

# Jet Evolution within Deconfined QCD Matter

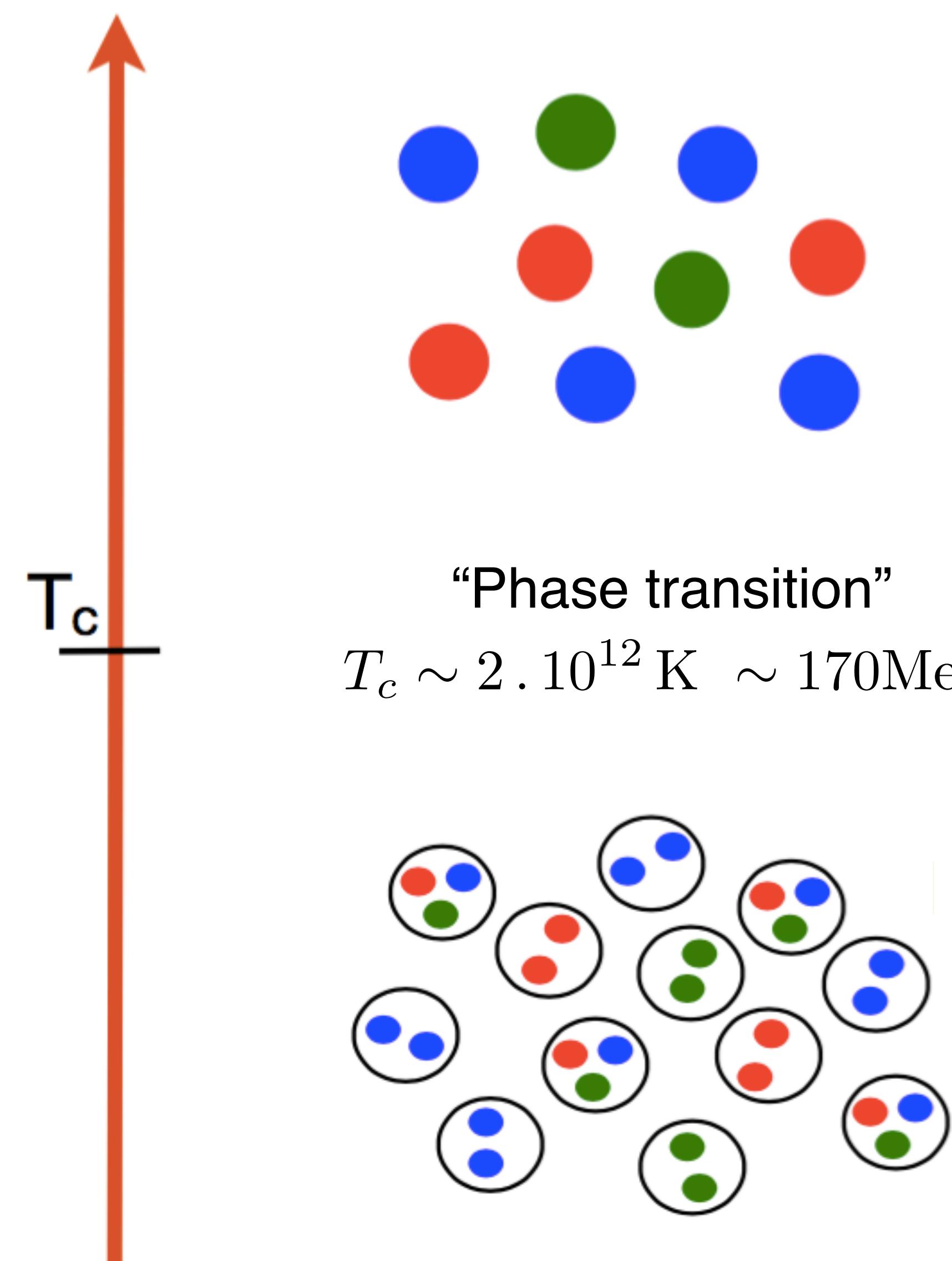
Daniel Pablos - INFN Torino



Istituto Nazionale di Fisica Nucleare

This project has received funding from the European Union's Horizon 2020 research and innovation programme under the Marie Skłodowska-Curie grant agreement n. 754496.

Fellini Seminar  
1st Dec. 2023



A New Phase: *Quark-Gluon Plasma (QGP)*:

- Filled the universe  $\mu$ s after Big Bang.
- Colour is liberated.
- A gas of quarks and gluons.

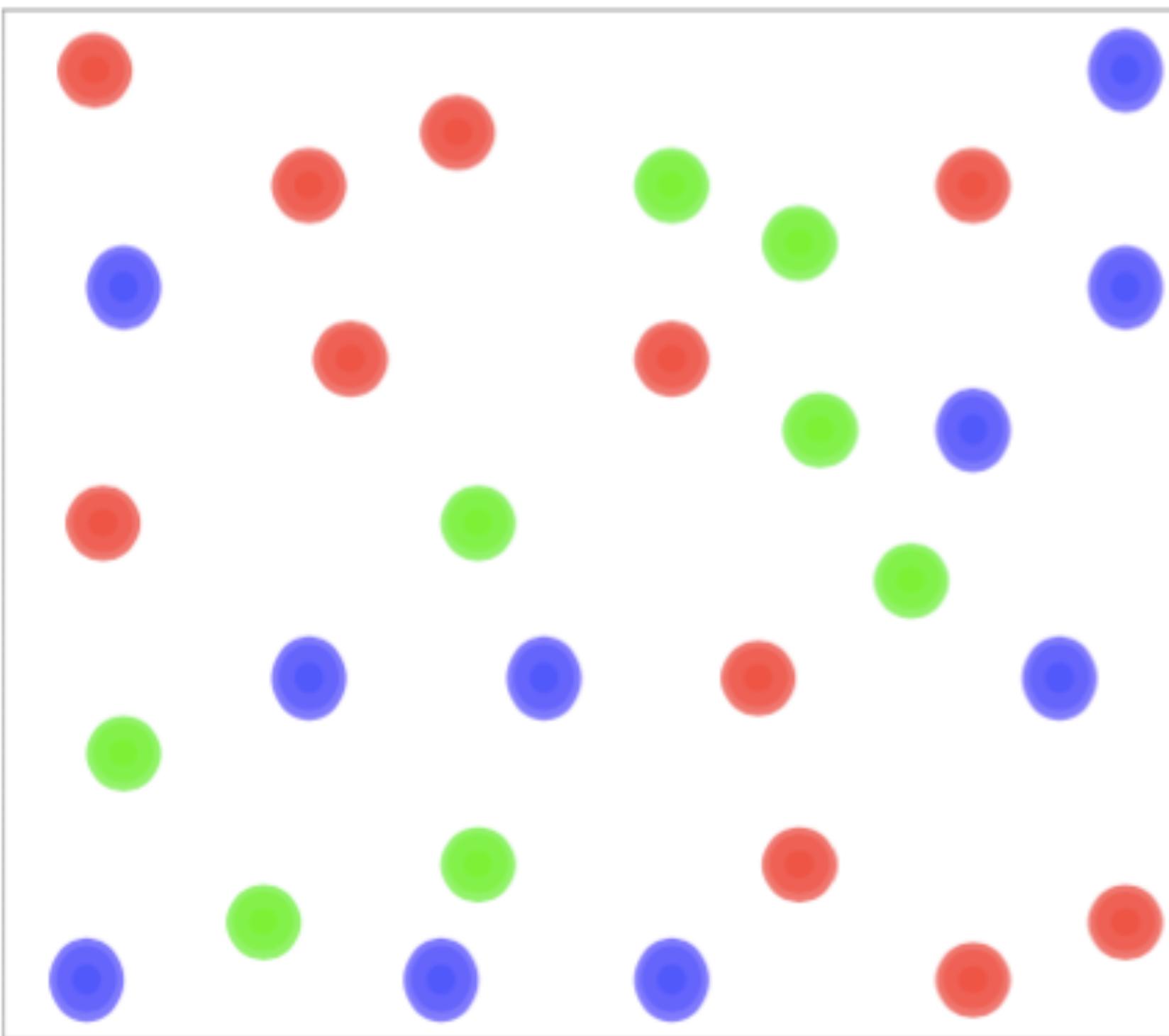
*What are the properties of the plasma close to the transition?*

Hadron Gas:

- Color is confined.
- Hadrons re-scatter.

# A Gas of Quarks and Gluons

$$T > 10^4 \text{ GeV}$$



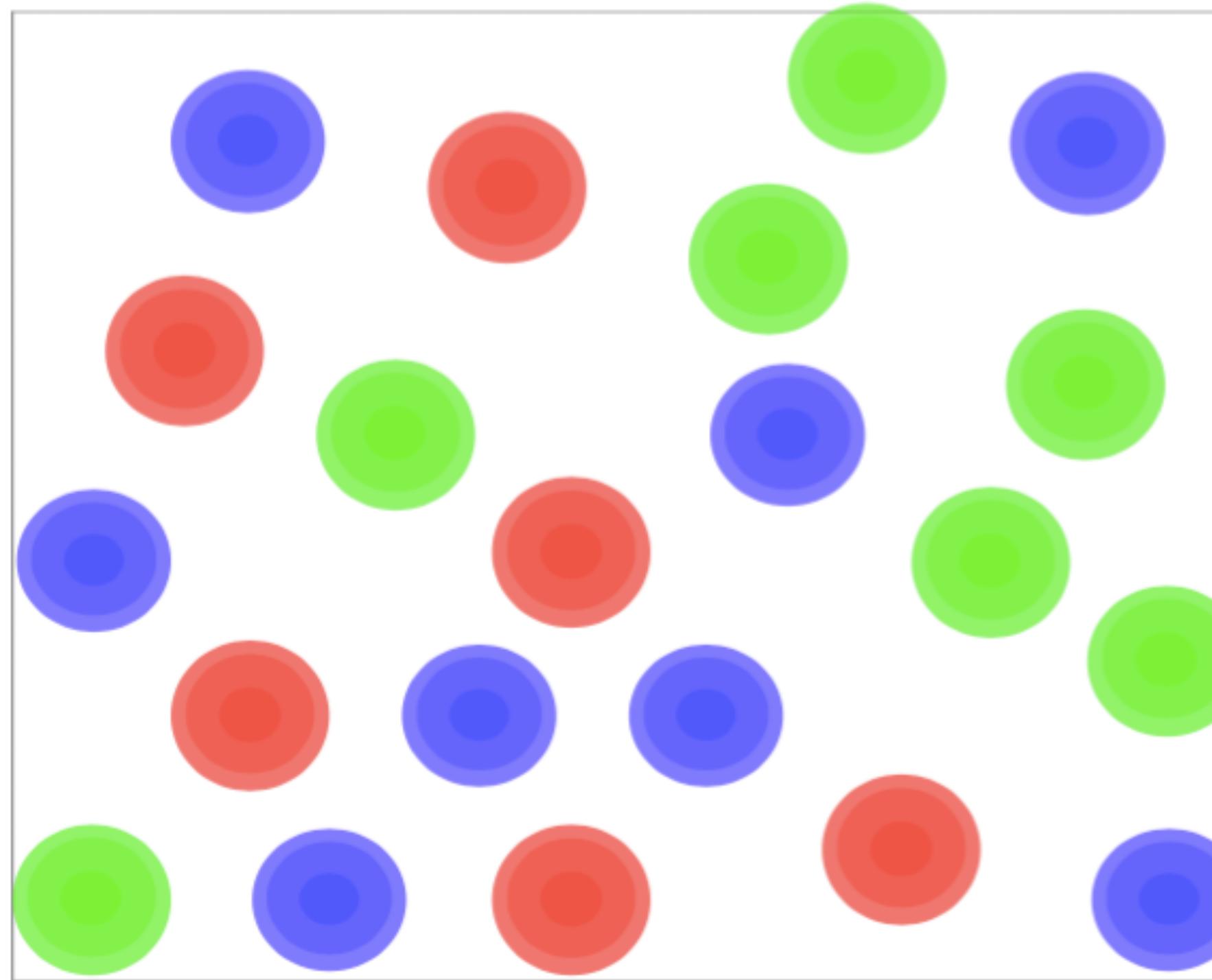
Resummation techniques can bring the validity of perturbative methods to much lower temperatures  
(e.g. Hard Thermal Loop)

$$\frac{1}{T} \ll \frac{1}{gT} \ll \frac{1}{g^2 T}$$

Inter-particle spacing      Interaction range      Mean free path

# Which is the Correct Picture of the Plasma?

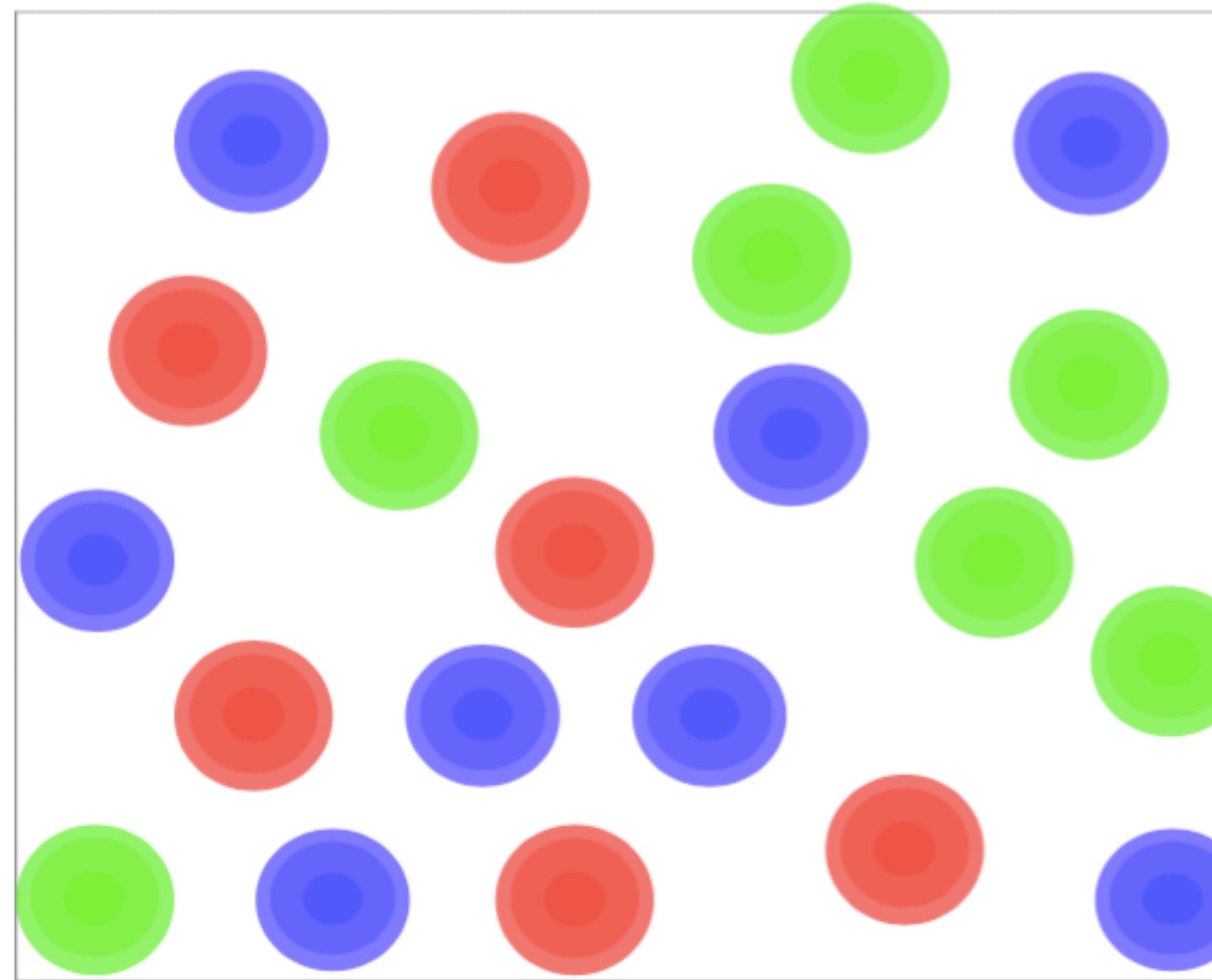
$T \sim 0.2 \text{ GeV}$



Is it a gas of quarks and gluons?

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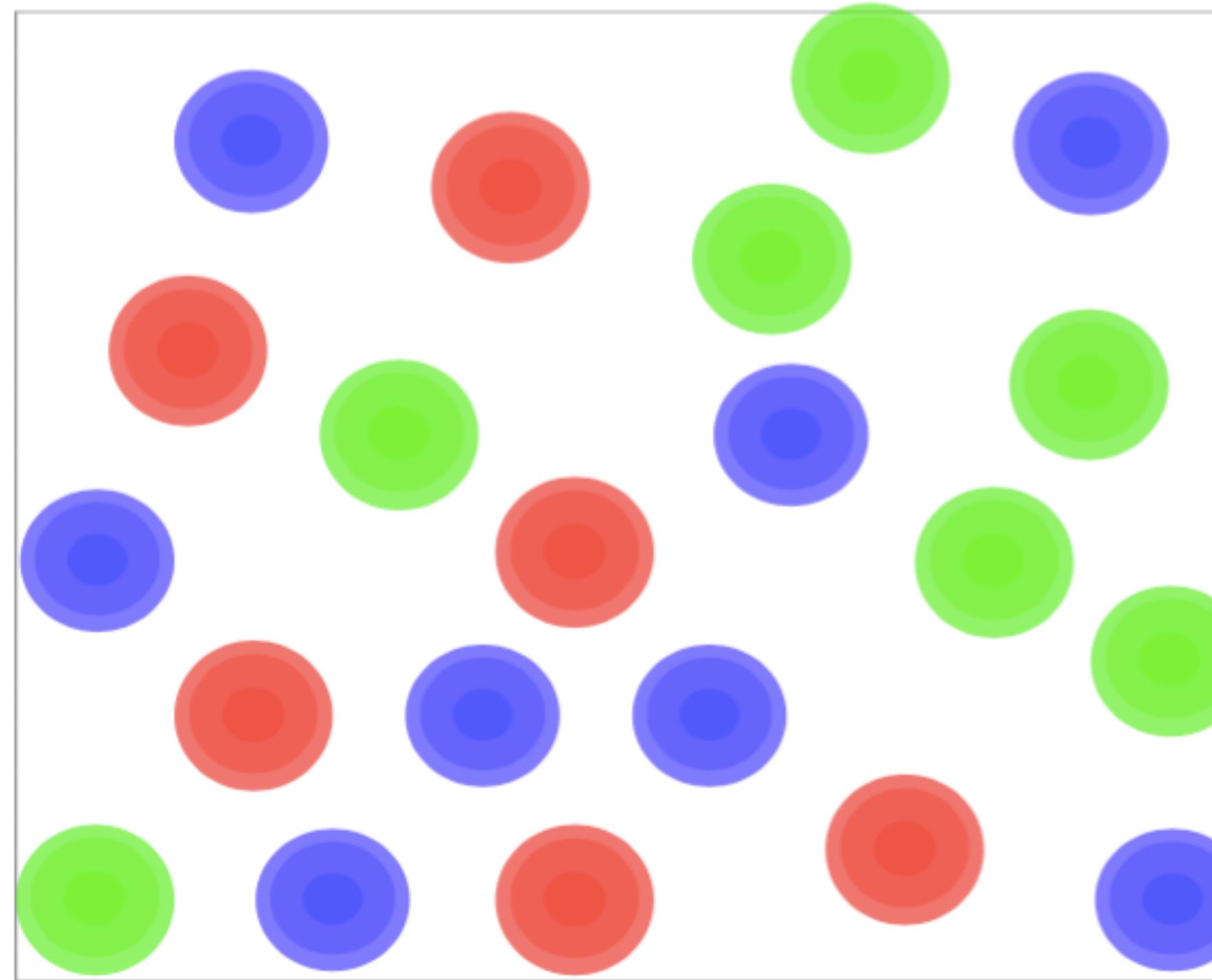


Is it a gas of quarks and gluons?

$$\alpha_s = 0.3 \rightarrow g = 2$$

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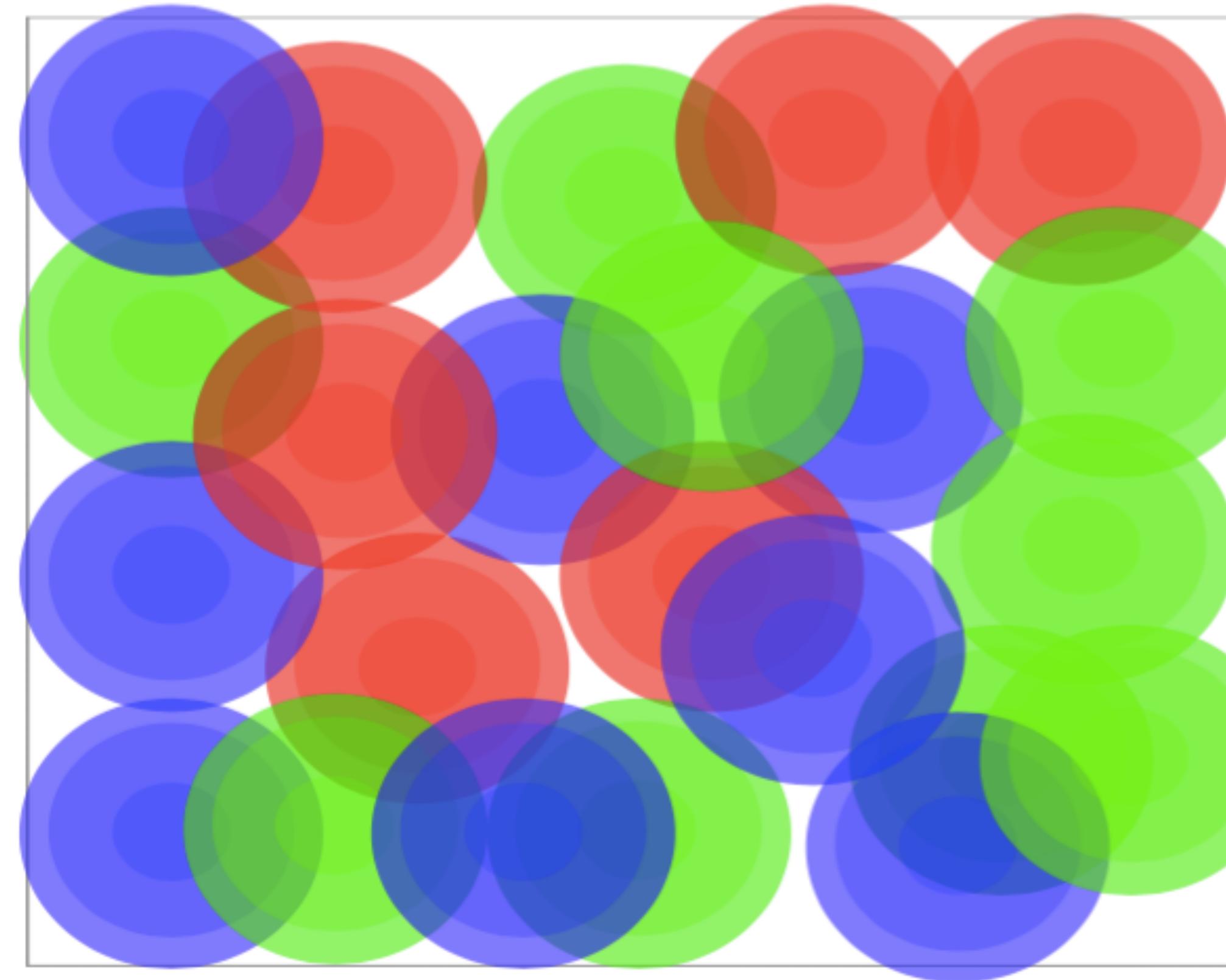
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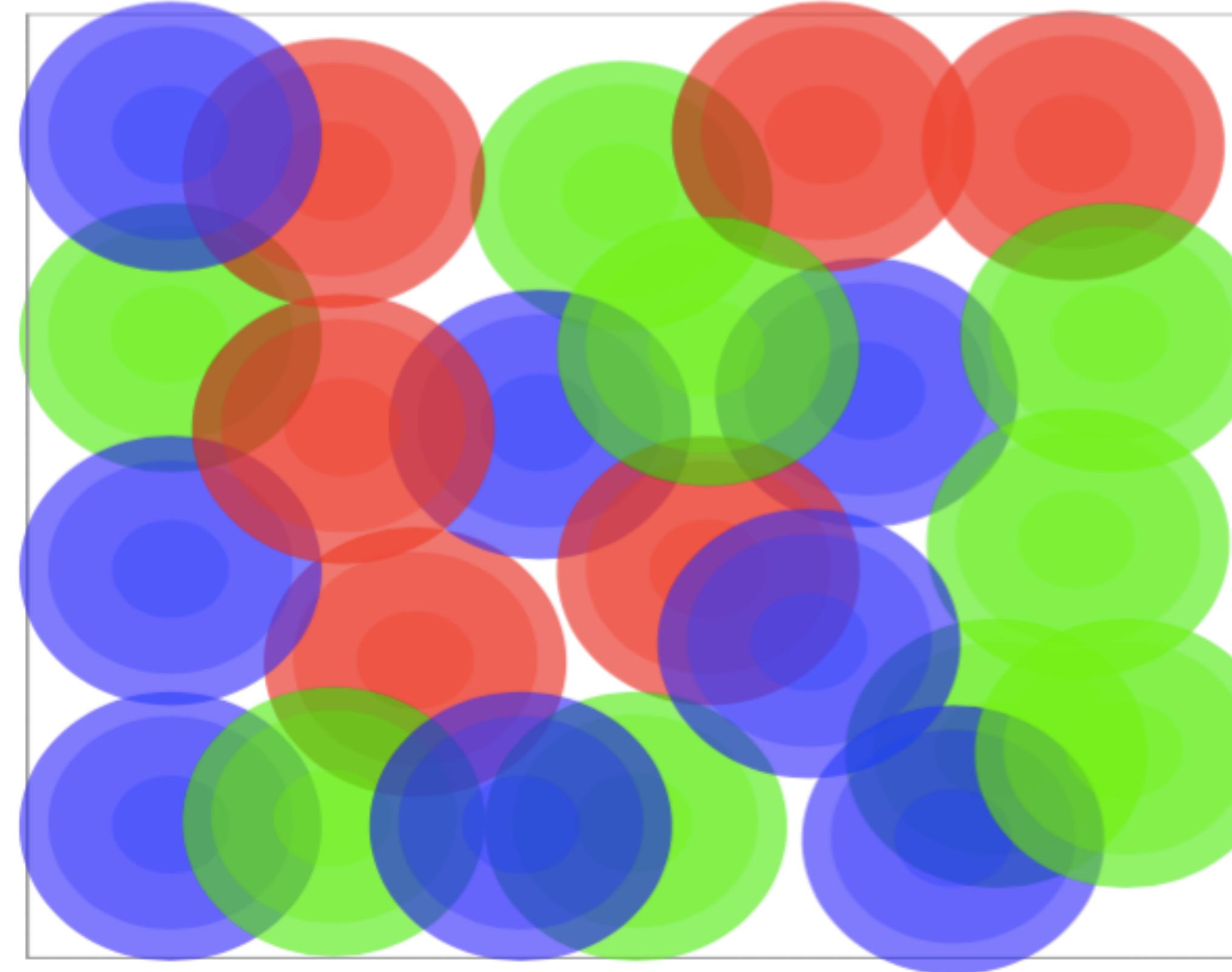
Is it a system with no long lived excitations?

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# Which is the Correct Picture of the Plasma?

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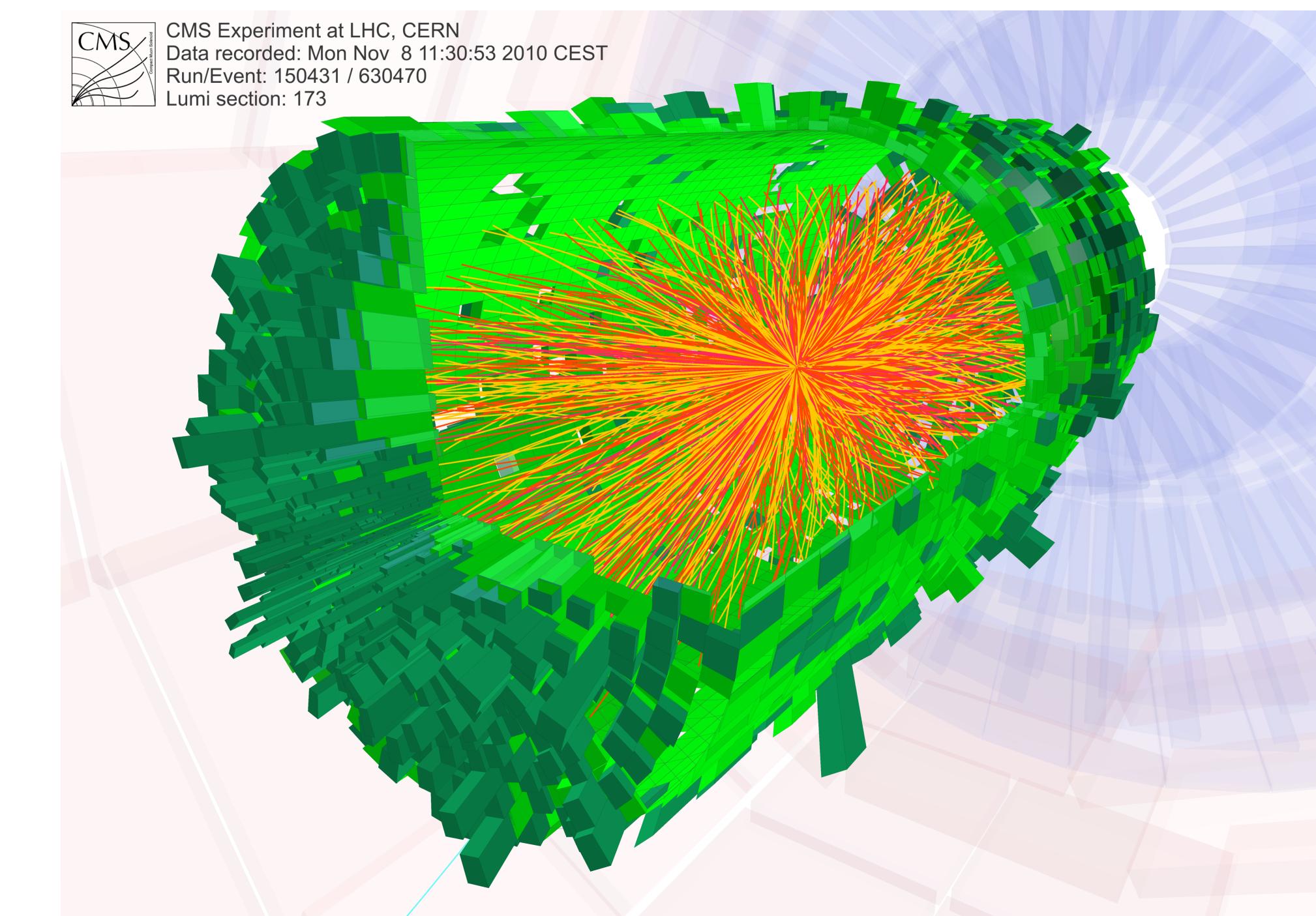
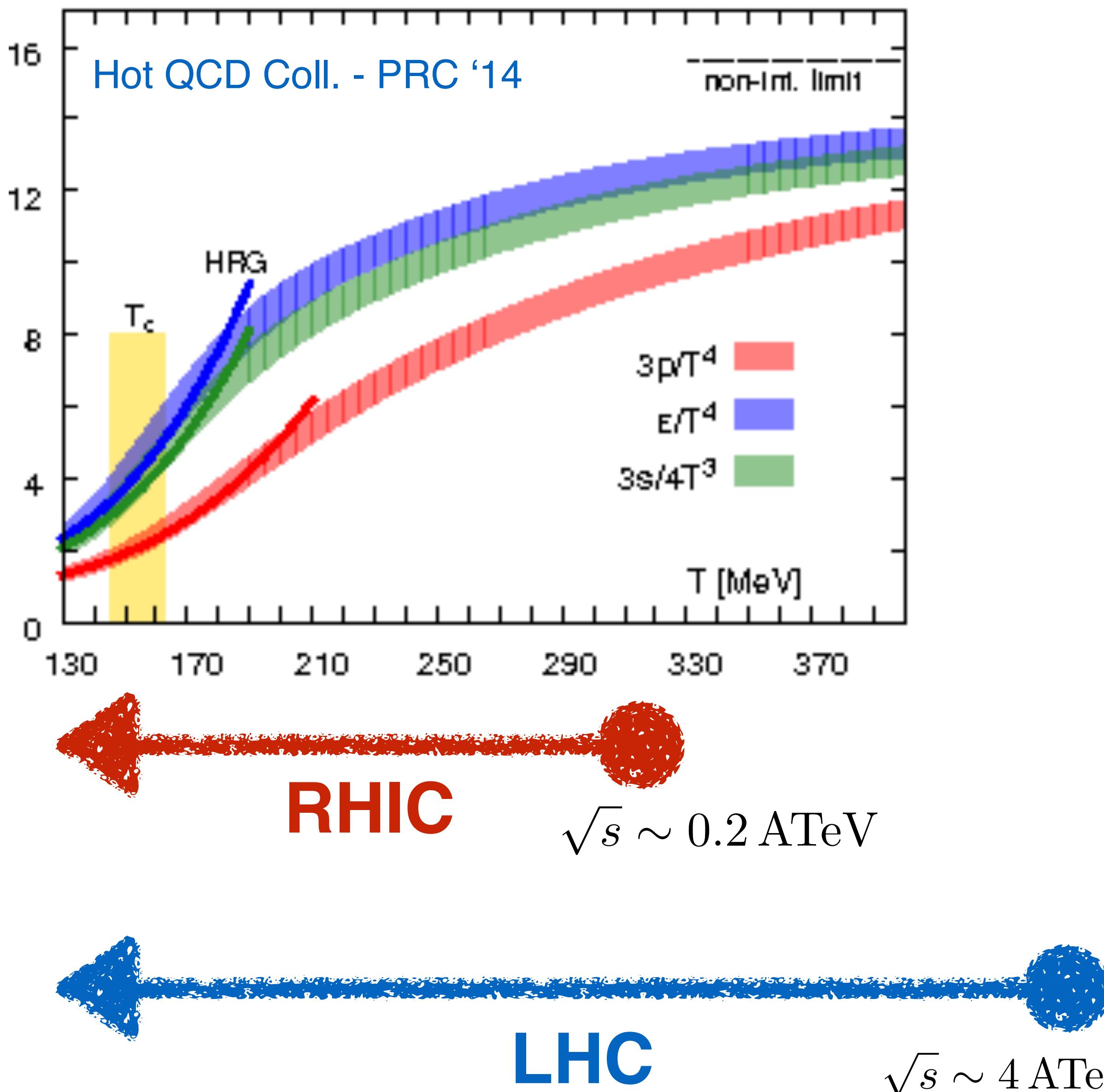


Is it a system with no quasiparticles?

$$\alpha_s = 0.3 \rightarrow g = 2$$

$$T \sim gT \sim g^2T$$

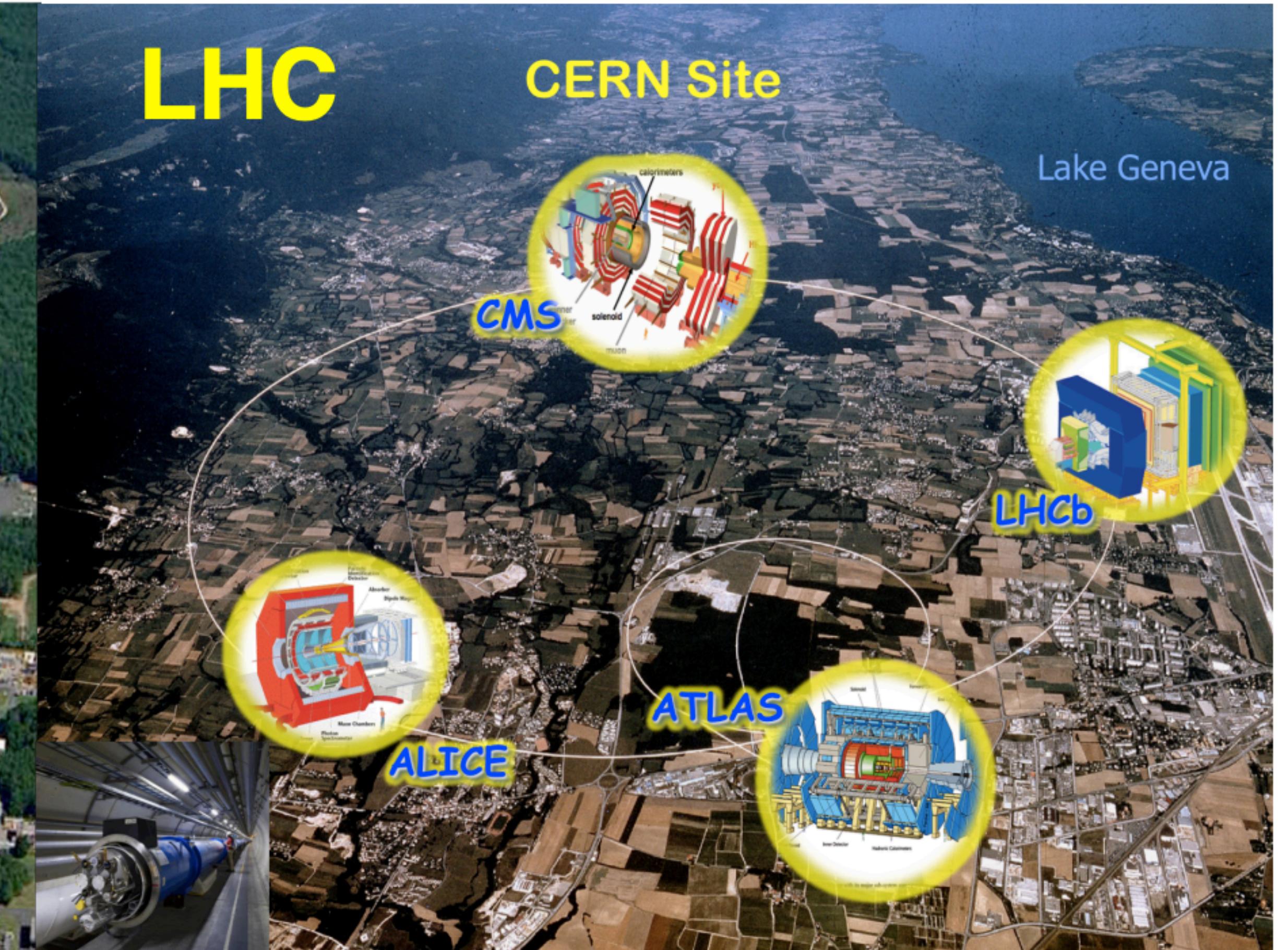
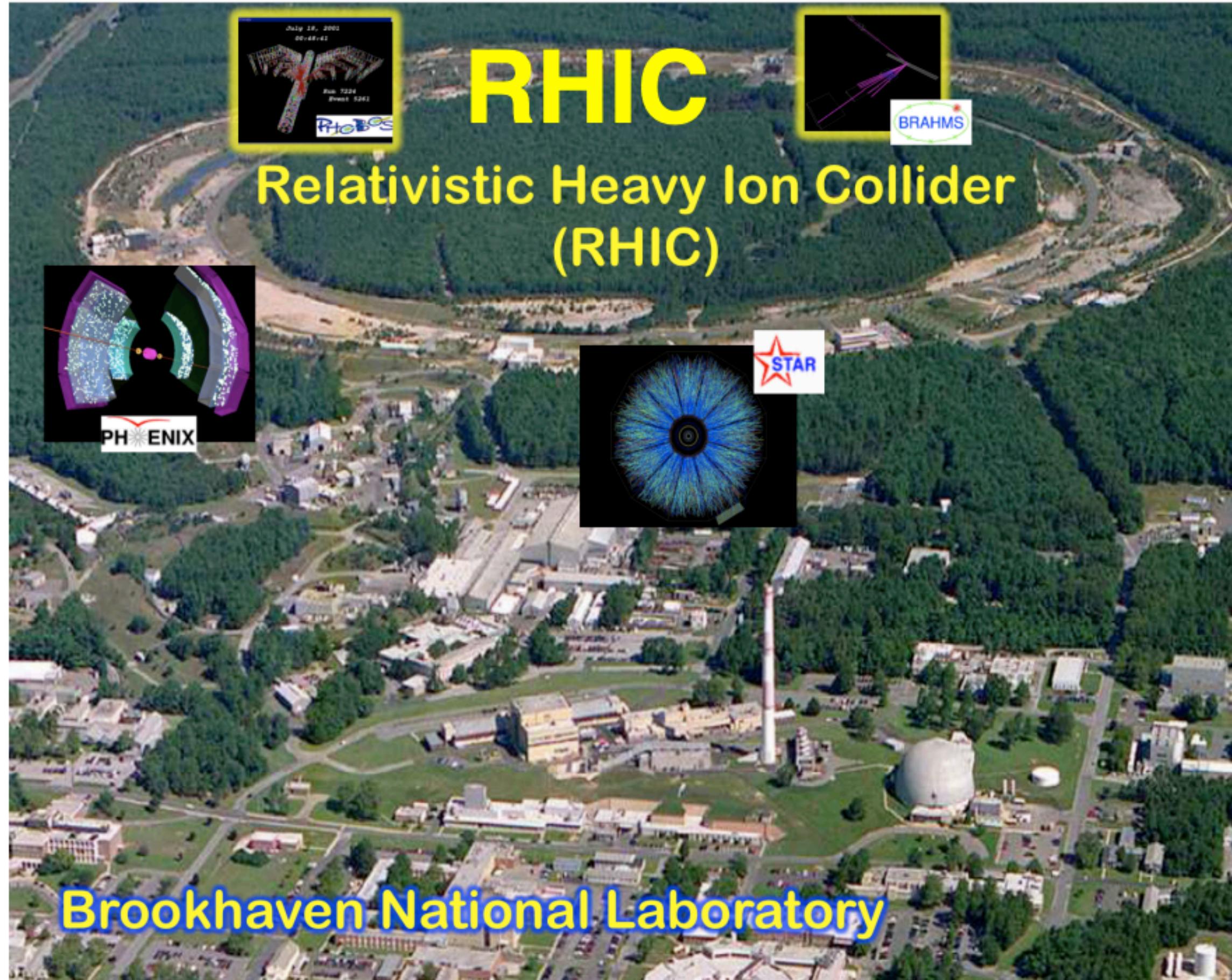
# Heavy-Ion Collisions (HIC): The Little Bangs



- Deconfined matter in experiments:
  - Very strong collective effects.
  - Thousands of particles correlated according to initial geometry.
  - Hydrodynamic explosion!

# Heavy-Ion Collisions (HIC): The Little Bangs

slide adapted from Z. Chen

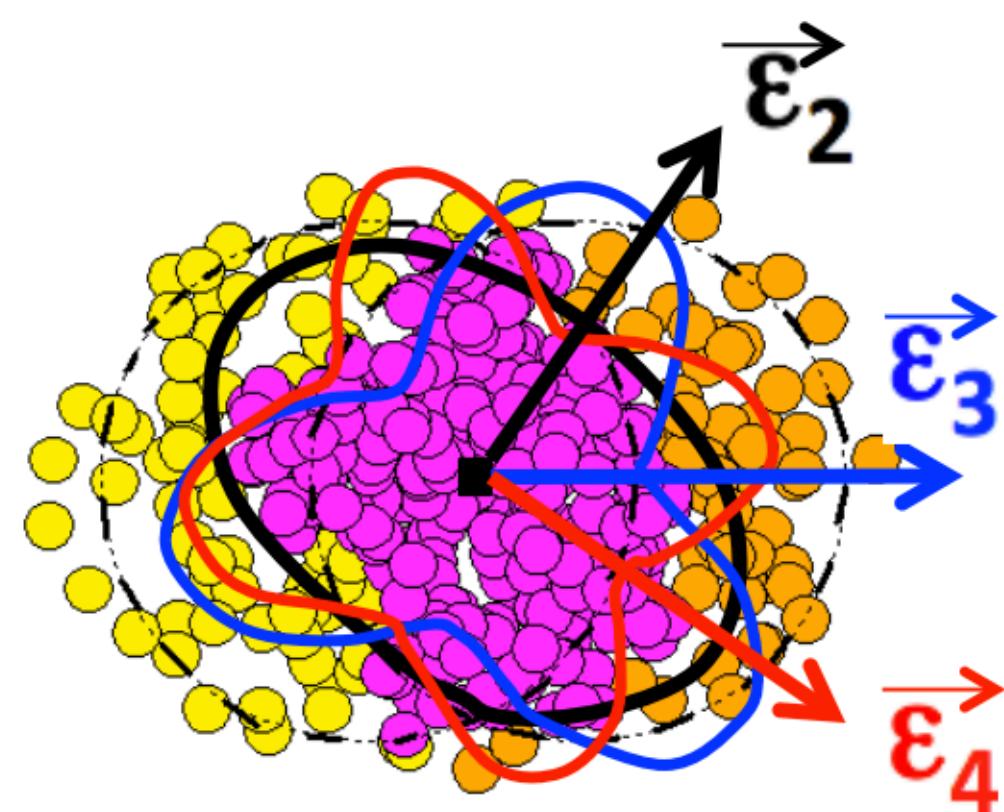


# Evidence of Fluidity

slide adapted from Z. Chen

$$\varepsilon_2 + \varepsilon_3 + \varepsilon_4 + \dots = \cos 2\Delta\phi + \cos 3\Delta\phi + \cos 4\Delta\phi$$

Initial state

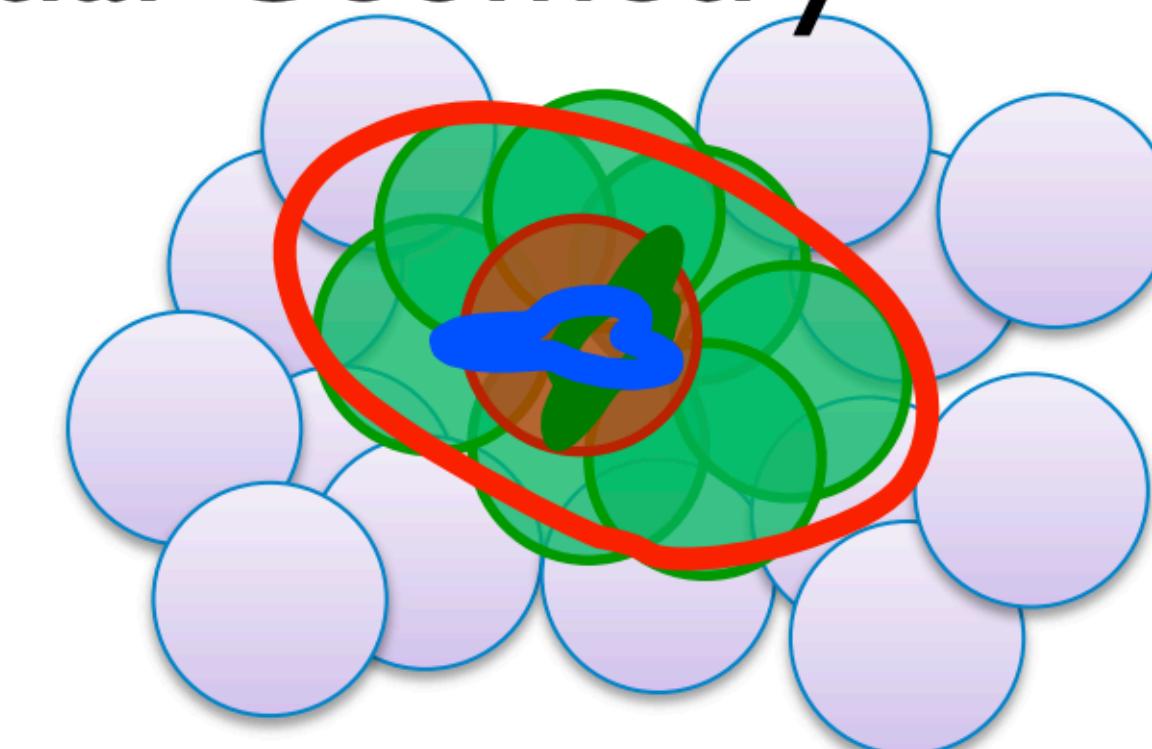


$$\vec{\epsilon}_n \equiv \epsilon_n e^{in\Phi_n^*} \equiv -\frac{\langle r^n e^{in\phi} \rangle}{\langle r^n \rangle}$$

