

LIGHT DARK MATTER DETECTION

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CYGNO Collaboration meeting, December 2022

OUTLINE

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- Searching for keV-MeV dark matter

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- Down to the MeV: Migdal effect

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- Down to the MeV: Migdal effect
- Down to the keV: collective excitations

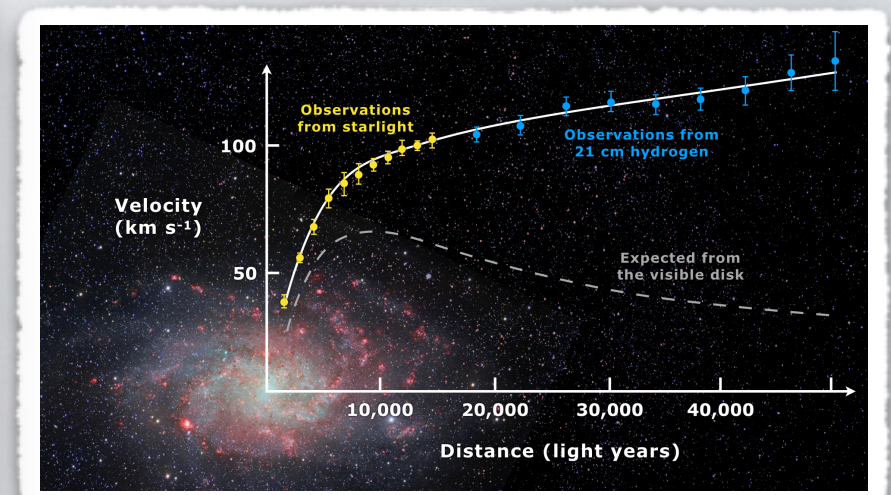
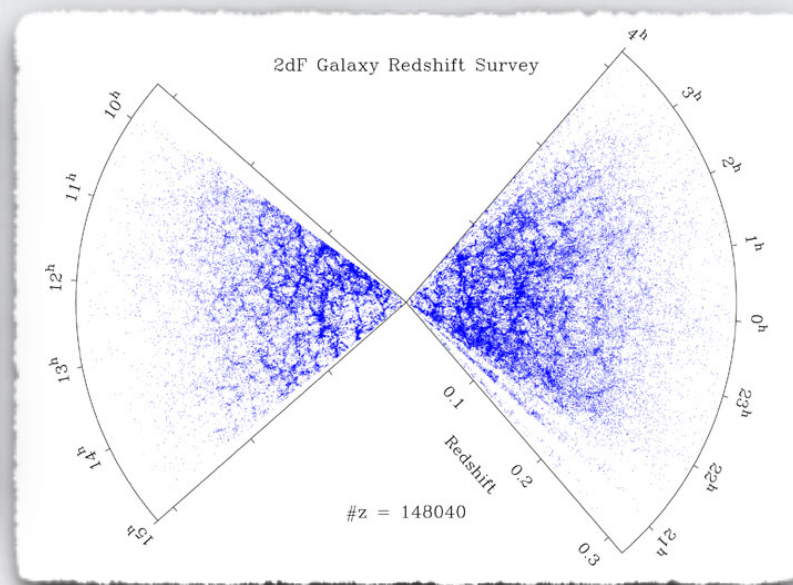
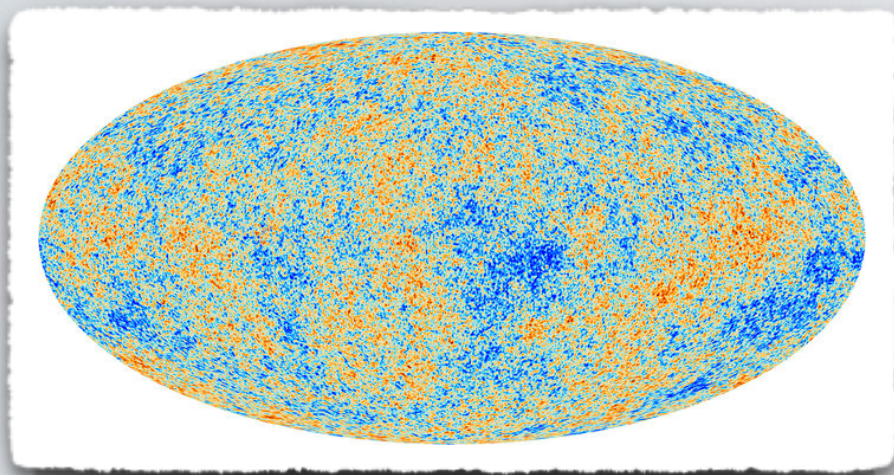
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- Searching for keV-MeV dark matter
- Down to the MeV: Migdal effect
- Down to the keV: collective excitations
- Outlook

SUB-GEV DARK MATTER

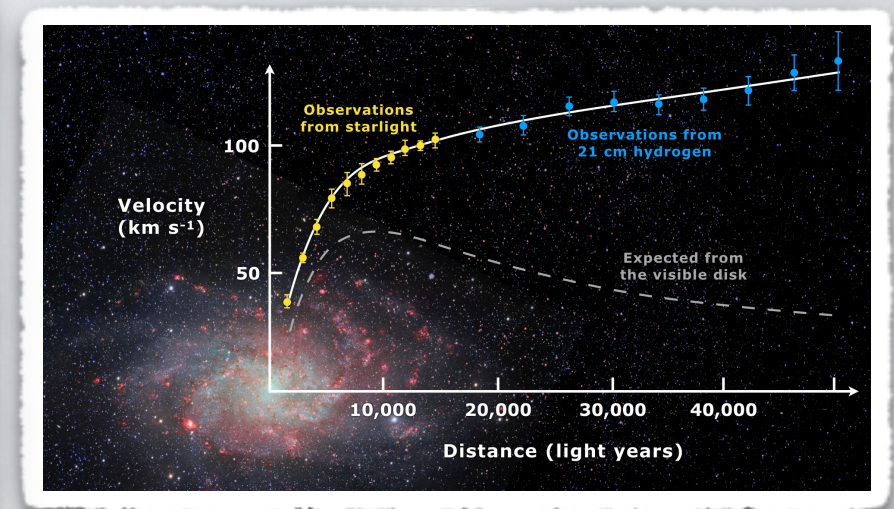
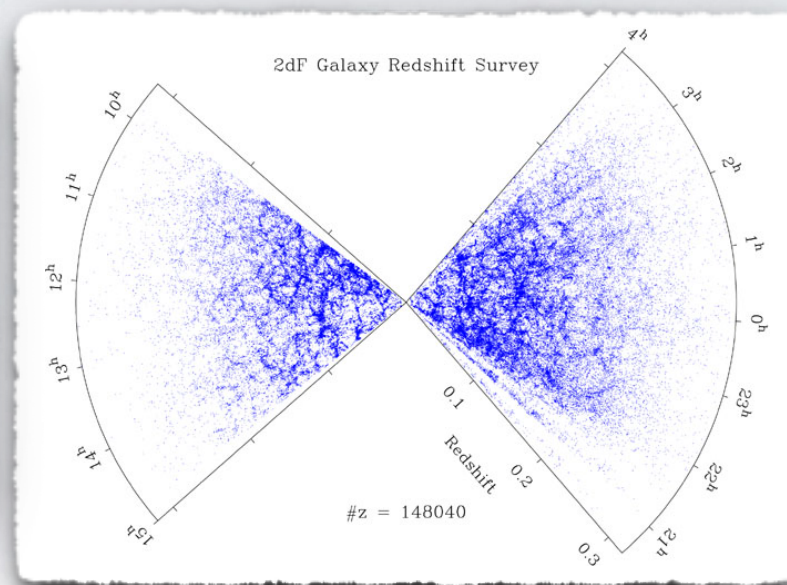
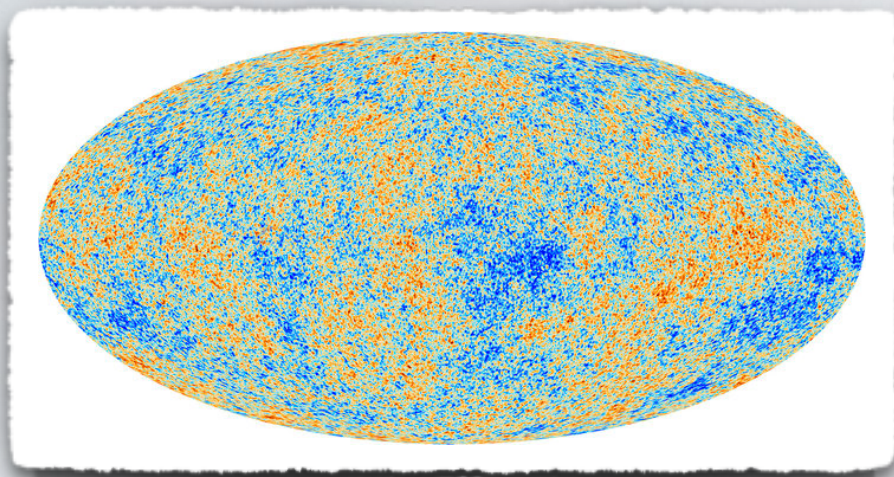
SUB-GEV DARK MATTER

- Most of the matter ($\sim 80\%$) that interacts gravitationally is dark



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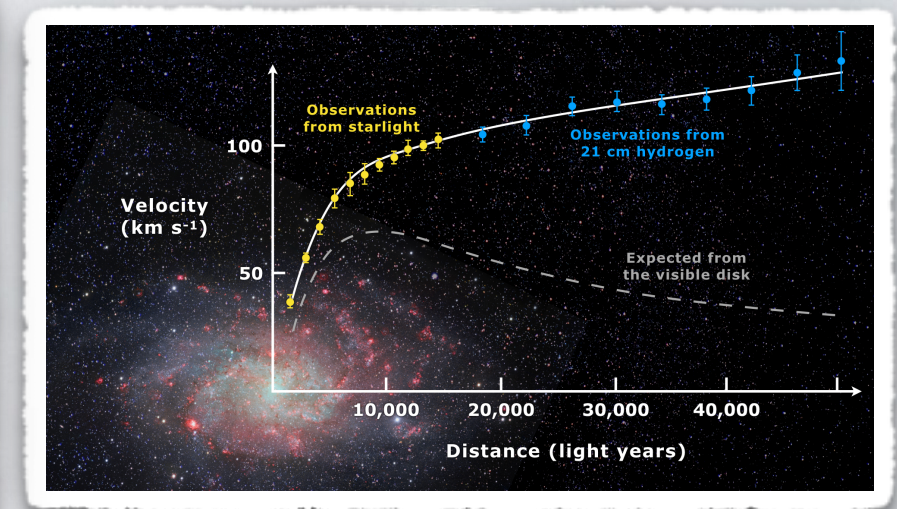
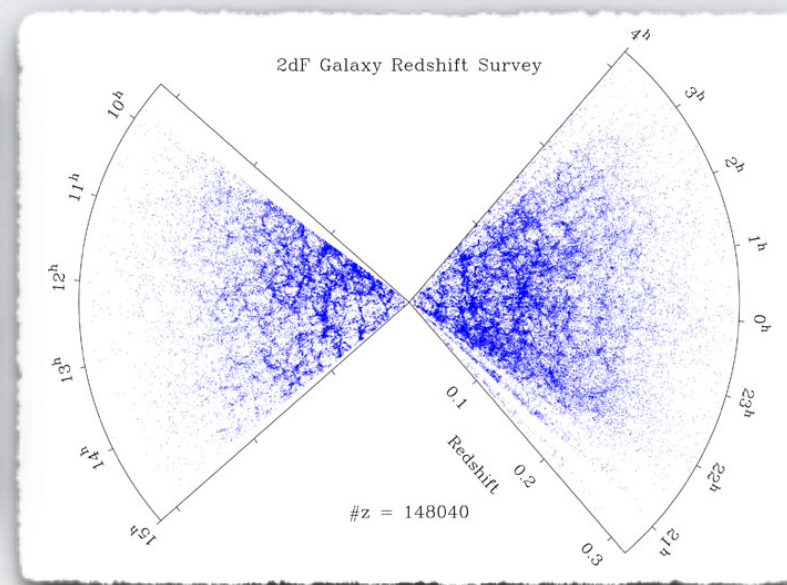
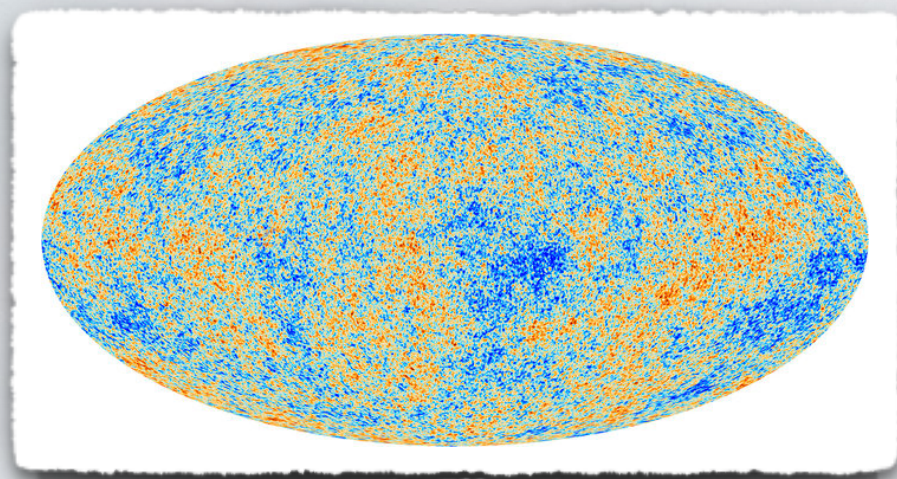
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- One of the strongest evidences for [physics beyond the Standard Model](#)

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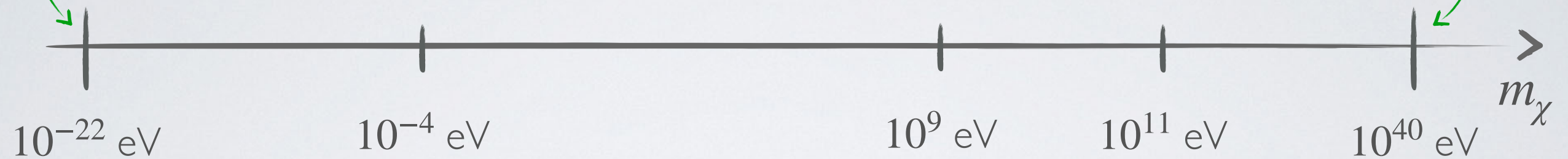
- One of the strongest evidences for physics beyond the Standard Model
- However... huge possible mass range → detection techniques vary widely depending on the dark matter mass

SUB-GEV DARK MATTER

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too light to explain halo structure

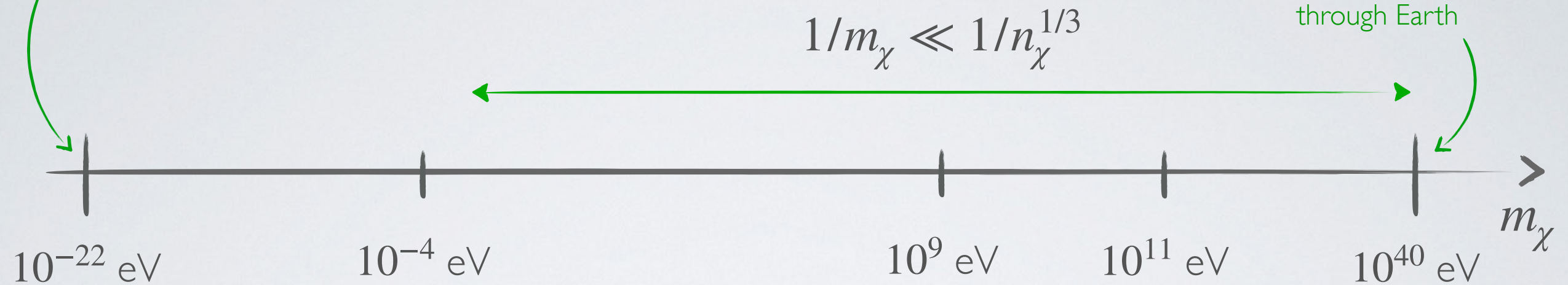
less than 1 dark matter per year through Earth



