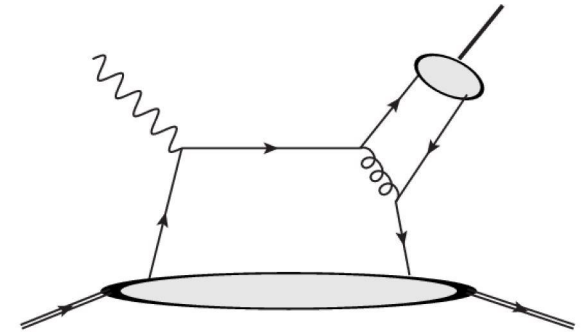
Summary

- Generalized TMDs/Wigner functions are the holy grail of spin physics



Summary

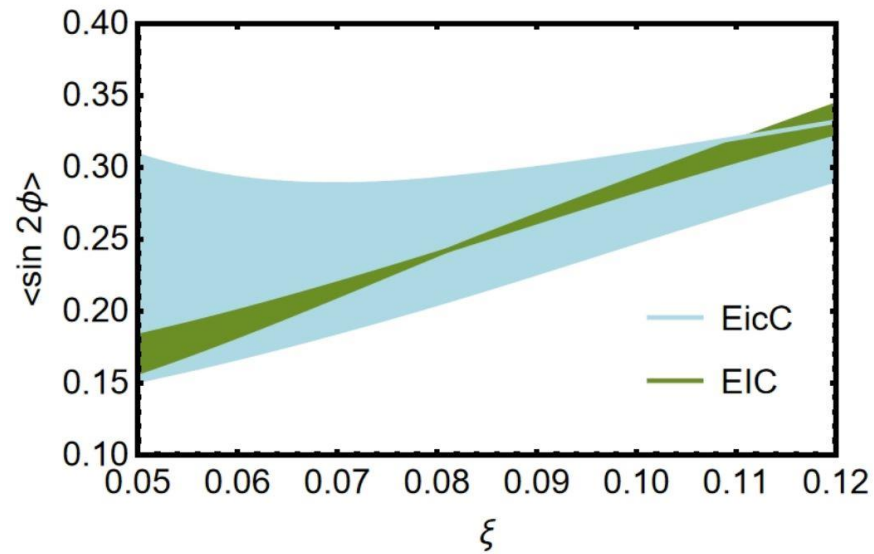
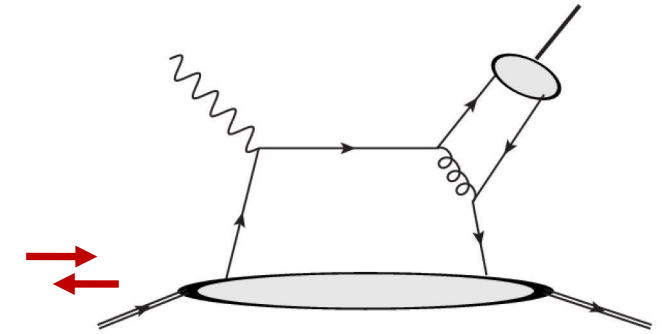
- Generalized TMDs/Wigner functions are the holy grail of spin physics
- Probe **quark OAM** via exclusive π^0 production in ep collisions
- Circumvent challenges associated with double Drell-Yan process





Summary

- Generalized TMDs/Wigner functions are the holy grail of spin physics
- Probe **quark OAM** via exclusive π^0 production in ep collisions
- Circumvent challenges associated with double Drell-Yan process

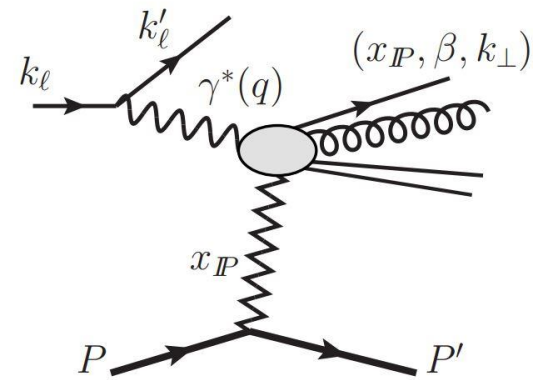
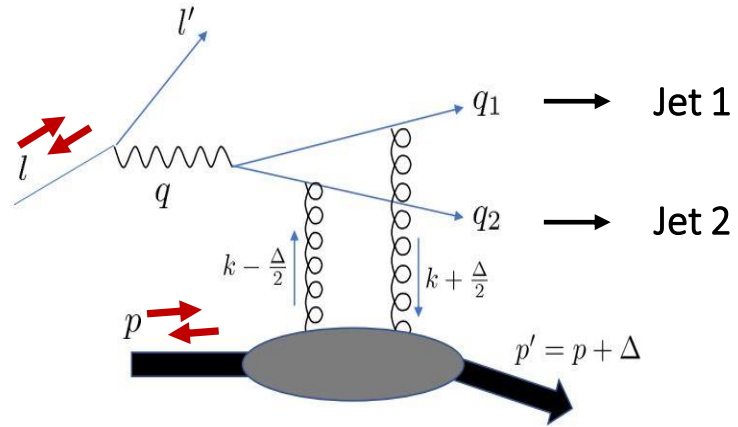


- Longitudinal single-target spin asymmetry is not power suppressed
- Asymmetry is substantial & thus exclusive π^0 production in ep collisions maybe a promising route to constrain quark OAM



Summary

- Probe **gluon OAM** via exclusive di-jet production/ SIDDIS in ep collisions





Summary

- Probe **gluon OAM** via exclusive di-jet production/ SIDDIS in ep collisions