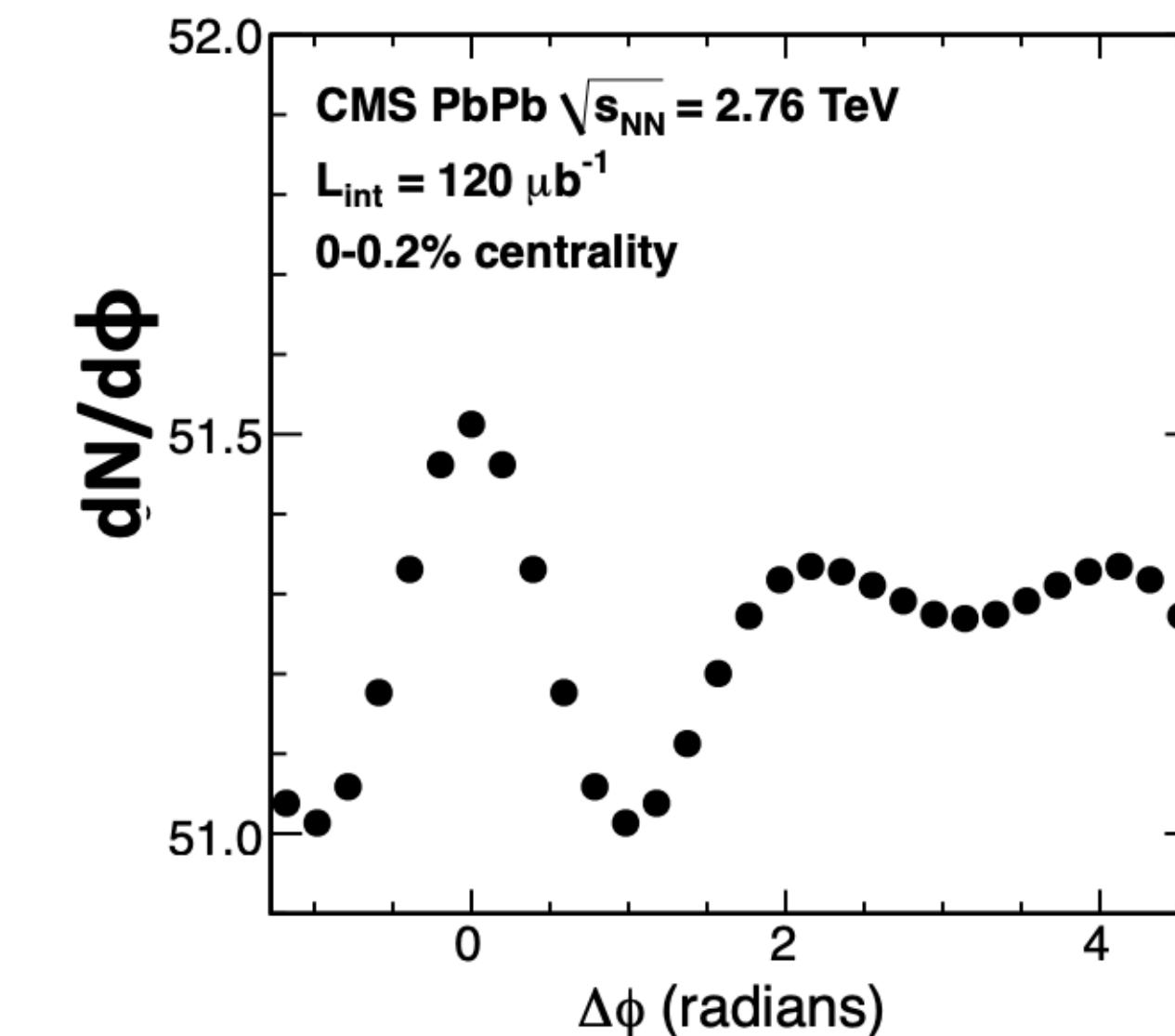
Hydro-response

Space-time dynamics

Initial Geometry



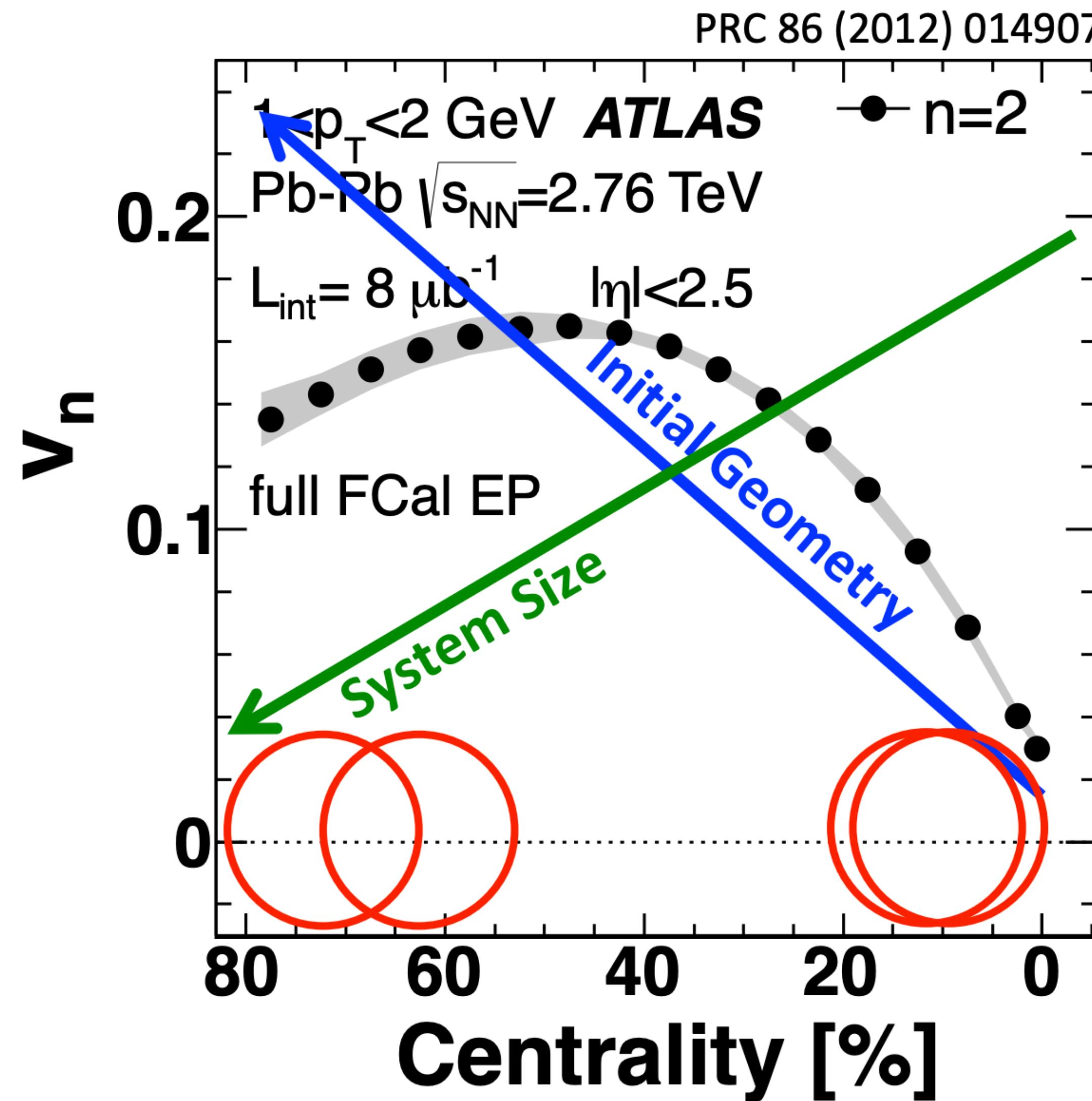
Particle distribution



23

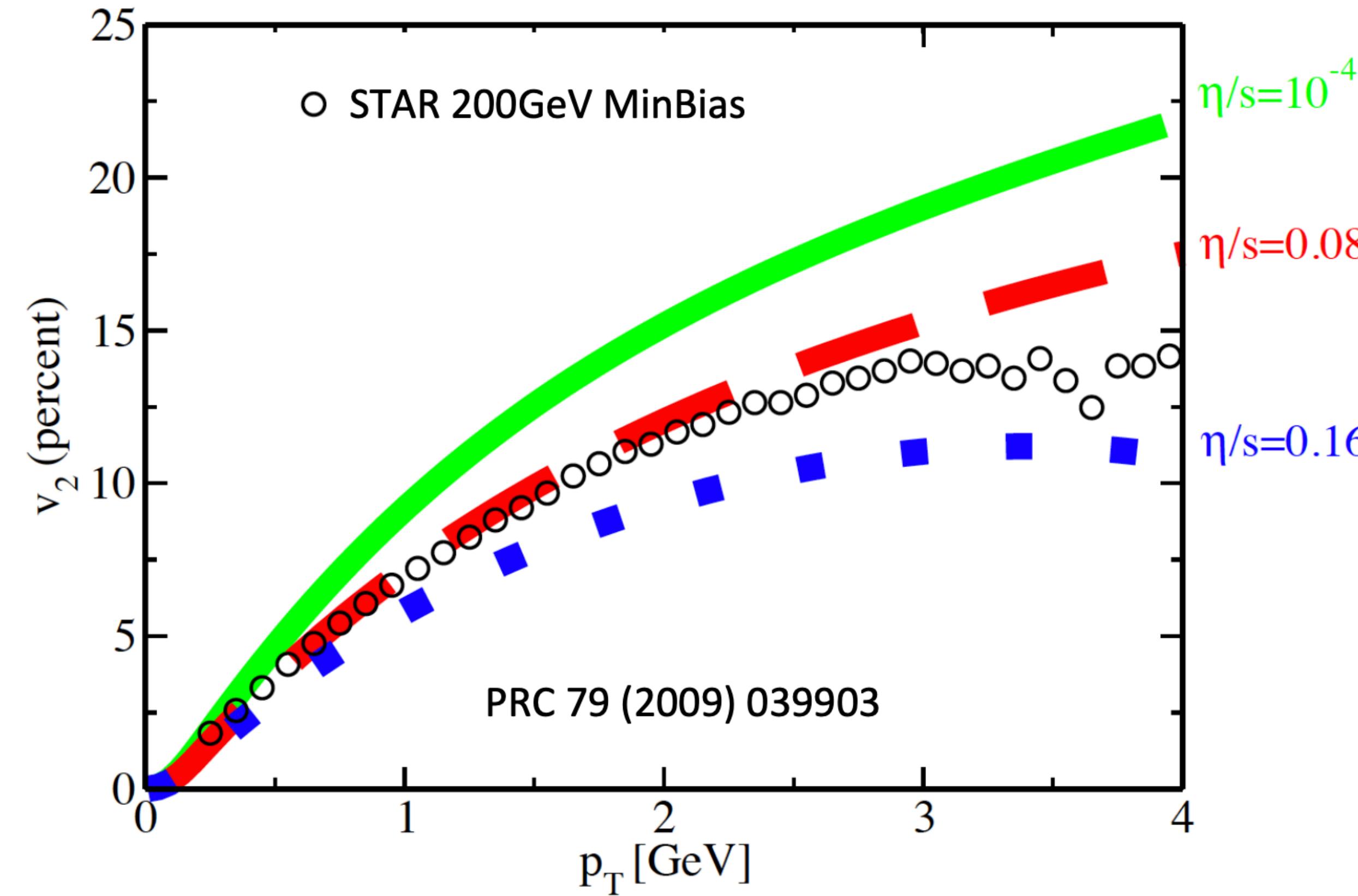
# Elliptic Flow vs Centrality

slide adapted from Z. Chen



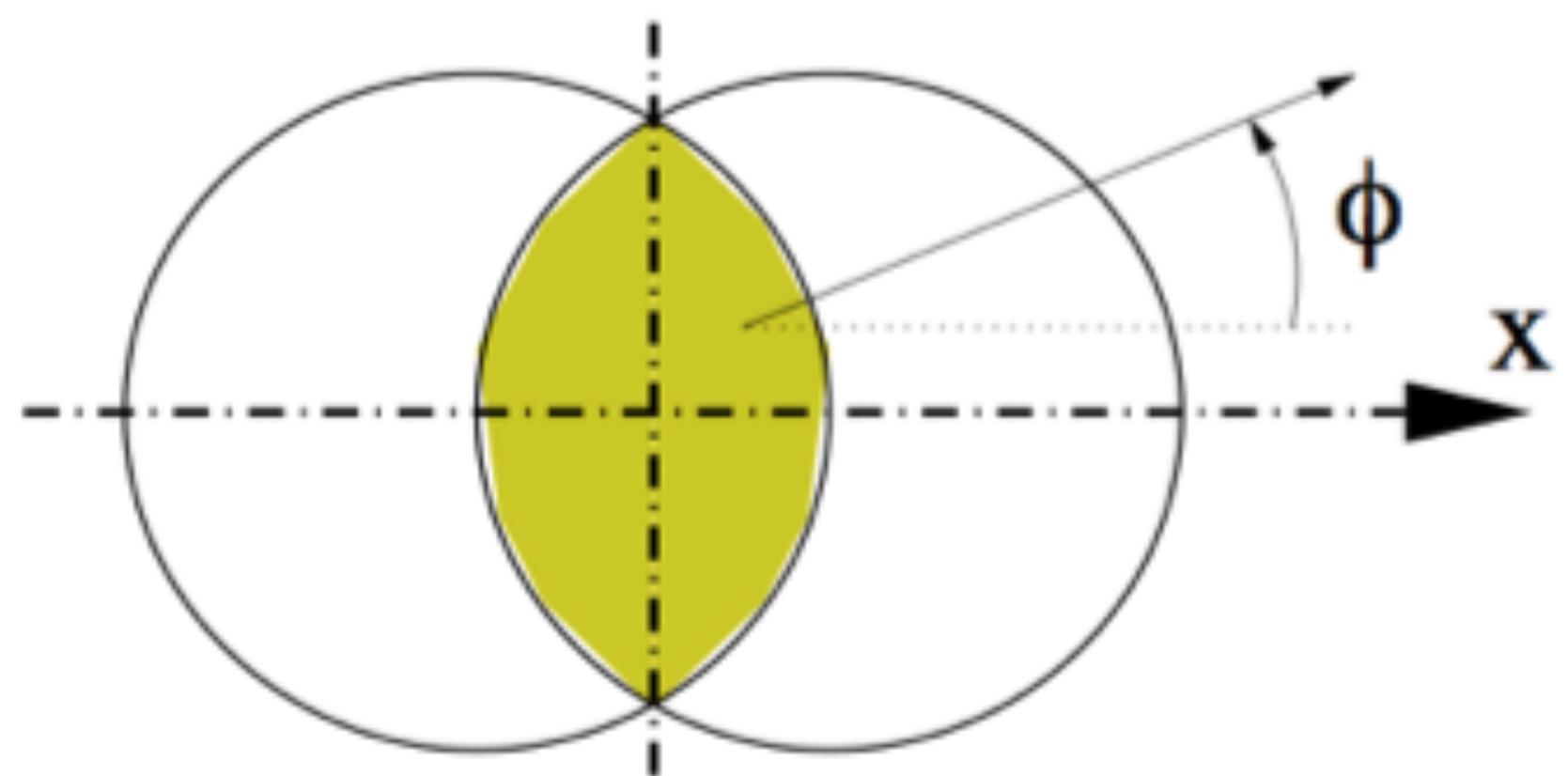
- “Pancake” overlap determines initial eccentricities. Also determines multiplicity.
- To leading order  $v_n \propto A\varepsilon_n$ .
- As system size decreased, less flow.

# Elliptic Flow and Viscosity



- Strong sensitivity of elliptic flow to the value of viscosity (microscopic details).

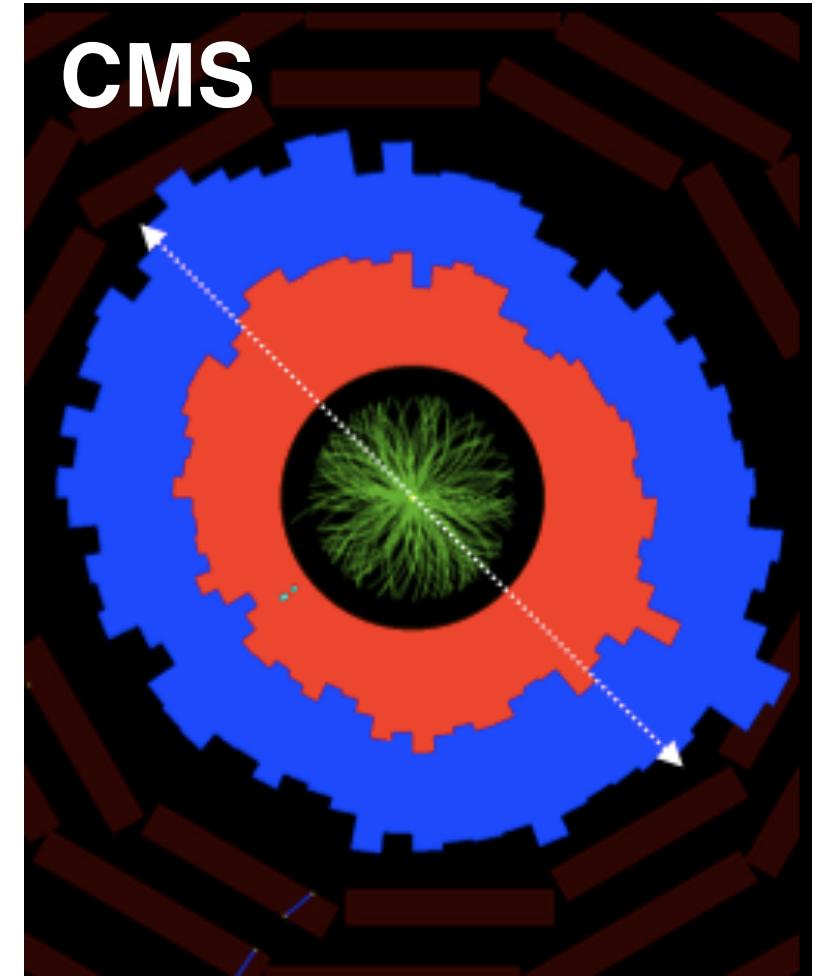
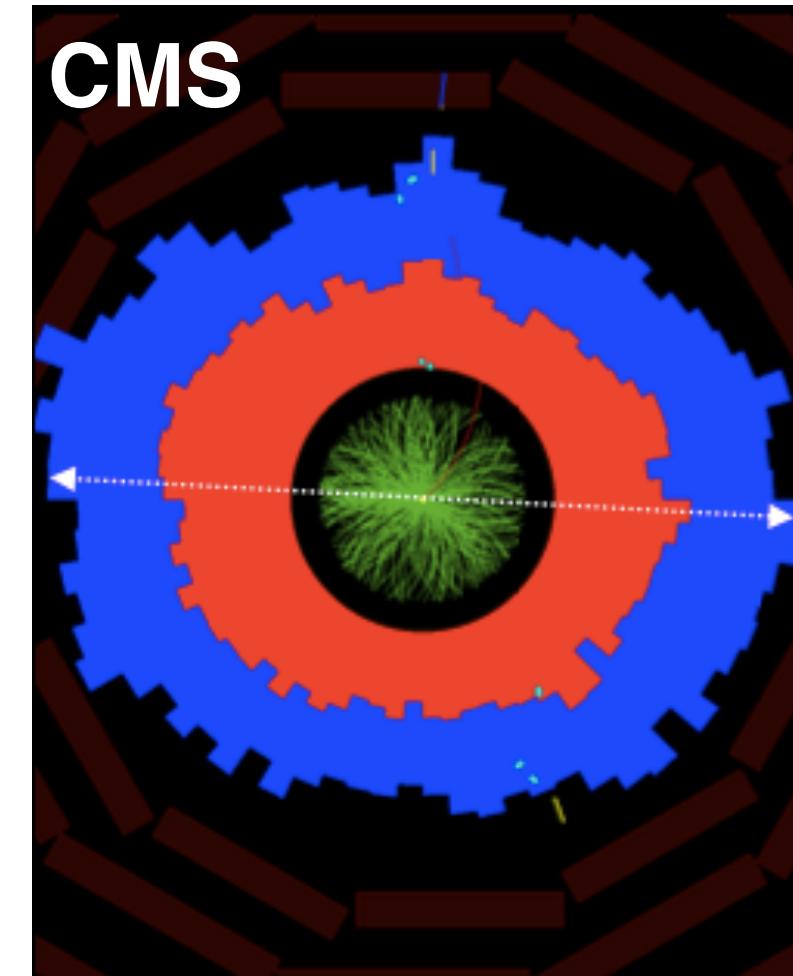
# QGP: Most Perfect Liquid



*Hydrodynamics:*  
Spatial anisotropies.



Pressure gradients.



- Correlations quantified in the experiments through so-called flow coefficients:

$$E \frac{d^3 N}{d^3 p} = \frac{1}{2\pi} \frac{d^2 N}{p_t dp_t dy} \left( 1 + \sum_{n=1}^{\infty} 2v_n \cos[n(\phi - \Psi_R)] \right)$$

$\Psi_R$  is event plane angle.

Preferred  
by data

$v_2$



$v_3$



$v_4$



etc...

- Hydrodynamic simulations point to almost ideal fluid:

$$\left(\frac{\eta}{s}\right)_{T_c} \simeq 0.08$$

Bernhard et al. - PRC '16

$$\frac{\eta_{\lambda \rightarrow 0}}{s_{\lambda \rightarrow 0}} = \frac{A}{\lambda^2 \log(B/\sqrt{\lambda})}$$

N=4 SYM @ weak coupling

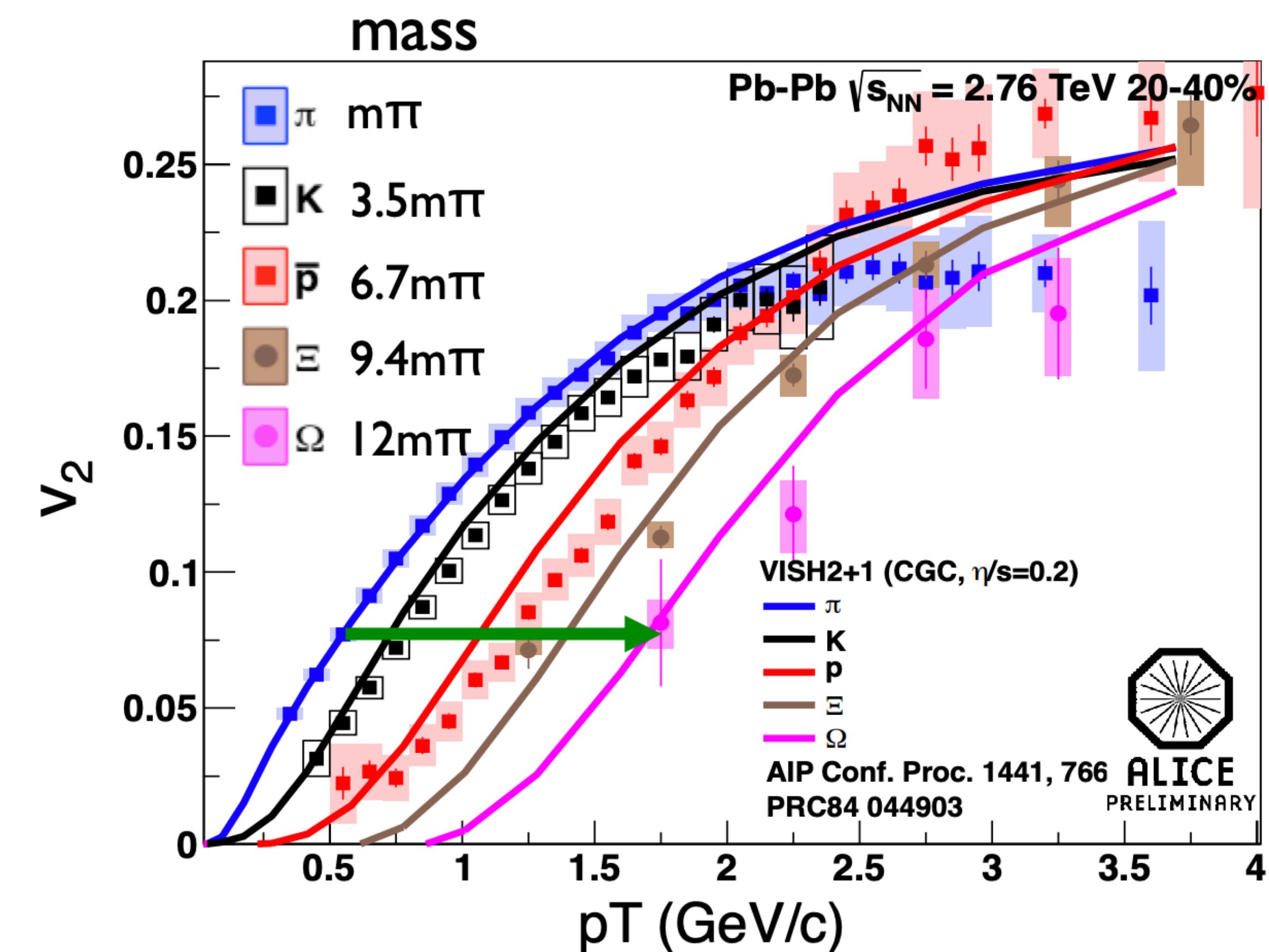
$$\frac{\eta_{\lambda=\infty}}{s_{\lambda=\infty}} = \frac{1}{4\pi}$$

N=4 SYM @ strong coupling

Gauge/String Duality, Hot QCD  
and Heavy Ion Collisions -  
Cambridge University Press '14

# Mass Ordering of Flow

slide adapted from Z. Chen



Boost:  
 $\Delta p_T \sim m \beta_T$

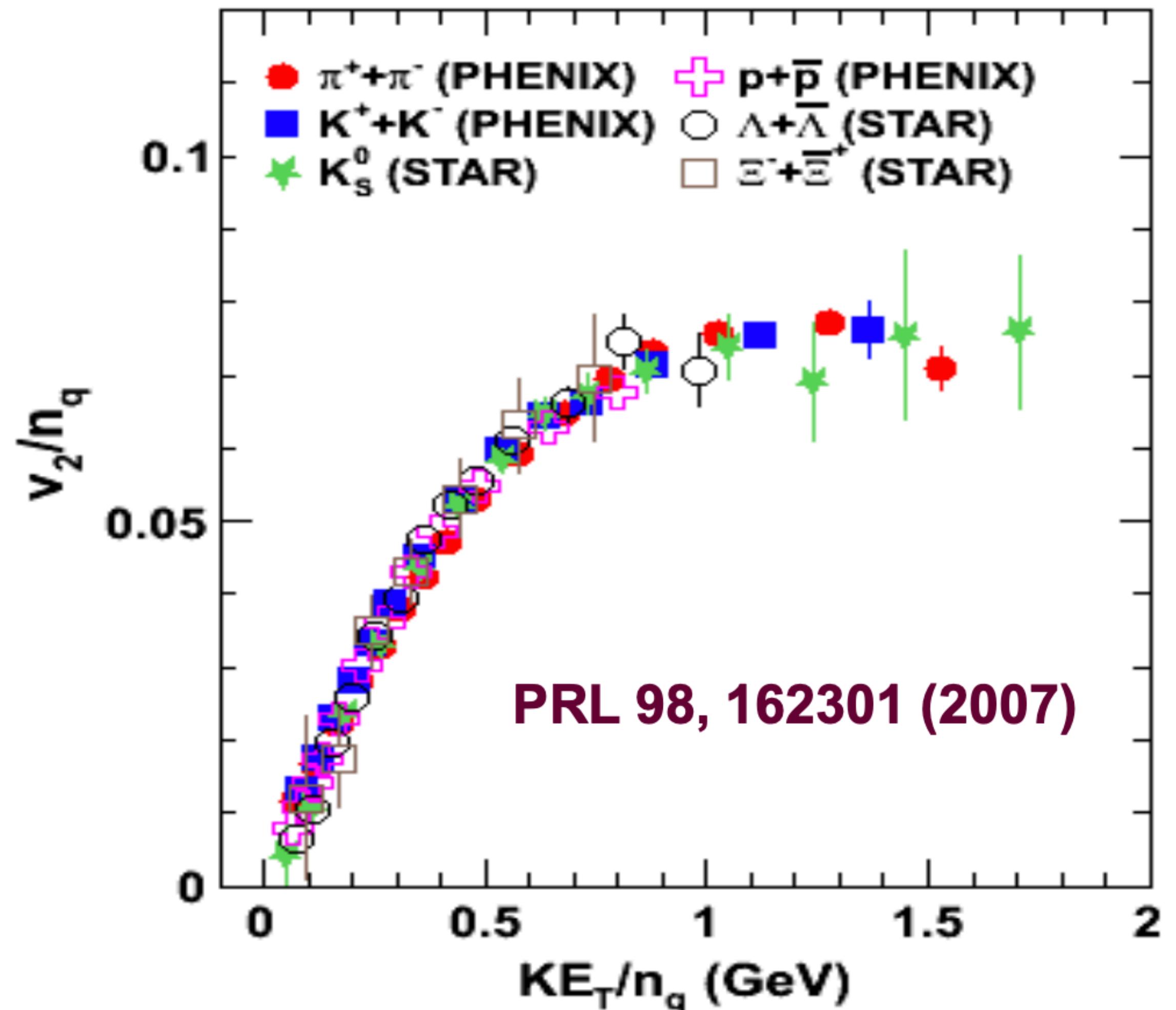
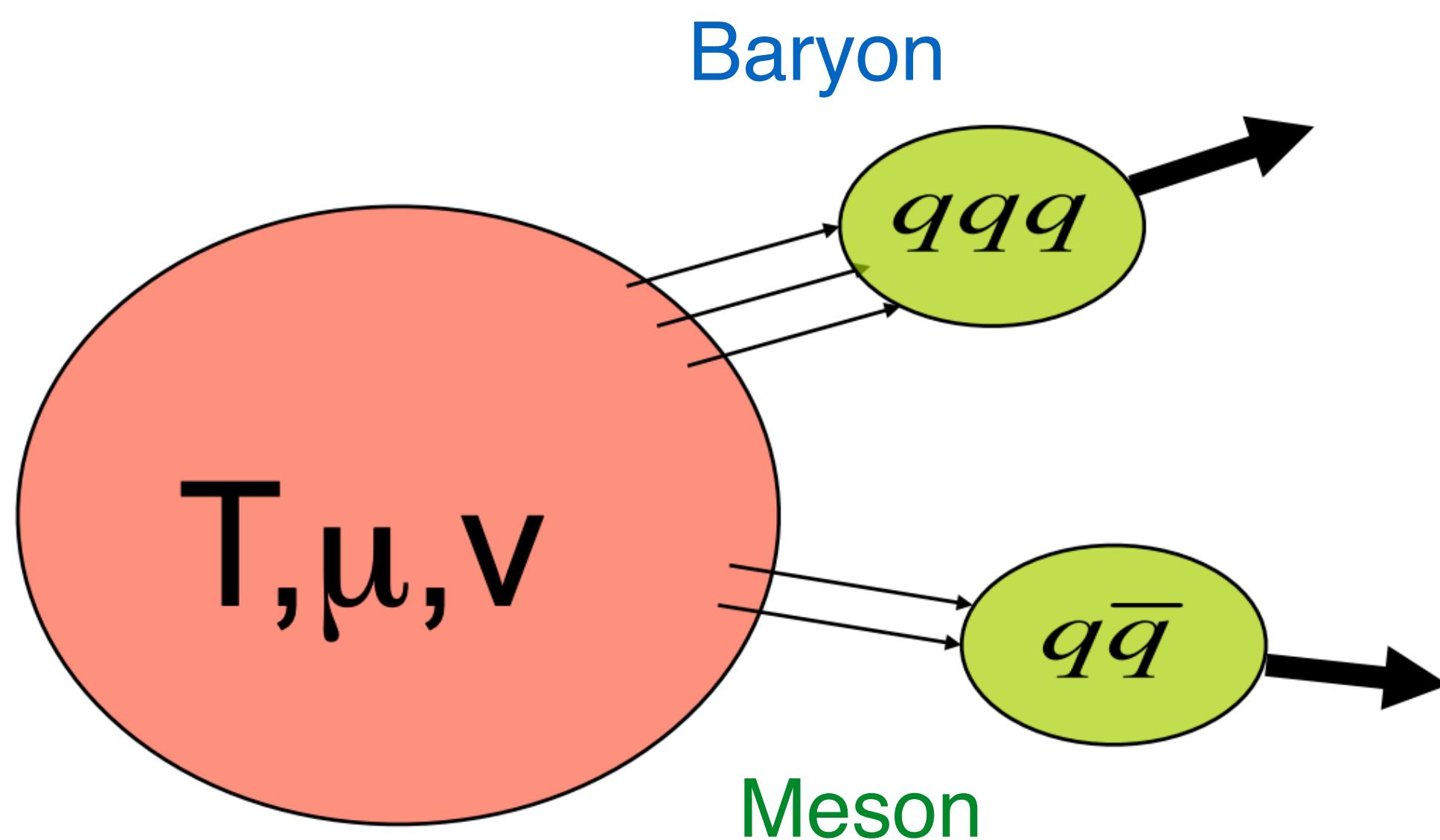
- Heavier particle has smaller  $v_2$  for same  $p_T$ .
  - Predicted by hydro: common boost at partonic level.

# Quark Coalescence

slide adapted from B. Mueller

$$v_2^M(p_T) = 2 v_2^q(p_T/2)$$

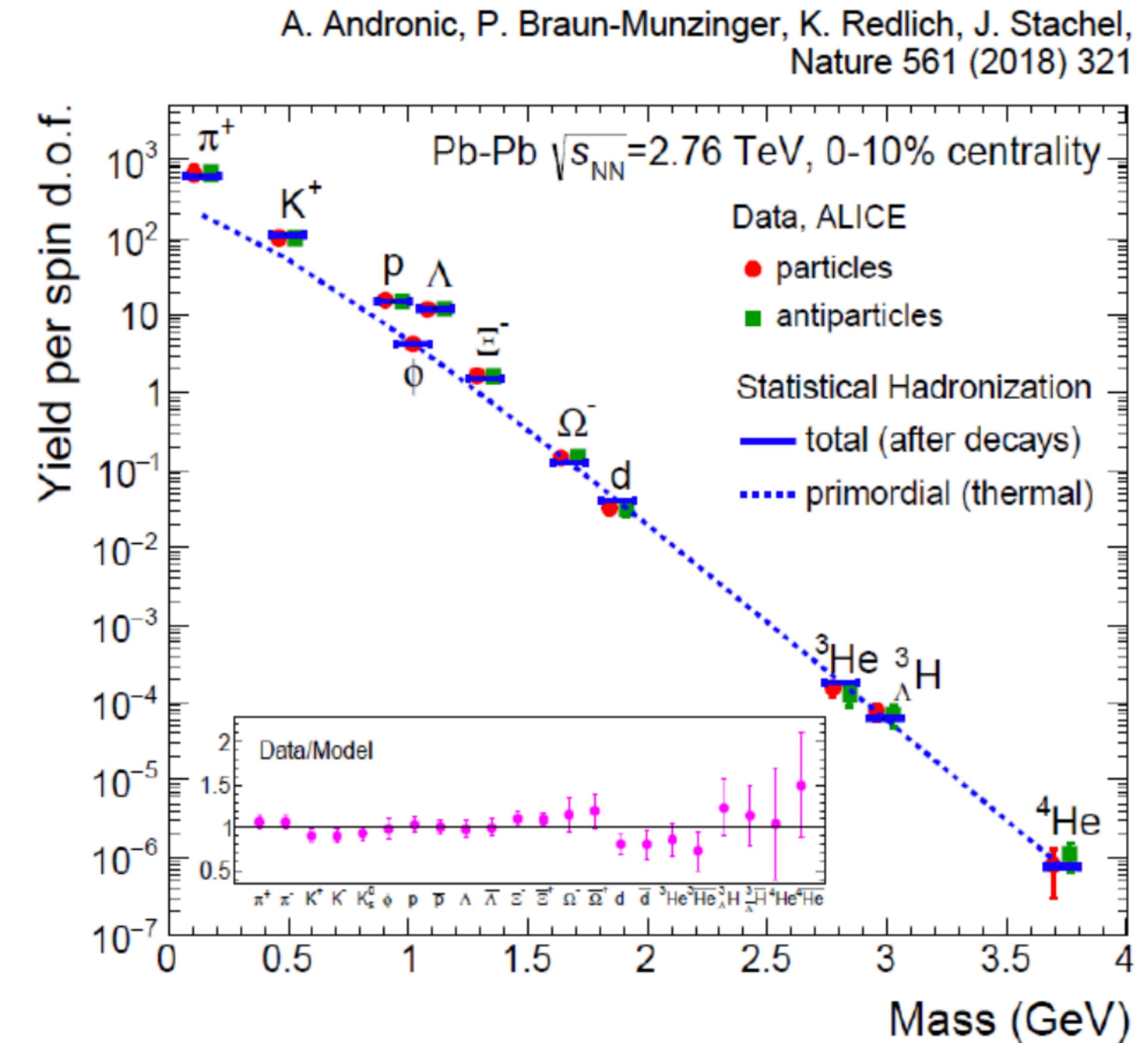
$$v_2^B(p_T) = 3 v_2^q(p_T/3)$$



- Scaling of elliptic flow with number of quarks.
- Driven by flowing partonic d.o.f.

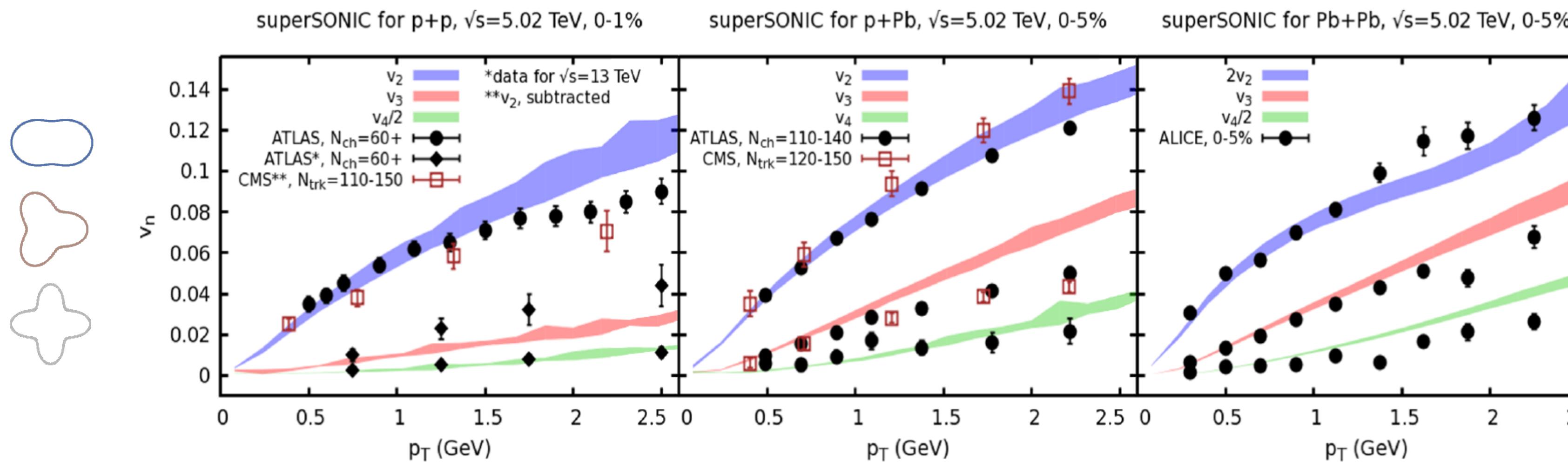
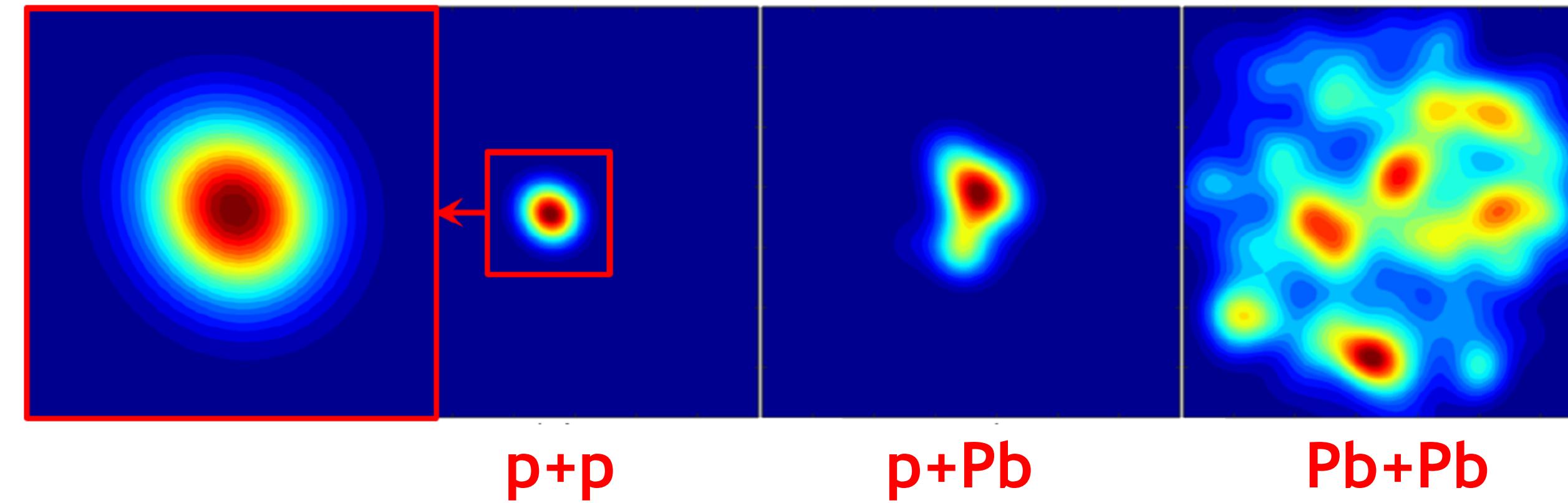
# Statistical Hadronization Model

- Thermal production of hadrons using canonical or grand-canonical ensembles.
  - 1 free parameter:  $T \sim 156.5(1.5)$  MeV
- Describes yields accurately in *all collision systems*.
  - How is thermalization achieved!?
- Some ideas: analogy between confinement and black hole physics.
  - Event horizon for colored signals, causally disconnected region. (Hawking-Unruh hadronization).



# Flow in Small Systems

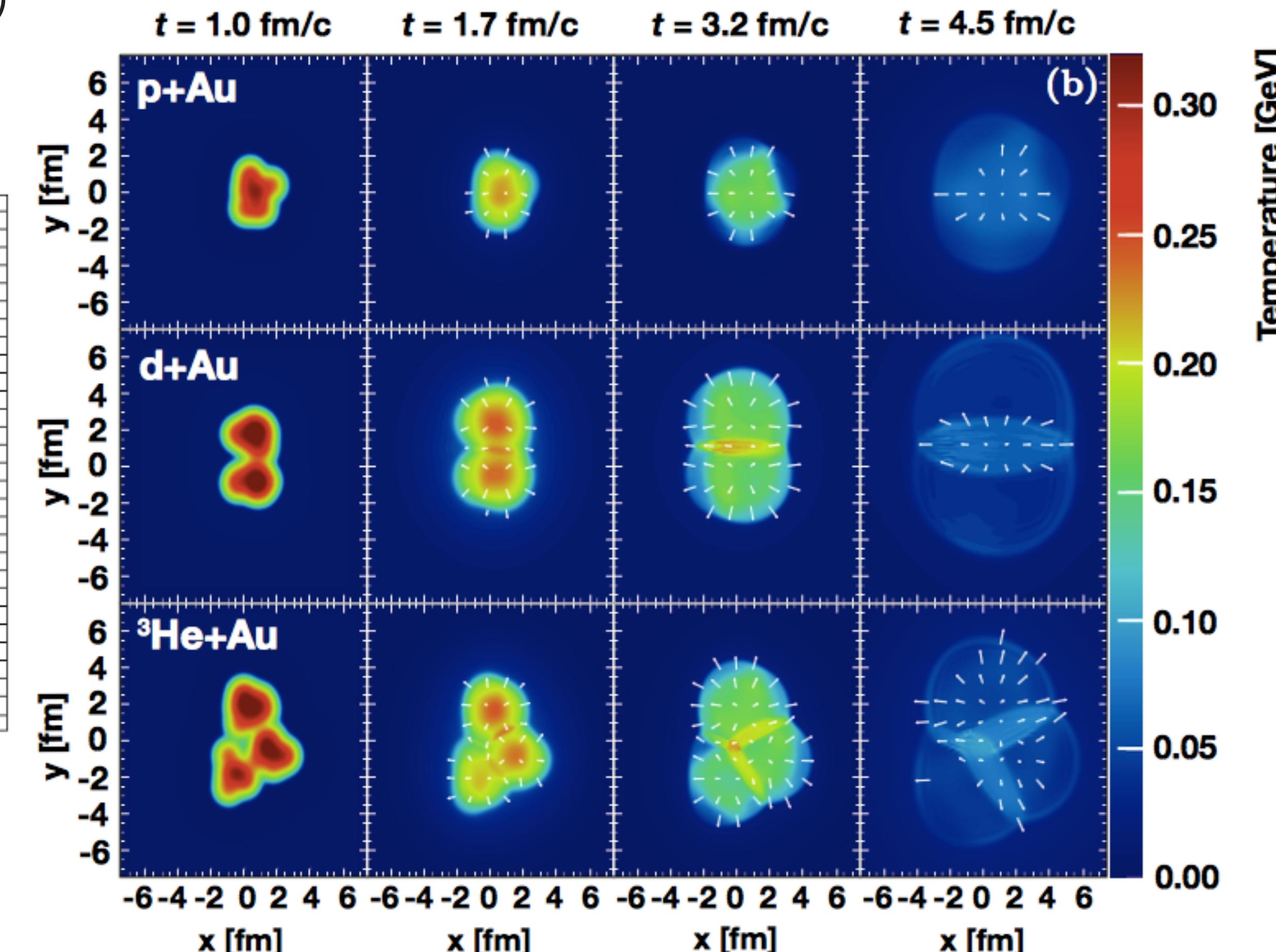
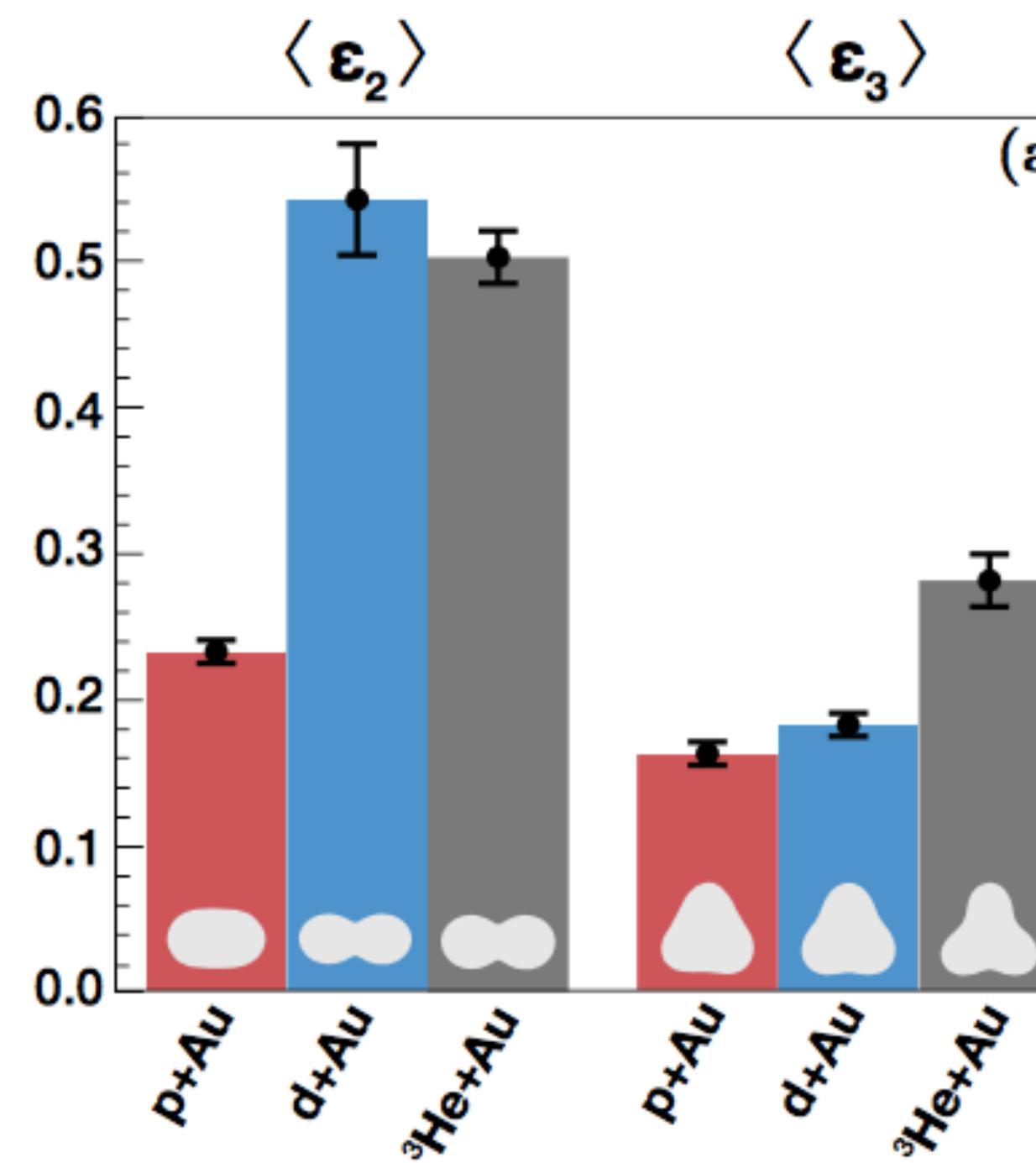
“One fluid to rule them all”



Weller and Romatschke, 1701.07145

# Tuning Eccentricities in Small Systems

*Nature Physics* **15**, 214–220 (2019)  
PHENIX collaboration

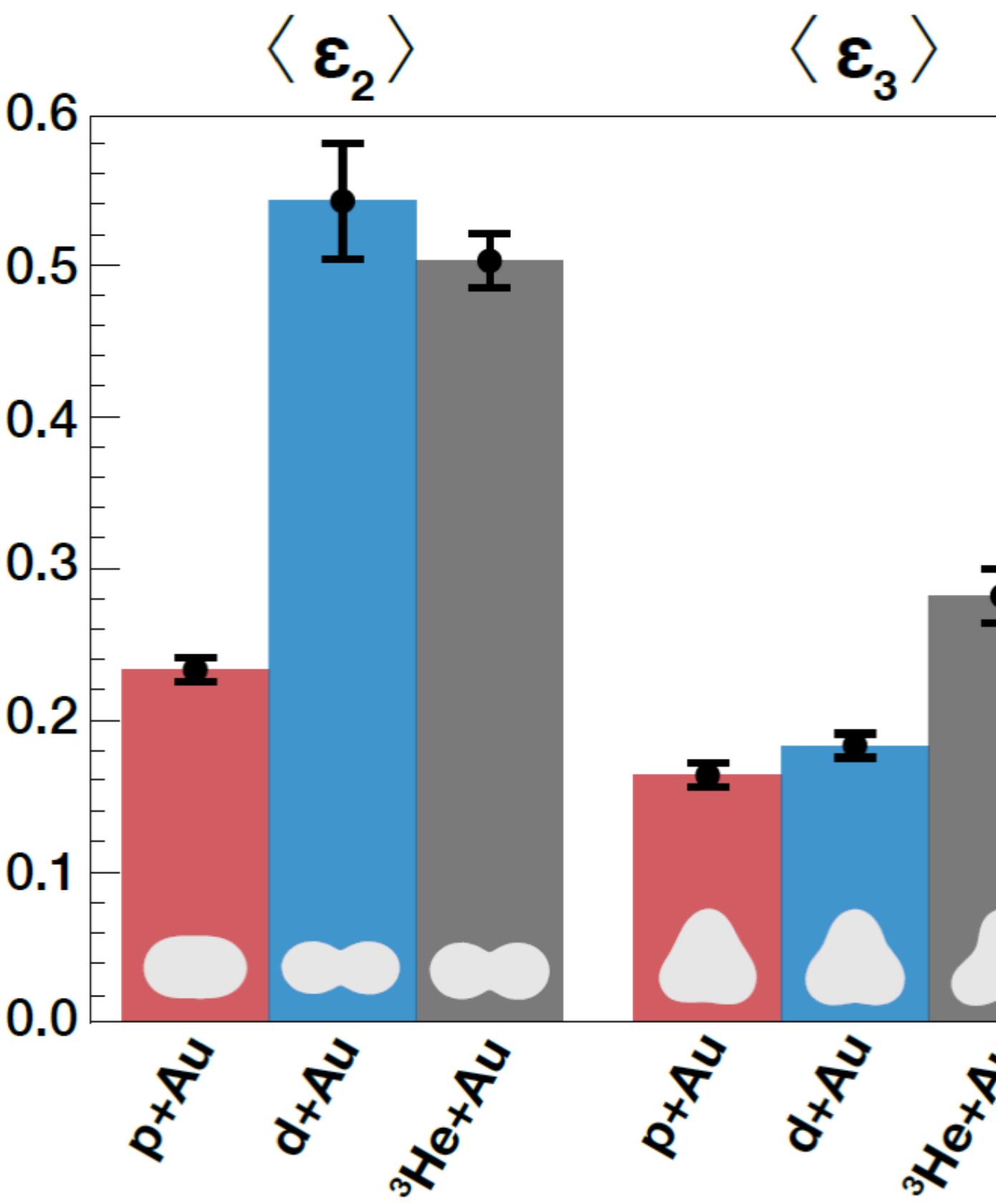
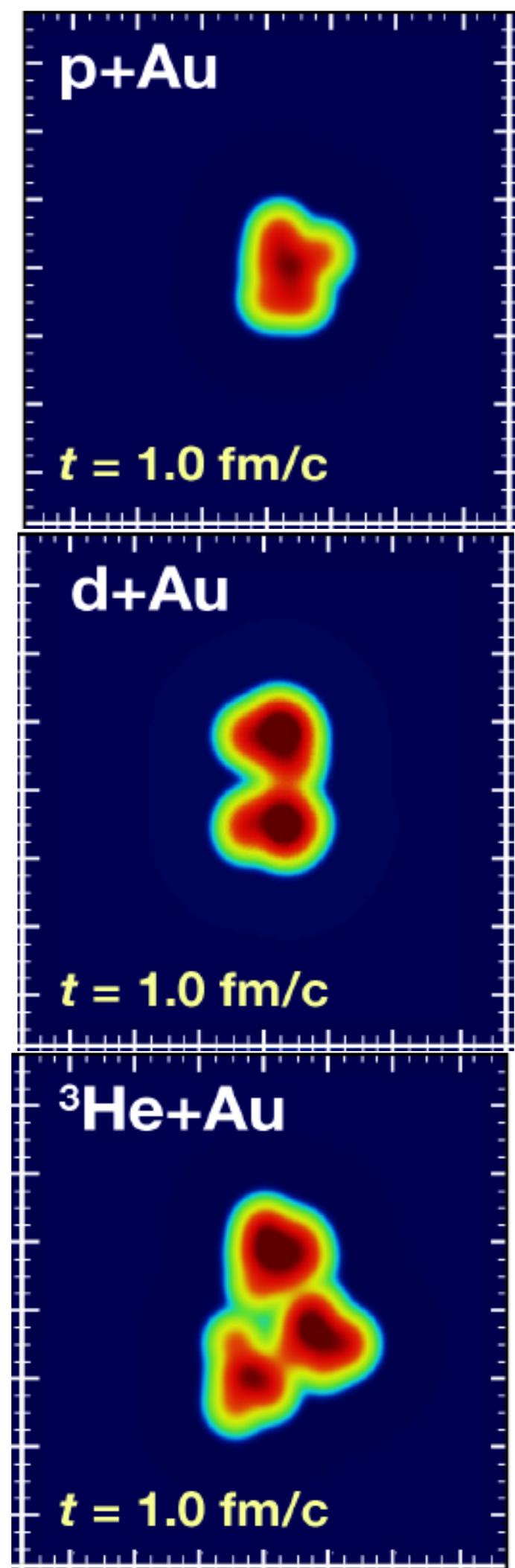


→ Expectation from hydro arguments:

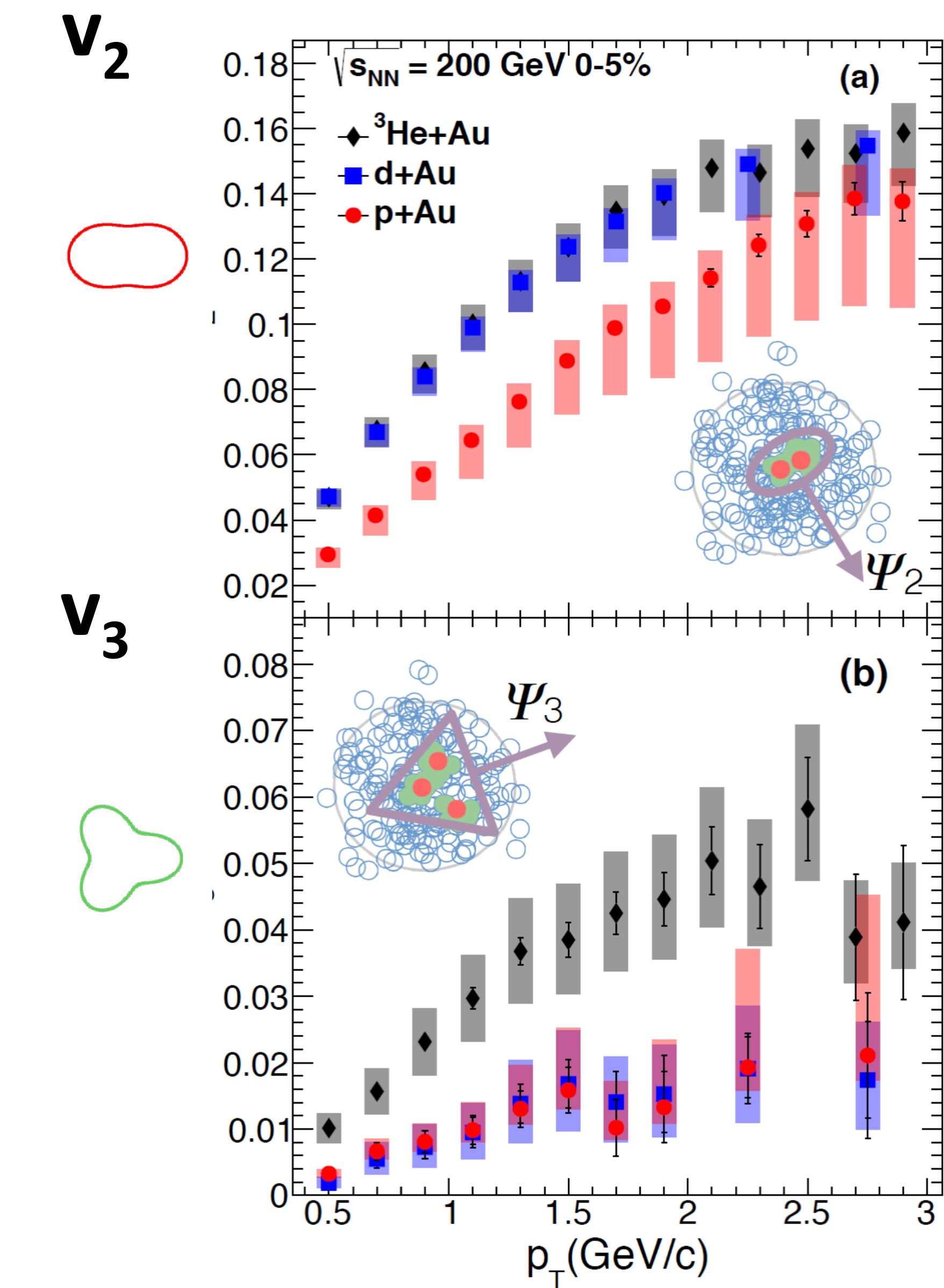
$$v_2^{p+\text{Au}} < v_2^{d+\text{Au}} \approx v_2^{^3\text{He}+\text{Au}},$$

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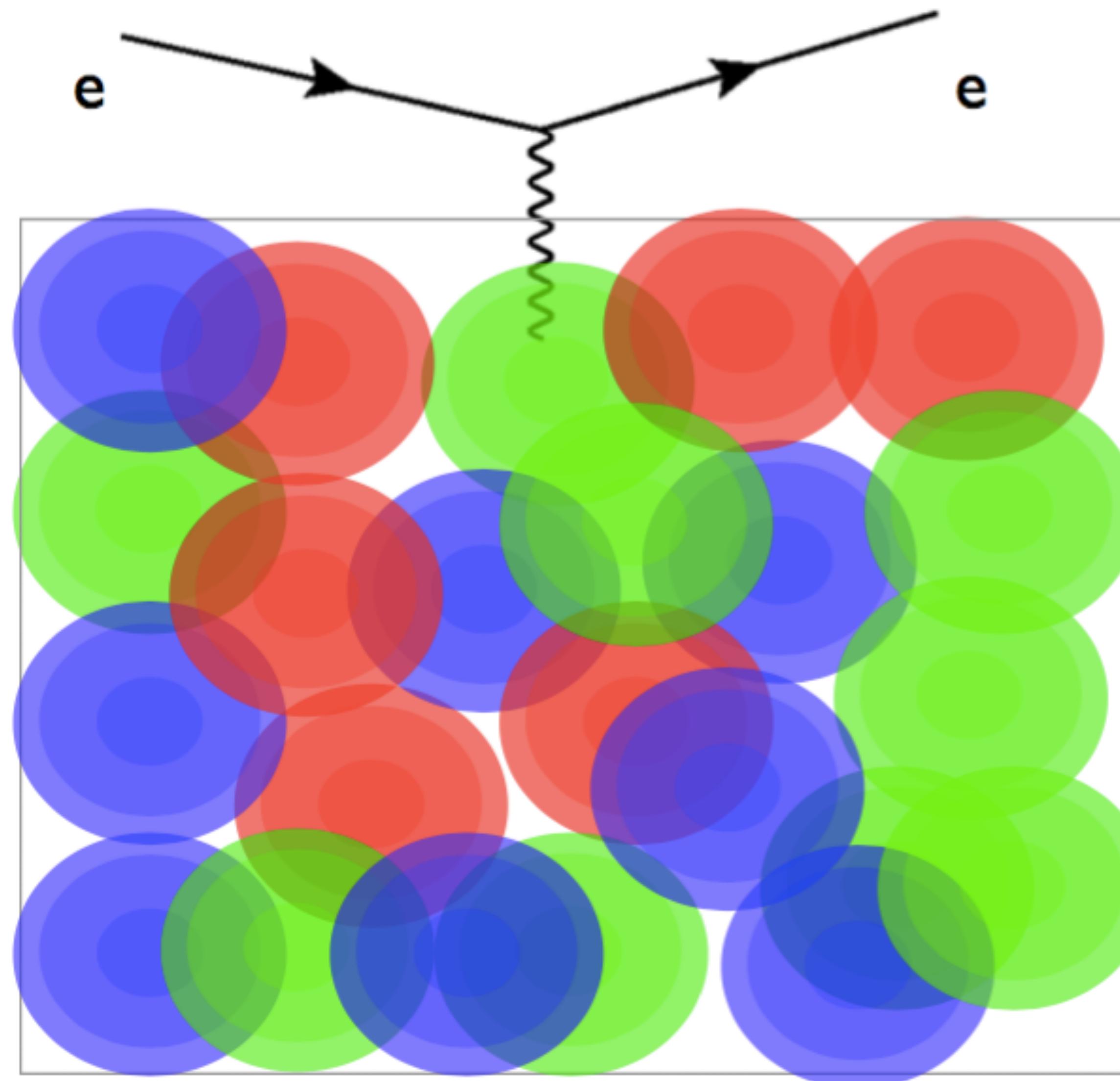
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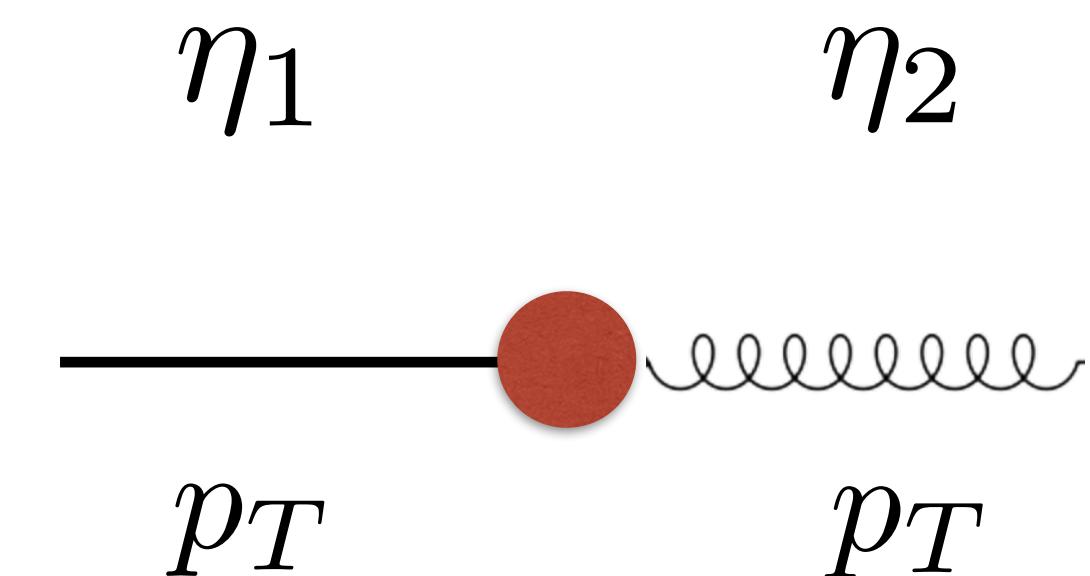


# How Can We Probe the QGP?



# Jets in pp

- Hard parton pairs produced back-to-back in transverse plane, misaligned in rapidity.