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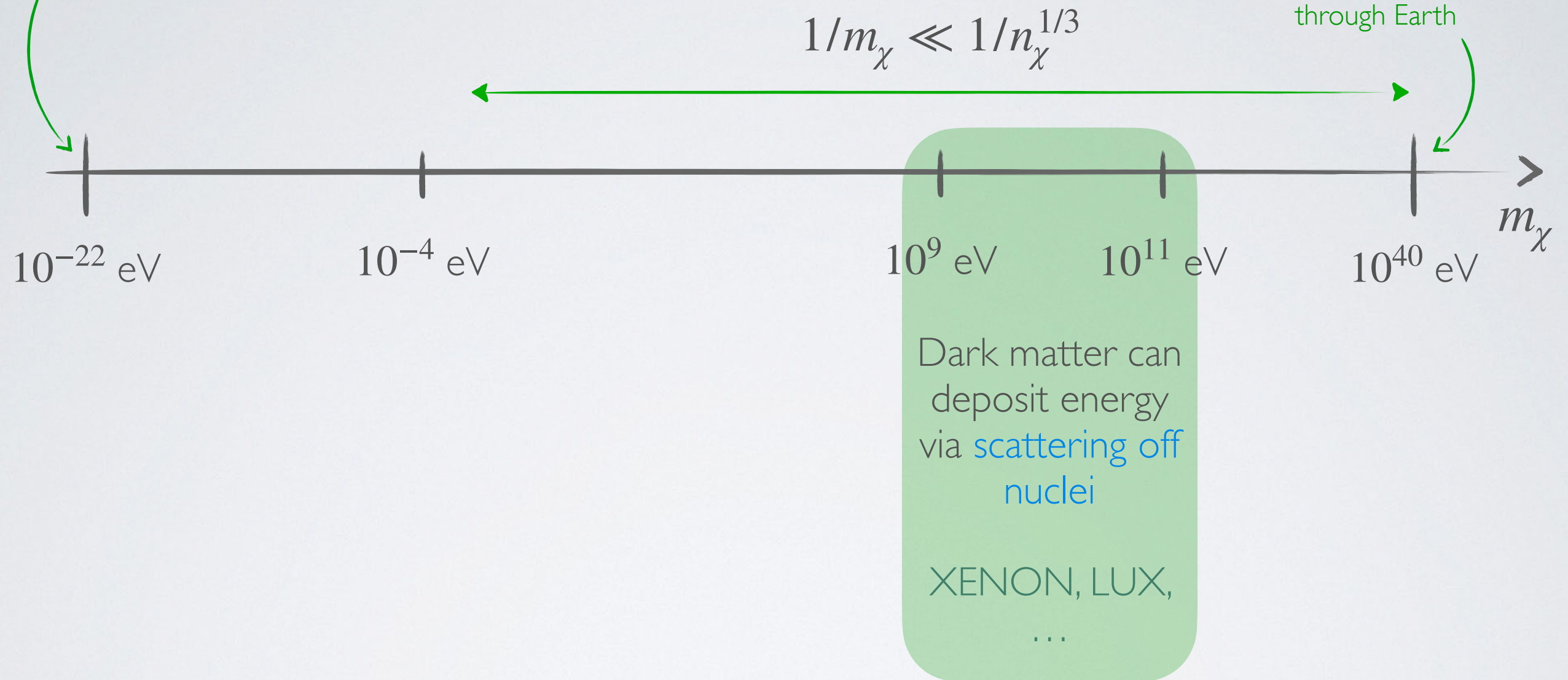
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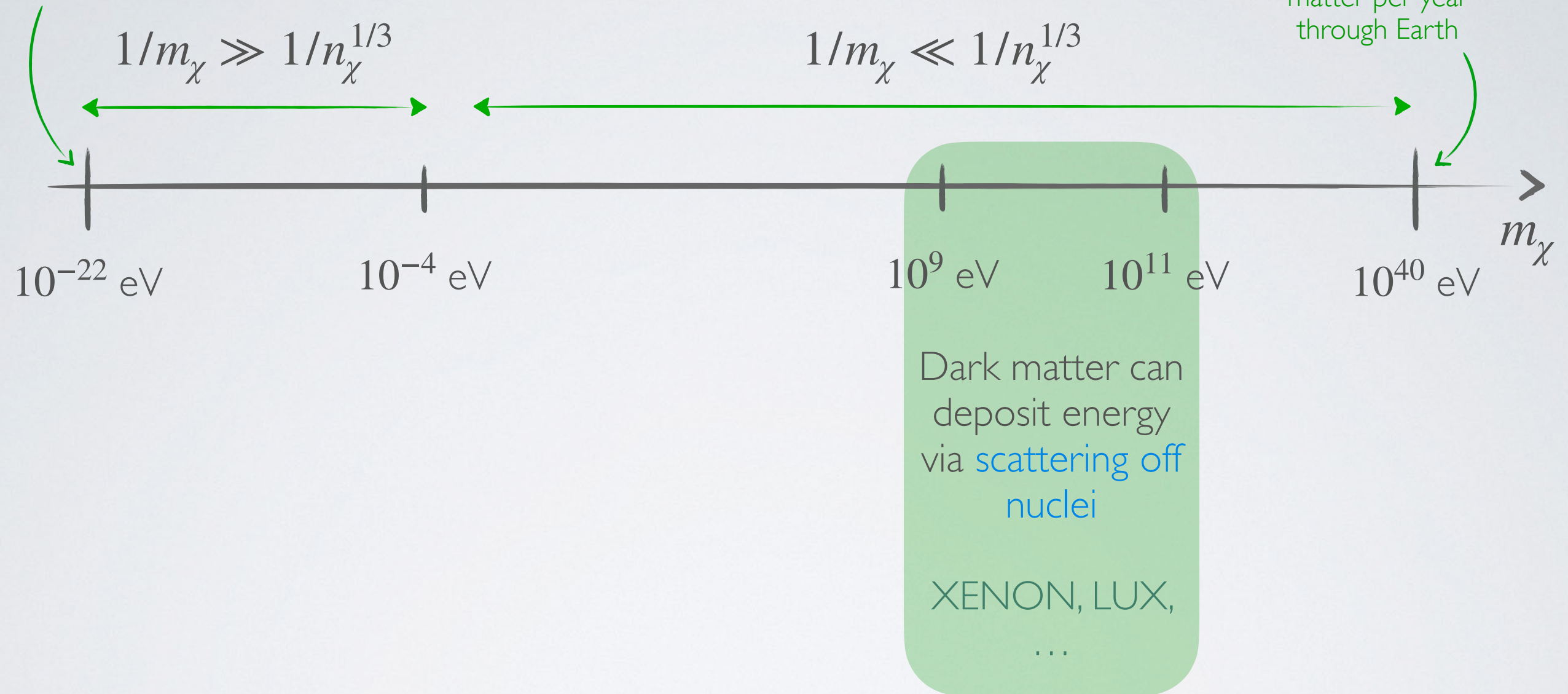
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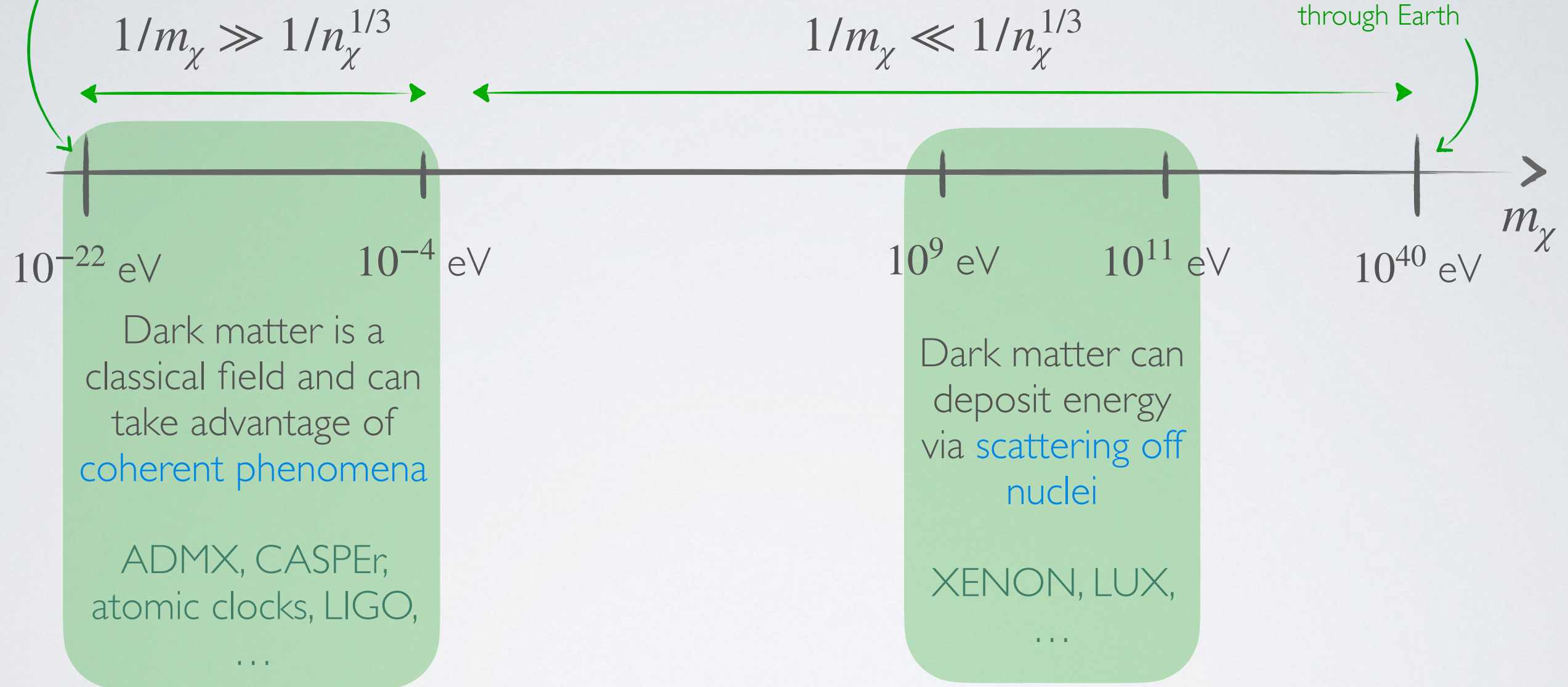
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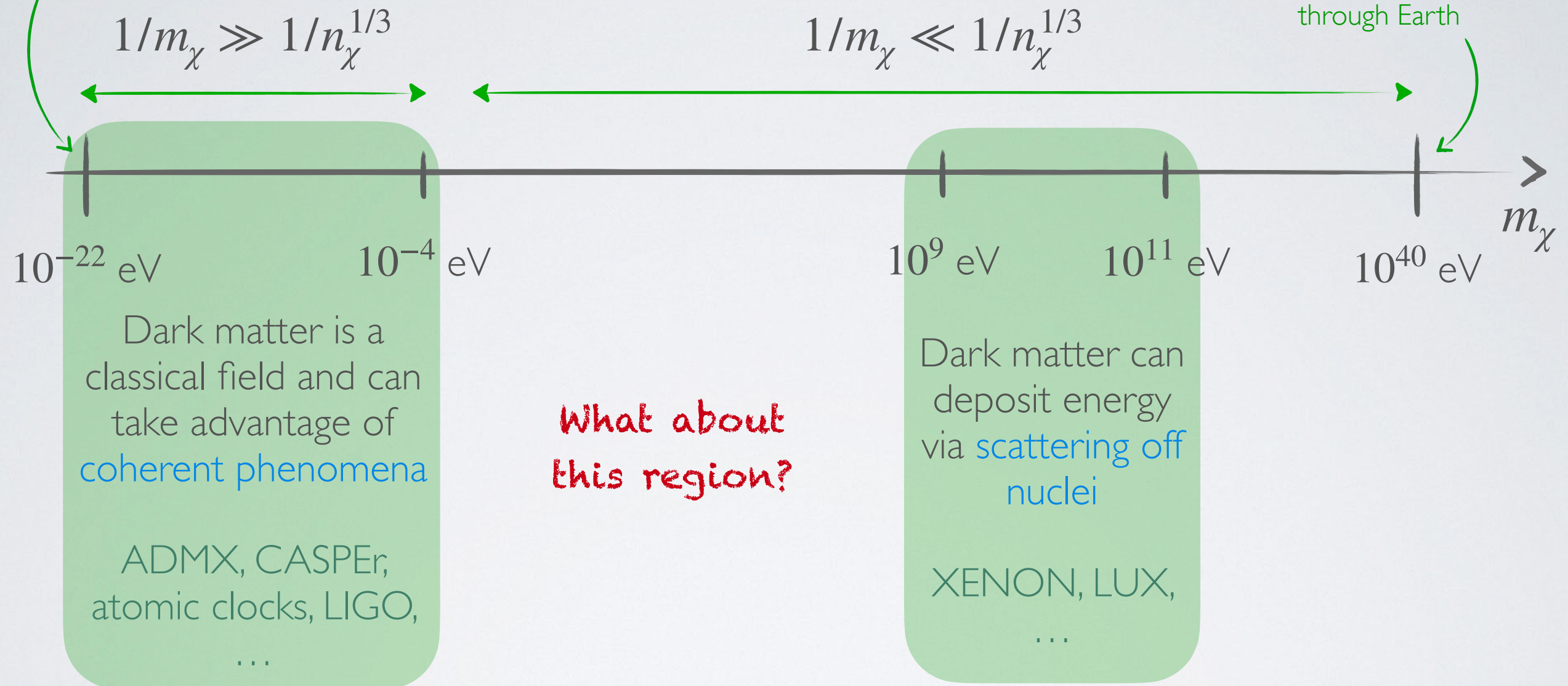
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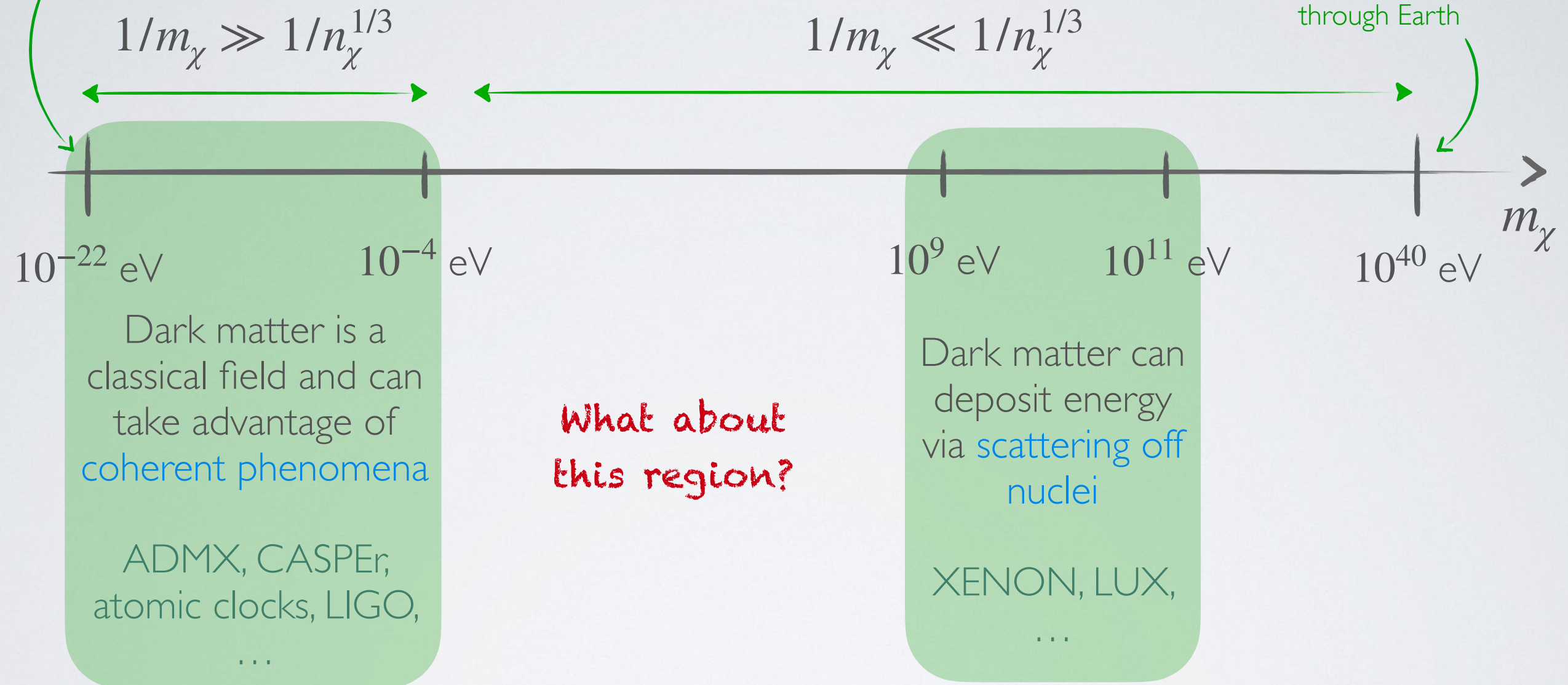
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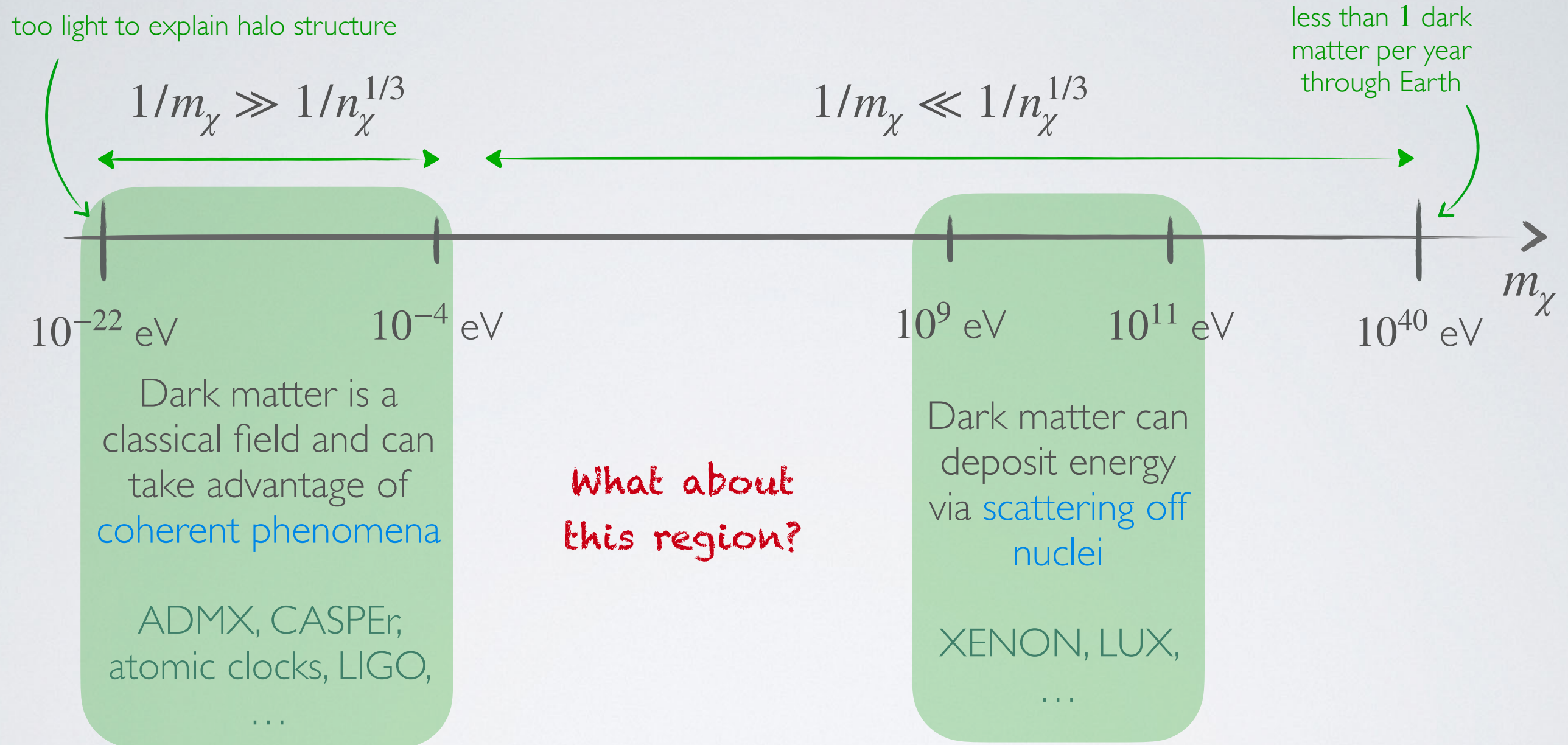
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- Dark matter is a particle but too light for nuclear recoil