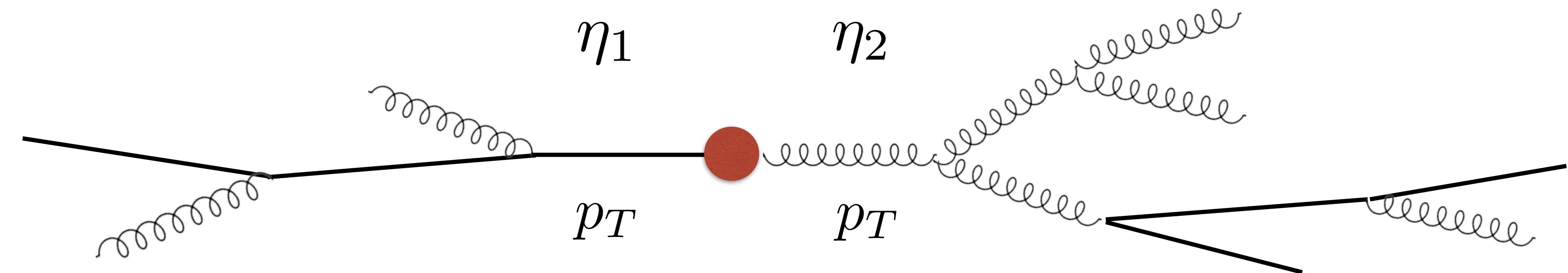


# Jets in pp

- Hard parton pairs produced back-to-back in transverse plane, misaligned in rapidity.

- Parton density evolution described via DGLAP:

$$t \frac{\partial}{\partial t} f(x, t) = \int \frac{dz}{z} \frac{\alpha_s}{2\pi} P_+(z) f\left(\frac{x}{z}, t\right)$$



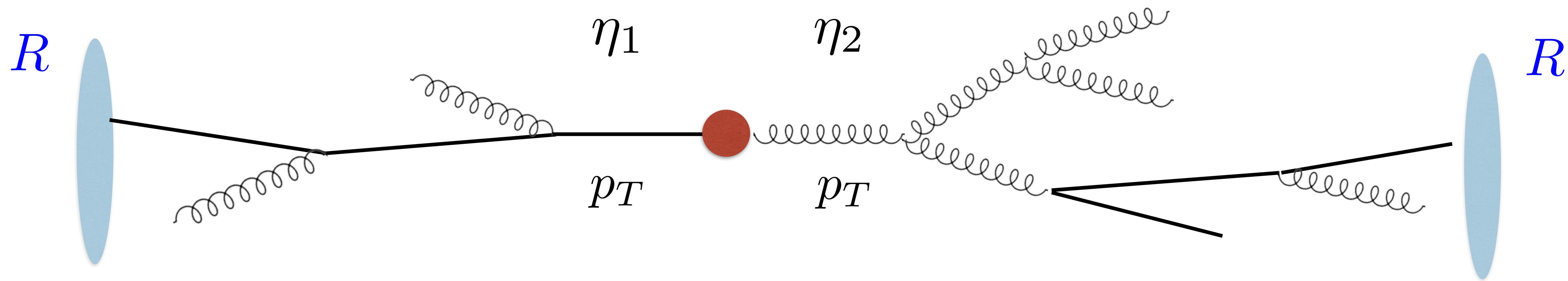
- Collimated structure enforced through collinear divergences & color coherence.

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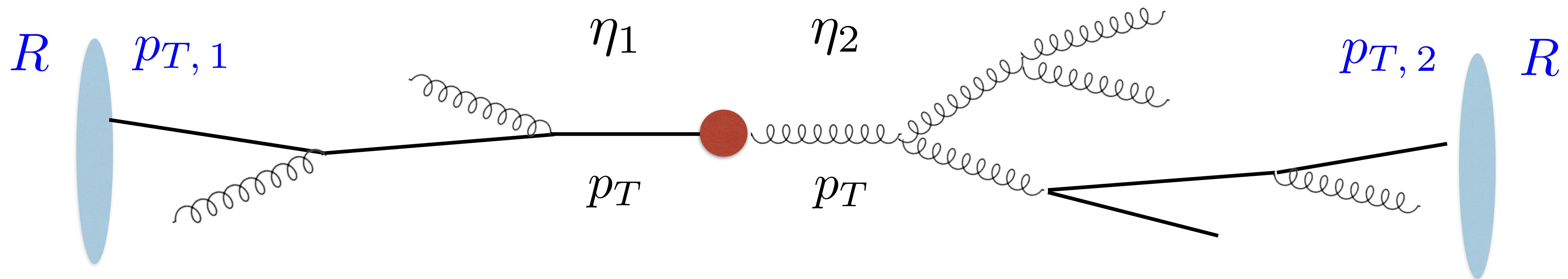
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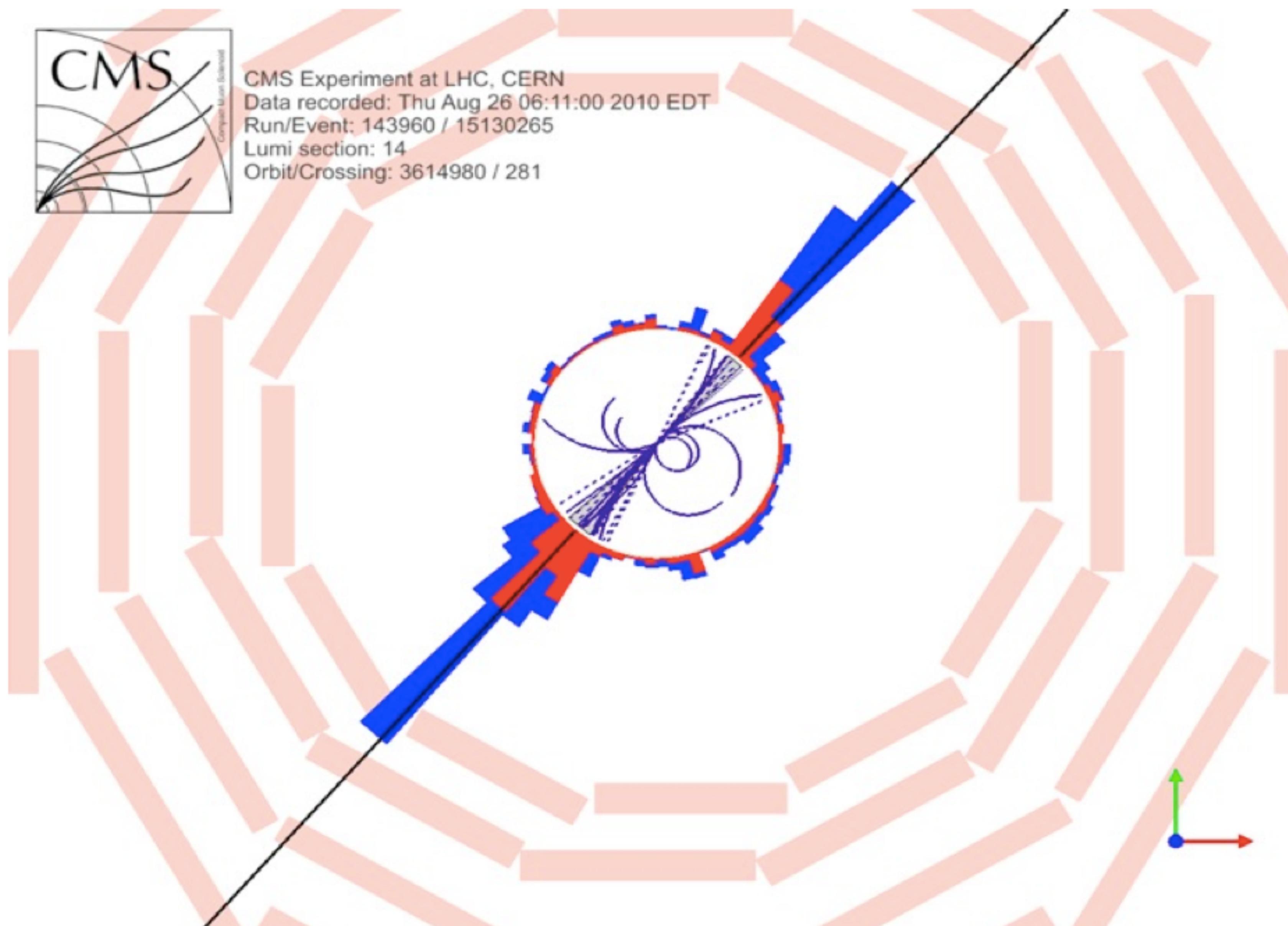
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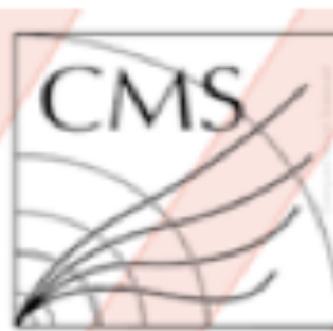
→ Degree of jet activity determines, e.g., out-of-cone radiation (causes dijet asymmetry in pp).

$$p_{T,1} > p_{T,2}$$

# Jets in Proton-Proton Collisions

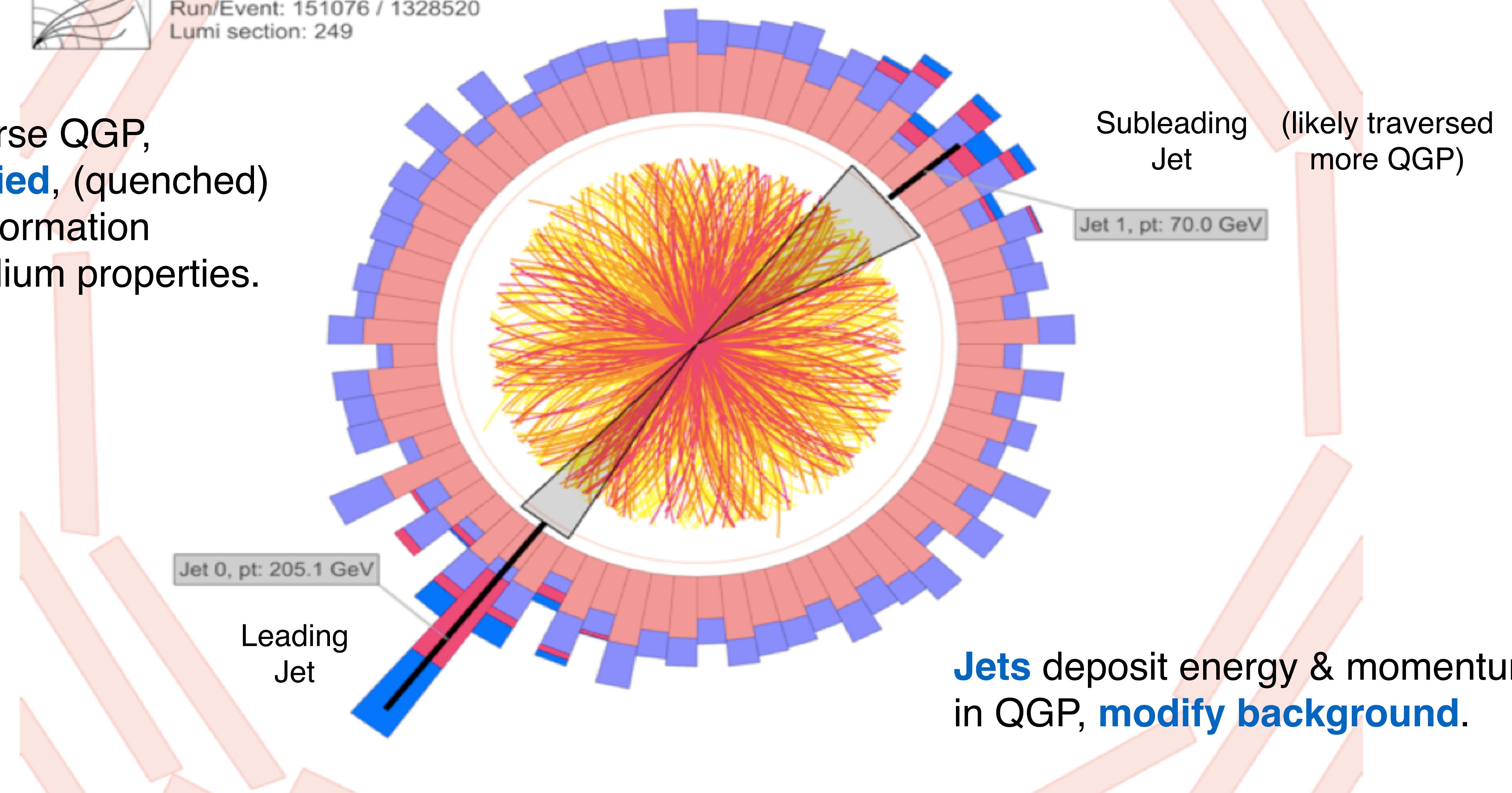


# Jets in HIC



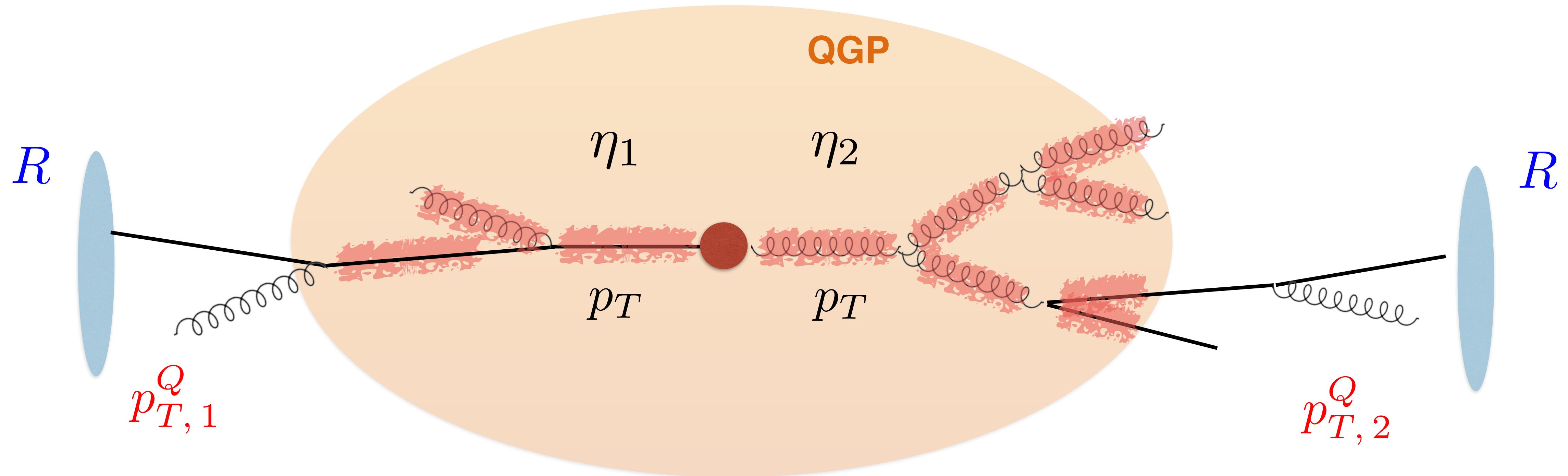
CMS Experiment at LHC, CERN  
Data recorded: Sun Nov 14 19:31:39 2010 CEST  
Run/Event: 151076 / 1328520  
Lumi section: 249

**Jets** traverse QGP,  
**get modified**, (quenched)  
provide information  
about medium properties.



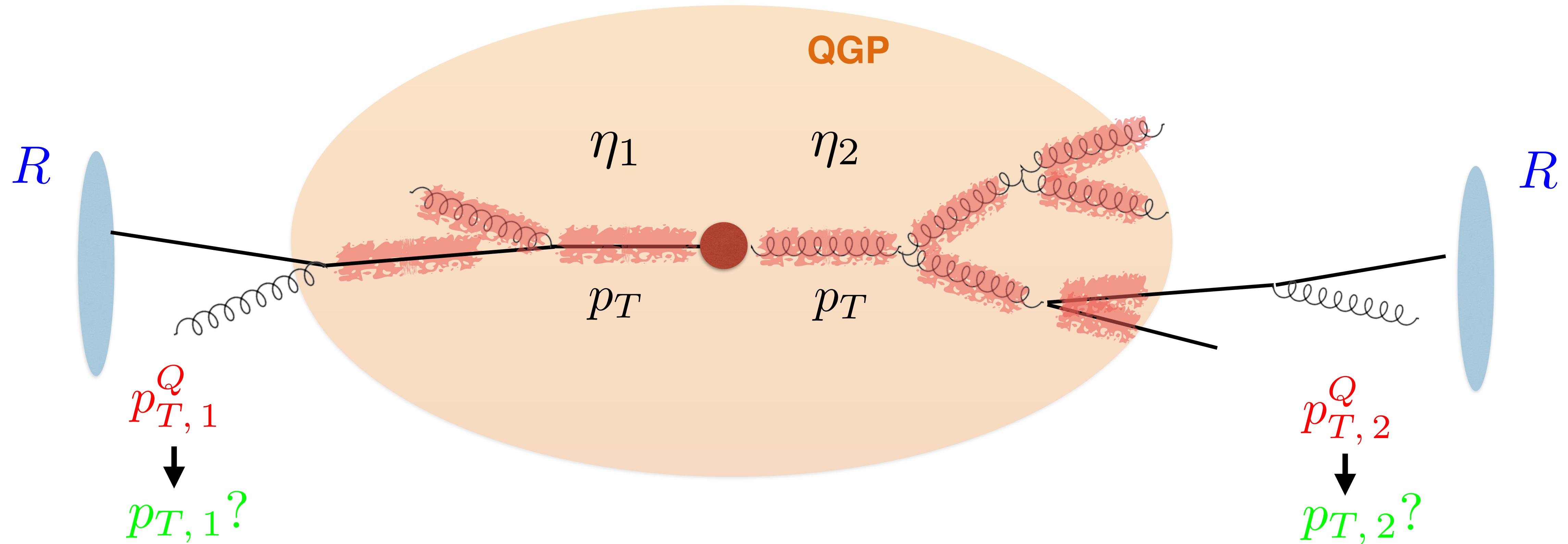
# Outline

- Jet partons interact with QGP and experience energy loss.



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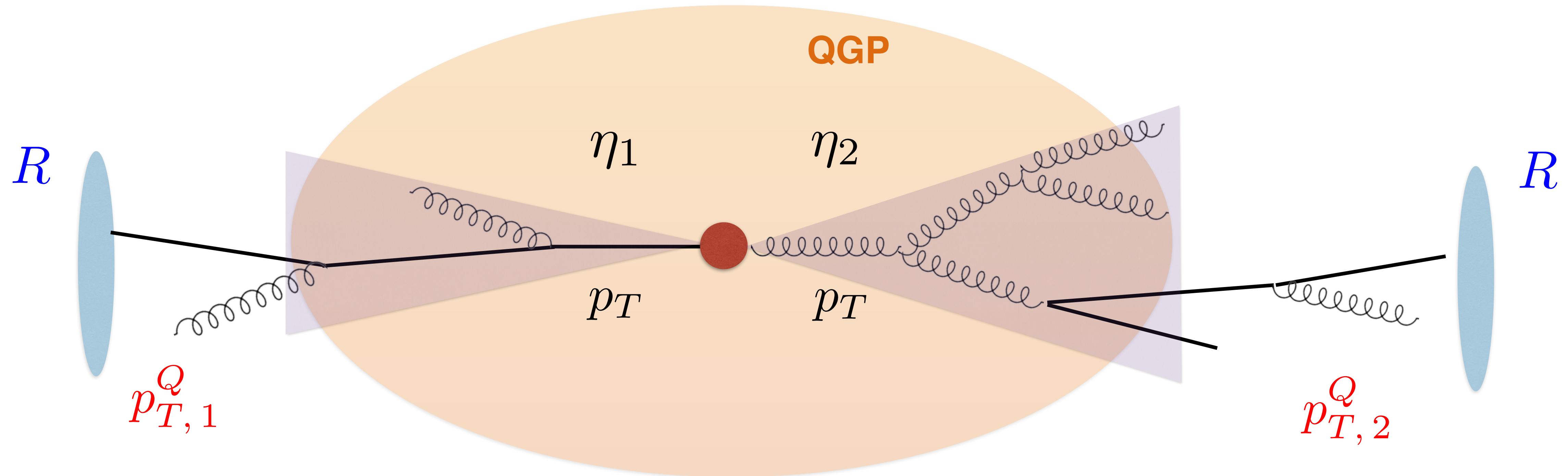
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- What can we learn by knowing how much energy a given jet has lost?

# Outline

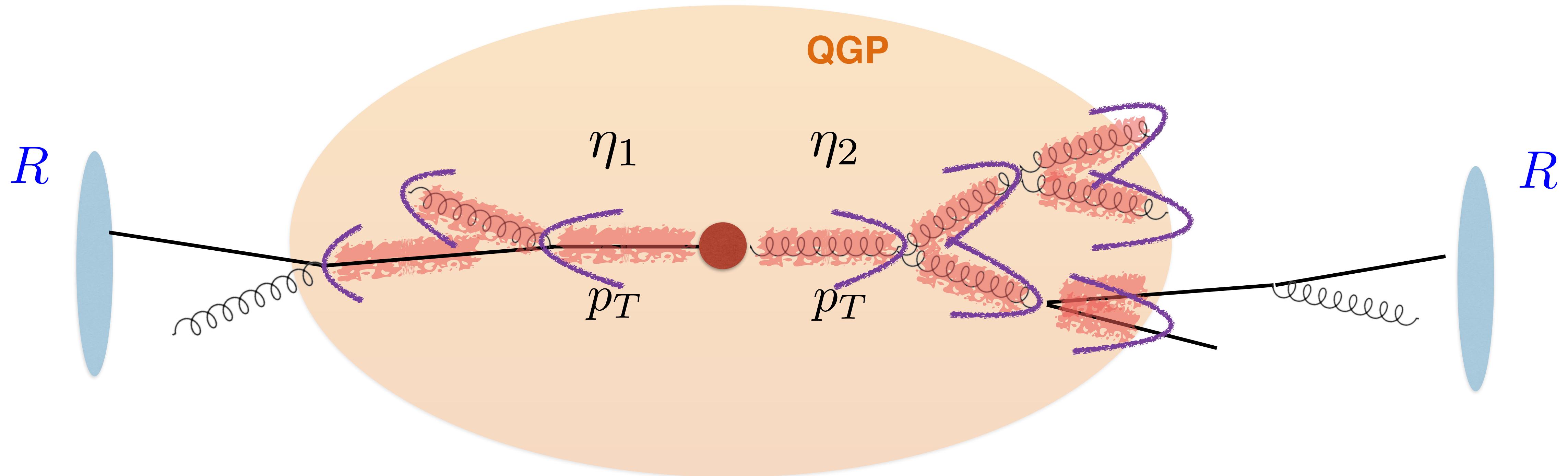
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- How sensitive is the medium to jet substructure fluctuations?  
Does it resolve anything beyond total charge?

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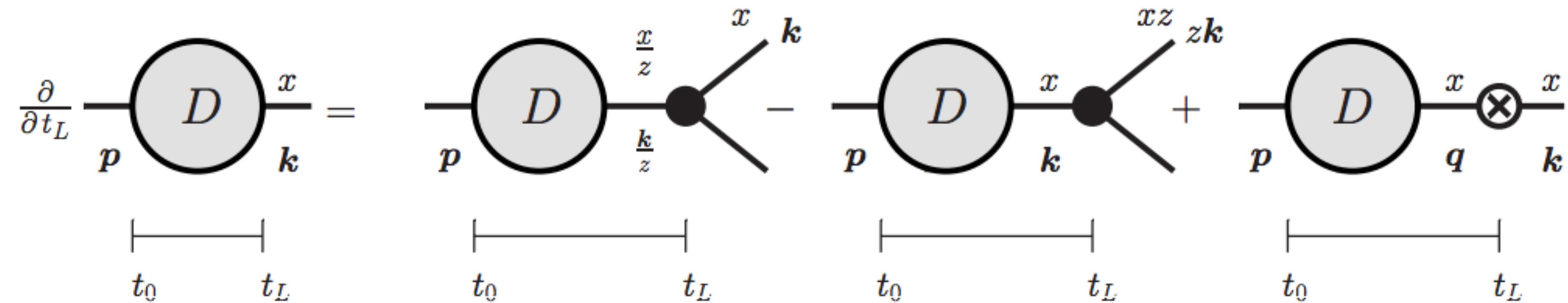
- Non-perturbative modelling of long wavelength jet modes:  
Where does “lost” energy go to?

# Parton Energy Loss

pQCD

High energy partons in the QGP:

→ emit quanta, which in turn emit more quanta, and should (eventually) hydrodynamize.



$D(x, \mathbf{k}, t)$  is one-gluon distribution.

Blaizot et al. - JHEP '13 & '14, PRL '13

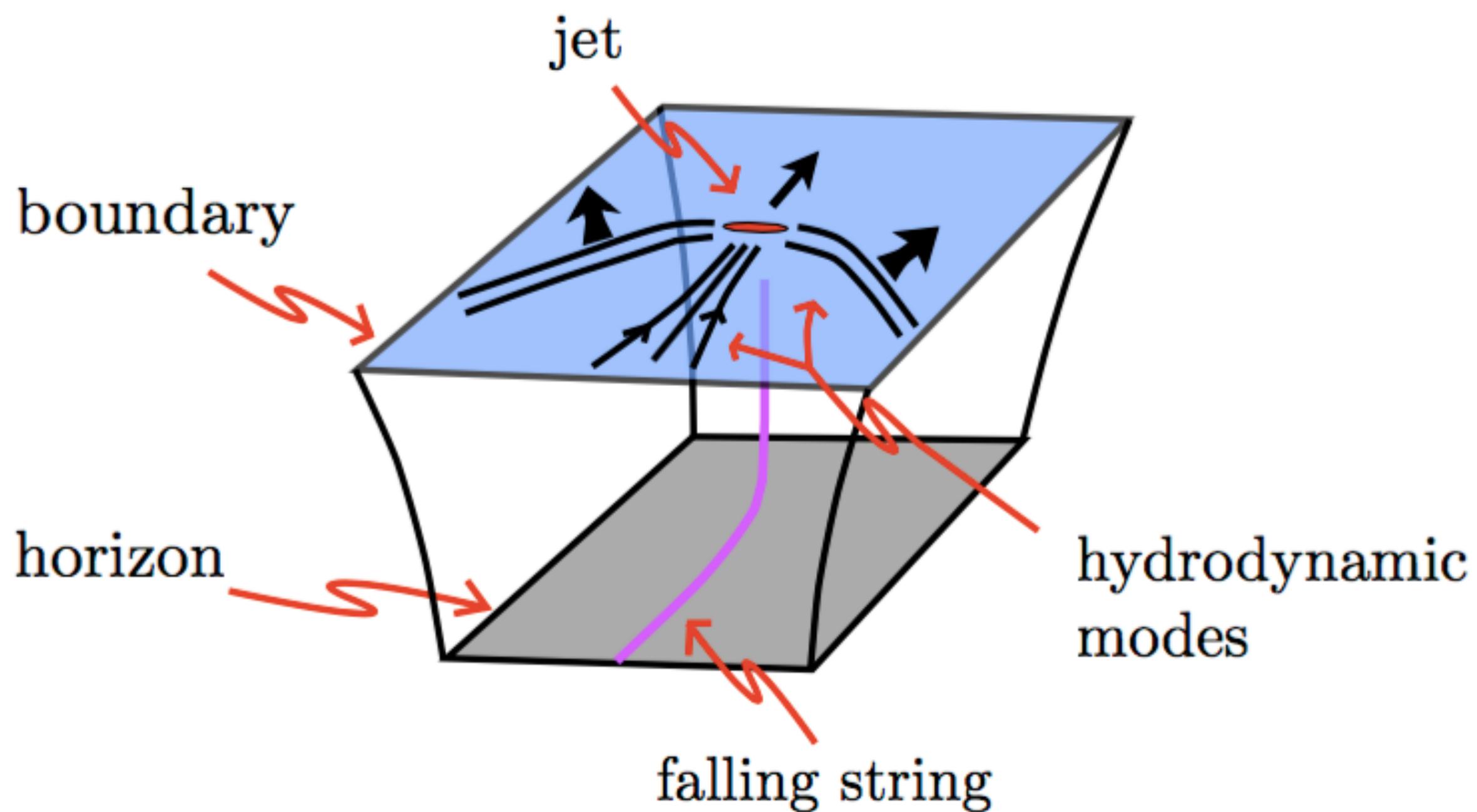
- Turbulent cascade develops, with a sink at  $E \sim T$ .
- Necessary length to reach the turbulent regime?

# Parton Energy Loss

npSYM

High energy partons in the QGP:

- are dual to strings falling into a black hole, hydrodynamizing.



Chesler & Rajagopal - PRD '14, JHEP '16

$$\langle \Delta T^{\mu\nu}(t, \mathbf{x}) \rangle = \frac{L^3}{4\pi G_{\text{Newton}}} H_{\mu\nu}^{(4)}(t, \mathbf{x})$$

“Jet” induced EM tensor:  
hard + soft modes.

Perturbed metric  
@ boundary.

↓  
Long wavelength limit  
(hydrodynamization rate):

$$\frac{1}{E_{\text{init}}} \frac{dE_{\text{jet}}}{dx} = - \frac{4x^2}{\pi x_{\text{therm}}^2 \sqrt{x_{\text{therm}}^2 - x^2}}$$

# Interpretation of Observables

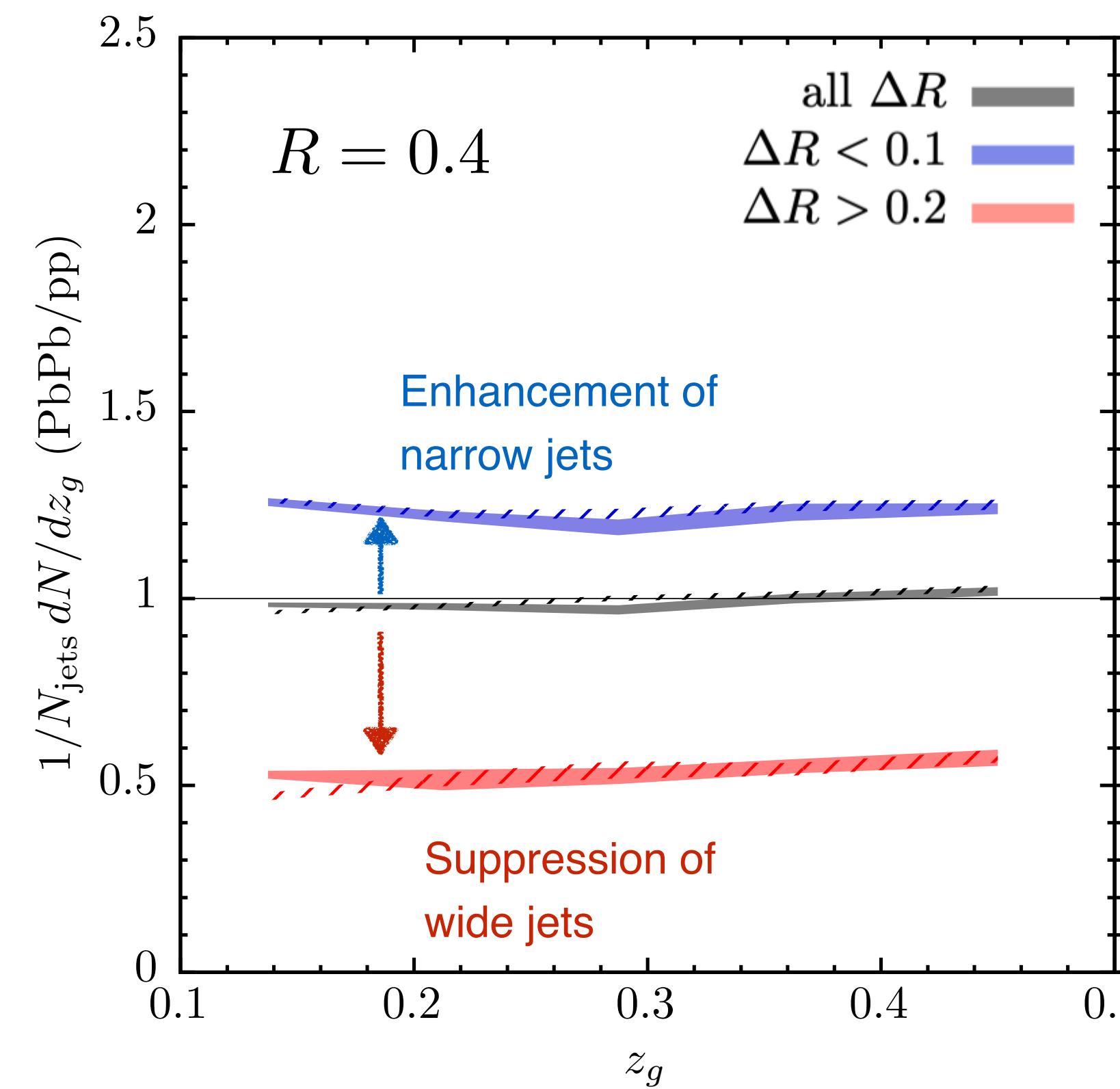
Jet observables in heavy ion collisions:

- usually look at differences, ratios, between medium and vacuum jet ensembles selected with a given  $p_T > p_T^{\text{cut}}$

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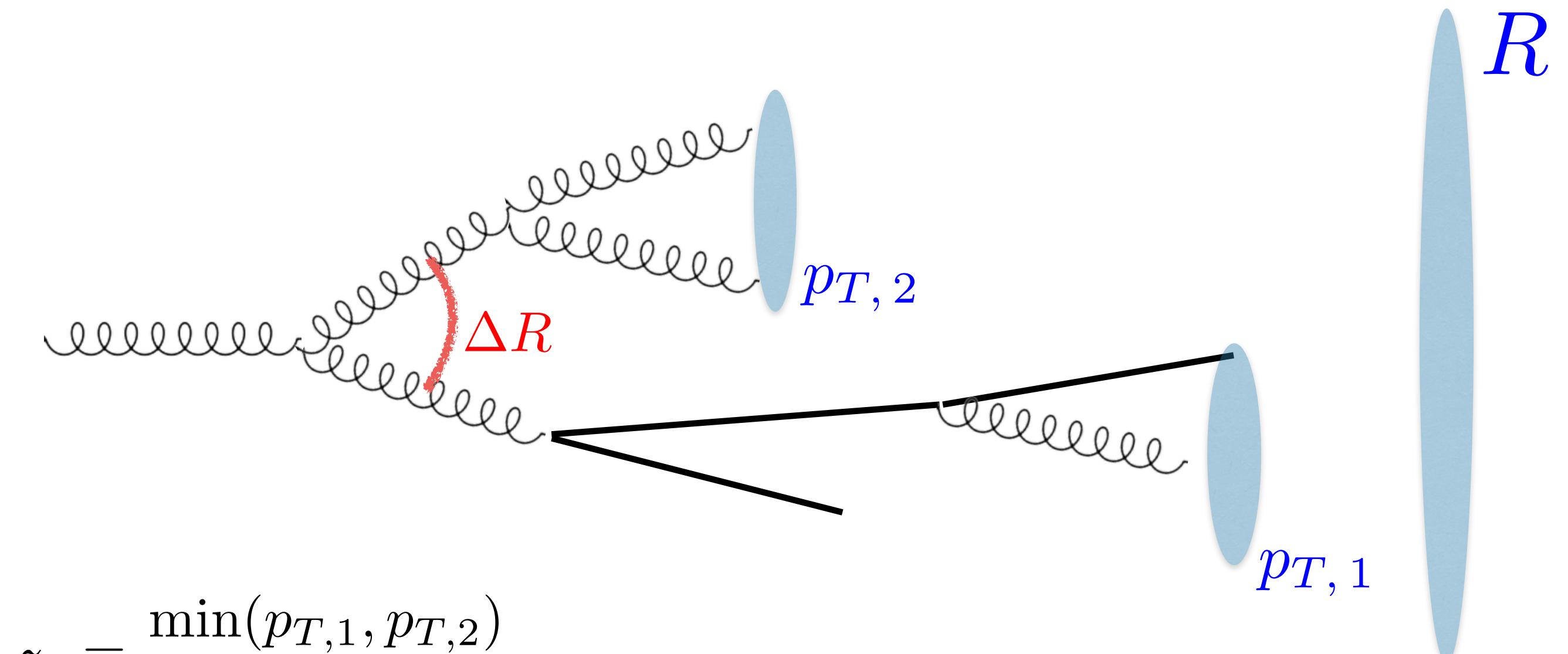
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Casalderrey-Solana, Milhano, DP, Rajagopal, JHEP '20

## Test case: $\Delta R$ (or $R_g$ )

$\Delta R$  is groomed angle of 1st SoftDrop (SD) with  $z_{\text{cut}}=0.1$  and  $\beta=0$ .

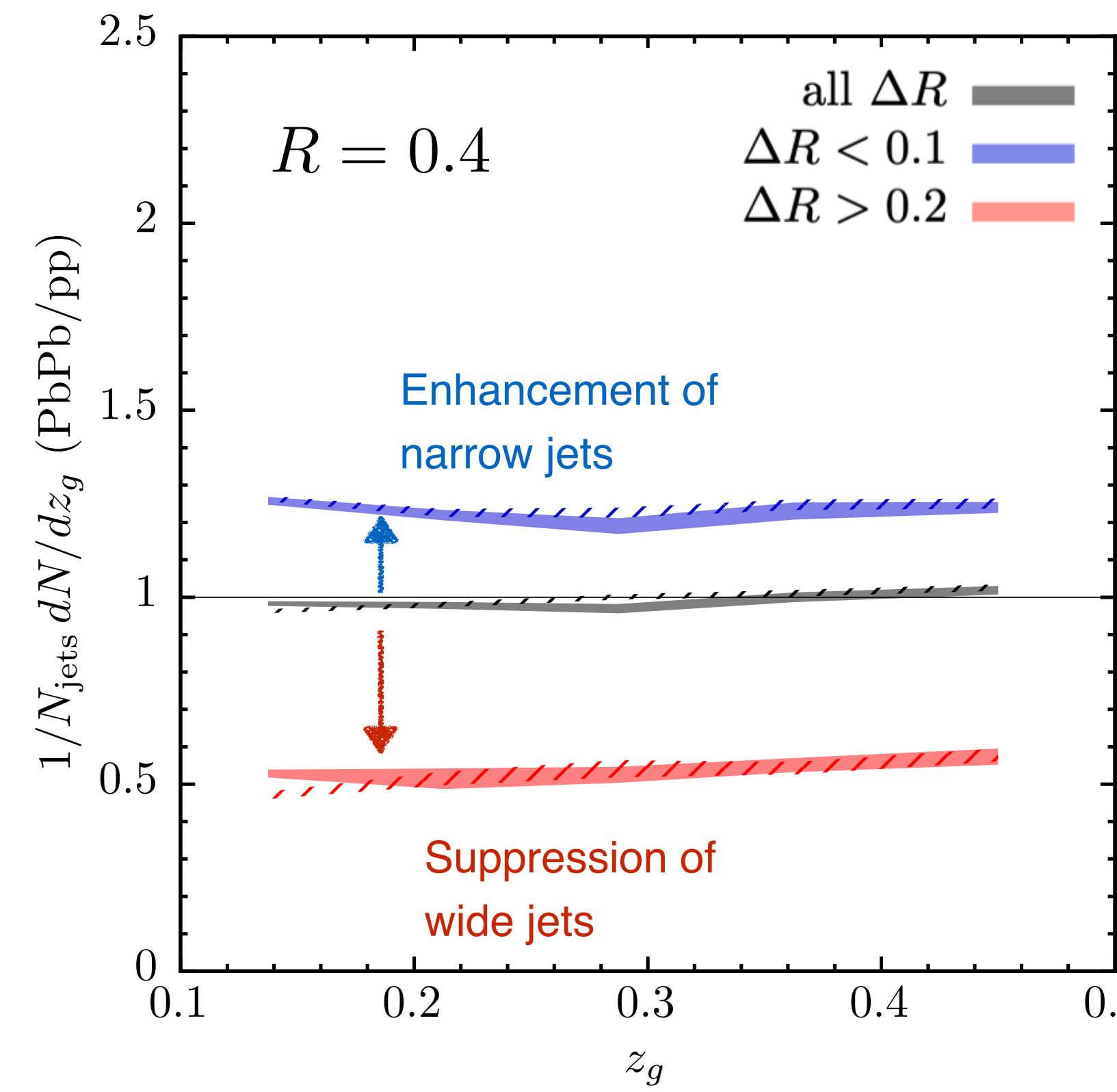


$$z_g \equiv \frac{\min(p_{T,1}, p_{T,2})}{p_{T,1} + p_{T,2}}$$

# Interpretation of Observables

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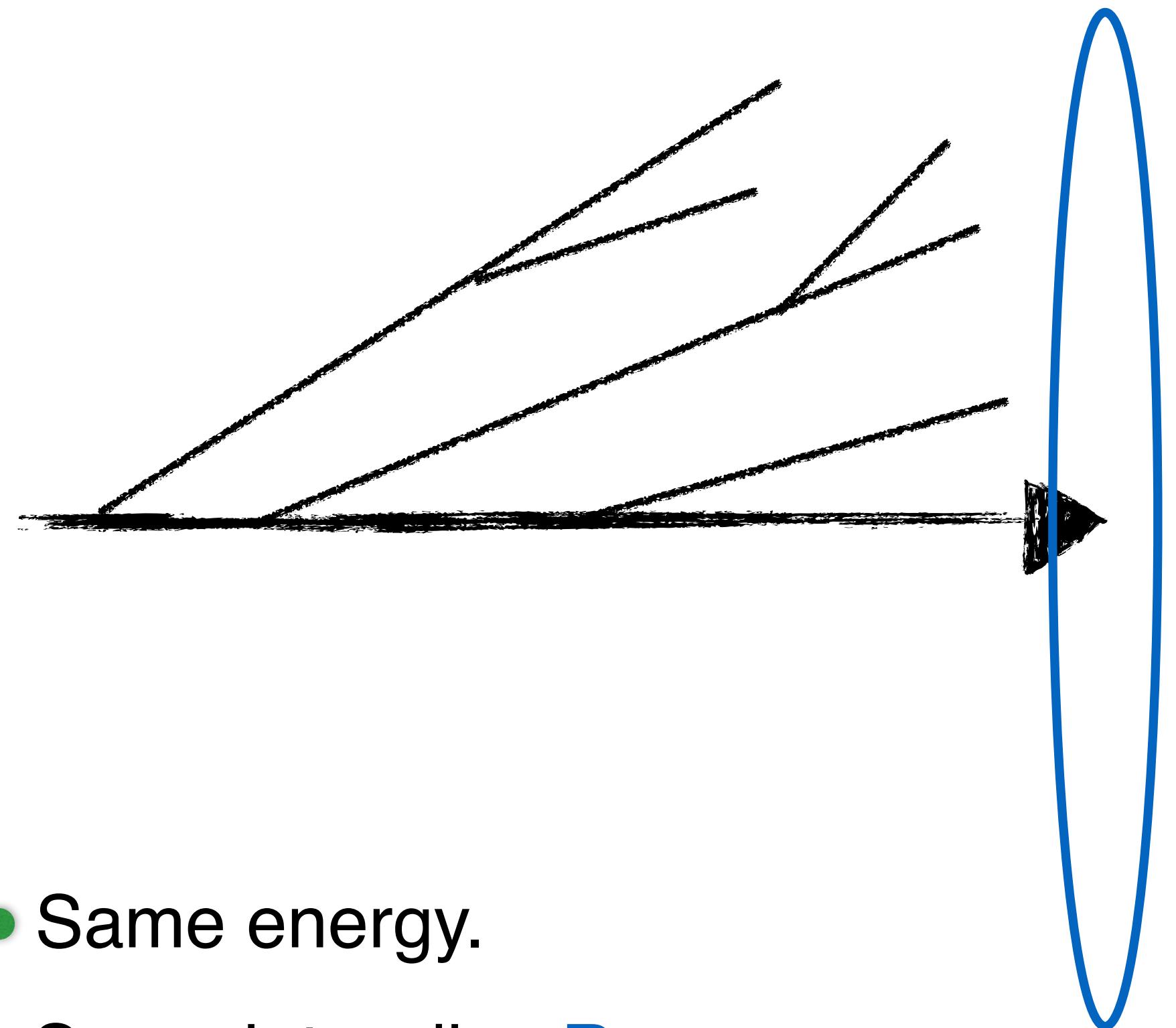
$\Delta R$  is groomed angle of 1st SoftDrop (SD) with  $z_{\text{cut}}=0.1$  and  $\beta=0$ .

Some possible interpretations:

- Jets in medium produce emissions with smaller  $\Delta R$  than in vacuum.  
Presumes such physics dominated by medium scale.
- Jets with larger  $\Delta R$  are more suppressed and don't pass the  $p_T$  cut of the distribution.  
Presumes such physics dominated by vacuum scale.

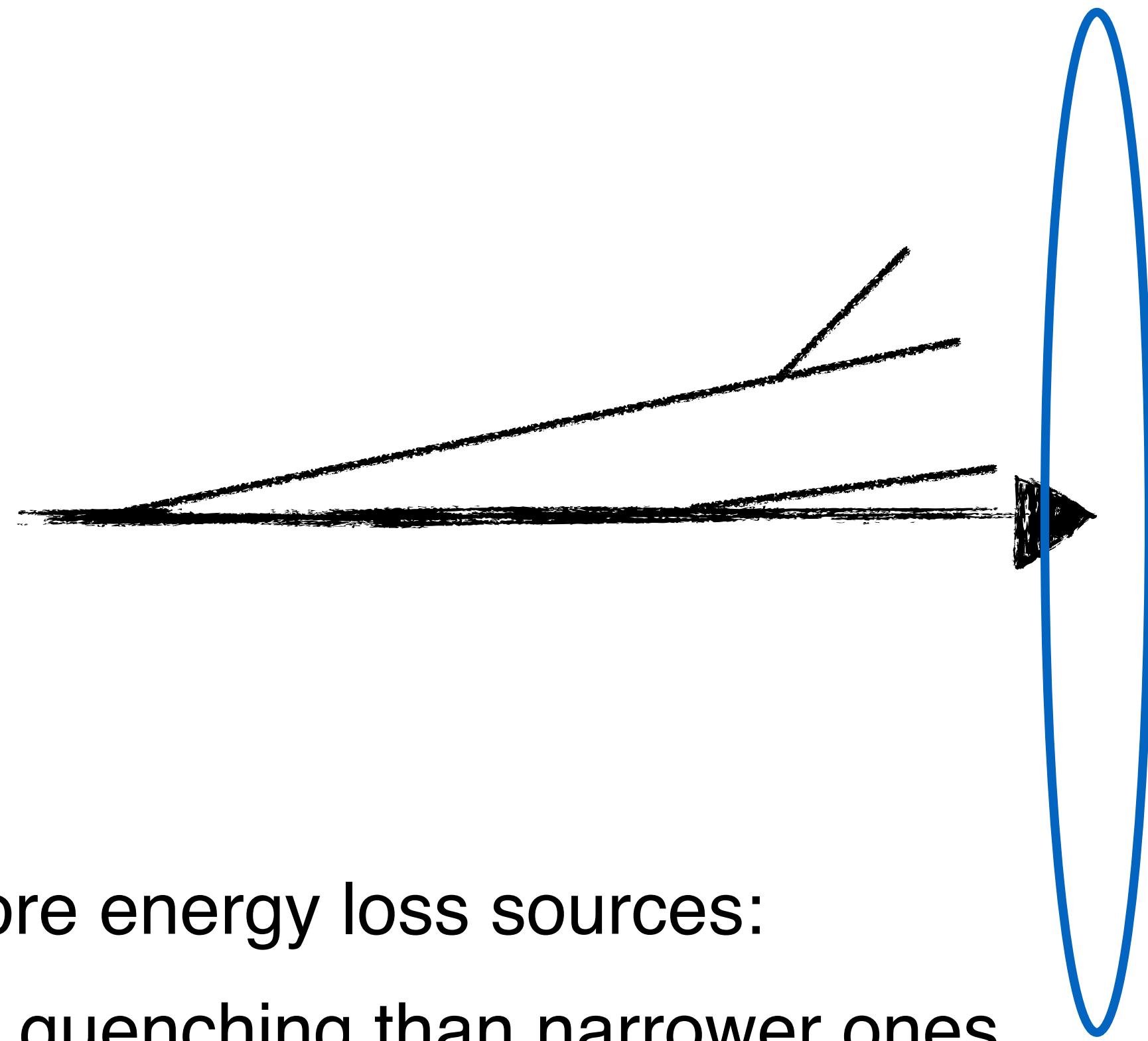
# Jets and Jets

Wide jet



- Same energy.
- Same jet radius  $R$ .
- Different fragmentation pattern.