SUB-GEV DARK MATTER



- Dark matter is a particle but too light for nuclear recoil
- Need new materials or observables

SUB-GEV DARK MATTER

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- For an [elastic scattering](#), it must be

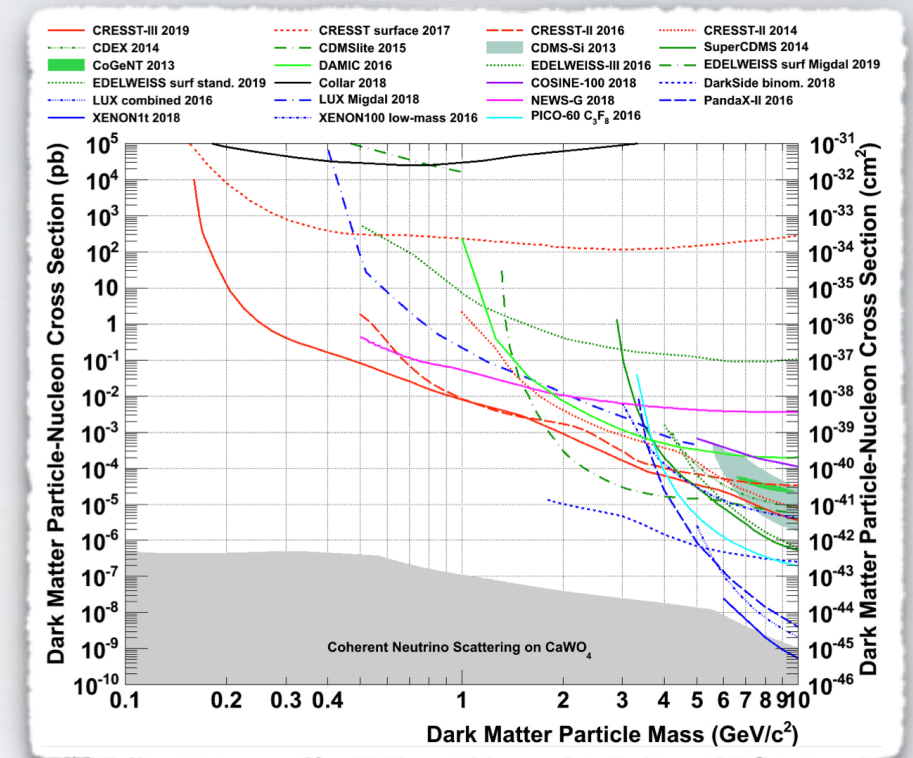
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- For $m_\chi \lesssim 1$ GeV elastic scattering off nuclei is very inefficient



[CRESST – PRD 2019, 1904.00498]

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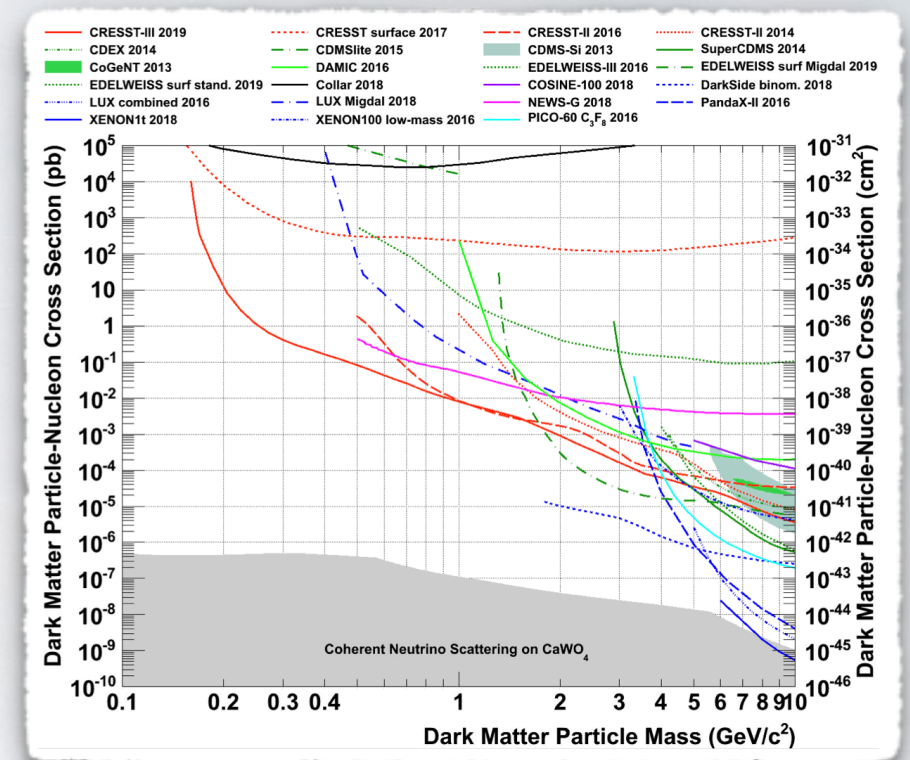
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- Two possibilities:

- Look into lighter scattering targets
- Look into inelastic processes

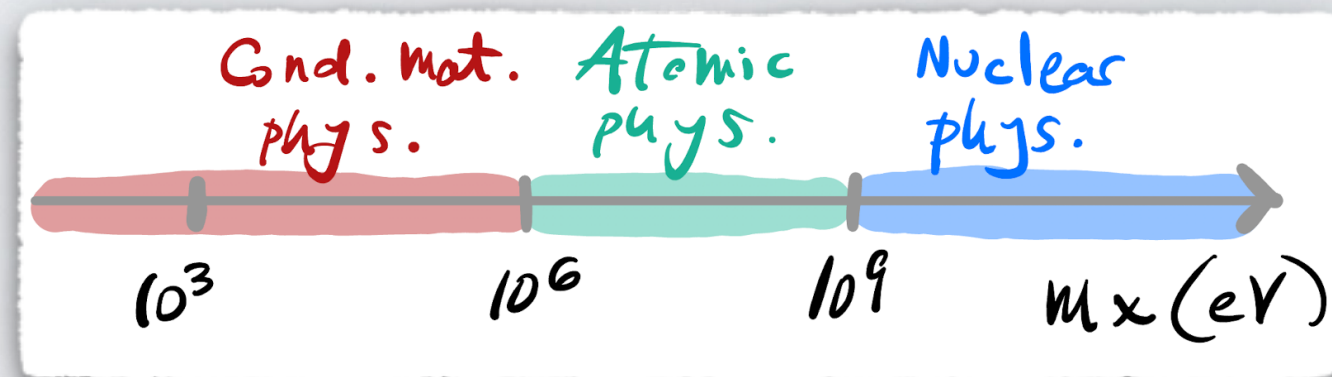


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NASTY STUFF

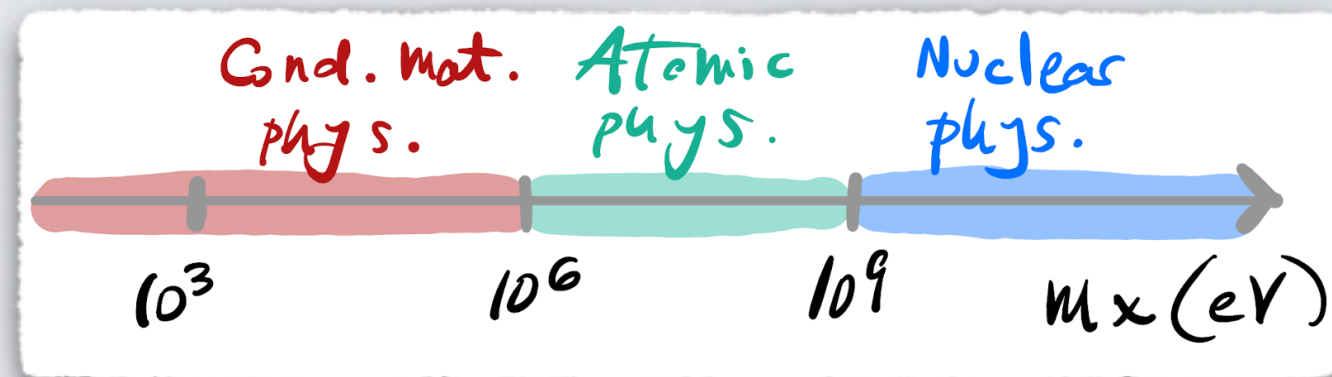
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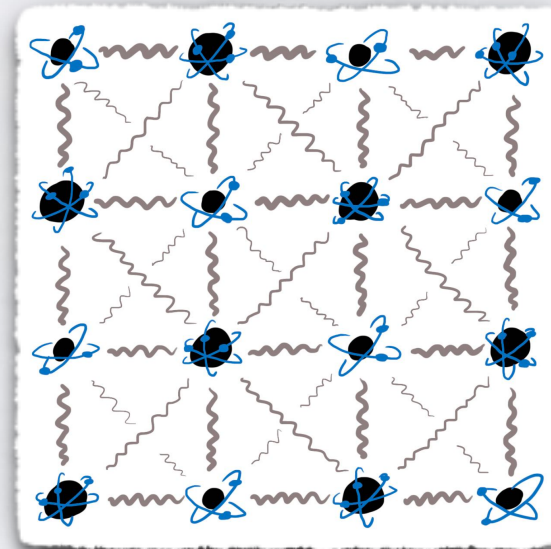


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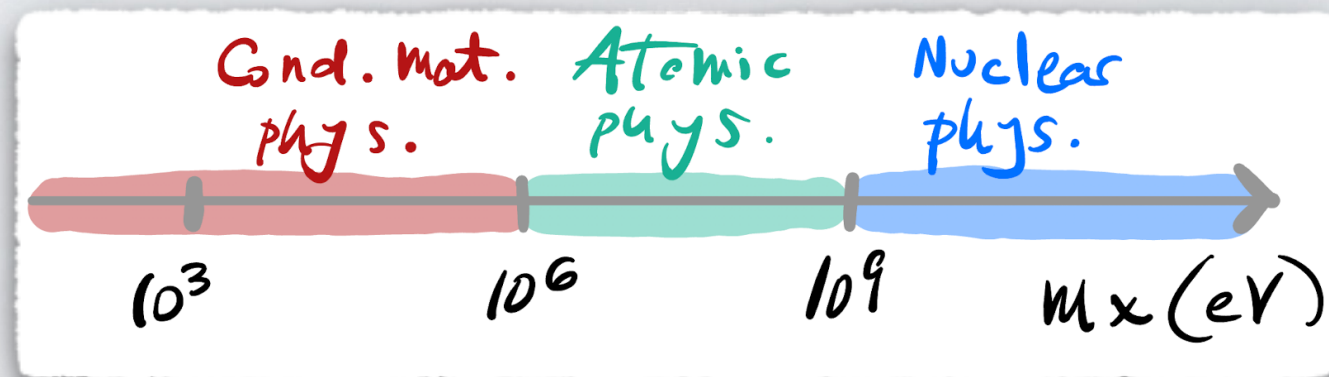


- Need to **account for the complicated many-body physics** (correlations, strong coupling, ...)

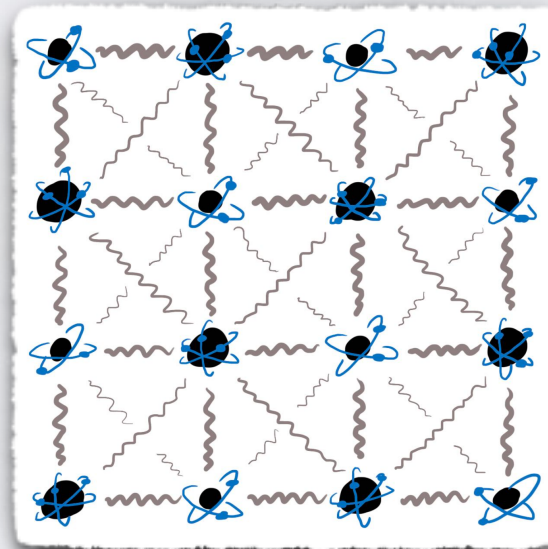


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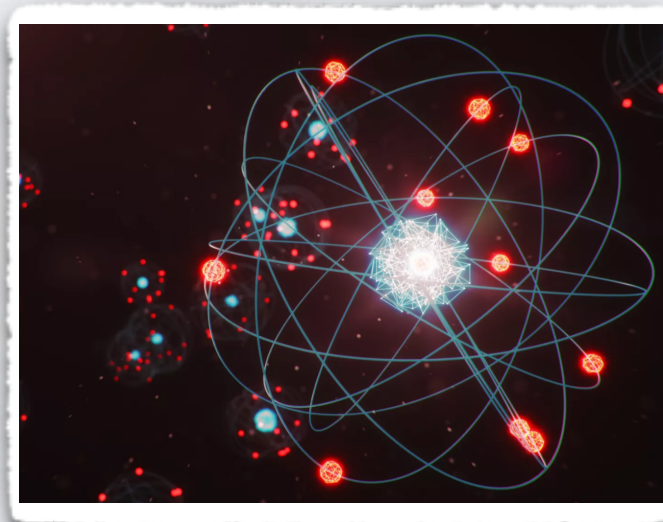


- Need to **account for the complicated many-body physics** (correlations, strong coupling, ...)
- Need to find theoretical tools** that allow to solve or bypass these problems (measured correlation functions, EFTs, ...)



Down to the MeV

Migdal effect in semiconductors



MIGDAL EFFECT

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- For sub-GeV dark matter nuclear recoil signals become challenging
→ sensitivity can be lowered by [looking for inelastic processes](#)

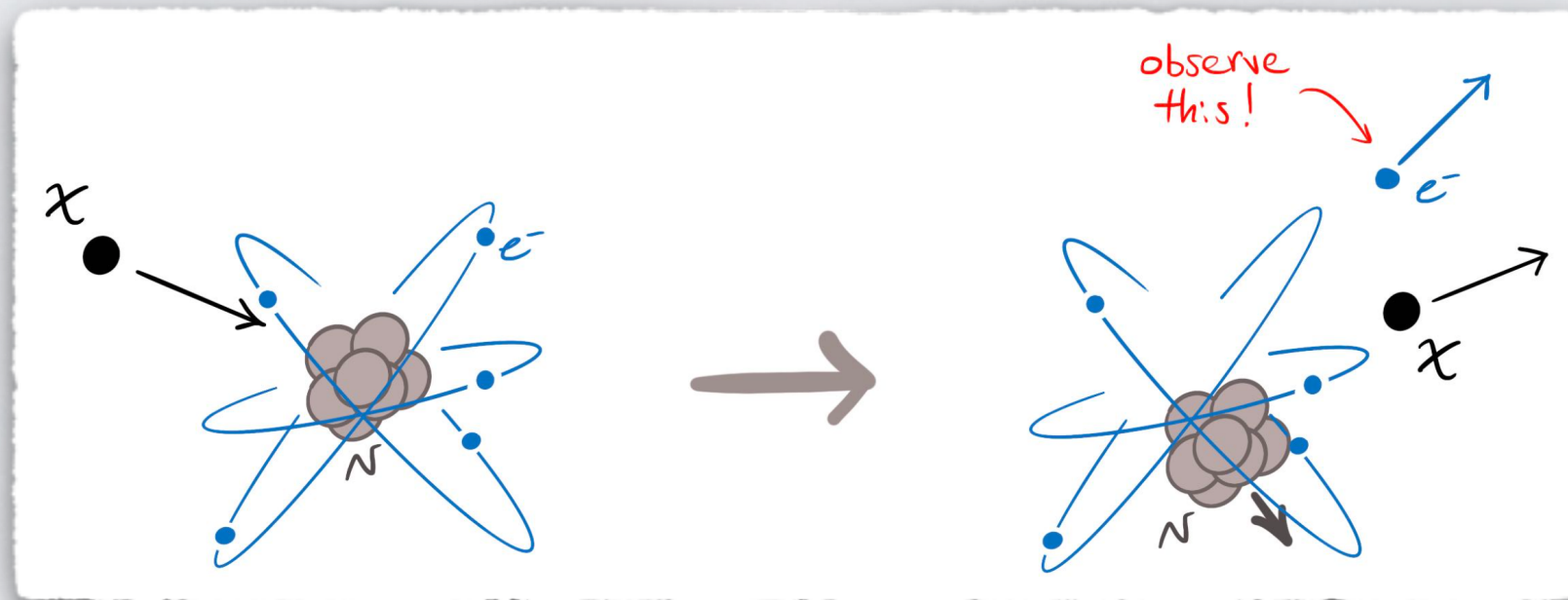
[e.g., Essig, Mardon, Volansky – PRD 2012, 1108.5383; Kouvaris, Pradler – PRL 2017, 1607.01789]

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- Hadrophilic dark matter on free nuclei → **Migdal effect**

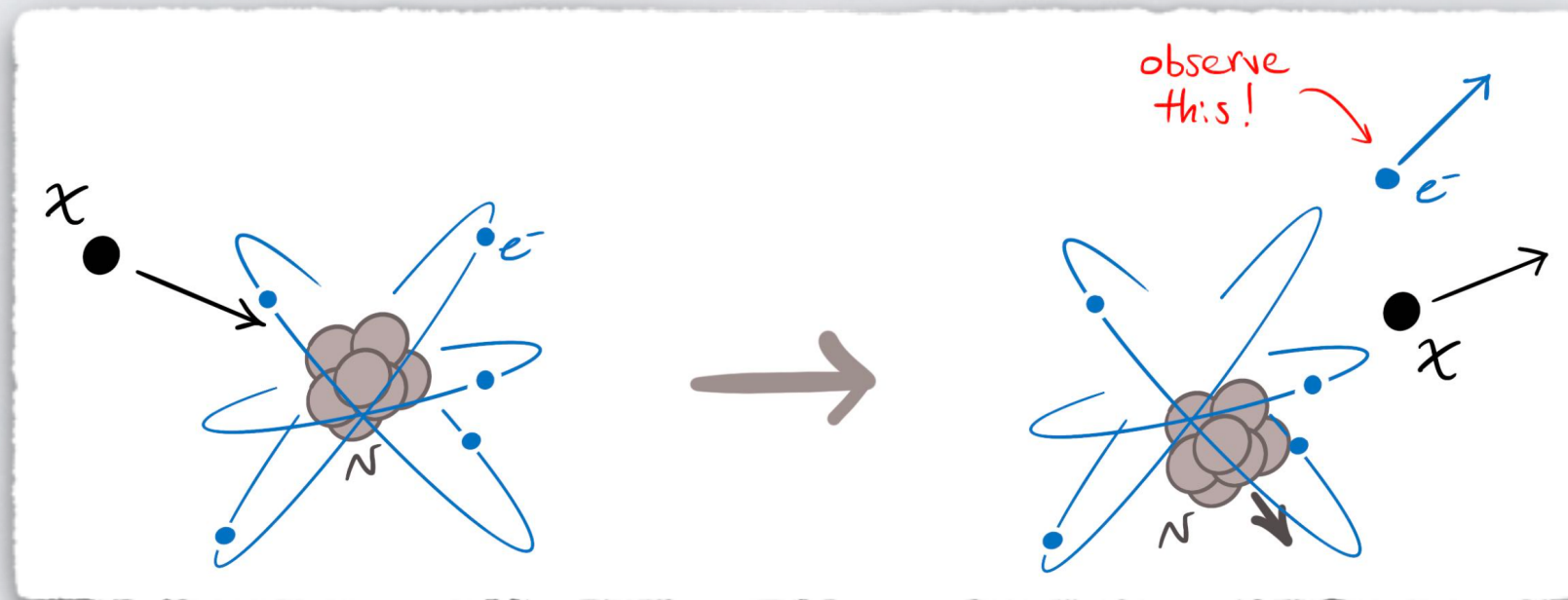


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- Less likely... but lower threshold! → sensitivity **down to**

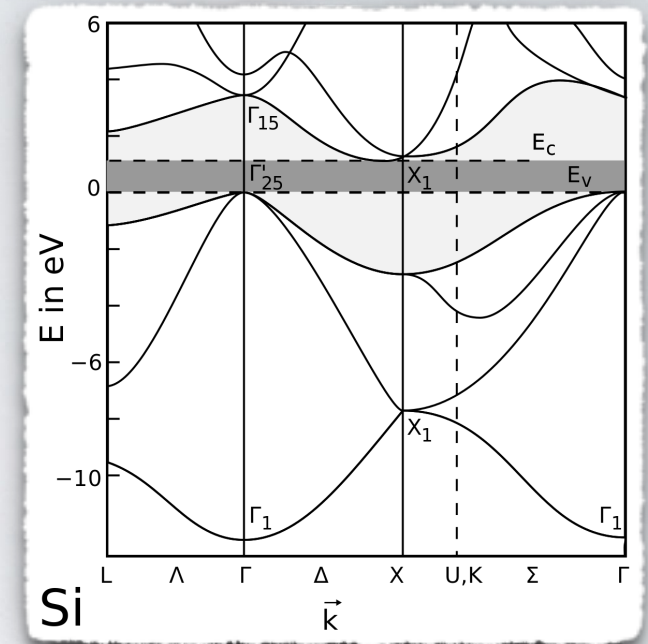
$\mathcal{O}(100 \text{ MeV})$ masses (see Giovanni's talk)

[e.g., Ibe, Nakano, Shoji, Suzuki – JHEP 2018, 1707.07258; DarkSide – 2207.11967]

MIGDAL EFFECT

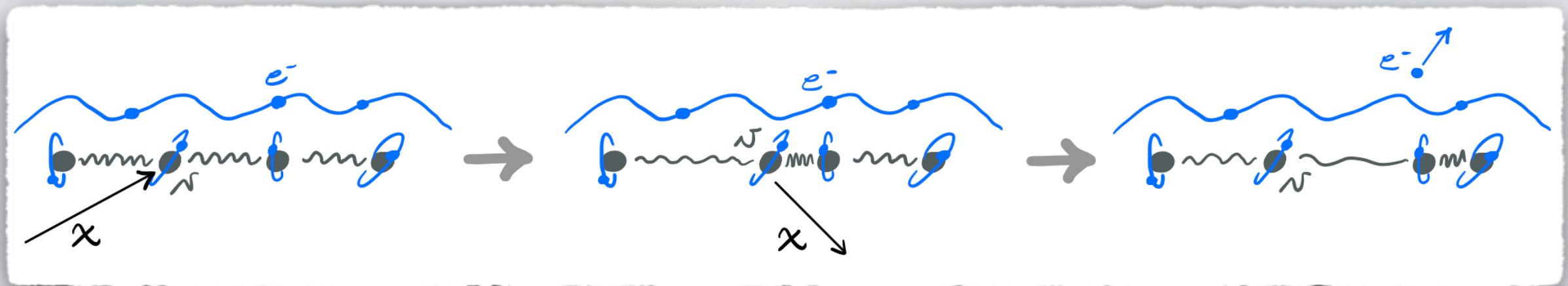
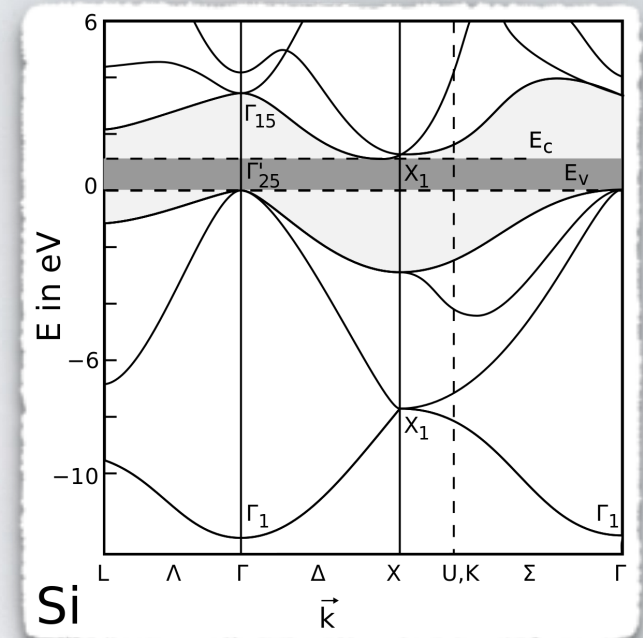
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- Semiconductors (Si, Ge, ...) have small $\mathcal{O}(\text{eV})$ bandgaps $\rightarrow$ Migdal effect should allow to probe down to $\mathcal{O}(\text{MeV})$ masses



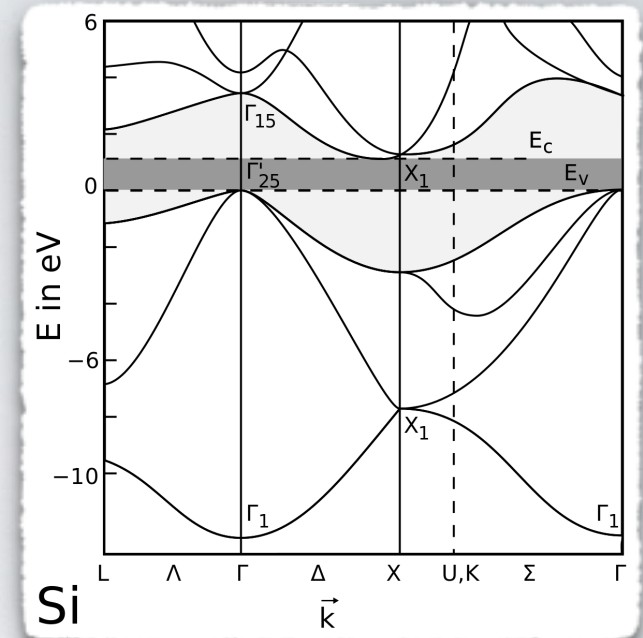
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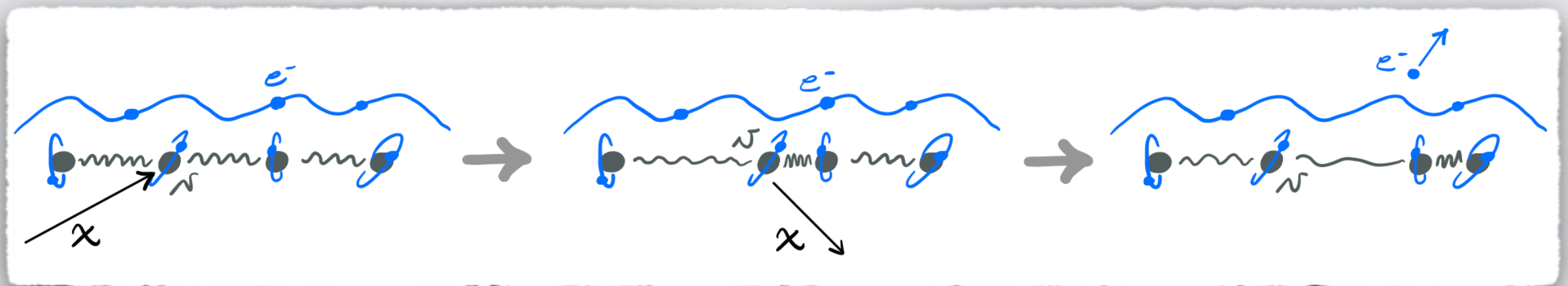


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- How to describe nucleus-nucleus and nucleus-electron interactions in a strongly correlated system?