Narrow jet



Vacuum-like  
emission

Wider jets have more energy loss sources:

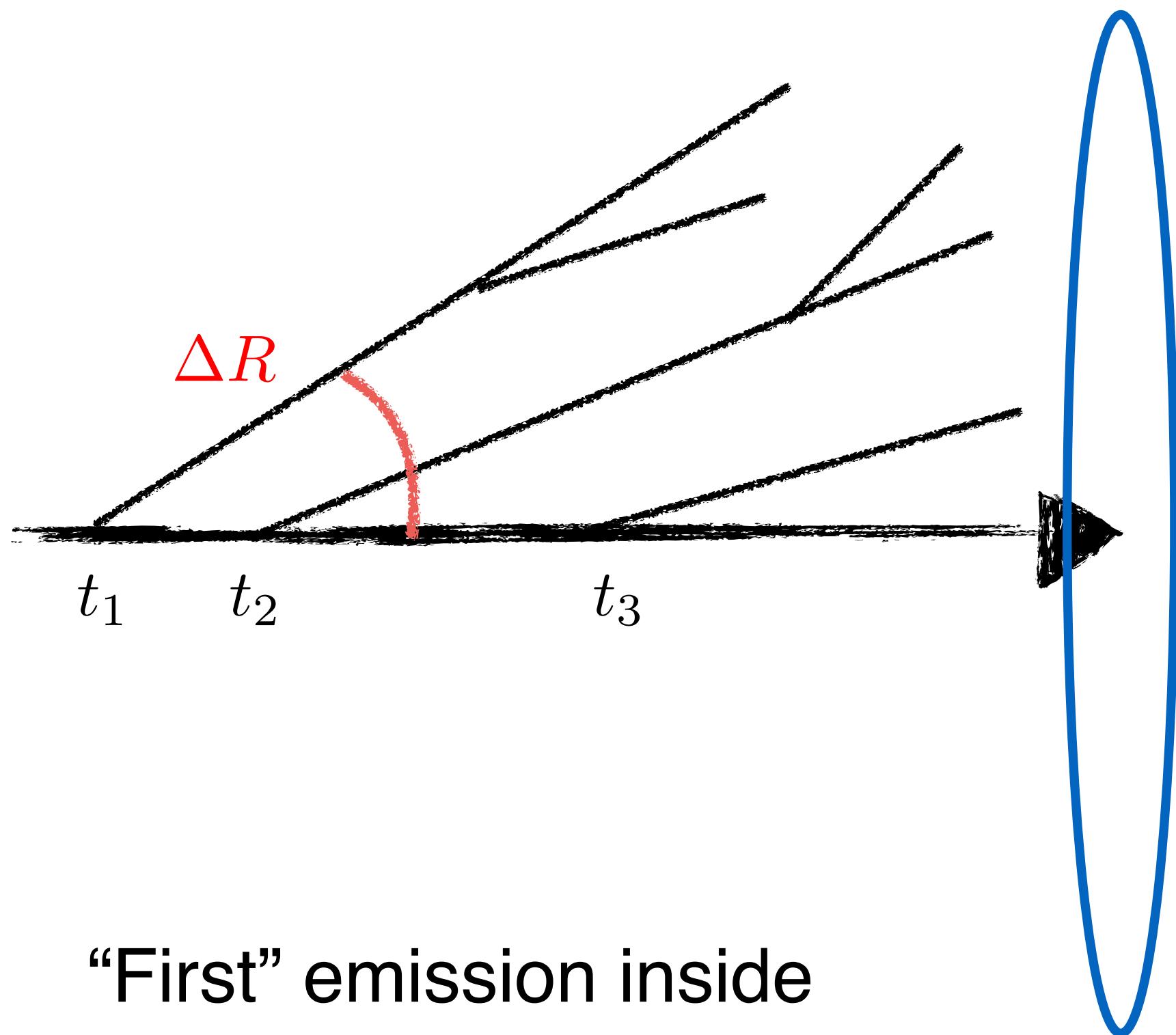
→ more total quenching than narrower ones.

Assuming:

- most of the energy goes out of the cone.
- internal structure resolved by QGP.

# Jets and Jets

Wide jet

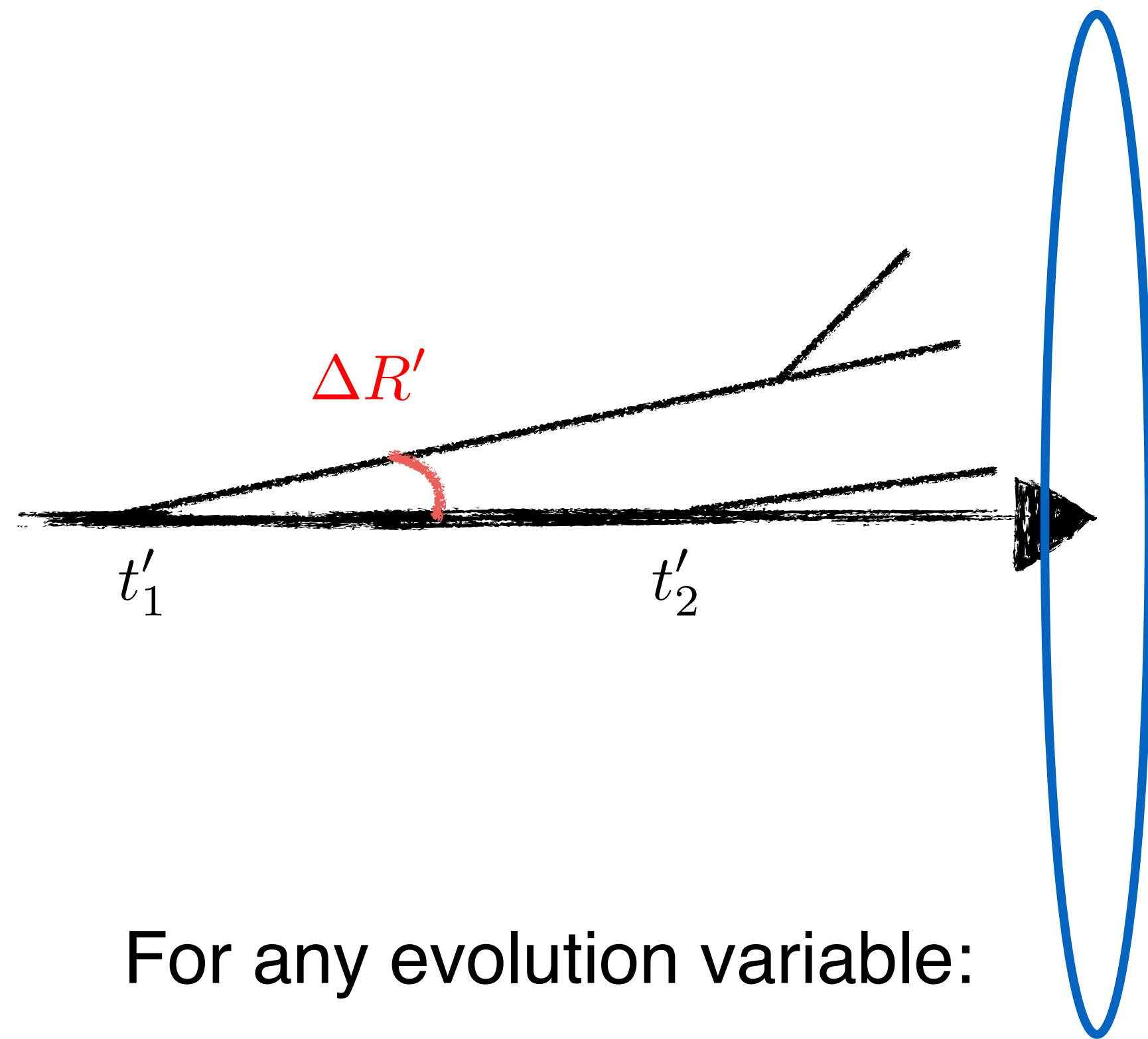


“First” emission inside  
the jet cone determines  
available phase space  
for further in-cone emissions.

Groomed angle is  
proxy for jet activity.

$$t_1 > t'_1$$

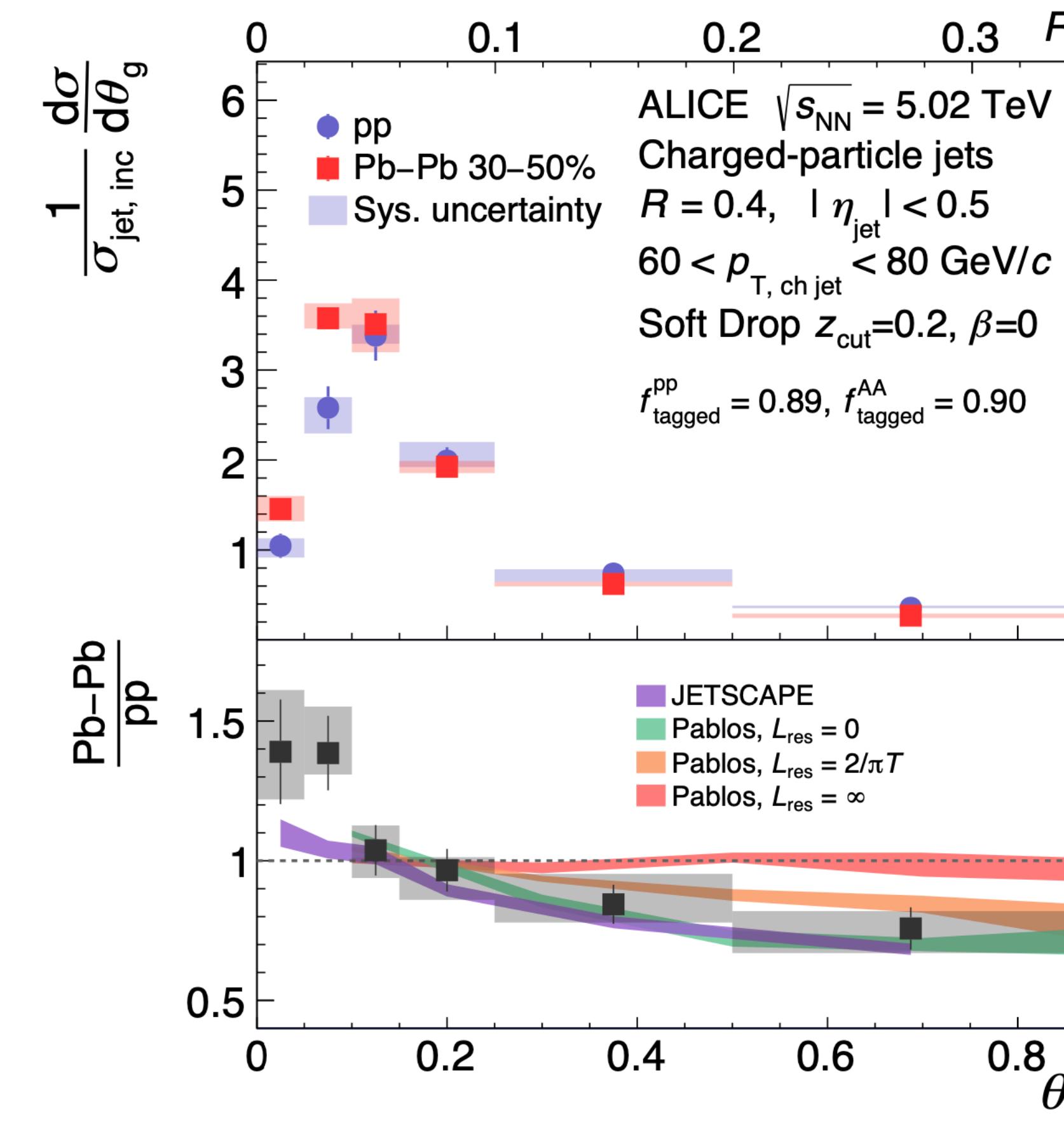
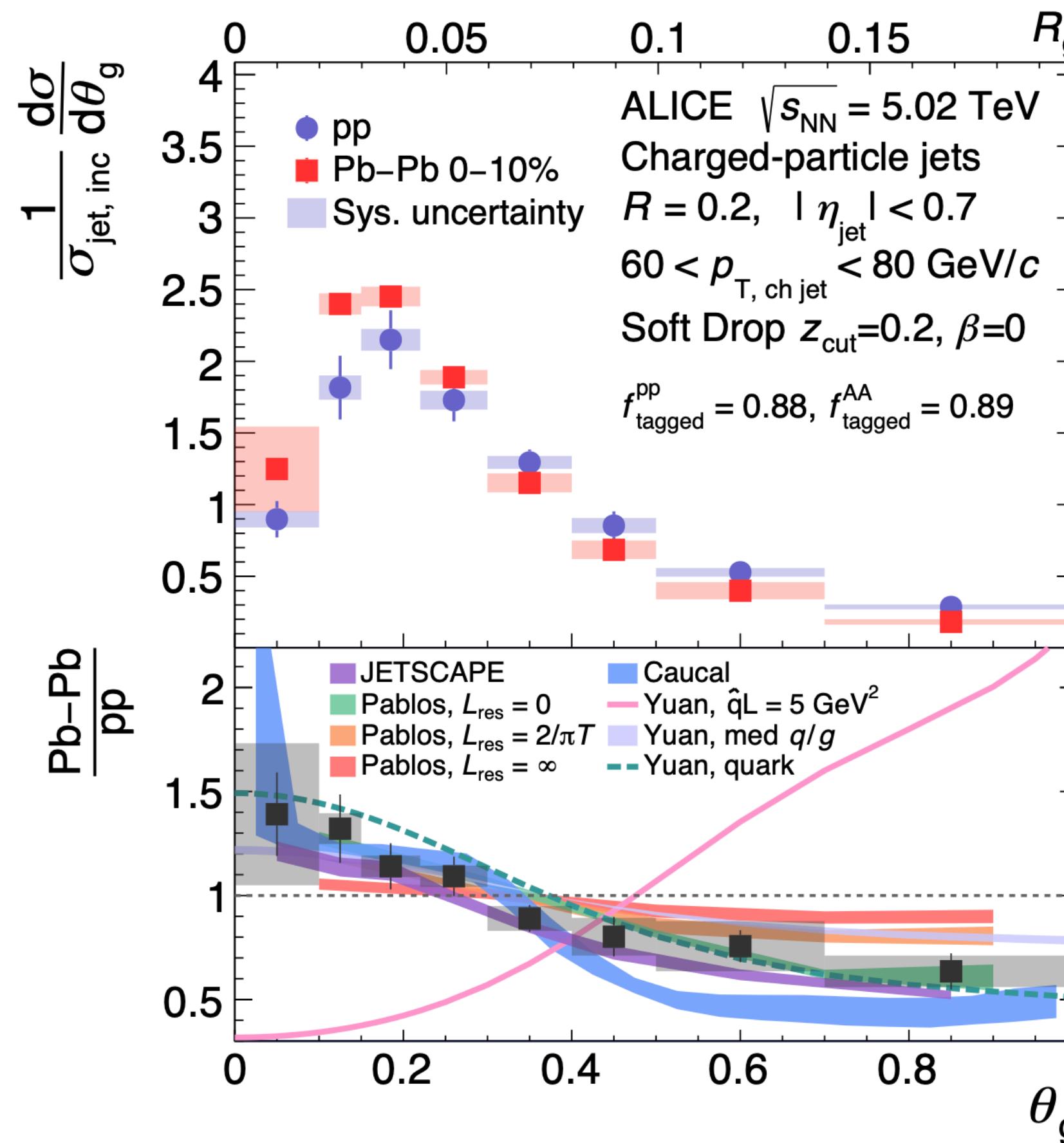
Narrow jet



For any evolution variable:

$$\begin{aligned} t_1 &\propto \Delta R \\ t'_1 &\propto \Delta R' \end{aligned}$$

# Common feature among MC models



ALICE - PRL '22

$\Delta R$  narrowing observed in data, well reproduced by variety of models.

We observe the absence of wide jets because of  $p_T$  cut, selection bias.

Most relevant common feature between MCs:

→ dominance of vacuum physics at early, high energy stages of the shower.

# Vacuum-like Jets in the Medium

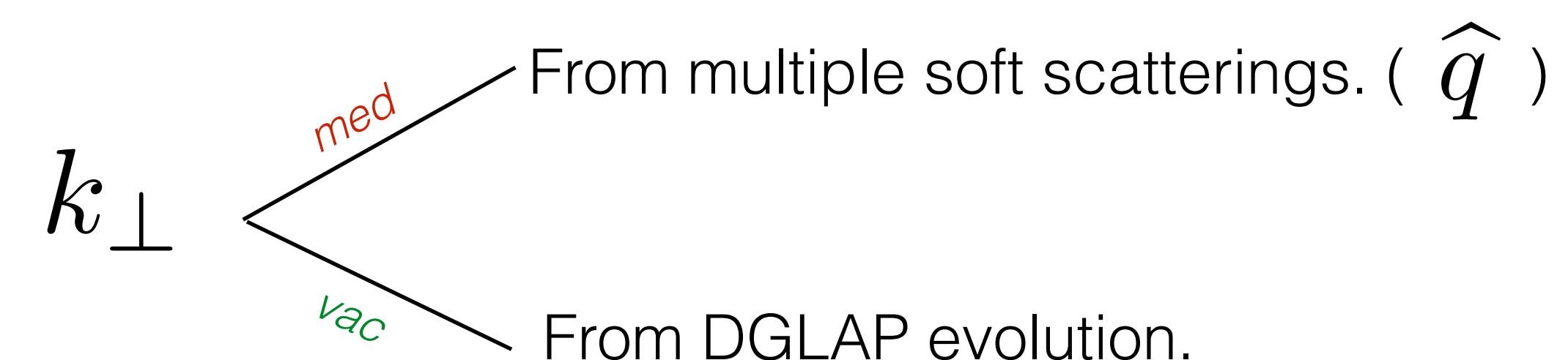
Jets experience part of their evolution as if they were in vacuum, *formation times arguments*.

Formation time  $\mathcal{T}_f$  : when wavelength of emitted gluon resolves transverse separation.

A given emission is vacuum-like (VLE) if:

$$\mathcal{T}_f \ll \tau_{\text{med}}$$

Implies separation  
of momenta.



A given dipole is resolved (both legs lose energy) if:

$$\tau_{\text{coh}} < L \quad \rightarrow \quad \theta > \theta_c \sim 1/\sqrt{\hat{q}L^3}$$

Time it takes a dipole to decohere  
via multiple color rotations.

All VLE are angular ordered, since  $\mathcal{T}_v < \tau_{\text{coh}}$ . [Caucal et al. - 1801.09703](#)

VLEs included in MC, either full factorization, or allowing corrections from rare kicks (JEWEL, MATTER).

# Vacuum-like Jets in the Medium

Jets experience part of their evolution as if they were in vacuum, *formation times arguments*.

Formation time  $\tau_f$ : synchrotron wavelength of emitted gluon rescale transverse separation.

A given emission is vacuum-like (VLE) if:

$$\tau_f \ll \tau_{\text{med}}$$

implies separation  
of momenta.

## Vacuum-like & Medium-induced

A given dipole is resolved (both legs lose energy) if:

$$\tau_{\text{coh}} < \theta_c / \sqrt{\hat{q} L^3}$$

Time it takes a dipole to decohere  
via multiple color rotations.

## not well understood!

All VLE are angular ordered, since  $\tau_v < \tau_{\text{coh}}$ . Caucal et al. - [1801.09703](#)

VLEs included in MC, either full factorization, or allowing corrections from rare kicks (JEWEL, MATTER).

# Diagnosing jet energy loss with deep learning

Selection bias is a dominant effect for many jet observables:

- Common to all calculations, jet MCs, that include jet substructure fluctuations.
- Obscures the interpretation of data: how do quenched jets really look like?

→ Use deep learning techniques to determine amount of energy loss jet-by-jet:

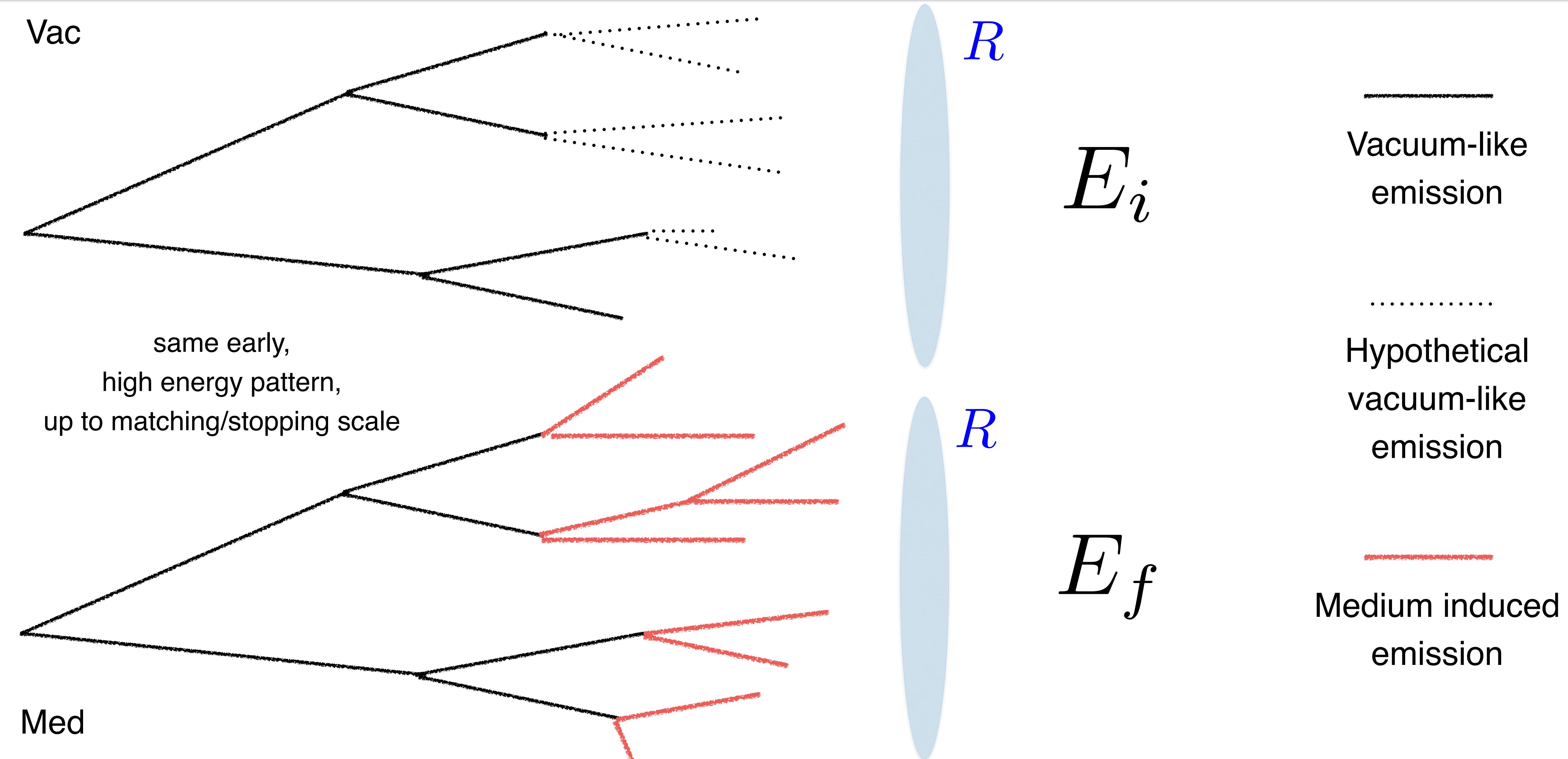
Energy loss ratio:  $\chi_{jh} \equiv \frac{E_f}{E_i}$

Final, measurable jet energy.  
Vacuum energy (had there been no medium).

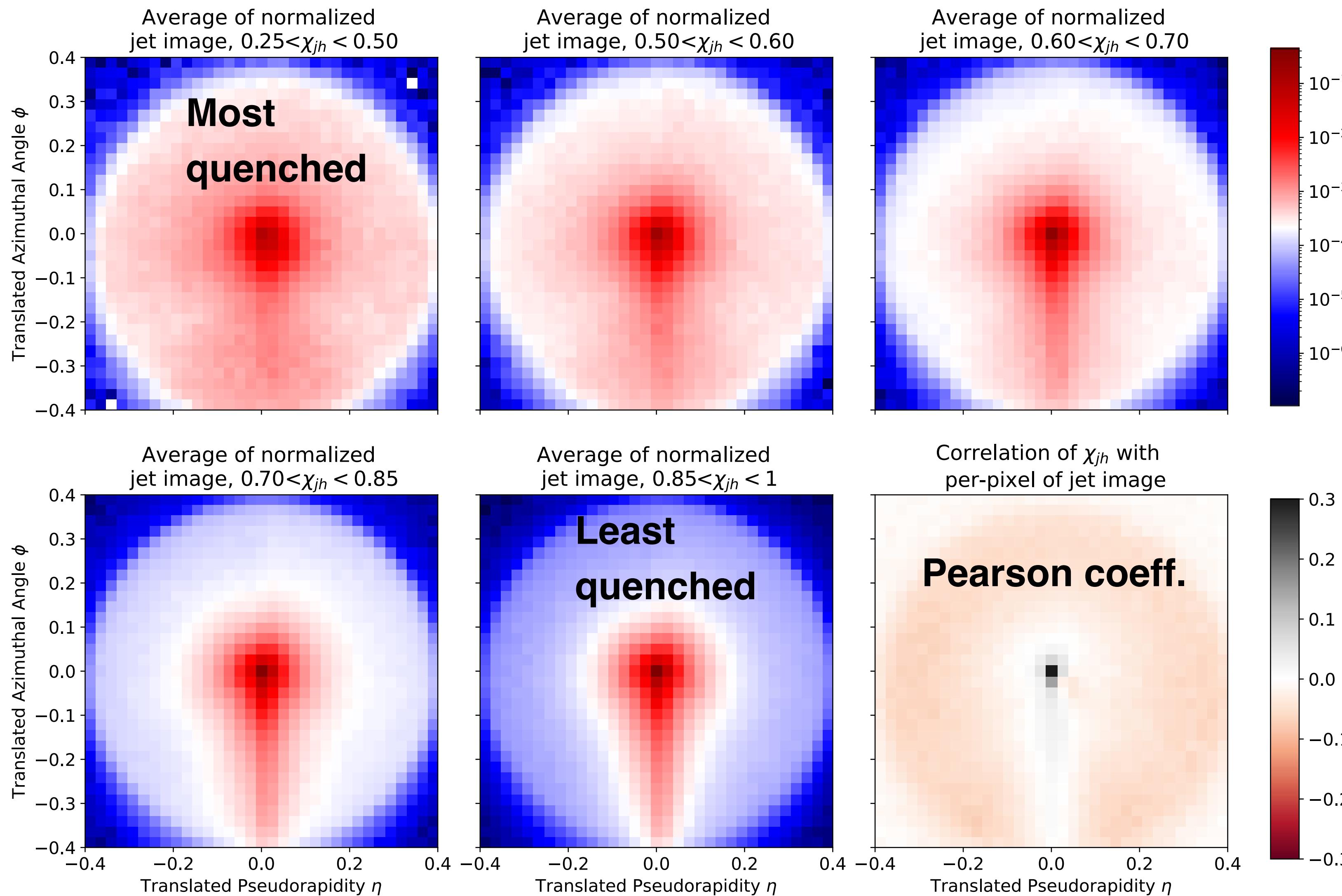
Want to:

- Understand true, most revealing features of energy loss.
- Extract amount of energy loss jet-by-jet in experimental data.

# Defining the Energy Loss Ratio



# Jet Image



**Image preprocessing:**

- $\Phi$  and  $\eta$  coord. w.r.t. jet axis.
- Rotate image to have groomed subjet at  $\Phi = -\pi/2$ .

**Recognize basic features of jet quenching:**

→ Energy loss increases number of soft particles at large angles.

# Prediction Performance

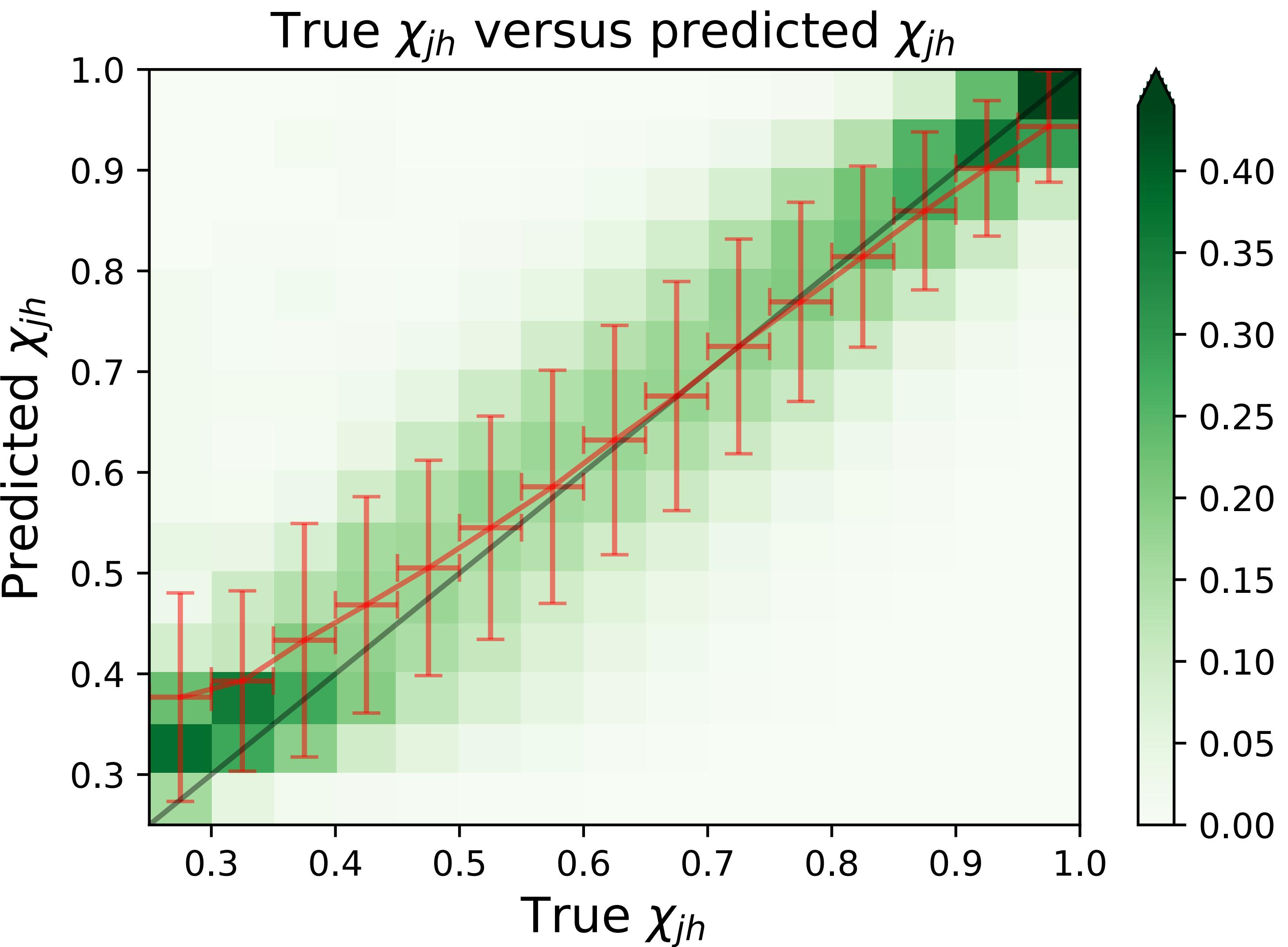
Good performance over wide range of  $\chi$ .

Histo: Probability of predicted  $\chi$  given true  $\chi$ .

Bars: Average and standard deviation.

Sanity checks:

- Performance not species dependent (quark or gluon initiated jet).
- Network predicts  $\chi = 0.98(3)$  for pp jets.



# Applications: Groomed Observables

$R_g$  ratio between PbPb and pp:

FES:

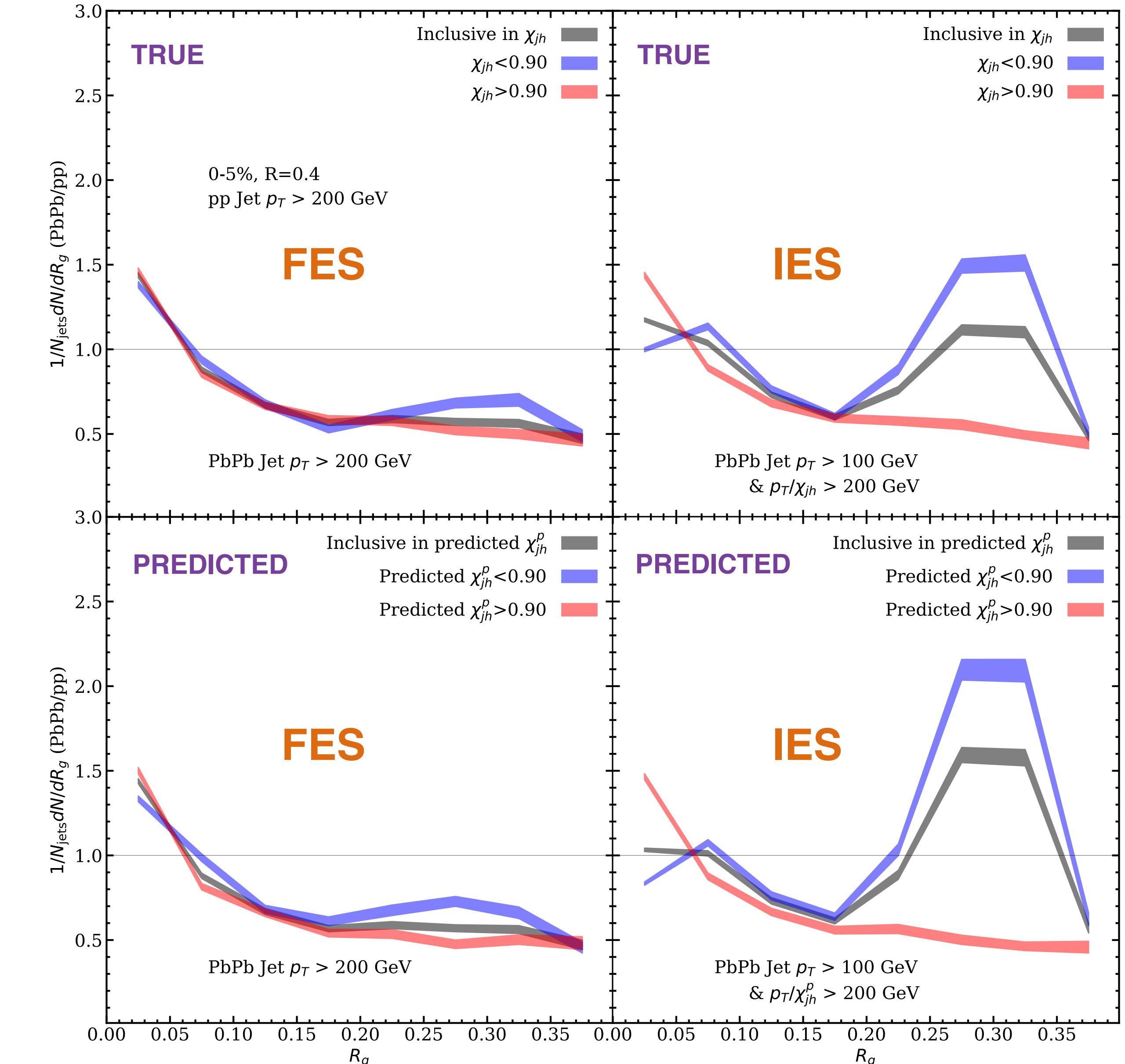
Observe selection bias towards jets with small  $R_g$ .

IES:

Quenched class presents features actually related to energy loss:

→ Enhancement at large  $R_g$ .

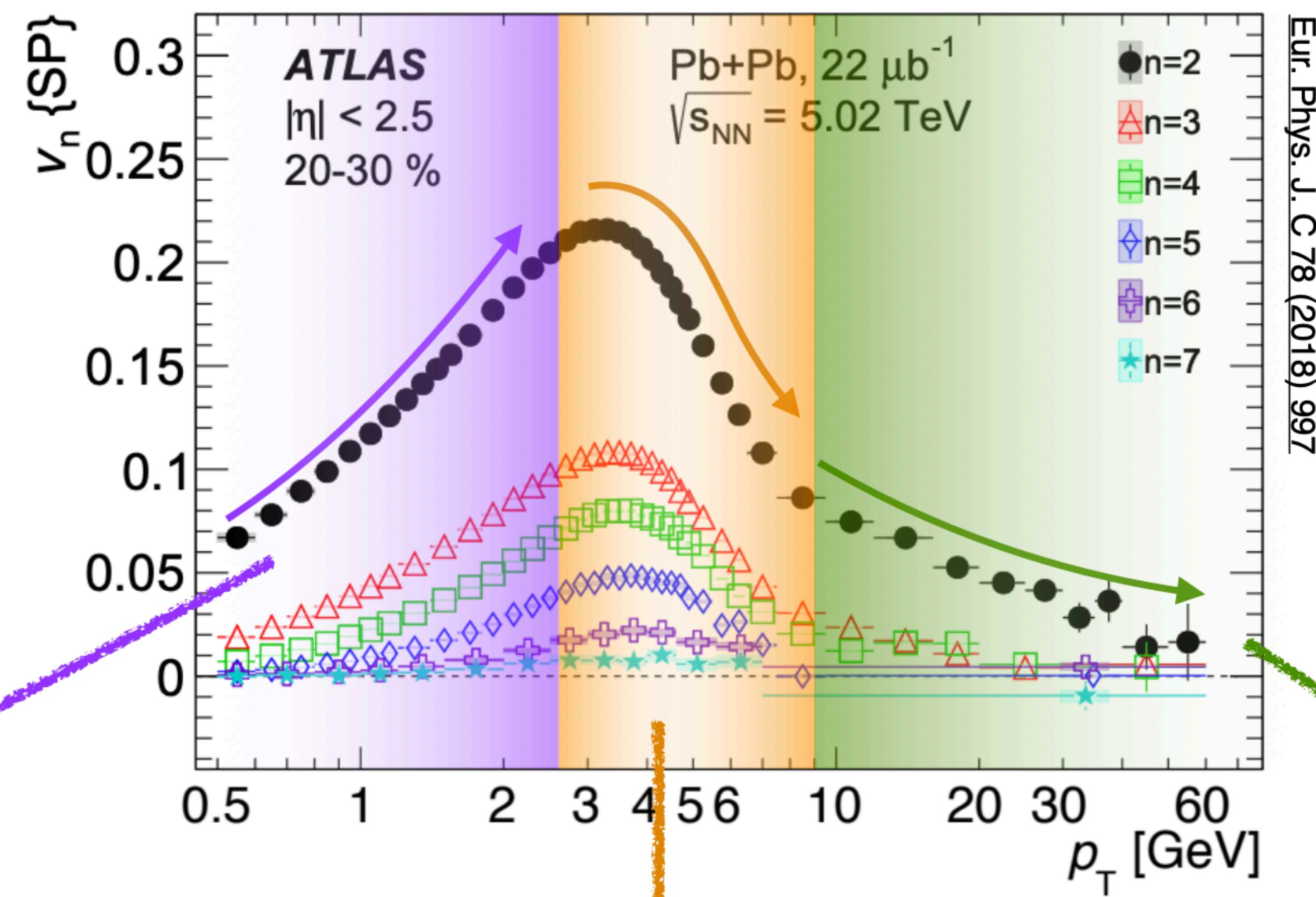
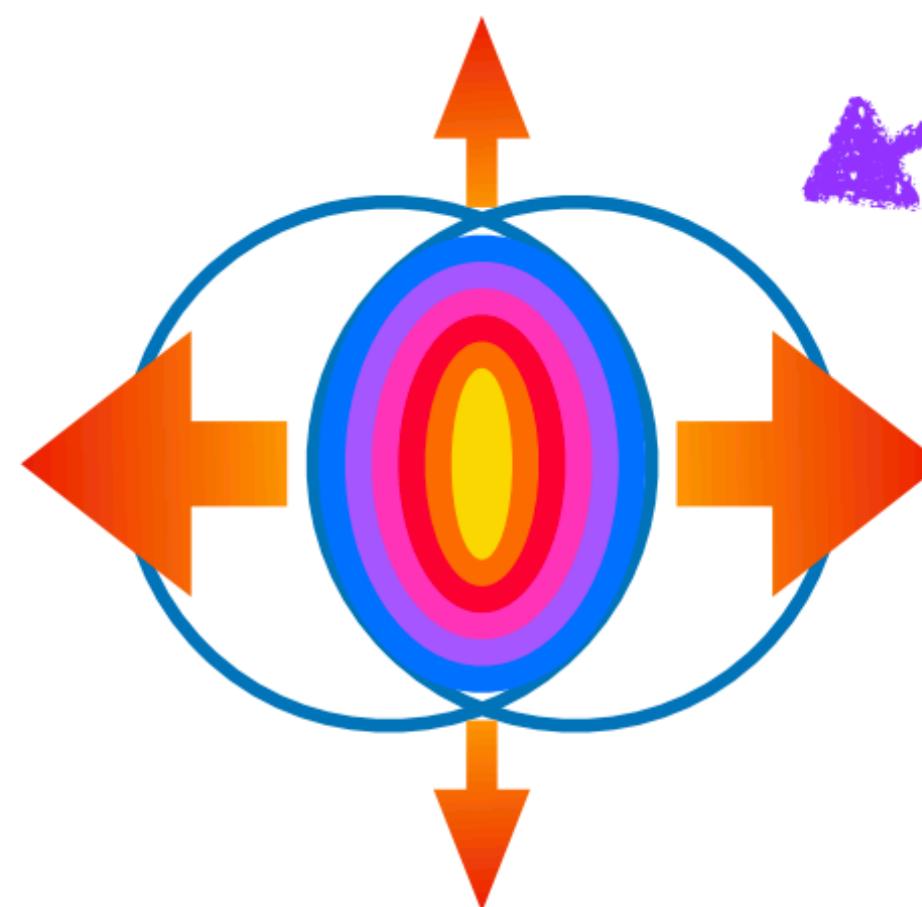
Unquenched class still biased (to belong to this class, a jet needs to be of a special kind).



# Jet Azimuthal Anisotropy

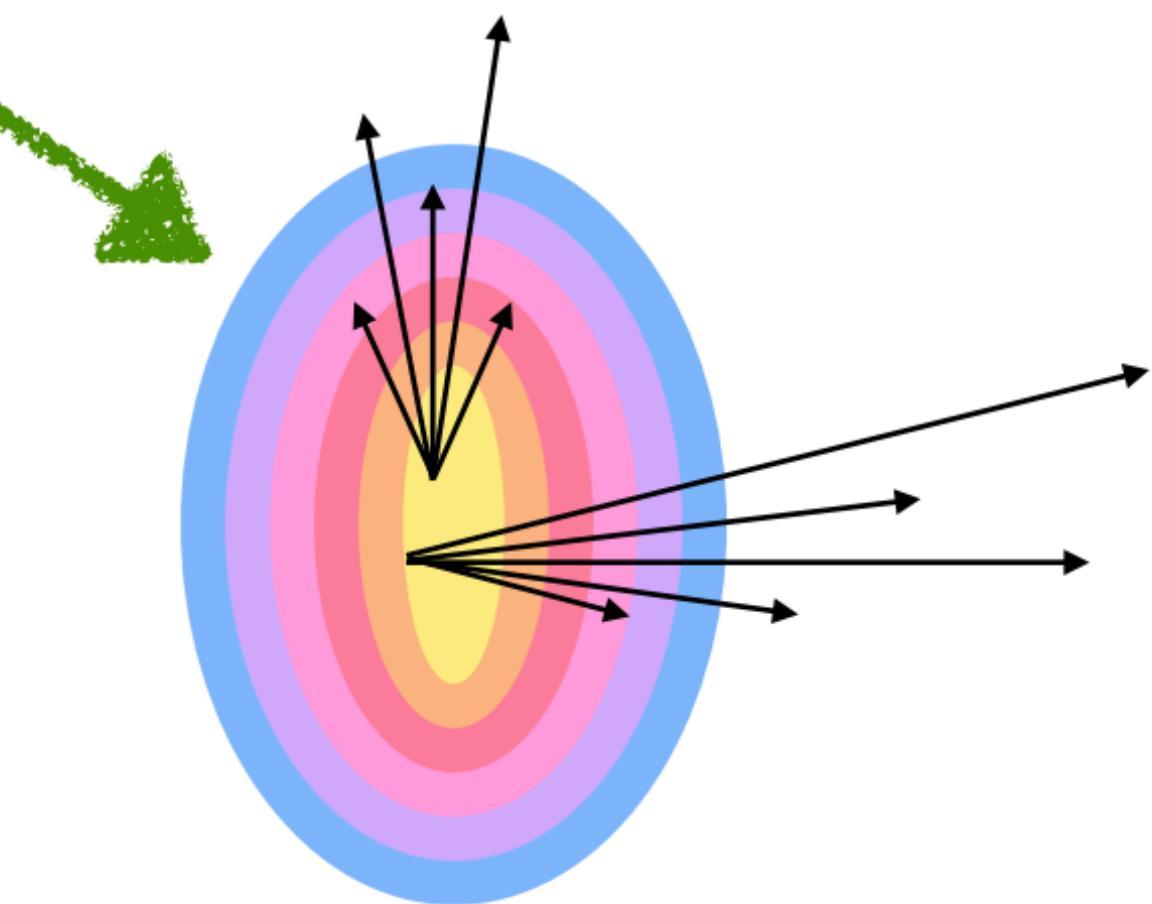
Slide from  
K. Hill at QM'19

Hydrodynamics



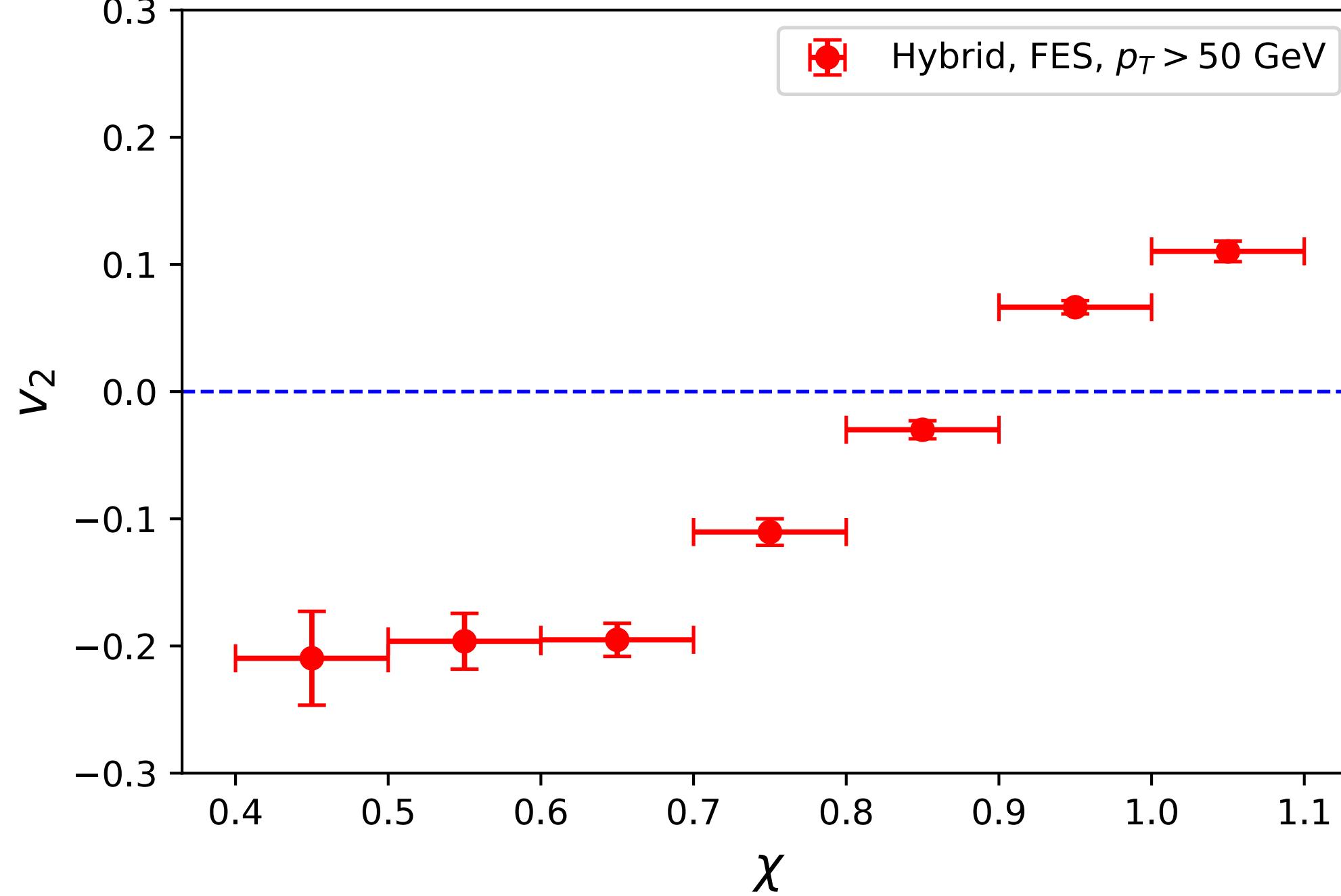
Transition region

Differential  
energy loss

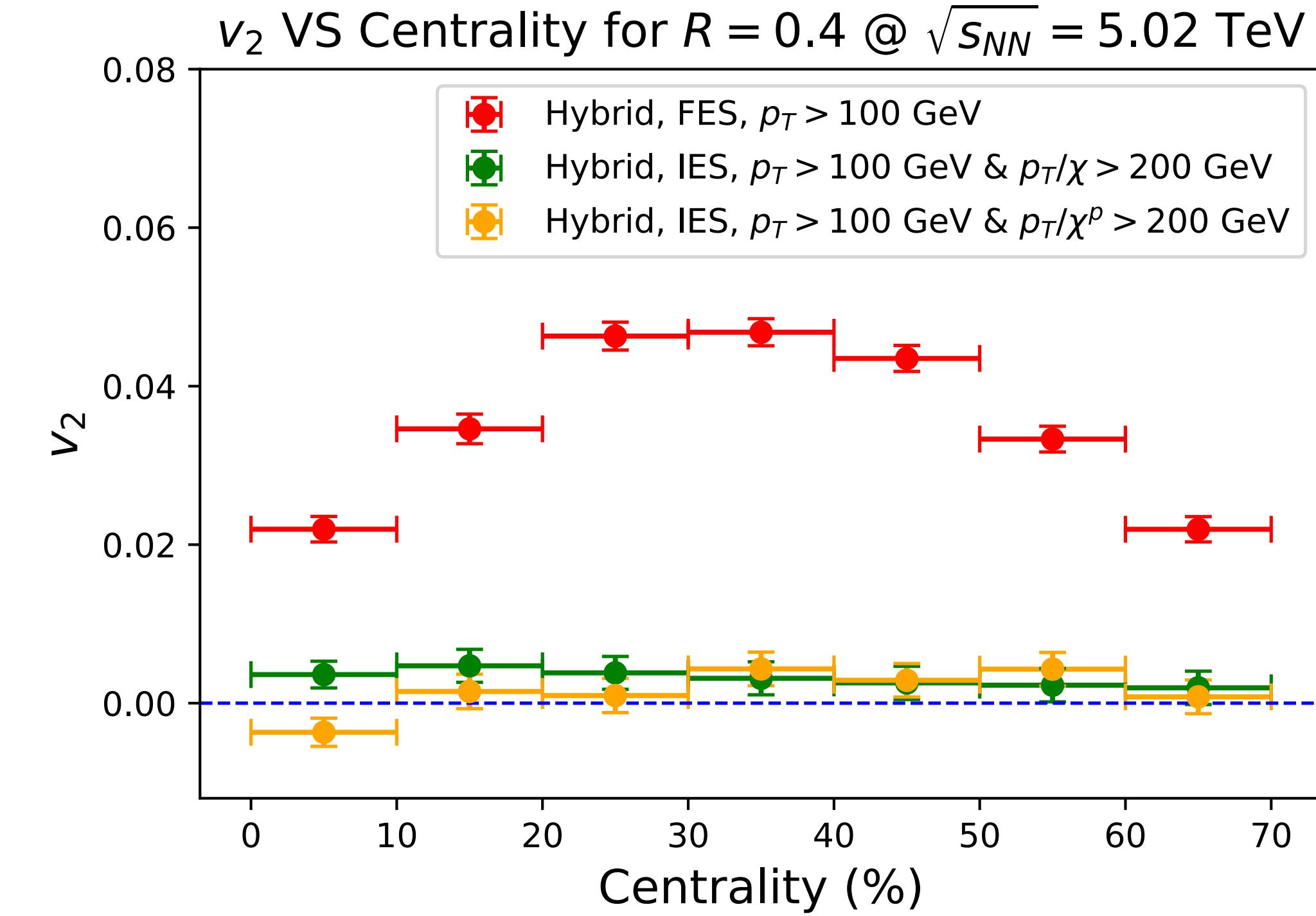


# Accessing Initial Jet Anisotropies

$v_2$  VS  $\chi$  for centrality 30-40%,  
 $R = 0.2$  @  $\sqrt{s_{NN}} = 2.76$  TeV



Du, DP, Tywoniuk - PRL '21



- Intuitive origin of high- $p_T$  jet anisotropies:

Small  $\chi$  (large energy loss):

- longer path length;
- $v_2 < 0$ .

and viceversa for large  $\chi$ .

- However, if use IES:

Reveals initial azimuthal anisotropies.

In this model: none →  $v_2 \sim 0$ .

And in experiments?

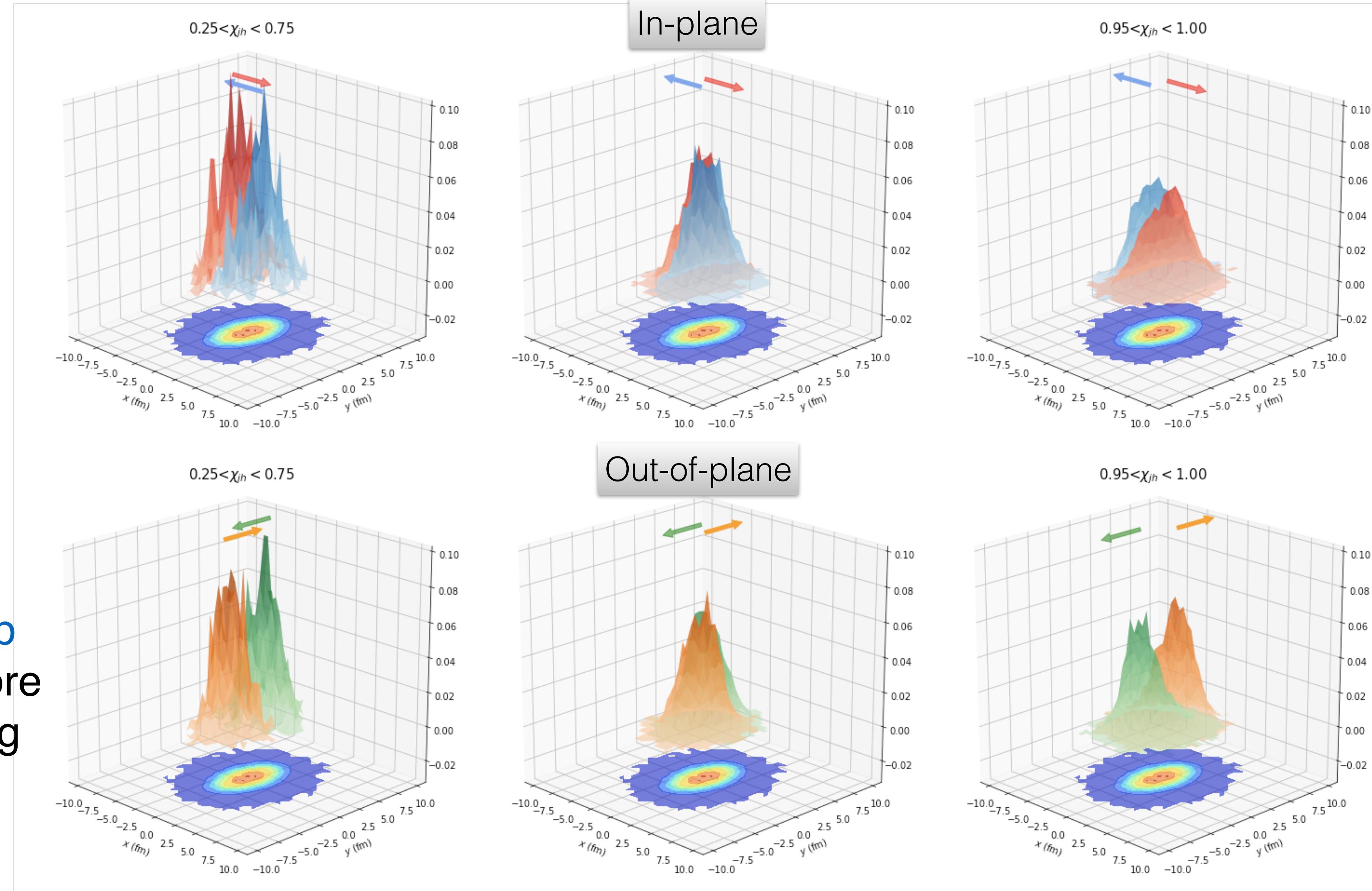
# Tomography with Deep Learning

Determination of production point in transverse plane.