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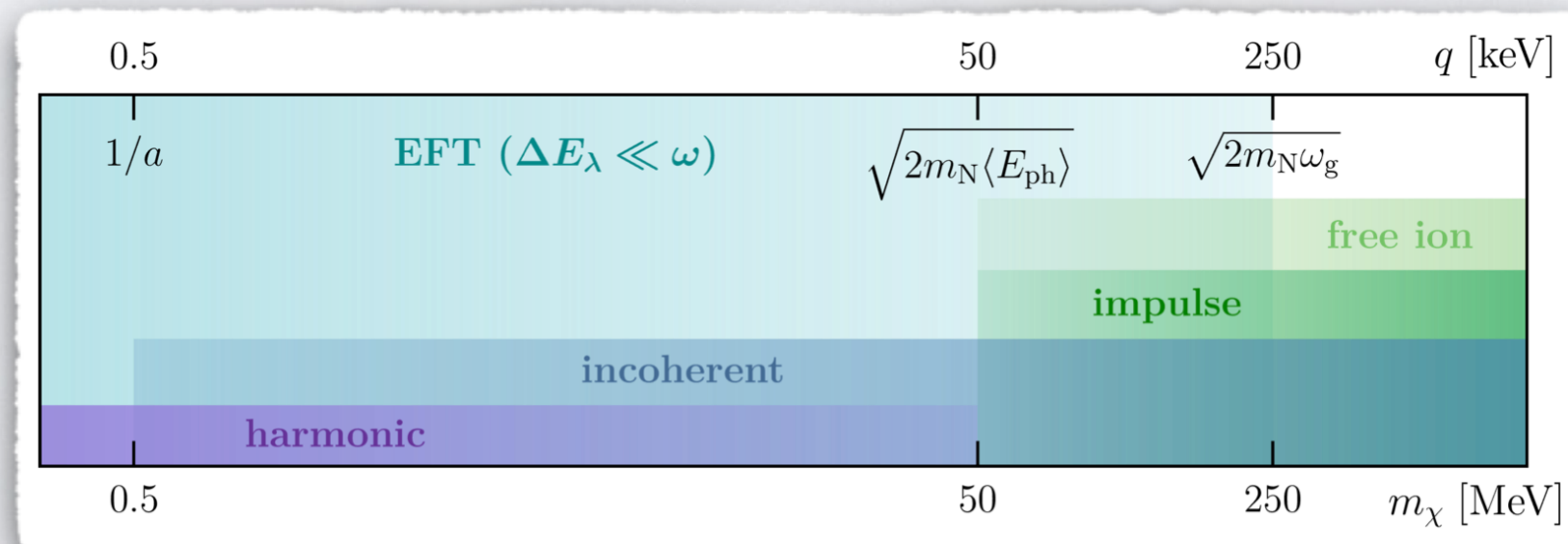
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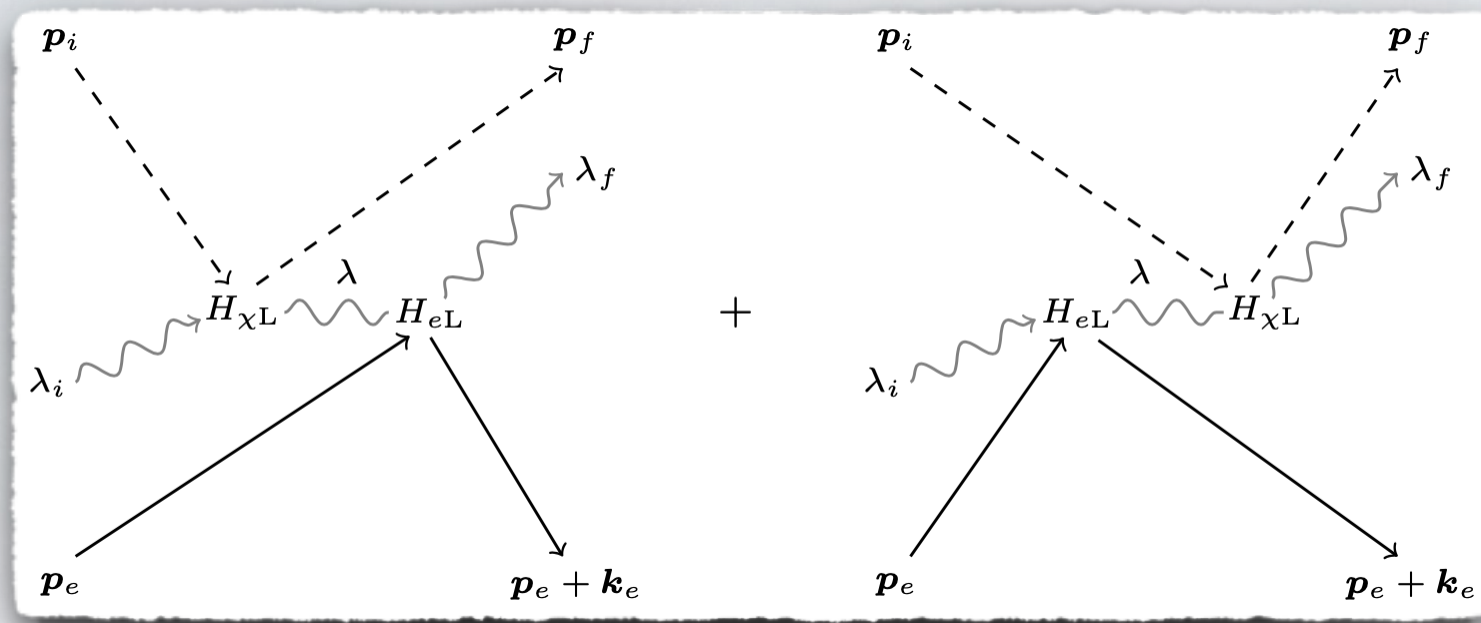
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EFT

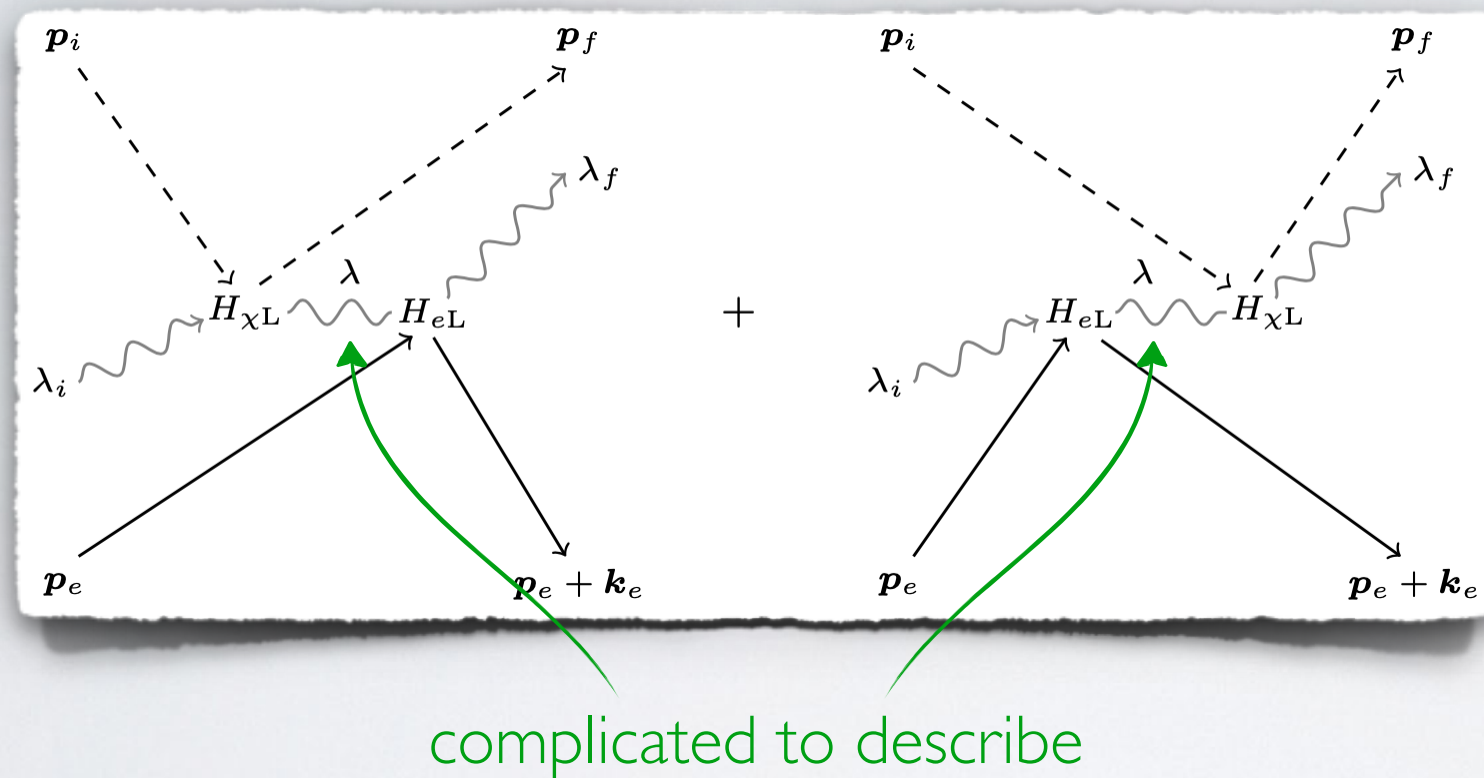
EFT

- Migdal effect in old-fashioned perturbation theory



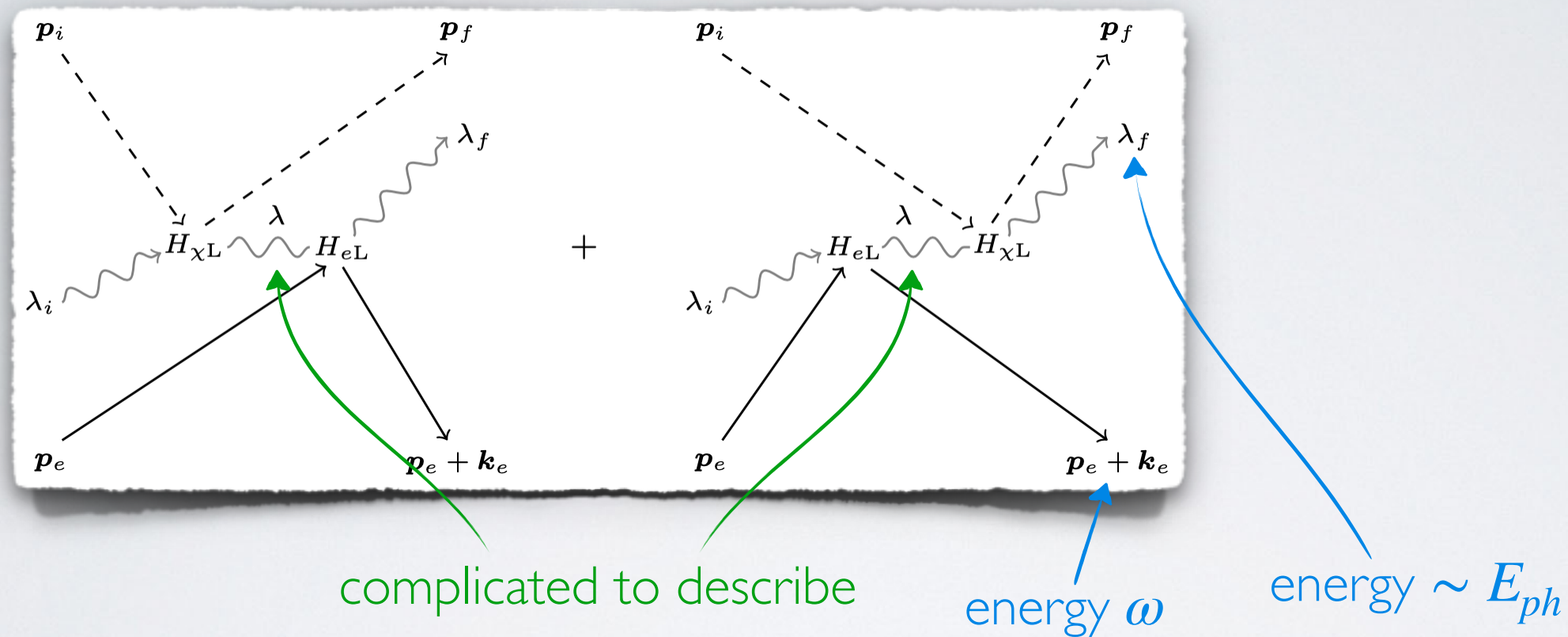
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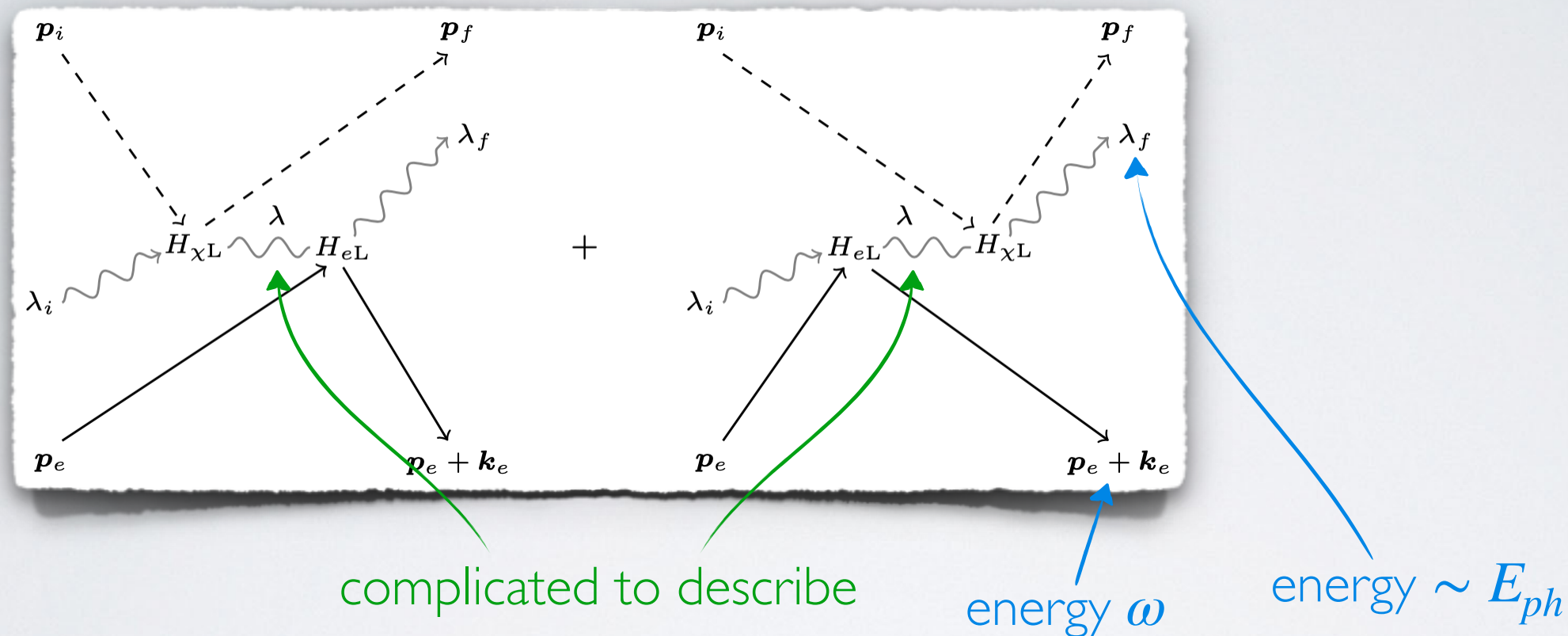
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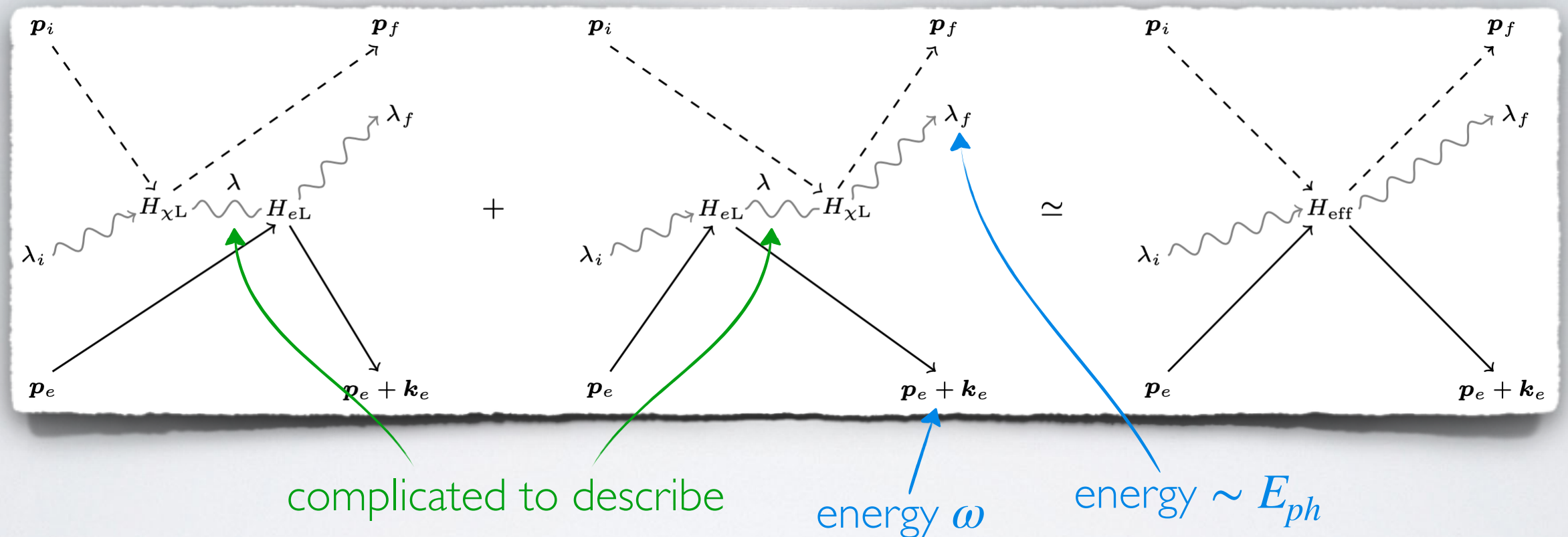
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- Separation of scales ($\omega \sim \text{eV} \gg E_{ph} \sim 10 \text{ meV}$) allows to integrate out the intermediate lattice mode

EFT

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$$H_{eff} = \frac{1}{m_N \omega^2} \vec{\nabla} H_{\chi L} \cdot \vec{\nabla} H_{eL} + \mathcal{O}\left(\frac{1}{\omega^3}\right)$$

[Berghaus, **AE**, Essig, Sholapurkar – JHEP 2020, 2210.06490]

MIGDAL RATE

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- Now simple to determine the [rate for Migdal emission](#)

$$\frac{d^2\Gamma}{d\omega dE_{ph}} \propto \sum_{\mathbf{k}} \sum_{\mathbf{K}, \mathbf{Q}} \frac{\mathbf{q} \cdot (\mathbf{k} + \mathbf{K}) \mathbf{q} \cdot (\mathbf{k} + \mathbf{K})}{|\mathbf{k} + \mathbf{K}| |\mathbf{k} + \mathbf{Q}|} \text{Im}(-\epsilon_{\mathbf{KQ}}^{-1}(\mathbf{k}, \omega)) S(\mathbf{q} - \mathbf{k} - \mathbf{K}, E_{ph})$$

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- Energy loss function** is already well studied

[e.g., Knapen, Kozaczuk, Lin — PRD 2021, 2101.08275; Hochberg et al. — PRL 2021, 2101.08263; Knapen, Kozaczuk, Lin — PRD 2022, 2104.12786]

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structure factor — crystal response

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- No data yet** in the range of interest ($q \simeq 10 \text{ keV} - 100 \text{ keV}$)

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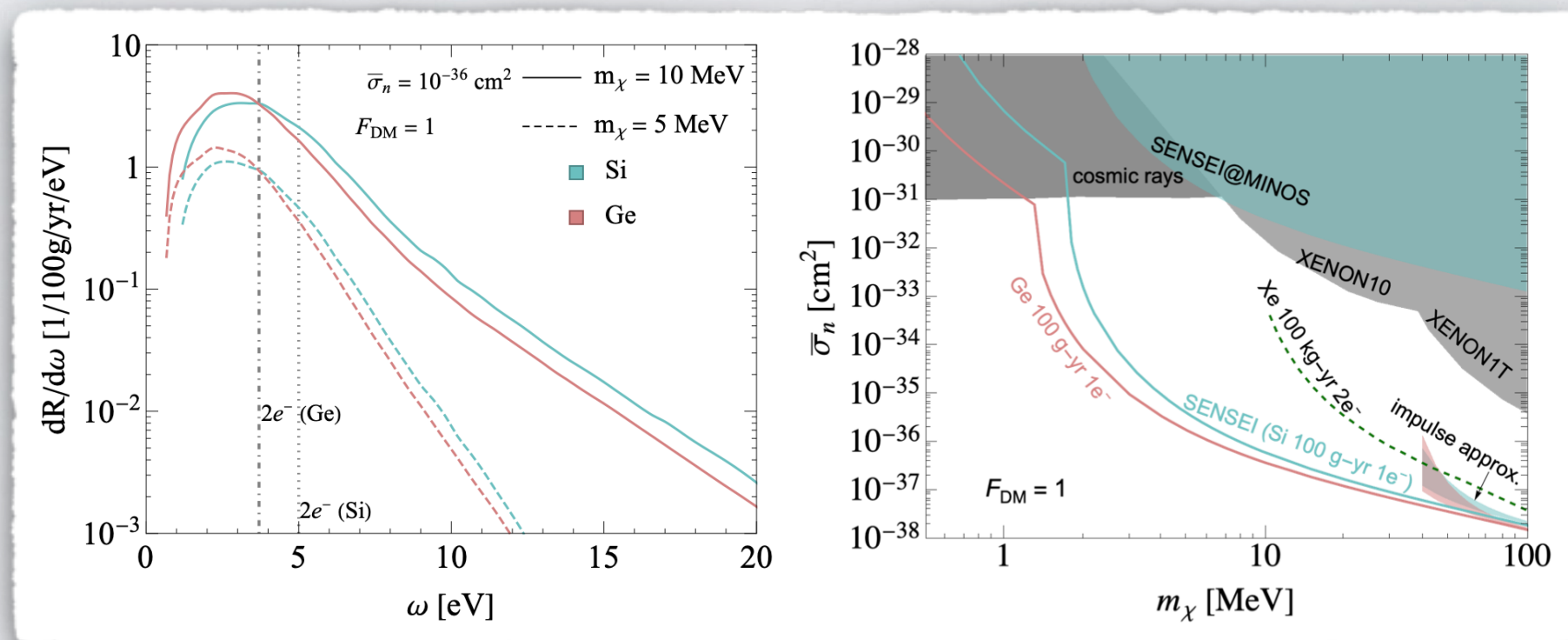
- If **only** interested in electron energy, the rate is **independent** on the details of the crystal lattice

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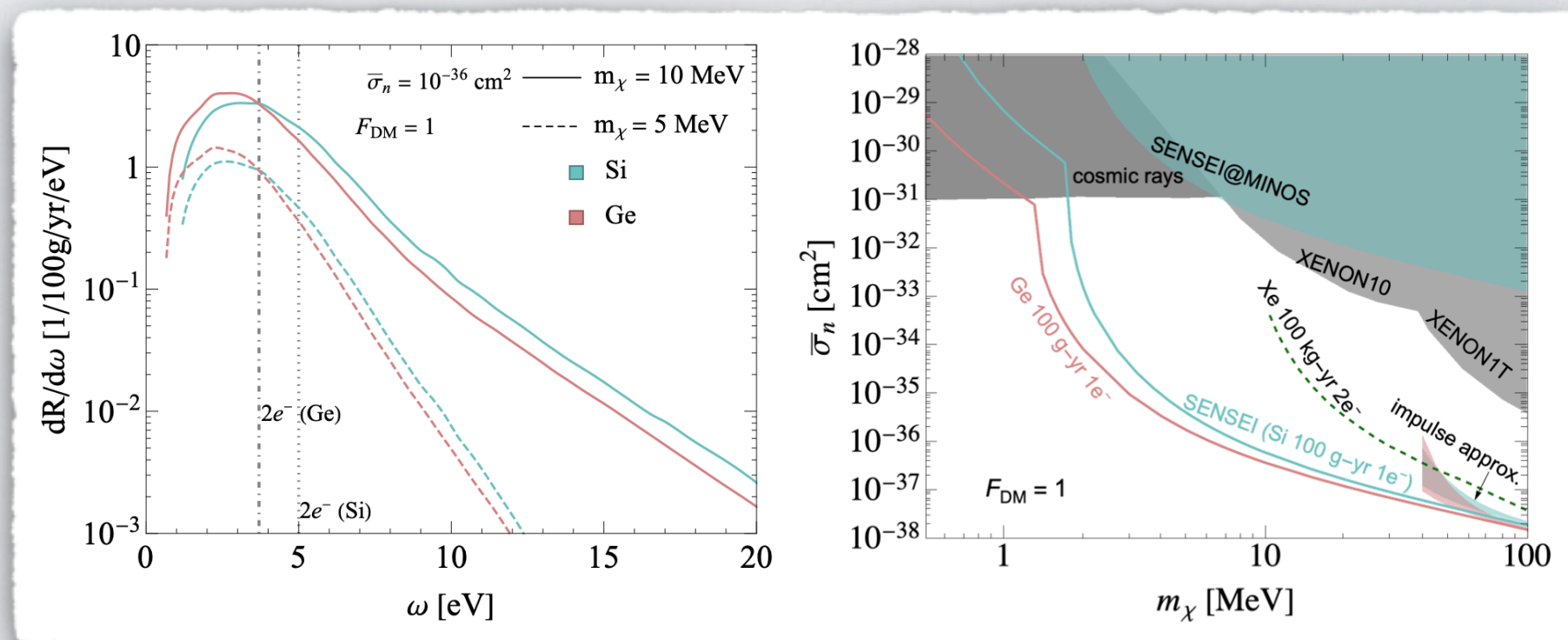


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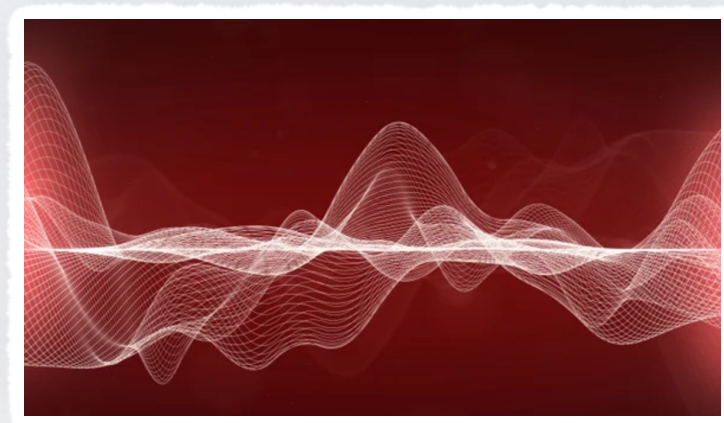
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- The description of Migdal effect in semiconductor is now complete

Down to the keV collective excitations



COLLECTIVE EXCITATIONS

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- For $m_\chi \lesssim \mathcal{O}(\text{MeV})$, dark matter scattering can transfer a momentum

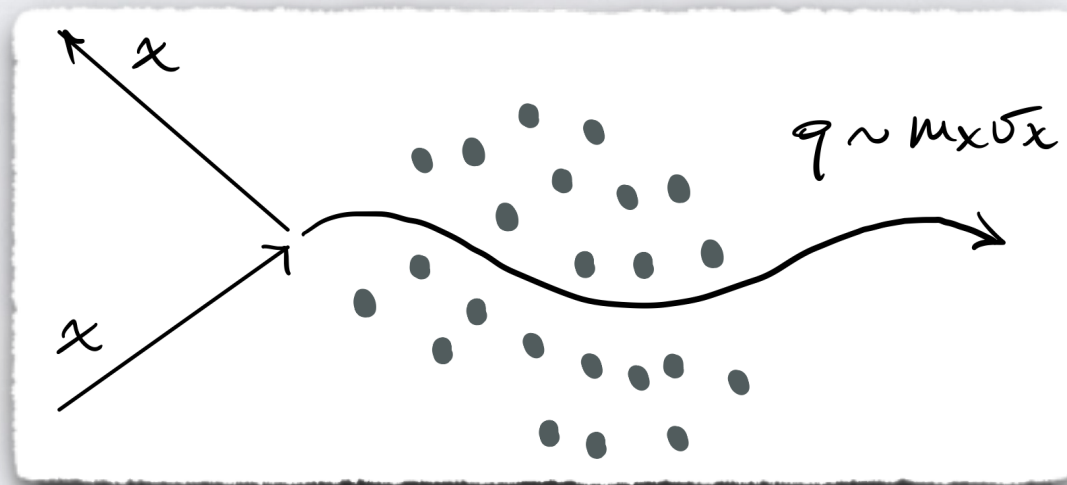
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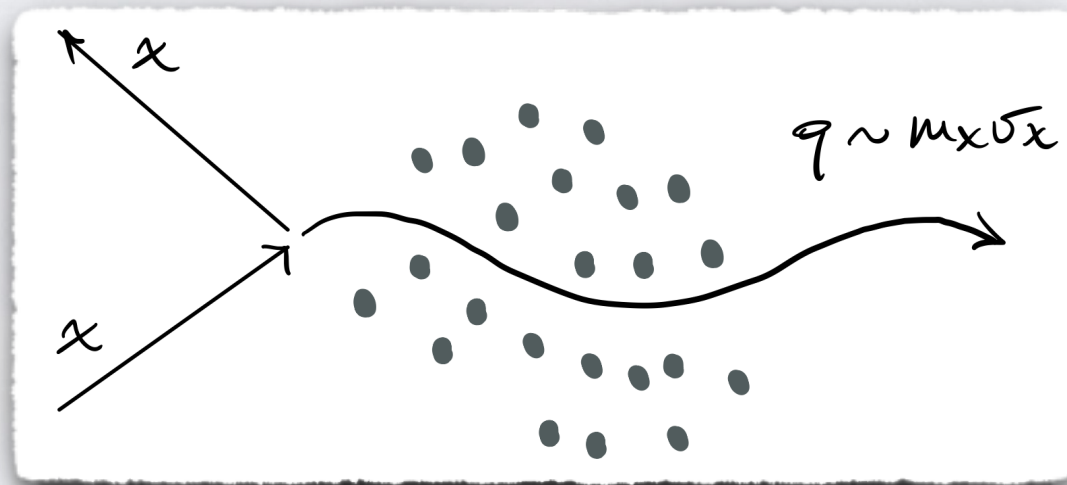


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- Typically, no more single particle final states $\rightarrow$ signatures involve collective excitation
- [see e.g., Trickle et al. – JHEP 2020, 1910.08092; Griffin et al. – PRD 2020, 1910.10716; Coskuner et al. – PRD 2022, 2102.09567]

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- I will focus on those I know best...

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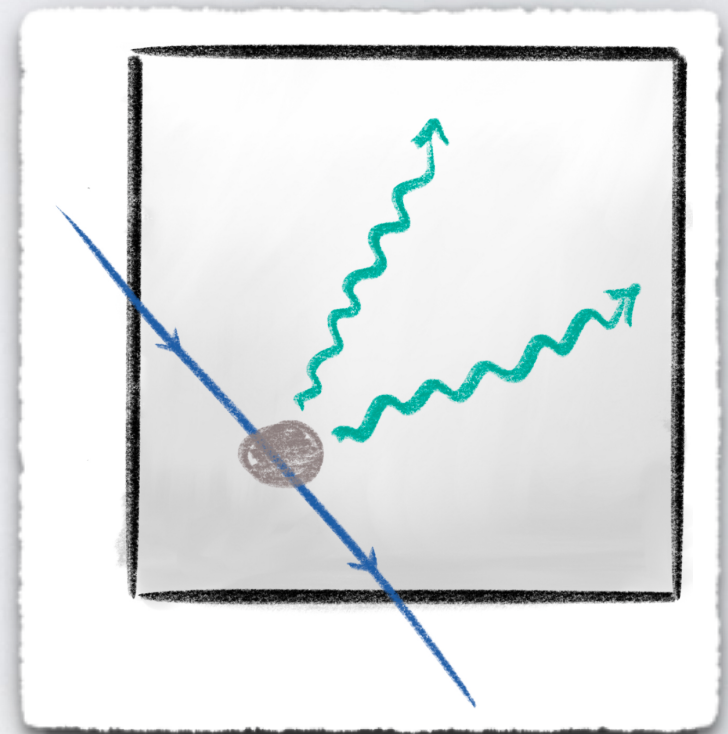
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- Idea: look for events where the dark matter produces more than one phonon

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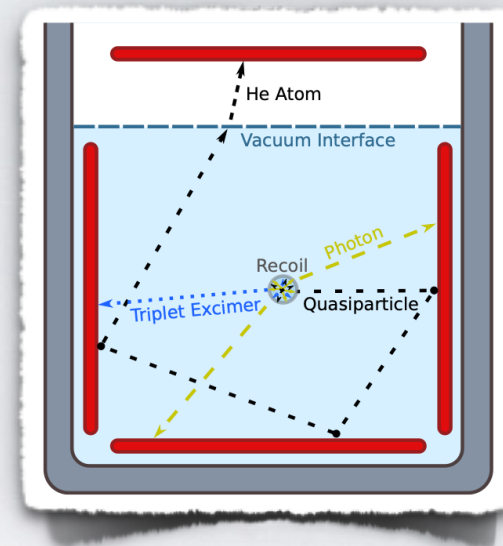
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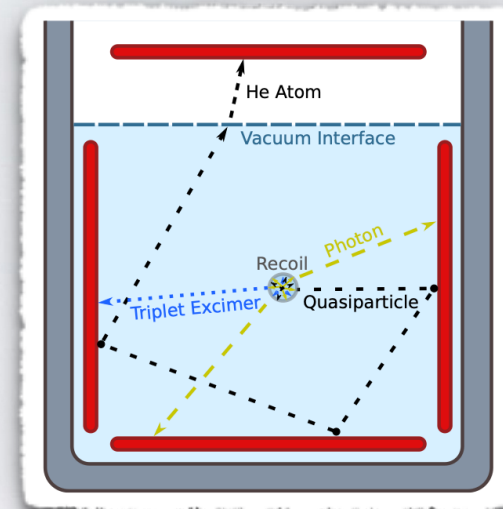