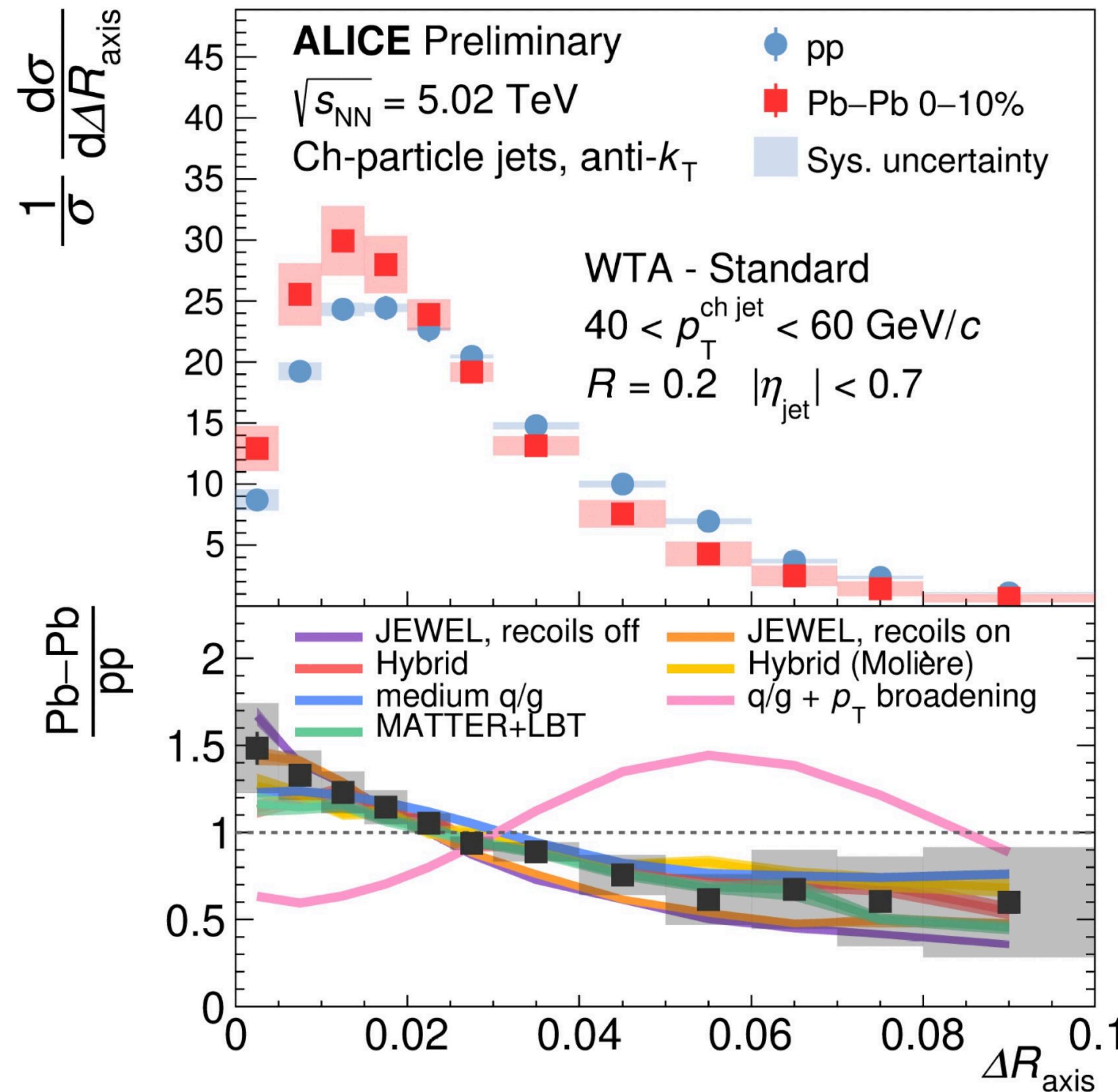
Differential in:

- Orientation w.r.t. event plane.
- Energy loss ratio  $\chi$ .

Production points **swap** in order to traverse more medium with increasing energy loss.



# Narrowing of Jet Substructure



Example: WTA axis distance w.r.t. anti- $k_T$  axis

Many Monte Carlo models get similar results.

Bias towards narrower, less active jets.

Medium q/g can also account for the signal.

Strong suppression of gluon jets (factor 4 w.r.t. pp).

Qiu et al. - PRL '19

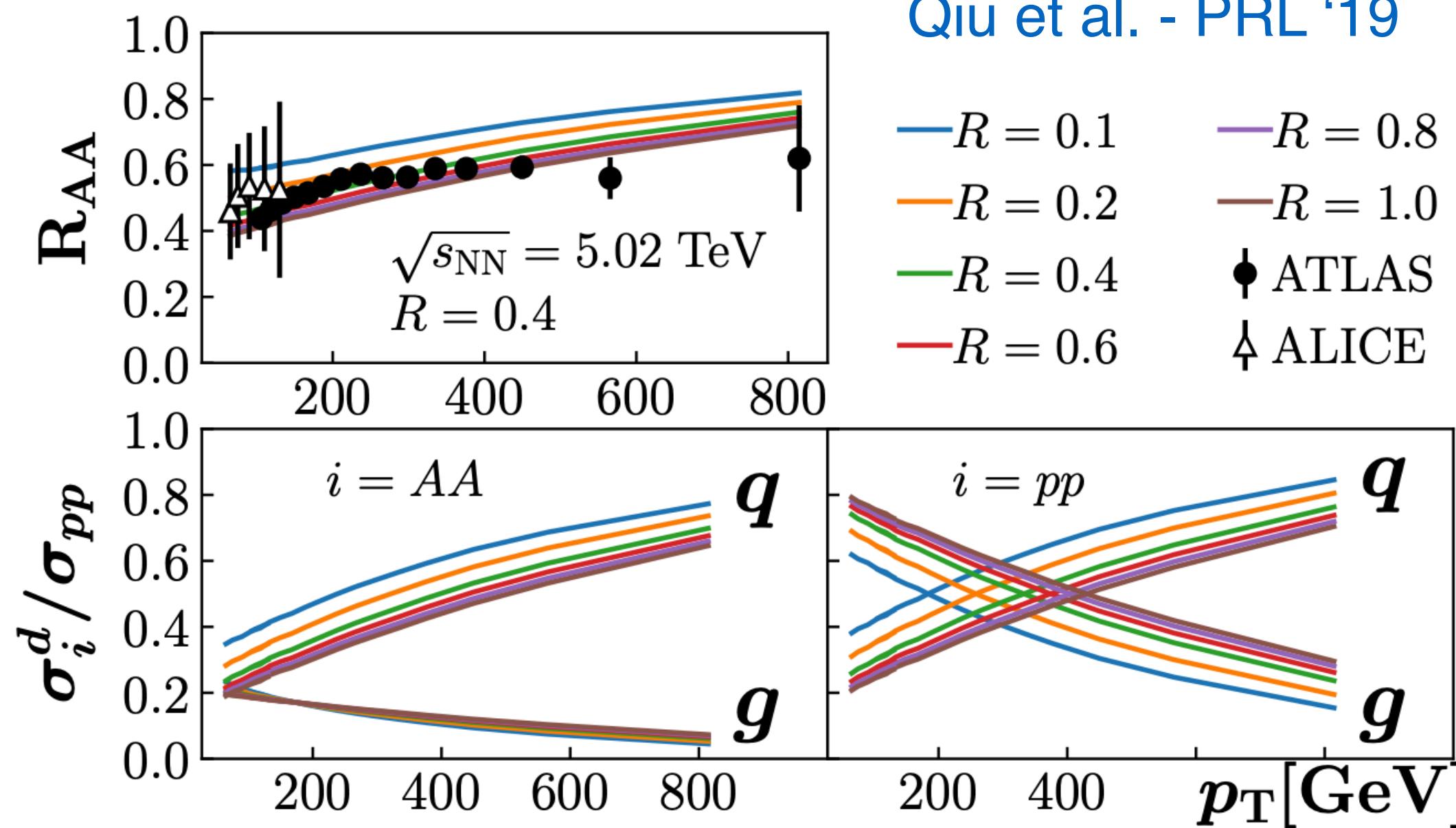
Medium q/g +  $p_T$  broadening fails.

Not accounting for selection bias, while broadening emissions, results in a broader jet ensemble.

Ringer et al. - PLB '19

R. Cruz-Torres talk at QM22

# Modified q/g Fraction



- Combination of quark and gluon contributions:

$$\frac{1}{\sigma_{\text{incl}}} \frac{d\Sigma(\theta_g)}{dp_T d\eta} = f_q \Sigma_q(\theta_g) + f_g \Sigma_g(\theta_g)$$

- Broadening added as non-perturbative kick.

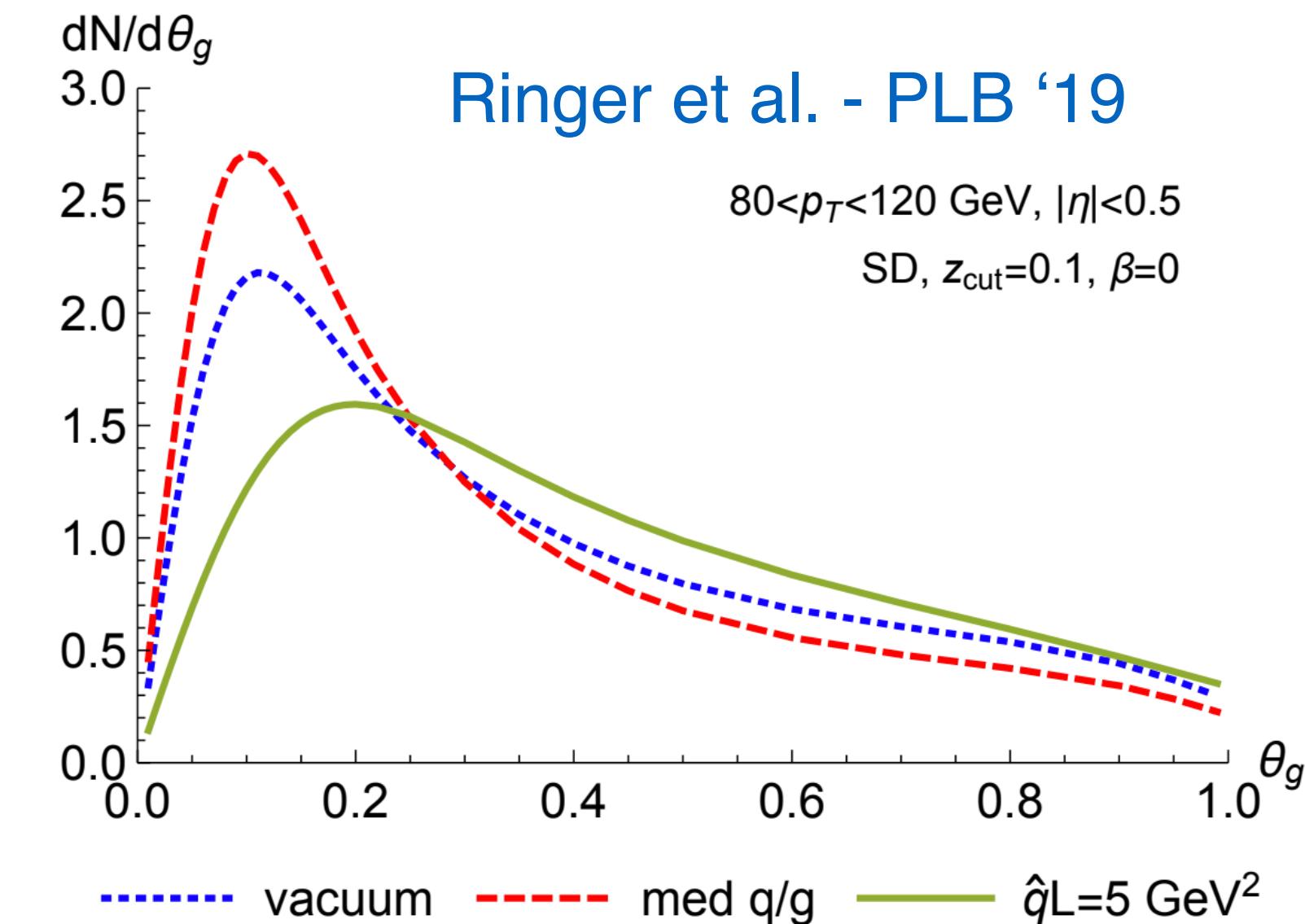
- Parametrization of modification of jet function (similar to nPDF).

$$\mu \frac{d}{d\mu} J_c(z, p_T R, \mu) = \sum_d P_{dc}(z) \otimes J_d(z, p_T R, \mu)$$

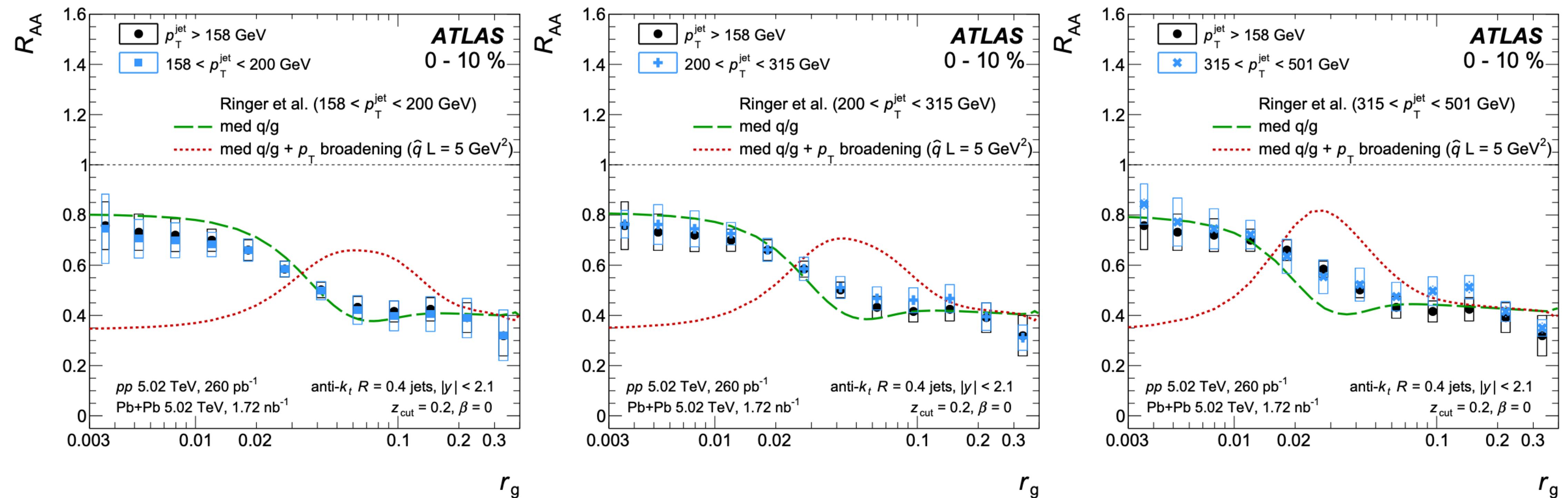
$$J_c^{\text{med}}(z, p_T R, \mu_J) = W_c(z) \otimes J_c(z, p_T R, \mu_J)$$

$$W_c(z) = \epsilon_c \delta(1-z) + N_c z^{\alpha_c} (1-z)^{\beta_c}$$

→ Best fit seems to leave quark jets untouched.



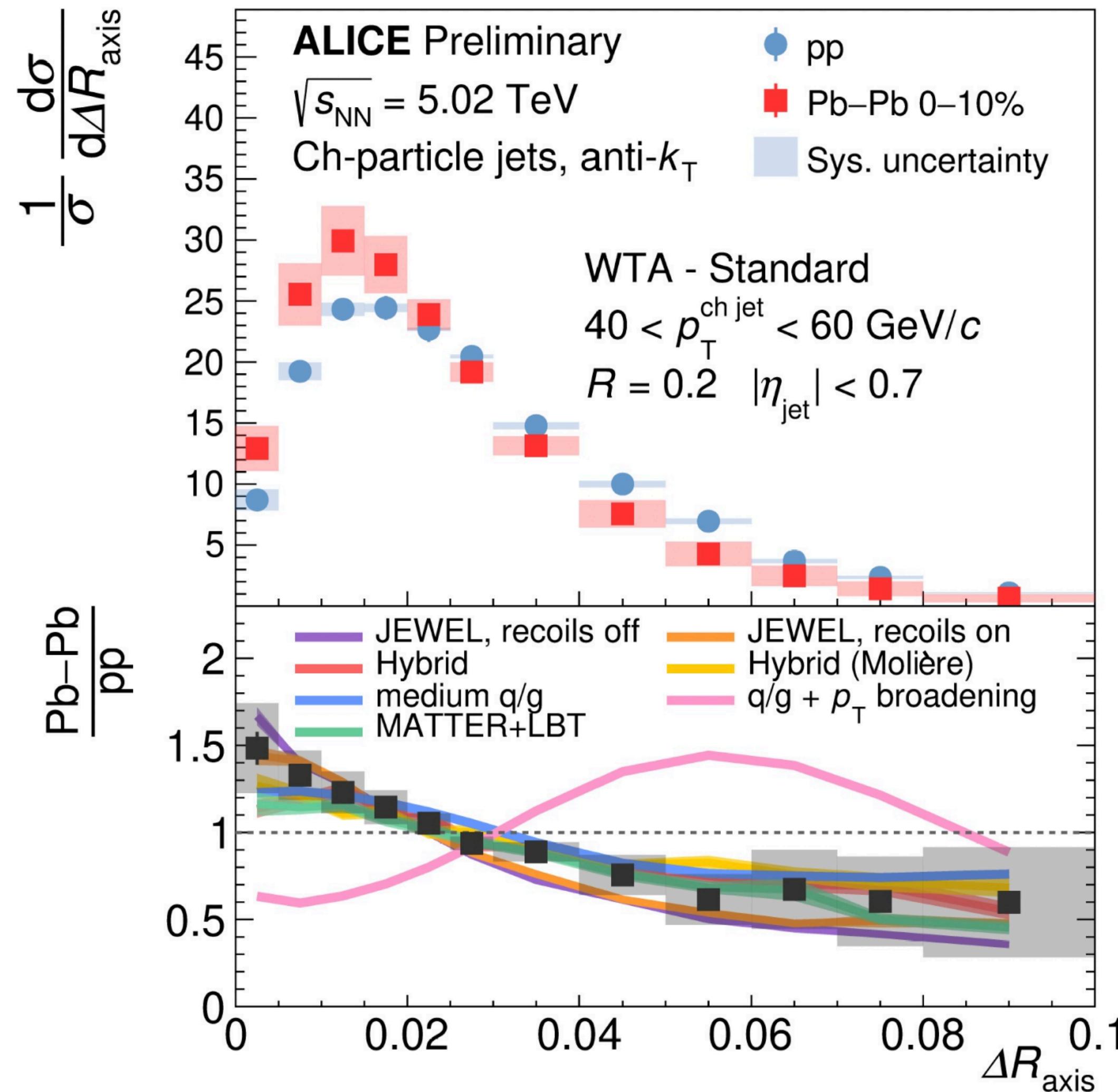
# Substructure dependent jet suppression



ATLAS - 2211.11470

- Recent ATLAS results for  $R_{AA}$  vs  $r_g$  can also be explained by modified q/g fraction model.

# Narrowing of Jet Substructure



R. Cruz-Torres talk at QM22

How can we discriminate between:

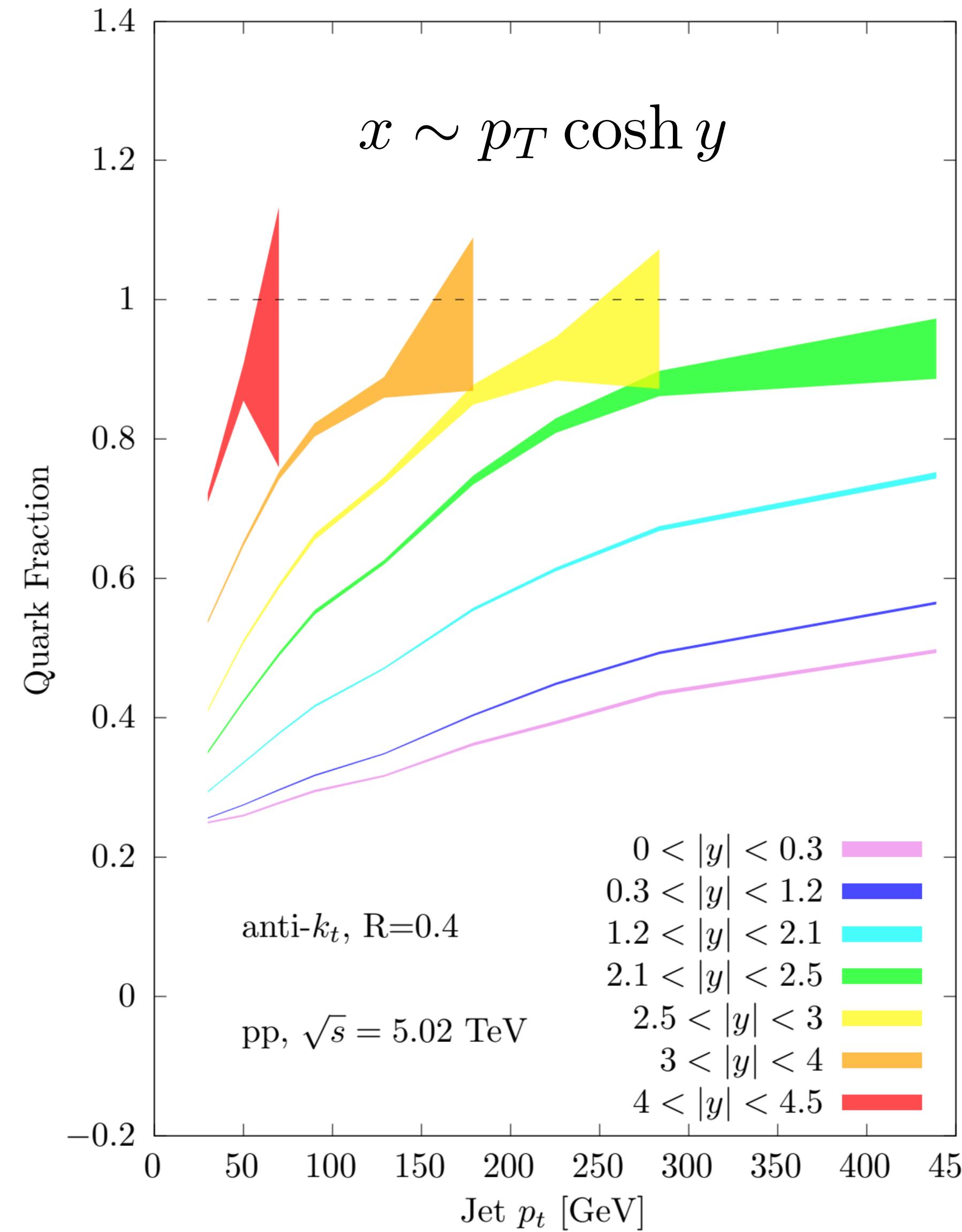
- Quenching of wider jets, either quark or gluon (medium sensitive to jet substructure fluctuations).
- Modification of q/g fraction (medium sensitive to total charge only).

*Simple proposal:*

→ Use an **enriched quark sample**, so that over-quenching of gluons has very little effect.

# Rapidity Evolution of Quark Fraction

DP & A. Soto-Ontoso - PRD '23



- Quark enriched samples can be obtained from e.g. inclusive b-tagged jets, semi-inclusive boson-jets.
- In this work: exploit **rapidity evolution of quark fraction** to engineer quark enriched samples.

*Extended rapidity coverages available in future detector upgrades.*

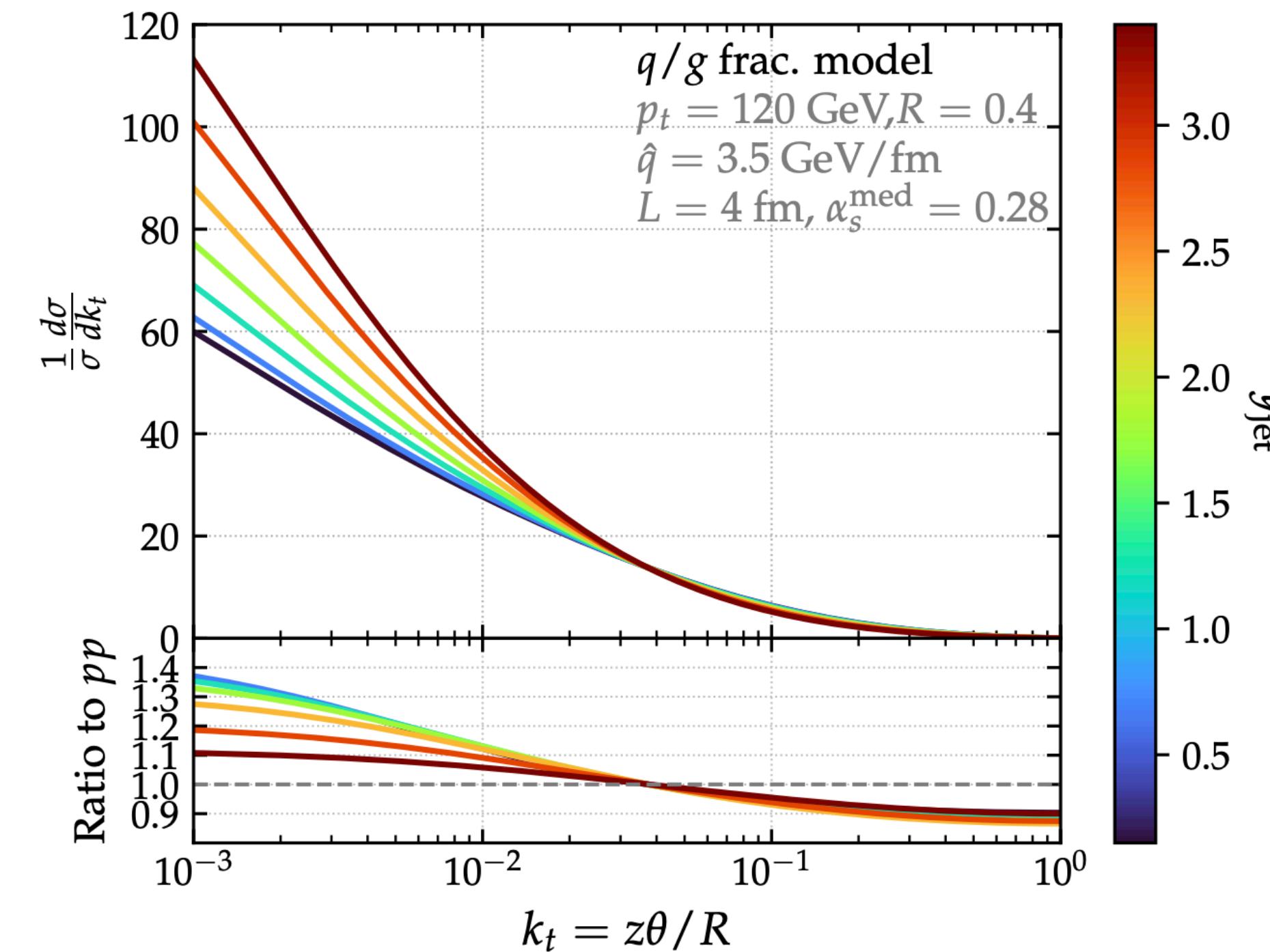


Run 6 with  $|y| < 4$  and great  $p_T$  resolution.

CERN-LHCC-2022-009

Also ATLAS and CMS!

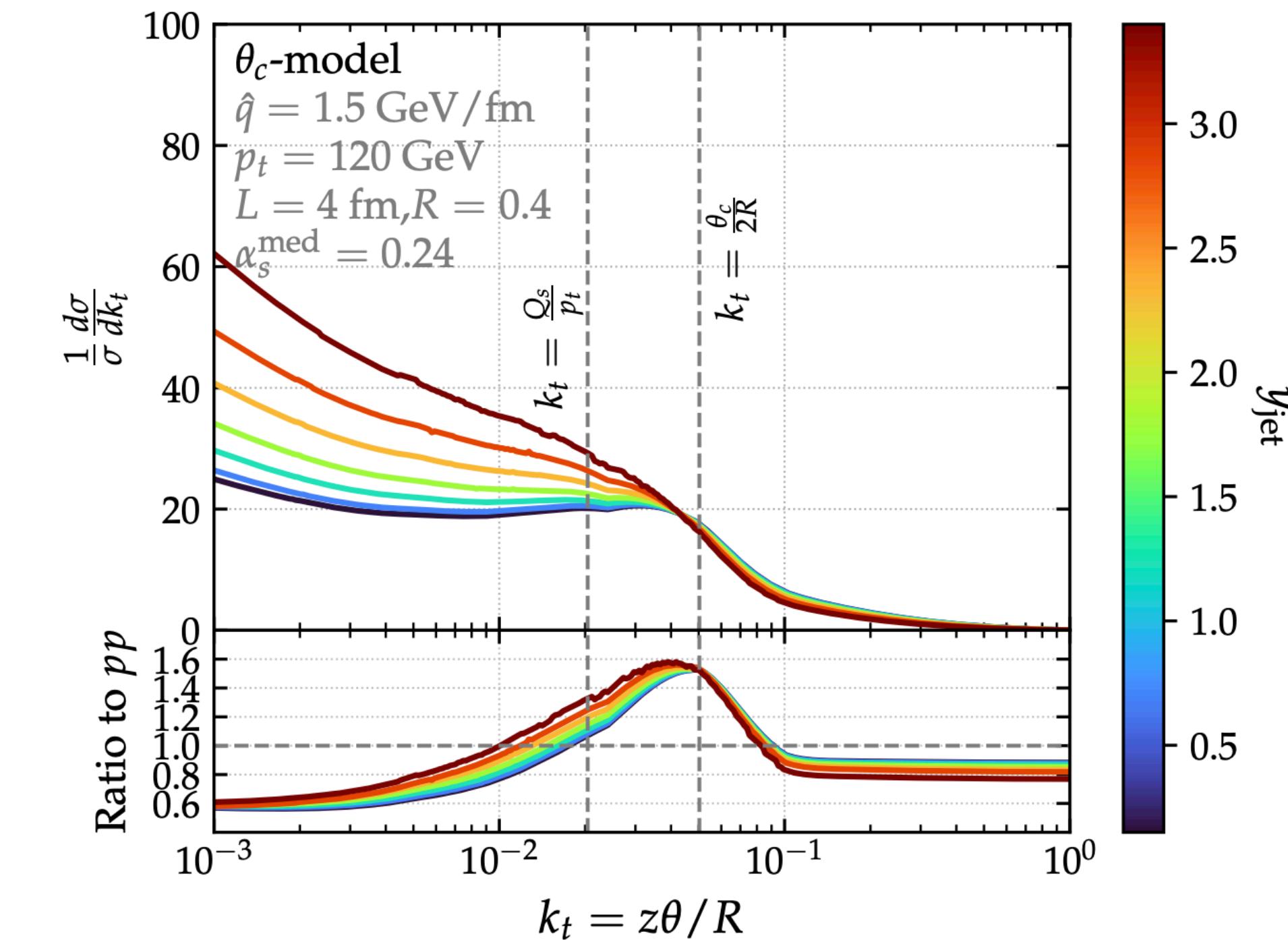
# Analytic Estimates at DLA - Summary



q/g frac model:

→ Quenching of leading charge only.

Less narrowing with increasing rapidity.

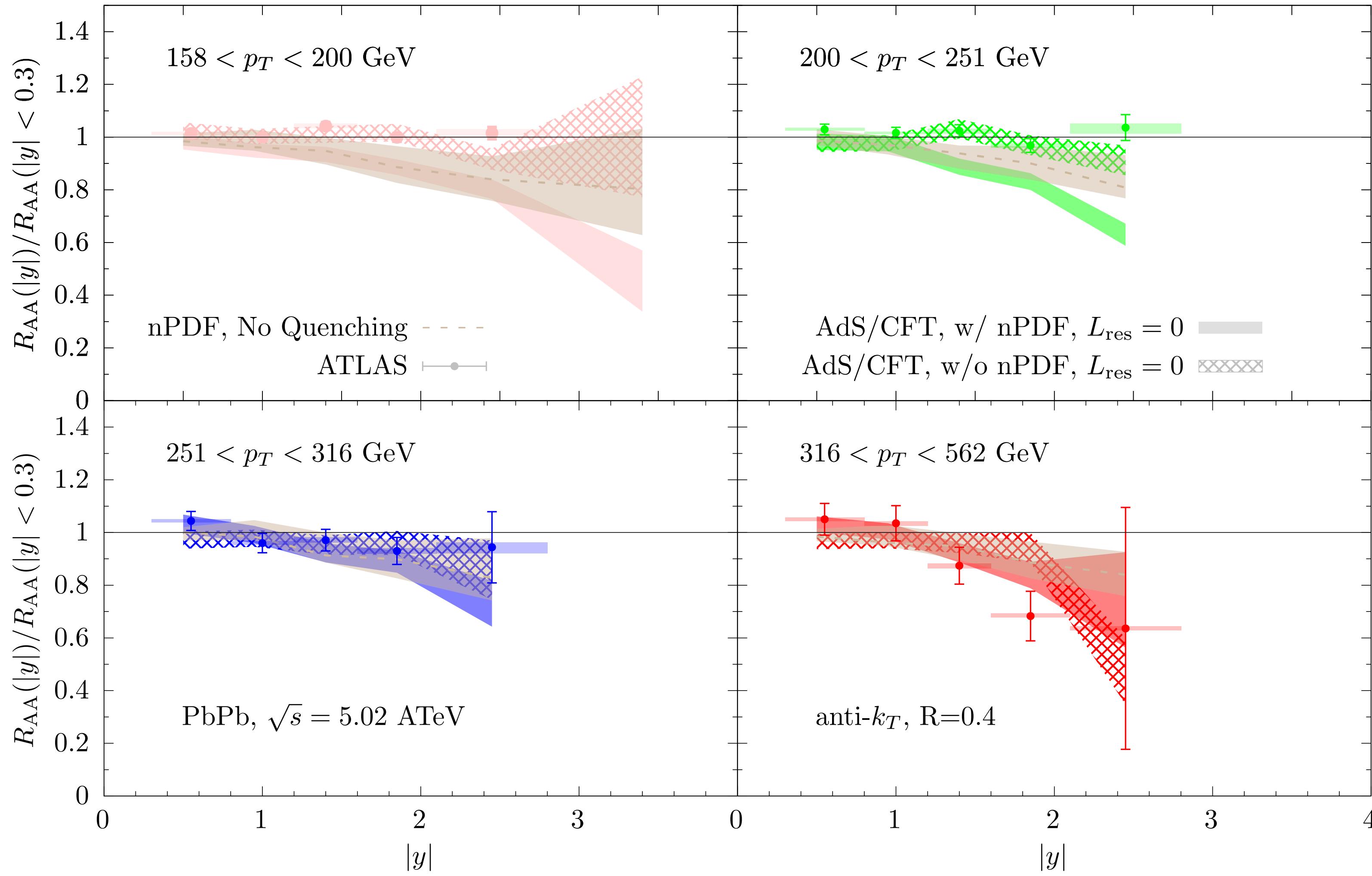


$\theta_c$  model:

→ Quenching of leading and tagged prongs if resolved (i.e. with  $\theta > \theta_c$ ).

Narrowing persists also at forward rapidities.

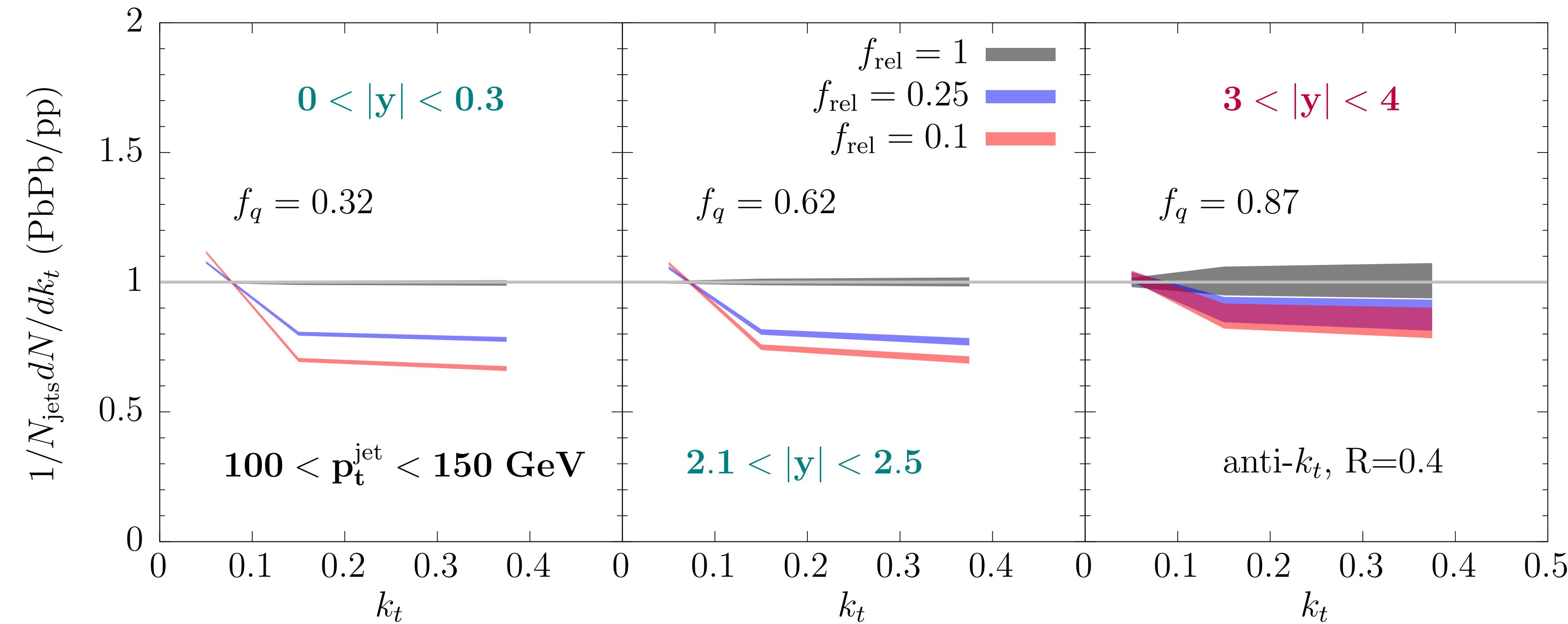
# Rapidity Dependence of $R_{AA}$



- Without nPDF, flatness of  $R_{AA}$  result of competing effects:  
**Steepness of spectrum, change in q-fraction.**
- Initial state effects affect  $R_{AA}$  vs rapidity.  
(Also observed in Adhya et al. - EPJC '22.)
- Need to check with updated sets EPPS21 and nNNPDF3.0.  
Differences among nPDF?  
Could we constrain nPDF?

# Toy q/g Fraction Model

*Using statistics projected for HL-LHC*



**BDMPS-Z:**

$$f_{\text{rel}} = Q_q^{C_A/C_F - 1}$$

$$f_{\text{rel}} \approx 0.5$$

for  $Q_q = 0.6$

$$\frac{1}{\sigma} \frac{d\sigma}{dk_t} \Big|_{AA} = \mathcal{N}^{-1} \left[ f_q \frac{d\sigma_q}{dk_t} \Big|_{pp} + f_{\text{rel}}(1 - f_q) \frac{d\sigma_g}{dk_t} \Big|_{pp} \right]$$

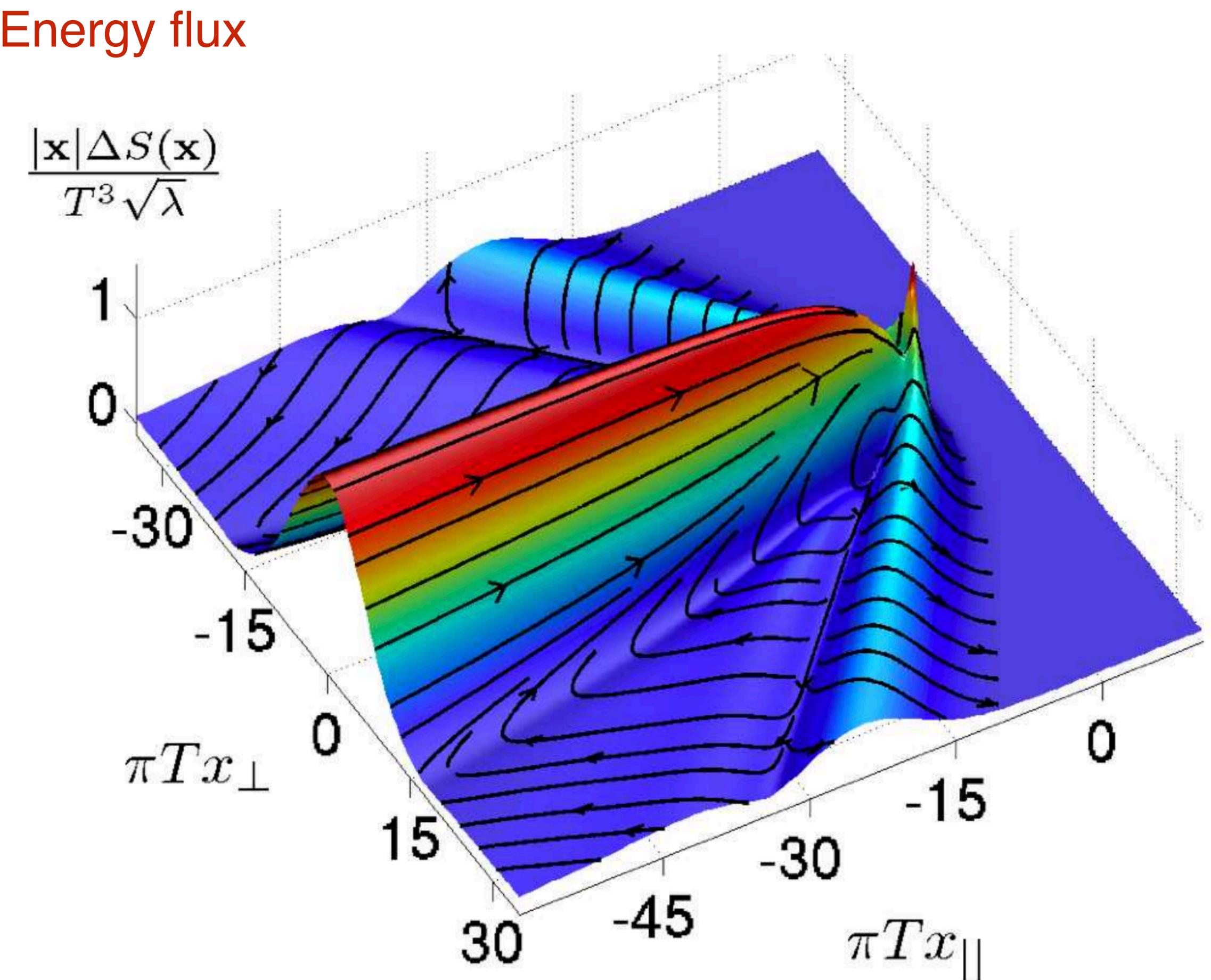
Combine quark and gluon pp templates  
with modified q/g fraction.

- Strong narrowing observed at mid-rapidity fades away toward forward rapidities.

# The Wake of a Quark

- At strong coupling:

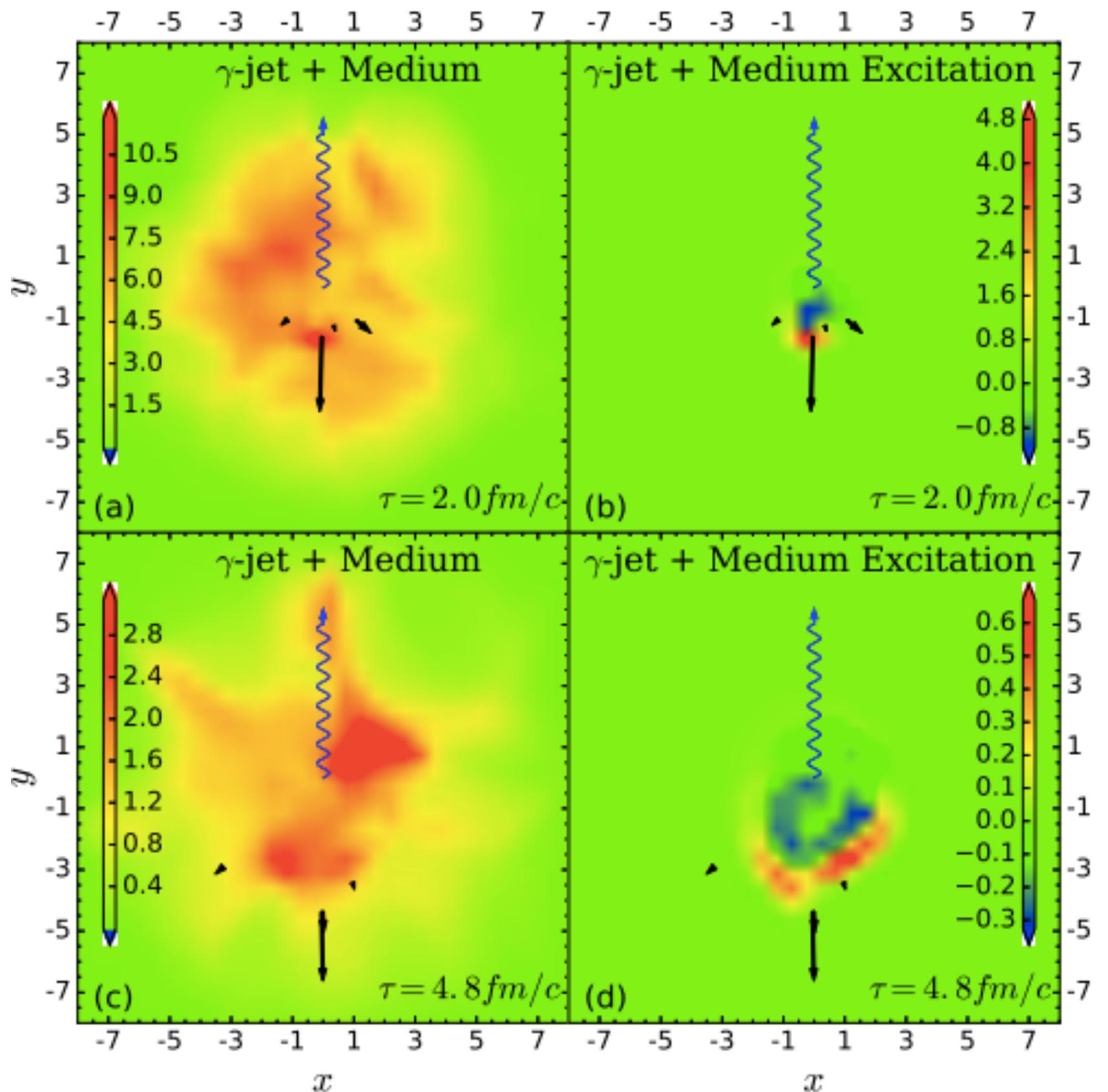
- Modification of stress-energy tensor due to supersonic quark contains sound and diffusive modes.
- Effective source for hydro corresponds to drag force on the quark.
- Agreement between hydrodynamics & wake of a quark even for small distances  $\sim 1/T$ .



*Fulfils Energy-Momentum Conservation  
in the Jet+Plasma Interplay.*

Chesler & Yaffe - [0712.0050](#)

# The Diffusion Wake

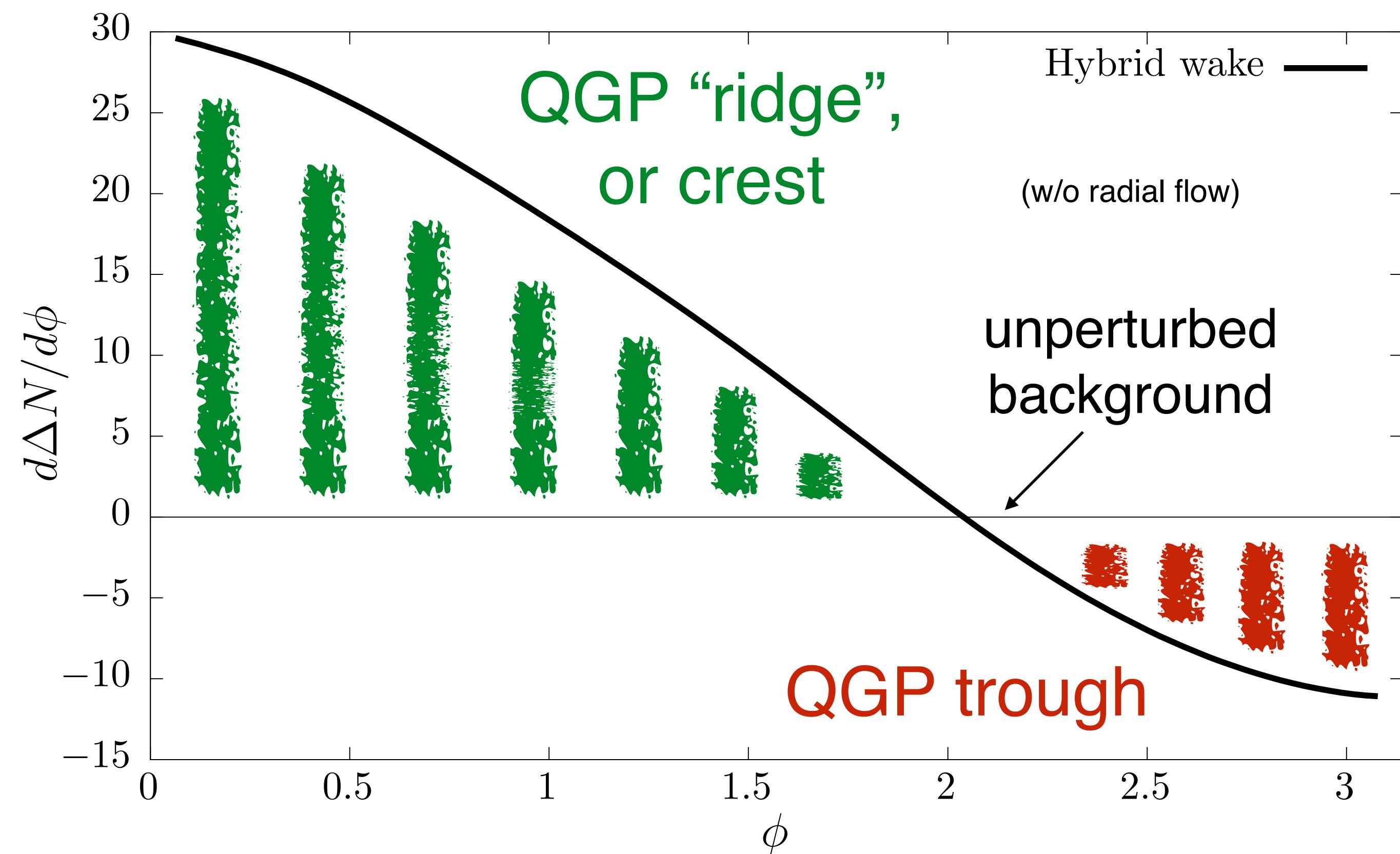


Chen et al. - [1704.03648](#)

Ex: depletion in the away-side  
for boson-jet events with CoLBT model.

QGP trough arises due to the diffusion wake:

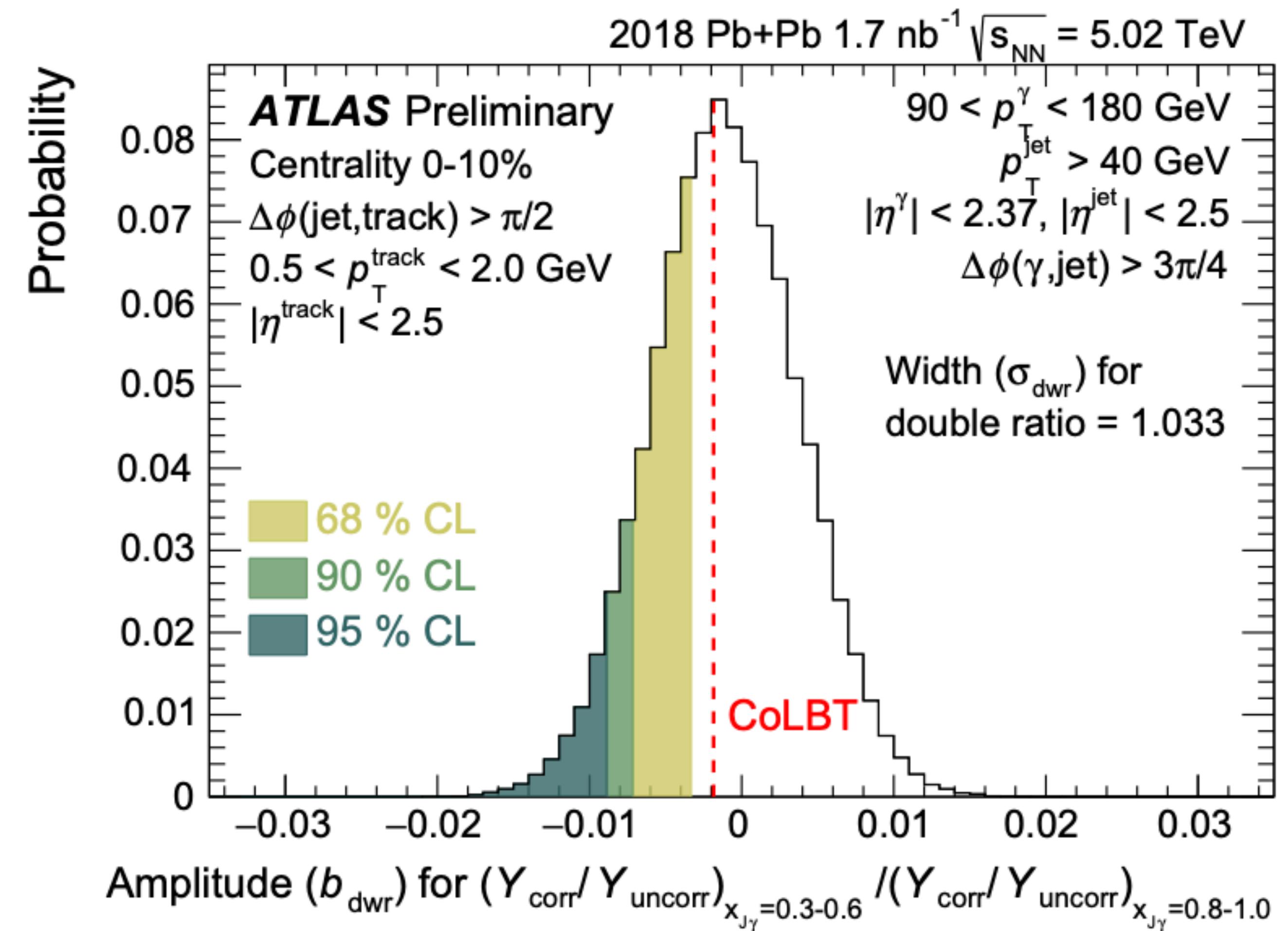
- Depletion of energy density behind the jet (the jet drags the fluid along its direction of propagation, reduces yield of particles in the opposite direction).