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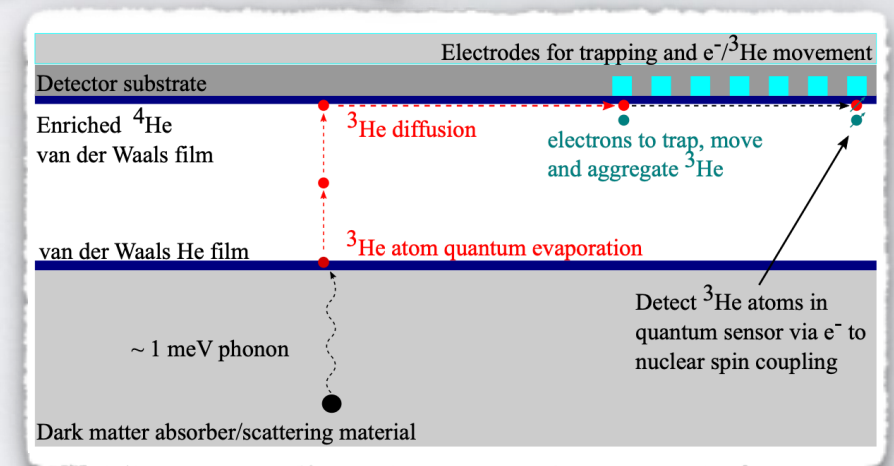
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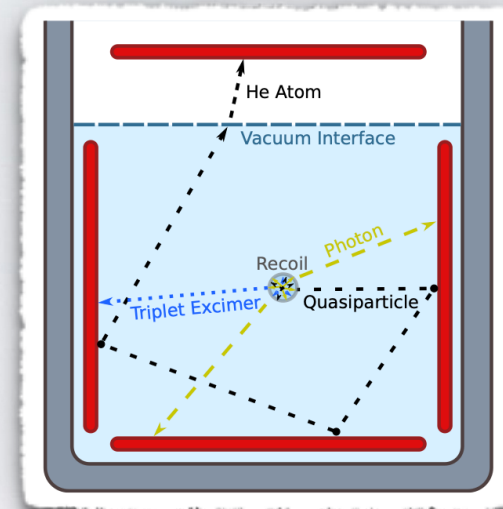


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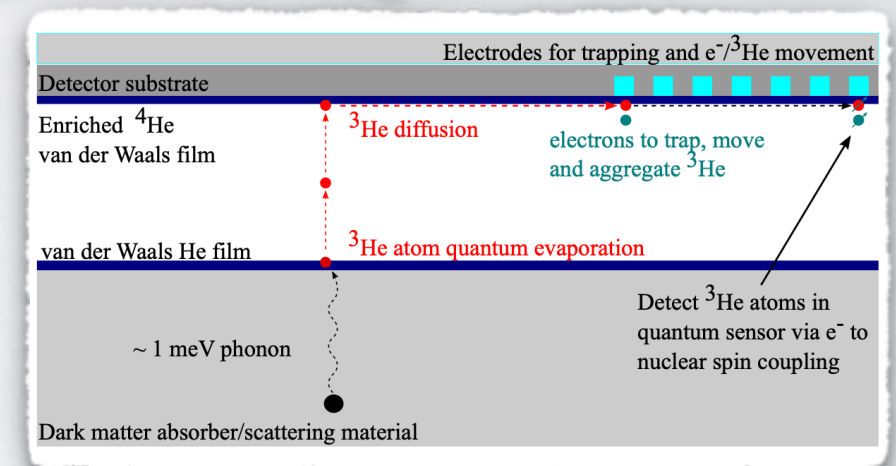
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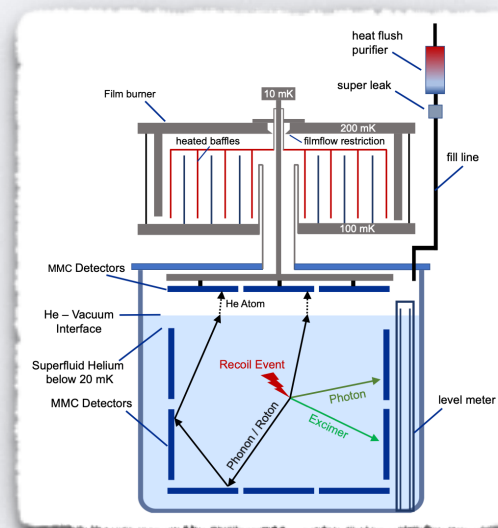
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3. DELight

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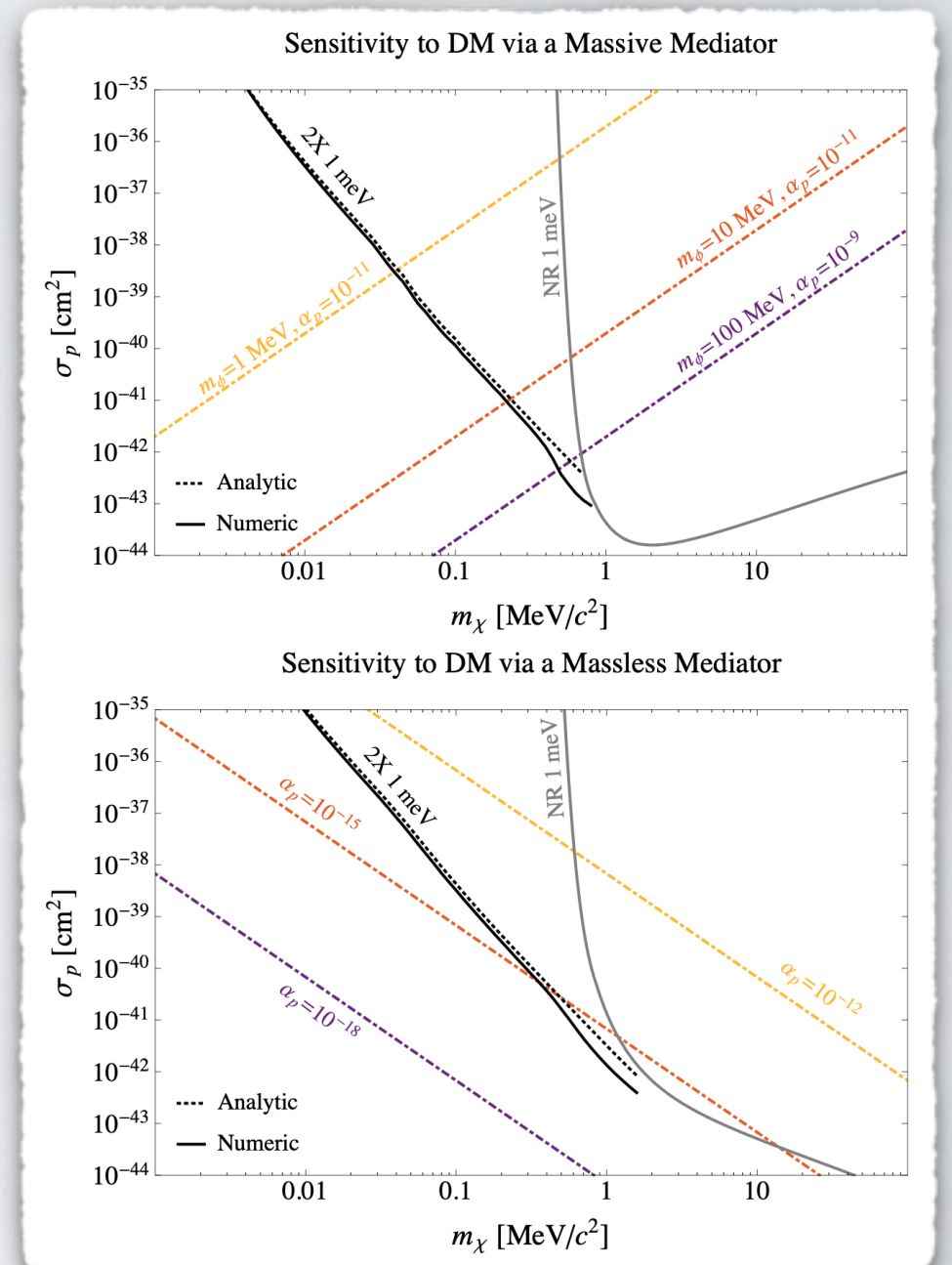
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$$\frac{d^2\Gamma}{d\omega dq} = \frac{\rho_{\text{He}} \sigma_{\chi n} q}{2m_\chi m_{\text{He}} p_i} S(q, \omega)$$

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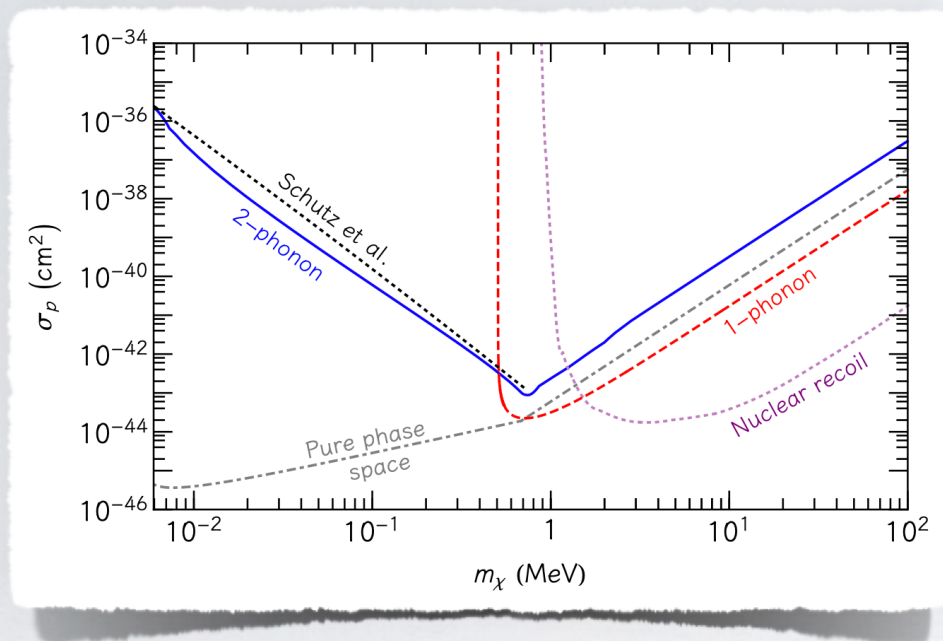
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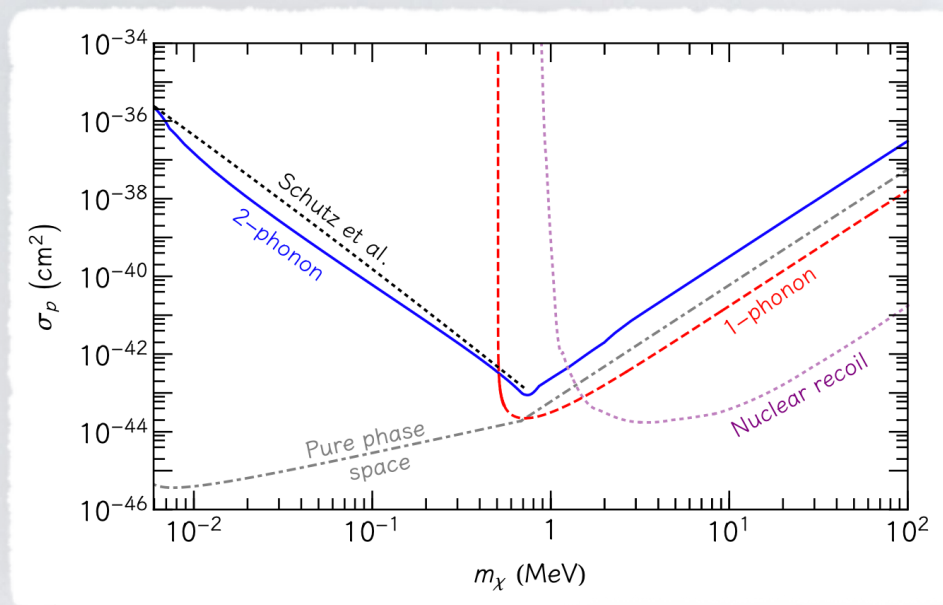
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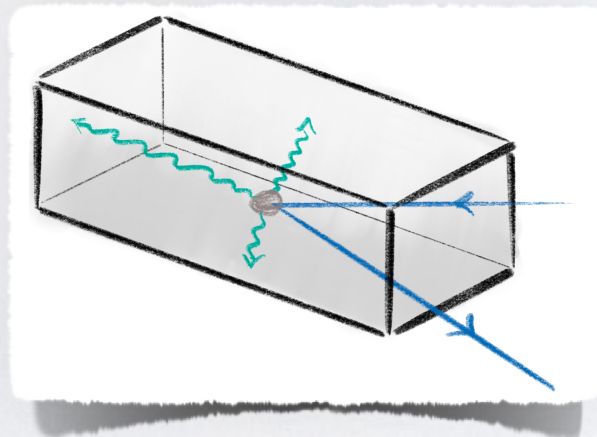
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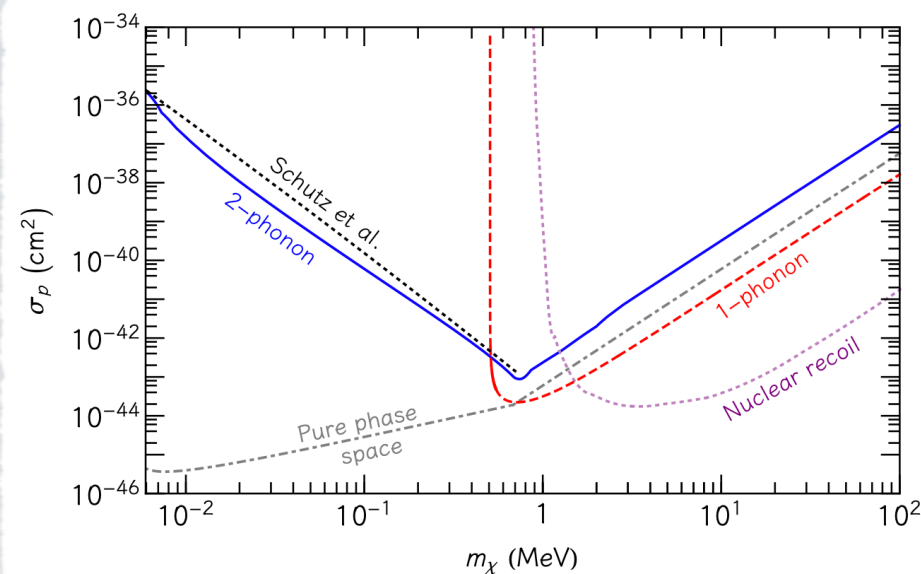