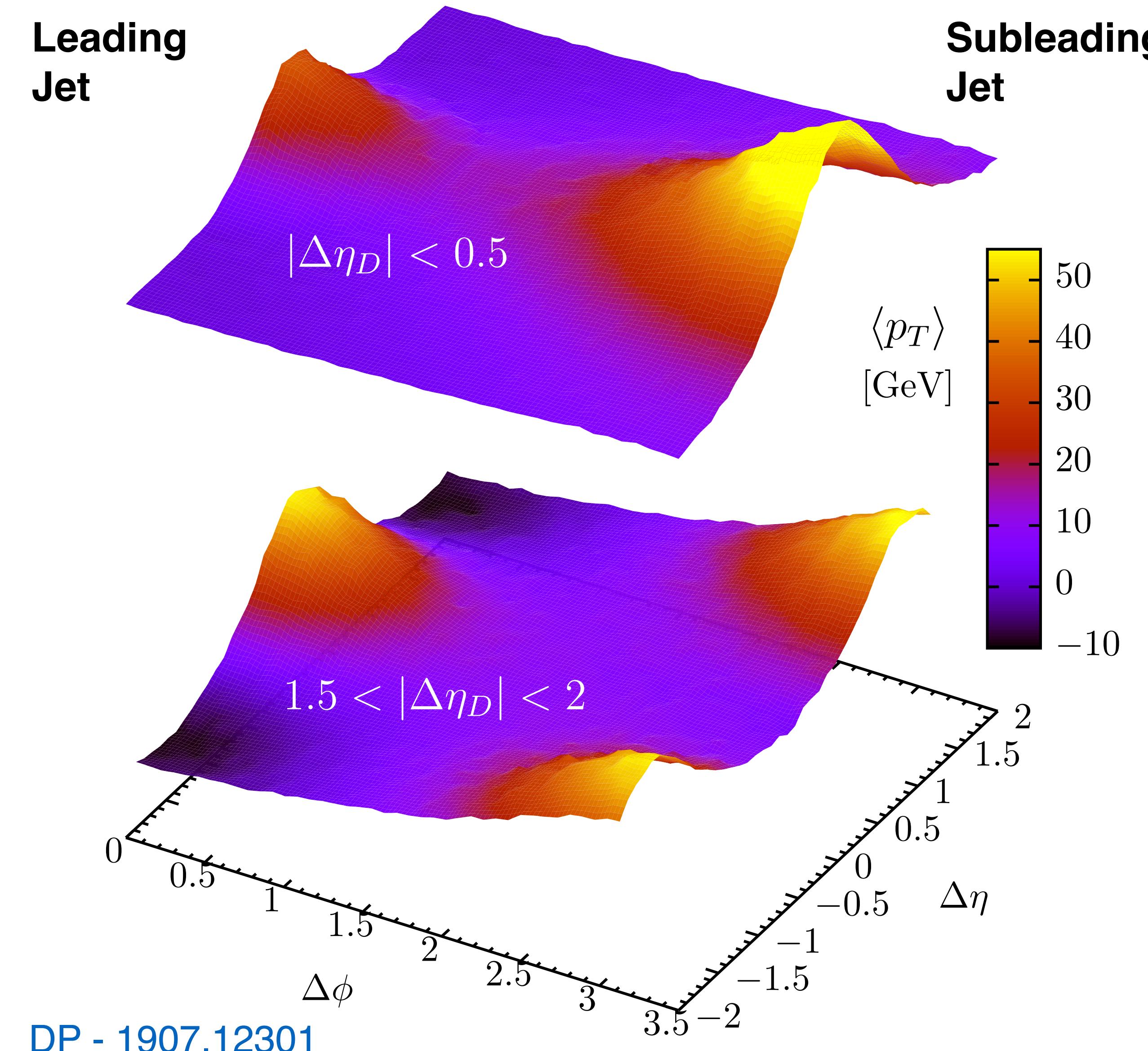
# Looking For the Diffusion Wake

[ATLAS-CONF-2023-054](#)

- No evidence for diffusion wake in recent results from ATLAS.
- 95% CL at 0.8% perturbation on bulk, compatible with CoLBT 0.2% prediction.
- Statistics will be improved in Run 3.



# The Effect of the Recoiling Jet



$\langle p_T \rangle$  density of wake hadrons  
w.r.t leading jet axis.

*Aligned in rapidity*

Subleading jet's **QGP trough**  
**hits leading jet.**

*Separated in rapidity*

Subleading jet's **QGP trough**  
**misses leading jet.**

$$\begin{aligned} p_T^L &> 250 \text{ GeV} \\ p_T^S &> 80 \text{ GeV} \\ \Delta\phi_D &> 2\pi/3 \end{aligned}$$

differential in  
 $|\eta_D| \equiv |\eta_L - \eta_S|$

# Leading Jet Suppression vs. $|\eta_{DL}|$

DP - 1907.12301

*A new observable.*

**R = 0.4**

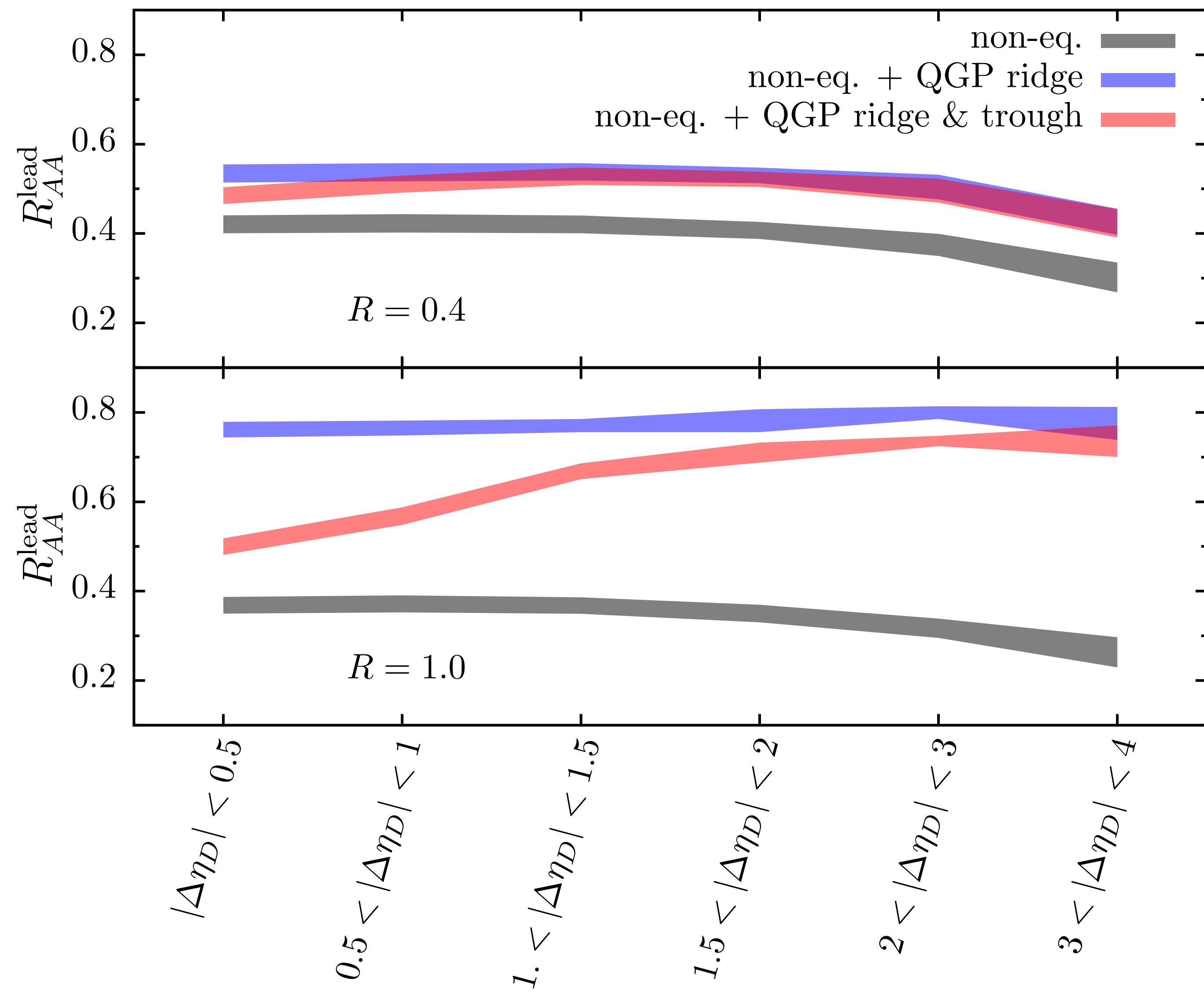
leading jet area easy to miss;  
small effect from QGP trough.

**R = 1.0**

strong dependence on  $|\eta_{DL}|$ ;  
knee visible when  $|\eta_{DL}| \sim R$ .

$p_T^L > 250$  GeV  
 $p_T^S > 80$  GeV  
 $\Delta\phi_D > 2\pi/3$

differential in  
 $|\eta_D| \equiv |\eta_L - \eta_S|$



# Leading Jet Suppression vs. $|\eta_{DL}|$

Benefits of the strategy:

- Much higher stats for inclusive jets compared to boson-jets.
- Can reach higher  $p_T$ , larger wake effects.
- Many systematics cancelled in ratios between different  $|\eta_{DL}|$ .

Also: replace subleading jet by high- $p_T$  hadron (just need an axis!).

# Jet Suppression: Framework

- Use microjet distributions derived using Generating Functional (GF) framework:

Vacuum evol.  
obeys DGLAP:

$$\frac{df_{j/i}^{\text{incl}}(z, t)}{dt} = \sum_k \int_z^1 \frac{dz'}{z'} P_{jk}(z') f_{k/i}^{\text{incl}}(z/z', t)$$

Dasgupta et al. - JHEP '14

- Extend GF in the medium to resum energy loss effects due to multi-particle nature of jet:

$$\begin{aligned} \frac{\partial Q_i(p, \theta)}{\partial \ln \theta} &= \int_0^1 dz \frac{\alpha_s(k_\perp)}{2\pi} p_{ji}^{(k)}(z) \Theta_{\text{res}}(z, \theta) \\ &\times [Q_j(zp, \theta)Q_k((1-z)p, \theta) - Q_i(p, \theta)] \end{aligned}$$

**PS<sub>in</sub> constraint**

Initial condition at zero angle  
is single charge quenching factor:

$$Q_i(p, 0) = Q_{\text{rad}, i}^{(0)}(p_T) Q_{\text{el}, i}^{(0)}(p_T)$$

Radiative  
energy loss

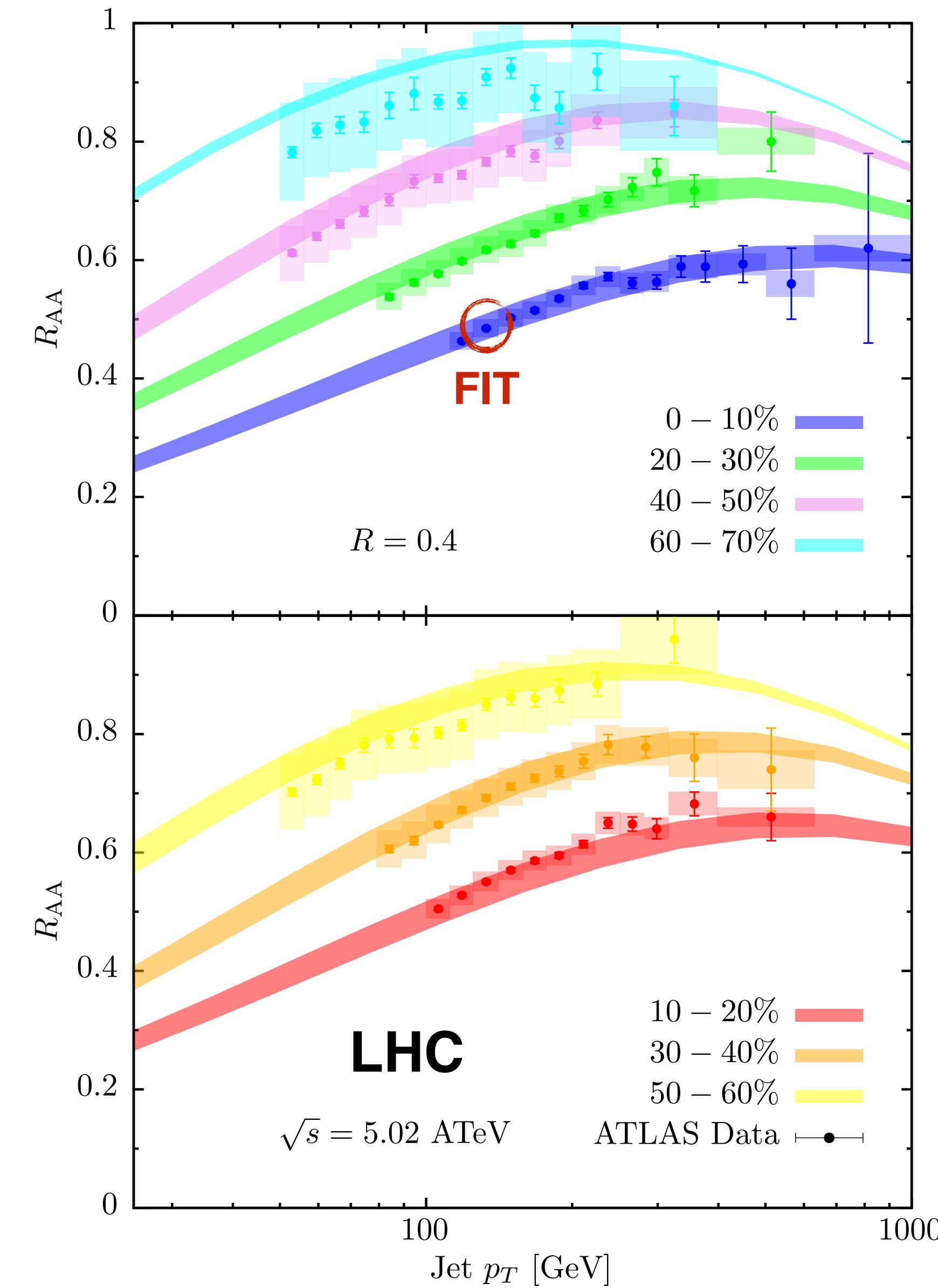
Elastic  
energy loss

- Energy loss versus R displays non-monotonic behaviour. Competing effects:

- Increasing R means more likely to retain emitted (or thermalised) quanta: **less quenching**.
- Increasing R means larger quenched phase space: **more quenching**.

Mehtar-Tani, DP, Tywoniuk - PRL '21

# Jet Suppression at LHC



- Modelling sensitivity at  $p_T=110 \text{ GeV}$  for  $\mathbf{R}$  between **0.2 and 0.6**:

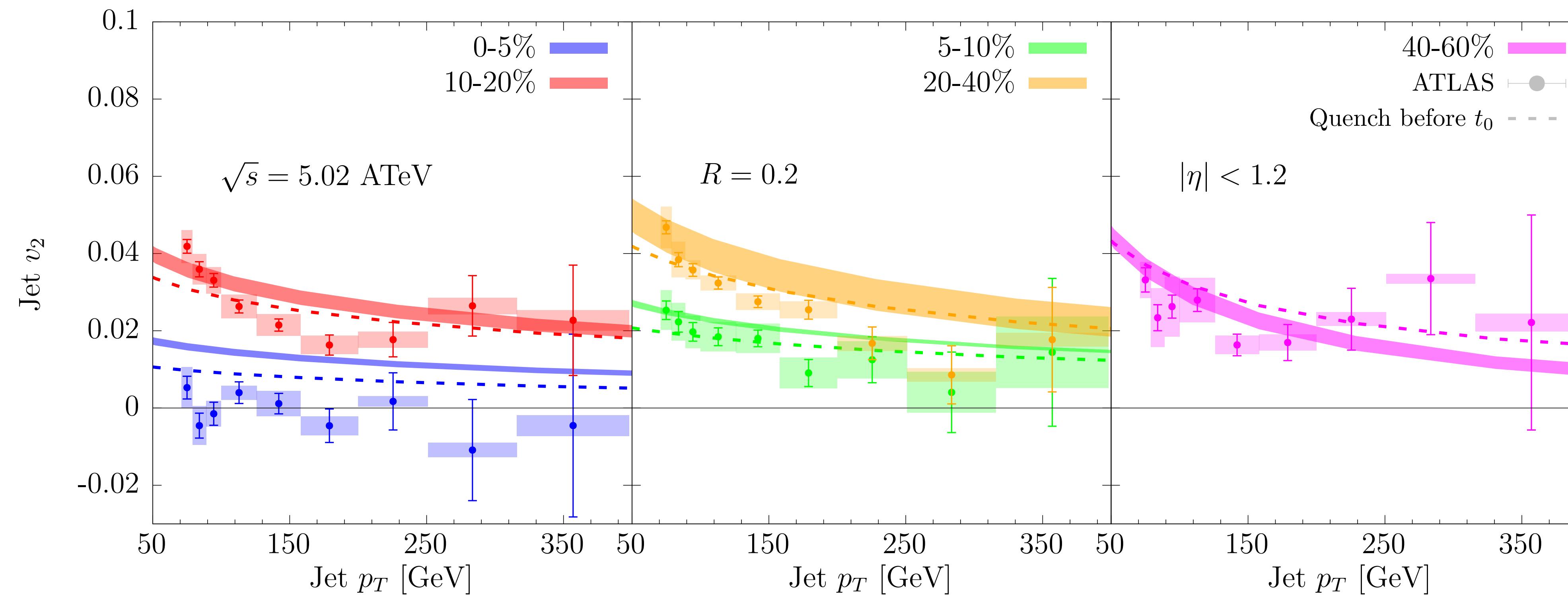
Parameter	Variation	Effect
$\theta_c$	$[\theta_c/2, 2\theta_c]$	$\lesssim 20\%$
IOE	LO/NLO	$\sim 2\%$
$n$	$\pm 1$	$\sim 10\%$
$R_{rec}$	$[1, \infty]$	$\lesssim 10\%$
$\omega_s$	$[\omega_s/2, 2\omega_s]$	$\lesssim 8\%$

- NLO contribution very small (hard emissions tend to be collinear).
  - Modelling of fate of lost energy relatively small.
  - Determination of quenched phase space relatively large. Improvable in pQCD.
- Need to improve perturbative sector before non-perturbative becomes relevant (for  $R < 0.6$ !)

Mehtar-Tani, DP,  
Tywoniuk - PRL '21

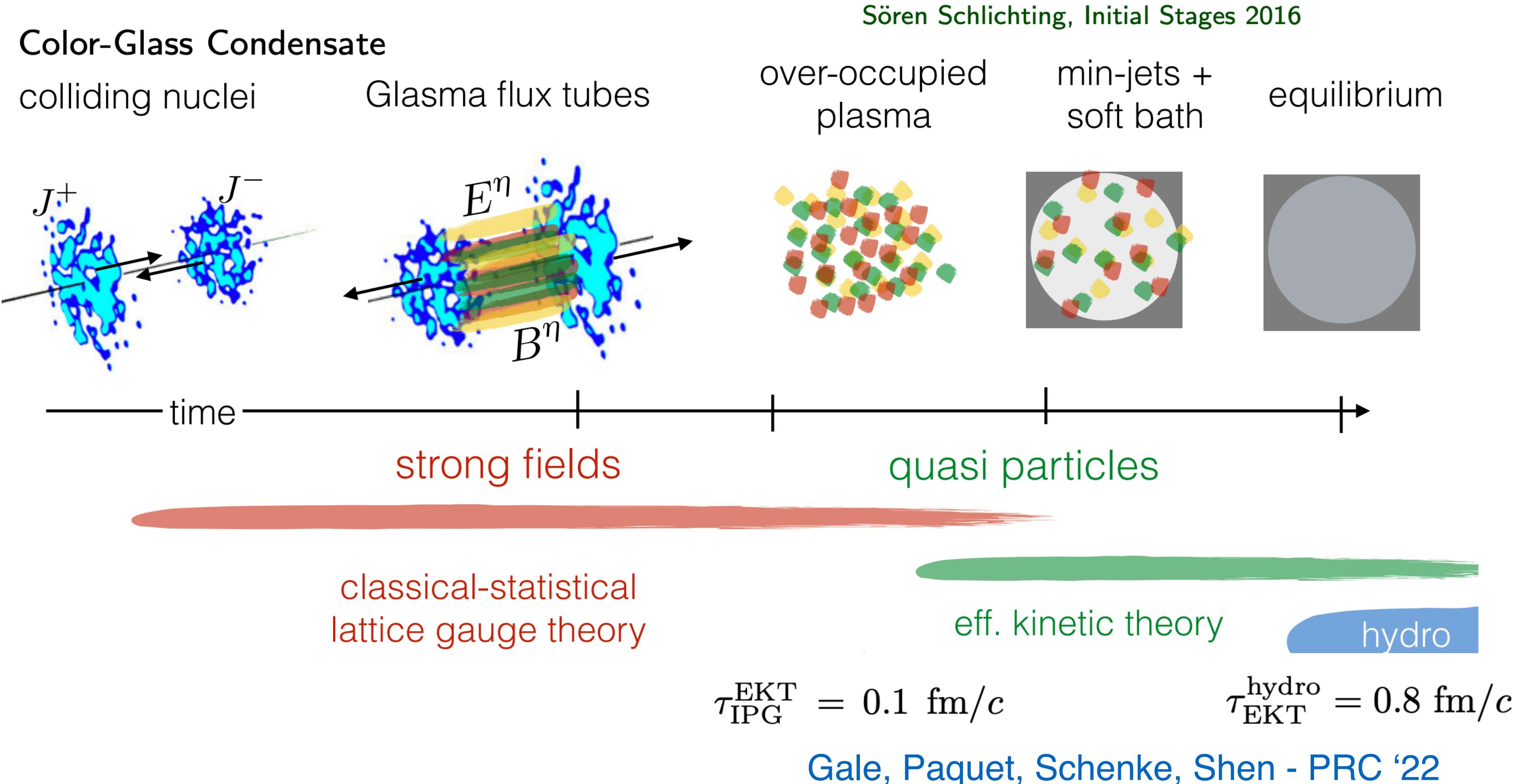
# Jet Azimuthal Anisotropy at LHC

Mehtar-Tani, DP,  
Tywoniuk - in preparation



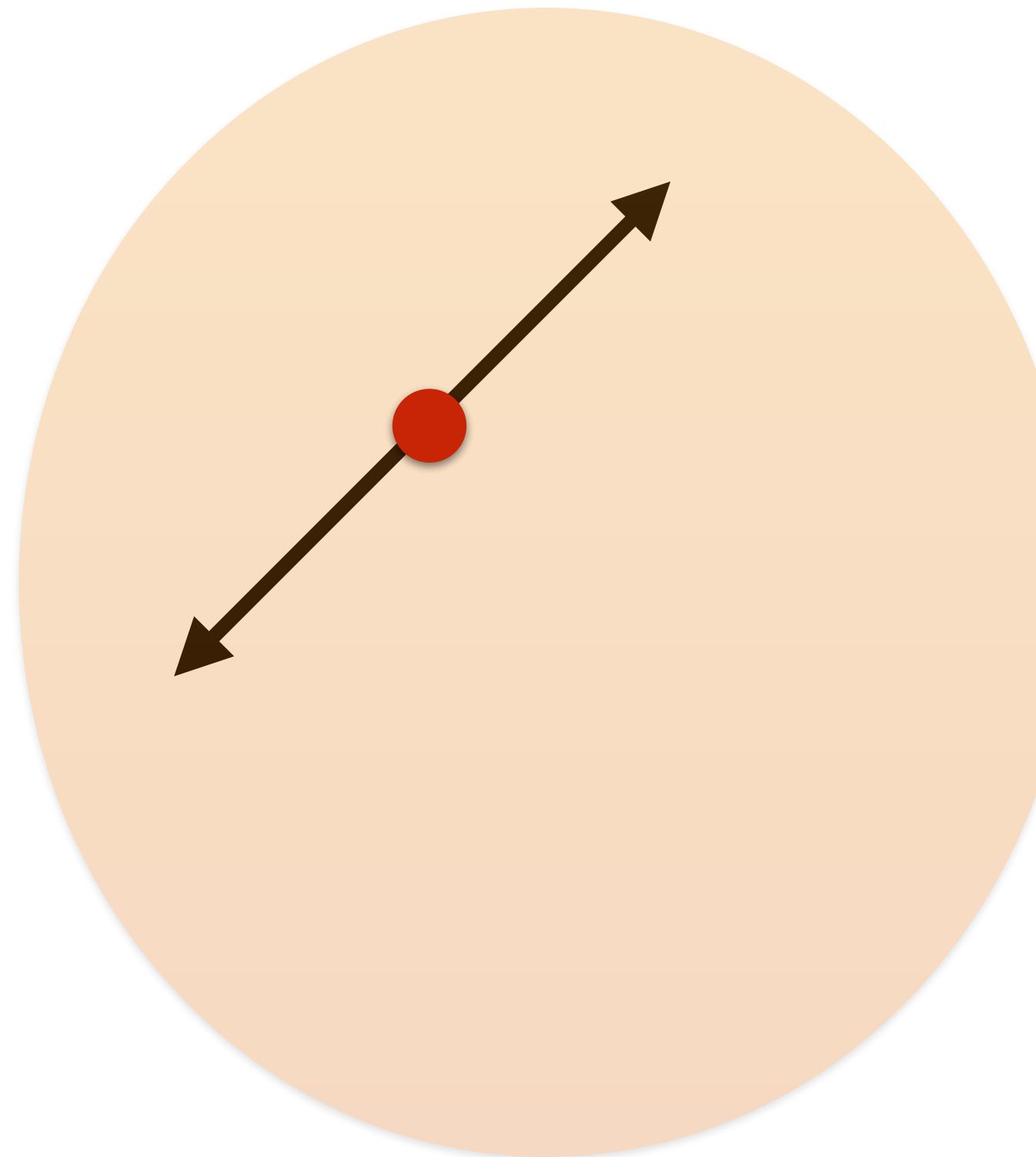
- First analytical description of jet  $v_2$ .
- Sensitivity of jet  $v_2$  to non-equilibrium stage.

# Current Perspective on Early Times



- Bulk of the system assumed to be produced with momenta  $p \sim Q_s \sim 2 \text{ GeV}$ .
- Effective description switches at a fixed time.

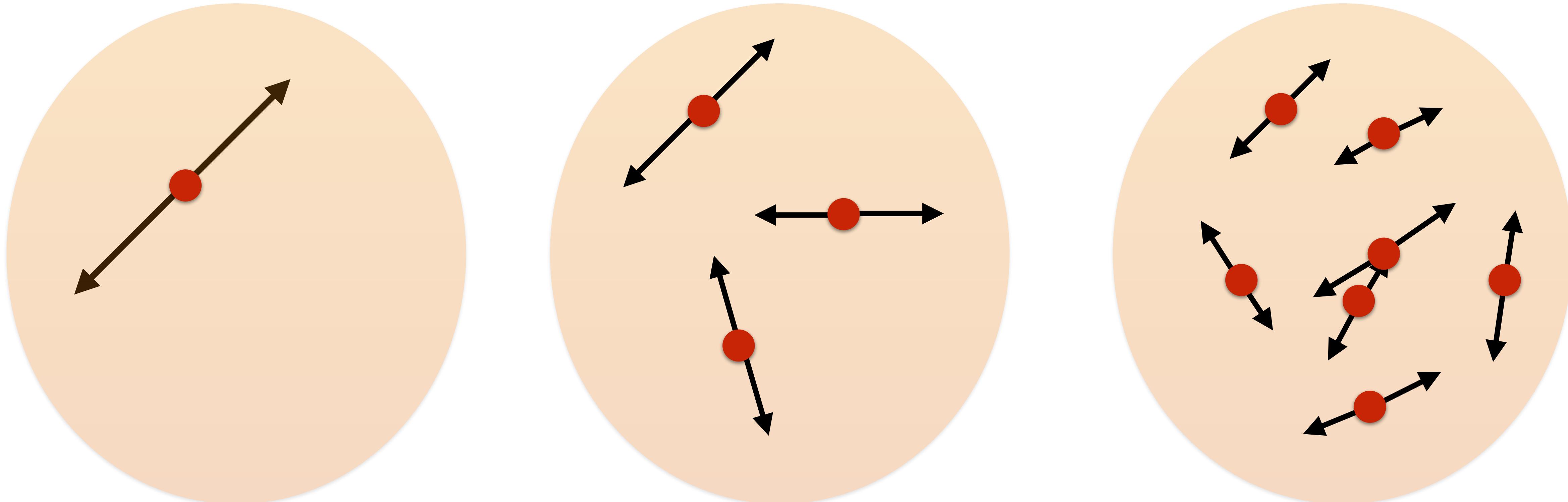
# Mini-Jets in Heavy-ions



- Consider particle production with  $p > Q_s$ .
    - Perturbative process.
    - Production probability proportional to  $N_{\text{coll}}$ .
    - Can split and produce color coherent objects.
    - Random orientation in transverse plane and rapidity.
- Mini-jets are an additional source of fluctuations.*

For  $p_T \sim 20$  GeV, one or zero dijet pair produced at central collisions at LHC...

# Mini-Jets in Heavy-ions



→ As we consider lower  $p_T$ , mini-jet production becomes increasingly abundant.

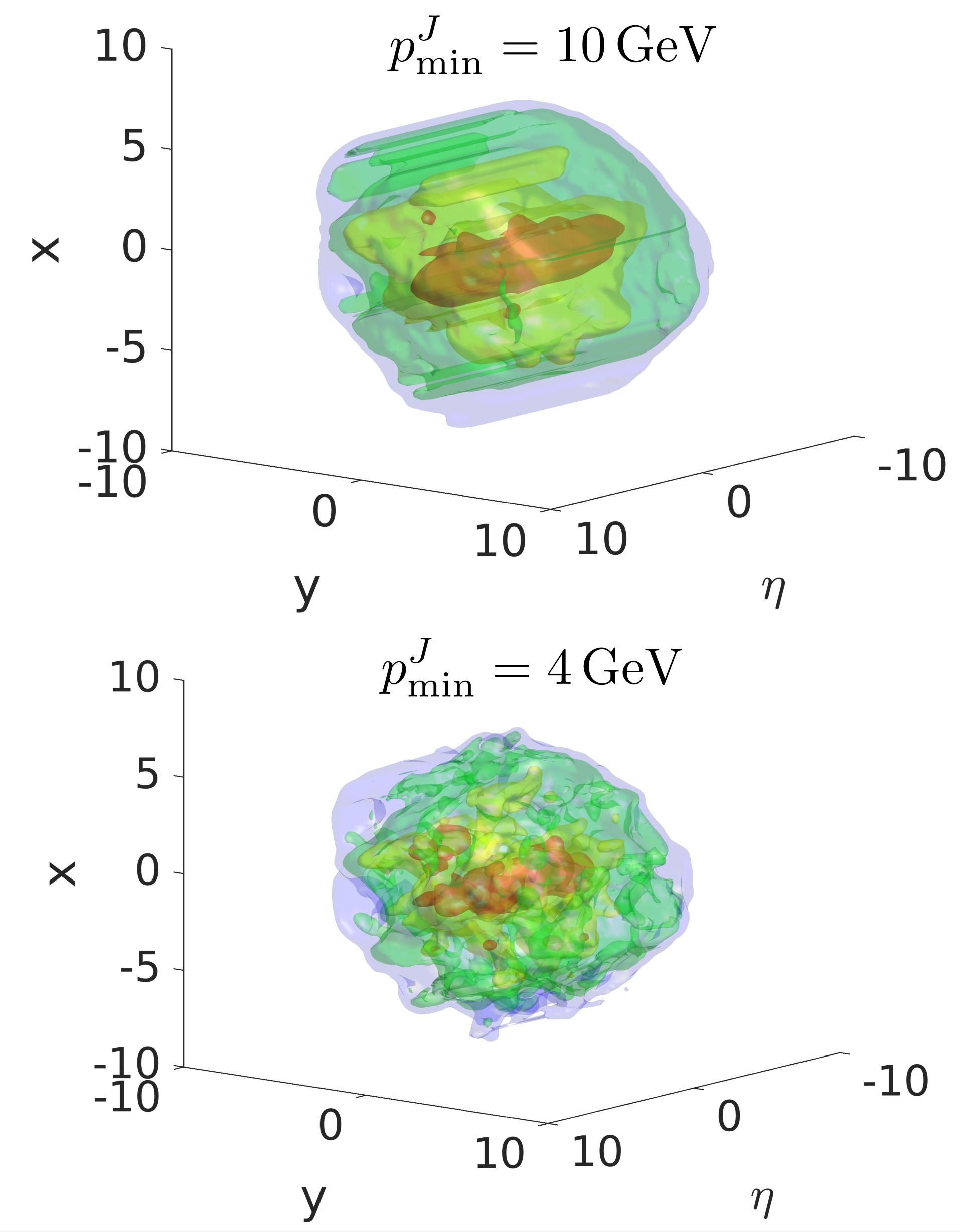
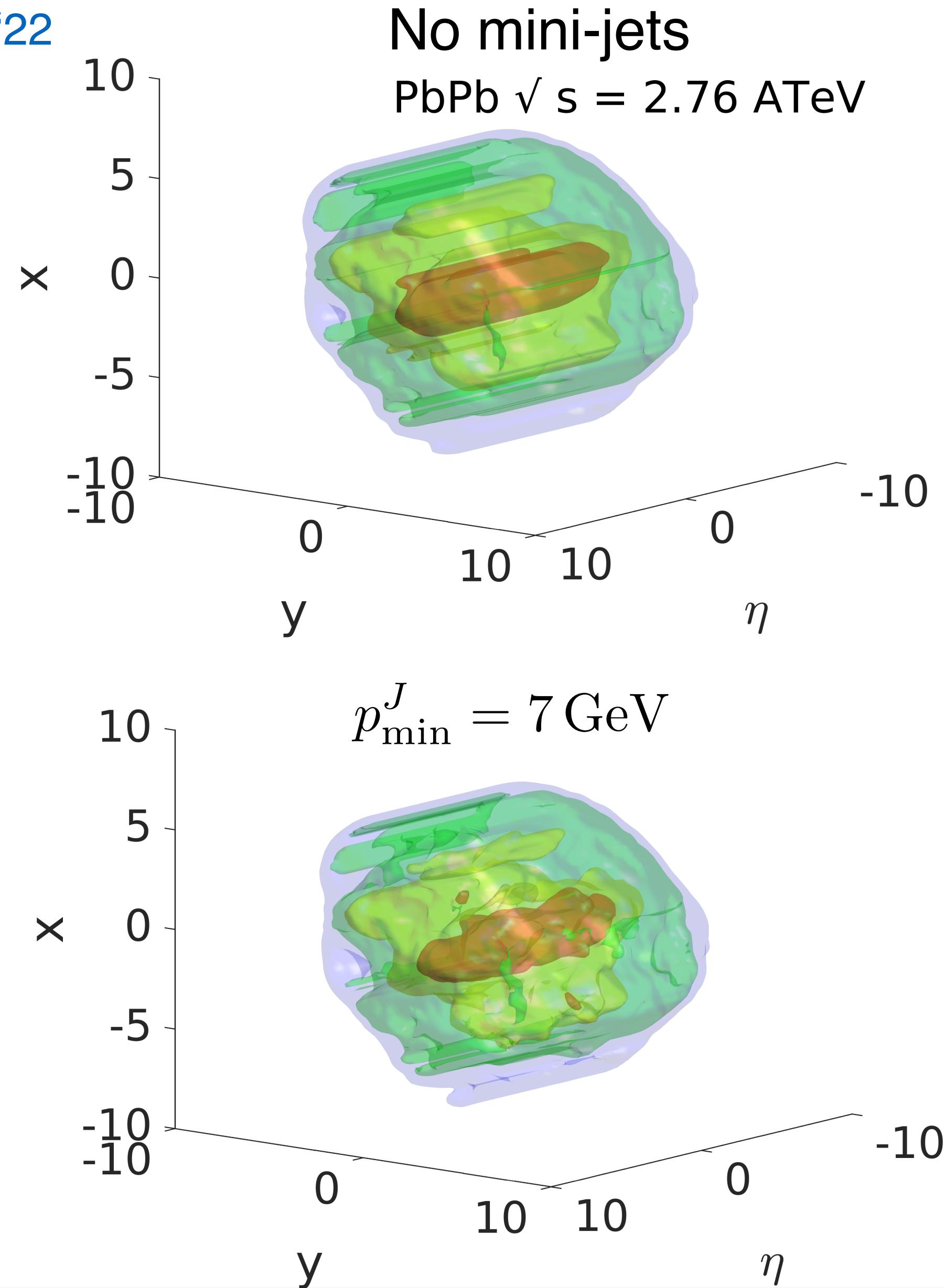
# A Spikier Evolution

DP, Singh, Gale, Jeon - PRC '22

3D isotherms at temperatures  
220 MeV (red),  
195 MeV (yellow),  
170 MeV (green)  
and 145 MeV (blue).

$\tau = 3.4 \text{ fm}/c$

40-50% Centrality



# Minimal Tuning

DP, Singh, Gale, Jeon - PRC '22

- To describe multiplicity, tune down amount of energy attributed to IP-Glasma ( $S_{\text{factor}}$ ), for each  $p_{\min}^J$ :

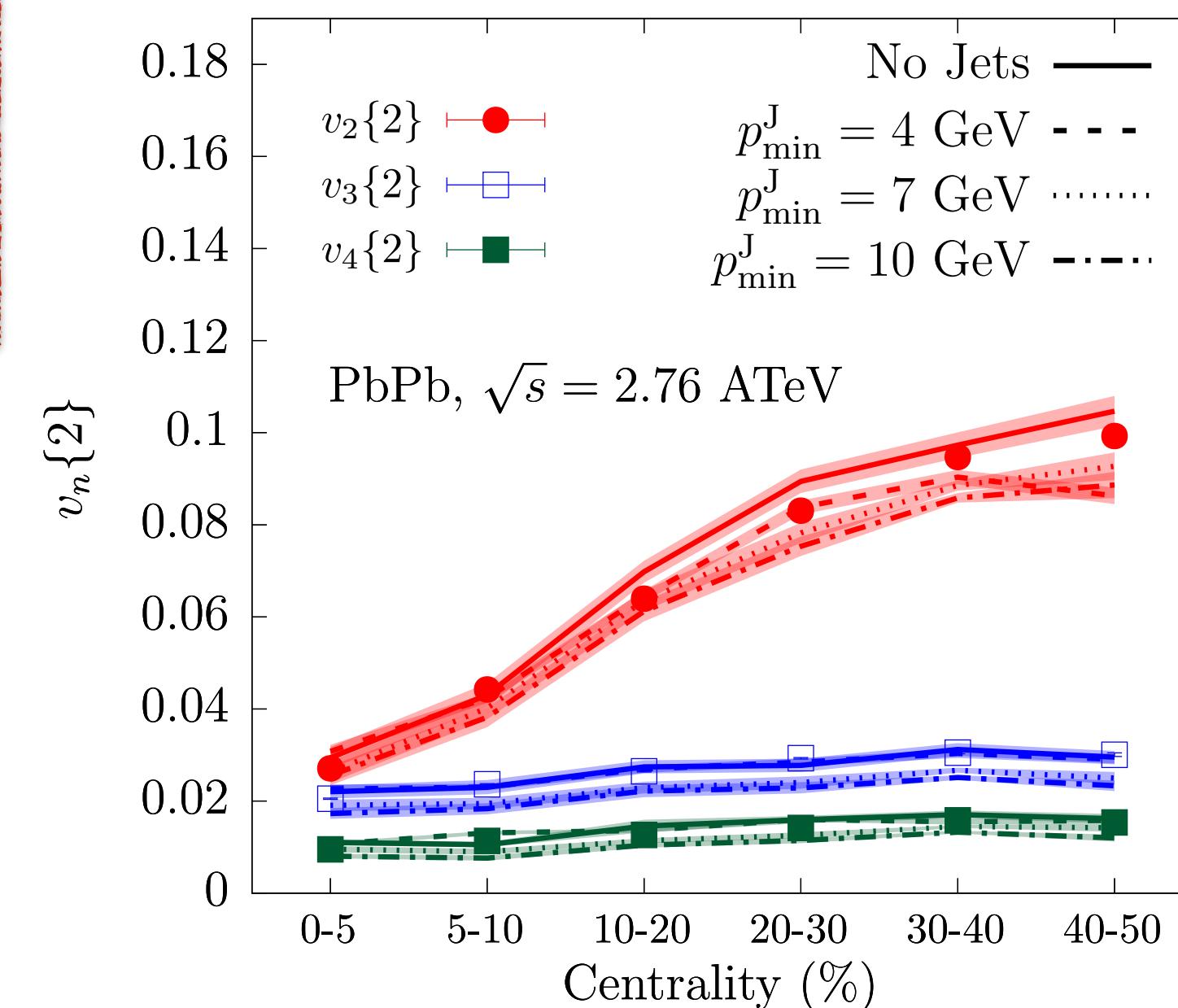
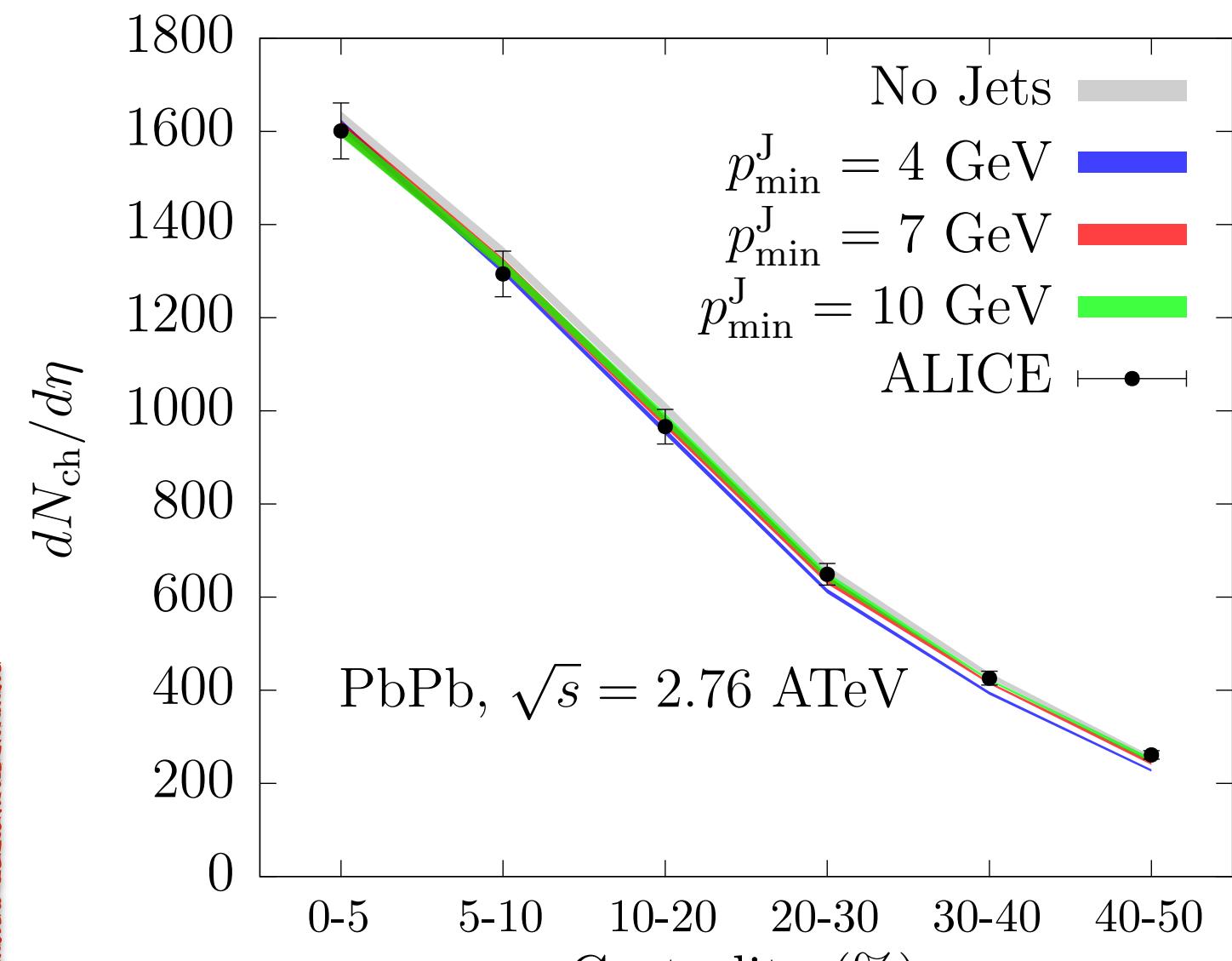
→ Single choice of  $S_{\text{factor}}$  works for all centralities.

$p_{\min}^J$	$S_{\text{factor}}$	$\eta/s$
4 GeV	0.45	0.02
7 GeV	0.82	0.1
10 GeV	0.9	0.125
No Jets	0.915	0.13

- Mini-jet orientation is decorrelated with energy gradients at  $\tau_{\text{hydro}}$ , reducing overall flow:

→ Need to recalibrate (constant)  $\eta/s$  to accommodate integrated and differential flow coeffs.

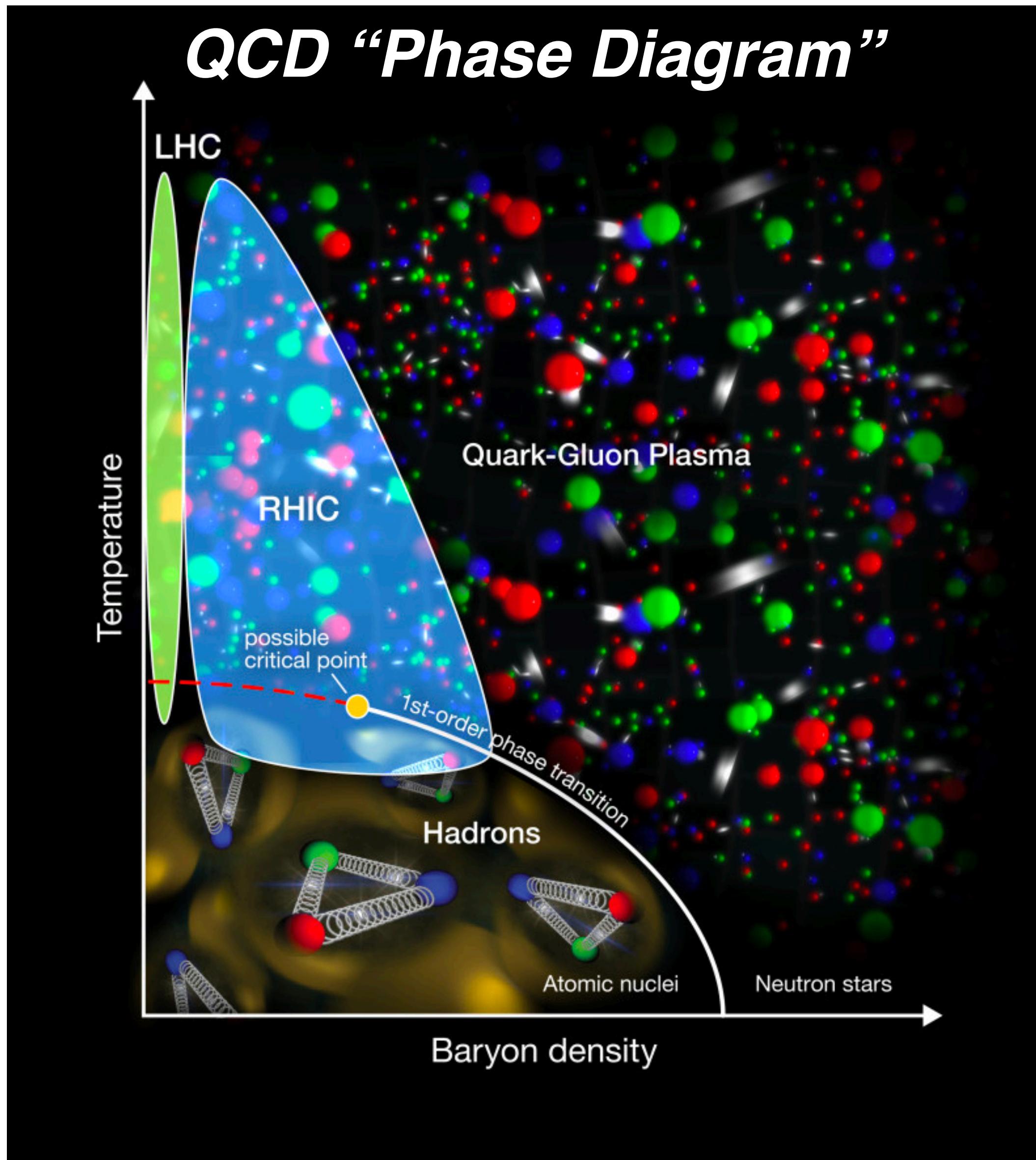
see also: Schulc & Tomasic - PRC '14  
Okai et al. - PRC '17



# My Fellini

- Have enjoyed complete independence
  - Mini-jets (McGill, Vanderbilt)
  - Linearized Hydro (MIT, UB, INT)
  - Analytical jet suppression (Bergen U., BNL)
  - Moliere scatterings in QGP (MIT, Stanford)
  - Rapidity dependence (CERN)
  - Heavy quarks in small syst. (INFN Torino)
  - Perturbative splittings in HI (CERN, Heidelberg)
- 7 talks at Hard Probes '23, 5 talks at Quark Matter '23, ***plenary*** at Quark Matter '23.
  - Invited by ALICE, PHENIX, STAR for jet theory talks several times.
- Secondment institution: Oviedo U.
  - Working with student on antenna scatterings.
  - Working with host supervisor on holographic energy loss.
- Now moving to Santiago for postdoc. Wish me luck.

## *QCD “Phase Diagram”*



**Thanks for your  
attention!**

**e Buon Natale!**



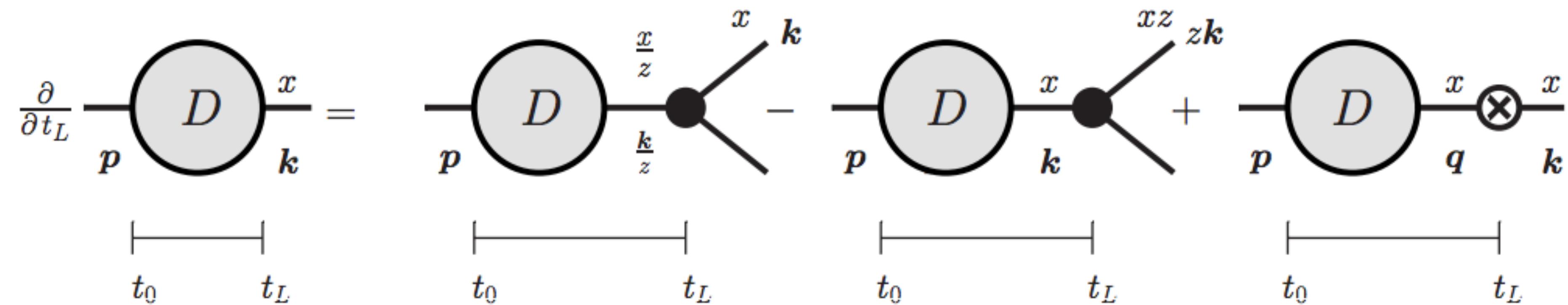
# Backup Slides

# Parton Energy Loss

pQCD

High energy partons in the QGP:

- emit quanta, which in turn emit more quanta, and should (eventually) hydrodynamize.



$D(x, \mathbf{k}, t)$  is one-gluon distribution.

Blaizot et al. - JHEP '13 & '14, PRL '13

- Turbulent cascade develops, with a sink at  $E \sim T$ .
- Necessary length to reach the turbulent regime?

# Radiative Energy Loss

- Framework: Light-Cone Perturbation Theory.
- Integrated medium induced spectrum:

$$\omega \frac{dI}{d\omega} = \frac{\alpha_s C_R}{\omega^2} \int_0^\infty dt_2 \int_0^{t_2} dt_1 \partial_{\mathbf{x}} \cdot \partial_{\mathbf{y}} [\mathcal{K}(\mathbf{x}, t_2 | \mathbf{y}, t_1) - \mathcal{K}_0(\mathbf{x}, t_2 | \mathbf{y}, t_1)]_{\mathbf{x}=\mathbf{y}=0}$$

- Resummed propagator due to multiple interactions with the medium satisfies 2D Schrödinger-like equation:

$$\left[ i\partial_t + \frac{\partial^2}{2\omega^2} + iv(\mathbf{x}) \right] \mathcal{K}(\mathbf{x}, t_2 | \mathbf{y}, t_1) = i\delta(\mathbf{x} - \mathbf{y})\delta(t_2 - t_1)$$

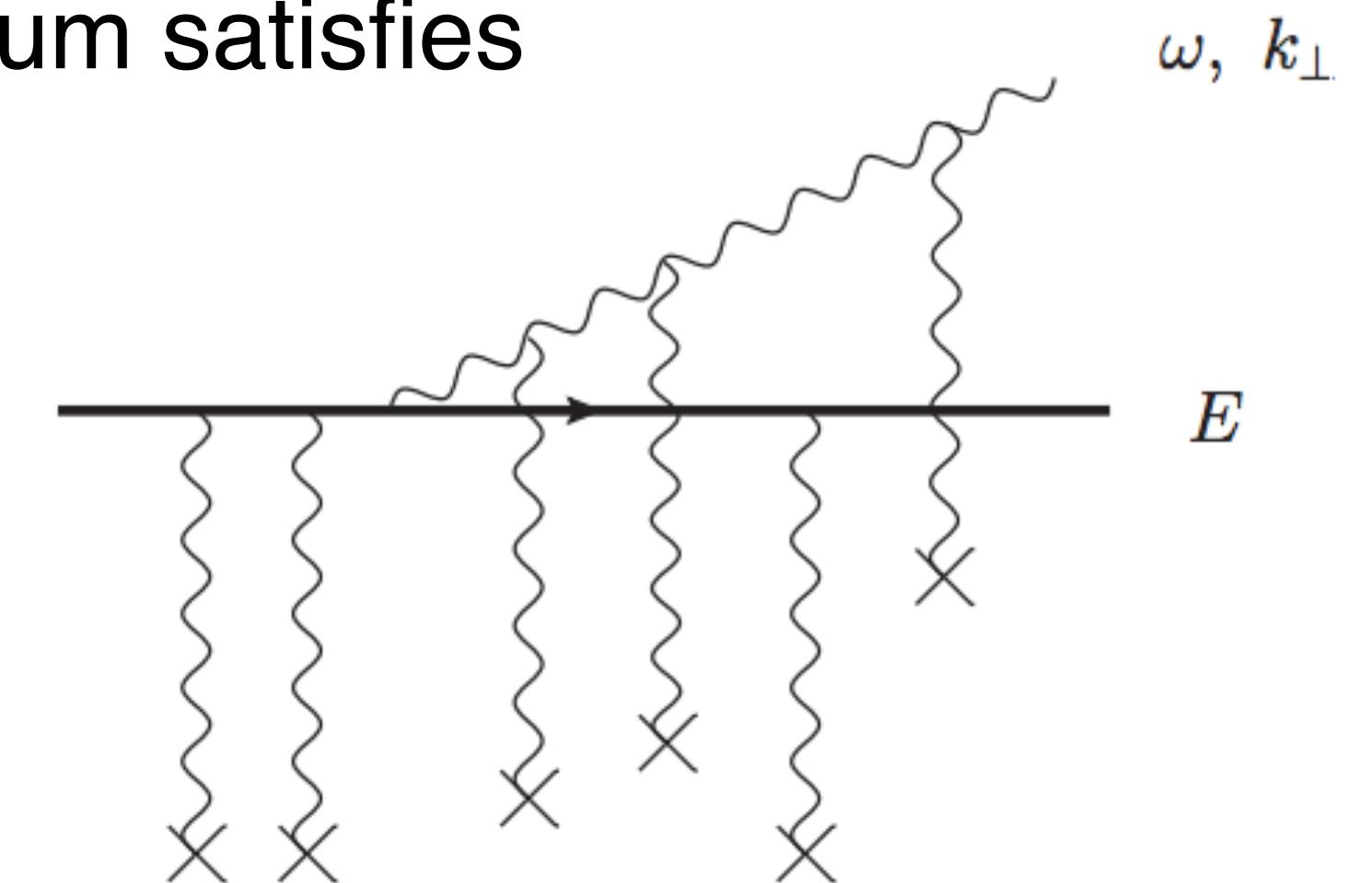
- With potential:  $v(\mathbf{x}, t) = C_A \int_{\mathbf{k}} \frac{d^2\sigma}{d^2\mathbf{k}} (1 - e^{i\mathbf{k}\cdot\mathbf{x}})$   
and scattering cross-section:

Hard Thermal Loop:

$$\left( \frac{d^2\sigma}{d^2\mathbf{q}} \right)^{\text{HTL}} = \frac{g^2 m_D^2 T}{\mathbf{q}^2 (\mathbf{q}^2 + m_D^2)}$$

Gyulassy-Wang:

$$\left( \frac{d^2\sigma}{d^2\mathbf{q}} \right)^{\text{GW}} = \frac{g^4 n(t)}{(\mathbf{q}^2 + \mu^2)^2}$$



Mehtar-Tani - JHEP '19

# Usual Approximations of the Spectrum

- Dilute medium: expand to leading order in  $v(\mathbf{x})$  (N=1 opacity expansion):

$$\omega \frac{dI_{\text{GLV}}}{d\omega} = 32\pi \alpha_s C_R \hat{q}_0 \int_0^L ds \int_{\mathbf{p}, \mathbf{q}} \frac{\mathbf{p} \cdot \mathbf{q}}{\mathbf{p}^2 (\mathbf{p} - \mathbf{q})^2 (\mathbf{q}^2 + \mu^2)^2} \left\{ 1 - \cos \left[ \frac{(\mathbf{p} - \mathbf{q})^2}{2\omega} s \right] \right\}$$

Gyulassy-Levai-Vitev spectrum

Wiedemann - NPB '00

Single hard scattering, preserves full form of potential.

Gyulassy, Levai, Vitev - NPB '00

Wang, Guo - NPA '01

Majumder - PRD '12

Sievert, Vitev, Yoon - PLB '19

- Harmonic oscillator (diffusion) approximation:

$$v(\mathbf{x}, t) = C_A \int_{\mathbf{k}} \frac{d^2 \sigma}{d^2 \mathbf{k}} (1 - e^{i \mathbf{k} \cdot \mathbf{x}}) \equiv \frac{1}{4} \hat{q}(\mathbf{x}^2, t) \mathbf{x}^2 = \frac{1}{4} \hat{q}_0 \mathbf{x}^2 \log \left( \frac{1}{\mu^{*2} \mathbf{x}^2} \right)$$

neglect logarithmic dependence

$$\mu^{*2} \sim 1/\mathbf{x}^2$$

$$\omega \frac{dI_{\text{HO}}}{d\omega} = 2\bar{\alpha} \ln |\cos(\Omega L)| \quad \Omega(t) = \frac{1 - i}{2} \sqrt{\frac{\hat{q}(t)}{\omega}}$$

BDMPS - ASW spectrum

BDMPS-Z

Salgado, Wiedemann - PRD '03

Armesto, Salgado, Wiedemann - PRD '04

Large medium, resums multiple soft interactions.

# Improved Opacity Expansion (IOE)

- Perform “opacity” expansion on top of harmonic oscillator solution:

$$v(\mathbf{x}, t) = \frac{1}{4} \mathbf{x}^2 \log\left(\frac{1}{\mu^{\star 2} \mathbf{x}^2}\right) = \frac{1}{4} \mathbf{x}^2 \left( \log\left(\frac{Q^2}{\mu^{\star 2}}\right) + \log\left(\frac{1}{Q^2 \mathbf{x}^2}\right) \right) \equiv v_{\text{HO}}(\mathbf{x}, t) + \delta v(\mathbf{x}, t)$$

$$\mathcal{K}(\mathbf{x}, t, \mathbf{y}, s) = - \int_{\mathbf{z}} \int_s^t du \mathcal{K}_{\text{HO}}(\mathbf{x}, t | \mathbf{z}, u) \delta v(\mathbf{z}, u) \mathcal{K}(\mathbf{z}, u | \mathbf{y}, s)$$

Mehtar-Tani - JHEP '19

Mehtar-Tani, Tywoniuk - JHEP '19

Barata, Mehtar-Tani - JHEP '20

- Can systematically compute corrections up to arbitrary order in  $\delta v(\mathbf{x}, t)$  :

$$\omega \frac{dI}{d\omega} = \omega \frac{dI^{\text{HO=LO}}}{d\omega} + \omega \frac{dI^{\text{NLO}}}{d\omega} + \dots = \omega \frac{dI^{\text{LO}}}{d\omega} + \sum_{m=1}^{\infty} \omega \frac{dI^{\text{N}^m \text{LO}}}{d\omega}$$

- Spectrum should be independent of  $Q^2$  scale when all orders are included:

→ This leads to  $Q^4 = \hat{q}_0 \omega \ln Q^2 / \mu_*^2$  (trans. mom. acquired by radiated gluon – natural scale)

Spectrum @ NLO  
in the soft limit in IOE:

$$\frac{dI^{(0)}}{d\omega} = \frac{2\alpha_s C_R}{\pi\omega} \ln |\cos \Omega L| ,$$

$$\frac{dI^{(1)}}{d\omega} = \frac{\alpha_s C_R \hat{q}_0}{2\pi} \text{Re} \int_0^L ds \frac{-1}{k^2(s)} \ln \frac{-k^2(s)}{Q^2 e^{-\gamma_E}}$$

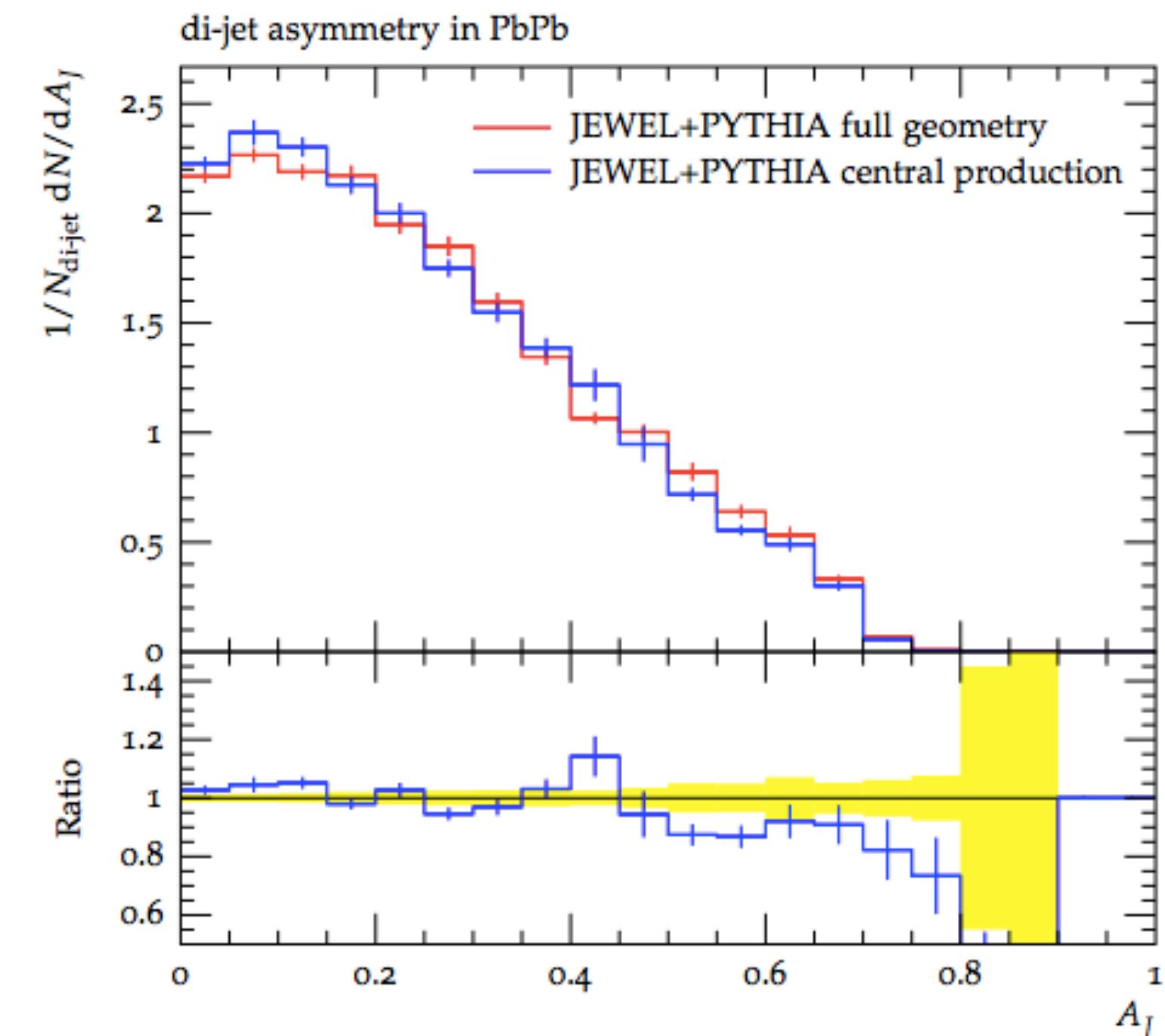
$$\begin{aligned} \hat{q} &= \hat{q}_0 \ln \frac{Q^2}{\mu_*^2} \\ \Omega &= (1 - i) \sqrt{\hat{q}/(4\omega)} \\ k^2(s) &= i \frac{\omega \Omega}{2} [\cot \Omega s - \tan \Omega(L-s)] \end{aligned}$$

# Jet Substructure

- Monte Carlo jet quenching models have provided crucial insights:

→ Naturally include multi-particle nature of jets.

Essential in our current understanding of jet substructure in heavy-ion collisions:

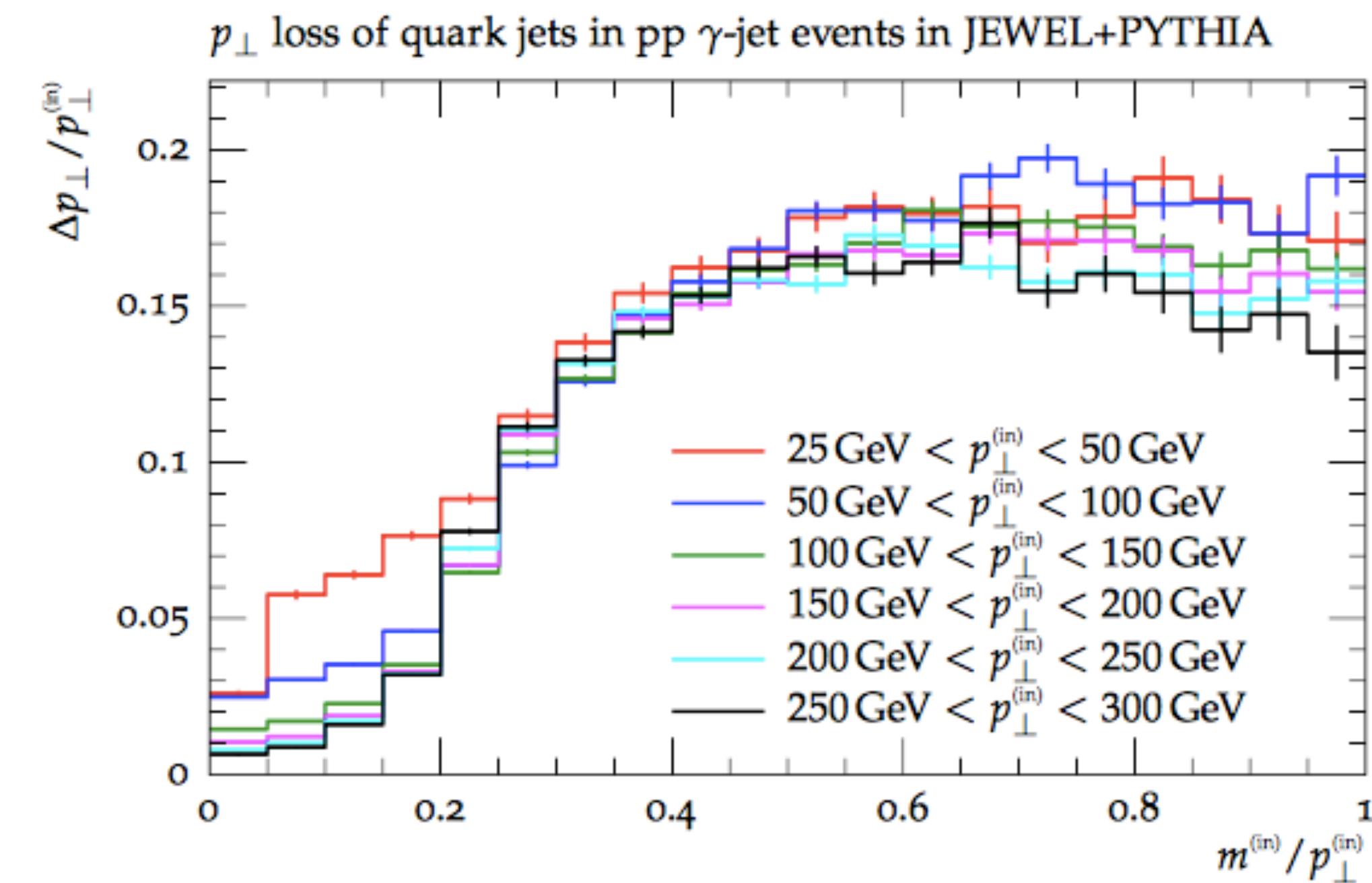


Full geometry

vs

Central production

JEWEL



Dijet asymmetry dominated by mass to momentum ratio, proxy for # vacuum splittings.

Milhano & Zapp - EPJ '16

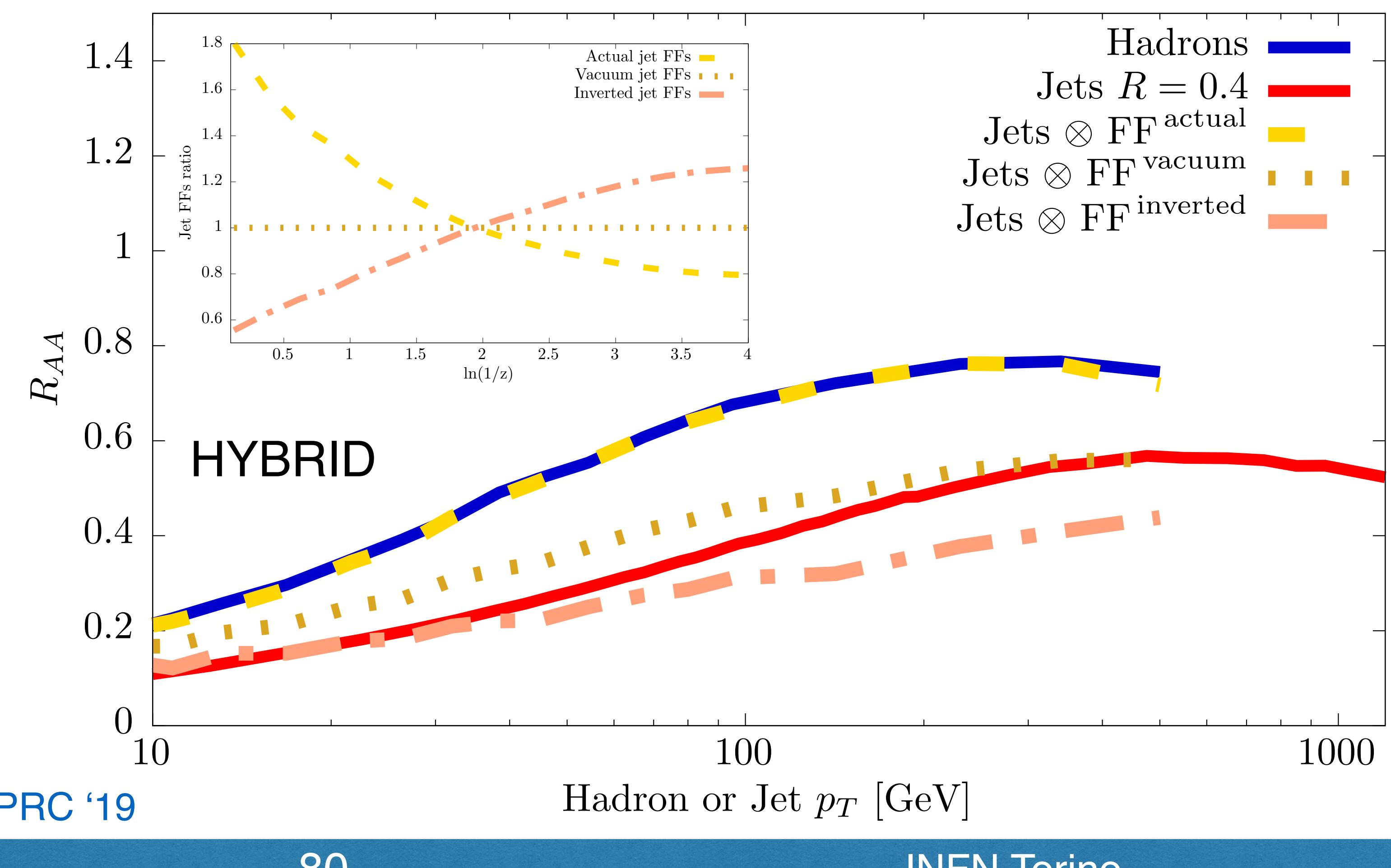
# Jet Substructure

- Monte Carlo jet quenching models have provided crucial insights:  
→ Naturally include multi-particle nature of jets.

Essential in our current understanding of jet substructure in heavy-ion collisions:

Jet suppression  
vs  
Hadron suppression

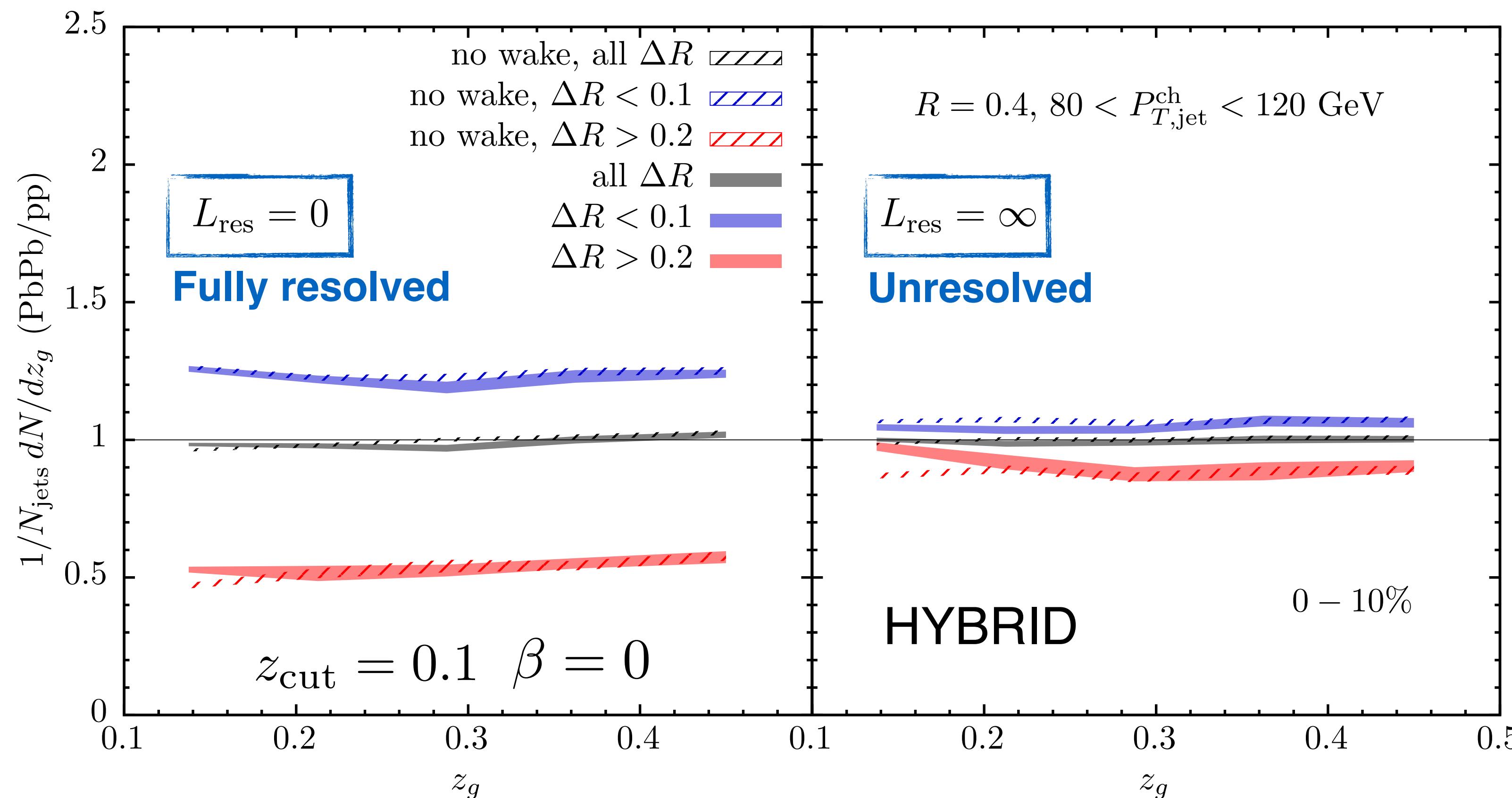
Leading partons belong  
to narrower, less  
suppressed jets  
(high z enhancement).



# Jet Substructure

- Monte Carlo jet quenching models have provided crucial insights:
  - Naturally include multi-particle nature of jets.

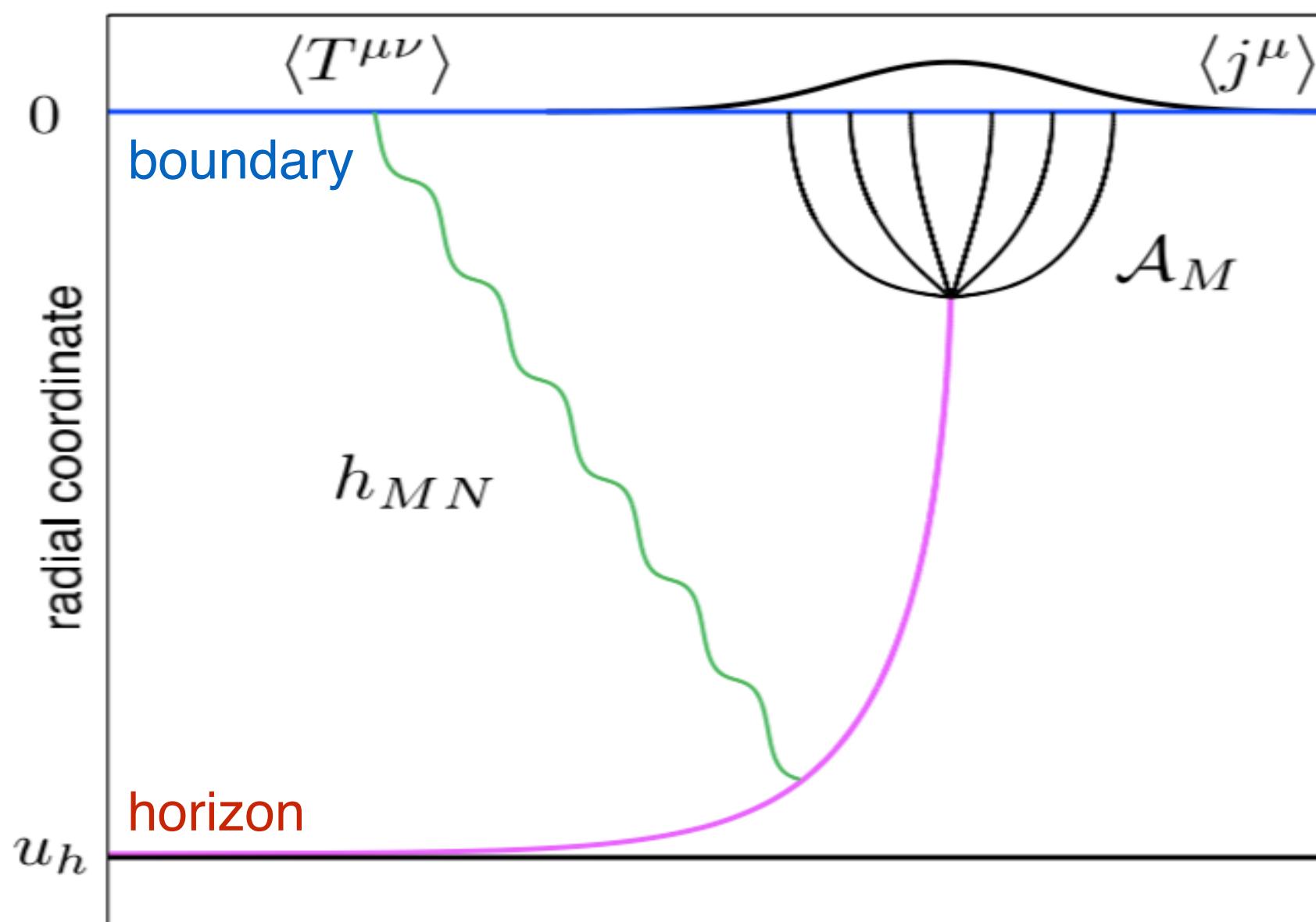
Essential in our current understanding of jet substructure in heavy-ion collisions:



Strong ordering in  $\Delta R$   
(if parton shower resolved):

Larger  $\Delta R$ ;  
↓  
Larger phase-space  
for emissions;  
↓  
Larger quenching,  
smaller survival rate;

# Proxies for jets as falling strings



Chesler et al. - PRD '09

- dressed quarks are **open strings** attached to a D7 flavour brane
- charged under U(1) gauge field sourcing baryon current at boundary
- depth of string endpoint determines localisation of excitation at **boundary**

presence of string **perturbs metric**

$$G_{MN} = G_{MN}^{(0)} + \frac{L^2}{u^2} H_{MN}$$

satisfies linearised Einstein's equations

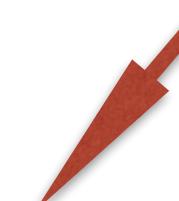
$$\mathcal{L}_{AB}^{MN} H_{MN} = 8\pi G_{\text{Newton}} \boxed{J_{AB}} \text{ string sourced}$$

near boundary expression  
of energy-momentum tensor

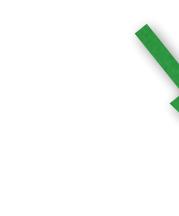
$$\langle \Delta T^{\mu\nu}(t, \mathbf{x}) \rangle = \frac{L^3}{4\pi G_{\text{Newton}}} H_{\mu\nu}^{(4)}(t, \mathbf{x})$$

Chesler & Rajagopal, JHEP '16

hydro (long wavelength)

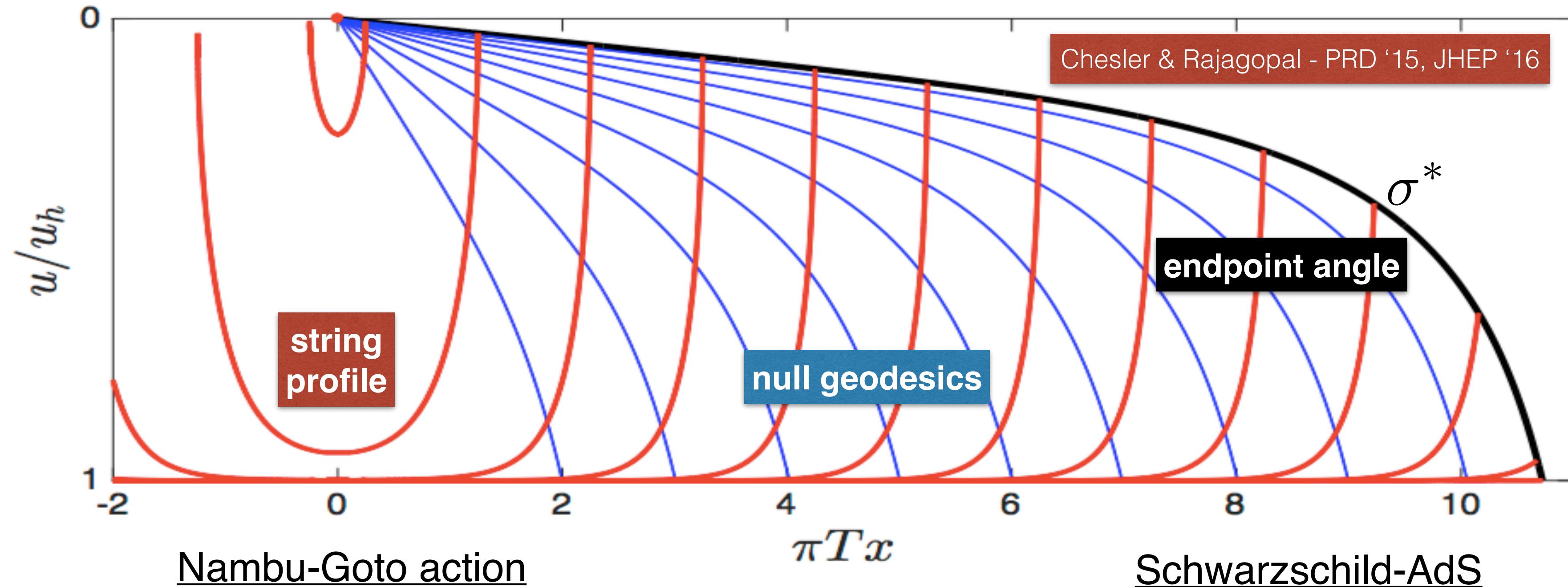


non-hydro (jet modes)



$$\langle \Delta T^{\mu\nu} \rangle \equiv \langle T^{\mu\nu} \rangle - \langle T_{\text{eq}}^{\mu\nu} \rangle$$

# Null falling string approximation



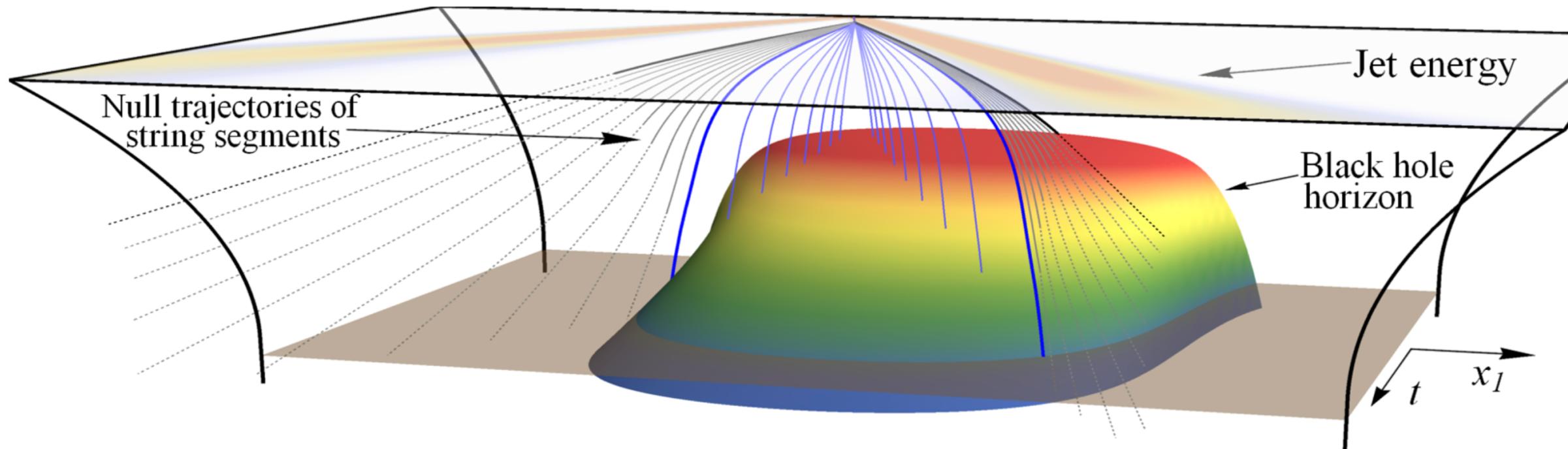
$$S = -\frac{\sqrt{\lambda}}{2\pi L^2} \int d\tau d\sigma \sqrt{-g}$$

$$ds^2 = \frac{L^2}{u^2} \left[ -f dt^2 + dx^2 + \frac{du^2}{f} \right] \quad f \equiv 1 - \frac{u^4}{u_h^4}$$

1. Solve E.O.M. by finding null geodesic profile:  $x_{\text{geo}}(t)$ ,  $u_{\text{geo}}(t)$
2. Find energy carried by each geodesic:  $\Pi_0^\tau(\sigma)$  (peaks at the endpoint)
3. Construct the string energy-momentum tensor:

$$J^{MN} = \int d\sigma J_{\text{particle}}^{MN}(\sigma) \quad J_{\text{particle}}^{MN} = \frac{\Pi_0^\tau}{G_{00}} \frac{dX_{\text{geo}}^M}{dt} \frac{dX_{\text{geo}}^N}{dt} \frac{1}{\sqrt{-G}} \delta^3(\mathbf{x} - \mathbf{x}_{\text{geo}}) \delta(u - u_{\text{geo}})$$

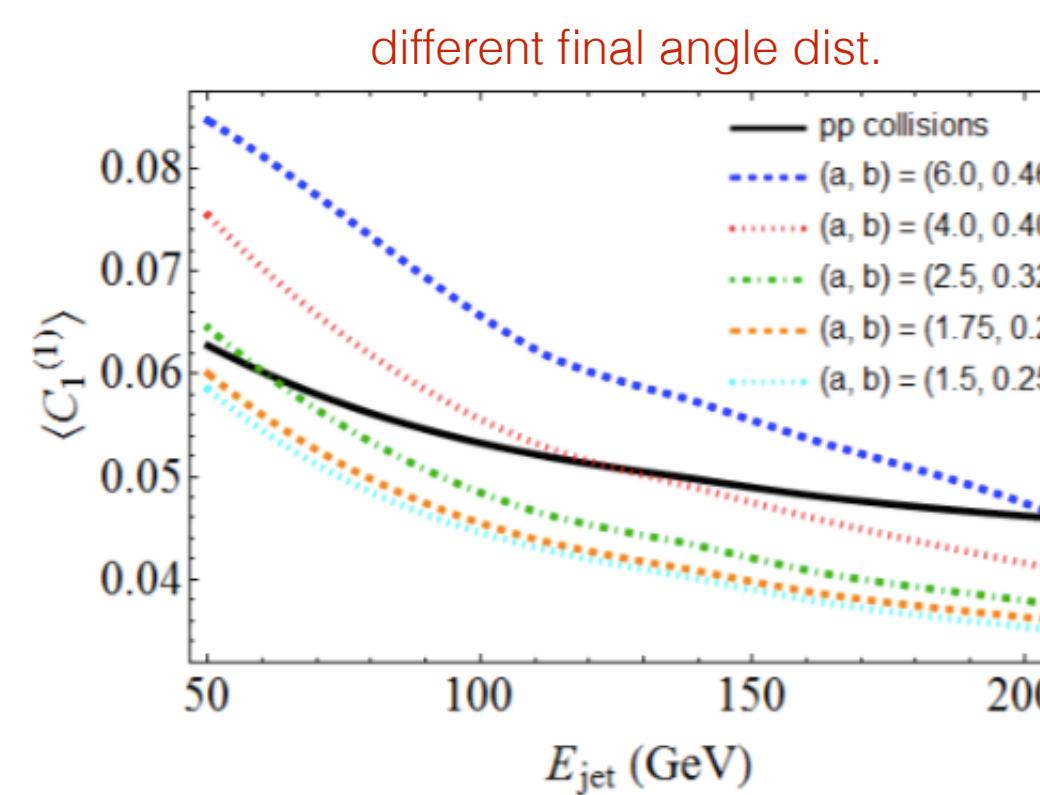
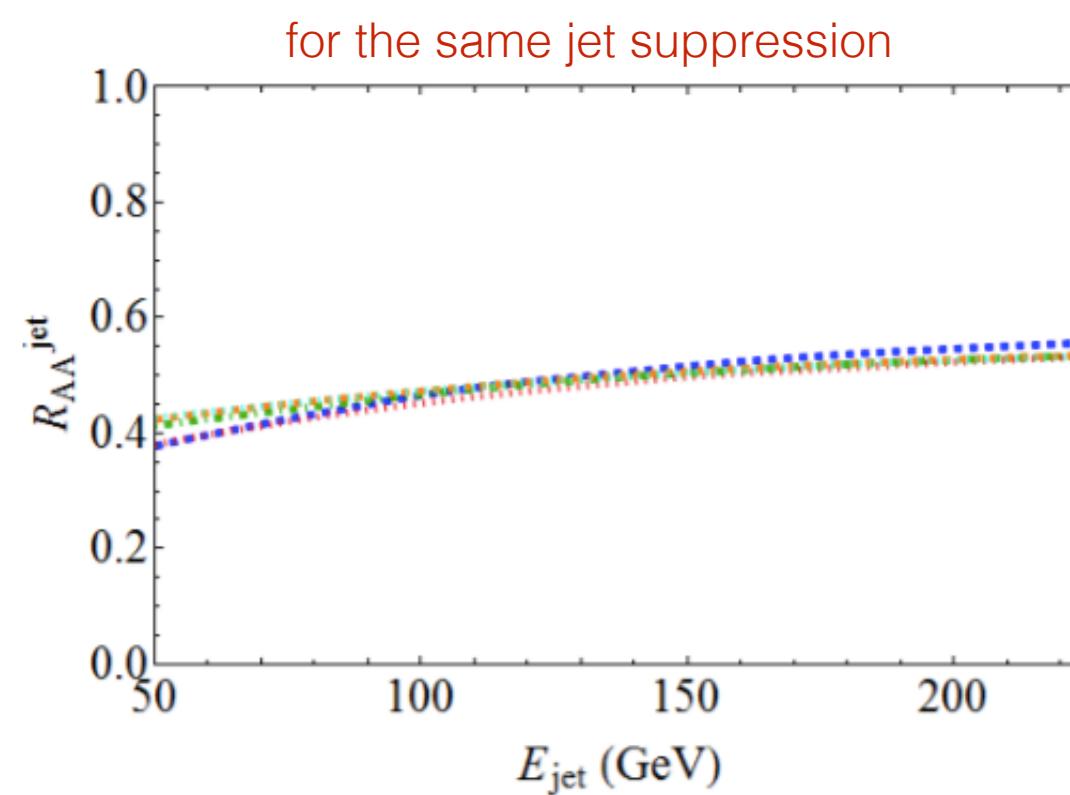
# Holographic quenching with pure strings



the *string* is treated as a model for the *jet as a whole*

Rajagopal, Sadofyev, van der Schee '16

- consider an *ensemble* of such jets by choosing initial distributions of energy & angle from pQCD
- competing effects: each individual jet widens, while wider jets lose more energy

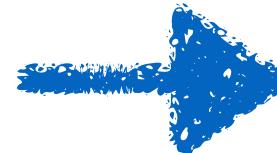


$$C_1^{(\alpha)} \equiv \sum_{i,j} z_i z_j \left( \frac{|\theta_{ij}|}{R} \right)^\alpha \quad C_1^{(1)} = a \sigma_0 \quad T_{\text{SYM}} = b T_{\text{QCD}}$$

measures jet angle in pQCD

also observed in pQCD  
Milhano & Zapp '15

# Diagnosing Jet Energy Loss

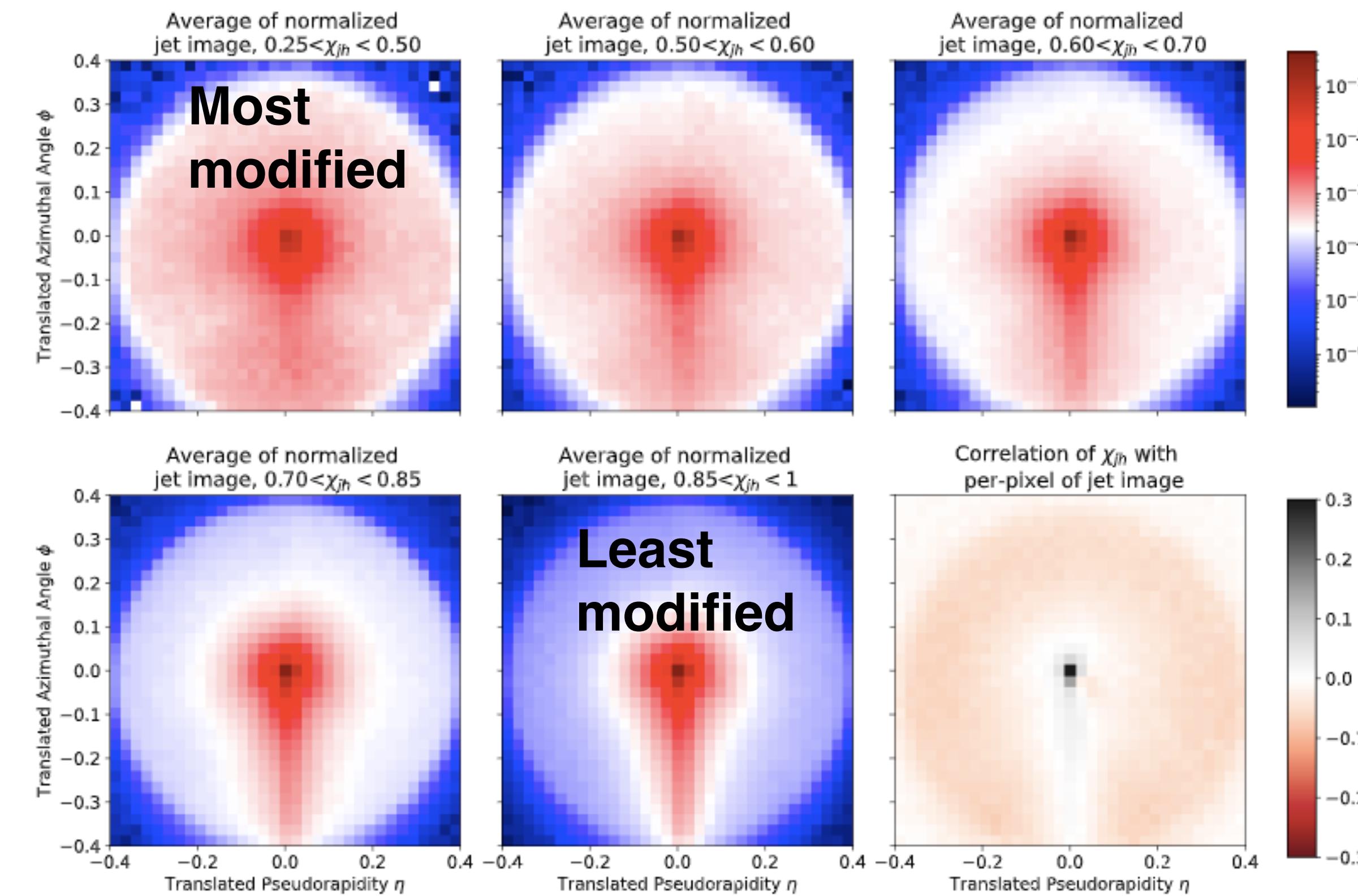
- Experimentally, so far is impossible to know how much energy a given jet has lost.
- Moreover, due to steep falling jet spectrum,  
what we observe is jets that lost the least energy.  
 Selection (or survival) bias.
- Hinders our ability to analyse true effects of energy loss. E.g.:
  - Measure jets above  $p_T > 100 \text{ GeV}$ .
  - Observe that they are narrower in PbPb than in pp:
    - ★ Energy loss makes jets narrower?
    - ★ Observe the surviving (less quenched) jets, which are narrow?
- Exploit deep learning techniques to extract energy loss jet-by-jet.

Energy loss ratio:  $\chi \equiv \frac{E_f}{E_i}$

Final, measurable jet energy.

Vacuum energy (had there been no medium).

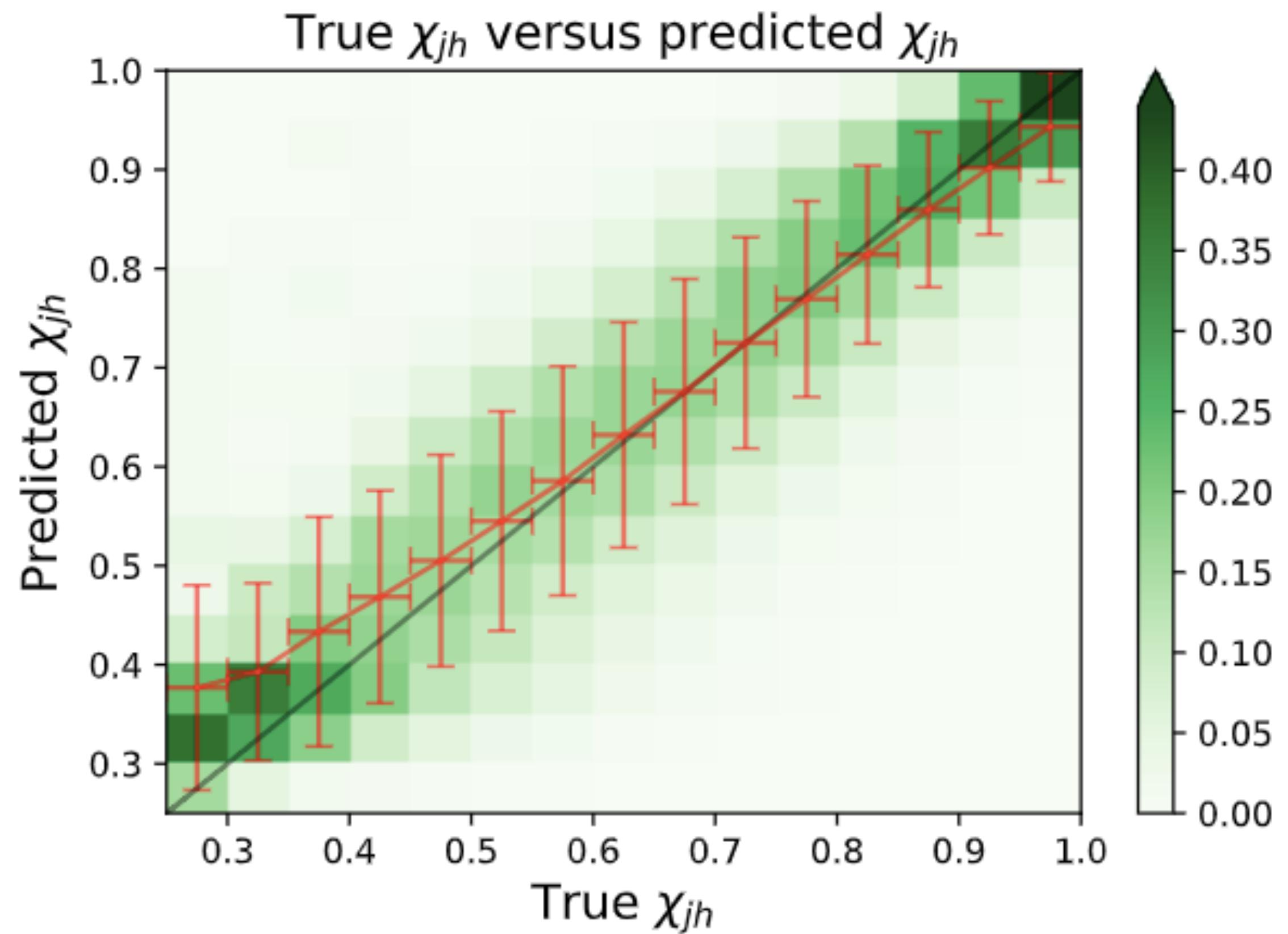
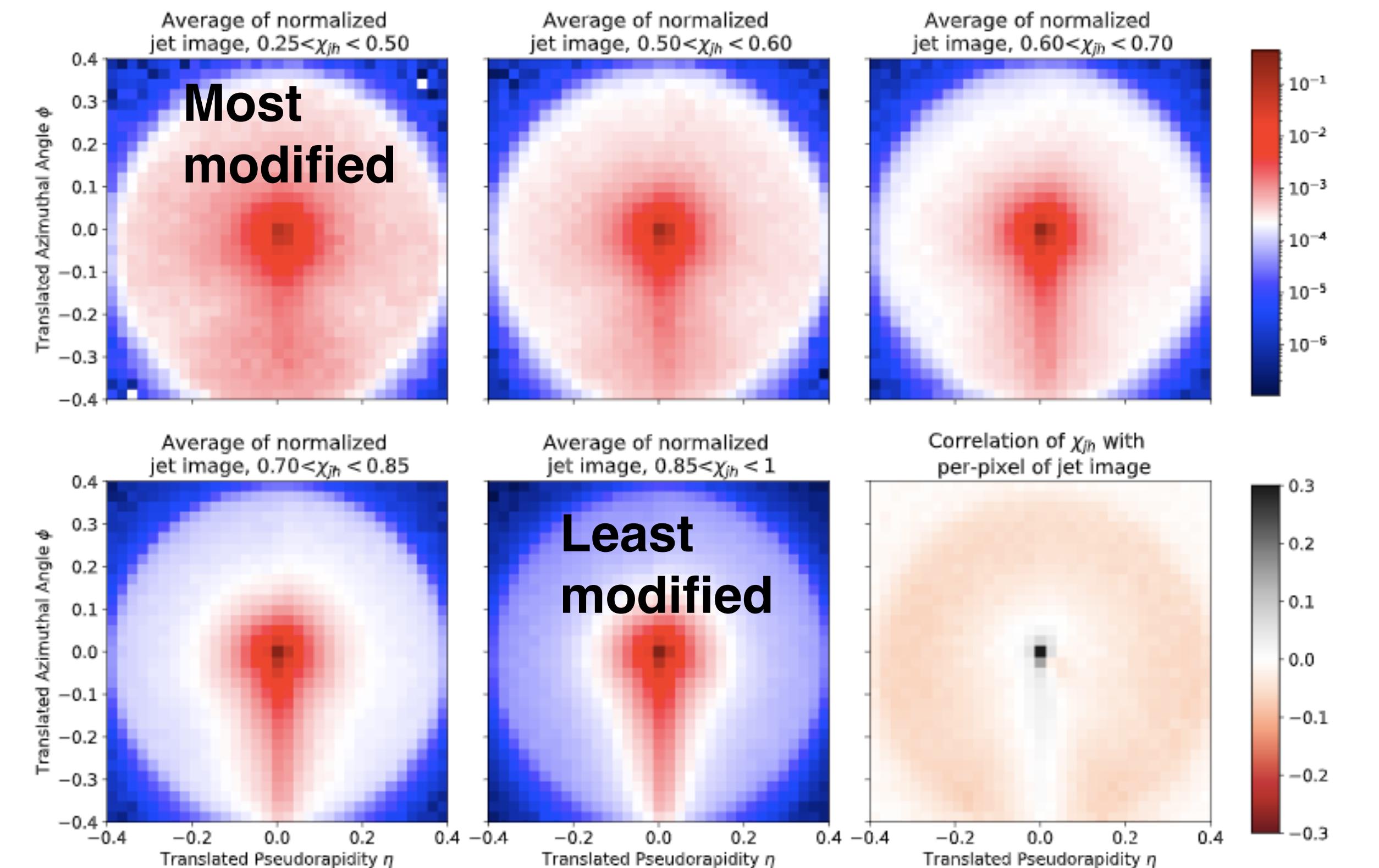
# Deep Learning Jet Modifications



- Most models: Energy loss transfers jet energy to large angles in the form of soft particles.

- Use jet images as inputs for CNN. Main result.
- Use jet observables as inputs for FCNN. Mainly used for interpretability.