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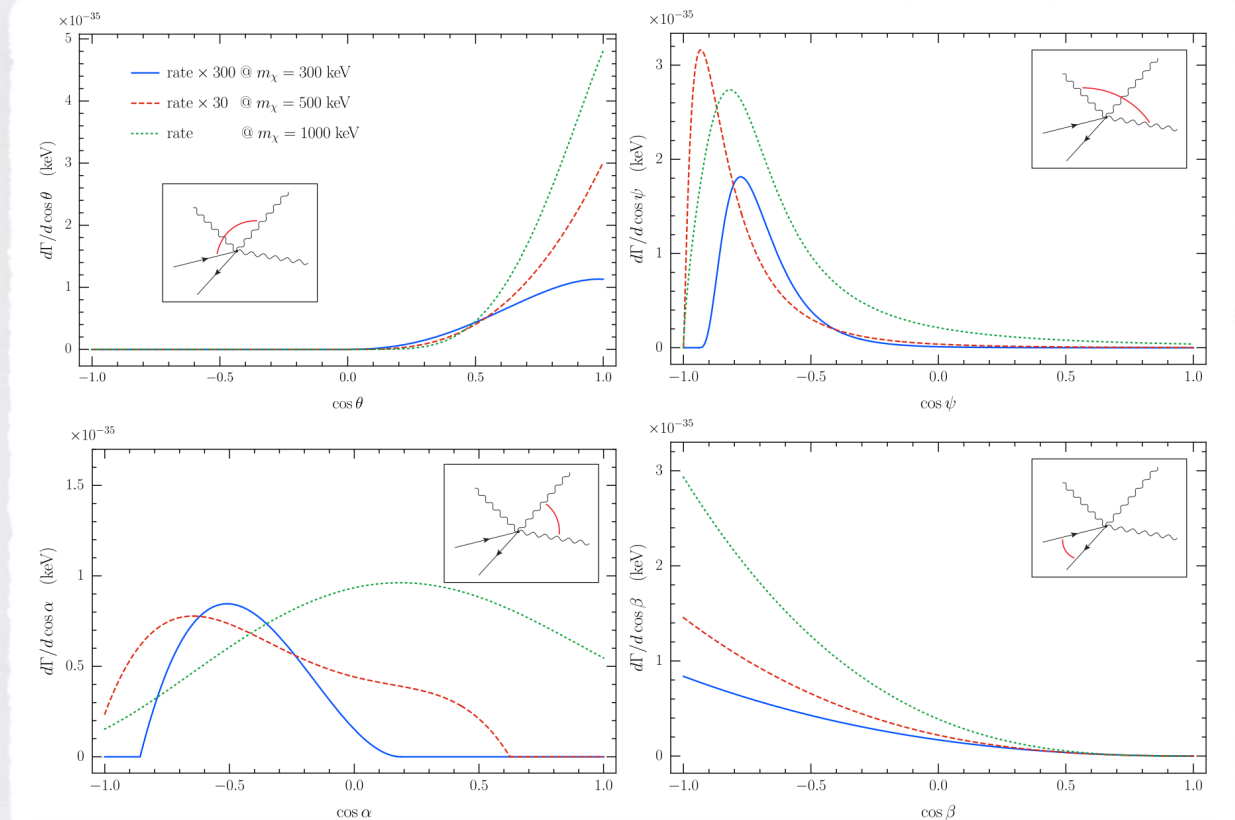
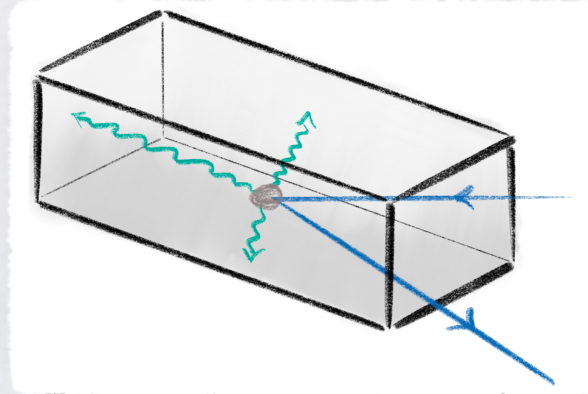
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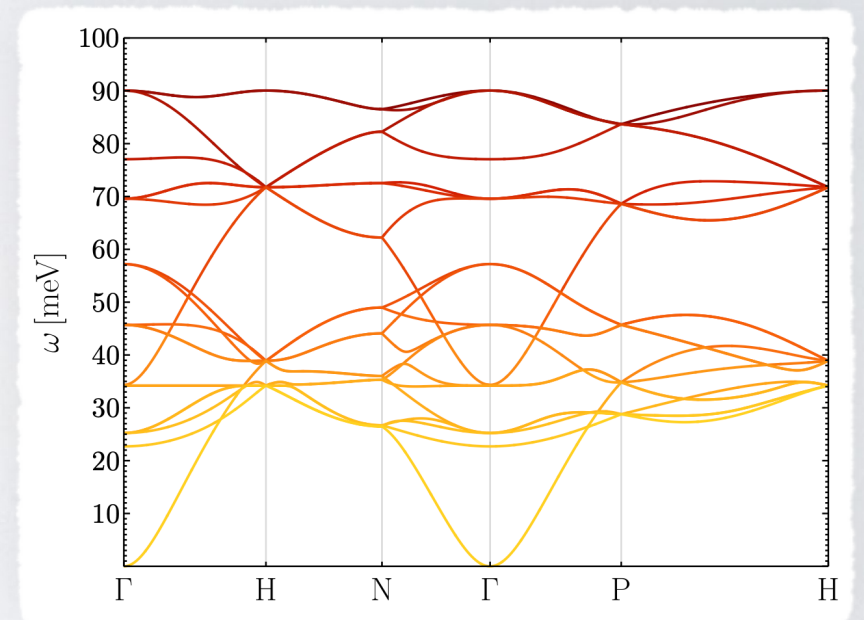
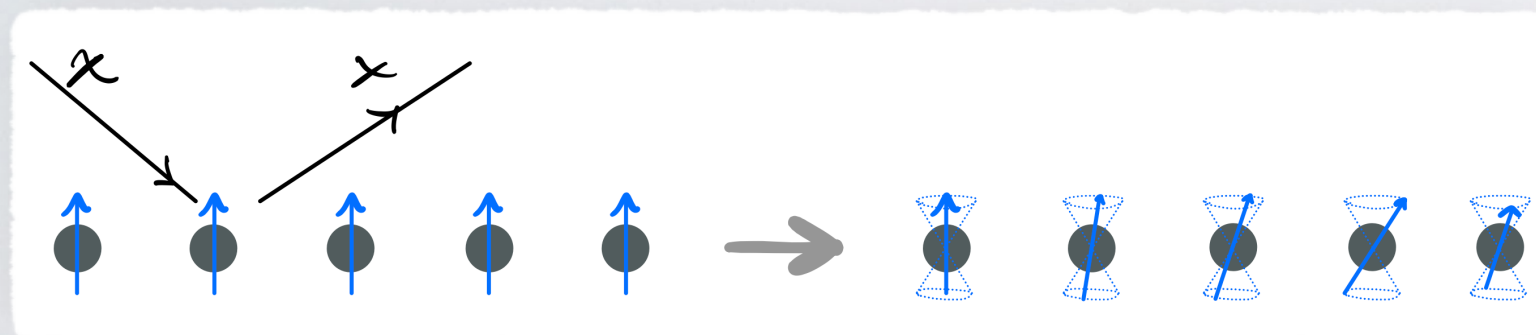
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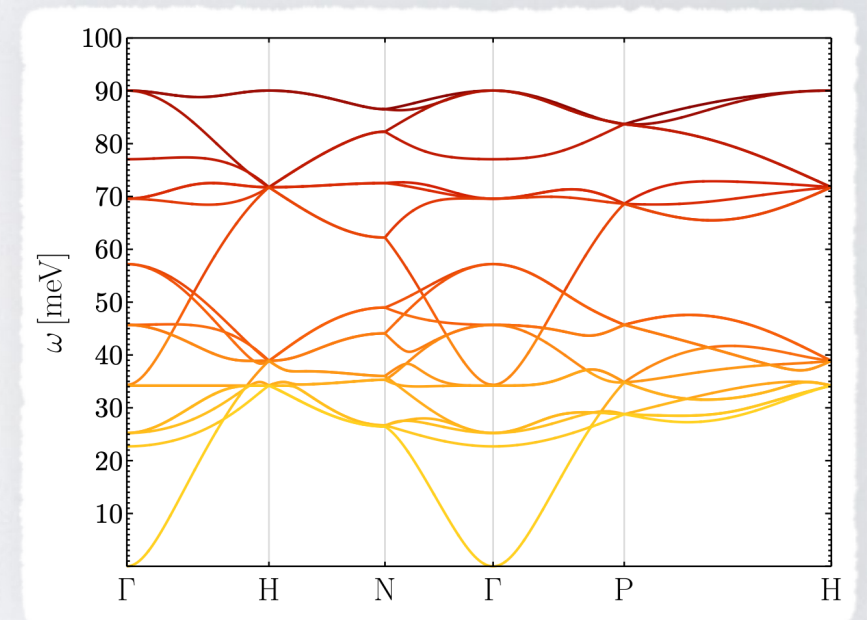
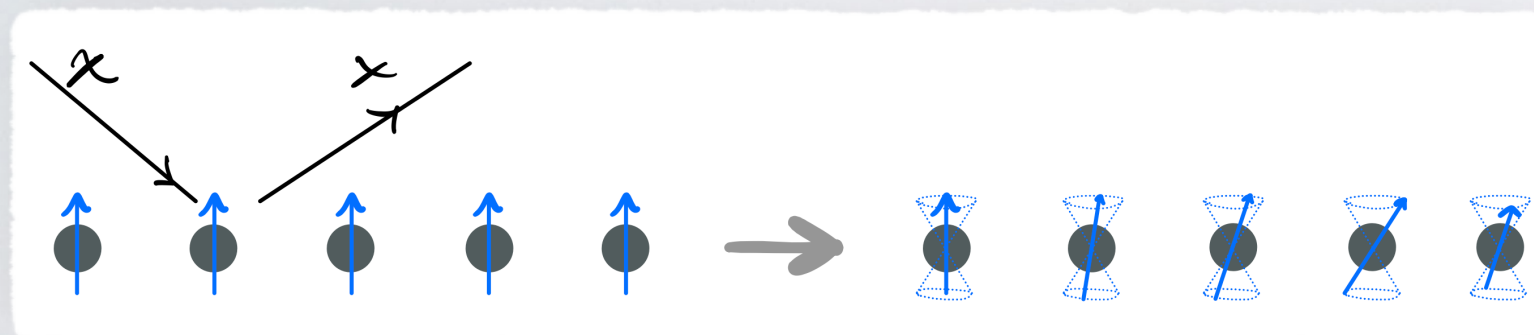
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- Ways to detect few magnons have been proposed and under work (TES, MKID, quantum sensors)

[Trickle, Zhang, Zurek – PRL 2020, 1905.13744; Lachance-Quirion et al. – Science Advances 2017; Lachance-Quirion et al. – Science 2020]

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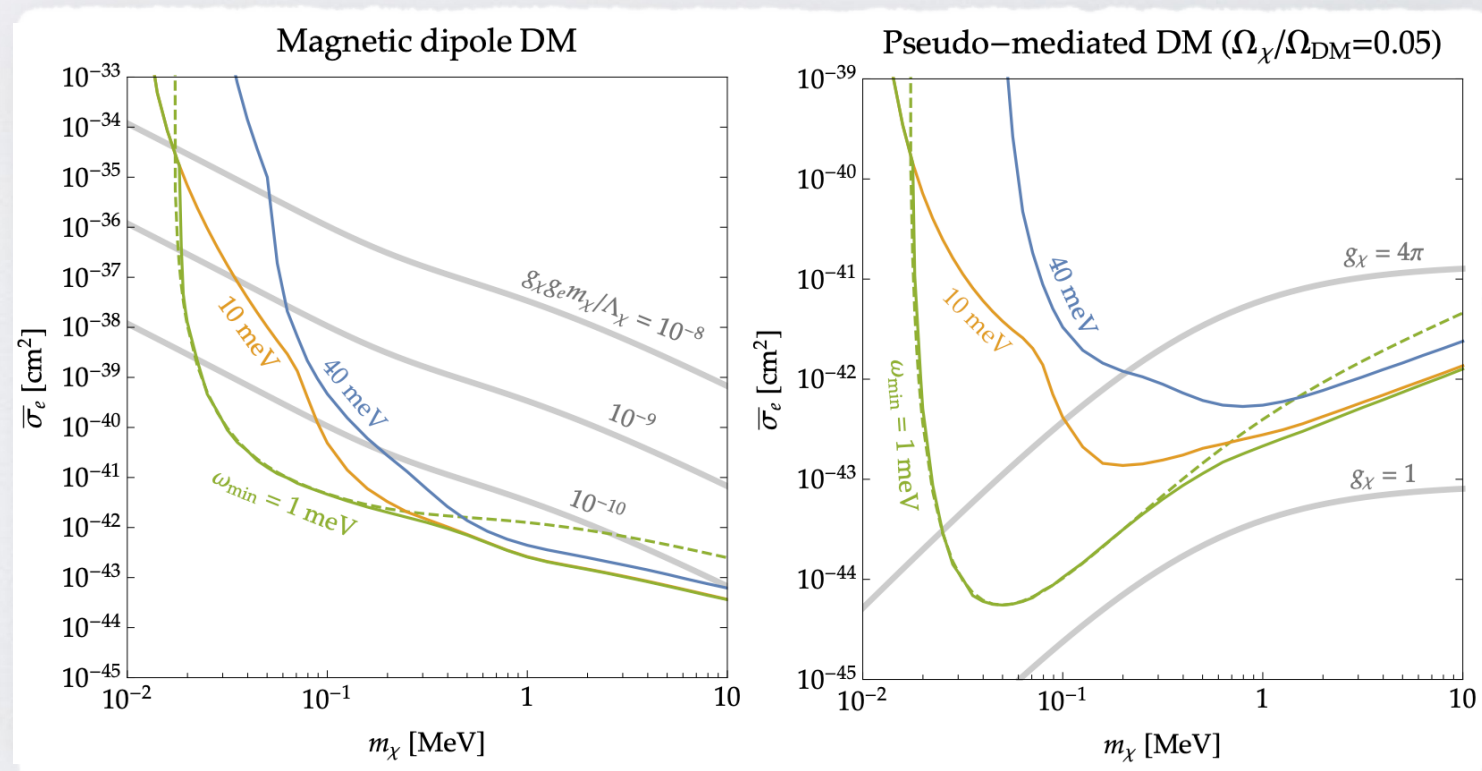
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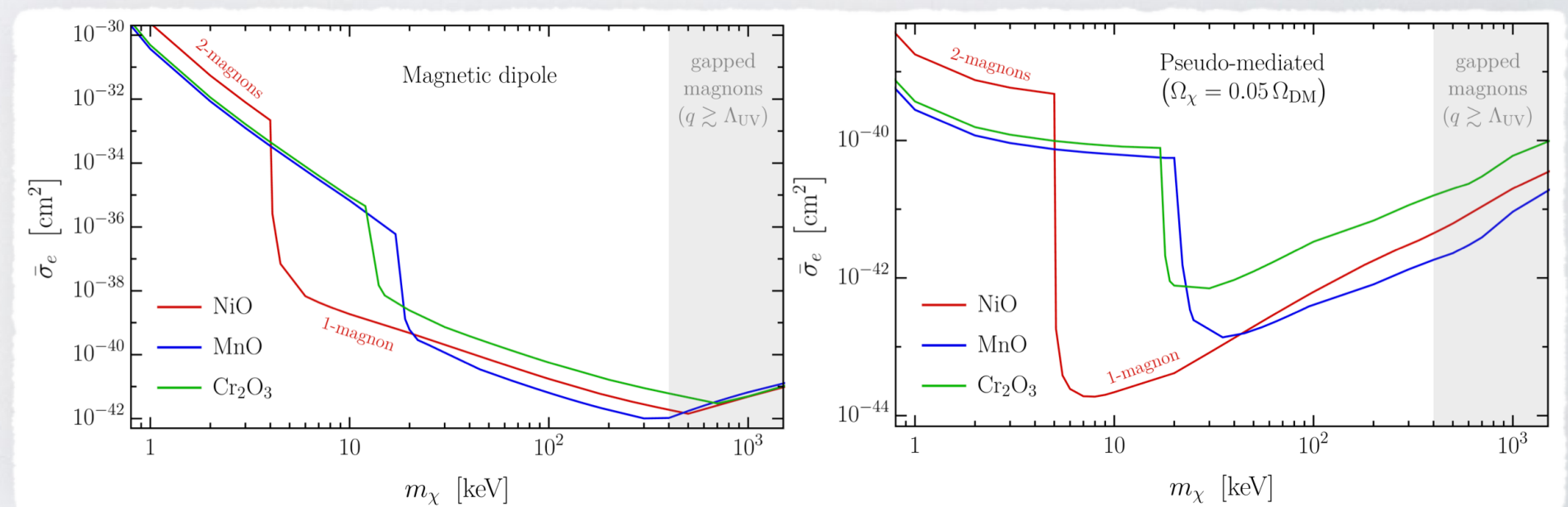
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Thanks for your attention!