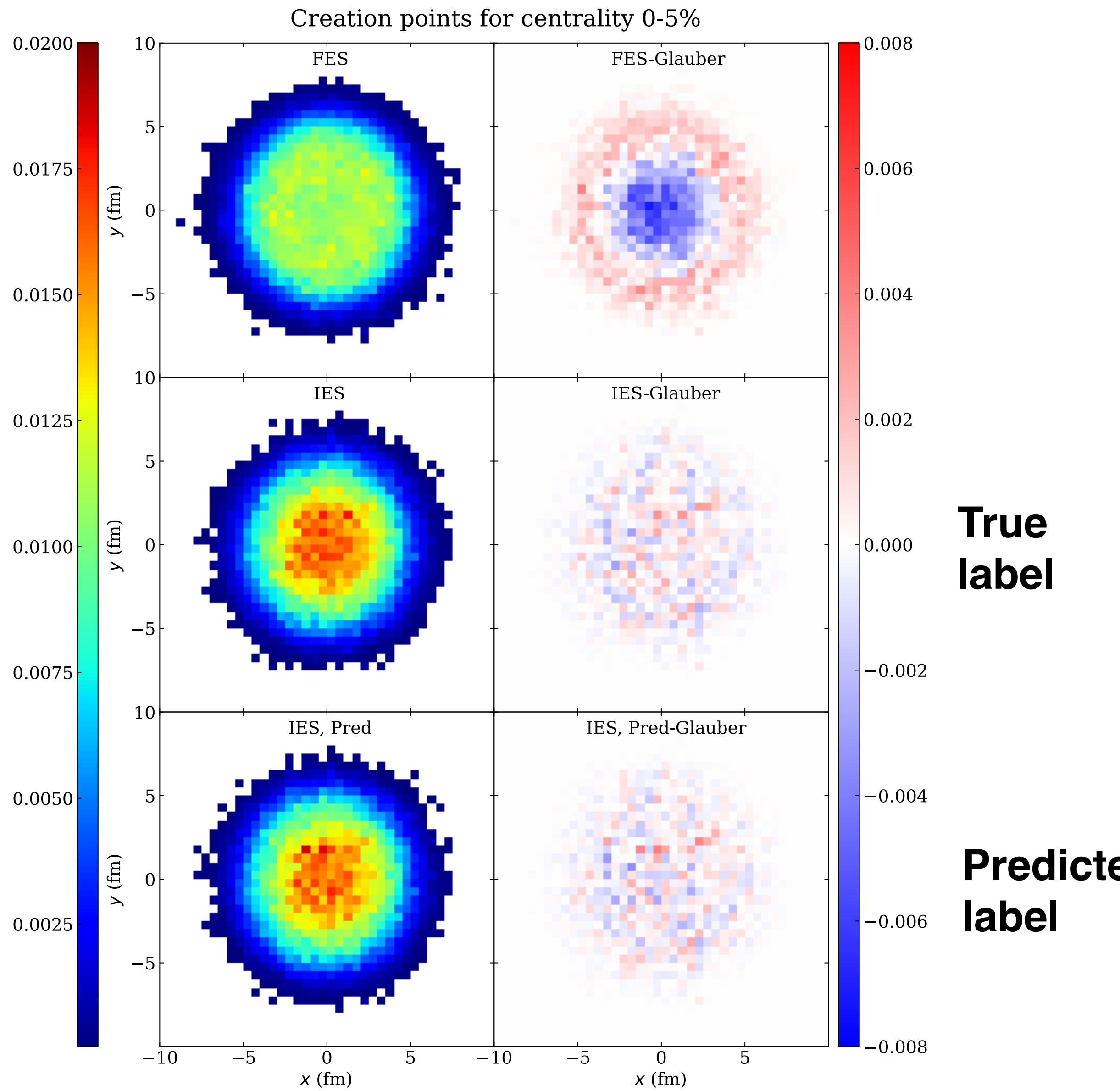
# Deep Learning Jet Modifications



- Use jet images as inputs for CNN. Main result.
- Use jet observables as inputs for FCNN.  
Mainly used for interpretability.

- Good performance across a wide range in  $\chi$
- Consistency check:  
pp (vacuum) jets get  $\chi \simeq 1$

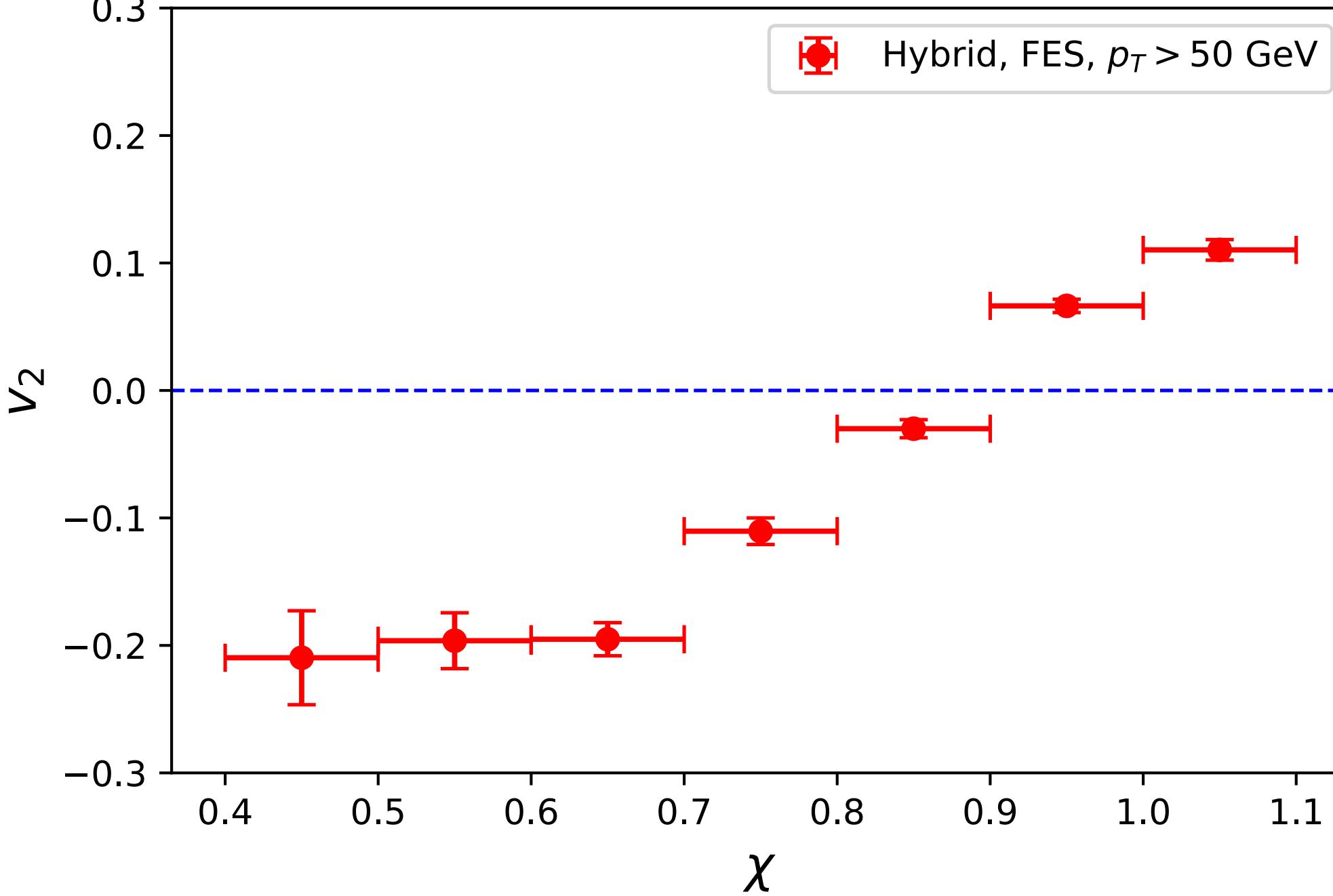
# Accessing True Path Length Distributions



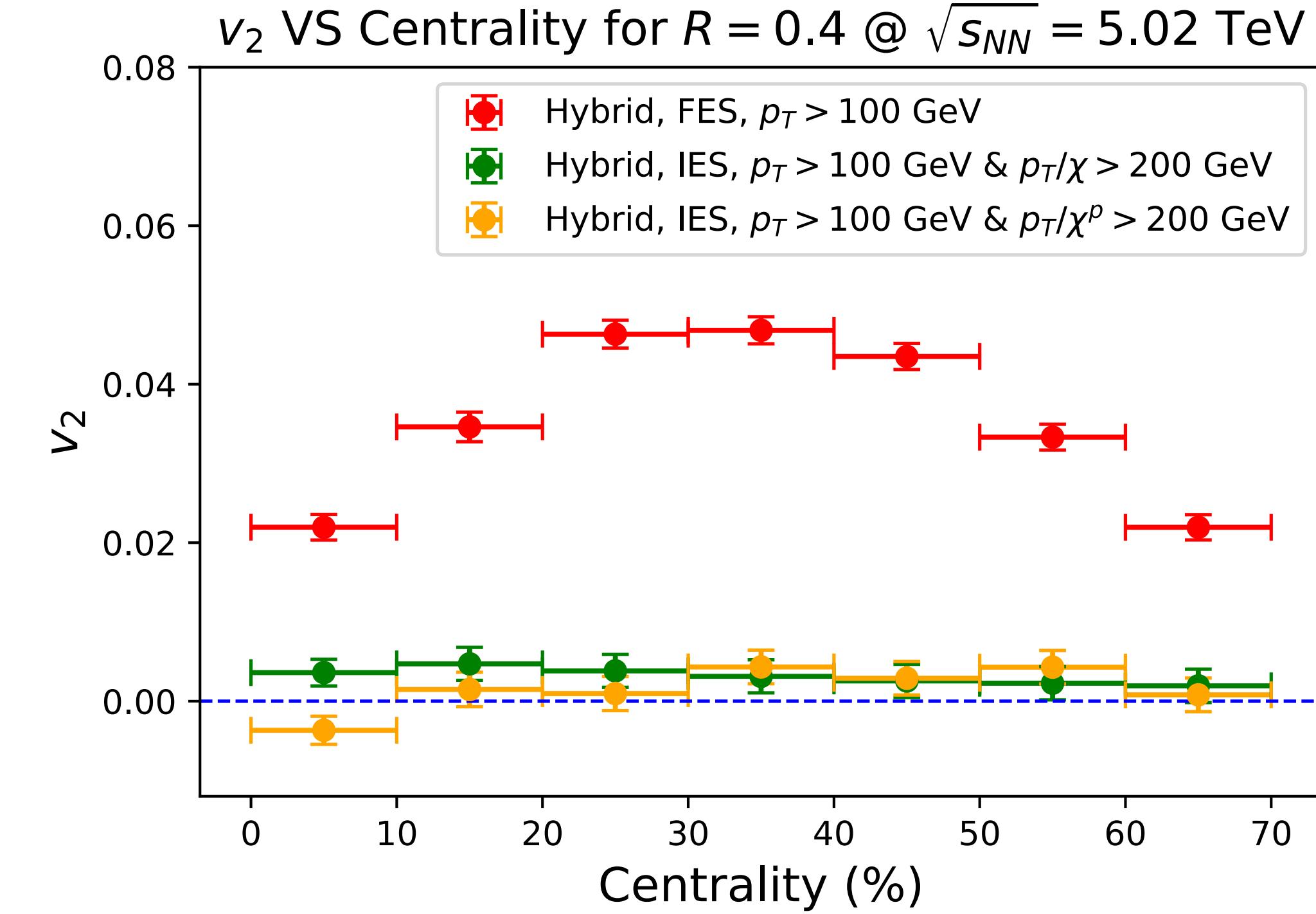
- **FES:** Select jets according to final energy.  
 $E_f > E_{\text{cut}}$   
→ Surface bias compared to actual nuclear overlap density.
- **IES:** Select jets according to “initial” energy.  
 $E_f/\chi > E_{\text{cut}}$   
→ Production point density unbiased w.r.t. true underlying distribution.

# Accessing Initial Jet Anisotropies

$v_2$  VS  $\chi$  for centrality 30-40%,  
 $R = 0.2$  @  $\sqrt{s_{NN}} = 2.76$  TeV



Du, DP, Tywoniuk - in preparation



- Intuitive origin of high- $p_T$  jet anisotropies:

Small  $\chi$  (large energy loss):  
 → longer path length;  
 →  $v_2 < 0$ .

and viceversa for large  $\chi$ .

- However, if use IES:  
 Reveals initial azimuthal anisotropies.  
 In this model: none →  $v_2 \sim 0$ .

And in experiments?

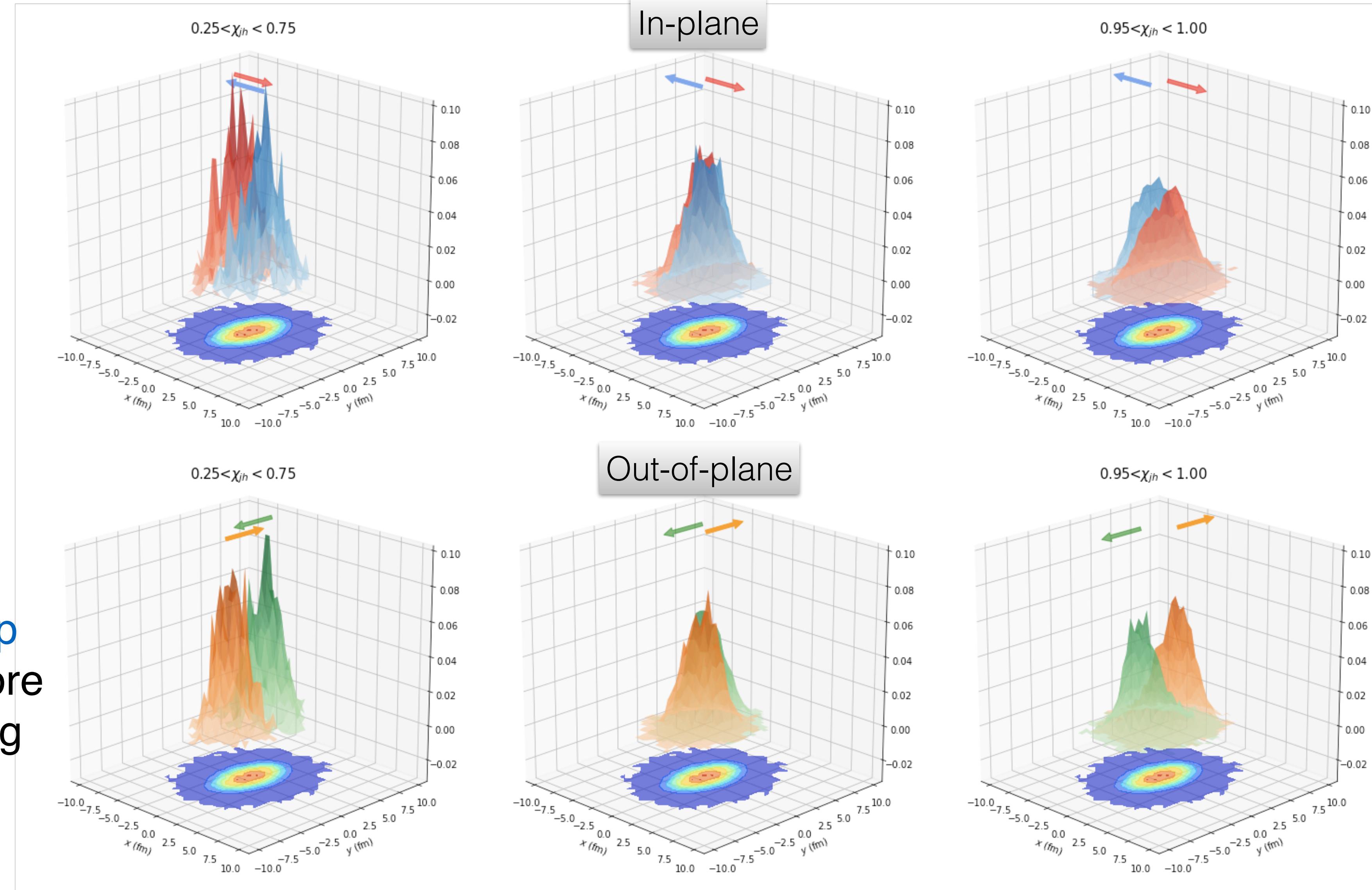
# Tomography with Deep Learning

Determination of production point in transverse plane.

Differential in:

- Orientation w.r.t. event plane.
- Energy loss ratio  $\chi$ .

Production points **swap** in order to traverse more medium with increasing energy loss.



# Collectivity from interference

## Motivation

Absence of jet quenching phenomena  
(energy loss of high  $p_T$  particles by traversing a medium)

in small systems ( $pA$ ,  $pp$ )

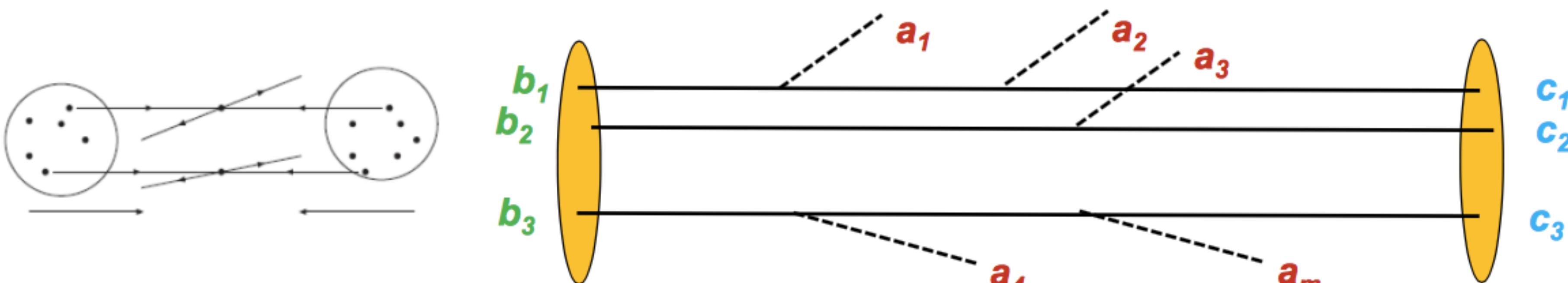
calls to question the presence of deconfined medium (or hydro behaviour).

Are jet quenching effects too small to be observed (yet)?

Origin of **collectivity in small systems** is not final state interactions?  
Can it be **quantum interference**?

# A simple model

- Schematic picture:  $pp$  collision = multiple parton-parton interactions at positions  $y_i$ .



Source lines start (end) with colors  $b_i$  ( $c_i$ ) at rapidity of 1<sup>st</sup> (2<sup>nd</sup>) hadron.

- Diagrammatic rules: gluon emission keeps track of color and phases exactly.

(basis for understanding QCD interference effects)

$$\text{Diagram showing a source line } b \text{ at rapidity } y_j \text{ emitting a gluon } a. \quad = T_{b_i c_i}^a \int d\mathbf{x} \vec{f}(\mathbf{x} - \mathbf{y}) e^{i \mathbf{k} \cdot \mathbf{x}} = T_{b_i c_i}^a \vec{f}(\mathbf{k}) \exp[i \mathbf{y} \cdot \mathbf{k}]$$

Simplifications:

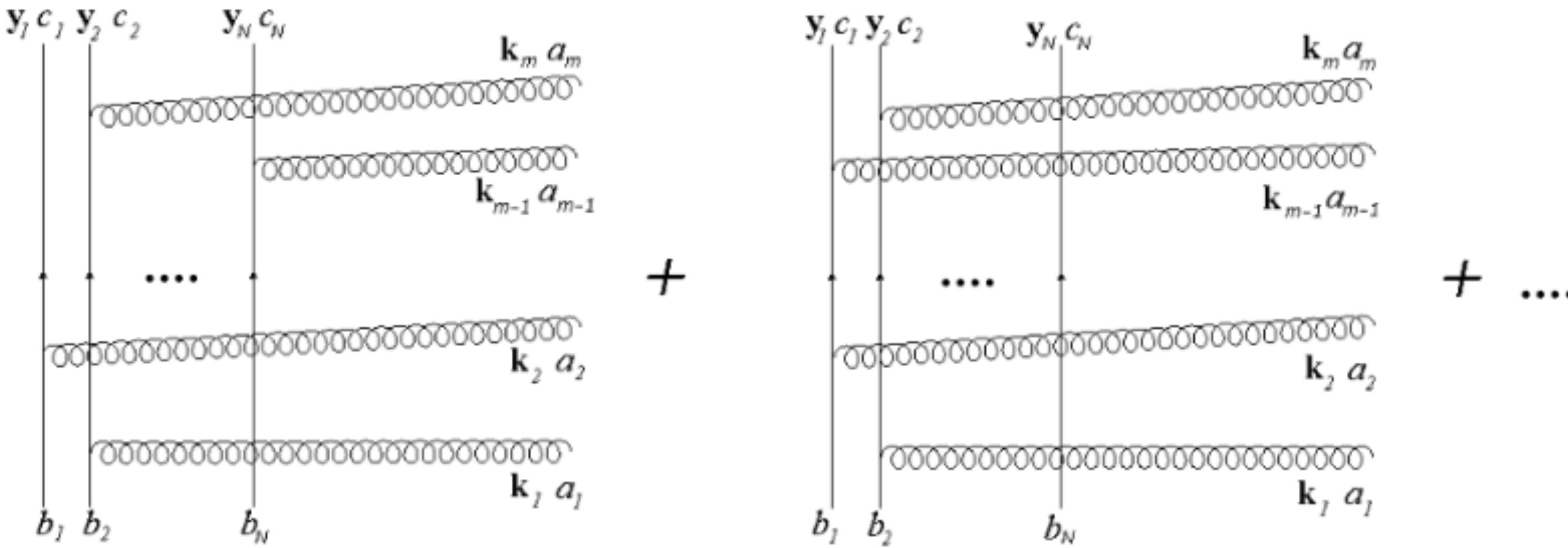
$$\rho(\mathbf{y}_1, \mathbf{y}_2) = \frac{1}{(2\pi B)^2} \exp \left[ -\frac{\mathbf{y}_1^2}{2B} - \frac{\mathbf{y}_2^2}{2B} \right]$$

- Don't specify the kinematics, flat rapidity dependence
- Assign a classical, gaussian weight to the distribution of sources in hadron (GPDs in mean field approximation). B scale from  $pp$  soft processes

**B can be related to Qs, but note azimuthal isotropy!**

# $m$ gluons from $N$ sources

- This model has  $N^m$  different  $m$ -particle emission amplitudes:



- Summing up and squaring these emission amplitudes returns a **gluon spectrum for a fixed set of transverse positions  $y_i$** . Averaging over transverse positions with a **classical weight**, one finds the spectrum

$$\frac{d\Sigma}{d\mathbf{k}_1 \dots d\mathbf{k}_m} = \int \left( \prod_{i=1}^N dy_i \right) \rho(\{y_i\}) \hat{\sigma}(\{\mathbf{k}_j\}, \{y_i\})$$

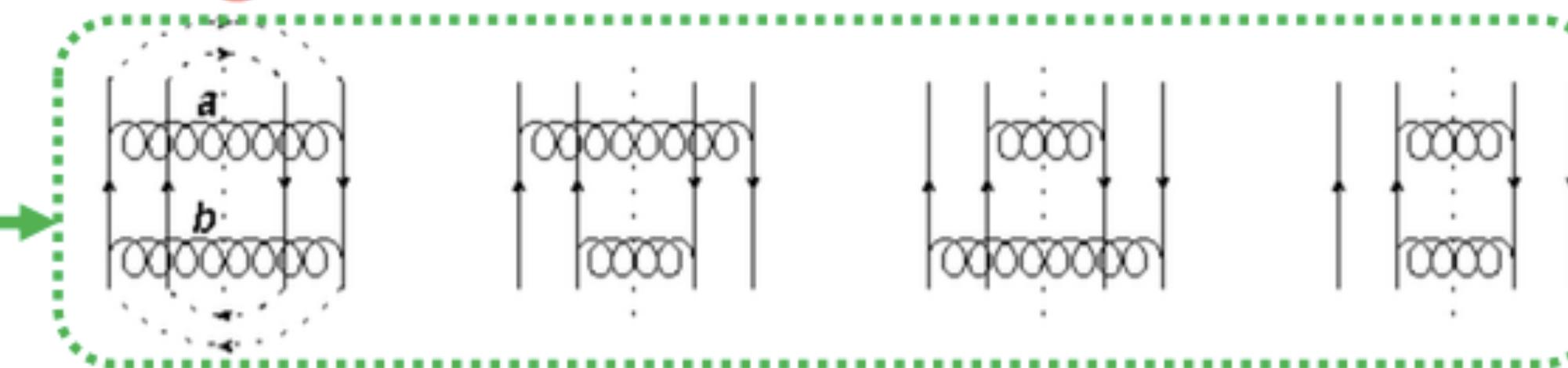
We want to calculate this spectrum and its azimuthal anisotropies  $v_n\{2k\}$  for arbitrary  $m$  and  $N$ .

## Simplest case: emitting m=2 gluons from N=2 sources

- Color can be read easily from diagrams

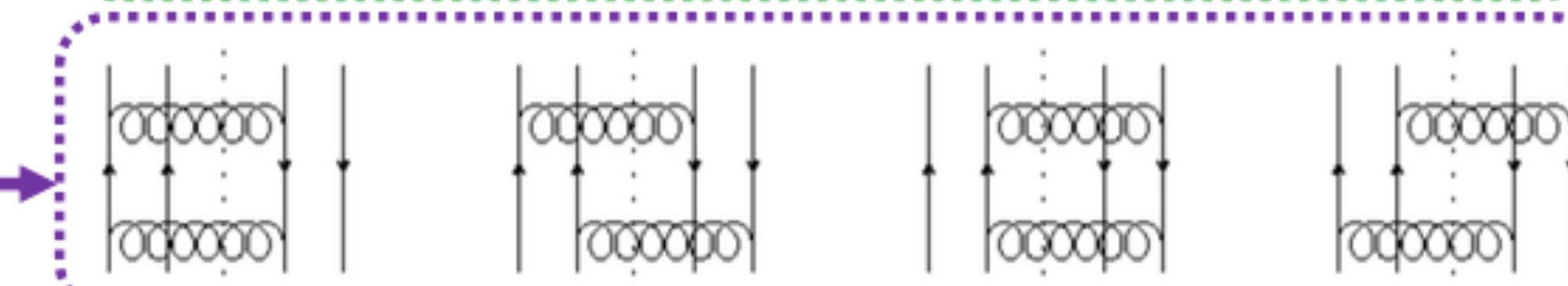
$$\text{Tr} [T^a T^b T^b T^a] \text{Tr} [\mathbb{1}] = N_c^2 (N_c^2 - 1)^2$$

diagonal → no interference

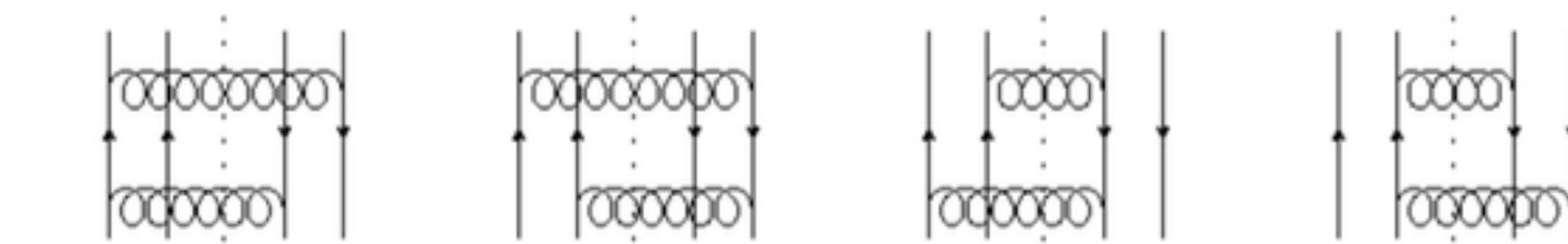


$$\text{Tr} [T^a T^b] \text{Tr} [T^b T^a] = N_c^2 (N_c^2 - 1)$$

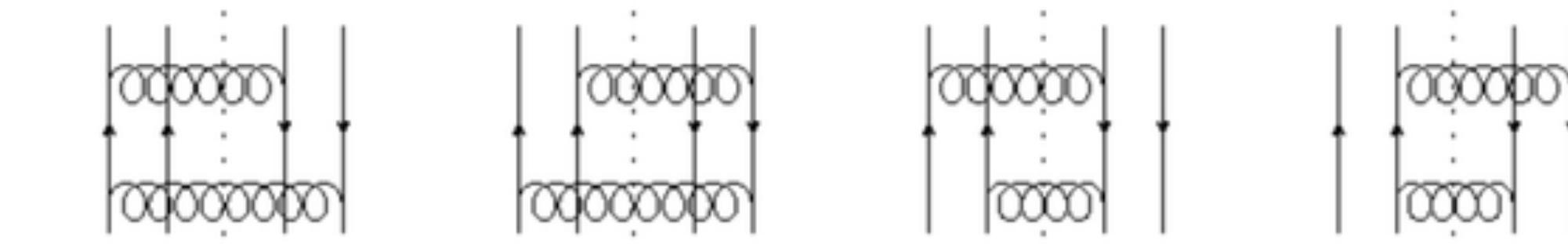
off-diagonal → interference



correlation in azimuth arises  
from two gluons emitted from  
**same source pair**



**vanish in QCD**



$$\frac{d\Sigma}{d\mathbf{k}_1 d\mathbf{k}_2} \propto |\vec{f}(\mathbf{k}_1)|^2 |\vec{f}(\mathbf{k}_2)|^2 \left[ 1 + \frac{\left( e^{-B(\mathbf{k}_1+\mathbf{k}_2)^2} + e^{-B(\mathbf{k}_1-\mathbf{k}_2)^2} \right)}{(N_c^2 - 1)} \right]$$

- For  $B = 1/Q_s^2$ , this QCD agrees with CGC calculations,

Altinoluk et al, PLB 751 (2015) 448; PLB 752 (2016) 113  
Lappi, Schenke, Schlichting, Venugopalan JHEP 1601 (2016) 061

but it does not invoke saturation effects.

# Odd harmonics

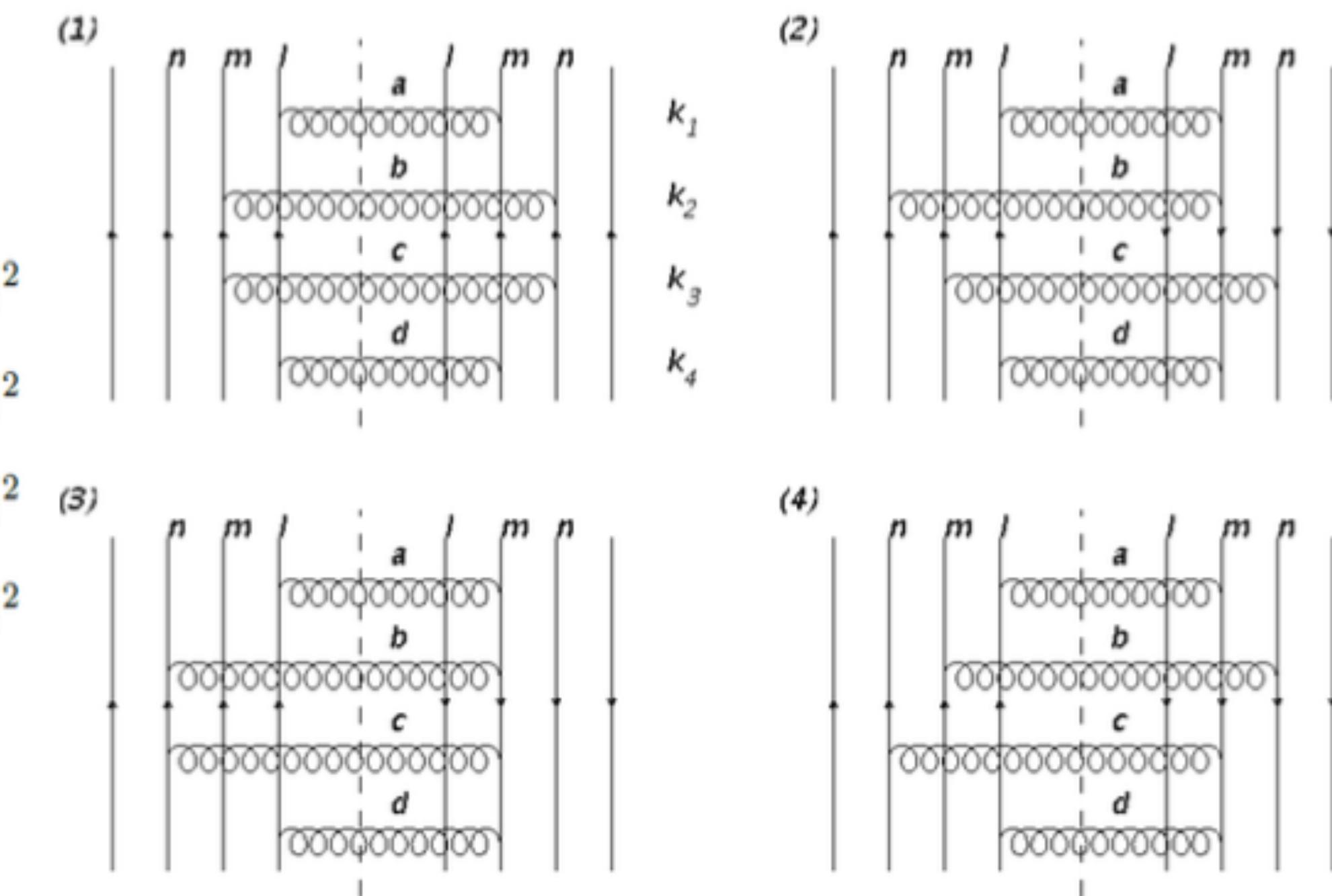
$$N = m = 4$$

$$\text{Tr}[1] \text{Tr}[T^c T^b] \text{Tr}[T^b T^c T^d T^a] \text{Tr}[T^a T^d] = N_c^4 (N_c^2 - 1)^2$$

$$\text{Tr}[1] \text{Tr}[T^b T^c] \text{Tr}[T^c T^d T^b T^a] \text{Tr}[T^a T^d] = \frac{1}{2} N_c^4 (N_c^2 - 1)^2$$

$$\text{Tr}[1] \text{Tr}[T^b T^c] \text{Tr}[T^d T^c T^b T^a] \text{Tr}[T^a T^d] = N_c^4 (N_c^2 - 1)^2$$

$$\text{Tr}[1] \text{Tr}[T^c T^b] \text{Tr}[T^b T^d T^c T^a] \text{Tr}[T^a T^d] = \frac{1}{2} N_c^4 (N_c^2 - 1)^2$$



*To order  $1/N$ , differences in color factors break the  $k$  to  $-k$  symmetry*

$$\begin{aligned}
 & e^{i \mathbf{k}_2 \cdot \Delta \mathbf{y}_{mn}} \left( e^{i \mathbf{k}_3 \cdot \Delta \mathbf{y}_{mn}} + \frac{1}{2} e^{-i \mathbf{k}_3 \cdot \Delta \mathbf{y}_{mn}} \right) + e^{-i \mathbf{k}_2 \cdot \Delta \mathbf{y}_{mn}} \left( \frac{1}{2} e^{i \mathbf{k}_3 \cdot \Delta \mathbf{y}_{mn}} + e^{-i \mathbf{k}_3 \cdot \Delta \mathbf{y}_{mn}} \right) \\
 &= 3 \cos(\mathbf{k}_2 \cdot \Delta \mathbf{y}_{mn}) \cos(\mathbf{k}_3 \cdot \Delta \mathbf{y}_{mn}) - \sin(\mathbf{k}_2 \cdot \Delta \mathbf{y}_{mn}) \sin(\mathbf{k}_3 \cdot \Delta \mathbf{y}_{mn}) . \tag{5}
 \end{aligned}$$

**Odd harmonics arise due to non-abelian nature of QCD**

# Results for flow coefficients

- Once spectrum is known, azimuthal phase space averages can be formed

$$T_n(k_1, k_2) = \binom{m}{2} \int_{\rho} \int_0^{2\pi} d\phi_1 d\phi_2 \exp[in(\phi_1 - \phi_2)] \left( \int \prod_{b=3}^m k_b dk_b d\phi_b \right) \hat{\sigma}$$

- Suitably normalized, these define  $v_n$ 's (2<sup>nd</sup> order cumulants)

$$\bar{T}(k_1, k_2) = \binom{m}{2} \int_{\rho} \int_0^{2\pi} d\phi_1 d\phi_2 \left( \int \prod_{b=3}^m k_b dk_b d\phi_b \right) \hat{\sigma}$$

$$v_n^2\{2\}(k_1, k_2) \equiv \langle\langle e^{in(\phi_1 - \phi_2)}\rangle\rangle(k_1, k_2) \equiv \frac{T_n(k_1, k_2)}{\bar{T}(k_1, k_2)}$$

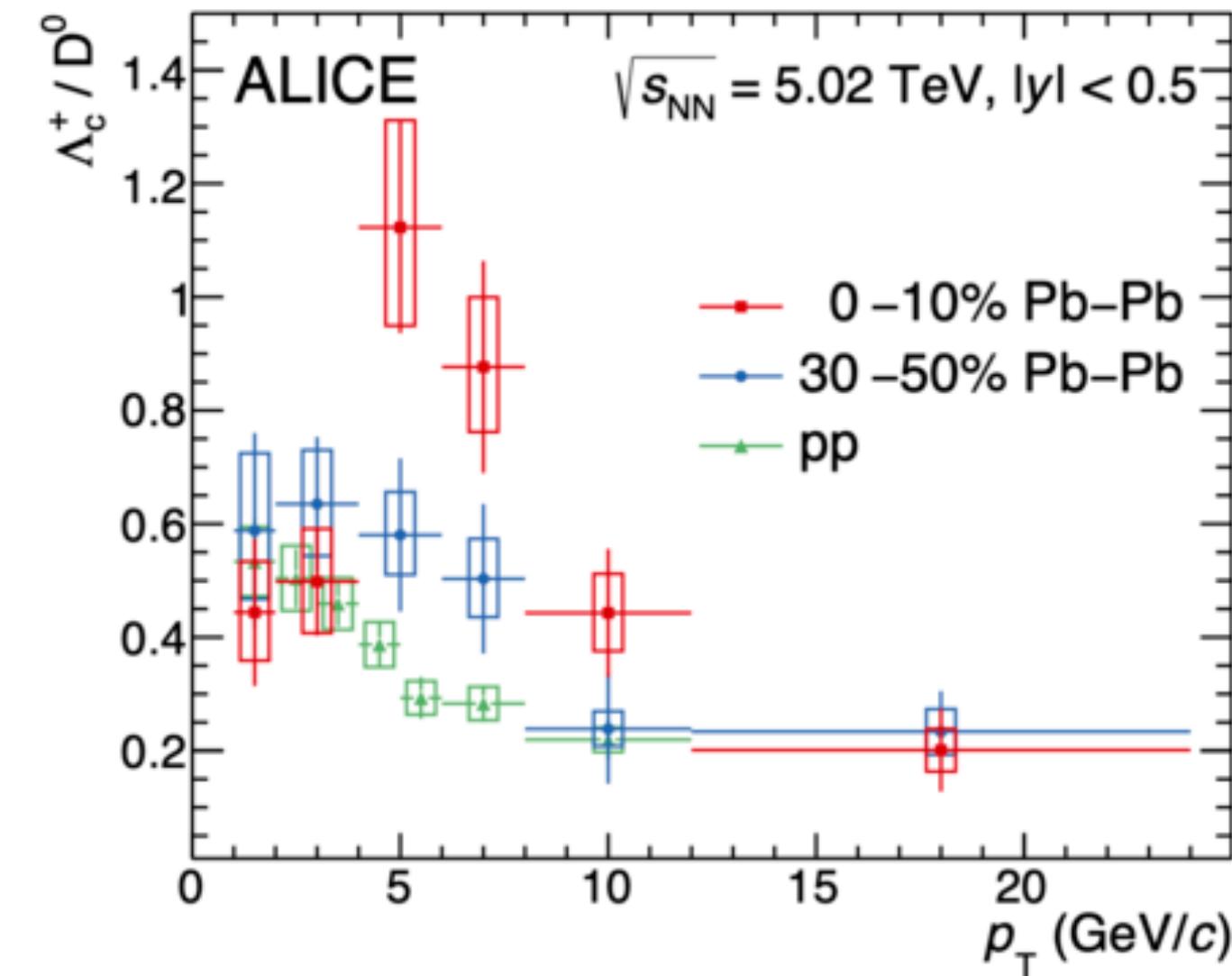
- Higher order cumulants** obtained in close similarity

$$S(k_1, k_2, k_3, k_4) = \binom{m}{4} \int_{\rho} \int_0^{2\pi} d\phi_1 d\phi_2 d\phi_3 d\phi_4 e^{in(\phi_1 + \phi_2 - \phi_3 - \phi_4)} \left( \int \prod_{b=5}^m k_b dk_b d\phi_b \right) \hat{\sigma}$$

$$\begin{aligned} \langle\langle e^{in(\phi_1 + \phi_2 - \phi_3 - \phi_4)}\rangle\rangle_c &= \langle\langle e^{in(\phi_1 + \phi_2 - \phi_3 - \phi_4)}\rangle\rangle \\ &\quad - \langle\langle e^{in(\phi_1 - \phi_3)}\rangle\rangle \langle\langle e^{in(\phi_2 - \phi_4)}\rangle\rangle - \langle\langle e^{in(\phi_1 - \phi_4)}\rangle\rangle \langle\langle e^{in(\phi_2 - \phi_3)}\rangle\rangle \end{aligned}$$

associated to hydro behaviour

# Collectivity in Small Systems



Baryon to meson enhancement observed also in pp collisions.

- Hadron spectra and yields can be described by thermal distribution... even in proton-proton!
  - Connection with microscopic description of hadronization? Colour-reconnection, entanglement...
- Improve understanding of **hadronization**, in large and small systems, using **heavy quark probes**.
  - Model proton-proton system as a droplet of liquid QGP.
  - Use novel hadronization mechanisms involving recombination.

Beraudo, De Pace, Nardi, Prino, DP - in preparation

# Concurrent Mini-jet+Hydro Evolution

Elements of the framework:

- Initial state from IP-Glasma.
- Finite mini-jet production probability at each binary collision.
- Hydro. energy-momentum from IP-Glasma.
- Mini-jets lose energy to the QGP (Hybrid Model) above  $T_c$ :  
→ Gaussian source into hydro. e.o.m.

$$\tau = 0$$

$$\tau = 0.4 \text{ fm}/c$$

- Cooper-Frye bulk.
- Hadronize non-stopped partons through Lund string model:
  - If parton close to hypersurface, sample thermal partons to build colourless string.
  - If not, construct single colourless string with all such “corona” partons.
- Everything evolves with UrQMD.

$$\tau_{\text{freeze-out}}$$

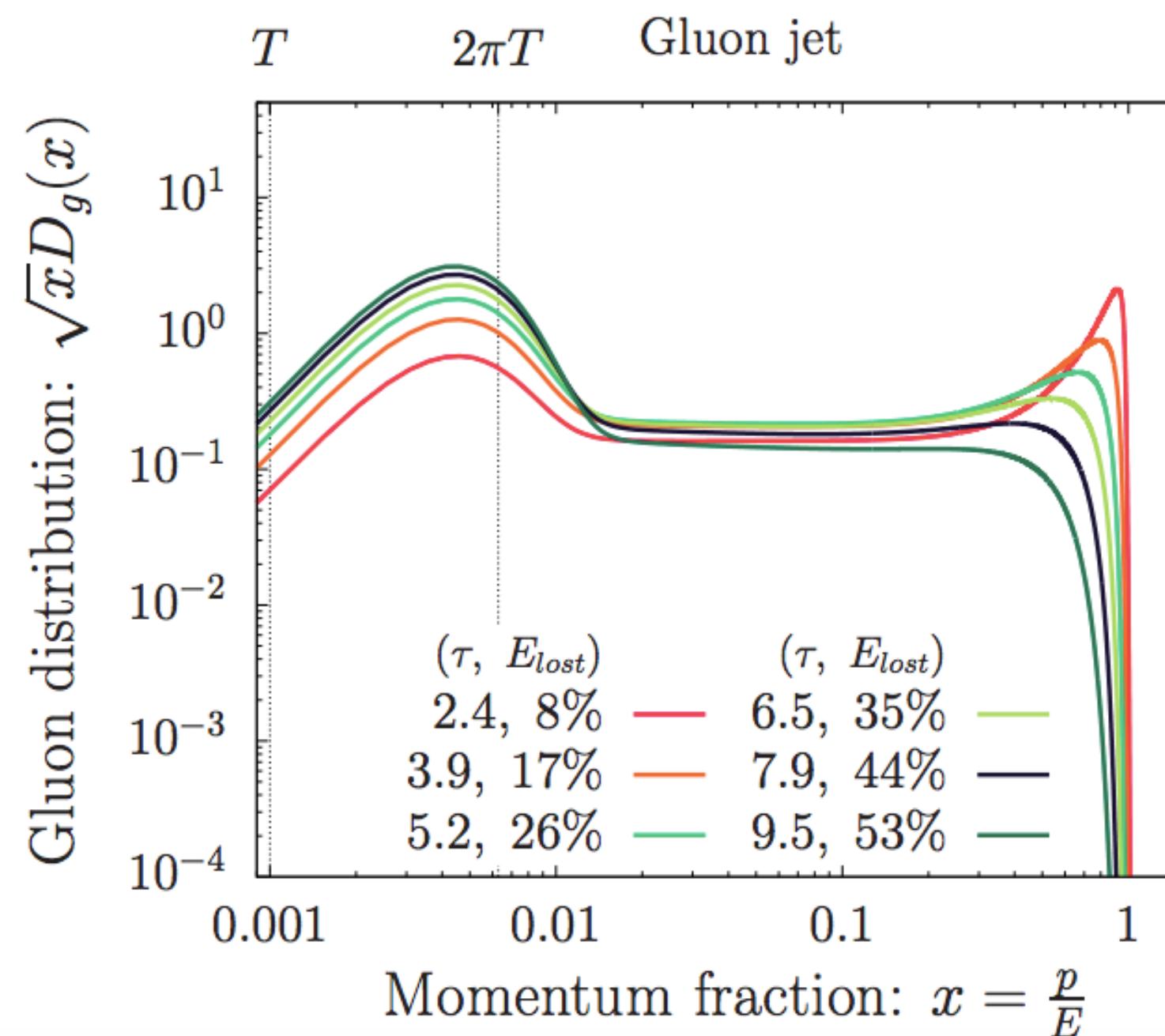
DP, Singh, Gale, Jeon - PRC '22

# Further Improvements on Single Charge Energy Loss

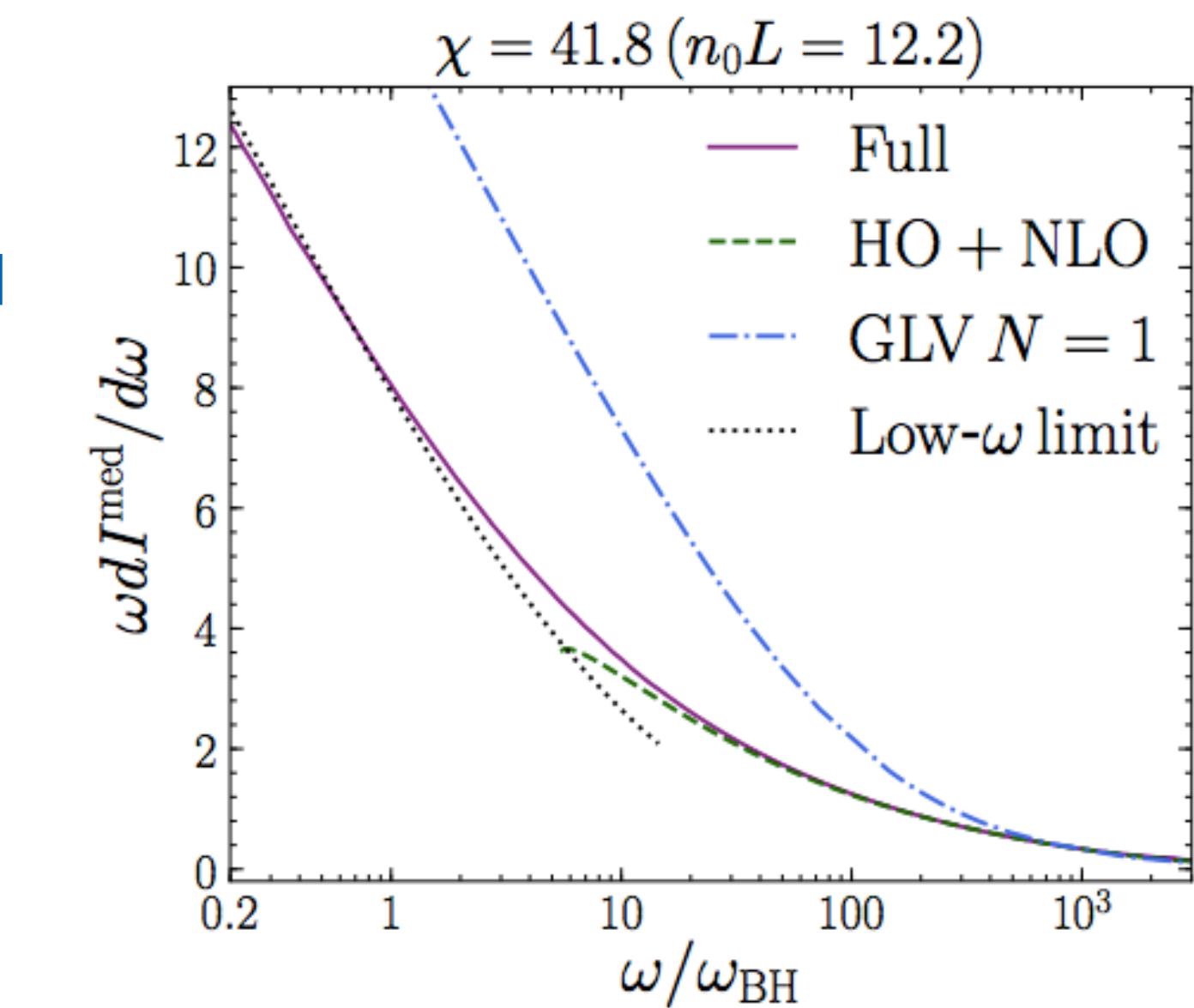
- All order resummation of medium induced radiation spectrum.
- Resummed Opacity Expansion (ROE) to cover Bethe-Heitler regime.

Feal et al. - PRD '18 & '19  
Andrés et al. - JHEP '20 & '21

Isaksen et al. - arXiv:2206.02811



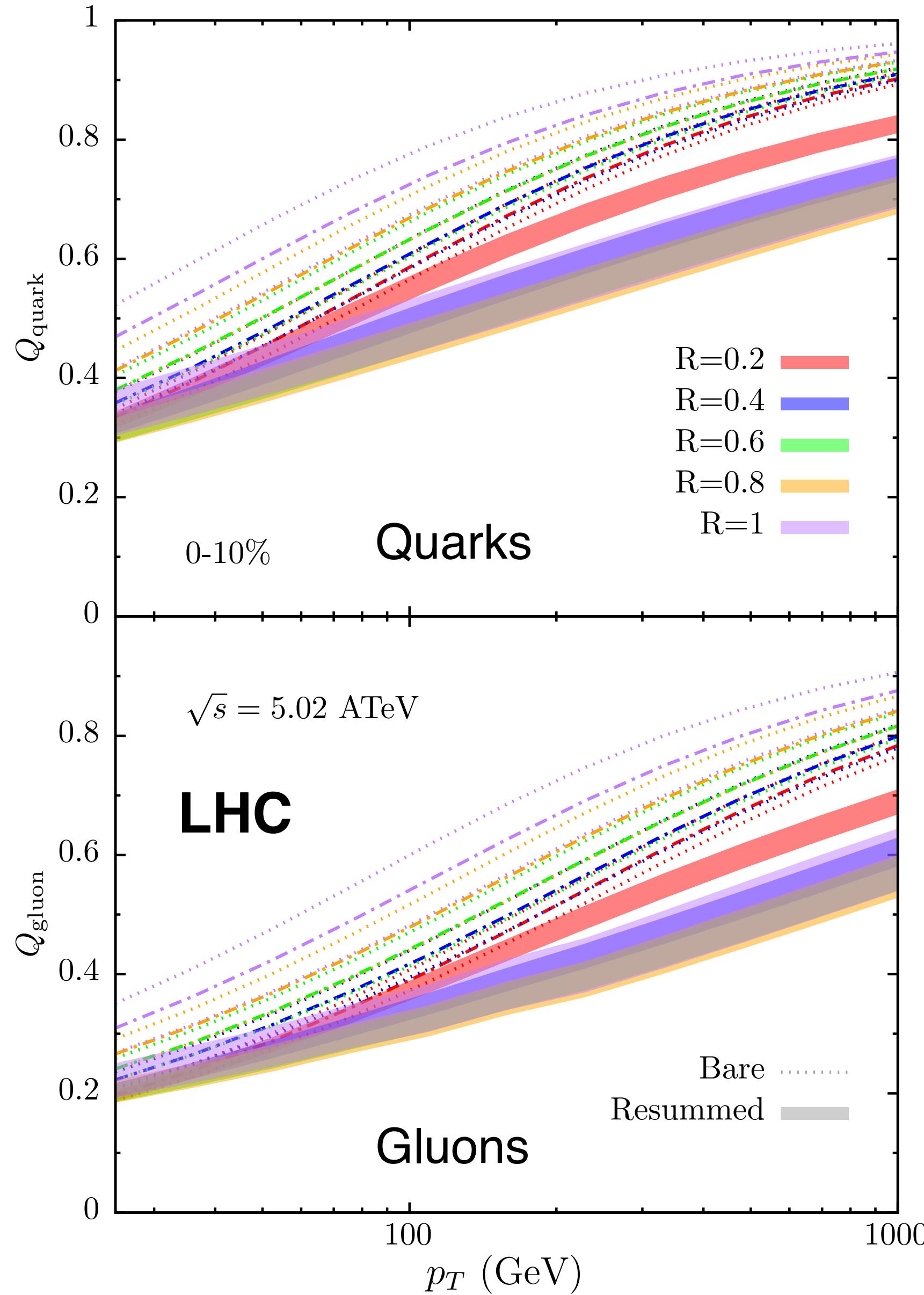
Schlichting & Soudi - JHEP '20



- In-medium fragmentation of hard parton in QGP through effective kinetic theory.
  - Includes  $1 \leftrightarrow 2$  and  $2 \leftrightarrow 2$  processes.
  - Features turbulent cascade, modified chemistry around the jet.

Detailed analysis of dynamics, can account for medium response.

# Resummed Quenching Factor



- Bare quenching factors (dashed):
  - less quenching for larger R.
  - Easier to keep (recover) the emitted (thermalised) modes.
- Resummed quenching factors (solid):
  - larger R can lead to more quenching.
  - Interplay between energy recovery and size of quenched phase space.